

# Freeze-out in Au+Au@19.6GeV (UrQMD)

Sachenko D.I., Nigmatkulov G.A., Sinyukov Y.M.,  
Khyzhniak E.V.,

# We do we want to study?

- Emission function and other hypersurfaces for mesons and baryons.
- Particle freeze-out time and compare received results from femtoscopy analysis with time of maximum emission function

Methods of analyzing freeze-out time using femtoscopy analysis is presented in article of Y.M. Sinyukov et al. in 2015



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## On $m_T$ dependence of femtoscopy scales for meson and baryon pairs

Yu.M. Sinyukov <sup>\*</sup>, V.M. Shapoval, V.Yu. Naboka

*Bogolyubov Institute for Theoretical Physics, Metrolohichna str. 14b, 03680 Kiev, Ukraine*

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### Abstract

The  $m_T$ -dependencies of the femto-scales, the so-called interferometry and source radii, are investigated within the hydrokinetic model for different types of particle pairs — pion–pion, kaon–kaon, proton–proton and proton–lambda, — produced in Pb+Pb and  $p + p$  collisions at the LHC. In particular, such property of the femto-scales momentum behavior as  $m_T$ -scaling is studied for the systems with (w) and without (w/o) intensive transverse flow, and also w and w/o re-scattering at the final afterburner stage of the matter evolution. The detailed spatiotemporal description obtained within hydrokinetic model is compared with the simple analytical results for the spectra and longitudinal interferometry radii depending on the effective temperature on the hypersurface of maximal emission, proper time of such emission, and intensity of transverse flow. The derivation of the corresponding analytical formulas and discussion about a possibility for their utilization by the experimentalists for the simple femtoscopy data analysis is the main aim of this theoretical investigation.

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# Theory of analytical model for the interferometry radii

To get single particle spectra  $p_0 d^3 N / d^3 p$  and the correlation function of bosons  $C(p, q)$  we use the generalized Cooper-Frye method

$$p_0 \frac{d^3 N}{d^3 p} = \int_{\sigma_{m.e.}(p)} d\sigma_\mu p^\mu f_{l.eq.}(x, p), \quad (1)$$

$$C(p, q) \approx 1 + \frac{\left| \int_{\sigma_{m.e.}(k)} d\sigma_\mu k^\mu f_{l.eq.}(x, k) \exp(iqx) \right|^2}{\left( \int_{\sigma_{m.e.}(k)} d\sigma_\mu k^\mu f_{l.eq.}(x, k) \right)^2}, \quad (2)$$

Correlation function in *long* direction depends only on the parameter  $\alpha = R_v^2 / R_T^2$  and does not depend on the transverse velocity profile at the hypersurface of maximal emission.

Because of this, we will analyze and use only the longitudinal projection of the correlation function.

Then:

$$C(k, q_l, q_s = q_o = 0) = 1 + \frac{\exp\left[\frac{2}{\lambda^2} \left(1 - \sqrt{1 + \tau^2 \lambda^4 q_l^2}\right)\right]}{[1 + \tau^2 \lambda^4 q_l^2]^{3/2}} \xrightarrow{k_T \rightarrow \infty} 1 + \exp(-\lambda_l^2 q_l^2). \quad (3)$$

Where  $\lambda$  associated with the homogeneity length in longitudinal direction:

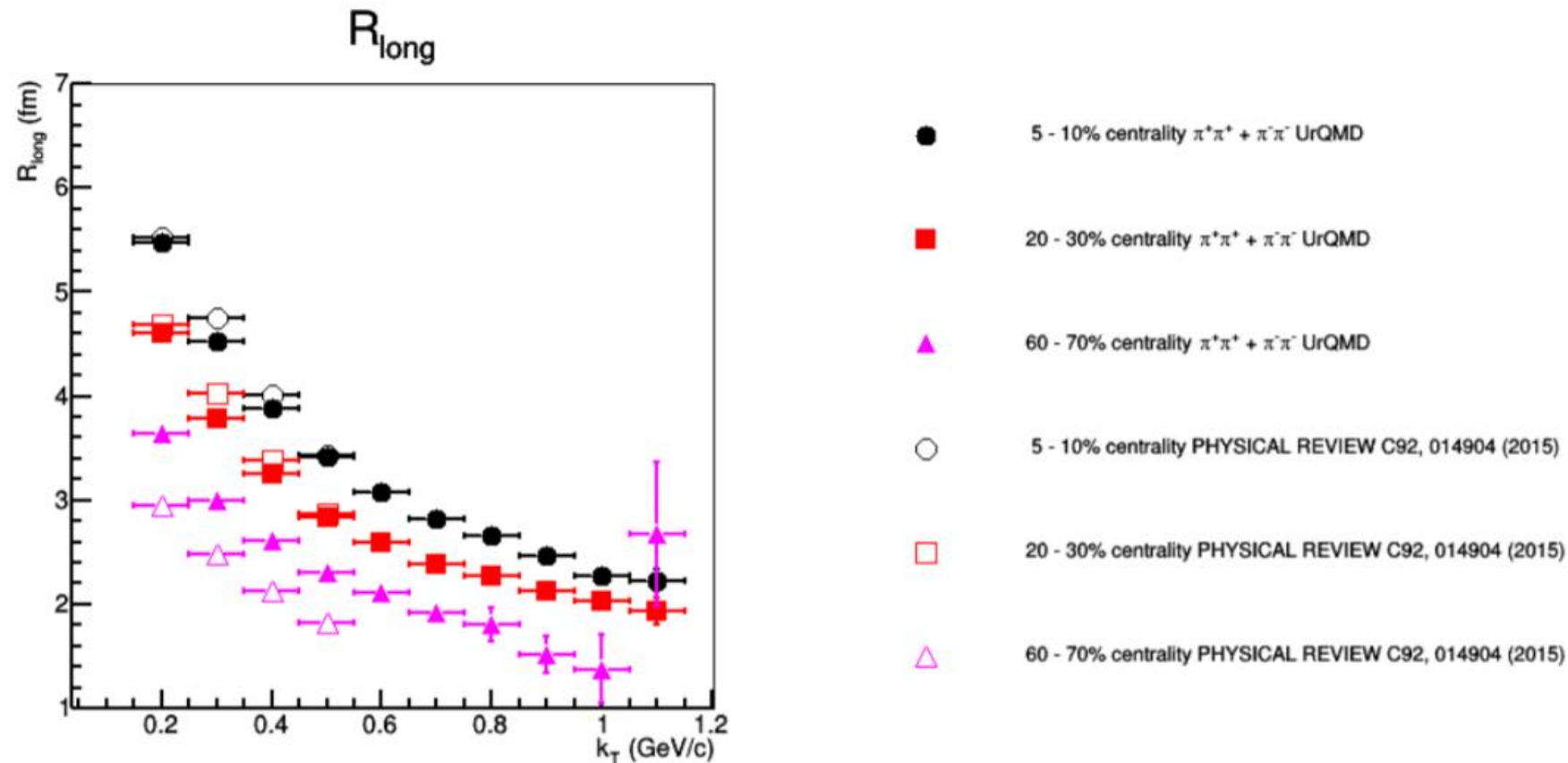
$$\lambda^2 = \frac{\lambda_l^2}{\tau^2} = \frac{T}{m_T} (1 - \bar{v}_T^2)^{1/2}, \quad (4) \text{ , where } \bar{v}_T = k_T / (m_T + \alpha T).$$

The approximation of the correlation function at small  $q_l$  leads to the following analytical result for the interferometry radii:

$$R_l^2(k_T) = \tau^2 \lambda^2 \left(1 + \frac{3}{2} \lambda^2\right) \quad (5)$$

