

# Gravitational waves from first order phase transition

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March 9, 2019

Toyama International Symposium on "Physics at the Cosmic Frontier"  
University of Toyama

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- References:  
- Hashino, Jinno, MK, Kanemura, Takahashi and Takimoto, arXiv:1809.04994  
Accepted by Physical Review D

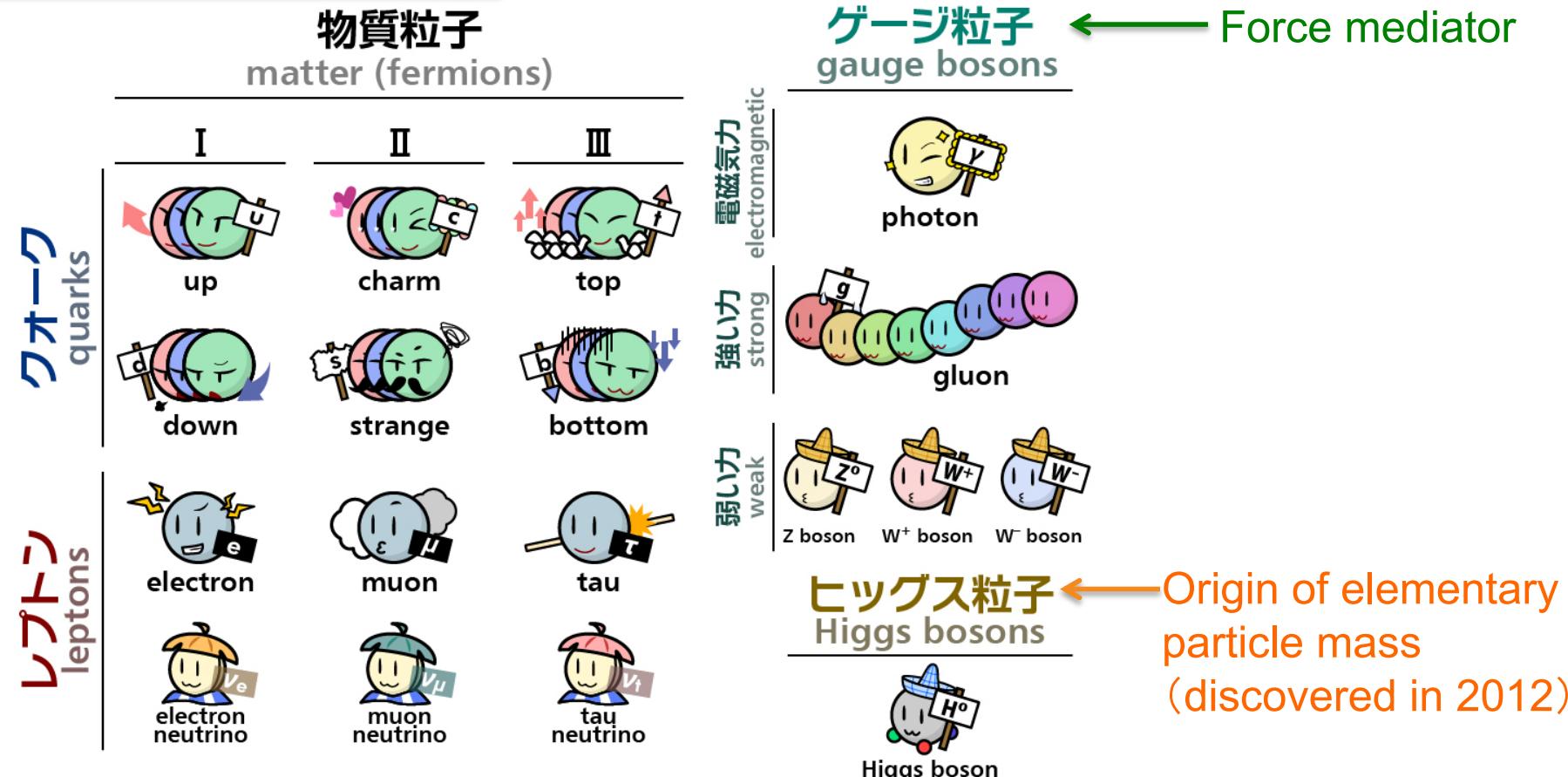
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# Standard Model of Particle Physics

## Standard Model (SM)



- Established theory describing elementary particles
- But, some phenomena demand new physics beyond the SM

# New Physics Beyond the Standard Model

Beyond the Standard Model → Aoki

Experimental problems:

Neutrino oscillations → Sugiyama, Okui

Baryon asymmetry → Asaka

Existence of dark matter → Ishiwata

Cosmic inflation → Kubo

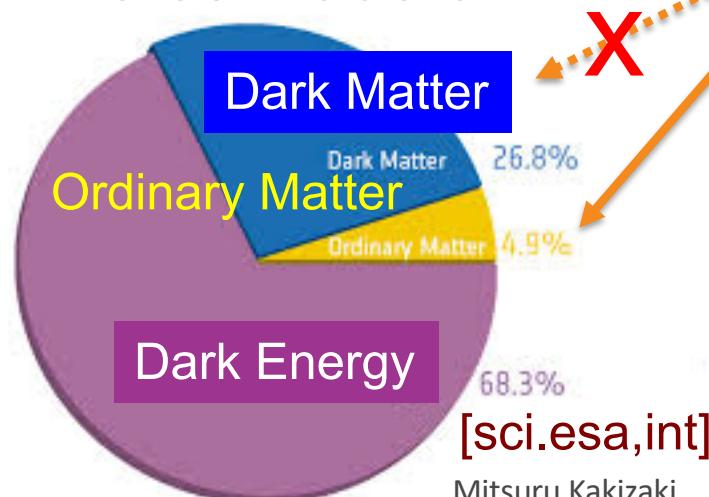
Existence of dark energy → Shima

Other anomalies

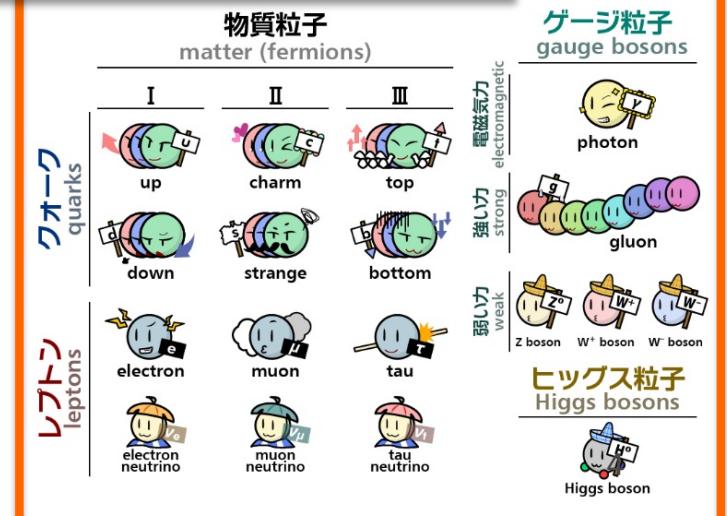
Theoretical puzzles:

Structure of the Higgs sector, Hierarchy problem, etc.

What is the Universe made of?



