

Precision (Anti)Neutrino Scattering off Nucleons and Nuclei

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*Neutrino Platform Week 2019: Hot Topics in Neutrino Physics
CERN, Geneva, Switzerland, October 8, 2019*

I Introduction

- ◆ *Electron and ν probes*
- ◆ *Status of ν scattering experiments*

II Requirements for Precision Physics

- ◆ *Statistics vs. resolution*
- ◆ *Control of the targets*
- ◆ *Control of the fluxes*

III Precision Measurements

- ◆ *Electroweak measurements*
- ◆ *Adler sum rule*
- ◆ *Isospin physics*
- ◆ *Nuclear modifications of nucleon properties*

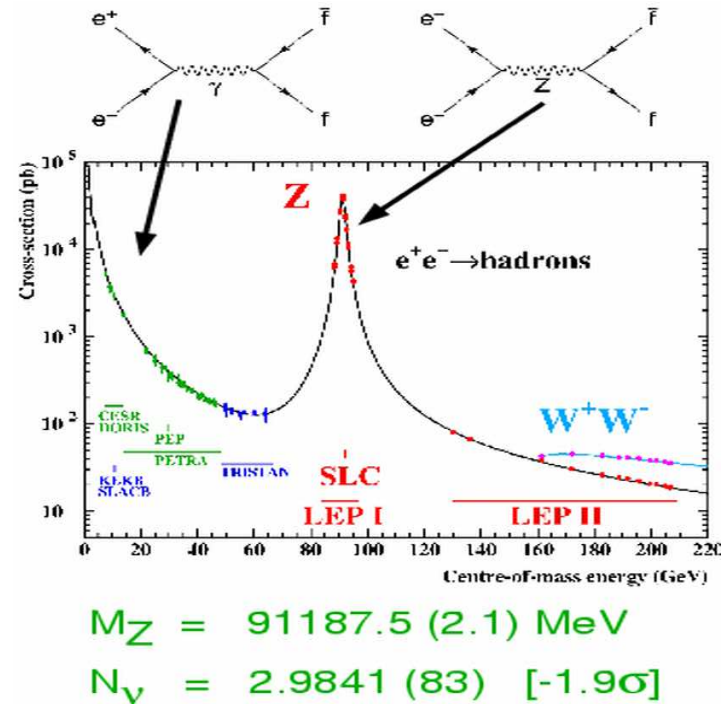
IV Summary

PRECISION PHYSICS: e^\pm PROBE

- ◆ Reference EW studies in e^+e^- at LEP by enhancing weak σ at the Z^0 mass pole:

	Number of Z^0	Number of W
LEP	18×10^6	80×10^3

⇒ High-statistics electroweak measurements at LEP/SLC reached a precision $< 10^{-3}$.



- ◆ Reference QCD studies in ep at HERA with measurements $\sim 10^{-2}$ of the nucleon structure complementary to fixed target from JLab, COMPASS, SLAC, NMC, BCDMS etc.

⇒ Can a modern $\nu(\bar{\nu})$ facility deliver comparable precisions adding insights complementary to planned fixed-target & collider programs?

◆ *Neutrinos offer an ideal probe for EW physics and partonic/hadronic structure of matter:*

- Clean probe since only weak interaction, full polarization;
- Complete flavor separation in Charged Current interactions (d/u , s/\bar{s} , \bar{d}/\bar{u})
- Separation of valence (xF_3) and sea (F_2) distributions, complementary to e^\pm .

⇒ *Potential so far only partially explored due to 3 (main) limitations*

◆ **STATISTICS**

Tiny cross-sections with limited beam intensities required massive & coarse detectors.

◆ **TARGETS**

Need of massive nuclear targets did not allow a precise control of the interactions.

◆ **FLUXES**

Incoming (anti)neutrino energy unknown implied substantial flux uncertainties.

STATISTICS vs. RESOLUTION

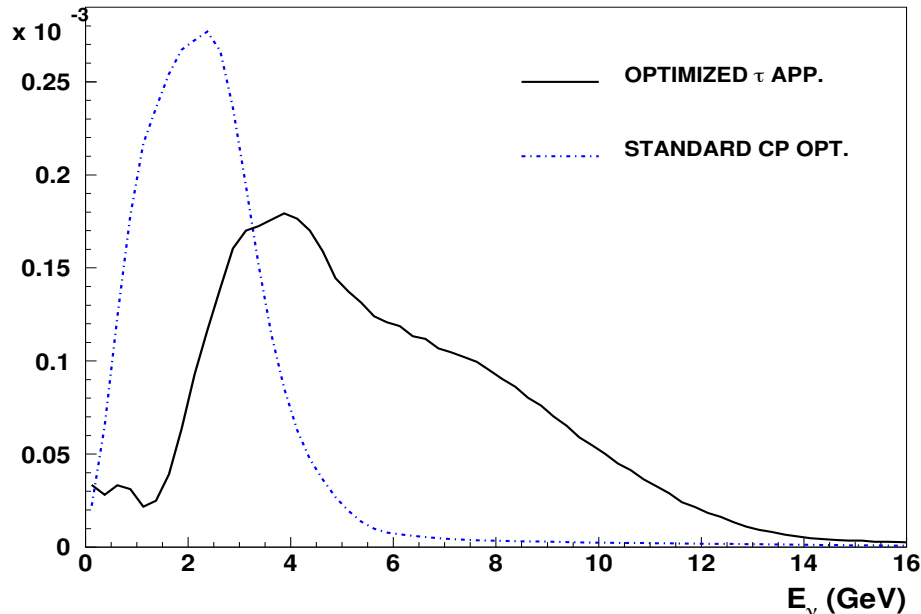
- Existing detectors compromise between high (low) statistics and coarse (high) resolution: *affected by systematics on E_μ , E_H scales, nuclear targets & flux*

Experiment	Mass	ν_μ CC Stat.	Target	E_ν (GeV)	ΔE_μ	ΔE_H
CDHS	750 t	10^7	p,Fe	20-200	2.0%	2.5%
BEBC	various	5.7×10^4	p,D,Ne	10-200		
CCFR	690 t	1.0×10^6	Fe	30-360	1.0%	1.0%
NuTeV	690 t	1.3×10^6	Fe	30-360	0.7%	0.43%
CHORUS	100 t	3.6×10^6	Emul.,Pb	10-200	2.5%	5.0%
NOMAD	2.7 t	1.5×10^6	C,Fe	5-200	0.2%	0.5%
MINOS ND	980 t	3.6×10^6	Fe	3-50	2-4%	5.6%
T2K ND	1.9 t	10^5	CH,H ₂ O	0.2-5	0.6%	2-4%
MINER ν A	5.4 t	10^7	CH,C,Fe,Pb	1-30	2%	

⇒ Significant progress requires about 10^8 CC AND high resolution $\Delta E_\mu \leq 0.2\%$

- Precision EW and QCD studies prefer high energy (anti)neutrinos

⇒ Modern beam facilities optimized at lower energies for detection of oscillations



Process	Events (5 t)
<i>Standard CP optimized (1.2 MW):</i>	
ν_μ CC (FHC, 5 y)	34×10^6
$\bar{\nu}_\mu$ CC (RHC, 5 y)	13×10^6
<i>Optimized ν_τ appearance (2.4 MW):</i>	
ν_μ CC (FHC, 2 y)	66×10^6
$\bar{\nu}_\mu$ CC (RHC, 2 y)	24×10^6
TOTAL W^+	100×10^6
TOTAL W^-	37×10^6
TOTAL Z^0	44×10^6

◆ *Available LBNF – Long-Baseline Neutrino Facility – beam optimized for FD ν_τ appearance:*
 Conceivable dedicated run after 5y FHC + 5y RHC with the "standard" beams optimized for CP

- *LBNF:* 120 GeV p, 1.2 MW, 1.1×10^{21} pot/y, ND at 574m;
- *LBNF upgrade:* 120 GeV p, **2.4 MW (x 2)**, $\sim 3 \times 10^{21}$ pot/y.

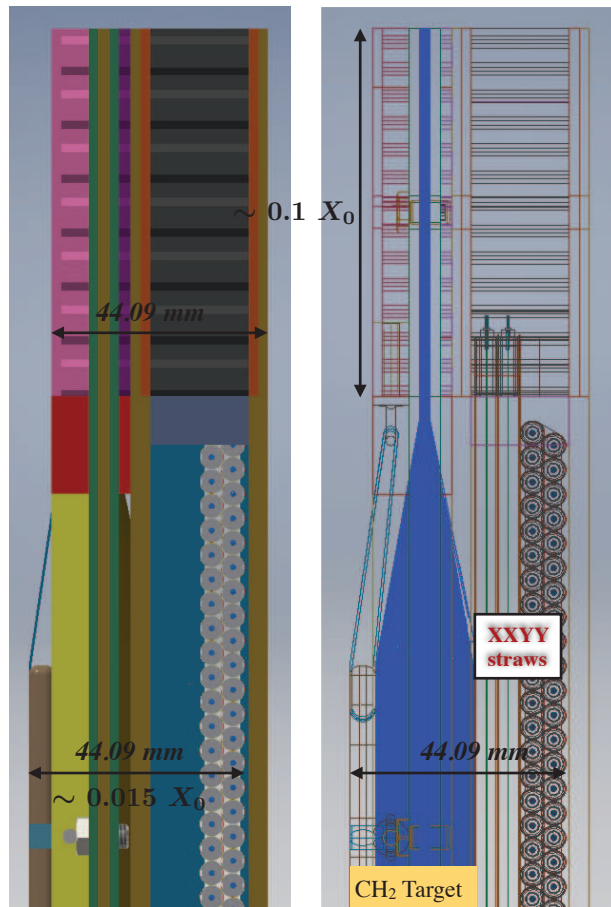
◆ Assume a modest 2y FHC run with ν_τ optimized beam & LBNF upgrade

⇒ *Can afford a high resolution ND of a few tons and still collect desired statistics $\sim 10^8$*

CONTROL OF TARGETS

- ◆ Precision EW & QCD measurements *require control of ν -target(s) as in e^\pm DIS:*
 - Massive ν detectors intrinsically limited by the knowledge of the target composition & materials;
 - Possible accurate control of target(s) by separating target(s) from active detector(s);
 - Thin targets spread out uniformly within tracker by keeping low density $0.005 \leq \rho \leq 0.18 \text{ g/cm}^3$.

