

Light charged Higgs boson with dominant decay to  $cb$   
quarks and  $b$ -tagging search at  $e^+e^-$  colliders  
[arXiv:1810.05403],[arXiv:1908.00826]

Muyuan Song

University of Southampton

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*Supervisors: Prof. Stefano Moretti  
Dr. Andrew Akeroyd*

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# Motivation of charged Higgs and MHDM (Multi-Higgs-Doublets-Model)

- Existence of Charged Higgs boson?

	SPIN 0	SPIN 1/2	SPIN 1
Charge 0	$H$	$\nu_e, \nu_\mu, \nu_\tau$	$\gamma, Z, g$
Charge $\pm 1$	$H^\pm ?$	$e^\pm, \mu^\pm, \tau^\pm, u, d, c, s, t, b$	$W^\pm$

Reason for MHDM:

- Supersymmetry, Dark Matter...
- Extra sources of CP-violation (Matter-antimatter asymmetry)...

# Light charged Higgs in 3HDM (Weinberg)

- Three active isospin fields  $\Phi_i (i = 1, 2, 3)$  are introduced, and each contain a vacuum expectation value with sum rule

$$\Phi_i = \begin{pmatrix} \phi_i^+ \\ (v_i + \phi_i^{0,real} + i\phi_i^{0,imag})/\sqrt{2} \end{pmatrix}, \sum_i v_i^2 = v_{sm}^2 = (246 \text{ GeV})^2$$

- A unitary  $3 \times 3$  matrix  $U$  is introduced in order to specify charged Higgs mass eigenstates from charged fields rotation:  
[C. Albright, J. Smith and S.-H.H. Tye 1980] [Y. Grossman 1994]

$$\begin{pmatrix} G^+ \\ H_2^+ \\ H_3^+ \end{pmatrix} = U \begin{pmatrix} \phi_1^+ \\ \phi_2^+ \\ \phi_3^+ \end{pmatrix}.$$

# Yukawa Couplings of lighter charged Higgs in 3HDM

- We take  $H_3^+$  to be much heavier than  $H_2^+$ , the Yukawa interactions of  $H_2^+$  is:

$$\mathcal{L}_{H_2^\pm} = -H_2^+ \left\{ \frac{\sqrt{2}V_{ud}}{v_{sm}} \bar{u}(m_d X P_R + m_u Y P_L)d + \frac{\sqrt{2}m_l}{v_{sm}} Z \bar{\nu}_L l_R \right\} + H.c.$$

- Yukawa couplings for  $H_2^+$  can be written as:

$$X = \frac{U_{d2}^\dagger}{U_{d1}^\dagger}, \quad Y = -\frac{U_{u2}^\dagger}{U_{u1}^\dagger}, \quad Z = \frac{U_{\ell 2}^\dagger}{U_{\ell 1}^\dagger}.$$

- Five independent versions of Yukawa interactions of 3HDM with NFC based on charged assignment of two softly-broken discrete  $Z_2$  symmetries.

	$u$	$d$	$\ell$
3HDM(Type I)	2	2	2
3HDM(Type II)	2	1	1
3HDM(Lepton-specific)	2	2	1
3HDM(Flipped)	2	1	2
3HDM(Democratic)	2	1	3

# Mixing matrix $U$ in 3HDM

- The matrix  $U$  can be written explicitly as a function of four parameters  $\tan \beta$ ,  $\tan \gamma$ ,  $\theta$ , and  $\delta$ , where

$$\tan \beta = v_2/v_1, \quad \tan \gamma = \sqrt{v_1^2 + v_2^2}/v_3.$$

- $v_1$ ,  $v_2$ , and  $v_3$  are the vacuum expectation values of the three Higgs doublets.
- $\theta$  is the mixing angle between  $H_2^+$  and  $H_3^+$
- $\delta$  is the CP-violating phase.
- The explicit form of  $U$  given as :  
[C. Albright, J. Smith and S.-H.H. Tye 1980]

