

QCD factorization and universality of jet cross sections in heavy-ion collisions

Felix Ringer

UC Berkeley/LBNL

In collaboration with Jian-Wei Qiu, Nobuo Sato, Pia Zurita

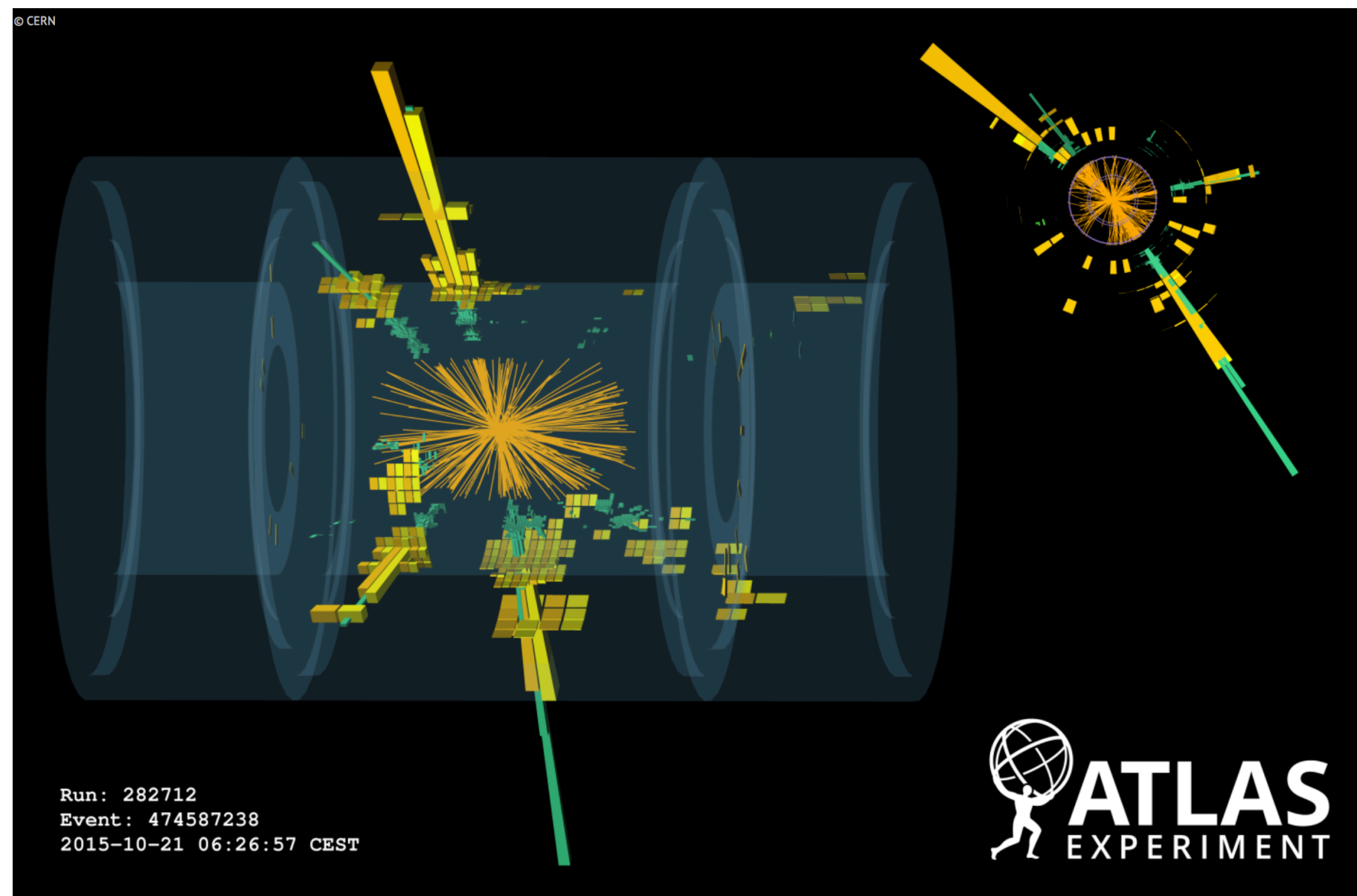


Quark Matter 2019, Wuhan, 11/06/19

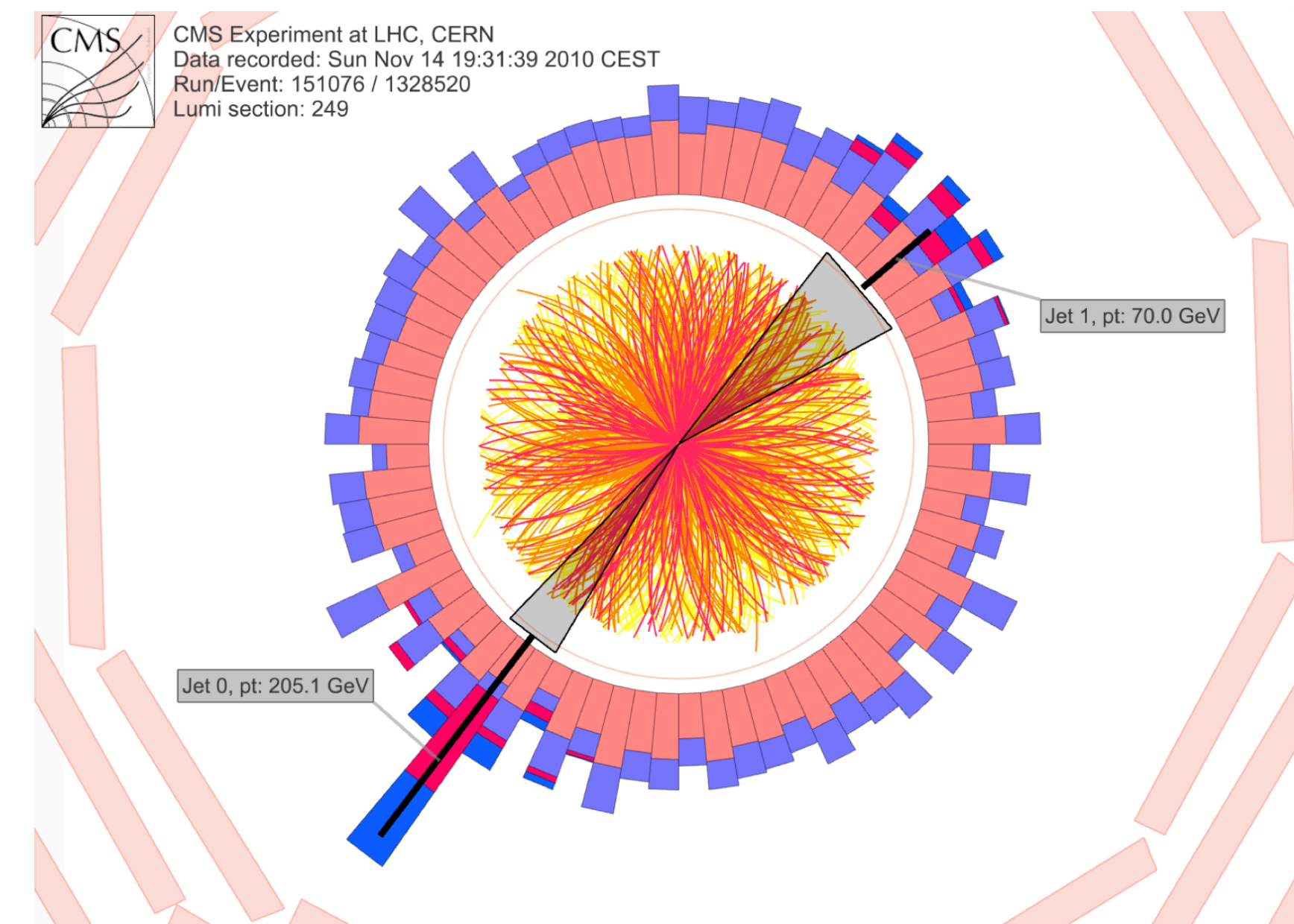


Jets in proton-proton and heavy-ion collisions

$$pp \rightarrow \text{jet} + X$$



$$AA \rightarrow \text{jet} + X$$



- Inclusive jet cross section $\frac{d\sigma^{pp \rightarrow \text{jet} + X}}{dp_T d\eta}$
- Precision calculations available in perturbative QCD

- Nuclear modification factor $R_{AA}^{\text{jet}} = \frac{d\sigma^{\text{PbPb} \rightarrow \text{jet} + X}}{\langle T_{AA} \rangle d\sigma^{pp \rightarrow \text{jet} + X}}$
- QCD Factorization?

Outline

- Introduction
- QCD factorization and universality
- Inclusive jets in heavy-ion collisions
- Conclusions

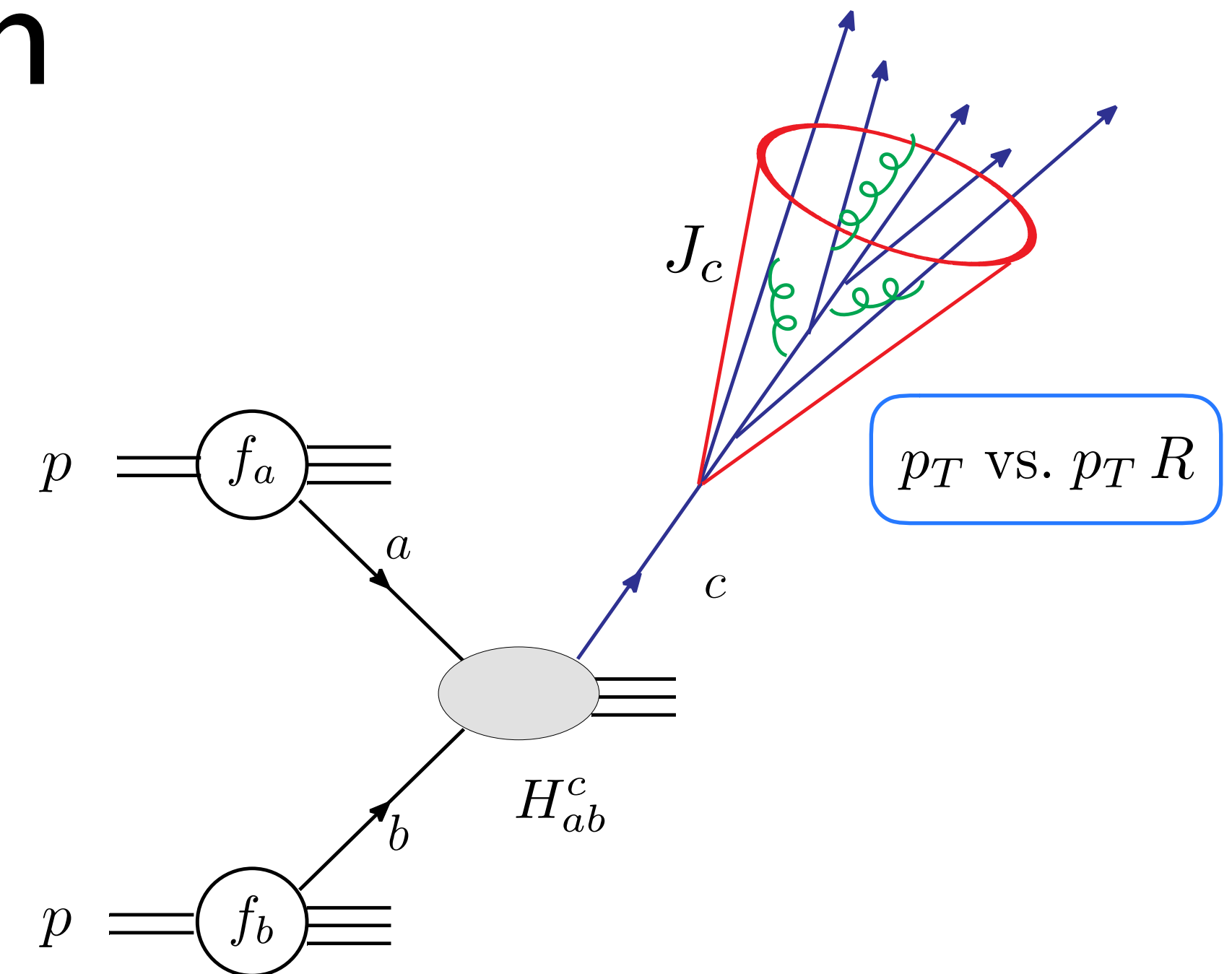
QCD factorization

- Inclusive jet production $pp \rightarrow \text{jet} + X$

$$\frac{d\sigma^{pp \rightarrow \text{jet} + X}}{dp_T d\eta} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes J_c$$

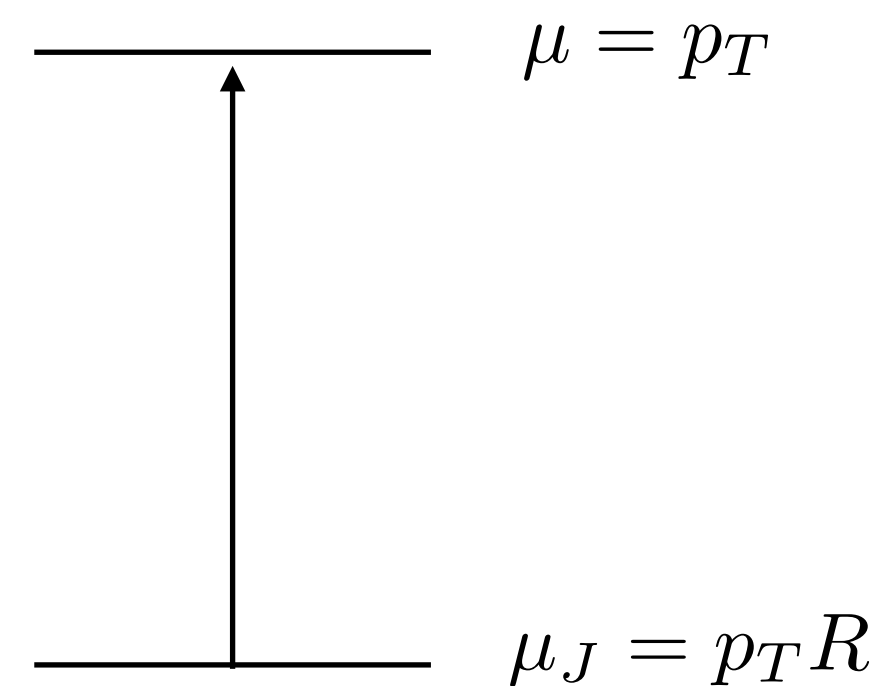
PDFs
Jet functions

Hard-scattering



- Hard and jet function calculable
- DGLAP evolution equation
- Resummation of $\alpha_s^n \ln^n R^2$

$$\mu \frac{d}{d\mu} J_i = \sum_j P_{ji} \otimes J_j$$

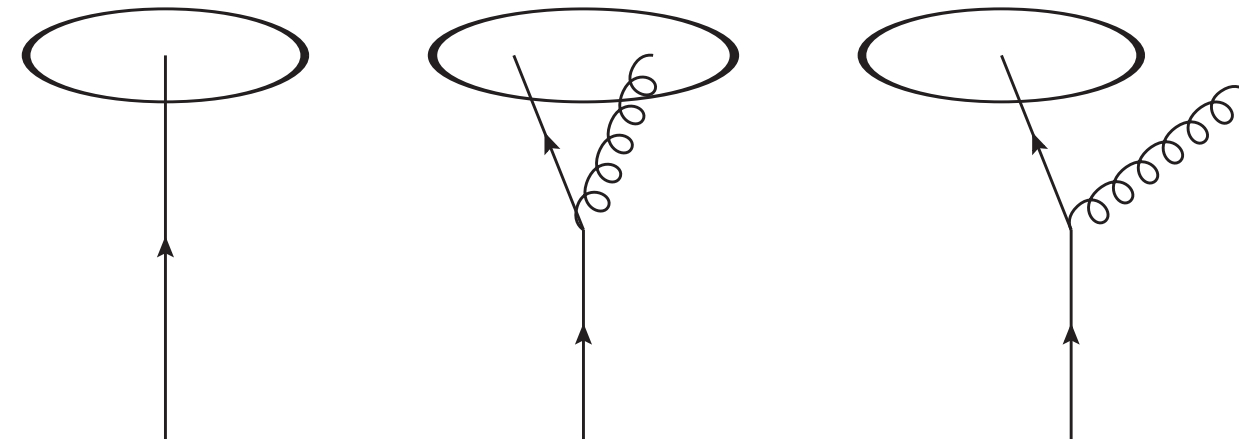


Ellis, Kunszt, Soper '90
 Dasgupta, Dreyer, Salam, Soyez '15
 Kaufmann, Mukherjee, Vogelsang '15
 Kang, FR, Vitev '16
 Dai, Kim, Leibovich '16