⇒ Straw Tube Tracker (STT) in $B \sim 0.6 \text{ T}$ with 4π electromagnetic calorimeter

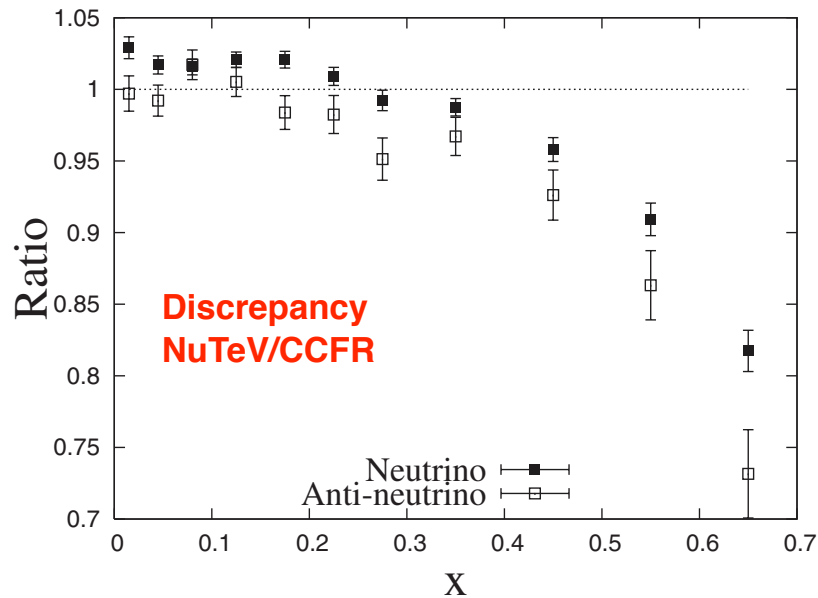


- ◆ Targets (100% purity) account for $\sim 97\%$ of STT mass (straws 3%) and can be tuned to achieve desired statistics & resolutions.
- ◆ Separation from excellent vertex, angular & timing resolutions.
- ◆ Thin targets can be replaced during data taking: C, Ca, Ar, Fe, Pb, etc.

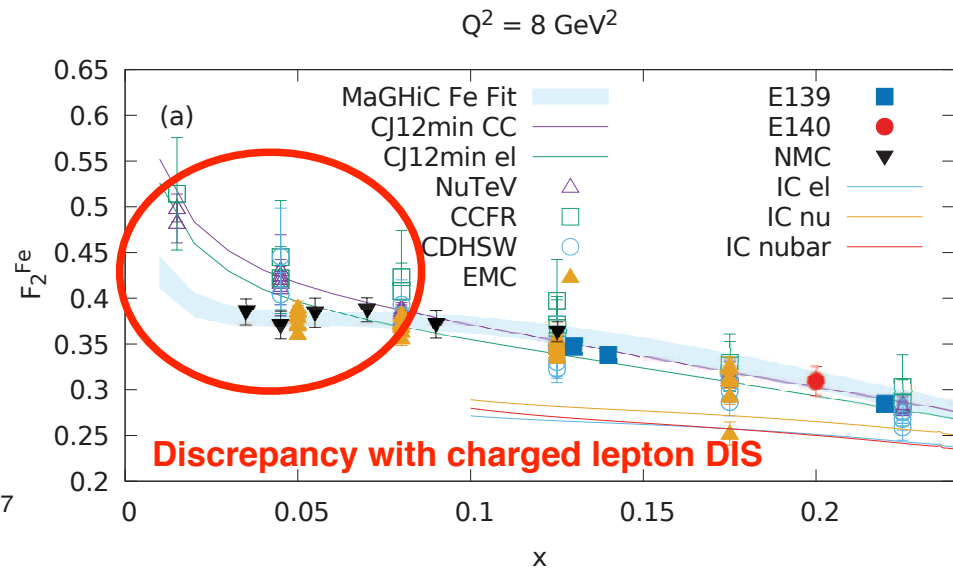
◆ *Need to understand nuclear modifications & corresponding systematic uncertainties:*

- Use of heavy target material(s) unavoidable to achieve desired statistics;
- Complexity of weak current (vs. EM) + substantial nuclear modifications (primary & FSI);
- Cannot rely only on model corrections for precision EW & QCD studies.

⇒ *Necessary condition availability of (complementary) free nucleon target: hydrogen*



NuTeV Coll., PRD 74 (2006) 012008

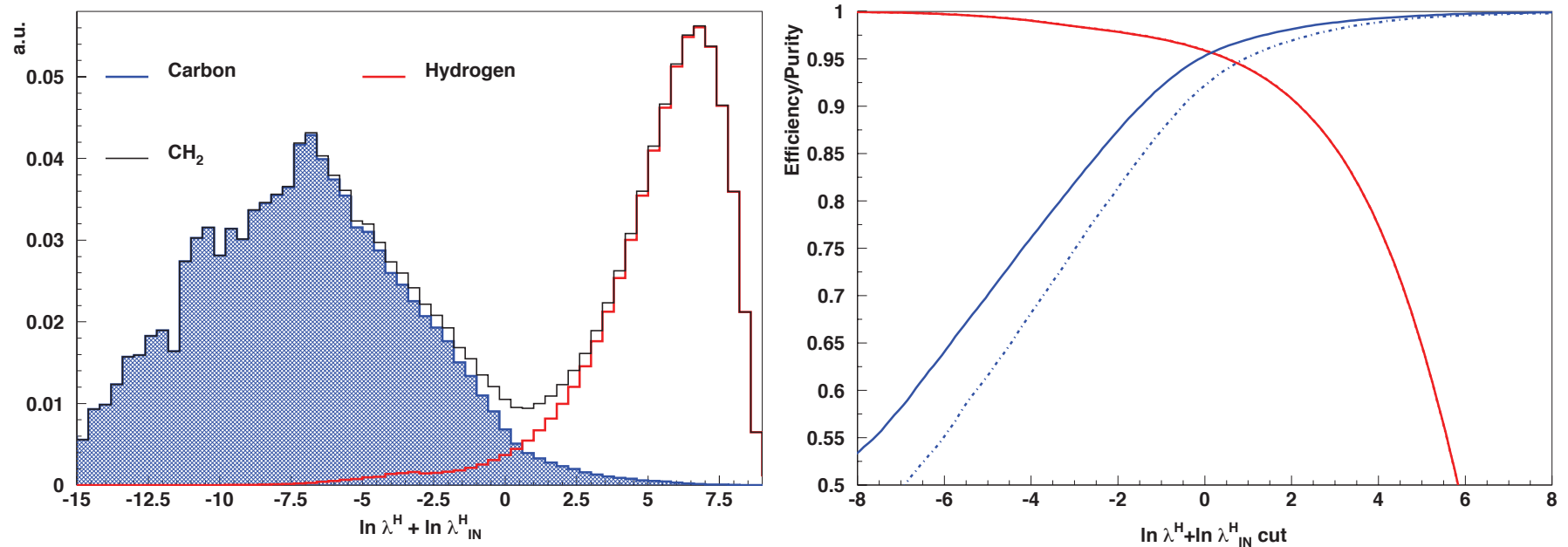


N. Kalantarians, C. Keppel, M.E. Cristy, PRC 96 (2017) 032201

◆ *Novel technique to get $\nu(\bar{\nu})$ -Hydrogen by subtracting CH_2 and C targets (solid H):*

- *Exploit high resolutions & control of chemical composition and mass of targets in STT;*
- *Model-independent data subtraction of dedicated C (graphite) target from main CH_2 target;*
- *Kinematic selection provides large H samples of inclusive & exclusive CC topologies with 80-95% purity and $>90\%$ efficiency before subtraction.*

⇒ *Viable and realistic alternative to liquid H_2 detectors*

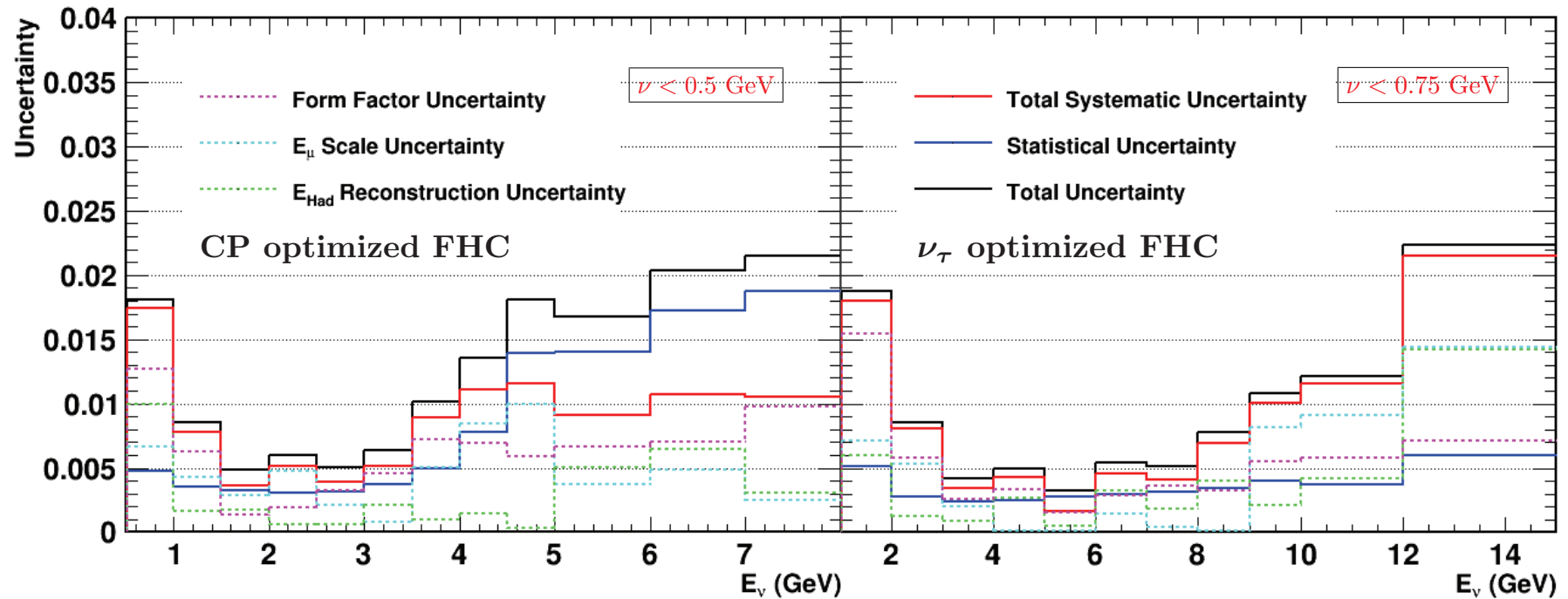


H. Duyang, B. Guo, S.R. Mishra, RP, arXiv:1809.08752 [hep-ph]

◆ *Relative ν_μ flux vs. E_ν from exclusive $\nu_\mu p \rightarrow \mu^- p \pi^+$ on Hydrogen:*

- Select well reconstructed $\mu^- p \pi^+$ topology on H ($\delta p/p \sim 3.5\%$);
- Cut $\nu < 0.5(0.75)$ GeV flattens cross-sections reducing uncertainties on E_ν dependence;
- Systematic uncertainties dominated by muon energy scale ($\Delta E_\mu \sim 0.2\%$ in STT from K_0 mass).

