
Flavour Physics

lecture 2

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Useful resources & acknowledgments

- Heavy Flavour Averaging Group (HFLAV) <https://hflav.web.cern.ch>
- CKMfitter ckmfitter.in2p3.fr Ufit www.utfit.org/UTfit/
- Particle Data Group reviews pdg.lbl.gov
- Books:
 - CP violation, I.I. Bigi and A.I. Sanda (CUP, 2000)
 - CP violation, G.C. Branco, L. Lavoura & J.P.Silva (OUP, 1999)
- Reviews & lectures:
 - M. Blanke, [arXiv:1704.03753](https://arxiv.org/abs/1704.03753)
 - O. Gedalia & G. Perez, [arXiv:1005.3106](https://arxiv.org/abs/1005.3106)
 - Y. Grossman & P. Tanedo, [arXiv:1711.03624](https://arxiv.org/abs/1711.03624)
 - J.F. Kamenik, [arXiv:1708.00771](https://arxiv.org/abs/1708.00771)
 - Z. Ligeti, [arXiv:1502.01372](https://arxiv.org/abs/1502.01372)
 - Y. Nir, [arXiv:0708.1872](https://arxiv.org/abs/0708.1872), [arXiv:1605.00433](https://arxiv.org/abs/1605.00433)

Thanks to flavour lecturers at this school in previous years, who provided inspiration for some of the material shown (esp. T. Gerson, J. Zupan & M-H. Schune).

Lecture outline

- Introduction ✓
- Birth of flavour physics & the kaon sector ✓
- The beautiful millennium ✓
- Flavour structure of the SM ✓
- The Unitarity Triangle and CPV measurements - topic begun
- Spectroscopy (a brief digression)
- FCNCs or 'rare decays'
- Charm physics
- Future of flavour

Note the approach will (necessarily) be from an experimentalist's perspective.

CKM matrix expressed in Wolfenstein parametrisation

[Wolfenstein, PRL 51, 1945]

From last time

In the Wolfenstein parameterisation the matrix is expanded in orders of $\lambda \sim 0.23$.

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

This is expanded to λ^3 , which will be adequate for most of our subsequent discussion, but not all...

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

V_{ub} and V_{td} are the only complex elements (at this order) \rightarrow special role in CPV

'The' Unitarity Triangle

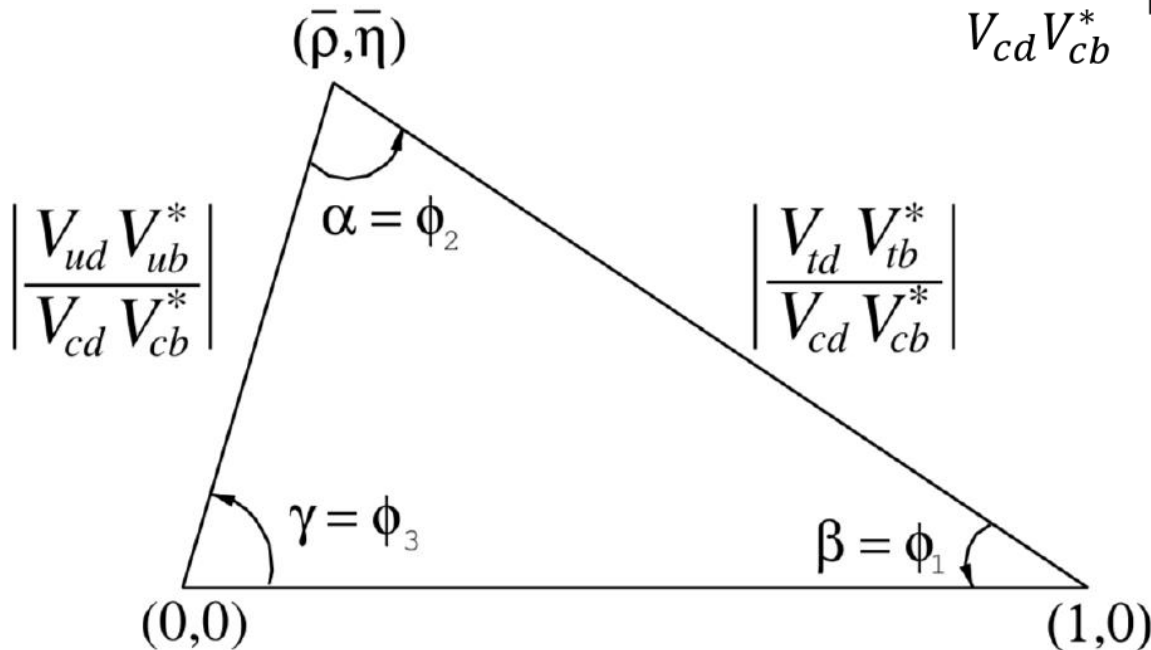
From last time

Three complex vectors sum to zero

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

→ triangle in Argand plane

$$\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + 1 + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0$$



Expressions for angles:

$$\alpha = \arg \left[-\frac{V_{td}V_{tb}^*}{V_{ub}V_{cb}^*} \right]$$

$$\beta = \arg \left[-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right]$$

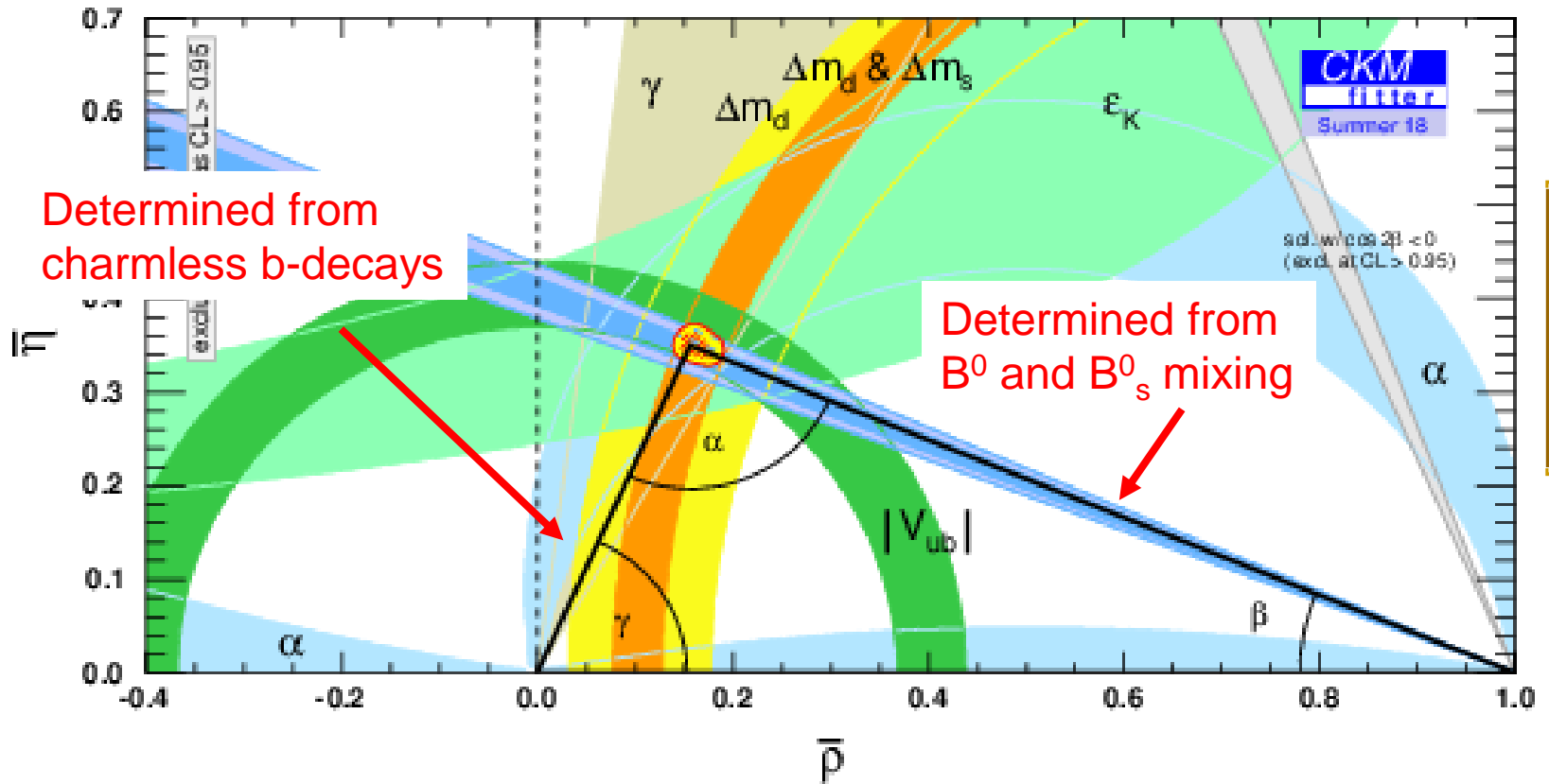
$$\gamma = \arg \left[-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right]$$

Upper vertex: $\bar{\rho} + i\bar{\eta} = -(V_{ud}V_{ub}^*)/(V_{cd}V_{cb}^*)$

$\bar{\rho} = \rho(1 - \lambda^2/2 + \dots)$ $\bar{\eta} = \eta(1 - \lambda^2/2 + \dots)$ (ϕ_2, ϕ_1 & ϕ_3 alternative notation)

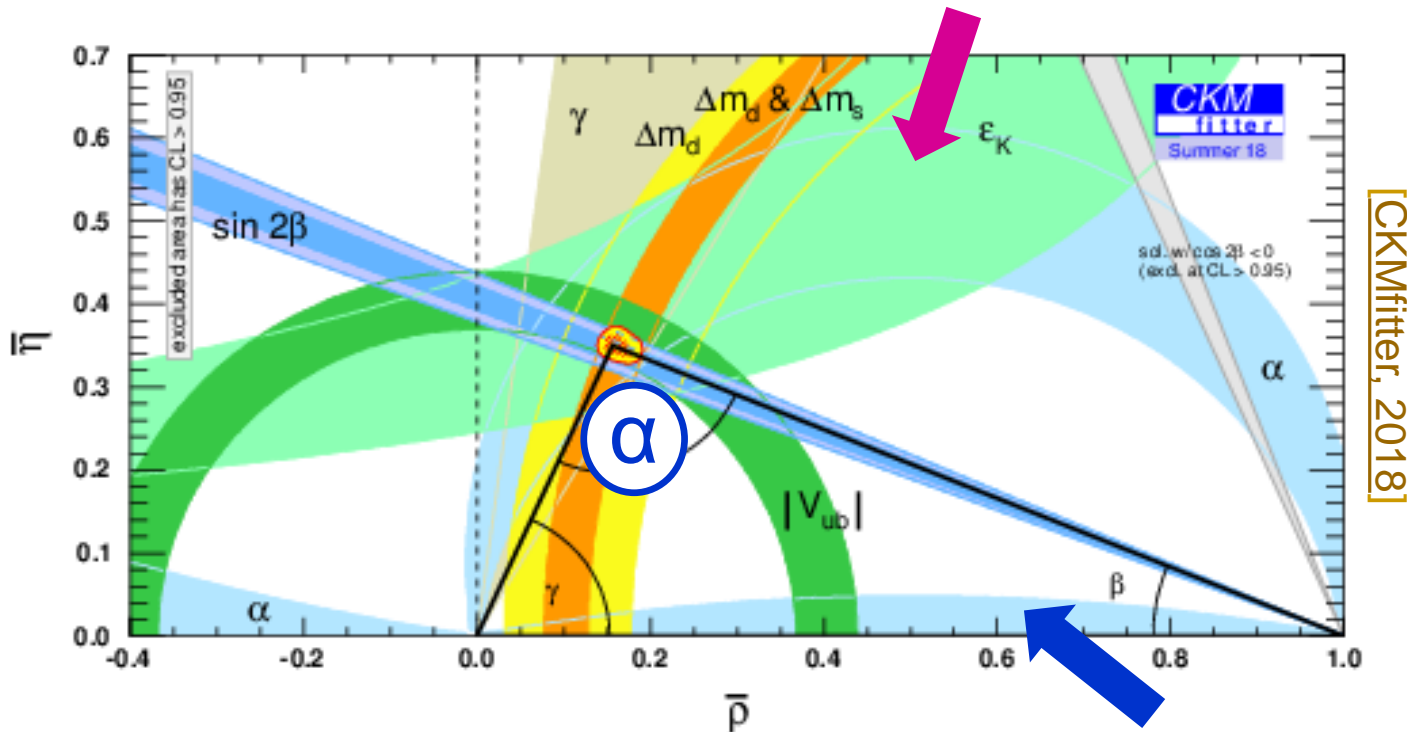
The Unitarity Triangle – how do we know what we know ?

From last time



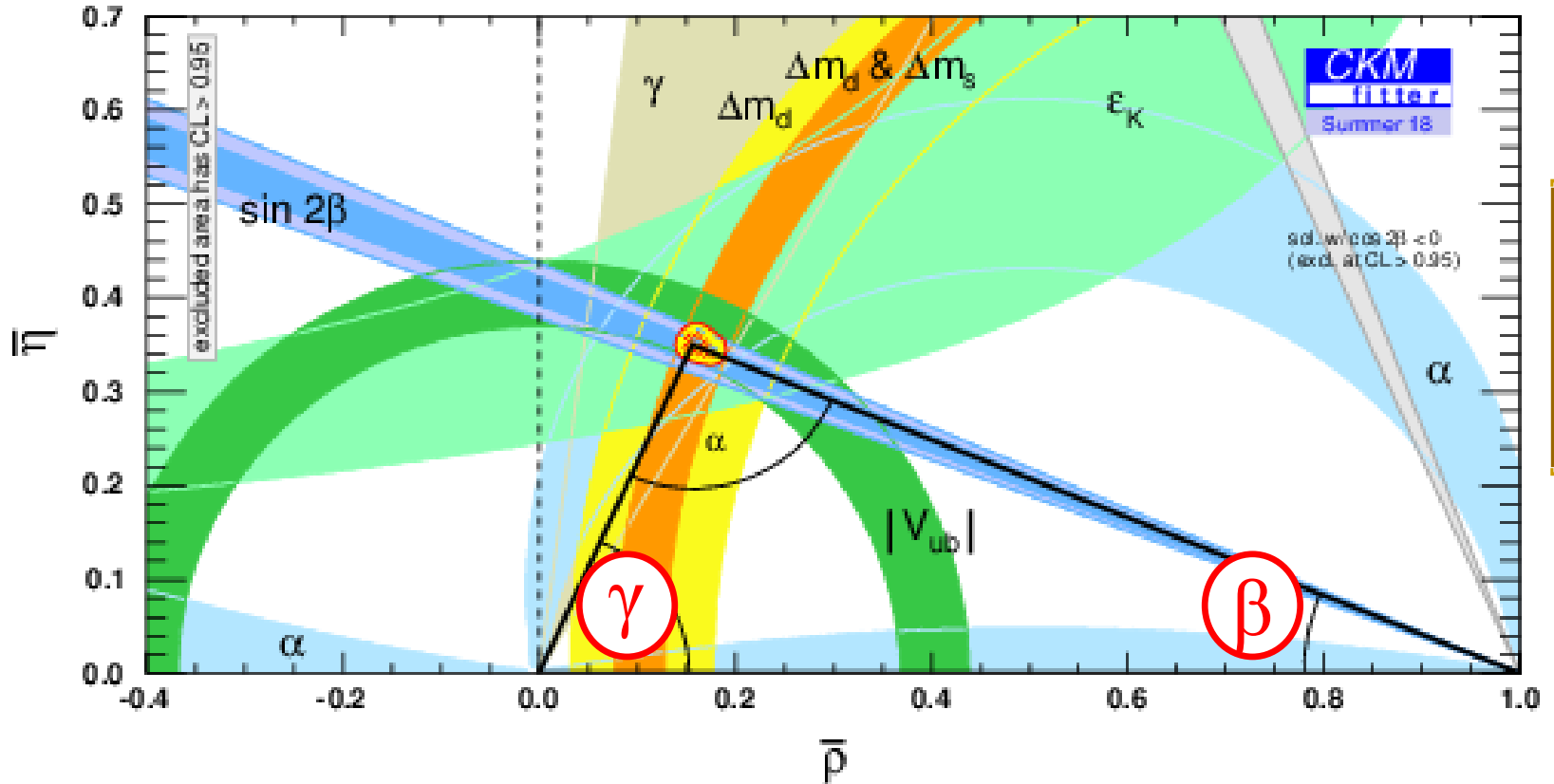
The Unitarity Triangle – how do we know what we know ?

This band comes from CPV measurements in kaon decays. Theory limited.



Information on α comes from time-dependent measurements on B^0 decays to charmless final states, e.g. $B \rightarrow \rho^+ \rho^-$. It probes a combination of the processes that occur in the β and γ measurements, and IMO does not bring independent info, & we will not discuss it further. (But of course any measurement is valuable!)

The Unitarity Triangle – how do we know what we know ?



Now we will discuss the CPV measurements that access the angles β and γ .

Decays into CP eigenstates: $B^0 \rightarrow J/\psi K_S$

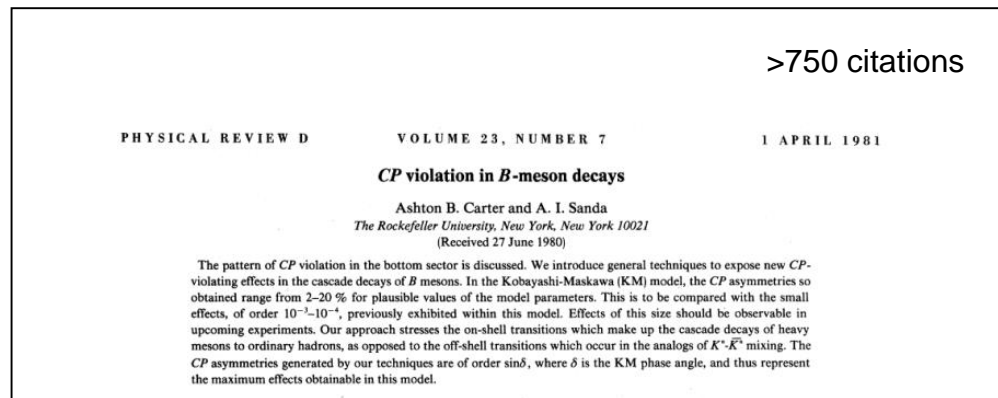
Potential for clean measurement of substantial CPV in B system first appreciated in early 1980s: [Carter and Sanda, [PRD 23 \(1981\) 1567](#)], [Bigi and Sanda, [NPB 193 \(1981\) 85](#)].

Incidentally, someone who was amongst the first to realise the potential of b-hadrons in CPV studies, and one responsible for a seminal paper, has since followed a very different career...

Obama-era U.S. defense secretary toasts the latest CP-violation results from LHCb



*



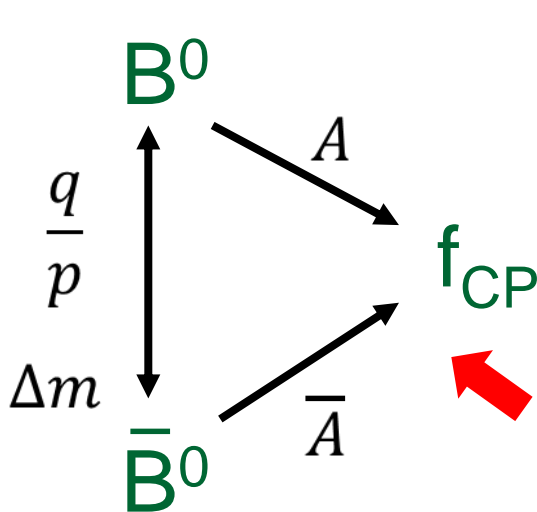
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$$\Gamma(B_{phys}^0 \rightarrow f_{CP}(t)) \propto e^{-\Gamma t} (1 - (S \sin(\Delta m t) - C \cos(\Delta m t))) \quad *$$

$$\Gamma(\bar{B}_{phys}^0 \rightarrow f_{CP}(t)) \propto e^{-\Gamma t} (1 + (S \sin(\Delta m t) - C \cos(\Delta m t)))$$



$$S = \frac{2 \Im(\lambda_{CP})}{1 + |\lambda_{CP}^2|} \quad C = \frac{1 - |\lambda_{CP}^2|}{1 + |\lambda_{CP}^2|} \quad \lambda_{CP} = \frac{q}{p} \frac{\bar{A}}{A}$$

Key point: to observe a complex phase we need to have two (or more) interfering amplitudes, as here

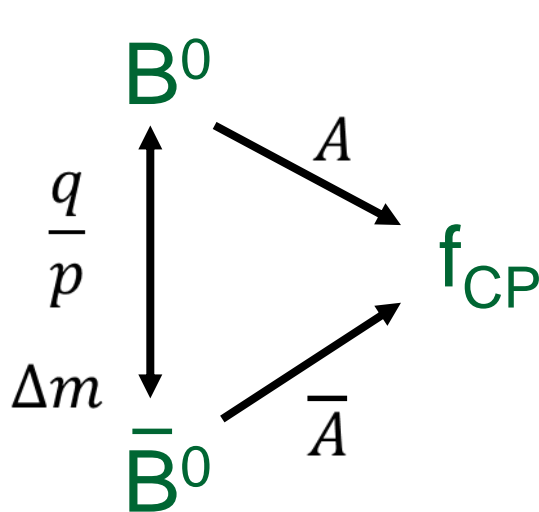
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There are three ways that CP violation can appear:

CPV in the decay (or 'direct CPV').

(This is also the only possibility that applies for charged hadron decays.)

$$|A| \neq |\bar{A}|$$

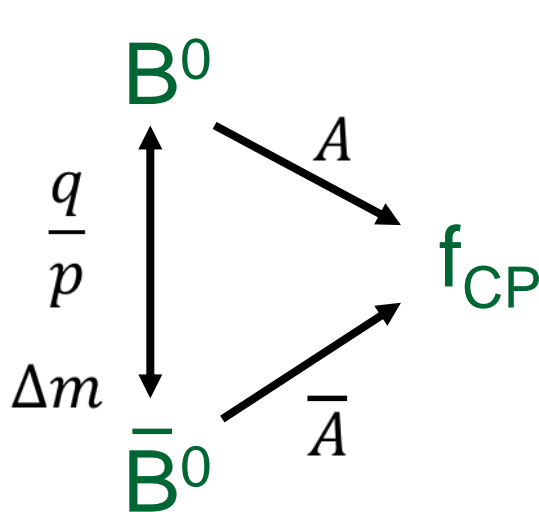
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There are three ways that CP violation can appear:

CPV in the mixing (one category of so-called 'indirect CPV').

Occurs if there are different ways to oscillate $B^0 \leftrightarrow B^0$ bar. In SM very small.

$$\left| \frac{q}{p} \right| \neq 1$$

* These expressions assumes width-splitting $\Delta\Gamma=0$, which is an excellent approximation in B^0 system.

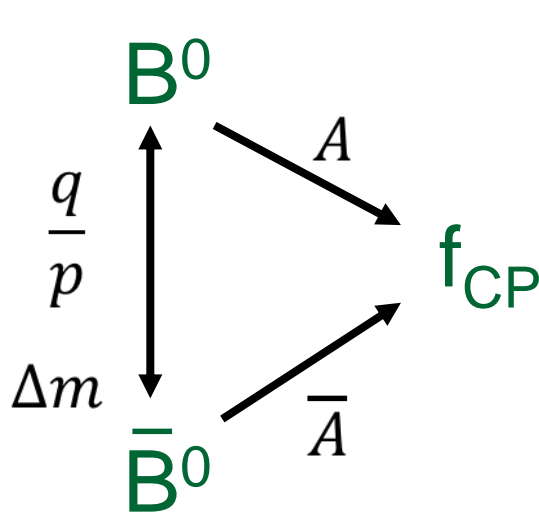
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There are three ways that CP violation can appear:

CPV in mixing-decay interference (also a category of 'indirect CPV', & the most relevant in the $B^0 B^0$ bar and $B_s^0 B_s^0$ bar systems).

$\text{Im} \lambda_{CP} \neq 0$

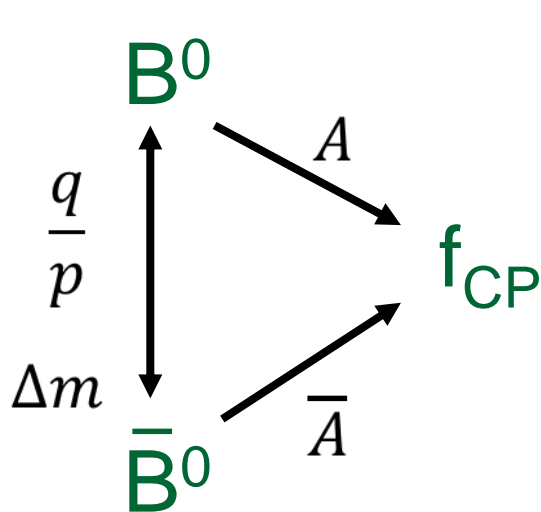
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Consider the classic case $B^0 \rightarrow J/\psi K_S$:

- Compared to the CPV signal we are expecting in B physics, we can treat K_S as a CP eigenstate.
- And in this decay $C \approx 0$, with no significant direct CPV (all the CPV comes from *mixing-decay interference*).

NB both these assumptions can be checked / corrected for.

