

Primordial gravitational waves

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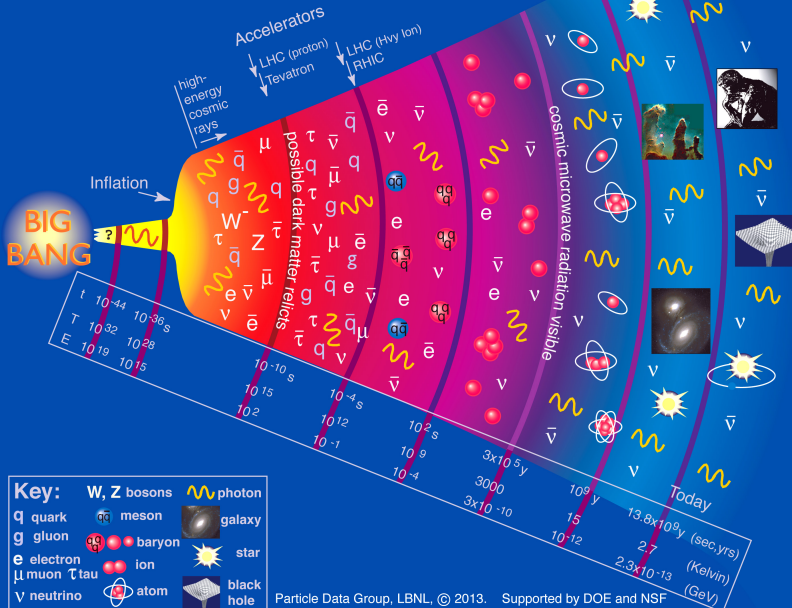
Based on:

J. Ellis, ML, J. M. No, V Vaskonen arXiv:1903.09642

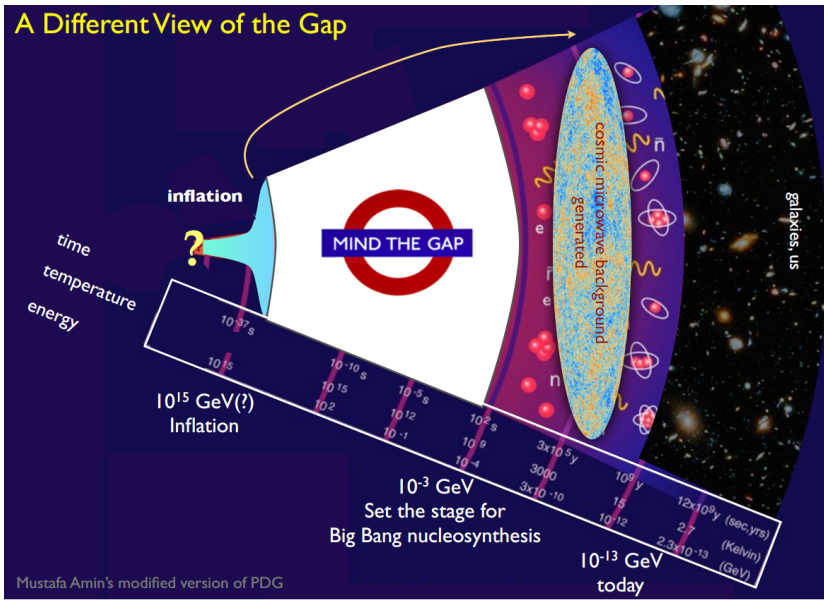
J. Ellis, ML, J. M. No arXiv:1809.08242

Y. Cui, D. Morrissey, ML and J. D. Wells. arXiv:1711.03104, arXiv:1808.08968

History of the Universe



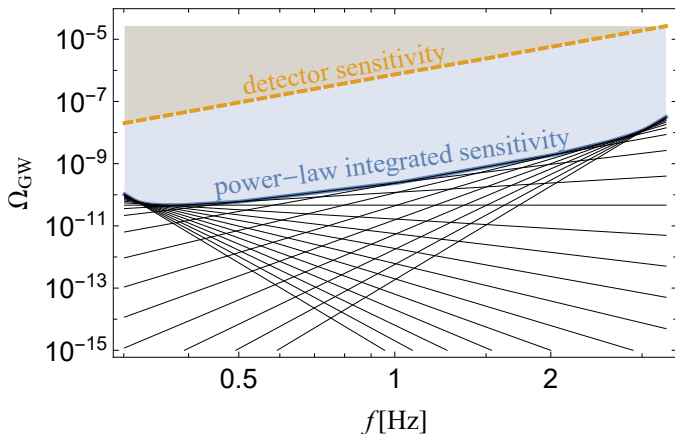
A Different View of the Gap

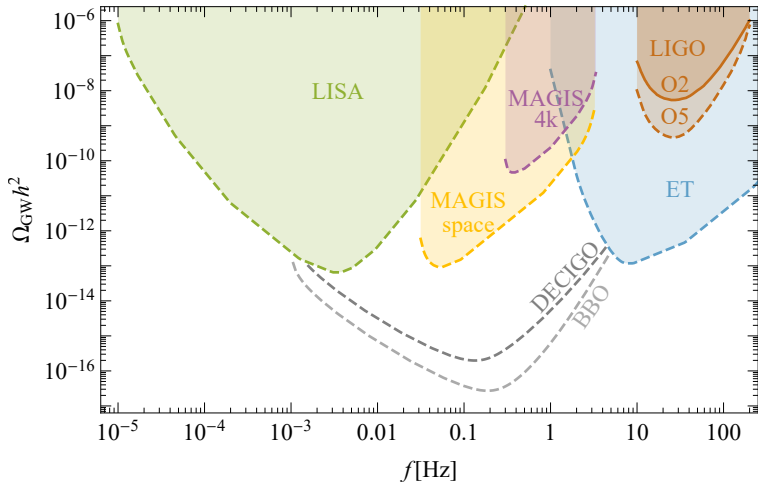


Mustafa Amin's modified version of PDG

Power-law integrated sensitivity

$$\Omega_{\text{GW}} = \frac{2\pi}{3} \frac{f^3 S_h^2}{H_0^2}, \quad \text{SNR} = \sqrt{\tau \int df \left(\frac{\Omega_{\text{GW}}^{\text{signal}}}{\Omega_{\text{GW}}^{\text{noise}}} \right)^2}$$





phase transition dynamics

Bubble: static field configuration passing the barrier (excited through thermal fluctuations)

- decay rate

$$\Gamma(T) \approx T^4 \exp\left(-\frac{S_3(T)}{T}\right),$$

- $\mathcal{O}(3)$ symmetric action

$$S_3(T) = 4\pi \int dr r^2 \left[\frac{1}{2} \left(\frac{d\phi}{dr} \right)^2 + V(\phi, T) \right].$$

- EOM \rightarrow bubble profile

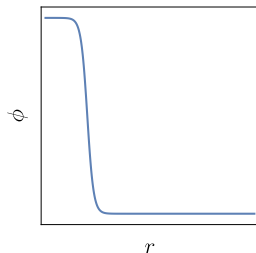
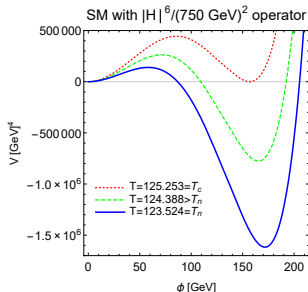
$$\frac{d^2\phi}{dr^2} + \frac{2}{r} \frac{d\phi}{dr} - \frac{\partial V(\phi, T)}{\partial \phi} = 0,$$

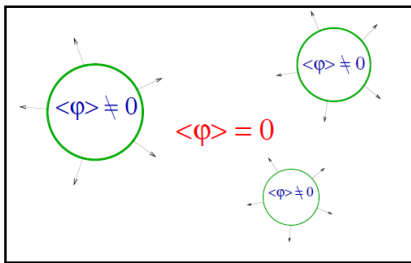
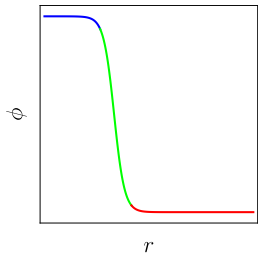
$$\phi(r \rightarrow \infty) = 0 \quad \text{and} \quad \dot{\phi}(r=0) = 0.$$

