

Measurement of the transfer rate from muonic hydrogen to oxygen with FAMU

Emiliano Mocchiutti
on behalf of the FAMU Collaboration

ECSAC2019 – The Proton Radius
Veli Lošinj – 16/20 September 2019

Outline

- Introduction
- The FAMU experiment
- Apparatus setup
- Measurement of the transfer rate $\Lambda_{\mu p \rightarrow \mu O}$
(a.k.a. Λ_{pO}):
 - Data selection and selection efficiencies
 - Background evaluation
 - Time dependence fit
- Results
- Summary

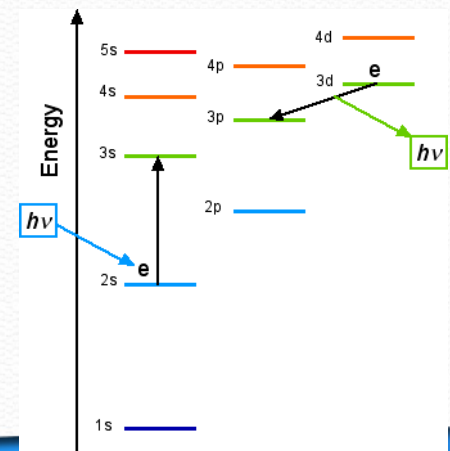
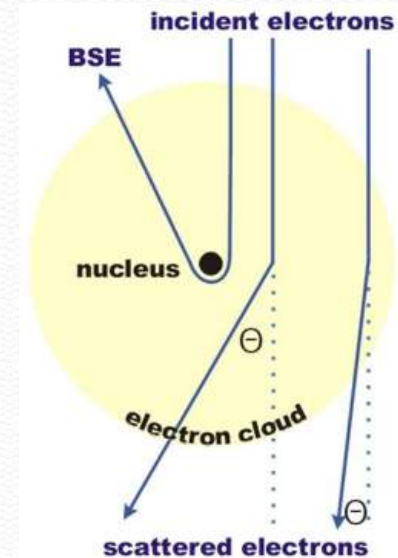
Introduction

FAMU: HFS of μ^-p ground level

Study of the properties of the proton

- 1) scattering: electron experiments
- 2) scattering: elastic muon-proton
- 3) spectroscopy: electronic atoms and ions
- 4) spectroscopy: exotic atoms

HFS of muonic hydrogen
ground level



The FAMU experiment

Fisica Atomi MUonici (Physics with muonic atoms)

FAMU: μ^-p spectroscopy

“Usual” spectroscopic flow:

- 1) create muonic hydrogen
- 2) laser excitation
- 3) count triplets

repeat varying laser frequency to find resonance value.

How is it possible to distinguish HFS excited states?

Hyperfine splitting of $(\mu^-p)_{1S} \sim 183$ meV...

Summary of muon atomic capture physics (in H gas)

1. Hydrogen gas at room temperature (i.e. H_2 molecules mean kinetic energy 30 meV – 0.03 eV)

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5. The system muon-proton (muonic hydrogen) gains kinetic energy (average energy about 2 eV !)

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Summary of muon atomic capture physics (in H gas)

1. Hydrogen gas at room temperature (i.e. H₂ molecules mean kinetic energy 30 meV – 0.03 eV)
2. Muon slows down and reaches a H₂ molecule
3. Muon is captured at high quantum state and H₂ molecule breaks
4. Muon goes down to ground level losing energy by Auger effect (electron is kicked away) and radiative processes (X-ray emission)
5. The system muon-proton (muonic hydrogen) gains kinetic energy (average energy about 2 eV !)
6. The muonic hydrogen thermalizes due to collision with other molecules (thermalization time depends on density and temperature, order of 100 ns @ 40 bar 300 K)
7. The muon decays OR it is transferred OR it undergoes nuclear capture ($\mu^- + p \rightarrow n + \nu_\mu$)

FAMU: μ^-p spectroscopy

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HFS de-excitation: μ^-p gains kinetic energy

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How is it possible to distinguish HFS excited states?

Hyperfine splitting of $(\mu^-p)_{1S} \sim 183 \text{ meV} \dots$

... but in the triplet to singlet transition muonic hydrogen gains kinetic energy ($\sim 120 \text{ meV}$, 0.12 eV)

μ^- transfer rate to high-Z atoms is energy dependent

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How is it possible to distinguish HFS excited states?

Hyperfine splitting of $(\mu^-p)_{1s} \sim 183$ meV...

... but in the triplet to singlet transition muonic hydrogen gains kinetic energy (~ 120 meV, 0.12 eV)

Key point:

The muon transfer rate to higher-Z atoms in collisions is (kinetic) energy dependent at epithermal energies ($\sim 100/200$ meV)

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- H. Schneuwly, Z. Phys. C - Particles and Fields 56, 280 (1992).
- R. Jacot-Guillarmod, Muon transfer from thermalized muonic hydrogen isotopes Phys. Rev. A51, 2179 ~1995.
- F. Mulhauser and H. Schneuwly, J. Phys. B 26, 4307 ~1993.
- L. Schellenberg, P. Baeriswyl, R. Jacot-Guillarmod, B. Mis- chler, F. Mulhauser, C. Piller, and L. A. Schaller, in *Muonic Atoms and Molecules*, edited by L. A. Schaller and C. Petitjean ~Birkhäuser-Verlag, Basel, 1993, p. 187.
- R. Jacot-Guillarmod, F. Bienz, M. Boschung, C. Piller, L. A. Schaller, L. Schellenberg, H. Schneuwly, W. Reichart, and G. Torelli, Phys. Rev. A 38, 6151 ~1988.
- A. Werthmüller, A. Adamczak, R. Jacot-Guillarmod, F. Mulhauser, C. Piller, L. A. Schaller, L. Schellenberg, H. Schneuwly, Y.-A. Thalmann, and S. Tresch, Hyperfine Interact. 103, 147~1996.
- A. Werthmüller et. al. Energy dependence of the charge exchange reaction from muonic hydrogen to oxygen ; Hyperfine Interactions 116 (1998) 1–16 1.

μ^- transfer rate to high-Z atoms is energy dependent

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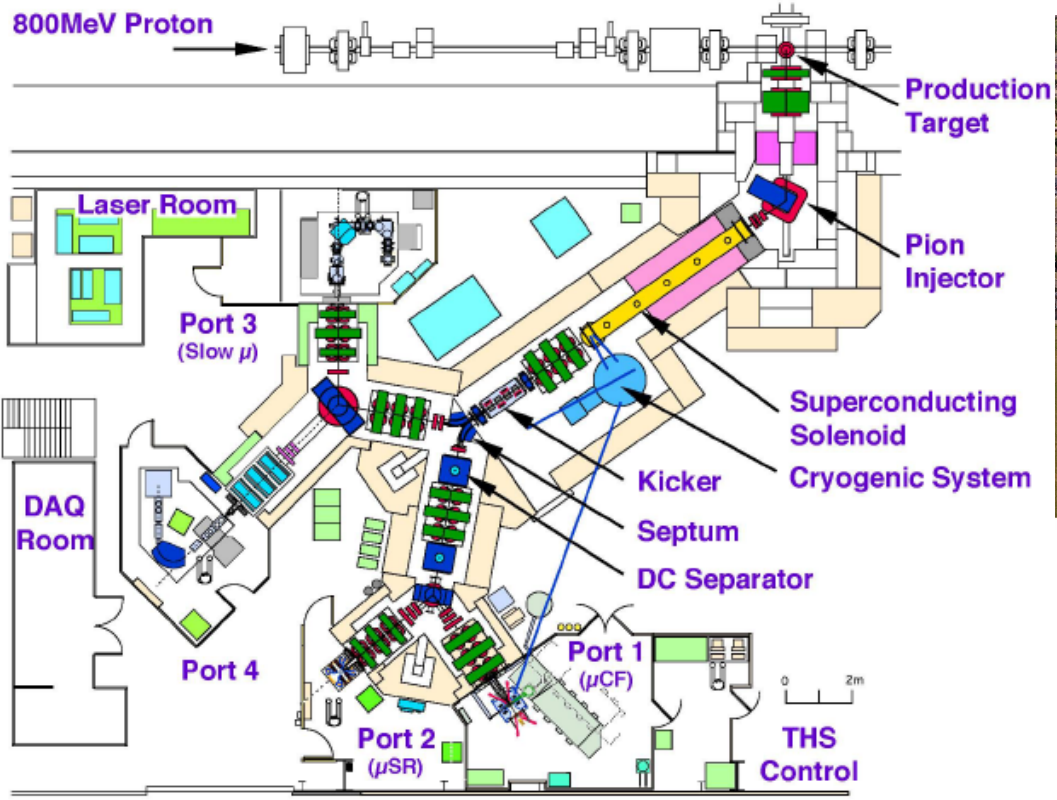
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Many indications, no accurate and comprehensive study of this effect!

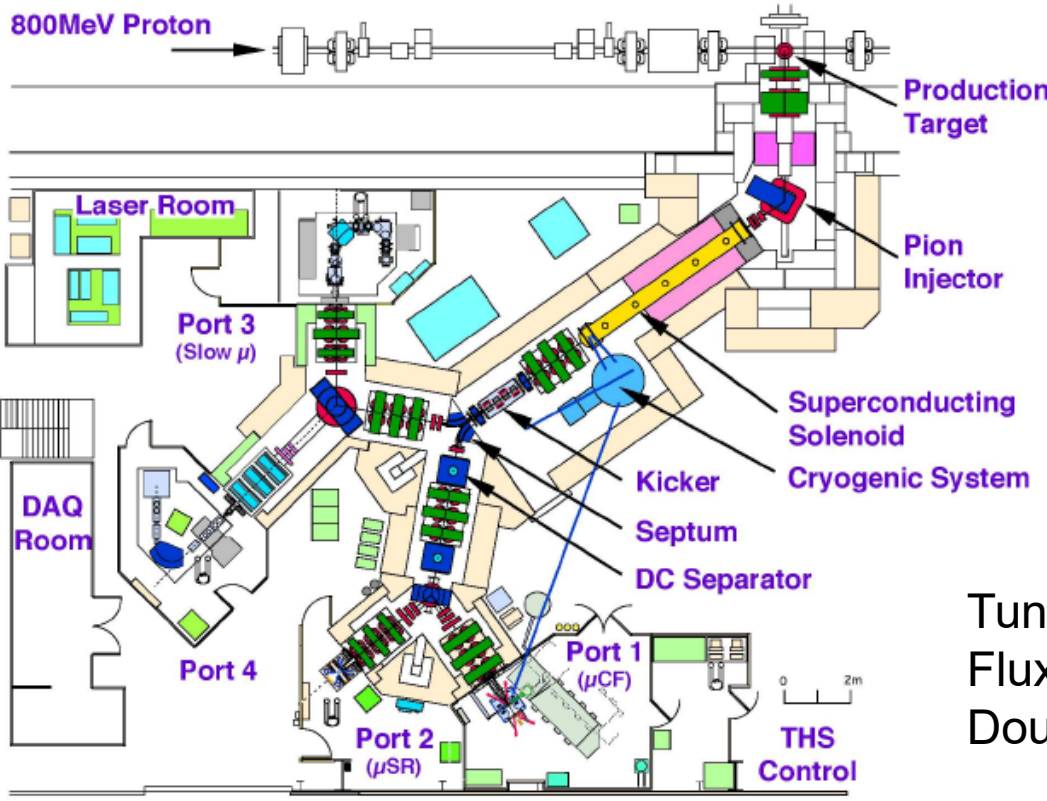
Apparatus setup

RIKEN – RAL muon facility

Rutherford Appleton Laboratory – Oxfordshire UK

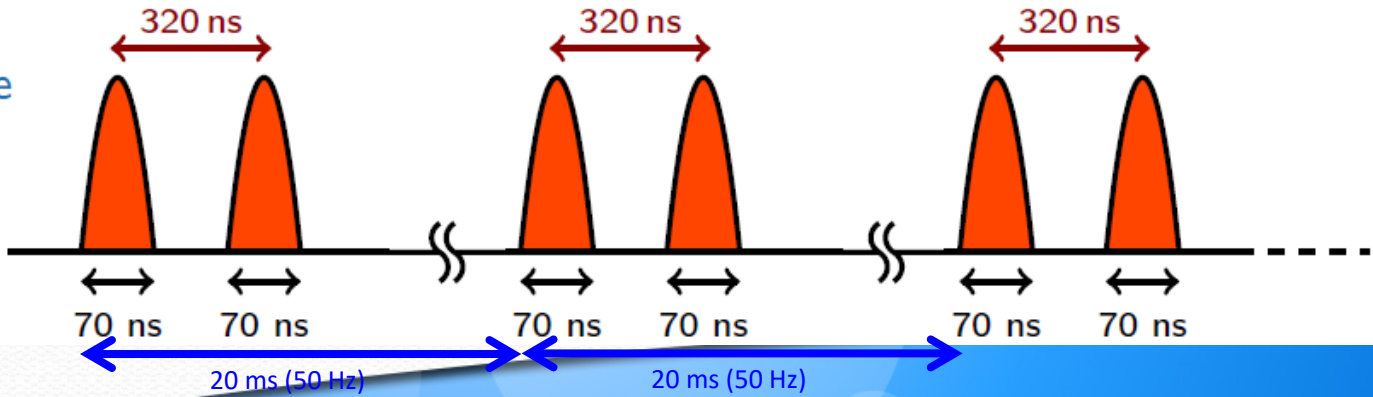


High intensity muon beam

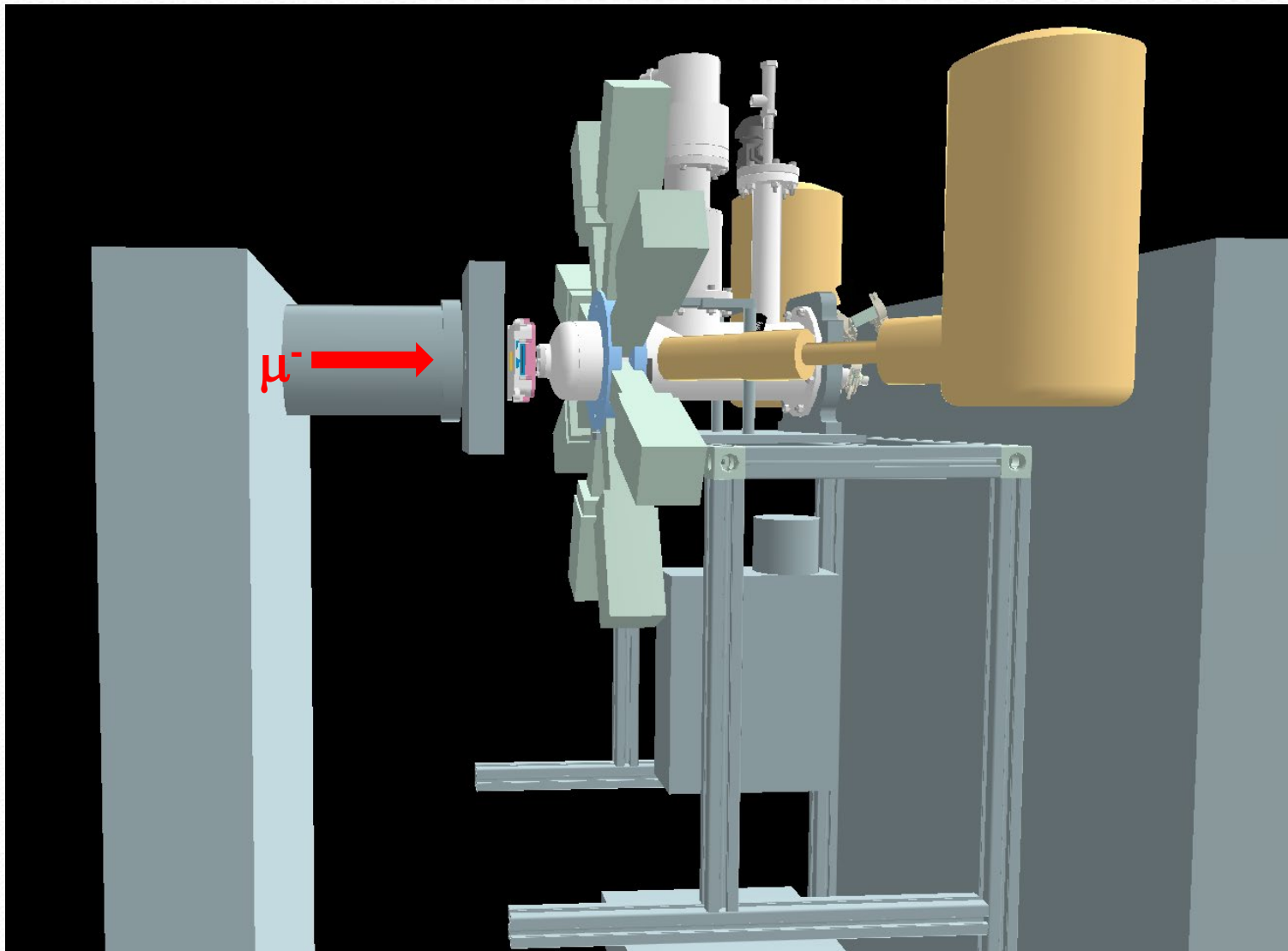


Tunable momentum: 20 – 120 MeV/c
 Flux μ^- : 7×10^4 muons/s
 Double pulsed beam

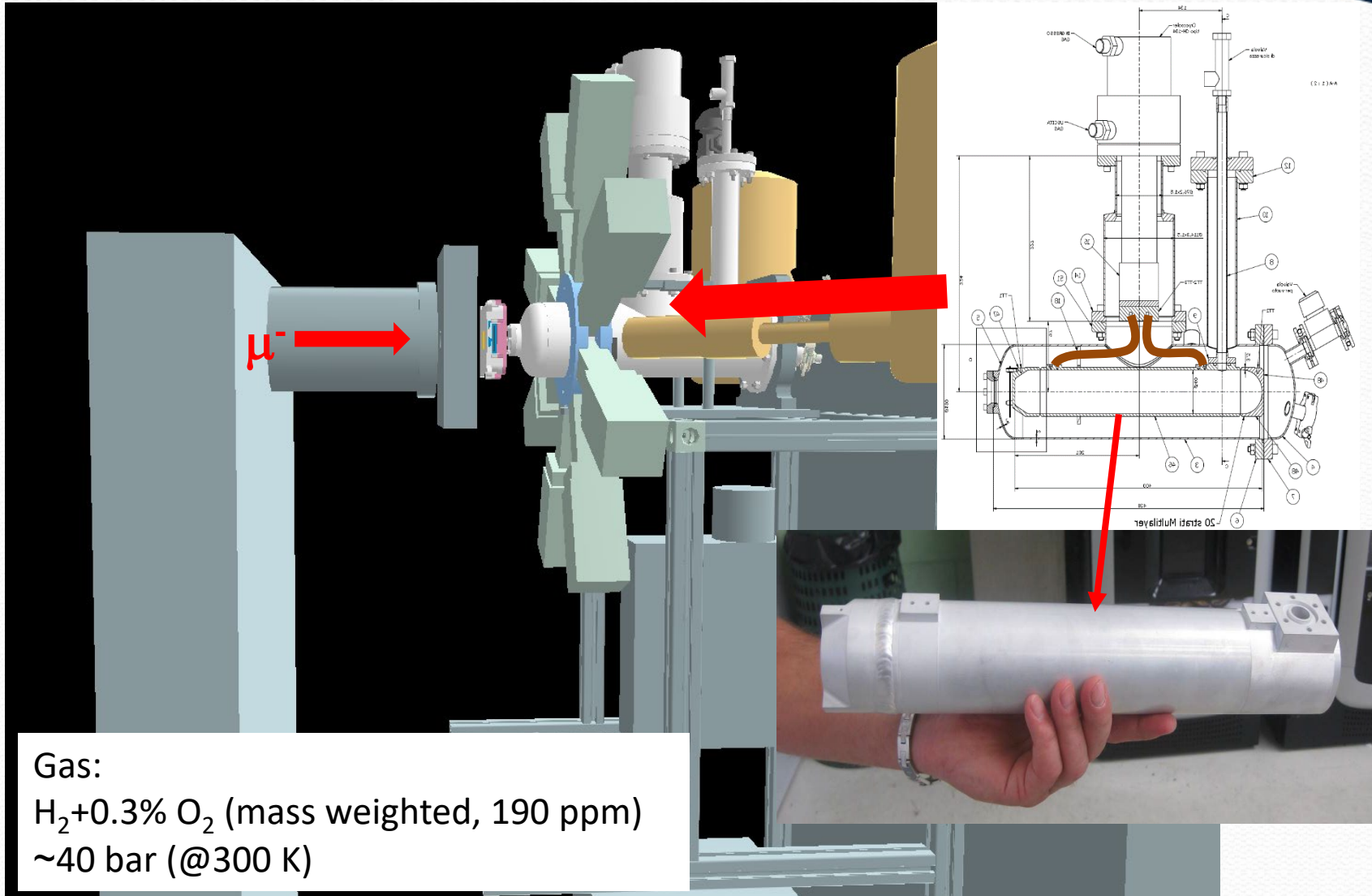
Beam time structure



2016: experimental setup

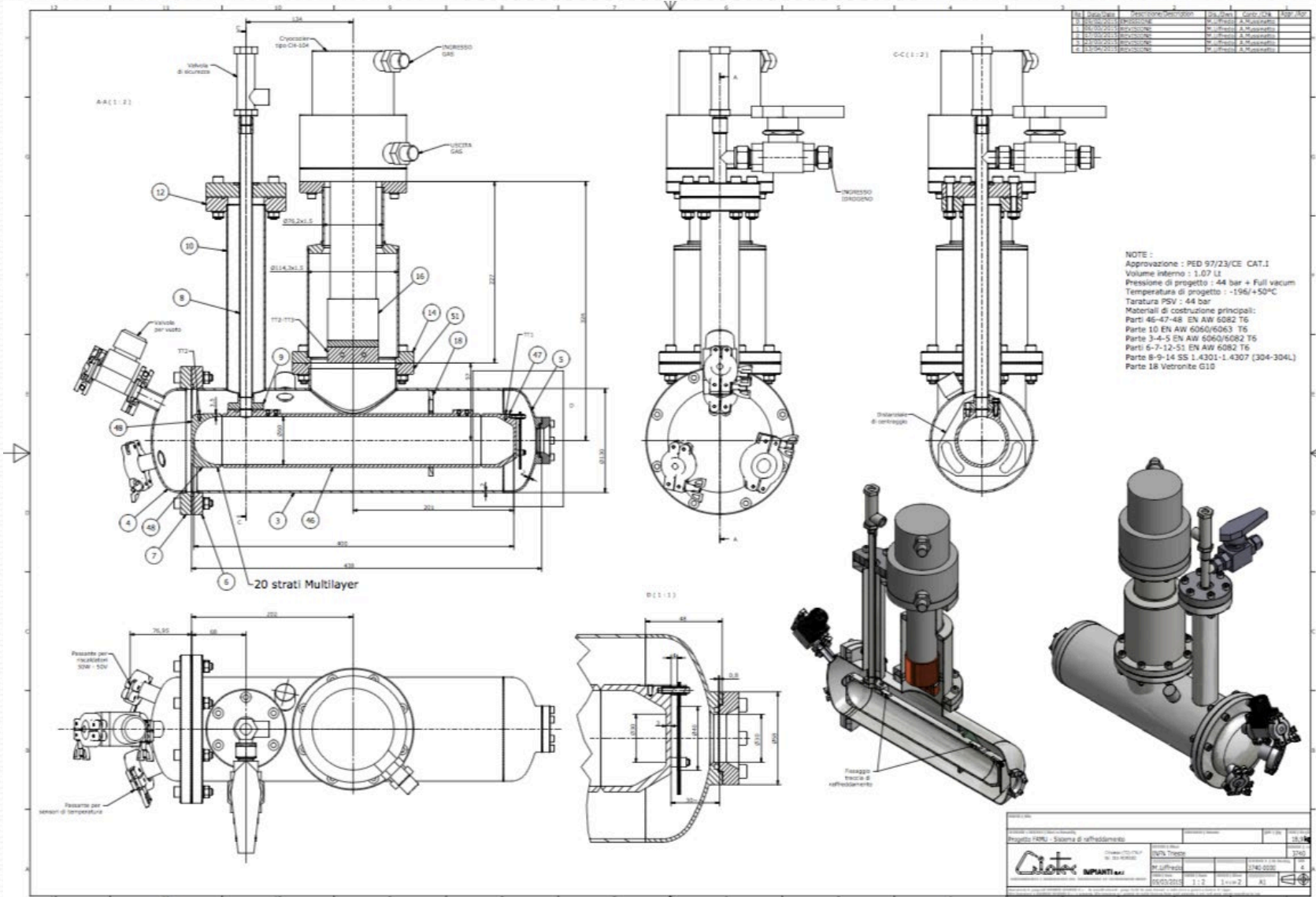


Cryogenic thermalized target

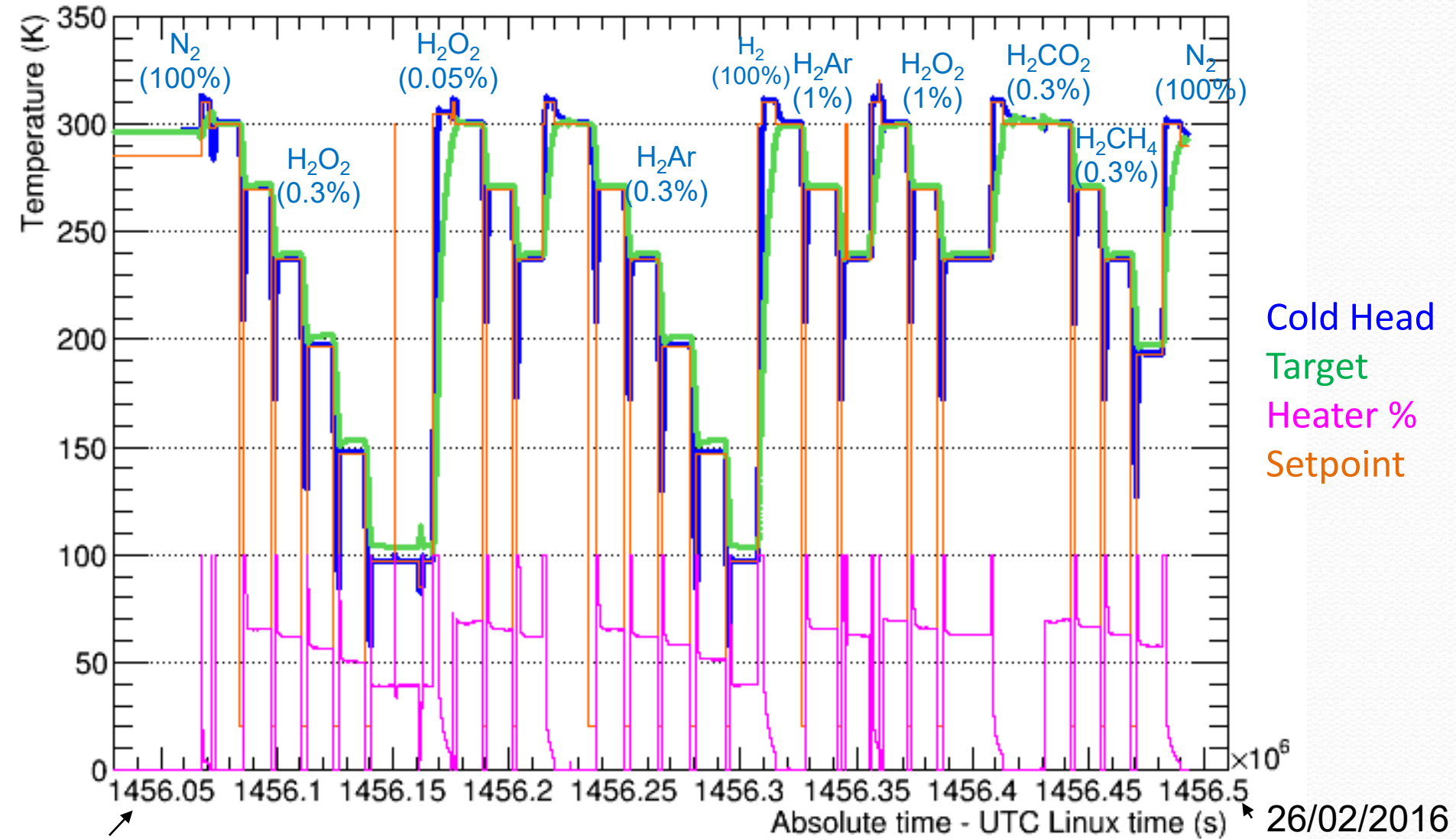


Gas:
 $\text{H}_2 + 0.3\% \text{O}_2$ (mass weighted, 190 ppm)
~40 bar (@300 K)

2016 cryogenic target

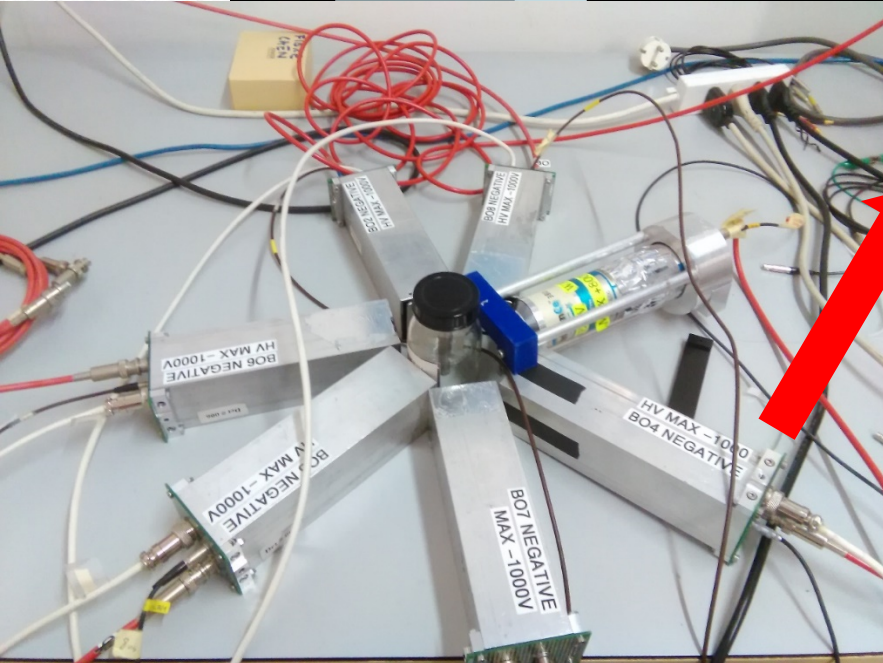
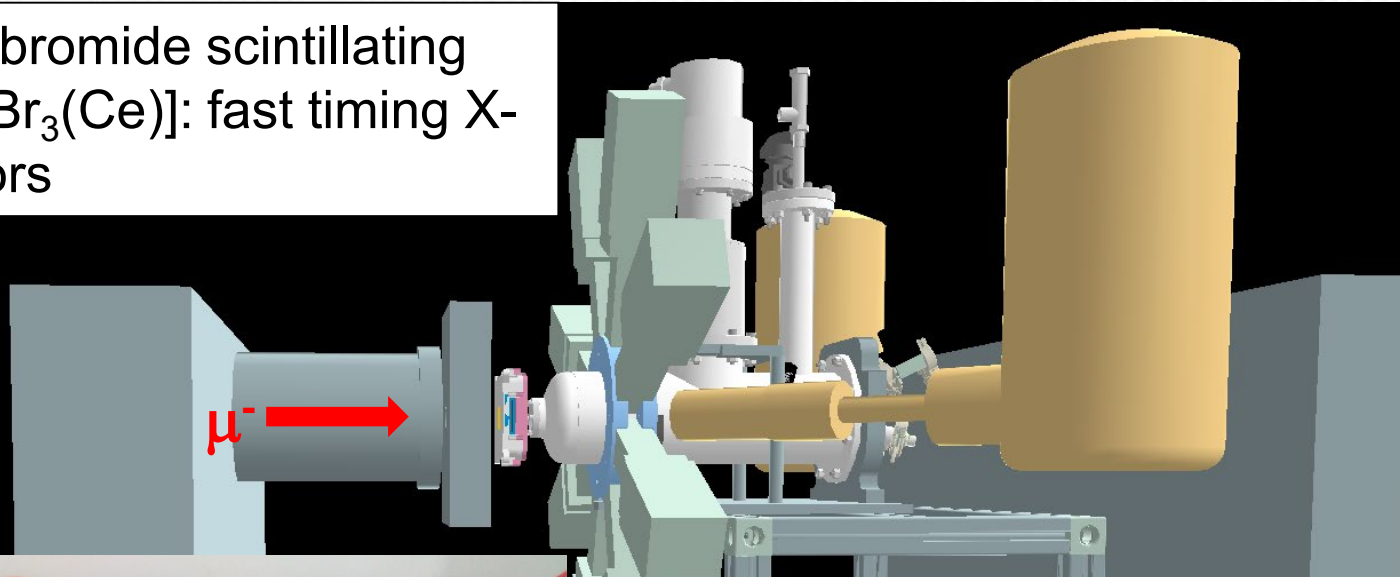


Thermal cycles 2016



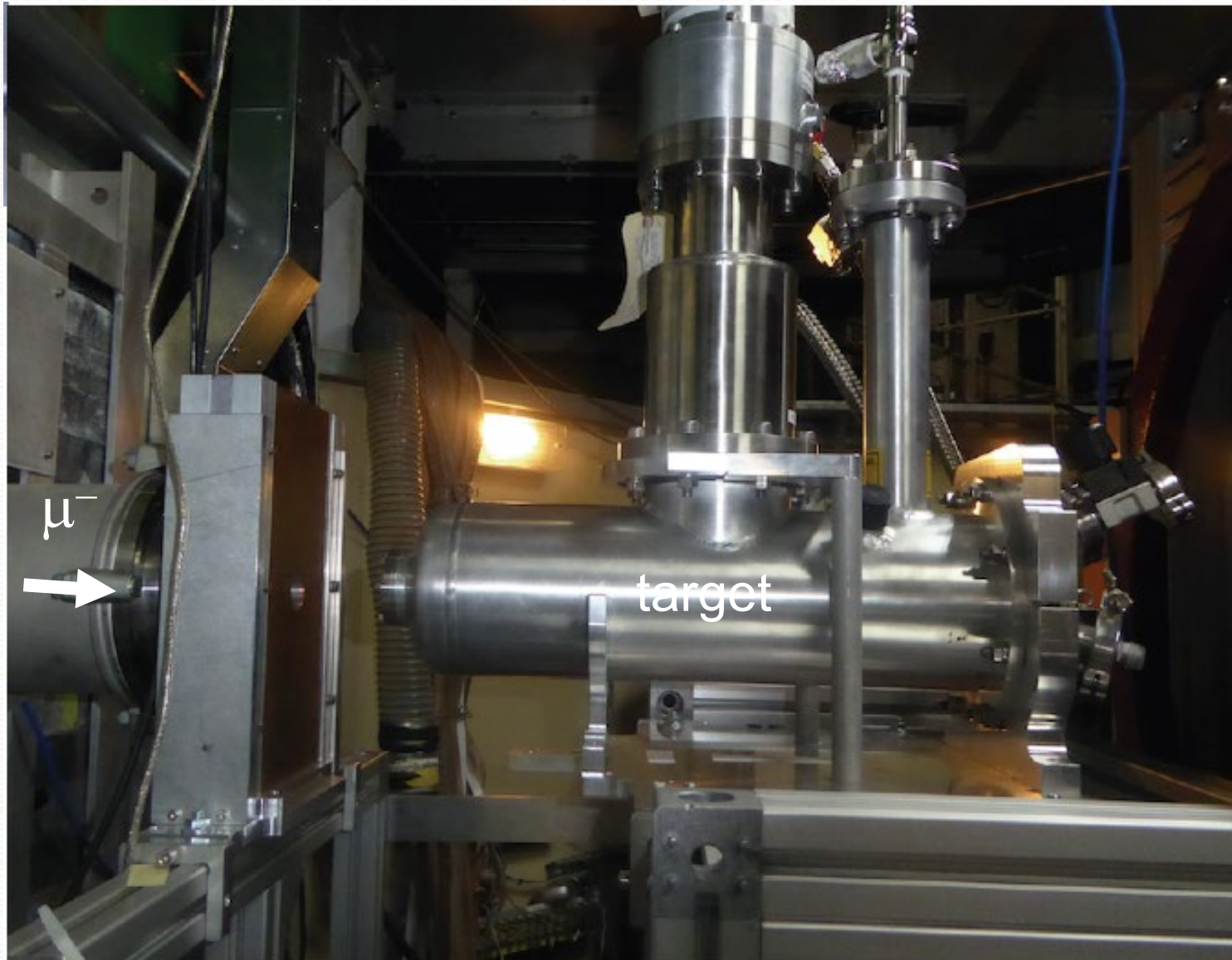
2016: experimental setup

Lanthanum bromide scintillating crystals [LaBr₃(Ce)]: fast timing X-rays detectors

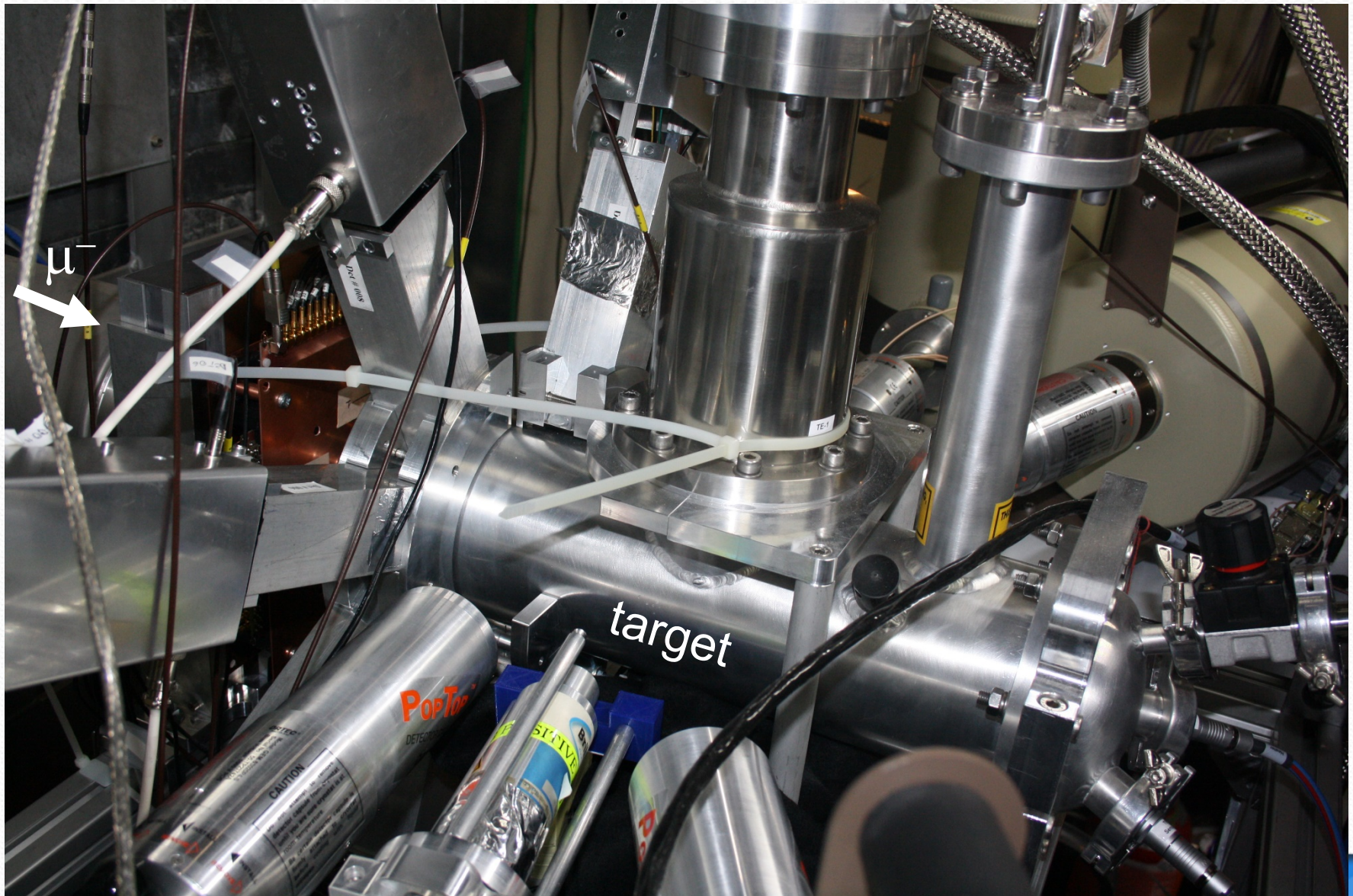


- 8 cylindrical 1 inch diameter 1 inch long LaBr₃(5%Ce) crystals
- read by PMTs
- fast electronics and fast digital processing signal available

