

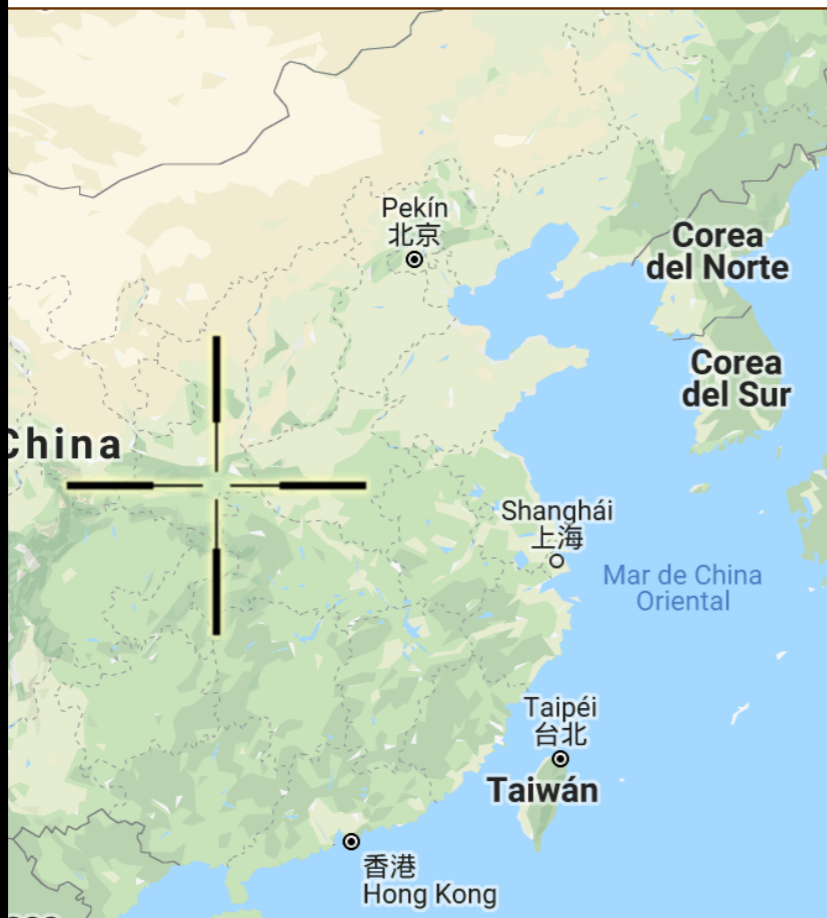
FLASY 上海 合肥 2019 中國

Dissecting a derivative effective operator:
3-loop neutrino masses and their links to
dark matter



Maximiliano A. Rivera U*
Universidad Técnica Federico Santa María,
Chile

*In collaboration with Michael Gustafsson y José M. No



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Open Questions

- What is the mechanism that gives small neutrinos masses?
- What is its particle nature: Dirac or Majorana?
- What is the origin of the flavor mixing structures?

Dark Matter

- What is its nature?
 - Few properties known, but many candidates

How to make a model linking these questions?

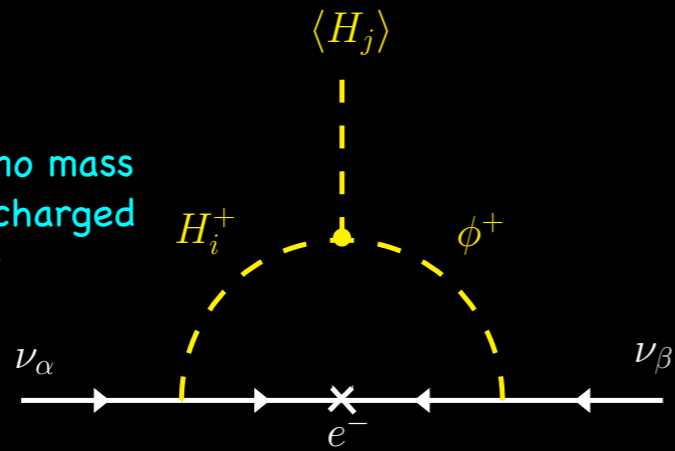
What are its experimental tests/constraints?

History

History

Zee Model

The first radiative neutrino mass mechanism: extra single charged scalar singlet + a doublet

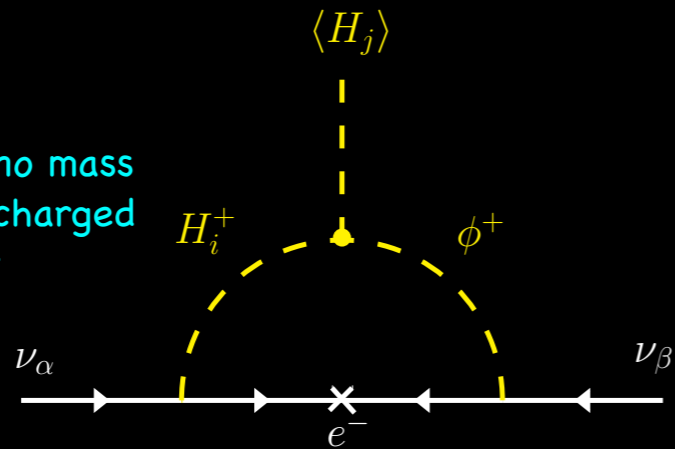


A. Zee, Phys. Lett. B 93 (1980) 389

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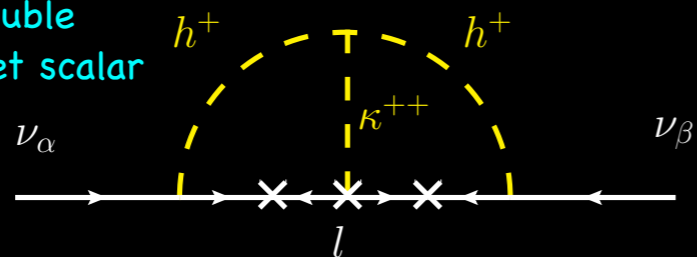
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Zee-Babu Model

An extra single and double charged complex singlet scalar

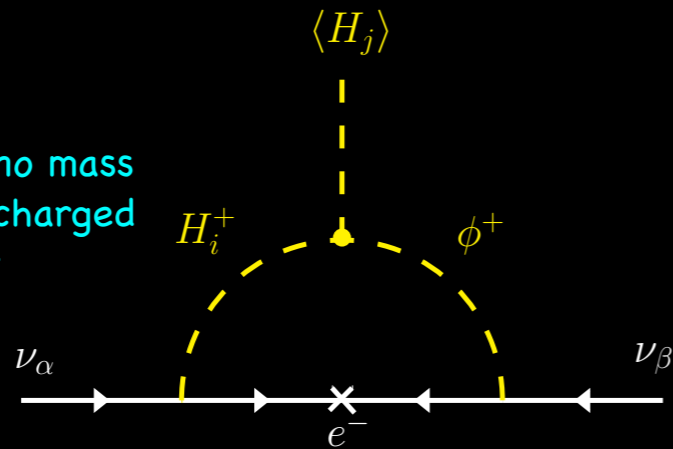


K. S. Babu, *Phys. Lett. B* 203 (1988) 132

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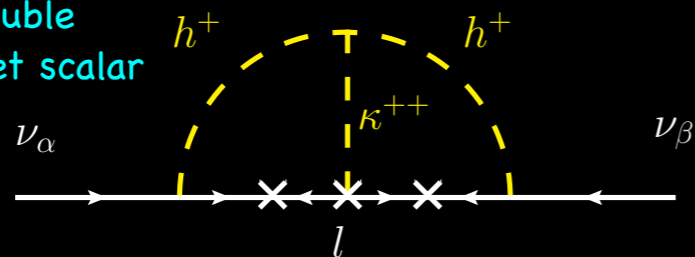
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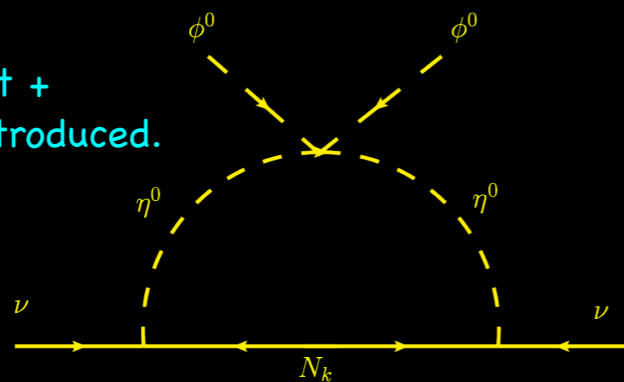
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An extra Inert Doublet + RH heavy neutrino is introduced.
Scotogenic Model

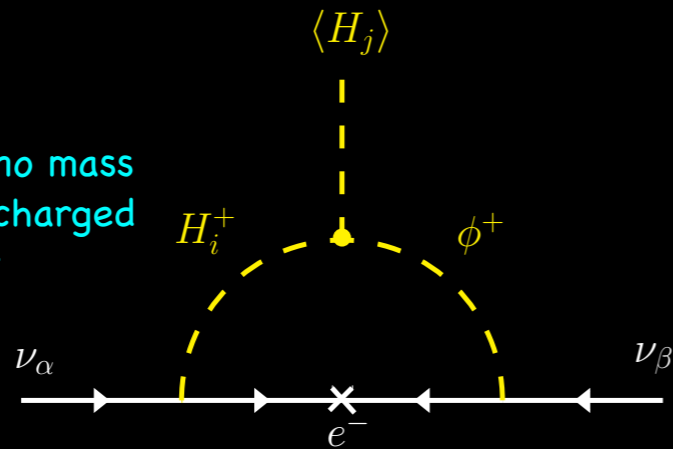


Ernest Ma, *Phys.Rev. D*73 (2006) 077301

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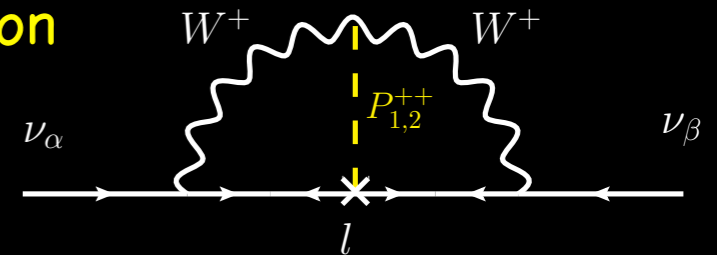
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Asiatic Collaboration

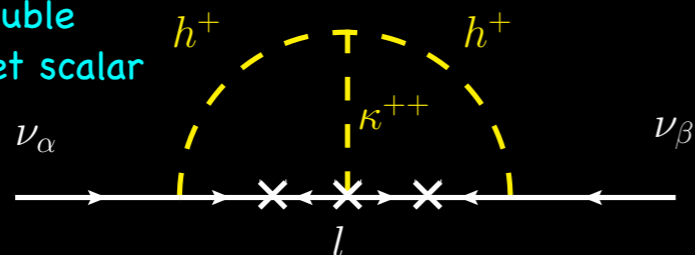
A UV completion of a new effective operator is introduced.



C. S. Chen, C. Q. Geng & J. N. Ng, *Phys. Rev. D* 75 (2007) 053004

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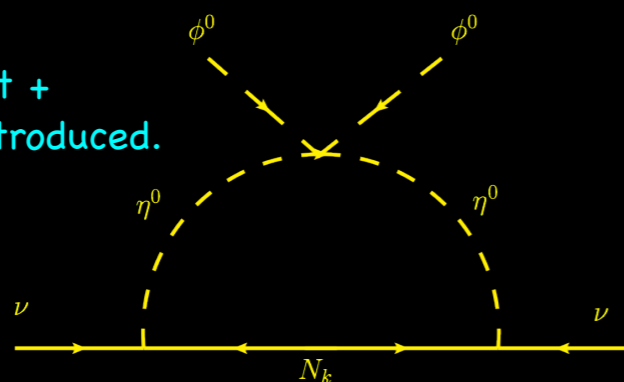
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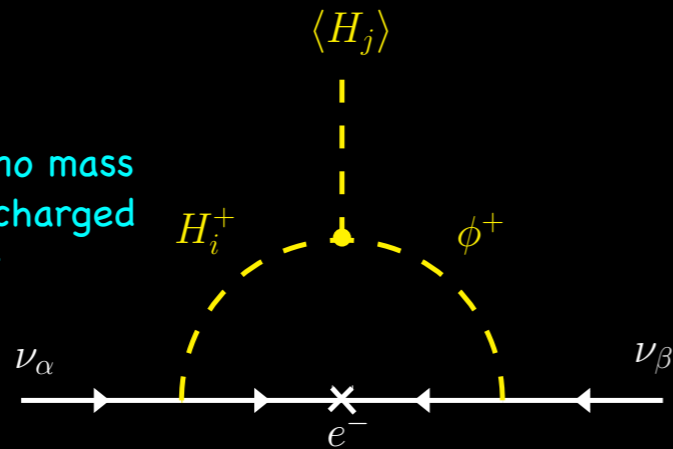


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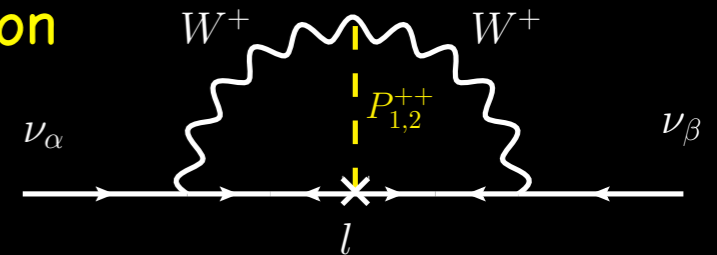
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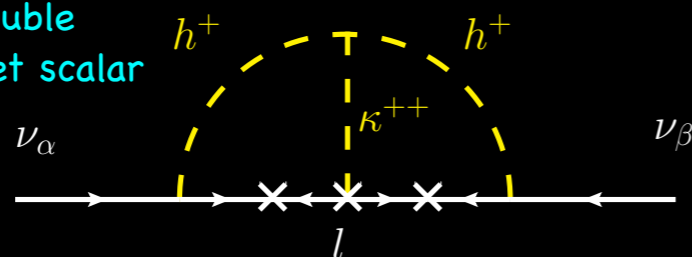
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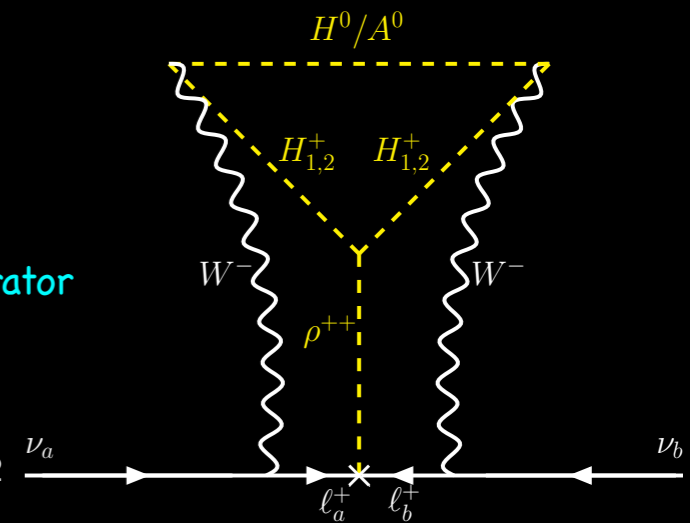
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Cocktail Model

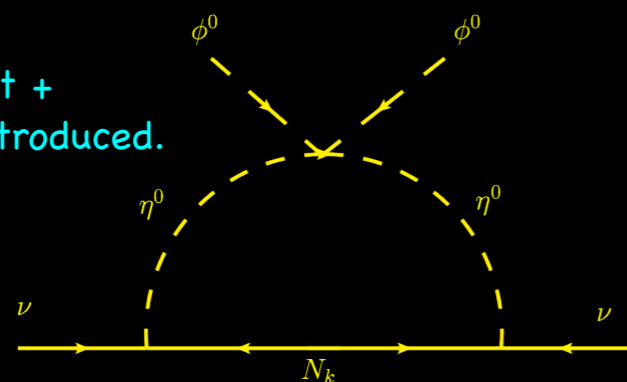
A non-trivial realisation of scotogenic model without RH through a non-Weinberg operator



M. Gustafsson, J.M. No, M. Rivera *Phys. Rev. Lett* 110 (2013) 211802

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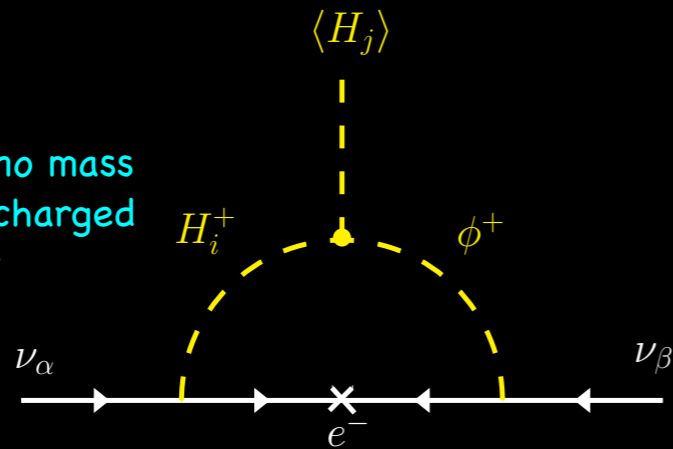


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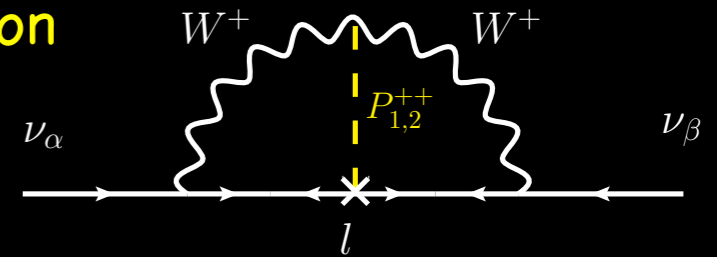
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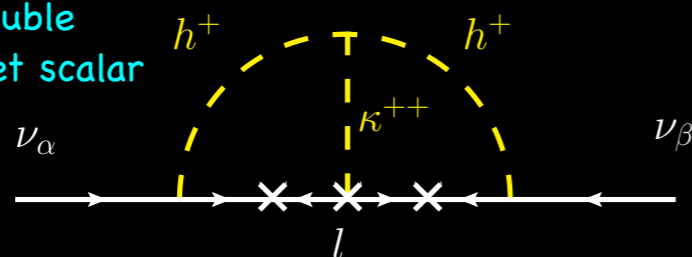
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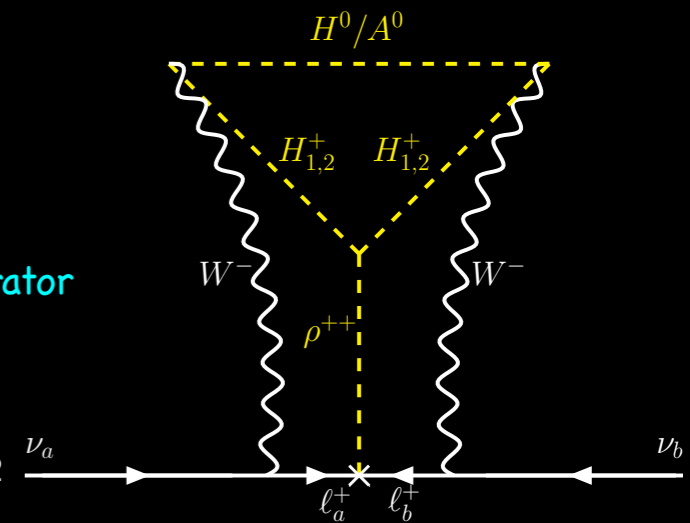
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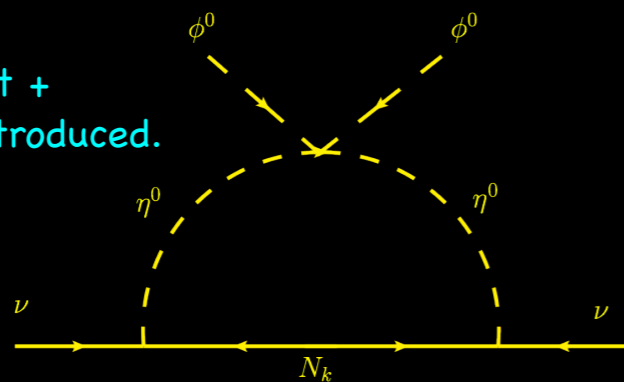
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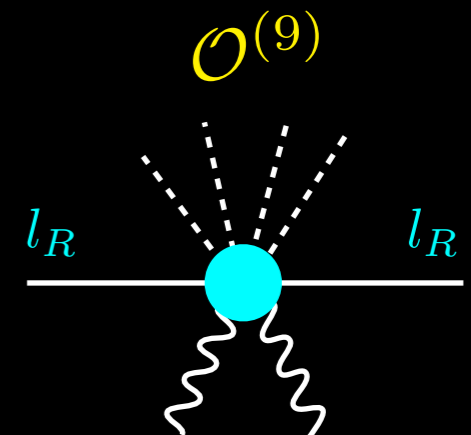
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Ernest Ma, *Phys.Rev. D*73 (2006) 077301

Spanish Collaboration

An study of effective operators involve gauge boson is given

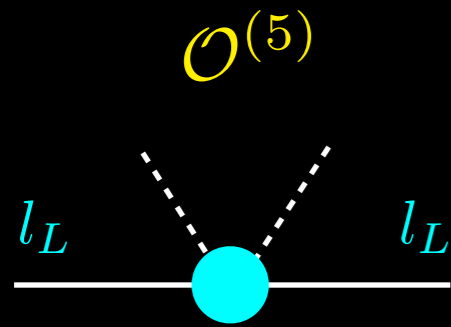


Francisco del Aguila, et al *JHEP* 1205 (2012) 133

Effective Operator Neutrino Mass Generation

l_R

Effective Operator Neutrino Mass Generation



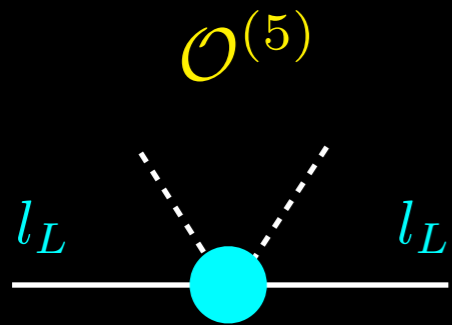
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$$(m_\nu)_{ab} \propto \frac{v^2}{\Lambda} C_{ab}^{(5)}$$