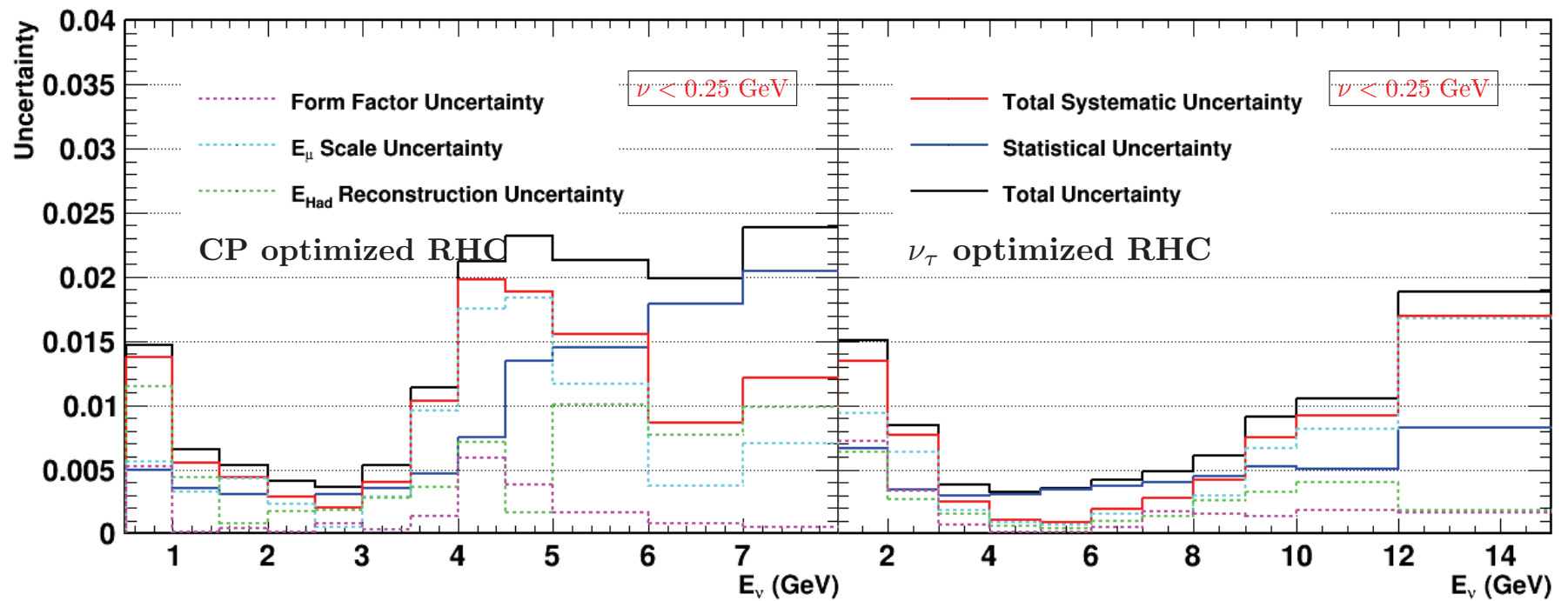
⇒ *Dramatic reduction of systematics vs. techniques using nuclear targets*



H. Duyang, B. Guo, S.R. Mishra, RP, PLB 795 (2019) 424, arXiv:1902.09480 [hep-ph]

◆ *Relative $\bar{\nu}_\mu$ flux vs. E_ν from exclusive $\bar{\nu}_\mu p \rightarrow \mu^+ n$ QE on Hydrogen:*

- E_ν from QE kinematics on H and reconstructed direction of interacting neutrons ($\sim 80\%$);
- Cut $\nu < 0.1(0.25)$ GeV flattens cross-sections reducing uncertainties on E_ν dependence;
- Systematics and total uncertainties comparable to relative ν_μ flux from $\nu_\mu p \rightarrow \mu^- p \pi^+$ on H.



H. Duyang, B. Guo, S.R. Mishra, RP, PLB 795 (2019) 424, arXiv:1902.09480 [hep-ph]

- ◆ Possible to address the main limitations of neutrino experiments (statistics, control of targets & fluxes) largely *filling the precision gap with electron experiments*.

⇒ *Exploit the unique properties of the (anti)neutrino probe to study fundamental interactions & structure of nucleons and nuclei*

- ◆ *Turn the LBNF ND site into a general purpose ν & $\bar{\nu}$ physics facility with broad program complementary to ongoing fixed-target, collider and nuclear physics efforts:*

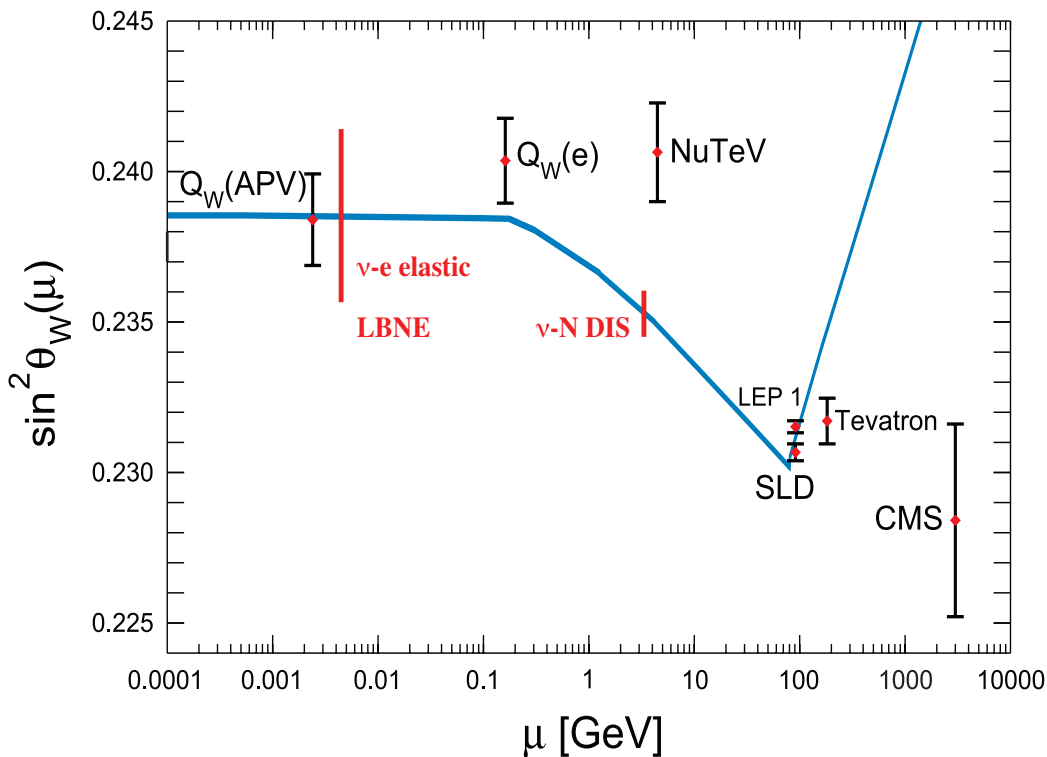
- *Measurement of $\sin^2 \theta_W$ and electroweak physics;*
- *Precision tests of isospin physics & sum rules (Adler, GLS);*
- *Measurements of strangeness content of the nucleon ($s(x)$, $\bar{s}(x)$, Δs , etc.);*
- *Studies of QCD and structure of nucleons and nuclei;*
- *Precision tests of the structure of the weak current: PCAC, CVC;*
- *Measurement of nuclear physics and (anti)-neutrino-nucleus interactions; etc.*
- *Precision measurements as probes of New Physics (BSM);*
- *Searches for New Physics (BSM)*

⇒ *Discovery potential & hundreds of diverse physics topics*

- ◆ *Same control of targets & fluxes reduces systematics for long-baseline oscillations.*

◆ Sensitivity expected from ν scattering at LBNF comparable to the Collider precision:

- *Different scale* of momentum transfer with respect to LEP/SLD (off Z^0 pole);
- Direct measurement of neutrino couplings to Z^0
 \implies *Only other measurement LEP $\Gamma_{\nu\nu}$*
- *Single experiment to directly check the running of $\sin^2 \theta_W$* ;
- *Independent cross-check of the NuTeV $\sin^2 \theta_W$ anomaly ($\sim 3\sigma$ in ν data) in a similar Q^2 range.*



◆ *Different independent channels:*

- $\mathcal{R}^\nu = \frac{\sigma_{\text{NC}}^\nu}{\sigma_{\text{CC}}^\nu}$ in ν -N DIS ($\sim 0.35\%$)
- $\mathcal{R}_{\nu e} = \frac{\sigma_{\text{NC}}^{\bar{\nu}}}{\sigma_{\text{NC}}^\nu}$ in ν - e^- NC elastic ($\sim 1\%$)
- NC/CC ratio ($\nu p \rightarrow \nu p$)/($\nu n \rightarrow \mu^- p$) in (quasi)-elastic interactions
- NC/CC ratio ρ^0/ρ^+ in coherent processes

\implies *Combined EW fits like LEP*

◆ *Further reduction of uncertainties depending upon beam exposure*

- ◆ The Adler integral provides the **ISOSPIN** of the target and is derived from current algebra:

$$S_A(Q^2) = \int_0^1 \frac{dx}{2x} \left(F_2^{\bar{\nu}p} - F_2^{\nu p} \right) = I_p$$