Decays into CP eigenstates: $B^0 \rightarrow J/\psi K_S$

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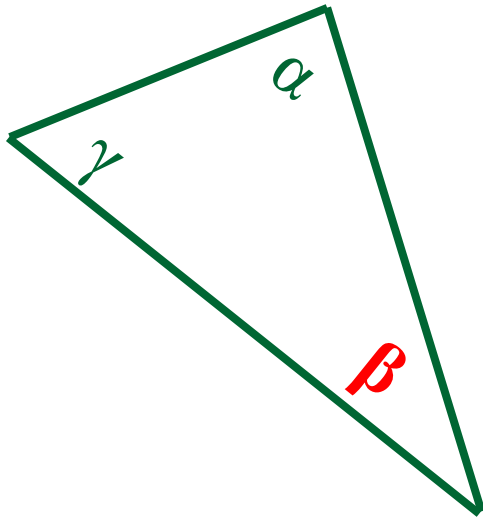
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Consider the classic case $B^0 \rightarrow J/\psi K_S$:

$$\lambda_{J/\psi K_S} = \frac{V_{tb}^* V_{td} V_{cb} V_{cs}^*}{V_{tb} V_{td}^* V_{cb}^* V_{cs}} = e^{i2\beta} \quad \text{Im } \lambda_{J/\psi K_S} = \sin 2\beta$$



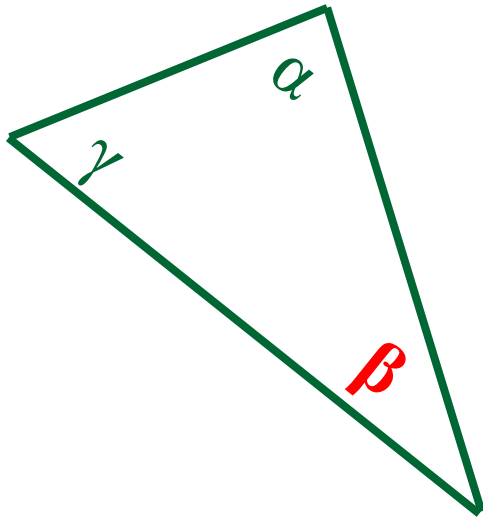
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In practice we measure a t -dependent CP asymmetry:

$$\begin{aligned} a_{CP}(t) &\equiv \frac{\Gamma(\bar{B}_s^0(t) \rightarrow J/\psi K_S^0) - \Gamma(B_s^0(t) \rightarrow J/\psi K_S^0)}{\Gamma(\bar{B}_s^0(t) \rightarrow J/\psi K_S^0) + \Gamma(B_s^0(t) \rightarrow J/\psi K_S^0)} \\ &= \sin 2\beta \sin(\Delta m t) \end{aligned}$$

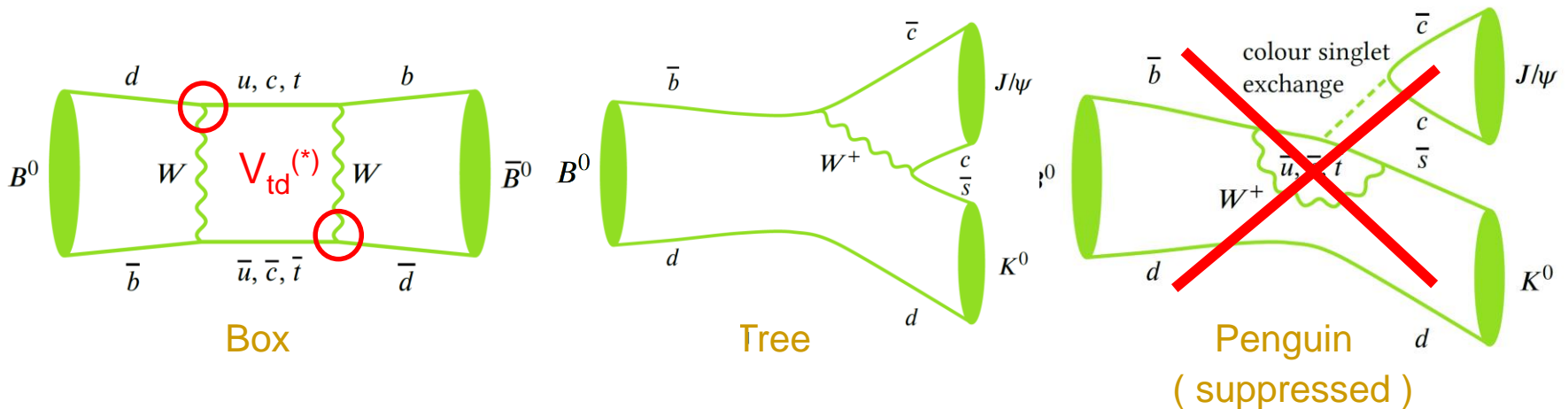
This is theoretically **clean!**
(no QCD murkiness)

* These expressions assume width-splitting $\Delta\Gamma=0$, which is an excellent approximation in B^0 system.

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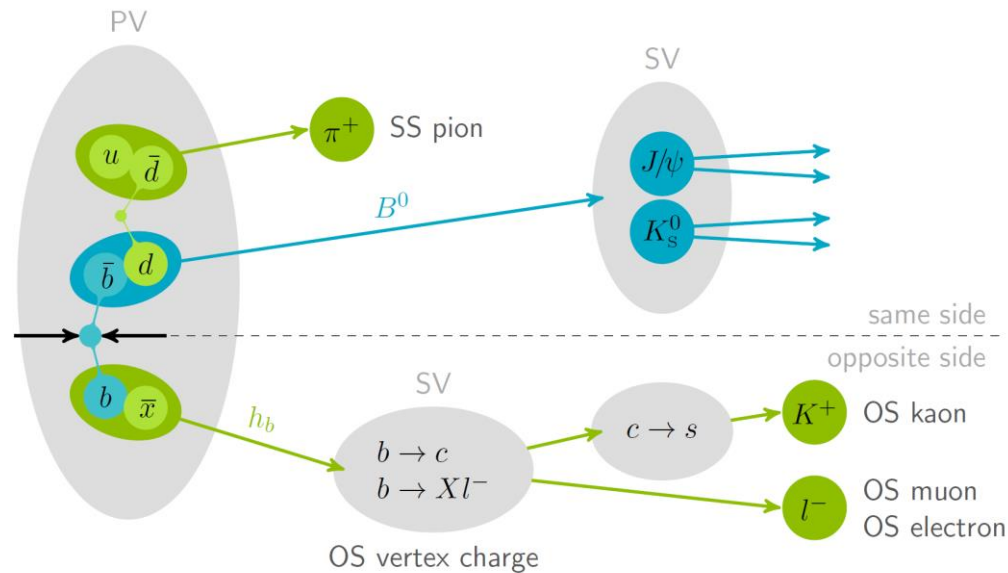
To reiterate, measurement probes interference between box and tree diagrams:



Sensitive to any CP violating phases in either, but these are only expected in the box. In the SM come from phase-difference associated with V_{td} coupling, but could arise from other sources in New Physics. So possible $\sin 2\beta_{\text{meas}} \neq \sin 2\beta_{\text{SM}}$!

Flavour tagging & other practical considerations

Measurement demands we know whether decaying meson was B^0 or B^0 bar at birth. This requires *flavour tagging* *. Look at either decay products of the other b-hadron ('opposite sign') or for fragmentation products associated with signal B ('same sign').



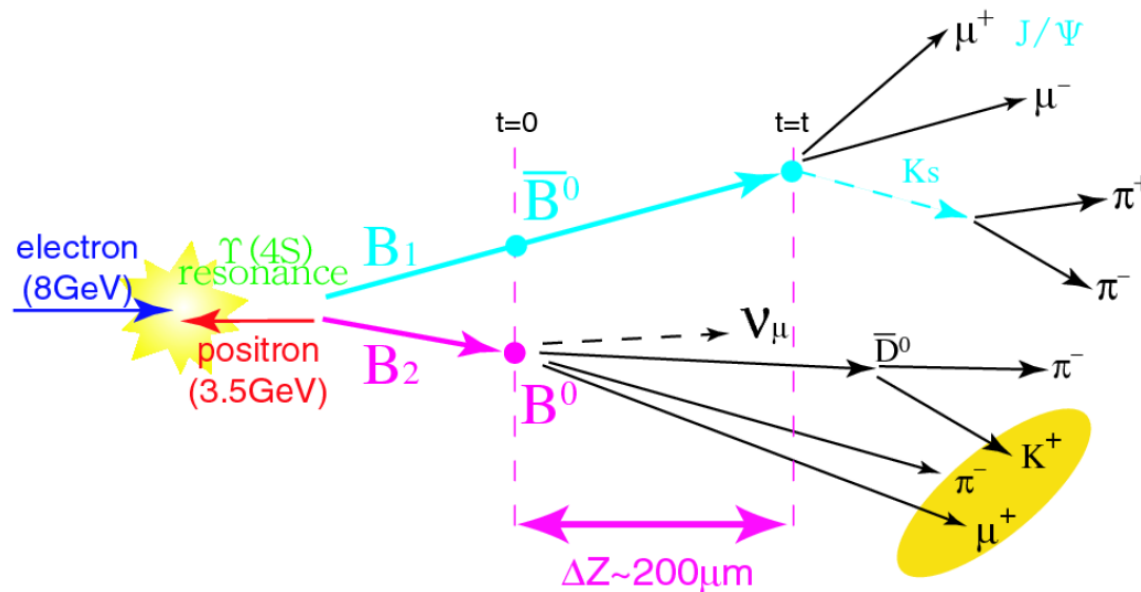
Flavour tag decision can be wrong, either through misidentification or mixing of OS b-hadron. This leads to *dilution* of asymmetry, and reduces effective signal statistics by a large factor (up to $\times \sim 1/30$) at hadron collider experiments.

For t variable in asymmetry, we need to know proper time between birth & death of signal B, which at LHC is related to distance between primary and decay vertices.

* NB in high- p_T physics the term 'flavour tagging' means something different, typically 'is this jet b-like or c-like?'.

Flavour tagging & other practical considerations

Life is easier for BaBar/Belle and Belle-II Life at the $\Upsilon(4S)$ means no fragmentation particles and production of coherent B^0 - \bar{B}^0 system \rightarrow (i) No same sign tag (bad), (ii) many fewer mistags (very good), (iii) no mixing until one B decays (very good).



The dilution is less than at LHC, and reduces effective signal statistics by only $\sim 1/3$.

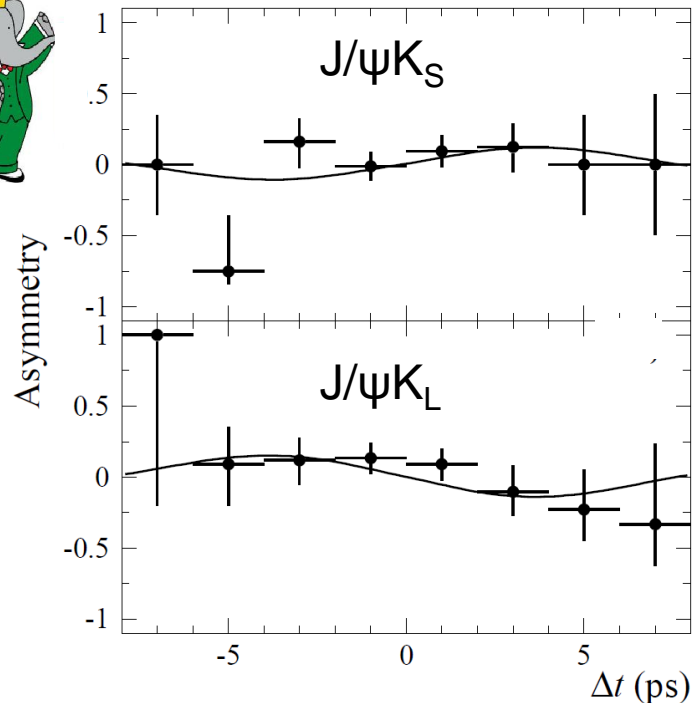
Why do B-factories have asymmetric beam energies? For coherent system what matters is the time-difference Δt between the two B decays. At the $\Upsilon(4S)$ the mesons are produced at rest, & so it is necessary to *boost* system to measure Δt .

2001 - dawn of modern flavour physics

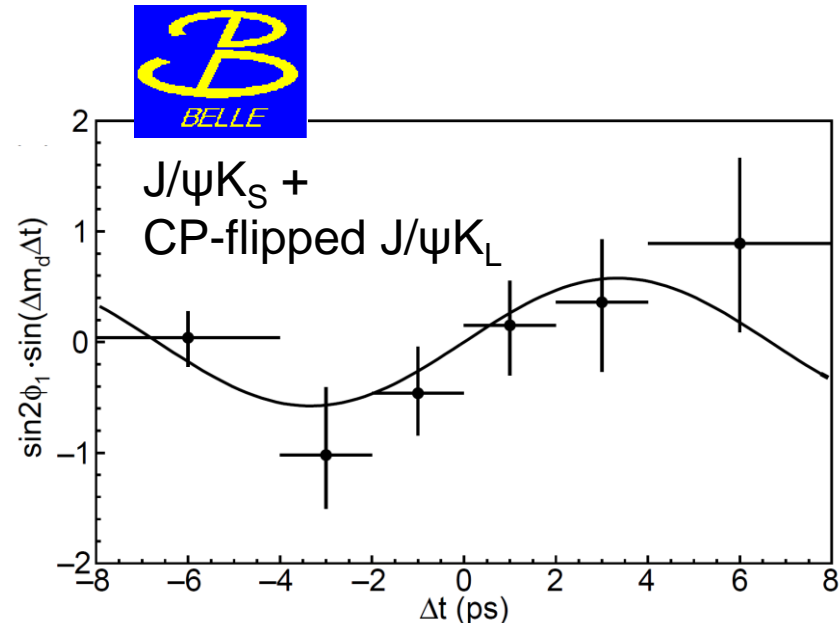
2008
Nobel
Prize



We can date the start of modern flavour physics to the 2001 measurements of the CP-violating asymmetry in $B^0 \rightarrow J/\psi K^0$ decays that give unitarity triangle angle β .



[BaBar, [PRL 86 \(2001\) 2515](#)]



[Belle, [PRL 86 \(2001\) 2509](#)]

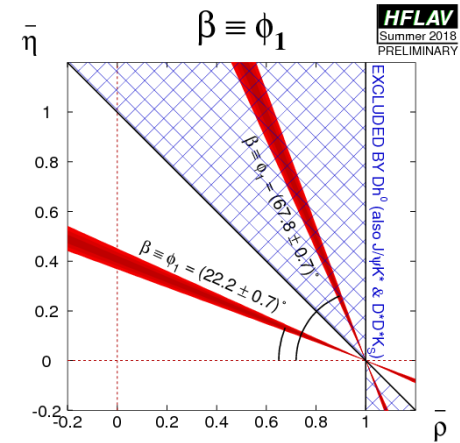
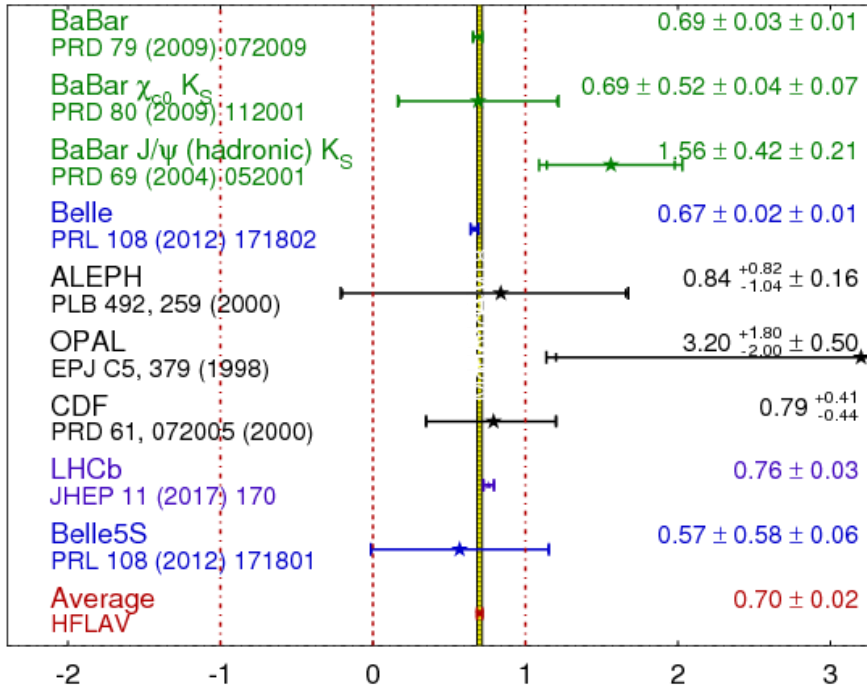
These studies, when improved with larger samples, confirmed the CKM paradigm as the dominant mechanism of CP violation in nature (\rightarrow 2008 Nobel Prize), and also opened up a rich and wide spectrum of complementary measurements.

sin2β: current status and impact of the LHC

Global state of play:

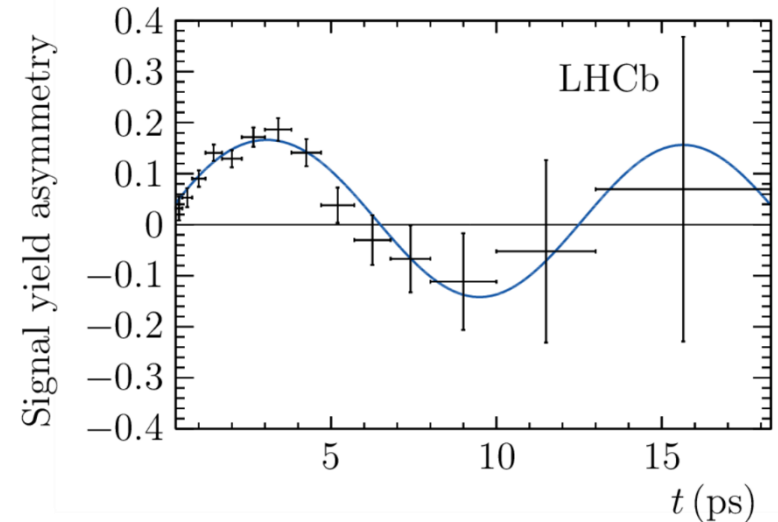
$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFLAV
Moriond 2018
PRELIMINARY



Both solutions for β shown in UT plane. →

LHCb run 1 $J/\psi K_S$ result has similar precision to B factories

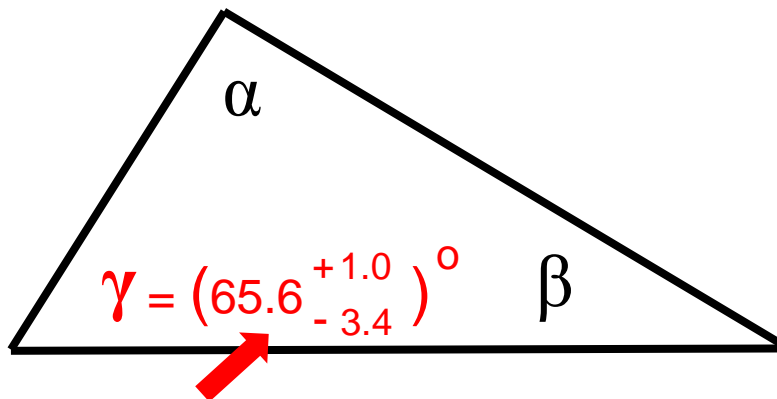


[LHCb, PRL 115 (2015) 031601]

sin2β now known to 3%, with significant improvements expected in coming decade

The long march: towards a precise determination of the UT angle γ

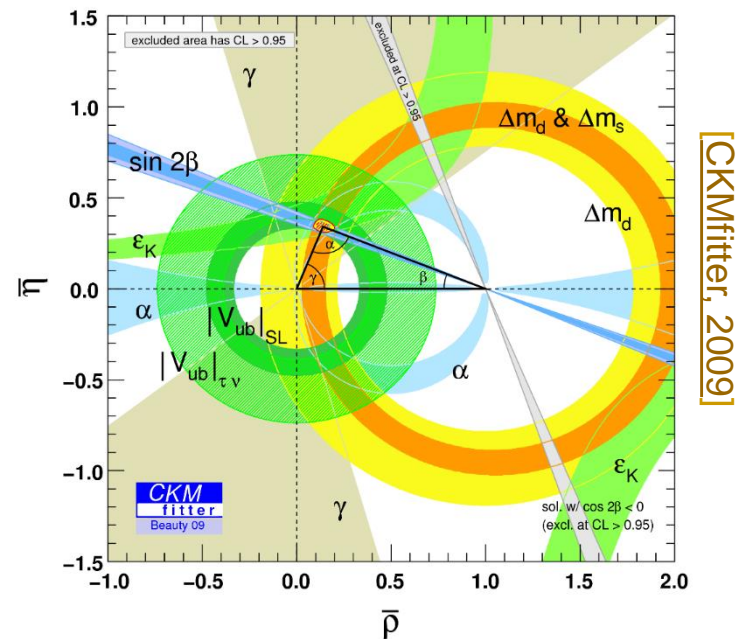
A particular responsibility for flavour physics at the LHC (& Belle II) is to improve our knowledge of the angle γ .



The predicted value of γ in context of SM is known very well from other triangle parameters (& will be known even better as experiment & lattice QCD improve).

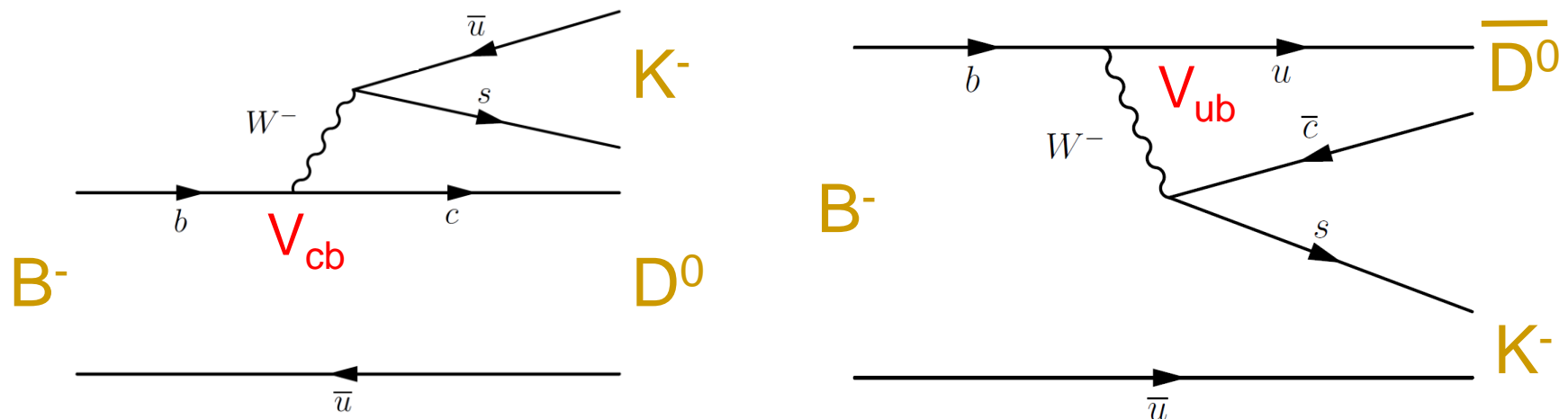
A key task of flavour physics is to match this precision in a direct measurement !

At LHC turn-on γ uncertainty was $>20^\circ$.



The long march: towards a precise determination of the UT angle γ

This angle is special – it can be measured at tree-level through $B \rightarrow DK$ decays.



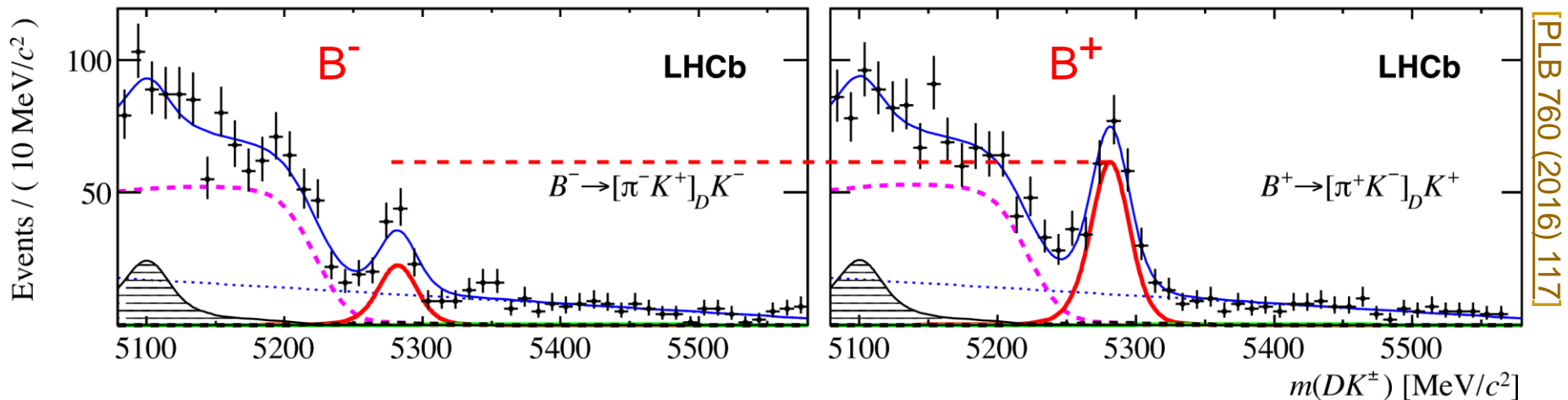
If we reconstruct D^0 and \bar{D}^0 in a state accessible to both, Interference occurs & decay rates become sensitive to relative phase between V_{cb} and V_{ub} , which is γ .

