



Fast Acceleration of Muons: RCS as accelerator and as collider ring, HTS magnet R&D

Vladimir SHILTSEV (Fermilab)

Muon Collider – EPPSU Preparatory Meeting, CERN

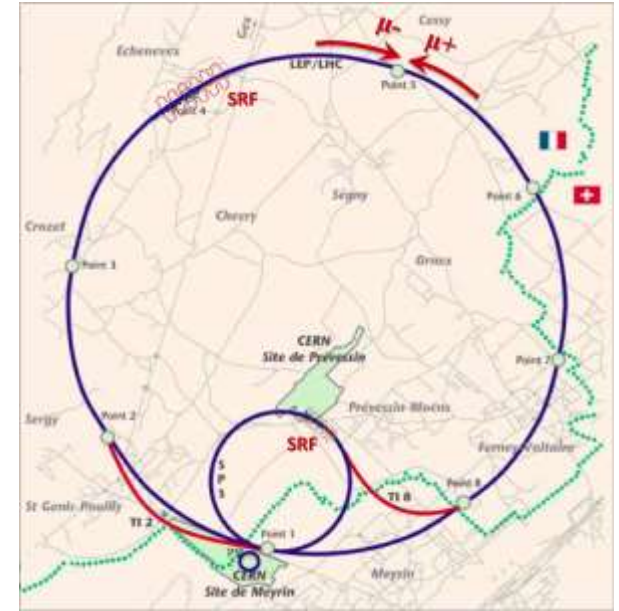
11 April 2019

Muon Collider : Where's the cost hidden?

- *ee linear*
 - ILC
 - CLIC
- *ee circular*
 - LEP3
 - FCC-ee
 - CepC
 - HF-FNAL

Cost Considerations : eg 14 TeV

- reuse the existing 27 km LHC tunnel, the 7 km SPS tunnel and most of CERN infrastructure.
- Beyond that – only very rough estimates (so called “ $\alpha\beta\gamma$ -law”)



$$\text{Total Project Cost} \approx \alpha \times (\text{Length}/10\text{km})^{1/2} + \beta \times (\text{Energy}/\text{TeV})^{1/2} + \gamma \times (\text{Power}/100\text{MW})^{1/2}$$

- the incremental cost : “**PS**” configuration 2B\$ × sqrt(14TeV of SC magnets) + 10 B\$ × sqrt(0.02TeV of SRF) = **8.9 ± 3 B\$**.
- “**MAP**” configuration : extra ~10B\$ × sqrt(0.008 TeV of SRF) + 2B\$ × sqrt(0.2 for 20 MW) = **1.8 ± 0.6 B\$**.
- “**LEMC**” configuration : extra ~1B\$ × sqrt(0.045 TeV e+ ring) + 10B\$ × sqrt(0.001 TeV SRF) + 2B\$ × sqrt(2.5 250 MW power) = **3.6 ± 1.2 B\$**

On the feasibility of a pulsed 14 TeV c.m.e. muon collider in the LHC tunnel

! WARNING !

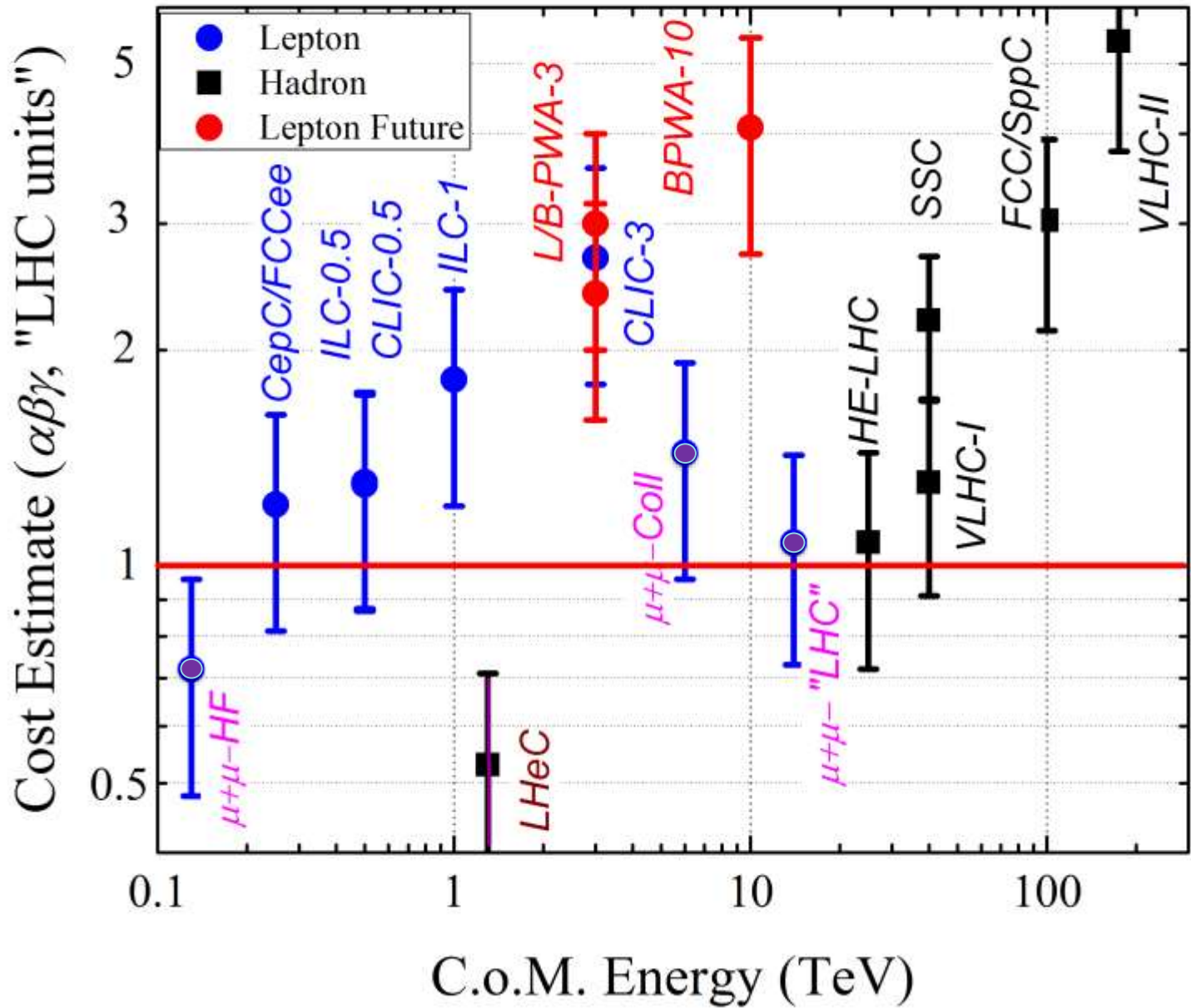
$\alpha\beta\gamma$ - Cost Estimate Model:

$$\text{Cost(TPC)} = \alpha L^{1/2} + \beta E^{1/2} + \gamma P^{1/2}$$

- a) $\pm 33\%$ estimate, for a “green field” accelerators
- b) “US-Accounting” = TPC ! ($\sim 2\text{-}2.5 \times$ *European Accounting*)
- c) Coefficients (units: 10 km for L , 1 TeV for E , 100 MW for P)
 - $\alpha \approx 2\text{B}\$/\text{sqrt}(L/10 \text{ km})$
 - $\beta \approx 10\text{B}\$/\text{sqrt}(E/\text{TeV})$ for SC/NC RF
 - $\beta \approx 2\text{B}\$ /\text{sqrt}(E/\text{TeV})$ for SC magnets
 - $\beta \approx 1\text{B}\$ /\text{sqrt}(E/\text{TeV})$ for NC magnets
 - $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$

USE AT YOUR OWN RISK!