Standard Model

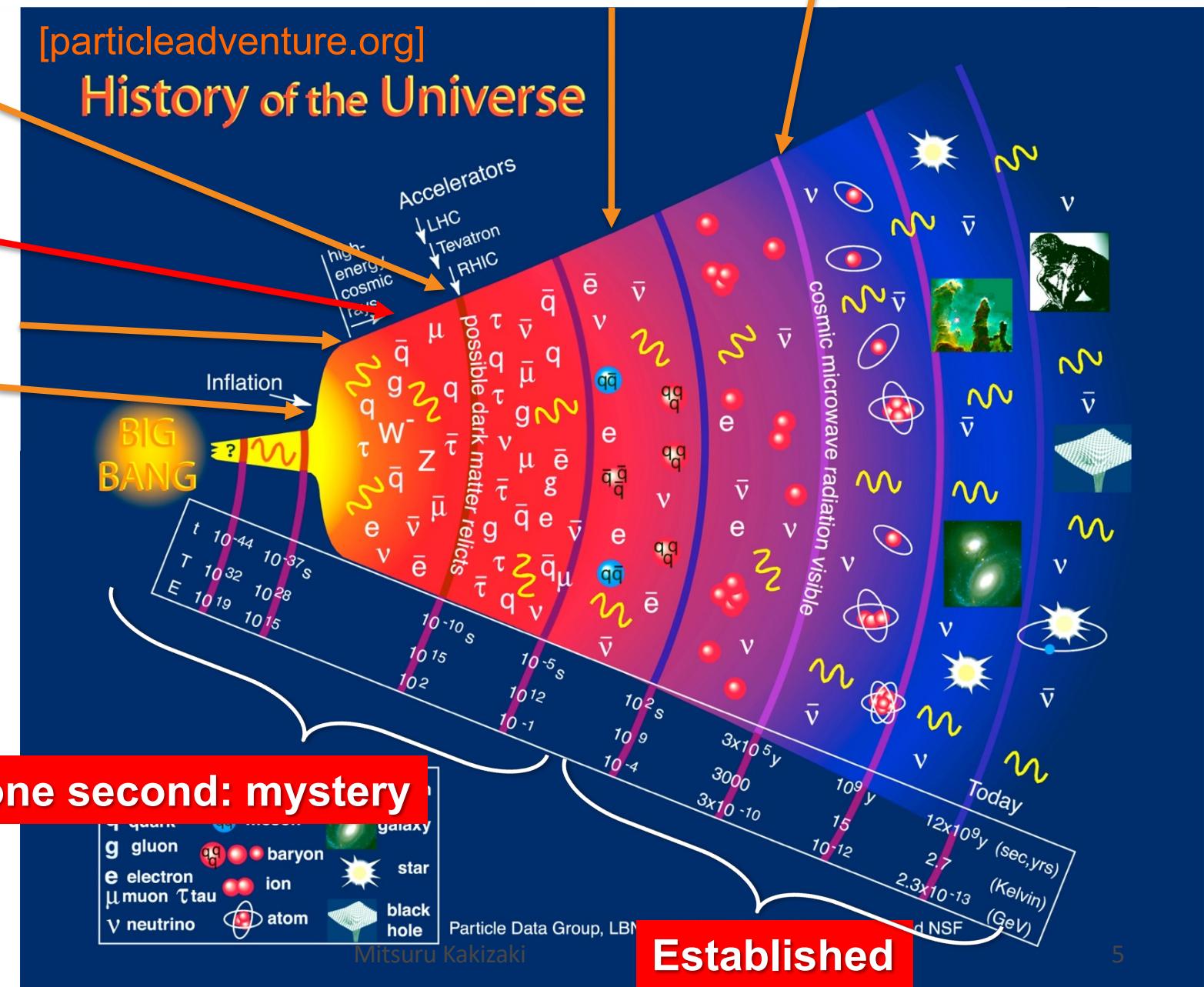


# History of the Universe

Big bang  
nucleosynthesis

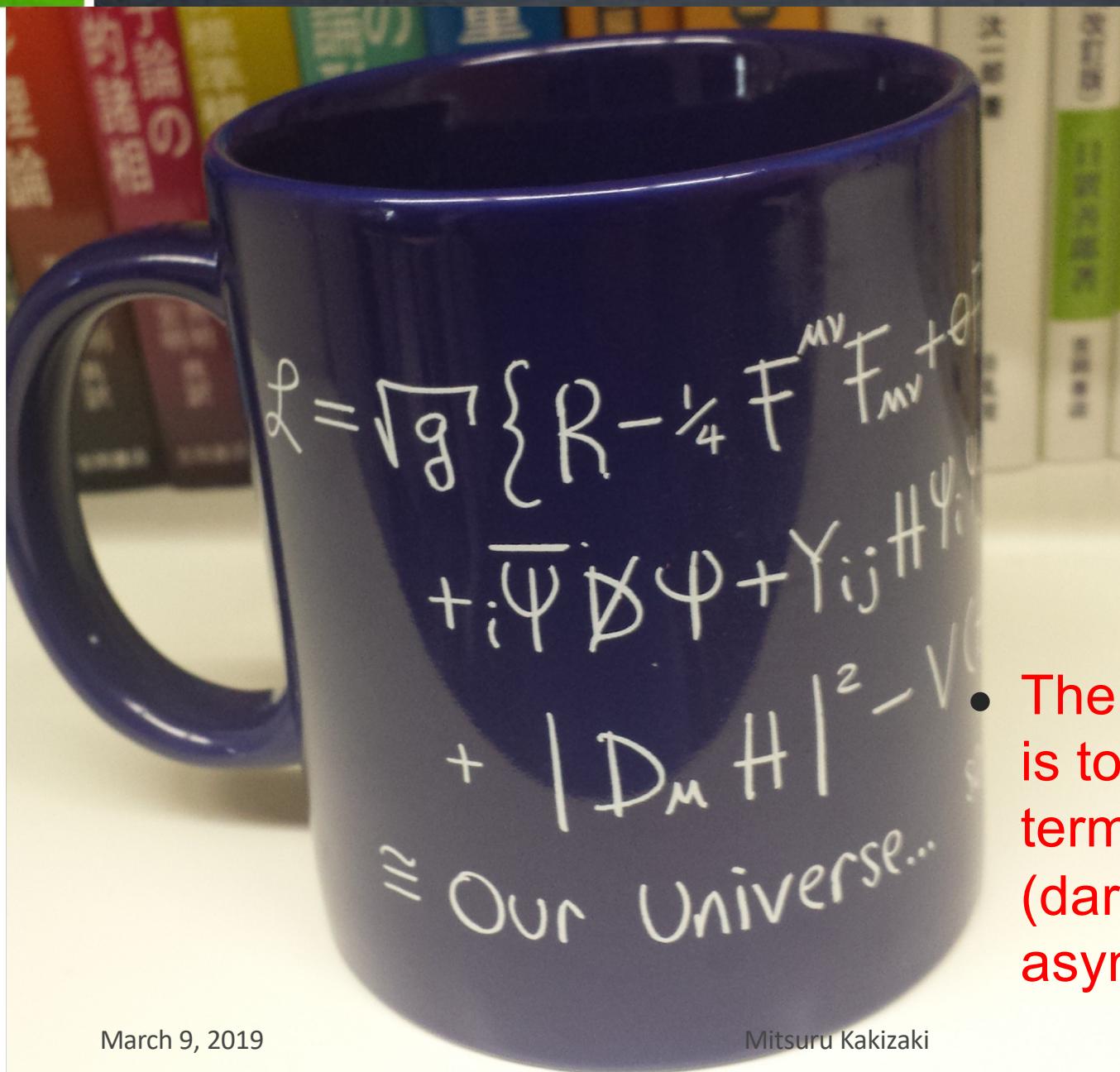
Recombination  
(Cosmic microwave bg.)

- Generation of dark matter?
- Electroweak phase transition?
- Baryogenesis?
- Cosmic Inflation



# Our Universe (in mathematical language)

= Standard Model x General Relativity + New Physics



- The goal of this research is to reveal unknown terms for new physics (dark matter, baryon asymmetry, etc.)

