

# QUARK MATTER 2019

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## Charm-Hadron Production in $pp$ & AA Collisions

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Based on recent work done in collaboration with  
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# Contents

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## 1. Introduction

- Heavy quark probes & charm hadronization

## 2. Charm-hadron production in pp

- SHM augmented with RQM, vs PDG
- Charm-baryon enhancement

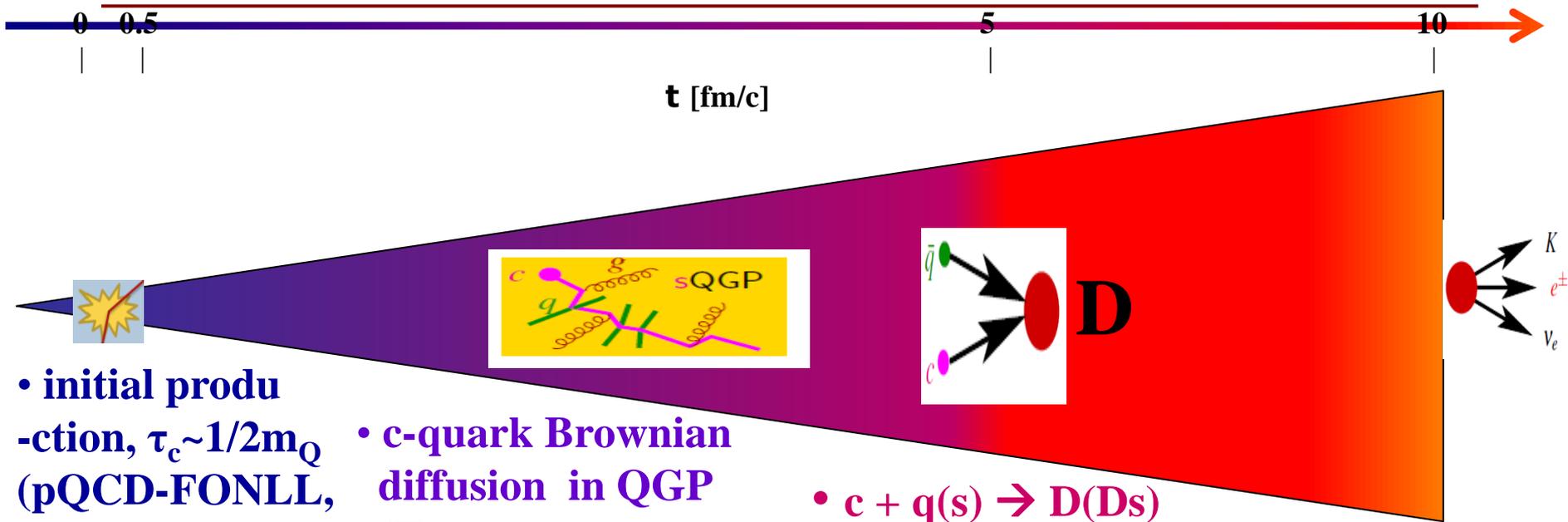
## 3. Charm-hadron production in AA

- 2- & 3-body RRM, equilibrium mapping
- Space-momentum correlations
- Event-by-event implementations of hydro-Langevin-RRM
- RQM augmented baryons

## 4. Results

- Collectivity pattern:  $R_{AA}$ ,  $v_2$  & charm hadro-chemistry:  $D_s^+/D^0$ ,  $\Lambda_c^+/D^0$
- Extraction of charm transport coefficient

# Heavy flavor transport in hot QCD matter



- initial production,  $\tau_c \sim 1/2m_Q$  (pQCD-FONLL, shadowing)

- c-quark Brownian diffusion in QGP (T-mat. reso. corr.)  
low  $p_T$  thermalization  
high  $p_T$  e-loss

- $c + q(s) \rightarrow D(Ds)$

- $c + q + q \rightarrow \Lambda_c$  resonance recombination

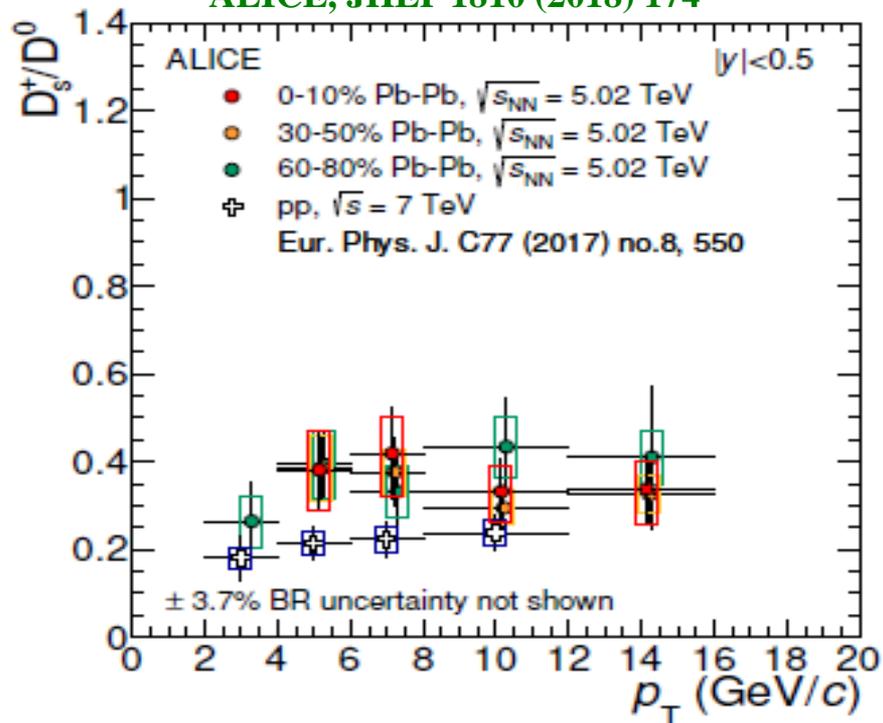
- D-meson diffusion in hadronic liquid

□ Controlled baseline (pQCD), delayed thermalization by  $m_Q/T$ , tagged probe participating in the full fireball history  $\rightarrow$  spectrum & chemistry modifications

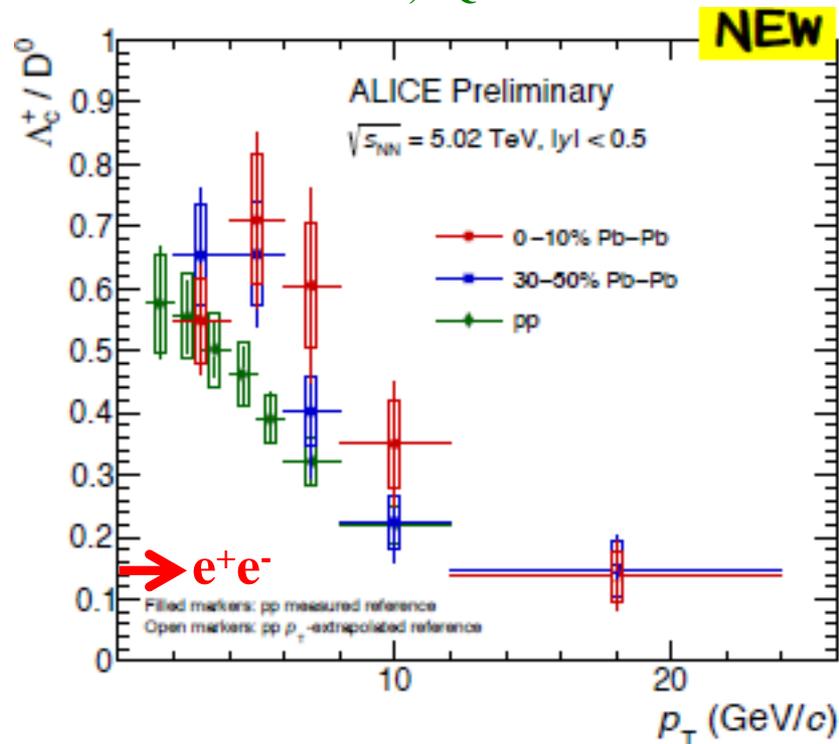
□ Transport coeffi., + diffusion/hadronization simulation on top of bulk hydro  $\rightarrow$  Micro & Macro physics combined vs quantum effects

# $D_s$ & $\Lambda_c$ : Probing charm hadronization

ALICE, JHEP 1810 (2018) 174



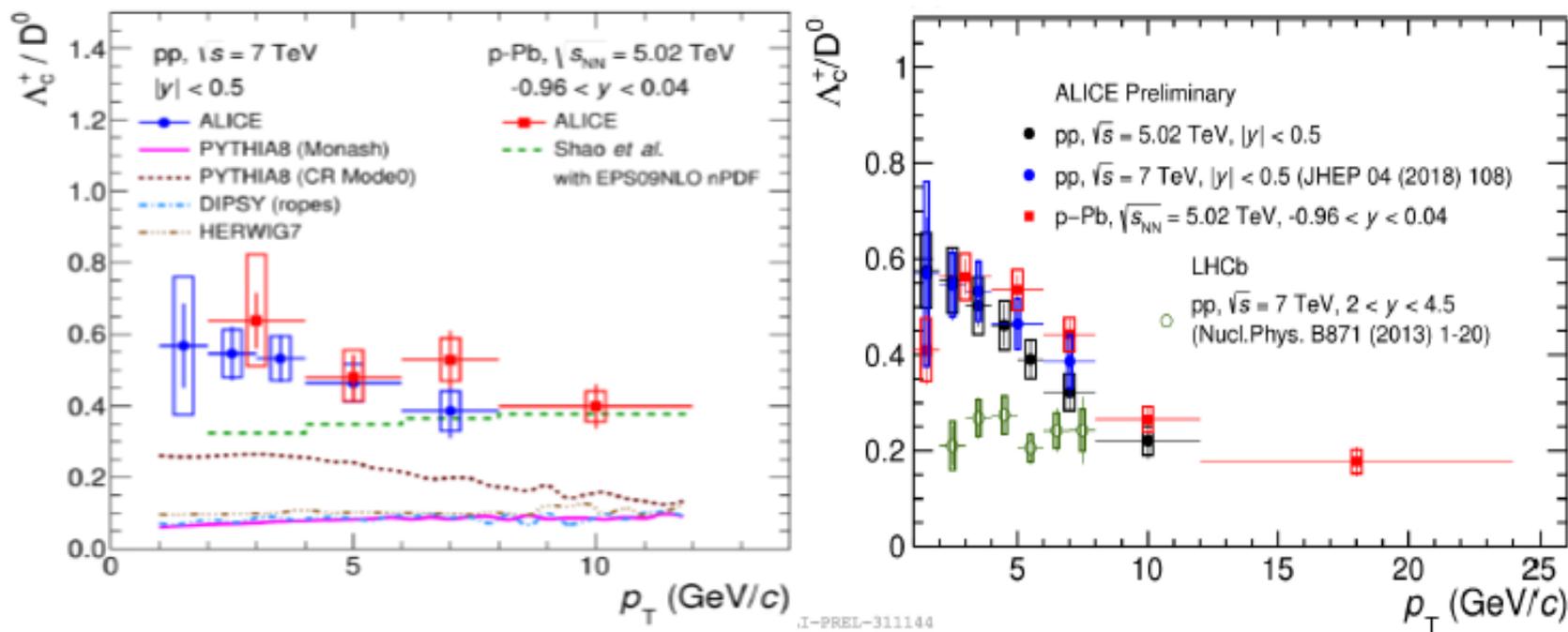
ALICE, SQM19



- $e^+e^-$  : **vacuum fragmentation**, costly to excite  $s\bar{s}$ -pair or diquark-antidiquark pair from vacuum  $\rightarrow D_s$  and  $\Lambda_c$  much suppressed
- high-energy pp: **likely coalescence for  $\Lambda_c$**  in a quark-rich environment!
- AA: **recombination hadronization in QGP**  $\rightarrow$  modifying charm hadro-chemistry

# Charm-hadron production in pp collisions

- Enhanced  $\Lambda_c^+/D^0$  w.r.t. pQCD based MC event generators
- Already a puzzle in pp? → **statistical coalescence (SHM) in a quark-rich environment?!**



- Standard SHM (with PDG only spectra)  $\Lambda_c^+/D^0 \sim 0.22$  too small **P. B.-M.**
- Tension between ALICE (mid-rapidity) vs LHCb (forward-rapidity)?

