

New Model for Radiative Neutrino Masses and Higgs LFV Decays

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SK, Sugiyama (1015)

SK, Sakurai, Sugiyama (2016)

Aoki, SK, Sakurai, Sugiyama (2017)

Enomoto, SK, Sakurai, Sugiyama (2019)

First Mediterranean Conference on Higgs Physics
at Conseil regional Tanger-Tétouan-AlHoceima, 23-27 September 2019

Evidences of beyond-SM

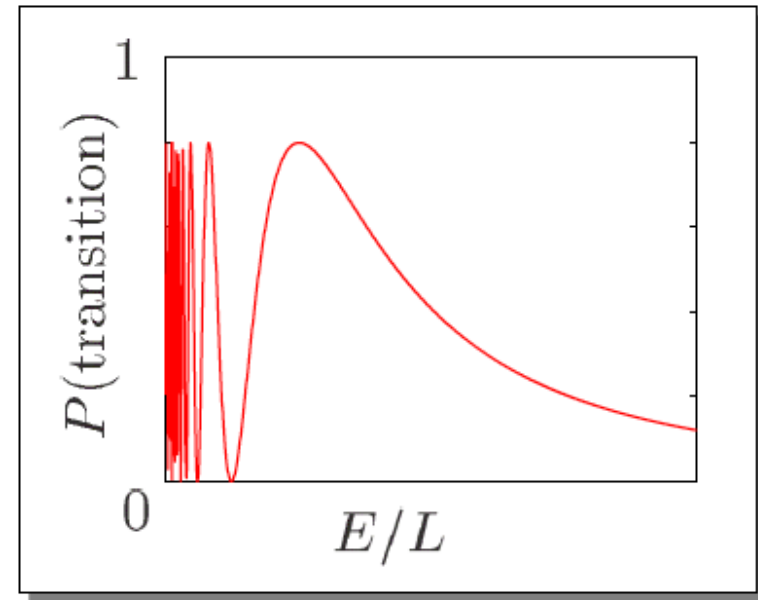
- **Dark Matter**
- **Baryon Asymmetry of Universe**
- **Neutrino Oscillation**
- **Cosmic Inflation**
- ...

Neutrino Oscillation

Transition prob.

$$\Delta m^2 \equiv m_2^2 - m_1^2$$

$$P(\nu_e \rightarrow \nu_{e'}) \simeq \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$



Nonzero neutrino masses

cf. Massless in the SM

Lepton flavor violation (LFV)

cf. Conserved in the SM

Two evidences

for physics beyond the SM

Tiny Neutrino Masses

If the same mechanism as for quarks or charged leptons,

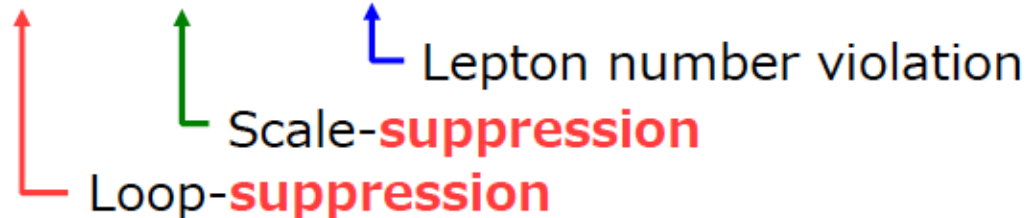
$$y_\nu \bar{L} \epsilon \Phi^* \nu_R \longrightarrow m_\nu = \frac{y_\nu}{\sqrt{2}} v$$

$$m_\nu \sim 0.1 \text{ eV} \Rightarrow y_\nu \sim 10^{-12}$$

Unnaturally small !

Tiny neutrino mass would be generated in a non-trivial way

$$\text{e.g., } \left(\frac{1}{16\pi^2} \right)^n \frac{1}{\Lambda} \bar{L} \epsilon \Phi^* \Phi^\dagger \epsilon L^c$$


Loop-suppression
Scale-suppression
Lepton number violation

LFV in Oscillation = Large Mixing

Flavor $\nu_\ell = \sum_i \underbrace{(U_{\text{MNS}})_{\ell i}} \nu_i$ **Mass**

Mixing : $U_{\text{MNS}} \sim \begin{pmatrix} 0.83 & 0.54 & 0.15 \\ -0.47 & 0.53 & 0.71 \\ 0.31 & -0.66 & 0.69 \end{pmatrix} \leftarrow \text{Large mixings}$

cf. Quark mixing

$$V_{\text{CKM}} \sim \begin{pmatrix} 0.97 & 0.23 & 0 \\ -0.23 & 0.97 & 0 \\ 0 & 0 & 1.0 \end{pmatrix} \leftarrow \text{Small mixings}$$

Significant sources for LFV associated with neutrinos

This talk

- **Classification of neutrino mass models from the view point of LFV sources (new Yukawas)**
- **If Higgs LFV decays will be discovered in the future, a wide class of simple models for neutrino masses will be excluded**
- **We discuss a new model which can survive even if Higgs LFV decays are discovered**

Classification of neutrino mass models

Models of neutrino mass

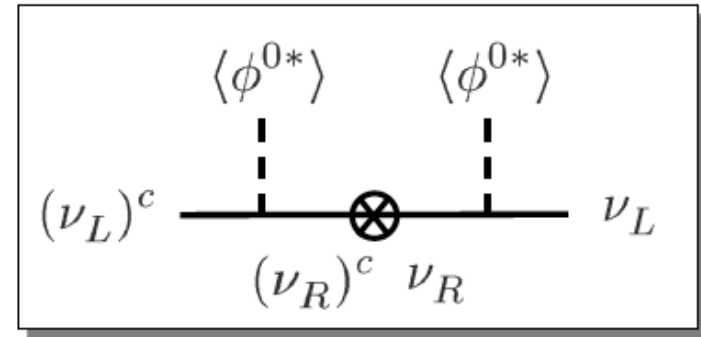
Seesaw Mechanism

$$\mathcal{L} = y_\nu \bar{L} \epsilon \Phi^* \nu_R + \frac{1}{2} M_R \overline{(\nu_R)^c} \nu_R + \dots$$

(lepton # violation)



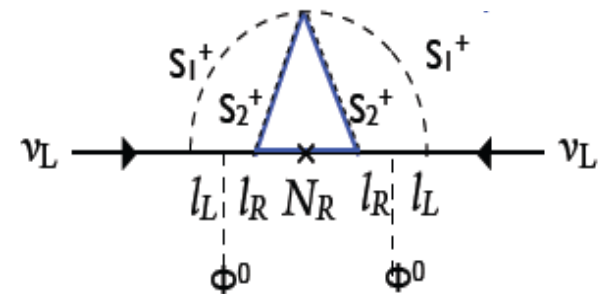
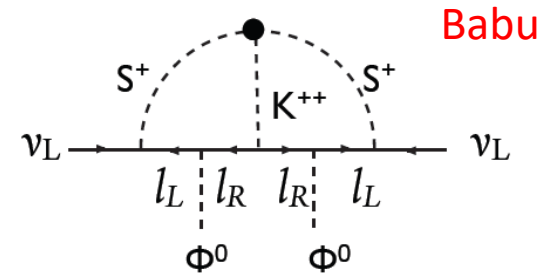
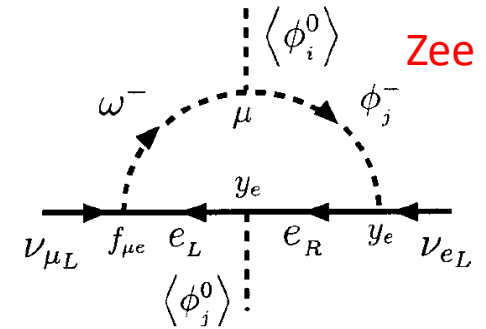
$$\frac{1}{2} m_M \overline{(\nu_L)^c} \nu_L \quad m_M \simeq \frac{y_\nu^2 \langle \phi^{0*} \rangle^2}{M_R}$$



Loop induced masses

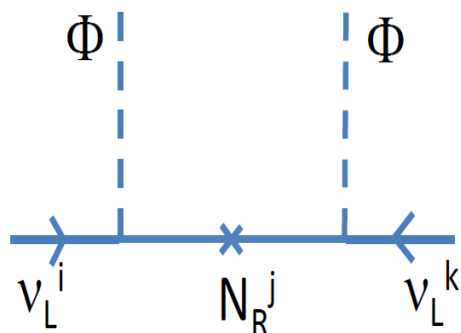
Tiny ν -Masses may come from loop effects

- Zee (1980, 1985)
- Zee, Babu (1988)
- Krauss-Nasri-Trodden (2002)
- Ma (2006),
-