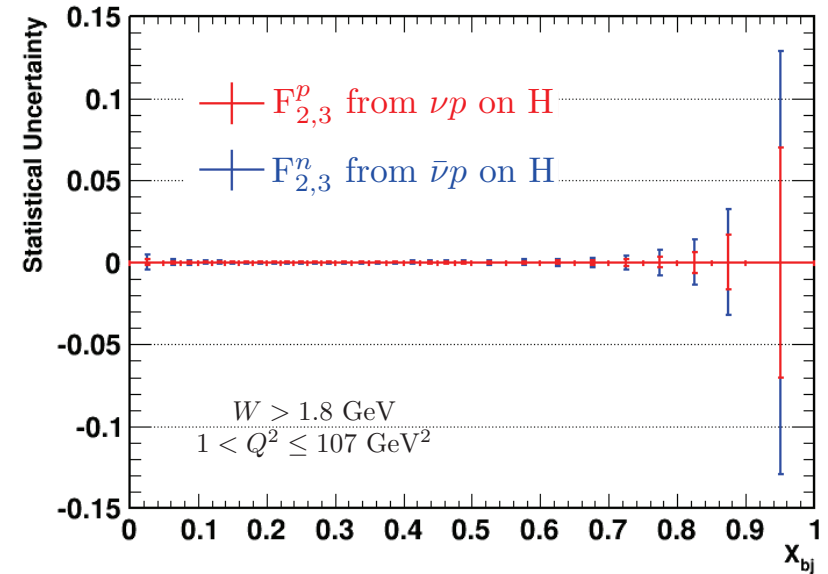
- At large Q^2 (quarks) sensitive to $(s - \bar{s})$ asymmetry, isospin violations, heavy quark production
- Apply to nuclear targets and test nuclear effects (S. Kulagin and R.P. PRD 76 (2007) 094023)

⇒ Precision test of S_A at different Q^2 values

- ◆ Only measurement available from BEBC based on 5,000 νp and 9,000 $\bar{\nu} p$ (D. Allasia et al., ZPC 28 (1985) 321)

- ◆ Direct measurement of $F_{2,3}^{\nu n} / F_{2,3}^{\nu p}$ free from nuclear uncertainties and comparisons with e/μ DIS

⇒ d/u at large x and verify limit for $x \rightarrow 1$

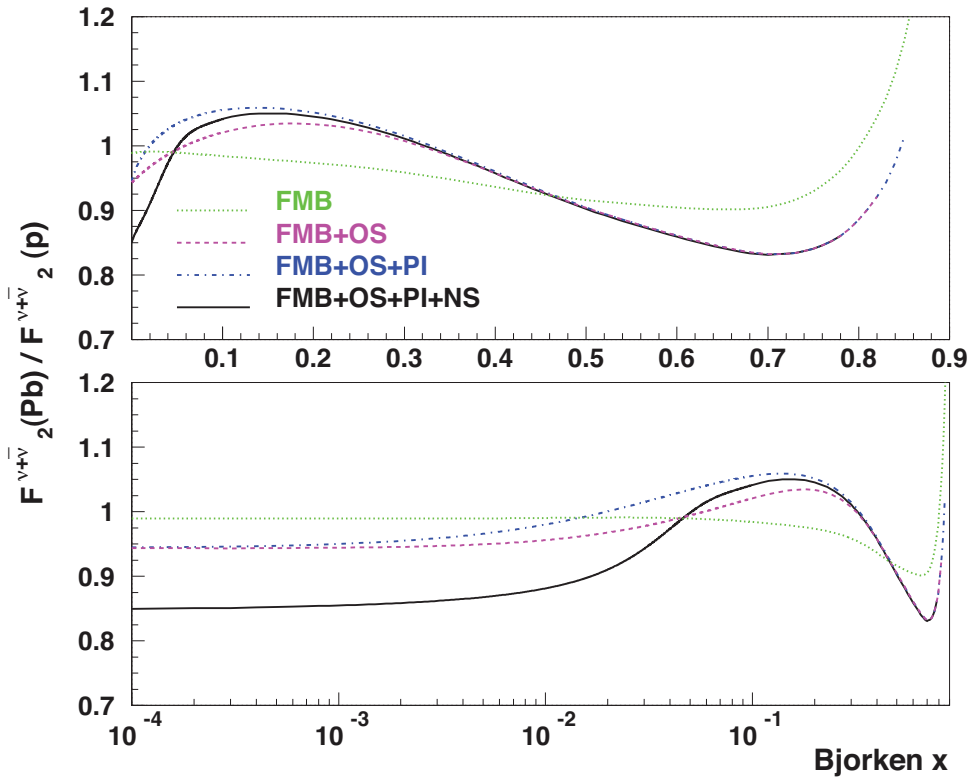


Process	$\nu(\bar{\nu})\text{-H}$
Standard CP optimized:	
ν_μ CC (5 y)	3.4×10^6
$\bar{\nu}_\mu$ CC (5 y)	2.5×10^6
Optimized ν_τ appearance:	
ν_μ CC (2 y)	6.5×10^6
ν_μ CC (2 y)	4.3×10^6

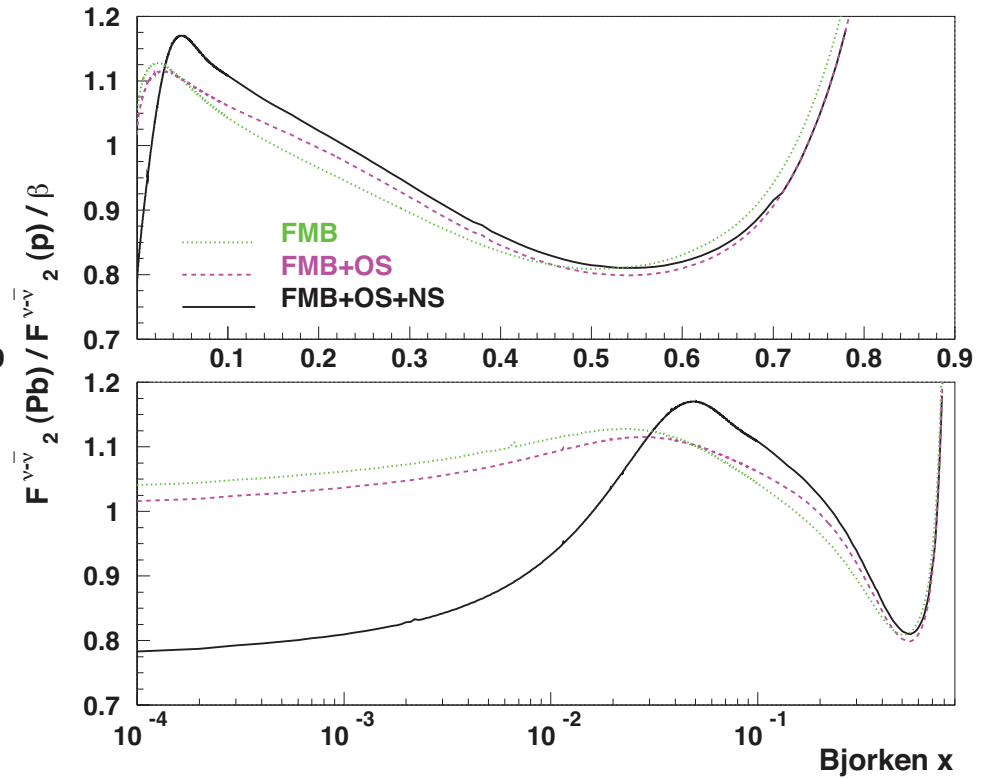
- ◆ Availability of ν -H & $\bar{\nu}$ -H allows direct measurement of nuclear modifications of $F_{2,3}$:

$$R_A \stackrel{\text{def}}{=} \frac{2F_{2,3}^{\nu A}}{F_{2,3}^{\nu p} + F_{2,3}^{\nu \bar{p}}}(x, Q^2) = \frac{F_{2,3}^{\nu A}}{F_{2,3}^{\nu N}}$$

- Comparison with e/μ DIS results and nuclear models;
 - Study flavor dependence of nuclear modifications using ν & $\bar{\nu}$ (W^\pm/Z helicity, C-parity, Isospin);
 - Effect of the axial-vector current.
- ◆ Study nuclear modifications to parton distributions in a wide range of Q^2 and x .
 - ◆ Study non-perturbative contributions from High Twists, PCAC, etc. and quark-hadron duality in different structure functions $F_2, xF_3, R = F_L/F_T$.
 - ◆ Nuclear modifications of nucleon form factors e.g. using NC elastic, CC quasi-elastic and resonance production.
 - ◆ Coherent meson production off nuclei in CC & NC and diffractive physics.
- ⇒ Synergy with Heavy Ion and EIC physics programs for cold nuclear matter effects.

