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Supersede ATLAS-CONF-2019-009. List of changes : <https://cds.cern.ch/record/2693198>

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## **Measurement of the CP violation phase $\phi_s$ in $B_s^0 \rightarrow J/\psi\phi$ decays in ATLAS at 13 TeV**

A measurement of the  $B_s^0 \rightarrow J/\psi\phi$  decay parameters using  $80.5 \text{ fb}^{-1}$  of integrated luminosity collected with the ATLAS detector from 13 TeV  $pp$  collisions at the LHC is presented. The measured parameters include the CP-violating phase  $\phi_s$ , the width difference  $\Delta\Gamma_s$  between the  $B_s^0$  meson mass eigenstates and the average decay width  $\Gamma_s$ . The values measured for the physical parameters are combined with those from  $19.2 \text{ fb}^{-1}$  of 7 TeV and 8 TeV data, leading to the following:

$$\begin{aligned}\phi_s &= -0.096 \pm 0.036 \text{ (stat.)} \pm 0.024 \text{ (syst.) rad} \\ \Delta\Gamma_s &= 0.0696 \pm 0.0042 \text{ (stat.)} \pm 0.0029 \text{ (syst.) ps}^{-1} \\ \Gamma_s &= 0.6684 \pm 0.0014 \text{ (stat.)} \pm 0.0018 \text{ (syst.) ps}^{-1}\end{aligned}$$

Results for  $\phi_s$  and  $\Delta\Gamma_s$  are also presented as 68% likelihood contours in the  $\phi_s - \Delta\Gamma_s$  plane. Furthermore the transversity amplitudes and corresponding strong phases are measured. All measurements are in agreement with the Standard Model predictions.

To be submitted to: EPJC

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# ATLAS Paper

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## Measurement of the CP violation phase $\phi_s$ in $B_s^0 \rightarrow J/\psi\phi$ decays in ATLAS at 13 TeV

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The ATLAS Collaboration

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# 1 Introduction

In the presence of New Physics (NP) phenomena, sources of CP violation in  $b$ -hadron decays can arise in addition to those predicted by the Standard Model (SM) [1]. In the  $B_s^0 \rightarrow J/\psi\phi$  decay, CP violation occurs due to interference between a direct decay and a decay with  $B_s^0 - \bar{B}_s^0$  mixing. The oscillation frequency of  $B_s^0$  meson mixing is characterised by the mass difference  $\Delta m_s$  of the heavy ( $B_H$ ) and light ( $B_L$ ) mass eigenstates. The CP violating phase  $\phi_s$  is defined as the weak phase difference between the  $B_s^0 - \bar{B}_s^0$  mixing amplitude and the  $b \rightarrow c\bar{c}s$  decay amplitude. In the SM the phase  $\phi_s$  is small and is related to Cabibbo–Kobayashi–Maskawa (CKM) quark mixing matrix elements via the relation  $\phi_s \simeq -2\beta_s$ , with  $\beta_s = \arg[-(V_{ts}V_{tb}^*)/(V_{cs}V_{cb}^*)]$ ; assuming no NP contributions to  $B_s^0$  mixing and decays, a value of  $-2\beta_s = -0.0363_{-0.0015}^{+0.0016}$  rad can be predicted by combining beauty and kaon physics observables [2]. While large NP enhancements of the mixing amplitude have been excluded by the precise measurement of the oscillation frequency [3], the NP couplings involved in the mixing may still increase the size of the observed CP violation by enhancing the mixing phase  $\phi_s$  with respect to the SM value.

Other physical quantities involved in  $B_s^0 - \bar{B}_s^0$  mixing are the decay width  $\Gamma_s = (\Gamma_L + \Gamma_H)/2$  and the width difference  $\Delta\Gamma_s = \Gamma_L - \Gamma_H$ , where  $\Gamma_L$  and  $\Gamma_H$  are the decay widths of the light and heavy mass eigenstates, respectively. In the SM the width difference is predicted to be  $\Delta\Gamma_s = 0.087 \pm 0.021$  ps<sup>-1</sup> [4]. A potential NP enhancement of  $\phi_s$  would also decrease the size of  $\Delta\Gamma_s$ , however it is not expected to be affected as significantly as  $\phi_s$  [5]. Nevertheless, extracting  $\Delta\Gamma_s$  from data is interesting as it allows theoretical predictions to be tested [5].

The analysis of the time evolution of the  $B_s^0 \rightarrow J/\psi\phi$  decay provides the most precise determination of  $\phi_s$  and  $\Delta\Gamma_s$ . Previous measurements of these quantities have been reported by the D0, CDF, LHCb, ATLAS and CMS collaborations [Aad:2016tdj, 6–10]. Additional improvements in measuring  $\phi_s$  from  $B_s^0$  decays to  $\psi(2S)\phi$  and to  $D_s^+D_s^-$  have been achieved by the LHCb collaboration [Aaij:2016psitwoS, Aaij:2014Ds].

The analysis presented here introduces a measurement of the  $B_s^0 \rightarrow J/\psi\phi$  decay parameters using 80.5 fb<sup>-1</sup> of LHC  $pp$  data collected by the ATLAS detector during 2015 – 2017 at a centre-of-mass energy,  $\sqrt{s}$ , equal to 13 TeV. The analysis closely follows a previous ATLAS measurement [Aad:2016tdj] that was performed using 19.2 fb<sup>-1</sup> of data collected at 7 TeV and 8 TeV and introduces more precise models for both signal and backgrounds.

## 2 ATLAS detector and Monte Carlo simulation

The ATLAS detector\* consists of three main components: an inner detector (ID) tracking system immersed in a 2 T axial magnetic field, electromagnetic and hadronic calorimeters, and a muon spectrometer (MS). The inner tracking detector covers the pseudorapidity range  $|\eta| < 2.5$ , and consists of silicon pixel, silicon micro-strip, and transition radiation tracking detectors. The ID is surrounded by a high-granularity liquid-argon (LAr) sampling electromagnetic calorimeter. A steel/scintillator tile calorimeter provides hadronic coverage in the central rapidity range. The end-cap and forward regions are equipped with LAr

\* ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point. The  $z$ -axis is along the beam pipe, the  $x$ -axis points to the centre of the LHC ring and the  $y$ -axis points upward. Cylindrical coordinates  $(r, \phi)$  are used in the transverse plane,  $r$  being the distance from the origin and  $\phi$  being the azimuthal angle around the beam pipe. The pseudorapidity  $\eta$  is defined as  $\eta = -\ln[\tan(\theta/2)]$  where  $\theta$  is the polar angle.

54 calorimeters for electromagnetic and hadronic measurements. The MS surrounds the calorimeters and  
 55 provides a system of tracking chambers and detectors for triggering. A full description can be found in  
 56 Refs. [11–13].

57 The muon and tracking systems are of particular importance in the reconstruction of  $B$  meson candidates.  
 58 Only data collected when both these systems were operating correctly and when the LHC beams were  
 59 declared to be stable are used in the analysis. The data were collected during periods with different  
 60 instantaneous luminosity, therefore several triggers were used in the analysis. All triggers were based on  
 61 the identification of a  $J/\psi \rightarrow \mu^+ \mu^-$  decay, with transverse momentum ( $p_T$ ) thresholds of either 4 GeV or  
 62 6 GeV for the muons.

63 The measurement uses  $80.5 \text{ fb}^{-1}$  of  $pp$  collision data. The uncertainty in the combined 2015–2017  
 64 integrated luminosity is 2.0%. It is derived, following a methodology similar to that detailed in Ref. [14],  
 65 and using the LUCID-2 detector for the baseline luminosity measurements [15], from calibration of the  
 66 luminosity scale using  $x$ – $y$  beam-separation scans.

67 To study the detector response, estimate backgrounds, and model systematic effects, 100M Monte Carlo  
 68 (MC) simulated  $B_s^0 \rightarrow J/\psi \phi$  events were generated using PYTHIA 8.210 [16] tuned with ATLAS data,  
 69 using the A14 set of parameters [17] together with the CTEQ6L1 set [18]. The detector response was  
 70 simulated using the ATLAS simulation framework based on GEANT4 [19, 20]. In order to account for  
 71 the varying number of proton–proton interactions per bunch crossing (pile-up) and trigger configurations  
 72 during data-taking, the MC events were weighted to reproduce the same pile-up and trigger conditions  
 73 as in data. Additionally, the background samples of both exclusive ( $B_d^0 \rightarrow J/\psi K^{0*}$  and  $\Lambda_b \rightarrow J/\psi p K^-$ )  
 74 and inclusive ( $b\bar{b} \rightarrow J/\psi X$  and  $pp \rightarrow J/\psi X$ ) decays were simulated, using the same simulation tools  
 75 as in case of the signal events. For validation studies related to *flavour tagging*, detailed in 4, events of  
 76  $B^\pm \rightarrow J/\psi K^\pm$  exclusive decays were also simulated.

### 77 3 Reconstruction and candidate selection

78 The reconstruction and candidate selection for the decay  $B_s^0 \rightarrow J/\psi(\mu^+ \mu^-)\phi(K^+ K^-)$  is described here.  
 79 Events must pass the trigger selections described in Section 2. In addition, each event must contain at least  
 80 one reconstructed primary vertex, formed from at least four ID tracks, and at least one pair of oppositely  
 81 charged muon candidates that are reconstructed using information from the MS and the ID. The muon  
 82 track parameters used in this analysis are determined from the ID measurement alone, since the precision  
 83 of the measured track parameters is dominated by the ID track reconstruction in the  $p_T$  range of interest  
 84 for this analysis. Pairs of oppositely charged muon tracks are refitted to a common vertex and the pair is  
 85 accepted for further consideration if the quality of the fit meets the requirement  $\chi^2/\text{n.d.o.f.} < 10$ . In order  
 86 to account for varying mass resolution in different parts of the detector, the  $J/\psi$  candidates are divided  
 87 into three subsets according to the pseudorapidity  $\eta$  of the muons. In the first subset both muons have  
 88  $|\eta| < 1.05$ , where the values  $\eta = \pm 1.05$  correspond to the edges of the barrel part of the MS. In the  
 89 second subset one muon has  $1.05 < |\eta| < 2.5$  and the other muon  $|\eta| < 1.05$ . The third subset contains  
 90 candidates where both muons have  $1.05 < |\eta| < 2.5$ . A maximum-likelihood fit is used to extract the  $J/\psi$   
 91 mass and the corresponding mass resolution for these three subsets, and in each case the signal region is  
 92 defined symmetrically around the fitted mass, so as to retain 99.7% of the  $J/\psi$  candidates identified in the  
 93 fits.

94 The candidates for the decay  $\phi \rightarrow K^+K^-$  are reconstructed from all pairs of oppositely charged  
 95 tracks, with  $p_T > 1$  GeV and  $|\eta| < 2.5$ , that are not identified as muons. Candidate events for  
 96  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$  decays are selected by fitting the tracks for each combination of  $J/\psi \rightarrow \mu^+\mu^-$   
 97 and  $\phi \rightarrow K^+K^-$  to a common vertex. The fit is also constrained by fixing the invariant mass calculated  
 98 from the two muon tracks to the  $J/\psi$  mass [21]. A quadruplet of tracks is accepted for further analysis  
 99 if the vertex fit has  $\chi^2/\text{n.d.o.f.} < 3$ . For the  $\phi \rightarrow K^+K^-$  candidate, the invariant mass of the track pairs  
 100 (using a kaon mass hypothesis) must fall within the interval  $1.0085 \text{ GeV} < m(K^+K^-) < 1.0305 \text{ GeV}$ .  
 101 The interval, chosen using MC simulation, is selected to retain 98% of true  $\phi \rightarrow K^+K^-$  decays. The  
 102  $B_s^0$  candidate with the lowest  $\chi^2/\text{n.d.o.f.}$  is selected in cases where more than one candidate passes all  
 103 selections. In total, 2 977 526  $B_s^0$  candidates are collected within the mass range of 5.150–5.650 GeV.  
 104 This range is chosen to give enough background events in the side bands of the mass distributions to allow  
 105 a high precision determination of the properties of background events. The mass window choice has been  
 106 varied and found to have a negligible systematic effect on the results.