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# Gravitational Waves

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## Gravitational waves (GWs)

- Non-uniform motion of a massive object
  - ➡ Ripples of spacetime propagating at the speed of light
    - c.f. Non-uniform motion of a charged object
    - ➡ Electromagnetic waves

## Properties of gravitational waves

- Transverse to the direction of propagation
- Spin 2
- 2 polarization modes: Plus mode  $h^+$  & Cross mode  $h\times$

## Sources of gravitational waves

### Astrophysical origin

- Binaries (NS, BH, ...)
- Supernovae
- etc.

### Cosmological origin

- 1st order phase transition
- Cosmic inflation
- Topological defects

# Gravitational Waves as a Probe for the Early Universe

## Weak field approximation

- Metric close to flat  $g_{\mu\nu}(x) = \eta_{\mu\nu} + \underline{h_{\mu\nu}(x)}$ ,  $|h_{\mu\nu}| \ll 1$

→ Linearized Einstein equation in vacuum

$$\square h_{\mu\nu} = 0 \quad \text{Wave equation!}$$

## Interaction rate of gravitational waves

- Interaction rate:  $\Gamma = n\sigma v$

$$T^3 \quad G_N^2 T^2 = \frac{T^2}{M_{Pl}^4} \quad 1$$

- Expansion rate of the Universe:  $H \sim \frac{T^2}{M_{Pl}}$

$$\rightarrow \frac{\Gamma}{H} \sim \frac{T^3}{M_{Pl}^3}$$

GWs decouple at temperatures below the Planck scale

# Universe earlier than big bang nucleosynthesis can be probed by using GWs

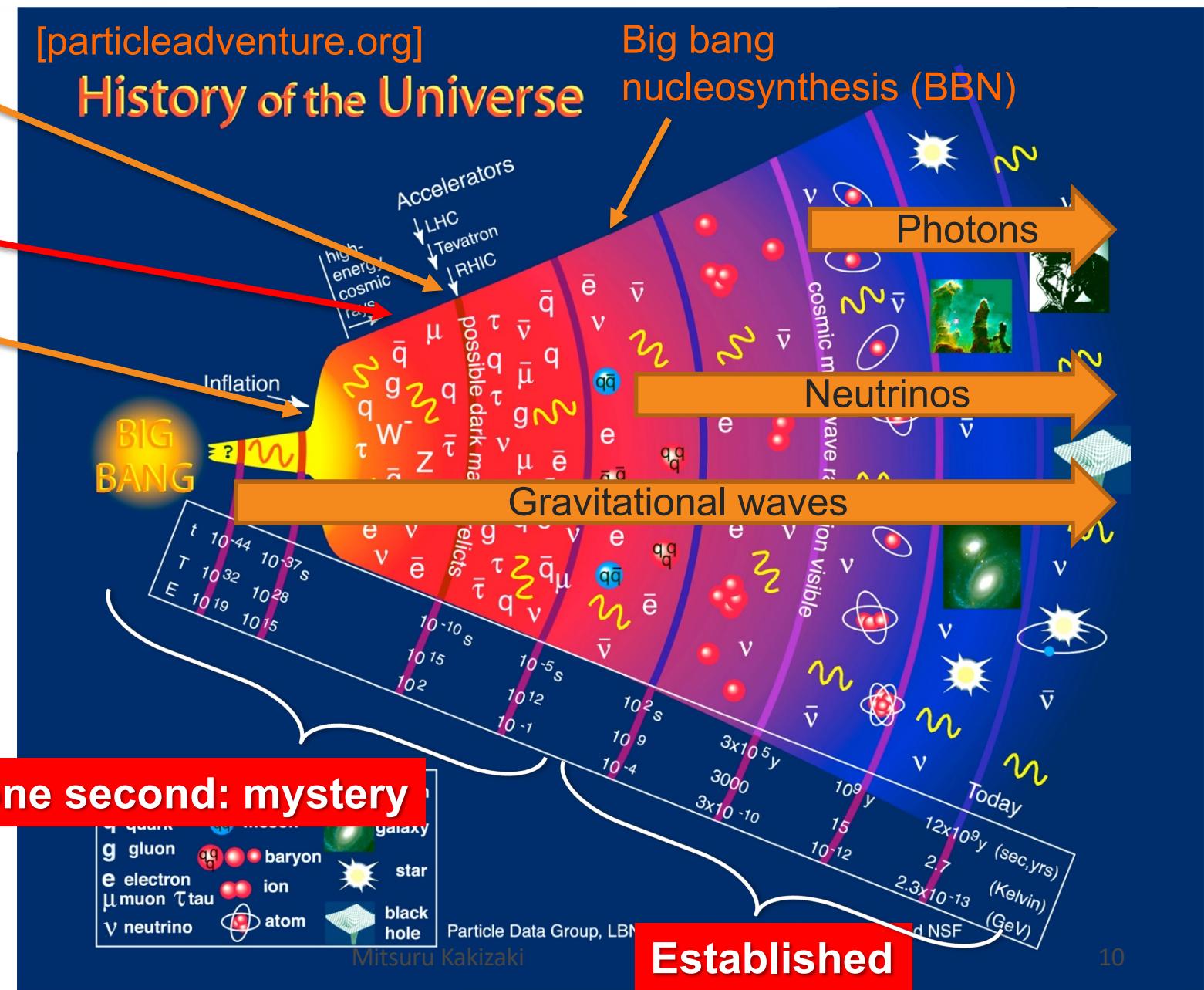
Generation of dark matter?

Electroweak phase transition?

Cosmic Inflation

The first one second: mystery

Established



# Relic gravitational waves

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## Characteristics of relic gravitational waves

- Homogeneous
- Isotropic
- Static
- Unpolarized

→ Relic GWs are characterized only by frequency  $f$

## Energy density of relic gravitational waves

$$\rho_{\text{GW}} = \frac{1}{32\pi G} \langle \dot{h}_{ij} \dot{h}_{ij} \rangle$$

- Normalized Energy density per unit logarithmic interval of frequency

$$\Omega_{\text{GW}}(f) \equiv \frac{1}{\rho_c} \frac{d\rho_{\text{GW}}}{d \ln f}$$

$$\rho_c = \frac{3H_0^2}{8\pi G} \quad : \text{Critical density}$$

# Typical frequency of relic gravitational waves

Gravitational waves produced with frequency  $f_t$ , abundance  $\Omega_{\text{GW}}^t$  are red-shifted due to the expansion of the Universe

- Frequency and energy density scale as  $f \propto \frac{1}{a}$        $\rho_{\text{GW}} \propto \frac{1}{a^4}$
- Conservation of entropy:  $sa^3 = \text{const.}$        $a$ : scale factor

→ Red-shifted GW relic abundance observed today:

$$\Omega_{\text{GW}} h^2 \simeq 1.7 \times 10^{-5} \left( \frac{100}{g_*^t} \right)^{1/3} \Omega_{\text{GW}}^t$$

Red-shifted typical frequency observed today:

$$f_0 \simeq 1.7 \times 10^{-5} \left( \frac{g_*^t}{100} \right)^{1/6} \left( \frac{T_t}{100 \text{ GeV}} \right) \frac{f_t}{H_t} \text{ Hz}$$

For typical electroweak phase transition:

$$T_t \sim 100 \text{ GeV} \quad f_t/H_t \sim 10^2 - 10^4 \rightarrow \underline{f_0 \sim 10^{-3} - 10^{-1} \text{ Hz}}$$

Range for future space-based interferometers

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# Motivation

## Discovery of the 125 GeV Higgs boson $h$ at the CERN LHC

- The Standard Model (SM) has been established as a low-energy effective theory below  $O(100)$  GeV

This is not the end of the story

## Puzzles in the Higgs sector

- Guiding principle?
- Shape of the Higgs potential (multiplets, symmetries, ...)?
- Dynamics behind the electroweak symmetry breaking (EWSB)?

