# Toward a unified description of high energy cross sections

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# **OUTLINE**

# QCD at high transverse momentum:

parton model collinear factorization (twist expansion)

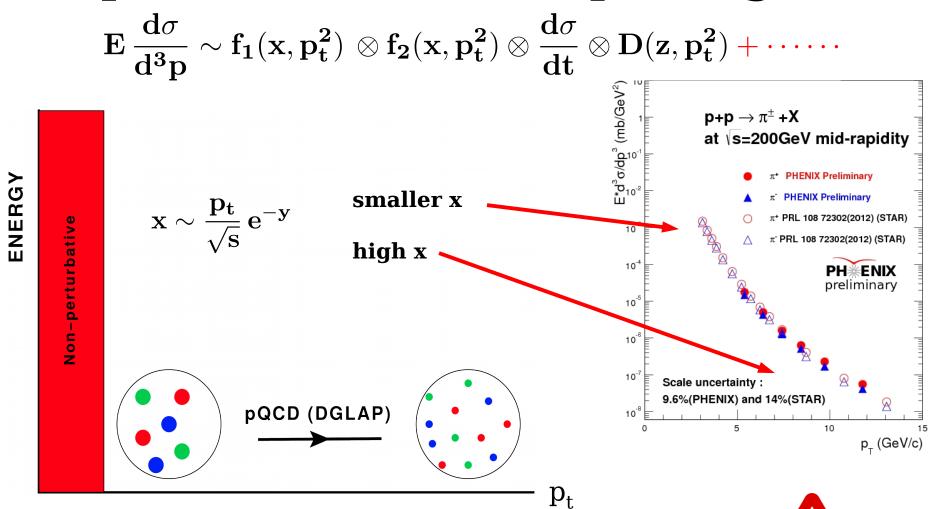
# QCD at high energy (CGC):

high gluon density effects high energy effects

#### Toward a unified formalism:

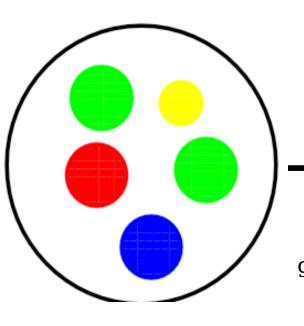
beyond eikonal approximation

# pQCD: the standard paradigm



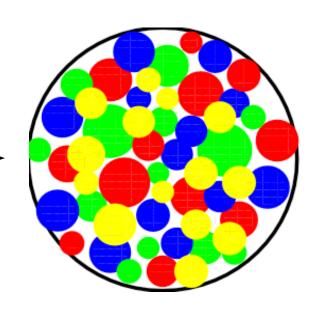
bulk of QCD phenomena happens at low  $p_t$  (small x)





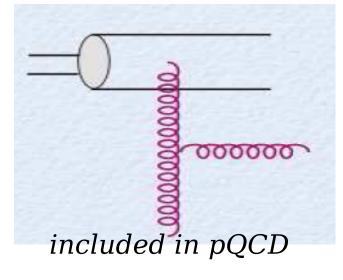
$$S \to \infty, \ Q^2 \ fixed$$
  $x_{Bj} \equiv \frac{Q^2}{S} \to 0$ 

gluon radiation  $\mathbf{P_{gg}}(\mathbf{x}) \sim \frac{1}{\mathbf{x}}$ 



#### collinear factorization breaks down at small x

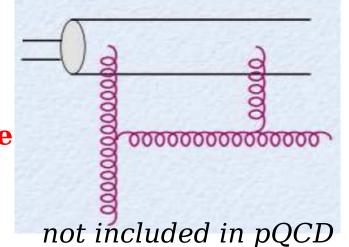
"attractive" bremsstrahlung vs. "repulsive" recombination



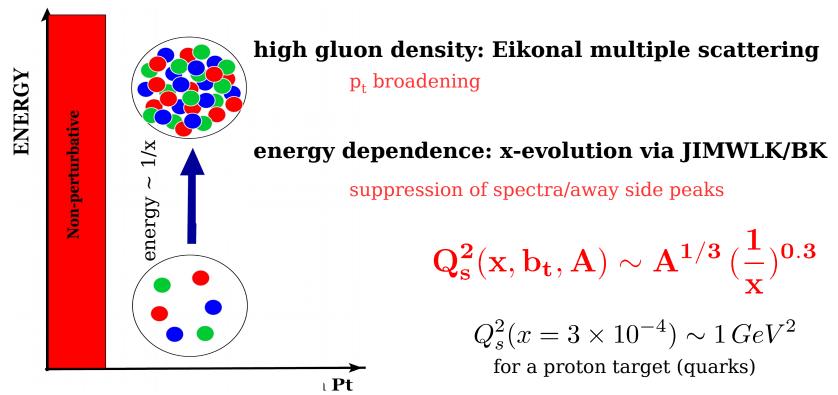
$$rac{lpha_{\mathbf{s}}}{\mathbf{Q^2}} \, rac{\mathbf{x} \mathbf{G}(\mathbf{x}, \mathbf{Q^2})}{\pi \mathbf{r^2}} \sim \mathbf{1}$$

saturation scale

$$Q_s^2(x, b_t, A)$$



#### A hadron/nucleus at high energy: gluon saturation



a framework for multi-particle production in QCD at small x/low  $p_t$ 

Shadowing/Nuclear modification factor Azimuthal angular correlations (di-jets,...) Long range rapidity correlations (ridge,...) Initial conditions for hydro Thermalization

