







# X-band RF electron gun injector design

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#### Summary

- The main objective is to design a 5.6 cell X-band RF photoinjector fed by a coaxial coupler, the Avni gun prototype has been taken as reference
- Since the entire device (RF gun + coupler) is rotationally symmetric, the RF design was carried out with the 2D software SUPERFISH, which has the advantage of being much faster than full 3D commercial codes such as HFSS or CST
- This design is focused on the optimization of: the resonant frequency, the coupling factor, the maximum values of the RF electric fields in each cavity, the mode separation, and the superficial RF electric field at irises



In the current design it has been taken into account some comments and suggestions made at the XLS First Annual Meeting

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#### RF gun design

#### > After the optimization, the final dimensions for the RF gun are







#### Multipactor analysis in the coaxial coupler

- $\geq$ After the presentation of the first RF gun prototype at the XLS meeting, a concern was expressed about the likely presence of multipactor discharge in coaxial couplers
- Multipactor risk at the coaxial coupler was assessed by means of numerical simulations using our in-house developed code 12000

Numerical simulations were launched at several RF voltage values up to the maximum RF voltage reached at the coaxial coupler



Capture of the output results for the multipactor code



Coaxial voltage amplitude during the cavity filling

Thus, the coaxial does not suffer multipactor at the steady operating voltage (13.226 kV), however it is likely to appear during the filling of the RF gun cavity

$$V(t) = V_0 \left( 1 - e^{-\frac{t}{\tau_F}} \right)$$

First window 
$$\rightarrow \Delta t = 15 \ ns, \ \Delta t/T = 180$$

$$t_F = 112.5 \ ns$$
 Second window  $\rightarrow \Delta t = 23 \ ns$ ,  $\Delta t/T =$ 



 $t_F = \frac{2Q_L}{\omega}$ 













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#### Multipactor analysis in the coaxial coupler

- Despite the multipactor risk appearance at the coupler has been evidenced, it is not a crucial problem since it can be suppressed by means of an external magnetic field
- This fact was both theoretically and experimentally demonstrated for a coaxial line<sup>1</sup>, thus the following conclusions arise:
  - Multipactor can be suppressed provided that a strong enough magnetic field is applied along the coaxial axis
  - As an approximate rule, the minimum magnetic field to mitigate the discharge is given by

$$f_c \approx f$$
  $f_c = \frac{1}{2\pi} \frac{e}{m} B_{dc}$ 

f is the RF frequency $f_c$  is the cyclotron frequency $B_{dc}$  is the external magnetic field-e is the electron chargem is the electron mass-e is the electron charge

In our case, the above condition gives  $B_{dc} = 428.5 mT$ 

- ✓ Numerical simulations support that no multipactor discharge is expected with such external magnetic field
- ✓ In fact, it is found that a  $B_{dc} = 360 mT$  is enough to suppress the discharge, according to the numerical simulations







Multipactor RF power threshold as a function of the ratio between the cyclotron frequency and the RF frequency. For a coaxial line at f = 1.145 GHz

<sup>1</sup>D. González-Iglesias et al., "Multipactor Mitigation in Coaxial Lines by Means of Permanent Magnets", IEEE Transactions on Electron Devices, vol. 61, no. 12, pp. 4224-4231, Dec. 2014.

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#### RF breakdown

The risk of RF breakdown in the component is assessed by means the breakdown rate (BDR), which is obtained by computing the modified Poynting vector<sup>1</sup>

 $BDR \equiv \frac{number \ of \ breadowns}{pulse \cdot 1m \ structure \ length}$ 

Modified Poynting vector  $S_c = |Re\{\vec{S}\}| + g_c |Im\{\vec{S}\}|$ 

 $0.15 \le g_c \le 0.2$  typically  $g_c = \frac{1}{6}$ 

On the right it is depicted the  $S_c$  value at the RF gun surfaces (using a value of  $g_c=1/6$ ) for a cathode electric field of 200 MV/m, which is selected as the maximum electric field operating value

The BDR follows the next empirical law:

 $\frac{S_c^{15} t_p^5}{BDR} = C \qquad \qquad \begin{array}{c} t_p \text{ is the pulse length} \\ C \text{ is a constant} \end{array}$ 

