

Physics with heavy ions at FCC

Liliana Apolinário



on behalf of the FCC-hh working group

Based on:

A. Dainese et al. arXiv:1605.01389 and the chapter 16 of FCC-CDR Volume 1



"Physics at FCC: overview of the Conceptual Design Report"

March 2019, CERN

- ◆ Large increase in Centre-of-mass energies:

$$pp: \sqrt{s_{NN}} = 100 \text{ TeV}$$

$$pPb: \sqrt{s_{NN}} = 63 \text{ TeV}$$

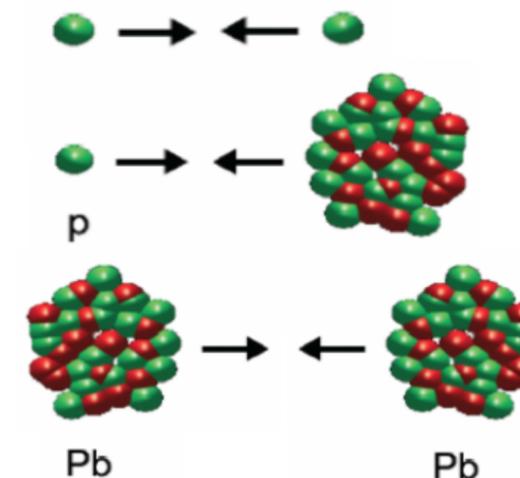
$$PbPb: \sqrt{s_{NN}} = 39 \text{ TeV}$$

- ◆ Why a heavy-Ion program?

- ◆ Fundamental questions about nature of QCD matter at high temperature and density:

How collective phenomena emerge from a QFT?

How is the partonic structure of nucleons and nuclei at small-x?



- ◆ More info: <https://fcc.web.cern.ch>

<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/HeavyIons>

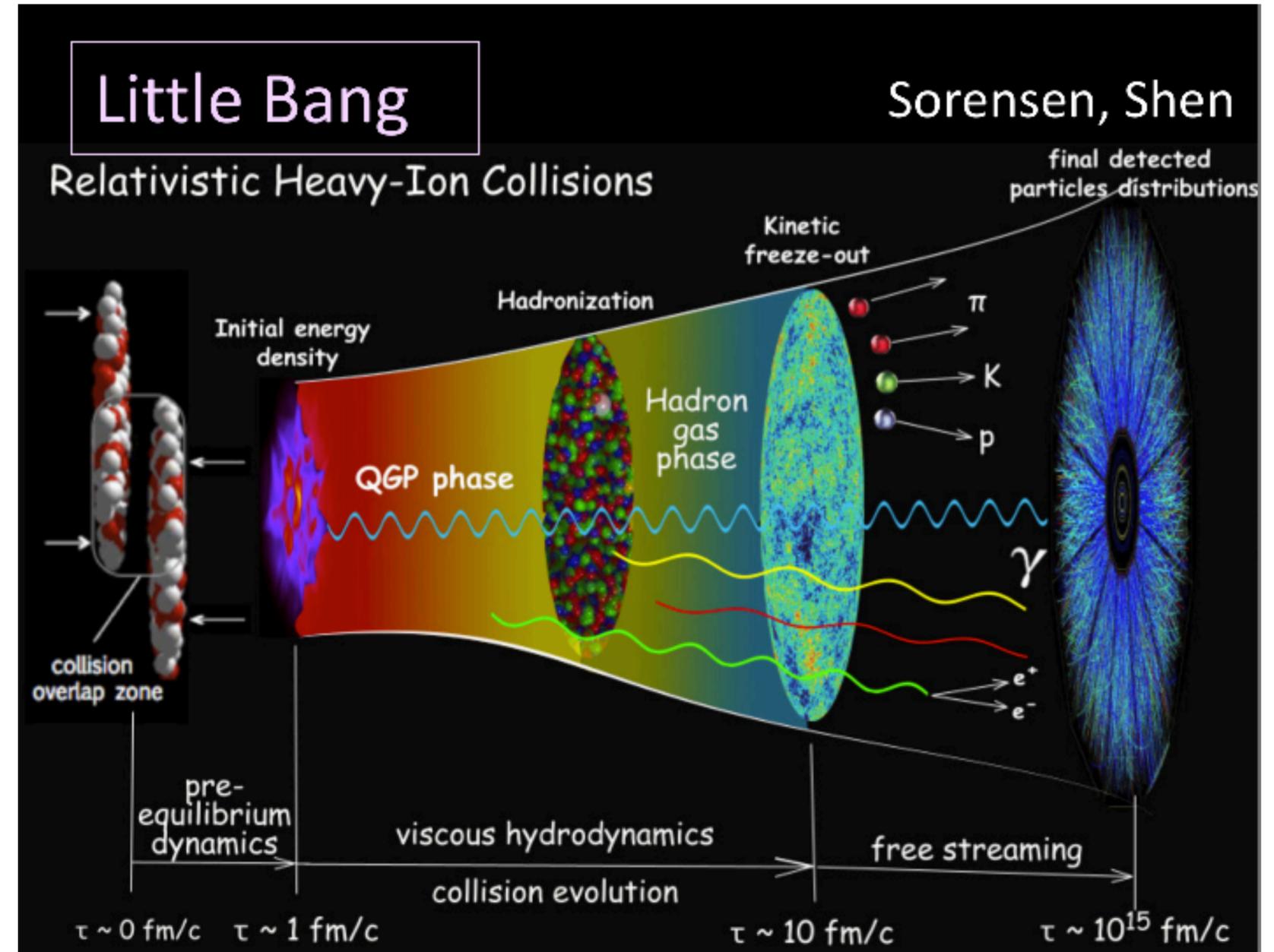
Ch.4 of CERN YR: arXiv:1605.01389

Section editors:

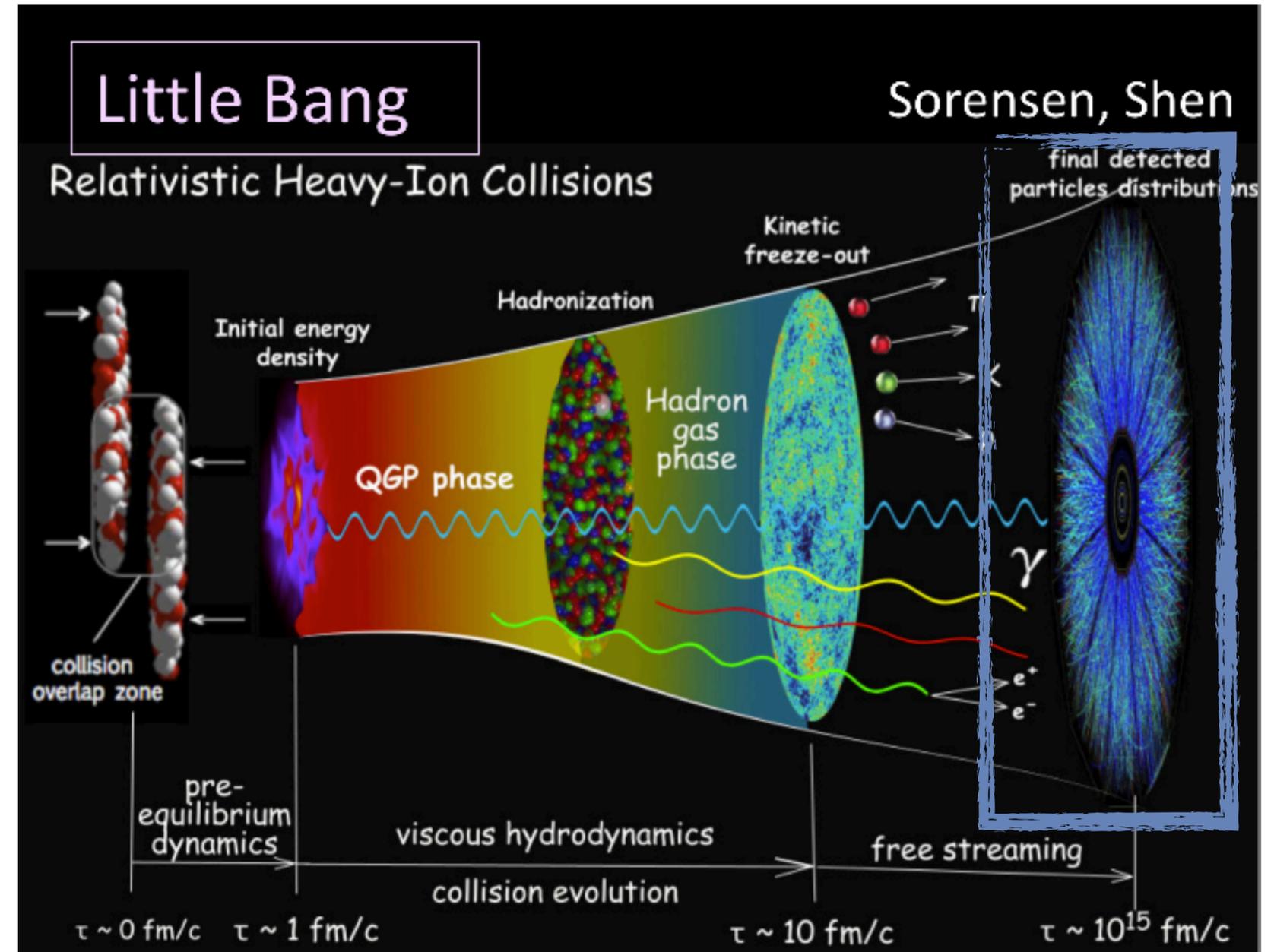
N. Armesto, A. Dainese, D. d'Enterria, J. Jowett, J.P.Lansberg, G.

Milhano, C. Salgado, M. Schaumann, M. van Leeuwen, U. Wiedemann

- ◆ Heavy-Ion Collisions:
 - ◆ Study of nuclear matter in extreme regimes of temperature and density in a controlled environment;
 - ◆ Very short lifetime \Rightarrow Only indirect probing:
 - ◆ Direct decay products of its evolution (Soft Probes)
 - ◆ High momentum particles produced within the collision (Hard Probes)



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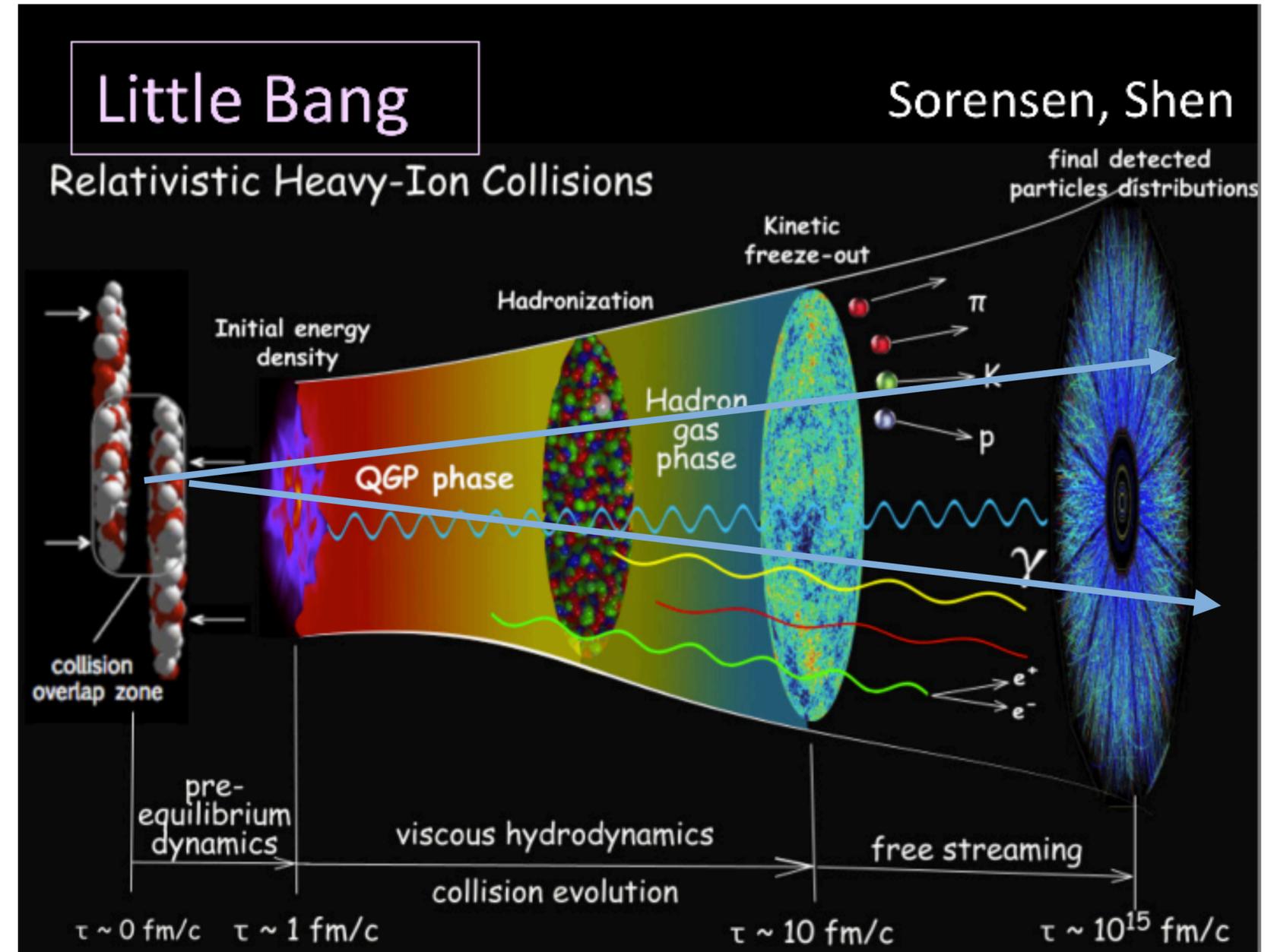
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*See Monday talks
(D. Schulte and W. Riegler)*

◆ FCC parameters for PbPb and pPb collisions:

	Unit	FCC Injection	FCC Collision	
Operation mode		Pb	Pb–Pb	p–Pb
Beam energy	[TeV]	270	4100	50
$\sqrt{s_{NN}}$	[TeV]	-	39.4	62.8

vs LHC: 5.5 (PbPb) and 8.8 (pPb)

	Unit	Baseline		Ultimate	
Operation mode	-	PbPb	pPb	PbPb	pPb
Number of Pb bunches	-	2760		5400	
Bunch spacing	[ns]	100		50	
Peak luminosity (1 experiment)	$[10^{27} \text{cm}^{-2} \text{s}^{-1}]$	80	13300	320	55500
Integrated luminosity (1 experiment, 30 days)	$[\text{nb}^{-1}]$	35	8000	110	29000

*(ultimate scenario)
1 month ~ 10x LHC*

- ◆ Focus on qualitative advances from the FCC:

QGP bulk properties

Decay products of QGP

- ⌄ Volume and Lifetime

- ⌄ Temperature: charm thermal production

- ⌄ Multiplicity: Collectivity in small systems

Hard probes

Indirect probing of the QGP

- ⌄ Production Rate: tops, Higgs,...

Boosted objects: QGP time evolution

Quarkonia: QGP temperature evolution

Initial State

Fix initial conditions for collectivity

- ⌄ Parton densities: Saturation Physics

- ⌄ Energy: nuclear PDFs in different kinematic range

QGP Bulk Properties

The image shows a wide, panoramic view of a mountainous region. In the foreground, a snow-covered slope descends towards a valley. The middle ground features a dense forest of evergreen trees. In the background, a long, low mountain range stretches across the horizon under a clear blue sky. The text 'QGP Bulk Properties' is centered in the image in a bold, white font. There are several hand-drawn scribbles: a blue line that loops around the text and extends across the middle of the image, and a black line that forms a large, irregular shape around the text and extends towards the left and bottom edges.

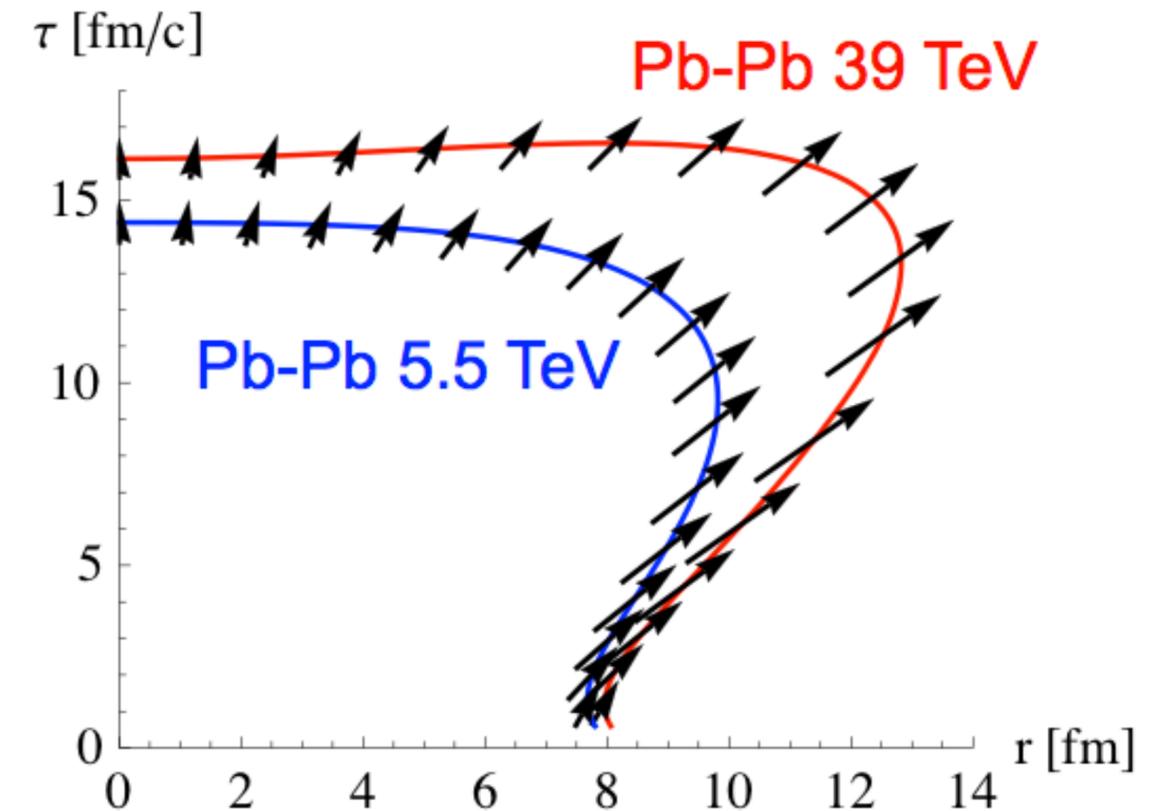
◆ Global properties:

Quantity	Pb–Pb 5.5 TeV	Pb–Pb 10.6 TeV	Pb–Pb 39 TeV
$dN_{\text{ch}}/d\eta$ at $\eta = 0$	2000	2400	3600
$dE_{\text{T}}/d\eta$ at $\eta = 0$	2.3–2.6 TeV	3.1–3.4 TeV	5.2–5.8 TeV
Homogeneity volume	6200 fm ³	7400 fm ³	11000 fm ³
Decoupling time	11 fm/c	11.5 fm/c	13 fm/c
ε at $\tau = 1$ fm/c	16–17 GeV/fm ³	22–24 GeV/fm ³	35–40 GeV/fm ³

~ x 1.5-2 w.r.t
(HE)-LHC TeV

◆ Expected impact on medium bulk properties:

- ◆ Denser medium \Rightarrow longer expansion and larger volume
(before freeze-out)



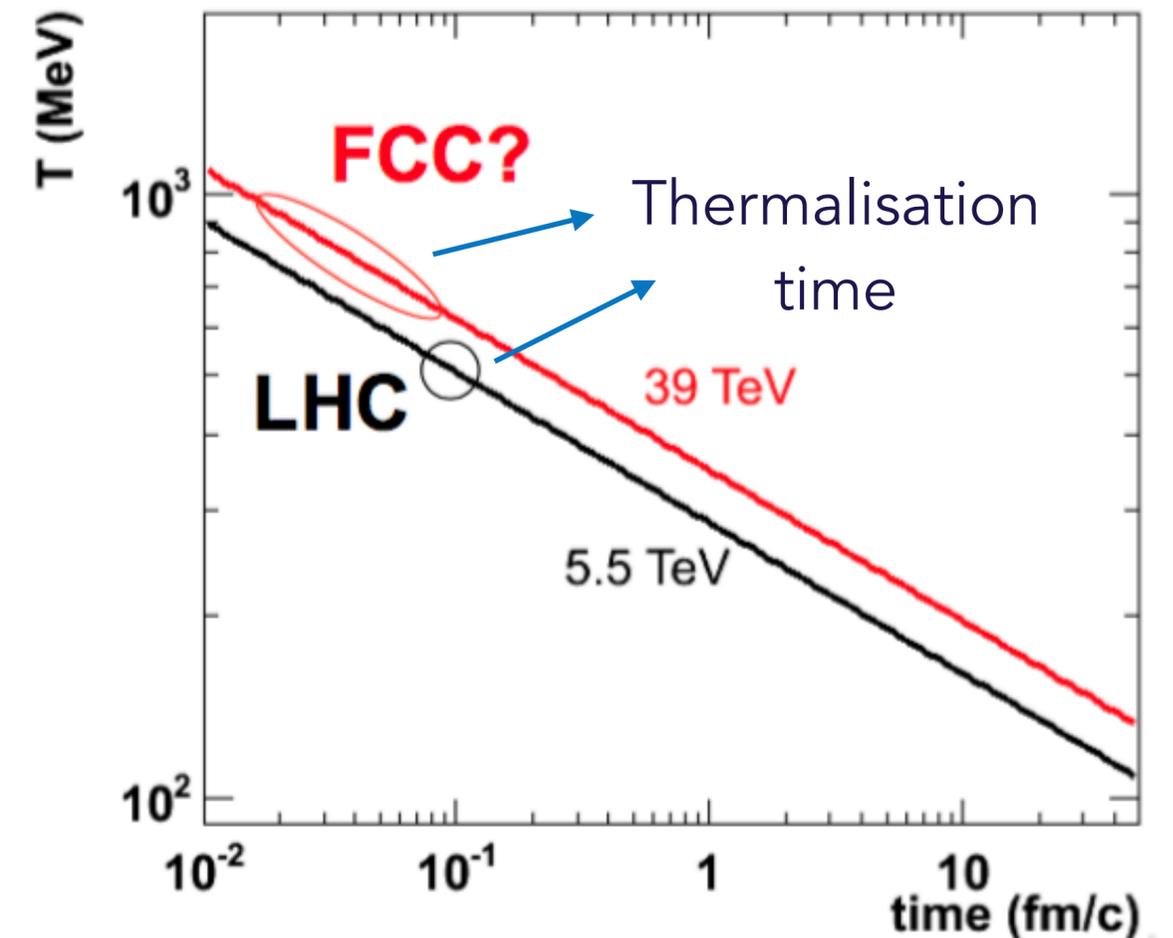
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- ◆ Higher initial energy \Rightarrow larger temperature and smaller
thermalisation time



Medium Bulk Properties

◆ Global properties:

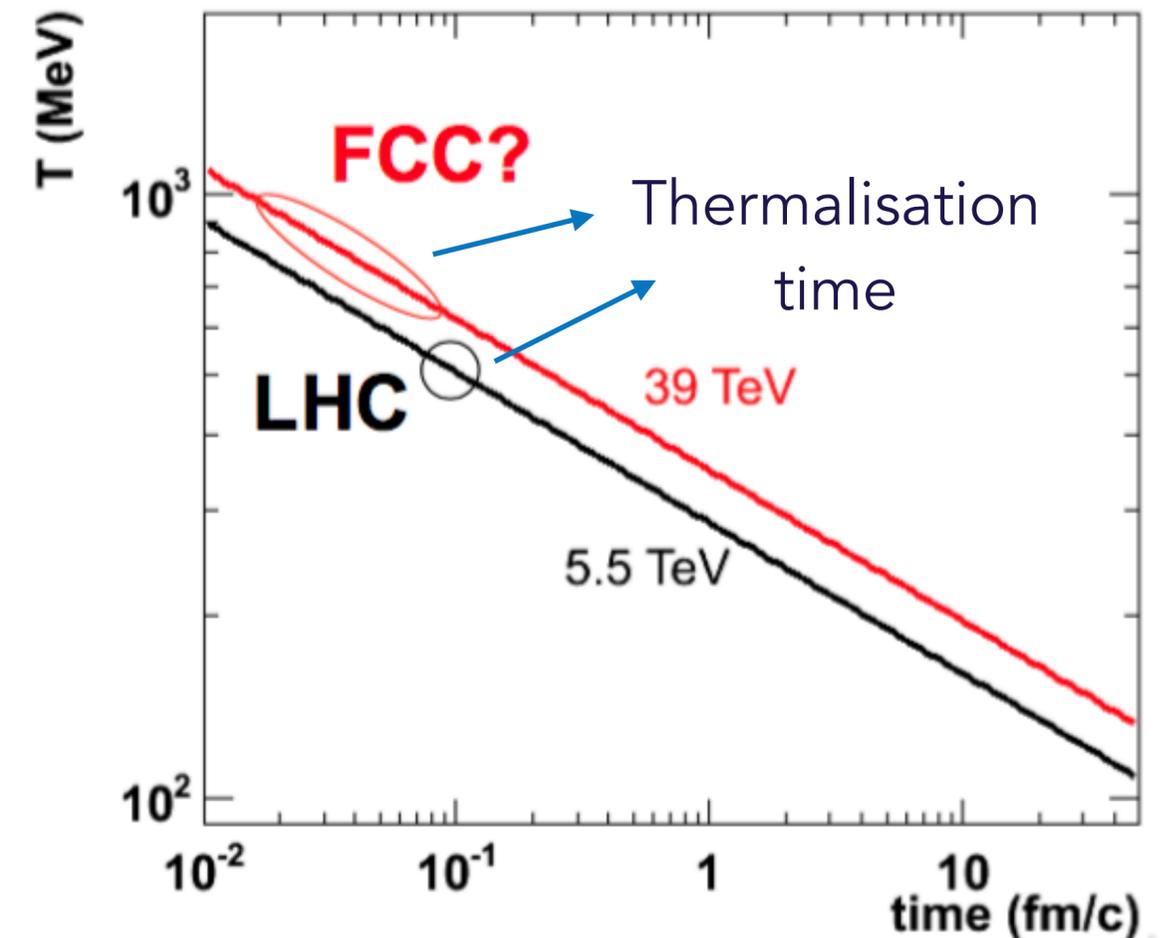
Quantity	Pb–Pb 5.5 TeV	Pb–Pb 10.6 TeV	Pb–Pb 39 TeV
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(HE)-LHC TeV

*What can this
larger/denser/hotter
medium do for us?*

◆ Expected impact on medium bulk properties:

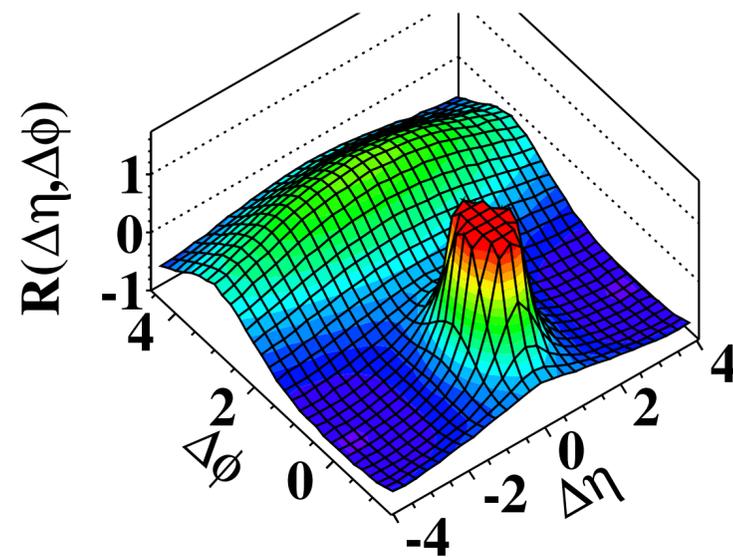
- ◆ Denser medium \Rightarrow longer expansion and larger volume (before freeze-out)
- ◆ Higher initial energy \Rightarrow larger temperature and smaller thermalisation time



- ◆ Collectivity signs in pA and high multiplicity pp?
- ◆ System size dependence of flow needs higher order cumulants (large multiplicities)

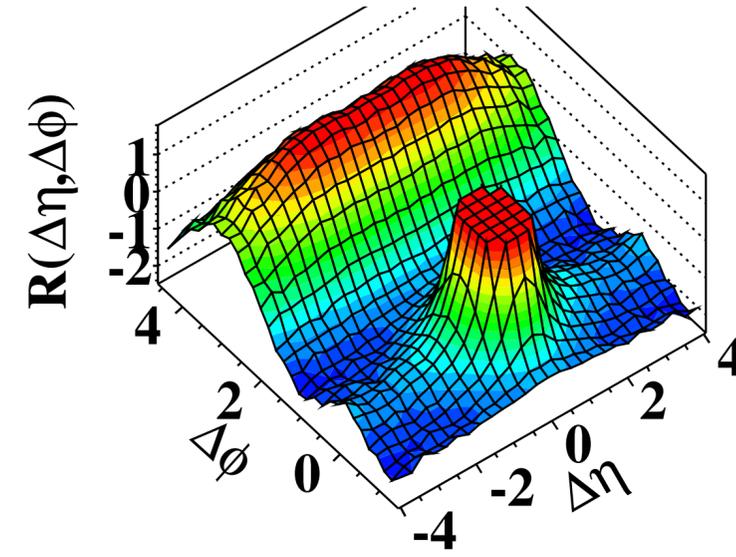
pp@7TeV

(b) CMS **MinBias**, $1.0\text{GeV}/c < p_T < 3.0\text{GeV}/c$



pp@7TeV

(d) CMS **$N \geq 110$** , $1.0\text{GeV}/c < p_T < 3.0\text{GeV}/c$

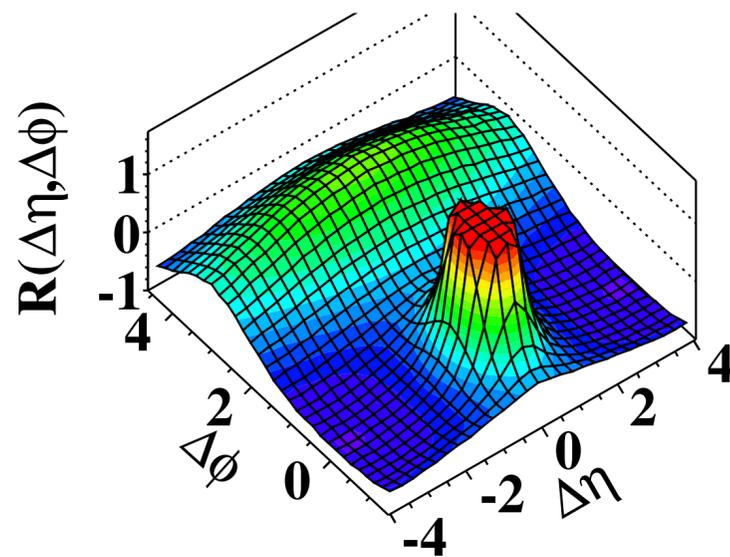


CMS [1009.4122]

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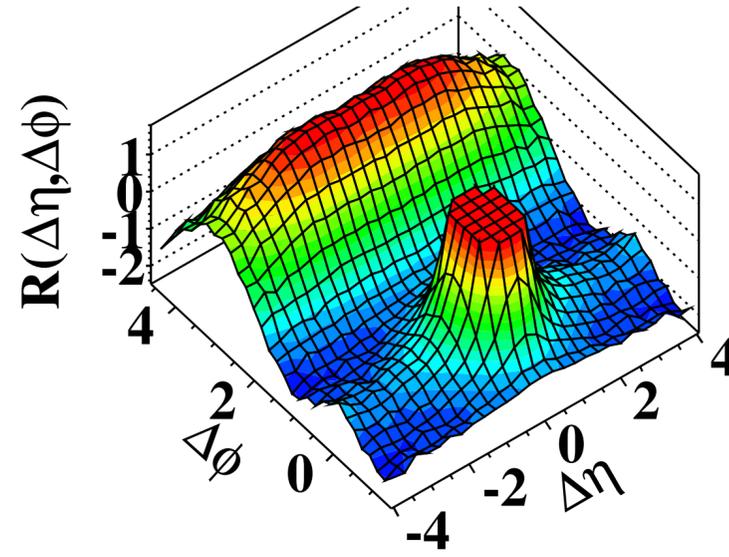
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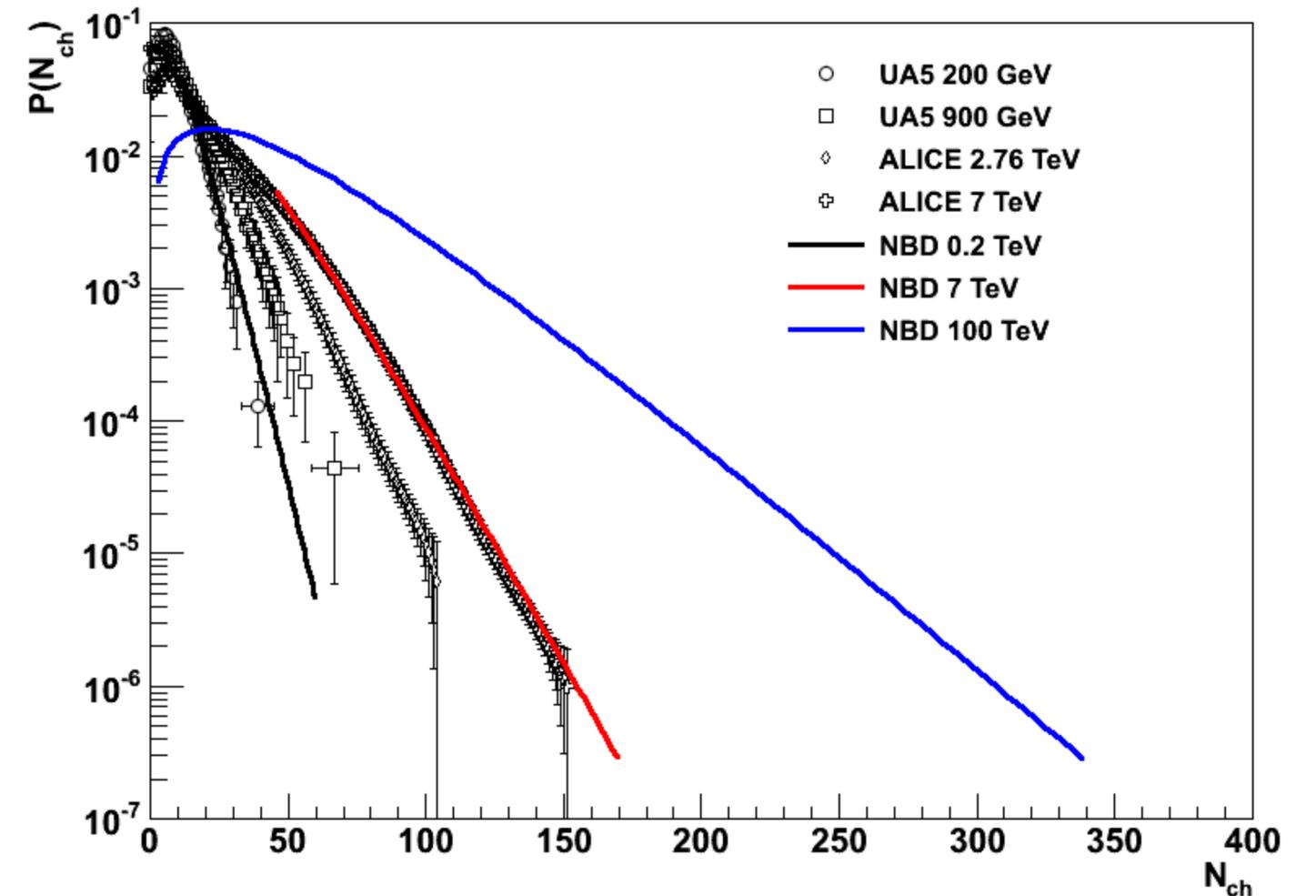