107 The mean number of interactions per bunch crossing is 30, necessitating a choice of the best candidate for  
 108 the primary vertex at which the  $B_s^0$  meson is produced. The variable used is the three-dimensional impact  
 109 parameter  $a_0$ , which is calculated as the minimum distance between each primary vertex candidate and  
 110 the line extrapolated from the reconstructed  $B_s^0$  meson vertex in the direction of the  $B_s^0$  momentum. The  
 111 chosen primary vertex is the one with the smallest  $a_0$ .

112 For each  $B_s^0$  meson candidate the proper decay time  $t$  is estimated using:

$$t = \frac{L_{xy} m_B}{p_{T_B}},$$

113 where  $p_{T_B}$  is the reconstructed transverse momentum of the  $B_s^0$  meson candidate and  $m_B$  denotes the  
 114 mass of the  $B_s^0$  meson, taken from Ref. [21]. The transverse decay length,  $L_{xy}$ , is the displacement in  
 115 the transverse plane of the  $B_s^0$  meson decay vertex with respect to the primary vertex, projected onto the  
 116 direction of the  $B_s^0$  transverse momentum. The primary vertex position is recalculated after removing any  
 117 tracks used in the  $B_s^0$  meson candidate to avoid biasing  $L_{xy}$ .

## 118 4 Flavour tagging

119 To identify, or *tag*, the flavour of a neutral  $B$  meson at the point of production, information is extracted  
 120 using the decay of the other (or *opposite*)  $b$ -hadron that is produced from the pair production of  $b$  and  $\bar{b}$   
 121 quarks. This approach is called opposite-side tagging (OST).

122 The OST algorithms each define a discriminating variable, based on charge information, which is sensitive  
 123 to the flavour (ie.  $b$ - or  $\bar{b}$ -quark) of the opposite-side  $b$ -hadron. The algorithms thus provide a probability  
 124 that a signal  $B$  meson in a given event is produced in a given flavour. The calibration of the OST  
 125 algorithms proceeds using data containing  $B^\pm \rightarrow J/\psi K^\pm$  candidate decays, where the charge of the kaon  
 126 determines the flavour of the  $B$  meson, providing a self-tagging sample of events. These OST algorithms  
 127 are calibrated as a function of the discriminating variable, using yields of signal  $B^\pm$  mesons extracted from  
 128 fits to the data. Once calibrated, the OST algorithms are applied to  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$  candidate  
 129 events to provide a probability that each candidate was produced in a  $B_s^0$  or  $\bar{B}_s^0$  meson state, which is used  
 130 in the maximum likelihood fit (described in Section 5). Section 4.1 describes the reconstruction of the  
 131  $B^\pm \rightarrow J/\psi K^\pm$  candidates, followed by a description of the OST methods in Section 4.2. The performance

of the OST algorithms on the calibration sample is given in Section 4.3, and details on how the probabilities from the OST algorithms are used in the maximum likelihood fit, including the determination of the distributions of these probabilities in signal and background, are discussed in Section 4.4.

#### 4.1 $B^\pm \rightarrow J/\psi K^\pm$ event selection

Candidate  $B^\pm \rightarrow J/\psi K^\pm$  decays are identified in a series of steps described here. First,  $J/\psi$  candidates are selected from oppositely charged muon pairs forming a good vertex, as described in Section 3. Each muon is required to have  $p_T > 4$  GeV and  $|\eta| < 2.5$ . Dimuon candidates with invariant mass  $2.8 < m(\mu^+ \mu^-) < 3.4$  GeV, as determined from the refitted track parameters of the vertex, are retained for further analysis. To form the  $B^\pm$  candidate, an additional track is required. The track is assigned the charged kaon mass hypothesis and combined with the dimuon candidate using a vertex fit, performed with the mass of the dimuon pair constrained to the  $J/\psi$  mass [21]. Prompt background contributions are suppressed with the requirement on the proper decay time of the  $B^\pm$  candidate of  $t > 0.2$  ps.

The tagging probabilities are determined from  $B^+$  and  $B^-$  signal events. These signal yields are derived from fits to the invariant mass distribution,  $m(J/\psi K^\pm)$ , and performed in intervals of the discriminating variables. To describe the  $B^\pm \rightarrow J/\psi K^\pm$  signal, two Gaussian functions with a common mean are used. An exponential function is used to describe the combinatorial background and a hyperbolic tangent function to parametrise the low-mass contribution from incorrectly or partially reconstructed  $b$ -hadron decays. A Gaussian function is used to describe the  $B^\pm \rightarrow J/\psi \pi^\pm$  contribution, with fixed parameters taken from simulation except for the normalisation, which is a free parameter. A fit to the overall mass distribution constrains the shapes of the signal and backgrounds, excluding the slope of the exponential function. Subsequent fits are performed in the intervals of the tagging discriminating variables, separately for  $B^+$  and  $B^-$  candidate events, with the normalisation (and exponential slope) parameters left free. The  $B^+$  and  $B^-$  signal yields are extracted from these fits. Figure 1 shows the invariant mass distribution of  $B^\pm$  candidates overlaid with a fit to all selected candidates, and including the individual fit components for the signal and backgrounds.

#### 4.2 Flavour tagging methods

The flavour of the signal  $B$  meson at the point of production is inferred using several methods, which differ in their efficiency and discrimination power. The measured charge of a lepton (electron or muon) from the semileptonic decay of a  $B$  meson provides strong discrimination; however, the  $b \rightarrow \ell$  transitions are diluted through processes that can change the charge of the observed lepton, such as through neutral  $B$  meson oscillations, or through cascade decays  $b \rightarrow c \rightarrow \ell$ . The separation power of lepton tagging is enhanced by considering a weighted sum of the charge of the tracks in a cone around the lepton, with parameters determined separately for each tagging method based on optimisation of the tagging performance. If no lepton is present, a weighted sum of the charge of the tracks in a jet associated with the opposite-side  $b$ -hadron decay is used to provide discrimination. This weighted sum, or *cone charge*, is defined as:

$$Q_x = \frac{\sum_i^{N \text{ tracks}} q_i \cdot (p_{Ti})^\kappa}{\sum_i^{N \text{ tracks}} (p_{Ti})^\kappa}, \quad (1)$$

where  $x = \{\mu, e, \text{jet}\}$  refers to muon, electron, or jet charge, respectively, and the summation is made over a selected set of tracks — including the lepton — in a cone,  $\Delta R = \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$ , around the lepton or

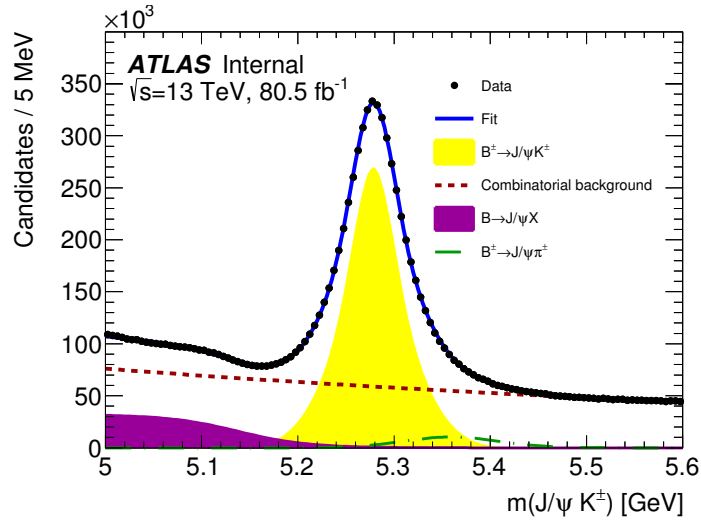


Figure 1: The invariant mass distribution for selected  $B^\pm \rightarrow J/\psi K^\pm$  candidates. Data are shown as points, and the overall result of the fit is given by the blue curve. The contributions from the combinatorial background component are indicated by the red dotted line, partially reconstructed  $b$ -hadron decays by the purple shaded area, and decays of  $B^\pm \rightarrow J/\psi \pi^\pm$ , where the pion is misassigned as a kaon, by the green dashed line.

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169 jet direction. The requirements on the tracks and  $\Delta R$  are described below, dependent on the OST method.  
 170 Two sub-categories of  $Q_x$  are considered: the first *discrete* category is used in the case where the cone  
 171 charge is formed either from only one track or from more than one track of the same charge; this results  
 172 in a cone charge of  $Q_x = \pm 1$ . The second *continuous* category is used when more than one track is  
 173 considered, and the sum contains tracks of both negative and positive charge. In the continuous case,  $Q_x$   
 174 is divided into intervals within the range  $-1 < Q_x < 1$  for each OST algorithm.

175 A probability  $P(B|Q_x)$  is constructed, which is defined as the probability that a  $B$  meson is produced in  
 176 a state containing a  $\bar{b}$ -quark, given the value of the cone charge  $Q_x$ . An equivalent probability for the  
 177  $b$ -quark case is defined as  $P(\bar{B}|Q_x)$ . Using the  $B^\pm$  calibration samples,  $P(Q_x|B^\pm)$  for each tagging method  
 178 used can be defined. The probability to tag a  $B_s^0$  meson as containing a  $\bar{b}$ -quark is therefore given as  
 179  $P(B|Q_x) = P(Q_x|B^+) / (P(Q_x|B^+) + P(Q_x|B^-))$ , and correspondingly  $P(\bar{B}|Q_x) = 1 - P(B|Q_x)$ . If there  
 180 is no OST information available for a given  $B_s^0$  meson, a probability of 0.5 is assigned to that candidate.

181 The OST algorithms used in the analysis are described below, noting that the same algorithms are used  
 182 for the calibrations using  $B^\pm$  mesons, and as applied to  $B_s^0$  meson candidates to infer the initial flavour.

### 183 Muon tagging

184 For muon-based tagging, at least one additional muon is required in the event, with  $p_T > 2.5$  GeV,  
 185  $|\eta| < 2.5$  and with  $|\Delta z| < 5$  mm, where  $|\Delta z|$  is the difference in  $z$  between the primary vertex and the  
 186 longitudinal impact parameter of the ID track associated to the muon. Muons are classified and kept



187 if their identification quality selection working point is either *Tight*<sup>†</sup> or *Low- $p_T$* <sup>‡</sup>, these categories are  
 188 subsequently treated as distinct flavour tagging methods. For muons with  $p_T > 4$  GeV, Tight muons are  
 189 the dominant category, with the Low- $p_T$  requirement typically identifying muons of  $p_T < 4$  GeV. In  
 190 the case of multiple muons passing selection criteria in one event, Tight muons are chosen over Low- $p_T$   
 191 muons. Within the same muon category, the muon with the highest  $p_T$  that passes the selections is used.

192 A muon cone charge variable,  $Q_\mu$ , is constructed in the same way as Eq. 1, with  $\kappa = 1.1$  and the sum  
 193 over the reconstructed ID tracks within a cone,  $\Delta R = 0.5$ , around the muon direction. These tracks must  
 194 have  $p_T > 0.5$  GeV,  $|\eta| < 2.5$ , and  $|\Delta z| < 5$  mm. Tracks associated with the decay of a  $B$  meson signal  
 195 candidate are excluded from the sum. In each interval of  $Q_\mu$ , a fit to the  $J/\psi K^\pm$  invariant mass spectrum  
 196 is performed and the number of signal events extracted. The fit model used is described in Section 4.1.  
 197 Figure 2 shows the distributions of the muon cone charge using  $B^\pm$  signal candidates for Tight muons, and  
 198 includes the tagging probability as a function of the cone charge variable. The corresponding distributions  
 199 for Low- $p_T$  muons are shown in Figure 3.