- nucleation temperature

$$N(T_n) = \int_{t_c}^{t_n} dt \frac{\Gamma(t)}{H(t)^3} = \int_{T_n}^{T_c} \frac{dT}{T} \frac{\Gamma(T)}{H(T)^4} = 1$$

Linde '81 '83





Morrissey '12

Gravitational waves from a PT

- Strength of the transition

$$\alpha \approx \left. \frac{\Delta V}{\rho_R} \right|_{T=T_*}, \quad \Delta V = V_f - V_t$$

- Characteristic scale

$$HR_* = H_* N_b^{-\frac{1}{3}} = H_* \left(\int dt' \left(\frac{a(t')}{a(t)} \right)^3 \Gamma(t') P(t') \right)^{-\frac{1}{3}}$$

- Signals are produced by three main mechanisms:

- collisions of bubble walls: $\Omega_{\text{col}} \propto \left(\frac{\kappa_{\text{col}} \alpha}{\alpha + 1} \right)^2 (HR_*)^2$

Kamionkowski '93, Huber '08, Hindmarsh '18,

- sound waves: $\Omega_{\text{sw}} \propto \left(\frac{\kappa_{\text{sw}} \alpha}{\alpha + 1} \right)^2 HR_* \frac{HR_*}{U_f}$

Hindmarsh '13 '15 '17

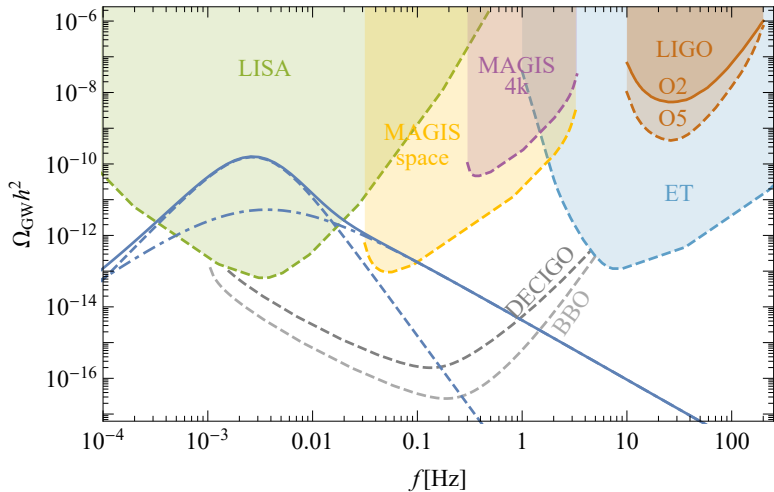
Ellis '18

- turbulence $\Omega_{\text{turb}} \propto \left(\frac{\kappa_{\text{turb}} \alpha}{\alpha + 1} \right)^{\frac{3}{2}} HR_*$

