# Measurement of tt+bb and news on its simulation

HELMHOLTZ RESEARCH FOR GRAND CHALLENGES

#### May 28th 2019, LHC Top Working Group Meeting Judith Katzy on behalf of ATLAS







### Motivation

- tt+HF tt+Heavy Flavour production is large and irreducible background limiting the precision of ttH (H->bb) measurements and searches.
- In the most signal like region, signal yields are ~20% over 80% ttbb background; only ~5-8% of all ttbb events are in this region
  - low uncertainty on the background modelling in total and in the tails of the differential distributions is mandatory to measure ttH signal
- Provide measurements to better understand QCD HF production; constrain MC models for ttbb
- Depending on the signal region definition, tt+light and tt+charm jets are non-negligible background
  - Development in simulation: Inclusive prediction of jet production in top pair events including precise b-pair production desired







#### What are the theoretical difficulties to calculate tt+HF?

- Complex calculations:
  - >= 8 parton final state
  - >= 6 colored partons
- Multiple scales between 5 GeV and 500 GeV
- Large scale dependence •



Different approaches to predict full events:

- •

tt ME@NLO + g->bb in PS (5FS)

tt+0,1,2 ME@NLO massless b-quarks (5FS)

ttbb ME@NLO with massive b-quarks (4FS)

Fusing of 4FS and 5FS



### Observables to separate ttbb from ttH(H->bb)

- - good description of full event important

Variable	Definition	$SR_1^{\geq 4j}$	$SR_2^{\geq 4j}$	$SR_3^{\geq 4j}$
General kinematic variables				
$m_{bb}^{\min}$	Minimum invariant mass of a <i>b</i> -tagged jet pair	√	$\checkmark$	-
$m_{bb}^{\rm max}$	Maximum invariant mass of a <i>b</i> -tagged jet pair	-	-	V
$m_{bb}^{\min\Delta R}$	Invariant mass of the <i>b</i> -tagged jet pair with minimum $\Delta R$	$\checkmark$	-	$\checkmark$
$m_{ii}^{max p_{T}}$	Invariant mass of the jet pair with maximum $p_{\rm T}$	$\checkmark$	-	-
$m_{bb}^{\max p_{\mathrm{T}}}$	Invariant mass of the <i>b</i> -tagged jet pair with maximum $p_{\rm T}$	$\checkmark$	-	$\checkmark$
$\Delta \eta^{ m avg}_{bb}$	Average $\Delta \eta$ for all <i>b</i> -tagged jet pairs	$\checkmark$	$\checkmark$	$\checkmark$
$\Delta \eta_{\ell,i}^{\max}$	Maximum $\Delta\eta$ between a jet and a lepton	-	$\checkmark$	$\checkmark$
$\Delta R_{bb}^{\max p_{\mathrm{T}}}$	$\Delta R$ between the <i>b</i> -tagged jet pair with maximum $p_{\rm T}$	-	$\checkmark$	$\checkmark$
$N_{bb}^{ m Higgs~30}$	Number of <i>b</i> -tagged jet pairs with invariant mass within 30 GeV of the Higgs-boson mass	$\checkmark$	$\checkmark$	-
$n_{\text{jets}}^{p_{\text{T}}>40}$	Number of jets with $p_{\rm T} > 40 \text{ GeV}$	-	$\checkmark$	$\checkmark$
Aplanarity <sub>b-jet</sub>	1.5 $\lambda_2$ , where $\lambda_2$ is the second eigenvalue of the momentum tensor [99] built with all <i>b</i> -tagged jets	-	$\checkmark$	-
$H_{ m T}^{ m all}$	Scalar sum of $p_{\rm T}$ of all jets and leptons	-	-	$\checkmark$

#### **BDT** dilepton channel

#### Measure these observables at particle level

Known separating features between tt+HF and ttHbb are dR between b-jets, mass of bb system and HT

ML algorithm may also pick-up on correlations between observables and on particular event topologies