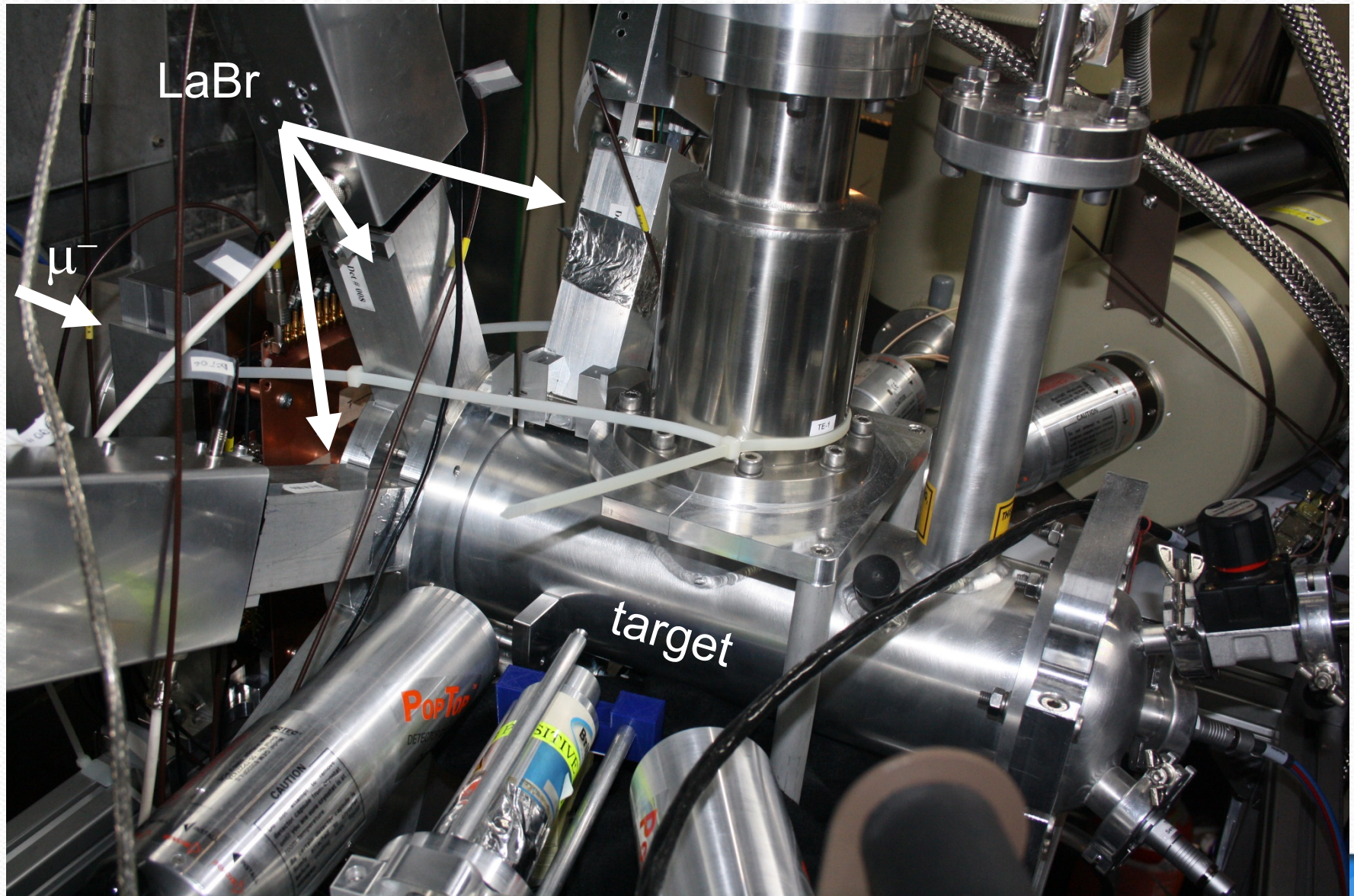
2016: experimental setup



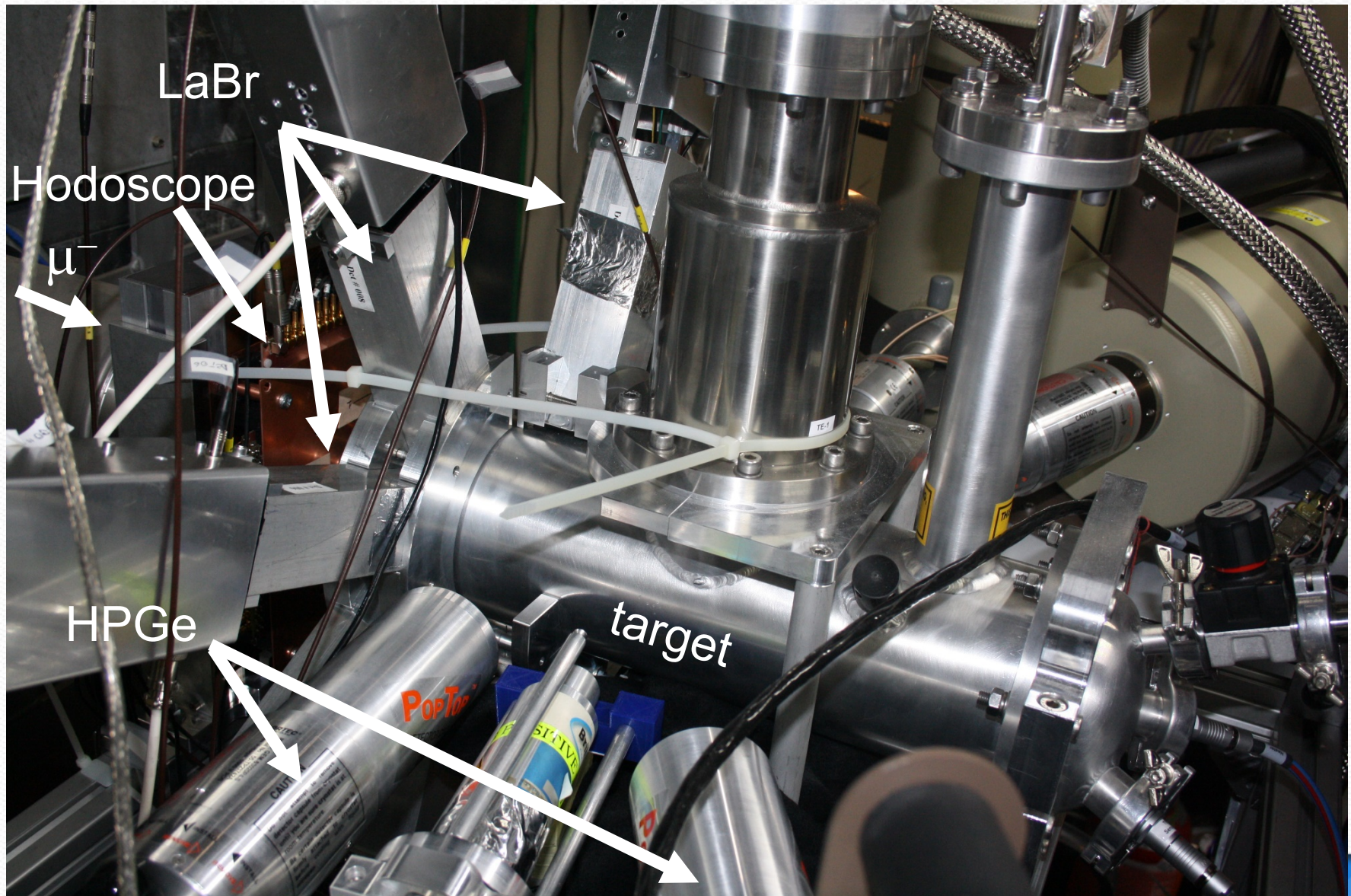
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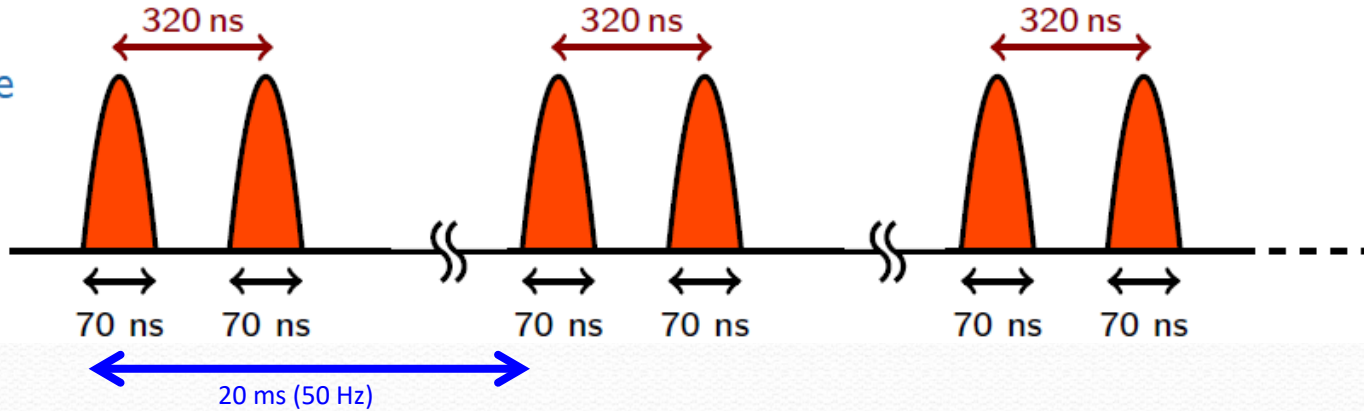
2016: experimental setup



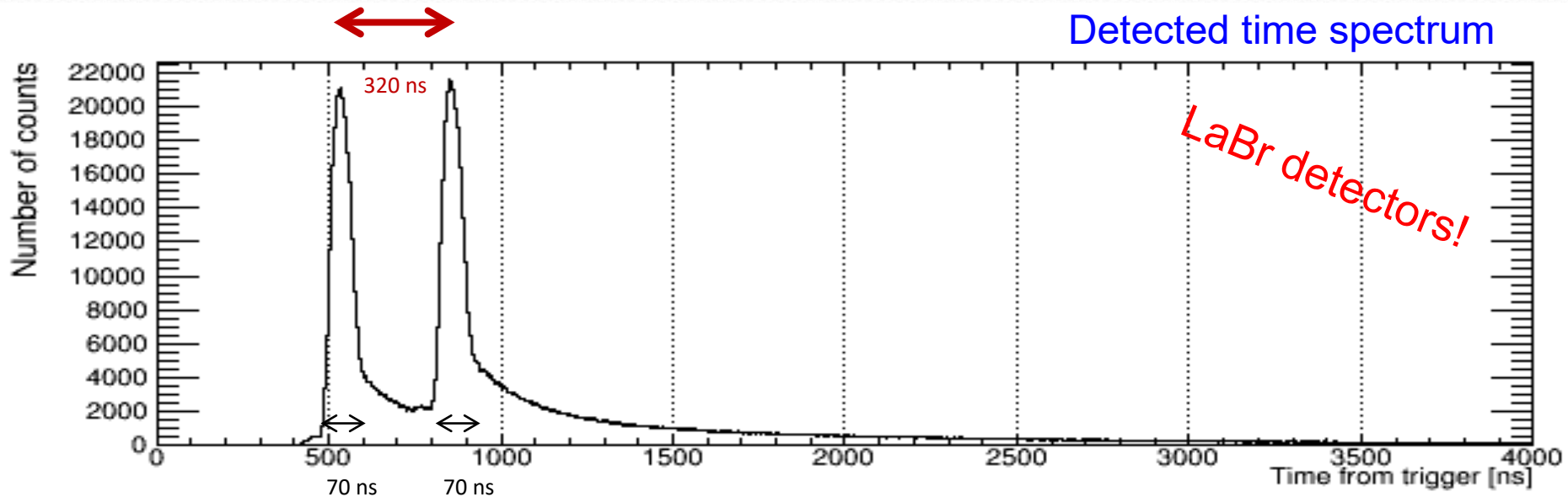
Measurement of the transfer rate $\Lambda_{\mu p \rightarrow \mu O}$

Time spectrum: peaks and tails

Beam time structure

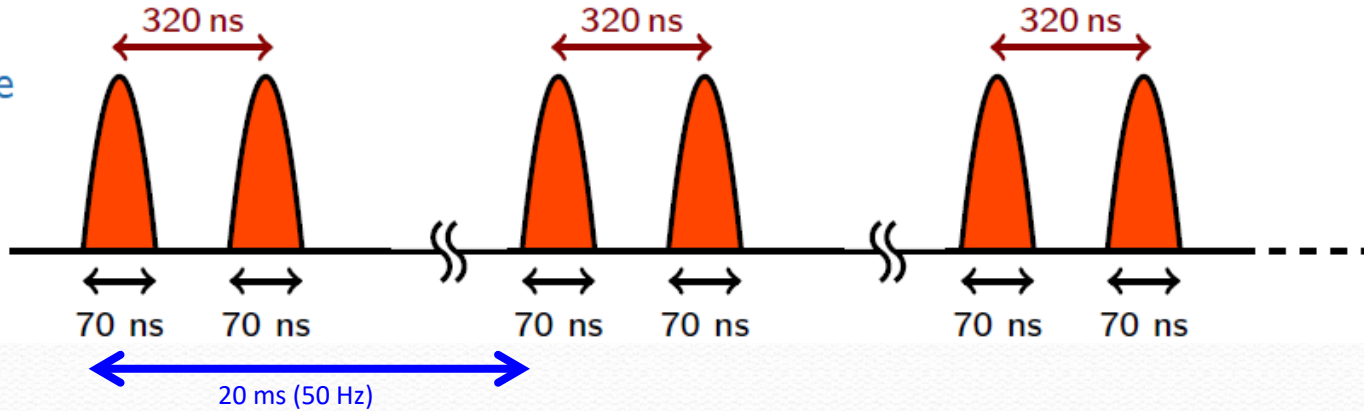


Detected time spectrum

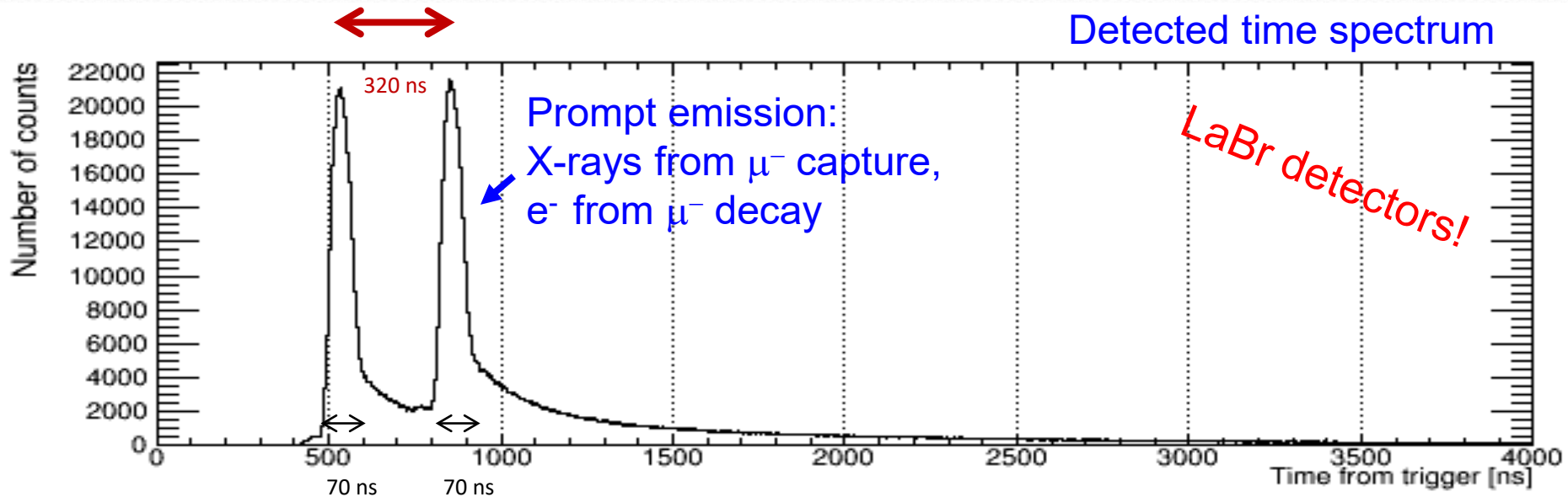


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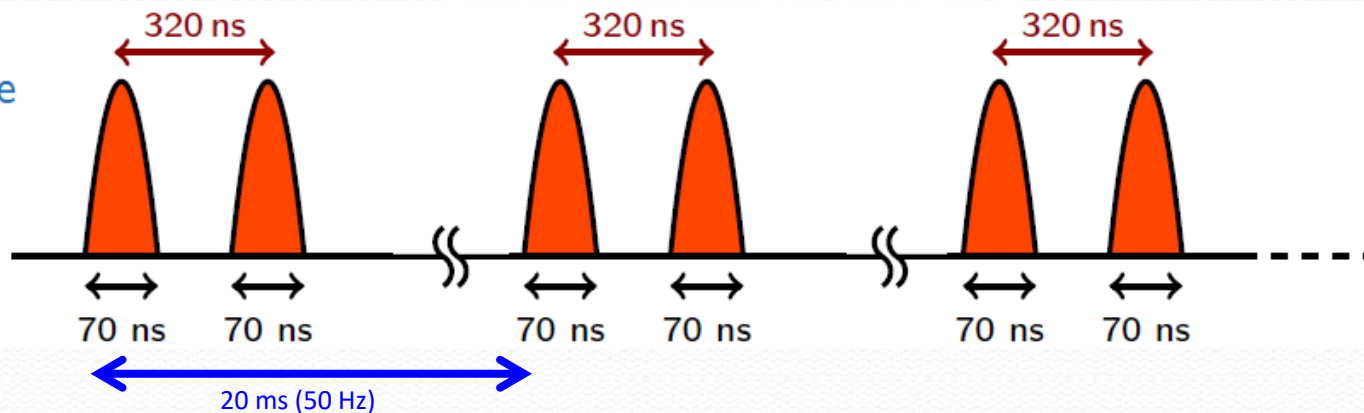


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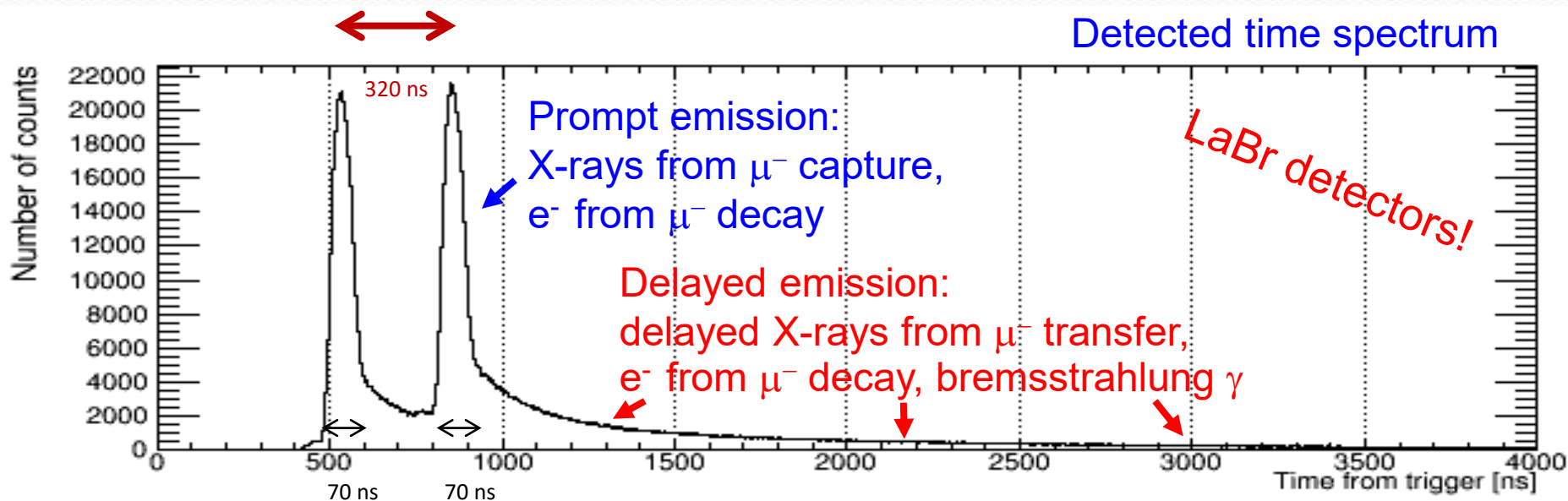


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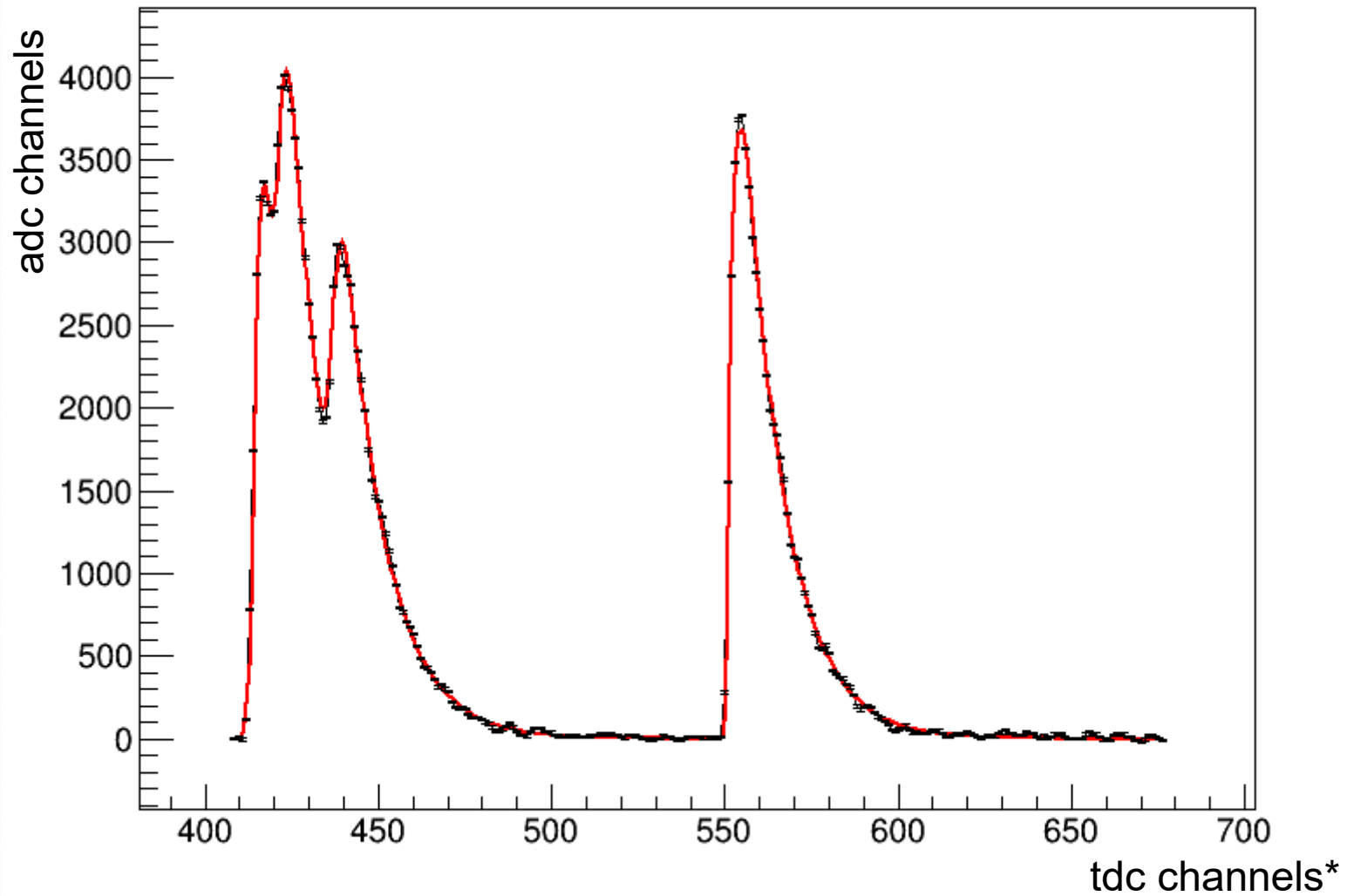


Transfer rate measurement

Steps:

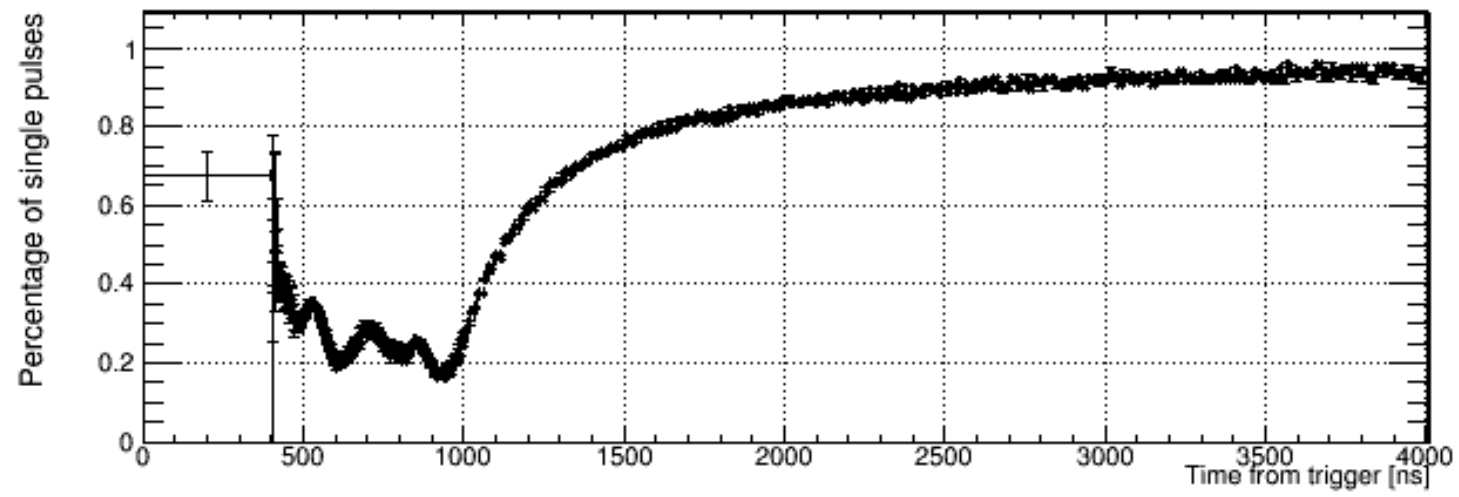
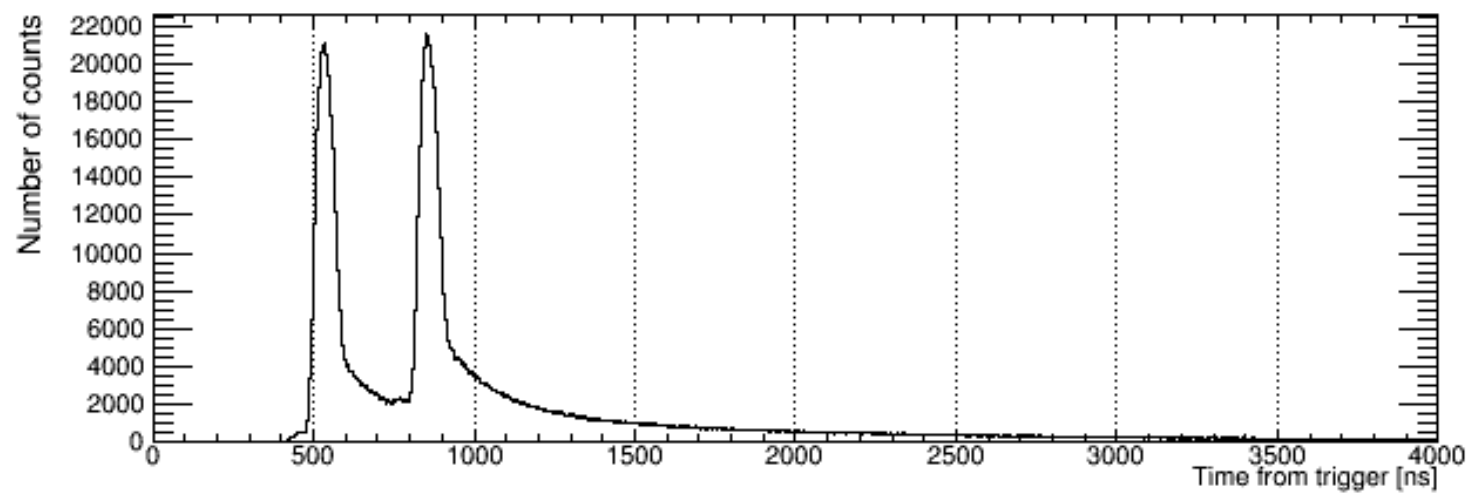
- 1) fix a target temperature (i.e. mean kinetic energy of gas constant)
- 2) produce μp and wait for thermalization
- 3) study time evolution of Oxygen X-rays (133 keV/ \sim 160 keV)
- 4) repeat with different temperature

Waveforms fit



* 1 tdc = 2 ns

Mostly single pulses in delayed phase

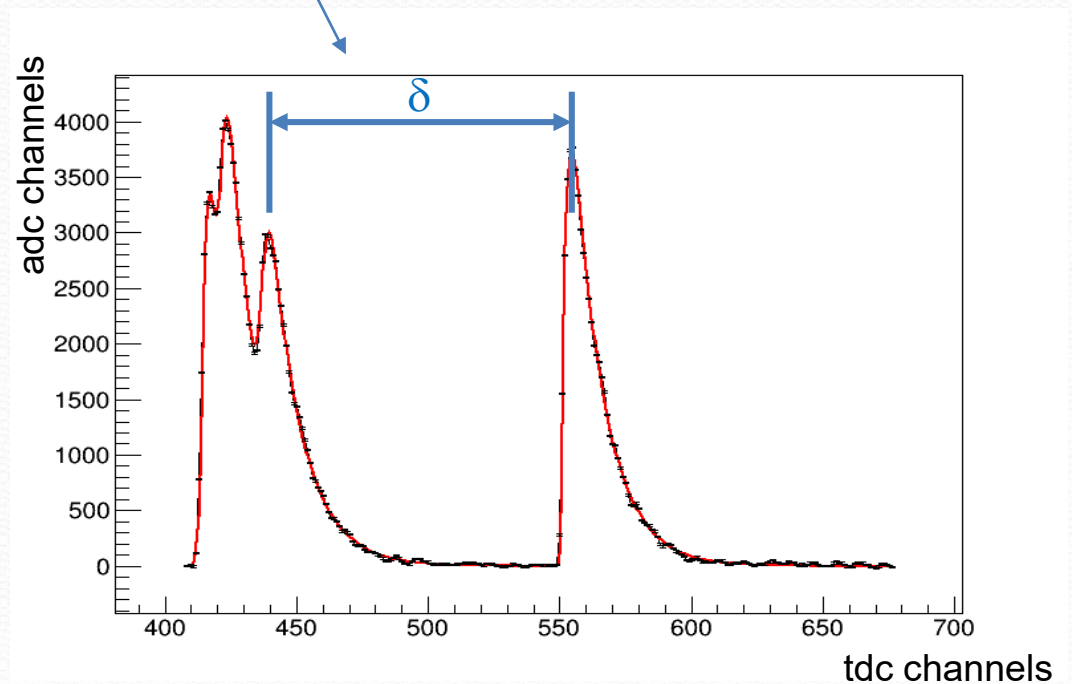


Data selection

1. “Reasonable” reduced χ^2 from the fit

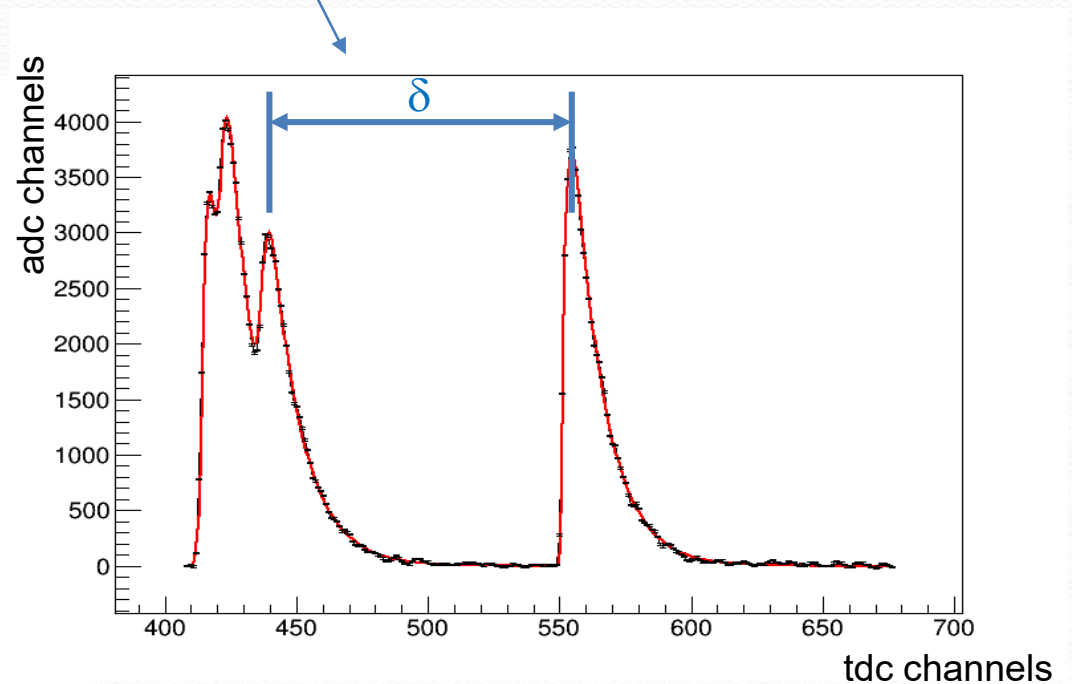
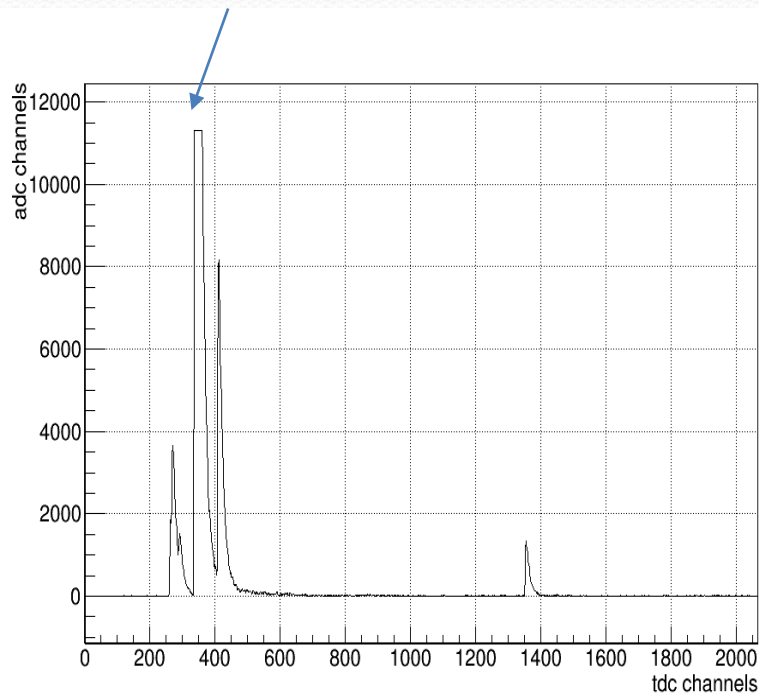
Data selection

1. “Reasonable” reduced chi2 from the fit
2. Distance (δ) between pulses > 30 ns

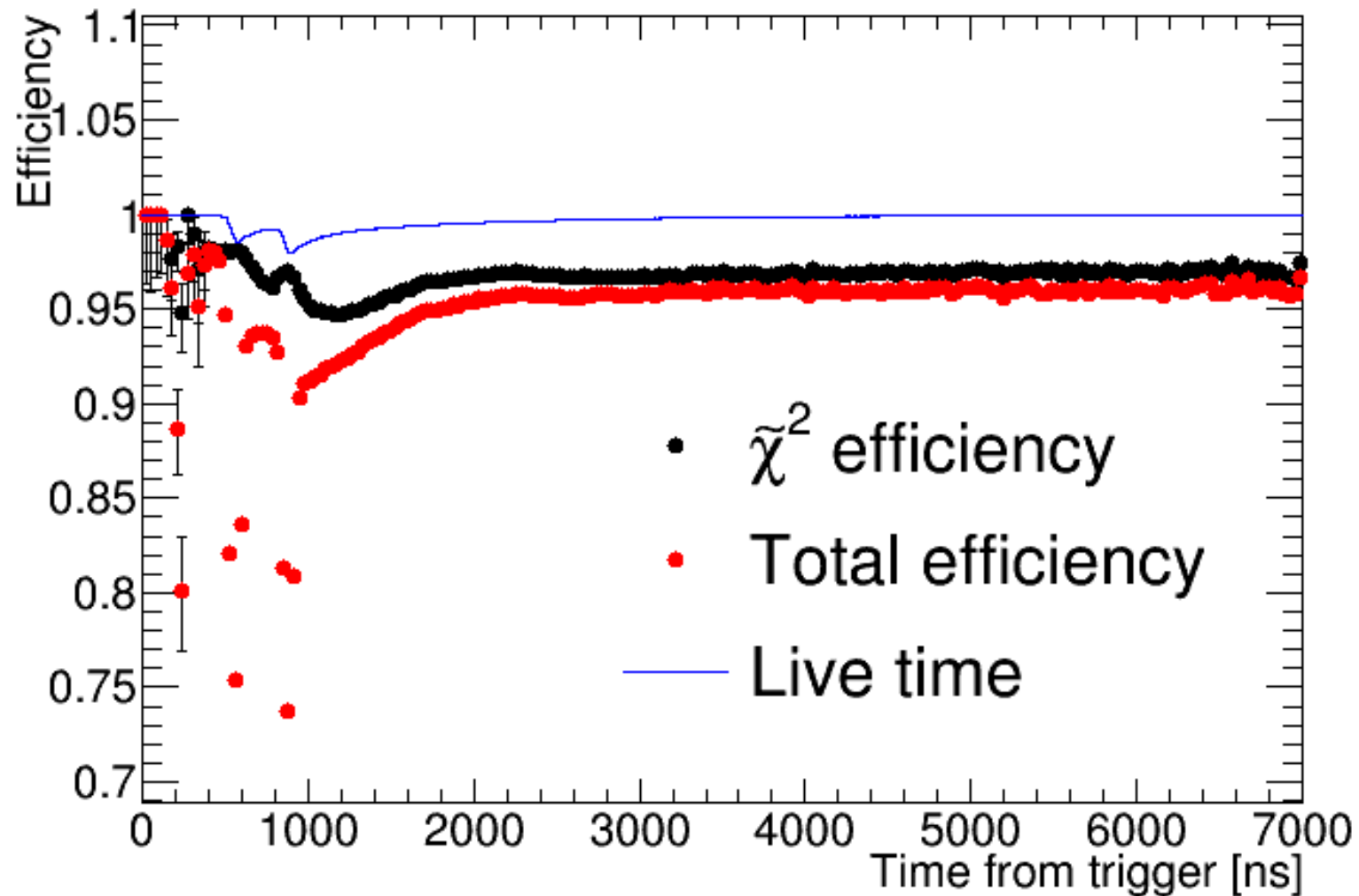


Data selection

1. “Reasonable” reduced chi2 from the fit
2. Distance (δ) between pulses > 30 ns
3. No saturated events



