

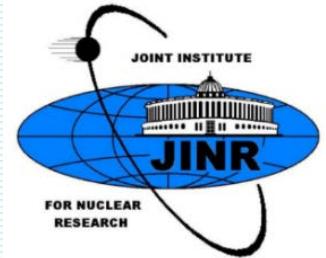


Colloquium Prague v19

J. Heyrovsky Institute of Physical Chemistry, 24-25 October 2019



Neutrinoless Double Beta Decay Theory **Fedor Šimkovic**



OUTLINE

I. Introduction

(Majorana ν 's)

II. The $0\nu\beta\beta$ -decay scenarios due neutrinos exchange

(simplest, sterile ν , LR-symmetric model)

III. DBD NMEs – Current status

(deformation, scaling relation?, exp. support, ab initio...)

IV. Quenching of g_A

(Ikeda sum rule, $2\nu\beta\beta$ -calc., novel approach for effective g_A)

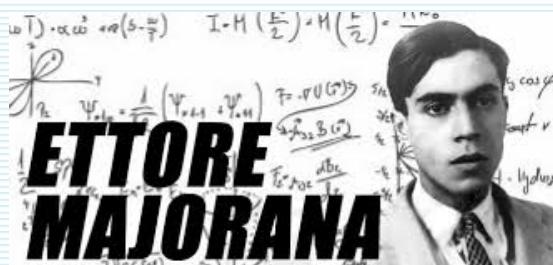
V. Looking for a signal of lepton number violation

(LHC study, resonant $0\nu ECEC$...)

Acknowledgements: **A. Faessler** (Tuebingen), **P. Vogel** (Caltech), **S. Kovalenko** (Valparaiso U.), **M. Krivoruchenko** (ITEP Moscow), **D. Štefánik**, **R. Dvornický** (Comenius U.), **A. Babič**, **A. Smetana** (IEAP CTU Prague), ...

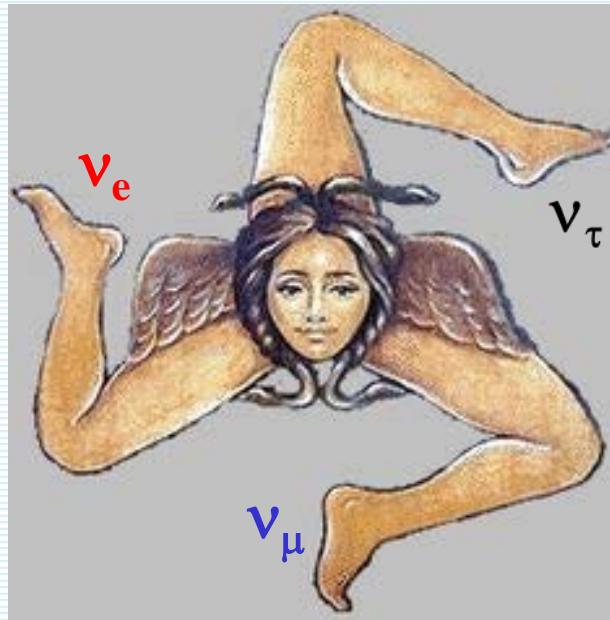
After 89/63 years
we know

- 3 families of light (V-A) neutrinos:
 ν_e, ν_μ, ν_τ
- ν are massive:
we know mass squared differences
- relation between flavor states and mass states (neutrino mixing)



The observation of neutrino oscillations has opened a new excited era in neutrino physics and represents a big step forward in our knowledge of neutrino properties

Fundamental ν properties

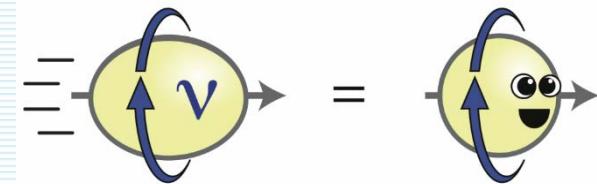


No answer yet

- Are ν Dirac or Majorana?
- Is there a CP violation in ν sector?
- Are neutrinos stable?
- What is the magnetic moment of ν ?
- Sterile neutrinos?
- Statistical properties of ν ? Fermionic or partly bosonic?

Currently main issue

Nature, Mass hierarchy,
CP-properties, sterile ν



Majorana fermion



https://en.wikipedia.org/wiki/File:Ettore_Majorana.jpg



CNNP 2018, Catania, October 15-21, 2018

10/24/2019

Fedor S.

TEORIA SIMMETRICA DELL'ELETTRONE E DEL POSITRONE

Nota di ETTORE MAJORANA

Symmetric Theory of Electron and Positron Nuovo Cim. 14 (1937) 171

Sunto. - Si dimostra la possibilità di pervenire a una piena simmetrizzazione formale della teoria quantistica dell'elettrone e del positrone facendo uso di un nuovo processo di quantizzazione. Il significato delle equazioni di DIRAC ne risulta alquanto modificato e non vi è più luogo a parlare di stati di energia negativa; né a presumere per ogni altro tipo di particelle, particolarmente neutre, l'esistenza di « antiparticelle » corrispondenti ai « vuoti » di energia negativa.

L'interpretazione dei cosiddetti « stati di energia negativa » proposta da DIRAC (¹) conduce, come è ben noto, a una descrizione sostanzialmente simmetrica degli elettroni e dei positroni. La sostanziale simmetria del formalismo consiste precisamente in questo, che fin dove è possibile applicare la teoria girando le difficoltà di convergenza, essa fornisce realmente risultati del tutto simmetrici. Tuttavia gli artifici sconosciuti non danno alla teoria una forma simmetrica che si accorda sia perché sia perché la simmetria non dà alla teoria una forma simmetrica isfacenti; trica, sia iante tali che possano via che conduce più direttamente alla meta.

Per quanto riguarda gli elettroni e i positroni, da essa si può veramente attendere soltanto un progresso formale; ma ci sembra importante, per le possibili estensioni analogiche, che venga a cadere la nozione stessa di stato di energia negativa. Vedremo infatti che è perfettamente possibile costruire, nella maniera più naturale, una teoria delle particelle neutre elementari senza stati negativi.

(¹) P. A. M. DIRAC, « Proc. Camb. Phil. Soc. », **30**, 150, 1924. V. anche W. HEISENBERG, « ZS. f. Phys. », **90**, 209, 1934.



MESONIUM AND ANTIMESONIUM

B. PONTECORVO

Joint Institute for Nuclear Research

Submitted to JETP editor May 23, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 33, 549-551 (August, 1957)

INVERSE BETA PROCESSES AND NONCONSERVATION OF LEPTON CHARGE

B. PONTECORVO

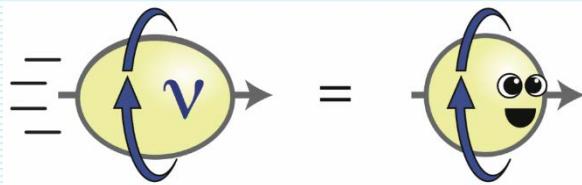
Joint Institute for Nuclear Research

Submitted to JETP editor October 19, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 34, 247-249
(January, 1958)



$\nu \leftrightarrow \bar{\nu}$ oscillation
(neutrinos are Majorana particles)

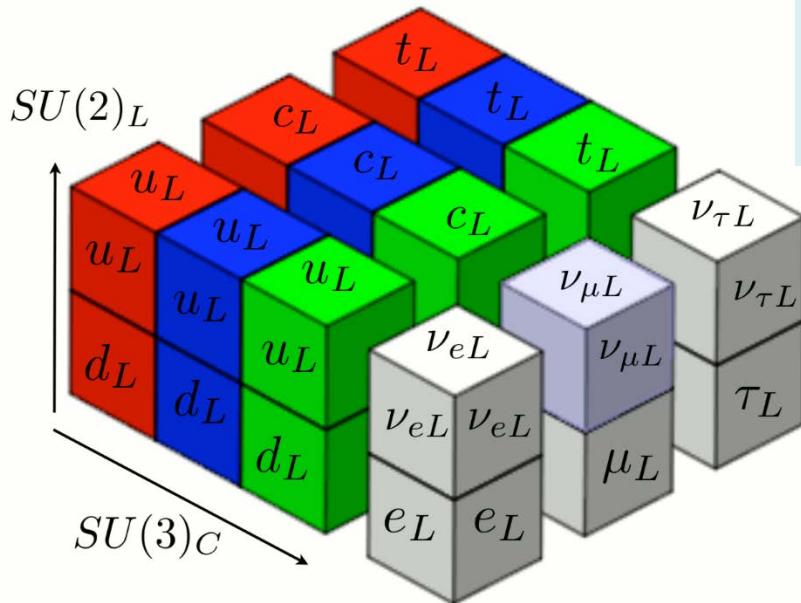


It follows from the above assumptions that in vacuum a neutrino can be transformed into an antineutrino and vice versa. This means that the neutrino and antineutrino are “mixed” particles, i.e., a symmetric and antisymmetric combination of two truly neutral Majorana particles ν_1 and ν_2 of different combined parity.⁵

1968 Gribov, Pontecorvo [PLB 28(1969) 493]
oscillations of neutrinos - a solution
of deficit of solar neutrinos in Homestake exp.

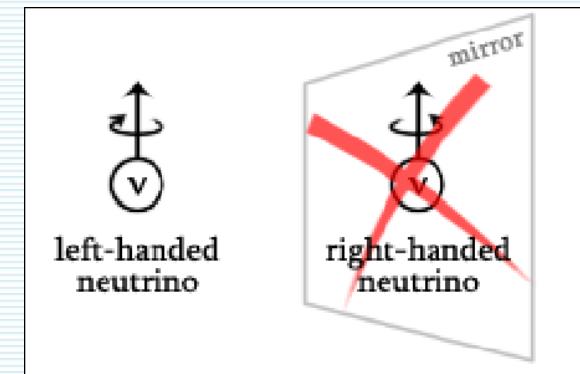


Standard Model (an astonishing successful theory, based on few principles)



Neutrino is a special particle in SM:

- It is the only fermion that does not carry electric charge (like bosons γ, g, H^0) !
- In the SM, the only left-handed neutrinos ν_L appears in the theory.
- One cannot obtain a mass for ν_L with any renormalizable coupling with the Higgs fields through SSB.



However, we know that ν 's do have mass from the ν -oscillation experiments!
 => Thus the neutrino mass indicates that there is something new = **BSM physics!**

Majorana ν -mass \Rightarrow Lepton number violation

The absence of the RH ν fields in the SM is the simplest, most economical scenario. The ν -masses and mixing are generated by the L-number violating Majorana mass term coming from dimension-5 effective Weinberg operator:

$$L = \frac{\lambda(LH)(LH)}{\Lambda} + h.c.$$

(LH) is a SM singlet, Λ - mass scale, λ -dimensionless coupling. After SSB

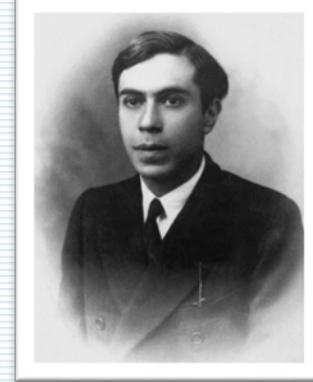
$$L = \frac{\lambda v^2}{2\Lambda} (\nu_L \nu_L + h.c.)$$

The Majorana ν -mass term violates total lepton number

Make $\nu_L \rightarrow e^{i\phi} \nu_L$, L changes by $e^{2i\phi}$

Majorana Neutrinos

- LN violating
- $\nu = \nu^c$
- $\nu = \nu_L + (\nu_L)^c$



In the SM, The term like $\nu_L \nu_L$ is not allowed by $SU(2) \times U(1)$ \Rightarrow there is no natural Majorana mass term for the LH ν . However, dim-5 L-number non-conserving operator is allowed leading to a Majorana mass

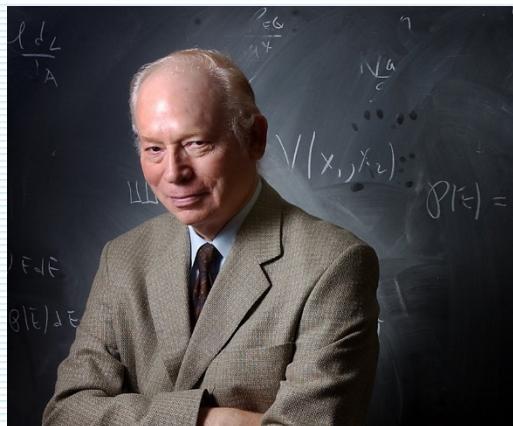
$$m_M = \frac{\lambda v^2}{\Lambda}$$

This is a seesaw formula, in the sense that small ν -mass can be understood when Λ is large. To get meV mass, we need

$$\Lambda = 10^{16} GeV \text{ (GUT scale)}$$

CERN COURIER

VOLUME 57 NUMBER 9 NOVEMBER 2017

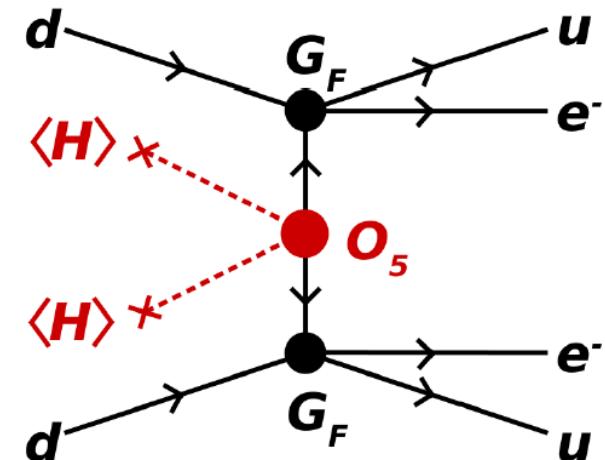


Weinberg, 1979: d=5

$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$

10/24/2019

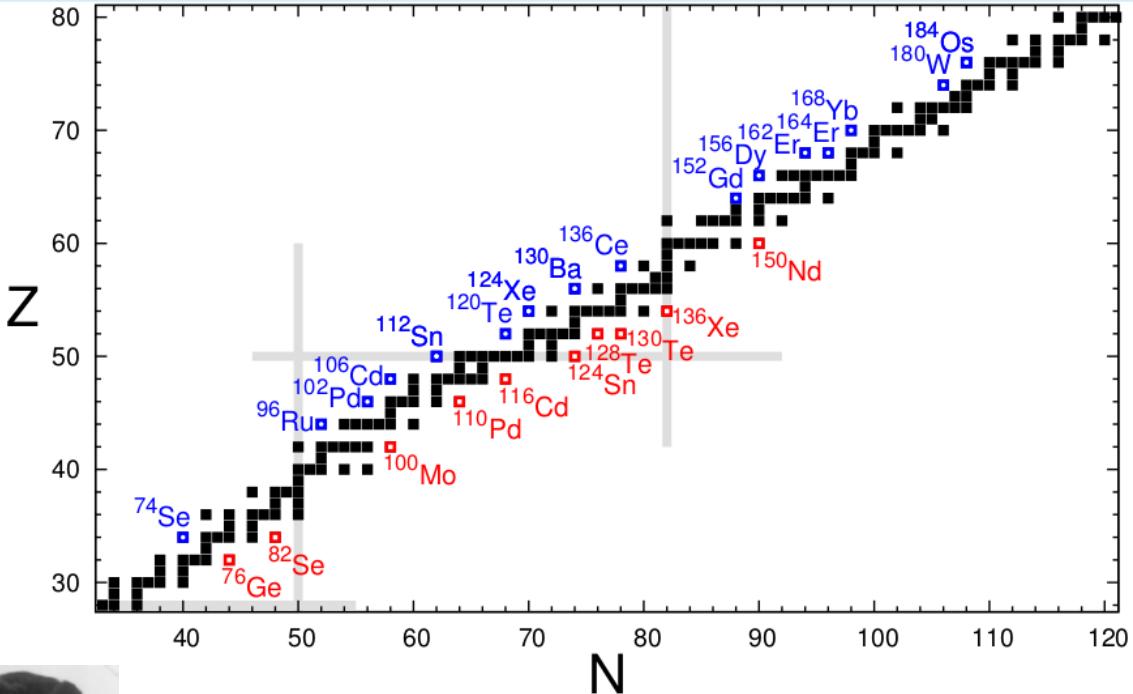
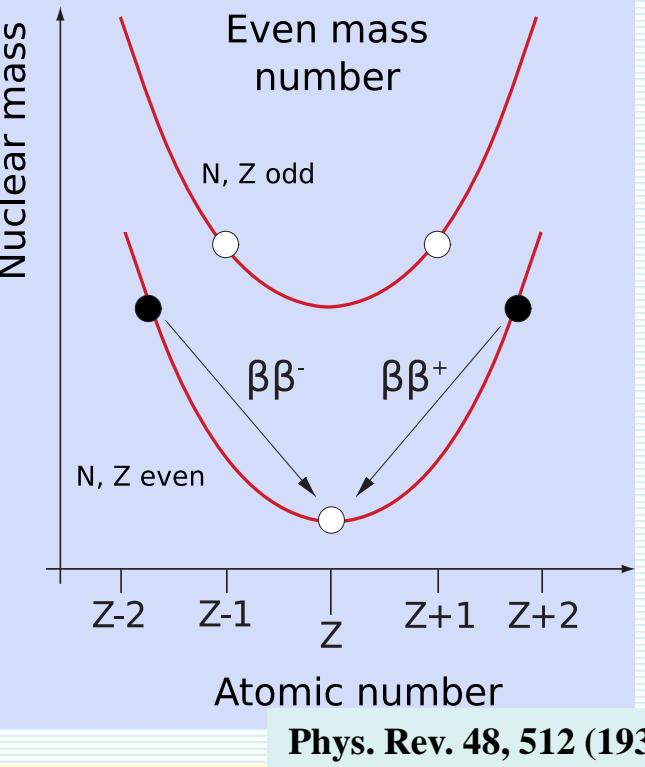
$0\nu\beta\beta$ decay:



. Weinberg does not take credit for predicting neutrino masses, but he thinks it's the right interpretation. What's more, he says, the non-renormalisable interaction that produces the neutrino masses is probably also accompanied with non-renormalisable interactions that produce proton decay and other things that haven't been observed, such as violation of baryon-number conservations. “We don't know anything about the details of those terms, but I'll swear they are there.”

II. The $0\nu\beta\beta$ -decay scenarios

Nuclear double- β decay (even-even nuclei, pairing int.)



Two-neutrino double- β decay – LN conserved
 $(A, Z) \rightarrow (A, Z+2) + e^- + e^- + \nu_e + \bar{\nu}_e$

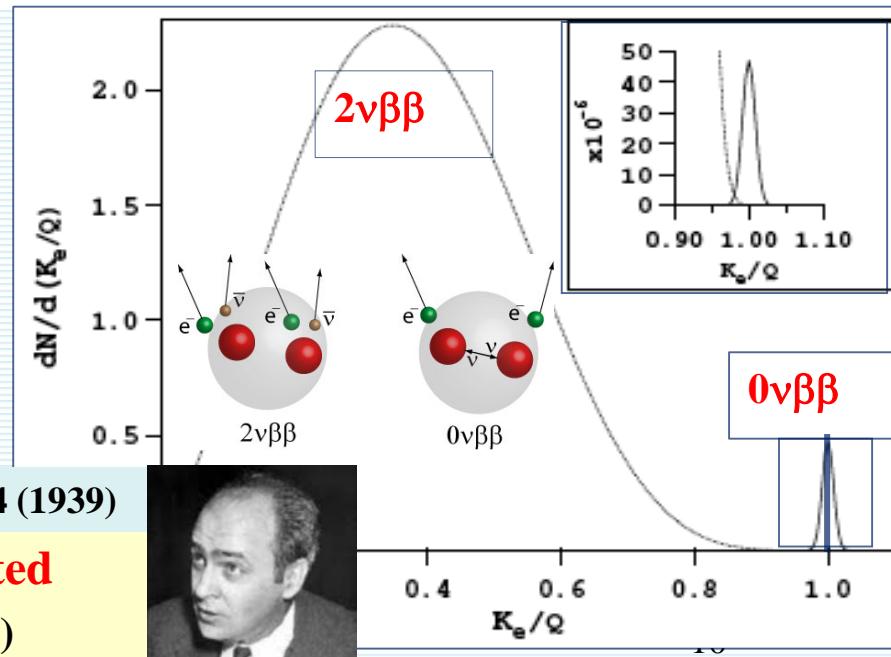
Goeppert-Mayer – 1935. 1st observation in 1987



Nuovo Cim. 14, 322 (1937)

Phys. Rev. 56, 1184 (1939)

Neutrinoless double- β decay – LN violated
 $(A, Z) \rightarrow (A, Z+2) + e^- + e^-$ (Furry 1937)
 Not observed yet. Requires massive Majorana ν 's



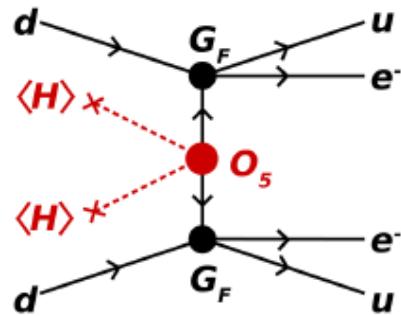
Collaboration	Isotope	Technique	mass ($0\nu\beta\beta$ isotope)	Status
CANDLES	Ca-48	305 kg CaF ₂ crystals - liq. scint	0.3 kg	Construction
CARVEL	Ca-48	⁴⁸ CaWO ₄ crystal scint.	~ ton	R&D
GERDA I	Ge-76	Ge diodes in LAr	15 kg	Complete
GERDA II	Ge-76	Point contact Ge in LAr	31	Operating
MAJORANA DEMONSTRATOR	Ge-76	Point contact Ge	25 kg	Operating
LEGEND	Ge-76	Point contact with active veto	~ ton	R&D
NEMO3	Mo-100 Se-82	Foils with tracking	6.9 kg 0.9 kg	Complete
SuperNEMO Demonstrator	Se-82	Foils with tracking	7 kg	Construction
SuperNEMO	Se-82	Foils with tracking	100 kg	R&D
LUCIFER (CUPID)	Se-82	ZnSe scint. bolometer	18 kg	R&D
AMoRE	Mo-100	CaMoO ₄ scint. bolometer	1.5 - 200 kg	R&D
LUMINEU (CUPID)	Mo-100	ZnMoO ₄ / Li ₂ MoO ₄ scint. bolometer	1.5 - 5 kg	R&D
COBRA	Cd-114,116	CdZnTe detectors	10 kg	R&D
CUORICINO, CUORE-0	Te-130	TeO ₂ Bolometer	10 kg, 11 kg	Complete
CUORE	Te-130	TeO ₂ Bolometer	206 kg	Operating
CUPID	Te-130	TeO ₂ Bolometer & scint.	~ ton	R&D
SNO+	Te-130	0.3% natTe suspended in Scint	160 kg	Construction
EXO200	Xe-136	Xe liquid TPC	79 kg	Operating
nEXO	Xe-136	Xe liquid TPC	~ ton	R&D
KamLAND-Zen (I, II)	Xe-136	2.7% in liquid scint.	380 kg	Complete
KamLAND2-Zen	Xe-136	2.7% in liquid scint.	750 kg	Upgrade
NEXT-NEW	Xe-136	High pressure Xe TPC	5 kg	Operating
NEXT-100	Xe-136	High pressure Xe TPC	100 kg - ton	R&D
PandaX - III	Xe-136	High pressure Xe TPC	~ ton	R&D
DCBA	Nd-150	Nd foils & tracking chambers	20 kg	R&D

$$\mathcal{L} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} \sum_i c_i^{(5)} \mathcal{O}_i^{(5)} + \frac{1}{\Lambda^2} \sum_i c_i^{(6)} \mathcal{O}_i^{(6)} + O(\frac{1}{\Lambda^3})$$

Beyond the SM physics

Amplitude for
 $(A, Z) \rightarrow (A, Z+2) + 2e^-$
can be divided into:

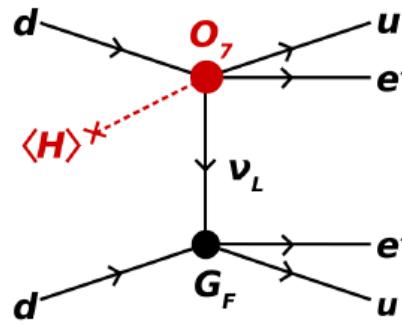
mass mechanism: d=5



$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$

Weinberg, 1979

long range: d=7



$$\mathcal{O}_2 \propto LLL e^c H$$

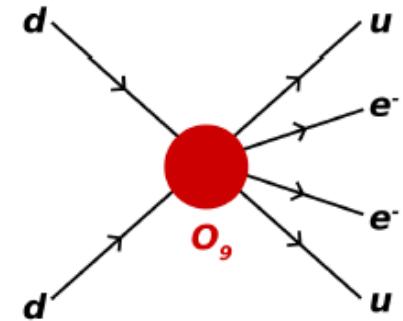
$$\mathcal{O}_3 \propto LLQ d^c H$$

$$\mathcal{O}_4 \propto LL\bar{Q} \bar{u}^c H$$

$$\mathcal{O}_8 \propto L\bar{e}^c \bar{u}^c d^c H$$

Babu, Leung: 2001
de Gouvea, Jenkins: 2007

short range: d=9 (d=11)



$$\mathcal{O}_5 \propto LLQ d^c H H H^\dagger$$

$$\mathcal{O}_6 \propto LL\bar{Q} \bar{u}^c H H^\dagger H$$

$$\mathcal{O}_7 \propto LQ\bar{e}^c \bar{Q} H H H^\dagger$$

$$\mathcal{O}_9 \propto LLL e^c L e^c$$

$$\mathcal{O}_{10} \propto LLL e^c Q d^c$$

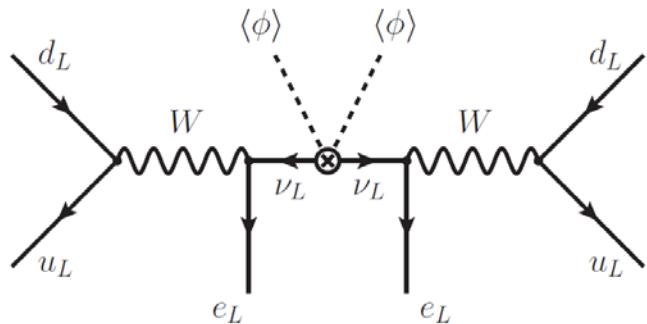
$$\mathcal{O}_{11} \propto LLQ d^c Q d^c$$

.....

