

Proton Radius Measurement with Muonic Atoms

K. Ishida

RIKEN

Proton Radius Puzzle

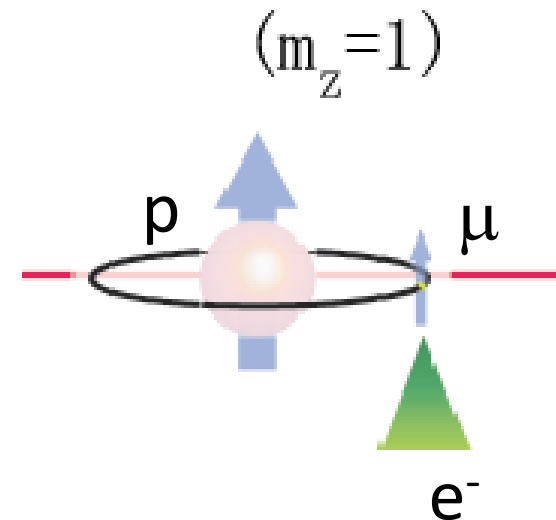
Muonic hydrogen atom (vs normal atom)

Zemach radius and hyperfine splitting

Plan of our measurement

Estimation

Progress and Status by S. Kanda



Proton size effect in atomic binding energy

Principle of radius measurement from atomic spectroscopy:

Finite charge distribution affects binding energy due to reduced attraction **while the electron/muon spends inside the nuclei**

$$\psi = 2 (Z/a_B)^{3/2} \exp(-Zr/a_B) e^{i\phi}$$

(Z: atomic number, a_B Bohr radius)

Energy shift by reduced charge inside nuclei

$$\Delta E = \int_0^{a_N} [\psi H' \psi] d^3r \text{ (in 1st order)}$$

$$H' = 2Za_B R_Y [(-1/a_N + 1/r) + (r^2 - a_N^2)/2a_N^3]$$

(hard sphere model)

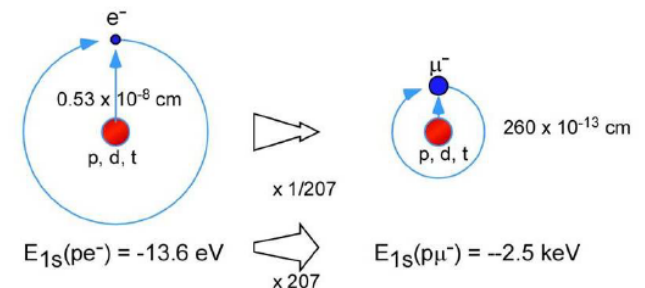
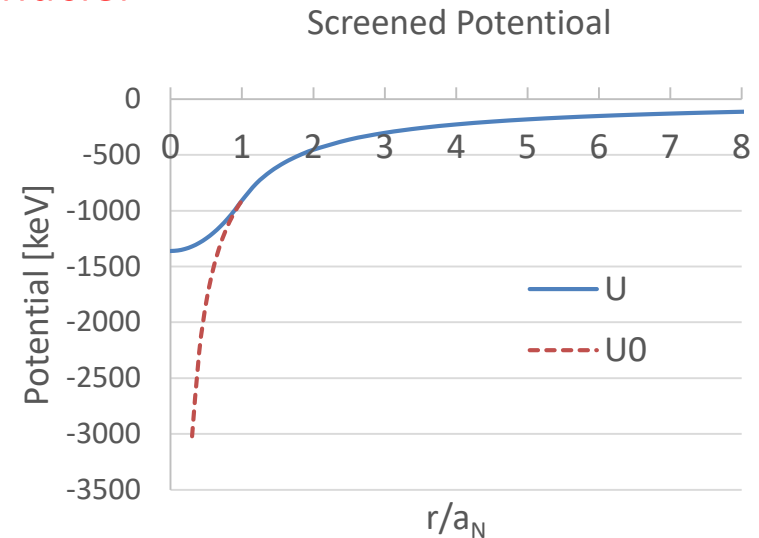
$$\Delta E = 16\pi Z^4 R_Y (a_N/a_B)^2$$

$R_E = 0.8768(69)$ fm CODATA

$$R_E = \int d^3r r^2 \rho_E(r)$$

While Bohr radius $a_e = 53$ pm $\Rightarrow R_E/a_e = 1.6 \times 10^{-5}$

200² times energy shift for **muonic atom**, while x200 in total energy scale relatively 200 times more sensitivity for proton radius



Proton Charge Radius Puzzle

PSI Measurement (μp 2s-2p by CREMA collaboration)

R. Pohl et al.,

Can. J. Nucl. Phys. 89, 37 (2011)

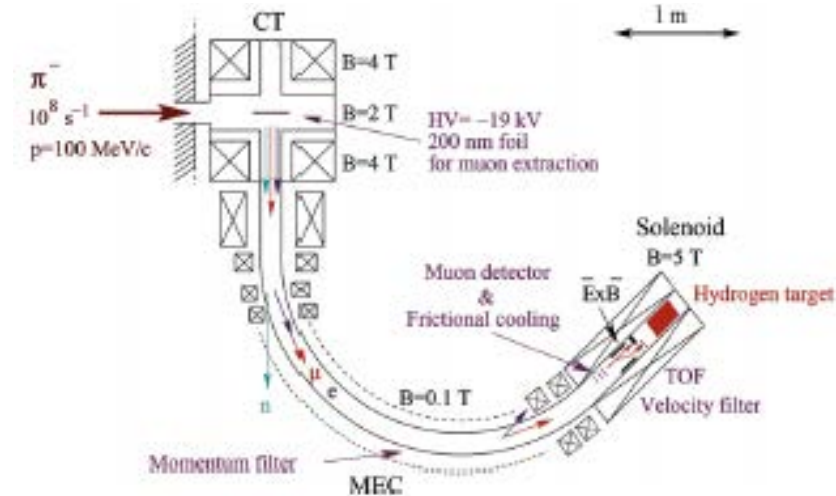
Measurement of 2s-2p energy difference

Formation of μp (1% feeds 2s)

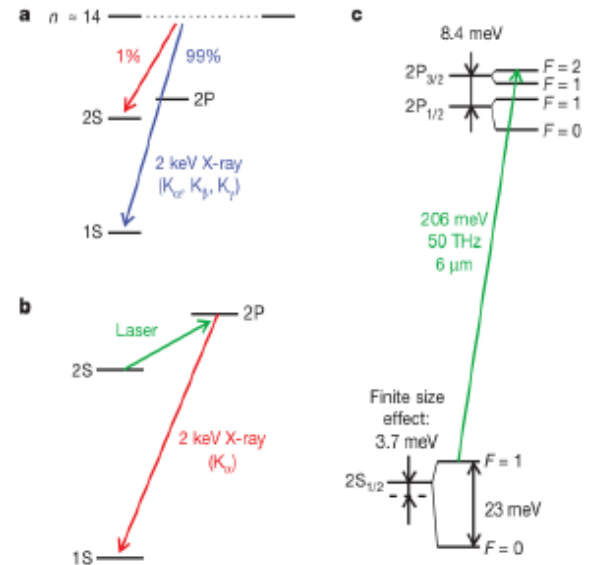
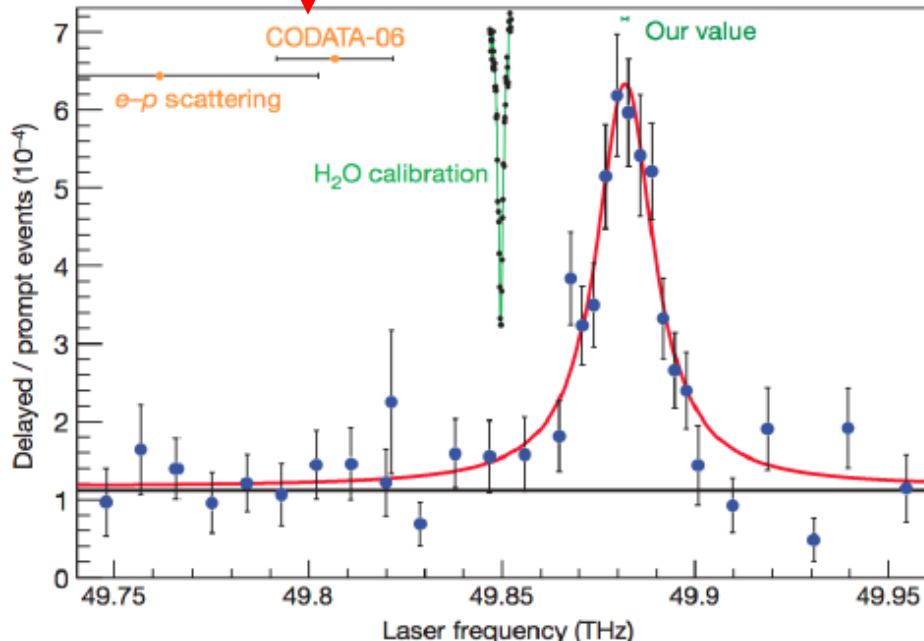
Laser resonant excitation of 2s-2p (Lamb Shift)

Observation: 2s metastable state \rightarrow 2p \rightarrow 1s

Frequency calibration relative H₂O absorption line



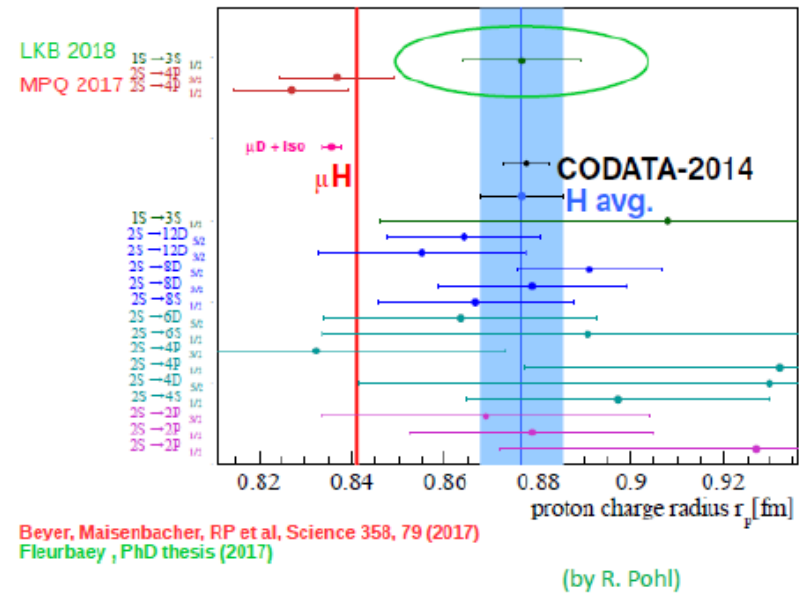
expected position



Where will we go?