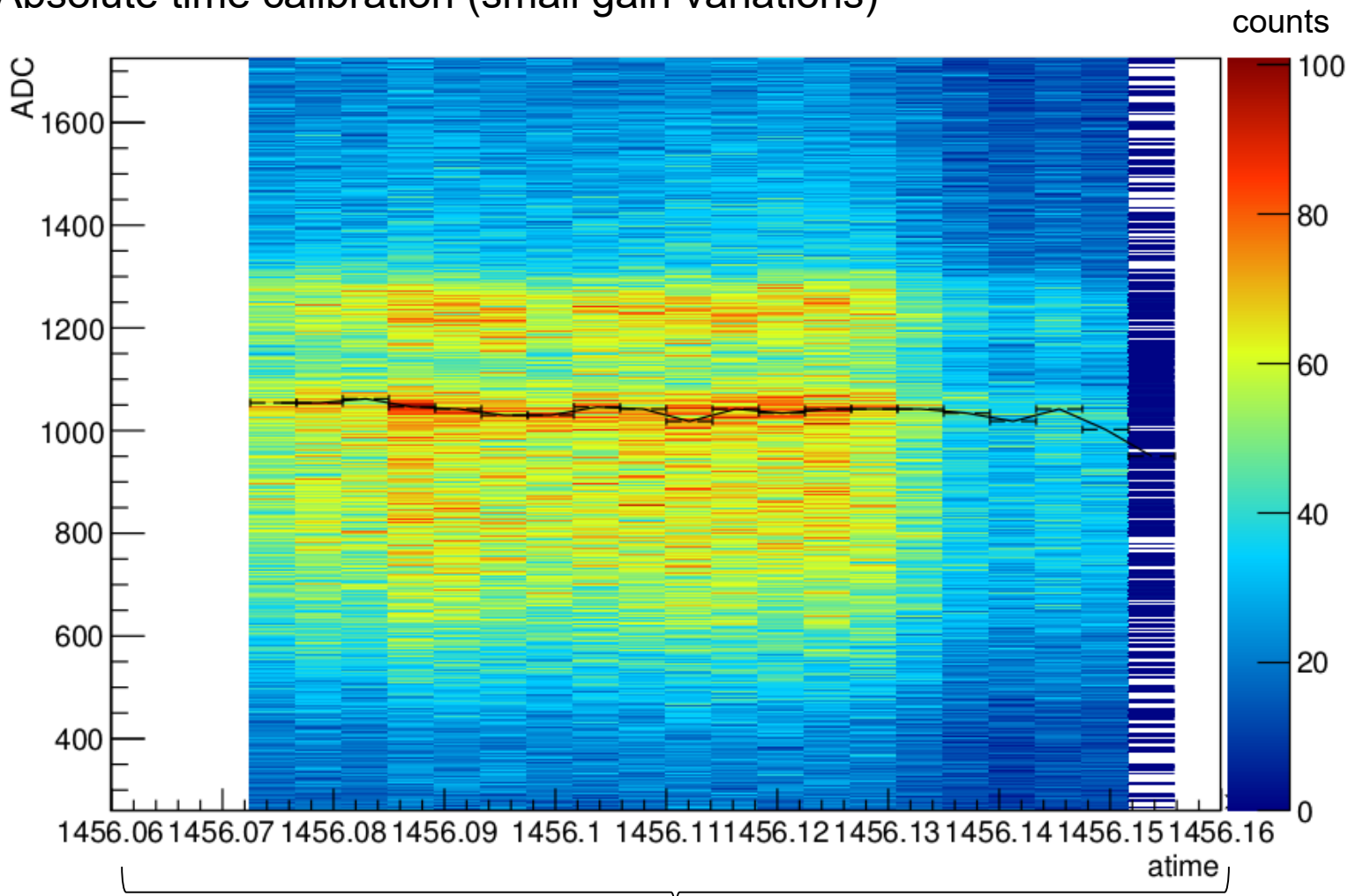
High selection efficiencies



Calibrations

LaBr3 detectors calibration

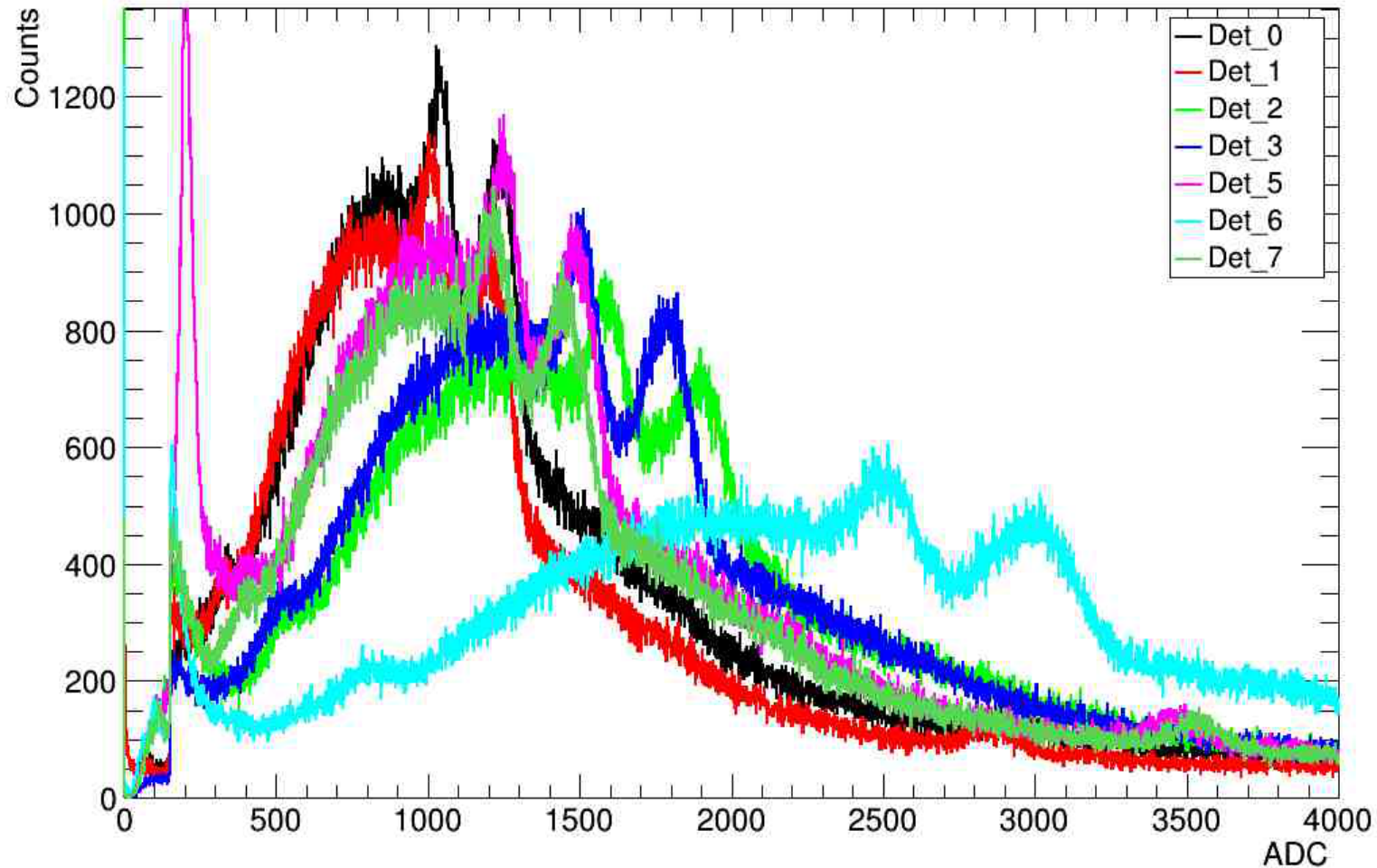
Absolute time calibration (small gain variations)



~1 day of data

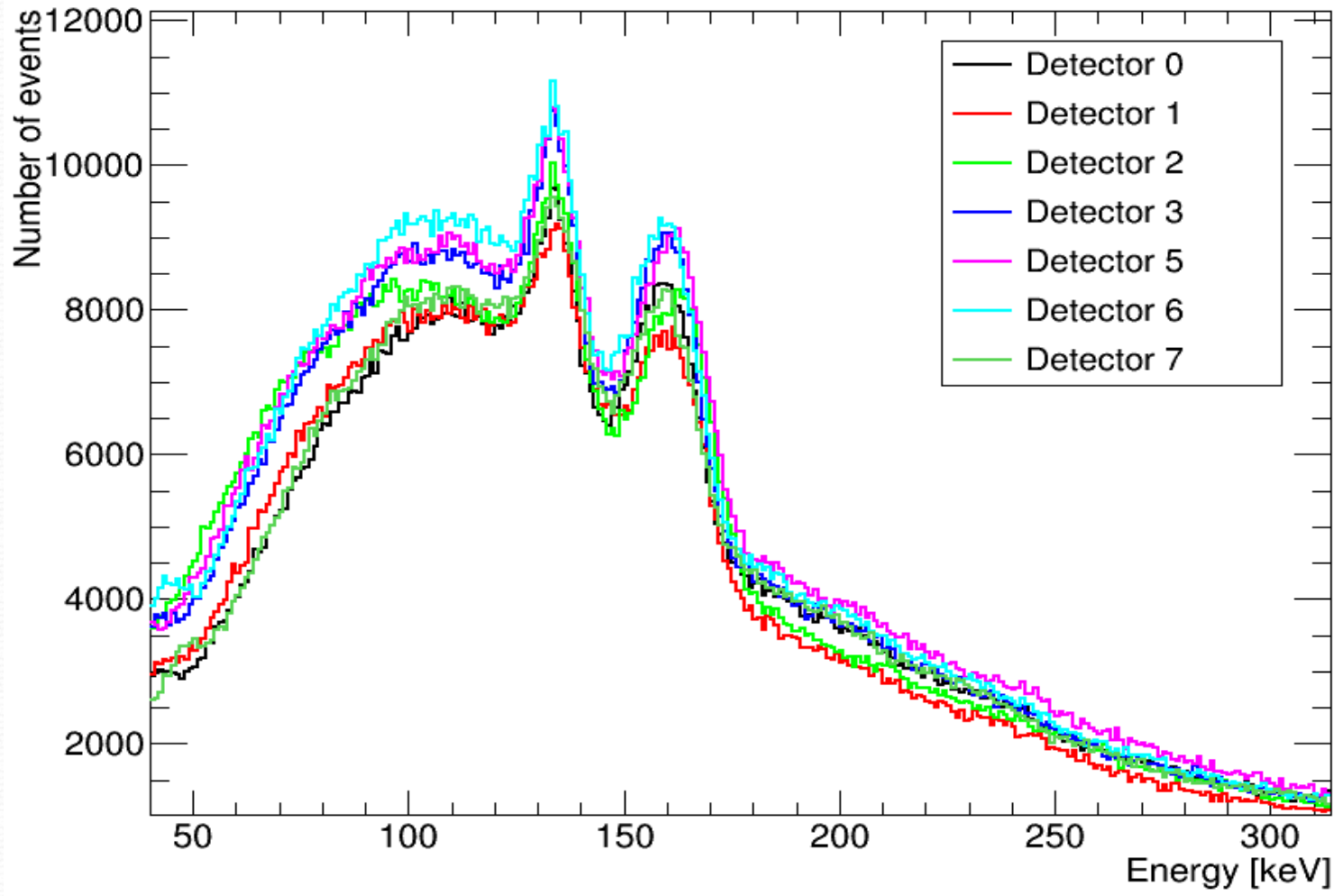
LaBr3 detectors calibration

Oxygen lines (uncalibrated)

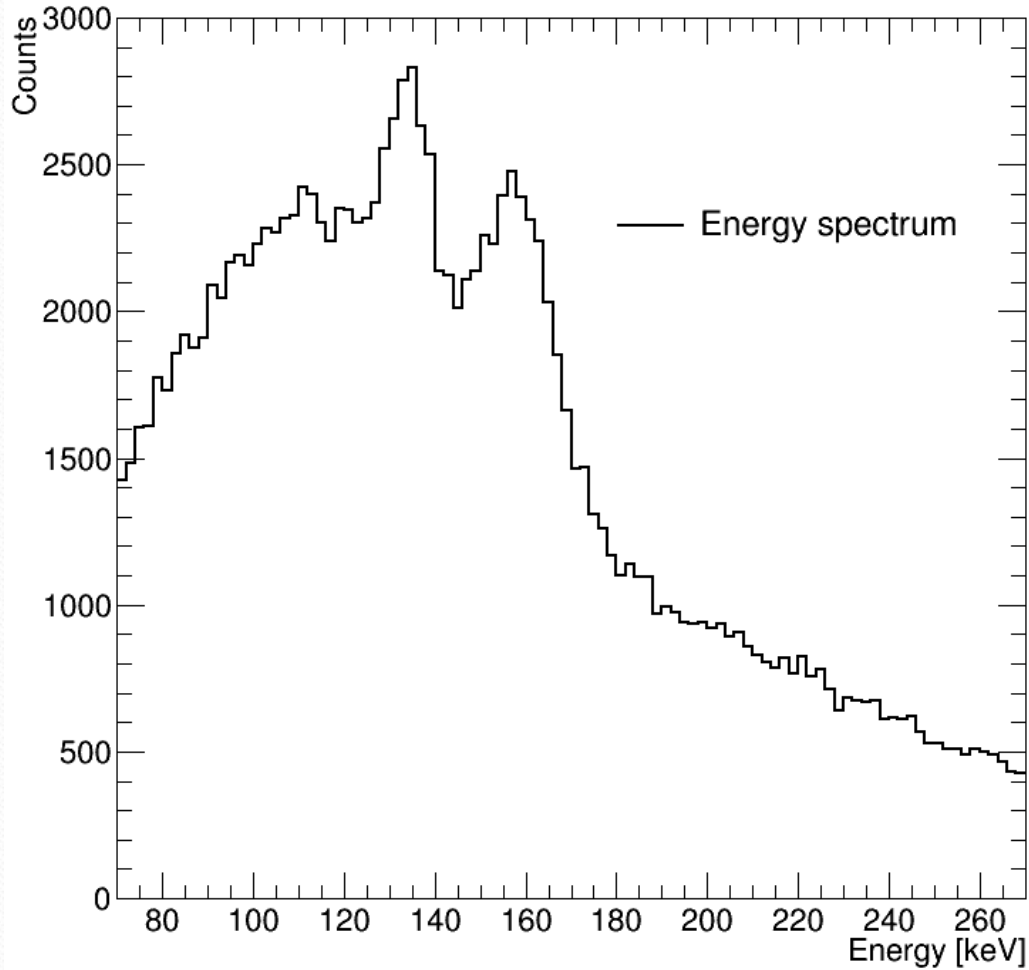


LaBr3 detectors calibration

Oxygen lines (calibrated)



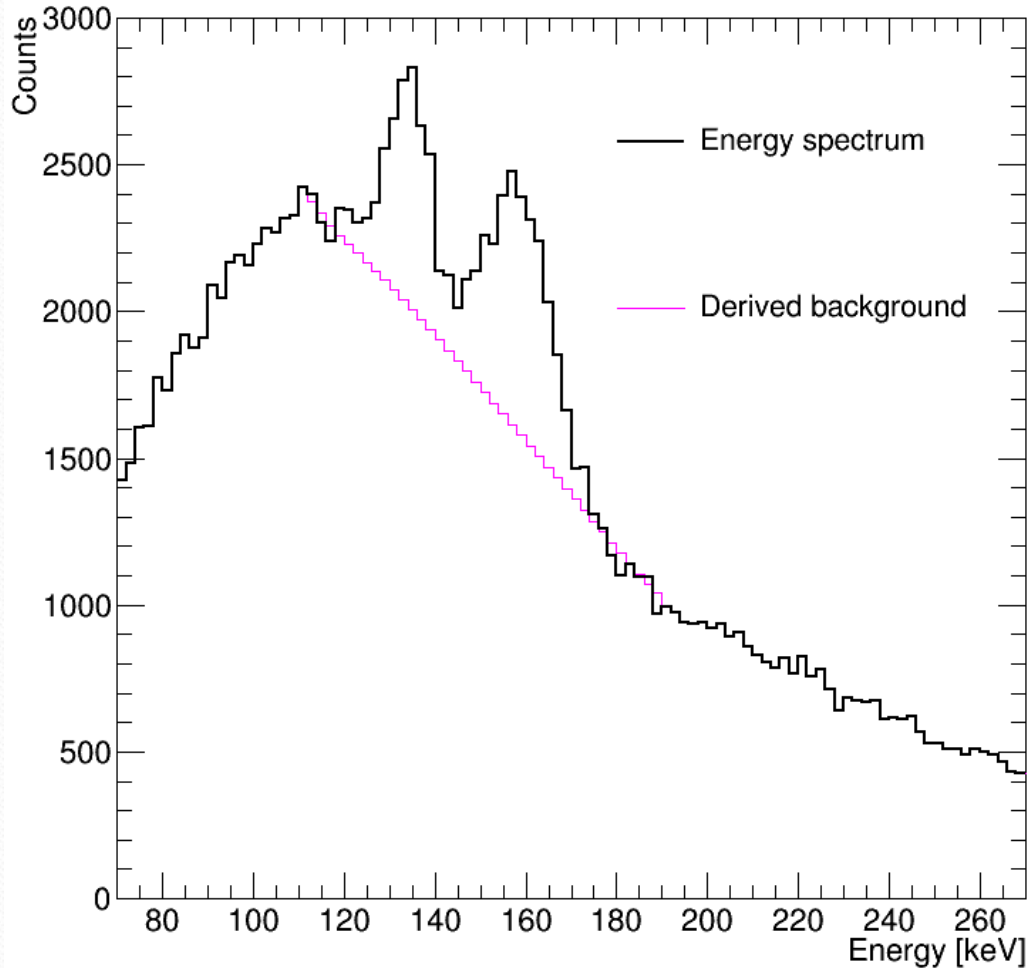
The background problem...



$T = 300 \text{ K}$

Time bin = [1450, 1650] ns

Simplest solution: "straight line"



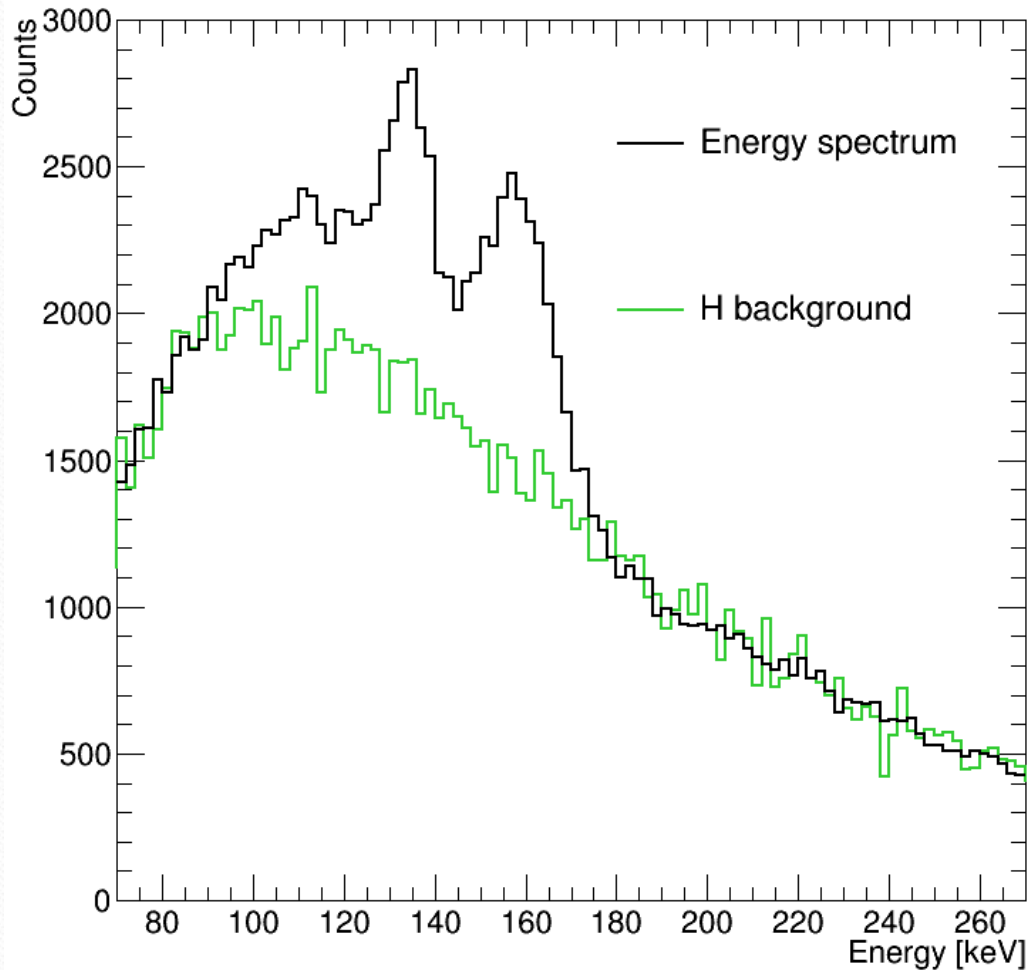
$T = 300 \text{ K}$

Time bin = [1450, 1650] ns

Using ROOT/"TSpectrum"
class – spectroscopic
algorithms

Problem: unstable results...

Better solution: pure hydrogen



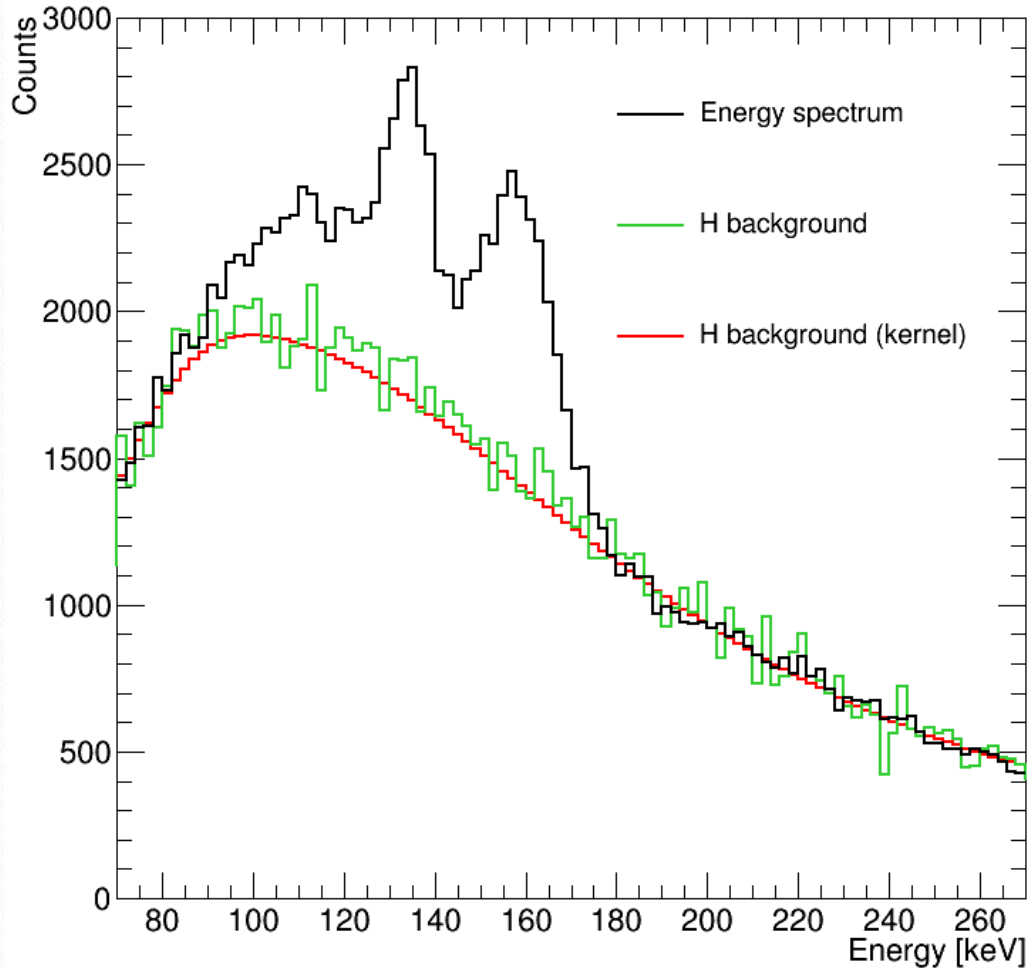
$T = 300 \text{ K}$

Time bin = [1450,1650] ns

Pure hydrogen data taking within the same beam time and with the same pressure and temperatures.

However: poor statistics...

Best solution: pure H smoothing

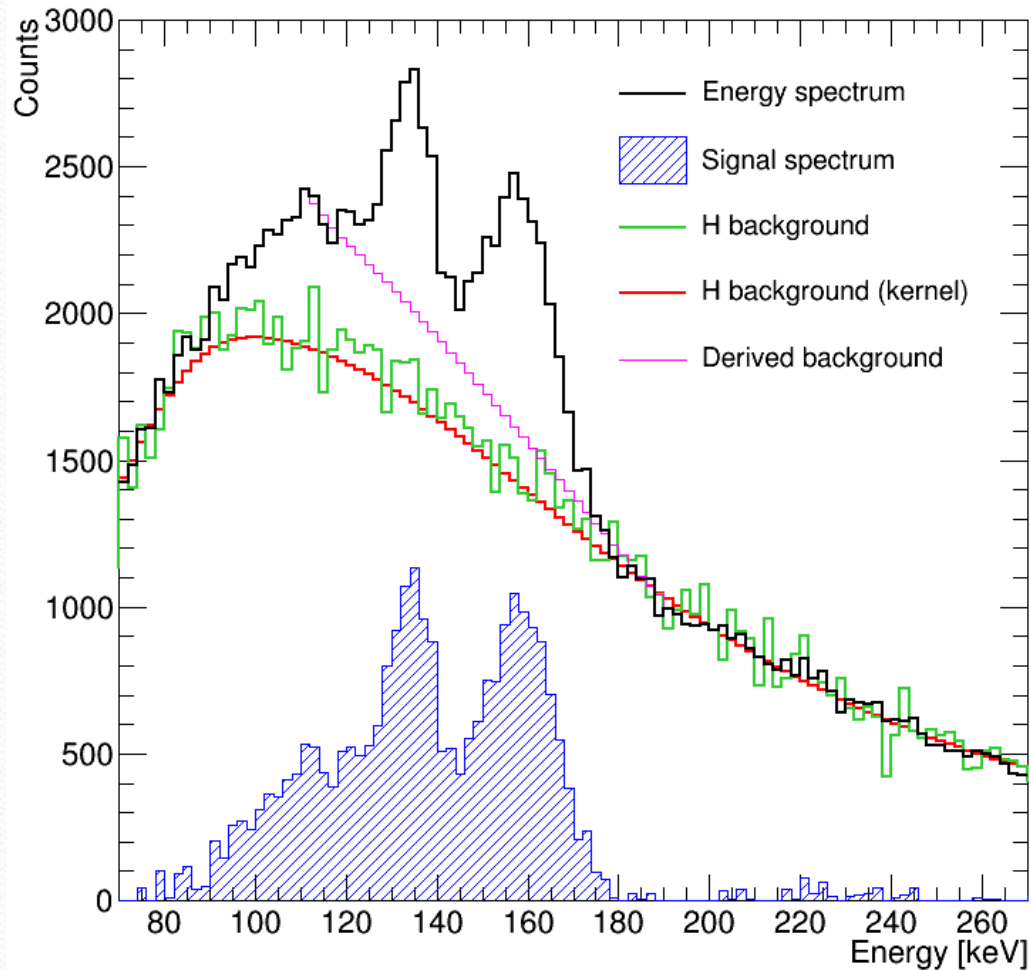


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Simulation studies

GEANT4 simulation with tuning

FAMU 2016 apparatus and detectors simulation:

- Geometry
- Digitization
- Reconstruction using the same programs used for real data

GEANT4 physics tuning, corrections and add-ons:

- Muonic X-ray lines not reproduced correctly
- Transfer rate process not implemented

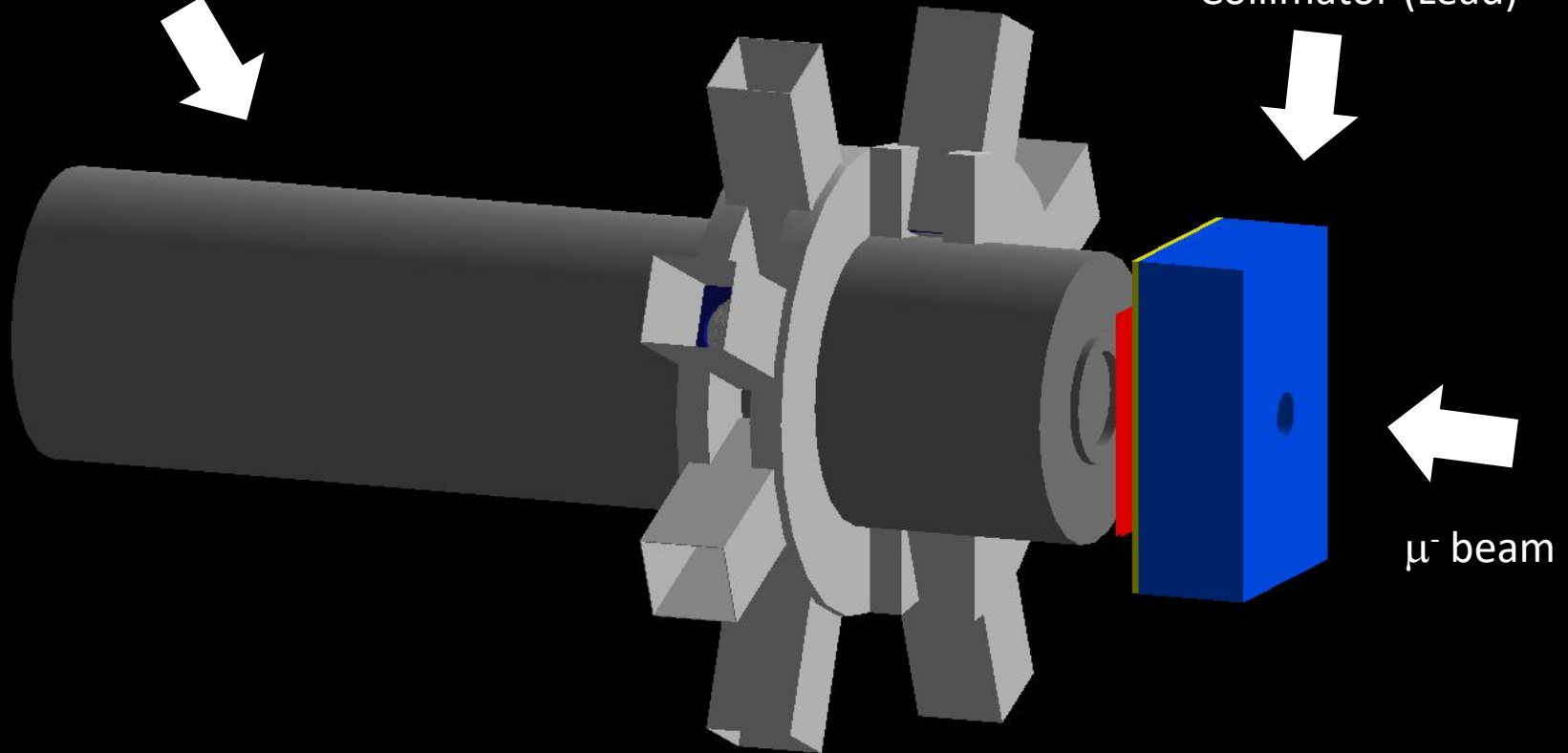
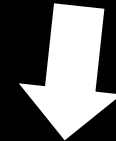
Custom physics-list which solves (partially) these missing items

FAMU simulated geometry

Cryogenic container (Aluminium)

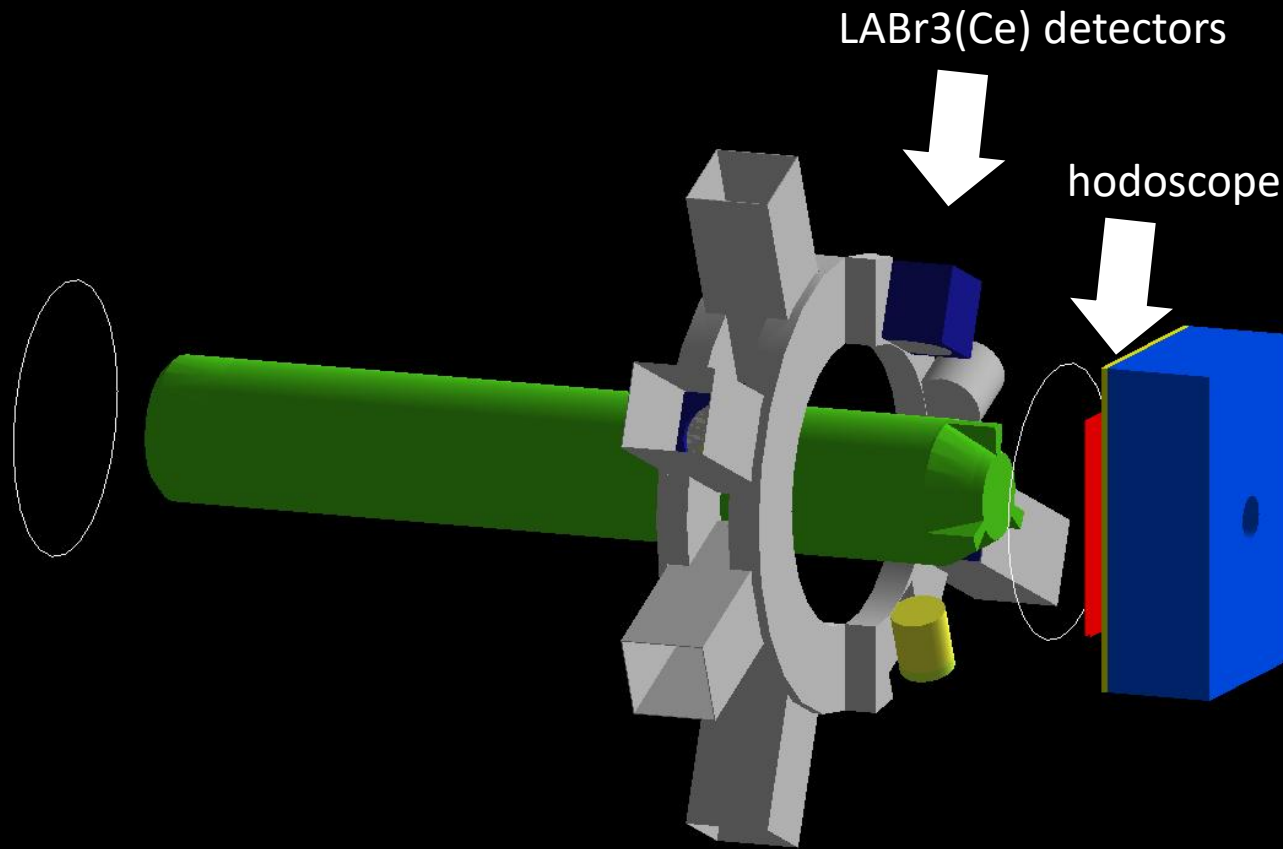


Collimator (Lead)