$$= \begin{pmatrix} s_\gamma c_\beta & s_\gamma s_\beta & c_\gamma \\ -c_\theta s_\beta e^{-i\delta} - s_\theta c_\gamma c_\beta & c_\theta c_\beta e^{-i\delta} - s_\theta c_\gamma s_\beta & s_\theta s_\gamma \\ s_\theta s_\beta e^{-i\delta} - c_\theta c_\gamma c_\beta & -s_\theta c_\beta e^{-i\delta} - c_\theta c_\gamma s_\beta & c_\theta s_\gamma \end{pmatrix}$$

Here  $s$ ,  $c$  denote the sine or cosine of the respective parameter.

# Experiment constraints on $X, Y$

$$X = \frac{U_{d2}^\dagger}{U_{d1}^\dagger}, \quad Y = -\frac{U_{u2}^\dagger}{U_{u1}^\dagger}, \quad Z = \frac{U_{\ell 2}^\dagger}{U_{\ell 1}^\dagger}.$$

- $b \rightarrow s\gamma$  constrains the real part of  $(XY^*)$ . For  $m_{H^\pm} = 100$  GeV case within  $2\sigma$  interval: [Michael Trott, Mark B. Wise, arXiv:1009.2813v3]

$$-1.1 \leq \text{Re}(XY^*) \leq 0.7.$$

- The **Electric Dipole Moment** (EDM) of the neutron (CP-violation can manifest from Yukawa couplings) gives the following constraint for  $m_{H^\pm} = 100$  GeV :

$$|\text{Im}(XY^*)| \leq 0.1.$$

# Study dominant tree-level fermionic decay modes of light $H^\pm$

- Take  $M_{H^\pm} < M_t$  limit and study leading decays.
- Only focus on fermions by considering additional neutral scalars to be much heavier than  $H^\pm$ .

Tree-level partial width of  $H^\pm$ :

- $$\Gamma(H^\pm \rightarrow \ell^\pm \nu) = \frac{G_F m_{H^\pm} m_\ell^2 |Z|^2}{4\pi\sqrt{2}},$$

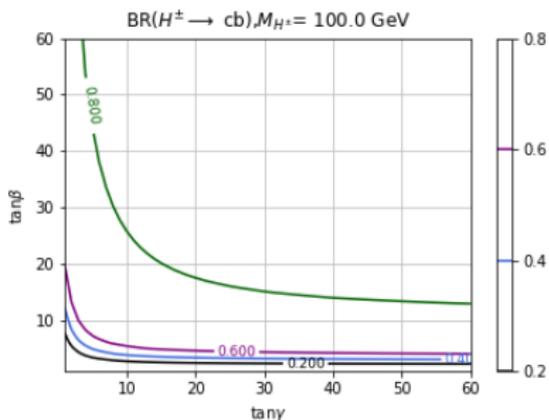
- $$\Gamma(H^\pm \rightarrow ud) = \frac{3G_F V_{ud} m_{H^\pm} (m_d^2 |X|^2 + m_u^2 |Y|^2)}{4\pi\sqrt{2}}.$$

