

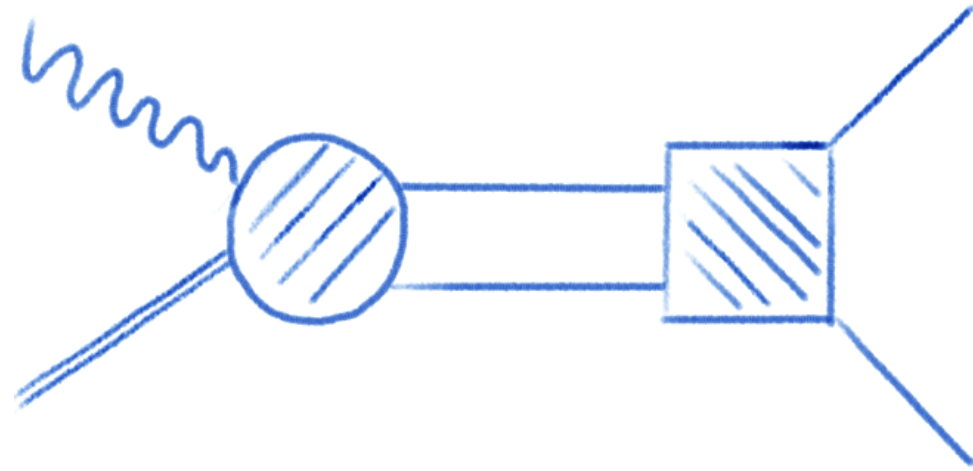
Photoproduction of Resonances on the Lattice

Luka Leskovec

PWA11/ATHOS6

2-6 September 2019

Centro Brasileiro de Pesquisas Físicas



Hadrons

• π^\pm	$1^-(0^-)$	• $f_1(1510)$	$0^+(1^{++})$
• π^0	$1^-(0^{+})$	• $f_2'(1525)$	$0^+(2^{++})$
• η	$0^+(0^{+})$	• $f_2(1565)$	$0^+(2^{++})$
• $f_0(500)$ aka σ ; was $f_0(600)$	$0^+(0^{++})$	• $\rho(1570)$	$1^+(1^{--})$
• $\rho(770)$	$1^+(1^{--})$	• $h_1(1595)$	$0^-(1^{+-})$
• $\omega(782)$	$0^-(1^{--})$	• $\pi_1(1600)$	$1^-(1^{+-})$
• $\eta'(958)$	$0^+(0^{+})$	• $a_1(1640)$	$1^-(1^{++})$
• $f_0(980)$	$0^+(0^{++})$	• $f_2(1640)$	$0^+(2^{++})$
• $a_0(980)$	$1^-(0^{++})$	• $\eta_2(1645)$	$0^+(2^{-+})$
• $\phi(1020)$	$0^-(1^{--})$	• $\omega(1650)$	$0^-(1^{--})$
• $h_1(1170)$	$0^-(1^{+-})$	• $\omega_3(1670)$	$0^-(3^{--})$
		• $\pi_2(1670)$	$1^-(2^{-+})$

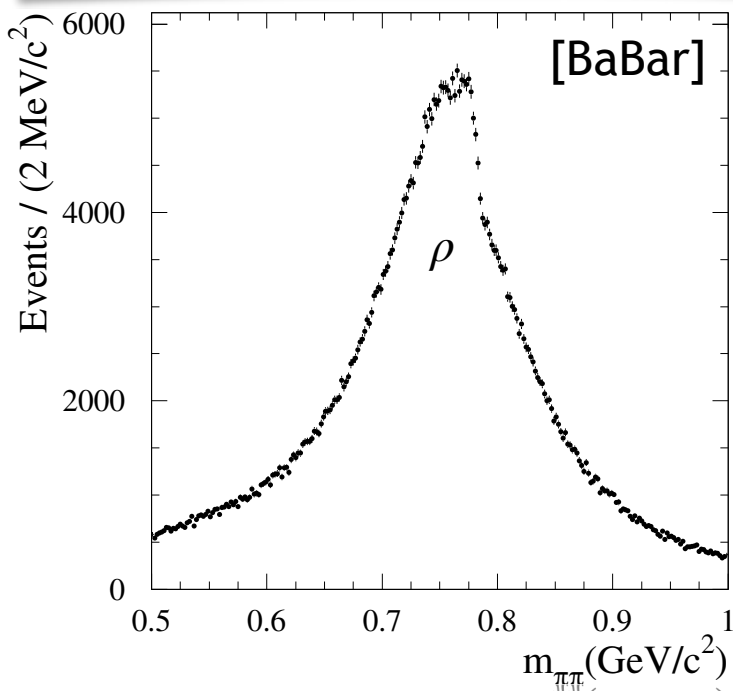
- interesting phenomena

- (un)similar to atoms

- QCD stable hadrons
(π , K , η)

- QCD unstable hadrons
(ρ , σ , a_0 , ...)

- resonances are most of the hadronic spectrum



What do we know about Hadrons?



<https://www.jlab.org/research/jleic/overview>

- but can we learn more about unstable hadrons?

Photoproduction Amplitudes

- Stable Hadrons from first principles:
 - masses
 - structure
- Unstable Hadrons from first principles:
 - resonance masses
 - strong decay widths
 - couplings to channels
 - Branching Ratios
 - scattering amplitudes

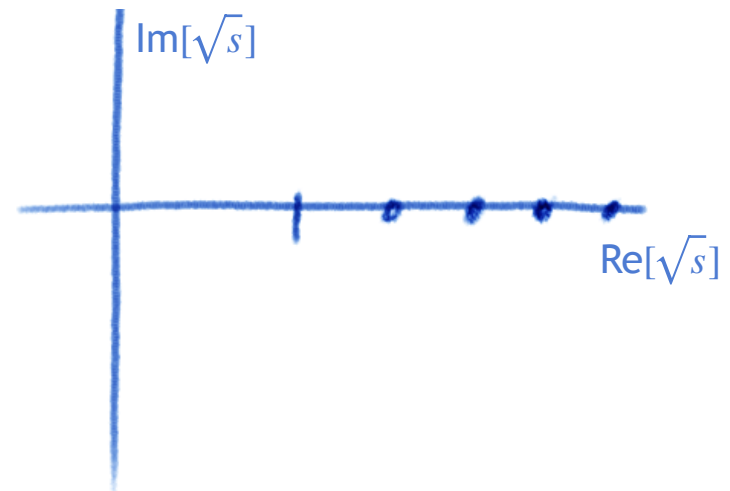
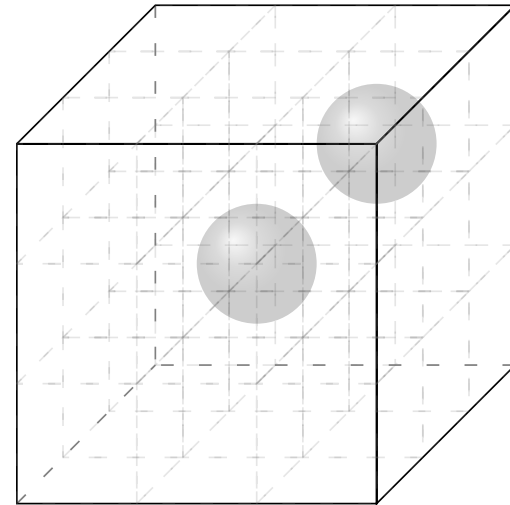
more lattice:

-> M. Döring Tue@++

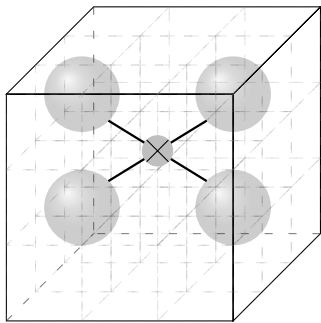
-> ₃D.Wilson Thu@17:00

Intro to Lattice QCD

- Euclidean space-time
- Monte Carlo sample the Feynman Path Integral
- $m_\pi \geq m_\pi^{phys}$
- Finite Volume Box
- $\psi(x) = \psi(x + L)$
- discrete spectrum

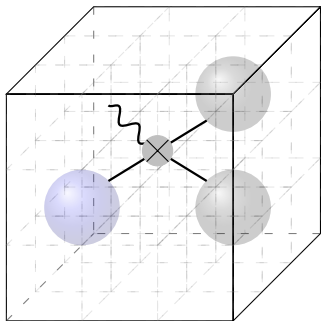
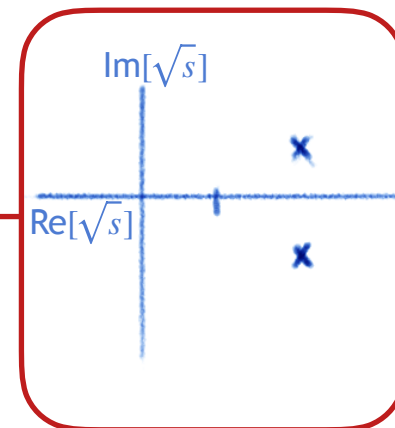
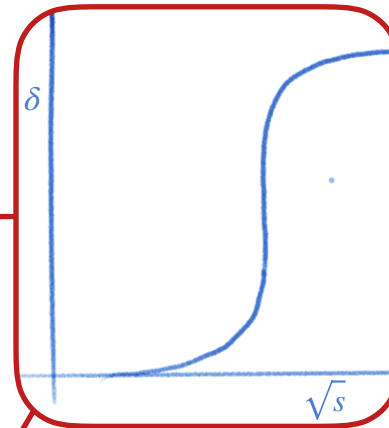


Photoproduction on the Lattice



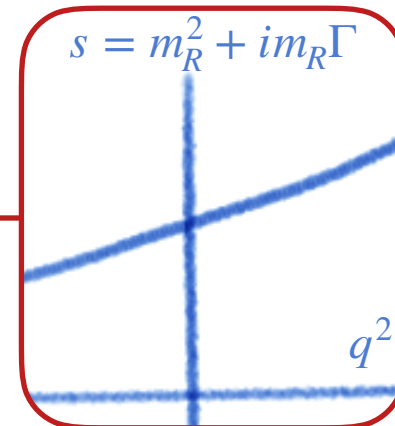
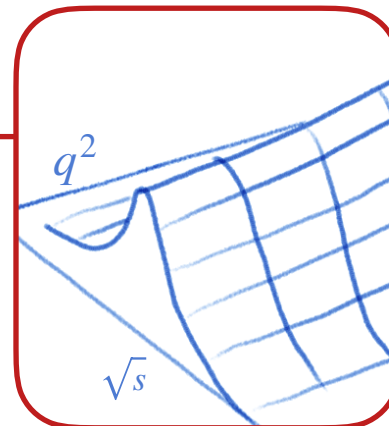
Lüscher analysis

$$\det [F^{-1} + M]$$



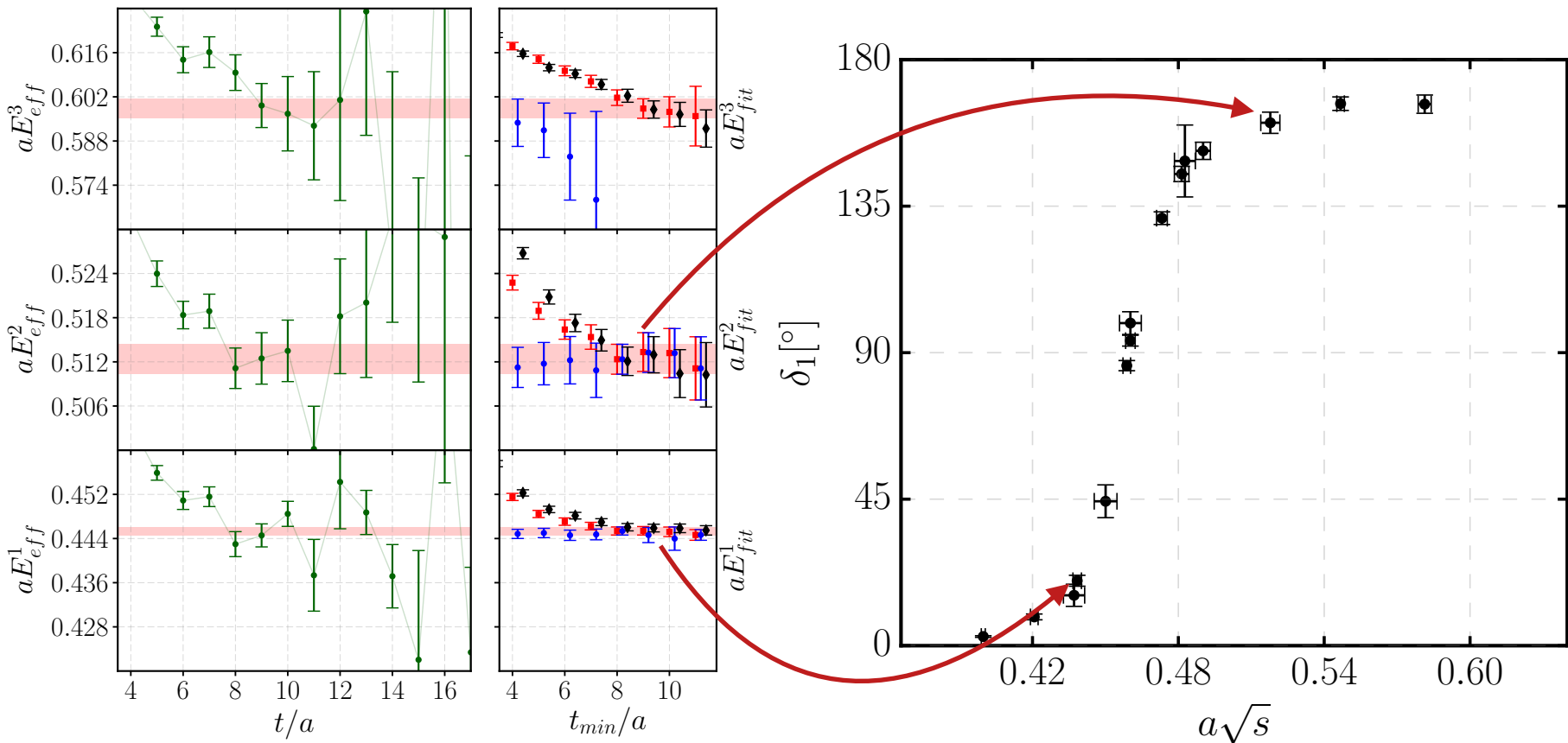
$$\lim_{E \rightarrow E_n} \frac{E - E_n}{F^{-1} + M}$$

Briceño-Hansen-Walker-Loud analysis



Lüscher analysis

$$|\vec{P}| = \frac{2\pi}{L}, \Lambda = A_2, \text{ basis: } O_{1234}$$



[Briceño, Dudek, Young 2018]