Jet functions in the vacuum

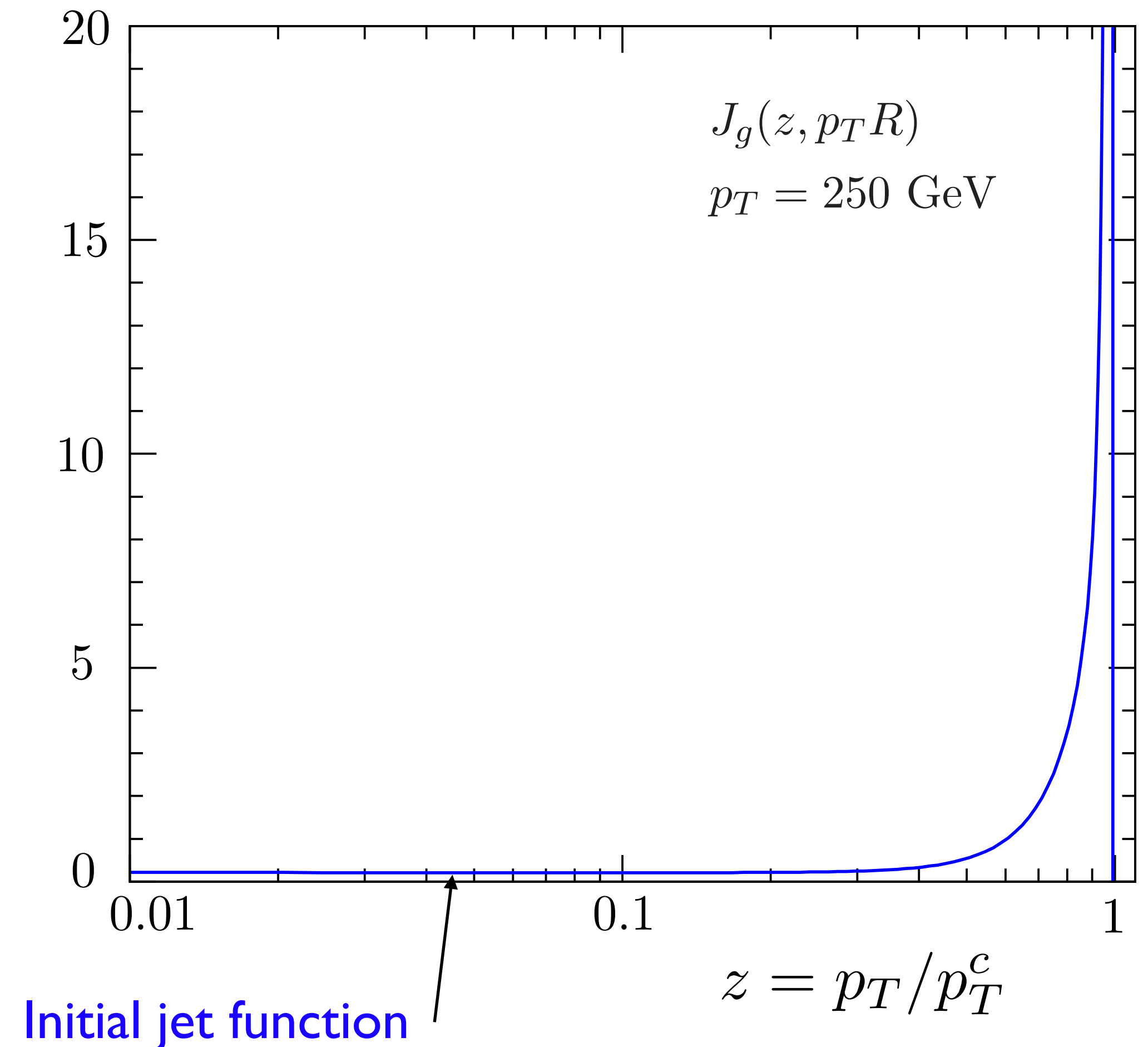
Kang, FR, Vitev '16

- NLO result



$$\begin{aligned}
 J_q(z, p_T R, \mu) &= \delta(1-z) \\
 &+ \frac{\alpha_s}{2\pi} \left(\frac{1}{\epsilon} + \ln \left(\frac{\mu^2}{p_T^2 R^2} \right) \right) [P_{qq}(z) + P_{gq}(z)] \\
 &- \frac{\alpha_s}{2\pi} \left\{ C_F \left[2(1+z^2) \left(\frac{\ln(1-z)}{1-z} \right)_+ + (1-z) \right] - \delta(1-z) d_J^{q, \text{alg}} \right. \\
 &\left. + P_{gq}(z) 2 \ln(1-z) + C_F z \right\}
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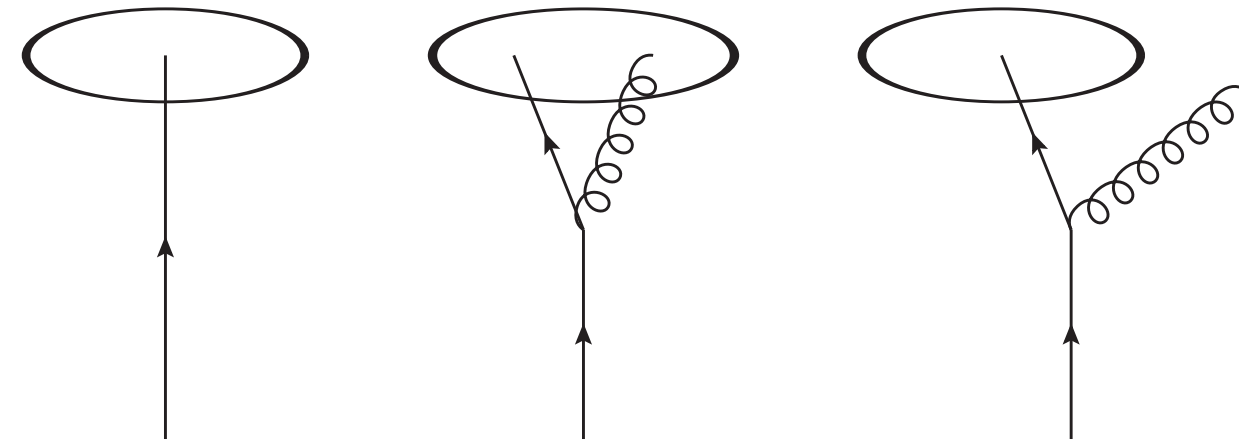
- Initial condition for the evolution (blue), independent of the jet radius
- DGLAP evolution $p_T R \rightarrow p_T$
- Number density similar to fragmentation functions



Jet functions in the vacuum

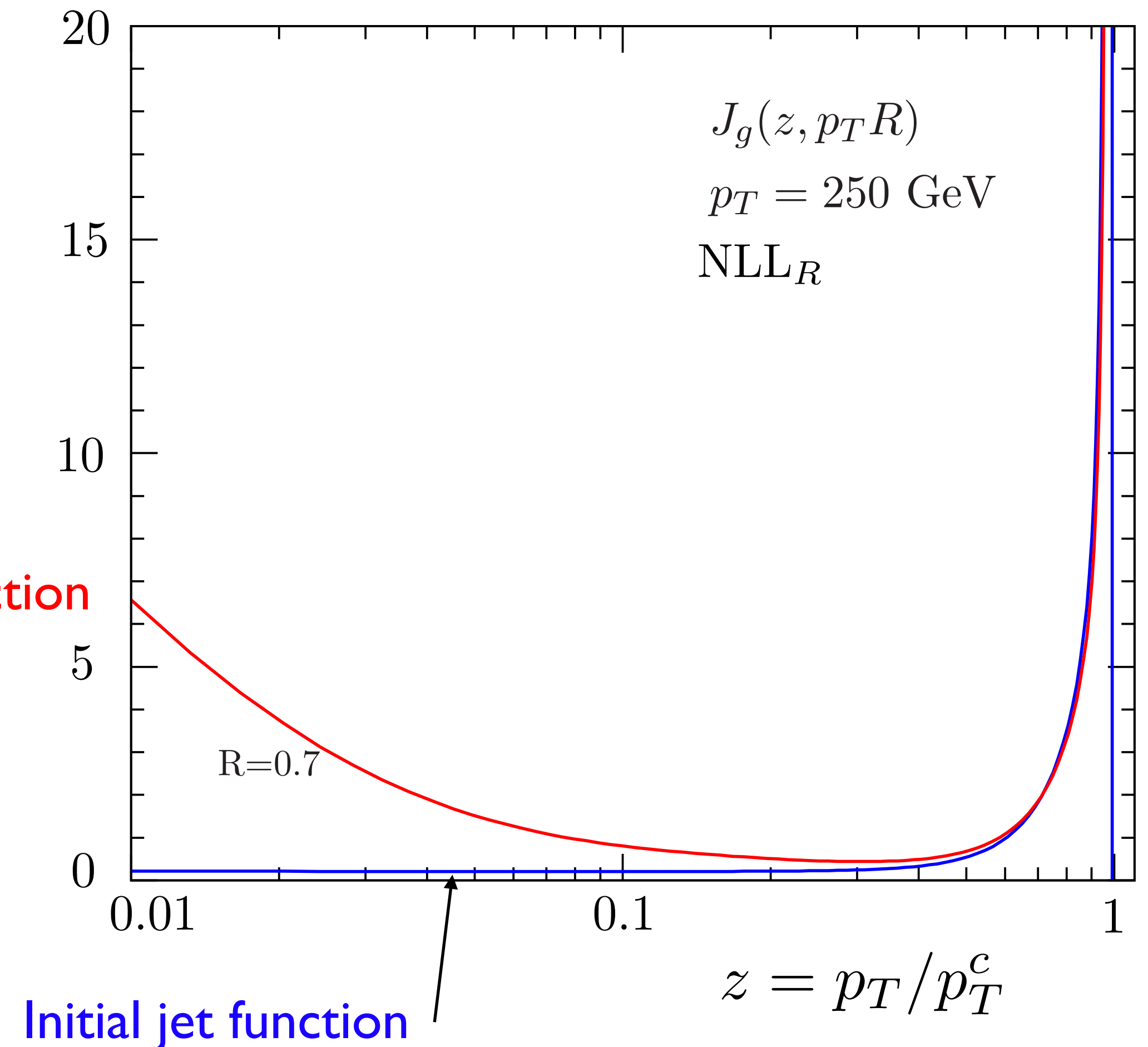
Kang, FR, Vitev '16

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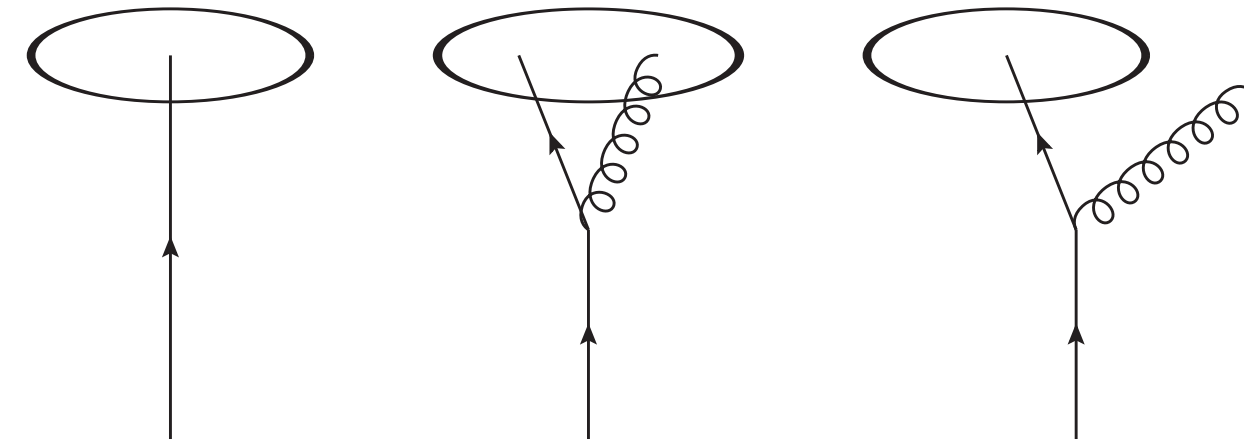
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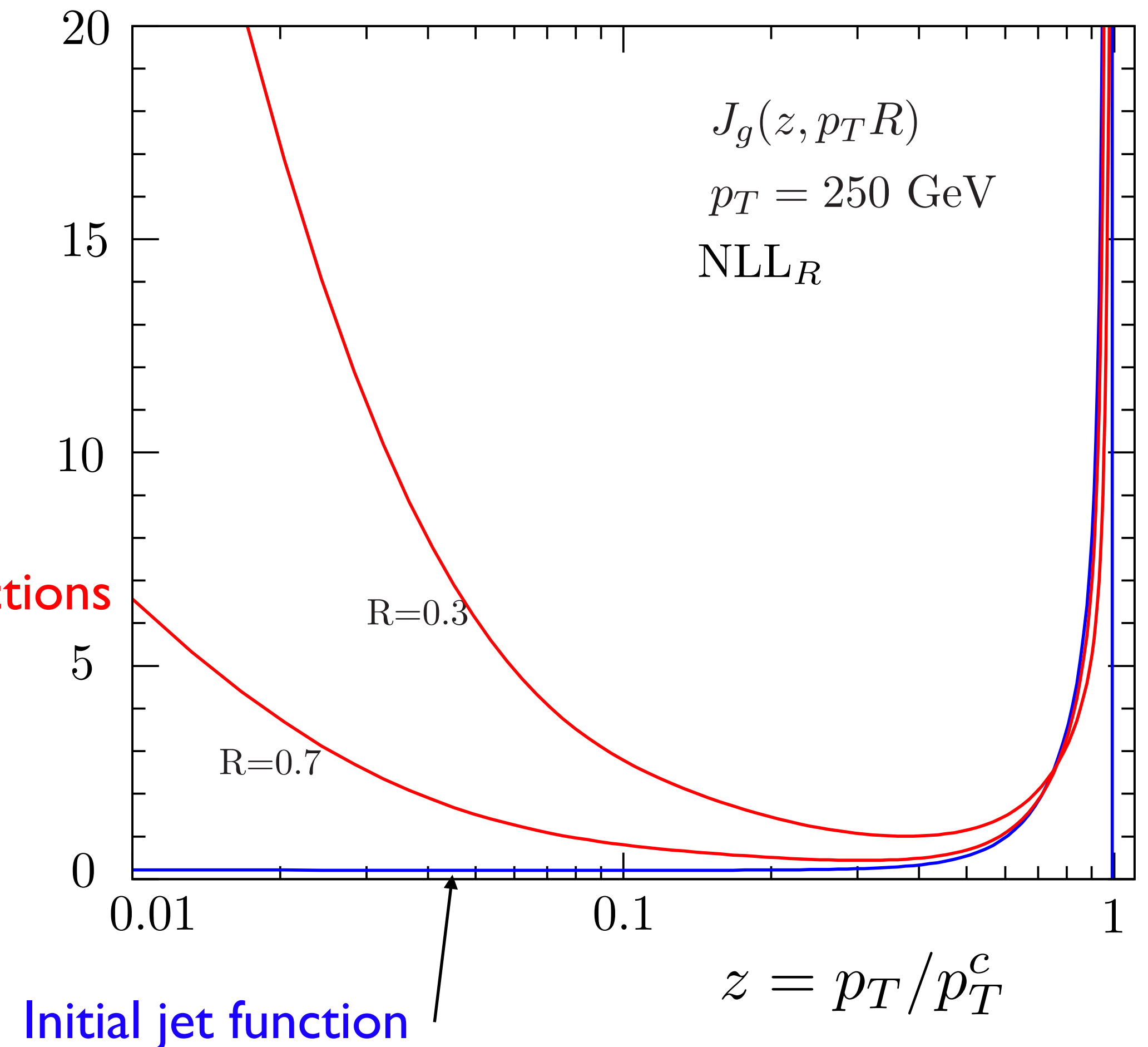
Kang, FR, Vitev '16

