



Probing CP-odd Higgs couplings

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Probing CP-odd Higgs couplings

“Everything has been said, but not yet by everybody”

[Karl Valentin]

Michael Spannowsky

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Existing experimental results in searches of CP violating effects in Higgs coupling measurements

[ATLAS 1602.04516]

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \tilde{g}_{HAA} H \tilde{A}_{\mu\nu} A^{\mu\nu} + \tilde{g}_{HAZ} H \tilde{A}_{\mu\nu} Z^{\mu\nu} + \tilde{g}_{HZZ} H \tilde{Z}_{\mu\nu} Z^{\mu\nu} + \tilde{g}_{HWW} H \tilde{W}_{\mu\nu}^+ W^{-\mu\nu}$$

→ Only 2 linearly indep. due to gauge invariance

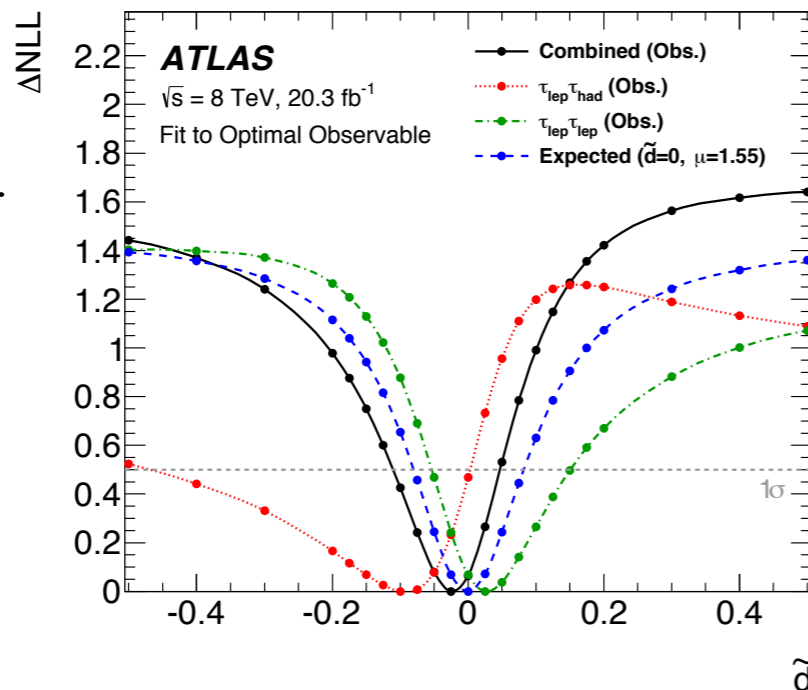
→ relate two parameters → get \tilde{d}

In WBF H → $\tau\tau$

Excluded at 68% CL

$$\tilde{d} < -0.11$$

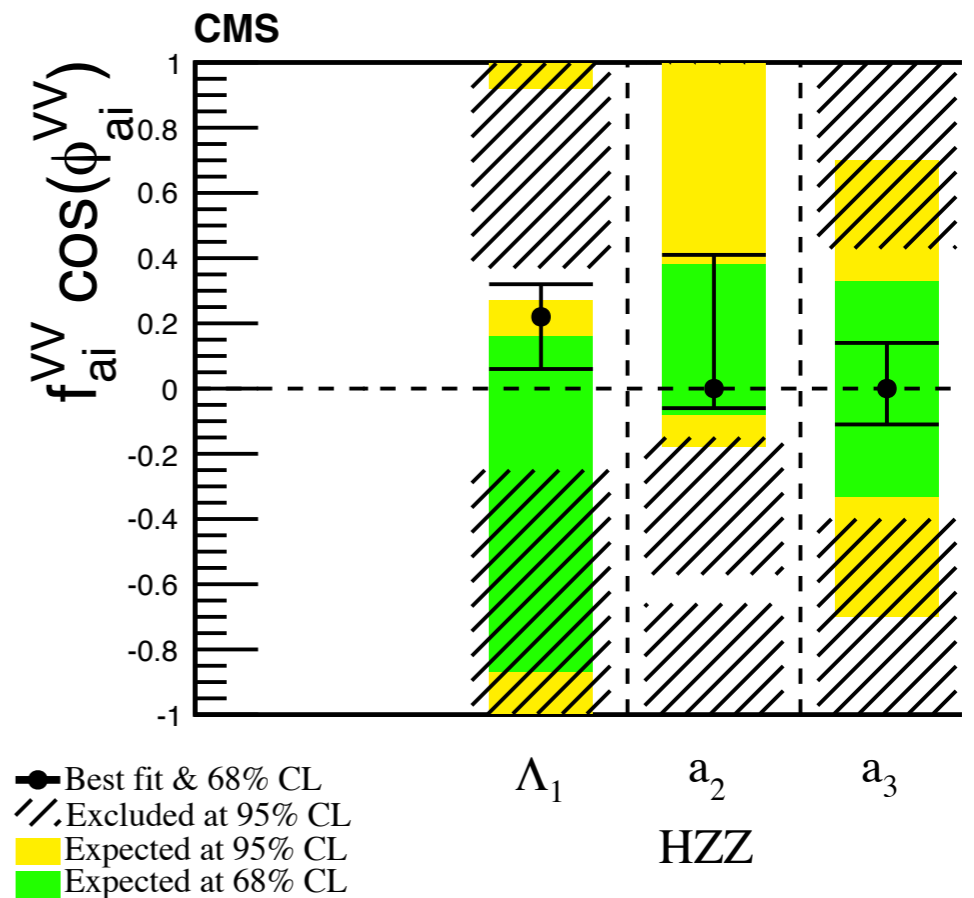
$$\tilde{d} > 0.05$$



[CMS 1411.3441]

$$A(\text{HVV}) \sim \left[a_1^{\text{VV}} + \frac{\kappa_1^{\text{VV}} q_{V1}^2 + \kappa_2^{\text{VV}} q_{V2}^2}{(\Lambda_1^{\text{VV}})^2} \right] m_{V1}^2 \epsilon_{V1}^* \epsilon_{V2}^* + a_2^{\text{VV}} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + a_3^{\text{VV}} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

Measurement in H → 4l



So, why do we look for CP-violation in the Higgs sector?

one reason: Matter-antimatter asymmetry

Baryon-to-photon ratio $Y_B = \frac{n_B}{s} = (8.59 \pm 0.11) \times 10^{-11}$ [Planck Data]

asymmetry parameter $\frac{\eta_B - \eta_{\bar{B}}}{\gamma} \simeq 10^{-9}$

Pre-inflation asymmetry would have been washed out

Sakharov conditions:

(for dynamical generation of Baryon asymmetry)

- B violation
- CP violation
- Departure from thermal equilibrium



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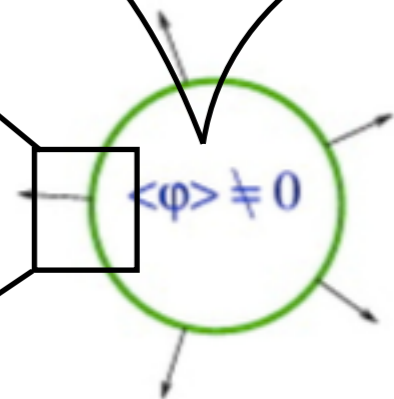
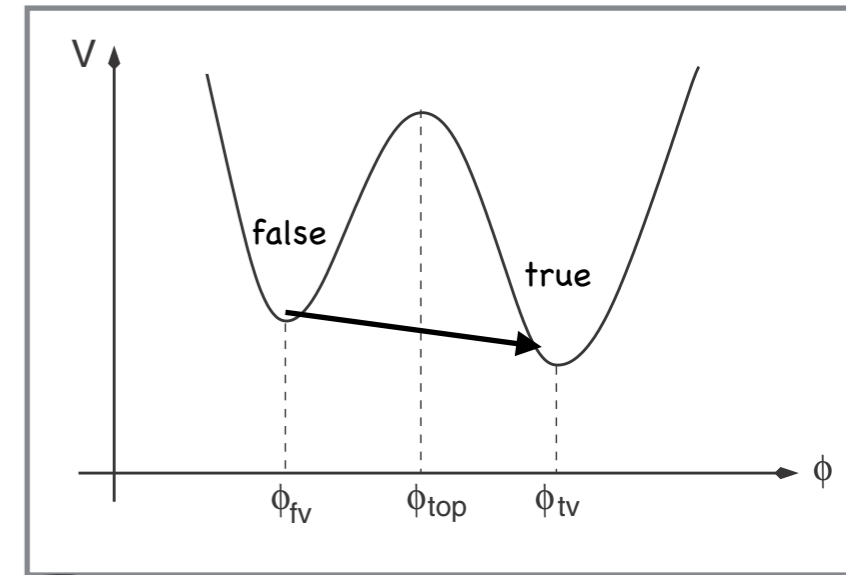
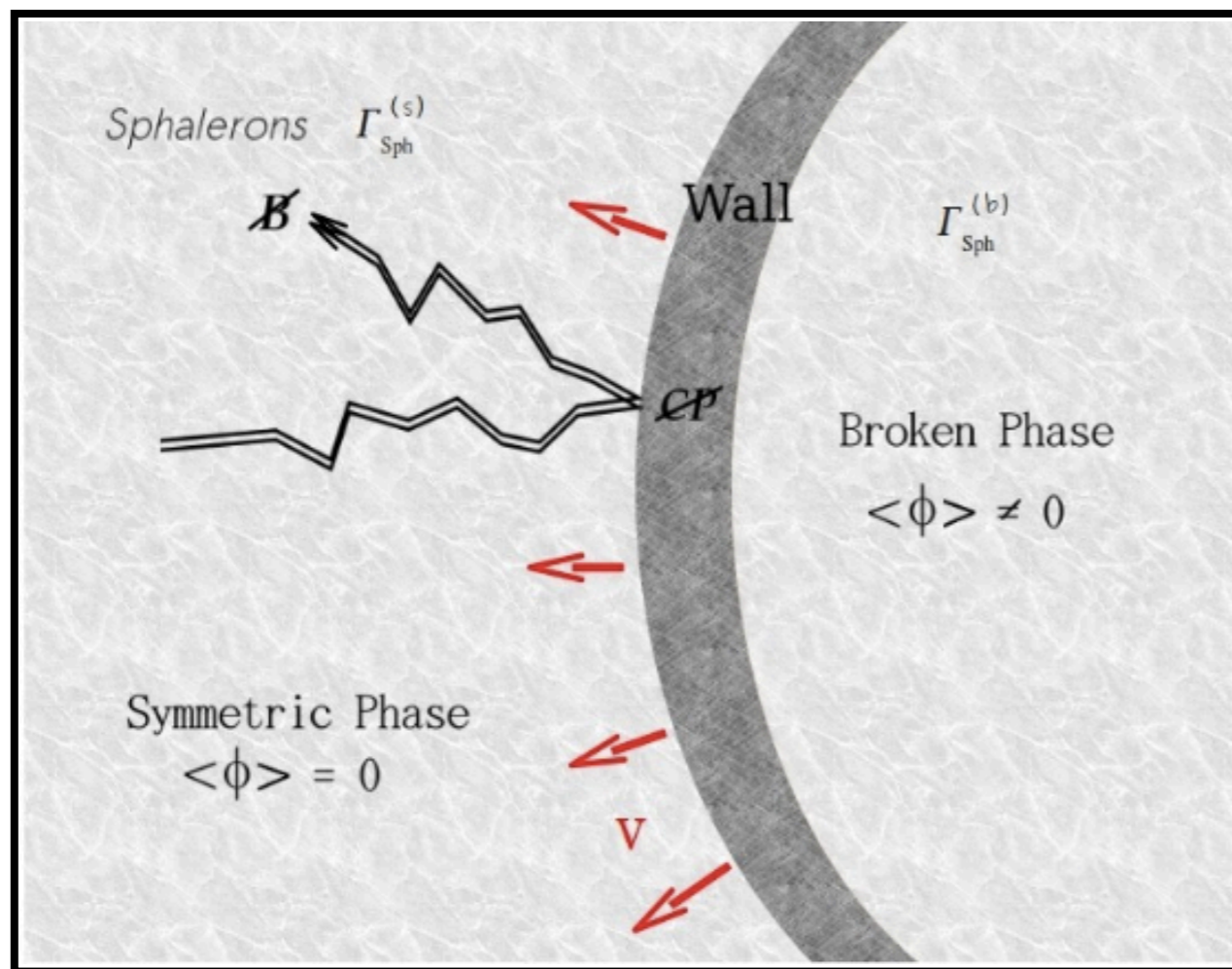
- B violation ✓ **Sphaleron**
- CP violation ⚡ **not enough**
- Departure from thermal equilibrium ⚡ **not enough**



