

Open heavy flavour at LHC

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based on work in collaboration with
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- ① OVERVIEW AND MOTIVATION
- ② ONE-PARTICLE INCLUSIVE PRODUCTION IN A GM-VFNS
- ③ FRAGMENTATION FUNCTIONS IN A GM-VFNS
- ④ APPLICATIONS
- ⑤ SUMMARY

Overview and Motivation

Quarks heavy $\Leftrightarrow m_h \gg \Lambda_{\text{QCD}} \sim 250 \text{ MeV}$

- $m_h \gg \Lambda_{\text{QCD}} \Rightarrow \alpha_s(m_h^2) \propto \ln^{-1}\left(\frac{m_h^2}{\Lambda_{\text{QCD}}^2}\right) \ll 1$ (asymptotic freedom)
- m_h sets hard scale; acts as long distance cut-off

charm:	$m_c \sim 1.5 \text{ GeV}$	$\Lambda_{\text{QCD}}/m_c \sim 0.17$	$\alpha_s(m_c^2) \sim 0.34$
bottom:	$m_b \sim 5 \text{ GeV}$	$\Lambda_{\text{QCD}}/m_b \sim 0.05$	$\alpha_s(m_b^2) \sim 0.21$
top:	$m_t \sim 175 \text{ GeV}$	$\Lambda_{\text{QCD}}/m_t \sim 0.001$	$\alpha_s(m_t^2) \sim 0.11$

\Rightarrow PERTURBATION THEORY (PQCD) APPLICABLE!

- The smaller the ratio Λ_{QCD}/m_h , the smaller effects of non-perturbative QCD (such as hadronization)
- Top quark decays before it could hadronize due to its large mass ($\Gamma \propto m_t^3$):

$$\Gamma \simeq \Gamma(t \rightarrow bW) \simeq \frac{G_F m_t^3}{8\pi\sqrt{2}} |V_{tb}|^2 \simeq 1.76 \text{ GeV} \left(\frac{m_t}{175 \text{ GeV}}\right)^3$$

Extensively studied at e^+e^- , photon–hadron, and hadron–hadron colliders. Why?

Many topics (production and decay of heavy quarks):

- Tests of pQCD
 - Factorization, PDFs, FFs, resummations, higher order calculations
 - $g + g \rightarrow b + \bar{b}$: gluon PDF
 - $g + s \rightarrow W + c$: strange PDF; $g + c \rightarrow \gamma + c$: charm PDF
- Important for new physics
 - Understand production of known heavy objects to find new heavy objects
 - New physics often couples to heavy states
 - Higgs boson discovery
 - Background to new physics
- CKM matrix, $B - \bar{B}$ mixing, CP violation
- Measurement of the spin (top decays before hadronization and the products retain all spin correlations)

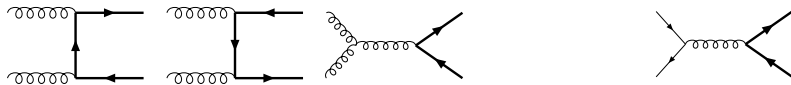
This talk: interested in QCD aspects of open heavy flavour production

- **Top quarks:** decay before hadronization \rightarrow Not considered here.
- **Charm and bottom quarks:** hadronize into
 - c and b hadrons: D, B, Λ_c, \dots (\rightarrow open heavy flavour)
 - $c\bar{c}$ and $b\bar{b}$ bound states: $J/\psi, \Upsilon, \dots$

OPEN HEAVY FLAVOUR PRODUCTION : \Leftrightarrow FINAL STATE HADRONS WITH $C \neq 0$ OR $B \neq 0$

Leading order subprocesses:

1. $gg \rightarrow Q\bar{Q}$
2. $q\bar{q} \rightarrow Q\bar{Q}$ ($q = u, d, s$)



- The gg -channel is dominant at the LHC ($\sim 85\%$ at $\sqrt{S} = 14$ TeV).
- The total production cross section for **heavy quarks** is finite.
The minimum virtuality of the t-channel propagator is m^2 . Sets the scale in α_s .
Perturbation theory should be reliable.
- Note: For $m^2 \rightarrow 0$ total cross section would diverge.

See M. Mangano, hep-ph/9711337; Textbook by Ellis, Stirling and Webber

Next-to-leading order (NLO) subprocesses:

1. $gg \rightarrow Q\bar{Q}g$
2. $q\bar{q} \rightarrow Q\bar{Q}g$ ($q = u, d, s$)
3. $gg \rightarrow Q\bar{Q}q, g\bar{q} \rightarrow Q\bar{Q}\bar{q}$ [new at NLO]
4. Virtual corrections to $gg \rightarrow Q\bar{Q}$ and $q\bar{q} \rightarrow Q\bar{Q}$

NLO corrections for σ_{tot} and differential cross sections $d\sigma/dp_T dy$ known since long:

- Nason, Dawson, Ellis, NPB303(1988)607; Beenakker, Kuif, van Neerven, Smith, PRD40(1989)54 [σ_{tot}]
- NDE, NPB327(1989)49; (E)B335(1990)260; Beenakker *et al.*, NPB351(1991)507 [$d\sigma/dp_T dy$]

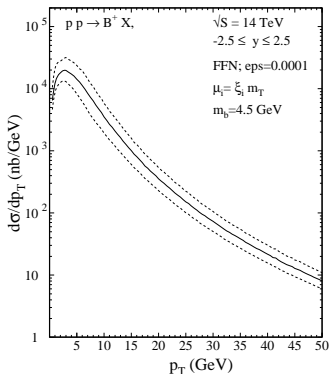
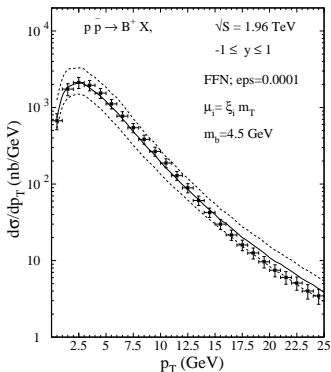
Well tested by recalculations and zero-mass limit:

- Bojak, Stratmann, PRD67(2003)034010 [$d\sigma/dp_T dy$ (un)polarized]
- Kniehl, Kramer, Spiesberger, IS, PRD71(2005)014018 [$m \rightarrow 0$ limit of diff. x-sec]
- Czakon, Mitov, NPB824(2010)111 [σ_{tot} , fully analytic]

Next-to-next-to-leading order (NNLO):

- See, e.g., [Bonciani, Ferroglia, arXiv:0909.2980](#) for an overview

- $d\sigma/dp_T$ for the process $pp \rightarrow B^+ X$; Fragmentation $b \rightarrow B$ via Peterson-FF
- Prediction in NLO perturbation theory



Remarks:

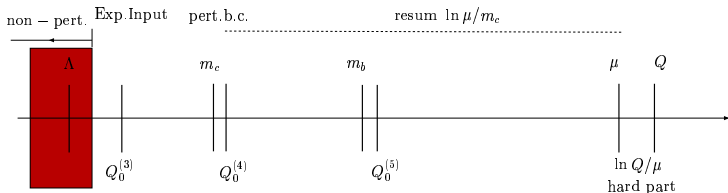
- Fixed order theory in reasonable agreement with Tevatron data up to $p_T \simeq 5m_b$
- At $p_T \lesssim m_b$ factorization less obvious. Depends on definition of convolution variable z : $p_B = zp_b$ or $p_T^B = zp_T^b$ or $p_B^+ = zp_b^+$ or $\vec{p}_B = z\vec{p}_b$
- Less hadronization effects than originally believed:
 ϵ -parameter small corresponding to a hard fragmentation function.
- Only the 4th or 5th Mellin-moment of the FF is relevant (M. Mangano):
 $d\sigma^b/dp_T(b) \simeq A/p_T(b)^n$ with $n \simeq 4, \dots, 5$

$$d\sigma^B/dp_T(B) = \int dz/z D(z) d\sigma^b/dp_T(b)[p_T(b) = p_T(B)/z] = A/p_T(B)^n \times \int dz z^{n-1} D(z)$$

- What about $\ln m_b/p_T$ at large $p_T \gg m_b$?

Fixed Order Perturbation Theory:

- **finite** collinear logs $\ln Q/m_c$ arise \rightarrow can be kept in hard part
Of course need **exp. Input** for u, d, s, g PDFs at scale $Q_0^{(3)}$



Variable Flavour Number Scheme (VFNS):

- often large ratios of scales involved: **multi-scale problems**
For $Q \gg m_c$: write $\ln Q/m_c = \ln Q/\mu + \ln \mu/m_c$, **subtract** $\ln \mu/m_c$ and **resum** $\ln \mu/m_c$
by introducing charm PDF at $Q_0^{(4)} \simeq m_c$ using a **perturbative** boundary condition

Two basic approaches:

- Fixed Order Perturbation Theory (FFNS) \leftrightarrow GRV, nDS
- Parton Model (ZM-VFNS) \leftrightarrow CTEQ5, CTEQ6.1M, MRS, HKN, EKS

Interpolating schemes combining the good features:

- Parton Model with quark masses (GM-VFNS, ACOT) \leftrightarrow CTEQ6.6M, MRST/MSTW, nCTEQ
- FONLL \leftrightarrow NNPDF

Glossary:

- ZM: Zero Mass
- GM: General Mass
- VFNS: Variable Flavour Number Scheme
- FFNS: Fixed Flavour Number Scheme

One-particle inclusive production in a GM-VFNS

OVERVIEW

- One-particle inclusive production of heavy hadrons $H = D, B, \Lambda_c, \dots$
- General-Mass Variable Flavour Number Scheme (GM-VFNS): [1]
 - Collinear logarithms of the heavy-quark mass $\ln \mu/m_h$ are **subtracted** and **resummed**
 - Finite non-logarithmic m_h/Q terms are kept in the hard part/taken into account
 - Scheme guided by the factorization theorem of Collins with heavy quarks [2]

Ongoing effort to compute all relevant processes in the GM-VFNS at NLO:

- Available:
 - $e^+ + e^- \rightarrow (D^0, D^+, D^{*+}) + X$: FFs [3]
 - $\gamma + \gamma \rightarrow D^{*+} + X$: direct process [4]
 - $\gamma + \gamma \rightarrow D^{*+} + X$: single-resolved process [5]
 - $\gamma + p \rightarrow D^{*+} + X$: direct process [6]
 - $\gamma + p \rightarrow D^{*+} + X$: resolved process [7]
 - $p + \bar{p} \rightarrow (D^0, D^+, D^{*+} D_s^+, \Lambda_c^+, B^0, B^+) + X$ [1]

[1] Kniehl, Kramer, IS, Spiesberger, PRD71(2005)014018; EPJC41(2005)199; PRL96(2006)012001; PRD77(2008)014011; arXiv:0901.4130[hep-ph], PRD (in press)

[2] Collins, PRD58(1998)094002

[3] Kneesch, Kniehl, Kramer, IS, NPB799(2008)34

[4] Kramer, Spiesberger, EPJC22(2001)289; [5] EPJC28(2003)495; [6] EPJC38(2004)309