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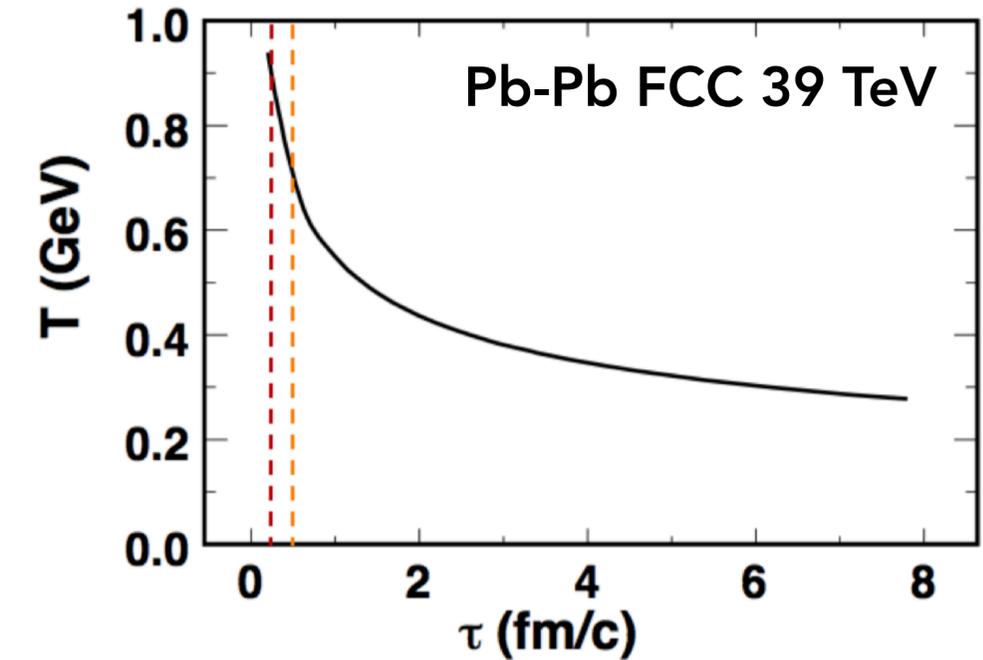
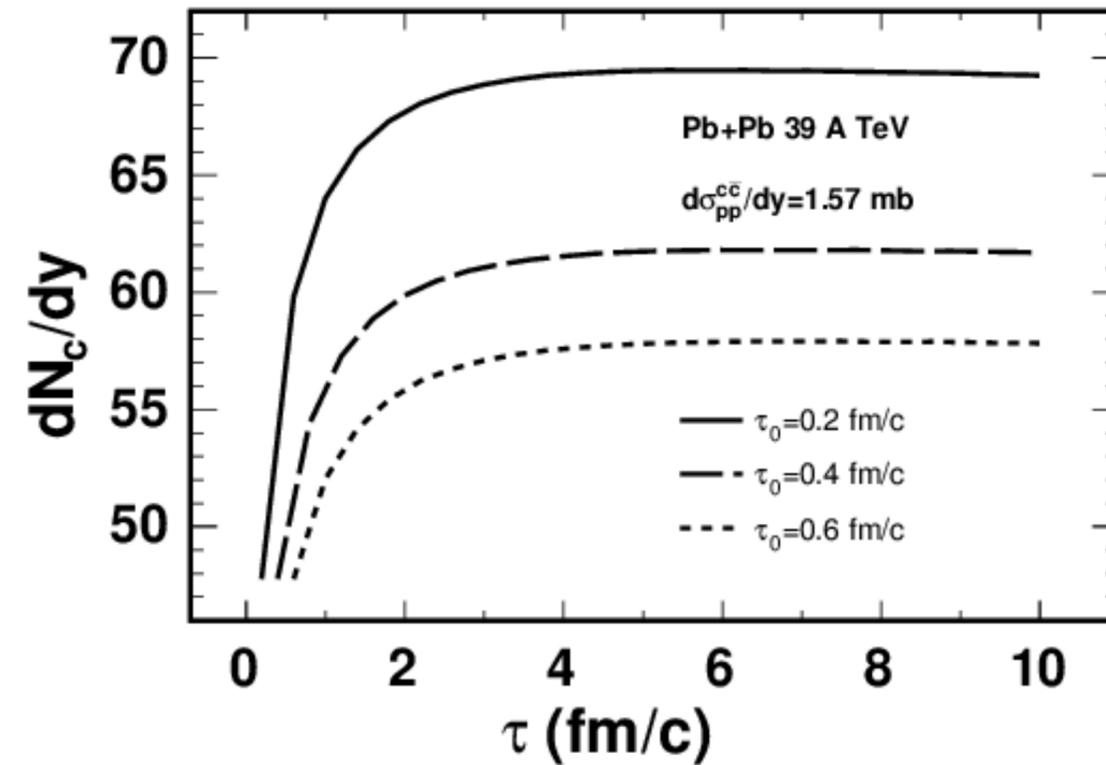
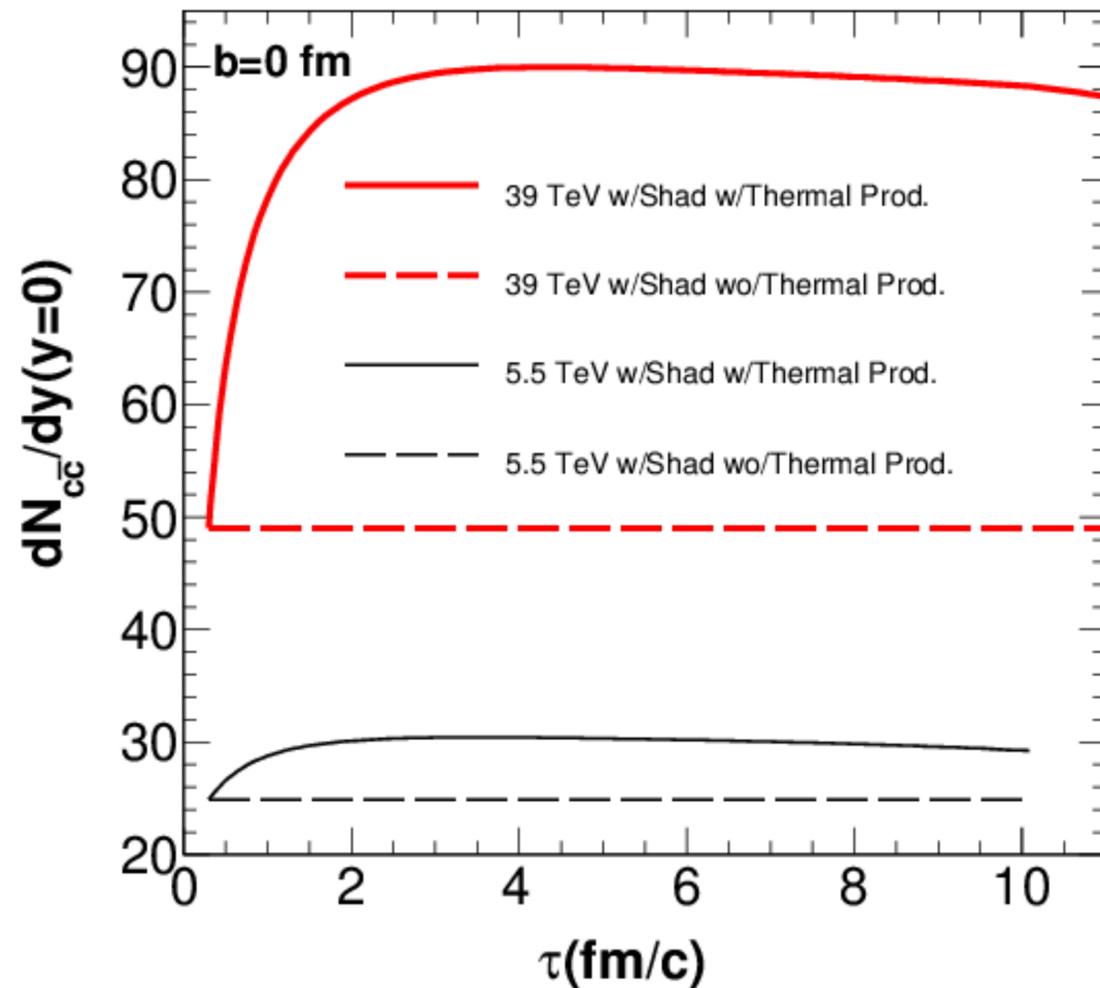


✓ Increase of multiplicity at FCC can help to answer this question!

Thermal Charm Production

Zhou et al (16), Uphoff et al (10-14), Liu et al (16)

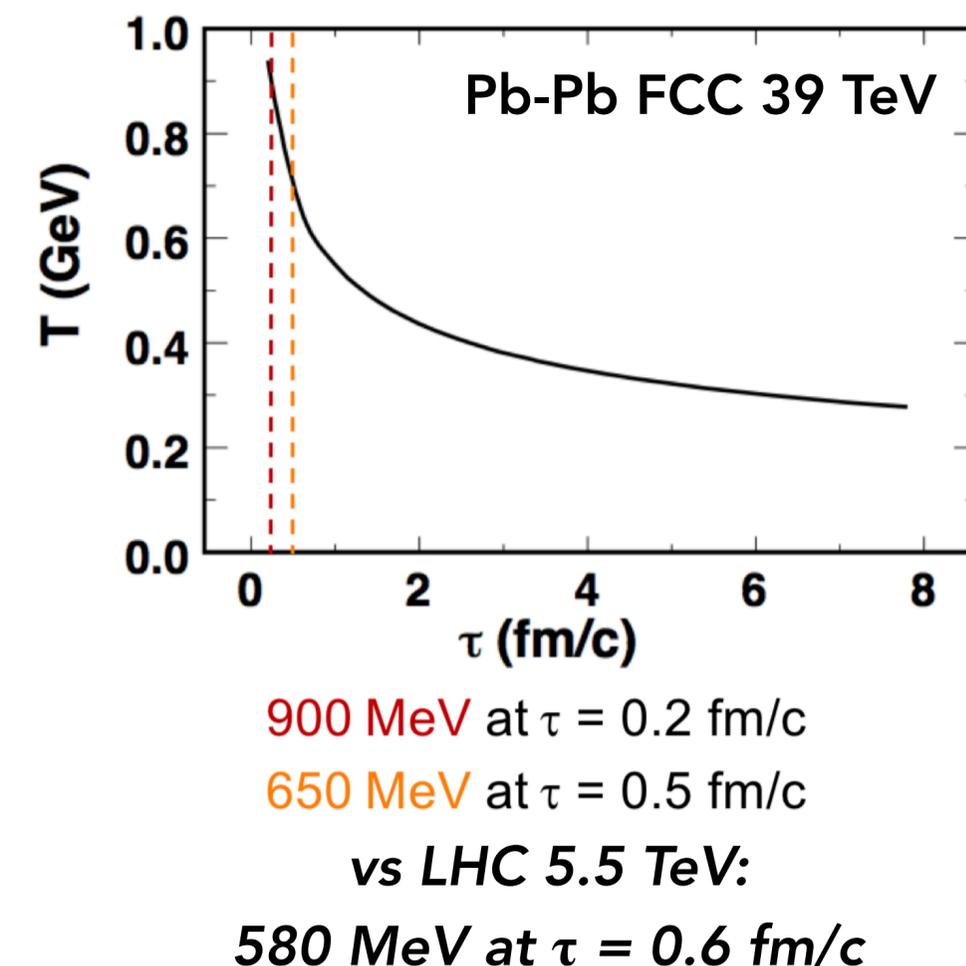
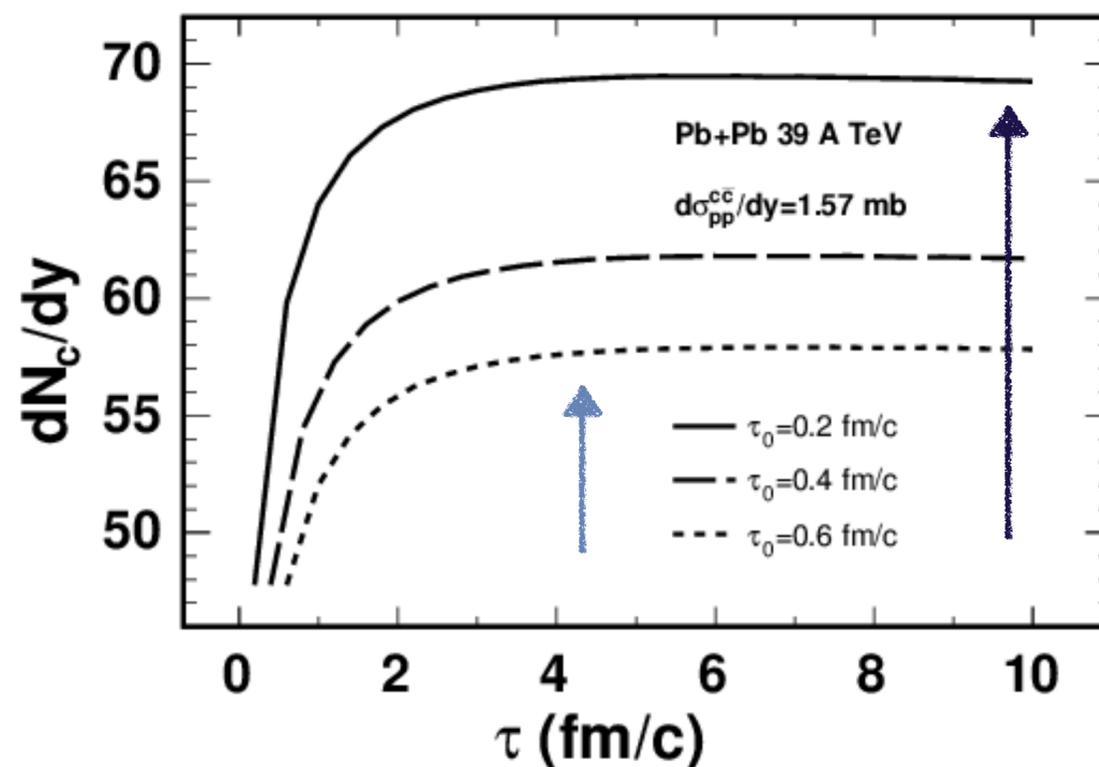
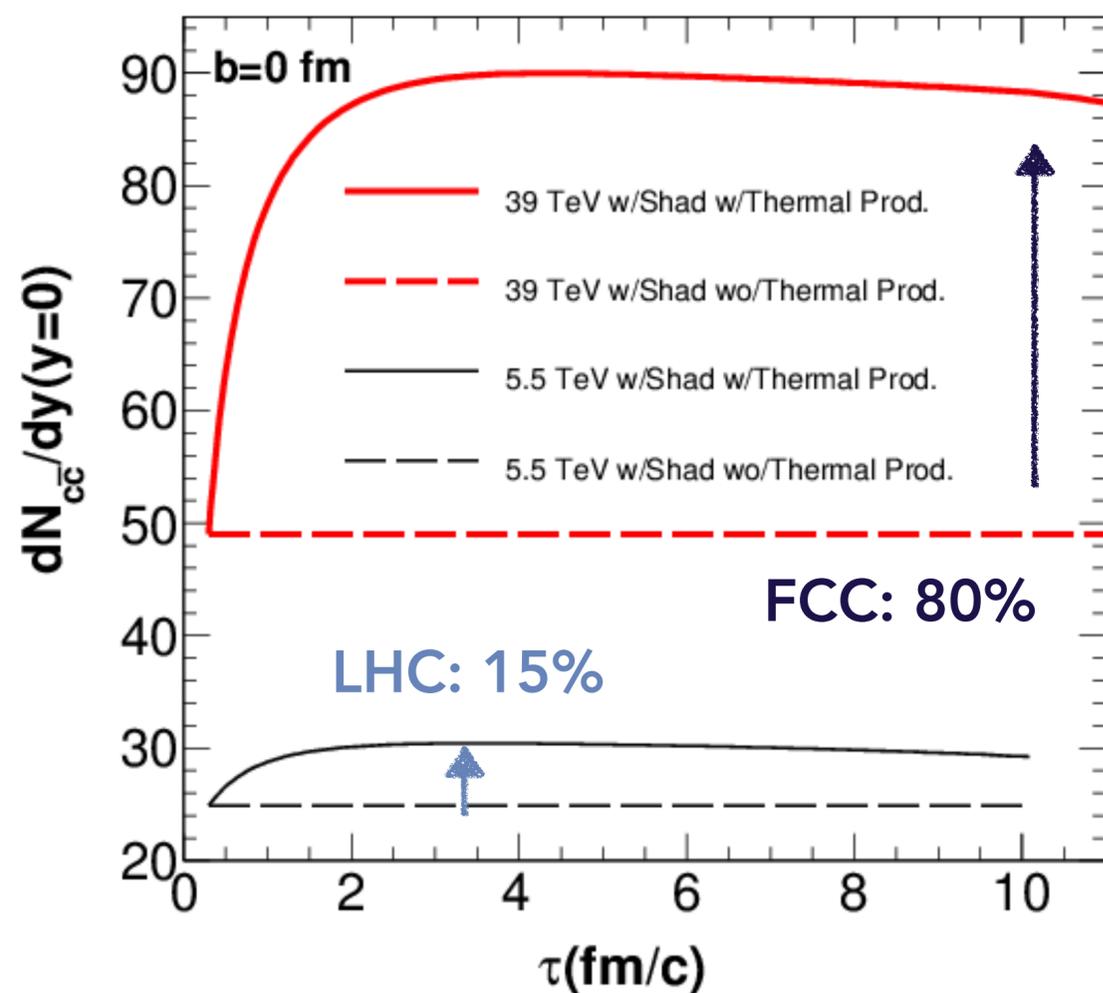
◆ Increase of temperature \Rightarrow Production of low p_T $c\bar{c}$ pairs



900 MeV at $\tau = 0.2$ fm/c
 650 MeV at $\tau = 0.5$ fm/c
 vs LHC 5.5 TeV:
 580 MeV at $\tau = 0.6$ fm/c

Zhou et al (16), Uphoff et al (10-14), Liu et al (16)

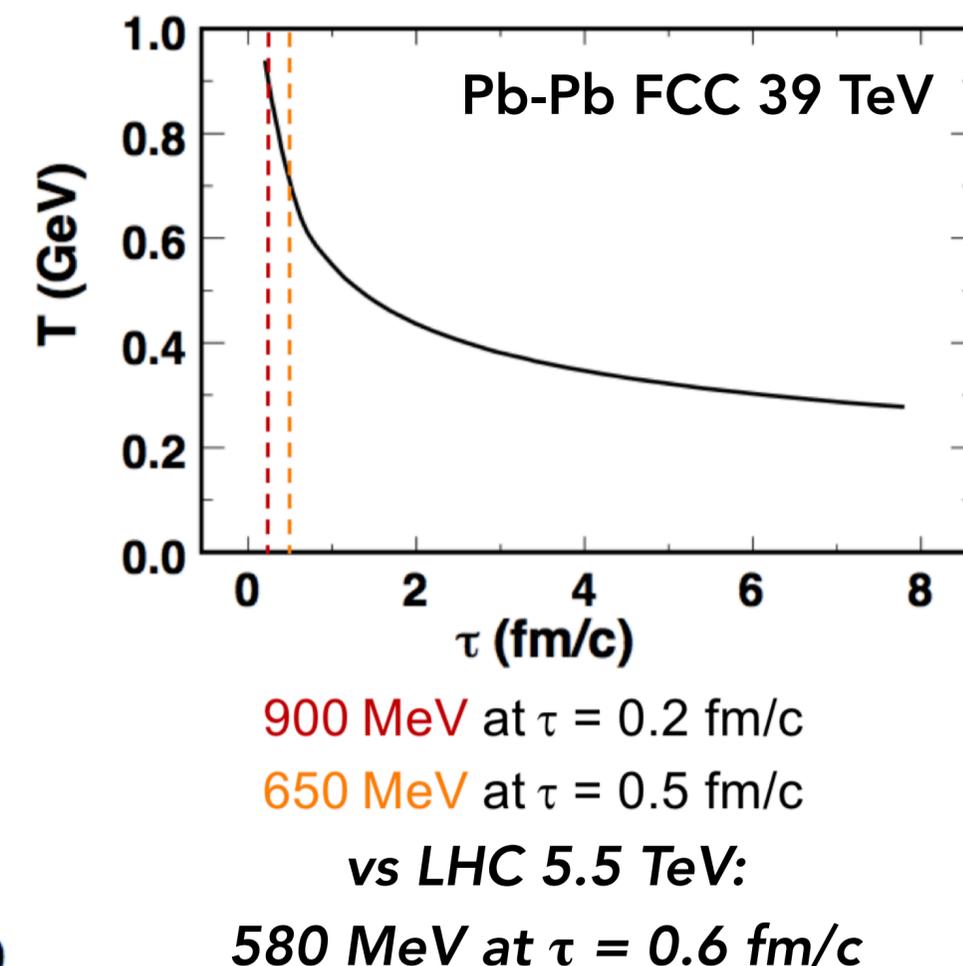
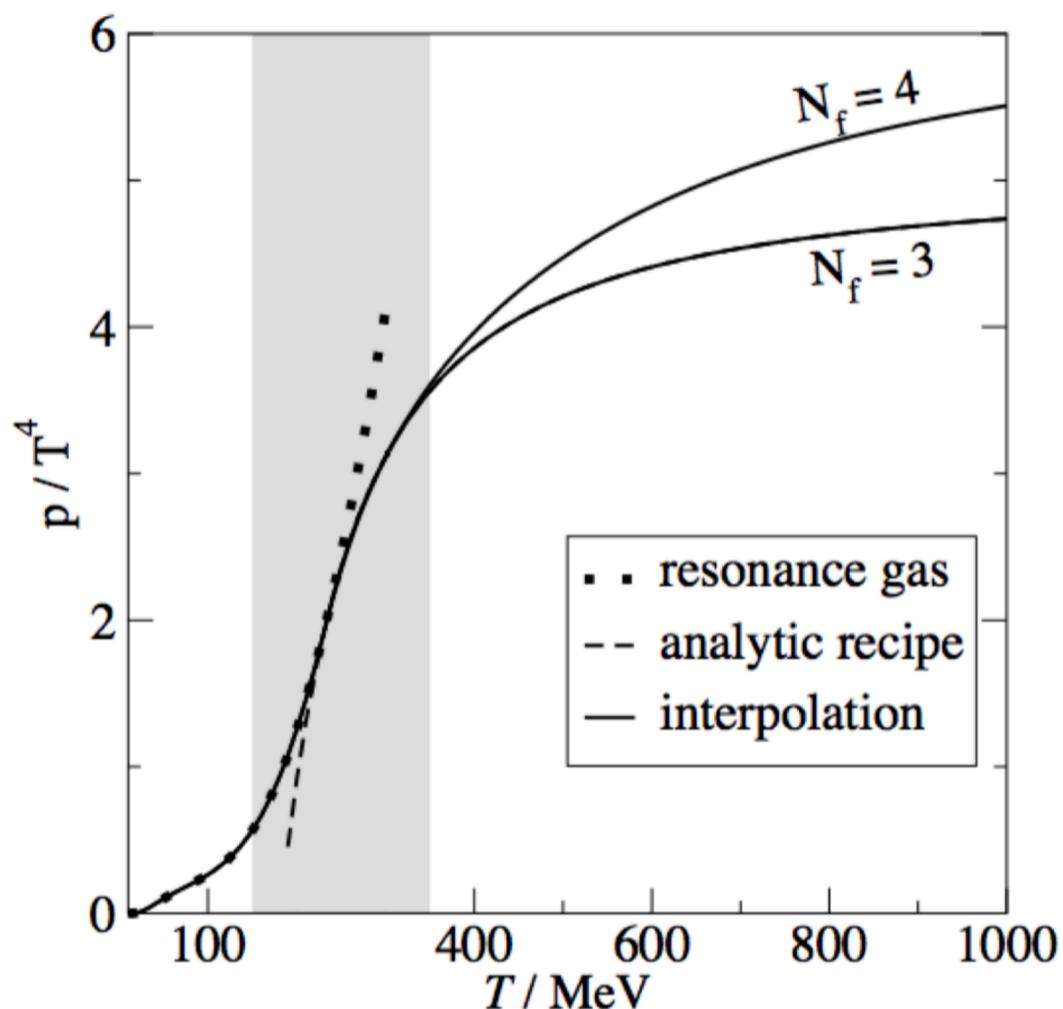
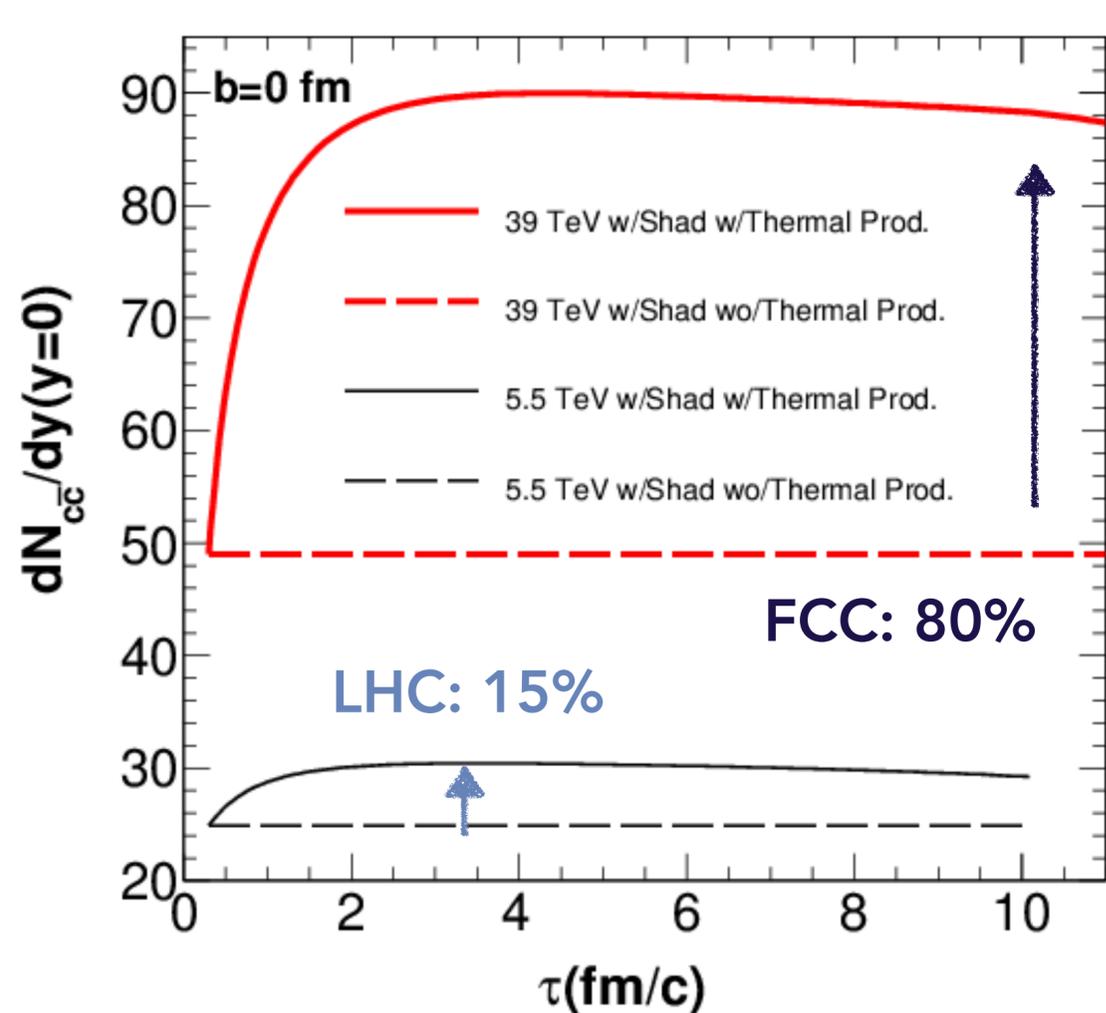
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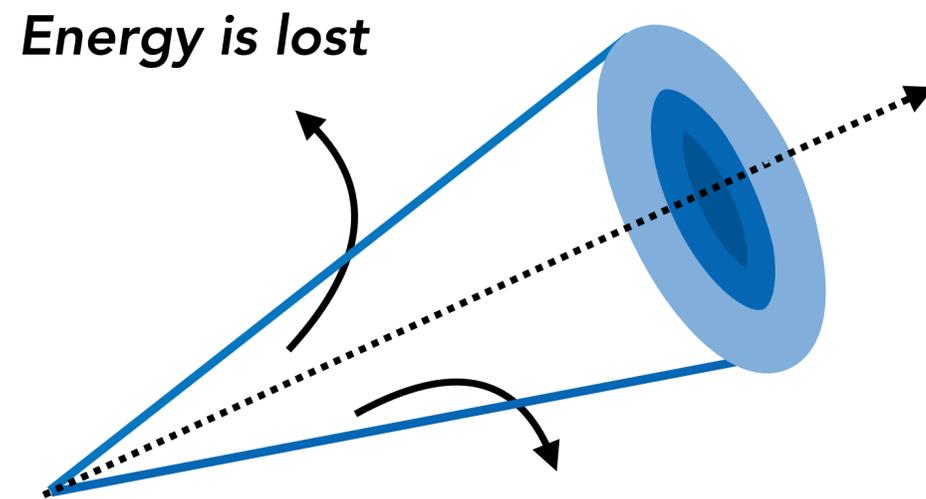


- ✓ FCC: handle on the QGP temperature evolution and formation time!
- ✓ FCC: charm start contribute to QCD equation of state!

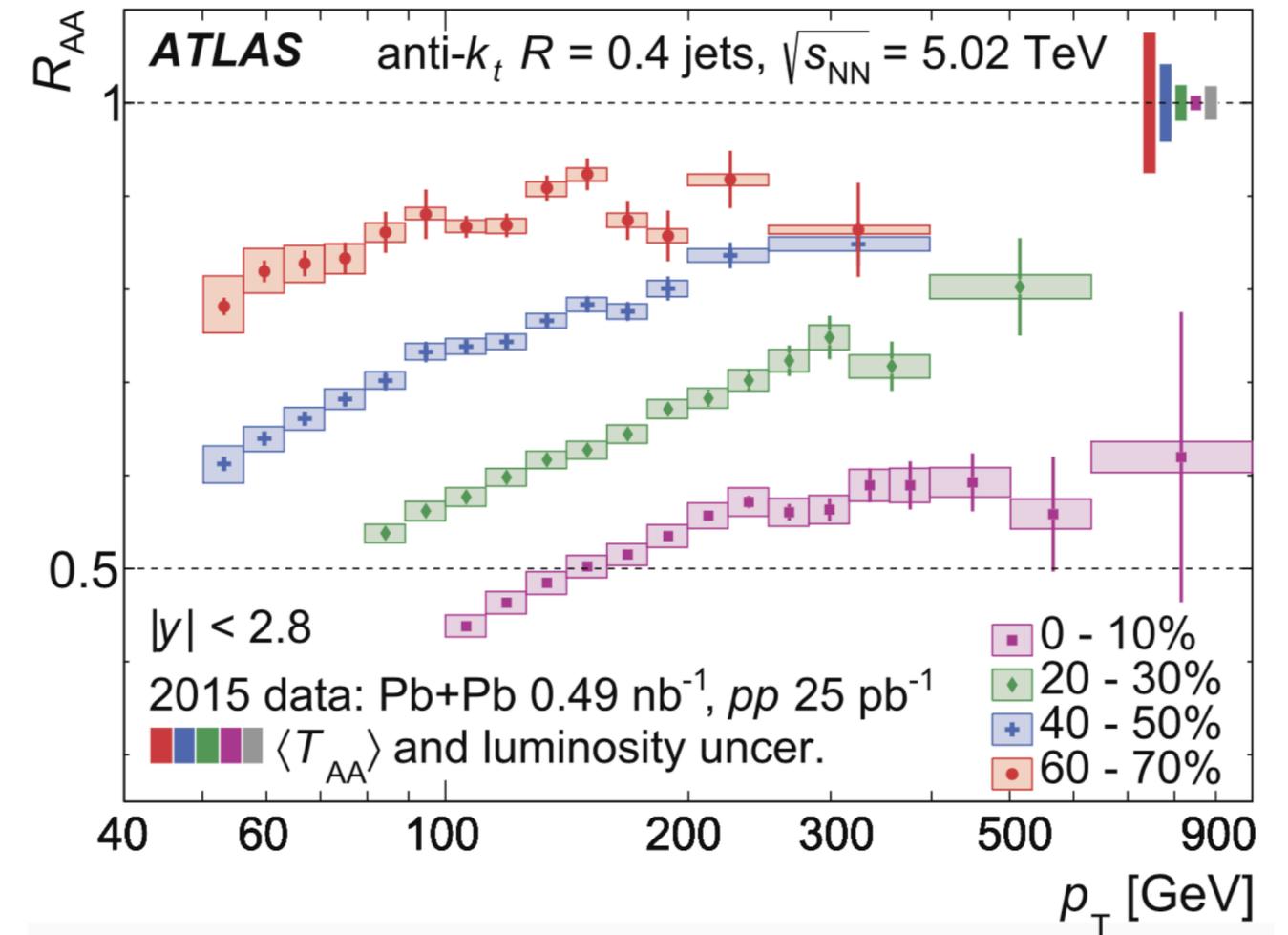


Hard Probes

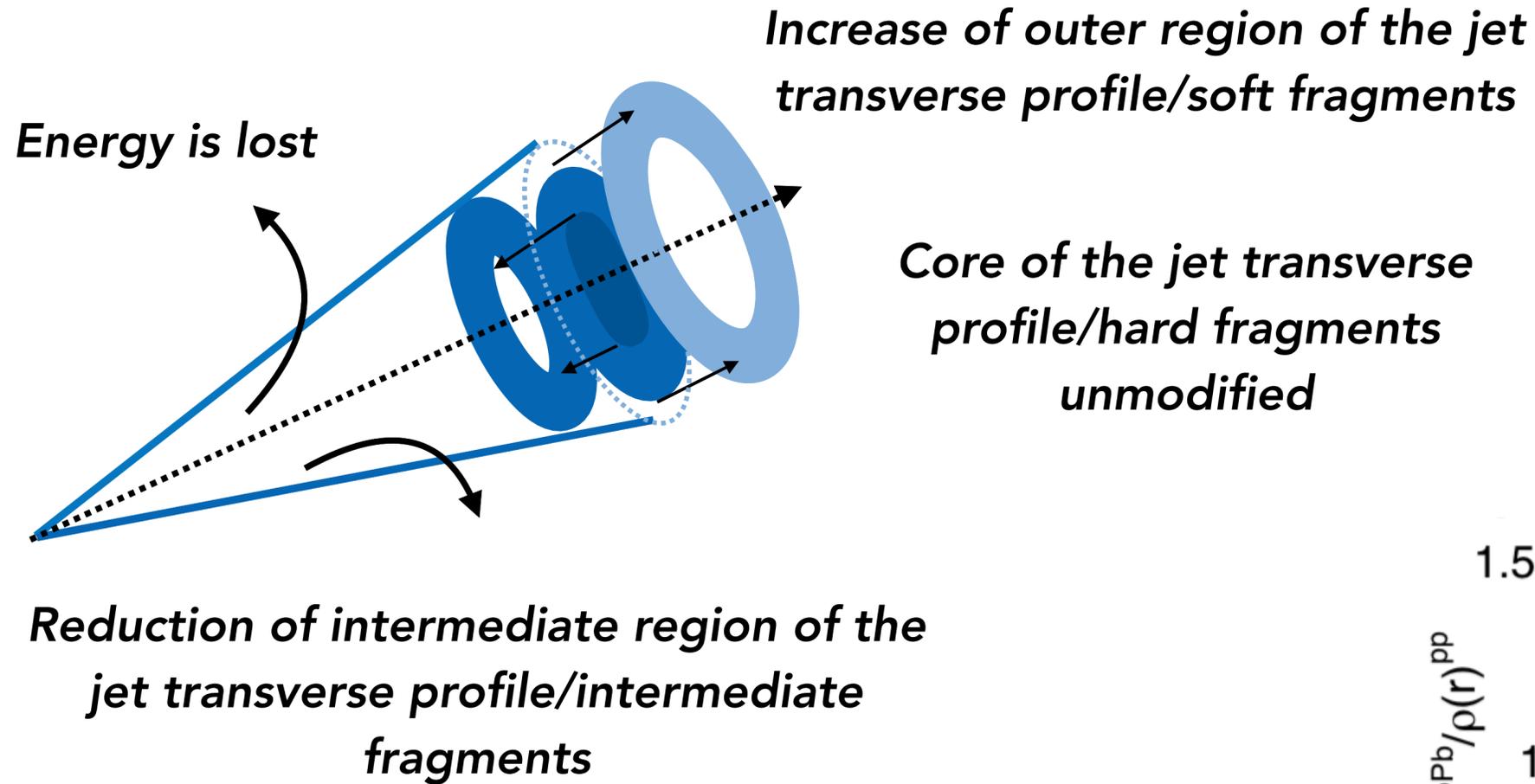
- ◆ Current picture of a medium-modified jet:



**Jet Transverse momentum spectrum
(pp/PbPb)**



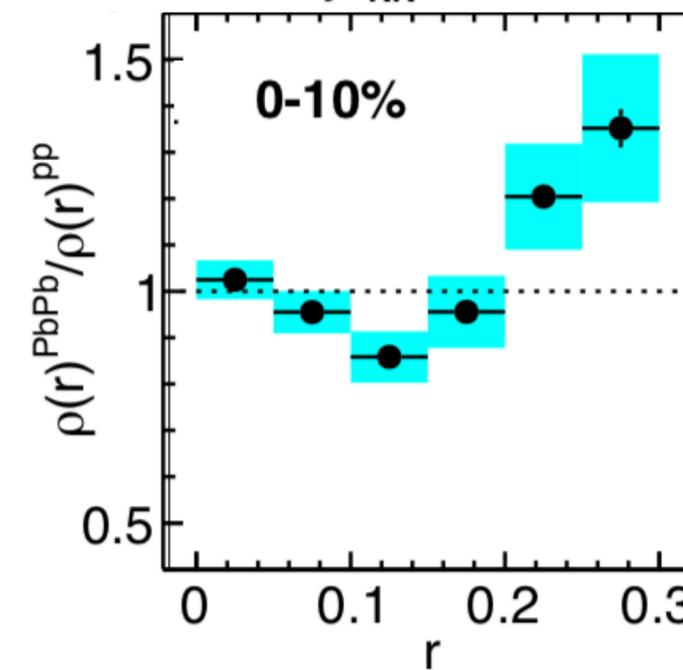
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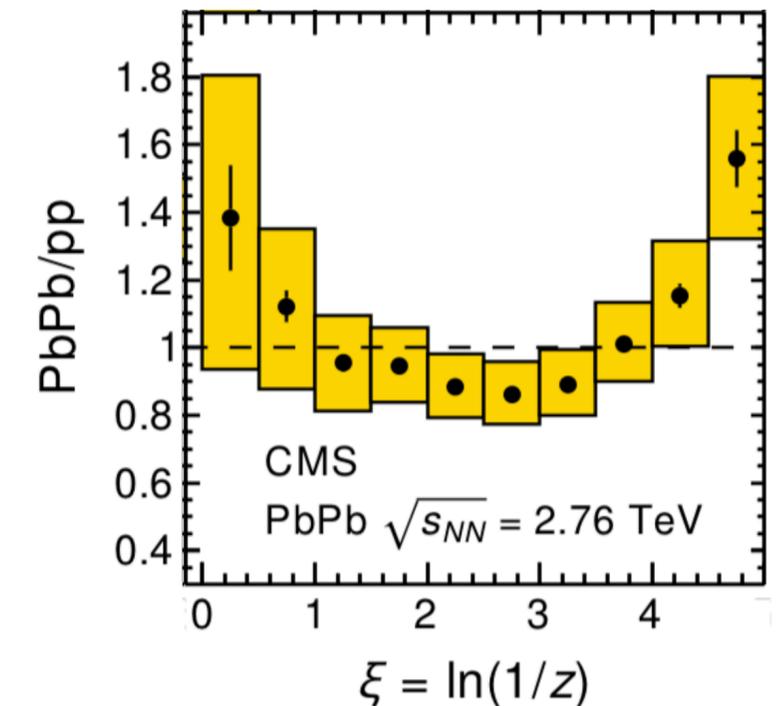
@ LHC: Jets can provide a range of scales to probe the QGP!