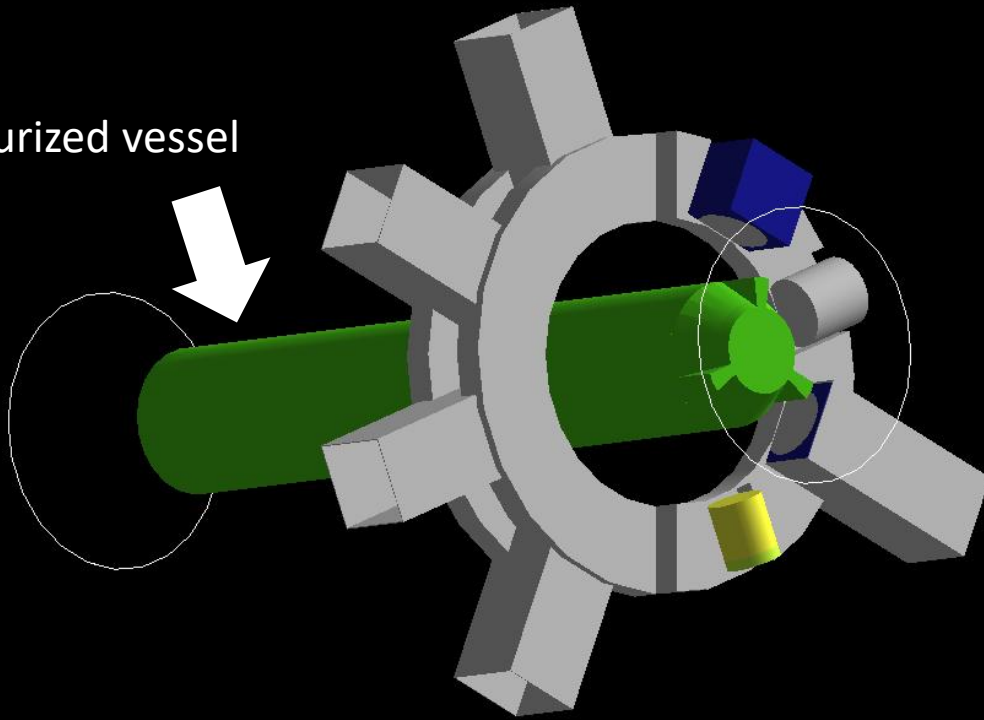
μ^- beam

FAMU simulated geometry

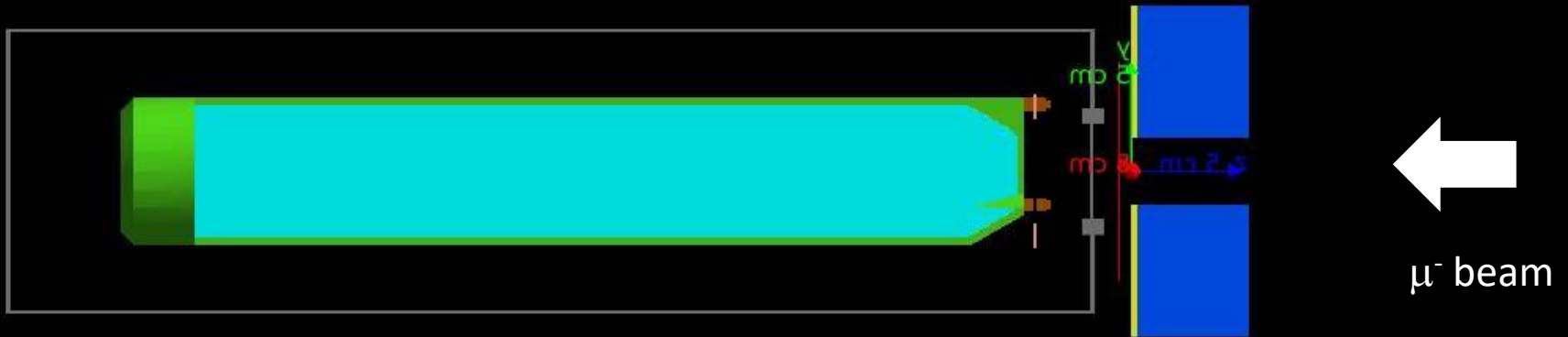


FAMU simulated geometry

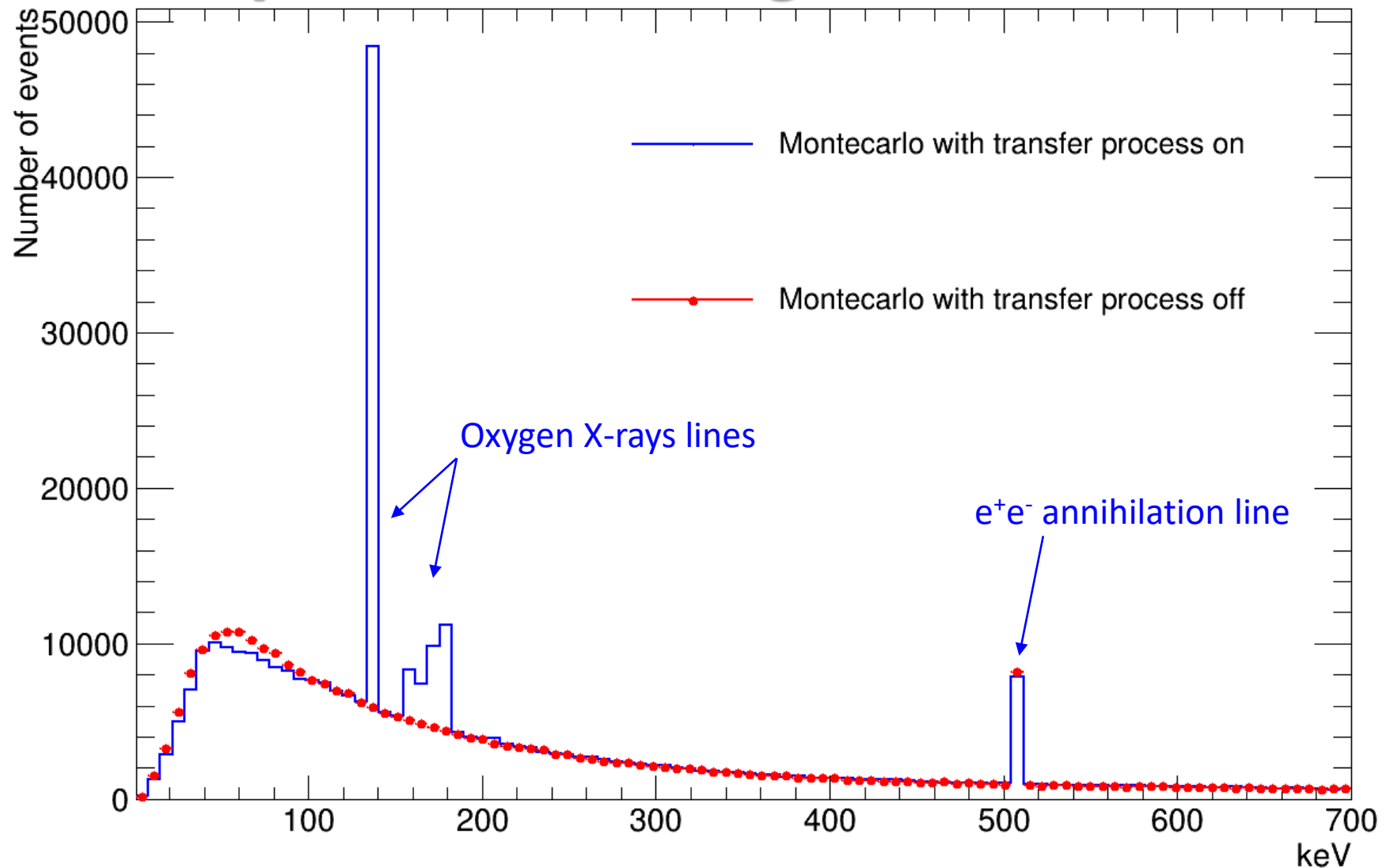
Pressurized vessel



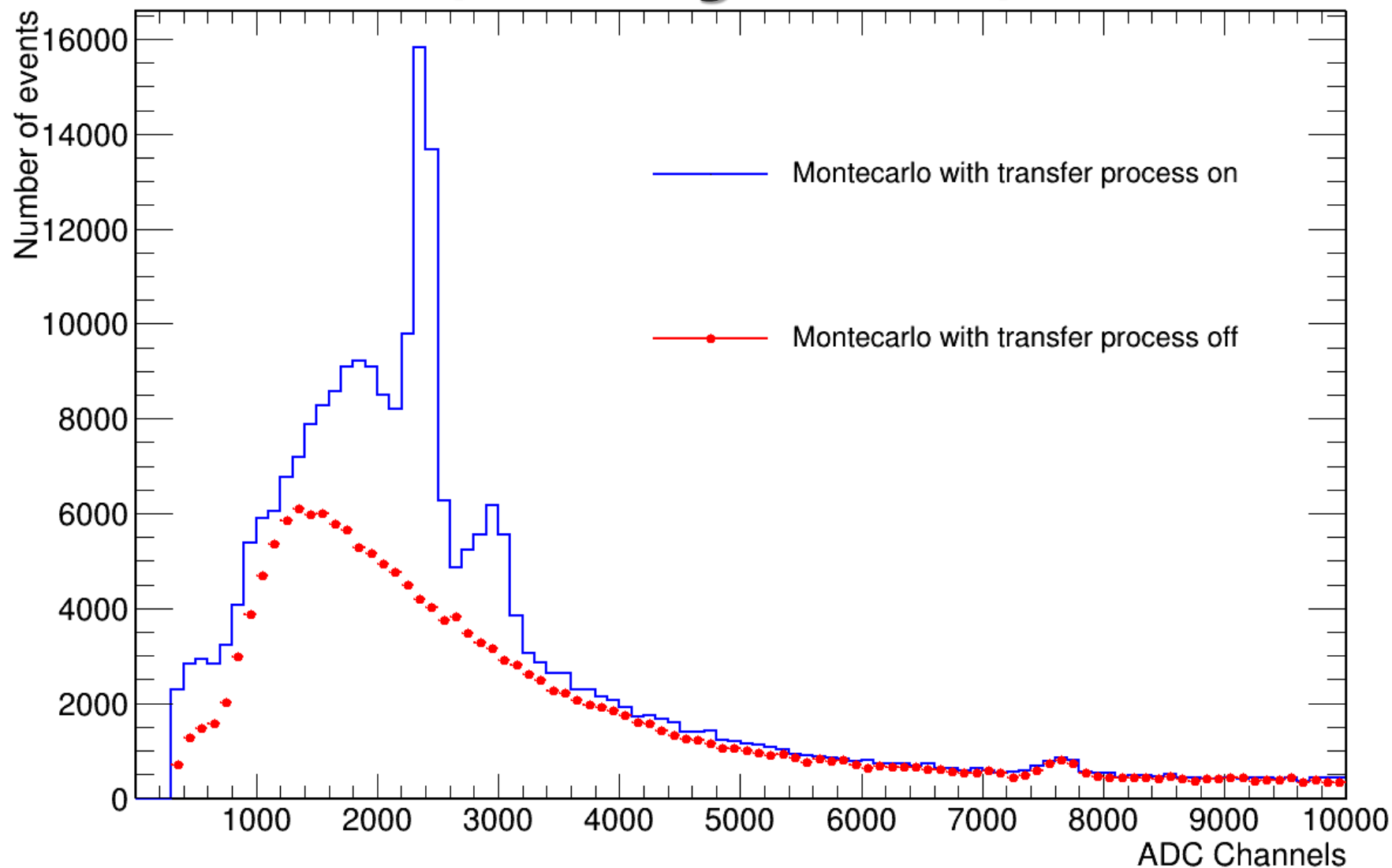
FAMU simulated geometry



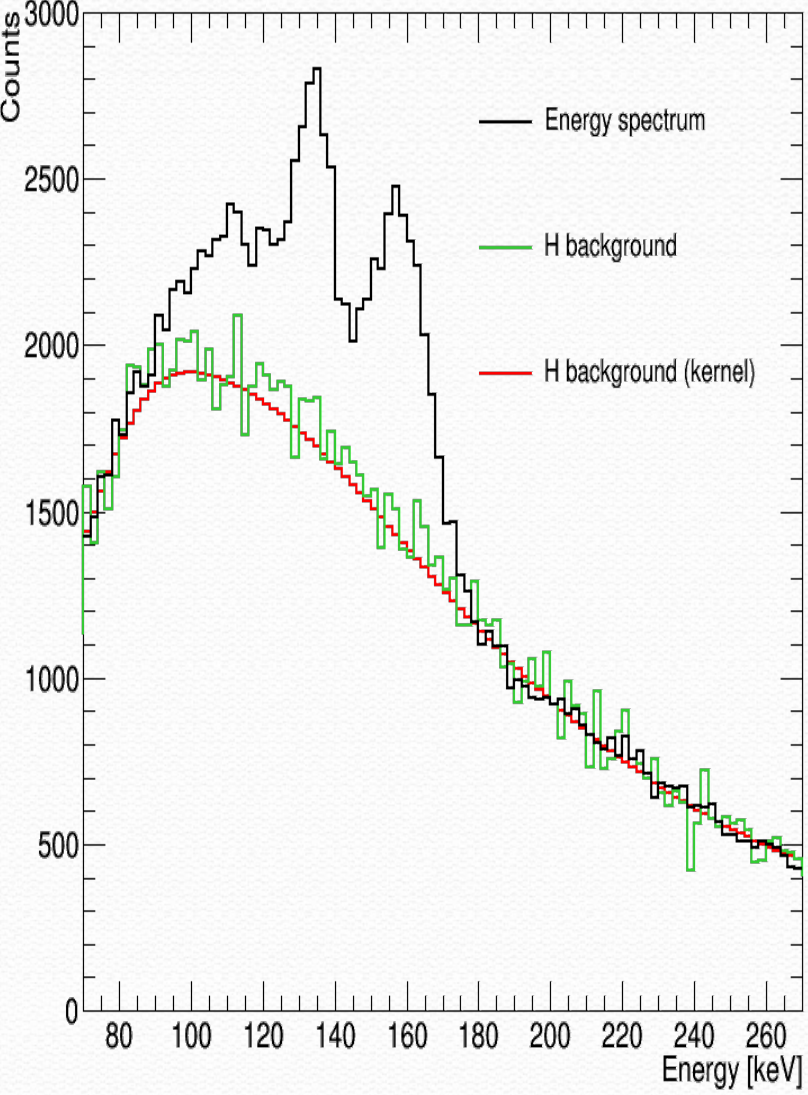
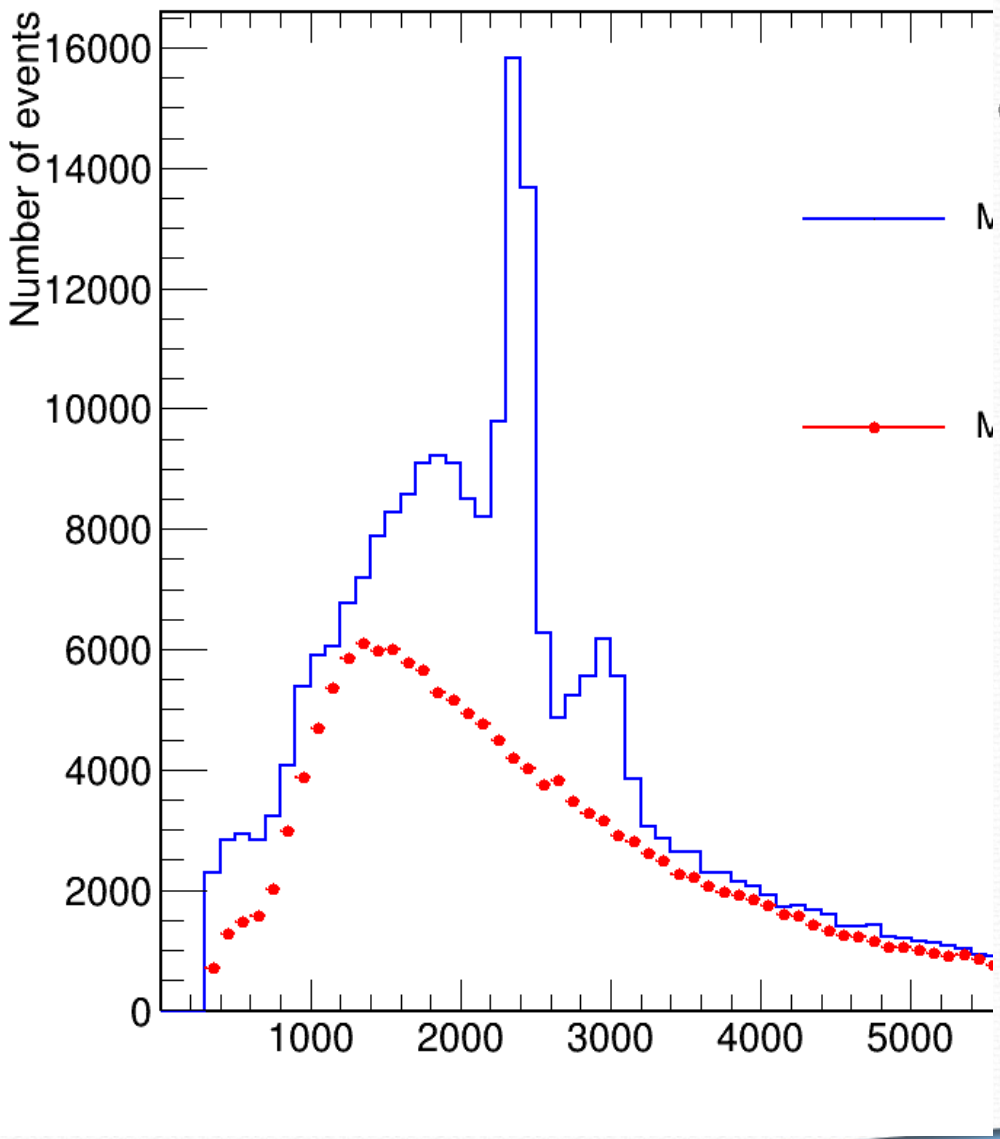
Simulation: energy at generation time of particles entering the detectors



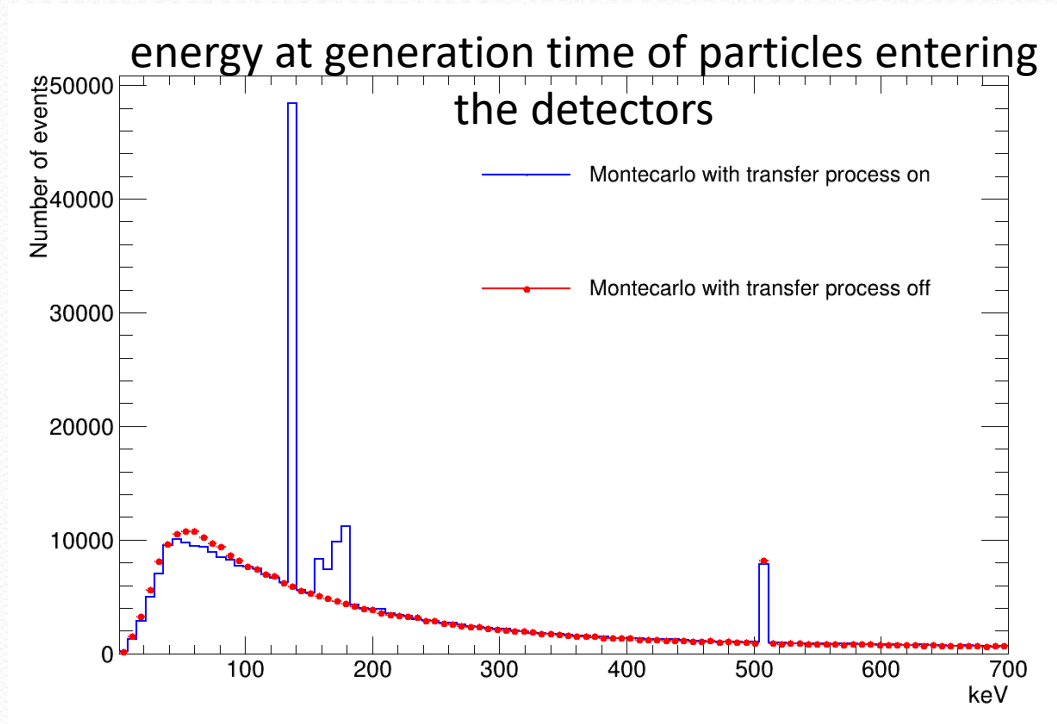
Simulation: energy measured by the detectors (after digitization)



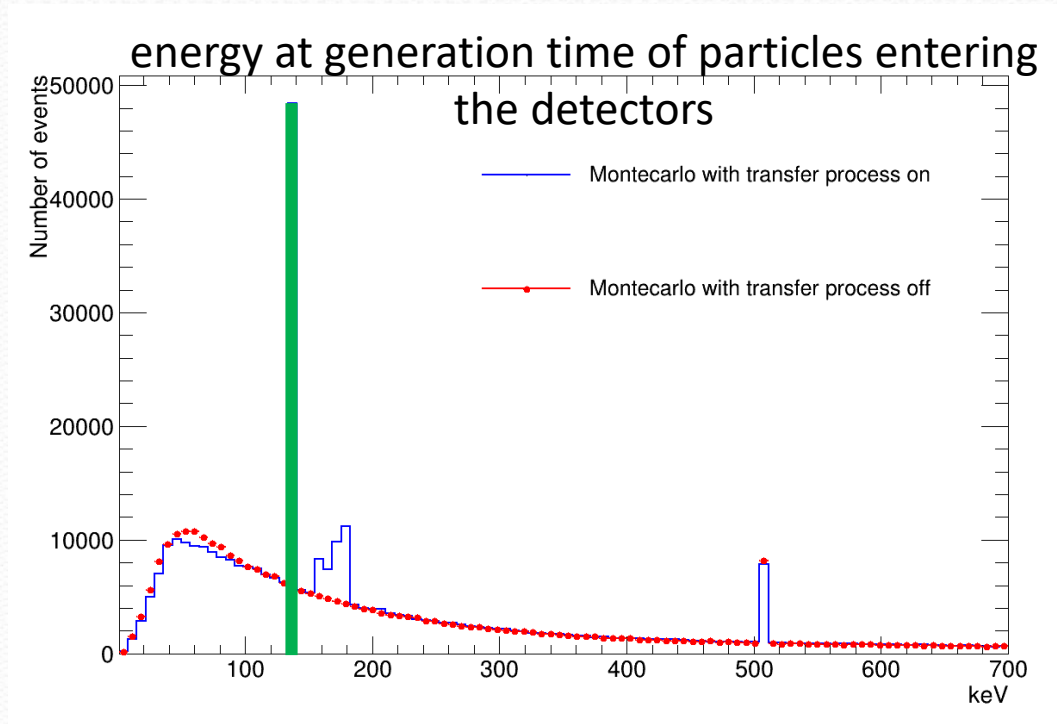
Simulation vs data: pretty similar!



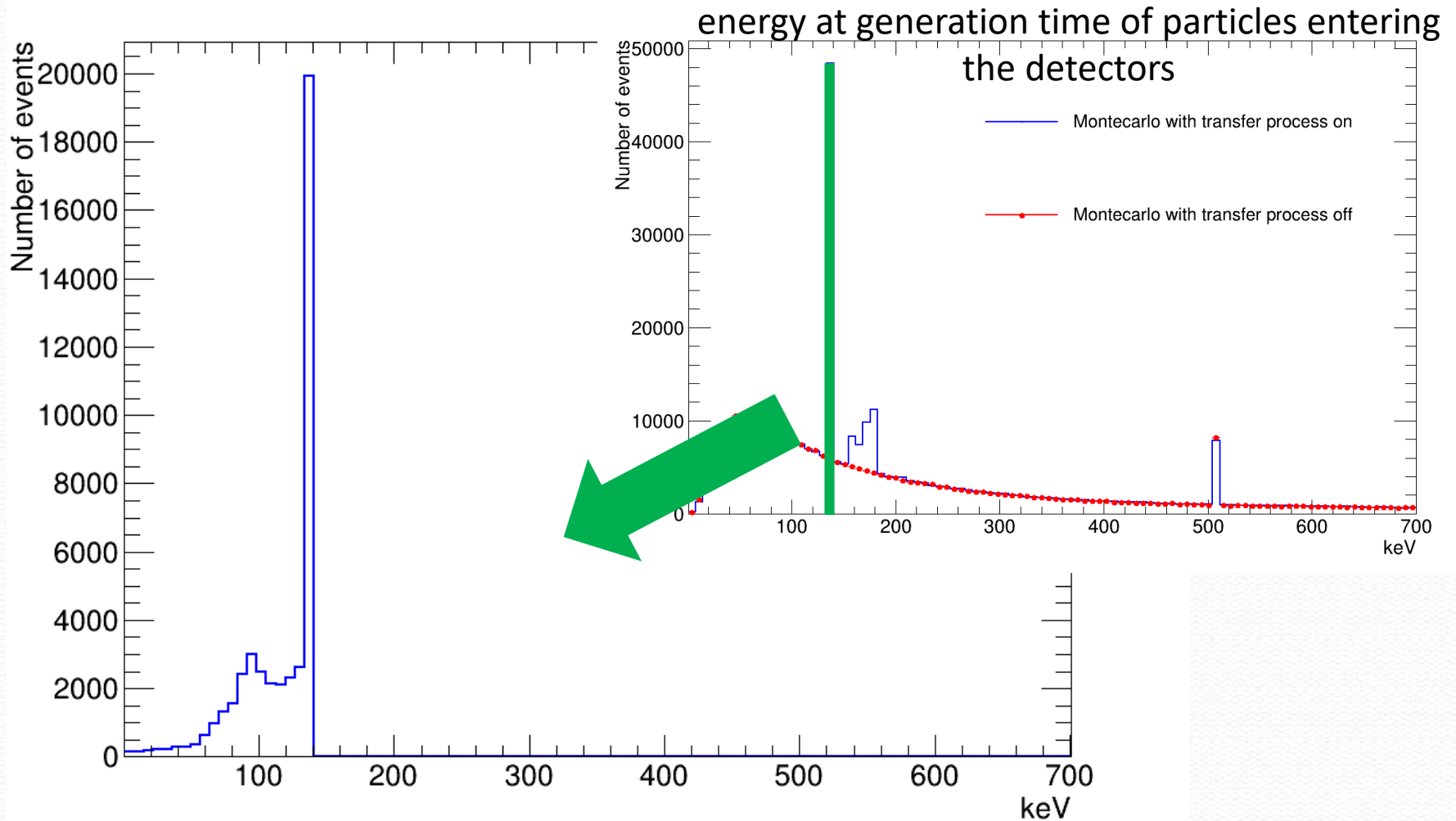
Simulation: energy released in the detector for 133 keV line



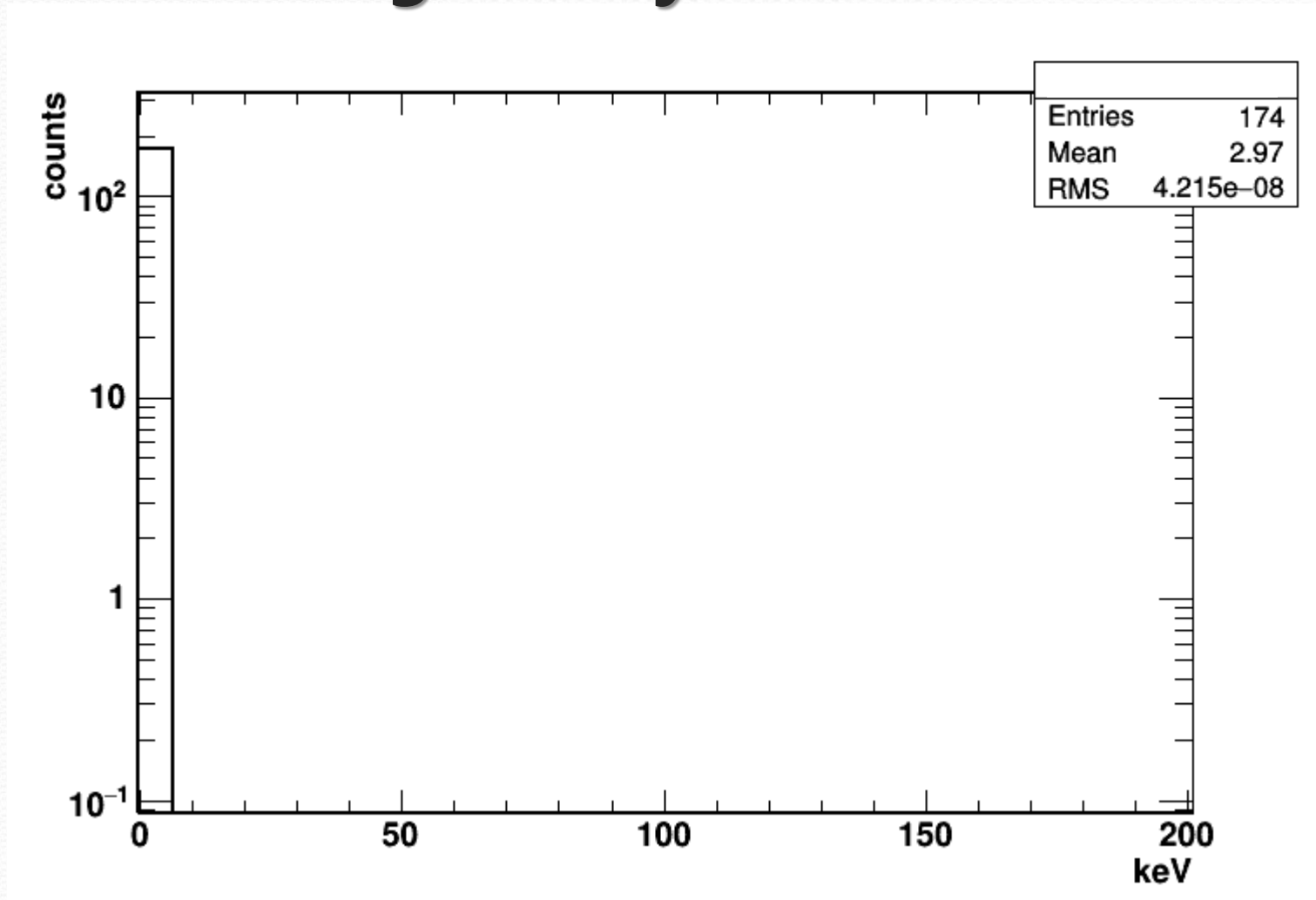
Simulation: energy released in the detector for 133 keV line



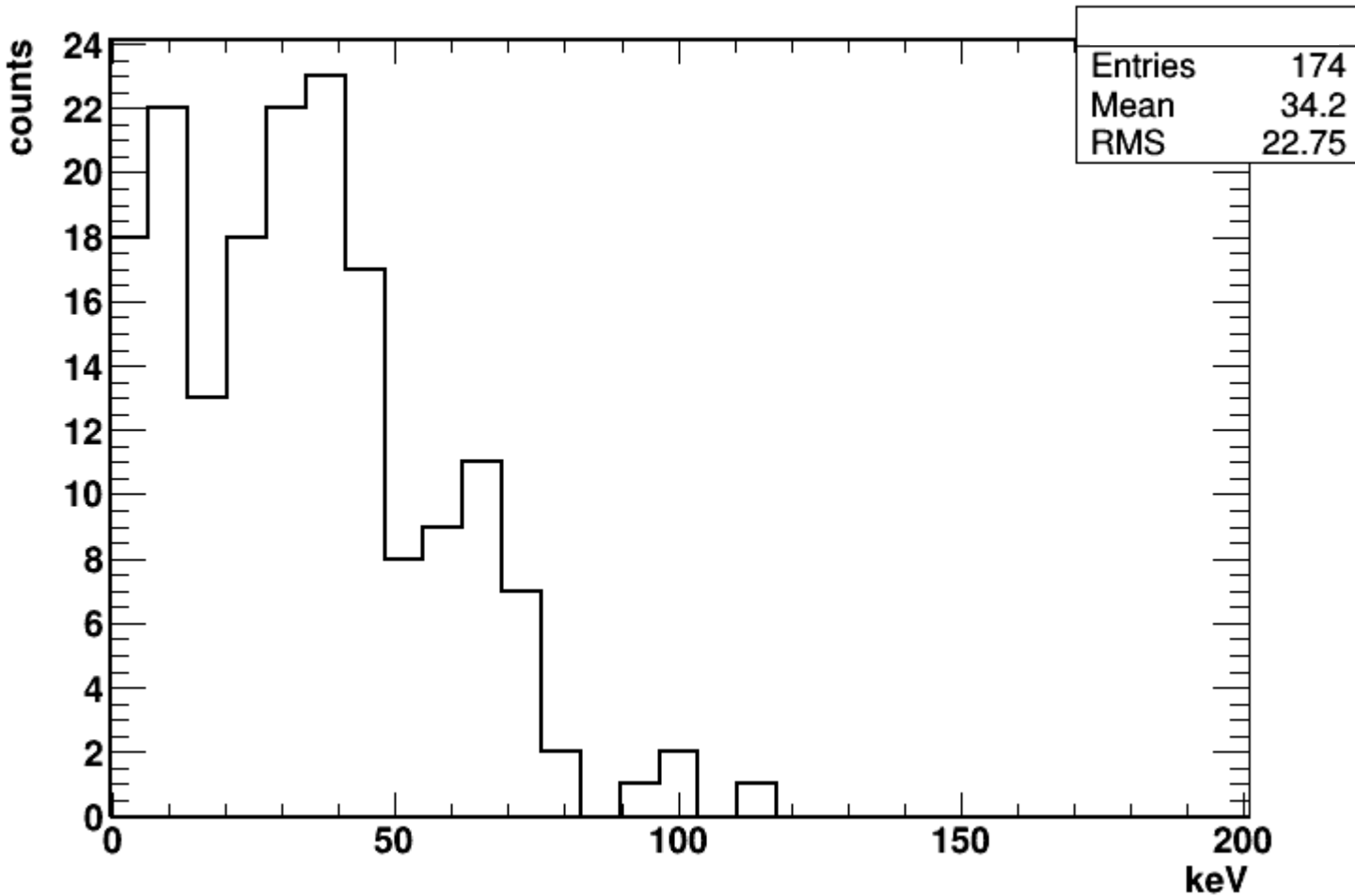
Simulation: energy released in the detector for 133 keV line



Simulation: energy loss by particles BEFORE entering the crystal

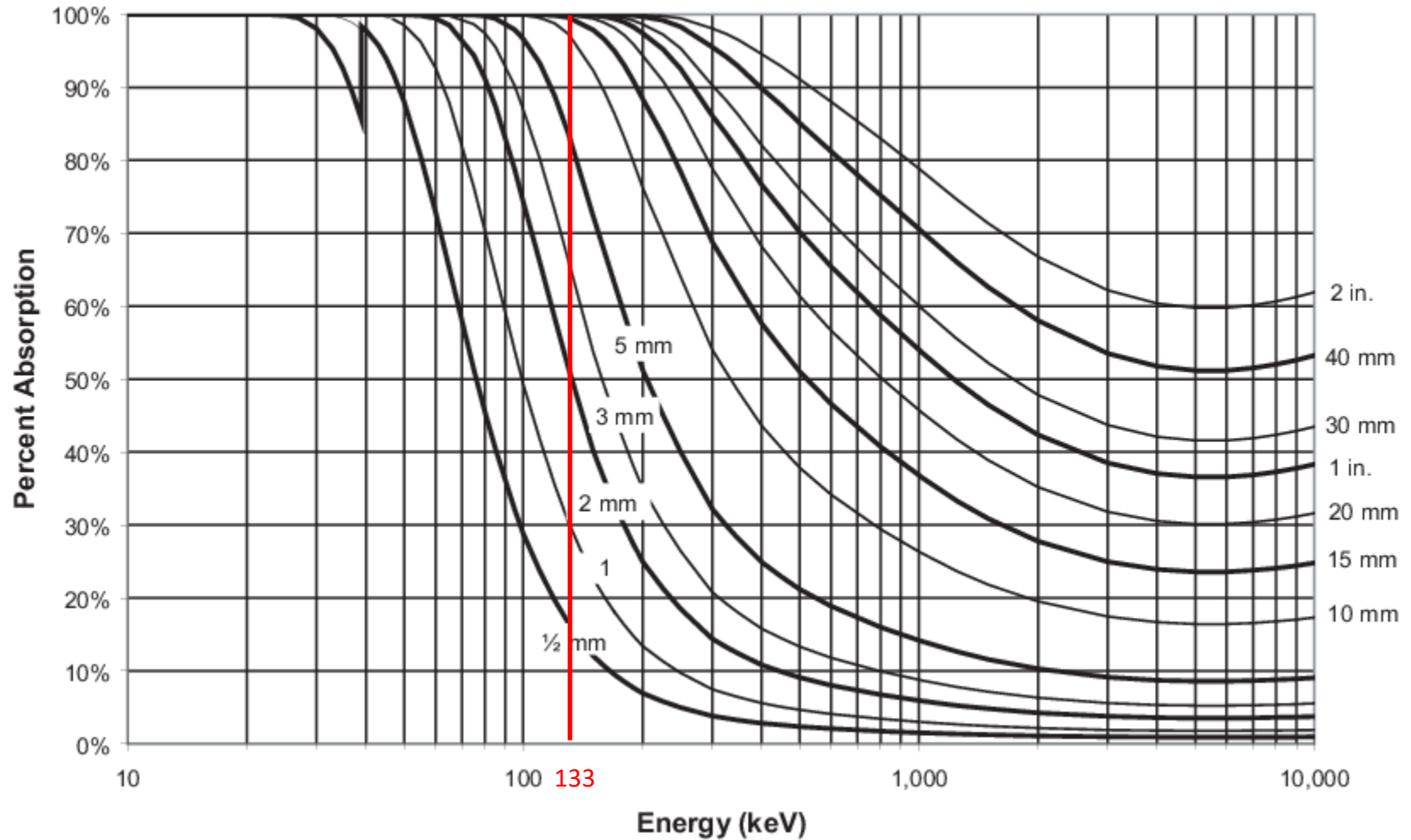


Simulation: energy deposit outside the crystal after the first interaction (leakage)



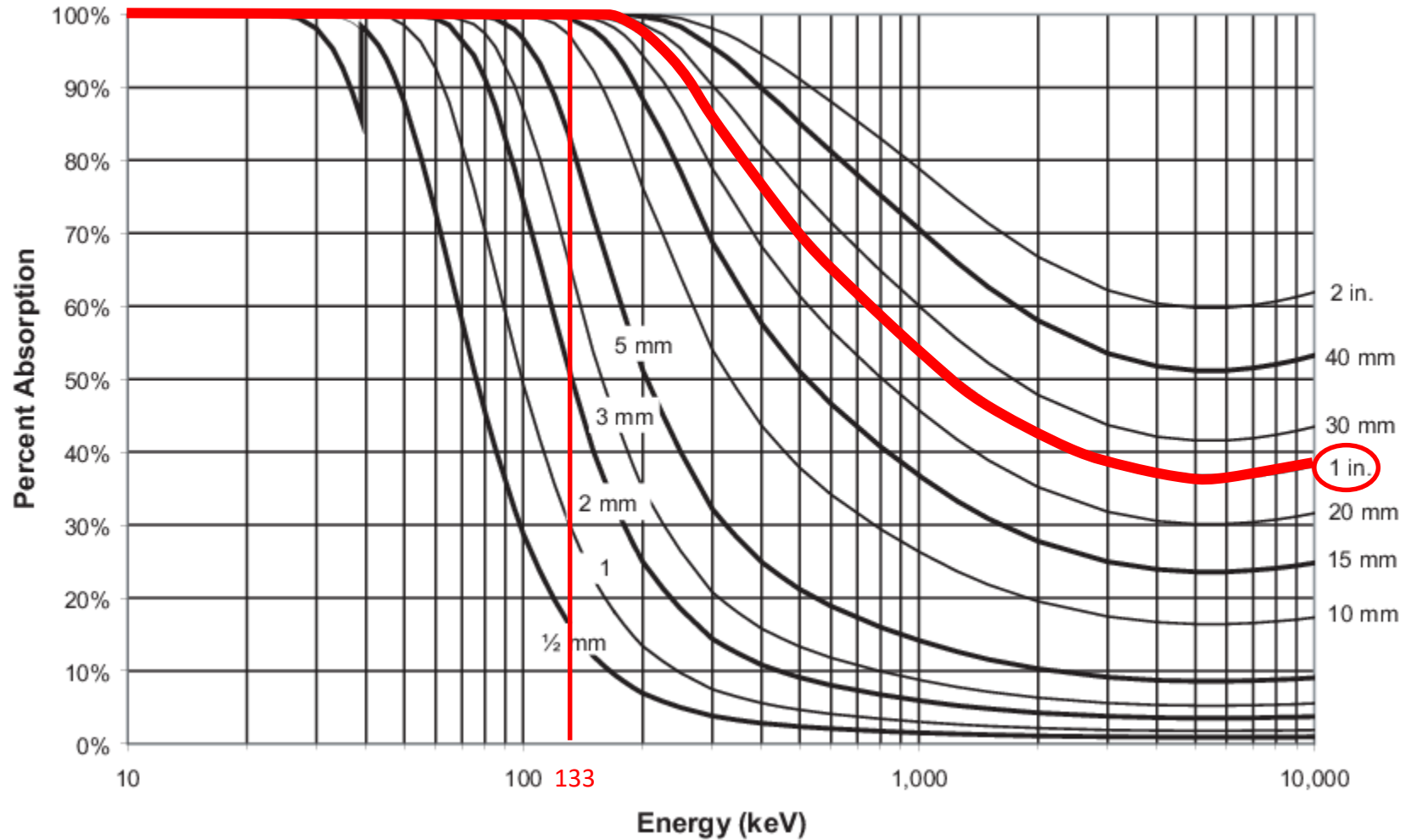
LaBr₃(Ce) absorption graph: 133 keV photon: 80% in 5 mm

[LaBr₃(Ce)]

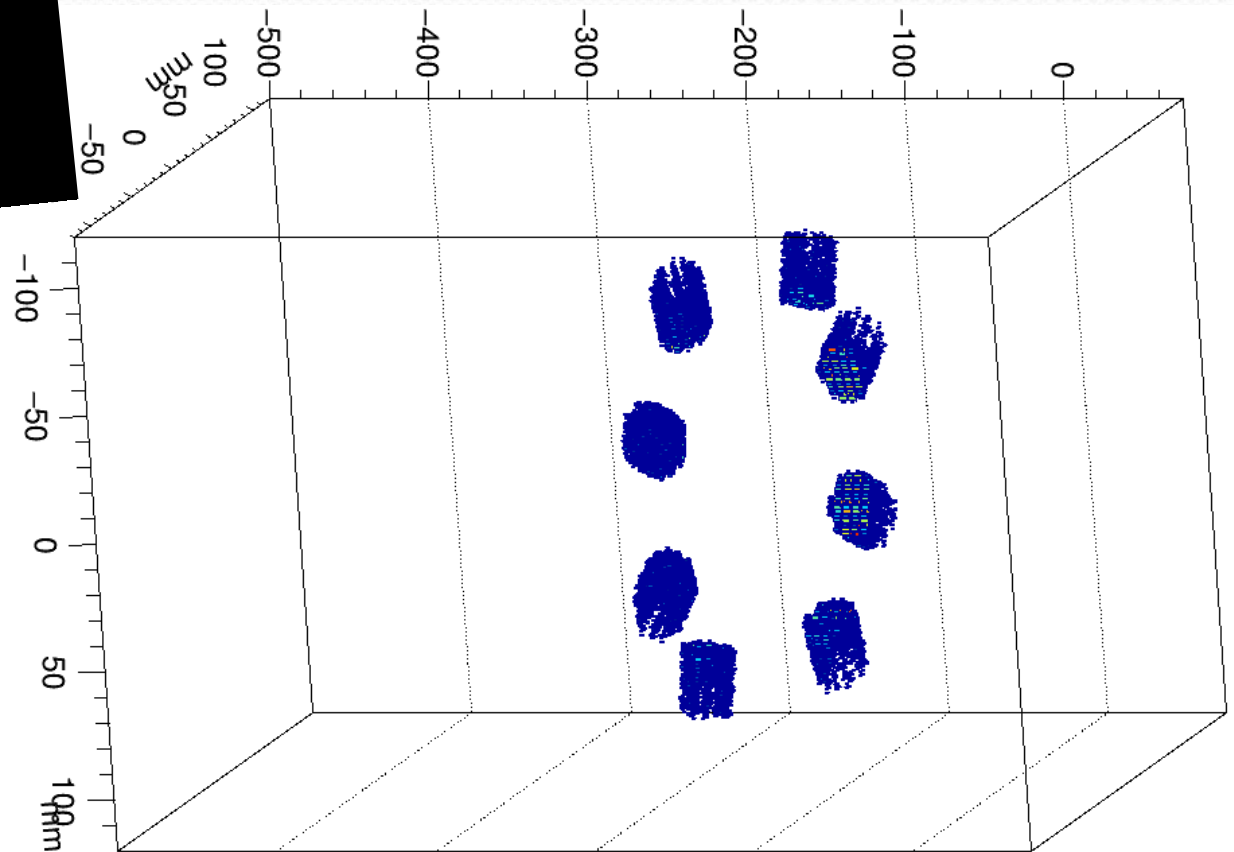
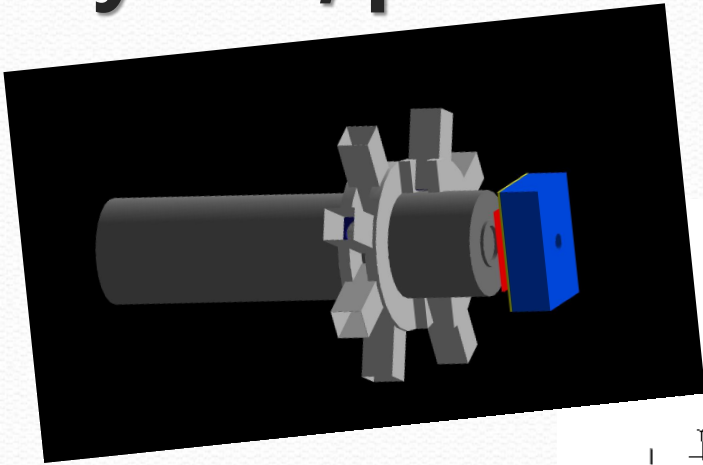


LaBr₃(Ce) absorption graph: 133 keV photon: 80% in 5 mm

[LaBr₃(Ce)]

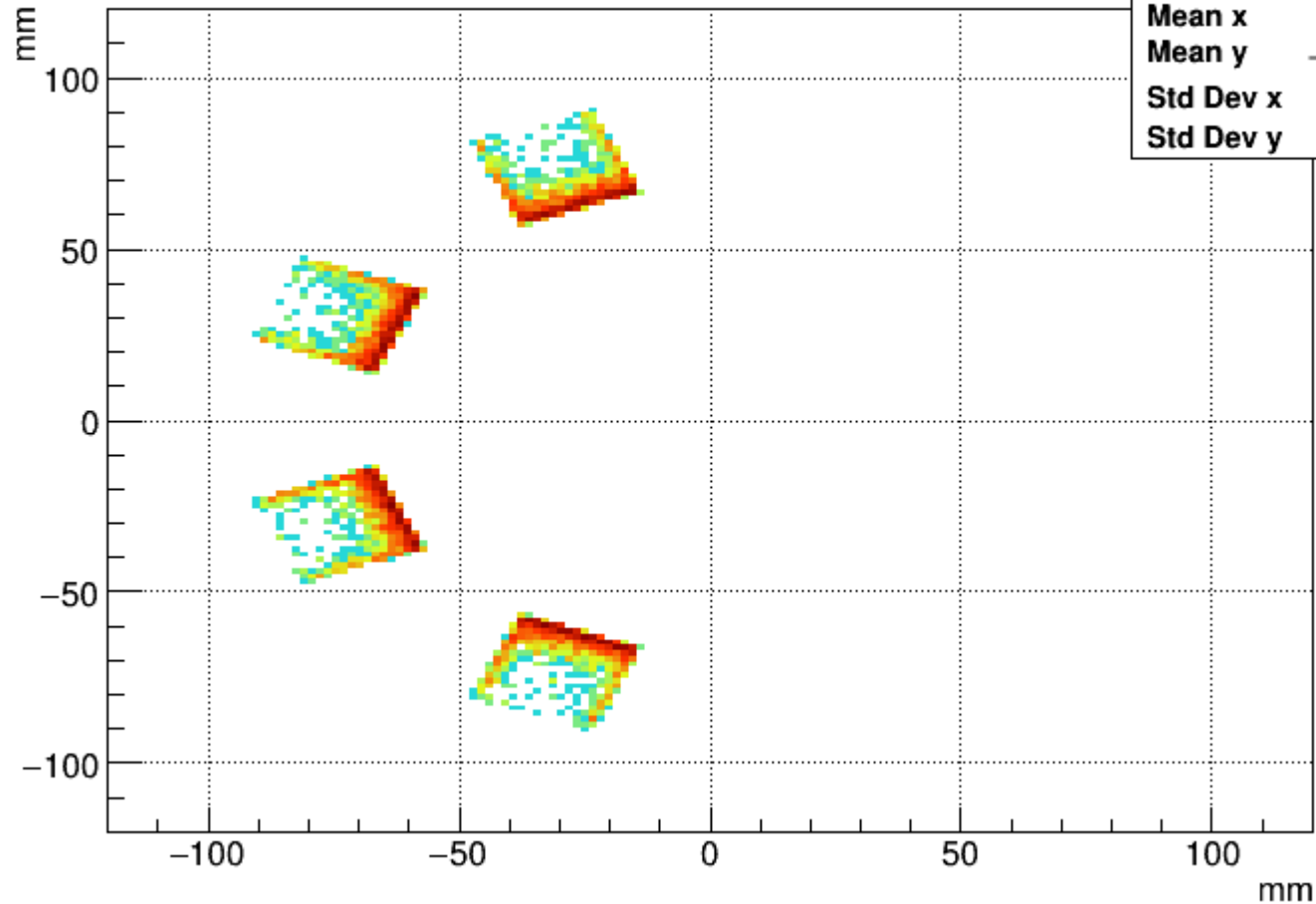


Simulation: impact point in the crystals, particles at any energy



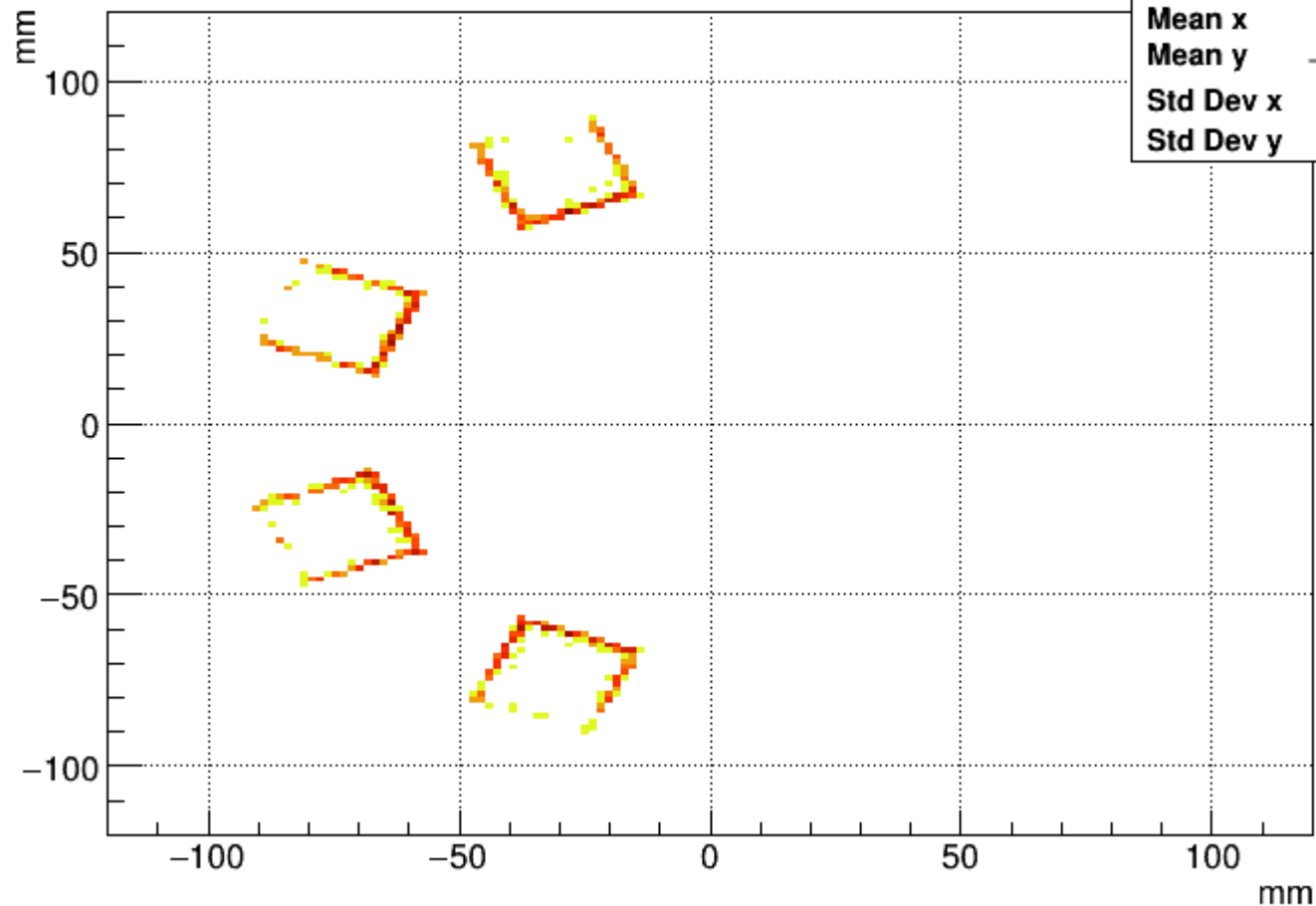
Simulation: impact point in the crystals, 133 keV energy deposit