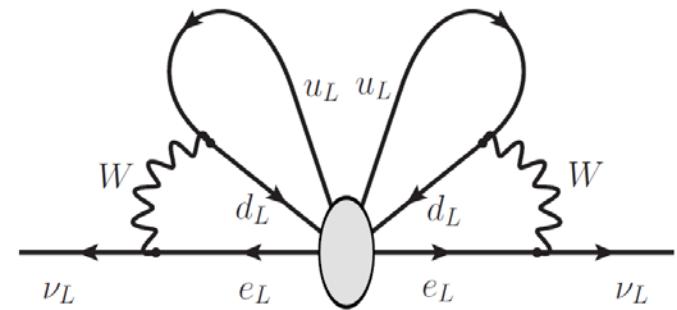
Valle

If $0\nu\beta\beta$ is observed the ν is
a Majorana particle

Majorana $m_\nu \Rightarrow 0\nu\beta\beta$



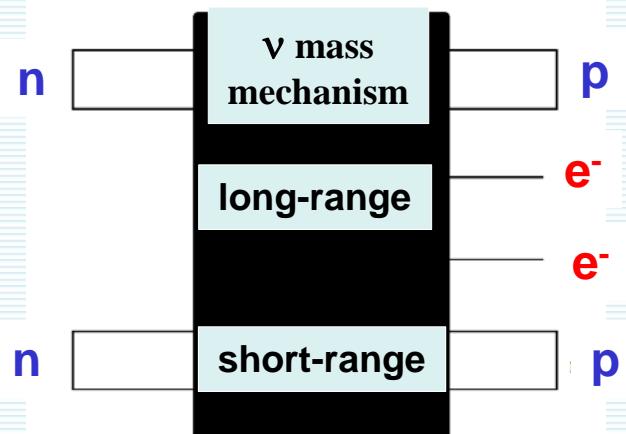
$0\nu\beta\beta \Rightarrow$ Majorana m_ν



Schechter, Valle: PRD 1982

Different $0\nu\beta\beta$ -decay scenarios

Can we say
something about
content
of the black box?



- Considering
- Sterile ν
 - Different LNV scales
 - Right-handed currents
 - Non-standard ν -interactions
 -

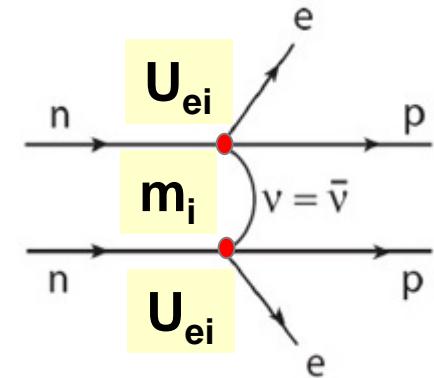
$0\nu\beta\beta$ -decay ($V-A$ SM int., light ν -exchange)

$(A, Z) \rightarrow (A, Z+2) + e^- + e^-$

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 |M_\nu^{0\nu}|^2 G^{0\nu}$$

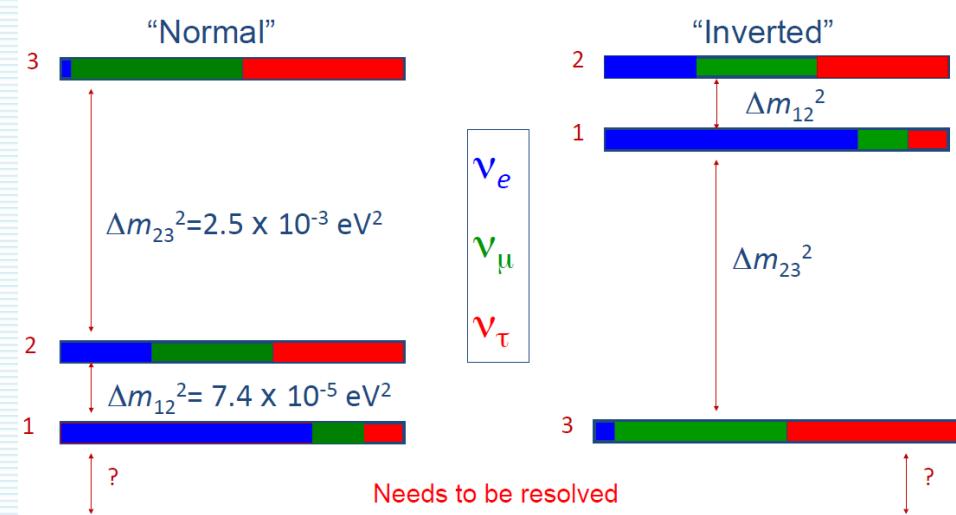
NME must be evaluated using tools of nuclear theory

Phase factor well understood



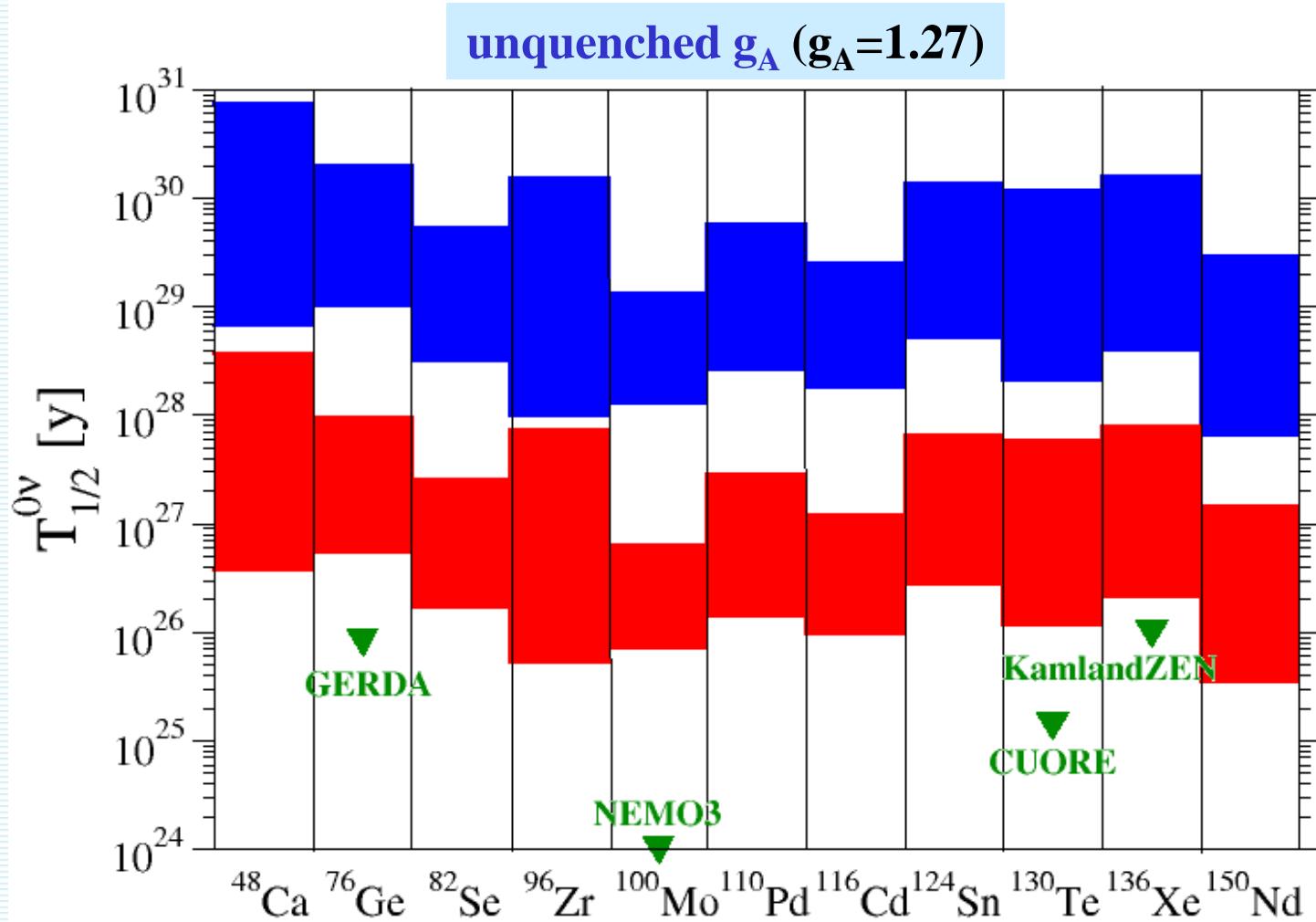
$$m_{\beta\beta} = \left| c_{13}^2 c_{12}^2 e^{i\alpha_1} m_1 + c_{13}^2 s_{12}^2 e^{i\alpha_2} m_2 + s_{13}^2 m_3 \right|$$

Effective Majorana mass can be evaluated. It depends on $m_1, m_2, m_3, \theta_{12}, \theta_{13}, \alpha_1, \alpha_2$ (3 unknown parameters: $m_1/m_3, \alpha_1, \alpha_2$)



$$U^{PMNS} = \begin{pmatrix} c_{12}c_{13} & c_{13}s_{12} & e^{-i\delta}s_{13} \\ -c_{23}s_{12} - e^{i\delta}c_{12}s_{13}s_{23} & c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23} & c_{13}s_{23} \\ s_{12}s_{23} - e^{i\delta}c_{12}c_{23}s_{13} & -e^{i\delta}c_{23}s_{12}s_{13} - c_{12}s_{23} & c_{13}c_{23} \end{pmatrix} \begin{pmatrix} e^{i\alpha_1} & 0 & 0 \\ 0 & e^{i\alpha_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

0νββ –half lives for NH and IH with included uncertainties in NMEe



NH:

$$m_1 \ll m_2 \ll m_3 \quad m_3 \simeq \sqrt{\Delta m^2}$$

$$m_1 \ll \sqrt{\delta m^2}. \quad m_2 \simeq \sqrt{\delta m^2}$$

$$1.4 \text{ meV} \leq m_{\beta\beta} \leq 3.6 \text{ meV}$$

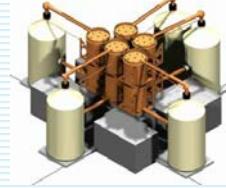
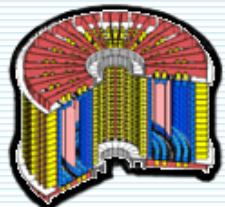
IH:

$$m_3 \ll m_1 < m_2 \quad m_1 \simeq m_2 \simeq \sqrt{\Delta m^2}$$

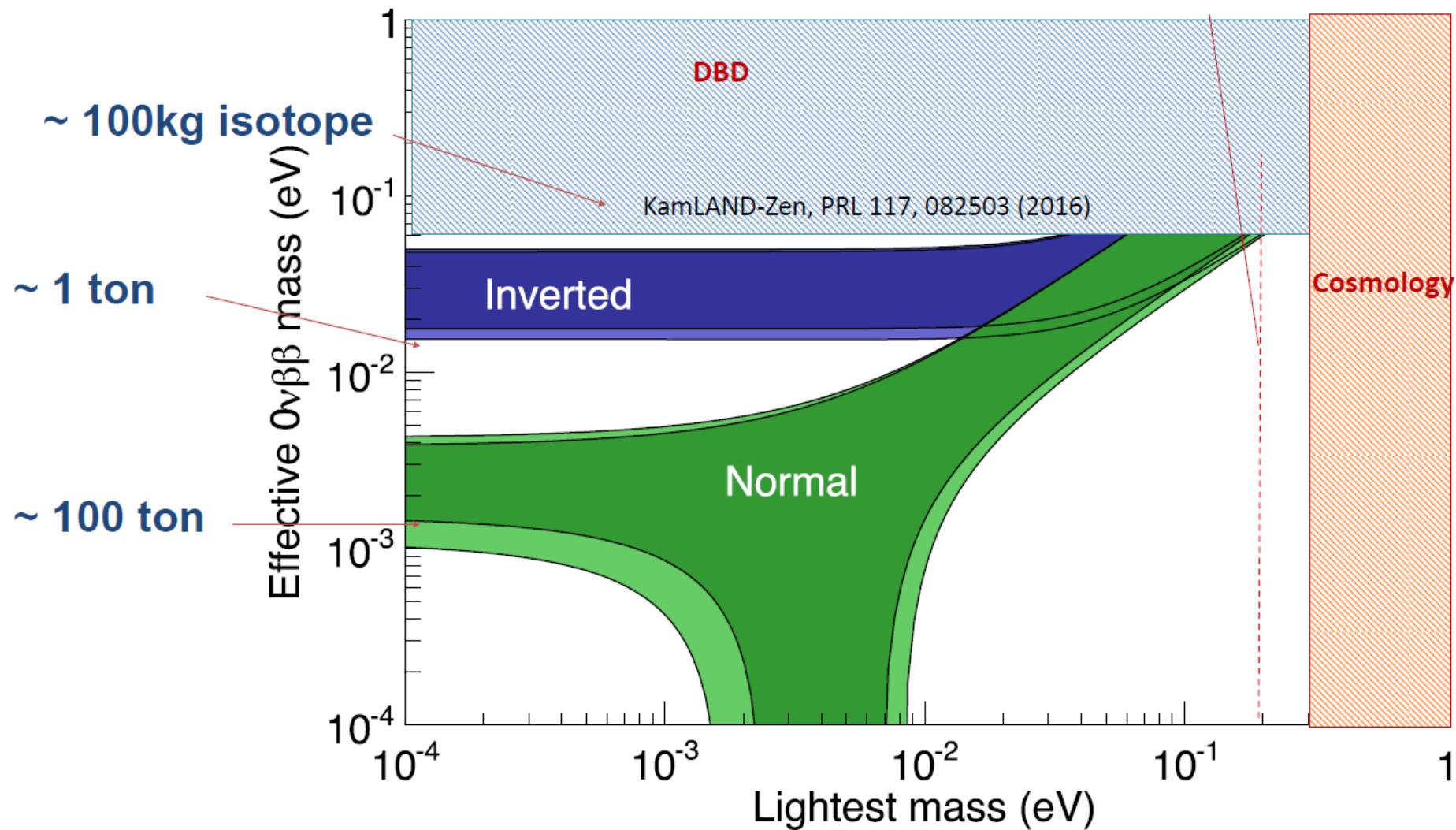
$$m_3 \ll \sqrt{\Delta m^2}$$

Lightest ν-mass equal to zero

$$20 \text{ meV} \leq m_{\beta\beta} \leq 49 \text{ meV}$$

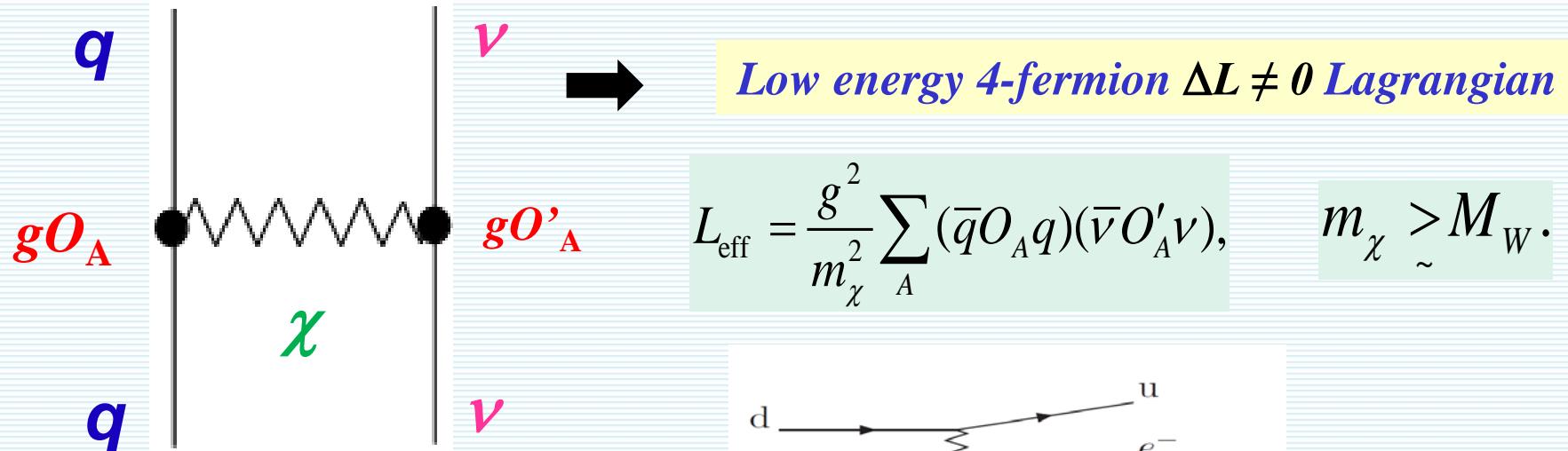


Estimated KATRIN Sensitivity



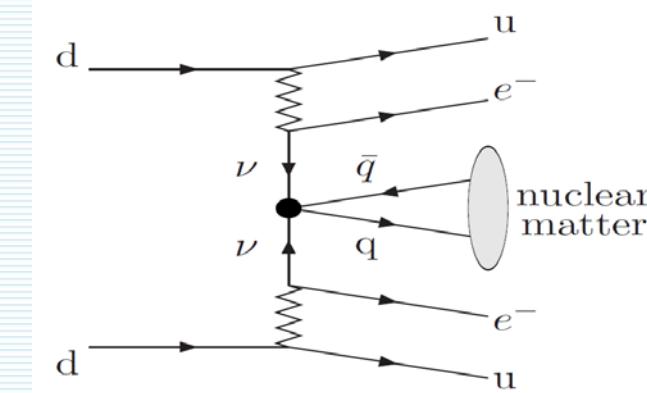
II.b Nuclear medium effect on the light neutrino mass exchange mechanism of the $0\nu\beta\beta$ -decay

S.G. Kovalenko, M.I. Krivoruchenko, F. Š., Phys. Rev. Lett. 112 (2014) 142503



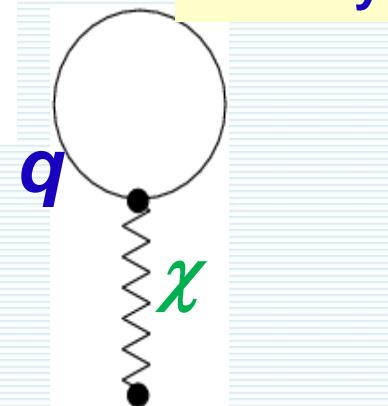
*oscillation experiments,
tritium β -decay
cosmology*

$$\sum_\nu^{\text{vac}} = \times, ---$$



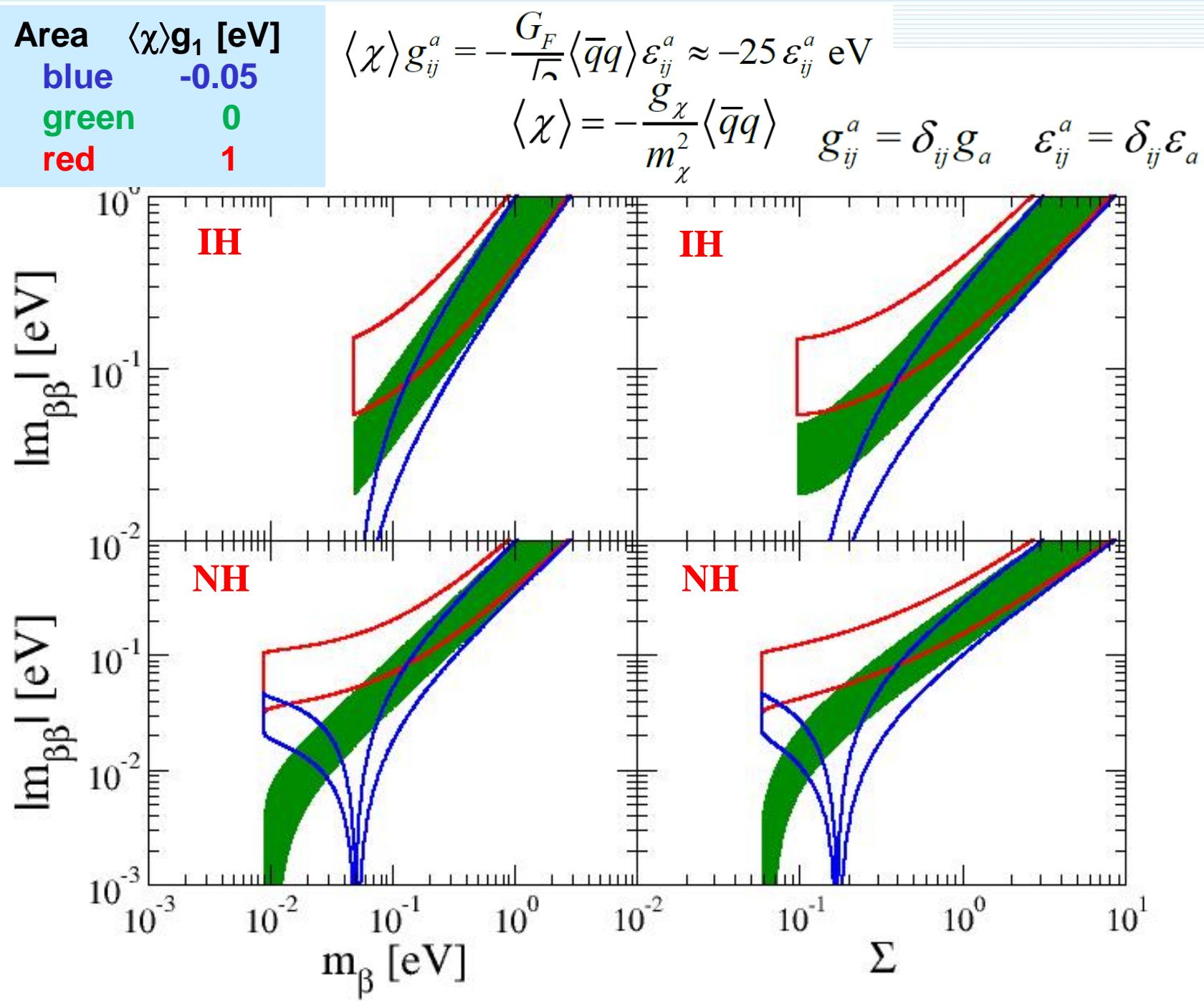
$0\nu\beta\beta$ -decay

$$\sum_\nu^{\text{medium}} = -\times- +$$



density

Complementarity between β -decay, $0\nu\beta\beta$ –decay and cosmological measurements might be spoiled



II.c. *The sterile ν mechanism of the $0\nu\beta\beta$ -decay (D-M mass term, V-A,SM int.) Interpolating formula*

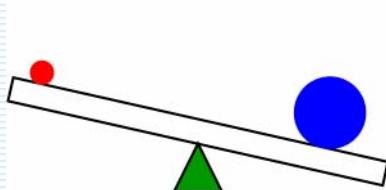
**Dirac-Majorana
mass term**

$$N = \sum_{\alpha=s,e,\mu,\tau} U_{N\alpha} \nu_\alpha$$

**Mixing of
active-sterile
neutrinos**

small ν masses due to see-saw mechanism

$$\begin{pmatrix} 0 & m_D \\ m_D & m_{LNV} \end{pmatrix}$$



Light ν mass $\approx (m_D/m_{LNV}) m_D$
Heavy ν mass $\approx m_{LNV}$

**Neutrinos masses offer a great opportunity to jump
beyond the EW framework via see-saw ...**

Different motivations for the LNV scale Λ

eV
light sterile ν
 10^{-6} GeV

keV
hot DM
 10^{-6} GeV

Fermi
LHC
 10^{-6} GeV or Si
 10^3 GeV

TeV
GUT
 10^{16} GeV

Planck
 10^{19} GeV

Left-handed neutrinos: Majorana neutrino mass eigenstate \mathbf{N} with arbitrary mass m_N

Faessler, Gonzales, Kovalenko, F. Š., PRD 90 (2014) 096010]

$$[T_{1/2}^{0\nu}]^{-1} = G^{0\nu} g_A^4 \left| \sum_N \left(U_{eN}^2 m_N \right) m_p M'^{0\nu}(m_N, g_A^{\text{eff}}) \right|^2$$