Electroweak Baryogenesis

- Spontaneous symmetry breaking after temperature cooled down during expansion of early Universe

→ violent process, formation of bubbles



Electroweak Baryogenesis

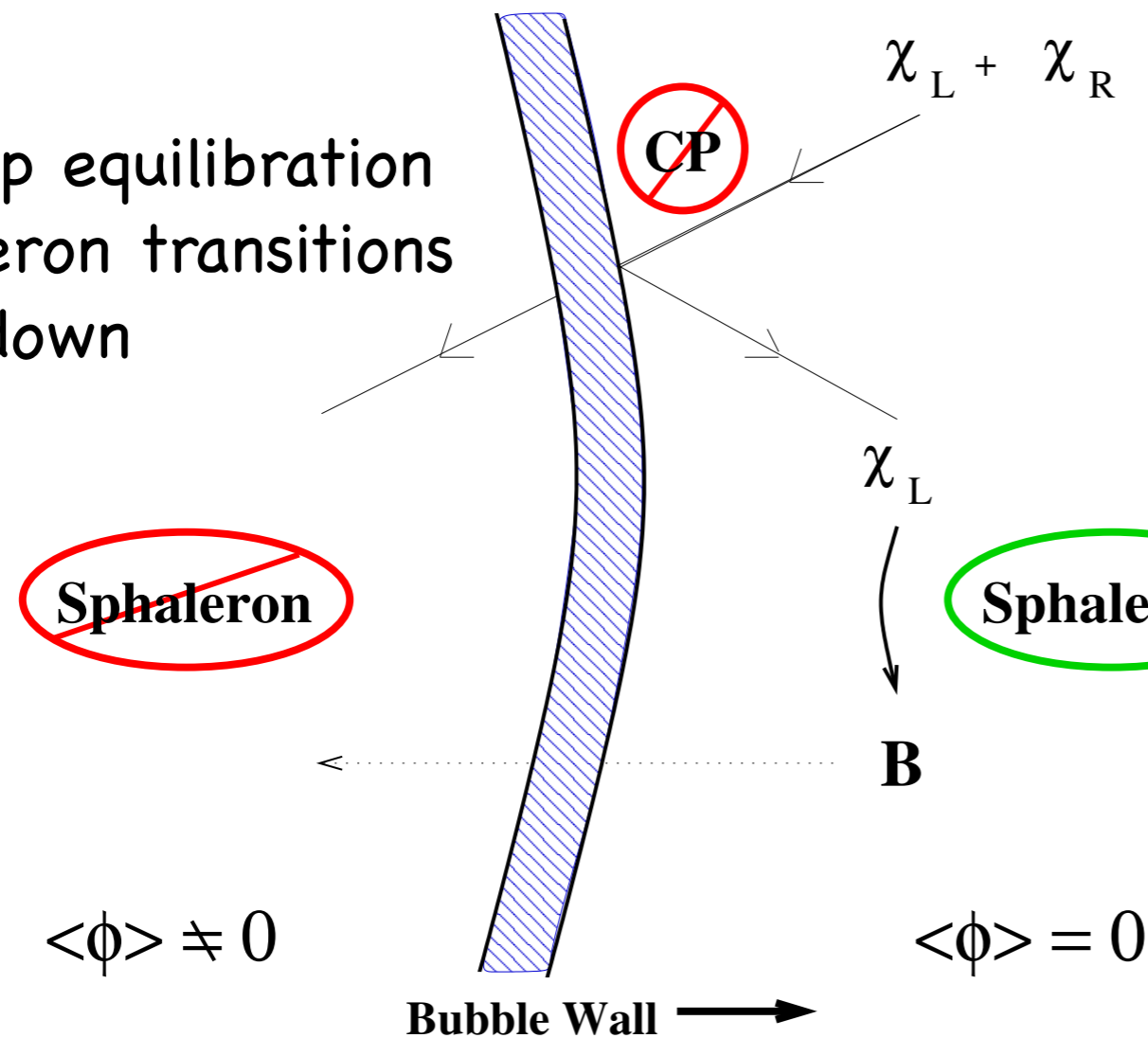
[Kuzmin, Rubakov, Shaposhnikov '85]

[Cohen, Kaplan, Nelson '91]

1. Nucleation and expansion of bubbles of broken phase

2. CP violation at phase interface responsible for mechanism of charge separation

4. To stop equilibration sphaleron transitions shut down



→ chiral flux in front of wall

3. In symmetric phase, very active sphalerons convert chiral asymmetry into baryon asymmetry

[Morrissey, Ramsey-Musolf '12]

CP violation during Electroweak Baryogenesis

$$Y_B = \frac{n_b}{s} = -\frac{3\Gamma_{ws}}{2v_w s} \int_{-\infty}^0 n_L(z) e^{z\mathcal{R}\Gamma_{ws}/v_w} dz$$

entropy density $s = 2\pi^2/(45)g_*S T^3$ sphaleron rate $\Gamma_{ws} = 6\kappa\alpha_w^5 T$

$$Y_B \sim \frac{\Gamma_{ws} \delta_{CP}}{g_* L_w T^2} \sim \frac{10^{-6} \delta_{CP}}{g_*} \sim 10^{-8} \delta_{CP}$$

→ CPV needs to be order 1

Amount of CP violation in quark sector not sufficient. Thus need new sources of CP violation.

[Gavela, Hernandez, Orloff, Pene, Quimbay '94]

Simple gauge-invariant operator upon elw. sym. breaking

$$\mathcal{L}_{\text{eff}} \supset -\left(\alpha + \beta \frac{H^\dagger H}{\Lambda^2}\right) H \ell_{3L}^\dagger \tau_R + \text{c.c.}$$

with α and β complex parameters. After elw sym breaking

$$\mathcal{L}_{\text{eff}} \supset -\left(\alpha + \beta \frac{v^2}{\Lambda^2}\right) v \tau_L^\dagger \tau_R - \left(\alpha + 3\beta \frac{v^2}{\Lambda^2}\right) \frac{h}{\sqrt{2}} \tau_L^\dagger \tau_R + \text{c.c.}$$



$$\alpha + \beta \frac{v^2}{\Lambda^2} = y_\tau^{\text{SM}} > 0$$

$$\mathcal{L} = m_f \bar{f}_L f_R + \frac{y_f}{\sqrt{2}} e^{i\Delta} h \bar{f}_L f_R + \text{h.c.}$$



$$\mathcal{L} = m_f \bar{f} f + \frac{y_f}{\sqrt{2}} \cos\Delta h \bar{f} f + i \frac{y_f}{\sqrt{2}} \sin\Delta h \bar{f} \gamma_5 f$$

New sources of CP-violation can be accommodated in several ways

(not exhaustive)

- Yukawa-Higgs coupling

CP-violating Yukawa-type interactions

$$|c_f| \frac{m_f}{v} \bar{f} (\cos \phi_f + i\gamma_5 \sin \phi_f) f h_{\text{phys}}$$



- gauge-Higgs coupling

CP-violating terms between scalar and gauge boson

$$\frac{e^2}{2} \tilde{c}_{\gamma\gamma} h^2 \tilde{F}_{\mu\nu} F^{\mu\nu}$$

- Scalar-Higgs coupling

CP-violating terms in the scalar potential

$$V_H \sim - \left(m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right) + \left[\frac{1}{2} \lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \lambda_6 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_1^\dagger \Phi_2 \right) + \lambda_7 \left(\Phi_2^\dagger \Phi_2 \right) \left(\Phi_1^\dagger \Phi_2 \right) + \text{H.c.} \right]$$

Relation between matter-antimatter asymmetry and CPV in a concrete model, i.e. 2HDM

