

# Hot Axions and the $H_0$ tension

Alessio Notari <sup>1</sup>

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talk @ Benasque, Light Scalars, 2019.

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<sup>1</sup>In collaboration with R.Z. Ferreira, F. D'Eramo, J.L. Bernal. Work in progress with L.Merlo, F. Arias-Aragon.

# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

The **QCD Axion** ( $a$ ) is a very light particle that

- Solves the “**Strong CP problem**” via coupling to gluons

$$\mathcal{L}_a = \frac{\alpha_s}{8\pi} \frac{a}{f} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

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- **But:** boundary term sensitive to QCD Instantons,
  - 1 Induces a potential  $V(a) \approx \Lambda_{\text{QCD}}^4 \cos(a/f)$ ;
  - 2  $\implies$  Drives  $\cancel{\text{CP}}$  to zero
  - 3  $\implies$  Axion mass  $m_a \approx \frac{\Lambda_{\text{QCD}}^2}{f}$

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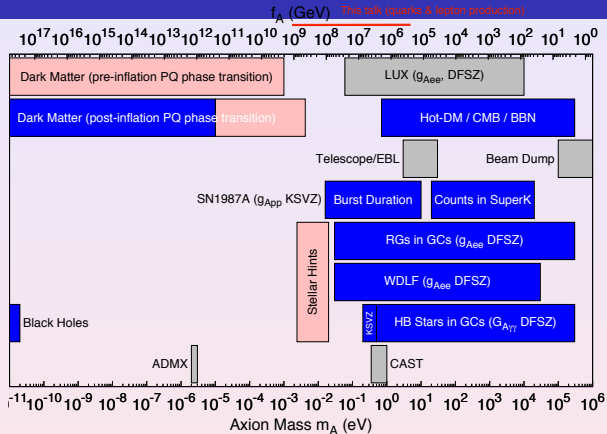
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- Bounds on  $f \Leftrightarrow$  bounds on  $m_a$

# Axion: constraints



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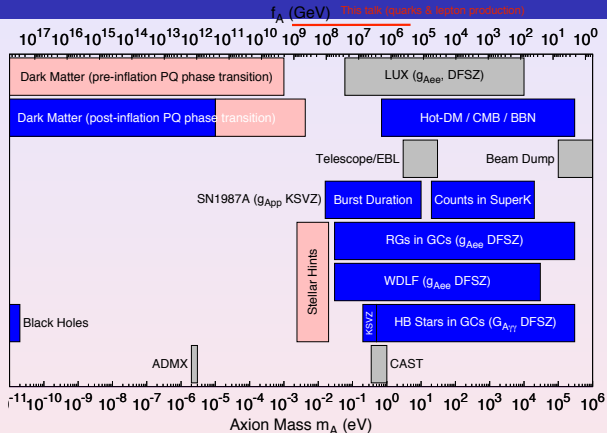
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Axions as Hot Relics

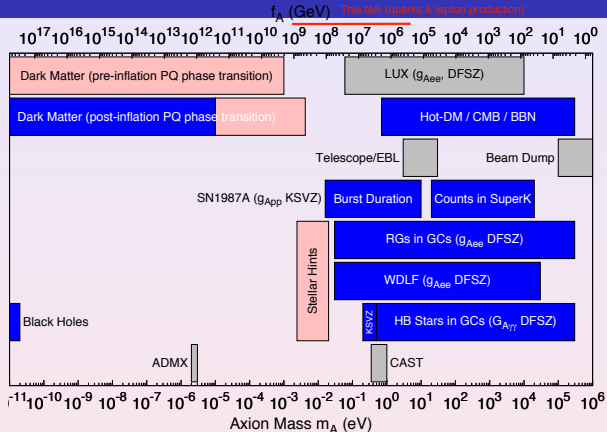
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- **Caveat:** Constraints based on couplings with  $e, \gamma$ , nucleons... Expected  $\mathcal{O}(1/f)$ , but model dependent.
- Small  $m_a \ll \mathcal{O}(\text{eV}) \implies$  acts as **Radiation**, visible in CMB (*Cosmic Axion Background*)



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- 2 **Only** breaking: Instanton-induced (tiny) mass

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- **Axions:**

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- **Terminology:**

- 1 If it couples to  $G\tilde{G} \Rightarrow$  "QCD Axion"
- 2 If not:  $\Rightarrow$  Axion-Like Particle ("**ALP**")

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→ **hot relic (dark radiation)**  
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- Scattering rate (via gluons) vs. Hubble

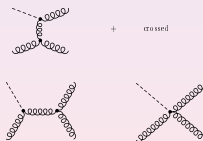


Figure: (Masso et al. Phys.Rev. D66 (2002).).

