Vector-like leptonic dark matter, neutrino mass and collider signatures

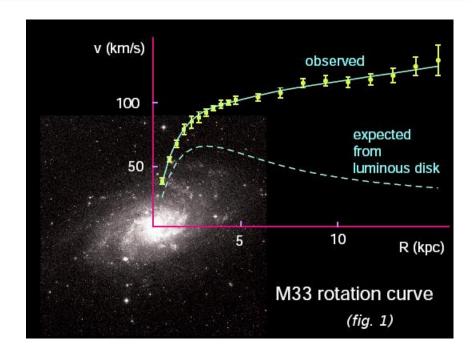
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Introduction

Evidence of DM from rotation curve

$$\frac{mv_r^2}{r} = \frac{GM_rm}{r^2}$$



$$v_r \sim rac{1}{r^{1/2}}$$

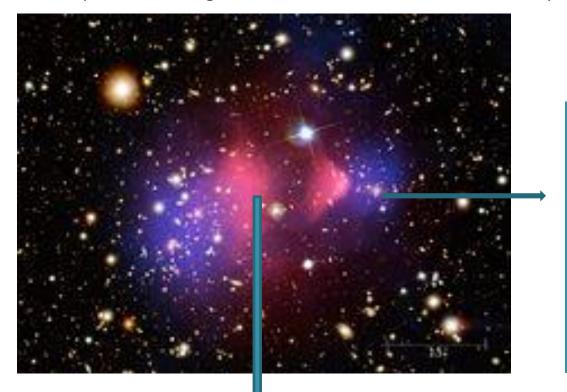
 $v_r \sim \frac{1}{r^{1/2}}$ (Keplerian Decline)



Missing mass ~ Non-baryonic

Evidence of DM in bullet cluster

(Collision of galaxies in Bullet cluster I E 0657-56)

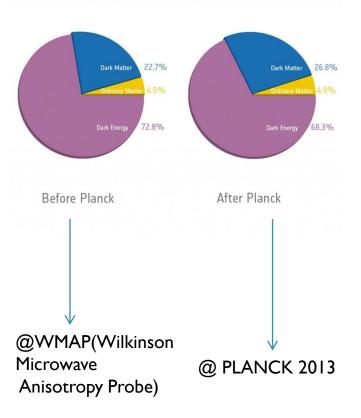


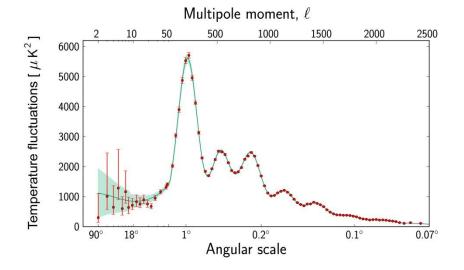
(Blue color)
Dark matter
seen through
gravitational
lensing and is
found to be 7
times larger
than baryonic
mass.

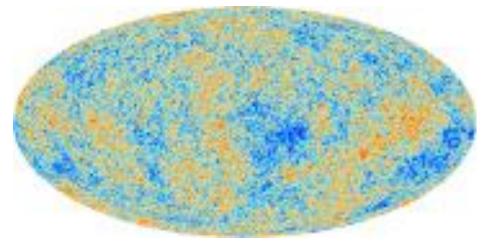
Markevitch et.al, Astro Phy J, 2004

(Pink color) Hot gas seen through X-ray by Chandra X-ray observatory at the central part

Evidence of DM in CMB







Nature of Dark Matter...

From the astrophysical evidences of dark matter one infers that...

- ✓ DM should be a massive particle and hence interact gravitationally.
- ✓ It is electrically neutral and colorless. Therefore it could hide
 itself easily.
- ✓ It is stable on the cosmological time scale and therefore the large scale structure exists.

However, We don't know ...

Mass of DM=?
Spin of DM=?, Charge of DM=?
Interaction apart from gravity?
Relic abundance
(symmetric/asymmetric?)

Many unanswered questions!

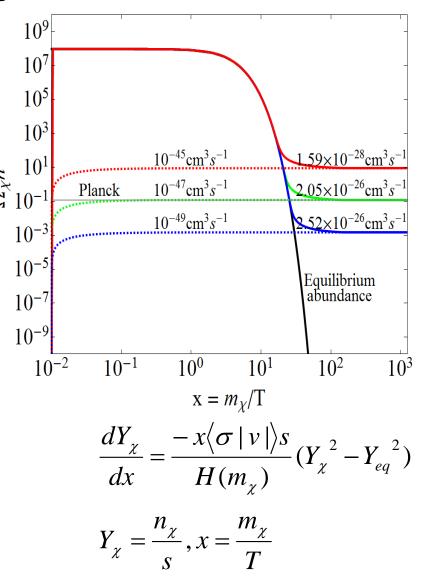


Q. How to probe the DM at terrestrial laboratories, which is required for the existence of our Universe?

Is DM a WIMP (Gravity+ weak)?

Steigman and Turner, 1984

The DM is assumed to be in equilibrium in the early Universe via the weak interaction processes. As the temperature, due to expansion of the Universe, falls below the mass scale of DM, the latter gets freeze-out from the thermal bath and gives the correct relic abundance.



$$\Omega_{DM}h^{2} = \frac{1.1 \times 10^{9} GeV^{-1}x_{F}}{g_{*}^{1/2} M_{pl} \langle \sigma | v | \rangle_{F}} = 0.1198 \pm 0.0026$$

Analytical estimation of a WIMP relic density

The observed relic abundance of DM by WMAP and PLANCK

$$<\sigma |v|>|_{E} \approx 3 \times 10^{-26} cm^{3} / sec \approx 2.6 \times 10^{-9} GeV^{-2}$$

$$\approx O(10^{-36})cm^2$$



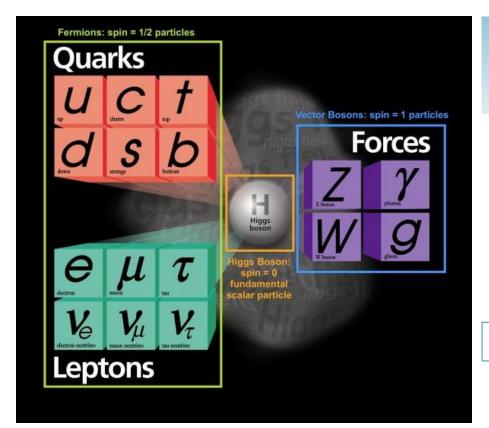
Which is typically a weak interaction cross-section.

WIMP Miracle

Therefore one believes that DM could be a WIMP.

Dark matter: Physics beyond the SM?

DM: The physics beyond the SM



The only particles in SM which seem to satisfy some properties of DM are neutrinos:

$$\Omega_{\nu}h^{2} = \frac{\sum m_{\nu}}{91.5eV} \approx 0.0024$$

$$<<\Omega_{DM}h^{2}$$

Cowsik and McClelland, PRL 1972

So, we need to look for a candidate of DM in the beyond standard model of particle physics, which is probably heavy (> a few GeV).