Complex Poynting vector



According to ref. (1), a value of  $S_c = 5 \text{ W}/\mu\text{m}^2$  for a pulse length of 200 ns gives a breakdown rate of BDR =  $10^{-6}$  bpp/m. Using this data, the constant can be evaluated  $C = 9.765625 \times 10^{27} \text{ W}^{15} \cdot \text{ns}^5 \cdot \text{m} \cdot \mu\text{m}^{-7.5} \text{bpp}^{-1}$ 

Modified Poynting vector at the RF gun surfaces as a function of the axial position, for cathode field of 200 MV/m

 $\vec{S} = \frac{1}{2}\vec{E} \times \vec{H}^*$ 

 $BDR = \frac{S_c^{15} t_p^5}{C} \quad (eq. 1)$ Maximum modified Poynting vector  $\longrightarrow \max(S_c) = 4.88 W / \mu m^2$ Mean value of modified Poynting vector  $\longrightarrow \max(S_c) = 2.00 W / \mu m^2$ 

<sup>1</sup>A. Grudiev et al., "New local field quantity describing the high gradient limit of accelerating structures", Physical Review Special Topics – Accelerators and Beams, 12, 102001 (2009).







#### RF breakdown

➢ In eq. 1 is assumed (see ref. 1 of previous slide) that the amplitude of the RF electromagnetic field is constant over the entire RF pulse, whilst in the RF gun case there is a transitory behavior during the filling and emptying of the structure

$$E = E_0 \sin(\omega t) \qquad H_0 = \frac{E_0}{Z} \qquad \vec{S} = \frac{1}{2} \vec{E} \times \vec{H}^* \qquad S \propto E_0^2$$
In ref. 1  $\rightarrow$   $S_c(t) = S_{c,0}, \qquad 0 \le t \le t_p \qquad \Rightarrow BDR = \frac{S_{c,0}^{15} t_p^5}{C} \qquad (eq. 1)$ 
For the RF gun  $\rightarrow$   $S_c(t) = \begin{cases} S_{c,0} \left(1 - e^{-t/t_F}\right)^2, & 0 \le t \le T_{on} \\ S_{c,0} \left(1 - e^{-Ton/t_F}\right)^2 e^{-\frac{2(t-T_{on})}{t_F}}, & t \ge T_{on} \end{cases}$ 
To is the time that the RF generator is on  $\omega$  is the angular RF frequency  $\psi_F$  is the filling time of the cavity  $\psi_T$ 

➢ For the RF gun case, the BDR can be calculated by splitting the RF pulse as the sum of many short pulses, each of them with its corresponding BDR given for the uniform S<sub>c</sub> amplitude case of eq. 1:

$$BDR_{pulse} = \sum_{k=1}^{n} BDR(k) = \frac{1}{C} \sum_{k=1}^{n} S_{c}^{15}(t_{k}) t_{p}^{5} = \frac{1}{C} \sum_{k=1}^{n} S_{c}^{15}(t_{k}) \left(\frac{T_{p}}{n}\right)^{5}$$

$$BDR_{pulse} = \frac{1}{C} \lim_{n \to \infty} \sum_{k=1}^{\infty} S_c^{15}(t_k) \left(\frac{T_p}{n}\right)^2 = \frac{1}{C} \int_0^{t_p} S_c^{15}(t) d(t^5)$$

$$BDR_{pulse} = \frac{5}{C} \int_0^{T_p} S_c^{15}(t) t^4 dt \qquad T_p = n$$
$$t_n = k$$

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 $T_{p}$  is the pulse length

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 $\lim_{n \to \infty} \sum_{k=1}^n f(x_k) \Delta x_k = \int_a^b f(x) \, dx$ 

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#### RF breakdown

Taking into account that for the RF gun,  $\max(S_c) = S_{c,0} = 4.88 W/\mu m^2$ , the BDR can be obtained as a function of the pulse length:



BDR as a function of the time that the generator is on, for the RF gun operating with 200 MV/m at cathode

> In the graph it is depicted the BDR obtained both using the approximation of time-constant RF electromagnetic field  $(S_{c,0})$  and computing the integral assuming the time-variation of  $S_c$ 

$$BDR = \frac{S_{c,0}^{15} t_p^5}{C}$$

$$BDR_{pulse} = \frac{5}{C} \int_0^{T_p} S_c^{15}(t) t^4 dt$$

As it is expected, when T<sub>p</sub>>>t<sub>F</sub>, the BDR calculated by means of integration of S<sub>c</sub> tends to the approximated calculation of constant S<sub>c,0</sub>

















