

The Jülich-Bonn coupled-channel model and the Λ decay parameter α_{Λ}

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Jefferson Lab

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[several slides by
D. Rönchen and M. Mai]

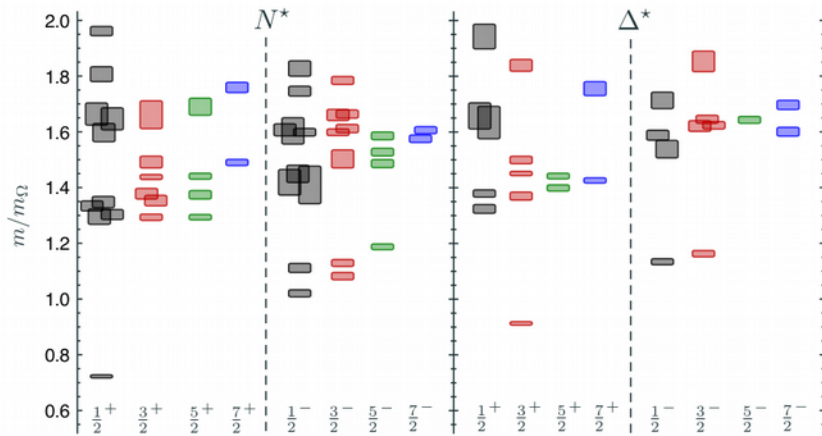
Degrees of freedom: Quarks or hadrons?

The Missing Resonance Problem

- above 1.8 GeV much more states are predicted than observed,

“Missing resonance problem”

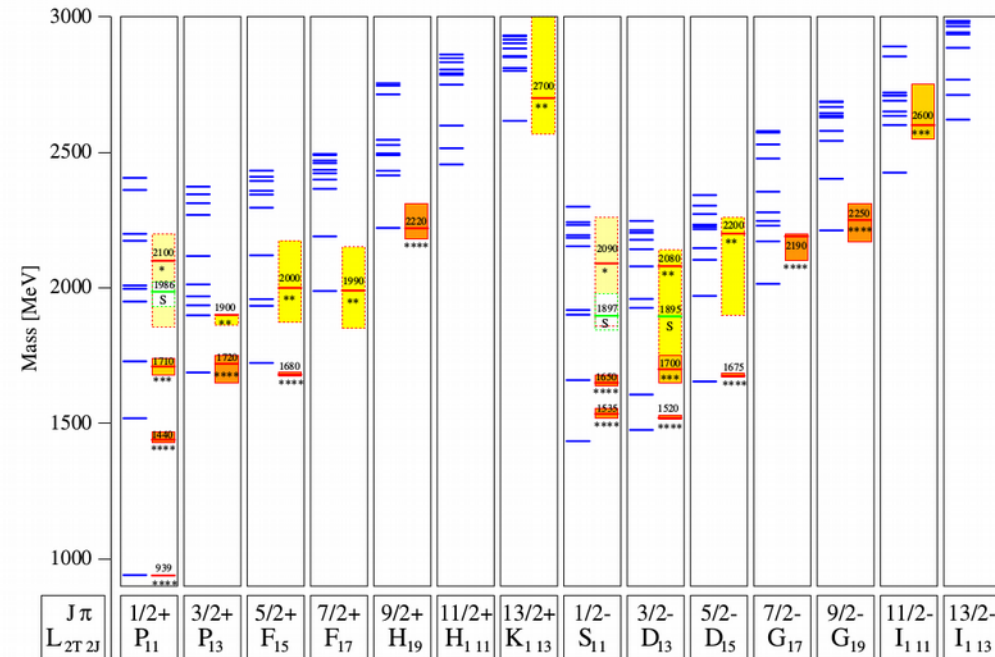
Lattice calculation (single hadron approximation):



[Edwards *et al.*, Phys.Rev. D84 (2011)]

- only 15 established N^* states (PDG 2015)
- $\sim 48\%$ of the states have **** or *** status (PDG 1982: 58% with **** or ***)

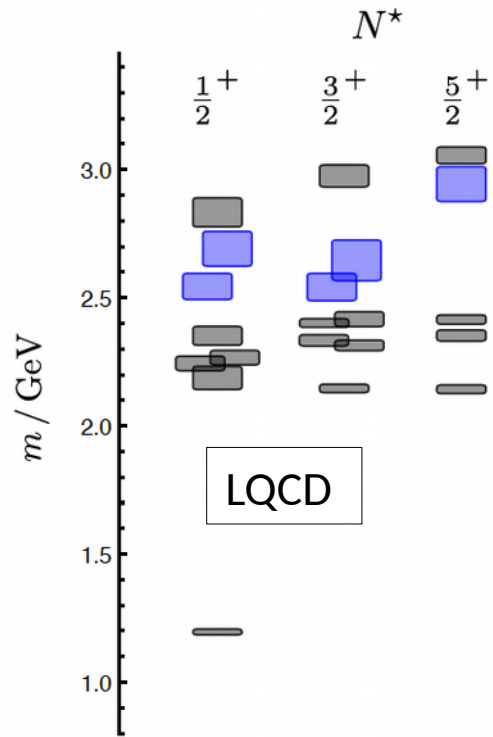
N^* spectrum in a relativistic quark model:



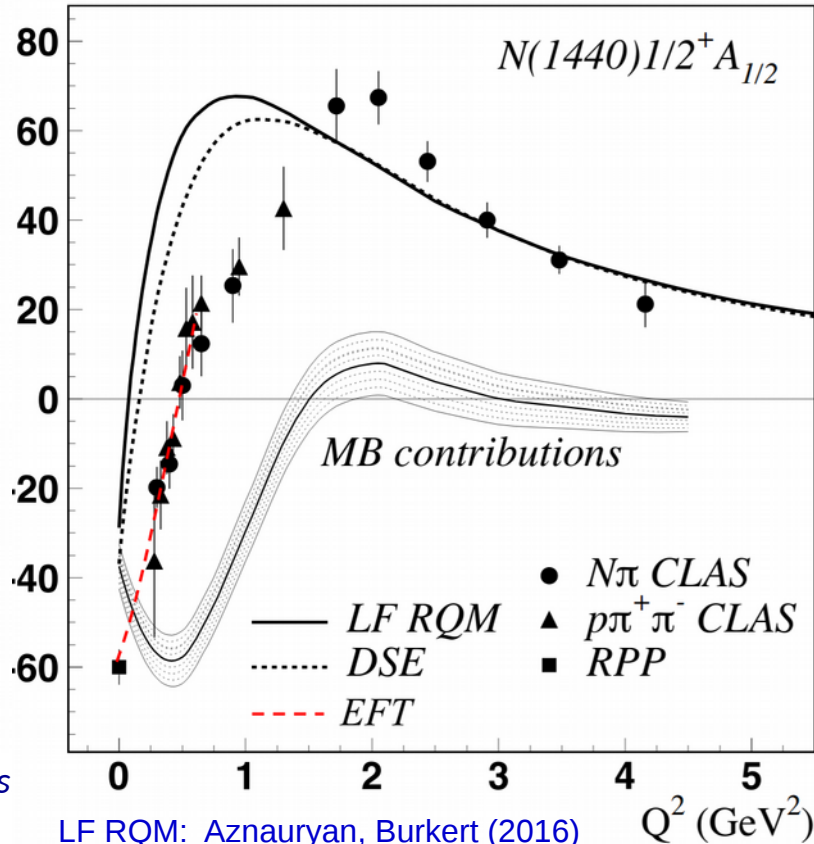
Löring *et al.* EPJ A 10, 395 (2001), experimental spectrum: PDG 2000

Overviews: Crede, Roberts, Rep. Prog. Phys. 76 (2013)
Aznauryan *et al.*, Int. J. Mod. Phys. E 22 (2013)

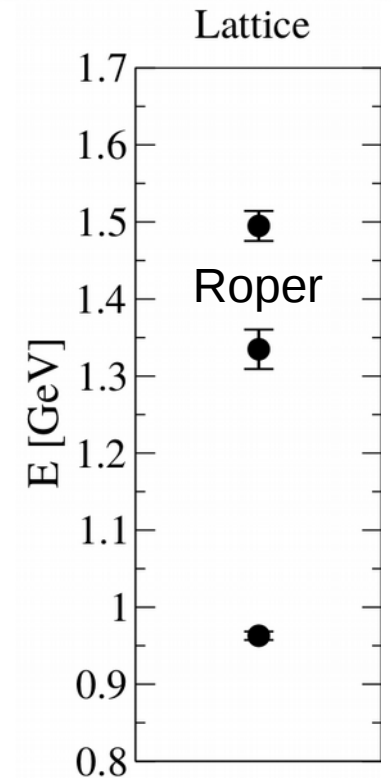
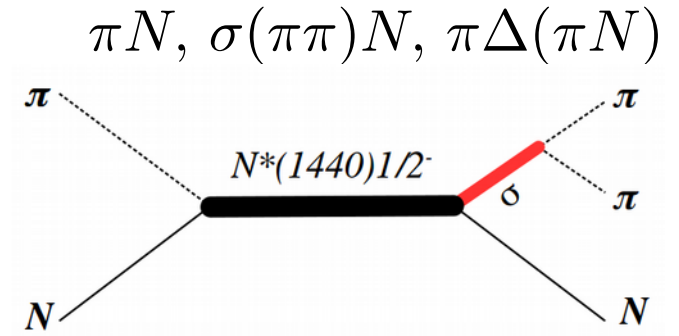
Hybrid Baryons



J.J. Dudek and R.G. Edwards
PRD85 (2012)



LF RQM: Aznauryan, Burkert (2016)
DSE: Segovia, Roberts, PRC (2016)
EFT: Bauer, Scherer, Tiator, PRC (2014)



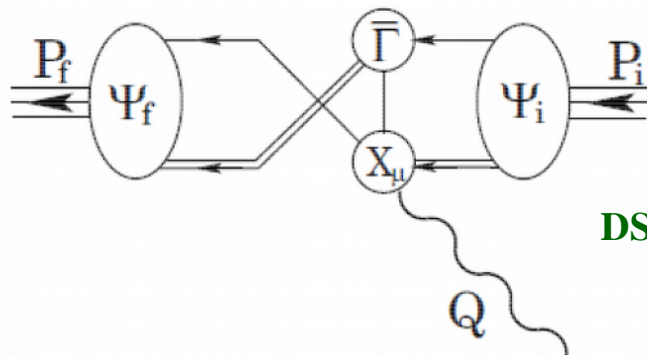
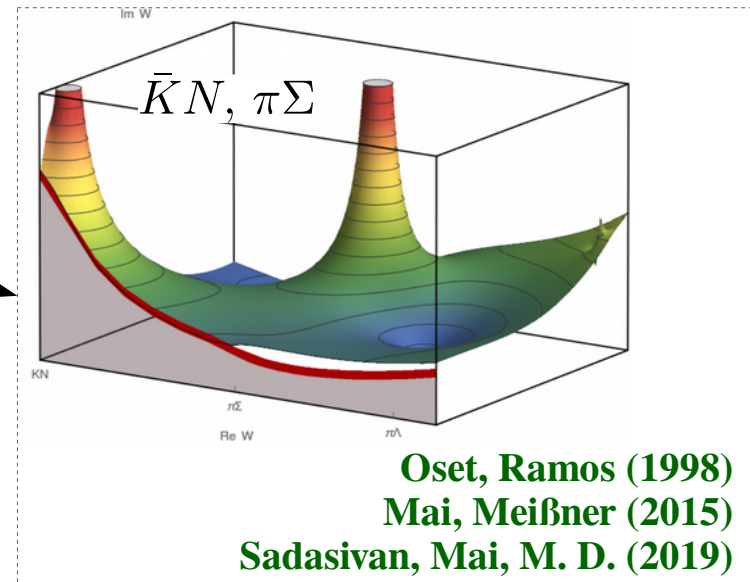
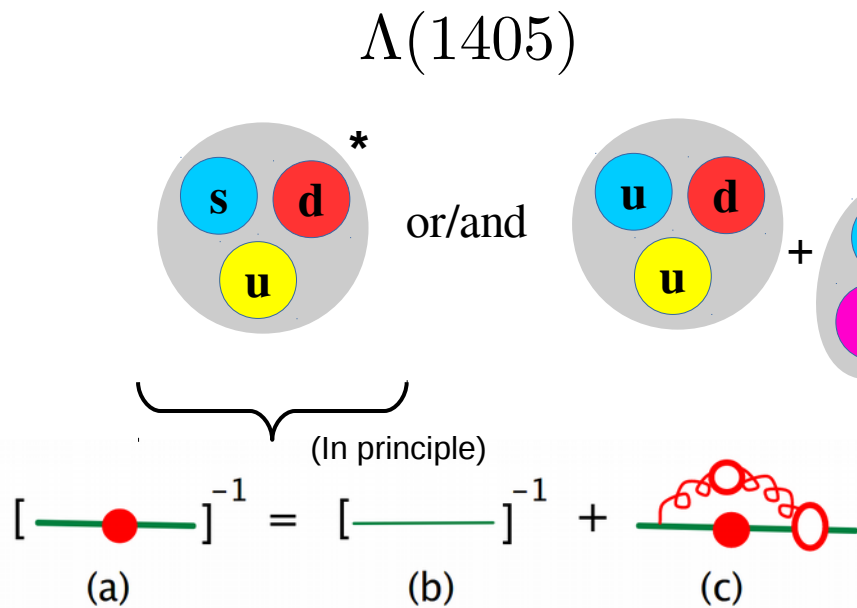
Data: [Lang et al., Phys.Rev. D95 (2017), 014510]

Hybrid states: same J^P values as q^3 baryons.
Identification? Measure Q^2 dependence of
electro-couplings (**CLAS 12**)

[parts of slide courtesy of V. Burkert]

- **QCD** at low energies
- Non-perturbative dynamics
 - Q1:** how many are there?
 - Q2:** what are they?

- *mass generation & confinement*
- rich spectrum of excited states
(missing resonance problem)
(2-quark/3-quark, hadron molecules, exotics,...)