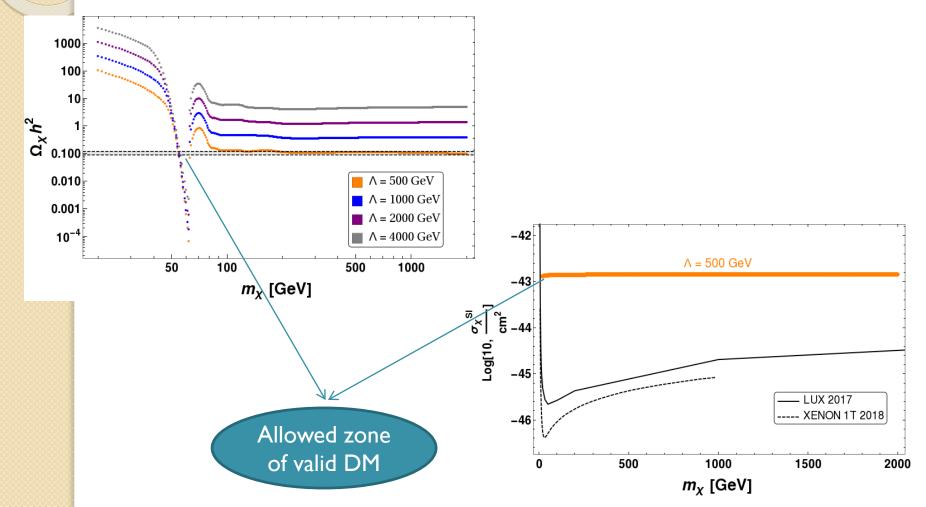
Lee and Weinberg, PRL 1977

Vector-like fermions as DM candidates in BSM scenarios

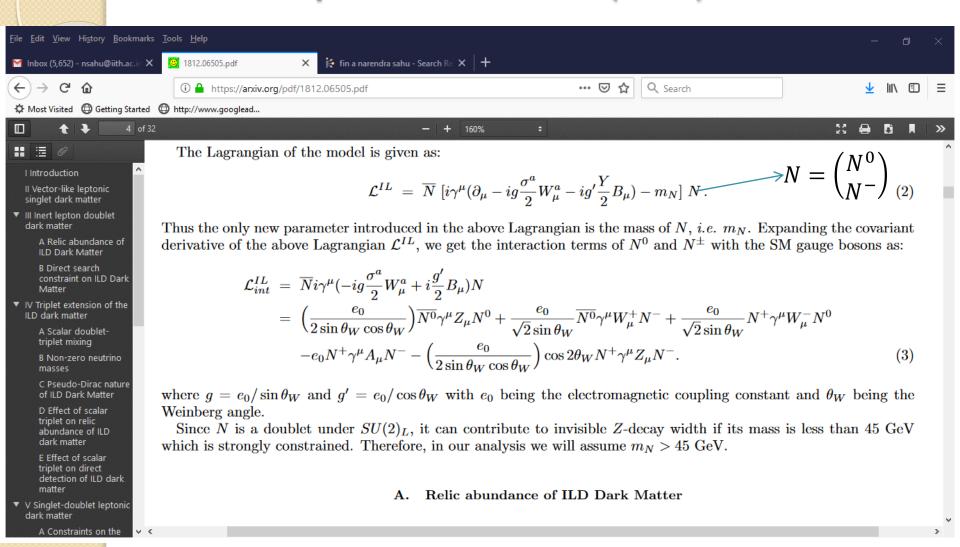
- (1) S. Bhattacharya, Nirakar Sahoo and N. Sahu, PRD93, 2016
- (2) S. Bhattacharya, S Patra, Nirakar Sahoo, N.Sahu, JCAP 1606, 2016
- (3) S. Bhattacharya, Nirakar Sahoo and N. Sahu, PRD96, 2017
- (4) S. Bhattacharya, Purusottam Ghosh, Nirakar Sahoo and **N. Sahu**, 1812.06505 (Front.in Phys.7 (2019)
- (5) B. Barman, S. Bhattacharya, P. Ghosh, S. Kadam and **N. Sahu**, 1902.01217 (PRD 100, 2019)

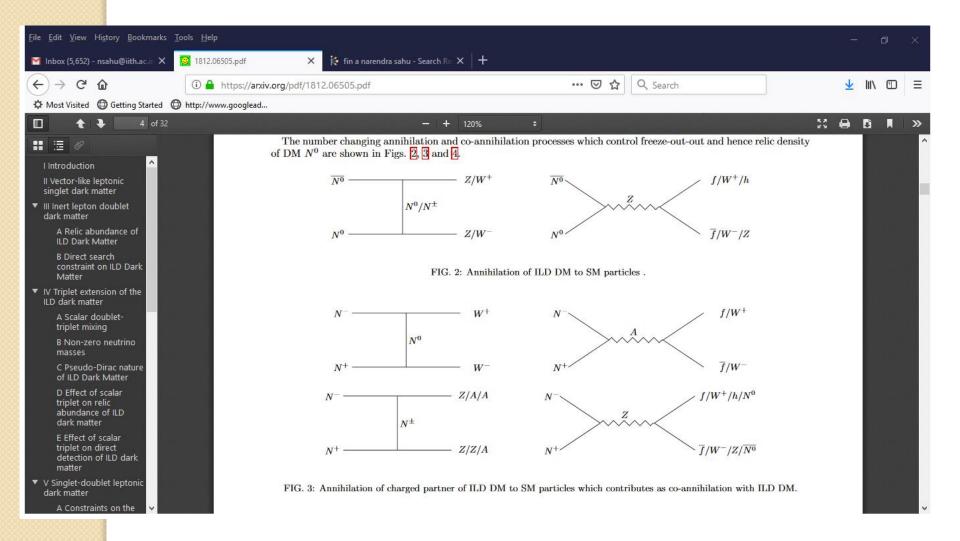
Vector-like singlet fermion DM

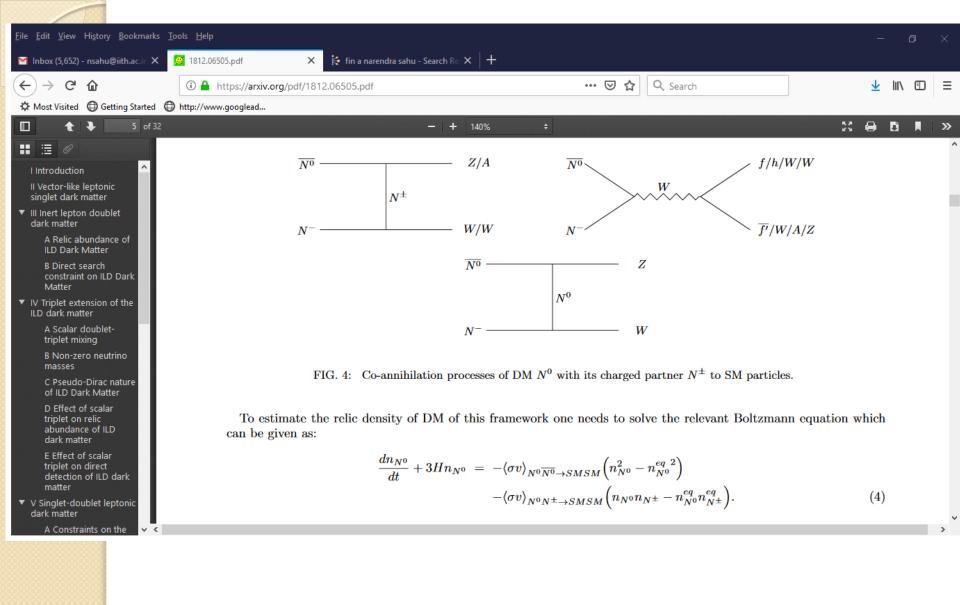
$$\mathcal{L}_{DM} = \overline{\chi} (i \gamma^{\mu} \partial_{\mu} - m_{\chi}) \chi - \frac{1}{\Lambda} (H^{\dagger} H - \frac{v^{2}}{2}) \overline{\chi} \chi$$

