



# Emergence of collectivity near a critical point

Maximilian Attems

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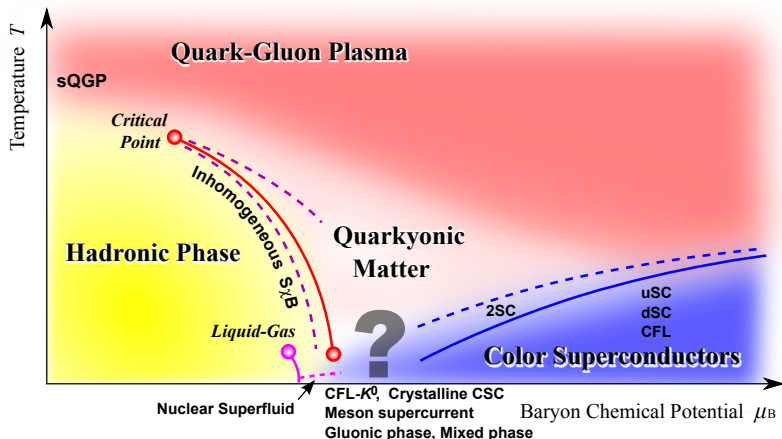
Collaborators:

Yago Bea (UB), Jorge Casalderrey-Solana (Oxford, UB),  
David Mateos (UB), Miguel Zilhao (CENTRA)

2nd joint workshop IGFAE/LIP

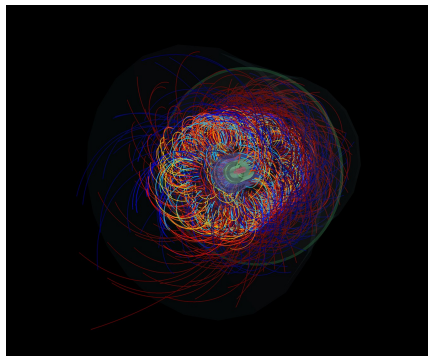
# Motivation I - QCD phase diagram

RHIC and FAIR colliders search for the critical point, the endpoint of the phase transition between QGP and Hadrons:



Crucial to probe dynamical properties of a critical point  
[Fukushima, Hatsudo 2010]

## Quark-Gluon Plasma:



LHC reconstructed event from the first heavy ion collisions [ALICE 2010]

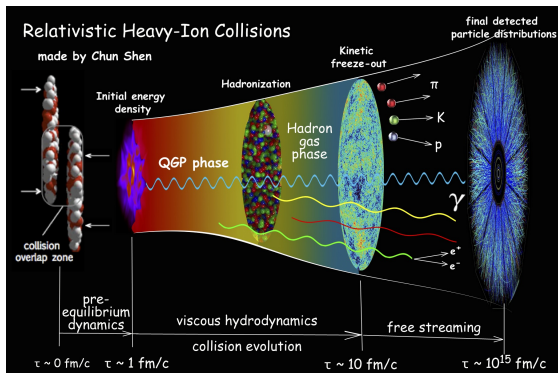
## Black Holes:



First Black Hole image (M87) [Event Horizon Telescope Collaboration 2019]

**gauge/gravity** correspondence:  
bridge between physical phenomena in gauge theories and gravity.

# Introduction Heavy-Ion collision - the 'little bang'



Stages of HI collision:

- 1) Out of equilibrium
- 2) Quark-Gluon Plasma
- 3) Hot Hadron Gas

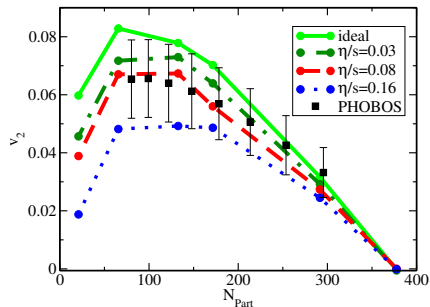
How can we describe the first stage at strong coupling?

How long is the first stage? LHC Data indicates  $\leq 10^{-23}$  s

What determines when hydro becomes applicable?

What are the initial conditions for the Quark-Gluon-Plasma?

> 10y success of viscous hydrodynamics



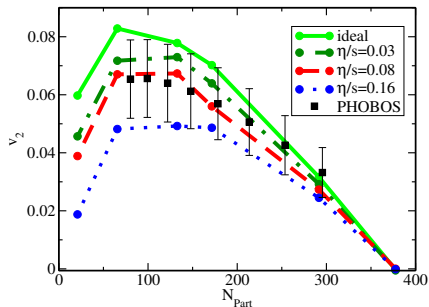
shear viscosity over entropy

density ratio  $\eta/s \approx 0.08$

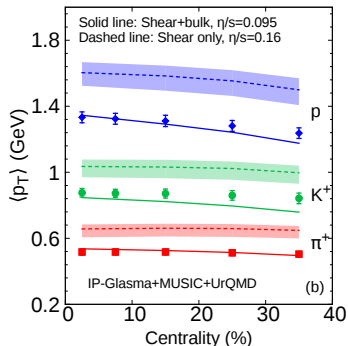
→ nearly perfect fluid

[Romatschke 2007]