[7] Kniehl, Kramer, IS, Spiesberger, arXiv:0902.3166[hep-ph], EPJC (in press)

OVERVIEW -CONTINUED-

Input for the computation: Fragmentation Functions (FFs) into heavy hadrons H

- FFs from fits to e^+e^- data from Z factories
- Include also B factories \rightarrow Switch from ZM to GM
- Use initial scale $\mu_0 = m$ (instead of $\mu_0 = 2m$) for consistency with PDFs \rightarrow important for gluon fragmentation

H	Data	Scheme	Reference
D^{*+}	ALEPH,OPAL	ZM $2m$	BKK, PRD58(1998)014014
$D^0, D^+, D_s^+, \Lambda_c^+$	OPAL	ZM $2m$	KK, PRD71(2005)094013
$D^0, D^+, D^{*+}, D_s^+, \Lambda_c^+$	OPAL	ZM m	KK, PRD74(2006)037502
D^0, D^+, D_s^+	Belle,CLEO,ALEPH,OPAL	GM m	KKKSc, NPB799(2008)34
B^0, B^+	OPAL	ZM $2m$	BKK, PRD58(1998)034016
B^0, B^+	ALEPH,OPAL,SLD	ZM m	KKScSp, PRD77(2008)014011

Goal:

- Test pQCD formalism, scaling violations and universality of FFs in as many processes as possible

$$A + B \rightarrow H + X: \quad d\sigma = \sum_{i,j,k} f_i^A(x_1) \otimes f_j^B(x_2) \otimes d\sigma(ij \rightarrow kX) \otimes D_k^H(z)$$

sum over all possible subprocesses $i + j \rightarrow k + X$

Parton distribution functions:

$f_i^A(x_1, \mu_F), f_j^B(x_2, \mu_F)$
non-perturbative input
 long distance
 universal

Hard scattering

cross section:
 $d\sigma(\mu_F, \mu_F', \alpha_s(\mu_R), [\frac{m_h}{p_T}])$
perturbatively computable
 short distance
 (coefficient functions)

Fragmentation functions:

$D_k^H(z, [\mu_F'])$
non-perturbative input
 long distance
 universal

Accuracy:

light hadrons: $\mathcal{O}((\Lambda/p_T)^p)$ with p_T hard scale, Λ hadronic scale, $p = 1, 2$

heavy hadrons: if m_h is neglected in $d\sigma$: $\mathcal{O}((m_h/p_T)^p)$

Details (subprocesses, PDFs, FFs; mass terms) depend on
 the **Heavy Flavour Scheme**

LIST OF SUBPROCESSES: GM-VFNS

Only light lines

- 1 $gg \rightarrow qX$
- 2 $gg \rightarrow gX$
- 3 $qg \rightarrow gX$
- 4 $qg \rightarrow qX$
- 5 $q\bar{q} \rightarrow gX$
- 6 $q\bar{q} \rightarrow qX$
- 7 $qg \rightarrow \bar{q}X$
- 8 $qg \rightarrow \bar{q}'X$
- 9 $qg \rightarrow q'X$
- 10 $qq \rightarrow gX$
- 11 $qq \rightarrow qX$
- 12 $q\bar{q} \rightarrow q'X$
- 13 $q\bar{q}' \rightarrow gX$
- 14 $q\bar{q}' \rightarrow qX$
- 15 $qq' \rightarrow gX$
- 16 $qq' \rightarrow qX$

⊕ charge conjugated processes

Heavy quark initiated ($m_Q = 0$)

- 1 -
- 2 -
- 3 $Qg \rightarrow gX$
- 4 $Qg \rightarrow QX$
- 5 $Q\bar{Q} \rightarrow gX$
- 6 $Q\bar{Q} \rightarrow QX$
- 7 $Qg \rightarrow \bar{Q}X$
- 8 $Qg \rightarrow \bar{q}X$
- 9 $Qg \rightarrow qX$
- 10 $QQ \rightarrow gX$
- 11 $QQ \rightarrow QX$
- 12 $Q\bar{Q} \rightarrow qX$
- 13 $Q\bar{q} \rightarrow gX, q\bar{Q} \rightarrow gX$
- 14 $Q\bar{q} \rightarrow QX, q\bar{Q} \rightarrow qX$
- 15 $Qq \rightarrow gX, qQ \rightarrow gX$
- 16 $Qq \rightarrow QX, qQ \rightarrow qX$

Mass effects: $m_Q \neq 0$

- 1 $gg \rightarrow QX$
- 2 -
- 3 -
- 4 -
- 5 -
- 6 -
- 7 -
- 8 $qg \rightarrow \bar{Q}X$
- 9 $qg \rightarrow QX$
- 10 -
- 11 -
- 12 $q\bar{q} \rightarrow QX$
- 13 -
- 14 -
- 15 -
- 16 -

Mass terms contained in the hard scattering coefficients:

$$d\hat{\sigma}(\mu_F, \mu_{F'}, \alpha_s(\mu_R), \frac{m}{p_T})$$

Two ways to derive them:

- (1) Compare **massless limit** of a massive fixed-order calculation with a massless $\overline{\text{MS}}$ calculation to determine subtraction terms

OR

- (2) Perform **mass factorization** using partonic PDFs and FFs

- Compare limit $m \rightarrow 0$ of the massive calculation (Merebashvili et al., Ellis, Nason; Smith, van Neerven; Bojak, Stratmann; ...) with massless $\overline{\text{MS}}$ calculation (Aurenche et al., Aversa et al., ...)

$$\lim_{m \rightarrow 0} d\tilde{\sigma}(m) = d\hat{\sigma}_{\overline{\text{MS}}} + \Delta d\sigma$$

