

FLUCTUATIONS AND CORRELATIONS STUDY AT NA61/SHINE



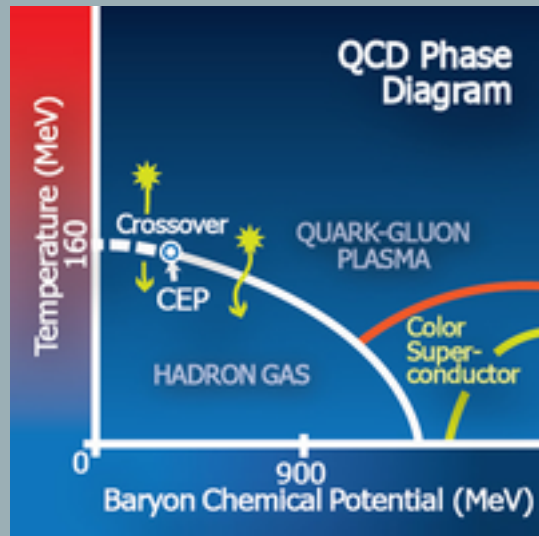
Daria Prokhorova
for the NA61/SHINE Collaboration
St. Petersburg State University
Laboratory of Ultra-High Energy Physics



October 22, III NICA days, Warsaw, Poland
MPD/SHINE Joint Session

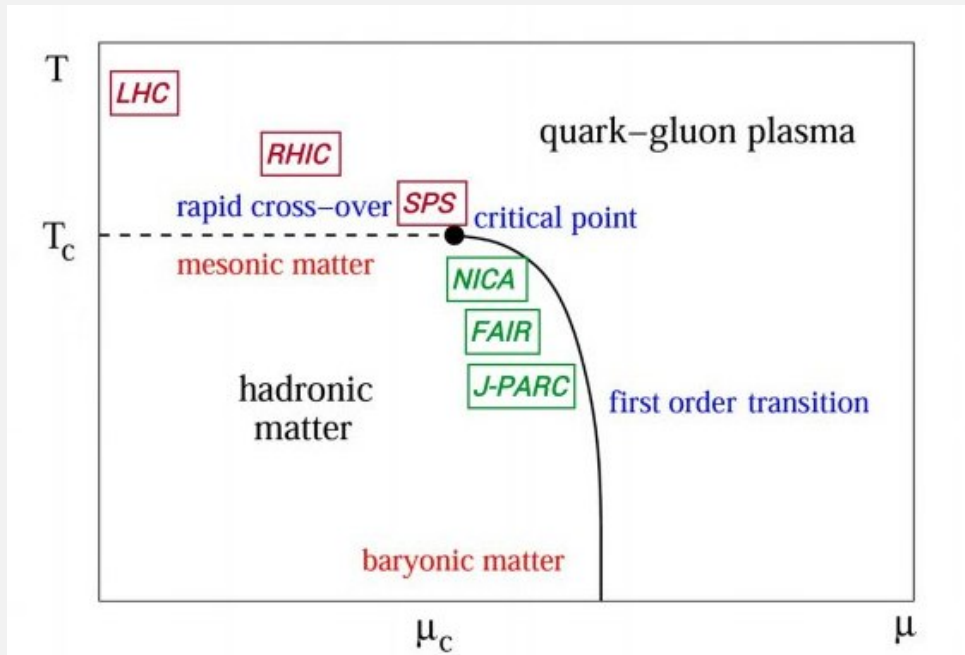
OUTLINE

1. Search for the critical point
2. NA61/SHINE experiment
3. Fluctuation measures
4. Results corrections and possible systematic problems
5. Conclusions



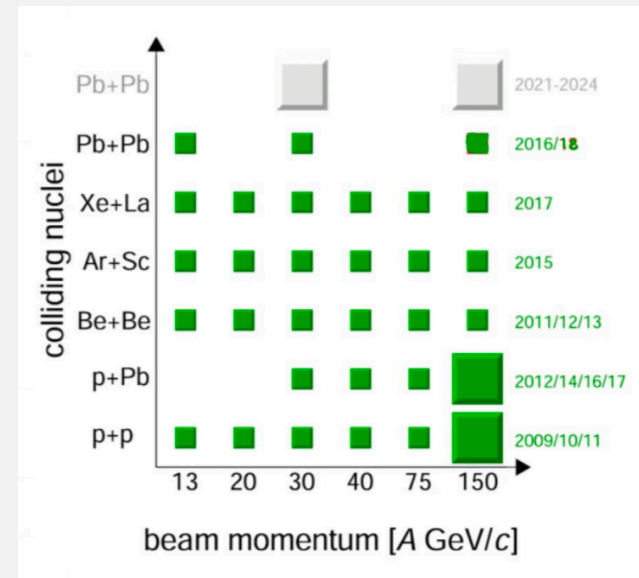
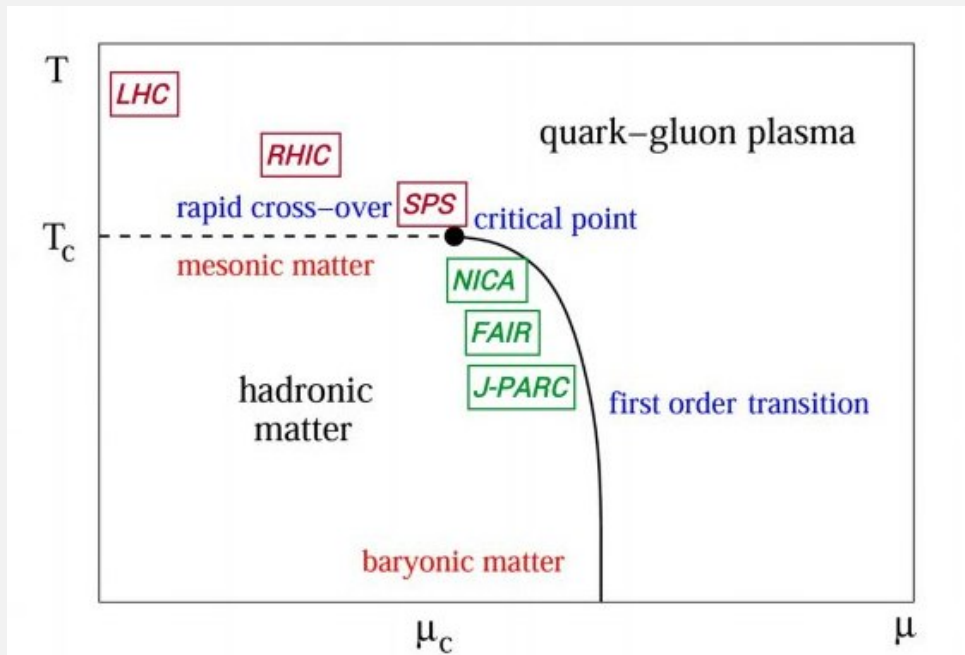
SEARCH FOR THE CRITICAL POINT

The most popular scenario:



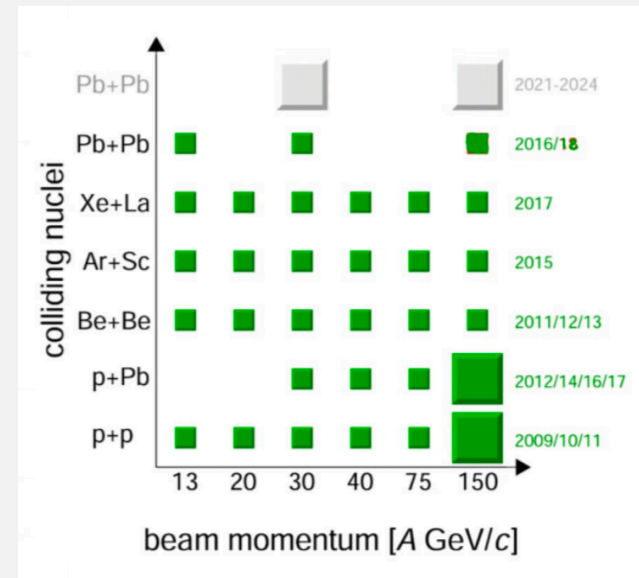
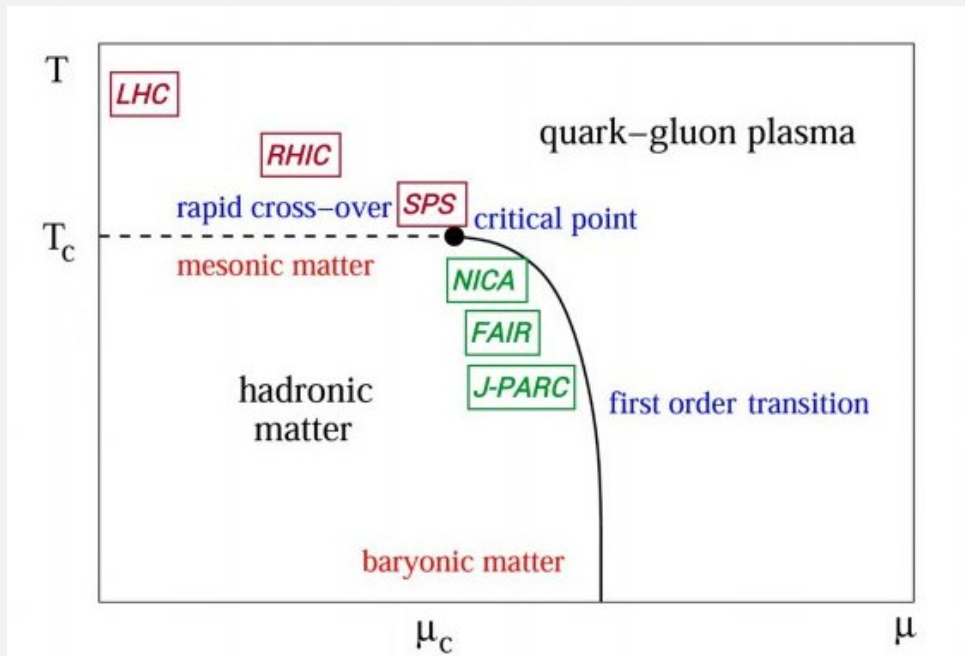
Scan in system size and beam energy → search for the **critical point**

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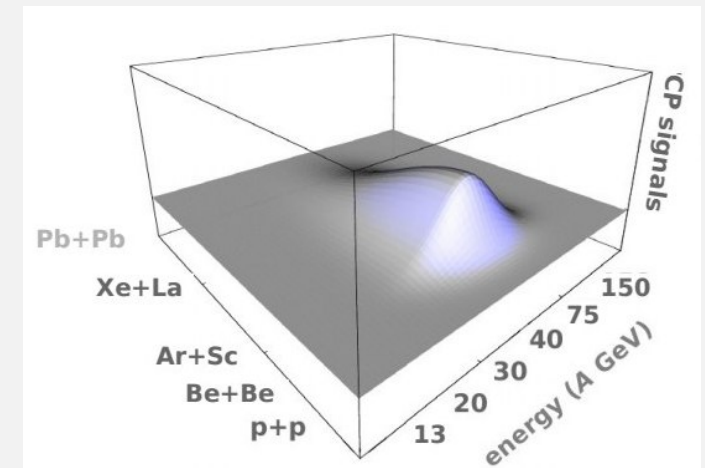


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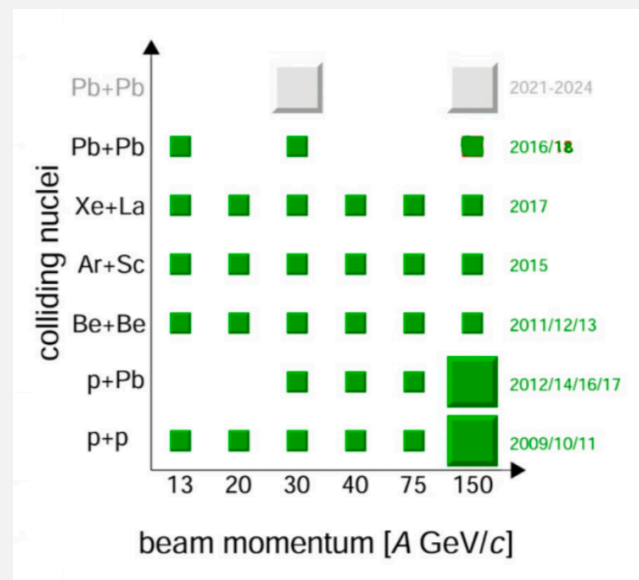
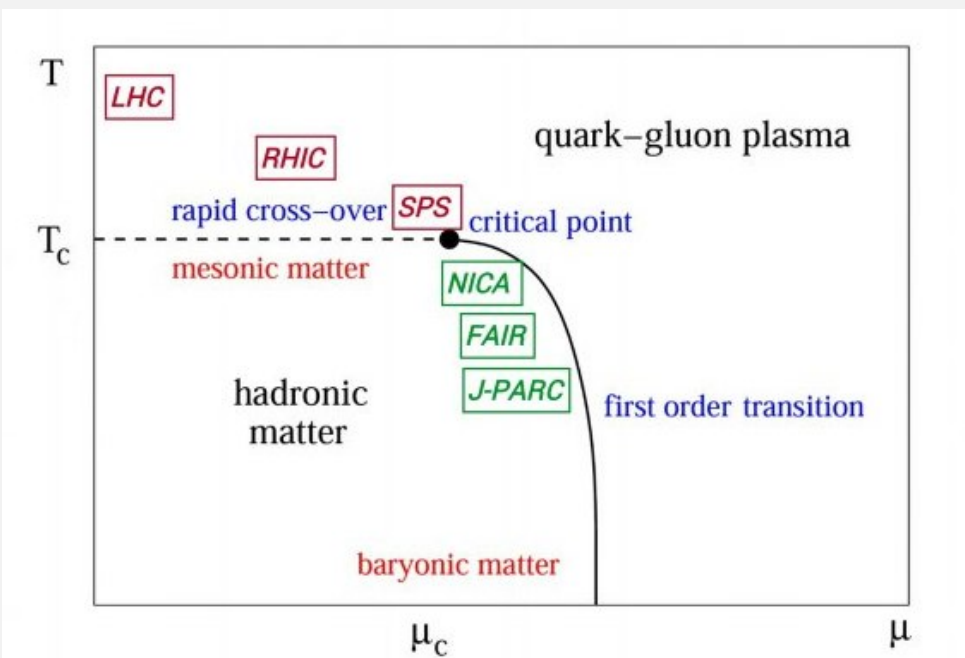


Expected region of enhanced fluctuations

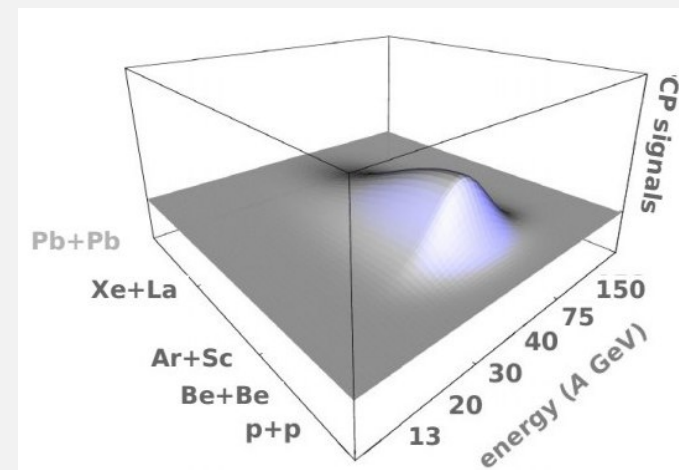


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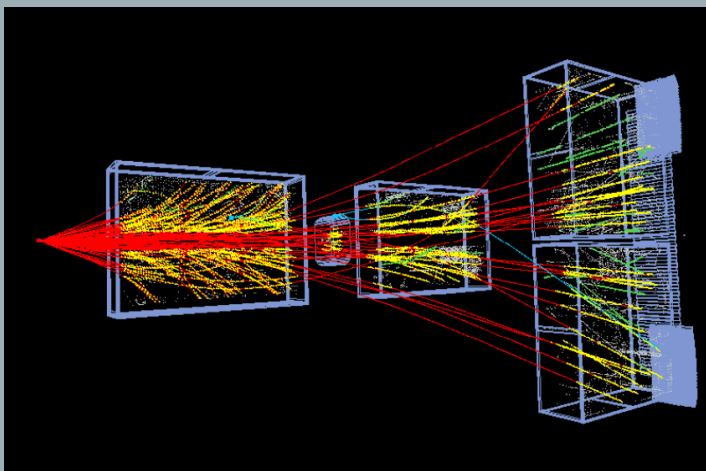


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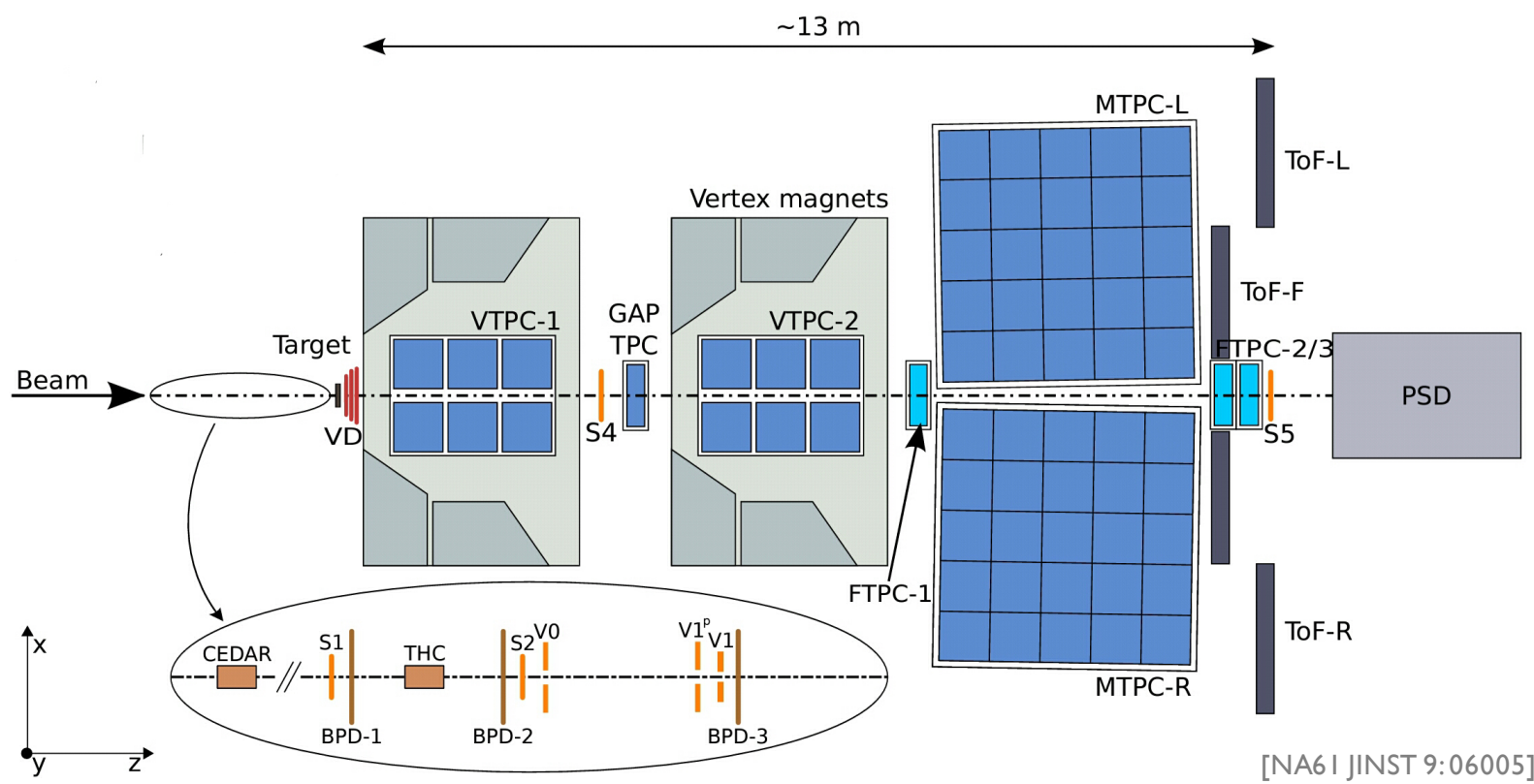
NA6I/SHINE strong interactions programme:

- study the properties of the onset of deconfinement
- search for the critical point of strongly interacting matter