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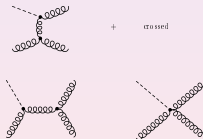


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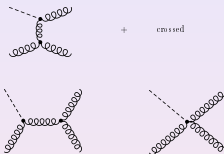


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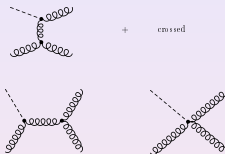


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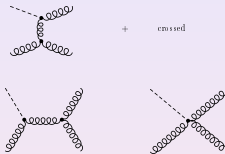


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- At  $T > T_{DEC} \equiv$  thermal equilibrium
- Example:
  - $f = 10^9 \text{ GeV} \implies T_{DEC} \approx 10 \text{ TeV}$
  - $f = 10^{10} \text{ GeV} \implies T_{DEC} \approx 10^4 \text{ TeV}$

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- Affects Matter-Radiation equality (if  $m \ll \mathcal{O}(0.1 \sim 1 \text{ eV})$ )  
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- $N_{\text{eff}} = 3.046 + \Delta N_{\text{eff}}$

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- $$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,DEC}^{4/3}}.$$

# $\Delta N_{\text{eff}}$ diluted by $g_{*,DEC}$

- Abundance  $\Delta N_{\text{eff}}$  diluted if total number of relativistic species in the plasma  $g_{*,DEC}$  is large

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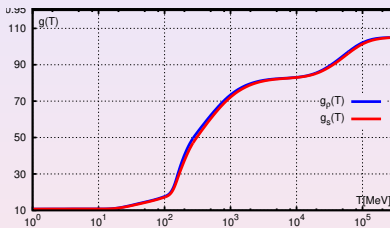
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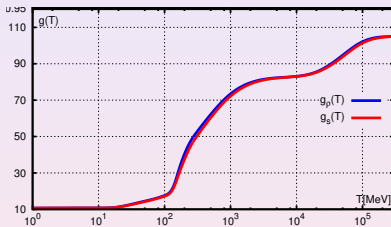
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- $$\Delta N_{\text{eff}} \approx \frac{13.6}{g_{*,\text{DEC}}^{4/3}}$$
- If  $T_{\text{DEC}} \gg 100 \text{ GeV}$ ,  $\Rightarrow g_{*,\text{DEC}} \geq 106.75$
- $\Rightarrow \Delta N_{\text{eff}} \lesssim 0.027$  (only upper bound!)  
(maybe detectable by CMB-Stage 4 experiments)



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- If  $f \lesssim 10^9\text{-}10^{10}$  GeV dominant channels can be via **quarks & leptons**<sup>2</sup>  $\implies T_{DEC} \leq \text{Electroweak scale}$

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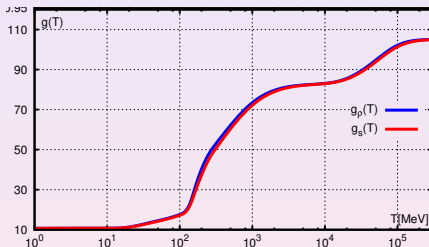
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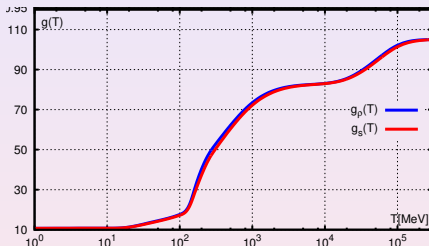
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## ADVANTAGES:

- 1  $g_*^{SM}$  is smaller  $\Rightarrow$  **larger  $N_{\text{eff}}$**
- 2 Here we are confident on  $g_*^{SM} \Rightarrow$  **Precise predictions**
- 3 Lower  $f \Rightarrow$  more accessible by **direct searches**  
(**CAST, IAXO**)