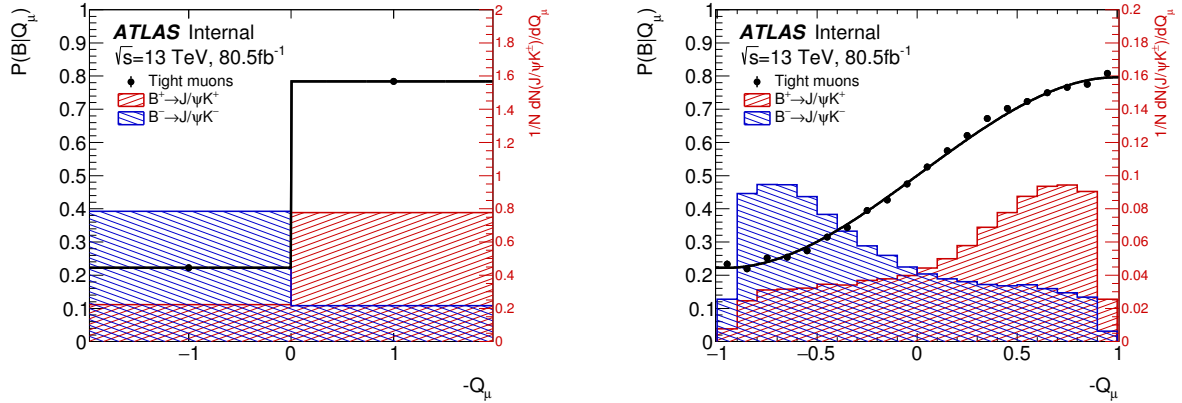


Figure 2: Cone charge distributions,  $Q_\mu$ , for Tight muons, shown for cases of discrete charge (left), and for the continuous distribution (right). For each plot, in red (blue), the normalised  $B^+$  ( $B^-$ ) cone charge distribution is shown (corresponding to the right axis scale). Superimposed is the distribution of the tagging probability,  $P(B|Q_\mu)$ , as a function of the cone charge, derived from a data sample of  $B^\pm \rightarrow J/\psi K^\pm$ , and defined as the probability to have a  $B^+$  meson (on the signal-side) given a particular cone charge  $Q_\mu$ . The fitted parametrization, shown in black, is used as the calibration curve to infer the probability to have a  $B_s^0$  or  $\bar{B}_s^0$  meson at production in the decays to  $J/\psi \phi$ .

## 200 Electron tagging

201 Electrons are identified using inner detector and calorimeter information, which satisfy the *Medium*  
 202 electron quality criteria [23]. The inner detector track associated with the electron is required to have  
 203  $p_T > 0.5$  GeV,  $|\eta| < 2.5$ , and  $|\Delta z| < 5$  mm. To reject electrons from the signal-side of the decay, electrons  
 204 with opening angle between the  $B$  meson candidate and electron momenta,  $\zeta_b$ , of  $\cos(\zeta_b) > 0.93$  are not

<sup>†</sup> Tight muon reconstruction is optimised to maximise the purity of muons at the cost of some efficiency, requiring combined muons with hits in at least two stations of the MS and additional criteria, described in Ref. [22].

<sup>‡</sup> This working point is optimized to provide good muon reconstruction efficiency down to a  $p_T$  of  $\approx 3$  GeV, while controlling the fake rate. It allows  $\geq 1$  ( $\geq 2$ ) MDT station tracks up to  $|\eta| < 1.3$  ( $1.3 < |\eta| < 1.55$ ) for candidates reconstructed by algorithms utilizing inside-out combined reconstruction [22]. Additional cuts on the number of precision stations and on variables very sensitive to the decays in flight of hadrons are also applied to suppress fakes.

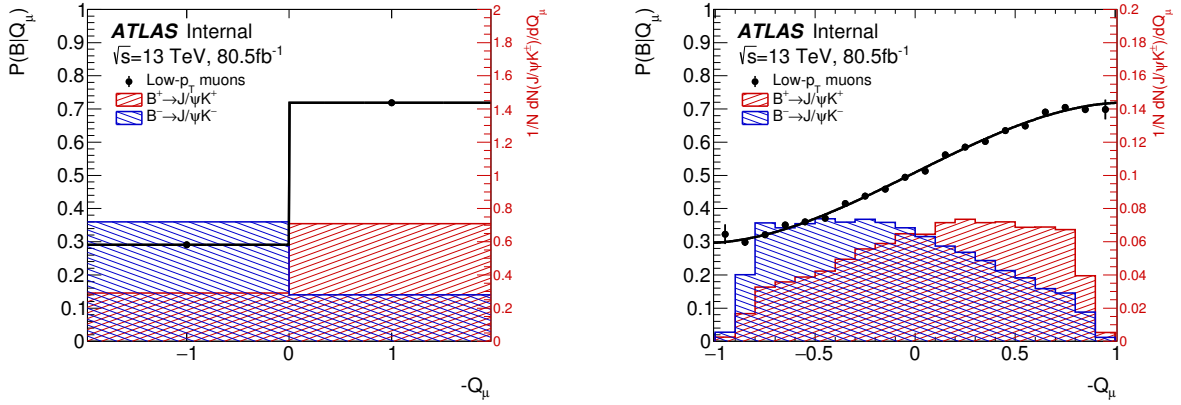


Figure 3: Normalised cone charge distributions,  $Q_\mu$ , for  $B^+$  ( $B^-$ ) events shown in red (blue) for Low- $p_T$  muons, for cases of discrete charge (left), and for the continuous distribution (right). Superimposed is the distribution of the tagging probability,  $P(B|Q_\mu)$ .

205 considered. In the case of more than one electron passing the selection, the electron with the highest  $p_T$  is  
 206 chosen. Charged-particle tracks within a cone of size  $\Delta R = 0.5$  are used to form the electron cone charge  
 207  $Q_e$ , constructed in the same way as Eq. 1, with  $\kappa = 1.0$ . The resulting electron cone charge distributions  
 208 are shown in Figure 4, together with the corresponding tagging probability.

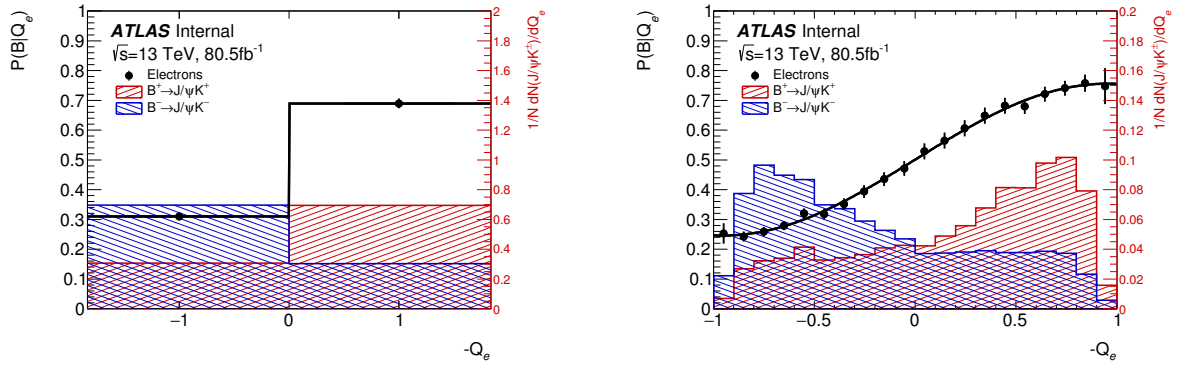


Figure 4: Normalised cone charge distributions,  $Q_e$ , for  $B^+$  ( $B^-$ ) events shown in red (blue) for electrons, for cases of discrete charge (left), and the continuous distribution (right). Superimposed is the distribution of the tagging probabilities,  $P(B|Q_e)$ .

## 209 Jet tagging

210 In the absence of a muon or electron, a jet identified as containing a  $b$ -hadron is required. Jets are  
 211 reconstructed from calorimetric information using the anti- $k_t$  algorithm [24, 25] with a radius parameter  
 212  $R = 0.4$ . The identification of a  $b$ -tagged jet uses a multivariate algorithm  $MV2c10$  [26], utilising boosted  
 213 decision trees (BDT), which output a classifier value. Jets are selected that exceed the BDT classifier  
 214 output value of 0.56. This value is optimised to maximise the tagging power of the calibration sample.

215 In the case of multiple selected jets, the jet with the highest value of the multivariate output classifier is  
 216 used. Jets associated to the signal decay are not considered in this selection.

217 Tracks within a cone of size  $\Delta R = 0.5$  of the jet axis are used to define a jet cone charge,  $Q_{\text{jet}}$ , constructed  
 218 in the same way as Eq. 1, where  $\kappa = 1.1$  and the sum is over the tracks associated with the jet, with  
 219  $|\Delta z| < 5$  mm, and excluding tracks from the decay of the signal  $B$  meson candidate. The signal yields  
 220 are extracted from the data from fits to the  $J/\psi K^\pm$  invariant mass spectrum, using the same procedure  
 221 described for muon tagging. Figure 5 shows the distribution of the opposite side jet cone charge for  $B^\pm$   
 222 signal candidates.

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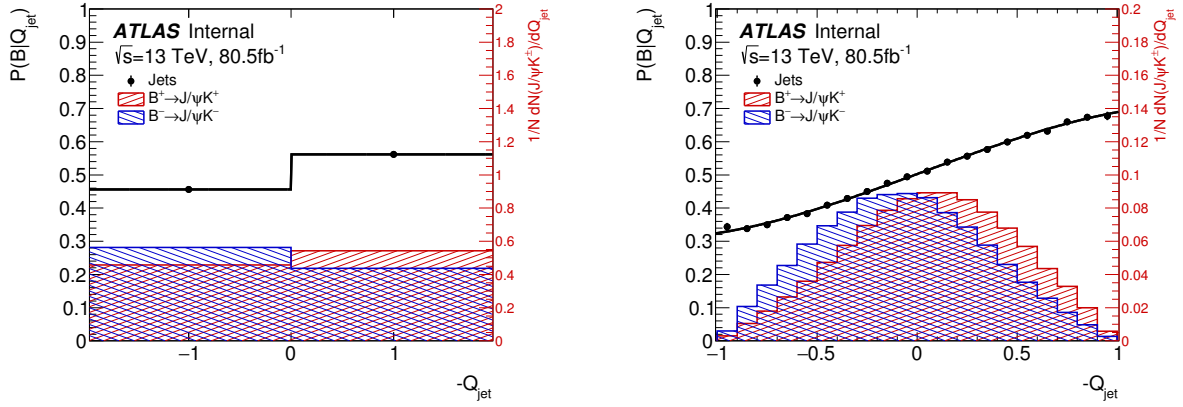


Figure 5: Normalised cone charge distributions,  $Q_{\text{jet}}$ , for  $B^+$  ( $B^-$ ) events shown in red (blue) for jets, for cases of discrete charge (left), and the continuous distribution (right). Superimposed is the distribution of the tag probability,  $P(B|Q_{\text{jet}})$ .

### 223 4.3 Flavour tagging performance

224 In order to quantify and compare the performance of the various tagging methods, three figure-of-merit  
 225 terms are constructed, which describe: the fraction of events used by a given tagging method, the purity  
 226 of the method, and the overall power of the tagging method in the sample. The efficiency,  $\epsilon_x$ , of an  
 227 individual tagging method is defined as the fraction of signal events tagged by that method compared to  
 228 the total number of signal events in the sample. The purity of a particular flavour tagging method, called  
 229 the dilution, is defined as  $\mathcal{D}(Q_x) = 2P(B|Q_x) - 1$ . The tagging power of a particular tagging method is  
 230 then defined as  $T_x = \sum_i \epsilon_{xi} \cdot \mathcal{D}^2(Q_{xi})$ , where the sum is over the probability distribution in intervals of  
 231 the cone charge variable. An effective dilution,  $D_x = \sqrt{T_x/\epsilon_x}$ , is calculated from the measured tagging  
 232 power and efficiency.

233 By definition, there is no overlap between lepton-tagged and jet-charge-tagged events. The overlap  
 234 between events with both a muon (either Tight or Low- $p_T$ ) and electron, corresponds to around 0.6% of  
 235 all tagged events. In the case of multiply-tagged events, the OST method is selected in order: Tight muon,  
 236 electron, Low- $p_T$  muon, jet. However, the ordering of muon- and electron-tagged events is shown to have  
 237 negligible impact on the final results. A summary of the tagging performance for each method and the  
 238 overall performance on the  $B^\pm$  sample is given in Table 1.