# Study dominant tree-level fermionic decay modes of light $H^\pm$

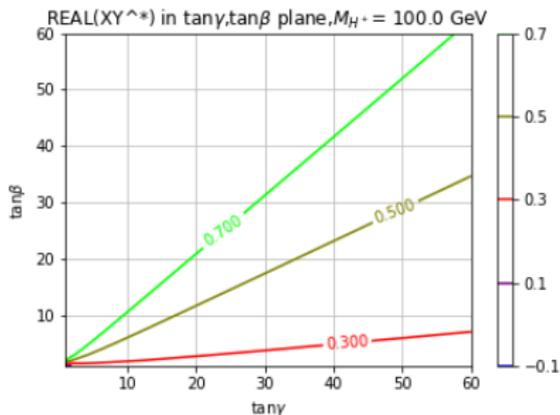
- $|X| \gg |Y|, |Z|$ ,  $BR(H^\pm \rightarrow cb)$  could be dominant ( $\sim 80\%$ ).  
[Grossman 1994, AGA/Sterling 1994]
- $BR(H^\pm \rightarrow cs)$  and  $BR(H^\pm \rightarrow \tau\nu)$  are usually dominant at 2HDM / 3HDM (Type I, Type II, Lepton-specific).
- Study  $BR(H^\pm \rightarrow cb)$  for different types of 3HDM as function of mixing matrix parameters ( $\tan\beta$ ,  $\tan\gamma$ ,  $\theta$ ,  $\delta$ ).
- 2 types (**Flipped and Democratic**) can have large  $BR(H^\pm \rightarrow cb)$ .

	$u$	$d$	$\ell$
3HDM(Type I)	2	2	2
3HDM(Type II)	2	1	1
3HDM(Lepton-specific)	2	2	1
3HDM(Flipped)	2	1	2
3HDM(Democratic)	2	1	3

# Results for $BR(H^\pm \rightarrow cb)$ in Flipped 3HDM in $[\tan\gamma, \tan\beta]$ plane



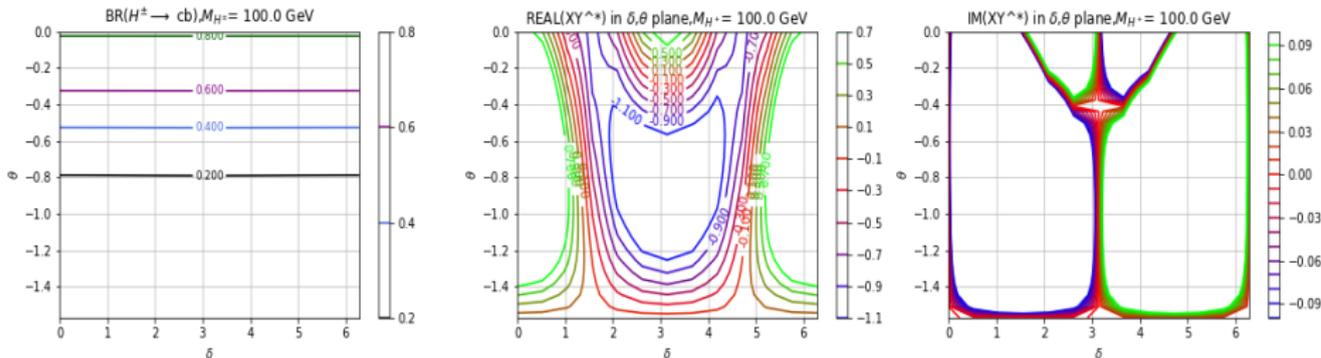
(a)



(b)

**Figure:** Branching ratio of  $H^\pm \rightarrow cb$  with  $\theta = -\pi/3, \delta = 0, M_{H^\pm} = 100$  GeV in  $[\tan\gamma, \tan\beta]$  plane. **Left Panel:** Contours of  $BR(H^\pm \rightarrow cb)$ . **Right Panel:** Contours of  $Re(XY^*)$  ( $b \rightarrow s\gamma$  constraint).

# Results for $BR(H^\pm \rightarrow cb)$ in Democratic 3HDM in $[\delta, \theta]$ plane



**Figure:** Branching ratio of  $H^\pm$  decay through  $cb$  channel with  $\tan\beta = 40$ ,  $\tan\gamma = 10$ ,  $M_{H^\pm} = 100$  GeV in  $[\delta, \theta]$  plane. **Left Panel:** Contours of  $BR(H^\pm \rightarrow cb)$ . **Central Panel:** Contours of  $Re(XY^*)$  in  $[\delta, \theta]$  plane ( $b \rightarrow s\gamma$  constraint). **Right Panel:** Contours of  $Im(XY^*)$  in  $[\delta, \theta]$  plane (Neutron EDM constraint).