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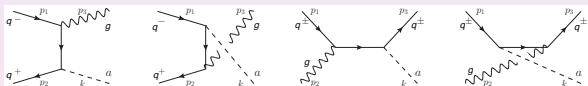
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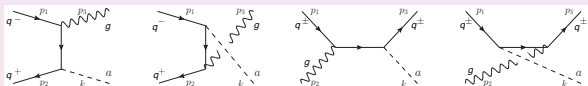
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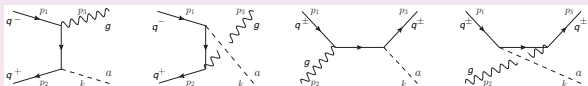
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- Indeed:
  - This coupling can be **rotated away**  $q \rightarrow e^{i\frac{c_i a}{f} \gamma^5} q$
  - But it **reappears in the mass term**  $m_q e^{i\frac{c_i a}{f}} \bar{q} q$

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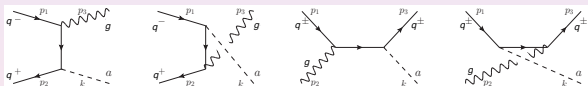
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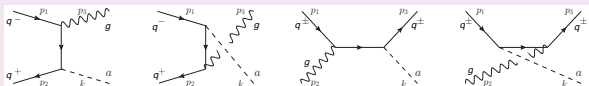
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  - But it **reappears in the mass term**  $m_q e^{i\frac{c_i a}{f}} \bar{q} q$

$$\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}}$$

# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

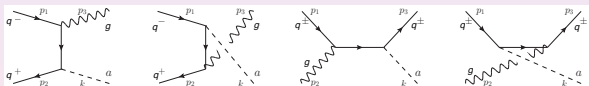
Axion/ALPs  
via Leptons

The  $H_0$   
tension

- If  $a$  is directly coupled to SM **heavy quarks** ( $c, b, t$ ):

$$\mathcal{L}_{a-q} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{q}_i \gamma^\mu \gamma^5 q_i,$$

- Scattering rate (via quarks, e.g.  $qg \leftrightarrow qa$ ) vs. Hubble



- If  $m_q = 0 \implies$  the **vertex vanishes**
- Indeed:
  - This coupling can be **rotated away**  $q \rightarrow e^{i\frac{c_i a}{f} \gamma^5} q$
  - But it **reappears in the mass term**  $m_q e^{i\frac{c_i a}{f}} \bar{q} q$

$$\Gamma_s = \left(\frac{c_i}{f}\right)^2 g_s^2 m_q^2 T \cdot e^{-\frac{m_q}{T}} \text{ vs. } H \approx \frac{T^2}{M_{Pl}}$$

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The QCD  
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The  $H_0$   
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---

<sup>3</sup>R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

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The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Ratio peaks at  $T \approx m_q$

---

<sup>3</sup>R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

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Axions as Hot  
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The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Ratio peaks at  $T \approx m_q$
- Axions/ALPs produced **dominantly** via quarks

$$1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$$

- Range  $10^9 \text{ GeV} \gtrsim f/c_i \gtrsim 10^7 \text{ GeV}$  <sup>3</sup>

<sup>3</sup>R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
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Axions via  
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Axion/ALPs  
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The  $H_0$   
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$$1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$$

- Range  $10^9 \text{ GeV} \gtrsim f/c_i \gtrsim 10^7 \text{ GeV}$ <sup>3</sup>
- Tension with SN bounds (for QCD Axion,  $c_i = 1$ )
- Interesting for **direct detection** (e.g. **IAXO**),  
 $m_a \approx 10^{-1} \sim 10^{-3} \text{ eV}$ ,

<sup>3</sup>R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

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Axions as Hot  
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The QCD  
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The  $H_0$   
tension

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- Interesting for **direct detection** (e.g. **IAXO**),  
 $m_a \approx 10^{-1} \sim 10^{-3} \text{ eV}$ , (+ *Hints from stellar cooling*)

<sup>3</sup>R.Ferreira & A.N., PRL 2018. See also Turner PRL 1987, Brust et al. JHEP 2013, Baumann et al. PRL 2016.

# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

- $g_{*,DEC}$  is smaller at  $1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$
- **Prediction:** larger  $N_{\text{eff}} \lesssim 0.05 - 0.06$   
(\*Not just upper bound!\*)

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension



# QCD Axion through $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
Axion

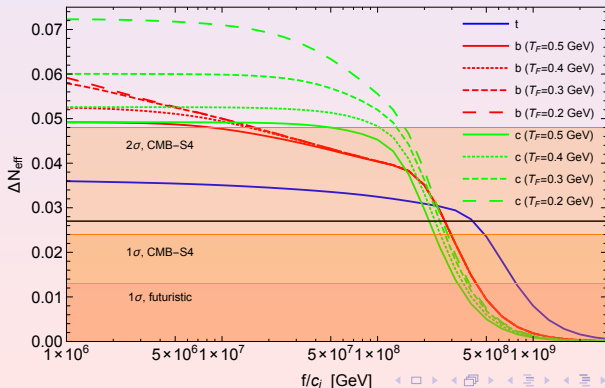
Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- $g_{*,DEC}$  is smaller at  $1 \text{ GeV} \lesssim T \lesssim 100 \text{ GeV}$
- Prediction:** larger  $N_{\text{eff}} \lesssim 0.05 - 0.06$   
(\*Not just upper bound!\*)
- Solving **Boltzmann equations for  $n_a$ :**



# Interplay with IAXO

Axions as Hot  
Relics

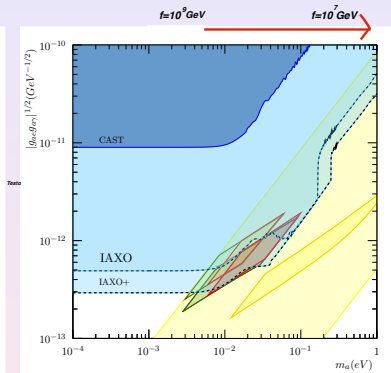
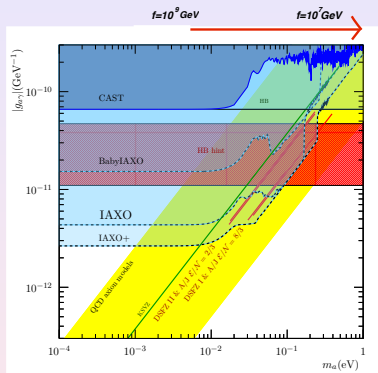
The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension



**Figure:** Physics potential of the International Axion Observatory (IAXO)

$$10^9 \text{ GeV} \gtrsim f/c_i \gtrsim 10^7 \text{ GeV}$$

$$5 \times 10^{-3} \text{ eV} \gtrsim m_a \gtrsim 0.5 \text{ eV}$$

$$(c_i = 1, \text{ for QCD Axion})$$

# Hot Axions via Leptons

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- The same can be done with **leptons** ( $\mu$  and  $\tau$ )<sup>4</sup>
- $a$ -electron uninteresting (strongly constrained)

---

<sup>4</sup>F.D'Eramo, A.N., R.Z.Ferreira, J.L.Bernal, JCAP 2018.

# Hot Axions via Leptons

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

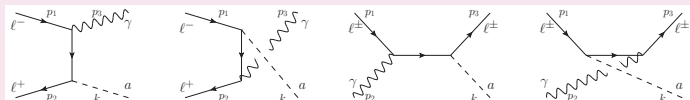
Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- The same can be done with **leptons** ( $\mu$  and  $\tau$ )<sup>4</sup>
- $a$ -electron uninteresting (strongly constrained)
- Direct coupling to **heavy leptons** ( $\mu, \tau$ ):

$$\mathcal{L}_{a-\ell} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{\ell}_i \gamma^\mu \gamma^5 \ell_i,$$



<sup>4</sup>F.D'Eramo, A.N.,R.Z.Ferreira, J.L.Bernal, JCAP 2018.

# Hot Axions via Leptons

Axions as Hot Relics

The QCD Axion

Axions via Gluons

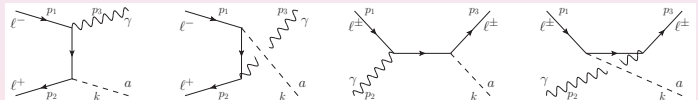
Axion via Quarks

Axion/ALPs via Leptons

The  $H_0$  tension

- The same can be done with **leptons** ( $\mu$  and  $\tau$ )<sup>4</sup>
- $a$ -electron uninteresting (strongly constrained)
- Direct coupling to **heavy leptons** ( $\mu, \tau$ ):

$$\mathcal{L}_{a-\ell} = \partial_\mu a \sum_i \frac{c_i}{2f} \bar{\ell}_i \gamma^\mu \gamma^5 \ell_i,$$



- Slightly smaller  $f/c_\ell$
- Ratio peaks at  $T \approx m_\ell \implies$  **Larger  $N_{eff}$**

<sup>4</sup>F.D'Eramo, A.N.,R.Z.Ferreira, J.L.Bernal, JCAP 2018.

