

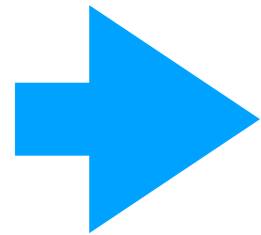
*Muon Collider - Preparatory Meeting  
CERN, 10-11 April 2019*

# WHEN MUONS

# COLLIDE

*Less Obvious Physics  
at the Muon Collider*

our "reference frame"



$\sqrt{S}_{\mu\mu} \sim 10, 14, 30 \text{ TeV}$

\* as envisaged in :

### Muon Colliders

#### The Muon Collider Working Group

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Muon colliders have a great potential for high-energy physics. They can offer collisions of point-like particles at very high energies, since muons can be accelerated in a ring without limitation from synchrotron radiation. However, the need for high luminosity faces technical challenges which arise from the short muon lifetime at rest and the difficulty of producing large numbers of muons in bunches with small emittance. Addressing these challenges requires the development of innovative concepts and demanding technologies.

The document summarizes the work done, the progress achieved and new recent ideas on muon colliders. A set of further studies and actions is also identified to advance in the field. Finally, a set of recommendations is listed in order to make the muon technology mature enough to be favourably considered as a candidate for high-energy facilities in the future.

Input to the European Particle Physics Strategy Update

arXiv:1901.06150v1 [physics.acc-ph] 18 Jan 2019

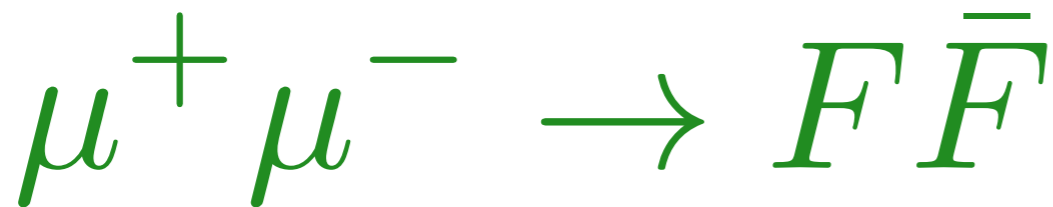
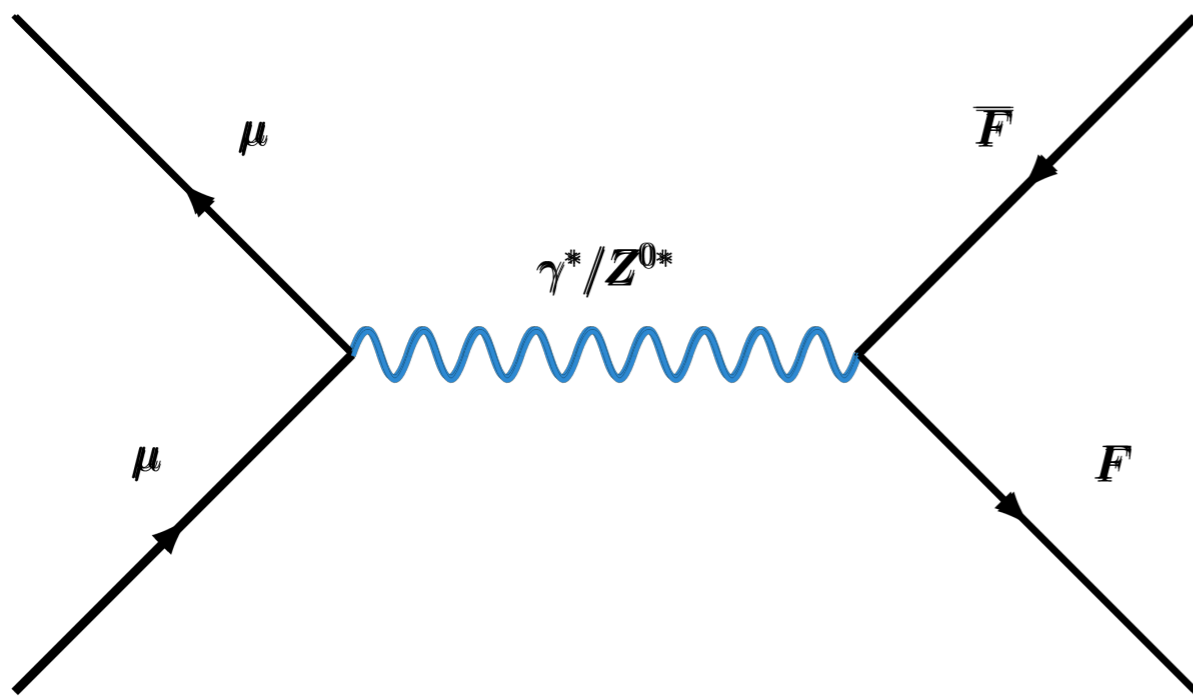
\* what can one do with muon collisions

@  $\sqrt{S_{\mu\mu}}$  up to a few tens of TeV ???

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@  $\sqrt{S_{\mu\mu}}$  up to a few tens of TeV ???

FIRST AND FOREMOST



\* plain pair production of new heavy states...

$$m_F \lesssim \sqrt{S_{\mu\mu}}/2$$

~ 5, 7, 15 TeV !!!

# → Luminosity ruled by heavy pair x-section

rate for new p.le pair production :

$$\sigma_{EW} \sim \sigma(\mu^+ \mu^- \rightarrow \gamma^* \rightarrow e^+ e^-) \sim \frac{4\pi\alpha^2}{3S}$$

point x-section

$$\rightarrow 1 \text{ fb} \left( \frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

no  $m_e$  dependence  
up to  $m_e \sim \sqrt{S}/2$  !

$$L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1} \sim 1 \text{ ab}^{-1} / \text{y}$$

$$\rightarrow 1000 \text{ evs/y} \left( \frac{10 \text{ TeV}}{\sqrt{S}} \right)^2$$

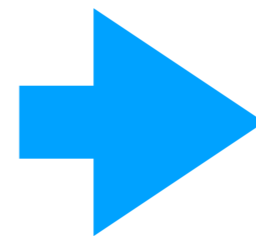
$$\sqrt{S}_{\mu\mu}$$

$$\int L_{10y}$$

$$10 \text{ TeV}$$

$$10 \text{ ab}^{-1}$$

$$10^4 \text{ evs} / (10 \text{ years})$$



$$14 \text{ TeV}$$

$$20 \text{ ab}^{-1}$$

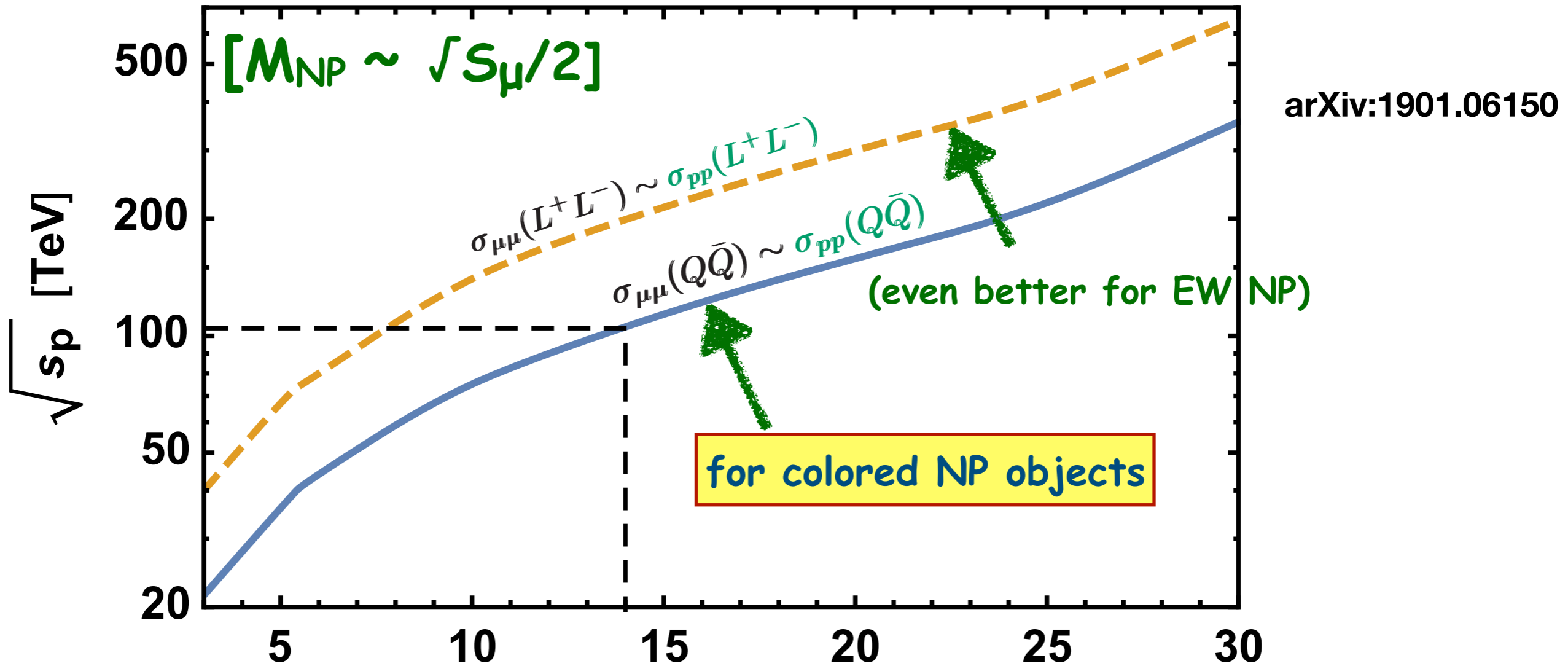
$$\delta_{\text{stat}} \sim 1\%$$

$$30 \text{ TeV}$$

$$100 \text{ ab}^{-1}$$

$$L \sim 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$$

# "equivalent" reach in pp after rescaling for pdf's



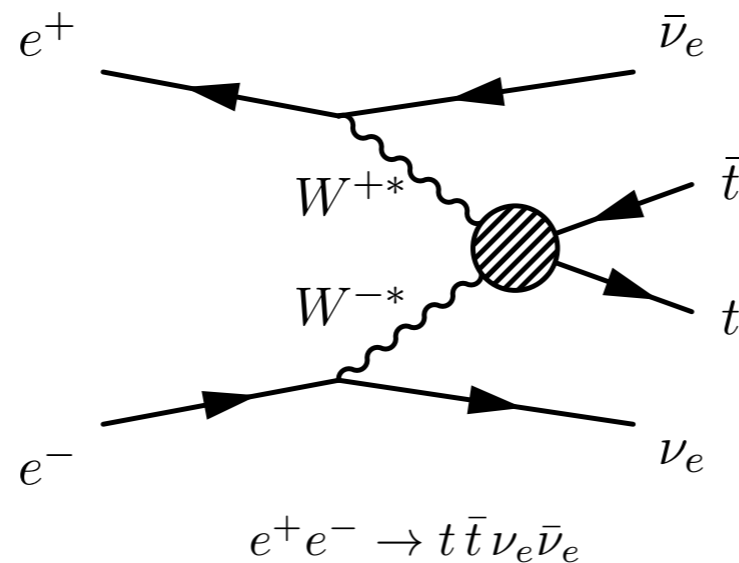
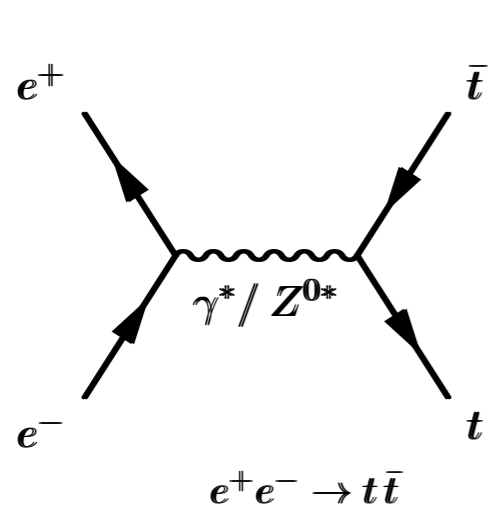
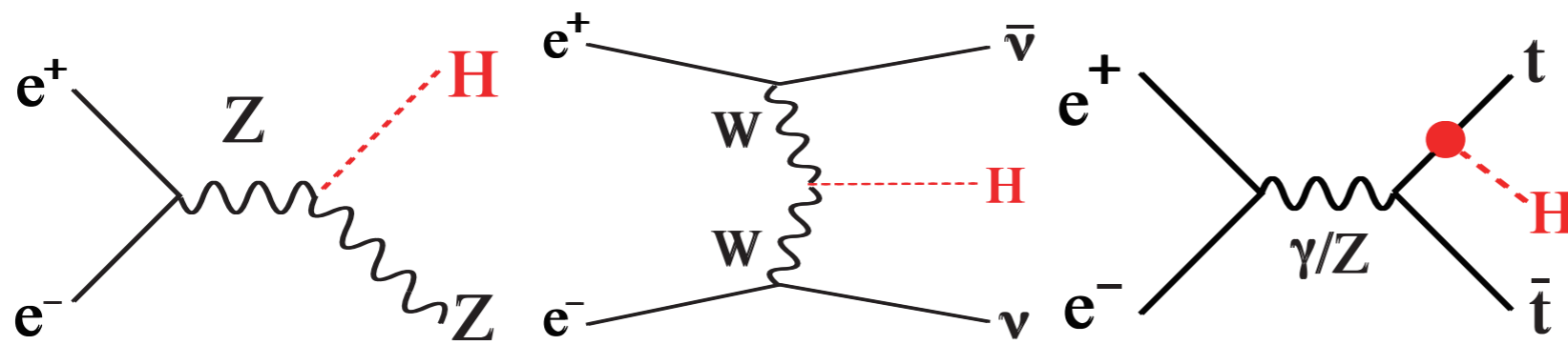
- \*  $\mu\mu$  @ 14 TeV  $\rightarrow$  pp @ 100 (200)<sub>EW</sub> TeV !
  - \*  $\mu\mu$  @ 30 TeV  $\rightarrow$  pp @ 350 (600)<sub>EW</sub> TeV !!
- yet unexplored pheno !!!*