General case

$$M'^{0\nu}(m_N, g_A^{\text{eff}}) = \frac{1}{m_p m_e} \frac{R}{2\pi^2 g_A^2} \sum_n \int d^3x d^3y d^3p \quad M'^{0\nu}(m_N \rightarrow 0, g_A^{\text{eff}}) = \frac{1}{m_p m_e} M'_\nu^{0\nu}(g_A^{\text{eff}})$$

$$\times e^{ip \cdot (x-y)} \frac{\langle 0_F^+ | J^{\mu\dagger}(x) | n \rangle \langle n | J_\mu^\dagger(y) | 0_I^+ \rangle}{\sqrt{p^2 + m_N^2} (\sqrt{p^2 + m_N^2} + E_n - \frac{E_I - E_F}{2})} M'^{0\nu}(m_N \rightarrow \infty, g_A^{\text{eff}}) = \frac{1}{m_N^2} M_N'^{0\nu}(g_A^{\text{eff}})$$

light ν exchange

heavy ν exchange

Particular cases

$$[T_{1/2}^{0\nu}]^{-1} = G^{0\nu} g_A^4 \times$$

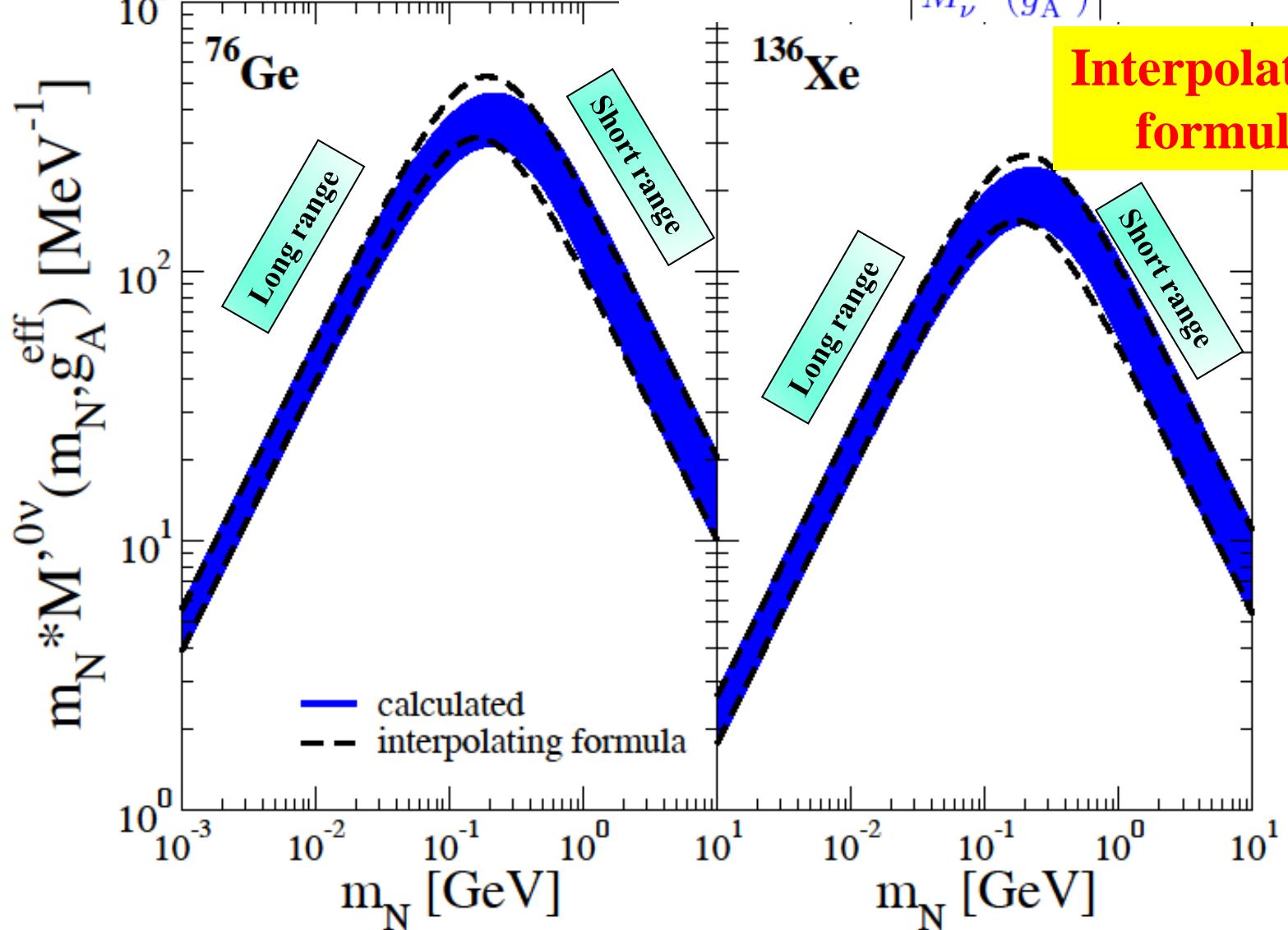
$$\times \begin{cases} \left| \frac{\langle m_\nu \rangle}{m_e} \right|^2 \left| M'_\nu(g_A^{\text{eff}}) \right|^2 & \text{for } m_N \ll p_F \\ \left| \langle \frac{1}{m_N} \rangle m_p \right|^2 \left| M_N'^{0\nu}(g_A^{\text{eff}}) \right|^2 & \text{for } m_N \gg p_F \end{cases}$$

$$\langle m_\nu \rangle = \sum_N U_{eN}^2 m_N$$

$$\left\langle \frac{1}{m_N} \right\rangle = \sum_N \frac{U_{eN}^2}{m_N}$$

$$[T_{1/2}^{0\nu}]^{-1} = \mathcal{A} \cdot \left| m_p \sum_N U_{eN}^2 \frac{m_N}{\langle p^2 \rangle + m_N^2} \right|^2, \quad \mathcal{A} = G^{0\nu} g_A^4 \left| M_N^{0\nu}(g_A^{\text{eff}}) \right|^2,$$

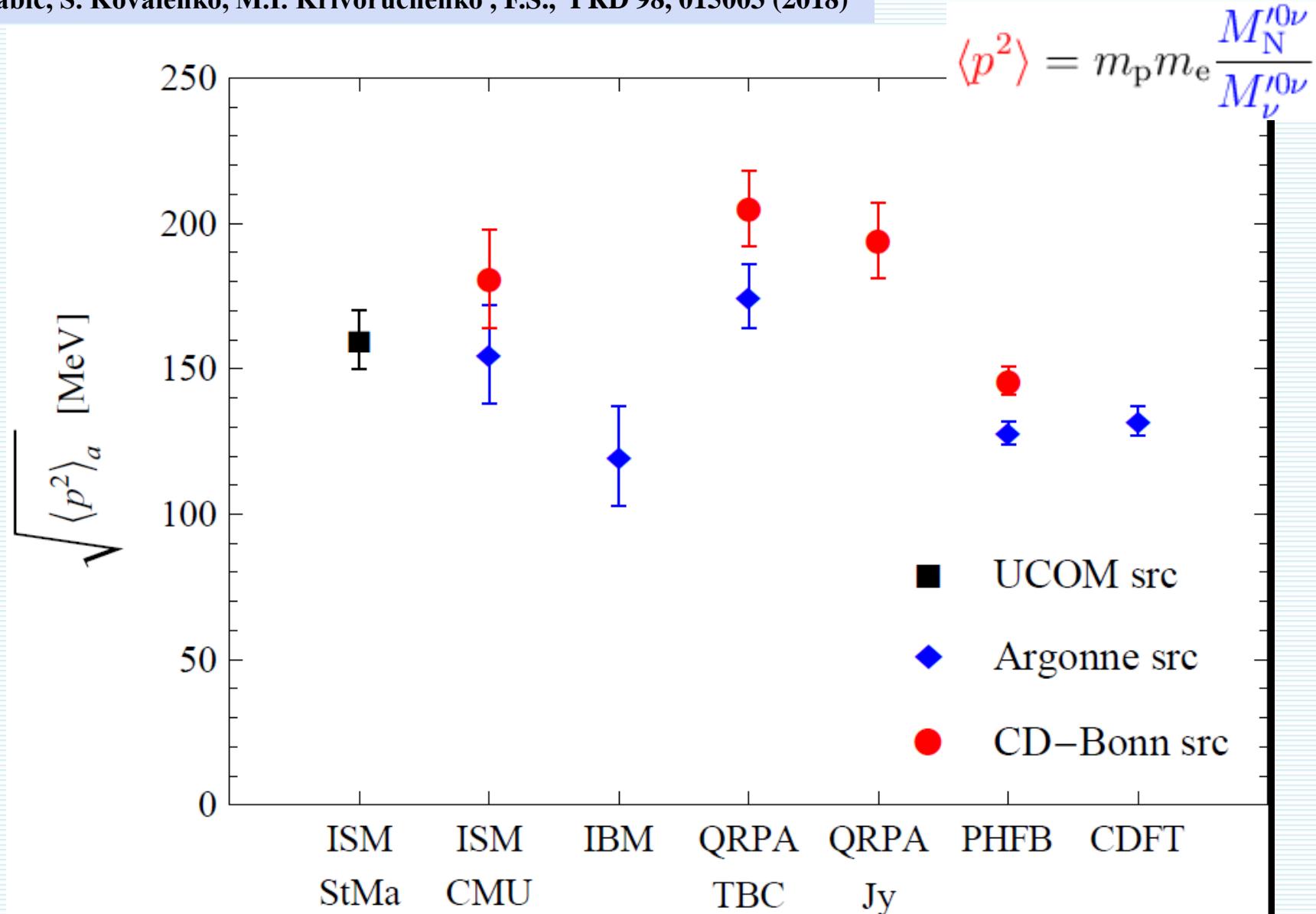
$$\langle p^2 \rangle = m_p m_e \left| \frac{M_N^{0\nu}(g_A^{\text{eff}})}{M_\nu^{0\nu}(g_A^{\text{eff}})} \right| \approx 200 \text{ MeV}$$



**Interpolating formula is justified
by practically no dependence $\langle p^2 \rangle$ on A**

$$[T_{1/2}^{0\nu}]^{-1} = \mathcal{A} \cdot \left| m_p \sum_N U_{eN}^2 \frac{m_N}{\langle p^2 \rangle + m_N^2} \right|^2,$$

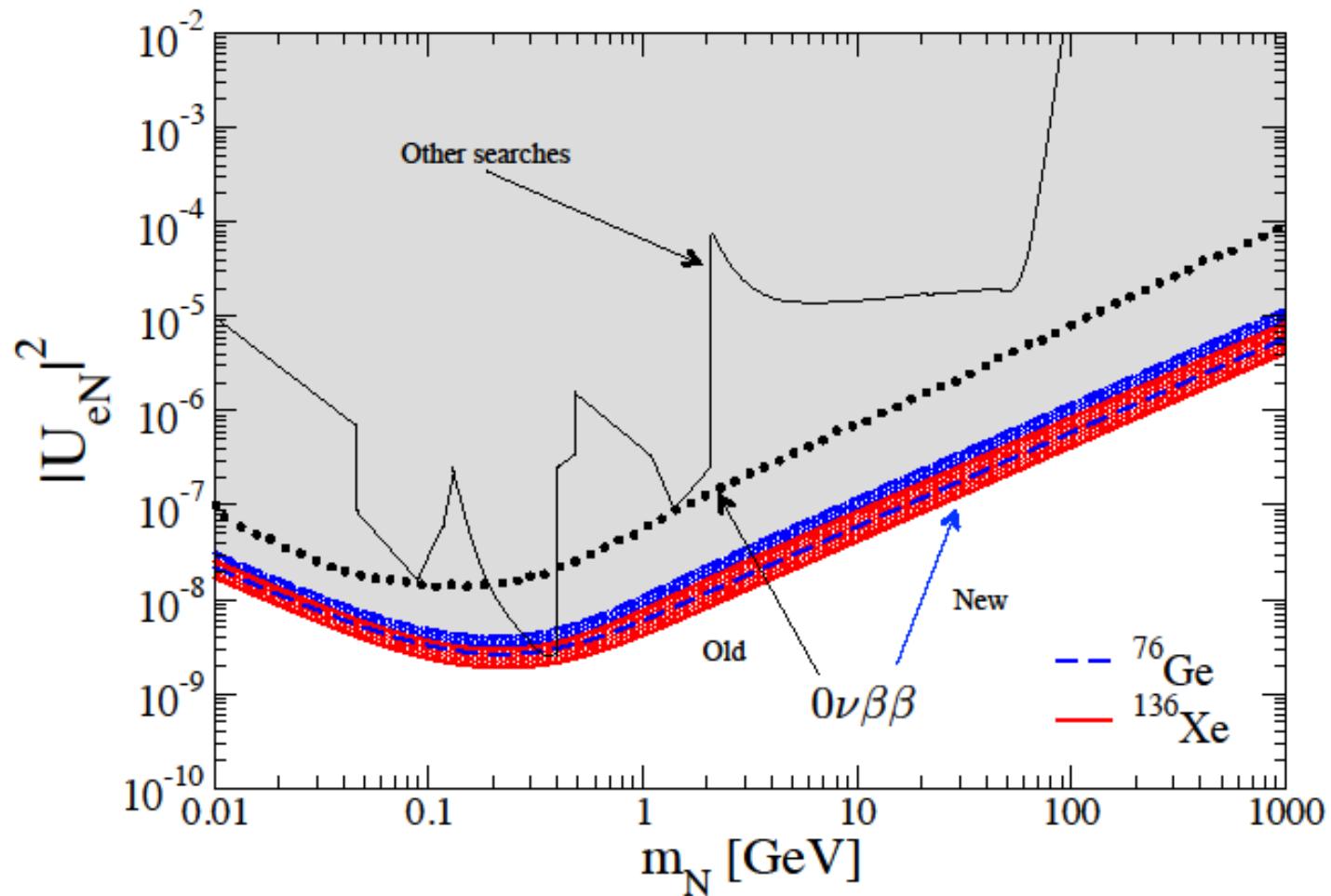
A. Babič, S. Kovalenko, M.I. Krivoruchenko , F.Š., PRD 98, 015003 (2018)



Exclusion plot in $|U_{eN}|^2 - m_N$ plane

$$T^{0\nu}_{1/2}(^{76}\text{Ge}) \geq 3.0 \cdot 10^{25} \text{ yr} \Rightarrow 0.9 \cdot 10^{26} \text{ yr}$$

$$T^{0\nu}_{1/2}(^{136}\text{Xe}) \geq 3.4 \cdot 10^{25} \text{ yr} \Rightarrow 1.1 \cdot 10^{26} \text{ yr}$$



QRPA (constrained Hamiltonian by $2\nu\beta\beta$ half-life, self-consistent treatment of src, restoration of isospin symmetry ...)

II.d. The $0\nu\beta\beta$ -decay within L-R symmetric theories (interpolating formula)

(D-M mass term, see-saw, V-A and V+A int., exchange of heavy neutrinos)

A. Babič, S. Kovalenko, M.I. Krivoruchenko , F.Š., PRD 98, 015003 (2018)

$$[T_{1/2}^{0\nu}]^{-1} = \eta_{\nu N}^2 C_{\nu N} \quad C_{\nu N} = g_A^4 \left| M_\nu^{0\nu} \right|^2 G^{0\nu}$$

Mixing of light and heavy neutrinos

$$\mathcal{U} = \begin{pmatrix} U & S \\ T & V \end{pmatrix}$$

$$\begin{aligned} \nu_{eL} &= \sum_{j=1}^3 \left(U_{ej} \nu_{jL} + S_{ej} (N_{jR})^C \right), \\ \nu_{eR} &= \sum_{j=1}^3 \left(T_{ej}^* (\nu_{jL})^C + V_{ej}^* N_{jR} \right) \end{aligned}$$

Effective LNV parameter within LRS model (due interpolating formula)

$$\begin{aligned} \eta_{\nu N}^2 &= \left| \sum_{j=1}^3 \left(U_{ej}^2 \frac{m_j}{m_e} + S_{ej}^2 \frac{\langle p^2 \rangle_a}{\langle p^2 \rangle_a + M_j^2} \frac{M_j}{m_e} \right) \right|^2 \\ &\quad + \lambda^2 \left| \sum_{j=1}^3 \left(T_{ej}^2 \frac{m_j}{m_e} + V_{ej}^2 \frac{\langle p^2 \rangle_a}{\langle p^2 \rangle_a + M_j^2} \frac{M_j}{m_e} \right) \right|^2 \end{aligned}$$

$$\langle p^2 \rangle = m_p m_e \frac{M_N'^{0\nu}}{M_\nu'^{0\nu}}$$

6x6 PMNS see-saw ν-mixing matrix

(the most economical one, prediction for mixing of heavy neutral leptons)

6x6 neutrino mass matrix

$$\mathcal{U} = \begin{pmatrix} U & S \\ T & V \end{pmatrix} \quad \text{Basis} \quad (\nu_L, (N_R)^c)^T$$

$$\mathcal{M} = \begin{pmatrix} M_L & M_D \\ M_D & M_R \end{pmatrix}$$

6x6 matrix: 15 angles, 10+5 CP phases

3x3 matrix: 3 angles, 1+2 CP phases

3x3 block matrices **U, S, T, V** are generalization of **PMNS** matrix

Assumptions:

- i) the see-saw structure
- ii) mixing between different generations is neglected

$$\mathcal{U}_{\text{PMNS}} = \begin{pmatrix} U_{\text{PMNS}} & \zeta \mathbf{1} \\ -\zeta \mathbf{1} & U_{\text{PMNS}}^\dagger \end{pmatrix} \quad \mathcal{U}_{\text{PMNS}} \mathcal{U}_{\text{PMNS}}^\dagger = \mathcal{U}_{\text{PMNS}}^\dagger \mathcal{U}_{\text{PMNS}} = 1$$

see-saw parameter

$$\zeta = \frac{m_{\text{D}}}{m_{\text{LNV}}}$$

6x6 matrix: 3 angles, 1+2 CP phases, 1 see-saw par.

6x6 PMNS see-saw ν -mixing matrix (the most economical one)

$$\mathcal{U} = \begin{pmatrix} U_0 & \zeta \mathbf{1} \\ -\zeta \mathbf{1} & V_0 \end{pmatrix}$$

$$U_0 = U_{\text{PMNS}}$$

A. Babič, S. Kovalenko, M.I. Krivoruchenko, F.Š., PRD 98, 015003 (2018)

$$V_0 = U_{\text{PMNS}}^\dagger =$$

$$\begin{pmatrix} c_{12} c_{13} e^{-i\alpha_1} & \left(-s_{12} c_{23} - c_{12} s_{13} s_{23} e^{-i\delta} \right) e^{-i\alpha_1} & \left(s_{12} s_{23} - c_{12} s_{13} c_{23} e^{-i\delta} \right) e^{-i\alpha_1} \\ s_{12} c_{13} e^{-i\alpha_2} & \left(c_{12} c_{23} - s_{12} s_{13} s_{23} e^{-i\delta} \right) e^{-i\alpha_2} & \left(-c_{12} s_{23} - s_{12} s_{13} c_{23} e^{-i\delta} \right) e^{-i\alpha_2} \\ s_{13} e^{i\delta} & c_{13} s_{23} & c_{13} c_{23} \end{pmatrix}$$

Assumption about heavy neutrino masses M_i (by assuming see-saw)

Inverse proportional

$$m_i M_i \simeq m_D^2$$

$$M_{\beta\beta}^R = \lambda \frac{\langle p^2 \rangle_a}{m_D^2} \left| \sum_{j=1}^3 (U_0^\dagger)_{ej}^2 m_j \right|$$

Proportional

$$m_i \simeq \zeta^2 M_i$$

$$M_{\beta\beta}^R = \lambda \zeta^2 \left| \sum_{j=1}^3 (U_0^\dagger)_{ej}^2 \frac{\langle p^2 \rangle_a}{m_j} \right|$$

$M_{\beta\beta}^R$ depends on
“Dirac” CP phase δ
unlike “Majorana”
CP phases α_1 and α_2

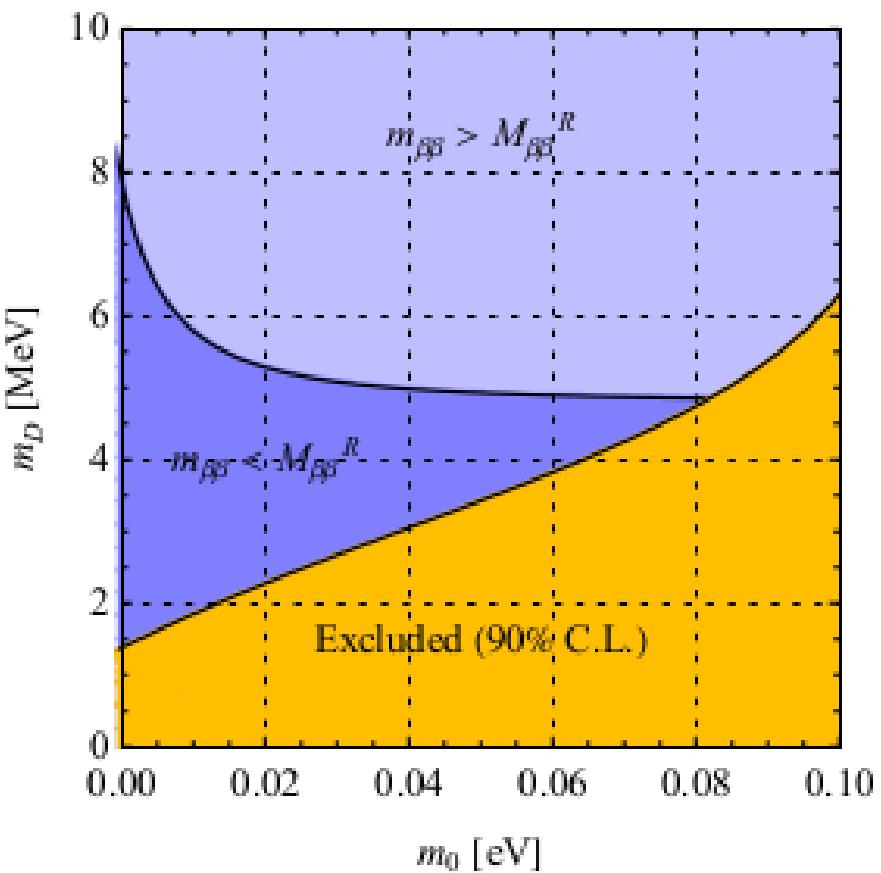
Heavy Majorana mass $M_{\beta\beta}^R$ depends on the “Dirac” CP violating phase δ

See-saw scenario

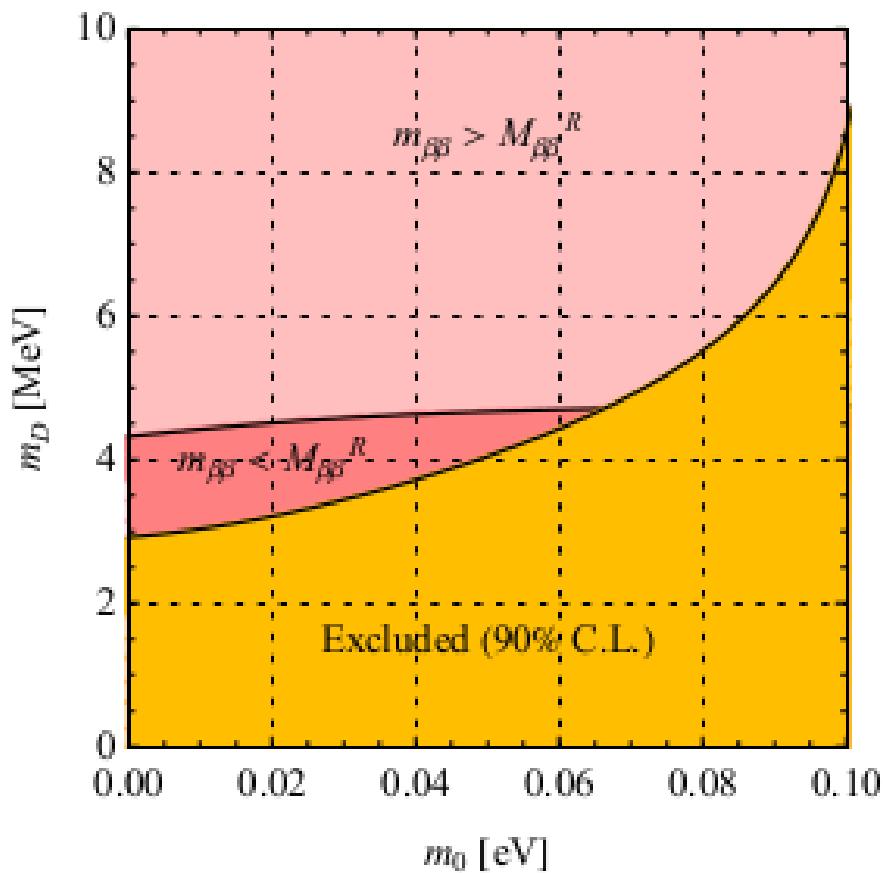
$$m_i M_i \simeq m_D^2$$

$$M_{\beta\beta}^R = \lambda \frac{\langle p^2 \rangle_a}{m_D^2} \left| \sum_{j=1}^3 (U_0^\dagger)_{ej}^2 m_j \right|$$