1. Need to be checked/confirmed more evidences, theories, ...

Rp from H spectroscopy



2. Other r_E measurements with muons

Muonic deuterium (done)

Muonic He3, He4 (nearly done)

μp and ep scattering (MUSE) in progress

3. **Zemach radius r_Z**

another proton radius accessible by spectroscopy

includes magnetic structure

Zemach radius

How about magnetic radius of proton?

=> **Hyperfine splitting** is related to magnetic moment.

Zemach radius A.C. Zemach, Phs.Rev.C 104, 1771(1956).

$$R_Z = \int d^3r r \int d^3r' \rho_E(r') \rho_M(r - r')$$

convolution of charge and magnetic moment distribution

Why **not only magnetic** distribution?

In point charge limit

=> Hyperfine coupling with distributed magnetic moment

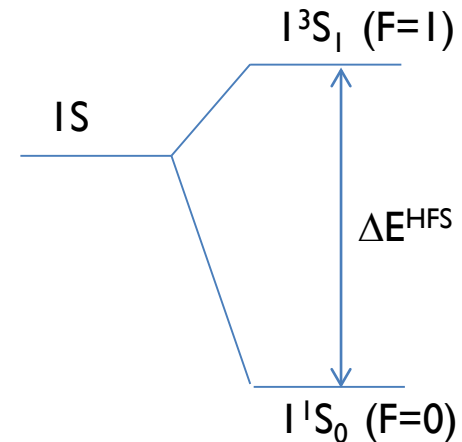
Coupling largest for moments at center, becomes weaker outside.

In point magnetic moment limit.

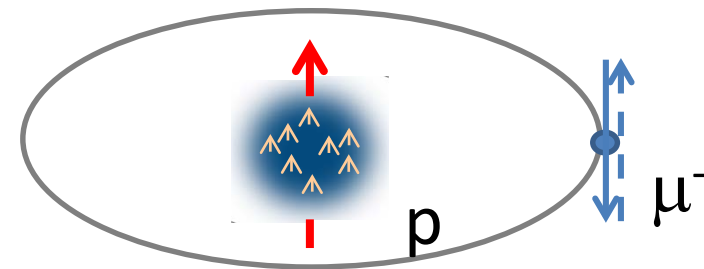
=> Charge distribution reduces muon attraction,

lower muon overlap with nuclear charge

In both cases, lead to smaller HFS energy



F : total angular momentum



Zemach radius

Zemach radius A.C. Zemach, Phs.Rev.C 104, 1771(1956).

$$R_Z = \int d^3r r \int d^3r' \rho_E(r') \rho_M(r - r')$$

If the muon and electron determination of Zemach radius are consistent

-> some problem in charge radius measurements?

If they are different

-> radius puzzle continues,
size of discrepancies may give us hint

Zemach radius so far

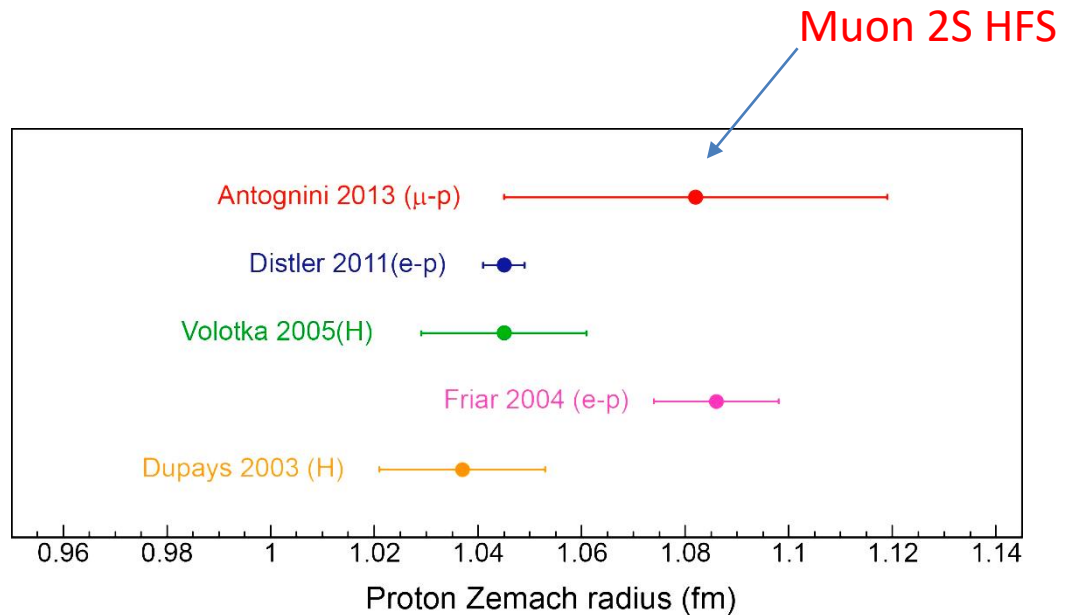
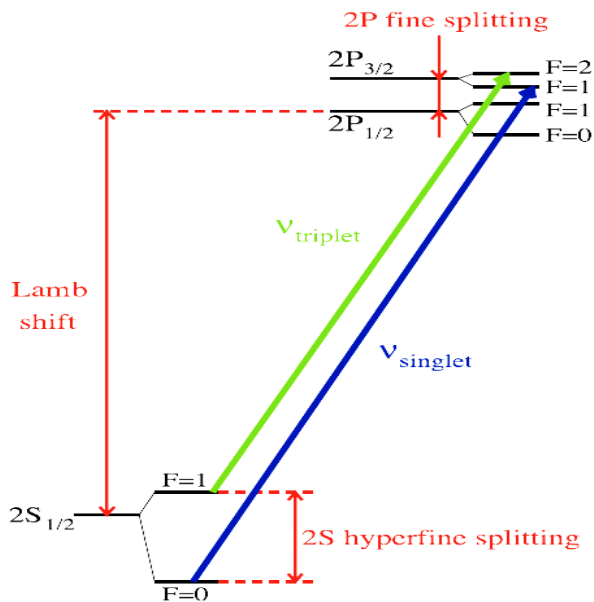
2s HFS was indirectly determined in the same CREMA experiment at PSI (from two lines)

$R_Z = 1.082(37)$ fm [A. Antognini, et al., Science 339 (2013) 417]

from e-p : 1.086(12), 1.045(4) fm

from H spectroscopy : 1.047(16) , 1.037(16) fm

No definitive interpretation with proton radius puzzle because of the **large error bar**



Need high precision values

Direct measurement of 1s HFS has chance to determine R_Z to better than 1%

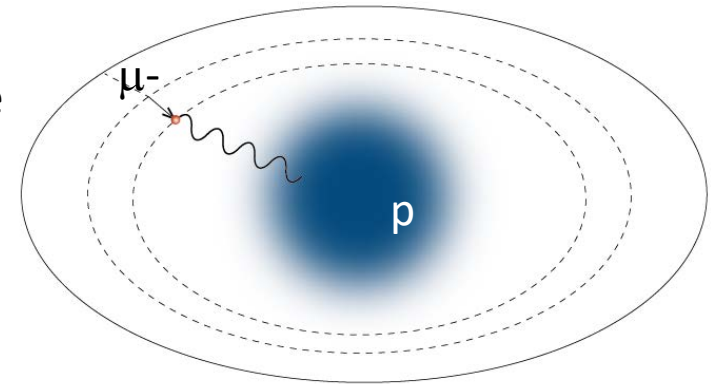
Formation of Muonic Hydrogen atom (μ^-p)

Muon stops in hydrogen

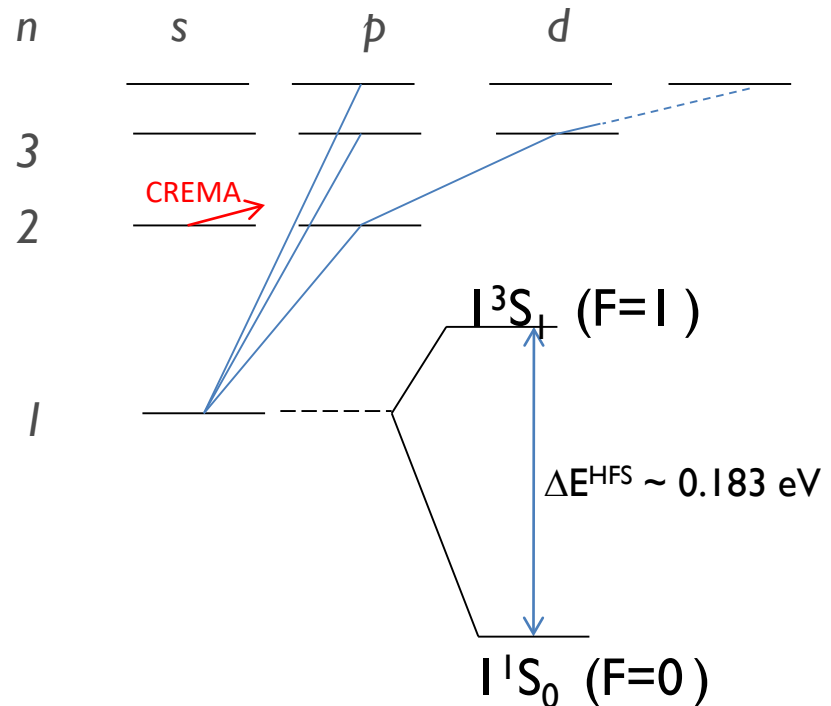
Muon capture at high orbit and cascade to ground state

Rapid conversion to lower hyperfine state
=> no muon polarization left

All muons reach 1s ground state
vs. 1% only to 2S in PSI Lam Shift measurement



→ g.s. μ^-p atom



HFS splitting energy

How is the Zemach radius determined?