# WHAT ELSE ?

# WHAT ELSE ?

\*  $\mu^+\mu^-$  scattering very similar to  $e^+e^-$  one  
 [apart from QED-radiation and (tiny !) Yukawa effects]

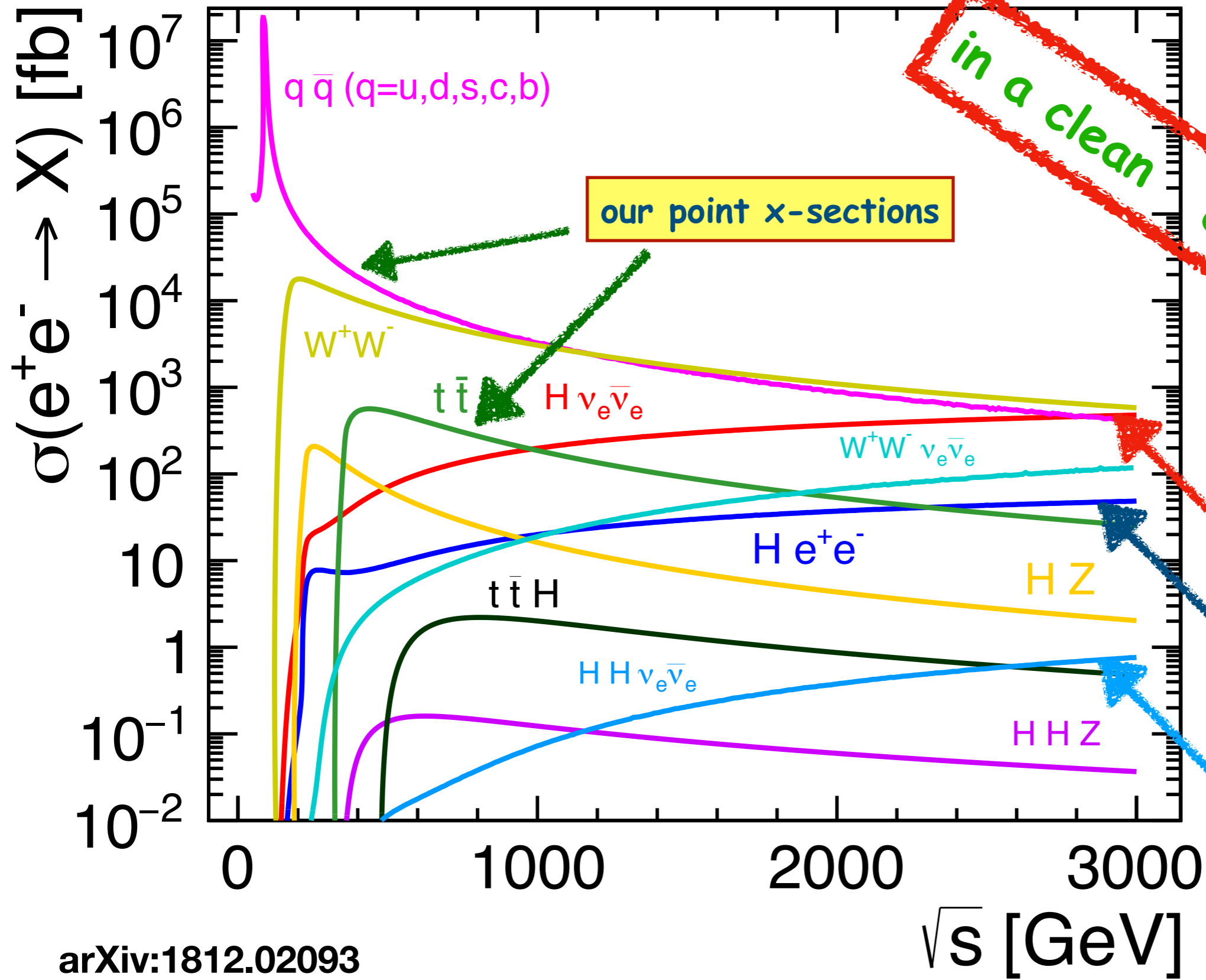
→ try and extrapolate CLIC studies @3TeV to higher  $\sqrt{S}$



$(e^+, e^-, \nu_e, \bar{\nu}_e)$   
 $\rightarrow (\mu^+, \mu^-, \nu_\mu, \bar{\nu}_\mu)$