Steven Weinberg
Phys.Rev.Lett 43 (1979) 1566

l_R

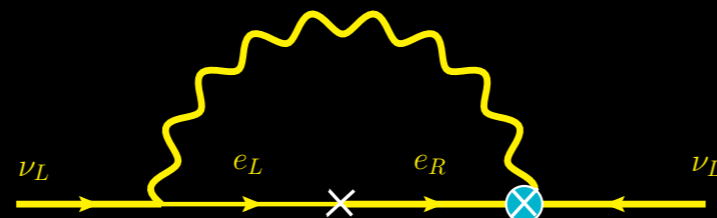
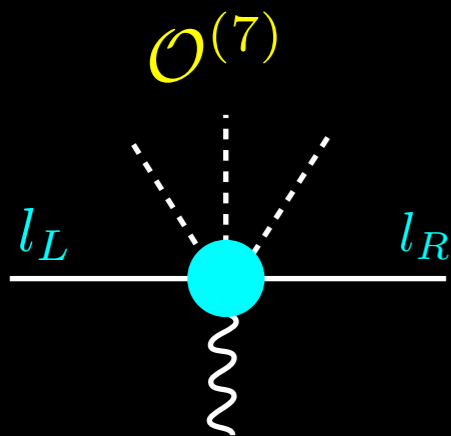
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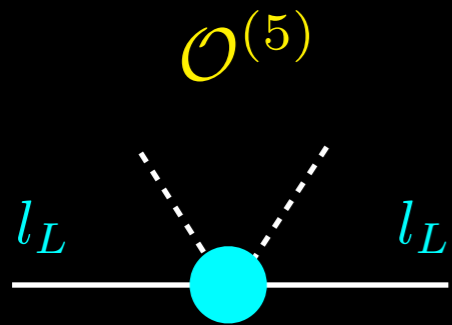


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Francisco del Aguila, et al,
JHEP 1206 (2012) 146

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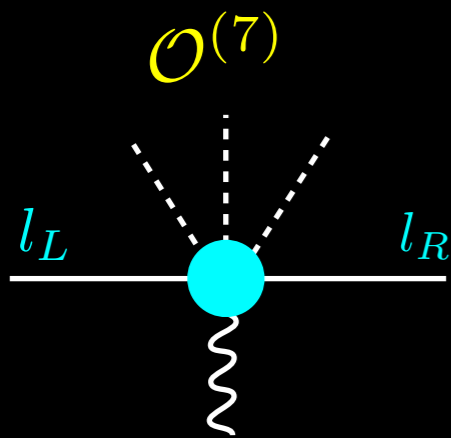
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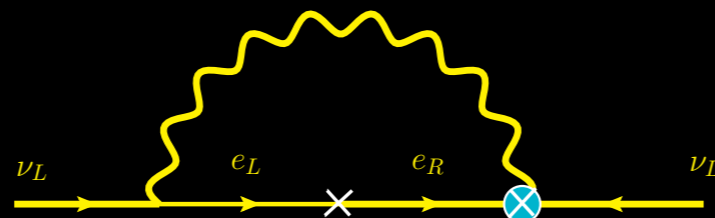
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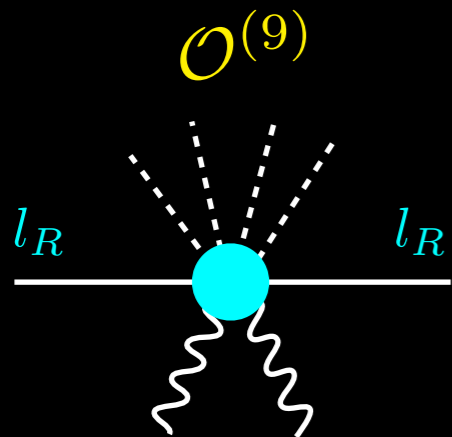
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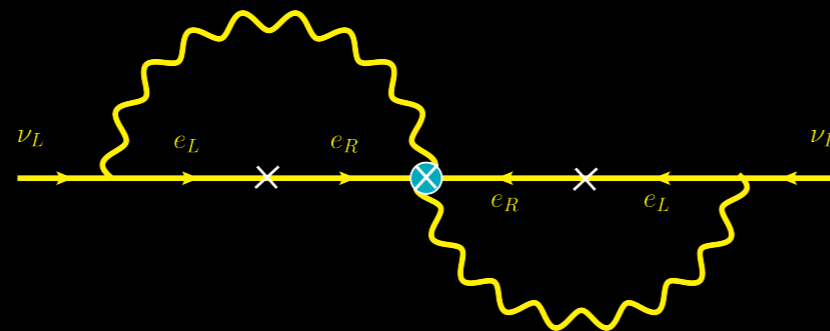
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$$C_{ab} \bar{l}_{R_a}^c l_{R_b} [(D_\mu H)^T i\sigma_2 H]^2$$



$$(m_\nu)_{ab} \propto \frac{1}{(16\pi^2)^2 \Lambda} m_a m_b C_{ab}^{(9)}$$

Mass Matrix Structure \leftrightarrow Flavour Mixing

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$$U = \text{Diag} \left(e^{i\alpha_1/2}, e^{i\alpha_2/2}, 1 \right) \times \begin{pmatrix} c_{13}c_{12} & -c_{23}s_{12} - s_{23}c_{12}s_{13}e^{i\delta} & s_{23}s_{12} - c_{23}c_{12}s_{13}e^{i\delta} \\ c_{13}s_{12} & c_{23}c_{12} - s_{23}s_{12}s_{13}e^{i\delta} & -s_{23}c_{12} - c_{23}s_{12}s_{13}e^{i\delta} \\ s_{13}e^{-i\delta} & s_{23}c_{13} & c_{23}c_{13} \end{pmatrix}$$

2 Majorana phases

α_1, α_2

3 Mixing Angles

$\theta_{12}, \theta_{13}, \theta_{23}$

1 CP phase

δ

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The neutrino mass matrix, can be diagonalized as follow:

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Texture

$$\begin{pmatrix} m_{ee} & m_{e\mu} & m_{e\tau} \\ m_{\mu e} & m_{\mu\mu} & m_{\mu\tau} \\ m_{\tau e} & m_{\tau\mu} & m_{\tau\tau} \end{pmatrix}$$

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M Gustafsson, José M. No and MR
Phys.Rev. D90 (2014) 013012

$$\begin{pmatrix} 0 & \times & \times \\ \times & \times & \times \\ \times & \times & \times \end{pmatrix}, \begin{pmatrix} 0 & 0 & \times \\ 0 & \times & \times \\ \times & \times & \times \end{pmatrix}, \begin{pmatrix} 0 & \times & 0 \\ \times & \times & \times \\ 0 & \times & \times \end{pmatrix}$$

Effective Operator Neutrinoless Double beta Decay

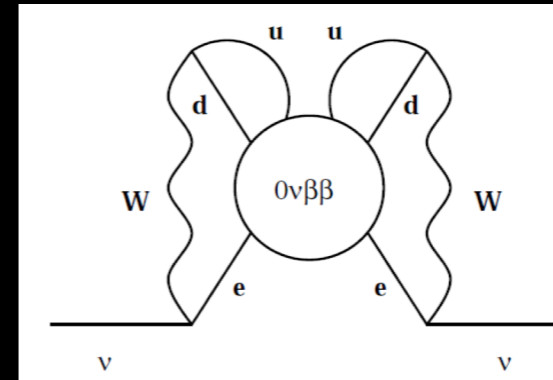
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Neutrinoless Double beta Decay

Black box Theorem:

If NLDBD is observed, neutrino
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Schechter and J.W.F Valle
Phys.Rev.D 25 (1982) 2951



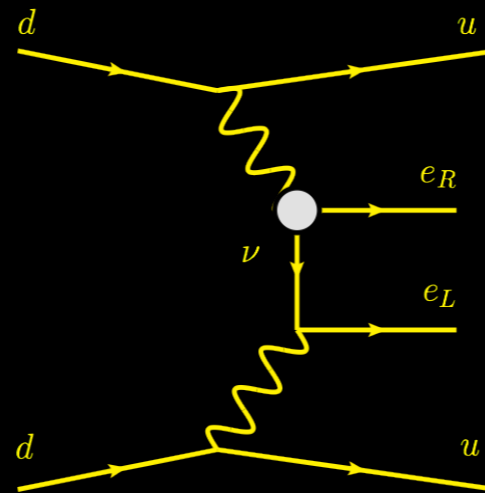
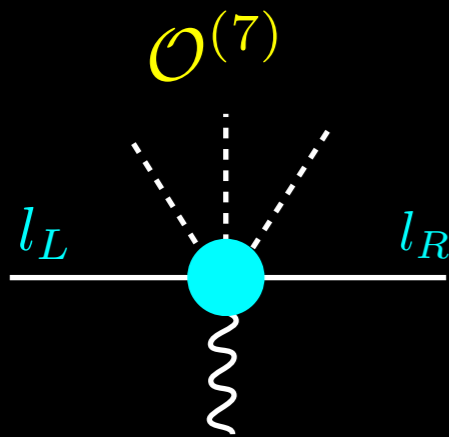
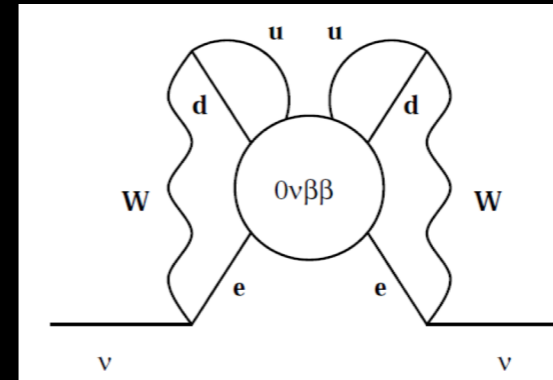
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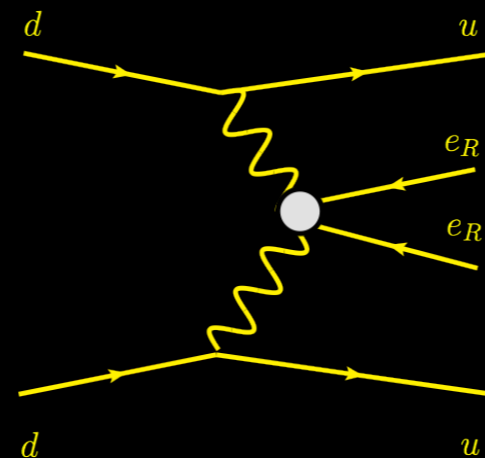
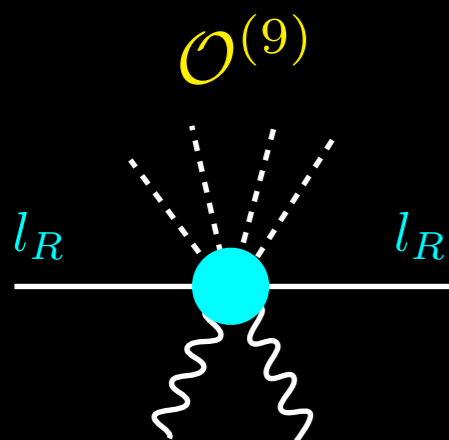
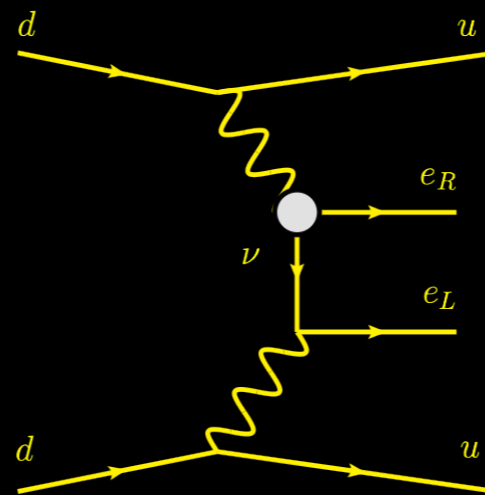
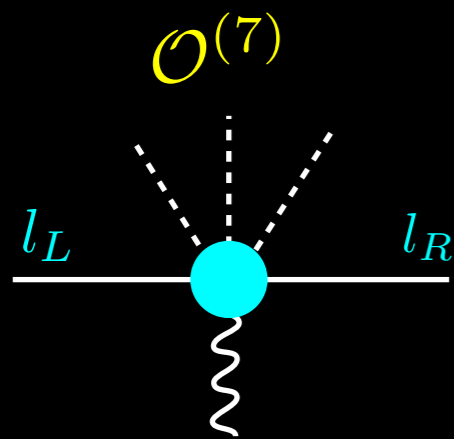
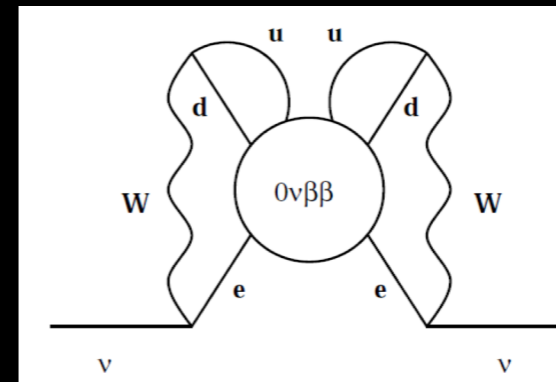


Effective Operator

Neutrinoless Double beta Decay

Black box Theorem:
 If NLDBD is observed, neutrino
 has majorana mass

Schechter and J.W.F Valle
 Phys.Rev.D 25 (1982) 2951

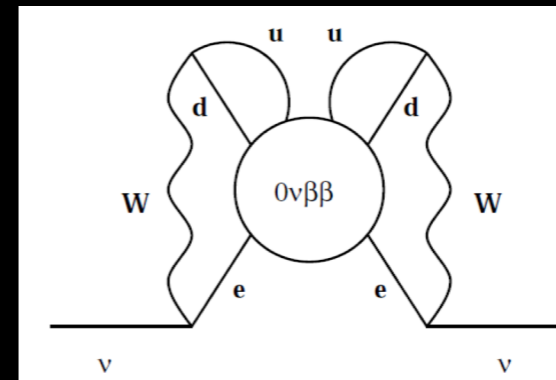


Effective Operator

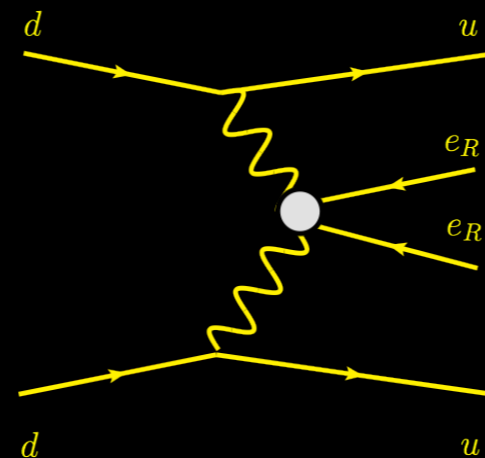
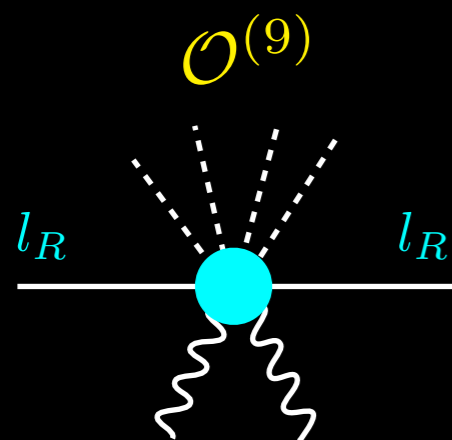
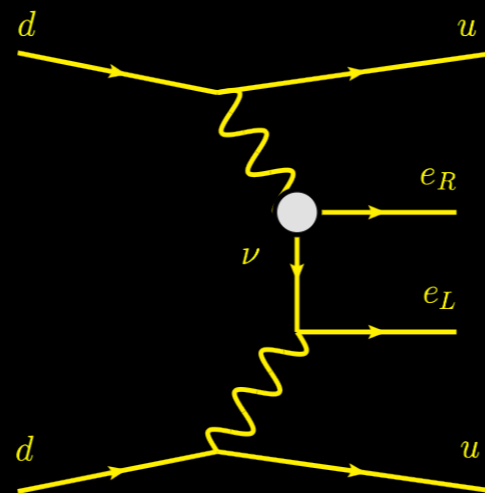
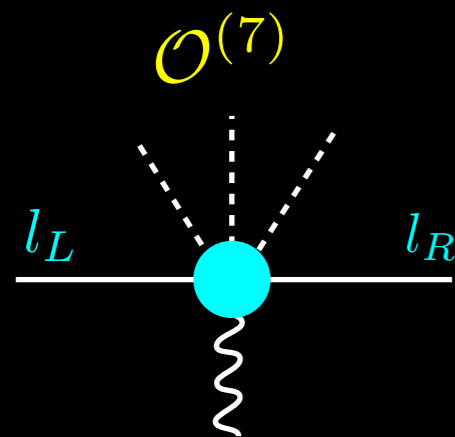
Neutrinoless Double beta Decay

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Special Interest:
 if polarisation can be
 measured

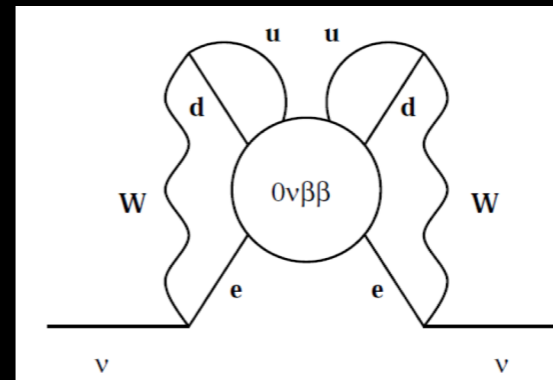


Effective Operator

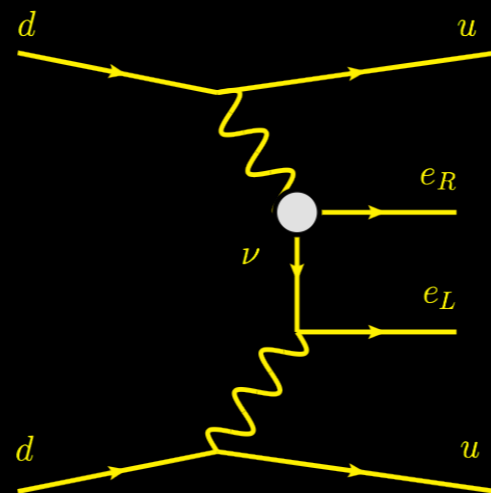
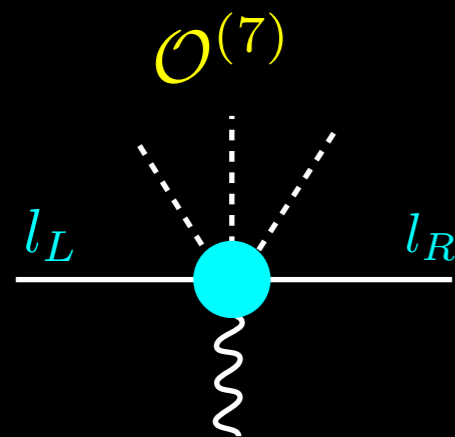
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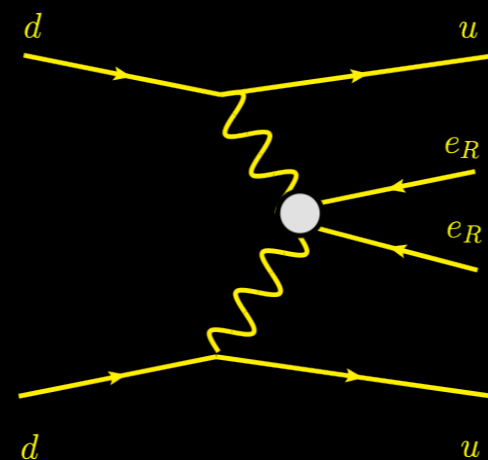
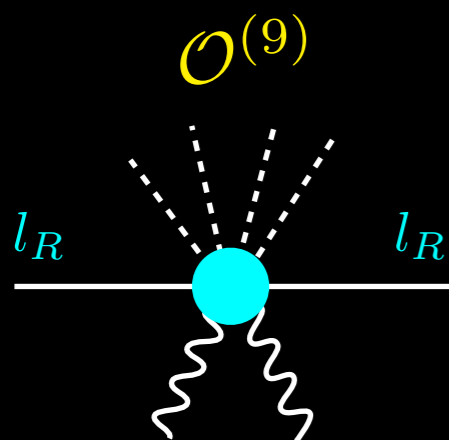
Special Interest:
 if polarisation can be
 measured



$$A_{0\nu\beta\beta}^\nu \sim \frac{G_F^2}{p_{\text{eff}}^2} |m_{ee}^\nu|$$

$$A_{0\nu\beta\beta}^{SD} \sim \frac{G_F^2 v^4 C_{ee}^{(9)}}{\Lambda^5}$$

$$\frac{A_{0\nu\beta\beta}^{SD}}{A_{0\nu\beta\beta}^\nu} \sim \left(16\pi^2 \frac{v^2}{\Lambda^2} \frac{p_{\text{eff}}}{m_e}\right)^2 \sim 10^9$$