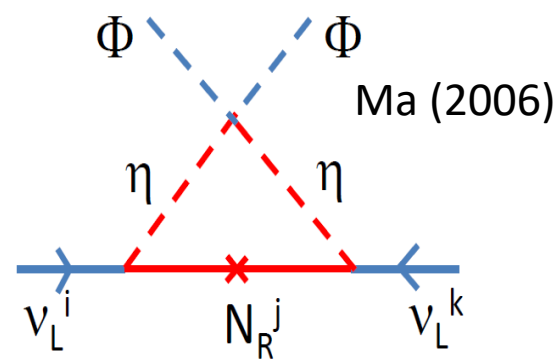


Krauss, Nasri, Trodden

Zee; Babu

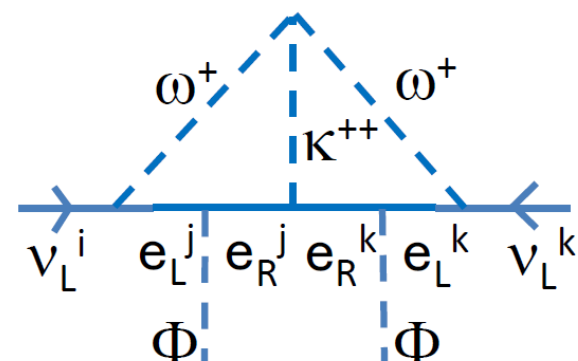


Yanagida; Gell-Mann; Minkowski
 $(m, n) = (0, 0)$



$(1, 0)$

Ma (2006)

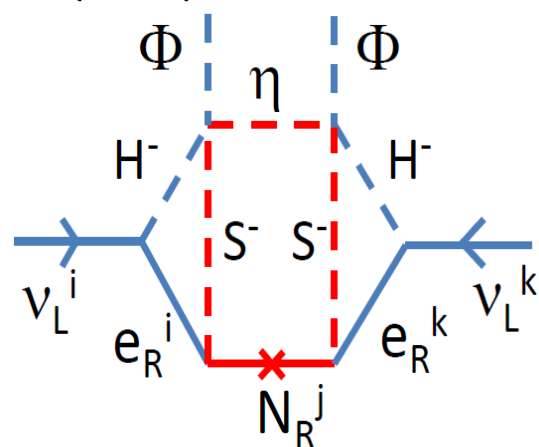


$(2, 0)$

$$m_\nu \sim c' \left(\frac{1}{16\pi^2} \right)^m \left(\frac{v}{\Lambda} \right)^{2n+1} v$$

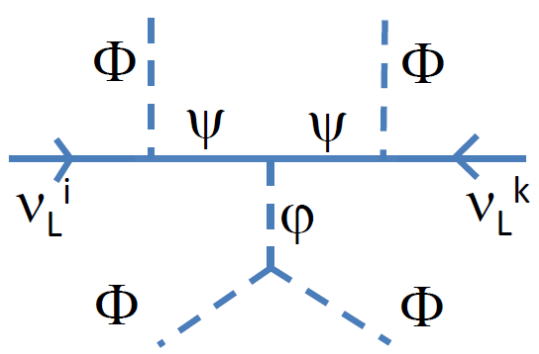
Dim $5+n$ Operator
 m -loop induced

Aoki, SK, Seto (2008)



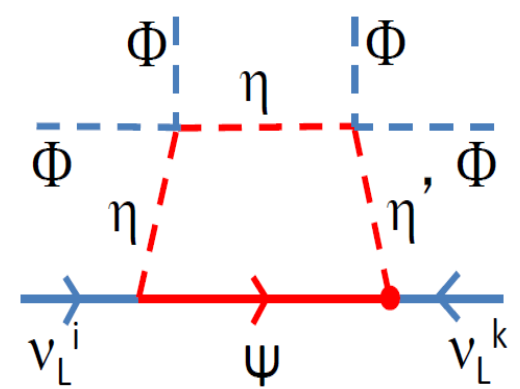
$(3, 0)$

Bonnet, et al. (2009)



$(0, 1)$

SK, Ota (2010)

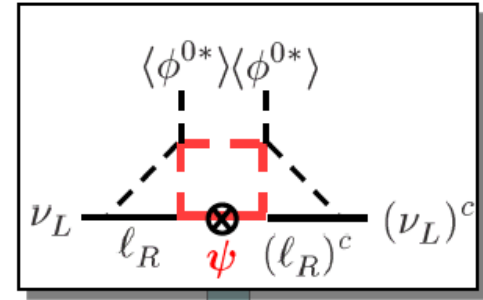
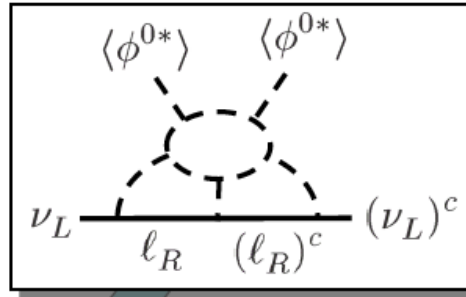
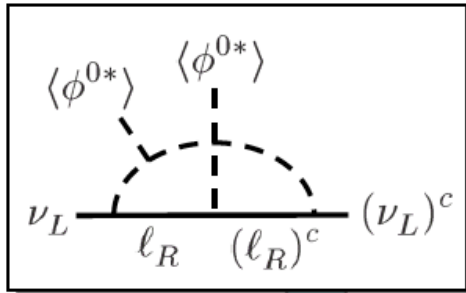


$(1, 1)$

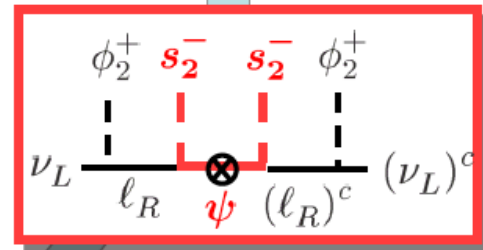
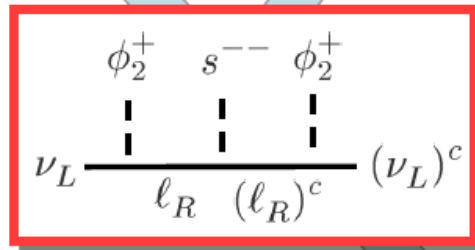
Z_2 -odd fields are in red letters

Classification of Models

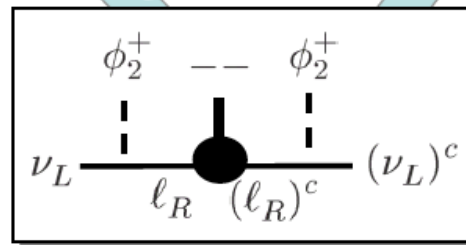
- Models (full Lagrangian)



- Concentrating on Yukawa int.

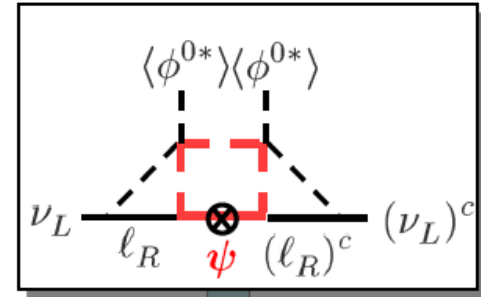
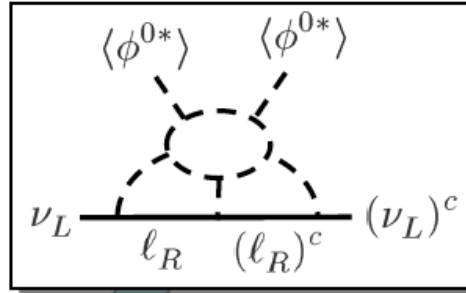
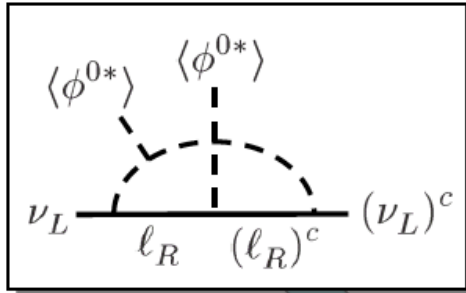


- Concentrating on Yukawa int. between leptons

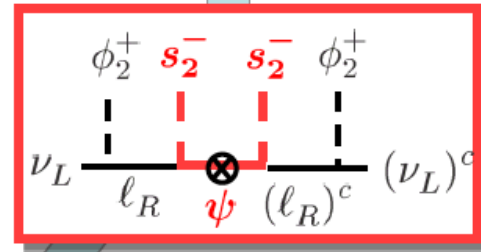
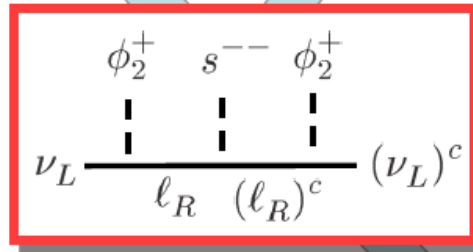


Classification of Models

- Models (full Lagrangian)

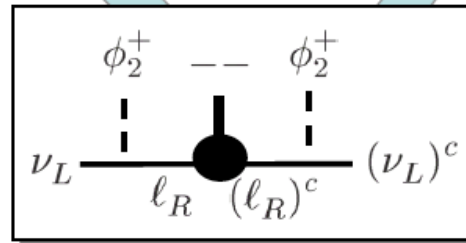


- Concentrating on Yukawa int.