ProjectionXY of binz=58 [z=-172.2..-166]



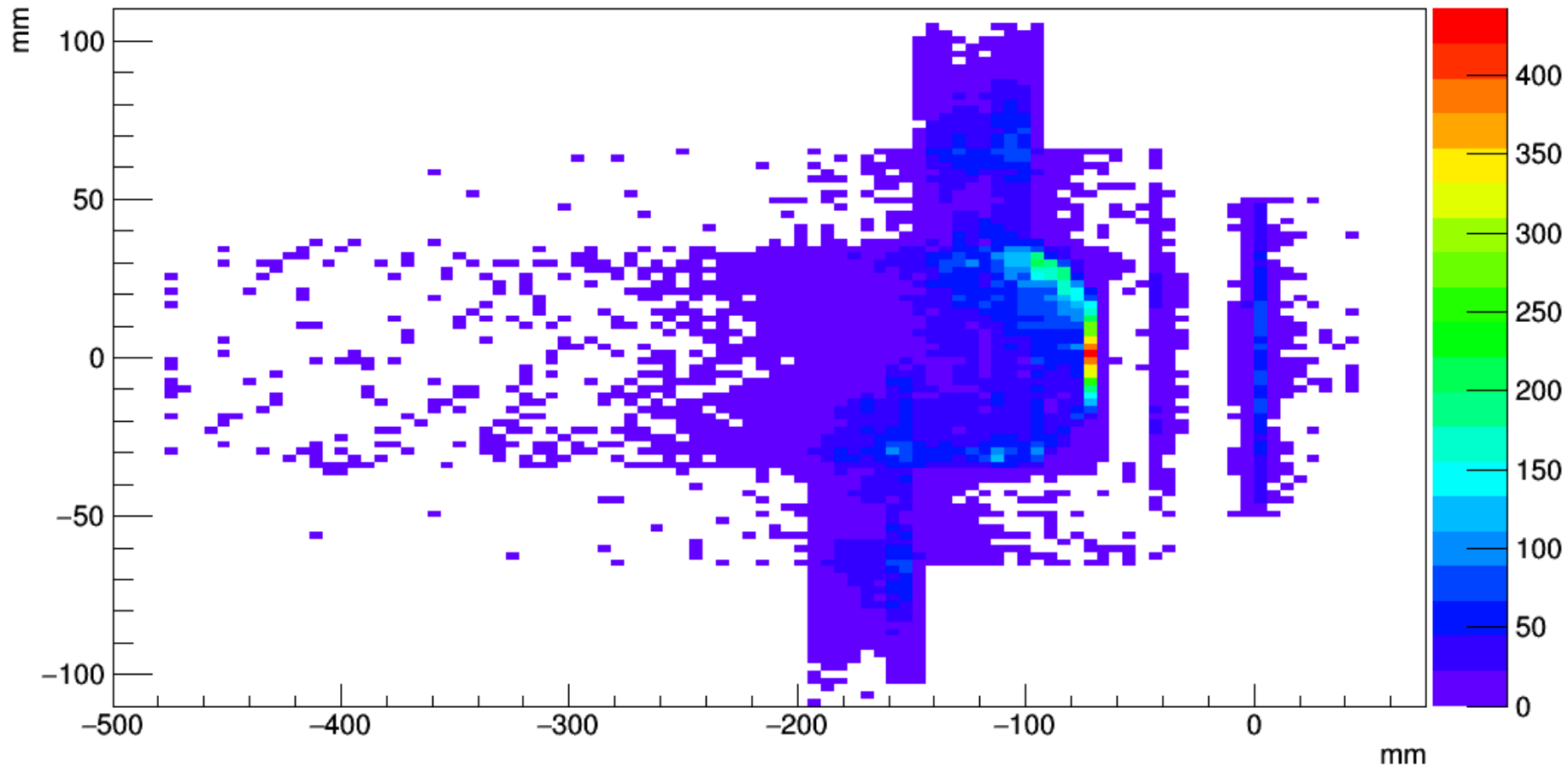
Simulation: impact point in the crystals, <133 keV energy deposit

ProjectionXY of binz=58 [z=-172.2..-166]

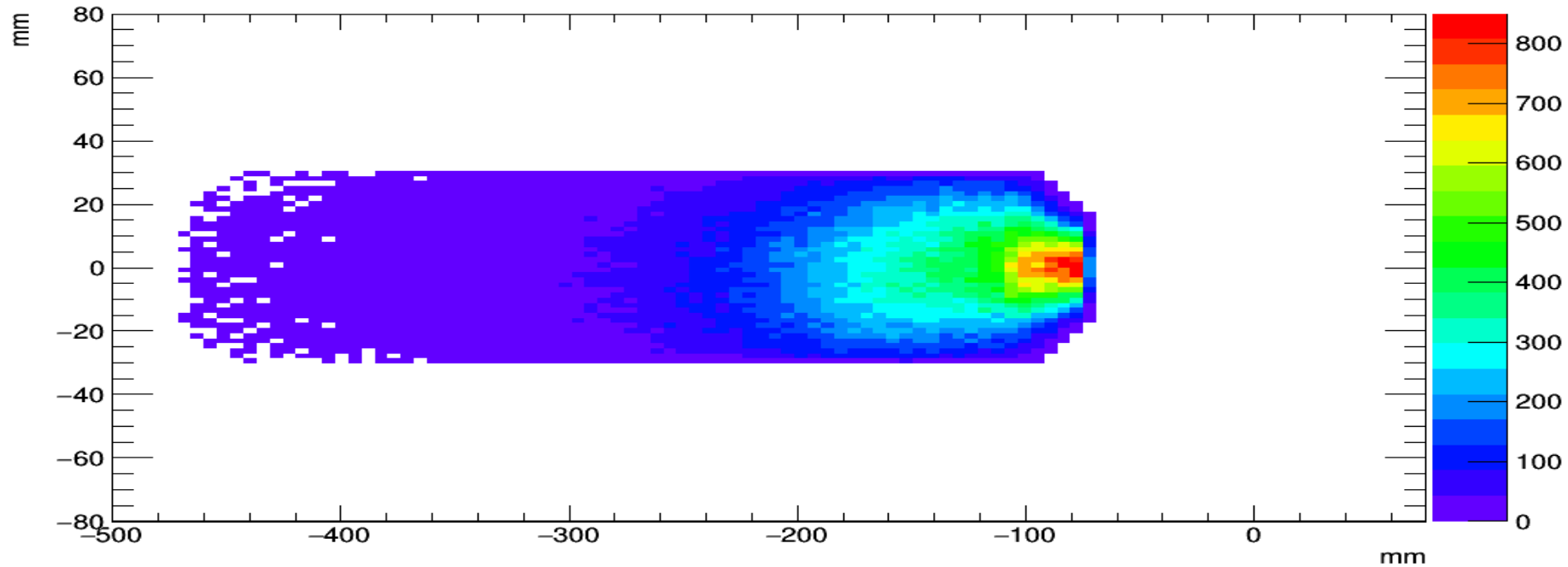


hYXZ_test133_xy	
Entries	956
Mean x	-48.34
Mean y	-0.5456
Std Dev x	21.21
Std Dev y	52.61

Simulation: origin of X-rays (not coming from gas)

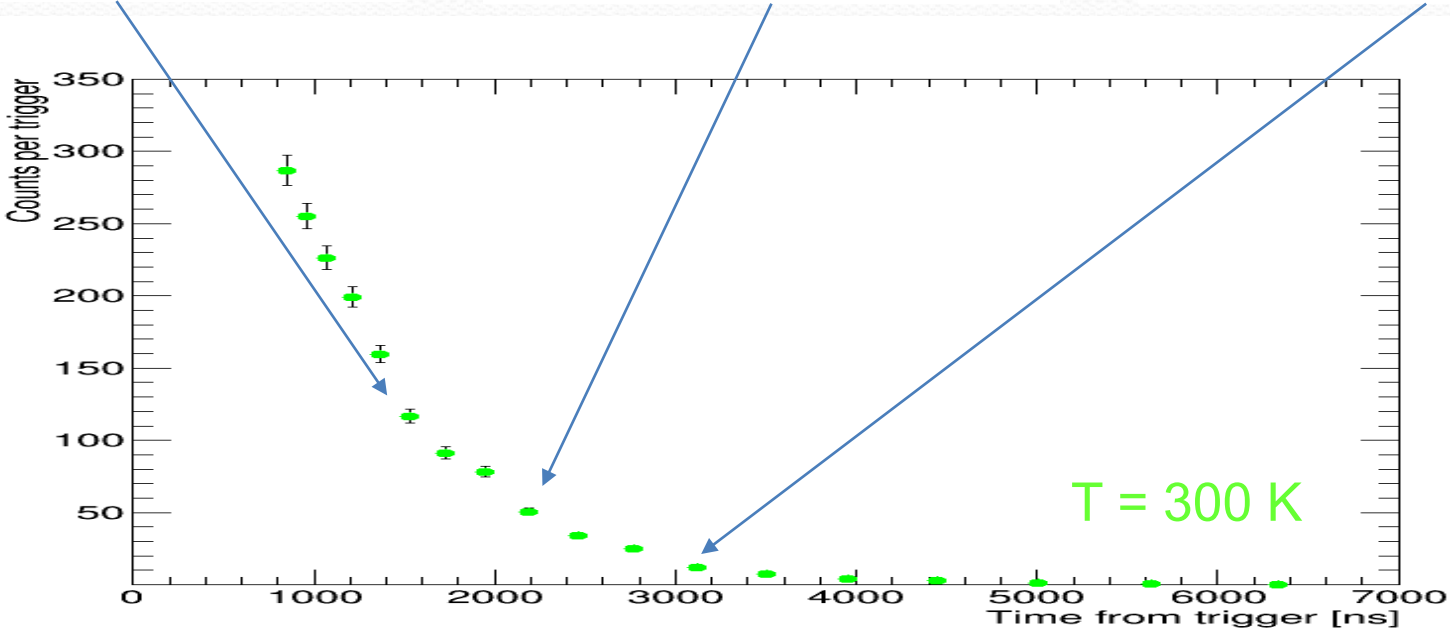
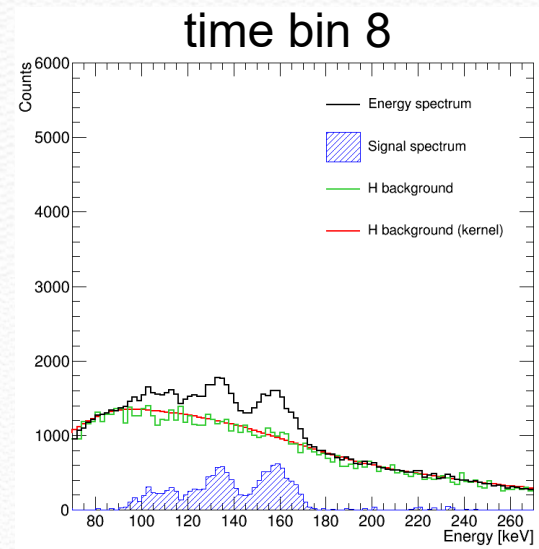
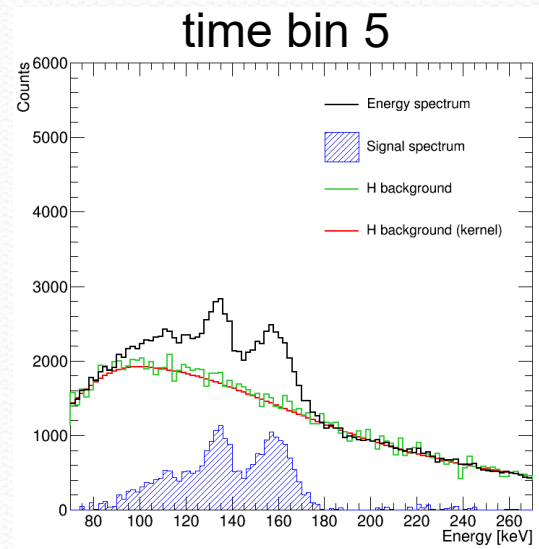
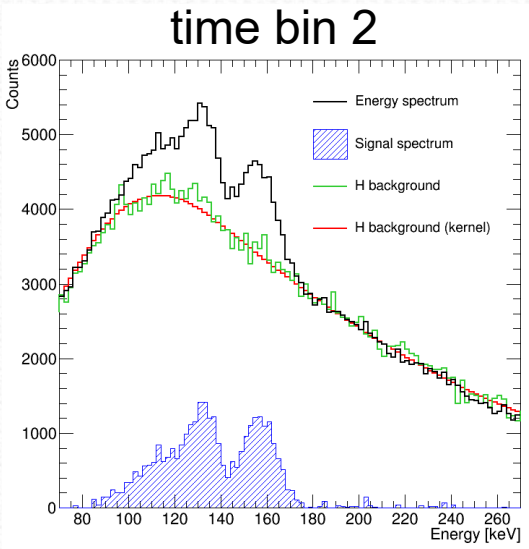


Simulation: origin of X-rays coming from gas

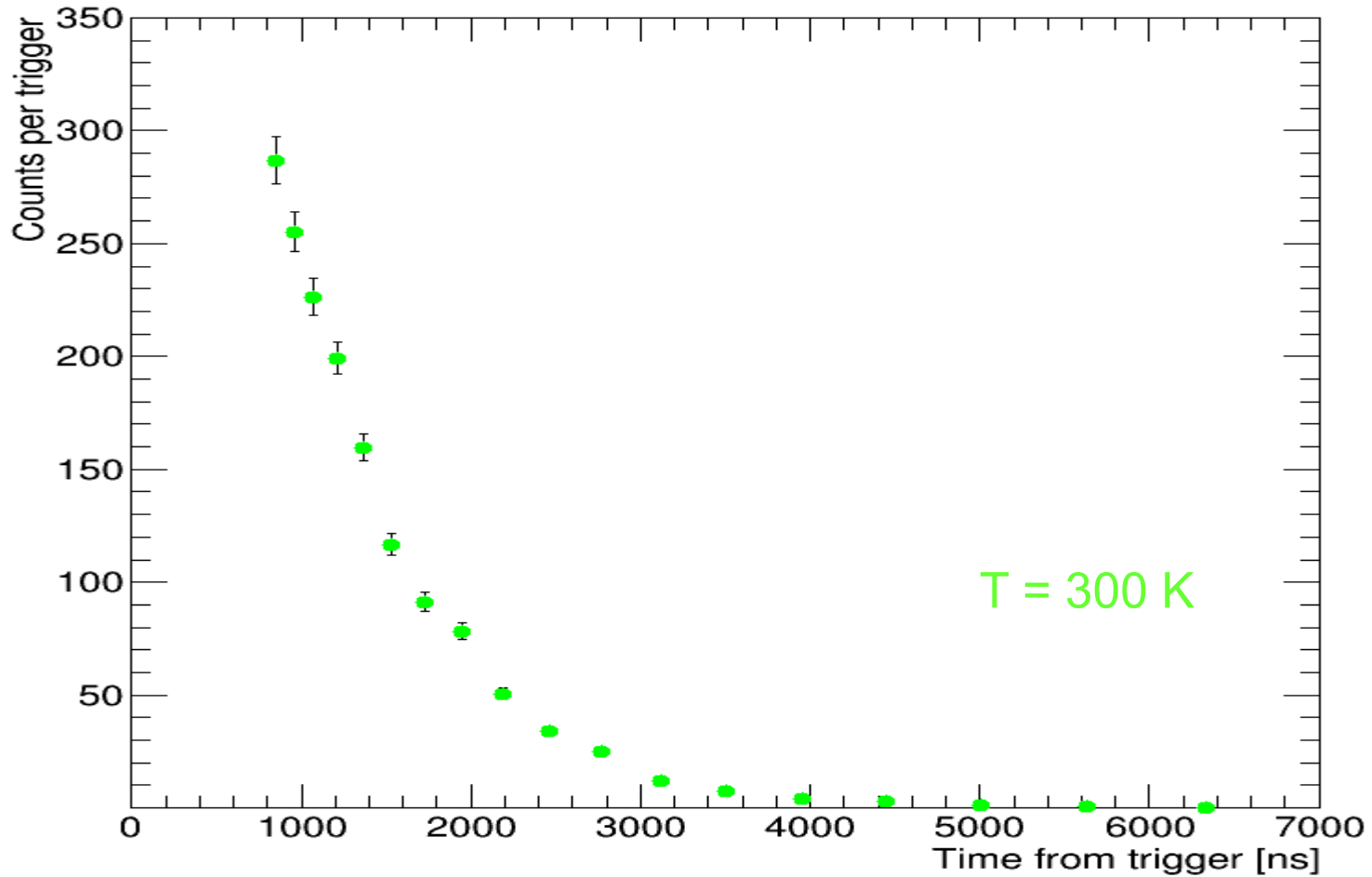


Transfer rate evaluation

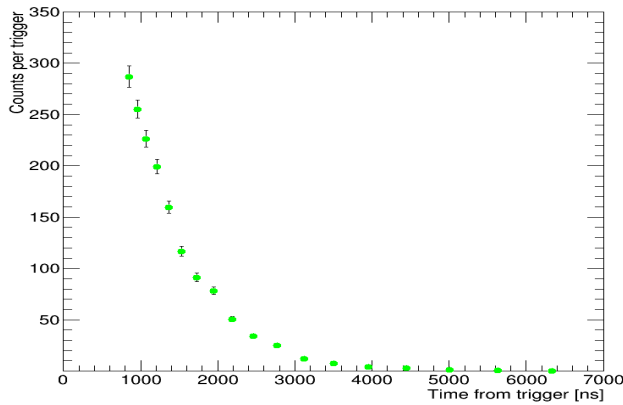
Fixed temperature: time evolution



Temperature and time evolution



Temperature and time evolution



$$dN_{\mu p}(t) = -N_{\mu p}(t) \lambda_{\text{dis}}(T) dt$$

Disappearance rate

$$\lambda_{\text{dis}}(T) = \lambda_0 + \phi [c_p \Lambda_{pp\mu} + c_d \Lambda_{pd}(T) + c_o \Lambda_{pO}(T)]$$

Rate of disappearance of muons bounded to p (decay, ..)

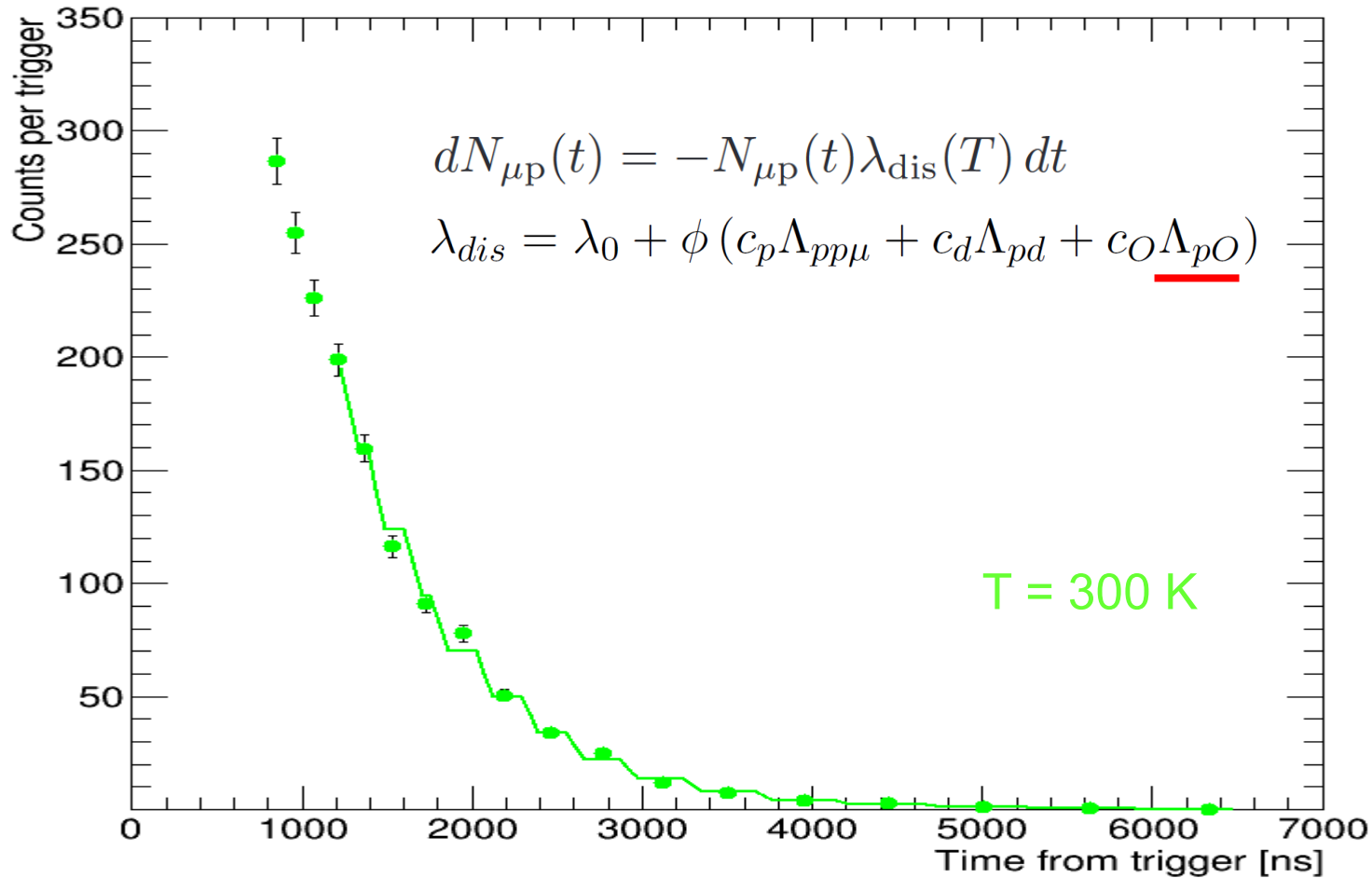
ϕ number density of atoms in the gas target

$\Lambda_{pp\mu}, \Lambda_{\dots}$, transfer rates

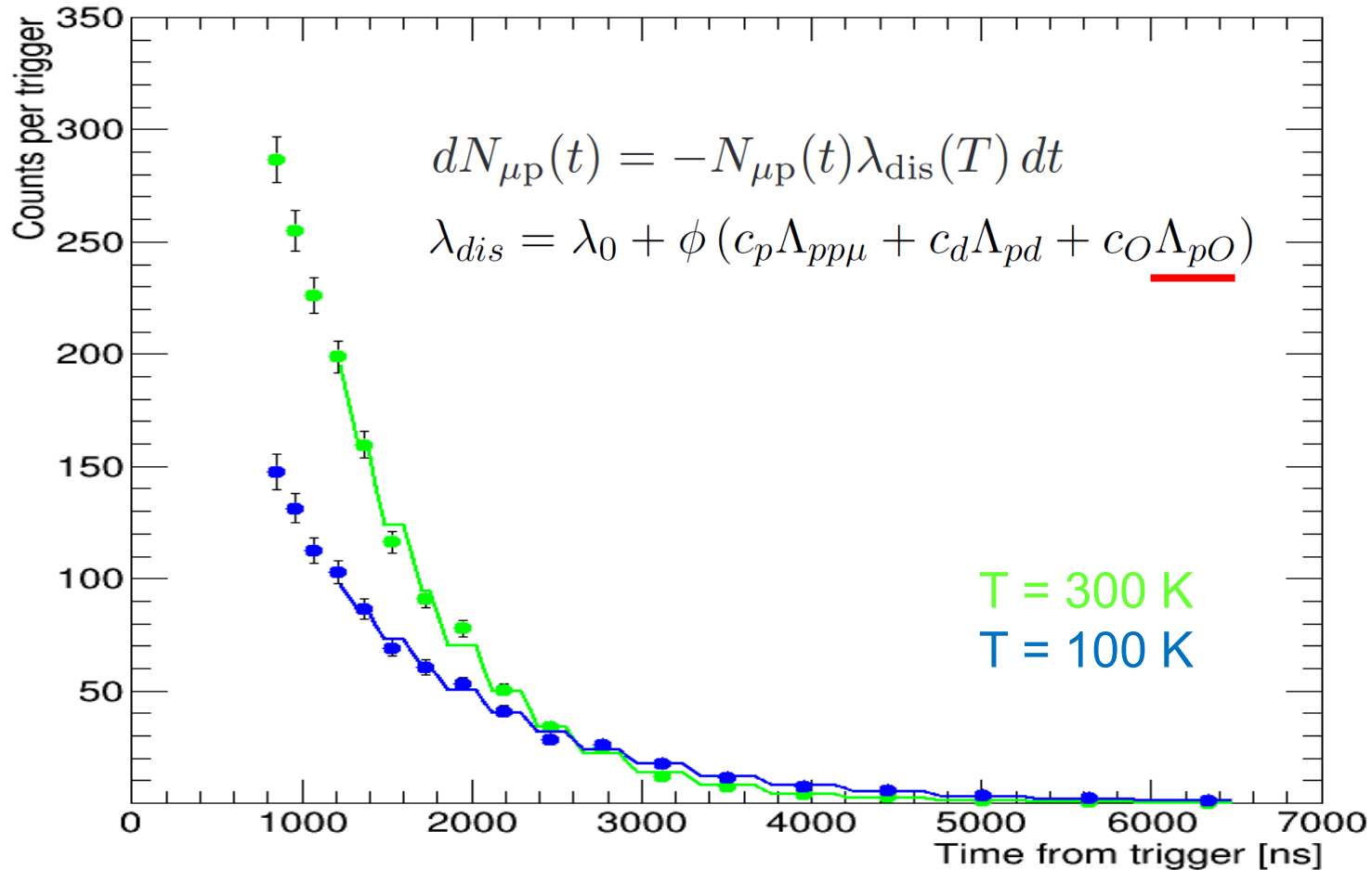
c_p, c_{\dots} concentrations of hydrogen, deuterium, oxygen

UNKNOWN TERM

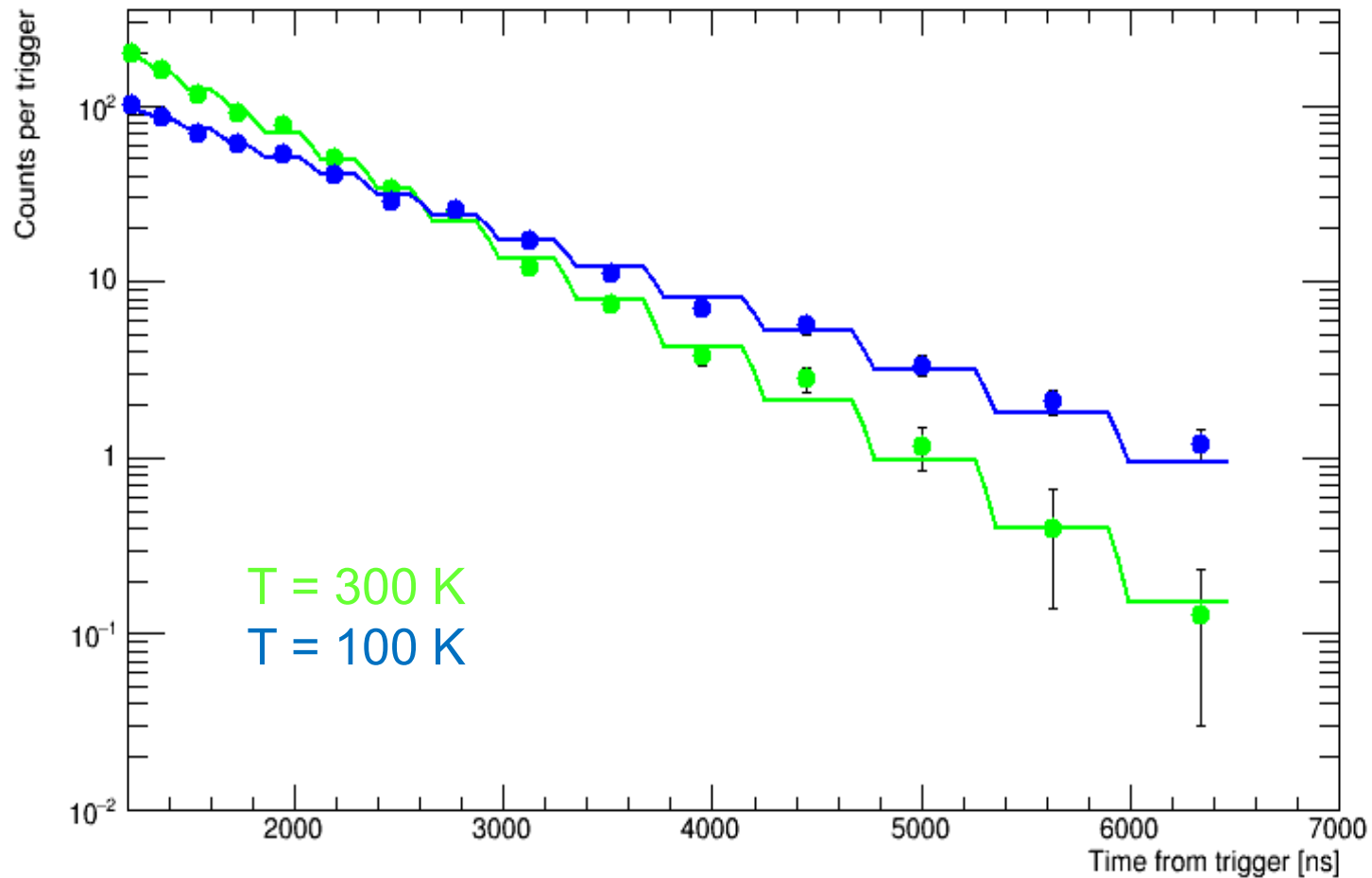
Temperature and time evolution



Temperature and time evolution

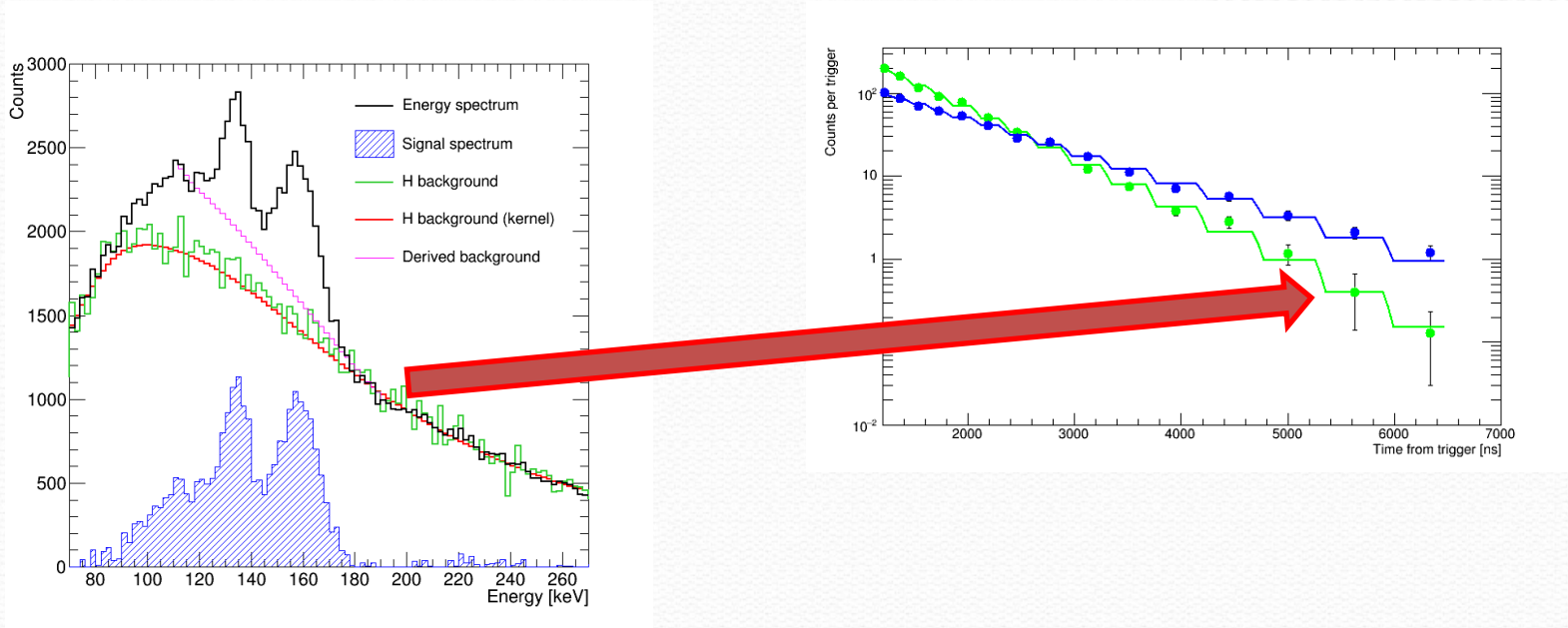


Temperature and time evolution



Systematics

1. Background estimation and normalization



Effect: fluctuations (5÷20%) of points used in the fit

➡ fluctuations of the transfer rate results

This uncertainty was quadratically summed to statistical errors

Systematics

1. Background estimation and normalization
2. Uncertainty on the density (ϕ) \blacktriangleright $\sim 3\%$ effect on transfer rate (solid shift of points)

$$dN_{\mu p}(t) = S(t)dt - N_{\mu p}(t)\lambda_{dis}dt$$

$$\lambda_{dis} = \lambda_0 + \phi (c_p \Lambda_{pp\mu} + c_d \Lambda_{pd} + c_O \Lambda_{pO})$$

Systematics

1. Background estimation and normalization
2. Uncertainty on the density (ϕ) \blacktriangleright $\sim 3\%$ effect on transfer rate (solid shift of points)
3. Uncertainty on oxygen concentration (c_O) \blacktriangleright $\sim 3\%$ effect on transfer rate (solid shift of points)

$$dN_{\mu p}(t) = S(t)dt - N_{\mu p}(t)\lambda_{dis}dt$$

$$\lambda_{dis} = \lambda_0 + \phi (c_p\Lambda_{pp\mu} + c_d\Lambda_{pd} + \underline{c_O}\Lambda_{pO})$$

Systematics

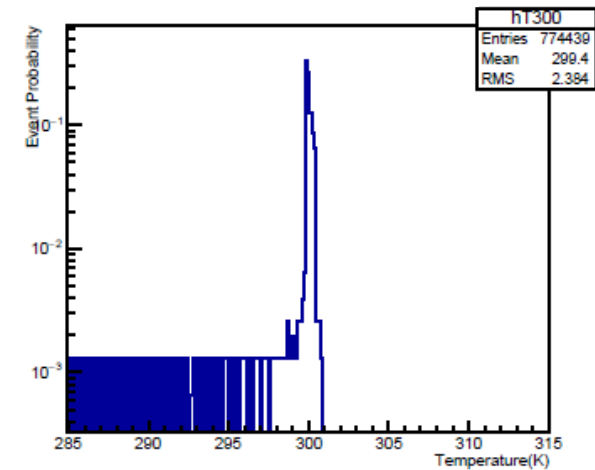
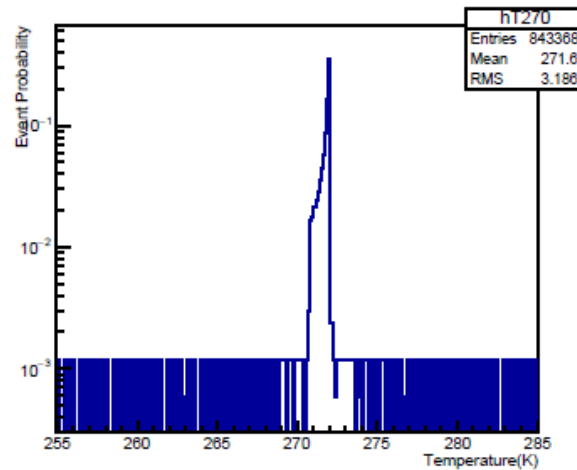
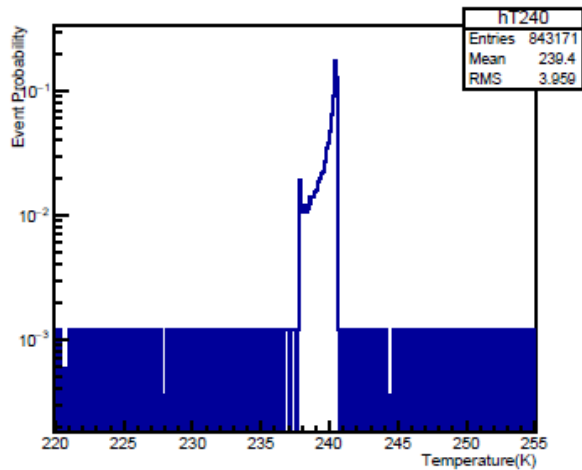
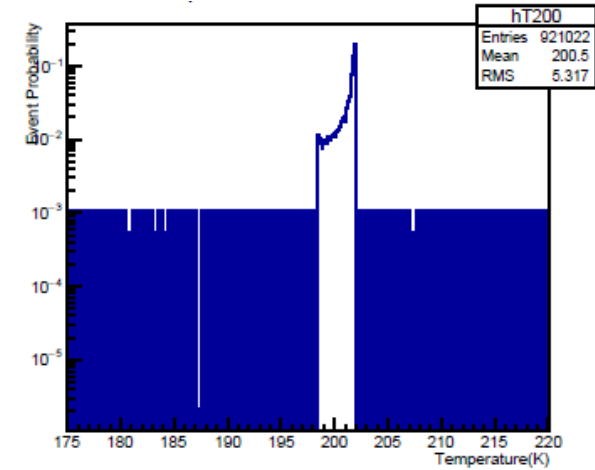
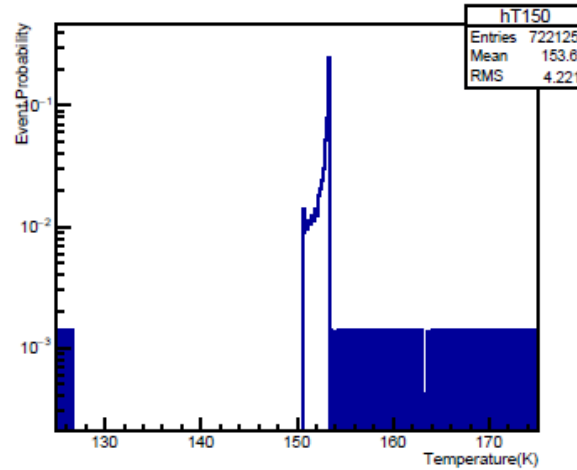
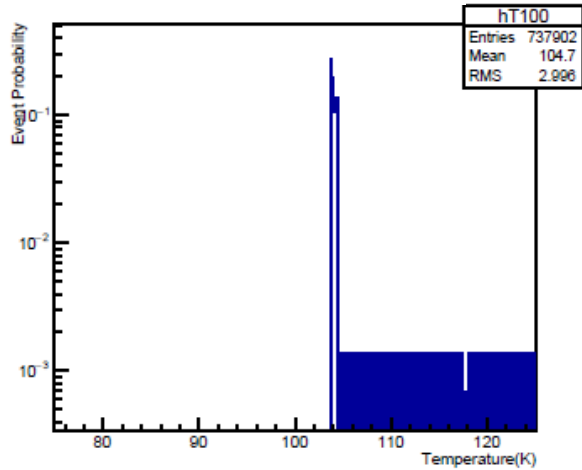
1. Background estimation and normalization
2. Uncertainty on the density (ϕ) \blacktriangleright $\sim 3\%$ effect on transfer rate (solid shift of points)
3. Uncertainty on oxygen concentration (c_O) \blacktriangleright $\sim 3\%$ effect on transfer rate (solid shift of points)
4. Other uncertainties, negligible (\ll statistical error)

$$dN_{\mu p}(t) = S(t)dt - N_{\mu p}(t)\lambda_{dis}dt$$

$$\lambda_{dis} = \lambda_0 + \phi (\underbrace{c_p \Lambda_{pp\mu}} + \underbrace{c_d \Lambda_{pd}} + \underbrace{c_O \Lambda_{pO}})$$