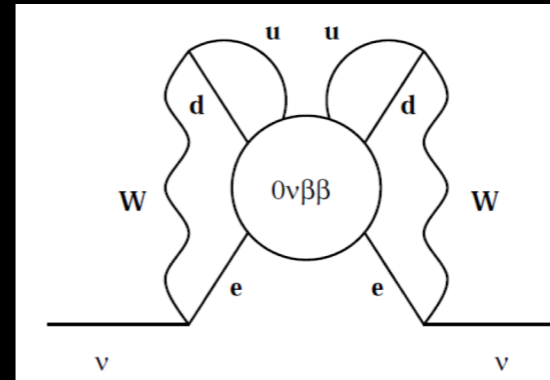


Effective Operator

Neutrinoless Double beta Decay

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Special Interest:
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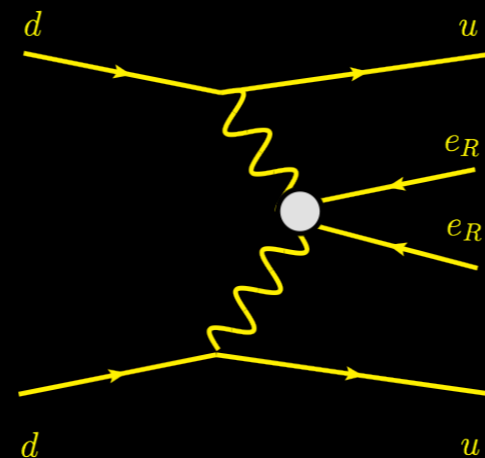
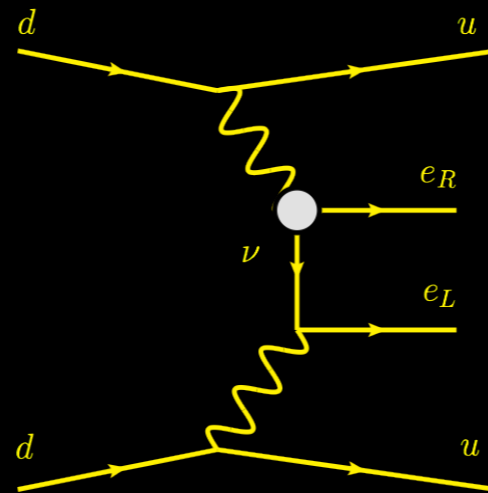
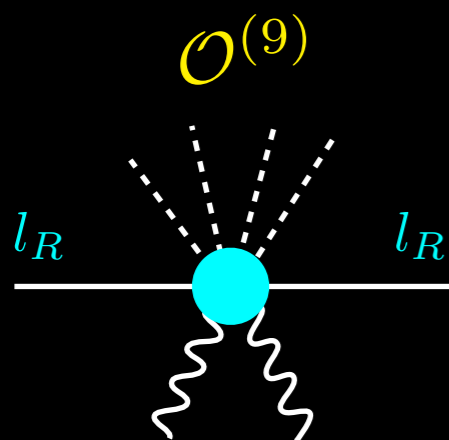
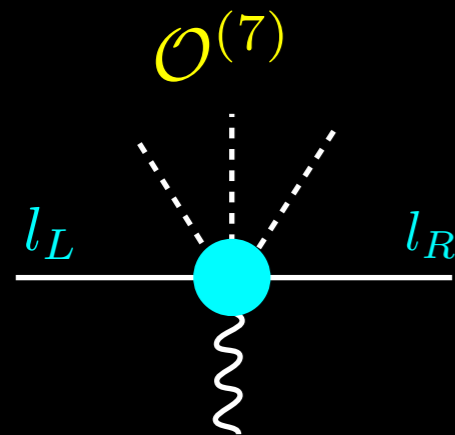
$$A_{0\nu\beta\beta}^\nu \sim \frac{G_F^2}{p_{\text{eff}}^2} |m_{ee}^\nu|$$

$$A_{0\nu\beta\beta}^{SD} \sim \frac{G_F^2 v^4 C_{ee}^{(9)}}{\Lambda^5}$$

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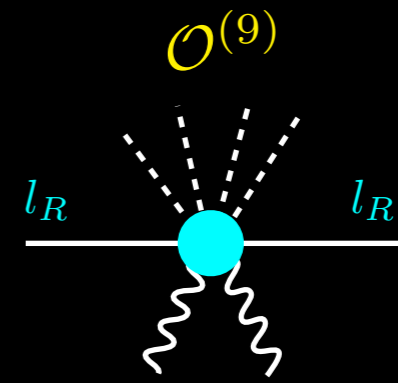
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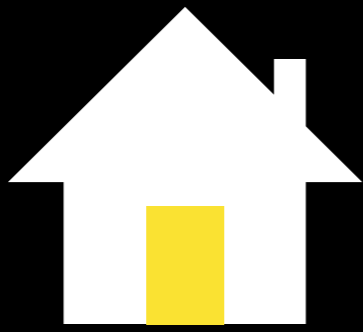
Francisco del Aguila, et al,
JHEP 1206 (2012) 146



LFV Operator

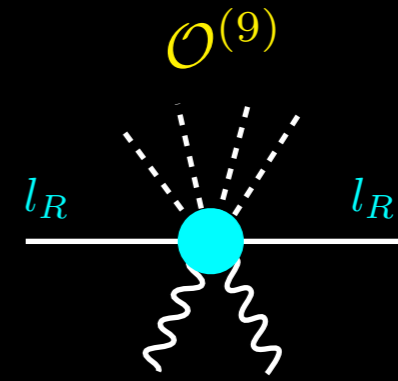
$$\mathcal{O}_9 \equiv \bar{\ell}_{R_a}^c \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$

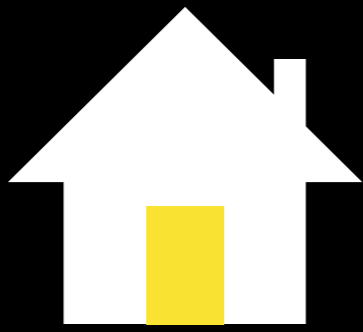




LFV Operator

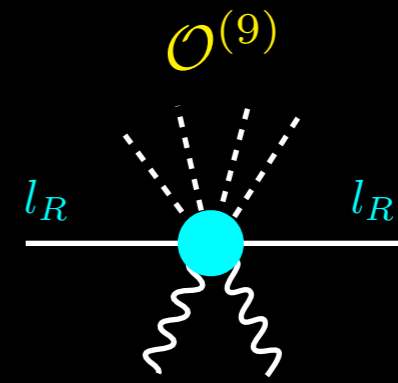
$$\mathcal{O}_9 \equiv \bar{\ell}_{R_a}^c \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





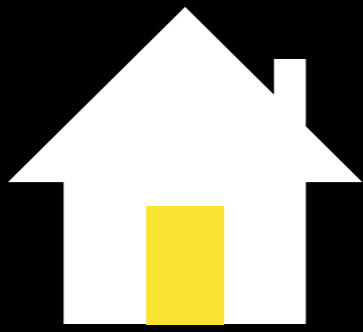
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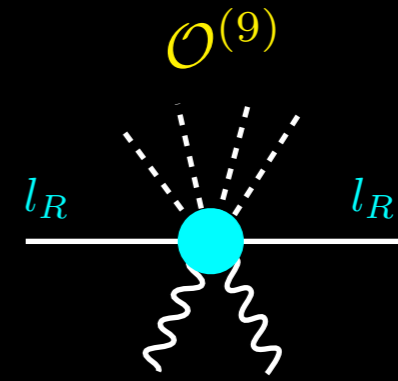
Class 1

$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



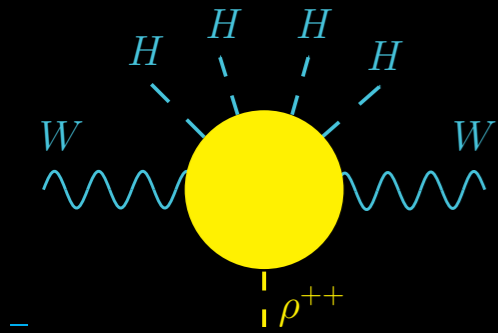
LFV Operator

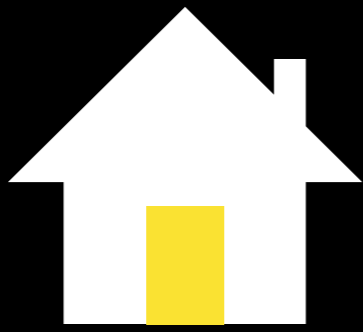
$$\mathcal{O}_9 \equiv \bar{\ell}_{R_a}^c \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

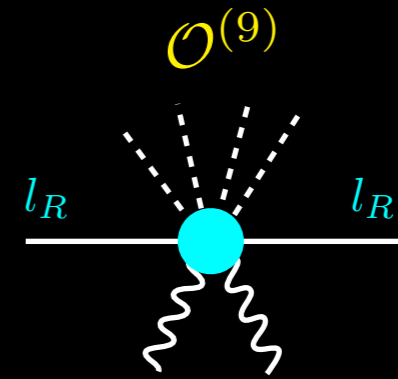
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





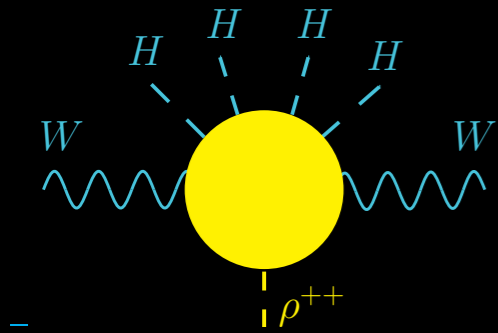
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



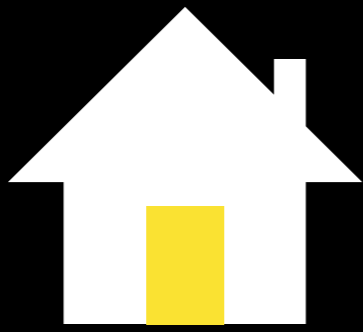
Class 1

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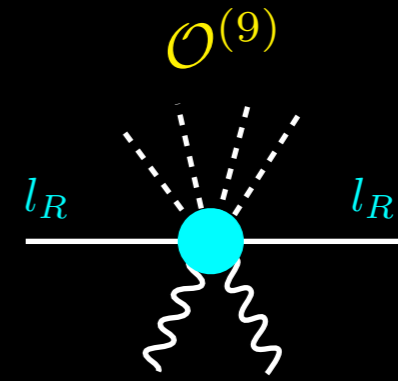
Class 2a

$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



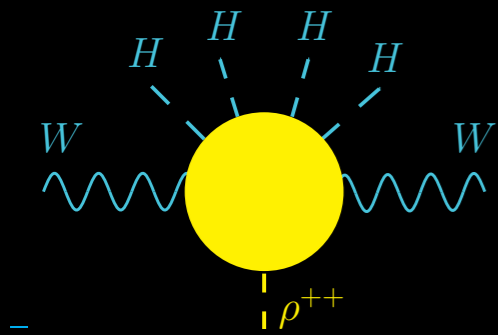
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



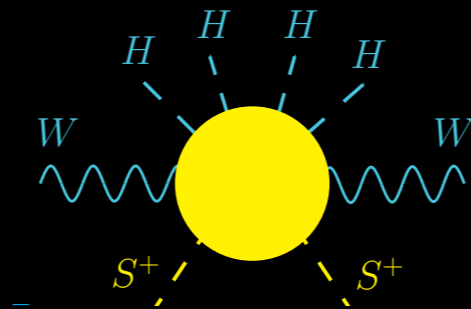
Class 1

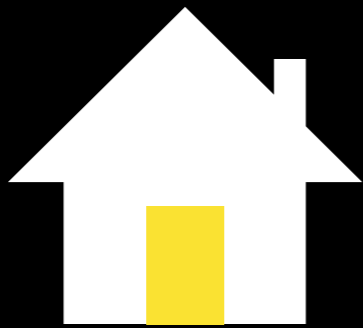
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 2a

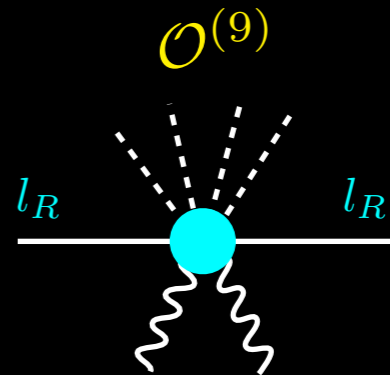
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





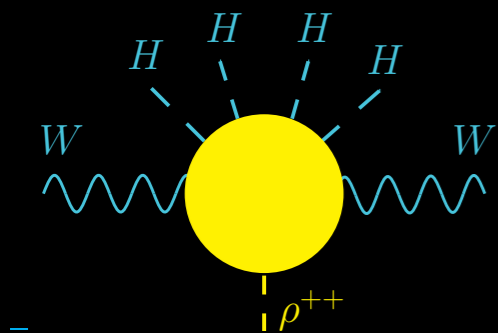
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



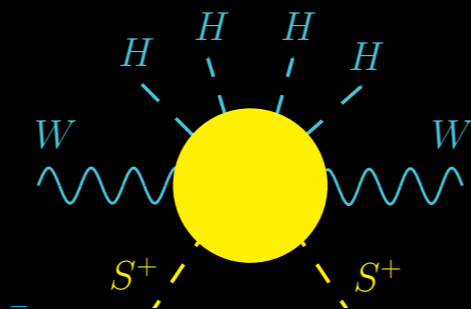
Class 1

$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



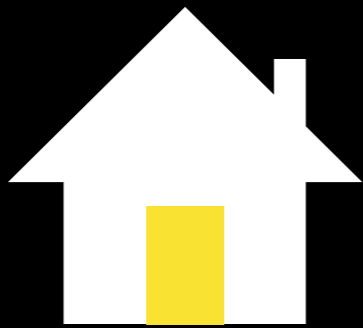
Class 2a

$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



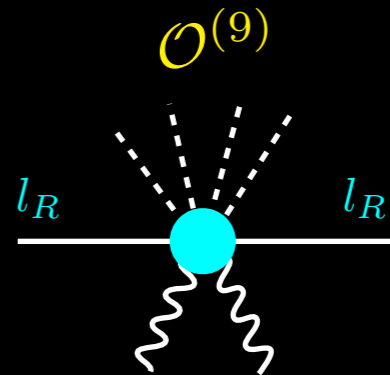
Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



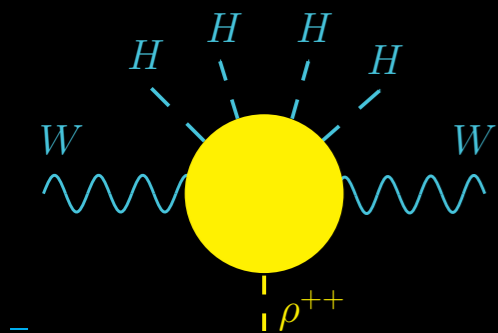
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



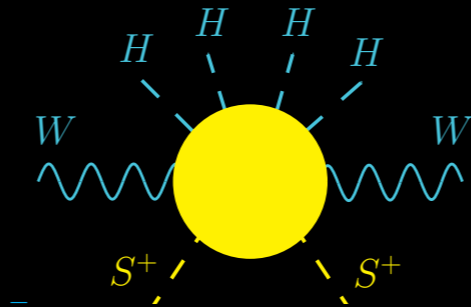
Class 1

$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



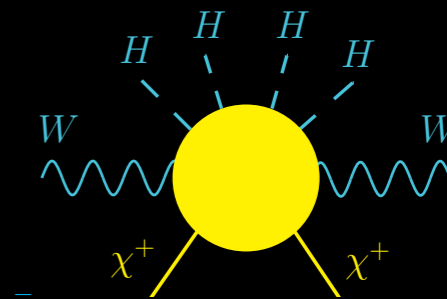
Class 2a

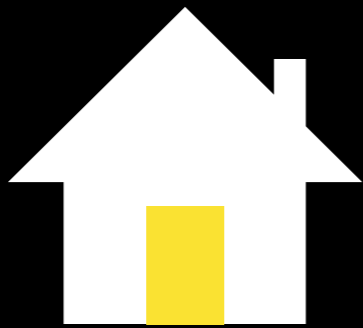
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 2b

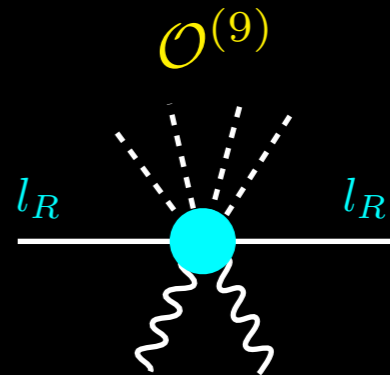
$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





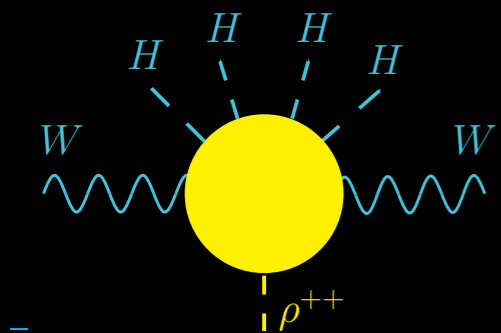
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

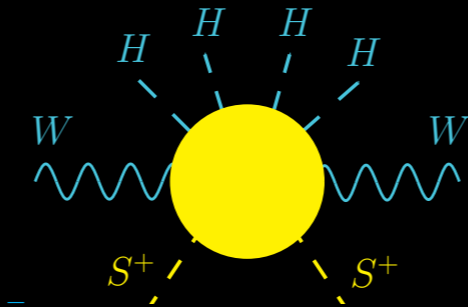
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{\ell}^c_{R_a} \ell_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

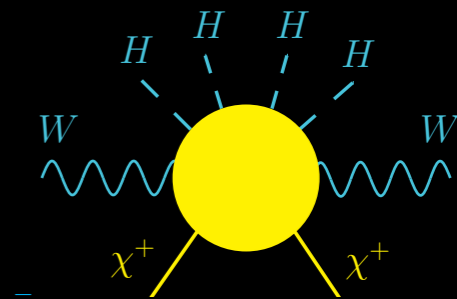
Class 2a

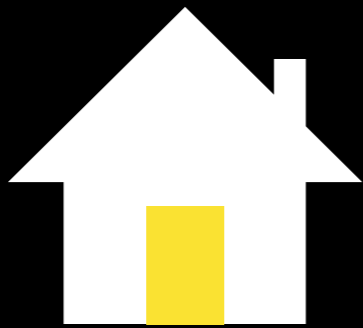
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 2b

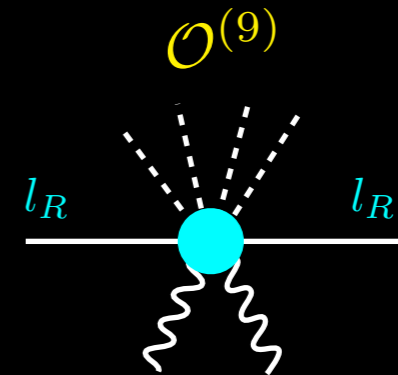
$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





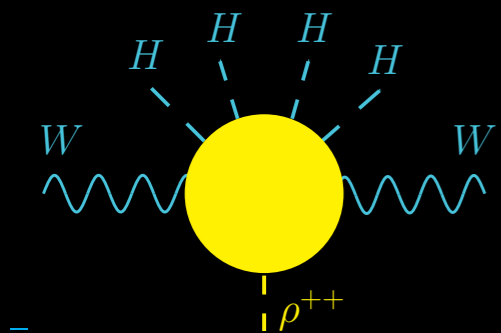
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

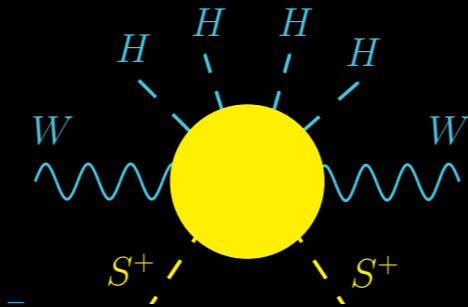
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{\ell}^c_{R_a} \ell_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

Class 2a

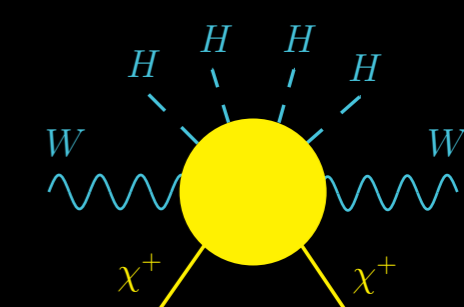
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$

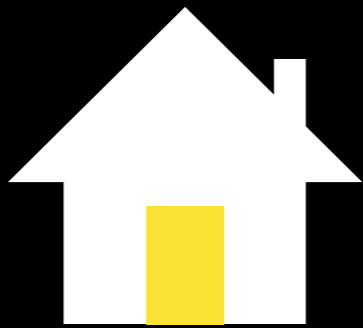


$$g_a \ell_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

Class 2b

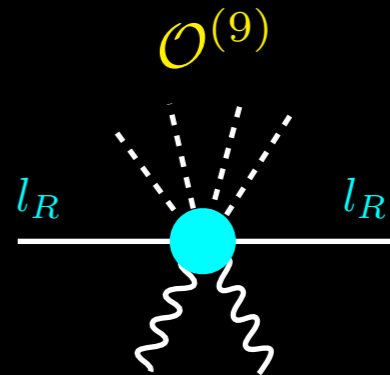
$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$





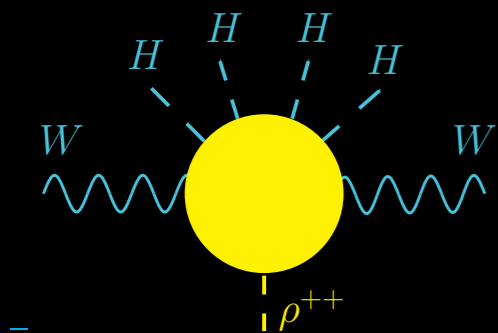
LFV Operator

$$\mathcal{O}_9 \equiv \bar{\ell}^c_{R_a} \ell_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

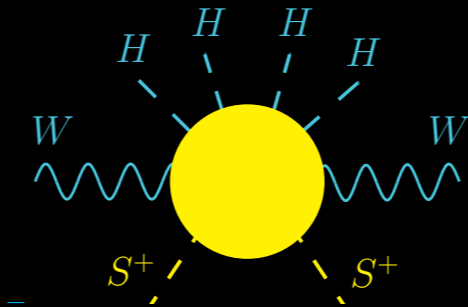
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{\ell}^c_{R_a} \ell_{R_b} \rho + \text{h.c.} \quad \text{key icon}$$

Class 2a

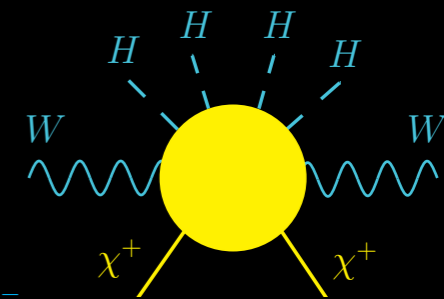
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$g_a \ell_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{key icon}$$

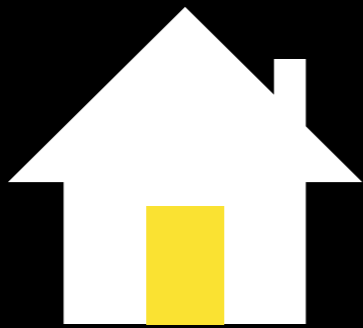
Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



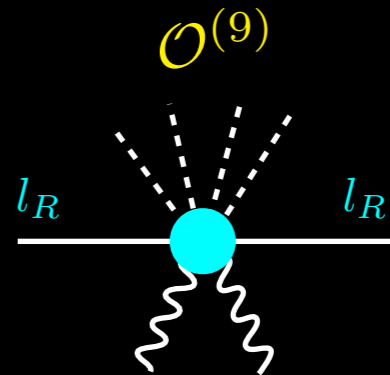
$$g_a \ell_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{key icon}$$





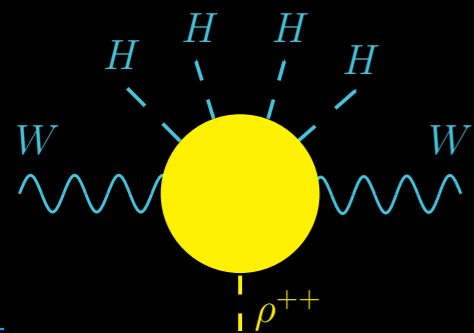
LFV Operator

$$\mathcal{O}_9 \equiv \bar{l}_{R_a}^c l_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

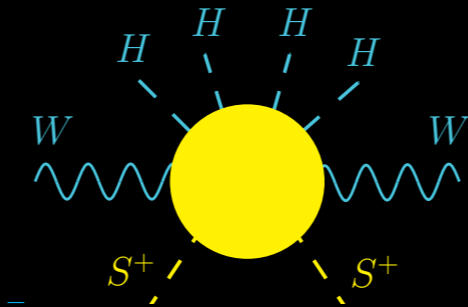
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