Jet radial profile (pp/PbPb)

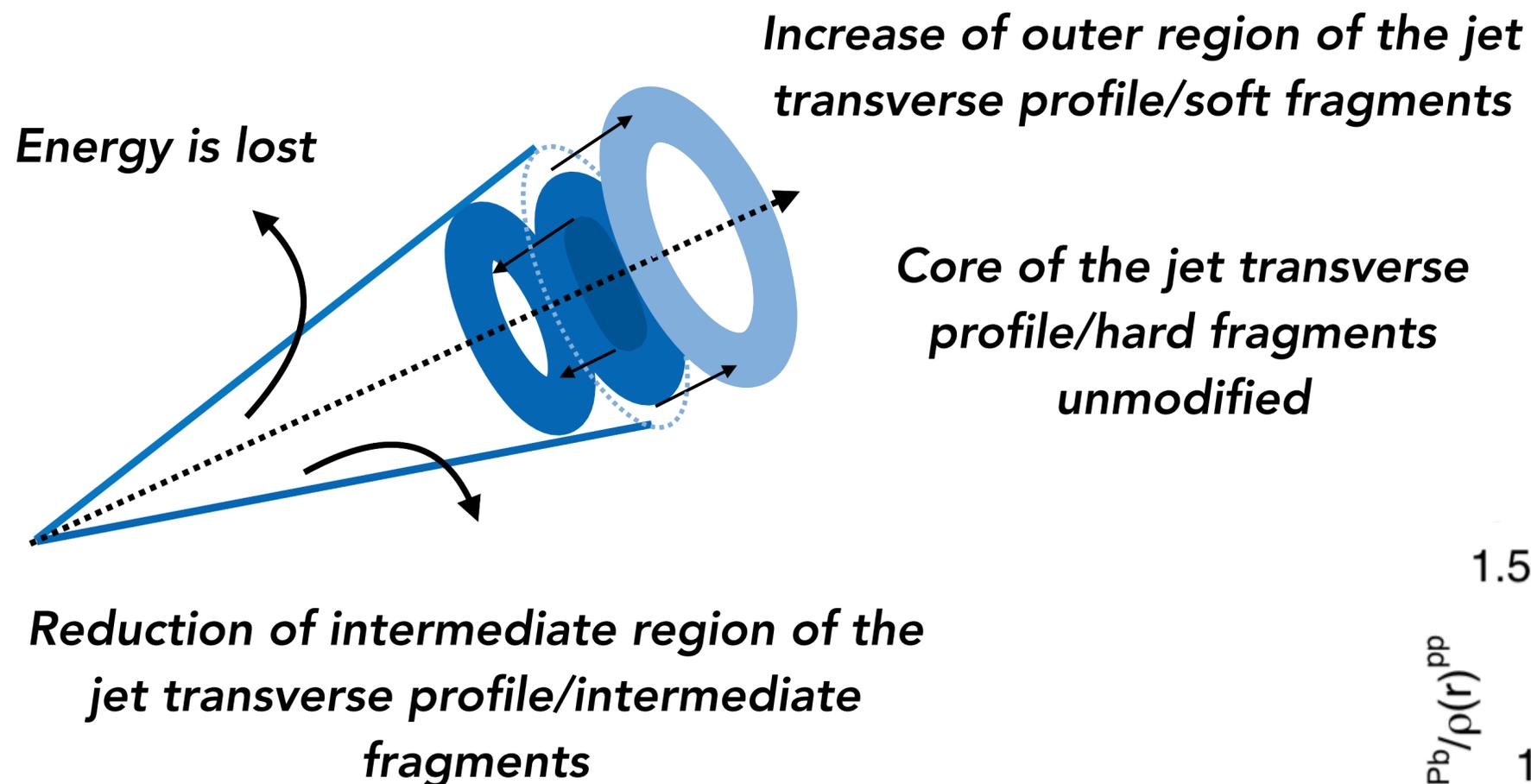
CMS, $\sqrt{s_{NN}} = 2.76$ TeV



Fraction of energy of jet fragments (pp/PbPb)



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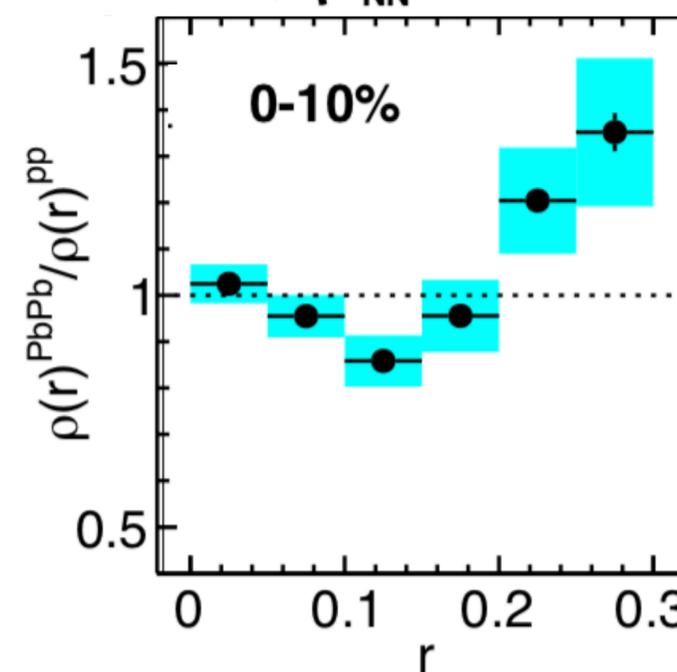


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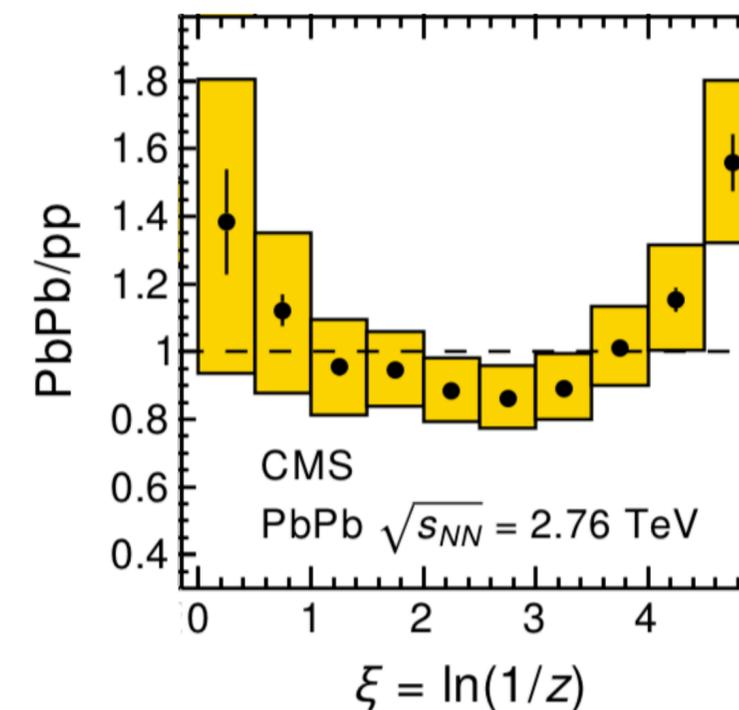
@ FCC: What can it bring of new?

Jet radial profile (pp/PbPb)

CMS, $\sqrt{s_{NN}} = 2.76$ TeV

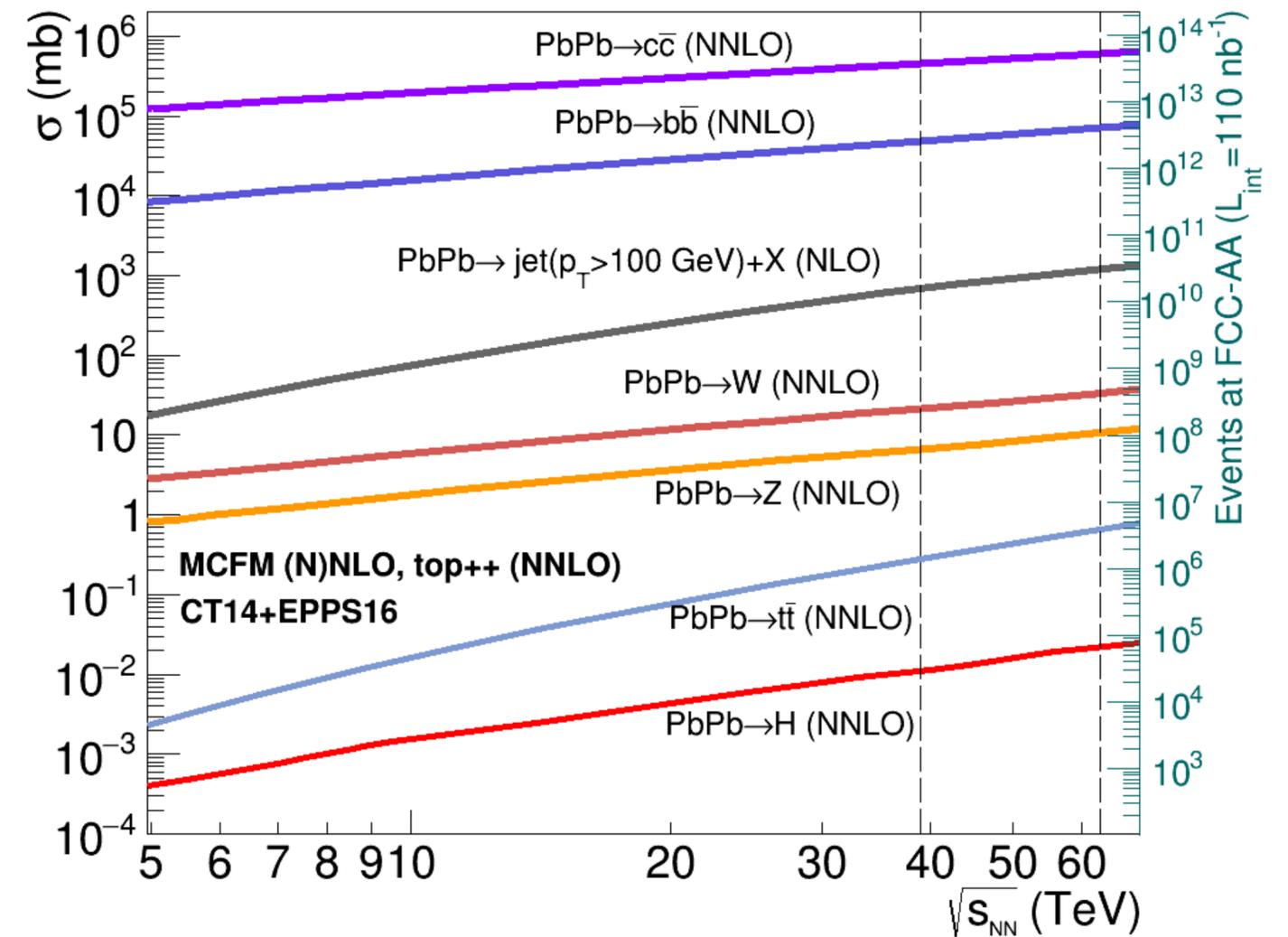
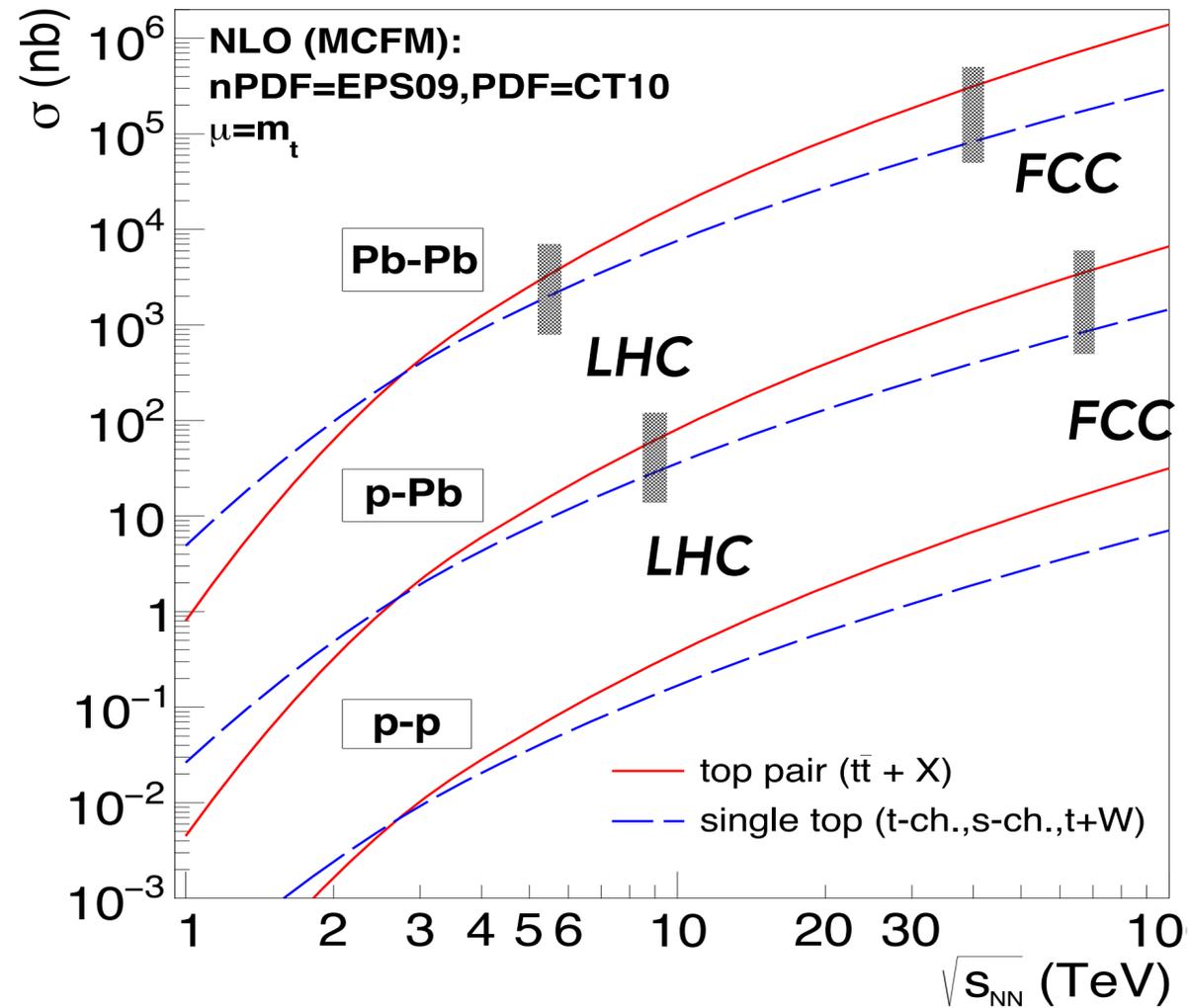


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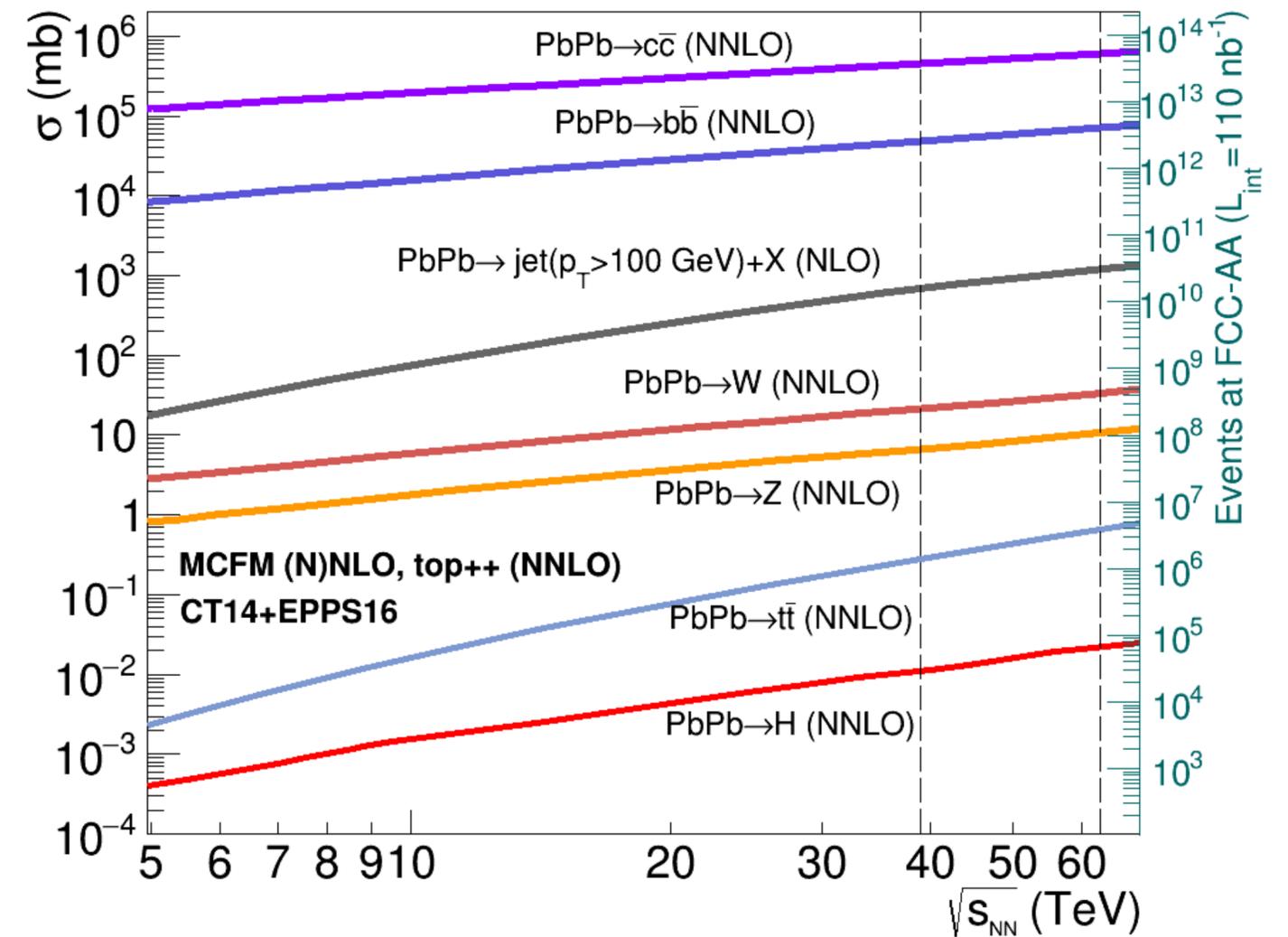
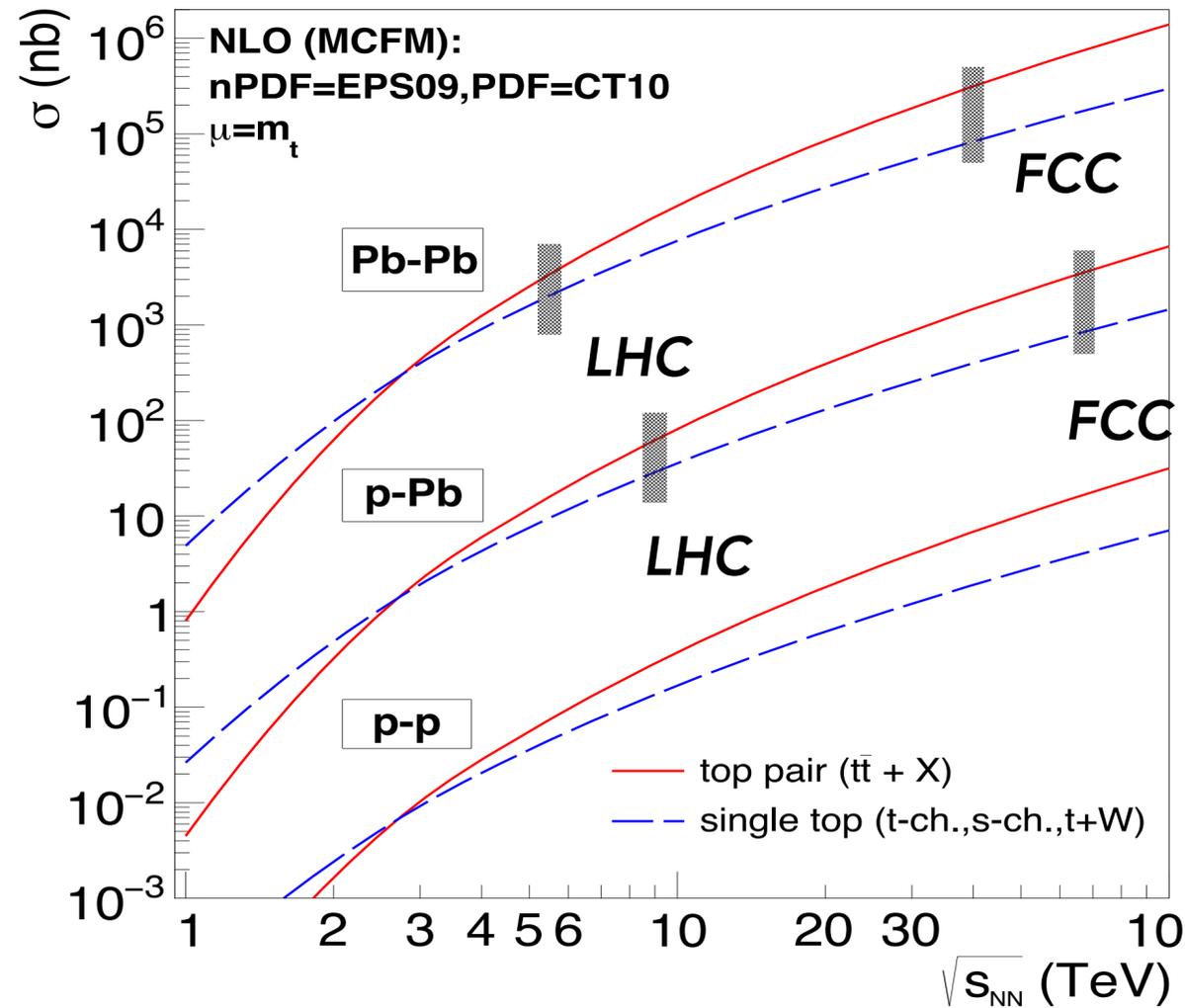
- ◆ Top cross section increases by x80 from 5.5 TeV to 39 TeV

- ◆ Boson-Jet cross-section increases by x20
- ◆ Bottom cross-section increases by x6



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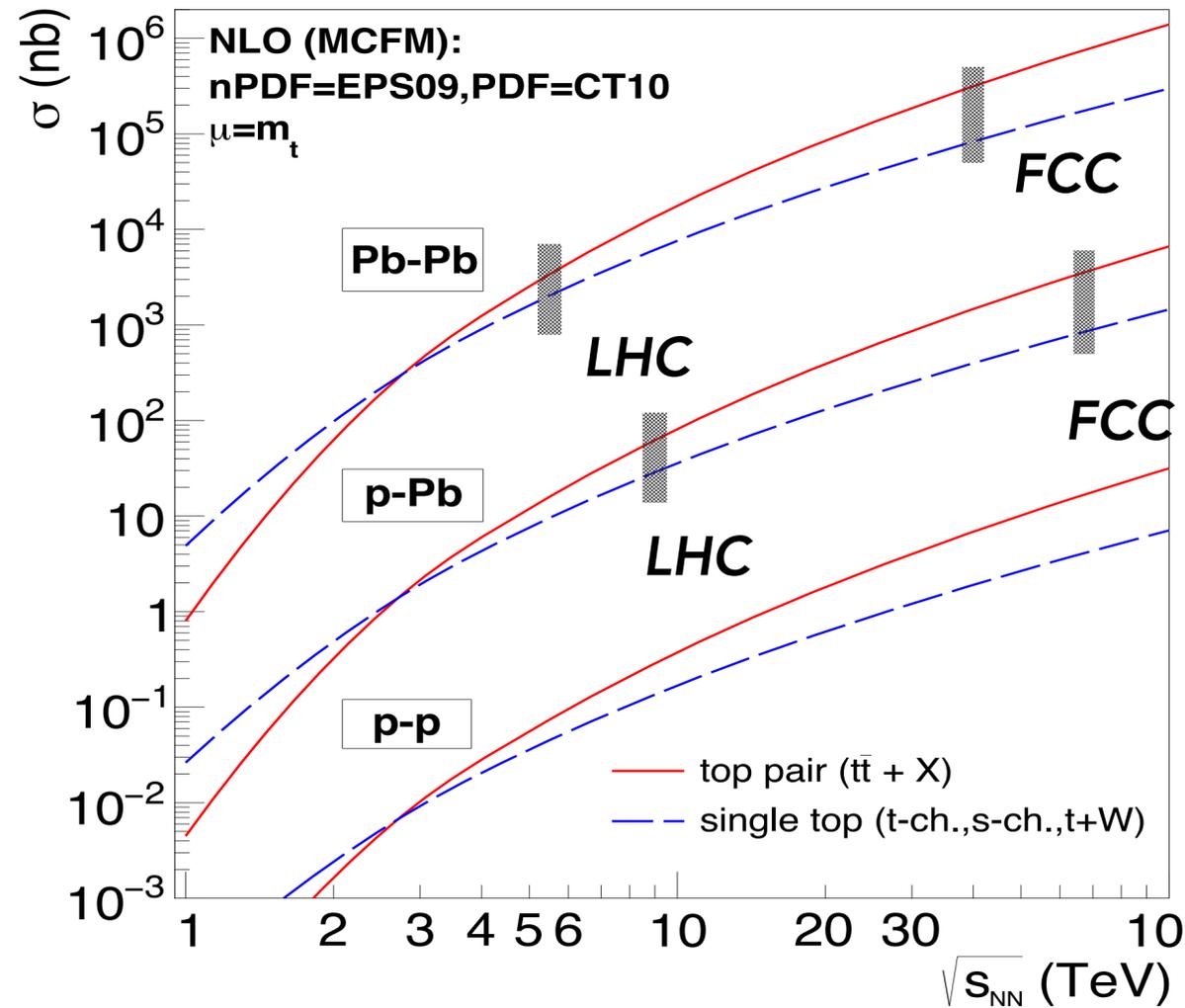
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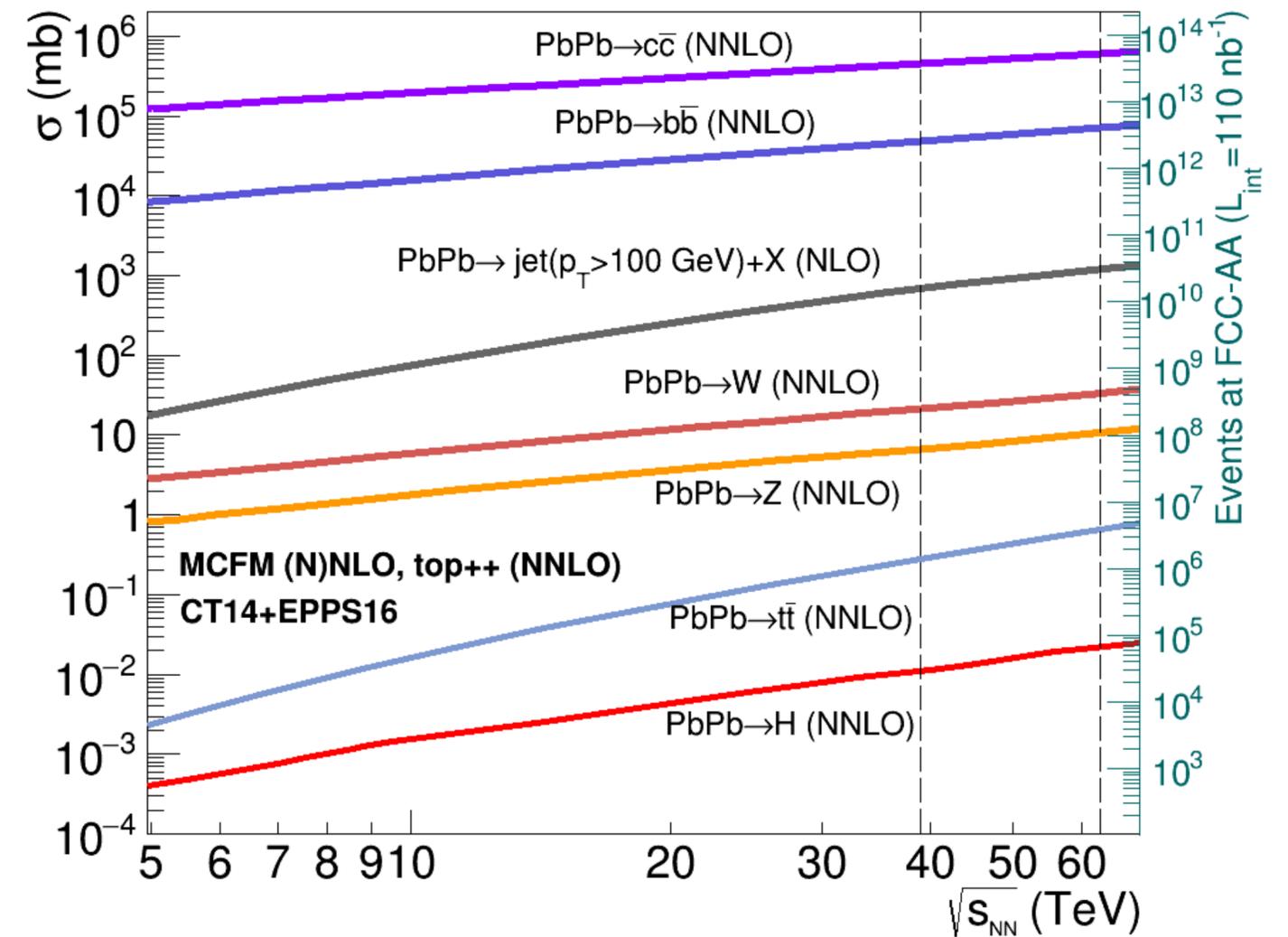
✓ Accurate Jet quenching studies