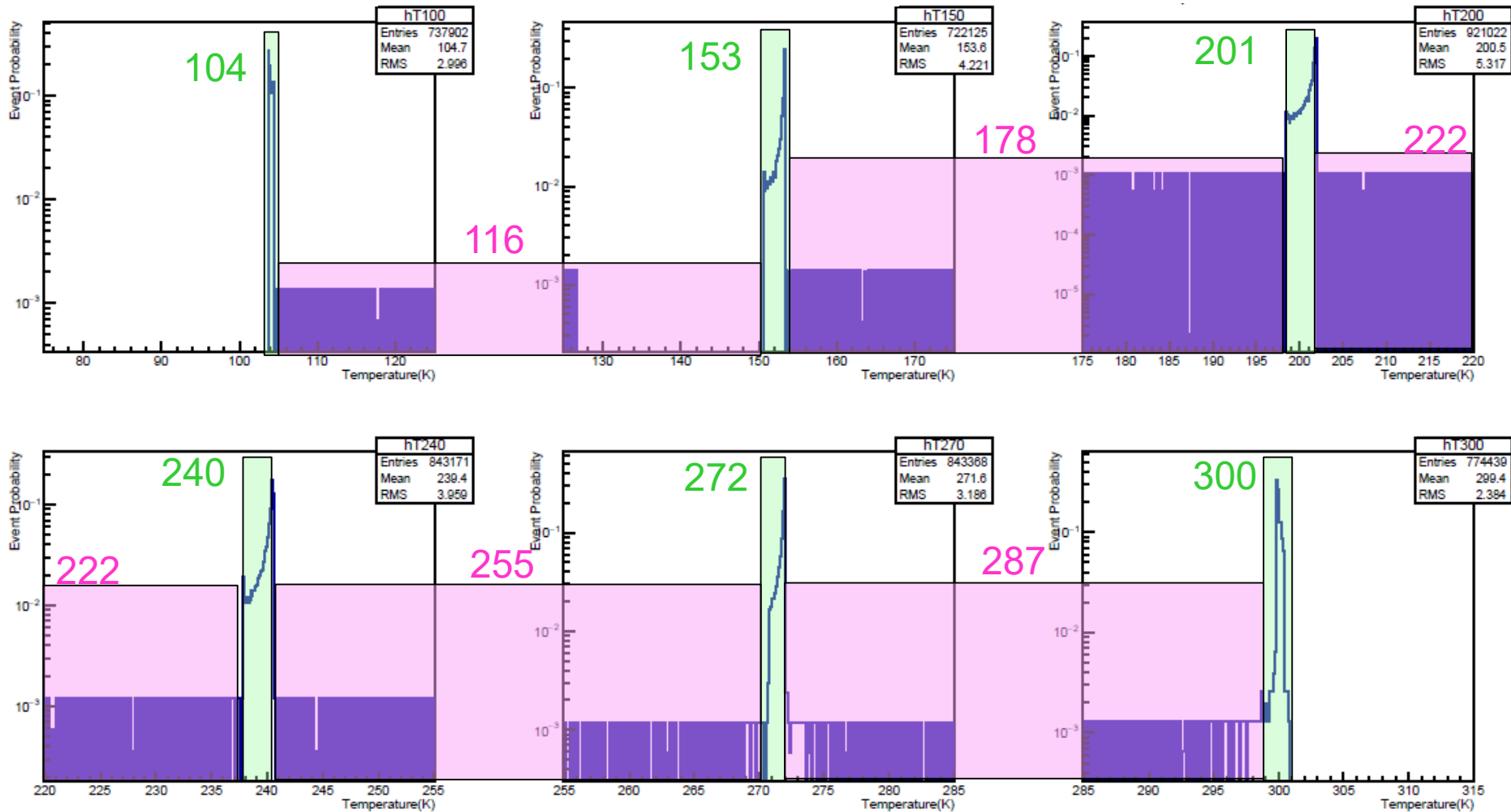
Temperature bins

6 fixed steps + 5 intermediate temperatures

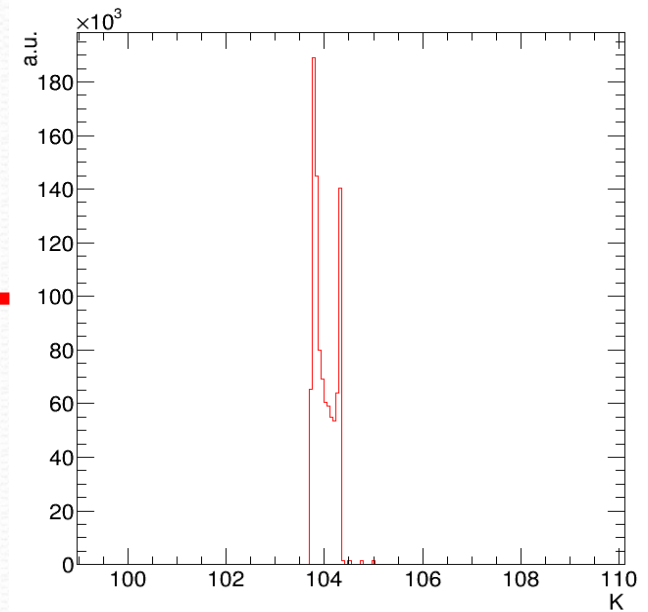
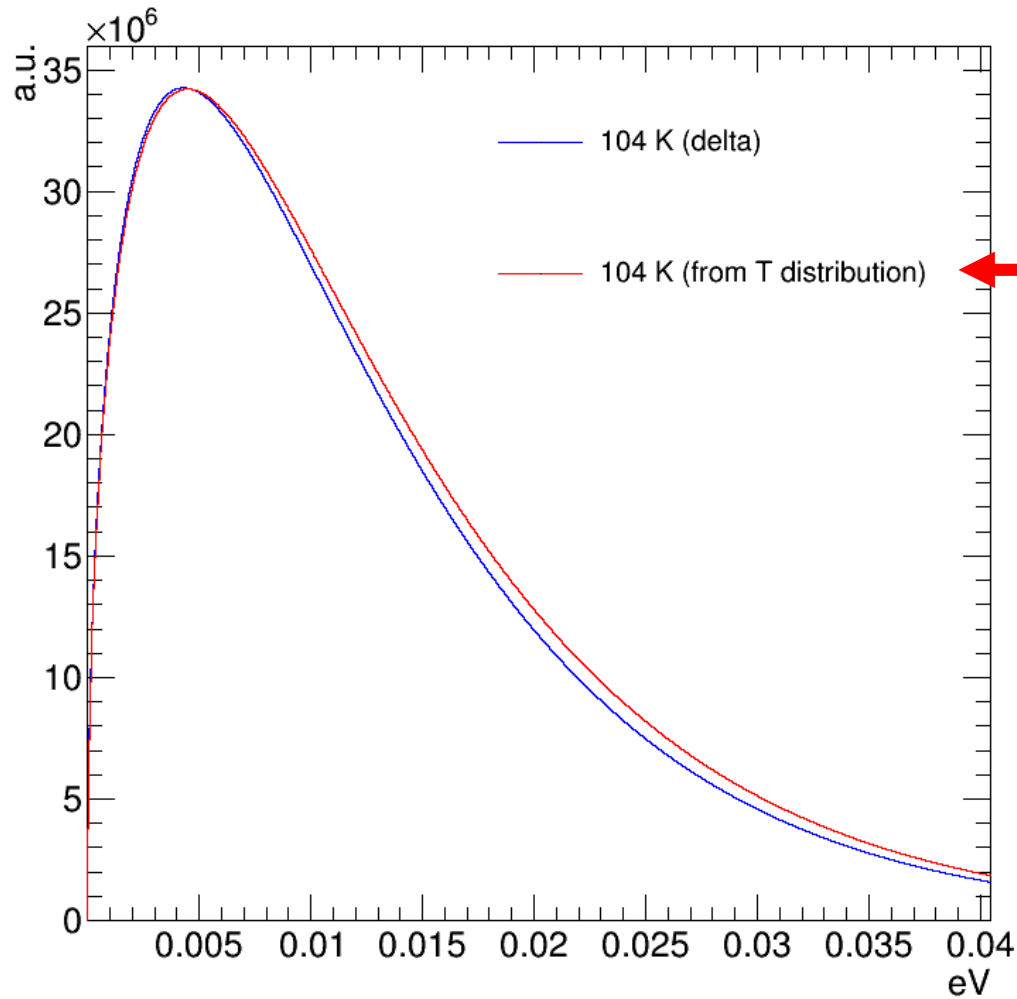