### RF pulse heating

RF magnetic field on metallic device surfaces induces electric currents that increases the wall temperature due to Joule effect, this phenomenon is known as RF pulse heating



$$P = \frac{1}{2} \int \vec{J} \cdot \vec{E}^* dV \qquad P = \frac{1}{2} R_s A \left| H_{||,0} \right|^2 \qquad \frac{P(x)}{A} = \frac{R_s}{2} \left| H_{||,0} \right|^2 \frac{2}{\delta} e^{-2x/\delta} \begin{cases} \sum_{k=0}^{\infty} 1 \\ \sum_{k=0.5}^{\infty} 0 \end{bmatrix} \quad t/T \end{cases}$$
$$\vec{J} = \sigma \vec{E}$$
Heat transfer equation 
$$\frac{\partial T}{\partial t} = \frac{k}{\rho C_{\epsilon}} \nabla^2 T + f(\vec{r}, t) \qquad R_s = \frac{1}{\delta \sigma} \qquad \delta = \sqrt{\frac{2}{\sigma \mu_0 \omega}}$$

An approximate formula describing the temperature rise for a semi-infinite body (1D model) is given in (1):

Temperature rise (approximation)  $\Delta T = \frac{\left|H_{||}\right|^2 \sqrt{t_p}}{\sigma \delta \sqrt{\pi \rho C_{\epsilon} k}}$ 



Temperature increase as a function of time

 $\sigma$  is the electric conductivity k is the thermal conductivity A is the area L is the wall length

 $a = \sqrt{\frac{k}{\rho C_{\epsilon}}}$  $\alpha = \frac{1}{2} \frac{R_s}{\rho C_{\epsilon}} \left| H_{||} \right|^2$ 

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Temperature rise obtained from analytically solving the heat transfer equation

$$\Delta T(x,t) = \frac{\alpha}{L} \left( 1 - e^{-\frac{2L}{\delta}} \right) t + \sum_{n=1}^{\infty} \left( \frac{L}{\pi n a} \right)^2 \frac{8\alpha L}{4L^2 + (\pi \delta n)^2} \left( 1 - e^{-\frac{2L}{\delta}} (-1)^n \right) \left( 1 - e^{-\left(\frac{\pi n a}{L}\right)^2 t} \right) \cos\left(\frac{\pi n x}{L}\right)$$

 $\begin{array}{ll} H_{||} \text{ is the magnetic field parallel to the surface} & t_p \text{ is the RF pulse length} \\ \rho \text{ is the density} & C_\epsilon \text{ is the specific heat} \\ \omega \text{ is the angular frequency} & \mu_0 \text{ is the magnetic permeability of vacuum} \\ T \text{ is the temperature} & f(\vec{r}, t) \text{ are the heat sources} \end{array}$ 

<sup>1</sup>D. P. Pritzkau, "RF Pulsed Heating", SLAC-Report-577 , Ph.D. Dissertation, Stanford University, 2001.

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### RF pulse heating

- The previous temperature rise approximation, as well as the exact solution based on the series, are assuming an RF electromagnetic field of constant amplitude in time
- However, this is not true in the RF gun due to the transient during the filling and emptying of the device. This effect must be considered when resolving the heat transfer equation:

$$f(x,t) = \frac{P(x,t)}{A} = \frac{R_s}{2} |H_{\parallel,0}(t)|^2 \frac{2}{\delta} e^{-2x/\delta} \qquad f(x,t) = g(x)h(t)$$

$$H_{\parallel,0}(t) = \begin{cases} H_{\parallel,0}\left(1 - e^{-t/t_F}\right), & 0 \le t \le t_{on} \\ H_{\parallel,0}\left(1 - e^{-T^p/t_F}\right) e^{-\frac{(t-T^p)}{t_F}}, & t \ge t_{on} \end{cases} \xrightarrow{\otimes} \frac{1}{\sqrt{2}} \int_{0}^{t} \frac{\partial T}{\partial t} = \frac{k}{\rho C_e} \nabla^2 T + f(\vec{r},t) \\ \text{Heat transfer equation} \end{cases}$$

$$\Delta T(x,t) = \begin{cases} u_0(t) + \sum_{n=1}^{\infty} u_n(t) \cos\left(\frac{\pi nx}{L}\right), & 0 \le t \le t_{on} \\ u_0(t_0) + v_0(t) + \sum_{n=1}^{\infty} \left(v_n(t) + u_0(t_{on})e^{-\left(\frac{\pi nn}{L}\right)^2}\right)\cos\left(\frac{\pi nx}{L}\right), & t \ge t_{on} \end{cases} \qquad g_n = \frac{2}{L} \int_{0}^{t} g(\xi) \cos\left(\frac{\pi n\xi}{L}\right) d\xi$$