Table 1: Summary of tagging performances for the different flavour tagging methods on the sample of  $B^\pm$  signal candidates, as described in the text. Uncertainties shown are statistical only. The efficiency ( $\epsilon_x$ ) and tagging power ( $T_x$ ) are each determined by summing over the individual bins of the cone charge distribution. The effective dilution ( $D_x$ ) is obtained from the measured efficiency and tagging power. For the efficiency, effective dilution, and tagging power, the corresponding uncertainty is determined by combining the appropriate uncertainties in the individual bins of each charge distribution.

Tag method	$\epsilon_x$ [%]	$D_x$ [%]	$T_x$ [%]
Tight muon	$4.50 \pm 0.01$	$43.8 \pm 0.2$	$0.862 \pm 0.009$
Electron	$1.57 \pm 0.01$	$41.8 \pm 0.2$	$0.274 \pm 0.004$
Low- $p_T$ muon	$3.12 \pm 0.01$	$29.9 \pm 0.2$	$0.278 \pm 0.006$
Jet	$12.04 \pm 0.02$	$16.6 \pm 0.1$	$0.334 \pm 0.006$
Total	$21.23 \pm 0.03$	$28.7 \pm 0.1$	$1.75 \pm 0.01$

#### 4.4 Using tag information in the $B_s^0$ fit

For the maximum likelihood fit performed on the  $B_s^0$  data, and described in detail in Section 5, the per-candidate probability,  $P(B|Q_x)$ , that the  $B$  meson candidate was produced in a state  $B_s^0$  (versus a  $\bar{B}_s^0$ ) is provided using the calibrations derived from the  $B^\pm \rightarrow J/\psi K^\pm$  sample, described above, and shown in Figures 2–5. As the distributions of  $P(B|Q_x)$  from signal  $B_s^0$  mesons and background data can be expected to be different, separate probability density functions (PDFs) are necessary to describe these distributions in the likelihood function. These PDFs are defined as  $P_s(P(B|Q_x))$  and  $P_b(P(B|Q_x))$ , describing the probability distributions for signal and background, respectively, and are extracted using the sample of  $B_s^0$  candidates. The PDFs consist of the fraction of events that are tagged with a particular method (or are untagged), the fractions of those events categorised as discrete or continuous, and for those that are continuous, a PDF of the corresponding probability distribution.

#### Continuous PDF

The parametrisations of the continuous PDF components of  $P_{s,b}(P(B|Q_x))$  for each OST method are defined as follows: In the sideband regions,  $5.150 < m(J/\psi KK) < 5.317$  GeV and  $5.417 < m(J/\psi KK) < 5.650$  GeV, unbinned maximum likelihood fits are performed to  $P(B|Q_x)$  distributions to extract the background (continuous category) PDFs for  $P_b(P(B|Q_x))$ . For the Tight muon and electron methods, the parametrisation has the form of the sum of a second-order polynomial and two exponential functions. A Gaussian function is used for the Low- $p_T$  muons. For the jet tagging algorithm an eighth-order polynomial is used.

For the signal, fits are performed to the  $P(B|Q_x)$  distributions, using all events in the  $m(J/\psi KK)$  distributions to extract the signal (continuous category) PDFs for  $P_s(P(B|Q_x))$ . In these fits, the previously extracted parameters to describe the background PDFs are fixed, as is the relative normalisation of signal and background, extracted from a fit to the  $m(J/\psi KK)$  distribution. For the signal PDFs, the Tight muon tagging method uses the sum of two exponential functions and a constant function to describe the signal. For the electron tagging method, the signal function has the form of the sum of a second-order polynomial and two exponential functions, and for the Low- $p_T$  muon and jet tagging methods a Gaussian function is used.

266 **Discrete PDF**

267 In the case where the cone charge is discrete, the fractions of events  $f_{+1}$  ( $f_{-1}$ ) with cone charges +1 (−1)  
 268 are determined separately for signal and background using events from the signal and sideband regions  
 269 of the  $B_s^0$  mass distribution (as defined in Section 3). The remaining fraction of events,  $1 - f_{+1} - f_{-1}$ ,  
 270 corresponds to the continuous parts of the distribution. Positive and negative charges are equally probable  
 271 for background candidates formed from a random combination of a  $J/\psi$  and a pair of tracks, but this is not  
 272 necessarily the case for background candidates formed from a partially reconstructed  $b$ -hadron. Table 2  
 273 summarises for the different tagg methods, the fractions  $f_{+1}$  and  $f_{-1}$  obtained for signal and background  
 events.

Table 2: Fractions  $f_{+1}$  and  $f_{-1}$  of events with cone charges of +1 and −1 respectively, for signal and background events and for the different tagging methods. Only statistical uncertainties are given.

Tag method	Signal		Background	
	$f_{+1}$ [%]	$f_{-1}$ [%]	$f_{+1}$ [%]	$f_{-1}$ [%]
Tight muon	$6.9 \pm 0.3$	$7.5 \pm 0.3$	$4.7 \pm 0.1$	$4.9 \pm 0.1$
Electron	$20 \pm 1$	$19 \pm 1$	$16.8 \pm 0.2$	$17.3 \pm 0.2$
Low- $p_T$ muon	$10.9 \pm 0.5$	$11.6 \pm 0.5$	$7.0 \pm 0.1$	$7.5 \pm 0.1$
Jet	$3.60 \pm 0.15$	$3.54 \pm 0.15$	$3.05 \pm 0.03$	$3.17 \pm 0.03$

274

275 The relative fractions of signal and background events tagged using the different OST methods are found  
 276 using a similar sideband-subtraction method, and are summarised in Table 3.

Table 3: Relative fractions of signal and background events tagged using the different methods. The efficiencies include both the continuous and discrete contributions. Only statistical uncertainties are quoted.

Tag method	Signal efficiency [%]	Background efficiency [%]
Tight muon	$4.06 \pm 0.06$	$3.21 \pm 0.01$
Electron	$1.86 \pm 0.04$	$1.48 \pm 0.01$
Low- $p_T$ muon	$2.95 \pm 0.05$	$2.70 \pm 0.01$
Jet	$12.1 \pm 0.1$	$9.41 \pm 0.02$
Untagged	$79.1 \pm 0.3$	$83.20 \pm 0.05$

277 To account for possible deviations between data and the selected fit models, variations of the procedure  
 278 described here are used to determine systematic uncertainties, as described in Section 6.

279 **5 Maximum likelihood fit**

280 An unbinned maximum-likelihood fit is performed on the selected events to extract the parameter values  
 281 of the  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$  decay. The fit uses information about the reconstructed mass  $m$ , the  
 282 measured proper decay time  $t$ , the measured proper decay time uncertainty  $\sigma_t$ , the tagging probability,  
 283  $P(B|Q_x)$ , and the transversity angles  $\Omega$  of each  $B_s^0 \rightarrow J/\psi\phi$  decay candidate. The measured proper  
 284 decay time uncertainty  $\sigma_t$  is calculated from the covariance matrix associated with the vertex fit for each

285 candidate event. The transversity angles  $\Omega = (\theta_T, \psi_T, \phi_T)$  are defined in Section 5.1. The likelihood  
 286 function is defined as a combination of the signal and background PDFs as follows:

$$\begin{aligned} \ln \mathcal{L} = \sum_{i=1}^N w_i \cdot \ln [ & f_s \cdot \mathcal{F}_s(m_i, t_i, \sigma_{m_i}, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) + f_s \cdot f_{B^0} \cdot \mathcal{F}_{B^0}(m_i, t_i, \sigma_{m_i}, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) \\ & + f_s \cdot f_{\Lambda_b} \cdot \mathcal{F}_{\Lambda_b}(m_i, t_i, \sigma_{m_i}, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) \\ & + (1 - f_s \cdot (1 + f_{B^0} + f_{\Lambda_b})) \mathcal{F}_{\text{bkg}}(m_i, t_i, \sigma_{m_i}, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) ], \end{aligned} \quad (2)$$

287 where  $N$  is the number of selected candidates,  $w_i$  is a weighting factor to account for the trigger efficiency  
 288 (described in Section 5.3).  $\mathcal{F}_s$ ,  $\mathcal{F}_{B^0}$ ,  $\mathcal{F}_{\Lambda_b}$  and  $\mathcal{F}_{\text{bkg}}$  are the PDFs modelling the signal,  $B^0$  background,  $\Lambda_b$   
 289 background, and the other background distributions, respectively. The term  $f_s$  is the fraction of signal  
 290 candidates and  $f_{B^0}$  and  $f_{\Lambda_b}$  are the background fractions of  $B^0$  mesons and  $\Lambda_b$  baryons misidentified as  
 291  $B_s^0$  candidates, calculated relative to the number of signal events. These background fractions are fixed  
 292 to their expectation from the MC simulation, and variations are applied as part of the evaluation of the  
 293 effects of systematic uncertainties. The mass  $m_i$ , the proper decay time  $t_i$  and the decay angles  $\Omega_i$  are the  
 294 values measured from the data for each event  $i$ . A detailed description of the signal PDF terms in Eq. (2)  
 295 is given in Section 5.1. The three background functions are described in Section 5.2.

## 296 5.1 Signal PDF

297 The PDF used to describe the signal events,  $\mathcal{F}_s$ , has the following composition:

$$\begin{aligned} \mathcal{F}_s(m_i, t_i, \sigma_{m_i}, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) = & P_s(m_i, \sigma_{m_i}) \cdot P_s(\sigma_{m_i}) \cdot P_s(\Omega_i, t_i, P_i(B|Q_x), \sigma_{t_i}) \\ & \cdot P_s(\sigma_{t_i}) \cdot P_s(P_i(B|Q_x)) \cdot A(\Omega_i, p_{T_i}) \cdot P_s(p_{T_i}). \end{aligned}$$

298 The mass term  $P_s(m_i, \sigma_{m_i})$  is modelled in the following way:

$$P_s(m_i, \sigma_{m_i}) \equiv \frac{1}{\sqrt{2\pi} S_m \sigma_{m_i}} \cdot e^{\frac{-(m_i - m_{B_s^0})^2}{2(S_m \sigma_{m_i})^2}}. \quad (3)$$

299 The term  $P_s(m_i, \sigma_{m_i})$  uses per-candidate mass errors,  $\sigma_{m_i}$ , calculated for each  $J/\psi\phi$  candidate from the  
 300 covariance matrix associated with the 4-track vertex fit. Each measured candidate mass is convoluted by a  
 301 Gaussian function with a width equal to  $\sigma_{m_i}$  multiplied by a scale factor  $S_m$ , introduced to account for any  
 302 mismeasurements. Both  $S_m$  and the mean value  $m_{B_s^0}$ , which is the  $B_s^0$  meson mass, are free parameters  
 303 determined in the fit.

304 The probability terms  $P_s(\sigma_{m_i})$ ,  $P_s(\sigma_{t_i})$  and  $P_s(p_{T_i})$  are introduced to account for differences between  
 305 signal and background events for the values of the per-candidate mass error, time error and  $p_{T_i}$  values,  
 306 respectively. Distributions of these variables for signal and background are described by gamma functions  
 307 and the method is unchanged from the analysis explained in Ref. [27]. The tagging probability term for  
 308 signal  $P_s(P_i(B|Q_x))$  is described in Section 4.4. The term  $A(\Omega_i, p_{T_i})$  is the acceptance function, described  
 309 at the end of the current Section 5.1.