It is, in first order, proportional to muon and proton magnetic moments ($1/m_\mu$ and μ_p) and to $1/R_{\mu p}^3$ but with correction terms, some are structure dependent

$$\Delta E_{HFS}^{exp} = E_F (1 + \delta_{QED} + \delta_{Zemach} + \delta_{recoil} + \delta_{pol} + \delta_{hvp})$$

Fermi term:

$$E_F = \frac{8}{3} \alpha^4 \frac{m_{\mu(e)}^2 m_p^2}{(m_{\mu(e)} + m_p)^3} \mu_p$$

δ_{QED} : higher order QED correction (well known)

$$\delta_{Zemach} = -2\alpha m_{\mu p} R_z + O(\alpha^2)$$

δ_{recoil} : recoil (well known)

δ_{pol} : proton polarizability (internal dynamics of protons)

δ_{hvp} : hadron vacuum polarization (small)

$$R_Z = \left\{ \left(E_F (1 + \delta_{QED} + \delta_{recoil} + \delta_{pol} + \delta_{hvp}) - \Delta E_{HFS}^{exp} \right) / 1.281 \right\} = 1.0XX(13) \text{ fm}$$

1130(1) ppm
1700(1) ppm
20(2) ppm

460(80) ppm
(2) ppm

proton polarizability

R_Z will be improved to 1 % (even with present limitation by δ_{pol} precision).

We request improvement of δ_{pol} (by QCD?).

Expected precision of Zemach radius

$$R_Z = \left\{ \left(E_F (1 + \delta_{QED} + \delta_{recoil} + \delta_{pol} + \delta_{hvp}) - \Delta E_{HFS}^{exp} \right) / 1.281 \right\}$$

1130(1) ppm
1700(1) ppm
460(80) ppm
20(2) ppm
(2) ppm

Dupays et al., PRA 2003

$R_Z = 1.0XX(13) \text{ fm}$

is dominated in precision, but improved factor ~3 from PSI results, we need help of theorists to improve precision.

	Hydrogen		Muonic hydrogen	
	Magnitude	Uncertainty	Magnitude	Uncertainty
E^F	1418.84 MHz	0.01 ppm	182.443 meV	0.1 ppm
δ^{QED}	1.13×10^{-3}	$< 0.001 \times 10^{-6}$	1.13×10^{-3}	10^{-6}
δ^{rigid}	39×10^{-6}	2×10^{-6}	7.5×10^{-3}	0.1×10^{-3}
δ^{recoil}	6×10^{-6}	10^{-8}	1.7×10^{-3}	10^{-6}
δ^{pol}	1.4×10^{-6}	0.6×10^{-6}	<u>0.46×10^{-3}</u>	<u>0.08×10^{-3}</u>
δ^{hvp}	10^{-8}	10^{-9}	0.02×10^{-3}	0.002×10^{-3}

Improvement of proton polarizability correction (δ_{pol}) drastically reduces uncertainty of R_Z

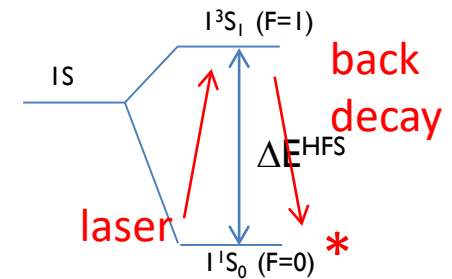


check with R_Z determined by “electronic” and “muonic” measurement

Zemach radius measurement with muons

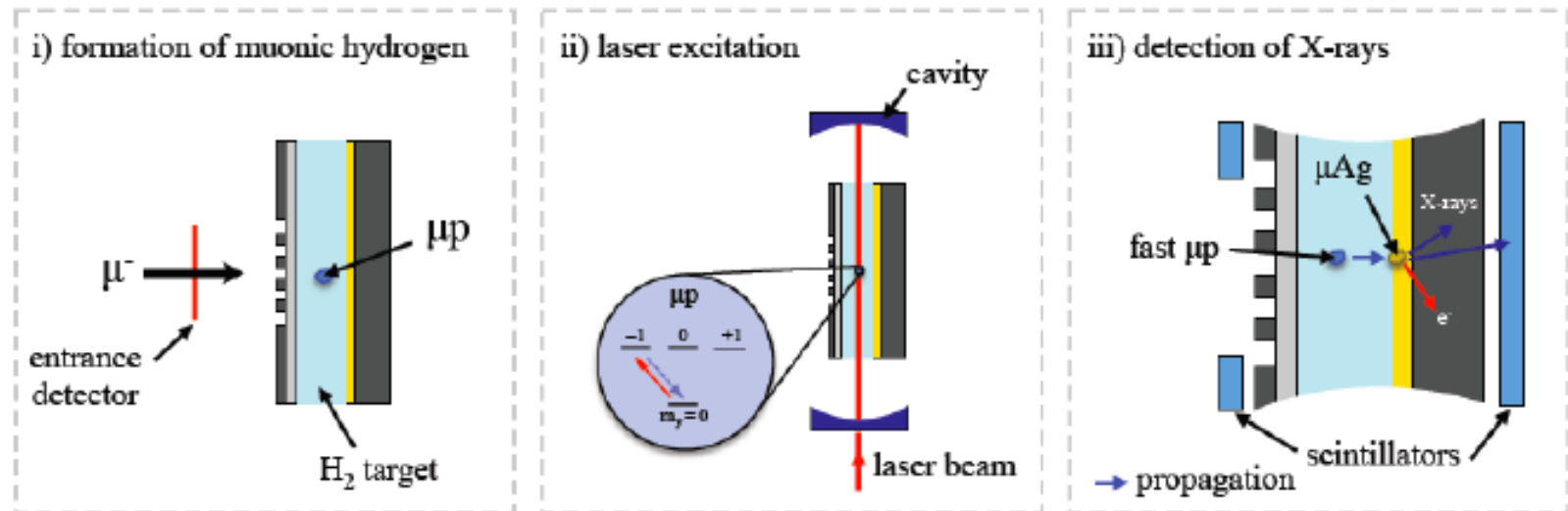
There are three proposals

Two groups use **increased μp kinetic energy** after back decay from laser excited states



1) **CREMA-3** at PSI

Faster μp diffusion to wall



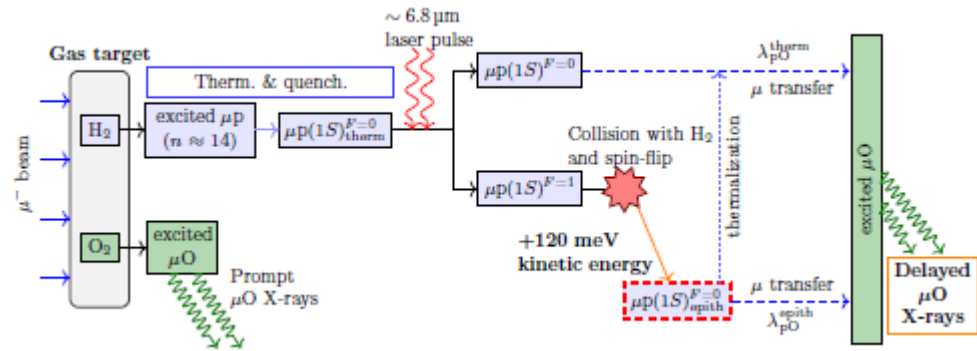
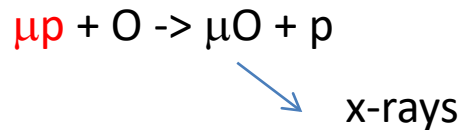
- steel
- hydrogen target (~3 bar)
- titanium foil
- gold foil

Zemach radius measurement with muons

2) **FAMU** at RIKEN-RAL (Vachi's talk and others)

energy dependent **muon transfer** rate to admixture oxygen

Bakalov et al., Phys. Lett. A 172 (1993) 277



Several papers on kinetic energy depend transfer measurement published

Adamczak et al, JINST 11, 05007 (2016)

Mocchuuttiet al, JINST 13,12033 (2018)

Adamczak et al, JINST 13, 02019 (2018)

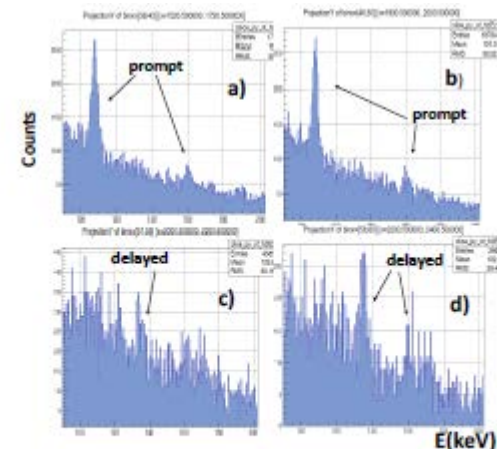
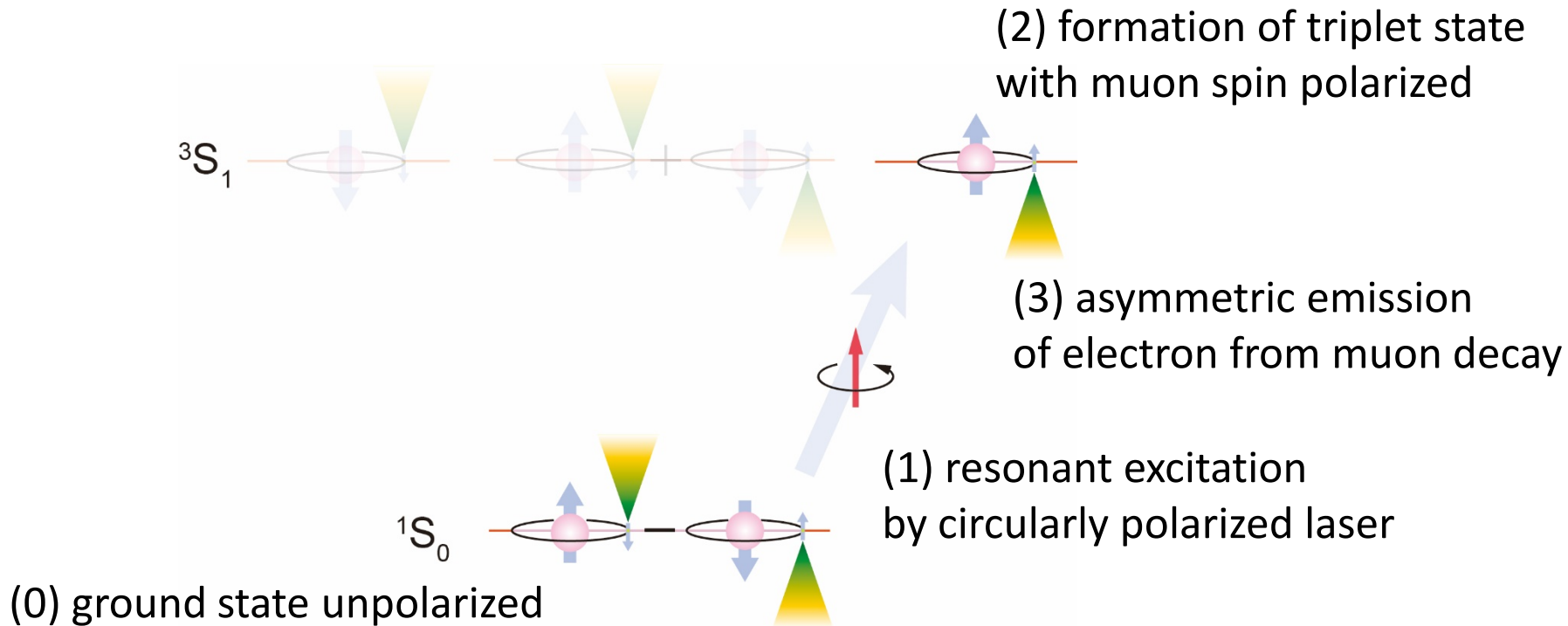