## Phenomena beyond the SM (BSM)

- Baryon asymmetry of the Universe (BAU)
- Existence of dark matter
- Cosmic inflation
- Neutrino oscillations

## Idea: Higgs sector = Window to New Physics

- The structure of the Higgs sector is related to BSM models

Information on new physics can be obtained by investigating the properties of the Higgs sector

# Electroweak baryogenesis (EWBG) relates the Higgs sector and BSM phenomena

## Sakharov's conditions for BAU

1. Baryon number violation  $\leftarrow$  Sphaleron
2. C and CP violation  $\leftarrow$  Extended Higgs sector
3. Departure from thermal equilibrium  
 $\uparrow$  Strongly first order phase transition  
 $(1^{\text{st}} \text{ OPT}): \varphi_c/T_c \gtrsim 1$

## SM Higgs potential w/ one doublet:

- PT is NOT of 1<sup>st</sup> order for  $m_h = 125$  GeV
- e.g. Two Higgs doublet model (2HDM)

$$\varphi_c/T_c \gtrsim 1 \rightarrow \Delta\lambda_{hhh}/\lambda_{hhh}^{\text{SM}} \gtrsim 10\%$$

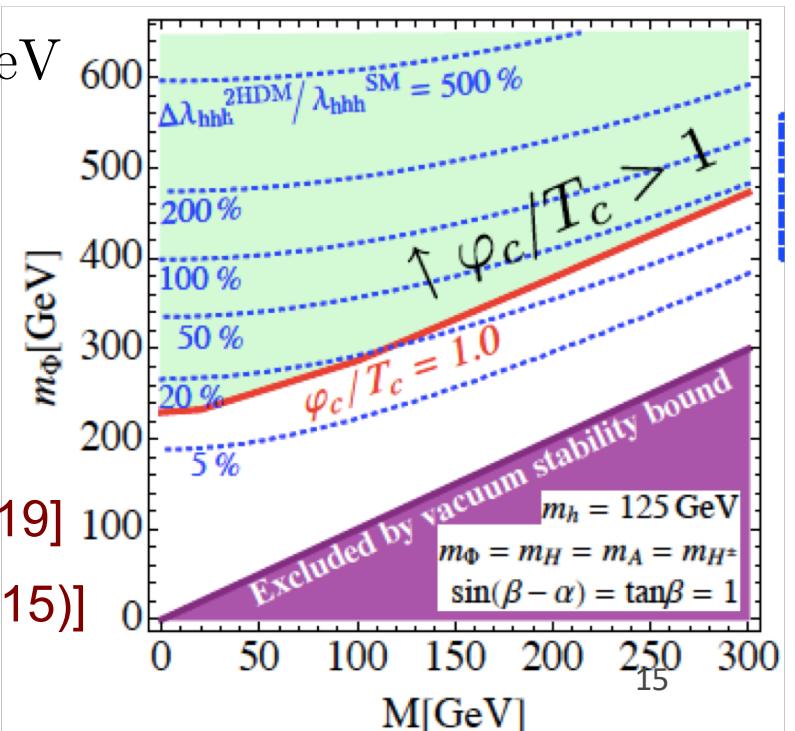
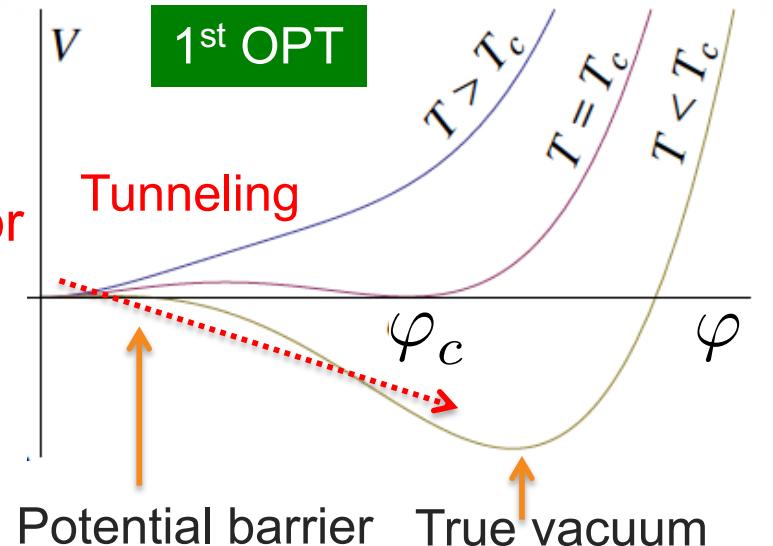
[Kanemura, Okada, Senaha (2005)]

## Future accuracy:

- High-Luminosity LHC:

$$-1.3 \lesssim \Delta\lambda_{hhh}/\lambda_{hhh}^{\text{SM}} \lesssim 8.7 \quad [\text{ATL-PHYS-PUB-2014-019}]$$

- ILC 1 TeV:  $\Delta\lambda_{hhh} : 10\%$  [Fujii et al. (2015)]



# Gravitational waves (GWs) as a probe of EWPT

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Ground-based interferometers:

advanced LIGO, advanced Virgo, KAGRA, ...

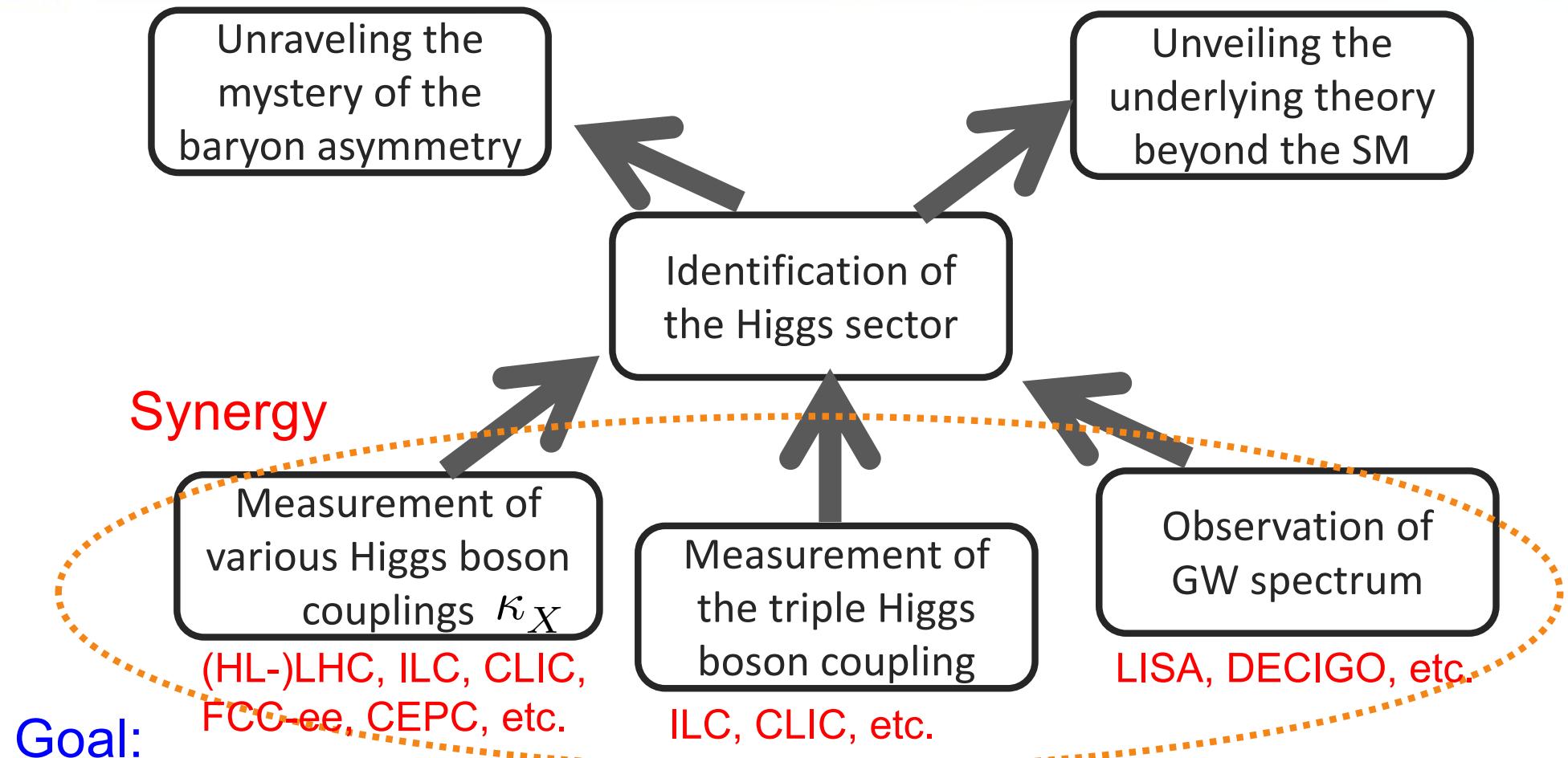
- Main targets: GWs from binary systems, supernovae, ...
- aLIGO made the first direct observation of GWs  
→ New era of GW astronomy [LIGO and Virgo (2016)]