⇒ Subtraction terms

$$d\sigma_{\text{sub}} \equiv \Delta d\sigma = \lim_{m \rightarrow 0} d\tilde{\sigma}(m) - d\hat{\sigma}_{\overline{\text{MS}}}$$

- Subtract $d\sigma_{\text{sub}}$ from massive partonic cross section while keeping mass terms

$$d\hat{\sigma}(m) = d\tilde{\sigma}(m) - d\sigma_{\text{sub}}$$

→ $d\hat{\sigma}(m)$ short distance coefficient including m dependence

→ allows to use PDFs and FFs with $\overline{\text{MS}}$ factorization \otimes massive short distance cross sections

- Treat contributions with charm in the initial state with $m = 0$
- Massless limit: technically non-trivial, map from phase-space slicing to subtraction method

Mass factorization

Subtraction terms are associated to mass singularities:
can be described by

partonic PDFs and FFs for collinear splittings $a \rightarrow b + X$

- initial state:

$$f_{g \rightarrow Q}^{(1)}(x, \mu^2) = \frac{\alpha_s(\mu)}{2\pi} P_{g \rightarrow q}^{(0)}(x) \ln \frac{\mu^2}{m^2}$$

$$f_{Q \rightarrow Q}^{(1)}(x, \mu^2) = \frac{\alpha_s(\mu)}{2\pi} C_F \left[\frac{1+z^2}{1-z} \left(\ln \frac{\mu^2}{m^2} - 2 \ln(1-z) - 1 \right) \right]_+$$

$$f_{g \rightarrow g}^{(1)}(x, \mu^2) = -\frac{\alpha_s(\mu)}{2\pi} \frac{1}{3} \ln \frac{\mu^2}{m^2} \delta(1-x)$$
- final state:

$$d_{g \rightarrow Q}^{(1)}(z, \mu^2) = \frac{\alpha_s(\mu)}{2\pi} P_{g \rightarrow q}^{(0)}(z) \ln \frac{\mu^2}{m^2}$$

$$d_{Q \rightarrow Q}^{(1)}(z, \mu^2) = C_F \frac{\alpha_s(\mu)}{2\pi} \left[\frac{1+z^2}{1-z} \left(\ln \frac{\mu^2}{m^2} - 2 \ln(1-z) - 1 \right) \right]_+$$
- Other partonic distribution functions are zero to order α_s

Mele, Nason; Kretzer, Schienbein; Melnikov, Mitov

(2) SUBTRACTION TERMS VIA $\overline{\text{MS}}$ MASS FACTORIZATION: $a(k_1)b(k_2) \rightarrow Q(p_1)X$ [1]

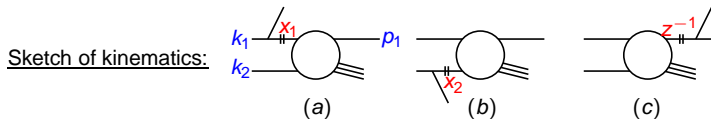


Fig. (a):

$$d\sigma^{\text{sub}}(ab \rightarrow QX) = \int_0^1 dx_1 f_{a \rightarrow i}^{(1)}(x_1, \mu_F^2) d\hat{\sigma}^{(0)}(ib \rightarrow QX)[x_1 k_1, k_2, p_1]$$

$$\equiv f_{a \rightarrow i}^{(1)}(x_1) \otimes d\hat{\sigma}^{(0)}(ib \rightarrow QX)$$

Fig. (b):

$$d\sigma^{\text{sub}}(ab \rightarrow QX) = \int_0^1 dx_2 f_{b \rightarrow j}^{(1)}(x_2, \mu_F^2) d\hat{\sigma}^{(0)}(aj \rightarrow QX)[k_1, x_2 k_2, p_1]$$

$$\equiv f_{b \rightarrow j}^{(1)}(x_2) \otimes d\hat{\sigma}^{(0)}(aj \rightarrow QX)$$

Fig. (c):

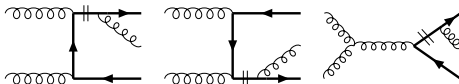
$$d\sigma^{\text{sub}}(ab \rightarrow QX) = \int_0^1 dz d\hat{\sigma}^{(0)}(ab \rightarrow kX)[k_1, k_2, z^{-1} p_1] d_{k \rightarrow Q}^{(1)}(z, \mu_F^2)$$

$$\equiv d\hat{\sigma}^{(0)}(ab \rightarrow kX) \otimes d_{k \rightarrow Q}^{(1)}(z)$$

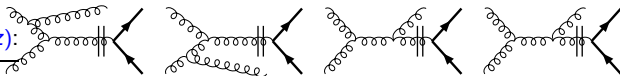
[1] Kniehl, Kramer, I.S., Spiesberger, EPJC41(2005)199

GRAPHICAL REPRESENTATION OF SUBTRACTION TERMS FOR $gg \rightarrow Q\bar{Q}g$

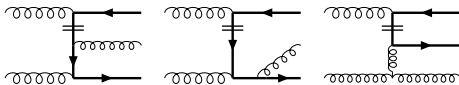
$$\underline{d\hat{\sigma}^{(0)}(gg \rightarrow Q\bar{Q}) \otimes d_{Q \rightarrow Q}^{(1)}(z):}$$



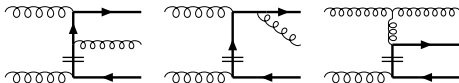
$$\underline{d\hat{\sigma}^{(0)}(gg \rightarrow gg) \otimes d_{g \rightarrow Q}^{(1)}(z):}$$