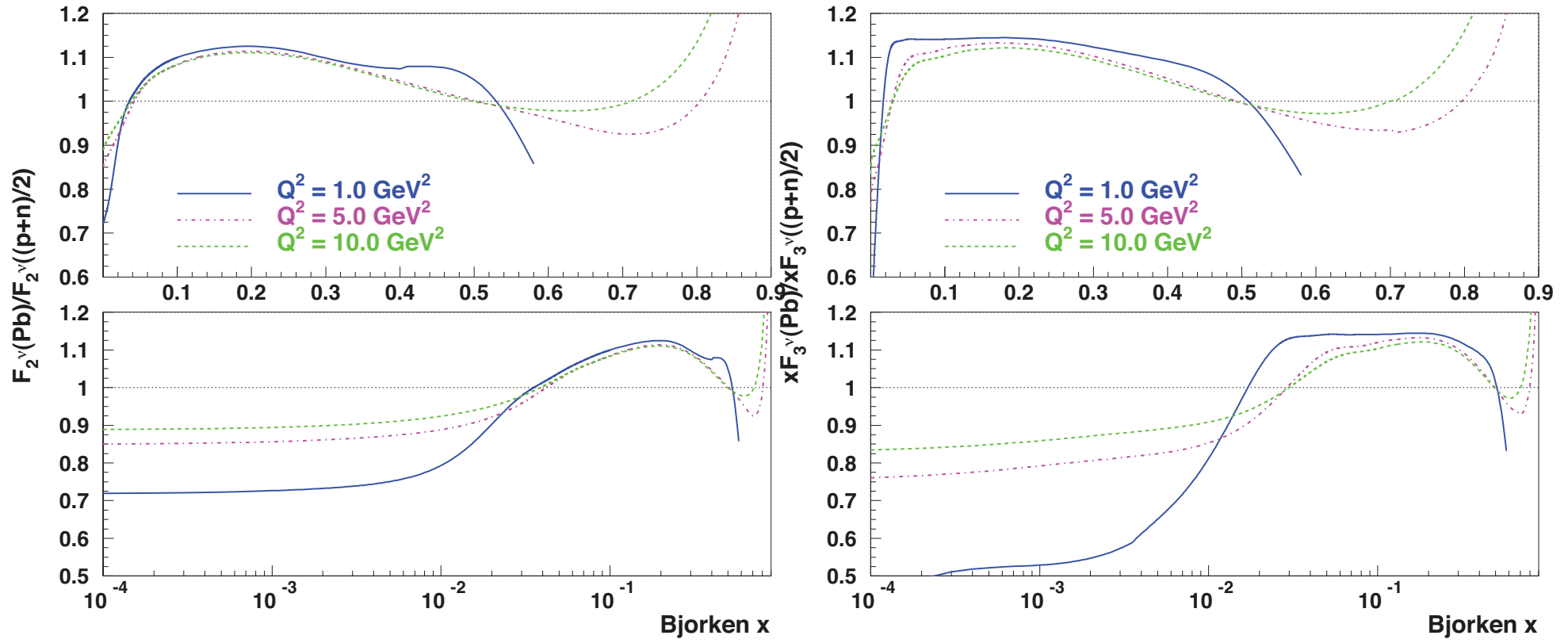


$$\frac{1}{A} F_2^{(\nu+\bar{\nu})A} / F_2^{(\nu+\bar{\nu})p} \text{ for } ^{207}\text{Pb} \\ \text{at } Q^2 = 5 \text{ GeV}^2$$



$$\frac{1}{A} F_2^{(\nu-\bar{\nu})A} / (\beta F_2^{(\nu-\bar{\nu})p}) \text{ for Pb, } Q^2 = 5 \text{ GeV}^2 \\ \beta = (Z - N)/A$$

S. Kulagin and R.P., NPA 765 (2006) 126; PRD 76 (2007) 094023, PRC 90 (2014) 045204



Ratio of Charged Current structure functions on ^{207}Pb and isoscalar nucleon $(p+n)/2$

S. Kulagin and R.P., NPA 765 (2006) 126; PRD 76 (2007) 094023, PRC 90 (2014) 045204

- ◆ Neutrino scattering is characterized by an **AXIAL-VECTOR CURRENT** in addition to the the Vector current.

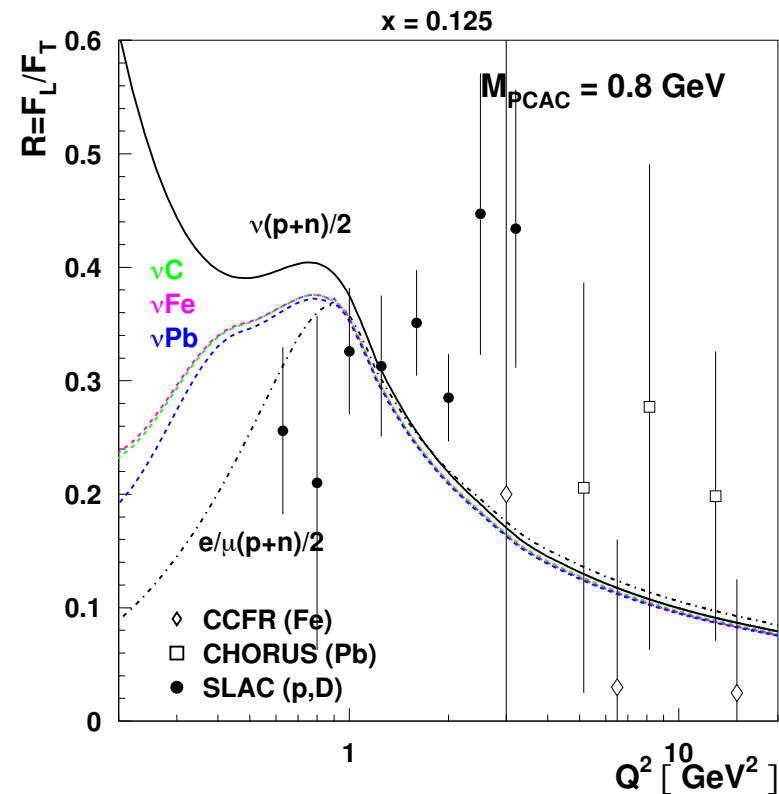
- ◆ Axial Current is only Partially Conserved (PCAC) and dominates SFs at low Q^2 :

$$F_2 \rightarrow F_L = \frac{f_\pi^2 \sigma_\pi}{\pi} \quad Q^2 \rightarrow 0$$

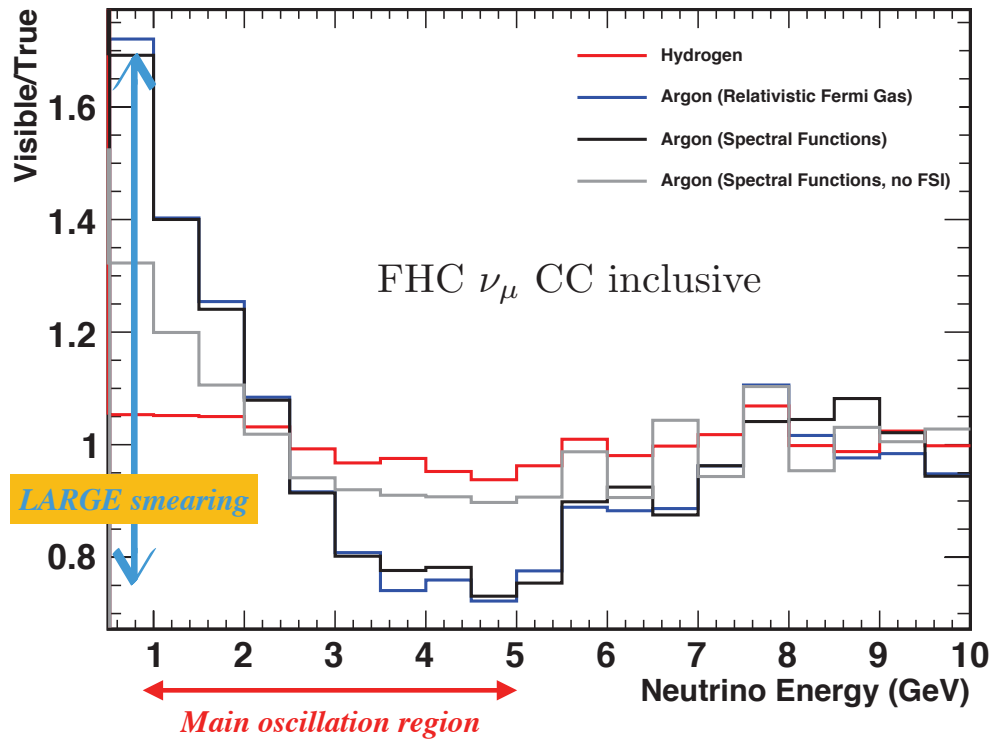
- ◆ The finite PCAC contribution to F_L strongly affects the asymptotic behaviour of **$R = \sigma_L/\sigma_T$** for $Q^2 \rightarrow 0$:

$$F_T \sim Q^2 \quad F_L \sim \frac{f_\pi^2 \sigma_\pi}{\pi} > 0$$

⇒ Substantial difference with respect to charged lepton scattering.



S. Kulagin and R.P., PRD 76 (2007) 094023



*Comparing Ar and H measurements
imposes stringent constraints
on the nuclear smearing in Ar*

*Understanding of nuclear smearing (response function for unfolding)
crucial for systematics in DUNE oscillation analyses*

- ◆ Extraction of $\sin^2 \theta_W$ from νN DIS sensitive to violations of isospin symmetry in nucleon, $u_{p(n)} \neq d_{n(p)}$. Measure ν AND $\bar{\nu}$ on **H AND C TARGETS**:

$$R_{2,3}^H \stackrel{\text{def}}{=} \frac{F_{2,3}^{\bar{\nu}p}}{F_{2,3}^{\nu p}}(x, Q^2) = \frac{F_{2,3}^{\nu n}}{F_{2,3}^{\nu p}}; \quad R_{2,3}^C \stackrel{\text{def}}{=} \frac{F_{2,3}^{\bar{\nu}C}}{F_{2,3}^{\nu C}}(x, Q^2) - 1 = \frac{\Delta F_{2,3}^{\bar{\nu}-\nu}}{F_{2,3}^{\nu}}$$

- Structure function ratio reduces systematic uncertainties;
 - Need to take into account *charm quark effects* $\propto \sin^2 \theta_C$. Sensitivity to m_c ;
 - A non-vanishing *strange sea asymmetry* $s(x) - \bar{s}(x)$ would affect the result.
Need combined analysis with charm production in ν and $\bar{\nu}$ interactions;
 - Potential effect of nuclear environment e.g. with Coulomb field.
- ◆ Collect ν and $\bar{\nu}$ interactions on both **Ca AND Ar TARGETS** to *disentangle nuclear effects from isospin effects* in nucleon structure functions.
- Measure ratios $R_{2,3}^A = \Delta F_{2,3}^{(\bar{\nu}-\nu)A} / F_{2,3}^{\nu A}(x, Q^2)$;
 - Use heavier isoscalar target, ${}^{20}_{40}\text{Ca}$, to verify nuclear effects in ${}^6_{12}\text{C}$;
 - Use second target with isovector component but same A as Ca: ${}^{18}_{40}\text{Ar}$.