The ρ resonance mass and decay width

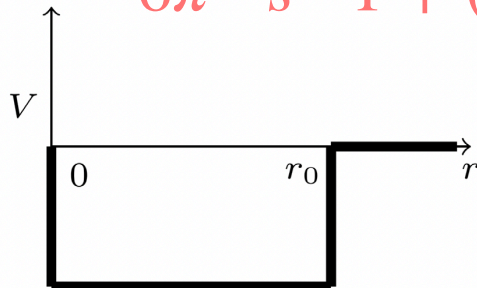
$$M_i = \frac{16\pi}{k} \frac{s\Gamma_i}{m_R^2 - s - i\sqrt{s}\Gamma_i}$$

- $i = \text{BW I:}$

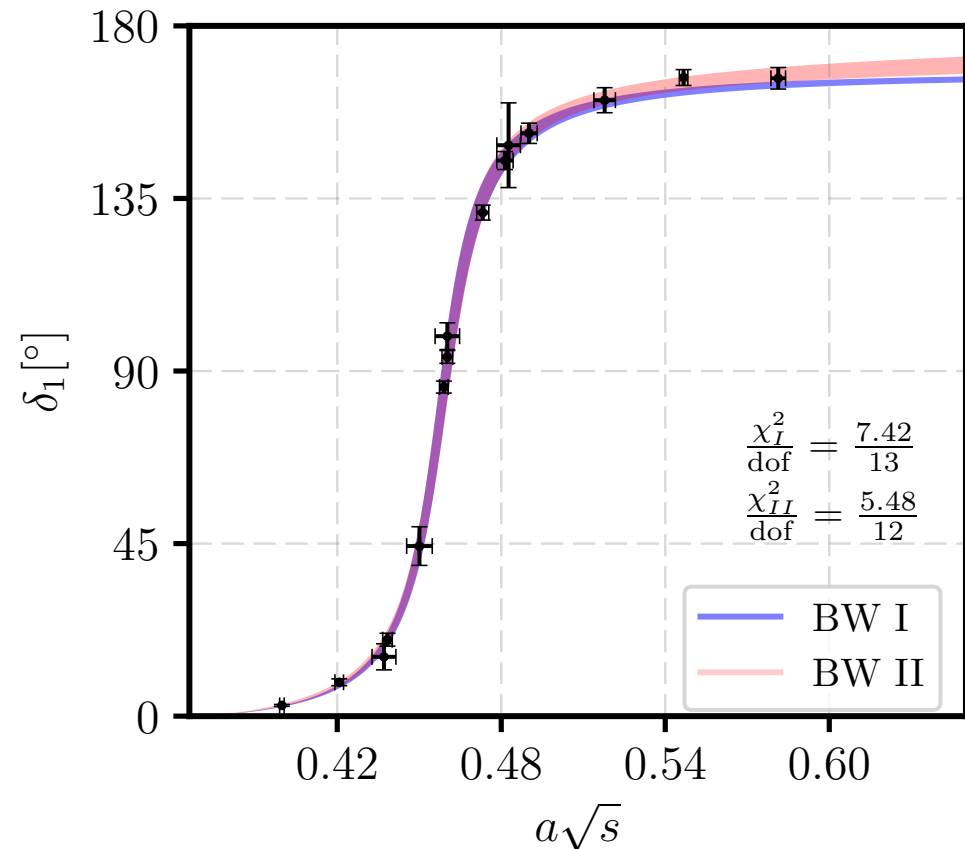
$$\Gamma_I = \frac{g_{\rho\pi\pi}^2 k^3}{6\pi s}$$

- $i = \text{BW II:}$

$$\Gamma_{II} = \frac{g_{\rho\pi\pi}^2 k^3}{6\pi s} \frac{1 + (k_R r_0)^2}{1 + (k r_0)^2}$$



[Feng et al., Lang et al., Aoki et al., Pelissier et al., HadSpec, HadSpec, RQCD, Bulava et al., Guo et al., Fu et al., Bulava et al., ETMC, ...]

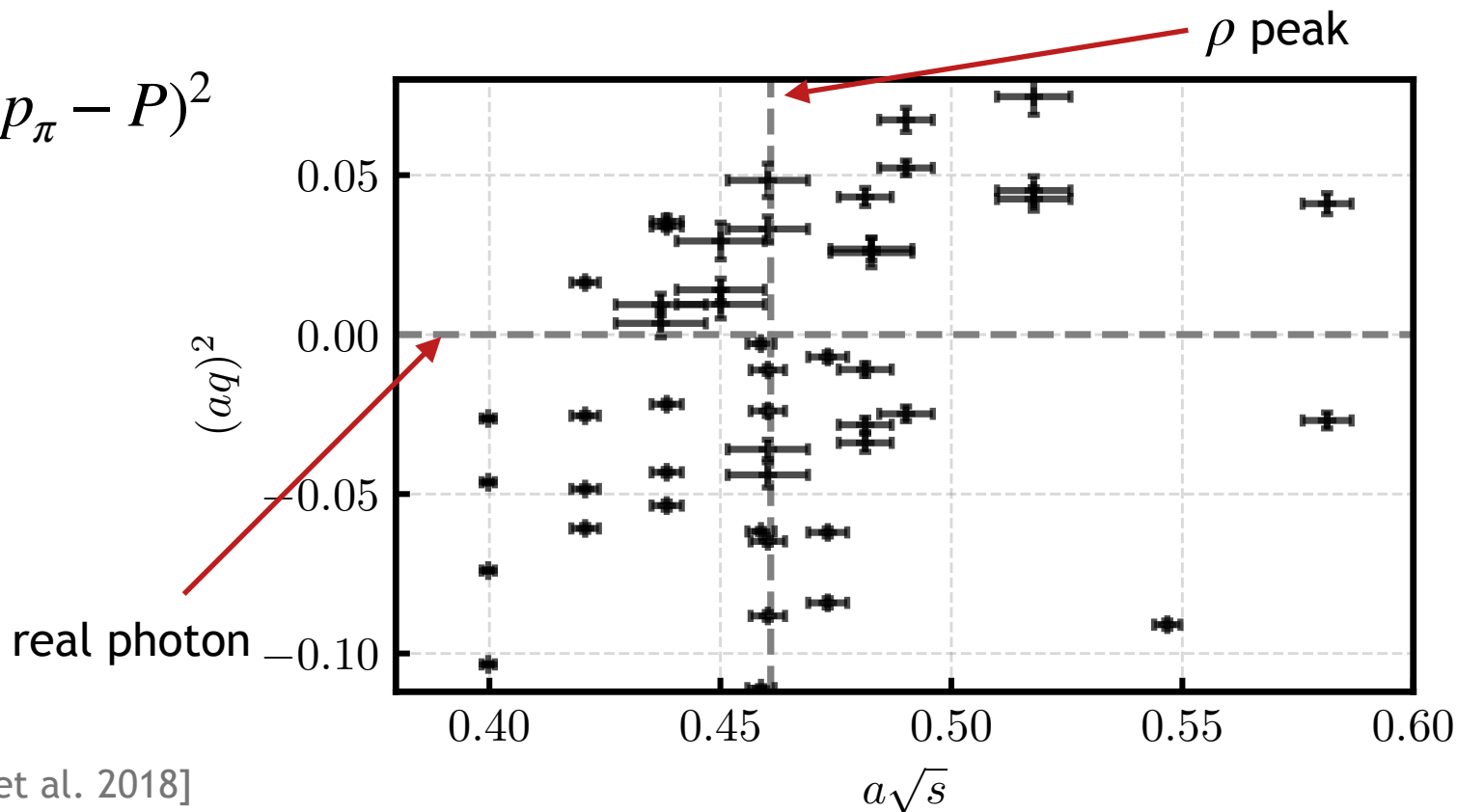


[Alexandrou et al. 2017]