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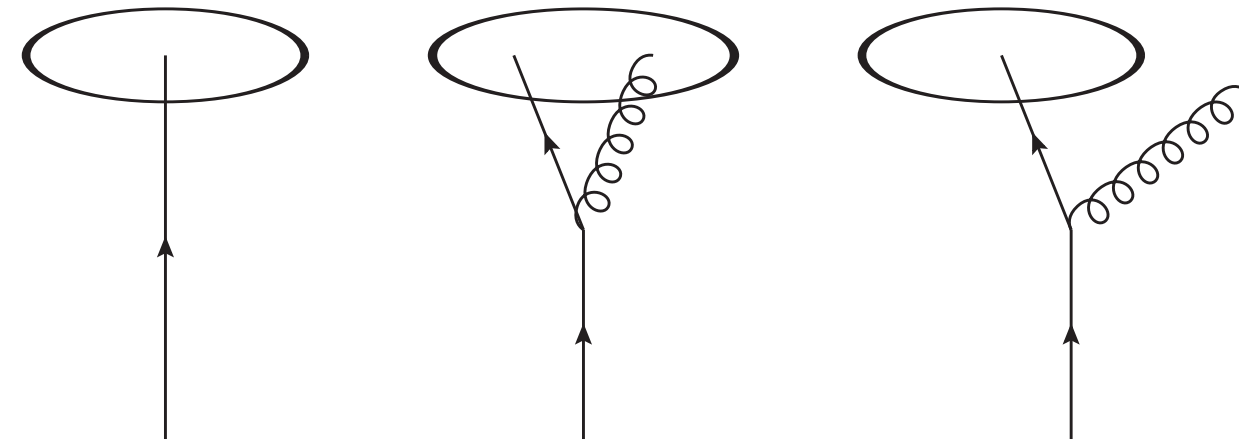
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Jet functions in the vacuum

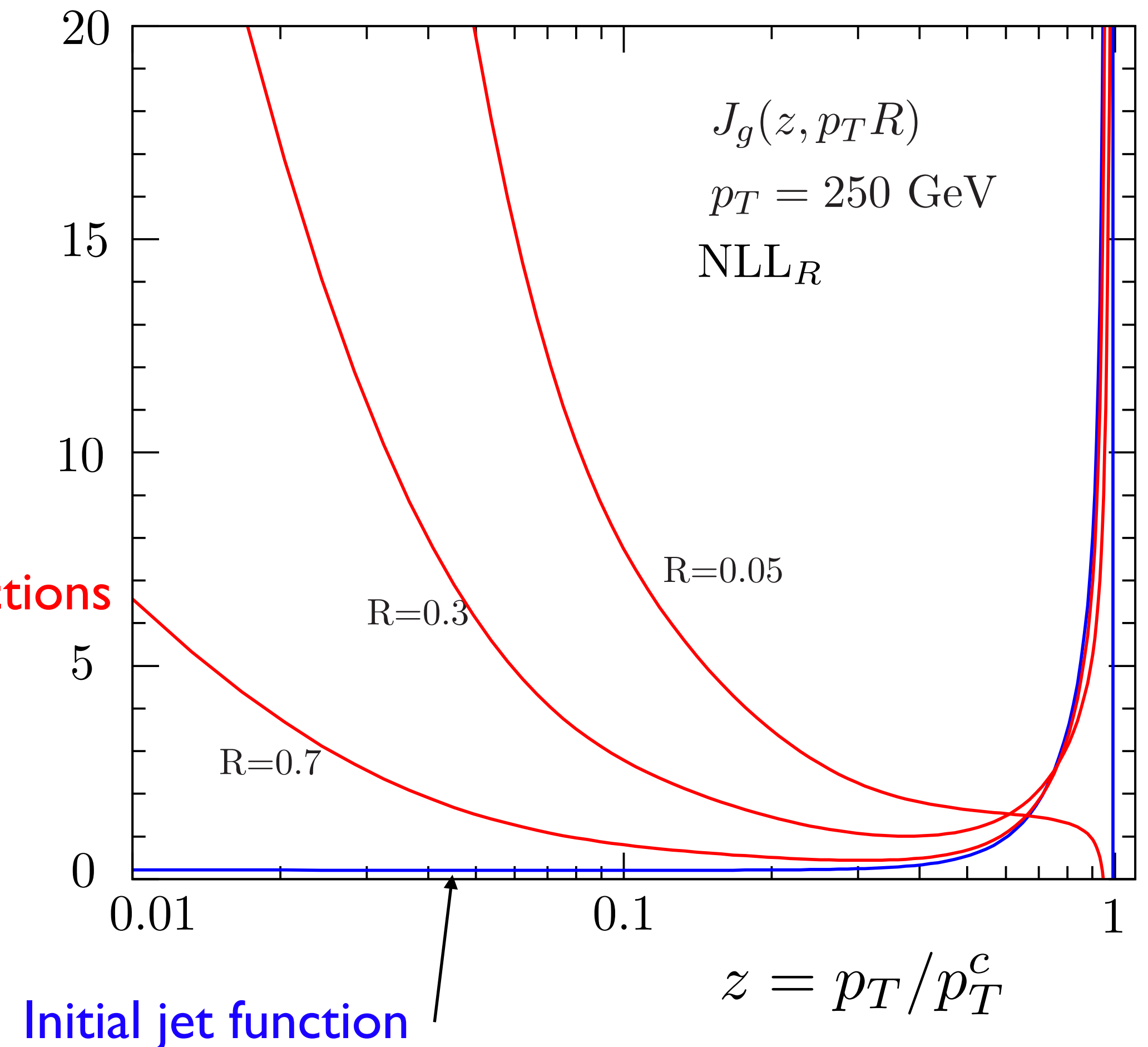
Kang, FR, Vitev '16

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QCD factorization

- Proton-proton

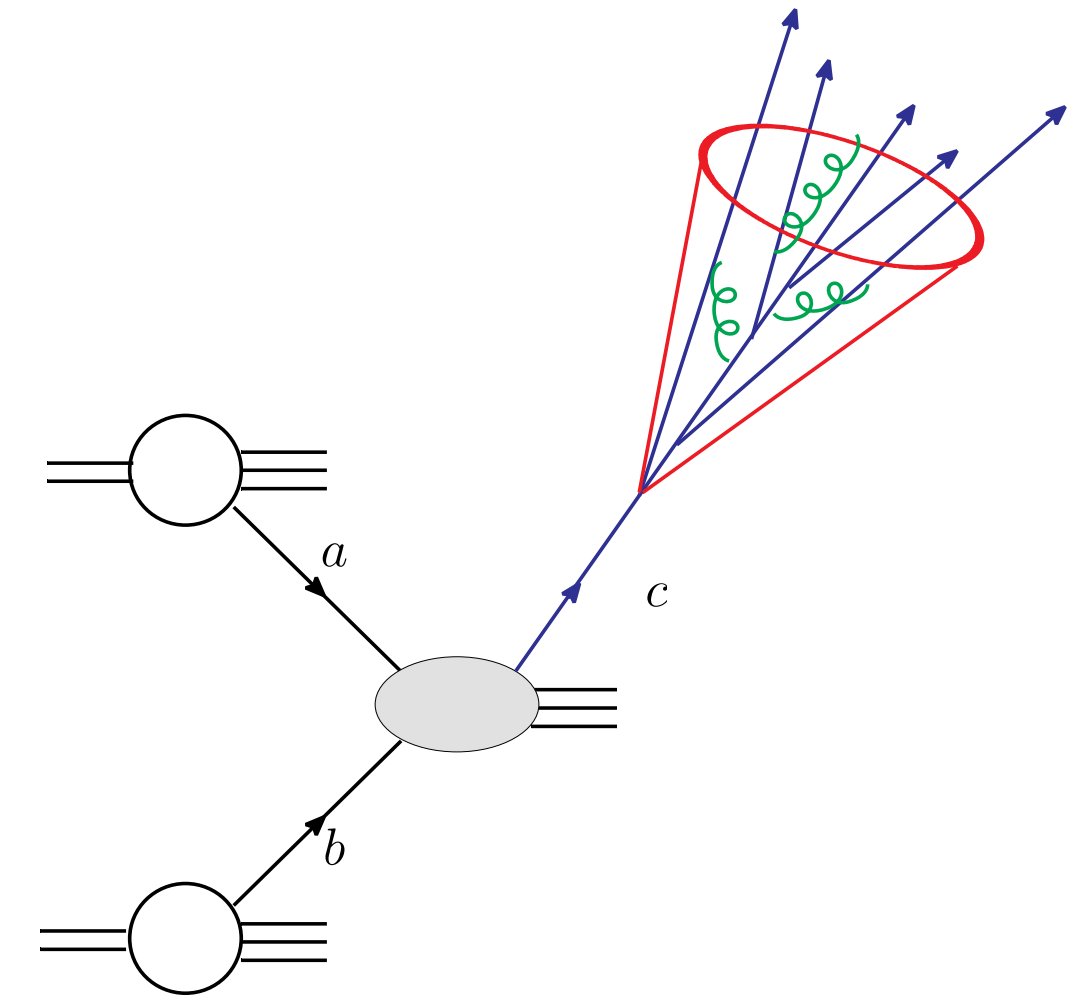
- Proof from first principles for the Drell-Yan process *Collins, Soper, Sterman '85, Bodwin '85*

- Partial proofs: $pp \rightarrow h + X$ *Nayak, Qiu, Sterman '05*

- And phenomenologically well established:

Global analyses of PDFs give a consistent picture!

ABMP, CJ, CT, JAM, MMHT, NNPDF ...



$$\frac{d\sigma^{pp \rightarrow \text{jet} + X}}{dp_T d\eta} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes J_c$$

QCD factorization

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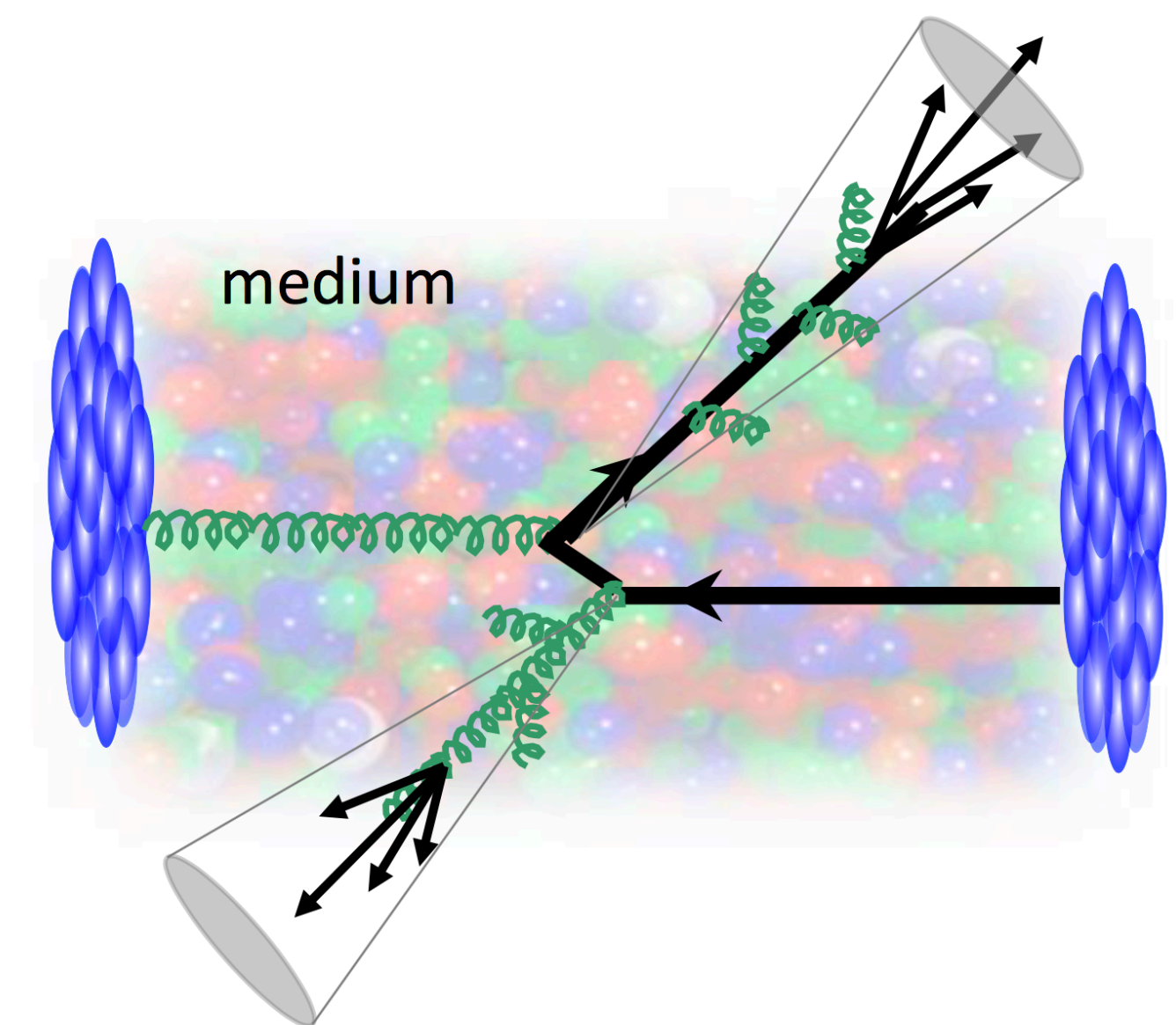
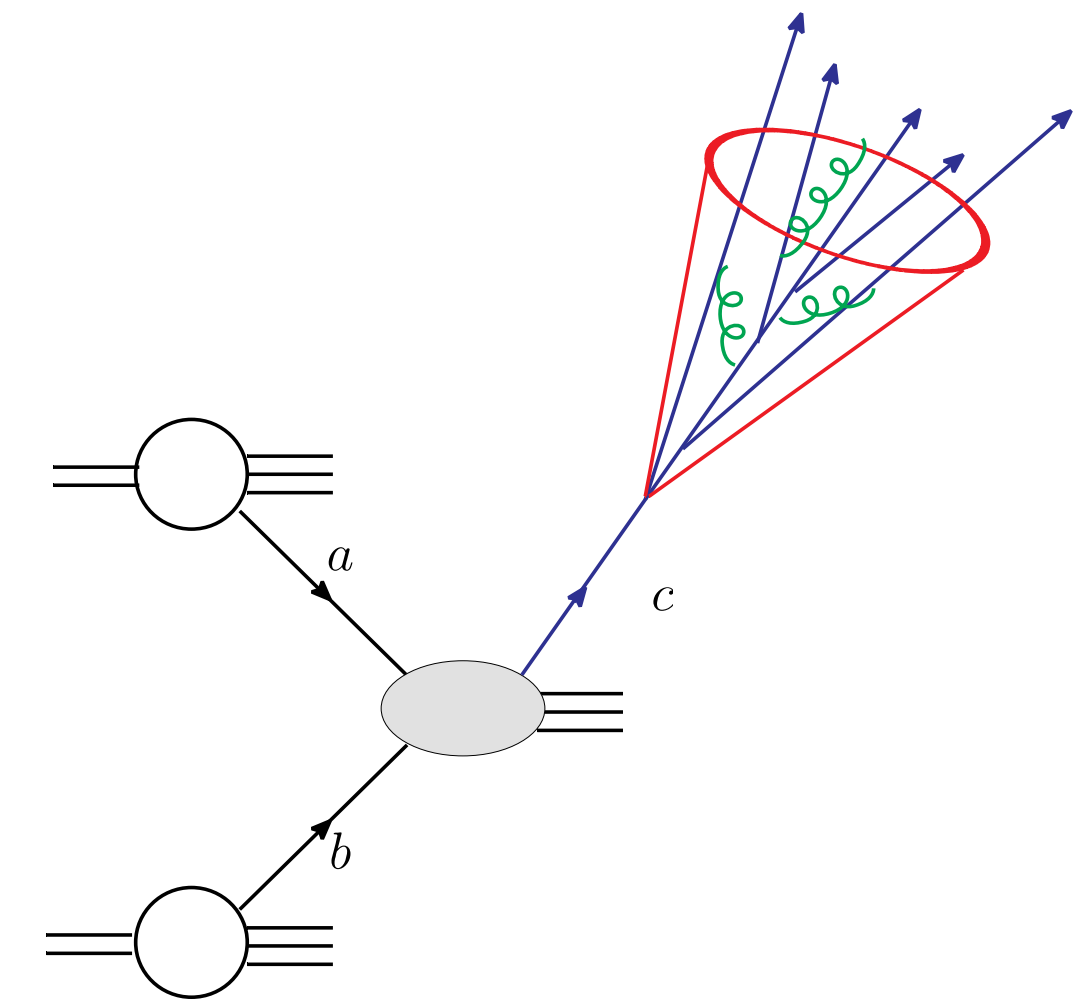
Global analyses of PDFs give a consistent picture!