Variable	Definition	$SR_{1,2,3}^{\geq 6j}$	SR <sup>5j</sup> <sub>1,2</sub>	
General kiner	General kinematic variables			
$\Delta R_{bb}^{ m avg}$	Average $\Delta R$ for all <i>b</i> -tagged jet pairs	$\checkmark$	$\checkmark$	
$\Delta R_{bb}^{\max p_{\mathrm{T}}}$	$\Delta R$ between the two <i>b</i> -tagged jets with the largest vector sum $p_{\rm T}$	$\checkmark$	_	
$\Delta \eta_{ m jj}^{ m max}$	Maximum $\Delta \eta$ between any two jets	$\checkmark$	$\checkmark$	
$m_{bb}^{\min \Delta R}$	Mass of the combination of two <i>b</i> -tagged jets with the smallest $\Delta R$	$\checkmark$	_	
$m_{ m jj}^{ m min\;\Delta R}$	Mass of the combination of any two jets with the smallest $\Delta R$	_	$\checkmark$	
$N_{bb}^{\text{Higgs 30}}$	Number of <i>b</i> -tagged jet pairs with invariant mass within 30 GeV of the Higgs-boson mass	$\checkmark$	$\checkmark$	
$H_{ extsf{T}}^{ extsf{had}}$	Scalar sum of jet $p_{\rm T}$	—	$\checkmark$	
$\Delta R^{ m min}_{\ell,bb}$	$\Delta R$ between the lepton and the combination of the two <i>b</i> -tagged jets with the smallest $\Delta R$	_	$\checkmark$	
Aplanarity	1.5 $\lambda_2$ , where $\lambda_2$ is the second eigenvalue of the momentum tensor [99] built with all jets	$\checkmark$	$\checkmark$	
$H_1$	Second Fox–Wolfram moment computed using all jets and the lepton	$\checkmark$	$\checkmark$	

BDT I+jets channel



## Angular distribution of gluon splitting

- The angular distributin of gluon splitting may have significant experimental effects:
  - For DR(bb)->0 both additional b-quarks (B-hadrons) might be contained in one jet "ttB"
  - Large DR g->bb splitting may lead to b-jet due to loss of the other b-jet outside detector acceptance "ttb"
- Different topologies of additional b-jets have different separation power in ttHbb (e.g. ttB more signal like, ttb more background like)
- Measurement of xsec for >= 3b and >=4b









## ttbb measurement @ 13 TeV

Measure b-jet pair production in ttbar events without selecting production channel or identifying b-jets origin

#### em-channel:

- e, m with pT>27GeV, OS, b-jets @ 77% WP, b-jet pT>25 GeV
- Very low background
- differential measurements in 3b



#### Lepton+jets channel:

- exactly 1 e or m with pT>27GeV, 5 jets with pT>25 GeV, b-jets@60% WP
- background for additional b-jets from W->cs decays
- high stats to measure differential distributions in 4b





#### ttbb measurement @ 13 TeV

em-channel

Experimental uncertainties on b-jets ~10%



Lepton+jets channel:

Experimental uncertainties on b-jet ~15-20%





## Determination of flavour of additional jets

- Perform binned likelihood template fit to determine background from tt+jets and tt+charm
- Categorise events according to particle level jets into templates of ttc, ttl, ttb and background



$$\nu_k(\alpha_b,\alpha_{cl}) = \alpha_b N_{t\bar{t}b}^k + \alpha_{cl} \left( N_{t\bar{t}c}^k + N_{t\bar{t}l}^k \right) + N_{\text{non-}t\bar{t}}^k$$

- Fit performed in measurement phase space
- Uncertainty from variation of ttc template by 40% => systematic uncertainty of  $a_b=11\%$ ,  $a_{cl}=7\%$

B-tagging efficiency known from calibration but mistag efficieny for charm- and light-jets and xsec for ttcc poorly known

b-tag bins: efficiency 1:100-85% 2: 85-77% 3: 77-70% 4: 70-60% 5: 60- 0%



 $v_k(\alpha_b, \alpha_c, \alpha_l) = \alpha_b N_{t\bar{t}b}^k + \alpha_c N_{t\bar{t}c}^k + \alpha_l N_{t\bar{t}l}^k + N_{\text{non-}t\bar{t}}^k$ 

- Fit performed in all b-tagging bins
- Systematic uncertainty from varying MC models for templates



### Reconstruction level distributions with flavour scale factors



Good agreement with data also in differential distributions of measured phase space