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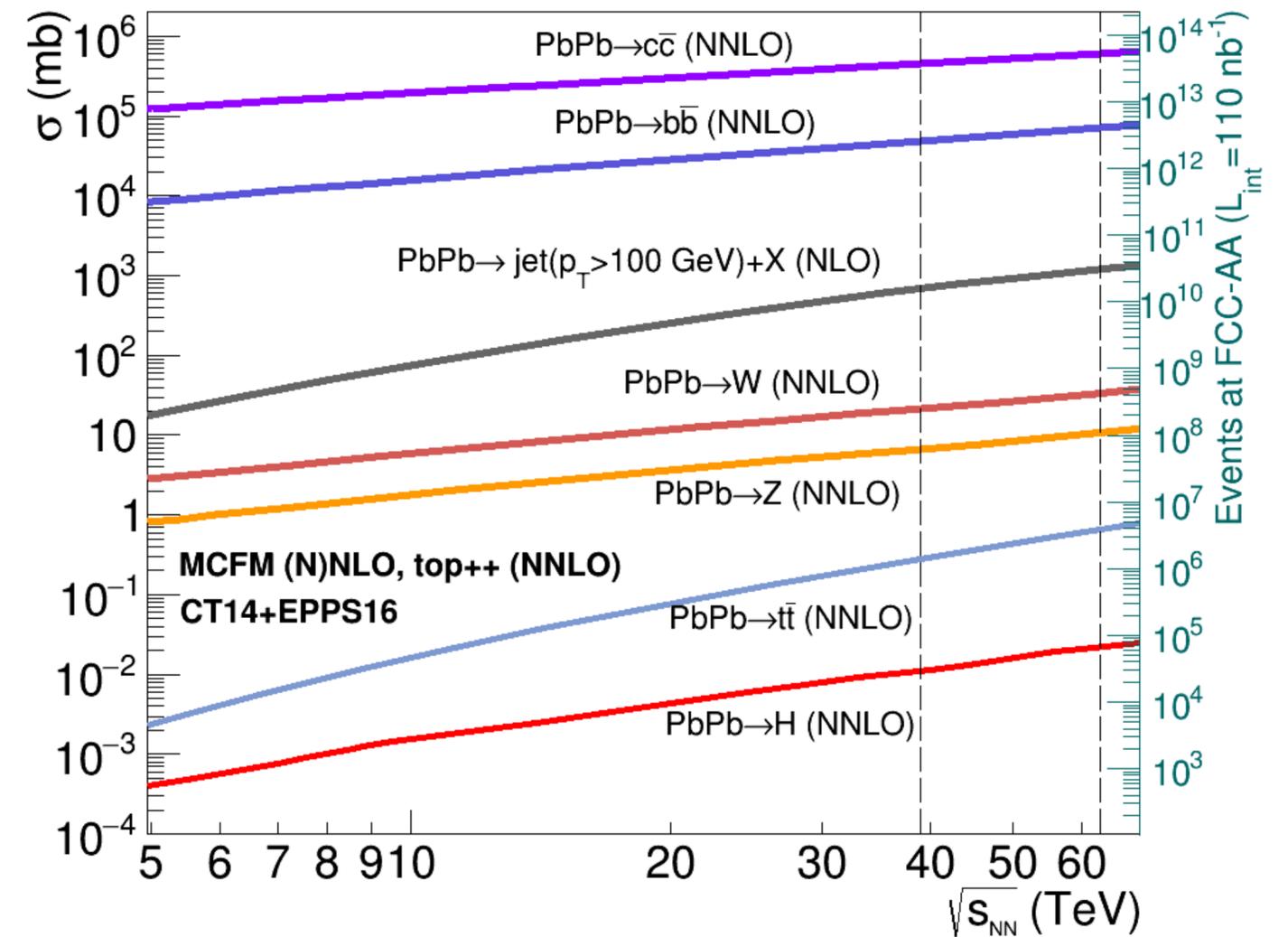
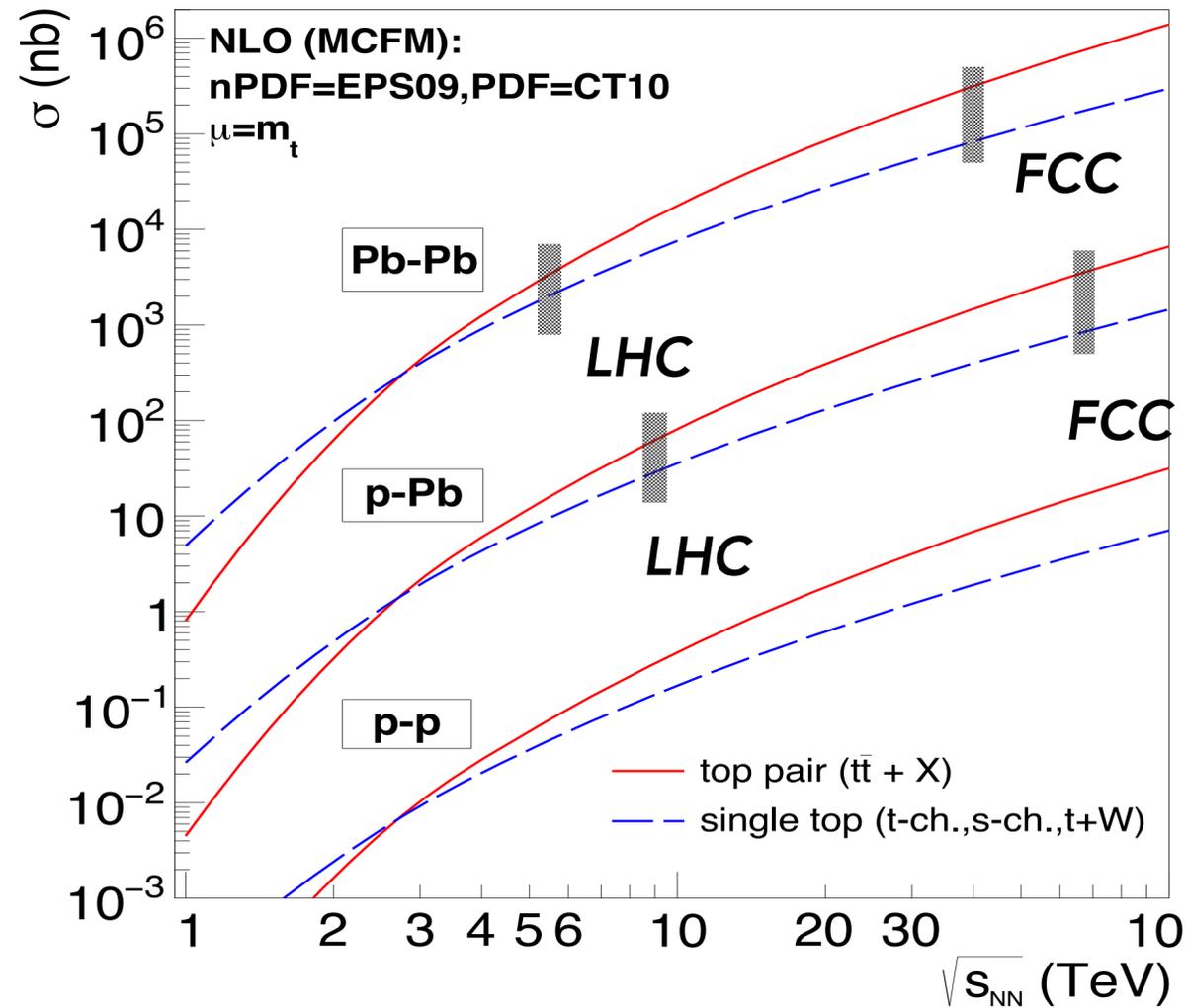
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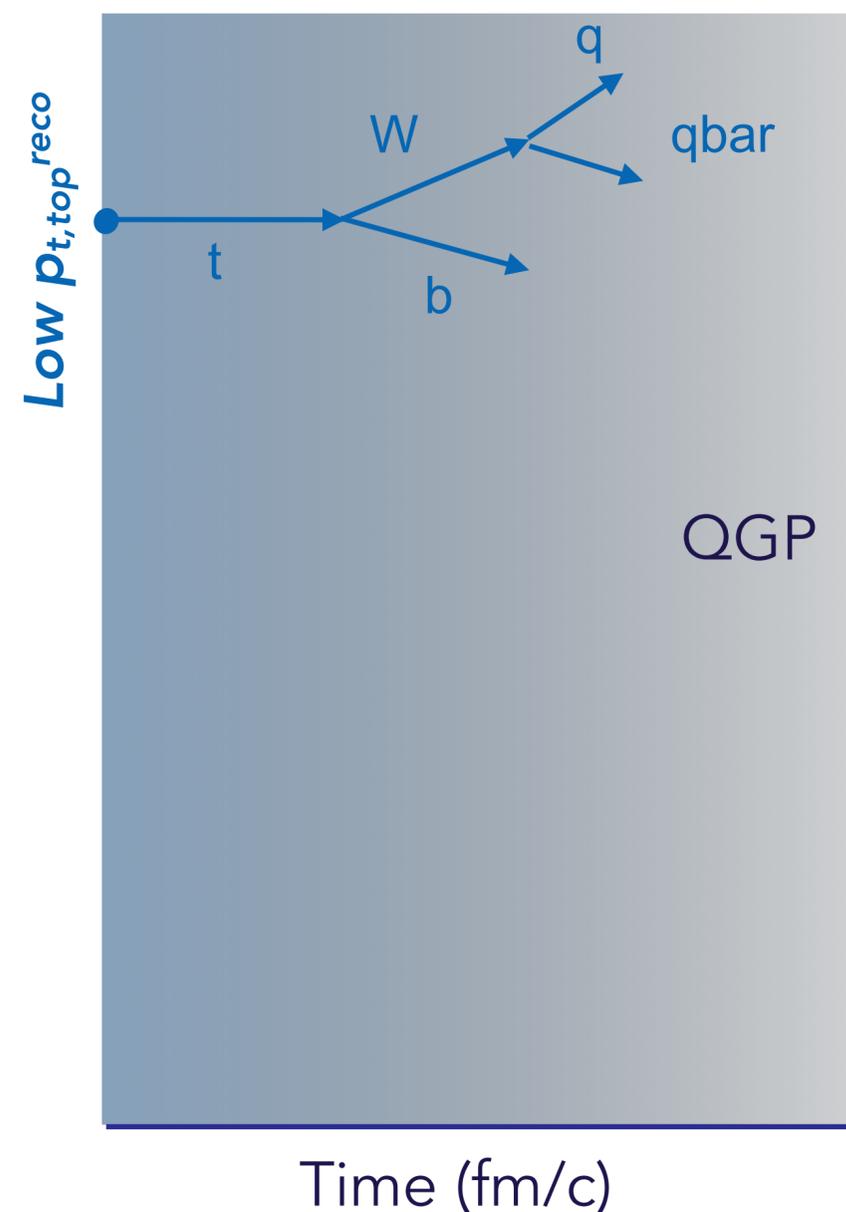
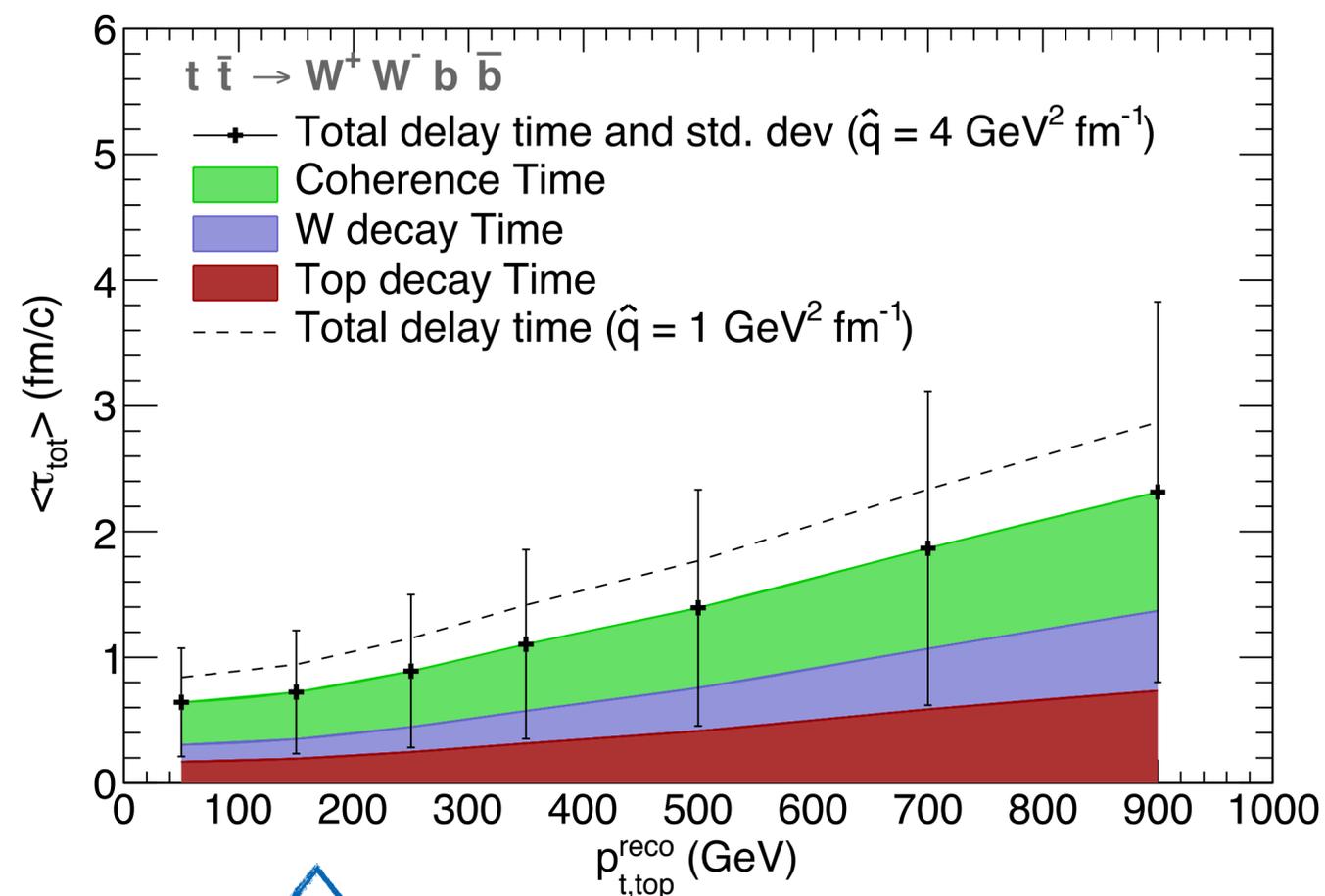
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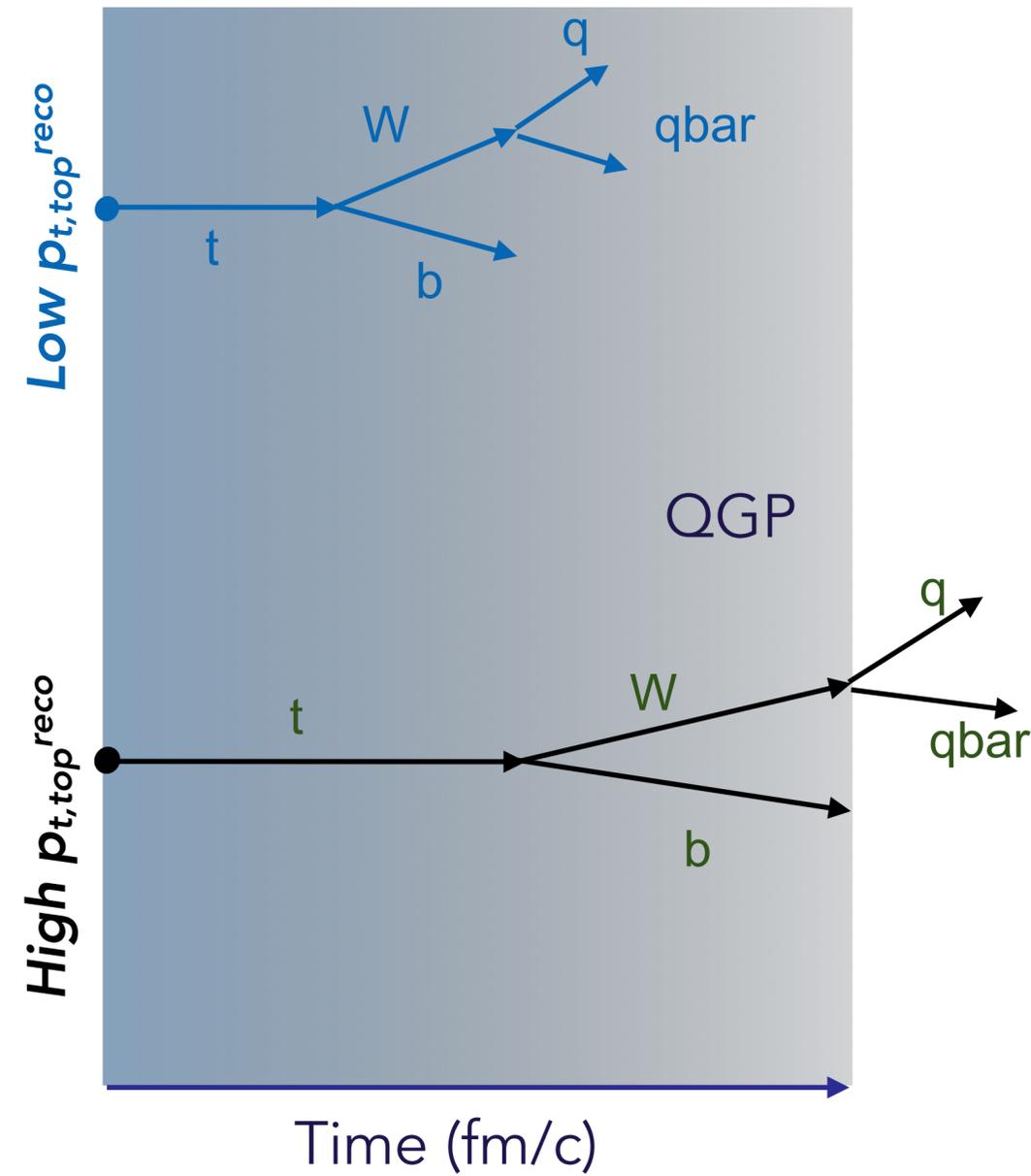
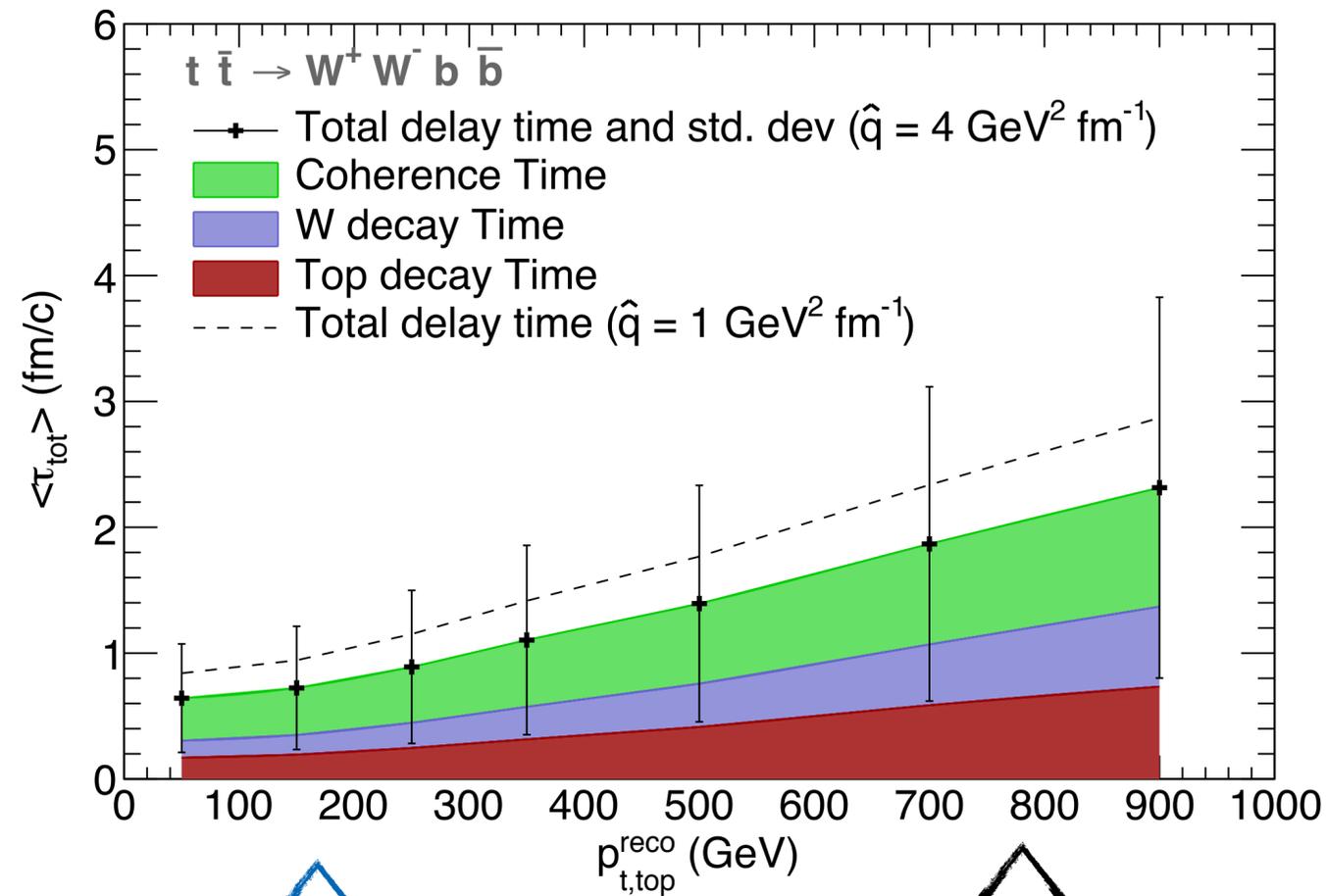
✓ Boosted objects ← *What can we do with these?*

✓ Accurate Jet quenching studies

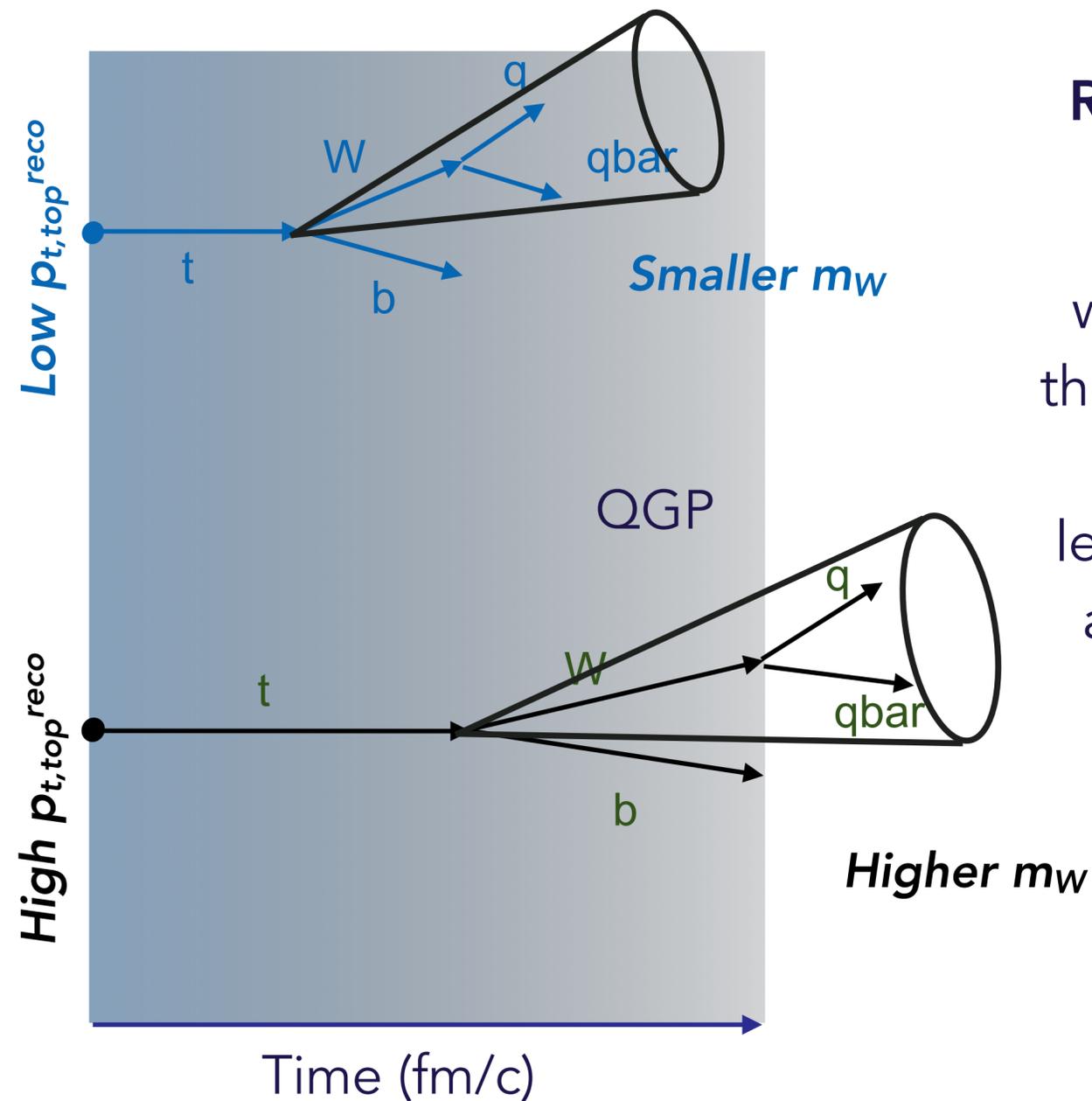
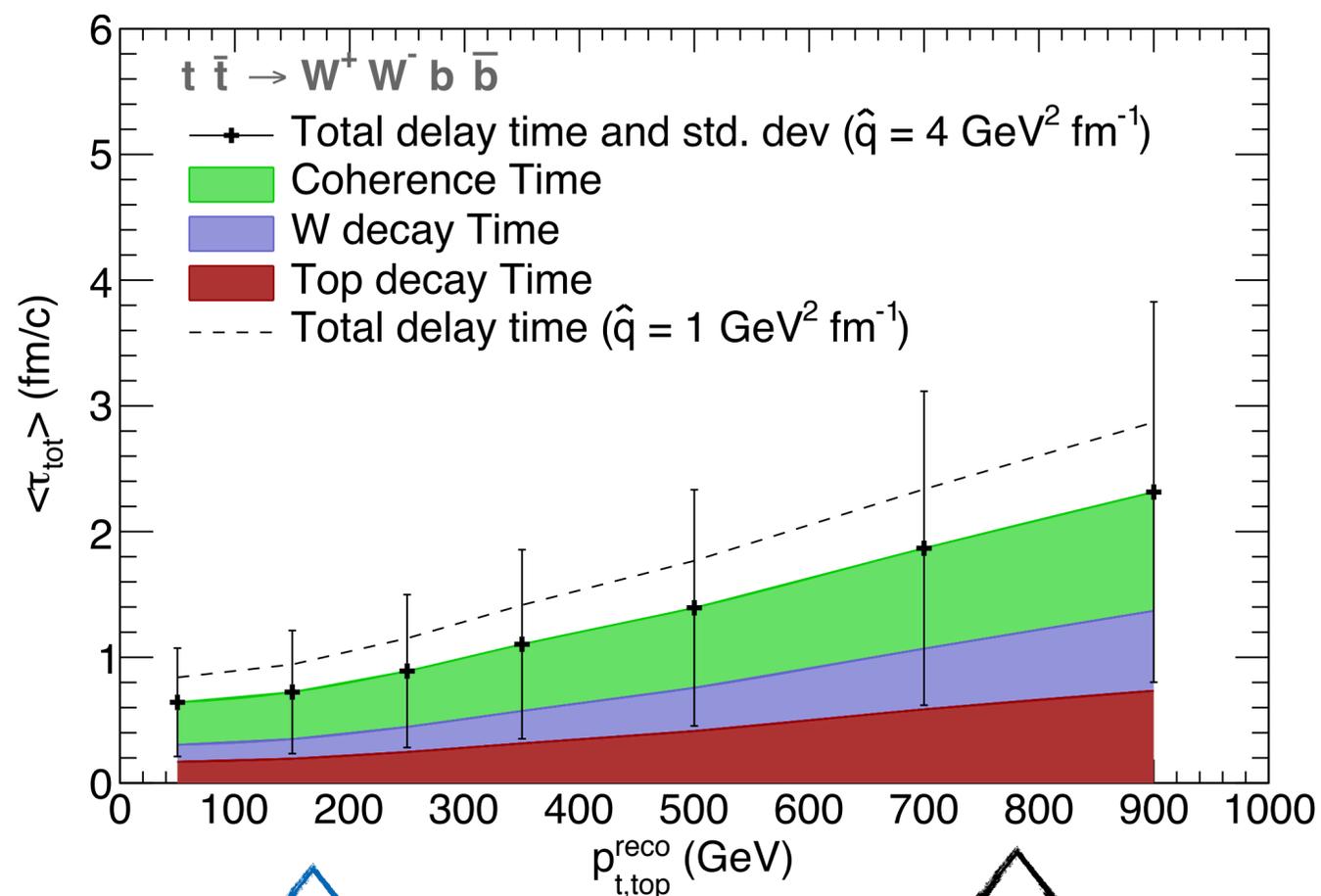
- ◆ Semi-leptonic decay of $t\bar{t}$ events produce jets that start interacting with the QGP only at later times



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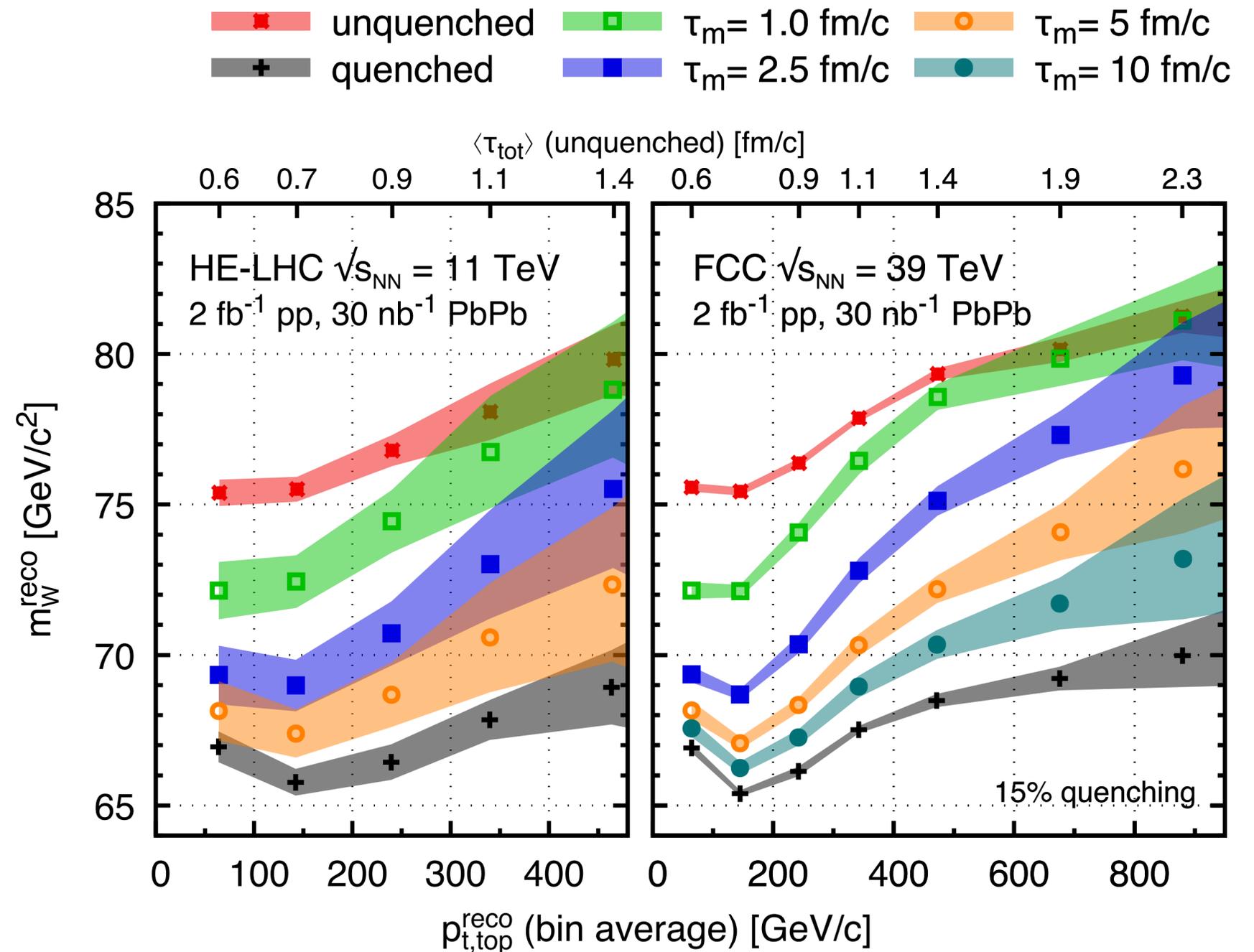
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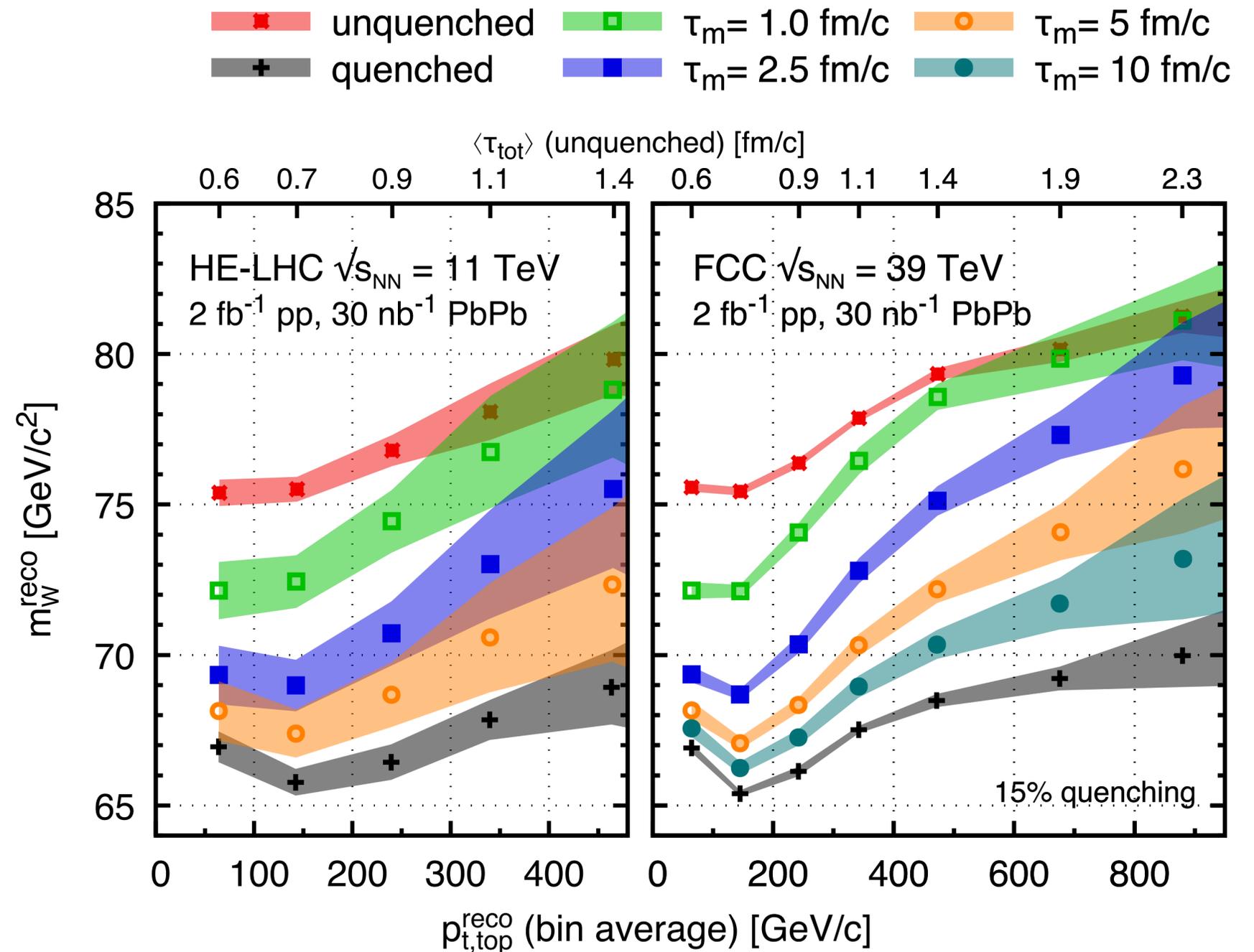
**Reconstructed
W mass: m_W**

will depend on
the energy that is
lost (medium
length that jet is
able to "see")