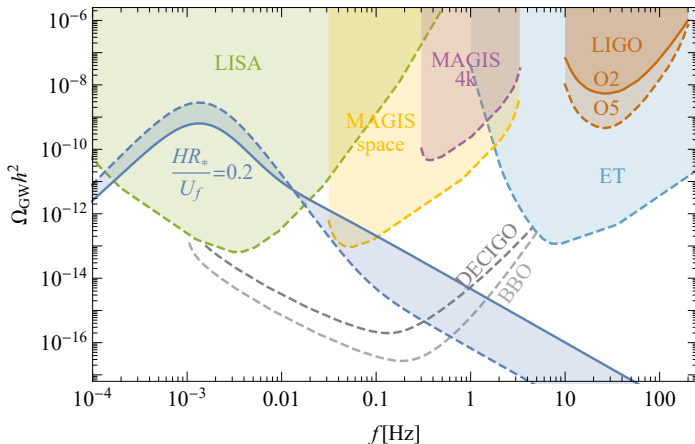
Caprini '09

- The frequency of the signal changes as $f \propto \frac{T_*}{HR_*}$

$$T_* = 100 \text{ GeV}, \alpha = 1, HR_* = 5 \times 10^{-2}$$



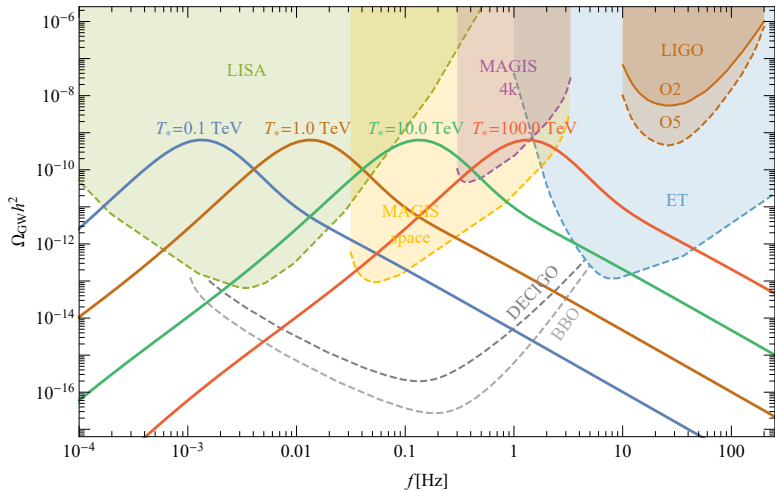
$$T_* = 100 \text{ GeV}, \quad \alpha = 1, \quad HR_* = 10^{-1}$$

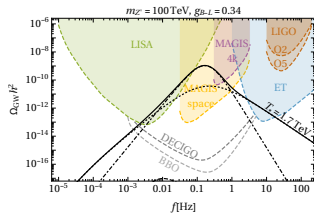
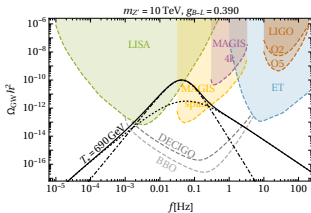
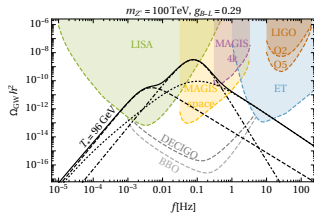
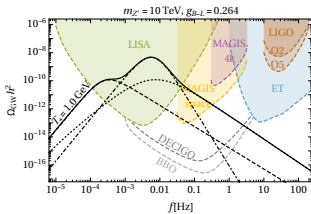
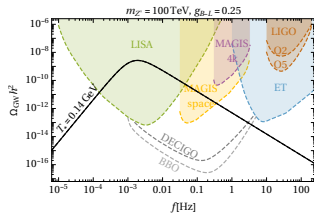
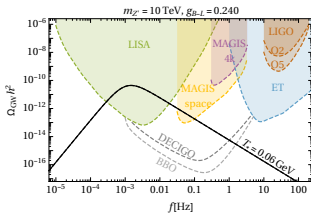


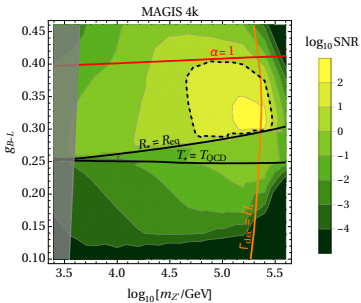
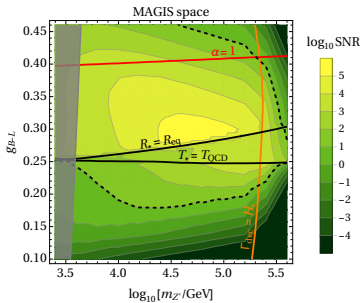
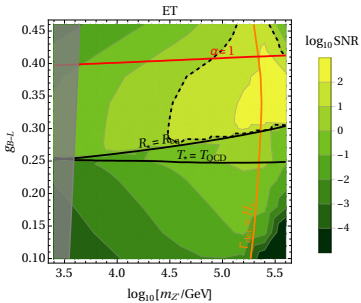
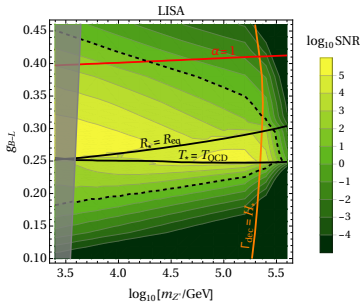
- Root-mean-square four-velocity of the plasma