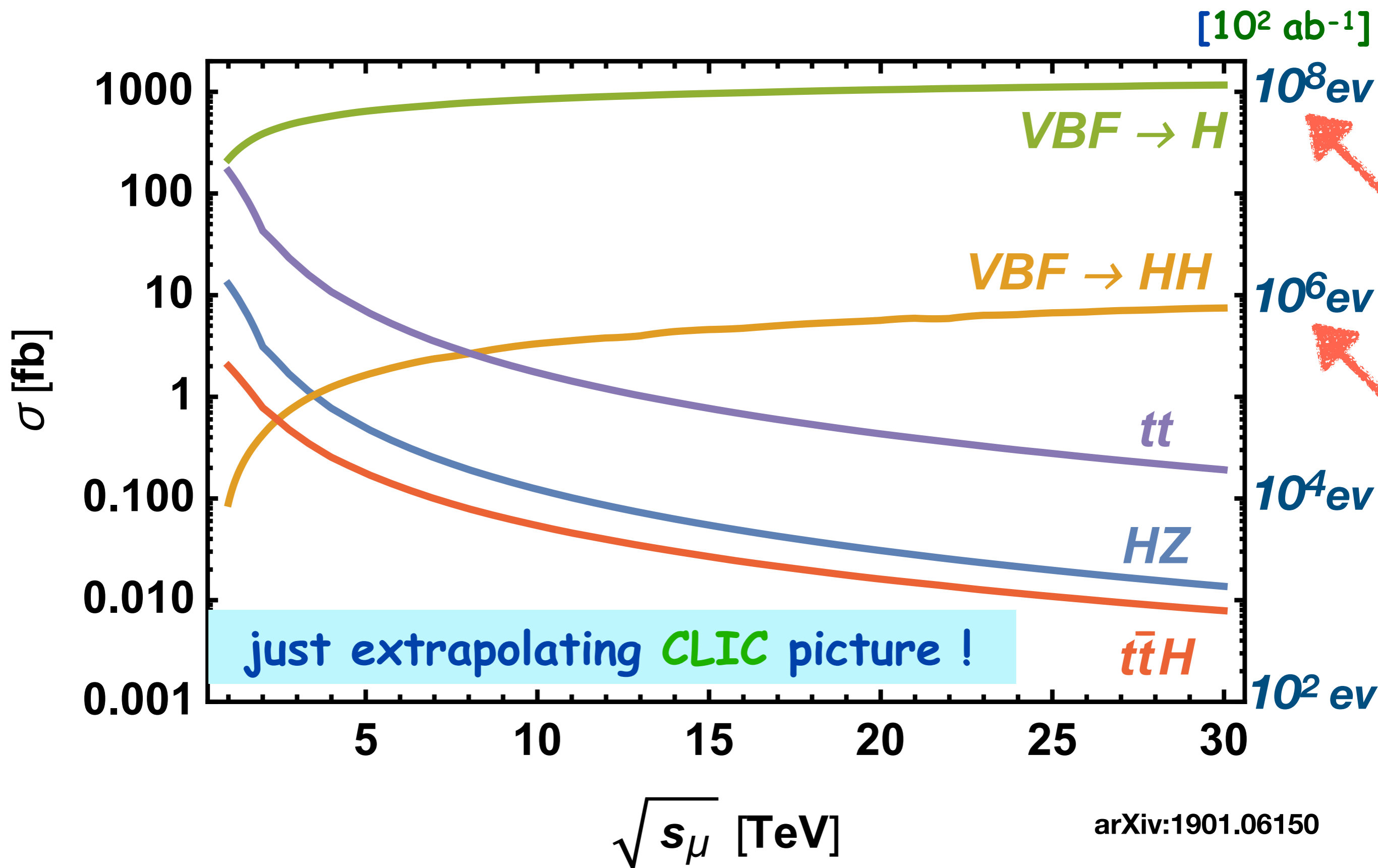


# point x-sections dominant at CLIC !

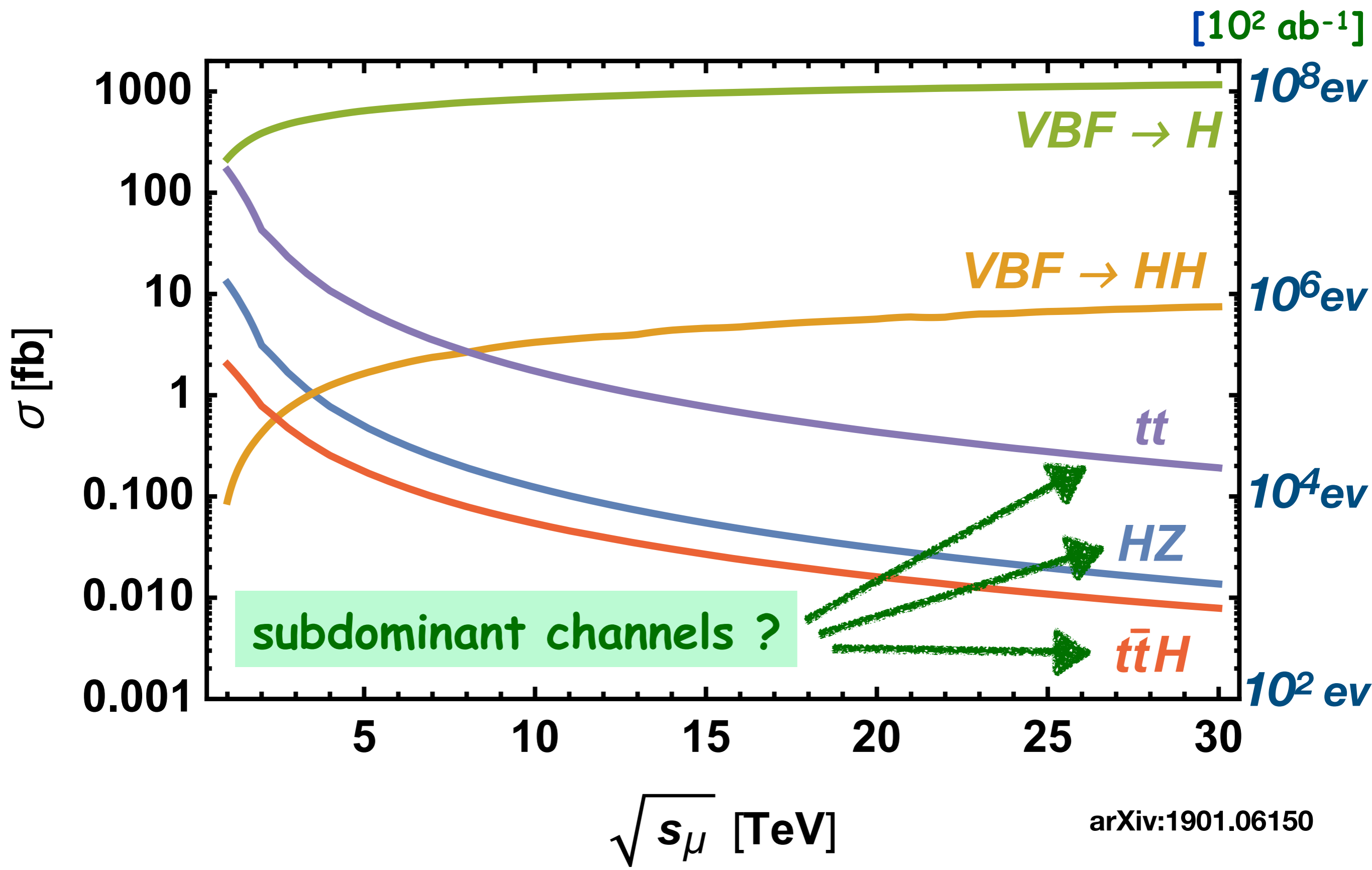


arXiv:1812.02093

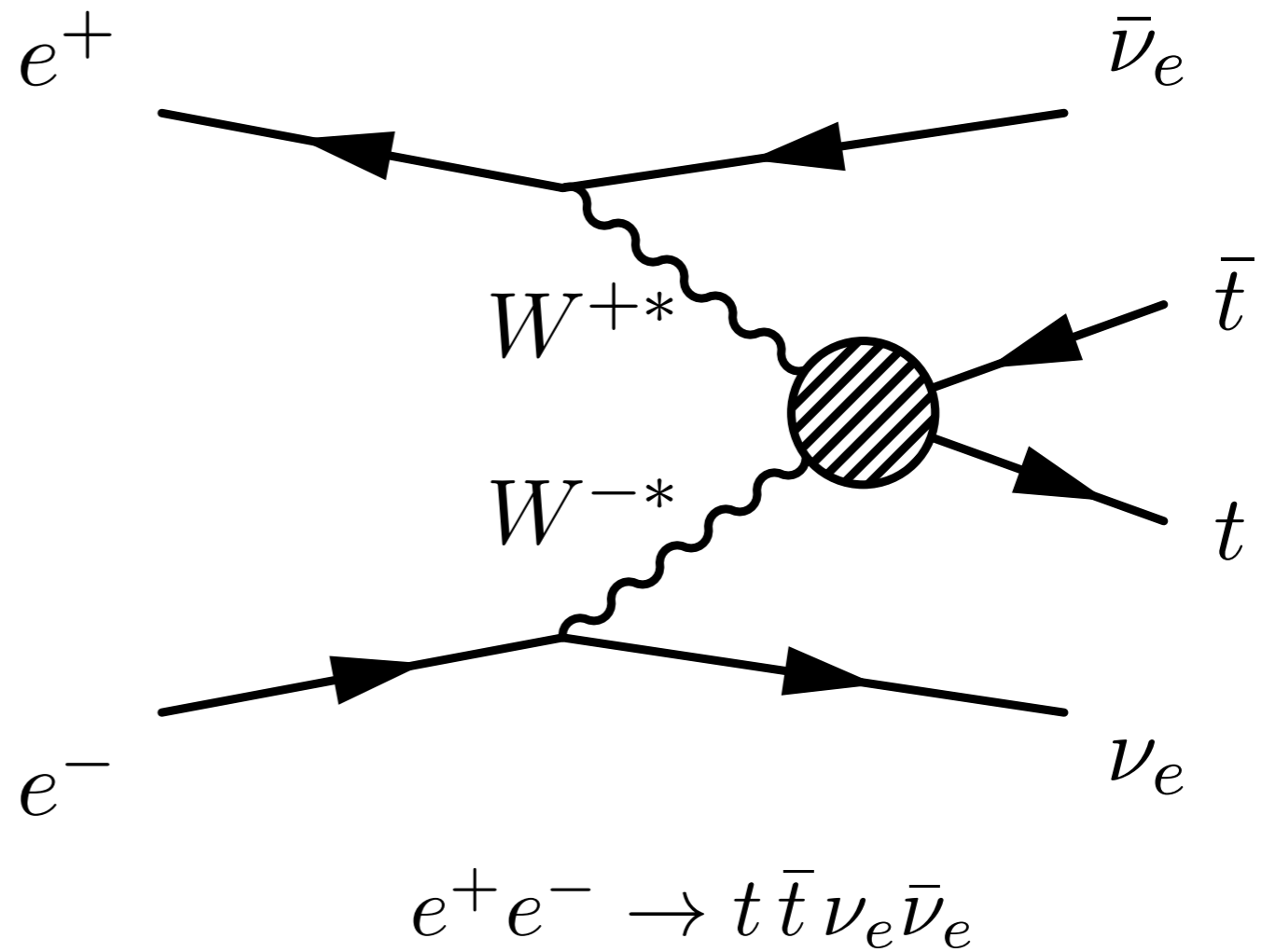
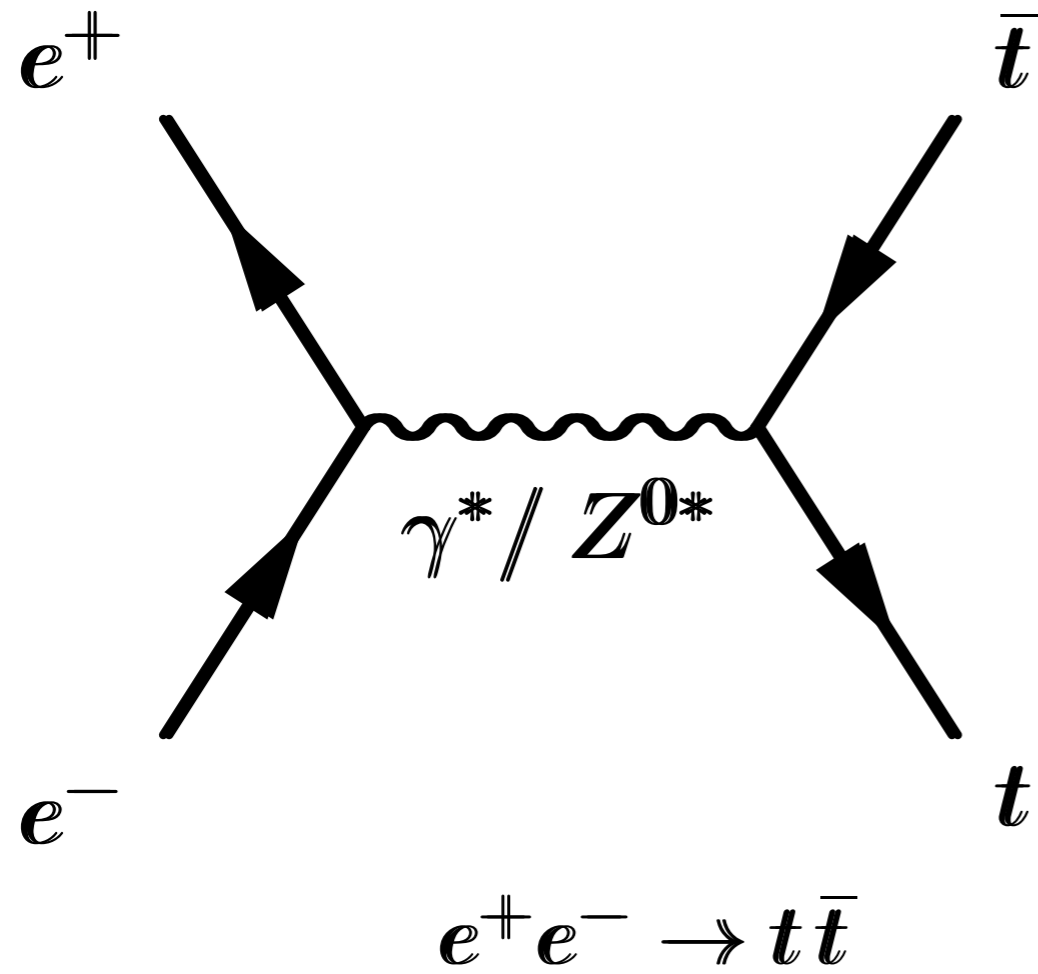
at  $\sqrt{s_{\mu\mu}} \sim 10-30 \text{ TeV}$  [ $L \sim 10^{1-2} \text{ ab}^{-1}$ ] plenty of Higgs's !



at  $\sqrt{s_{\mu\mu}} \sim 10-30 \text{ TeV}$  plenty of Higgs's with  $L \sim 10^{1-2} \text{ ab}^{-1}$

