



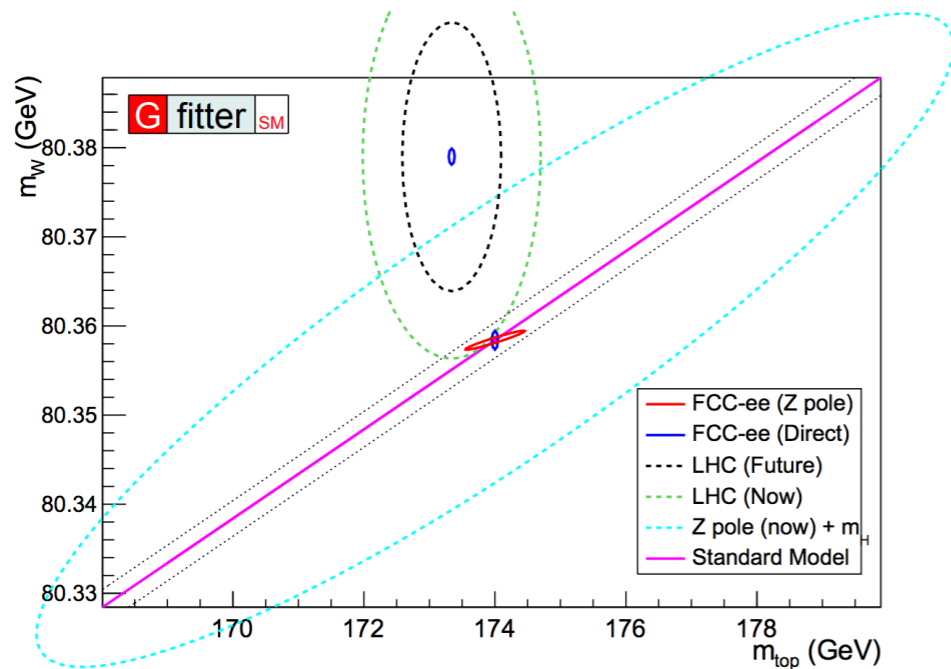
# BSM benchmarks at a muon collider: few results and many ideas

Dario Buttazzo



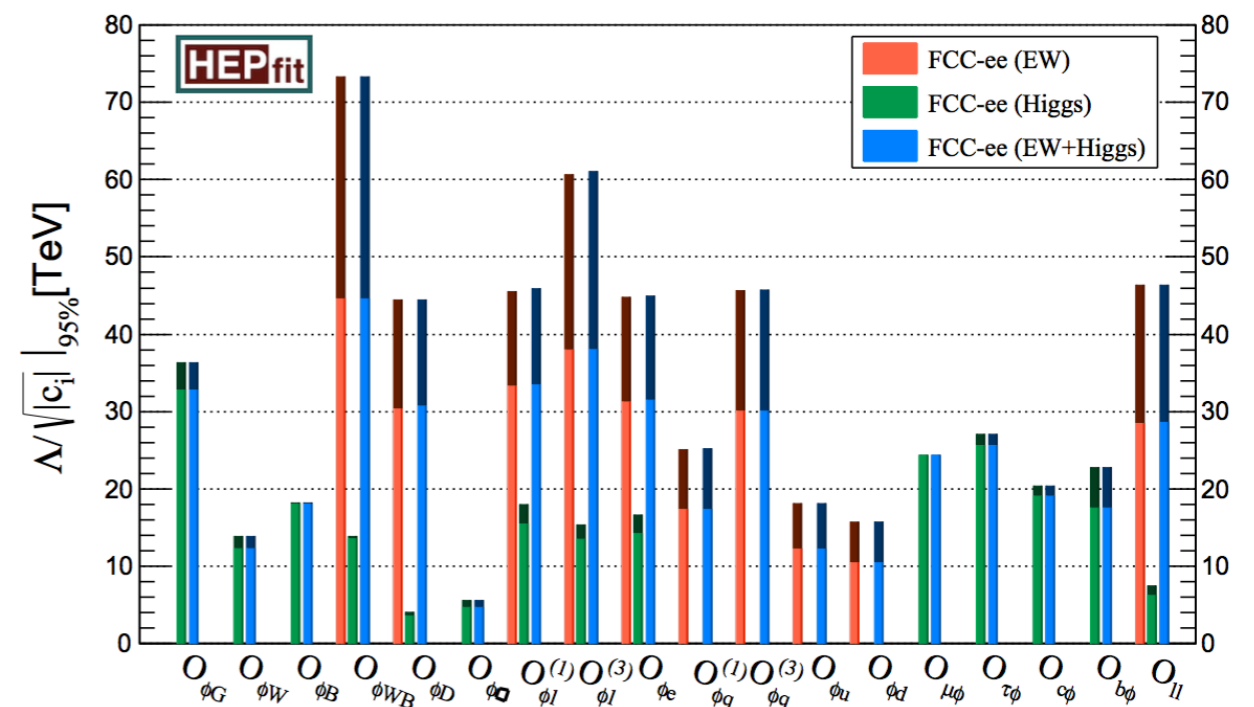
# Why a High Energy Lepton Collider?

- ◆ High-Intensity Lepton Colliders: ultimate precision on EW/Higgs physics



- ▶ FCC-ee can measure Z-pole parameters with a precision of a few  $10^{-5}$

- ▶ FCC-ee/ILC/CLIC can measure Higgs pole parameters with a precision of a few  $10^{-3}$



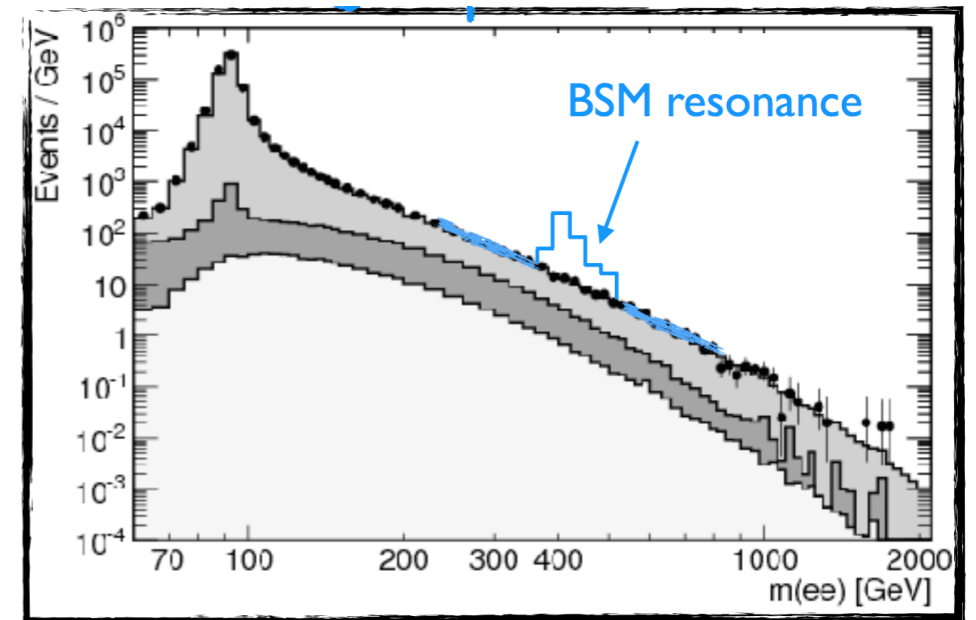
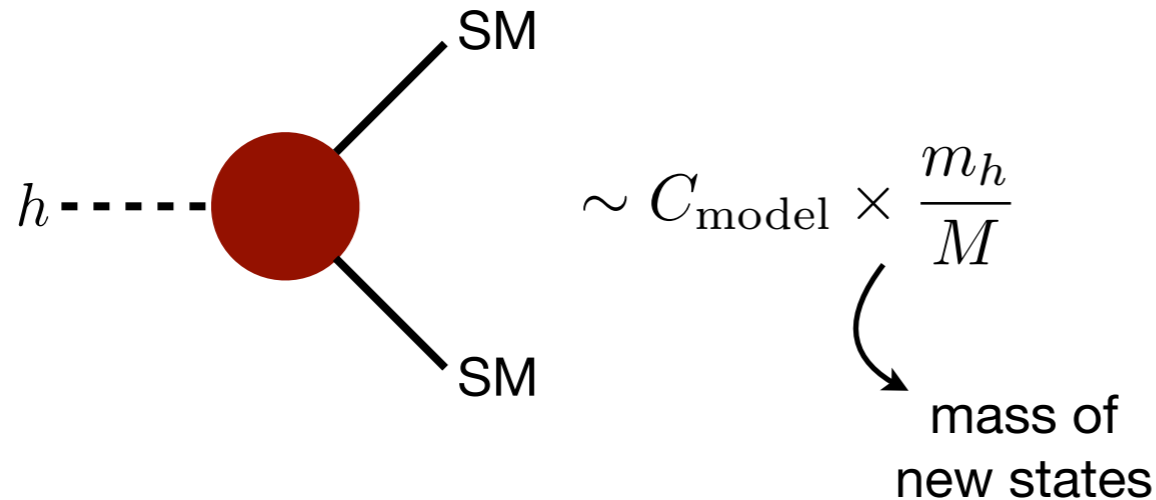
(these measurements are limited by systematic/parametric uncertainties)

- ◆ Energy frontier: FCC-hh can directly probe c.o.m. energies  $> 10$  TeV

*Can a very High Energy Lepton Collider tell us more?*

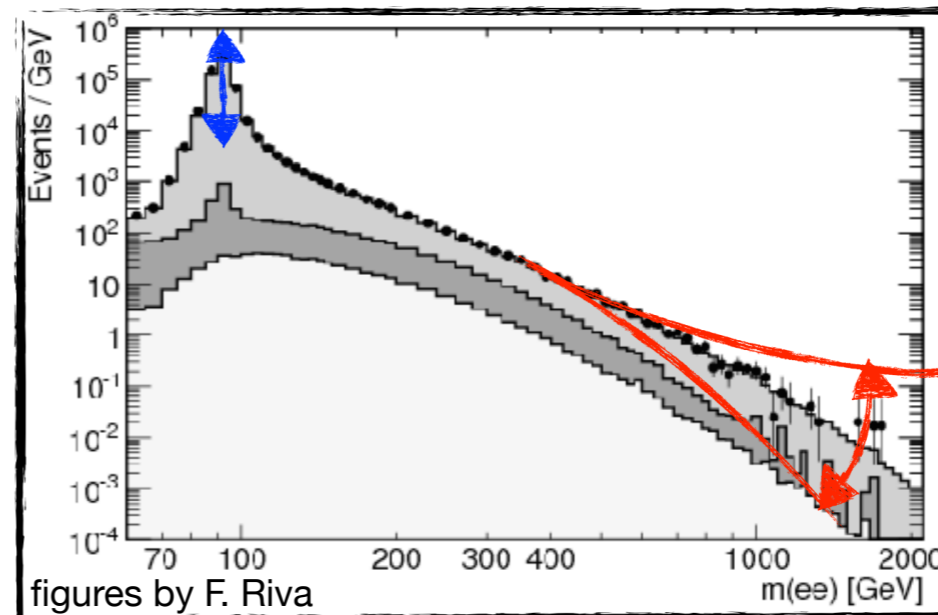
# Precision vs Energy

## I. New physics is light enough: direct searches



## II. New physics is heavy: EFT

- ♦ pole observables  $\propto m_{\text{EW}}^2 / M^2$
- ♦ high energy tails  $\propto E^2 / M^2$



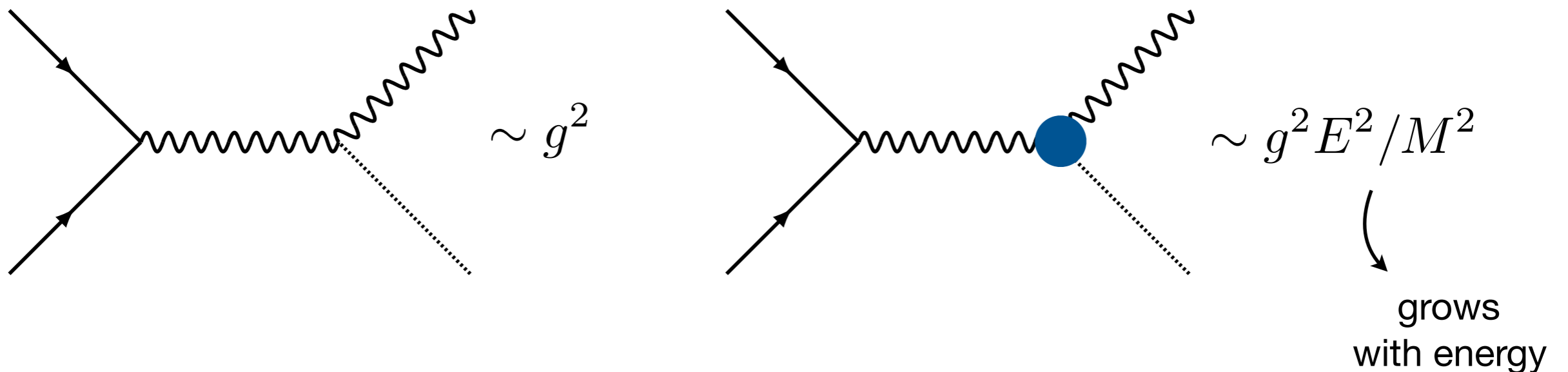
With the same experimental accuracy, high-energy measurements yield a precision gain of  $E^2 / m_{\text{EW}}^2$