Class 2a

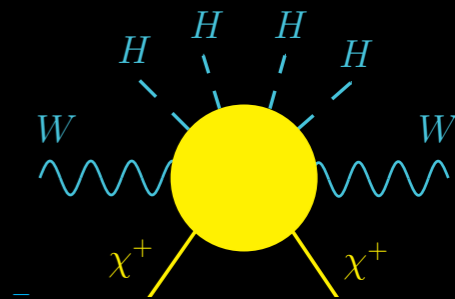
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



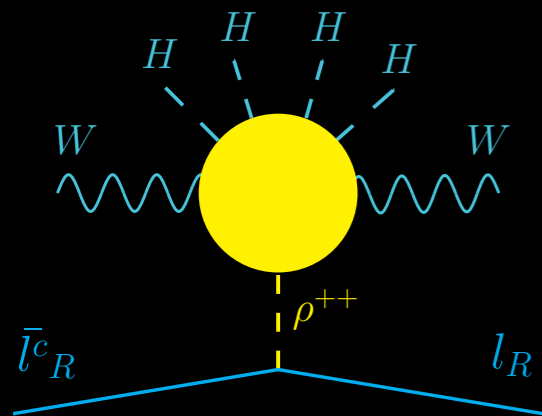
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

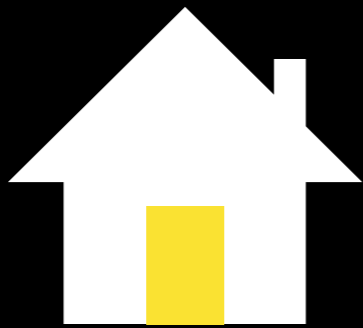
Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



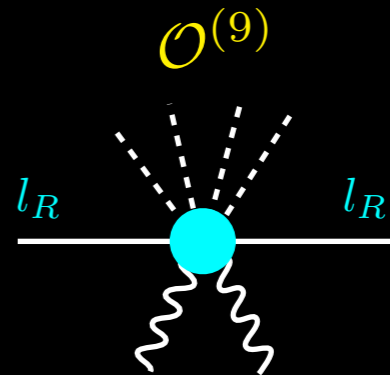
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$





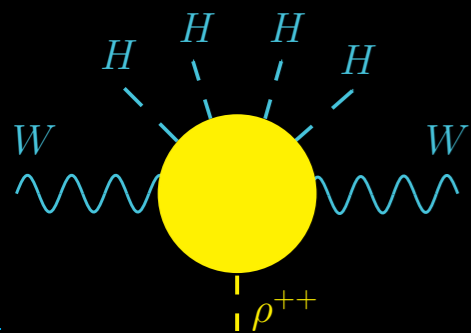
LFV Operator

$$\mathcal{O}_9 \equiv \bar{l}_{R_a}^c l_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

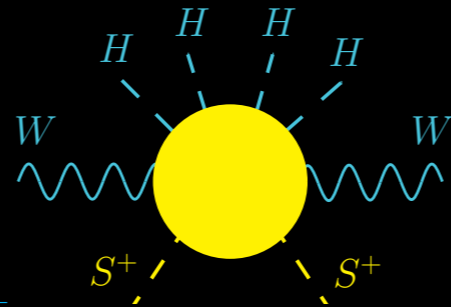
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

Class 2a

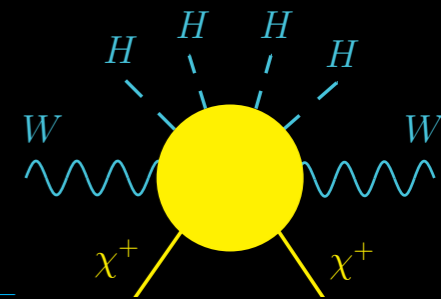
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv S S \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



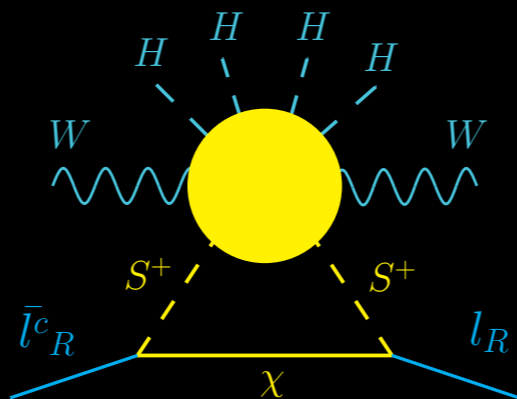
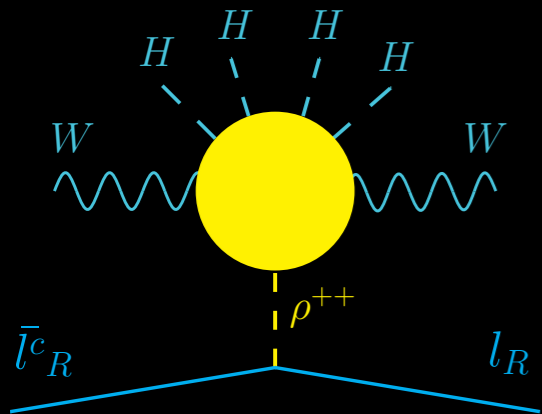
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

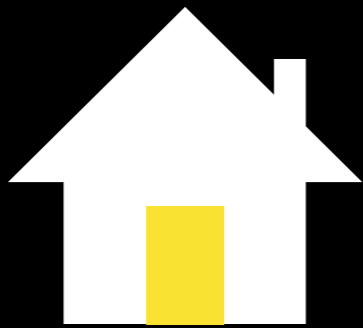
Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



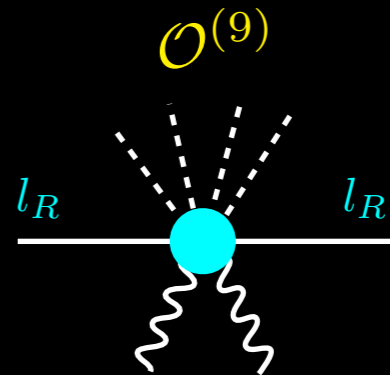
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$





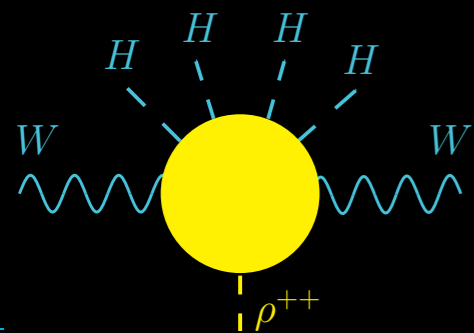
LFV Operator

$$\mathcal{O}_9 \equiv \bar{l}_{R_a}^c l_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

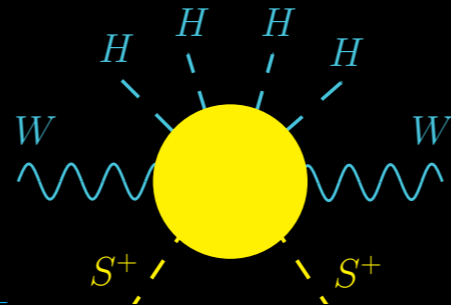
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

Class 2a

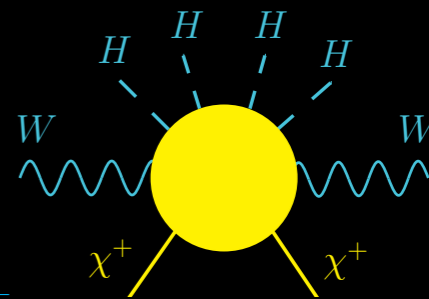
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



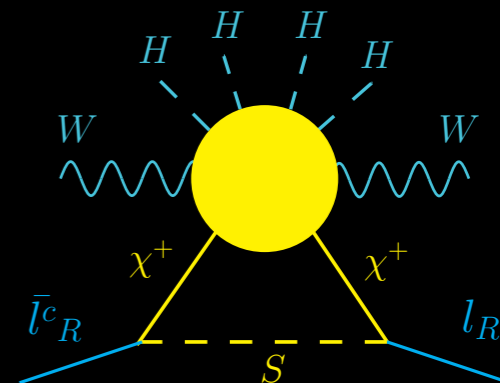
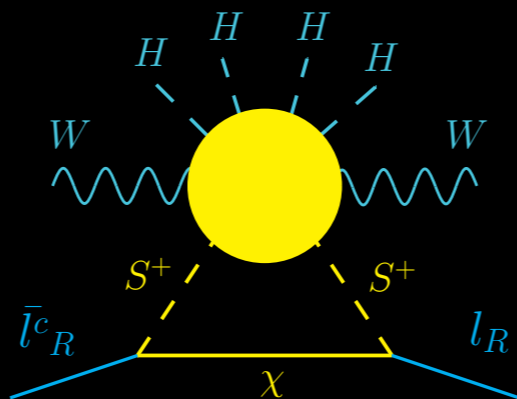
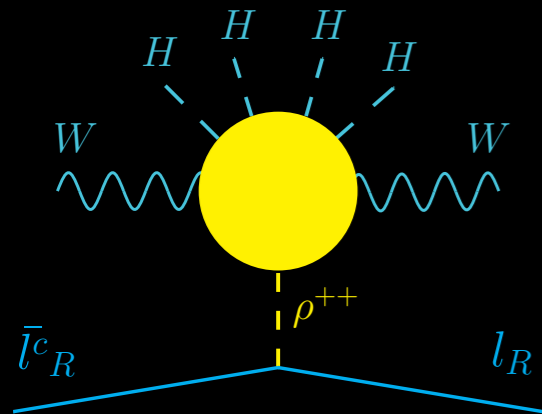
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

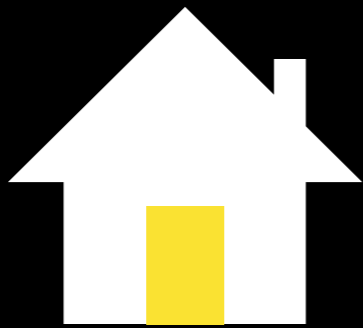
Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



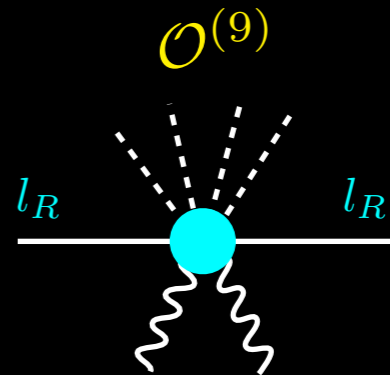
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$





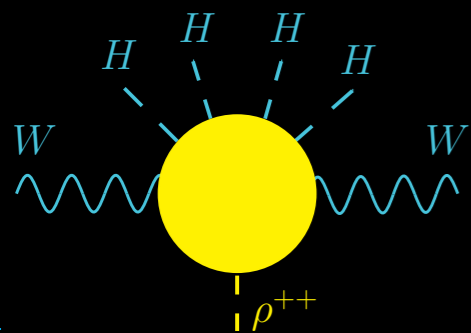
LFV Operator

$$\mathcal{O}_9 \equiv \bar{l}_{R_a}^c l_{R_b} \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



Class 1

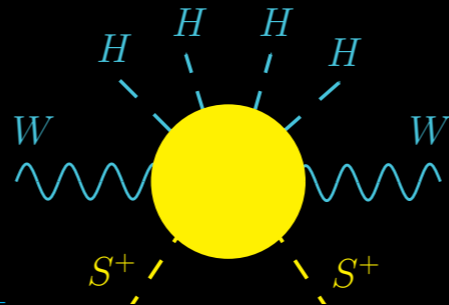
$$\mathcal{O}_{\text{BSM}}^1 \equiv \rho \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



$$C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho + \text{h.c.} \quad \text{🔑}$$

Class 2a

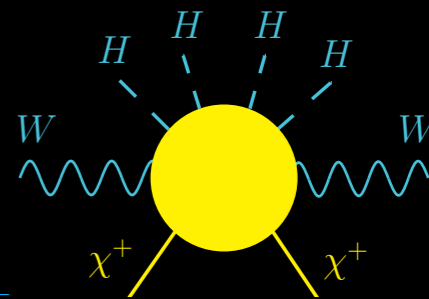
$$\mathcal{O}_{\text{BSM}}^{2a} \equiv SS \left[(D_\mu H)^T i\sigma_2 H \right]^2$$



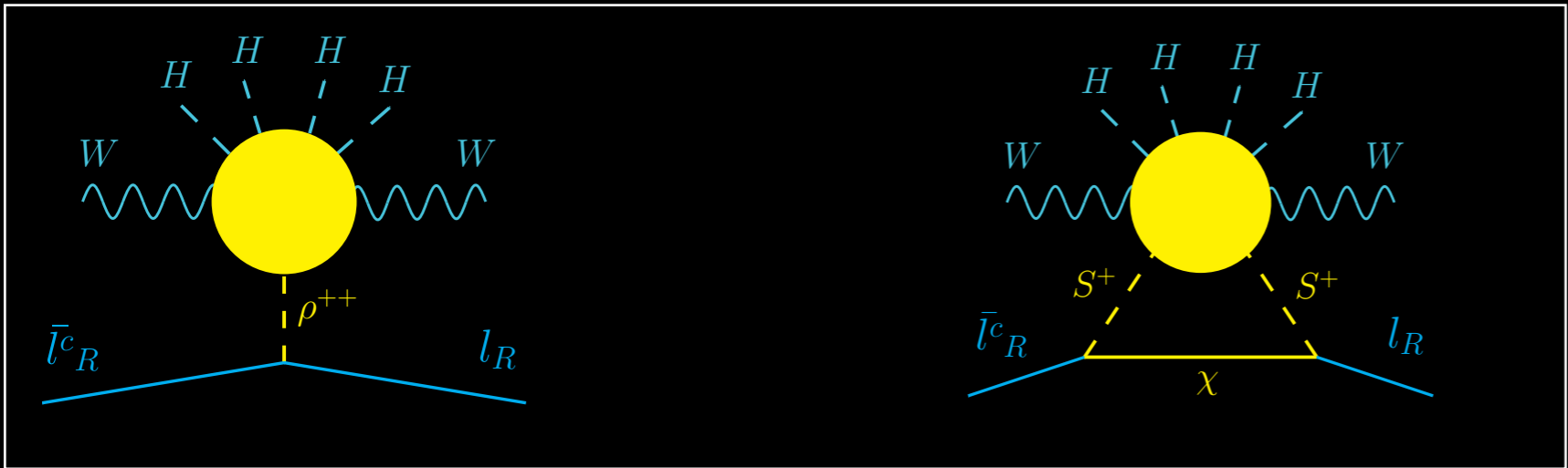
$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

Class 2b

$$\mathcal{O}_{\text{BSM}}^{2b} \equiv \bar{\chi}^c \chi \left[(D_\mu H)^T i\sigma_2 H \right]^2$$

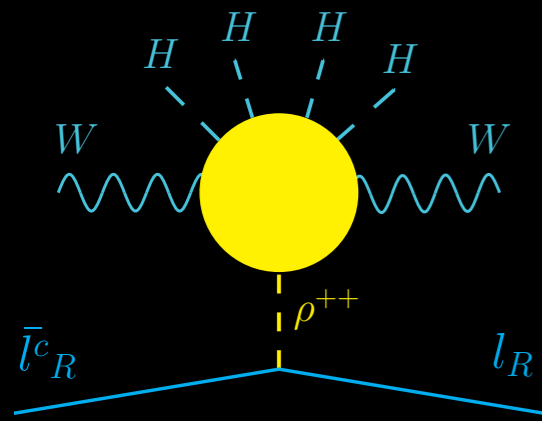


$$g_a l_{R_a} (\chi \cdot S) + \text{h.c.} \quad \text{🔑}$$

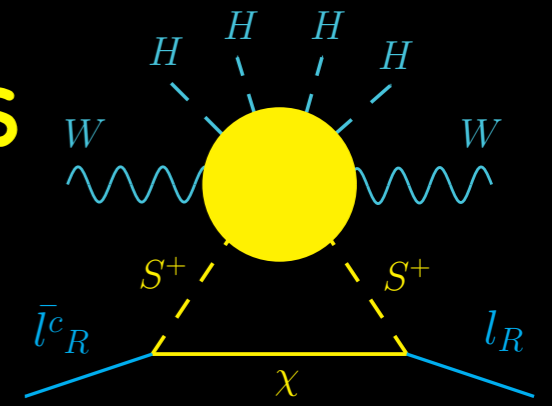


Effective Operator

Differences between Classes



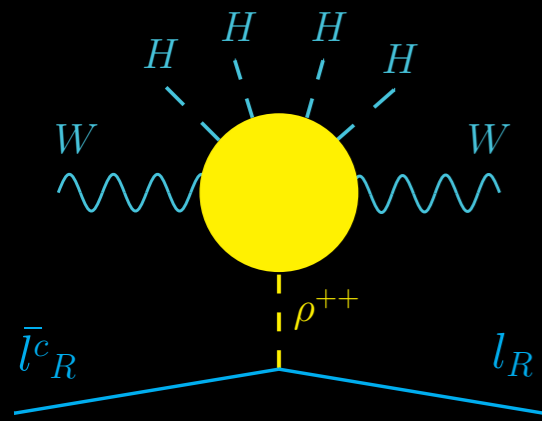
Class 1



Class 2a

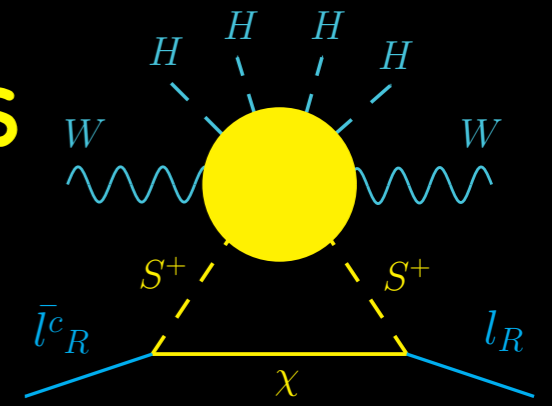
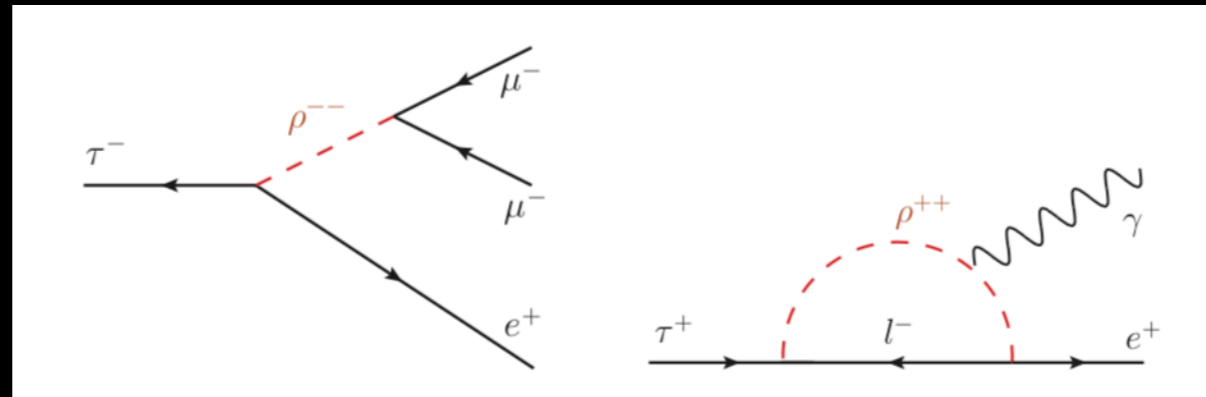
Effective Operator