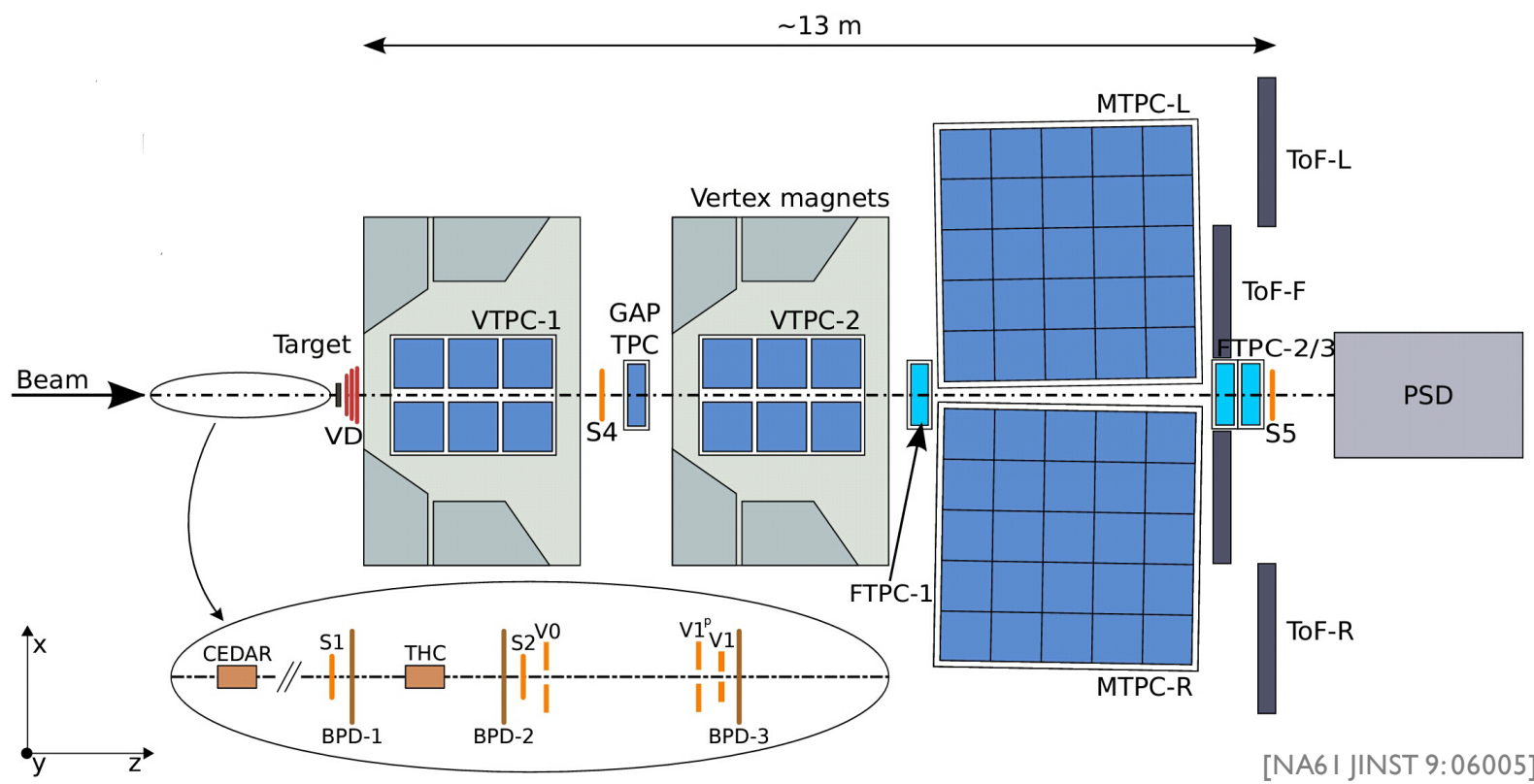


NA61/SHINE EXPERIMENT

SHINE - **SPS** Heavy Ion and **N**eutrino **E**xperiment

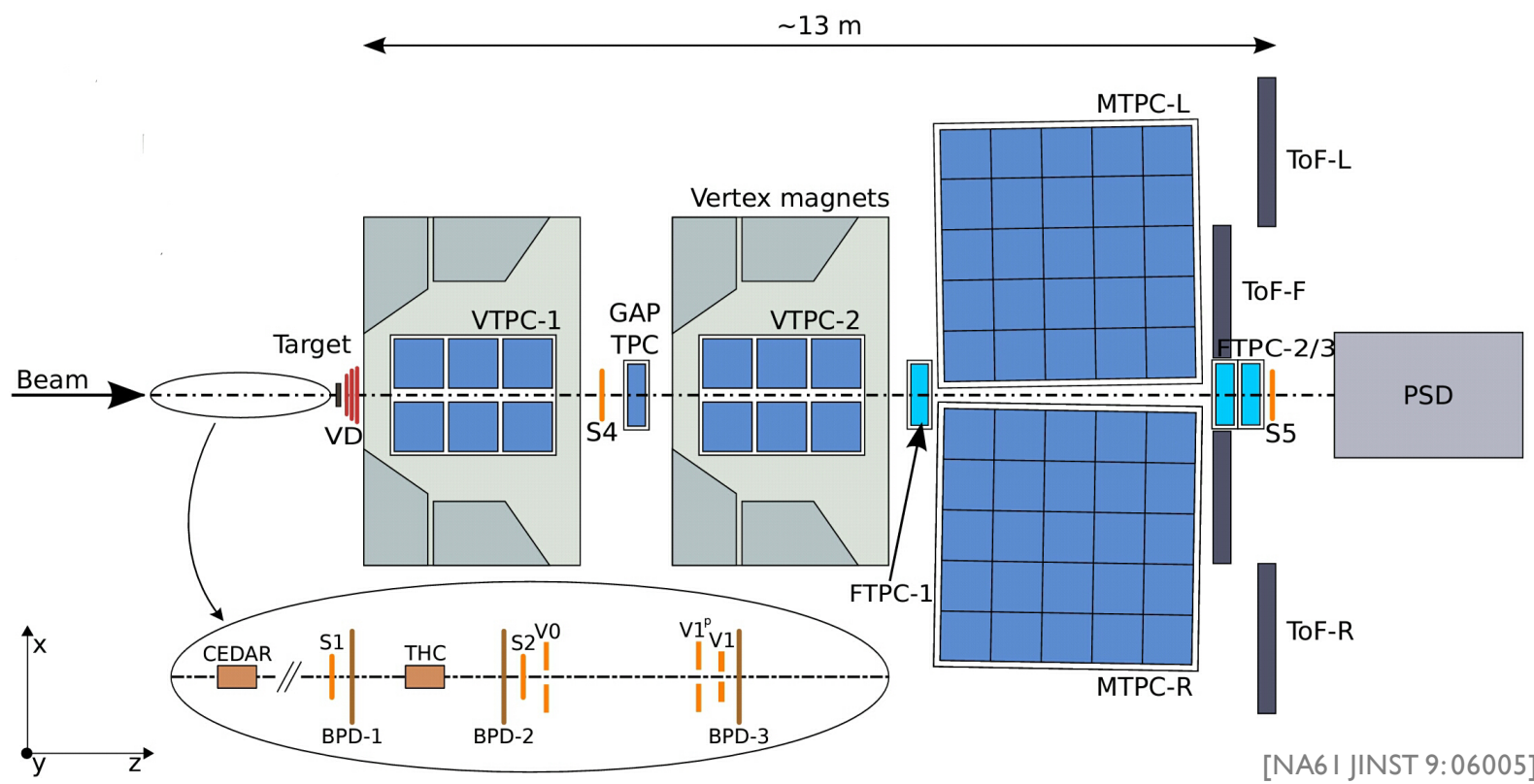


SHINE - SPS Heavy Ion and Neutrino Experiment



Performs the scan of beam momenta (13A - 150/158A GeV/c) and system size (p+p, p+Pb, Be+Be, Ar+Sc, Xe+La, Pb+Pb)

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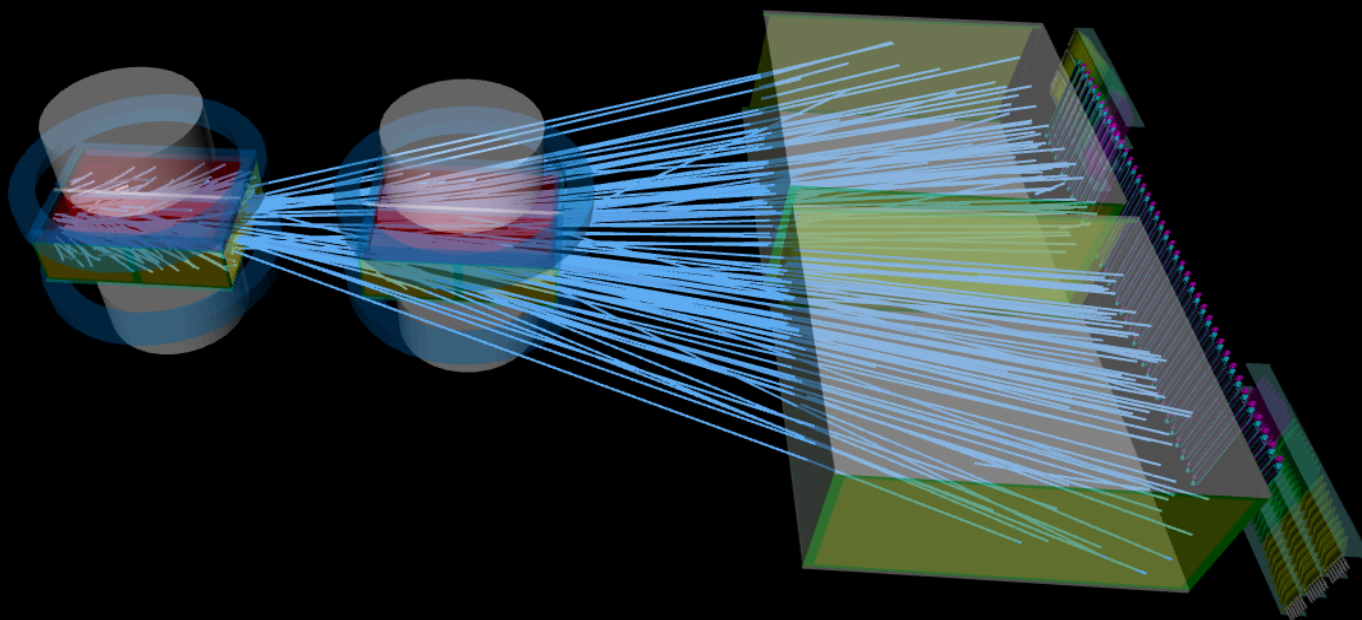


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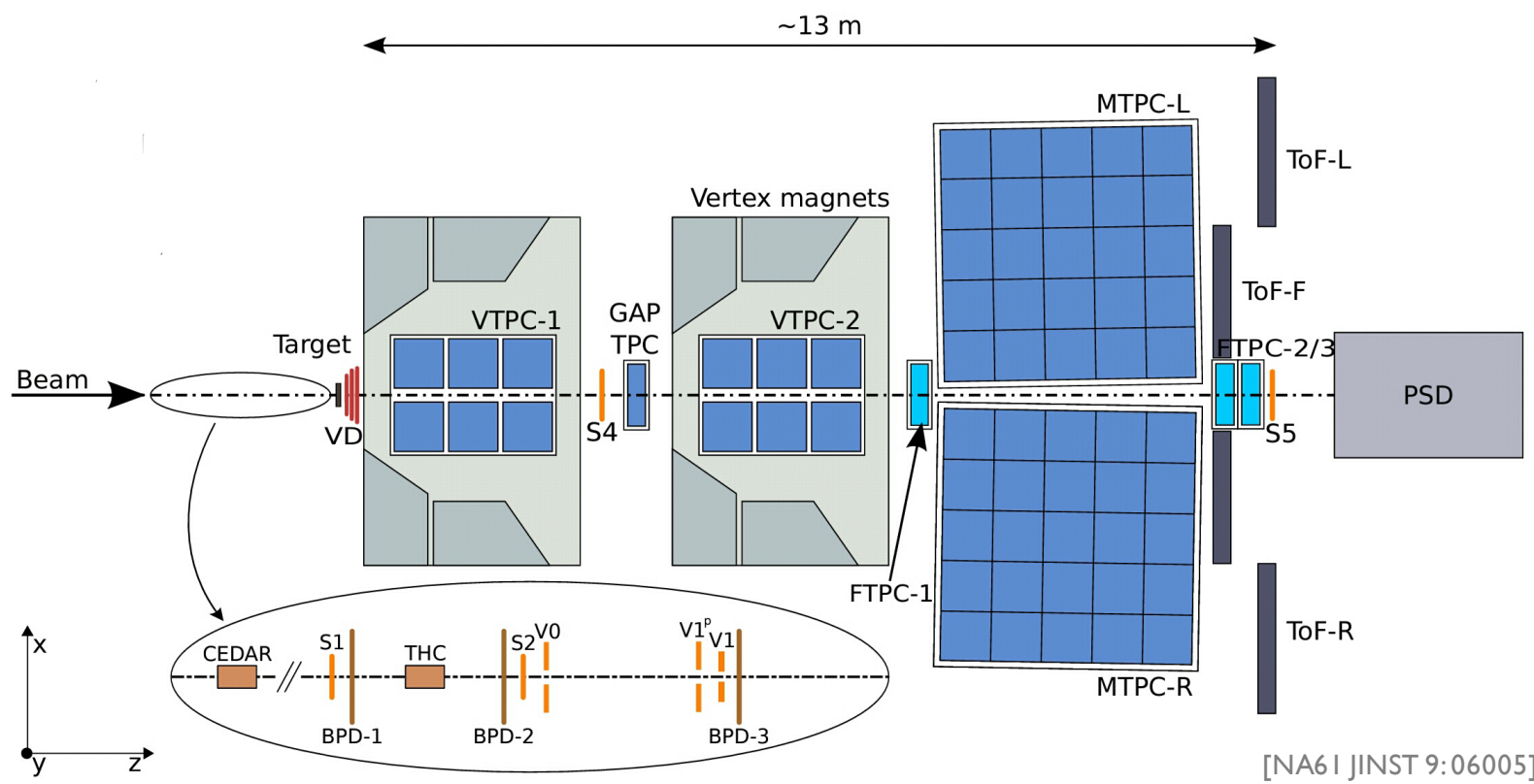
NA61/SHINE event display



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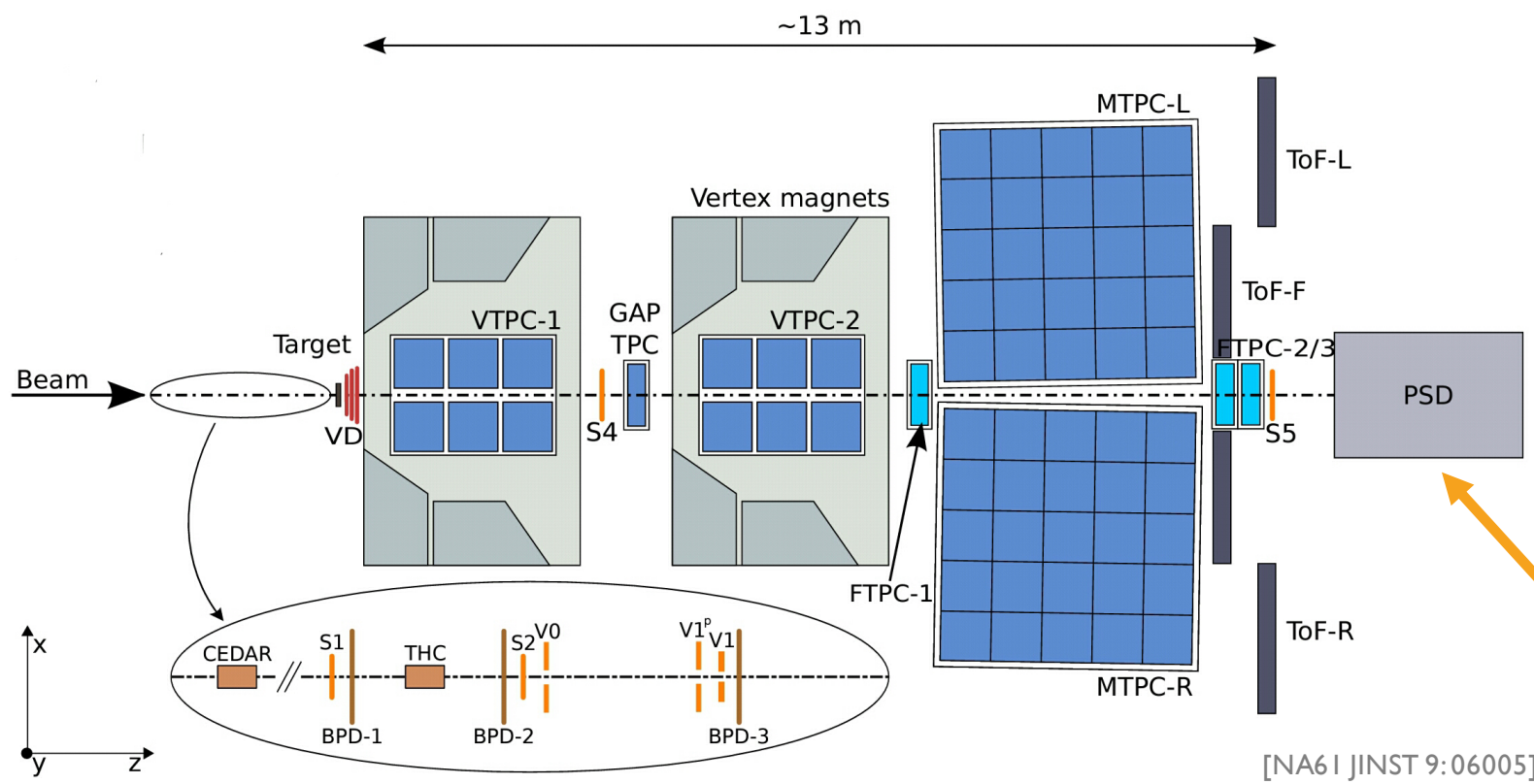


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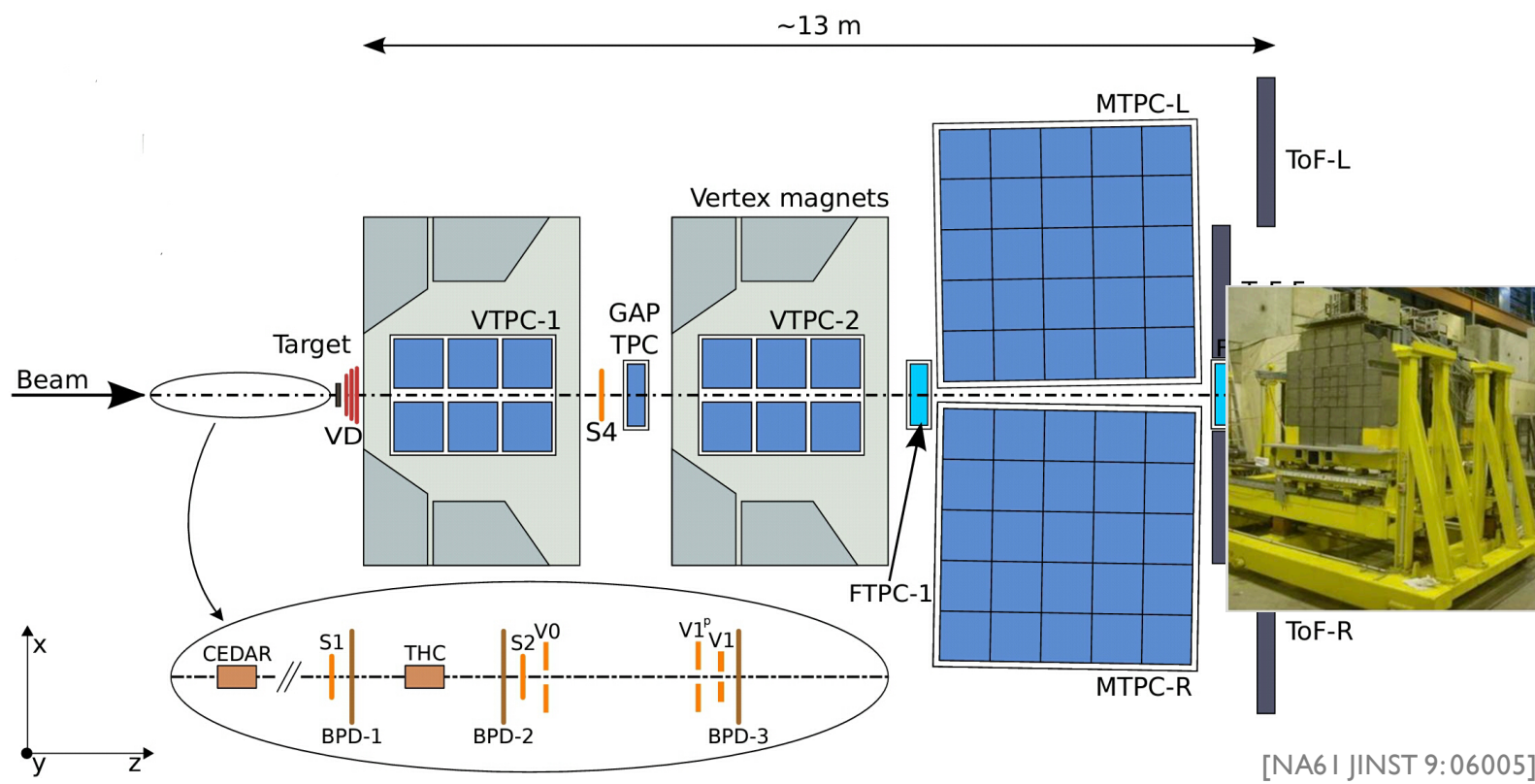


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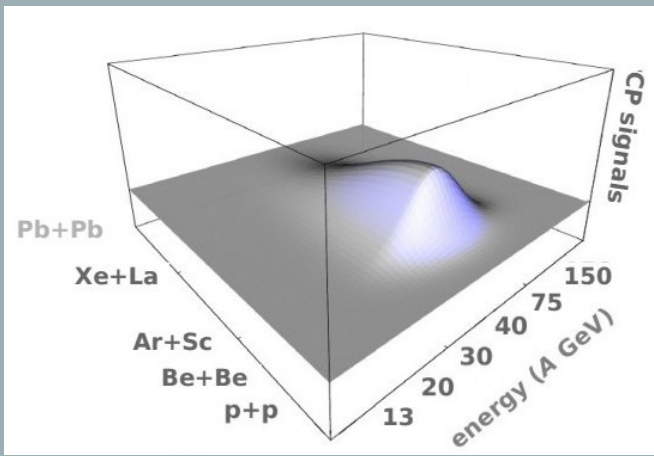
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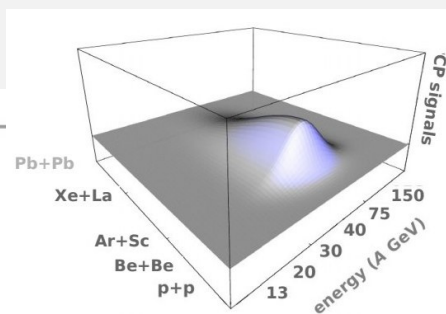
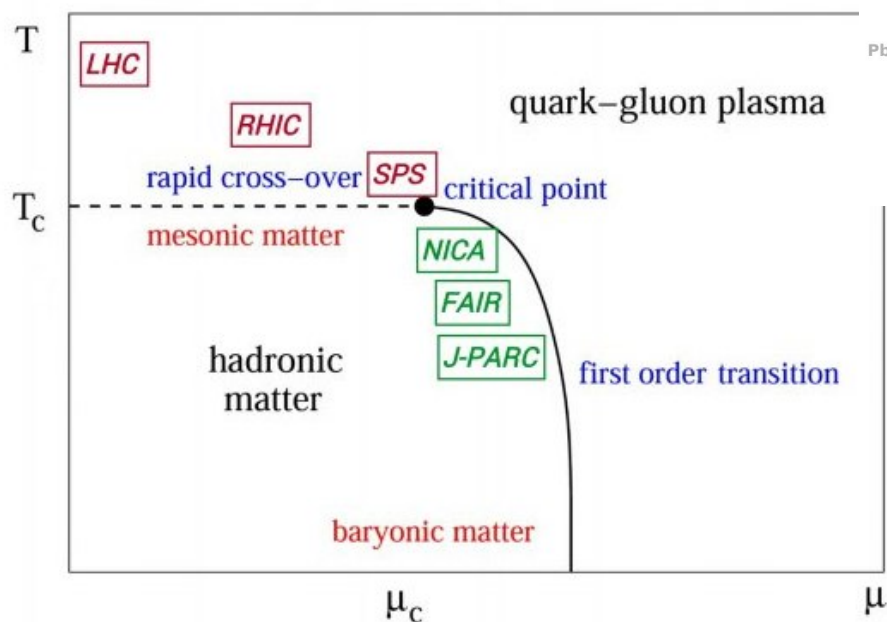
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FLUCTUATION MEASURES