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• Heavy-ion

- Try to establish a phenomenological approach

- Possibly broken. If so, how large is the effect?



The predictive power of QCD and universality

- Inclusive jet production $pp \rightarrow \text{jet} + X$
- Related to hadron production $pp \rightarrow h + X$
- The jet fragmentation function
- Inclusive subjets

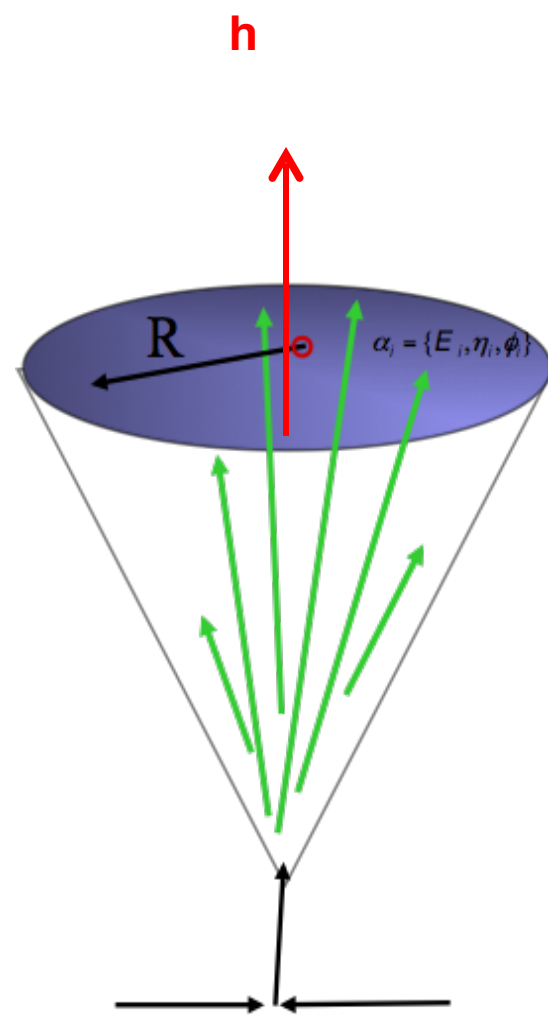
$$H_{ab}^c \otimes J_c$$

$$H_{ab}^c \otimes D_c^h$$

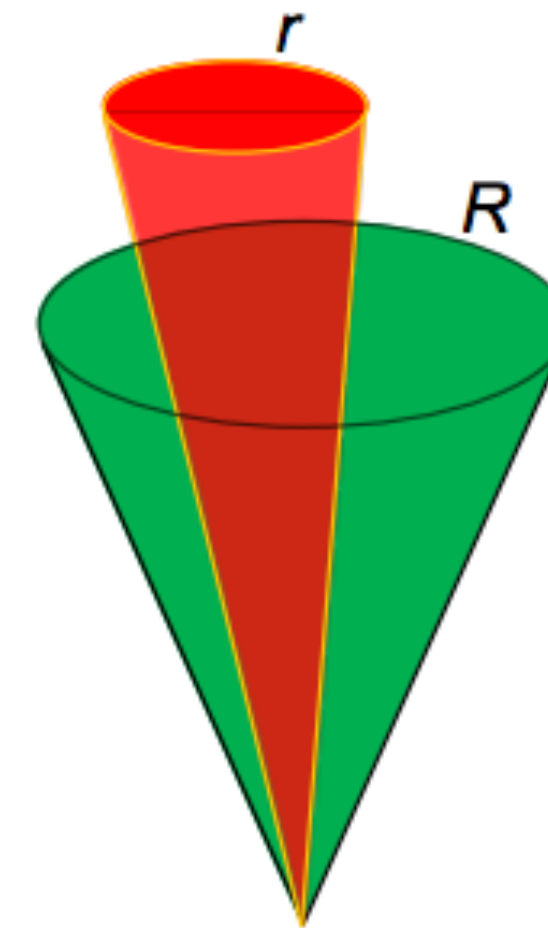
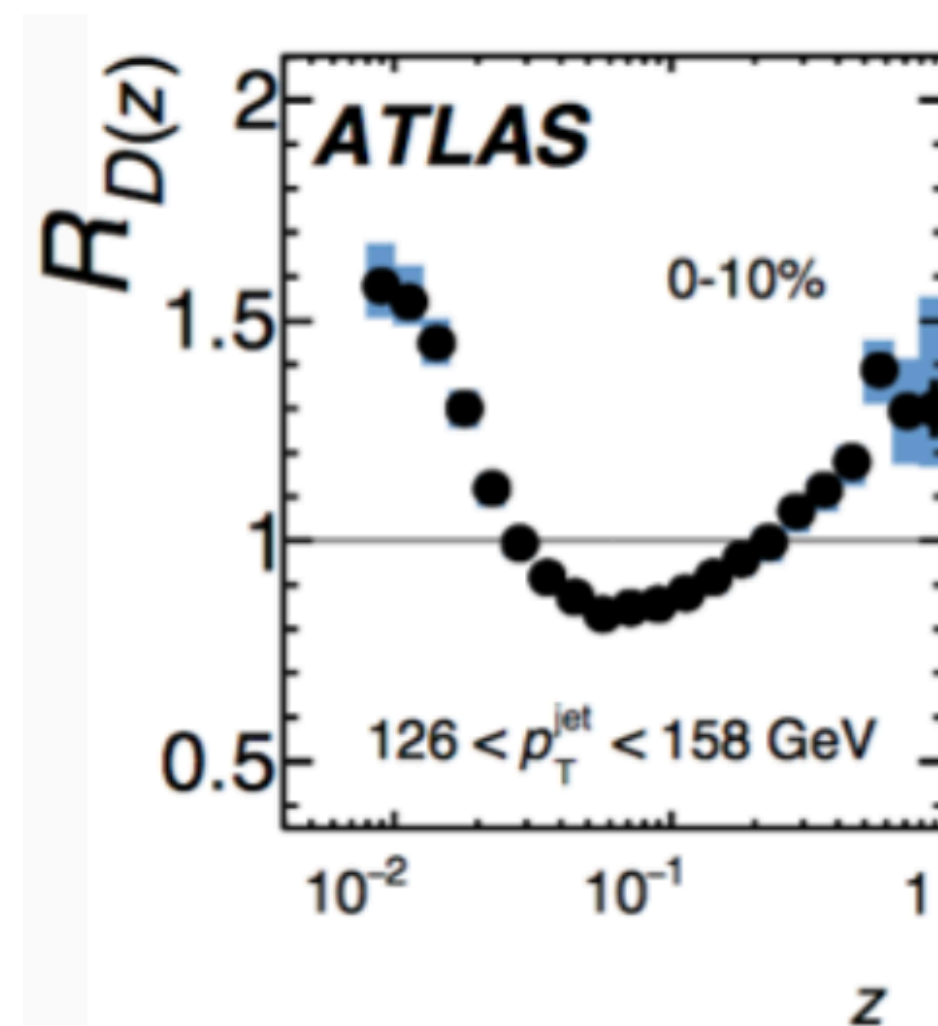
$$H_{ab}^c \otimes J_c \otimes D_c^h$$

$$H_{ab}^c \otimes J_c \otimes J_c$$

Reuse universal functions in other factorization theorems



ATLAS, PRC 98 (2018) 024908



The predictive power of QCD and universality

- Inclusive jet production $pp \rightarrow \text{jet} + X$
- Related to hadron production $pp \rightarrow h + X$
- The jet fragmentation function
- Inclusive subjets
- Quark/gluon fractions of any jet substructure observable

For example the soft drop groomed radius

$$\begin{aligned}
 \frac{d\sigma^{pp}}{dp_T d\eta d\theta_g} &= \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \\
 &\otimes \sum_{i=q,\bar{q},g} \sum_n \mathcal{H}_{c \rightarrow i}^n(z, p_T R, \mu) \otimes_{\Omega} S_{i,n}^{\notin \text{gr}}(z_{\text{cut}} p_T R, \mu; \beta) \\
 &\times \sum_m C_i^m(\theta_g p_T R, \mu) \otimes_{\Omega} S_{i,m}^{\in \text{gr}}(z_{\text{cut}} \theta_g^{1+\beta} p_T R, \mu; \beta)
 \end{aligned}$$

$$H_{ab}^c \otimes J_c$$

$$H_{ab}^c \otimes D_c^h$$

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$$H_{ab}^c \otimes J_c \otimes J_c$$

$$H_{ab}^c \otimes J_c \otimes \mathcal{G}_c(\tau)$$

Reuse universal functions in other factorization theorems

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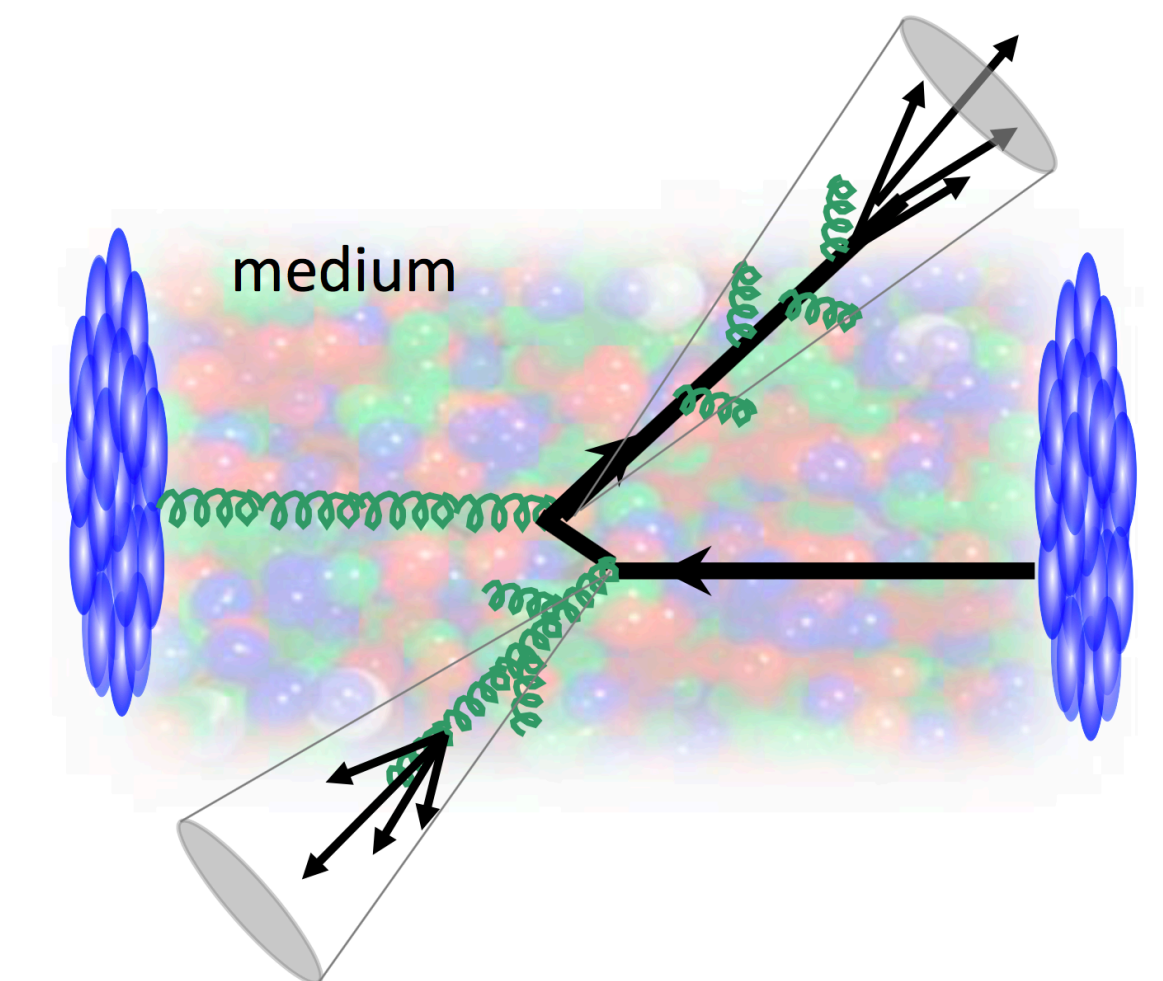
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$$H_{ab}^c \otimes J_c \otimes J_c$$

$$H_{ab}^c \otimes J_c \otimes \mathcal{G}_c(\tau)$$

Reuse universal functions in other factorization theorems

- Can we use similar approach in AA ?
- Minimal theory assumptions
- Factorization breaking effects in AA \longleftrightarrow universality ?
- Can we find medium jet functions for AA ?