# Hot Axions via Lepton Scatterings

Axions as Hot  
Relics

The QCD  
Axion

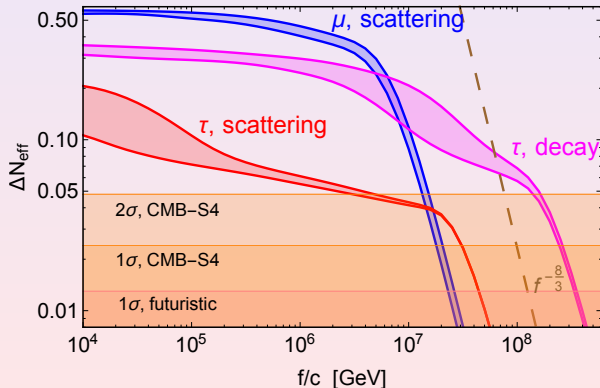
Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Smaller  $f/c_i \lesssim \text{few} \cdot 10^7 \text{ GeV}$
- Ratio peaks at  $T \approx m_\ell \Rightarrow$  Larger  $N_{\text{eff}}$



# Hot Axions via Lepton Decays

Axions as Hot  
Relics

- $a - \ell$  interaction can be **flavor non-diagonal**

$$\mathcal{L}_{a-\ell} = \partial_\mu a \sum_{\ell \neq \ell'} \bar{\ell}' \gamma^\mu (\mathcal{V}_{\ell'\ell} + \mathcal{A}_{\ell'\ell} \gamma^5) \ell + \text{h.c.} ,$$

- Decays  $\tau \rightarrow \mu + a, \tau \rightarrow e + a$

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

# Hot Axions via Lepton Decays

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

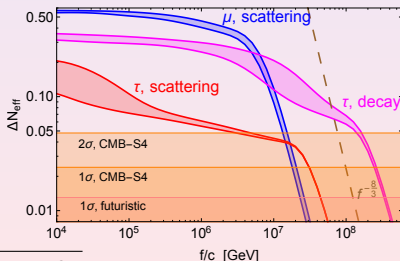
Axion/ALPs  
via Leptons

The  $H_0$   
tension

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- Decays  $\tau \rightarrow \mu + a$ ,  $\tau \rightarrow e + a$



$$(c_{\ell\ell'} \equiv \sqrt{\mathcal{V}_{\ell'\ell}^2 + \mathcal{A}_{\ell'\ell}^2})$$



# Hot Axions via Lepton Decays

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

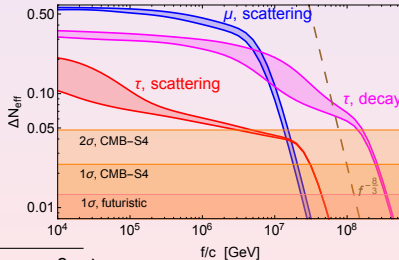
Axion/ALPs  
via Leptons

The  $H_0$   
tension

- $a - \ell$  interaction can be **flavor non-diagonal**

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- Decays  $\tau \rightarrow \mu + a$ ,  $\tau \rightarrow e + a$



$$(c_{\ell\ell'} \equiv \sqrt{\mathcal{V}_{\ell'\ell}^2 + \mathcal{A}_{\ell'\ell}^2})$$

- More efficient** than scatterings (**larger  $f/c$** )

# Hot Axions via quark Decays

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- $a$ -quarks interaction can be **flavor non-diagonal**

# Hot Axions via quark Decays

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- $a$ -quarks interaction can be **flavor non-diagonal**

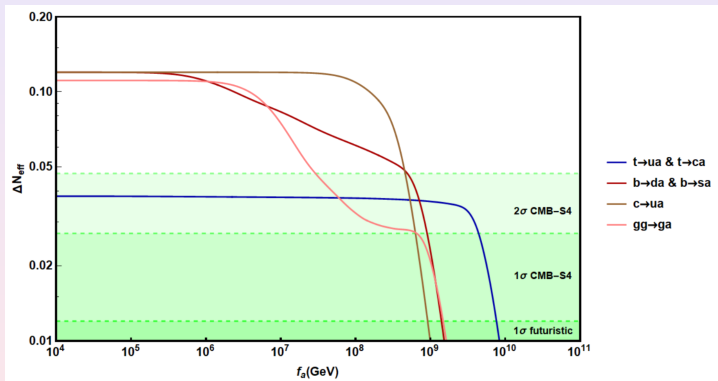


Figure: Preliminary.