Future space-based interferometers:

LISA (2034-), DECIGO, ...

- Sensitive to GWs from the early Universe  
(Strongly 1<sup>st</sup> OPT, cosmic inflation, ...)  
→ New era for fundamental physics

# Synopsis



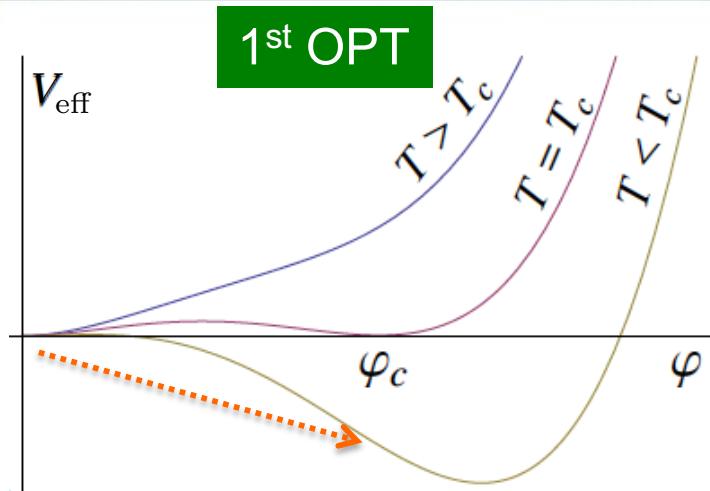
- We investigate expected precision for the parameters of models with 1<sup>st</sup> OPT using future space-based GW observations to maximize the synergy with colliders

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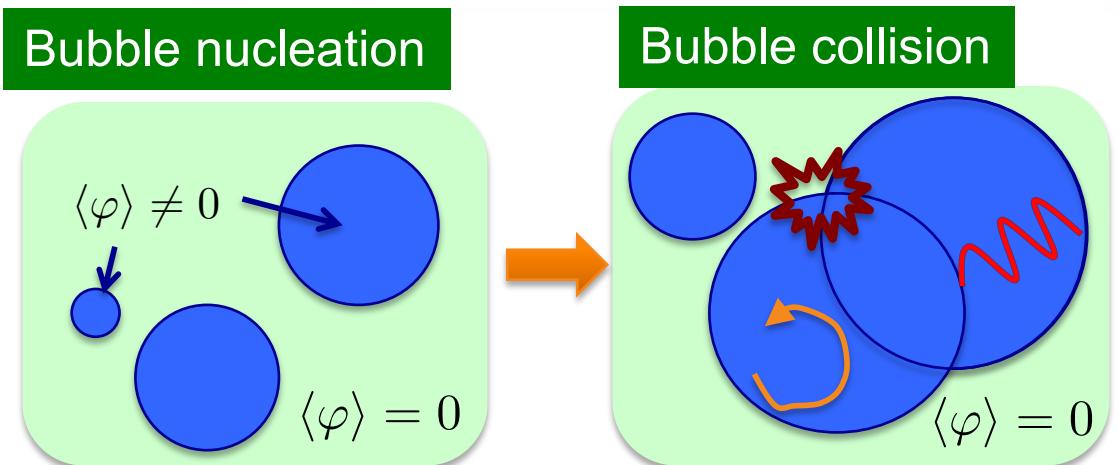
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# GWs from 1st OPT



Bubble nucleation



Linearized Einstein equation for the metric perturbation  $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$

$$\square h_{\mu\nu} \sim T_{\mu\nu}$$

Sources of GWs

1. Collision of bubble walls
2. Sound wave
3. Plasma turbulence

- GW spectrum is derived from finite temperature effective potential  $V_{\text{eff}}$

# Important quantities for GW spectrum

Bubble nucleation rate per unit volume per unit time:

$$\Gamma(t) = \Gamma_0(t) \exp[-S_E(t)] \quad S_E(T) = S_3(T)/T, \quad S_3 = \int d^3r \left[ \frac{1}{2}(\vec{\nabla}\varphi_b)^2 + V_{\text{eff}}(\varphi_b, T) \right]$$

Transition temperature  $T_*$

$$\left. \frac{\Gamma}{H^4} \right|_{T=T_*} \sim 1 \quad \rightarrow \quad \frac{S_3(T_*)}{T_*} = 4 \ln(T_*/H_*) \sim 140$$

Released false vacuum energy (Latent heat)

$$\epsilon(T) = -V_{\text{eff}}(\varphi_B(T), T) + T \frac{\partial V_{\text{eff}}(\varphi_B(T), T)}{\partial T} \quad \text{Normalized parameter: } \alpha = \frac{\epsilon(T_*)}{\rho_{\text{rad}}(T_*)}$$