Scan in system size and beam energy → search for the **critical point**

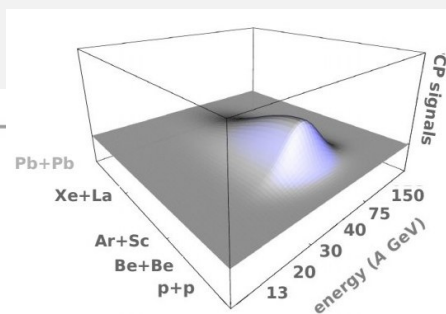
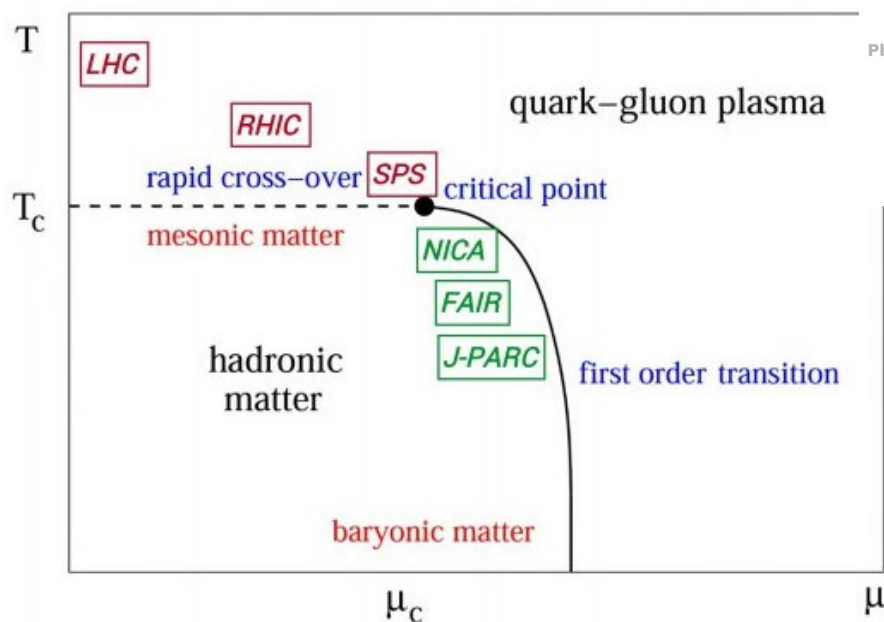
[Gazdzicki, M., Seyboth, P. *Acta Phys. Pol. B* 47, 1201 (2016)]



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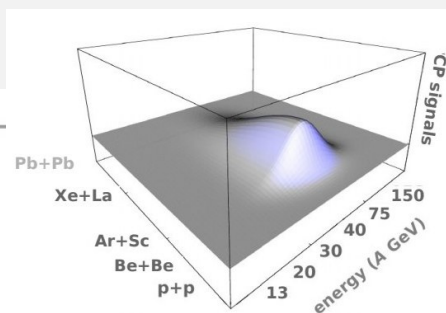
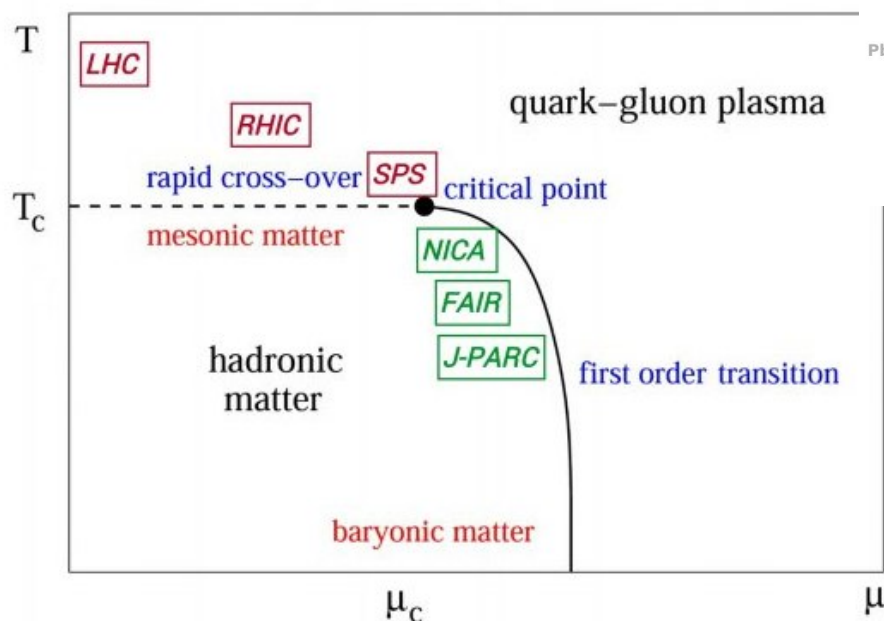
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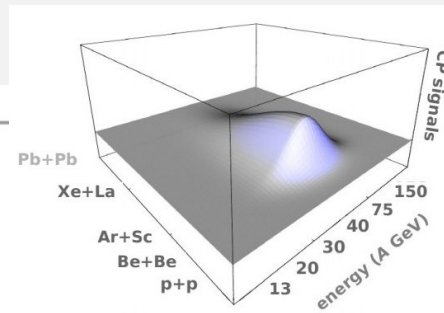
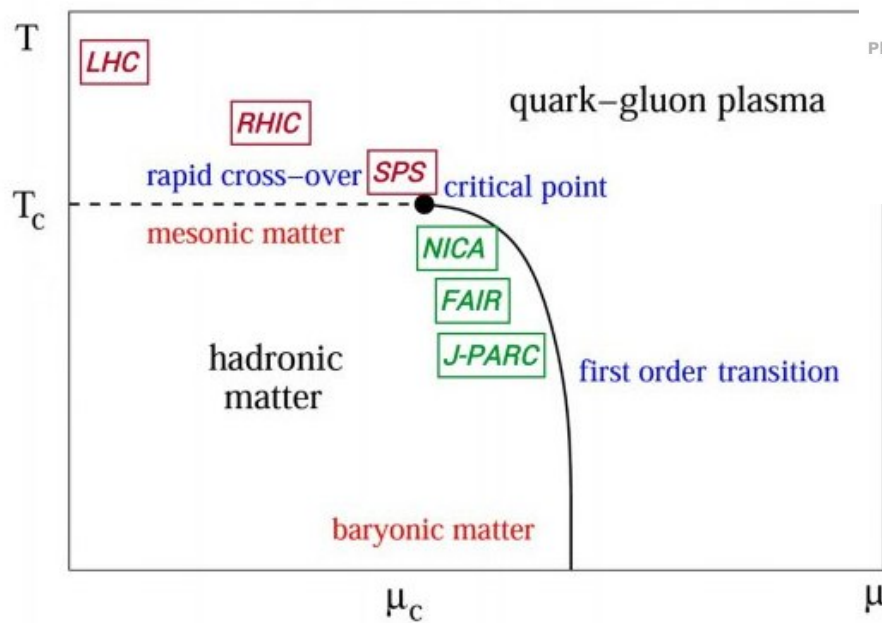
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What is the CP signal amplitude?

What if it is shadowed by trivial fluctuations?

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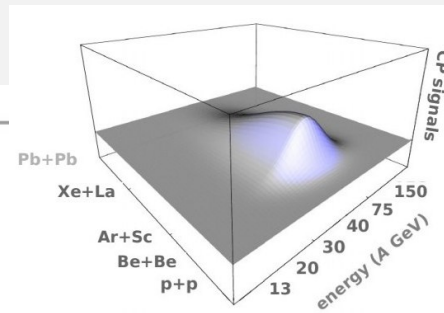
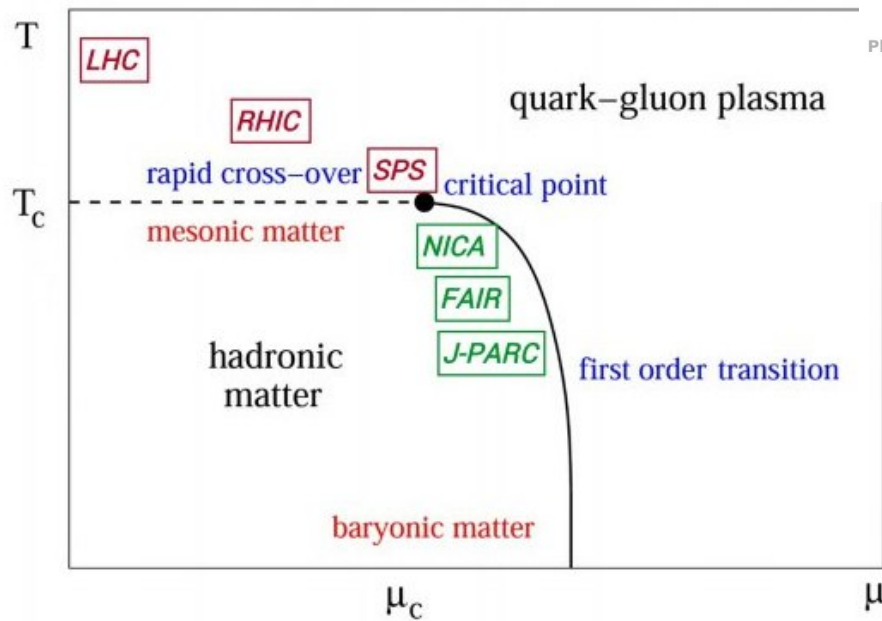
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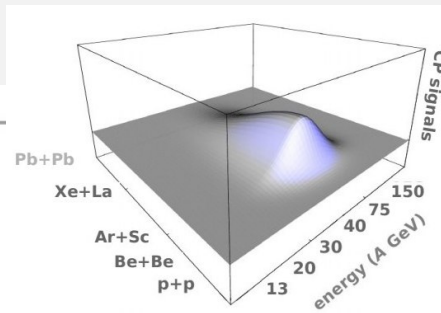
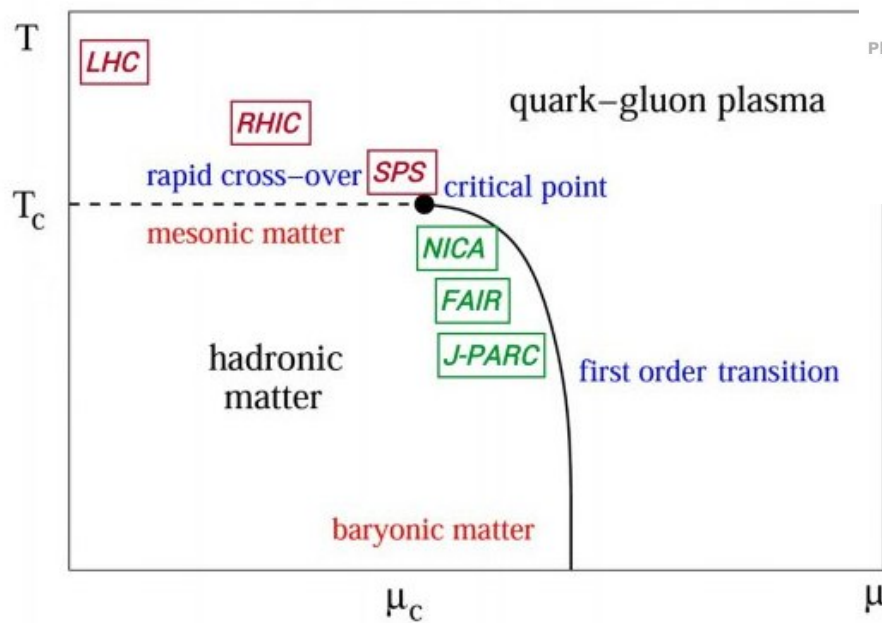
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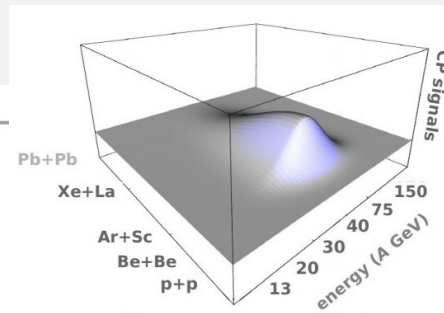
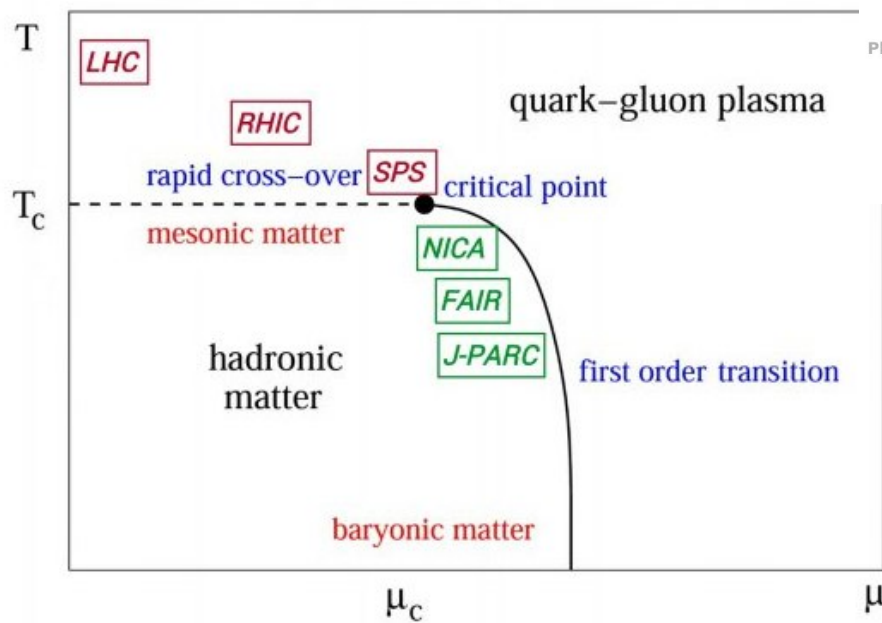
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Intensive fluctuation measure: independent of the number of sources or the system volume

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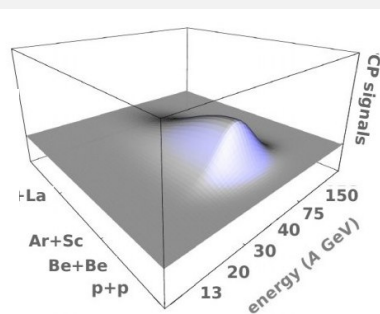
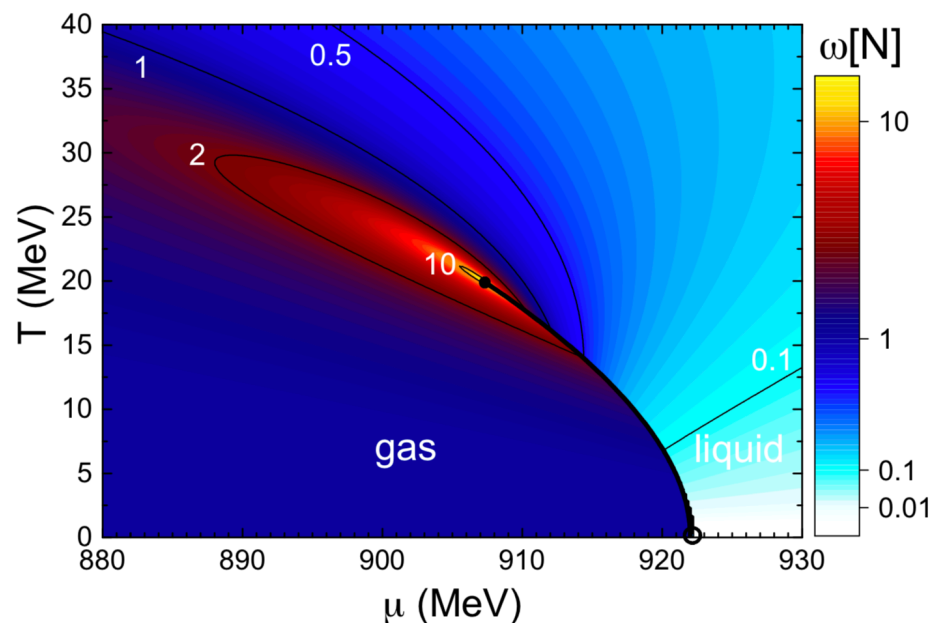
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Possible sensitivity:



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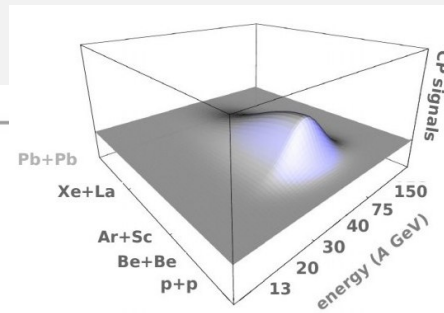
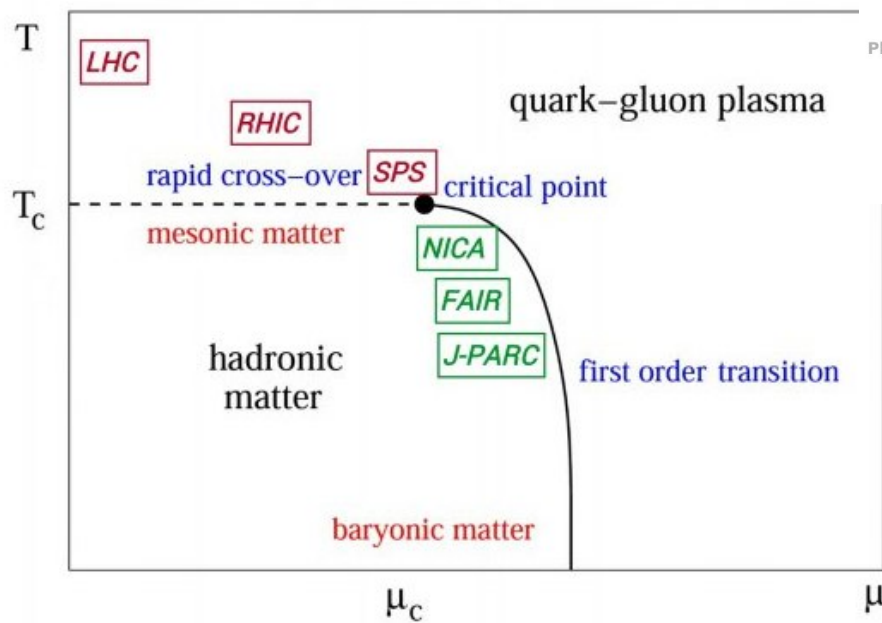
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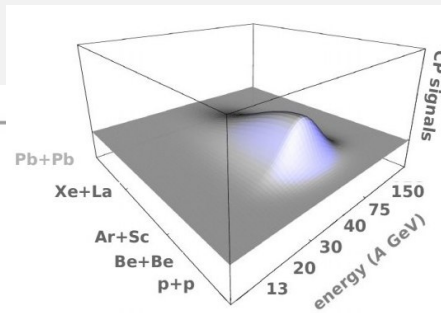
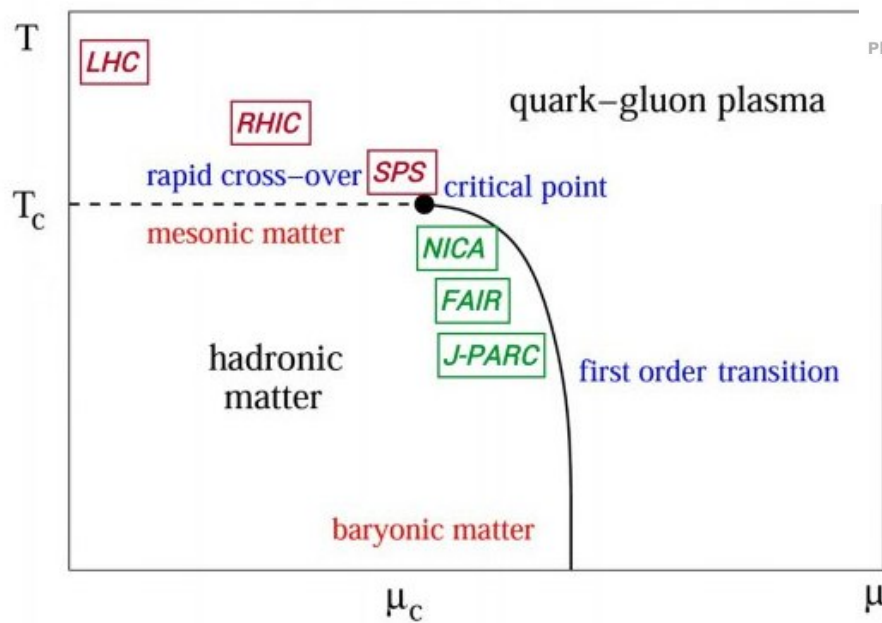
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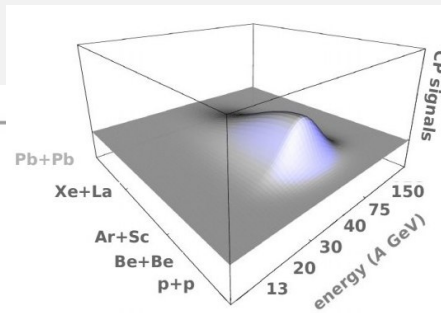
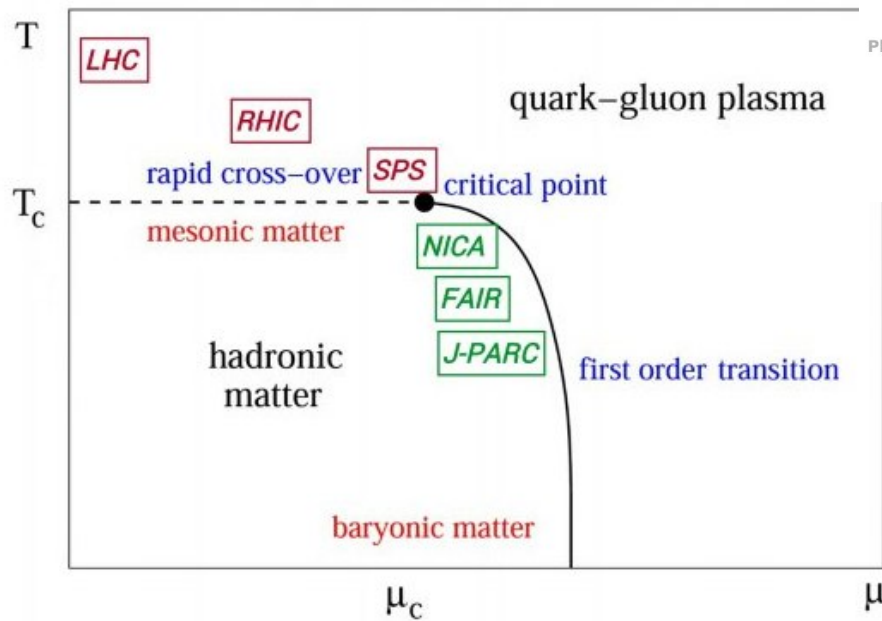
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More sensitivity