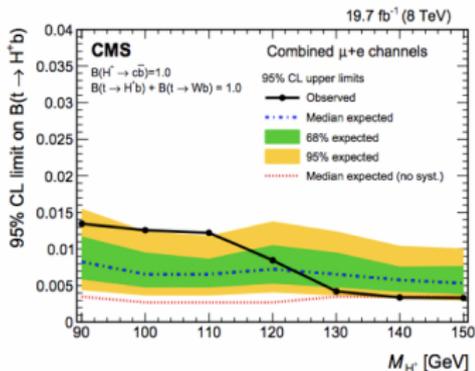
# Dominant $cb$ decay from light $H^\pm$ in 3HDM

Benefit of  $cb$ :

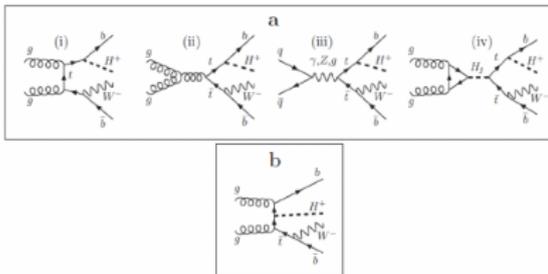
- Distinctive decay channel to separate NFC 2HDM and NFC 3HDM.
- $H^\pm \rightarrow cb$  can be large in Flipped 2HDM for  $M_{H^\pm} \leq M_t$ , but  $M_{H^\pm} \leq M_t$  scenario is ruled out by  $b \rightarrow s\gamma$  constraint.
- In 3HDM, large  $H^\pm \rightarrow cb$  and  $M_{H^\pm} \leq M_t$  is allowed by  $b \rightarrow s\gamma$ .
- Beneficial for  $M_{H^\pm} \sim M_w$  search.
- Search gap at LHC within region 80 GeV  $\rightarrow$  90 GeV.
- Background to  $H^\pm \rightarrow cb$  from  $W^\pm \rightarrow cb$  is small due to small CKM matrix element ( $V_{cb} \approx 0.04$ ).
- Use b-tagging to select signal events and to suppress the background.

# Search for light charged Higgs from LHC and LEP2

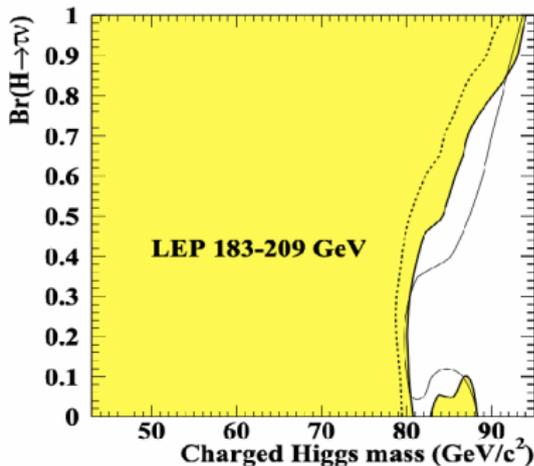
LHC [arXiv:1808.06575]



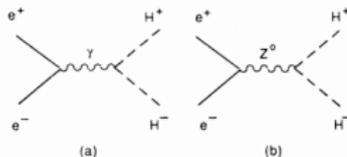
$gg, q\bar{q}, b\bar{b}(\rightarrow t\bar{t} \rightarrow b\bar{t}H^+) \rightarrow b\bar{b}W^-H^+,$   
 $gg(\rightarrow b\bar{t}H^+) \rightarrow b\bar{b}W^-H^+$



LEP [arXiv:1301.6065]