About $\pi\gamma^* \rightarrow \pi\pi$

$$\langle \pi\pi; P, m | J^\mu(0) | \pi \rangle = \frac{2i\mathcal{V}_{\pi\gamma \rightarrow \pi\pi}(q^2, s)}{m_\pi} \epsilon^{\nu\mu\alpha\beta} \epsilon_\nu(P, m) (p_\pi)_\alpha (P)_\beta$$

$$q^2 = (p_\pi - P)^2$$



[Alexandrou et al. 2018]

Briceno-Hansen-Walker-Loud analysis

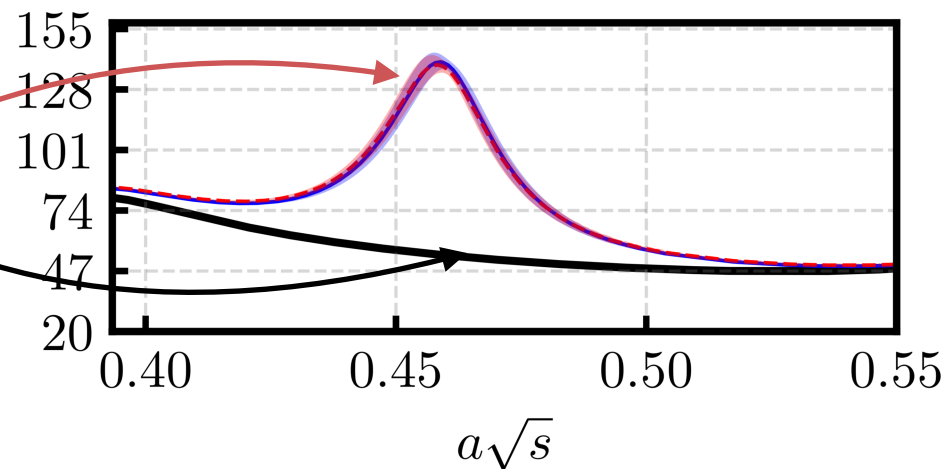
$$\mathcal{V}_{\pi\gamma \rightarrow \pi\pi}^{FV}(q^2, s) = \sqrt{R \mathcal{V}_{\pi\gamma \rightarrow \pi\pi}^{IV}(q^2, s) R}$$

[Lellouch, Lüscher 2000, ...,
Briceño, Hansen, Walker-Loud 2015]

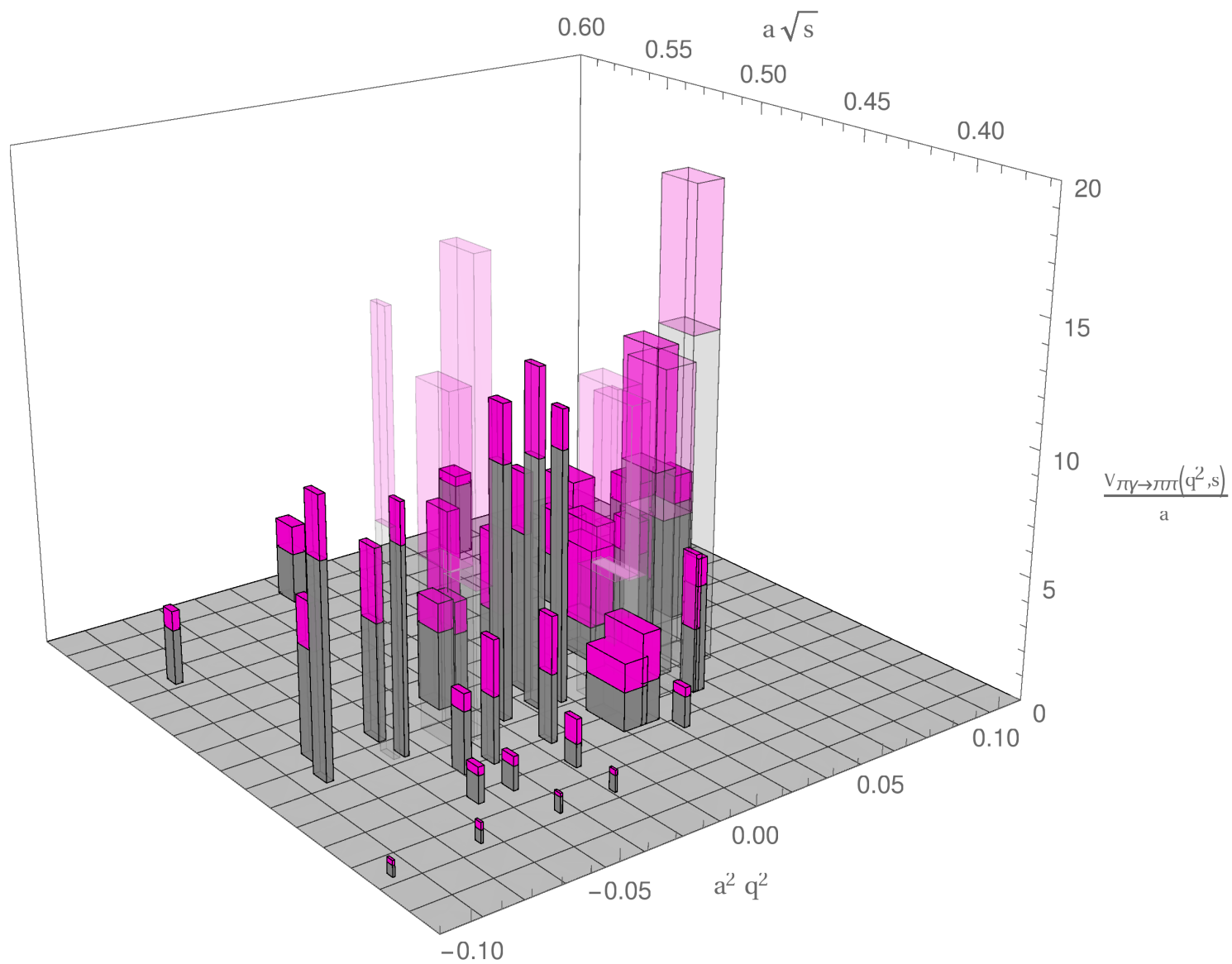
- caveats:

- FV quantum numbers
- only example (!)
- F^{-1} contribution
- $F^{-1} + M_i$
 - $i = \text{BW I}$
 - $i = \text{BW II}$

$$R = \lim_{E \rightarrow E_n} \frac{E - E_n}{F^{-1} + M}$$



Briceno-Hansen-Walker-Loud analysis



Fitting $\mathcal{V}_{\pi\gamma\rightarrow\pi\pi}^{IV}(q^2, s)$

- Watson's theorem

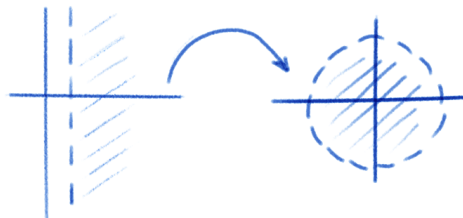
$$\mathcal{V}_{\pi\gamma\rightarrow\pi\pi,i}^{IV}(q^2, s) = \sqrt{\frac{16\pi}{k\Gamma_i} \frac{F(q^2, s)}{\cot\delta_i - i}}$$

$$F(q^2, s) = \frac{\sum_{n,m} A_{nm} z^n \mathcal{S}^m}{1 - \frac{q^2}{m_p^2}}$$