There are QCD nuisance parameters involved, but sufficient observables can be measured to determine these without any assumption. Theoretically ultra clean !

Tree level means New Physics unlikely to perturb measured value from the γ of the SM (*c.f.* β), hence measurement provides 'SM benchmark' for other tests !

The Unitarity Triangle: measuring γ

To access these interference effects means looking for rather suppressed decays, e.g. this $B^- \rightarrow DK^-$ decay, with $D \rightarrow K^+\pi^-$ (and B^+ conjugate case): visible BR $\sim 10^{-8}$. Hence out of reach to previous generation of flavour physics experiments.

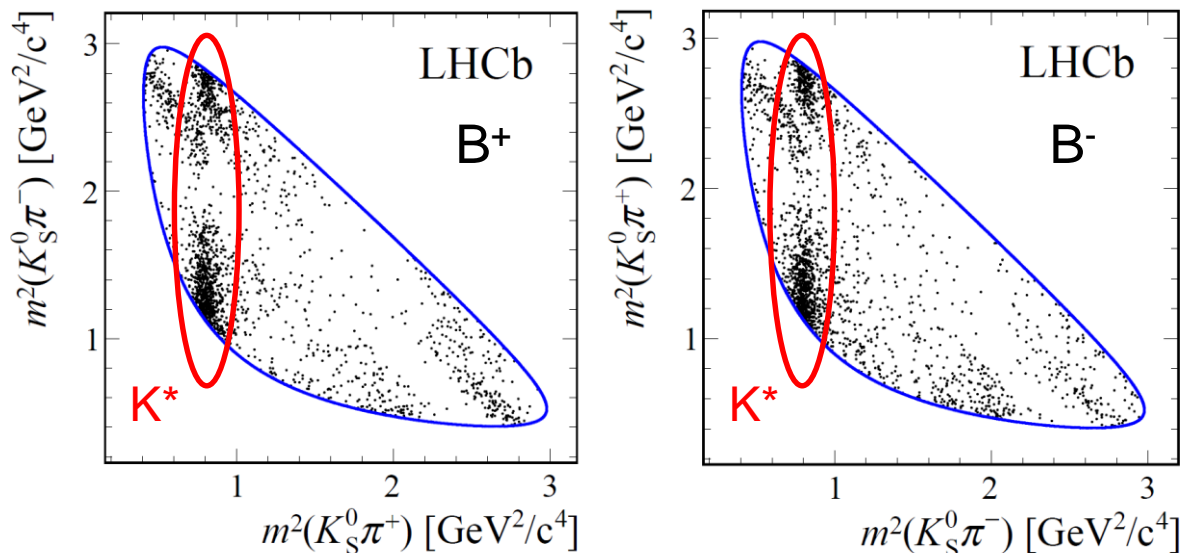


Very significant CP violation observed, that can be cleanly related to the phase γ .

γ measurement at LHCb with $B \rightarrow DK$ decays: $D \rightarrow K_S \pi \pi$ (and $K_S KK$) with Run 2 data [JHEP 08 (2018) 176]

A powerful sub-set of $B \rightarrow DK$ analyses is when the D decays into a multibody final state, of which $K_S \pi \pi$ is the most prominent example. Variation of D strong phase over Dalitz space leads to corresponding variation in interference and CP violation.

Analysis of ~ 3000 decays from 2 fb^{-1} of early Run 2 data.



A *Dalitz plot* is a 2D display of phase space for a three-body decay, where bands manifest intermediate resonances, and their spin structure

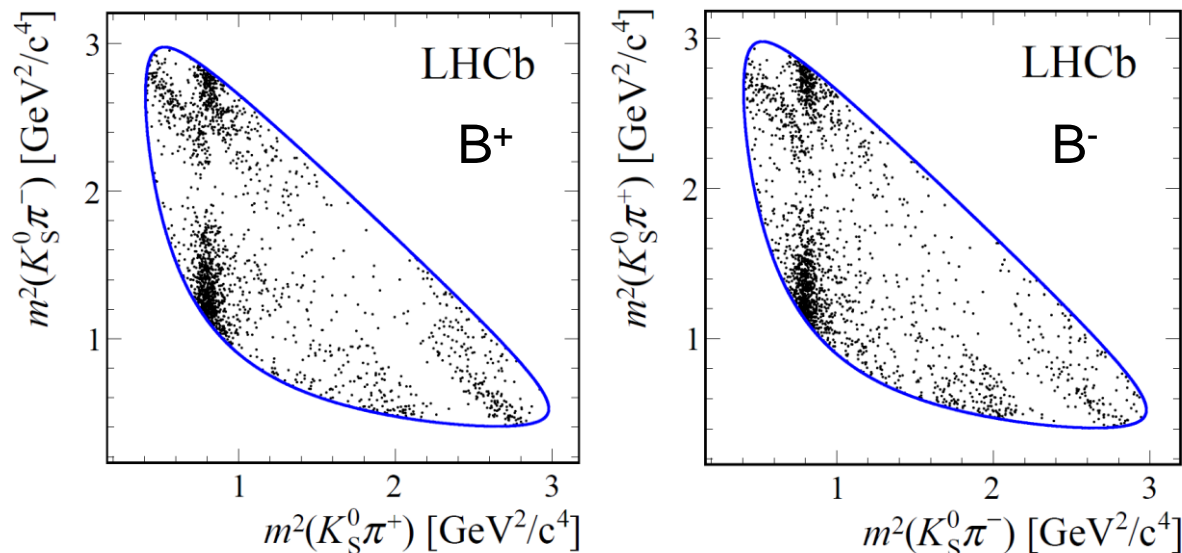
e.g. $D \rightarrow K^*(892)\pi$

These are the Dalitz plots of the $D \rightarrow K_S \pi \pi$ decays arising from the $B \rightarrow DK$ decays.

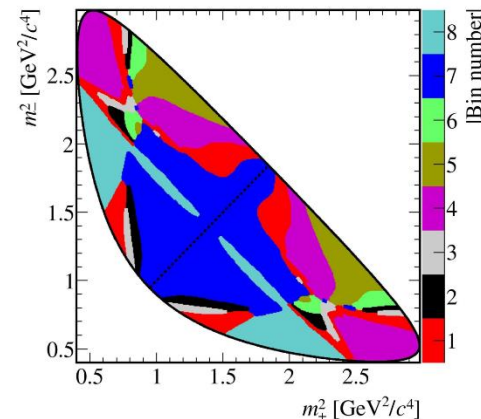
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Study yields in *bins* of Dalitz space, chosen for optimal sensitivity.

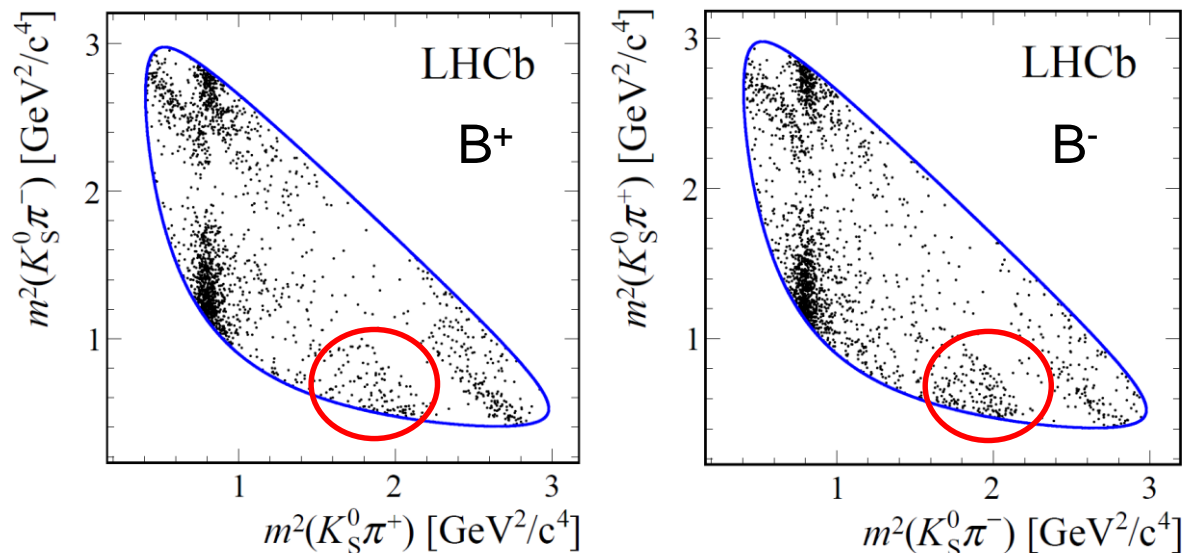


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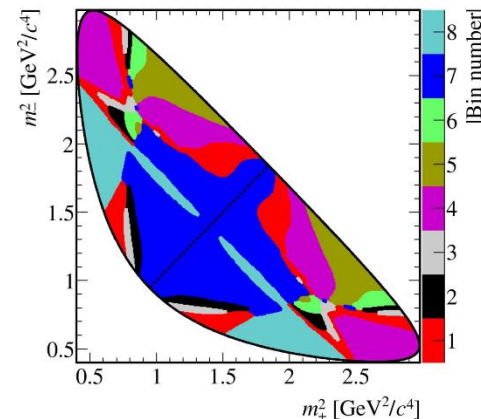
γ measurement at LHCb with $B \rightarrow DK$ decays: $D \rightarrow K_S \pi \pi$ (and $K_S KK$) with Run 2 data [\[JHEP 08 \(2018\) 176\]](#)

A powerful sub-set of $B \rightarrow DK$ analyses is when the D decays into a multibody final state, of which $K_S \pi \pi$ is the most prominent example. Variation of D strong phase over Dalitz space leads to corresponding variation in interference and CP violation.

Analysis of ~ 3000 decays from 2 fb^{-1} of early Run 2 data.



Study yields in *bins* of Dalitz space, chosen for optimal sensitivity.

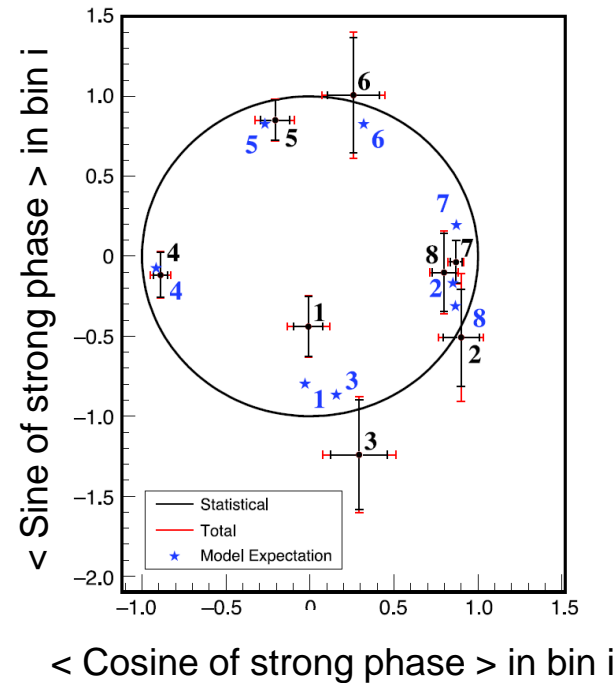
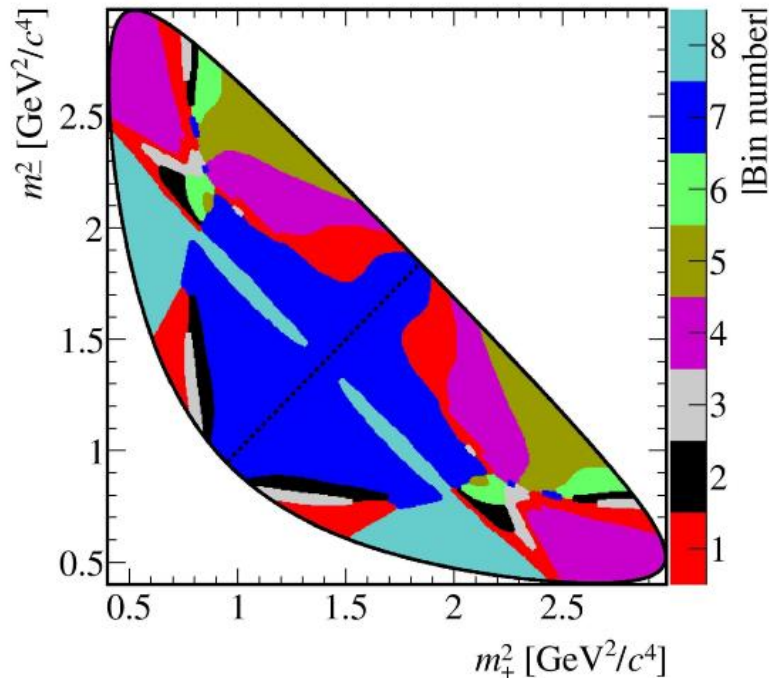


CP asymmetries visible by eye, but quantitative analysis requires external input...

Measuring γ – a synergy of experiments

In order to make sense of these CP asymmetries, we need to know how the CP-conserving strong phase between D & Dbar varies over the Dalitz plot.

This information can be measured in bins on the Dalitz plot from quantum-correlated $\psi(3770) \rightarrow D\bar{D}$ events, available at CLEO-c [[PRD 82 \(2010\) 112006](#)].



CLEO-c data adequate for current LHCb sample sizes.

LHCb Upgrade data & Belle II will require improved measurements from BES III !

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These strong-phase measurements are an excellent example of synergy between HEP facilities !



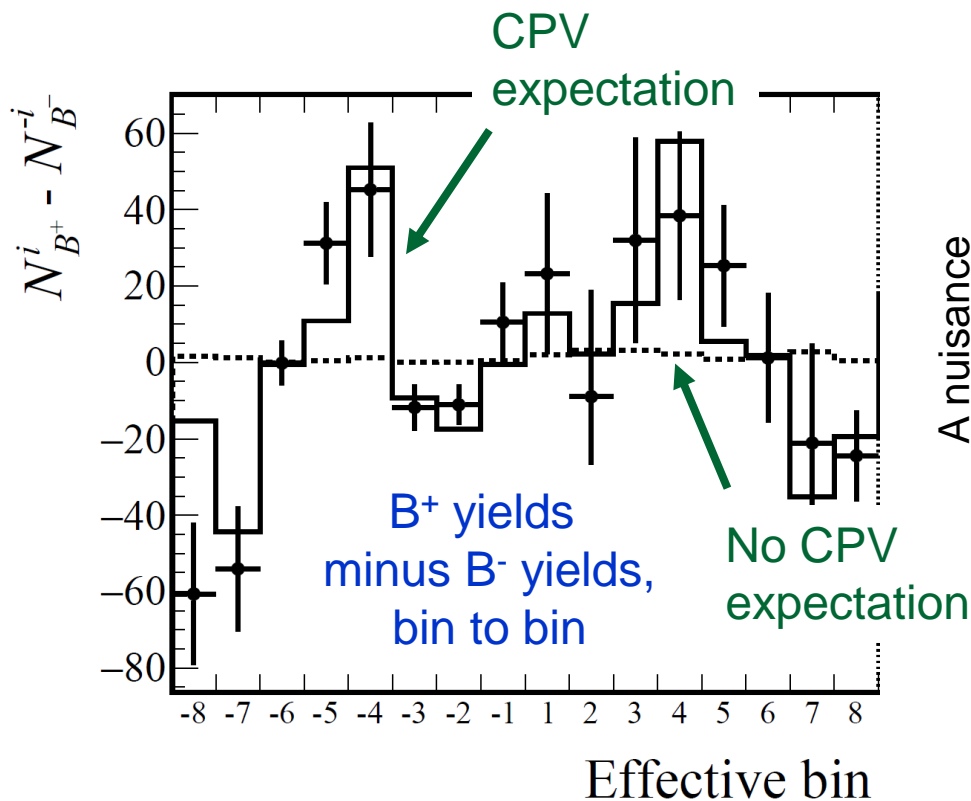
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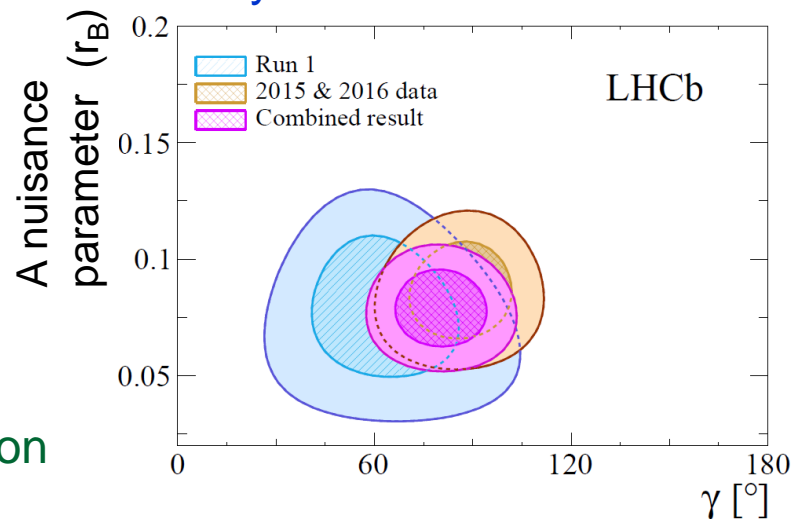
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A powerful sub-set of $B \rightarrow DK$ analyses is when the D decays into a multibody final state, of which $K_S \pi \pi$ is the most prominent example. Variation of D strong phase over Dalitz space leads to corresponding variation in interference and CP violation.



Compatible with Run 1 analysis of same channel

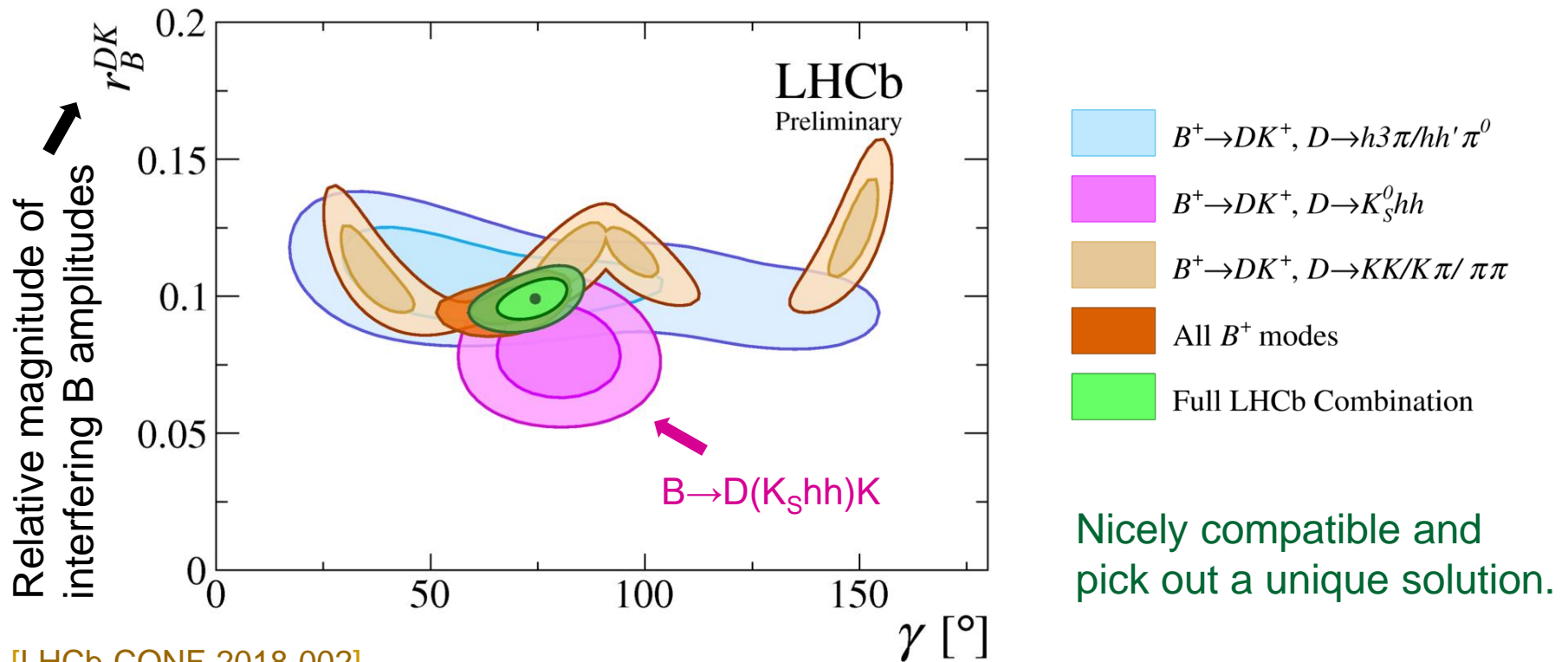


Together gives:

$$\gamma = 80^\circ \pm 10^\circ_{-9^\circ}$$

LHCb: combining $B \rightarrow DK$ modes for γ

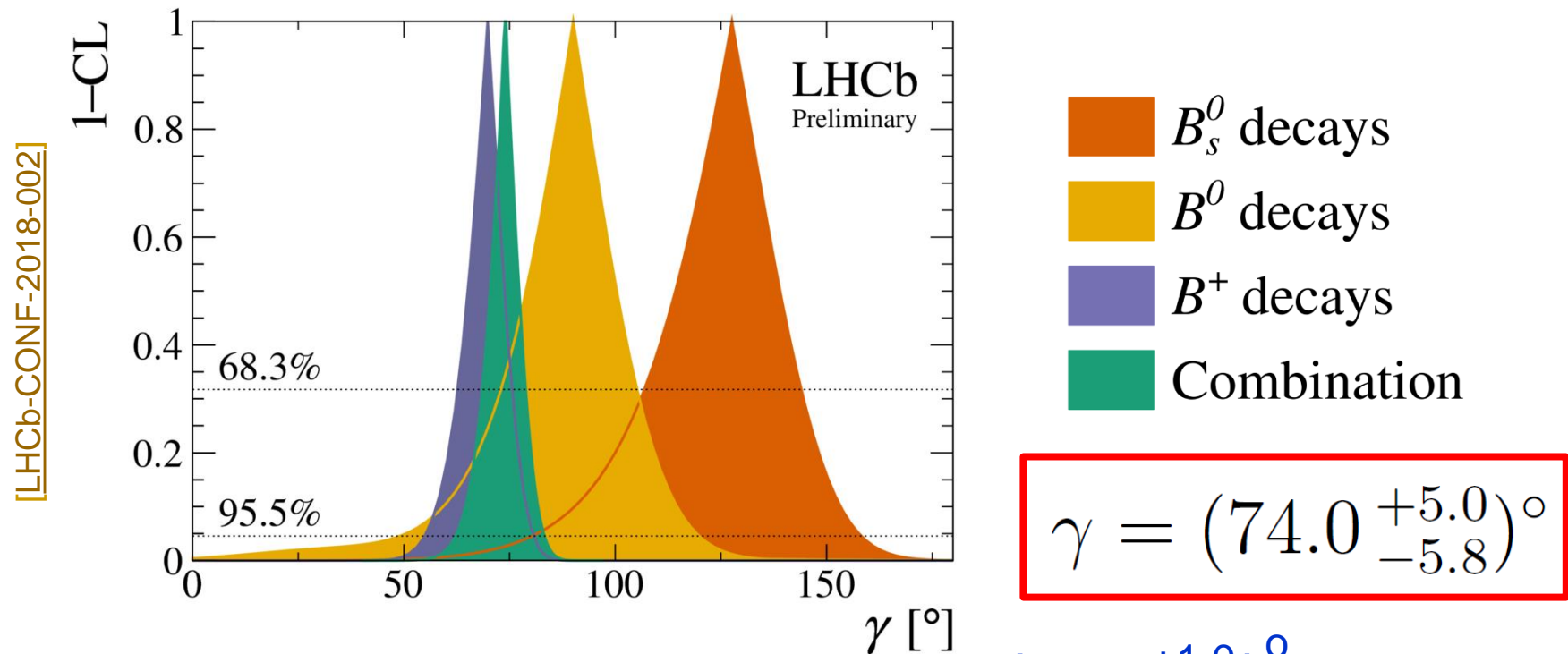
The $B \rightarrow D(K_S \pi \pi, K_S K K) K$ result may be combined together with those of other $B \rightarrow DK$ analyses. They depend on common nuisance parameters, but have difference degeneracies \rightarrow whole is greater than the sum of the parts !