Figure 23. Time evolution of the $K_{\alpha}(2p \rightarrow 1s)$ line energy distribution, as reconstructed from the GEM-S HPGc detector, in four time slices. (a) 1520–1720 ns, (b) 1800–2000 ns, (c) 2000–2200 ns and (d) 2200–2400 ns.

Zemach radius measurement with muons

3) **RIKEN group** propose **spin polarization measurement** at RAL and J-PARC
(idea started in discussion in RIKEN including M. Iwasaki and Ishida in 2013)



All based only on well known processes!
No need of phenomenological simulation

RIKEN MuP Collaboration

K. Ishida, S. Kanda, M. Iwasaki, M. Sato*, Y. Ma,
S. Okada, S. Aikawa, H. Ueno, A. Takamine,
K. Midorikawa, N. Saito, S. Wada, M. Yumoto

RIKEN

Y. Matsuda, K. Tanaka**

Graduate of School of Arts and Science, The University of Tokyo

Y. Oishi

KEK

* Present address: KEK

** *Present address: CYRIC, Tohoku Univ.*

New collaborators are welcome

Key for the measurement

1. Increase **excitation** rate (M1 transition) and polarization

Intense mid infrared laser developed at RIKEN +multi-pass cavity

2. Many muonic hydrogen atoms

Intense pulsed muon beam at RIKEN-RAL and J-PARC

Optimum gas condition, gas container,
muon stopping simulation/measurement (test at RIKEN-RAL)

3. Optimization of **polarization detection**

Detectors, Filtering by lifetime, Background reduction

Laser excitation

Laser requirement for $\mu\text{p } 1\text{S HFS}$

$$0.183 \text{ eV} = 6.8 \text{ } \mu\text{m} = 44 \text{ THz}$$

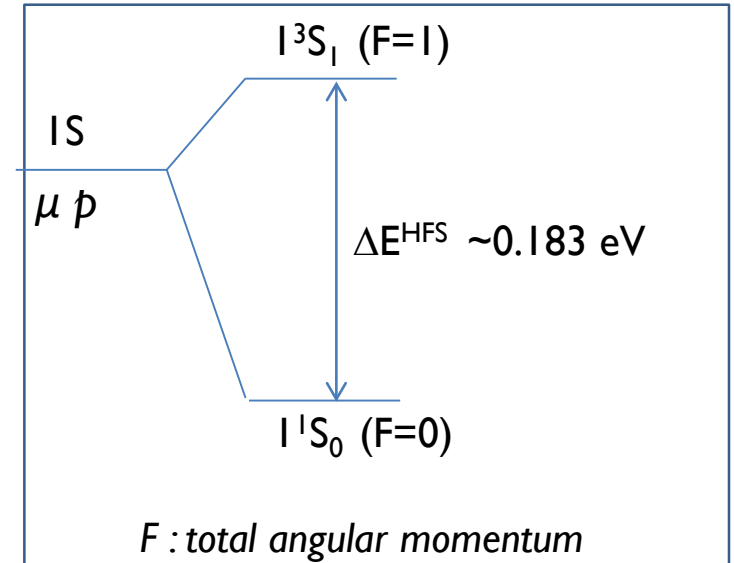
tunable by $\sim 10^{-3}$ (40 GHz) - to cover uncertainty

narrow band width 50 MHz (1 ppm)

Magnetic transition

$$\mathbf{B}_+(\mathbf{t}) = (1/\sqrt{2} B_0 \cos\omega t, 1/\sqrt{2} B_0 \sin\omega t, 0)$$

$$dP/dt = 2\pi/\hbar |(\mu_\mu + \mu_p)B_0|^2 / 4 \delta(\nu - \nu_0)$$



with convolution of Doppler broadening by μp velocity distribution ($\sim \sqrt{T}$)

(A. Adamczak et al., NIM B 281 (2012) 72, with correction by 1/4 , private communication)

Single shot transition probability

$$P = 2 \times 10^{-5} \frac{E}{S\sqrt{T}}$$

E/S : laser power density [J/m^2], T : temperature [K]

Doppler broadening (cooling to ~ 20 K helps \Rightarrow 63 MHz)

Laser excitation

Small excitation rate because of M1 transition

$$\bar{P} = 2 \times 10^{-5} \frac{E}{S\sqrt{T}}$$

E/S : laser power density [J/m^2], T : temperature [K]

ex. $E = 40 \text{ mJ}$, $S = 4 \text{ cm}^2$, $T = 20 \text{ K}$, then $P = 4.5 \times 10^{-4}$

too low efficiency with one pass

use of multi-pass cavity (like PSI)

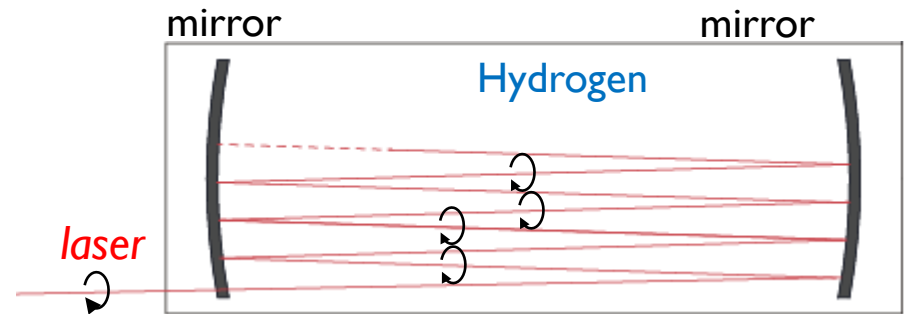
high reflective mirror 99.95%

Cavity ray tracking calculation

$P = 45\%$ with 1000 pass

(P reduced to $\sim 7\%$ expected if quench is included : see below)

40mJ per pulse and 50Hz laser is required



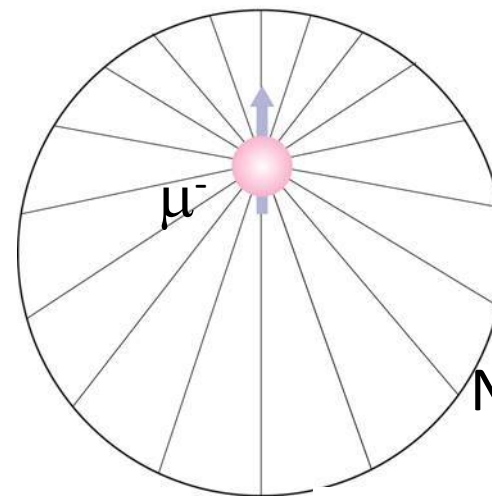
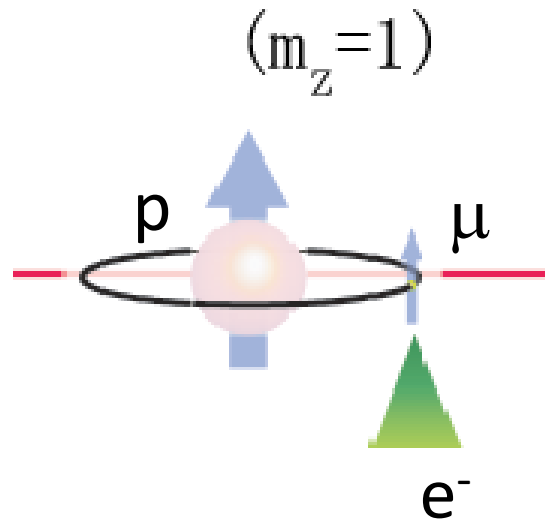
Detection of Polarization

Circularly polarized laser select of one sub-state in excitation to triplet state.

=> complete muon spin polarization in excited state.

Muon decays with 2.2 μs lifetime and emits electrons asymmetrically to the spin.

$\mu^- \rightarrow e^-$



parity-violating
muon decay!

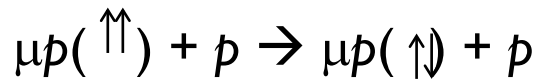
$$d\sigma_{e^-}(\theta)d\Omega \propto \left(1 - \frac{1}{3}P \cos\theta\right)d\Omega$$

M. Sato, et al. "Laser Spectroscopy of Ground State Hyperfine Splitting Energy of Muonic Hydrogen"

JPS Conf. Proc. 8 , 025005 (2015)

Obstacle to the experiment - quench rate

Triplet to singlet quenching before muon decay
by **external** collision



will lose muon polarization.