Energy Frontier Colliders in "LHC Units" (~10B\$ TPC)



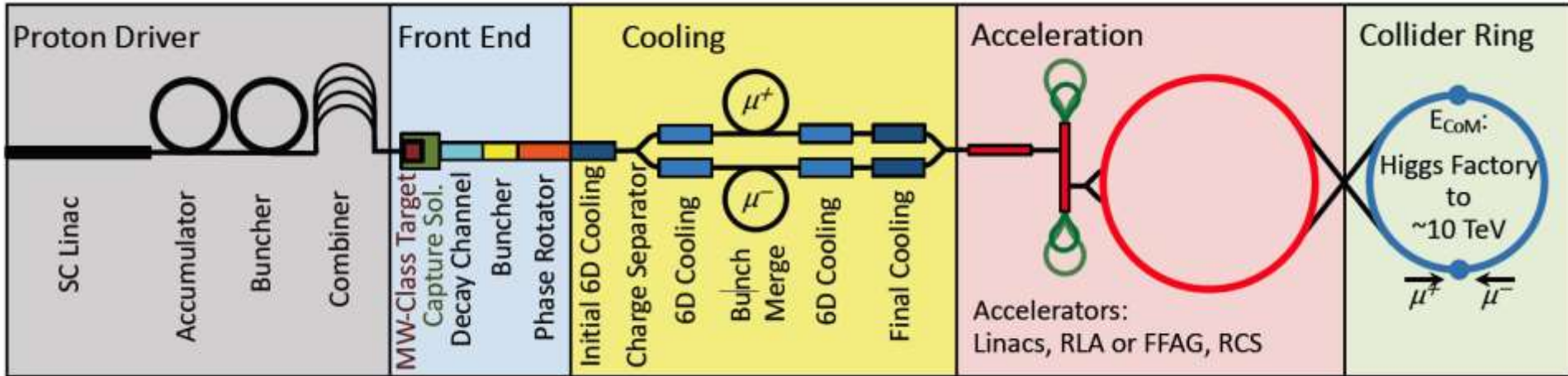
Muon Collider : Where's the Cost Hidden?



$\mu^+\mu^-$ captured,
bunched and cooled

Acceleration to
collision energy

Collision



4-8 GeV, 4 MW
proton driver

Some 4 GeV of NC RF and
~100 m 4T SC solenoids +
few 20T ones

~14-60+ GeV SRF in
2 RLAs (1 – 6+ km)

3-14 TeV SC
magnets, 6-
27 km

10-15% for new
4 MW
“0” if 0.4-1 MW
is enough

7-15%
1/2 RF
1/2 SCM

35-50%
1/3 SRF
1/3 Civil
1/3 Infrastr

40-50%
2/3 SCM
1/3 Civil

What can be used to save big?

- RF is ~5-10 x more expensive than SC – NC magnets
- Minimize RF → eg (from Daniel's talk)

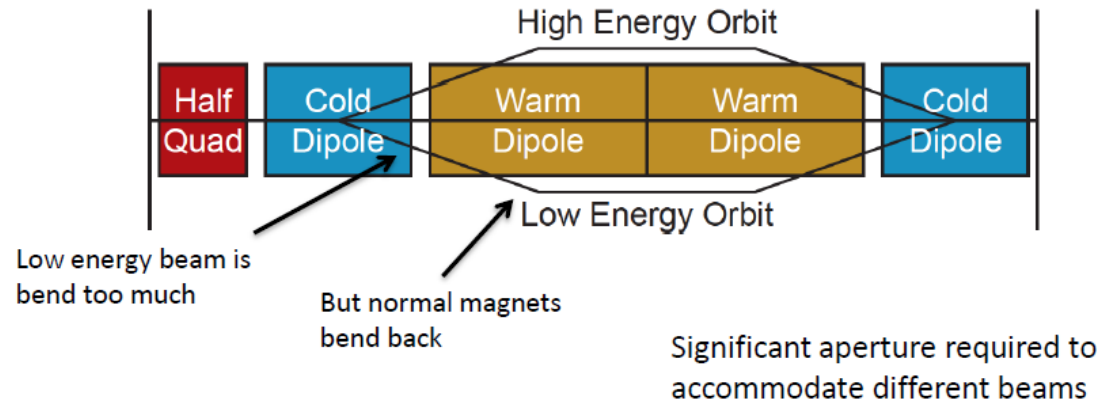
Rapid Cycling Synchrotron

Use fast ramping normal conducting magnets

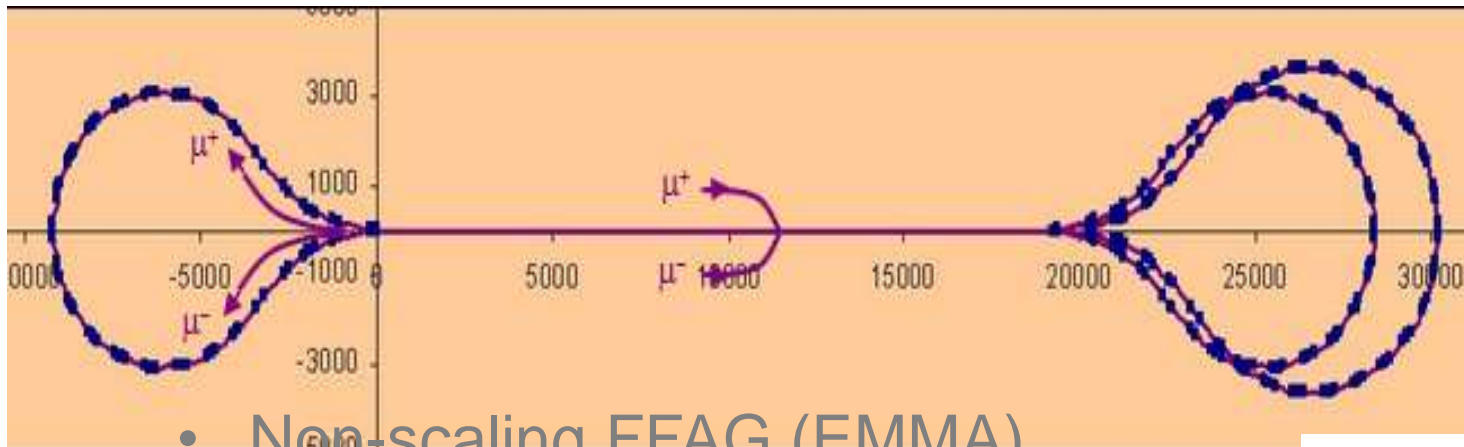
- Limits field to 1.4-2 T

Use mixture of high field static magnets and fast ramping normal conducting magnets

- Normal magnets change sign
- Can about double the effective field reach



How much energy is required to ramp magnets?
Can some be recovered?