$e^+e^- \rightarrow H^+H^-$



# Prospect searches for $H^\pm$ at LEP2 within mass region 80 GeV $\rightarrow$ 90 GeV

- LHC search covered ( $cb, cs$  and  $\tau\nu$ ), while LEP search only covered ( $cs$  and  $\tau\nu$ ).
- LHC did not cover mass between 80 and 90 GeV while LEP search did not cover b-tagging strategy.
- We took 4-jet decay searches ( $cs/cb + cb/cs$ ) and 2-jet decay searches ( $cs/cb + \tau\nu$ ) from  $\sigma(e^+e^- \rightarrow H^+H^-)$
- Requiring exactly two and exactly one b-jet in 4-jet search / exactly one b-jet in 2-jet search to evaluate event signals.
- Take b-tagging efficiency ( $e_b$ ) and fake-b tagging efficiencies ( $e_c, e_s$ ) to calculate significances ( $\frac{S}{\sqrt{B}}$ ) based on the background event numbers from OPAL result. [Eur. Phys. J.C (2012) 72:2076]

# Proposed search in significances of $H^\pm$ at LEP2 under 4 jets

$M_{H^\pm}$	80 GeV	85 GeV	89 GeV	80 GeV	85 GeV	89 GeV	
	$S$	$S$	$S$	$\frac{S}{\sqrt{B}}$	$\frac{S}{\sqrt{B}}$	$\frac{S}{\sqrt{B}}$	$B$
4j0b	69.50	46.01	29.07	2.08	1.38	0.87	1117.8
4j1b	31.74	21.01	13.27	3.32	2.20	1.39	91.44
4j2b	22.43	14.85	9.38	7.12	4.71	3.00	9.94

**Table:** Number of signal events ( $S$ ), number of background events ( $B$ ), and corresponding significances ( $\frac{S}{\sqrt{B}}$ ) in single experiment at LEP2 under 4-jets ( $H^+H^- \rightarrow jjjj$ ).

- **4-jet channels** with  $\text{BR}(H^\pm \rightarrow cb) = 0.8$  and  $\text{BR}(H^\pm \rightarrow cs) = 0.2$ .
- **4j0b** is the LEP2 search without b-tagging.  $\frac{S}{\sqrt{B}}$  is small.
- **4j1b** and **4j2b** have sensitivity between  $80 < M_{H^\pm} < 90$  GeV.  
(Especially **4j2b** is about 3 times larger than the no b-tagging search.)

# Proposed search in significances of $H^\pm$ at LEP2 under 2 jets

$M_{H^\pm}$	80 GeV	85 GeV	89 GeV	80 GeV	85 GeV	89 GeV	
	$S$	$S$	$S$	$\frac{S}{\sqrt{B}}$	$\frac{S}{\sqrt{B}}$	$\frac{S}{\sqrt{B}}$	$B$
2j0b	26.89	17.80	11.24	1.51	1.00	0.63	316.9
2j1b	15.28	10.11	6.39	4.08	2.70	1.71	14.04

**Table:** Number of signal events ( $S$ ), number of background events ( $B$ ), and corresponding significances ( $\frac{S}{\sqrt{B}}$ ) in single experiment at LEP2 under 2-jets ( $H^+H^- \rightarrow jjl\nu$ ).

- **2-jet channels** with  $\text{BR}(H^\pm \rightarrow \tau\nu) = 0.5$ ,  $\text{BR}(H^\pm \rightarrow cb) = 0.4$  and  $\text{BR}(H^\pm \rightarrow cs) = 0.1$ .
- **2j0b** is the LEP2 search without b-tagging.  $\frac{S}{\sqrt{B}}$  is small.
- **2j1b** improved the sensitivity between  $80 < M_{H^\pm} < 90$  GeV.