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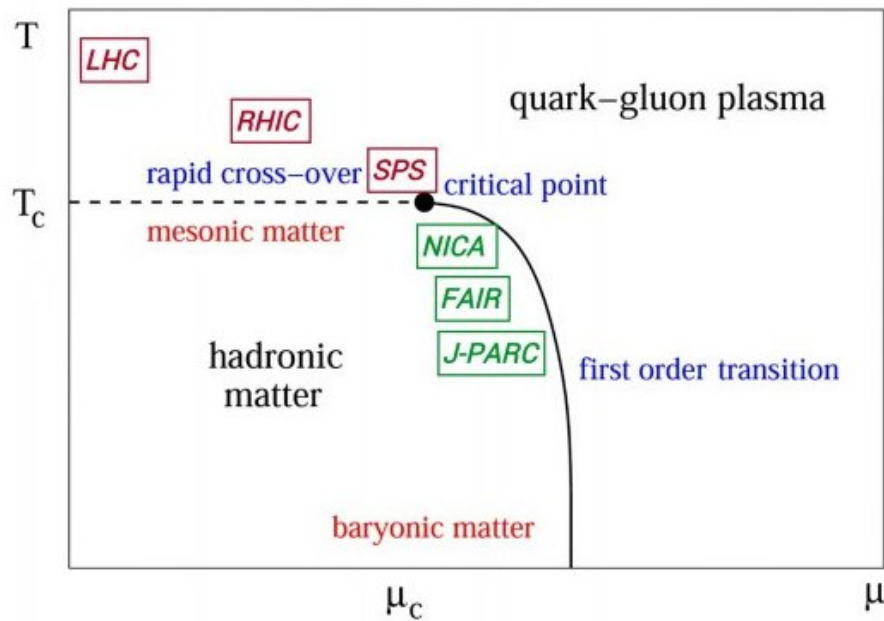
More sensitivity

Higher order moments: **intensive skewness and kurtosis** of conserved quantities distributions are more sensitive to the correlation length divergence

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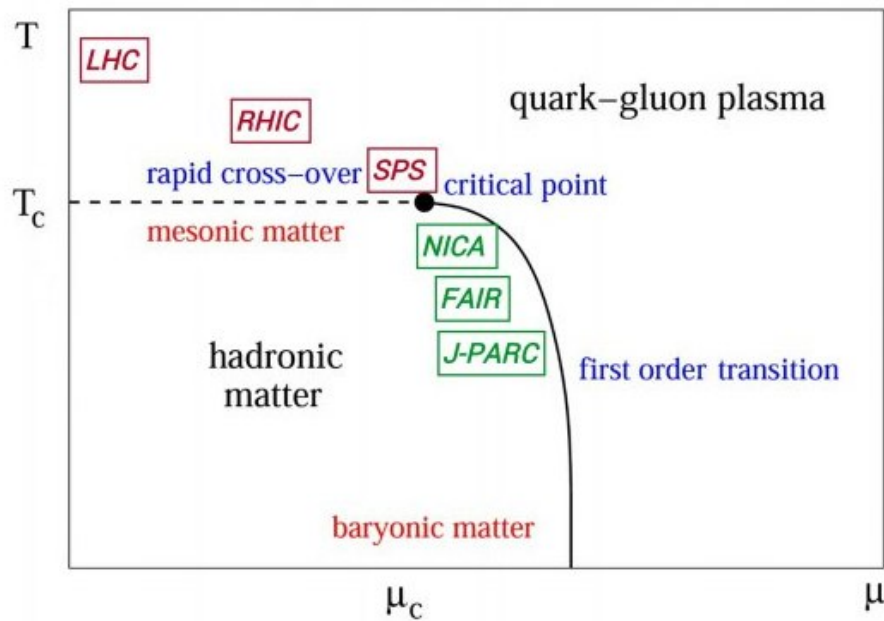


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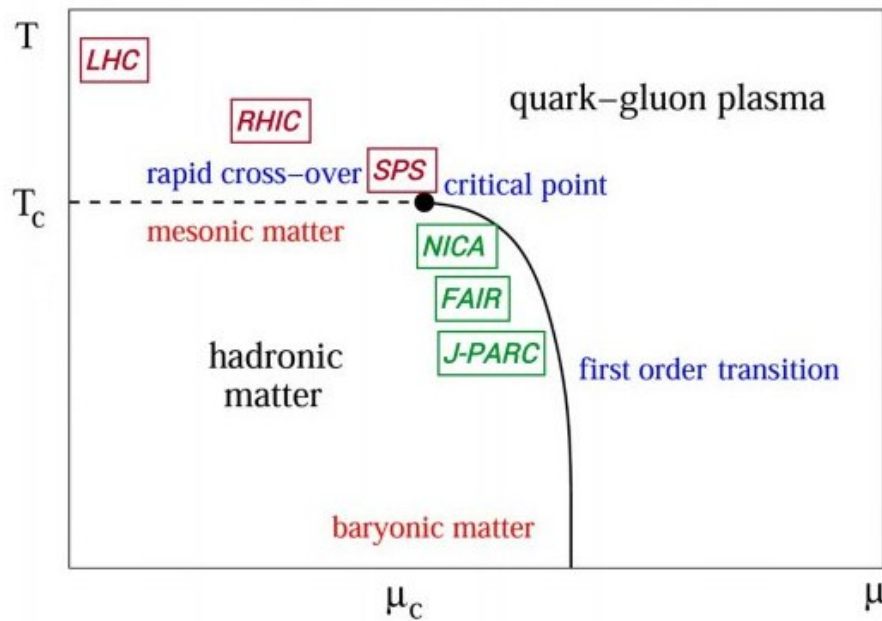
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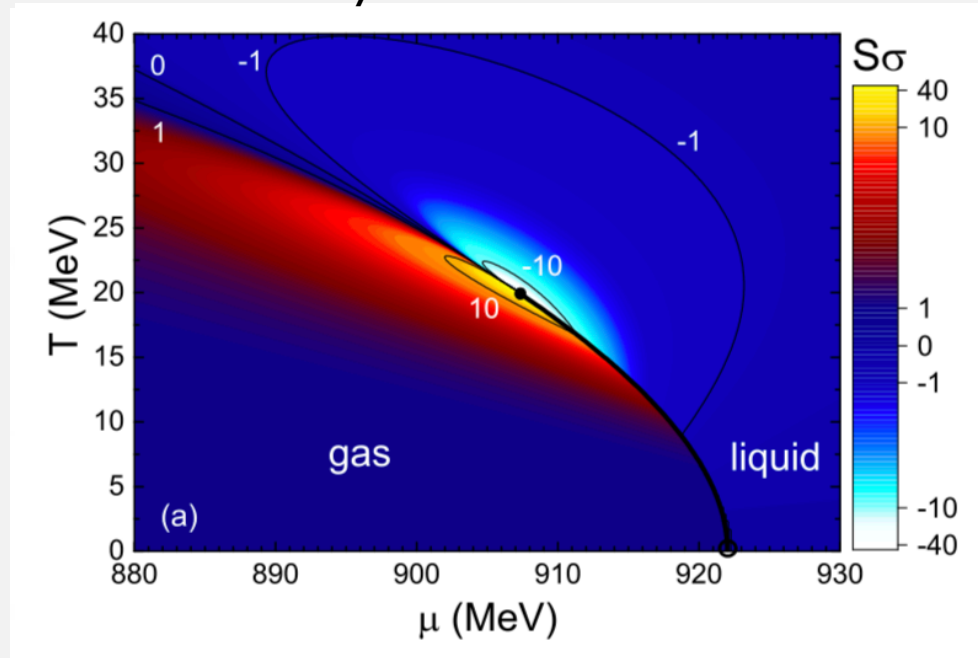
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Possible sensitivity:



Nucleon system with van der Waals EOS in GCE formulation in the vicinity of the Critical Point

[Vovchenko, Gorenstein, Stoecker, PRL 118: 182301, Vovchenko, et al., JPA 48: 305001]

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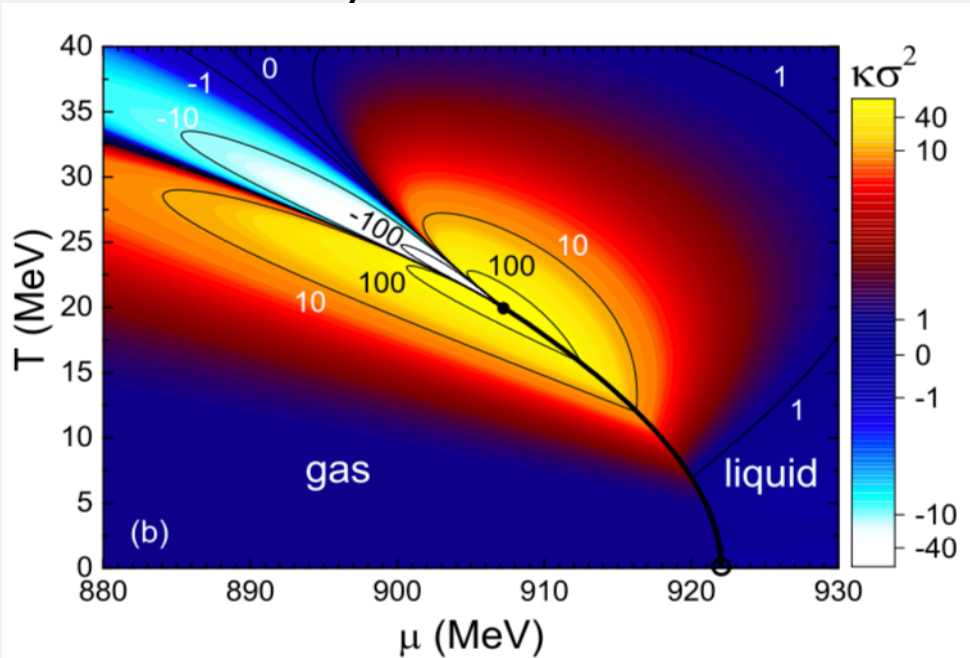
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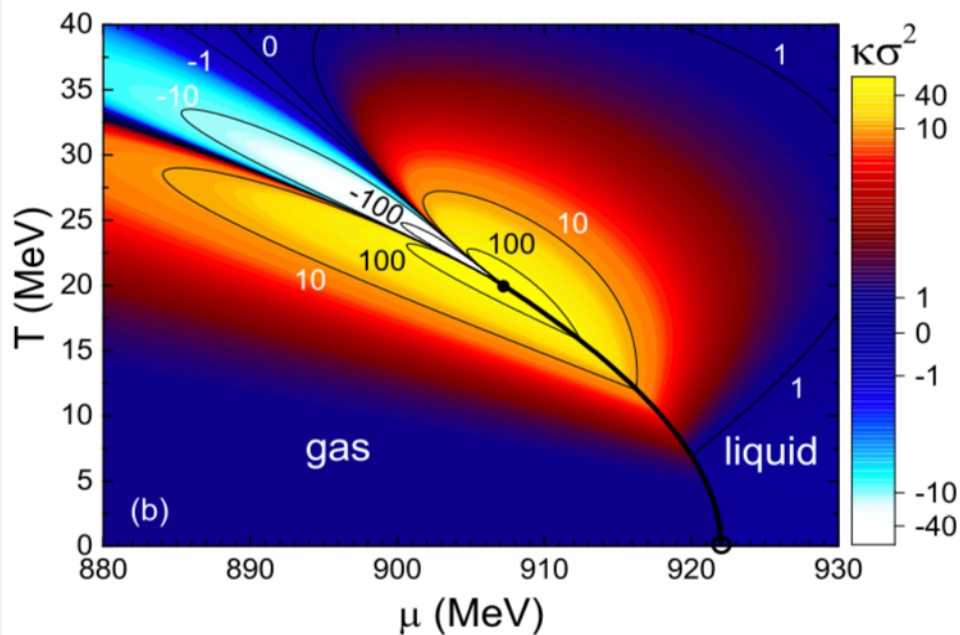
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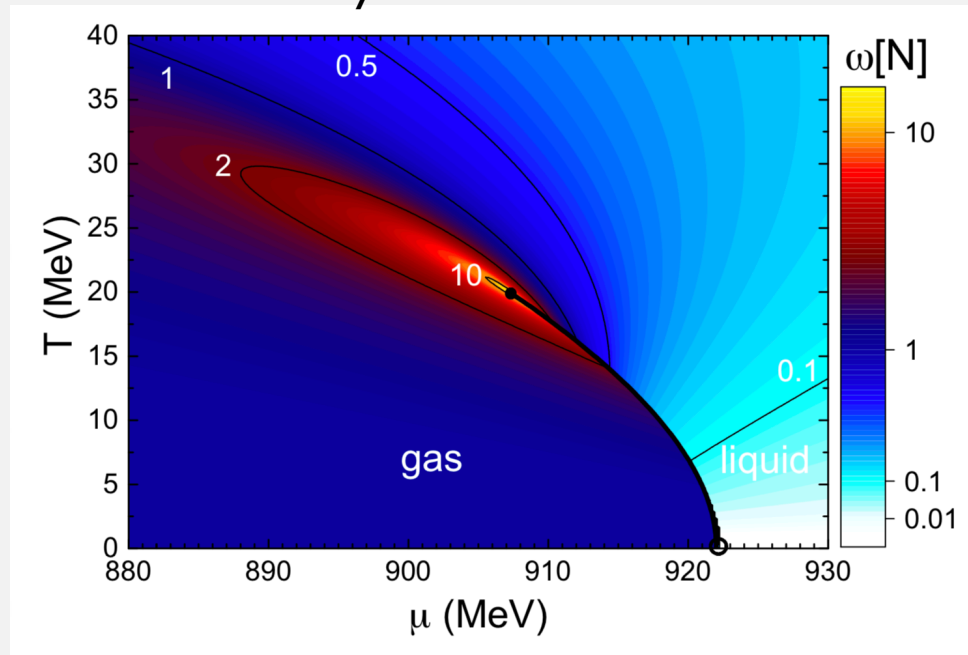
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but the problem is that the dependence on the volume distribution remains

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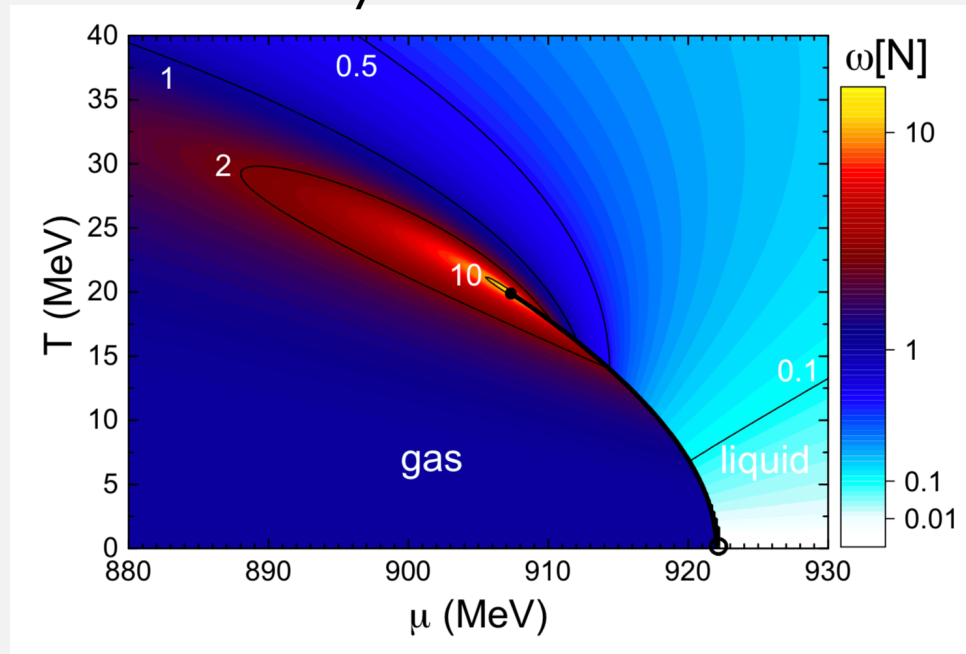
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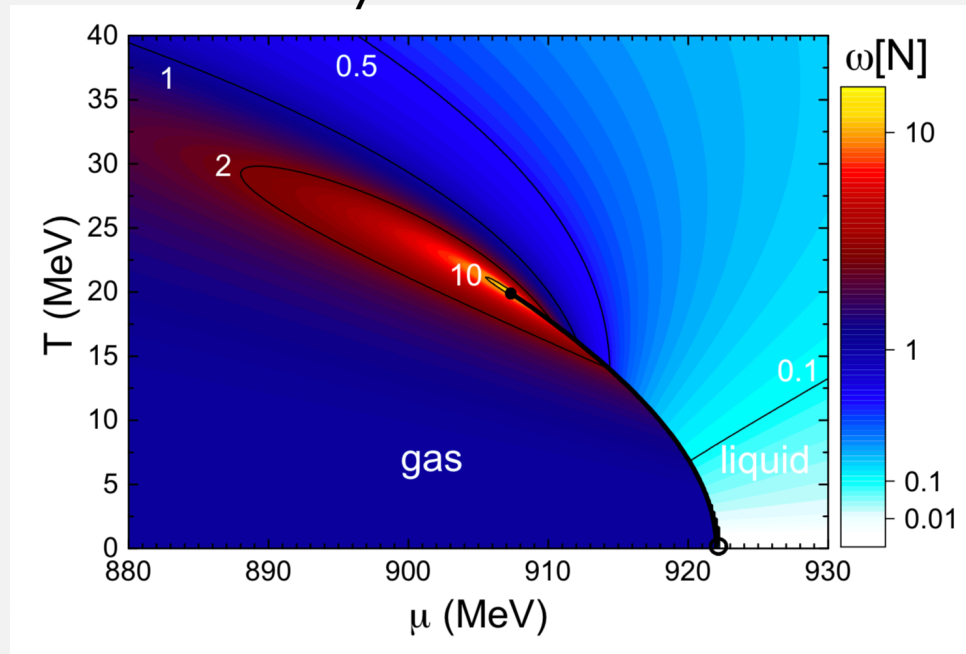
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scaled variance of the quantity A for each source

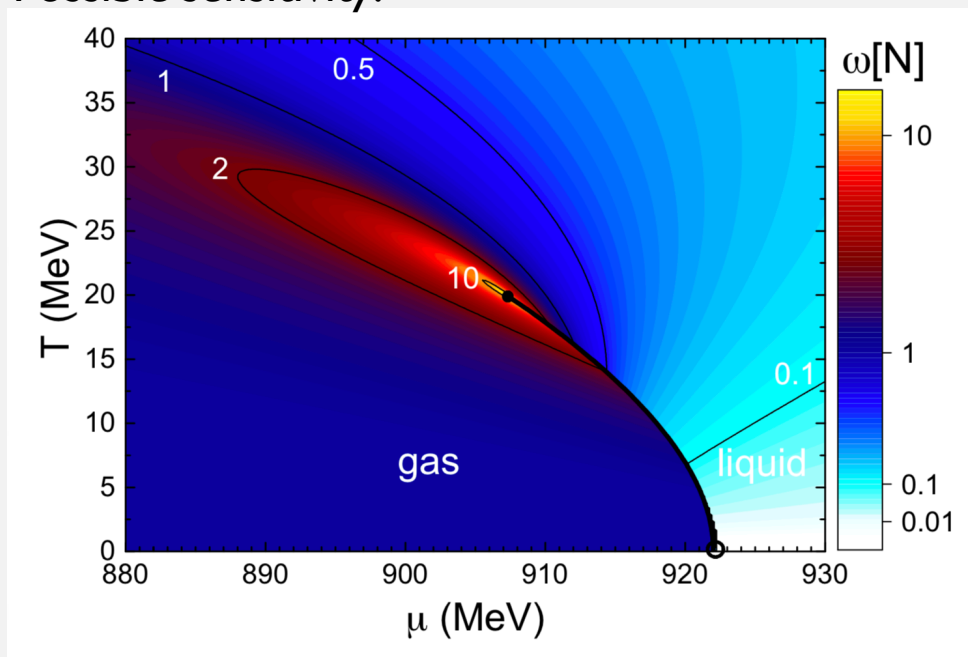
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[Vovchenko, Gorenstein, Stoecker, PRL 118: 182301, Vovchenko, et al., JPA 48: 305001]

$$\omega[N] = \frac{\langle (\Delta N)^2 \rangle}{\langle N \rangle}$$

Intensive fluctuation measure: independent of the number of sources or the system volume

$$\omega_A \equiv \frac{\langle A^2 \rangle - \langle A \rangle^2}{\langle A \rangle} = \frac{\langle a^2 \rangle - \langle a \rangle^2}{\langle a \rangle} + \langle a \rangle \frac{\langle N_s^2 \rangle - \langle N_s \rangle^2}{\langle N_s \rangle} \equiv \omega_a^* + \langle a \rangle \omega_s$$