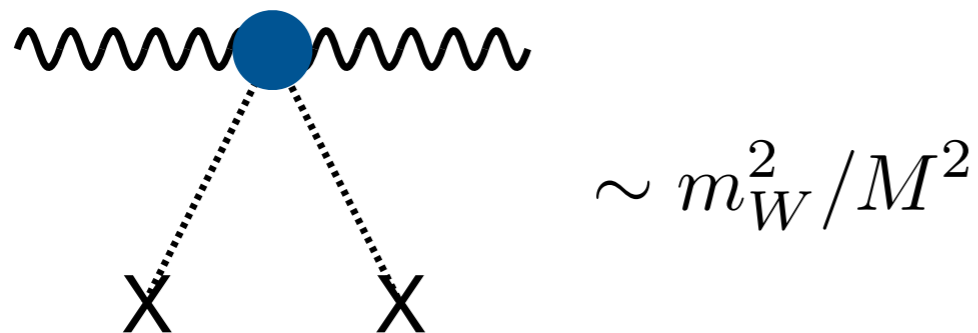
# Example: Zh & S parameter

Consider the dim. 6 operator  $\mathcal{O}_W = \frac{g}{M^2} D^\mu W_{\mu\nu}^a (H^\dagger \sigma^a D^\nu H)$

♦ contribution to  $\ell^+ \ell^- \rightarrow Zh$  scattering



♦ contribution to Z-pole observables (S parameter)



(also contribution from  $\mathcal{O}_B = \partial^\mu B_{\mu\nu} (H^\dagger \partial^\nu H)$ )

can be constrained with  $\ell^+ \ell^- \rightarrow WW$

$$\hat{S} = c_W + c_B$$

Higgs couplings not relevant here...

➔ see Andrea's talk

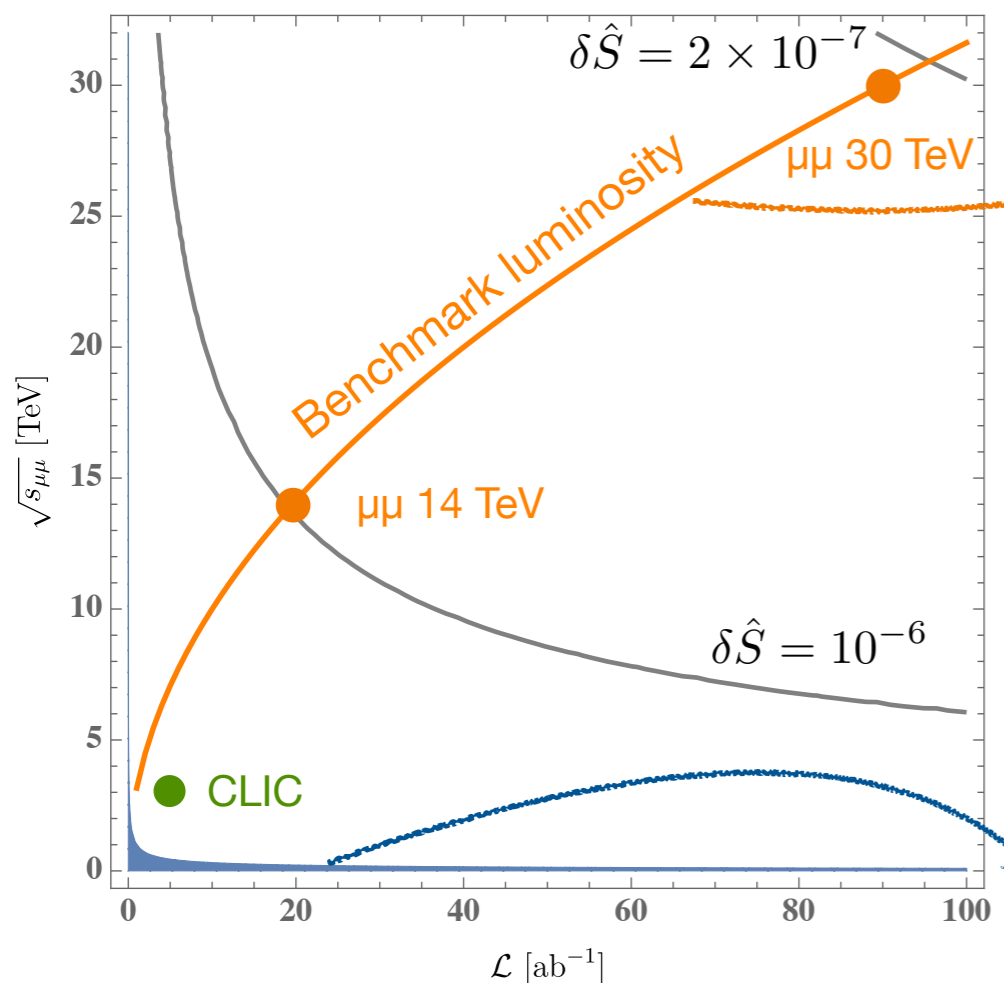
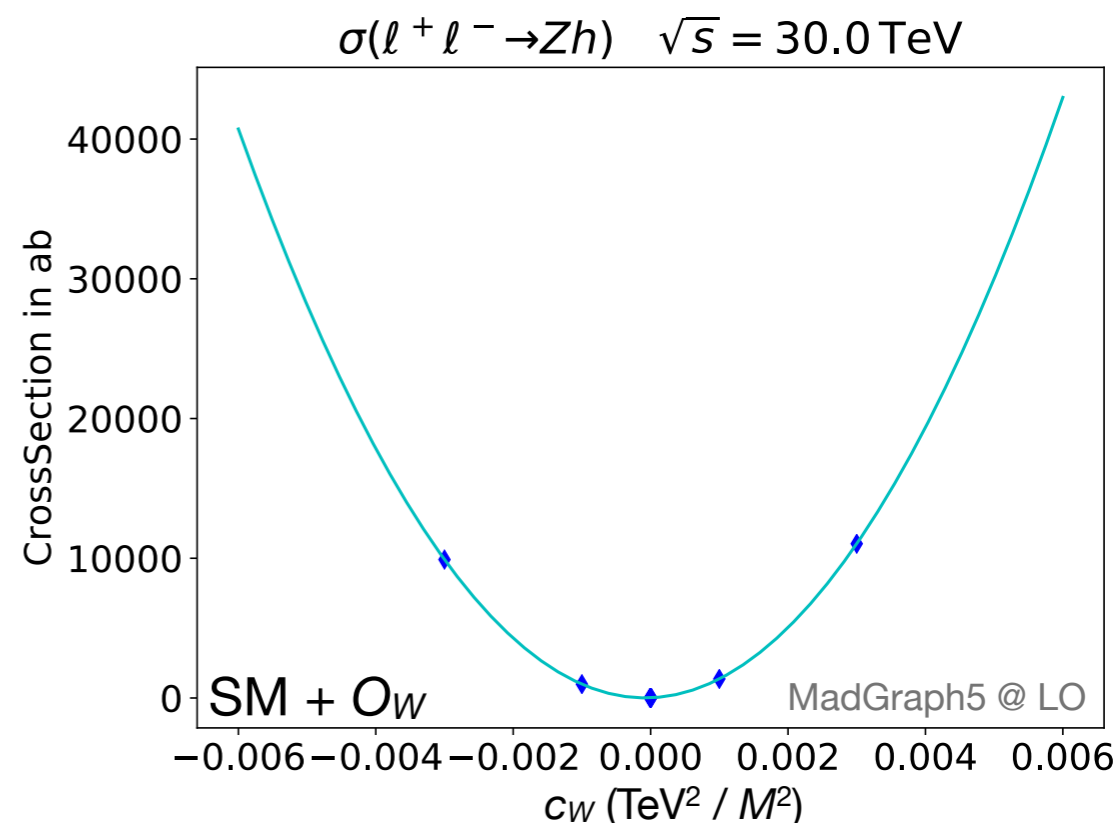
# Example: Zh & S parameter

$\sqrt{s}$ [TeV]	$\sigma_{\text{SM}}$ [ab]	$\mathcal{L}$ [ $\text{ab}^{-1}$ ]	$M_{95\% \text{ CL}}$ [TeV]
3	1363	2	[12.8, -12.2]
14	62.3	20	[58, -55]
30	13.5	90	[124, -118]

Expected precision on cross-section

(statistical only):  $\delta\sigma_{95\%} = 2\sqrt{\sigma_{\text{SM}}/\mathcal{L}}$

$\Rightarrow$  bound on  $c_W/M^2$  (or equivalently on  $\hat{S}$ )



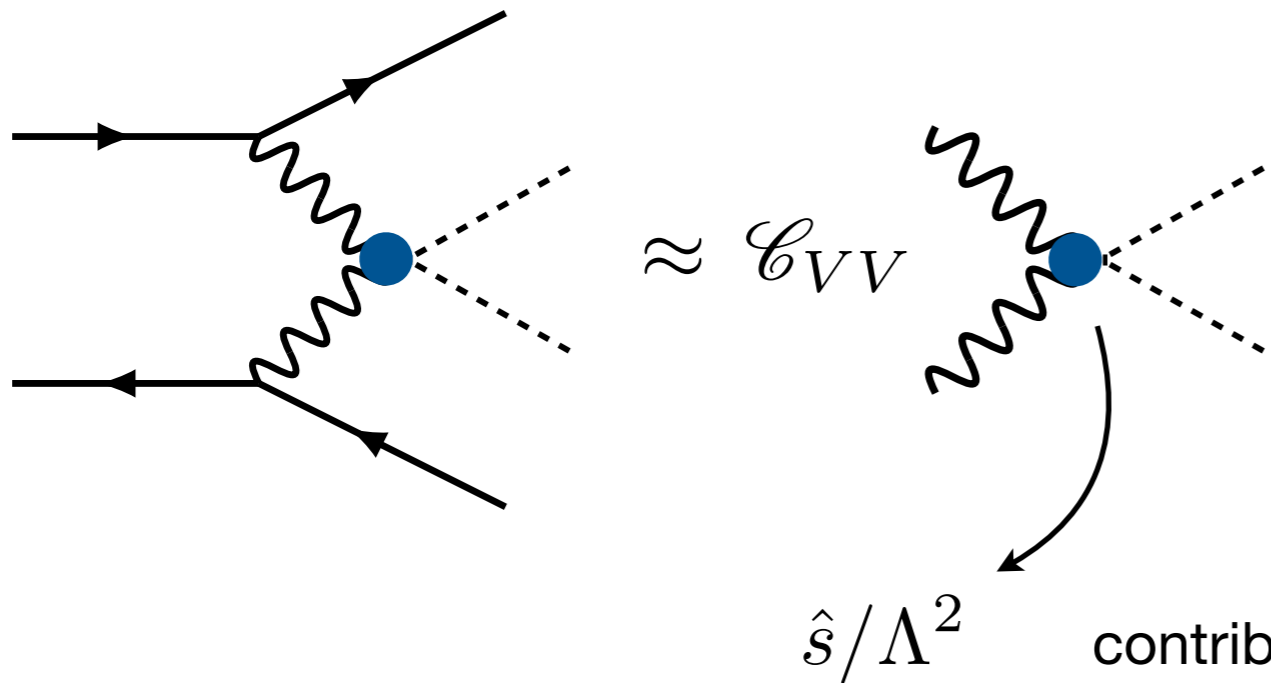
$$\mathcal{L} = 10 \text{ ab}^{-1} \frac{s}{(10 \text{ TeV})^2} \quad (\text{talk by Andrea})$$

A multi-TeV collider (already CLIC) can reach much better precision than the maximal one achievable on  $\hat{S}$  at FCC