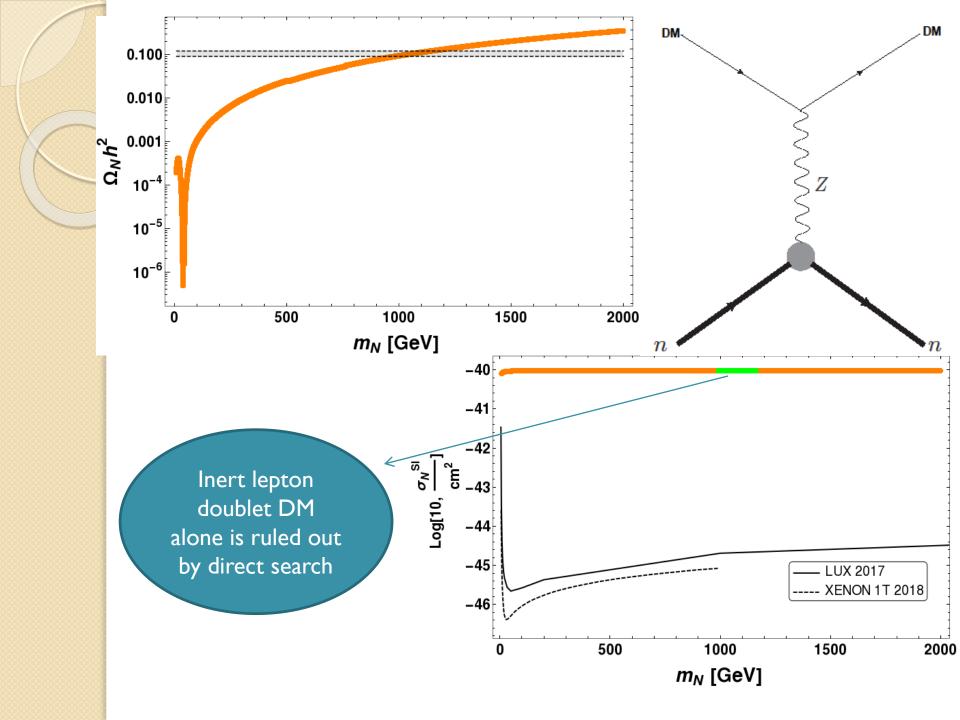


Inert lepton doublet (ILD) DM

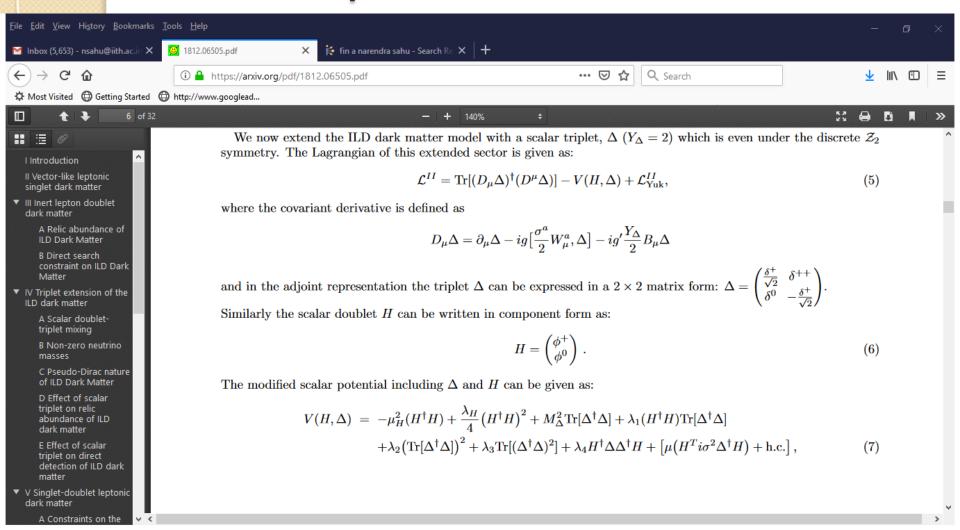








Scalar triplet extension of ILD DM



Where Δ is a scalar triplet and does not acquire any vev. After electroweak phase transition, it acquires a small induced vev.

$$\mathcal{L}_{yuk} = \frac{1}{\sqrt{2}} [(f_L)_{\alpha\beta} \overline{L_{\alpha}^{c}} i \tau_2 \Delta L_{\beta} + f_N \overline{N_{\beta}^{c}} i \tau_2 \Delta N + h.c.$$

Majorana mass of neutrino:

Lepton number violation by two units

$$M_{v} = f_{L} < \Delta > = -f_{L}f_{H} \frac{v^{2}}{M_{\Delta}}$$

$$\rho = \frac{M_w^2}{M_Z^2 \cos^2 \theta_w} = \frac{\frac{g^2}{4} (\langle H \rangle^2 + 2 \langle \Delta \rangle^2)}{\frac{g^2 + g'^2}{4 \cos^2 \theta_w} (\langle H \rangle^2 + 4 \langle \Delta \rangle^2)} = 1.00037 \pm 0.00023$$

$$\Rightarrow <\Delta >< 3.64 GeV$$

A free lunch

The scalar triplet also induces a Majorana mass to DM, which does not affect the relic abundance of DM, but it evades the constraints from Z-mediated direct detection. HOW?

$$-\mathcal{L} = M_N \overline{N^0} N^0 + f_N \overline{(N^0)^c} N^0 \langle \Delta \rangle$$

The Majorana mass splits the DM (Dirac fermion) into two pseudo-Dirac fermions with a small mass splitting:

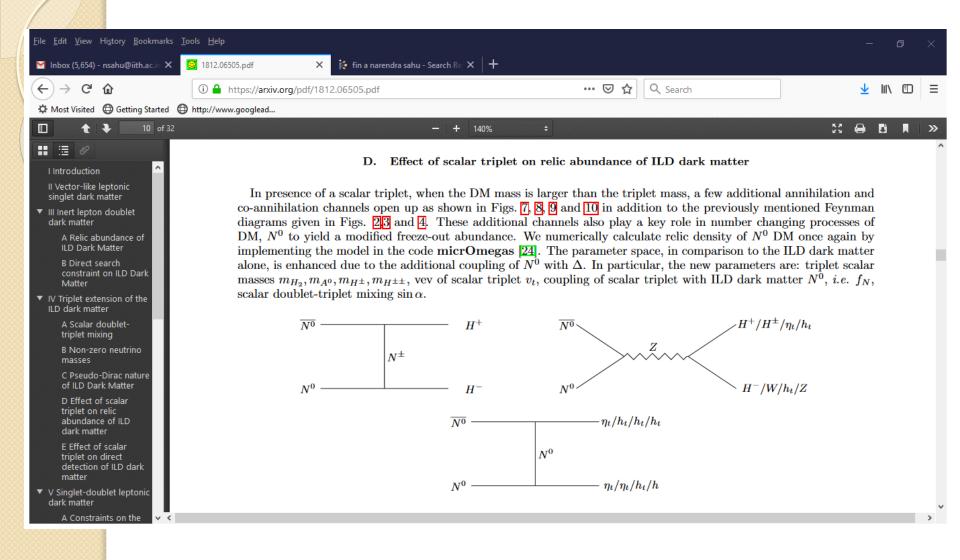
$$\begin{pmatrix} m & M_N \\ M_N & m \end{pmatrix}$$

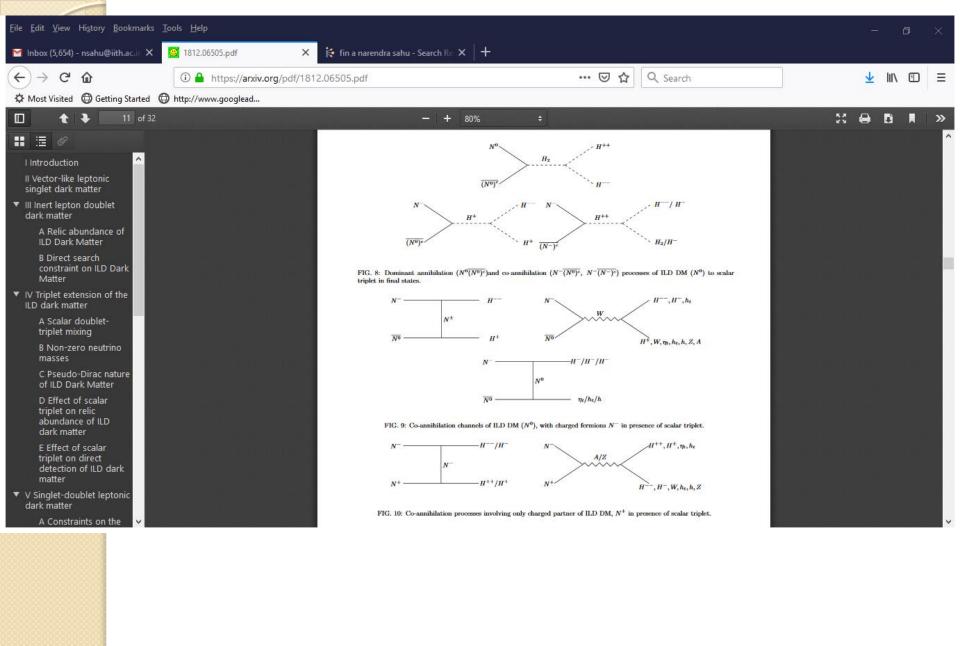
$$\delta = 2m$$

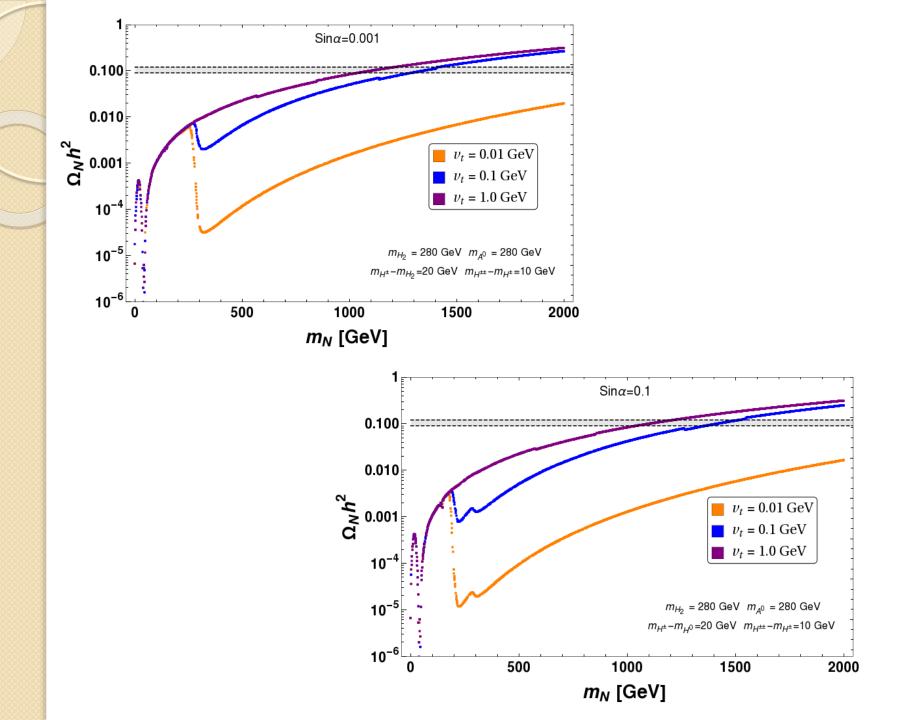
$$= 2f_N < \Delta >= -2f_N f_H \frac{v^2}{M_\Delta} = O(MeV - GeV)$$

$$R = \frac{M_V}{\delta} = \frac{f_L}{f_V} < 10^{-5}$$

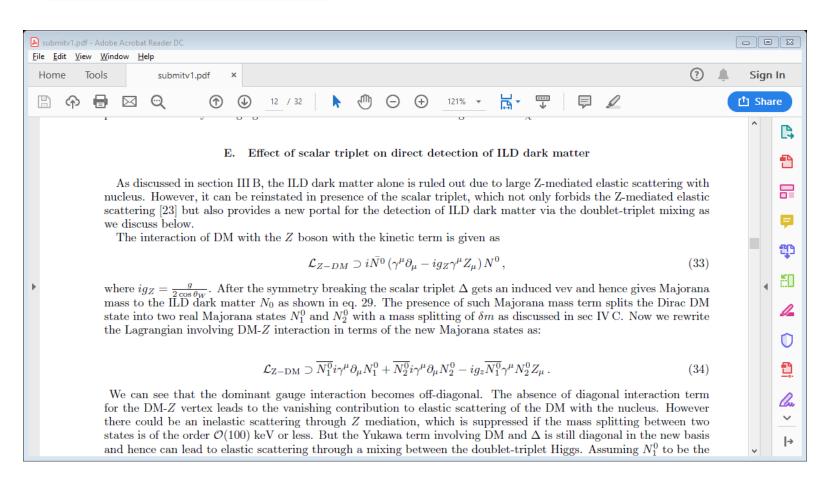
This forbids the DM-nucleon scattering via Z-mediated process, which is good for us.

