

# Dark matter in the $Z_3$ I(2+1)HDM

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The I(2+1)HDM history:

V. Keus, S.F. King, S. Moretti, D. Sokolowska

- \* Constraints and DM phenomenology [JHEP 1401 (2014) 051],[Phys.Rev.D 90,075015 (2014)]
- \* Heavy DM [JHEP 1511 (2015) 003]

A. Cordero, J. Hernández-Sánchez, V. Keus, S.F. King, S. Moretti,  
D. Rojas-Ciofalo, D. Sokolowska

- \* CP Violation [JHEP 1612 (2016) 014]
- \* LHC signatures [JHEP 1805 (2018) 030]
- \* Work in progress (lepton collider signatures, CP invariants)

- The stability of DM is guaranteed by residual  $Z_N$  symmetry
- $Z_2$  has been widely studied but  $N > 2$  is also interesting
- $Z_3$  models in the literature:
  - supersymmetric models
  - extra dimensions
  - vector DM models
  - many other
- New DM processes appear:
  - semiannihilation
  - DM conversion

# Some remarks

- Just starting the project
- Not any result yet
- We are testing the parameter space to obtain a good relic density

# The $Z_3$ 1(2+1)HDM

The most general phase invariant part of a 3HDM potential is<sup>1</sup>

$$V_0 = -\mu_i^2(\Phi_i^\dagger \Phi_i) + \lambda_{ij}(\Phi_i^\dagger \Phi_i)(\Phi_j^\dagger \Phi_j) + \lambda'_{ij}(\Phi_i^\dagger \Phi_j)(\Phi_j^\dagger \Phi_i)$$

and, considering an unbroken  $Z_3$  symmetry we add the terms:

$$\begin{aligned} V_{Z_3} = & -\mu_{12}^2(\phi_1^\dagger \phi_2) + \lambda_1(\phi_2^\dagger \phi_1)(\phi_3^\dagger \phi_1) + \lambda_2(\phi_1^\dagger \phi_2)(\phi_3^\dagger \phi_2) \\ & + \lambda_3(\phi_1^\dagger \phi_3)(\phi_2^\dagger \phi_3) + \text{h.c.} \end{aligned}$$

where

$$g_{Z_2} = (1, 2, 0)$$

and

$$\Phi_\alpha = \begin{pmatrix} H_\alpha^\pm \\ \frac{1}{\sqrt{2}}(H_\alpha + iA_\alpha) \end{pmatrix}, \quad \alpha = 1, 2, 3$$

1,2 are the *inert doublets* and 3 is the *active*

<sup>1</sup>V. Keus, S. F. King and S. Moretti, Phys. Rev. D 90, no. 7, 075015 (2014)  
doi:10.1103/PhysRevD.90.075015 [arXiv:1408.0796 [hep-ph]].

## Mass eigenstates: neutral sector

$$\begin{aligned}m_{H_1}^2 &= (-\mu_1^2 + \Lambda_1) \cos^2 \theta_h + (-\mu_2^2 + \Lambda_2) \sin^2 \theta_h - \Lambda_h \sin \theta_h \cos \theta_h \\m_{H_2}^2 &= (-\mu_1^2 + \Lambda_1) \sin^2 \theta_h + (-\mu_2^2 + \Lambda_2) \cos^2 \theta_h + \Lambda_h \sin \theta_h \cos \theta_h \\m_{A_1}^2 &= (-\mu_1^2 + \Lambda_1) \cos^2 \theta_a + (-\mu_2^2 + \Lambda_2) \sin^2 \theta_a - \Lambda_a \sin \theta_a \cos \theta_a \\m_{A_2}^2 &= (-\mu_1^2 + \Lambda_1) \sin^2 \theta_a + (-\mu_2^2 + \Lambda_2) \cos^2 \theta_a + \Lambda_a \sin \theta_a \cos \theta_a\end{aligned}$$

where:

$$\Lambda_1 = \frac{1}{2}(\lambda_{31} + \lambda'_{31})v^2, \quad \Lambda_2 = \frac{1}{2}(\lambda_{23} + \lambda'_{23})v^2,$$

$$\Lambda_h = \mu_{12}^2 - \frac{1}{2}\lambda_3 v^2, \quad \Lambda_a = \mu_{12}^2 + \frac{1}{2}\lambda_3 v^2$$

$$\tan 2\theta_{h,a} = \frac{2\Lambda_{h,a}}{\mu_1^2 - \Lambda_1 - \mu_2^2 + \Lambda_2} \quad (1)$$