14 TeV  $\mu$ -collider:  $\hat{S} < 10^{-6} \Rightarrow M > 80 \text{ TeV}$

FCC-ee Z-pole fit:  $\hat{S} < 6 \cdot 10^{-5}$

# Double Higgs production



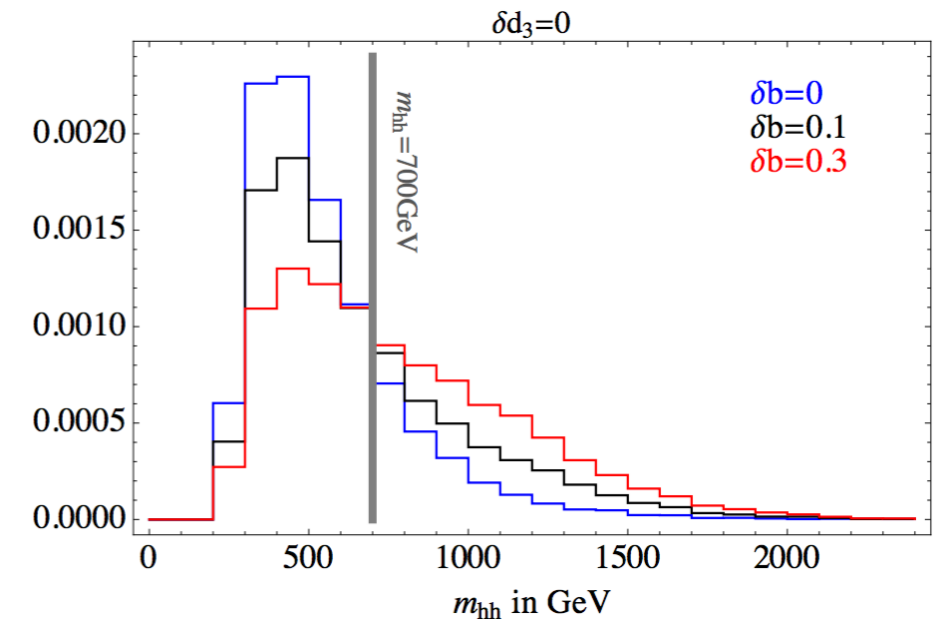
A High Energy Lepton Collider is a “vector boson collider”

$$\mathcal{C}_{VV} \approx \frac{s}{\hat{s}} \log \frac{s}{\hat{s}} \quad \text{Dawson, 1984}$$

$$\mathcal{O}_H = \frac{c_H}{f^2} (\partial_\mu |H|^2)^2$$

- From measurement of high invariant mass  $e^+e^- \rightarrow hh\nu\nu$  cross-section at 3 TeV CLIC:

$$\xi = \frac{v^2}{f^2} \lesssim 0.01 \quad \text{Contino et al. 1309.7038}$$



- Higgs couplings modification from  $\mathcal{O}_H$ :  $\Delta g_{hWW} \propto v^2/f^2 \lesssim 10^{-3}$

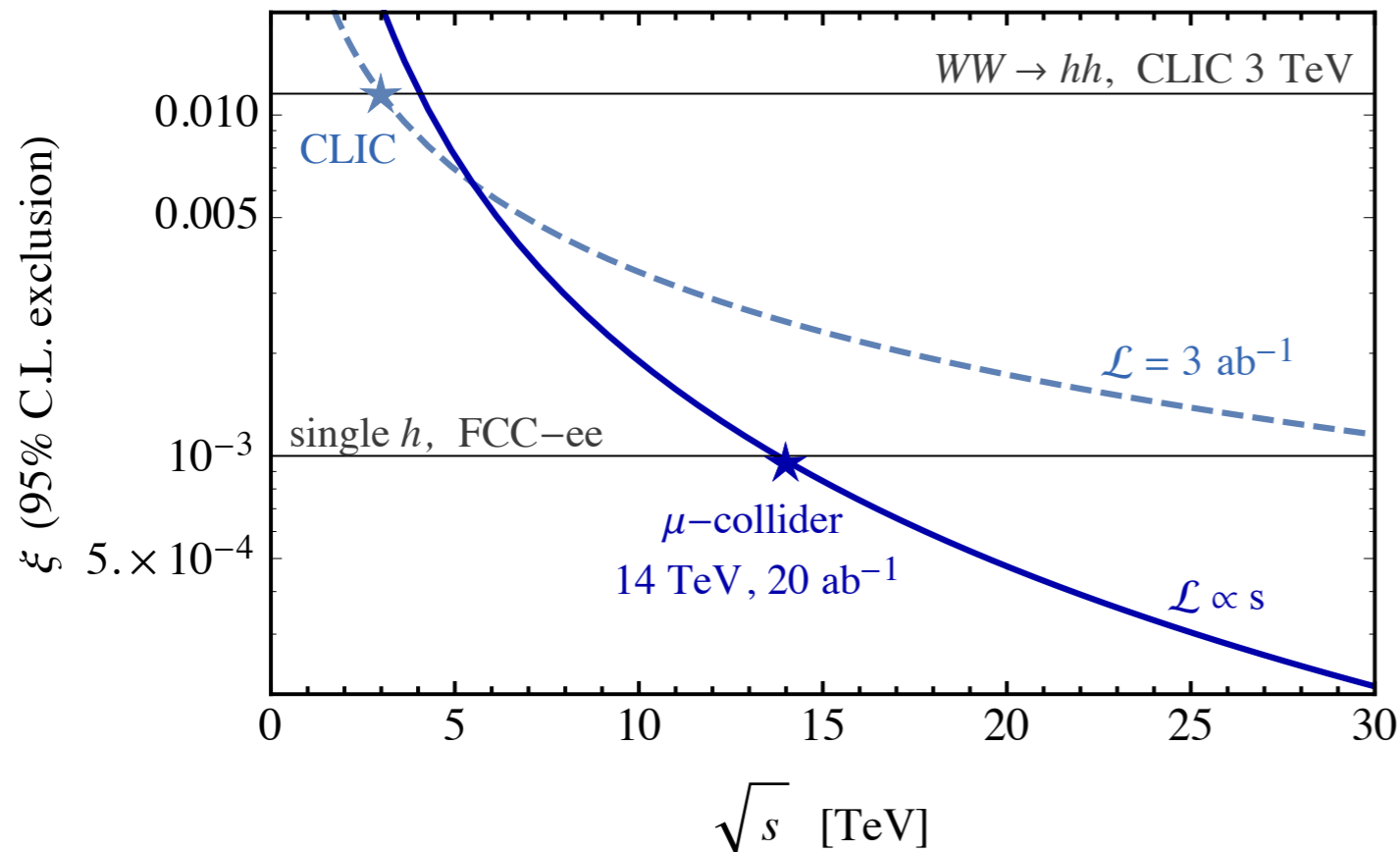
High energy  $VV \rightarrow hh$  at CLIC is not able to compete with single Higgs

# Double Higgs production

- ◆  $E = 3 \text{ TeV}, \mathcal{L} = 3 \text{ ab}^{-1}: \xi = v^2/f^2 \lesssim 0.01$  Contino et al. 1309.7038

- ◆ Rescale to higher energies:  $\xi \propto \frac{1}{E^2} \frac{1}{\sqrt{N_{\text{bkg}}}} \propto \frac{1}{E^2} \frac{1}{\sqrt{\mathcal{L}/E^2}} = \frac{1}{E\sqrt{\mathcal{L}}}$

(assumption: cuts rescaled with E, and bkg composition unchanged)



High-energy  $WW \rightarrow hh$  becomes more sensitive than Higgs pole physics at energies  $> 14 \text{ TeV}$

$$\sqrt{s} = 14 \text{ TeV}, \mathcal{L} = 20 \text{ fb}^{-1}$$

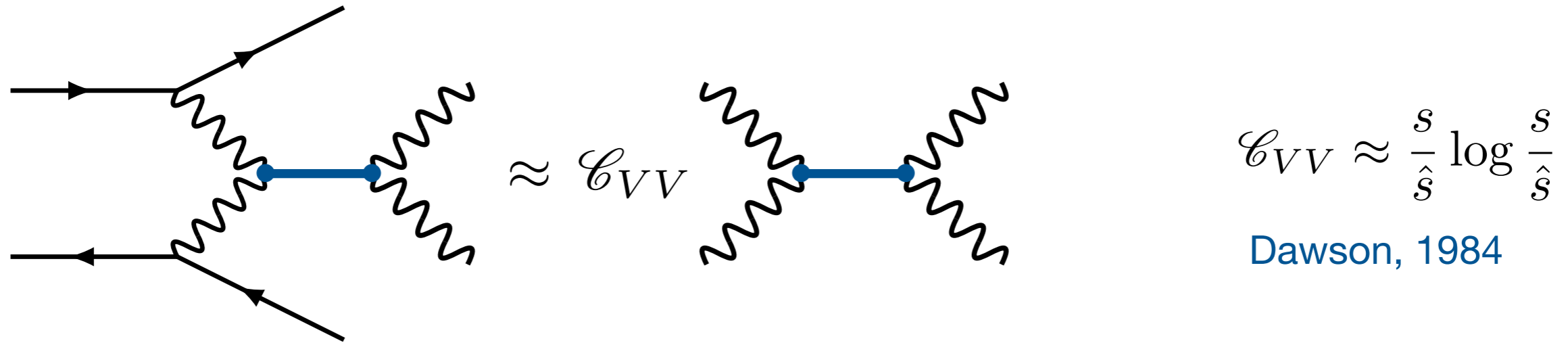
$$\xi < 10^{-3} \quad f > 8 \text{ TeV}$$

$$\sqrt{s} = 30 \text{ TeV}, \mathcal{L} = 90 \text{ fb}^{-1}$$

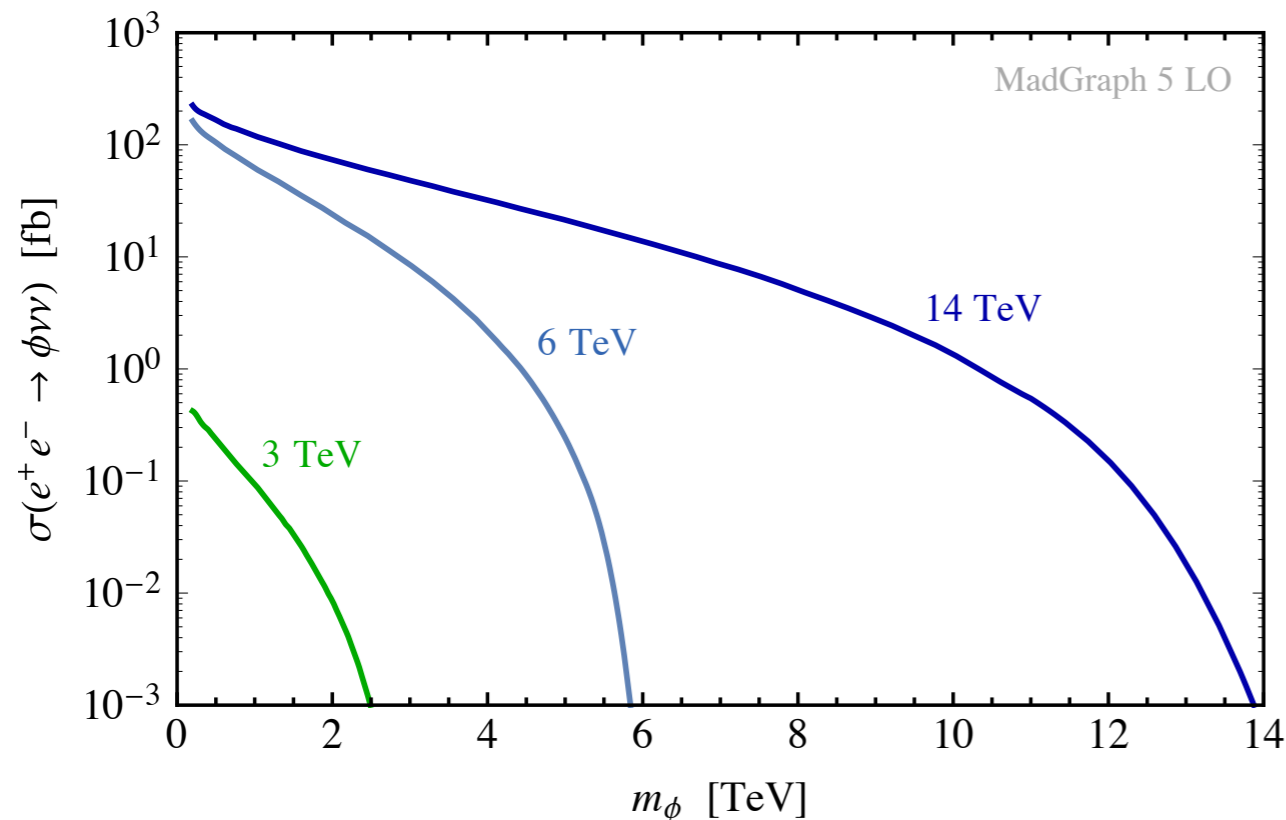
$$\xi < 2 \times 10^{-4} \quad f > 17 \text{ TeV}$$