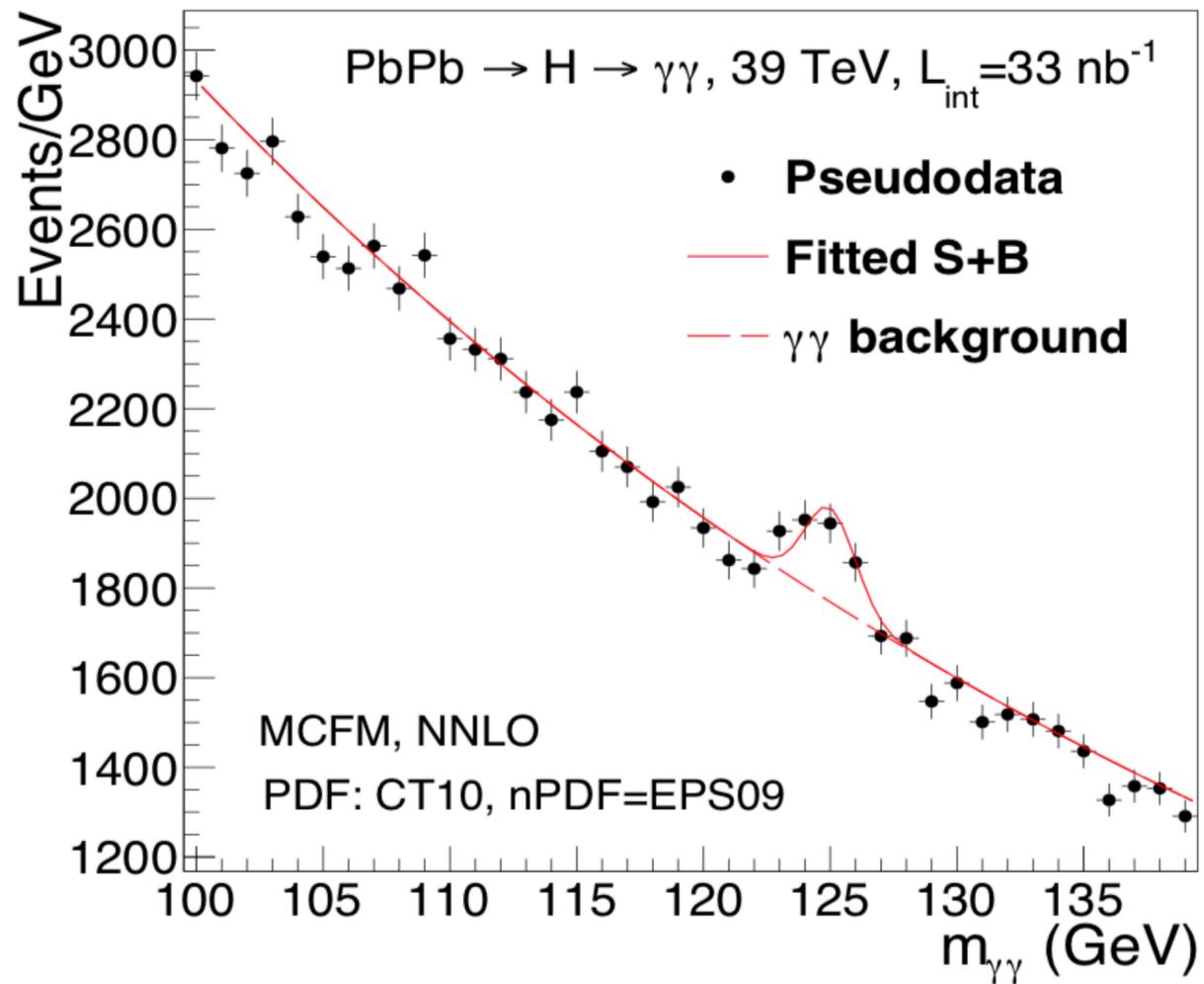
- ◆ Reconstructed W Mass as a function of the top p_T :
- ◆ Useful probe of the QGP density evolution



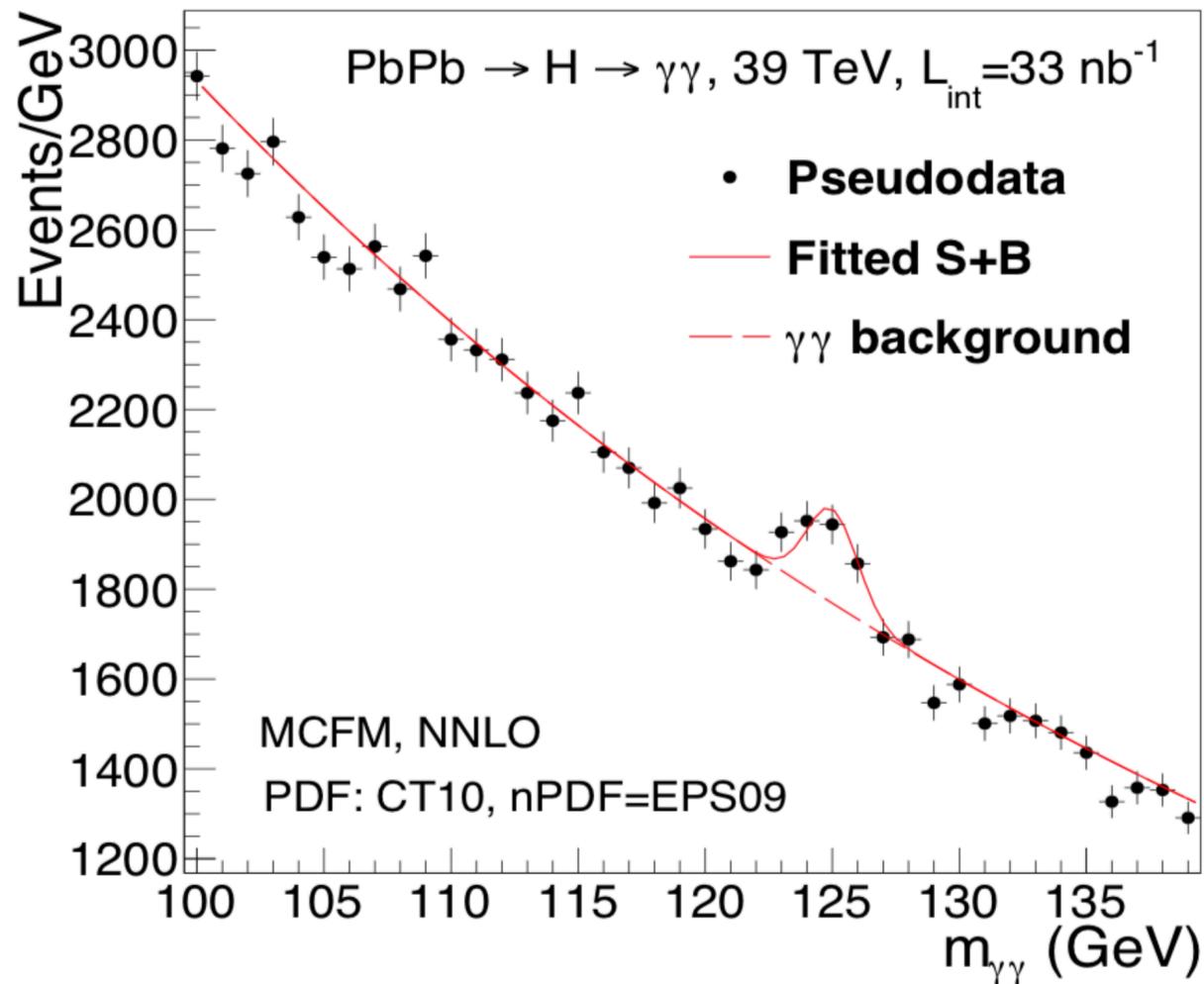
- ◆ Reconstructed W Mass as a function of the top p_T :
- ◆ Useful probe of the QGP density evolution
- ◆ QGP tomography:
 - ◆ HE-LHC: Some discrimination between short vs long lived medium
 - ✓ FCC: able to scan entire QGP lifetime!



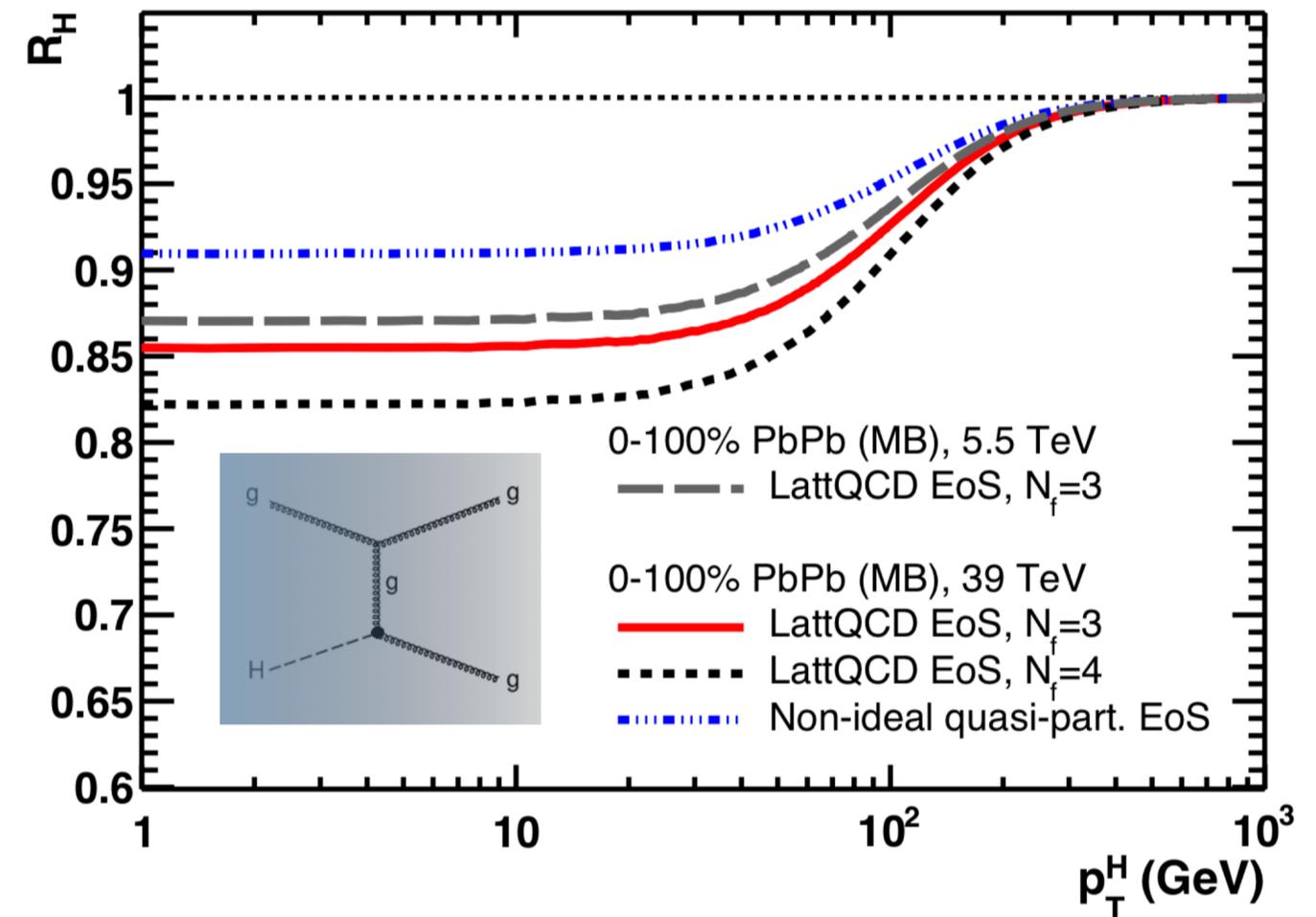
- ◆ Possible to measure $Higgs \rightarrow \gamma\gamma$ with 5.5σ in one Pb-Pb month with baseline L_{int}



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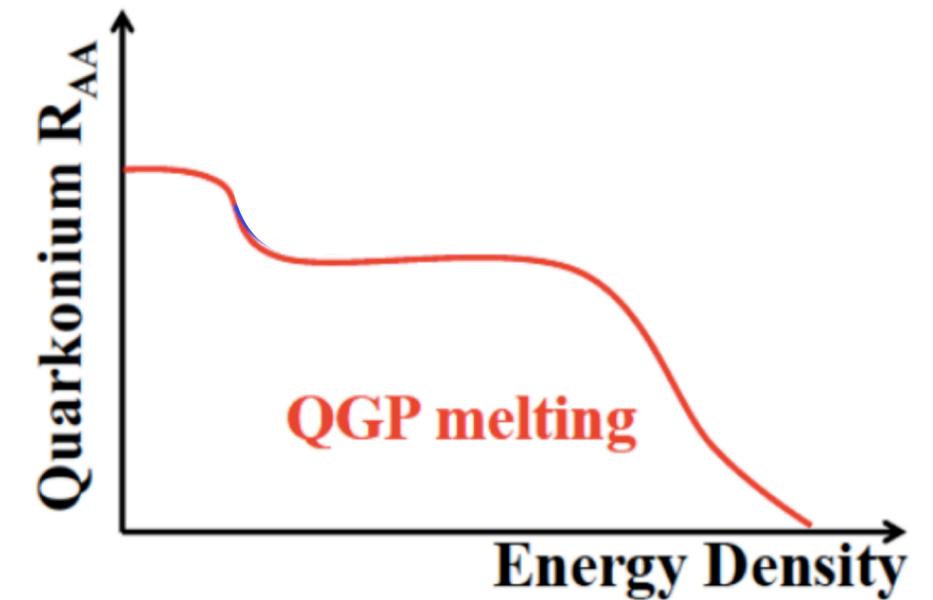
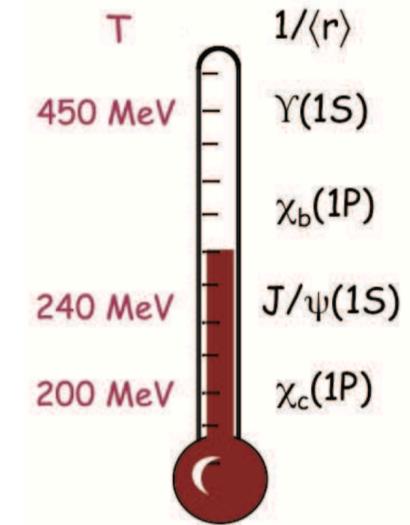
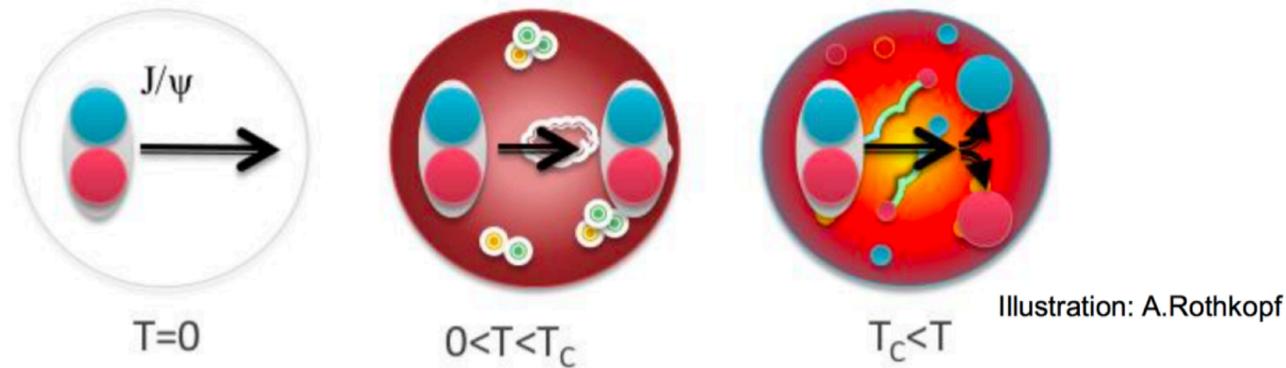


- ◆ Interaction with QGP will induce a decay to gg (reducing other boson decays) \Rightarrow Suppression of the Higgs yield

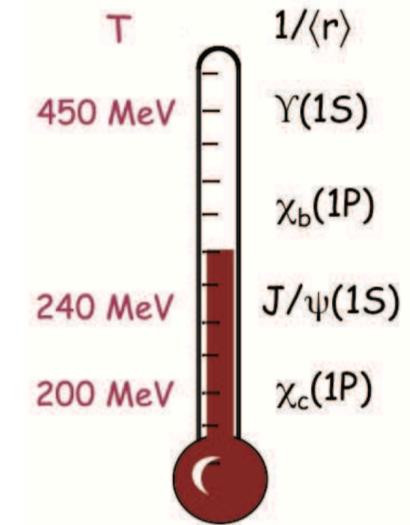
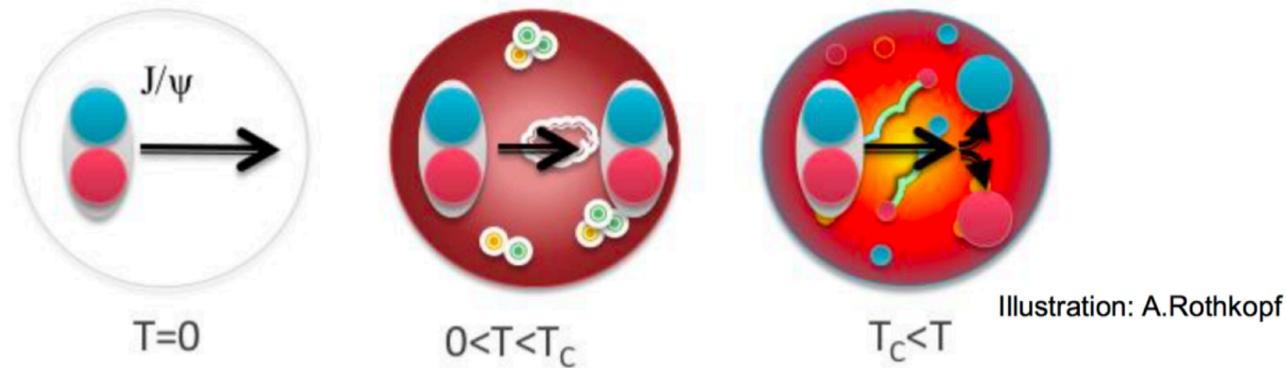


FCC: Higgs Suppression depends on EoS (but virtual corrections lead to a null impact in the Higgs hadronic width)

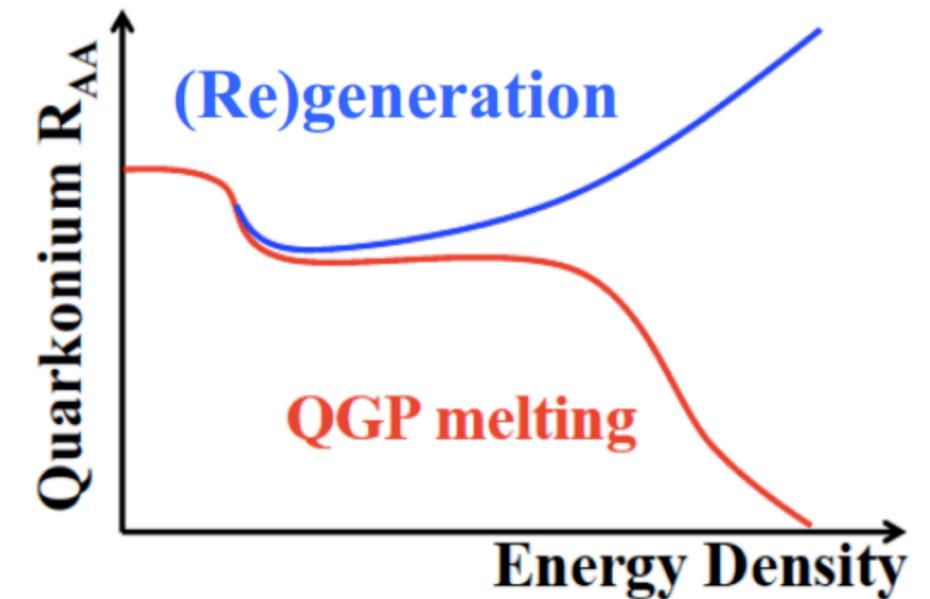
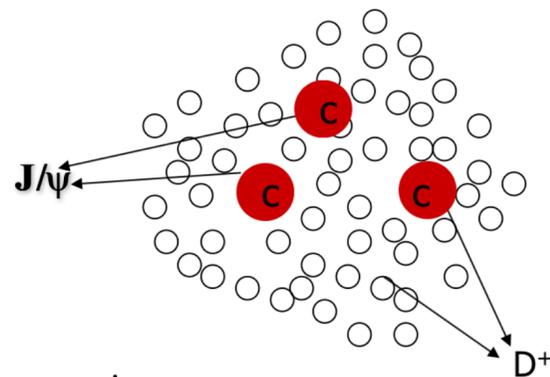
- ◆ Quarkonia production in the presence of a medium:
 - ◆ Sequential melting can be used as a thermometer of the QGP!



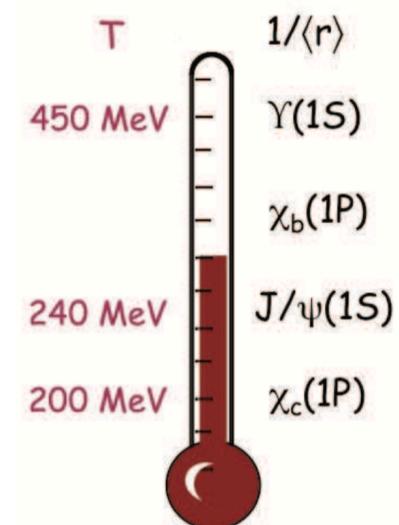
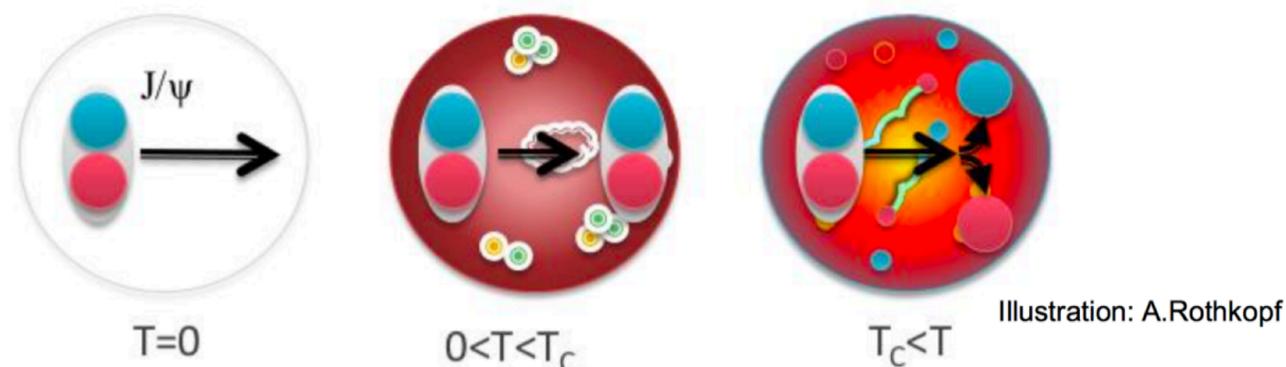
- ◆ Quarkonia production in the presence of a medium:
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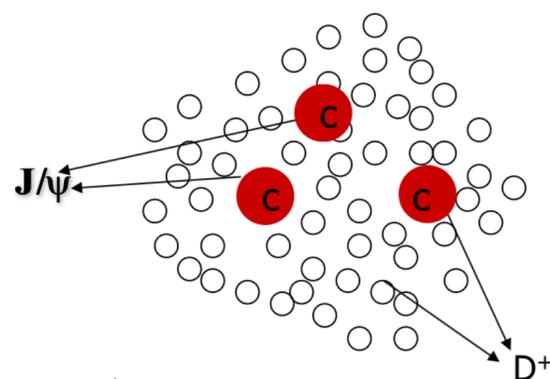
- ◆ Final yield is a competition between QGP melting and regeneration with QGP thermal quarks



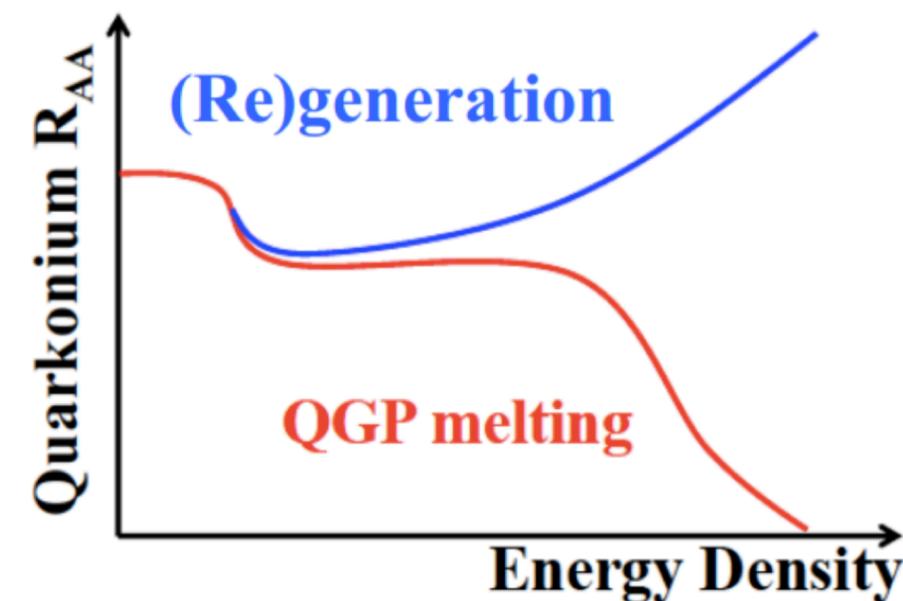
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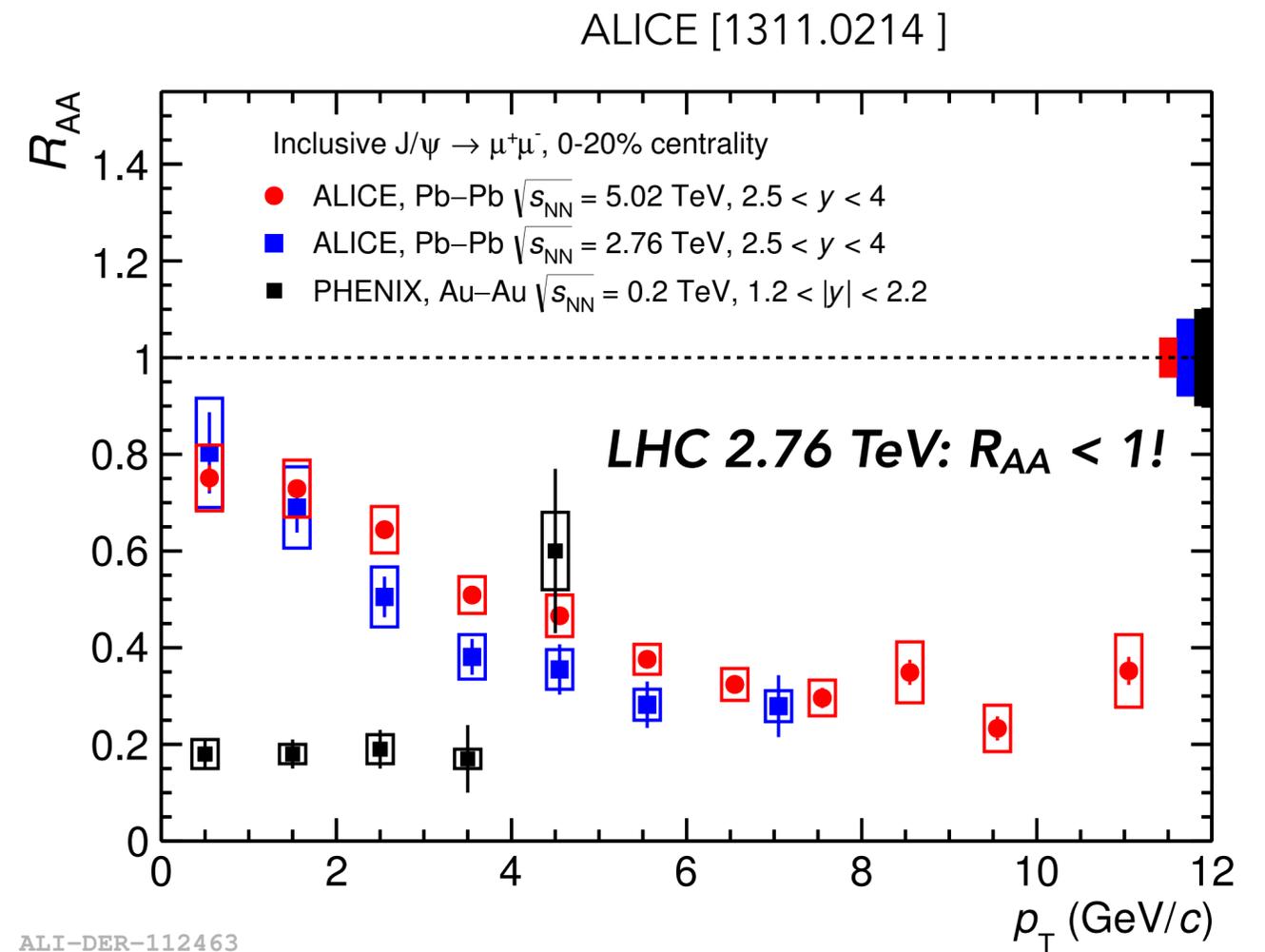
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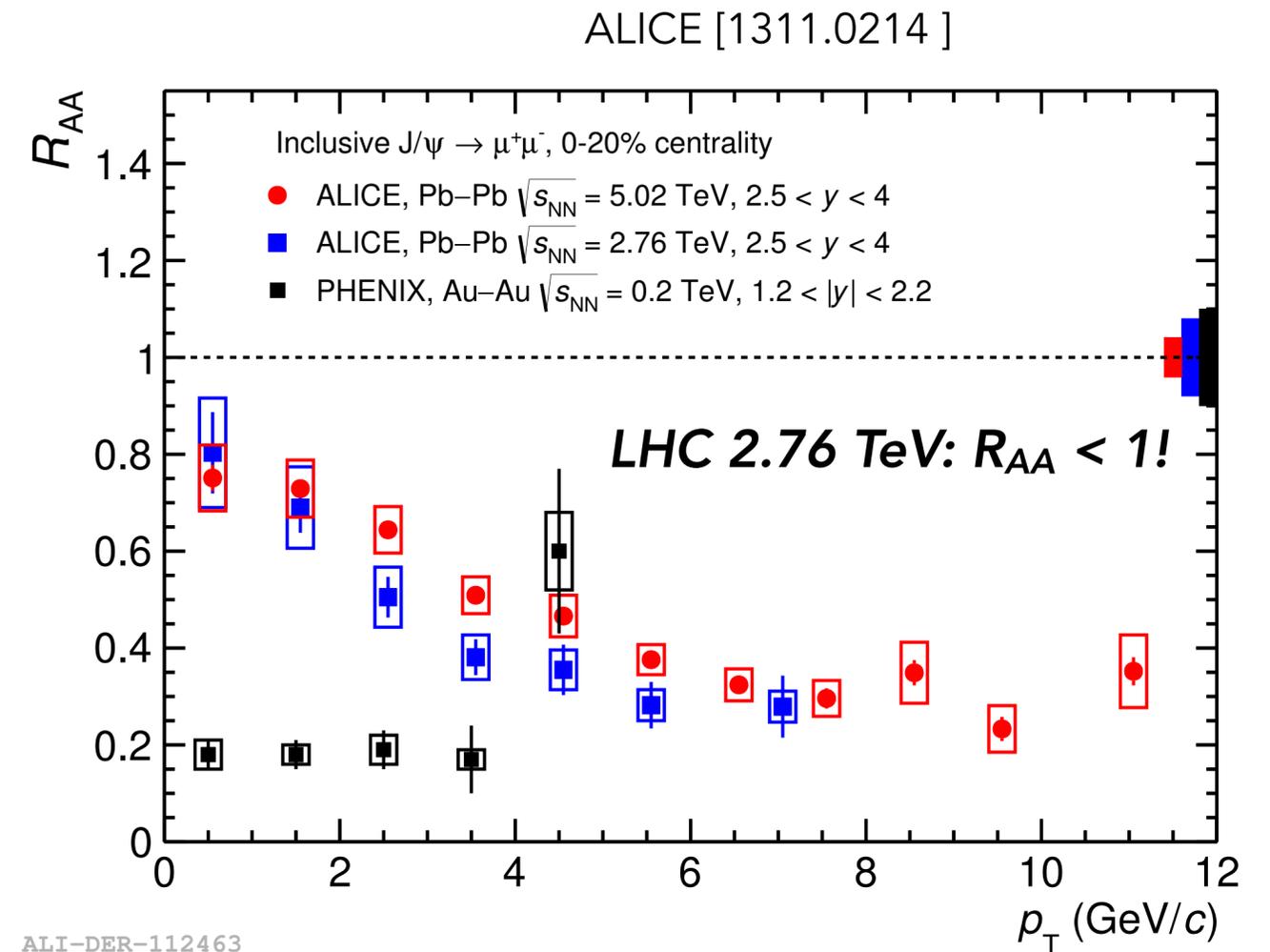
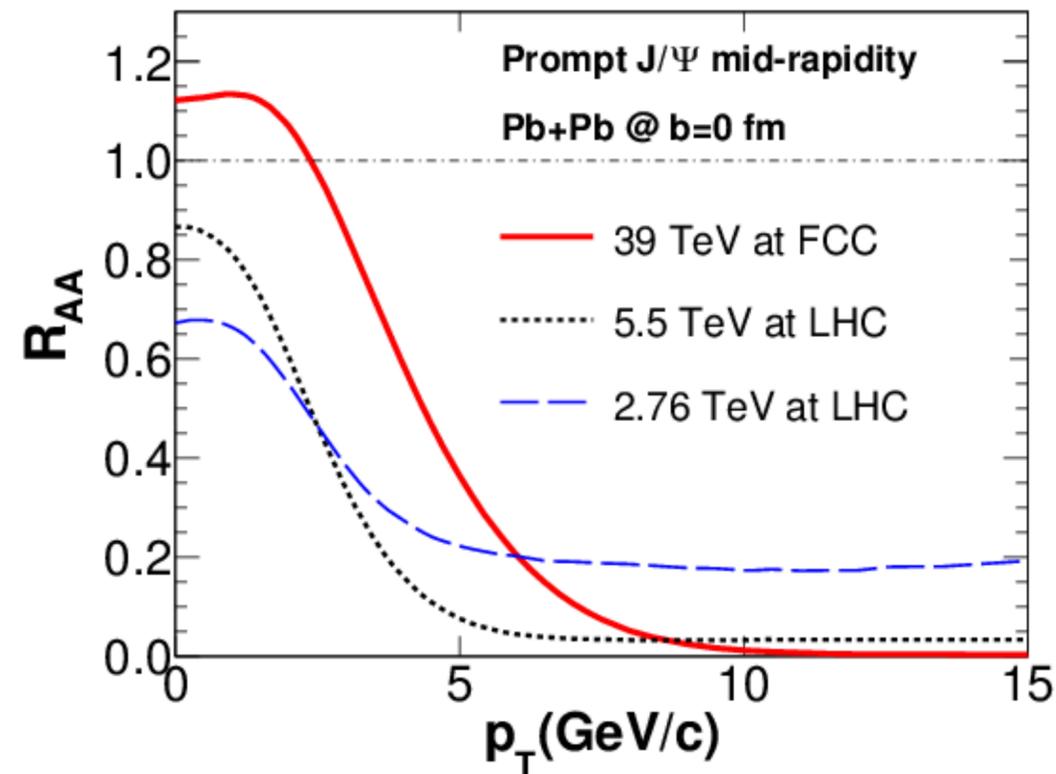
Expected changes at the FCC?