Normal spectrum



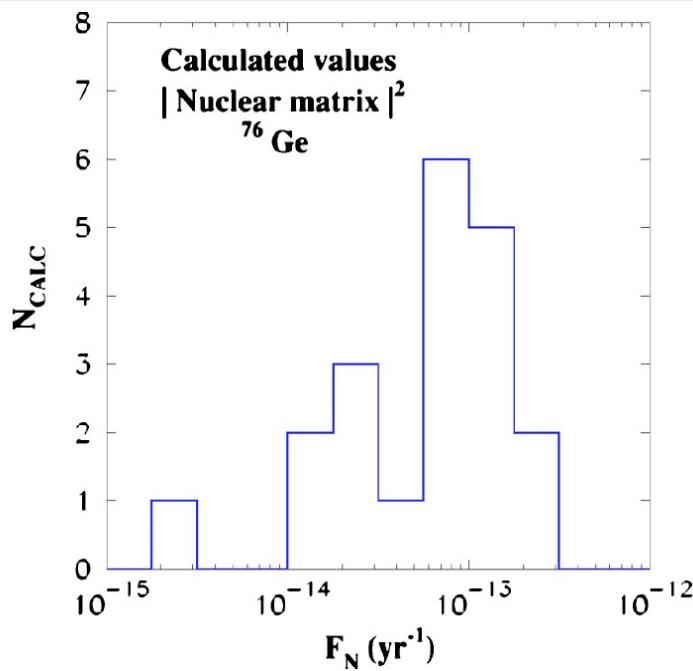
Inverted spectrum



III. $0\nu\beta\beta$ decay NMES

2004 (factor 10)

few groups, 2 nuclear
structure methods:
**Nuclear Shell Model,
QRPA**

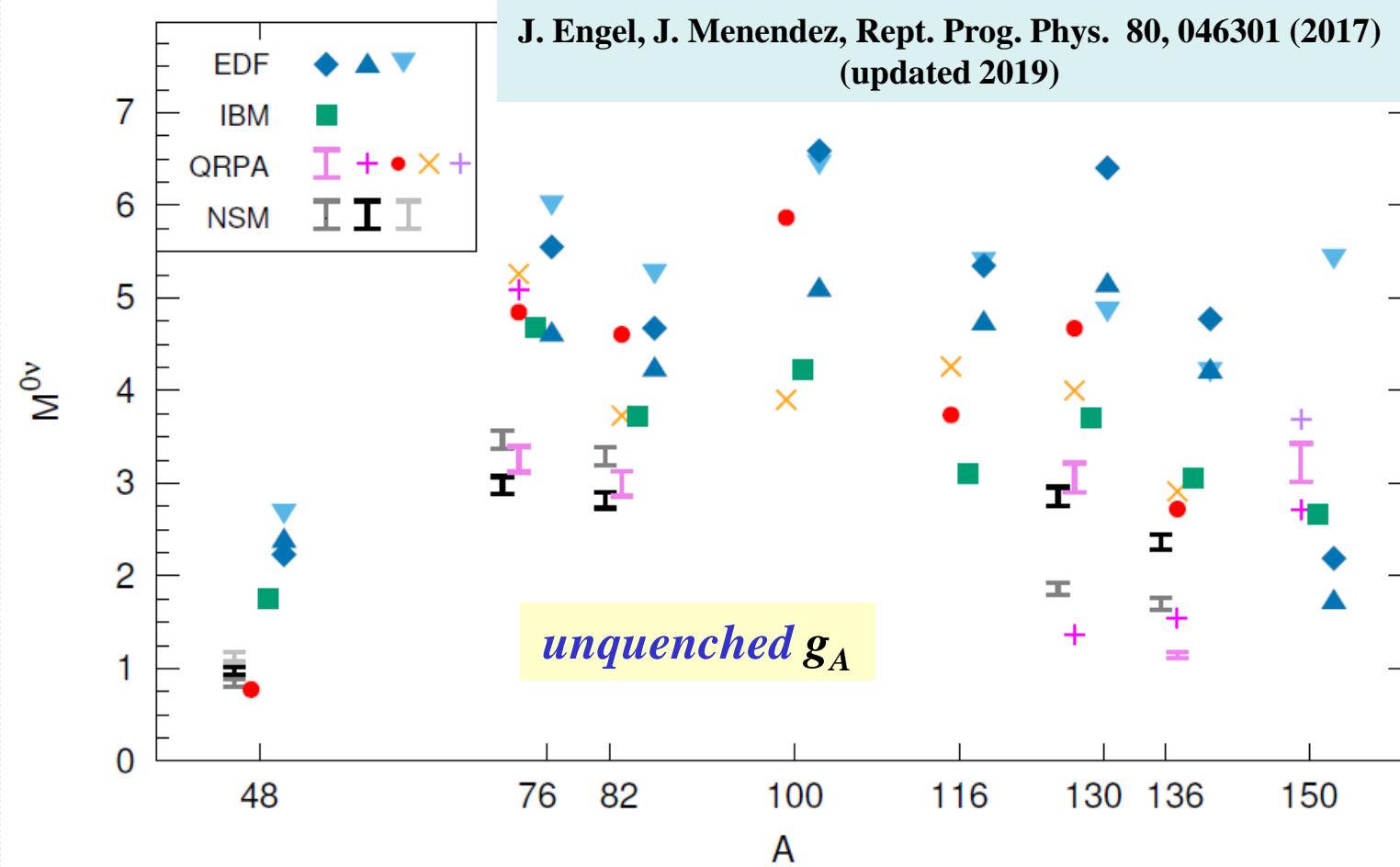


Bahcall, Maruyama, Pena-Garay,
PRC 70, 033012 (2004)

2019 (factor 2-3)

many groups, many nuclear
structure methods:
**Nuclear Shell Model, QRPA,
Interacting Boson Model, Energy
Density Functional**

Attempts (light nuclear systems):
**Ab initio calculations by different
approaches – No Core Shell Model,
Green's Function Monte Carlo,
Coupled Cluster Method, Lattice QCD**



*All
 models
 missing
 essential
 physics*

*Impossible
 to assign
 rigorous
 uncertainties*

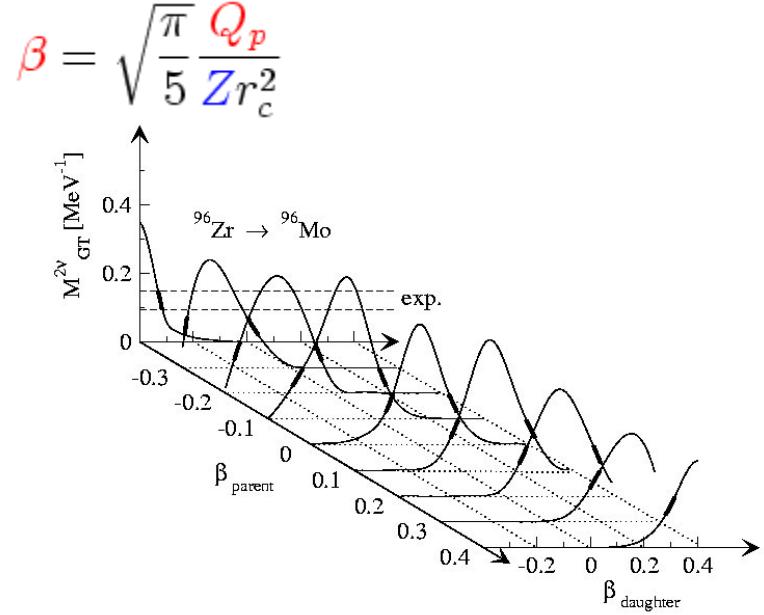
Nuclear Shell Model (Madrid-Strasbourg, Michigan, Tokyo): Relatively small model space (1 shell), all correlations included, solved by direct diagonalization

QRPA (Tuebingen-Bratislava-Calltech, Jyvaskyla, Chapel Hill, Lanzhou, Prague): Several Shells, only simple correlations included

Interacting Boson Method (Yale-Concepcion): Small space, important proton-neutron Pairing correlations missing

Energy Density Functional theory (Madrid, Beijing): >10 shells, important proton-neutron pairing missing

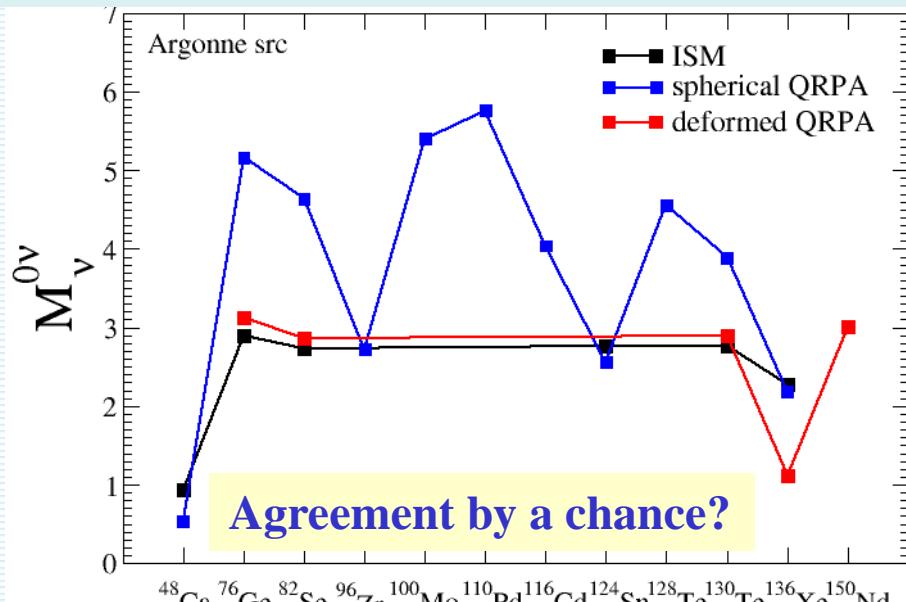
Suppression of the $\beta\beta$ -decay NMEs due to different deformation of initial and final nuclei



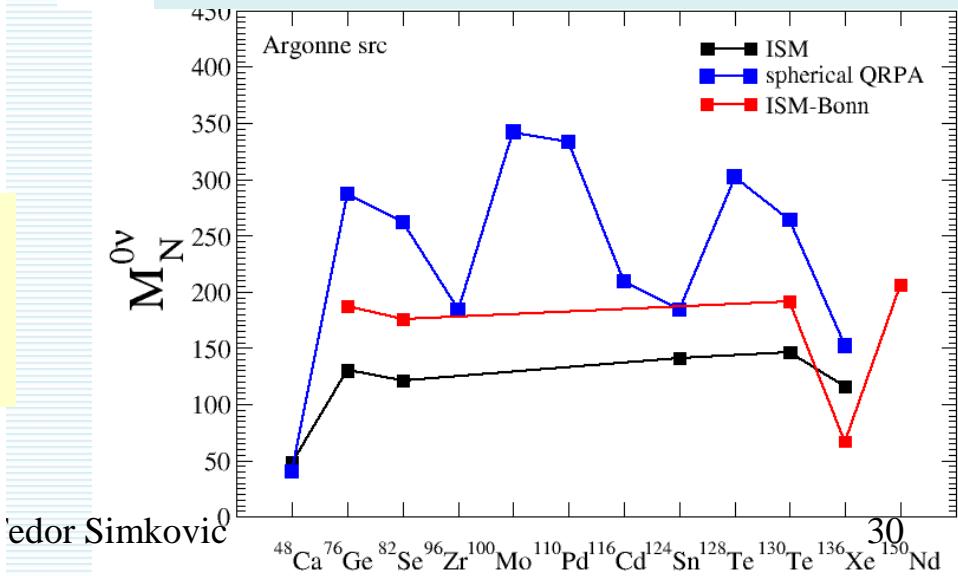
Systematic study of the deformation effect on the $2\nu\beta\beta$ -decay NME Within deformed QRPA

F.Š., Pacearescu, Faessler, NPA 733 (2004) 321

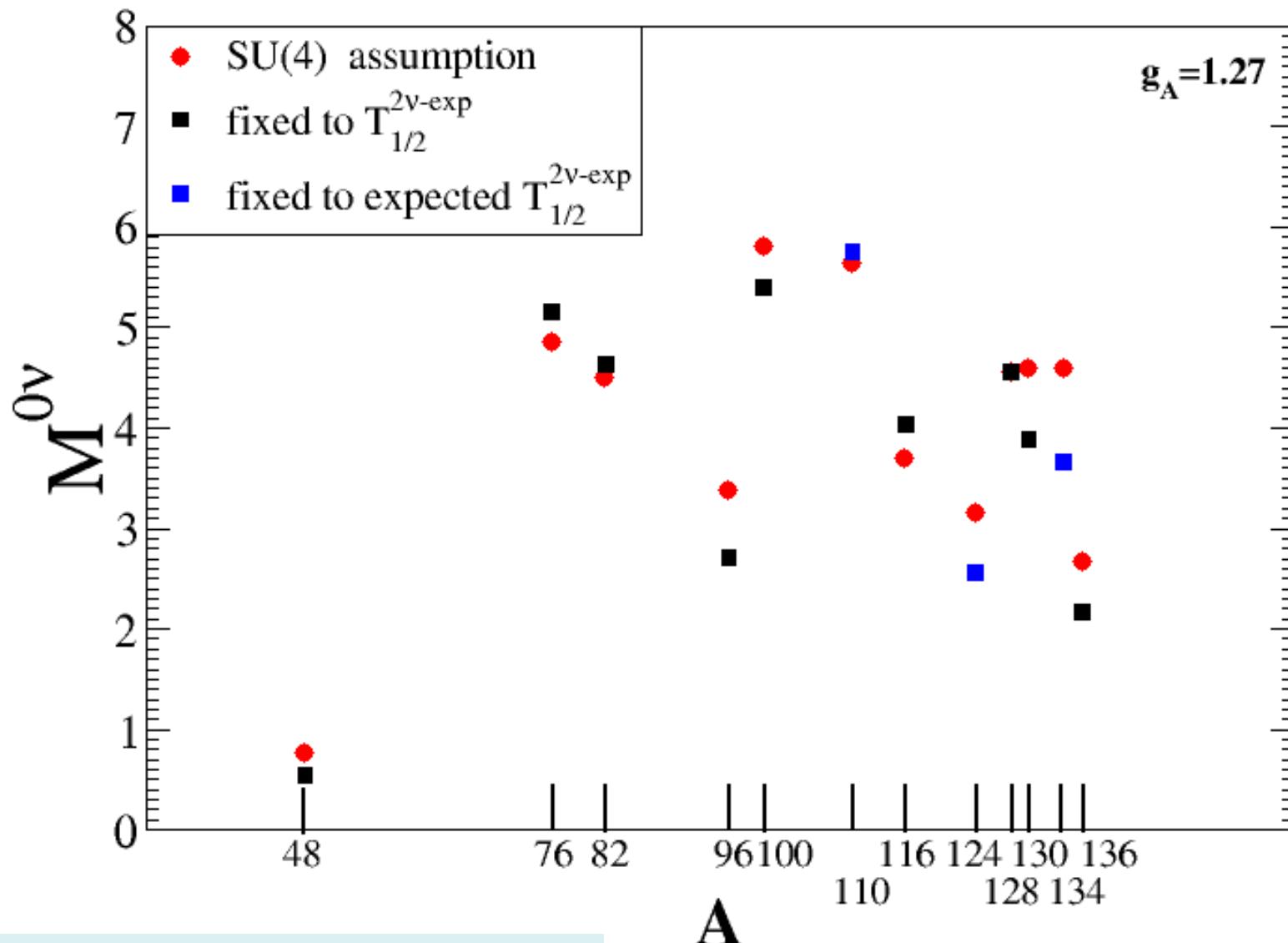
$0\nu\beta\beta$ -decay NMEs within deformed QRPA with partial restoration of isospin symmetry



D. Fang, A. Faessler, F.Š., PRC 97, 045503 (2018)



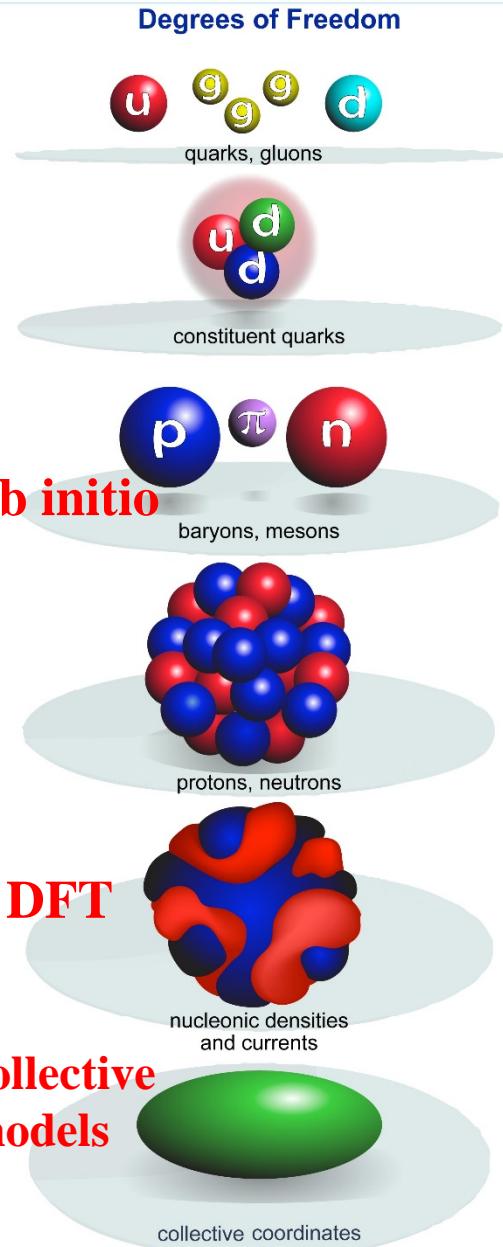
New QRPA calculations based on restoration of the SU(4) symmetry ($M^{2\nu}_{GT-cl}=0$)



Ab Initio Nuclear Structure

(Often starts with chiral effective-field theory)

Physics of Hadrons



Energy (MeV)

940
neutron mass

140
pion mass

8
proton separation
energy in lead

1.12
vibrational
state in tin

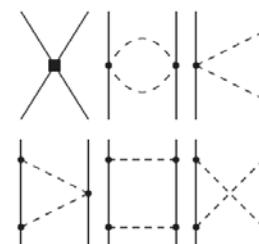
0.043
rotational
state in uranium

2N Force

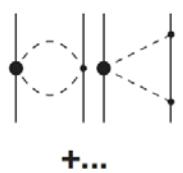
Q^0
LO



Q^2
NLO



Q^3
NNLO

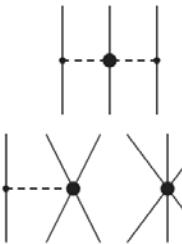


...

3N Force

4N Force

Calculation for the hypothetical $0\nu\beta\beta$ decay:
 $^{10}\text{He} \rightarrow ^{10}\text{Be} + e^- + e^-$
masses, spectra

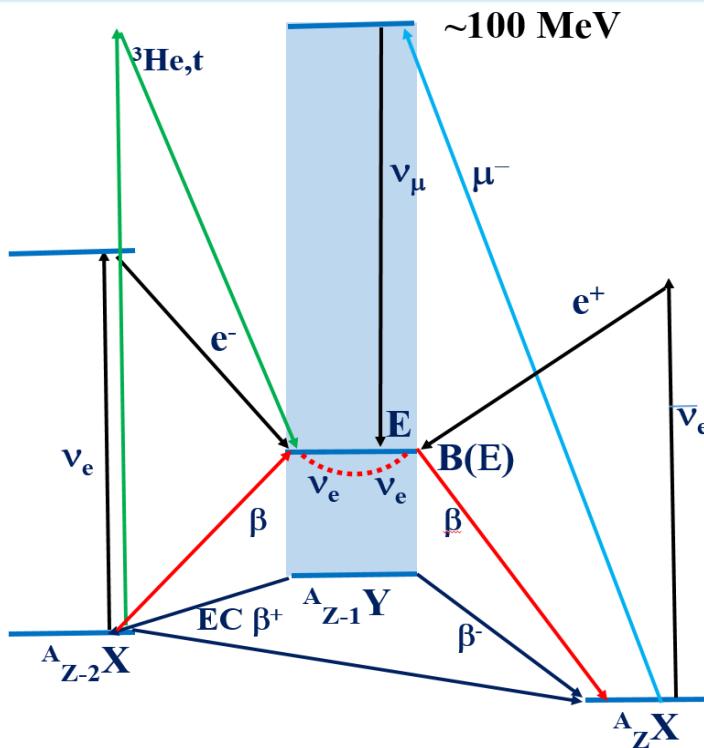


...

A. Schwenk,
P. Navratil,
J. Engel,
J. Menendez

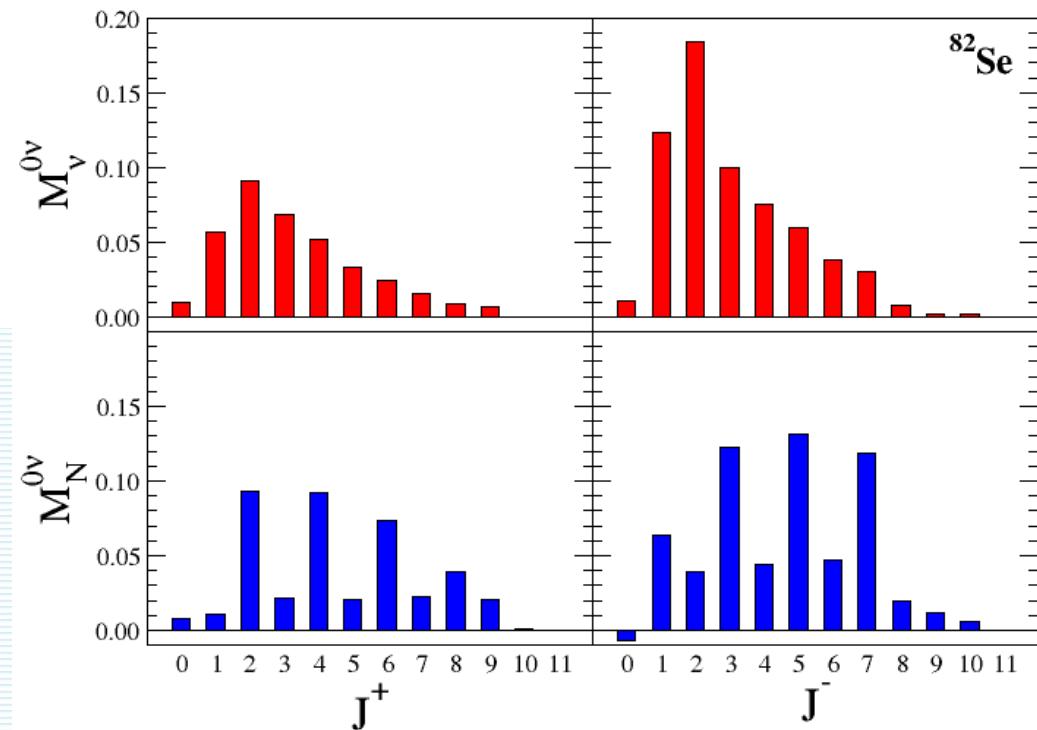
Moore's law: exponential growth in computing power

Exploiting charge-exchange reactions (${}^3\text{He},t$) and μ -capture to constrain $0\nu\beta\beta$ -decay NMEs (presentation by Hiro Ejiri)



*Higher multipoles
are populated mostly
due large ν -momenta
transfer*

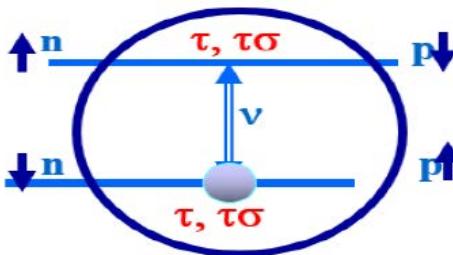
*Multipole decomposition of light and heavy
 $0\nu\beta\beta$ -decay NMEs
normalized to unity*



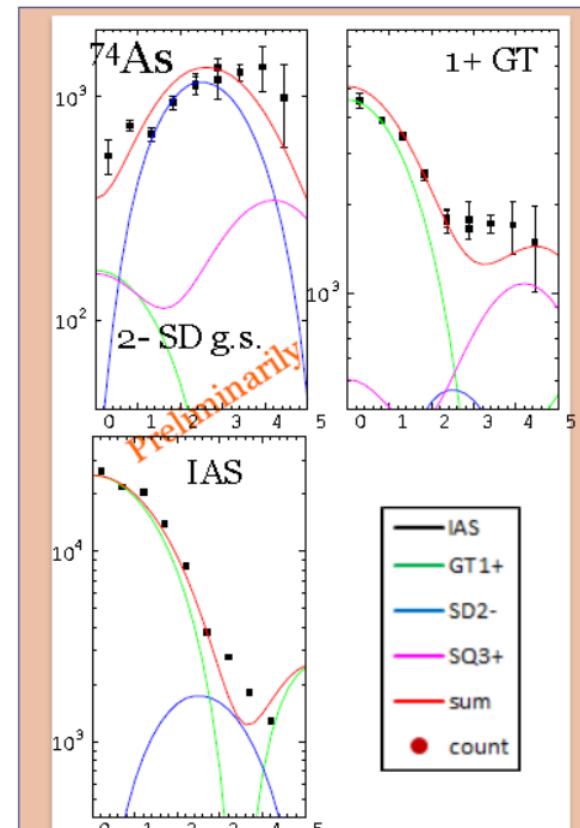
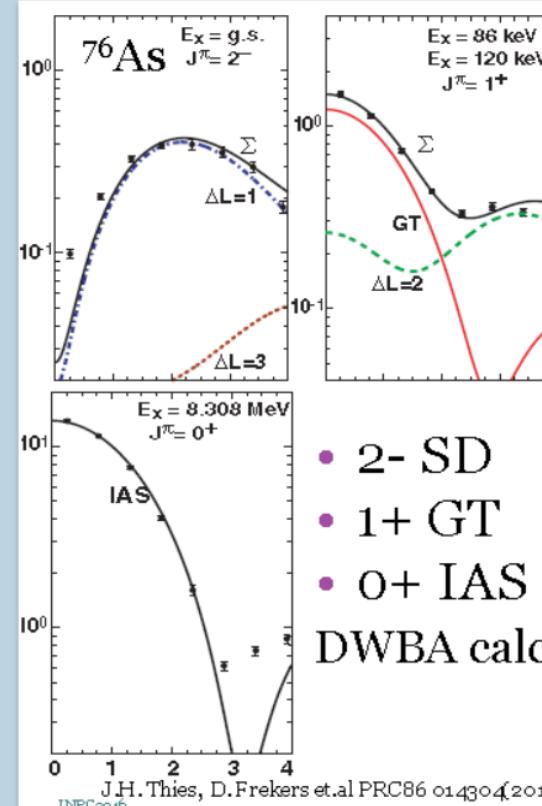


Measuring of GT-like (2^- , 3^+) strengths distribution for $^{74,76}\text{Ge} \rightarrow ^{74,76}\text{As}$ with ($^3\text{He},t$) reactions

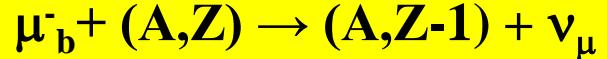
H. Akimune, H. Ejiri, RCNP,
Catania, KVI , Munster ▪ ▪