## Unfolding

- Unfolding is done in fiducial phase space to stable final state particles with life time >30ps.
- Signal consists of QCD production of ttbb+ttHbb+ttVbb



Final state leptons and jets are required to have pT>25GeV and letal<2.5, b-jets are defined as containing a B-hadron with pT> 5GeV

$$f_{\text{matching}}^{j} f_{\text{accept}}^{j} f_{t\bar{t}b}^{j} (N_{\text{data}}^{j} - N_{\text{non-}t\bar{t}\text{-}\text{bkg}}^{j})$$

$$f_{t\bar{t}b}^{j} = \frac{\alpha_{b} N_{t\bar{t}b,\text{reco}}^{j}}{\alpha_{b} N_{t\bar{t}b,\text{reco}}^{j} + \mathcal{B}^{j}}$$

$$\begin{array}{c} \text{em channel} \\ \mathcal{B}^{j} = \alpha_{cl} \left( N_{t\bar{t}c,\text{reco}}^{j} + N_{t\bar{t}l,\text{reco}}^{j} \right) \\ \mathcal{B}^{j} = \alpha_{c} N_{t\bar{t}c,\text{reco}}^{j} + \alpha_{l} N_{t\bar{t}l,\text{reco}}^{j} \end{array}$$





#### Uncertainties

Estimate detector effects from varying input distributions and performing flavour fit+unfolding

Estimate modelling uncertainties by replacing MC but keeping unfolding corrections from nominal MC; take particle level difference to nominal sample

> Powheg+Pythia8 vs Powheg+Herwig7 Powheg+Pythia8 vs Sherpa 2.2.1 Powheg+Pythia8 RadHi/RadLo

Xsec varied within measured uncertainties

Tota Tota

Measurement uncertainties dominated by systematics

Source	Fiducial cross-section phase space			
	$e\mu$		lepton	+ jets
	≥ 3 <i>b</i> unc. [%]	≥ 4 <i>b</i> unc. [%]	$\geq 5j, \geq 3b$ unc. [%]	$\geq 6j, \geq 4b$ unc. [%]
Data statistics	2.7	9.0	1.7	3.0
Luminosity	2.1	2.1	2.3	2.3
Jet	2.6	4.3	3.6	7.2
<i>b</i> -tagging	4.5	5.2	17	8.6
Lepton	0.9	0.8	0.8	0.9
Pile-up	2.1	3.5	1.6	1.3
$t\bar{t}c$ fit variation	5.9	11	-	-
Non- <i>tt</i> bkg	0.8	2.0	1.7	1.8
Detector+background total syst.	8.5	14	18	12
Parton shower	9.0	6.5	12	6.3
Generator	0.2	18	16	8.7
ISR/FSR	4.0	3.9	6.2	2.9
PDF	0.6	0.4	0.3	0.1
$t\bar{t}V/t\bar{t}H$	0.7	1.4	2.2	0.3
MC sample statistics	1.8	5.3	1.2	4.3
$t\bar{t}$ modelling total syst.	10	20	21	12
Total syst.	13	24	28	17
Total	13	26	28	17

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### Inclusive fiducial cross section



- MC Models of ttbb ME in 4FS predict lower xsec than data
- Effect is bigger for phase space with >=3b

Modelling of small angle gluon splitting (B-jets)? b-jet  $p_T$  too low? Missing ISR contributions?



## ttbb ME@NLO with massive b-quarks (4FS)

#### Advantage:

- ME@NLO calculation has less uncertainty than LO PS calculation
- Due to massive b-quarks soft gluon splitting doesn't have a singularity at collinear splittings
  - full phase space covered by ME
- Covers also double soft gluon splittings
  - estimated in Higgs region up to 30%



#### Caveat:

- $\alpha_{\rm S} \ln(m_{\rm b}/Q)$  terms that arise from IS g->bb splittings are not resummed through the PDF evolution.
  - ttHbb
- No prediction for the inclusive top pair production including additional light and charm jets

MGaMC@NLO 4F ttbb Matchbox+Herwig 4F ttbb Sherpa 4FS, 1309.5912 PowHel 4FS Powheg-Box-Res ttbb, 1802.00426

