

**Low temperature
chemistry using the
R-matrix method**

H^+



$H-H$

Jonathan Tennyson
University College London

Outer region

Inner region

Few Body Systems
Surrey
Sept 2019

The RmatReact Team

Tom Rivlin



Dr Laura McKemmish



EPSRC

Engineering and Physical Sciences
Research Council



Marie Skłodowska-Curie
Actions

The RmatReact Team

Tom Rivlin



Dr Eyrn Spinlove



EPSRC

Engineering and Physical Sciences
Research Council

UK AMOR

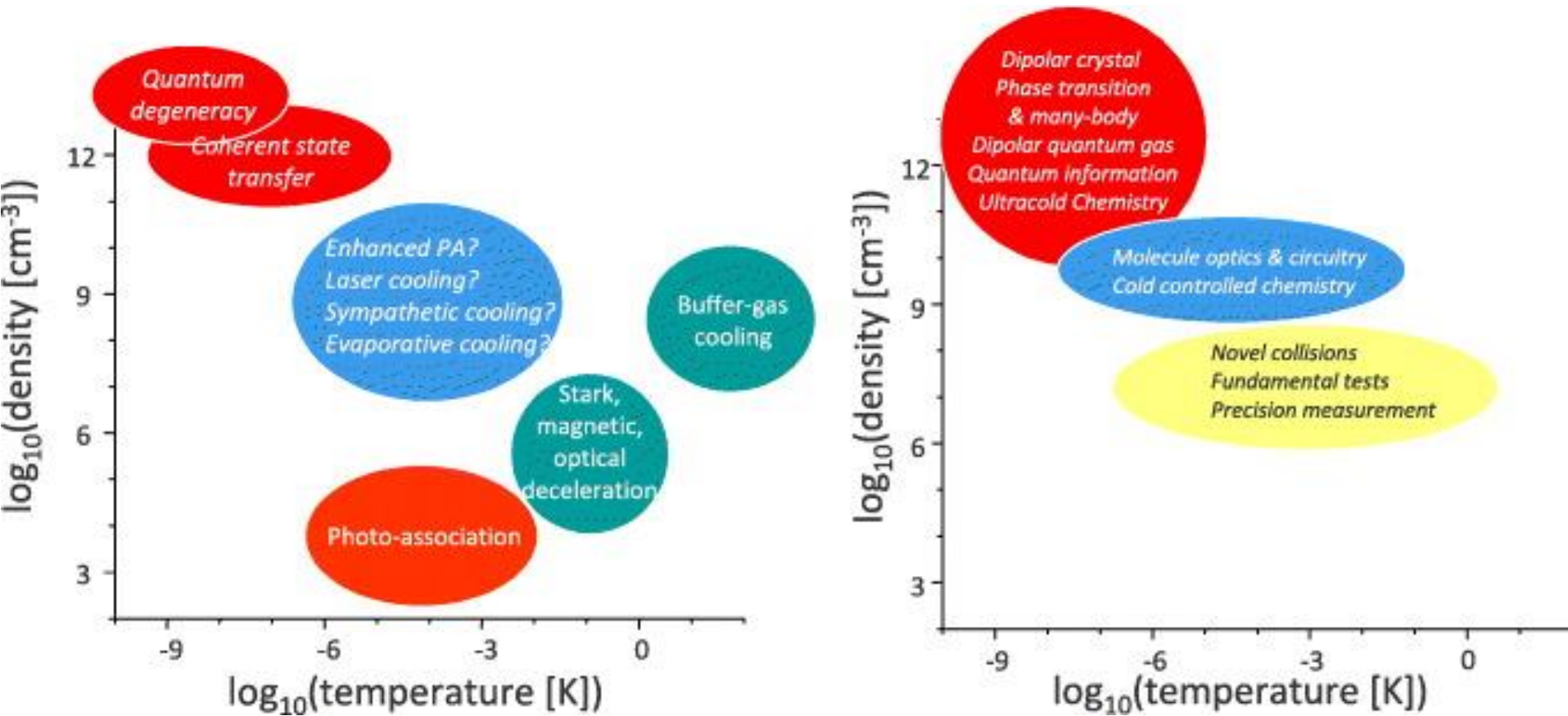


UNSW
SYDNEY

Contents

- 1. Cold Chemistry**
2. Wavefunctions at dissociation
3. R-matrix Theory
4. The RmatReact approach

Cold and ultracold molecules



LD Carr, D DeMille, RV Krems, J Ye, *New. J. Phys.*, 11, 055049 (2009)