Outline

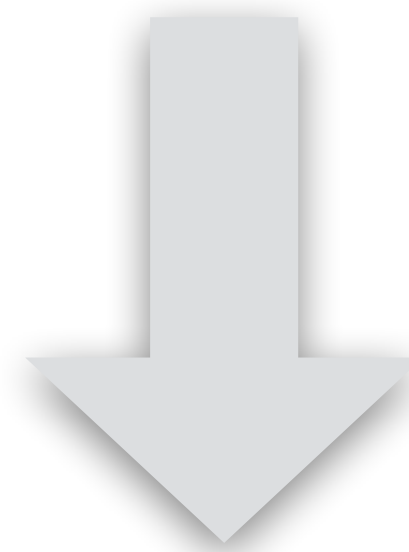
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Factorization for jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

• Proton-proton

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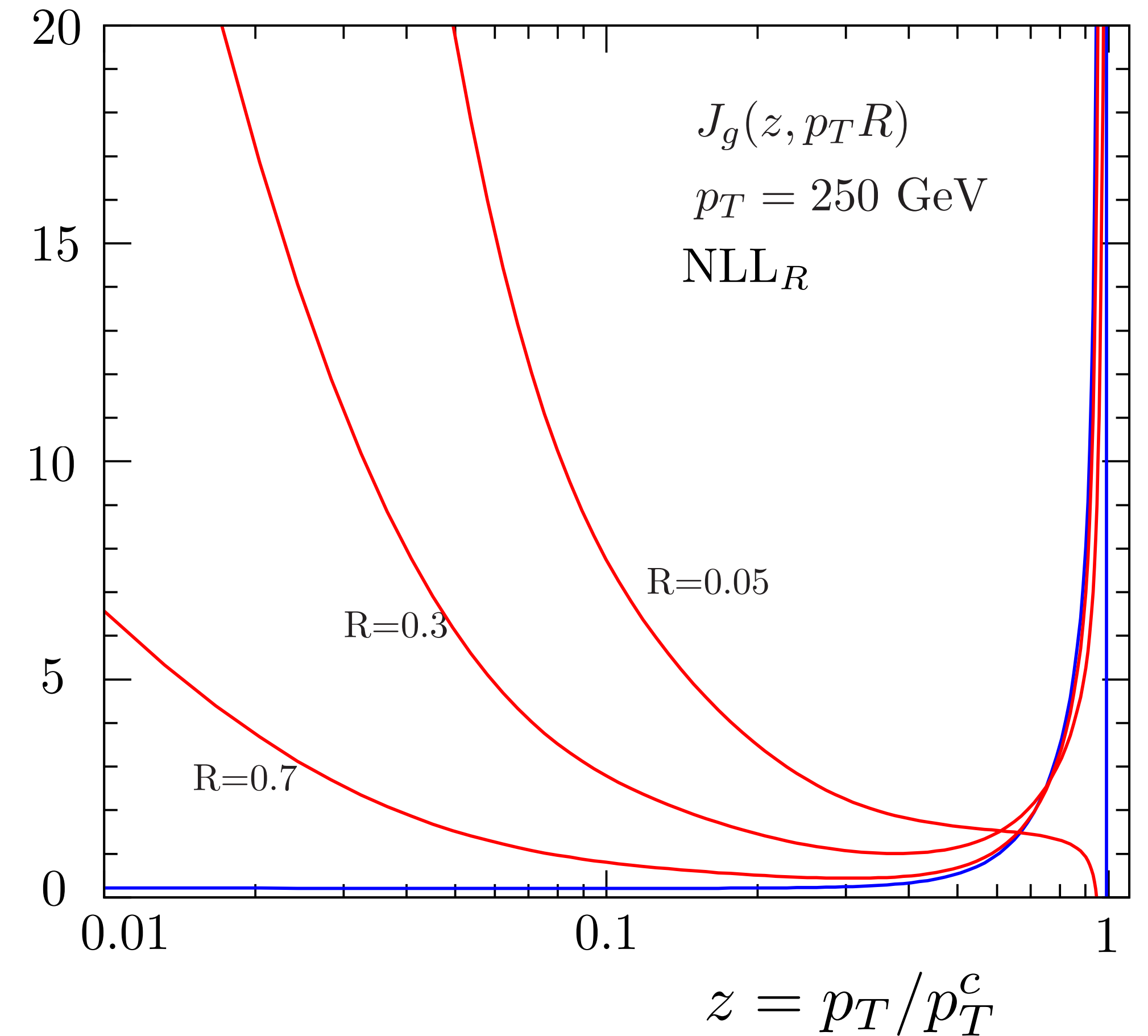


• Heavy-ion

$$\frac{d\sigma^{AA \rightarrow \text{jet}+X}}{dp_T d\eta} = \sum_{abc} f_{a/A} \otimes f_{b/A} \otimes H_{ab}^c \otimes J_c^{\text{med}}$$

Initial state e.g. nPDFs

Medium jet functions



see also: Kang, FR, Vitev '17
 He, Pang, Wang '18
 Sirimanna, Cao, Majumder '19

Factorization for jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

- Introduce a modification at the initial scale $\mu = p_T R$

$$J_c^{\text{med}}(z, p_T R, \mu_J) = W_c(z) \otimes J_c(z, p_T R, \mu_J)$$

$$W_c(z) = \epsilon_c \delta(1-z) + N_c z^{\alpha_c} (1-z)^{\beta_c}$$

- Momentum sum rule

$$\int_0^1 dz z J_c(z, p_T^c R, \mu) = 1$$

- Monte Carlo sampling approach

NNPDF '17, JAM '16

nPDFs Eskola, Paakkinen, Paukkunen, Salgado '17, Kovarik et al. '16
de Florian, Sassot, Zurita, Stratmann '12 ...

nFFs Sassot, Stratmann, Zurita '10

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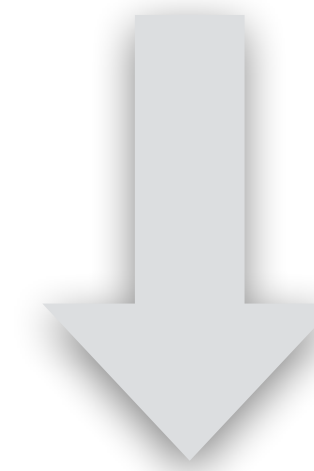
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- A modification of the evolution?

$$\mu^2 \frac{d}{d\mu^2} J_i = \sum_j P_{ji} \otimes J_j$$



$$\mu^2 \frac{d}{d\mu^2} J_i = \sum_j P_{ji} \otimes J_j + \frac{1}{\mu^2} \Gamma \otimes T$$

$$\mu^2 \frac{d}{d\mu^2} T = \gamma \otimes T$$

Kang, Ma, Qiu, Sterman '14

Factorization for jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

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- A modification of the evolution?
- Comparison to medium parton shower

vacuum shower

$\sim \mathcal{O}(10 \text{ GeV})$

medium modified shower

- LBT Li, Liu, Ma, Wang, Zhu '11
- MATTER Majumder '13, Kordell, Majumder '17

see also Hybrid, JEWEL, Martini, Q-Pythia, JETSCAPE ...

Factorization for jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

- Introduce a modification at the initial scale $\mu = p_T R$

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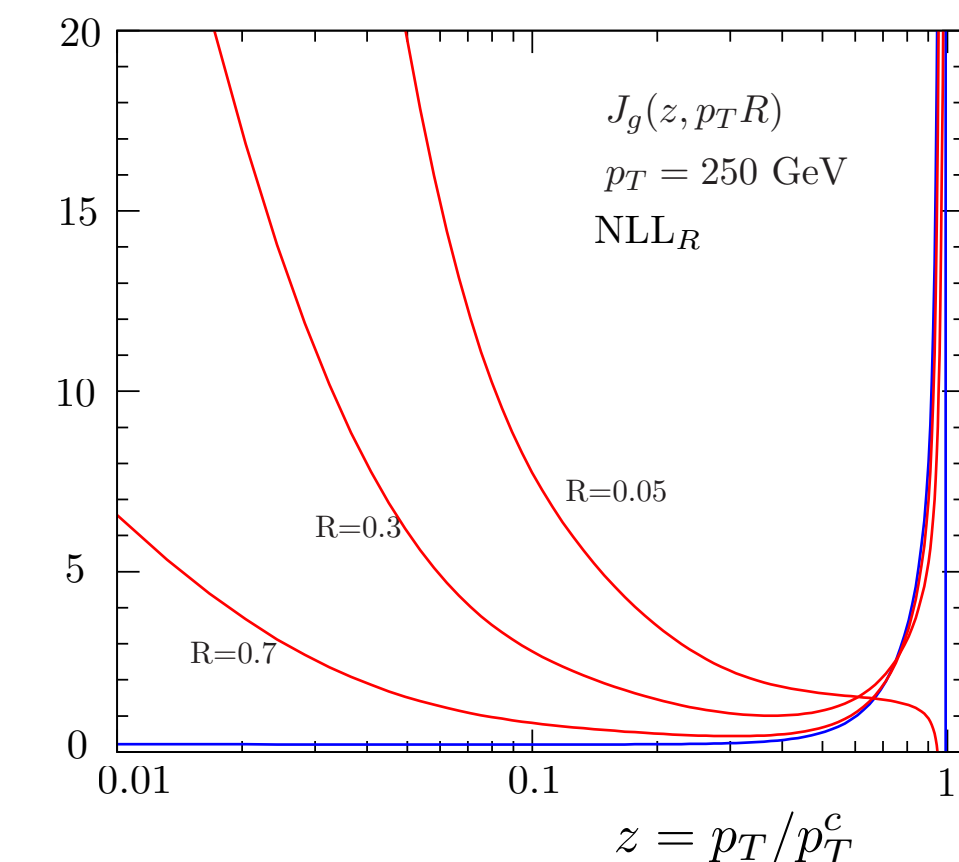
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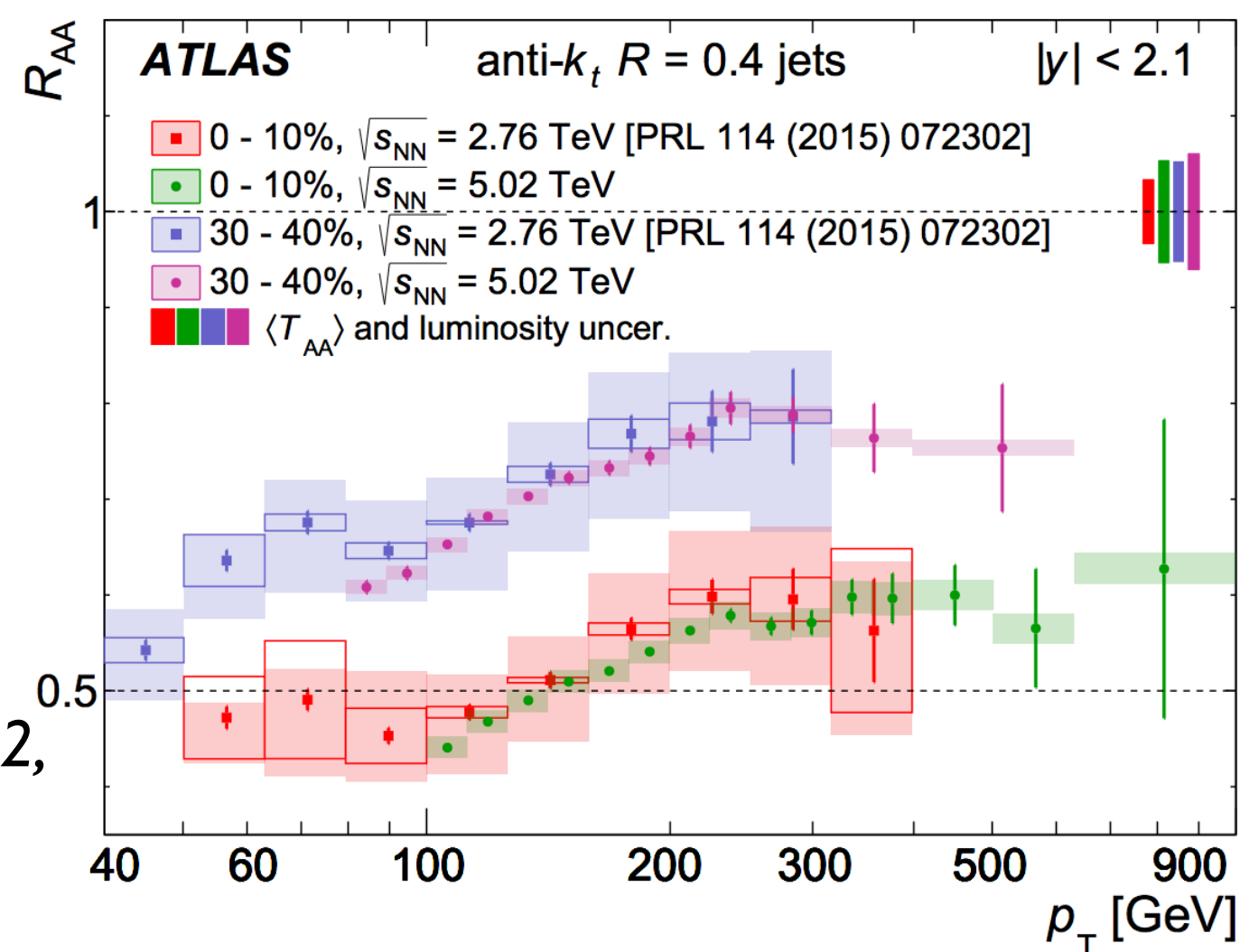
vacuum shower