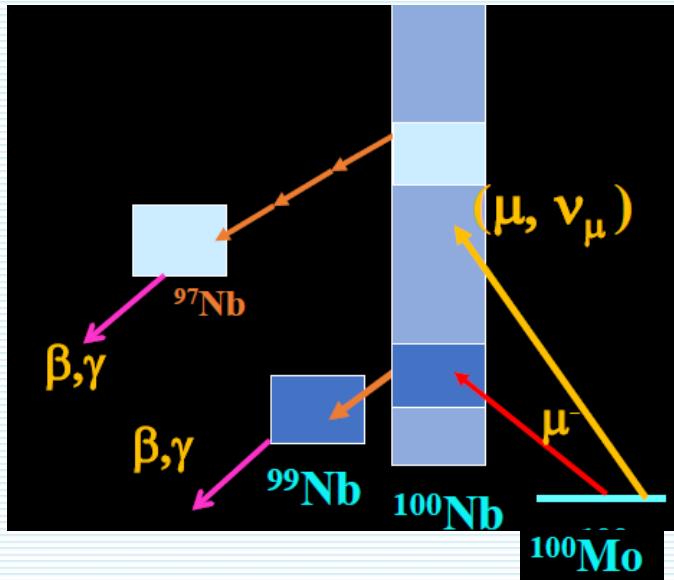
$^{74,76}\text{Ge} (^3\text{He},t) ^{74,76}\text{As}$ Angular distribution



Measurement of GT strength via μ -capture



CER ($\mu, \nu_\mu, xn\gamma$) $\nu - \beta^+$
Responses $q \sim 80$ MeV
 2^- 3^+ multipoles

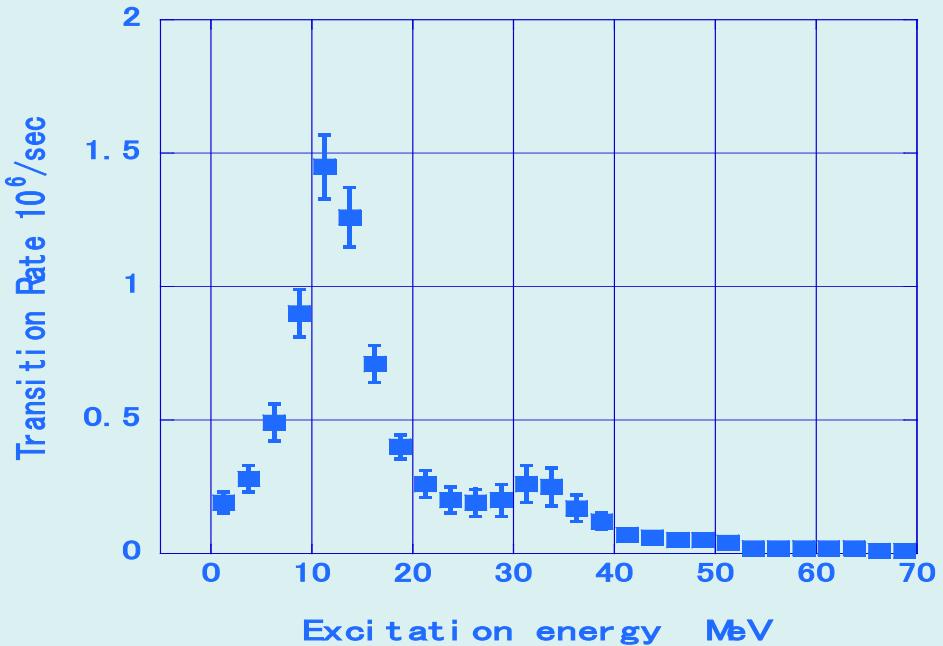


⇒ Small basis nuclear structure calculations (NSM, IBM) are disfavored. ⇒

J-PARC 3-50 GeV p, ν, μ

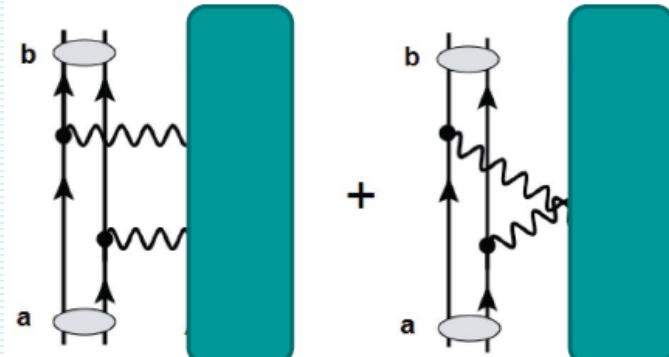
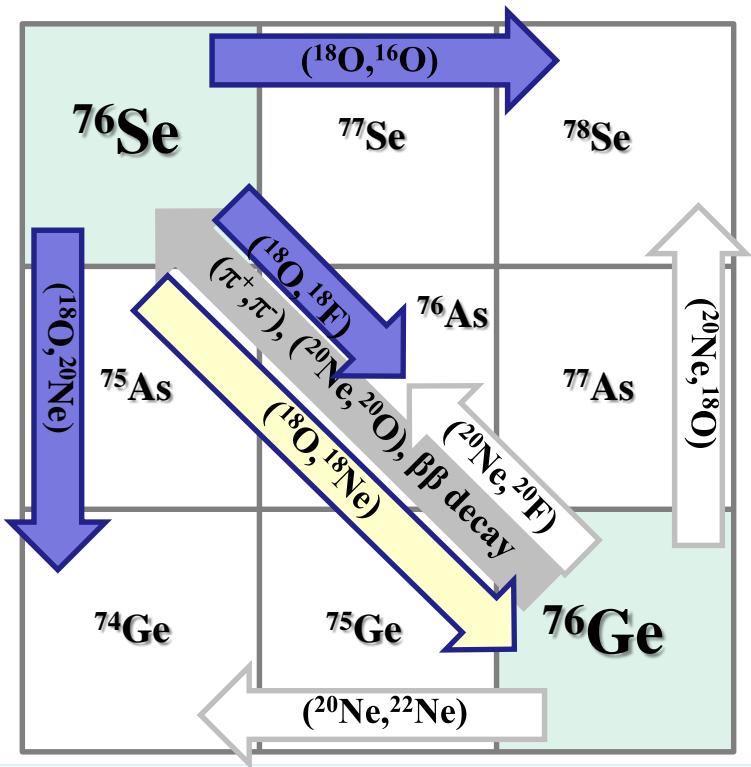


I. Hashim H. Ejiri , MXG16, PR C 97 2018



Supporting nuclear physics experiments

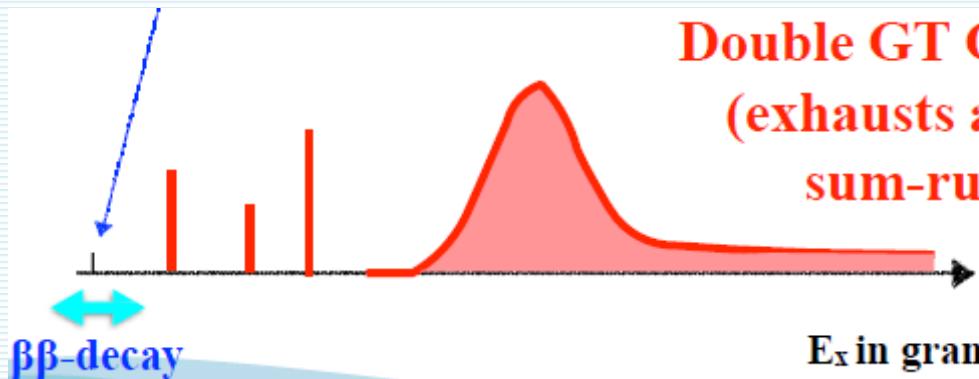
($2\nu\beta\beta$ -decay, μ -capture ChER, pion and heavy ion DCX, nucleon transfer reactions etc)

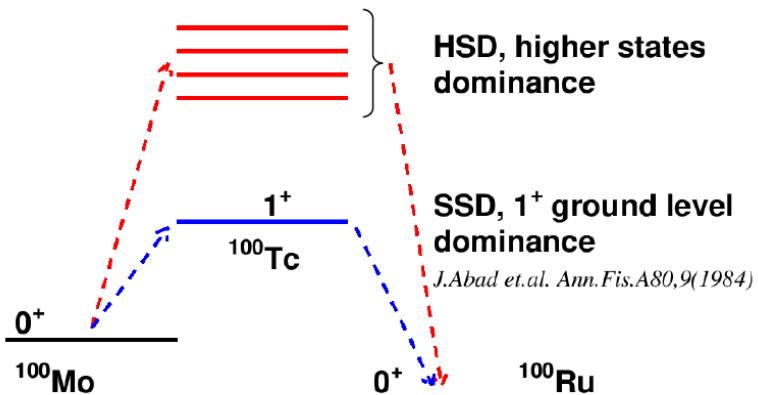


H. Lenske group
Theory of heavy ion DCX and
connection to DBD NMEs

Heavy ion DCX: **NUMEN** (LNC-INFN), **HIDCX** (RCNP/RIKEN)

Double GT Giant resonances
(exhausts a major part of
sum-rule strength)

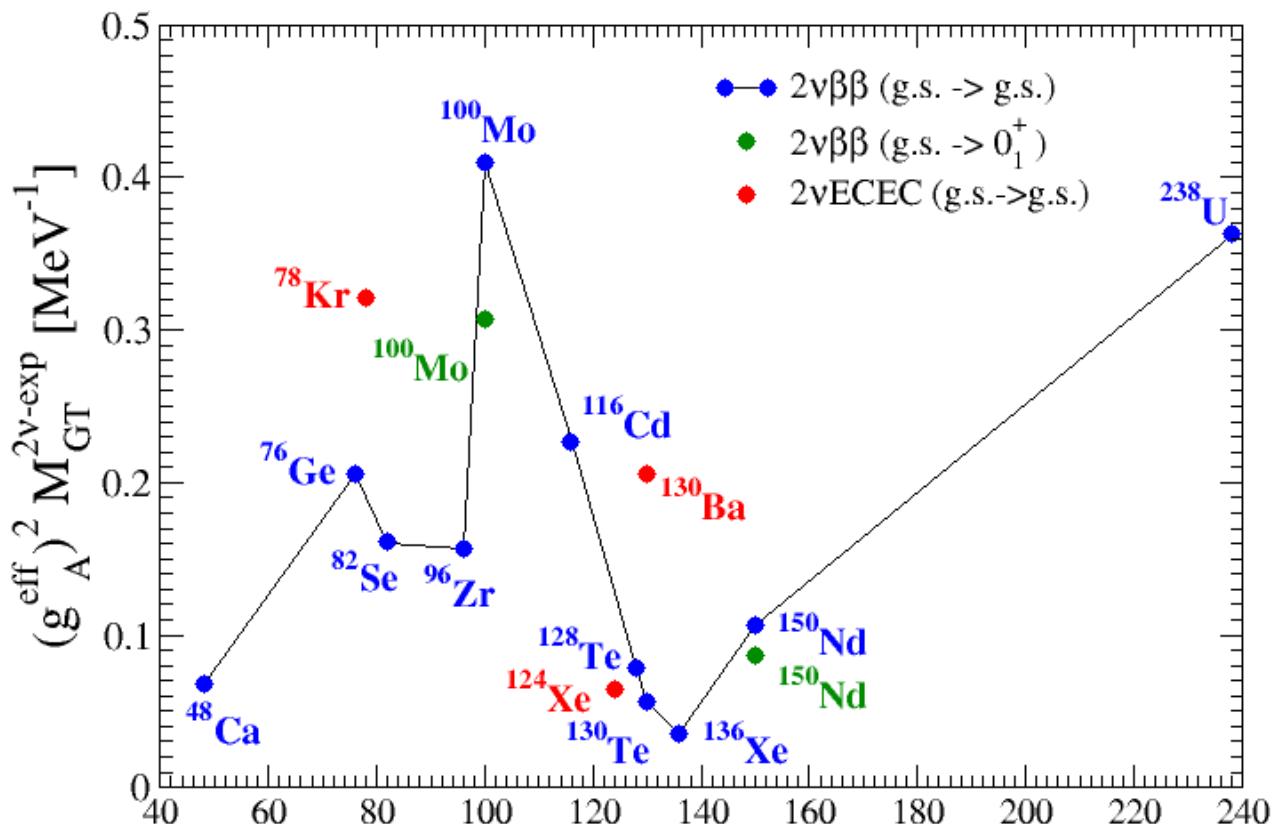




*Understanding of the 2νββ-decay NMEs
is of crucial importance for correct
evaluation of the 0νββ-decay NMEs*

$$M_{GT}^{2\nu} = \sum_m \frac{<0_f^+||\tau^+\sigma||1_m^+><1_m^+||\tau^+\sigma||0_i^+>}{E_m - E_i + \Delta}$$

There is no reliable calculation of the 2νββ-decay NMEs yet



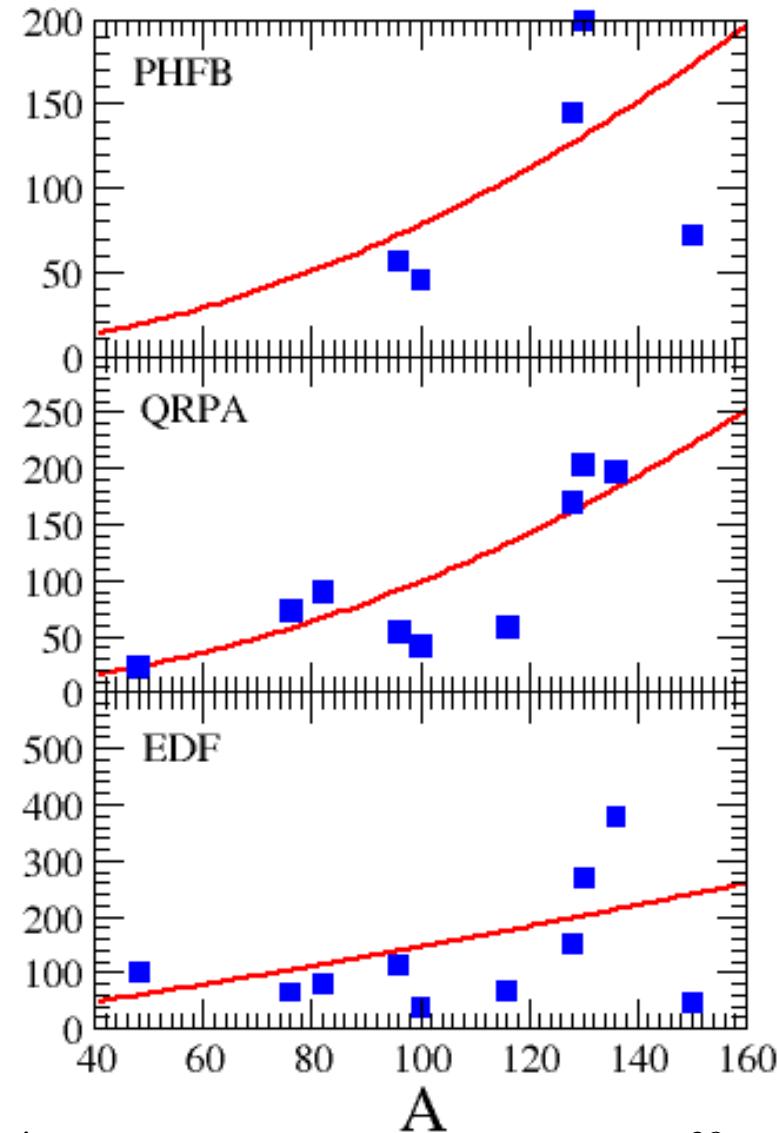
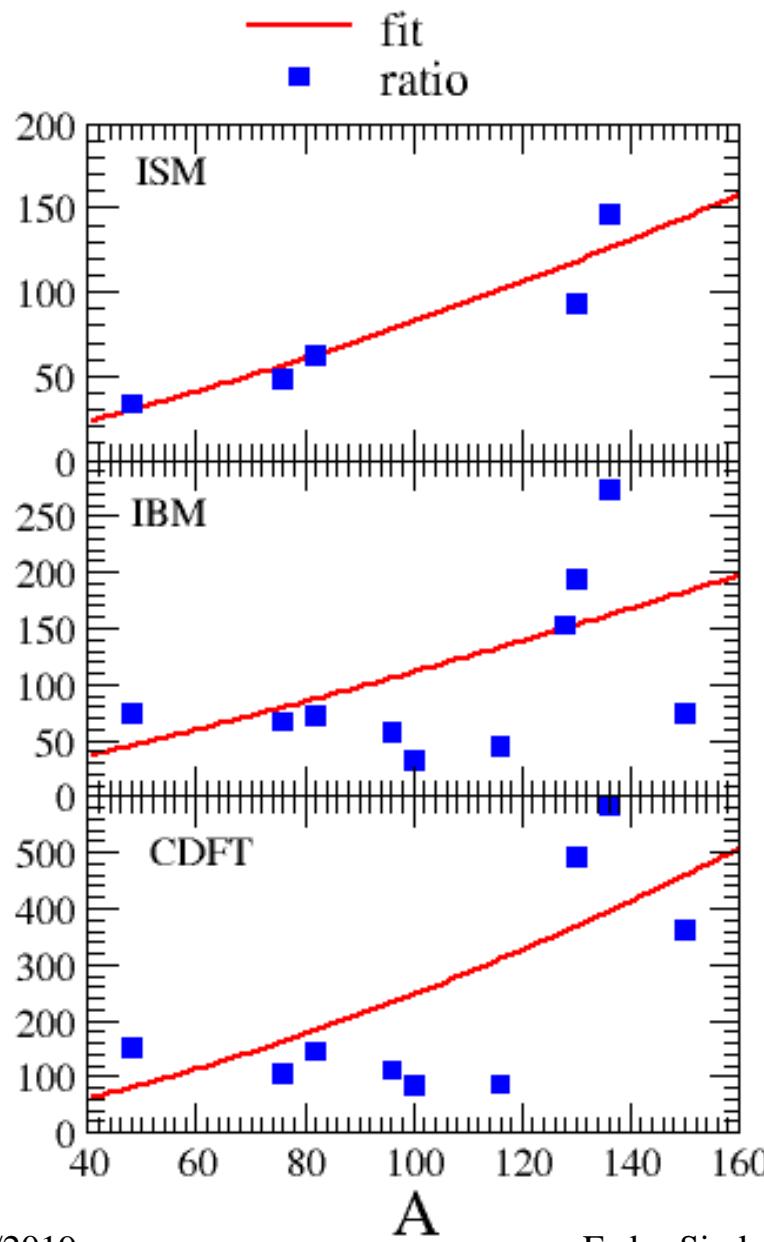
Both 2νββ and 0νββ operators connect the same states. Both change two neutrons into two protons. Explaining 2νββ-decay is necessary but not sufficient

Is there a proportionality between $0\nu\beta\beta$ - and $2\nu\beta\beta$ -decay NMEs?

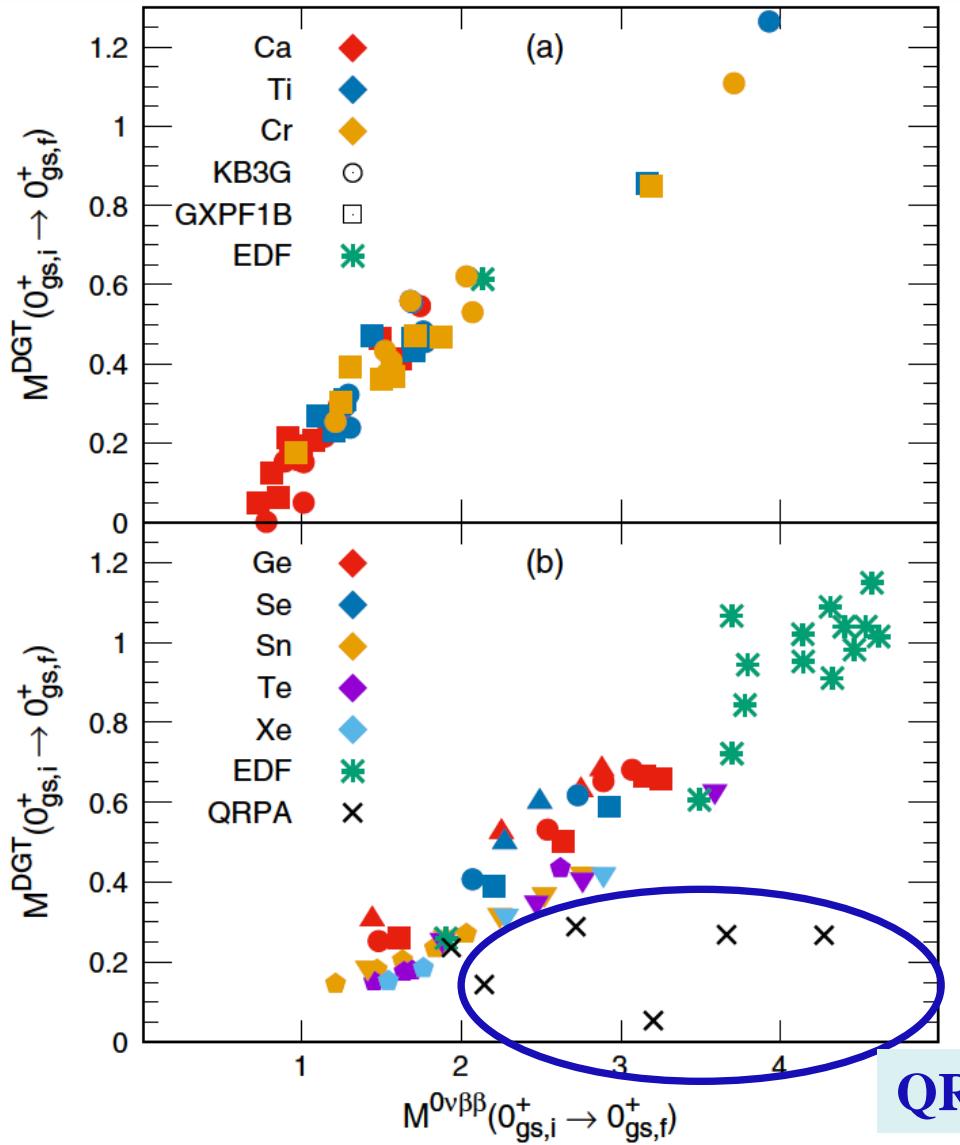
Known
from
measured
 $2\nu\beta\beta$ -
decay
half-life

$M_{\nu}^{0\nu}/(m_e M^{2\nu\text{-exp}})$

Calc.
within
nuclear
model



$M^{0\nu} \propto M^{2\nu}_{\text{GT-cl}}$: ISM, EDF



QRPA?

ISM: N. Shimizu, J. Menendez, K. Yako,
PRL 120, 142502 (2018) Fedor Simkovic

$M^{\text{DGT}} = M^{2\nu}_{\text{GT}}$

SSD ChER

^{48}Ca	0.22
^{76}Ge	0.52
^{96}Zr	0.22
^{100}Mo	0.35
^{116}Cd	0.35
^{128}Te	0.41

EDF: $0.6 \rightarrow 1.2$

ISM: $0.1 \rightarrow 0.7$

IBM: $1.6 \rightarrow 4.4$

QRPA: $|0.1| \rightarrow |0.7|$

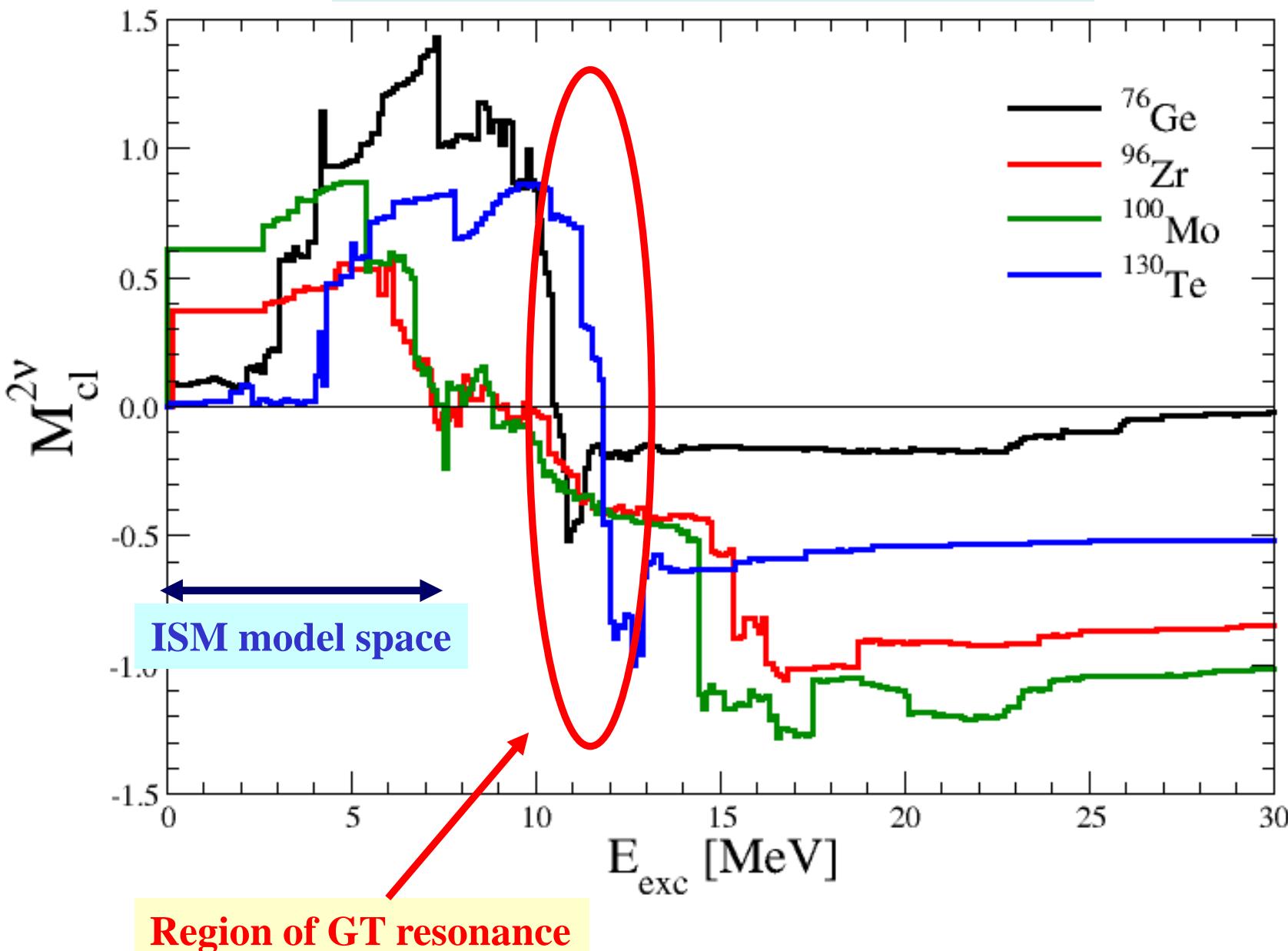
IBM: J. Barea, J. Kotila, F. Iachello,
PRC 91, 034304 (2015)

QRPA: F.Š., R. Hodák, A. Faessler, P. Vogel,
PRC 83, 015502 (2011)

M^{DGT} – only 1^+
 $M^{0\nu}$ - contribution
from many J^π (!)