# Charm-hadron production: pp SHM

- PDG: 5  $\Lambda_C$  (I=0), 3  $\Sigma_C$  (I=1), 8  $\Xi_C$  (I=1/2), 2  $\Omega_C$  (I=0) → missing baryons?!  
 RQM: 18 extra  $\Lambda_C$ , 42 extra  $\Sigma_C$ , 62 extra  $\Xi_C$ , 34 extra  $\Omega_C$  up to 3.5 GeV  
 → supported by lattice [PRD 84 \(2011\) 014025](#); [PoS LAT. 2014 \(2015\) 084](#); [PLB 737 \(2014\) 210](#)

- Statistical Hadronization Model (SHM): 
$$n_i = \frac{d_i}{2\pi^2} m_i^2 T_H K_2\left(\frac{m_i}{T_H}\right)$$

Thermal densities of “prompt” ground-state charmed hadrons for hadronization temperatures of  $T_H = 170$  and 160 MeV (including strong feeddowns) in the PDG and RQM scenarios (assuming 100% BR of  $\Lambda_c^+$ 's and  $\Sigma_c^+$ 's above the DN threshold into  $\Lambda_c^+$ ).

$n_i$ ( $\cdot 10^{-4} \text{ fm}^{-3}$ )	$D^0$	$D^+$	$D^{*+}$	$D_s^+$	$\Lambda_c^+$	$\Xi_c^{+0}$	$\Omega_c^0$
<u>PDG(170)</u>	1.161	0.5098	0.5010	0.3165	<u>0.3310</u>	0.0874	0.0064
PDG(160)	0.4996	0.2223	0.2113	0.1311	0.1201	0.0304	0.0021
<u>RQM(170)</u>	1.161	0.5098	0.5010	0.3165	<u>0.6613</u>	0.1173	0.0144
RQM(160)	0.4996	0.2223	0.2113	0.1311	0.2203	0.0391	0.0044

- Strong feeddowns of excited states all included: BR=100% to  $\Lambda_c^+$  for all  $\Lambda_C$  &  $\Sigma_C$  even above DN (2805 MeV) threshold

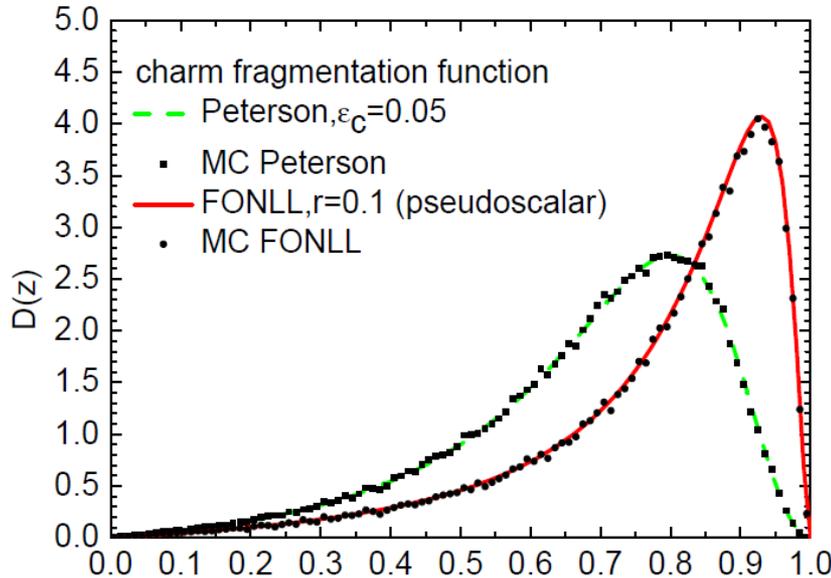
Ratios of  $D^+$ ,  $D^{*+}$ ,  $D_s^+$  and  $\Lambda_c^+$  to  $D^0$  at  $T_H = 170$  and 160 MeV (including strong feeddowns) in the PDG and RQM scenarios.

$r_i$	$D^+/D^0$	$D^{*+}/D^0$	$D_s^+/D^0$	$\Lambda_c^+/D^0$
<u>PDG(170)</u>	0.4391	0.4315	<u>0.2736</u>	<u>0.2851</u>
PDG(160)	0.4450	0.4229	0.2624	0.2404
<u>RQM(170)</u>	0.4391	0.4315	<u>0.2726</u>	<u>0.5696</u>
RQM(160)	0.4450	0.4229	0.2624	0.4409

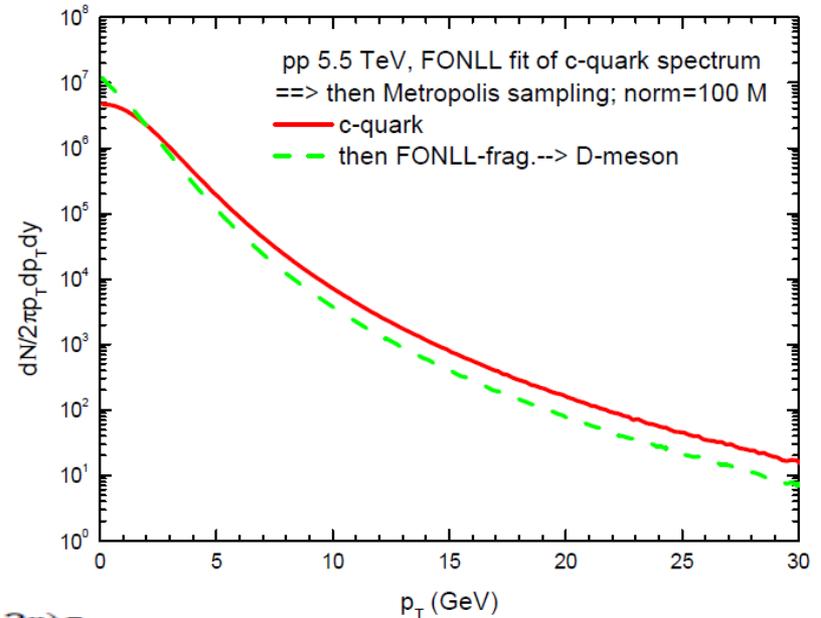
- Strangeness supp.  $\gamma_s=0.6$

# Charm fragmentations and decays

- FONLL fragmentation of charm quarks into all kinds of charm-hadron**  
**relative weight:** according to the SHM thermal densities



$$D_{c \rightarrow H}(z) = N_H \frac{rz(1-z)^2}{[1 - (1-r)z]^6} [(6 - 18(1-2r)z + (21 - 74r + 68r^2)z^2 - 2(1-r)(6 - 19r + 18r^2)z^3 + 3(1-r)^2(1-2r+2r^2)z^4],$$

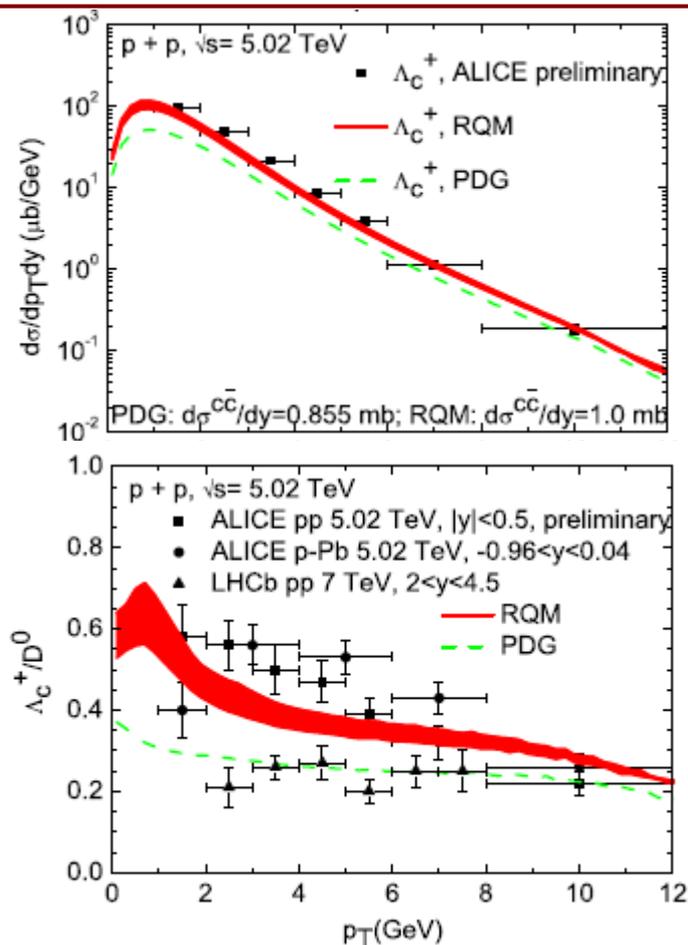
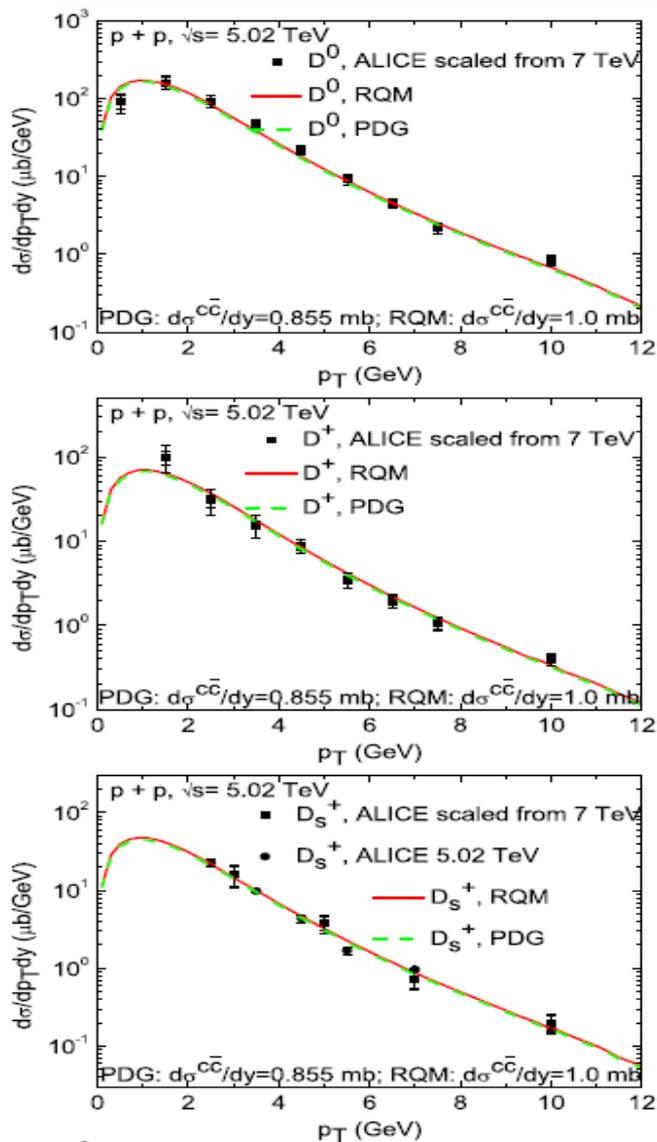


$$r_M/r_{D^0} = ((m_M - m_c)/m_M)/((m_{D^0} - m_c)/m_{D^0})$$

$$r_B/r_{\Lambda_c^+} = ((m_B - m_c)/m_B)/((m_{\Lambda_c^+} - m_c)/m_{\Lambda_c^+})$$

- Decay simulations of all excited states to ground state  $D^0$ ,  $D^+$ ,  $D_s^+$ ,  $\Lambda_c^+$ ,  $\Xi_c$  &  $\Omega_c$**

# Results: pp 5.02 TeV collisions



- Low  $p_T$  enhancement from feeddowns of RQM augmented baryons
- Uncertainty band: BR=50%-100% to  $\Lambda_c^+$  for  $\Lambda_c$  &  $\Sigma_c$  above DN (2805 MeV) threshold

# Charm-hadron production in AA collisions

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- **Charm quark diffusion in QGP: T-matrix & Langevin**
- **2- & 3-body RRM, equilibrium mapping**
- **Space-momentum correlations (SMCs)**
- **Event-by-event implementations of hydro-Langevin-RRM**
- **Analysis: role of SMCs & RQM augmented baryons**
- **Results & observables**