We focus on the fermion line
To extract the flavor structure

Concentrating on Yukawa int. between leptons



Neutrino mass and leptonic Yukawa couplings

Extension of the Higgs sector (scalar sector)

Many models $\xrightarrow{\text{Classification}}$ Efficient study

- Setup for our analyses

New scalars with leptonic Yukawa int.

$$[\text{New scalar}] - [\text{Lepton}] - [\text{Lepton}]$$

Assumption : **No FCNC at the tree level**

Z_2 -odd singlet fermion ψ_R^0
 Z_2 -odd scalars with leptonic Yukawa int. (unbroken)

} \longrightarrow Dark matter

$$[Z_2\text{-odd scalar}] - [\text{Lepton}] - \psi_R^0$$

ν_R for Dirac neutrinos
(lepton number conservation)

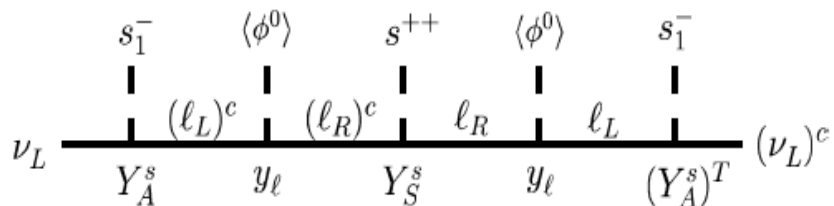
Models for Majorana masses

All new Yukawa interactions and new scalars

Bilinears	New Scalars			Yukawa Interaction
	Fields	SU(2) _L	U(1) _Y	
$\overline{L}_L^i \ell_R^j$	ϕ_2	2	$+\frac{1}{2}$	$y_i \overline{L}_L^i \phi_2 \ell_R^j$
$(\ell_R^i)^c \ell_R^j$	s^{++}	1	+2	$(Y_s^S)_{ij} (\ell_R^i)^c \ell_R^j s^{++}$
$(L_L^i)^c L_L^j$	s_1^+	1	+1	$(Y_s^A)_{ij} (L_L^i)^c L_L^j s_1^+$
	Δ	3	+1	$(Y_\Delta^S)_{ij} (L_L^i)^c \Delta L_L^j$
$(\psi_R^a)^c \ell_R^i$	s_2^+	1	+1	$(Y_s)_{ai} (\psi_R^a)^c \ell_R^i s_2^+$
$\overline{L}_L^i \psi_R^a$	η	2	$+\frac{1}{2}$	$(Y_\eta)_{ia} \overline{L}_L^i \eta^c \psi_R^a$

Select scalars for ν mass diagram

e.g.) fermion line in M1

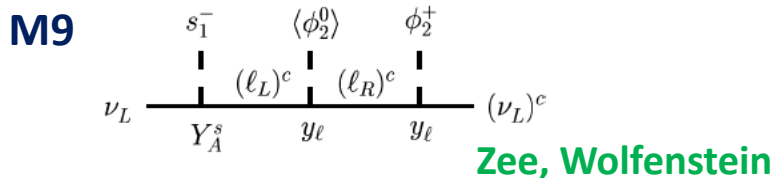
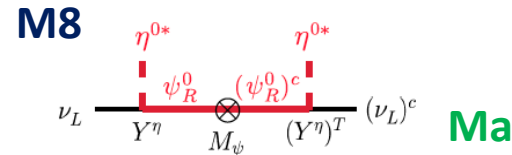
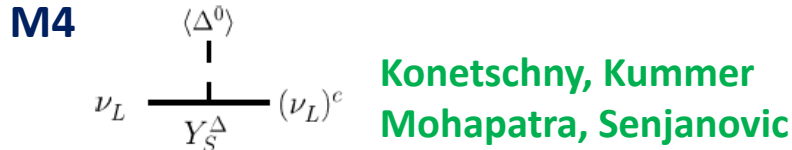
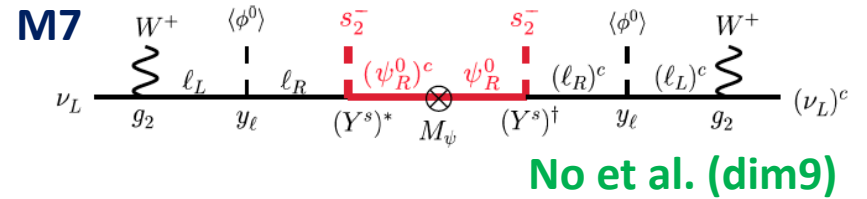
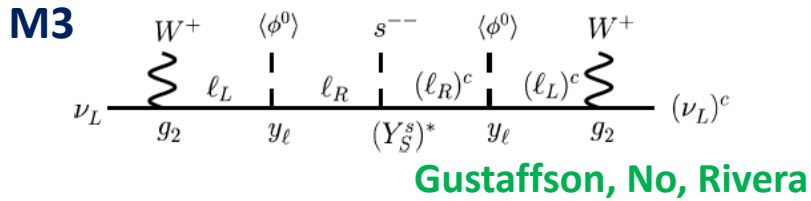
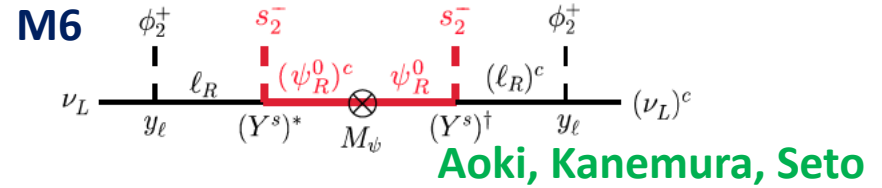
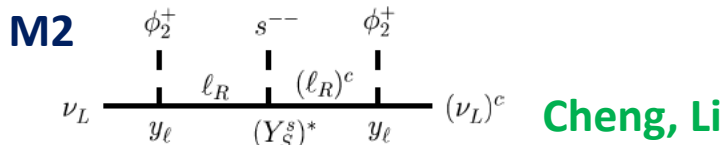
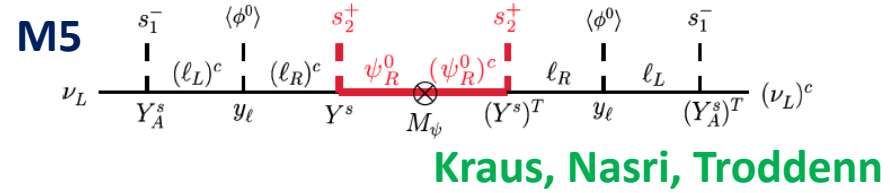
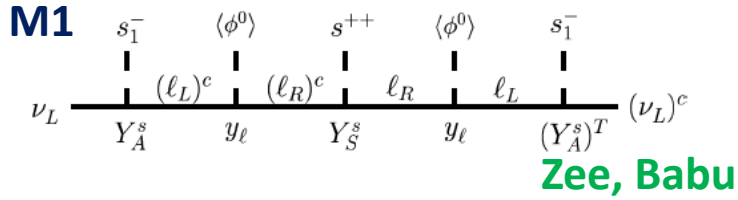


Z_2 -odd fields are in red letters

Models for Majorana ν masses

	Δ	ϕ_2	s^{++}	s_L^+	η	s_2^+
SU(2) _L	3	2	1	1	2	1
U(1) _Y	+1	+1/2	+2	+1	+1/2	+1
Z_2	Even				Odd	
M1			✓	✓		
M2		✓	✓			
M3			✓			
M4	✓					
M5				✓		✓
M6		✓				✓
M7						✓
M8					✓	

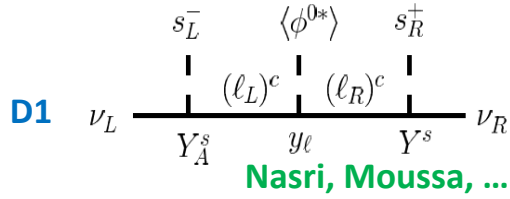
Models of Radiative Neutrino Mass (Majorana Type)