• Powheg study:  $\alpha_{s} \ln(m_{b}/Q)$  not relevant for low mass region, compensated by interference effects for H region in



## Further MC predictions for ttbb

#### tt ME@NLO + g->bb in PS

Large theoretical uncertainties due to additional b-quark production in LO PS

PS tuned to tt+jets, top pt,... ATLAS data with decent agreement in jet inclusive distributions

ATLAS samples:

- Powheg+Pythia8 (ttbar nominal, RadHi, RadLo)
- Powheg+Herwig7
- MC@NLO+Pythia8

#### (N)LO tt+0,1,2 ME + PS (5FS)

- ME calculation of QCD radiation more precise than PS
- $\alpha_{S} \ln(m_{b}/Q)$  terms from IS g->bb splittings are resummed through the PDF evolution
- Prediction inclusive in flavour of additional jets
- But even though ttbb (with  $m_b=0$ ) is available at ME, most events have b-jets from PS (study in 1802.00426)
- Gluon->bb typically softer than 1st and 2nd splitting
- At  $m_{bb} \sim m_H$  still almost 50% b-jets from PS (tt+0b)

ATLAS sample: Sherpa 2.2 (5FS)



## ATLAS ttbb measurements differential in b-jet multiplicity



- Powheg+Pythia8 and all other MC with b-quark production only from PS predicts too few additional b-jets(N<sub>b-jets</sub>>=3)
- >QCD scale in PS not able to fix this
- >Very good agreement over the full phase space for Sherpa 2.2 5FS based on ME with ttj@NLO + 4 partons@LO







## ATLAS: differential kinematic distributions, dilepton (>=3b)



> PowHel 5FS is excluded by the differential measurement >All other MC models agree with data and their variations is significantly less than the measurement uncertainty >Sherpa 2.2 tt (= 5FS) describes all ttbb observables well simultaneously (however predicts too many light jets)





#### Inclusive xsecs compared to Sherpa 5FS





## ATLAS differential kinematic distributions 4b (I+jets)



- Close to ttHbb signal region
- Normalised fiducial cross sections agree with all MC models
- Variations between models significantly smaller than experimental uncertainties



#### C models n experimental uncertainties



## Other ways to constrain models of g->bb splitting?

- Measure g->bb in a more "pure" event topology: Zbb
- Caveat: this process comes also with other production modes



Enhanced in Z+1b Used to determine b-quark PDF

ATLAS measurements @ 7 TeV prefer 4FS for Z+1b, 5FS for Z+b





Enhanced in Z+2b



## New algorithm: Fusing of 4FS + 5FS for HF production

#### Goal:

- Better description of ttbar with additional b and light jet radiation in ME => reduced uncertainty
- Description of tt+jets inclusive in jet flavour

#### Algorithm:

- 1. HFOR a la multi-leg merging:
  - Cluster fully showered event using reverse shower
  - Look at leading 2 emission:
    - Heavy flavour -> keep from ttbb+PS simulation
    - Light flavour -> keep from tt+jets MEPS@NLO simulation
    - => Sub(sub) leading g->bb splitting not from ttbb ME but from ttjjj ME or from PS
- 2. Embed ttbb as merged contribution to tt+jets MEPS@NLO
- 3. Match 4FS/5FS in a<sub>S</sub> and PDF

S.Höche, J.Krause, F.Siegert arXiv:1904.09382v1



## Probing fusing in Z+jets events

Control fragmentation component in Z+jets events and both components in Z+b-jets eventt



(a) The transverse momentum of the Z boson.

Algorithm to incorporate 4FS and 5FS calculations and smooth transition between them! 

S.Höche, J.Krause, F.Siegert arXiv:1904.09382v1



## Fusing algorithm for ttbb+ttjj predictions

- Direct component in fused sample: ttbb ME@NLO in 4FS component in fused sample Fragmentation component in fused sample: g->bb PS splitting and b-jets from tt+jets (mb=0) • Compare to tt+jets 5FS and ttbb 4FS standalone calculations



• At 1.5 < DR(bb) <2.5 (Higgs region) 80% direct component • At Higgs mass region still significant contributions from fragmentation component