 $x \le 0.01$ 

#### Scattering at high energy (small x) (proton-nucleus)

#### **Eikonal approximation**

$$J_a^\mu \simeq \delta^{\mu-} \rho_a$$
 
$$D_\mu J^\mu = D_- J^- = 0$$
 
$$\partial_- J^- = 0 \quad \text{(in A}^+ = 0 \text{ gauge)}$$
 does not depend on x

solution to EOM: 
$$A_a^-(x^+, x_t) \equiv n^- S_a(x^+, x_t)$$

with 
$$n^{\mu} = (n^{+} = 0, n^{-} = 1, n_{\perp} = 0)$$
$$n^{2} = 2n^{+}n^{-} - n_{\perp}^{2} = 0$$

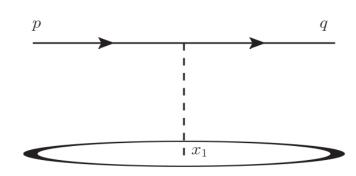
recall (eikonal limit): 
$$\bar{u}(q)\gamma^{\mu}u(p) \to \bar{u}(p)\gamma^{\mu}u(p) \sim p^{\mu}$$
  
 $\bar{u}(q)Au(p) \to p \cdot A \sim p^{+}A^{-}$ 

multiple scattering of a quark from background color field  $S_a(x^+,x_t)$ 

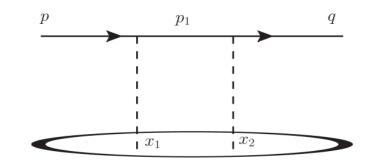
$$i\mathcal{M}_{1} = (ig) \int d^{4}x_{1} e^{i(q-p)x_{1}} \bar{u}(q) \left[ \not h S(x_{1}) \right] u(p)$$

$$= (ig)(2\pi)\delta(p^{+} - q^{+}) \int d^{2}x_{1t} dx_{1}^{+} e^{i(q^{-} - p^{-})x_{1}^{+}} e^{-i(q_{t} - p_{t})x_{1t}}$$

$$\bar{u}(q) \left[ \not h S(x_{1}^{+}, x_{1t}) \right] u(p)$$



$$i\mathcal{M}_2 = (ig)^2 \int d^4x_1 d^4x_2 \int \frac{d^4p_1}{(2\pi)^4} e^{i(p_1-p)x_1} e^{i(q-p_1)x_2}$$
$$\bar{u}(q) \left[ p S(x_2) \frac{ip_1}{p_1^2 + i\epsilon} p S(x_1) \right] u(p)$$



$$\int \frac{dp_1^-}{(2\pi)} \frac{e^{ip_1^-(x_1^+ - x_2^+)}}{2p^+ \left[p_1^- - \frac{p_{1t}^2 - i\epsilon}{2p^+}\right]} = \frac{-i}{2p^+} \theta(x_2^+ - x_1^+) e^{i\frac{p_{1t}^2}{2p^+}(x_1^+ - x_2^+)}$$

contour integration over the pole leads to path ordering of scattering

ignore all terms:  $O(\frac{p_t}{p^+}, \frac{q_t}{q^+})$  and use  $\sqrt{\frac{p_1}{2n \cdot n}} \sqrt{n} = \sqrt{n}$ 

$$i\mathcal{M}_{2} = (ig)^{2} (-i)(i) 2\pi \delta(p^{+} - q^{+}) \int dx_{1}^{+} dx_{2}^{+} \theta(x_{2}^{+} - x_{1}^{+}) \int d^{2}x_{1t} e^{-i(q_{t} - p_{t}) \cdot x_{1t}}$$
$$\bar{u}(q) \left[ S(x_{2}^{+}, x_{1t}) / S(x_{1}^{+}, x_{1t}) \right] u(p)$$

$$A_a^-(x^+, x_\perp) \equiv n^- S_a(x^+, x_\perp)$$

$$P_{n-1} \quad p_n \quad q$$

$$| x_1 \quad | x_2 \quad | x_3 \quad | x_{n-2} \quad | x_{n-1} \quad | x_n \quad |$$