Temperature bins

6 fixed steps + 5 intermediate temperatures

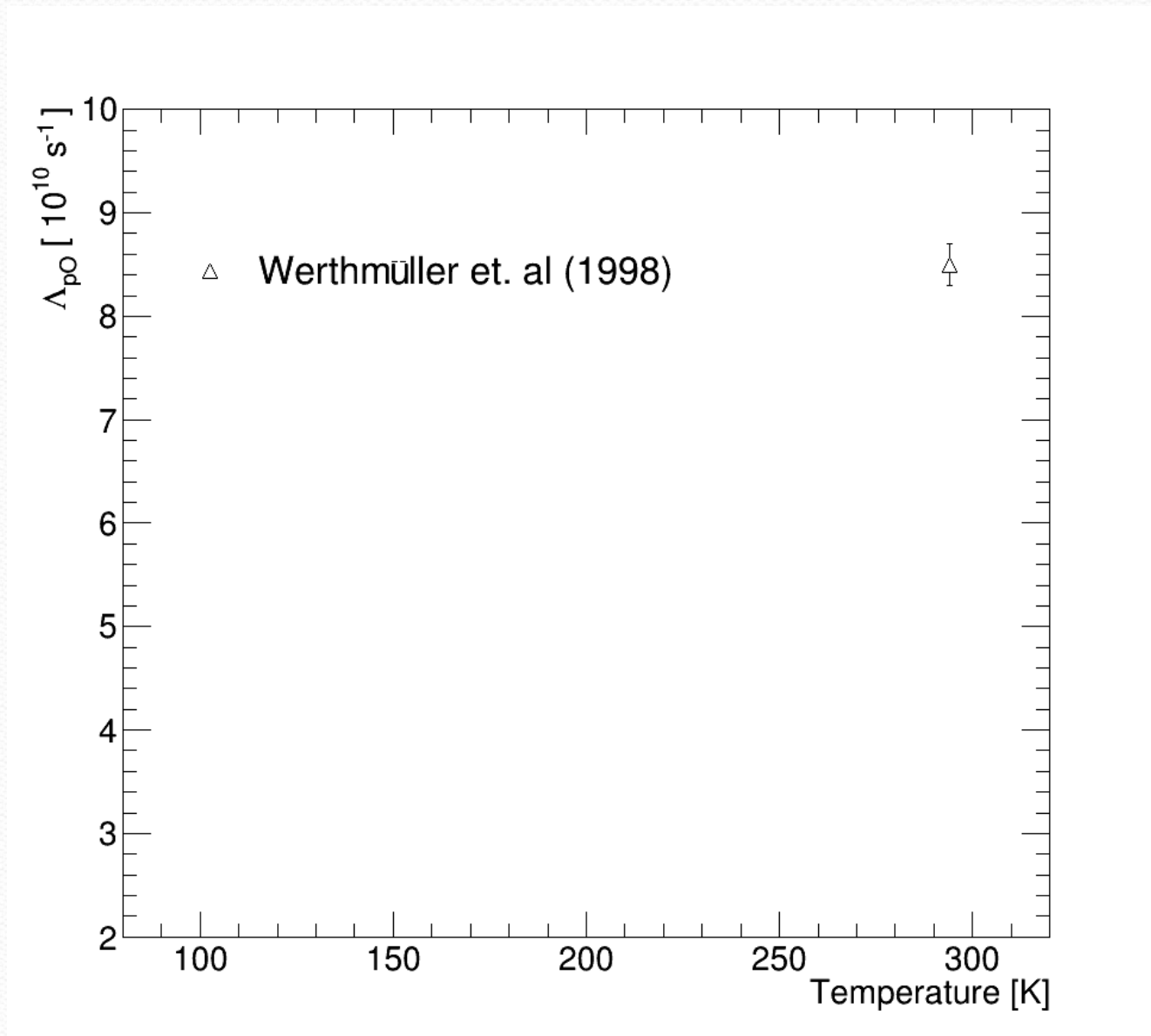


Very close to Maxwell-Boltzmann distribution

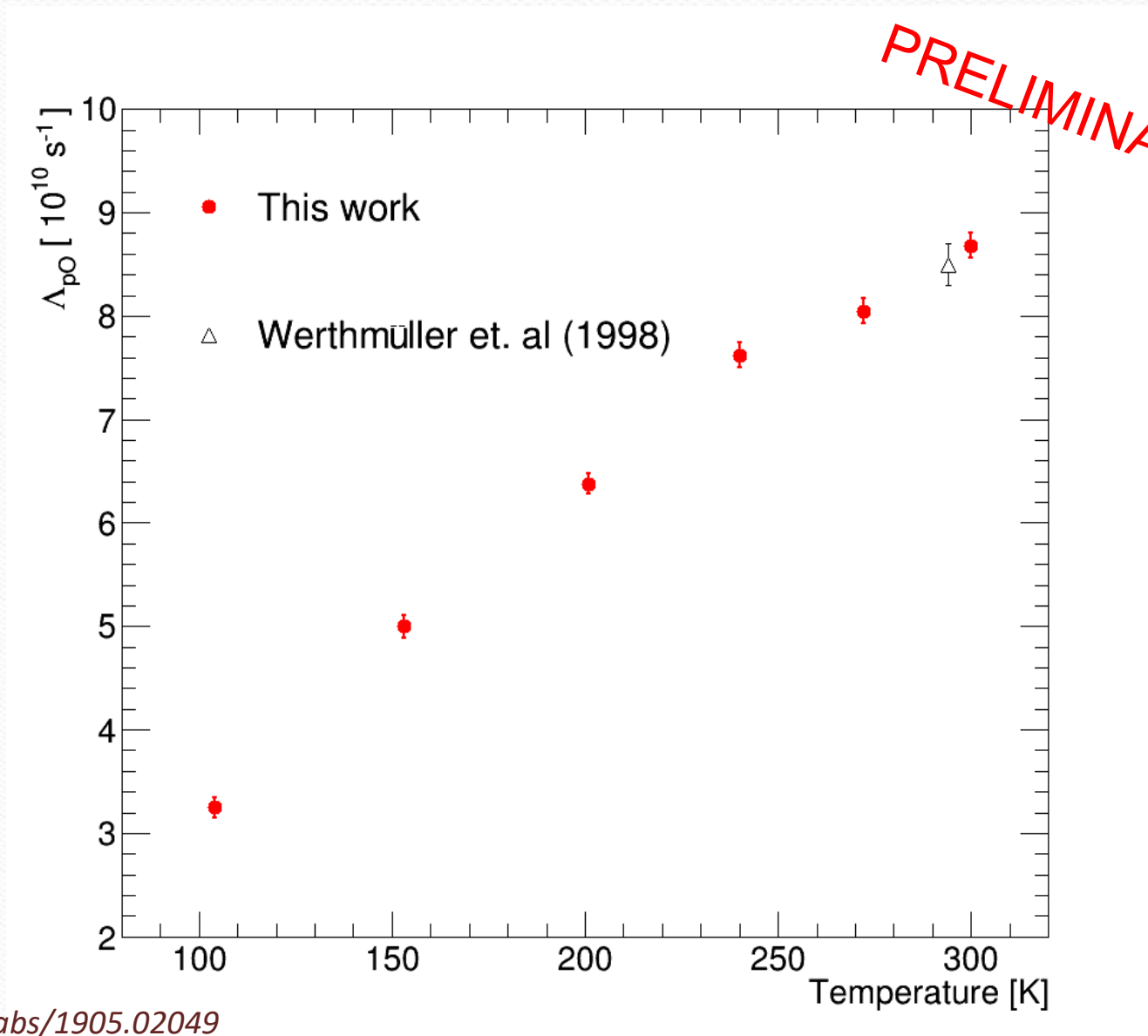


Results

Transfer rate measurement

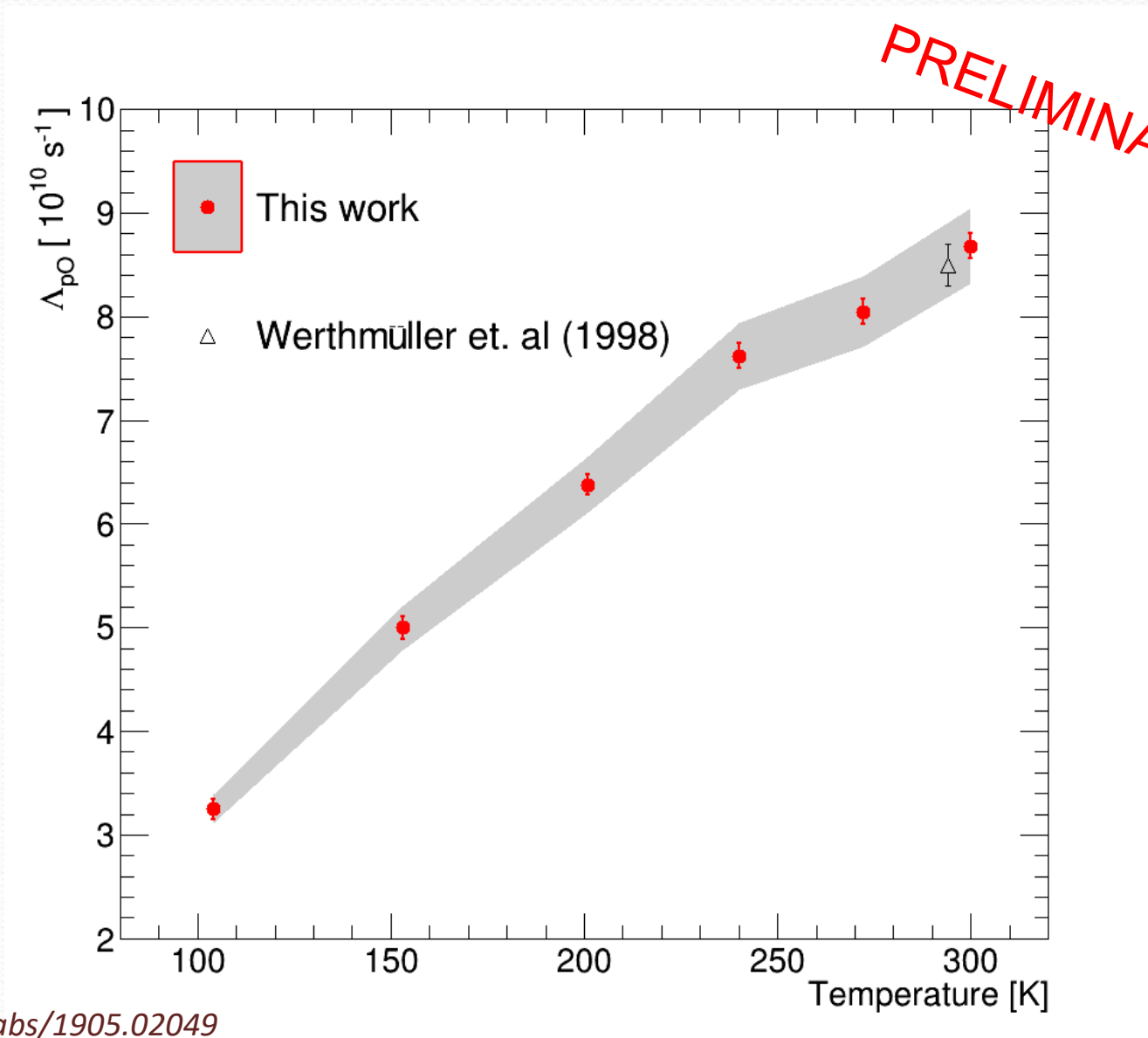


Transfer rate measurement



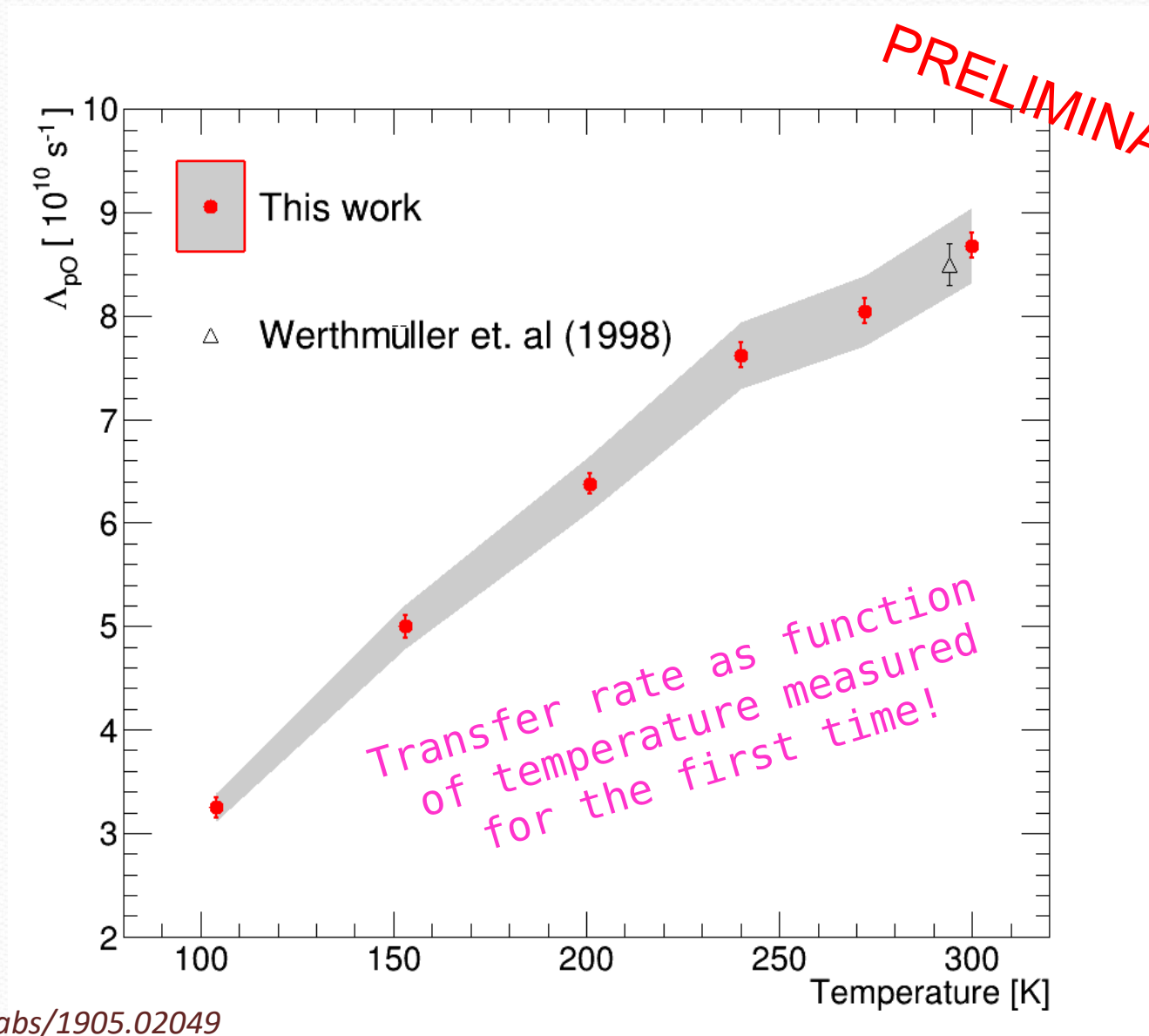
<http://arxiv.org/abs/1905.02049>

Transfer rate measurement



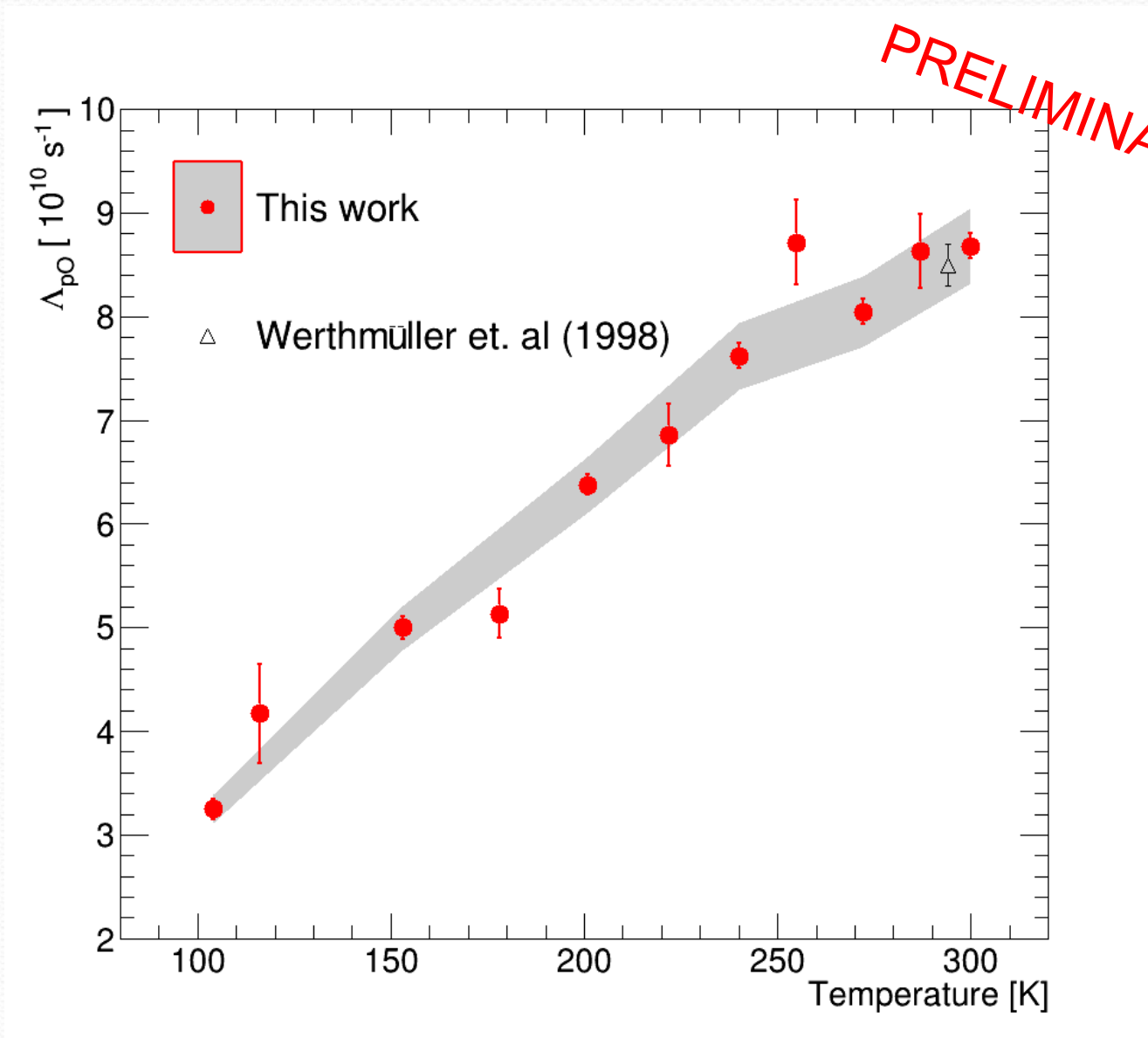
<http://arxiv.org/abs/1905.02049>

Transfer rate measurement

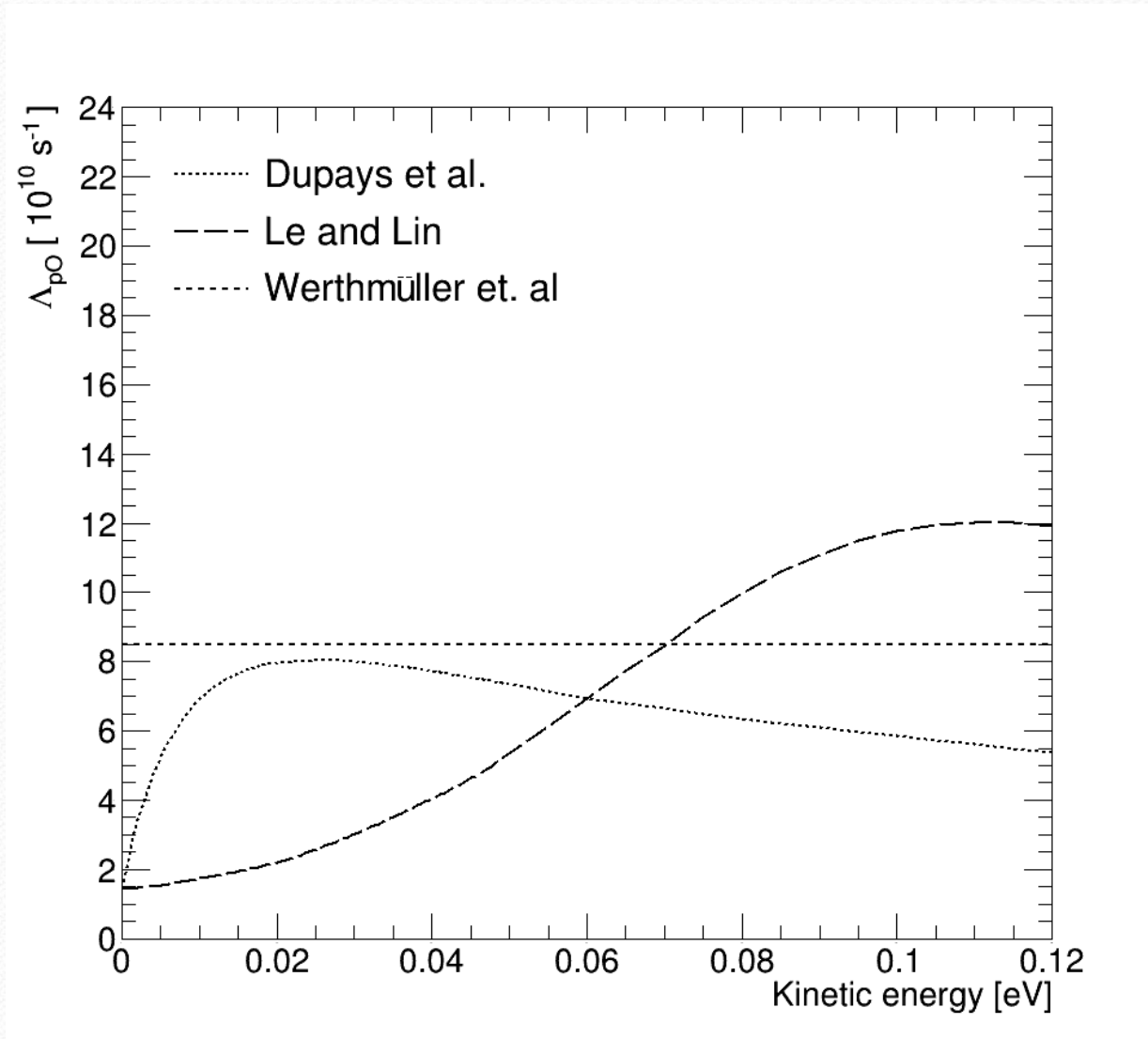


<http://arxiv.org/abs/1905.02049>

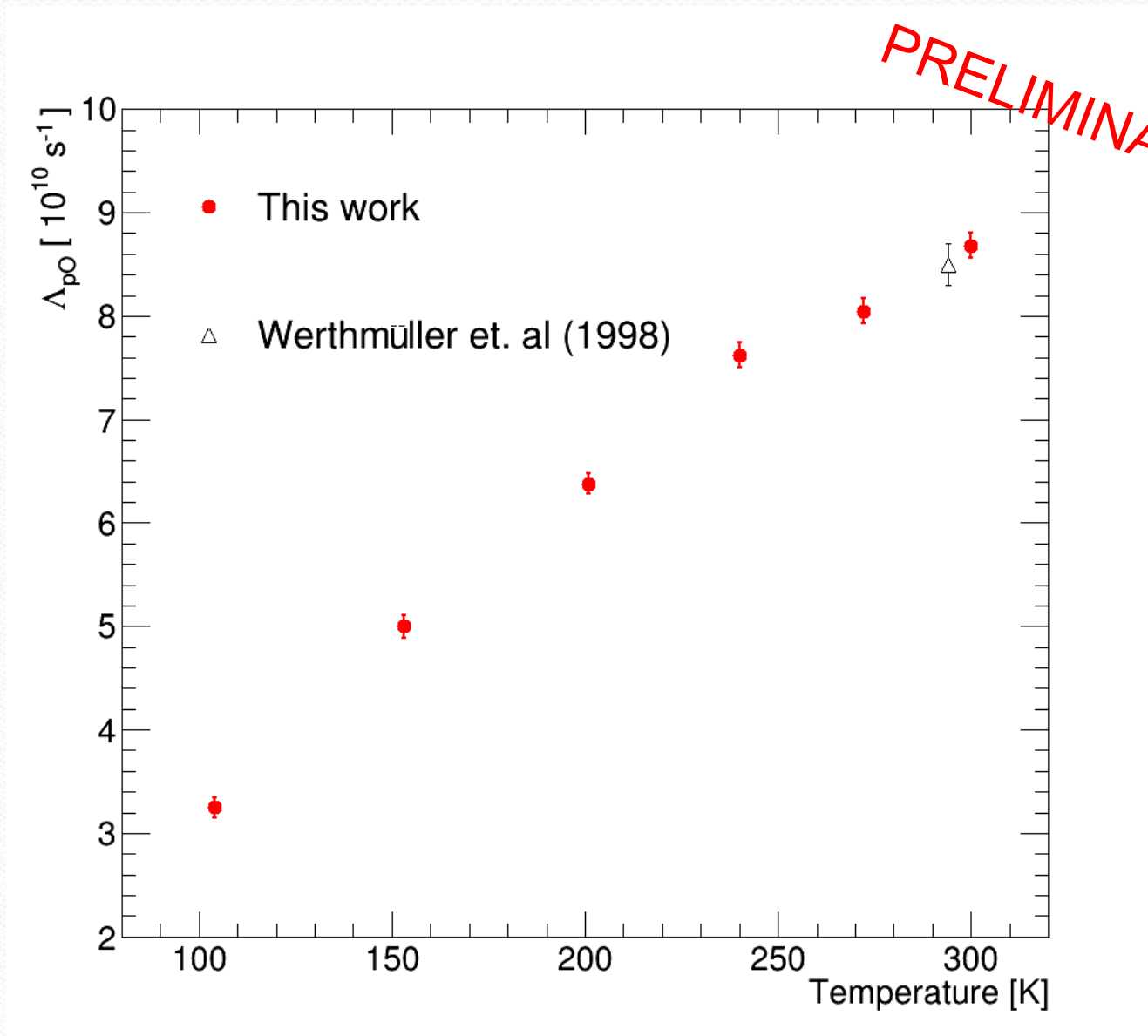
Transfer rate measurement



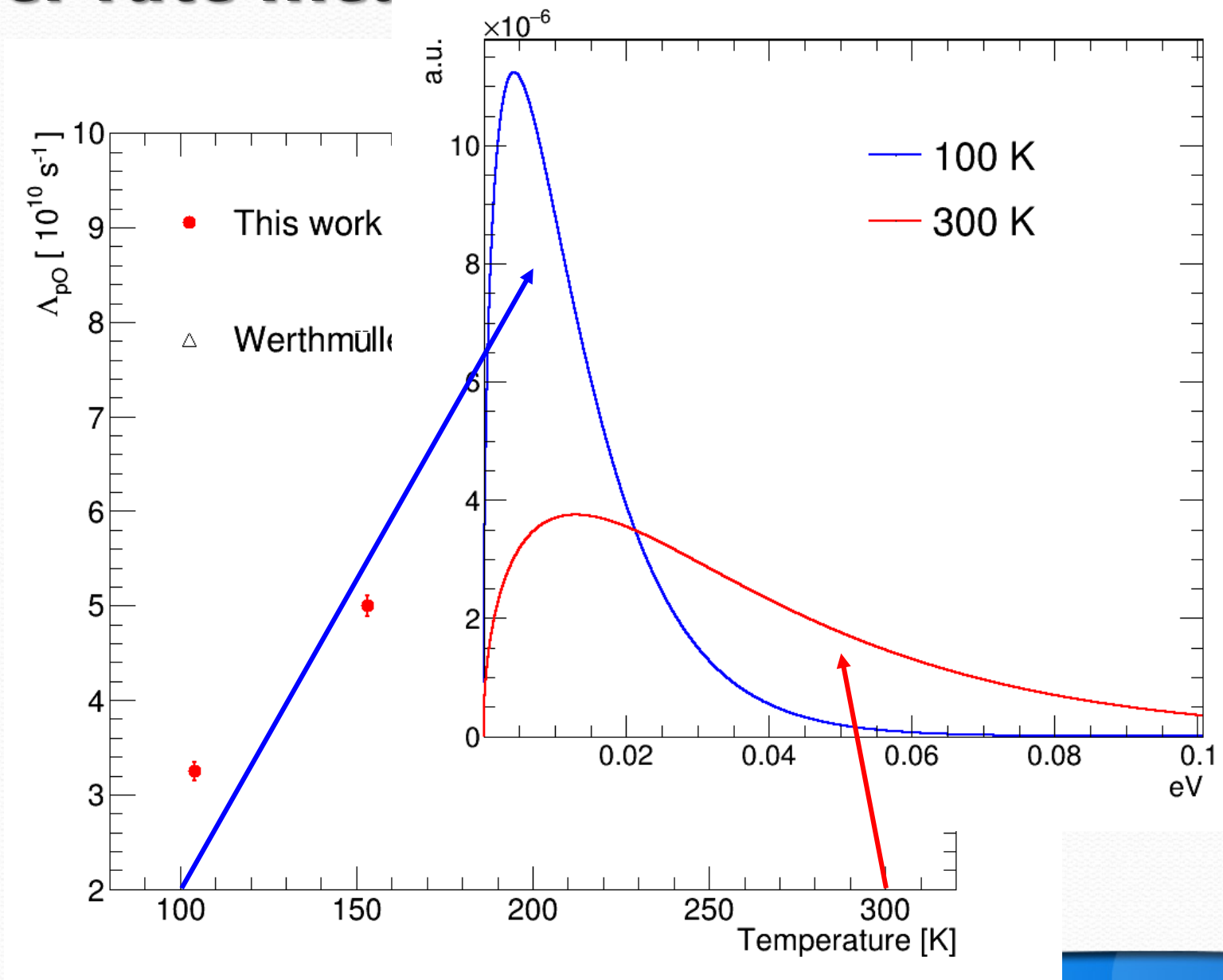
Transfer rate measurement



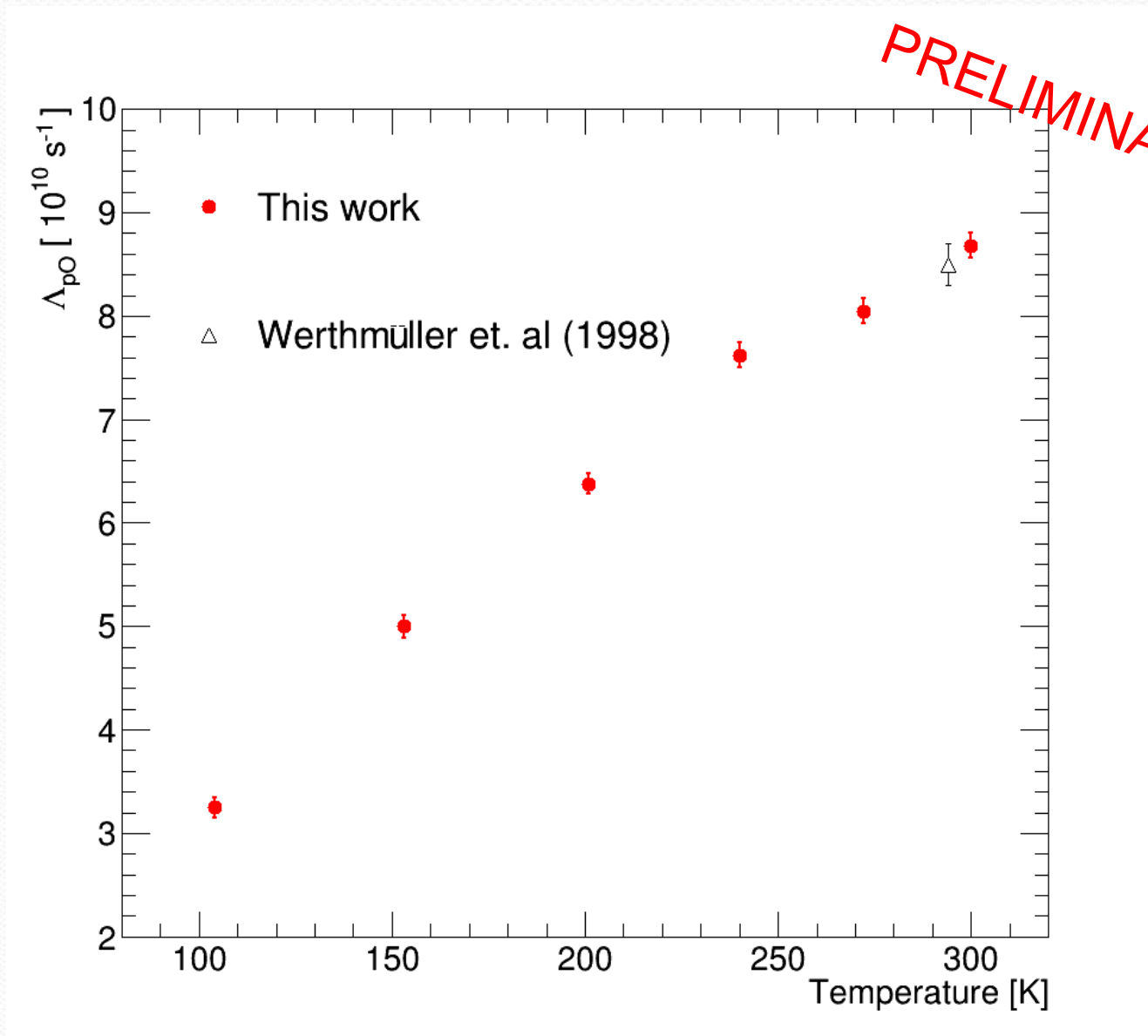
Transfer rate measurement



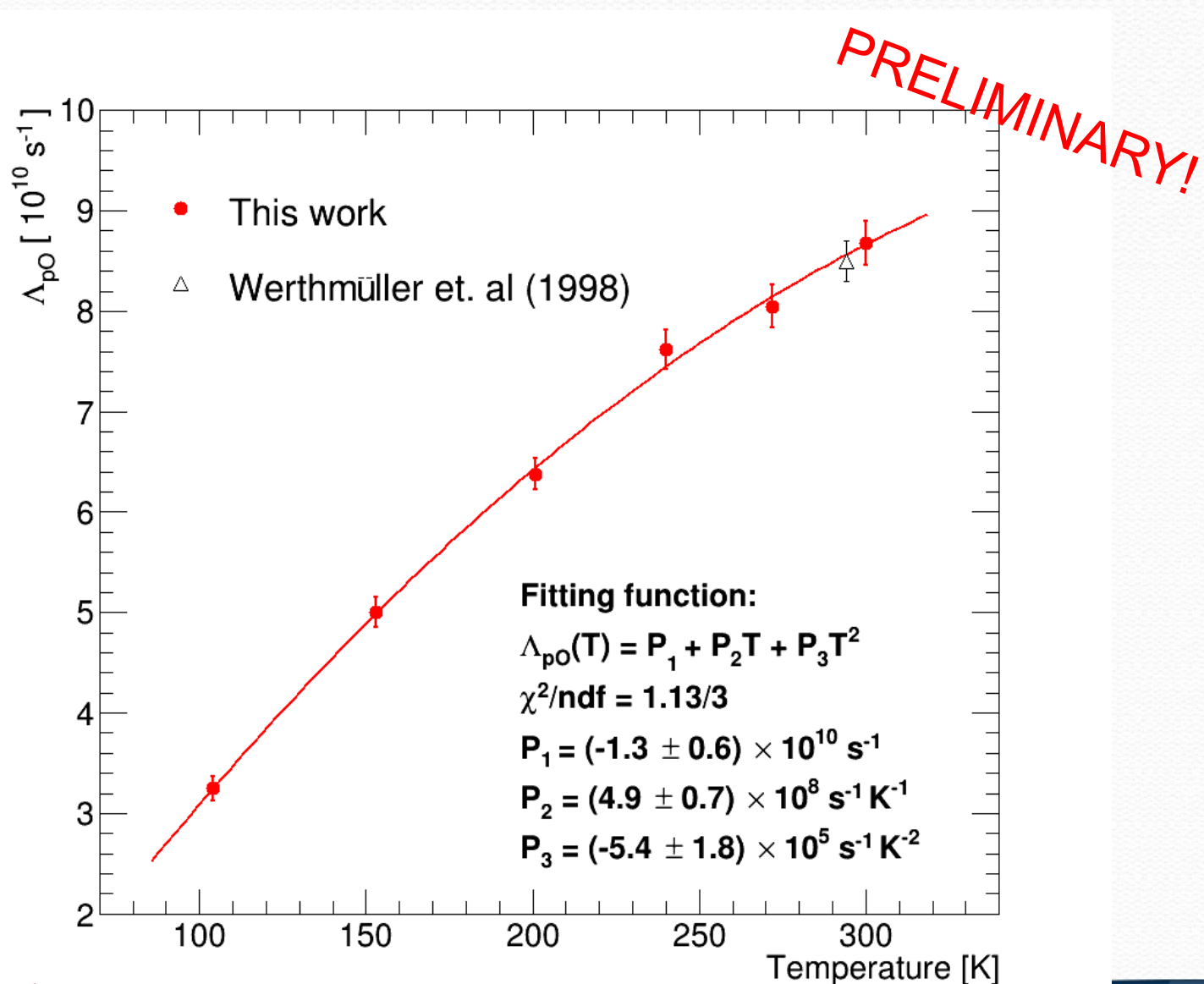
Transfer rate mea



Transfer rate measurement

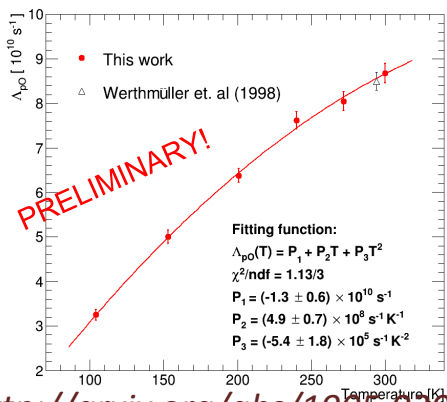
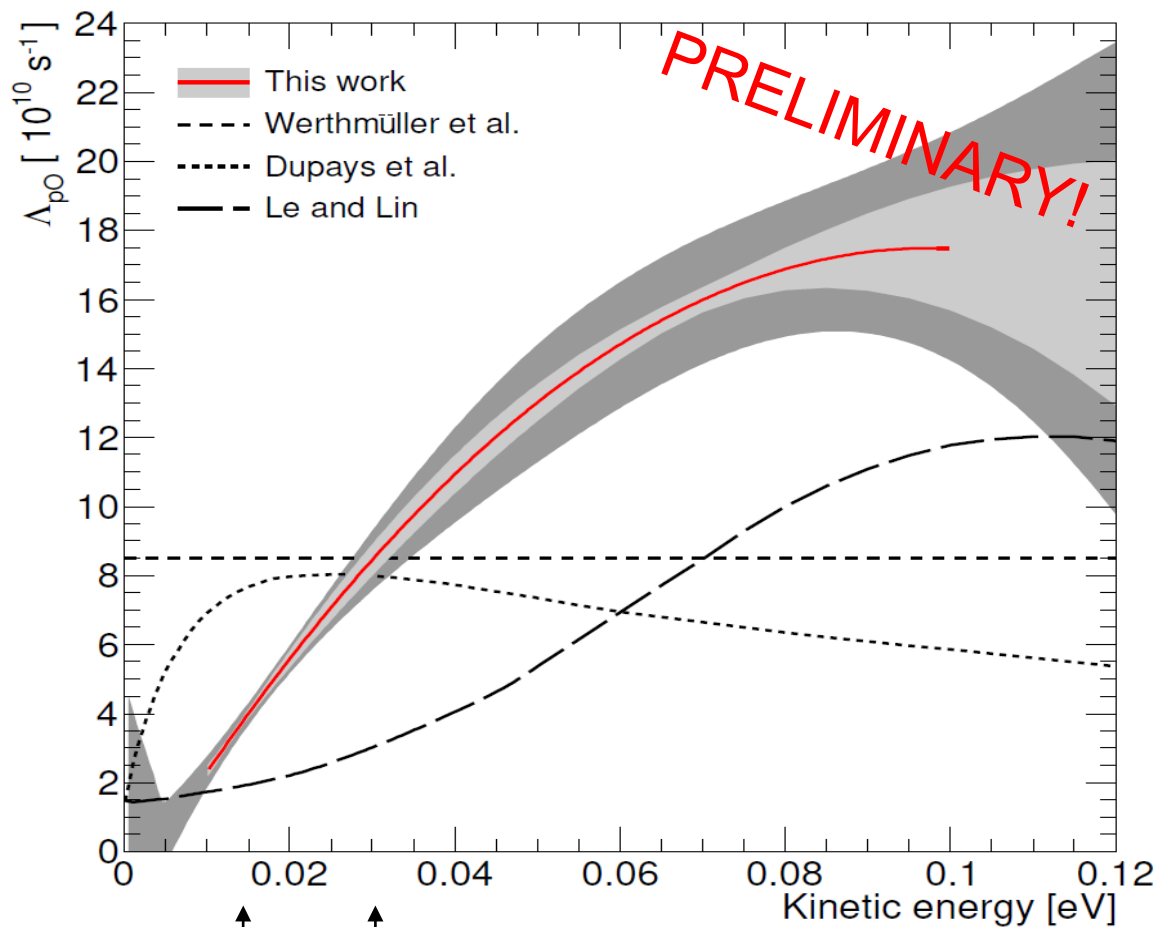
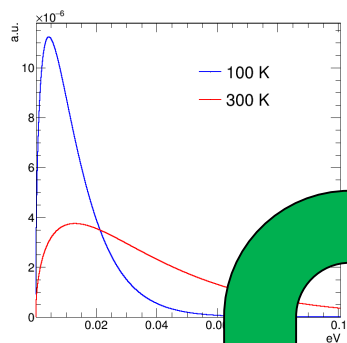


Transfer rate measurement



<http://arxiv.org/abs/1905.02049>

Transfer rate up to 120 meV



~100 K

~300 K

μp energy after de-excitation

<http://arxiv.org/abs/1905.02049>

Summary

- FAMU: measurement of the $(\mu^-p)_{1S}$ hyperfine splitting
- An exciting journey:
 - started *25 years ago*
 - *most intense pulsed beam* in the world
 - *best detectors* for energy and time observation
 - *first measurement of the energy dependence of muon transfer rate to Oxygen*
 - *innovative* and powerful laser system

Looking forward to perform the spectroscopic measurement!

Summary

- FAMU: measurement of the $(\mu^-p)_{1S}$ hyperfine splitting
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 - *first measurement of the energy dependence of muon transfer rate to Oxygen*
 - *innovative* and powerful laser system

Looking forward to perform the spectroscopic measurement!

Thanks!

Spare

Target: a necessary trade-off

Main requirements:

- Operating temperature range: $40 \text{ K} \leq T \leq 325 \text{ K}$
- Temperature control for measurement runs at fixed T steps from 300 K to 50K
- Gas @ constant density, H₂ charge pressure at room T is ~40 atm
- International safety certification (Directive 97/23/CE PED)
- Minimize walls and windows thickness
- Target shape and dimensions to
 - maximize muon stop in gas
 - to minimize distance gas – detectors
 - to be compliant to allowable volume at Riken Port
- H₂ compatible

... and, of course, all the above within time and cost constraints!

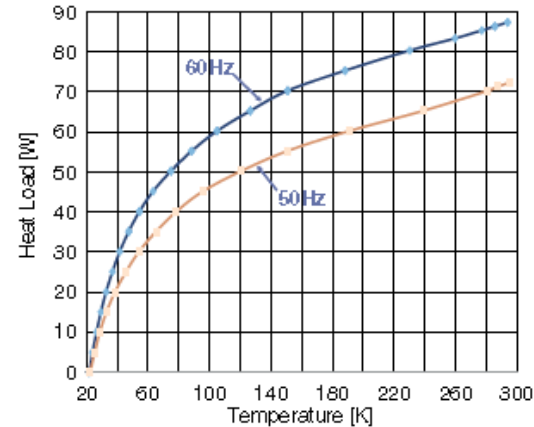
Thermal control

CH-104 77K CRYOCOOLER SERIES

Performance Specifications

Power Supply Hz	50	60
1st Stage Capacity Watts @ 77 K	34	42
Cooldown Time to 20 K Minutes	40	30
Weight kg (lbs.)	7.9 (17.5)	
Maintenance Hours	13,000	

CH-104 Cold Head Capacity Map (50/60 Hz)

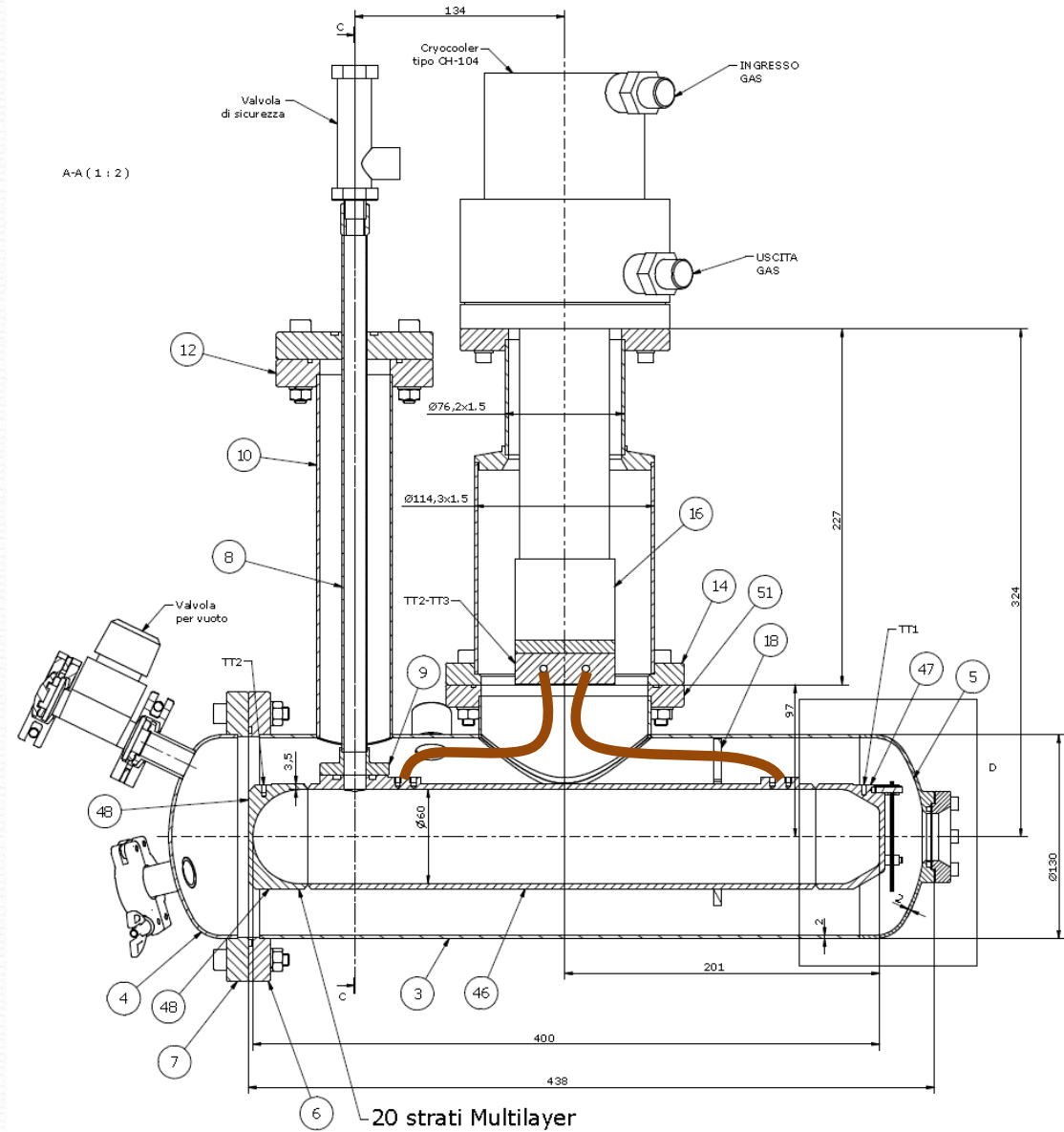


Standard Scope of Supply

- CH-104 Cold Head
- Zephyr®, HC-4E1, HC-8E4 or F-70L/H Compressor
- 3 m (10 ft.) Helium Gas Lines
- 3.5 m (11 ft.) Cold Head Cable
- Tool Kit



Best solution



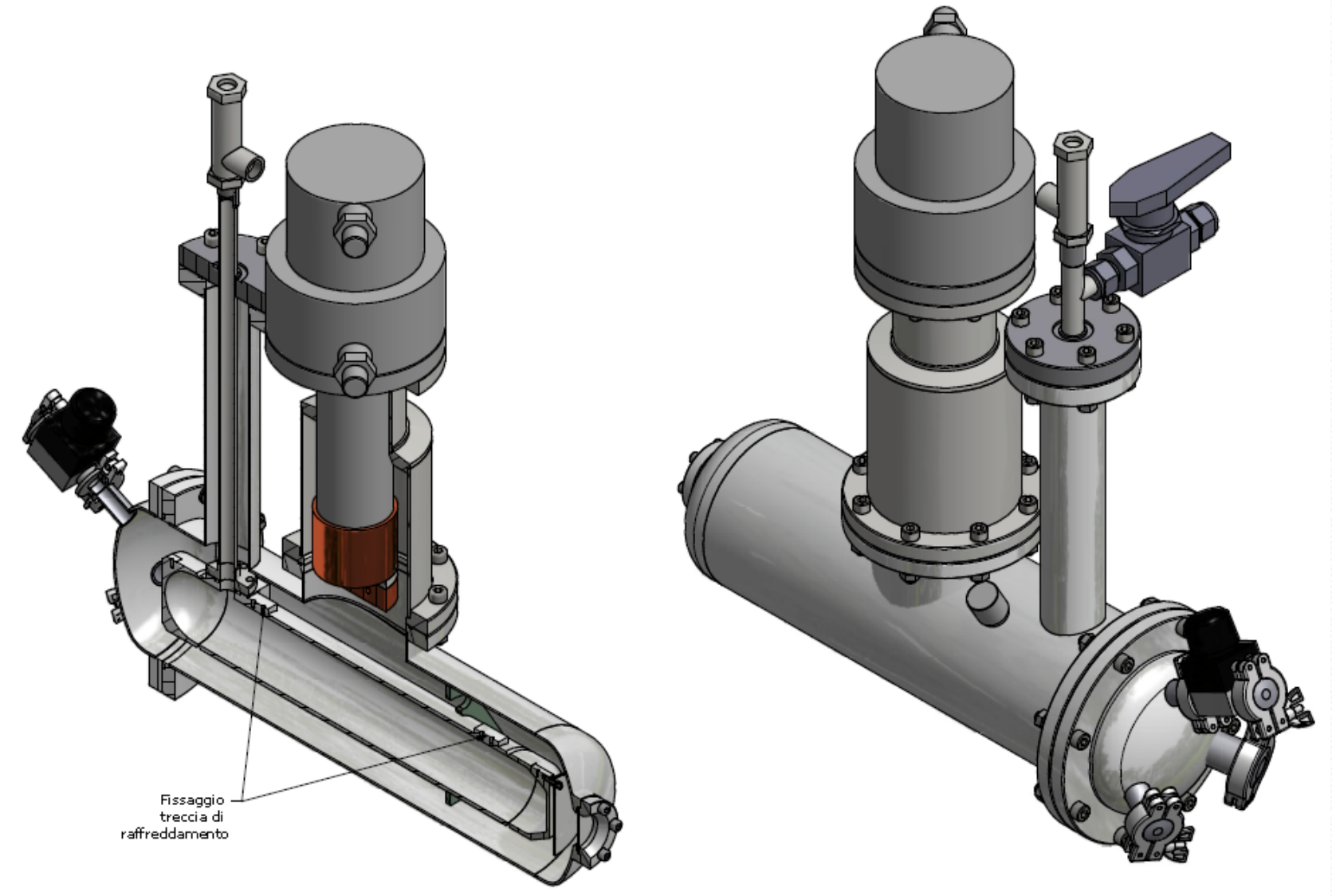
Target= Inner vessel with high P gas (44 bar)

- Al alloy 6082 T6 cylinder D = 60 mm and L = 400 mm, inner volume of 1.08 l
- Internally Ni/Au plated (L = 280 mm)
- Cylinder side wall thickness = 3.5 mm
- Wrapped in 20 layers of MLI
- Front window D= 30 mm 2.85 mm thick
- Three discs of 0.075 mm Al foil for window radiative shield
- 304L SS gas charging tube
- 304L SS cooler cold-end support
- G10 mechanical strut
- Two Cu straps for cooling

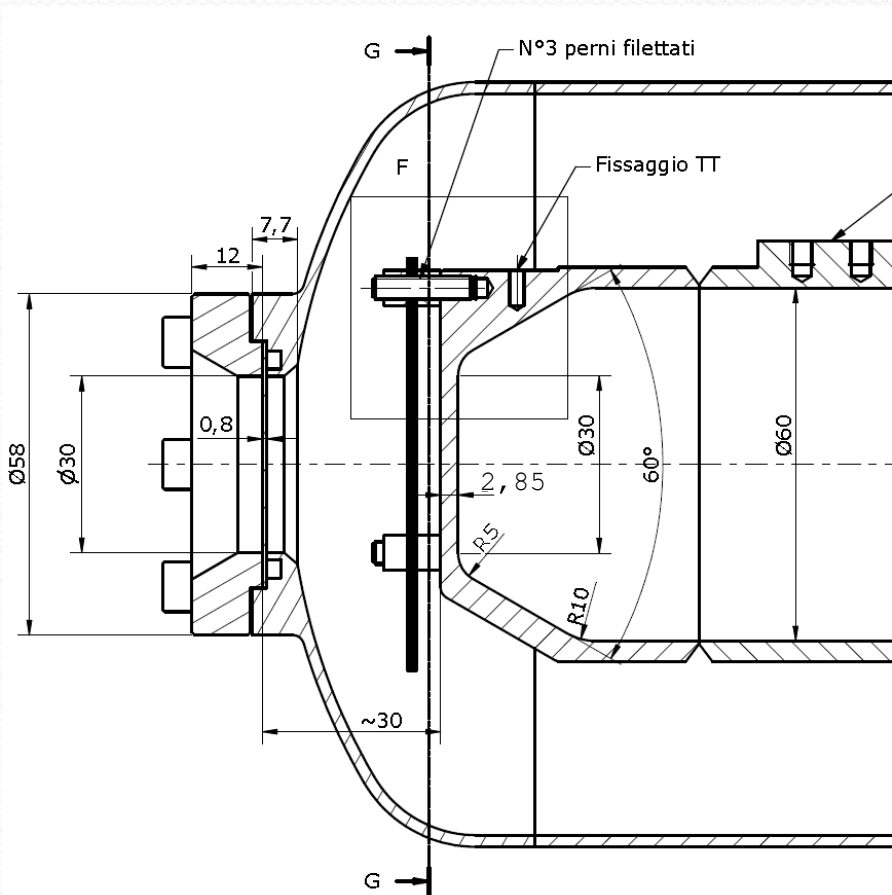
Vacuum vessel = outer cylinder (P atm)

- Al6060 D=130 mm, 2 mm thick walls
- ≈30mm between inner/outer walls
- Flanged Al window 0.8 mm thick
- Pumping valve & harness feed-tru's

Drawings



Front window



Thickness

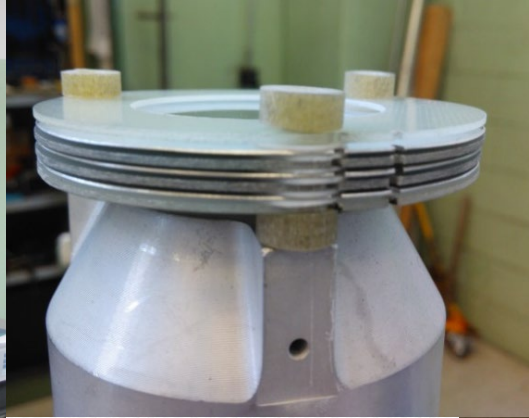
Side walls (inner vessel, MLI, outer shell)

- $t_{\text{inner}} = 3.5 \text{ mm Al6082}$
- $t_{\text{Ni_Au}} = 150 + 10 \mu\text{m} \approx 0.16 \text{ mm}$
- $t_{\text{MLI_Al}} = 1.6 \mu\text{m pure Al} = 0.0016 \text{ mm}$
- $t_{\text{MLI_Poly}} < 130 \mu\text{m Polyester} = 0.13 \text{ mm}$
- $t_{\text{outer}} = 2 \text{ mm Al6060}$

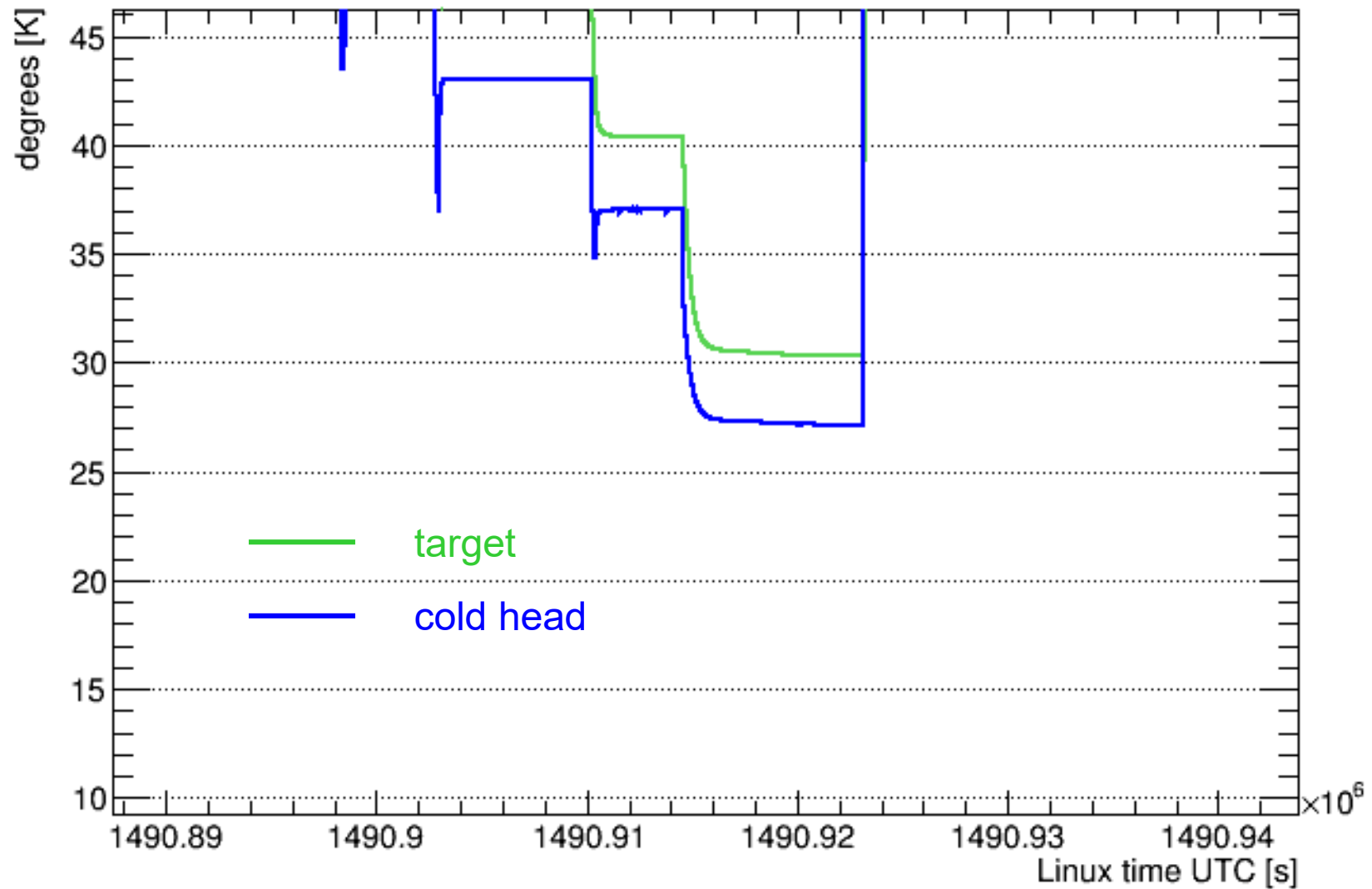
Windows

- $t_{\text{inner_w}} = 2.85 \text{ mm Al}$
- $t_{\text{Ni_Au}} = 0.16 \text{ mm}$
- $t_{\text{Al_shields}} = 0.225 \text{ mm Al}$
- $t_{\text{outer_w}} = 0.8 \text{ mm Al}$

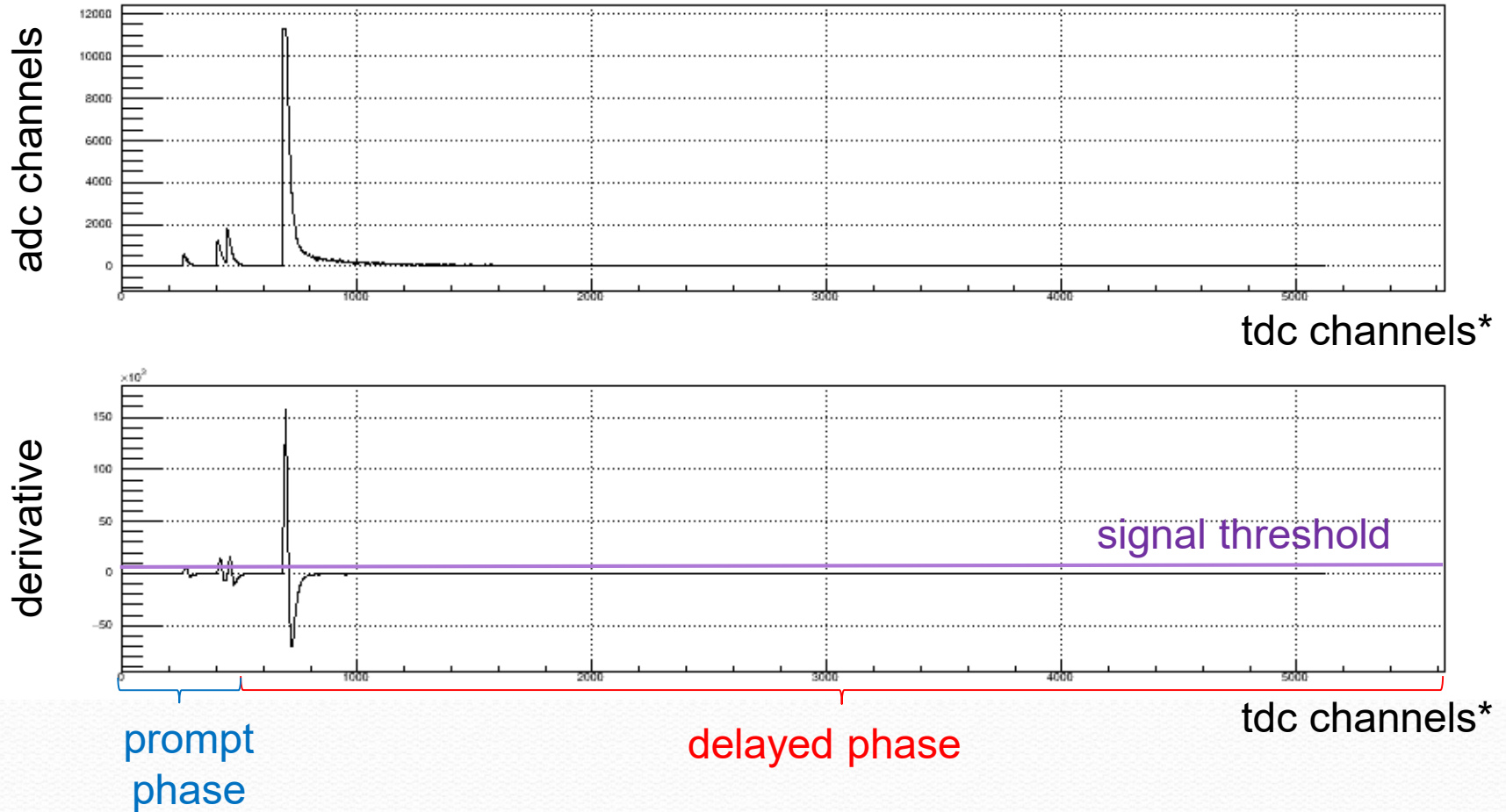
Target in lab



2017 on beam: lowest temperature

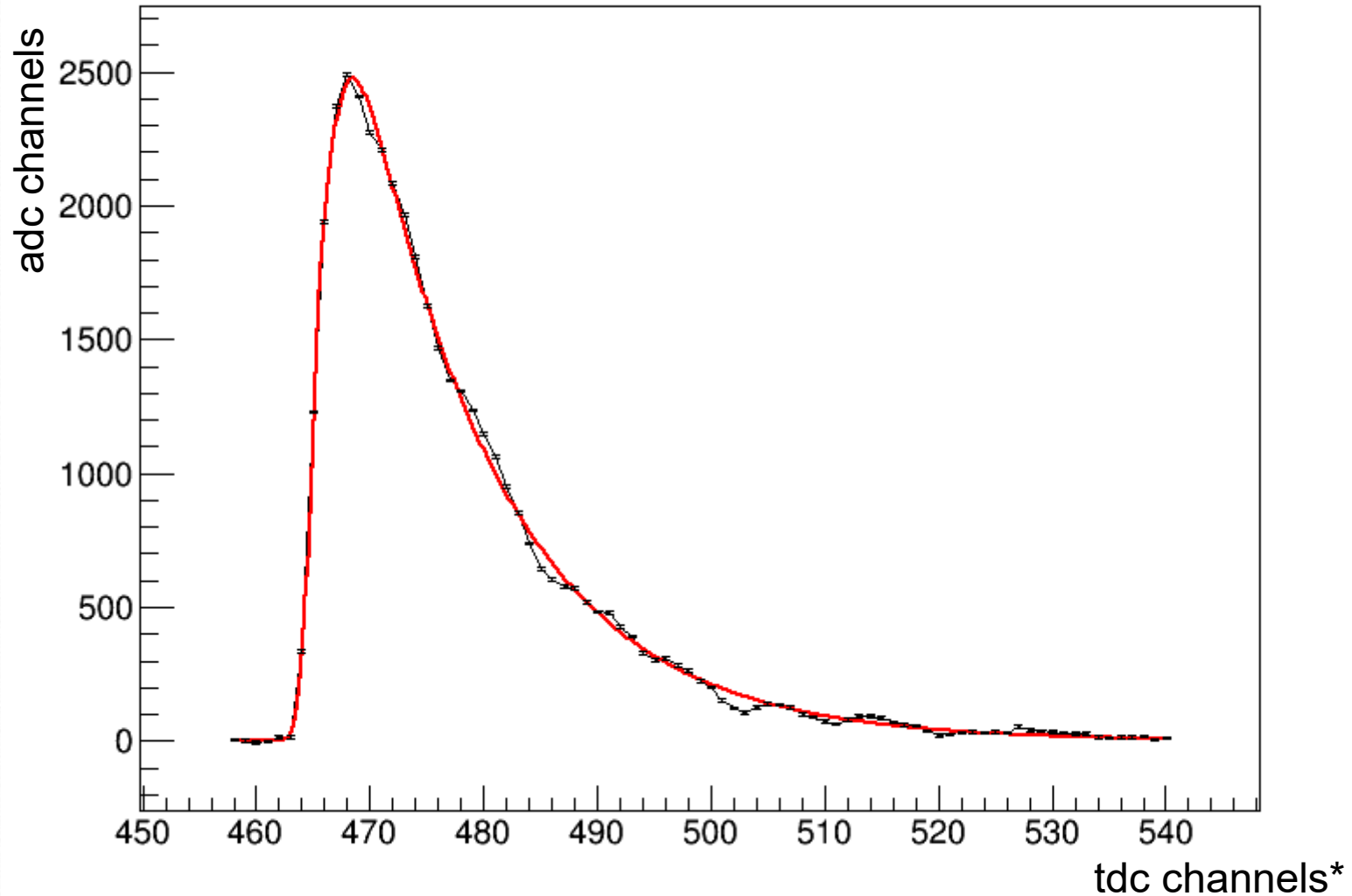


Waveform processing



* 1 tdc = 2 ns

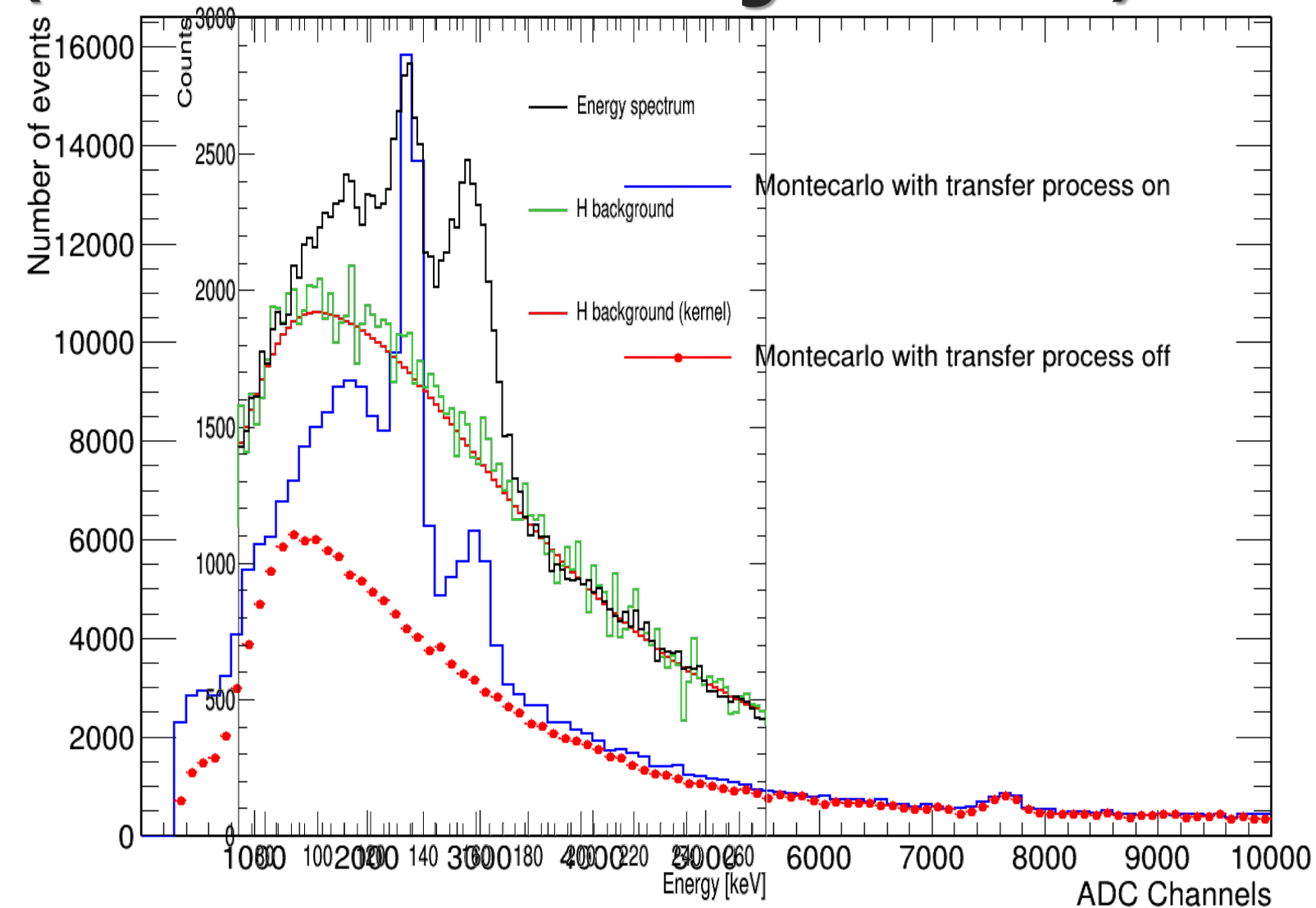
Single pulse fit



* 1 tdc = 2 ns

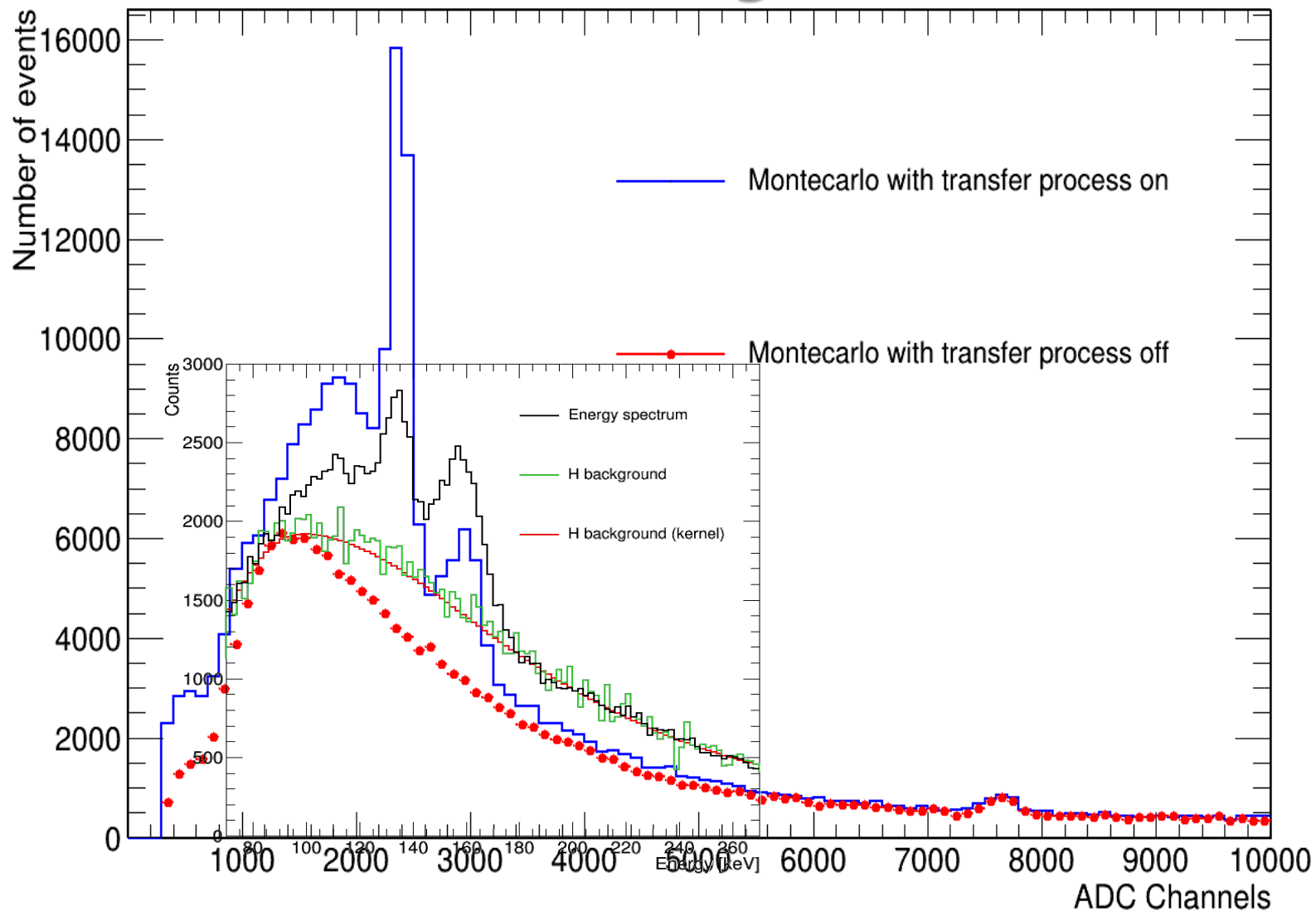
Similar tail!