Inverse of the duration of phase transition

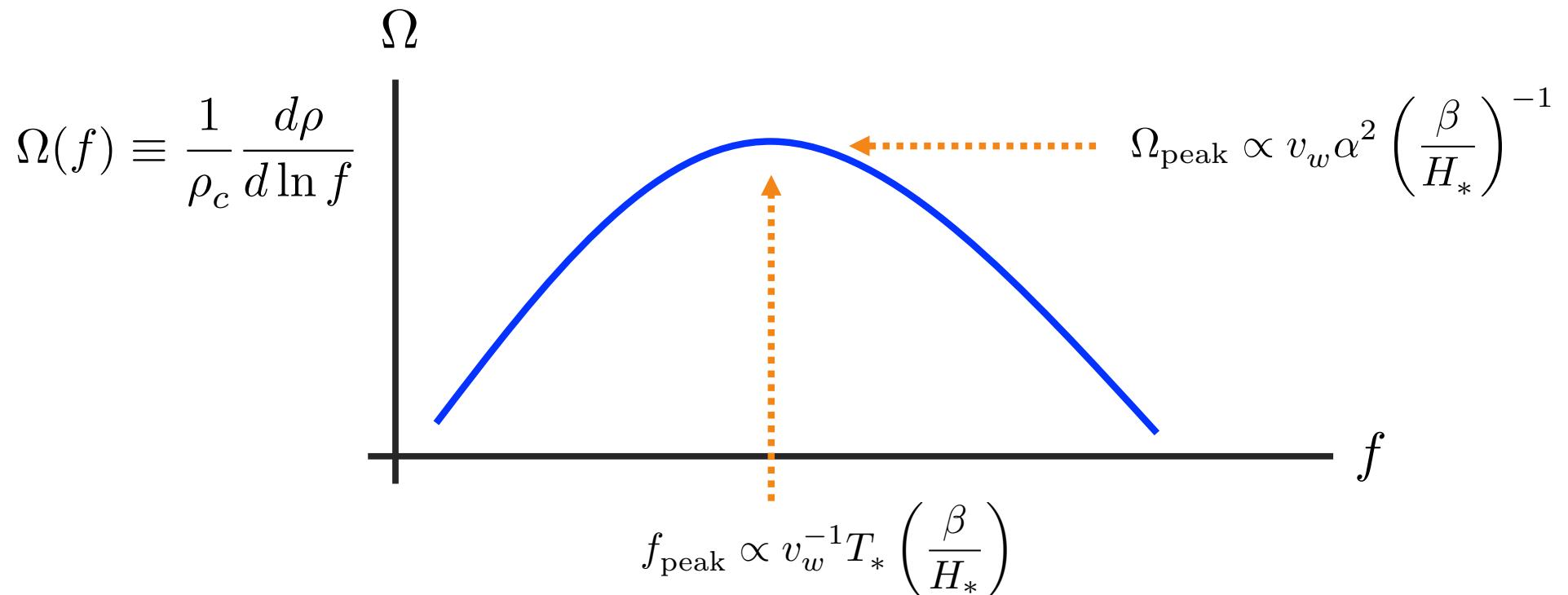
$$\beta = - \left. \frac{dS_E}{dt} \right|_{t=t_*} \simeq \left. \frac{1}{\Gamma} \frac{d\Gamma}{dt} \right|_{t=t_*}$$

Normalized parameter:  $\frac{\beta}{H_*} (= \tilde{\beta})$

Wall velocity  $v_w$

# GW spectrum

Rough spectrum from the dominant sound wave contribution



- Complicated numerical simulations are necessary
- Our analysis relies on the approximate fitting formula provided by Caprini et al. [Caprini et al. (2015)]

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# Fisher Analysis

Likelihood function

GW spectrum for parameter set  $\{p\}$

GW spectrum for fiducial parameter set  $\{\hat{p}\}$

$$\delta\chi^2(\{p\}, \{\hat{p}\}) = 2T_{\text{obs}} \int_0^\infty df \frac{[S_h(f, \{p\}) - S_h(f, \{\hat{p}\})]^2}{[S_{\text{eff}}(f) + S_h(f, \{\hat{p}\})]^2}$$

Observation period

Effective sensitivity of interferometer

$\downarrow$  Taylor expansion w.r.t.  $\{p\} = \{\hat{p}\}$

Confidence ellipse

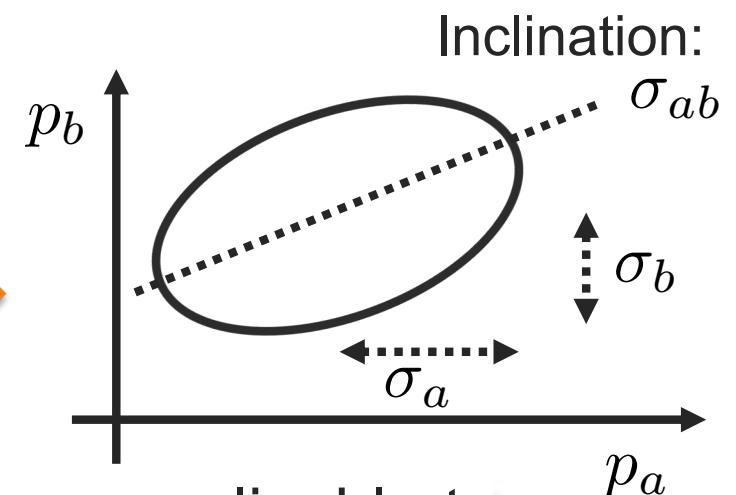
$$\delta\chi^2(\{p\}, \{\hat{p}\}) \simeq \mathcal{F}_{ab}(p_a - \hat{p}_a)(p_b - \hat{p}_b)$$

Fisher information matrix

$$\mathcal{F}_{ab} = 2T_{\text{obs}} \int_0^\infty df \frac{\partial_{p_a} S_h(f, \{\hat{p}\}) \partial_{p_b} S_h(f, \{\hat{p}\})}{[S_{\text{eff}}(f) + S_h(f, \{\hat{p}\})]^2}$$

The inverse  $\mathcal{F}_{ab}^{-1}$  is the covariance matrix

n.b.: we assume that these expressions are applicable to a single-detector like LISA