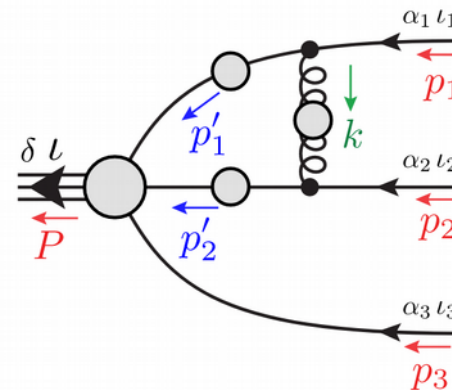
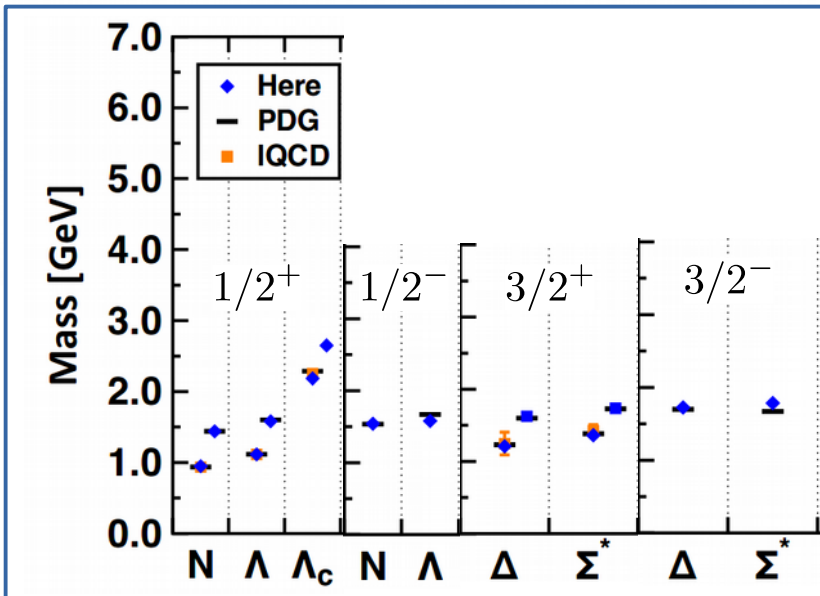
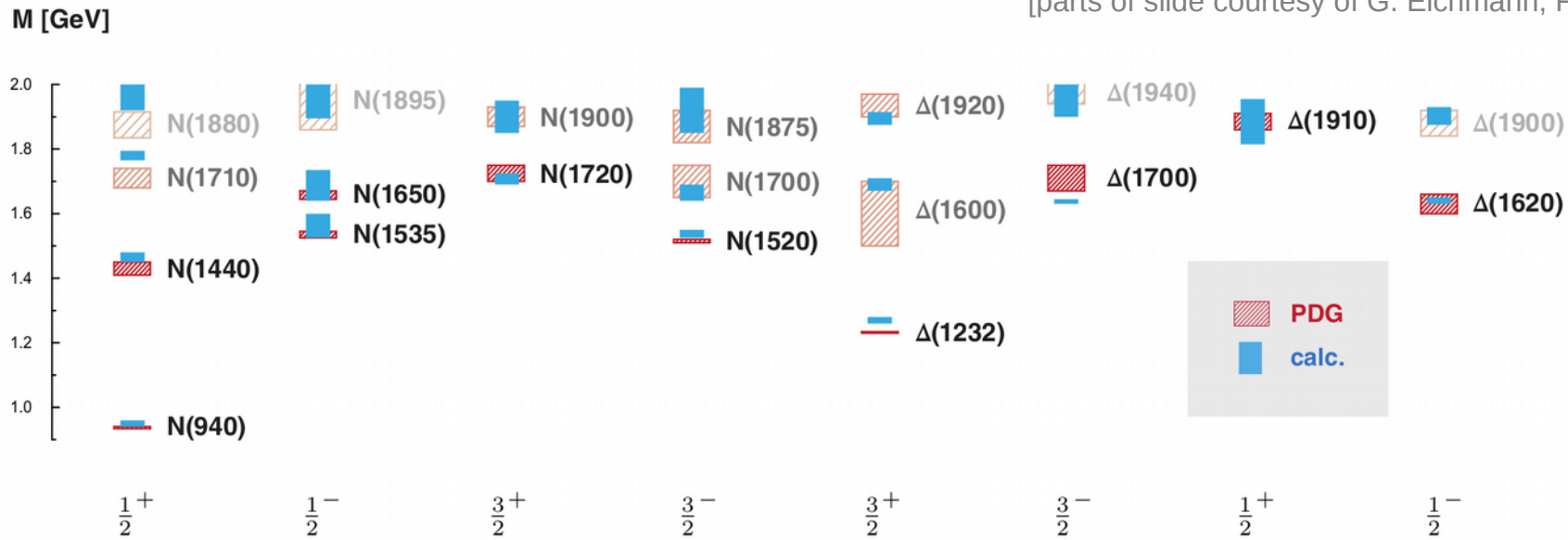
DSE (Wilson, Cloet, Chang, Roberts)

Talks on Thursday by
Maxim Mai and Daniel
Sadasivan

New results in dynamical quark picture

Quark-diquark with reduced pseudoscalar + vector diquarks: [GE, Fischer, Sanchis-Alepuz, PRD 94 \(2016\)](#)

[parts of slide courtesy of G. Eichmann, Few Body 2018]

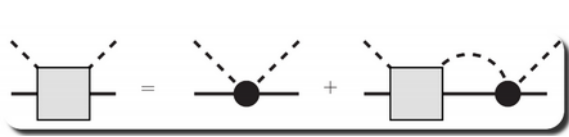


Poincaré-covariant analysis of heavy-quark baryons, Qin, Roberts, Schmidt, PRD (2018)
Spectrum of light- and heavy-baryons, Qin, Roberts, Schmidt, Few Body Syst. 60 (2019)

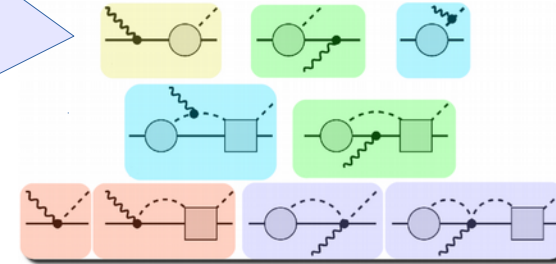
Using ONLY meson-baryon degrees of freedom (no explicit quark dynamics):

Manifestly gauge invariant approach based on full BSE solution

[Ruic, M. Mai, U.-G. Meissner PLB 704 (2011)]



Gauge invariance



Fit

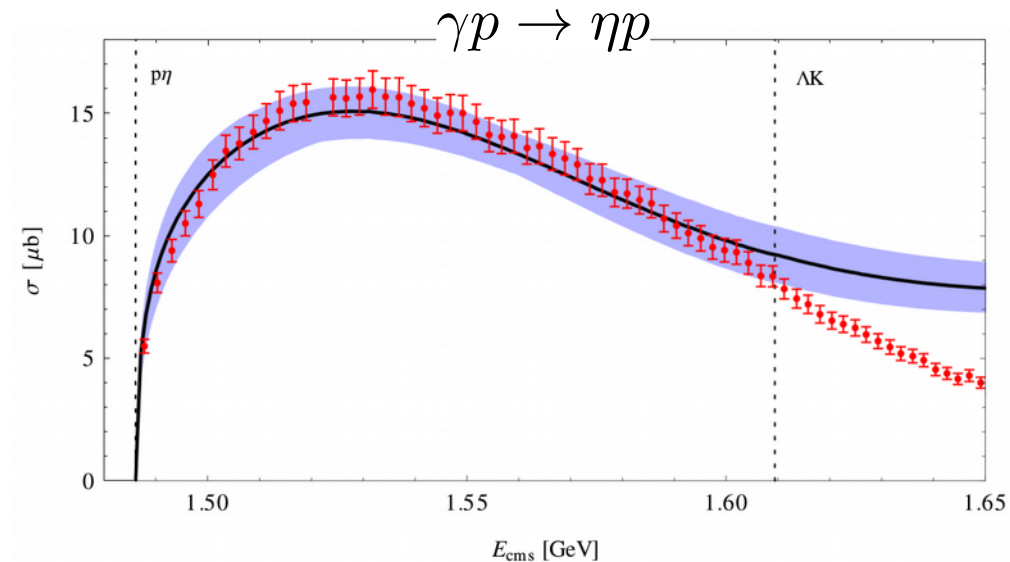
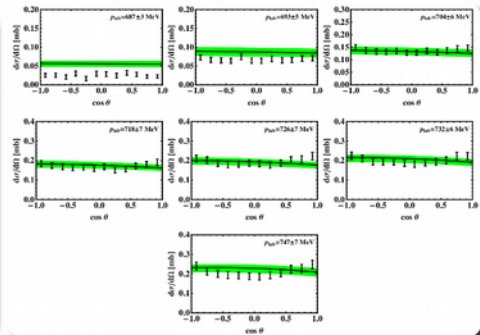
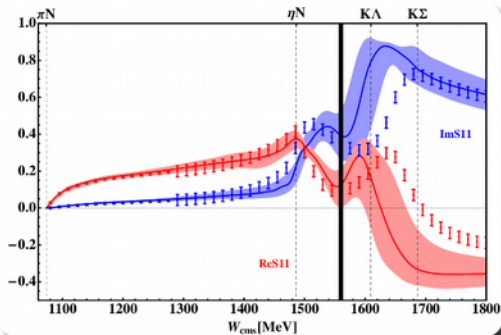
► Exact unitary meson-baryon scattering amplitude T with parameters, fixed to reproduce:

► πN -partial wave S_{11} and S_{31} for $\sqrt{s} < 1560$ MeV

Arndt et al. (2012)

► $\pi^- p \rightarrow \eta n$ differential cross sections

Prakhov et al. (2005)

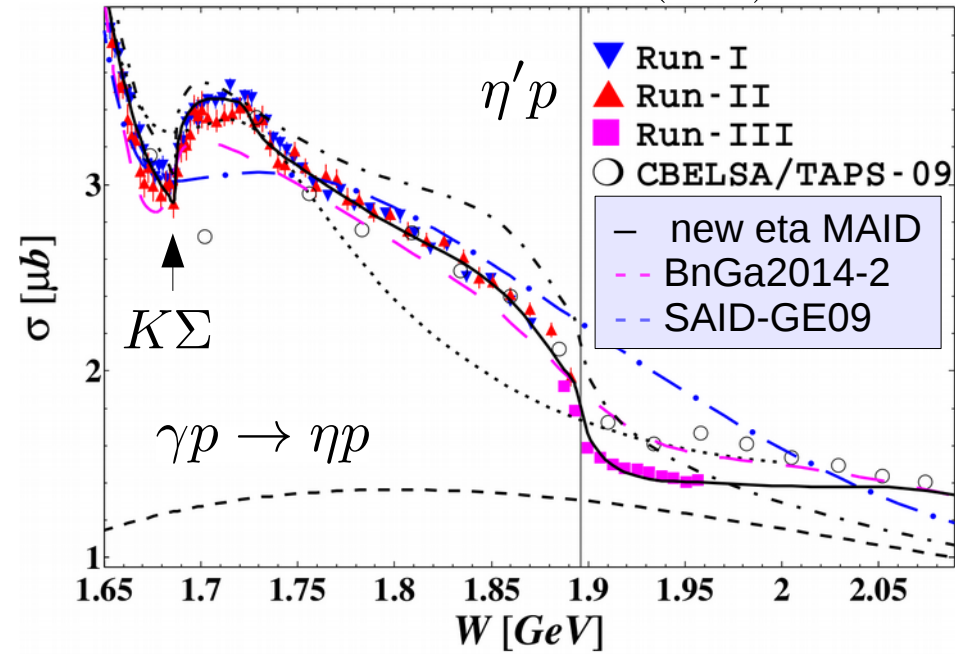


→ Making the “Missing resonance problem” worse ?!

Phenomenology

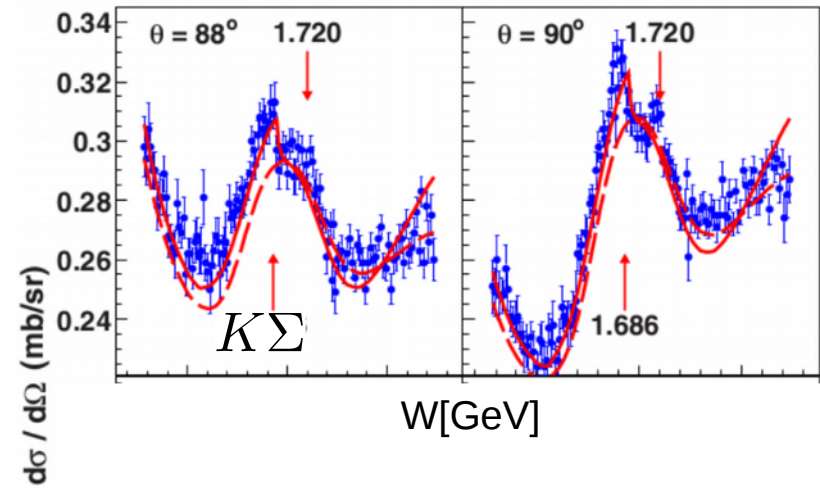
Resonances or not?

A2 MAMI, PRL 118 (2017) $S_{11}(1895)$

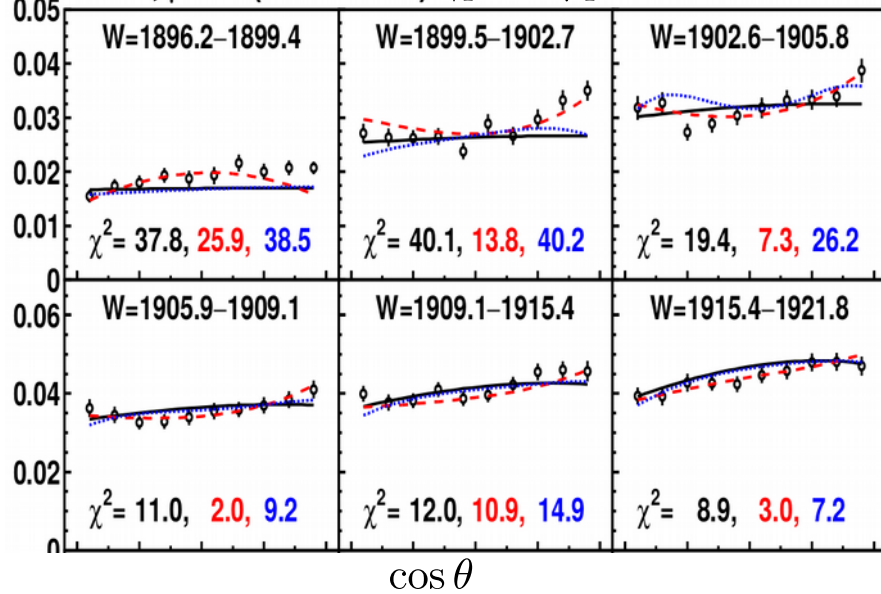


$\pi N \rightarrow \pi N$

EPECUR/SAID PRC 93 (2016)



$d\sigma/d\Omega, \mu\text{b/sr}$ (MAMI 2017) $\gamma p \rightarrow \eta' p$



BnGa
PLB785 (2018):

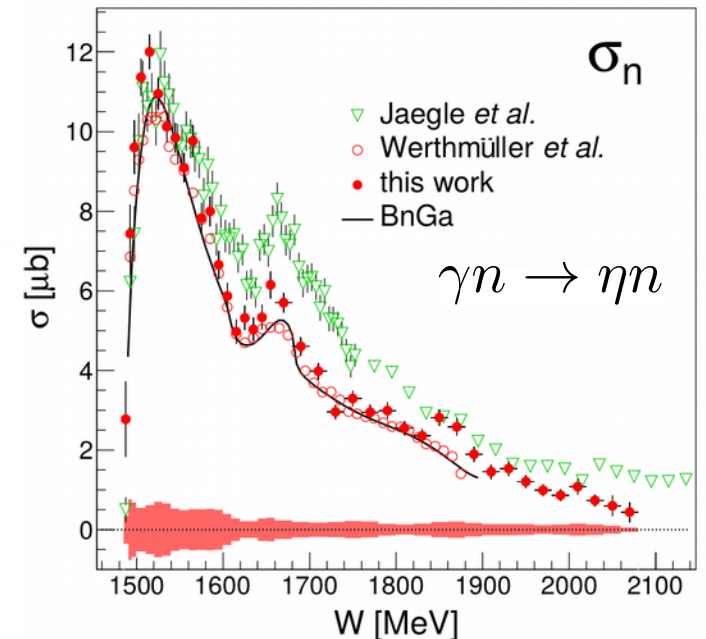
No narrow
resonance

$3/2^-$ narrow
Resonance

$5/2^-$ narrow
Resonance

Data: A2.Mami
PRL 118 (2017)

[CBELSA/TAPS EPJA 53 (2017)]