Differences between Classes



Class 1

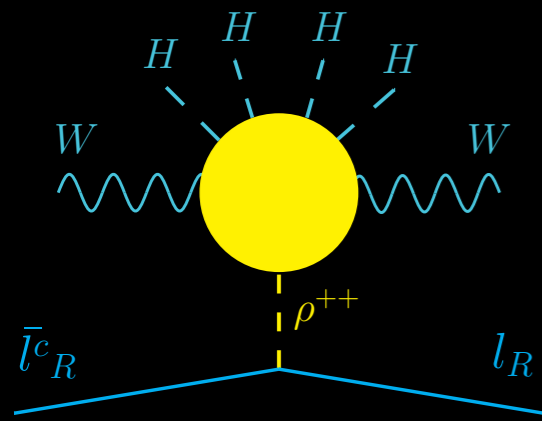
- LFV Processes



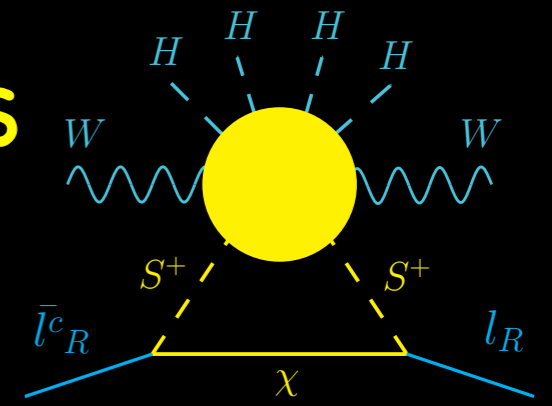
Class 2a

Effective Operator

Differences between Classes

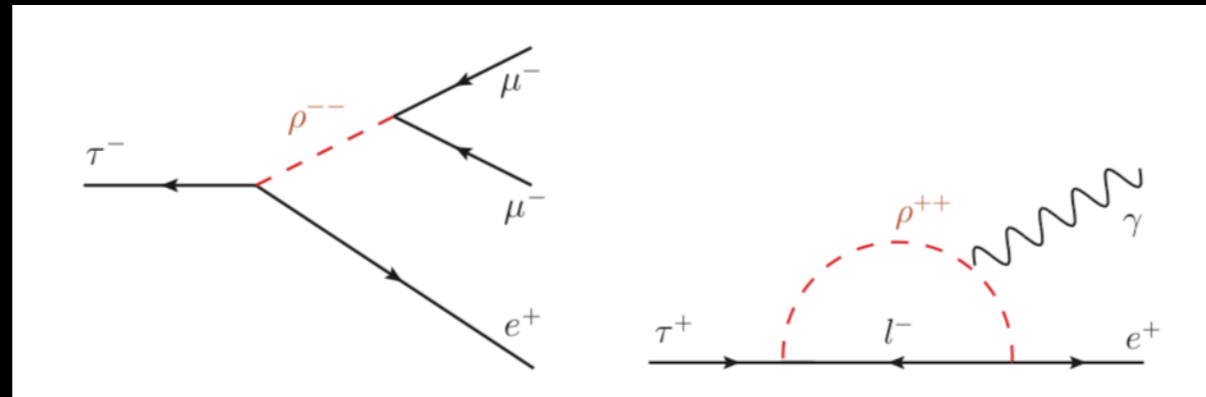


Class 1



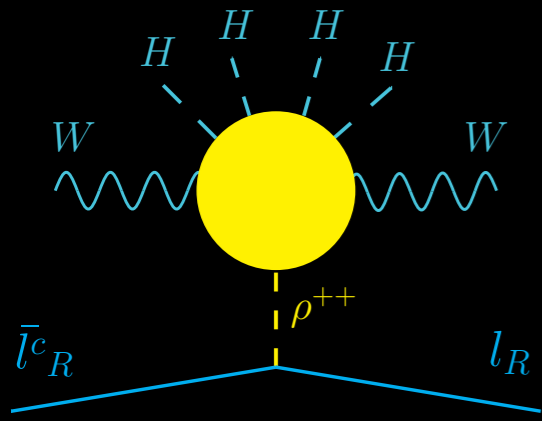
Class 2a

- LFV Processes



Effective Operator

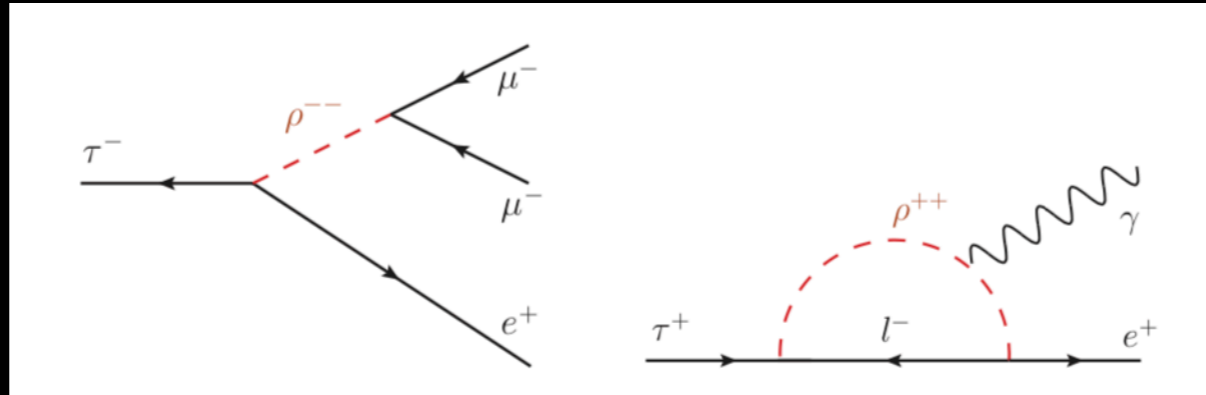
Differences between Classes



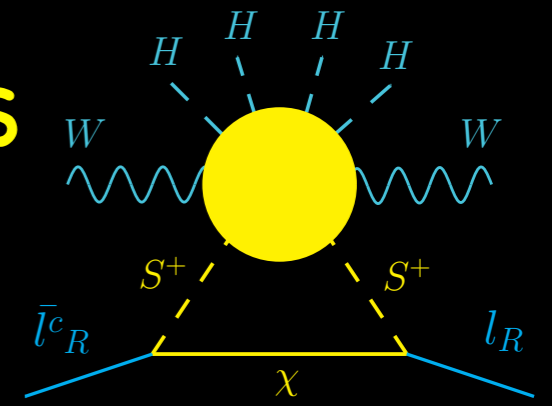
Class 1

- LFV Processes

Tree-level and one loop contribution



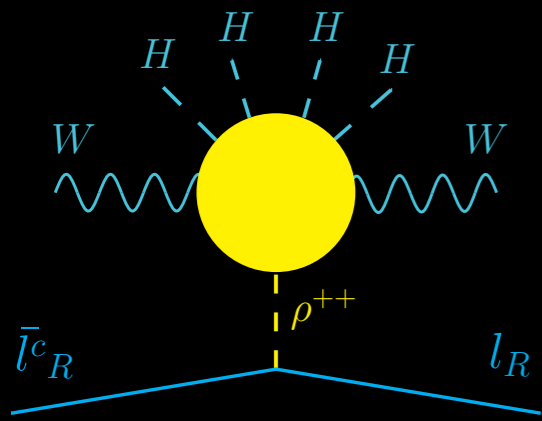
One loop contribution Only



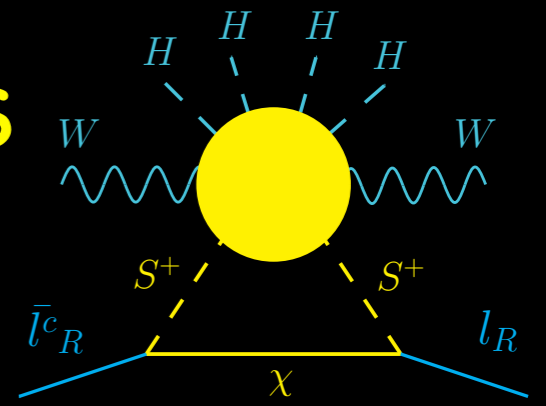
Class 2a

Effective Operator

Differences between Classes



Class 1



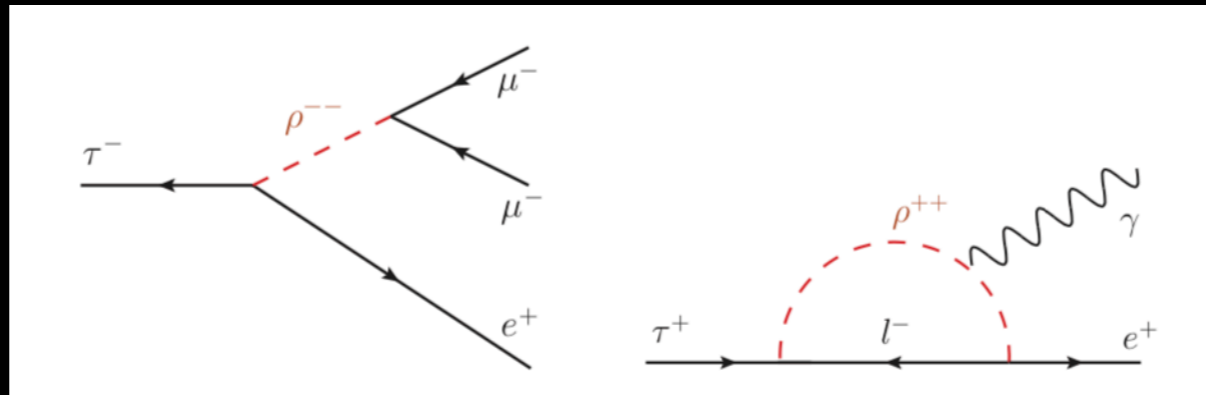
Class 2a

● LFV Processes

Tree-level and one loop contribution

$$\mu \rightarrow e \gamma$$

$$\tau \rightarrow e \mu \mu$$



One loop contribution Only

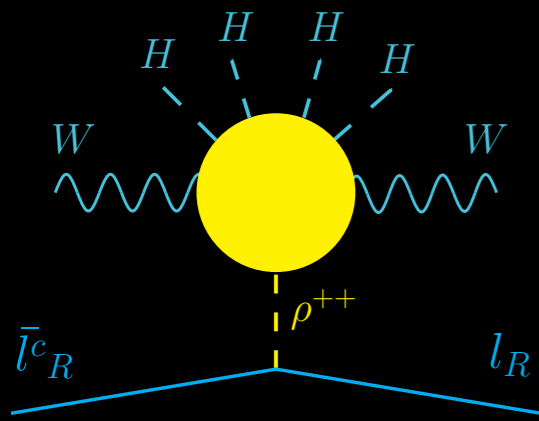
$$C_{\mu\mu}/m_\rho \gtrsim 10^{-2}/\text{TeV}$$

$$C_{\mu\tau}/m_\rho \gtrsim 10^{-3}/\text{TeV}$$

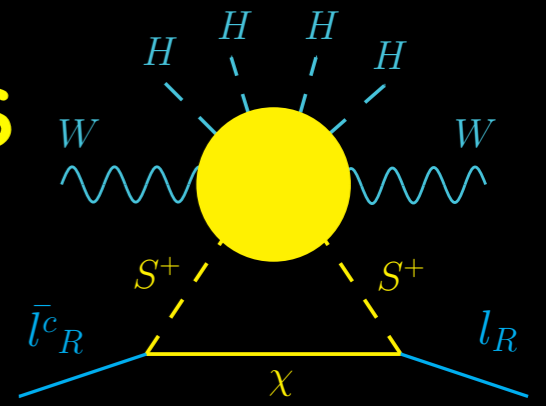
$$C_{e\tau}/m_\rho \gtrsim 0.1/\text{TeV}$$

Effective Operator

Differences between Classes

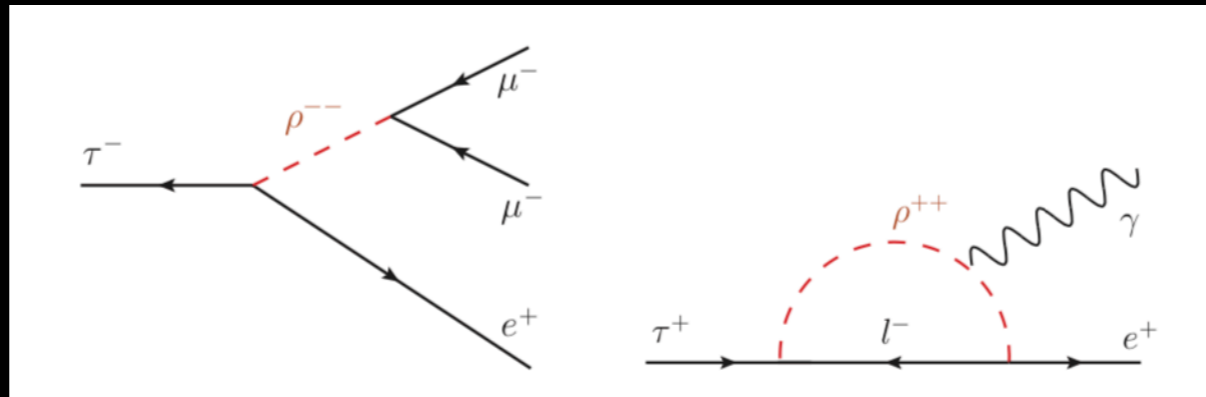


Class 1



Class 2a

- LFV Processes



Tree-level and one loop contribution

$$\mu \rightarrow e \gamma$$

$$\tau \rightarrow e \mu \mu$$

$$C_{\mu\mu}/m_\rho \gtrsim 10^{-2}/\text{TeV}$$

$$C_{\mu\tau}/m_\rho \gtrsim 10^{-3}/\text{TeV}$$

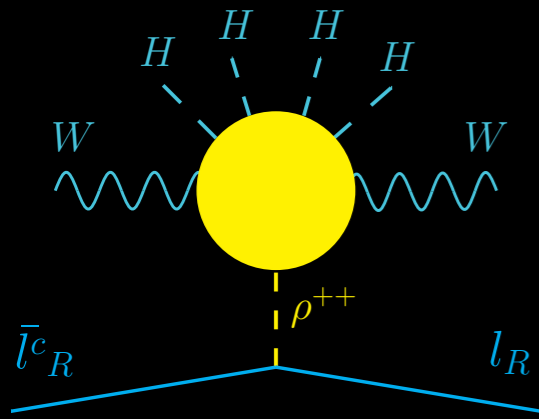
$$C_{e\tau}/m_\rho \gtrsim 0.1/\text{TeV}$$

One loop contribution Only

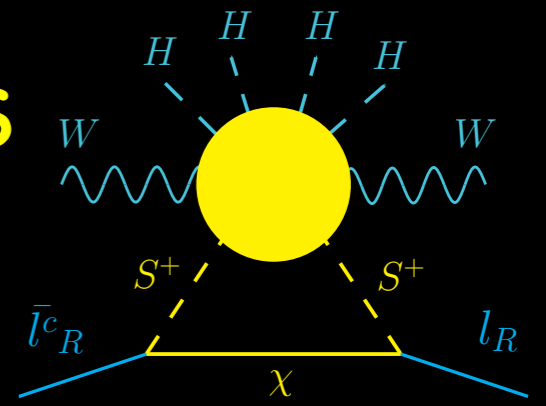
- Neutrino Mass and the Yukawa's structure

Effective Operator

Differences between Classes

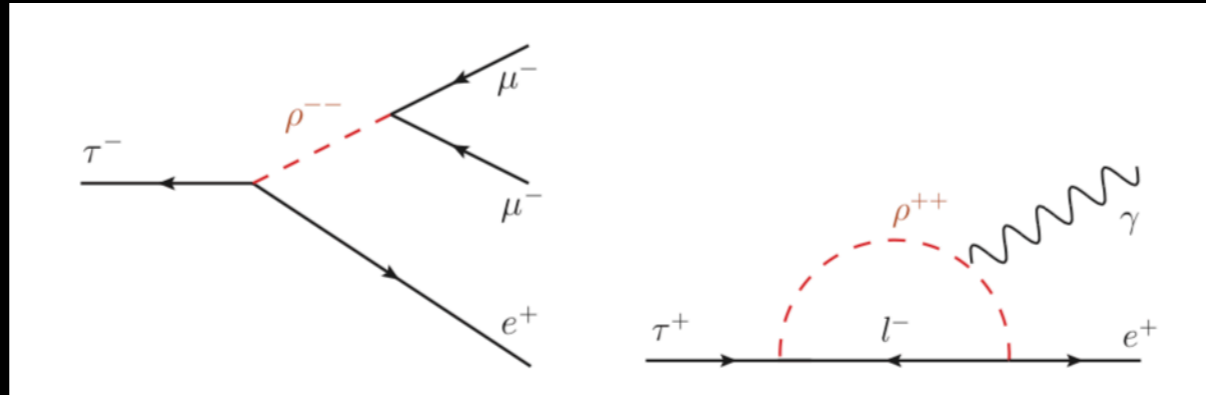


Class 1



Class 2a

- LFV Processes



Tree-level and one loop contribution

$$\mu \rightarrow e\gamma$$

$$\tau \rightarrow e\mu\mu$$

$$C_{\mu\mu}/m_\rho \gtrsim 10^{-2}/\text{TeV}$$

$$C_{\mu\tau}/m_\rho \gtrsim 10^{-3}/\text{TeV}$$

$$C_{e\tau}/m_\rho \gtrsim 0.1/\text{TeV}$$

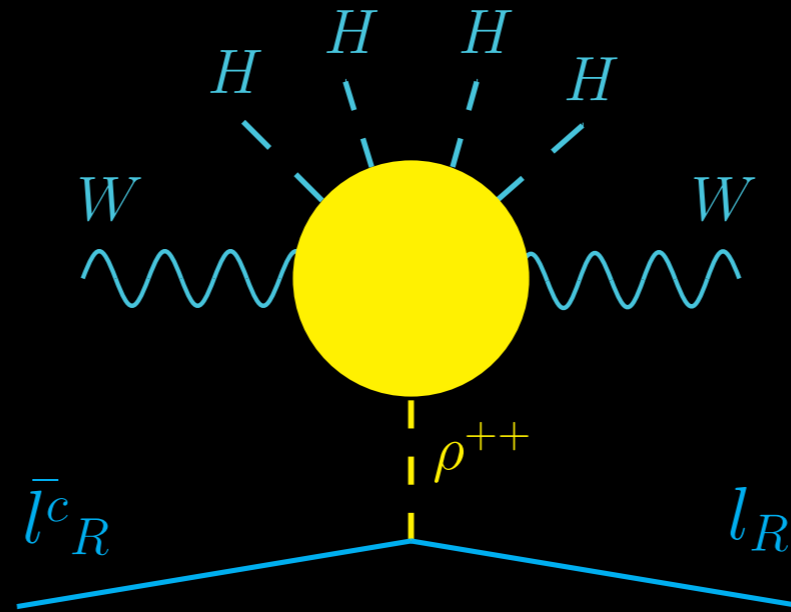
One loop contribution Only

- Neutrino Mass and the Yukawa's structure

$$m_{ab}^\nu = \frac{1}{(16\pi^2)^{L+2}} C_{ab} \frac{m_a^\ell m_b^\ell}{\Lambda}$$

$$m_{ab}^\nu = \frac{1}{(16\pi^2)^{L+3}} g_a g_b \frac{m_a^\ell m_b^\ell}{\Lambda'}$$

UV Completions Class 1



**The Cocktail Model:
Inert Doublet**

Gustafsson, No and MR.

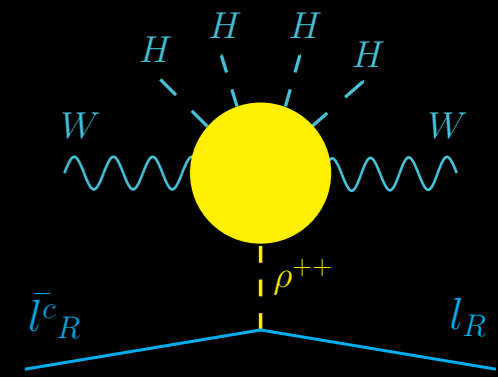
Phys.Rev.Lett. 110 (2013) no.21, 211802

**The Lollipop Model:
Inert Triplet**

J. Alcaide, D. Das and A. Santamaria,

JHEP 1704, 049 (2017)

The Cocktail Model $1_2 2_2$

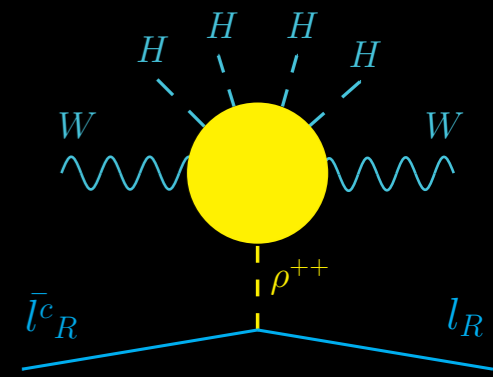


The Cocktail Model $1_2 2_2$



Inert Doublet Model

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

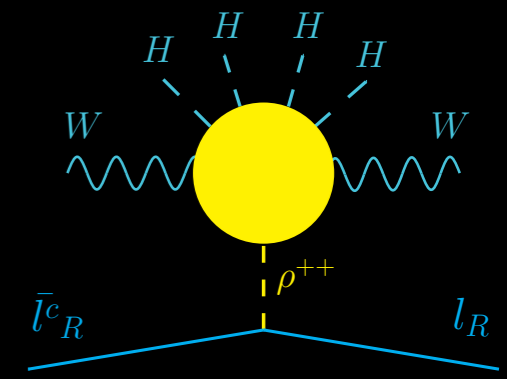


The Cocktail Model 1₂2₂



Inert Doublet Model “&” Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix} \quad S^+, \quad \rho^{++}$$



The Cocktail Model 1₂2₂

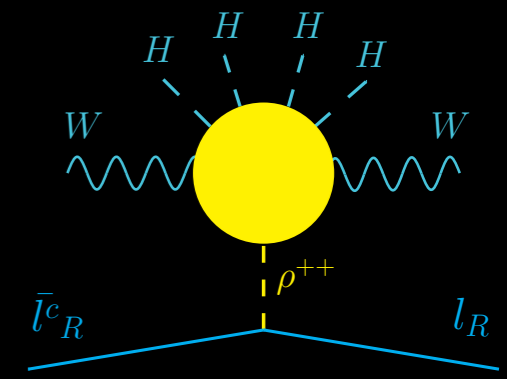


Inert Doublet Model “&” Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

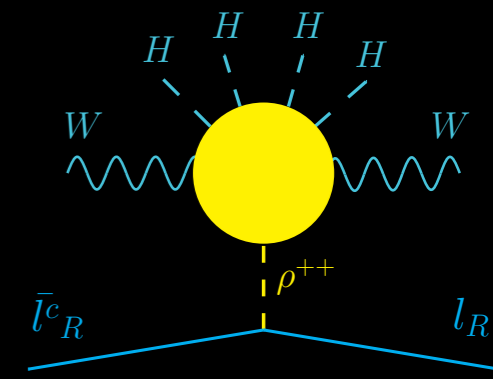
$S^+, \quad \rho^{++}$

$Z_2 \quad + \quad - \quad - \quad +$





The Cocktail Model $1_2 2_2$



Inert Doublet Model “&” Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

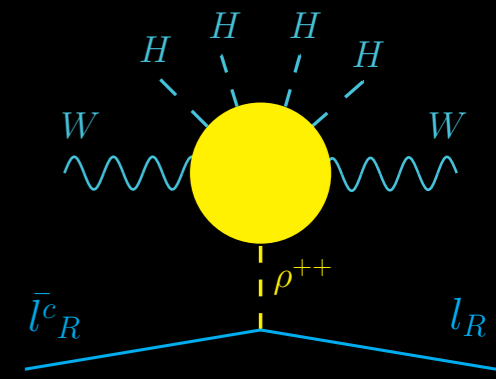
Z_2 + - - +

$S^+, \quad \rho^{++}$

Field	$SU(2)$	$U(1)_Y$	Z_2
ϕ_1	2	-1/2, 1/2	+
ϕ_2	2	-1/2, 1/2	-
S^+	1	+1	-
ρ^{++}	1	+2	+



The Cocktail Model $1_2 2_2$



Inert Doublet Model

“&”

Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

Z_2 + - - +

S^+ , ρ^{++}

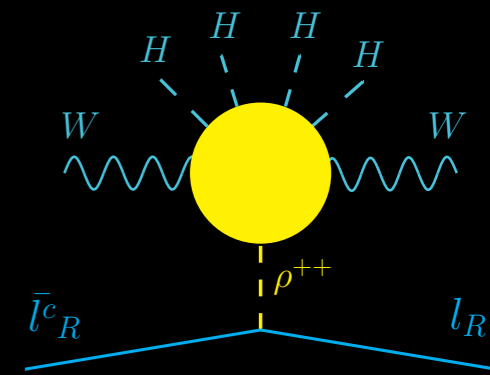
Field	$SU(2)$	$U(1)_Y$	Z_2
ϕ_1	2	-1/2, 1/2	+
ϕ_2	2	-1/2, 1/2	-
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ρ^{++}	1	+2	+

The Lagrangian

$$\Delta \mathcal{L}_{GNR} = -C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho^{++} + \kappa_1 \Phi_2^T i \sigma_2 \Phi_1 S^- + \kappa_2 \rho^{++} S^- S^- + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_{\rho S} \Phi_2^T i \sigma_2 \Phi_1 S^+ \rho^{--} + h.c. + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + V(|\Phi_1|^2, |\Phi_2|^2, |S|^2, |\rho|^2)$$