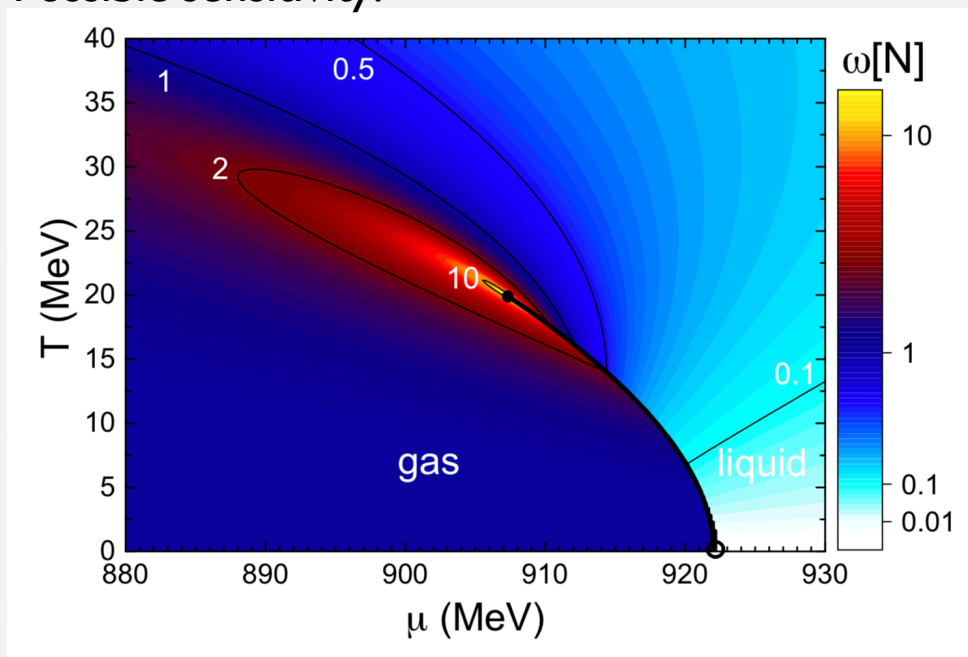
scaled variance of the quantity A for each source

scaled variance of the number of sources

Scan in system size and beam energy → search for the **critical point**

~ region of enhanced fluctuations

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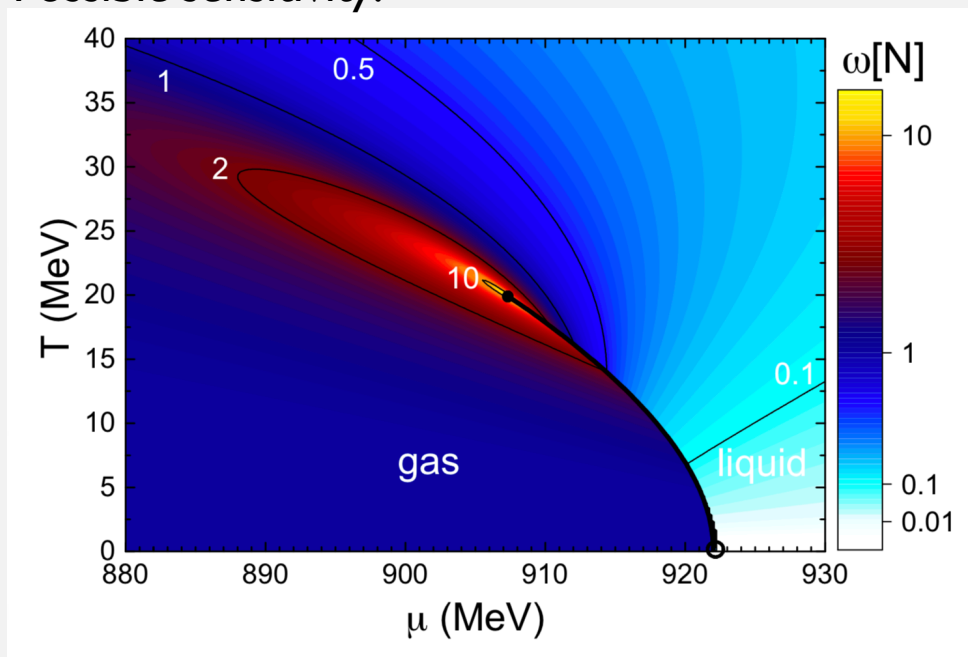
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scaled variance of the quantity A for each source

System volume ↔ scaled variance of the number of sources

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$$\omega[N] = \frac{\langle (\Delta N)^2 \rangle}{\langle N \rangle}$$

Intensive fluctuation measure: independent of the number of sources or the system volume, **but still depend on the volume fluctuations**

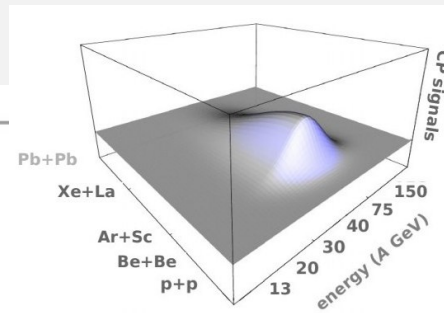
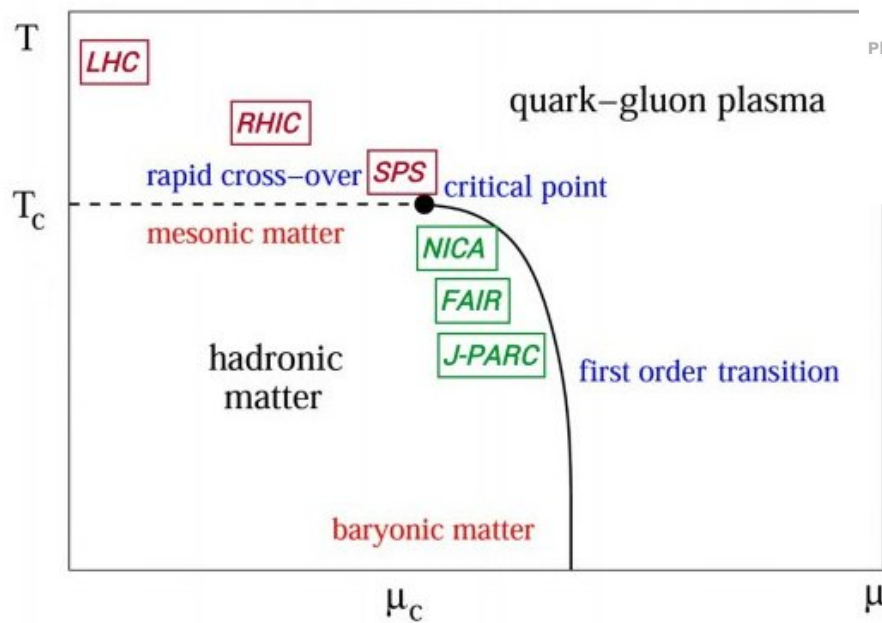
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Scan in system size and beam energy → search for the **critical point**

[Gazdzicki, M., Seyboth, P. *Acta Phys. Pol. B* 47, 1201 (2016)]



~ region of enhanced fluctuations

What is the CP signal amplitude?

What if it is shadowed by trivial fluctuations?

Proper measures are required

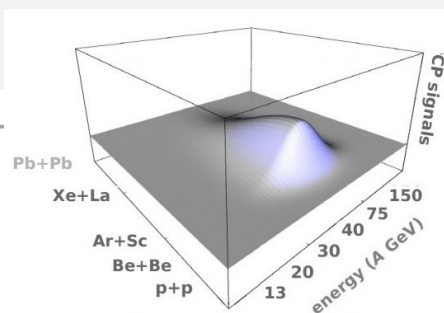
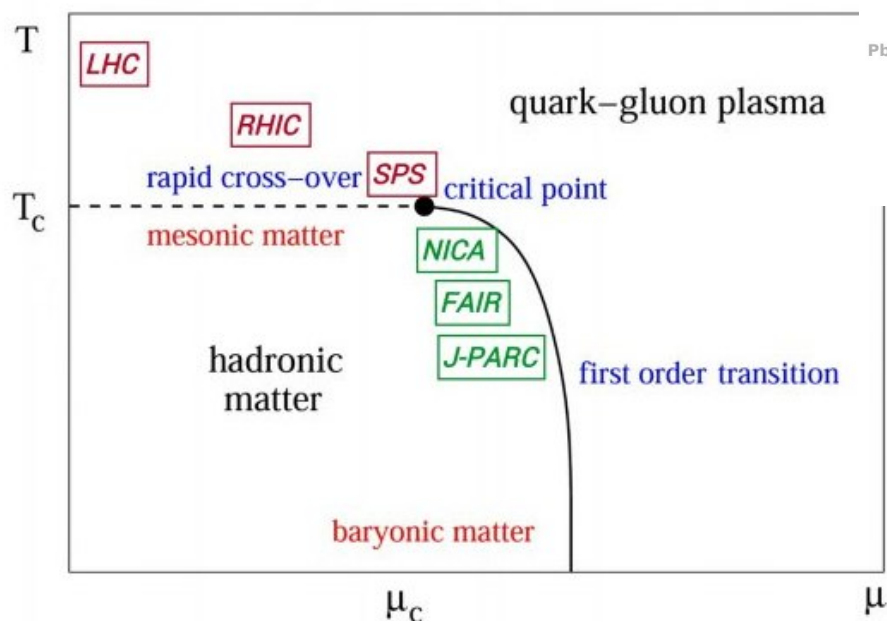
Baseline: construct quantities with the trivial properties in the reference models

+

More sensitivity

Scan in system size and beam energy → search for the **critical point**

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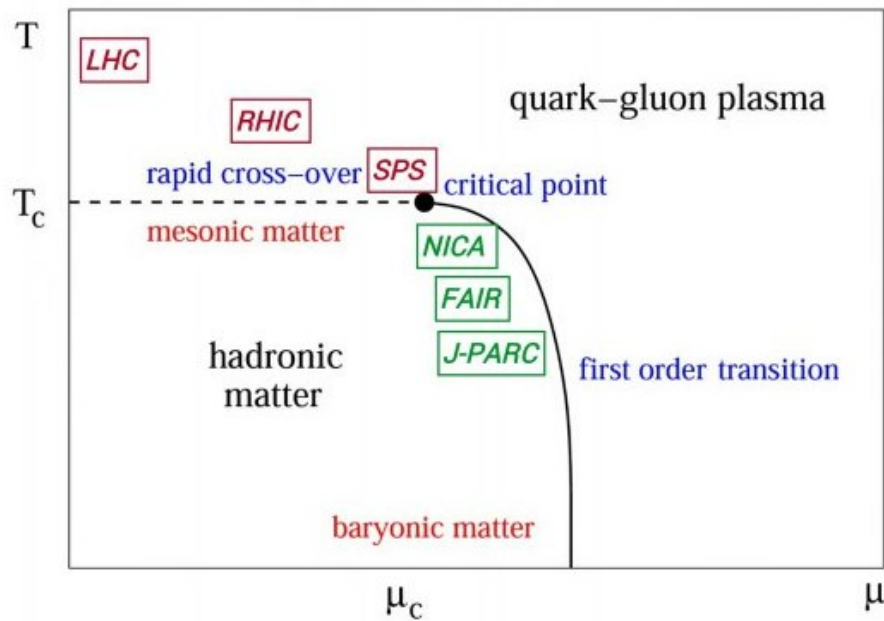
+

Exclude the impact of trivial (volume) fluctuations

Scan in system size and beam energy → search for the **critical point**

~ region of enhanced fluctuations

[Gazdzicki, M., Seyboth, P. *Acta Phys. Pol. B* 47, 1201 (2016)]

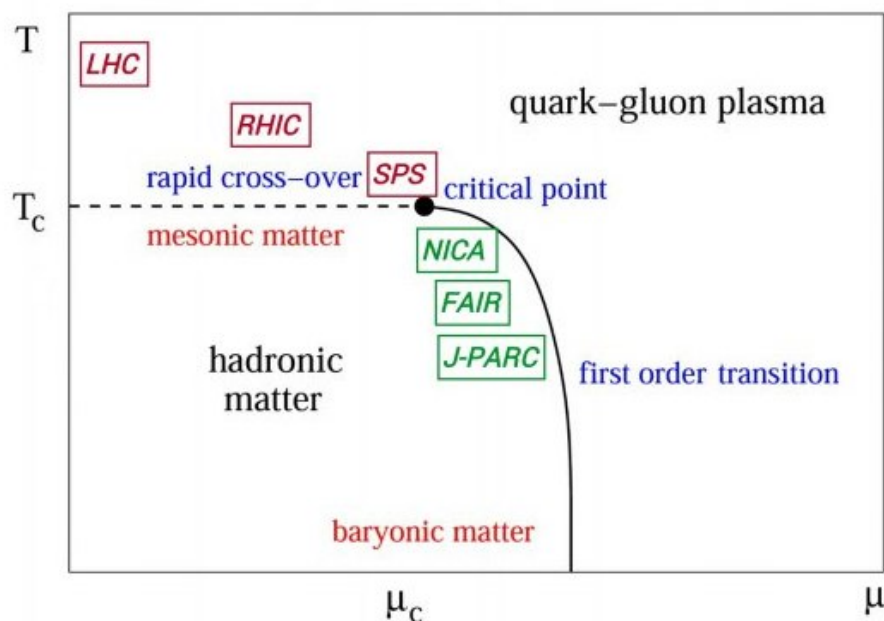


Strongly intensive quantities: are independent both on the volume and the event-by-event fluctuations of the volume in statistical model of the ideal Boltzmann gas in the grand canonical ensemble

Scan in system size and beam energy → search for the **critical point**

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[Gazdzicki, M., Seyboth, P. *Acta Phys. Pol. B* 47, 1201 (2016)]



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[Gazdzicki et al. PRC 88:024907]

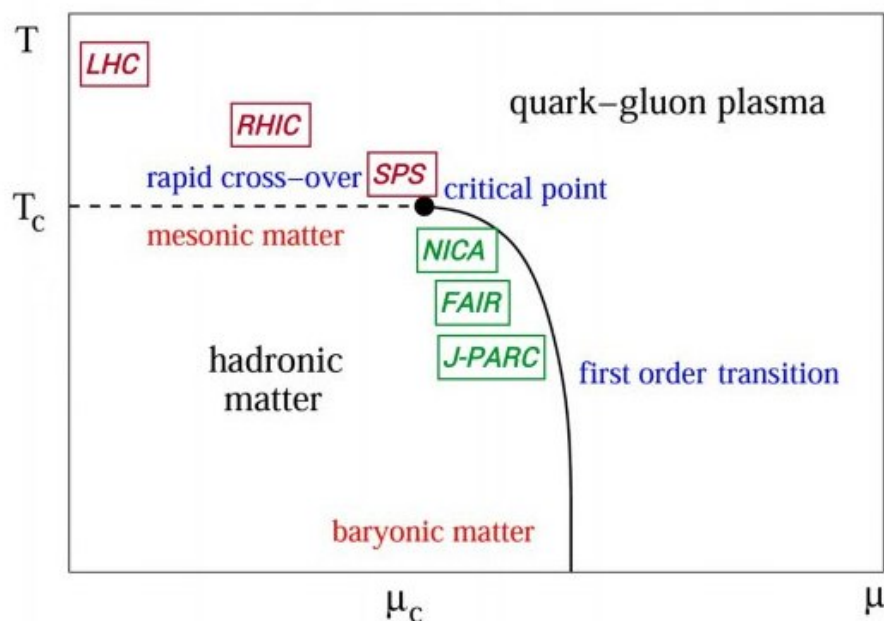
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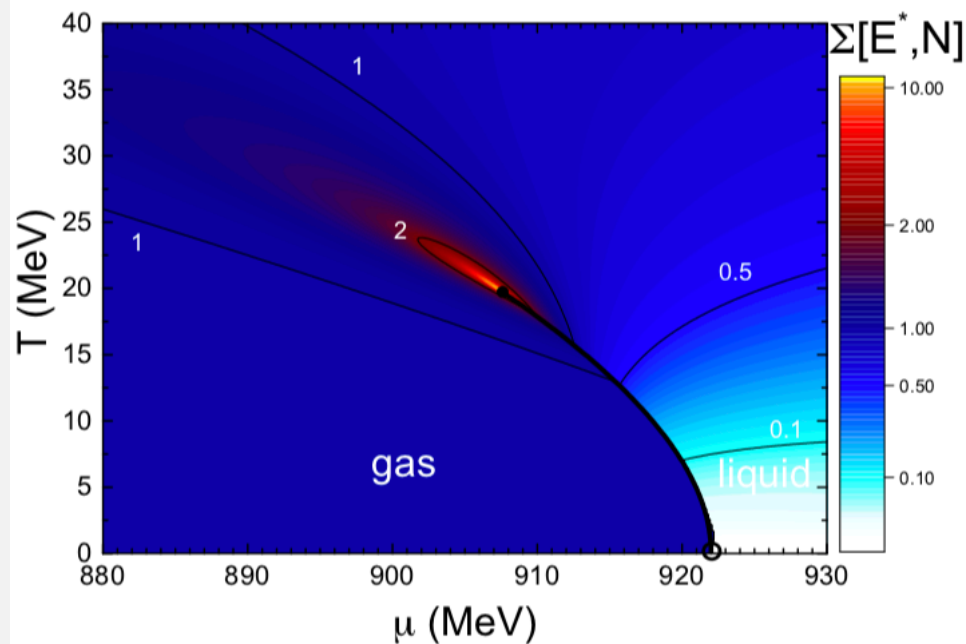
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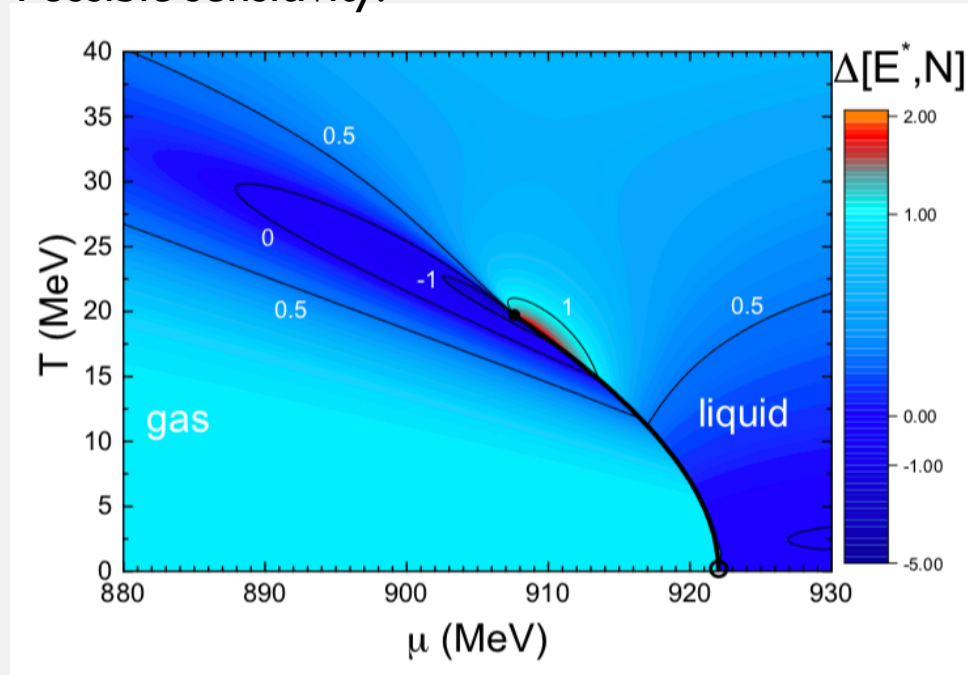
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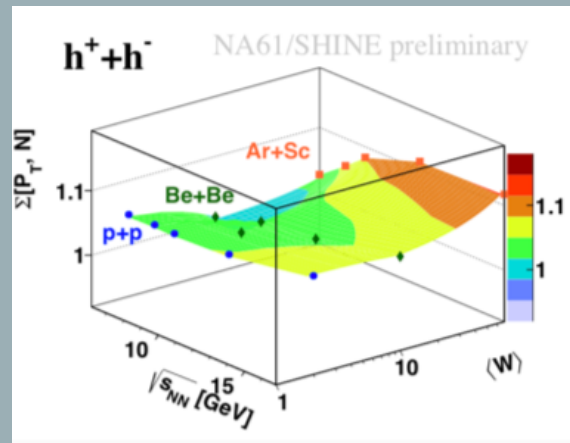
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SOME NA61/SHINE RESULTS

Moments of **negatively charged hadrons** distribution

$$\omega[h^-] = 1$$

$$S\sigma[h^-] = 1$$

$$\kappa\sigma^2[h^-] = 1$$

$$\omega[h^-] = 0$$

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Moments of **negatively charged hadrons** distribution

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Moments of **net charge** distribution ($h^+ - h^-$)

REFERENCE VALUES

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Scellam distribution - works if h^+ and h^- are distributed according to independent Poisson distributions

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$$\begin{aligned}\omega[h^+ - h^-] &= (\mu_+ + \mu_-)/(\mu_+ - \mu_-) \\ S\sigma[h^+ - h^-] &= (\mu_+ - \mu_-)/(\mu_+ + \mu_-) \\ \kappa\sigma^2[h^+ - h^-] &= 1\end{aligned}$$

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simple reference
(a single number)

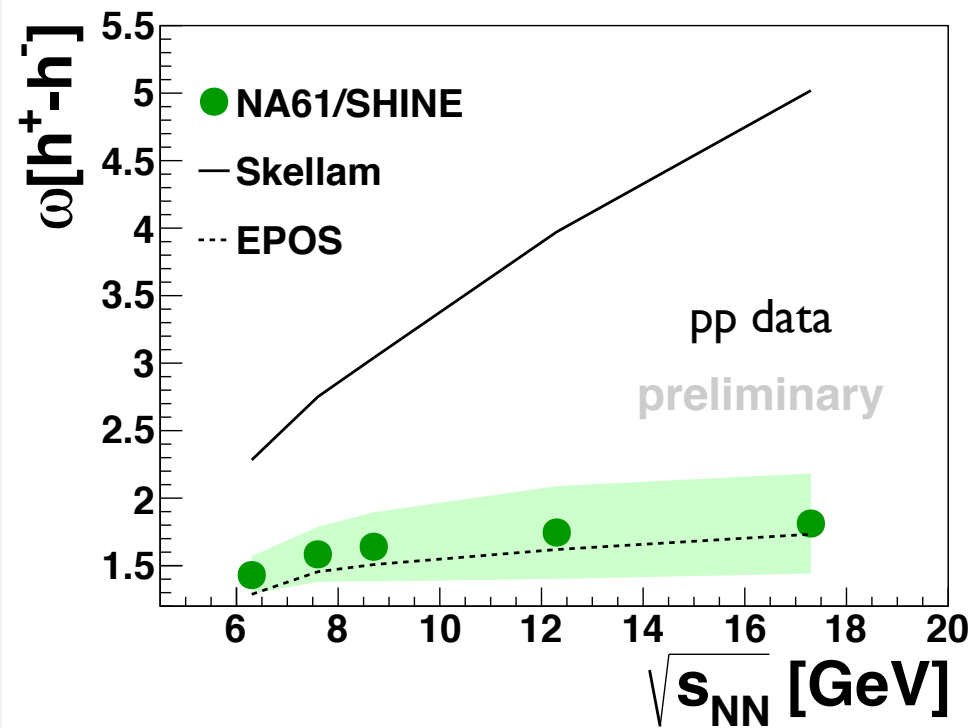
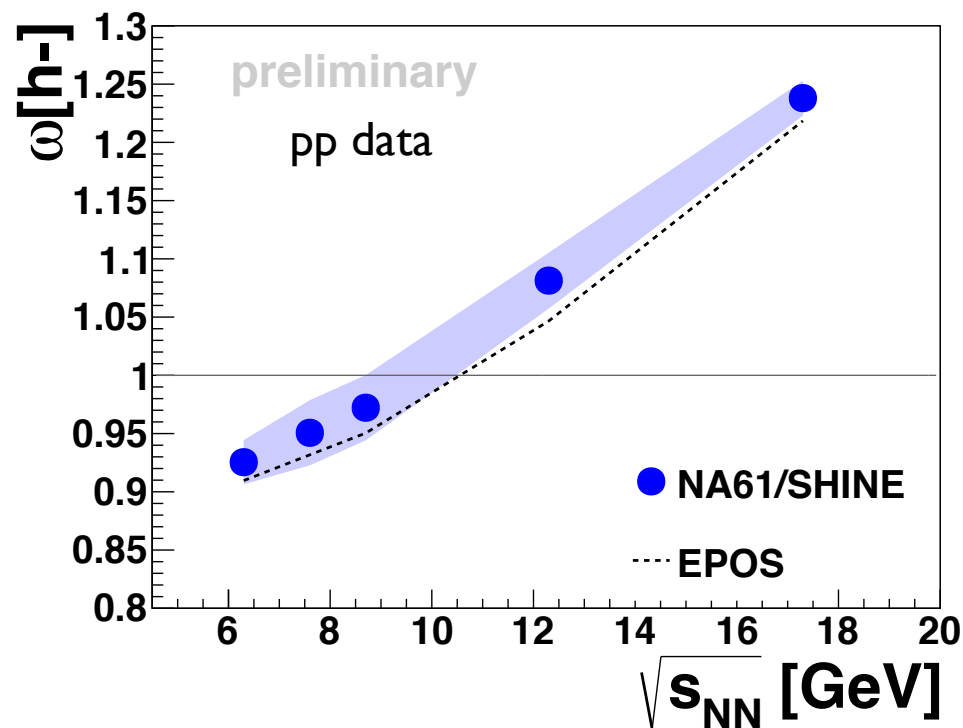
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complicated one
(depends on mean values)