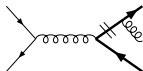
$$\underline{f_{g \rightarrow Q}^{(1)}(x_1) \otimes d\hat{\sigma}^{(0)}(Qg \rightarrow Qg):}$$



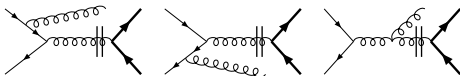
$$\underline{f_{g \rightarrow Q}^{(1)}(x_2) \otimes d\hat{\sigma}^{(0)}(gQ \rightarrow Qg):}$$



$d\hat{\sigma}^{(0)}(q\bar{q} \rightarrow Q\bar{Q}) \otimes d_{Q \rightarrow Q}^{(1)}(z):$



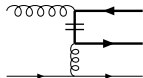
$d\hat{\sigma}^{(0)}(q\bar{q} \rightarrow gg) \otimes d_{g \rightarrow Q}^{(1)}(z):$



$d\hat{\sigma}^{(0)}(gq \rightarrow gq) \otimes d_{g \rightarrow Q}^{(1)}(z):$



$f_{g \rightarrow Q}^{(1)}(x_1) \otimes d\hat{\sigma}^{(0)}(Qq \rightarrow Qq):$



Fragmentation Functions in a GM-VFNS

D^0, D^+, D^{*+} FFS WITH FINITE-MASS CORRECTIONS [1]

FORMALISM

- $e^+ + e^- \rightarrow (\gamma, Z) \rightarrow H + X, \quad H = D^0, D^+, D^{*+}, \dots$
- $x = 2(p_H \cdot q)/q^2 = 2E_H/\sqrt{s} \quad \sqrt{\rho_H} \leq x \leq 1 \quad (\rho_H = 4m_H^2/s)$

$$\frac{d\sigma}{dx}(x, s) = \sum_a \int_{y_{\min}}^{y_{\max}} \frac{dy}{y} \frac{d\sigma_a}{dy}(y, \mu, \mu_f) D_a\left(\frac{x}{y}, \mu_f\right)$$

$d\sigma_a/dy$ at NLO with $m_q = 0$ [2] and $m_q \neq 0$ [1,3]

- $x_p = p/p_{\max} = \sqrt{(x^2 - \rho_H)/(1 - \rho_H)} \quad 0 \leq x_p \leq 1$

$$\frac{d\sigma}{dx_p}(x_p) = (1 - \rho_H) \frac{x_p}{x} \frac{d\sigma}{dx}(x)$$

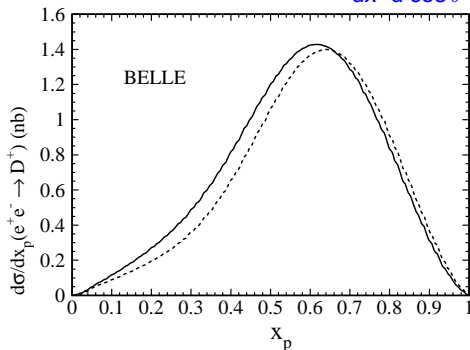
[1] Kneesch, B.K., Kramer, Schienbein, NPB799(2008)34

[2] Baier, Fey, ZPC2(1979)339; Altarelli et al. NPB160(1979)301

[3] Nason, Webber, NPB421(1994)473

- Use radiator D_{e^\pm} [1]

$$\frac{d\sigma_{\text{ISR}}}{dx}(x, s) = \int dx_+ dx_- dx' d\cos\theta' \delta(x - x(x_+, x_-, x', \cos\theta')) \\ \times D_{e^+}(x_+, s) D_{e^-}(x_-, s) \frac{d^2\sigma}{dx' d\cos\theta'}(x', \cos\theta', x_+ x_- s)$$



[1] Kuraev, Fadin, SJNP41(1985)466; Nicrosini, Trentadue, PLB196(1987)551

- Experimental data

Type	\sqrt{s} [GeV]	H	Collaboration
$d\sigma/dx_p$	10.52	D^0, D^+, D^{*+}	Belle 06
$d\sigma/dx_p$	10.52	D^0, D^+, D^{*+}	CLEO 04
$(1/\sigma_{\text{tot}})d\sigma/dx$	91.2	D^{*+}	ALEPH 00
$(1/\sigma_{\text{tot}})d\sigma/dx$	91.2	D^0, D^+, D^{*+}	OPAL 96,98

- Theoretical input

- $m_c = 1.5$ GeV, $m_b = 5.0$ GeV, $\alpha(m_\Upsilon) = 1/132$,
 $\alpha_s(m_Z) = 0.1176 \rightsquigarrow \Lambda_{\text{QCD}}^{(5)} = 221$ MeV
- Bowler ansatz [1]

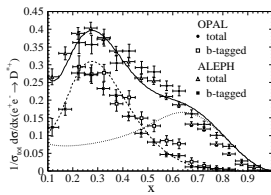
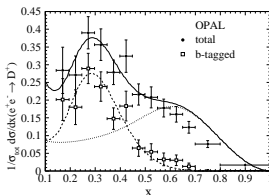
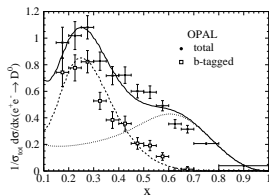
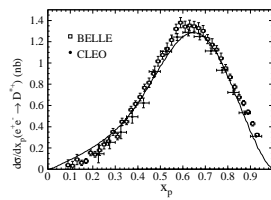
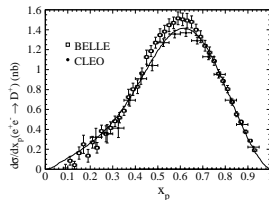
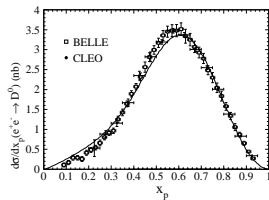
$$D_Q^{H_c}(z, \mu_0) = Nz^{-(1+\gamma^2)}(1-z)^a e^{-\gamma^2/z}$$