[LHCb-CONF-2018-002]

LHCb: current precision on γ

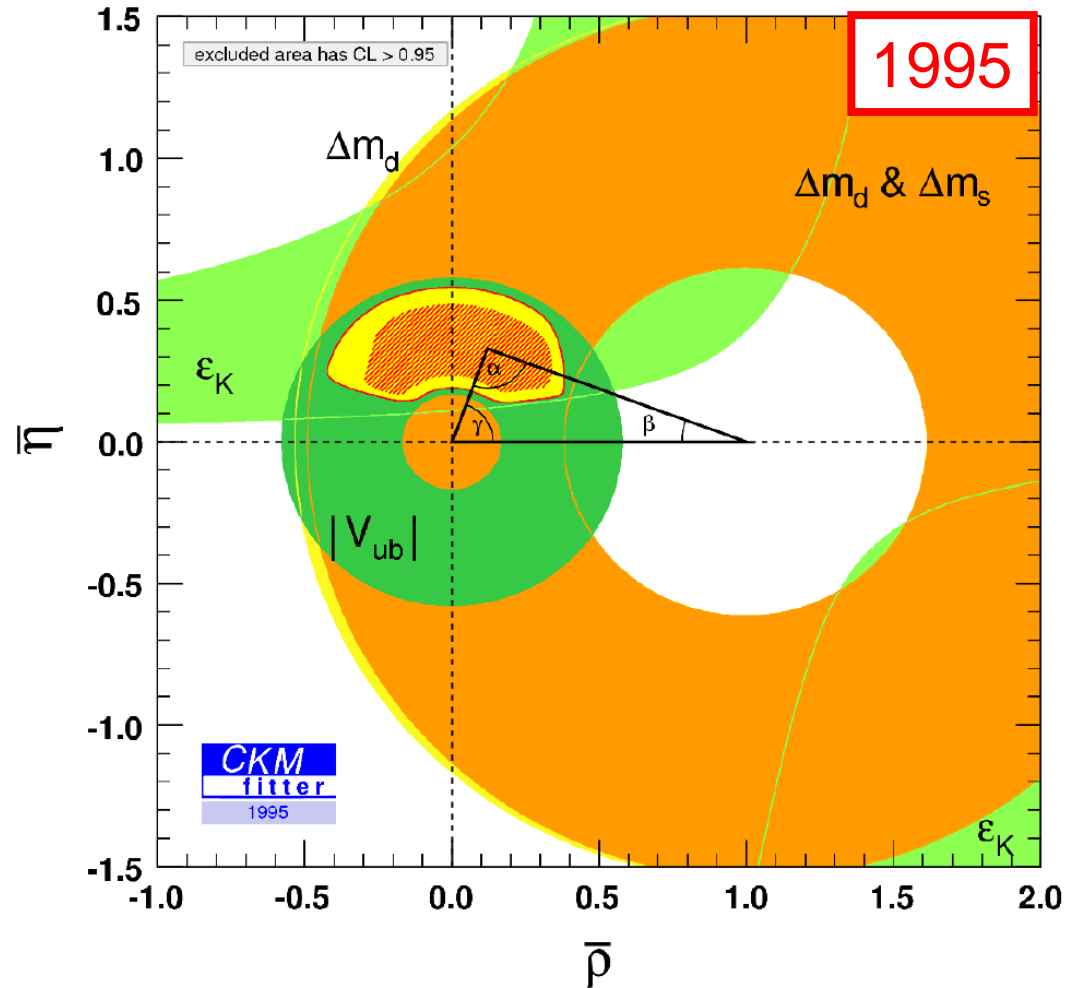
Global LHCb average, now including information from time-dependent analyses of Run 1 data with B_s [JHEP 03 (2018) 059] and B^0 decays [JHEP 06 (2018) 084].



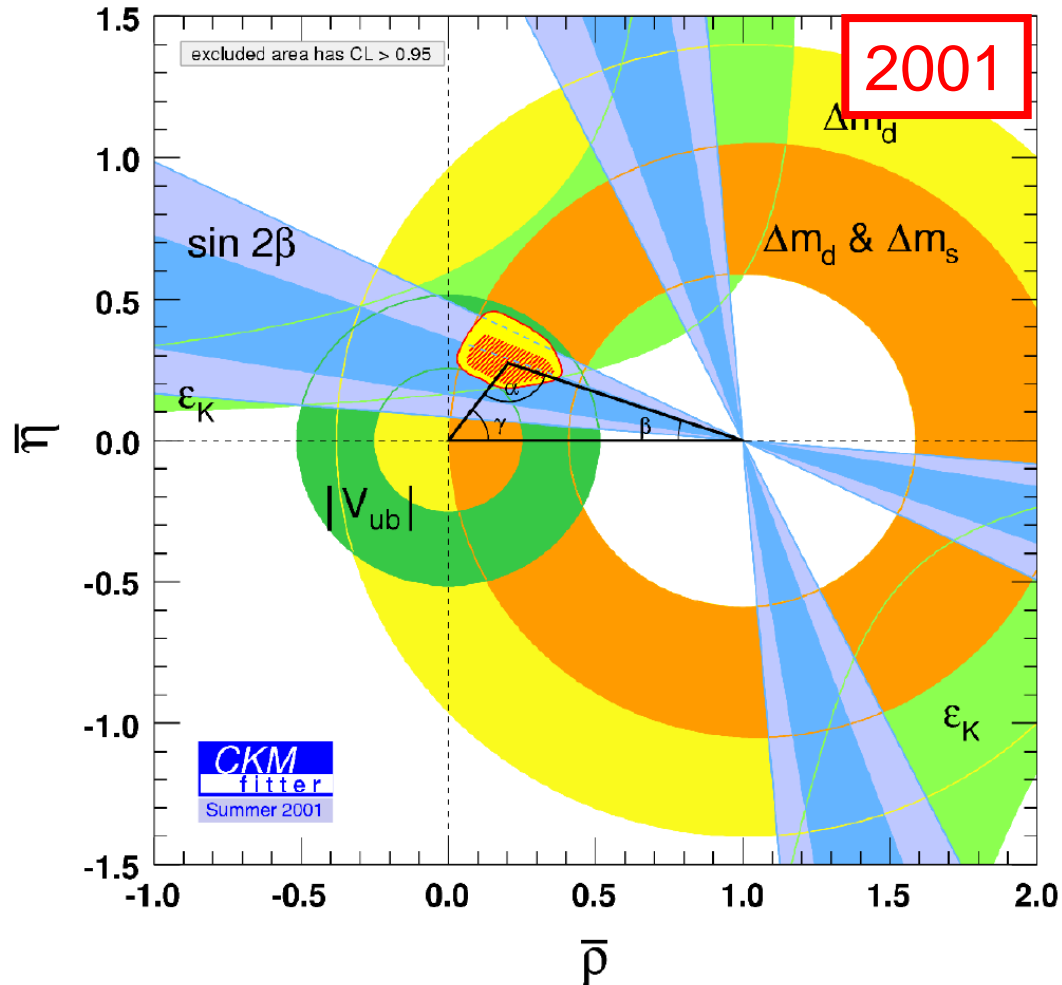
Result is to be compared with indirect prediction of $(65.6^{+1.0}_{-3.4})^\circ$ [CKMfitter, 2018].
Compatible, albeit with a little tension ($\sim 2\sigma$).

Big improvements expected in near future, as still little Run 2 data in average.

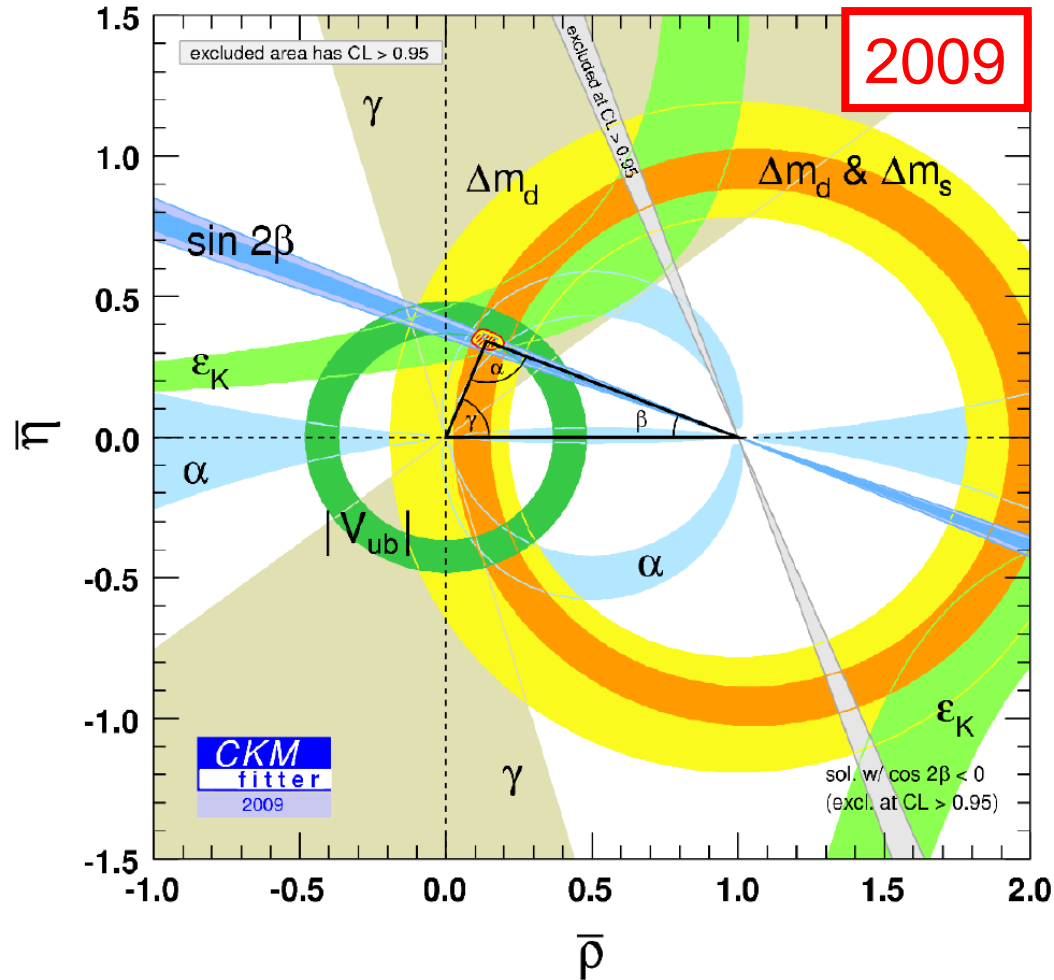
Unitarity Triangle: ~25 years of progress



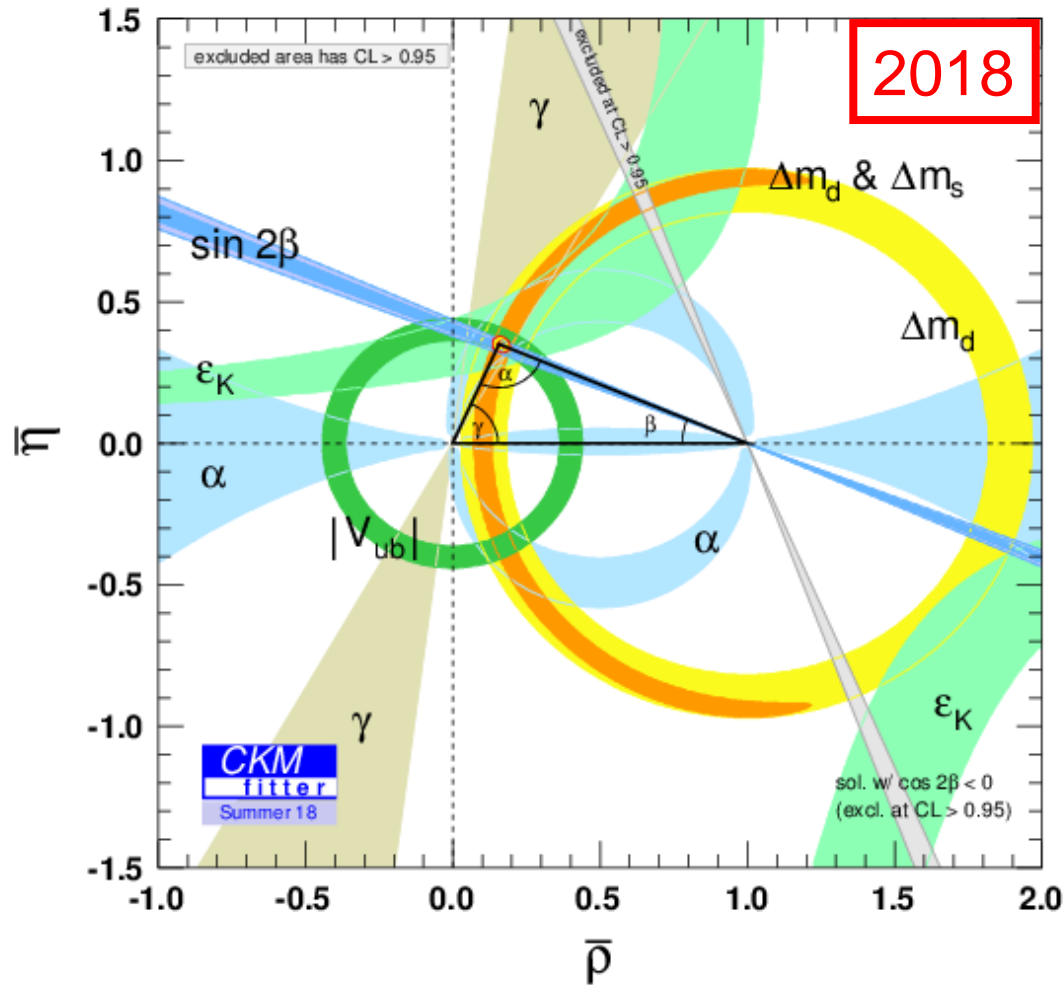
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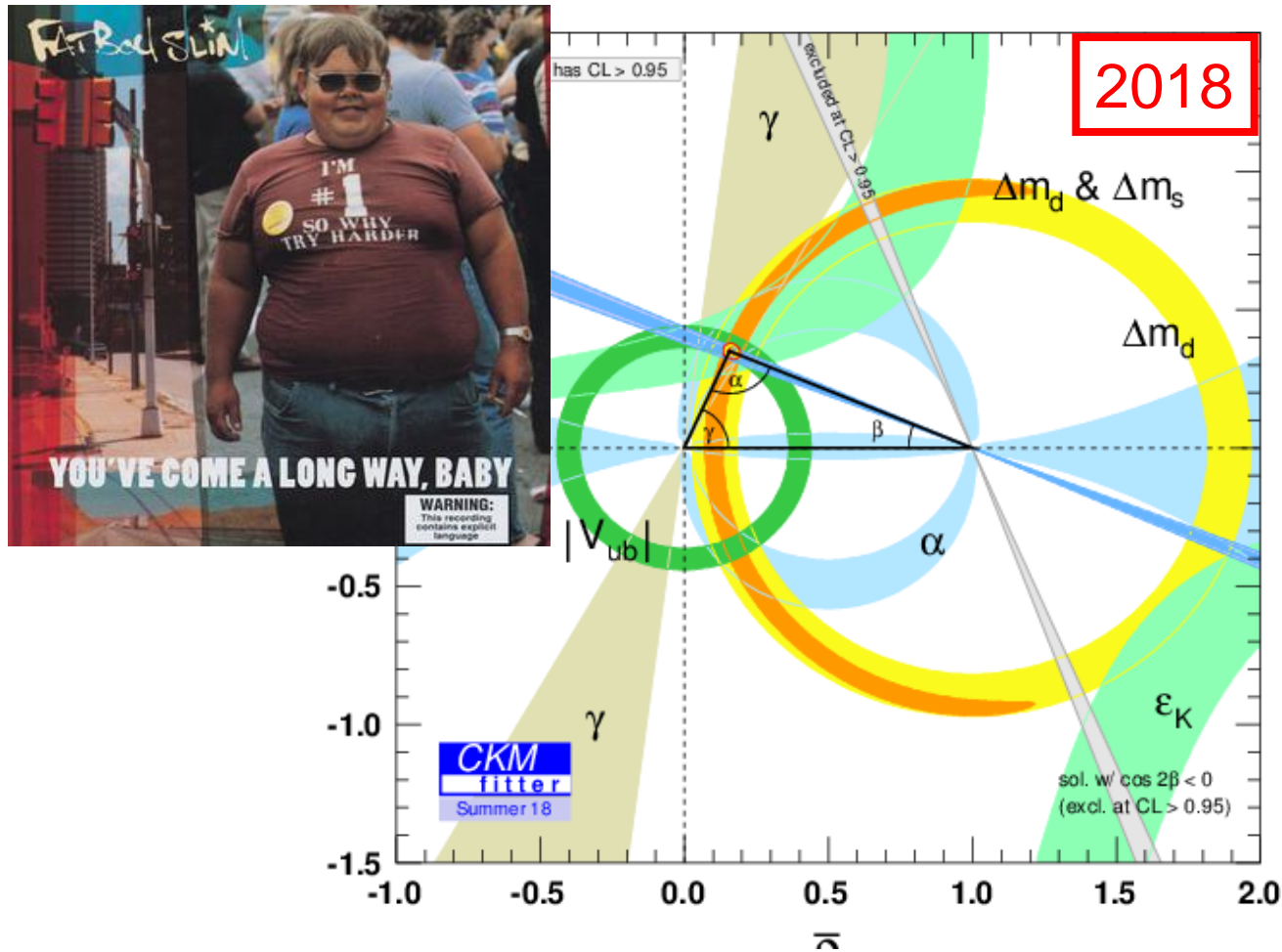
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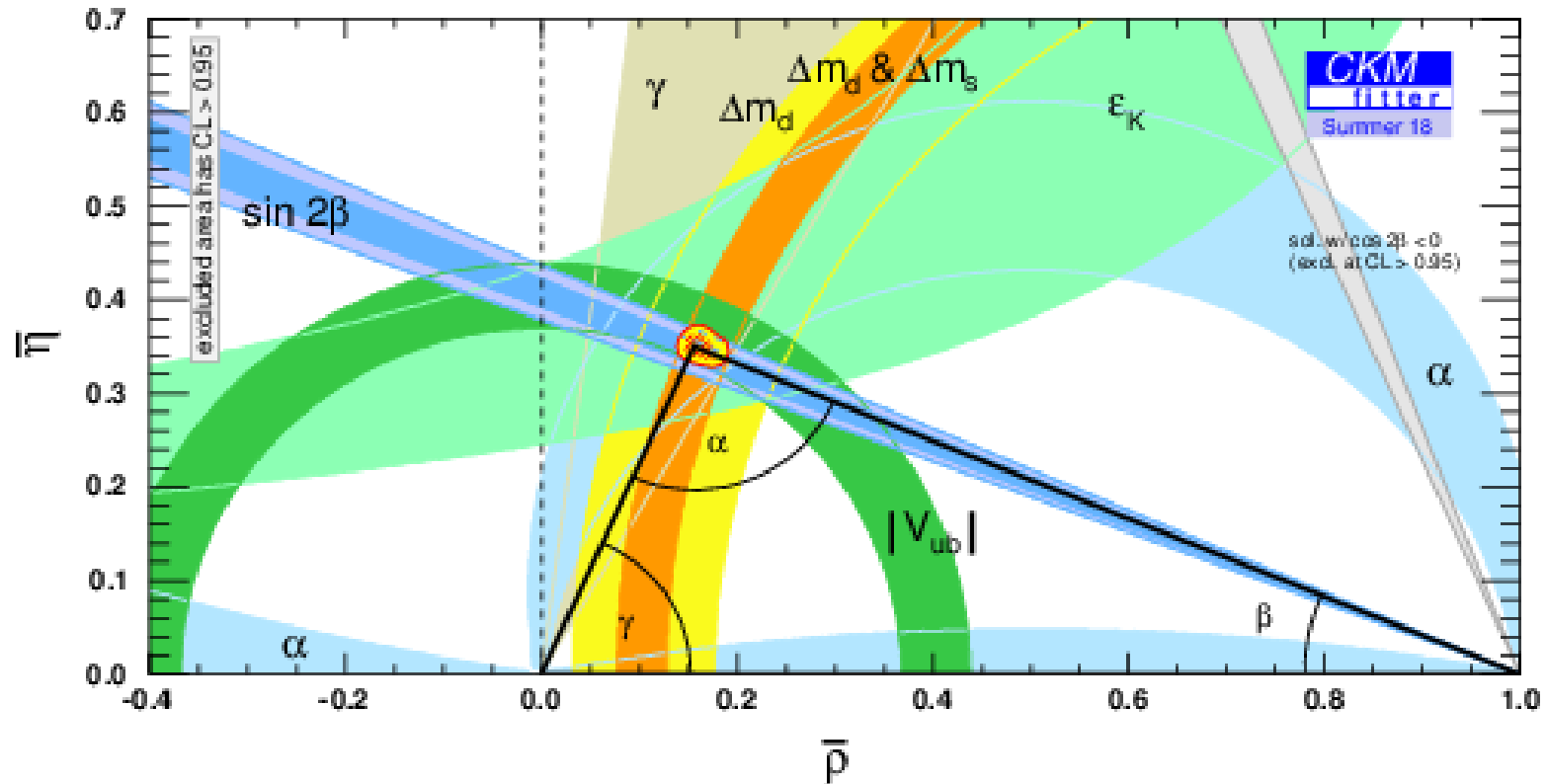
Unitarity Triangle: ~25 years of progress



Enormous improvements in precision, thanks to both experiment and theory (esp. lattice) !

Overall consistency of the Unitarity Triangle

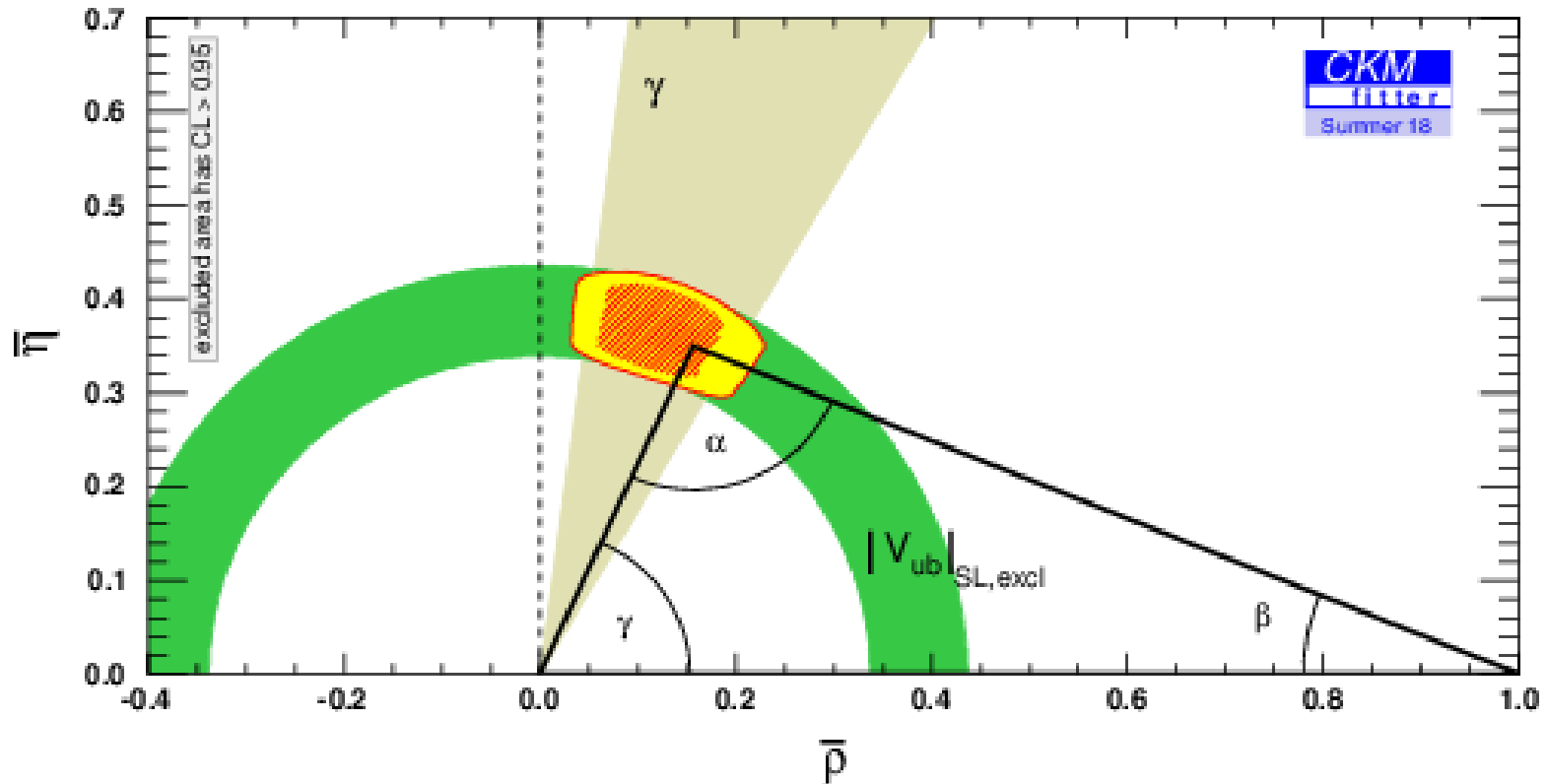
There is broad consistency between all current measurements of the UT. (But, a closer look can reveal intriguing tensions, e.g. [Blanke & Buras, EPJC 79 (2019) 159].)



The CKM paradigm is the dominant mechanism of CPV in nature, but it is certainly possible for New Physics to give $\sim 10\%$ level effects. More measurements needed !