# Resonance searches

A High Energy Lepton Collider is a “vector boson collider”



VBF resonance production cross-section enhanced by  $\log s/m_\phi^2$



► Example: scalar production

$$\sigma(l^+ l^- \rightarrow h \nu \bar{\nu}) \approx \frac{g^4}{256\pi^3 v^2} \left[ \log \frac{s}{m_h^2} - 2 \right]$$

cross-section grows at high energy due to longitudinal W-fusion



# A simple example: scalar singlet

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 - \underbrace{a_{HS}|H|^2 S}_{\text{portal coupling}} - \frac{\lambda_{HS}}{2}|H|^2 S^2 - V(S)$$

controls Higgs-singlet mixing  $\sim \sin \gamma$

portal coupling

triple couplings:  
 $\text{BR}(\phi \rightarrow hh)$ ,  $g_{hhh}$

$$\sin \gamma \sim \frac{a_{HS} v}{m_S^2}$$

mass eigenstates:  $h = \cos \gamma H^0 + \sin \gamma S$

$$\phi = -\sin \gamma H^0 + \cos \gamma S$$

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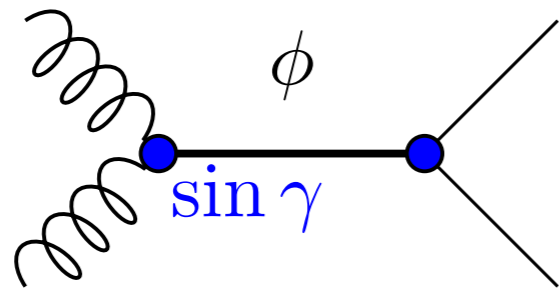
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- ▶  $\phi$  can be singly produced:

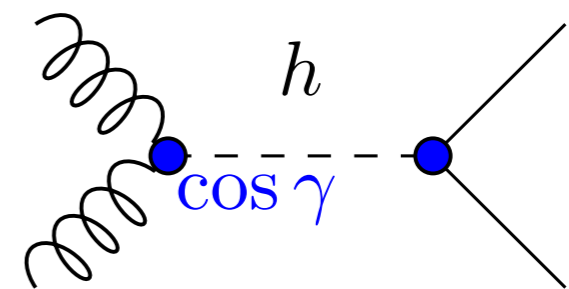


$$\sigma_\phi = \sigma_{\text{SM}}(m_\phi) \times \sin^2 \gamma$$

- ▶  $\phi$  decays to SM:

$$\text{BR}_{\phi \rightarrow VV, ff} = \text{BR}_{\text{SM}}(m_\phi) [1 - \text{BR}_{\phi \rightarrow hh}]$$

- ▶ Higgs signal strengths:



$$\mu_h = \mu_{\text{SM}} \times \cos^2 \gamma$$

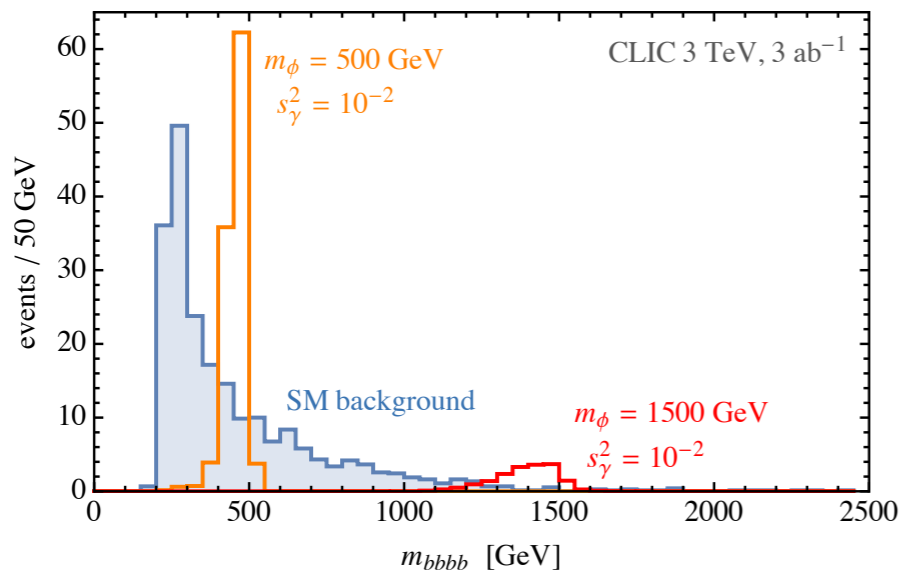
$\phi$  is like a heavy SM Higgs with narrow width +  $hh$  channel

# Resonant hh & VV searches

Main decay channels:  $\phi \rightarrow hh, WW, ZZ$ .

$$\text{BR}_{\phi \rightarrow VV} \approx 1 - \text{BR}_{\phi \rightarrow hh} \quad VV \text{ and } hh \text{ channels are complementary}$$

- Cut & count experiment around resonance



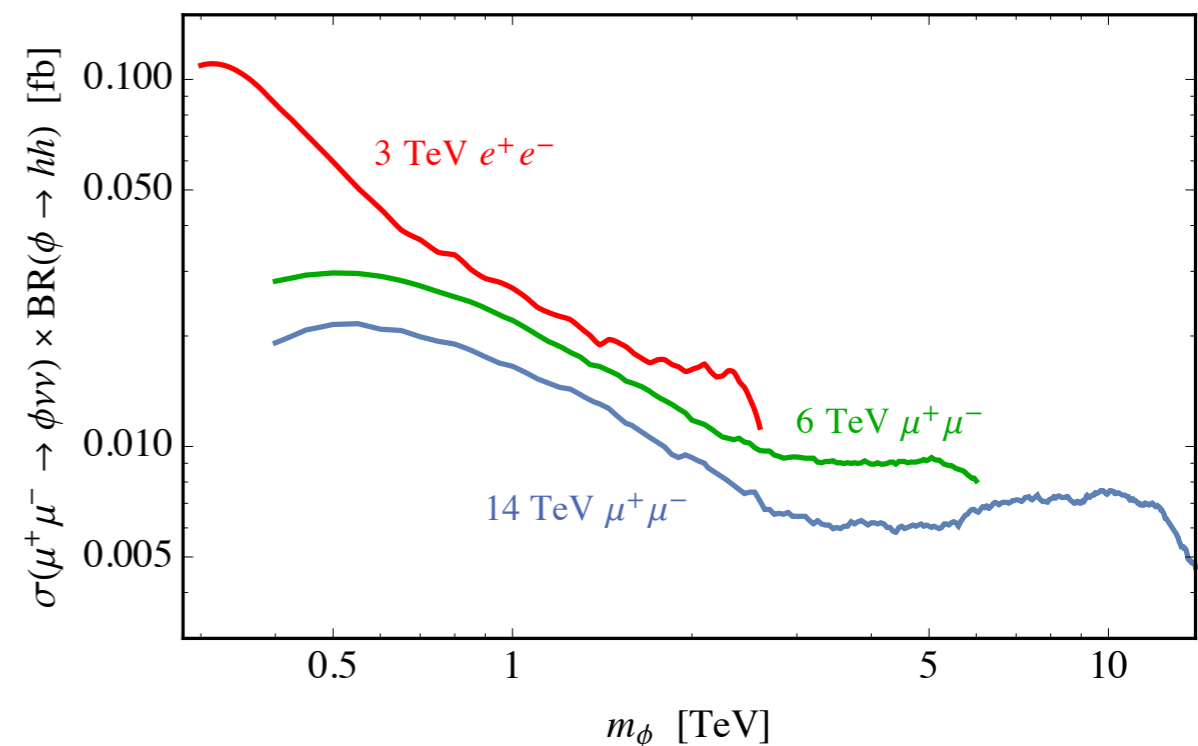
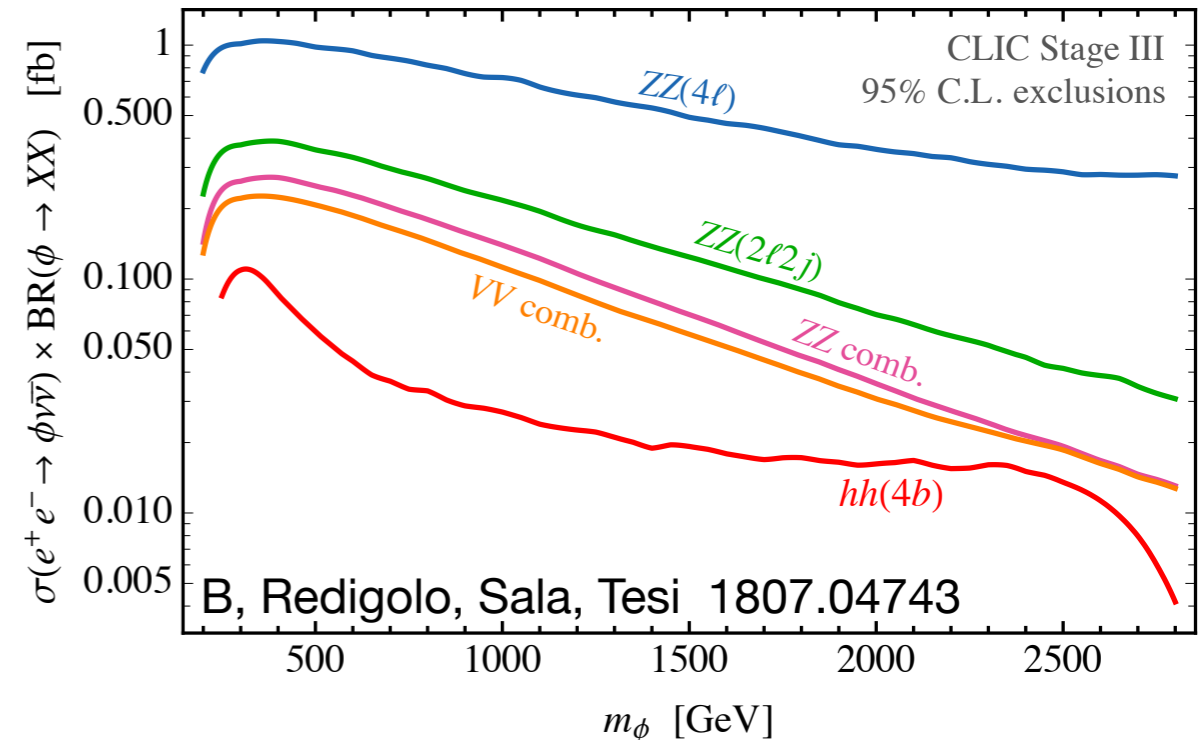
- Very small background at high masses, the error is dominated by statistics

$$\text{In the limit of no bkg: } [\sigma_{95\%} \times \text{BR}] \simeq 3/\mathcal{L}$$

- Parton-level analysis for  $\phi \rightarrow hh(4b)$ :