Theoretical calculations

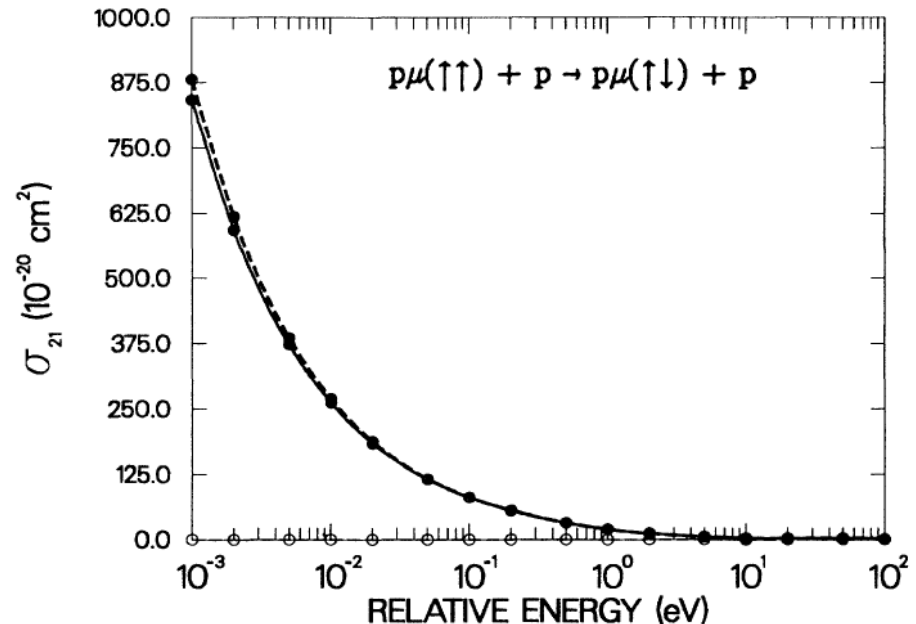
J. Cohen, Phys. Rev. A 43 (1991) 466

No experimental data on μp yet
(rate for μd is slower and
well known by μCF)

Cross section proportional to $1/v$

So, quench rate is almost energy (or temperature) independent.

Triplet state lifetime ~ 50 ps at liquid hydrogen density (LHD)



How we manage the difficulty - quench rate

Triplet state lifetime 50 ps at liquid hydrogen density (LHD)

For polarization measurement by muon decay (2.2 μs),
we need longer keeping time.

Will use low density hydrogen

50 ns at 0.001 LHD,

500 ns at 0.0001 LHD

⇒ Target Requirement

Large muon stopping -> **high** density, **large** volume

Small μp quenching -> **low** density

High laser density -> **small** volume

We need to optimize the target volume and the gas density

We have other option to avoid this quench
with novel target => Kanda's talk

Polarization vs time

Calculation of muon polarization build up with

Excitation per single pass (4.5×10^{-4})

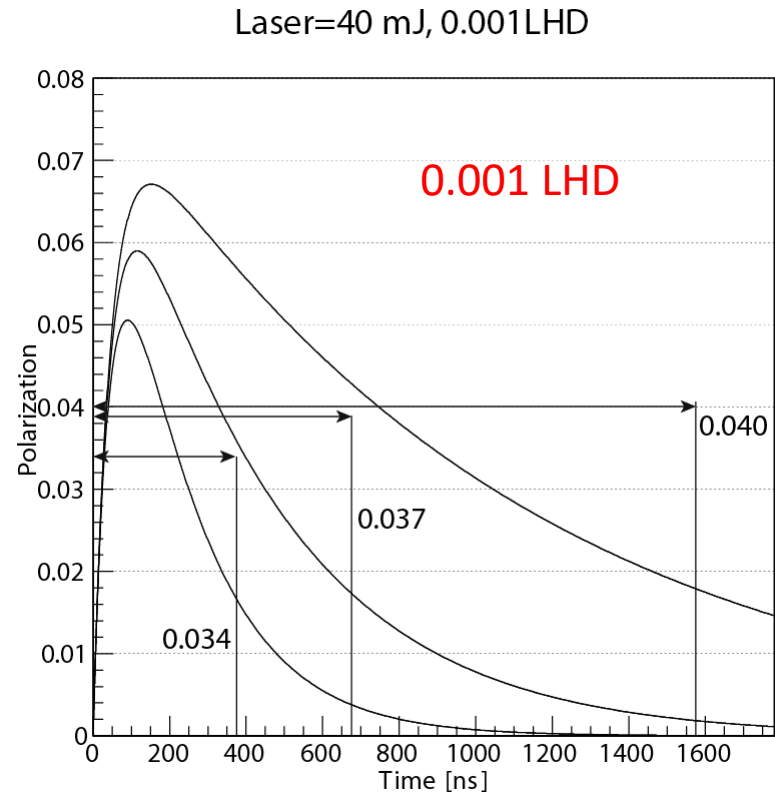
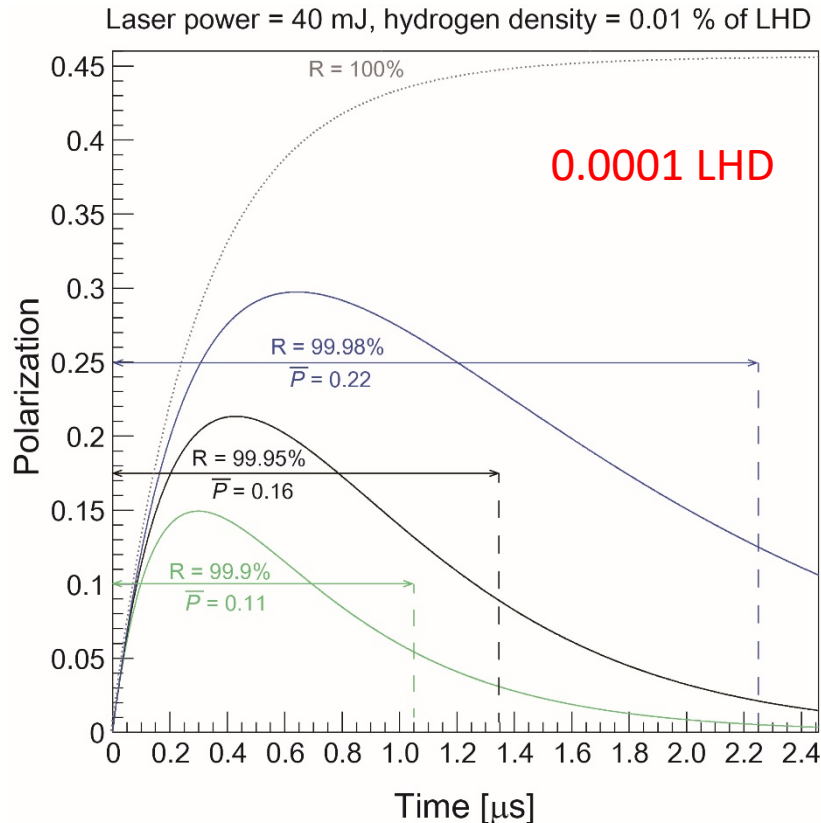
Multi-pass laser cavity with loss by reflectivity

and μp HFS quenching (500 ns for 0.0001 LHD, 50 ns for 0.001 LHD)

Average polarization

0.16 in a time gate 1.33 μs (0.0001 LHD)

0.037 in 0.67 μs for 0.001 LHD)



Target & Detector

Target Requirement

Optimization of gas density

Number of stop muons or polarization

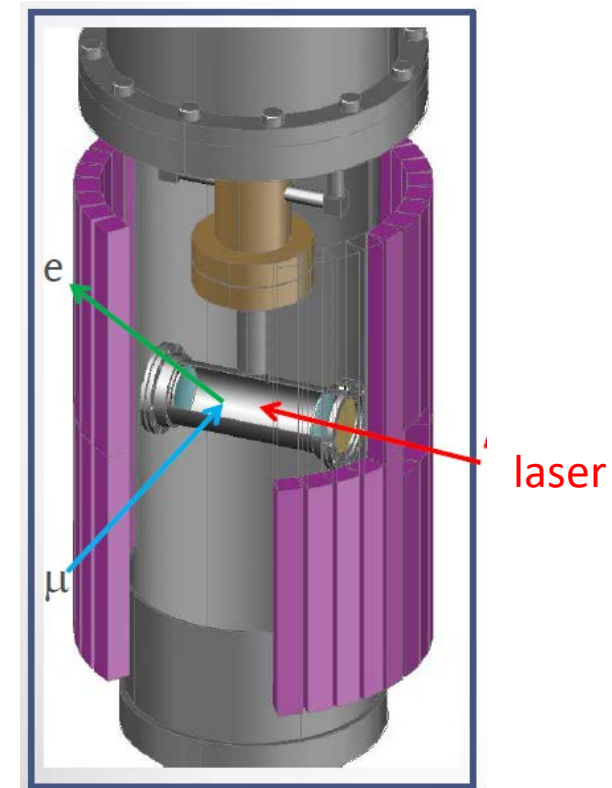
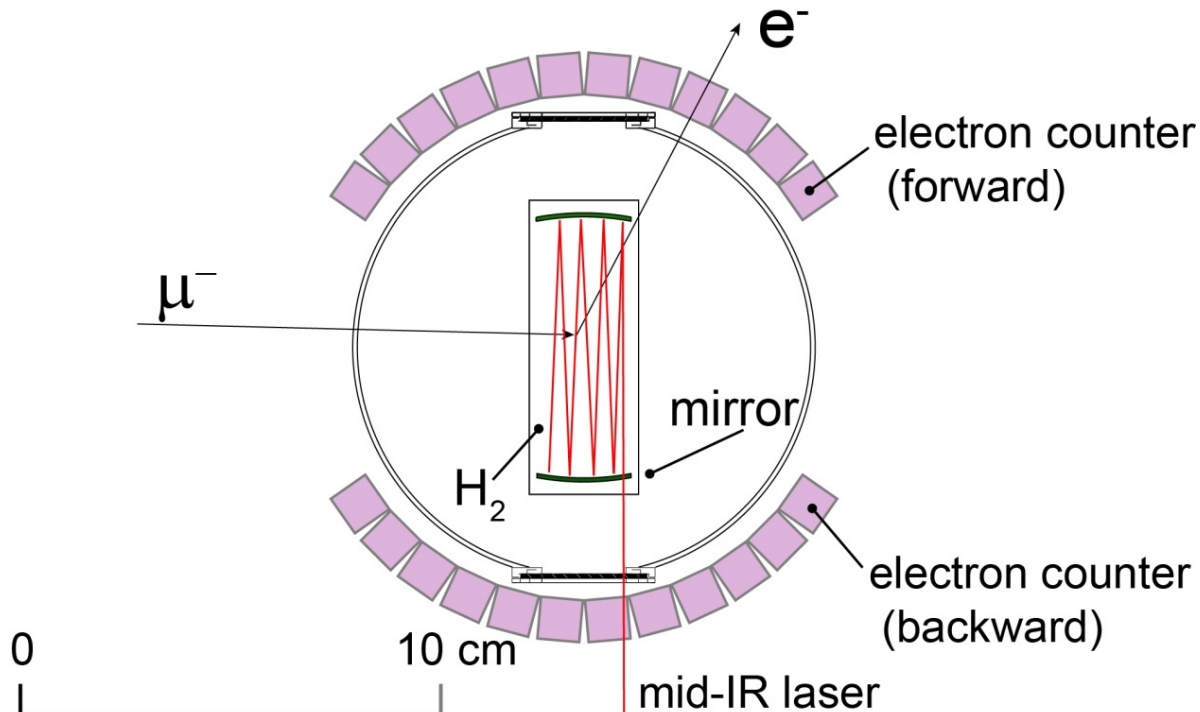
=> Let's take 0.0001 LHD and 4 cm² x 6 cm