Low-energy collision processes

Elastic scattering



Inelastic scattering



Reactive scattering



Charge exchange



Photodissociation



Radiative association



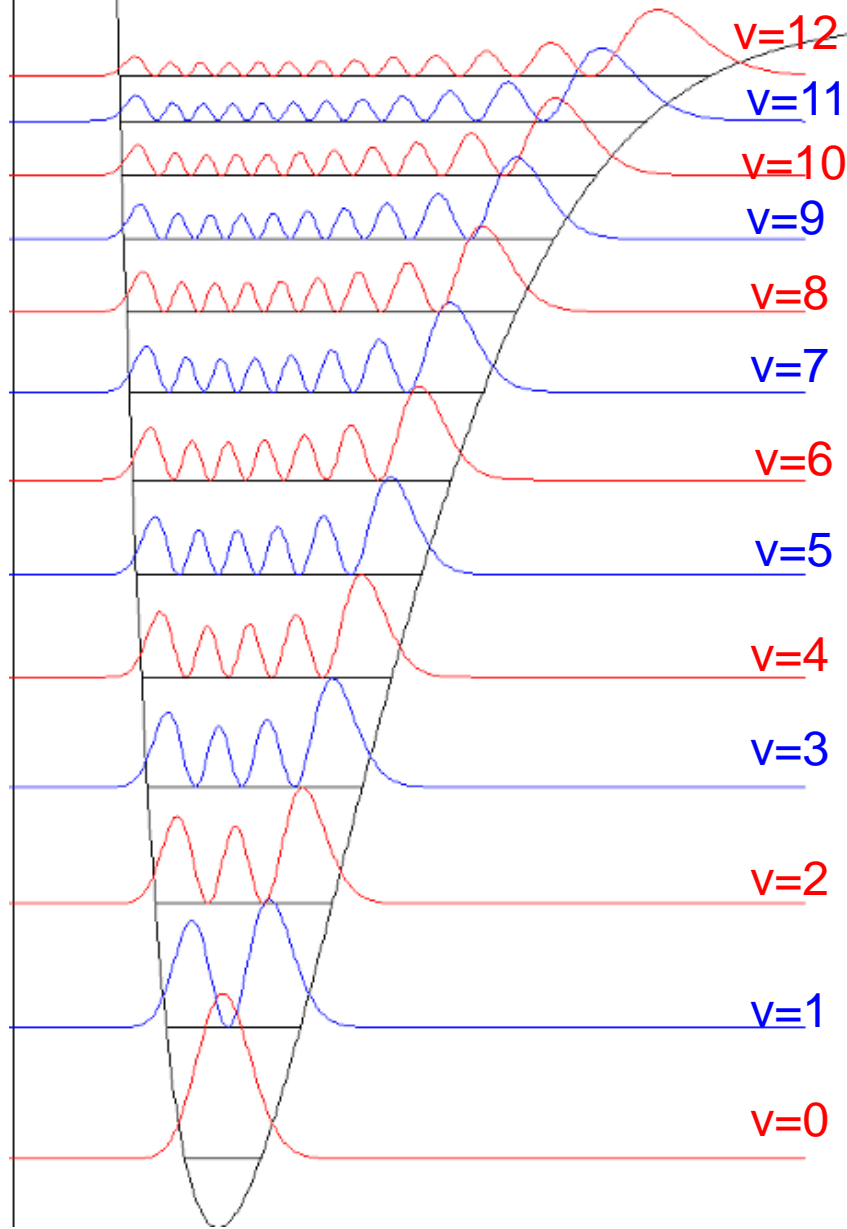
Predissociation

not important for H_2D^+

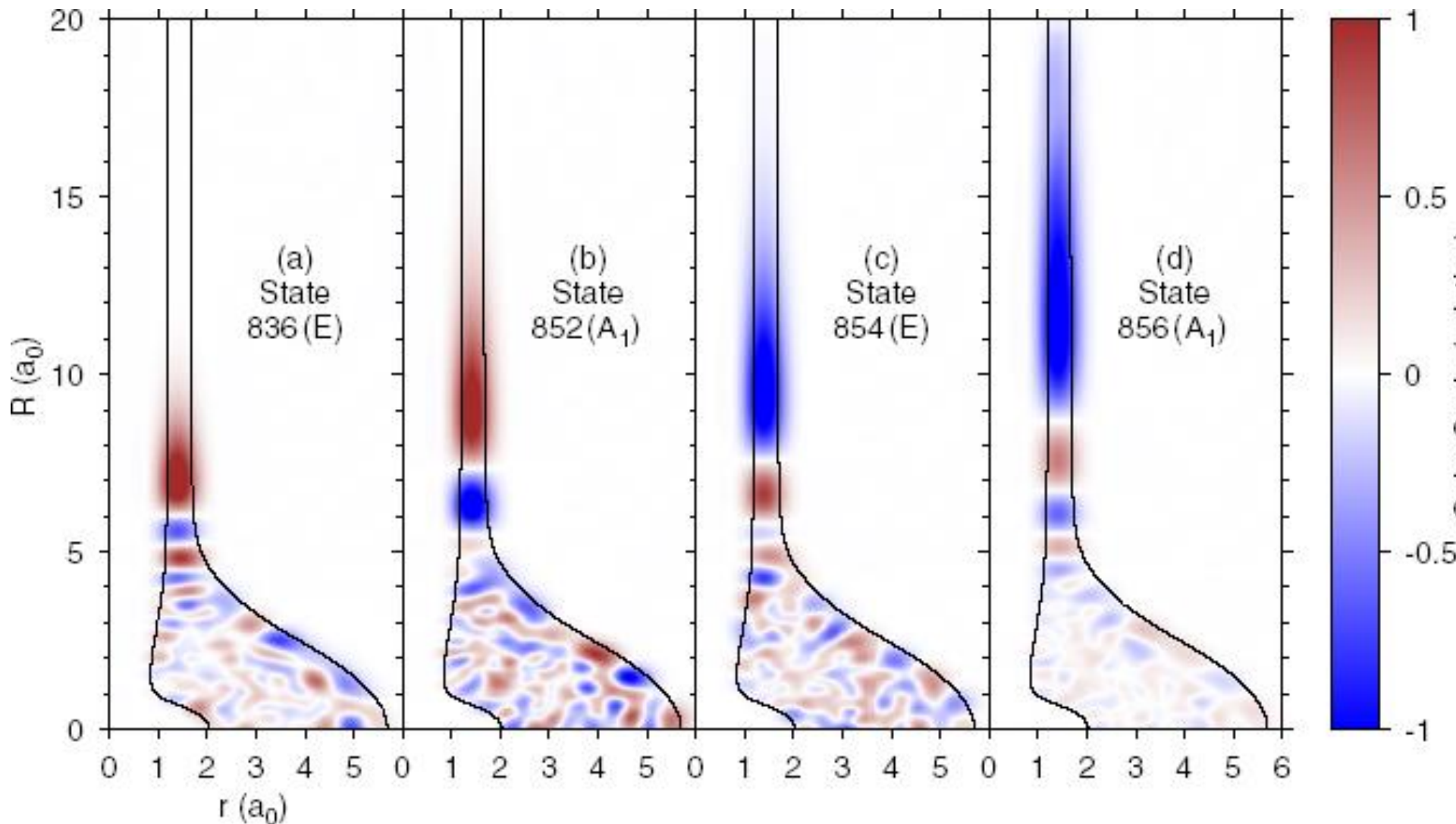
Long-range, weakly-bound states

H_2D^+
as an
example

H₂ vibrational wavefunctions

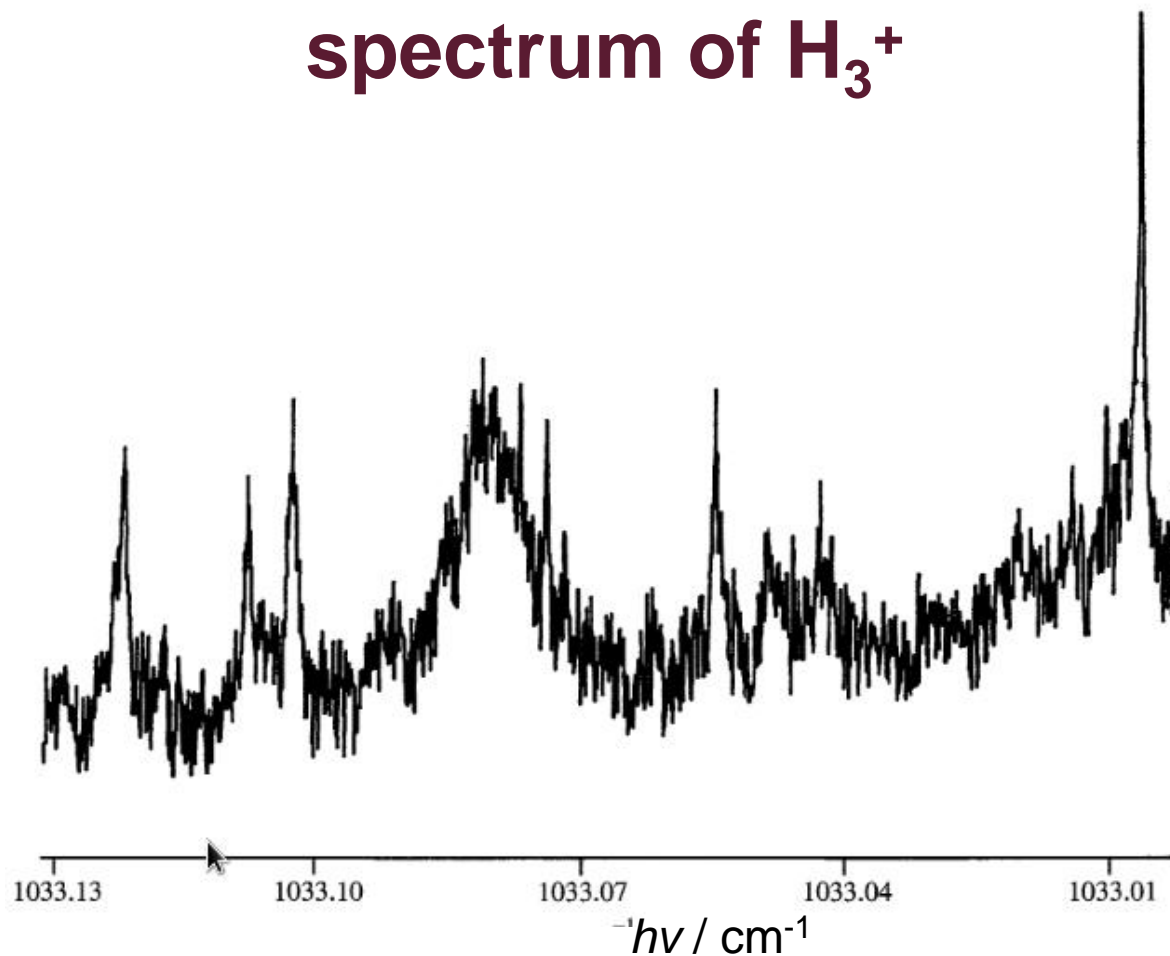


H_3^+ vibrational wavefunctions near dissociation



J.J. Munro, J. Ramanlal & J. Tennyson, *New J. Phys.*, 7, 196 (2005)

Near threshold photodissociation spectrum of H_3^+



F Kemp, CE Kirk & IR McNab *Phil. Trans. R. Soc. Lond. A* 358, 2403 (2000).

Low energy collisions with systems with deep potential wells

Naturally divide into two regions:

Long-range:

- simple s-wave scattering

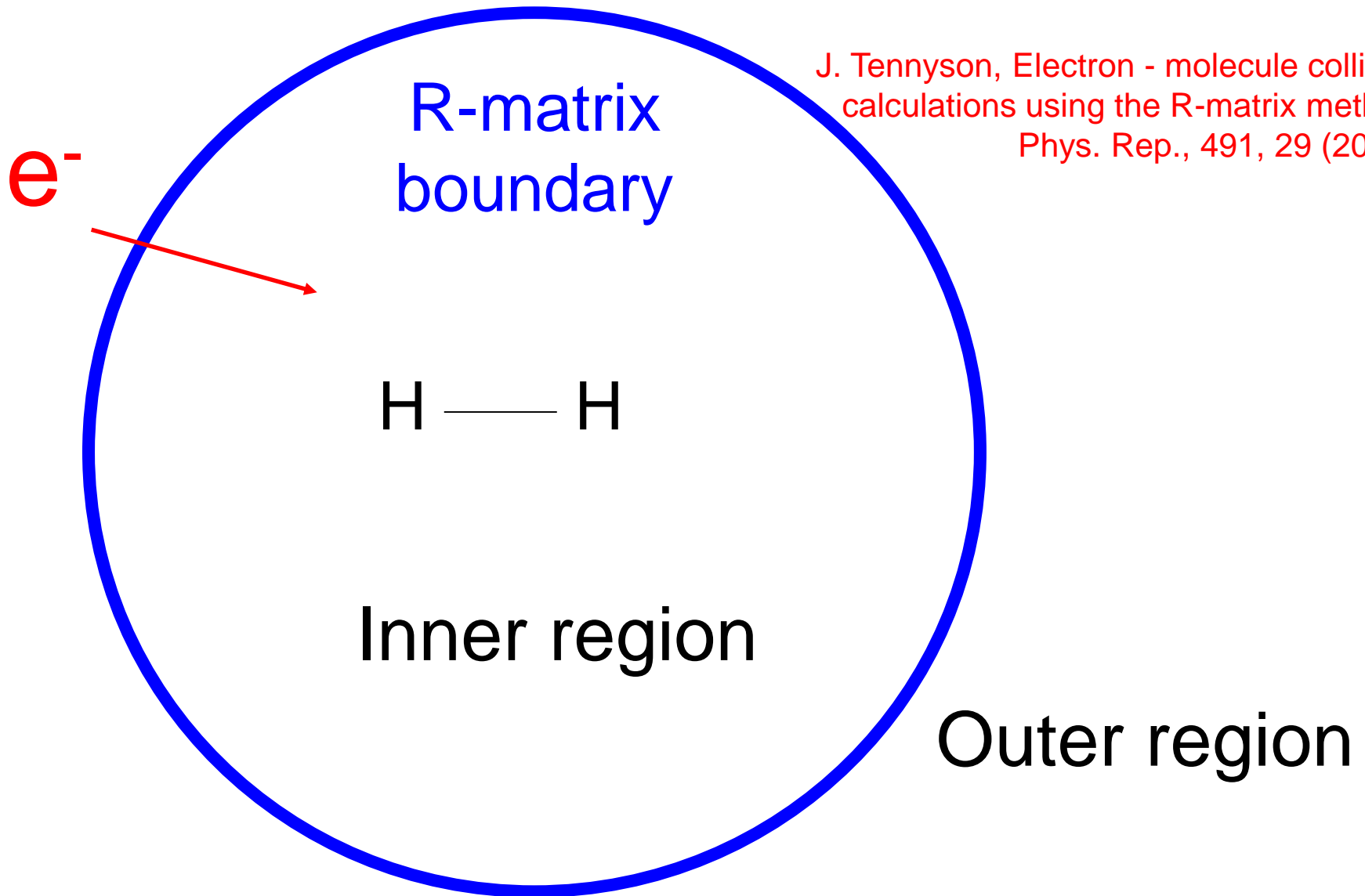
Short-range:

- complicated structures even near threshold
- many resonances

The R-matrix method

PG Burke, R-Matrix Theory of Atomic Collisions Application to Atomic, Molecular and Optical Processes (Springer, 2011)

J. Tennyson, Electron - molecule collision calculations using the R-matrix method, Phys. Rep., 491, 29 (2010).



R-Matrix theory:

1940s Introduced by Wigner & Eisenbud for nuclear physics: **phenomenological**

1960s **Calculable** theory for electron – atom/ion collisions (Burke et al)

1970s **Calculable** electron-molecule collisions (Schneider, Burke and others)
(**Phenomenological** also used by Fabrikant, Meyer, etc)