310 The term  $P_s(\Omega_i, t_i, P_i(B|Q_x), \sigma_{t_i})$  is a joint PDF for the decay time  $t$  and the transversity angles  $\Omega$  for the  
 311  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$  decay. Ignoring detector effects, the distribution for the time  $t$  and the angles  
 312  $\Omega$  is given by the differential decay rate [28]:

$$\frac{d^4\Gamma}{dt d\Omega} = \sum_{k=1}^{10} O^{(k)}(t) g^{(k)}(\theta_T, \psi_T, \phi_T),$$

313 where  $O^{(k)}(t)$  are the time-dependent functions corresponding to the contributions of the four different  
 314 amplitudes ( $A_0$ ,  $A_{\parallel}$ ,  $A_{\perp}$ , and  $A_S$ ) and their interference terms, and  $g^{(k)}(\theta_T, \psi_T, \phi_T)$  are the angular  
 315 functions. Table 4 shows the time-dependent and the angular functions of the transversity angles. The  
 316 formulae for the time-dependent functions have the same structure for  $B_s^0$  and  $\bar{B}_s^0$  but with a sign reversal  
 317 in the terms containing  $\Delta m_s$ , which is a fixed parameter of the fit (using Ref. [21]). The formalism  
 318 used throughout this analysis assumes no direct CP violation. In Table 4, the parameter  $A_{\perp}(t)$  is the  
 319 time-dependent amplitude for the CP-odd final-state configuration while  $A_0(t)$  and  $A_{\parallel}(t)$  correspond  
 320 to CP-even final-state configurations. The amplitude  $A_S(t)$  gives the contribution from the CP-odd  
 321 non-resonant  $B_s^0 \rightarrow J/\psi K^+ K^-$  S-wave state (which includes the  $f_0$ ). The corresponding functions are  
 322 given in the last four lines of Table 4 ( $k = 7-10$ ). The amplitudes are parametrised by  $|A_i|e^{i\delta_i}$ , where  
 323  $i = \{0, \parallel, \perp, S\}$ , with  $\delta_0 = 0$  and are normalised such that  $|A_0(0)|^2 + |A_{\perp}(0)|^2 + |A_{\parallel}(0)|^2 = 1$ .  $|A_{\perp}(0)|$   
 324 is determined according to this condition, while the remaining three amplitudes are parameters of the fit.  
 325 The phase  $\delta_S$  is the phase difference between  $A_S(0)$  and  $A_0(0)$  at the resonance peak.  $|A_S|^2$  gives the ratio  
 326 of non-resonant over resonant yield in the interval of  $m(K^+K^-)$  used in the analysis. In the sum over the  
 327 mass interval, the interference terms (lines 8 – 10 in Table 4) are corrected by a factor  $\alpha = 0.51 \pm 0.02$  that  
 328 takes into account the mass-dependent differences in absolute amplitude and phase between the resonant  
 329 and the S-wave amplitudes. The correction is based on the Breit-Wigner description of the resonance  
 330 and on the assumption of uniform  $A_S$ . The uncertainty on the value of  $\alpha$  has been calculated based on  
 331 the Flatté parametrisation [Flatte:1976xu] and the corresponding systematic uncertainty is explained in  
 332 Section 6.

333 The angles  $(\theta_T, \psi_T, \phi_T)$ , are defined in the rest frames of the final-state particles. The  $x$ -axis is determined  
 334 by the direction of the  $\phi$  meson in the  $J/\psi$  rest frame, and the  $K^+K^-$  system defines the  $x$ - $y$  plane, where  
 335  $p_y(K^+) > 0$ . The three angles are defined as:

- 336 •  $\theta_T$ , the angle between  $\vec{p}(\mu^+)$  and the normal to the  $x$ - $y$  plane, in the  $J/\psi$  meson rest frame,
- 337 •  $\phi_T$ , the angle between the  $x$ -axis and  $\vec{p}_{xy}(\mu^+)$ , the projection of the  $\mu^+$  momentum in the  $x$ - $y$  plane,  
 338 in the  $J/\psi$  meson rest frame,
- 339 •  $\psi_T$ , the angle between  $\vec{p}(K^+)$  and  $-\vec{p}(J/\psi)$  in the  $\phi$  meson rest frame.

340 The PDF term  $P_s(\Omega_i, t_i, P_i(B|Q_x), \sigma_{t_i})$  takes into account the lifetime resolution, so each time element  
 341 in Table 4 is smeared with a Gaussian function. This smearing is performed numerically on an event-by-  
 342 event basis where the width of the Gaussian function is the proper decay time uncertainty, measured for  
 343 each event, multiplied by a scale factor to account for any mismeasurements. The average value of this  
 344 uncertainty for signal events is 69 fs.

345 The angular acceptance of the detector and the kinematic cuts on the angular distributions are included  
 346 in the likelihood function through  $A(\Omega_i, p_{Ti})$ . This is calculated using a 4D binned acceptance method,  
 347 applying an event-by-event efficiency according to the transversity angles  $(\theta_T, \psi_T, \phi_T)$  and the  $p_T$  of the  
 348 candidate. The  $p_T$  binning is necessary, because the angular acceptance is influenced by the  $p_T$  of the  $B_s^0$

349 candidate. The acceptance is calculated from the  $B_s^0 \rightarrow J/\psi\phi$  MC events with additional weighting for  
 350  $p_T$  and  $\eta$  distributions. In the likelihood function, the acceptance is treated as an angular acceptance PDF,  
 351 which is multiplied with the time- and angle-dependent PDF describing the  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$   
 352 decays. As both the acceptance and time- and angle-dependent decay PDFs depend on the transversity  
 353 angles they must be normalised together. This normalisation is done numerically during the likelihood  
 354 fit. The PDF is normalised over the entire  $B_s^0$  mass range, 5.150–5.650 GeV.

## 355 5.2 Background PDF

356 The background PDF has the following composition:

$$\begin{aligned} \mathcal{F}_{\text{bkg}}(m_i, t_i, \sigma_{t_i}, \Omega_i, P_i(B|Q_x), p_{T_i}) &= P_b(m_i) \cdot P_b(t_i|\sigma_{t_i}) \cdot P_b(P_i(B|Q_x)) \\ &\cdot P_b(\Omega_i) \cdot P_b(\sigma_{t_i}) \cdot P_b(p_{T_i}). \end{aligned}$$

357 The proper decay time function  $P_b(t_i|\sigma_{t_i})$  is parametrized as a prompt peak modelled by a Gaussian  
 358 distribution, two positive exponential functions and a negative exponential function. These functions are  
 359 smeared with the same resolution function as the signal decay time-dependence. The prompt peak models  
 360 the combinatorial background events, which are expected to have reconstructed lifetimes distributed  
 361 around zero. The two positive exponential functions represent a fraction of longer-lived backgrounds with  
 362 non-prompt  $J/\psi$ , combined with hadrons from the primary vertex or from a  $B/D$  meson in the same event.  
 363 The negative exponential function takes into account events with poor vertex resolution. The probability  
 364 terms,  $P_b(\sigma_{t_i})$  and  $P_b(p_{T_i})$ , are described by gamma functions. They are unchanged from the analysis  
 365 described in Ref. [27] and explained in detail there. The tagging probability term for background events  
 366  $P_b(P_i(B|Q_x))$  is described in Section 4.4.

367 The shape of the background angular distribution,  $P_b(\Omega_i)$  arises primarily from detector and kinematic  
 368 acceptance effects. The best description has been achieved by Legendre polynomial functions:

$$\begin{aligned} Y_l^m(\theta_T) &= \sqrt{(2l+1)/(4\pi)} \sqrt{(l-m)!/(l+m)!} P_l^{|m|}(\cos\theta_T) \\ P_k(x) &= \frac{1}{2^k k!} \frac{d^k}{dx^k} (x^2 - 1)^k \end{aligned} \quad (4)$$

$$\mathcal{P}_b(\theta_T, \psi_T, \phi_T) = \sum_{k=0}^{14} \sum_{l=0}^{14} \sum_{m=-l}^l \begin{cases} a_{k,l,m} \sqrt{2} Y_l^m(\theta_T) \cos(m\phi_T) P_k(\cos\psi_T) & \text{where } m > 0 \\ a_{k,l,m} \sqrt{2} Y_l^{-m}(\theta_T) \sin(m\phi_T) P_k(\cos\psi_T) & \text{where } m < 0 \\ a_{k,l,m} \sqrt{2} Y_l^0(\theta_T) P_k(\cos\psi_T) & \text{where } m = 0 \end{cases}$$

369 where the coefficients  $a_{k,l,m}$  are adjusted to give the best fit to the angular distributions for events in the  
 370 sidebands of the  $B_s^0$  mass distribution. These parameters are then fixed in the main fit, defined by Eq. (2).  
 371 The  $B_s^0$  mass interval used for the background fit is between 5.150 and 5.650 GeV excluding the signal  
 372 mass region  $|(m(B_s^0) - 5.366)| < 0.110$  GeV. Higher order Legendre polynomial functions were tested as  
 373 a systematic check, described in Section 6.

374 The background mass model,  $P_b(m_i)$  is an exponential function with a constant term added.

375 Contamination from  $B_d \rightarrow J/\psi K^{0*}$  and  $\Lambda_b \rightarrow J/\psi p K^-$  events mis-reconstructed as  $B_s^0 \rightarrow J/\psi\phi$  is  
 376 accounted for in the fit through the  $\mathcal{F}_{B^0}$  and  $\mathcal{F}_{\Lambda_b}$  terms in the PDF function described in Eq. (2). The  
 377 fractions of these contributions,  $f_{B^0} = (4.3 \pm 0.5)\%$  and  $f_{\Lambda_b} = (2.1 \pm 0.6)\%$ , are defined relative to the  
 378 number of the  $B_s^0 \rightarrow J/\psi\phi$  signal events and are evaluated from MC simulation using production cross



Table 4: The ten time-dependent functions,  $\mathcal{O}^{(k)}(t)$  and the functions of the transversity angles  $g^{(k)}(\theta_T, \psi_T, \phi_T)$ . The amplitudes  $|A_0(0)|^2$  and  $|A_{\parallel}(0)|^2$  are for the  $CP$ -even components of the  $B_S^0 \rightarrow J/\psi\phi$  decay,  $|A_{\perp}(0)|^2$  is the  $CP$ -odd amplitude; they have corresponding strong phases  $\delta_0, \delta_{\parallel}$  and  $\delta_{\perp}$ . By convention,  $\delta_0$  is set to be zero. The  $S$ -wave amplitude  $|A_S(0)|^2$  gives the fraction of  $B_S^0 \rightarrow J/\psi K^+ K^- (\bar{f}_0)$  and has a related strong phase  $\delta_S$ . The factor  $\alpha$  is described in the text of Section 5.1. The  $\pm$  and  $\mp$  terms denote two cases: the upper sign describes the decay of a meson that was initially a  $B_S^0$  meson, while the lower sign describes the decays of a meson that was initially  $\bar{B}_S^0$ .