Identification cut:  $m_{4b} = m_\phi \pm 15\%$   
b-tag efficiency 30%

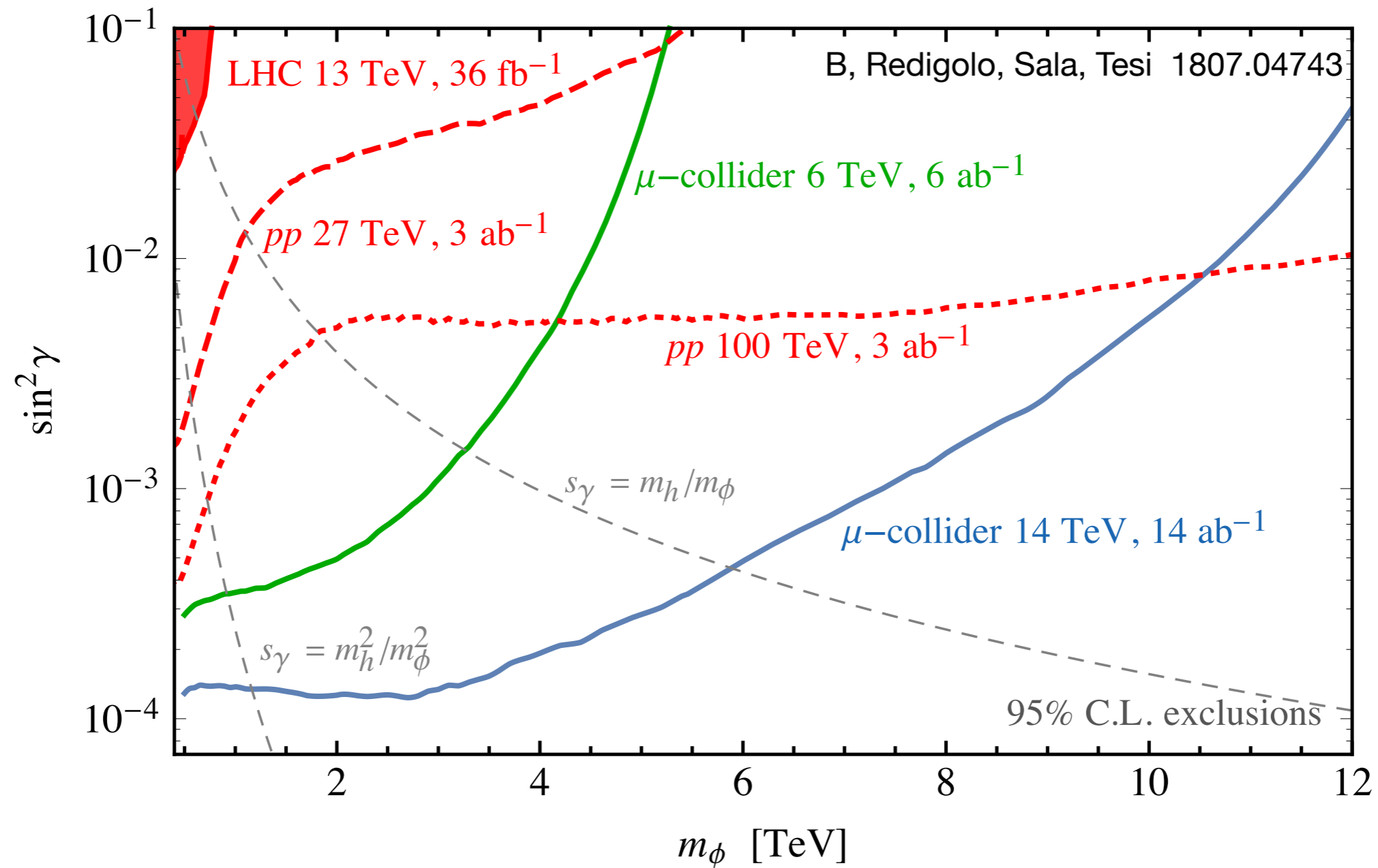
(validated with simulation at 3 TeV CLIC)



# Direct vs indirect

Compare the reach of very high energy lepton & hadron colliders

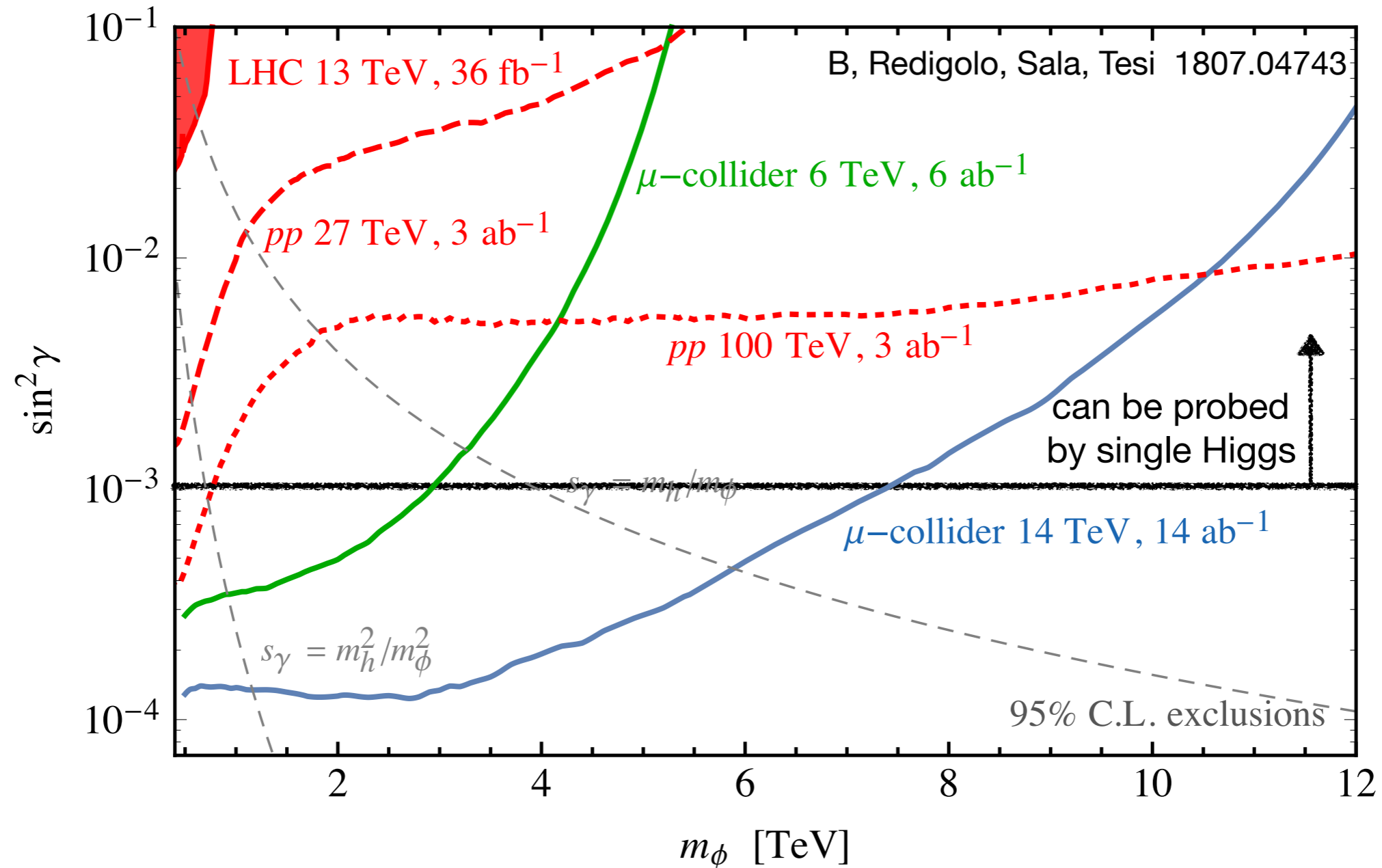
$$\sin^2 \gamma \approx \Delta\mu_h / \mu_h^{\text{SM}} \approx \sigma_{VV \rightarrow \phi} / \sigma_{VV \rightarrow h}^{\text{SM}}$$



# Direct vs indirect

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$$\sin^2 \gamma \approx \Delta\mu_h / \mu_h^{\text{SM}} \approx \sigma_{VV \rightarrow \phi} / \sigma_{VV \rightarrow h}^{\text{SM}}$$



For this class of models, a high-energy  $\mu^+\mu^-$  collider has an amazing reach if compared to single Higgs meas. or direct searches at a 100 TeV pp collider



# Applications: SUSY (the NMSSM)

Three Higgs fields:  $H_u, H_d$  doublets +  $S$  singlet  $\mathcal{W} = \mathcal{W}_{\text{MSSM}} + \lambda S H_u H_d + f(S)$

- ◇ Extra tree-level contribution to the Higgs mass
- ◇ Alleviates fine-tuning in  $v$  for  $\lambda \gtrsim 1$  and moderate  $\tan \beta$

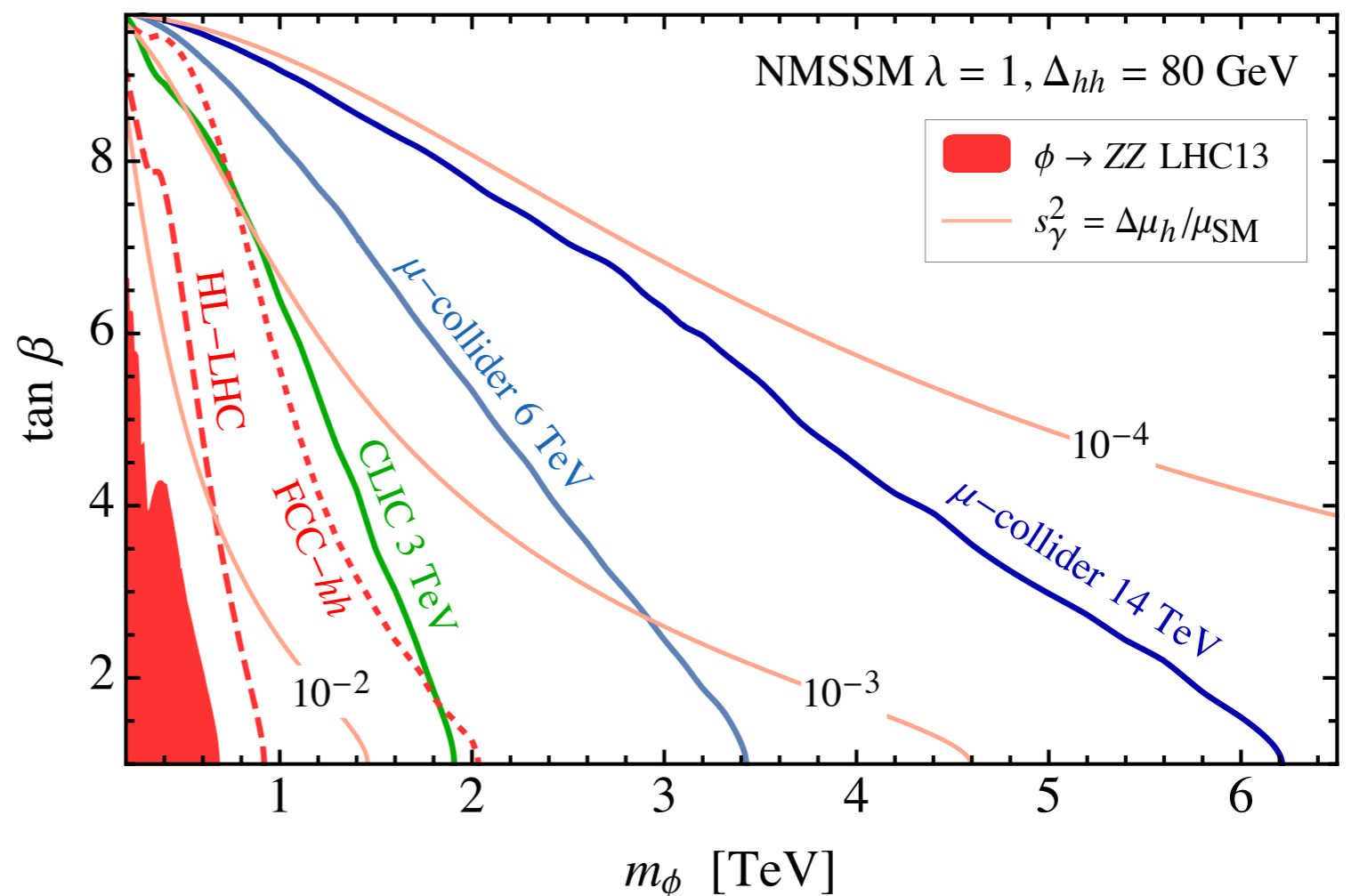
The singlet can be the lightest new state of the Higgs sector

Recast the previous bounds:

$$\sin^2 \gamma = \frac{M_{hh}^2 - m_h^2}{m_\phi^2 - m_h^2}$$

$$M_{hh}^2 = m_Z^2 c_{2\beta}^2 + \lambda^2 v^2 s_{2\beta}^2 + \Delta^2$$

loop correction to Higgs mass from top-stop



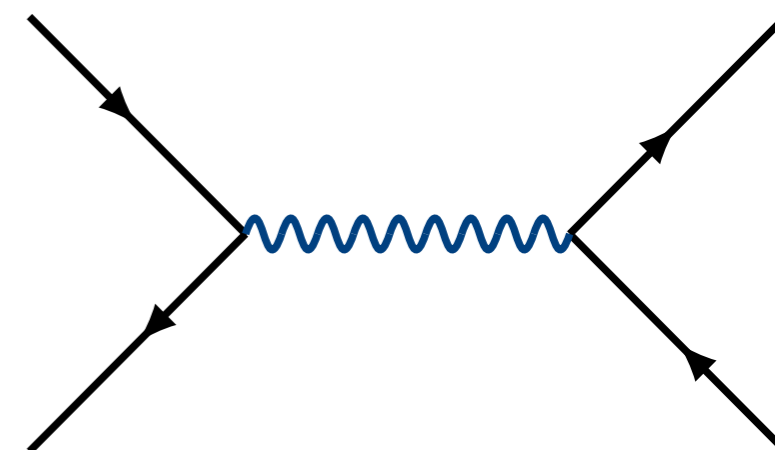
Weakly coupled & low mass: direct searches very powerful!