SOME NA61/SHINE RESULTS: SCALED VARIANCE

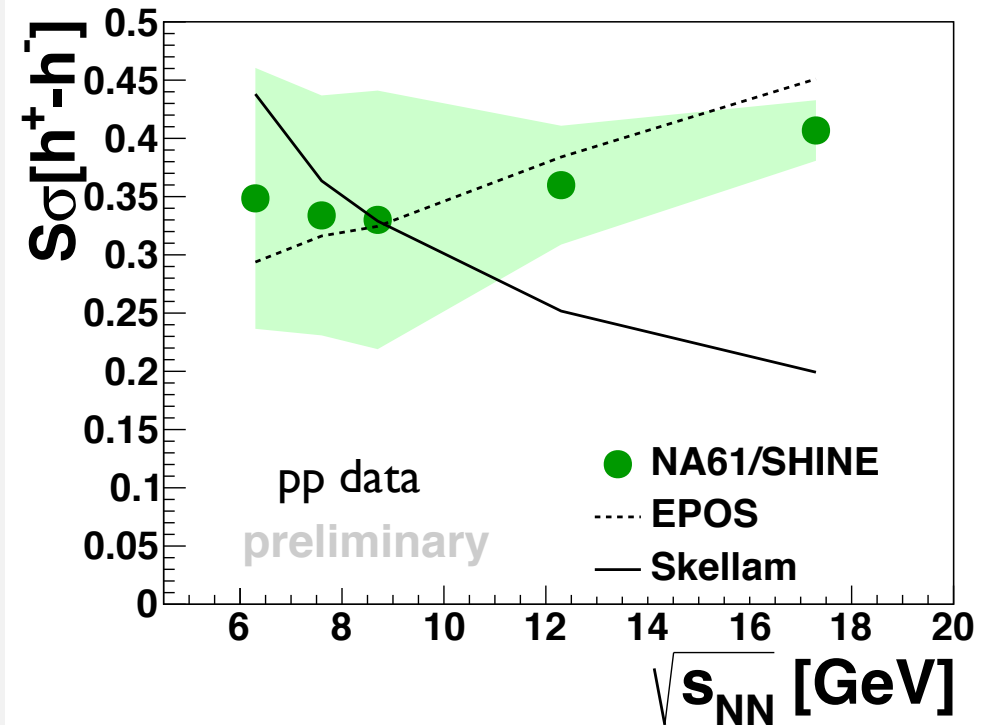
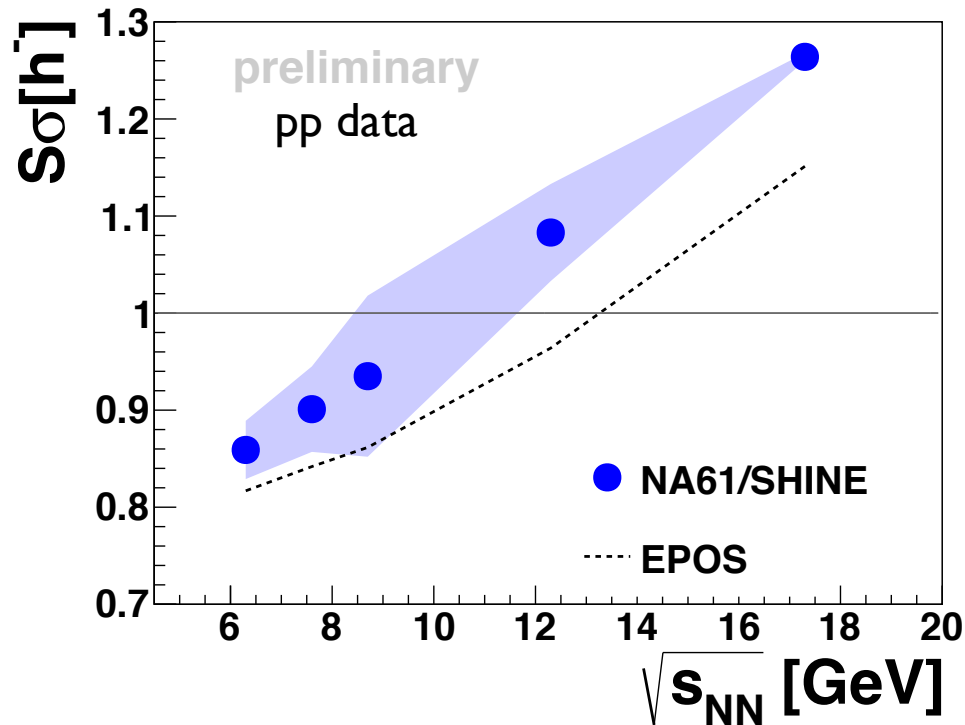


Reference lines:

$\omega[h^-] = 1$ for independent particle production (Poisson)
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Scellam distribution works if h^+ and h^- are distributed
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SOME NA61/SHINE RESULTS: SKEWNESS

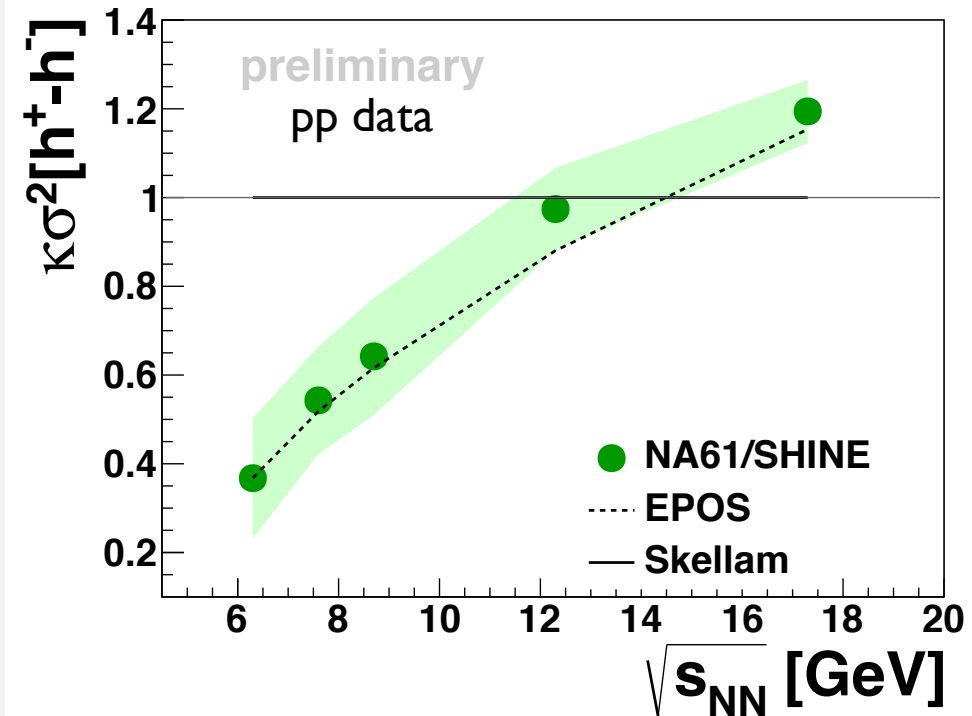
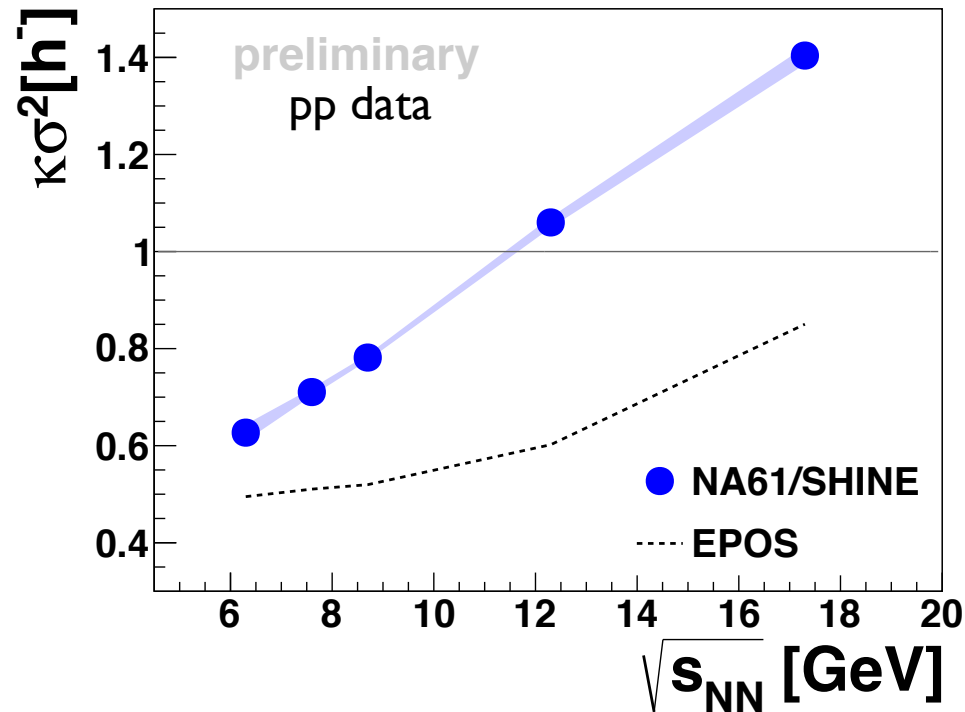


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SOME NA61/SHINE RESULTS: KURTOSIS



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Scellam distribution works if h^+ and h^- are distributed according to independent Poisson distributions

SOME NA61/SHINE RESULTS: SIQ

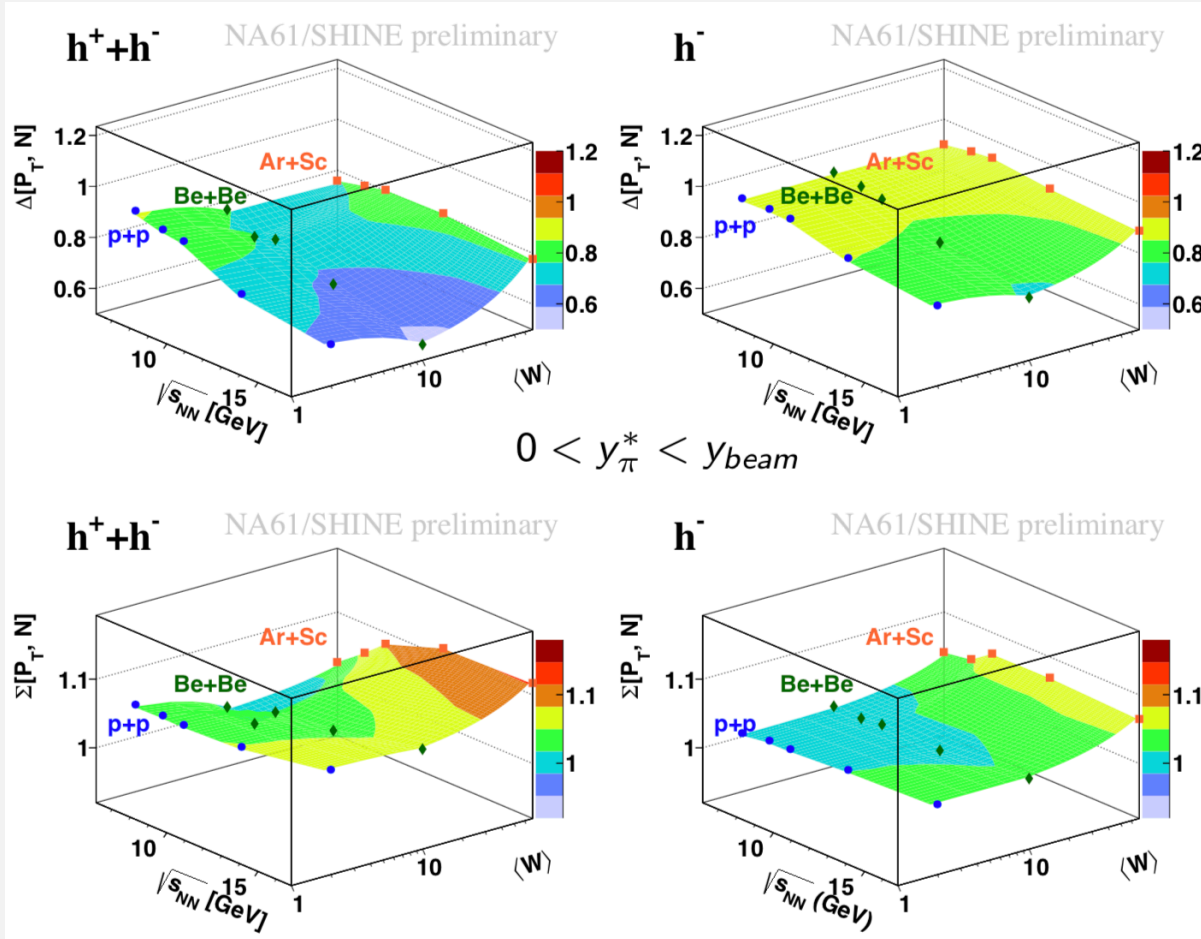
Strongly intensive quantities

$$\Sigma[P_T, N] = \frac{1}{C_\Sigma} [\langle N \rangle \omega[P_T] + \langle P_T \rangle \omega[N] - 2 \cdot (\langle P_T \cdot N \rangle - \langle P_T \rangle \langle N \rangle)]$$

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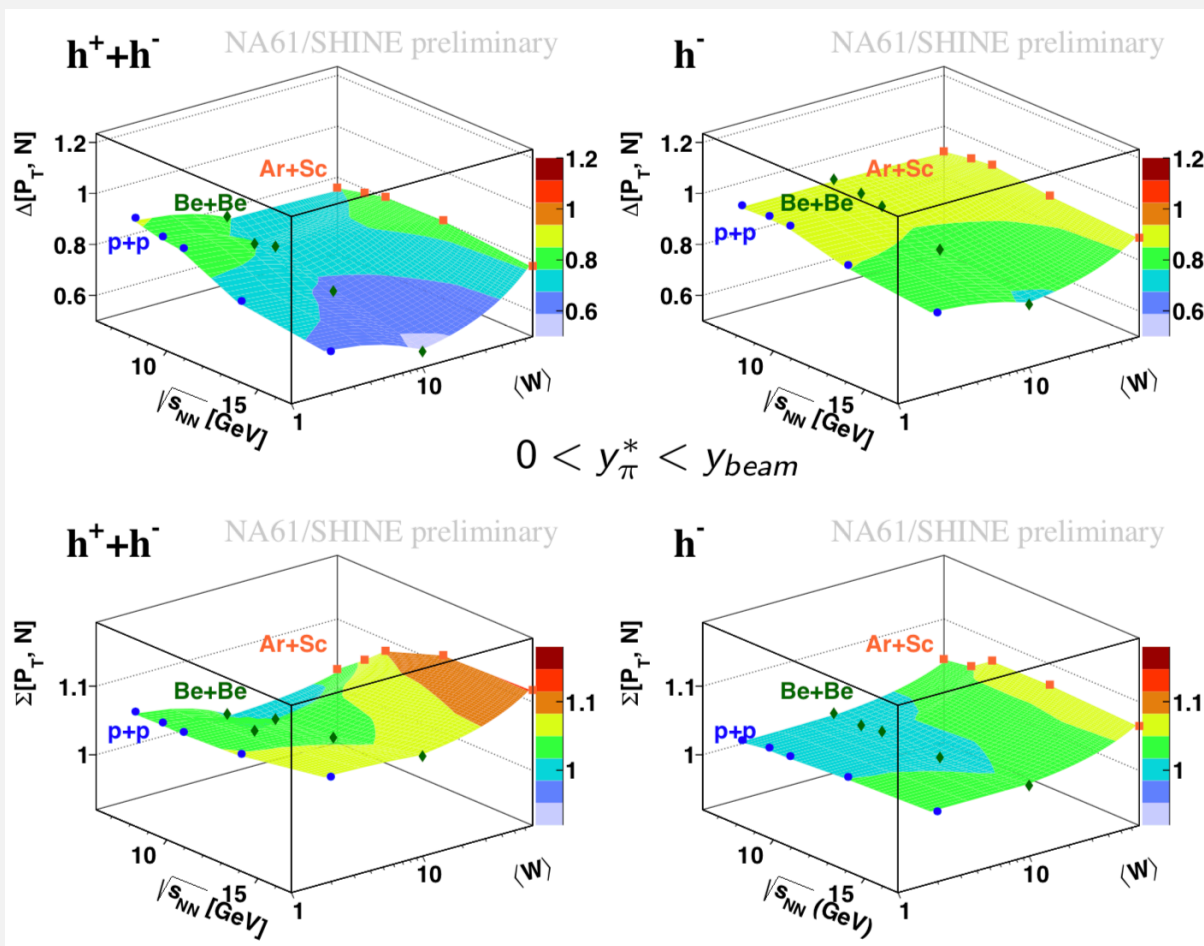


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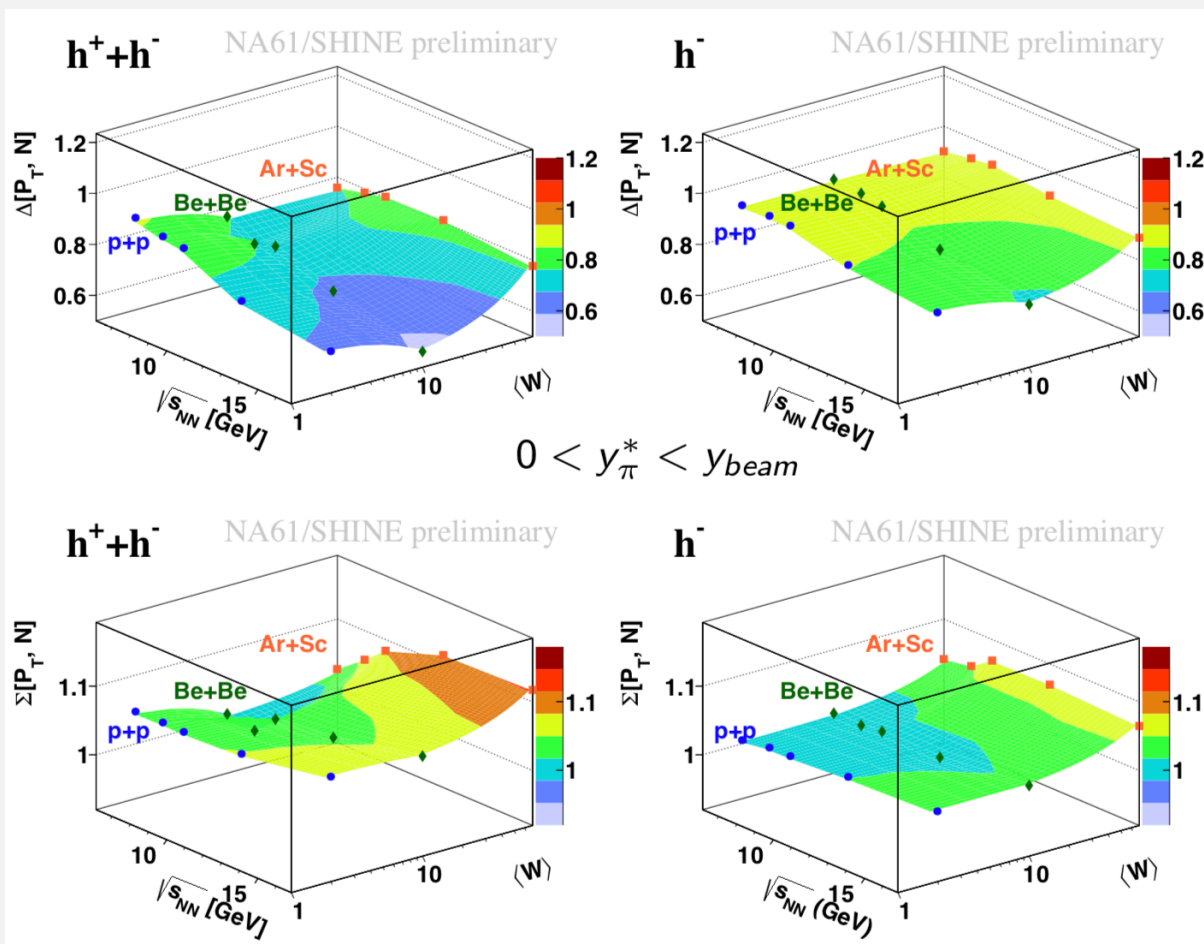
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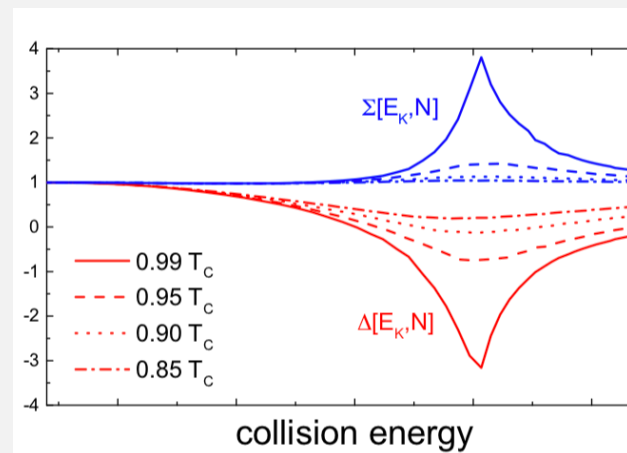
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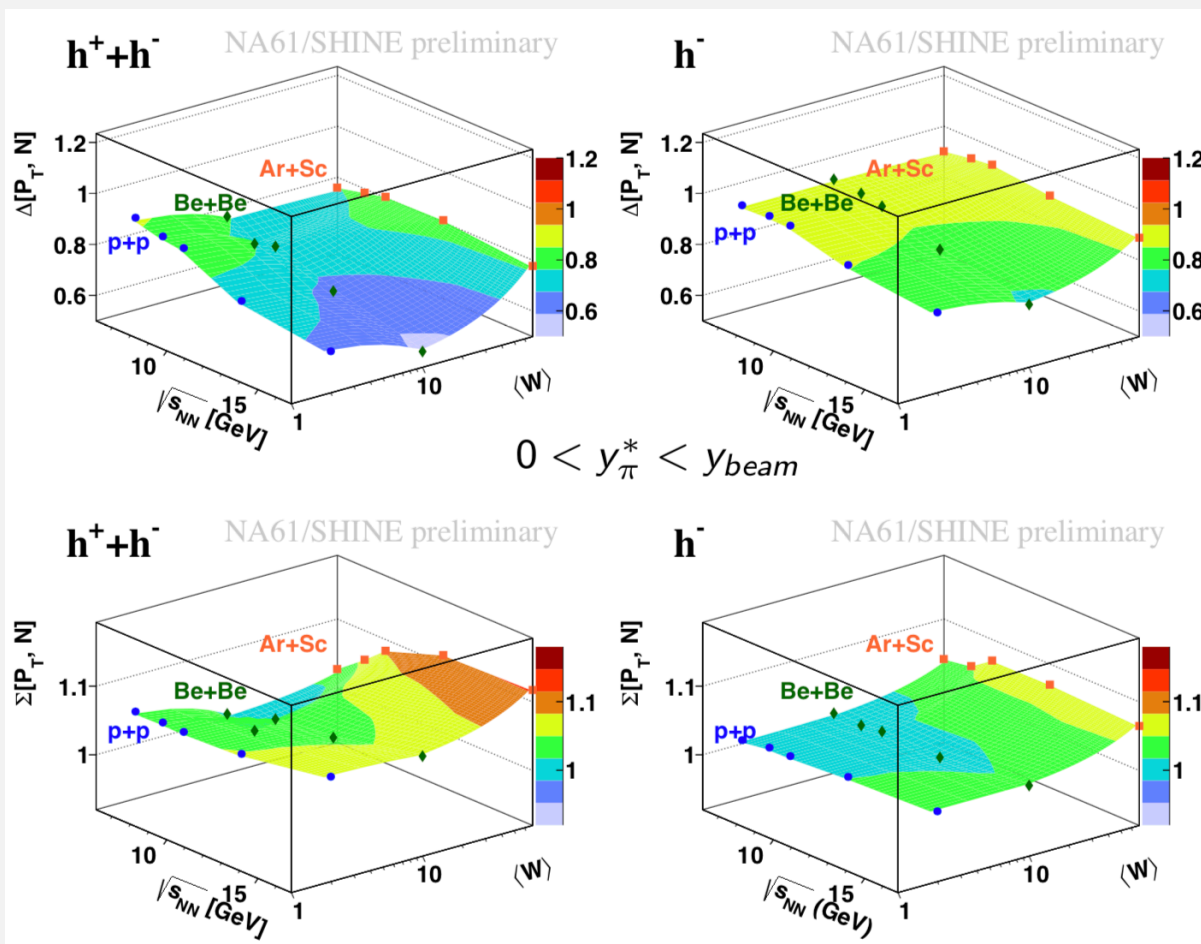