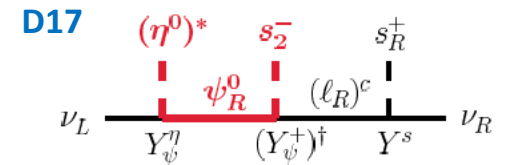
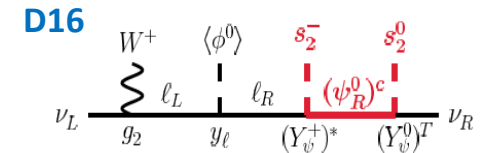
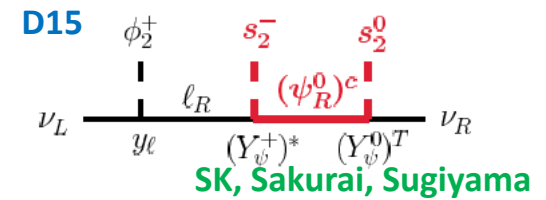
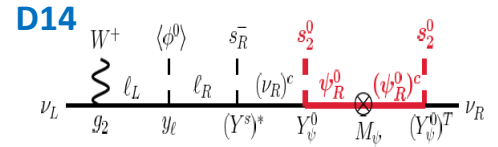
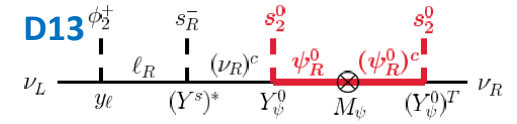
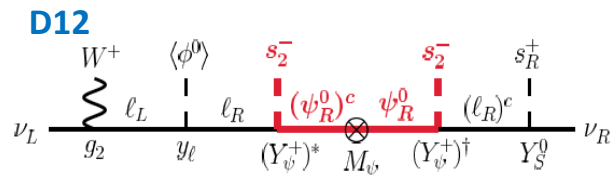
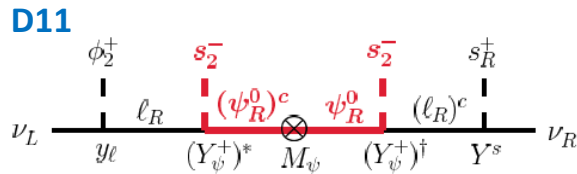
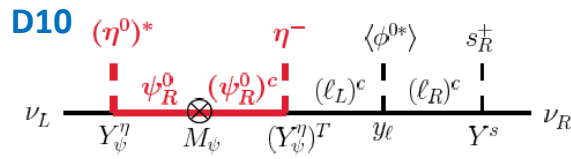
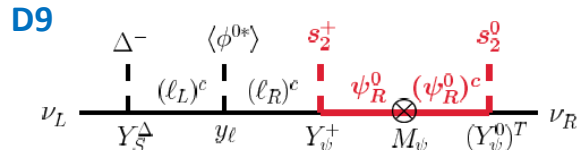
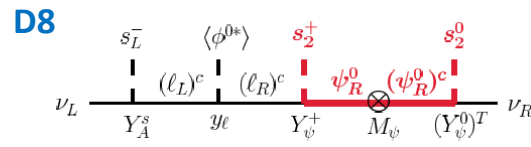
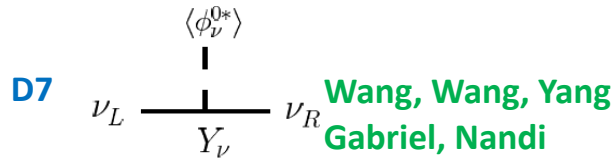
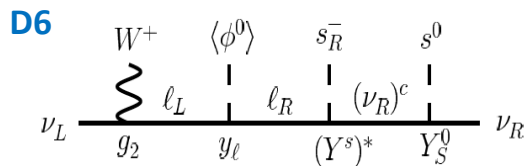
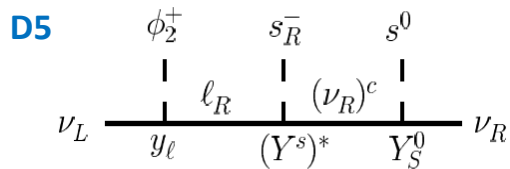
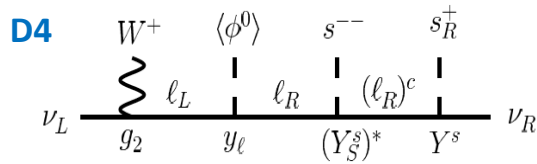
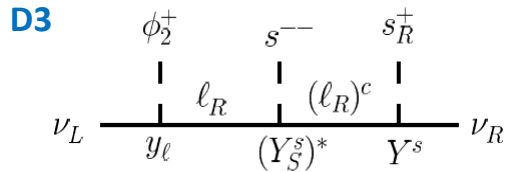
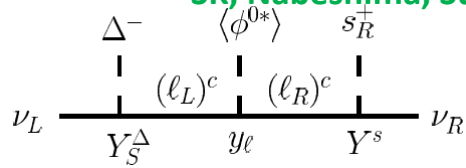
Models for Majorana masses

	Scalar with leptonic Yukawa int.					
					Z_2 -odd	
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>
$U(1)_Y$	1	2	1/2	1	1	1/2
Unbroken Z_2	+	+	+	+	-	-
M1	✓	✓				
M2		✓	✓			
M3		✓				
M4				✓		
M5	✓				✓	
M6			✓		✓	
M7					✓	
M8						✓

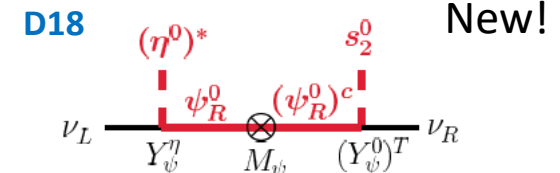
Models of Radiative Neutrino Mass (Dirac Type)



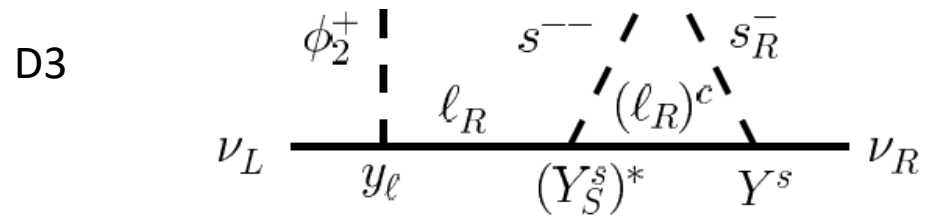
SK, Nabeshima, Sugiyama



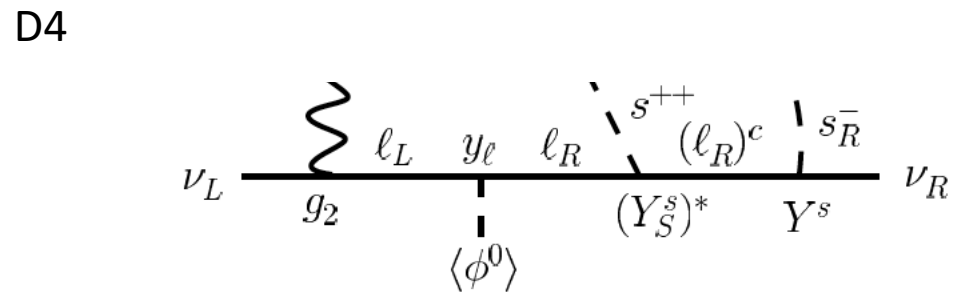
Aoki, SK, Sakurai, Sugiyama



Example to close scalar lines of D3



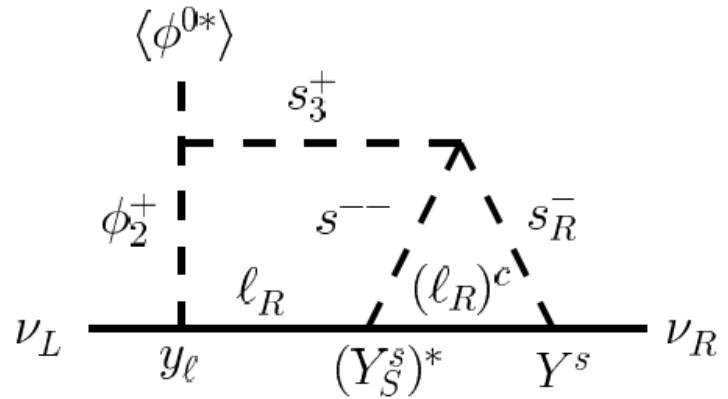
Example to close scalar lines of D4



Example to close scalar lines of D3

Dim 4 (2 loop)

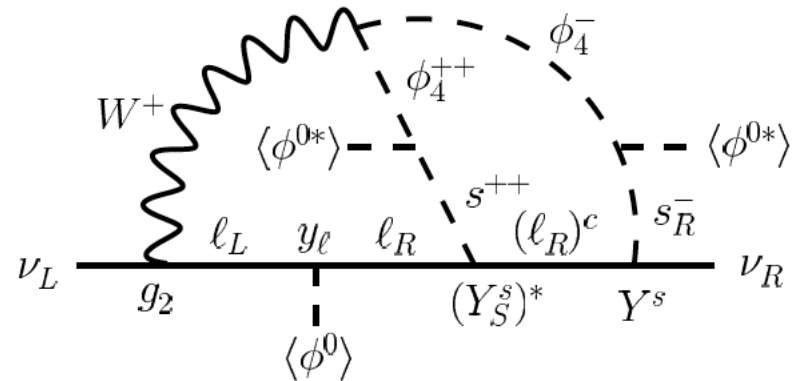
D3



Example to close scalar lines of D4

Dim 6 (2 loop)

D4



Models for Dirac masses

S. K., K. Sakurai, H. Sugiyama, PLB (2016)


Additional assumptions

- New fermions :


$$\nu_R^i \quad (i = 1, 2, 3)$$

- New symmetries :

Lepton # conservation

 $\overline{\nu_R^i} \left(\nu_R^j \right)^c$

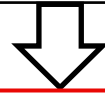
Softly broken Z_2 sym.