Unitarity Triangle: tree-level observables

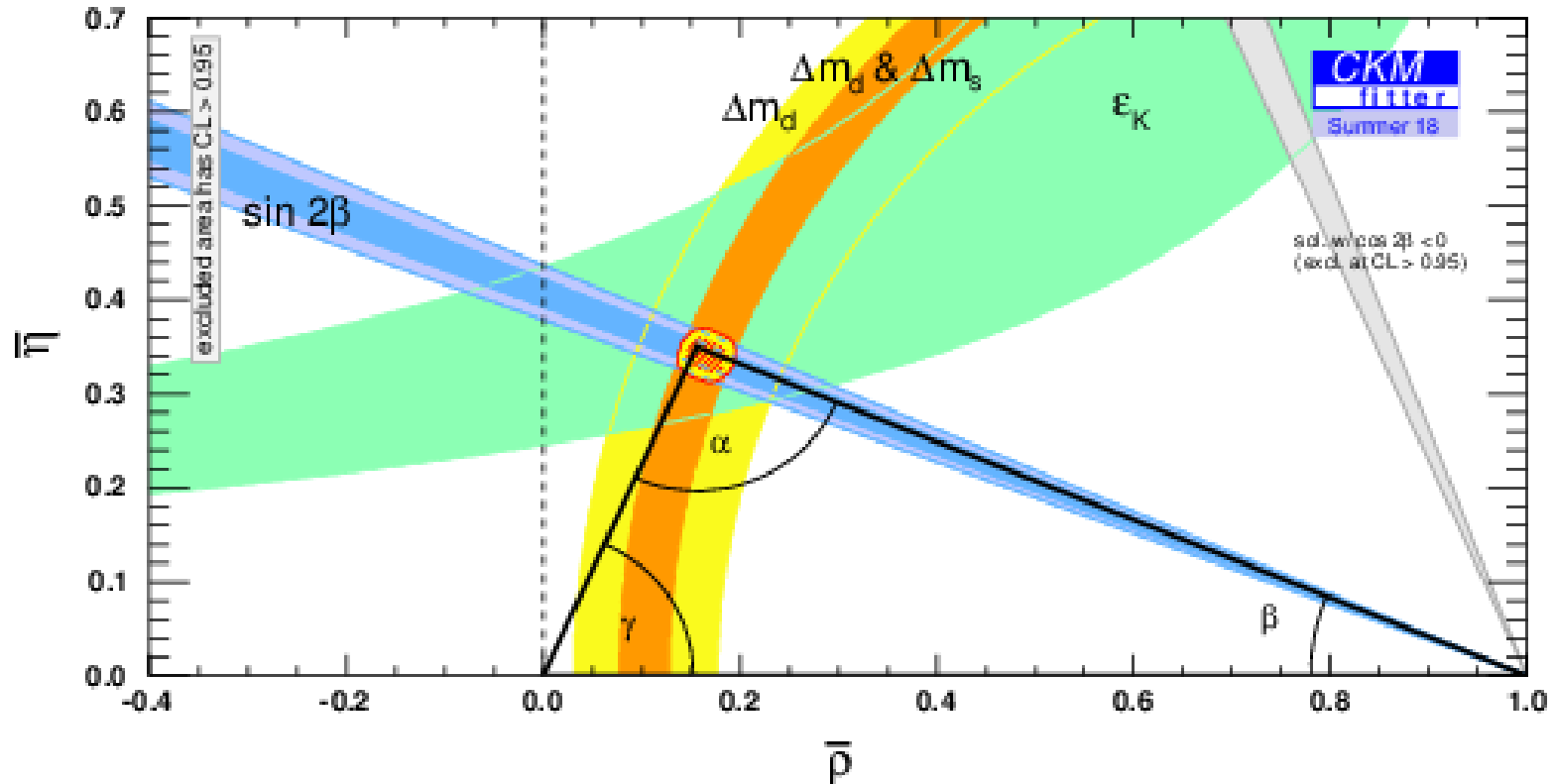
Unitarity Triangle formed from only tree-level quantities \rightarrow assumed pure SM.



Tree observables are γ & the $|V_{ub}|/|V_{cb}|$ side, here showing exclusive measurement.

Unitarity Triangle: loop-level observables

Unitarity Triangle formed from only loop-level quantities \rightarrow possibility of NP effects.

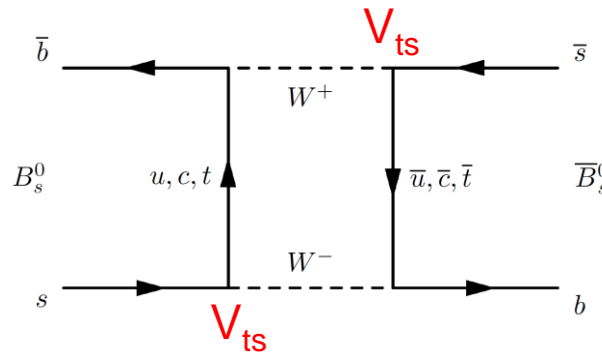


There is good consistency between the tree and loop measurements. There's a need to improve the precision of former to allow for a more sensitive comparison.

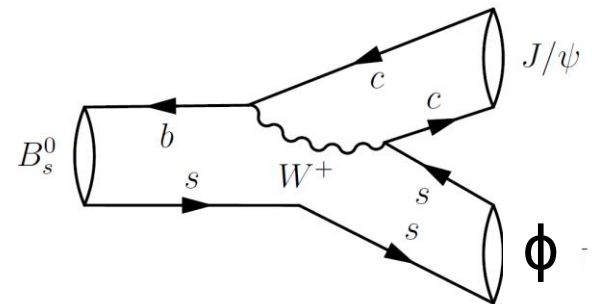
Indirect CPV in B_s system: φ_s

Measuring the CPV phase, φ_s , in B_s mixing-decay interference, e.g. with $B_s \rightarrow J/\psi\Phi$, is **the B_s analogue of the $\sin 2\beta$ measurement**. In the SM this phase is very small & precisely predicted. Box diagram offers tempting entry point for NP !

Once more interference between mixing...



...and decay



Now we probe CKM elements that are complex only at higher order

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

$$\begin{pmatrix} -\frac{1}{8}\lambda^4 + \mathcal{O}(\lambda^6) & \mathcal{O}(\lambda^7) & 0 \\ \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] + \mathcal{O}(\lambda^7) & -\frac{1}{8}\lambda^4(1 + 4A^2) + \mathcal{O}(\lambda^6) & \mathcal{O}(\lambda^8) \\ \frac{1}{2}A\lambda^5(\rho + i\eta) + \mathcal{O}(\lambda^7) & \frac{1}{2}A\lambda^4(1 - 2(\rho + i\eta)) + \mathcal{O}(\lambda^6) & -\frac{1}{2}A^2\lambda^4 + \mathcal{O}(\lambda^6) \end{pmatrix}$$

$$\phi_s^{\text{SM}} \equiv -2\arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right) = -36.3_{-1.5}^{+1.6} \text{ mrad}$$

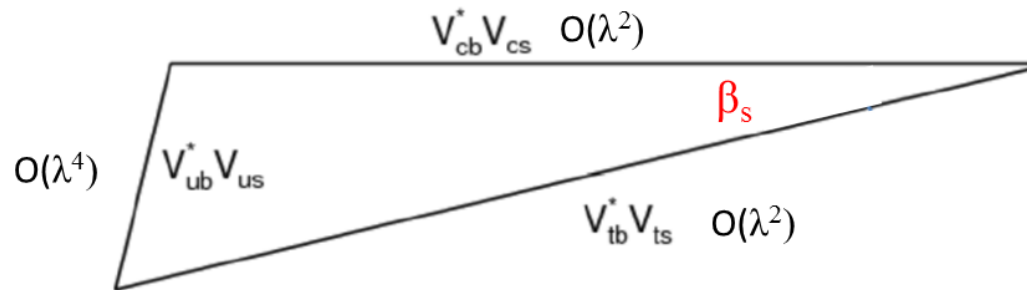
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Once mo
interferen
between
mixing...

Now we
elements
complex

Recall the squashed B_s^0 triangle:



In SM $\varphi_s = -2\beta_s$

$$\begin{pmatrix} 0 & 0 & 0 \\ \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] + \mathcal{O}(\lambda^7) & -\frac{1}{8}\lambda^4(1 + 4A^2) + \mathcal{O}(\lambda^6) & \mathcal{O}(\lambda^8) \\ \frac{1}{2}A\lambda^5(\rho + i\eta) + \mathcal{O}(\lambda^7) & \boxed{\frac{1}{2}A\lambda^4(1 - 2(\rho + i\eta)) + \mathcal{O}(\lambda^6)} & -\frac{1}{2}A^2\lambda^4 + \mathcal{O}(\lambda^6) \end{pmatrix}$$

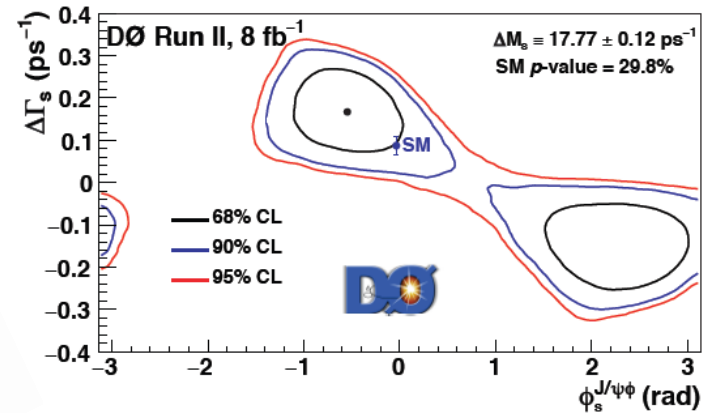
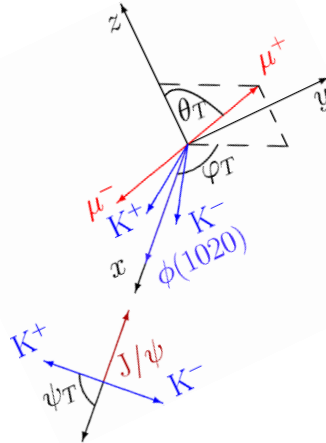
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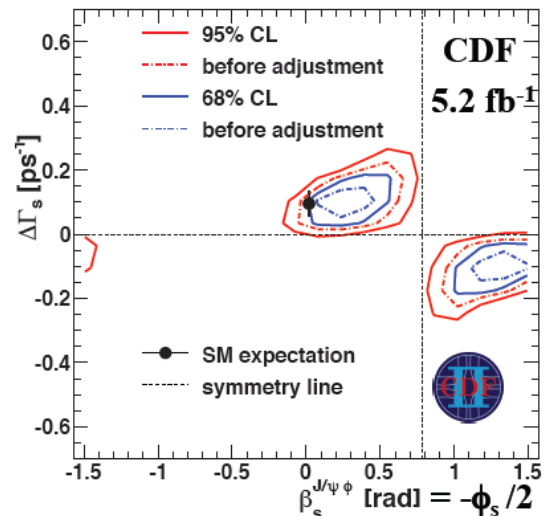
However the measurement is considerably trickier than is the case for $\sin 2\beta$:

- $J/\psi\phi$ is a vector-vector final state, so requires angular analysis to separate out CP+ & CP-
- Very fast oscillations ($\Delta m_s \gg \Delta m_d$)
- Possibility of KK S-wave under ϕ



[PRD 85 (2012) 032006]

Heroic early analyses performed by Tevatron. Consistent results and mild ($\sim 1\sigma$) tension with SM.



[PRD 85 (2012) 072002]

Indirect CPV in B_s system: φ_s

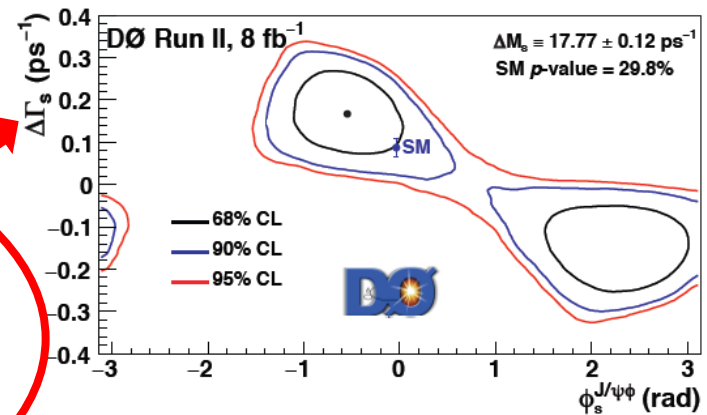
Measuring the CPV phase, φ_s , in B_s mixing-decay interference, e.g. with $B_s \rightarrow J/\psi\Phi$, is **the B_s analogue of the $\sin 2\beta$ measurement**. In the SM this phase is very small & precisely predicted. Box diagram offers tempting entry point for NP !

However the measurement is considerably trickier than is the B^0 case.

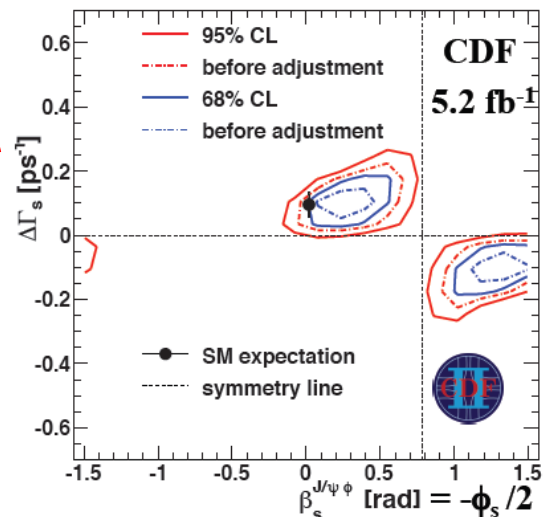
One other detail: in contrast to the B^0 case, the width-splitting $\Delta\Gamma_s$ between the mass eigenstates is here non-negligible (~ 0.1). When included in the formalism this brings additional handles to the analysis, & also provides an additional observable to be measured.

- Possibility of KK S-wave under φ

Heroic early analyses performed by Tevatron. Consistent results and mild ($\sim 1\sigma$) tension with SM.



[PRD 85 (2012) 032006]

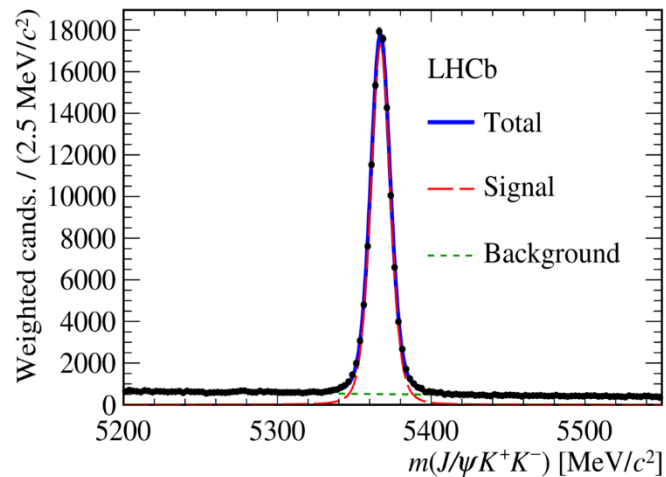


[PRD 85 (2012) 072002]

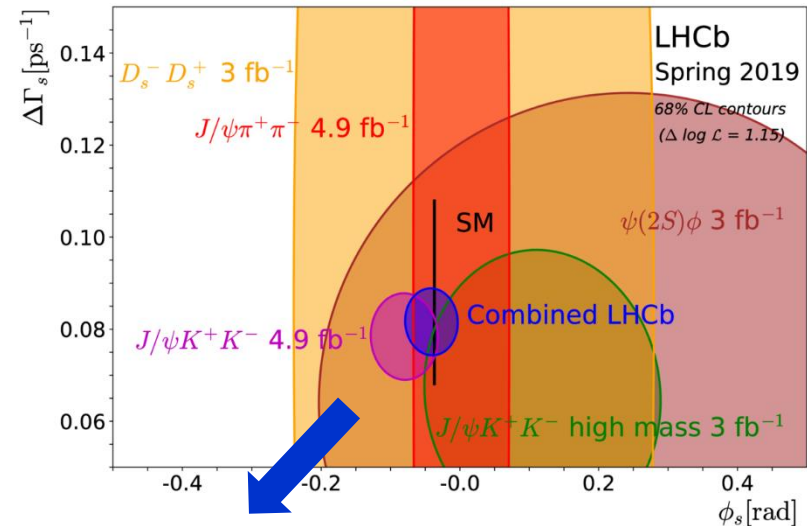
ϕ_s – impact of LHCb

LHC has been able to go far beyond the Tevatron measurements, thanks to much larger yields, and (in case of LHCb) excellent proper time resolution, & access to complementary modes beyond $J/\psi\phi$ (e.g. $B_s \rightarrow J/\psi\pi\pi$ pursued in [PLB 713 (2012) 378] .)

$B_s \rightarrow J/\psi\phi$ signal peak in early Run 2 analysis (117k decays, in 1.9 fb^{-1} c.f. 6.5k at CDF).



Results for early Run 2 $J/\psi\phi$ study, together with Run 1 measurements.



[EPJC 79 (2019) 706]

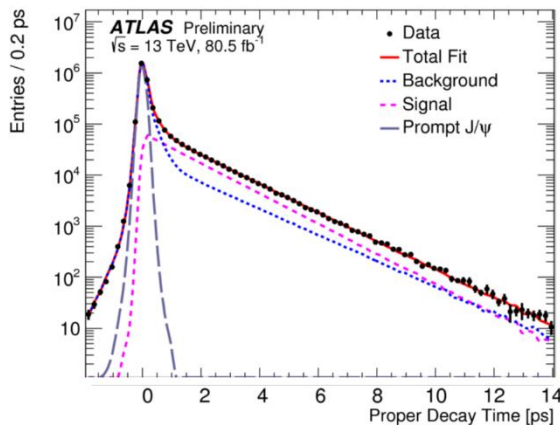
$$\phi_s = -0.041 \pm 0.025 \text{ rad} \quad \Delta\Gamma_s = 0.0816 \pm 0.0048 \text{ ps}^{-1}$$

Measurement of ϕ_s at ATLAS and CMS

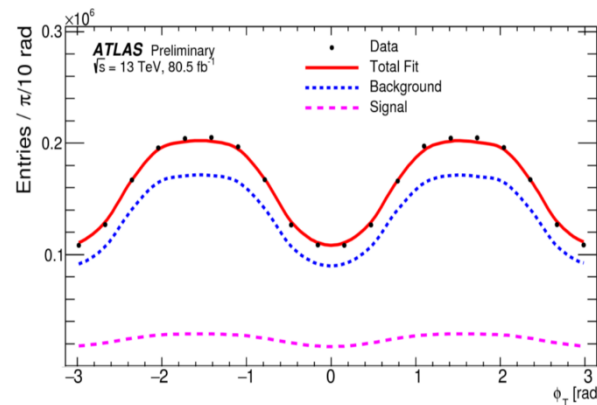
Measurement of ϕ_s is a key goal of the ATLAS and CMS flavour physics programme, enabled by excellent detector performance and $J/\Psi \rightarrow \mu\mu$ trigger.

e.g. ATLAS $B_s \rightarrow J/\Psi\phi$ preliminary Run 2 analysis with 80 fb^{-1} [[ATL-CONF-2019-009](#)]:

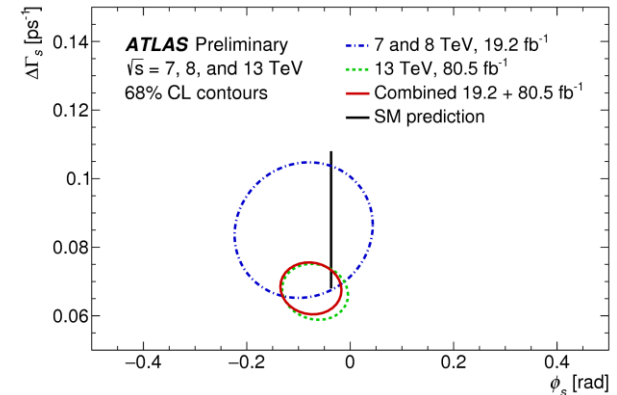
Proper decay time



Transversity angle ϕ_T



Results, including those of Run 1 [[JHEP 08 \(2016\) 147](#)]



Combining with Run 1 results [[JHEP 08 \(2016\) 147](#)]

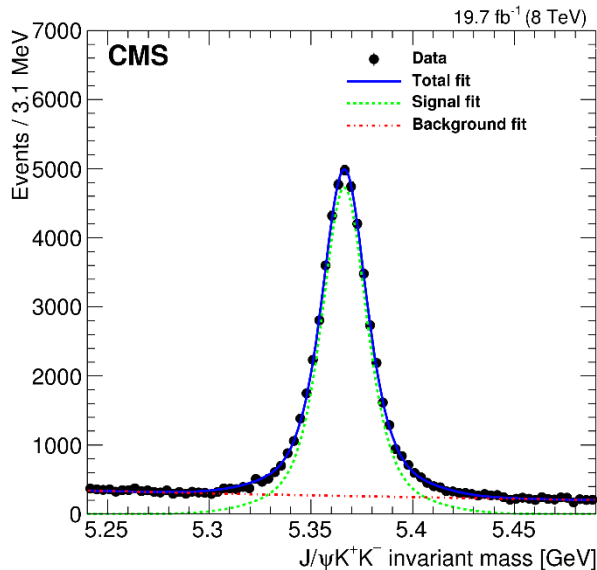
$$\begin{aligned} \phi_s &= -0.076 \pm 0.034 \text{ (stat.)} \pm 0.019 \text{ (syst.) rad} \\ \Delta\Gamma_s &= 0.068 \pm 0.004 \text{ (stat.)} \pm 0.003 \text{ (syst.) ps}^{-1} \end{aligned}$$

Measurement of ϕ_s at ATLAS and CMS

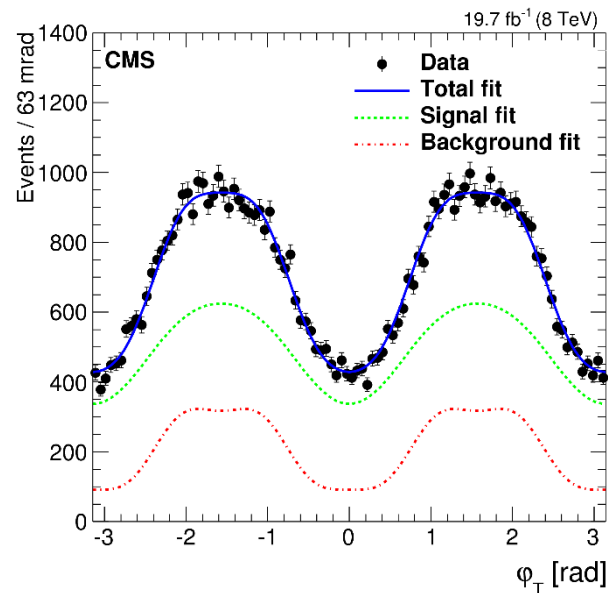
Measurement of ϕ_s is a key goal of the ATLAS and CMS flavour physics programme, enabled by excellent detector performance and $J/\Psi \rightarrow \mu\mu$ trigger.

e.g. CMS $B_s \rightarrow J/\Psi\phi$ 8 TeV analysis [[PLB 757 \(2016\) 97](#)]