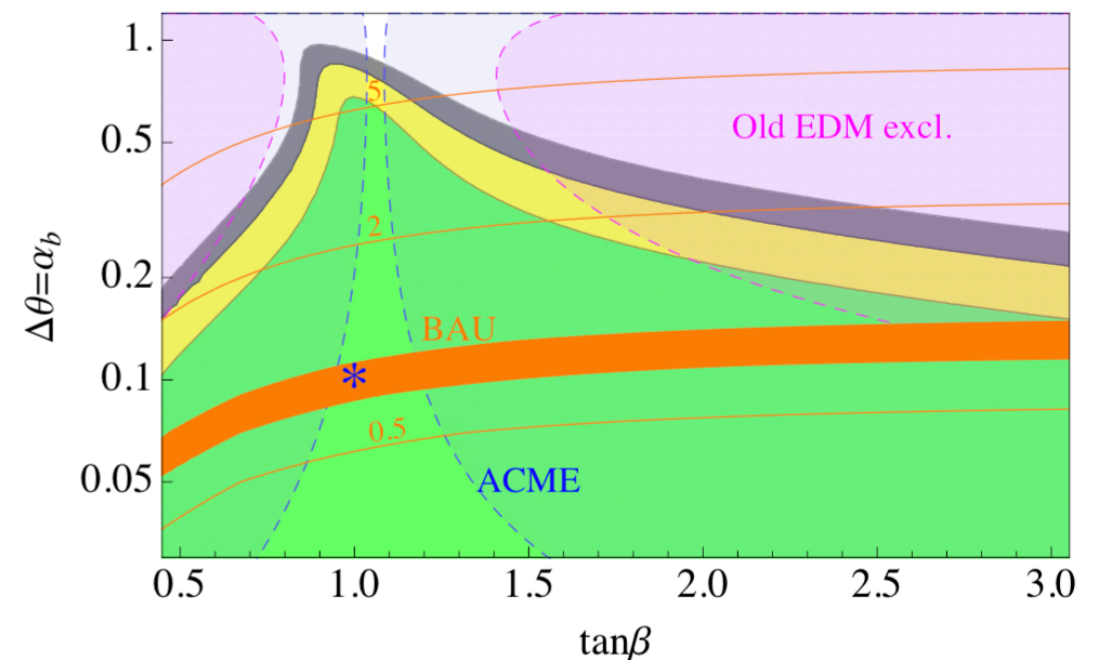
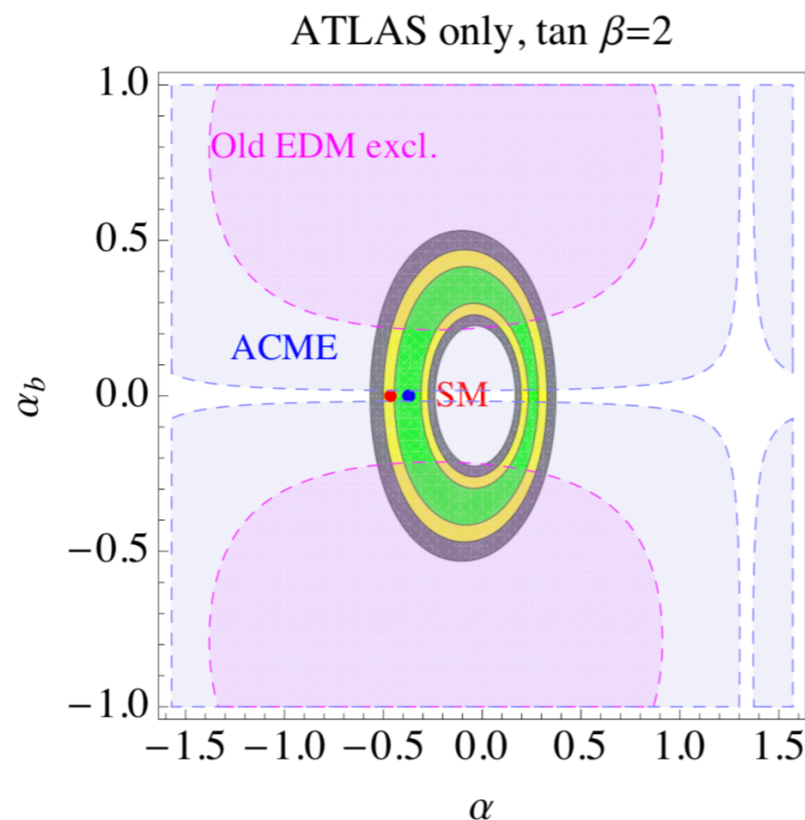
$$V = \frac{\lambda_1}{2}(\phi_1^\dagger\phi_1)^2 + \frac{\lambda_2}{2}(\phi_2^\dagger\phi_2)^2 + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) \quad [\text{Shu and Zhang '13}]$$

$$+ \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) + \frac{1}{2} \left[\lambda_5(\phi_1^\dagger\phi_2)^2 + \text{h.c.} \right]$$

$$- \frac{1}{2} \left\{ m_{11}^2(\phi_1^\dagger\phi_1) + \left[m_{12}^2(\phi_1^\dagger\phi_2) + \text{h.c.} \right] + m_{22}^2(\phi_2^\dagger\phi_2) \right\},$$

assumed all real but m_{12}^2

$$h_1 = -\sin\alpha \cos\alpha_b H_1^0 + \cos\alpha \cos\alpha_b H_2^0 + \sin\alpha_b A^0.$$

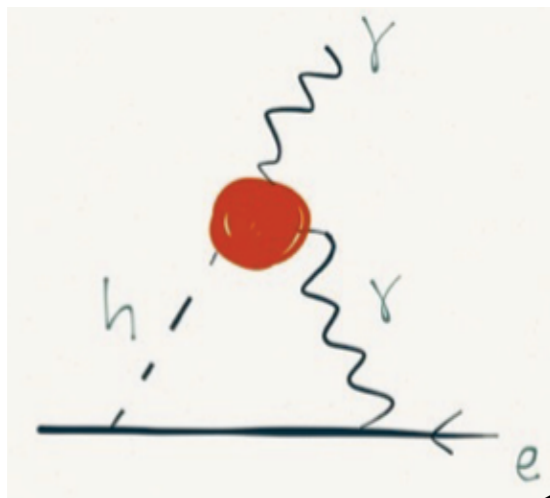


Higgs CP properties

eff. operators mediating CP-odd Higgs interactions:

indirect constraints

EDM



$$\tilde{c}_{\gamma\gamma}^{-1/2} \geq 24 \text{ TeV}$$

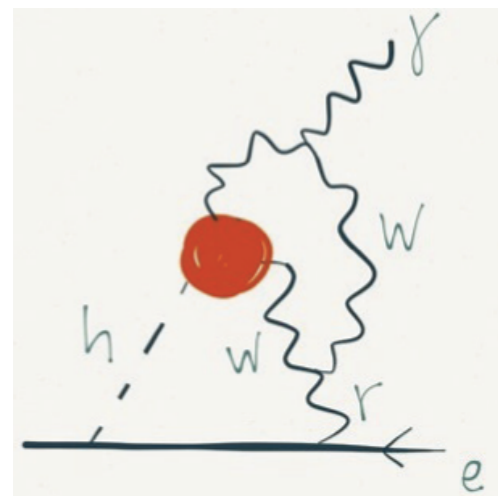
$$\frac{e^2}{2} \tilde{c}_{\gamma\gamma} h^2 \tilde{F}_{\mu\nu} F^{\mu\nu}$$

photons

$$\frac{g_2^2}{2} \tilde{c}_{WW} h^2 \tilde{W}_{\mu\nu}^+ W^{\mu\nu-}$$

massive gauge bosons

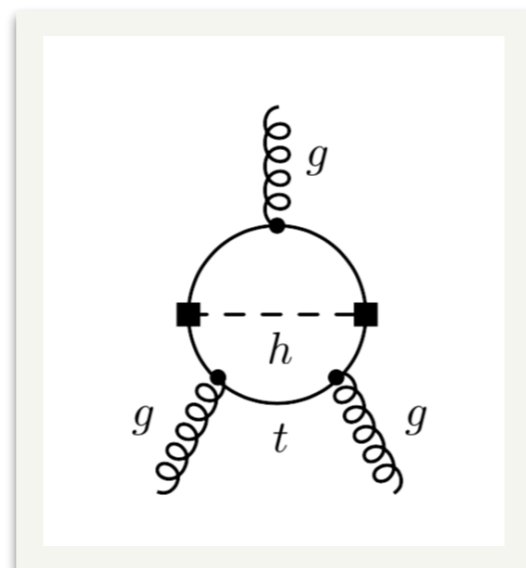
$$\frac{g_Z^2}{2} \tilde{c}_{ZZ} h^2 \tilde{Z}_{\mu\nu} Z^{\mu\nu}$$



$$\tilde{c}_{WW}^{-1/2} \geq 600 \text{ GeV}$$

$$\frac{g_s^2}{2} \tilde{c}_{gg} h^2 \tilde{G}_{\mu\nu} G^{\mu\nu}$$

gluons



$$\rightarrow |c_f| \frac{m_f}{v} \bar{f} (\cos \phi_f + i \gamma_5 \sin \phi_f) f h_{\text{phys}}$$

fermions

[McKeen, Pospelov, Ritz '12]

[Delaunay et al '14]

[Brod, Haisch, Zupan '13]

Higgs CP properties

eff. operators mediating CP-odd Higgs interactions:

@ colliders:

Look at interference effects
between
 $h \rightarrow ZZ^* \rightarrow 4l$ and $h \rightarrow \gamma^* \gamma^* \rightarrow 4l$

[Chen, Harnik, Vega Morales '14]

[Bolognesi et al '12]

$$\frac{e^2}{2} \tilde{c}_{\gamma\gamma} h^2 \tilde{F}_{\mu\nu} F^{\mu\nu}$$

photons

$$\frac{g_2^2}{2} \tilde{c}_{WW} h^2 \tilde{W}_{\mu\nu}^+ W^{\mu\nu-}$$

massive gauge
bosons

$$\frac{g_Z^2}{2} \tilde{c}_{ZZ} h^2 \tilde{Z}_{\mu\nu} Z^{\mu\nu}$$

tau phase in angular distributions of
 $\tau^\pm \rightarrow \rho^\pm (\pi^\pm \pi^0) \nu$

[Harnik, Martin, Okui, Primulando, Yu '13]

$$\frac{g_s^2}{2} \tilde{c}_{gg} h^2 \tilde{G}_{\mu\nu} G^{\mu\nu}$$

gluons

Angular correlations in $t\bar{t}h$
production

[Buckley, Goncalves '15]

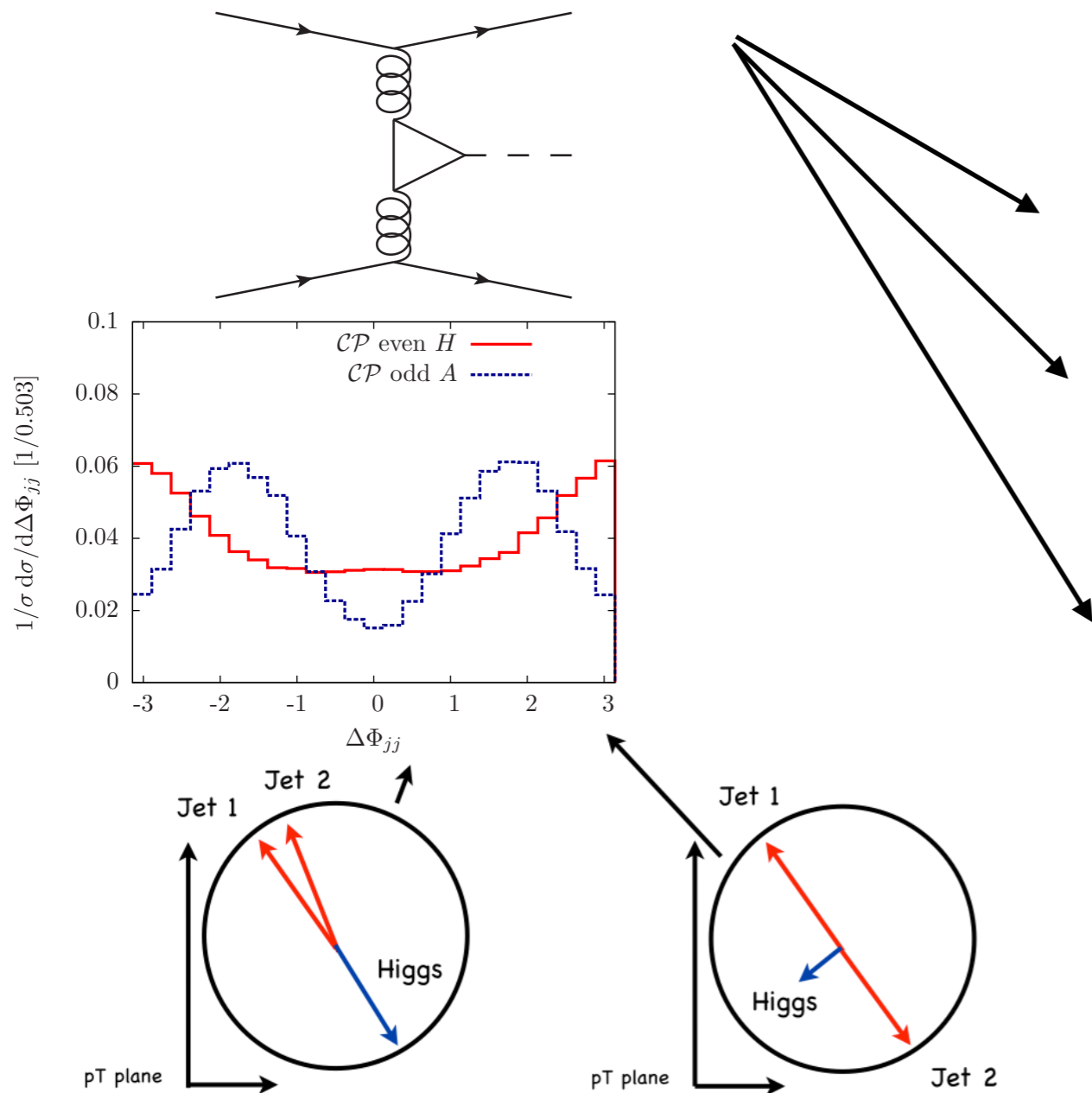
$$|c_f| \frac{m_f}{v} \bar{f} (\cos \phi_f + i\gamma_5 \sin \phi_f) f h_{\text{phys}}$$

fermions

Higgs CP properties

eff. operators mediating CP-odd Higgs interactions:

Weak-boson and gluon fusion



$$\frac{e^2}{2} \tilde{c}_{\gamma\gamma} h^2 \tilde{F}_{\mu\nu} F^{\mu\nu}$$

photons

$$\frac{g_2^2}{2} \tilde{c}_{WW} h^2 \tilde{W}_{\mu\nu}^+ W^{\mu\nu-}$$

massive
gauge bosons

$$\frac{g_Z^2}{2} \tilde{c}_{ZZ} h^2 \tilde{Z}_{\mu\nu} Z^{\mu\nu}$$

$$\frac{g_s^2}{2} \tilde{c}_{gg} h^2 \tilde{G}_{\mu\nu} G^{\mu\nu}$$

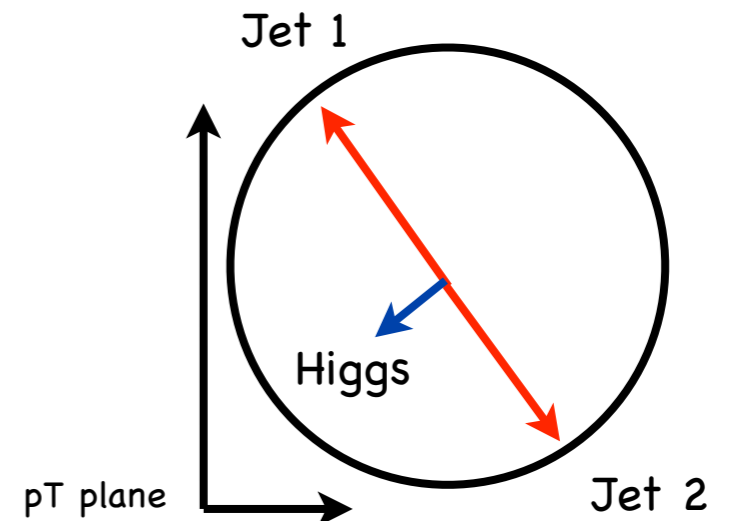
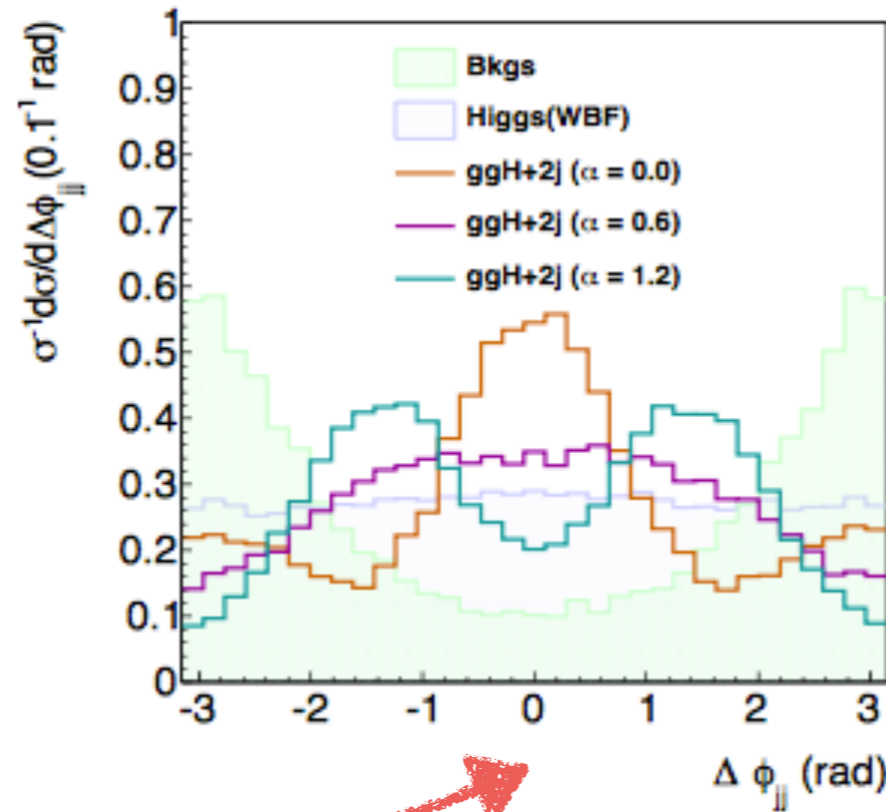
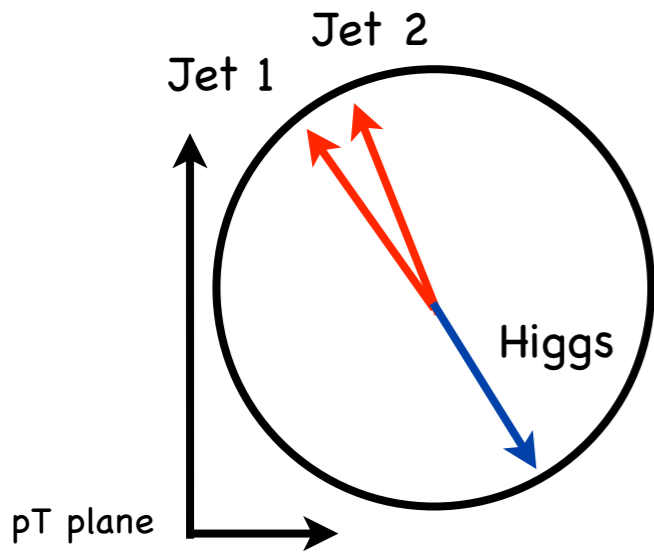
gluons

$$|c_f| \frac{m_f}{v} \bar{f} (\cos \phi_f + i\gamma_5 \sin \phi_f) f h_{\text{phys}} \quad \text{fermions}$$

[Plehn, Rainwater, Zeppenfeld '01][Klamke, Zeppenfeld '07]

Mixed physical state:

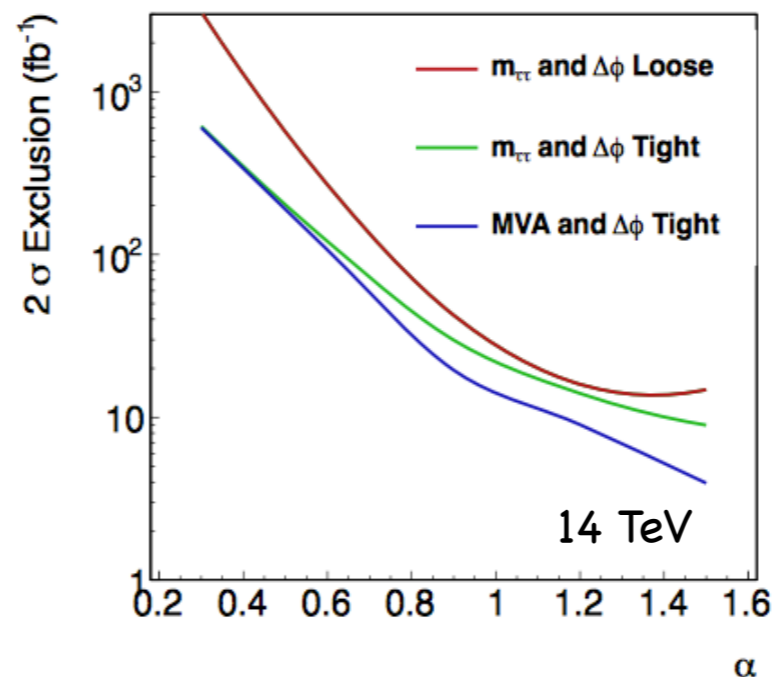
$$\mathcal{L}_{hgg} = \cos \alpha \frac{\alpha_S}{12\pi v} h G_{\mu\nu}^a G^{a,\mu\nu} + \sin \alpha \frac{\alpha_S}{4\pi v} h G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$



Can constrain/exclude mixed CP-states

to

$\alpha < 0.3$ with 500 fb^{-1}



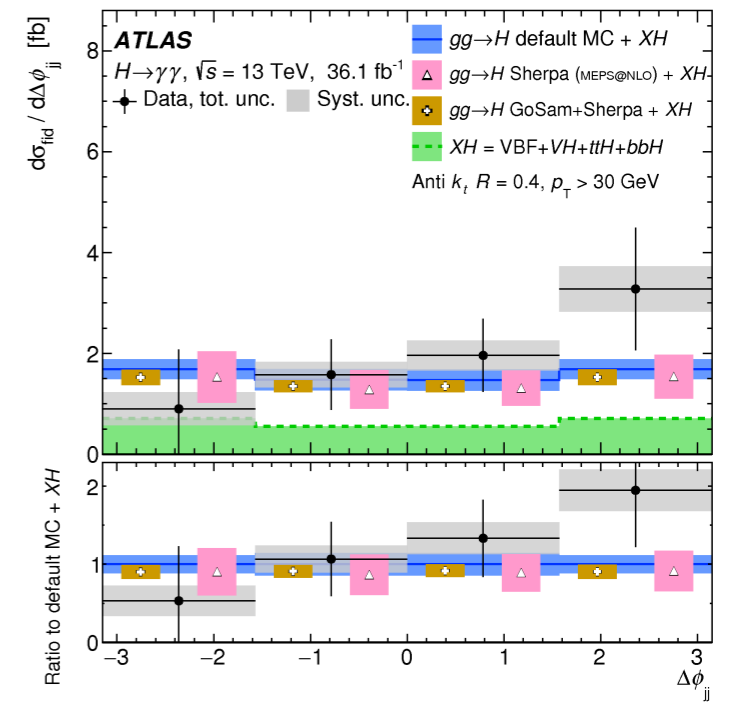
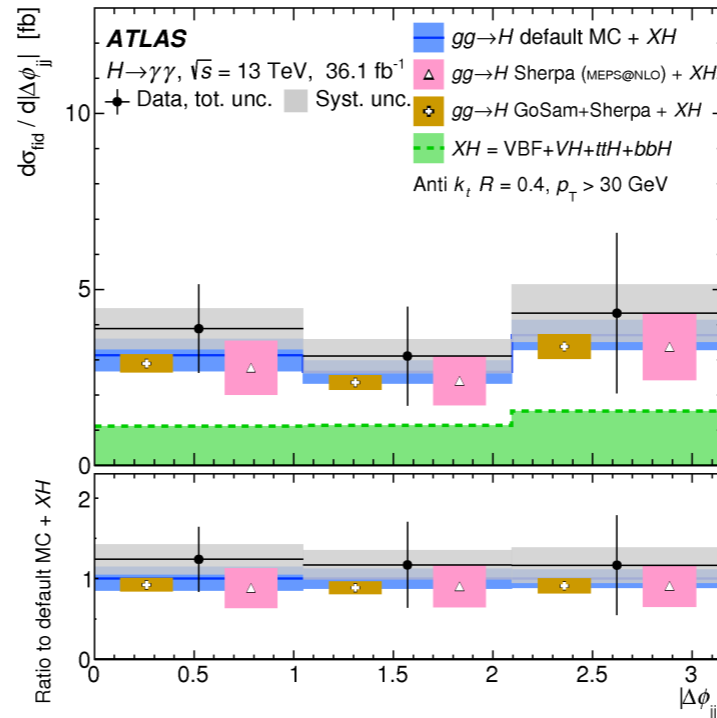
[Dolan, Harris, Jankowiak, MS '14]