$$\begin{split} i\mathcal{M}_n &= 2\pi\delta(p^+ - q^+)\,\bar{u}(q) \not\!\! h \, \int d^2x_t \, e^{-i(q_t - p_t)\cdot x_t} \\ & \left\{ (ig)^n \, (-i)^n (i)^n \, \int dx_1^+ \, dx_2^+ \, \cdots \, dx_n^+ \, \theta(x_n^+ - x_{n-1}^+) \, \cdots \, \theta(x_2^+ - x_1^+) \right. \\ & \left. \left[ S(x_n^+, x_t) \, S(x_{n-1}^+, x_t) \, \cdots \, S(x_2^+, x_t) S(x_1^+, x_t) \right] \right\} u(p) \\ & i\mathcal{M} = \sum_n i \, \mathcal{M}_n \\ & i\mathcal{M}(p, q) = 2\pi\delta(p^+ - q^+) \, \bar{u}(q) \not\!\! h \, \int d^2x_t \, e^{-i(q_t - p_t)\cdot x_t} \, \left[ V(x_t) - 1 \right] \, u(p) \\ & \text{with } V(x_t) \equiv \hat{P} \exp \left\{ ig \int_{-\infty}^{+\infty} dx^+ \, n^- \, S_a(x^+, x_t) \, t_a \right\} \\ & \text{DIS, proton-nucleus collisions involve} & < Tr \, V(x_\perp) \, V^\dagger(y_\perp) > \end{split}$$

scattering from small x modes of the target can cause only a *small angle deflection* 

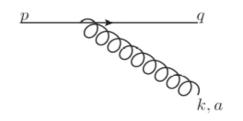
large x partons of target are needed to cause a large angle deflection of quark

$$A_a^{\mu}(x^+, x^-, x_{\perp})$$

#### 1-loop correction: energy dependence

basic ingredient: soft radiation vertex (LC gauge)

$$g \, \bar{u}(q) \, t^a \, \gamma_\mu \, u(p) \, \epsilon^{\mu}_{(\lambda)}(k) \longrightarrow 2 \, g \, t^a \, \frac{\epsilon_{(\lambda)} \cdot k_t}{k_t^2}$$

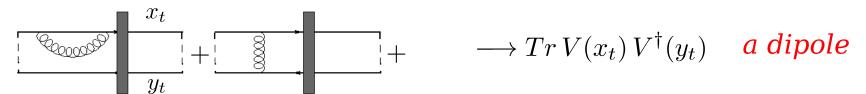


#### coordinate space:

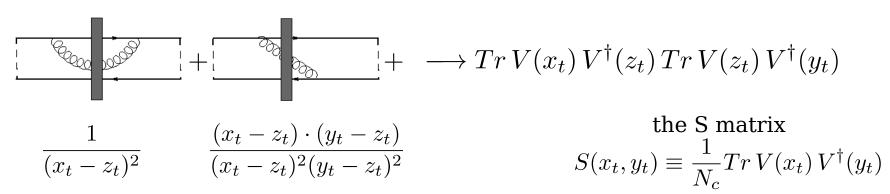
$$\int \frac{d^2 k_t}{(2\pi)^2} e^{ik_t \cdot (x_t - z_t)} 2g t^a \frac{\epsilon_{(\lambda)} \cdot k_t}{k_t^2} = \frac{2ig}{2\pi} t^a \frac{\epsilon_{(\lambda)} \cdot (x_t - z_t)}{(x_t - z_t)^2}$$

x<sub>t</sub>, z<sub>t</sub> are transverse coordinates of the quark and gluon

#### virtual corrections:



#### real corrections:



#### 1-loop correction: BK eq.

at large 
$$N_c$$
  $_{3\otimes\bar{3}=8\oplus1\simeq8}$  where  $\sim$  \_\_\_\_\_

$$\frac{d}{dy}T(x_t, y_t) = \frac{N_c \alpha_s}{2\pi^2} \int d^2 z_t \frac{(x_t - y_t)^2}{(x_t - z_t)^2 (y_t - z_t)^2} \left[ T(x_t, z_t) + T(z_t, y_t) - T(x_t, y_t) - \frac{T(x_t, z_t)T(z_t, y_t)}{T(z_t, y_t)} \right]$$

$$T \equiv 1 - S$$

$$\frac{d}{dy} = \frac{z_t}{y_t} + \frac{z_t}{y_t}$$

$$\tilde{T}(p_t) \sim \frac{1}{p_t^2} \left[ \frac{Q_s^2}{p_t^2} \right] \qquad Q_s^2 \ll p_t^2$$

$$\tilde{T}(p_t) \sim \log \left[ \frac{Q_s^2}{p_t^2} \right] \qquad Q_s^2 \gg p_t^2$$

$$\tilde{T}(p_t) \sim \frac{1}{p_t^2} \left[ \frac{Q_s^2}{p_t^2} \right]^{\gamma} \qquad Q_s^2 < p_t^2$$

nuclear modification factor

$$R_{pA} \equiv \frac{\frac{d\sigma^{pA}}{d^2 p_t dy}}{A^{1/3} \frac{d\sigma^{pp}}{d^2 p_t dy}}$$

suppression of  $p_t$  spectra nuclear shadowing .....