#### J.Katzy, J.Krause, C.Pollard, F.Siegert<sup>22</sup> Work in progress



#### Fusing compared to ttbb measurement

Decayed tops, PS+hadronisation in Sherpa 2.2.6 



#### J.Katzy, J.Krause, C.Pollard, F.Siegert Work in progress



## Summary and Conclusion

- stats
  - uncertainties
- > Predictions of tt+HF involve many theoretical aspects
  - > New algorithm "fusing" applied to ttbb + tt+jets

explored experimentally and in phenomenology

>ttbb rare process, first differential measurements exist with 32fb-1 (ATLAS) and 2.3 fb-1 (CMS) but lack

>With full Run2 more observables are possible and improved analysis techniques will give smaller

>Constraining ttbb background for ttHbb is a challenging but not hopeless task with many new ideas to be







### **BACK-UP**



#### Monte Carlo samples

Generator sample	Process	Matching	Tune	Use
Powheg-Box v2 + Рутніа 8.210 MadGraph5_aMC@NLO + Рутніа 8.210	$t\bar{t}$ NLO $t\bar{t} + V/H$ NLO	POWHEG $h_{damp} = 1.5m_t$ MC@NLO	A14 A14	nom. nom.
Powheg-Box v2 + Pythia 8.210 RadLo Powheg-Box v2 + Pythia 8.210 RadHi Powheg-Box v2 + Herwig 7.01 Sherpa 2.2.1 <i>tī</i>	tī NLO tī NLO tī NLO tī +0,1 parton at NLO +2,3,4 partons at LO	POWHEG $h_{damp} = 1.5m_t$ POWHEG $h_{damp} = 3.0m_t$ POWHEG $h_{damp} = 1.5m_t$ MEPS@NLO	A14Var3cDown A14Var3cUp H7UE Sherpa	syst. syst. syst. syst.
MadGraph5_aMC@NLO + Pythia 8.210 Sherpa 2.2.1 <i>tībī</i> (4FS) PowHel + Pythia 8.210 (5FS) PowHel + Pythia 8.210 (4FS) Powheg-Box v2 + Pythia 8.210 <i>tībī</i> (4FS)	tī NLO tībb NLO tībb NLO tībb NLO tībb NLO	MC@NLO MC@NLO Powheg $h_{damp} = H_T/2$ Powheg $h_{damp} = H_T/2$ Powheg $h_{damp} = H_T/2$	A14 Sherpa A14 A14 A14	comp. comp. comp. comp.



### Binned Maximum Likelihood Fit

 $\mathcal{L}(\vec{\alpha}|x_1,\ldots,x_n)$ 

em channel

 $v_k(\alpha_b, \alpha_{cl}) = \alpha_b N_{t\bar{t}b}^k + \alpha_{cl} \left( N_{t\bar{t}c}^k + N_{t\bar{t}l}^k \right) + N_{\text{non-}t\bar{t}}^k$ 

$$f_n) = \prod_k^n \frac{e^{-\nu_k(\vec{\alpha})}\nu_k(\vec{\alpha})^{x_k}}{x_k!}$$

#### I+jets channel

$$v_k(\alpha_b, \alpha_c, \alpha_l) = \alpha_b N_{t\bar{t}b}^k + \alpha_c N_{t\bar{t}c}^k + \alpha_l N_{t\bar{t}l}^k + N_{\text{non-}t\bar{t}}^k$$



## Template fit event categorization

Table 4: Event categorisation (for the definition of the MC templates) based on the particle-level selections of *b*-jets, *c*-jets and light-flavour jets.

Category	eμ
tīb	$\geq 3 b$ -jets
tīc	$< 3 b$ -jets and $\geq 1 c$ -jet
tīl	events that do not meet above crite







## Unfolding

$$\frac{\mathrm{d}\sigma^{\mathrm{fid}}}{\mathrm{d}X^{i}} = \frac{N_{\mathrm{unfold}}^{i}}{\mathcal{L}\,\Delta X^{i}} = \frac{1}{\mathcal{L}\,\Delta X^{i}\,f_{\mathrm{eff}}^{i}}\sum_{j=1}^{N_{\mathrm{unfold}}^{i}} \sum_{j=1}^{N_{\mathrm{unfold}}^{i}} \sum_{j=1}^{N_$$

$$f_{t\bar{t}b}^{j} = \frac{\alpha_b N_{t\bar{t}b,\text{reco}}^{j}}{\alpha_b N_{t\bar{t}b,\text{reco}}^{j} + \mathcal{B}^{j}}$$