Detector

Solid angle ~28% each

Asymmetry factor

(polarization sensitivity) ~0.23



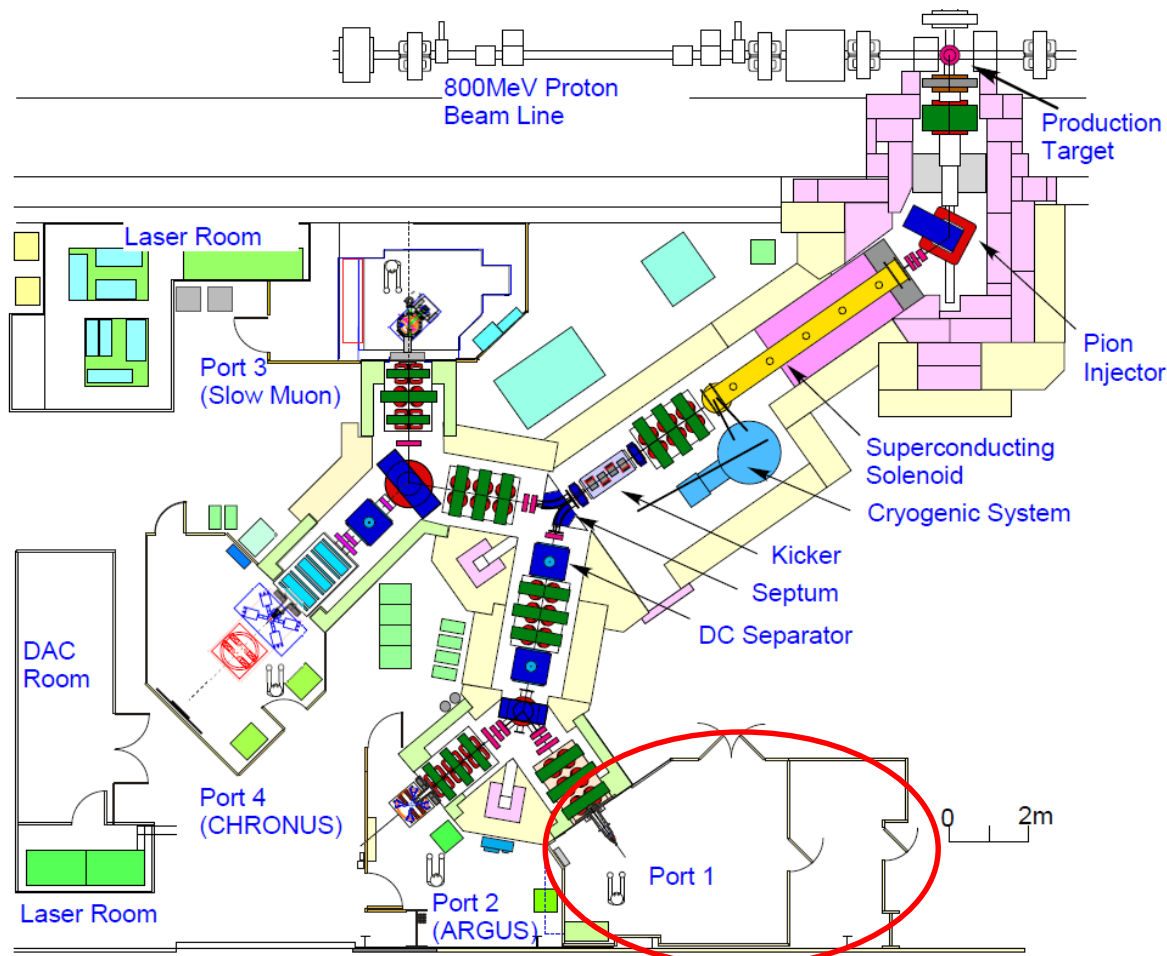
Muon beam at RIKEN-RAL Muon Facility

RIKEN-RAL Muon Facility in ISIS, UK

Pulsed muon is a good match to high intensity laser

Port 4 has been used for test measurements.

Port 1 is being converted to laser compatible room (Vachi's talk).



Typical muon intensity
 $2.2 \times 10^4 \text{ [s}^{-1}\text{]}$
at $p = 40 \text{ MeV/c}$

Muon stopping simulation and background

Condition:

Hydrogen target cell cooled to 20 K by GM-type refrigerator
40 MeV/c pulsed muon beam at RIKEN-RAL Muon Facility

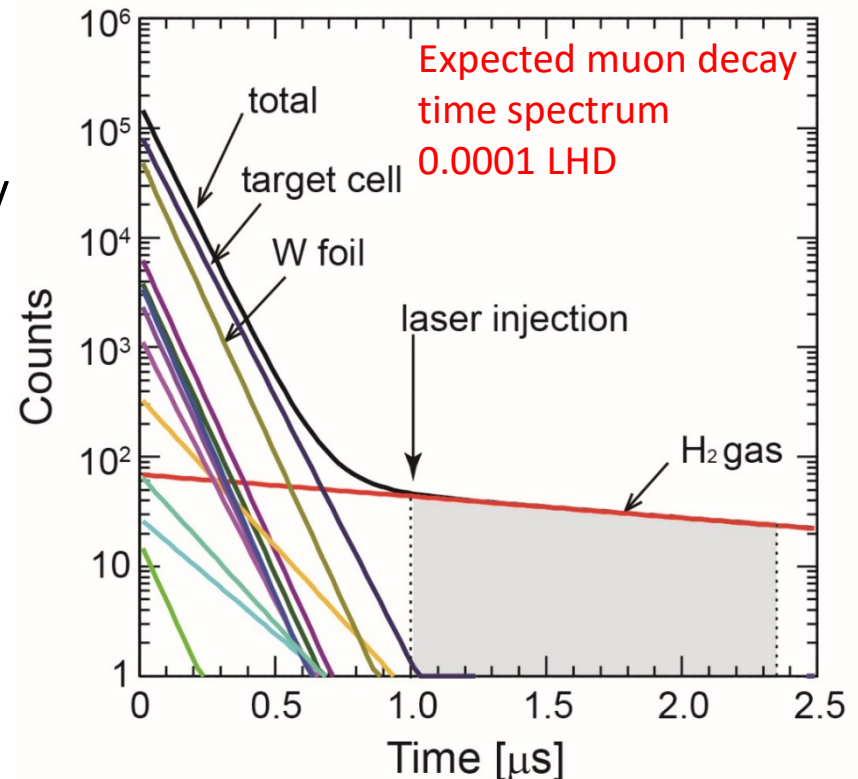


Geant Result:

0.1% of incoming muons stops in 0.0001 LHD hydrogen gas
(or 1% at 0.001 LHD)

Using **high-Z materials as the target cell**,
muons in those materials disappear quickly
by nuclear capture (90ns in silver)

Laser injection after 1 μs
when backgrounds died away



Beam test of background level

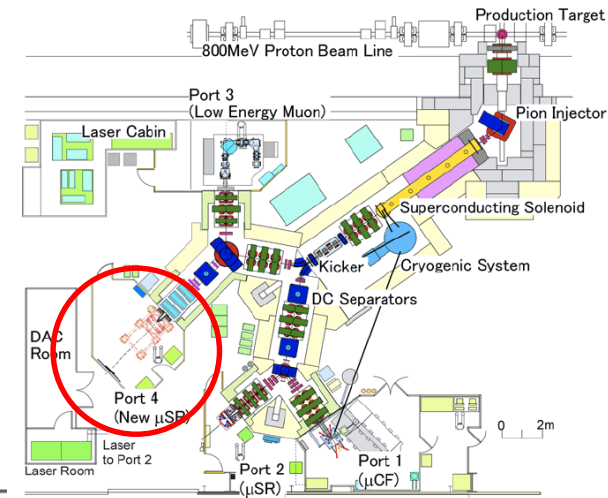
Beam test at RIKEN-RAL

Muons stopped in Cu target

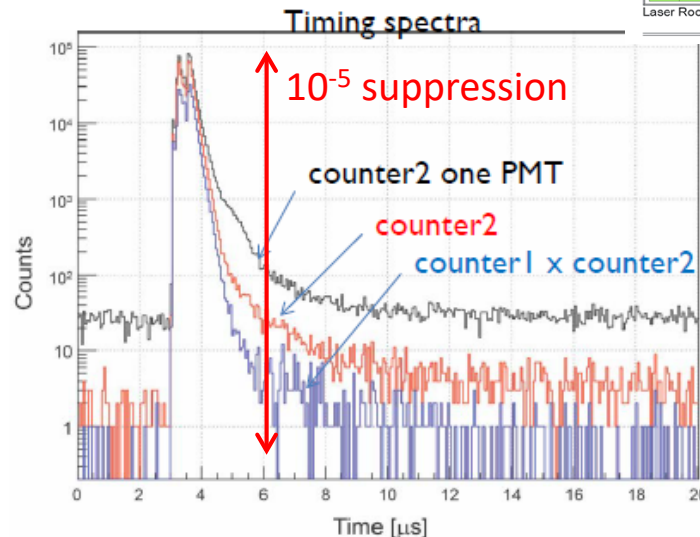
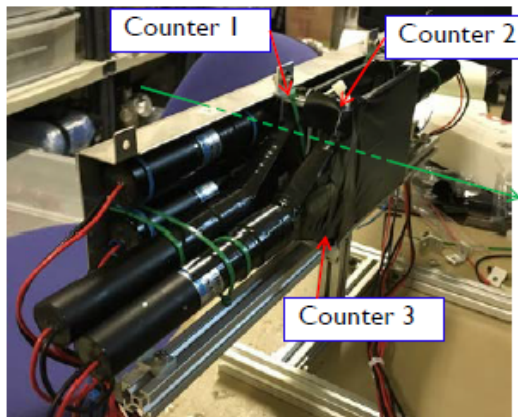
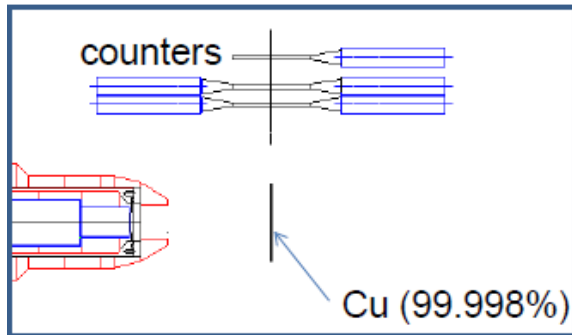
We confirmed