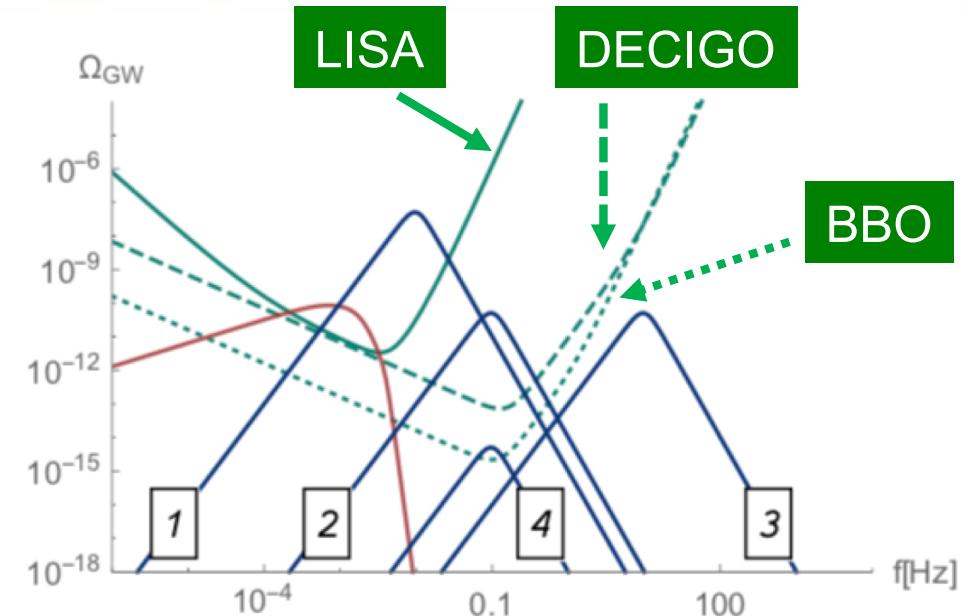


# Constraints on the shape of GW spectrum

## GW spectrum

- Fiducial values

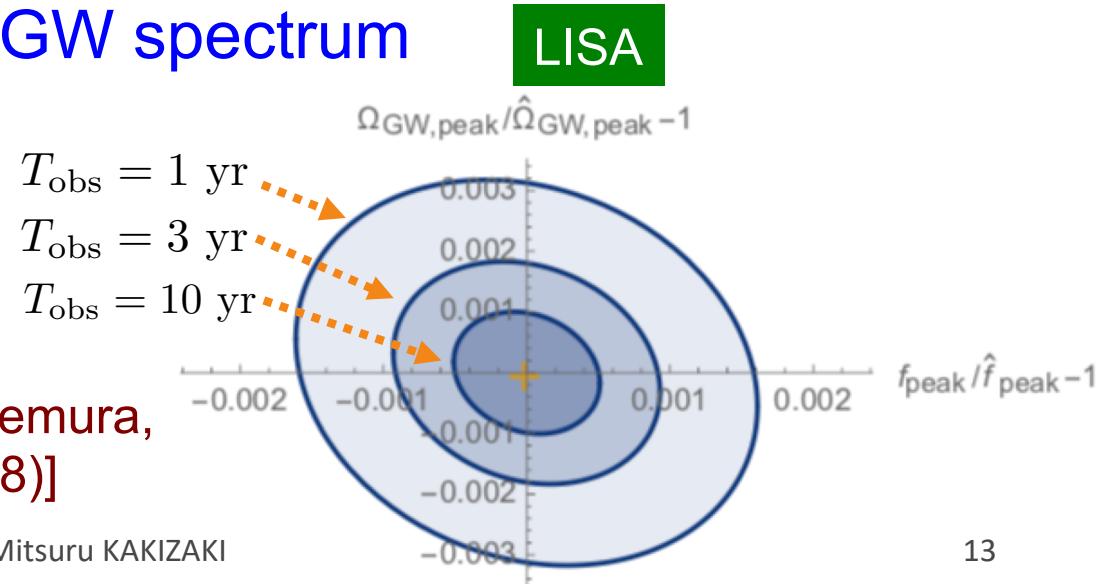
- Point 1:  $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-2} \text{ Hz}, 10^{-7})$ ,
- Point 2:  $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-1} \text{ Hz}, 10^{-10})$ ,
- Point 3:  $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10 \text{ Hz}, 10^{-10})$ ,
- Point 4:  $(f_{\text{peak}}, \Omega_{\text{peak}}) = (10^{-1} \text{ Hz}, 10^{-14})$ .



## Expected constraints on the GW spectrum

- $1\sigma$  confidence ellipse in  $(f_{\text{peak}}, \Omega_{\text{peak}})$  for Point 1

[Hashino, Jinno, MK, Kanemura,  
Takahashi, Takimoto (2018)]



# Constraints on transition parameters

## Constraining parameters

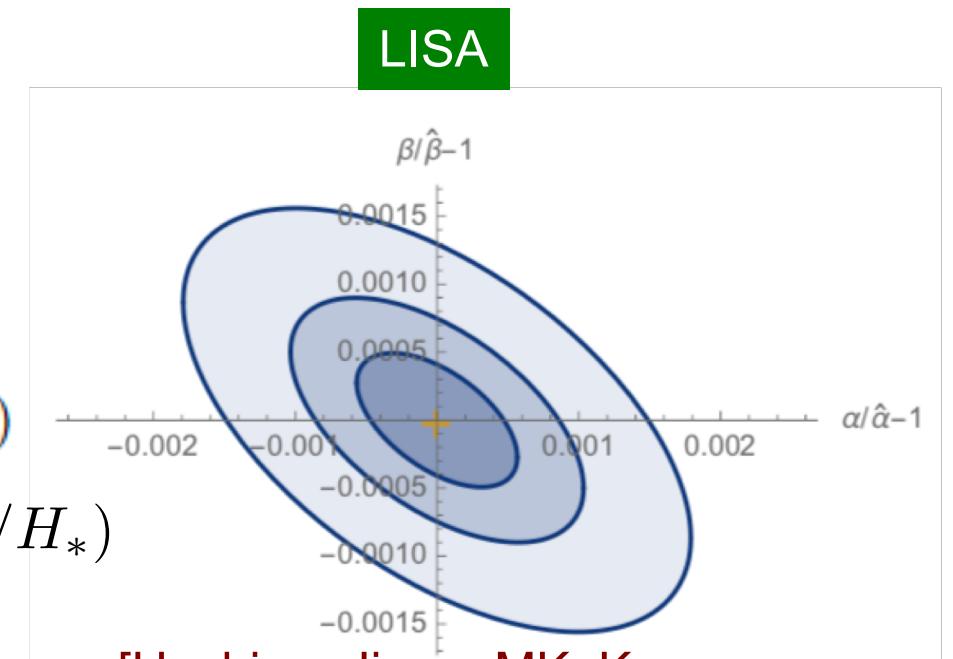
- The GW spectrum is determined by  $f_{\text{peak}}$ ,  $\Omega_{\text{peak}}$   
→ Our Fisher analysis generically constrain 2 combinations of underlying parameters

## Quantities describing transition dynamics

$$T_*, \quad v_w, \quad \alpha, \quad \frac{\beta}{H_*}$$

## Expected constraints on the transition parameters

- Fiducial values  
 $(\alpha, \beta/H_*, v_w, T_*) = (1, 100, 1, 100 \text{ GeV})$
- $1\sigma$  confidence ellipse in  $(\alpha, \beta/H_*)$  for fixed  $T_*$  and  $v_w$



[Hashino, Jinno, MK, Kanemura,  
Takahashi, Takimoto (2018)] 25

# Models with $O(N)$ symmetry with and without CSI

Typical examples for 1<sup>st</sup> OPT from thermal loop effects

- Models with CSI

- Tree-level Higgs potential

$$V_0 = \lambda_\Phi |\Phi|^4 + \frac{\lambda_S}{4} |\vec{S}|^4 + \frac{\lambda_{\Phi S}}{2} |\Phi|^2 |\vec{S}|^2$$

$\Phi$ :Higgs doublet

$$\vec{S} = (S_1, \dots, S_N)$$

- Fiducial parameters

$$(N, \lambda_S) = (2, 0.1)$$

$$\rightarrow (\alpha, \beta/H_*, T_* [\text{GeV}]) \simeq (0.080, 1000, 82)$$

- Models without CSI

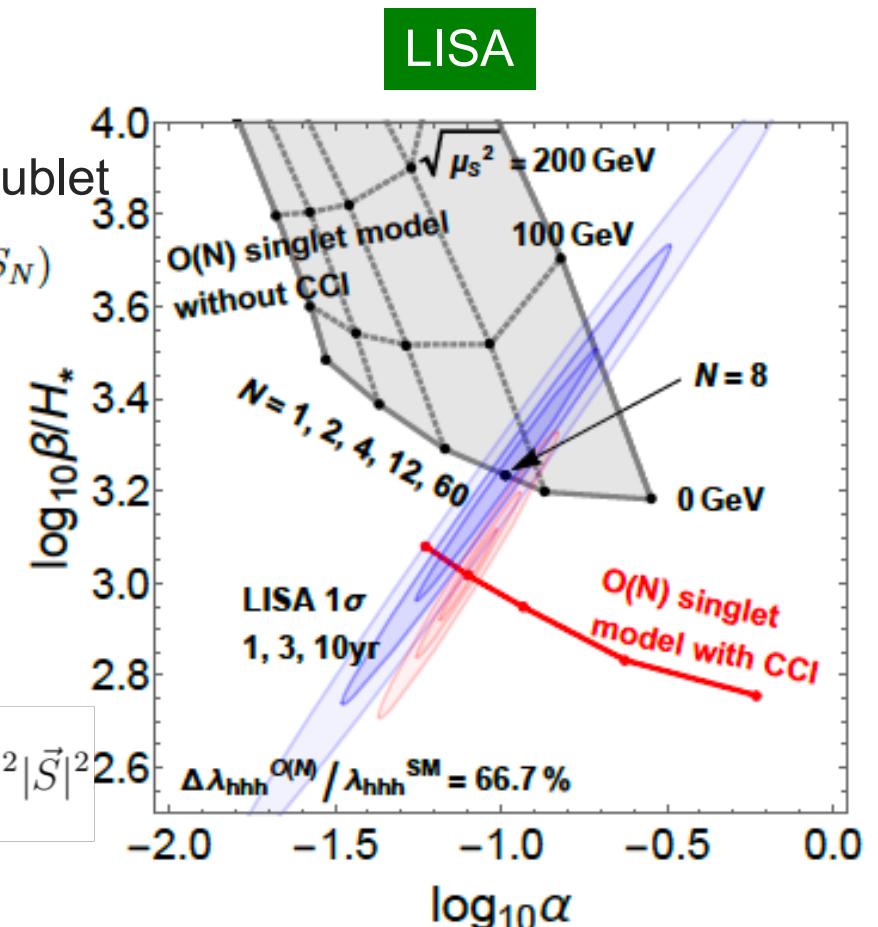
- Tree-level Higgs potential

$$V_0 = -\mu^2 |\Phi|^2 + \mu_S^2 |\vec{S}|^2 + \lambda_\Phi |\Phi|^4 + \frac{\lambda_S}{4} |\vec{S}|^4 + \frac{\lambda_{\Phi S}}{2} |\Phi|^2 |\vec{S}|^2$$