[1] Bowler, ZPC11(1981)169

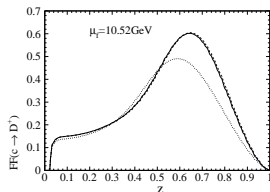
- $\chi^2/\text{d.o.f.}$

H	VFNS	Belle/CLEO	ALEPH/OPAL	Global
D^0	GM	3.15	0.794	4.03
	ZM	3.25	0.789	4.66
D^+	GM	1.30	0.509	1.99
	ZM	1.37	0.507	2.21
D^{*+}	GM	3.74	2.06	6.90
	ZM	3.69	2.04	7.64

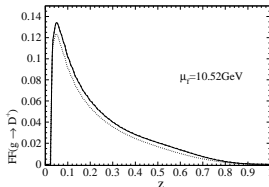
- Quark mass effects improve global fits and Belle/CLEO fits for D^0 , D^+ , but have no impact on ALEPH/OPAL fits.
- Belle and CLEO data on D^0 , D^{*+} moderately compatible.
- OPAL fits for D^0 , D^+ excellent; ALEPH and OPAL data on D^{*+} moderately compatible.
- Tension between Belle/CLEO and ALEPH/OPAL data.



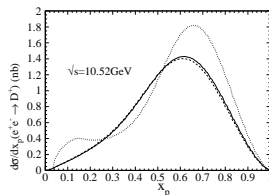
- Belle/CLEO data push $\langle z \rangle_c(m_Z)$ up by 0.03–0.04



$c \rightarrow D^+$ FF



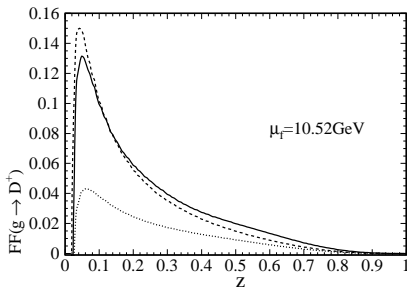
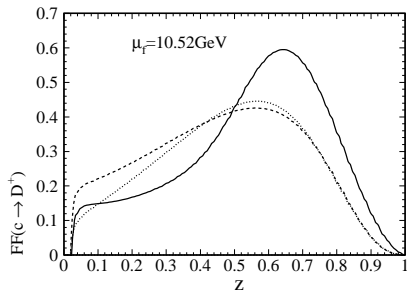
$g \rightarrow D^+$ FF



$d\sigma/dx_p$ w/ Belle/CLEO-GM FFs

- dotted: $m_c = m_H = 0$
- dashed: $m_c = 0 \neq m_H$ (ZM-VFNS)
- solid: $m_c \neq 0 \neq m_H$ (GM-VFNS)

- Hadron mass effects on FFs important, quark mass effects marginal



$c \rightarrow D^+$ FF

dotted: $m_c = 0 = m_H$ $\mu_0 = 2m_c$ Peterson
 dashed: $m_c = 0 = m_H$ $\mu_0 = m_c$ Peterson
 solid: $m_c \neq 0 \neq m_H$ $\mu_0 = m_c$ Bowler

$g \rightarrow D^+$ FF

OPAL KK 05
 OPAL KK 06
 Belle,CLEO,OPAL KKKSc 08

- Strong pull of Belle/CLEO data on $c \rightarrow D^+$ FF
- Reduction in μ_0 increases $g \rightarrow D^+$ FF

Applications

Applications available for

- $\gamma + \gamma \rightarrow D^{*\pm} + X$
direct and resolved contributions
- $\gamma^* + p \rightarrow D^{*\pm} + X$
photoproduction
- $p + \bar{p} \rightarrow (D^0, D^{*\pm}, D^\pm, D_s^\pm, \Lambda_c^\pm) + X$
good description of Tevatron data
- $p + \bar{p} \rightarrow B + X$
works for Tevatron data at large p_T
- work in progress for $e + p \rightarrow D + X$

EPJC22, EPJC28

EPJC38, arXiv:0902.3166 [EPJC]

PRD71, PRL96, arXiv:0901.4130

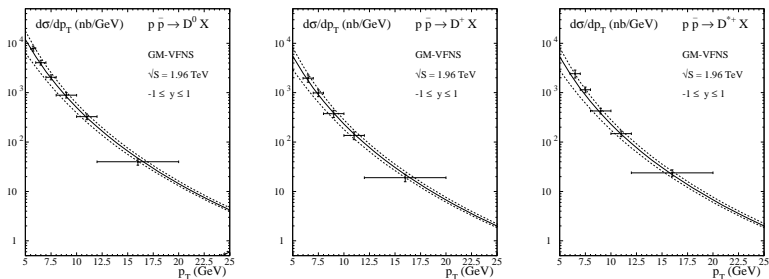
PRD77

Input parameters:

- $\alpha_s(M_Z) = 0.1181$
- $m_c = 1.5 \text{ GeV}, m_b = 5 \text{ GeV}$
- PDFs: CTEQ6M (NLO)
- FFs: NLO FFs from fits to LEP-OPAL data,
initial scale for evolution: $\mu_0 = m_c$ (D -mesons) resp. $\mu_0 = m_b$ (B -mesons)
- Default scale choice: $\mu_R = \mu_F = \mu'_F = m_T$ where $m_T = \sqrt{p_T^2 + m^2}$