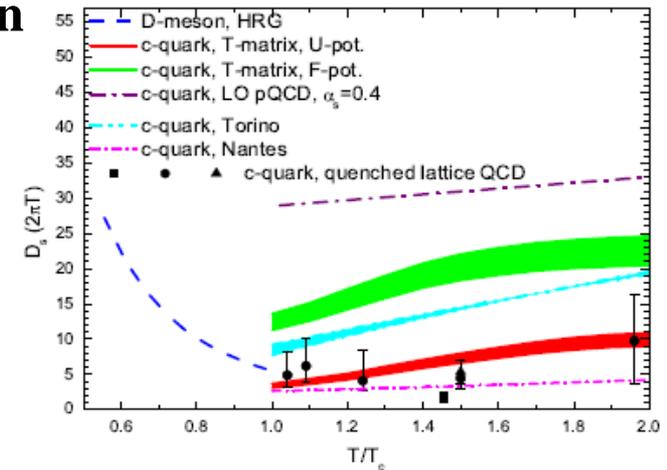
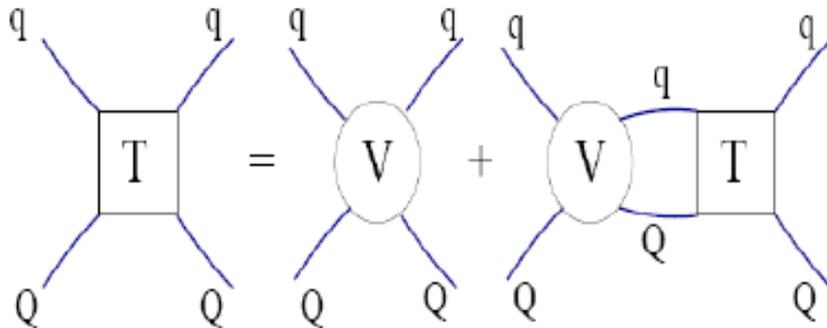
# Charm in QGP: transport coeffi. & diffusion

Langevin + hydro simulation down to  $T_c=170$  MeV  
fluid rest frame updates  $\rightarrow$  boost to lab frame

$$dx_j = \frac{p_j}{E} dt,$$

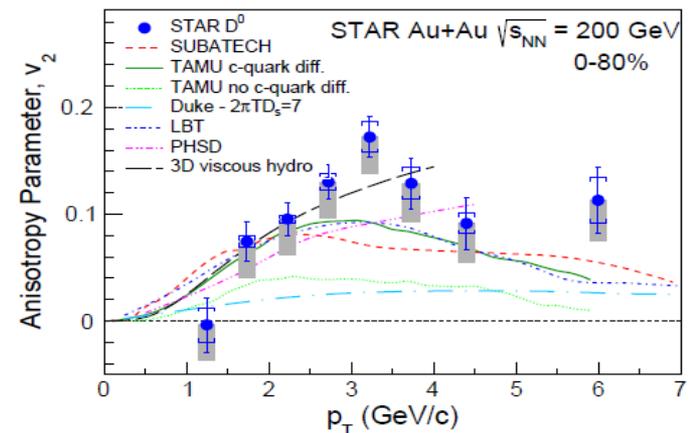
$$dp_j = -\Gamma(p)p_j dt + \sqrt{2dt D(|p + \xi d p|)} \rho_j.$$

## □ Lattice HQ U-pot. T-matrix resummation



## □ p- and T-dependent transport with $\mathcal{D}_s(2\pi T) \sim 2-4$ near $T_{pc}$

## □ Observed large D-meson $v_2$ --- strong coupling of charm with QGP near $T_{pc}$ He, Fries, Rapp



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# Resonance Recombination Model (RRM)

- ◆ Hadronization = Resonance formation  $c\bar{q} \rightarrow D$

→ consistent with T-matrix findings of resonance correlations towards  $T_c$

- ◆ Realized by Boltzmann equation **Ravagli & Rapp, 2007**

$$p^\mu \partial_\mu f_M(t, \vec{x}, \vec{p}) = -m\Gamma f_M(t, \vec{x}, \vec{p}) + p^0 \beta(\vec{x}, \vec{p})$$

$$\beta(\vec{x}, \vec{p}) = \int \frac{d^3 p_1 d^3 p_2}{(2\pi)^6} f_q(\vec{x}, \vec{p}_1) f_{\bar{q}}(\vec{x}, \vec{p}_2) \times \sigma(s) v_{\text{rel}}(\vec{p}_1, \vec{p}_2) \delta^3(\vec{p} - \vec{p}_1 - \vec{p}_2)$$

 gain term  
 Breit-Wigner  

$$\sigma(s) = g_\sigma \frac{4\pi}{k^2} \frac{(\Gamma m)^2}{(s - m^2) + (\Gamma m)^2}$$

- ◆ Equilibrium limit  $f_M(\vec{x}, \vec{p}) = \frac{\gamma_{p,M}}{\Gamma_M} \int \frac{d^3 \vec{p}_1 d^3 \vec{p}_2}{(2\pi)^3} f_q(\vec{x}, \vec{p}_1) f_{\bar{q}}(\vec{x}, \vec{p}_2) \times \sigma_M(s) v_{\text{rel}}(\vec{p}_1, \vec{p}_2) \delta^3(\vec{p} - \vec{p}_1 - \vec{p}_2)$ ,

- ◆ Energy conservation + **detailed balance**



equilibrium mapping between quark & meson distributions

# Generalization to 3-body RRM

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□ The 1<sup>st</sup> step:  $q_1(\mathbf{p}_1) + q_2(\mathbf{p}_2) \rightarrow$  diquark ( $\mathbf{p}_{12}$ )

$$f_d(\vec{x}, \vec{p}_{12}) = \frac{E_d(\vec{p}_{12})}{\Gamma_d m_d} \int \frac{d^3 p_1 d^3 p_2}{(2\pi)^3} f_1(\vec{x}, \vec{p}_1) f_2(\vec{x}, \vec{p}_2) \sigma_{12}(s_{12}) v_{\text{rel}}^{12}(\vec{p}_1, \vec{p}_2) \delta^3(\vec{p}_{12} - \vec{p}_1 - \vec{p}_2)$$

□ The 2<sup>nd</sup> step: diquark ( $\mathbf{p}_{12}$ ) +  $q_3(\mathbf{p}_3) \rightarrow$  baryon ( $\mathbf{p}$ )

$$\begin{aligned} f_B(\vec{x}, \vec{p}) &= \frac{E_B(\vec{p})}{\Gamma_B m_B} \int \frac{d^3 p_{12} d^3 p_3}{(2\pi)^3} f_d(\vec{x}, \vec{p}_{12}) f_3(\vec{x}, \vec{p}_3) \sigma_B(s_{d3}) v_{\text{rel}}^{d3}(\vec{p}_{12}, \vec{p}_3) \delta^3(\vec{p} - \vec{p}_{12} - \vec{p}_3) \\ &= \frac{E_B(\vec{p})}{\Gamma_B m_B} \int \frac{d^3 p_1 d^3 p_2 d^3 p_3}{(2\pi)^6} \frac{E_d(\vec{p}_{12})}{\Gamma_d m_d} f_1(\vec{x}, \vec{p}_1) f_2(\vec{x}, \vec{p}_2) f_3(\vec{x}, \vec{p}_3) \\ &\quad \times \sigma_{12}(s_{12}) v_{\text{rel}}^{12}(\vec{p}_1, \vec{p}_2) \sigma_B(s_{d3}) v_{\text{rel}}^{d3}(\vec{p}_{12}, \vec{p}_3) \Big|_{\vec{p}_{12}=\vec{p}_1+\vec{p}_2} \delta^3(\vec{p} - \vec{p}_1 - \vec{p}_2 - \vec{p}_3) \end{aligned}$$

--- baryons formed via “dynamically” generating an intermediate diquark resonance, finally still depending on 3 quark distributions on equal footing

□ Meson/baryon invariant spectra on hydrodynamic Cooper-Frye hypersurface at  $T_H=170$  MeV

$$\frac{dN_{M,B}}{p_T dp_T d\phi_p dy} = \int \frac{p \cdot d\sigma}{(2\pi)^3} f_{M,B}(\vec{x}, \vec{p})$$

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# Space-momentum correlations (SMCs)

- hydro: a manifestation of SMCs

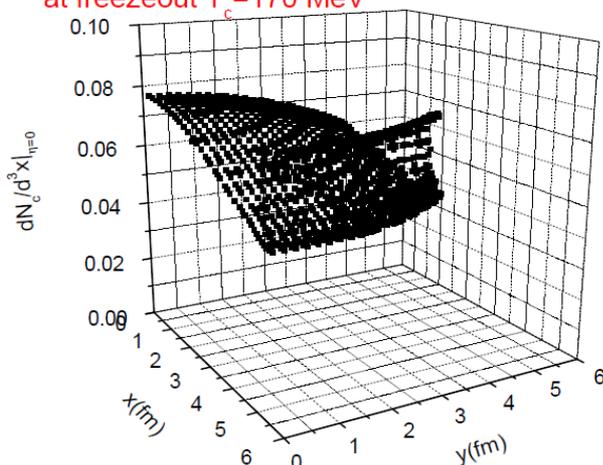
$$f_q^{eq}(\vec{x}, \vec{p}) = g_q e^{-p \cdot u(x)/T(x)} = g_q e^{-\gamma_T(x)[m_T \cosh(y-\eta) - \vec{p}_T \cdot \vec{v}_T(x)]/T(x)}$$

longitudinal boost invariance:  $y - \eta$

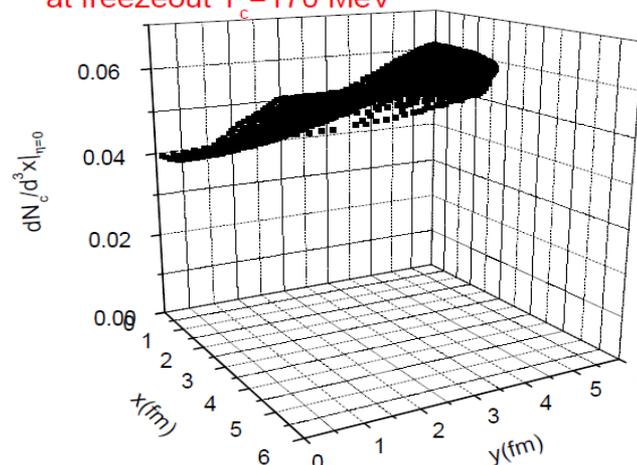
transverse SMCs  $\vec{p}_T \cdot \vec{v}_T$

- hydro-q density: low (high)  $p_T$ -q more concentrated in center (boundary)

hydro light quarks  $p_T=0.0-0.3$  GeV,  
at freezeout  $T_c=170$  MeV



hydro light quarks  $p_T=0.6-0.9$  GeV,  
at freezeout  $T_c=170$  MeV



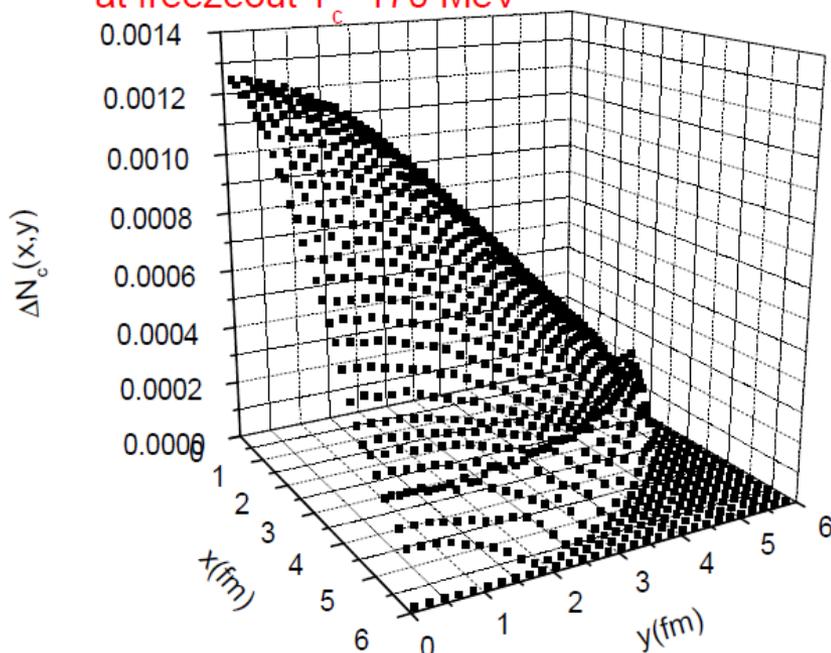
- what if neglecting SMCs: uniformly distributed independent of  $p_T$  as usually done in conventional instantaneous coalescence models

$$f_{c,q}(\vec{x}, \vec{p}) = (2\pi)^3 \frac{dN_{c,q}}{d^3\vec{x}d^3\vec{p}} = \frac{(2\pi)^3}{V E(\vec{p})} \frac{dN_{c,q}}{p_T dp_T d\phi_q dy} \quad \& \quad \int p \cdot d\sigma = E(\vec{p})V$$

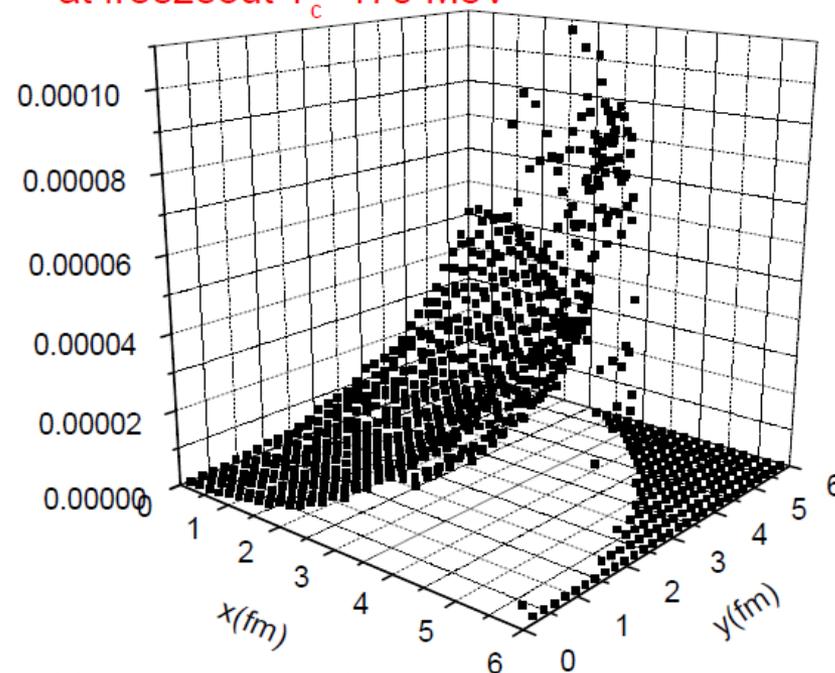
# SMCs: Langevin charm quarks

- Langevin simulation of charm quark diffusion in a hydrodynamically expanding QGP with T-matrix charm thermalization rate
- c-quarks: low (high)  $p_T$ -c more populated in central (outer) region

Langevin charm quarks  $p_T=0.0-1.0$  GeV,  
at freezeout  $T_c=170$  MeV



Langevin charm quarks  $p_T=3.0-4.0$  GeV,  
at freezeout  $T_c=170$  MeV



- SMCs usually neglected in ICMs: uniformly distributed independent of  $p_T$
- what will be the role of SMCs in recombination/RRM?