## Mass eigenstates: charged sector

$$\begin{aligned} m_{H_1^\pm}^2 &= (-\mu_1^2 + \Lambda'_1) \cos^2 \theta_c + (-\mu_2^2 + \Lambda'_2) \sin^2 \theta_c - 2\mu_{12}^2 \sin \theta_c \cos \theta_c \\ m_{H_2^\pm}^2 &= (-\mu_1^2 + \Lambda'_1) \sin^2 \theta_c + (-\mu_2^2 + \Lambda'_2) \cos^2 \theta_c + 2\mu_{12}^2 \sin \theta_a \cos \theta_a \end{aligned}$$

where:

$$\Lambda'_1 = \frac{1}{2} \lambda_{31} v^2, \quad \Lambda'_2 = \frac{1}{2} \lambda_{23} v^2 \tag{2}$$

$$\tan 2\theta_c = \frac{2\mu_{12}^2}{\mu_1^2 - \Lambda'_1 - \mu_2^2 + \Lambda'_2} \tag{3}$$

# Inert couplings

			Variational derivative of Lagrangian by fields
$h$	$H_1$	$H_1$	$-v((\lambda_{23} + \lambda'_{23})s_{\theta_c}^2 + (\lambda_{31} + \lambda'_{31})c_{\theta_h}^2 - 2\lambda_3 c_{\theta_h} s_{\theta_c})$
$h$	$H_1$	$H_2$	$v((\lambda_{23} + \lambda'_{23} + \lambda_{31} + \lambda'_{31})c_{\theta_c} s_{\theta_c} - \lambda_3 c_{2\theta_c})$
$h$	$H_2$	$H_2$	$-v((\lambda_{23} + \lambda'_{23})c_{\theta_c}^2 + (\lambda_{31} + \lambda'_{31})s_{\theta_h}^2 + 2\lambda_3 c_{\theta_h} s_{\theta_c})$
$A_1$	$A_1$	$H_1$	$-v(\lambda_1 c_{\theta_a} (c_{\theta_a} s_{\theta_c} - 2c_{\theta_h} s_{\theta_a}) - \lambda_2 s_{\theta_a} (s_{\theta_a} c_{\theta_h} - 2c_{\theta_a} s_{\theta_c}))$
$A_1$	$A_1$	$H_2$	$v(\lambda_1 c_{\theta_a} (c_{\theta_a} c_{\theta_h} + 2s_{\theta_a} s_{\theta_c}) + \lambda_2 s_{\theta_a} (s_{\theta_a} s_{\theta_c} + 2c_{\theta_a} c_{\theta_h}))$
$A_1$	$A_2$	$H_1$	$-v(\lambda_1 (c_{\theta_a} s_{\theta_a} s_{\theta_c} + c_{2\theta_a} c_{\theta_h}) + \lambda_2 (c_{\theta_a} s_{\theta_a} c_{\theta_h} - c_{2\theta_a} s_{\theta_c}))$
$A_1$	$A_2$	$H_2$	$v(\lambda_1 (c_{\theta_a} c_{\theta_h} s_{\theta_a} - c_{2\theta_a} s_{\theta_c}) - \lambda_2 (c_{\theta_a} s_{\theta_a} s_{\theta_c} + c_{2\theta_a} c_{\theta_h}))$
$A_2$	$A_2$	$H_1$	$-v(\lambda_1 s_{\theta_a} (s_{\theta_a} s_{\theta_c} + 2c_{\theta_a} c_{\theta_h}) - \lambda_2 c_{\theta_a} (c_{\theta_a} c_{\theta_h} + 2s_{\theta_a} s_{\theta_c}))$
$A_2$	$A_2$	$H_2$	$v(\lambda_1 s_{\theta_a} (s_{\theta_a} c_{\theta_h} - 2c_{\theta_a} s_{\theta_c}) + \lambda_2 c_{\theta_a} (c_{\theta_a} s_{\theta_c} - 2s_{\theta_a} c_{\theta_h}))$
$H_1$	$H_1$	$H_1$	$3v(\lambda_1 c_{\theta_h} - \lambda_2 s_{\theta_c})s_{\theta_c} c_{\theta_h}$
$H_1$	$H_1$	$H_2$	$-v(\lambda_1 c_{\theta_h} (1 - 3s_{\theta_c}^2) - \lambda_2 s_{\theta_c} (2 - 3s_{\theta_c}^2))$
$H_1$	$H_2$	$H_2$	$-v(\lambda_1 s_{\theta_c} (2 - 3s_{\theta_c}^2) + \lambda_2 c_{\theta_h} (1 - 3s_{\theta_c}^2))$
$H_2$	$H_2$	$H_2$	$-3v(\lambda_1 s_{\theta_c} + \lambda_2 c_{\theta_h})s_{\theta_c} c_{\theta_h}$