#### em channel

I+jets channel

 $\mathcal{B}^{j} = \alpha_{cl} \left( N^{j}_{t\bar{t}c,\text{reco}} + N^{j}_{t\bar{t}l,\text{reco}} \right)$ 

$$\mathcal{B}^{j} = \alpha_{c} N_{t\bar{t}c,\text{reco}}^{j} + \alpha_{l} N_{t\bar{t}l,\text{reco}}^{j}$$



$$f_{\text{accept}}^{j} = \frac{N_{t\bar{t}b,\text{reco} \text{part}}^{j}}{N_{t\bar{t}b,\text{reco}}^{j}}$$

 $\sum_{i} \mathcal{M}_{ij}^{-1} f_{\text{matching}}^{j} f_{\text{accept}}^{j} f_{t\bar{t}b}^{j} \left( N_{\text{data}}^{j} - N_{\text{non-}t\bar{t}-\text{bkg}}^{j} \right)$ 

$$f_{\text{matching}}^{j} = \frac{N_{t\bar{t}b, \text{reco} \text{part} \text{matched}}^{j}}{N_{t\bar{t}b, \text{reco} \text{part}}^{j}}$$

$$\sigma^{\text{fid}} = \int \frac{\mathrm{d}\sigma^{\text{fid}}}{\mathrm{d}X} \mathrm{d}X = \frac{\sum N_{\text{unfold}}^{i}}{\mathcal{L}}$$



#### ttbb vs tt+PS





Significant changes in light jet pt PS uncertainty doesn't cover the ttbb ME predictions

#### Ttbb PowHeg paper



Different ttbb ME@NLO calculations agree with each other





#### DRbb in Z+bb





#### Event yields 36 fb-1

Process	2	2 <i>b</i>	$\geq 3b$	$\geq 4b$
Signal $(t\bar{t} + t\bar{t}H + t\bar{t}V)$	74 400	±2900	3 200 ± 310	210 ± 29
tī	74 200	$\pm 2900$	$3100 \pm 310$	190 ± 29
tīH	45.3	± 6.6	$36.5 \pm 7.0$	$9.4 \pm 3.3$
$t\bar{t}V$	190	± 16	$33.5 \pm 6.7$	$4.4 \pm 2.2$
Background	3 1 5 0	± 810	$140 \pm 53$	$9.2 \pm 5.6$
Single top	2 4 6 0	± 540	$96 \pm 32$	$4.1 \pm 2.5$
NP and fake lep.	600	± 600	$43 \pm 43$	$5.1 \pm 5.1$
$Z/\gamma^*$ +jets	53	± 13	$1.3 \pm 0.3$	$0.07 \pm 0.02$
Diboson	38	± 20	$1.0 \pm 1.1$	< 0.01
Expected	77 600	± 3 000	3 320 ± 320	216 ± 30
Observed	76 425		3 809	267

Table 2: Predicted and observed  $e\mu$  channel event yields in 2b,  $\geq 3b$  and  $\geq 4b$  selections. The quoted errors are symmetrised and indicate total statistical and systematic uncertainties in predictions due to experimental sources.



#### MC predictions for ttbb





#### tt ME@NLO + g->bb in PS (5FS)

- Large theoretical uncertainties due to additional b-quark production in LO PS
- PS tuned to tt+jets, top pt,... ATLAS data with decent agreement in jet inclusive distributions

ATLAS nominal samples in this scheme (and CMS ttHbb samples):

- Powheg+Pythia8 (ttbar nominal + ttbar filtered for additional b-jet)
- Powheg+Herwig7
- MC@NLO+Pythia8





## (N)LO tt+0,1,2 ME + PS

Phenomenological study in PowHeg ttbb paper:

- Even though ttbb (with  $m_b=0$ ) is available at ME, most events have b-jets from PS
- Gluon->bb typically softer than 1st and 2nd splitting
- At  $m_{bb} \sim m_H$  still almost 50% b-jets from PS (tt+0b)



**Powheg ttbb paper** 