# Charm-hadron production in AA collisions

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- Charm quark diffusion in QGP: T-matrix & Langevin
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- **Event-by-event implementations of hydro-Langevin-RRM**
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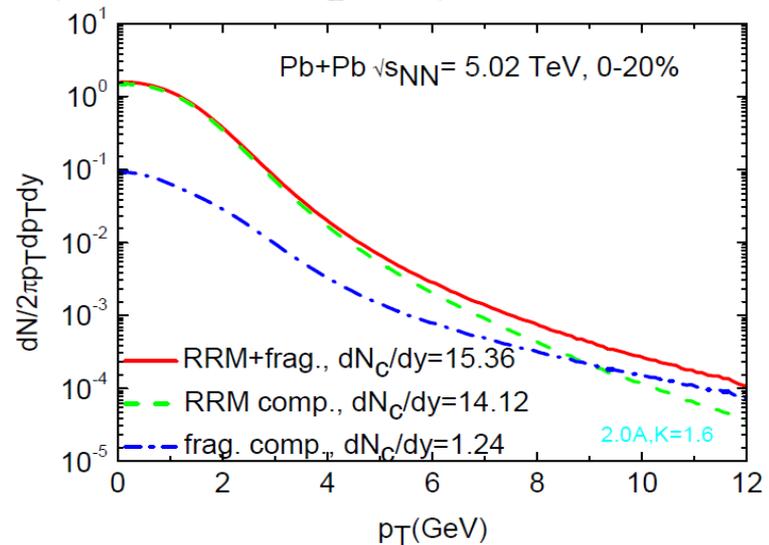
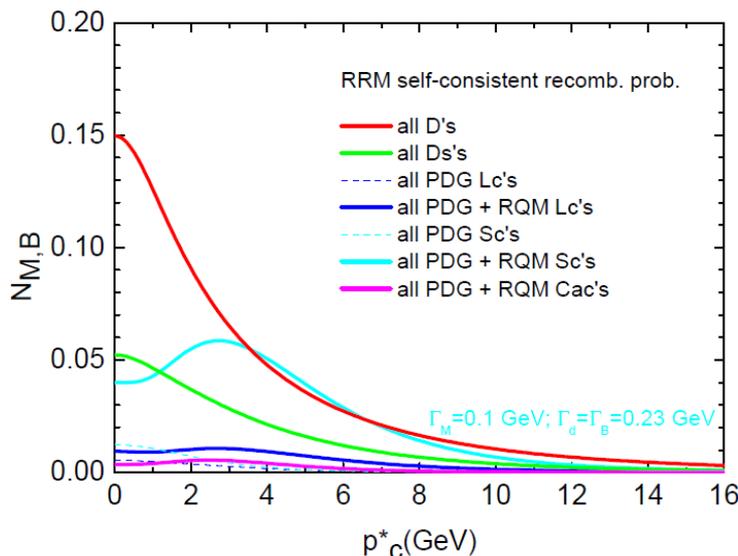
# Charm quark recombination probability

□ No. of mesons/baryons formed from a single c-quark of rest frame  $p_c^*$

$$N_M(p_c^*) = \int \frac{d^3 \vec{p}_1^*}{(2\pi)^3} g_q e^{-E(\vec{p}_1^*)/T_{pc}} \frac{E_M(\vec{p}^*)}{m_M \Gamma_M} \sigma(s) v_{rel},$$

$$N_B(p_c^*) = \int \frac{d^3 p_1 d^3 p_2}{(2\pi)^6} g_1 e^{-E(\vec{p}_1)/T_c} g_2 e^{-E(\vec{p}_2)/T_c} \frac{E_d(\vec{p}_{12})}{m_d \Gamma_d} \sigma(s_{12}) v_{rel}^{12}(\vec{p}_1, \vec{p}_2) \frac{E_B(\vec{p})}{m_B \Gamma_B} \sigma(s_{d3}) v_{rel}^{d3}(\vec{p}_{12}, \vec{p}_{30}),$$

□ Renormalizing  $N_M(p_c^*)$  and  $N_B(p_c^*)$  by a common factor  $\sim 3.6$  for all charmed mesons/baryons such that  $\sum_M P_{coal,M}(p_c^* = 0) + \sum_B P_{coal,B}(p_c^* = 0) = 1$



--- charm conservation consistently built in, in a (e-by-e) way without spoiling the relative chemical equilibrium realized by RRM

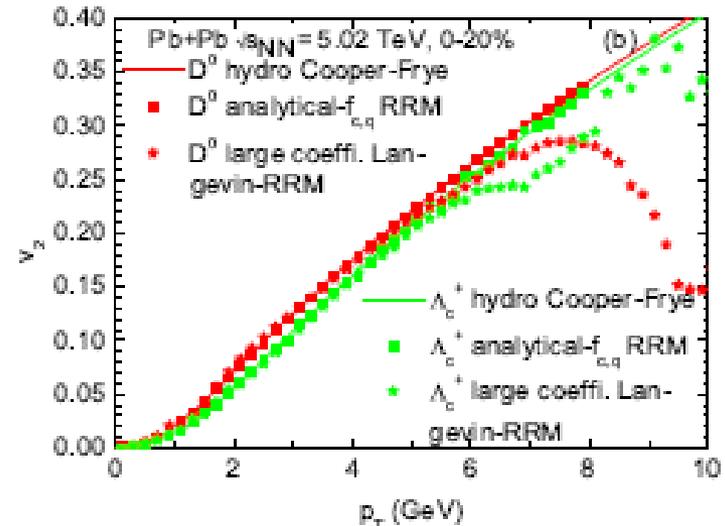
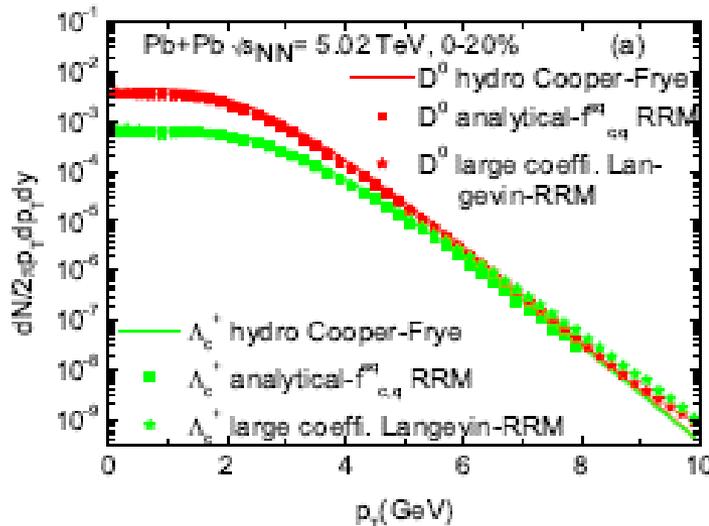
# Event-by-event Langevin-RRM simulation

- for a single Langevin c-quark, sample a/two thermal light-q distribution(s)

$$\frac{dN_M}{d\eta} \Big|_{\eta=0} \equiv \sum_n \Delta N_M[n] = \sum_n \frac{p \cdot d\sigma(j_0)}{m_M \Gamma_M} \sigma(s) v_{\text{rel}} \quad \vec{p} = \vec{p}_{1n} + \vec{p}_c$$

$$\begin{aligned} \frac{dN_B}{d\eta} \Big|_{\eta=0} &\equiv \sum_{n_1} \sum_{n_2} \Delta N_B[n_1, n_2] \\ &= \sum_{n_1} \sum_{n_2} \frac{p \cdot d\sigma(j_0)}{m_B \Gamma_B} \frac{E_d(\vec{p}_{12}^*)}{m_d \Gamma_d} \sigma(s_{12}) v_{\text{rel}}^{12}(\vec{p}_{1n_1}^*, \vec{p}_{2n_2}^*) \sigma(s_{d3}) v_{\text{rel}}^{d3}. \end{aligned} \quad \vec{p} = \vec{p}_{1n_1} + \vec{p}_{2n_2} + \vec{p}_c$$

- equil. mapping with large transport coeffi. checks out: **SMCs incorporated**



- equil. mapping: both **kinetic & chemical**  $\rightarrow$  **observables come out as RRM predictions with realistic T-matrix transport coefficient**

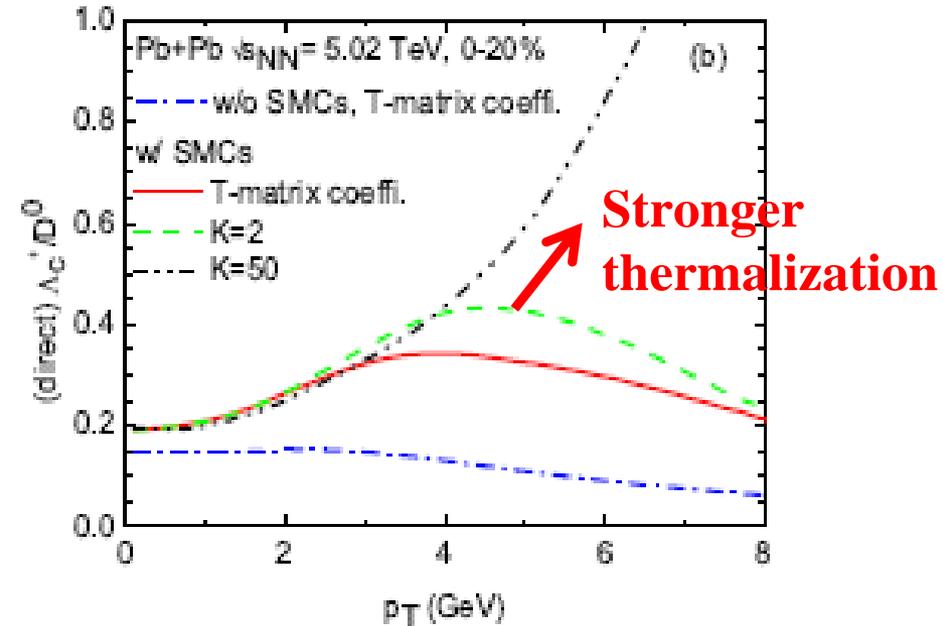
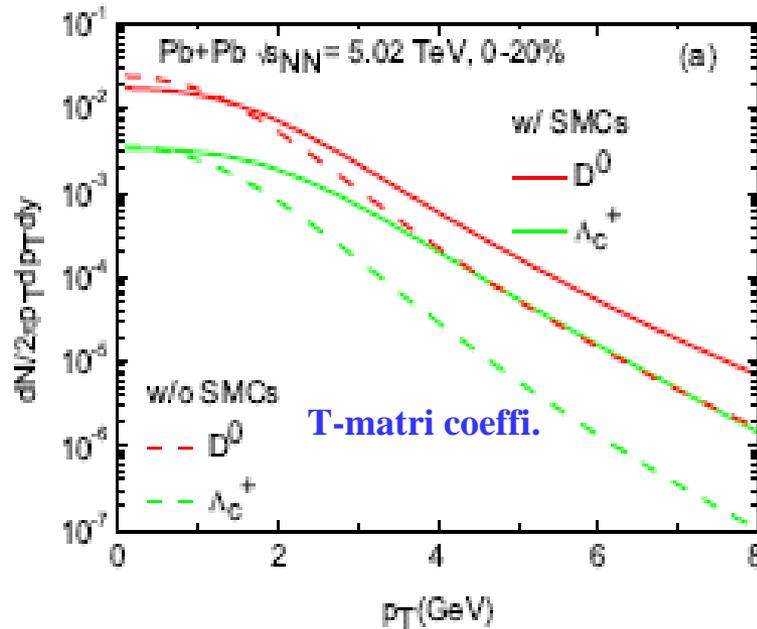
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# Direct $D^0$ & $\Lambda_c^+$ production via RRM