$$\bar{U}_f \approx \sqrt{\frac{3}{4} \frac{\kappa_{\text{sw}} \alpha}{1 + \alpha}} \xrightarrow{v_w \approx 1} \frac{\sqrt{3} \alpha}{2(1 + \alpha) \sqrt{0.73 + 0.083 \sqrt{\alpha} + \alpha}}.$$

$$\alpha=1, HR_*=10^{-1}$$







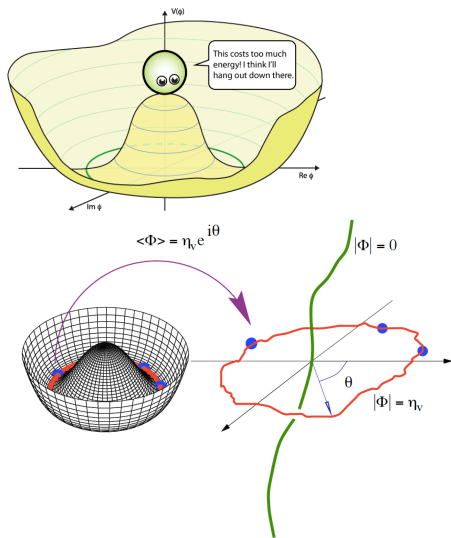
Cosmic String formation (Kibble mechanism)

- Charged complex scalar field

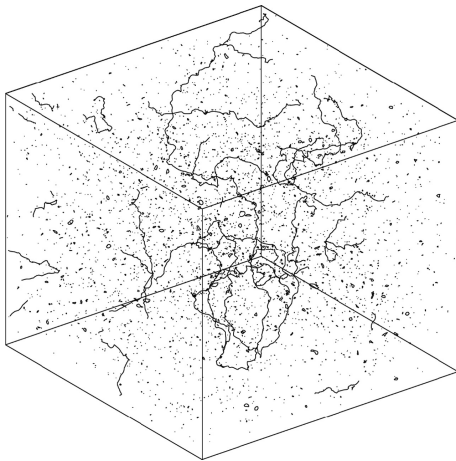
$$V = \lambda \left(\Phi^\dagger \Phi - \frac{v^2}{2} \right)^2$$

- Horizon size at early time (high temperature)
 $d_H \propto M_p/T^2$
- we need a solution:

$$\Phi \xrightarrow{r \rightarrow \infty} \frac{v}{\sqrt{2}} e^{i\theta}$$



Cosmic Strings



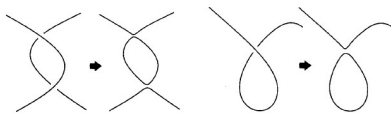
Vilenkin and Shellard '94

Cosmic String network

- Static string network would red-shift as

$$\rho_{\infty} \propto a^{-2}$$

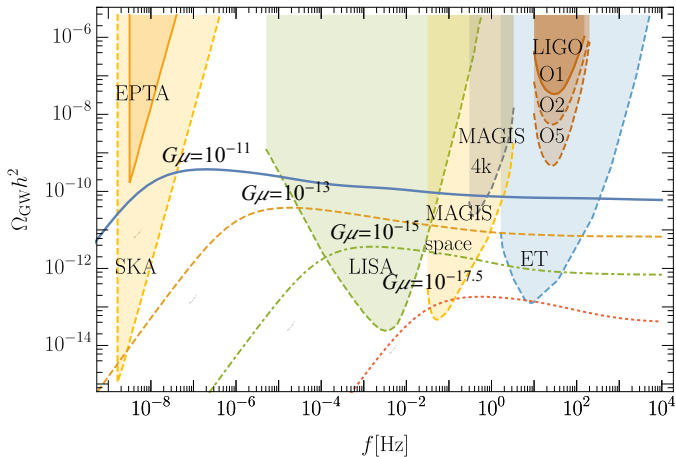
- strings intercommute on collision



- overall energy density of the network scales with total energy density

$$\frac{\rho_{\infty}}{\rho_{\text{tot}}} \propto G\mu$$

Stochastic GW background from Cosmic Strings

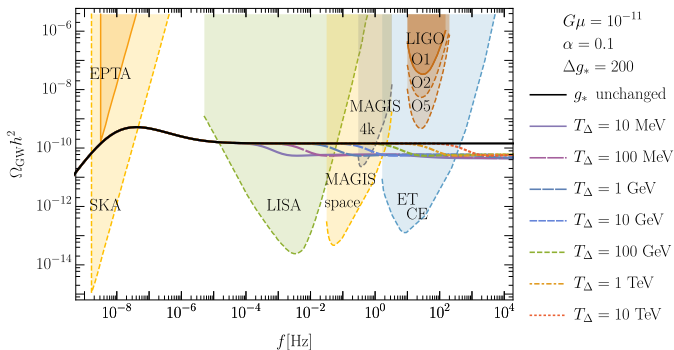


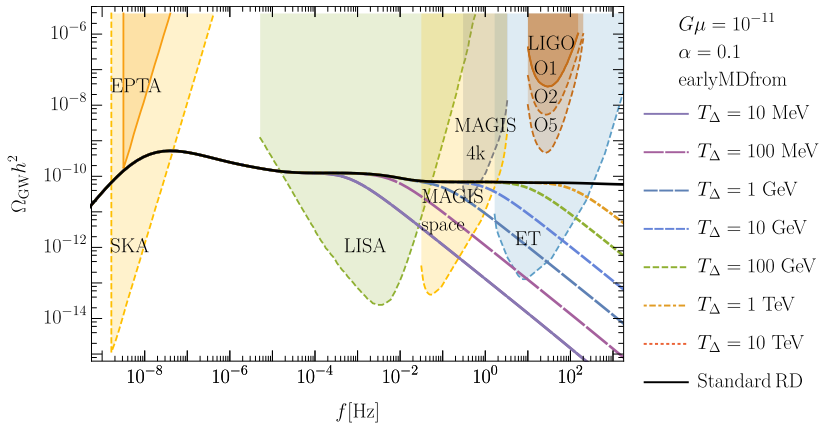
Extra DOF

- We add Δg_* new degrees of freedom at T_Δ

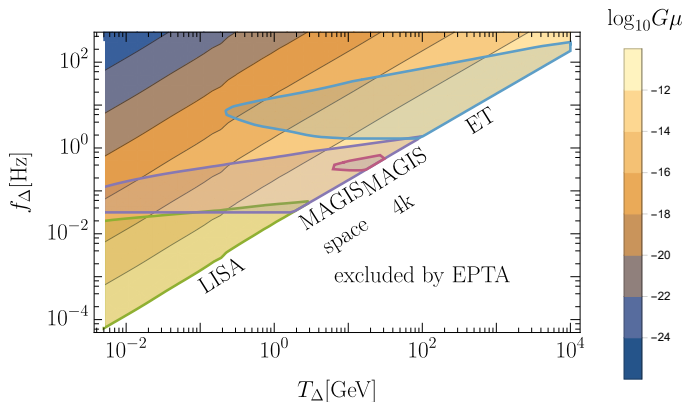
$$g_*(T) = \begin{cases} g_*^{\text{SM}}(T) & \text{for } T < T_\Delta \\ g_*^{\text{SM}}(T) + \Delta g_* & \text{for } T > T_\Delta \end{cases}$$

- An example with $\Delta g_* = 200$





Detection capabilities



- slightly better numerical result

$$f_\Delta = (8.67 \times 10^{-9} \text{ Hz}) \frac{T_\Delta / \text{GeV}}{\sqrt{\alpha G\mu}} \left(\frac{g_*(T_\Delta)}{g_*(T_0)} \right)^{\frac{8}{6}} \left(\frac{g_S(T_0)}{g_S(T_\Delta)} \right)^{-\frac{7}{6}}$$