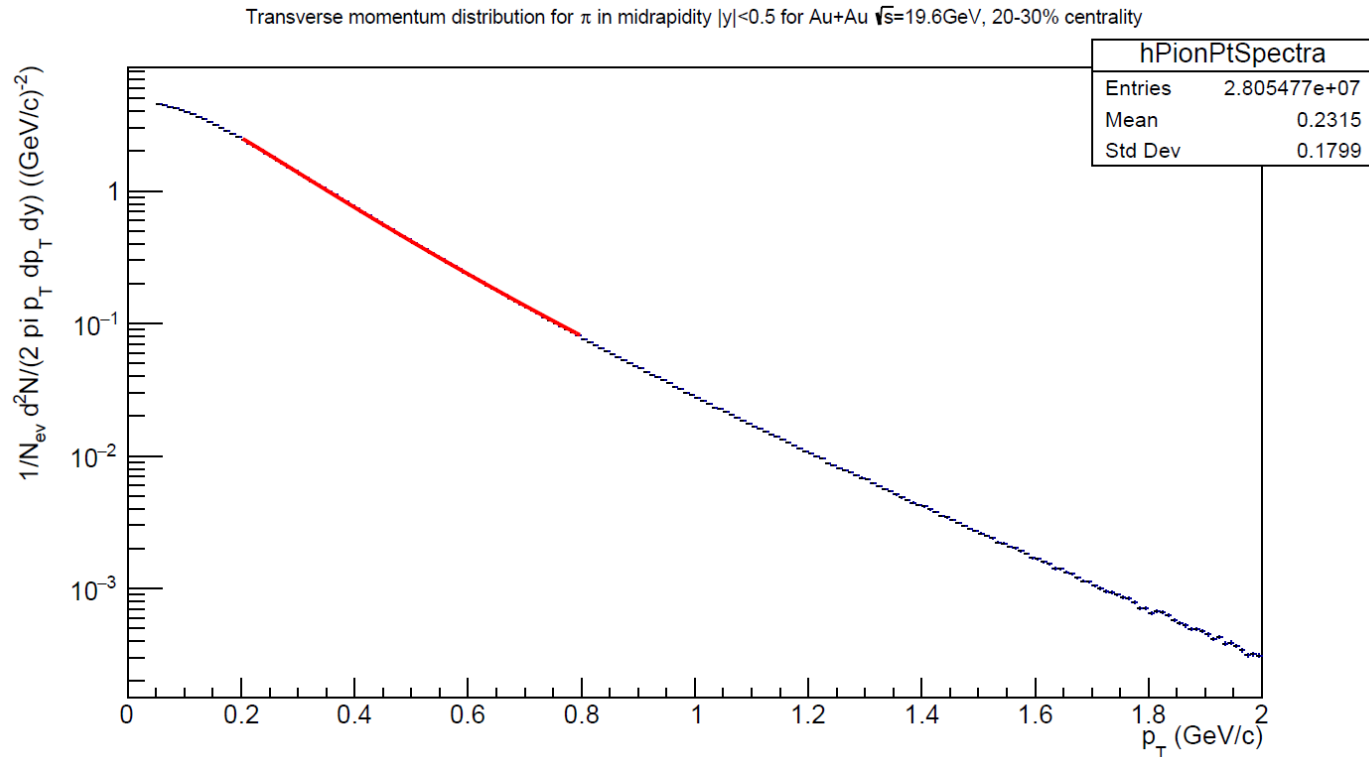
# Analytical fitting

Using femtoscopy analysis, Eugenia Khyzhniak had demonstrated radius dependence on transverse momentum of the pair for UrQMD and experimental data



In order to fit  $m_T$  dependence of longitudinal femtoscopy radius  $R_l$ , using formula (5), and extract  $\tau$ , is necessary to find Temperature  $T$  and parameter  $\alpha$ , which could be extracted from fit of pion momentum spectra

$$p_0 \frac{d^3 N}{d^3 p} \propto \exp[-(m_T/T + \alpha)(1 - \bar{v}_T^2)^{1/2}] \quad (6)$$