The Cocktail Model $1_2 2_2$



Inert Doublet Model “&” Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

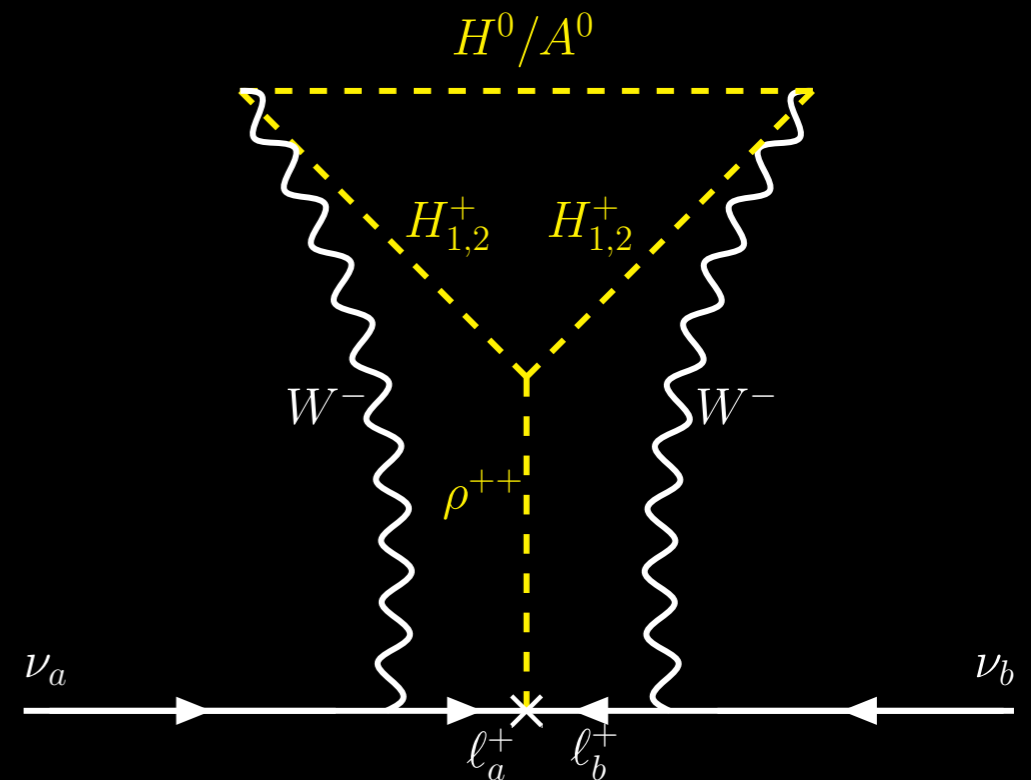
Z_2 + - - +

S^+ , ρ^{++}

Field	$SU(2)$	$U(1)_Y$	Z_2
ϕ_1	2	-1/2, 1/2	+
ϕ_2	2	-1/2, 1/2	-
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The Lagrangian

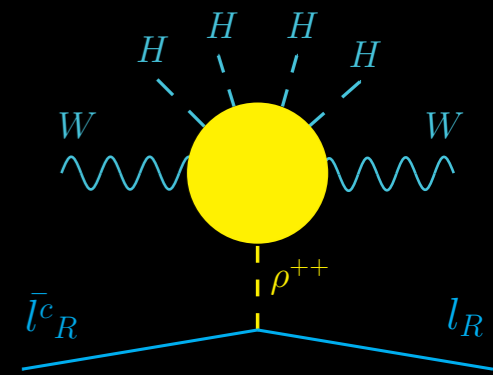
$$\Delta \mathcal{L}_{GNR} = -C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho^{++} + \kappa_1 \Phi_2^T i \sigma_2 \Phi_1 S^- + \kappa_2 \rho^{++} S^- S^- + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_{\rho S} \Phi_2^T i \sigma_2 \Phi_1 S^+ \rho^{--} + h.c. + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + V(|\Phi_1|^2, |\Phi_2|^2, |S|^2, |\rho|^2)$$



$C_{ab}, \lambda_5 \neq 0$ and two of $\kappa_1, \kappa_2, \lambda_{\rho S} \neq 0$ to break lepton number



The Cocktail Model $1_2 2_2$



Inert Doublet Model “&” Inspired by Babu/Zee

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} + v \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix}$$

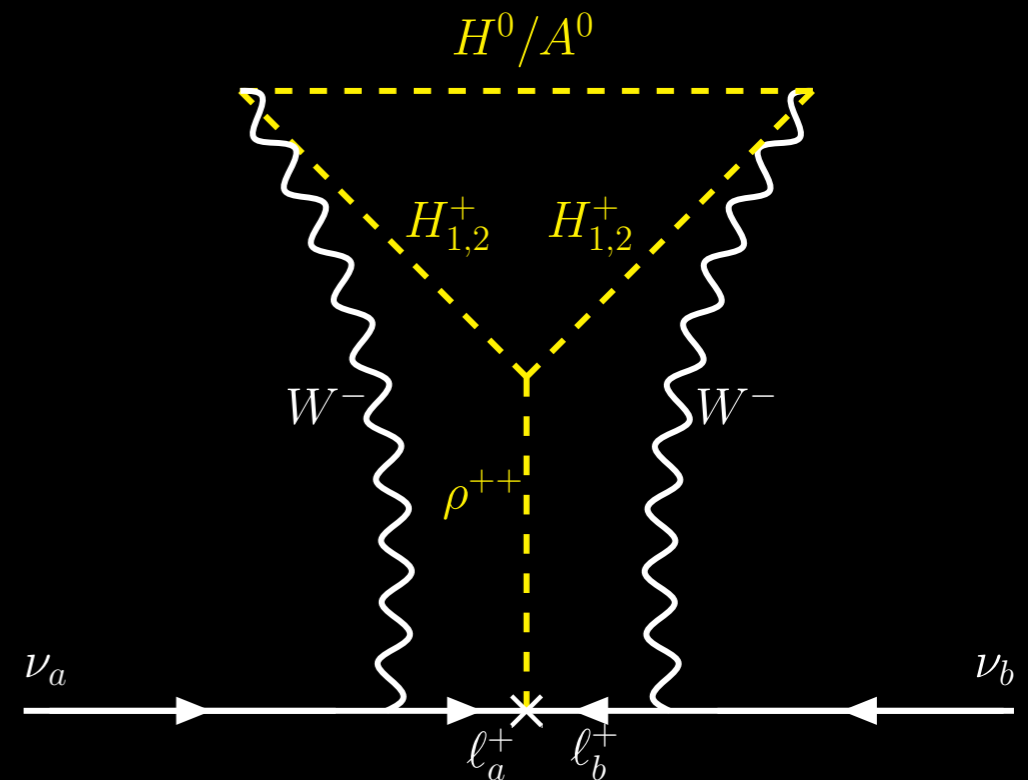
Z_2 + - - +

S^+ , ρ^{++}

Field	$SU(2)$	$U(1)_Y$	Z_2
ϕ_1	2	-1/2, 1/2	+
ϕ_2	2	-1/2, 1/2	-
S^+	1	+1	-
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The Lagrangian

$$\Delta\mathcal{L}_{GNR} = -C_{ab} \bar{l}_{R_a}^c l_{R_b} \rho^{++} + \kappa_1 \Phi_2^T i\sigma_2 \Phi_1 S^- + \kappa_2 \rho^{++} S^- S^- + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_{\rho S} \Phi_2^T i\sigma_2 \Phi_1 S^+ \rho^{--} + h.c. + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + V(|\Phi_1|^2, |\Phi_2|^2, |S|^2, |\rho|^2)$$



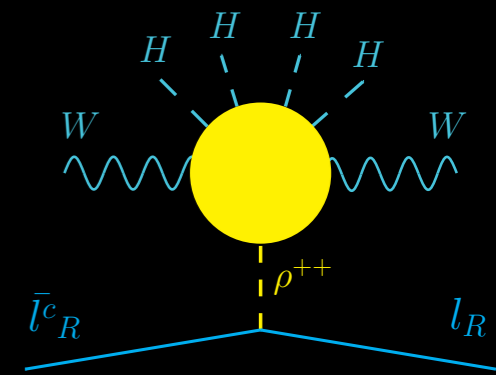
$C_{ab}, \lambda_5 \neq 0$ and two of $\kappa_1, \kappa_2, \lambda_{\rho S} \neq 0$ to break lepton number

$$m_{ab}^\nu = C_{ab} \frac{m_a^\ell m_b^\ell s_{2\beta}}{(16\pi^2)^3 m_\rho} \frac{M_W^4 \Delta m_+^2 \Delta m_0^2}{v^8} (\mathcal{A}_1 \mathcal{I}_1 + \mathcal{A}_2 \mathcal{I}_2)$$

$$\mathcal{A}_1 \simeq \frac{\kappa_2 s_{2\beta} + \xi v c_{2\beta}}{\sqrt{v m_\rho}}, \quad \mathcal{A}_2 \simeq 10\xi$$

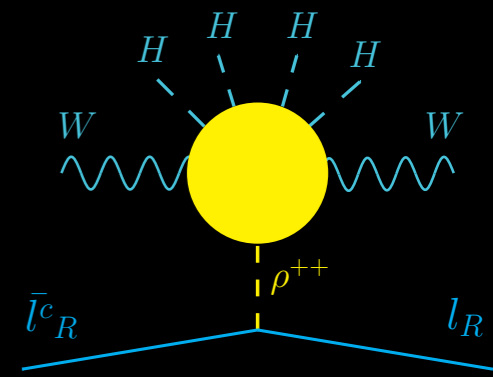


The Cocktail Model $1_2 2_2$ Phenomenology





The Cocktail Model 1₂2₂ Phenomenology



- EWPT

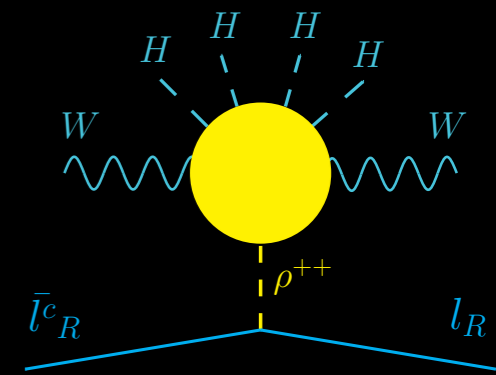
$$\Delta T = \frac{1}{16\pi m_w^2 s_{\theta_w}^2} \left[c_\beta^2 (F_{H_1, H_0} + F_{H_1, A_0}) + s_\beta^2 (F_{H_2, H_0} + F_{H_2, A_0}) - 2c_\beta^2 s_\beta^2 F_{H_1, H_2} - F_{H_0, A_0} \right]$$

$$F_{i,j} = \frac{m_i^2 + m_j^2}{2} - \frac{m_i^2 m_j^2}{m_i^2 - m_j^2} \ln \frac{m_i^2}{m_j^2}$$



The Cocktail Model 1₂2₂

Phenomenology



● EWPT

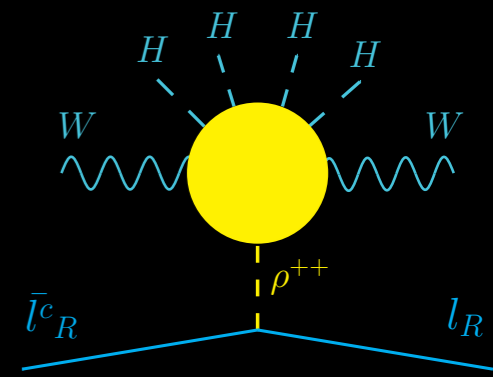
$$\Delta T = \frac{1}{16\pi m_w^2 s_{\theta_w}^2} \left[c_\beta^2 (F_{H_1, H_0} + F_{H_1, A_0}) + s_\beta^2 (F_{H_2, H_0} + F_{H_2, A_0}) - 2c_\beta^2 s_\beta^2 F_{H_1, H_2} - F_{H_0, A_0} \right]$$

$$F_{i,j} = \frac{m_i^2 + m_j^2}{2} - \frac{m_i^2 m_j^2}{m_i^2 - m_j^2} \ln \frac{m_i^2}{m_j^2}$$

Neutrino mass is proportional to $\Delta m_+^2, \Delta m_0^2 \gtrsim v^2$



The Cocktail Model 1₂2₂ Phenomenology



● EWPT

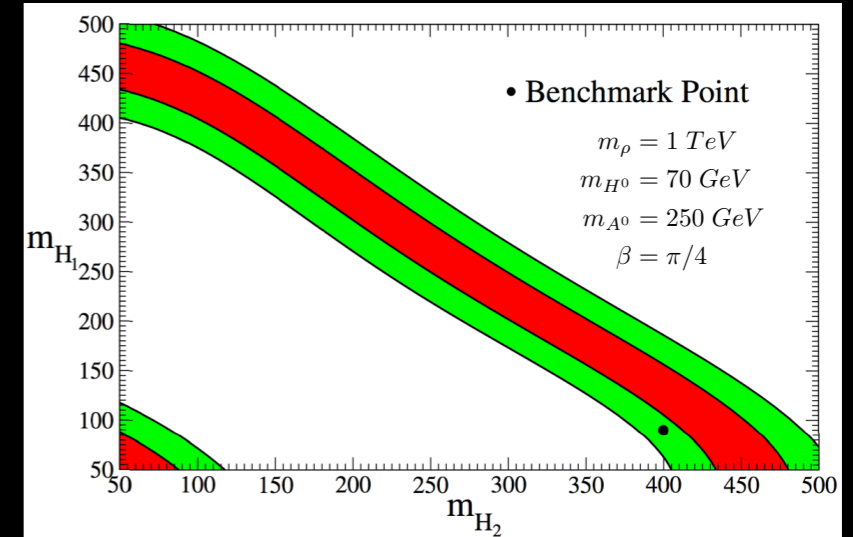
$$\Delta T = \frac{1}{16\pi m_w^2 s_{\theta_w}^2} \left[c_\beta^2 (F_{H_1, H_0} + F_{H_1, A_0}) + s_\beta^2 (F_{H_2, H_0} + F_{H_2, A_0}) - 2c_\beta^2 s_\beta^2 F_{H_1, H_2} - F_{H_0, A_0} \right]$$

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Neutrino mass is proportional to $\Delta m_{+}^2, \Delta m_0^2 \gtrsim v^2$

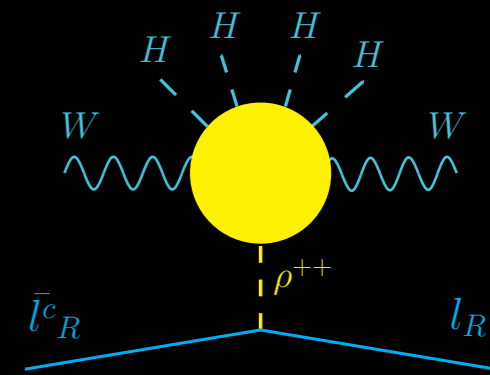
Mass correlation between new states

$$m_{H_2^+} \gg m_{A_0} \gg m_{H_1^+}, m_{H_0}$$





The Cocktail Model 1₂2₂ Phenomenology



● EWPT

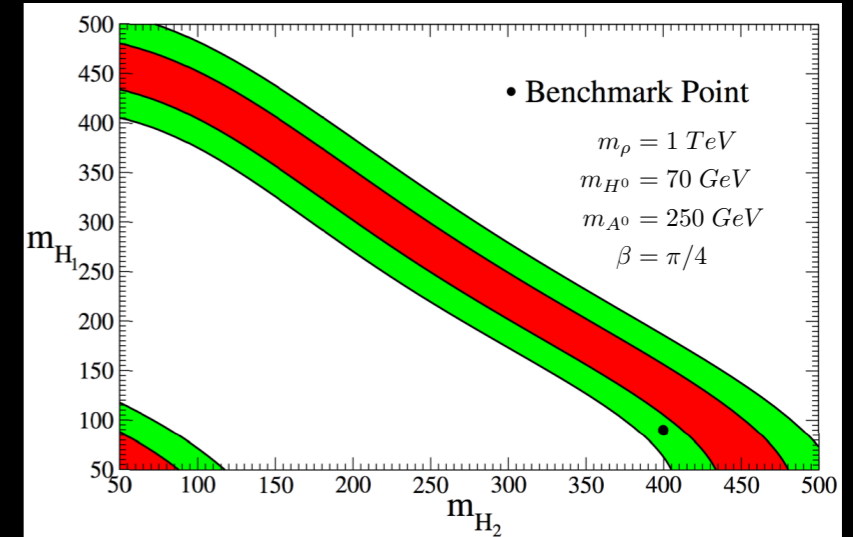
$$\Delta T = \frac{1}{16\pi m_w^2 s_{\theta_w}^2} [c_\beta^2 (F_{H_1, H_0} + F_{H_1, A_0}) + s_\beta^2 (F_{H_2, H_0} + F_{H_2, A_0}) - 2c_\beta^2 s_\beta^2 F_{H_1, H_2} - F_{H_0, A_0}]$$

$$F_{i,j} = \frac{m_i^2 + m_j^2}{2} - \frac{m_i^2 m_j^2}{m_i^2 - m_j^2} \ln \frac{m_i^2}{m_j^2}$$

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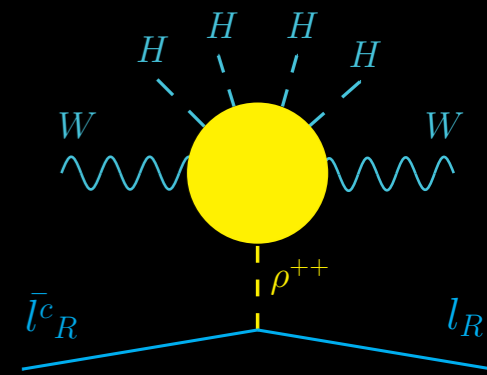
$$m_{H_2^+} \gg m_{A_0} \gg m_{H_1^+}, m_{H_0}$$



● Dark Matter



The Cocktail Model 1₂2₂ Phenomenology



● EWPT

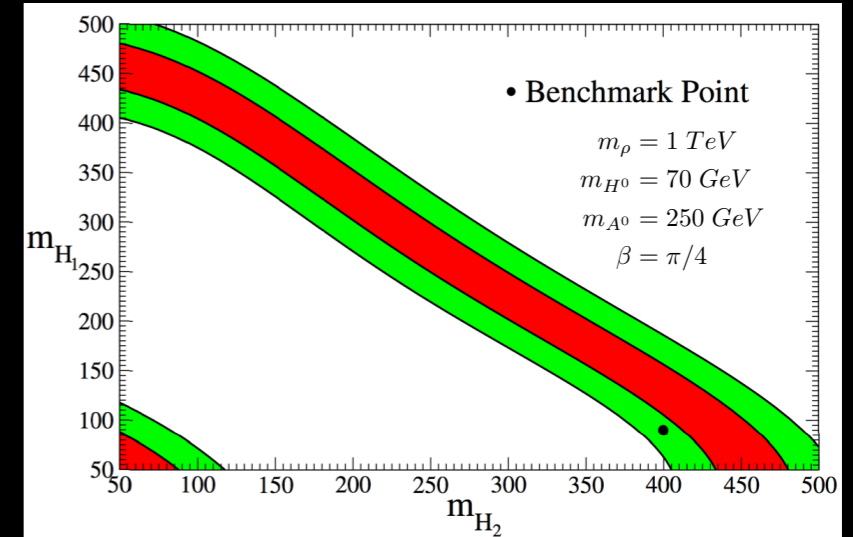
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Neutrino mass is proportional to $\Delta m_{+}^2, \Delta m_0^2 \gtrsim v^2$

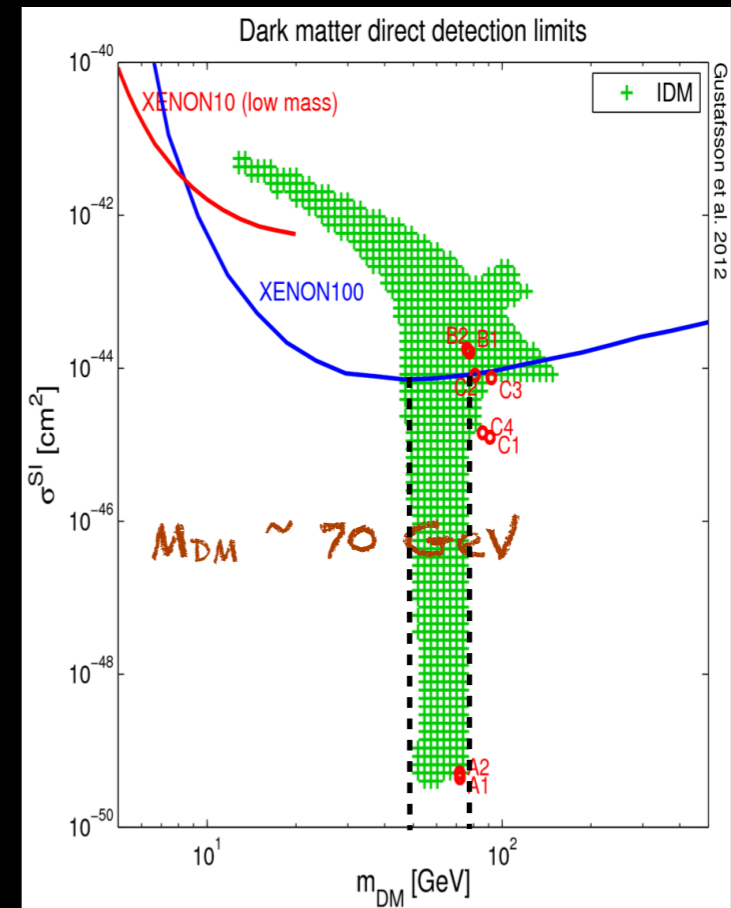
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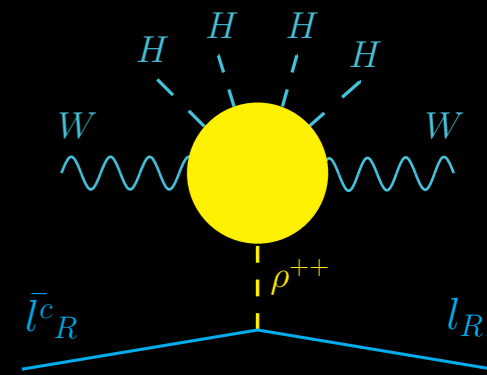
● Dark Matter

Basically 2HDM DM candidate





The Cocktail Model 1₂2₂ Phenomenology



● EWPT

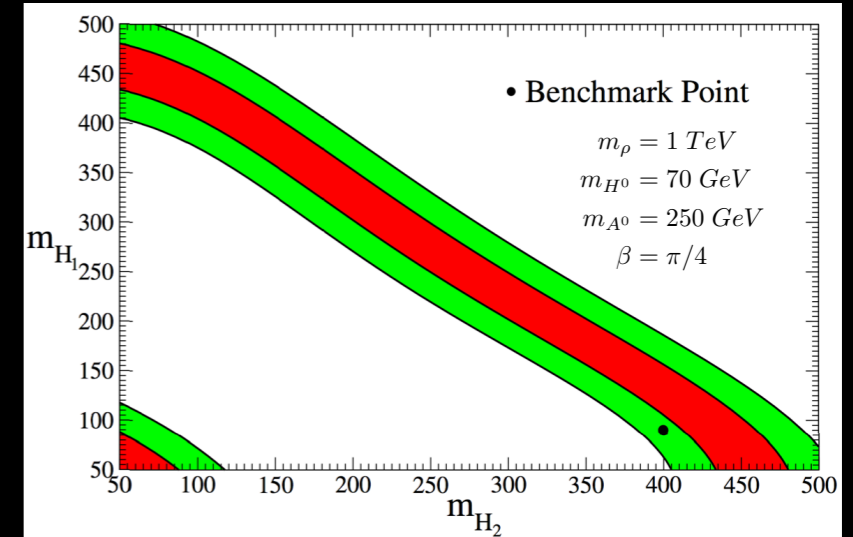
$$\Delta T = \frac{1}{16\pi m_w^2 s_{\theta_w}^2} [c_\beta^2 (F_{H_1, H_0} + F_{H_1, A_0}) + s_\beta^2 (F_{H_2, H_0} + F_{H_2, A_0}) - 2c_\beta^2 s_\beta^2 F_{H_1, H_2} - F_{H_0, A_0}]$$

$$F_{i,j} = \frac{m_i^2 + m_j^2}{2} - \frac{m_i^2 m_j^2}{m_i^2 - m_j^2} \ln \frac{m_i^2}{m_j^2}$$