Nucleon system with van der Waals EOS in GCE formulation in the vicinity of the Critical Point

[Vovchenko, Gorenstein, Stoecker, PRL 118: 182301,
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SOME NA61/SHINE RESULTS: SIQ

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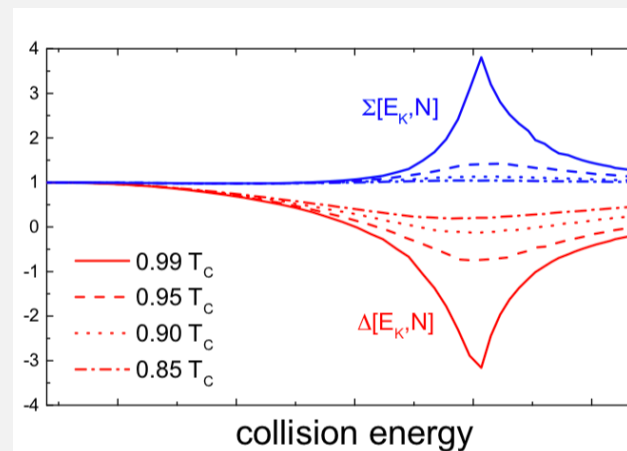


[Andronov, Acta Phys. Pol. B Proc. Suppl. 10 449]

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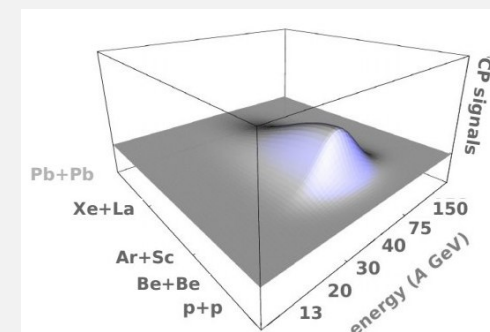
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Naive sketch

[Gazdzicki, M., Seyboth, P.
 Acta Phys. Pol. B 47, 1201 (2016)]

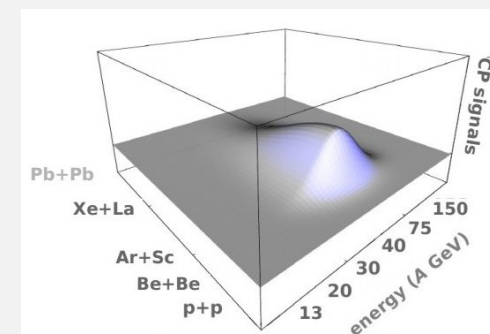
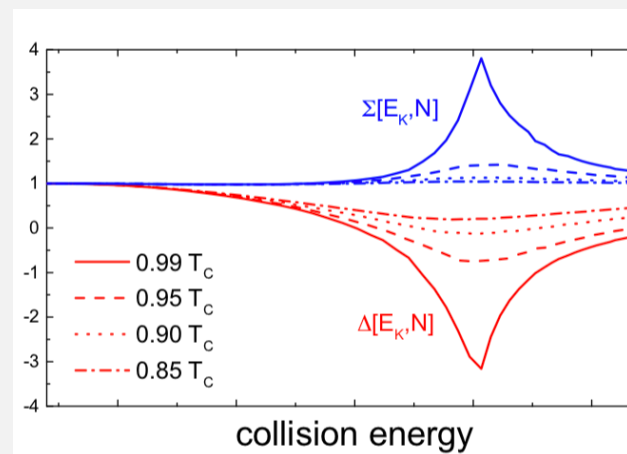
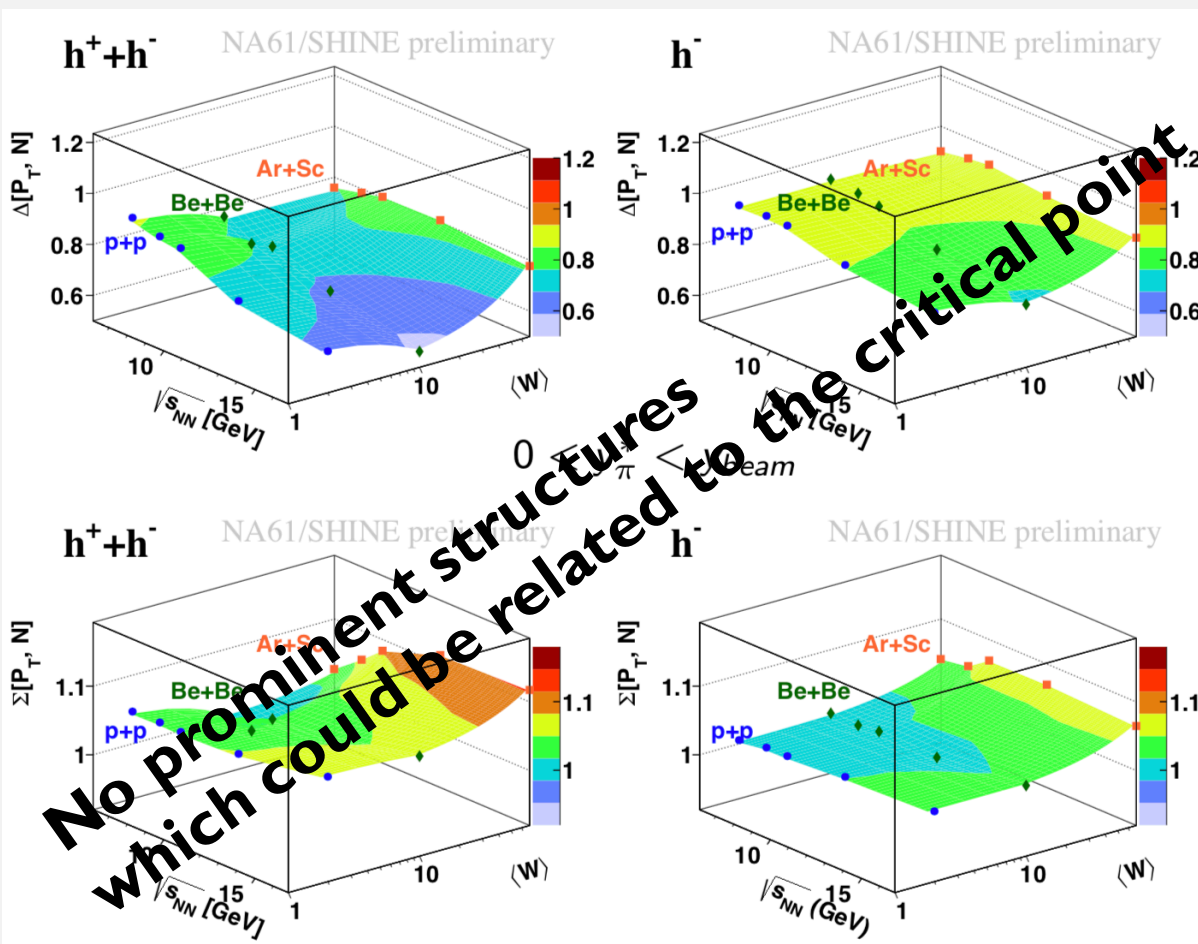
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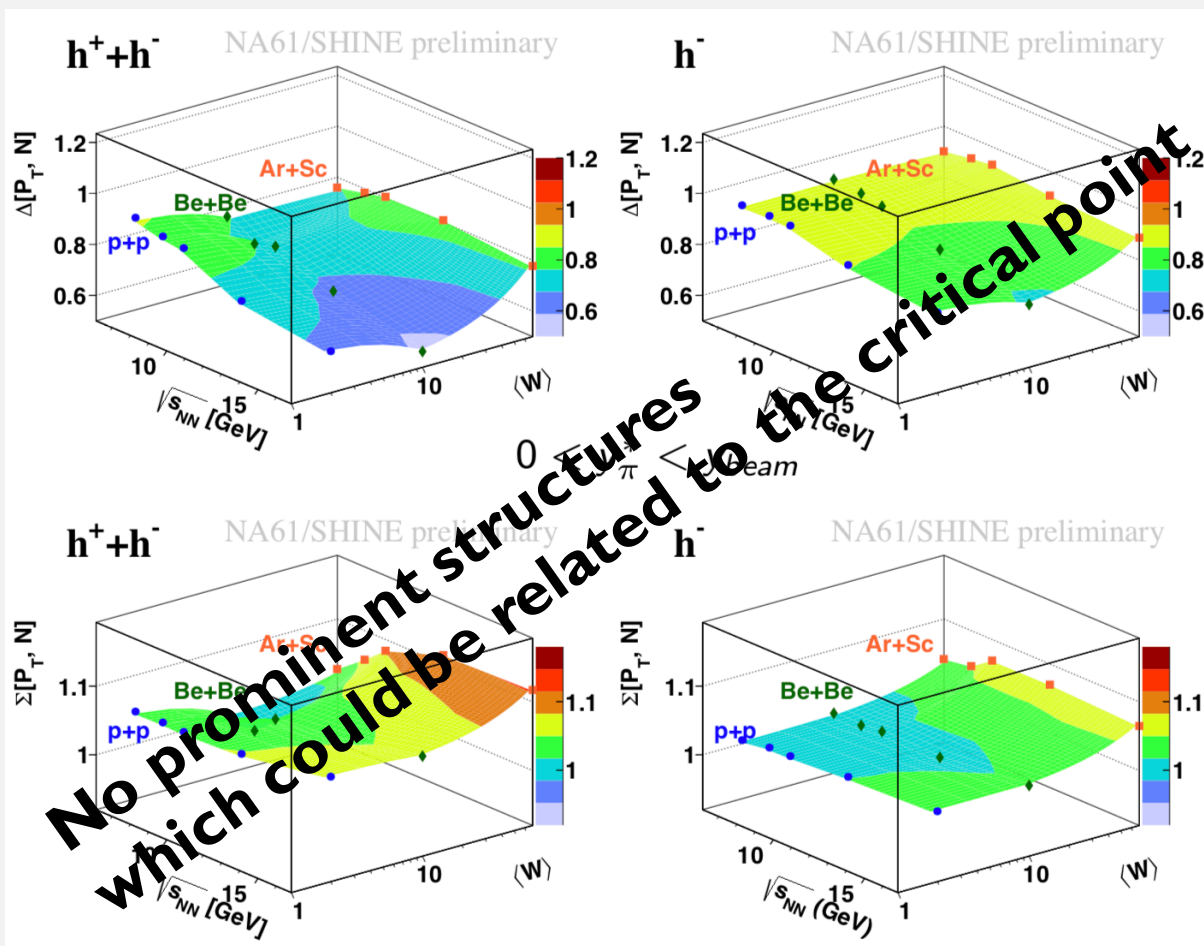


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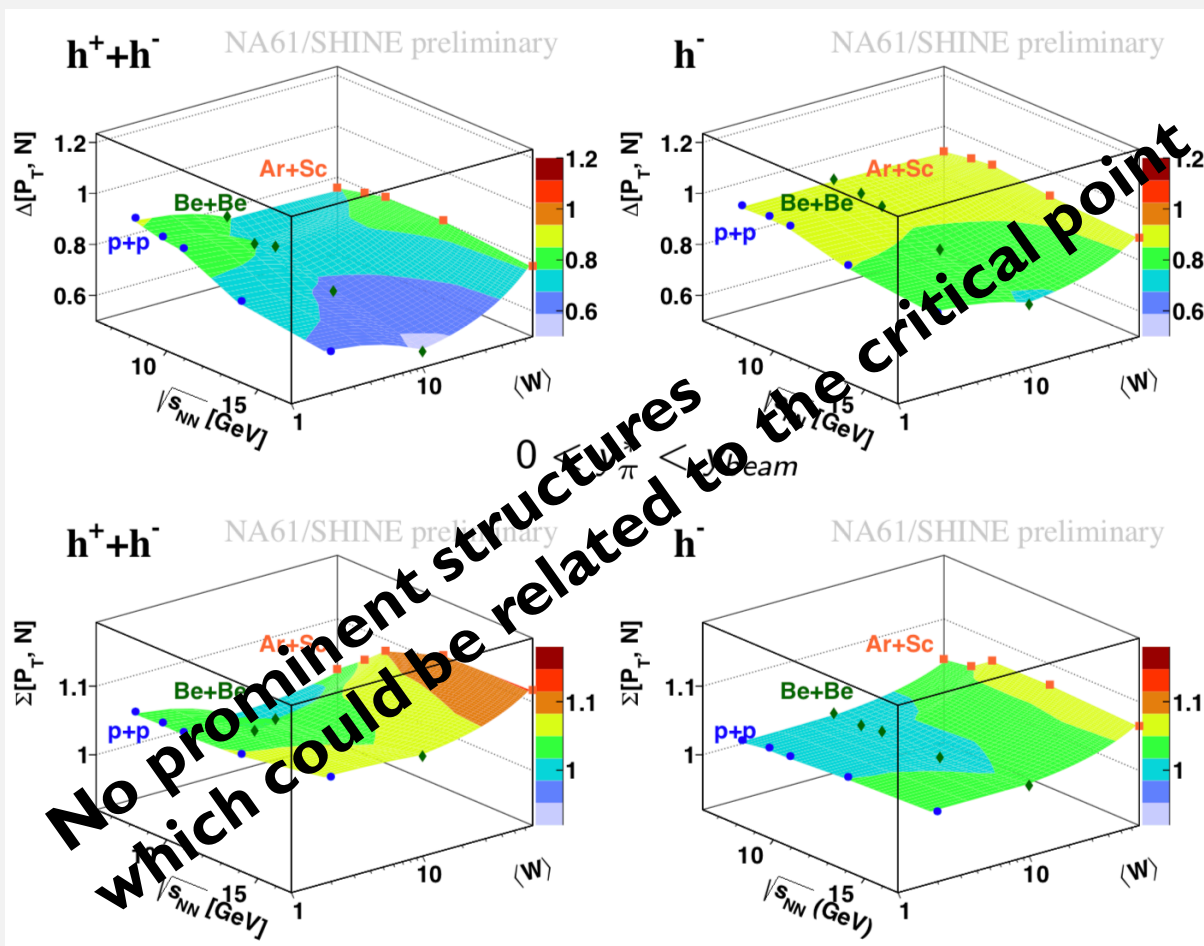
[Vovchenko, Gorenstein, Stoecker, PRL 118: 182301, Vovchenko, et al., JPA 48: 305001]

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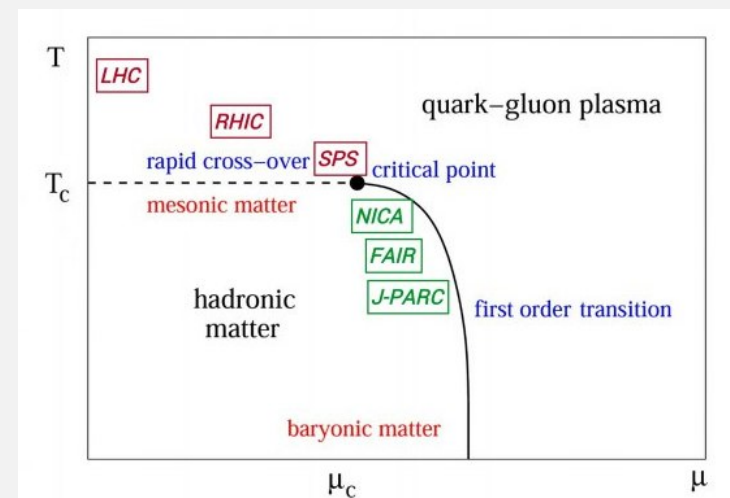
Additional possible analysis: choice of a phase space



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Each rapidity is associated with a different value of μ and therefore **probes a different part of the $(\mu-T)$ phase diagram**

Becattini F, Manninen J and Gazdzicki M PRC 73 044905

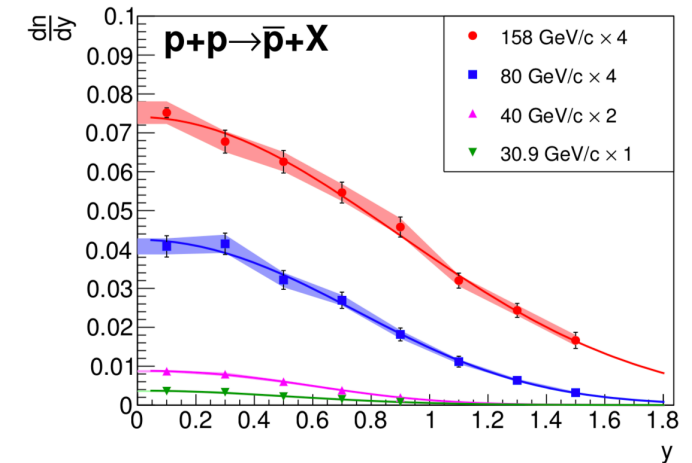
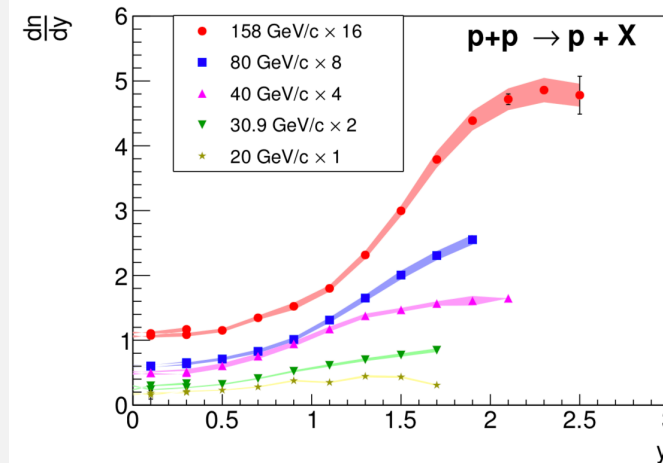


[Gazdzicki, M., Seyboth, P. *Acta Phys. Pol. B* 47, 1201 (2016)]

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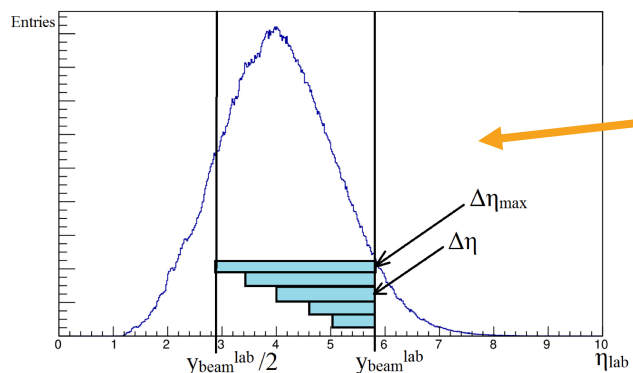
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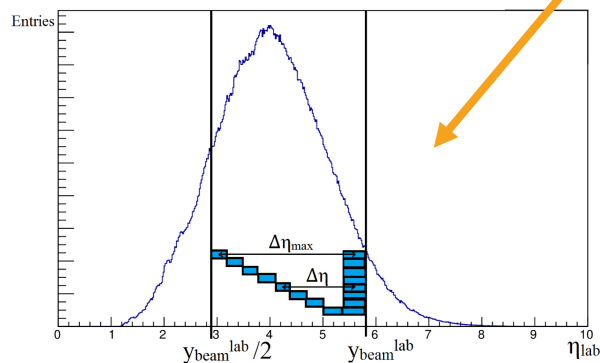


[NA61, EPJ C 77 10:671]

Moreover, the ratio of p and \bar{p} changes significantly with rapidity in inelastic $p + p$ at the SPS energies