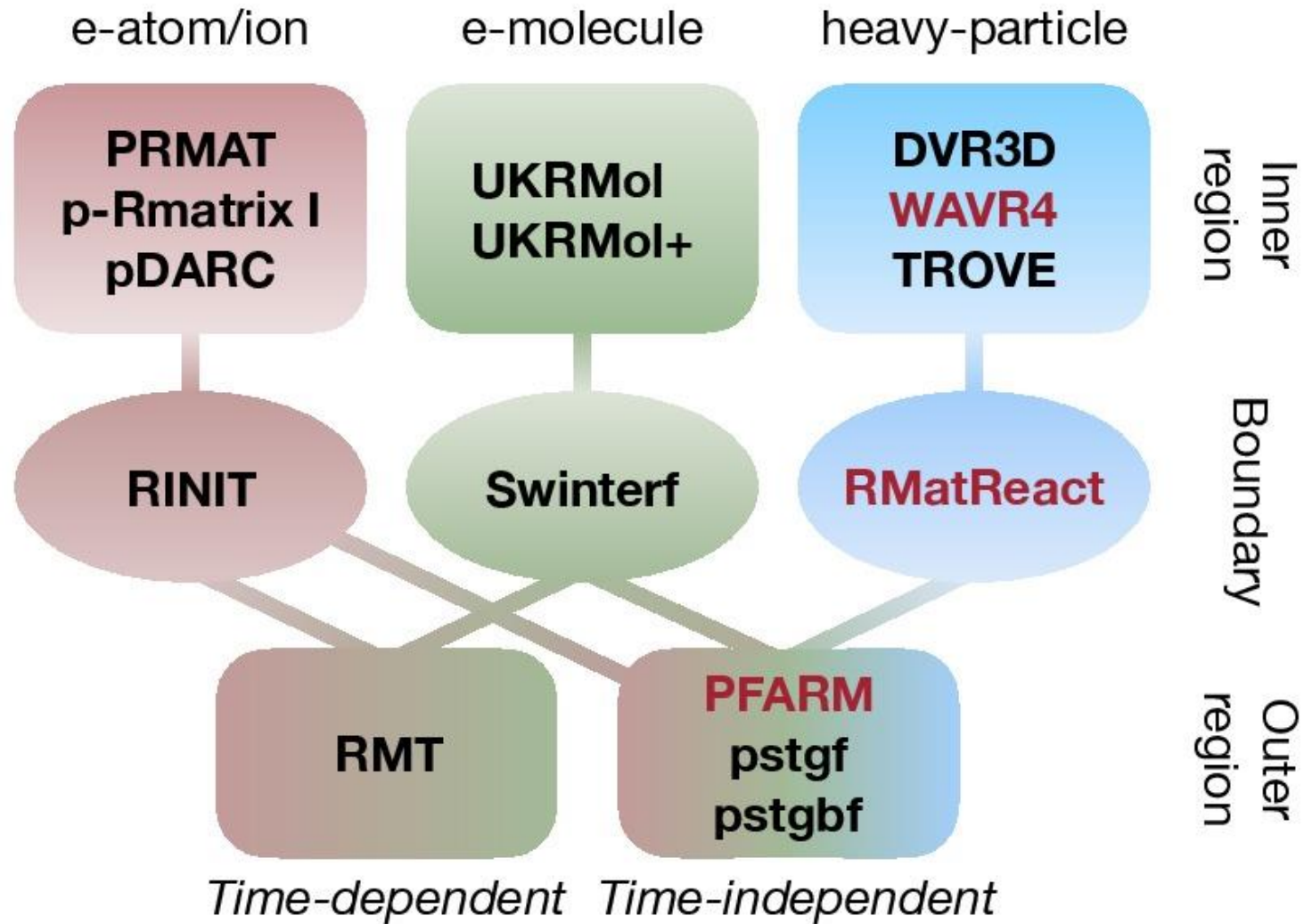
1980s Light-Walker **propagator** for reactive scattering

Present: **Calculable** R-matrix is method of choice for electron collision calculations
also time-dependent (fast laser studies)
used in nuclear physics and elsewhere



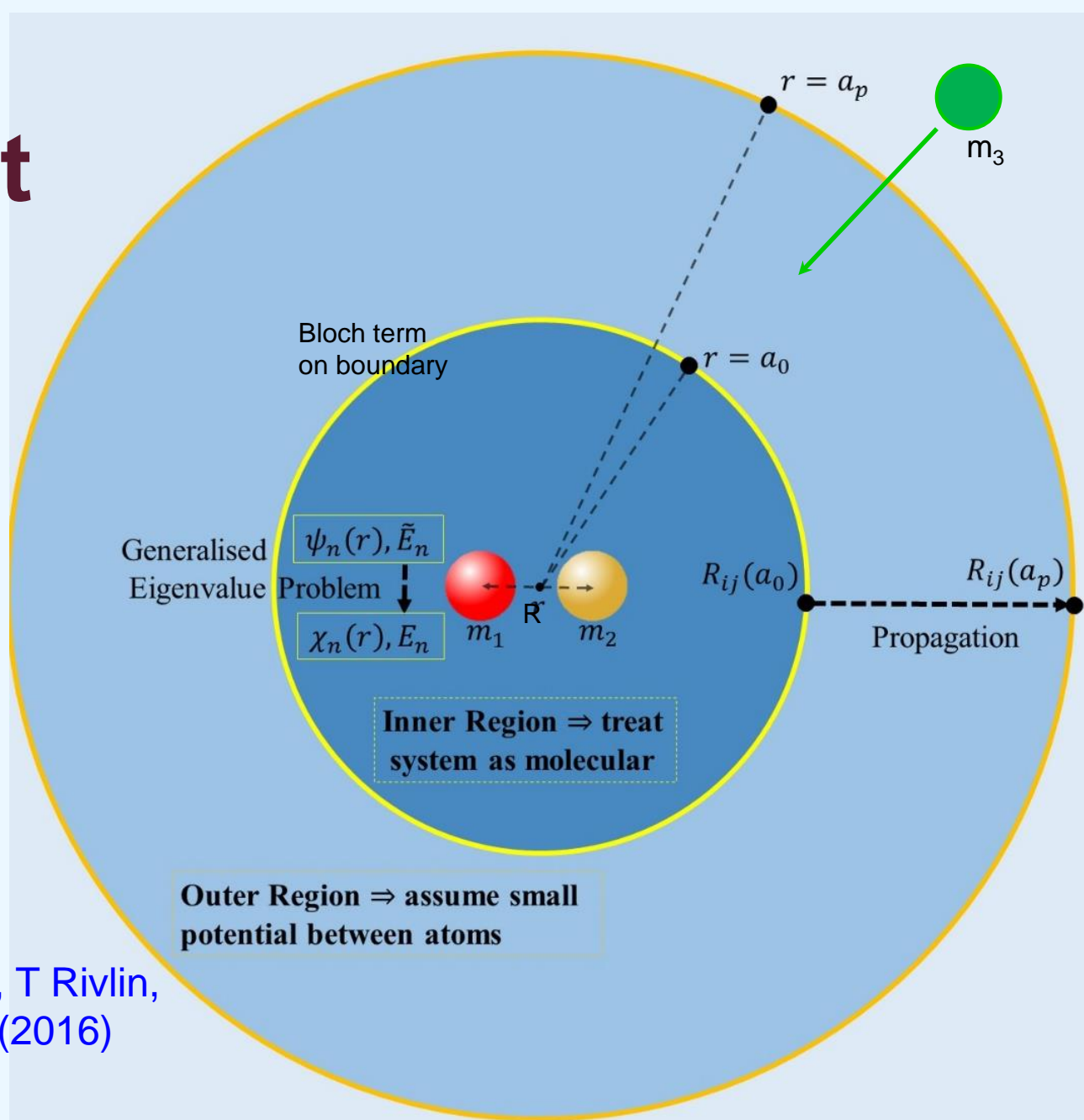
CCPQ

UK Atomic Molecular R-matrix code base



RmatReact

treatment
of reactive
scattering



J Tennyson, LK McKemmish, T Rivlin,
Faraday Discussion **195**, 31 (2016)

What is an R-matrix?

Relates (asymptotic) radial wavefunction to its derivative

$$\mathbf{R}(r, E) = \frac{\mathbf{F}(r)}{\mathbf{F}'(r)}$$

where $F_i(r)$ is the asymptotic radial wavefunction associated with channel i .

Each channel is associated with an asymptotic state

Eg in $\text{H}^+ + \text{H}_2$,

i represents (v, J) states of H_2 .

$$R_{i,j}(r, E) = \frac{F_i(r)}{F'_j(r)}$$

On the R-matrix boundary, $r=a$

$$R_{i,j}(E) = \frac{1}{2a} \sum_k \frac{\omega_{k,i}\omega_{k,j}}{E - E_k}$$

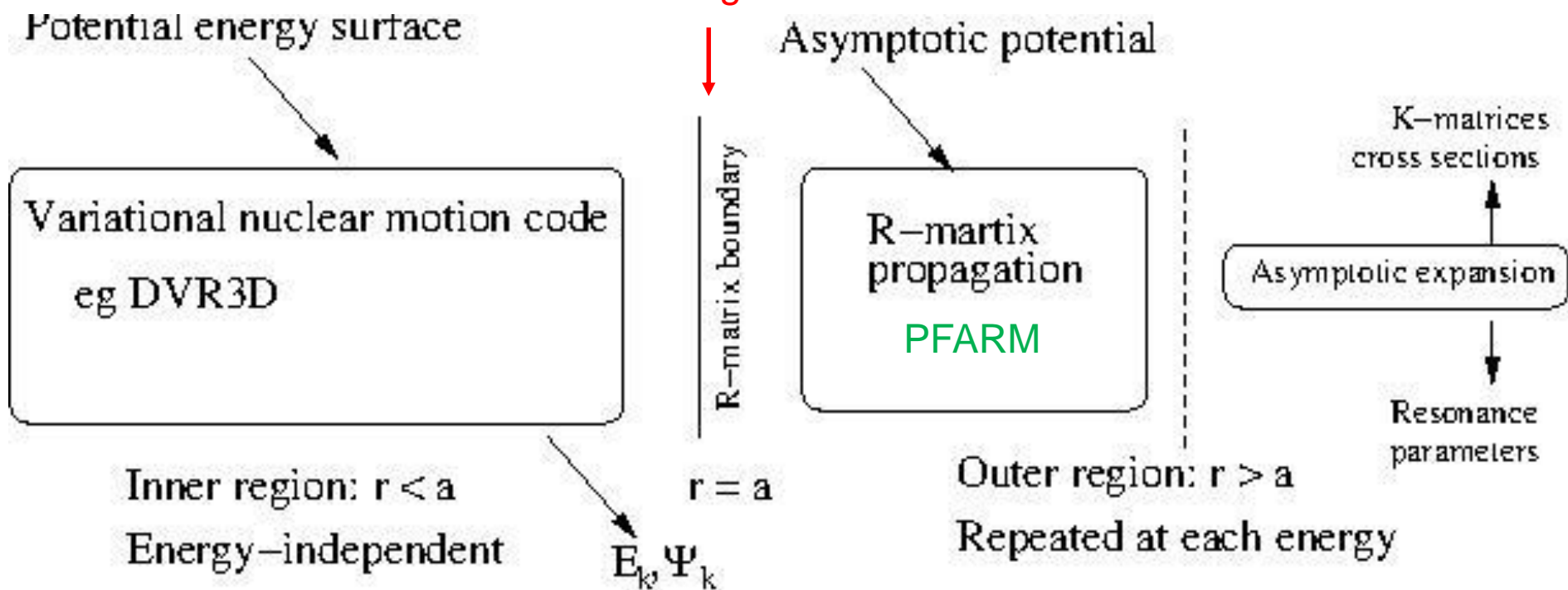
where E_k is the energy of the k^{th} inner region solution and $w_{i,k}$ is the amplitude of this solution in channel i