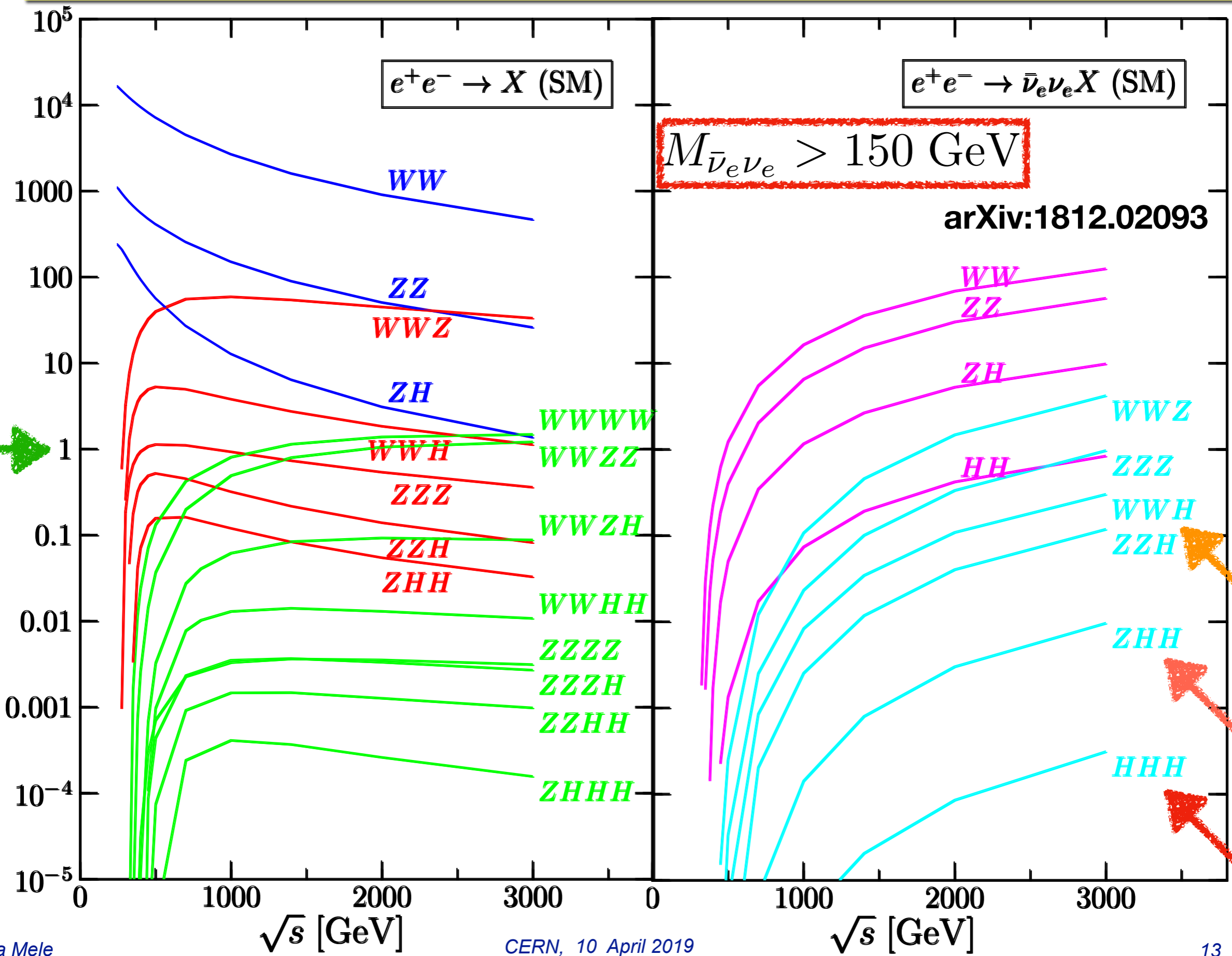


$\mu^+\mu^- \rightarrow X$  versus  $W^+W^- \rightarrow X$   $\nu\nu$

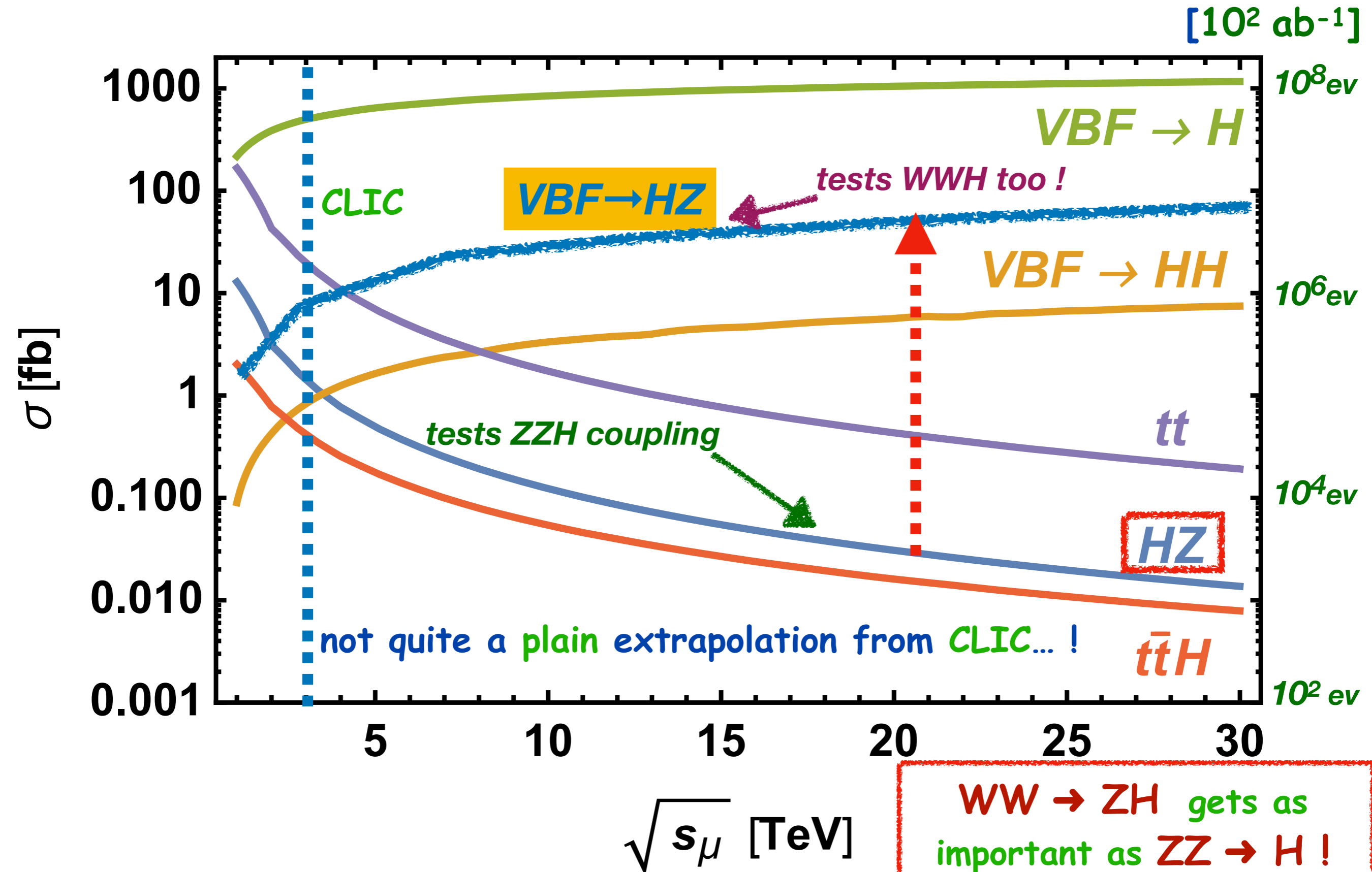


# $\ell^+\ell^- \rightarrow X$ versus $W^+W^- \rightarrow X$ @ CLIC

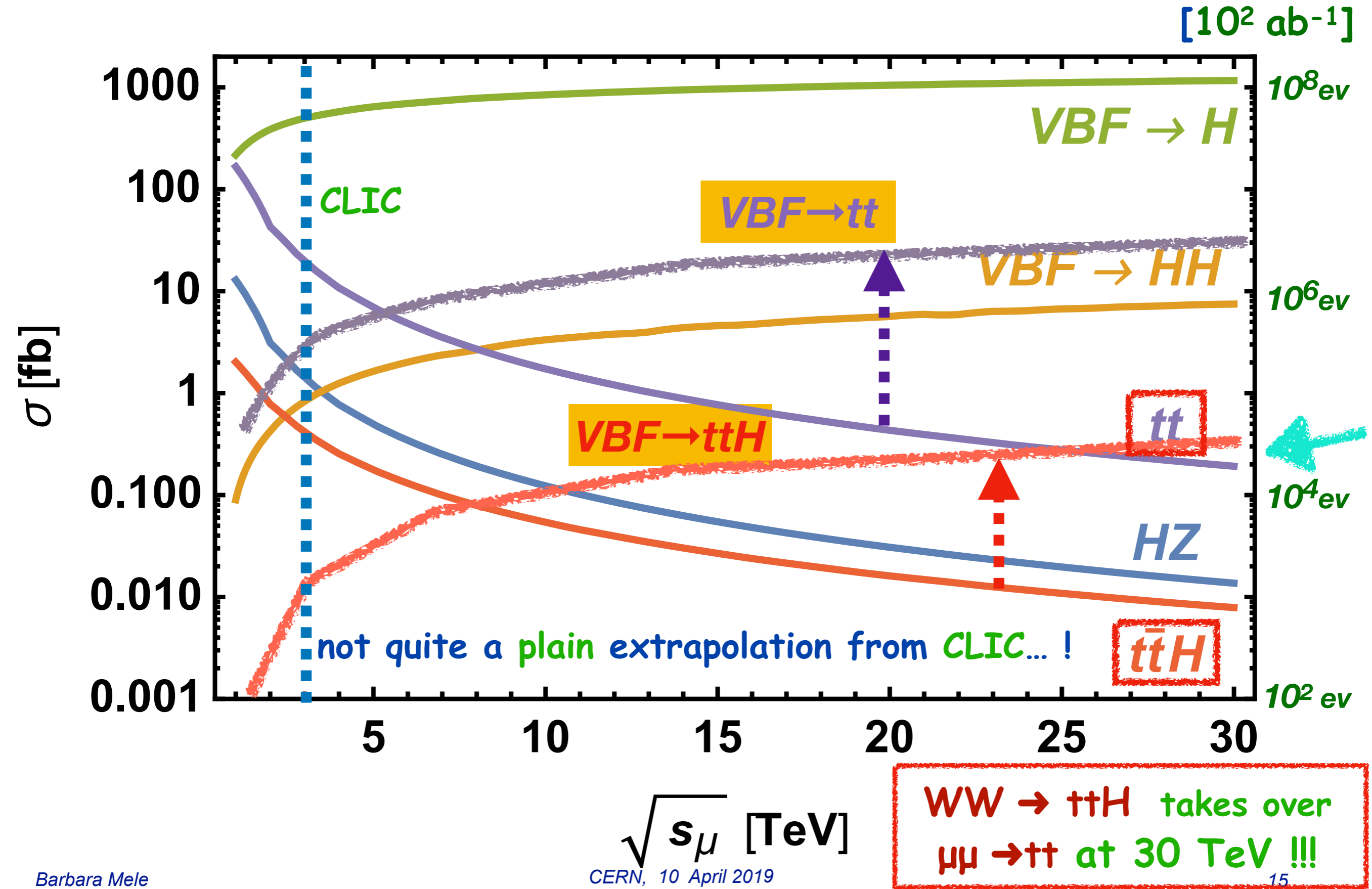
$\sigma$  [fb]



# $l^+l^- \rightarrow ZH$ vs $WW \rightarrow ZH$



# $\ell^+\ell^- \rightarrow tt (H)$ vs $WW \rightarrow tt (H)$



# # VBF events (green) + $\sigma_{WW \rightarrow X} / \sigma_{\mu\mu \rightarrow X}$ (red)

# events	3 TeV/5/ab	(VBF)/(s-ch)3TeV	14 TeV/20/ab	(VBF)/(s-ch)14TeV	30 TeV/100/ab	(VBF)/(s-ch)30TeV
<b>H</b>	2,5E+06		1,9E+07		1,2E+08	
<b>HZ</b>	4,9E+04	7	9,0E+05	700	7,4E+06	5300
<b>HZZ</b>	6,0E+02	1,5	3,2E+04	180	3,7E+05	1500
<b>HWW</b>	1,5E+03	0,3	6,8E+04	30	7,6E+05	190
<b>HH</b>	4,1E+03		8,8E+04		7,4E+05	
<b>HHZ</b>	4,7E+01	0,3	2,8E+03	40	3,3E+04	300
<b>HHZZ</b>	4,6E-01	0,1	7,8E+01	16	1,2E+03	130
<b>HHWW</b>	1,2E+00	0,02	1,8E+02	1	2,9E+03	1
<b>HHH</b>	1,5E+00		1,4E+02		1,9E+03	
<b>HHHZ</b>	2,4E-02	0,3	3,8E+00	12	5,1E+01	100

[MadGraph]

<b>tt</b>	2,6E+04	0,3	4,2E+05	24	3,1E+06	160
<b>ttH</b>	6,5E+01	0,03	3,0E+03	5	3,1E+04	40
<b>ttZ</b>	5,5E+02	0,07	2,6E+04	7	2,8E+05	50
<b>ttHH</b>	1,7E-01	0,006	1,3E+01	1	1,6E+02	10
<b>ttHZ</b>	1,8E+00	0,01	2,0E+02	2	2,7E+03	14
<b>ttZZ</b>	7,0E+00	0,03	1,2E+03	4	1,7E+04	30
<b>ttWW</b>	1,4E+01	0,008	2,2E+03	0,8	3,0E+04	5
<b>tttt</b>	3,4E-01	0,01	2,2E+01	0,4	2,1E+02	2



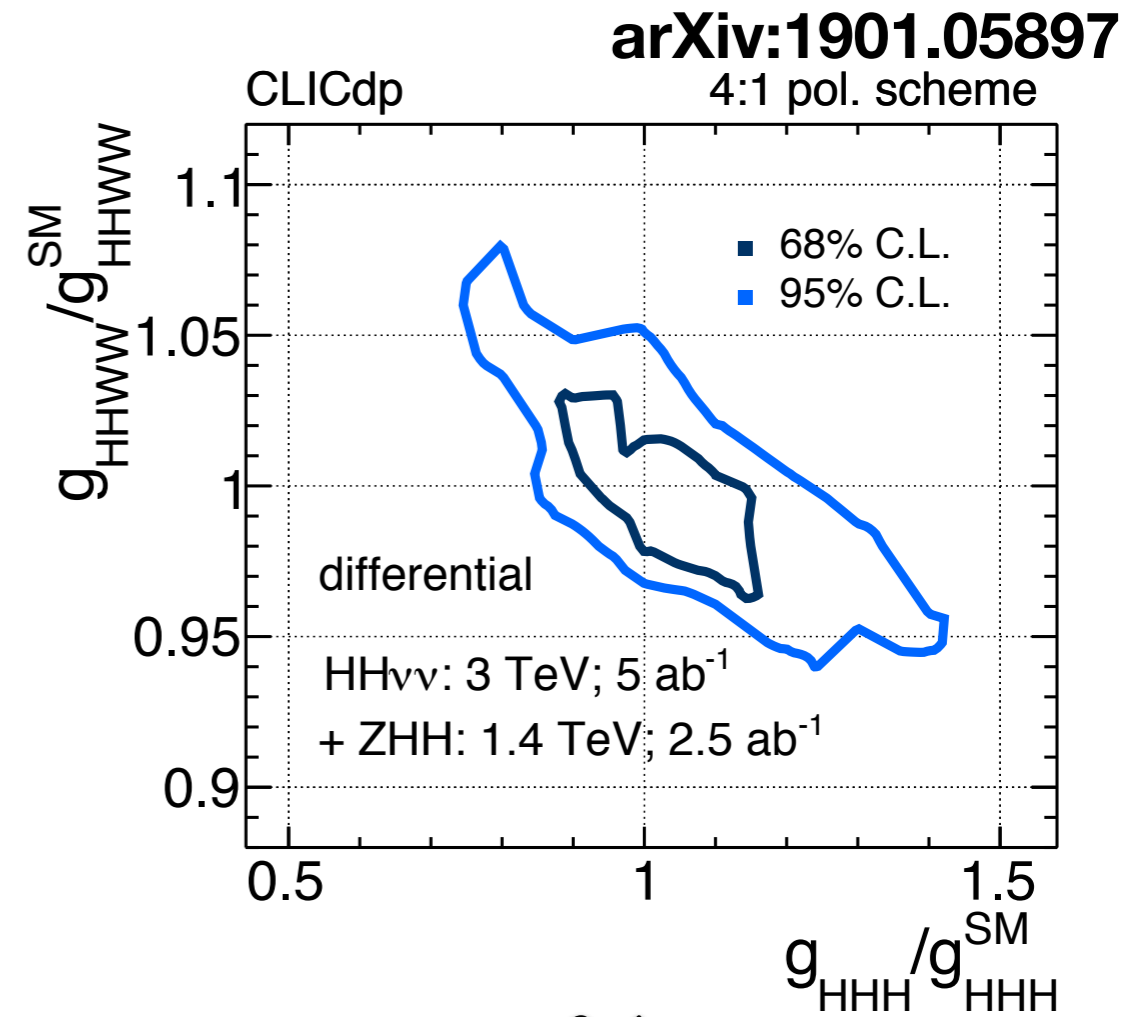
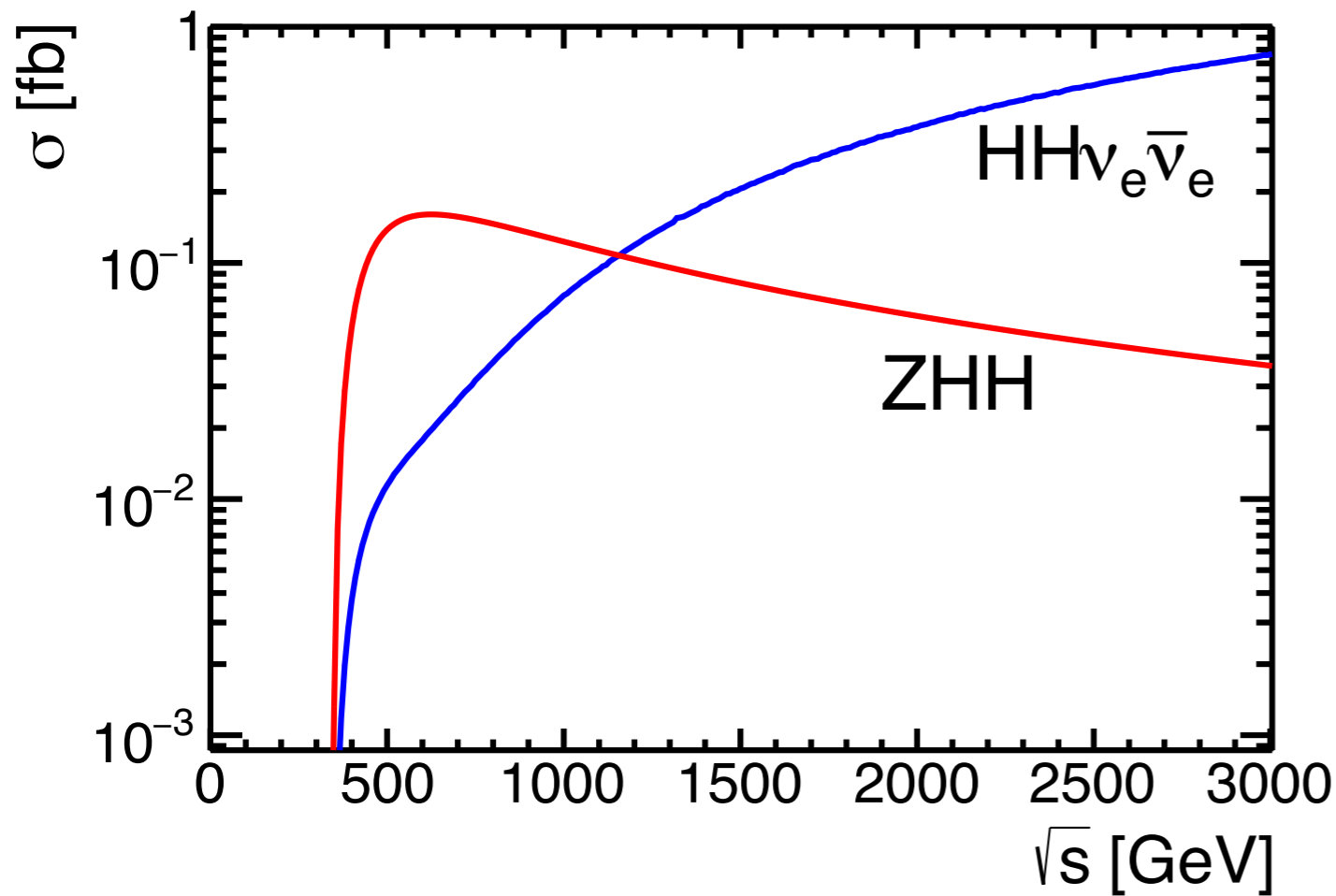
# Higgs self-interaction couplings

- \* the "tough topic" even at "most-future" colliders
- \* most interesting to measure from theory side....