 $\overline{L_L^i} \phi^c \nu_R^j$

	Δ	ϕ_2	ϕ_ν	s^{++}	s_R^+	s_L^+	s^0	η	s_2^+	s_2^0
SU(2) _L	3	2	2	1	1	1	1	2	1	1
U(1) _Y	+1	+1/2	+1/2	+2	+1	+1	0	+1/2	+1	0
Z_2	Even							Odd		
Lepton #	-2	0	0	-2	-2	-2	-2	-1	-1	-1
Z_2'	Even	Even	Odd	Even	Odd	Even	Even	Even	Even	Odd
D1					✓	✓				
D2	✓				✓					
D3		✓		✓	✓					
D4				✓	✓					
D5		✓			✓		✓			
D6					✓		✓			
D7			✓							
D8						✓			✓	✓
D9	✓								✓	✓
D10					✓			✓		
D11		✓			✓				✓	
D12					✓				✓	
D13		✓			✓					✓
D14					✓					✓
D15		✓							✓	✓
D16									✓	✓
D17					✓			✓	✓	
D18								✓		✓

Lepton Flavor Violation

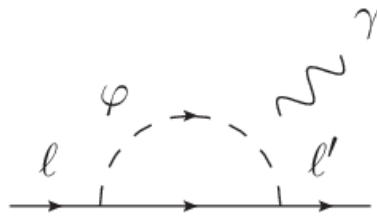
Neutrino oscillation + Models for neutrino masses



LFV processes

Lepton LFV decays

$$l \rightarrow l' \gamma$$

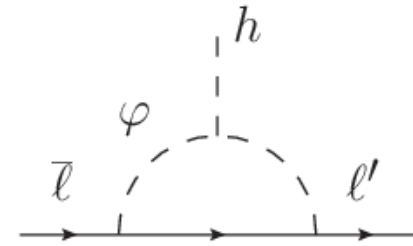


Current constraint

Process	Upper limit
$\mu \rightarrow e \gamma$	4.2×10^{-13}
$\tau \rightarrow e \gamma$	3.3×10^{-8}
$\tau \rightarrow \mu \gamma$	4.4×10^{-8}

Higgs LHV decays

$$h \rightarrow l l'$$

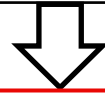


Current constraint

Process	Upper limit
$h \rightarrow \mu e$	3.5×10^{-4}
$h \rightarrow \tau e$	6.1×10^{-3}
$h \rightarrow \mu \tau$	2.5×10^{-3}

New observable

Neutrino oscillation + Models for neutrino masses

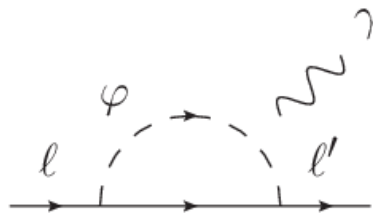


LFV processes

Lepton LFV decays

$$l \rightarrow l' \gamma$$

**Strongly
constrained !**



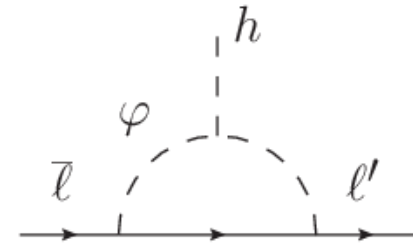
Current constraint

Process	Upper limit
$\mu \rightarrow e \gamma$	4.2×10^{-13}
$\tau \rightarrow e \gamma$	3.3×10^{-8}
$\tau \rightarrow \mu \gamma$	4.4×10^{-8}

Higgs LHV decays

$$h \rightarrow l l'$$

New observable



Current constraint

Process	Upper limit
$h \rightarrow \mu e$	3.5×10^{-4}
$h \rightarrow \tau e$	6.1×10^{-3}
$h \rightarrow \mu \tau$	2.5×10^{-3}

**Future
ILC250**

**3.3×10^{-5}
(2 ab⁻¹)**

LFV decays of the Higgs boson

$$\text{BR}(h \rightarrow \ell\ell') \equiv \text{BR}(h \rightarrow \bar{\ell}\ell') + \text{BR}(h \rightarrow \ell\bar{\ell}')$$

In 2015, there was
anomaly for $h \rightarrow \mu\tau$

		ATLAS 8 TeV, 20.3 fb ⁻¹ arXiv:1604.07730	CMS 8 TeV, 19.7 fb ⁻¹ arXiv:1607.03561; PLB749, 337 (2015)
$h \rightarrow e\mu$	Limit		$< 3.5 \times 10^{-4}$
	Best fit		
$h \rightarrow e\tau$	Limit	$< 1.04 \times 10^{-2}$	$< 6.9 \times 10^{-3}$
	Best fit	$-3.4^{+6.4}_{-6.6} \times 10^{-3}$	
$h \rightarrow \mu\tau$	Limit	$< 1.43 \times 10^{-2}$	$< 1.51 \times 10^{-2}$
	Best fit	$5.3^{+5.1}_{-5.1} \times 10^{-3}$	$8.4^{+3.9}_{-3.7} \times 10^{-3}$

2.4 σ excess

LFV decays of the Higgs boson

$$\text{BR}(h \rightarrow \ell\ell') \equiv \text{BR}(h \rightarrow \bar{\ell}\ell') + \text{BR}(h \rightarrow \ell\bar{\ell}')$$

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		ATLAS 8 TeV, 20.3 fb ⁻¹ arXiv:1604.07730	CMS 8 TeV, 19.7 fb ⁻¹ arXiv:1607.03561; PLB749, 337 (2015)
$h \rightarrow e\mu$	Limit		$< 3.5 \times 10^{-4}$
	Best fit		
$h \rightarrow e\tau$	Limit	$< 1.04 \times 10^{-2}$	$< 6.9 \times 10^{-3}$
	Best fit	$-3.4^{+6.4}_{-6.6} \times 10^{-3}$	
$h \rightarrow \mu\tau$	Limit	$< 1.43 \times 10^{-2}$	$< 1.51 \times 10^{-2}$
	Best fit	$5.3^{+5.1}_{-5.1} \times 10^{-3}$	$8.4^{+3.9}_{-3.7} \times 10^{-3}$

2.4 σ excess

It's already gone!
(No excess now)

Although the previous anomaly has been gone,
there can be discovery of $h \rightarrow \ell \ell'$ in the future

Esp at ILC

**What is the impact on the models
for neutrino masses?**

Higgs LFV decays occur at loop

Dimension-4 operator

$$\mathcal{L} = Y_4 [\bar{L} \Phi \ell'_R]$$

$$\text{Mass : } \frac{v}{\sqrt{2}} Y_4 [\bar{\ell}_L \ell'_R] \xrightarrow{\text{Diagonalize}} m_\ell [\bar{\ell}_L \ell_R]$$

$$\text{Int. : } \frac{1}{\sqrt{2}} Y_4 [\bar{\ell}_L \ell'_R h] \dashrightarrow \frac{m_\ell}{v} [\bar{\ell}_L \ell_R h] \quad \text{no LFV}$$

Higgs LFV decays occur at loop

Dimension-4 operator

$$\mathcal{L} = \mathbf{Y}_4 [\bar{L} \Phi \ell'_R]$$

$$\text{Mass : } \frac{v}{\sqrt{2}} \mathbf{Y}_4 [\bar{\ell}_L \ell'_R] \xrightarrow{\text{Diagonalize}} m_\ell [\bar{\ell}_L \ell_R]$$

$$\text{Int. : } \frac{1}{\sqrt{2}} \mathbf{Y}_4 [\bar{\ell}_L \ell'_R h] \dashrightarrow \frac{m_\ell}{v} [\bar{\ell}_L \ell_R h] \quad \text{no LFV}$$

Dimension-6 operator

$$\mathcal{L} = \mathbf{Y}_4 [\bar{L} \Phi \ell'_R] + \frac{\mathbf{Y}_6}{\Lambda^2} [\bar{L} \Phi \ell'_R (\Phi^\dagger \Phi)]$$

$$\text{Mass : } v \left(\frac{1}{\sqrt{2}} \mathbf{Y}_4 + \frac{v^2}{2\Lambda^2} \mathbf{Y}_6 \right) [\bar{\ell}_L \ell'_R] \xrightarrow{\text{Diag.}} m_\ell [\bar{\ell}_L \ell_R] \quad \text{LFV}$$