➡ see Andrea's talk for sparticle production!

# More resonances: $Z'$

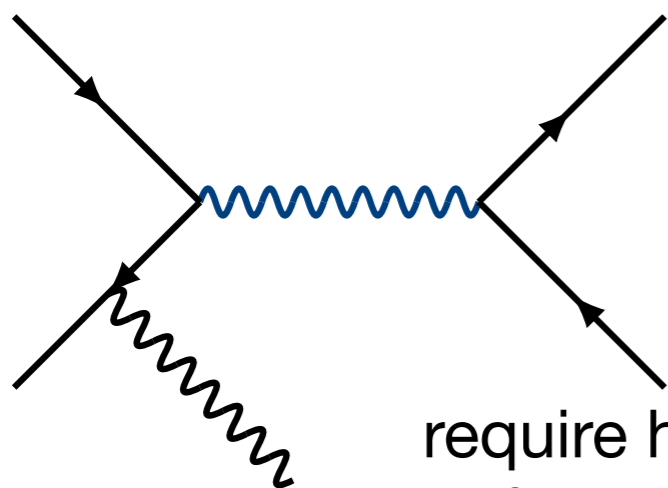
Most typical example of direct search:  
heavy s-channel resonance produced in Drell-Yan

If  $Z'$  produced on-shell, very large cross-section



Problem: how do we look for resonances of unknown mass at fixed  $\sqrt{s}$ ?

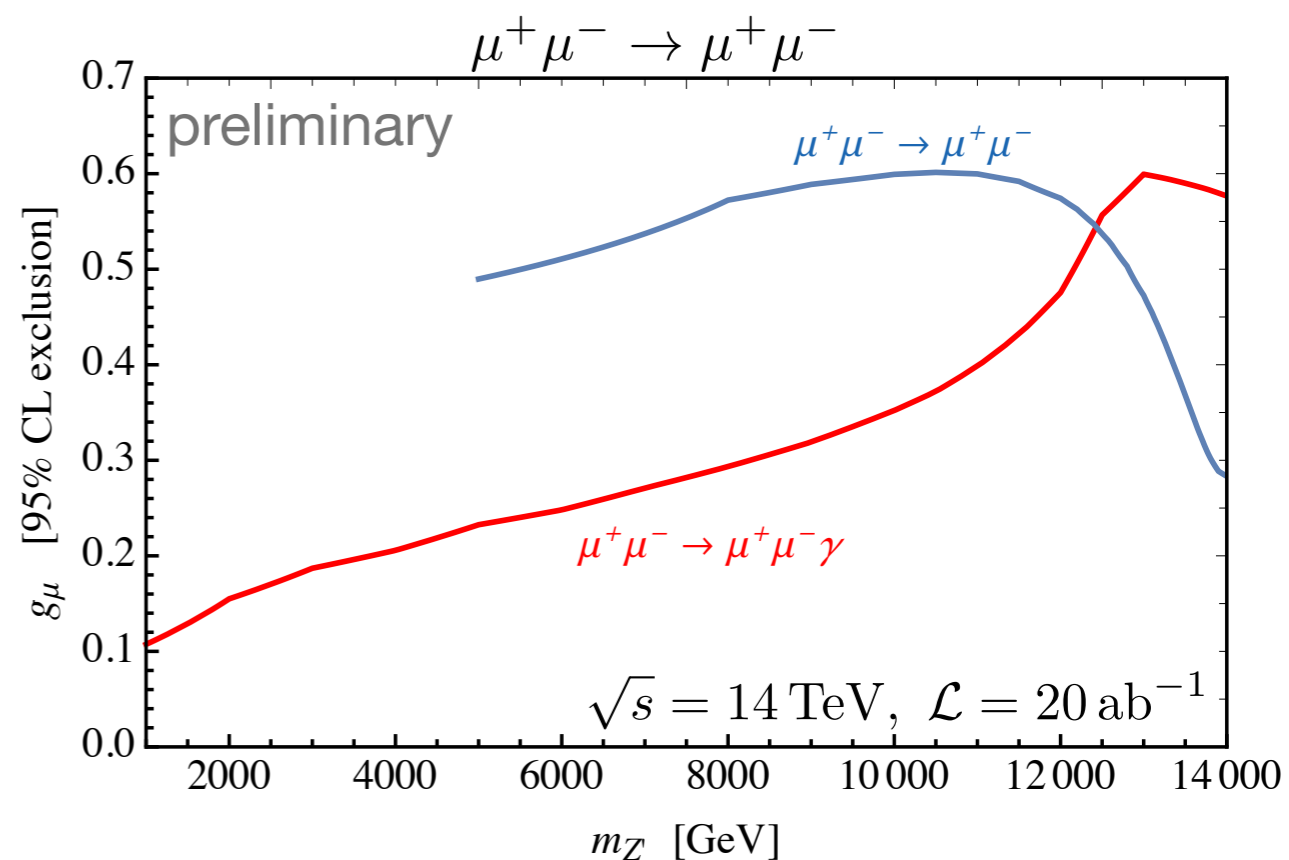
I. “Radiative return”: produce resonance on-shell with ISR



require hard photon

$$M^2 = m_{\ell\ell}^2 = s - 2\sqrt{s}E_\gamma$$

II. Off-shell  $Z'$  exchange  
( $\mu\mu \rightarrow f\bar{f}$  cross-section)

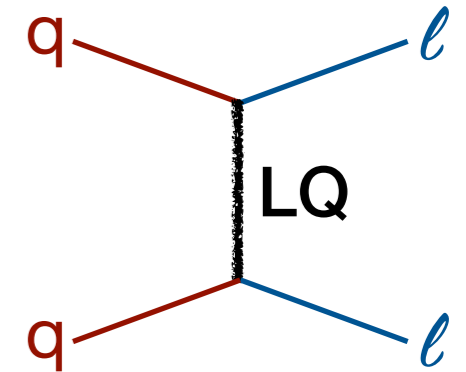


kinematical cuts:  $p_T > 20 \text{ GeV}, |\theta| > 5^\circ$

QED corrections  $\approx \frac{2\alpha}{\pi} \log \frac{s}{m_\mu^2} \lesssim 10\%$

# Coloured resonances: 3rd generation leptoquarks

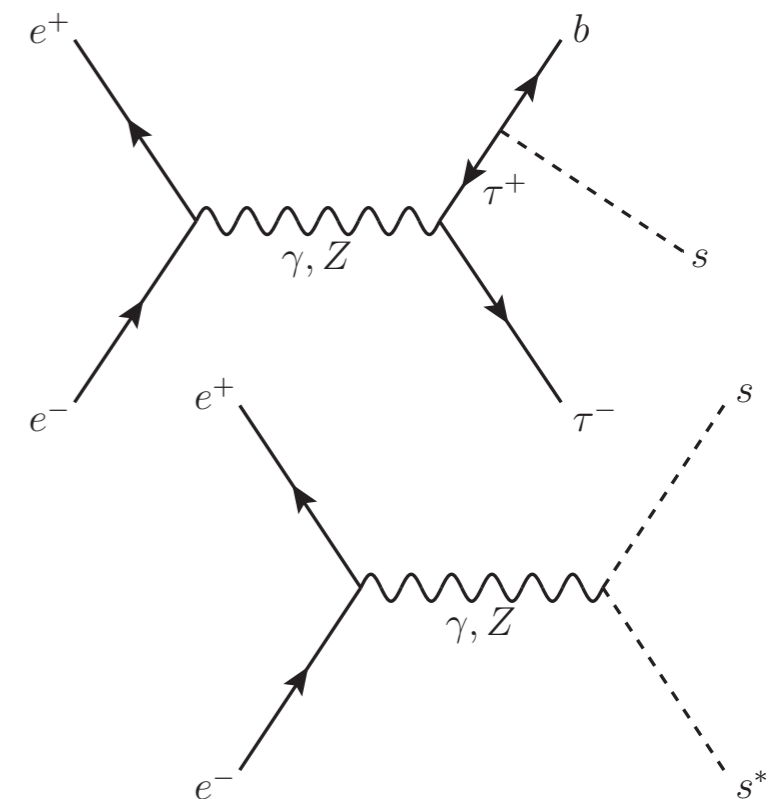
- ◆ Different signature compared to more “standard” BSM
- ◆ Interesting: NP coupled to 3rd generation fermions (*B physics anomalies!*)
- ◆ Can be either scalar or vector
- ◆ Difficult searches at LHC: High Lumi reach  $\sim 1.5$  TeV



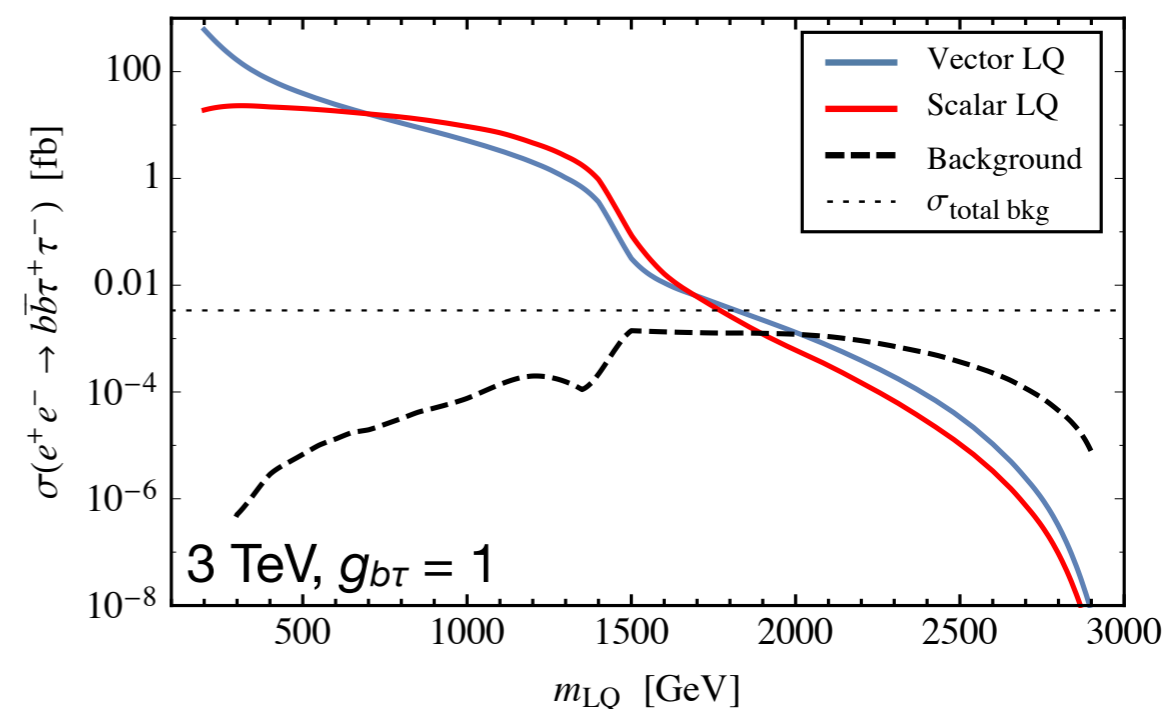
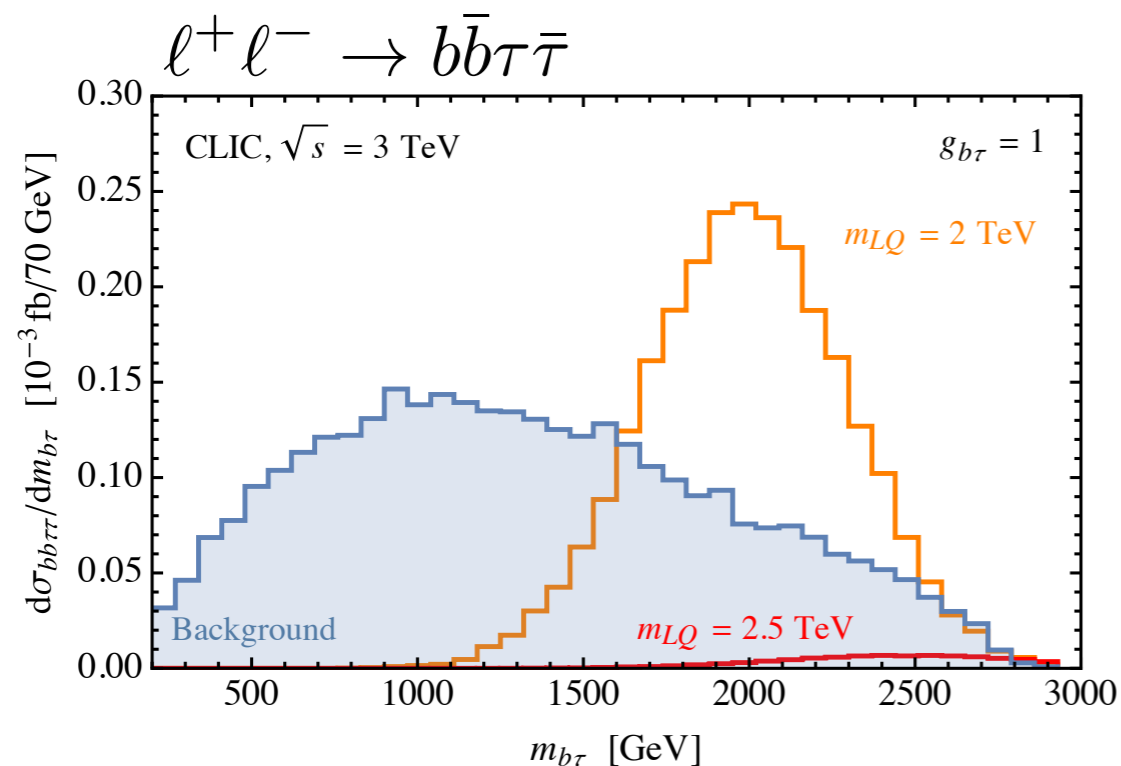
→  $\sqrt{s} > 3$  TeV interesting range for lepton colliders