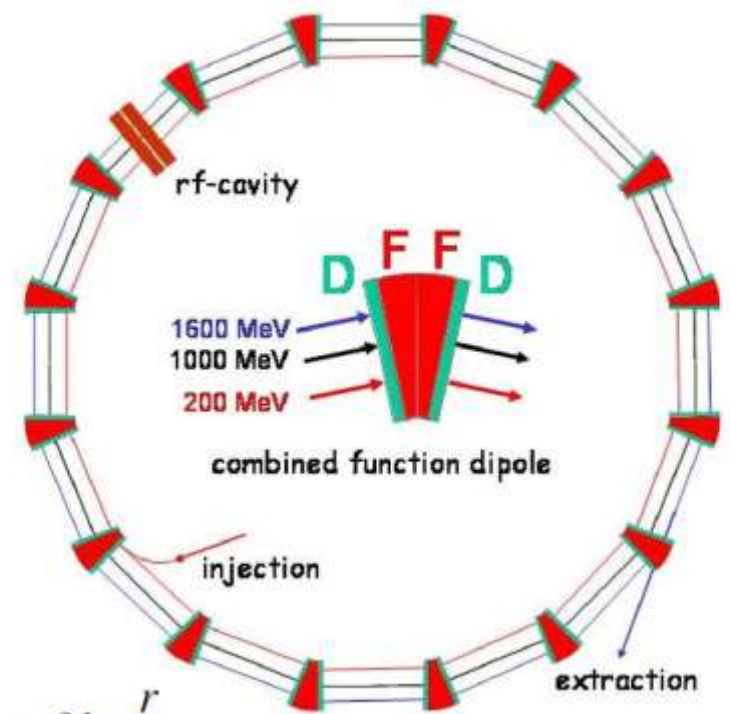
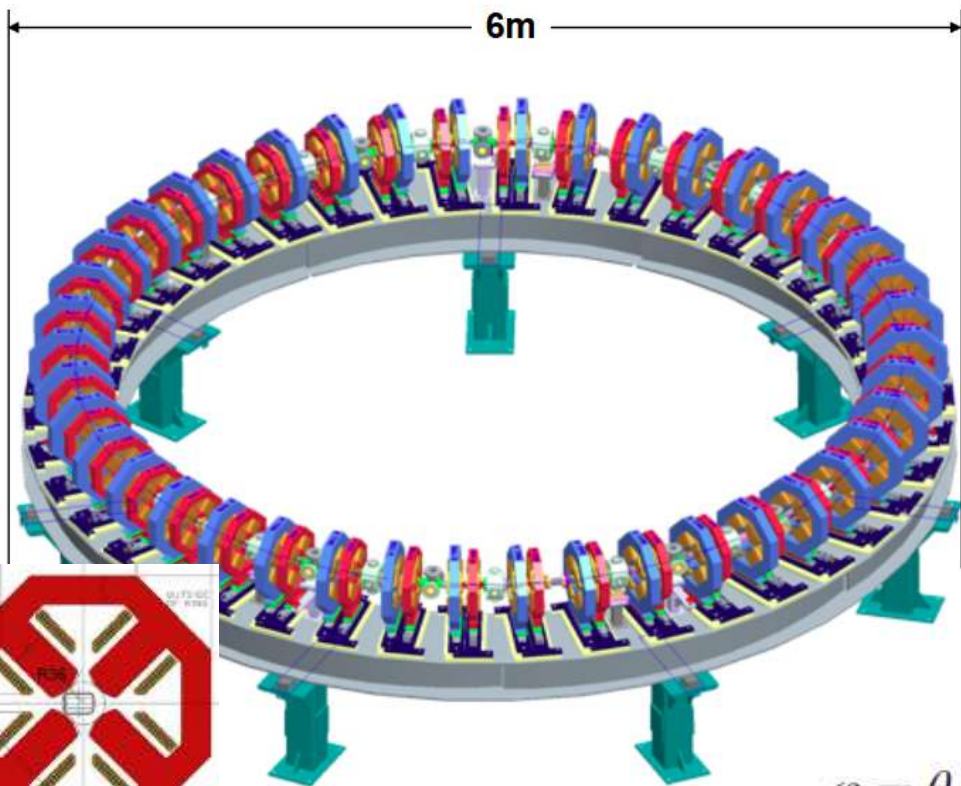


Recirculating Linear Accelerator (RLA)

- Non-scaling FFAG (EMMA)

Alternatives

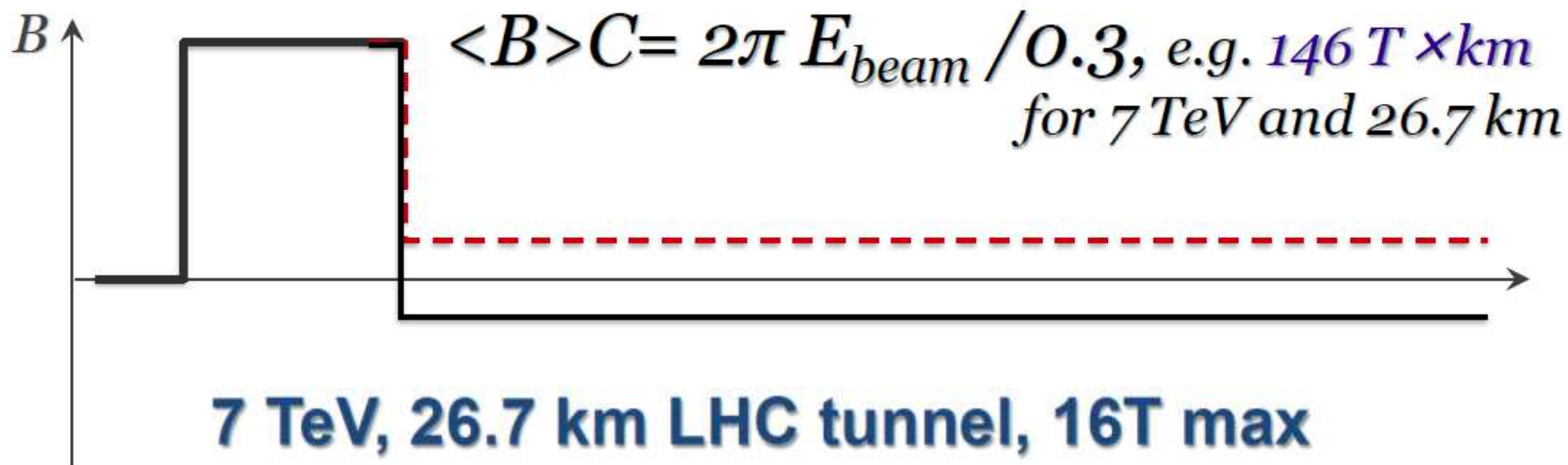
$$B_z(r, \theta) = B_{z0} \left(\frac{r}{r_0} \right)^k F(\varphi)$$