Fast decay out of muons in high-Z materials like Cu

Low background level ($< 10^{-4}$) at $\sim 1 \mu\text{s}$



Beam time in May (5/11-13) : CHRONUS \rightarrow coincidence counters



Further studies
with H2 target
 \Rightarrow Kanda's talk

background can be suppressed with hit-timing coincidence

\rightarrow design the prototype of electron counters
beam test with dilute gas

Yield estimation (statistics)

Take the **forward/backward ratio** for the polarization effect

N_F, N_B in time gate

$$(N_F - N_B) / (N_F + N_B) = A_0 P$$

Beam condition

Intensity 2.2×10^4 /s @40 MeV/c (**J-PARC**)

Momentum width $\sigma_p/p_0 = 2\%$

Target condition

H2 gas 0.001 LHD, Volume $4\text{cm}^2 \times 6\text{ cm}$

Laser

40 mJ, 99.95% reflectivity, cavity length

Detector (solid angle 28% each, polarization sensitivity factor 0.23)

Time gate : laser at $1.0 \mu\text{s}$ after muon + $1.33 \mu\text{s}$ detection gate

statistics in 5 hours

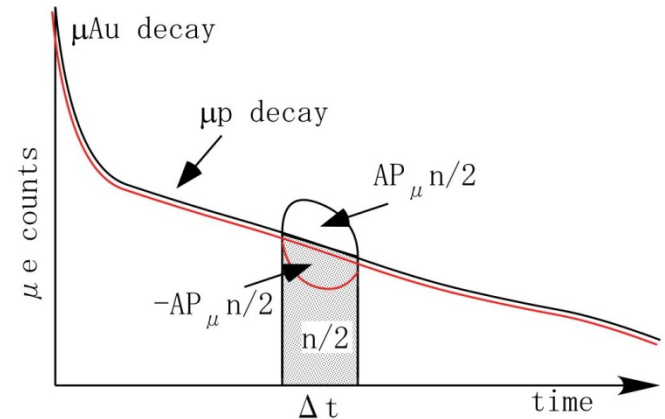
=> signal $N_F - N_B, \sim 240$

fluctuation $\Delta N_F + \Delta N_B \sim \sqrt{(N_F + N_B)} \sim 80$

significance = $(N_F - N_B) / \sqrt{(N_F + N_B)} \sim 3\sigma$

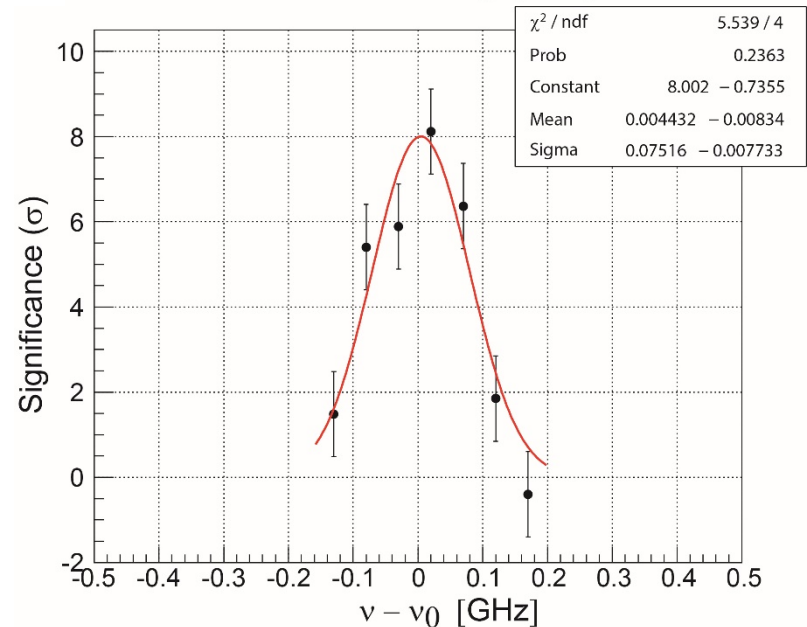
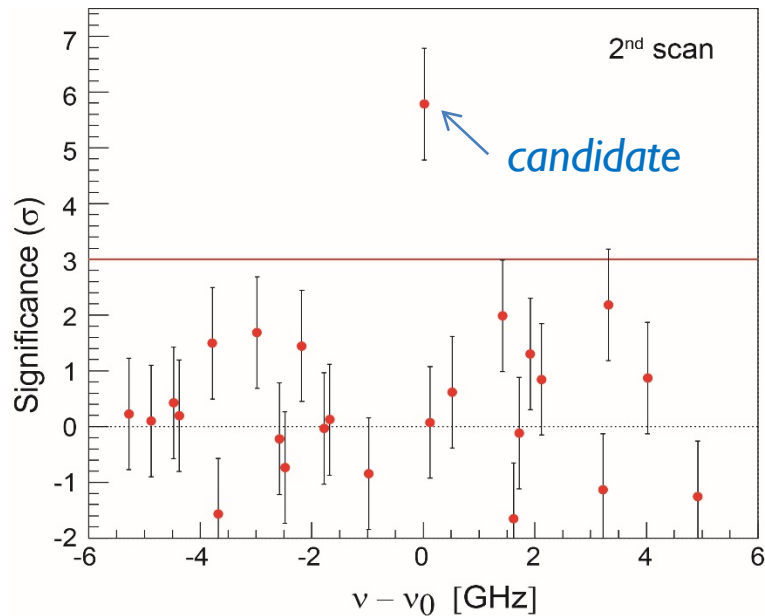
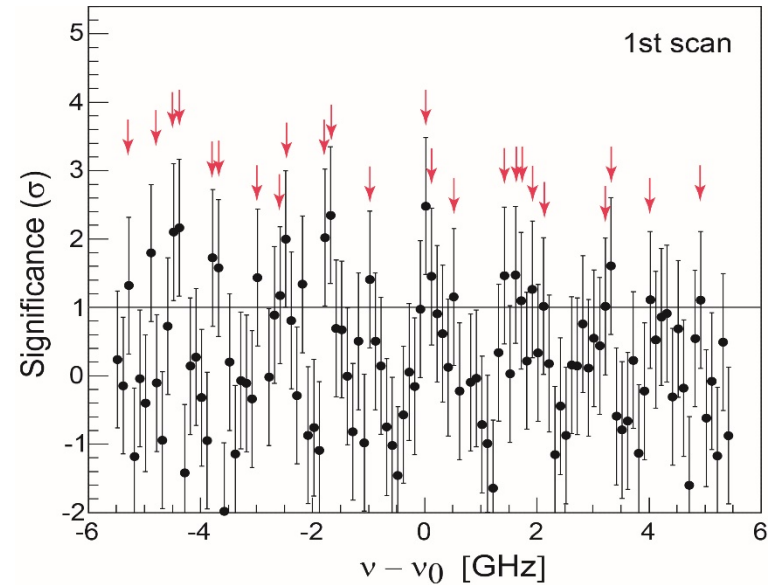
Time is doubled (~ 10 hour) for accumulating laser on and off

Scan of 100 laser wave length points = 1000 hours => 40~50 days



Resonance hunting & beam time estimate

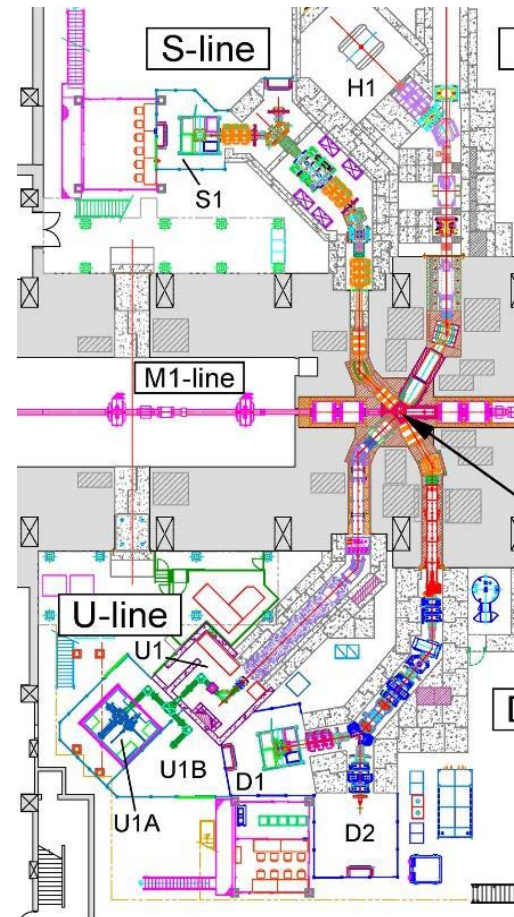
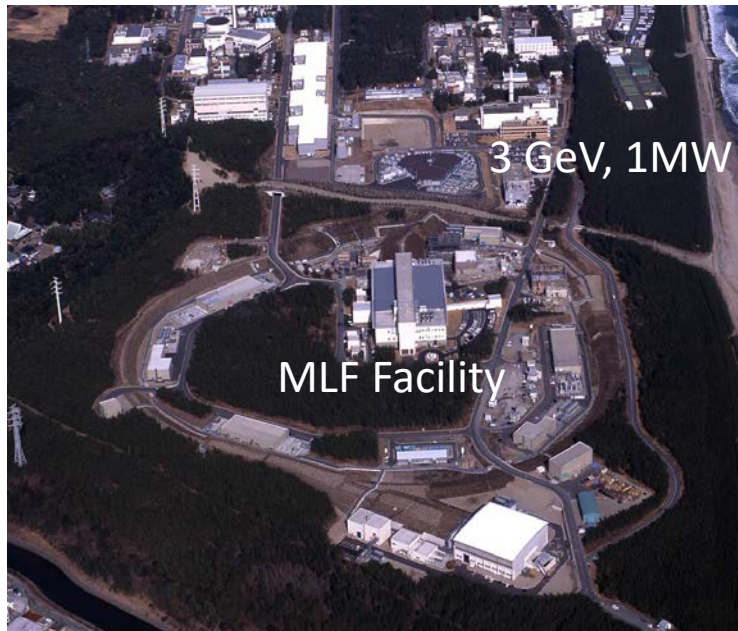
We plan **three steps hunting** of resonance over region ± 5.7 GHz (theoretical ambiguity $\times 3$)
100MHz step (matching the resonance width)
1) 3σ scan ~ 50 days (100 points)
2) 5σ scan ~ 24 days
3) resonance curve ~ 16 days
 \Rightarrow 3 months beam time