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Mass correlation between new states

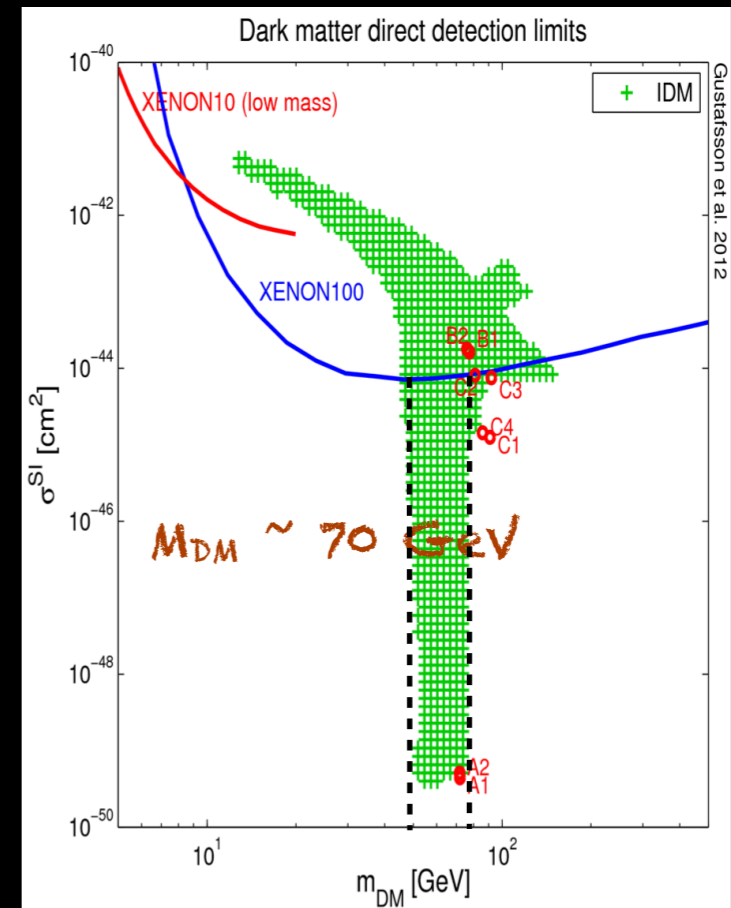
$$m_{H_2^+} \gg m_{A_0} \gg m_{H_1^+}, m_{H_0}$$



● Dark Matter

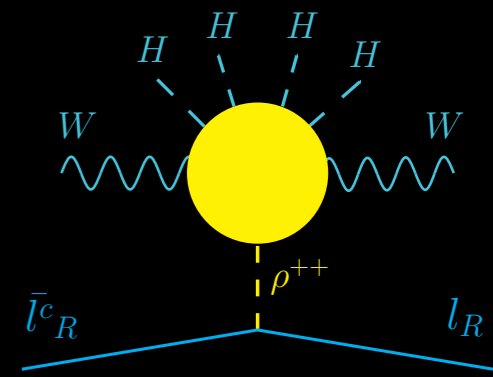
Basically 2HDM DM candidate

1. Higgs portal (resonance): ~ 60 GeV
2. Coannihilation with A^0 (gives too small m_ν)
3. $H^0 H^0 \rightarrow WW$ threshold effect: ~ 70 GeV (gives striking gamma-ray lines)





The Lollipop Model 1₂23





The Lollipop Model 1₂23

Inert triplet Model

“&”

Singlets

$$\Delta = \frac{1}{\sqrt{2}} \begin{pmatrix} \Delta^+ & \sqrt{2}\Delta^{++} \\ \Delta^0 + iA^0 & -\Delta^+ \end{pmatrix},$$

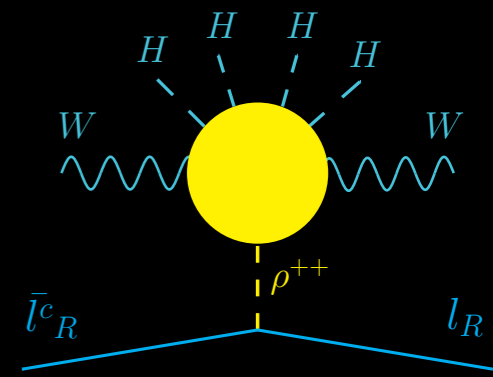
σ, ρ^{++}

Z_2

-

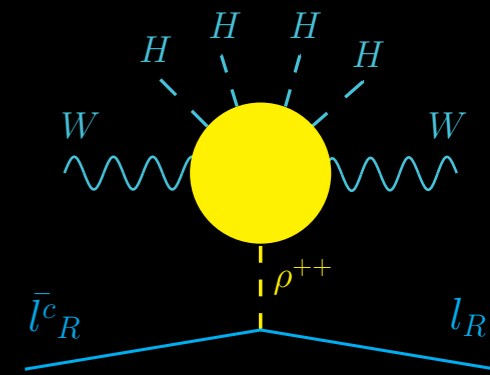
-

+





The Lollipop Model 1₂2₃



Inert triplet Model

“&”

Singlets

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$$\sigma, \quad \rho^{++}$$

Z_2

-

-

+

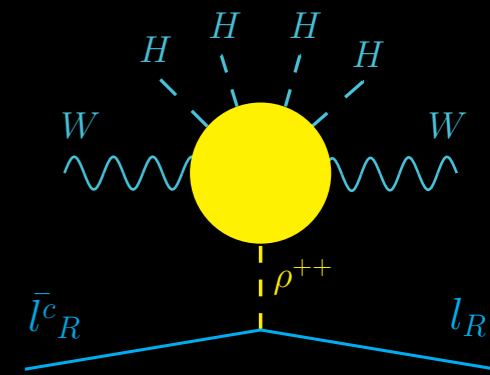
The Lagrangian

$$\begin{aligned} \mathcal{L} \supset & \text{Tr}[(D_\mu \Delta)^\dagger D^\mu \Delta] + \partial_\mu \sigma \partial^\mu \sigma + (D_\mu \rho)^\dagger D^\mu \rho - m_\Delta^2 \text{Tr}[\Delta^\dagger \Delta] - \frac{m_\sigma^2}{2} \sigma^2 \\ & - \lambda_{H\Delta} |H|^2 \text{Tr}[\Delta^\dagger \Delta] - \lambda_{H\sigma} |H|^2 \sigma^2 - \tilde{\lambda}_{H\Delta} H^\dagger \Delta \Delta^\dagger H - \kappa_2 \text{Tr}[\Delta \Delta] \rho^{--} \\ & - \lambda_6 \sigma H^\dagger \Delta \tilde{H} - C_{ab} \bar{\ell}^c_{R_a} \ell_{R_b} \rho^{++} + \text{h.c.} \end{aligned}$$

$$+V(\sigma, \rho, H, \Delta)$$



The Lollipop Model 1₂23



Inert triplet Model

“&”

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$$\Delta = \frac{1}{\sqrt{2}} \begin{pmatrix} \Delta^+ & \sqrt{2}\Delta^{++} \\ \Delta^0 + iA^0 & -\Delta^+ \end{pmatrix},$$

$$\sigma, \quad \rho^{++}$$

Z_2

-

-

+

The Lagrangian

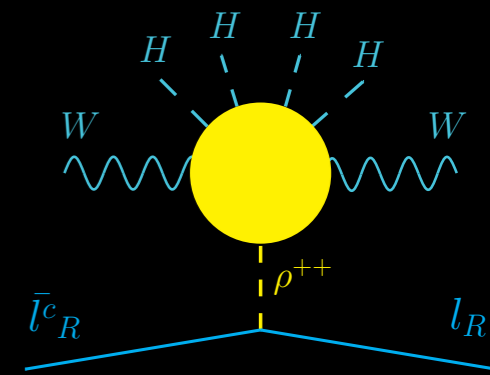
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$$+V(\sigma, \rho, H, \Delta)$$

$C_{ab}, \kappa_2, \lambda_6 \neq 0$
to break lepton number



The Lollipop Model 1₂23



Inert triplet Model

“&”

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$$\sigma, \quad \rho^{++}$$

Z_2

-

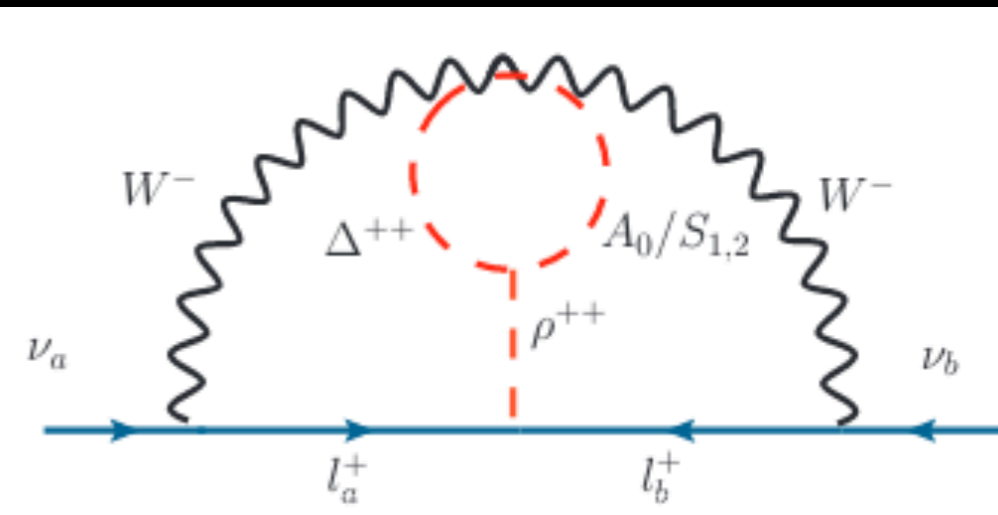
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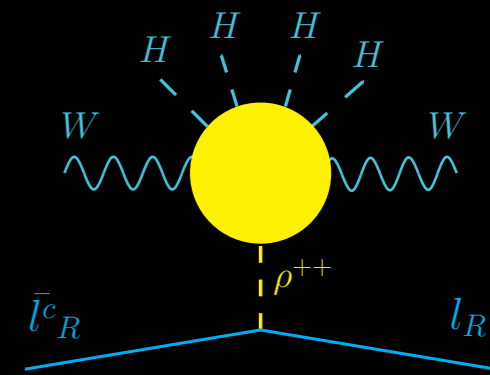
$$+V(\sigma, \rho, H, \Delta)$$



$C_{ab}, \kappa_2, \lambda_6 \neq 0$
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The Lollipop Model 1₂23



Inert triplet Model

“&”

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$$\Delta = \frac{1}{\sqrt{2}} \begin{pmatrix} \Delta^+ & \sqrt{2}\Delta^{++} \\ \Delta^0 + iA^0 & -\Delta^+ \end{pmatrix},$$

$$\sigma, \quad \rho^{++}$$

Z_2

-

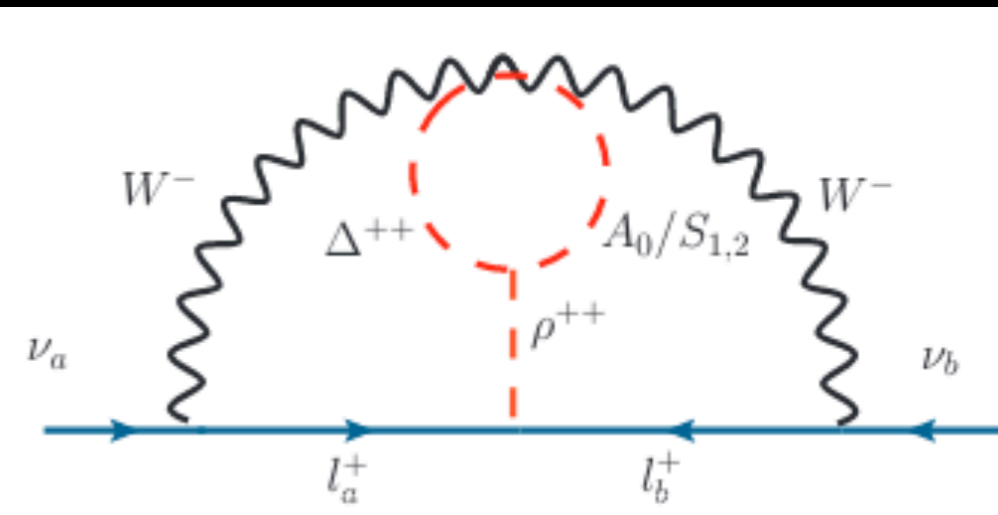
-

+

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$$+V(\sigma, \rho, H, \Delta)$$



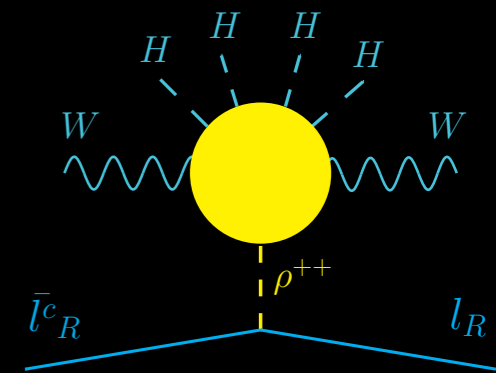
$C_{ab}, \kappa_2, \lambda_6 \neq 0$
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$$m_{ab}^\nu = C_{ab} \frac{m_a^\ell m_b^\ell}{(16\pi^2)^3 m_\rho^2} 8\kappa_2 \lambda_6^2 \times \mathcal{I}_\nu$$



The Lolipop Model 1₂23

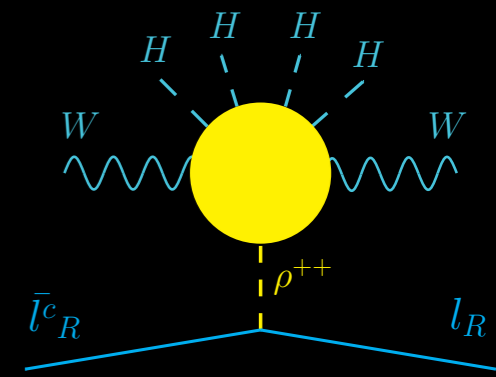
Phenomenology





The Lolipop Model 1₂23

Phenomenology



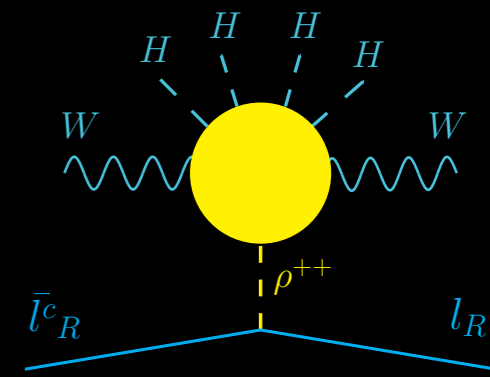
- EWPT

All Z_2 odd fields $\rho^{++}, \Delta^{++}, A_0, S_{1,2}$ contribute to S, T, U parameters



The Lolipop Model 1₂23

Phenomenology

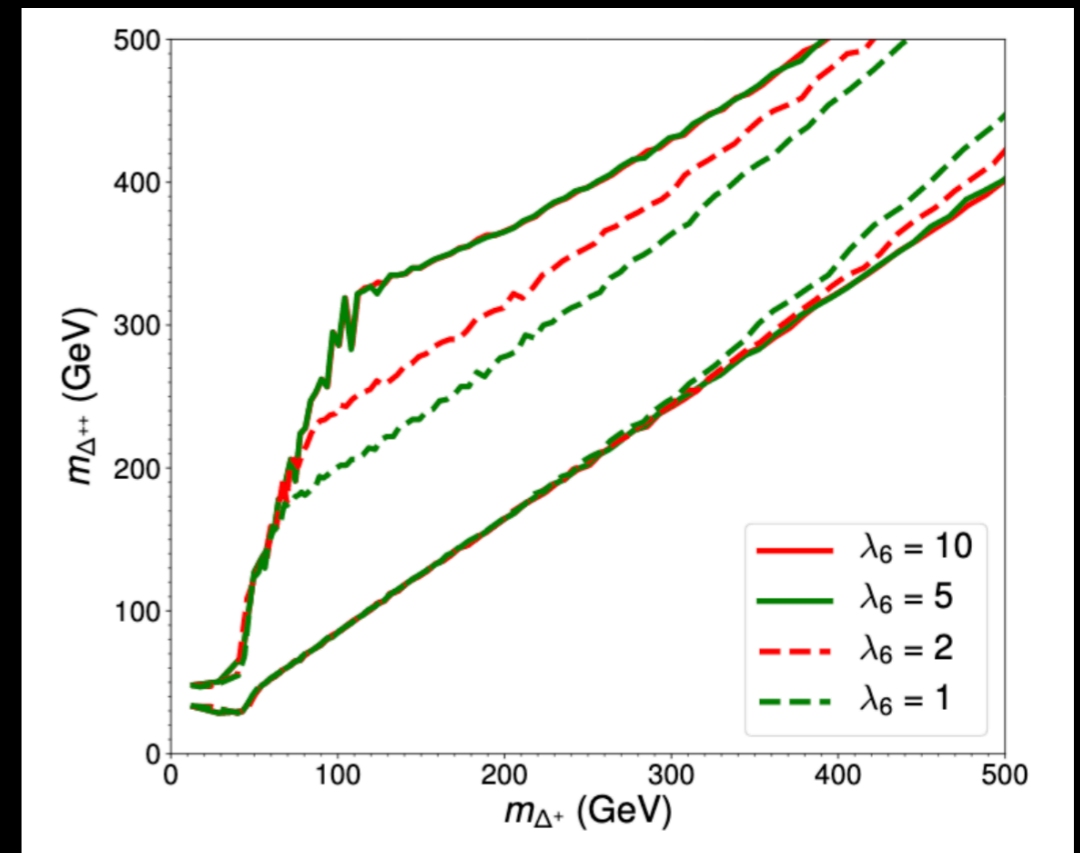


● EWPT

All Z_2 odd fields $\rho^{++}, \Delta^{++}, A_0, S_{1,2}$ contribute to S, T, U parameters

$$|m_{\Delta^{++}} - m_{\Delta^+}| \lesssim 100 \text{ GeV for } \lambda_6 \lesssim 1$$

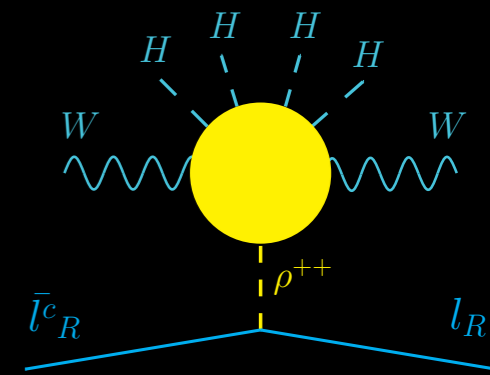
$$|m_{\Delta^{++}} - m_{\Delta^+}| \lesssim 200 \text{ GeV for } \lambda_6 \lesssim 4\pi$$





The Lolipop Model 1₂23

Phenomenology



● EWPT

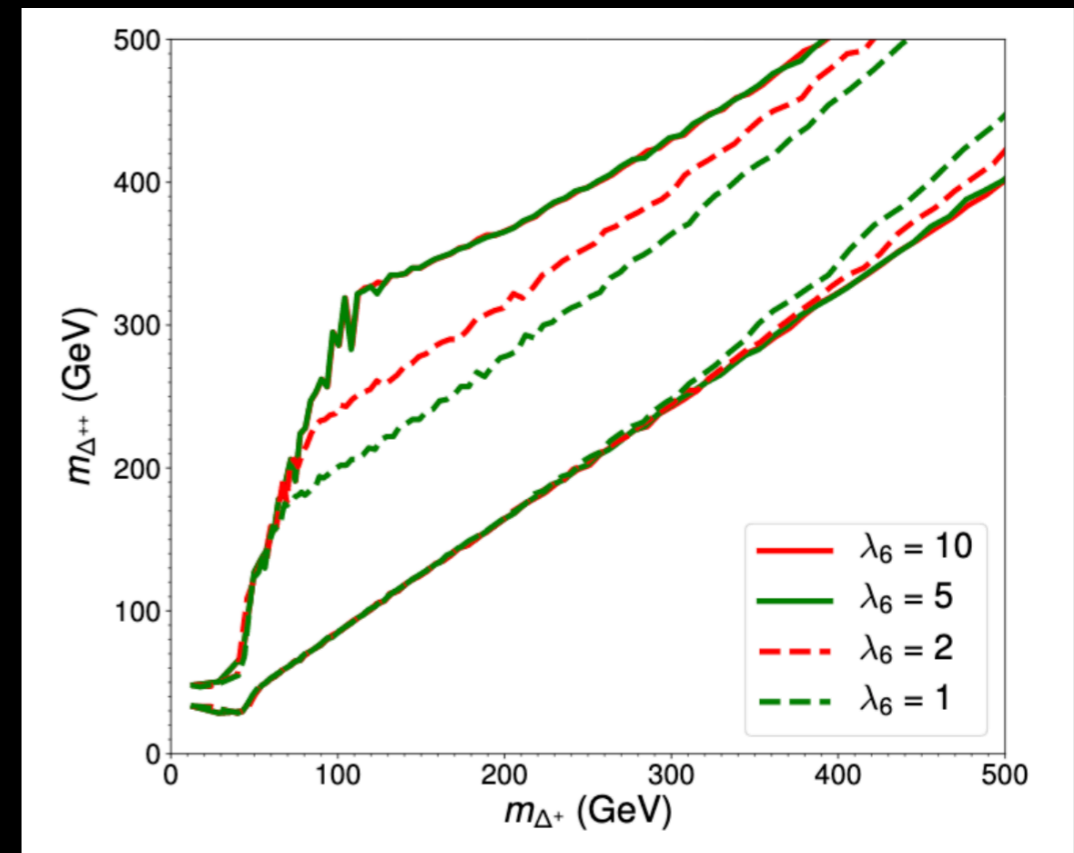
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● Dark Matter

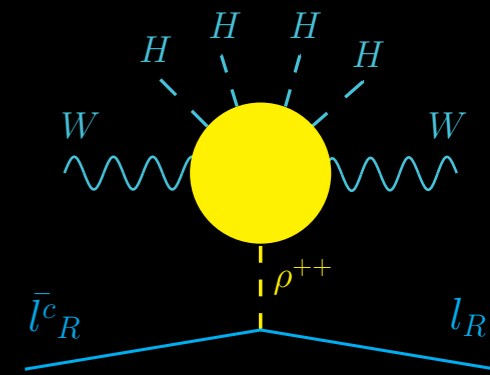
DM is mainly singlet \rightarrow the model resembles Higgs portal singlet scenario