Current state in η photoproduction: Multipoles from different groups

From: **EtaMAID2018**
[Tiator et al., EPJA54 (2018)]
Analyzes:

$$\gamma p \rightarrow \eta p$$

$$\gamma p \rightarrow \eta' p$$

$$\gamma n \rightarrow \eta n$$

$$\gamma n \rightarrow \eta' n$$

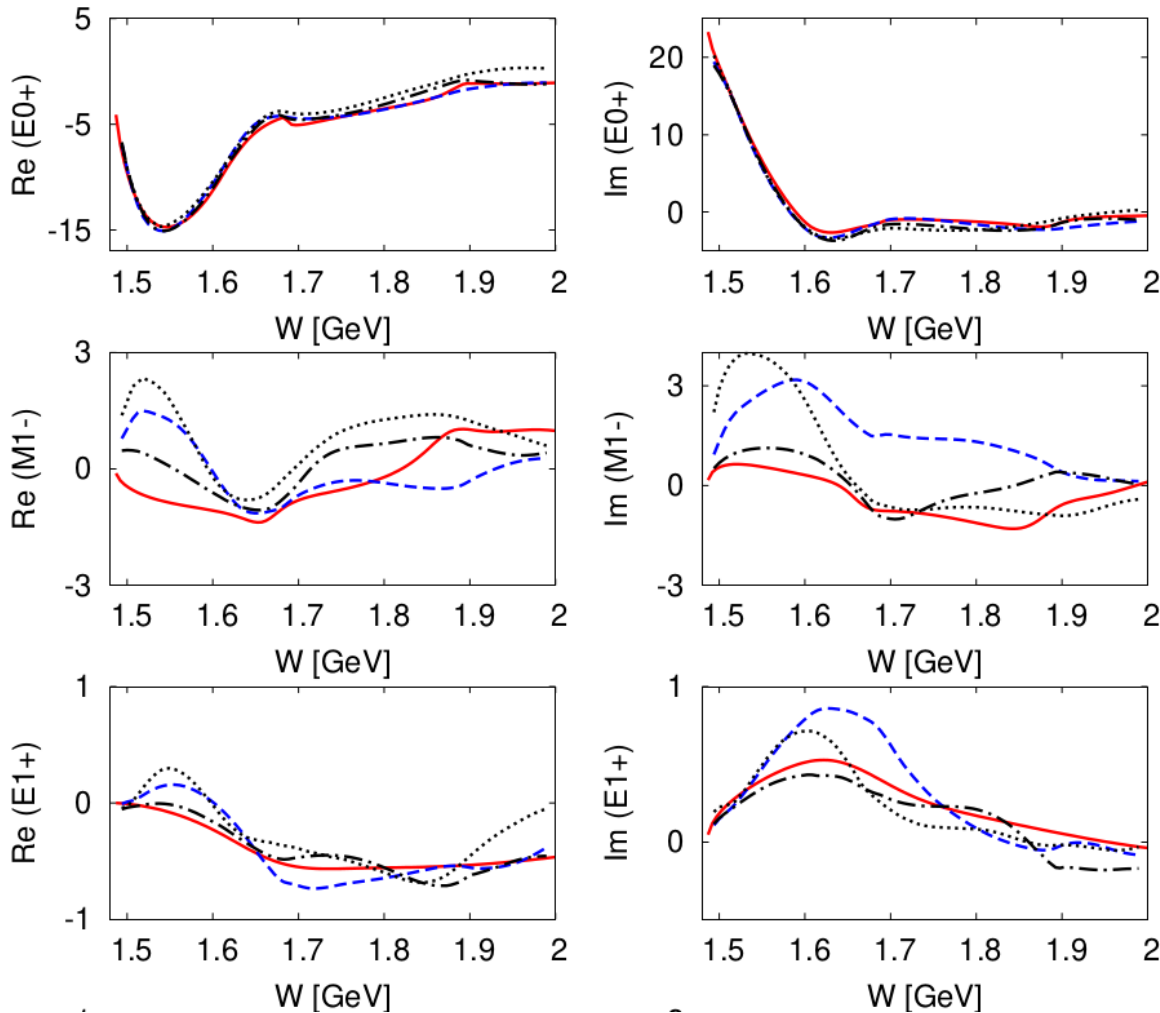
EtaMAID2018

BnGa [PLB 772 (2017)]

JuBo (dotted) [EPJA 54 (2018)]

KSU [1804.06031]

Review: Krusche, Wilkins,
[Prog.Part.Nucl.Phys. 80 (2014)]



Observable	σ	Σ	T	P	E	F	G	H	T_x	T_z	L_x	L_z	O_x	O_z	C_x	C_z
$\rho\pi^0$	✓	✓	✓		✓	✓	✓	✓								
$\eta\pi^+$	✓	✓	✓		✓	✓	✓	✓								
$\rho\eta$	✓	✓	✓		✓	✓	✓	✓								
$\rho\eta'$	✓	✓	✓		✓	✓	✓	✓								
$K^+\Lambda$	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
$K^+\Sigma^0$	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
$\rho\omega/\phi$	✓	✓	✓		✓	✓	✓	✓	✓ SDME							
$K^{*+}\Lambda$	✓			✓					SDME							
$K^{0*}\Sigma^+$	✓	✓								✓	✓	SDME				
$\rho\pi^-$	✓	✓			✓	✓	✓									
$\rho\rho^-$	✓	✓			✓	✓	✓									
$K^-\Sigma^+$	✓	✓			✓	✓	✓									
$K^0\Lambda$	✓	✓	✓	✓	✓	✓	✓		✓	✓	✓	✓	✓	✓	✓	✓
$K^0\Sigma^0$	✓	✓	✓	✓	✓	✓	✓		✓	✓	✓	✓	✓	✓	✓	✓
$K^{0*}\Sigma^0$	✓	✓									✓	✓				

Phys.Lett. B771 (2017)
Phys.Lett. B755 (2016)



$\gamma p \rightarrow X$

$\gamma n \rightarrow X$

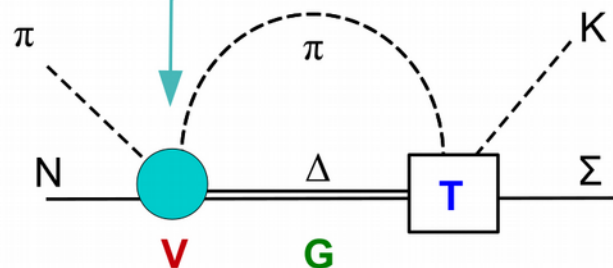
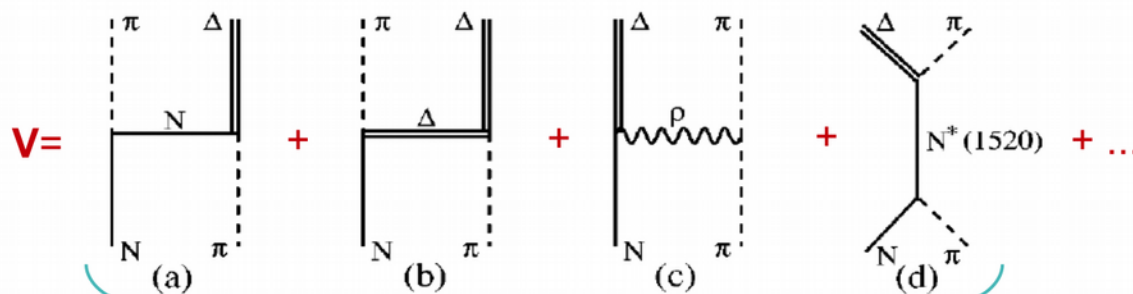
The Julich-Bonn Dynamical Coupled-Channel Approach

e.g. EPJ A 49, 44 (2013)

Dynamical coupled-channels (DCC): simultaneous analysis of different reactions

The scattering equation in partial-wave basis

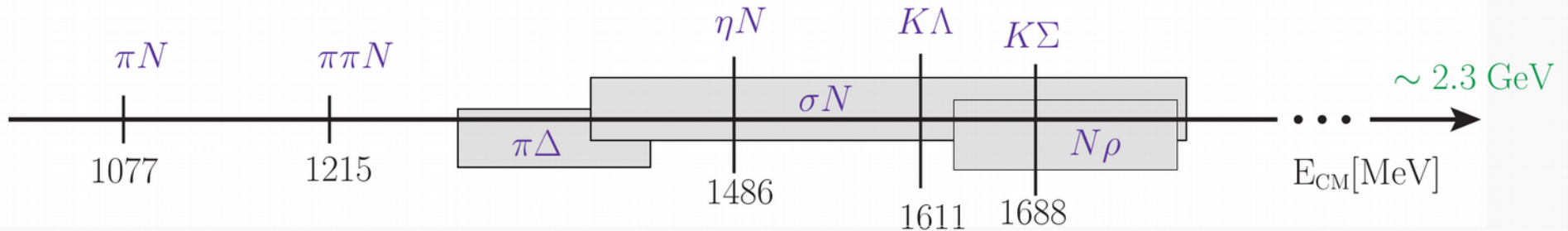
$$\langle L' S' p' | T_{\mu\nu}^{IJ} | L S p \rangle = \langle L' S' p' | V_{\mu\nu}^{IJ} | L S p \rangle + \sum_{\gamma, L'' S''} \int_0^\infty dq q^2 \langle L' S' p' | V_{\mu\gamma}^{IJ} | L'' S'' q \rangle \frac{1}{E - E_\gamma(q) + i\epsilon} \langle L'' S'' q | T_{\gamma\nu}^{IJ} | L S p \rangle$$



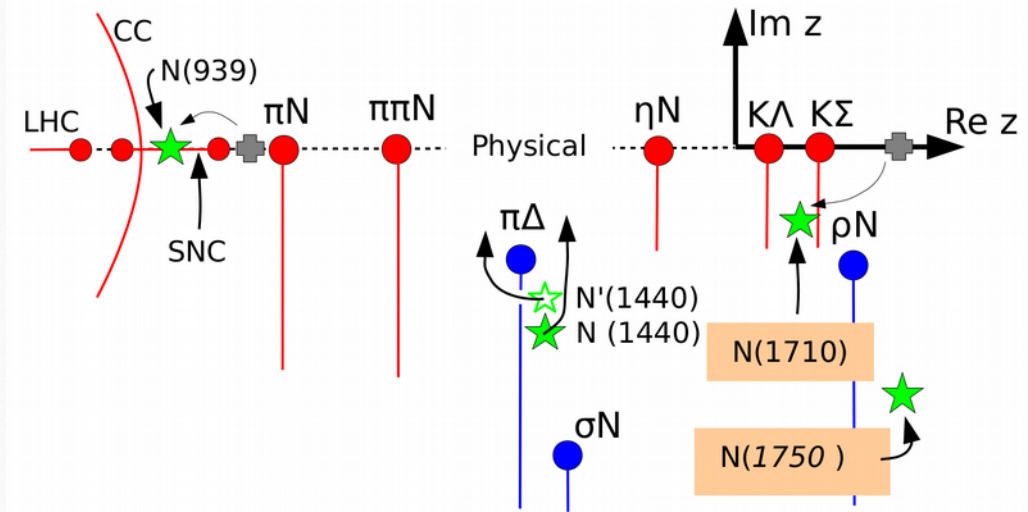
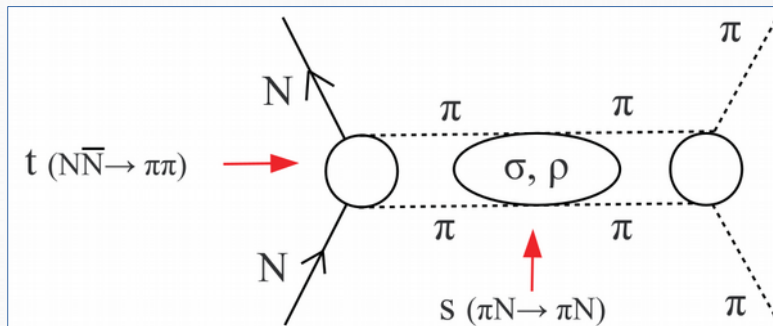
- potentials V constructed from effective \mathcal{L}
- s-channel diagrams: T^P
genuine resonance states
- t- and u-channel: T^{NP}
dynamical generation of poles
partial waves strongly correlated

JuBo: Channels and Analytic Structure

Channels included:



- (2-body) unitarity and analyticity respected
 - 3-body $\pi\pi N$ channel:
 - parameterized effectively as $\pi\Delta$, σN , ρN
 - $\pi N/\pi\pi$ subsystems fit the respective phase shifts
- ↳ branch points move into complex plane



JuBo: Data base

[D. Roenchen, M. D., U.-G. Meißner, EPJ A 54, 110 (2018)]

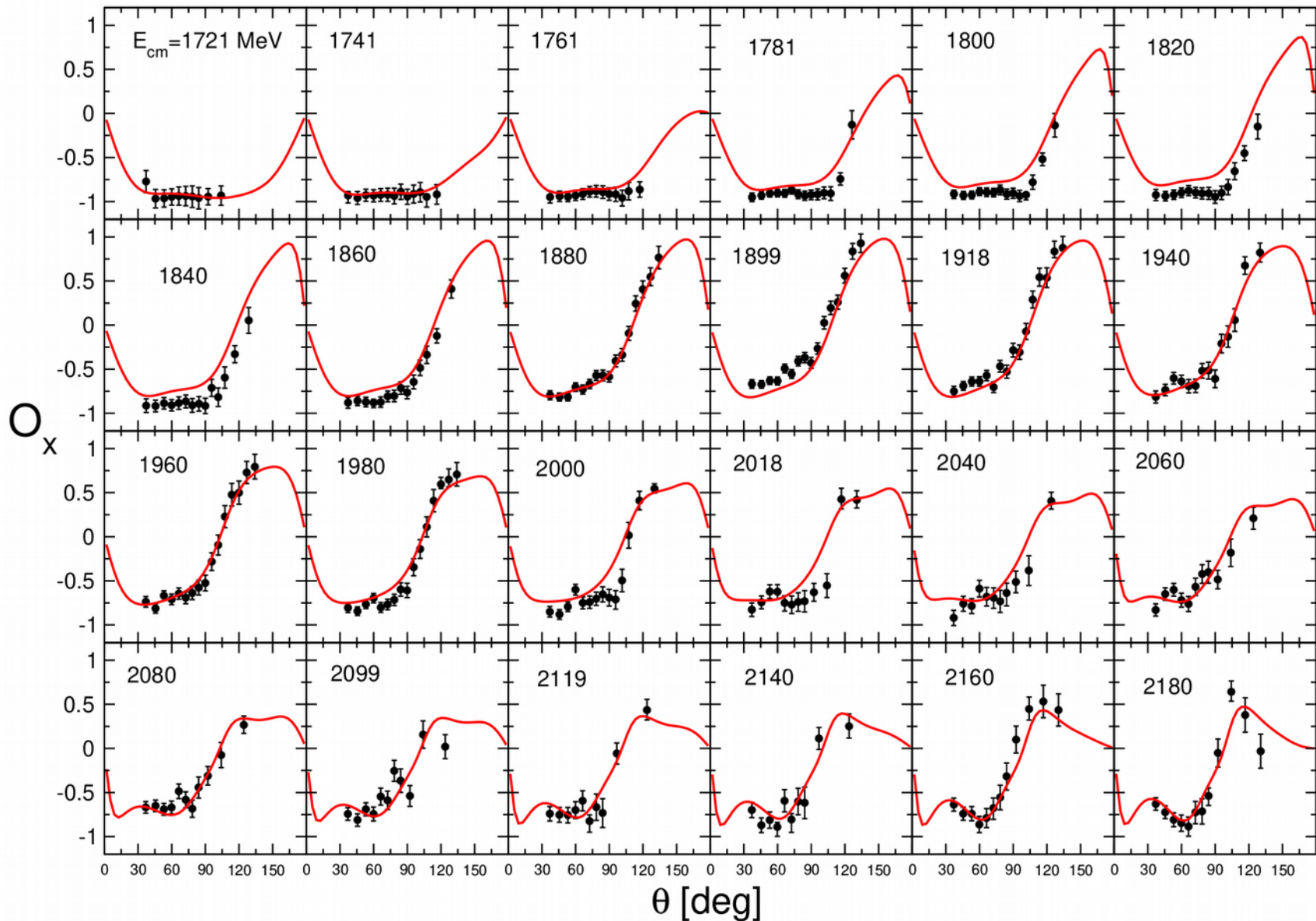
- $\pi N \rightarrow X$: > 7,000 data points ($\pi N \rightarrow \pi N$: GW-SAID WI08 (ED solution))
- $\gamma N \rightarrow X$:

Reaction	Observables (# data points)	p./channel
$\gamma p \rightarrow \pi^0 p$	$d\sigma/d\Omega$ (18721), Σ (2927), P (768), T (1404), $\Delta\sigma_{31}$ (140), G (393), H (225), E (467), F (397), $C_{x'}$ (74), $C_{z'}$ (26)	25,542
$\gamma p \rightarrow \pi^+ n$	$d\sigma/d\Omega$ (5961), Σ (1456), P (265), T (718), $\Delta\sigma_{31}$ (231), G (86), H (128), E (903)	9,748
$\gamma p \rightarrow \eta p$	$d\sigma/d\Omega$ (9112), Σ (403), P (7), T (144), F (144), E (129)	9,939
$\gamma p \rightarrow K^+ \Lambda$	$d\sigma/d\Omega$ (2478), P (1612), Σ (459), T (383), $C_{x'}$ (121), $C_{z'}$ (123), $O_{x'}$ (66), $O_{z'}$ (66), O_x (314), O_z (314),	5,936
$\gamma p \rightarrow K^+ \Sigma^0$	$d\sigma/d\Omega$ (4271), P (422), Σ (280), T (127), $C_{x',z'}$ (188), $O_{x,z}$ (254)	5,542
$\gamma p \rightarrow K^0 \Sigma^+$	$d\sigma/d\Omega$ (242), P (78)	320
	in total	57,027

Selected Fit Results (I)

● $\gamma p \rightarrow K^+ \Lambda$:

<http://collaborations.fz-juelich.de/ikp/meson-baryon/main>

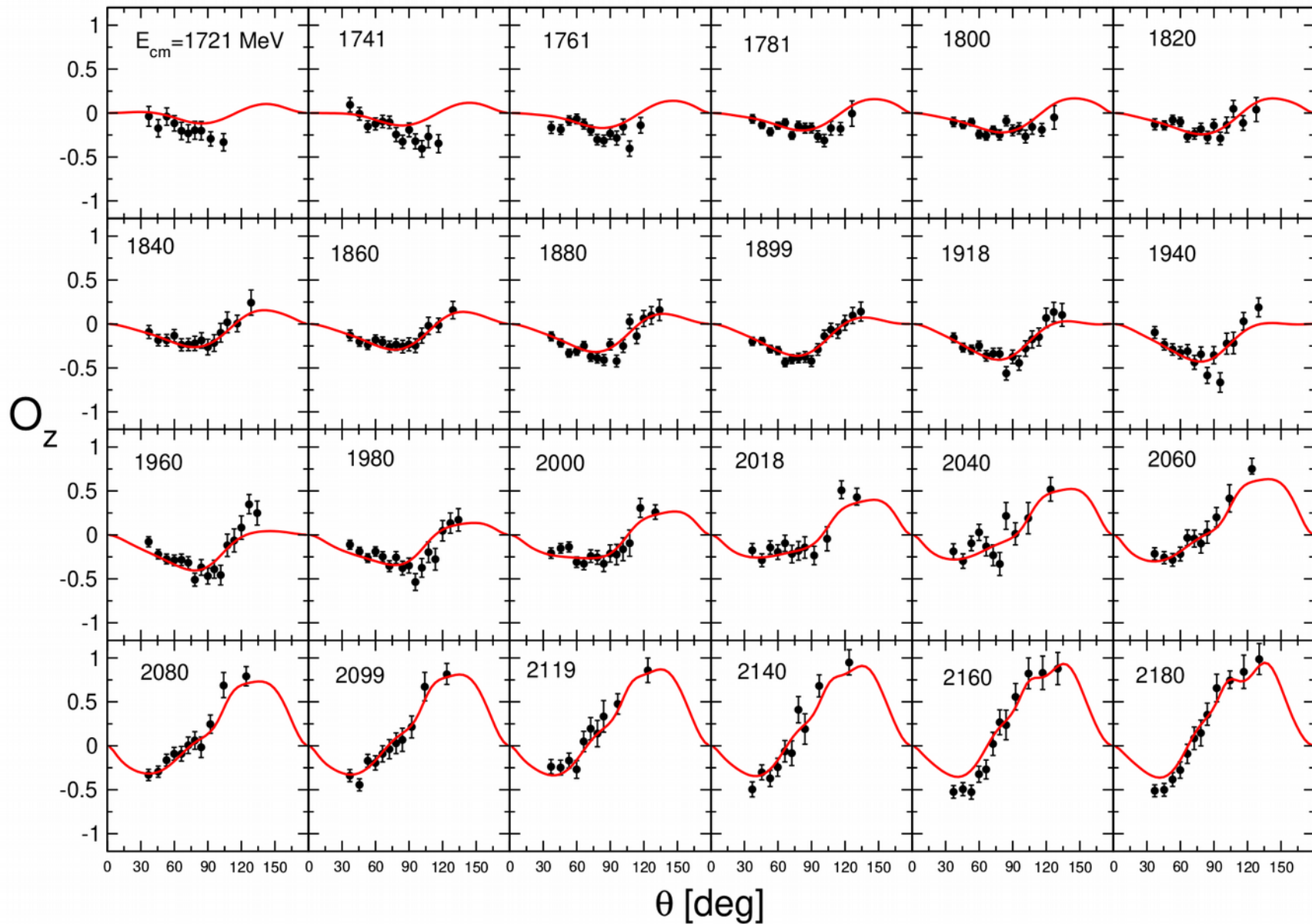


data: Paterson (CLAS) PRC 93, 065201 (2016), red line: fit JüBo2019

Selected Fit Results (II)

● $\gamma p \rightarrow K^+ \Lambda$:

<http://collaborations.fz-juelich.de/ikp/meson-baryon/main>

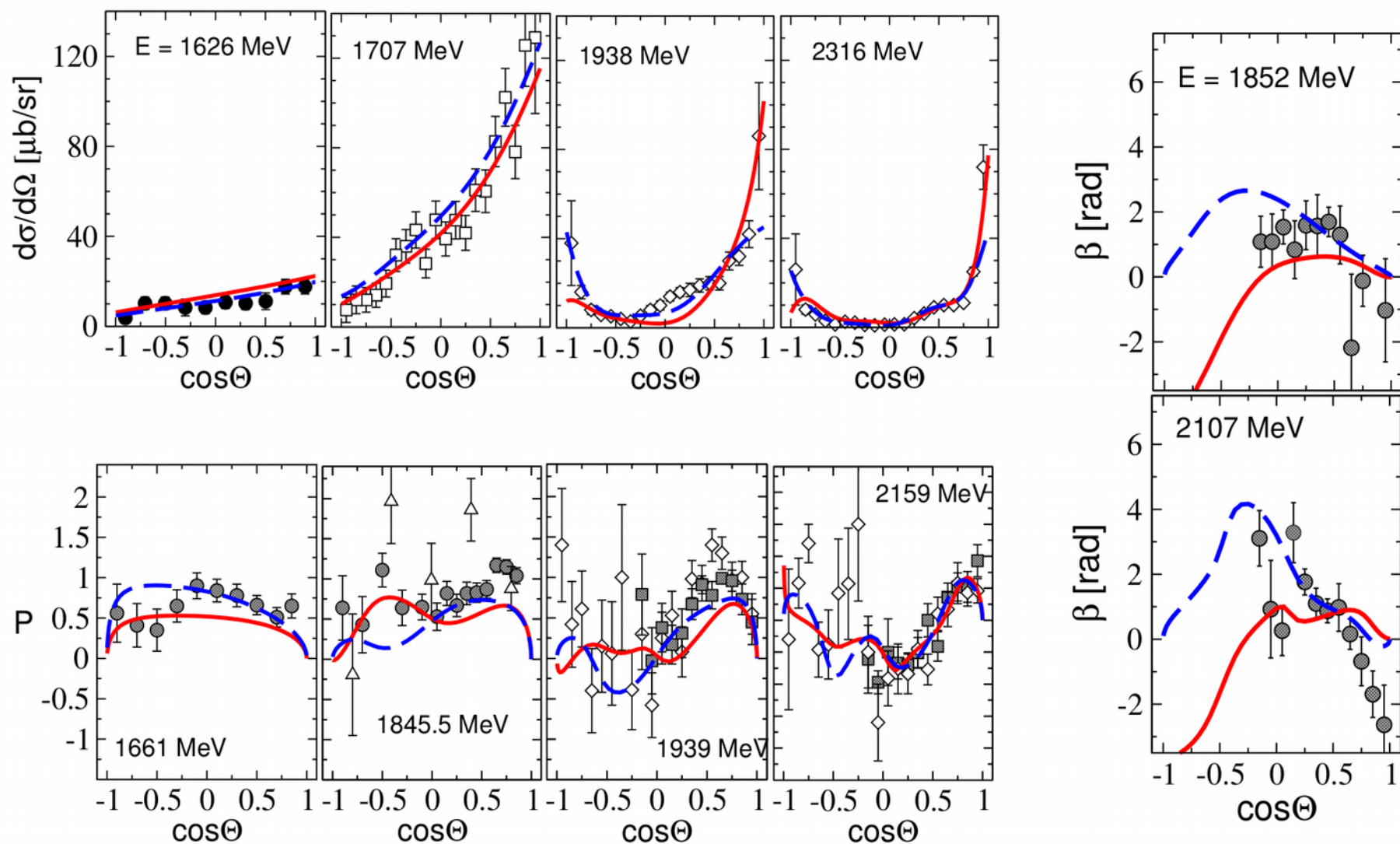


data: Paterson (CLAS) PRC 93, 065201 (2016), red line: fit JüBo2019

Fit to world data on $\pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$ ($\sim 10^5$ exp. points)

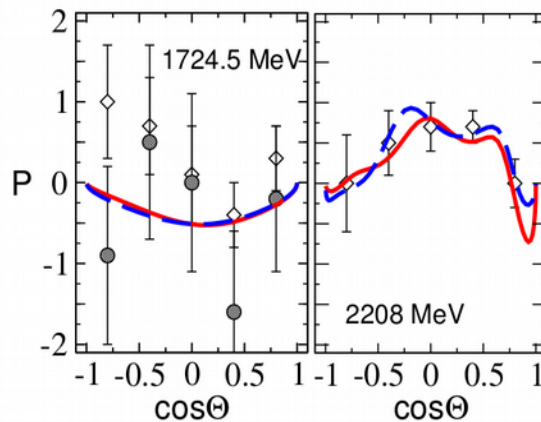
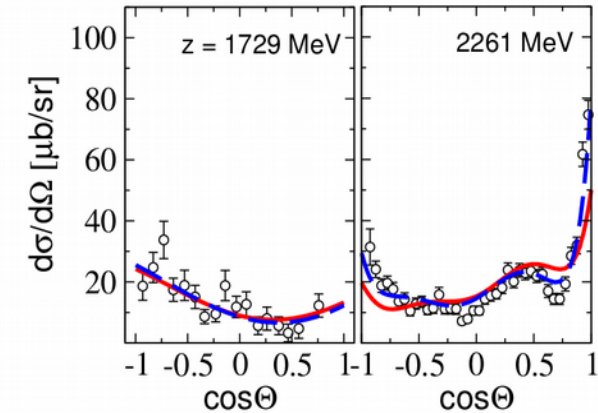
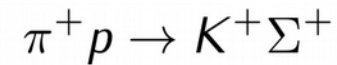
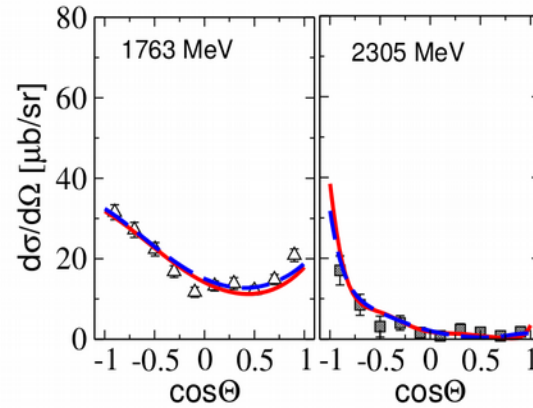
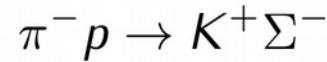
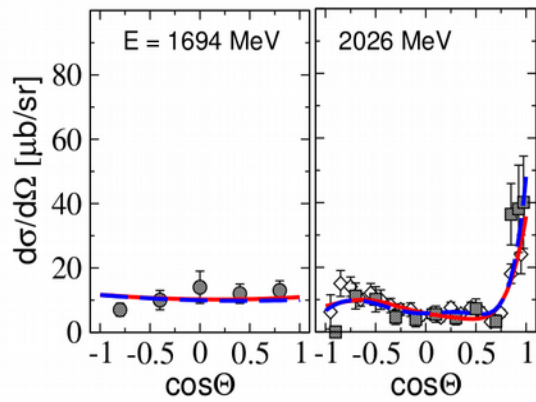
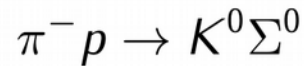
[Rönchen, M.D. *et al.*, EPJA 49 (2013)]

Selected results for $\pi^- p \rightarrow K^0 \Lambda$ [almost complete experiment]

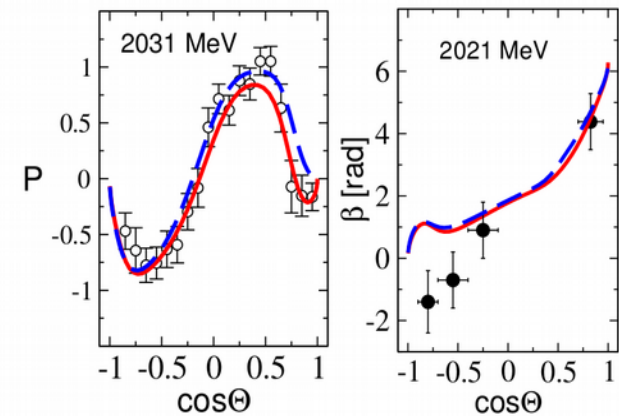


Re-measuring hadron-induced reactions

Fits: D. Rönchen, M.D., et al., EPJ A**49** (2013)



No polarization data!