- ◆ J/ψ regeneration depends
- ◆ QGP thermal cc production
- ◆ Larger hard cross-section

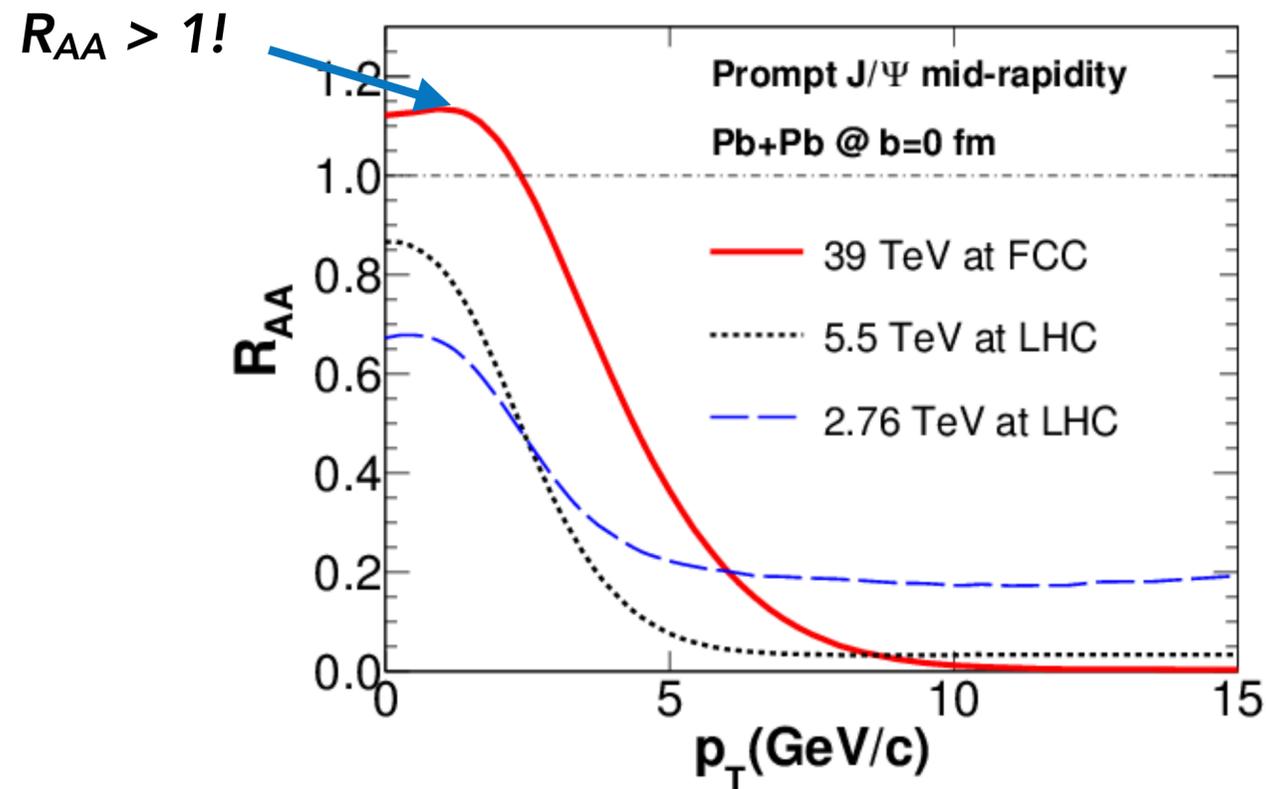


- ♦ J/ψ regeneration depends **FCC**
- ♦ QGP thermal cc production **x1.5 w.r.t LHC**
- ♦ Larger hard cross-section **x2-2.5 w.r.t LHC**



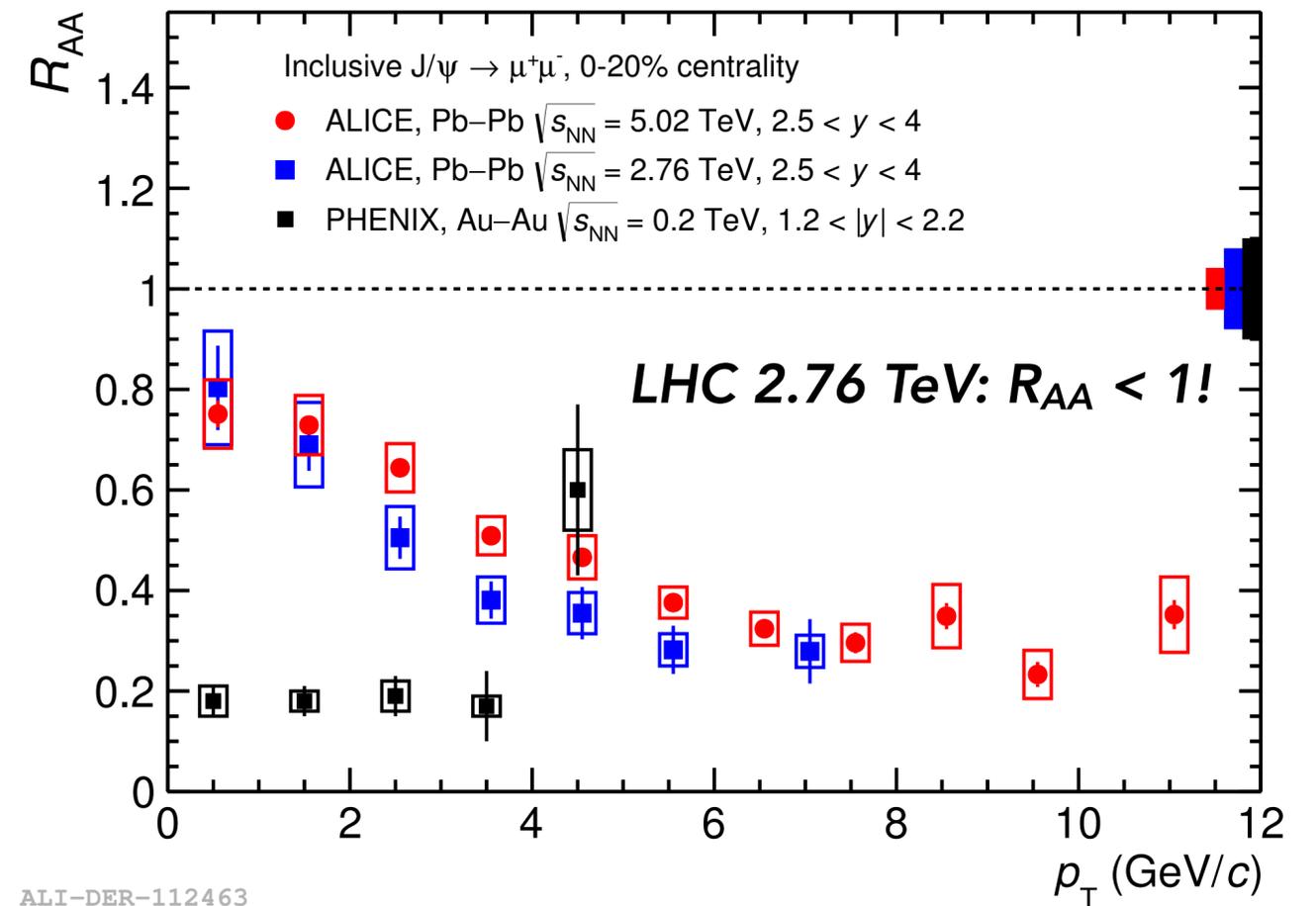
ALI-DER-112463

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✓ FCC: Striking evidence of cc recombination

ALICE [1311.0214]

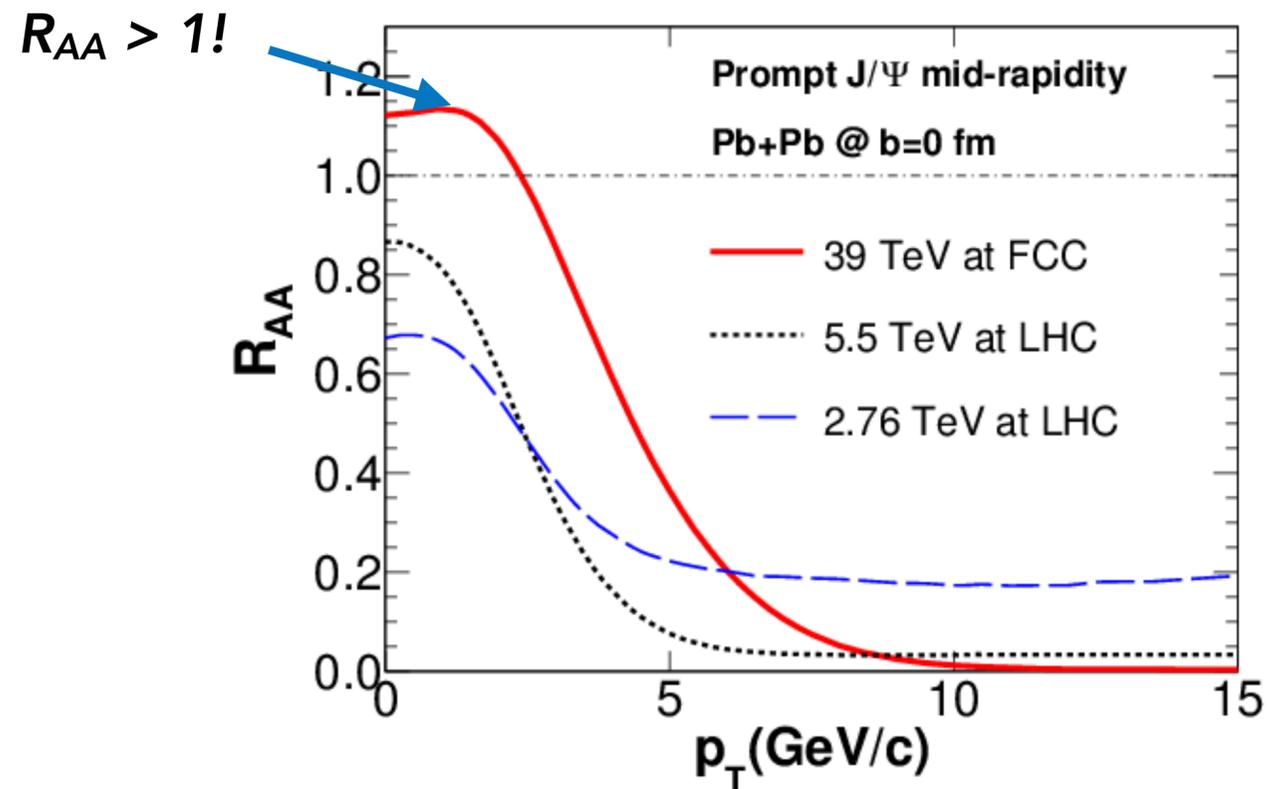


ALI-DER-112463

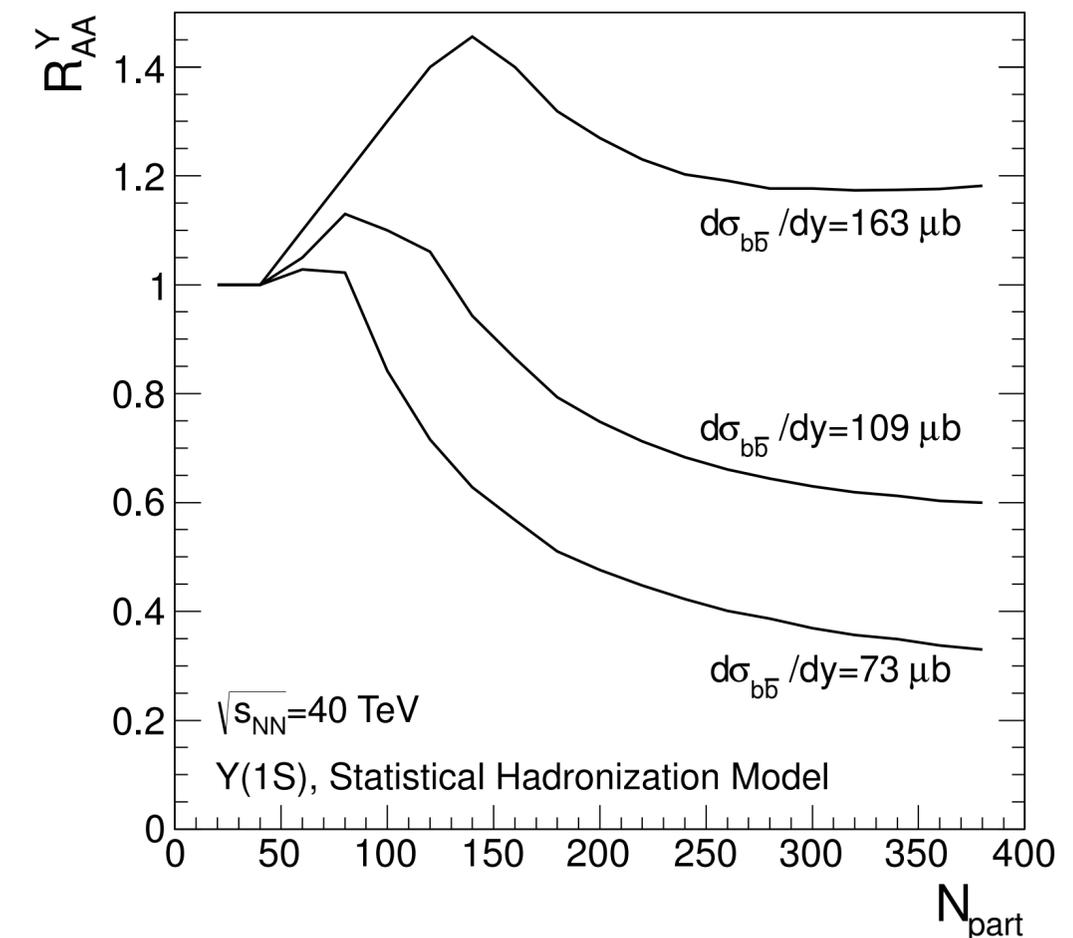
Liu et al (09), Zhao et al (11), Andronic et al, 11

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- ◆ $\Upsilon(2S)$ $\Upsilon(3S)$: partial/total suppression at LHC
- ◆ $\Upsilon(1S)$: interplay between regeneration and melting provide a range of possibilities



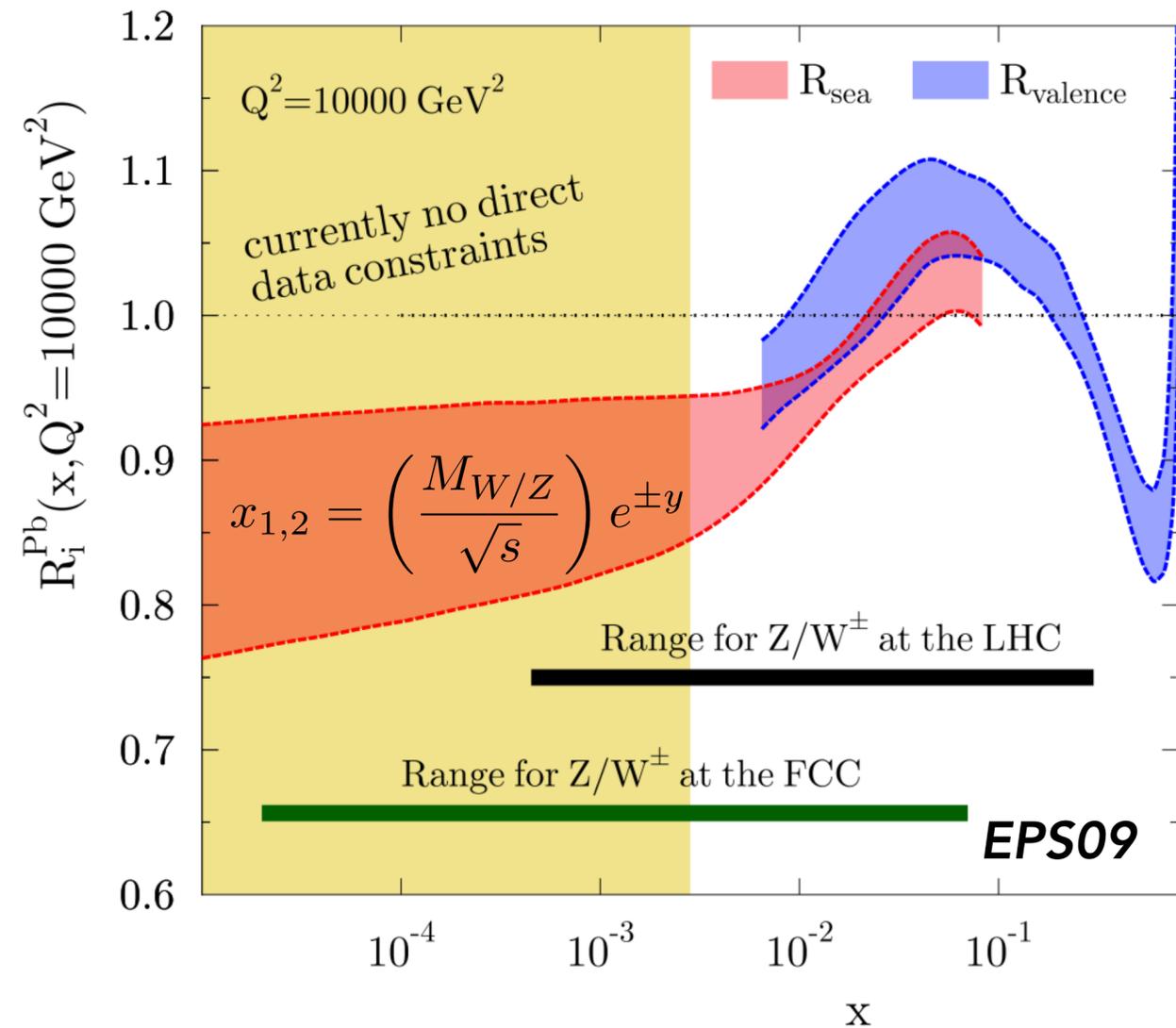
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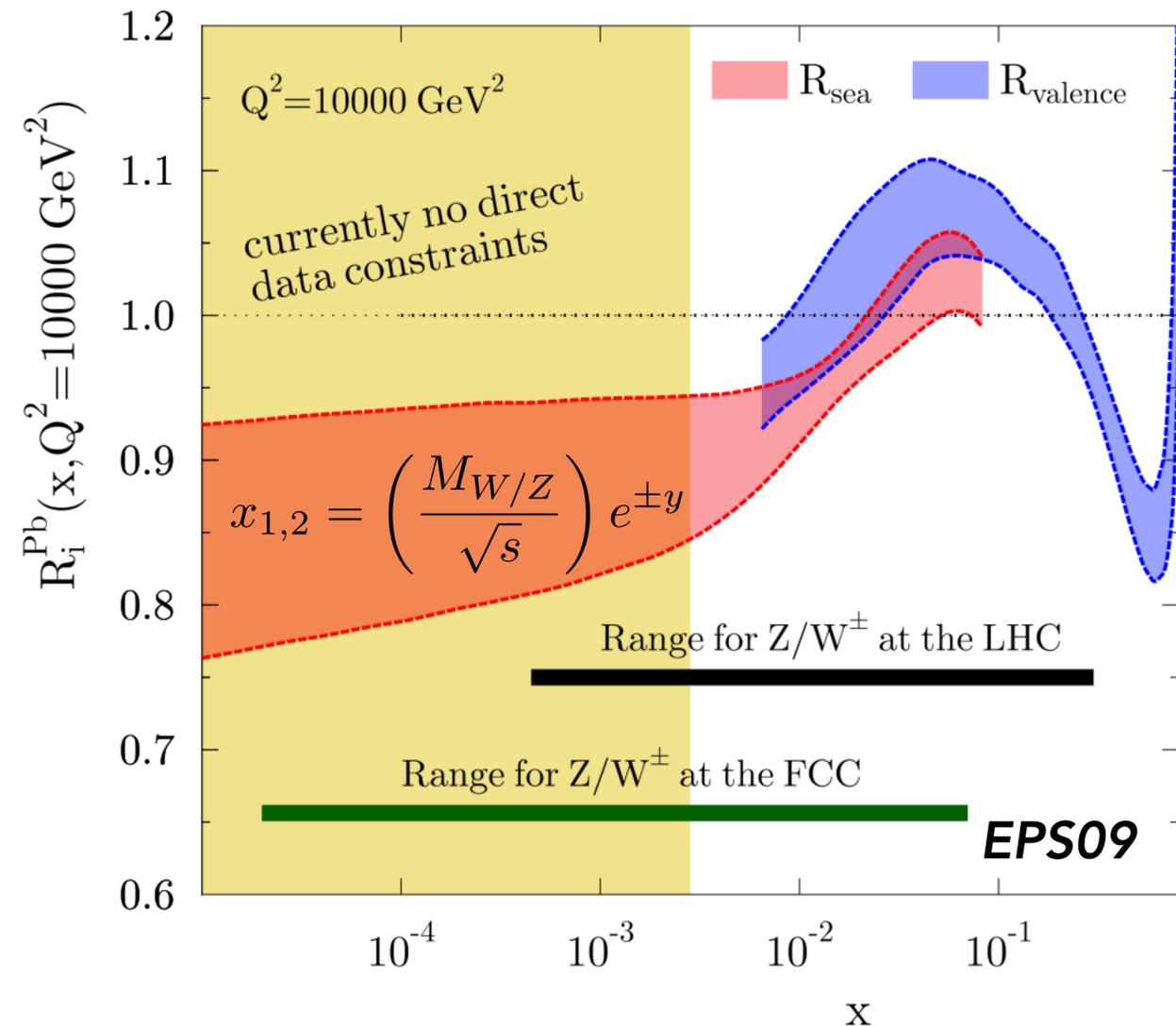


Initial State

- ♦ Extraction of QGP properties highly dependent on initial conditions
- ♦ Need a precise determination of nuclear PDFs!



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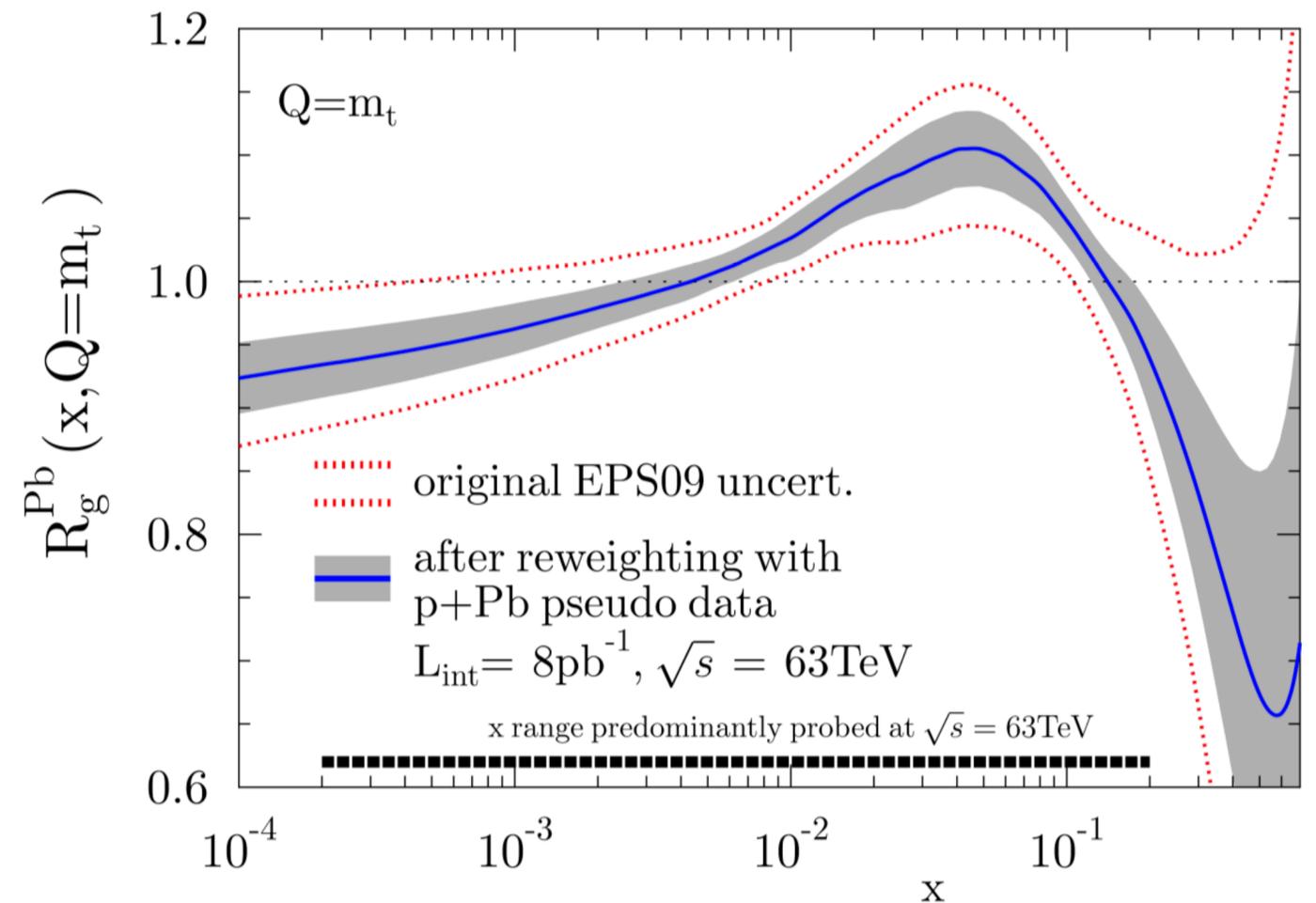
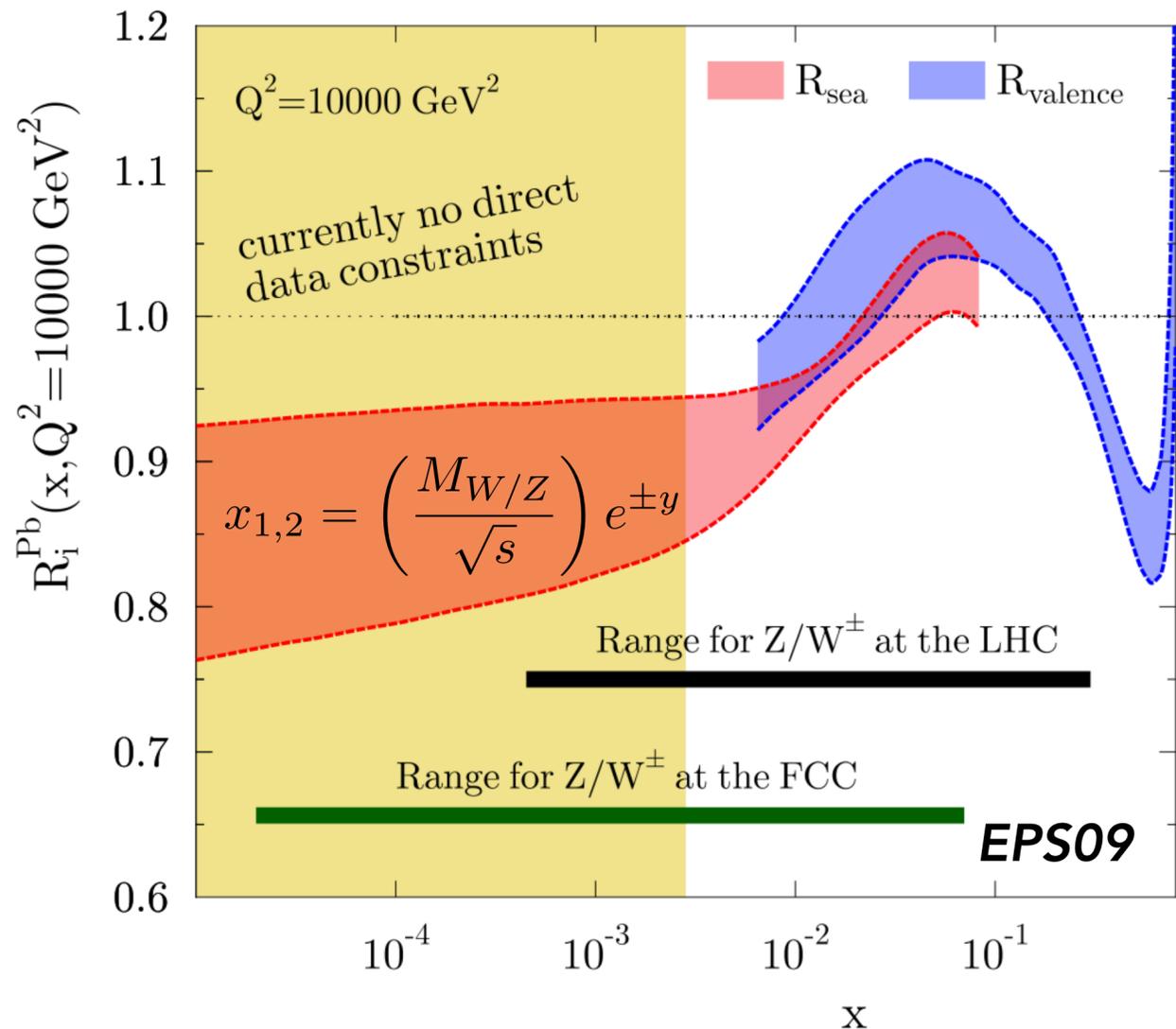


✓ FCC: Small-x reach 10x larger than LHC with bosons

♦ Extraction of QGP properties highly dependent on initial conditions

♦ Need a precise determination of nuclear PDFs!

✓ FCC: As in pp, top quarks can be used to reduce nPDF uncertainties (x2)



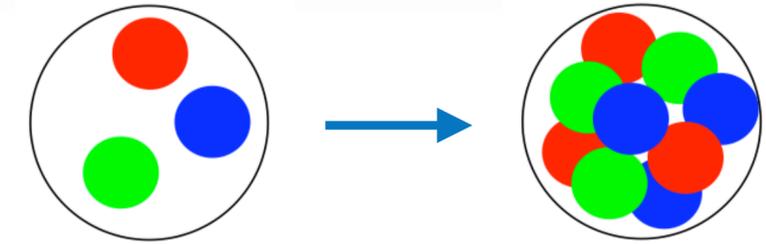
✓ FCC: Small-x reach 10x larger than LHC with bosons

- ◆ Non-linear phenomena to tame the growth of parton densities

- ◆ Onset of saturation:

Transverse area $\pi R_A^2 \sim \frac{Axg(x, Q_s^2)}{Q_s^2} \Rightarrow Q_s^2 \sim A^{1/3} (\sqrt{s_{NN}})^{0.3} e^{0.3y}$ Number of gluons

gluon size $\sim 1/Q_s^2$ **Increase \sqrt{s} , y and/or A**



- ◆ Collinear factorization: non-linear effects absorbed by nuclear PDFs

$$d\sigma_{(\text{med})}^{AA \rightarrow h + \text{rest}} = \sum_{ijk} f_{i/A}(x_1, Q^2) \otimes f_{j/A}(x_2, Q^2) \otimes \hat{\sigma}_{ij \rightarrow f+k} \otimes D_{f \rightarrow h}^{(\text{med})}(z, \mu_F^2).$$