CP violating interactions of the Higgs boson

[Bernlochner et al '18]

$$\begin{aligned}
 O_{H\tilde{G}} &= H^\dagger H G^{a\mu\nu} \tilde{G}_{\mu\nu}^a, \\
 O_{H\tilde{W}} &= H^\dagger H W^{a\mu\nu} \tilde{W}_{\mu\nu}^a, \\
 O_{H\tilde{B}} &= H^\dagger H B^{\mu\nu} \tilde{B}_{\mu\nu}, \\
 O_{H\tilde{W}B} &= H^\dagger \tau^a H B_{\mu\nu} \tilde{W}^{a\mu\nu},
 \end{aligned}$$

cp-violating tth interactions degenerate with $O_{H\tilde{G}}$ for our observables (blind direction)



Use recent ATLAS measurements in $h \rightarrow \gamma\gamma$ and $h \rightarrow ZZ^* \rightarrow 4\ell$

Need to construct CP sensitive observables in linearised framework $|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\text{Re}(\mathcal{M}_{\text{SM}}^* \mathcal{M}_{\text{d6}}) + \mathcal{O}(\Lambda^{-4})$.

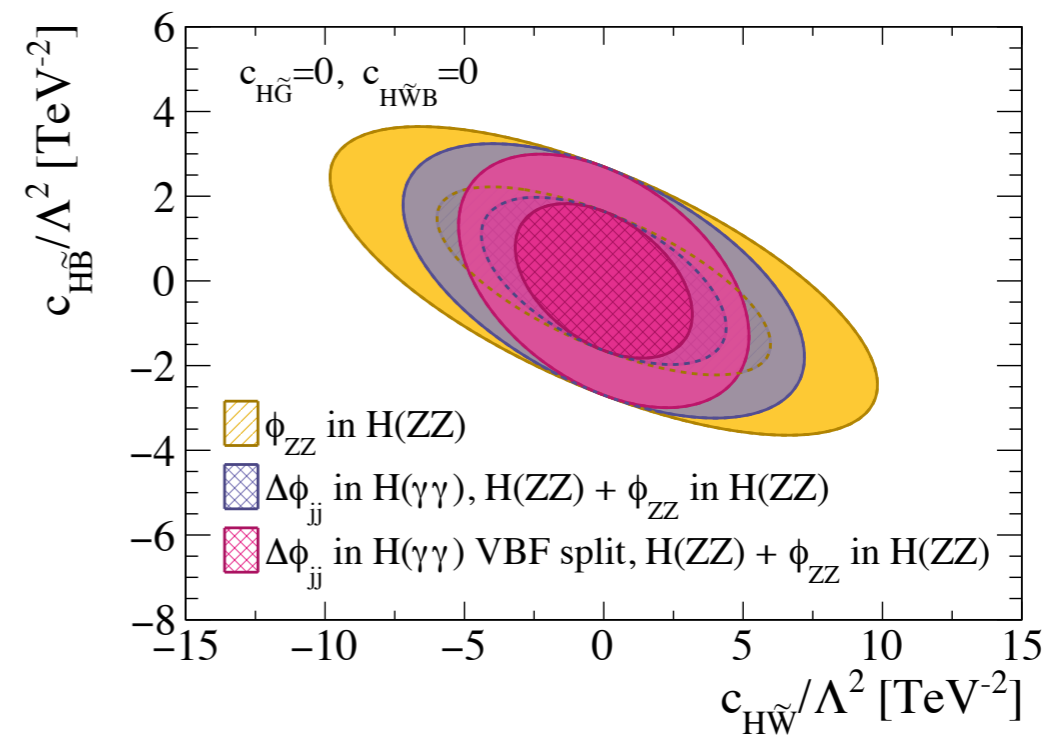
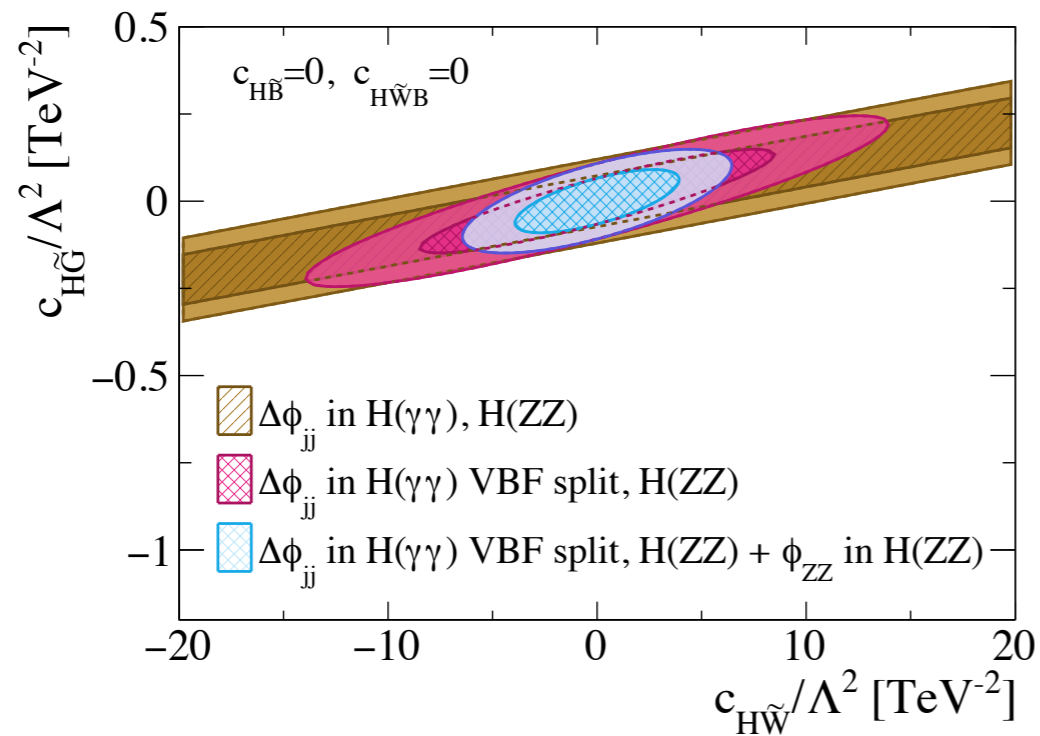
for example: $\Delta\phi_{jj} = \phi_1 - \phi_2$, in Hjj \rightarrow $A = \frac{\sigma(0 < \Delta\phi_{jj} < \pi) - \sigma(-\pi < \Delta\phi_{jj} < 0)}{\sigma(0 < \Delta\phi_{jj} < \pi) + \sigma(-\pi < \Delta\phi_{jj} < 0)}$

with ATLAS data one finds

$A = 0.3 \pm 0.2$

Future sensitivity can be improved by separating enriched regions of GF and WBF and by studying H→4l decay angles, e.g.

$$\cos \Phi = \frac{(\mathbf{p}_{l-} \times \mathbf{p}_{l+}) \cdot (\mathbf{p}_{l'-} \times \mathbf{p}_{l'+})}{\sqrt{(\mathbf{p}_{l-} \times \mathbf{p}_{l+})^2 (\mathbf{p}_{l'-} \times \mathbf{p}_{l'+})^2}} \Big|_h$$



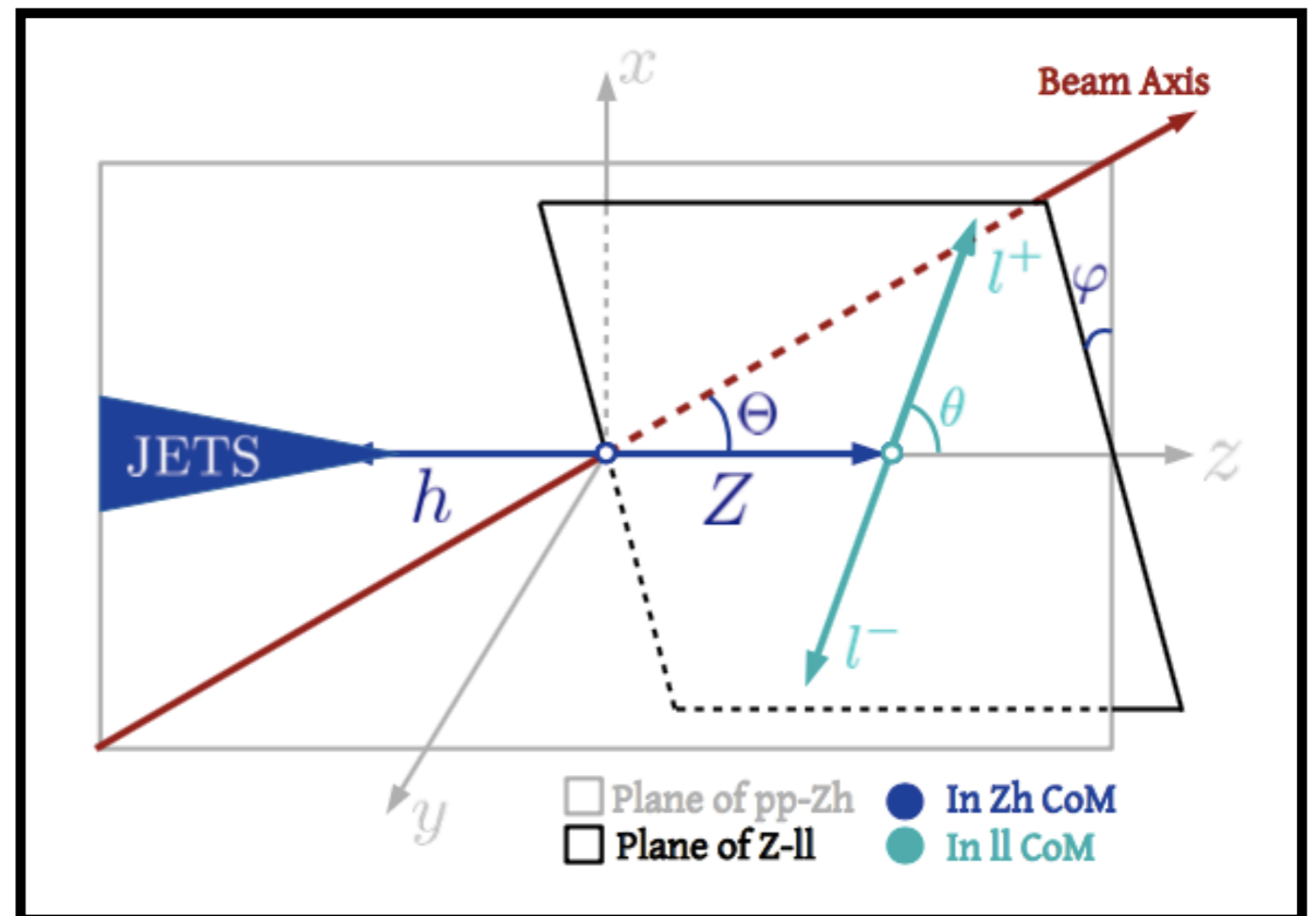
Coefficient [TeV ⁻²]	36.1 fb ⁻¹	300 fb ⁻¹	3000 fb ⁻¹
$c_{H\tilde{G}}/\Lambda^2$	[-0.19, 0.19]	[-0.067, 0.067]	[-0.021, 0.021]
$c_{H\tilde{W}}/\Lambda^2$	[-11, 11]	[-3.8, 3.8]	[-1.2, 1.2]
$c_{H\tilde{B}}/\Lambda^2$	[-5.9, 5.9]	[-2.1, 2.1]	[-0.65, 0.65]
$c_{H\tilde{W}B}/\Lambda^2$	[-14, 14]	[-4.9, 4.9]	[-1.5, 1.5]