[Boyd et al. 1994,
Bourelly et al. 2008]

- expand F in:

- $\mathcal{S} = \frac{s - m_R^2}{m_R^2}$



- $z = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+}}{\sqrt{t_+ - q^2} + \sqrt{t_+}}$

- $t_+ = (2m_\pi)^2$

- systematic truncations:

- F1: $n + m \leq K$

- F2: $n \leq N, m \leq K - n$

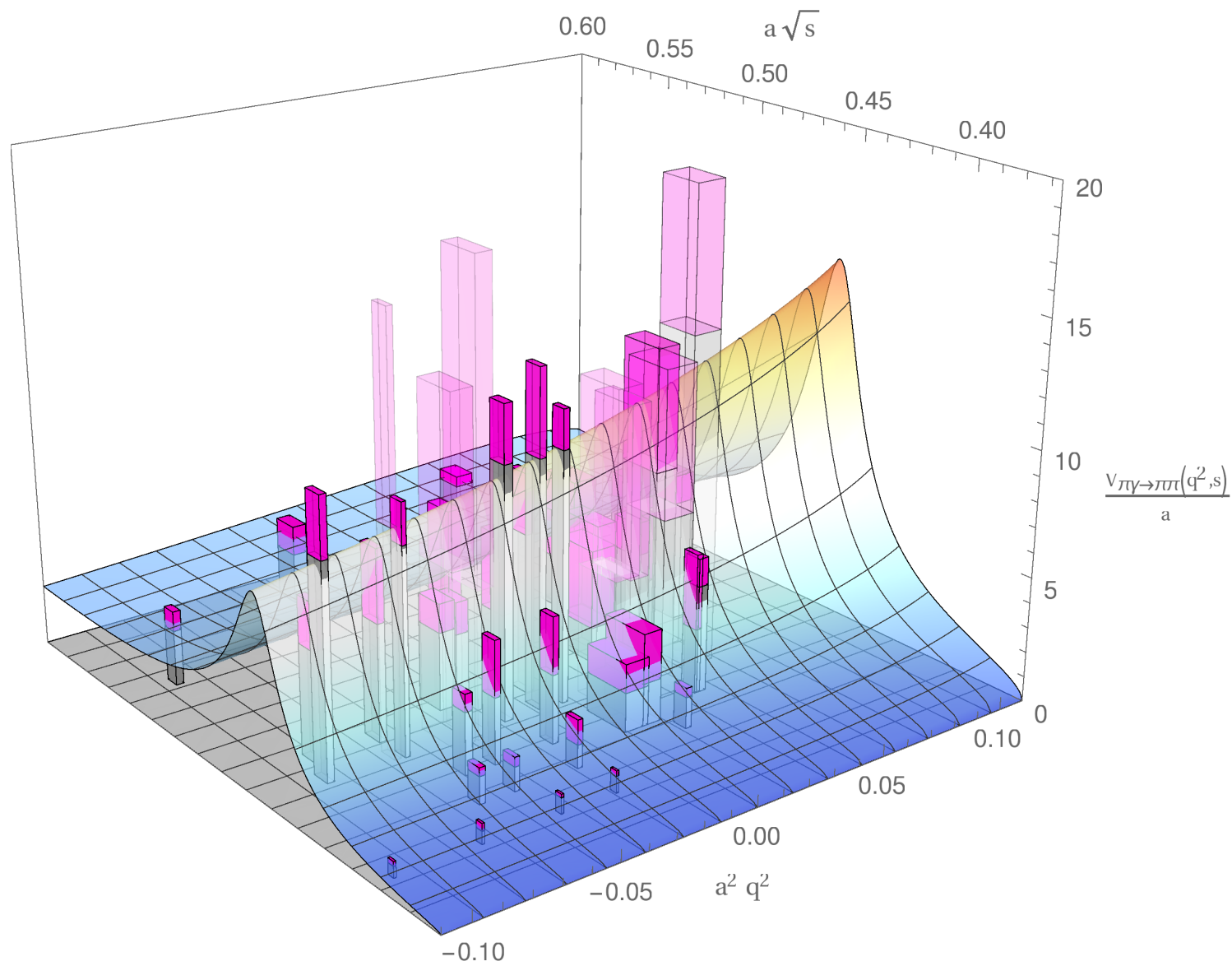