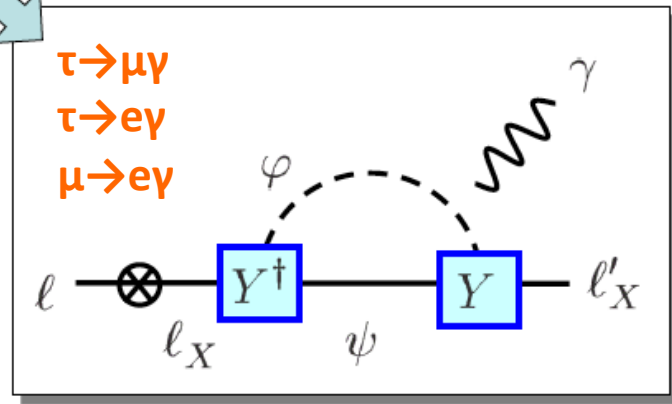
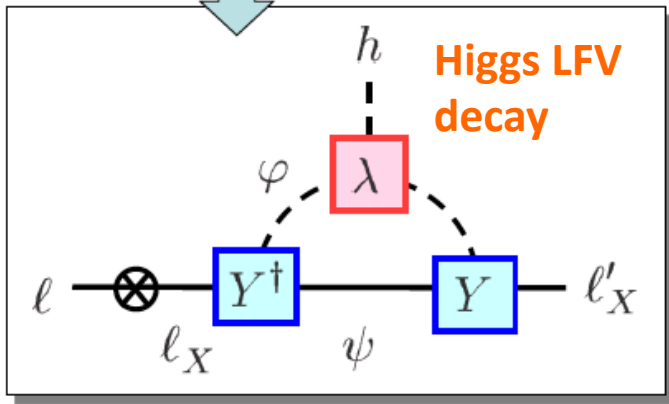
$$\text{Int. : } \left(\frac{1}{\sqrt{2}} \mathbf{Y}_4 + \frac{3v^2}{2\Lambda^2} \mathbf{Y}_6 \right) [\bar{\ell}_L \ell'_R h] \dashrightarrow \left(\frac{m_\ell}{v} \delta_{\ell\ell'} + \frac{v^2}{\Lambda^2} \mathbf{Y}_6 \right) [\bar{\ell}_L \ell'_R h]$$

Correlation

Toy model

$$\mathcal{L} = Y_{al} \left[\overline{\psi}_a l_X \varphi \right] - \lambda |\Phi|^2 |\varphi|^2 + \dots$$

$X = L, R$



$$\text{Br}(h \rightarrow ll') \sim 10^{-1} \text{Br}(l \rightarrow l' \gamma)$$

Too small $\text{Br}(h \rightarrow ll')$
to be observed.
If observed,
the toy model is excluded.



$$\left\{ \begin{array}{l} \text{BR}(\mu \rightarrow e \gamma) < 4.2 \times 10^{-13} \\ \text{MEG collab.}, \text{ arXiv:1605.05081} \\ \text{BR}(\tau \rightarrow e \gamma) < 3.3 \times 10^{-8} \\ \text{BR}(\tau \rightarrow \mu \gamma) < 4.4 \times 10^{-8} \\ \text{Babar collab.}, \text{ PRL104, 021802} \end{array} \right.$$

If $h \rightarrow \ell\ell'$ is observed

Models for Majorana neutrino masses

	Scalar with leptonic Yukawa int.						$\ell \rightarrow \ell'\gamma$	
					Z_2 -odd			
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η		
SU(2) _L	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>		
U(1) _Y	1	2	1/2	1	1	1/2		
Unbroken Z_2	+	+	+	+	-	-		
M1	✓	✓					✓	✓
M2		✓	✓					✓
M3		✓						✓
M4				✓			✓	
M5	✓				✓		✓	✓
M6			✓		✓			✓
M7					✓			✓
M8						✓	✓	

Only a LFV Yukawa \Rightarrow Same as the toy model

If $h \rightarrow \ell \ell'$ is observed

Models for Majorana neutrino masses

	Scalar with leptonic Yukawa int.						$\ell \rightarrow \ell' \gamma$	
					Z_2 -odd			
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	1	2	1/2	1	1	1/2		
Unbroken Z_2	+	+	+	+	-	-		
M1	✓	✓					✓	✓
M2		✓	✓					✓
M3		✓						✓
M4				✓			✓	
M5	✓				✓		✓	✓
M6			✓		✓			✓
M7					✓			✓
M8						✓	✓	

Two LFV Yukawa, but no cancellation to suppress $\ell \rightarrow \ell' \gamma$

If $h \rightarrow \ell \ell'$ is observed

Models for **Majorana**
neutrino masses

	Scalar with leptonic Yukawa int.						$\ell \rightarrow \ell' \gamma$	
					Z_2 -odd			
	s_L^+	s^{++}	Φ_2	Δ	s_2^+	η		
SU(2) _L	<u>1</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>2</u>		
U(1) _Y	1	2	1/2	1	1	1/2		
Unbroken Z_2	+	+	+	+	-	-		
M1	✓	✓					✓	✓
M2		✓	✓					✓
M3		✓						✓
M4				✓			✓	
M5	✓				✓		✓	✓
M6			✓		✓			✓
M7					✓			✓
M8						✓	✓	

All excluded for Majorana neutrinos !

If $h \rightarrow \ell\ell'$ is observed

Models for Dirac neutrino masses (1)

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell'\gamma$	
								Z_2 -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D1		✓	✓								✓	✓
D2			✓				✓				✓	✓
D3			✓	✓			✓					✓✓
D4			✓	✓								✓✓
D5	✓		✓				✓					✓
D6	✓		✓									✓
D7					✓						✓	

If $h \rightarrow \ell\ell'$ is observed

Models for Dirac neutrino masses (1)

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell'\gamma$	
								Z_2 -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D1		✓	✓								✓	✓
D2			✓				✓				✓	✓
D3			✓	✓		✓						✓✓
D4			✓	✓								✓✓
D5	✓		✓			✓						✓
D6	✓		✓									✓
D7					✓						✓	

D3 and D4 survive

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell' \gamma$	
								Z ₂ -odd			ℓ'_L	ℓ'_R
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
SU(2) _L	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
U(1) _Y	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z' ₂	+	+	-	+	-	+	+	-	+	+		
D3			✓	✓		✓						✓✓
D4			✓	✓								✓✓

$$\text{BR}(\ell \rightarrow \ell' \gamma) \propto \left| \frac{(Y^{s^\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} + \frac{(Y_S^{s^\dagger} Y_S^s)_{\ell\ell'}}{m_{s^{++}}^2} \right|^2 \ll \left| \frac{(Y^{s^\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} \right|^2$$

Cancellation is possible

$$\text{BR}(h \rightarrow \ell\ell') \propto \left| \lambda_{hs^+} \frac{(Y^{s^\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} + \lambda_{hs^{++}} \frac{(Y_S^{s^\dagger} Y_S^s)_{\ell\ell'}}{m_{s^{++}}^2} \right|^2 \sim \left| 2\lambda_{hs^+} \frac{(Y^{s^\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} \right|^2$$

Not cancelled if λ_{hs^+} and $\lambda_{hs^{++}}$ have opposite sign

Models for Dirac neutrino masses (2)

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell' \gamma$	
								Z_2 -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D8		✓						✓	✓		✓	✓
D9							✓	✓	✓		✓	✓
D10			✓							✓	✓	✓
D11			✓			✓			✓			✓✓
D12			✓						✓			✓✓
D13			✓			✓		✓				✓
D14			✓					✓				✓
D15						✓		✓	✓			✓
D16								✓	✓			✓
D17			✓						✓	✓	✓	✓✓
D18								✓		✓	✓	

Models for Dirac neutrino masses (2)

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell' \gamma$	
								Z_2 -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D8		✓						✓	✓		✓	✓
D9							✓	✓	✓		✓	✓
D10			✓							✓	✓	✓
D11			✓			✓			✓			✓✓
D12			✓						✓			✓✓
D13			✓			✓		✓				✓
D14			✓					✓				✓
D15						✓		✓	✓			✓
D16								✓	✓			✓
D17			✓						✓	✓	✓	✓✓
D18								✓		✓	✓	

Models for Dirac neutrino masses (1)&(2)

	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell' \gamma$	
								Z ₂ -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
SU(2) _L	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
U(1) _Y	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z' ₂	+	+	-	+	-	+	+	-	+	+		
D3			✓	✓		✓						✓✓
D4			✓	✓								✓✓
D11			✓			✓			✓			✓✓
D12			✓						✓			✓✓
D17			✓						✓	✓	✓	✓✓