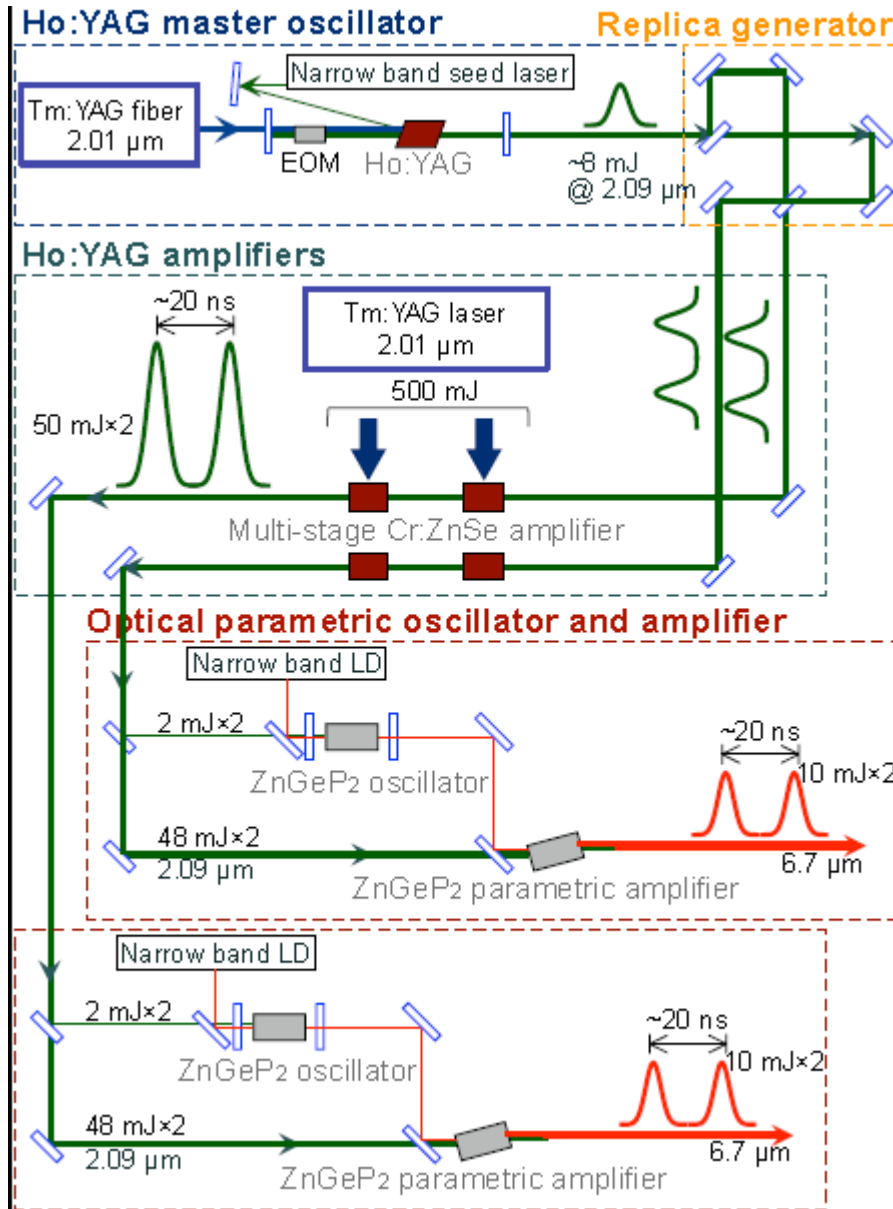
Beam time estimate: at J-PARC

At J-PARC MUSE D-line, we can earn statistics quicker (x8?) based on 40 MeV/c μ^- intensity and beam characteristics scaling. Same statistics could be obtained in ~ 12 days.

Laser installation & long term occupation of the area for preparation are issues to be discussed



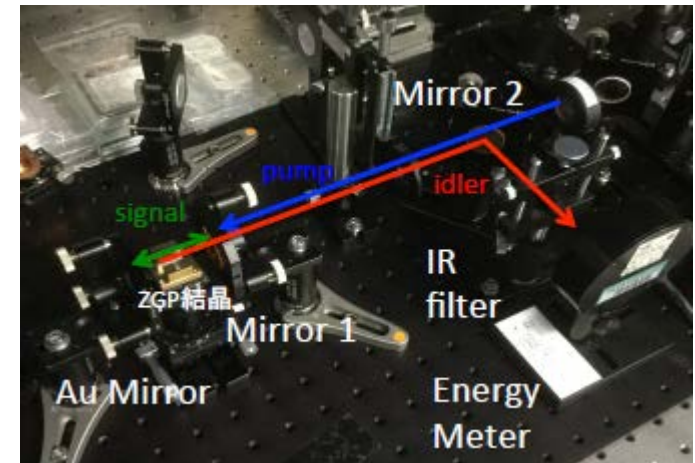
Keys: Laser



RIKEN laser group had experience of developing intense $6 \mu\text{m}$ laser (5mJ)
We apply frequency stabilization and increasing intensity based on this

Achieve 40 mJ with best matching component and multi-source injection

Components studies are in progress
Cr:ZnSe oscillation, Cr:ZnSe amplification.
ZGP OPO (\Rightarrow more in Kanda's talk)

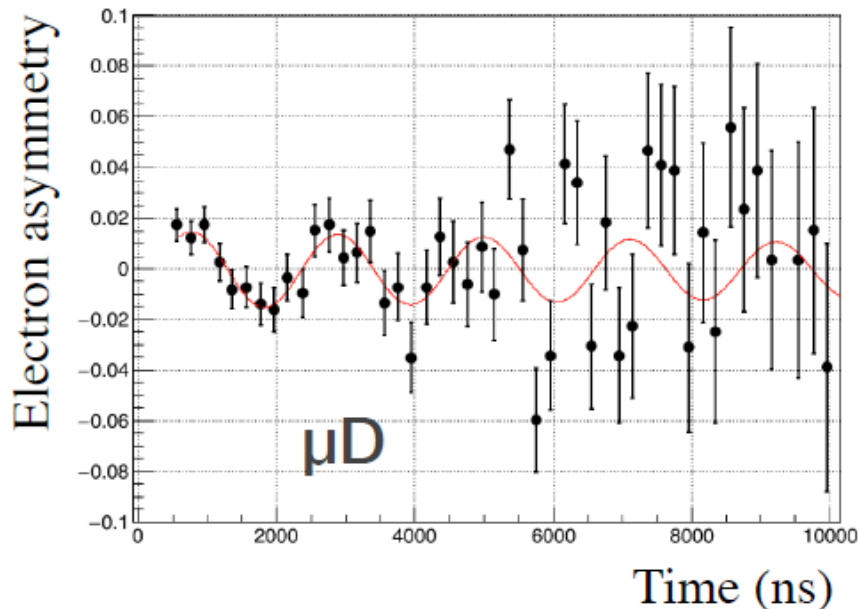
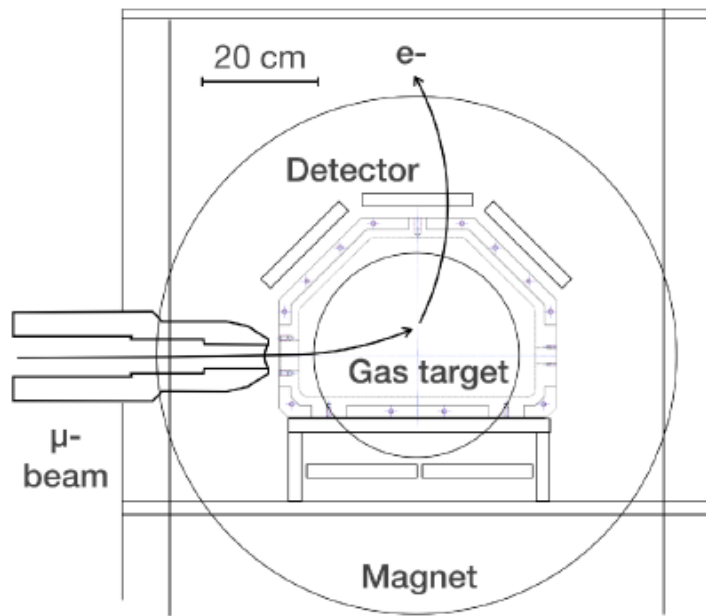


Keys: triplet-single quench rate

HF quench rate is the key factor

will be measured and compared with theoretical estimates

quartet μ D spin precession ($\sim 10\mu\text{s}$ lifetime in gas) done Sep 2018



triplet μ p quench rate ($< 1\mu\text{s}$ lifetime) planned in 2019

more challenging because of predicted short decay time

need of low density gas (~ 0.1 bar)

=> more detail in Kanda's talk

Summary

Large discrepancy in proton radius values between measurements
"Proton radius puzzle"

New measurements and more data are arriving
but the puzzle has not been solved yet.

How about Zemach radius from μp HFS?

We propose measurement of HFS energy
by laser excitation and detection with muon spin polarization

Preparation status to be presented by Sohtaro Kanda