- **More efficient** than scatterings (**larger**  $f/c \lesssim 10^{10}$  GeV)
- Survives better SN bounds for QCD Axion (with  $c_i = 1$ )

# $H_0$ tension

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Planck CMB data (2015 and recent 2018)
- Measured  $H_0$  in tension with direct local measurements from SN<sup>5</sup>

---

<sup>5</sup>Planck 2018 results. VI. Cosmological parameters. Bernal, Verde & Riess JCAP 2016. Riess et al. Astrophys. J., 2018.

# $H_0$ tension

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Planck CMB data (2015 and recent 2018)
- Measured  $H_0$  in tension with direct local measurements from SN<sup>5</sup>
  - $H_0 = 67.27 \pm 0.60 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (CMB)
  - $H_0 = 73.52 \pm 1.62 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (SN)
- Tension at  $3.5\sigma$  ( $3.46\sigma$  including BAO)

---

<sup>5</sup>Planck 2018 results. VI. Cosmological parameters. Bernal, Verde & Riess JCAP 2016. Riess et al. Astrophys. J., 2018.

# $H_0$ tension

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The  $H_0$   
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  - $H_0 = 73.52 \pm 1.62 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (SN)
- Tension at  $3.5\sigma$  ( $3.46\sigma$  including BAO)
- Recently (Riess et al. 2019) claim:  
 $H_0 = 74.03 \pm 1.42 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (SN)  $\Rightarrow 4.4\sigma$ (!)

---

<sup>5</sup>Planck 2018 results. VI. Cosmological parameters. Bernal, Verde & Riess JCAP 2016. Riess et al. Astrophys. J., 2018.

# $H_0$ vs $N_{eff}$

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- It is known that  $\Delta N_{eff} > 0$  correlates with a higher Hubble constant  $H_0$  from CMB

# $H_0$ vs $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
Axion

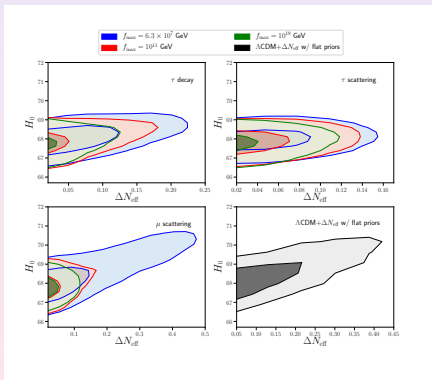
Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

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# $H_0$ vs $N_{\text{eff}}$

Axions as Hot  
Relics

The QCD  
Axion

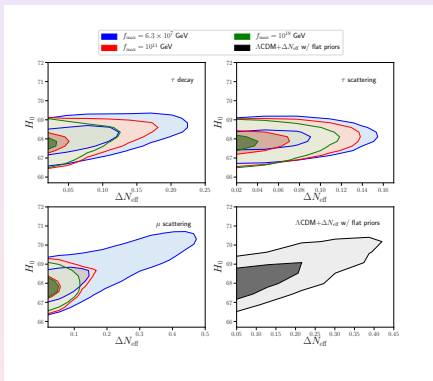
Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- It is known that  $\Delta N_{\text{eff}} > 0$  correlates with a higher Hubble constant  $H_0$  from CMB



- Flat prior on  $\log(f/c_i) \implies$  some prior dependence
- ALPs from  $\mu$  scatterings can significantly increase  $H_0$

# Hot axions and $H_0$ tension

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- Tension remains, but can be **alleviated** to  $3.6\sigma \rightarrow 3\sigma$