Marginalised over other coefficients

CPV in HZZ - a case study

- $H \rightarrow ZZ \rightarrow 4l$ standard candle to search for CPV in Higgs sector
- New physics unlikely to induce only one new operator
- Easier to disentangle EFT operators in the production, rather than decay
- Three body phase space so $3 \times 3 - 4 = 5$ kinematical variables completely define the final state
- Ignoring the boost there are 4:

$$\sqrt{s}, \Theta, \theta, \varphi$$



How much information does process provide differentially?

Free kinematic parameters

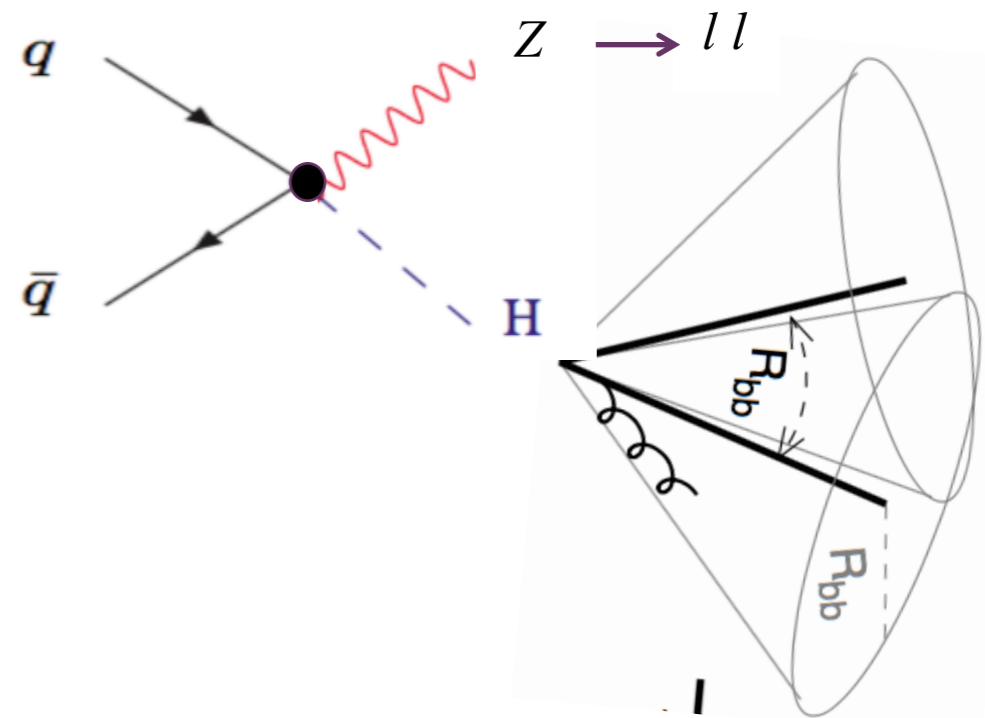
$$\sqrt{s}, \Theta, \theta, \varphi$$

If we separate each variable into 10 bins:
1000 numbers per energy bin to encapsulate full information



With some analysis, we can reduce that number to 9 per energy bin

HZ boosted, reconstructed with fat jet



Reconstruction: BDRS, ...

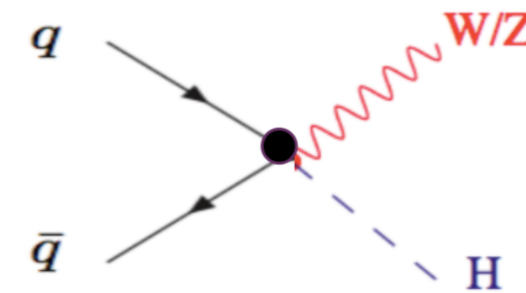
[Butterworth, Davidson, Rubin, Salam '08]

[Banerjee, Englert, Gupta, MS '18]

The $ff \rightarrow HZ$ interactions are defined by

$$\Delta\mathcal{L}_6^{hZ\bar{f}f} \supset \delta\hat{g}_{ZZ}^h \frac{2m_Z^2}{v} h \frac{Z^\mu Z_\mu}{2} + \sum_f g_{Zf}^h \frac{h}{v} Z_\mu \bar{f} \gamma^\mu f$$

$$+ \kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z_{\mu\nu} + \tilde{\kappa}_{ZZ} \frac{h}{2v} Z^{\mu\nu} \tilde{Z}_{\mu\nu}.$$



Process in terms of helicity amplitudes:

$$\mathcal{M}_\sigma^{\lambda=\pm} = \sigma \frac{1 + \sigma \lambda \cos \Theta}{\sqrt{2}} \frac{g g_f^Z}{c_{\theta_W}} \frac{m_Z}{\sqrt{\hat{s}}} \left[1 + \left(\frac{g_{Zf}^h}{g_f^Z} + \kappa_{ZZ} - i\lambda \tilde{\kappa}_{ZZ} \right) \frac{\hat{s}}{2m_Z^2} \right]$$

$$\mathcal{M}_\sigma^{\lambda=0} = -\sin \Theta \frac{g g_f^Z}{2c_{\theta_W}} \left[1 + \delta\hat{g}_{ZZ}^h + 2\kappa_{ZZ} + \frac{g_{Zf}^h}{g_f^Z} \left(-\frac{1}{2} + \frac{\hat{s}}{2m_Z^2} \right) \right],$$

Only a finite number of helicity amplitudes receive corrections up to Dim-6 order

$$\mathcal{A}_h(\hat{s}, \Theta, \hat{\theta}, \hat{\varphi}) = \frac{-i\sqrt{2}g_\ell^Z}{\Gamma_Z} \sum_\lambda \mathcal{M}_\sigma^\lambda(\hat{s}, \Theta) d_{\lambda,1}^{J=1}(\hat{\theta}) e^{i\lambda\hat{\varphi}} \rightarrow \sum_{L,R} |\mathcal{A}(\hat{s}, \Theta, \theta, \varphi)|^2 = 3 \times 3 = 9$$

Finally, 9 terms including 6 interference terms between different Z helicities

$$\begin{aligned}
\sum_{L,R} |\mathcal{A}(\hat{s}, \Theta, \theta, \phi)|^2 &= a_{LL} \sin^2 \Theta \sin^2 \theta + a_{TT}^1 \cos \Theta \cos \theta \\
&+ a_{TT}^2 (1 + \cos^2 \Theta)(1 + \cos^2 \theta) + \cos \varphi \sin \Theta \sin \theta \\
&\times (a_{LT}^1 + a_{LT}^2 \cos \theta \cos \Theta) + \sin \varphi \sin \Theta \sin \theta \\
&\times (\tilde{a}_{LT}^1 + \tilde{a}_{LT}^2 \cos \theta \cos \Theta) + a_{TT'} \cos 2\varphi \sin^2 \Theta \sin^2 \theta \\
&+ \tilde{a}_{TT'} \sin 2\varphi \sin^2 \Theta \sin^2 \theta.
\end{aligned}$$

- 9 coefficient are 9 angular moments for $pp > H(Z>ll)$
- They contain all kinematic information of the process

To extract use analog to Fourier analysis

$$P(\Omega) = \sum_i a_i \times g_i(\Omega)$$

Find reciprocal vector (weight function)

$$\boxed{w_i(\Omega) = \sum_j \lambda_{ij} g_j(\Omega)} \quad \longrightarrow \quad \boxed{\int d\Omega g_i(\Omega) w_j(\Omega) = \delta_{ij}}$$

Calculate

$$a_i = \int d\Omega P(\Omega) w_i(\Omega)$$

Dunietz, Quinn, Snyder, Toki & Lipkin (1991)

$$\sum_{L,R} |\mathcal{A}(\hat{s}, \Theta, \theta, \phi)|^2 = a_{LL} \sin^2 \Theta \sin^2 \theta + a_{TT}^1 \cos \Theta \cos \theta$$

$$+ a_{TT}^2 (1 + \cos^2 \Theta)(1 + \cos^2 \theta) + \cos \varphi \sin \Theta \sin \theta$$

$$\times (a_{LT}^1 + a_{LT}^2 \cos \theta \cos \Theta) + \sin \varphi \sin \Theta \sin \theta$$

$$\times (\tilde{a}_{LT}^1 + \tilde{a}_{LT}^2 \cos \theta \cos \Theta) + \tilde{a}_{TT'} \sin 2\varphi$$

- 9 coefficient
- They contain

To extract use an
Find reciprocal ve

$$w_i(\Omega) = \sum_i \lambda_i$$

$$g^1 = S_\Theta^2 S_\theta^2$$

$$g^2 = C_\Theta C_\theta$$

$$g^3 = (1 + C_\Theta^2)(1 + C_\theta^2)$$

$$g^4 = C_\varphi S_\Theta S_\theta$$

$$g^5 = C_\varphi S_\Theta S_\theta C_\Theta C_\theta$$

$$g^6 = S_\varphi S_\Theta S_\theta$$

$$g^7 = S_\varphi S_\Theta S_\theta C_\Theta C_\theta$$

$$g^8 = C_{2\varphi} S_\Theta^2 S_\theta^2$$

$$g^9 = S_{2\varphi} S_\Theta^2 S_\theta^2$$

$$\Theta \sin^2 \theta$$

pp > H(Z>ll)
of the process

$$P(\Omega) = \sum_i a_i \times g_i(\Omega)$$

$$w_i(\Omega) w_j(\Omega) = \delta_{ij}$$

Calculate

Junietz, Quinn, Snyder, Toki & Lipkin (1991)