QRPA: There is no proportionality between $0\nu\beta\beta$ -decay and $2\nu\beta\beta$ -decay NMEs

F.Š., R. Hodák, A. Faessler, P. Vogel, PRC 83, 015502 (2011)



A connection between closure $2\nu\beta\beta$ and $0\nu\beta\beta$ GT NMEs

F.Š., R. Hodák, A. Faessler, P. Vogel, PRC 83, 015502 (2011)
 F. Š., A. Smetana, P. Vogel, PRC 98, 064325 (2018)

Going to relative coordinates:

$$\begin{aligned} M_{\nu,N-I}^{0\nu} &= \int_0^\infty P_{I-src}^{\nu,N}(r) C_{I-cl}^{2\nu}(r) dr \\ &= \int_0^\infty f_{src}^2(r) P_I^{\nu,N}(r) C_{I-cl}^{2\nu}(r) dr \\ &\quad I = F, GT \text{ and } T \end{aligned}$$

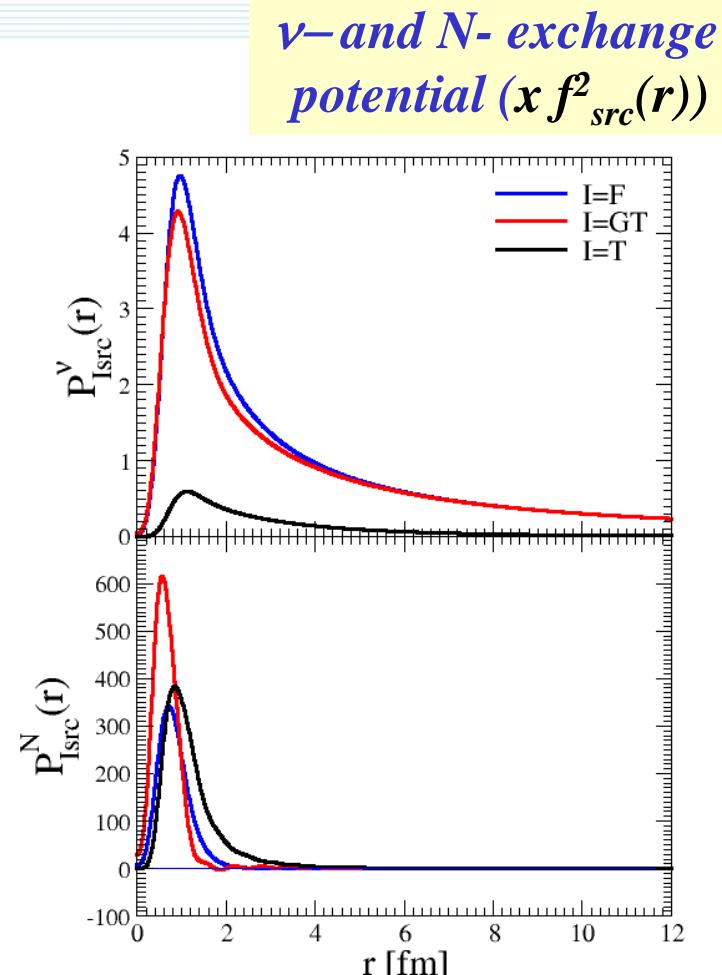
r- relative distance
of two decaying nucleons

$$M_{GT-cl}^{2\nu} = \int_0^\infty C_{GT-cl}^{2\nu}(r) dr$$

$$M_{GT-cl}^{2\nu} =$$

$$\sum_{J^\pi, m} \langle 0_f^+ | \tau^+ \vec{\sigma} | J^\pi, m \rangle \cdot \langle J^\pi, m | \tau^+ \vec{\sigma} | 0_i^+ \rangle$$

$$\sum_m \langle 0_f^+ | \tau^+ \vec{\sigma} | 1^+, m \rangle \cdot \langle 1^+, m | \tau^+ \vec{\sigma} | 0_i^+ \rangle$$



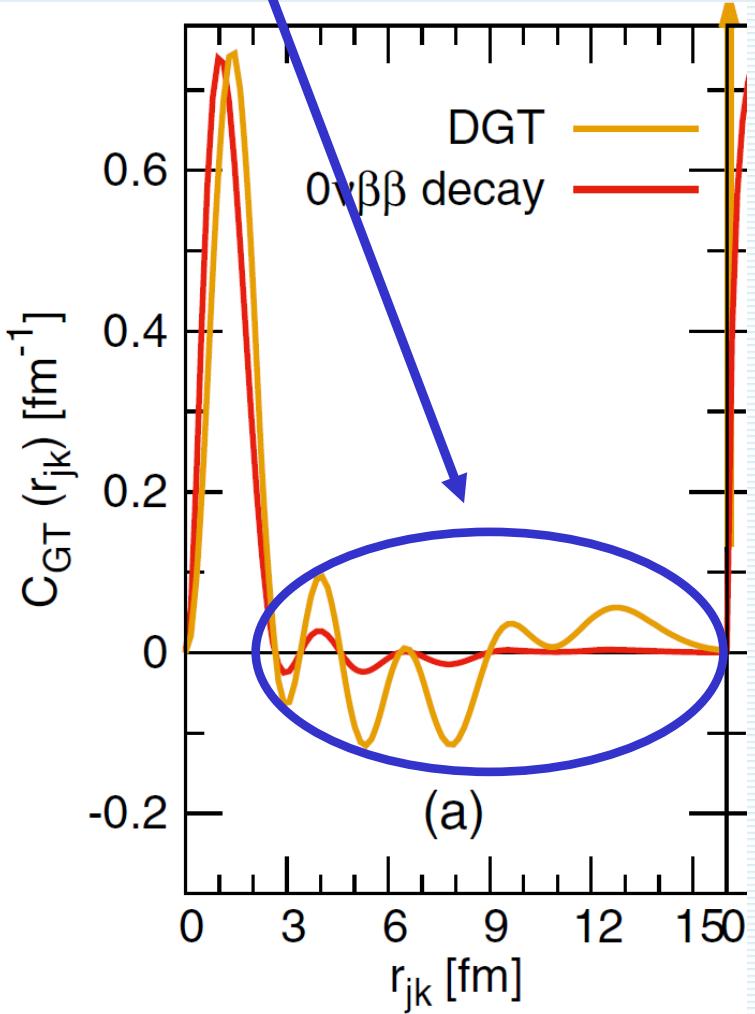
Neutrino potential prefers short distances

imkov

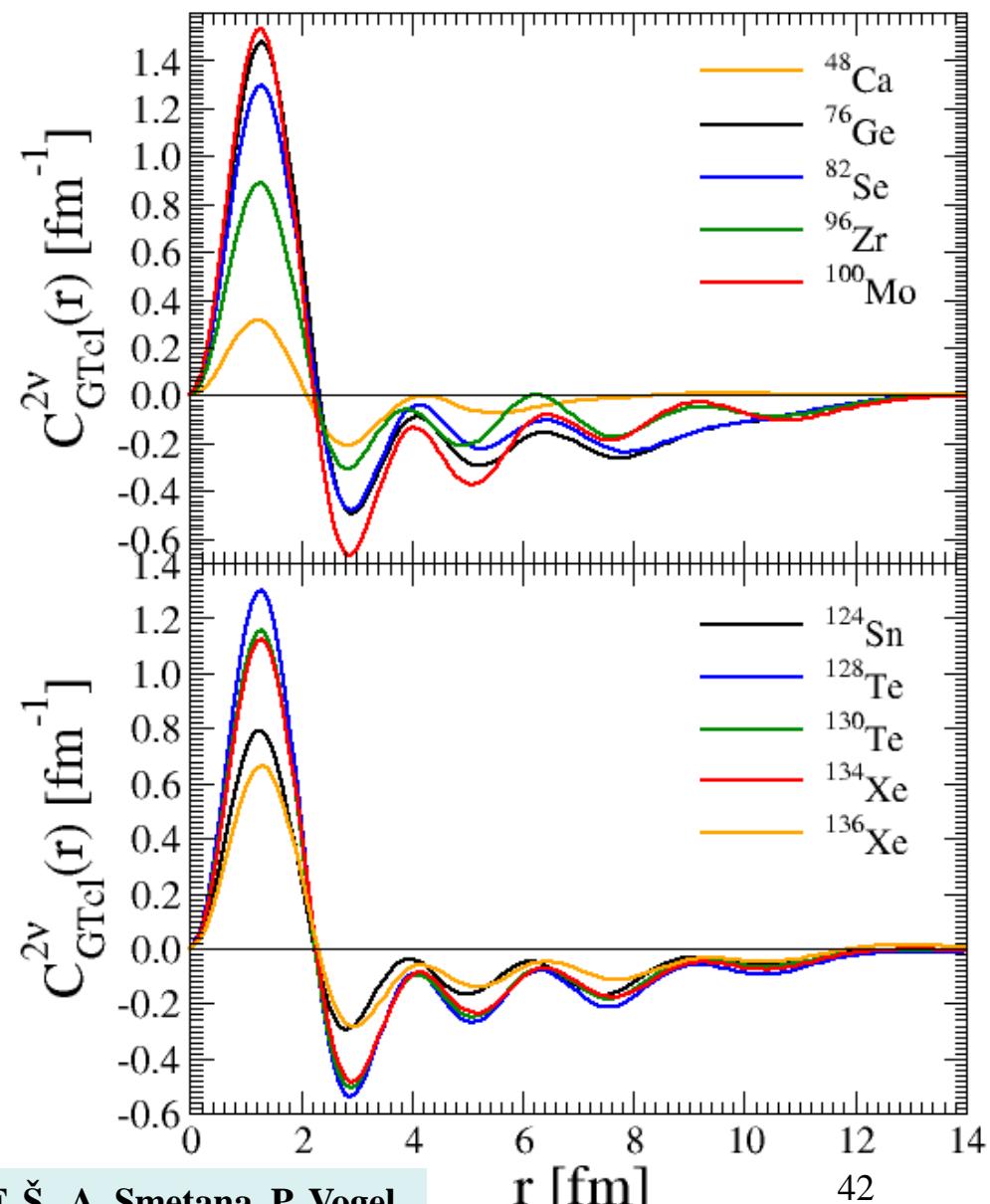
QRPA: Bump \approx - Tail $\Rightarrow M^{2\nu}_{\text{cl}} \approx 0$

**Close to restoration of the SU(4) symmetry
of residual Hamiltonian**

ISM: Tail ≈ 0 (?) $\Rightarrow M^{2\nu}_{\text{cl}} \gg 0$

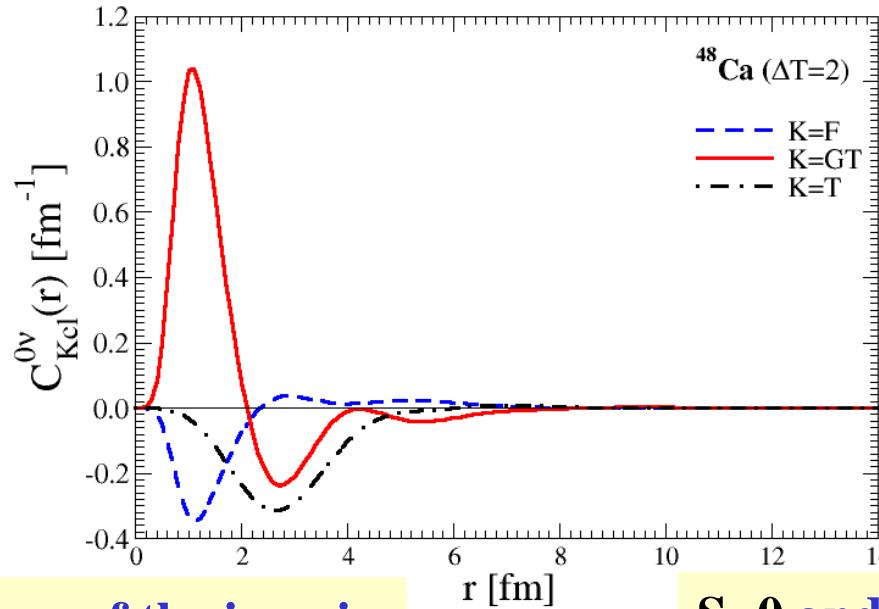


N. Shimizu, J. Menendez, K. Yako,
PRL 120, 142502 (2018)

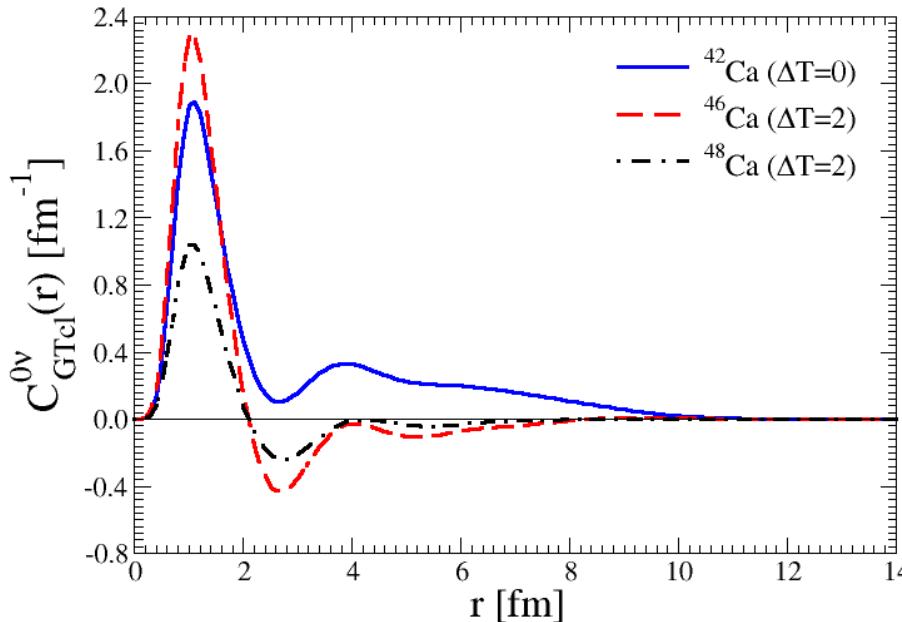


F. Š., A. Smetana, P. Vogel,
PRC 98, 064325 (2018)

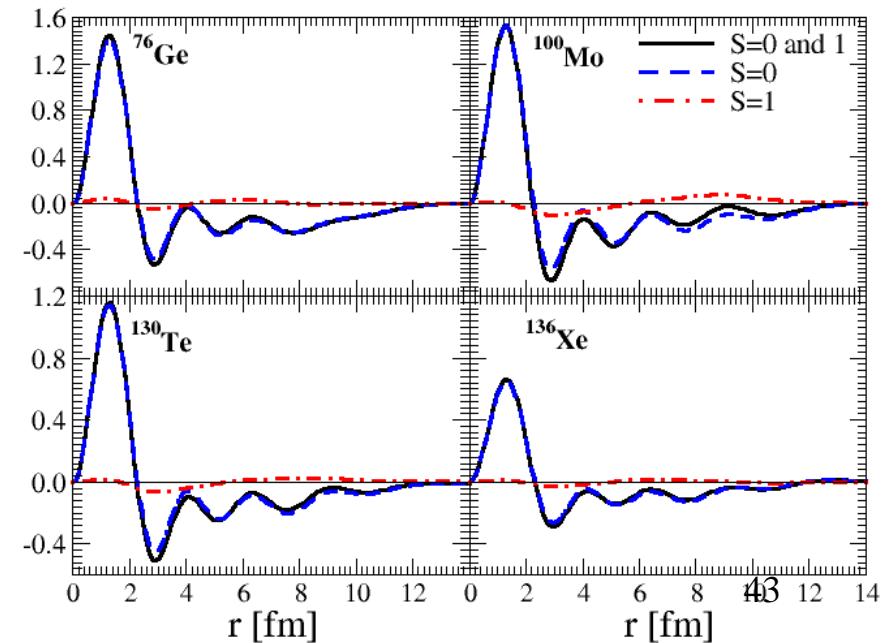
Fermi, Gamow-Teller and tensor



Role of the change of the isospin



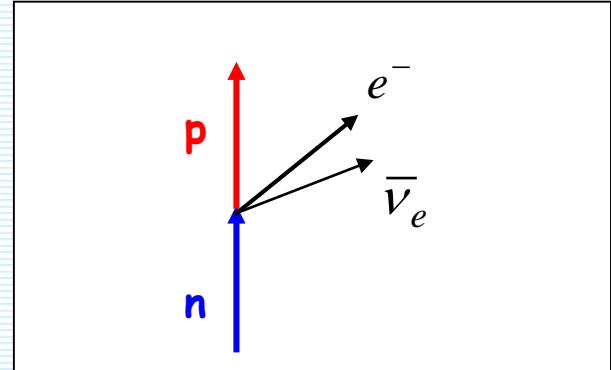
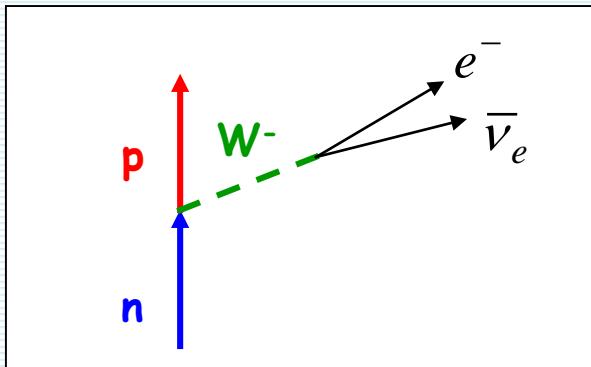
S=0 and S=1 contributions



V. Quenching of g_A ($q = g_{eff}^A / g_{free}^A$)

Should g_A be quenched in medium?
Missing wave-function correlations
Renormalized operator?
Neglected two-body currents?
Model-space truncations?

Quenching in nuclear matter: $g_{\text{eff}}^{\text{eff}}_A = q g_{\text{free}}^{\text{free}}_A$



$$\mathcal{L} = -\frac{G_\beta}{\sqrt{2}} [\bar{u}\gamma^\alpha(1-\gamma^5)d] [\bar{e}\gamma^\alpha(1-\gamma^5)\nu_e] \quad \mathcal{L} = -\frac{G_\beta}{\sqrt{2}} [\bar{p}\gamma^\alpha(g_V - g_A\gamma^5)n] [\bar{e}\gamma^\alpha(1-\gamma^5)\nu_e]$$

CVC hypothesis

$g_V = 1$ at the quark level

$g_V = 1$ at the nucleon level

$g_V = 1$ inside nuclei

Quenching of g_A

$g_A = 1$ at the quark level

$g_{\text{free}}^{\text{free}}_A = 1.27$ at the nucleon level

$g_{\text{eff}}^{\text{eff}}_A = ?$ inside nuclei

ISM: $(g_{\text{eff}}^{\text{eff}}_A)^4 \simeq 0.66$ (^{48}Ca), 0.66 (^{76}Ge), 0.30 (^{76}Se), 0.20 (^{130}Te) and 0.11 (^{136}Xe)

QRPA: $(g_{\text{eff}}^{\text{eff}}_A)^4 = 0.30$ and 0.50 for ^{100}Mo and ^{116}Cd

IBM: $(g_{\text{eff}}^{\text{eff}}_A)^4 \simeq (1.269 A^{-0.18})^4 = 0.063$

Faessler, Fogli, Lisi, Rodin, Rotunno, F. Š,
J. Phys. G 35, 075104 (2008).

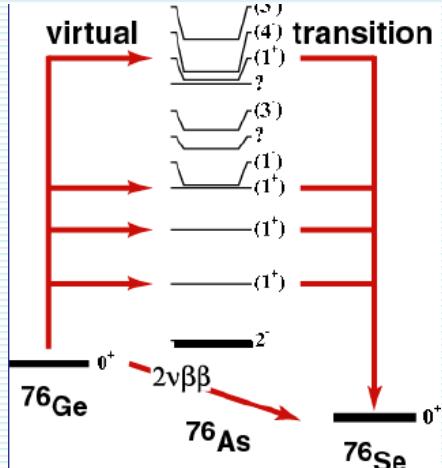
$$g_A^4 = (1.269)^4 = 2.6$$

Quenching of g_A (from exp.: $T_{1/2}^{0\nu}$ up 2.5 x larger)

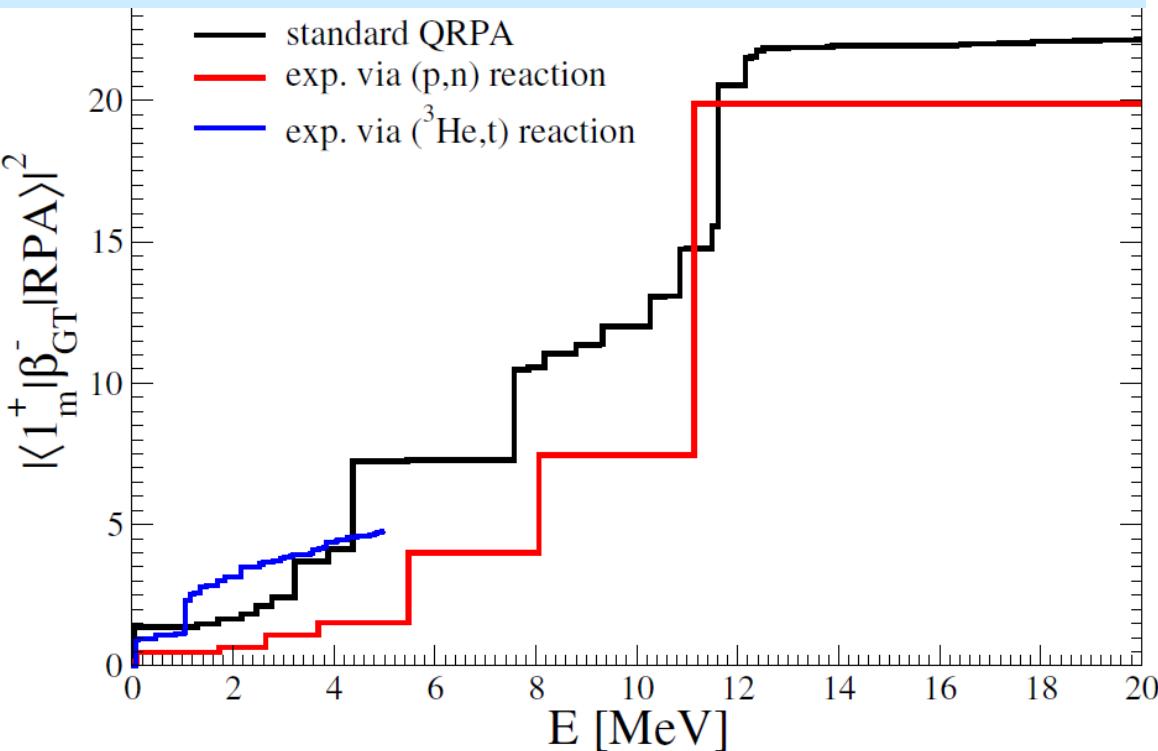
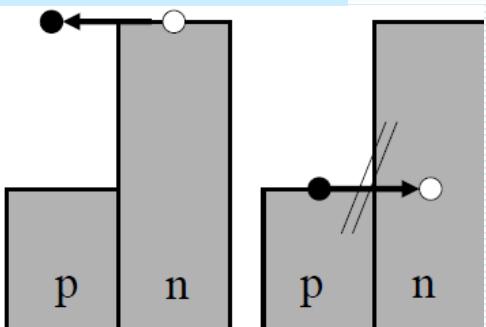
$$(g_A^{\text{eff}})^4 = 1.0$$

Strength of GT trans. (approx. given by **Ikeda sum rule** = $3(N-Z)$) has to be quenched to reproduce experiment.

$$\begin{array}{c} {}^{76}_{32}\text{Ge} \xrightarrow{44} \\ S_\beta^- - S_\beta^+ = 3(N-Z) = 36 \end{array}$$



Pauli blocking



Cross-section for charge exchange reaction:

$$\left[\frac{d\sigma}{d\Omega} \right] = \left[\frac{\mu}{\pi \hbar} \right]^2 \frac{k_f}{k_i} N_d |v_{\sigma\tau}|^2 |\langle f | \sigma\tau | i \rangle|^2$$