Expected to break if gluon phase space becomes saturated

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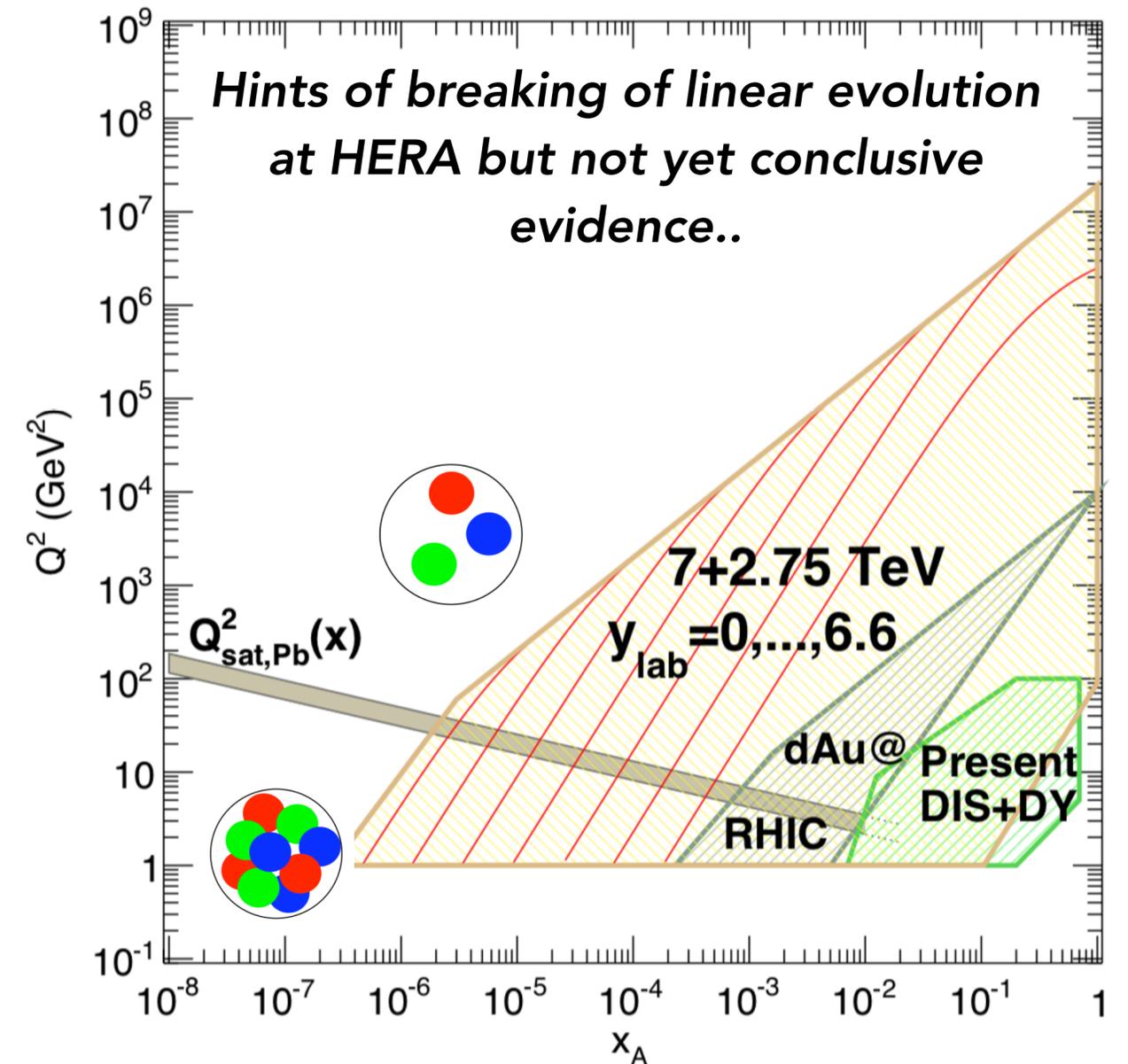
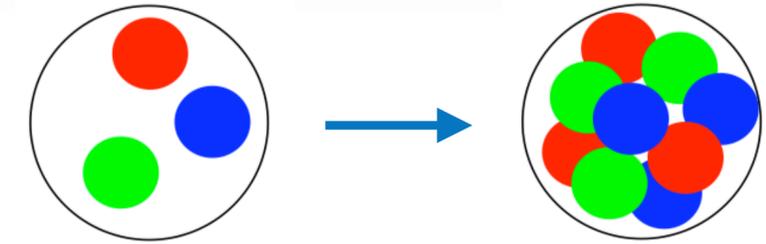
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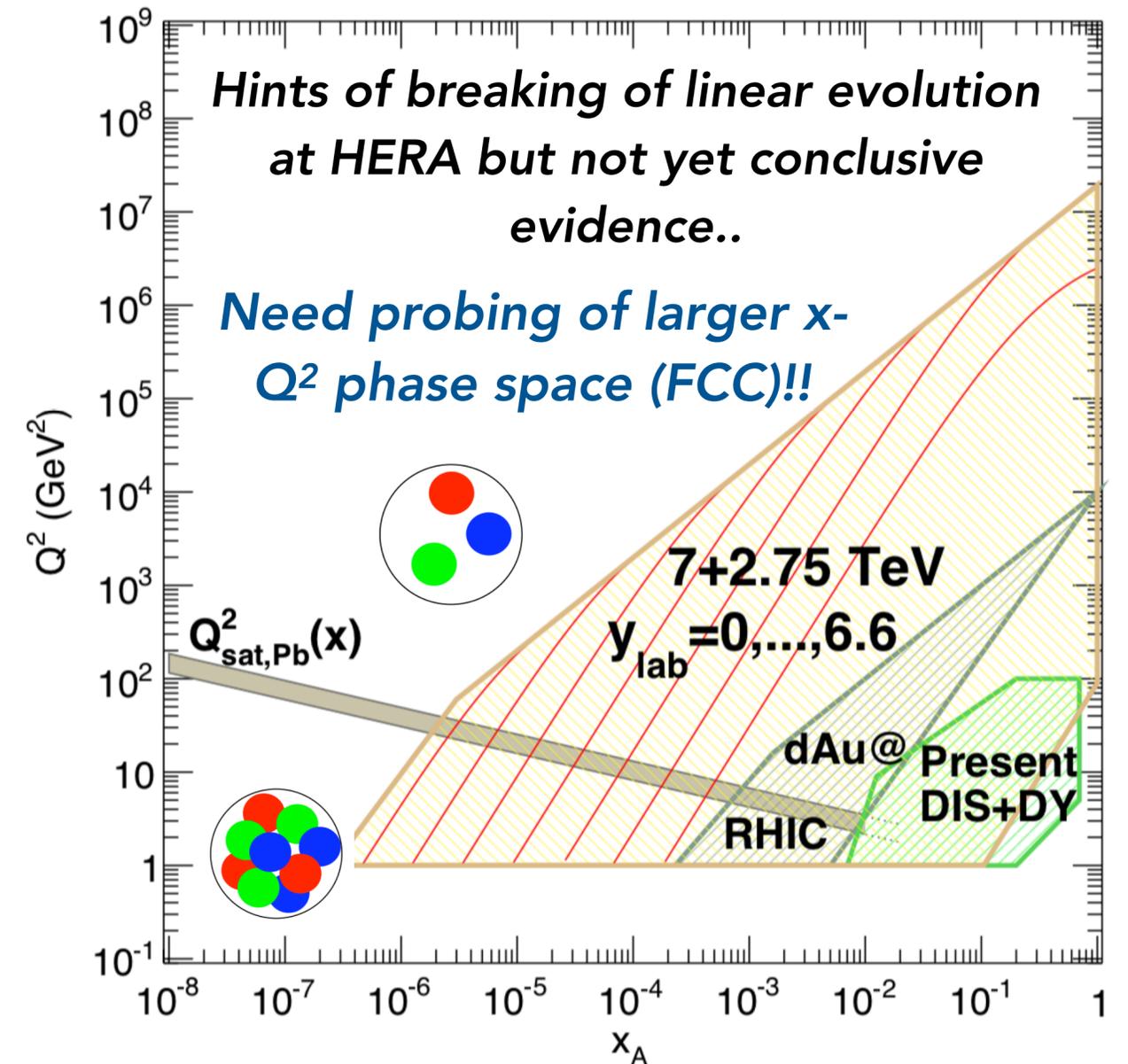
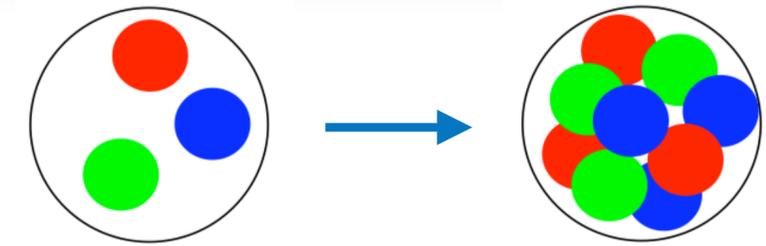
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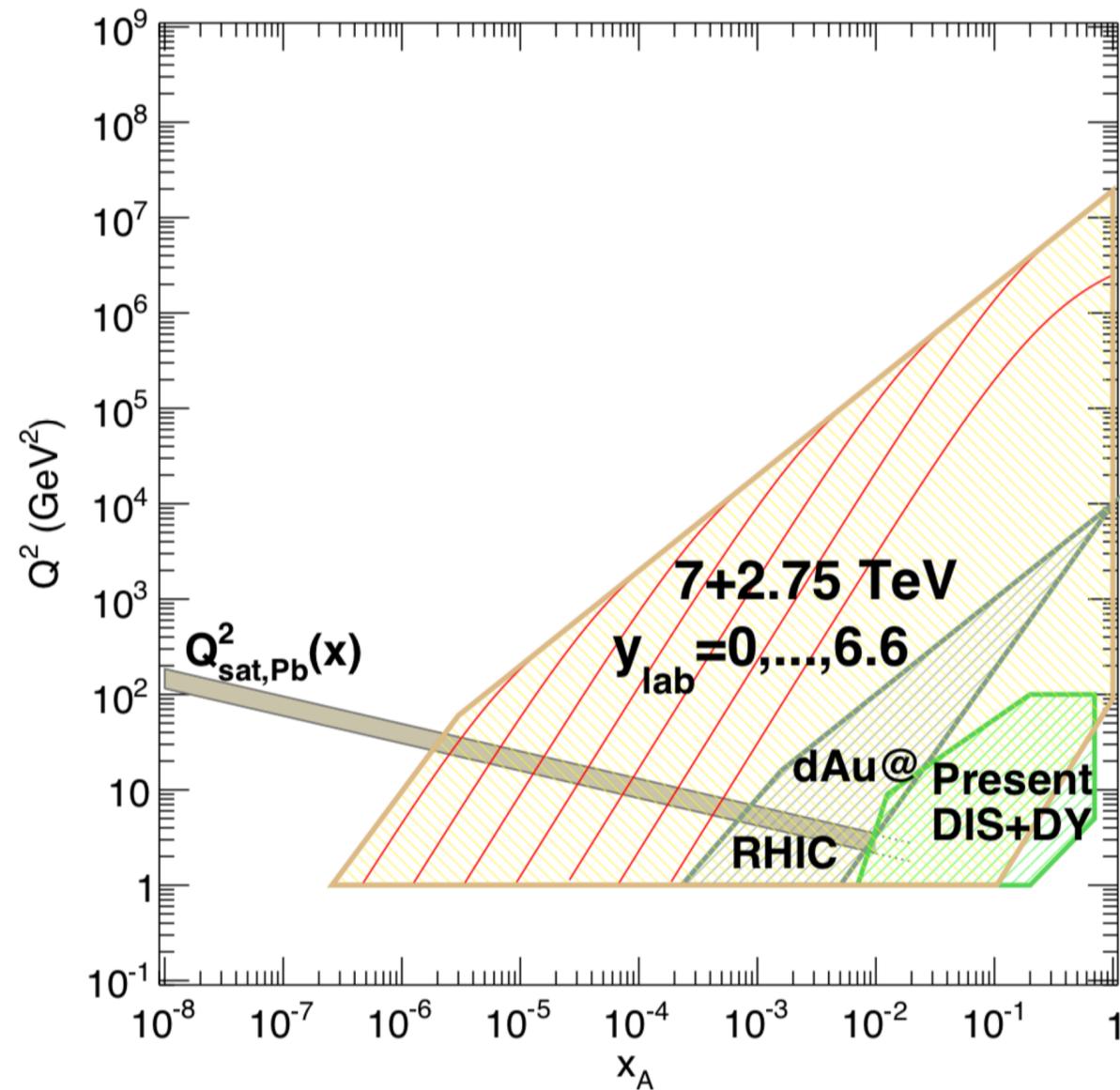
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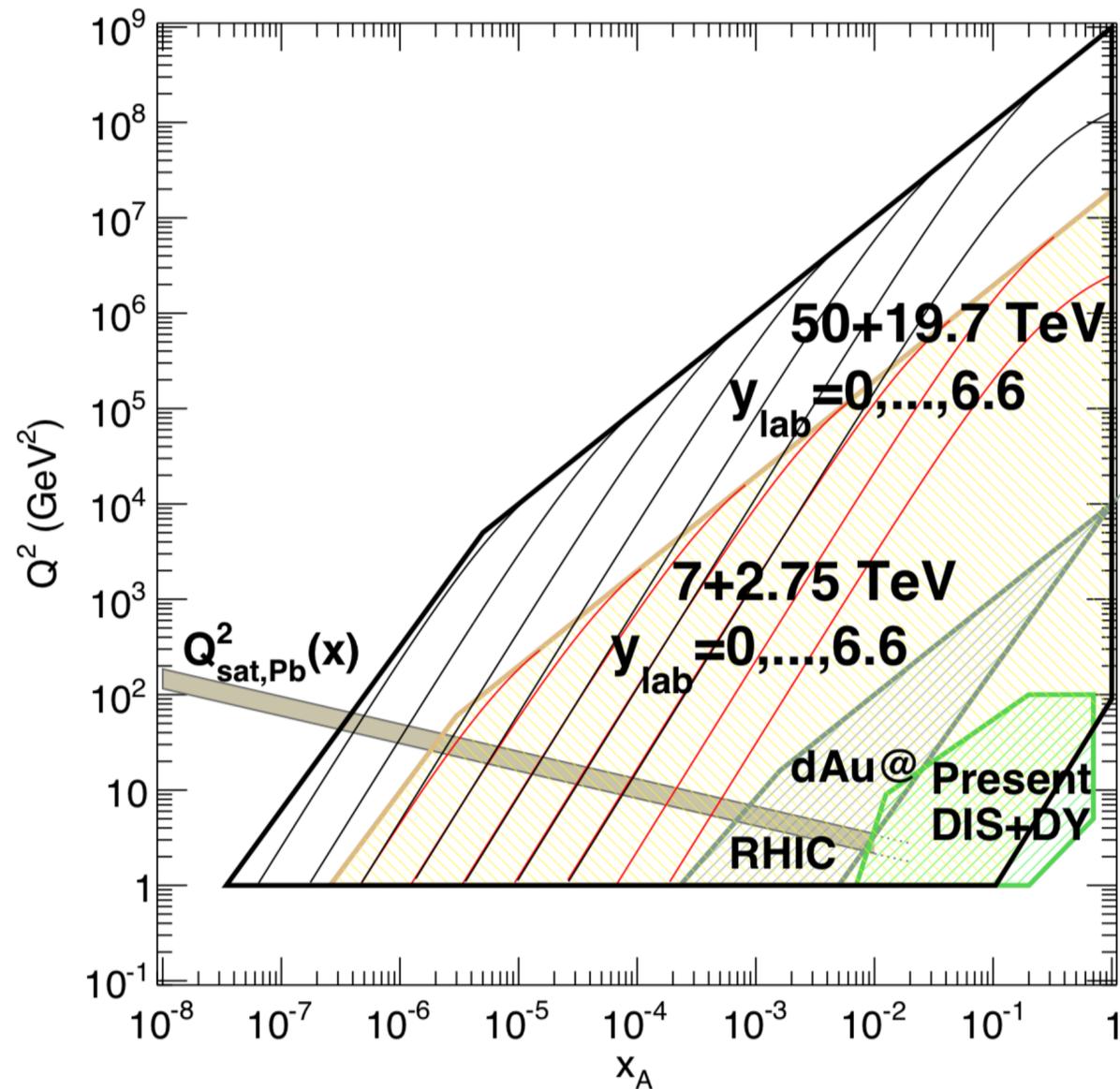
Expected to break if gluon phase space becomes saturated



◆ x - Q^2 phase space accessible at FCC:

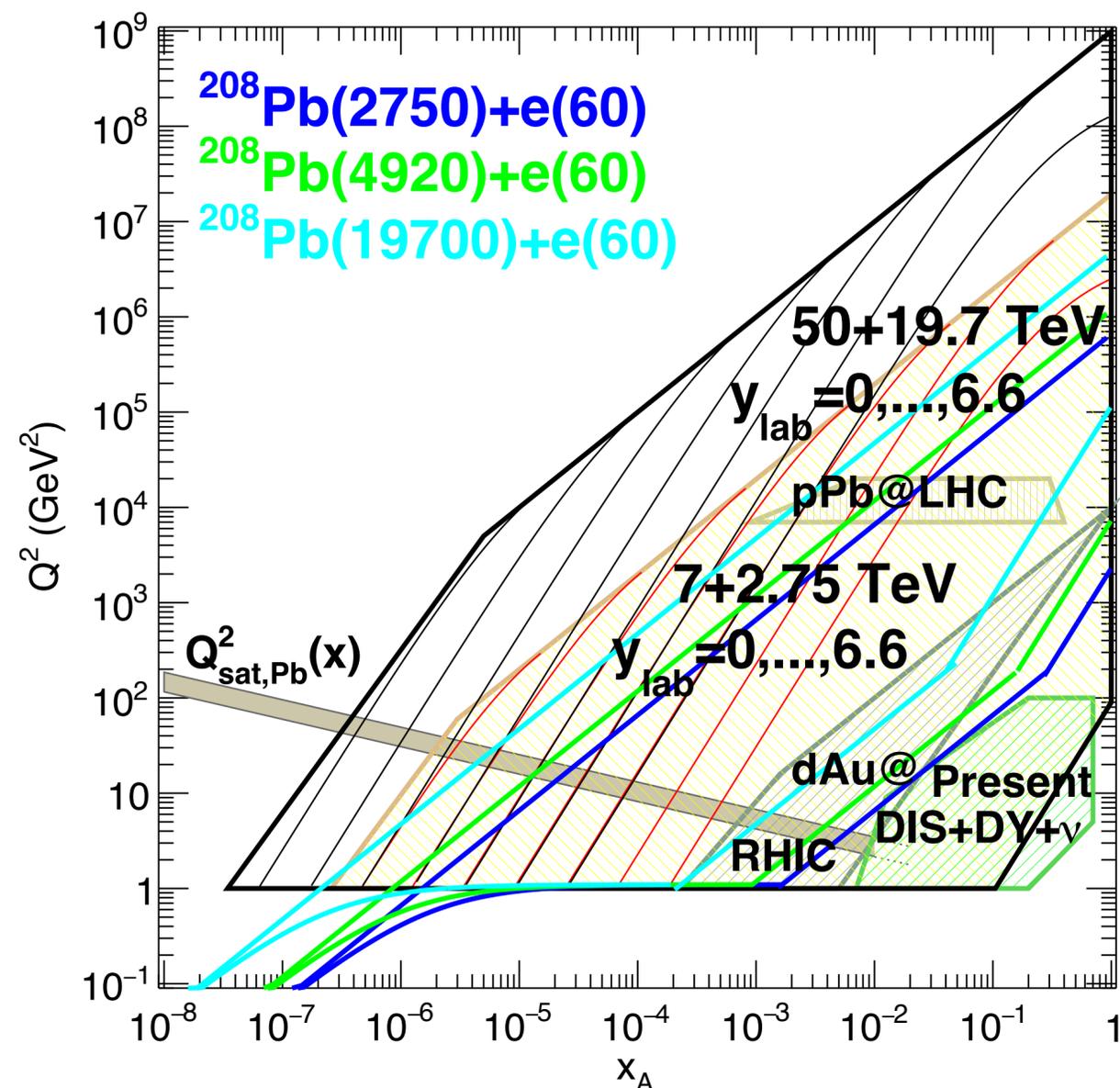


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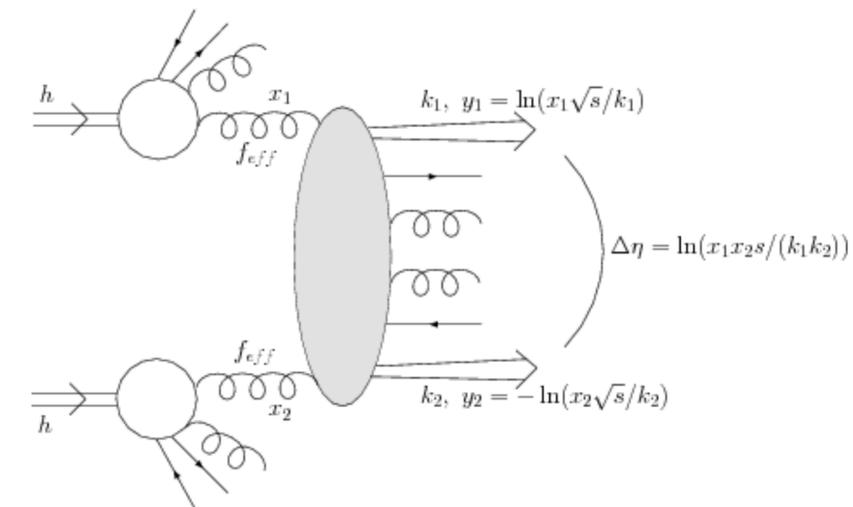
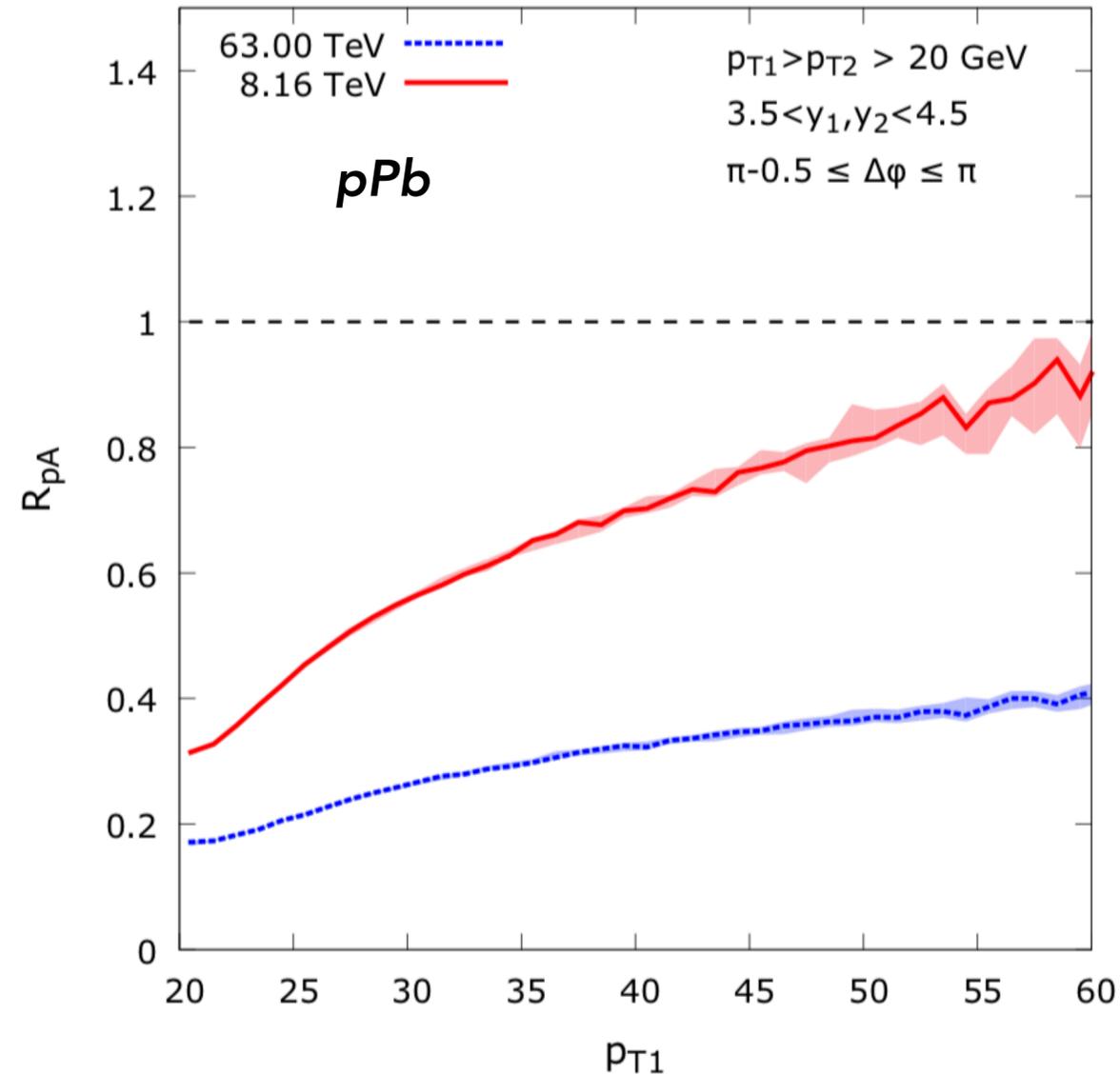
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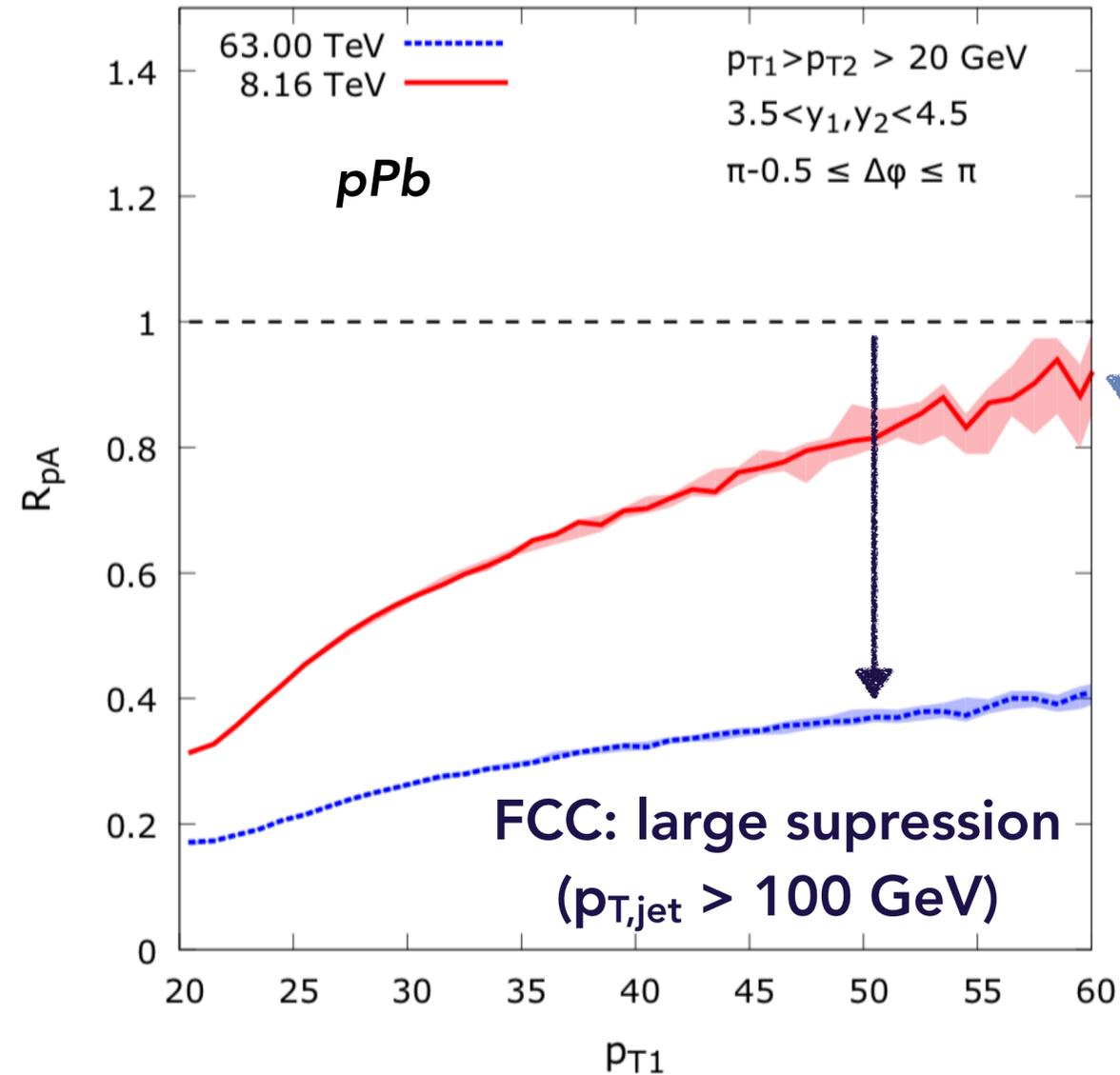
- ✓ FCC able to probe saturation at mid-rapidity
- ✓ Complementary eA/pA: precise knowledge on partonic structures at small- x (kinematics fully constrained)

- ◆ Where can we see saturation phenomena?
- ◆ Dijets at forward rapidity;

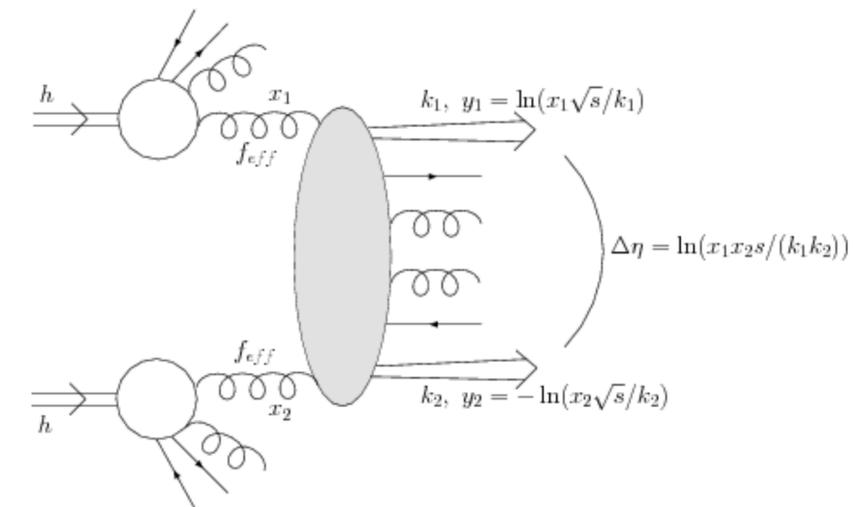


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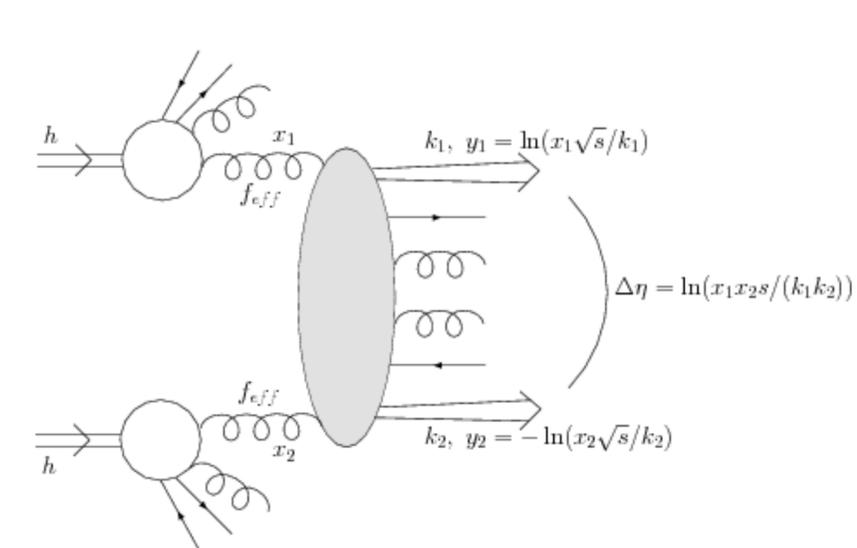
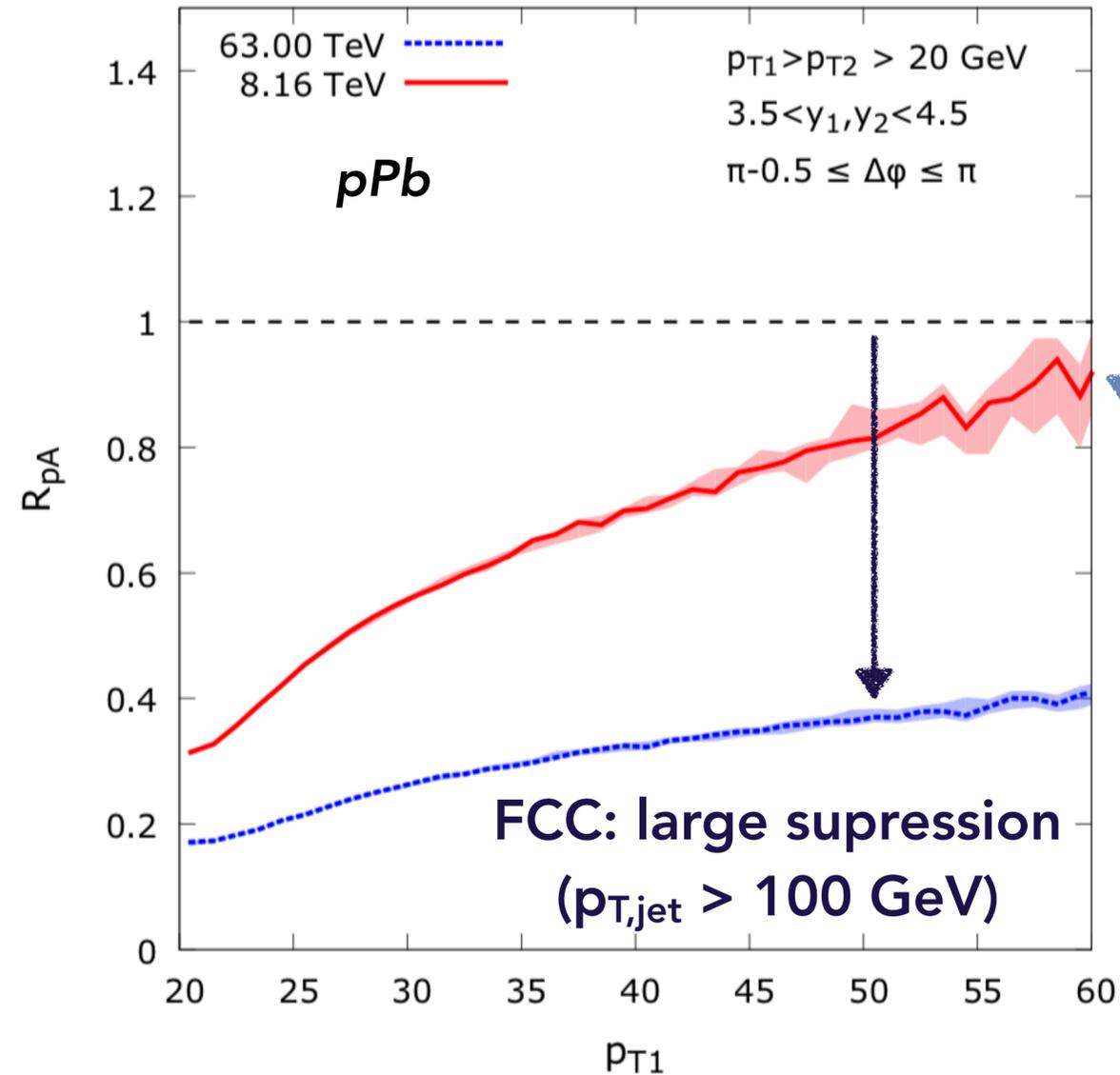
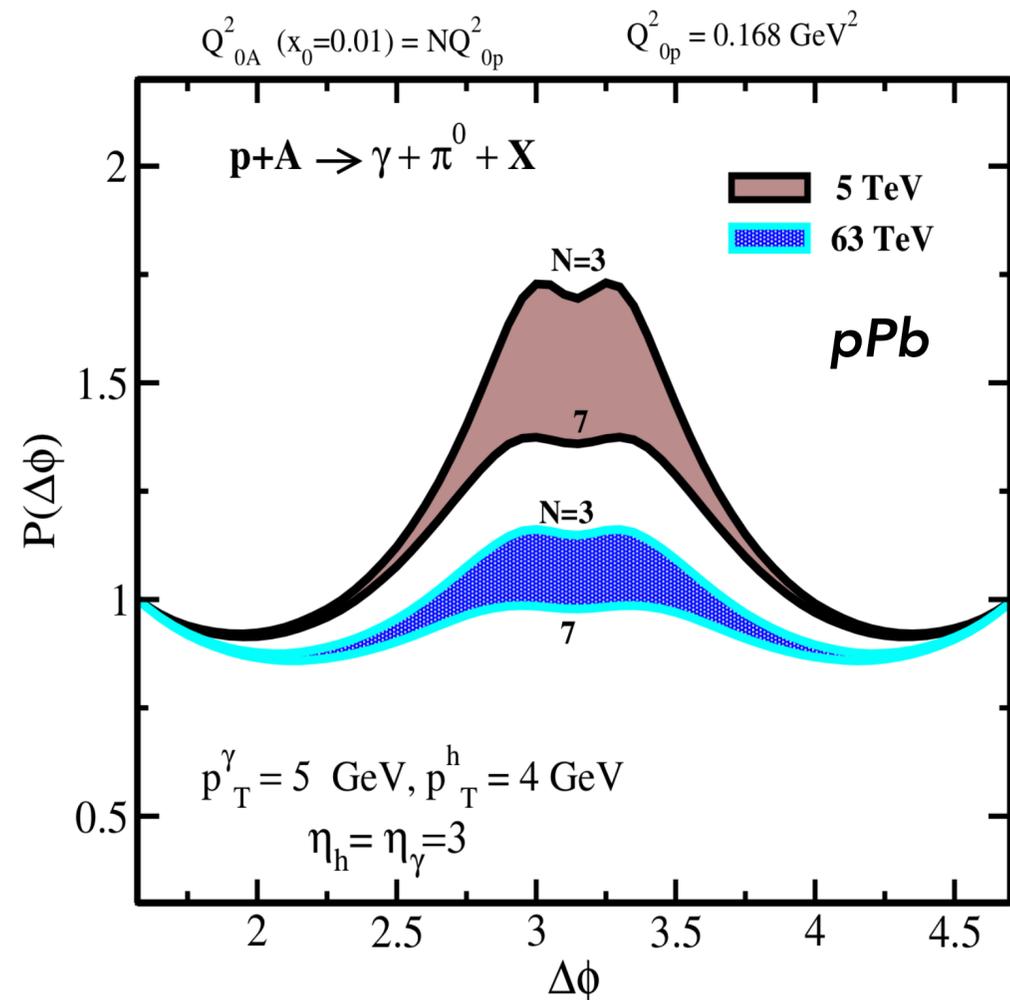
LHC: no effect



◆ Where can we see saturation phenomena?