Comparison of amplitude coefficients and their respective moments

a_{LL}	$\frac{\mathcal{G}^2}{4} \left[1 + 2\delta\hat{g}_{ZZ}^h + 4\kappa_{ZZ} + \frac{g_{Zf}^h}{g_f^h} (-1 + 4\gamma^2) \right]$
a_{TT}^1	$\frac{\mathcal{G}^2\sigma\epsilon_{LR}}{2\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{TT}^2	$\frac{\mathcal{G}^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^1	$-\frac{\mathcal{G}^2\sigma\epsilon_{LR}}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^2	$-\frac{\mathcal{G}^2}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
\tilde{a}_{LT}^1	$-\mathcal{G}^2\sigma\epsilon_{LR}\tilde{\kappa}_{ZZ}\gamma$
\tilde{a}_{LT}^2	$-\mathcal{G}^2\tilde{\kappa}_{ZZ}\gamma$
$a_{TT'}$	$\frac{\mathcal{G}^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
$\tilde{a}_{TT'}$	$\frac{\mathcal{G}^2}{2}\tilde{\kappa}_{ZZ}$

g^1	$= S_\Theta^2 S_\theta^2$
g^2	$= C_\Theta C_\theta$
g^3	$= (1 + C_\Theta^2)(1 + C_\theta^2)$
g^4	$= C_\varphi S_\Theta S_\theta$
g^5	$= C_\varphi S_\Theta S_\theta C_\Theta C_\theta$
g^6	$= S_\varphi S_\Theta S_\theta$
g^7	$= S_\varphi S_\Theta S_\theta C_\Theta C_\theta$
g^8	$= C_{2\varphi} S_\Theta^2 S_\theta^2$
g^9	$= S_{2\varphi} S_\Theta^2 S_\theta^2$

$\gamma = \sqrt{\hat{s}}/(2m_Z)$ and $\epsilon_{LR} = \alpha_L - \alpha_R$
↑ growth with energy ↑ small, accidental cancellation

Comparison of amplitude coefficients and their respective moments

Only sensitive to these if Z decay inclusively treated

Epsilon suppressed

a_{LL}	$\frac{g^2}{4} \left[1 + 2\delta\hat{g}_{ZZ}^h + 4\kappa_{ZZ} + \frac{g_{Zf}^h}{g_f^h} (-1 + 4\gamma^2) \right]$
a_{TT}^1	$\frac{g^2\sigma_{\epsilon LR}}{2\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{TT}^2	$\frac{g^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^1	$-\frac{g^2\sigma_{\epsilon LR}}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^2	$-\frac{g^2}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
\tilde{a}_{LT}^1	$-g^2\sigma_{\epsilon LR}\tilde{\kappa}_{ZZ}\gamma$
\tilde{a}_{LT}^2	$-g^2\tilde{\kappa}_{ZZ}\gamma$
$a_{TT'}$	$\frac{g^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^h} + \kappa_{ZZ} \right) \gamma^2 \right]$
$\tilde{a}_{TT'}$	$\frac{g^2}{2}\tilde{\kappa}_{ZZ}$

$$\gamma = \sqrt{\hat{s}}/(2m_Z) \quad \text{and} \quad \epsilon_{LR} = \alpha_L - \alpha_R$$

$g^1 = S_\Theta^2 S_\theta^2$
$g^2 = C_\Theta C_\theta$
$g^3 = (1 + C_\Theta^2)(1 + C_\theta^2)$
$g^4 = C_\varphi S_\Theta S_\theta$
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$g^6 = S_\varphi S_\Theta S_\theta$
$g^7 = S_\varphi S_\Theta S_\theta C_\Theta C_\theta$
$g^8 = C_{2\varphi} S_\Theta^2 S_\theta^2$
$g^9 = S_{2\varphi} S_\Theta^2 S_\theta^2$

Cross-helicity terms. Vanish upon inclusive integration over lepton phase space

Differential analysis a must

Comparison of amplitude coefficients and their respective moments

Only sensitive to these if Z decay inclusively treated

Epsilon suppressed

CP-even moments probe

$$\kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z_{\mu\nu}$$

CP-odd moments probe

$$\tilde{\kappa}_{ZZ} \frac{h}{2v} Z^{\mu\nu} \tilde{Z}_{\mu\nu}$$

a_{LL}	$\frac{g^2}{4} \left[1 + 2\delta\hat{g}_{ZZ}^h + 4\kappa_{ZZ} + \frac{g_{Zf}^h}{g_f^2} (-1 + 4\gamma^2) \right]$
a_{TT}^1	$\frac{g^2 \sigma_{\epsilon LR}}{2\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^2} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{TT}^2	$\frac{g^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^2} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^1	$-\frac{g^2 \sigma_{\epsilon LR}}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^2} + \kappa_{ZZ} \right) \gamma^2 \right]$
a_{LT}^2	$-\frac{g^2}{2\gamma} \left[1 + 2 \left(\frac{2g_{Zf}^h}{g_f^2} + \kappa_{ZZ} \right) \gamma^2 \right]$
\tilde{a}_{LT}^1	$-g^2 \sigma_{\epsilon LR} \tilde{\kappa}_{ZZ} \gamma$
\tilde{a}_{LT}^2	$-g^2 \tilde{\kappa}_{ZZ} \gamma$
$a_{TT'}$	$\frac{g^2}{8\gamma^2} \left[1 + 4 \left(\frac{g_{Zf}^h}{g_f^2} + \kappa_{ZZ} \right) \gamma^2 \right]$
$\tilde{a}_{TT'}$	$\frac{g^2}{2} \tilde{\kappa}_{ZZ}$

$$\gamma = \sqrt{\hat{s}}/(2m_Z) \quad \text{and} \quad \epsilon_{LR} = \alpha_L - \alpha_R$$

$$g^1 = S_\Theta^2 S_\theta^2$$

$$g^2 = C_\Theta C_\theta$$

$$g^3 = (1 + C_\Theta^2)(1 + C_\theta^2)$$

$$g^4 = C_\varphi S_\Theta S_\theta$$

$$g^5 = C_\varphi S_\Theta S_\theta C_\Theta C_\theta$$

$$g^6 = S_\varphi S_\Theta S_\theta$$

$$g^7 = S_\varphi S_\Theta S_\theta C_\Theta C_\theta$$

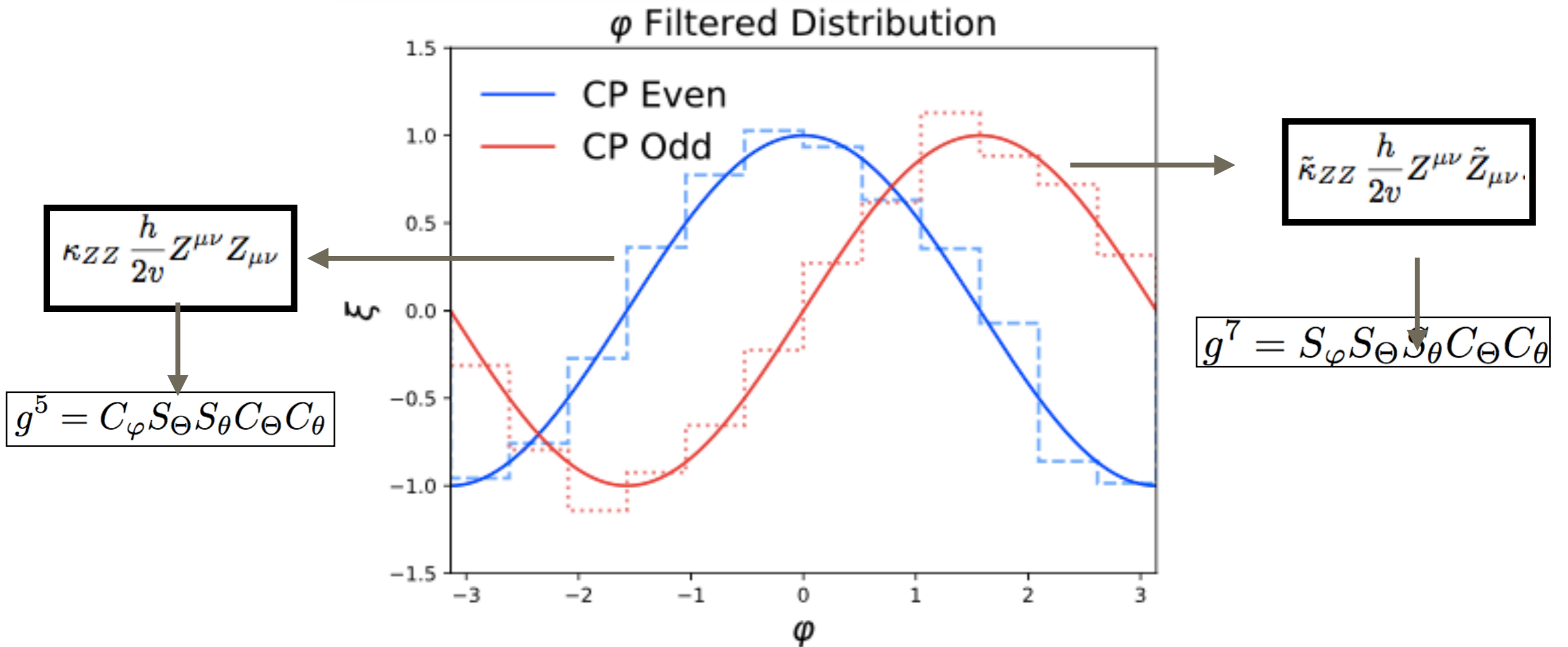
$$g^8 = C_{2\varphi} S_\Theta^2 S_\theta^2$$