© 1998 Shiltsev | MUMUKHOS and magnets

$$\varphi = \theta - \tan \delta \ln \frac{r}{r_0}$$

Acceleration: (1) pulsed magnets



$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

146 T × km 26.7km 16T 0.85 0.4=1/2.5

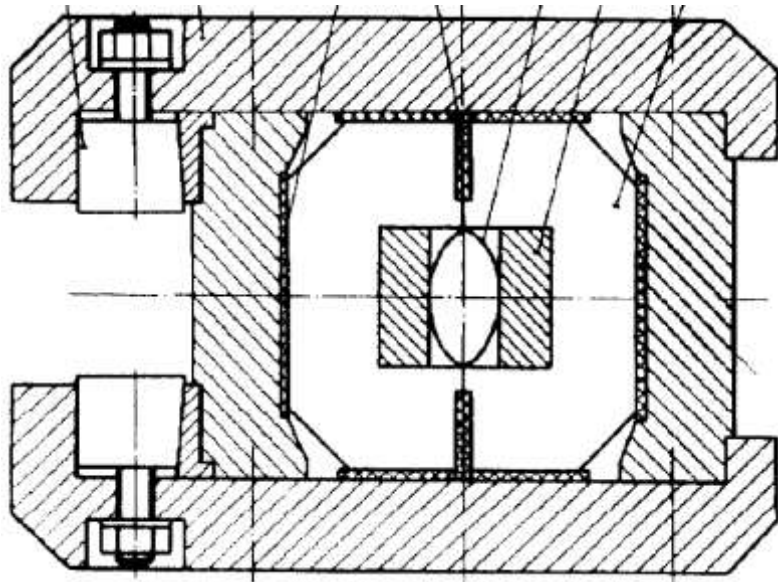
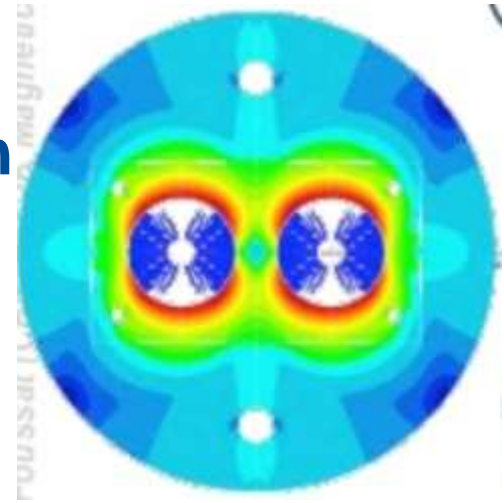
Table 1: Muon RCS accelerator parameters.

	“LHC-S”	“LHC-D”		“SPS”
C , km	26.7	26.7	26.7	6.9
E_{max} , TeV	7	7	4	0.45
E_{inj} , TeV	0.45	4	0.45	0.03
f_{rep} , Hz	5	4	4	20
$\Delta E/\text{turn}$, GeV	14.0	3.5	9.2	3.7
B_{SC} , T	16	16	16	8
L_{SC} , km	4.8	7.1	2.9	0.63
B_{pls} , T	3.8	2.0	1.9	0.8
τ_{ramp} , ms	42	76	34	2.6
dB_{pls}/dt , T/s	180	52	112	615

Magnets:

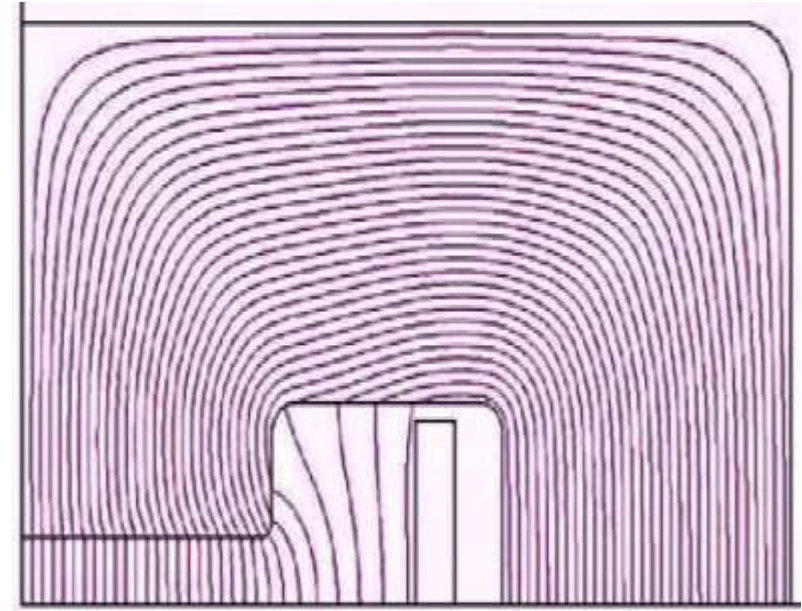
- DC – SC
- Pulsed – NC or SC

FCC 16T Nb₃Sn
Dipole



G.C. Willevald, V.N. Karasynuk, ИЯФ 2006-5
G.I. Silvestrov, T.V. Sokolova ts

5T, 2.8ms, 5Hz, 186kA,
2·10⁶ pulses



HTS 1.75T, ~1000T/s, 25kA

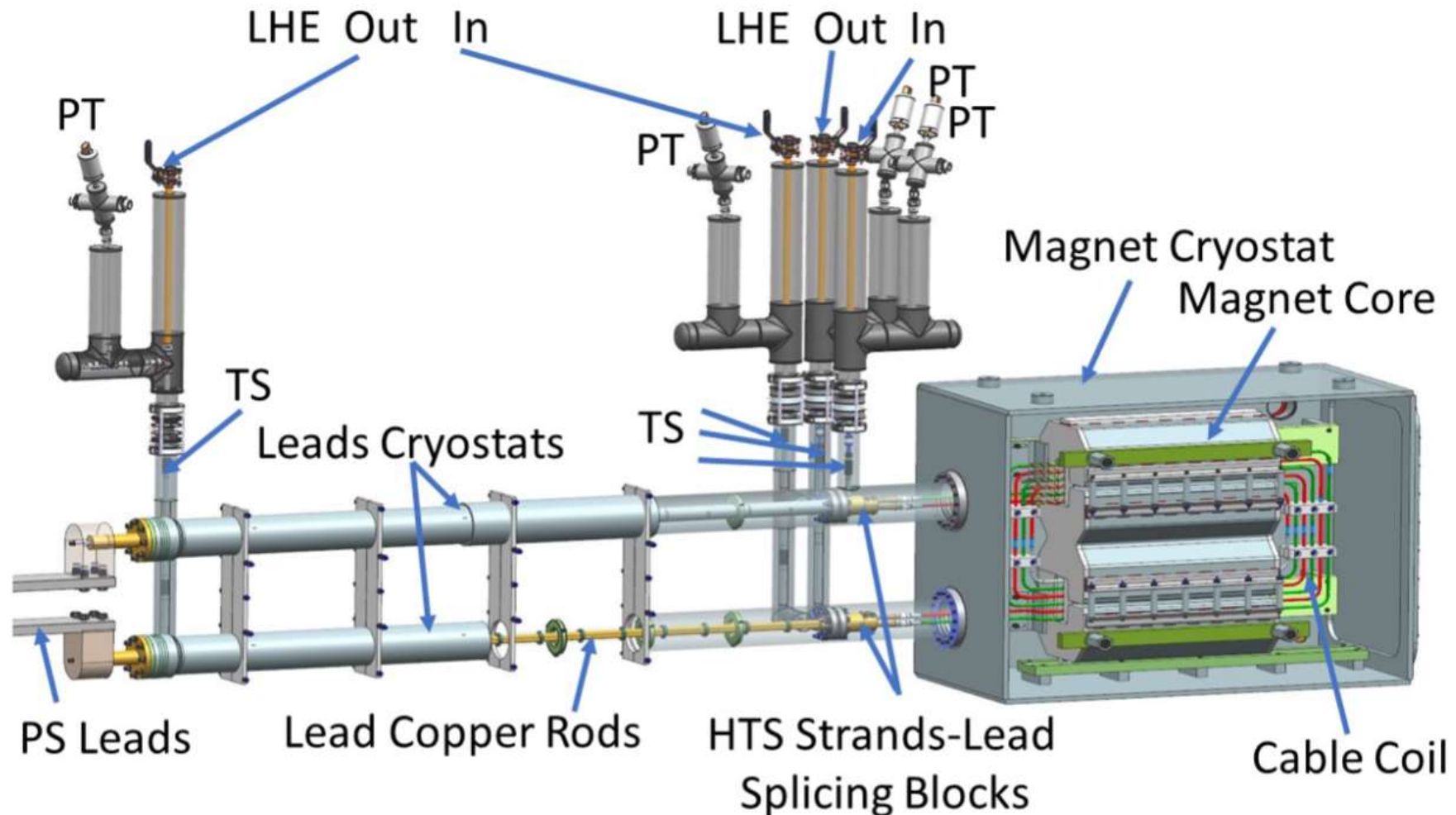
Henryk Piekarczyk VOL. 24, NO. 3, JUNE 2014