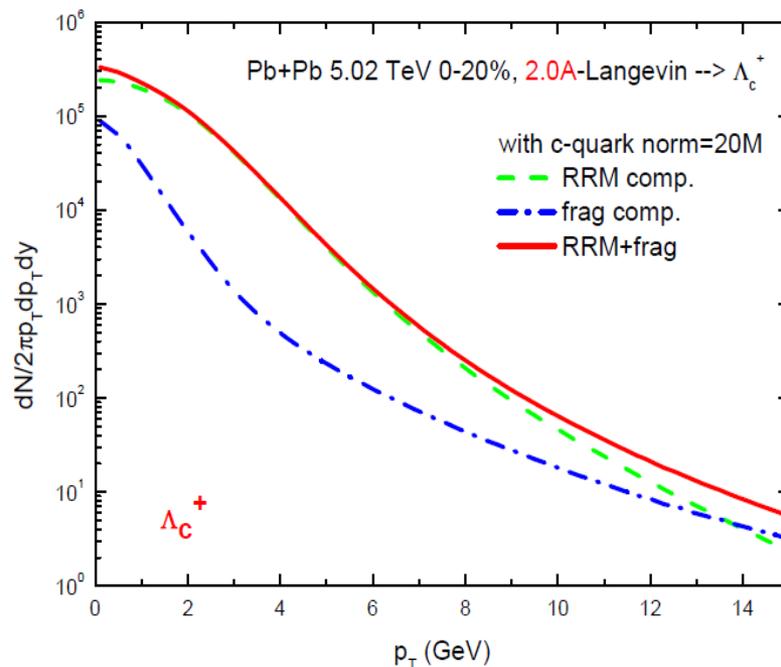
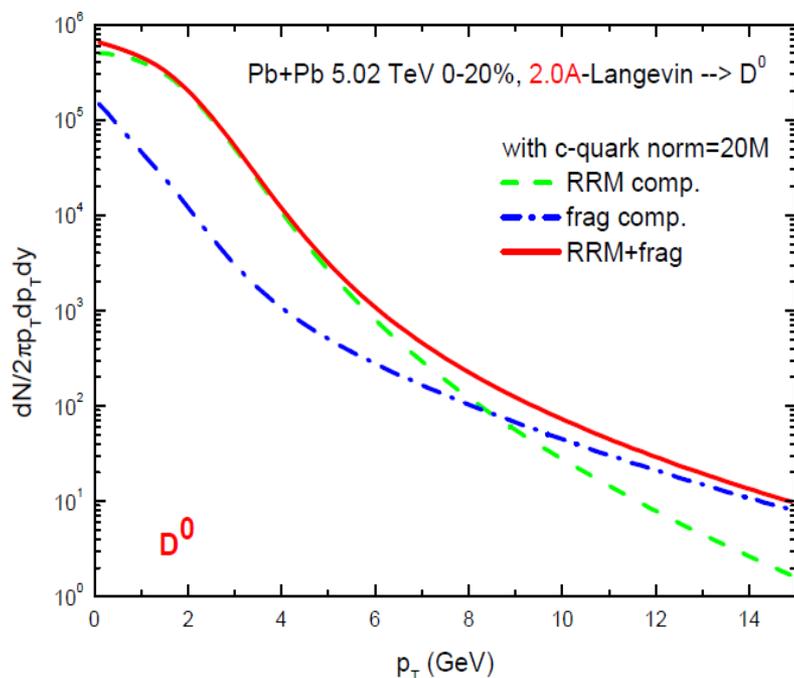
- Including **SMCs** makes the spectra harder & enhances the ratio  $\Lambda_c^+/D_0$



- Relatively fast-moving c-quarks [ $p_T \sim 3-4$  GeV] moving to the outer part of the fireball find higher-density of harder [ $p_T \sim 0.6-0.9$  GeV] light quarks for recombination
- An effect entering squared for the recombination production of  $\Lambda_c^+$

# Recombinant vs fragmenting spectra

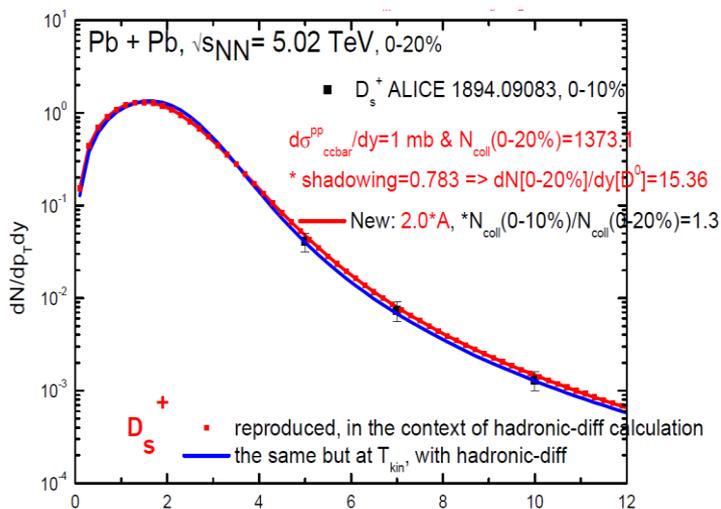
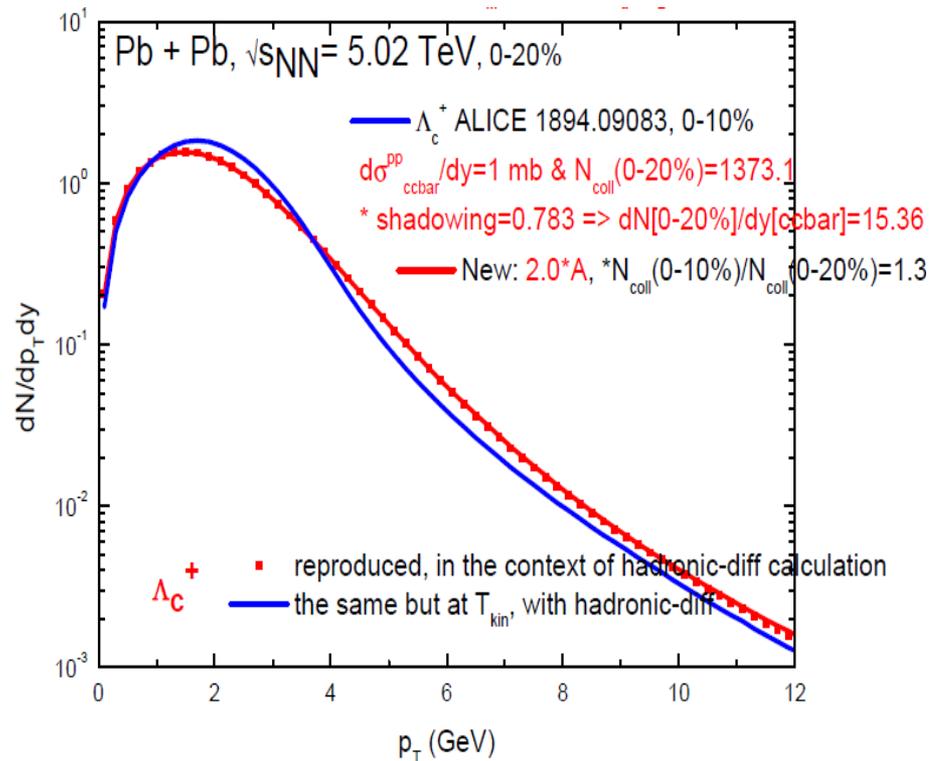
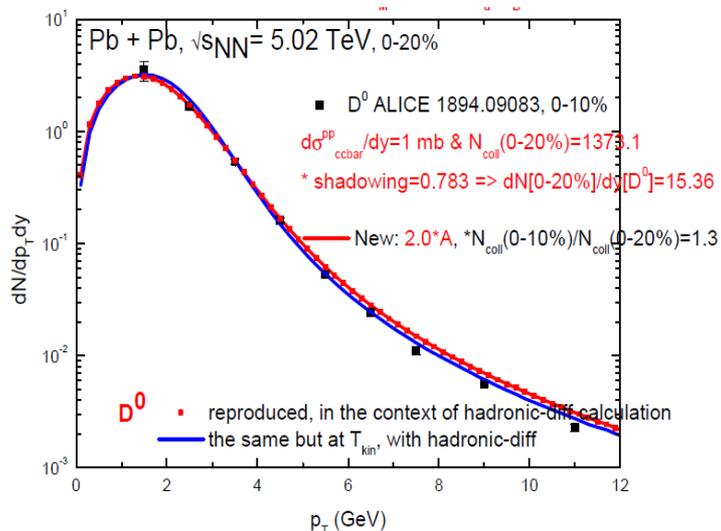
- █ **Hydro-Langevin-RRM(+fragmentation)**: for all charm-mesons/baryons  
 → higher states decay into ground state  $D^0$ ,  $D^+$ ,  $D_s^+$ ,  $\Lambda_C^+$



- █ **SMCs extend the recombinant component toward (quite) higher  $p_T$ ; RQM augmented higher baryon states' RRM spectra even harder (also thanks to SMCs) → RRM & frag. cross at  $p_T \sim 8.5$  (13) GeV for  $D^0$  ( $\Lambda_C^+$ )**

- █ **Helpful for large total  $v_2$  (weighted between RRM vs frag. components)**

# Further interaction in hadronic phase



- Charm-meson/baryon hadronic diffusion coeff.: empirical cross sections *He, Fries, Rapp'12*
- Further mild suppression & mild increase in  $v_2$

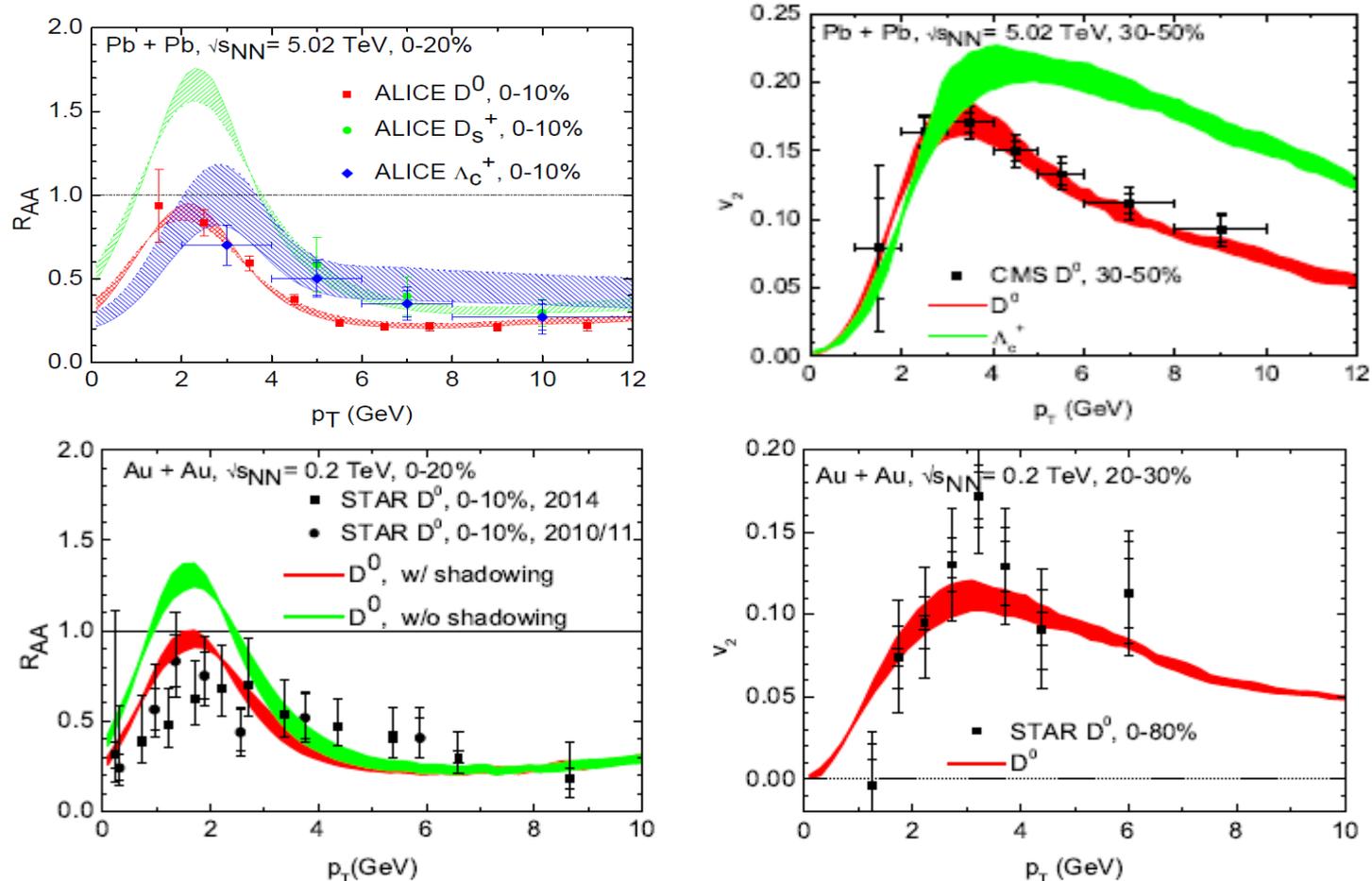
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- Analysis: role of SMCs & RQM augmented baryons
- **Results & observables**