$p_T R$

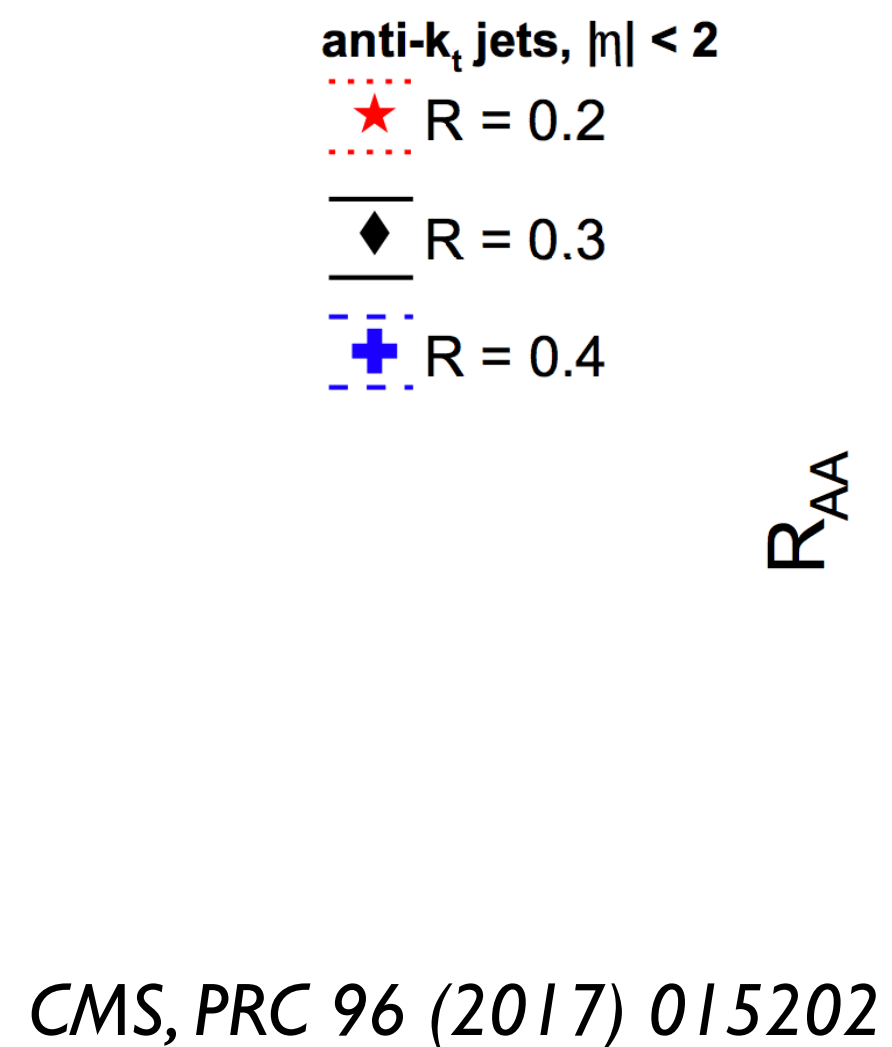
Fit to data



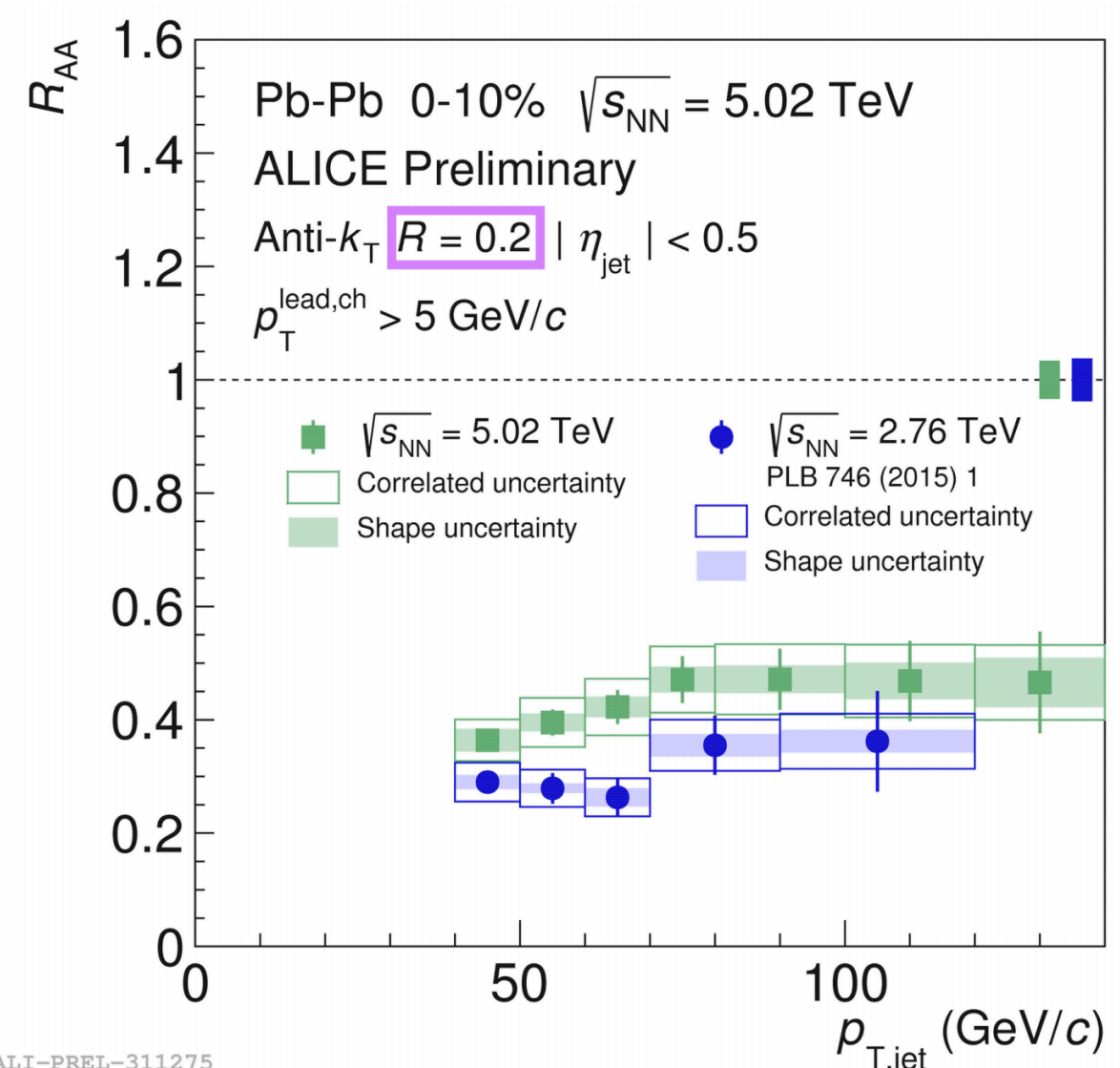
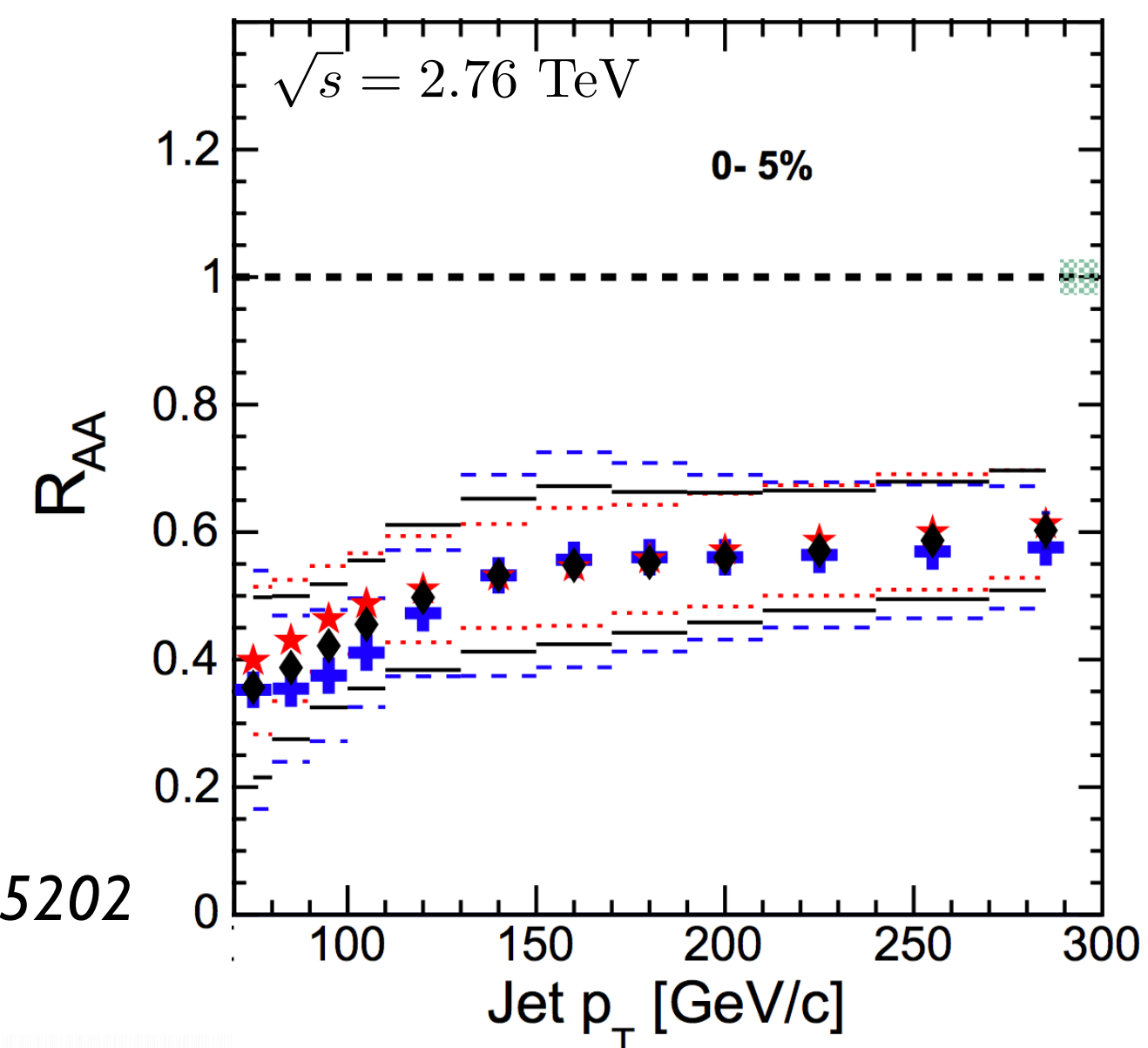
Inclusive jet data included in the analysis



ATLAS, PRL 114 (2015) 072302,
PLB 790 (2019) 108

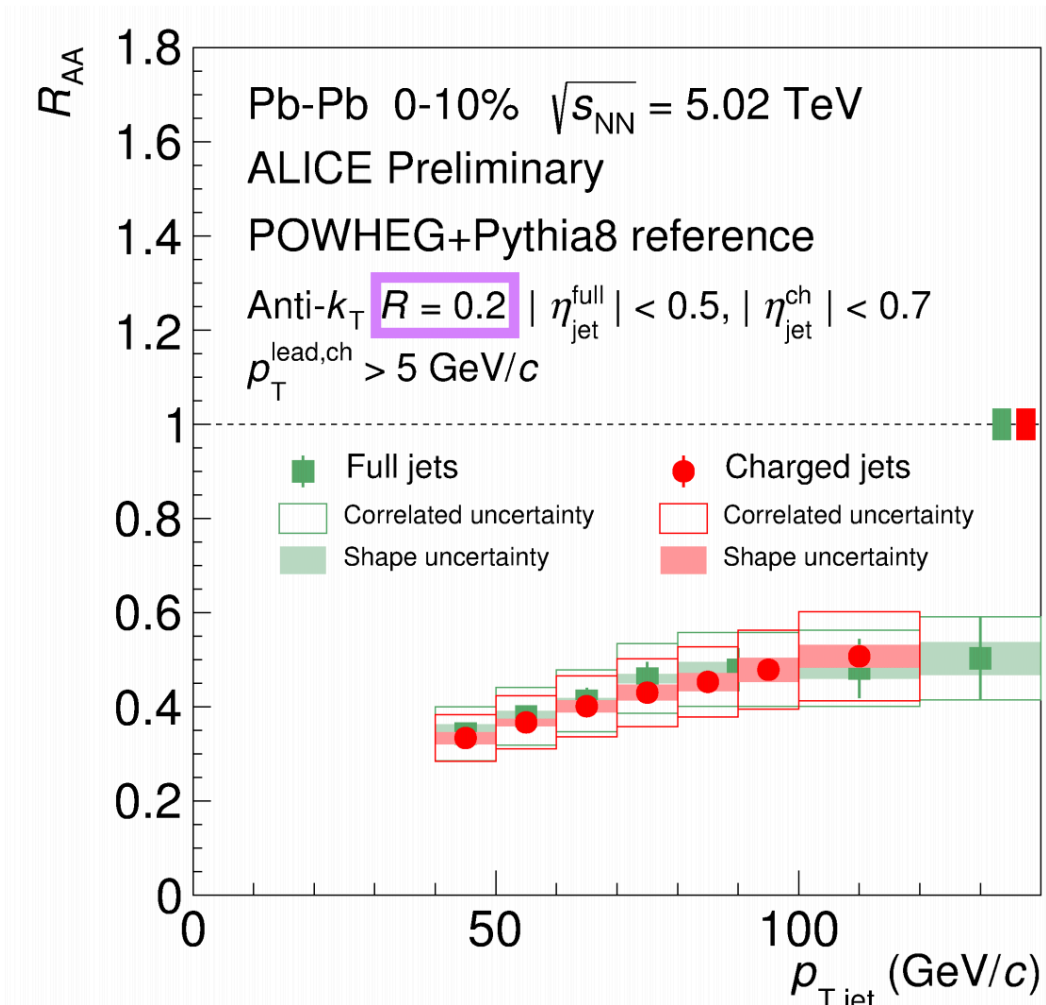


CMS, PRC 96 (2017) 015202



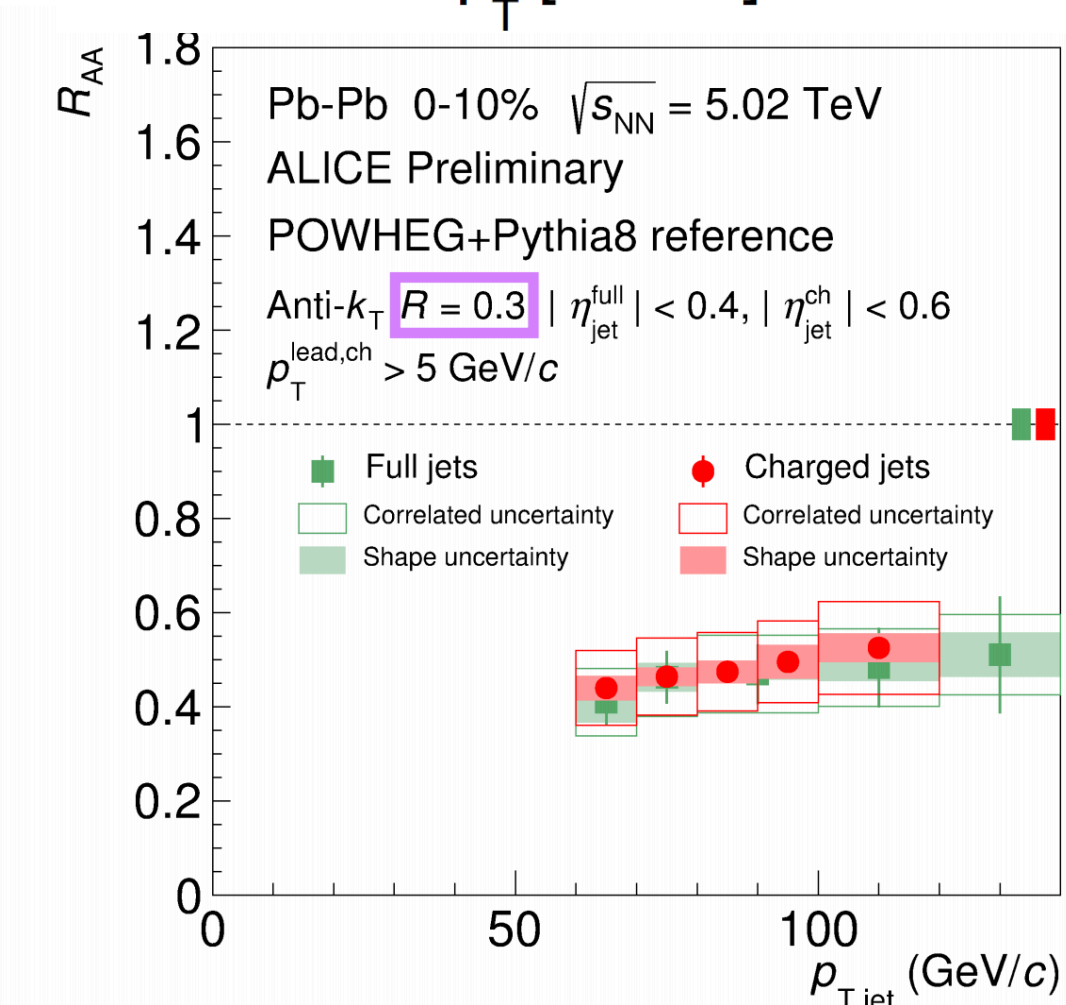
ALICE, PLB 746 (2015)

ALI-PREL-311275



ALI-PREL-159649

20



ALI-PREL-159653

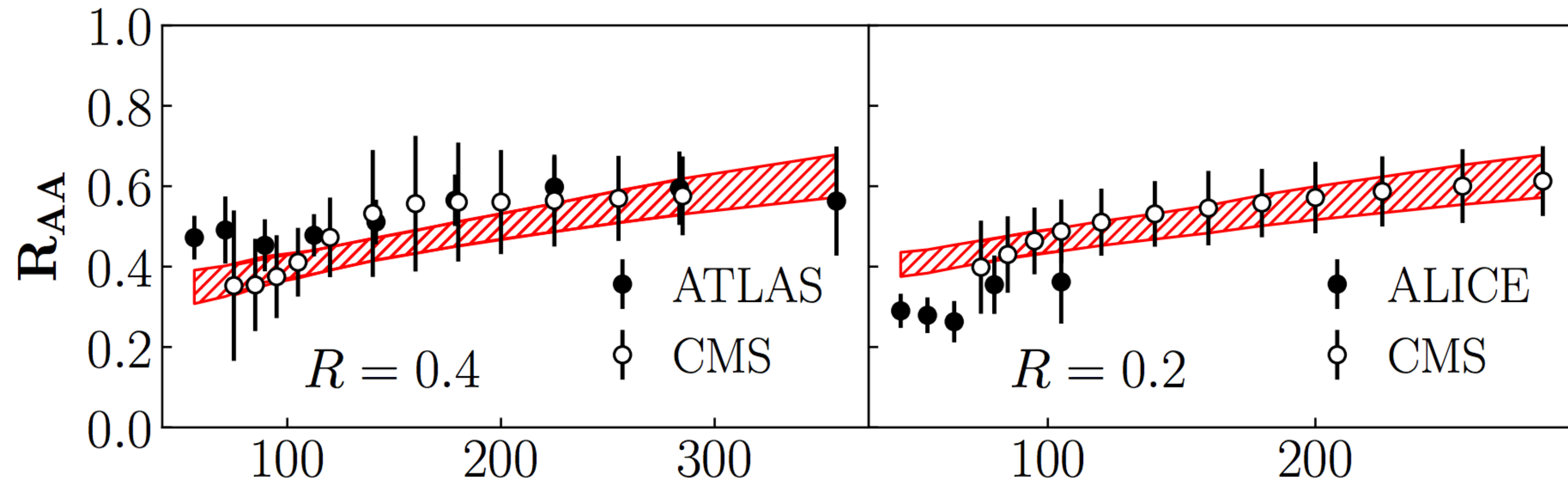
ALICE preliminary, J. Mulligan, HardProbes I 8