## Particle production in high energy collisions

pQCD and collinear factorization at high  $p_t$ 

breaks down at low  $p_t$  (small x)

CGC at low  $p_t$ 

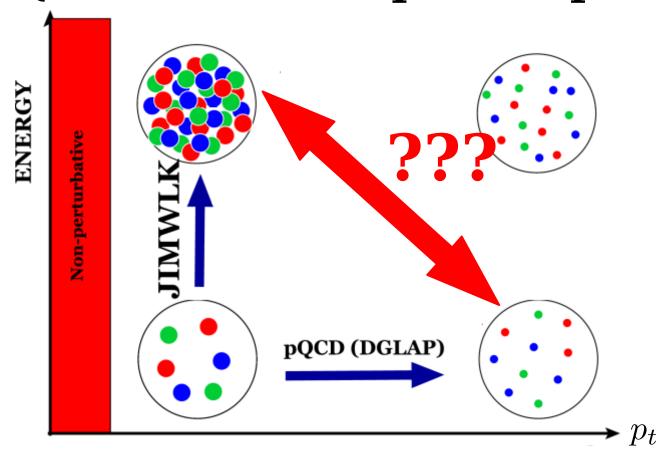
breaks down at large x (high  $p_t$ )

# need a unified formalism:

CGC at low x (low  $p_t$ )

leading twist pQCD (DGLAP) at large x (high  $p_t$ )

# QCD kinematic phase space



#### unifying saturation with high $p_t$ (large x) physics?

<u>kinematics of saturation: where is saturation applicable?</u>
jet physics, high  $p_t$  (polar and azimuthal) angular correlations cold matter energy loss, spin physics?, ......

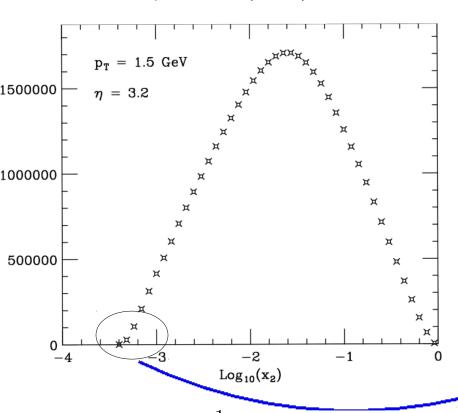
#### Pion production at RHIC: kinematics

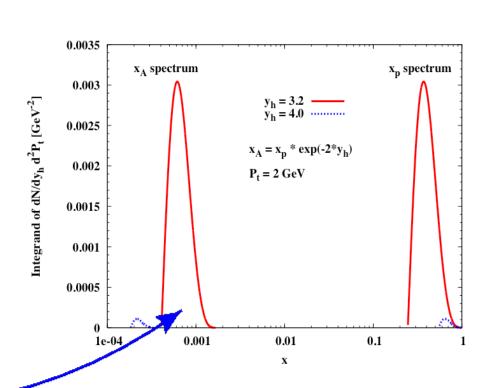
#### collinear factorization

**CGC** 

GSV, PLB603 (2004) 173-183

DHJ, NPA765 (2006) 57-70





$$\int_{x_{min}}^{1} dx \, x G(x, Q^2) \cdot \cdot \cdot \cdot \longrightarrow x_{min} G(x_{min}, Q^2) \cdot \cdot \cdot$$

this is an extreme approximation with potentially severe consequences!



#### Starting point/expression/operator?

pQCD: quark and gluon operators

$$\overline{\Psi}(y^-, 0_t)\gamma^+\Psi(0^-, 0_t)$$

renormalization lead to DGLAP evolution eq.

CGC: correlators of Wilson lines (DIS, Hybrid,....)

$$F_2 \sim Tr V(x_t) V^{\dagger}(y_t)$$

renormalization leads to JIMWLK/BK evolution eq.

# toward unifying small and large x (multiple scattering)

scattering from small x modes of the target field  $A^- \equiv n^- S$  involves only small transverse momenta exchange (small angle deflection)

$$p^{\mu} = (p^{+} \sim \sqrt{s}, p^{-} = 0, p_{t} = 0)$$
  
 $S = S(p^{+} \sim 0, p^{-}/P^{-} \ll 1, p_{t})$ 

allow hard scattering by including one hard field  $A_a^{\mu}(x^+, x^-, x_t)$  during which there is large momenta exchanged and quark can get deflected by a large angle.

include eikonal multiple scattering before and after (along a different direction) the hard scattering

hard scattering: large deflection scattered quark travels in the new "z" direction: 
$$\bar{z}$$
  $\begin{pmatrix} \bar{x} \\ \bar{y} \\ \bar{z} \end{pmatrix} = \mathcal{O} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$ 