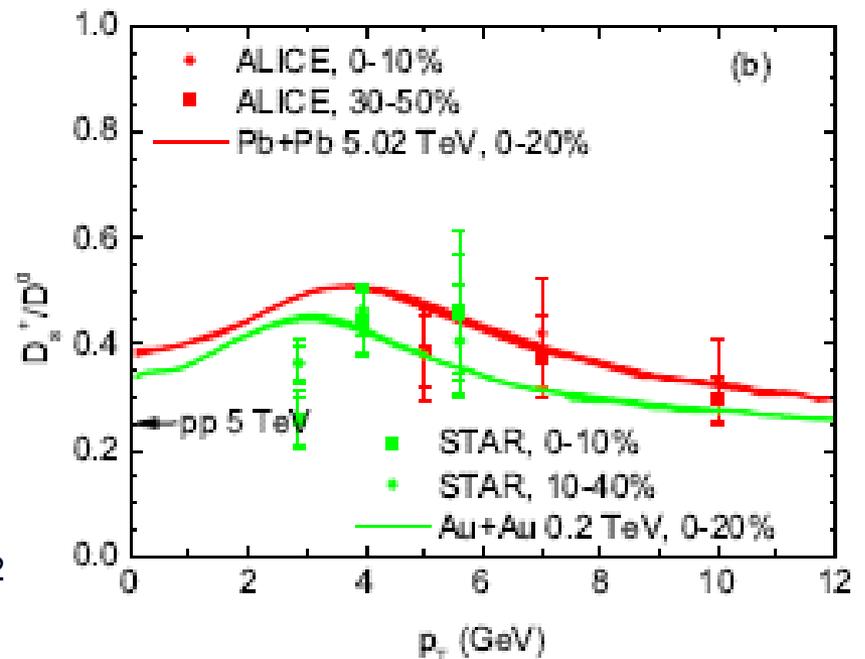
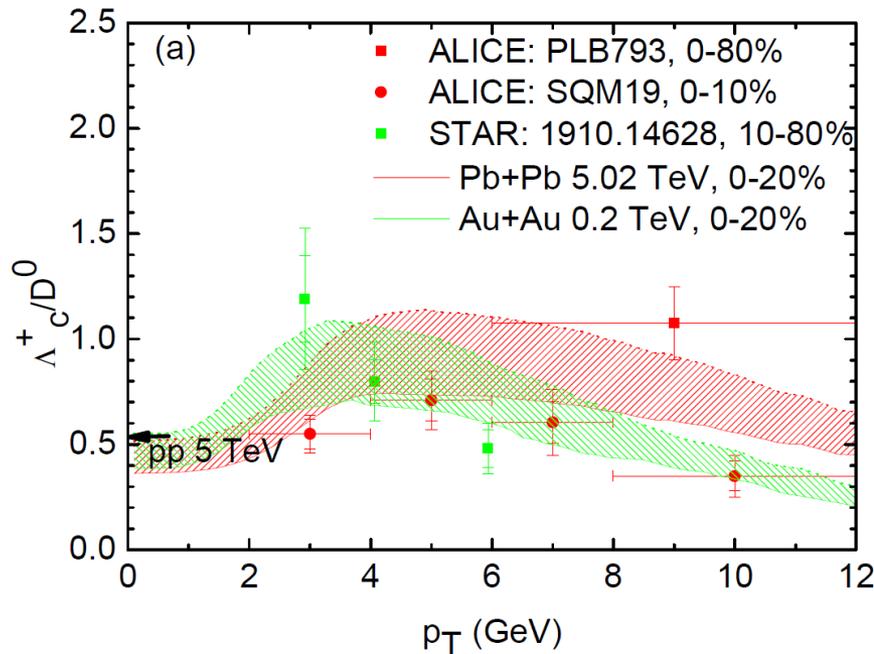
# $D^0$ , $D_s^+$ & $\Lambda_c^+$ suppression & elliptic flow

□ Final total  $D^0$ ,  $D_s^+$  &  $\Lambda_c^+$ , including feeddowns from all RQM baryons



□ T-matrix coefficient\*K-factor(=1.6), to compensate for radiative e-loss;  
uncertainty: **BR=50-100%** to  $\Lambda_c^+$  for  $\Lambda_c^+$ 's &  $\Sigma_c^+$ 's above DN (2805 MeV)

# Total $\Lambda_c^+/\mathbf{D}^0$ & $\mathbf{D}_s^+/\mathbf{D}^0$



- T-matrix coefficient\*K-factor(=1.6), to compensate for radiative e-loss;  
**BR=50-100%** to  $\Lambda_c^+$  for  $\Lambda_c$ 's &  $\Sigma_c$ 's above DN (2805 MeV) threshold
- $\Lambda_c^+/\mathbf{D}^0$ : low  $p_T$  RRM equil. limit = SHM pp; intermediate  $p_T$  enhancement from RRM with SMCs; high  $p_T$  fragmentation pp value;  
Data (updated RHIC and LHC) trend largely reproduced
- $\mathbf{D}_s^+/\mathbf{D}^0$  enhancement: recomb. of charm in a strangeness-equilibrated QGP

# Summary & outlook

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## >> Charm-hadron production in pp collisions

- RQM augmented SHM
- Low  $p_T$  enhancement of  $\Lambda_c^+$  from “missing” charm-baryons

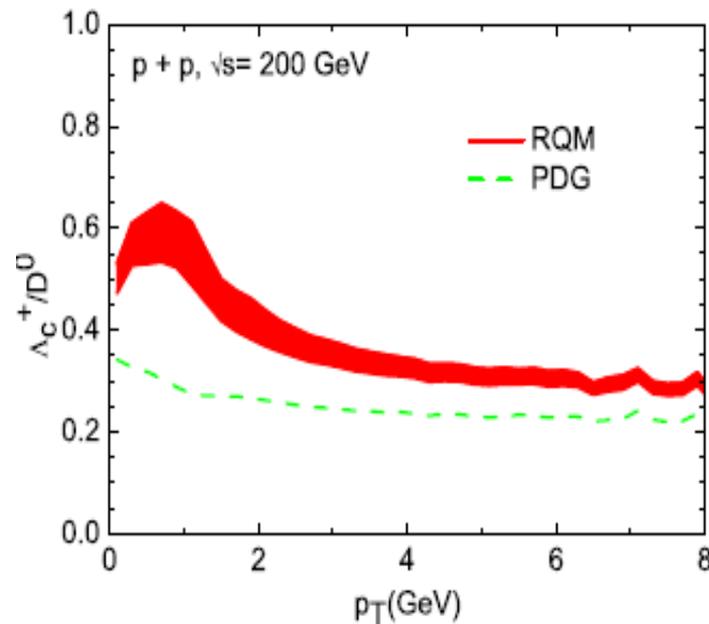
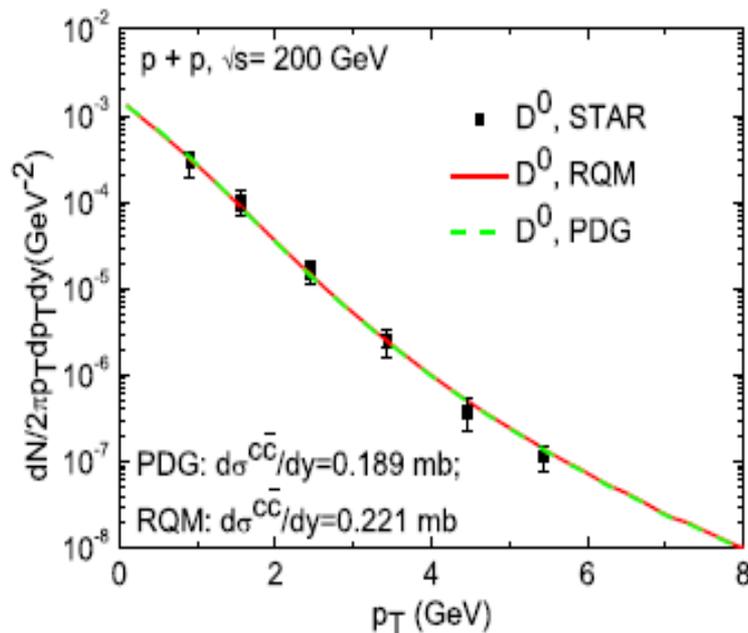
## >> Charm-hadron production in AA collisions

- 3-body RRM developed, equilibrium mapping (both kinetic & chemical) ensured by 4-momentum conservation
- Genuine space-momentum correlations (SMCs) enhancing  $\Lambda_c^+/D^0$ ; exact charm conservation implemented on an e-by-e basis

→ Both have been challenging within conventional instantaneous coalescence models

- $p_T$ -dependent  $\Lambda_c^+/D^0$  &  $D_s^+/D^0$  enhancement emerge from hydro-Langevin-RRM(+fragmentation) simulations; data trend largely reproduced within BR's uncertainties

# Back-up: pp 200 GeV collisions



- Low  $p_T$  enhancement from feeddowns of RQM augmented baryons
- Uncertainty band: BR=50-100% to  $\Lambda_C^+$  for  $\Lambda_C$  &  $\Sigma_C$  above DN (2805 MeV) threshold

# Conserving charm number: Ko & Greco

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of Fig. 3. Being convenient to implement in our event-by-event Langevin-RRM simulation, this *global* renormalization of charm quark coalescence probability does not change the *relative* difference between the  $p_T$  spectra of any two charmed hadrons, therefore not affecting the  $p_T$ -dependent  $\Lambda_c^+/D^0$ . This point is in marked contrast to the treatment in [14], where the authors reduced the harmonic oscillator frequency in determining the hadron wave functions and thereby significantly increased the radii of charmed mesons and baryons (relative to the quark model predictions), in order to use up low  $p_T$  charm quarks in coalescence; the resulting  $\Lambda_c^+/D^0$  was enhanced as a coincidence of using the *same* reduced frequency parameter for charmed mesons and baryons. The same purpose was achieved in [15] by artificially amplifying the normalization constants of the coalescence Wigner functions (the amplification factor of baryons is the square of that of mesons).

# SMCs enhance the $\Lambda_c^+ / D^0$ at $p_T \sim 4.2$ GeV(a)

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$p_{Tc} = 3-4$  GeV and light quarks of  $p_{Tq} = 0.6-0.9$  GeV are more densely distributed in the outer region of the fireball. Therefore these quarks occupy an *effectively smaller* (than the whole fireball volume  $V_{fb}$ ) volume  $V_{c,eff}$  and  $V_{q,eff}$  and thus have *effectively larger* density that can be schematically written as  $\Delta N_c(p_{Tc} = 3 - 4 \text{ GeV})/V_{c,eff}$  and  $\Delta N_q(p_{Tc} = 0.6 - 0.9 \text{ GeV})/V_{q,eff}$ .