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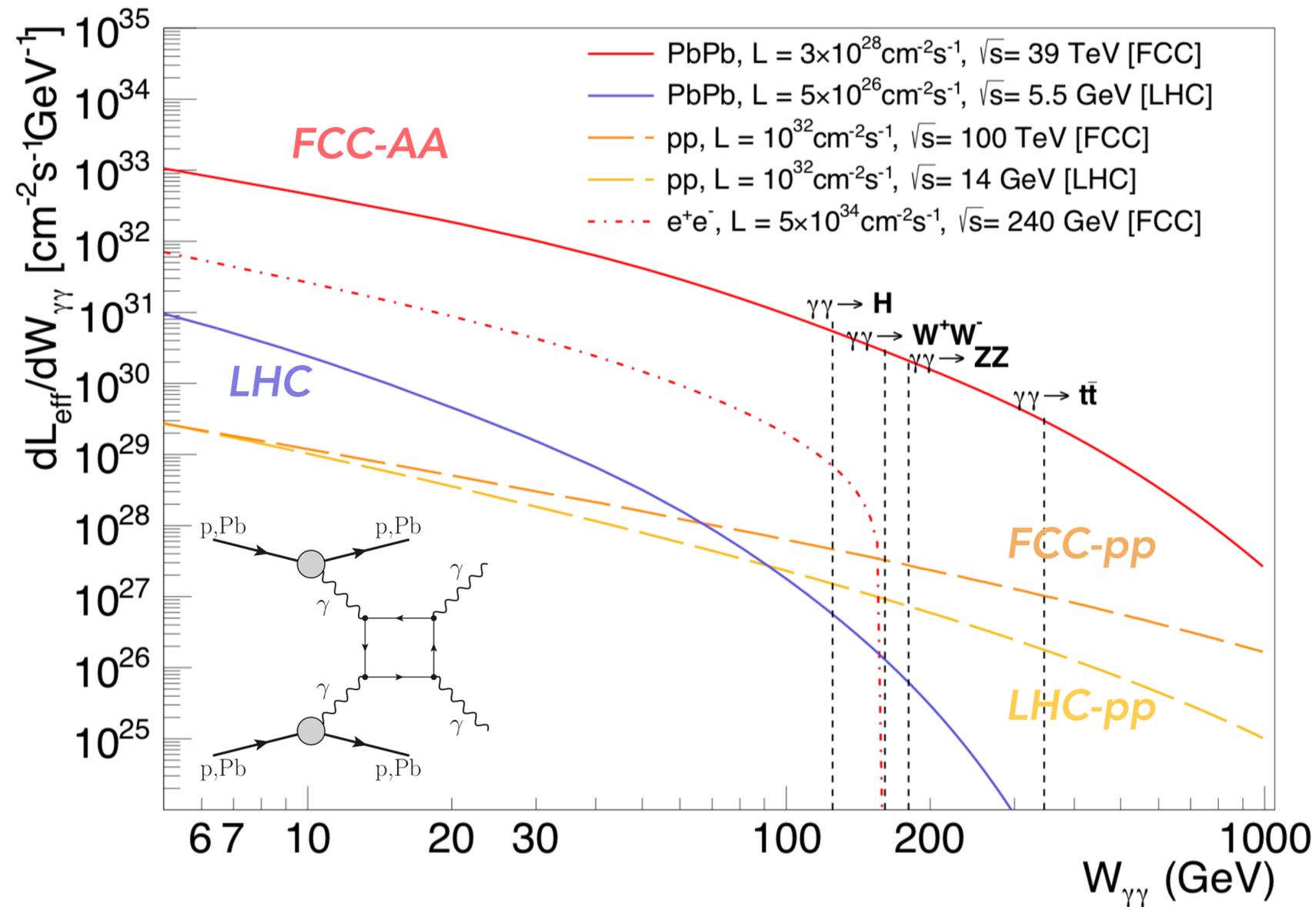
◆ Recoil from direct photon;





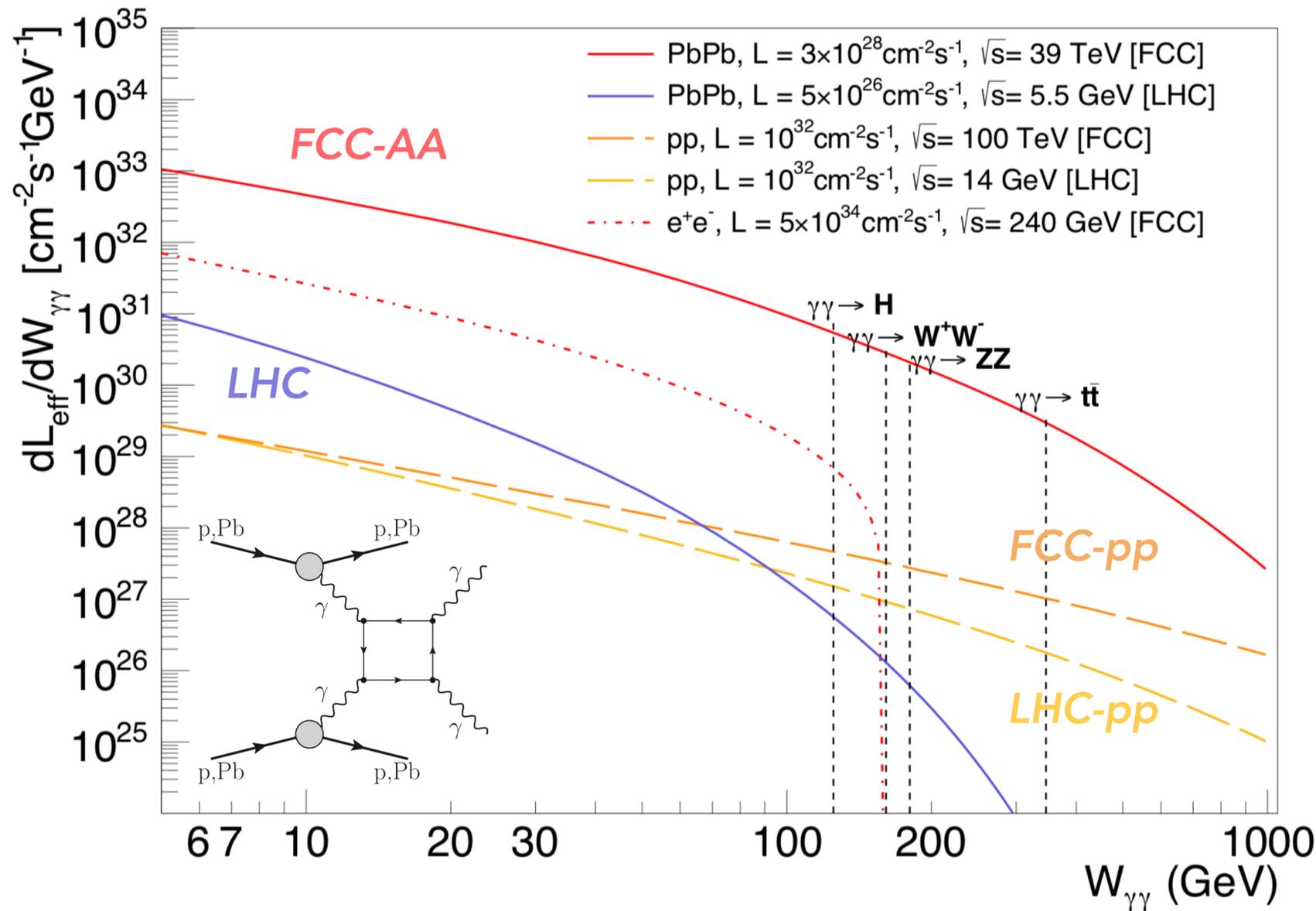
Other Sectors of High-Energy Physics

◆ Effective $\gamma\gamma$ luminosity:



✓ FCC-AA: largest $\gamma\gamma$ luminosity!

◆ Effective $\gamma\gamma$ luminosity:



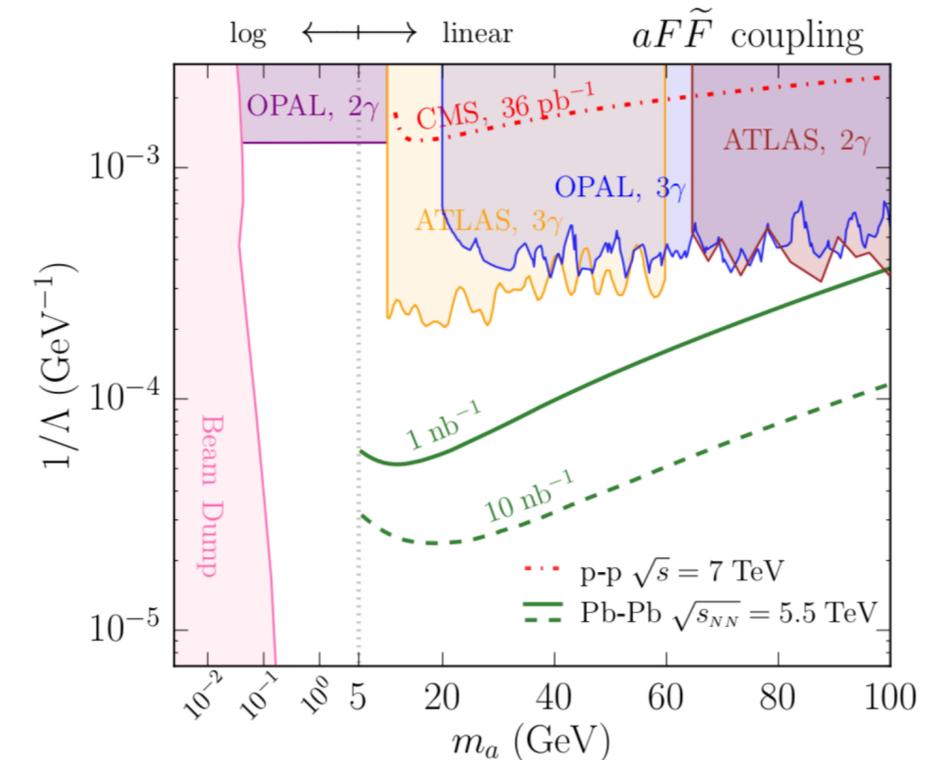
✓ FCC-AA: largest $\gamma\gamma$ luminosity!

◆ Light-by-light scattering measurement at FCC:

✓ Sensitivity to BSM physics (e.g: new heavy-charged SYSY particles)

✓ Axion-like particles

✓ ...





Summary

- ◆ FCC-hh study aimed to assess physics potential at a:
 - ◆ \sqrt{s} 7 x larger than nominal LHC energies; L_{int} projections >100 x LHC programme;
- ◆ FCC offers the possibility for an accurate determination of the QCD behaviour at large densities and temperatures:
 - ◆ Addressing current **open questions**:
 - ◆ Collectivity in small systems, Determination of saturation effects,...
 - ◆ **Unique physics opportunities**:
 - ◆ Soft probes sector: e.g: thermal charm production
 - ◆ Hard probes sector: e.g: top and Higgs to probe the QGP
 - ◆ Initial state sector: e.g: nPDFs up to a small-x reach

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Thank you!



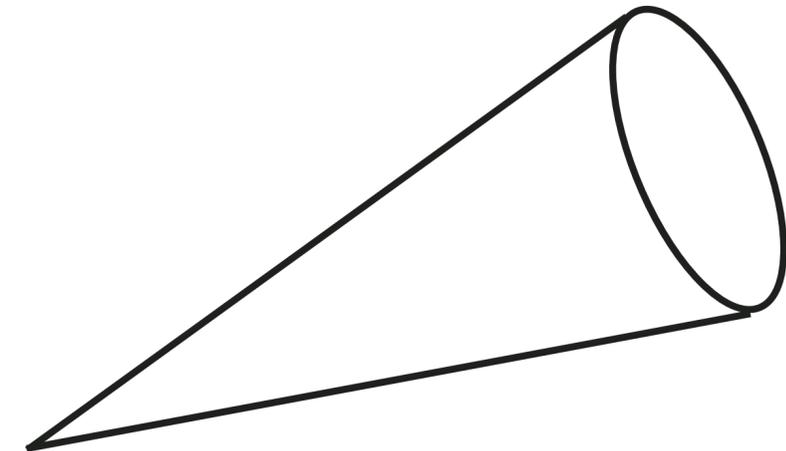
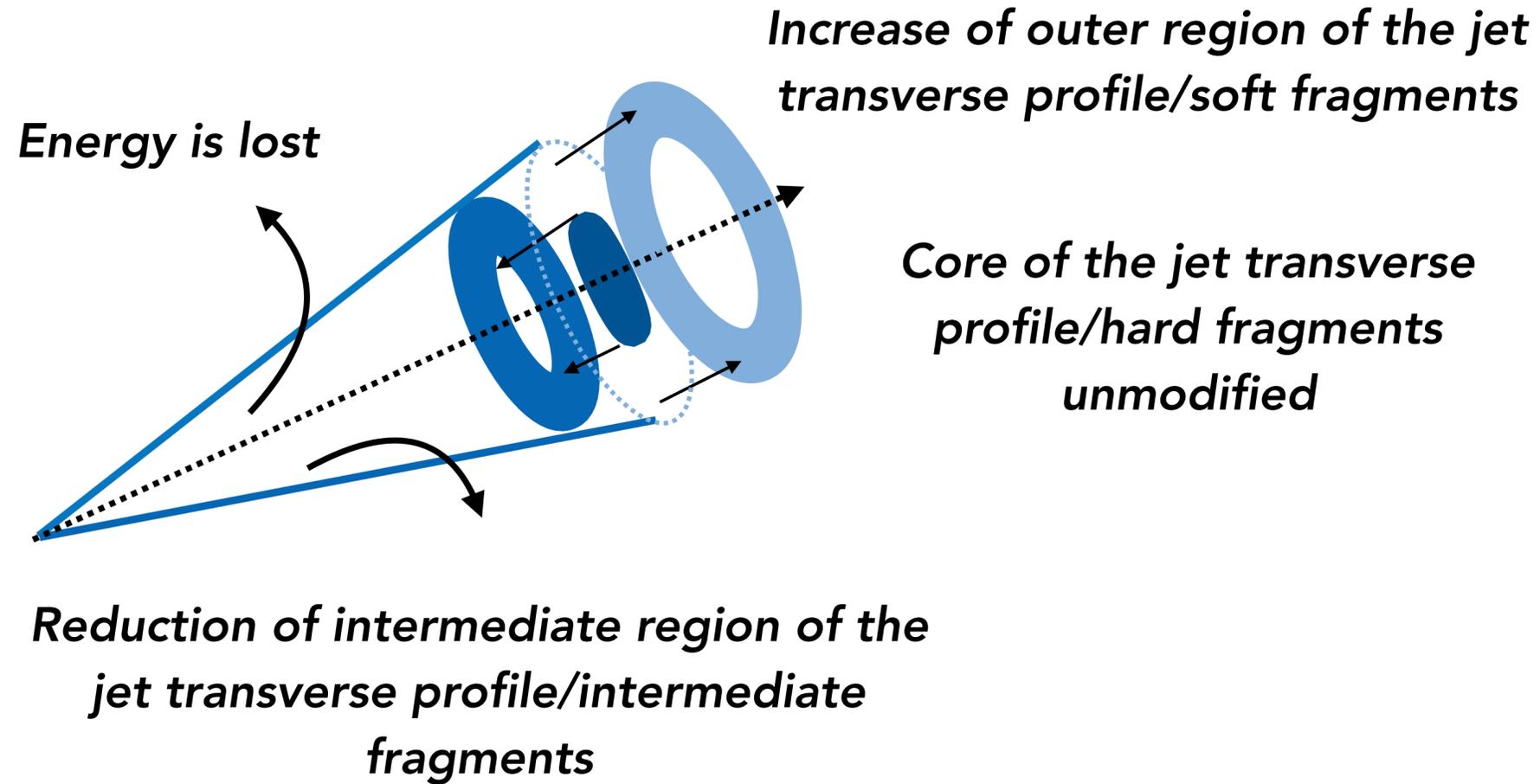
Acknowledgments



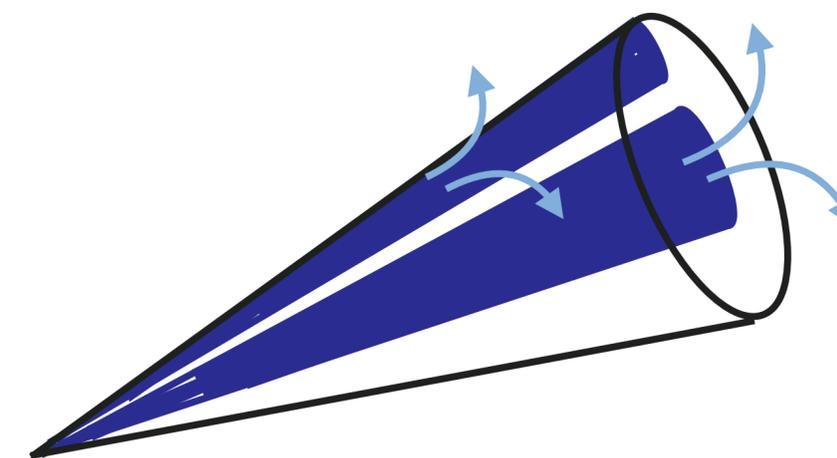
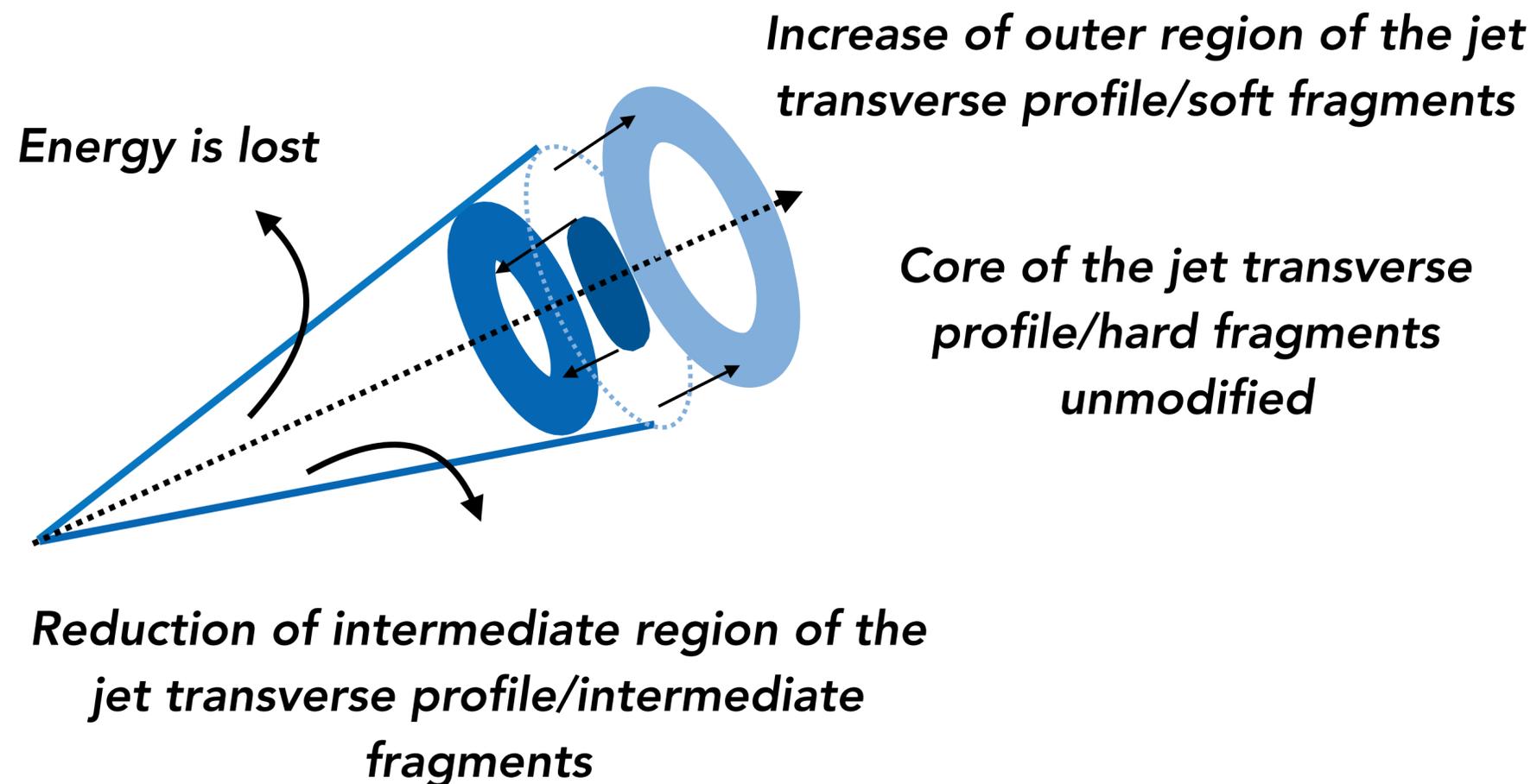
Backup Slides



- ◆ Current picture of a medium-modified jet:



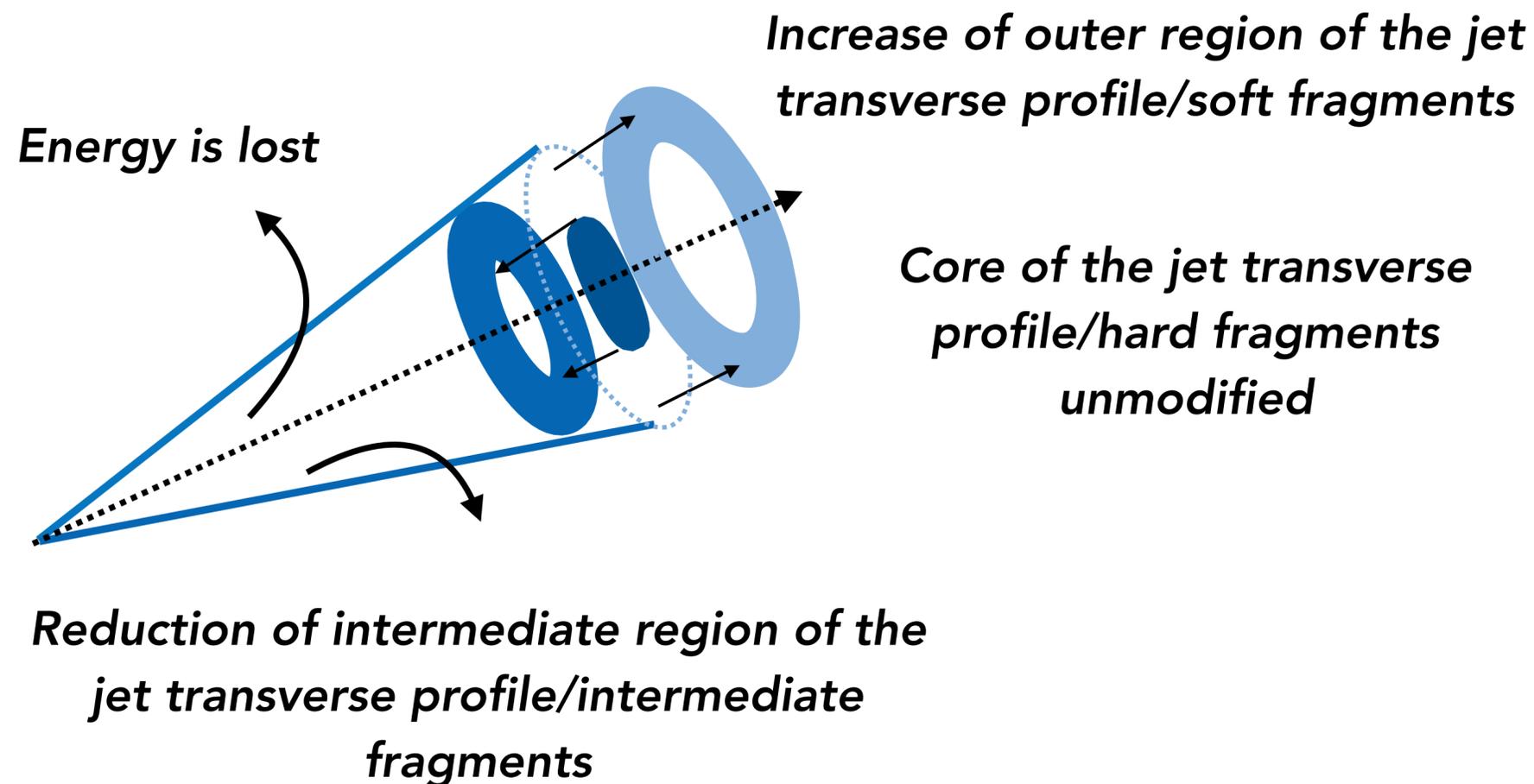
- ◆ Current picture of a medium-modified jet:



*Finite size angular ordered structures
(not resolved by the medium)*

Evolve as pp-like structures (angular ordered) and radiate in-medium radiation (+anti-angular ordered)

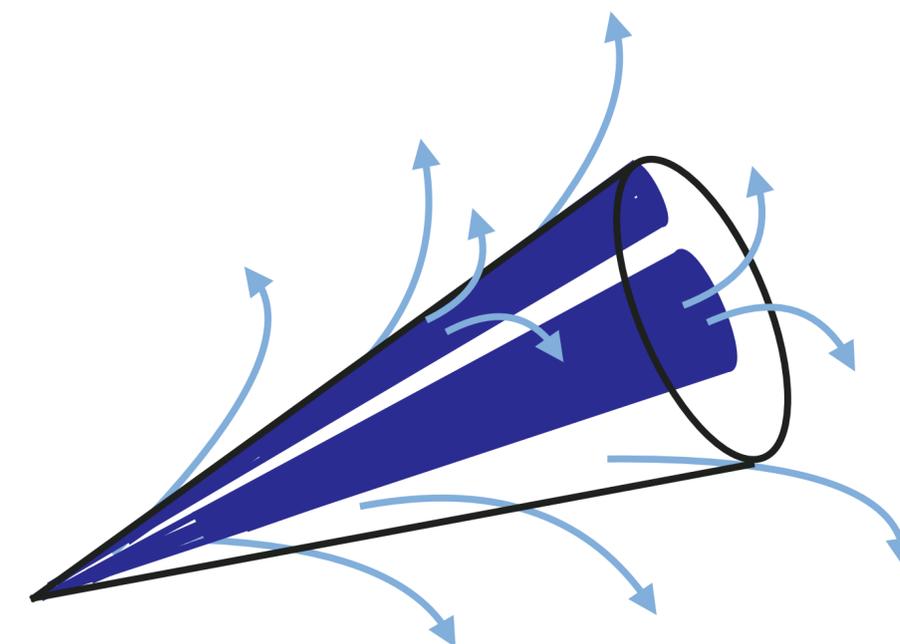
- ◆ Current picture of a medium-modified jet:



@ LHC: Jets can provide a range of scales to probe the QGP!

@ FCC: What can it bring of new?

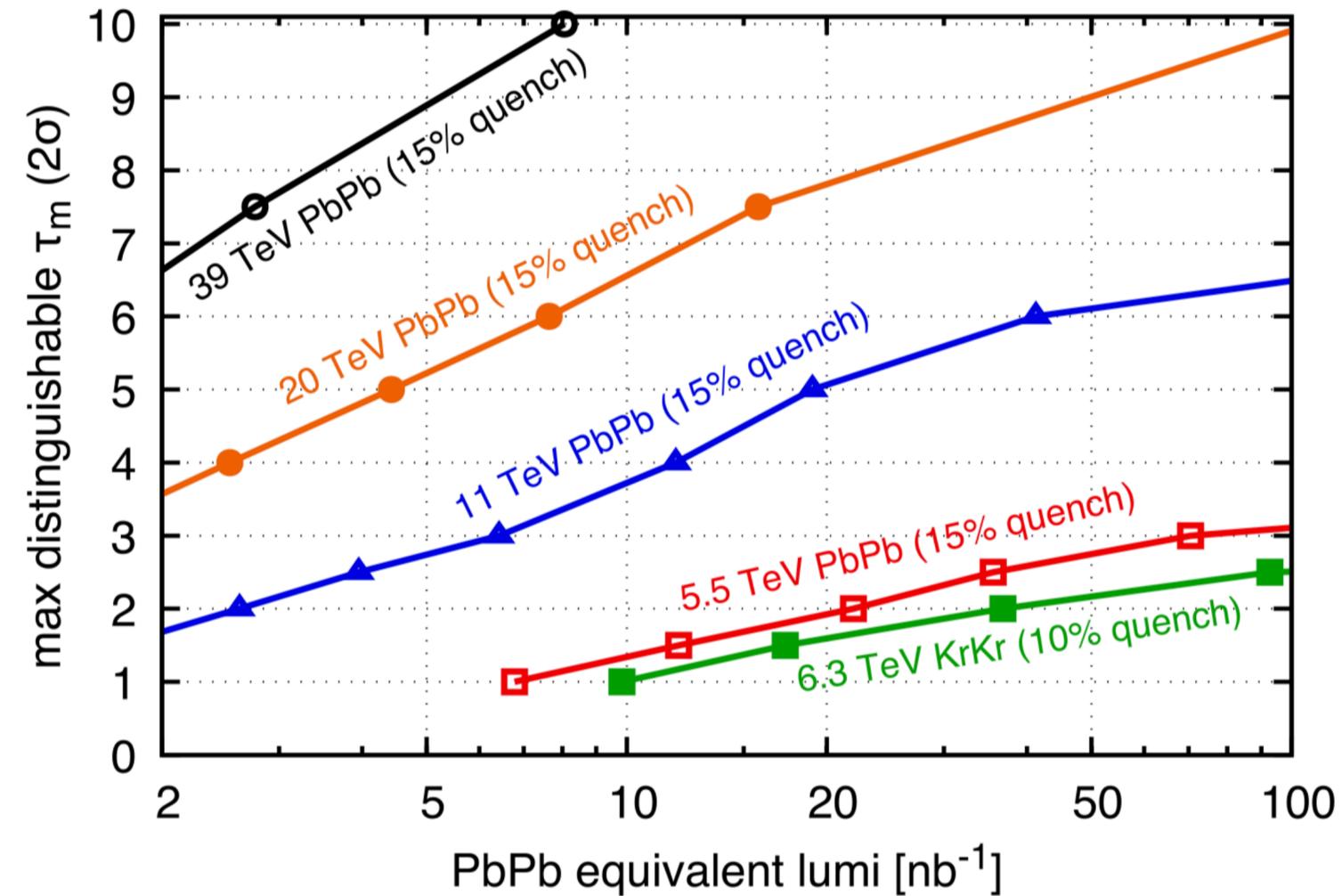
**Soft fragments:
momentum broadening**



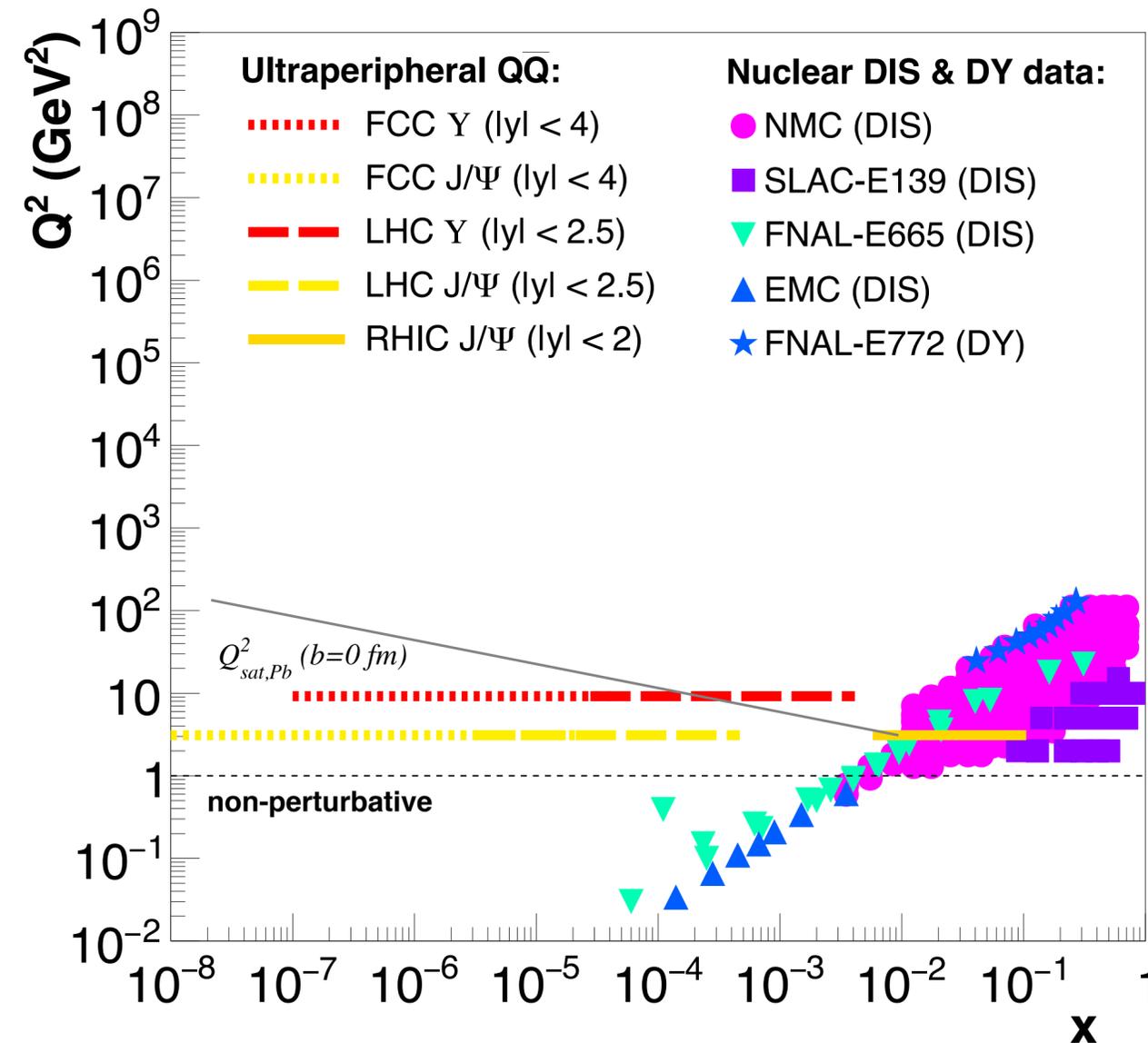
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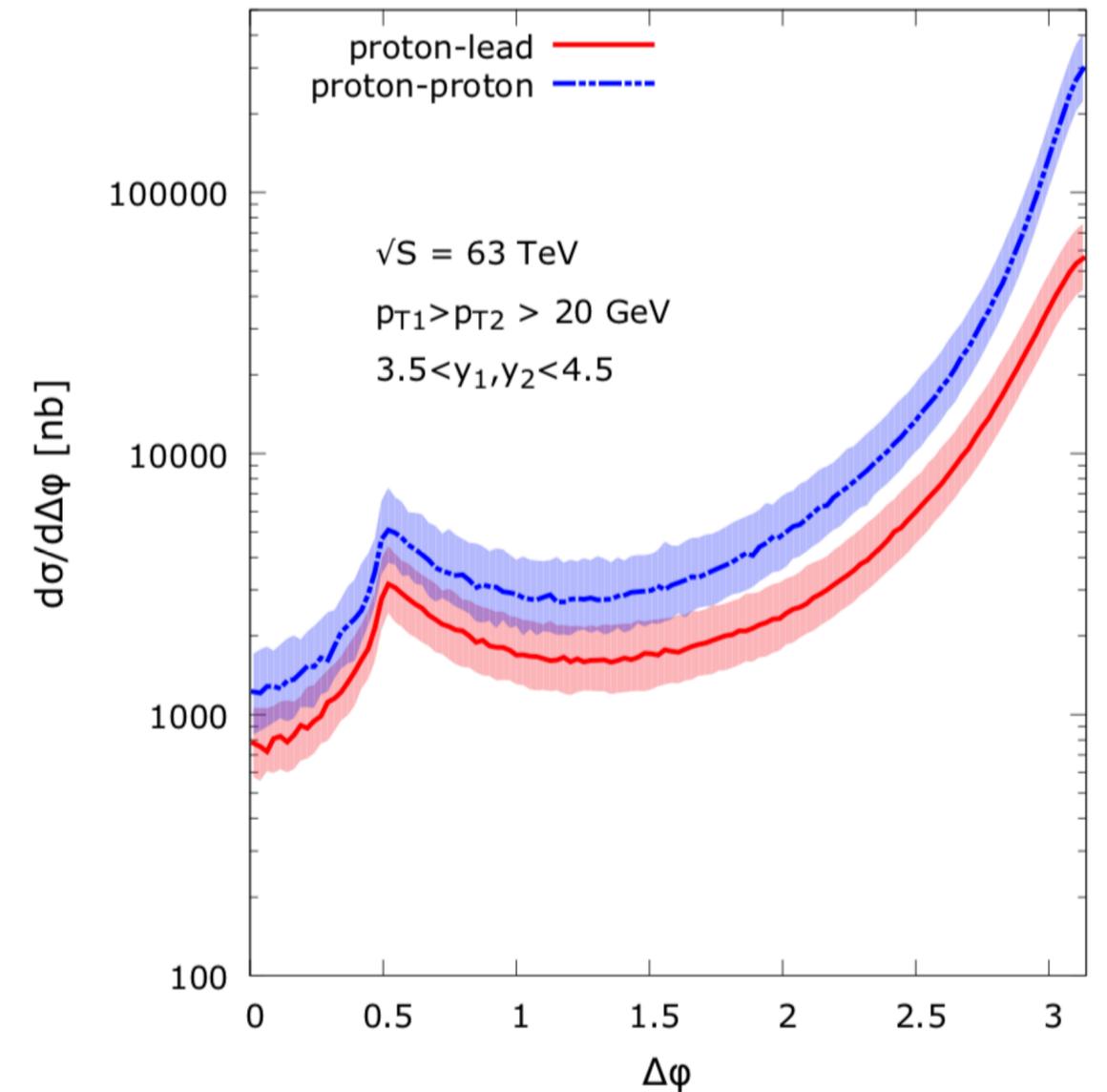
- ◆ Maximum timescales that can be distinguishable at each collider:



- ◆ Regions of $x-Q^2$ plane covered with quarkonia in ultra peripheral ion collisions



- ◆ The recoil suppression can be also be explored using dijets at forward rapidity:
- ◆ Expected broadening of the $\Delta\varphi$ distribution in pPb vs pp collisions:



- ◆ No detailed detector requirements so far... but:
 - ◆ Soft probes physics program require:
 - ◆ Charged-hadron identification to measure independently:
 - ◆ Low-pT charged mesons and baryons
 - ◆ Low-pT c and b mesons
 - ◆ Track reconstruction down to low pT, (starting from few MeV)
 - ◆ Combination of methods that include:
 - specific energy deposition in silicon trackers;
 - time-of-flight;
 - Cherenkov radiation,
 - ◆ Delicate interplay between material thickness of the inner tracker and strong magnetic field
 - General-purpose detector operated at $B \approx 1 \text{ T}$ (?)

- ◆ No detailed detector requirements so far... but:
 - ◆ Hard probes physics program should match the same for the pp program of the FCC:
 - ◆ Hadronic and electromagnetic calorimeters with:
 - ◆ Large acceptance;
 - ◆ High energy resolution at high p_T
 - ◆ High performance up to very large event multiplicities;