$$u_0(t) = \frac{g_0}{2} \left[ t + t_F \left(2e^{-\frac{t}{t_F}} - \frac{1}{2}e^{-\frac{2t}{T_F}} - \frac{3}{2}\right) \right] \qquad v_0(t) = \frac{g_0 t_F}{4} \left(1 - e^{-\frac{t}{t_F}}\right)^2 \left(1 - e^{-\frac{2t}{T_F}}\right)$$

$$u_n(t) = \frac{g_n \left(1 - e^{-\frac{\pi nn}{T_F}}\right)^2}{\left(\frac{\pi nn}{L}\right)^2 - \frac{2}{t_F}} \left(e^{-\left(\frac{\pi nn}{T_F}\right)^2}\right) + \frac{2g_n}{\left(\frac{\pi nn}{T_F}\right)^2 - \frac{1}{t_F}} \left(e^{-\left(\frac{\pi nn}{T_F}\right)^2}t - e^{-\frac{t}{t_F}}\right)$$





### RF pulse heating

Now, it can be estimated the temperature rise in the photoinjector surfaces for an RF pulse with 200 MV/m at cathode at the stationary state



Magnetic field at the gun surfaces as a function of the axial position for 1 MV/m at cathode

- Maximum temperature rise  $max(\Delta T) = 31^{\circ}C$ (for a pulse length of  $t_p = 400 \text{ ns}$ )
- This value is below 50°C, which is the maximum temperature rise suggested by Avni
- Other authors suggest a 60°C maximum increase<sup>1</sup>

Temperature rise along the RF gun surfaces



Maximum temperature increase in the RF gun as a function of time



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- > Despite the RF gun has been designed for operation with the  $\pi$ -mode, other neighbour modes present in the cavity might be excited during the transient regime
- To calculate the excitation of these neighbor modes, it is useful to use a equivalent circuital model to describe the mode excitation in the system composed by the RF generator, the coupler and the RF gun cavity<sup>1,2</sup>

$$\frac{\omega_m}{Q_0} \sqrt{\frac{\beta R}{Z_0}} V_{rf}(t) = \frac{dV_{cav}}{dt} + \frac{\omega_m}{Q_L} V_{cav} + \omega_m^2 \int V_{cav} dt$$
$$V_{cav}(t) = V_{cav,0} \left[ \sin(\omega t + \varphi_1) - \frac{e^{-\frac{\omega_m}{2Q_L}t}}{\sqrt{1 - \frac{1}{4Q_L^2}}} \sin\left(\omega_m \sqrt{1 - \frac{1}{4Q_L^2}}t + \varphi_2\right) \right]$$

$$V_{cav,0} = V_{rf,0} \frac{\omega_m \omega}{Q_0} \sqrt{\frac{\beta R}{Z_0}} \frac{1}{\sqrt{\left(\frac{\omega \omega_m}{Q_L}\right)^2 + (\omega_m^2 - \omega^2)^2}}$$



Equivalent circuit describing the RF generator, coupler and gun cavity (extracted from ref. 1)

$$\tan \varphi_1 = Q_L \frac{\omega_m - \omega}{\omega \omega_m}$$
$$\tan \varphi_2 = \sqrt{4Q_L^2 - 1} \frac{\omega_m^2 - \omega^2}{\omega_m^2 + \omega^2}$$

 $(\omega^2 - \omega^2)$ 

 $\beta$  is the coupling factor  $\omega$  is the RF generator angular frequency

 $\omega_m$  is the cavity mode angular frequency R is the circuit resistance

 $Q_L$  is the loaded cavity quality factor  $Q_0$  is the unloaded cavity quality factor  $Z_0$  is the high power transfer line impedance  $V_{rf}$  is the RF generator voltage

 $V_{rf}$  is the RF voltage in the gun cavity

<sup>1</sup>D. Alesini et al., "Design, realization, and high power test of high gradient, high repetition rate brazing-free S-band photogun", Physical Review Accelerators and Beams. 21, 112001 (2018)

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 $V_{cav}(t) \simeq V_{cav,0}[\sin(\omega t + \varphi_1)]$ 

<sup>2</sup> Thomas P. Wangler, "RF Linear Accelerators", Second Edition, 2008 WILEY-VCH Verlag GmbH & Co. KGaA

