

# Benchmarks for $hh$ , $hS$ , $SS$

Ian Lewis  
University of Kansas

Based on work by **I. Lewis**, M. Sullivan

C-Y. Chen, S. Dawson, **I. Lewis** PRD91 (2015) 035015; **I. Lewis**, M. Sullivan PRD96 (2017) 035037  
S. Dawson, M. Sullivan PRD97 (2018) 015022

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# Singlet Extensions of SM

- Consider two extensions of the SM:
  - Real singlet scalar.
  - Complex singlet scalar.
- Only couple to Higgs doublet at the renormalizable level.
- Useful laboratory to learn what Higgs physics can tell us about BSM, without showing up anywhere else.
- Can give a strong first order electroweak phase transition. See for example [JHEP 1708 \(2017\) 098](#) for importance of  $hS$  and  $SS$  production to probe the electroweak phase transition.

# Real Singlet Extension

- Based on C-Y. Chen, S. Dawson, I. Lewis PRD91 (2015) 035015; I. Lewis, M. Sullivan PRD96 (2017) 035037
- Extend the SM with a real, gauge singlet scalar  $S$ .
- Two largely studied scenarios:
  - $Z_2$  symmetric: impose  $S \rightarrow -S$  symmetry. See Robens, Stefaniak EPJC76 (2016) 268; EPJC75 (2015) 104; etc.
  - No additional  $Z_2$ .
- We study the case with no additional  $Z_2$ . Most general renormalizable scalar potential:

$$V(\Phi, S) = -\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2 + \frac{a_1}{2} \Phi^\dagger \Phi S + \frac{a_2}{2} \Phi^\dagger \Phi S^2 + b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

- Free to choose  $\langle S \rangle = 0$ .
- Rotate to mass eigenstates  $h_1, h_2$  with masses  $m_1 = 125$  GeV and  $m_2$ , respectively:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ S \end{pmatrix}$$

# Real Singlet Extension

- Parameter counting:

- 8 parameters in Lagrangian.
- 5 “physical” parameters:

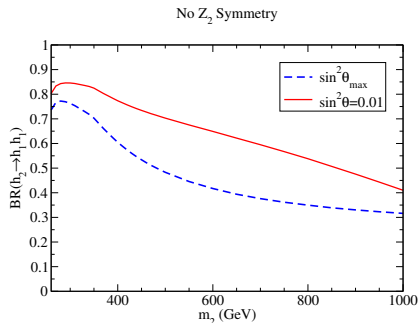
$$m_1 = 125 \text{ GeV}, m_2, \theta, v = 246 \text{ GeV}, \langle S \rangle = 0$$

- 3 leftover “free” parameters:

$$a_2, b_3, b_4.$$

- In  $Z_2$  symmetric limit:  $a_1 = b_1 = b_3 = 0$ .
  - 5 parameters in Lagrangian and 5 “physical” parameters. Fully determined.
- Vacuum structure is more complicated without  $Z_2$ .
  - Places constraints on how large  $\text{BR}(h_2 \rightarrow h_1 h_1)$  can be.
- Relevant theoretical constraints:
  - Make sure the global minimum is  $(v, \langle S \rangle) = (246 \text{ GeV}, 0)$ .
  - Checked that  $2 \rightarrow 2$  scalar scattering obeys perturbative unitarity.
  - Potential is bounded from below.

# Real Singlet Model-Benchmarks for $S \rightarrow hh$



- Maximum allow branching ratio for  $h_2 \rightarrow h_1 h_1$
- From Higgs precision:  $\sin \theta_{\max} = 0.22$  for  $m_2 < 650$  GeV.
- From  $W$ -mass constraints:  $\sin \theta_{\max} = 0.21$  for  $m_2 > 650$  GeV  
[López-Val, Robens PRD90 \(2014\) 114018](#)
- Production rates:

$$\sigma(pp \rightarrow h_1) = \cos^2 \theta \sigma_{SM}(pp \rightarrow h_1)$$

$$\sigma(pp \rightarrow h_2) = \sin^2 \theta \sigma_{SM}(pp \rightarrow h_2)$$

# Complex Singlet Model

- Much more complicated. The potential with no additional symmetries:

$$\begin{aligned} V(\Phi, S_c) &= \frac{\mu^2}{2} \Phi^\dagger \Phi + \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 + \frac{b_2}{2} |S_c|^2 + \frac{d_2}{4} |S_c|^4 + \frac{\delta_2}{2} \Phi^\dagger \Phi |S_c|^2 \\ &+ \left( a_1 S_c + \frac{b_1}{4} S_c^2 + \frac{e_1}{6} S_c^3 + \frac{e_2}{6} S_c |S_c|^2 + \frac{\delta_1}{4} \Phi^\dagger \Phi S_c + \frac{\delta_3}{4} \Phi^\dagger \Phi S_c^2 \right. \\ &\left. + \frac{d_1}{8} S_c^4 + \frac{d_3}{8} S_c^2 |S_c|^2 + \text{h.c.} \right) \end{aligned}$$