## 3rd generation LQ production at a lepton collider:

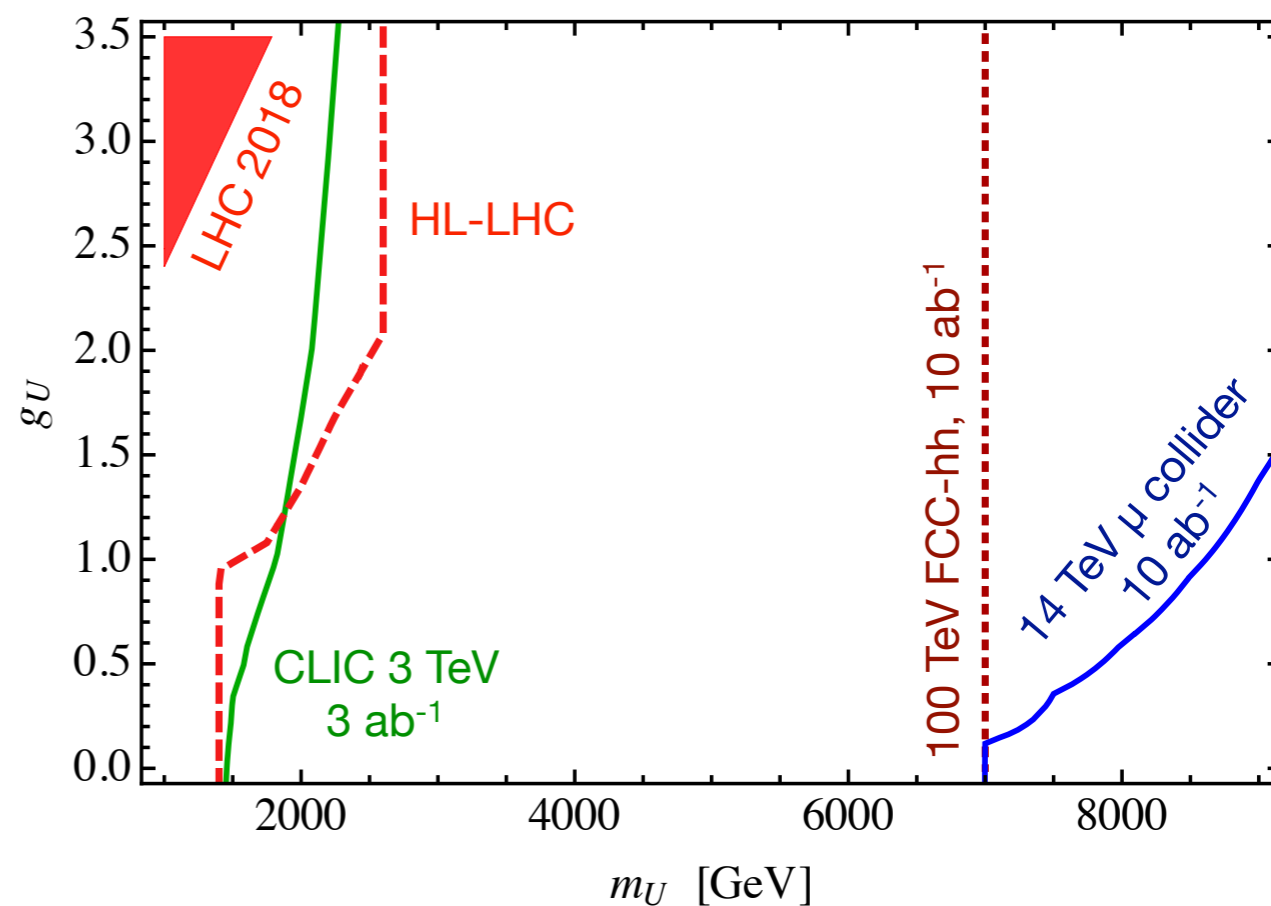
- Pair production: large cross-section when allowed, does not depend on coupling to fermions
- Single production: radiation from  $bb$  or  $\tau\tau$  pair
  - $bb\tau\tau$  final state, with  $m_{b\tau} \sim M_{LQ}$



# Coloured resonances: Leptoquarks



- ◆ Search is almost background-free:  
We set a bound simply by requiring 10 signal events
- ◆ The main limitation for CLIC is the c.o.m. energy: room for huge improvement at a  $\mu$ -collider



# Conclusions

A muon collider would be a “dream machine” for BSM physics:  
a way to access multi-TeV c.o.m. energies in a clean environment

- ◆ Would allow to reach **unmatchable precision in EW & Higgs physics** by means of high-energy scattering processes  
*(in some cases corresponding to a  $10^{-7}$  accuracy in pole observables)*
- ◆ **Powerful discovery machine**: direct reach often much better than what is attainable both at hadron machines and through precision measurements  
*EW scalars, vector resonances, coloured objects...*

*(Unfortunately) this is not a comparison with other future colliders...*

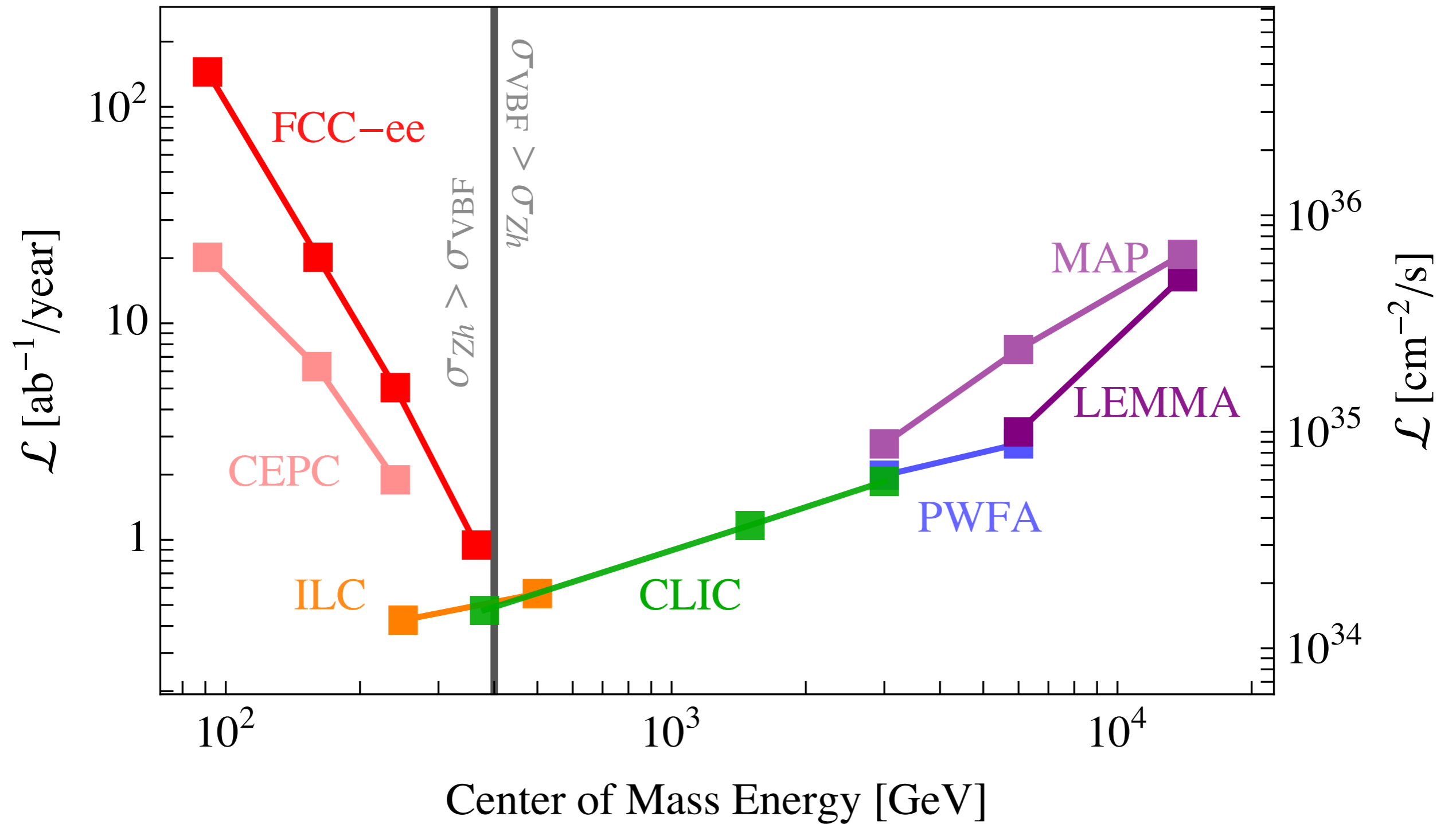
*... but a motivation to study the feasibility of such a machine*