In the inner region

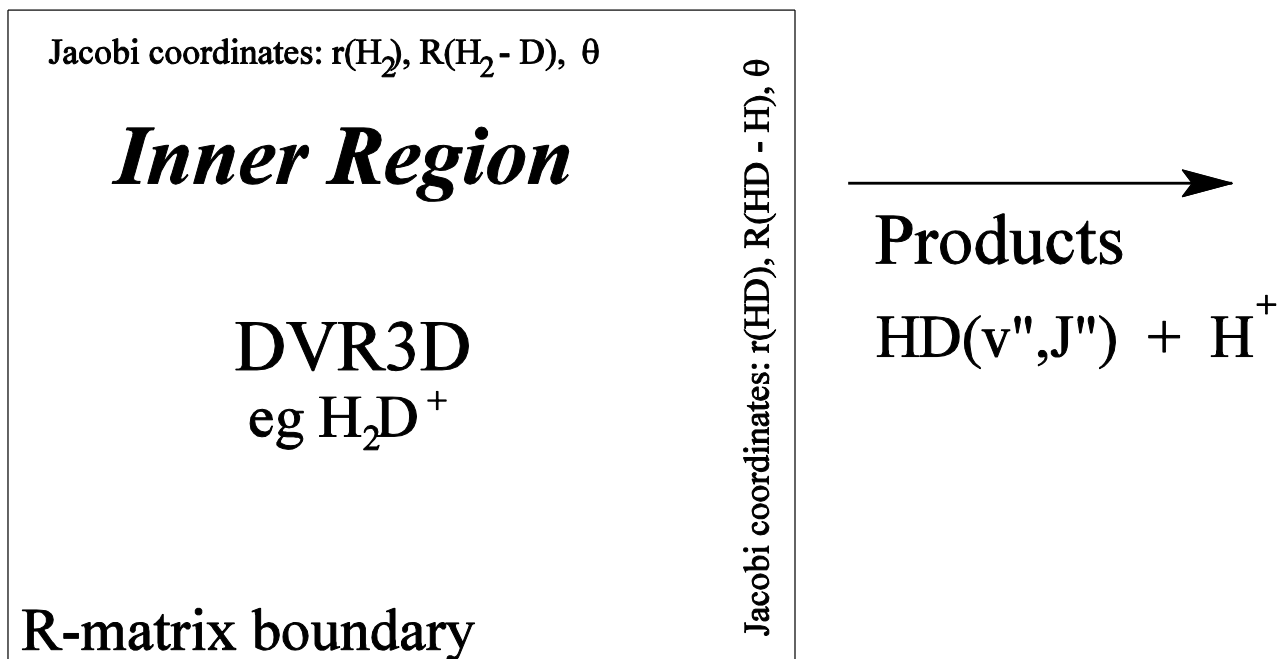
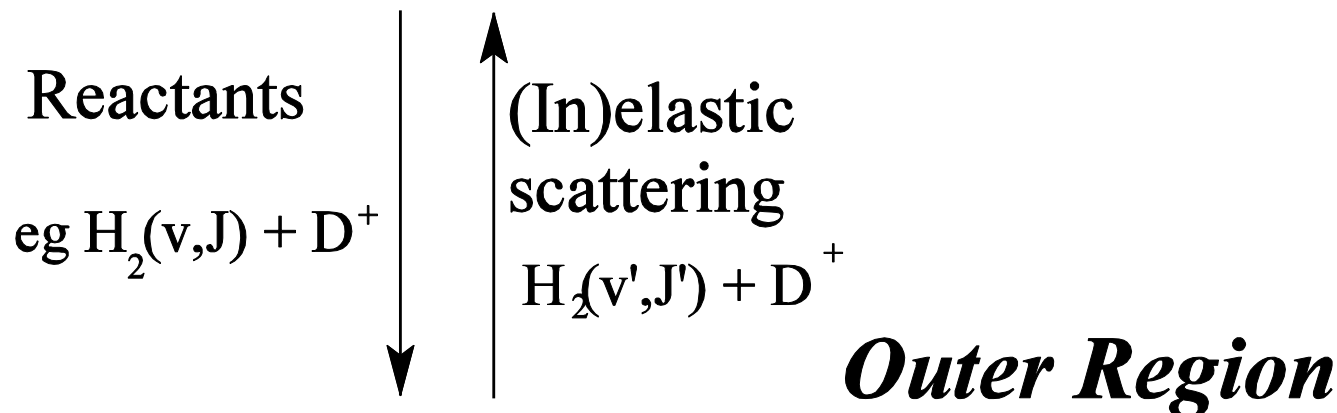
- Continuum wavefunctions are discretised
- Solutions do not depend on scattering energy

RmatReact summary

Flexible RmatReact harness
for inner region codes



Frame transformation (on the boundary):
Hyperfine coupling
Spin-orbit coupling
Magnetic fields



L.K. McKemmish and J. Tennyson,

General Mathematical Formulation of Reactive Atom-Diatomic Collisions in RmatReact Methodology
Phil. Trans. Royal Soc. London A, **377**, 20180409 (2019).

Inner region: variational nuclear motion programs

- Duo: vibronic spectra of diatomics **implementation complete**
- DVR3D: triatomics (exact kinetic energy) **partial implementation**
- WAVR4: tetratomics (exact kinetic energy) **to be done**
- TROVE: polyatomic (approx. kinetic energy) **to be done**

New general diatomic code Duo

Computer Physics Communications 202 (2016) 262–275

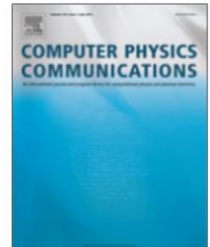


ELSEVIER

Contents lists available at [ScienceDirect](#)

Computer Physics Communications

journal homepage: www.elsevier.com/locate/cpc



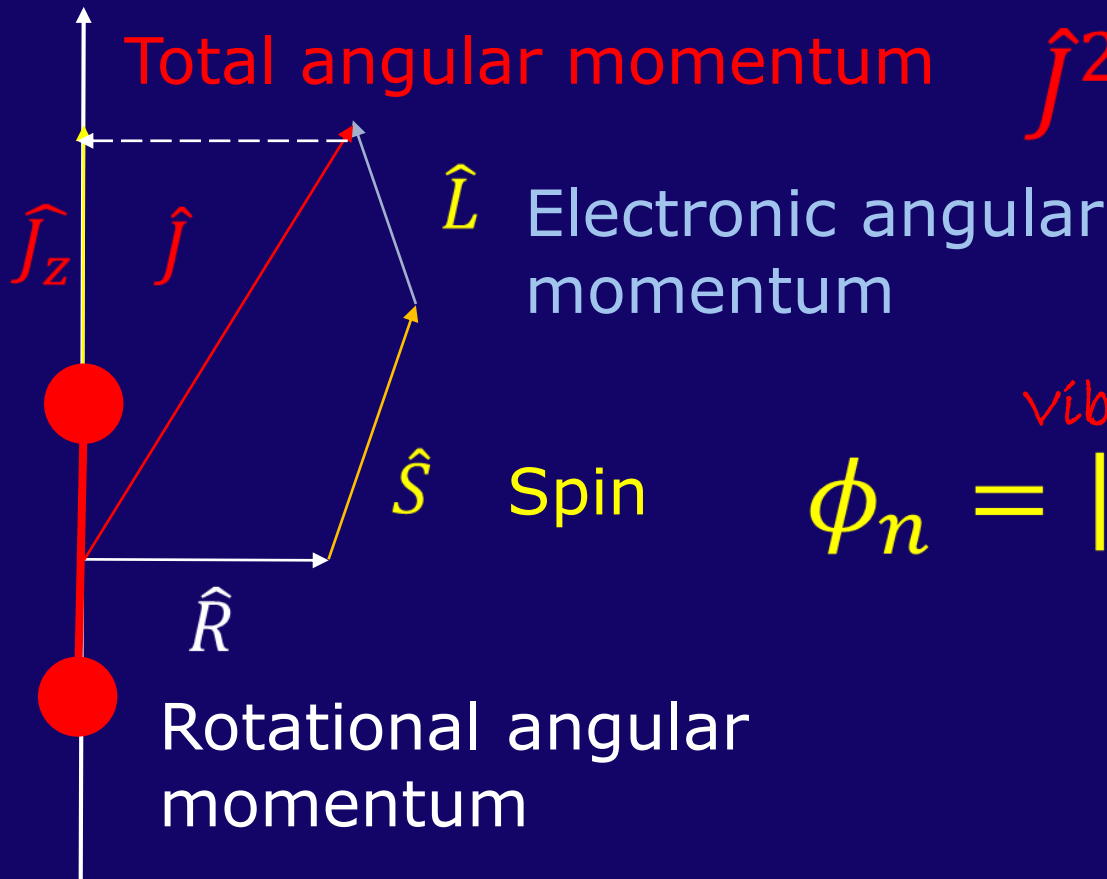
Duo: A general program for calculating spectra
of diatomic molecules[☆]

Sergei N. Yurchenko^{a,*}, Lorenzo Lodi^a, Jonathan Tennyson^a, Andrey V. Stoliarov^b

^a Department of Physics & Astronomy, University College London, Gower Street, London WC1E 6BT, United Kingdom