- We have studied the scenario of the lighter charged Higgs in 3HDM with  $m_{H^\pm} < m_t$ .
- Two types of 3HDM (Flipped and Democratic) can have large  $BR(H^\pm \rightarrow cb)$ . b-tagging could be a good strategy to search for charged Higgs signals.
- LHC searched for  $H^\pm \rightarrow cb, cs, \tau\nu$  but did not cover mass region between 80 to 90 GeV for hadronic decays. LEP only searched for  $H^\pm \rightarrow cs$  and  $\tau\nu$  in that mass region.
- Our analysis showed the significances of  $H^\pm$  with large  $BR(H^\pm \rightarrow cb)$  can be increased after b-tagging in both 4-jets and 2-jets channels .
- We suggest an updated LEP2 search that includes b-tagging in the mass region 80  $\rightarrow$  90 GeV.

# Thanks for Listening

# Backup slides

## 3HDM Scalar potential under $Z_2 \times Z_2$ symmetry

$$\begin{aligned} V = & \sum_{i=1}^3 m_{ii}^2 (\Phi_i^\dagger \Phi_i) - \left( \sum_{ij=12,13,23} m_{ij}^2 (\Phi_i^\dagger \Phi_j) + H.c \right) \\ & + \frac{1}{2} \sum_{i=1}^3 \lambda_i (\Phi_i^\dagger \Phi_i)^2 + \sum_{ij=12,13,23} \lambda_{ij} (\Phi_i^\dagger \Phi_i) (\Phi_j^\dagger \Phi_j) \\ & + \sum_{ij=12,13,23} \lambda'_{ij} (\Phi_i^\dagger \Phi_j) (\Phi_j^\dagger \Phi_i) + \frac{1}{2} \left[ \sum_{ij=12,13,23} \lambda''_{ij} (\Phi_i^\dagger \Phi_j)^2 + H.c \right] \end{aligned}$$

- 18 free parameters which two are fixed by W boson mass and SM neutral Higgs mass.

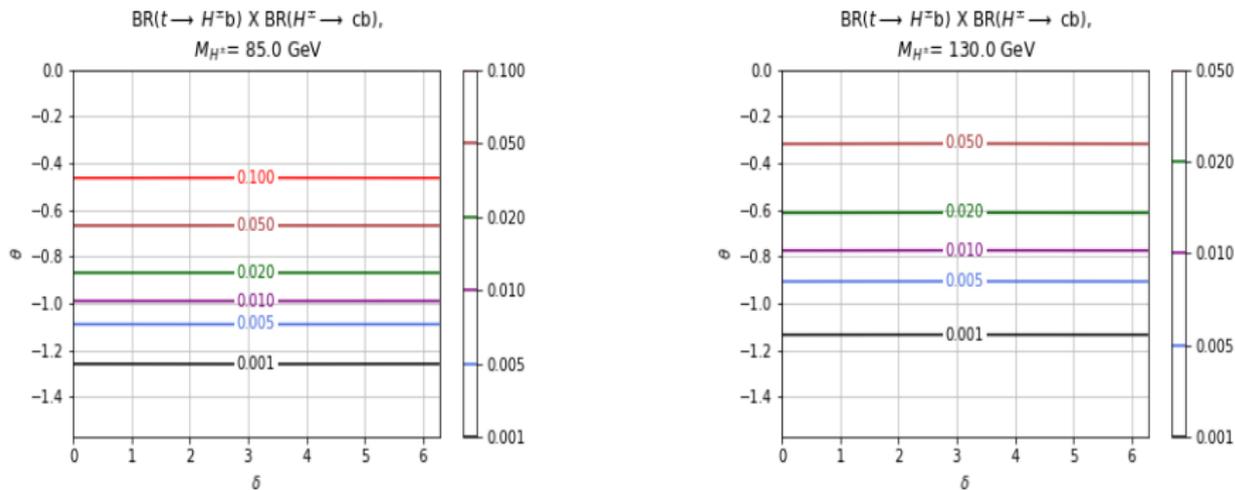
# Production mechanism of $H^\pm$ pair from LEP collider

Production cross-section of  $H^\pm$  pair:



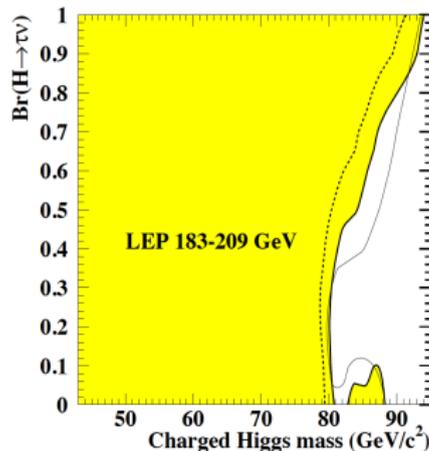
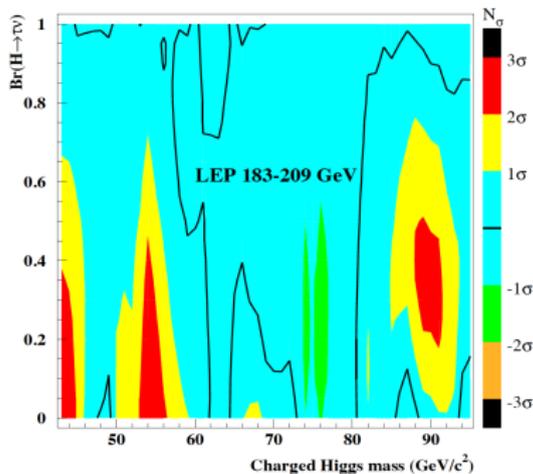
$$\sigma_{H^+H^-} = \frac{\pi\alpha^2}{3s} \left( \sqrt{1 - \frac{4M_{H^\pm}^2}{s}} \right)^3 F(s, M_z, \Gamma_z, \theta_w)$$

# Results of Democratic 3HDM approach with $BR(t \rightarrow H^\pm b) \times BR(H^\pm \rightarrow cb)$ in $[\delta, \theta]$ plane for LHC



**Figure:**  $BR(t \rightarrow H^\pm b) \times BR(H^\pm \rightarrow cb)$  in  $[\delta, \theta]$  plane with  $\tan\beta = 40, \tan\gamma = 10, M_{H^\pm} = 85, 130$  GeV. **Left Panel:**  $M_{H^\pm} = 85$  GeV plane. **Right Panel:**  $M_{H^\pm} = 130$  GeV plane.

# LEP search results on $Br(H^\pm \rightarrow \tau\nu)$ [arXiv: 1301.6065]



*Left Panel* : Statistical Significance from background expectation. *Right Panel* : excluded regions in the  $Br(H^\pm \rightarrow \tau\nu)$  vs  $M_{H^\pm}$  plane. The shaded area is excluded at 95 % C.L. or higher. Solid line is expected exclusion limit at 95 %. The dotted line is observed limit at 99.7 % C.L.



$$\Gamma(t \rightarrow W^\pm b) = \frac{G_F m_t}{8\sqrt{2}\pi} [m_t^2 + 2M_W^2] [1 - M_W^2/m_t^2]^2$$



$$\Gamma(t \rightarrow H^\pm b) = \frac{G_F m_t}{8\sqrt{2}\pi} [m_t^2 |Y|^2 + m_b^2 |X|^2] [1 - m_{H^\pm}^2/m_t^2]^2.$$