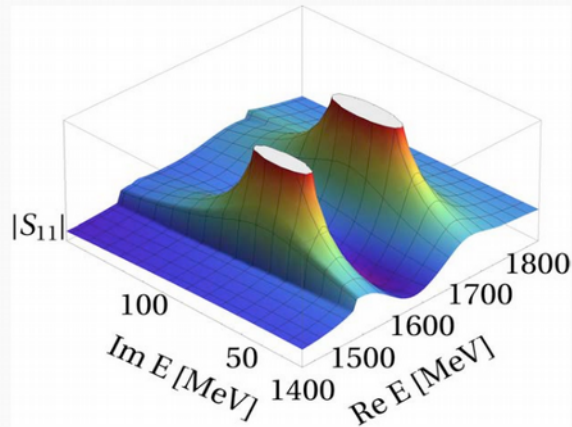
→ *Physics Opportunities with meson beams,*

Briscoe, M.D., Haberzettl, Manley, Naruki, Strakovsky, Swanson, EPJ A**51** (2015)

→ **J-PARC E45**

Resonance Couplings

Resonance states: Poles in the T -matrix on the 2nd Riemann sheet



- $\text{Re}(E_0)$ = “mass”, $-2\text{Im}(E_0)$ = “width”
- elastic πN residue ($|r_{\pi N}|, \theta_{\pi N \rightarrow \pi N}$), normalized residues for inelastic channels ($\sqrt{\Gamma_{\pi N} \Gamma_{\mu}} / \Gamma_{\text{tot}}, \theta_{\pi N \rightarrow \mu}$)
- photocouplings at the pole: $\tilde{A}_{\text{pole}}^h = A_{\text{pole}}^h e^{i\vartheta^h}$, $h = 1/2, 3/2$

Inclusion of $\gamma p \rightarrow K^+ \Lambda$ in JüBo (“JuBo2017-1”): 3 additional states

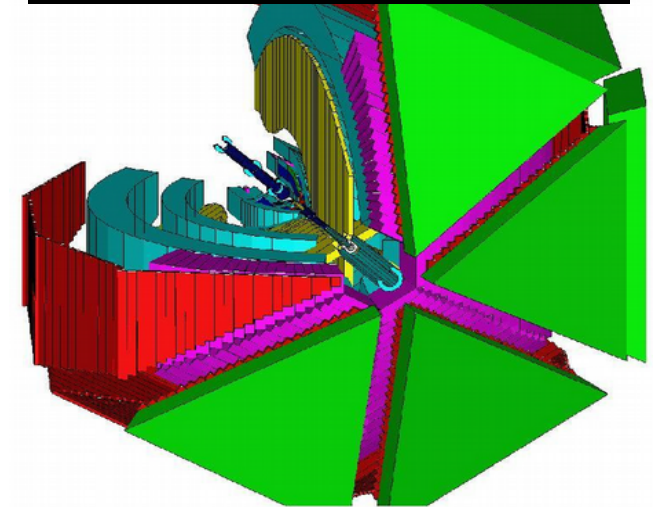
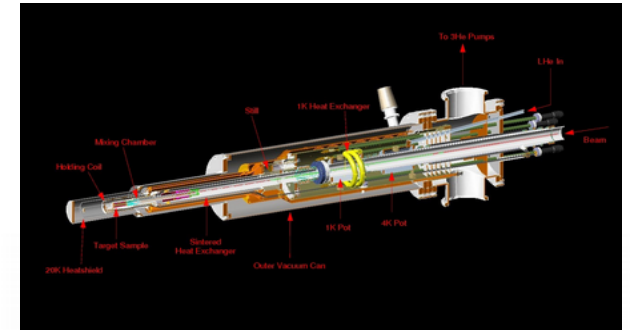
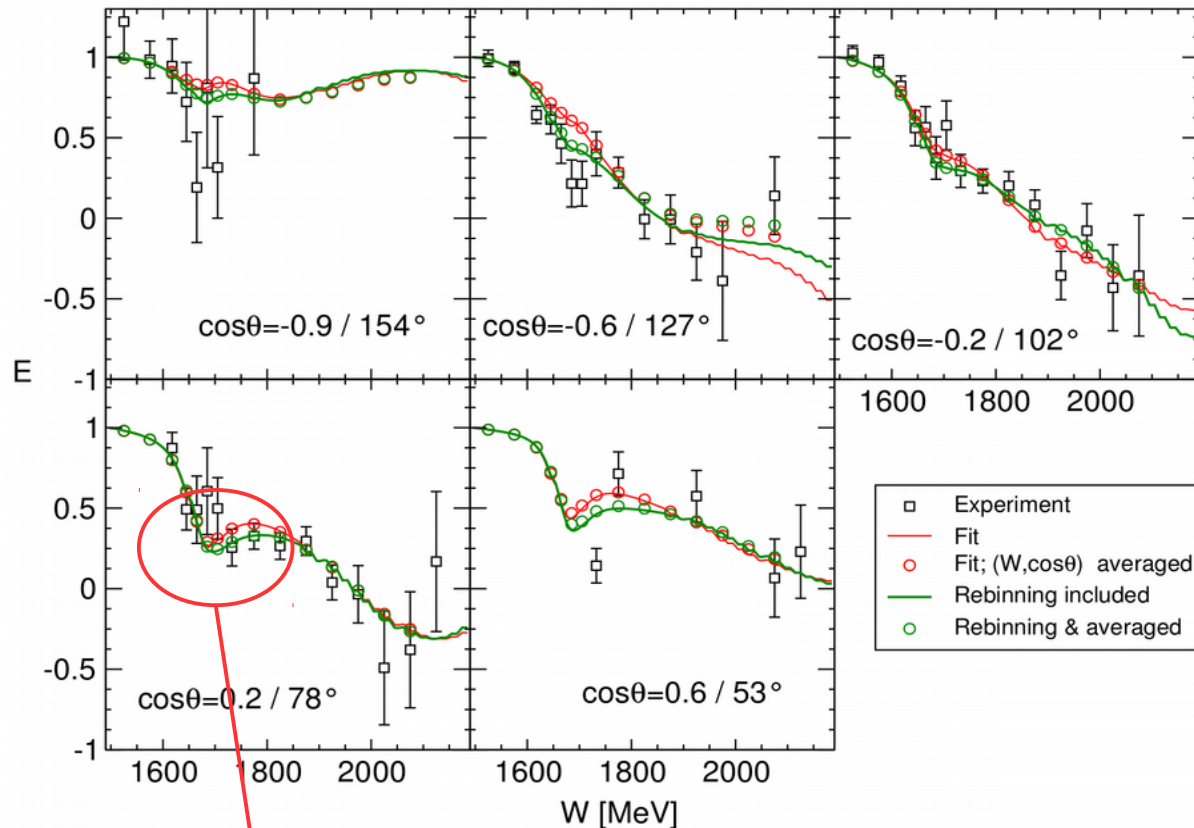
	z_0 [MeV]	$\frac{\Gamma_{\pi N}}{\Gamma_{\text{tot}}}$	$\frac{\Gamma_{\eta N}}{\Gamma_{\text{tot}}}$	$\frac{\Gamma_{K\Lambda}}{\Gamma_{\text{tot}}}$	$\frac{\Gamma_{K\Sigma}}{\Gamma_{\text{tot}}}$
N(1900)3/2 ⁺	1923 – i 108.4	1.5 %	0.78 %	2.99 %	69.5 %
N(2060)5/2 ⁻	1924 – i 100.4	0.35 %	0.15 %	13.47 %	27.02 %
$\Delta(2190)$ 1/2 ⁺	2191 – i 103.0	33.12 %			3.78 %

- N(1900)3/2⁺: s-channel resonances, seen in many other analyses of kaon photoproduction (BnGa), 3 stars in PDG
- N(2060)5/2⁻: dynamically generated, 2 stars in PDG, seen e.g. by BnGa
- $\Delta(2190)$ 1/2⁺: dyn. gen., no equivalent PDG state

Resonances and other structures

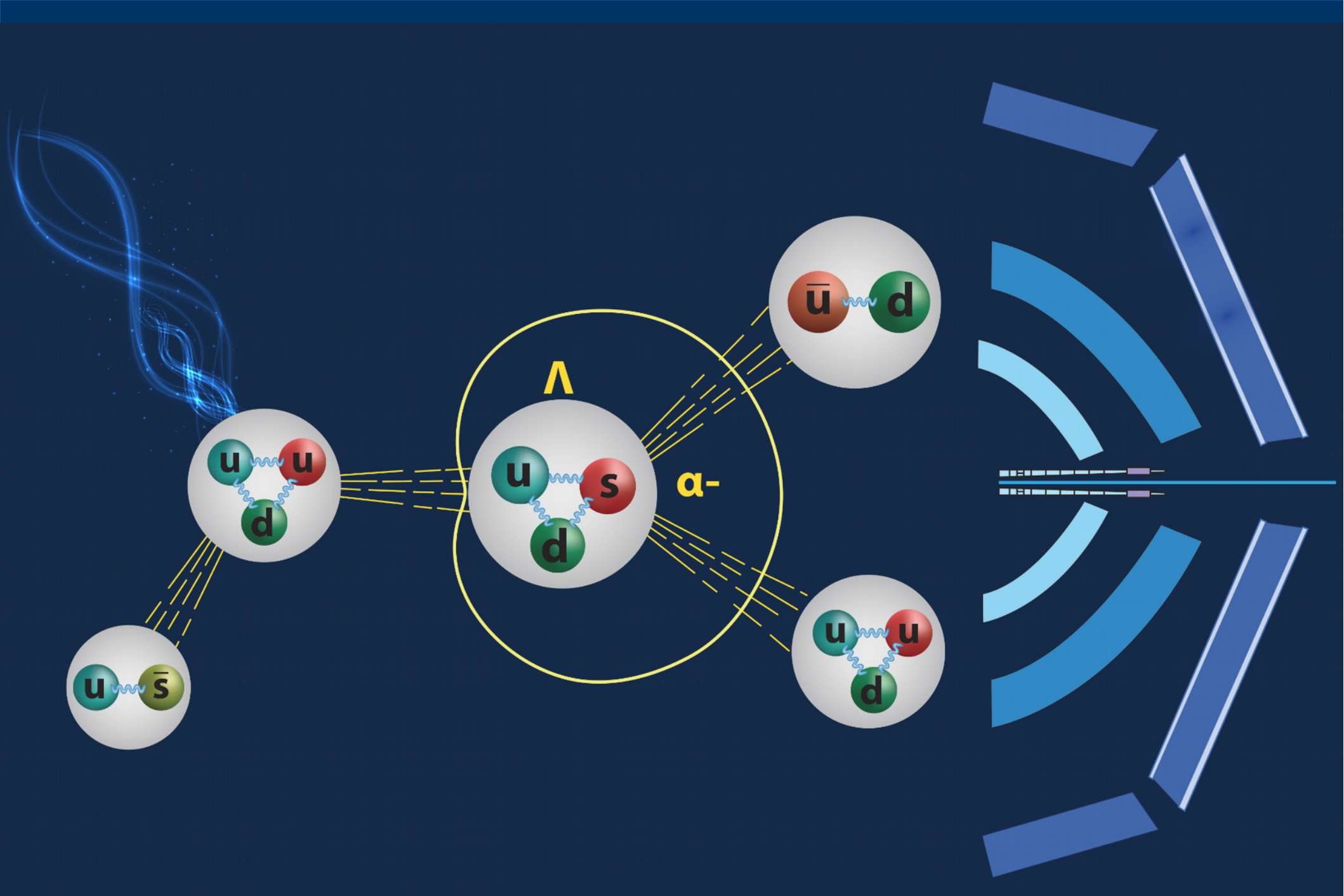
CLAS/JuBo (M. D., D. Rönchen), Phys.Lett. B755 (2016)

- First-ever measurement of observable E in η photo-production, enabled through the CLAS FROST target



Is this a new narrow baryonic resonance?

- Conventional explanation in terms of interference effects.
- Systematic elimination of resonance through model selection
- Talk by K. Nakayama on Friday [PRD99 (2019)]



● Λ decays weakly to $p\pi^+$

● The decay parameter: α_-

- essential for many modern experiments

e.g. LEAR@CERN, STAR@BNL, ATLAS@CERN

- affects decay parameters of other hyperons

e.g. Trippe et al. (1967), Bono et al. (CLAS) (2018)

Ω^- DECAY PARAMETERS	
$\alpha(\Omega^-) \alpha_-(\Lambda)$ FOR $\Omega^- \rightarrow \Lambda K^-$	
Some early results have been omitted.	
VALUE	EVTS
0.0115 ± 0.0015	OUR AVERAGE

Ξ^0 DECAY PARAMETERS	
See the "Note on Baryon Decay Parameters" in	
$\alpha(\Xi^0) \alpha_-(\Lambda)$	
This is a product of the $\Xi^0 \rightarrow \Lambda \pi^0$ and $\Lambda \rightarrow p \pi^-$ as)	
VALUE	EVTS
-0.261 ± 0.006	OUR AVERAGE

PDG live (2019)

- impacts LO parameters of SU(3) baryon ChPT

Holstein (2000)

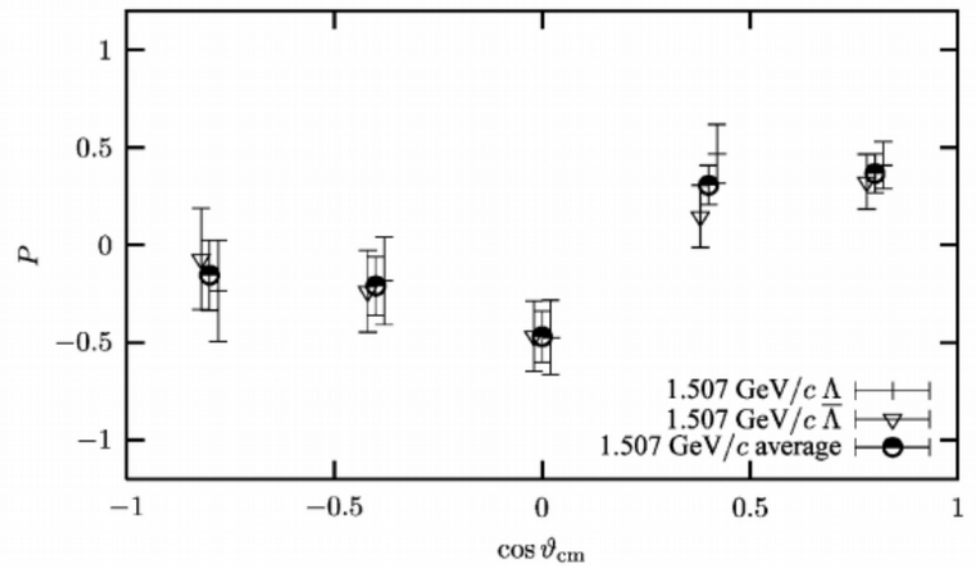
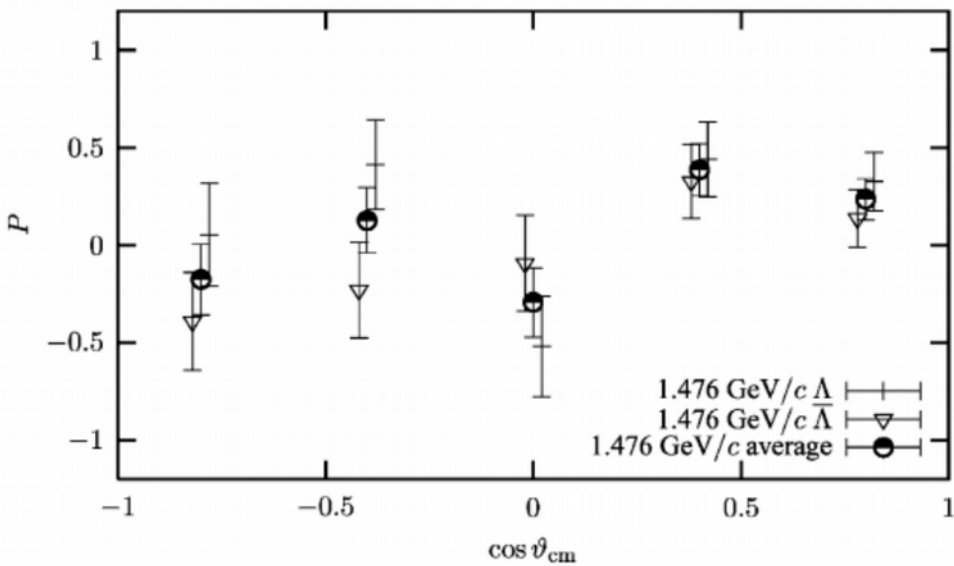
- essential for $(\gamma p \rightarrow K^+ \Lambda)$ — new measurement by (CLAS)