Hund's case (a)



$$\hat{J}^2 = \hat{L}^2 + \hat{S}^2 + \hat{R}^2$$

$$\phi_n = |v\rangle |J\Omega\rangle |S\Sigma\rangle |L\Sigma\rangle$$

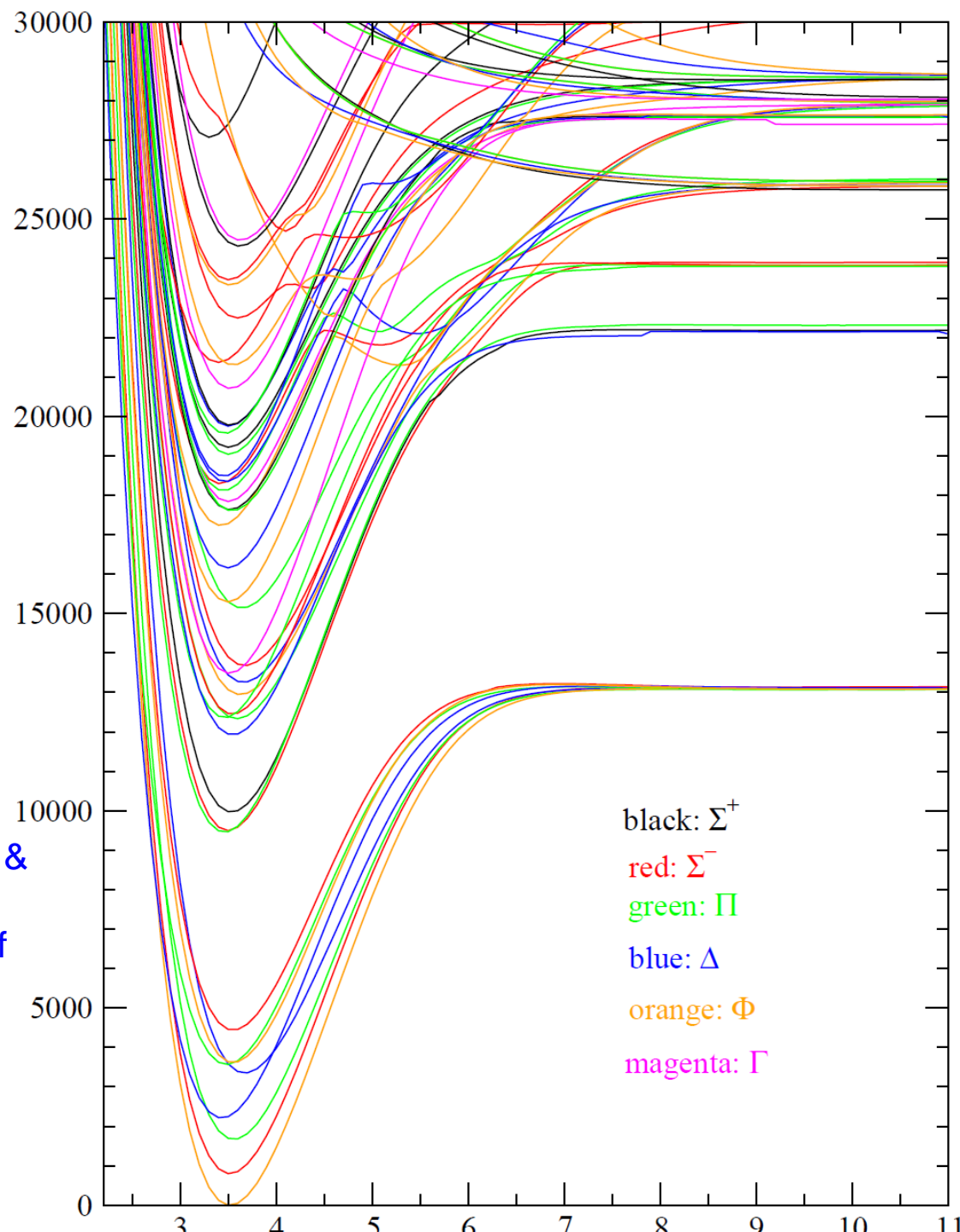
vibrational
Spin

Rotational
Electronic

Rotational angular momentum

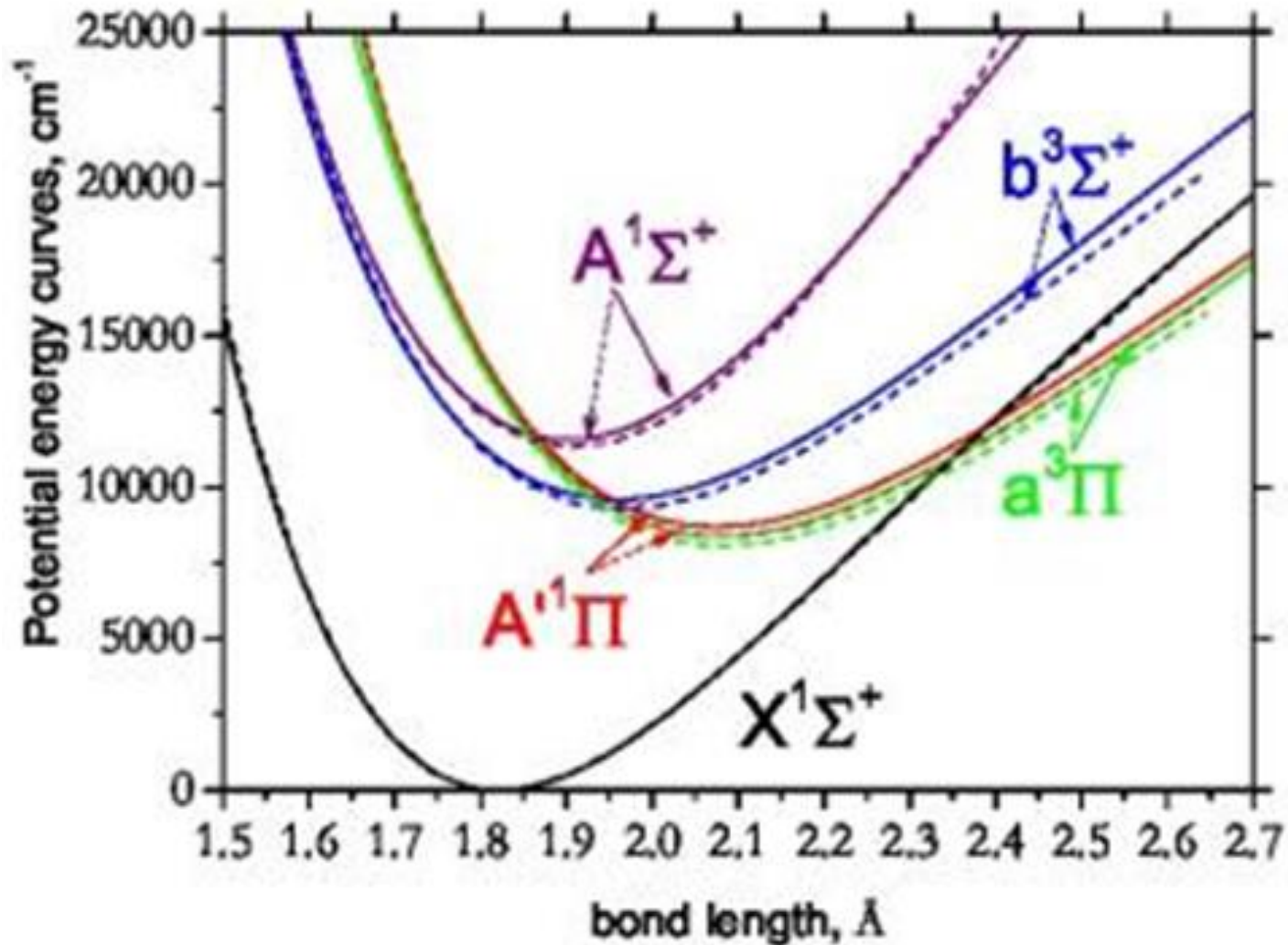
TiH

Lorenzo Lodi

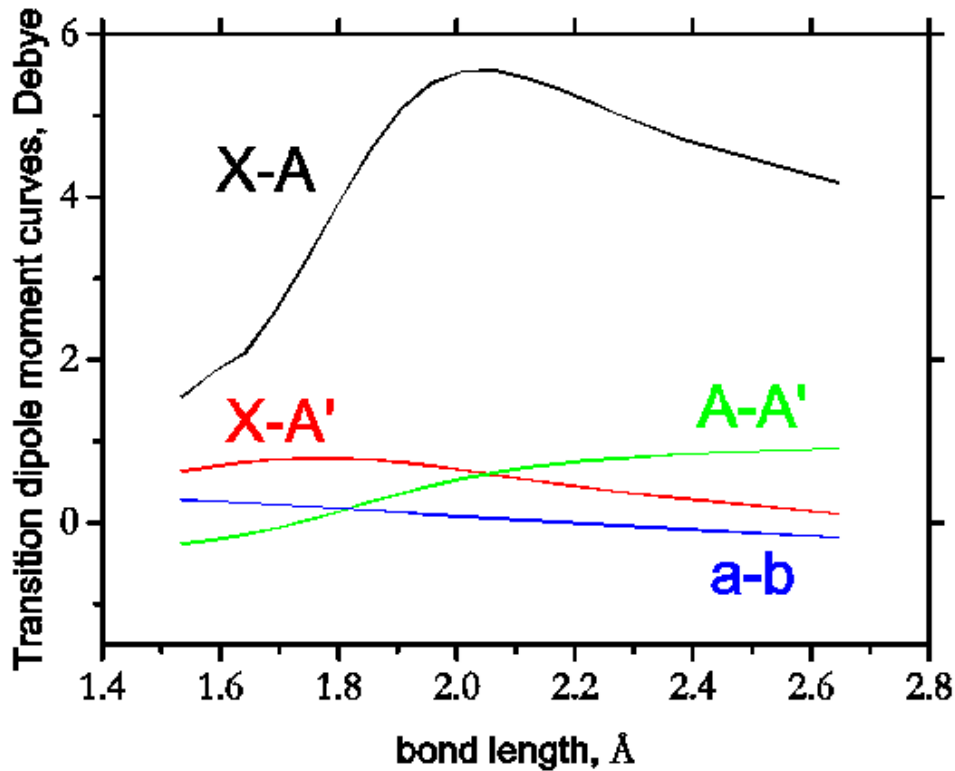


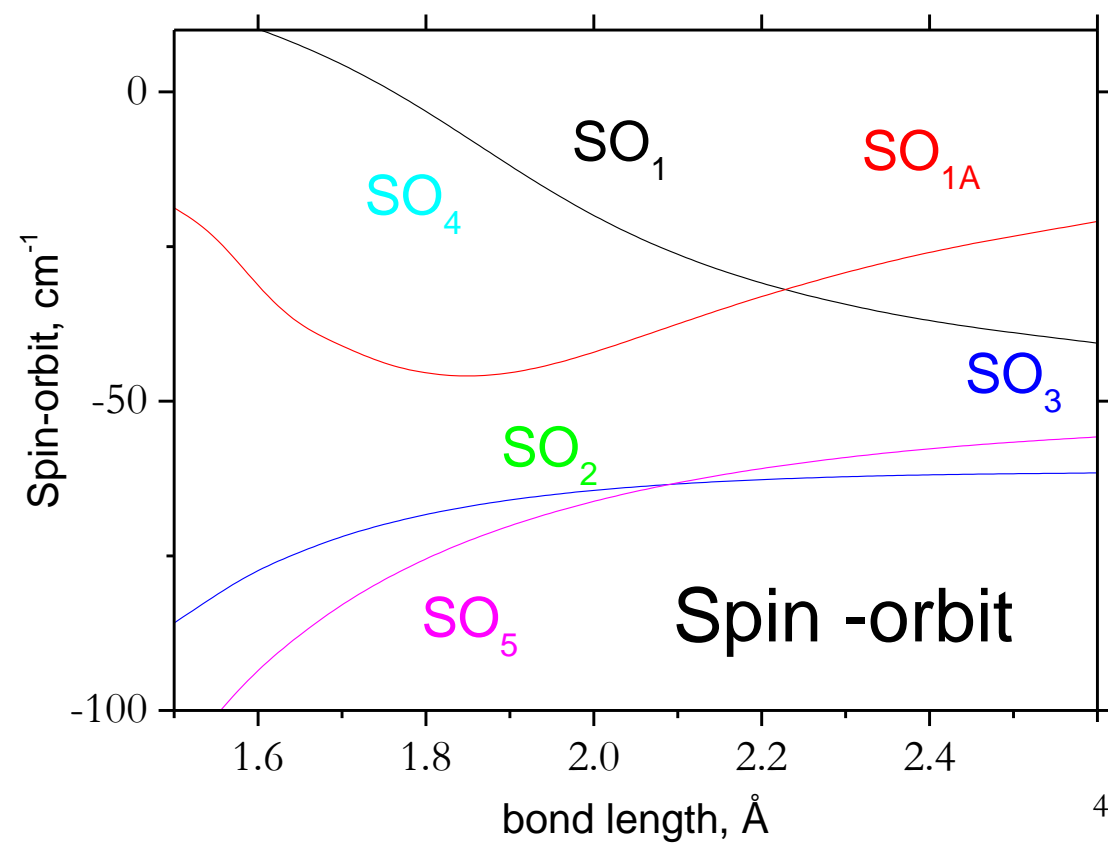
J Tennyson, L Lodi, LK McKemmish & SN Yurchenko,
The ab initio calculation of spectra of