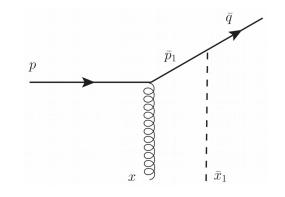
$$i\mathcal{M}_1 = (ig) \int d^4x \, e^{i(\bar{q}-p)x} \, \bar{u}(\bar{q}) \, \left[ A(x) \right] \, u(p)$$

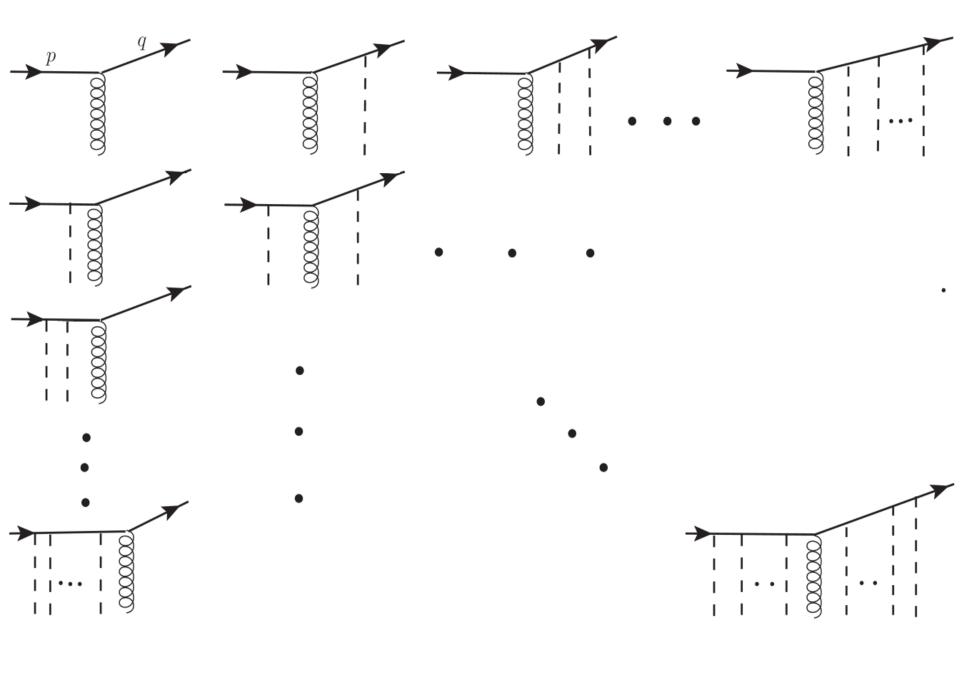
$$i\mathcal{M}_{2} = (ig)^{2} \int d^{4}x \, d^{4}x_{1} \int \frac{d^{4}p_{1}}{(2\pi)^{4}} e^{i(p_{1}-p)x_{1}} e^{i(\bar{q}-p_{1})x} \xrightarrow{p} \overline{u}(\bar{q}) \left[ A(x) \frac{ip_{1}}{p_{1}^{2}+i\epsilon} / S(x_{1}) \right] u(p)$$

$$i\mathcal{M}_{2} = (ig)^{2} \int d^{4}x \, d^{4}\bar{x}_{1} \int \frac{d^{4}\bar{p}_{1}}{(2\pi)^{4}} \, e^{i(\bar{p}_{1}-p)x} \, e^{i(\bar{q}-\bar{p}_{1})\bar{x}_{1}}$$

$$\bar{u}(\bar{q}) \left[ / \bar{p} \, \bar{S}(\bar{x}_{1}) \, \frac{i/ \bar{p}_{1}}{\bar{p}_{1}^{2} + i\epsilon} \mathcal{A}(x) \right] \, u(p)$$

with 
$$ec{ec{v}}=\mathcal{O}\,ec{v}$$





summing all the terms gives:

$$i\mathcal{M}_{1} = \int d^{4}x \, d^{2}z_{t} \, d^{2}\bar{z}_{t} \int \frac{d^{2}k_{t}}{(2\pi)^{2}} \, \frac{d^{2}k_{t}}{(2\pi)^{2}} \, e^{i(\bar{k}-k)x} \, e^{-i(\bar{q}_{t}-\bar{k}_{t})\cdot\bar{z}_{t}} \, e^{-i(k_{t}-p_{t})\cdot z_{t}}$$

$$\bar{u}(\bar{q}) \, \left[ \overline{V}_{AP}(x^{+},\bar{z}_{t}) \, \not \! n \, \frac{\bar{k}}{2\bar{k}^{+}} \, \left[ ig \mathcal{A}(x) \right] \, \frac{k}{2k^{+}} \, \not \! n \, V_{AP}(z_{t},x^{+}) \right] \, u(p)$$

with

$$\overline{V}_{AP}(x^+, \bar{z}_t) \equiv \hat{P} \exp \left\{ ig \int_{x^+}^{+\infty} d\bar{z}^+ \, \bar{S}_a^-(\bar{z}_t, \bar{z}^+) \, t_a \right\}$$

$$V_{AP}(z_t, x^+) \equiv \hat{P} \exp \left\{ ig \int_{-\infty}^{x^+} dz^+ S_a^-(z_t, z^+) t_a \right\}$$

can extract the effective quark propagator  $i\mathcal{M}(p,ar{q})=ar{u}(ar{q})\, au_F\,u(p)$ 