- F3: $n \leq N, m \leq M$

- analytic structure

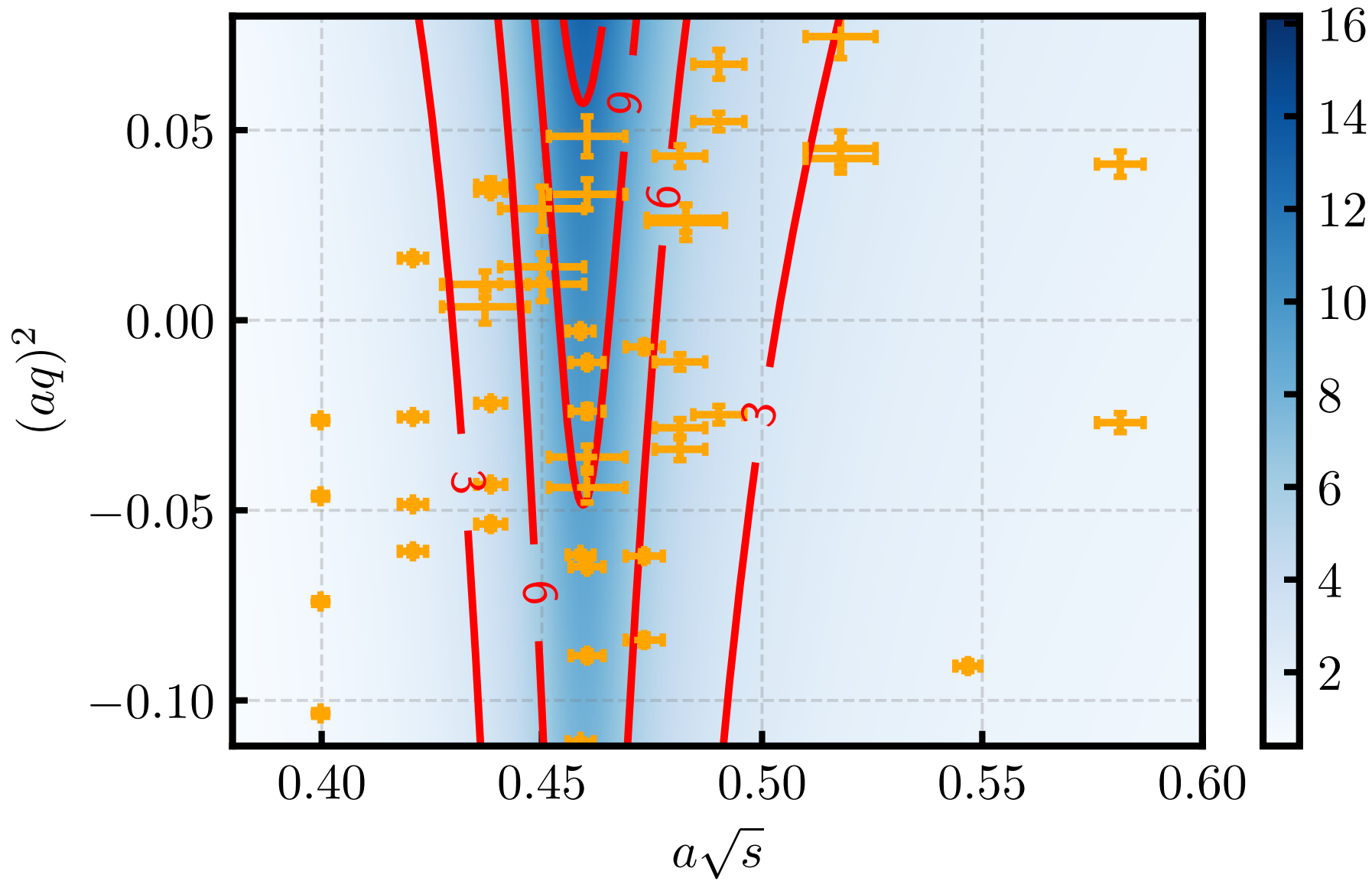
- needed

- not sensitive

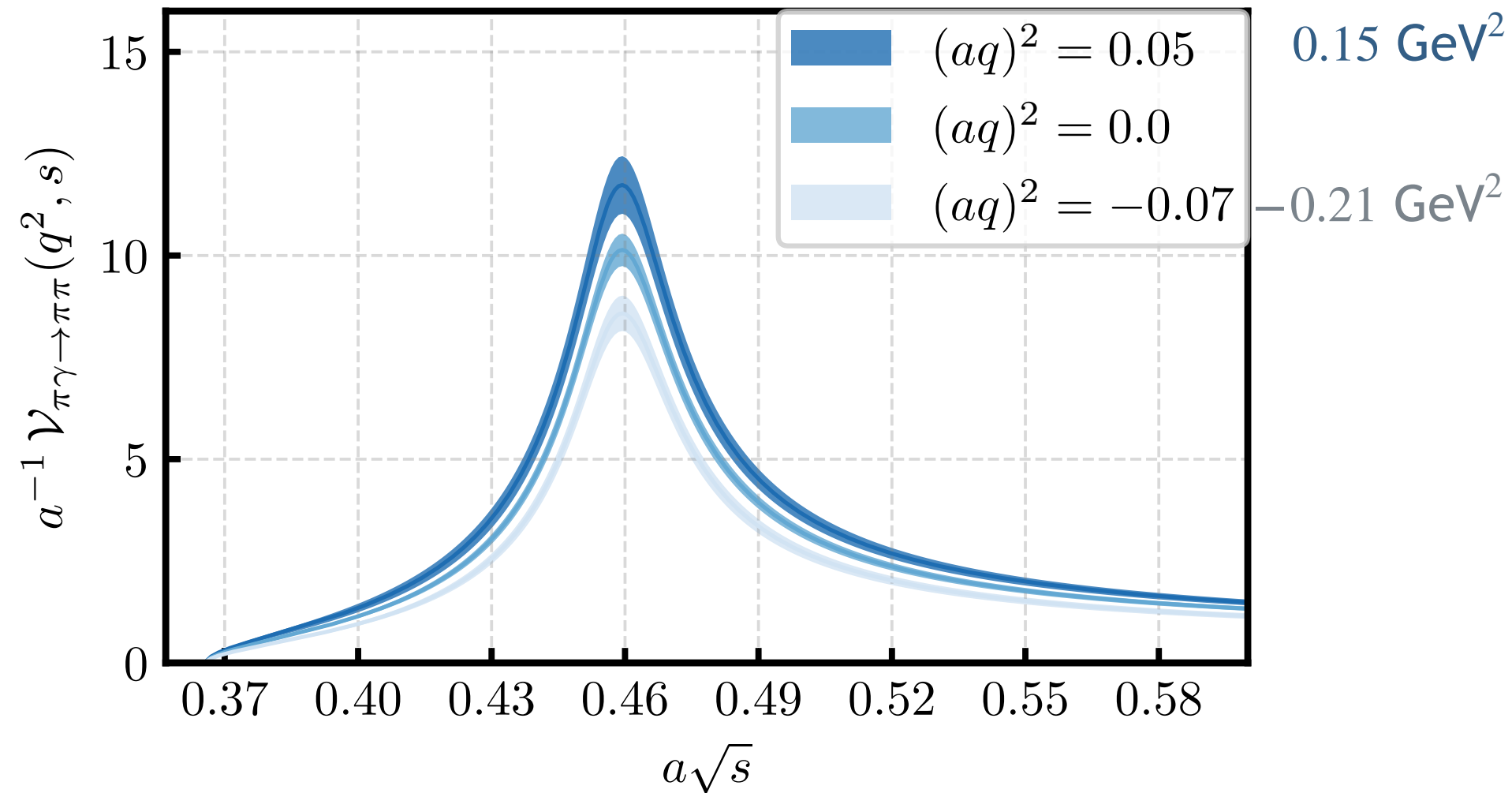
$\mathcal{V}_{\pi\gamma\rightarrow\pi\pi}^{IV}(q^2, s)$ 3-D view



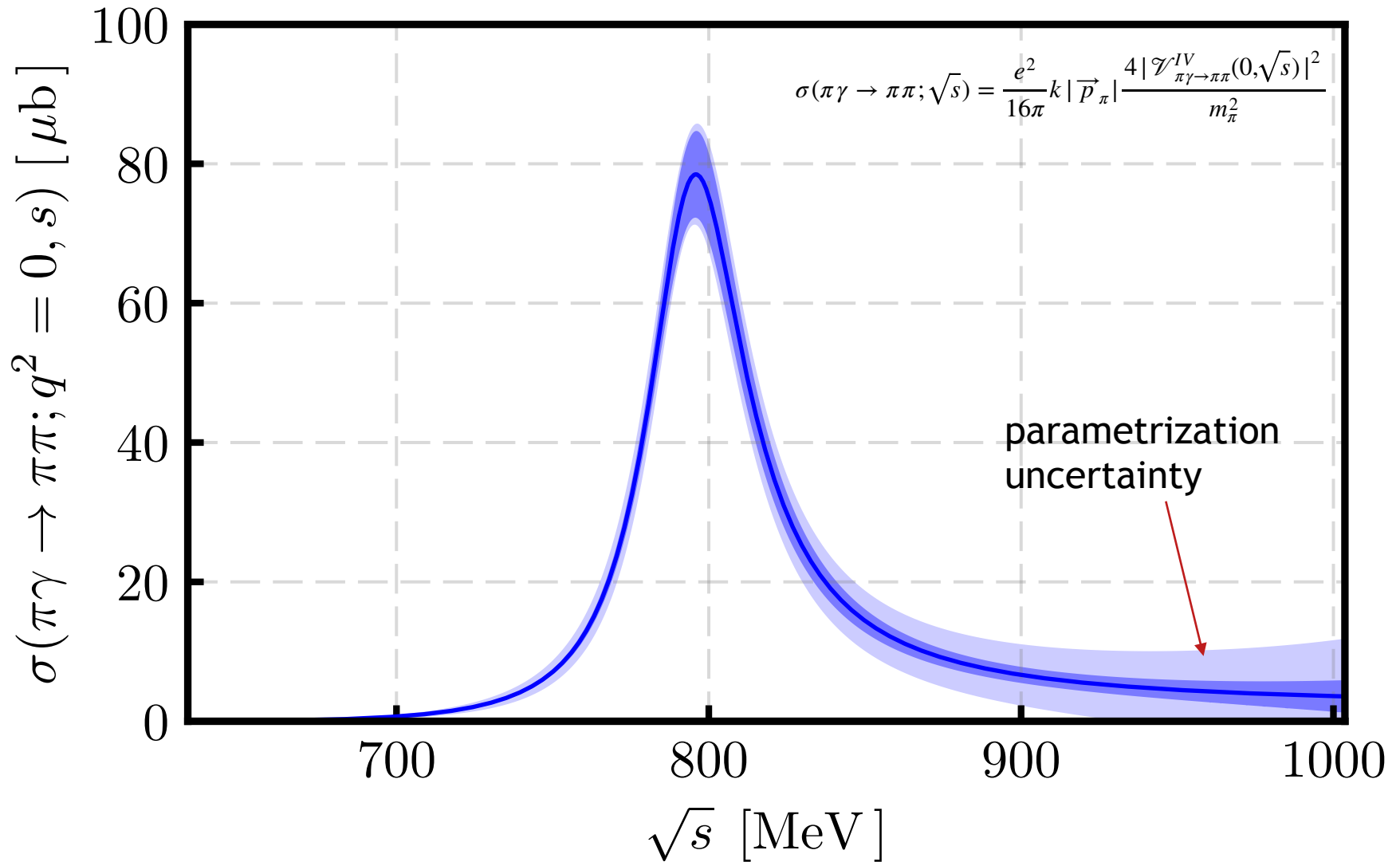
$\mathcal{V}_{\pi\gamma\rightarrow\pi\pi}^{IV}(q^2, s)$ top view