open shell diatomic molecules,
J. Phys. B, 49, 102001 (2016)
(Topical Review)

CaO: potential energy curves



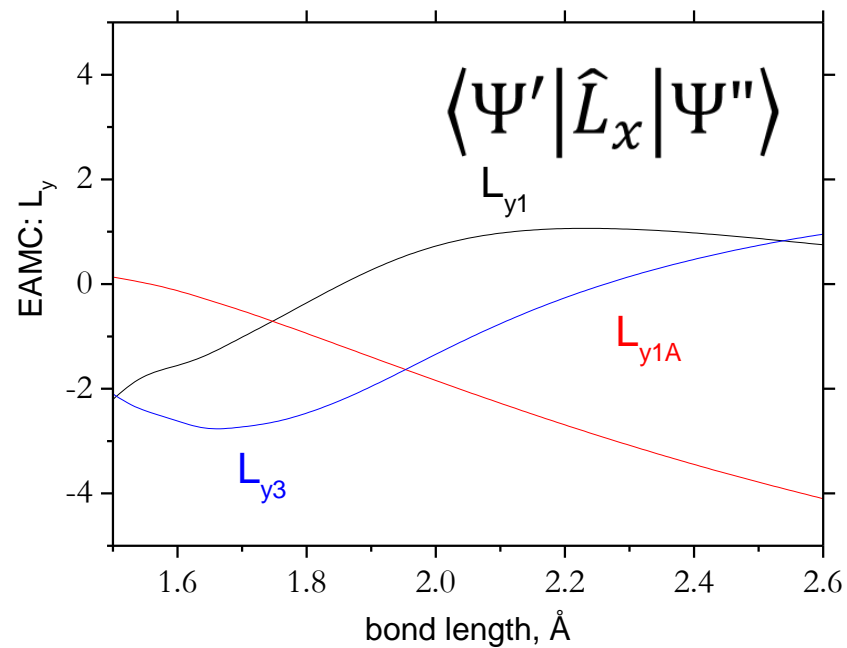
CaO: transition dipole moment curves



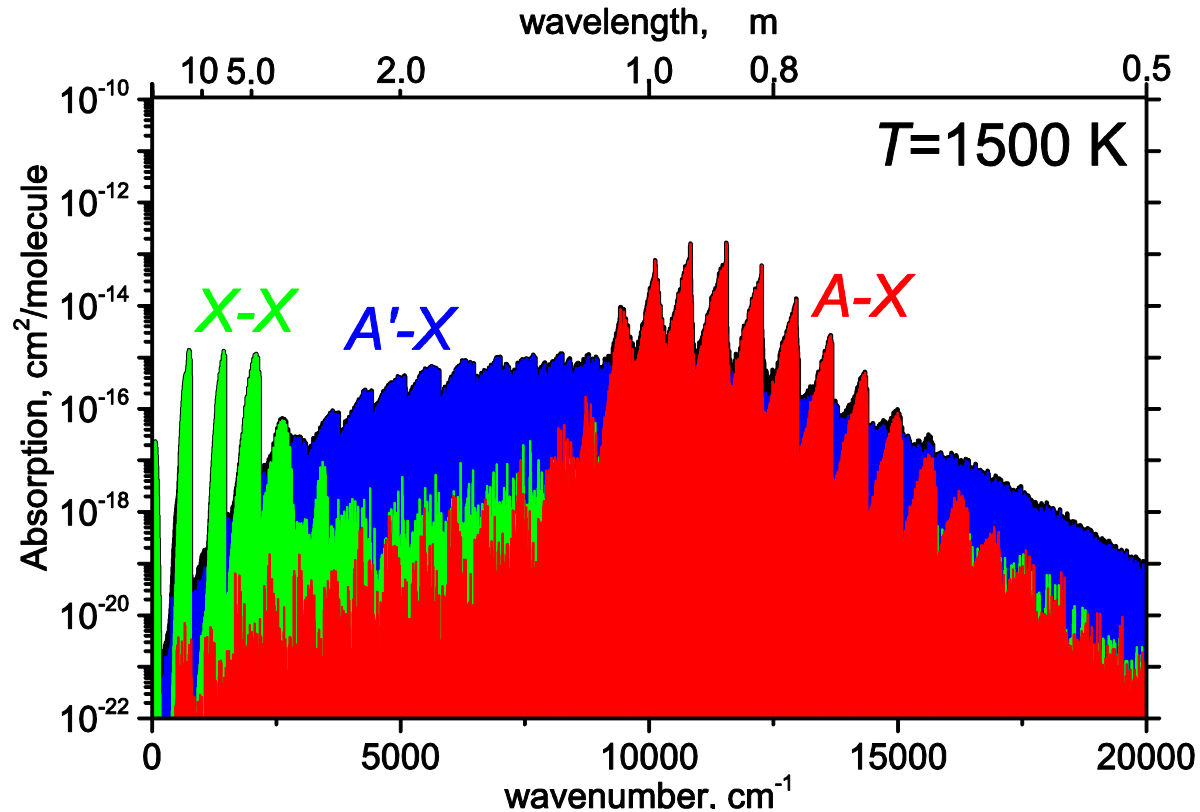
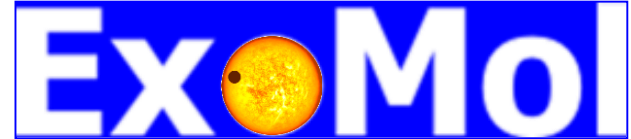


CaO

Curve-couplings



CaO: line list



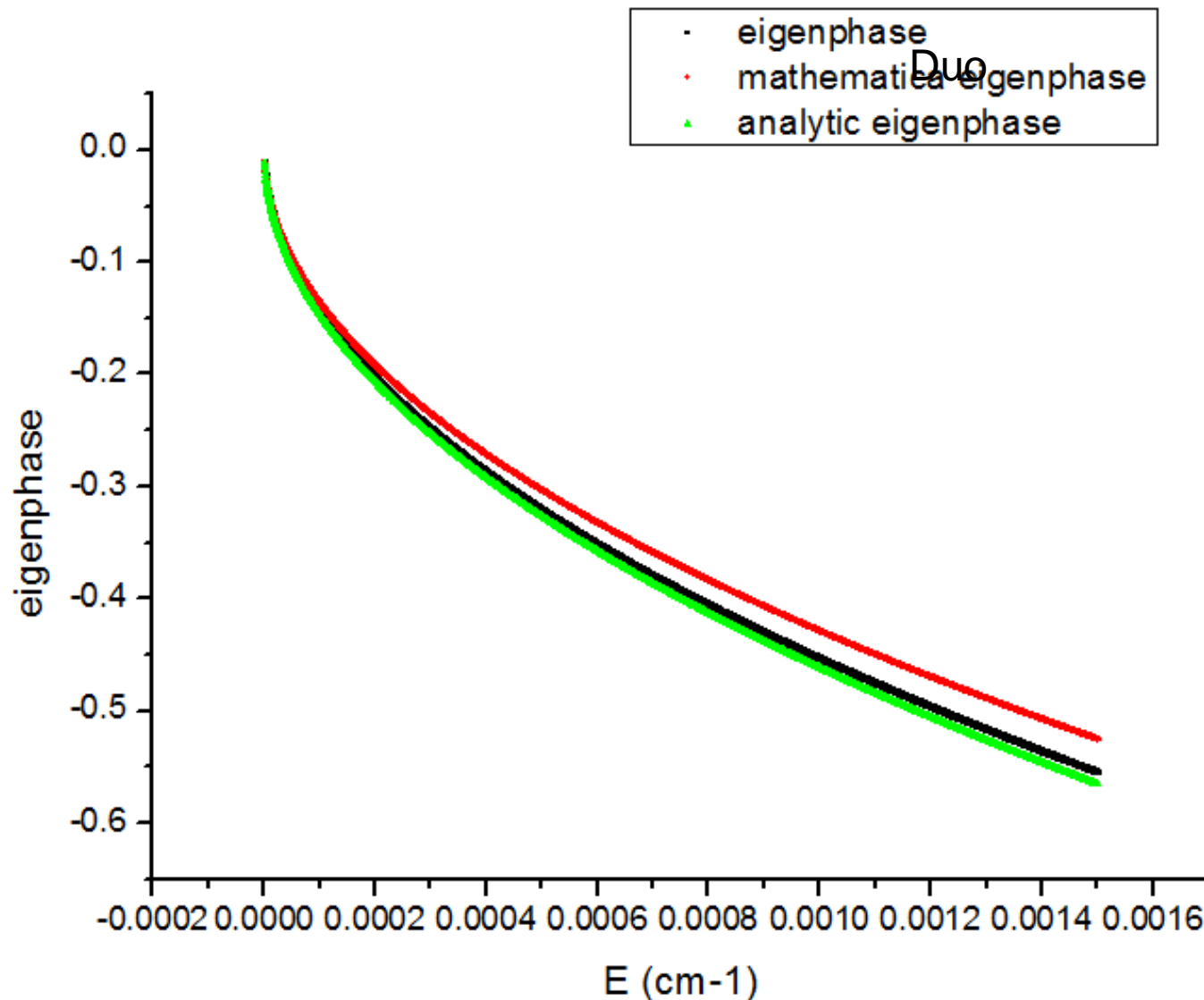
Line list: 22 M lines

S.N. Yurchenko, A. Blissett, U. Asari, M. Vasilios, C. Hill & J. Tennyson,
Mon. Not. R. astr. Soc., 456, 4524 (2016)