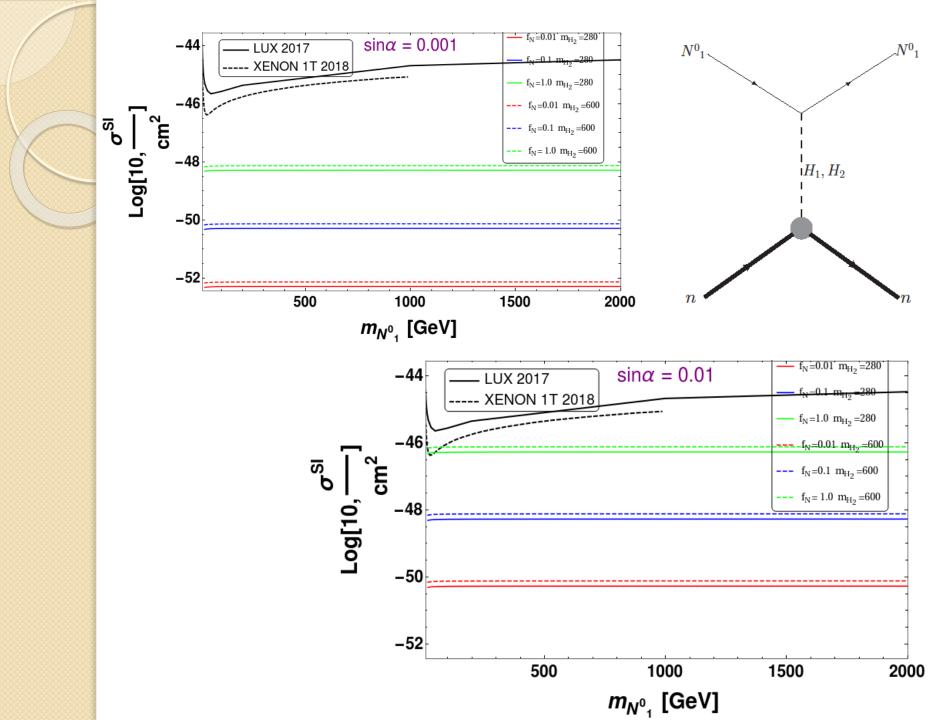






Effect of scalar triplet on direct detection of ILD dark matter





Thus the scalar triplet reinstate the ILD dark matter by splitting the Dirac fermion into two pseudo-Dirac states. However, it can not reduce the mass of DM to below TeV scales. Therefore, a complementary search of ILD dark matter at collider lacks any signal.

Singlet-Doublet mixed Fermion DM

We overcome the problem of small relic abundance by introducing a vector-like singlet fermion χ^0 , which mixes with the neutral component of the doublet fermion and decreases the annihilation cross-section. As a result we get the correct relic abundance.

$$\mathcal{L}_{DM} = M_N \overline{N} N + M_{\chi} \overline{\chi^0} \chi^0 + [Y \overline{N} \tilde{H} \chi^0 + h.c.]$$

$$+ \overline{N} i \gamma^{\mu} D_{\mu} N + \overline{\chi^0} i \gamma^{\mu} \partial_{\mu} \chi^0$$
where
$$N = \binom{N^0}{N^-} \equiv (1,2,-1), H = \binom{H^+}{H^0} \equiv (1,2,1), \chi^0 \equiv (1,1,0)$$

For various purpose see: hep-th/0501082, hep-ph/0510064, arXiv: 0705.4493, arXiv:0706.0918, arXiv:0804.4080, arXiv: 1404.4398 arXiv:1109.2604, arXiv:1311.5896, arXiv:1504.07892, arXiv:1505.03867

Singlet-Doublet mixed Fermion DM

Under \mathbb{Z}_2 symmetry both χ^0 and N are odd. As a result the DM emerges as a mixture of singlet fermion χ^0 and the neutral component of the vector-like doublet fermion N.

After EW phase transition the mass matrix for neutral vector-like fermions is given by

$$egin{pmatrix} igl(\overline{N^0} & \overline{\chi^0} igg) igg(M_N & m_D \ m_D & M_\chi igg) igg(\chi^0 igg) \end{pmatrix}$$

Where
$$m_D = Y < H >$$

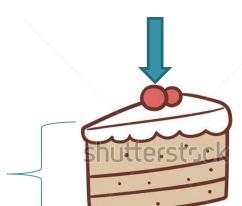
$$M_{1} = M_{\chi} - \frac{m_{D}^{2}}{M_{N} - M_{\chi}}; N_{1} = \cos\theta\chi^{0} + \sin\theta N^{0}$$

$$M_{2} = M_{N} + \frac{m_{D}^{2}}{M_{N} - M_{\chi}}; N_{2} = \cos \theta N^{0} - \sin \theta \chi^{0}$$

$$M^{\pm} = M_1 \sin^2 \theta + M_2 \cos^2 \theta = M_N; N^{\pm}$$

$$\tan 2\theta = \frac{m_D}{M_N - M_{\chi}}$$

The lightest particle is the N_1 , which is candidate of dark matter with appropriate mixing angle Θ



DOUBLET

$$sin\theta \leq 0.1$$
 \longrightarrow From exclusion of direct detection of dark matter

$$\sin \theta \ge O(10^{-5})$$
 — NLSP decay before the DM freezes out, so that no over production of dark matter

We will scan the parameter space within the the given range of singlet-doublet mixing:

$$10^{-5} < \sin \theta < 0.1$$

Relic density of mixed Fermion DM

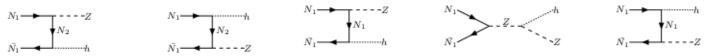
$$\Omega_{N_1} h^2 = \frac{1.09 \times 10^9}{g_*^{1/2} (M_{pl} / GeV)} \frac{1}{J(x_f)}$$

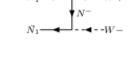
$$J(x_f) = \int_{x_f}^{\infty} \frac{\langle \sigma | v | \rangle_{eff}}{x^2} dx$$

Griest and Secklel: PRD 1991

Annihilation processes

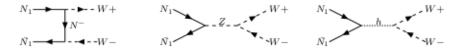
$$N_1 \overline{N_1} \rightarrow SM$$







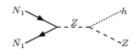
 N_1 N_1 N_2 N_1 N_2 N_3 N_4 N_4 N_5 N_5