THIS TALK: ESTIMATE α_-

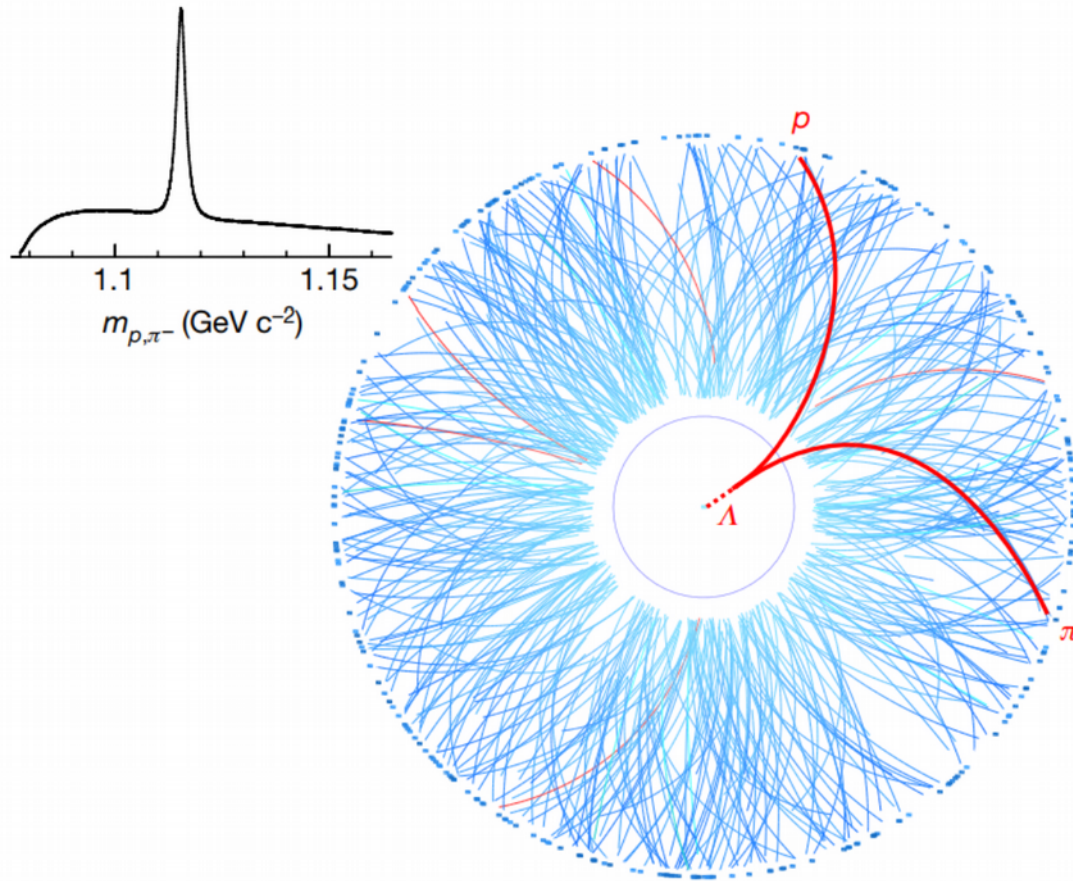
Where α matters (1):
Baryon spectroscopy

Where α matters (2):
 $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$

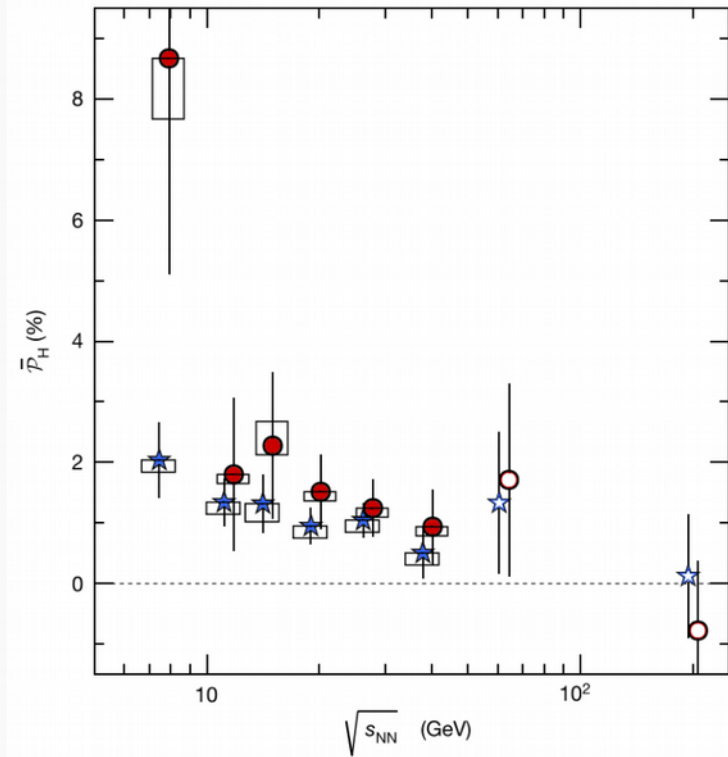


Where α matters (3): Global Λ polarization in nuclear collisions

STAR Au-Au collision

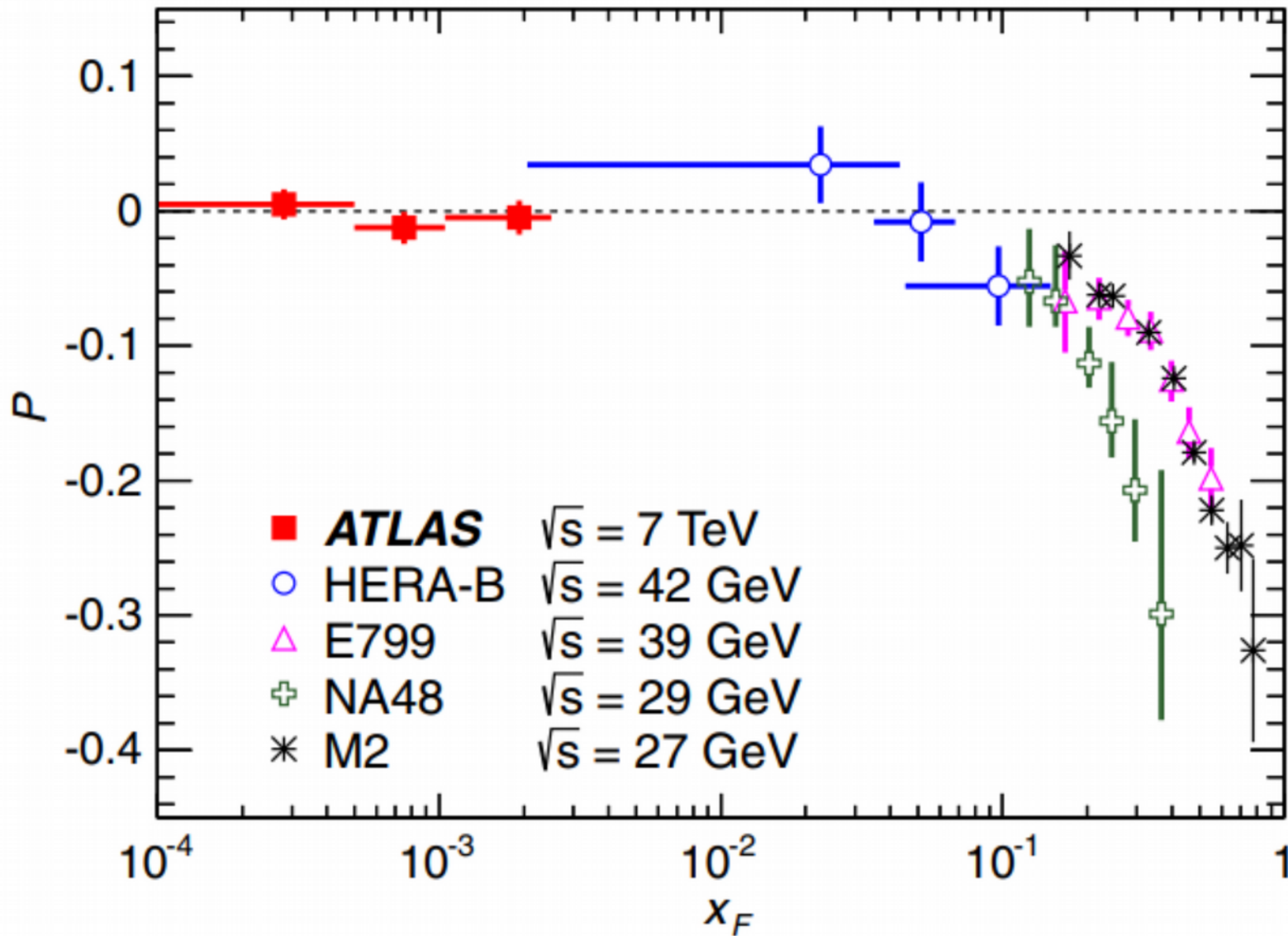


Average Λ ($\bar{\Lambda}$) polarization in collisions...



Where α matters (4):

Λ ($\bar{\Lambda}$) Transverse polarization with ATLAS



Measurements of α

Recent press coverage

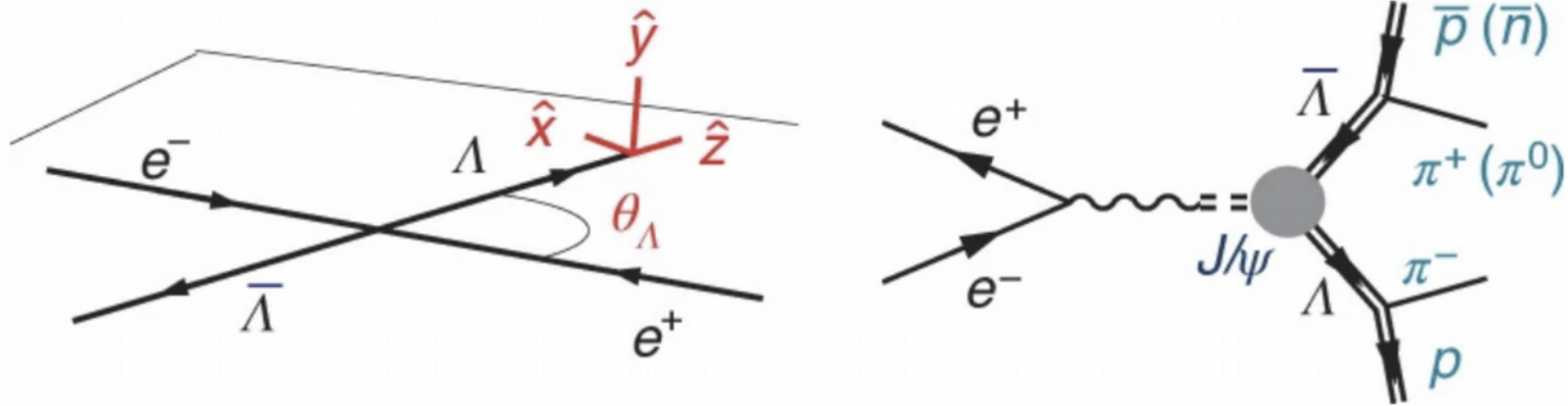


BESIII (2018) & this work



BESIII (2018)

BES III: Direct measurement



$\Lambda\bar{\Lambda}$ production process.

$$\begin{aligned}
 & \mathcal{W}(\xi; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_+) \\
 &= 1 + \alpha_\psi \cos^2 \theta_\Lambda + \alpha_- \alpha_+ \left[\sin^2 \theta_\Lambda (n_{1,x} n_{2,x} - \alpha_\psi n_{1,y} n_{2,y}) \right. \\
 & \quad \left. + (\cos^2 \theta_\Lambda + \alpha_\psi) n_{1,z} n_{2,z} \right] \\
 &+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (n_{1,x} n_{2,z} + n_{1,z} n_{2,x}) \\
 &+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y})
 \end{aligned}$$

$\Lambda\bar{\Lambda}$ intensity distribution

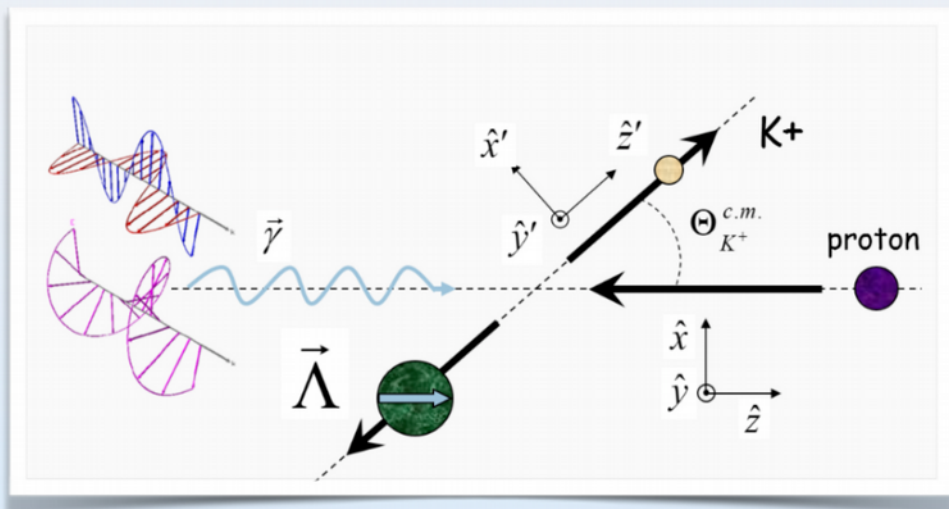
Table 1 | Summary of the results

Parameters	This work (BES III)	Previous results (PDG)
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 (ref. ¹⁴)
$\Delta\Phi$	$42.4 \pm 0.6 \pm 0.5^\circ$	-
α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 (ref. ⁶)
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 (ref. ⁶)
$\bar{\alpha}_0$	$-0.692 \pm 0.016 \pm 0.006$	-
A_{CP}	$-0.006 \pm 0.012 \pm 0.007$	0.006 ± 0.021 (ref. ⁶)
$\bar{\alpha}_0/\alpha_+$	$0.913 \pm 0.028 \pm 0.012$	-

> 5σ difference between new result and PDG¹².

Kaon photoproduction (this work)

Experimental setup



Intensity

$$(LP) : 1 + \alpha_- \cos \theta_y \mathbf{P}$$

$$- p_L^\gamma \cos 2\phi \mathbf{\Sigma}$$

$$- \alpha_- p_L^\gamma \cos 2\phi \cos \theta_y \mathbf{T}$$

$$- \alpha_- p_L^\gamma \sin 2\phi \cos \theta_x \mathbf{O}_x$$

$$- \alpha_- p_L^\gamma \sin 2\phi \cos \theta_z \mathbf{O}_z$$

$$(CP) : 1 + \alpha_- \cos \theta_y \mathbf{P}$$

$$+ p_C^\gamma \alpha_- \cos \theta_x \mathbf{C}_x$$

$$+ p_C^\gamma \alpha_- \cos \theta_z \mathbf{C}_z$$

● 7 polarization observables: $\mathbf{P}, \mathbf{\Sigma}, \mathbf{T}, \mathbf{O}_x, \mathbf{O}_z, \mathbf{C}_x, \mathbf{C}_z$

● Kinematic variables: θ_i, W_i

● 1 fundamental: α_- , and 2 calibration parameters: p_L^γ, p_C^γ

[CLAS] McCracken et al.(2010)
[CLAS] Bradford et al.(2007)
[CLAS] Paterson et al. (2016)

BUT: observables are not independent \longrightarrow **FIERZ IDENTITIES**

Chiang, Tabakin (1997)
Sandorfi et al. (2011)

Kaon photoproduction and Fierz identities

Helicity space maps on Clifford algebra \blacktriangleright Fierz identities:

Chiang, Tabakin (1997)

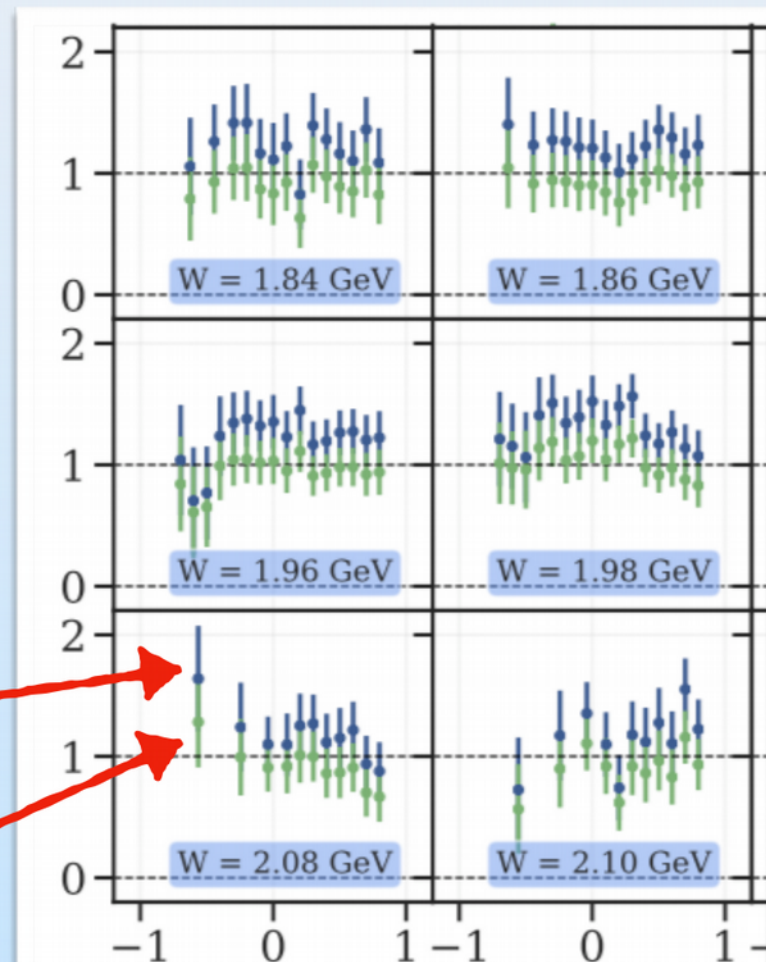
$$\Sigma\mathbf{P} - \mathbf{C}_x\mathbf{O}_z + \mathbf{C}_z\mathbf{O}_x - \mathbf{T} = 0 \quad \& \quad \mathbf{O}_x^2 + \mathbf{O}_z^2 + \mathbf{C}_x^2 + \mathbf{C}_z^2 + \Sigma^2 - \mathbf{T}^2 + \mathbf{P}^2 = 1$$

A-priori:

\Rightarrow Observables are not independent

\Rightarrow determine α_- such that FI are fulfilled

\Rightarrow statistically non-trivial question



$\alpha_- [\text{PDG}]$

$\alpha_- [\text{PDG}] / a$

Statistical Analysis

Definition of Fierz value and its distribution

◎ Define random variables:

$\mathcal{N}[\mu, \sigma^2]$ from CLAS measurements

$$\mathcal{F}_i^{(1)} = a^2 l^2 \left(\mathcal{O}_{x,i}^2 + \mathcal{O}_{z,i}^2 - \mathcal{T}_i^2 \right) + a^2 c^2 \left(\mathcal{C}_{x,i}^2 + \mathcal{C}_{z,i}^2 \right) + l^2 \Sigma_i^2 + a^2 \mathcal{P}_i^2$$

...similarly for second F.I.