Model	Coupling	Prior $(f/c)_{\max}$ [GeV]	$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	Tension ( $\sigma$ )
$\Lambda$ CDM+ $\Delta N_{\text{eff}}$	$\mu$ scattering	$3 \times 10^7$	$68.0^{+0.8}_{-0.7} (+2.3_{-1.1})$	3.06 (2.75*)
		$10^{11}$	$67.8^{+0.6}_{-0.5} (+1.4_{-1.1})$	3.36
		$10^{18}$	$67.7^{+0.5}_{-0.4} (+1.2_{-1.0})$	3.38
	$\tau$ decay	$6.3 \times 10^7$ GeV	$68.1^{+0.6}_{-0.5} (+1.2_{-1.0})$	3.18
		$10^{11}$	$67.8^{+0.6}_{-0.5} (+1.2_{-0.9})$	3.35
		$10^{18}$	$67.7^{+0.5}_{-0.4} (+1.1_{-0.9})$	3.39
	$\tau$ scattering	$5 \times 10^8$	$68.0^{+0.5}_{-0.5} (+1.0_{-1.0})$	3.25
		$10^{11}$	$67.8^{+0.5}_{-0.5} (+1.1_{-1.0})$	3.33
		$10^{18}$	$67.7^{+0.5}_{-0.5} (+1.1_{-0.9})$	3.39
	Flat prior on $N_{\text{eff}}$	-	$68.3^{+0.8}_{-0.7} (+1.8_{-1.2})$	2.93
$\Lambda$ CDM	No coupling	-	$67.7^{+0.5}_{-0.4} (+0.9_{-0.9})$	3.46

# Hot axions and $H_0$ tension

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

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	Flat prior on $N_{\text{eff}}$	-	$68.3^{+0.8}_{-0.7} (+1.8_{-1.2})$	2.93
$\Lambda$ CDM	No coupling	-	$67.7^{+0.5}_{-0.4} (+0.9_{-0.9})$	3.46

- Tension with new Riess et al. 2019 SN claim, **alleviated** to  $4.4\sigma \rightarrow 3.7\sigma$

# Conclusions

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- 1 If  $f \lesssim \mathcal{O}(10^9)$  GeV, coupling with **quarks and leptons** (with  $c_i = \mathcal{O}(1)$ ) dominates over  $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- 2 Efficiency peaks at  $T \approx m_f$

# Conclusions

Axions as Hot  
Relics

The QCD  
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The  $H_0$   
tension

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- 2 Efficiency peaks at  $T \approx m_f$
- 3 For **quarks** ( $t, b, c$ )  $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$   
(measurable at  $2\sigma$  by CMB S4)
- 4 For **leptons** ( $\mu, \tau$ )  $\implies N_{\text{eff}} \lesssim 0.6 - 0.15$   
(measurable by CMB S4)
- 5 Non-diagonal couplings  $\implies$  production via **Decays**  
more efficient ( $f \lesssim \mathcal{O}(10^{10})$  GeV)

# Conclusions

Axions as Hot  
Relics

The QCD  
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Axions via  
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Axion/ALPs  
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The  $H_0$   
tension

- 1 If  $f \lesssim \mathcal{O}(10^9)$  GeV, coupling with **quarks and leptons** (with  $c_i = \mathcal{O}(1)$ ) dominates over  $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- 2 Efficiency peaks at  $T \approx m_f$
- 3 For **quarks** ( $t, b, c$ )  $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$   
(measurable at  $2\sigma$  by CMB S4)
- 4 For **leptons** ( $\mu, \tau$ )  $\implies N_{\text{eff}} \lesssim 0.6 - 0.15$   
(measurable by CMB S4)
- 5 Non-diagonal couplings  $\implies$  production via **Decays**  
more efficient ( $f \lesssim \mathcal{O}(10^{10})$  GeV)
- 6  $\mu$  production can **alleviate  $H_0$  tension** level

# Conclusions

Axions as Hot  
Relics

The QCD  
Axion

Axions via  
Gluons

Axion via  
Quarks

Axion/ALPs  
via Leptons

The  $H_0$   
tension

- ① If  $f \lesssim \mathcal{O}(10^9)$  GeV, coupling with **quarks and leptons** (with  $c_i = \mathcal{O}(1)$ ) dominates over  $\frac{\alpha_s}{8\pi} \frac{a}{f} G\tilde{G}$
- ② Efficiency peaks at  $T \approx m_f$
- ③ For **quarks** ( $t, b, c$ )  $\implies N_{\text{eff}} \lesssim 0.05 - 0.07$  (measurable at  $2\sigma$  by CMB S4)
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- ⑤ Non-diagonal couplings  $\implies$  production via **Decays** more efficient ( $f \lesssim \mathcal{O}(10^{10})$  GeV)
- ⑥  $\mu$  production can **alleviate  $H_0$  tension** level
- ⑦ **Future CMB experiments** will tell in a few years about the **Axion** (and  $H_0$ )
- ⑧ Interplay with **direct detection** (e.g. **IAXO**)