> 10y success of viscous hydrodynamics

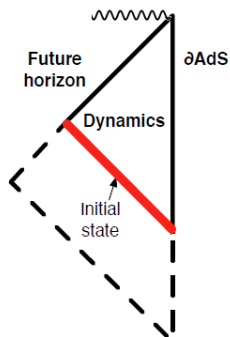


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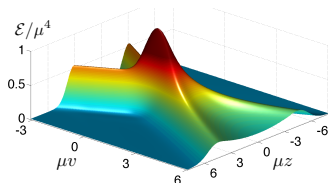
Hydro simulation agreement  
improves with bulk viscosity  $\zeta$   
[Denicol *et al.* 2015]

# Out-of-equilibrium challenges



Strong coupling toolkit for out of equilibrium dynamics:

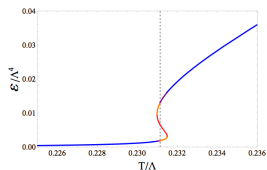
**Fast hydrodynamization** with first shockwave collisions in the characteristic formulation  $t_{\text{hyd}} < 10^{-23}$  although very anisotropic  $\frac{P_T}{P_L}|_{t_{\text{hyd}}} \gg 1$  at hydrodynamization [Chesler, Yaffe 2011]



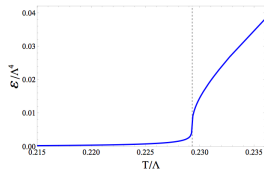
**EoSization**: seen in first non-conformal temperature scan new non-conformal relaxation time scale (= when ideal equation of state applies) [MA et al. 2016/2017]

# Collisions near a critical point

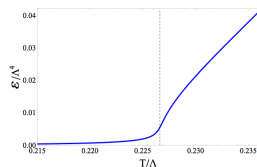
1st order:



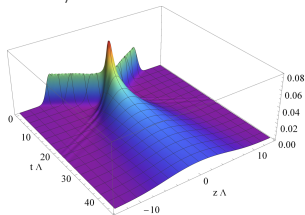
2nd order:



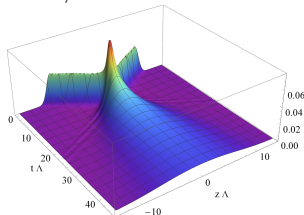
crossover:



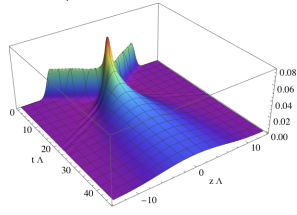
$10^2 \mathcal{E}/\Lambda^4$



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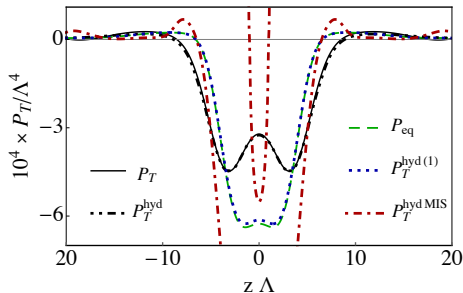
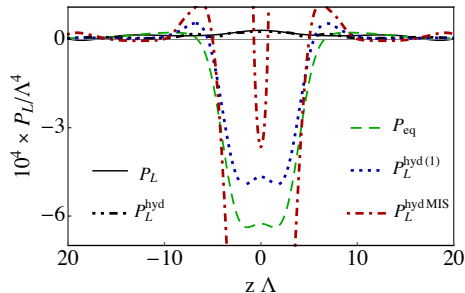
$10^2 \mathcal{E}/\Lambda^4$



Discovers long-lived, quasi-static blob of energy at mid-rapidity, with slow down of the dynamics, no remnants [MA et al. 2018]



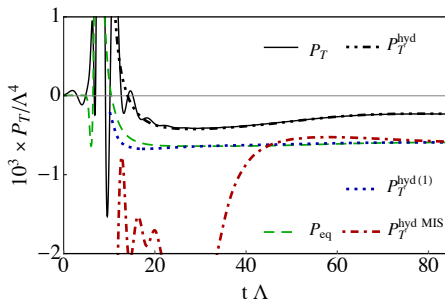
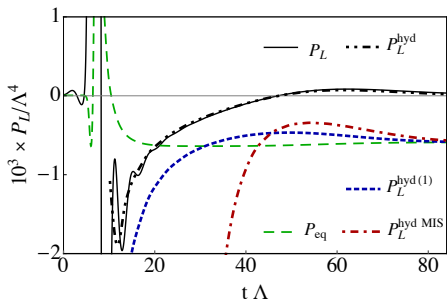
Müller-Israel-Stewart-type hydrodynamics fails to describe the pressure evolution at mid rapidity in the formed blob ( $t\Lambda = 50$ ):



Well described by the constitutive relations of second-order hydrodynamics that include all spatial second-order gradients.

# Pressure evolution near a critical point

Differences to QCD: no dynamical baryon charge density, no conserved order parameter, fluctuations  $1/N_c^2$  suppressed  
Similarities to QCD: vanishing speed of sound, large bulk viscosity



Need of a new causal hydrodynamics formulation near CP with suppressed first order gradients, but large second-order purely spatial gradients.

- New example of the **applicability of hydrodynamics** to systems with large gradients in energy densities - even in non-trivial phase structure
- **First simulation** of holographic heavy-ion collisions near a critical point
- Fluid slows down near CP to a long-lived, quasi-static blob
- **MIS hydrodynamics** fails near a critical-point
  - missing 2nd order spacial derivatives
- More studies on the way: spinodal instability, baryonic matter