Record fast-cycling accelerator magnet based on high temperature superconductors

Henryk Piekarz, Steven Hays, Jamie Blowers, Bradley Claypool, Vladimir Shiltsev

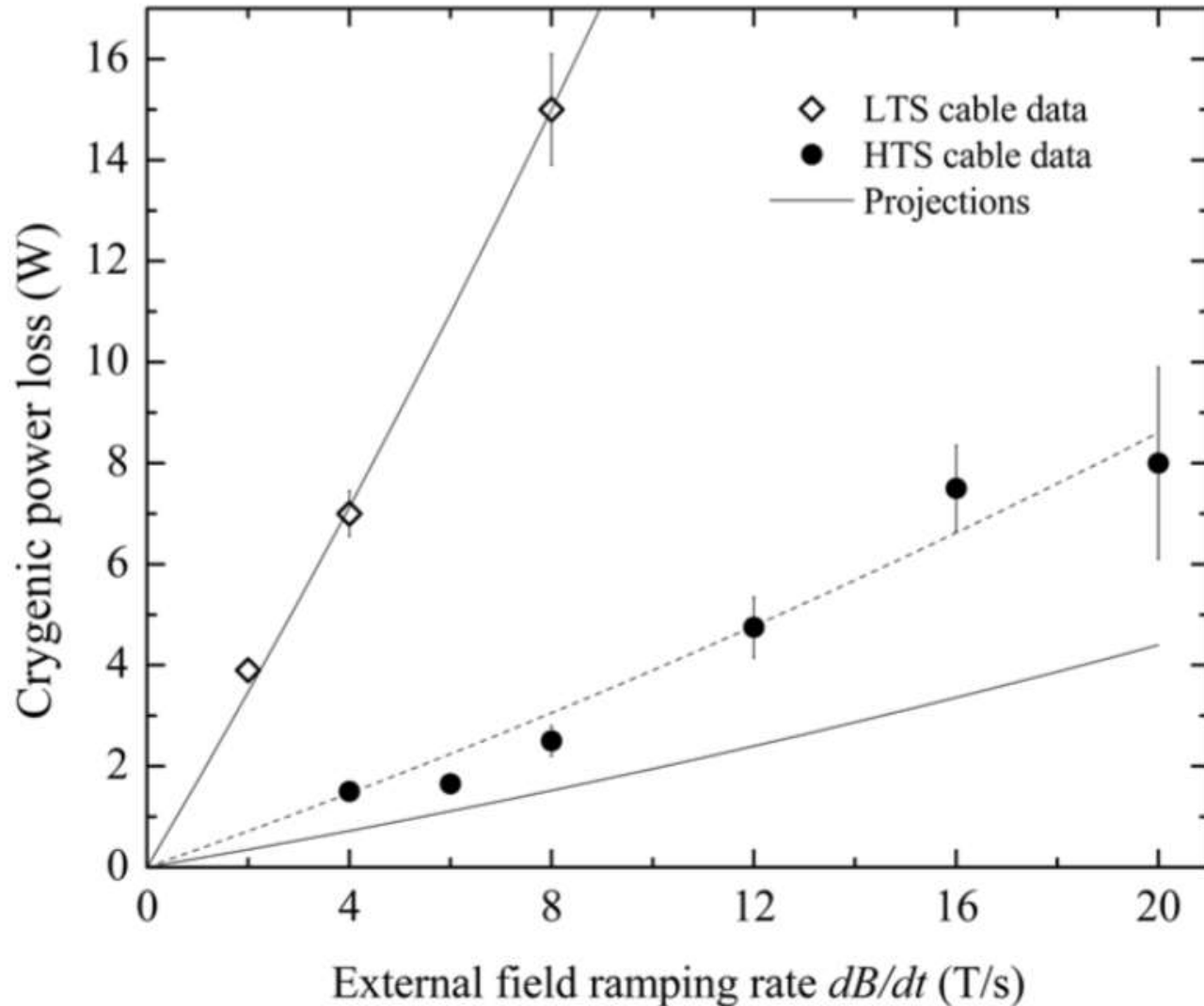
(Submitted on 9 Mar 2019)