### interactions of large and small x modes

$$i\mathcal{M} = \int_{acd} \int \frac{d^4k}{(2\pi)^4} d^4x d^4x_1 e^{i(\bar{q}-p-k)x_1} e^{ikx}$$

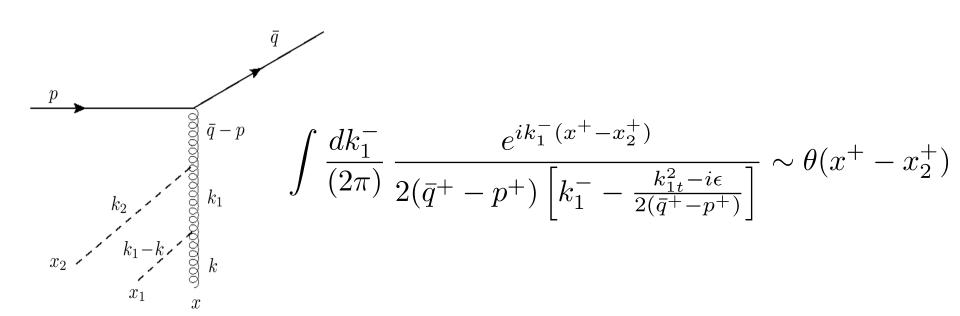
$$\bar{u}(\bar{q}) (ig \gamma^{\mu} t^a) u(p) A^c_{\lambda}(x) \left[ ig S^d(x_1) \right]$$

$$\frac{1}{(p-\bar{q})^2 + i\epsilon} \left[ -g^{\mu}_{\lambda} n \cdot (p-\bar{q}-k) + n^{\mu} \left[ p_{\lambda} - \bar{q}_{\lambda} \left( 1 - \frac{n \cdot k}{n \cdot (p-\bar{q})} \right) \right] \right]$$

performing  $k^-$  integration sets  $x_1^+ = x^+$ 

$$i\mathcal{M} = 2f_{acd} \int d^4x \, e^{i(\bar{q}-p)x}$$

$$\bar{u}(\bar{q}) \, \frac{\left[ n (p-\bar{q}) \cdot A_c(x) - A_c(x) \, n \cdot (p-\bar{q}) \right]}{(p-\bar{q})^2} \, (ig \, t^a) \, u(p) \, \left[ ig \, S^d(x^+, x_t) \right]$$



$$i\mathcal{M} = 2 f_{abc} f_{cde} \int d^4 x \, dx_2^+ \, \theta(x^+ - x_2^+) \, e^{i(\bar{q}^+ - p^+)x^- - i(\bar{q}_t - p_t) \cdot x_t}$$

$$\bar{u}(\bar{q}) \frac{\left[ \not h \, (p - \bar{q}) \cdot A_e(x) - \not A_c(x) \, n \cdot (p - \bar{q}) \right]}{(p - \bar{q})^2} \, (ig \, t^a) \, u(p)$$

$$\left[ ig \, S_d(x^+, x_t) \right] \left[ ig \, S_b(x_2^+, x_t) \right]$$

$$\bar{q} = \frac{2(i)^2}{(\bar{q} - p)^2} f^{abc} f^{cde} f^{egf} \int d^4x \, dx_2^+ dx_3^+ \, \theta(x^+ - x_2^+) \, \theta(x_2^+ - x_3^+) \\ \bar{u}(\bar{q}) \, (ig \, t^a) \left[ n \cdot (p - \bar{q}) A_f(x) - (p - \bar{q}) \cdot A_f(x) n \right] u(p) \\ \left[ ig \, S_g(x^+, x_t) \right] \left[ ig \, S_d(x_2^+, x_t) \right] \left[ ig \, S_b(x_3^+, x_t) \right] \\ e^{i(\bar{q}^+ - p^+)x^- - i(\bar{q}_t - p_t) \cdot x_t}$$