Inclusive jet production PbPb at the LHC

Qiu, FR, Sato, Zurita '19

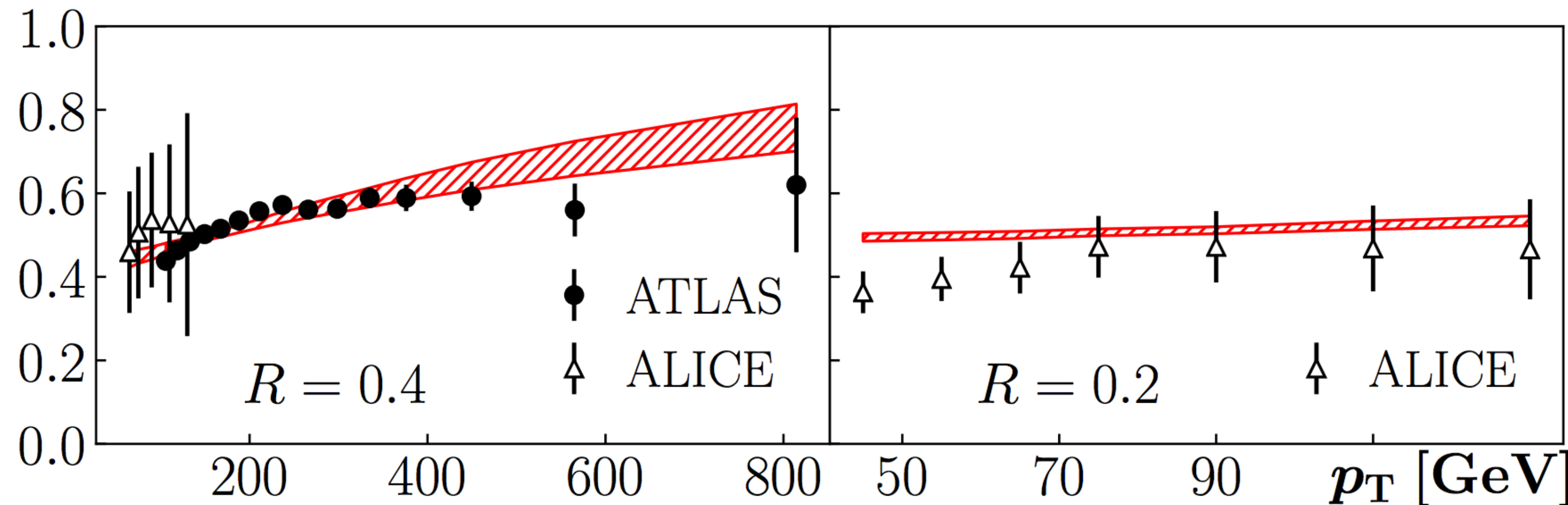
$$\sqrt{s_{NN}} = 2.76 \text{ TeV}$$

$$\chi^2/\text{d.o.f.} = 1.1$$



$$\sqrt{s_{NN}} = 5.02 \text{ TeV}$$

$$\chi^2/\text{d.o.f.} = 1.7$$



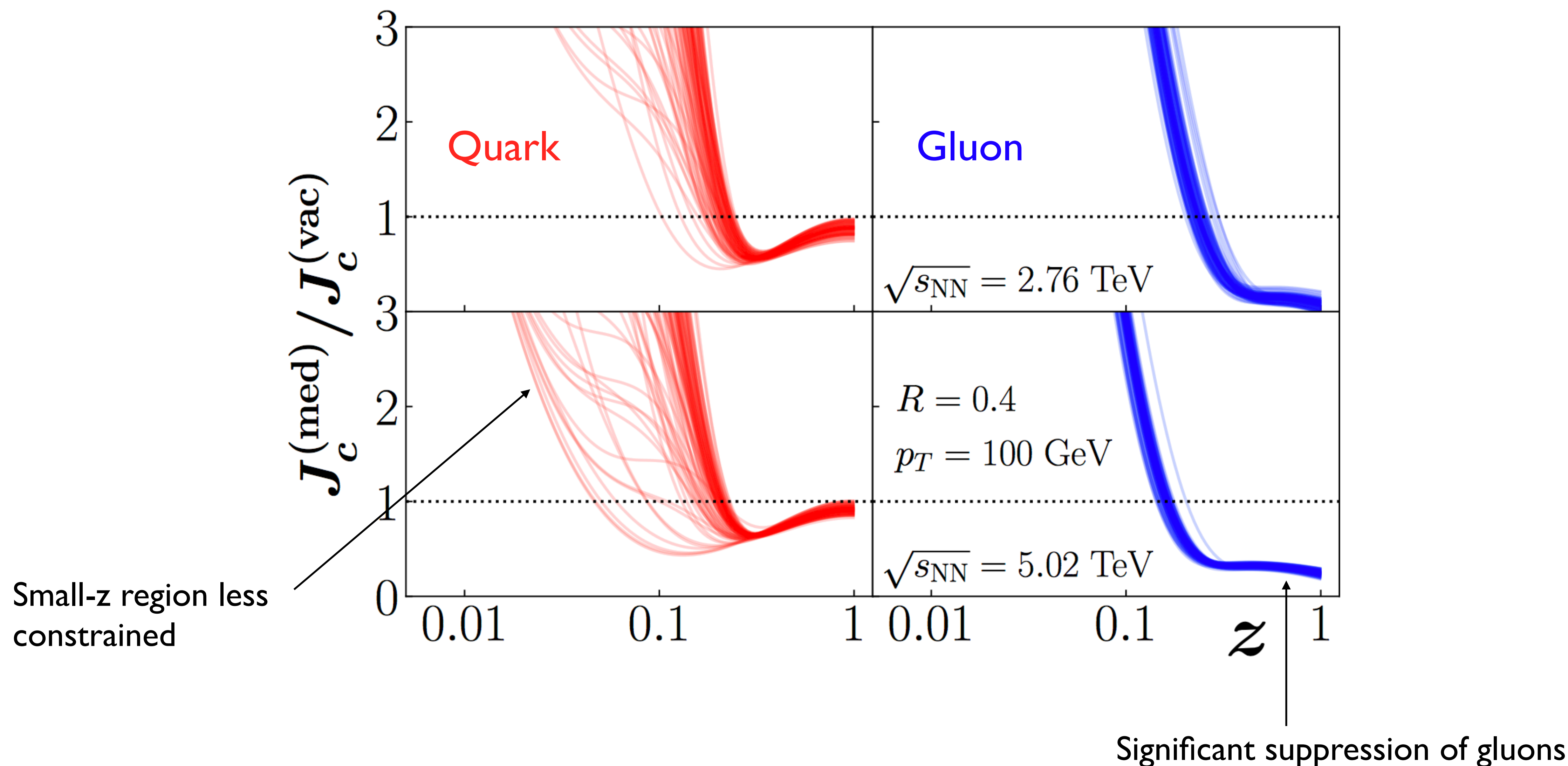
ALICE, PLB 746 (2015) 1
 ATLAS, PRL 114 (2015) 072302
 CMS, PRC 96 (2017) 015202