HADROPRODUCTION OF D^0, D^+, D^{*+}, D_S^+

GM-VFNS RESULTS W/ KKKSC FFs [1]

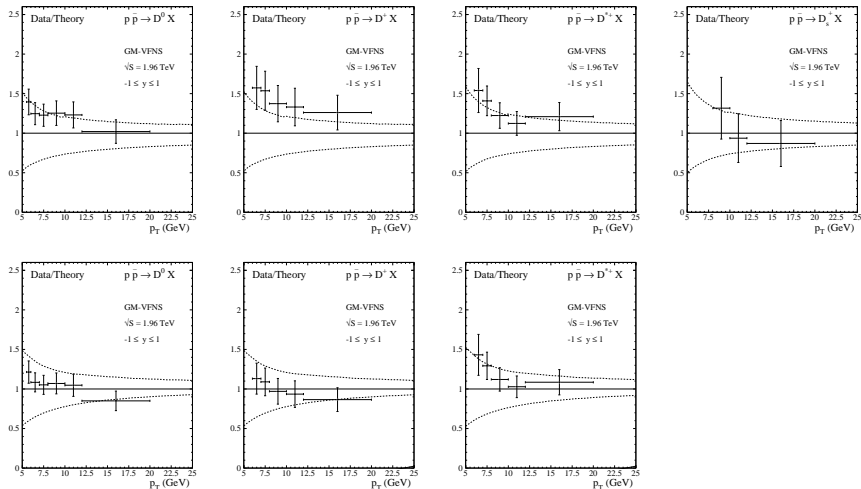


- $d\sigma/dp_T$ [nb/GeV] $|y| \leq 1$ prompt charm
- Uncertainty band: $1/2 \leq \mu_R/m_T, \mu_F/m_T \leq 2$ ($m_T = \sqrt{p_T^2 + m_c^2}$)
- CDF data from run II [2]
- GM-VFNS describes data within errors

[1] Kniehl, Kramer, IS, Spiesberger, arXiv:0901.4130[hep-ph], PRD(to appear)

[2] Acosta et al., PRL91(2003)241804

COMPARISON W/ PREVIOUS KK FFs [1]



- New KKKSc FFs improve agreement w/ CDF data.

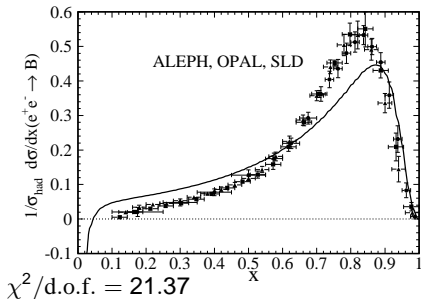
[1] Kniehl, Kramer, PRD74(2006)037502

HADROPRODUCTION OF B^0, B^+ [1]

NEW FFs FROM LEP1/SLC DATA [2]

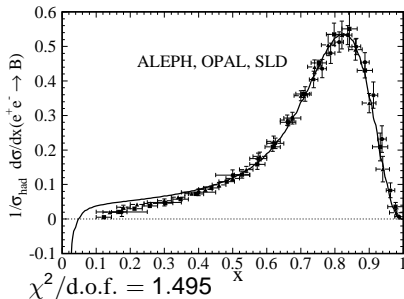
Petersen

$$D(x, \mu_0^2) = N \frac{x(1-x)^2}{[(1-x)^2 + \epsilon x]^2}$$



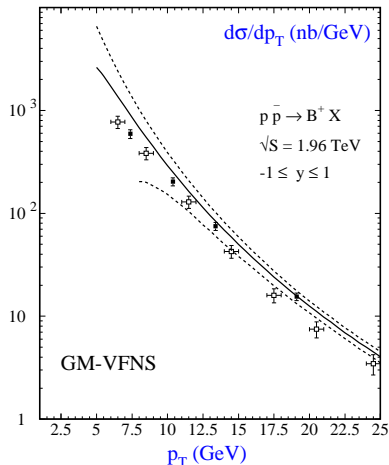
Kartvelishvili-Likhoded

$$D(x, \mu_0^2) = Nx^\alpha(1-x)^\beta$$



[1] Kniehl, Kramer, IS, Spiesberger, PRD77(2008)014011

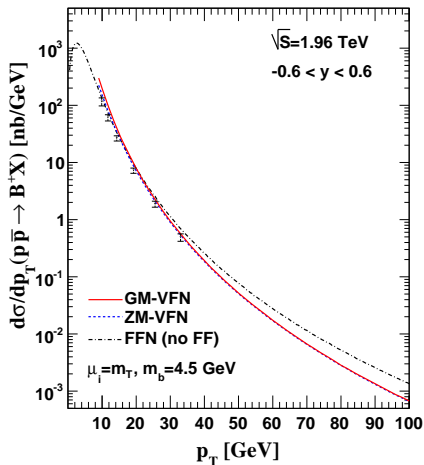
[2] ALEPH, PLB512(2001)30; OPAL, EPJC29(2003)463; SLD, PRL84(2000)4300;
PRD65(2002)092006



- CDF (1.96 TeV):
 - open squares $J/\psi X$ [1]
 - solid squares $J/\psi K^+$ [2]
- CTEQ6.1M PDFs
- $m_b = 4.5 \text{ GeV}$
- $\Lambda_{\overline{\text{MS}}}^{(5)} = 227 \text{ MeV} \rightsquigarrow \alpha_s^{(5)} = 0.1181$
- $1/2 \leq \mu_R/m_T, \mu_F/m_T, \mu_R/\mu_F \leq 2$
 $(m_T = \sqrt{p_T^2 + m_b^2})$