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For  $t >> \frac{\omega_m}{2Q_L}$ 







> Thus, the axial RF electric field of the mode cavity m is given by

 $E_{z,m}(z,t) = E_{0,cath,m}(t) g_m(z)$ 

and the total RF axial electric field in the RF gun due to the superposition of N cavity modes is obtained by means of the linear superposition of them:

$$E_{z}(z,t) = \sum_{i=1}^{N} E_{z,m}(z,t) = \sum_{i=1}^{N} E_{0,cath,m}(t) g_{m}(z)$$

For the RF gun, consisting of six cells, there will be five neighbor modes near the operating  $\pi$ -mode that could be excited, even if the RF generator excitation frequency perfectly matches the  $\pi$ -mode frequency

mode	f <sub>m</sub> (GHz)	Q <sub>L,m</sub>	β <sub>m</sub>	α <sub>m</sub> (Vm <sup>-1</sup> W <sup>-0.5</sup> )	
π	11.993996	4238.51	1.00477	42207.155	$E_{0,cath,m} \propto \frac{\omega_m \omega}{\sqrt{\left(\frac{\omega \omega_m}{Q_L}\right)^2 + (\omega_m^2 - \omega^2)^2}}$
1	11.9669	2927.36	1.816202	60021.928	
2	11.896	3411.46	1.405519	63107.831	
3	11.809	4447.77	0.8362	66482.625	
4	11.730	6115.44	0.3414	35850	
5	11.681	7924.16	0.0722	48378.9	

The amplitude of the excited modes decay as the mode resonant frequency moves away from the RF generator excitation frequency

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Since SUPERFISH provides  $g_m(z)$  for each cavity mode, the total RF electric field (due to the superimposition of modes)  $\geq$ along the gun axis can also be obtained:





For 
$$t \gg \frac{\omega_m}{2Q_L}$$
  $\longrightarrow$   $E_z(z,t) = \sum_{i=1}^N E_{0,cath,m} \sin(\omega t + \varphi_m) g_m(z)$ 













0.2

2 3



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z (cm) RF electric field along the gun only for  $\pi$ -mode

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- The consideration of the neighbor mode has revealed a slight distortion of the RF electric field profile (specially at the last gun cavities) from the original design goal, i.e., all cavities with the same maximum RF electric field amplitude
- Thus, a re-design of the RF gun taking the nearest neighbor mode has to be performed in order to correct such RF electric field distortion. After this, the following RF gun design arises:







## Summary

The RF electric and magnetic fields patterns along the device surfaces are compared with regard to the previous RF gun design (which was analyzed considering only the presence of the  $\pi$ -mode)





- It is observed that the RF electromagnetic pattern is the same for both RF gun designs
- Consequently, the results from the previous design involving the RF electromagnetic fields at surfaces (RF pulse heating, RF breakdown, multipactor) will still be valid for the new gun design















### Summary

> In this slide is summarized the performance of the 5.6 cell X-band RF gun prototype

Parameter			
E <sub>z</sub> flatness at peaks	>99 %		
Resonant frequency, $f_{\pi}$	11.9940380 GHz		
Mode separation, $\Delta f$	27.1 MHz		
Coupling factor, β	1.027		
Filling time, t <sub>F</sub>	112.5 ns		
$max(E_{surf})$ for 1 MV/m at cathode	0.988 MV/m		
BDR (for 400 ns pulse length)	$5.59 \times 10^{-6}  bpp/m$		
RF pulse heating (for 400 ns pulse length), max(Δ <i>T</i> )	31°C		
Multipactor power zones	0.035-0.560 MW, 1.20-3.10 MW		











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#### Future work

- We will perform beam dynamics simulations with the General Particle Tracer<sup>1</sup> (GPT) software in order to study the beam performance in the 5.6 cell RF gun photoinjector
- > It will be designed the solenoid for both emittance compensation and multipactor mitigation purposes
- A 4.6 cell RF gun photoinjector option will be designed, and its beam performance will be compared with the case of the 5.6 cell RF gun







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# Thank you!