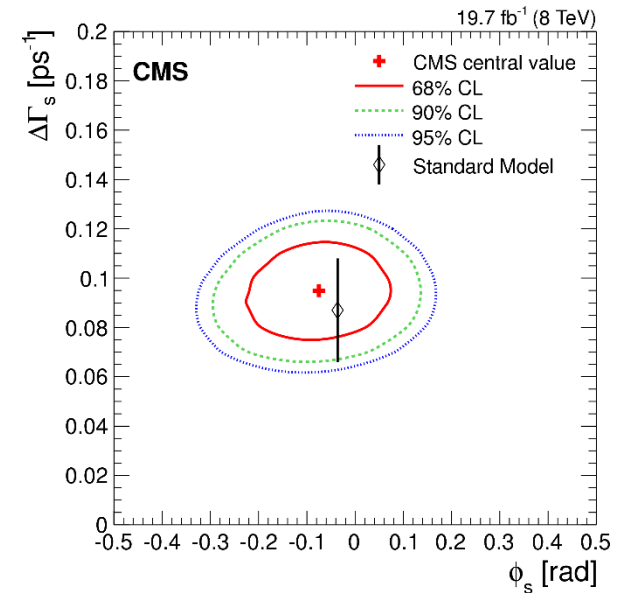
Invariant mass



Transversity angle ϕ_T

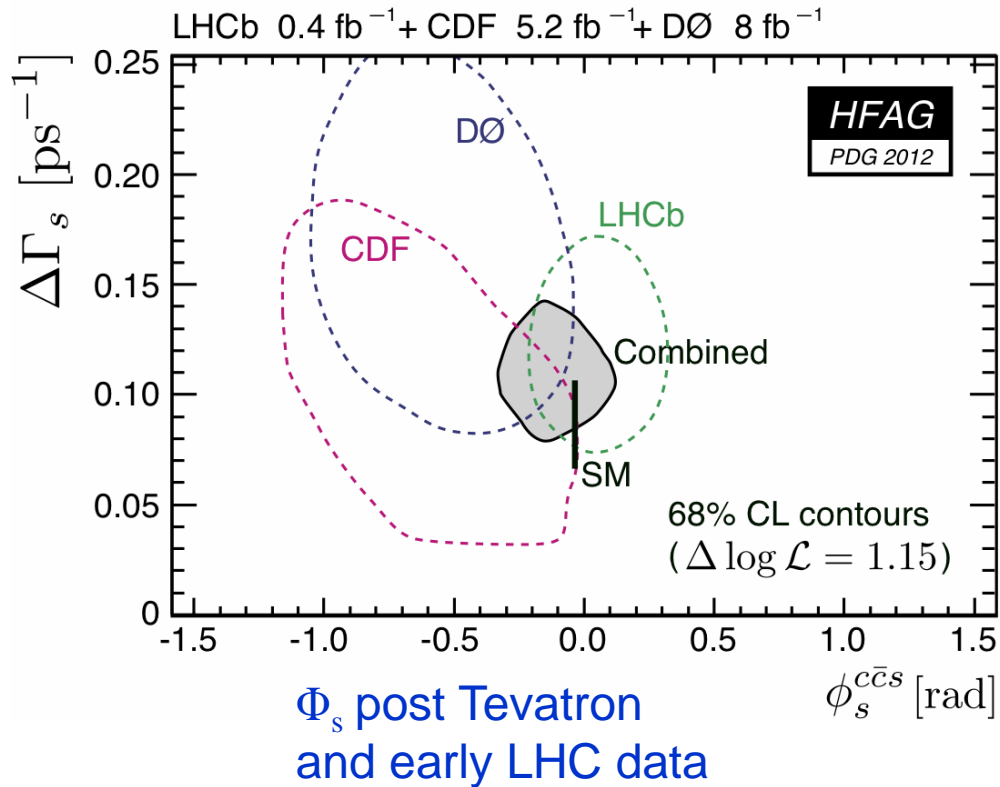


Result contours

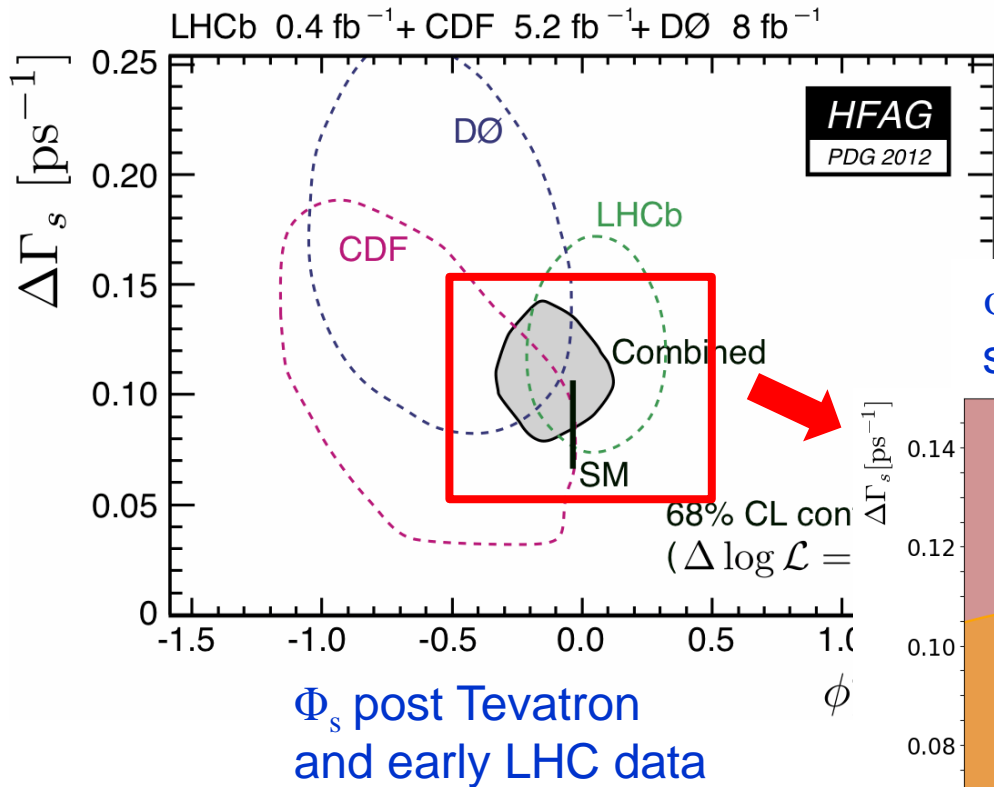


$$\phi_s = -0.075 \pm 0.097 \text{ (stat)} \pm 0.031 \text{ (syst)} \text{ rad},$$
$$\Delta\Gamma_s = 0.095 \pm 0.013 \text{ (stat)} \pm 0.007 \text{ (syst)} \text{ ps}^{-1}.$$

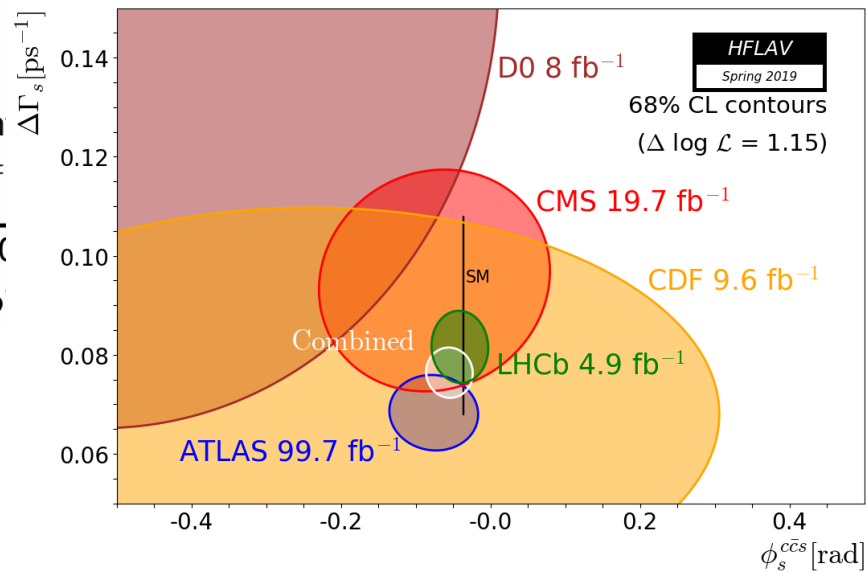
φ_s : the impact of the LHC



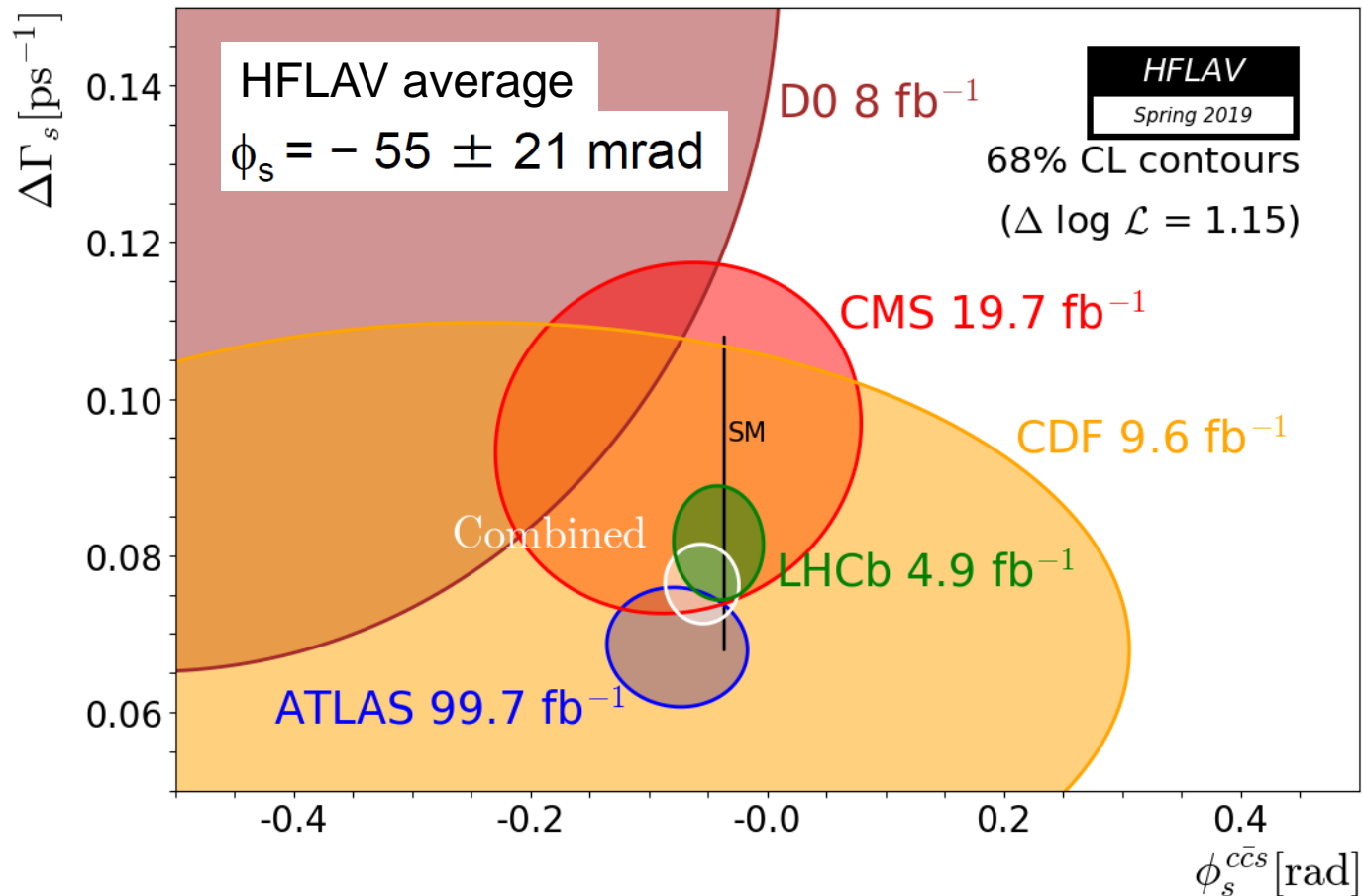
φ_s : the impact of the LHC



φ_s post Run 1 LHC and including
some Run 2 ATLAS & LHCb data



ϕ_s : the current state of play



ϕ_s now measured with ~ 20 mrad precision and so far compatible with SM.
Hint of non-zero value emerging – will be interesting with full Run 2 dataset !

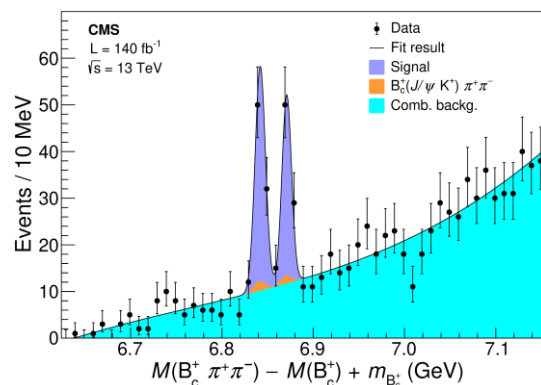
Spectroscopy (a digression)

Hadron spectroscopy is not flavour physics. However flavour-physics experiments are ideally suited for discovering and studying new states, and many high impact results have emerged of this nature.

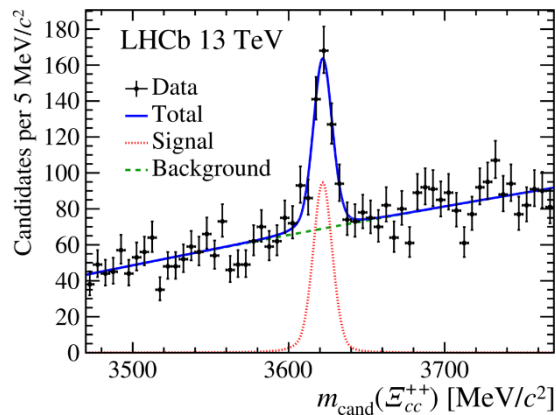
Spectroscopy - the conventional

Many new states found at the LHC, most of which fit within the 'vanilla' quark model

CMS discovery of excited B_c states [PRL 122 (2019) 132001]



LHCb discovery of the Ξ_{cc}^{++} [PRL 119 (2017) 112001]



“

Baryons can now be constructed from quarks by using the combinations qqq , $qqq\bar{q}$, etc, while mesons are made out of $q\bar{q}$, $q\bar{q}q\bar{q}$, etc.

Murray Gell-Mann

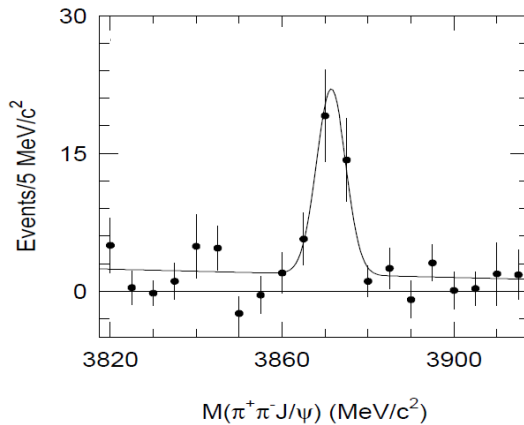
”

Spectroscopy - the exotic

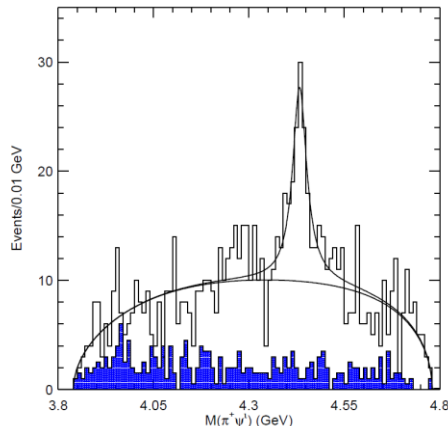
Other states, many discovered in e^+e^- , are good candidates to be 'exotic':

Both are strong candidates to be four-quark states

Observation of the X(3872) at Belle [PRL 91 (2003) 262001]



Observation of the Z(4430)⁺ at Belle [PRL 100 (2008) 142001]



“

Baryons can now be constructed from quarks by using the combinations qqq , $qqq\bar{q}$ etc, while mesons are made out of $q\bar{q}$, $q\bar{q}q\bar{q}$ etc.

Murray Gell-Mann

”

Spectroscopy results – provoke great interest among physicists

Top cited Belle physics papers

1. Observation of a narrow charmonium - like state in exclusive $B^+ \rightarrow K^+ \pi^+ \pi^- J/\psi$ decays

⁽¹⁶⁵⁶⁾ Belle Collaboration (S.K. Choi (Gyeongsang Natl. U.) *et al.*). Sep 2003. 10 pp.
Published in **Phys.Rev.Lett.** **91** (2003) 262001
DOI: [10.1103/PhysRevLett.91.262001](https://doi.org/10.1103/PhysRevLett.91.262001)
e-Print: [hep-ex/0309032](https://arxiv.org/abs/hep-ex/0309032) | [PDF](#)
[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[ADS Abstract Service](#); [ADS Abstract Service](#); [Link to PRESSRELEASE](#)
[Detailed record](#) - Cited by 1656 records **1000+**

2. Observation of large CP violation in the neutral B meson system

⁽⁹⁵¹⁾ Belle Collaboration (Kazuo Abe (KEK, Tsukuba) *et al.*). Jul 2001. 12 pp.
Published in **Phys.Rev.Lett.** **87** (2001) 091802
KEK-PREPRINT-2001-50, BELLE-PREPRINT-2001-10
DOI: [10.1103/PhysRevLett.87.091802](https://doi.org/10.1103/PhysRevLett.87.091802)
e-Print: [hep-ex/0107061](https://arxiv.org/abs/hep-ex/0107061) | [PDF](#)
[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[ADS Abstract Service](#); [OSTI.gov Server](#)
[Detailed record](#) - Cited by 951 records **500+**

Top cited LHCb physics papers

1. Test of lepton universality using $B^+ \rightarrow K^+ \ell^+ \ell^-$ decays

⁽⁸⁵³⁾ LHCb Collaboration (Roel Aaij (NIKHEF, Amsterdam) *et al.*). Jun 25, 2014. 10 pp.
Published in **Phys.Rev.Lett.** **113** (2014) 151601
CERN-PH-EP-2014-140, LHCb-PAPER-2014-024
DOI: [10.1103/PhysRevLett.113.151601](https://doi.org/10.1103/PhysRevLett.113.151601)
e-Print: [arXiv:1406.6482](https://arxiv.org/abs/1406.6482) [hep-ex] | [PDF](#)
[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[CERN Document Server](#); [ADS Abstract Service](#)
[Detailed record](#) - Cited by 853 records **500+**

2. Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays

⁽⁷⁹²⁾ LHCb Collaboration (Roel Aaij (CERN) *et al.*). Jul 13, 2015. 15 pp.
Published in **Phys.Rev.Lett.** **115** (2015) 072001
CERN-PH-EP-2015-153, LHCb-PAPER-2015-029
DOI: [10.1103/PhysRevLett.115.072001](https://doi.org/10.1103/PhysRevLett.115.072001)
e-Print: [arXiv:1507.03414](https://arxiv.org/abs/1507.03414) [hep-ex] | [PDF](#)
[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[CERN Document Server](#); [ADS Abstract Service](#); [Interactions.org article](#); [Link to BBC News article](#); [Link to Symmetry Magaz News article](#); [Link to PBS website](#); [Link to Scientific American article](#)
[Detailed record](#) - Cited by 792 records **500+**

Spectroscopy results – provoke great interest among public too

e.g. reactions to LHCb study of resonant nature of Z(4430)- [PRL 112 (2013) 222002]

 <p>LHCb confirms existence of exotic hadrons</p>	<p>How CERN's Discovery of Exotic Particles May Affect Astrophysics by BRIAN KOBERLEIN on APRIL 10, 2014</p>
<p>大型强子对撞机捕获到神秘粒子Z_c(4430) 或许成为物质形式“四夸克态”存在的有力证据</p>	<p>2014/04/13 15:46 LHCb実験を行っている国際研究チームが、4個のクォークが結合した粒子である「Z(4430)」を合成したと発表した。Z(4430)としては、初発見から7年目にしてようやく別の研究チームが存在を立証した事になる。</p>
<p>นักฟิสิกส์ยืนยันพบฮาดรอนสองควาร์กสองแอนติควาร์ก WRITTEN BY NATTY_SCI ON APRIL 13, 2014. POSTED BY... ล่าสุด เครื่อง LHCb ได้มีการศึกษาอีกครั้งและนักฟิสิกส์ชาวเยอรมันและ BaBar มาให้รายละเอียดด้วย</p>	 <p>Nowa forma materii: potwierdzono istnienie... ... DOTYCHCZAS WYRÓŻNIANO BARIONY I MEZONY</p>
<p>המאשר את קיומן של מצב זה "אמר דובר... ... והוכיח כי זהו באמת חלקיק...</p>	<p>...ательно доказал мезона Z(4430)</p>
<p>PISTOLA FU... LHCb kir... Mystisk p... Các nhà ngh...</p>	<p>Time To Open the Gates of Hell? CERN: Large Hadron Collider Discovers 'Very Exotic Matter' That Challenges Traditional Physics! (Must-See Videos) Thursday, April 17, 2014 19:57</p>
<p>Tetraquark: to hạp tạo... Thảo luận trong 'Chưa học' bắt đầu bởi ndmhdnc, 15/... ISNA شکرتاری دانشجویان ایران Iranian Students' News Agency</p>	 <p>...staan exotische hadronen</p>
<p>تاکنون کشف ذره Z(4430) در سال 2007 بنسبت جنجال برانگیز بود و فیزیکدانان بر سر موجودیت یا عدم موجودیت آن اختلاف نظر داشتند تأیید کنونی ذره با استفاده از آشکارساز LHCb ماوازی هرگونه تردید منطقی موجود است.</p>	<p>LHCb confirma la existencia de la partícula Z(4430) formada por cuatro quarks Παρασκευή, 11 Απριλίου 2014 O LHCb επιβεβαίωσε την ύπαρξη εξωτικού σωματιδίου, LHCb confirms existence of exotic hadrons</p>
<p>CONFIRMADA L'EXISTÈNCIA D'UNA NOVA PARTÍCULA SUBATÒMICA</p>	<p>SAT APR 12, 2014 AT 08:25 PM PDT Tetra Quark: Not a New Star Trek Character, a New State of Matter. Naturkundemuseum & Wissenschaft CERN-fysici bevestigen bestaan nieuw exotisch deeltje</p>

Spectroscopy results – provoke great interest among public too

e.g. reactions to LHCb study of resonant nature of $Z(4430)^-$ [[PRL 112 \(2013\) 222002](#)]

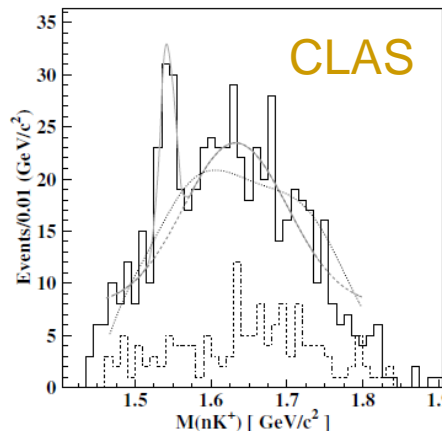
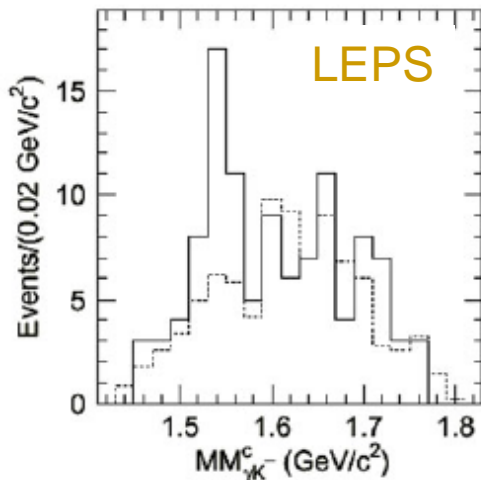
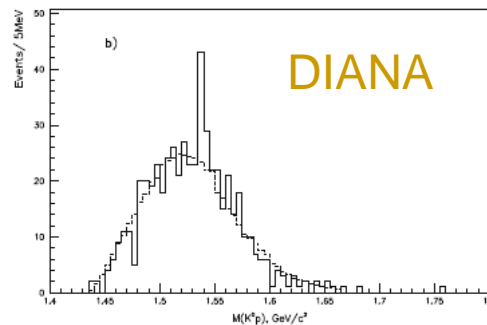
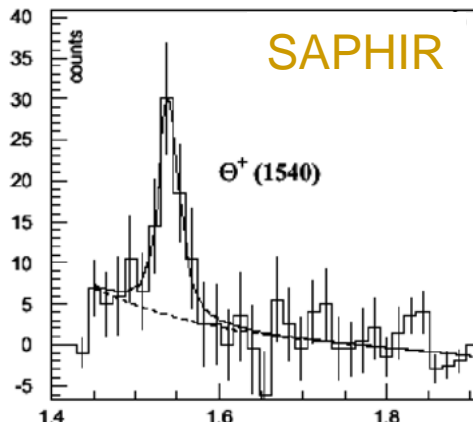


The image shows a YouTube video player interface. At the top, there is the YouTube logo and a search bar. The main content is a video frame showing four saxophonists performing on a stage. The video player includes a progress bar at the bottom of the frame, showing a timestamp of 0:07 / 1:17. Below the video frame, the title "Z(4430) for saxophone quartet by Roger Zare" is displayed. Under the title, there is a small profile picture of Roger Zare, a "Subscribe" button with a count of 52, and a view count of 152 views.

Montreux jazz festival, 2014

The hunt for pentaquarks – a long journey with several cul-de-sacs

Pentaquark signals have been claimed before, for example the Θ^+ ($\bar{s}uudd$) ‘seen’ by several experiments in the early 2000s.

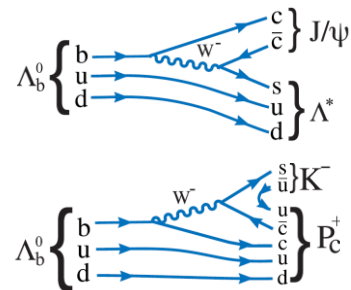


After an initial rush of confirmations, null results from more sensitive experiments appeared, & eventually it was accepted to be non-existent.

“ The whole story – the discoveries themselves, the tidal wave of papers by theorists and phenomenologists that followed, and the eventual ‘undiscovery’ - is a curious episode in the history of science.” PDG 2008

[for more information, see [Hicks, Eur. Phys. J. H 37 \(2012\) 1](#)]

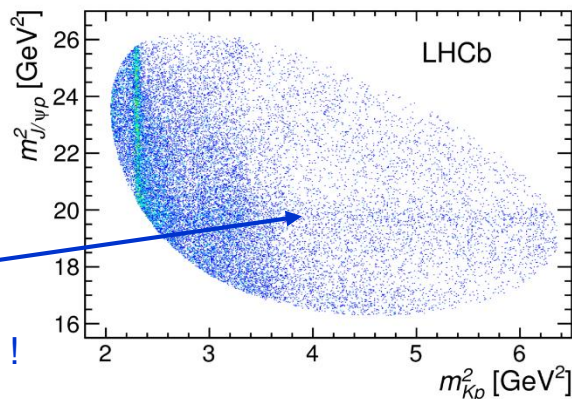
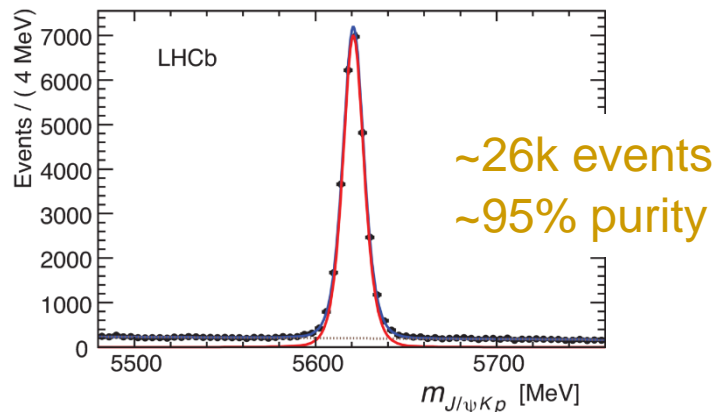
J/Ψp resonances consistent with pentaquark states



PRL 115
(2015) 0720011

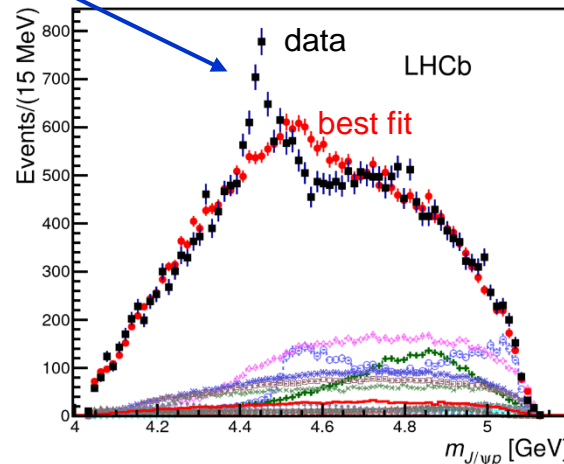
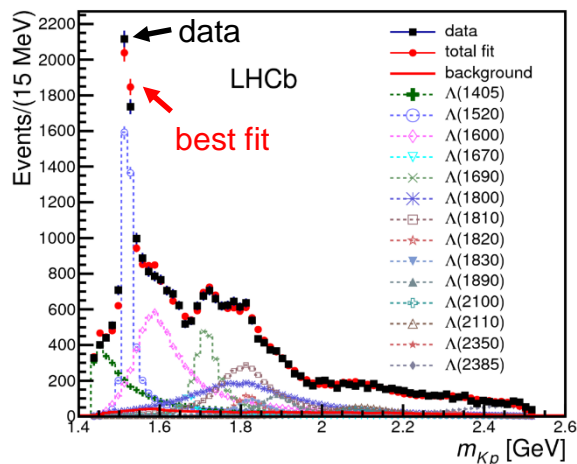
Large & pure sample of $\Lambda_b \rightarrow J/\Psi p K$ decays

Distinctive structure in $J/\Psi p$ spectrum



Amplitude model of conventional states can reproduce K_p spectrum well enough...