- Complex scalar singlet:  $S_c = (S_0 + iA)/\sqrt{2}$ .
- Can choose  $\langle S_c \rangle = 0$ .
- $a_1, b_1, e_2, e_2, \delta_1, \delta_3, d_1, d_3$  are complex parameters.
- See [Barger, Langacker, McCaskey, Ramsey-Musolf, Shaughnessy PRD79 \(2009\) 015018](#); [Coimbra, Sampaio, Santos, EPJC73 \(2013\) 248](#); [Gonderinger, Lim, Ramsey-Musolf PRD86 \(2012\) 043511](#); [Costa, Mülleitner, Sampaio, Santos JHEP06 \(2016\) 034](#) for analysis when additional symmetries are imposed upon  $S_c$ .

# Complex Singlet Model

- Three CP-even scalar bosons:  $h, S_0, A$ .
- In principle have to mix all three according to  $SO(3)$ .
  - Three mixing angles:  $\theta_1, \theta_2, \theta_3$ .
- $\theta_3$  is the mixing between  $S_0, A$ .
  - Equivalent to a phase rotation of  $S_c = (S_0 + iA)/\sqrt{2}$ .
  - Can be absorbed into the complex parameters.
- Left over rotation matrix:

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} \cos \theta_1 & -\sin \theta_1 & 0 \\ \sin \theta_1 \cos \theta_2 & \cos \theta_1 \cos \theta_2 & \sin \theta_2 \\ \sin \theta_1 \sin \theta_2 & \cos \theta_1 \sin \theta_2 & -\cos \theta_2 \end{pmatrix} \begin{pmatrix} h \\ S_0 \\ A \end{pmatrix}$$

- $h_1, h_2, h_3$  are mass eigenstates with masses  $m_1 = 125 \text{ GeV}, m_2, m_3$ , respectively.

# Complex Singlet Model

- Left over rotation matrix:

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} \cos \theta_1 & -\sin \theta_1 & 0 \\ \sin \theta_1 \cos \theta_2 & \cos \theta_1 \cos \theta_2 & \sin \theta_2 \\ \sin \theta_1 \sin \theta_2 & \cos \theta_1 \sin \theta_2 & -\cos \theta_2 \end{pmatrix} \begin{pmatrix} h \\ S_0 \\ A \end{pmatrix}$$

- In the limit  $\theta_2 \rightarrow 0$ :

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} \cos \theta_1 & -\sin \theta_1 & 0 \\ \sin \theta_1 & \cos \theta_1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} h \\ S_0 \\ A \end{pmatrix}$$

- $h_3$  inherits its couplings to fermions and gauge bosons from the SM Higgs.
  - If  $\theta \rightarrow 0$  no mixing with SM Higgs, hence no couplings to fermions or gauge bosons.
  - $h_3$  can only be produced from  $h_2$  or  $h_1$ .
  - If  $m_2 > 2m_3$  and  $m_2 > m_1 + m_3$  then major discovery mode of  $h_3$  are:

$$h_2 \rightarrow h_3 h_3 \text{ and } h_2 \rightarrow h_1 h_3.$$

- Why this is an interesting benchmark.



# Complex Singlet Model

- Major theory constraints:
  - Make sure the global minimum is  $(v, \langle S_c \rangle) = (246 \text{ GeV}, 0 + i0)$ .
  - Checked that  $2 \rightarrow 2$  scalar scattering obeys perturbative unitarity.
  - Potential is bounded from below.
- The width of  $h_2$  can be very large, comparable to the mass of  $h_2$   
[S. Dawson, M. Sullivan PRD97 \(2018\) 015022](#)
  - We demand that  $h_2$  be narrow and fix:

$$\Gamma(h_2)/m_2 = 10\%$$

- Find benchmarks by maximizing the branching ratios of  $h_2 \rightarrow h_3 h_3$  or  $h_2 \rightarrow h_1 h_3$  with the above constraints.
- Production rate of  $h_2$ :

$$\sigma(pp \rightarrow h_2) = \sin^2 \theta_1 \sigma_{SM}(pp \rightarrow h_2)$$

- Constraints on  $\theta_1$  are the same as the constraints on  $\theta$  in the real singlet model.