#### recall

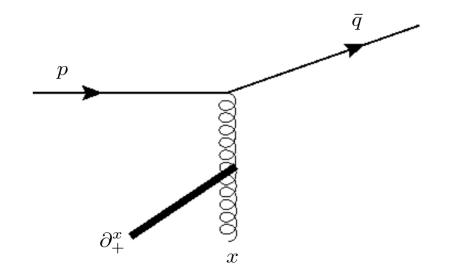
$$\partial_{x^{+}} \left[ U_{AP}^{\dagger}(x_{t}, x^{+}) \right]^{ab} = (if^{bca}) \left[ igS_{c}(x^{+}, x_{t}) \right]$$

$$+ (if^{bce}) \left( if^{eda} \right) \int dx_{1}^{+} \theta(x^{+} - x_{1}^{+}) \left[ \left[ igS_{c}(x^{+}, x_{t}) \right] \left[ igS_{d}(x_{1}^{+}, x_{t}) \right] \right]$$

$$+ (if^{bch}) \left( if^{gdf} \right) \left( if^{fea} \right) \int dx_{1}^{+} dx_{2}^{+} \theta(x^{+} - x_{1}^{+}) \theta(x_{1}^{+} - x_{2}^{+})$$

$$+ \left[ \left[ igS_{c}(x^{+}, x_{t}) \right] \left[ igS_{d}(x_{1}^{+}, x_{t}) \right] \left[ \left[ igS_{c}(x_{2}^{+}, x_{t}) \right] + \cdots \right]$$

all re-scatterings of hard Gluon can be re-summed

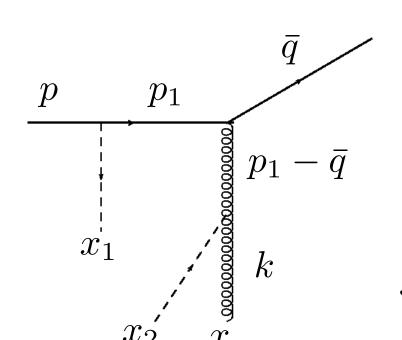


$$i\mathcal{M}_{2} = \frac{2i}{(p-\bar{q})^{2}} \int d^{4}x \, e^{i(\bar{q}-p)x} \, \bar{u}(\bar{q}) \left[ (ig \, t^{a}) \left[ \partial_{x^{+}} U_{AP}^{\dagger}(x_{t}, x^{+}) \right]^{ab} \right]$$

$$\left[ n \cdot (p-\bar{q}) \mathcal{A}_{b}(x) - (p-\bar{q}) \cdot A_{b}(x) \mathcal{N} \right] u(p)$$

with 
$$U_{AP}(x_t, x^+) \equiv \hat{P} \exp \left\{ ig \int_{-\infty}^{x^+} dz^+ S_a^-(z^+, x_t) T_a \right\}$$

#### but there is more!



# both initial state quark and hard gluon interacting:

integration over  $p_1^-$ 

$$\int \frac{dp_1^-}{2\pi} \frac{e^{ip_1^-(x_1^+ - x^+)}}{[p_1^2 + i\epsilon] [(p_1 - \bar{q})^2 + i\epsilon]}$$

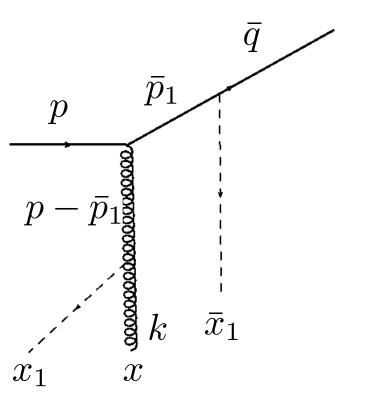
both poles are below the real axis, we get

$$\frac{e^{i\frac{p_{1t}^2}{2p^+}(x_1^+ - x^+)}}{\left[\frac{p_{1t}^2}{2p^+} - \bar{q}^- - \frac{(p_{1t} - \bar{q}_t)^2}{2(p^+ - \bar{q}^+)}\right]} + \frac{e^{i\left[\bar{q}^- + \frac{(p_{1t} - \bar{q}_t)^2}{2(p^+ - \bar{q}^+)}\right](x_1^+ - x^+)}}{\left[\bar{q}^- + \frac{(p_{1t} - \bar{q}_t)^2}{2(p^+ - \bar{q}^+)} - \frac{p_{1t}^2}{2p^+}\right]}$$

ignoring phases we get a cancellation!

this can be shown to hold to all orders whenever both initial state quark and hard gluon scatter from the soft fields!

#### how about the final state quark interactions?



integration over  $\bar{p}_1^-$ 

$$\int \frac{d\bar{p}_1^-}{2\pi} \frac{e^{i\bar{p}_1^-(\bar{x}_1^+ - x^+)}}{[\bar{p}_1^2 + i\epsilon] [(p_1 - \bar{p}_1)^2 + i\epsilon]}$$

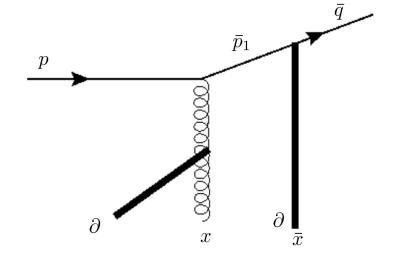
now the poles are on the opposite side of the real axis, we get both ordering

$$\theta(x^{+} - \bar{x}_{1}^{+}) \text{ and } \theta(\bar{x}_{1}^{+} - x^{+})$$

ignoring the phases the contribution of the two poles add! path ordering is lost!