# Dark democracy limit

We assume

$$\mu_1^2 = n\mu_2^2, \quad \lambda_{31} = n\lambda_{23}, \quad \lambda'_{31} = n\lambda'_{23}, \quad \lambda_1 = n\lambda_2, \quad (4)$$

resulting in

$$\Lambda_1 = n\Lambda_2, \quad \Lambda'_1 = n\Lambda'_2. \quad (5)$$

The masses are then simplified to

$$\begin{aligned} m_{H_1}^2 &= (-\mu_2^2 + \Lambda_2)(n \cos^2 \theta_h + \sin^2 \theta_h) - \Lambda_h \sin \theta_h \cos \theta_h \\ m_{H_2}^2 &= (-\mu_2^2 + \Lambda_2)(n \sin^2 \theta_h + \cos^2 \theta_h) - \Lambda_h \sin \theta_h \cos \theta_h \end{aligned} \quad (6)$$

with the CP-even mixing angle given by

$$\tan 2\theta = \frac{-2\Lambda_h}{(n-1)(\Lambda_2 - \mu_2^2)}, \quad (7)$$

$m_{A_1}^2$ ,  $m_{A_2}^2$  and  $m_{H_1^\pm}^2$ ,  $m_{H_2^\pm}^2$ , have similar values with  $\Lambda_h$ ,  $\Lambda_2$  replaced by  $\Lambda_a$ ,  $\mu_{12}^2$ ,  $\Lambda'_2$  and  $\theta_a$ ,  $\theta_c$  respectively.

# Inert couplings · Dark democracy

			Variational derivative of Lagrangian by fields
$h$	$H_1$	$H_1$	$-v((\lambda_{23} + \lambda'_{23})(s_{\theta_c}^2 + nc_{\theta_c}^2) - 2\lambda_3 c_{\theta_h} s_{\theta_c})$
$h$	$H_1$	$H_2$	$v((\lambda_{23} + \lambda'_{23})(n+1)c_{\theta_c} s_{\theta_c} - \lambda_3 c_{2\theta_c})$
$h$	$H_2$	$H_2$	$-v((\lambda_{23} + \lambda'_{23})(ns_{\theta_c}^2 + c_{\theta_c}^2) + 2\lambda_3 c_{\theta_h} s_{\theta_c})$
$h$	$H_1^\pm$	$H_1^\mp$	$-v\lambda_{23}(s_{\theta_c}^2 + nc_{\theta_c}^2)$
$h$	$H_1^\pm$	$H_2^\mp$	$v\lambda_{23}(1-n)c_{\theta_c} s_{\theta_c}$
$h$	$H_2^\pm$	$H_2^\mp$	$-v\lambda_{23}(c_{\theta_c}^2 + ns_{\theta_c}^2)$
$A_1$	$A_1$	$H_1$	$-v\lambda_2(\lambda_1 c_{\theta_a}(c_{\theta_a} s_{\theta_c} - 2c_{\theta_h} s_{\theta_a}) - \lambda_2 s_{\theta_a}(s_{\theta_a} c_{\theta_h} - 2c_{\theta_a} s_{\theta_c}))$
$A_1$	$A_1$	$H_2$	$v(\lambda_1 c_{\theta_a}(c_{\theta_a} c_{\theta_h} + 2s_{\theta_a} s_{\theta_c}) + \lambda_2 s_{\theta_a}(s_{\theta_a} s_{\theta_c} + 2c_{\theta_a} c_{\theta_h}))$
$A_1$	$A_2$	$H_1$	$-v(\lambda_1(c_{\theta_a} s_{\theta_a} s_{\theta_c} + c_{2\theta_a} c_{\theta_h}) + \lambda_2(c_{\theta_a} s_{\theta_a} c_{\theta_h} - c_{2\theta_a} s_{\theta_c}))$
$A_1$	$A_2$	$H_2$	$v(\lambda_1(c_{\theta_a} c_{\theta_h} s_{\theta_a} - c_{2\theta_a} s_{\theta_c}) - \lambda_2(c_{\theta_a} s_{\theta_a} s_{\theta_c} + c_{2\theta_a} c_{\theta_h}))$
$A_2$	$A_2$	$H_1$	$-v(\lambda_1 s_{\theta_a}(s_{\theta_a} s_{\theta_c} + 2c_{\theta_a} c_{\theta_h}) - \lambda_2 c_{\theta_a}(c_{\theta_a} c_{\theta_h} + 2s_{\theta_a} s_{\theta_c}))$
$A_2$	$A_2$	$H_2$	$v(\lambda_1 s_{\theta_a}(s_{\theta_a} c_{\theta_h} - 2c_{\theta_a} s_{\theta_c}) + \lambda_2 c_{\theta_a}(c_{\theta_a} s_{\theta_c} - 2s_{\theta_a} c_{\theta_h}))$
$H_1$	$H_1$	$H_1$	$3v\lambda_2(nc_{\theta_h} - s_{\theta_c})s_{\theta_c}c_{\theta_h}$
$H_1$	$H_1$	$H_2$	$-v\lambda_2(nc_{\theta_h}(1 - 3s_{\theta_c}^2) - s_{\theta_c}(2 - 3s_{\theta_c}^2))$
$H_1$	$H_2$	$H_2$	$-v\lambda_2(ns_{\theta_c}(2 - 3s_{\theta_c}^2) + c_{\theta_h}(1 - 3s_{\theta_c}^2))$
$H_2$	$H_2$	$H_2$	$-3v\lambda_2(ns_{\theta_c} + c_{\theta_h})s_{\theta_c}c_{\theta_h}$