arXiv:1903.03853

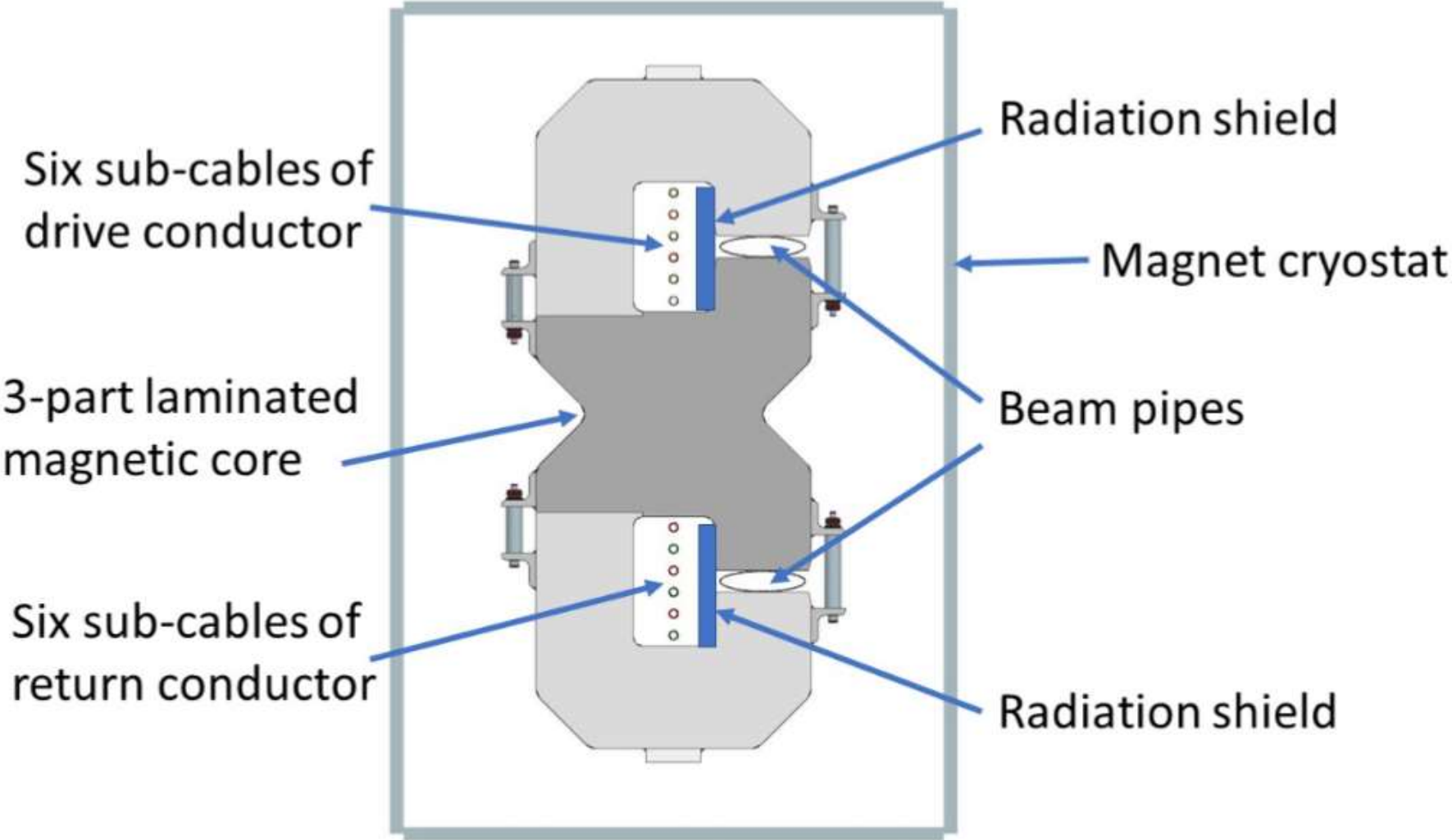




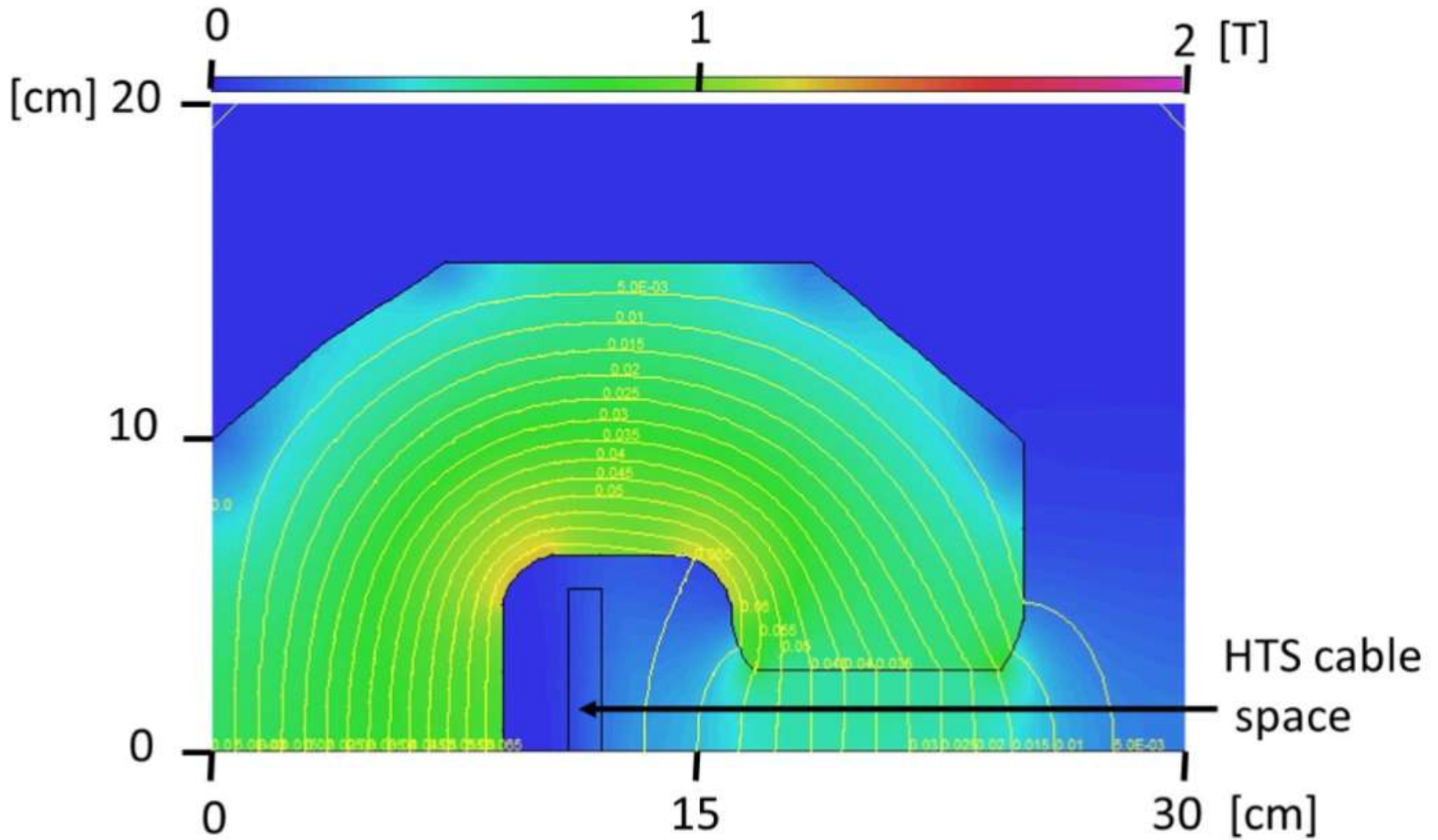
HTS Conductor has Small AC Losses (~ 1/5 – 1/10 LTS) + Operates at Higher T (30-60 K vs 2-4 K)