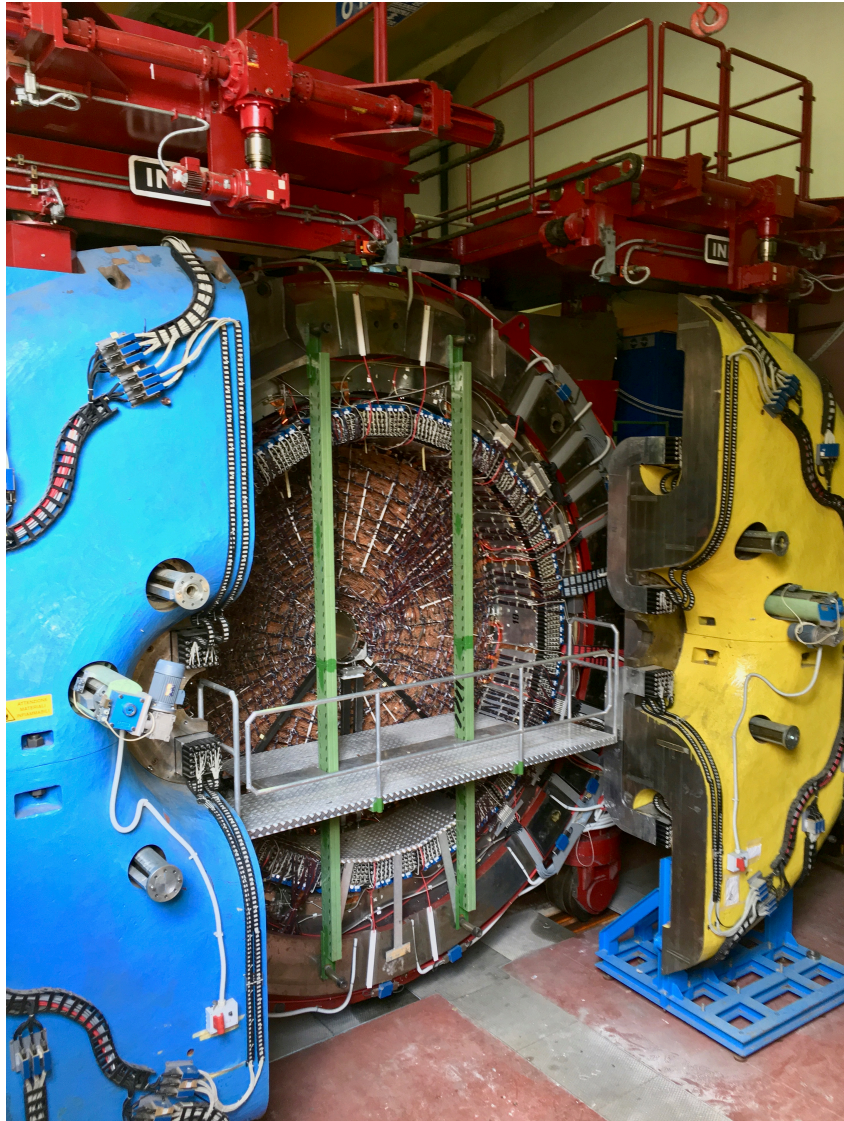
- ◆ *The intensity and $\nu(\bar{\nu})$ spectra available at the LBNF offer a unique opportunity for neutrino physics, if coupled with a high resolution ND of a few tons*
- ◆ *Possible to achieve a control of configuration, material & mass of neutrino targets similar to electron experiments & use a suite of various target materials.*
- ◆ *A novel technique can provide high statistics $\mathcal{O}(10^6)$ samples of $\nu(\bar{\nu})$ -hydrogen interactions, allowing *precisions in the measurement of ν & $\bar{\nu}$ fluxes $< 1\%$.**
- ◆ *Turn the DUNE ND site into a general purpose ν & $\bar{\nu}$ physics facility with broad program complementary to ongoing fixed-target, collider and nuclear physics efforts*

European Particle Physics Strategy Update 2018-2020:

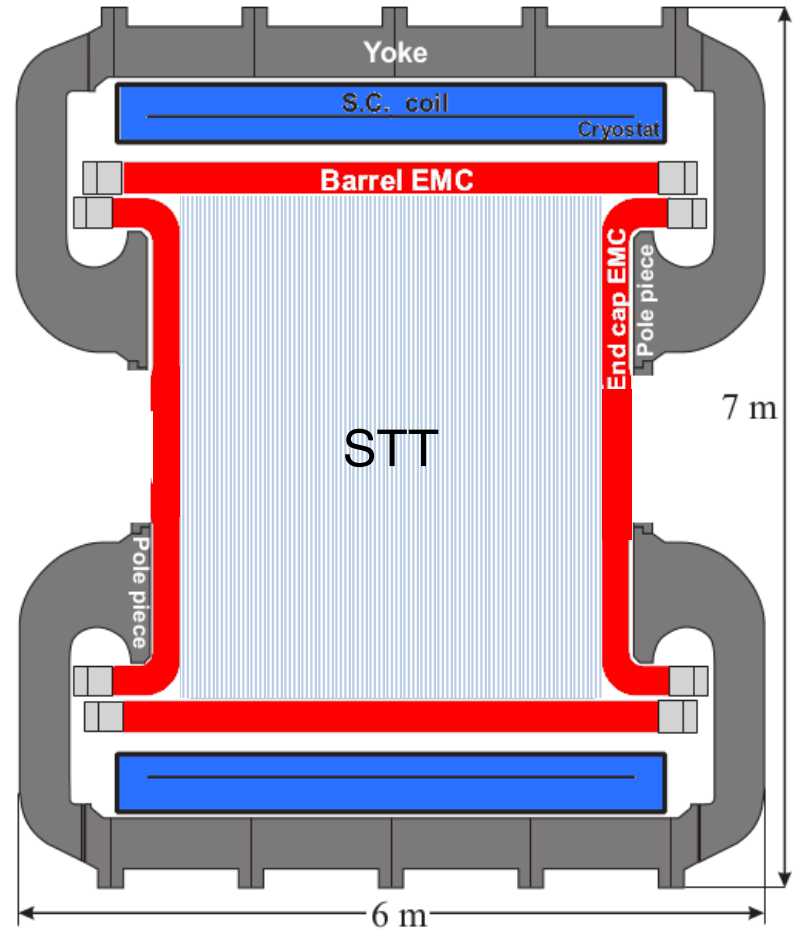
<https://indico.cern.ch/event/765096/contributions/3295805/>

⇒ Discovery potential & hundreds of diverse physics topics

Photo from workshop in Frascati, March 2019



Reuse existing KLOE magnet + ECAL and fill it with STT & nuclear targets



A Proposal to enhance the DUNE Near-Detector Complex

G. Adamov^{1,10}, L. Alvarez Ruso², I. Bagaturia¹, P. Bernardini^{3,4}, S. Bertolucci^{5,6},
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 N. Tsverava^{1,10}, and S. Zucchelli^{5,6}

Currently 74 physicists from 23 institutions and 7 countries

- ◆ *The intensity and $\nu(\bar{\nu})$ spectra available at the LBNF offer a unique opportunity for neutrino physics, if coupled with a high resolution ND of a few tons*
- ◆ *Possible to achieve a control of configuration, material & mass of neutrino targets similar to electron experiments & use a suite of various target materials.*
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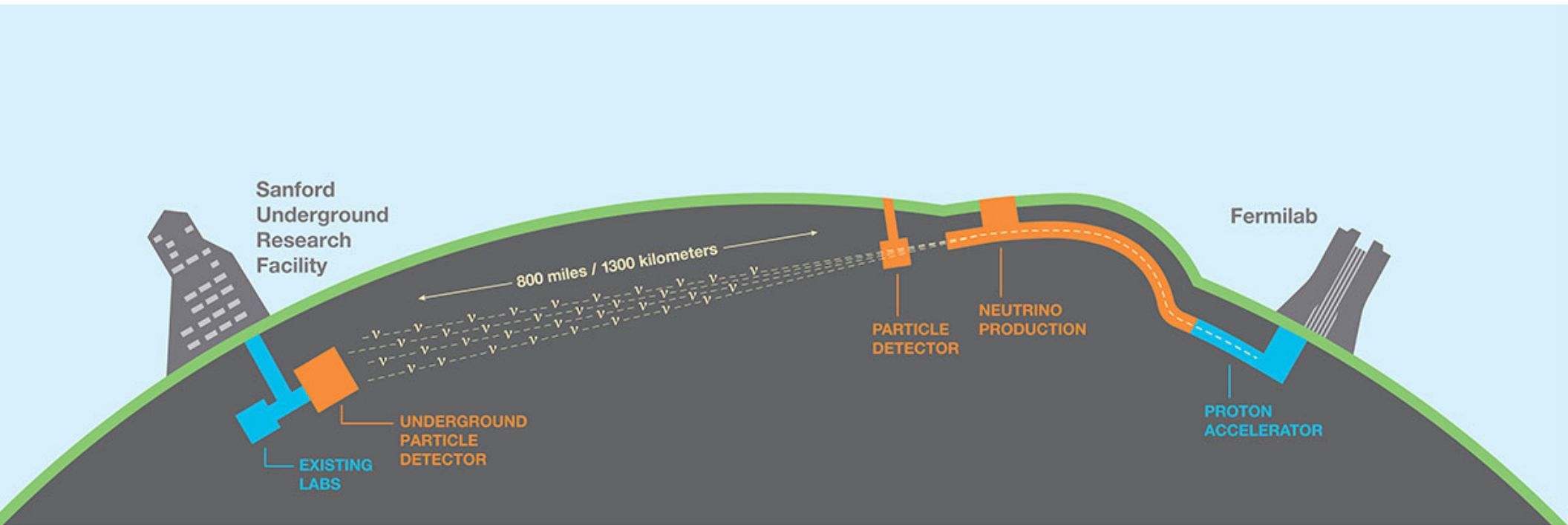
European Particle Physics Strategy Update 2018-2020:

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⇒ Discovery potential & hundreds of diverse physics topics

Looking for suggestions, feedback and/or potential interest

Backup slides



LBNF: Long-Baseline Neutrino Facility

DUNE: Deep Underground Neutrino Experiment

Process	ν_{μ} -H CC				$\bar{\nu}_{\mu}$ -H CC					
	$\mu^- p\pi^+$	$\mu^- p\pi^+ X$	$\mu^- n\pi^+\pi^+ X$	Inclusive	$\mu^+ p\pi^-$	$\mu^+ n\pi^0$	$\mu^+ n$	$\mu^+ p\pi^- X$	$\mu^+ n\pi\pi X$	Inclusive
Eff. ε	96%	89%	75%	93%	94%	84%	75%	85%	82%	80%
Purity	95%	93%	70%	93%	95%	84%	80%	94%	84%	84%

TABLE I. Efficiency ε and purity for the kinematic selection of H interactions from the CH₂ plastic target using the likelihood ratio $\ln \lambda^H + \ln \lambda_{\text{IN}}^H$ or $\ln \lambda_4^H + \ln \lambda_{\text{IN}}^H$. For the $\mu^+ n$ QE topologies $\ln \lambda_{\text{QE}}^H$ is used instead. The cuts applied for each channel are chosen to maximize the sensitivity defined as $S/\sqrt{S+B}$, where S is the H signal and B the C background. The CC inclusive samples are obtained from the combination of the corresponding exclusive channels.