Duo implementation:

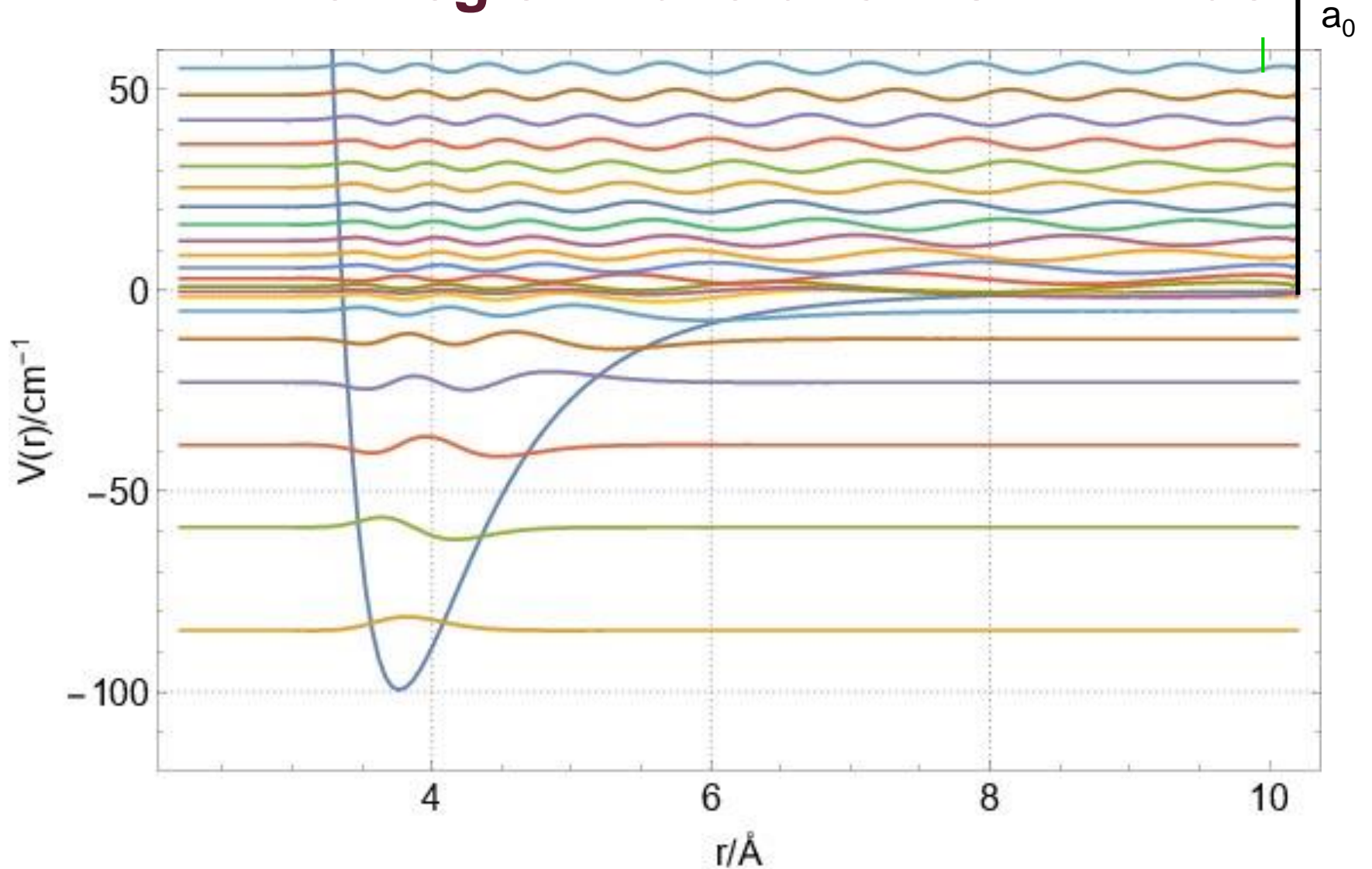
- Bloch term to allow for finite boundary
- Lobatto Shape function DVR used
- Initial tests on Ar – Ar (elastic scattering)
- Study of He – O(3P_j) (inelastic scattering)
- Code available on gitlab (via www.exomol.com)

Eigenphases for the Morse potential



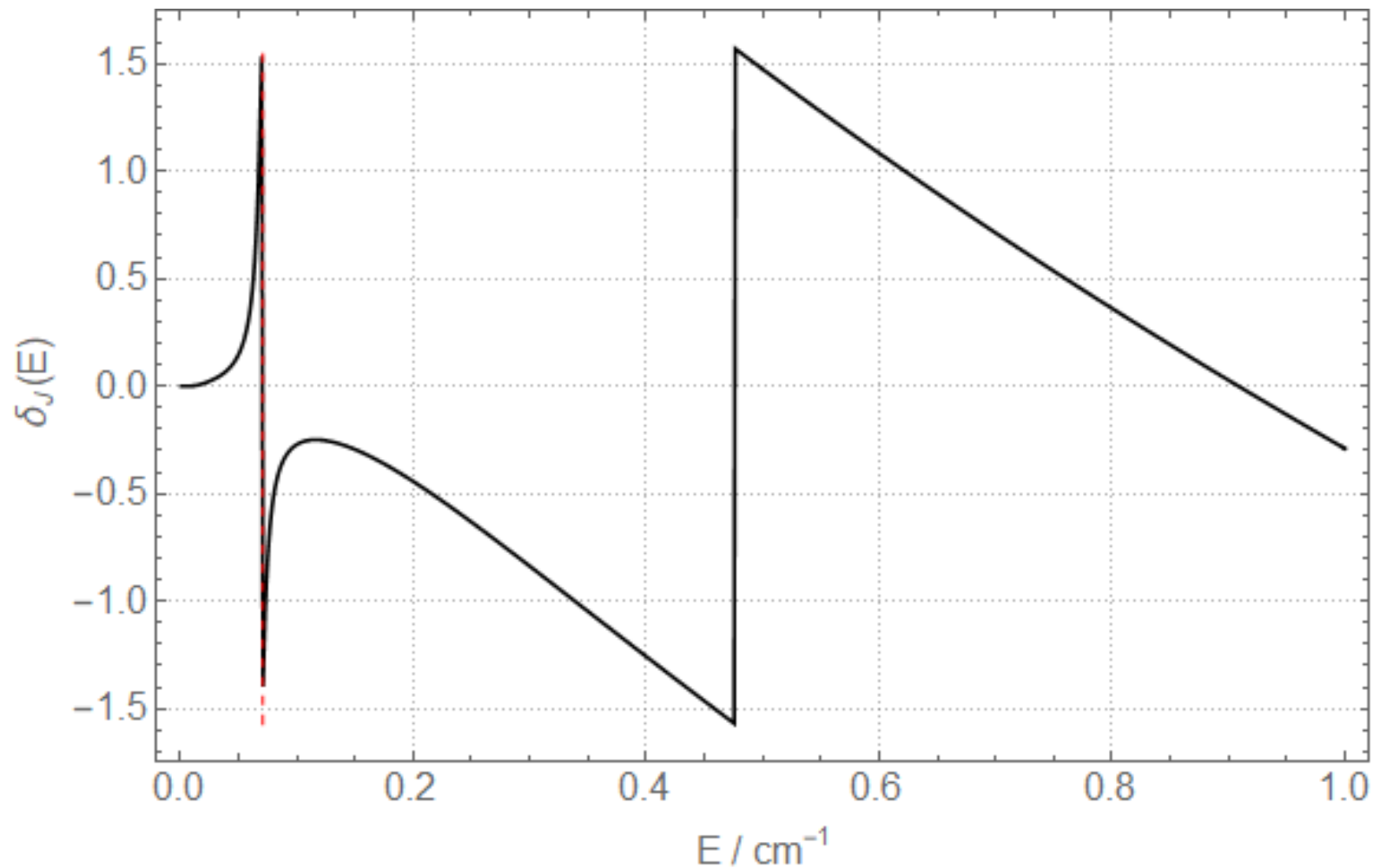
T. Rivlin, L.K. McKemmish and J. Tennyson,
Low temperature scattering with the R-matrix method: the Morse potential,
Springer Conference Proceedings. (in press)