The Lolipop Model 1₂23

Phenomenology



● EWPT

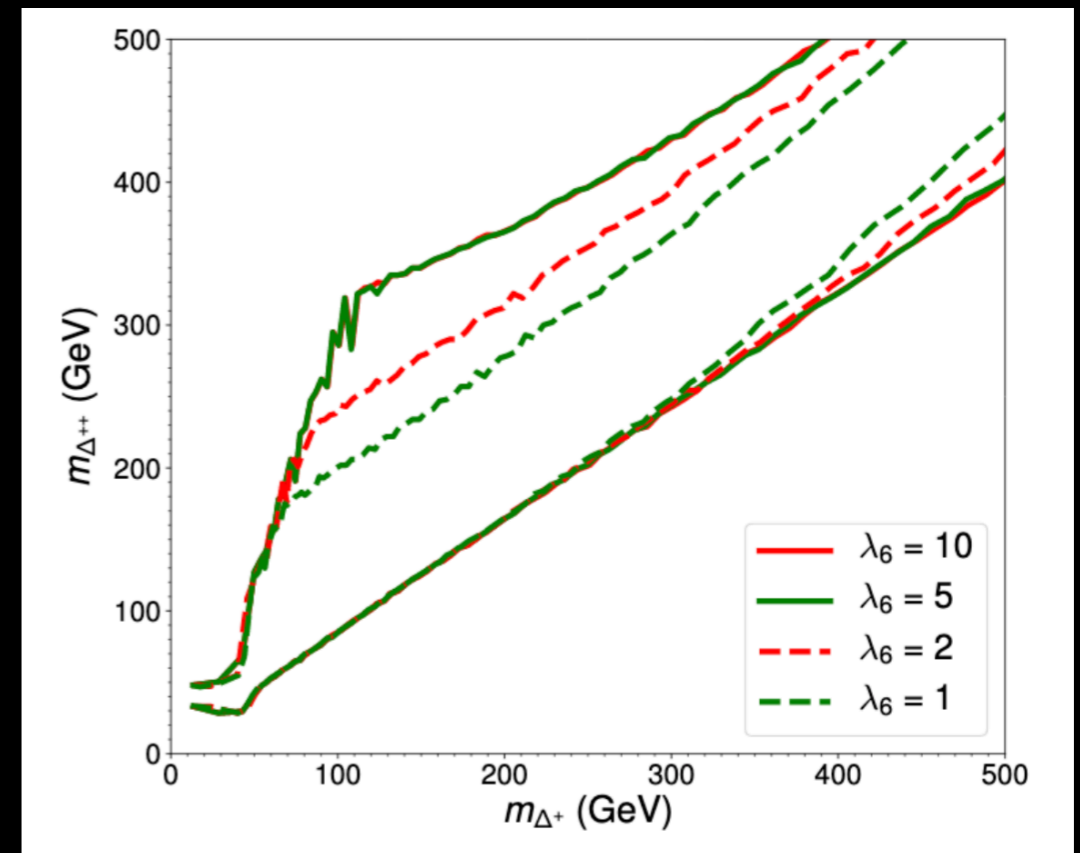
All Z_2 odd fields $\rho^{++}, \Delta^{++}, A_0, S_{1,2}$ contribute to S, T, U parameters

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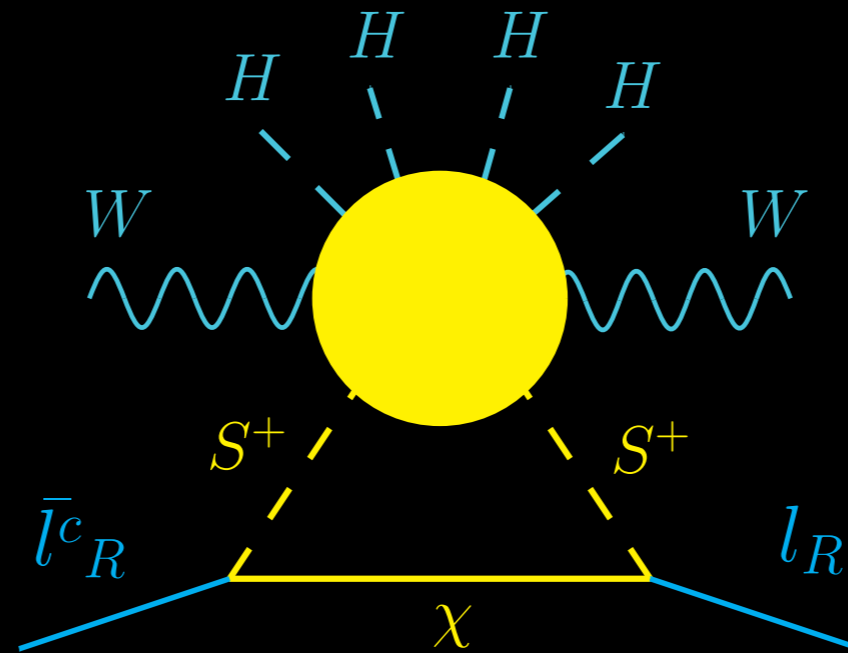
● Dark Matter

DM is mainly singlet \rightarrow the model resembles Higgs portal singlet scenario



$$\mathcal{L} \supset -\lambda_{S_2} S_2^2 \left(2\sqrt{2}vh + h^2 \right)$$

UV Completions Class 2a

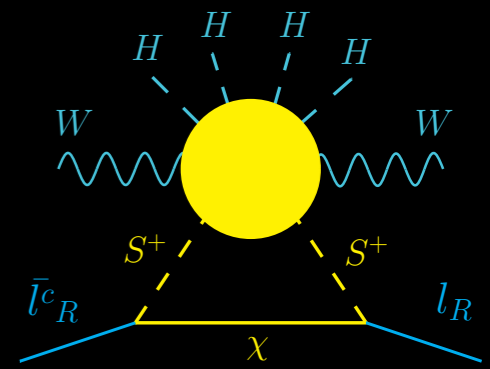


$SU(2)_L$ Singlet χ and S

Jin, Li-Gang *et al.* Phys.Lett. B741 (2015) 163-167

Chao-Qiang Geng *et al.* Phys.Lett. B745 (2015) 56-57

$SU(2)_L$ Singlet χ and S



$SU(2)_L$ Singlet χ and S

Singlets

$$\chi_i \equiv N_{R_i},$$

$$S^+,$$

Z_2

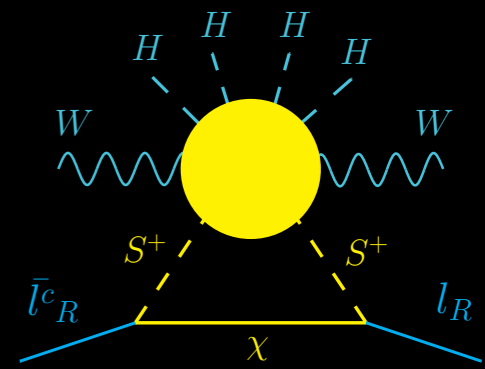
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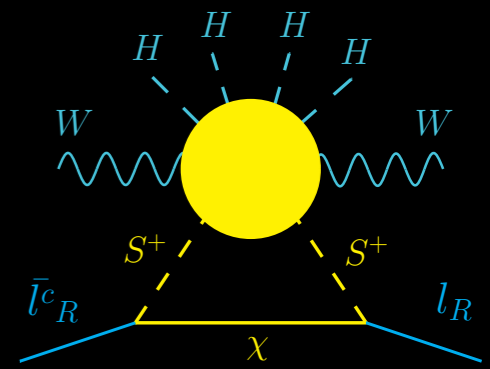
Triplet

$$\Delta = \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_0 & \Delta^+ \\ \Delta^- & -\frac{1}{\sqrt{2}}\Delta_0 \end{pmatrix}$$

-



$SU(2)_L$ Singlet χ and S



Singlets

$$\chi_i \equiv N_{R_i}, \quad S^+,$$

Z_2

-

-

Triplet

$$\Delta = \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_0 & \Delta^+ \\ \Delta^- & -\frac{1}{\sqrt{2}}\Delta_0 \end{pmatrix}$$

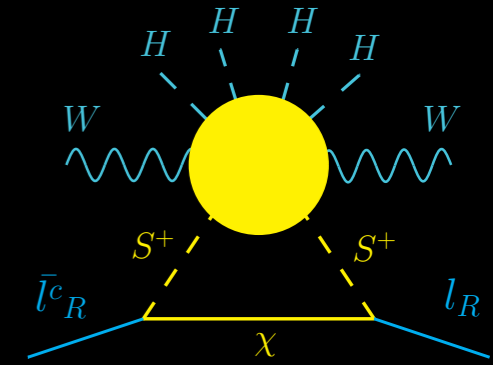
-

The Lagrangian

$$\mathcal{L} = \frac{1}{2} \text{Tr} \left[(D_\mu \Delta)^\dagger (D^\mu \Delta) \right] + (D_\mu S)^* (D^\mu S) + i \overline{N_{R_i}} \partial N_{R_i} - \frac{1}{2} m_{N_i} \overline{N_{R_i}} N_{R_i}^c - g_{ia} \overline{N_{R_i}} \ell_{R_a}^c S^+ + \text{h.c.}$$

$$+V(S, H, \Delta)$$

$SU(2)_L$ Singlet χ and S



Singlets

$$\chi_i \equiv N_{R_i},$$

$$S^+,$$

Triplet

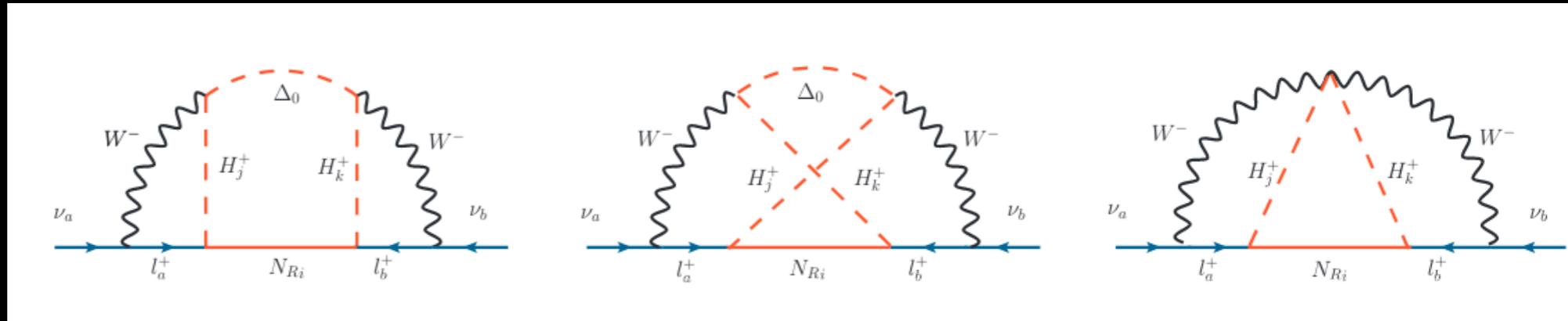
$$\Delta = \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_0 & \Delta^+ \\ \Delta^- & -\frac{1}{\sqrt{2}}\Delta_0 \end{pmatrix}$$

Z_2

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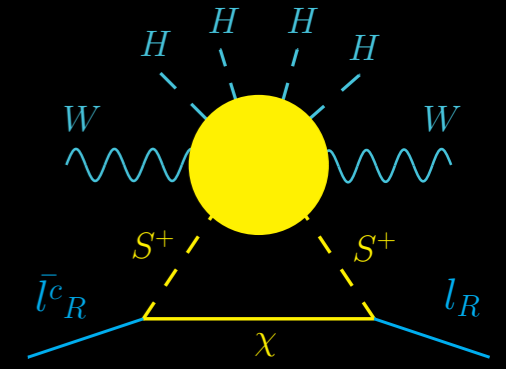


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$$+V(S, H, \Delta)$$

$SU(2)_L$ Singlet χ and S



Singlets

$$\chi_i \equiv N_{R_i},$$

$$S^+,$$

Triplet

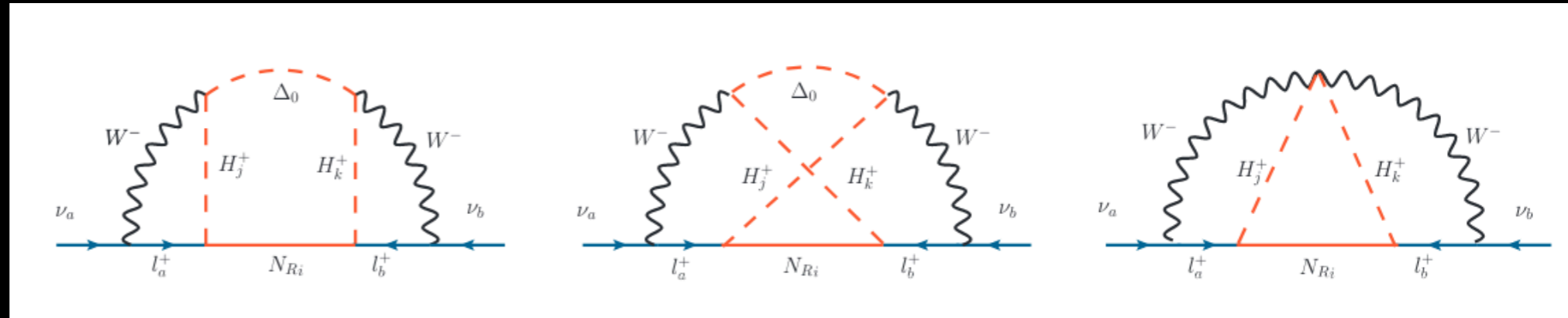
$$\Delta = \begin{pmatrix} \frac{1}{\sqrt{2}}\Delta_0 & \Delta^+ \\ \Delta^- & -\frac{1}{\sqrt{2}}\Delta_0 \end{pmatrix}$$

Z_2

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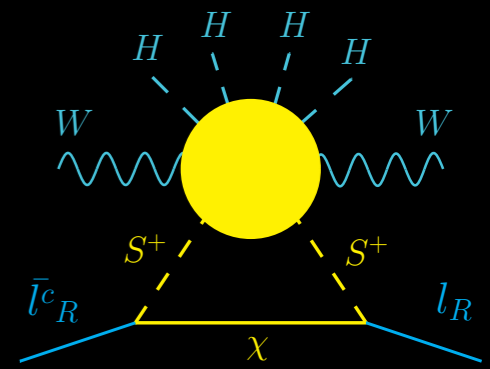
The Lagrangian

$$\mathcal{L} = \frac{1}{2} \text{Tr} \left[(D_\mu \Delta)^\dagger (D^\mu \Delta) \right] + (D_\mu S)^* (D^\mu S) + i \overline{N_{R_i}} \partial N_{R_i} - \frac{1}{2} m_{N_i} \overline{N_{R_i}} N_{R_i}^c - g_{ia} \overline{N_{R_i}} \ell_{R_a}^c S^+ + \text{h.c.}$$

$+V(S, H, \Delta)$

$$m_{ab}^\nu = \frac{m_W^4}{v^4} \frac{m_a^\ell m_b^\ell \sin^2(2\beta) (m_{H_1}^2 - m_{H_2}^2)^2}{(16\pi^2)^3} \times \sum_{j=1}^3 \sum_{i=1}^n m_{N_i} g_{ia} g_{ib} I_j(m_{N_i})$$

$SU(2)_L$ Singlet χ and S Phenomenology

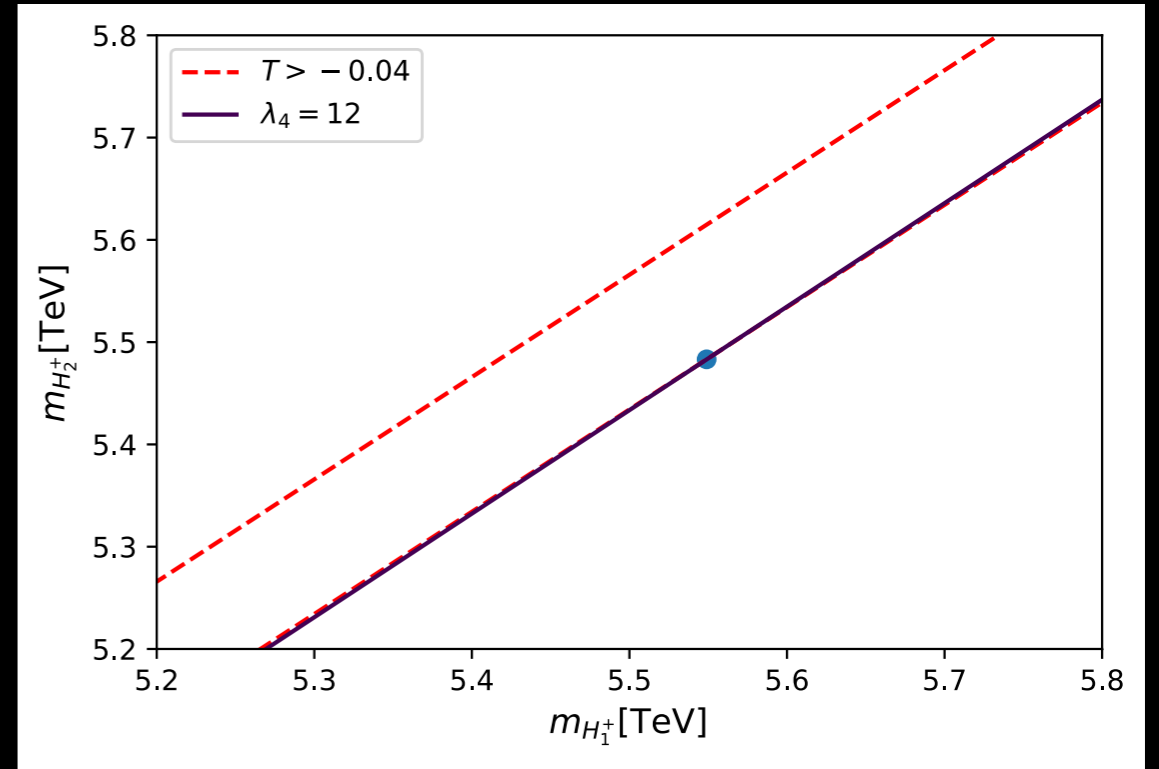


● EWPT

$$\Delta T = \frac{1}{4\pi s_W^2 m_W^2} [c_\beta^2 F_{\Delta^0, H_1} + s_\beta^2 F_{\Delta^0, H_2} - 2s_\beta^2 c_\beta^2 F_{H_1, H_2}]$$

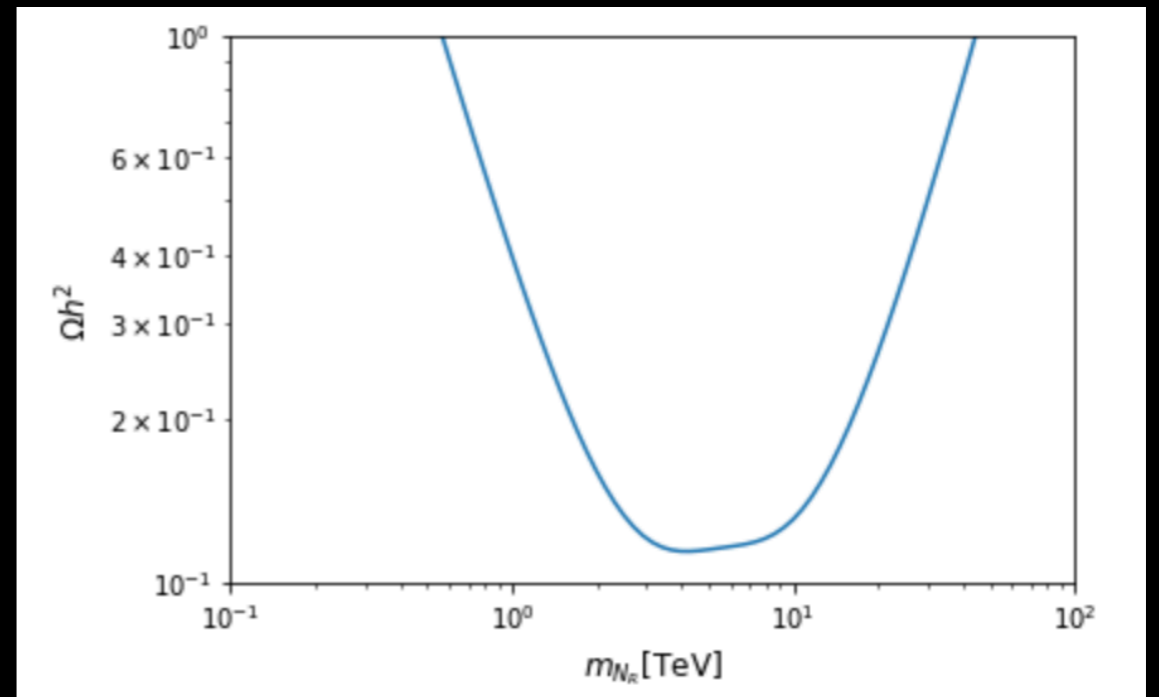
● Dark Matter

$$\sigma v_{\text{rel}} = \frac{\sum_{(\alpha, \beta)} |g_{1\alpha}^* g_{1\beta}|^2}{48\pi} m_{N_1}^2 F(m_{N_1}, m_{H_1^+}, m_{H_2^+}) v_{\text{rel}}^2 = a + b v_{\text{rel}}^2$$



$$\Omega_{N_1} h^2 \approx \frac{1.07 \times 10^9 \text{ GeV}^{-1}}{M_P} \frac{X_F^2}{\sqrt{g_*} 3b}$$

$$x_F = \ln \left[\frac{5}{4} \sqrt{\frac{45}{8}} \frac{g}{2\pi^3} \frac{M_P N_{N_1} 6b}{x_F \sqrt{g_*} \chi_F} \right]$$



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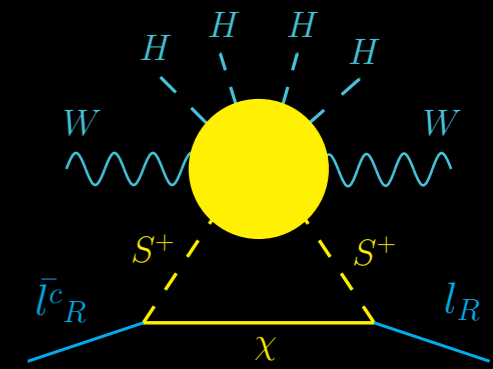
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Challenges

- To create a systematic exploration inside the classes , in order to build all UV completions

非常感謝

$SU(2)_L$ Singlet χ and S Phenomenology



- LFVP

$$\text{Br}(l_\alpha \rightarrow l_\beta \gamma) = \frac{3\alpha}{64\pi G_F^2} \left| \sum_{i=1,2} g_{i\alpha}^* g_{i\beta} G(\beta, m_{H_1^+}, m_{H_2^+}) \right|^2 \text{Br}(l_\alpha \rightarrow l_\beta \nu_\alpha \bar{\nu}_\beta)$$