# The case $n = 1$

$$\text{If } n = 1, \quad \tan 2\theta \rightarrow \infty \quad \Rightarrow \quad \theta = \pm\pi/4$$

for  $\theta = \theta_h, \theta_a, \theta_c$ .

If we assume  $\theta_h = \theta_c = -\theta_a = -\pi/4$ :

$$\begin{aligned} m_{H_1}^2 &= \frac{1}{2}\nu^2(\lambda_{23} + \lambda'_{23} + \lambda_3) - \mu_{12}^2 - \mu_2^2 \\ m_{A_1}^2 &= \frac{1}{2}\nu^2(\lambda_{23} + \lambda'_{23} + \lambda_3) + \mu_{12}^2 - \mu_2^2 \\ m_{H_2}^2 &= \frac{1}{2}\nu^2(\lambda_{23} + \lambda'_{23} - \lambda_3) + \mu_{12}^2 - \mu_2^2 \\ m_{A_2}^2 &= \frac{1}{2}\nu^2(\lambda_{23} + \lambda'_{23} - \lambda_3) - \mu_{12}^2 - \mu_2^2 \\ m_{H_1^\pm}^2 &= \frac{1}{2}\nu^2\lambda_{23} - \mu_{12}^2 - \mu_2^2 \\ m_{H_2^\pm}^2 &= \frac{1}{2}\nu^2\lambda_{23} + \mu_{12}^2 - \mu_2^2 \end{aligned} \tag{8}$$

# Inert couplings · $n = 1$ case

Fields in the vertex	Variational derivative of Lagrangian by fields
$h H_1 H_1$	$-\nu(\lambda_{23} + \lambda'_{23} + \lambda_3)$
$\cancel{h} H_1 H_2$	0
$h H_2 H_2$	$-\nu(\lambda_{23} + \lambda'_{23} - \lambda_3)$
$A_1 A_1 H_1$	$-\frac{1}{\sqrt{2}}\nu\lambda_2$
$A_1 A_1 H_2$	0
$A_1 A_2 H_1$	0
$A_1 A_2 H_2$	$-\frac{1}{\sqrt{2}}\nu\lambda_2$
$A_2 A_2 H_1$	$\frac{3}{\sqrt{2}}\nu\lambda_2$
$A_2 A_2 H_2$	0
$H_1 H_1 H_1$	$-\frac{3}{\sqrt{2}}\nu\lambda_2$
$H_1 H_1 H_2$	0
$H_1 H_2 H_2$	$\frac{1}{\sqrt{2}}\nu\lambda_2$
$H_2 H_2 H_2$	0

Note that in this case  $hH_1H_2 \rightarrow 0$ , do we have two DM candidates in this case?