- Fiducial parameters

$$(N, \lambda_S, m_S [\text{GeV}], \mu_S^2 [\text{GeV}^2]) = (8, 0.1, 385, 0)$$

$$\rightarrow (\alpha, \beta/H_*, T_* [\text{GeV}]) \simeq (0.10, 1700, 83)$$



[Hashino, Jinno, MK, Kanemura, Takahashi, Takimoto (2018)]

# Higgs singlet model

Typical example for 1<sup>st</sup> OPT from tree-level mixing

- Tree-level Higgs potential

$$V_0 = -\mu_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 + \mu_{\Phi S} |\Phi|^2 S + \frac{\lambda_{\Phi S}}{2} |\Phi|^2 S^2 + \mu_S^3 S + \frac{m_S^2}{2} S^2 + \frac{\mu'_S}{3} S^3 + \frac{\lambda_S}{4} S^4$$

LISA

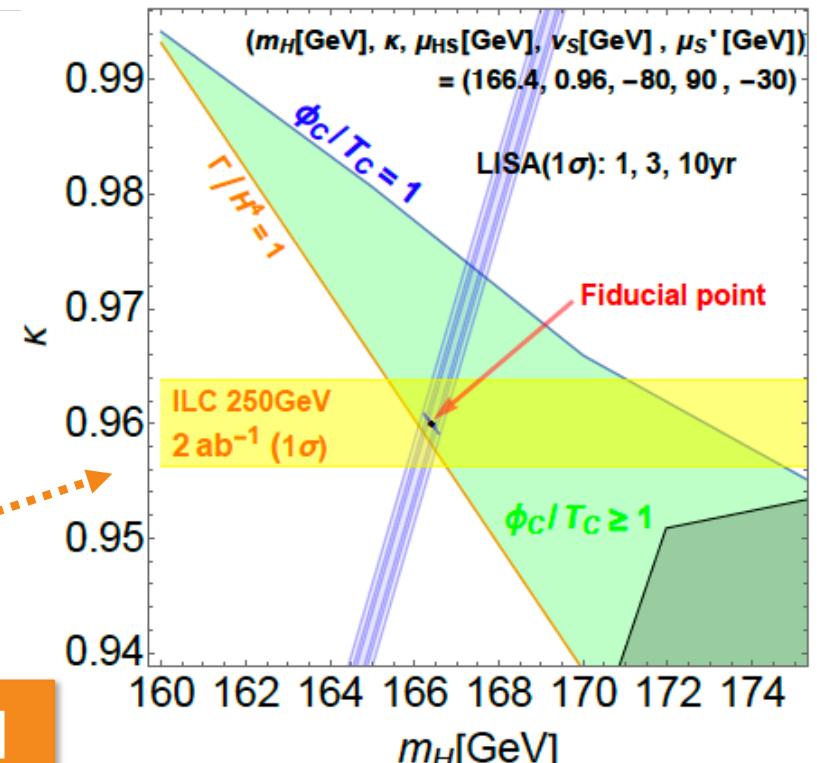
→ Additional Higgs boson mass:  $m_H$

Scaling factor:  $\kappa$  ( $\kappa = 1$  in the SM)

- Fiducial parameters

$$(m_H \text{ [GeV]}, \kappa, \mu_{\Phi S} \text{ [GeV]}, v_S \text{ [GeV]}, \mu'_S \text{ [GeV]}) \\ = (166, 0.96, -80, 90, -30)$$

→  $(\alpha, \beta/H_*, T_* \text{ [GeV]}) \simeq (0.085, 420, 93)$



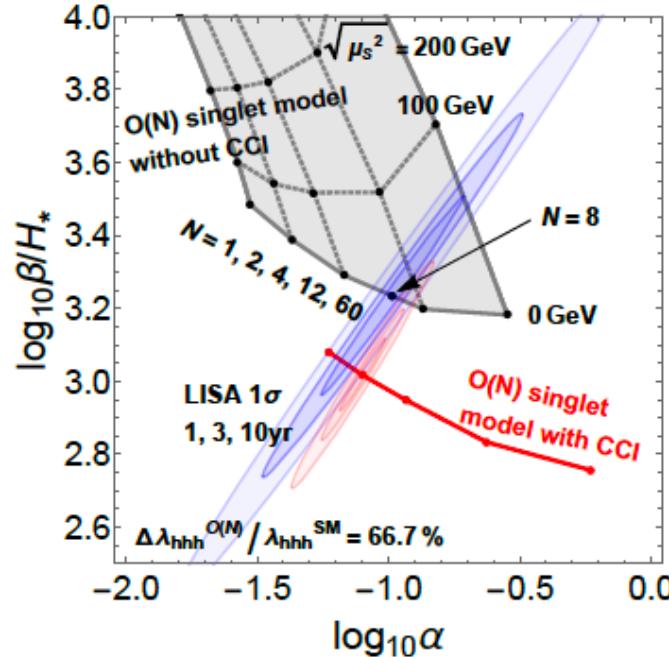
## Future colliders

- ILC [Fujii et al. (2017)]

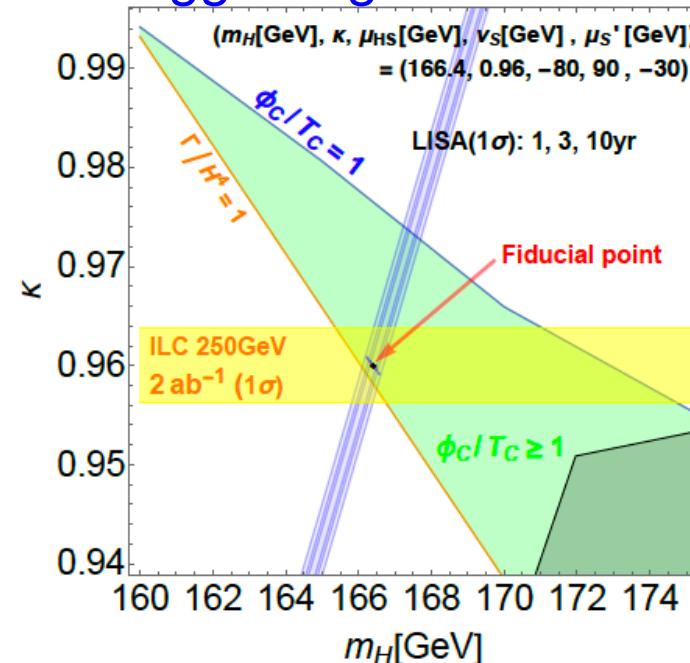
The synergy between colliders and GW observations can narrow down the allowed parameter space

# 6. Summary

- Models with additional singlet scalars



- Higgs singlet model



- We have evaluated the expected constraints on the parameters of new physics models with 1st OPT using future space-based GW observations
- We have shown that the synergy between future colliders and GW observations can play complementary roles in determining model parameters