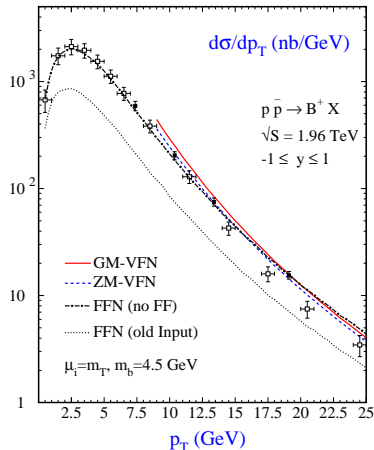
[1] CDF, PRD71(2005)032001

[2] CDF, PRD75(2007)012010



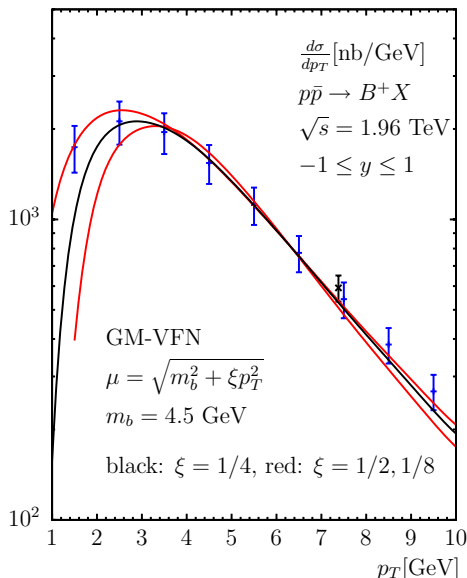
- CDF II (preliminary) [1]
- $\mu_R = \mu_F = m_T$
- for $p_T \gg m_b$:
 - GM-VFN merges w/ ZM-VFN
 - FFN breaks down
- data point in bin [29,40] favors GM-VFN

[1] Kraus, FERMILAB-THESIS-2006-47; Annovi, FERMILAB-CONF-07-509-E



- obsolete FFN as above
- up-to-date FFN evaluated with
 - CTEQ6.1M PDFs
 - $m_b = 4.5 \text{ GeV}$
 - $\Lambda_{\overline{MS}}^{(5)} = 227 \text{ MeV} \rightsquigarrow \alpha_s^{(5)} = 0.1181$
 - $D(x) = B(b \rightarrow B)\delta(1-x)$ with $B(b \rightarrow B) = 39.8\%$

[1] Kniehl, Kramer, IS, Spiesberger, PRD77(2008)014011



- evaluate $d\hat{\sigma}_{\text{ZM}}^{(1)}(Q + g/q \rightarrow Q + X)$
 @ LO to match
 $f_{g \rightarrow Q}^{(1)} \otimes d\hat{\sigma}^{(0)}(Q + g/q \rightarrow Q + g/q)$
- evaluate
 $d\hat{\sigma}^{(0)}(gg/q\bar{q} \rightarrow Q\bar{Q}) \otimes d_{Q \rightarrow Q}^{(1)}$
 w/ $m_Q \neq 0$ to match
 $d\hat{\sigma}_{\text{GM}}^{(1)}(gg/q\bar{q} \rightarrow Q/\bar{Q} + X)$
- impose $\theta(\hat{s} - 4m_Q^2)$ on massless kinematics
- choose $\mu_F^2 = m_Q^2 + \xi p_T^2$ so that
 $\mu_F \xrightarrow{p_T \rightarrow 0} m_Q = \mu_0$
- $G(m, p_T) \equiv 1$ in contrast to FONLL

- Discussion of 1-particle inclusive hadroproduction of heavy quarks in a **massive VFNS** (GM-VFNS)
- Available at NLO in the GM-VFNS:
 - $\gamma\gamma \rightarrow HX$
 - $\gamma p \rightarrow HX$
 - $p\bar{p} \rightarrow HX$
- Work in progress:
 - $ep \rightarrow HX$
 - Matching to the fixed order theory at small p_T
 - Updated predictions for the LHC (latest FFs, PDFs)

Backup Slides

$$\text{FONLL} = \text{FO} + (\text{RS} - \text{FOM0})G(m, p_T)$$

FO: Fixed Order; FOM0: Massless limit of FO; RS: Resummed

$$G(m, p_T) = \frac{p_T^2}{p_T^2 + 25m^2}$$

$$\Rightarrow \text{FONLL} = \begin{cases} \text{FO} & : p_T \lesssim 5m \\ \text{RS} & : p_T \gtrsim 5m \end{cases}$$

[1] Cacciari, Greco, Nason, JHEP05(1998)007

FONLL = FO + (RS - FOM0)G(m, p_T) with

$$G(m, p_T) = \frac{p_T^2}{p_T^2 + 25m^2}$$

GM-VFNS = FO + (RS - FOM0)G(m, p_T) with

$$\tilde{G}(m, p_T) = 1$$

FO: Fixed Order; FOM0: Massless limit of FO; RS \equiv ZM-VFNS: Resummed

- Both approaches interpolate between FO and ZM-VFNS
 - FONLL: obvious;
 - GM-VFNS: matching with FO at quark level (see Olness, Scalise, Tung, PRD59(1998)014506)
- Factor $\tilde{G}(m, p_T)$ follows from calculation; $\tilde{G}(m, p_T) = 1 \leftrightarrow$ S-ACOT scheme
- Different point-of-view: GM-VFNS finally needs PDFs and FFs in this scheme.
- Numerical comparisons interesting and should be done!