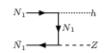


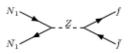


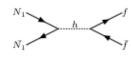


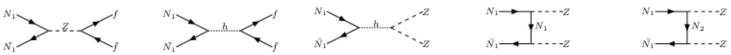


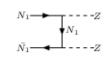














Co-annihilation process

$$N_1N_2 \rightarrow SM$$



$$N_1$$
 $W+$ N_2 $W-$



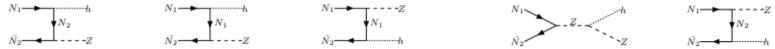


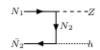


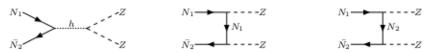










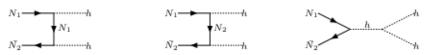




$$N_1$$
 N_2
 N_2
 N_2





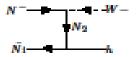


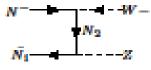
Co-annihilation process

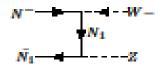
$$N_1N^- \rightarrow SM$$

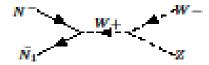


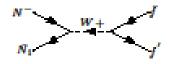




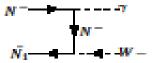








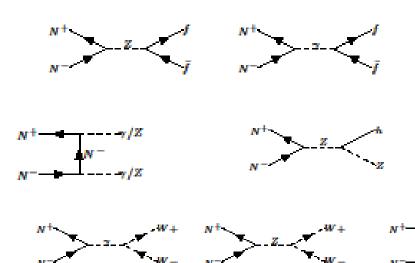
$$N^ N^+$$
 N^+
 N_1



$$N^ W^+$$
 \bar{N}_1

Co-annihilation process

$$N^+N^- \rightarrow SM$$

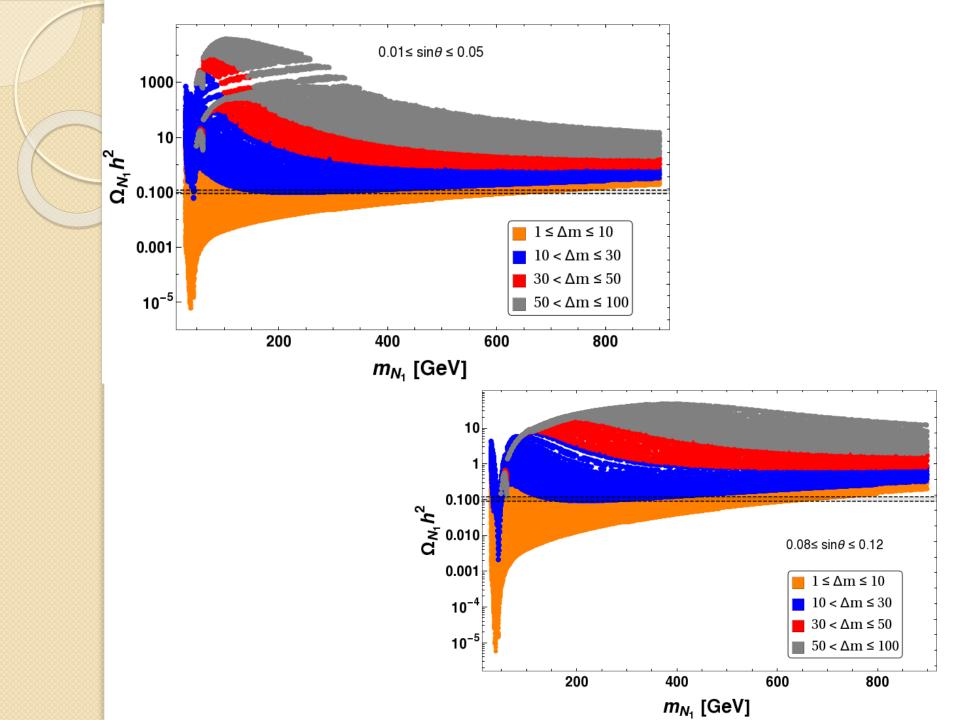


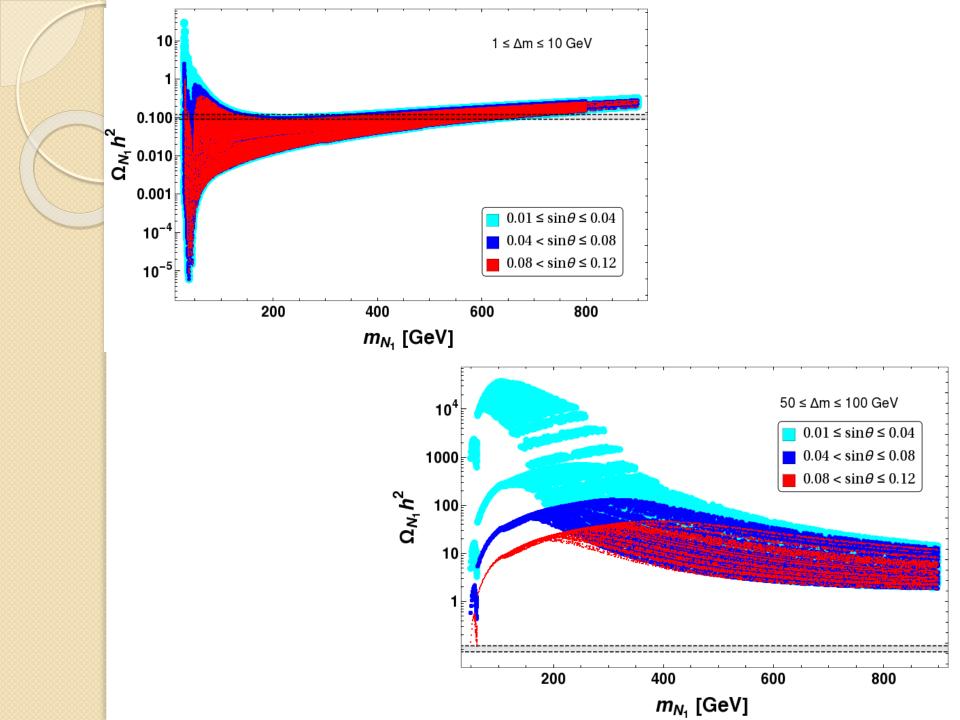
Note: These diagrams don't depend on singlet-doublet mixing. So in the small mixing limit these diagrams give relic abundance of dark matter.

Note: There are many additional channels in presence of the scalar triplet, which we have not drawn here.

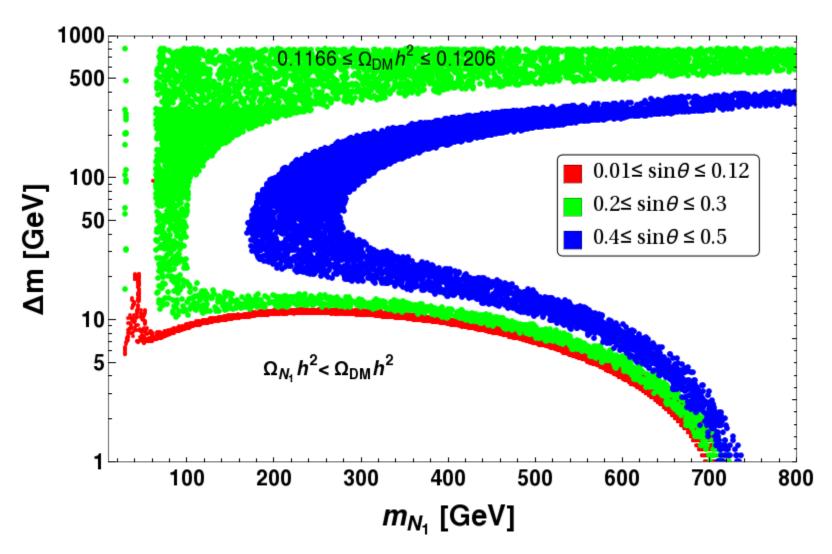
We look for the observed relic abundance in the parameter space spanned by