Process	ν_{μ} -H CC, $\varepsilon \equiv 75\%$				$\bar{\nu}_{\mu}$ -H CC, $\varepsilon \equiv 75\%$					
	$\mu^- p\pi^+$	$\mu^- p\pi^+ X$	$\mu^- n\pi^+\pi^+ X$	Inclusive	$\mu^+ p\pi^-$	$\mu^+ n\pi^0$	$\mu^+ n$	$\mu^+ p\pi^- X$	$\mu^+ n\pi\pi X$	Inclusive
Purity	99%	99%	70%	98%	99%	90%	80%	98%	90%	86%

TABLE II. Purity achieved with the kinematic selection of H interactions from the CH₂ plastic target using a cut on the likelihood ratio $\ln \lambda^H + \ln \lambda_{\text{IN}}^H$ or $\ln \lambda_4^H + \ln \lambda_{\text{IN}}^H$ resulting in the fixed H signal efficiency ε specified. For the $\mu^+ n$ QE topologies $\ln \lambda_{\text{QE}}^H$ is used instead. For illustration purpose, the value of the efficiency is chosen as the lowest among the ones listed in Tab. I for individual topologies. The CC inclusive samples are obtained from the combination of the corresponding exclusive channels.

STRANGENESS CONTENT OF NUCLEON

- ◆ **NC ELASTIC SCATTERING** neutrino-nucleus is sensitive to the *strange quark contribution to nucleon spin, Δs* , through axial-vector form factor G_1 :

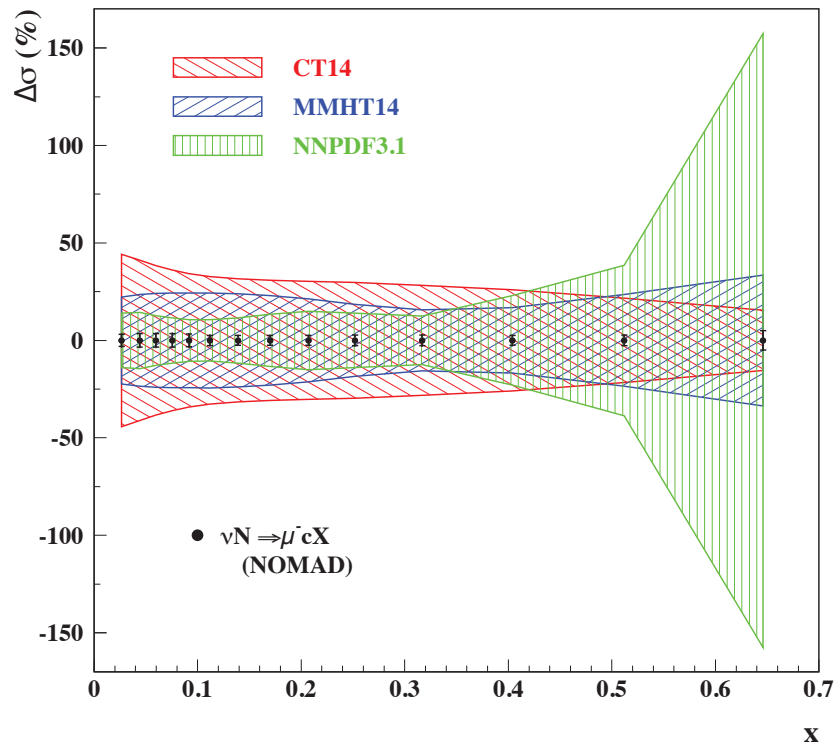
$$G_1 = \left[-\frac{G_A}{2} \tau_z + \frac{G_A^s}{2} \right]$$

At $Q^2 \rightarrow 0$ we have $d\sigma/dQ^2 \propto G_1^2$ and the *strange axial form factor $G_A^s \rightarrow \Delta s$* .

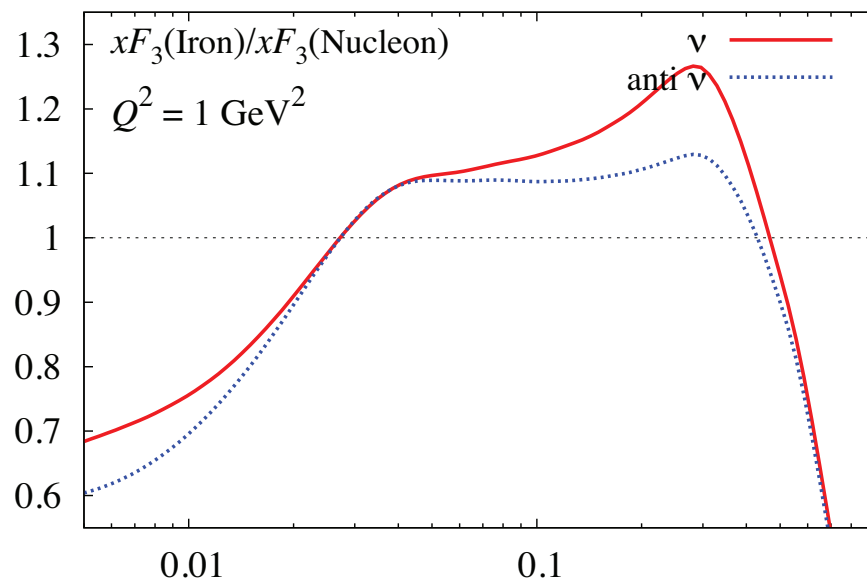
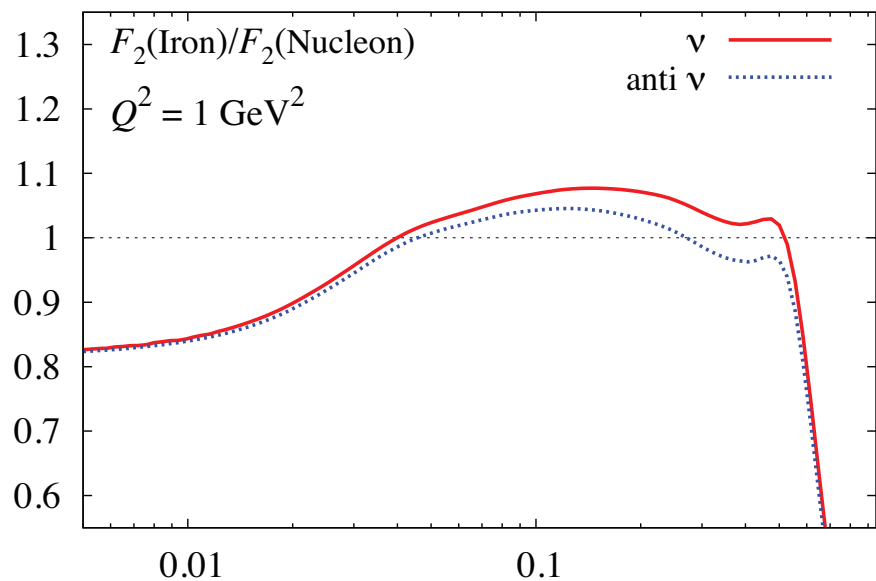
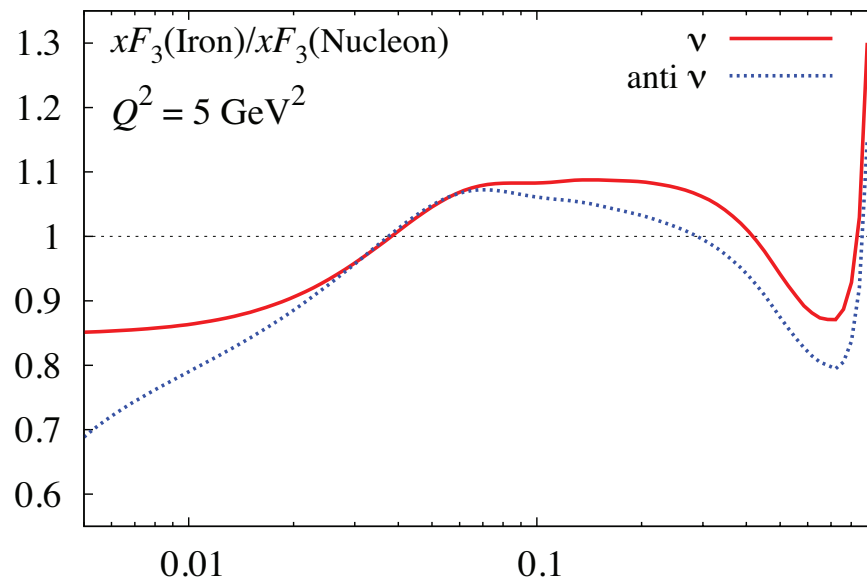
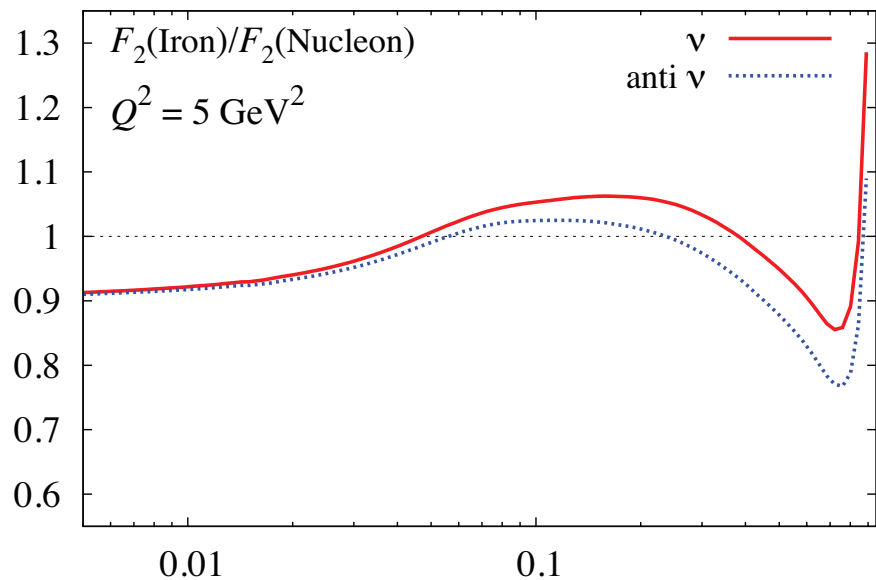
- ◆ Measure **NC/CC RATIOS** as a function of Q^2 to reduce systematics ($\sin^2 \theta_W$ as well):

$$R_\nu = \frac{\sigma(\nu p \rightarrow \nu p)}{\sigma(\nu n \rightarrow \mu^- p)}; \quad R_{\bar{\nu}} = \frac{\sigma(\bar{\nu} p \rightarrow \bar{\nu} p)}{\sigma(\bar{\nu} p \rightarrow \mu^+ n)}$$