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \lambda_4 \frac{m_h^2}{8v^2} h^4$$

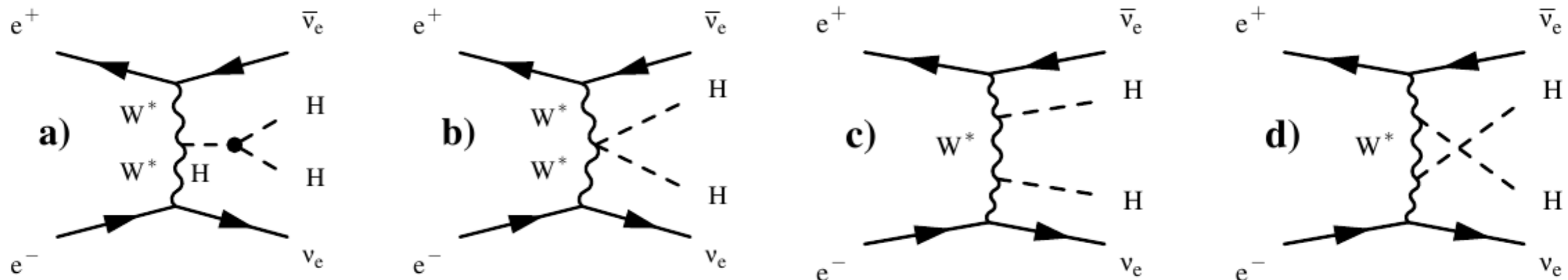
$$\lambda_3^{SM} = \lambda_4^{SM} = 1$$

# trilinear Higgs coupling at CLIC



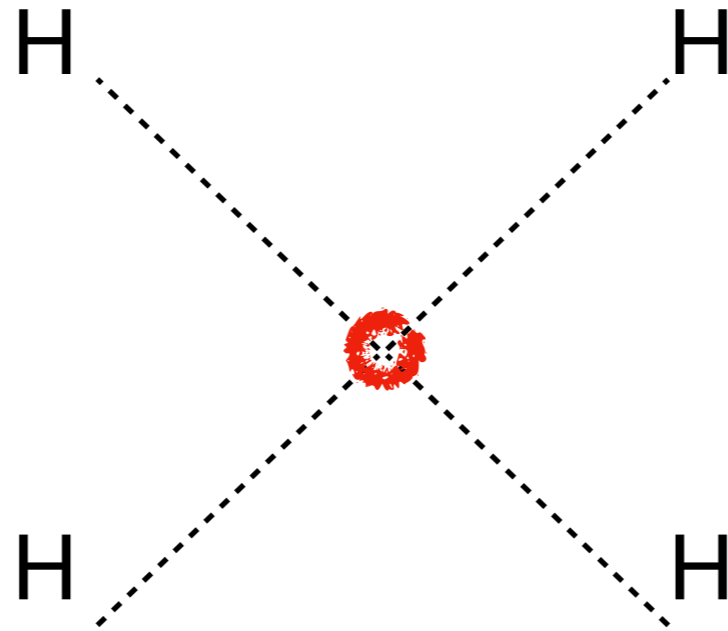
$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \lambda_4 \frac{m_h^2}{8v^2} h^4$$

$$\Delta\lambda_3 \sim 10\%$$



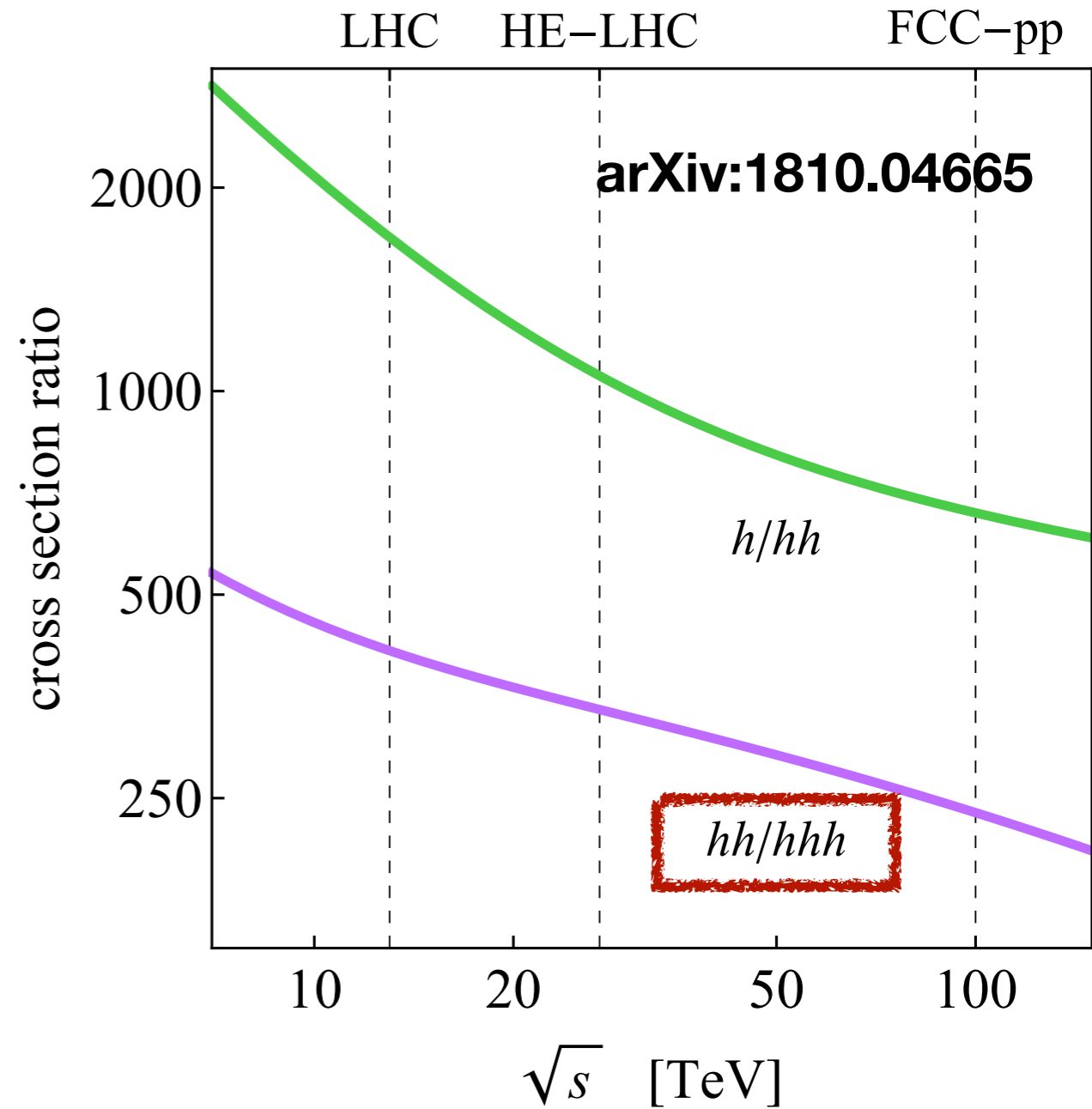
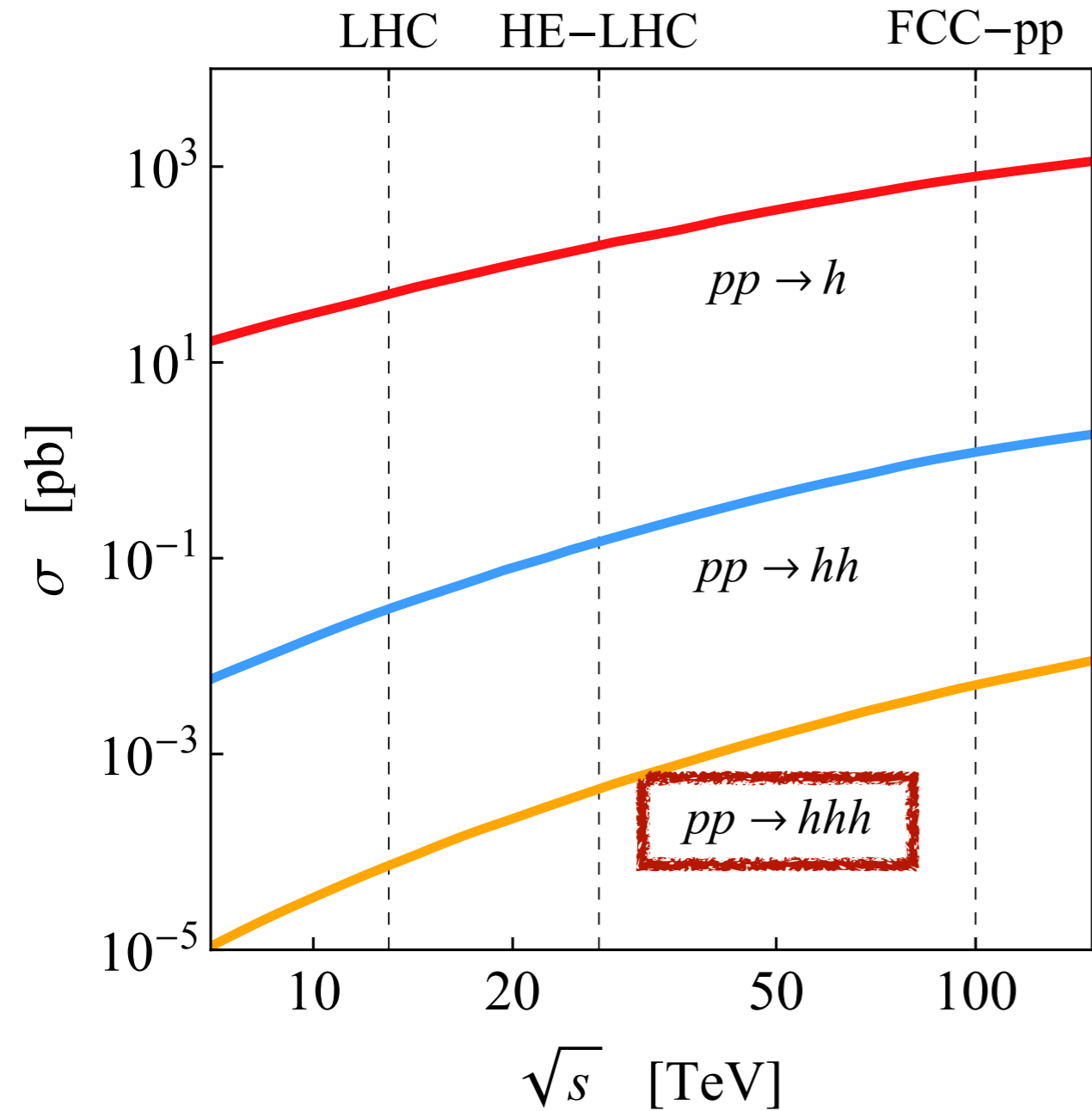
# what about 4-linear Higgs coupling ?

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \boxed{\lambda_4} \frac{m_h^2}{8v^2} h^4$$



**FCC-pp :  $\lambda_4$**

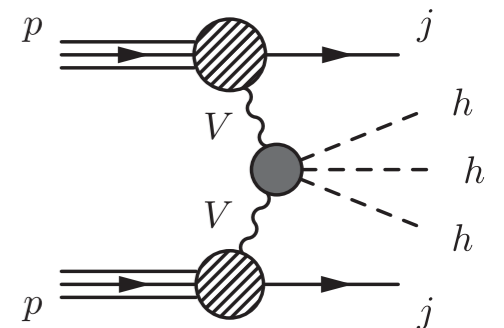
$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \lambda_4 \frac{m_h^2}{8v^2} h^4$$



**$hhh \rightarrow (b\bar{b})(b\bar{b})(\gamma\gamma)$  [optimistic scenario !!!] :**

**$\lambda_4 \in [\sim -4, \sim +16]$**   
**(95% C.L.)**

**at 100 TeV, 30  $ab^{-1}$**



**arXiv:1606.09408**

# anomalous Higgs self-coupling parametrization

$$\lambda_{hhh}^{\text{SM}} = \lambda_{hhhh}^{\text{SM}} = \frac{m_h^2}{2v^2}$$

$$V_h = \frac{m_h^2}{2} h^2 + (1 + \kappa_3) \lambda_{hhh}^{\text{SM}} v h^3 + \frac{1}{4} (1 + \kappa_4) \lambda_{hhhh}^{\text{SM}} h^4$$



typical of

well-behaved EFTs  $\rightarrow \rightarrow \kappa_3 = \bar{c}_6$

$$\kappa_4 = 6\bar{c}_6 + \bar{c}_8$$

$$V^{\text{NP}}(\Phi) \equiv \sum_{n=3}^{\infty} \frac{c_{2n}}{\Lambda^{2n-4}} \left( \Phi^\dagger \Phi - \frac{1}{2} v^2 \right)^n$$



$$\bar{c}_6 \equiv \frac{c_6 v^2}{\lambda^{\text{SM}} \Lambda^2} = \kappa_3$$

$$\bar{c}_8 \equiv \frac{4c_8 v^4}{\lambda^{\text{SM}} \Lambda^4} = \kappa_4 - 6\kappa_3$$

two interesting benchmarks :

- $g_{3H} = g_{3H}^{\text{SM}}, g_{4H} = (1 + \kappa_4) g_{4H}^{\text{SM}}$  ("free"  $\kappa_4$ )