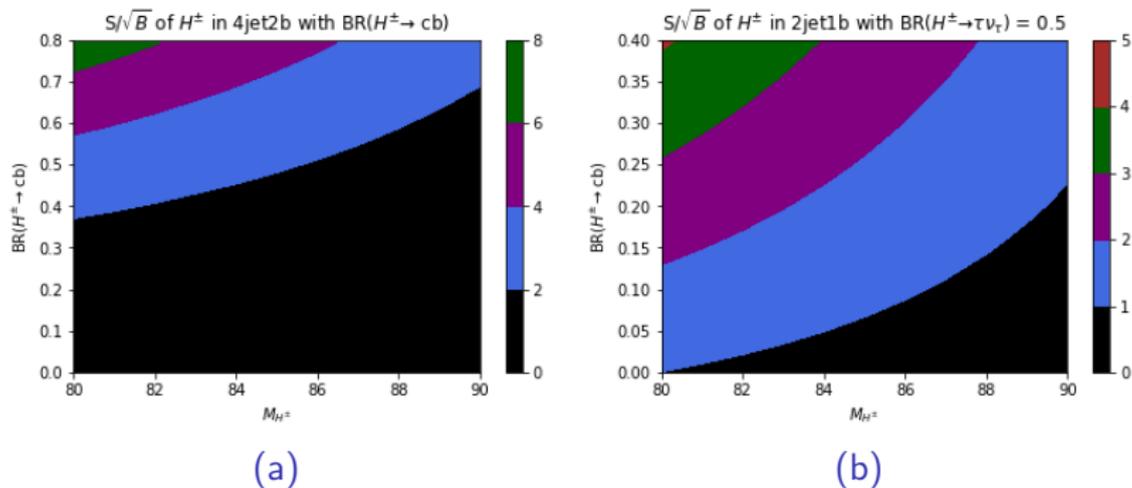
- $BR(t \rightarrow H^\pm b)$  depends on magnitudes of  $|X|, |Y|$ . It affects production rate of charged Higgs even LHC has sensitivity for mass region 80 to 90 GeV.
- LEP search involves only gauge couplings and unknown charged Higgs mass parameter.

# LEP2 and CEPC/FCC-ee Input parameters

	$\sqrt{s}$	$\mathcal{L}(\text{fb}^{-1})$	$\epsilon_b$	$\epsilon_c$	$\epsilon_j$	$M_{H^\pm}$
LEP2	189 GeV $\rightarrow$ 209 GeV	0.6	0.7	0.06	0.01	80 GeV $\rightarrow$ 90 GeV
CEPC/FCC-ee	240 GeV	1000	0.7	$0.01 < \epsilon_c < 0.06$	0.01	80 GeV $\rightarrow$ 120 GeV

**Table:** Input parameters used in the numerical analysis at LEP2 and at CEPC/FCC-ee.

# Numerical analysis in statistical Significances of $H^\pm$ against $\text{BR}(H^\pm \rightarrow cb)$



**Figure:** Values of  $S\sqrt{B}$  in the plane  $[M_{H^\pm}, \text{BR}(H^\pm \rightarrow cb)]$  at a single LEP2 experiment. **Left Panel:** In 4-jet channel with two b-tags, with  $\text{BR}(H^\pm \rightarrow cb) + \text{BR}(H^\pm \rightarrow cs) = 1$ . **Right Panel:** In 2-jet channel with one b-tag, with  $\text{BR}(H^\pm \rightarrow \tau\nu) = 0.5$ , and  $\text{BR}(H^\pm \rightarrow cb) + \text{BR}(H^\pm \rightarrow cs) = 0.5$ .



ATLAS Collaboration and others (2018)

Evidence for the associated production of the Higgs boson and a top quark pair with the ATLAS detector

*Journal Name Phys. Rev. D* 21 (1980) 711.



C. Albright, J. Smith and S.-H.H. Tye(1980)

Signatures for charged Higgs boson production in  $e + e$  collisions

*Journal Name Physical Review D*,85(11),115002.



Thomas G. Rizzo (1988)

$b \rightarrow s\gamma$  in the two-Higgs-doublet model

*Journal Name Physical Review D*,38, 820.



DØ Collaboration (2009)



S. L. Glashow and S. Weinberg, *Phys. Rev. D* 15 (1977) 1958



On theories of enhanced CP violation in  $B_{s,d}$  meson mixing, Michael Trott, Mark B. Wise