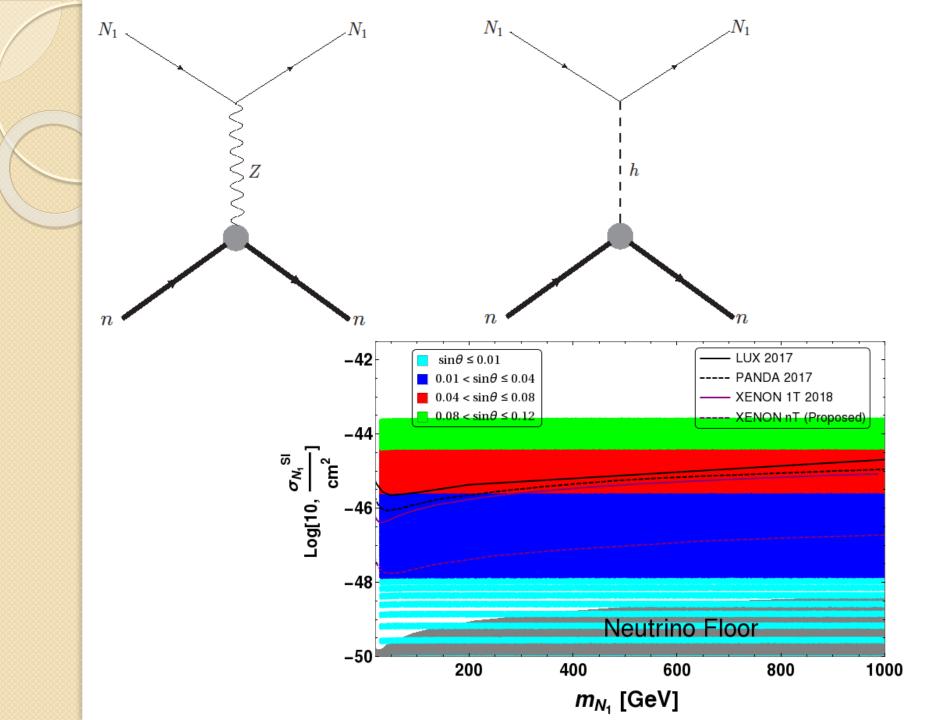
$$M_1, M_2 \approx M^{\pm}, \sin \theta$$
 $Y = \frac{\Delta M \sin 2\theta}{2v}$

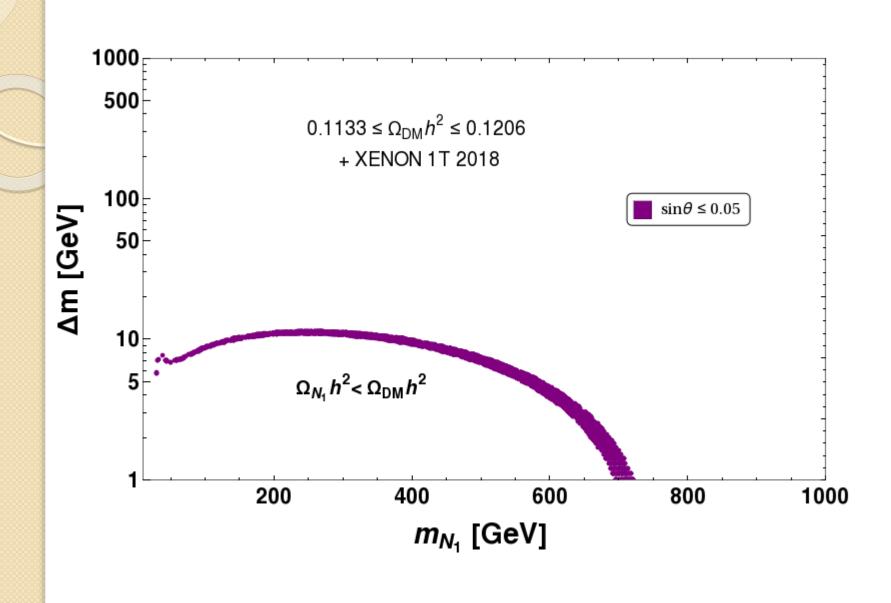




$$Y = \frac{\Delta M \sin 2\theta}{2v}$$

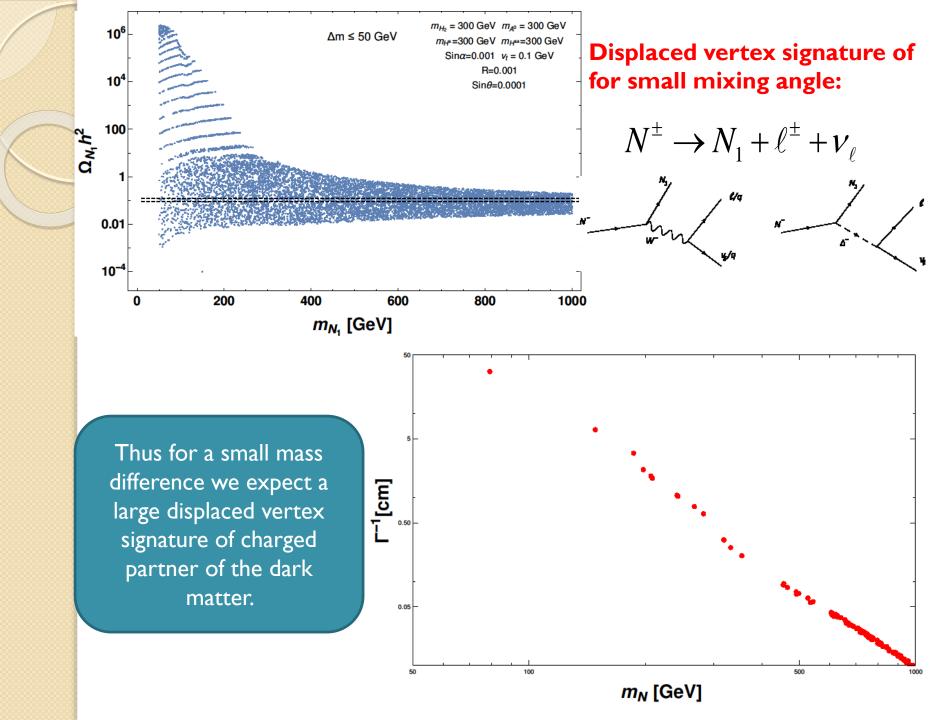






Small singlet-doublet mixing

Testing the Hypothesis at collider via displaced vertex signature...