$k$	$\mathcal{O}^{(k)}(t)$	$g^{(k)}(\theta_T, \psi_T, \phi_T)$
1	$\frac{1}{2}  A_0(0) ^2 \left[ (1 + \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 - \cos\phi_S) e^{-\Gamma_H^{(S)} t} \pm 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$2 \cos^2 \psi_T (1 - \sin^2 \theta_T \cos^2 \phi_T)$
2	$\frac{1}{2}  A_{\parallel}(0) ^2 \left[ (1 + \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 - \cos\phi_S) e^{-\Gamma_H^{(S)} t} \pm 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$\sin^2 \psi_T (1 - \sin^2 \theta_T \sin^2 \phi_T)$
3	$\frac{1}{2}  A_{\perp}(0) ^2 \left[ (1 - \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 + \cos\phi_S) e^{-\Gamma_H^{(S)} t} \mp 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$\sin^2 \psi_T \sin^2 \theta_T$
4	$\frac{1}{2}  A_0(0)  A_{\parallel}(0)  \cos\delta_{\parallel} \left[ (1 + \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 - \cos\phi_S) e^{-\Gamma_H^{(S)} t} \pm 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$\frac{1}{\sqrt{2}} \sin 2\psi_T \sin^2 \theta_T \sin 2\phi_T$
5	$ A_{\parallel}(0)  A_{\perp}(0)  \left[ \frac{1}{2} (e^{-\Gamma_L^{(S)} t} - e^{-\Gamma_H^{(S)} t}) \cos(\delta_{\perp} - \delta_{\parallel}) \sin\phi_S \pm e^{-\Gamma_S t} (\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_S t) - \cos(\delta_{\perp} - \delta_{\parallel}) \cos\phi_S \sin(\Delta m_S t)) \right]$	$-\sin^2 \psi_T \sin 2\theta_T \sin\phi_T$
6	$ A_0(0)  A_{\perp}(0)  \left[ \frac{1}{2} (e^{-\Gamma_L^{(S)} t} - e^{-\Gamma_H^{(S)} t}) \cos\delta_{\perp} \sin\phi_S \pm e^{-\Gamma_S t} (\sin\delta_{\perp} \cos(\Delta m_S t) - \cos\delta_{\perp} \cos\phi_S \sin(\Delta m_S t)) \right]$	$\frac{1}{\sqrt{2}} \sin 2\psi_T \sin 2\theta_T \cos\phi_T$
7	$\frac{1}{2}  A_S(0) ^2 \left[ (1 - \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 + \cos\phi_S) e^{-\Gamma_H^{(S)} t} \mp 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$\frac{2}{3} (1 - \sin^2 \theta_T \cos^2 \phi_T)$
8	$\alpha  A_S(0)  A_{\parallel}(0)  \left[ \frac{1}{2} (e^{-\Gamma_L^{(S)} t} - e^{-\Gamma_H^{(S)} t}) \sin(\delta_{\parallel} - \delta_S) \sin\phi_S \pm e^{-\Gamma_S t} (\cos(\delta_{\parallel} - \delta_S) \cos(\Delta m_S t) - \sin(\delta_{\parallel} - \delta_S) \cos\phi_S \sin(\Delta m_S t)) \right]$	$\frac{1}{3} \sqrt{6} \sin\psi_T \sin^2 \theta_T \sin 2\phi_T$
9	$\frac{1}{2} \alpha  A_S(0)  A_{\perp}(0)  \sin(\delta_{\perp} - \delta_S) \left[ (1 - \cos\phi_S) e^{-\Gamma_L^{(S)} t} + (1 + \cos\phi_S) e^{-\Gamma_H^{(S)} t} \mp 2e^{-\Gamma_S t} \sin(\Delta m_S t) \sin\phi_S \right]$	$\frac{1}{3} \sqrt{6} \sin\psi_T \sin 2\theta_T \cos\phi_T$
10	$\alpha  A_0(0)  A_S(0)  \left[ \frac{1}{2} (e^{-\Gamma_H^{(S)} t} - e^{-\Gamma_L^{(S)} t}) \sin\delta_S \sin\phi_S \pm e^{-\Gamma_S t} (\cos\delta_S \cos(\Delta m_S t) + \sin\delta_S \cos\phi_S \sin(\Delta m_S t)) \right]$	$\frac{4}{3} \sqrt{3} \cos\psi_T (1 - \sin^2 \theta_T \cos^2 \phi_T)$

sections and branching fractions from Refs. [21, 29–33]. MC simulated events are also used to determine the shape of the mass and transversity angle distributions. The 3D angular distributions of  $B_d^0 \rightarrow J/\psi K^{0*}$  and of the conjugate decay are modelled using input from Ref. [34], while angular distributions for  $\Lambda_b \rightarrow J/\psi p K^-$  and the conjugate decay are considered flat. These distributions are sculpted for detector acceptance effects and then described by Legendre polynomial functions, Eq. (4). These shapes are used as templates in the fit. The  $B_d$  and  $\Lambda_b$  lifetimes are accounted for in the fit by adding additional exponential terms, scaled by the ratio of  $B_d/B_s^0$  or  $\Lambda_b/B_s^0$  masses as appropriate, where the lifetimes and masses are taken from Ref. [21]. Systematic uncertainties due to the background from  $B_d \rightarrow J/\psi K^{0*}$  and  $\Lambda_b \rightarrow J/\psi p K^-$  decays are described in Section 6. The contribution of the  $S$ -wave  $B_d \rightarrow J/\psi K \pi$  decays as well as their interference with the  $P$ -wave  $B_d \rightarrow J/\psi K^{0*}$  decays are included in the PDF of the fit, using the parameters measured in Ref. [34].

### 5.3 Muon trigger proper decay time-dependent efficiency

Trigger muons with high values of transverse impact parameter are especially effected by the limited tracking acceptance; this results in inefficiency at large values of the proper decay time. This inefficiency is estimated using MC simulated events, by comparing the  $B_s^0$  proper decay time distribution obtained before and after applying the trigger selection. To account for this inefficiency in the fit, the events are reweighted by a factor  $w$ :

$$w = p_0 \cdot [1 - p_1 \cdot (\text{Erf}((t - p_3)/p_2) + 1)], \quad (5)$$

where Erf denotes the error function and  $p_0, p_1, p_2$  and  $p_3$  are parameters determined in the fit to MC events. No significant bias or inefficiency due to offline track reconstruction, vertex reconstruction, or track quality selection criteria is observed.

## 6 Systematic uncertainties

Systematic uncertainties are evaluated for effects that are described below.

- Flavour tagging:** There are two contributions to the uncertainties in the fit parameters due to the flavour tagging procedure, the statistical and systematic components. The statistical uncertainty due to the size of the sample of  $B^\pm \rightarrow J/\psi K^\pm$  decays is included in the overall statistical error. The systematic uncertainty arising from the precision of the OST calibration, described in Section 4.2, is estimated by changing the models used to parametrise the probability distribution,  $P(B|Q_x)$ , as a function of the cone charge from the function used by default (a third-order polynomial for muons and a sinusoidal for electrons) to one of several alternative functions. The alternative functions are: a linear function; a fifth-order polynomial; or two third-order polynomials that describe the positive and negative regions and have common constant and linear terms, but independent quadratic and cubic terms. The  $B_s^0$  fit is repeated using the alternative models and the largest difference with respect to the nominal fit is assigned as the systematic uncertainty. To verify the calibration procedure, calibration curves are derived from simulated samples of  $B^\pm$  and  $B_s^0$  signals. The variations between the curves from these two samples are propagated to the calibration curves derived from data. The differences in the parameters between the nominal fit and that with the variations of calibration curves are included in the systematic uncertainty. An additional systematic uncertainty is assigned due to potential dependency on the pile-up distribution. The calibration data

are split into subsets of approximately equal yields, separated according to the pile-up profile of the event, and separate calibrations are made for each subset. For the  $B_s^0$  fit, the fit is repeated using the calibrations corresponding to the pile-up profile of that event. Differences between the nominal and the modified fit for the parameters of interest are taken as the systematic uncertainty. For the terms  $P_b(P(B|Q_x))$  and  $P_s(P(B|Q_x))$ , variations of the parametrisation are considered (including using histograms in place of a parametrisation). The resulting changes in the parameters of the  $B_s^0$  fit are similarly included in the systematic uncertainties.

- **Angular acceptance method:** The angular acceptance of the detector and the kinematic cuts,  $A(\Omega_i, p_{T_i})$ , described in Section 5.1, is calculated from a binned fit to MC simulated data. In order to estimate the systematic uncertainty introduced from the choice of binning, different acceptance functions are calculated using different bin widths and central values.
- **Inner detector alignment:** Residual misalignments of the ID affect the impact parameter,  $d_0$ , distribution with respect to the primary vertex. The effects on the fit parameters have been studied and observed deviations are included in the systematics uncertainties.
- **Trigger efficiency:** To correct for the proper decay time dependent inefficiencies due to the triggers, the events are re-weighted according to Eq. (5). An alternative fit is performed using different sets of binning in the MC sample used to determine the efficiency. The systematic effects are found to be negligible.
- **Best candidate selection:** The systematic uncertainty of the  $B_s^0$  fit from the selection of the candidate with the best quality in the  $\approx 5\%$  of events that are found to contain multiple candidates after cuts is estimated. In the default fit, the  $B_s^0$  candidate with the lowest  $\chi^2/\text{n.d.o.f.}$  is selected. An equivalent sample is created where the candidate with the highest  $p_T$  is selected instead. Deviations from the default fit are included in the systematics of the measurement.
- **Background angles model:** The shape of the background angular distribution,  $P_b(\theta_T, \varphi_T, \psi_T)$ , is described by the Legendre polynomial functions of 14th degree, given in Eq. (4). Alternatively, higher order Legendre polynomial functions were tested, and the differences in fit parameters relative to the default fit are taken as systematic uncertainties.

The shapes are primarily determined by detector and kinematic acceptance effects and are sensitive to the  $p_T$  of the  $B_s^0$  meson candidate. For this reason, the parametrisation using the Legendre polynomial functions is performed in six  $p_T$  intervals: 10–15 GeV, 15–20 GeV, 20–25 GeV, 25–30 GeV, 30–55 GeV and  $>55$  GeV.

The systematic uncertainties due to the choice of  $p_T$  intervals are estimated by repeating the fit, with these intervals enlarged and reduced by 1 GeV and by 2 GeV. The biggest deviations observed in the fit results were taken to represent the systematic uncertainties.

The parameters of the Legendre polynomial functions given in Eq. (4) are adjusted to give the best fit to the angular distributions for events in the  $B_s^0$  mass sidebands. To test the sensitivity of the fit results to the choice of sideband regions, the fit is repeated with alternative choices for the excluded signal mass regions:  $|(m(B_s^0) - 5.366 \text{ GeV})| > 0.085 \text{ GeV}$  and  $|(m(B_s^0) - 5.366 \text{ GeV})| > 0.160 \text{ GeV}$  (instead of the default  $|(m(B_s^0) - 5.366 \text{ GeV})| > 0.110 \text{ GeV}$ ). The differences in the fit results are assigned as systematic uncertainties.

- 457 •  **$B_d$  contribution:** The contamination from  $B_d \rightarrow J/\psi K^{0*}$  events mis-reconstructed as  $B_s^0 \rightarrow$   
 458  $J/\psi\phi$  is accounted for in the final fit. Studies are performed to evaluate the effect of the uncertainties  
 459 in the  $B_d \rightarrow J/\psi K^{0*}$  fraction and the shapes of the distributions of the mass, transversity angles,  
 460 and lifetime. In the MC events the angular distribution of the  $B_d \rightarrow J/\psi K^{0*}$  decay is modelled  
 461 using parameters taken from Ref. [34]. The contribution of the  $S$ -wave  $B_d \rightarrow J/\psi K\pi$  decays as  
 462 well as its interference with the  $P$ -wave  $B_d \rightarrow J/\psi K^{0*}$  decays are also included in the PDF of the  
 463 fit, following the parameters measured in Ref. [34]. The uncertainties of these parameters are taken  
 464 into account in the estimation of systematic uncertainty. After applying the  $B_s^0$  signal selection cuts,  
 465 the angular distributions are fitted using Legendre polynomial functions. The uncertainties of this  
 466 fit are included within the systematic uncertainty.
  - 467 •  **$\Lambda_b$  contribution:** The contamination from  $\Lambda_b \rightarrow J/\psi p K^-$  events mis-reconstructed as  $B_s^0 \rightarrow J/\psi\phi$   
 468 is accounted for in the final fit. Studies are performed to evaluate the effect of the uncertainties  
 469 in the  $\Lambda_b \rightarrow J/\psi p K^-$  fraction  $f_{\Lambda_b}$ , and the shapes of the distributions of the mass, transversity  
 470 angles, and lifetime. Additional studies are performed to determine the effect of the uncertainties  
 471 in the  $\Lambda_b \rightarrow J/\psi \Lambda^*$  branching ratios used to reweight the generated MC.
  - 472 • **Fit model mass and lifetime:** To estimate the systematic uncertainties due to the signal  $B_s^0$  mass  
 473 model, the default model has been altered by adding a second Gaussian function in Eq. (3), which  
 474 has the same structure as the first Gaussian but a different scale factor,  $S_m^1$ , which is an additional  
 475 free parameter of the fit. Respective changes in fit parameters are found negligible.
- 476 To test the sensitivity of the part of the fit model describing the lifetime, two systematic tests are  
 477 performed. The determination of signal and background lifetime errors is sensitive to the choice  
 478 of  $p_T$  bins, in which the relative contributions of these two components are evaluated. To estimate  
 479 the systematic uncertainty, the fit is repeated varying the intervals of the default  $p_T$  binning. The  
 480 determination of signal and background lifetime errors is also sensitive to the determination of the  
 481 signal fraction. The fit is repeated by varying this fraction within one standard deviation of its  
 482 uncertainty and differences are included in the systematic uncertainty.
- 483 • **Fit model  $S$ -wave phase:** As explained in Section 5.1, the model for the interference between the  
 484  $B_s^0 \rightarrow J/\psi\phi(K^+K^-)$  and the  $S$ -wave  $B_s^0 \rightarrow J/\psi K^+K^-$  is corrected by a factor  $\alpha = 0.51 \pm 0.02$  to  
 485 account for the mass-dependent differences in absolute amplitude and phase between the resonant  
 486 and  $S$ -wave amplitudes. To account for uncertainty in  $\alpha$ , the fit was repeated with  $\alpha = 0.51 + 0.02$   
 487 and  $\alpha = 0.51 - 0.02$  values. The variations of the parameter values relative to those from the default  
 488 fit using the central value  $\alpha = 0.51$  are included in the systematic uncertainties.
  - 489 • **Limitations of data modelling:** Due to its complexity, the fit model can be sensitive to some  
 490 nuisance parameters. This limited sensitivity could potentially lead to a bias in the measured  
 491 physics parameters, even when the model perfectly describes the fitted data. To test the stability of  
 492 the results, due to the choice of default fit model, a set of pseudo-experiments are conducted using  
 493 the default model in both the generation and fit. The systematic uncertainties are determined from  
 494 the mean of the pull distributions of the pseudo-experiments scaled by the statistical error of that  
 495 parameter on the fit to data. The observed deviations are included in the systematics.