These mechanisms for generating masses of Dirac neutrinos can **survive** after discovery of $h \rightarrow \ell \ell'$

Models for Dirac neutrino masses (1)&(2)

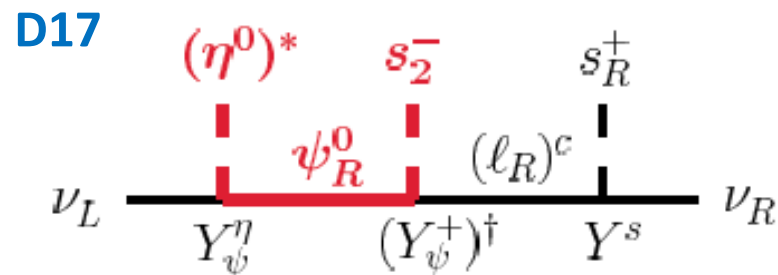
	Scalar with leptonic Yukawa int.										$\ell \rightarrow \ell' \gamma$	
								Z_2 -odd				
	s^0	s_L^+	s_R^+	s^{++}	Φ_ν	Φ_2	Δ	s_2^0	s_2^+	η		
$SU(2)_L$	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>2</u>	<u>2</u>	<u>3</u>	<u>1</u>	<u>1</u>	<u>2</u>		
$U(1)_Y$	0	1	1	2	1/2	1/2	1	0	1	1/2		
LN	-2	-2	-2	-2	0	0	-2	-1	-1	-1		
Z'_2	+	+	-	+	-	+	+	-	+	+		
D3			✓	✓		✓						✓✓
D4			✓	✓								✓✓
D11			✓			✓		✓				✓✓
D12			✓					✓				✓✓
D17			✓					✓	✓		✓	✓✓

Z_2 odd particles

These mechanisms for generating masses of Dirac neutrinos can **survive** after discovery of $h \rightarrow \ell \ell'$

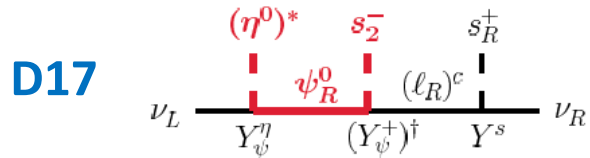
A new model
 for D17 which can survive even if Higgs LFV
 decays are detected in future experiments

K. Enomoto, SK, K. Sakurai, H. Sugiyama,
 Phys. Rev. D100, 015044 (2019)



New model for Dirac neutrino masses with the structure of D17

K. Enomoto, SK, K. Sakurai, H. Sugiyama,
Phys. Rev. D100, 015044 (2019)



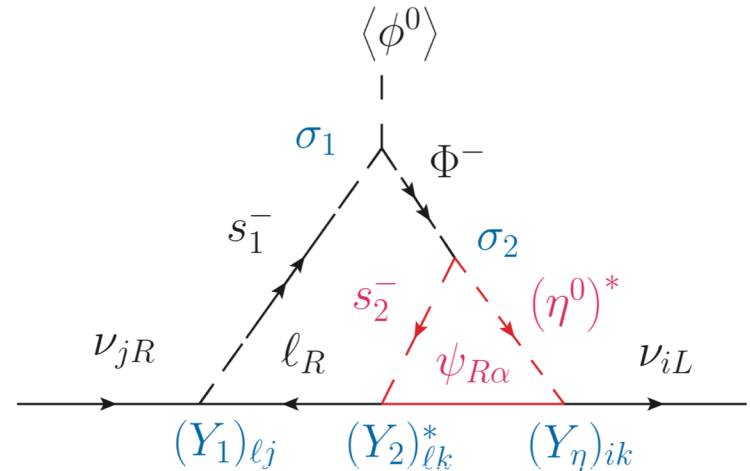
	Fermions		Scalars			
	ν_{Ri}	$\psi_{R\alpha}$	s_1^+	Φ	s_2^+	η
SU(2) _L	1	1	1	2	1	2
U(1) _Y	0	0	1	3/2	1	1/2
Unbroken Z ₂	Even	Odd	Even		Odd	
Z' ₂	-	+	-		+	+
Lepton #	1	0	-2	-2	-1	-1

$i, \alpha = 1 \sim 3$

$$\mathcal{L} = (Y_1)_{\ell i} \overline{(\ell_R)^c} \nu_{Ri} s_1^+ + (Y_2)_{\ell \alpha} \overline{(\ell_R)^c} \psi_{R\alpha} s_2^+ + (Y_\eta)_{\ell \alpha} \overline{L_\ell} \eta^c \psi_{R\alpha} + \text{h.c.}$$

$$V \ni \sigma_1 \Phi^\dagger \phi s_1^+ + \sigma_2 \Phi^\dagger \eta s_2^+ + \text{h.c.}$$

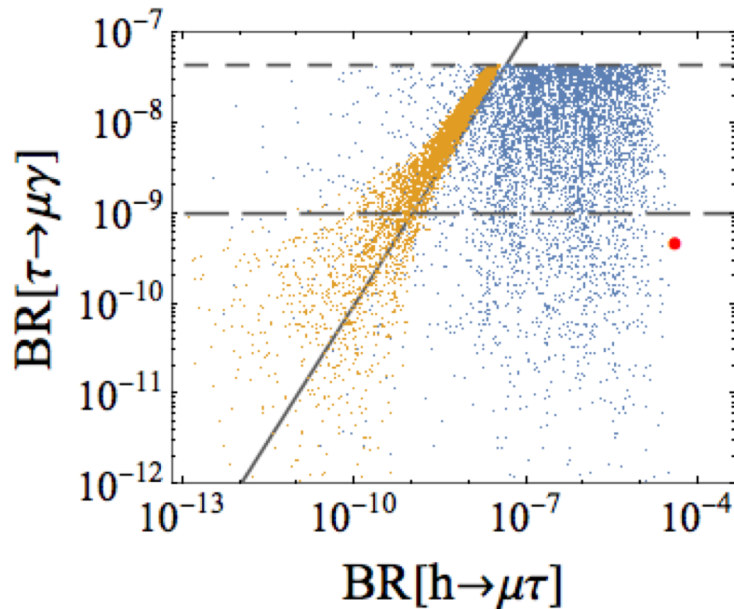
Neutrino masses



New model for Dirac neutrino masses with the structure of D17

K. Enomoto, SK, K. Sakurai, H. Sugiyama,
Phys. Rev. D100, 015044 (2019)

LFV Processes $(Y_1)_{\ell i} \overline{(\ell_R)^c} \nu_{Ri} s_1^+ + (Y_2)_{\ell \alpha} \overline{(\ell_R)^c} \psi_{R\alpha} s_2^+$



— $\text{Br}(\tau \rightarrow \mu\gamma) = \text{Br}(h \rightarrow \mu\tau)$

- - - Upper limit 4.4×10^{-8}

- - - Expected limit 1.0×10^{-9}
Belle II @ 50 ab^{-1}

Orange Points $\lambda_{hs_1} = \lambda_{hs_2} = 2.0$

Blue Points $\lambda_{hs_1} = -\lambda_{hs_2} = 2.0$

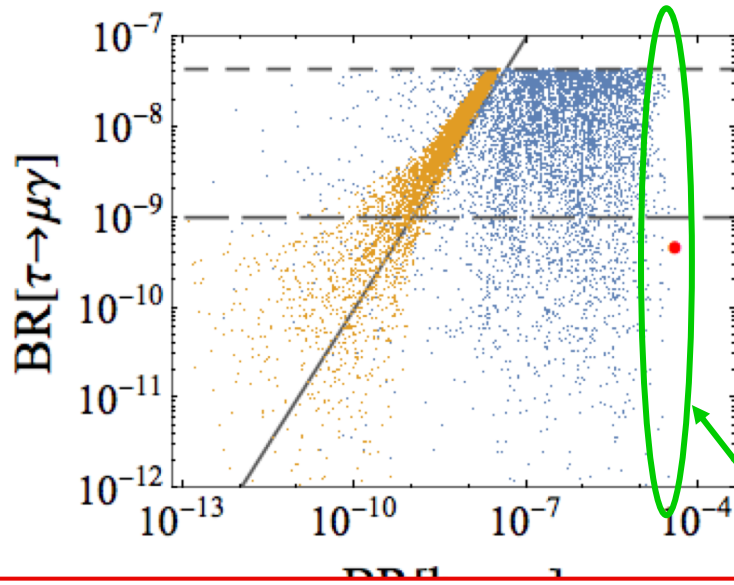
Red point Benchmark scenario

$$Y_a = \begin{pmatrix} 10^{-4} & 10^{-4} & 0.10 \\ x_a & y_a & 10^{-4} \\ z_a & w_a & 10^{-4} \end{pmatrix} \quad -3.0 \leq x_a, y_a, z_a \leq 3.0$$