$\mathcal{V}_{\pi\gamma\rightarrow\pi\pi}^{IV}(q^2, s)$ cuts in q^2

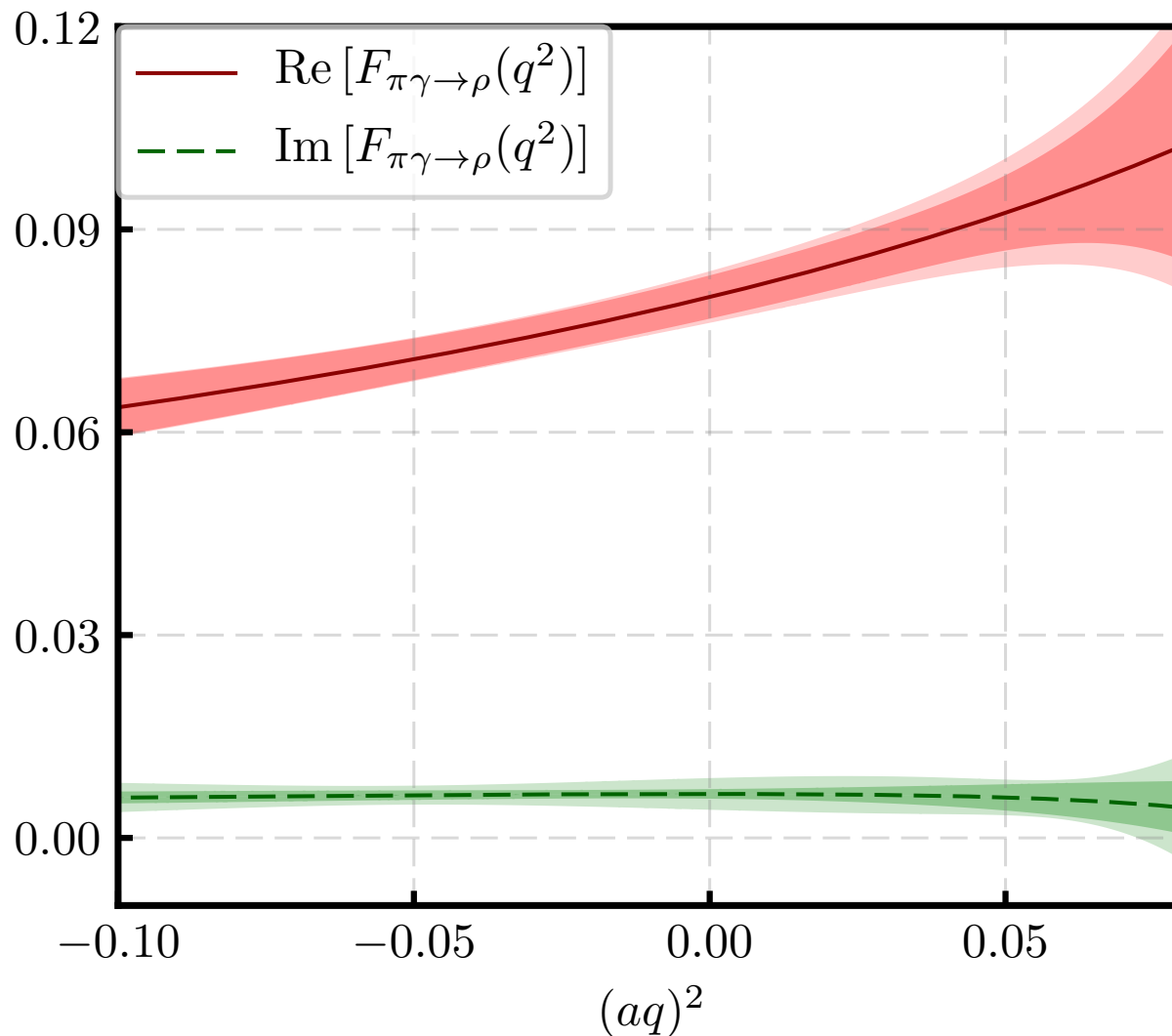


$\pi\gamma \rightarrow \pi\pi$ cross-section (@ $m_\pi = 320$ MeV)