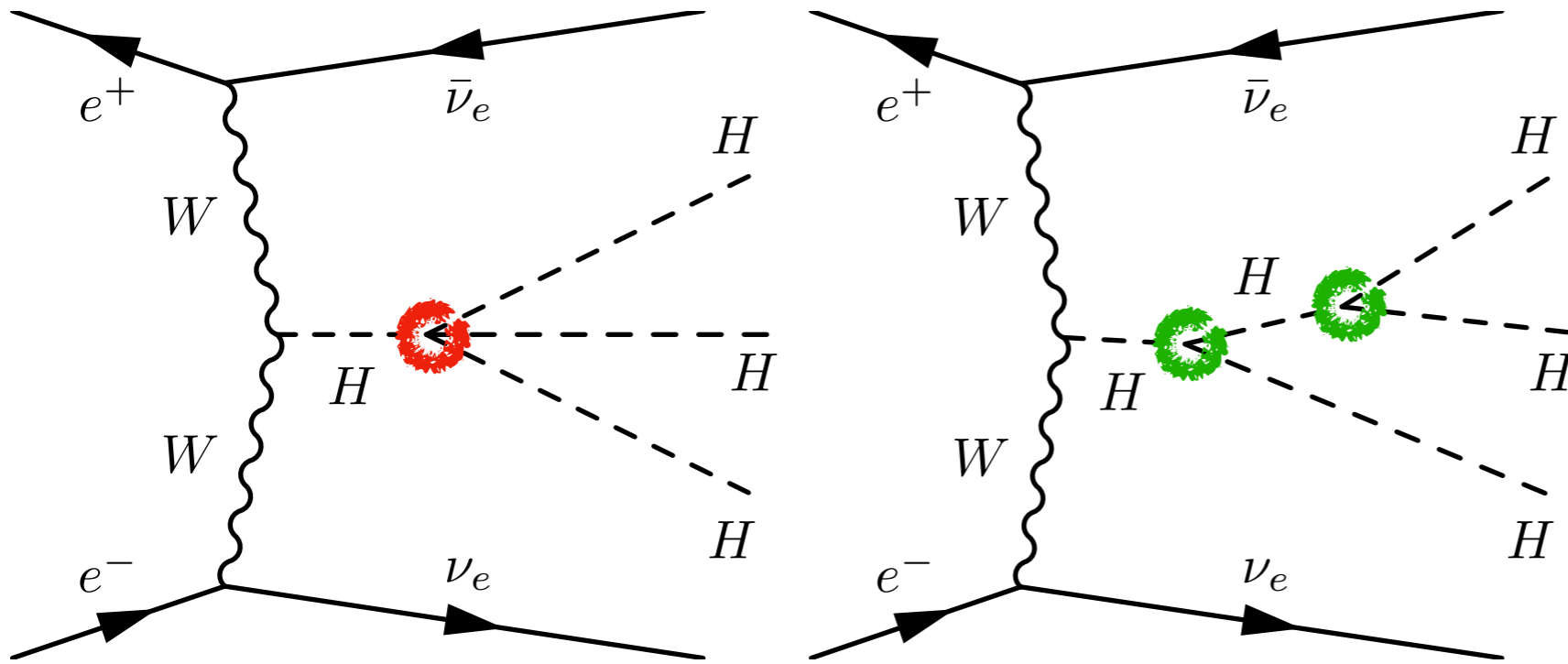
- $g_{3H} = (1 + \kappa_3) g_{3H}^{\text{SM}}, g_{4H} = (1 + 6\kappa_3) g_{4H}^{\text{SM}}$

well-behaved EFTs

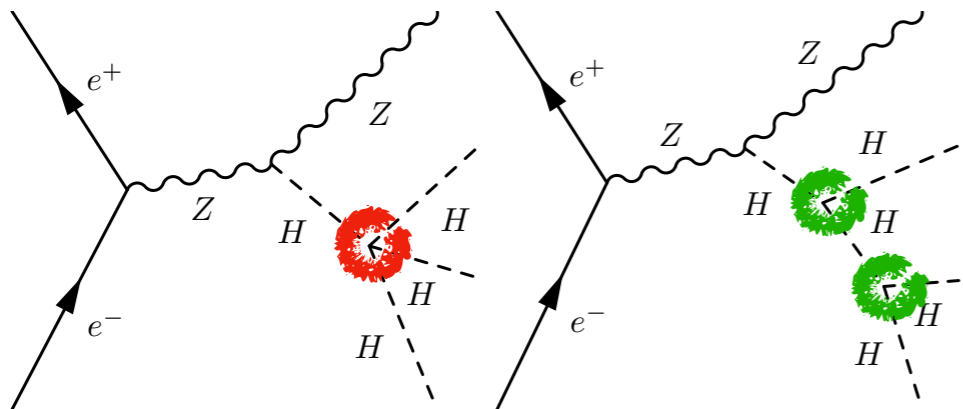
**otherwise :** be agnostic about how UV dynamics modifies Higgs self-interact.s  
 $\rightarrow$  no assumption about the actual size of  $(\kappa_3, \kappa_4)$

$$\mu^+ \mu^- \rightarrow H H H \nu \bar{\nu}, \quad (\nu = \nu_e, \nu_\mu, \nu_\tau)$$

$$V_h = \frac{m_h^2}{2} h^2 + (1 + \kappa_3) \lambda_{hhh}^{\text{SM}} v h^3 + \frac{1}{4} (1 + \kappa_4) \lambda_{hhhh}^{\text{SM}} h^4$$



$$\Delta = \frac{N - N_{SM}}{\sqrt{N_{SM}}} = \left( c_1 \kappa_3 + c_2 \kappa_4 + c_3 \kappa_3 \kappa_4 + c_4 \kappa_3^2 + c_5 \kappa_4^2 + c_6 \kappa_3^3 + c_7 \kappa_3^2 \kappa_4 + c_8 \kappa_3^4 \right)$$

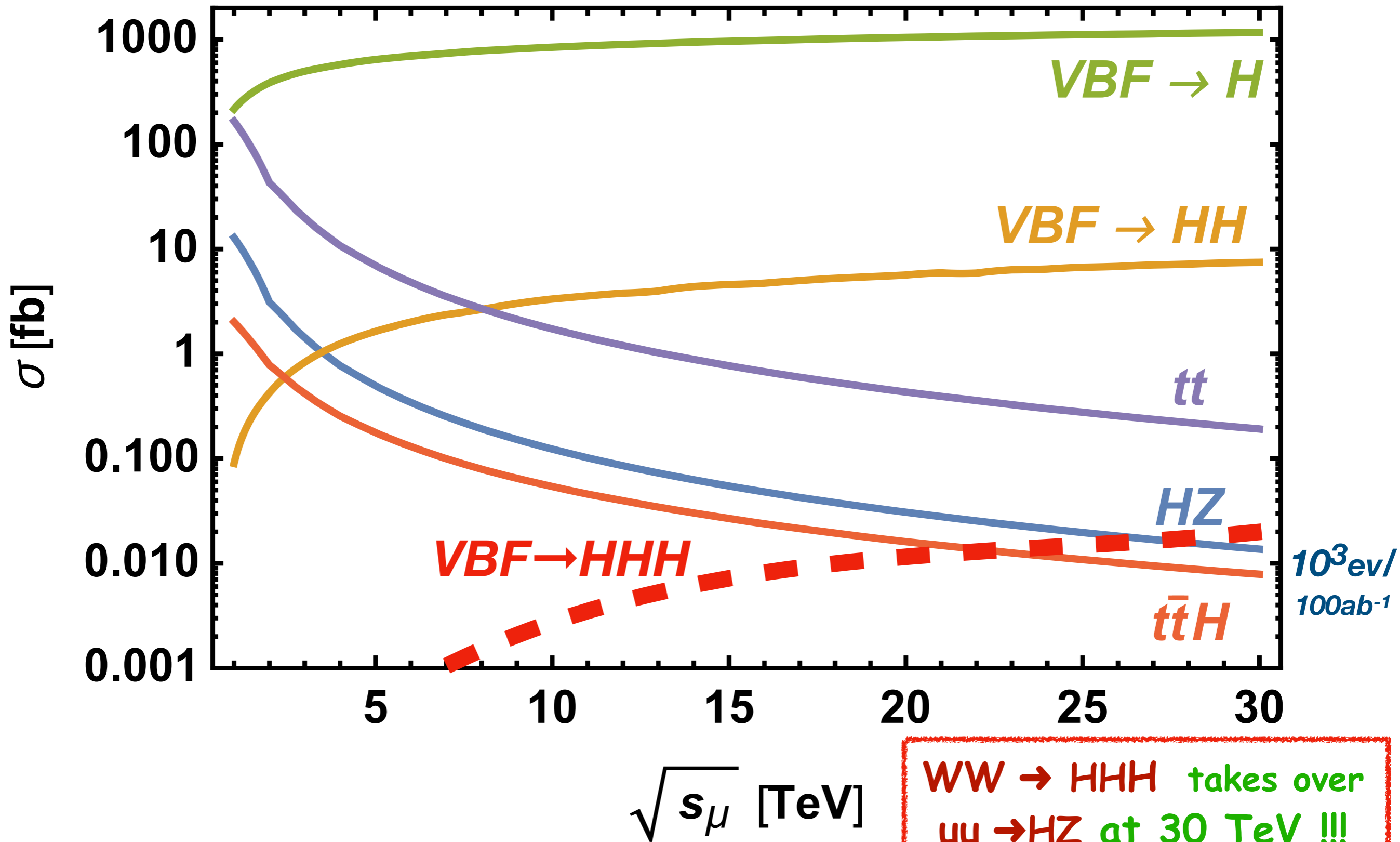


**HHHZ negligible !**

$$\sigma_{HHHZ} \sim 1/2 \sigma_{HHH} \text{ @ } 3\text{TeV}$$

$$\sim 1/50 \sigma_{HHH} \text{ @ } 30\text{TeV}$$

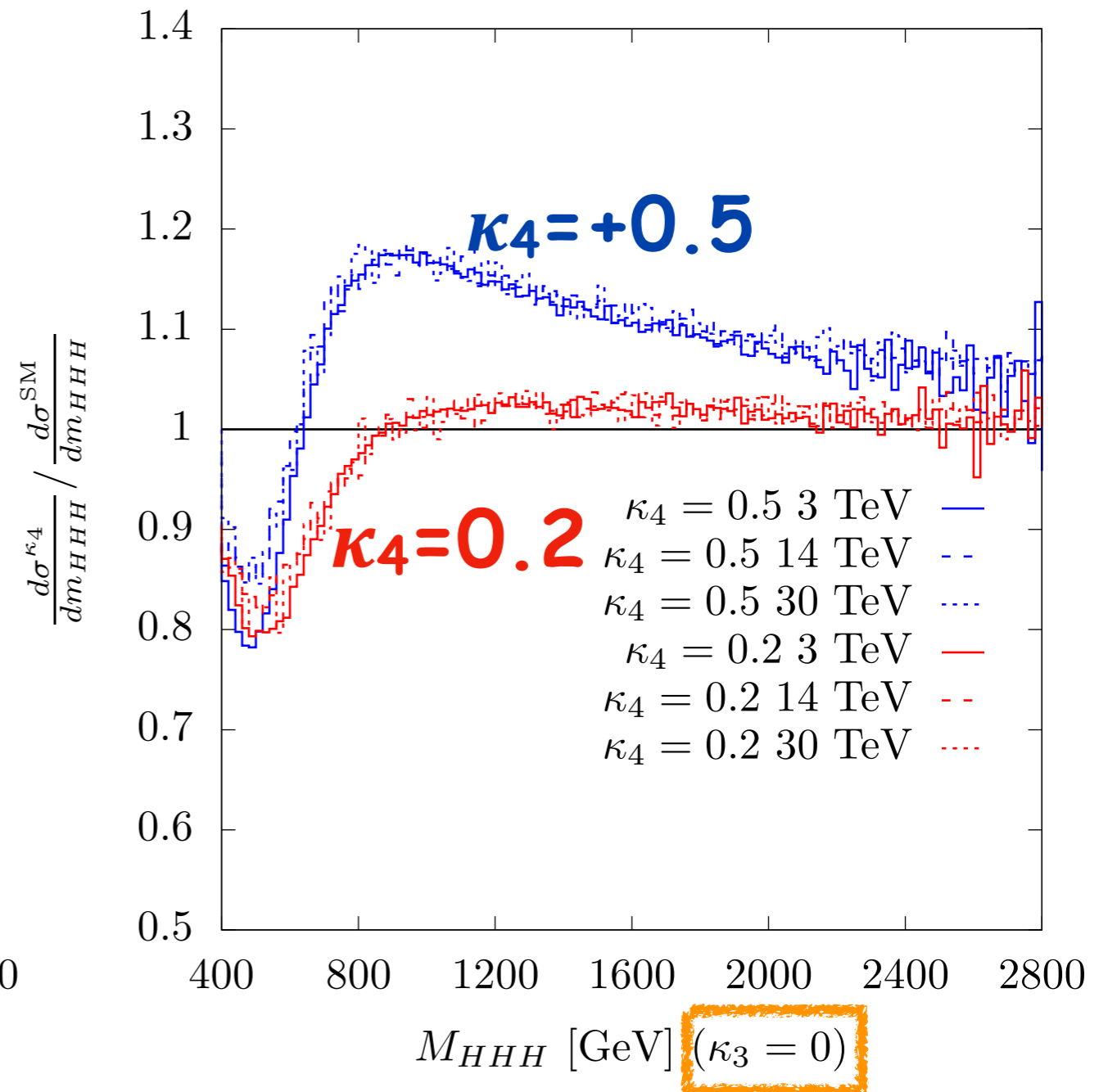
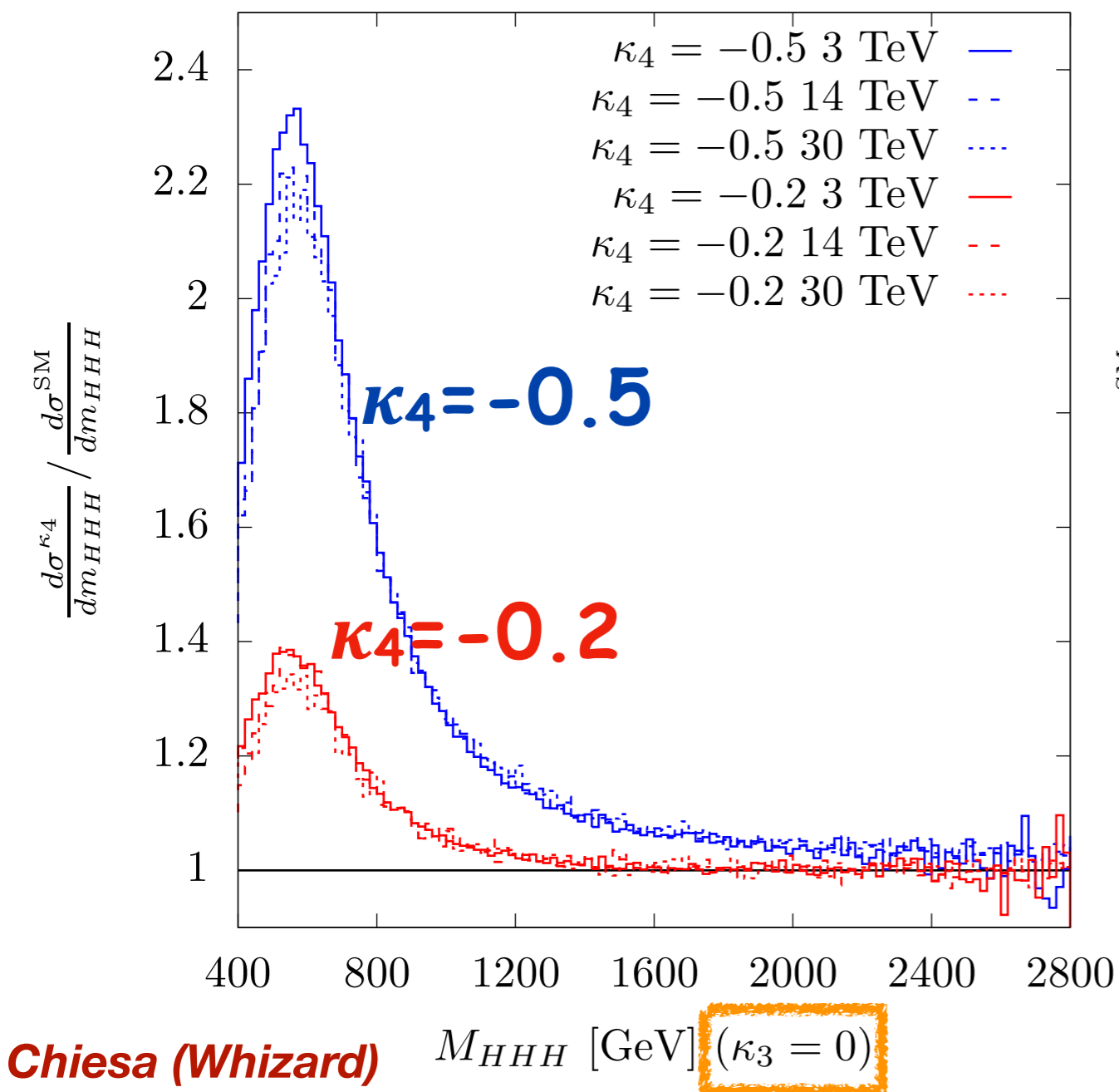
# VBF $\rightarrow$ HHH : SM x-sections