New model for Dirac neutrino masses with the structure of D17

K. Enomoto, SK, K. Sakurai, H. Sugiyama,
Phys. Rev. D100, 015044 (2019)

LFV Processes $(Y_1)_{li} \overline{(\ell_R)^c} \nu_{Ri} s_1^+ + (Y_2)_{l\alpha} \overline{(\ell_R)^c} \psi_{R\alpha} s_2^+$



— $\text{Br}(\tau \rightarrow \mu\gamma) = \text{Br}(h \rightarrow \mu\tau)$

- - - Upper limit 4.4×10^{-8}

- - - Expected limit 1.0×10^{-9}
Belle II @ 50 ab^{-1}

Orange Points $\lambda_{hs_1} = \lambda_{hs_2} = 2.0$

ILC250

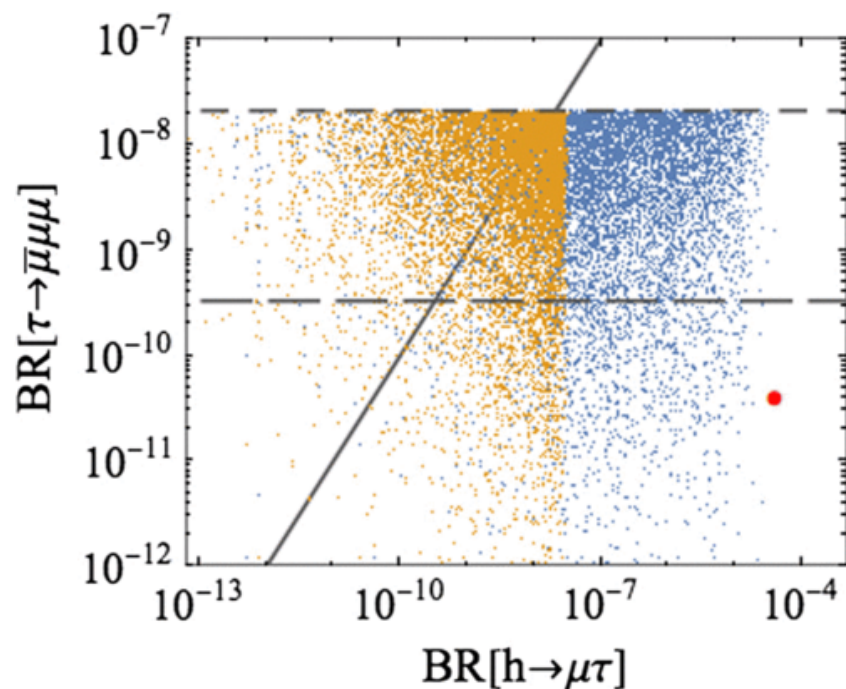
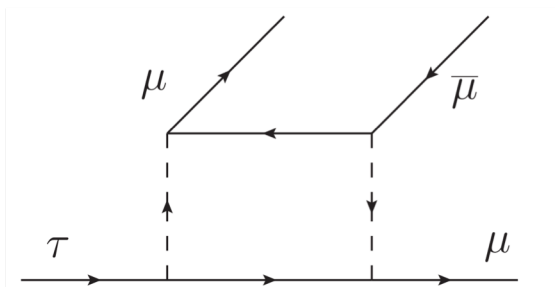
Expected limit $\text{BR}(h \rightarrow \mu\tau) = 4.0 \times 10^{-5}$ ($\mathcal{L} = 1350 \text{ fb}^{-1}$)

I. Chakraborty, A. Datta, A. Kundu, J.Phys (2016)

New model for Dirac neutrino masses with the structure of D17

K. Enomoto, SK, K. Sakurai, H. Sugiyama,
Phys. Rev. D100, 015044 (2019)

$$\tau \rightarrow \bar{\mu}\mu\mu \text{ vs } h \rightarrow \mu\tau$$



— $\text{Br}(\tau \rightarrow \mu\gamma) = \text{Br}(h \rightarrow \mu\tau)$

- - - Upper limit 4.4×10^{-8}

- · - Expected limit 1.0×10^{-9}
Belle II @ 50 ab^{-1}

Orange Points $\lambda_{hs_1} = \lambda_{hs_2} = 2.0$

Blue Points $\lambda_{hs_1} = -\lambda_{hs_2} = 2.0$

Red point Benchmark scenario

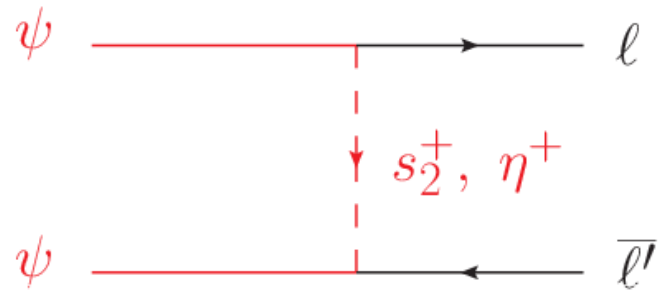
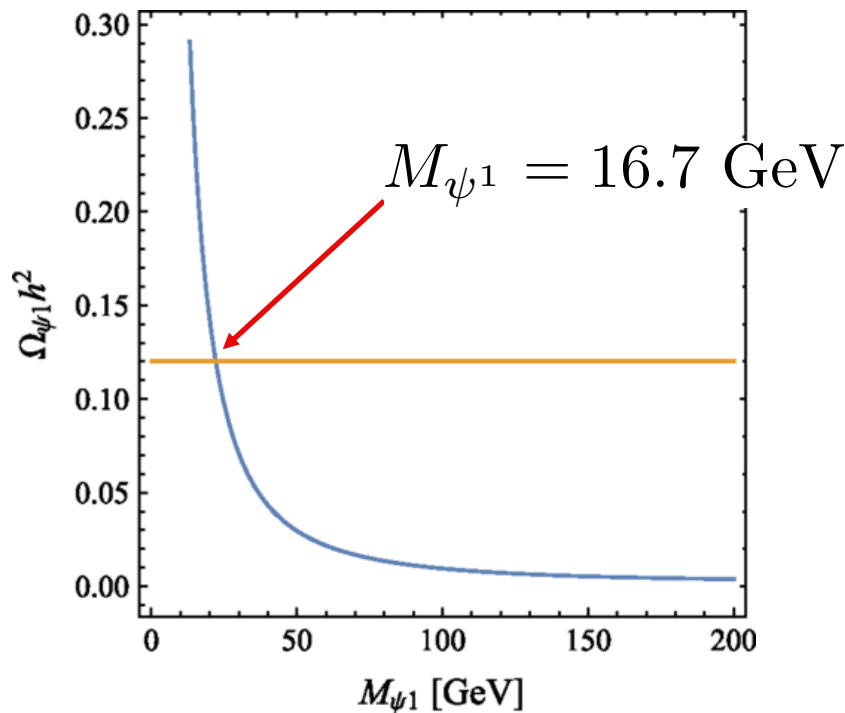
New model for Dirac neutrino masses with the structure of D17

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Dark matter candidates : η^0, ψ^a ($a = 1, 2, 3$)

In the benchmark scenario, dark matter particle is

the lightest Majorana fermion ψ^1



- Relic abundance of ψ^1
- $\Omega_{\text{DM}} h^2 = 0.1200 \pm 0.0012$

Summary

We discussed how observations of LFV decays of the Higgs boson can narrow down models of neutrino masses

We first classified neutrino mass models by focusing on the combination of new Yukawa coupling matrices with leptons

If Higgs LFV decays $h \rightarrow \ell \ell'$ are detected at future colliders, a wide class of models for neutrino masses can be excluded

In particular, simple typical models of Majorana neutrino masses cannot be compatible with the observation of $h \rightarrow \ell \ell'$

A model for Dirac neutrino masses can be compatible with a significant rate of the $h \rightarrow \ell \ell'$ process

Thank you



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LFV processes in benchmark scenario

Processes	Numerical results
$\mu \rightarrow e\gamma$	2.36×10^{-15}
$\tau \rightarrow e\gamma$	8.26×10^{-14}
$\tau \rightarrow \mu\gamma$	4.68×10^{-10}

Processes	Numerical results
$h \rightarrow \mu e$	1.43×10^{-16}
$h \rightarrow \tau e$	1.56×10^{-15}
$h \rightarrow \mu\tau$	4.05×10^{-5}

Processes	Numerical results
$\mu \rightarrow \bar{e}ee$	1.26×10^{-18}
$\tau \rightarrow \bar{e}ee$	4.28×10^{-18}
$\tau \rightarrow \bar{\mu}e\mu$	1.97×10^{-11}

Processes	Numerical results
$\mu \rightarrow \bar{e}\mu\mu$	1.26×10^{-18}
$\tau \rightarrow \bar{e}e\mu$	4.28×10^{-18}
$\tau \rightarrow \bar{\mu}ee$	1.97×10^{-11}
$\tau \rightarrow \bar{\mu}\mu\mu$	3.98×10^{-11}