Backup

# High Energy Lepton Colliders



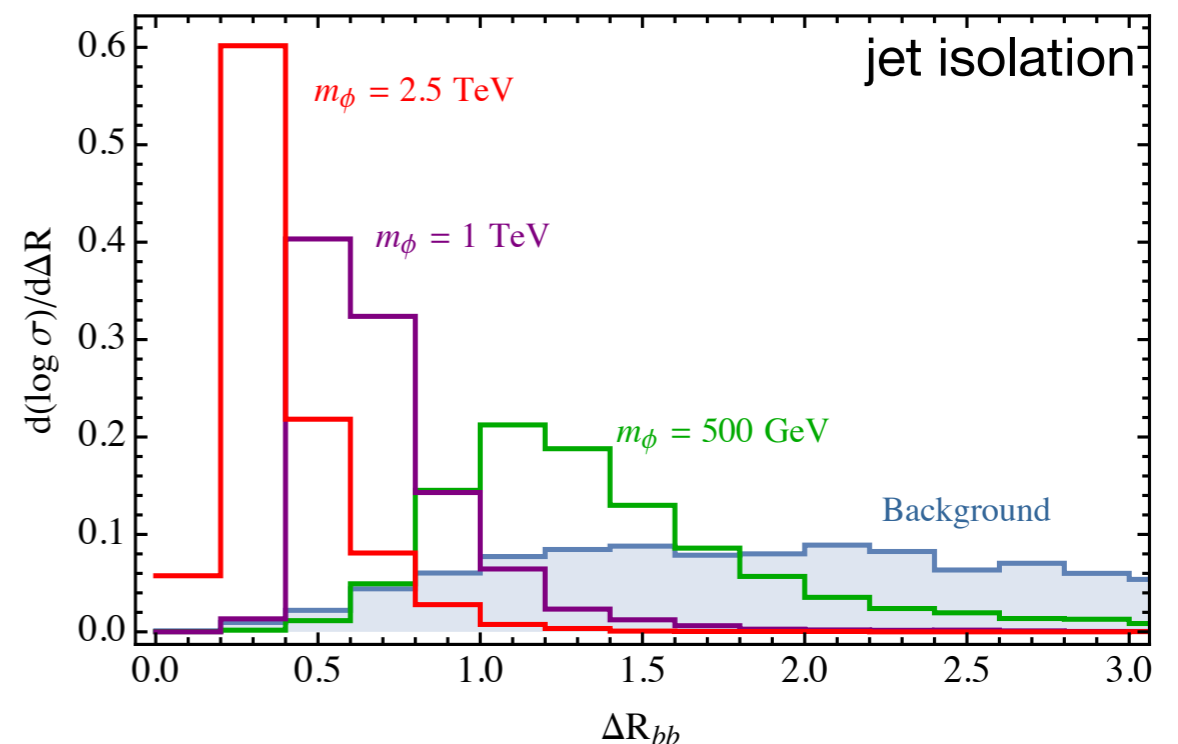
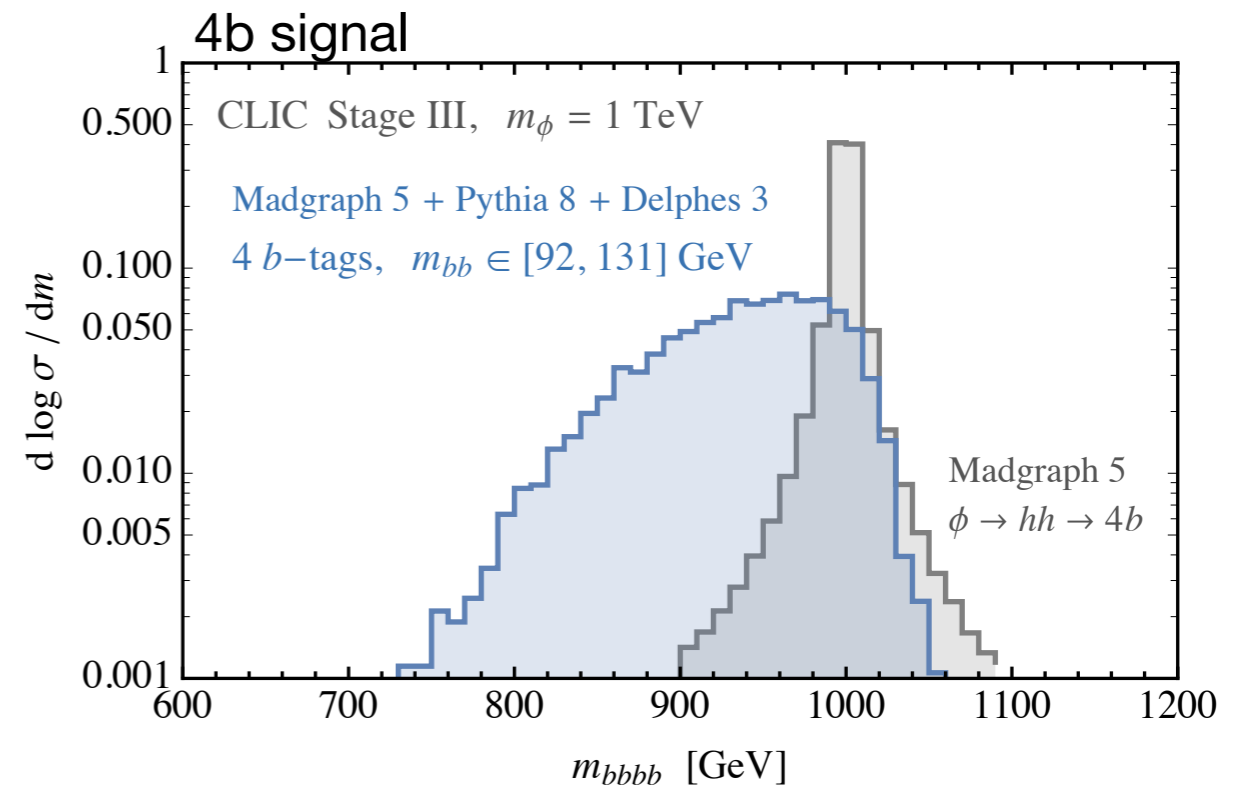
# $hh \rightarrow 4b$ at CLIC

Main backgrounds:  $hh$ ,  $ZZ$ ,  $Zh$ . We simulate the full process  $e^+e^- \rightarrow 4b + 2\nu$

- Detector simulation with CLICdp Delphes card  
(thanks to Ulrike Schnoor for support!)
- VLC exclusive jet reconstruction,  $N = 4$ ,  $R = 0.7$
- 4 b-tags (loose tagging algorithm)
- h reconstruction: select the b pairs that give the best fit to two 125 GeV Higgs bosons,  $90 \text{ GeV} < m_{bb} < 130 \text{ GeV}$
- $\phi$  reconstruction:  $0.75 m_\phi < m_{4b} < 1.05 m_\phi$
- Other cuts:  $p_T > 20 \text{ GeV}$ ,  $E_{\text{miss}} > 30 \text{ GeV}$ ,  $|\cos \theta_h| < 0.9$

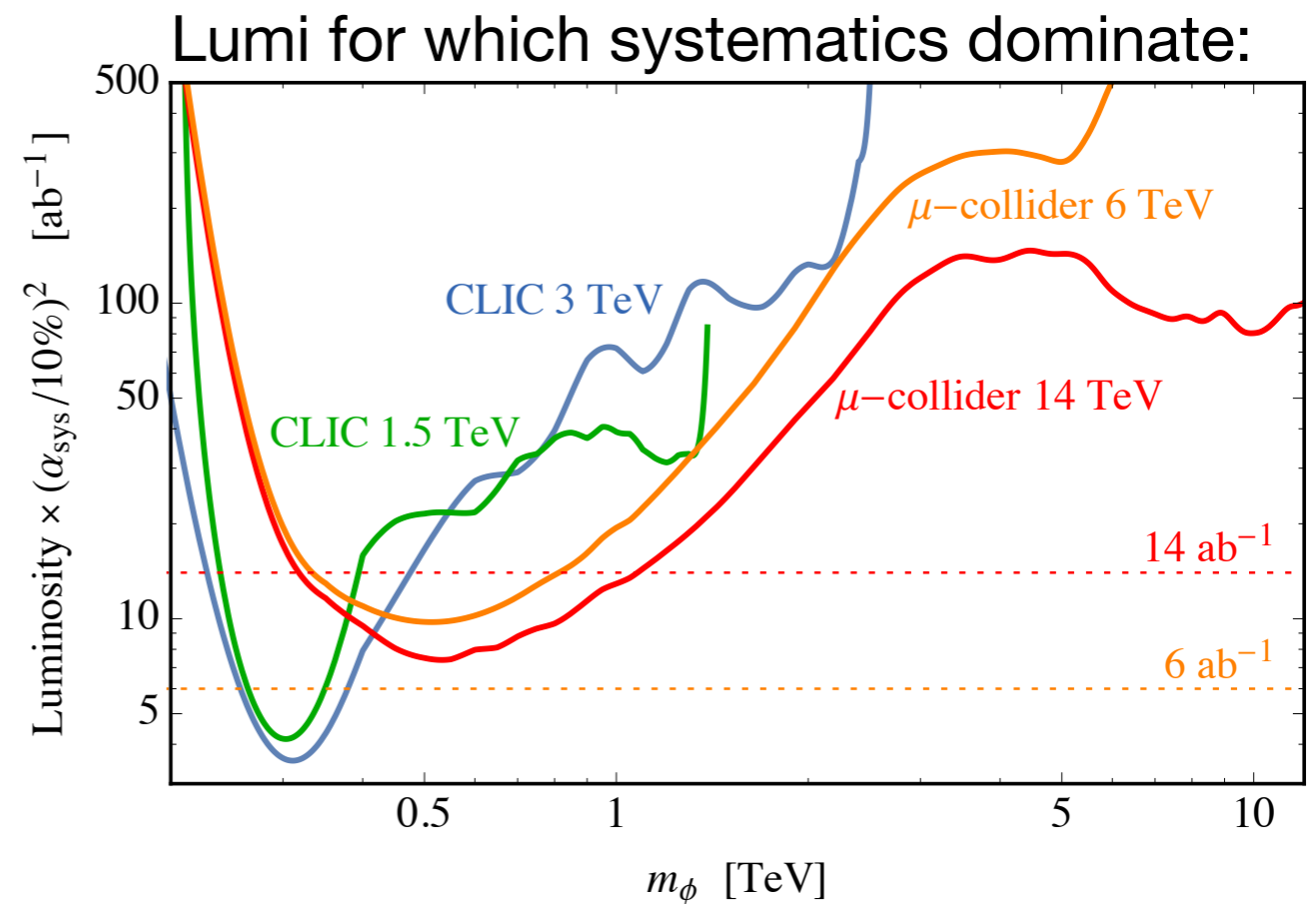
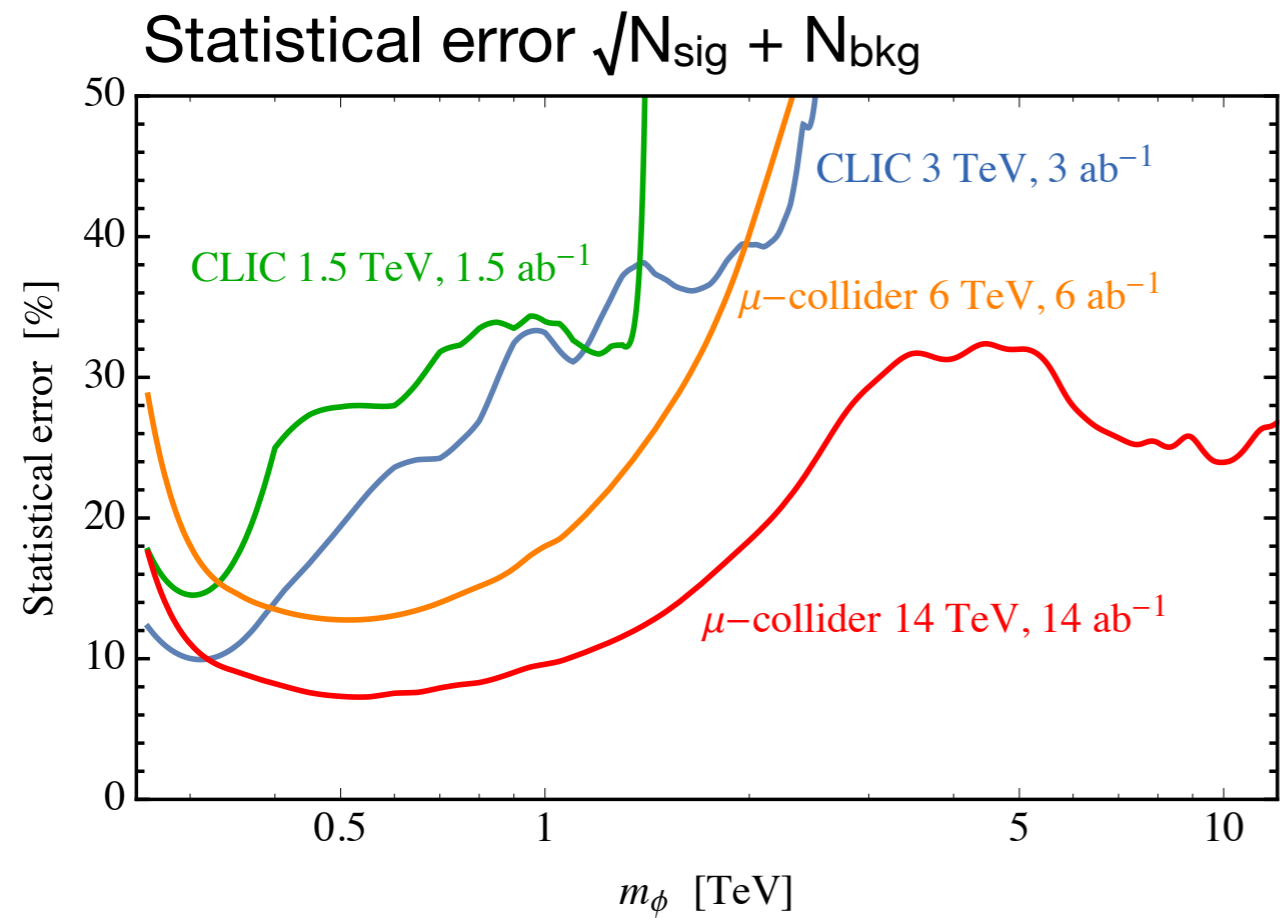
Signal efficiency  $\varepsilon_{\text{sig}} \sim 25 - 30\%$

Background reduced by  $\varepsilon_{\text{bkg}} \sim 10^{-3} - 10^{-4}$





# Statistical vs systematic error



# Applications: Twin Higgs

- ▶ If the Higgs is a pseudo-Goldstone boson,  $\sin^2 \gamma \sim v^2 / f^2$
- ▶ **Example: Twin Higgs**

Higgs mass is protected from radiative corrections without new light colored states

Model-independent tests:

- ✓ Higgs couplings
- ✓ Search for the singlet

B, Redigolo, Sala, Tesi 1807.04743  
(see also 1711.05300)