# Complex Singlet-Benchmarks for $hS$ production

$\sin \theta_1$	$m_2$ (GeV)	$\text{BR}(h_2 \rightarrow h_1 h_3)$	Parameters
0.22	400	0.966	$\delta_2 = 0.962, \delta_3 = 0.289 - 0.488 i, e_1/v = -2.94 + 23 i, e_2/v = -9.15 + 4.42 i$
0.22	500	0.938	$\delta_2 = 4.15, \delta_3 = -1.06 + 2.82 i, e_1/v = -1.91 + 40.9 i, e_2/v = -8.21 - 3.43 i$
0.22	600	0.909	$\delta_2 = 5.16, \delta_3 = 2.84 + 3.77 i, e_1/v = 2.38 + 44.8 i, e_2/v = 6.02 + 7.45 i$
0.22	700	0.876	$\delta_2 = 8.07, \delta_3 = 1.78 + 5.04 i, e_1/v = 2.24 + 55 i, e_2/v = 3.71 + 2.23 i$
0.1	400	0.993	$\delta_2 = 6.47, \delta_3 = -2.77 - 3.22 i, e_1/v = 2.41 + 38.8 i, e_2/v = 5.27 - 7.42 i$
0.1	500	0.987	$\delta_2 = 4.02, \delta_3 = 0.125 - 2.14 i, e_1/v = -1.63 + 52.4 i, e_2/v = -5.71 + 6.19 i$
0.1	600	0.981	$\delta_2 = 16.3, \delta_3 = -9.45 + 9 i, e_1/v = 2.39 + 141 i, e_2/v = 1.70 + 7.81 i$
0.1	700	0.974	$\delta_2 = 8.03, \delta_3 = 1.5 + 1.5 i, e_1/v = 3.31 + 106 i, e_2/v = 8.55 - 9.68 i$

**Table:** Benchmark points in the complex singlet model with large  $\text{BR}(h_2 \rightarrow h_1 h_3)$  for  $m_3 = 130 \text{ GeV}$  and  $\Gamma_2/m_2 = 0.1$ . Other parameters are set to  $\theta_2 = 0, d_1 = 0.1 + 0.1 i, d_2 = 0.4,$  and  $d_3 = 0.1 + 0.1 i$ .

# Complex Singlet-Benchmarks for $SS$ production

$\sin\theta_1$	$m_2$ (GeV)	$\text{BR}(h_2 \rightarrow h_3 h_3)$	Parameters
0.22	400	0.966	$\delta_2 = 0.42$ , $\delta_3 = -0.356 - 0.0186i$ , $e_1/v = -11.5 + 2.63i$ , $e_2/v = -9.71 - 8.05i$
0.22	500	0.938	$\delta_2 = 11$ , $\delta_3 = -5.76 + 8.87i$ , $e_1/v = -4.63 + 27.2i$ , $e_2/v = 7.47 - 2.35i$
0.22	600	0.909	$\delta_2 = 7.92$ , $\delta_3 = 1.49 + 7.57i$ , $e_1/v = 13.5 + 23.8i$ , $e_2/v = 3.75 - 3.81i$
0.22	700	0.876	$\delta_2 = 7.44$ , $\delta_3 = 0.277 + 5.54i$ , $e_1/v = -10.5 + 17.6i$ , $e_2/v = 3.20 - 3.42i$
0.1	400	0.993	$\delta_2 = 4.4$ , $\delta_3 = -2.39 + 3.05i$ , $e_1/v = -10.1 + 21.7i$ , $e_2/v = -6.59 - 1.36i$
0.1	500	0.987	$\delta_2 = 2.83$ , $\delta_3 = 2.08 - 1.91i$ , $e_1/v = 8.54 - 13.6i$ , $e_2/v = -4.09 + 0.887i$
0.1	600	0.981	$\delta_2 = 12.4$ , $\delta_3 = -4.54 - 5.99i$ , $e_1/v = 14.3 - 42.6i$ , $e_2/v = 4.98 + 2.76i$
0.1	700	0.974	$\delta_2 = 11.9$ , $\delta_3 = -4.71 + 10.3i$ , $e_1/v = -14.2 + 73i$ , $e_2/v = -6.77 - 3.94i$

**Table:** Benchmark points in the complex singlet model with large  $\text{BR}(h_2 \rightarrow h_3 h_3)$  for  $m_3 = 130$  GeV and  $\Gamma_2/m_2 = 0.1$ . Other parameters are set to  $\theta_2 = 0$ ,  $d_1 = 0.1 + 0.1i$ ,  $d_2 = 0.4$ , and  $d_3 = 0.1 + 0.1i$ .

# Thank You