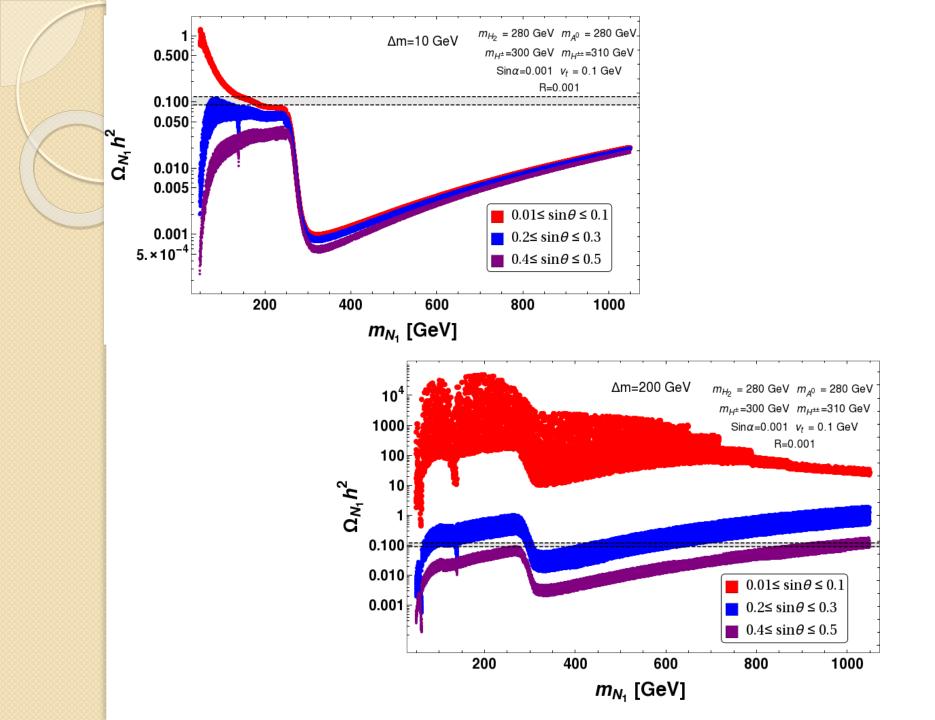


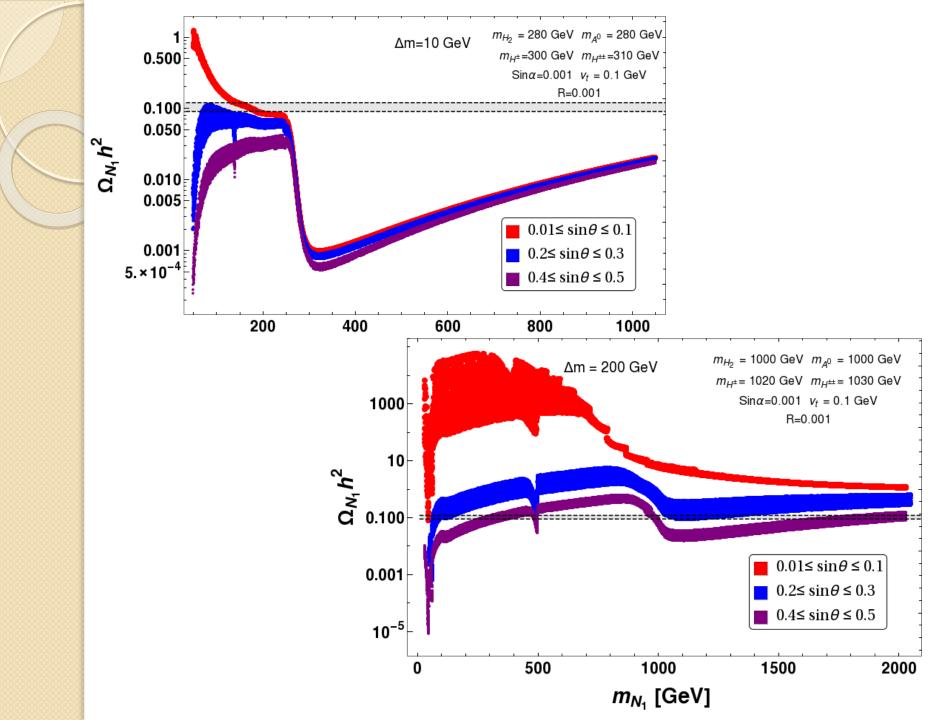
Effect of scalar triplet on Singlet-Doublet fermion DM

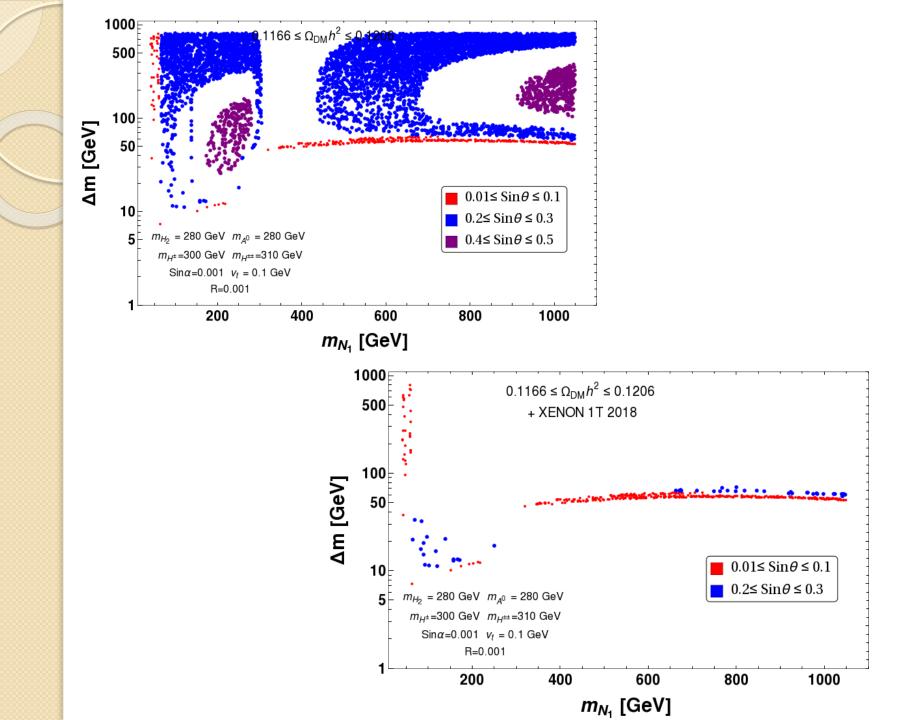
- (I) The scalar triplet generate sub-eV masses of active neutrinos.
- (2) It also splits the singlet-doublet DM in to two pseudo-Dirac states with a mass splitting of order 100 keV, which helps in forbidding the Z-mediated direct detection process.

$$\delta m = 2\sqrt{2}f_N \sin\theta^2 < \Delta >$$

$$R = \frac{M_v}{\delta m} < 10^{-3}$$







Conclusions

- (I)The observed relic abundance of DM implies that its freeze-out cross-section (~0.1pb) is typically a weak interaction cross-section. So it is largely believed that the DM is a WIMP.
- (2)We studied the case of a mixed (singlet+doublet) leptonic DM which satisfies the relic abundance in a large parameter space.
- (3) The spin independent direct detection cross-section is within the reach of Xenon-IT.
- (4) The displaced vertex signature of the charged partner of DM looks promising.
- (5)In presence of a scalar triplet large singlet-doublet mixing is allowed and hence lead to new collider signatures.