# $m_{HHH}$ distribution versus $g_{4H} = (1 + \kappa_4) g_{4H}^{SM}$

VBF  $\rightarrow$  HHH

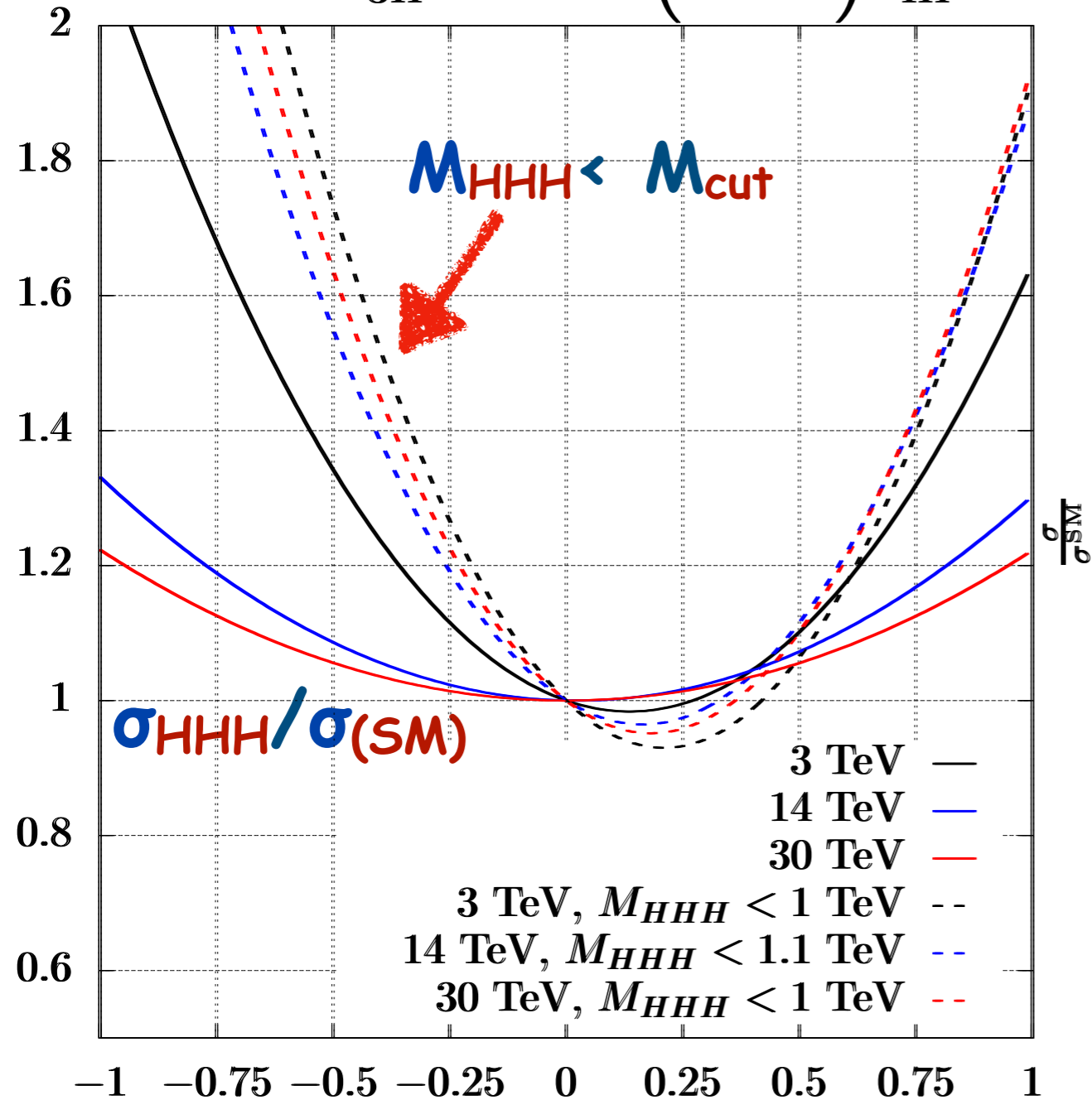
- $m_{HHH}$  shape variation (normalized to SM shapes) insensitive to  $\sqrt{S_{\mu\mu}}$  !





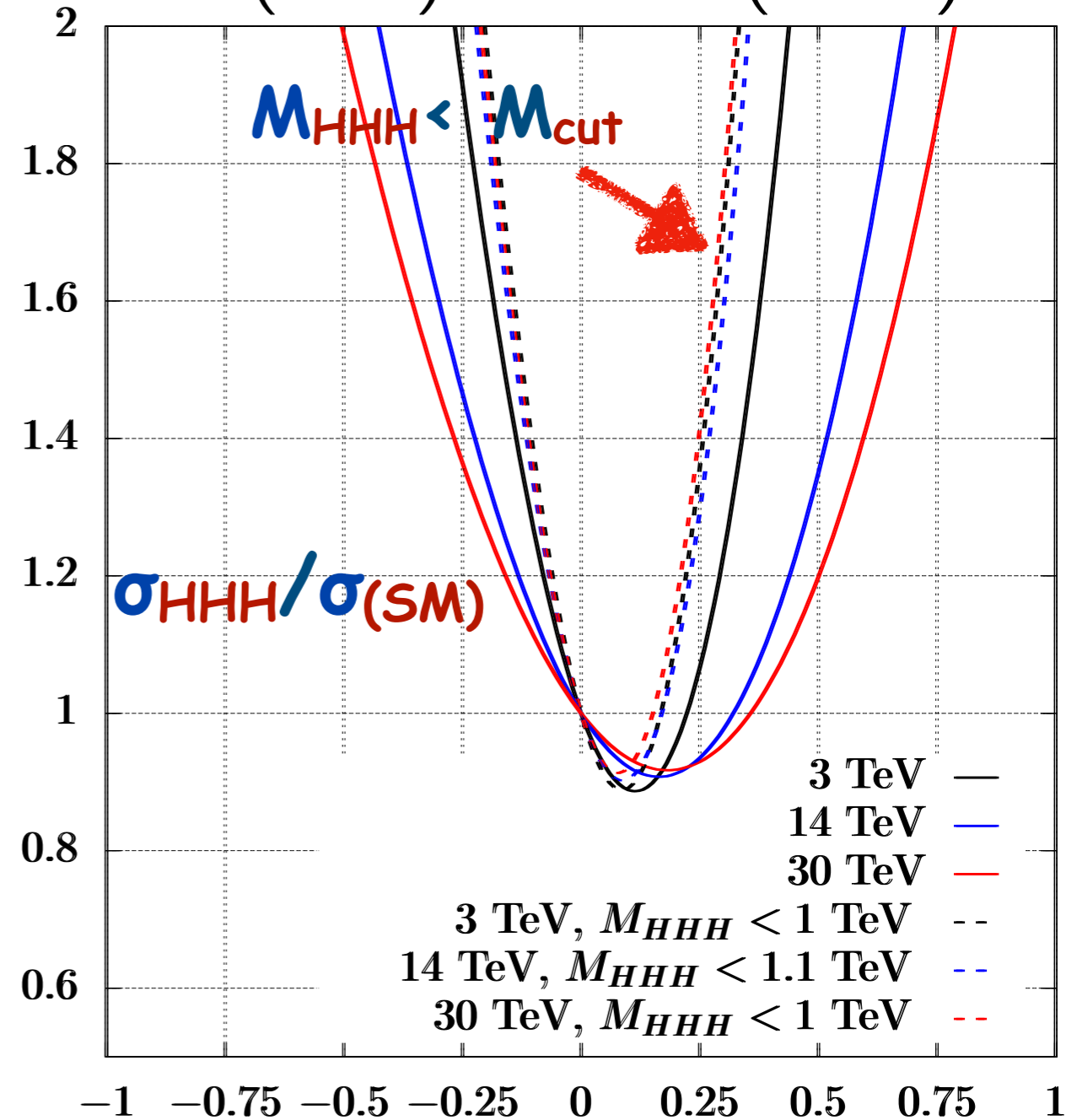
# $\sigma_{HHH}(\text{VBF})/\sigma(\text{SM})$ versus $(\kappa_3, \kappa_4)$

•  $g_{3H} = g_{3H}^{SM}, g_{4H} = (1 + \kappa_4)g_{4H}^{SM}$



$\kappa_4 (\kappa_3 = 0)$

•  $g_{3H} = (1 + \kappa_3)g_{3H}^{SM}, g_{4H} = (1 + 6\kappa_3)g_{4H}^{SM}$

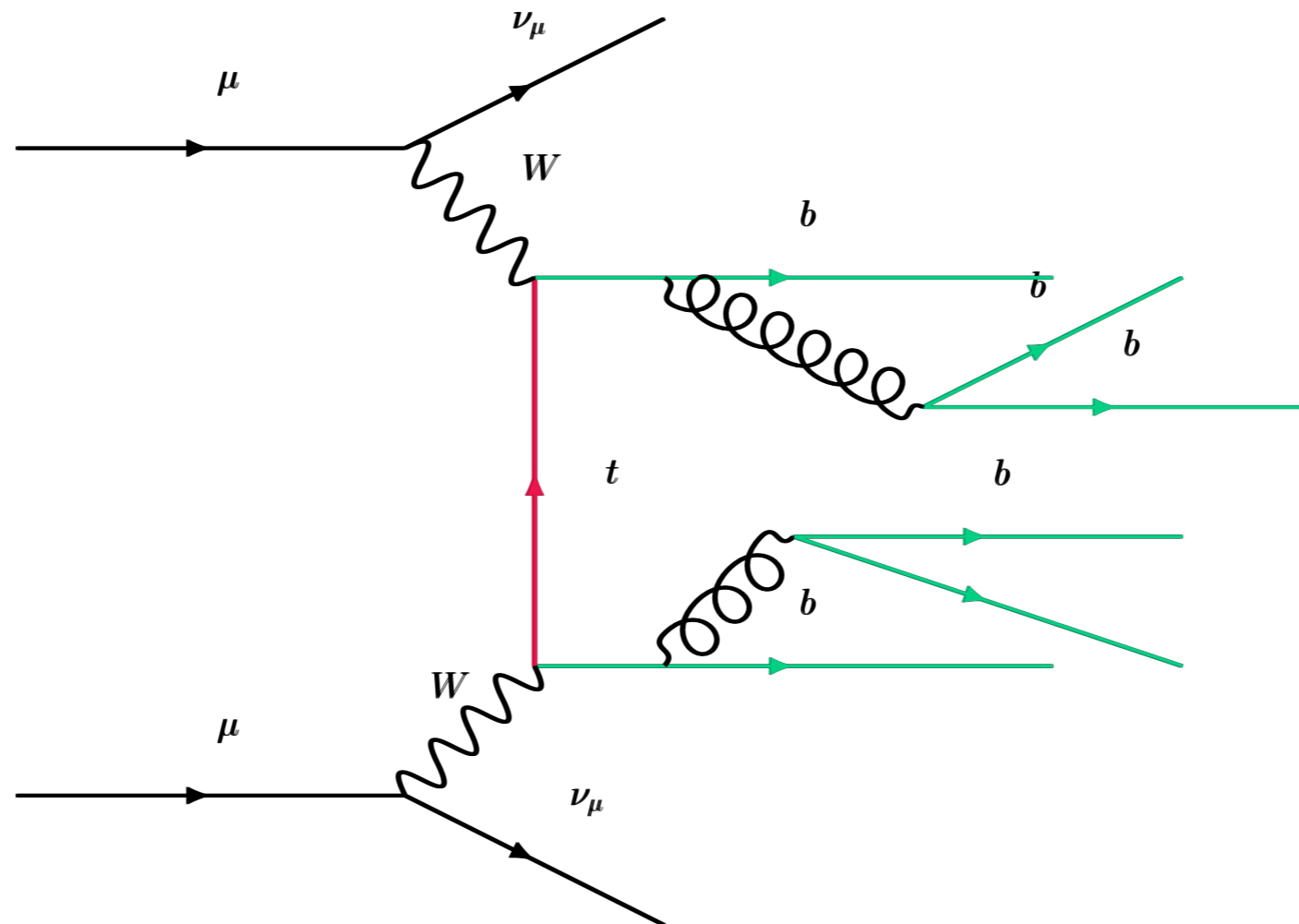


$\kappa_3, (\kappa_4 = 6\kappa_3)$

Chiesa (Whizard)