- Compare axial current charge radius r_A^2 with muon capture in muonic hydrogen (discrepancies);
 - Expect $\sim 2 \times 10^6$ ν NC and $\sim 1 \times 10^6$ $\bar{\nu}$ NC events (BNL E734: 951 νp and 776 $\bar{\nu} p$);
 - Precision measurement over an extended Q^2 range reduces systematic uncertainties from the Q^2 dependence of vector ($F_{1,2}^s$) and axial (G_A^s) strange form factors.
- ◆ *Direct probe of $s(x)$ & $\bar{s}(x)$ content of nucleon from charm production in both dilepton ($\sim 100k$ $\mu\mu$ & μe) and exclusive charmed hadrons (e.g. D^{*+} , D_s , Λ_c).*



- ◆ *NOMAD measurement allows reduction of $s(x)$ uncertainty down to $\sim 3\%$:*
 $\kappa_s = \int_0^1 x(s + \bar{s})dx / \int_0^1 x(\bar{u} + \bar{d})dx = 0.591 \pm 0.019$ (NPB 876 (2013) 339)
- ◆ *Improved determination of the \overline{MS} mass from global PDF fits:*
 $m_c(m_c) = 1.252 \pm 0.018 \pm 0.010(QCD)$ (S. Alekhin et al., PRD 96 (2017) 014011)
- ◆ *Recent ATLAS claims of enhanced $s(x)$ seems related to overconstrained PDF parameterization* (S. Alekhin et al., PLB 777 (2018) 134, PRD 91 (2015) 094002)



HELICITY, C-PARITY AND ISOSPIN

- ◆ The amplitude controlling nuclear shadowing depends on the helicity of boson ($\pm 1, 0$)

$$a_0 \rightarrow F_L$$

$$a_T = (a_{+1} + a_{-1})/2 \rightarrow F_1$$

$$a_\Delta = (a_{+1} - a_{-1})/2 \rightarrow F_3$$

- ◆ The amplitude depends on the isospin I (proton and neutron dependence) and on the

C -parity (ν and $\bar{\nu}$ dependence), $a_h^{(I,C)}$:

$$a_T^{(0,+)} \rightarrow F_1^{e/\mu(p+n)} \text{ and } F_1^{(\nu+\bar{\nu})(p+n)}$$

$$a_T^{(1,+)} \rightarrow F_1^{e/\mu(p-n)} \text{ and } F_1^{(\nu+\bar{\nu})(p-n)}$$

$$a_T^{(0,-)} \rightarrow F_1^{(\nu-\bar{\nu})(p+n)}$$

$$a_T^{(1,-)} \rightarrow F_1^{(\nu-\bar{\nu})(p-n)}$$

$$a_\Delta^{(0,-)} \rightarrow F_3^{(\nu+\bar{\nu})(p+n)}$$

$$a_\Delta^{(1,-)} \rightarrow F_3^{(\nu+\bar{\nu})(p-n)}$$

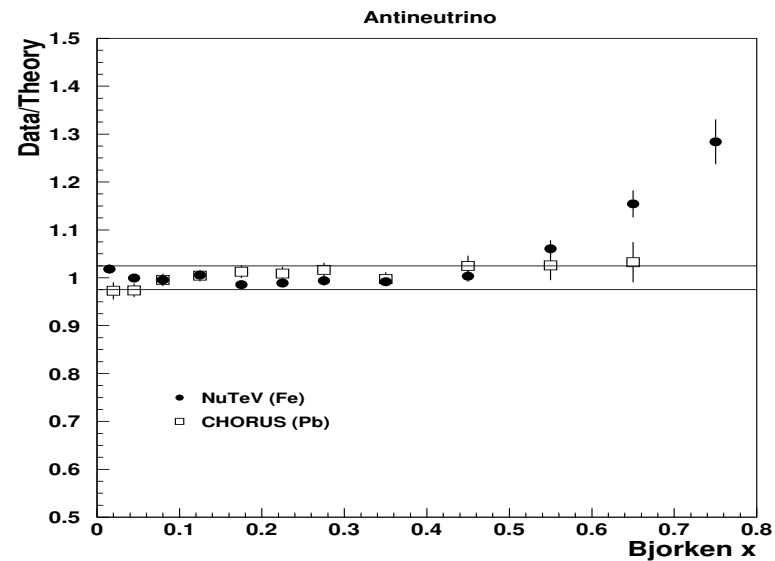
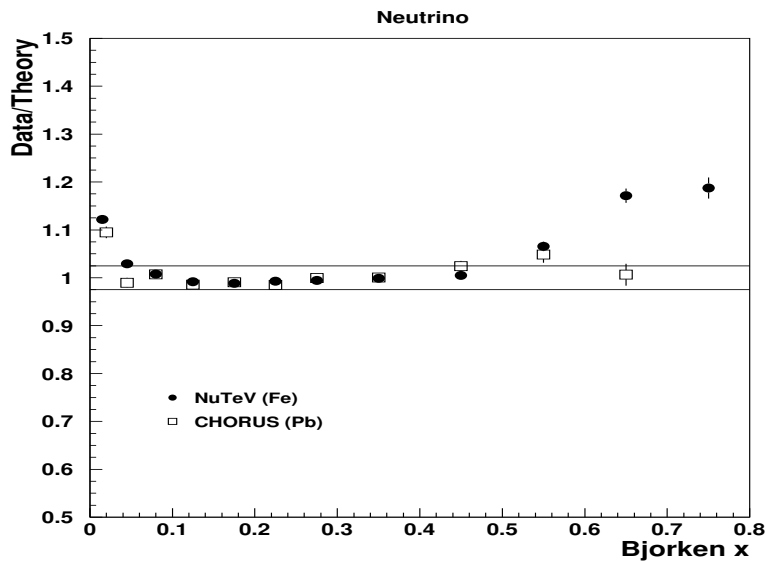
$$a_\Delta^{(0,+)} \rightarrow F_3^{(\nu-\bar{\nu})(p+n)}$$

$$a_\Delta^{(1,+)} \rightarrow F_3^{(\nu-\bar{\nu})(p-n)}$$

\implies Virtual photon γ^* C -even only, (anti)neutrino interactions both C -even and C -odd

- ◆ Isoscalar and Iovector spectral functions, \mathcal{P}_0 and \mathcal{P}_1 , enter nuclear convolution

$$F_2^A/A = \left\langle \frac{F_2^p + F_2^n}{2} \right\rangle_0 + \frac{\beta}{2} \langle F_2^p - F_2^n \rangle_1 \quad \beta = (Z - N)/A$$



- ◆ Limited $\nu(\bar{\nu})$ data on ratios $\sigma^{A'}/\sigma^A$ (BEBC, MINER ν A) and differential cross-sections $d\sigma^2/dx dy$ (NuTeV, CCFR, CHORUS)
- ◆ Model predictions agree with data in the bulk of phase space but show discrepancies at $x < 0.05$ and $x > 0.5$ (S. Kulagin and R.P., NPA 765 (2006) 126; PRD 76 (2007) 094023).
 \implies Need new precision measurements with both ν AND $\bar{\nu}$

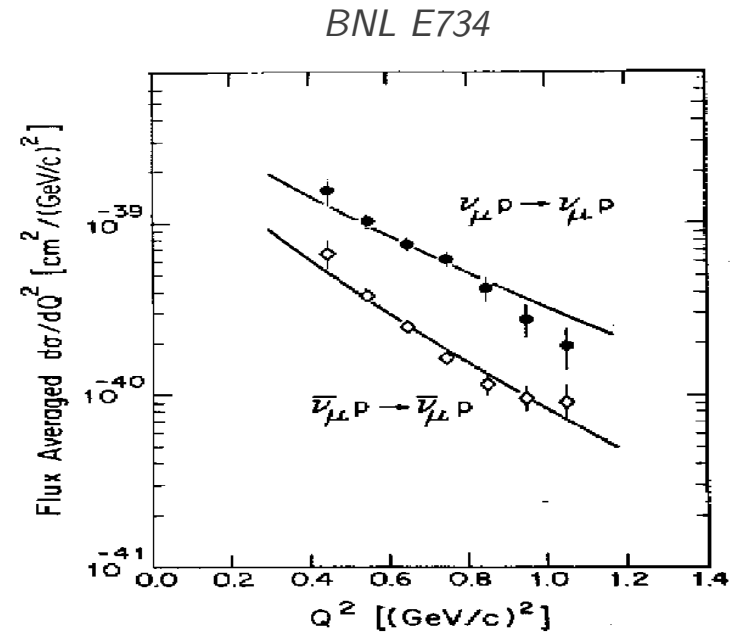
- ◆ Ratio of *NC elastic scattering neutrino-nucleus* to CC quasi-elastic scattering for both ν and $\bar{\nu}$ ($\sin^2 \theta_W$):

$$R_\nu = \frac{\sigma(\nu p \rightarrow \nu p)}{\sigma(\nu n \rightarrow \mu^- p)}; \quad R_{\bar{\nu}} = \frac{\sigma(\bar{\nu} p \rightarrow \bar{\nu} p)}{\sigma(\bar{\nu} p \rightarrow \mu^+ n)}$$

Determine axial form factor G_A from the CC sample.

- Significant reduction of systematics from NC/CC ratios.
- Estimate Q^2 values in NC from 2-body kinematics;
- $\sin^2 \theta_W$ sensitivity in vector $F_{1,2}$ form factors.

⇒ Systematics from FF, neutrons, nuclear effects?



- ◆ Additional sensitivity from the *NC/CC ratio of coherent ρ meson production*:

$$R_\rho = \frac{\sigma(\nu_\mu A \rightarrow \nu_\mu \rho^0 A)}{\sigma(\nu_\mu A \rightarrow \mu^- \rho^+ A)} = \frac{1}{2} (1 - 2 \sin^2 \theta_W)^2$$

expect ~ 30k coherent ρ⁰ and 200k coherent ρ⁺ in ND.

⇒ Systematics from background subtraction in the coherent ρ⁰ selection?