496 The systematic uncertainties are listed in Table 5. For each parameter, the total systematic uncertainty is  
 497 obtained by adding all of the contributions in quadrature.

Table 5: Summary of systematic uncertainties assigned to the physical parameters of interest.

	$\phi_s$ [ $10^{-3}$ rad]	$\Delta\Gamma_s$ [ $10^{-3}$ ps $^{-1}$ ]	$\Gamma_s$ [ $10^{-3}$ ps $^{-1}$ ]	$ A_{\parallel}(0) ^2$ [ $10^{-3}$ ]	$ A_0(0) ^2$ [ $10^{-3}$ ]	$ A_S(0) ^2$ [ $10^{-3}$ ]	$\delta_{\perp}$ [ $10^{-3}$ rad]	$\delta_{\parallel}$ [ $10^{-3}$ rad]	$\delta_{\perp} - \delta_S$ [ $10^{-3}$ rad]
Tagging	19	0.4	0.3	0.2	0.2	1.1	17	19	2.3
Acceptance	0.7	< 0.1	< 0.1	0.8	0.7	2.4	33	11	2.6
ID alignment	0.8	0.2	0.5	< 0.1	< 0.1	< 0.1	11	7.2	< 0.1
Best cand. sel.	0.5	0.4	0.7	0.5	0.2	0.2	12	17	7.5
Background angles model:									
Choice of fit function	2.5	< 0.1	0.3	1.1	< 0.1	0.6	12	0.9	1.1
Choice of $p_T$ bins	1.3	0.5	< 0.1	0.4	0.5	1.2	1.5	7.2	1.0
Choice of mass interval	0.4	0.1	0.1	0.3	0.3	1.3	4.4	7.4	2.3
Dedicated backgrounds:									
$B_d^0$	2.3	1.1	< 0.1	0.2	3.0	1.5	10	23	2.1
$\Lambda_b$	1.6	0.3	0.2	0.5	1.2	1.8	14	30	0.8
Fit model:									
Time res. sig frac	1.4	1.1	0.5	0.5	0.6	0.8	12	30	0.4
Time res. $p_T$ bins	0.7	0.5	0.8	0.1	0.1	0.1	2.2	14	0.7
$S$ -wave phase	0.2	< 0.1	< 0.1	0.3	< 0.1	0.3	11	21	8.4
Model limitation	4.1	1.7	0.9	1.4	< 0.1	1.5	19	0.9	7.0
<b>Total</b>	<b>20</b>	<b>2.5</b>	<b>1.7</b>	<b>2.2</b>	<b>3.4</b>	<b>4.4</b>	<b>52</b>	<b>62</b>	<b>14</b>

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## 7 Results

498

499 The full simultaneous unbinned maximum-likelihood fit contains nine physical parameters:  $\Delta\Gamma_s$ ,  $\phi_s$ ,  $\Gamma_s$ ,  
500  $|A_0(0)|^2$ ,  $|A_{\parallel}(0)|^2$ ,  $\delta_{\parallel}$ ,  $\delta_{\perp}$ ,  $|A_S(0)|^2$  and  $\delta_S$ . The other parameters in the likelihood function are the  $B_S^0$   
501 signal fraction  $f_s$ , parameters describing the  $J/\psi\phi$  mass distribution, parameters describing the decay  
502 time plus angular distributions of background events, parameters used to describe the estimated decay time  
503 uncertainty distributions for signal and background events, and scale factors between the estimated decay  
504 time uncertainties and their true uncertainties. In addition there are also nuisance parameters describing  
505 the background and acceptance functions that are fixed at the time of the fit.

506 Multiplying the total number of events supplied to the fit with the extracted signal fraction and its statistical  
507 uncertainty provides an estimate for the total number of  $B_S^0$  meson candidates of  $457\,720 \pm 750$ . The  
508 results and correlations of the physics parameters obtained from the fit are given in Tables 6 and 7. Fit  
509 projections of the mass, proper decay time and angles are given in Figures 6 and 7, respectively.

## 8 Combination with 7 TeV and 8 TeV results

510

511 The measured values are consistent with those obtained in a previous analysis [Aad:2016tdj], using  
512 ATLAS  $19.2 \text{ fb}^{-1}$  of data collected at  $\sqrt{s}$  of 7 TeV and 8 TeV. A Best Linear Unbiased Estimator (BLUE)  
513 combination [Nisius:2014wua] is used to perform a combination of the current measurements with those  
514 from  $19.2 \text{ fb}^{-1}$  of 7 TeV and 8 TeV data. The measured values, uncertainties, and correlations are taken  
515 from the measurements performed at each centre-of-mass energy. The statistical correlation between these  
516 three measurements is zero as the events are different. The correlations of the systematic uncertainties  
517 between the three measurements are estimated and tested in several categories depending of whether the  
518 given systematic effect changed significantly between the measurements. The combined results for the fit  
519 parameters and their uncertainties are given in Table 8.

Table 6: Fitted values for the physical parameters of interest with their statistical and systematic uncertainties.

Parameter	Value	Statistical uncertainty	Systematic uncertainty
$\phi_s$ [rad]	-0.093	0.041	0.020
$\Delta\Gamma_s$ [ps <sup>-1</sup> ]	0.0668	0.0046	0.0025
$\Gamma_s$ [ps <sup>-1</sup> ]	0.6662	0.0014	0.0017
$ A_{  }(0) ^2$	0.2195	0.0021	0.0022
$ A_0(0) ^2$	0.5156	0.0013	0.0034
$ A_S(0) ^2$	0.0378	0.0035	0.0044
$\delta_\perp$ [rad]	3.07	0.11	0.05
$\delta_{  }$ [rad]	3.31	0.06	0.06
$\delta_\perp - \delta_S$ [rad]	-0.23	0.04	0.01

Table 7: Fit correlations between the physical parameters of interest.

	$\Delta\Gamma$	$\Gamma_s$	$ A_{  }(0) ^2$	$ A_0(0) ^2$	$ A_S(0) ^2$	$\delta_{  }$	$\delta_\perp$	$\delta_\perp - \delta_S$
$\phi_s$	-0.10	0.02	0.00	-0.01	-0.01	0.02	0.01	-0.01
$\Delta\Gamma$	1	-0.57	0.10	0.09	0.04	0.04	0.00	0.01
$\Gamma_s$		1	-0.14	-0.04	0.10	-0.11	-0.03	0.02
$ A_{  }(0) ^2$			1	-0.35	-0.21	0.56	0.17	-0.05
$ A_0(0) ^2$				1	0.28	-0.12	-0.05	0.06
$ A_S(0) ^2$					1	-0.40	-0.17	0.20
$\delta_{  }$						1	0.32	-0.07
$\delta_\perp$							1	0.03

520 The two-dimensional likelihood contours in the  $\phi_s - \Delta\Gamma_s$  plane for the ATLAS results based on 7 TeV and  
521 8 TeV data, the result from 13 TeV, and the combined results from 7 TeV, 8 TeV and 13 TeV are shown  
522 in Figure 8. The statistical and systematic uncertainties are combined in quadrature and correlations are  
523 taken into account in the construction of Gaussian contours. The correlation between the  $\phi_s$  and  $\Delta\Gamma_s$  values  
524 determined in combination is  $-0.04$ .

525 Two-dimensional likelihood contours in the  $\phi_s - \Delta\Gamma_s$  plane are shown in Figure 9 for this ATLAS  
526 result, the result of CMS [9] using the  $B_s^0 \rightarrow J/\psi\phi$  decay, and a combination of three LHCb measure-  
527 ments [Aaij:2016psitwoS, Aaij:2014Ds, 8] using  $B_s^0 \rightarrow J/\psi\phi$ , and  $B_s^0$  decays to  $\psi(2S)\phi$  and to  $D_s^+D_s^-$ ,  
528 respectively. The contours are obtained interpreting each result as Gaussian 2D contour in the  $\phi_s - \Delta\Gamma_s$   
529 plane. All results are consistent between one other and with the SM [2, 4].

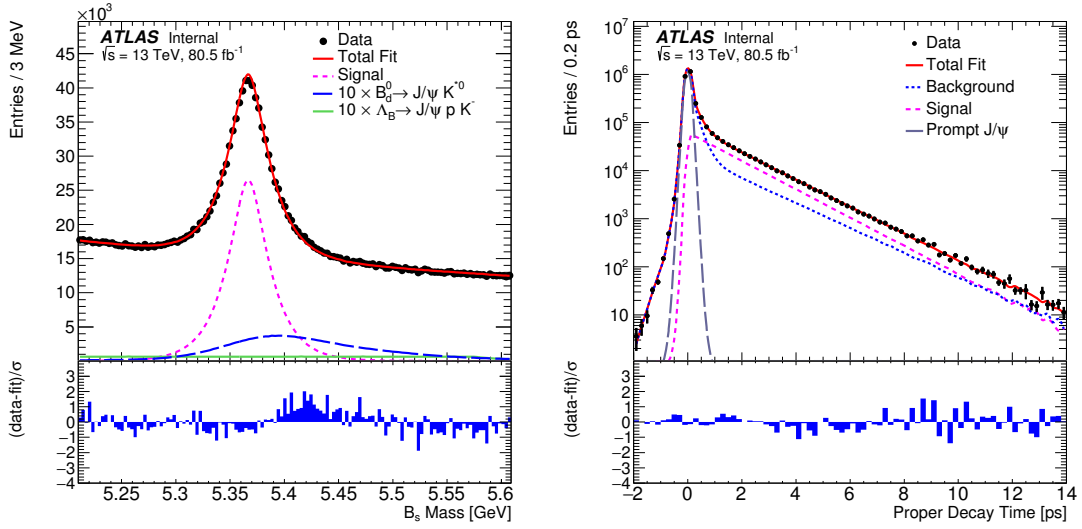


Figure 6: (Left) Mass fit projection for the  $B_s^0 \rightarrow J/\psi \phi$  sample. The red line shows the total fit, the short-dashed magenta line shows the  $B_s^0 \rightarrow J/\psi \phi$  signal component, the long-dashed blue line shows the  $B_d^0 \rightarrow J/\psi K^{0*}$  component, and the solid green line shows the contribution from  $\Lambda_b \rightarrow J/\psi p K^-$  events. (Right) Proper decay time fit projection for the  $B_s^0 \rightarrow J/\psi \phi$  sample. The red line shows the total fit while the short-dashed magenta line shows the total signal. The total background is shown as a blue dotted line, and a long-dashed grey line shows the prompt  $J/\psi$  background component. Below each figure is a ratio plot that shows the difference between each data point and the total fit line divided by the statistical and systematic uncertainties summed in quadrature ( $\sigma$ ) of that point.

Table 8: Values of the physical parameters extracted in the combination of 13 TeV results with those obtained from 7 TeV and 8 TeV data.