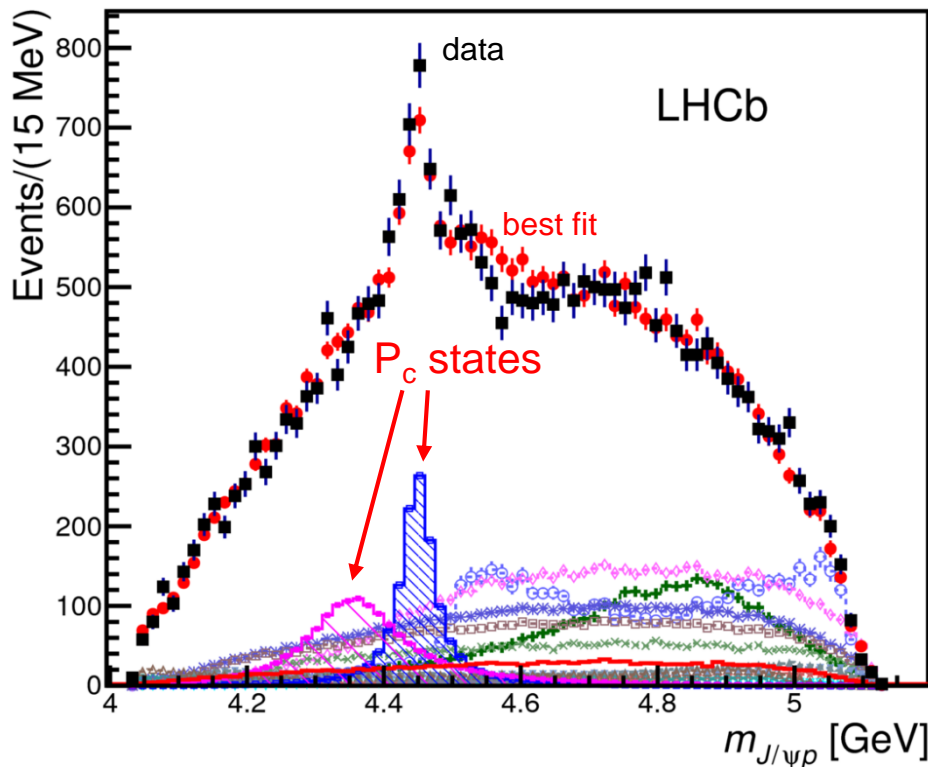
...but cannot describe the J/Ψ projection at all.



J/ Ψ p resonances consistent with pentaquark states

[PRL 115
(2015) 072001]

Can only describe data satisfactorily by adding two exotic pentaquark states with content uudccbar. Best fit has J=3/2 and 5/2 with opposite parities.



$P_c(4380)$:

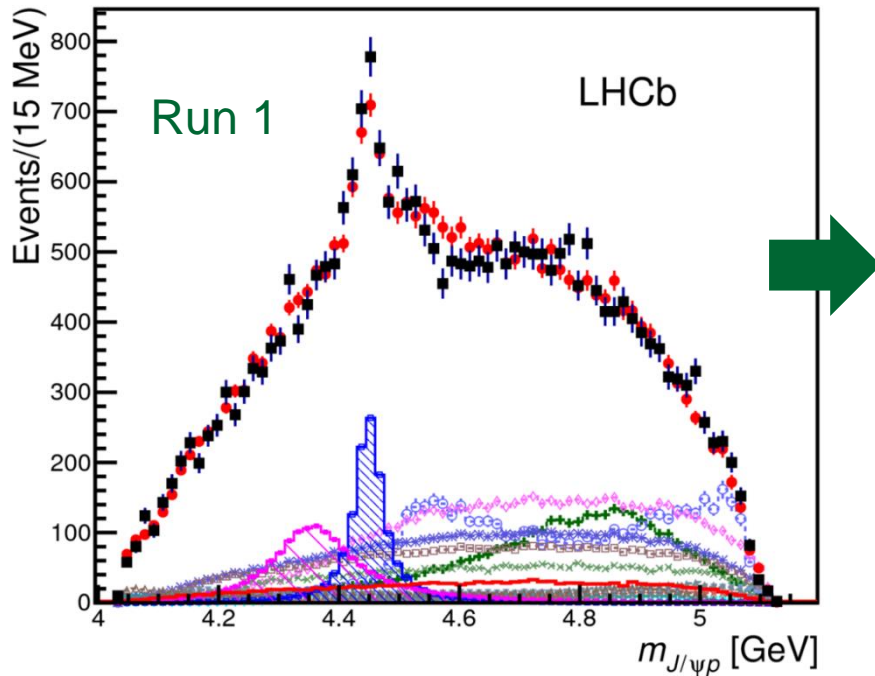
$$M = 4380 \pm 8 \pm 29 \text{ MeV},$$
$$\Gamma = 205 \pm 18 \pm 86 \text{ MeV}$$

$P_c(4450)$:

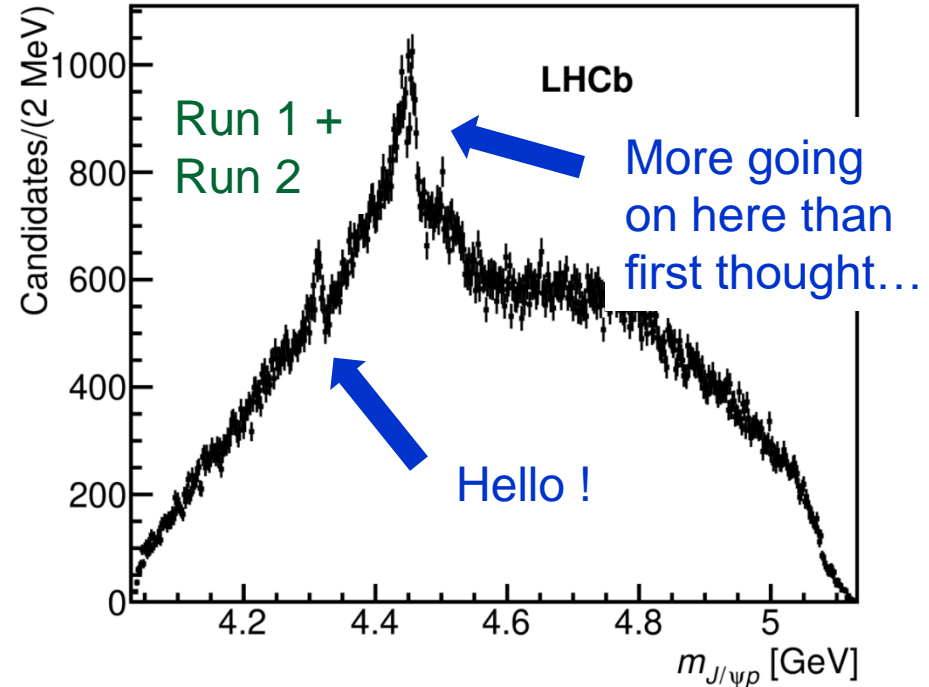
$$M = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$
$$\Gamma = 39 \pm 5 \pm 19 \text{ MeV}$$

Pentaquarks – why more data matters

Run 2 data and improved selection provide x9 increase in signal



[PRL 115 (2015) 072001]

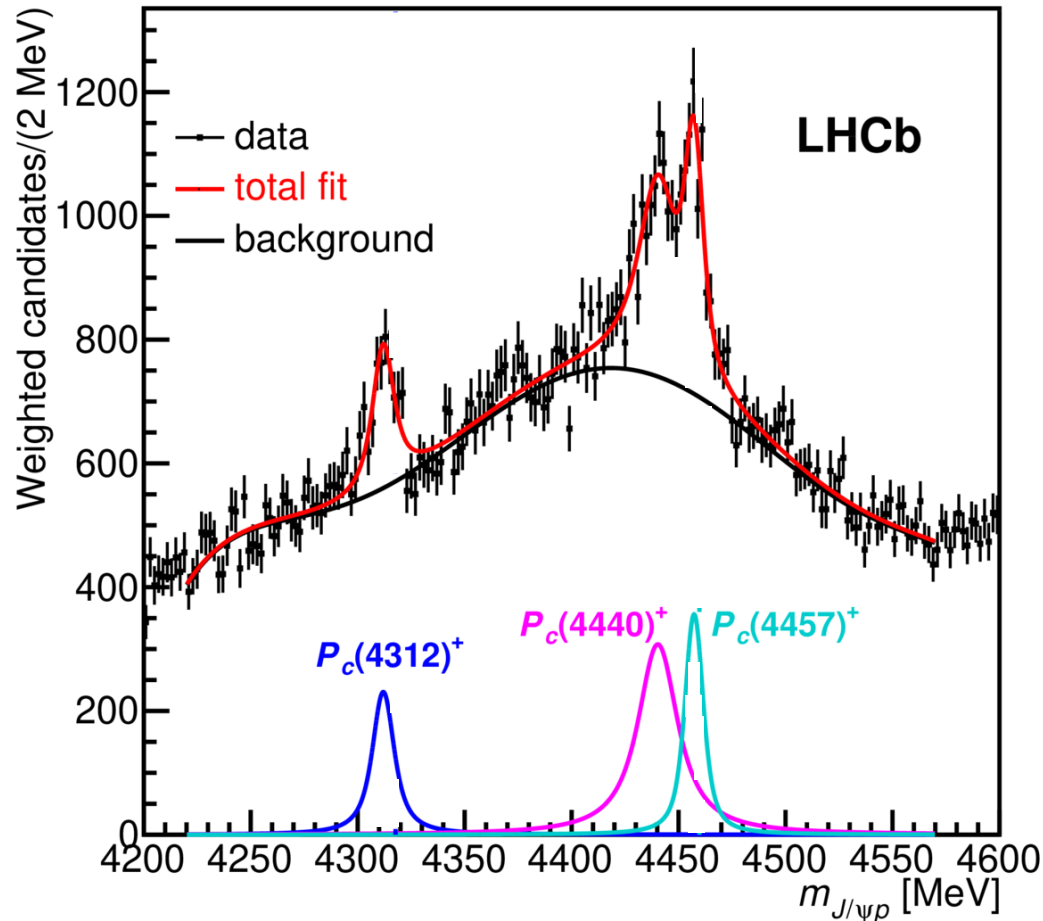


[PRL 122 (2019) 222001]

Not one narrow state, but three

A closer look at Run 2 data, after weighting to suppress effect of Λ^* background.

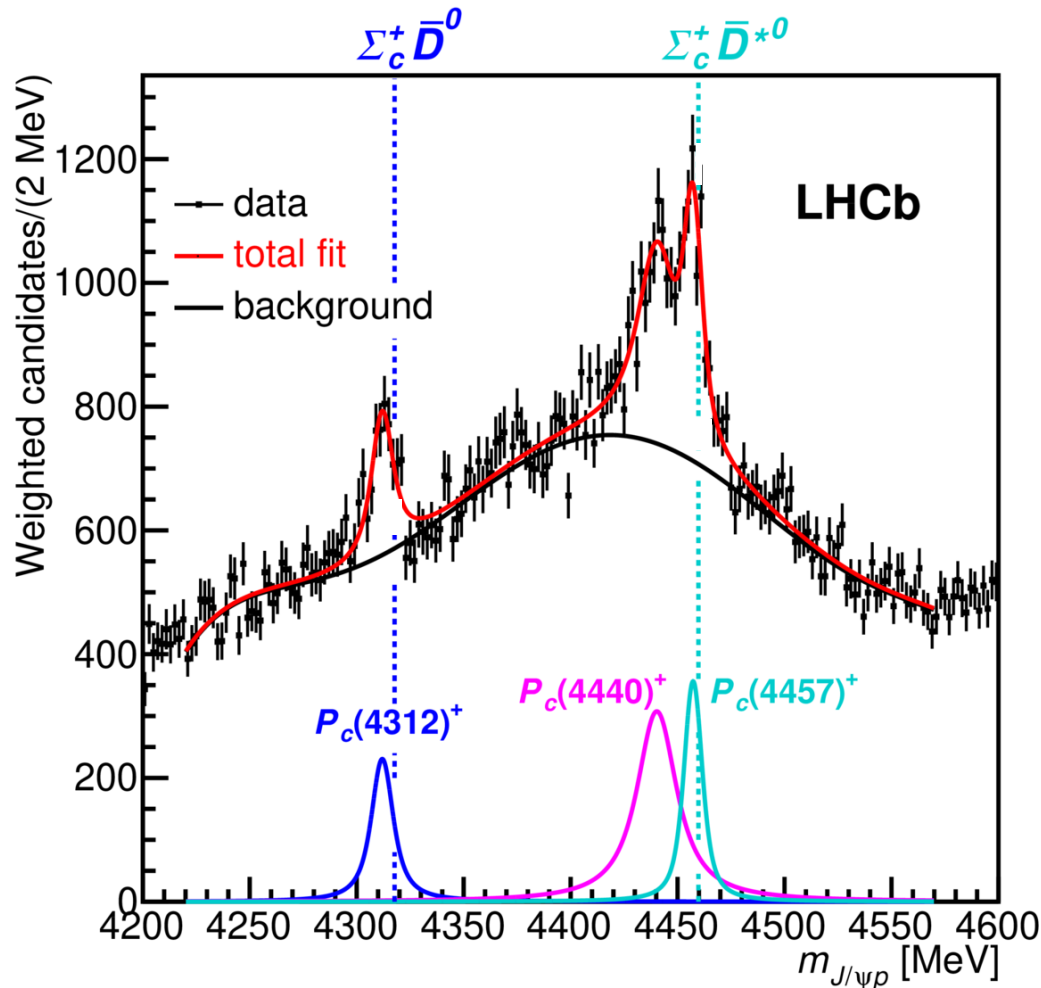
[PRL 122 (2019) 222001]



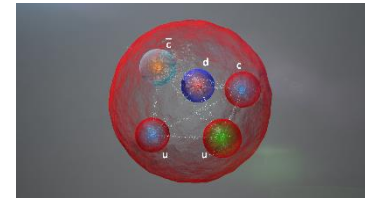
A new narrow state is observed at 4312 MeV, and the previous narrowish state is resolved into two close-lying narrower states. An amplitude analysis is required to determine J^P and decide on whether broad $P_c(4380)$ still required.

Not one narrow state, but three

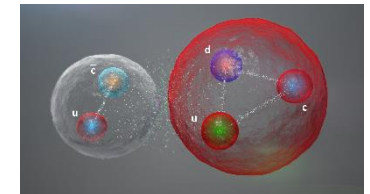
[PRL 122 (2019) 222001]



tightly-bound model



molecular model



Intriguingly, two of the states lie just below the $\Sigma_c D^{(*)0}$ thresholds, which supports a molecular meson-baryon bound state picture of the pentaquarks. See e.g.

[Wang *et al.*, PRC 84 (2011) 015203], [Zhang *et al.*, CPC 36 (2012) 6], [Wu *et al.*, PRC 85 (2012) 044002].

FCNCs ('rare decays')

We have been talking a lot about FCNCs already in the context of mixing, but now we switch the focus to very rare FCNC decay modes.

Flavour-changing Neutral Currents (FCNCs) or 'rare decays' as a probe of New Physics

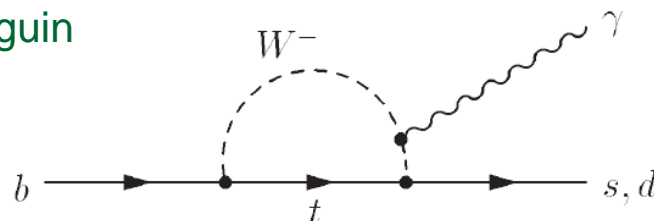
FCNC decays proceed through higher order diagrams → suppressed in SM and susceptible to New Physics contributions.

e.g. Penguin diagram (nomenclature introduced by John Ellis in 1977 after lost bet [[Ellis et al., NPB 131 \(1977\) 285](#)].)

Most interesting measurements involve EM & weak penguins, with photon or dileptons – precise predictions.

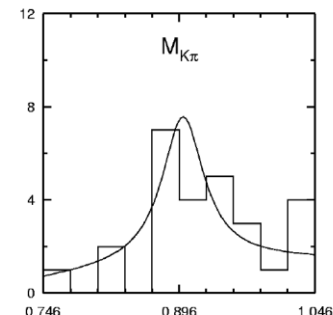
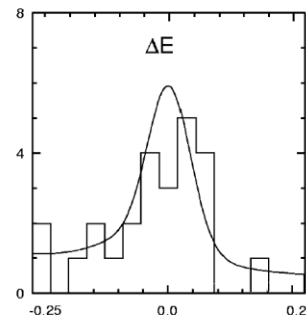
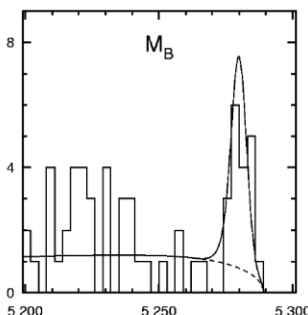


(EM) Radiative penguin



EM penguin first discovered by CLEO in $B \rightarrow K^*(892)\gamma$ ($BR \sim 10^{-5}$) [[CLEO, PRL 71 \(1993\) 674](#)].

Studies of radiative penguins still very important, but we will not discuss them further.



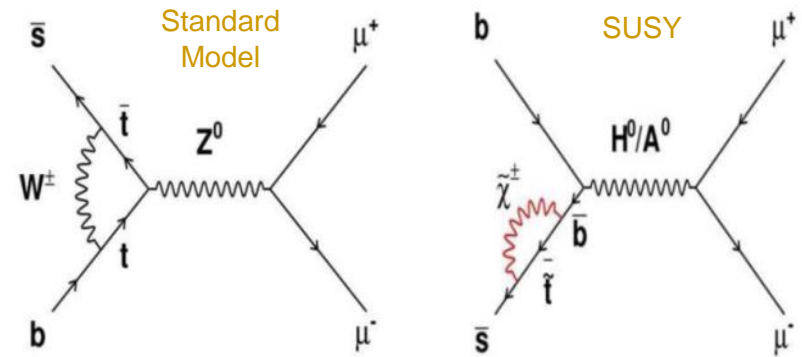
The golden modes: $B_s \rightarrow \mu^+ \mu^-$, $B^0 \rightarrow \mu^+ \mu^-$

These decay modes can only proceed through suppressed loop diagrams.

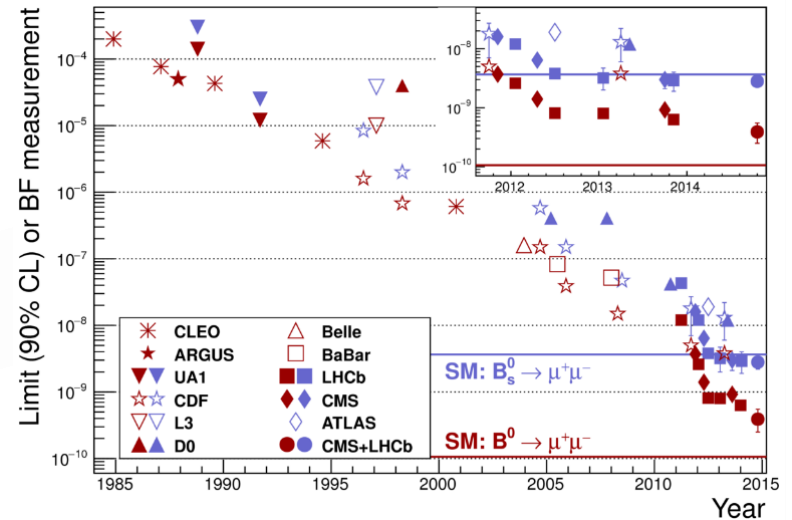
In SM they happen extremely rarely ($B_s \rightarrow \mu\mu \sim 4 \times 10^{-9}$, $B^0 \rightarrow \mu\mu$ 30x lower), but the rate is very well predicted (e.g. <5% for $B_s \rightarrow \mu\mu$).

Many models of New Physics (e.g. SUSY) can modify rate significantly !

A 'needle-in-the haystack' search, which has been pursued for over 25 years.



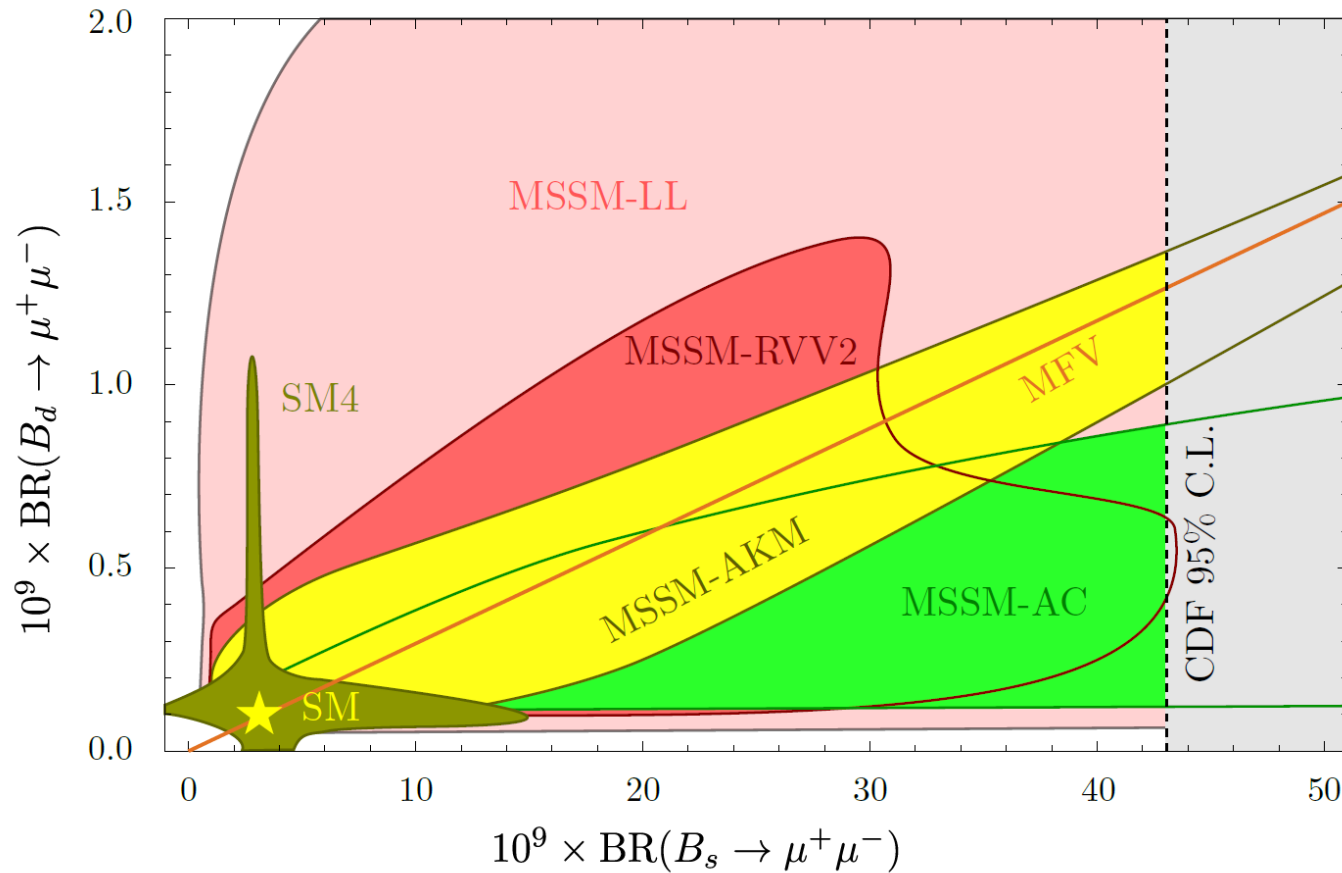
Decay channel	Upper limit
$B^0 \rightarrow e^+ e^-$	8.5
$B^0 \rightarrow \mu^+ \mu^-$	5.0
$B^0 \rightarrow \tau^+ \tau^-$	5.0



Before the LHC, Fermilab experiments were pushing the limits down towards 10^{-8} .