Consider, *e.g.*, the formation via RRM of  $D^0$  and  $\Lambda_c^+$  of the same  $p_T = 4.2$  GeV. In the most straightforward picture, recombination proceeds by adding the momenta of the participating constituent quarks according to their mass ratio  $m_c/m_q = 5$ , once they are spatially adjacent. Therefore, charm quarks of  $p_{Tc} = 3.0-3.5$  GeV that are already roaming around the outer region of the fireball, will have good chance to recombine with the light quarks of  $p_{Tq} = 0.6-0.7$  GeV (remember they are also most likely to show up in the outer region) to form  $D^0$  and  $\Lambda_c^+$  of (almost) the same  $p_T = 4.2$  GeV, roughly following the momentum addition rule  $3.5 + 0.7 = 4.2$  GeV and  $3.0 + 0.6 + 0.6 = 4.2$  GeV, respectively. Then the RRM production yield of  $D^0$  and  $\Lambda_c^+$  of the same  $p_T = 4.2$  GeV is schematically expressed as

# SMCs enhance the $\Lambda_c^+ / D^0$ at $p_T \sim 4.2$ GeV(b)

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$$\begin{aligned}\Delta N_{D^0}(4.2) &\sim \frac{\Delta N_c(3.0 - 3.5)}{V_{c,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}} & (8) \\ \Delta N_{\Lambda_c^+}(4.2) &\sim \frac{\Delta N_c(3.0 - 3.5)}{V_{c,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}}\end{aligned}$$

quarks in the specified  $p_T$  interval (*i.e.*,  $p_{Tc} = 3.0-3.5$  GeV for charm quarks and  $p_{Tq} = 0.6-0.7$  GeV for light quarks) becomes higher than the case of RRM neglecting space-momentum correlations, where  $V_{c/q,\text{eff}}$  is replaced with the whole fireball volume  $V_{\text{fb}}$  and the densities thus become *uniform* and *smaller*. Furthermore, while the higher light quark spatial density is counted only once in  $D^0$ 's RRM, the square of it comes into the  $\Lambda_c^+$ 's RRM, leading to a stronger enhancement in  $\Lambda_c^+$  spectra and thereby an enhanced  $\Lambda_c/D^0$  ratio, relative to the case of RRM without incorporating space-momentum correlations.

# Langevin equil. Limit with large coeffi.

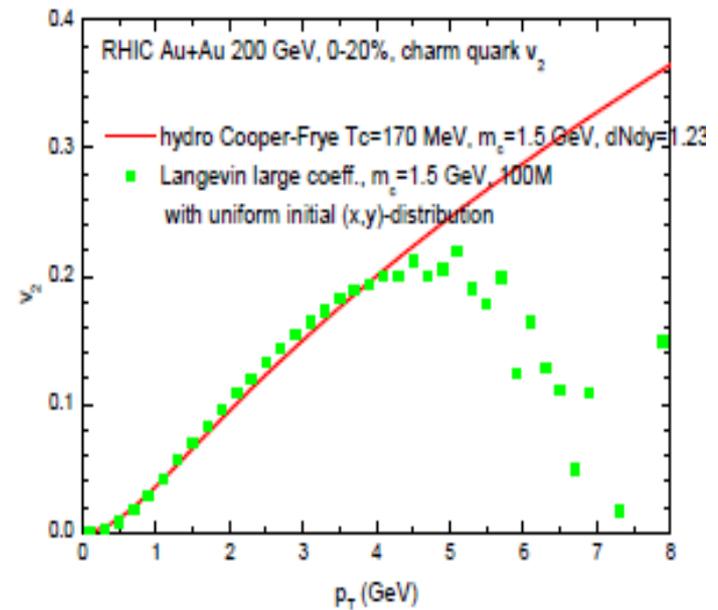
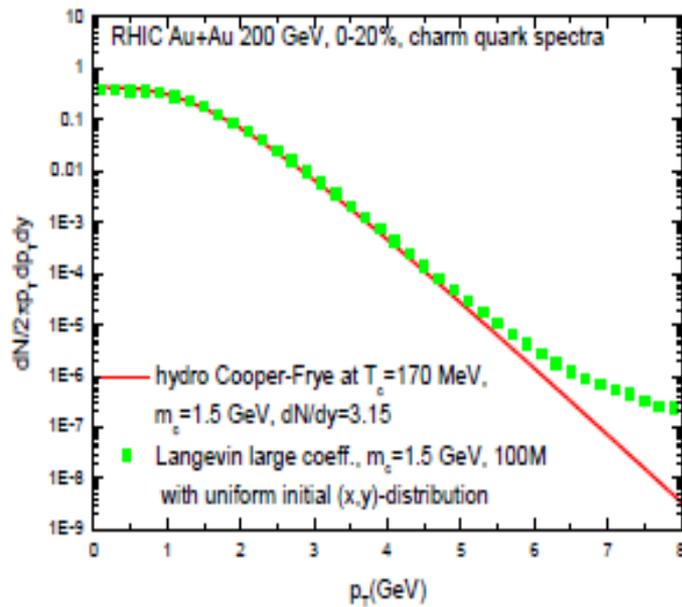
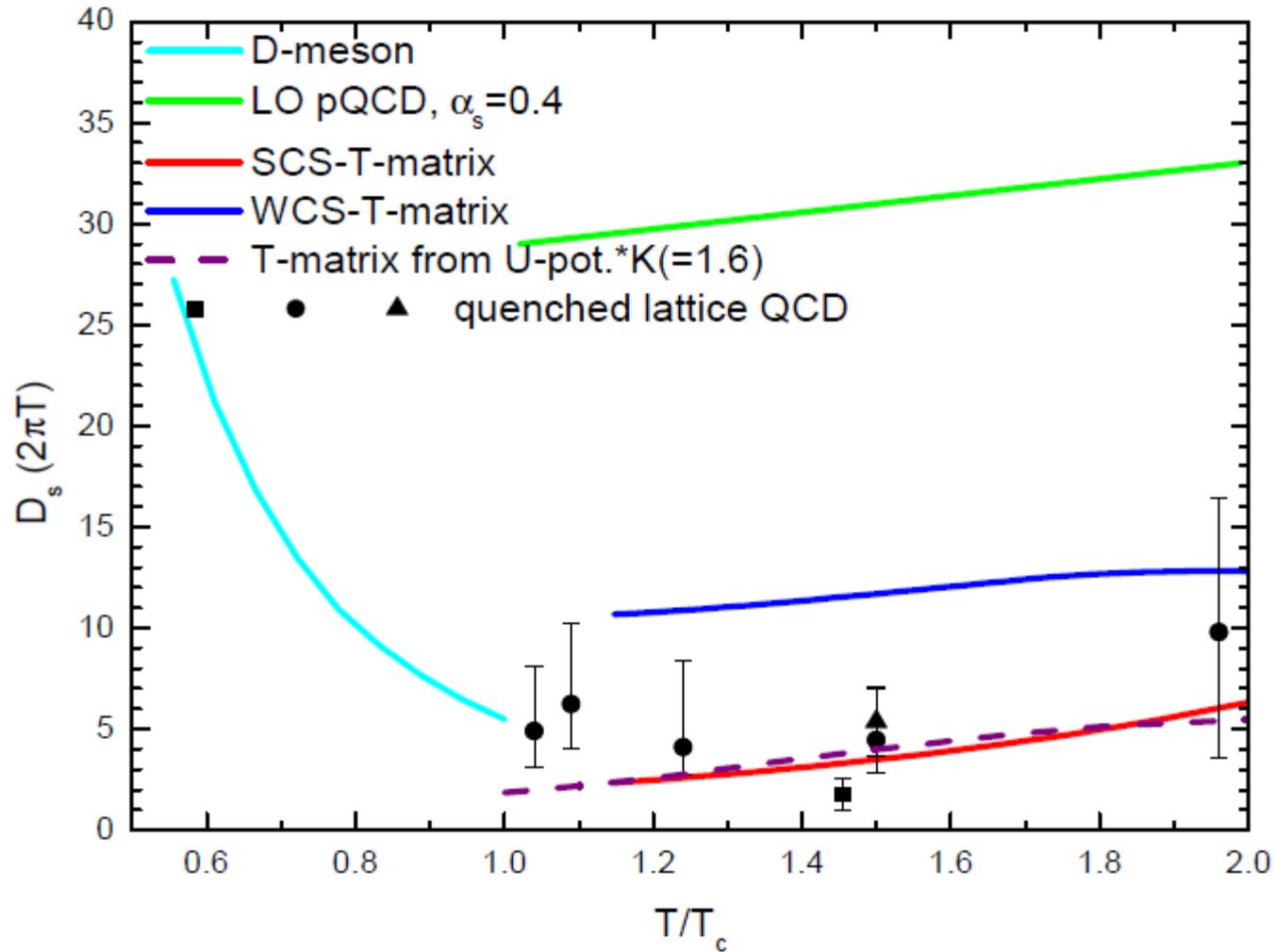
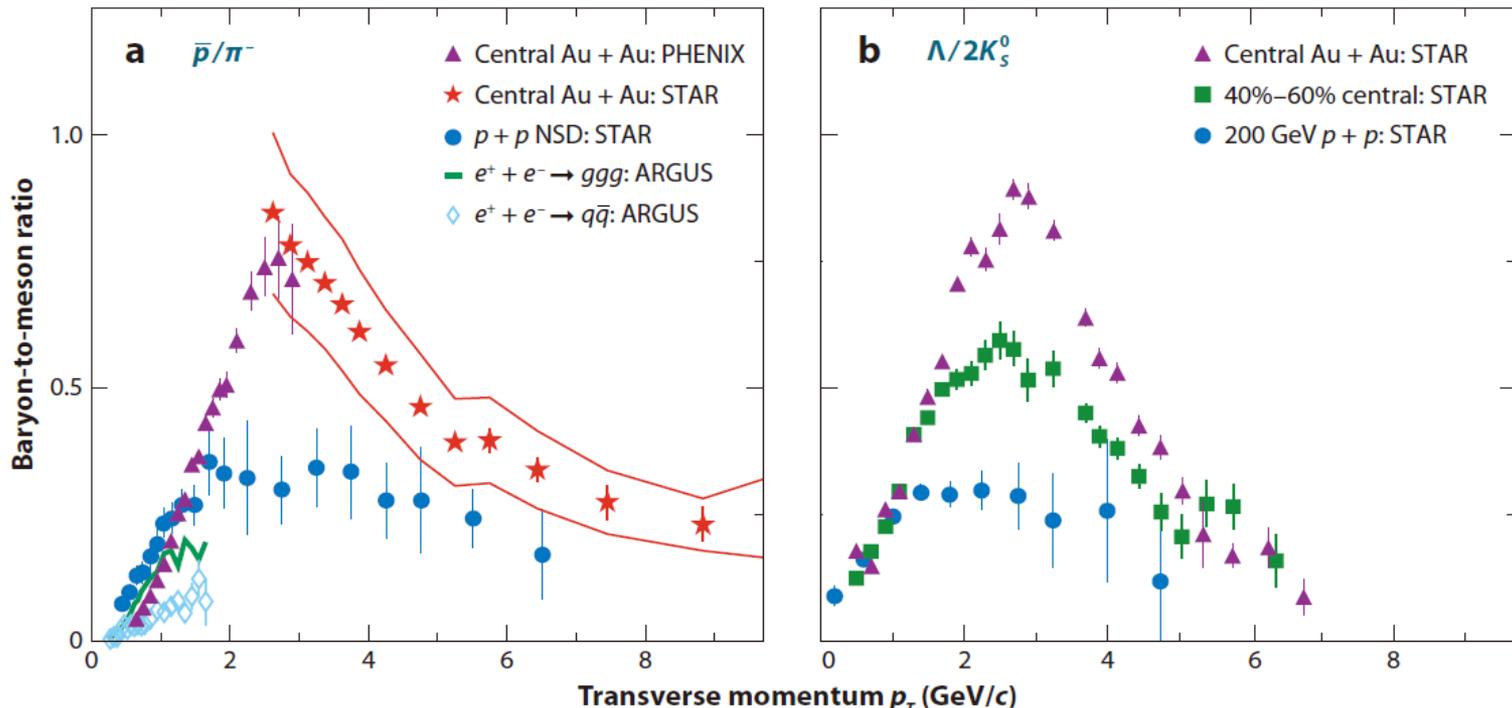


Figure 9. Langevin charm quark  $p_T$  spectra and  $v_2$  with large coefficient.