Ar – Ar inner region wavefunctions with Duo

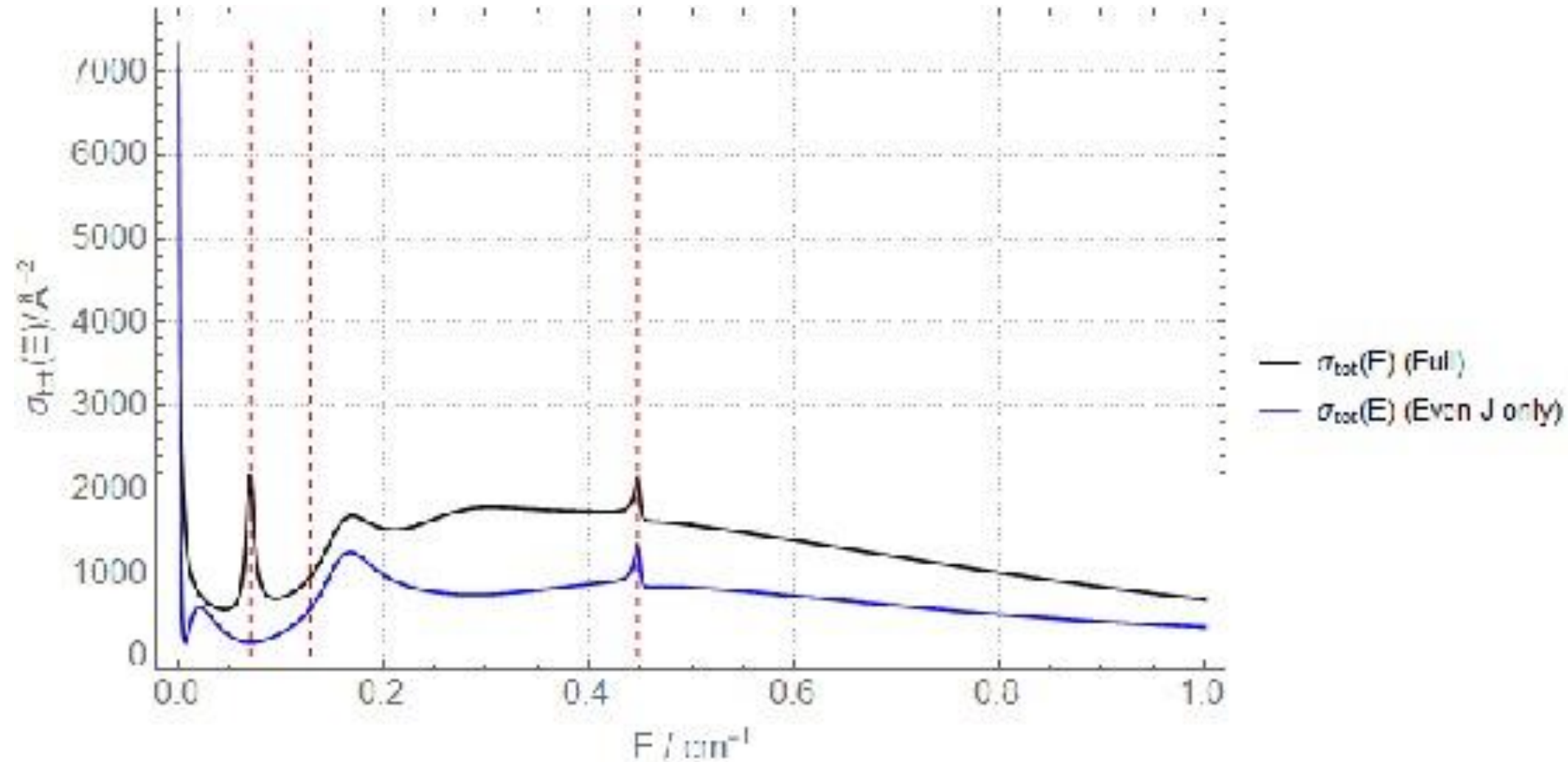


T. Rivlin, LK McKemmish, KE Spinlove & J Tennyson, Mol. Phys. (in press)

Ar – Ar low energy eigenphases: J=5



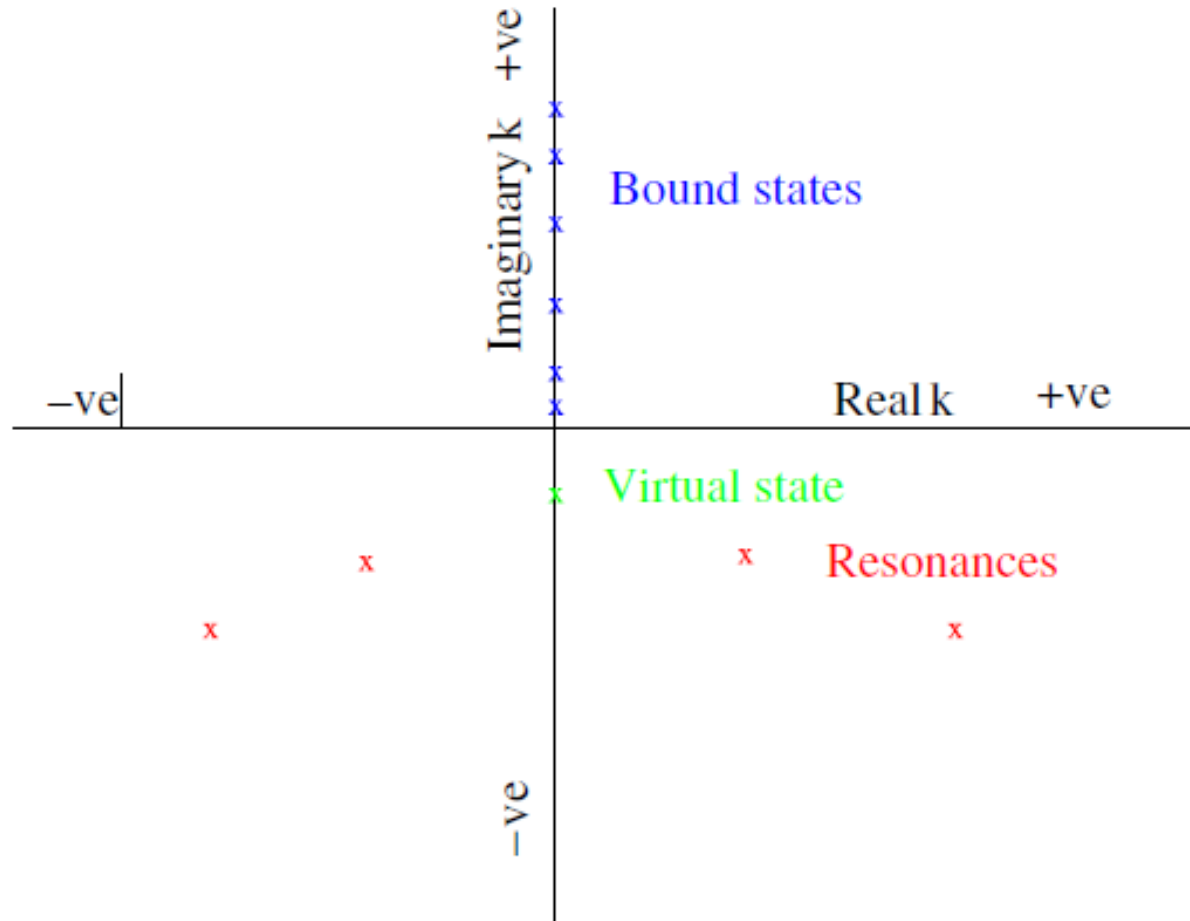
Ar – Ar total cross section at low energy



T. Rivlin, LK McKemmish, KE Spinlove & J Tennyson, Mol. Phys. (in press)

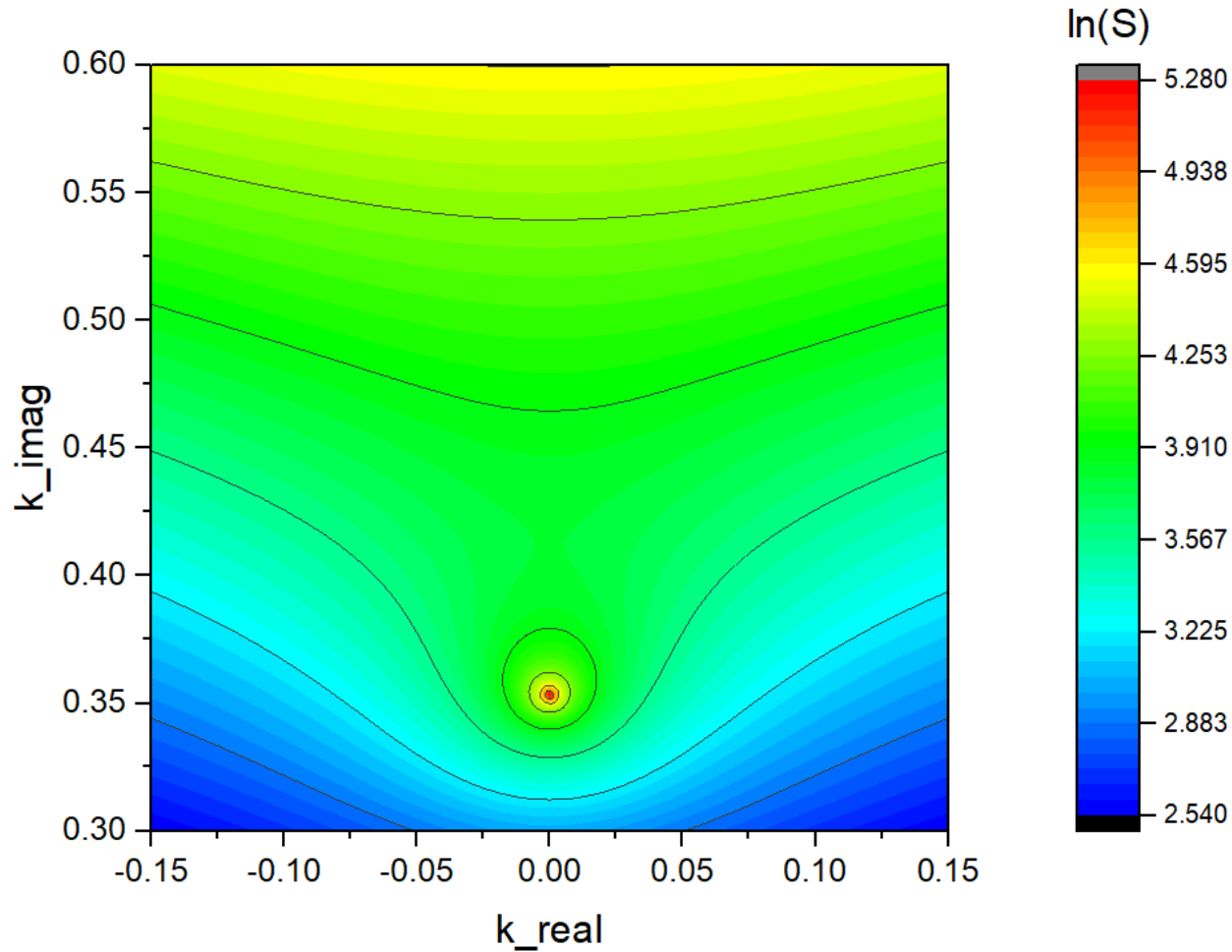
Structure of the S-matrix in the complex k-plane

$$E = k^2/2 \dots$$



PS Bingham & JD Gorfinkiel,
Reskit: A toolkit to determine the poles of an S-matrix
Computer Phys. Comms. 239 272 (2019)

Ar – Ar bound state as pole in S-matrix in the complex k-plane.



RmatReact: current status

- Ar – Ar elastic collisions: completed
- O(3P_J) – He inelastic collisions: nearing completion
- Triatomics (DVR3D) development in progress
- Collaboration with Brianna Heazlewood (Oxford) on ultralow energy ion – molecule collisions


Advanced Textbooks in Physics

Astronomical Spectroscopy

An Introduction to the Atomic and
Molecular Physics of Astronomical Spectroscopy

Third Edition

Jonathan Tennyson

 World Scientific

About the first edition

*“The best book for anyone who is
embarking on research in
astronomical spectroscopy”*

Contemporary Physics (2006)

3rd edition published 18 June 2019

www.worldscientific.com/worldscibooks/10.1142/q0207