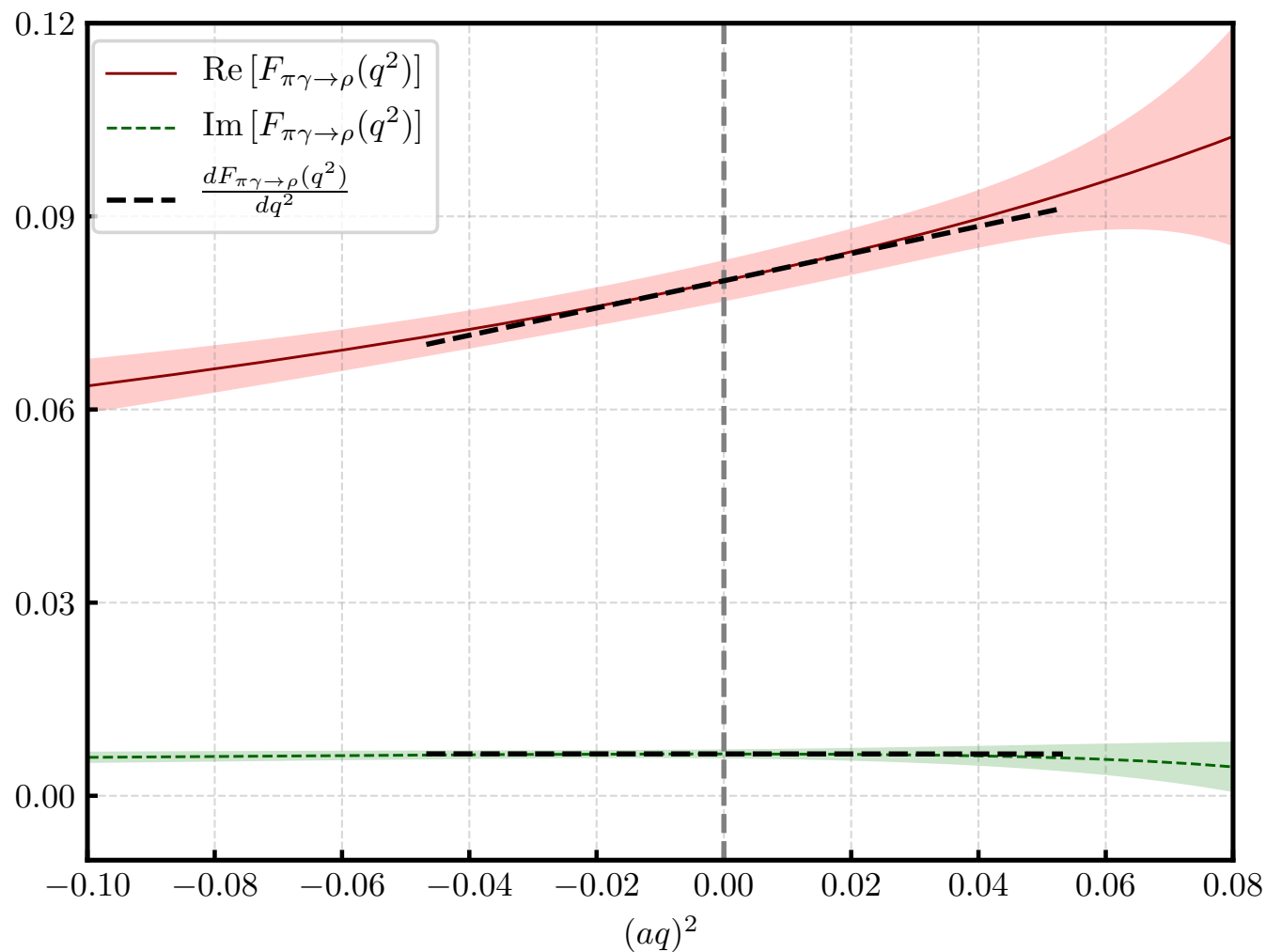


Resonant transition form factor

- analytical continuation to ρ pole $F_{\pi\gamma\rightarrow\rho}(q^2) = F(q^2, s = m_R^2 + im_R\Gamma_R)$



slope of $F_{\pi\gamma\rightarrow\rho}(q^2)$



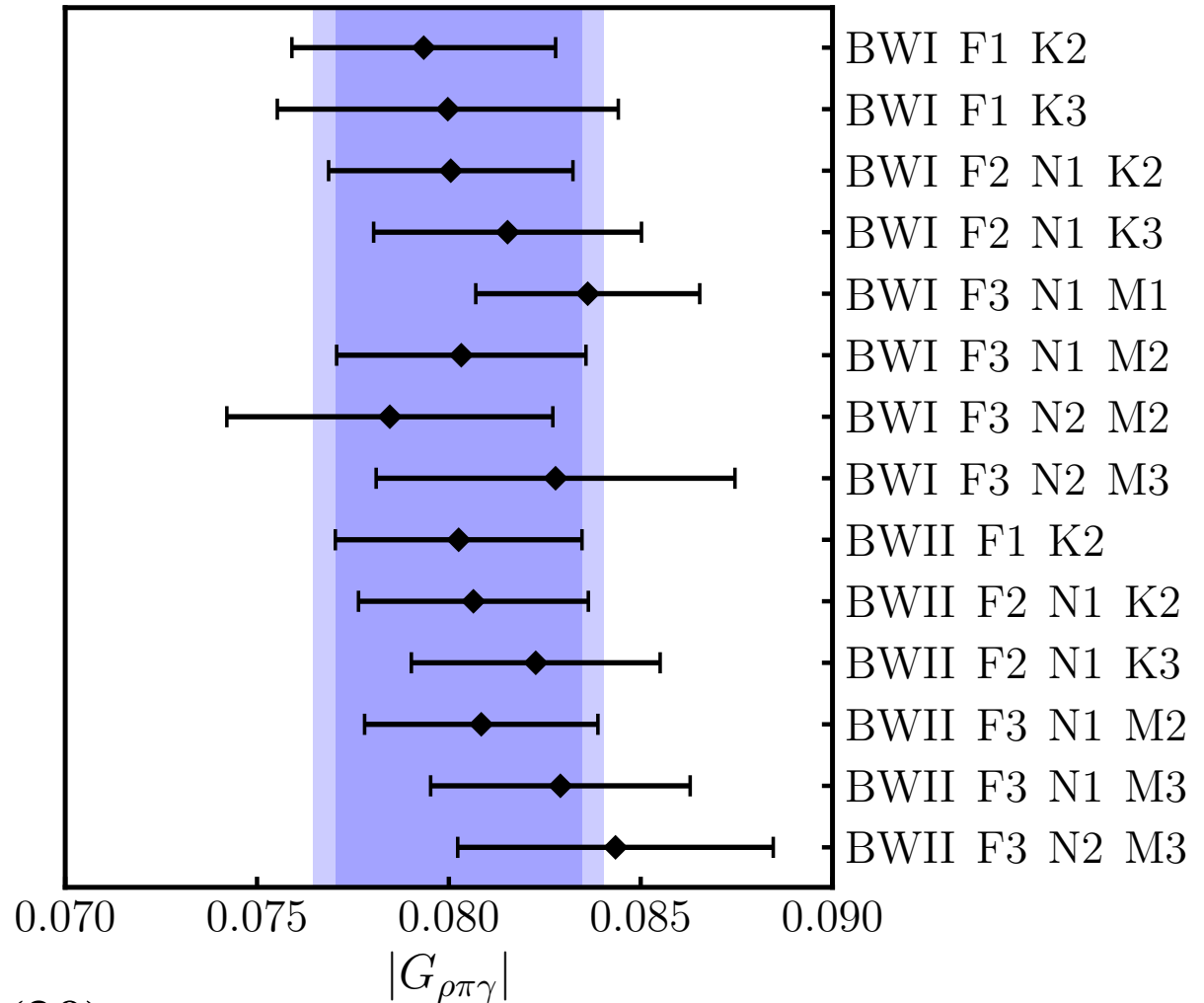
$$\left. \frac{dF_{\pi\gamma\rightarrow\rho}(q^2)}{dq^2} \right|_{q^2=0} = 0.63(22) \text{ GeV}^{-2}$$

Photocoupling

$$G_{\rho\pi\gamma} = F_{\pi\gamma\rightarrow\rho}(0)$$

uncertainties:

- path integral ⊗
- spectrum ⊗
- R-mapping ⊗
- spacing ⊗
- m_π ⊗
- higher L ⊗



$$|G_{\rho\pi\gamma}| = 0.0802(32)(20)$$

some properties of the ρ @ ($m_\pi = 320$ MeV)

	$g_{\rho\pi\pi}$	$G_{\rho\pi\gamma}$	m_ρ
this study	5.69(20)	0.0802(38)	797(7)
PDG	5.98	0.0736(73)	775.26

- photoproduction: these and HadSpec results only [HadSpec 2015, 2016]
- comparison: apples to oranges
- lattice results still need extrapolation $m_\pi \rightarrow m_\pi^{phys}$
- missing: continuum limit
- qualitatively good

Future outlook

- coupled channel resonances? (technical challenge)

$$|\langle 1 | J | 2 \rangle|^2 = \begin{bmatrix} V_{\pi\gamma \rightarrow \pi\pi} & V_{\pi\gamma \rightarrow K\bar{K}} \end{bmatrix} \begin{bmatrix} R_{\pi\pi, \pi\pi} & R_{\pi\pi, K\bar{K}} \\ R_{K\bar{K}, \pi\pi} & R_{K\bar{K}, K\bar{K}} \end{bmatrix} \begin{bmatrix} V_{\pi\gamma \rightarrow \pi\pi} \\ V_{\pi\gamma \rightarrow K\bar{K}} \end{bmatrix}$$

- probe contents of resonances?
- other channels and resonances

Summary

- strong $\pi\pi$ scattering
- ρ photoproduction on π
- interesting future ahead