$$g^9 = S_{2\varphi} S_\Theta^2 S_\theta^2$$

Cross-helicity terms. Vanish upon inclusive integration over lepton phase space

Differential analysis a must

A Triple Differential observable

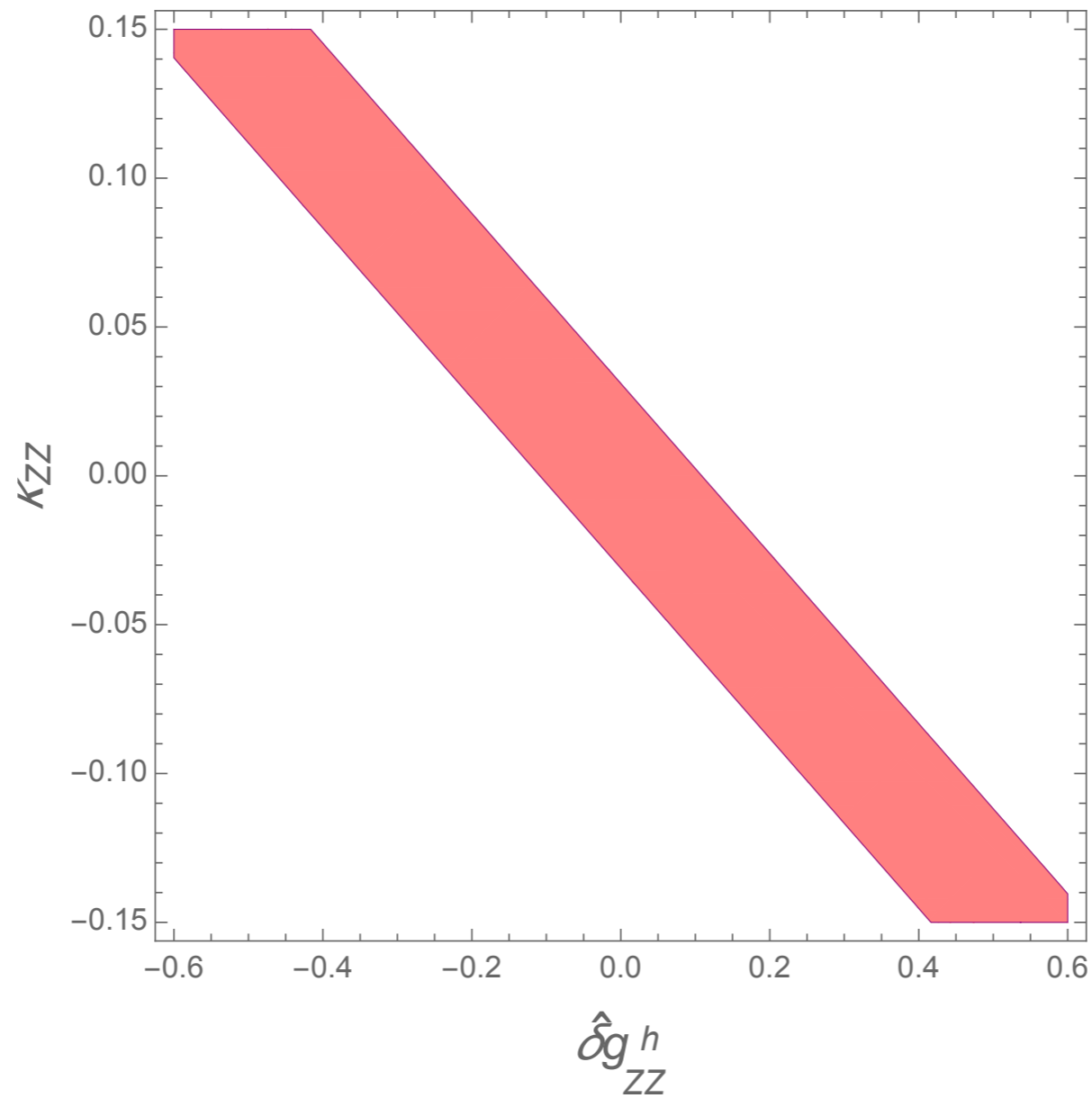


Dominant cross-helicity CP even & odd angular moment

[Banerjee, Gupta, Reines, MS '19]

Sensitivity result

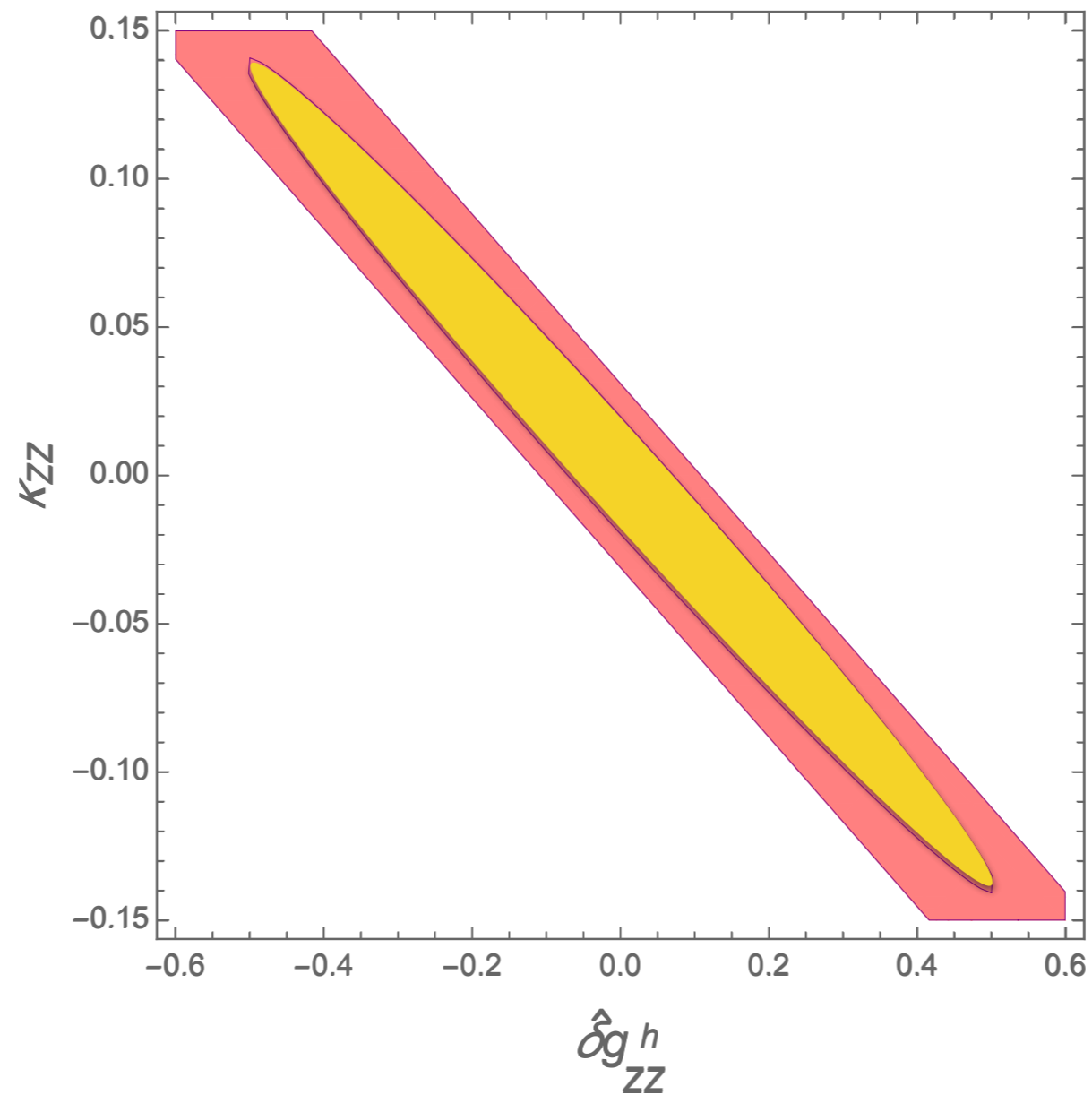
rates only



$$|g_{Zp}^h| < 5 \times 10^{-4}$$

Sensitivity result

Inclusive angular moments

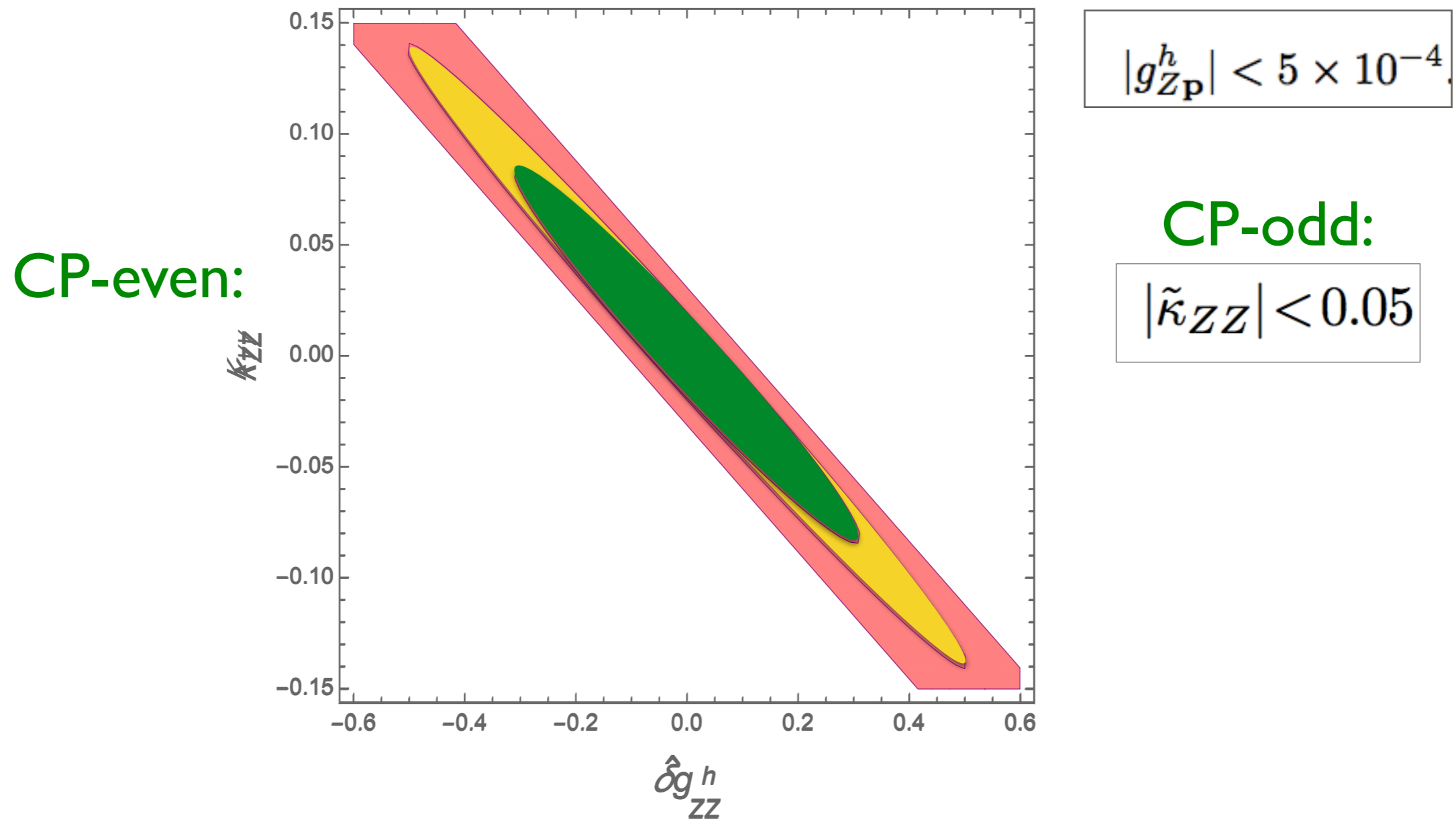


$$|g_{ZZ}^h| < 5 \times 10^{-4}$$

Inclusive moments not sensitive to CP-odd coupling

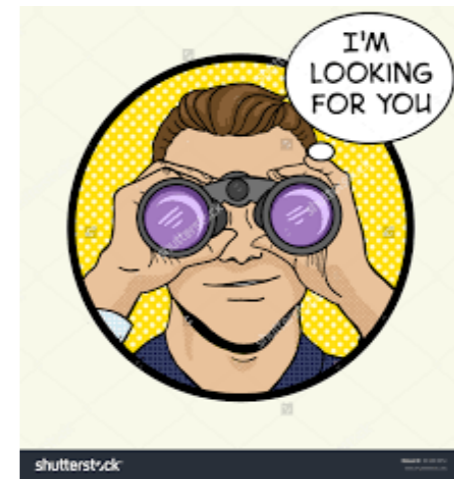
Sensitivity result

All angular moments





Summary



CP violation in the Higgs sector a likely ingredient
for electroweak baryogenesis
-> with reasonably large phases

Necessary to exploit all channels simultaneously

It can be beneficial to project onto maximum set of
kinematically independent moments to obtain optimal
sensitivity