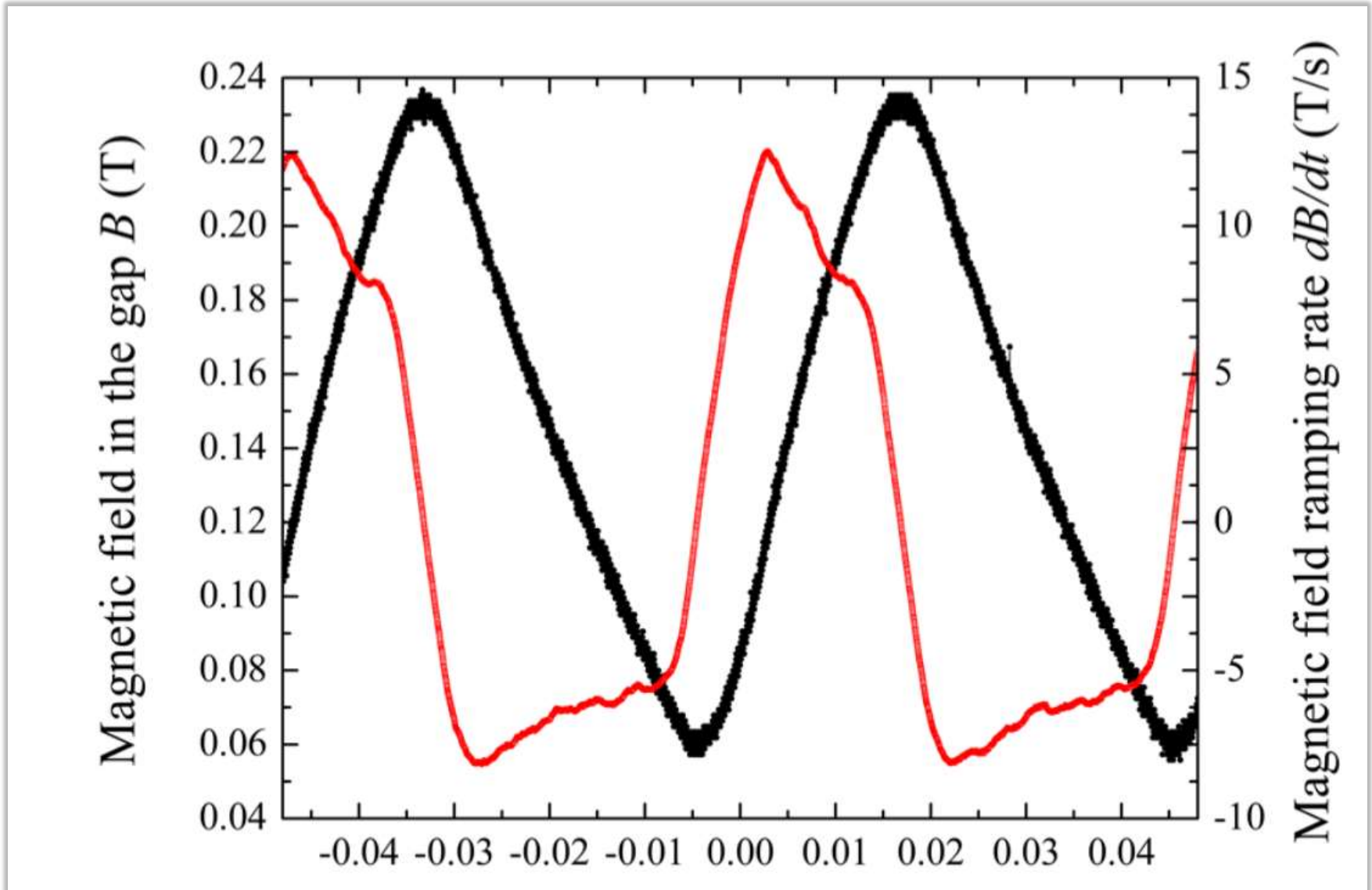
(Accelerator) Double-Bore HTS Magnet



Dipole filed in the gap (1/4 shown)



The result : PS limited (1.5V max) – 12 T/s, 2.4kG



Summary

- **Muon Colliders do have cost advantages**
 - \$\$ total construction cost
 - \$\$ / TeV
 - \$\$ / ab^{-1}
 - Operations
- **Each MC option requires cost optimization**
 - Higgs Factory, 3 TeV, 6 TeV, 14 TeV “LHC”, MAP/LEMC
- **Acceleration system is great part of the cost**
 - RCS might be very cost efficient
 - Initial R&D success indicate record high 12 T/s with HTS magnets (need 5-100) but needs further effort
- **Should be part of the *EuroMAP***

*Thank You for Your
Attention!*

Discussion : “Granada Message”

1. despite ups and downs over the past 20 years, the mumu concept is not going away and the reasons are [...]
2. $\mu\mu$ offers a "moderately conservative-moderately innovative" way to cost affordable energy frontier colliders
3. major advantages/promises are [...]
4. key challenges are [...]
5. to claim feasibility (CDR-level) in, say, 5(10?) years we need [....R&D program goals]

Luminosity and Cooling

- **Option “PS”**: use existing proton source 24 GeV, 8 bunches $6 \cdot 10^{12}$ protons at 1.2Hz → on target → ionization cooling of muons
- **Option “MAP”** : build dedicated 8 GeV proton source $2 \cdot 10^{14}$ p/pulse at 5Hz → on target → ionization cooling of muons
- **Option “Low Emittance”** : ~45 GeV 6.3km circumference e^+ storage ring → 0.3mm Be target → $\sim 10^{-7}$ muon pairs per e^+ bunch (100 bunches of 3×10^{11} e^+) → 63m 22 GeV μ rings accumulate μ 's for ~ 2500 turns, obtaining bunches of $\sim 4.5 \times 10^7$ μ 's at ~ 2200 Hz (10^{11} μ /s) → fast RLA

BACK-UP SLIDES

Table 2: Options for a 14 TeV $\mu^+ - \mu^-$ collider.

Parameter	“PS”	“MAP”	“LEMC”
Avg. luminosity	$1.2 \cdot 10^{33}$	$3.3 \cdot 10^{35}$	$2.4 \cdot 10^{32}$
Beam $\delta E/E$	0.1%	0.1%	0.2%
Rep rate, Hz	5	5	2200
N_μ/bunch	$1.2 \cdot 10^{11}$	$2 \cdot 10^{12}$	4.5×10^7
n_b	1	1	1
$\varepsilon_{t,N}$ mm-mrad	25	25	0.04
β^* , mm	1	1	0.2
$\sigma^*(\text{IR})$, μm	0.6	0.6	0.011
Bunch length, mm	0.001	0.001	0.0002
μ production source	24 GeV p	8 GeV p	45 GeV e^+
p or e/pulse	$6 \cdot 10^{12}$	$2 \cdot 10^{14}$	$3 \cdot 10^{13}$
Driver beam power	0.17MW	1.6MW	40 MW
Acceleration, GeV	1-3.5, 3.5-7	1-3.5, 3.5-7	40 GV, RLA 20 turn
ν radiation, mSv/yr	RCS 0.08	RCS 1.5	0.015

Neutrino Radiation

$$Dose \cong 0.57 \frac{N_{\mu}' E_{\mu}^3}{R_x^2} mSv / year$$

- N_{μ}' in $10^{13}/s$, E_{μ} is in TeV and R_x is 36 km for a 100m depth
- All options are safe

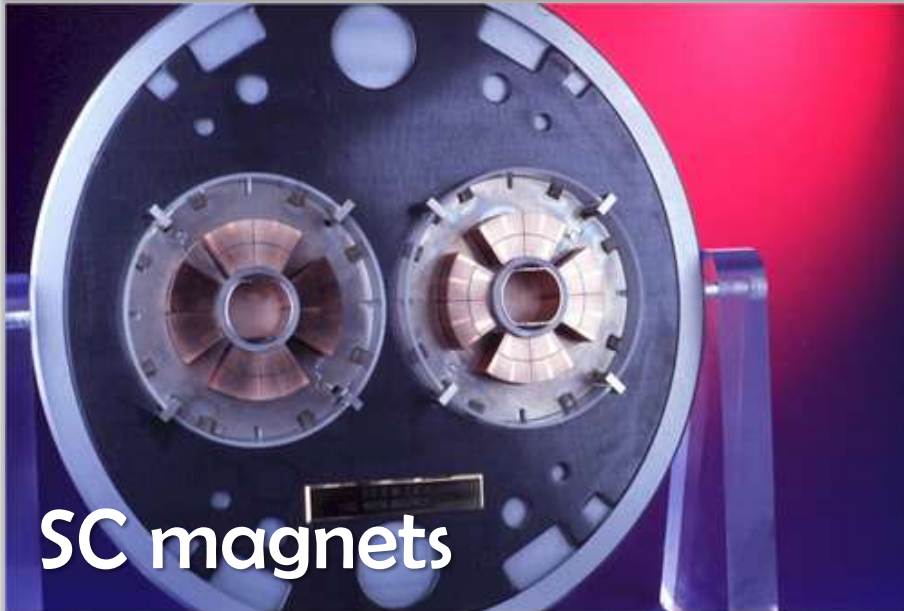
Four “Proven” Technologies



Normal Conducting Magnets



Normal Conducting RF



SC magnets



SC RF

Analysis:

2014 JINST 9 T07002

17 “Data Points” - Costs of Big Accelerators:

- Actually built:
 - RHIC, MI, SNS, LHC
- Under construction:
 - XFEL, FAIR, ESS
- Not built but costed:
 - SSC, VLHC, NLC
 - ILC, TESLA, CLIC, Project-X, Beta-Beam, SPL, ν -Factory

Wide range :

- 4 orders in Energy, >1 order in Power, >2 orders in Length
- Almost 2 orders in cost
 - (normalized to US TPC)

	Cost (B\$) Year	Energy (TeV)	Accelerator technology	Comments	Length (km)	Site power (MW)	TPC range (Y14 B\$)
SSC	11.8 B\$ (1993)	40	SC Mag	Estimates changed many times [6–8]	87	~ 100	19–25
FNAL MI	260M\$ (1994)	0.12	NC Mag	“old rules”, no OH, existing injector [9]	3.3	~ 20	0.4–0.54
RHIC	660M\$ (1999)	0.5	SC Mag	Tunnel, some infrastructure, injector re-used [10]	3.8	~ 40	0.8–1.2
TESLA	3.14 B€ (2000)	0.5	SC RF	“European accounting” [11]	39	~ 130	11–14
VLHC-I	4.1 B\$ (2001)	40	SC Mag	“European accounting”, existing injector [12]	233	~ 60	10–18
NLC	~ 7.5 B\$ (2001)	1	NC RF	~ 6 B\$ for 0.5 TeV collider. [13]	30	250	9–15
SNS	1.4 B\$ (2006)	0.001	SC RF	[14]	0.4	20	1.6–1.7
LHC	6.5 BCHF (2009)	14	SC Mag	collider only — existing injector, tunnel & infrstr., no OH, R&D [15]	27	~ 40	7–11
CLIC	7.4–8.3B CHF(2012)	0.5	NC RF	“European accounting” [16]	18	250	12–18
Project X	1.5 B\$ (2009)	0.008	SC RF	[17]	0.4	37	1.2–1.8
XFEL	1.2 B€ (2012)	0.014	SC RF	in 2005 prices, “European accounting” [18]	3.4	~ 10	2.9–4.0
NuFactory	4.7–6.5 B€ (2012)	0.012	NC RF	Mixed accounting, w. contingency [19]	6	~ 90	7–11
Beta-Beam	1.4–2.3 B€ (2012)	0.1	SC RF	Mixed accounting, w. contingency [19]	9.5	~ 30	3.7–5.4
SPL	1.2–1.6 B€ (2012)	0.005	SC RF	Mixed accounting, w. contingency [19]	0.6	~ 70	2.6–4.6
FAIR	1.2 B€ (2012)	0.003–0.08	SC Mag	“European accounting” [20], 6 rings, existing injector	~ 3	~ 30	1.8–3.0
ILC	7.8 B\$ (2013)	0.5	SC RF	“European accounting” [21]	34	230	13–19
SSS	1.84 B€ (2013)	0.0025	SC RF	4/11/2019 accounting” [22, 23]	0.4	37	2.5–3.8

! WARNING !

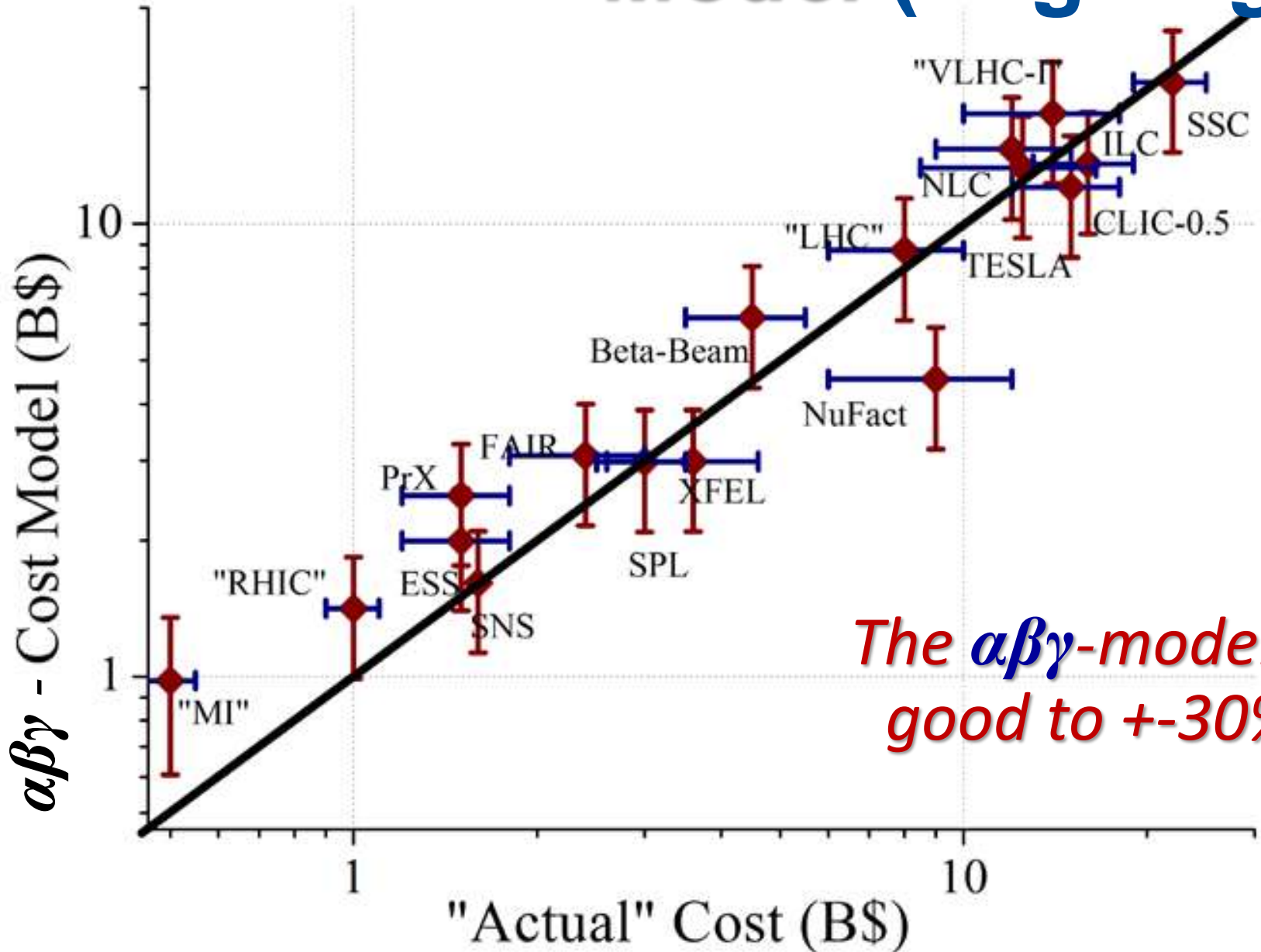
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 - $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$

USE AT YOUR OWN RISK!

Total Cost vs Model (Log-Log)



The $\alpha\beta\gamma$ -model is good to +/-30%