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#### Convergence analysis

> The convergence of the solution is checked by essaying different mesh size increments



DX, DY are the mesh increments along the z and r directions, respectively

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- > Despite the RF gun has been designed for operation with the  $\pi$ -mode, other neighbour modes present in the cavity might be excited during the transient regime
- To calculate the excitation of these neighbor modes, it is useful to use a equivalent circuital model to describe the mode excitation in the system composed by the RF generator, the coupler and the RF gun cavity<sup>1,2</sup>

$$\frac{\omega_m}{Q_0} \sqrt{\frac{\beta R}{Z_0}} V_{rf}(t) = \frac{dV_{cav}}{dt} + \frac{\omega_m}{Q_L} V_{cav} + \omega_m^2 \int V_{cav} dt$$

$$\mathcal{L}\{V_{cav}(t)\} = \frac{\omega_m}{Q_0} \sqrt{\frac{\beta R}{Z_0}} \frac{s}{\left(s + \frac{\omega_m}{2Q_L}\right)^2 + \omega_m^2 \left(1 - \frac{1}{4Q_L^2}\right)} \mathcal{L}\{V_{rf}(t)\}$$

$$V_{rf}(t) = V_{rf,0}\sin(\omega t)H(t) \longrightarrow \mathcal{L}\left\{V_{rf}(t)\right\} = V_{rf,0}\frac{\omega}{s^2 + \omega^2}$$



Equivalent circuit describing the RF generator, coupler and gun cavity (extracted from ref. 1)

 $\beta$  is the coupling factor  $\omega$  is the RF generator angular frequency  $\omega_m$  is the cavity mode angular frequency

R is the circuit resistance

 $Q_{I}$  is the loaded cavity quality factor

 $Q_0$  is the unloaded cavity quality factor

 $Z_0$  is the high power transfer line impedance

- V<sub>rf</sub> is the RF generator voltage
- $V_{cav}$  is the RF voltage in the gun cavity
- $\mathcal{L}$  is the Laplace transform operator

<sup>1</sup>D. Alesini et al., "Design, realization, and high power test of high gradient, high repetition rate brazing-free S-band photogun", Physical Review Accelerators and Beams. 21, 112001 (2018)

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<sup>2</sup> Thomas P. Wangler , "RF Linear Accelerators", Second Edition, 2008 WILEY-VCH Verlag GmbH & Co. KGaA

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 $\mathcal{L}\{V_{cav}(t)\} = V_{rf,0} \frac{\omega \omega_m}{Q_0} \sqrt{\frac{\beta R}{Z_0}} \frac{s}{(s^2 + \omega^2) \left[\left(s + \frac{\omega_m}{2Q_L}\right)^2 + \omega_m^2 \left(1 - \frac{1}{4Q_L^2}\right)\right]} \mathcal{L}\{V_{rf}(t)\}$ 









Finally the RF voltage for the m-mode at the gun cavity is  $\geq$ 

 $\omega$  is the RF generator angular frequency  $\omega_{\rm m}$  is the cavity mode angular frequency

$$V_{cav}(t) = V_{cav,0} \left[ \sin(\omega t + \varphi_1) - \frac{e^{-\frac{\omega_m t}{2Q_L}t}}{\sqrt{1 - \frac{1}{4Q_L^2}}} \sin\left(\omega_m \sqrt{1 - \frac{1}{4Q_L^2}}t + \varphi_2\right) \right]$$

$$V_{cav,0} = V_{rf,0} \frac{\omega_m \omega}{Q_0} \sqrt{\frac{\beta R}{Z_0}} \frac{1}{\sqrt{\left(\frac{\omega \omega_m}{Q_L}\right)^2 + (\omega_m^2 - \omega^2)^2}}}{\sin\left(\sqrt{\frac{\omega_m \omega_m}{Q_L}}\right)^2 + (\omega_m^2 - \omega^2)^2}$$

$$\tan \varphi_1 = Q_L \frac{\omega_m^2 - \omega^2}{\omega\omega_m} \qquad \tan \varphi_2 = \sqrt{4Q_L^2 - 1} \frac{\omega_m^2 - \omega^2}{\omega_m^2 + \omega^2}$$

 $\geq$ The RF cavity voltage can be related to the RF electric field amplitude at cathode

 $E_z(r = 0, z) = E_z(z) = E_{0,cath} g(z)$  ,  $g(z) \mid g(0) = 1$ 





> Using the previous expressions, the time variation of the RF electric field at cathode can be depicted as it is shown next:





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To validate the previous results obtained from SUPERFISH plus the circuital model treatment, a comparison with the results obtained from HFSS simulations is presented:





3D view of the RF gun with HFSS

It is evidenced the good agreement between the results obtained from HFSS and with SUPERFISH using the circuital model treatment

















#### RF power system











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