however further rescatterings are still path-ordered before/after  $\mathbf{X_1^+}, \mathbf{\bar{X}_1^+}$ 

#### these contributions re-sum to

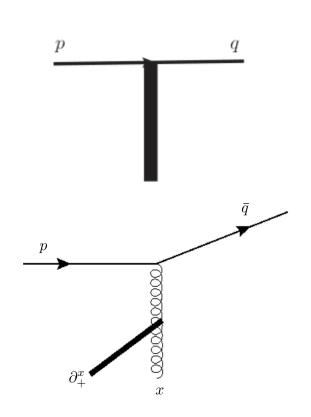


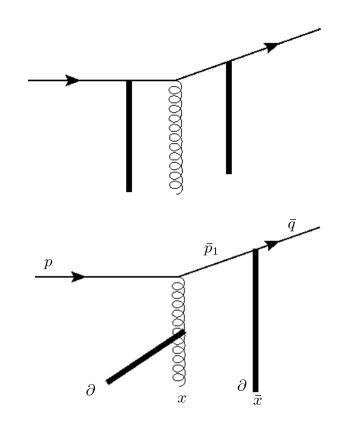
$$i\mathcal{M}_{3} = -2i \int d^{4}x \, d^{2}\bar{x}_{t} \, d\bar{x}^{+} \, \frac{d^{2}\bar{p}_{1t}}{(2\pi)^{2}} \, e^{i(\bar{q}^{+}-p^{+})x^{-}} \, e^{-i(\bar{p}_{1t}-p_{t})\cdot x_{t}} \, e^{-i(\bar{q}_{t}-\bar{p}_{1t})\cdot \bar{x}_{t}}$$

$$\bar{u}(\bar{q}) \left[ \left[ \partial_{\bar{x}^{+}} \, \overline{V}_{AP}(\bar{x}^{+}, \bar{x}_{t}) \right] \not n \not p_{1} \, (igt^{a}) \, \left[ \partial_{x^{+}} \, U_{AP}^{\dagger}(x_{t}, x^{+}) \right]^{ab} \right]$$

$$\frac{\left[ n \cdot (p - \bar{q}) \not A^{b}(x) - (p - \bar{p}_{1}) \cdot A^{b}(x) \not n \right]}{\left[ 2n \cdot \bar{q} \, 2n \cdot (p - \bar{q}) \, p^{-} - 2n \cdot (p - \bar{q}) \, \bar{p}_{1t}^{2} - 2n \cdot \bar{q} \, (\bar{p}_{1t} - p_{t})^{2} \right]} \, u(p)$$

# full amplitude: $i\mathcal{M} = i\mathcal{M}_{eik} + i\mathcal{M}_1 + i\mathcal{M}_2 + i\mathcal{M}_3$





 $\begin{array}{cccc}
A^{\mu}(x) & \to & n^{-}S(x^{+}, x_{t}) \\
n \cdot \overline{q} & \to & n \cdot p
\end{array}
\qquad i\mathcal{M} \longrightarrow i\mathcal{M}_{eik}$ soft (eikonal) limit:

cross section:  $|i\mathcal{M}|^2 = |i\mathcal{M}_{eik} + i\mathcal{M}_1 + i\mathcal{M}_2 + i\mathcal{M}_3|^2$ 

$$|i\mathcal{M}_{2}|^{2} = \frac{8g^{2}}{(p-\bar{q})^{4}} \int d^{4}x \, d^{4}y \, e^{i(\bar{q}^{+}-p^{+})(x^{-}-y^{-})} \, e^{-i(\bar{q}_{t}-p_{t})\cdot(x_{t}-y_{t})}$$

$$\left\{ p^{+}q^{-}(p^{+}-\bar{q})^{2} \, A_{\perp}^{b}(x) \cdot A_{\perp}^{c}(y) + 2 \, (p^{+})^{2} \, q_{\perp} \cdot A_{\perp}^{b}(x) \, q_{\perp} \cdot A_{\perp}^{c}(y) \right\}$$

$$\left[ \partial_{y^{+}} \, U_{AP}(y_{t},y^{+}) \right]^{ca} \left[ \partial_{x^{+}} \, U_{AP}^{\dagger}(x_{t},x^{+}) \right]^{ab}$$

other terms are more complicated: spinor helicity formalism for Dirac Algebra

DIS: structure functions, di-jet production

PA: single inclusive particle production

## **SUMMARY**

CGC is a systematic approach to high energy collisions

CGC breaks down at large x (high  $p_t$ )

a significant portion of EIC phase space is at large xtransition from DGLAP physics to CGC

#### Toward a unified formalism:

quark scattering from small and large x fields

particle production in pp, pA in both small and large x ( $p_t$ ) kinematics

spin asymmetries

DIS structure functions