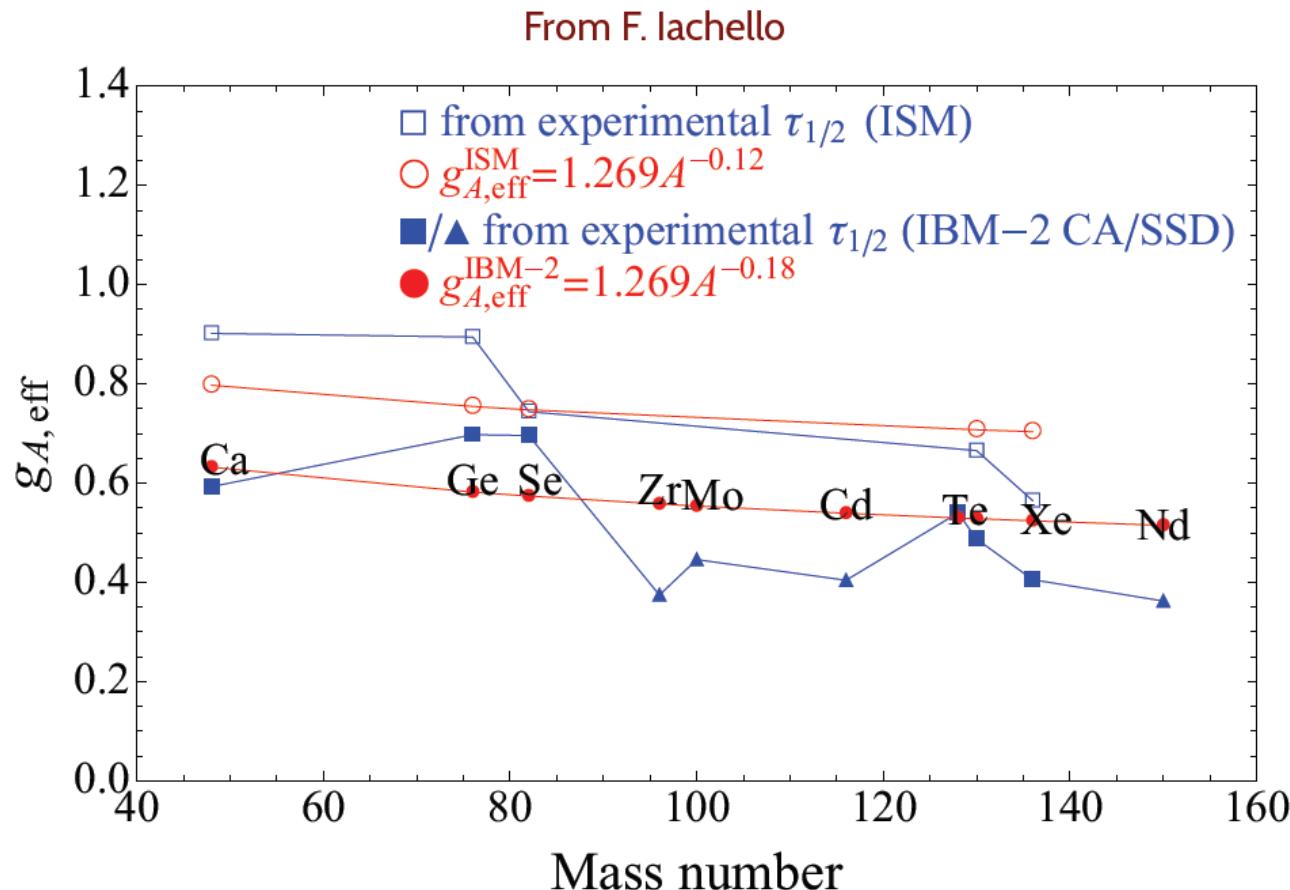
$q = 0!!$

largest at 100 - 200 MeV/A

Quenching of g_A -IBM ($T_{1/2}^{0\nu}$ suppressed up to factor 50)

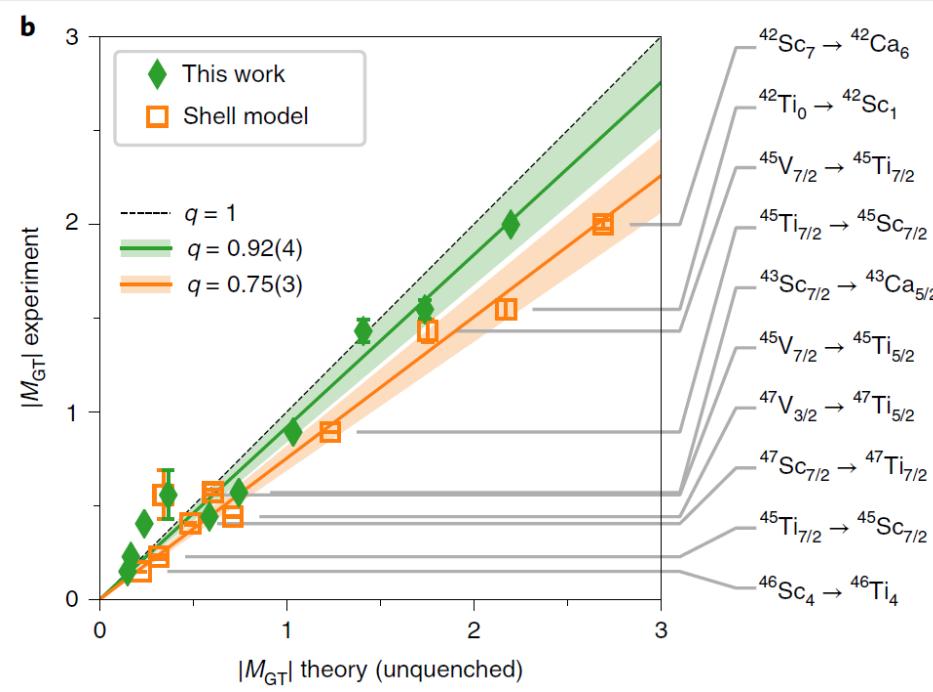
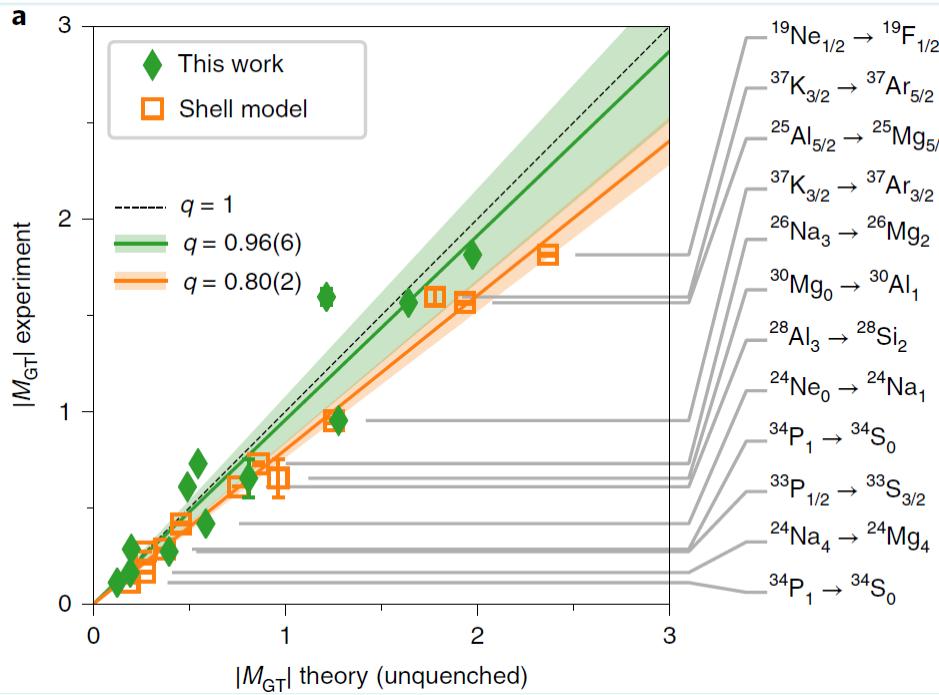
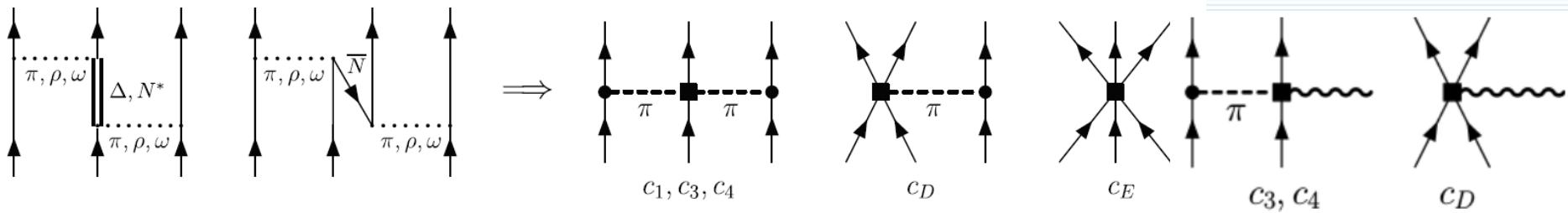
$(g_{A,\text{eff}}^{\text{ISM}})^4 \simeq (1.269 \text{ A}^{-0.18})^4 = 0.063$ (The Interacting Boson Model). This is an incredible result. The quenching of the axial-vector coupling within the IBM-2 is more like 60%.

It has been determined by theoretical prediction for the $2\nu\beta\beta$ -decay half-lives, which were based on within closure approximation calculated Corresponding NMEs, with the measured half-lives.



Discrepancy between experimental and theoretical β -decay rates resolved from first principles

Ab initio calculations
(light nuclear systems)
including meson-
exchange
currents do not need
any “quenching”

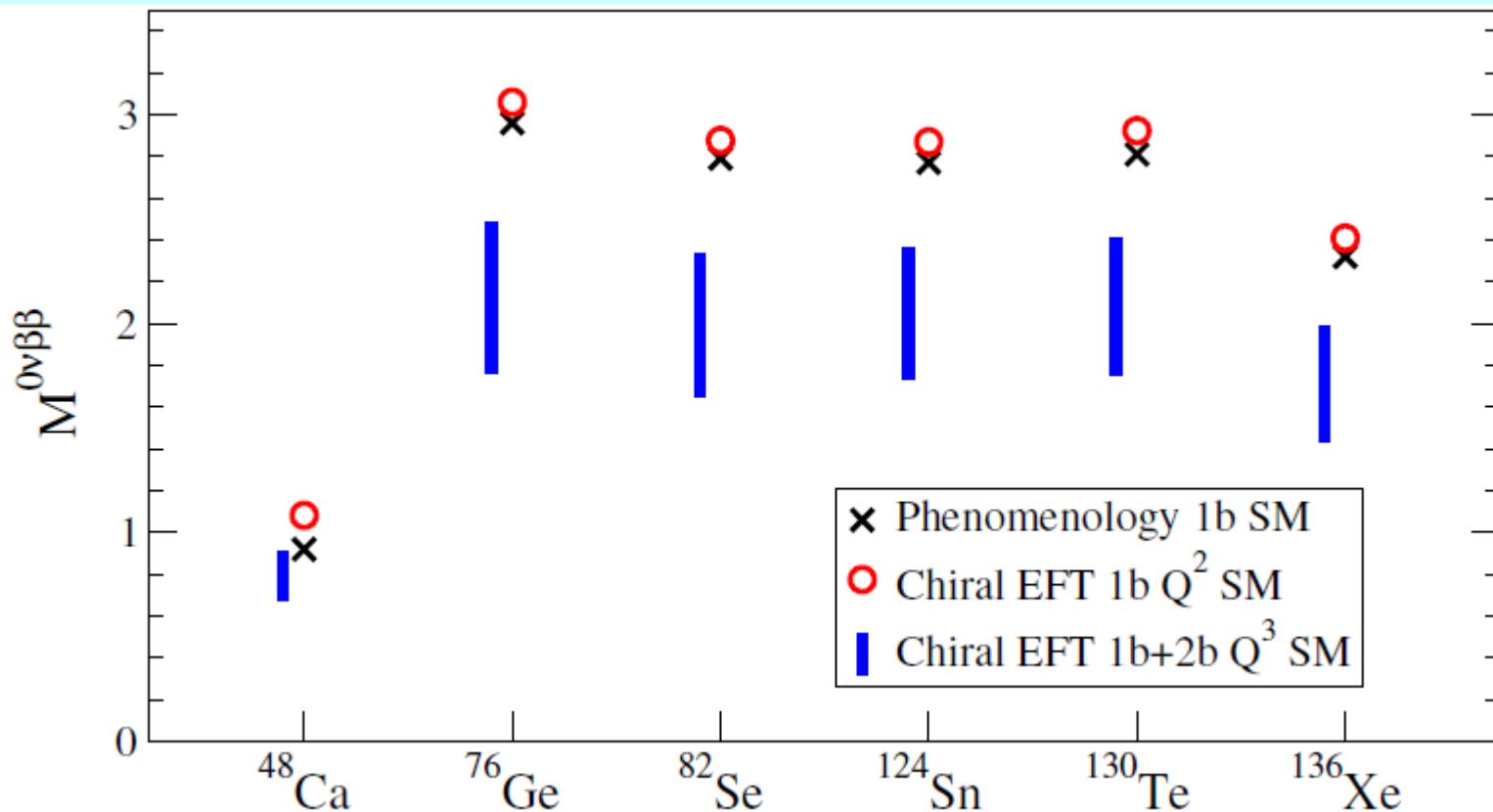


Quenching of g_A and two-body currents

Menendez, Gazit, Schwenk, PRL 107 (2011) 062501; MEDEX13 contribution

$$\mathbf{J}_{i,2b}^{\text{eff}} = -g_A \boldsymbol{\sigma}_i \tau_i^- \frac{\rho}{F_\pi^2} \left[\frac{2}{3} c_3 \frac{p^2}{4m_\pi^2 + p^2} + I(\rho, P) \left(\frac{1}{3} (2c_4 - c_3) + \frac{1}{6m} \right) \right] = -g_A \delta(p) \boldsymbol{\sigma}_i \tau_i^-$$

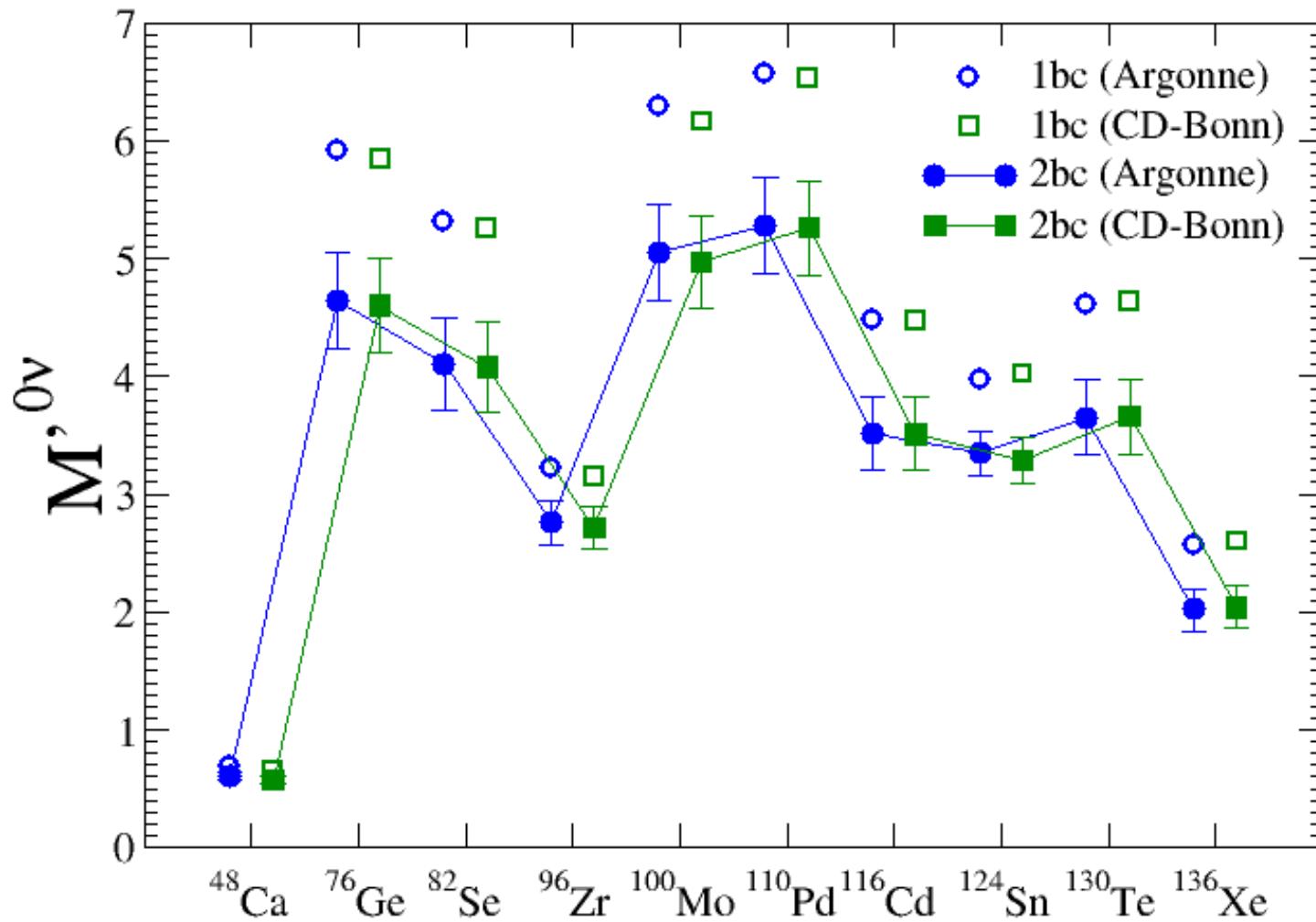
The $0\nu\beta\beta$ operator calculated within effective field theory. Corrections appear as 2-body current predicted by EFT. The 2-body current contributions are related to the quenching of Gamow-Teller transitions found in nuclear structure calc.



Quenching of g_A , two-body currents and QRPA

(*Suppression of the $0\nu\beta\beta$ -decay NME of about 20%*)

Engel, Vogel, Faessler, F.Š., PRC 89 (2014) 064308



But, a strong suppression of $2\nu\beta\beta$ -decay half-life, ($g_A^{\text{eff}} = g_A \delta(p=0) = 0.7\text{-}1.0$)

Improved description of the $0\nu\beta\beta$ -decay rate (and novel approach of fixing g_A^{eff})

F. Š, R. Dvornický, D. Štefánik, A. Faessler, PRC 97, 034315 (2018).

**Let perform
Taylor expansion**

$$M_{GT}^{K,L} = m_e \sum_n M_n \frac{E_n - (E_i + E_f)/2}{[E_n - (E_i + E_f)/2]^2 - \varepsilon_{K,L}^2}$$

$$\frac{\varepsilon_{K,L}}{E_n - (E_i + E_f)/2} \quad \begin{aligned} \epsilon_K &= (E_{e_2} + E_{\nu_2} - E_{e_1} - E_{\nu_1})/2 \\ \epsilon_L &= (E_{e_1} + E_{\nu_2} - E_{e_2} - E_{\nu_1})/2 \end{aligned} \quad \epsilon_{K,L} \in \left(-\frac{Q}{2}, \frac{Q}{2}\right)$$

We get

$$\left[T_{1/2}^{2\nu\beta\beta}\right]^{-1} \simeq \left(g_A^{\text{eff}}\right)^4 \left|M_{GT-3}^{2\nu}\right|^2 \frac{1}{|\xi_{13}^{2\nu}|^2} \left(G_0^{2\nu} + \xi_{13}^{2\nu} G_2^{2\nu}\right)$$

$$M_{GT-1}^{2\nu} = \sum_n M_n \frac{1}{(E_n - (E_i + E_f)/2)}$$

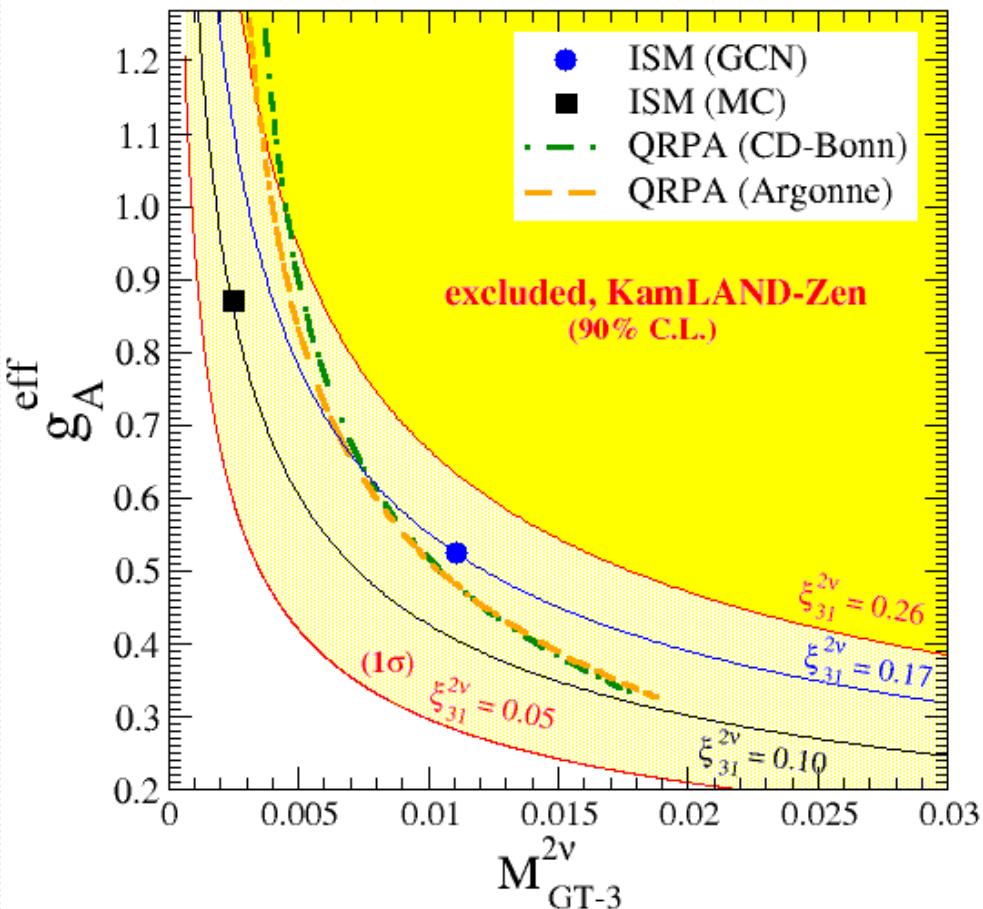
$$M_{GT-3}^{2\nu} = \sum_n M_n \frac{4 m_e^3}{(E_n - (E_i + E_f)/2)^3}$$

$$\xi_{13}^{2\nu} = \frac{M_{GT-3}^{2\nu}}{M_{GT-1}^{2\nu}}$$

The g_A^{eff} can be determined with measured half-life and ratio of NMEs and calculated NME dominated by transitions through low lying states of the intermediate nucleus (ISM?)

The g_A^{eff} can be determined with measured half-life and ratio of NMEs $\xi_{31}^{2\nu}$ and calculated NME dominated by transitions through low lying states of the intermediate nucleus.