# backgrounds to $VBF \rightarrow HHH$

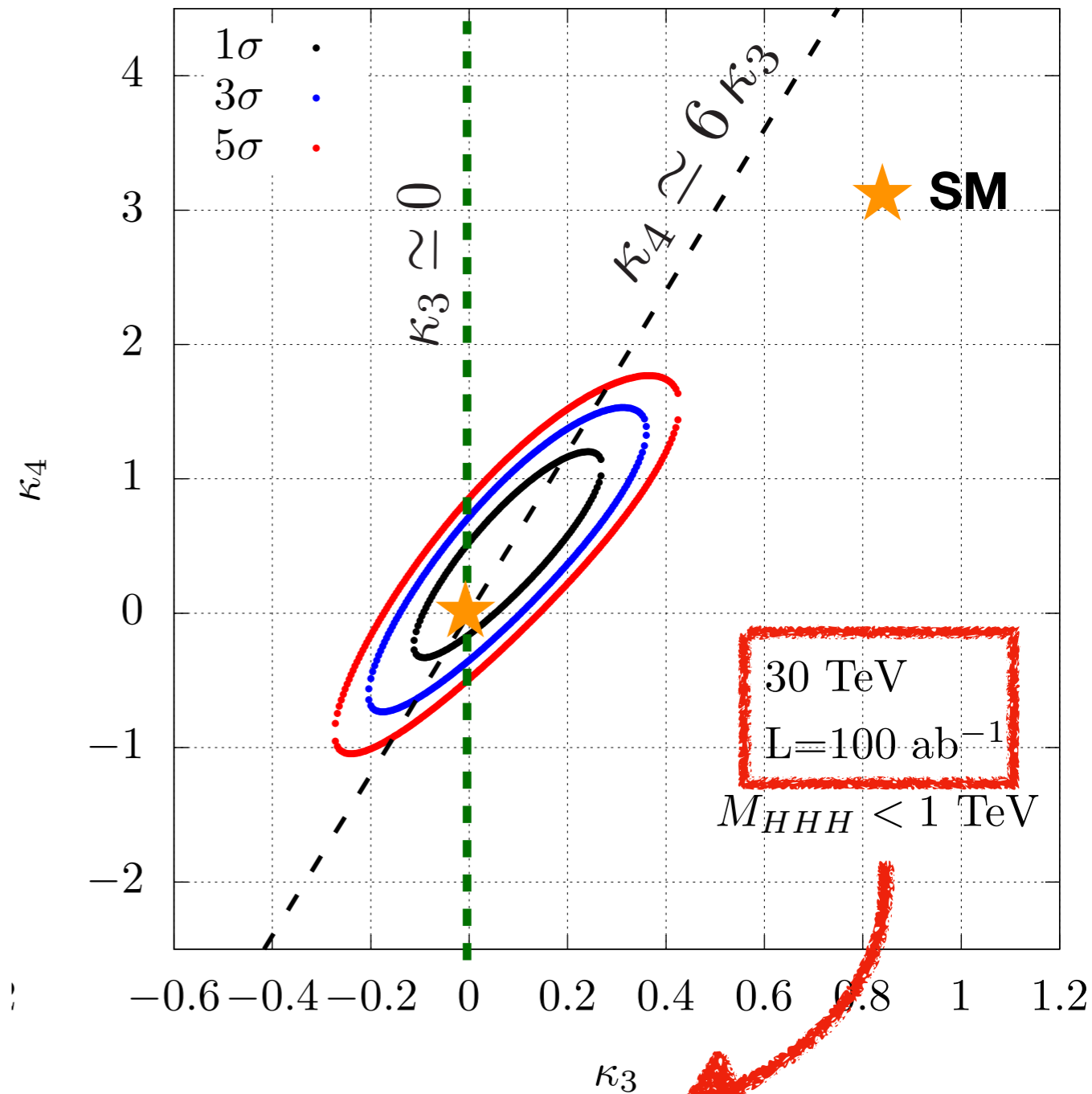
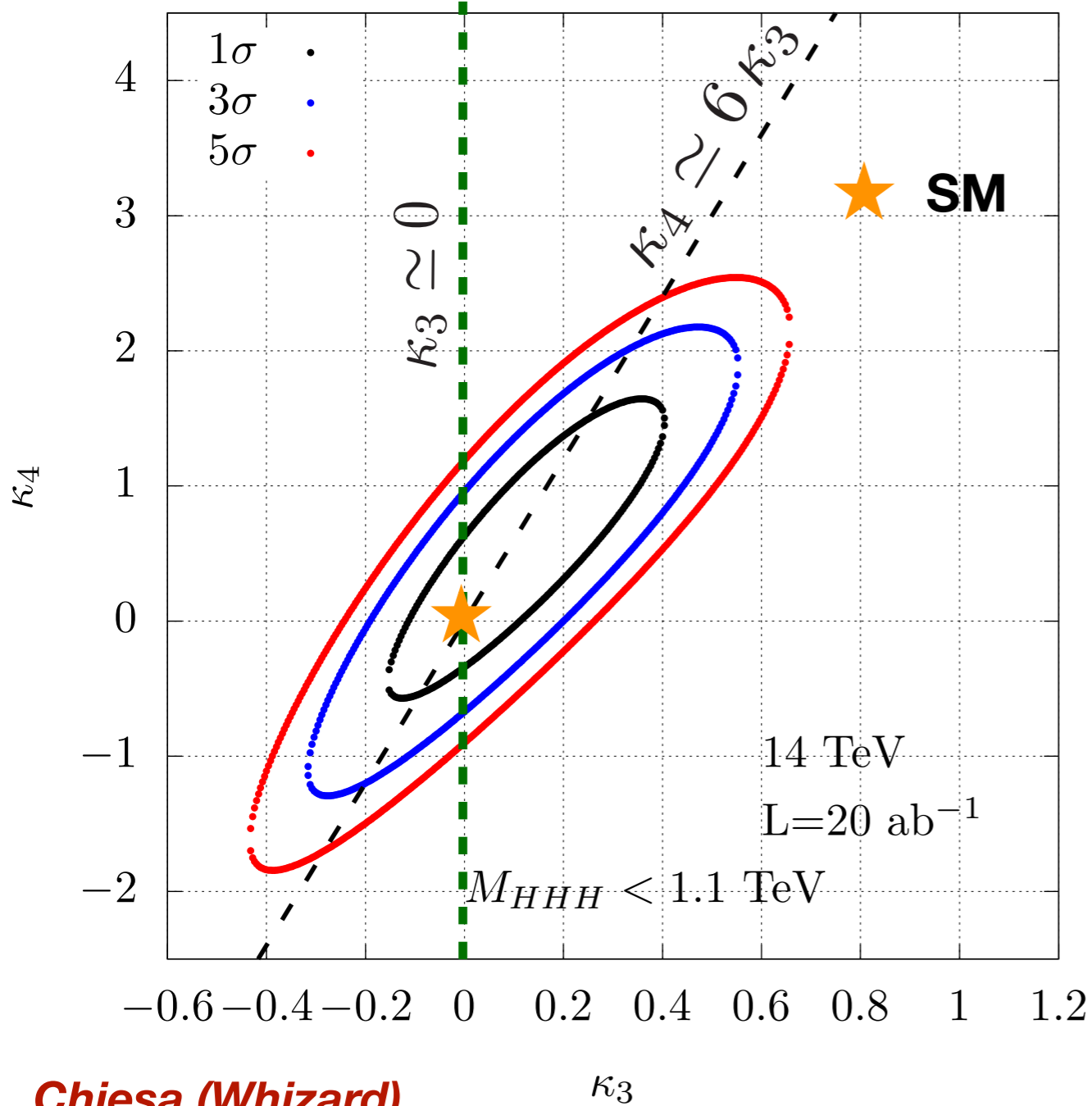
- \* 8-body final states (at least !)  
→ hard to evaluate via MC's
- \* all H decay modes are relevant ! [BR(HHH  $\rightarrow$  6 b)  $\sim$  20 %]
- \* 6b-jet bckgr moderate at FCC-pp [arXiv:1801.10157]
- \* might be  $S/B \gg 1$  at multi-TeV muon colliders...



# $(N - N_{SM}) / \sqrt{N_{SM}}$ versus $(\kappa_3, \kappa_4)$

## VBF $\rightarrow$ HHH

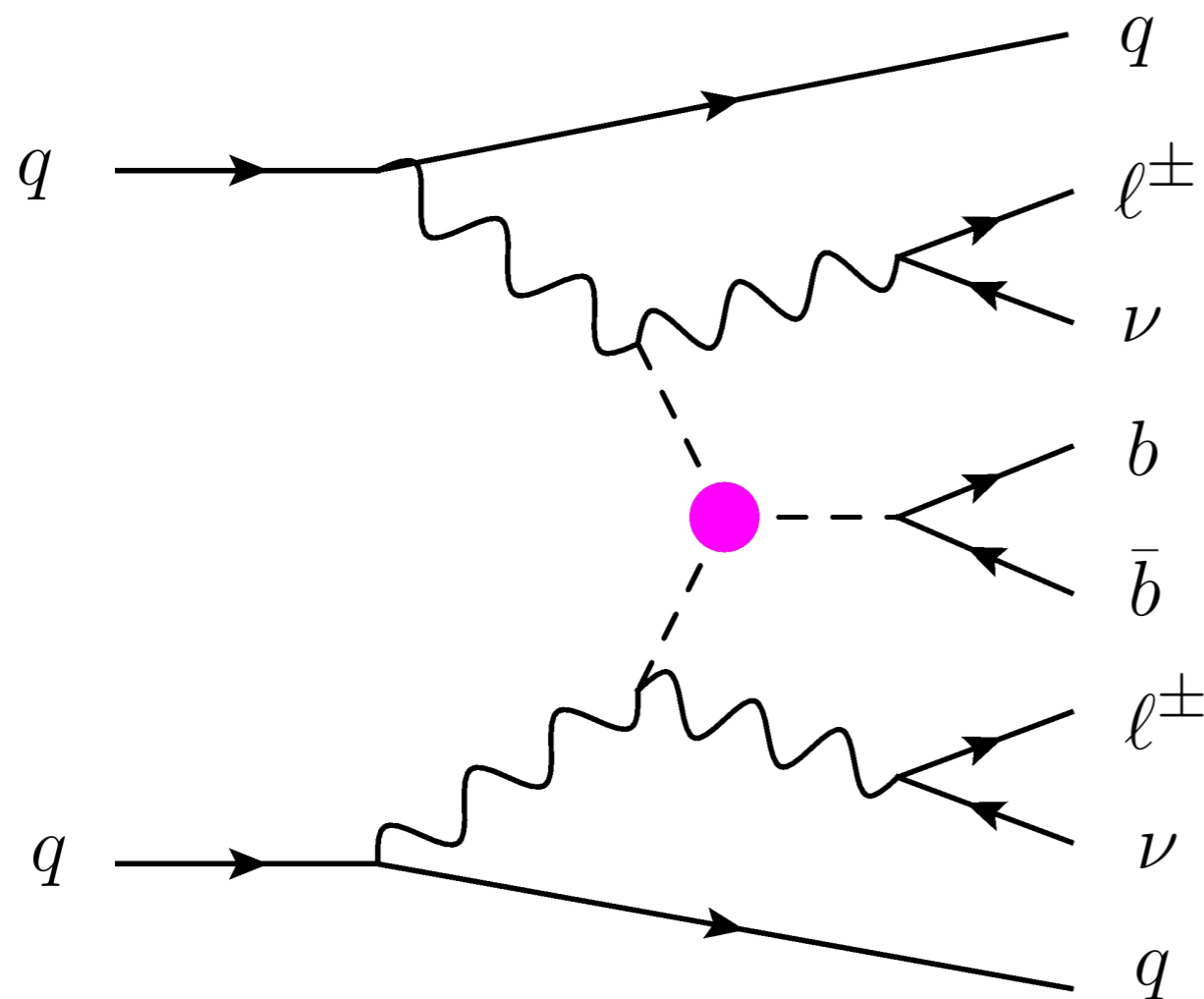
see also talk by M. Chiesa



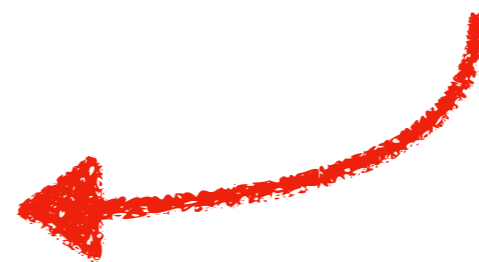
**[  $\kappa_3=0$  ]  $-0.2 < \kappa_4 < 0.5$  (68%CL) !!!**

# VBF $\rightarrow$ HVV, HHVV

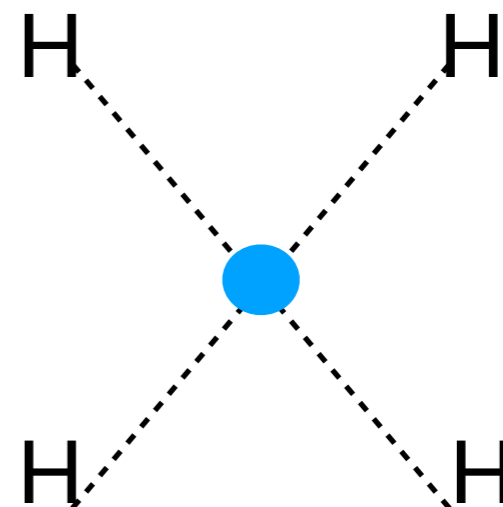
anomalous Higgs couplings induce energy-growing effects in amplitudes involving longitudinally polarized vector bosons



energy-growing sensitivity to  $\lambda_3$



• same in VBF  $\rightarrow$  HHVV for  $\lambda_3, \lambda_4$



arXiv:1812.09299

# a few final comments

- \* such a high energy at pointlike level opens up hugely new perspectives !
- \*  $\mu$  colliders @10's TeV can be considered WW colliders !
- \* qualitatively new Higgs physics
- \* physics bckgds expected mild also for hadronic final states but simulations are quite hard (many particles in phase-space)
- \* explore goodness of Equivalent Vector-Boson Approx.
- \* many many possible new directions for exploring BSM [VBF-production role to be extensively considered...]
- \* comparison with FCC (pp,ee) to be kept in mind ...
  - \* see also talks by M.Chiesa, X. Zhao....
- \* thanks to M.Chiesa, F.Maltoni, F.Piccinini, A.Wulzer for discussions !!!