# Ds(2piT): K=1.6 vs updated SCS T-matrix

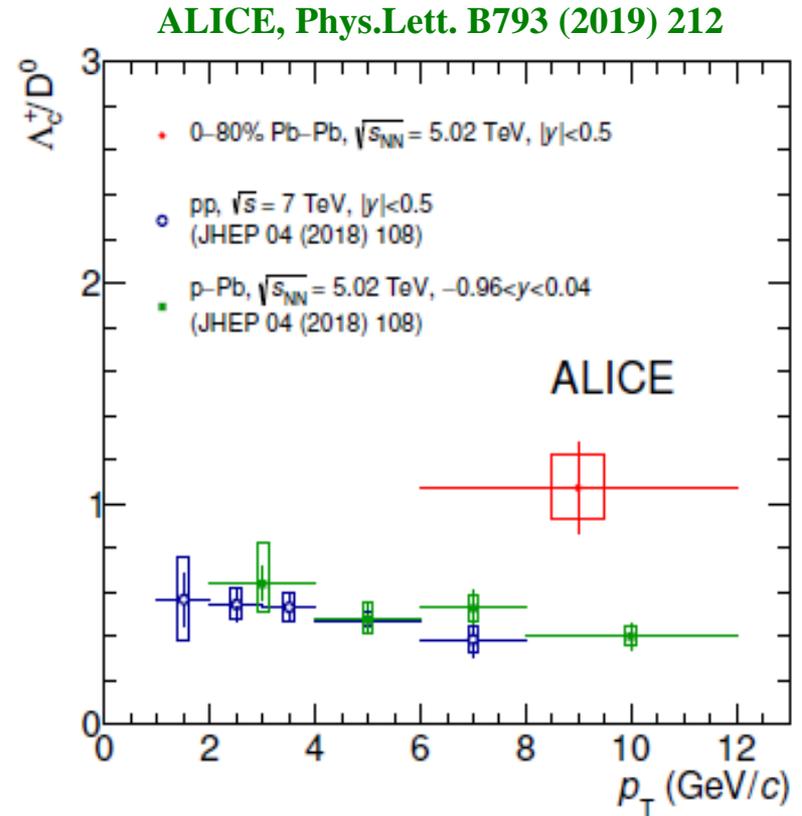
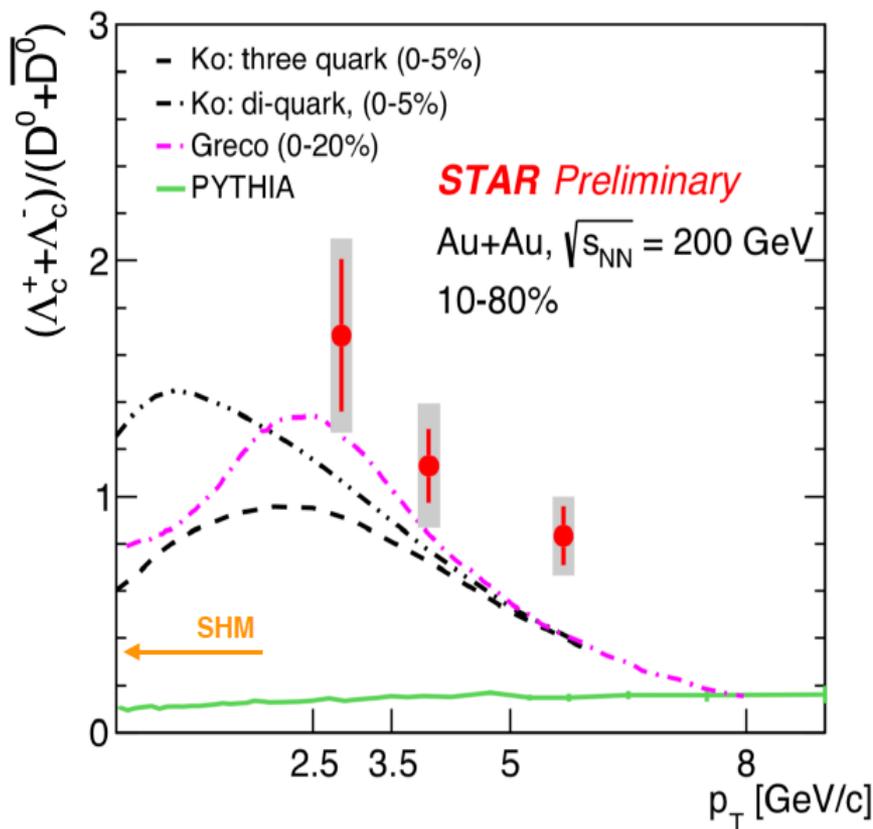


# Baryon to meson ratio enhancement



- B/M enhanced at intermediate  $p_T$  in central AA collisions
  - Nicely (straightforwardly) explained by coalescence models **Ko, Fries, Hwa**
  - A direct indication of the working of coalescence hadronization
- $$f_M(p_T) \sim f_q(p_T/2) * f_{q\bar{q}}(p_T/2) \quad \text{VS} \quad f_B(p_T) \sim f_q(p_T/3) * f_q(p_T/3) * f_q(p_T/3)$$

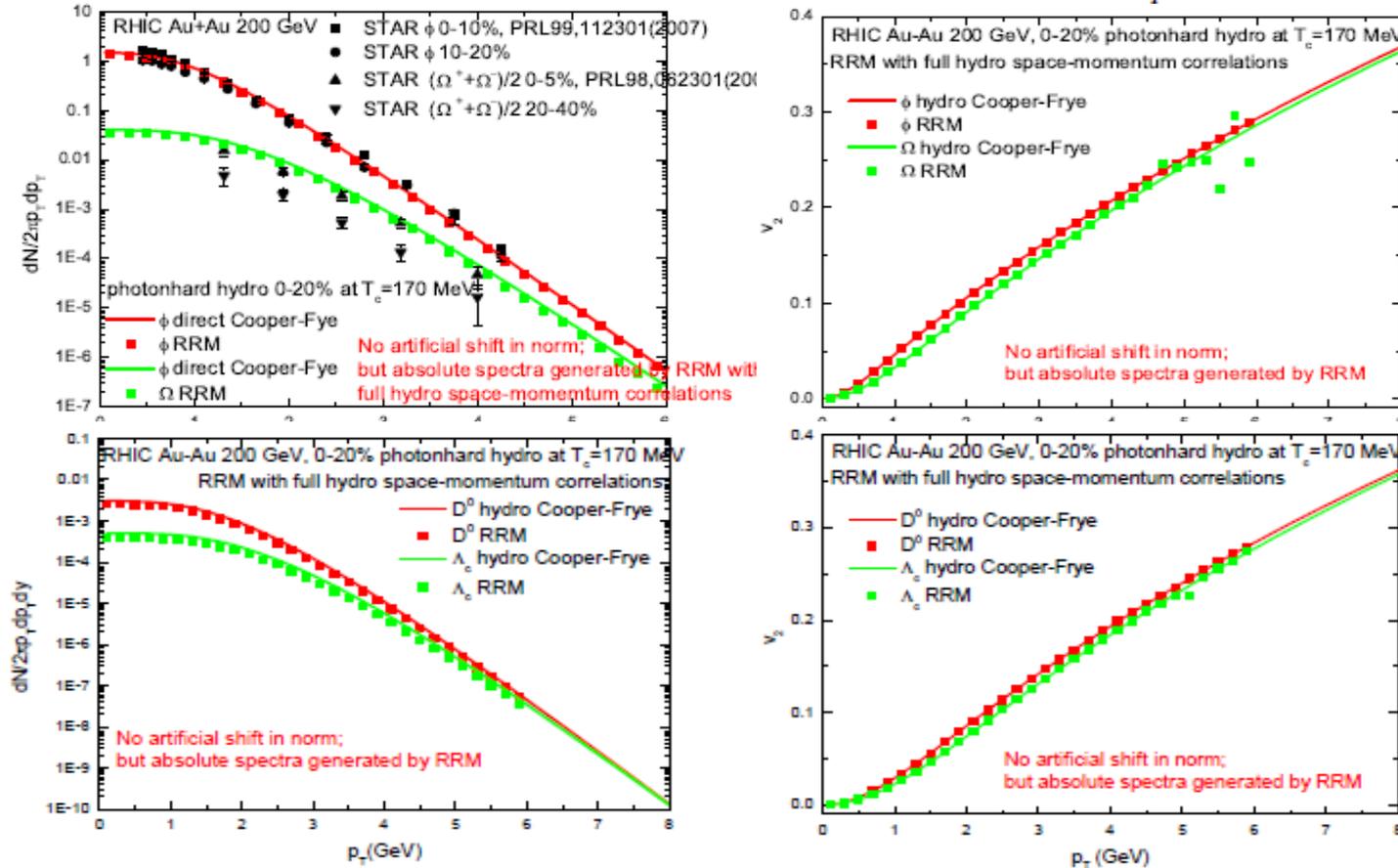
# Does it carry over to the HF sector?



- A sensitive probe of HQ hadronization via recombination in the presence of deconfined QGP
- A direct measure of the degree of HQ thermalization/interaction strength

# RRM: equilibrium mapping

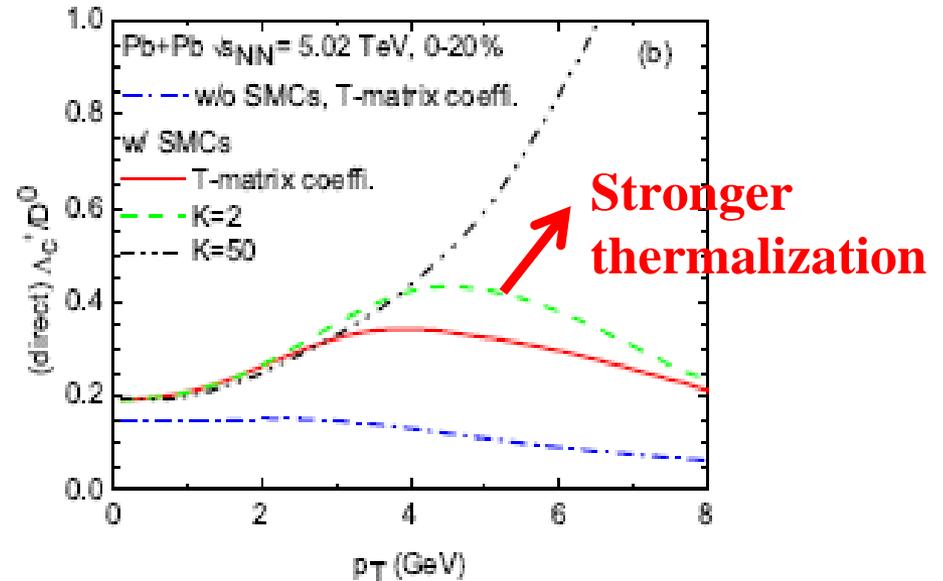
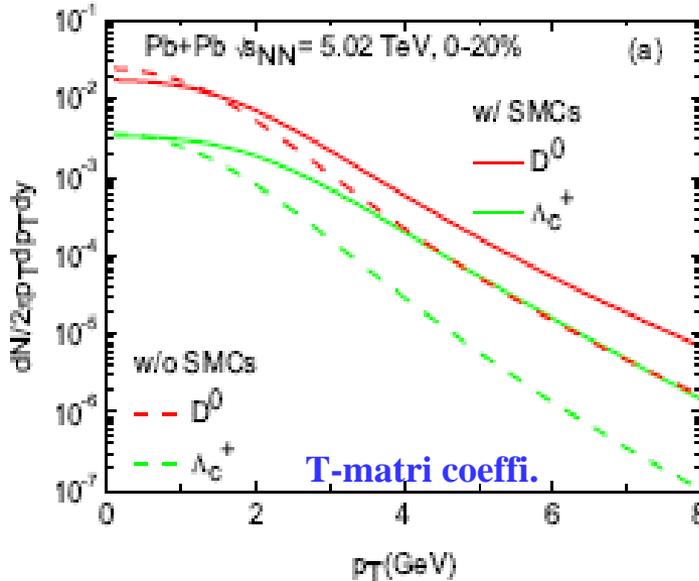
□ RRM on hydrofreezeout hypersurface at  $T_c$  with  $f_q^{eq}(\vec{x}, \vec{p}) = g_q e^{-p \cdot u(x)/T(x)}$



□ Equilibrium mapping: ensured by 4-momentum conservation in RRM  
 $m_q=0.3, m_s=0.4, m_c=1.5, \Gamma_M \sim 0.1 \text{ GeV}, \Gamma_d \sim 0.2 \text{ GeV}, \Gamma_B \sim 0.3 \text{ GeV}$

# Direct $D^0$ & $\Lambda_c^+$ production via RRM

- Including **SMCs** makes the spectra harder & enhances the ratio  $\Lambda_c^+/D^0$



- Consider RRM formation of  $D^0$  ( $3.5+0.7$ ) &  $\Lambda_c^+$  ( $3.0+0.6+0.6$ ) of  $p_T \sim 4.2$  GeV: **enhancement of density** of light- $q$  of  $p_T \sim 0.6-0.7$  GeV &  $c$  of  $p_T \sim 3.0-3.5$  GeV

$$\Delta N_{D^0}(4.2) \sim \frac{\Delta N_c(3.0 - 3.5)}{V_{c,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}} \quad (15)$$

--- **Rencombinant quark density enhanced vs w/o SMCs:  $V_{\text{eff}} < V_{\text{fb}}$**

$$\Delta N_{\Lambda_c^+}(4.2) \sim \frac{\Delta N_c(3.0 - 3.5)}{V_{c,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}} \cdot \frac{\Delta N_q(0.6 - 0.7)}{V_{q,\text{eff}}}$$

--- **Enhanced light- $q$  density entering  $D^0$  RRM only once vs twice (squared) for  $\Lambda_c^+$  RRM  $\rightarrow$  the ratio  $\Lambda_c^+/D^0$  enhanced!**