$M_{\text{GT-3}}$ have to be calculated by nuclear theory - ISM



$$(g_A^{\text{eff}})^2 = \frac{1}{|M_{\text{GT-3}}^{2\nu}|} \frac{|\xi_{13}^{2\nu}|}{\sqrt{T_{1/2}^{2\nu-\text{exp}} (G_0^{2\nu} + \xi_{13}^{2\nu} G_2^{2\nu})}}$$

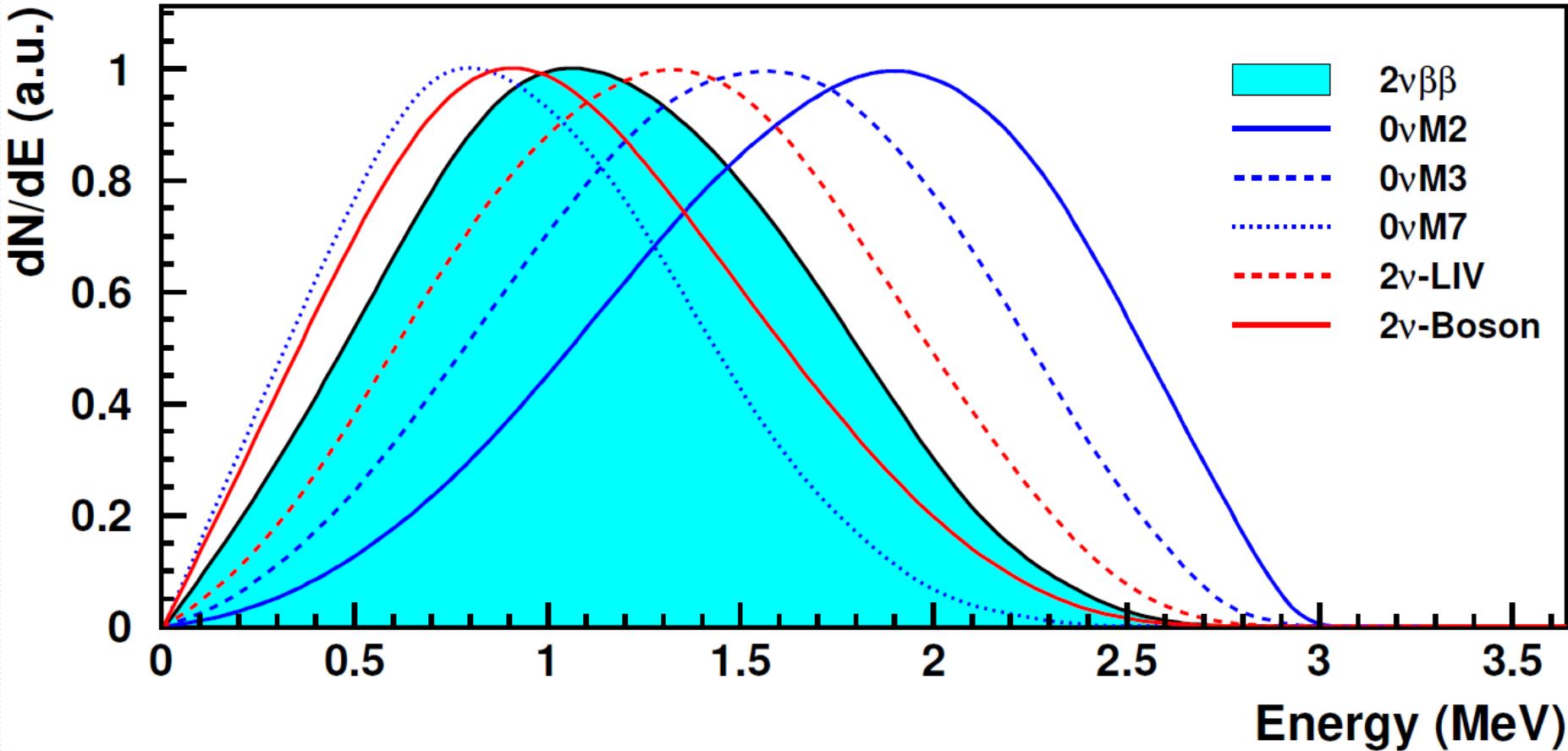
$$M_{\text{GT-1}}^{2\nu} = \sum_n M_n \frac{1}{(E_n - (E_i + E_f)/2)}$$

$$M_{\text{GT-3}}^{2\nu} = \sum_n M_n \frac{4 m_e^3}{(E_n - (E_i + E_f)/2)^3}$$

$$\xi_{13}^{2\nu} = \frac{M_{\text{GT-3}}^{2\nu}}{M_{\text{GT-1}}^{2\nu}}$$

KamLAND-Zen Coll. (+J. Menendez, F.Š.),
Phys.Rev.Lett. 122, 192501 (2019)

Looking for a new physics with differential characteristics



Spectral index n

10/24/2019

$$\frac{d\Gamma}{d\varepsilon_1 d\varepsilon_2} = C(Q - \varepsilon_1 - \varepsilon_2)^n [p_1 \varepsilon_1 F(\varepsilon_1)] [p_2 \varepsilon_2 F(\varepsilon_2)]$$

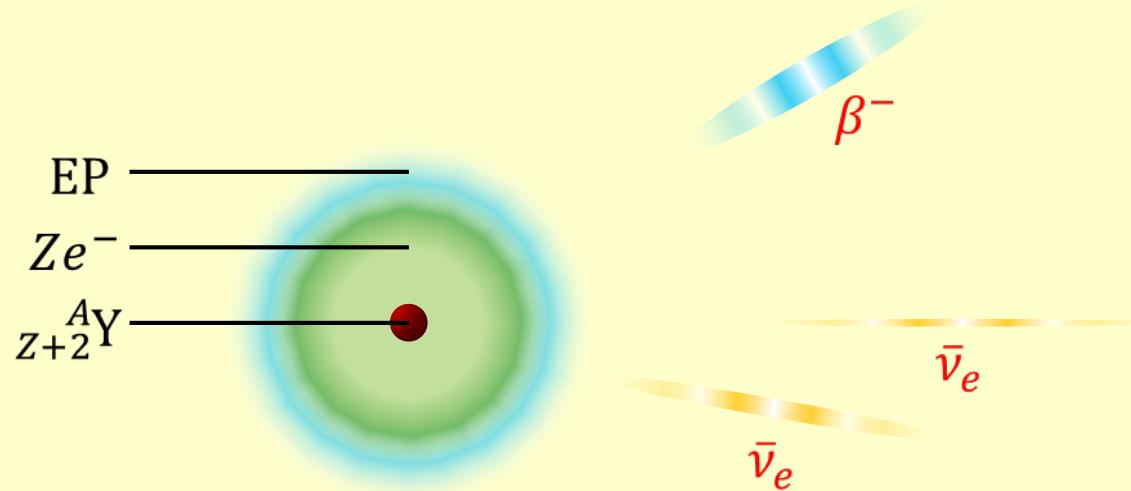
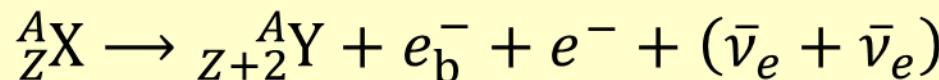
53

Double Beta Decay with emission of a single electron

A. Babič, M.I. Krivoruchenko, F.Š., PRC 98, 065501 (2018)

[Jung *et al.* (GSI), 1992] observed beta decay of $^{163}_{66}\text{Dy}^{66+}$ ions with Electron Production (EP) in K or L shells: $T_{1/2}^{\text{EP}} = 47 \text{ d}$

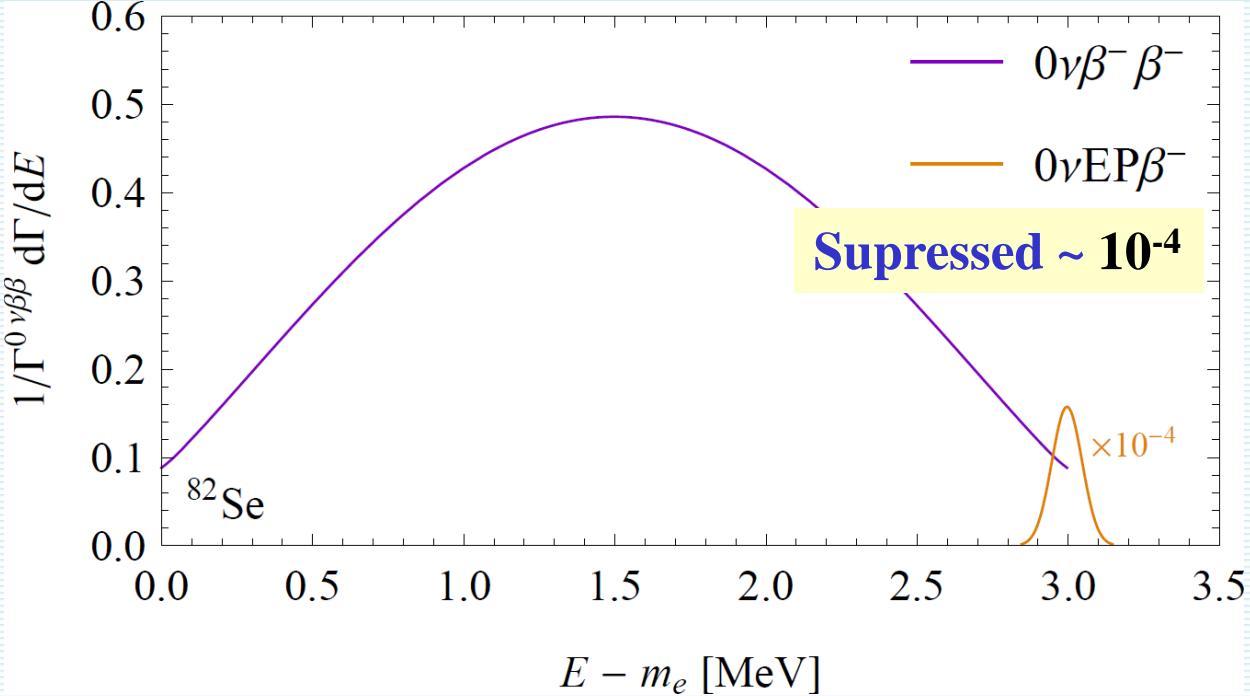
Bound-state double-beta decay $0\nu\text{EP}\beta^-$ ($2\nu\text{EP}\beta^-$) with EP in available $s_{1/2}$ or $p_{1/2}$ subshell of daughter 2^+ ion:



Search for possible manifestation in single-electron spectra...

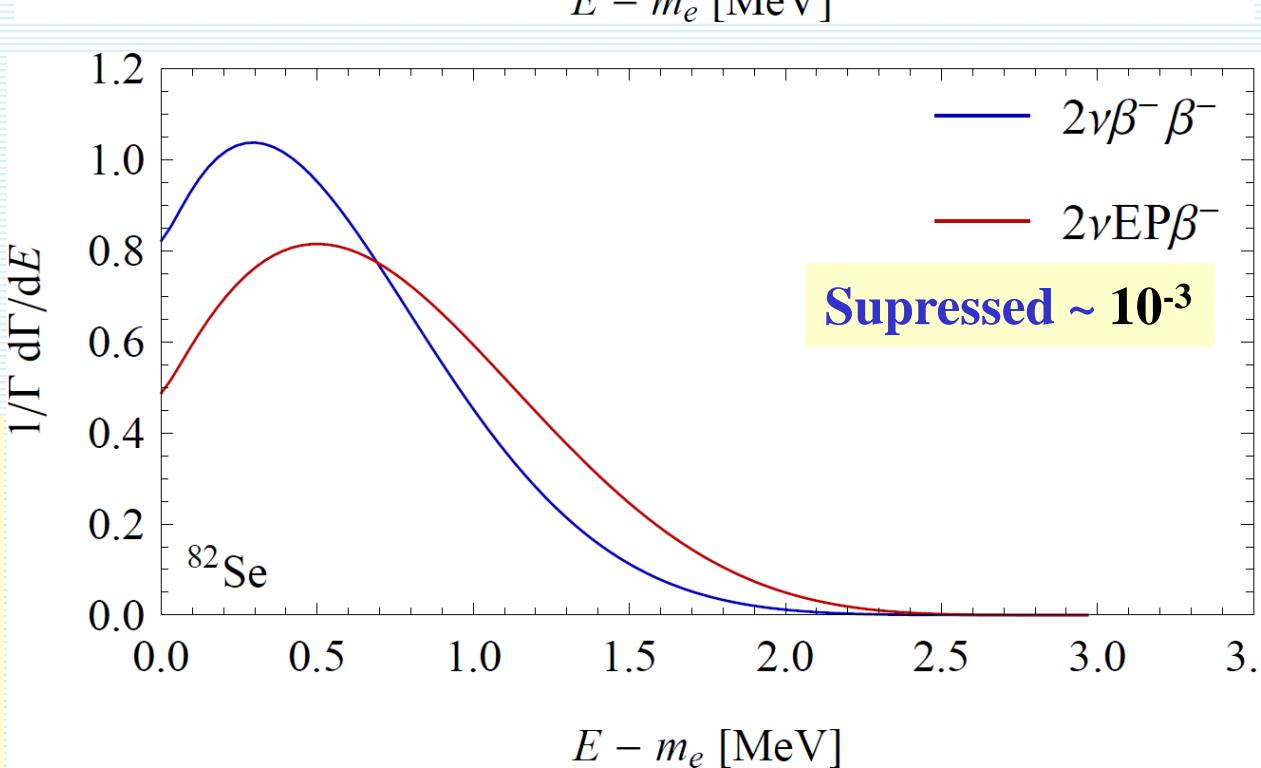
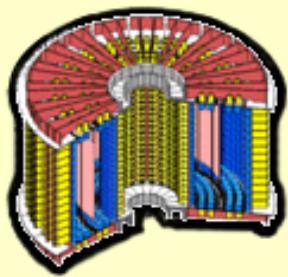
Energy distribution of a single electron

$0\nu\text{EP}\beta$ strongly
suppressed



$2\nu\text{EP}\beta$ could
be detected
Half-life
predictions
independent
n gA and value
of 2nbb NME

10/24/2019



V. On the search for the signal of the total LNV

*a resonance
production of heavy N*

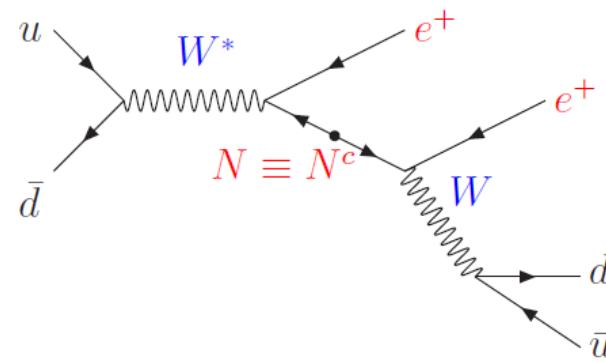
$0\nu\beta\beta$
*Avogadro number
is large ...*



*restrictions for future:
Solar neutrinos,
 $2\nu\beta\beta$ background*

=>

*Solution?
resonant
neutrinoless
double
electron
capture*

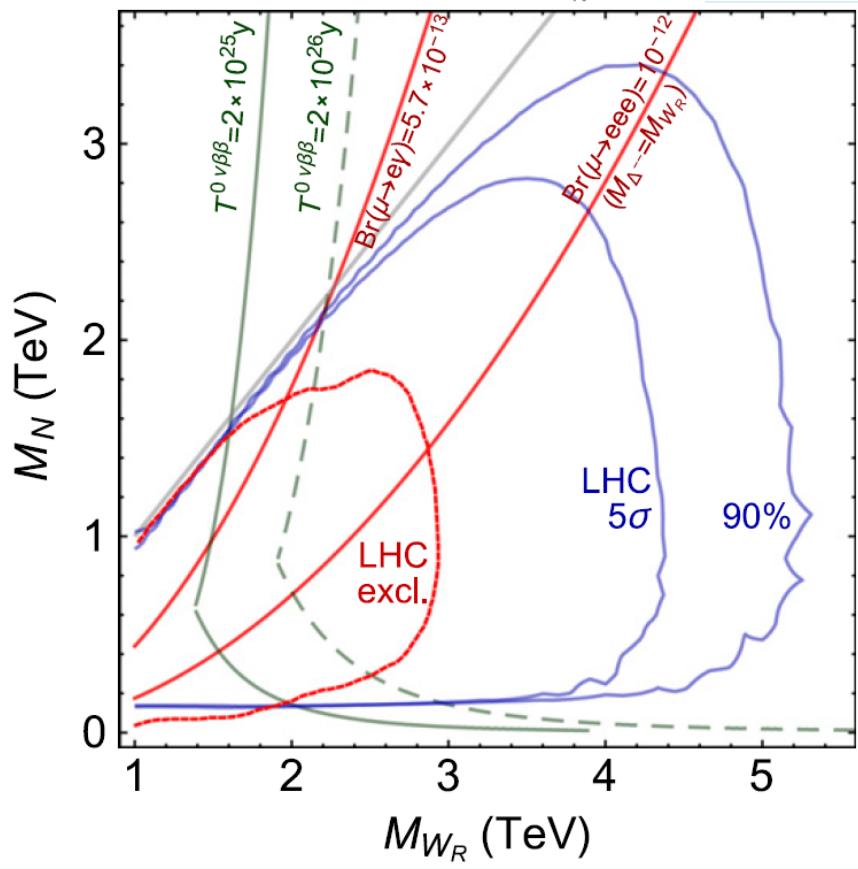
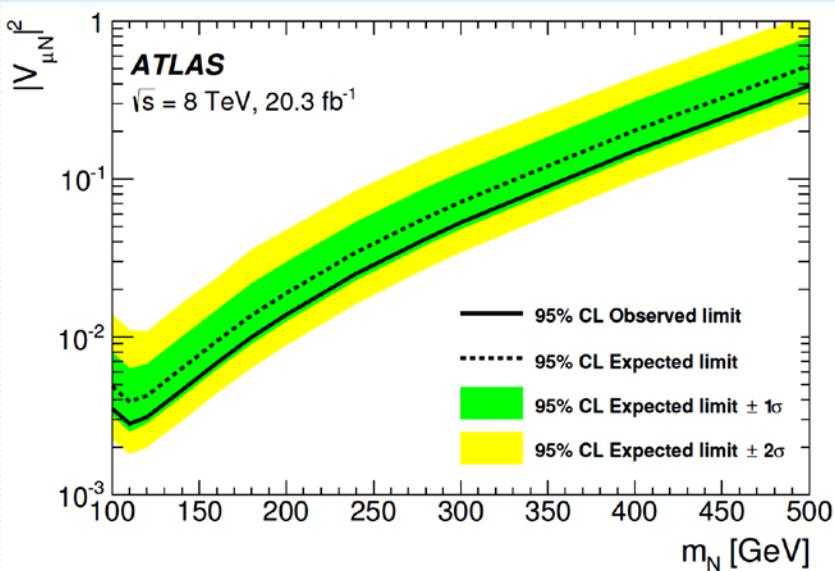
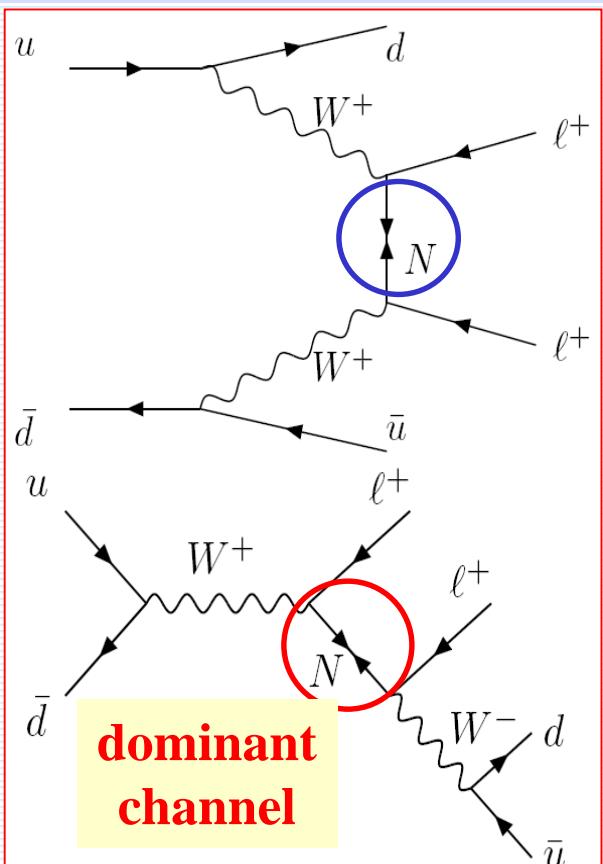


*Collider: $pp \rightarrow l^+l^+ + jj$
 $\mu^- + (A,Z) \rightarrow (A,Z-2) + e^+$
 $\mu^- + (A,Z) \rightarrow (A,Z-2) + \mu^+$
Mesons decays
*... many others**

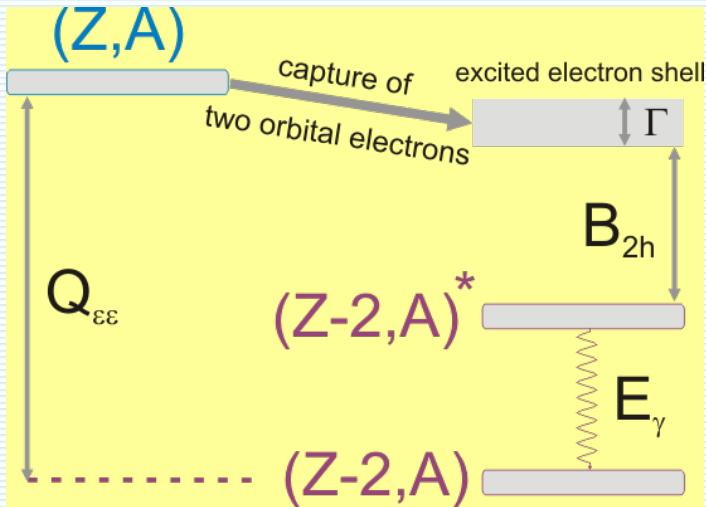
Direct searches for heavy ν 's at LHC \Rightarrow TeV mass limit

$$pp \rightarrow l^+l^+ + jj$$

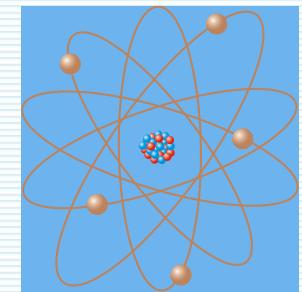
collider analogue to $0\nu\beta\beta$ decay



N can be produced on resonance



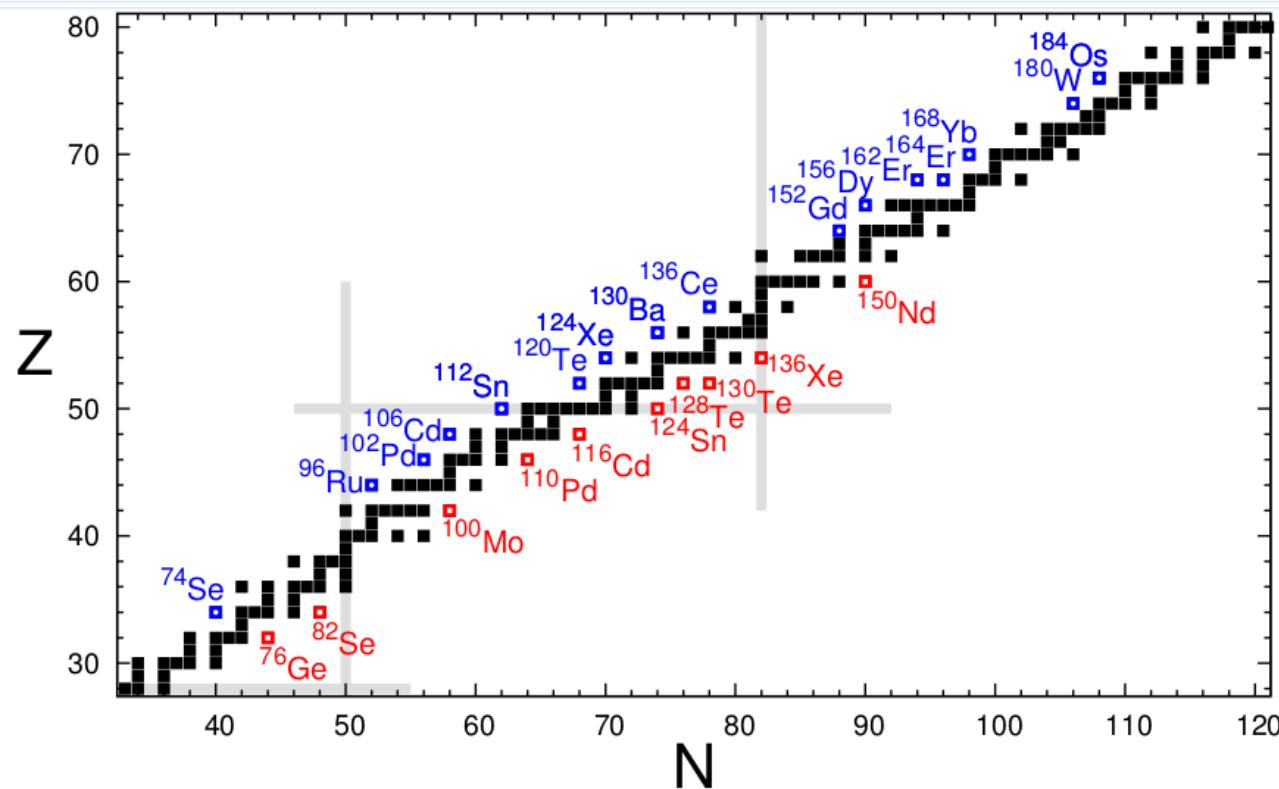
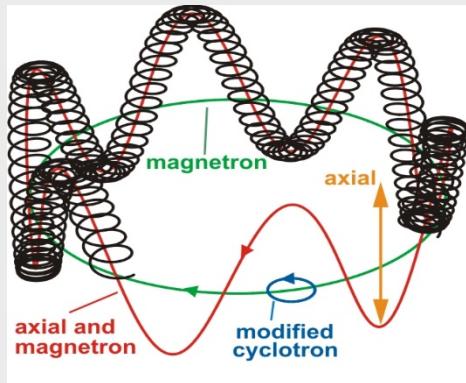
Resonant neutrinoless double-electron capture



$$\frac{1}{T_{1/2}} = A \cdot |\psi_{1e}|^2 \cdot |\psi_{2e}|^2 \cdot \frac{\Gamma}{(Q - B_{2h} - E_\gamma)^2 + \frac{1}{4}\Gamma^2}$$

152Gd⁺: $\Delta M=100$ eV

Penning Trap



A comparison

Resonance enhancement of neutrinoless double electron capture
M.I. Krivoruchenko, F. Š., D. Frekers, and A. Faessler,
Nucl. Phys. A 859, 140-171 (2011)



Perturbation theory

$$\frac{1}{T_{1/2}^{0\nu}} = \left| \frac{m_{\beta\beta}}{m_e} \right|^2 G^{01}(E_0, Z) |M^{0\nu}|^2$$



Breit-Wigner form

$$\Gamma^{0\nu ECEC}(J^\pi) = \frac{|V_{\alpha\beta}(J^\pi)|^2}{(M_i - M_f)^2 + \Gamma_{\alpha\beta}^2/4} \Gamma_{\alpha\beta}$$

- **2νββ-decay background and solar ν's can be a problem**
- **0⁺→ 0^{+,2⁺}** transitions
- **Large Q-value**
- **76Ge, 82Se, 100Mo, 130Te, 136Xe ...**
- **Many exp. in construction, potential for observation in the case of inverted hierarchy (2022)**

- **2νeeε-decay strongly suppressed**
- **No background from solar ν's**
- **0⁺→0^{+,0⁻, 1^{+,1⁻}}** transitions
- **Small Q-value**
- **Q-value measured with below 1 keV accuracy**
- **152Gd→152Sm (sensitivity to m_{ββ} by factor ~10 worse than by 0νββ)**
- **small experiments yet**
- **Can we manipulate atomic structure**

Conclusions and Outlook



$$\frac{1}{\Lambda} \sum_i c_i^{(5)} \mathcal{O}_i^{(5)}$$

ν 's, the
Standard
Model
misfits



*WE are at
the beginning
of the **Beyond
Standard Model
Road...***

*people often **overestimate** what will happen in the next **two years**
and **underestimate** what will happen in **ten** (Bill Gates)*