$B_s \rightarrow \mu^+ \mu^-$, $B^0 \rightarrow \mu^+ \mu^-$: the model killer

Historical plot from around the turn-on of the LHC, showing how a measurement of the BR of both modes provides powerful discrimination between New Physics models.



[D. Straub, arXiv:1012.3893]

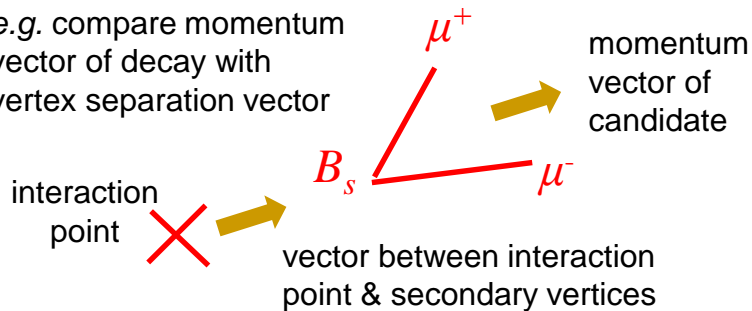
Finding the needle in the haystack

There are lots of B-decays that look rather similar to $B_s \rightarrow \mu\mu$. And 'rather similar' is very dangerous when you are searching for such a rare decay.

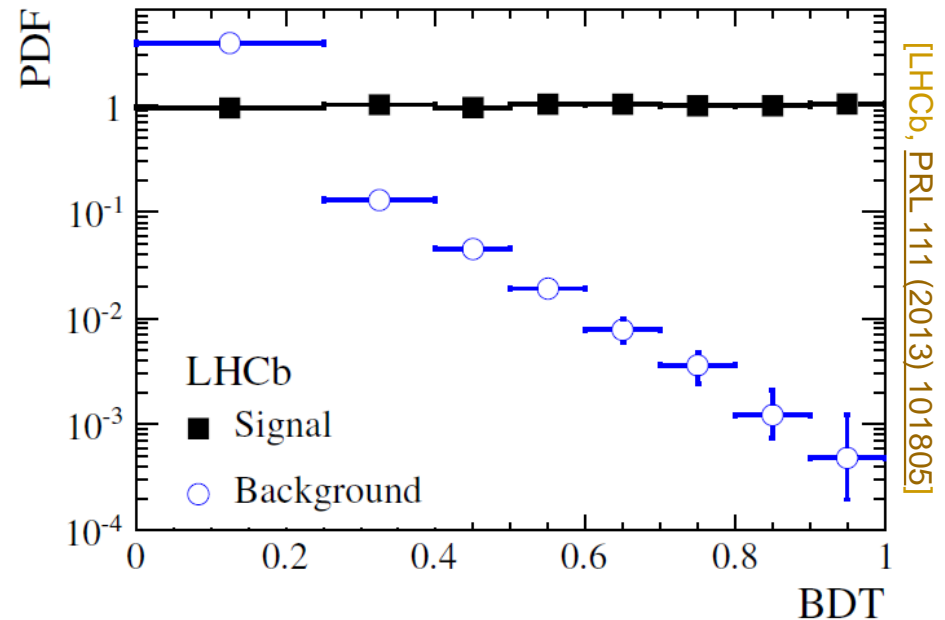
Most sensitive analyses (LHCb, CMS) do not rely on traditional 'cut-based' approach. Rather, they employ a sequence of two boosted decision trees (BDTs).

BDTs must not just search for a B-decay, as in trigger, but must look for one which is $B_s \rightarrow \mu\mu$

e.g. compare momentum vector of decay with vertex separation vector

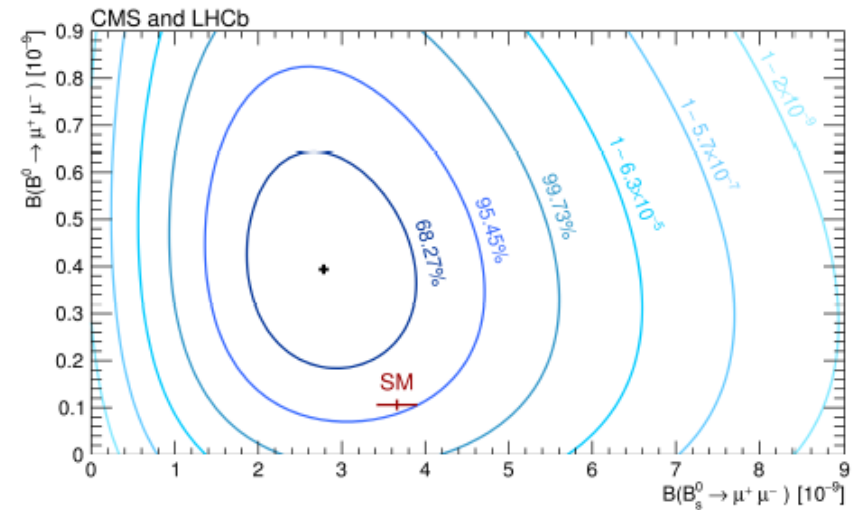
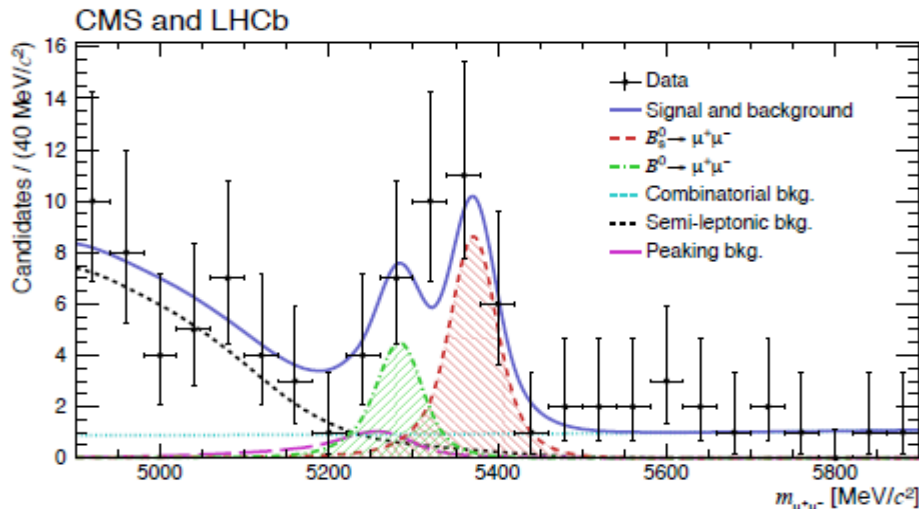


Above, just one of many signatures that are used. Where possible calibrate BDTs on data (e.g. same topology $B^0 \rightarrow K\pi$ decays). Normalise signal yield to $B_s \rightarrow J/\psi K$ or $B^0 \rightarrow K\pi$ to determine BR.



The search is over: $B_s \rightarrow \mu^+ \mu^-$ observed !

The signal finally showed up during Run 1, where LHCb found first evidence [[PRL 110 \(2013\) 021801](#)], & then a combined LHCb-CMS analysis yielded a 5σ observation [[Nature 522 \(2015\) 68](#)]. The BR, measured to 25%, agrees with the SM...



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8_{-0.6}^{+0.7}) \times 10^{-9} \quad (6.2\sigma)$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (3.9_{-1.4}^{+1.6}) \times 10^{-10} \quad (3.0\sigma)$$

[[arXiv:1411.4413](#),
[Nature 522 \(2015\) 68](#)]

...however the analysis also searched for the even rarer $B^0 \rightarrow \mu\mu$. Here there is also a hint of a signal. Picture is intriguing & provided encouragement for Run 2 !

LHCb $B^0_{(s)} \rightarrow \mu^+ \mu^-$ run 2 update

[PRL 118 (2017)
191801]

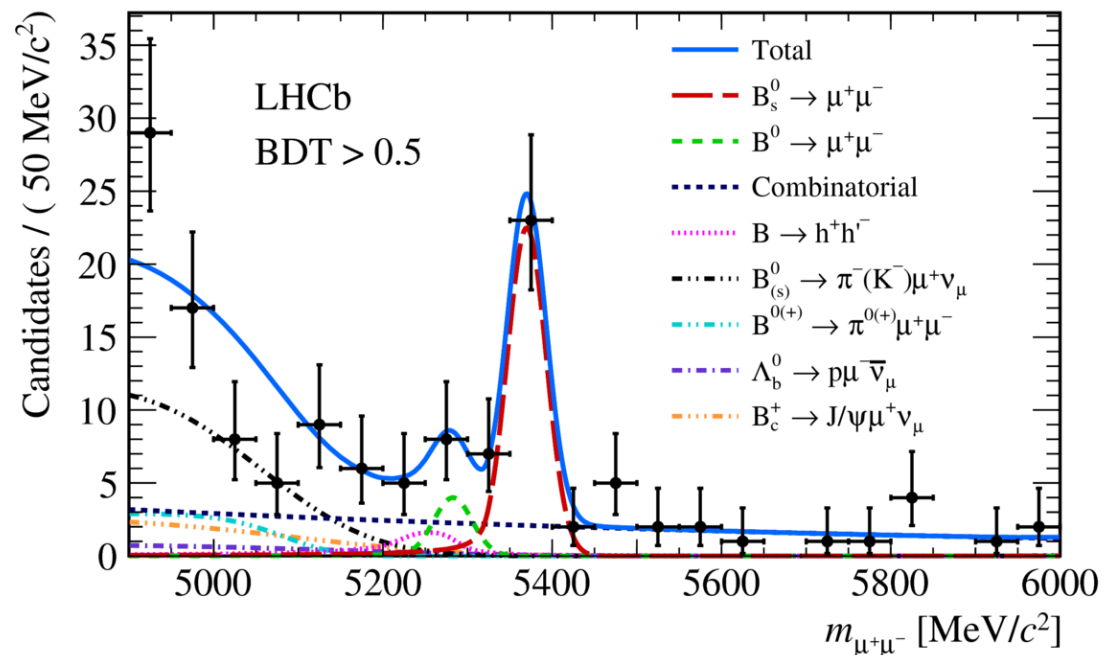
Early in Run 2 LHCb returned to this critical observable with an improved analysis (~50% combinatoric background than previously). Run 1 + 1.4 fb⁻¹ of Run 2 data.

- 7.8 σ signal & first single-experiment observation !

- Precise measurement of branching fraction

$$\mathcal{B}(B^0_s \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9}$$

- No evidence yet of the corresponding B^0 decay.



Uses only 1/4 of Run 2 data, so 'legacy' Run 1+2 result will be much more precise.

CMS $B^0_{(s)} \rightarrow \mu^+ \mu^-$ run 2 update

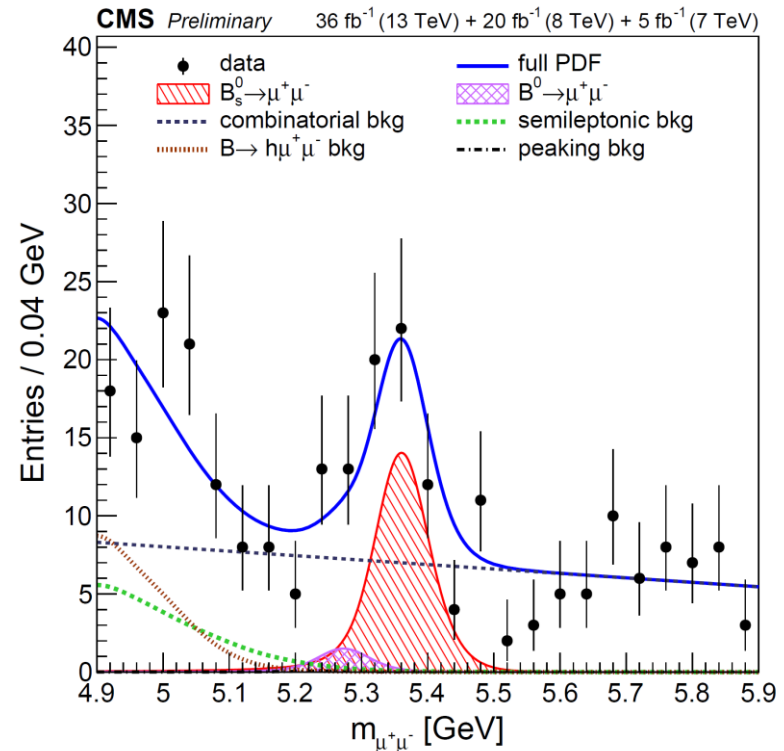
[CMS PAS
BPH-16-004]

Last month: a CMS preliminary update based on Run 1 (25 fb⁻¹) & 2016 Run 2 (36 fb⁻¹).

$$\mathcal{B}(B^0_s \rightarrow \mu^+ \mu^-) = [2.9^{+0.7}_{-0.6} (\text{exp}) \pm 0.2 (\text{frag})] \times 10^{-9}$$

The 'frag' systematic concerns knowledge of ratio of production of B_s to B^+ mesons (*i.e.* fragmentation). This enters because of $B^+ \rightarrow J/\psi K^+$ normalisation mode.

Measured by LHCb and extrapolated into kinematic acceptance of CMS.



Also this year, ATLAS published a 2015-16 run 2 update [[JHEP 04 \(2019\) 098](#)] to augment their Run 1 result [[EPJC 76 \(2016\) 513](#)]. We await full Run 2 results from all experiments !

The state of play

LHCb

[PRL 118 (2017) 191801]

$BR(B_s \rightarrow \mu\mu)$ $3.0^{+0.7}_{-0.6} \times 10^{-9}$
 $BR(B^0 \rightarrow \mu\mu)$
 [upper limit
 @ 95% C.L.] $< 3.4 \times 10^{-10}$

CMS (prelim)

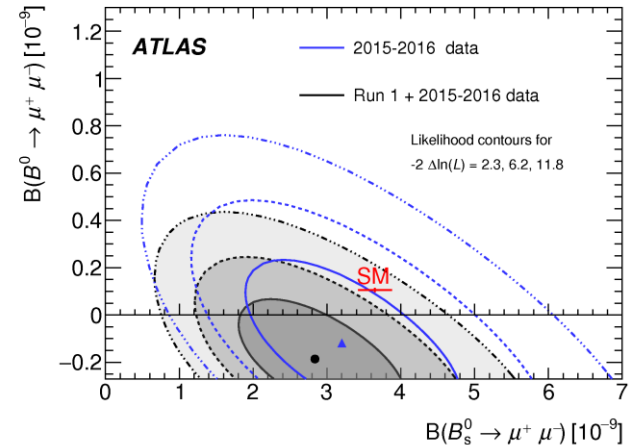
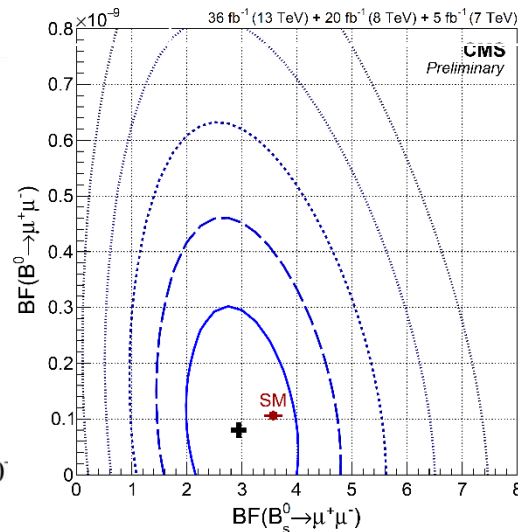
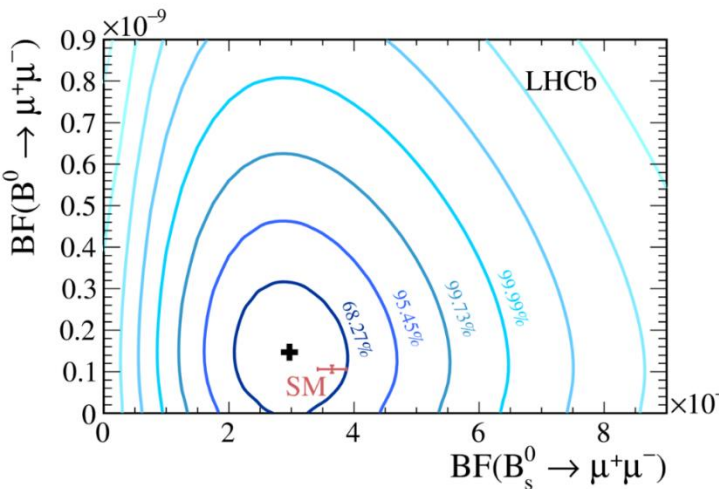
[CMS PAS BPH-16-004]

$2.9^{+0.7}_{-0.6} \times 10^{-9}$
 $< 3.6 \times 10^{-10}$

ATLAS

[JHEP 04 (2019) 098]

$2.8^{+0.8}_{-0.7} \times 10^{-9}$
 $< 2.1 \times 10^{-10}$

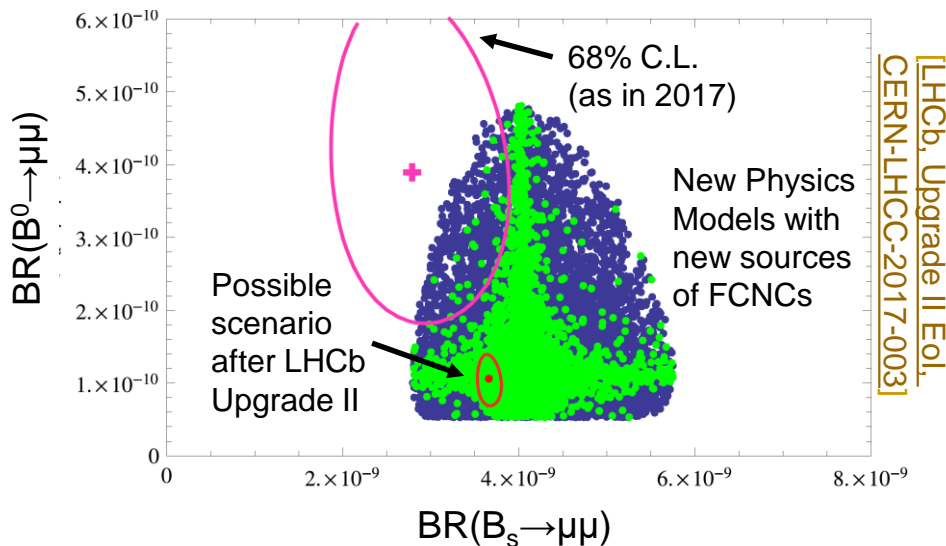
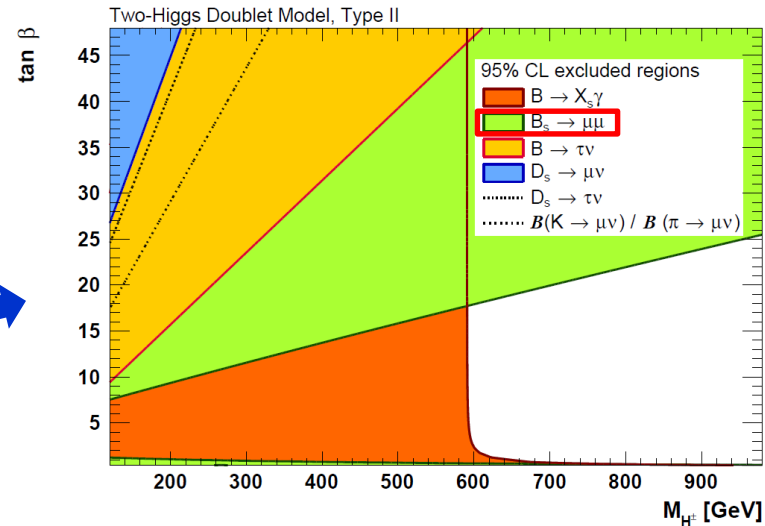


- Each result is compatible with the SM;
- $B_s \rightarrow \mu\mu$ measurements are clustering at a slightly lower value than SM (at level of $\sim 2\sigma$);
- $B^0 \rightarrow \mu\mu$ is proving elusive;
- Full Run 2 results will be interesting;

Lessons from, & future of, $B^0_{(s)} \rightarrow \mu\mu$ measurements

- Prior to LHC turn on, an enhanced $BR(B_s \rightarrow \mu\mu)$ was one of the great hopes for a rapid discovery of New Physics. This hope has not been realised.
- Nonetheless, the absence of an enhancement is a very powerful input in excluding certain classes of New Physics model.

e.g. 95% CL excluded region in M_{H^\pm} vs. $\tan\beta$ space for two-Higgs doublet model [Gfitter group, Hallet *et al.*, EPJC 78 (2018) 675].



- Better measurements are *essential*, as we are still far from theory limit (which will improve). Even truer for ratio $BR(B_s \rightarrow \mu\mu)/BR(B^0 \rightarrow \mu\mu)$. These decays still have much to tell us!
- Next step in the journey will be observation of $B^0 \rightarrow \mu\mu$.

Unlocking new observables with $B_s \rightarrow \mu^+ \mu^-$

Remarkably, the sample of $B_s \rightarrow \mu\mu$ decays now available is sufficient to begin probing new observables. *E.g.*, since the sample is in fact constituted of both B_s & B_s bar mesons, a lifetime measurement brings very valuable new information.

The effective lifetime [[K. De Bruyn et al., PRL 109 \(2012\) 041801](#)]:

$$\tau_{\mu^+\mu^-} = \frac{\tau_{B_s^0}}{1 - y_s^2} \left(\frac{1 + 2A_{\Delta\Gamma}^{\mu^+\mu^-} y_s + y_s^2}{1 + A_{\Delta\Gamma}^{\mu^+\mu^-} y_s} \right)$$

where

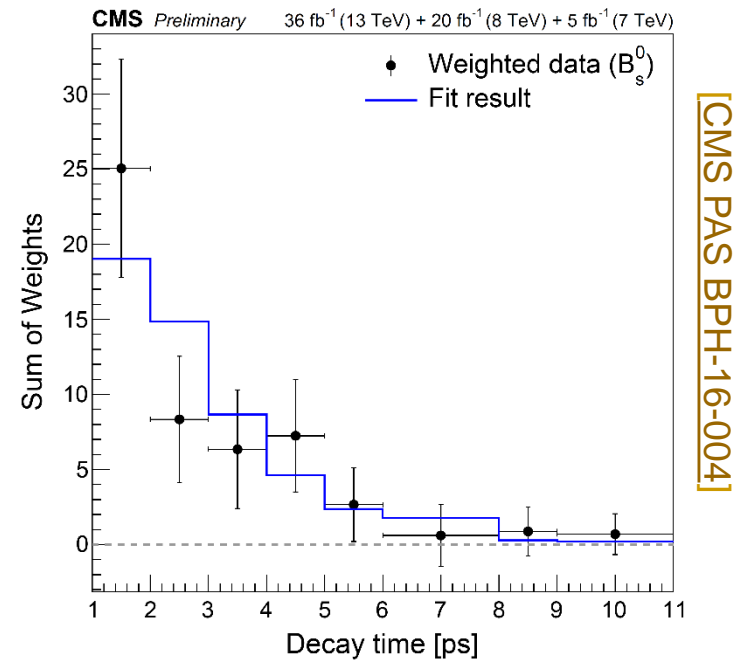
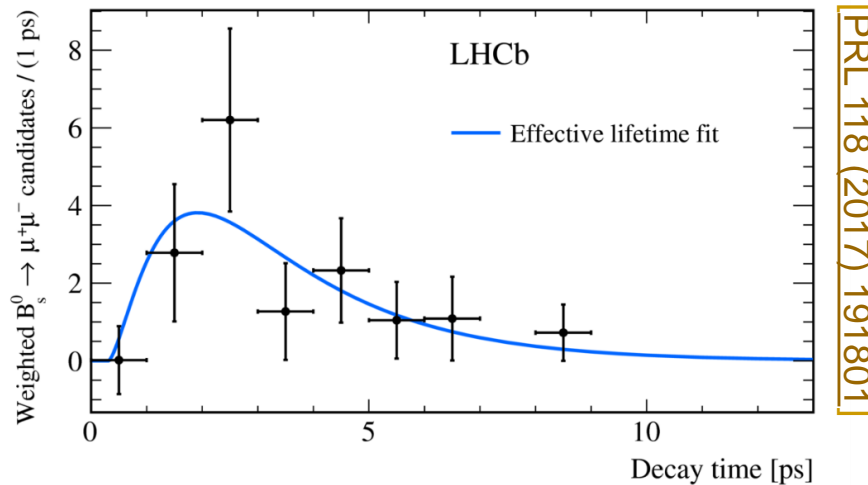
- $y_s \equiv \tau_{B_s^0} \Delta\Gamma / 2 \approx 0.06$, $\Delta\Gamma$ being the lifetime splitting between the mass eigenstates;
- $A_{\Delta\Gamma}^{\mu\mu}$ is a term that is 1 in SM, but can take any value between -1 & 1 for New Physics.

Accessing $A_{\Delta\Gamma}^{\mu\mu}$ through $\tau_{\mu\mu}$ tells us things that the BR alone does not.

Unlocking new observables with $B_s \rightarrow \mu^+ \mu^-$

Remarkably, the sample of $B_s \rightarrow \mu\mu$ decays now available is sufficient to begin probing new observables. *E.g.*, since the sample is in fact constituted of both B_s & B_s bar mesons, a lifetime measurement brings very valuable new information.

Proof-of-principle measurements conducted by LHCb and CMS:



During HL-LHC era these will reach very interesting levels of precision.

One may also dream of performing flavour-tagged CP asymmetry measurements !