ALICE preliminary, J. Mulligan, HardProbes 18
 ATLAS, PLB 790 (2019) 108

No initial state effects or nPDFs

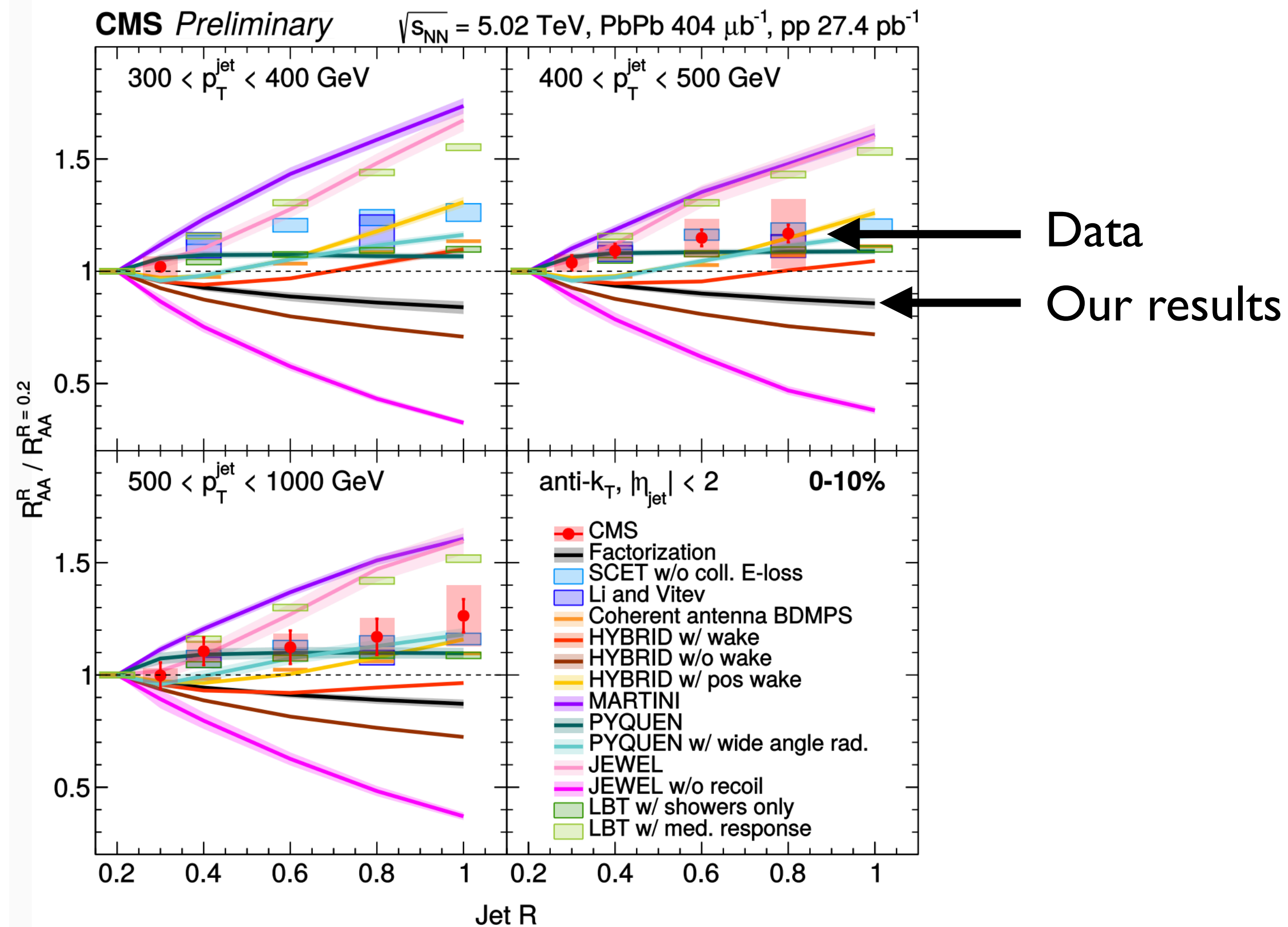
The extracted medium jet functions

Qiu, FR, Sato, Zurita '19

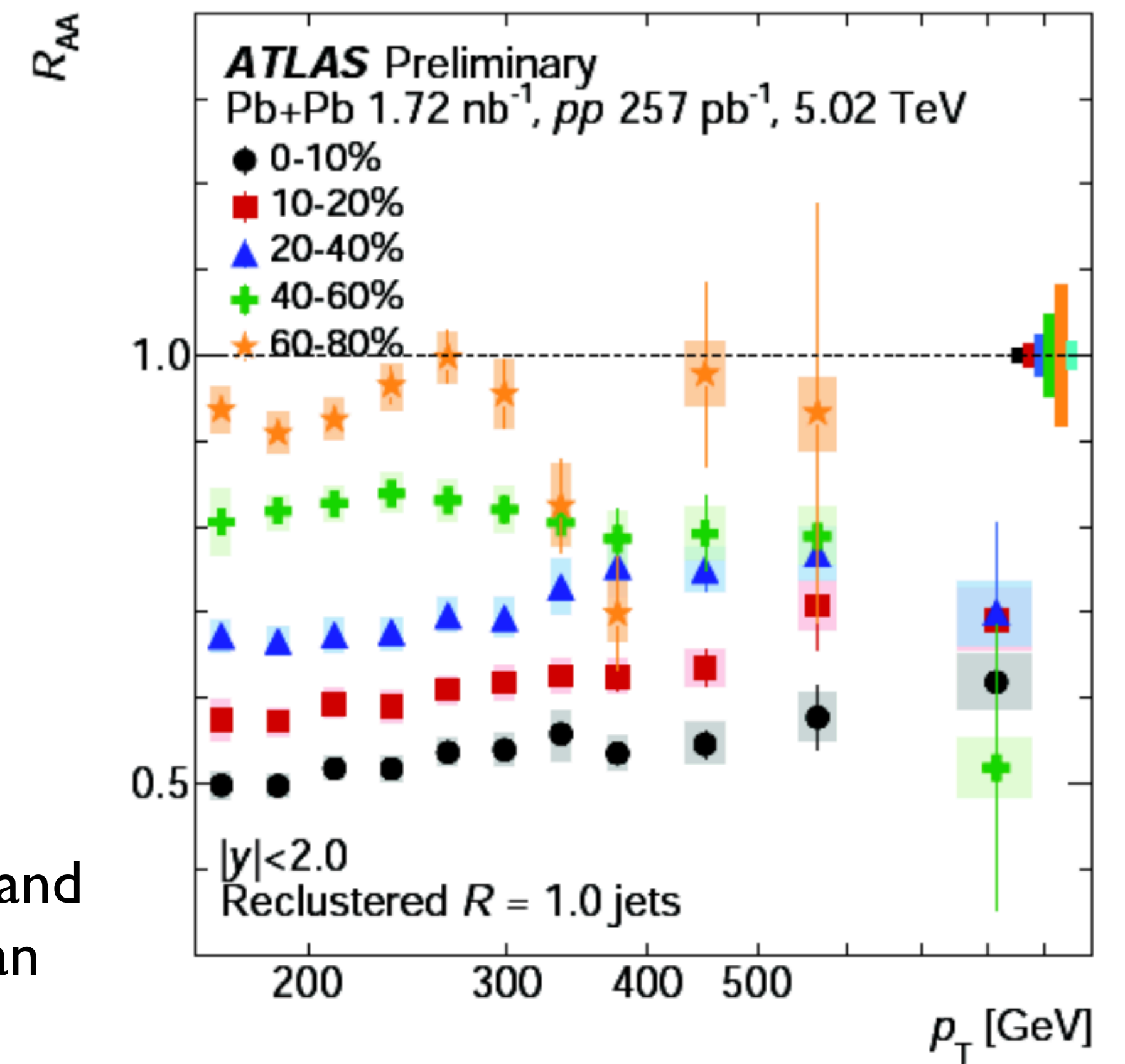


Comparison to QM19 results from ATLAS and CMS

See E. Chapon's talk



See M. Spousta's talk

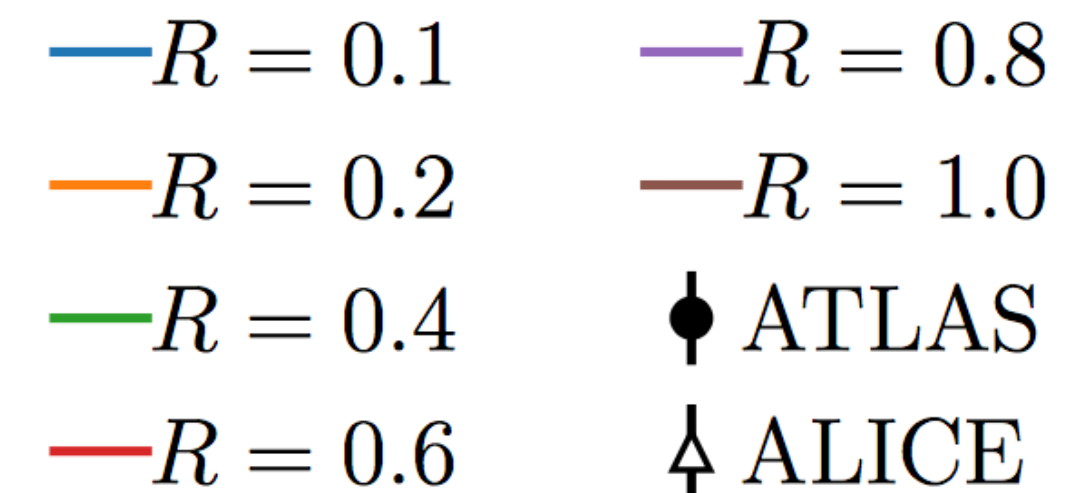
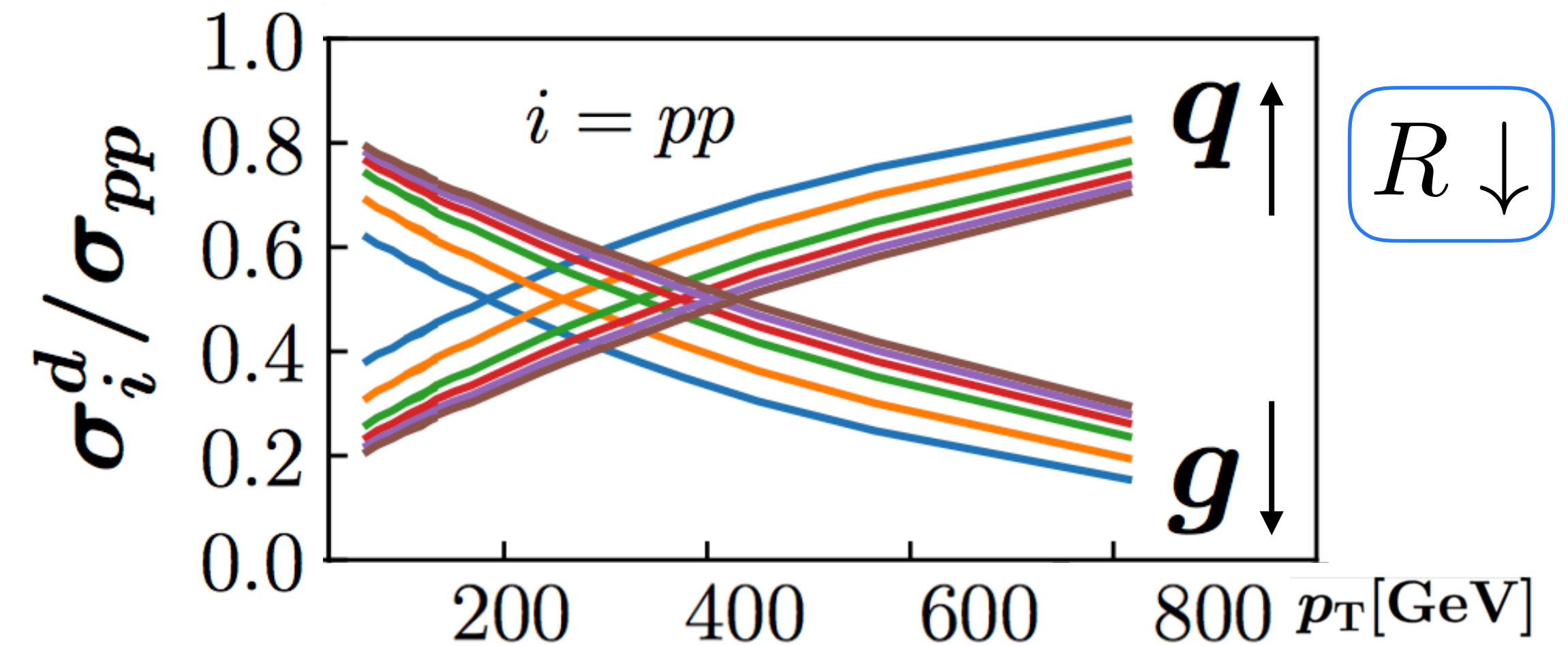


Similar trend and magnitude than $R=0.4$ jets

Quark/gluon fractions and the jet radius dependence

Qiu, FR, Sato, Zurita '19

- Definition of quark/gluon fractions at leading power
- Direct relation to the jet radius dependence

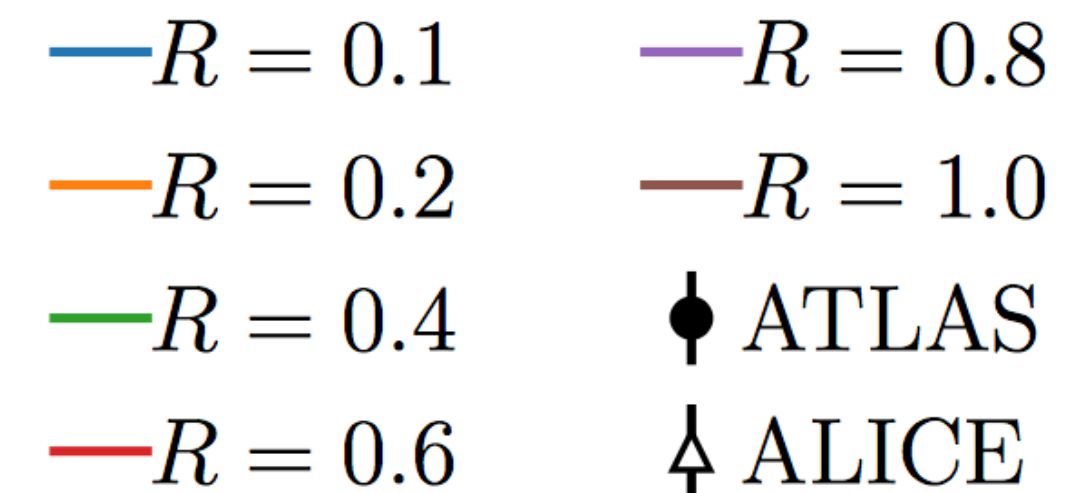
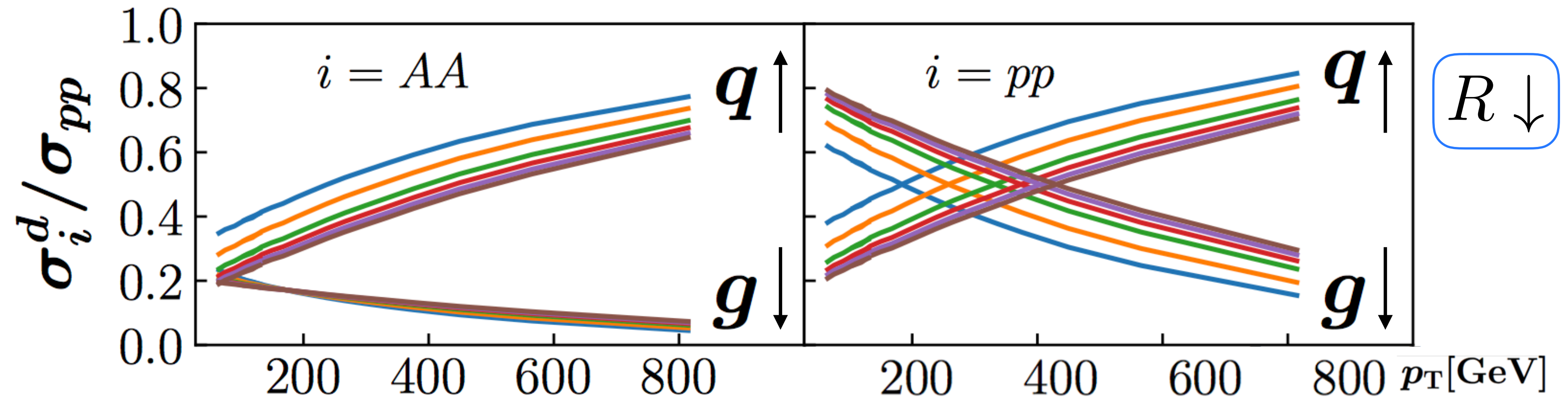


$$\sqrt{s} = 5.02 \text{ TeV}$$

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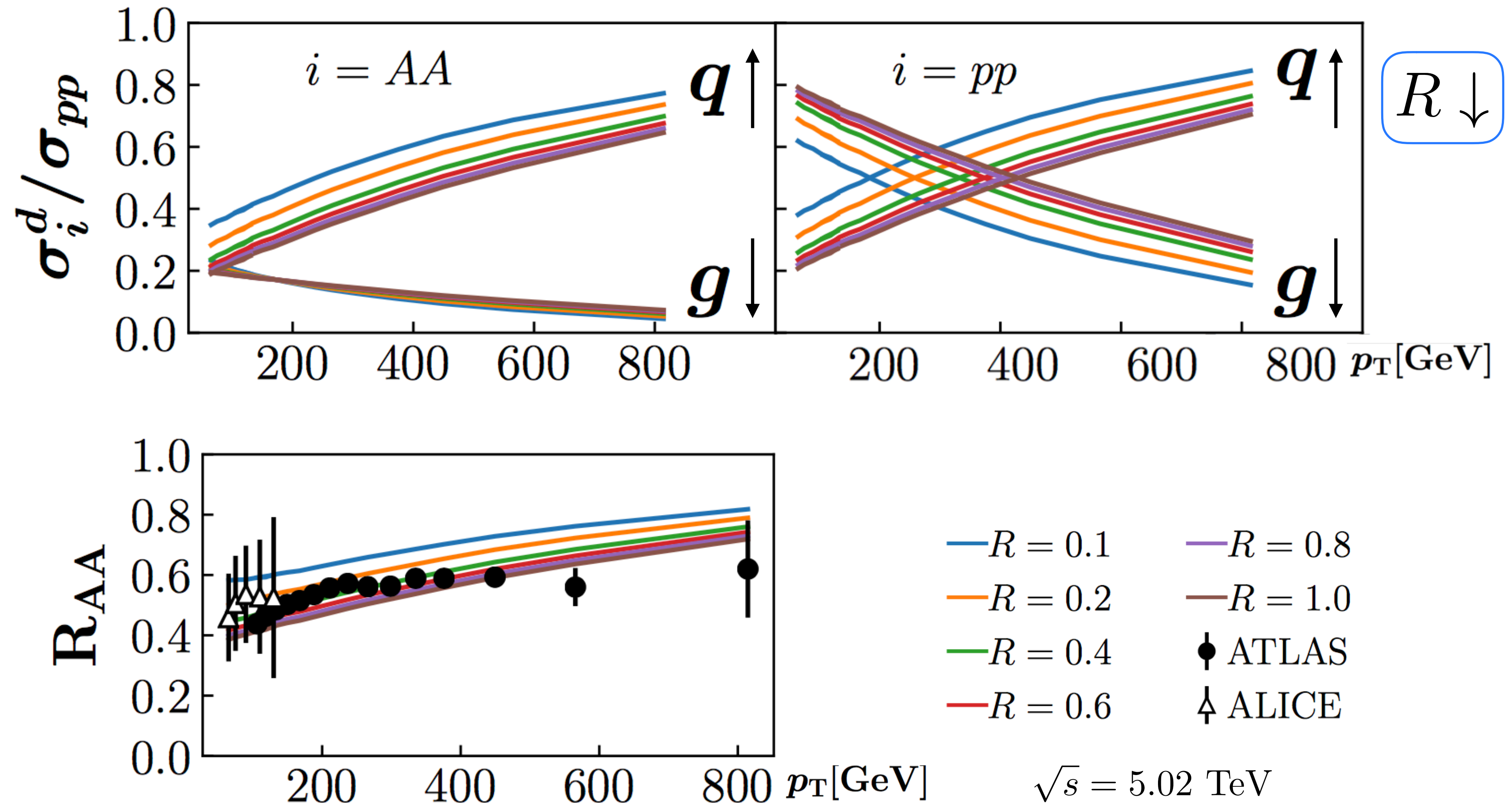


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Quark/gluon fractions and the jet radius dependence

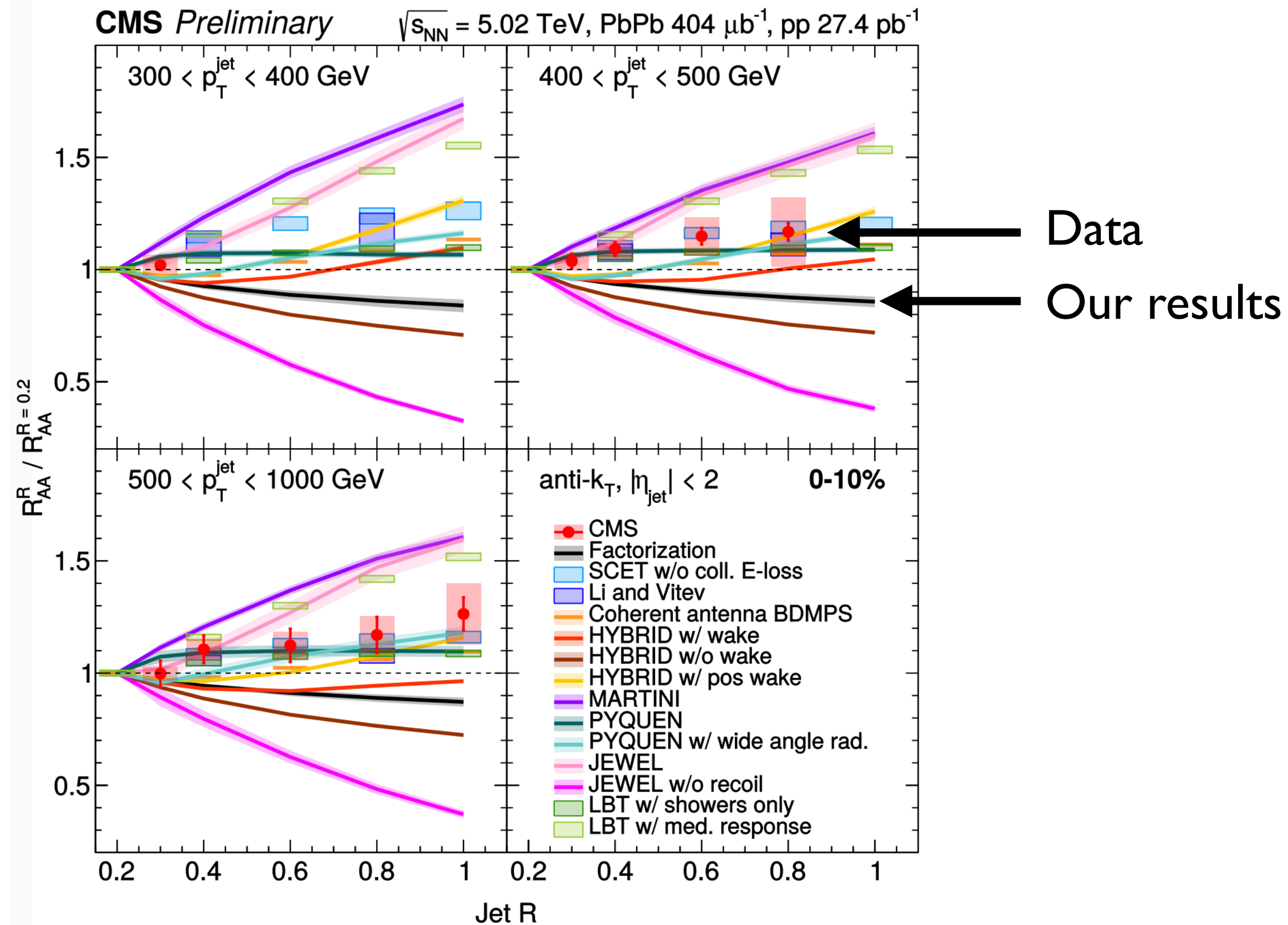
Qiu, FR, Sato, Zurita '19

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Possible explanations

- Refit?
- Different weight functions?
- Allow for a modified evolution?
- No factorization and universality?
- ...

Outline

- Introduction
- QCD factorization and universality
- Inclusive jets in heavy-ion collisions
- Conclusions

Conclusions

- A new framework to explore factorization and universality in heavy-ion collisions
- Minimal theory assumptions
- First global analysis of in-medium jet functions
- Test of universality
- Extracted quark/gluon fractions relevant for jet substructure
- Understand the medium modified parton shower
- Provide guidance for constructing microscopic models