(even if a better tuning is needed)



Similar tail!

(even if a better tuning is needed)



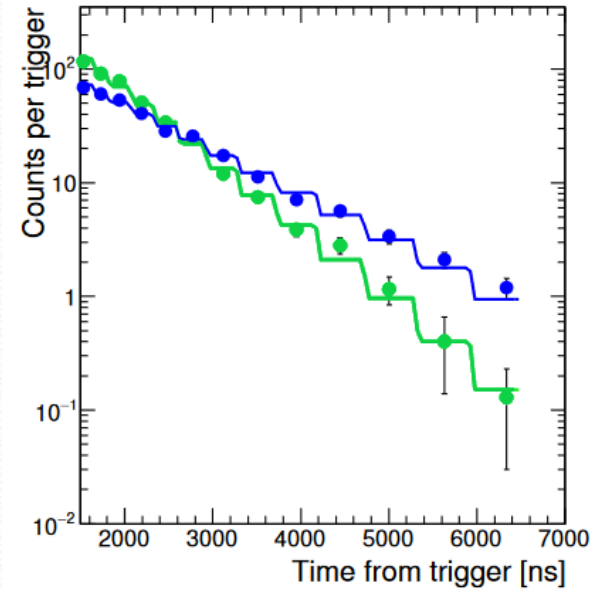
Data Fit

Variation of the number of mu-p atoms in the time dt:

$$dN_{\mu p}(t) = -N_{\mu p}(t) \lambda_{\text{dis}}(T) dt$$

Disappearance rate

Fit: numerical integration



$$\lambda_{\text{dis}}(T) = \lambda_0 + \phi [c_p \Lambda_{pp\mu} + c_d \Lambda_{pd}(T) + c_o \Lambda_{pO}(T)]$$

UNKNOWN TERM

Rate of disappearance of muons bounded to p (decay, ..)

$\Lambda_{pp\mu}, \Lambda_{...}$, transfer rates

$c_p, c_{...}$ concentrations of hydrogen, deuterium, oxygen

ϕ number density of atoms in the gas target

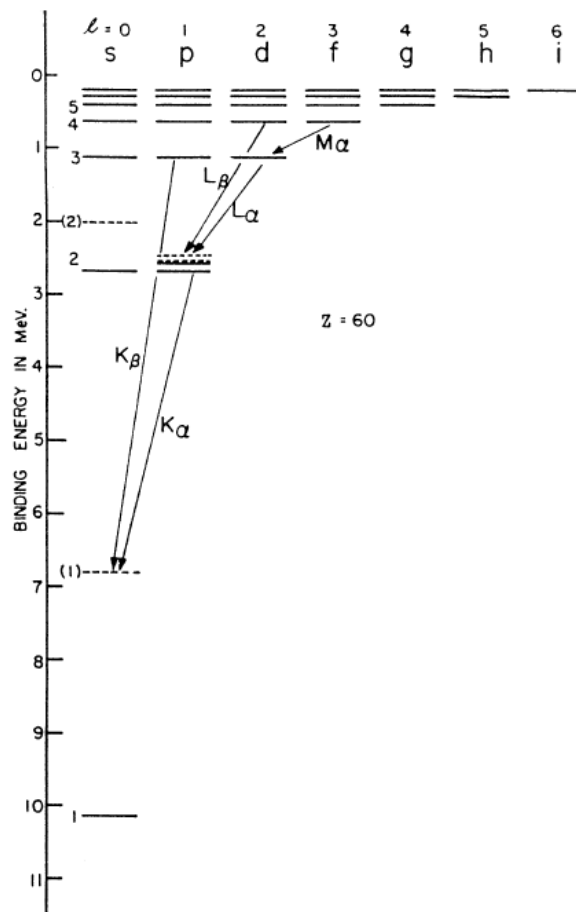
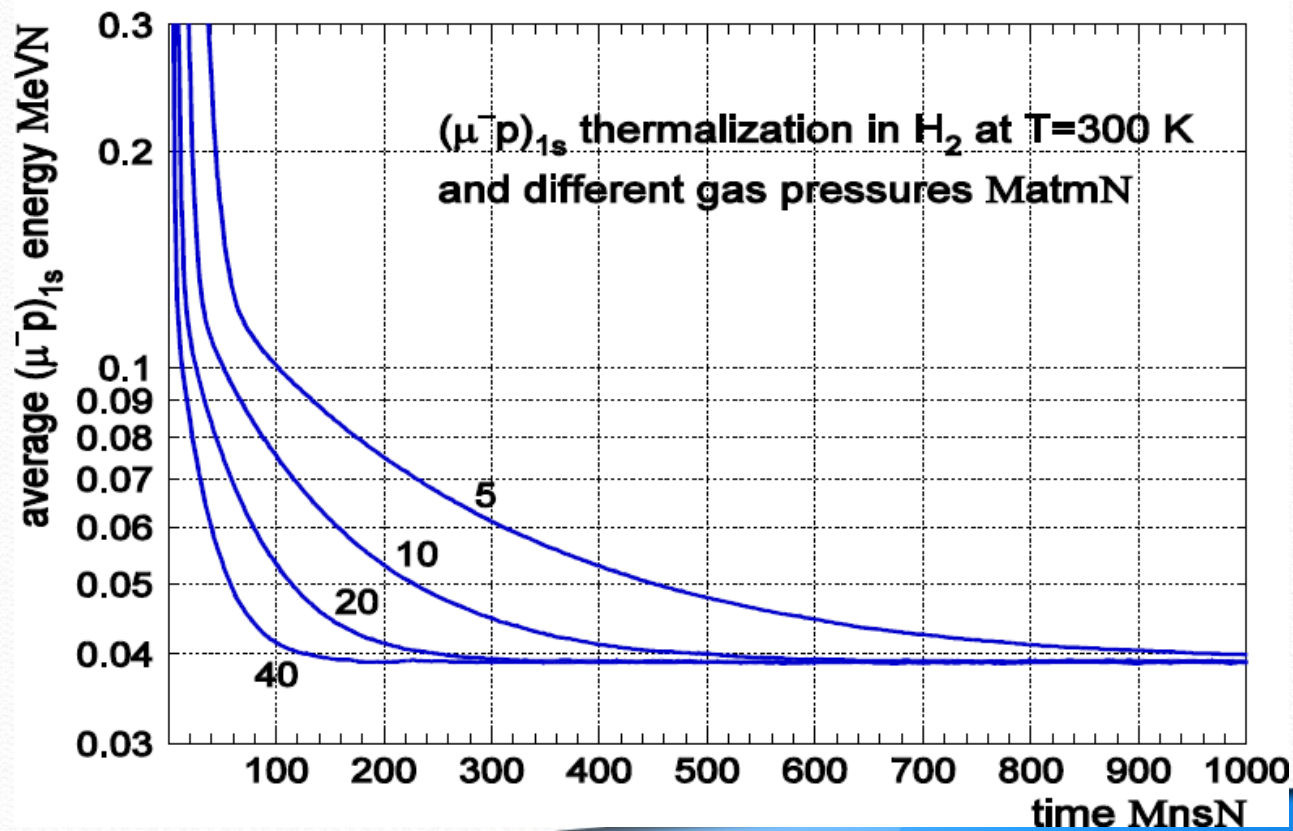
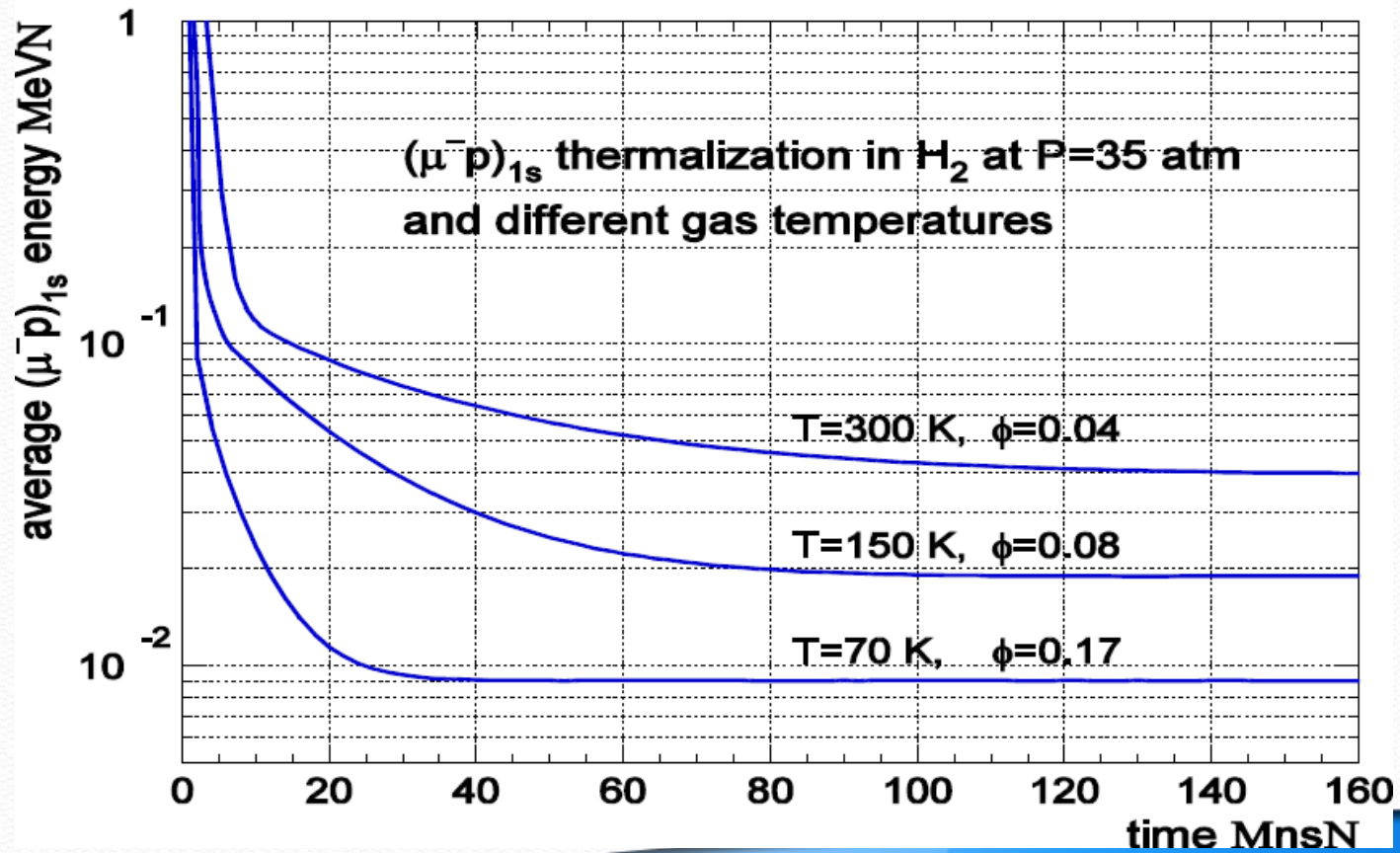


Fig. 3.3. Levels of a muonic atom, showing notation for X-rays. For $Z = 60$ the 1s state is raised by 3.3 MeV (dashed level) because of the finite size of the nuclear charge [117].

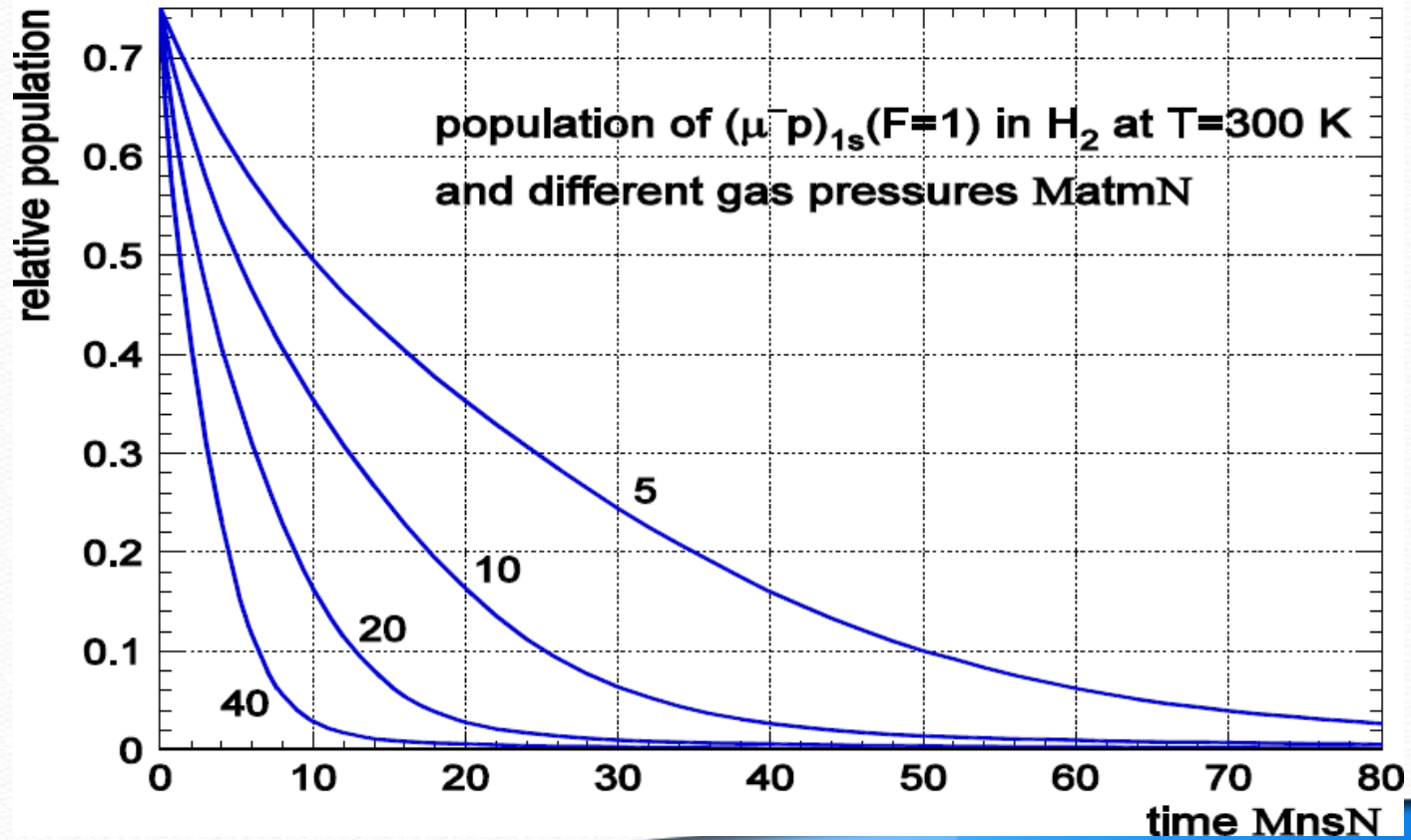
Thermalization of μp



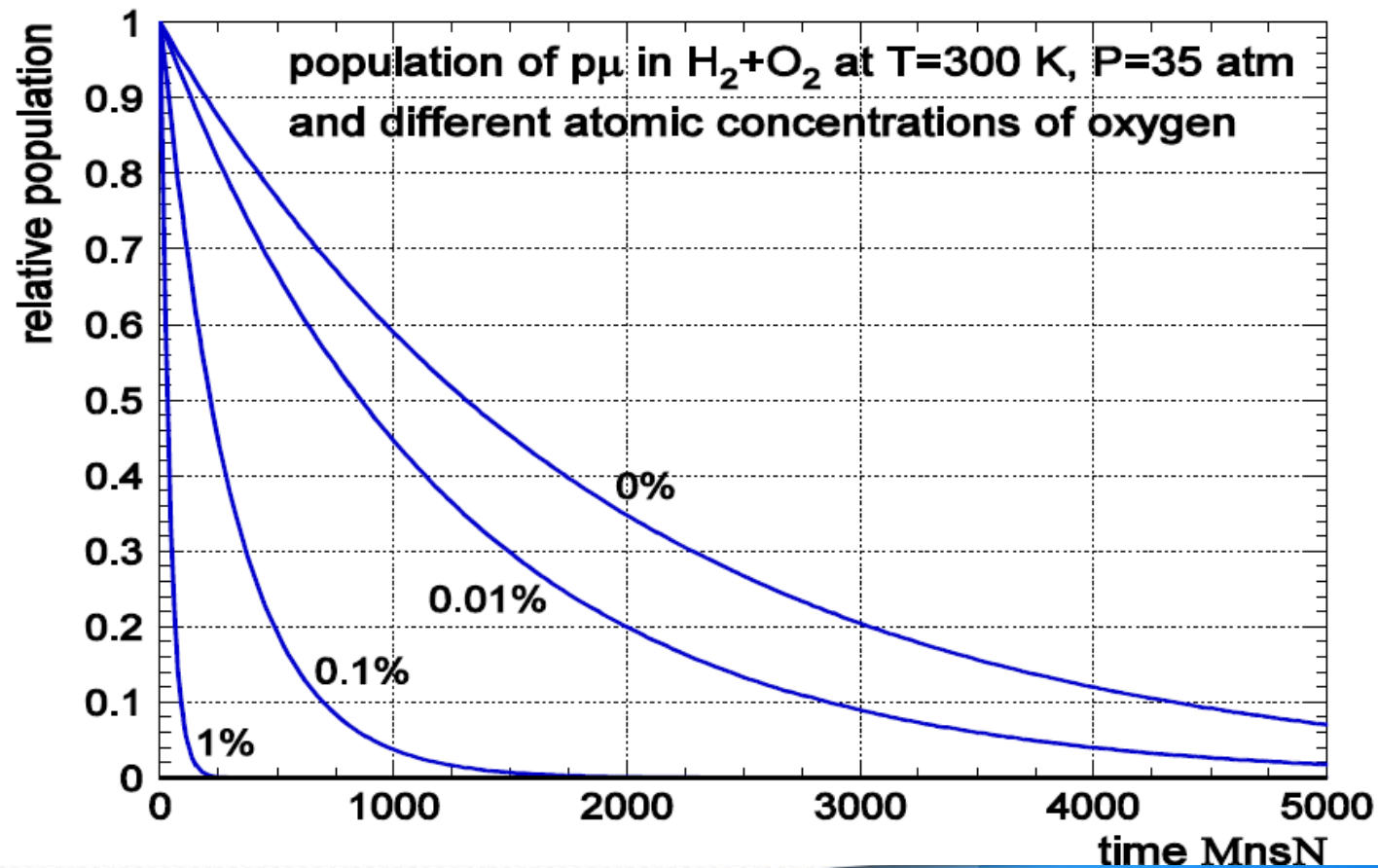
Thermalization of μp



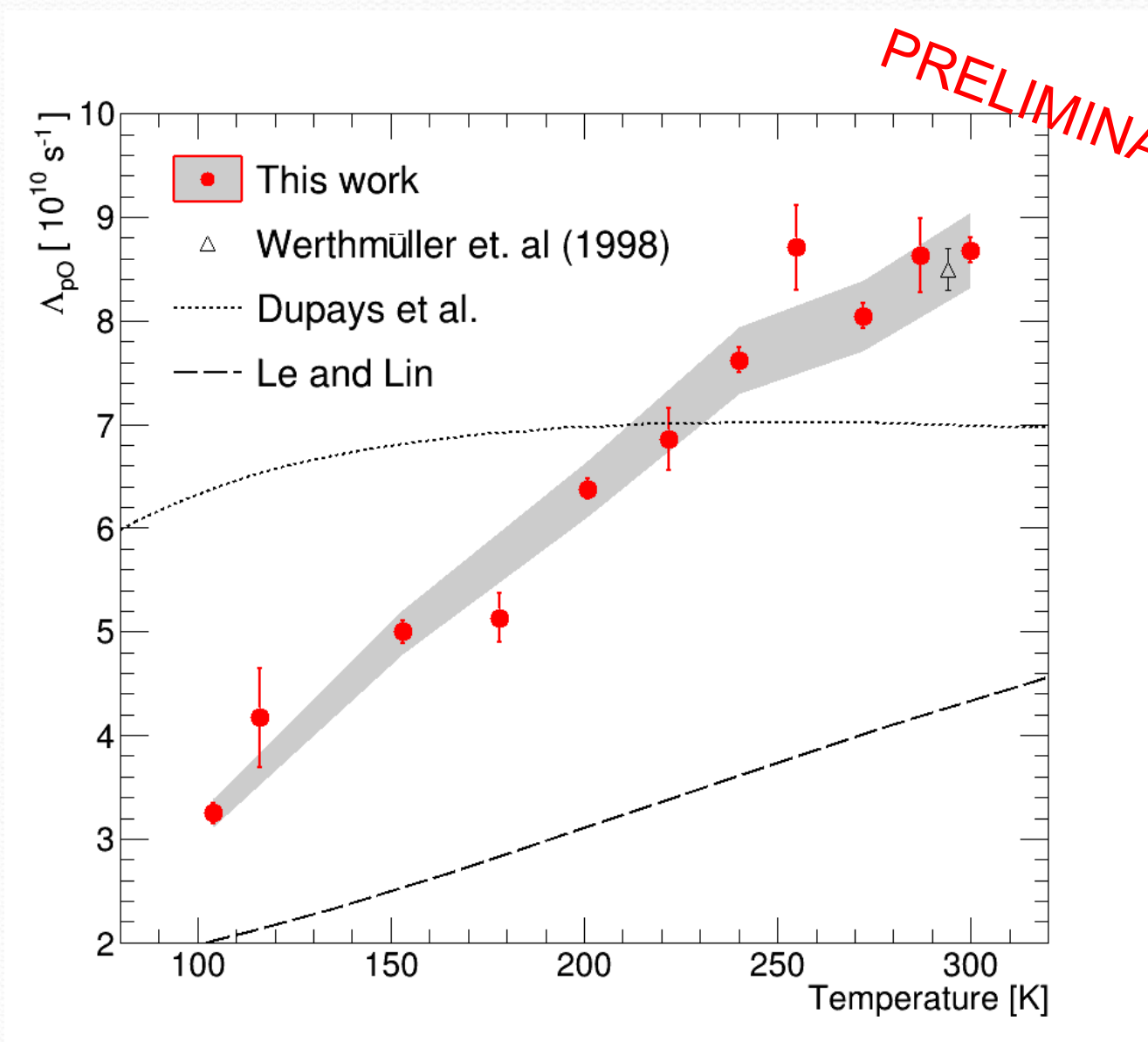
Depolarization of μp



Lifetime of μp and muon transfer

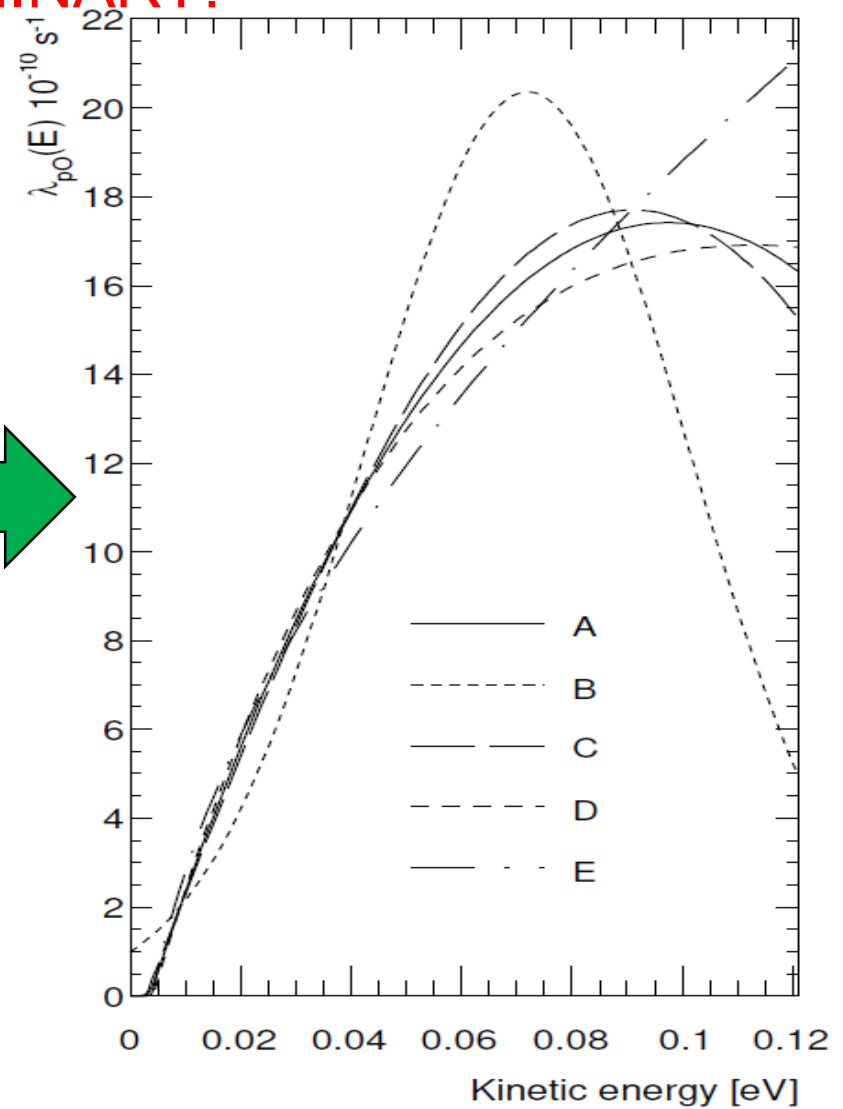
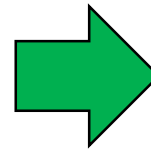
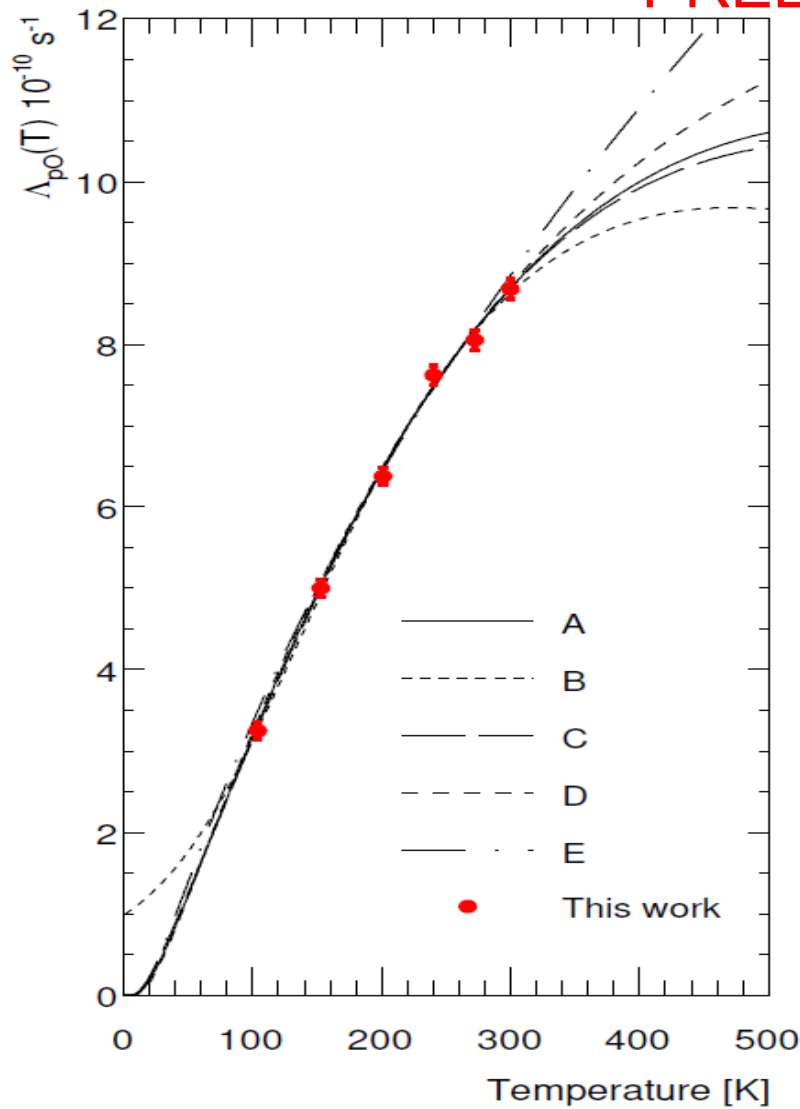


Transfer rate measurement



Transfer rate up to 120 meV

PRELIMINARY!

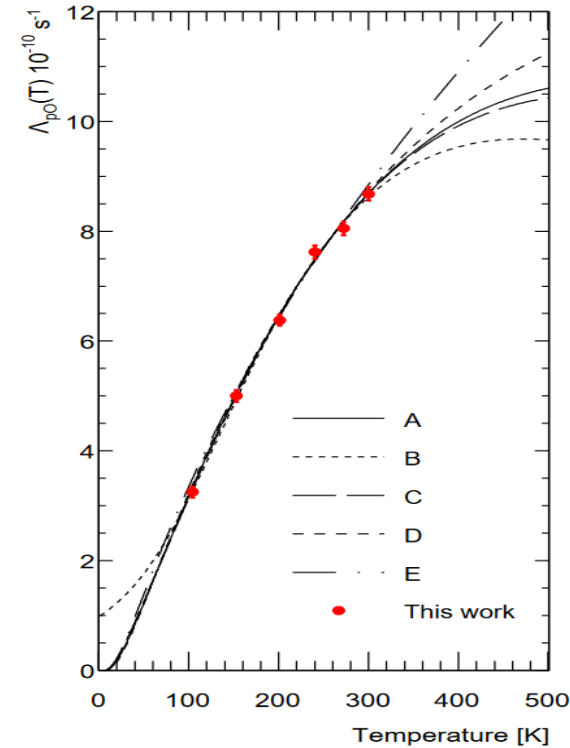


<http://arxiv.org/abs/1905.02049>

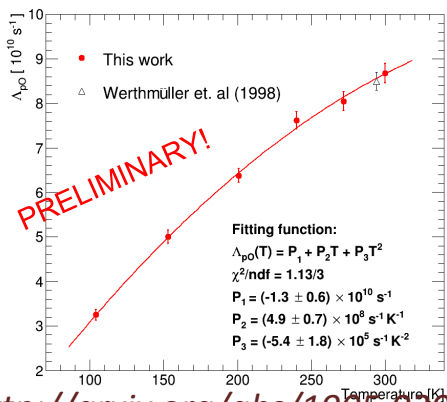
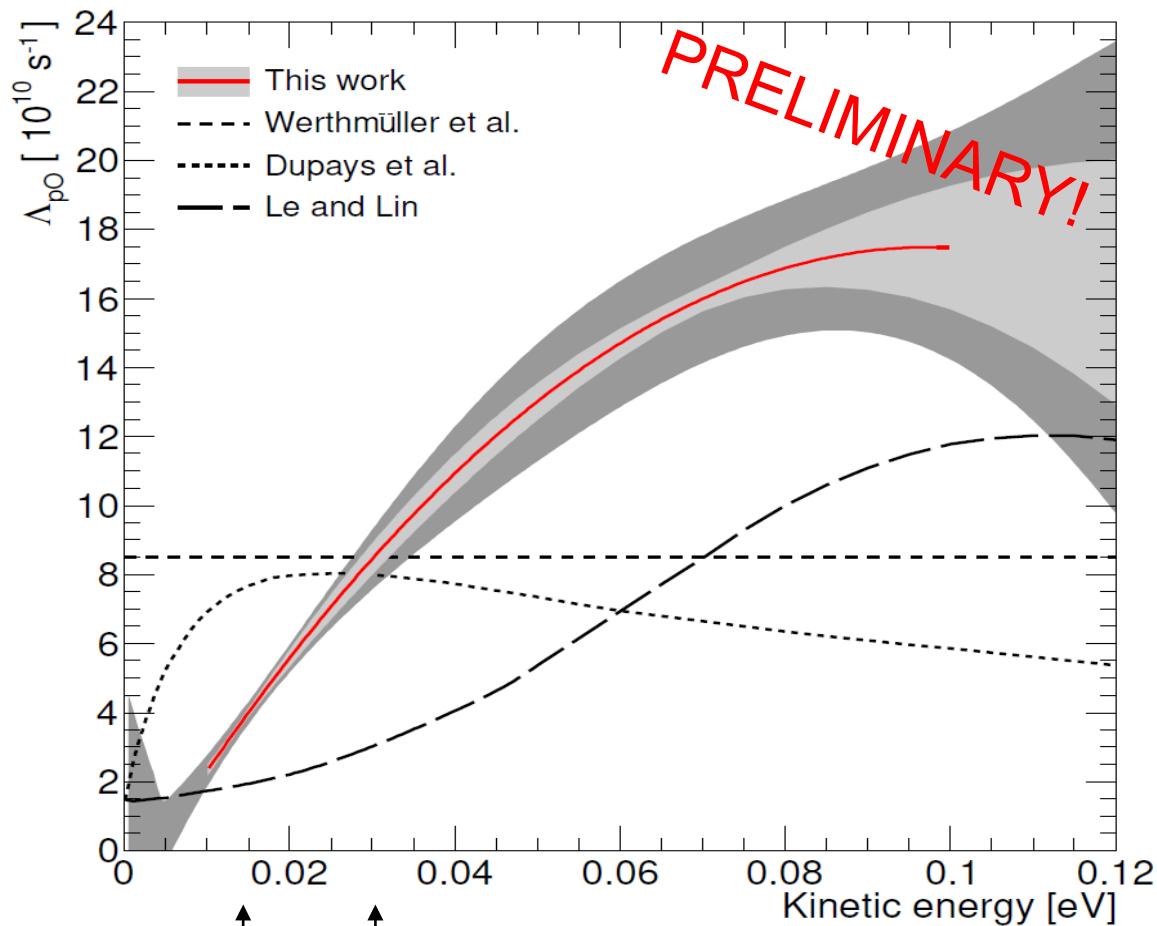
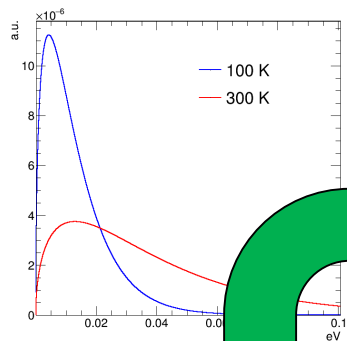
Tested functions transfer rate $\Lambda_{pO}(T)$

<http://arxiv.org/abs/1905.02049>

Fit	Analytical expressions and χ^2	Optimal values of the parameters
A	$\lambda_{pO}(E; p) = \sum_{k=1}^3 p_k E^{k-1}$ $\Lambda_{pO}(T; p) = \sum_{k=1}^3 (2k-1)!! p_k (k_B T/2)^{k-1}$ $\chi^2/ndf = 1.13/3$	$p_1 = (-1.32 \pm 0.61) \times 10^{10} \text{ s}^{-1}$ $p_2 = (3.85 \pm 0.54) \times 10^{12} \text{ s}^{-1} \text{ eV}^{-1}$ $p_3 = (-1.98 \pm 0.65) \times 10^{13} \text{ s}^{-1} \text{ eV}^{-2}$
B	$\lambda_{pO}(E; p) = p_1 e^{-((E-p_2)/p_3)^2}$ $\Lambda_{pO}(T; p) = p_1 \frac{e^{-p_2^2/p_3^2}}{\sqrt{\pi}} \left(\frac{p_3}{k_B T}\right)^{\frac{3}{2}} \left(\Gamma\left(\frac{3}{4}\right) {}_1F_1\left(\frac{3}{4}, \frac{1}{2}, X^2\right) - 2X\Gamma\left(\frac{5}{4}\right) {}_1F_1\left(\frac{5}{4}, \frac{3}{2}, X^2\right)\right)$, $X = \frac{p_3^2 - 2p_2 k_B T}{2p_3 k_B T}$ $\chi^2/ndf = 1.23/3$	$p_1 = (20.4 \pm 0.97) \times 10^{10} \text{ s}^{-1}$ $p_2 = (0.0719 \pm 0.0077) \text{ eV}$ $p_3 = (0.0413 \pm 0.0058) \text{ eV}$
C	$\lambda_{pO}(E; p) = p_1 + p_2 \sin(p_3 E)$ $\Lambda_{pO}(T; p) = (p_1 + p_2 \sin(\frac{3}{2} \arctan(p_3 k_B T))) \times (1 + (p_3 k_B T)^2)^{-3/4}$ $\chi^2/ndf = 1.11/3$	$p_1 = (-0.917 \pm 0.54) \times 10^{10} \text{ s}^{-1}$ $p_2 = (18.6 \pm 1.2) \times 10^{10} \text{ s}^{-1}$ $p_3 = (17.2 \pm 2.8) \text{ eV}^{-1}$
D	$\lambda_{pO}(E; p) = (p_1 + p_2 E) \exp(-p_3 E)$ $\Lambda_{pO}(T; p) = p_1 \left(1 + \left(p_3 + \frac{2p_2}{2p_1}\right) k_B T\right) (1 + p_3 k_B T)^{-5/2}$ $\chi^2/ndf = 1.23/3$	$p_1 = (-1.8 \pm 0.95) \times 10^{10} \text{ s}^{-1}$ $p_2 = (4.4 \pm 0.94) \times 10^{12} \text{ s}^{-1} \text{ eV}^{-1}$ $p_3 = (9.22 \pm 3.24) \text{ eV}^{-1}$
E	$\lambda_{pO}(E; p) = p_1 + p_2 \sqrt{E}$ $\Lambda_{pO}(T; p) = p_1 + 2p_2 \sqrt{k_B T/\pi}$ $\chi^2/ndf = 2.11/4$	$p_1 = (-4.62 \pm 0.36) \times 10^{10} \text{ s}^{-1}$ $p_2 = (74.1 \pm 2.5) \times 10^{10} \text{ s}^{-1} \text{ eV}^{-1/2}$



Transfer rate up to 120 meV



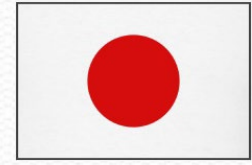
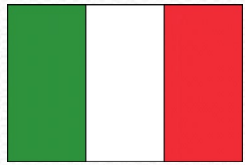
~100 K

~300 K

μp energy after de-excitation

<http://arxiv.org/abs/1905.02049>

FAMU Collaboration



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Thanks!