## Parameters in the $n = 1$ case

The following equations relate different parameters:

$$\begin{aligned}\mu_{12}^2 &= \frac{\Delta_+}{2}, & \lambda_{23} &= \frac{3\Delta_1 - \Delta_2}{v^2} + \lambda_3, \\ \lambda'_{23} &= -\frac{\Delta_1}{v^2} - \lambda_3, & \mu_2^2 &= -m_{H_1}^2 - \frac{2\Delta_+ - \Delta_0}{2} + \frac{v^2}{2}\lambda_3,\end{aligned}\quad (9)$$

with  $\Delta_i > 0$ , where:

$$\Delta_0 = m_{H_2}^2 - m_{H_1}^2, \quad \Delta_{1,2} = m_{H_{1,2}^\pm}^2 - m_{H_{1,2}}^2, \quad \Delta_+ = m_{H_2^\pm}^2 - m_{H_1^\pm}^2$$

And  $\lambda_3$  relate the DM-higgs couplings of the two sectors,

$$\lambda_3 = \frac{g_{hH_1H_1} - g_{hH_2H_2}}{2}, \quad (10)$$

where  $v g_{hH_iH_i}$  is the coefficient of the  $H_i H_i h$  term in the potential.  
Therefore, our input parameters are:  $m_{H_1}, m_{H_2}, m_{H_1^\pm}, m_{H_2^\pm}, \lambda_3$   
and also:  $\lambda_{11}, \lambda_{22}, \lambda_{12}, \lambda'_{12}, \lambda_2$ .

# Relic density

Three different processes can be identified that could impact the dark matter relic abundance of the two DM sectors:

- Semi-annihilation processes: These are (assuming  $m_{H_2} > m_{H_1}$ )  $S_2 S_2 \rightarrow h S_1$  ( $S = H, A$ ), and all of these vertices are proportional to  $\lambda_2$ .
- Partial DM conversion: These are  $S_2 S_2 \rightarrow S_2 S_1$  ( $S = H, A$ ), and all of these vertices are proportional to  $\lambda_{11} - \lambda_{22}$ .
- Total DM conversion: These are  $S_2 S_2 \rightarrow S_1 S_1$  ( $S = H, A$ ), and all of these vertices are proportional to  $(\lambda_{11} + \lambda_{22})$  and  $(\lambda_{12} + \lambda'_{12})$ .

In order to keep these processes under control we need small lambdas, most of all  $\lambda_2$  should be small to avoid the heavier DM candidate having a small relic density.