◎ FV , a , l , c become random variables, but:

A. Scaling: $\left\{ \begin{array}{l} \text{Data and errors are scaled with } a, l, c \\ \text{Normalization of } PDF[a^2 \mathcal{P}_i^2] \end{array} \right.$

d'Agostini (1994)

B. Most “observables” and scale parameters enter quadratically

& Is there a closed form of $PDF[\mathcal{F}_i]$?

Roe (2015)

Statistical challenges (1)

A. Scaling

Imagine linear case: $\mathcal{F} := a \mathcal{O} = 1$

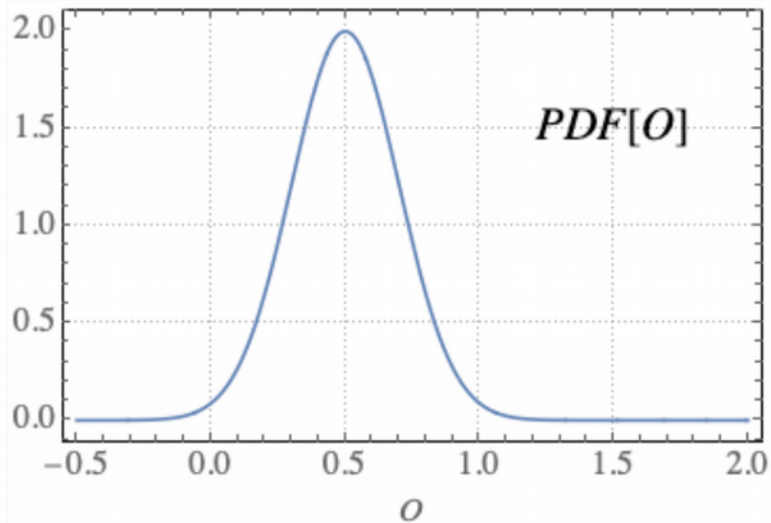
$$\mathcal{O} = \mathcal{N}[\mu, \sigma^2]$$

$$p_{\mathcal{F}}(f, a) = \int dO p(O) \delta(aO - f)$$

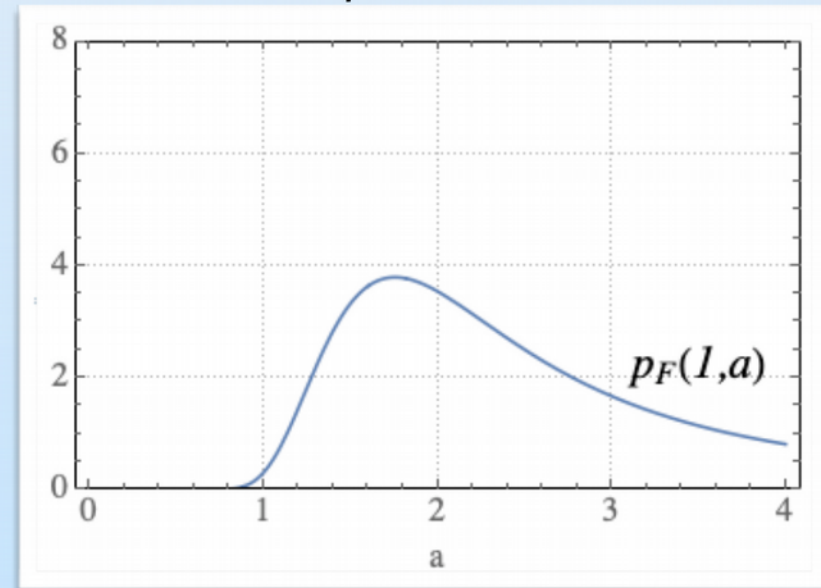
$$p_{\mathcal{F}}(1, a) = \frac{1}{a\sqrt{2\pi\mu\sigma}} e^{-\frac{(1-a\mu)^2}{2(a\sigma)^2}}$$

conditional probability

PDF of \mathcal{O} suggests $a=2$



PDF of \mathcal{F} peaks at $a < 2$



\Rightarrow remove a -dependence from the normalization

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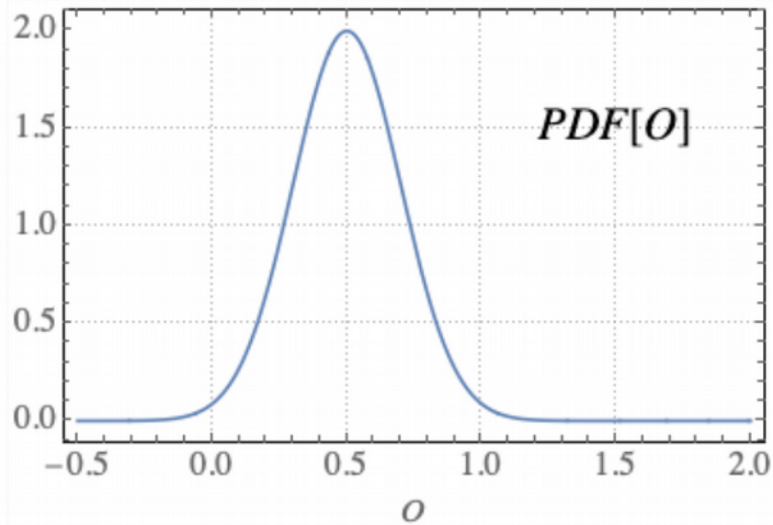
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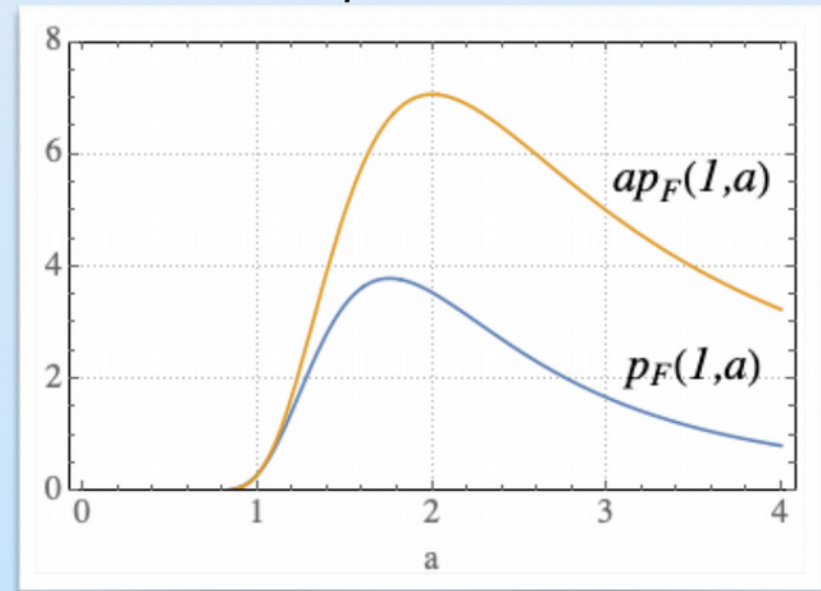
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Statistical challenges (2)

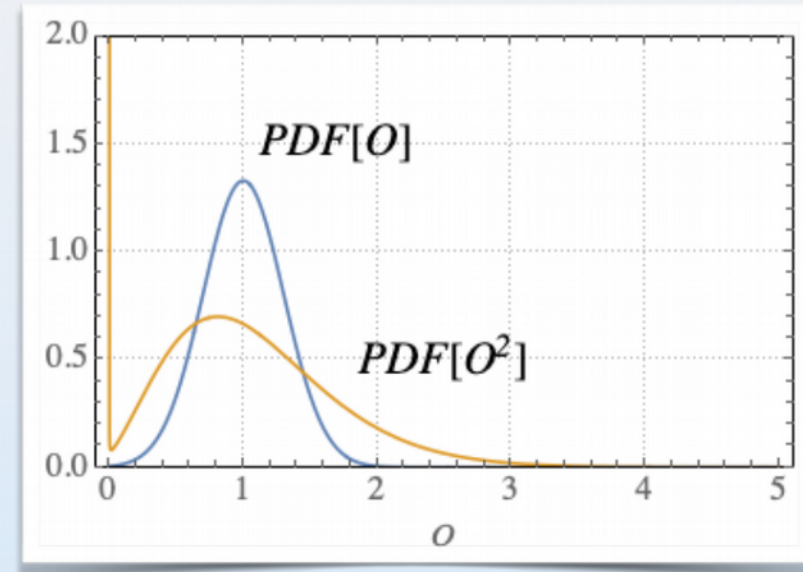
B. Non-linearity

$$\mathcal{O} \sim \mathcal{N}[\mu, \sigma^2] \implies \mathcal{Y} = \mathcal{O}^2 \sim NC_{\chi^2}$$

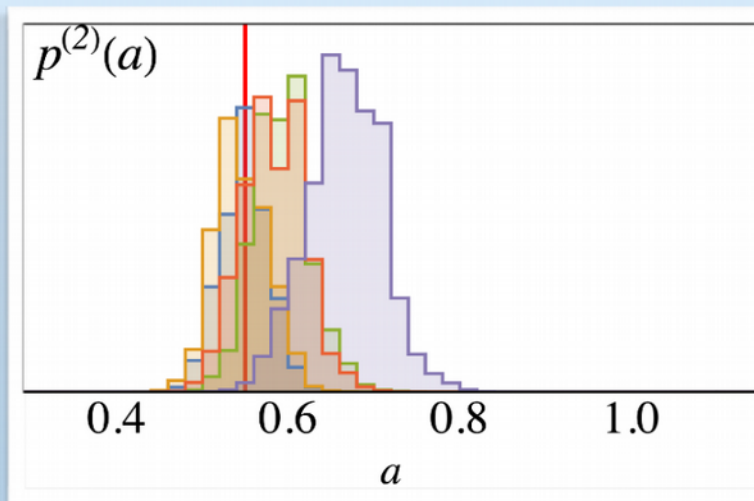
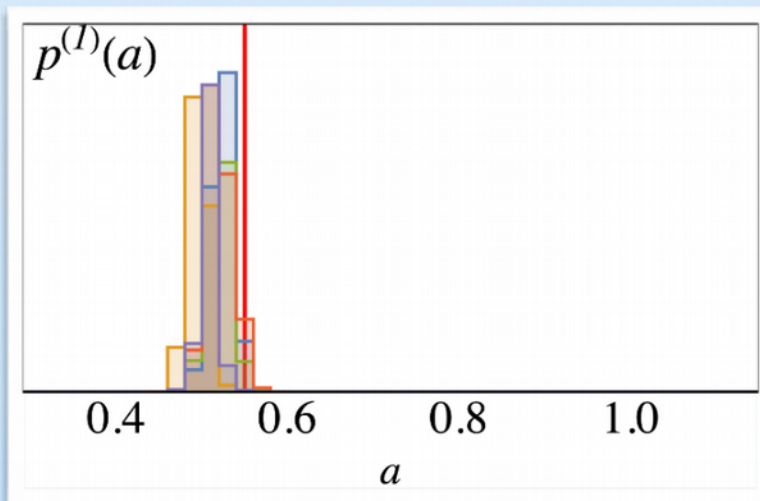
non-central chi squared distribution

$$\mu_{\mathcal{Y}} = \mu_{\mathcal{O}}^2 + \sigma_{\mathcal{O}}^2, \quad \sigma_{\mathcal{Y}}^2 = 2\sigma_{\mathcal{O}}^2(2\mu_{\mathcal{O}}^2 + \sigma_{\mathcal{O}}^2)$$

\implies Expectation value of Fierz identity $\neq 1$



Ultimately – blind test on synthetic data

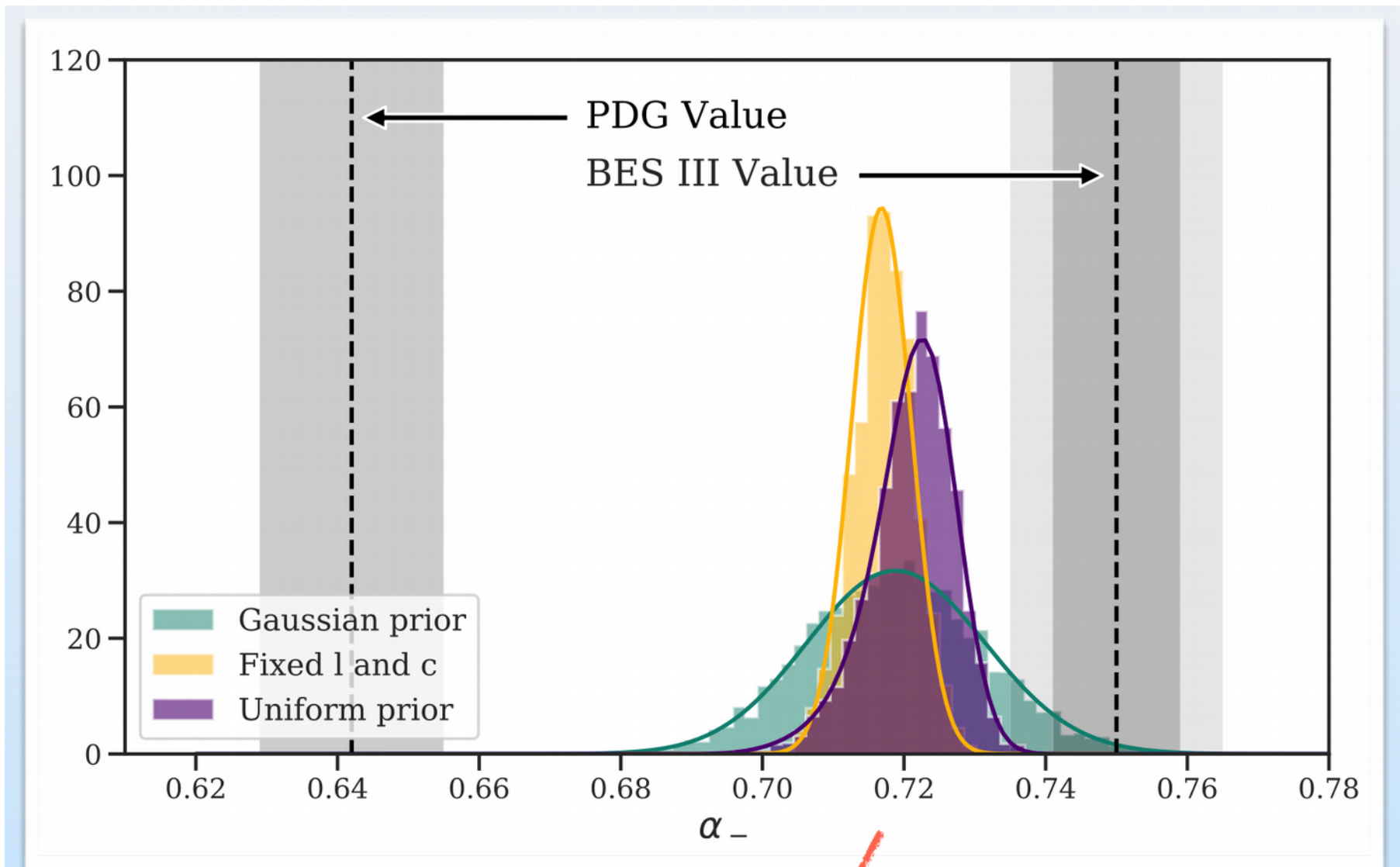


re-sampling test of both Fierz identities:

- 300 kin. points
- 200 000 samples
- **$a_{\text{test}} = 0.55$**

Results

Overall result

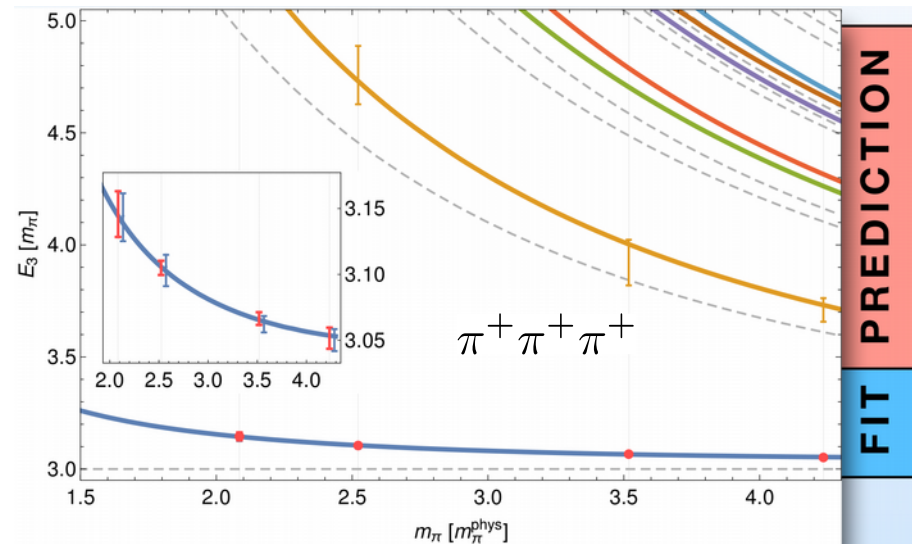


$$\alpha_- = 0.721 \pm 0.006 \pm 0.005$$

Summary

- Complicated phenomenology of excited baryons through coupled-channel and three-body effects

→ Conceptual progress needed to connect to lattice QCD calculations.
→ D. Wilson's talk on Thursday

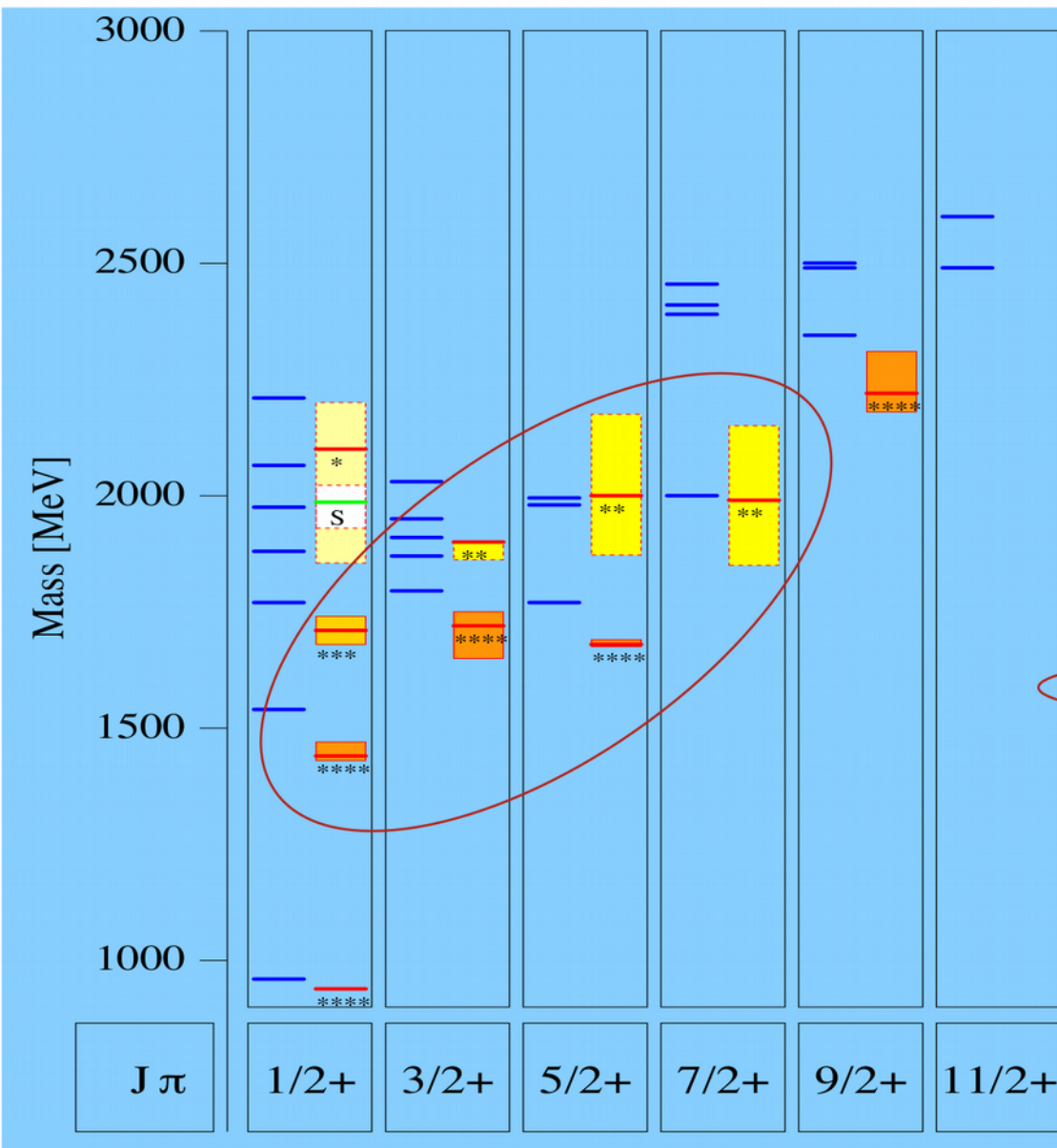


[M. Mai, MD, PRL (2019)]

- Global analyses of pion and photon-induced reactions
 - Jülich-Bonn analysis finds/confirmes new states in analysis of photoproduction data
- Data-driven new value for α_- determined. Changes polarization measurements at CLAS (baryon spectroscopy) but has impact in wide areas of hadron physics

Spare slides

Spectrum of N* resonances



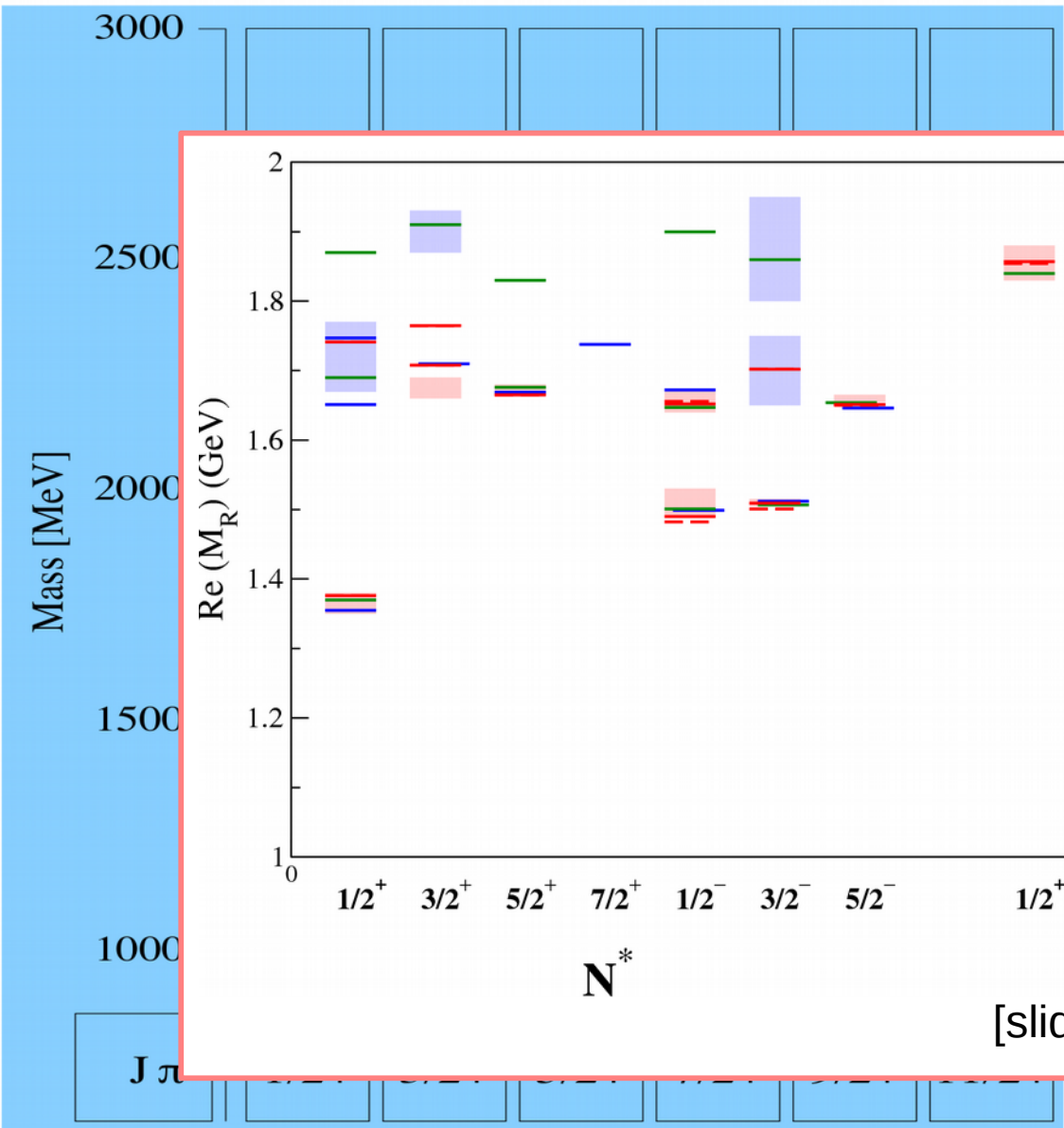
N^*	$J^P (L_{2l,2J})$	2010	2014
$N(1440)$	$1/2^+ (P_{11})$	* * *	* * *
$N(1520)$	$3/2^- (D_{13})$	* * *	* * *
$N(1535)$	$1/2^- (S_{11})$	* * *	* * *
$N(1650)$	$1/2^- (S_{11})$	* * *	* * *
$N(1675)$	$5/2^- (D_{15})$	* * *	* * *
$N(1680)$	$5/2^+ (F_{15})$	* * *	* * *
$N(1685)$			*
$N(1700)$	$3/2^- (D_{13})$	* * *	* * *
$N(1710)$	$1/2^+ (P_{11})$	* * *	* * *
$N(1720)$	$3/2^+ (P_{13})$	* * *	* * *
$N(1860)$	$5/2^+$		**
$N(1875)$	$3/2^-$		* * *
$N(1880)$	$1/2^+$		**
$N(1895)$	$1/2^-$		**
$N(1900)$	$3/2^+ (P_{13})$	**	* * *
$N(1990)$	$7/2^+ (F_{17})$	**	**
$N(2000)$	$5/2^+ (F_{15})$	**	**
$N(2080)$	D_{13}	**	
$N(2090)$	S_{11}	*	
$N(2040)$	$3/2^+$		*
$N(2060)$	$5/2^-$		**
$N(2100)$	$1/2^+ (P_{11})$	*	*
$N(2120)$	$3/2^-$		**
$N(2190)$	$7/2^- (G_{17})$	* * *	* * *
$N(2200)$	D_{15}	**	

- Most new resonances by Bonn-Gatchina group;
- Many from kaon photoproduction

[Slide: V. Crede/Nstar 2017, slight modifications]

[See also: Crede, Roberts, Rep. Prog. Phys. 76 (2013)]

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[slide: ANL/Osaka Kamano@N*2017]

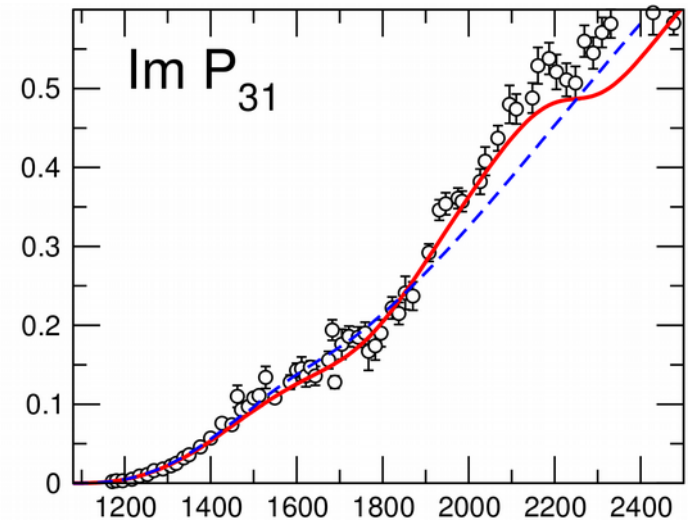
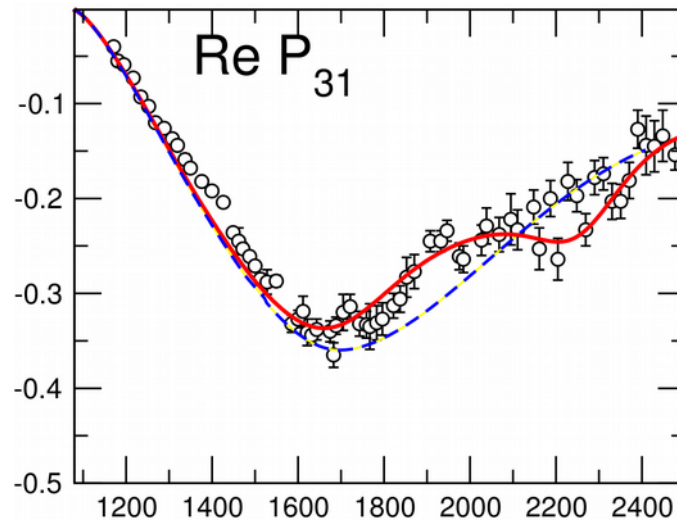
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Visible influence of new states

$\Delta(2190)3/2^+$ in πN PW



$N(1900)3/2^+$, $N(2060)5/2^-$ in σ_{tot} in $\pi^- p \rightarrow K^+ \Sigma^-$