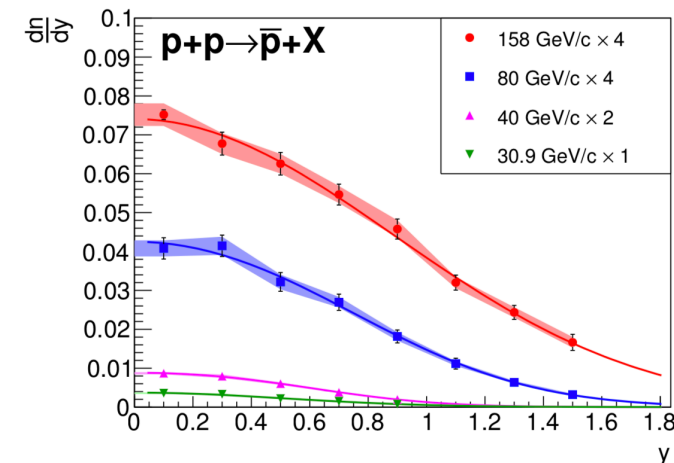
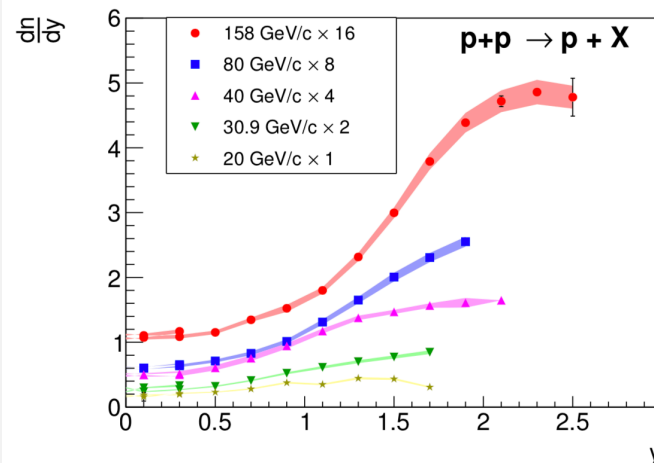
[D. Prokhorova, KnE Energ. Phys. 3 (2018) 217–225]



Additional possible analysis: choice of a phase space

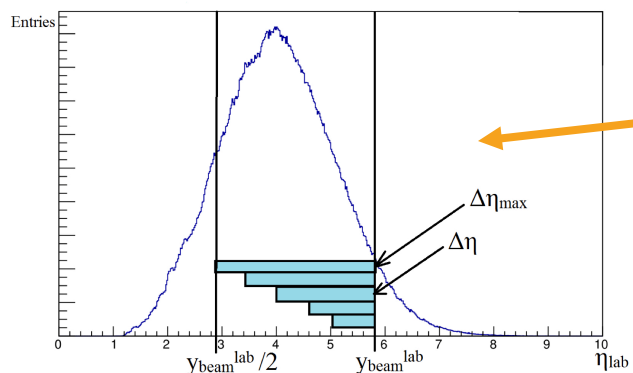
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[Becattini F, Manninen J and Gazdzicki M PRC 73 044905]

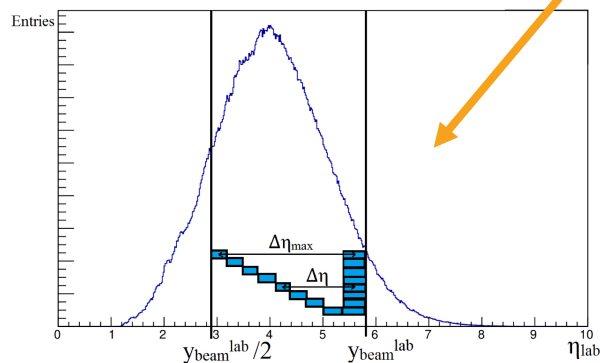


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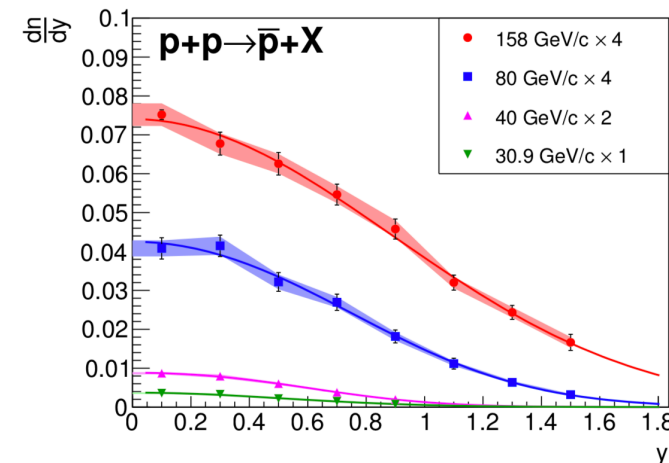
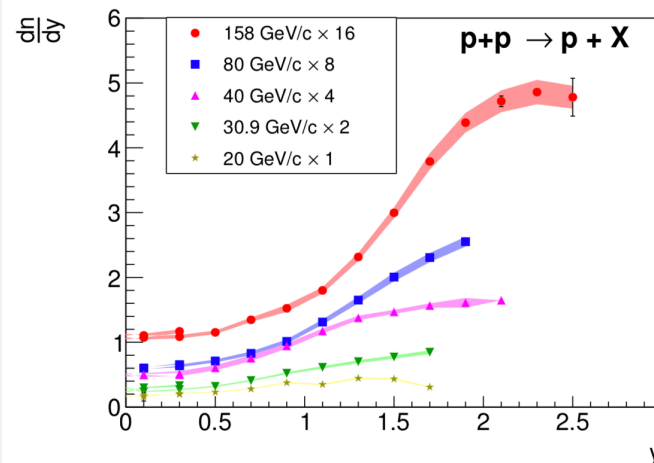


In this case we also probe the short- and long-range correlations and access the information about particle sources

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FLUCTUATION STUDIES WITH PSEUDORAPIDITY

Strongly intensive variables defined in two kinematically separated regions

$$\Sigma[N_F, N_B] = \frac{1}{C_\Sigma} [\langle N_B \rangle \omega[N_F] + \langle N_F \rangle \omega[N_B] - 2 \cdot (\langle N_F \cdot N_B \rangle - \langle N_F \rangle \langle N_B \rangle)]$$

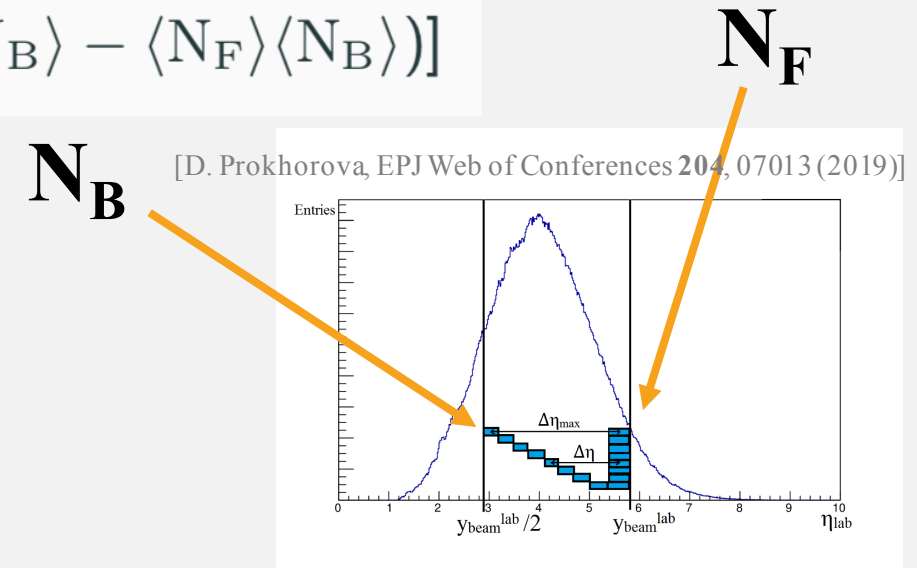
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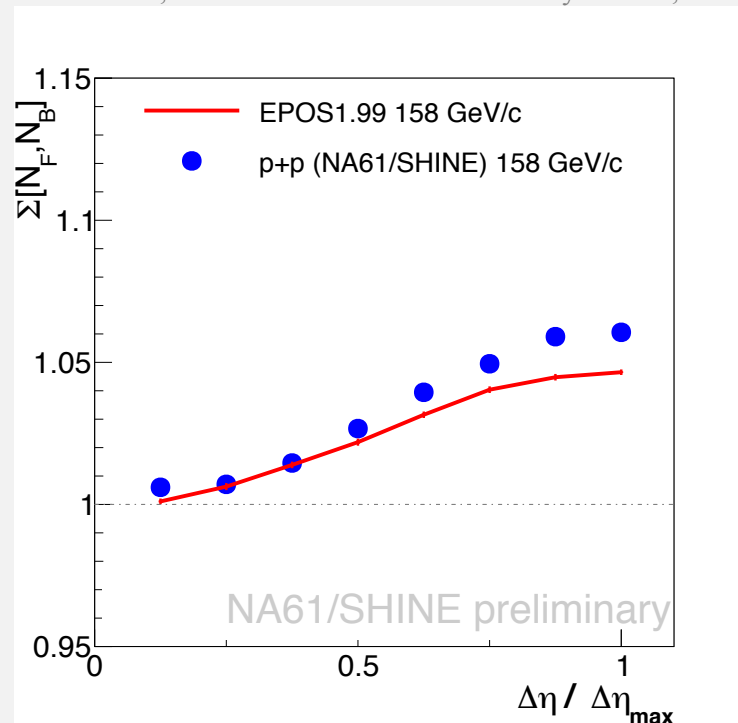


uncorrected rapidity distribution of all charged hadrons produced in p + p @158 GeV/c in NA61/SHINE experimental acceptance

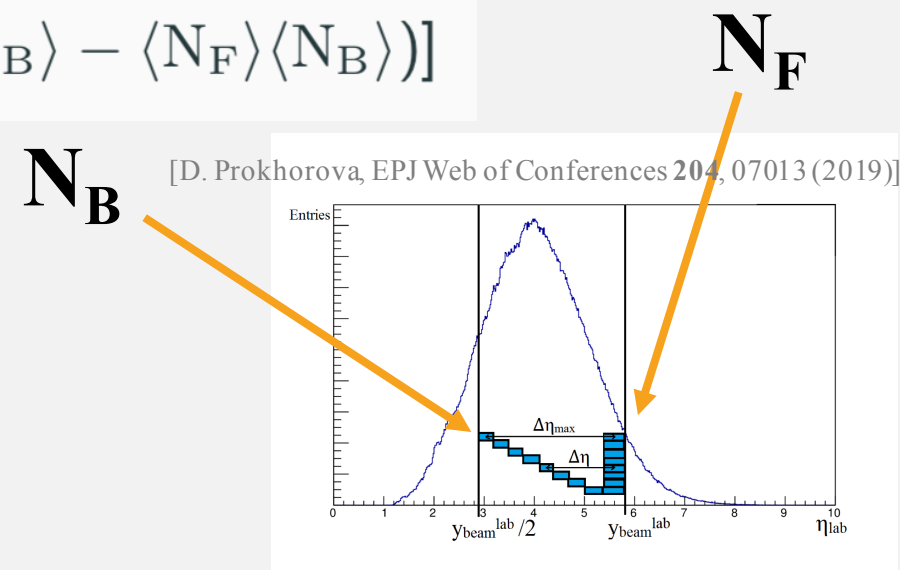
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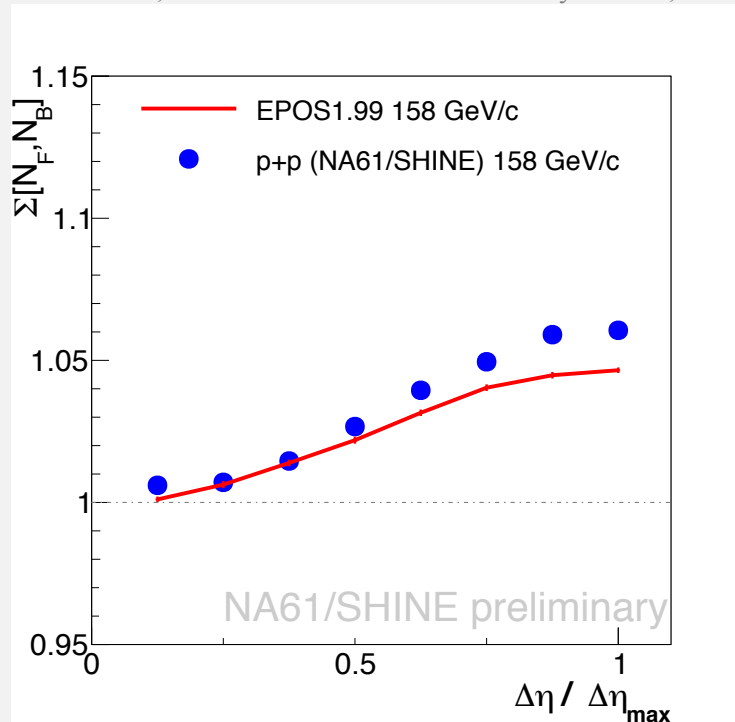


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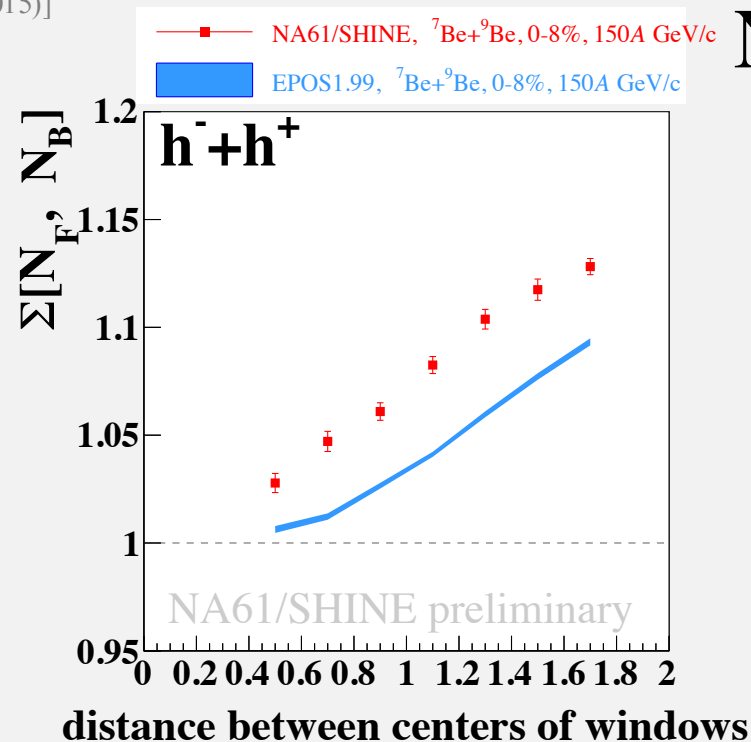
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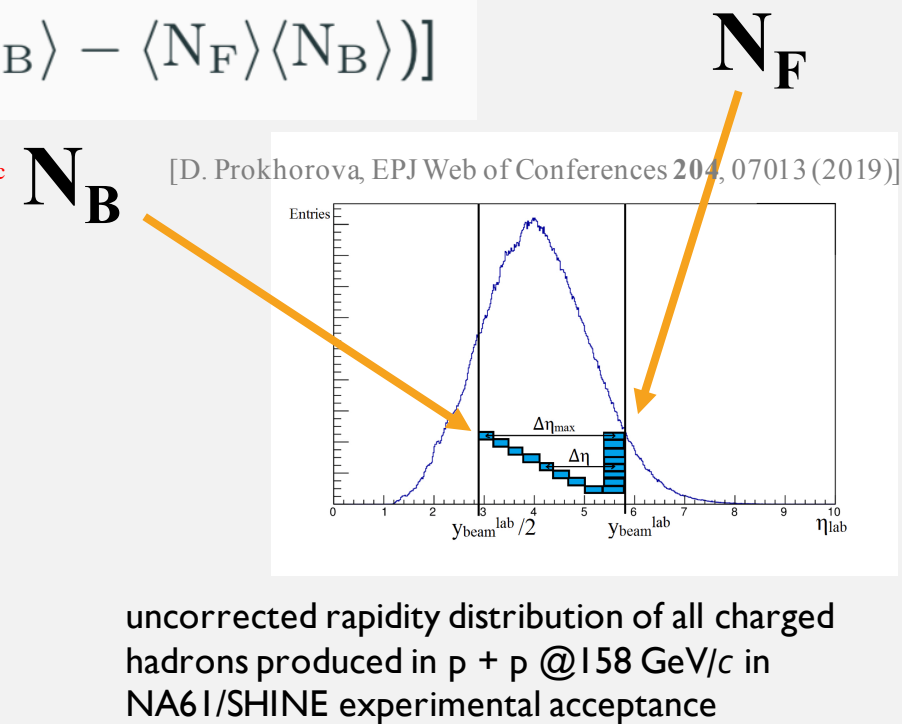
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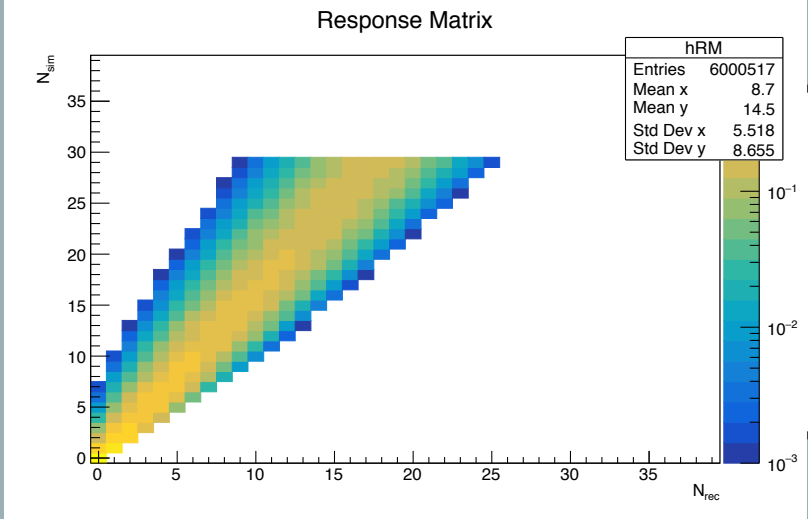


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RESULTS CORRECTIONS

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Issues— detector inefficiencies:

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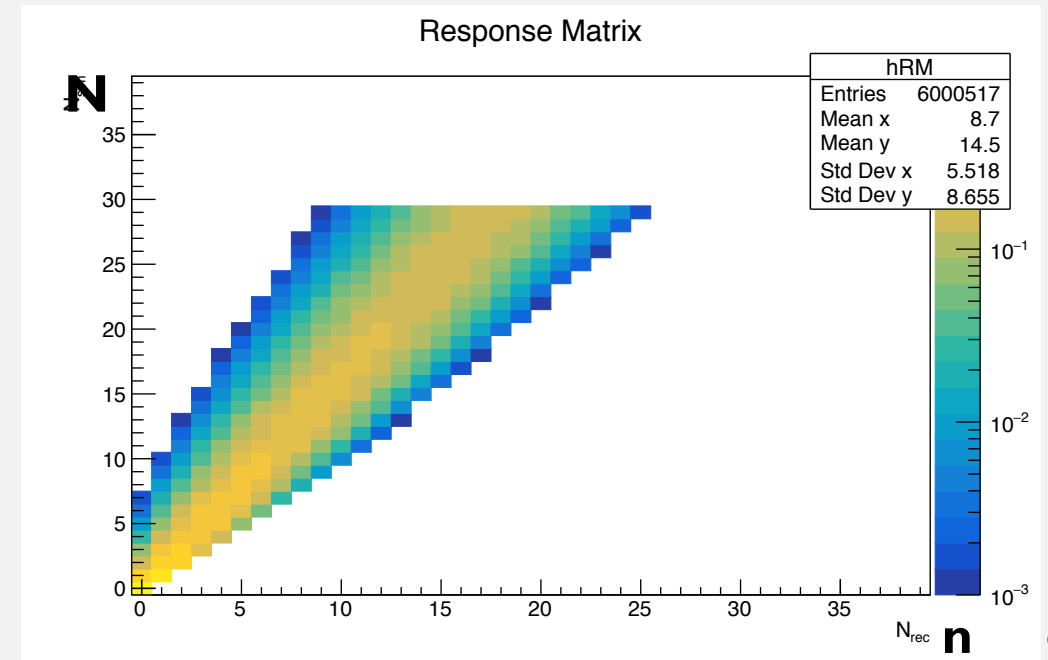
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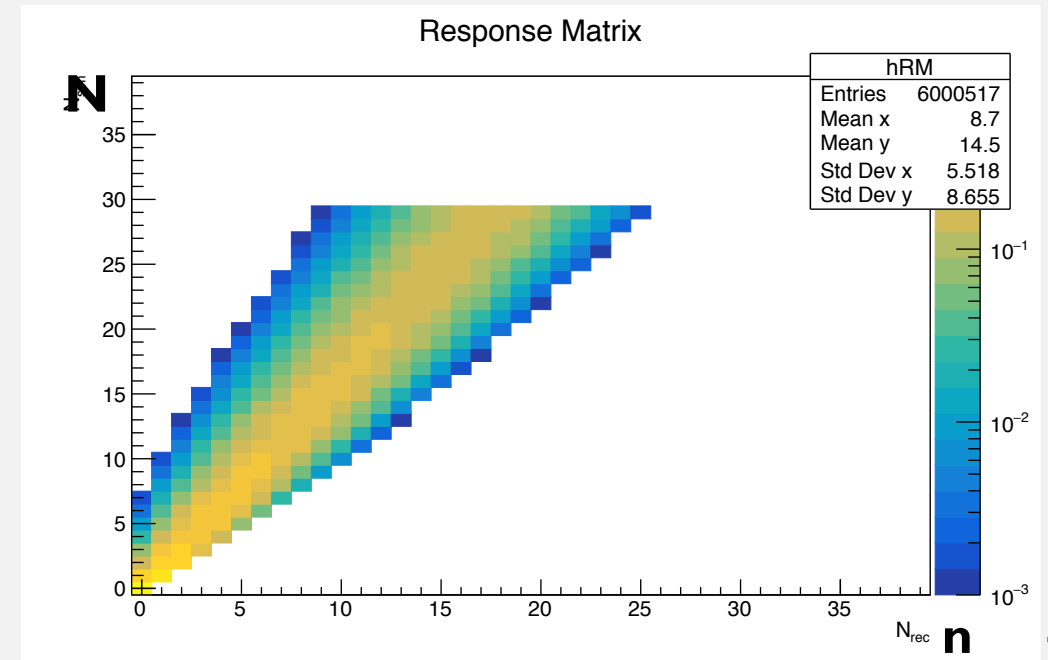
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- Event losses are considered in the Response Matrix normalization



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CONCLUSION

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The detailed analysis of the accumulated experimental data is continued. **Stay tuned!**

NA61/SHINE Collaboration Meeting at St. Petersburg, 2018



Have a SHINY day!

THANK YOU FOR YOUR ATTENTION



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