Parameter	Value	Statistical uncertainty	Systematic uncertainty
$\phi_s$ [rad]	-0.096	0.036	0.024
$\Delta\Gamma_s$ [ $\text{ps}^{-1}$ ]	0.0696	0.0042	0.0029
$\Gamma_s$ [ $\text{ps}^{-1}$ ]	0.6684	0.0014	0.0018
$ A_{\parallel}(0) ^2$	0.2210	0.0019	0.0026
$ A_0(0) ^2$	0.5178	0.0014	0.0040
$ A_S ^2$	0.0407	0.0032	0.0057
$\delta_{\perp}$ [rad]	3.19	0.11	0.07
$\delta_{\parallel}$ [rad]	3.32	0.06	0.09
$\delta_{\perp} - \delta_S$ [rad]	-0.23	0.04	0.02

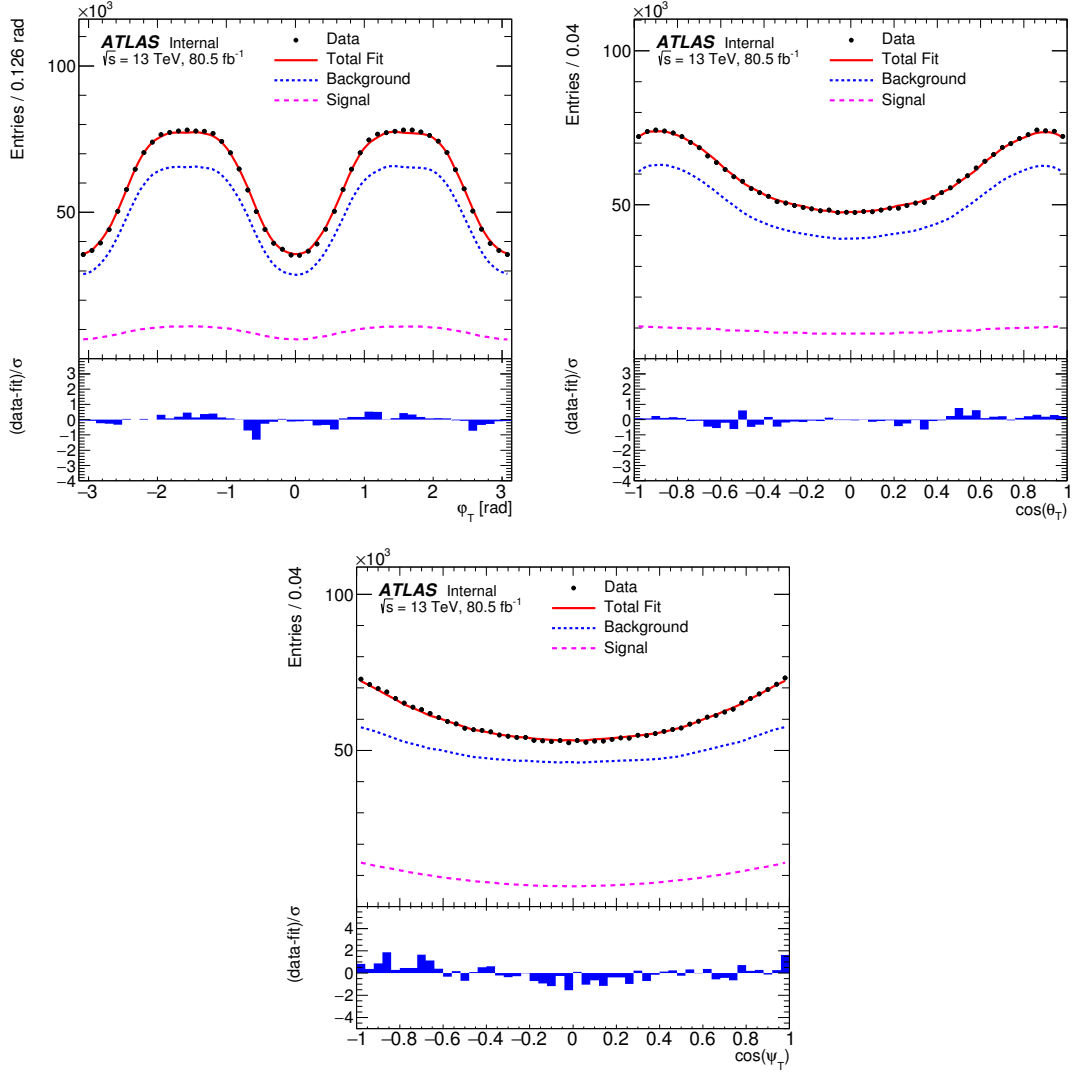


Figure 7: Fit projections for the transversity angles  $\phi_T$  (top left),  $\cos(\theta_T)$  (top right), and  $\cos(\psi_T)$  (bottom). In all three plots the red solid line shows the total fit, the  $B_s^0 \rightarrow J/\psi\phi$  signal component is shown by the magenta dashed line and the blue dotted line shows the contribution of all background components. Below each figure is a ratio plot that shows the difference between each data point and the total fit line divided by the statistical and systematic uncertainties summed in quadrature ( $\sigma$ ) of that point.



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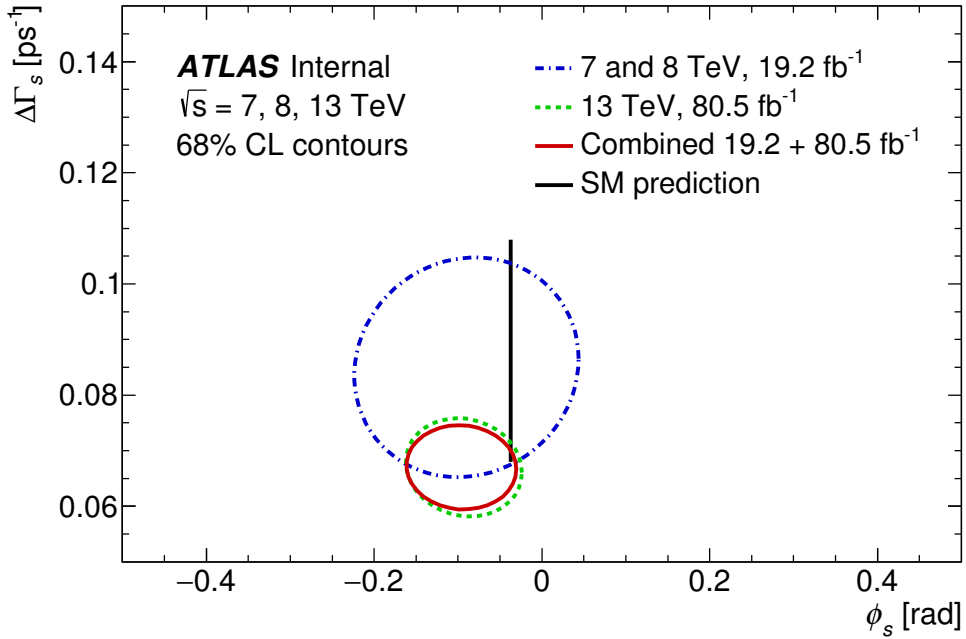


Figure 8: Likelihood 68% confidence level contours in the  $\phi_s - \Delta\Gamma_s$  plane, showing ATLAS results for 7 TeV and 8 TeV data (blue dashed-dotted curve), for 13 TeV data (green dashed curve) and for 13 TeV data combined with 7 TeV and 8 TeV (red solid curve) data. In all contours the statistical and systematic uncertainties are combined in quadrature and correlations are taken into account.

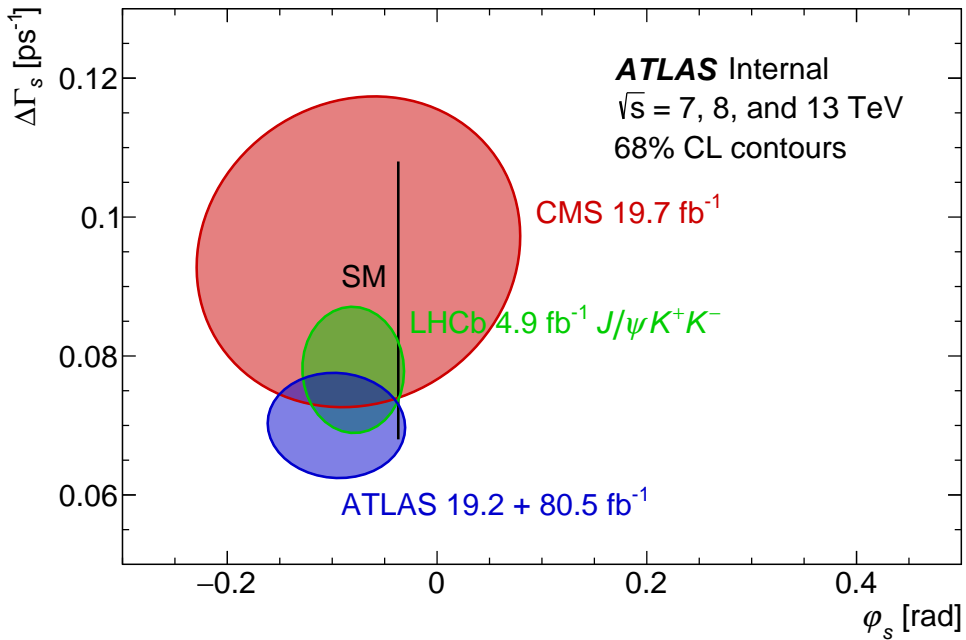


Figure 9: Likelihood 68% confidence level contours in the  $\phi_s - \Delta\Gamma_s$  plane, including results from LHCb (green) and CMS (red) using 7 TeV and 8 TeV data. The brown contour shows the ATLAS result for 13 TeV combined with 7 TeV and 8 TeV. In all contours the statistical and systematic uncertainties are combined in quadrature.

## 530 9 Summary

531 A measurement of the time-dependent  $CP$  asymmetry parameters in  $B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi(K^+K^-)$  decays  
 532 from a  $80.5 \text{ fb}^{-1}$  data sample of  $pp$  collisions collected with the ATLAS detector during the 13 TeV LHC  
 533 run is presented. The values from the 13 TeV analysis are consistent with those obtained in the previous  
 534 analysis using 7 TeV and 8 TeV ATLAS data [**Aad:2016tdj**]. The two measurements are statistically  
 535 combined, leading to the following results:

$$\begin{aligned}
 \phi_s &= -0.096 \pm 0.036 \text{ (stat.)} \pm 0.024 \text{ (syst.) rad} \\
 \Delta\Gamma_s &= 0.0696 \pm 0.0042 \text{ (stat.)} \pm 0.0029 \text{ (syst.) ps}^{-1} \\
 \Gamma_s &= 0.6684 \pm 0.0014 \text{ (stat.)} \pm 0.0018 \text{ (syst.) ps}^{-1} \\
 |A_{\parallel}(0)|^2 &= 0.2210 \pm 0.0019 \text{ (stat.)} \pm 0.0026 \text{ (syst.)} \\
 |A_0(0)|^2 &= 0.5178 \pm 0.0014 \text{ (stat.)} \pm 0.0040 \text{ (syst.)} \\
 |A_S(0)|^2 &= 0.0407 \pm 0.0032 \text{ (stat.)} \pm 0.0057 \text{ (syst.)} \\
 \delta_{\perp} &= 3.19 \pm 0.11 \text{ (stat.)} \pm 0.07 \text{ (syst.) rad} \\
 \delta_{\parallel} &= 3.32 \pm 0.06 \text{ (stat.)} \pm 0.09 \text{ (syst.) rad} \\
 \delta_{\perp} - \delta_S &= -0.23 \pm 0.04 \text{ (stat.)} \pm 0.02 \text{ (syst.) rad}
 \end{aligned}$$

537 The new ATLAS measurement on the  $CP$  violation phase  $\phi_s$  increased a precision of the previous ATLAS  
 538 measurement using 7 TeV and 8 TeV ATLAS data [**Aad:2016tdj**], and the new result is still consistent  
 539 with the Standard Model prediction.

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