## Two possible benchmarks

A

B

$$m_{H_1} = 75$$

$$\lambda_{11} = 0.02$$

$$m_{H_2} = 205$$

$$\lambda_{22} = 0.01$$

$$m_{H_1^\pm} = 320$$

$$\lambda_{12} = 0.02$$

$$m_{H_2^\pm} = 360$$

$$\lambda'_{12} = 0.01$$

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$$m_{A_1} = 181.2$$

$$m_{A_2} = 74.6$$

$$\Omega_1 h^2 = 3.75 \times 10^{-2}$$

$$\Omega_2 h^2 = 7.67 \times 10^{-2}$$

$$m_{H_1} = 90$$

$$\lambda_{11} = 0.3$$

$$m_{H_2} = 120$$

$$\lambda_{22} = 0.3$$

$$m_{H_1^\pm} = 210$$

$$\lambda_{12} = 0.3$$

$$m_{H_2^\pm} = 225$$

$$\lambda'_{12} = 0.3$$

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$$m_{A_1} = 120.9$$

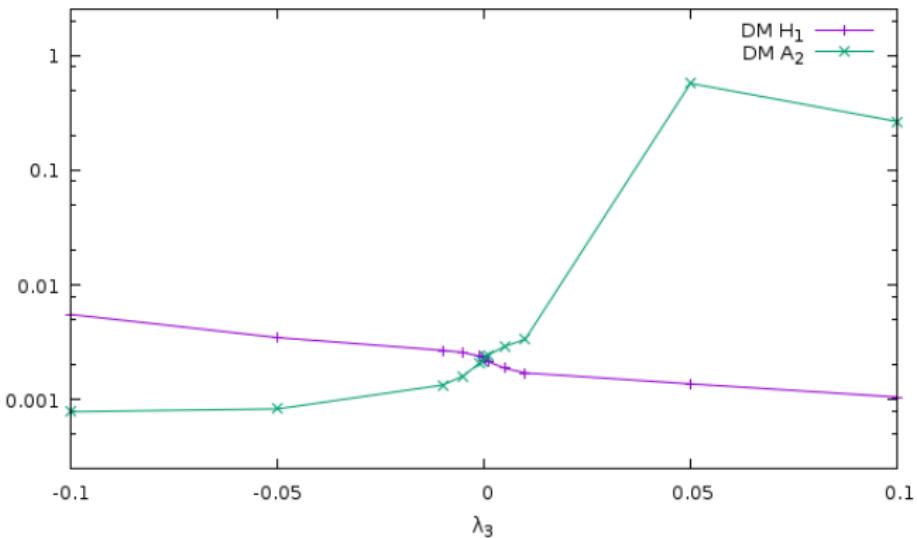
$$m_{A_2} = 160.6$$

$$\Omega_1 h^2 = 0.125$$

$$\Omega_2 h^2 = 2.51 \times 10^{-4}$$

Masses in GeV,  $\lambda_2 = 0.0001$

# A test plot



In this plot we take the values from scenario B and change the value of  $\lambda_3$ . Note that for  $\lambda_3 < 0 \rightarrow m_{A_2} > m_{H_1}$  and for  $\lambda_3 > 0 \rightarrow m_{A_2} < m_{H_1}$



# Testing inert interacions

We can see how the relic density depends on the lambdas by fixing the masses<sup>2</sup>.

- Test 1: All lambdas equal to zero. Then, both DM sectors are completely independent.

$$\Omega_1 h^2 = 1.62 \times 10^{-4}, \quad \Omega_2 h^2 = 4.90 \times 10^{-4}.$$

- Test 2:  $\lambda_{11} = \lambda_{22} = \lambda_{12} = \lambda'_{12} = 0.1$ ,  $\lambda_2 = 0$ . Then, only total DM conversion processes are present.

$$\Omega_1 h^2 = 1.63 \times 10^{-4}, \quad \Omega_2 h^2 = 5.29 \times 10^{-4}.$$

- Test 3:  $\lambda_{11} = -\lambda_{22} = 0.1$ ,  $\lambda_{12} = \lambda'_{12} = \lambda_2 = 0$ . Then, only partial DM conversion processes are present.

$$\Omega_1 h^2 = 1.28 \times 10^{-4}, \quad \Omega_2 h^2 = 2.24 \times 10^{-10}.$$

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<sup>2</sup>We assumed:  $m_{H_1} = m_{A_1} = 100\text{GeV}$ ,  $m_{H_2} = m_{A_2} = 200\text{GeV}$ ,  
 $m_{H_1^\pm} = m_{H_2^\pm} = 400\text{GeV}$

- Test 4:  $\lambda_{11} = 2\lambda_{22} = 0.2$ ,  $\lambda_{12} = \lambda'_{12} = 0.1$ ,  $\lambda_2 = 0$ . Then, all DM conversion processes are present, but no semi-annihilation.

$$\Omega_1 h^2 = 1.28 \times 10^{-4}, \quad \Omega_2 h^2 = 3.15 \times 10^{-9}.$$

- Test 5:  $\lambda_{11} = \lambda_{22} = \lambda_{12} = \lambda'_{12} = 0$ ,  $\lambda_2 = 0.25$ . Then, semi-annihilation processes are present, but no DM conversion.

$$\Omega_1 h^2 = 4.69 \times 10^{-6}, \quad \Omega_2 h^2 = 2.46 \times 10^{-11}.$$

- Test 6: All lambdas different from zero:  
 $\lambda_{11} = 2\lambda_{22} = \lambda_{12} = 2\lambda'_{12} = 0.2$ ,  $\lambda_2 = 0.25$ . Now all these interactions are present.

$$\Omega_1 h^2 = 4.70 \times 10^{-6}, \quad \Omega_2 h^2 = 2.20 \times 10^{-11}.$$

- Now with  $\lambda_2 = 0.025$ :

$$\Omega_1 h^2 = 1.01 \times 10^{-4}, \quad \Omega_2 h^2 = 2.52 \times 10^{-9}.$$

# What's next?

- Study DM phenomenology
- Constraints on parameters
- Direct and indirect DM detection
- Comparation with  $Z_2$  model
- Colliders signatures: LHC and ILC

Thank you for your attention!