$T = 108.9$  MeV,  
 $\alpha = 7.32$

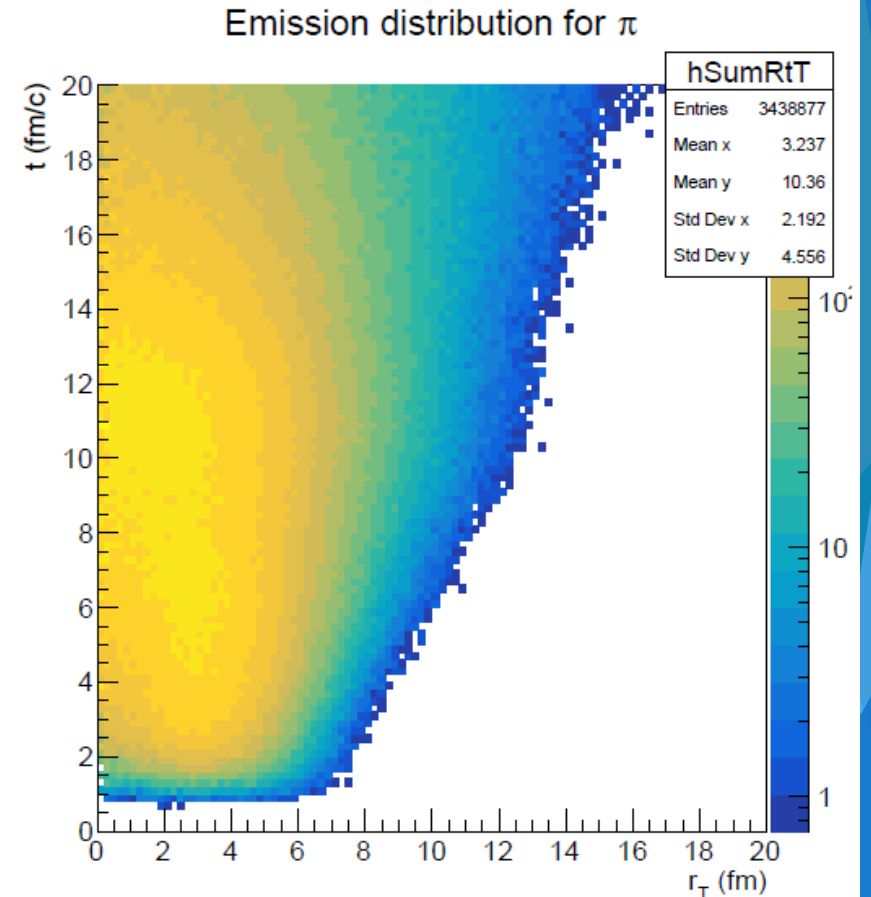
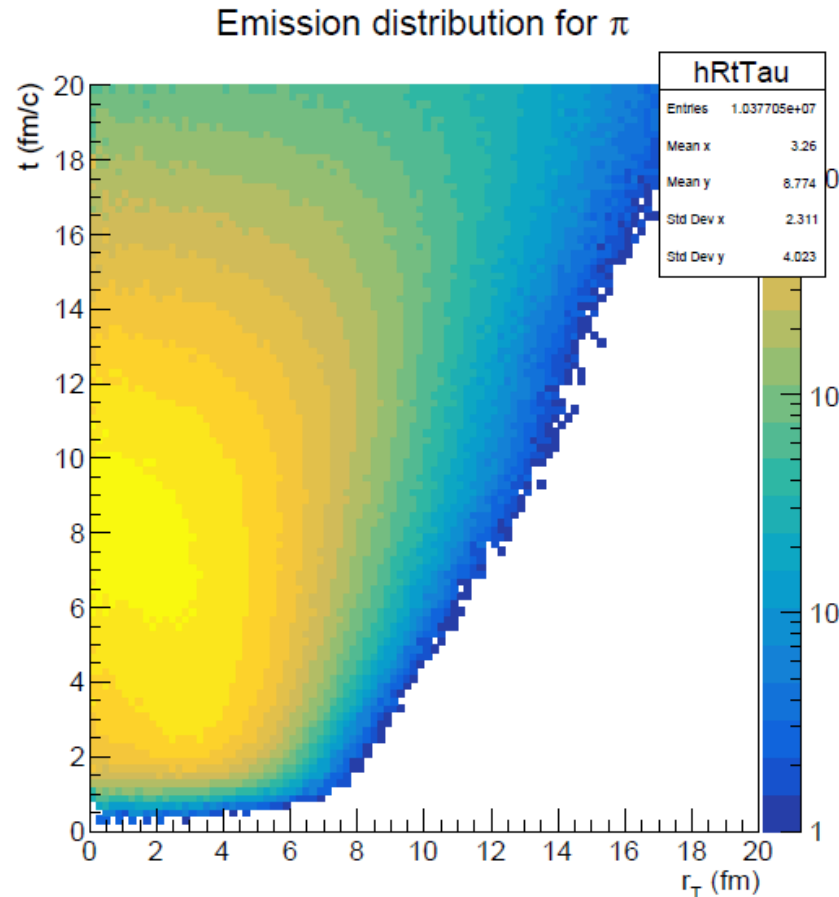
# Emission functions for pions

To compare freeze-out time of pions, obtained in different ways, we have to also analyse emission functions.

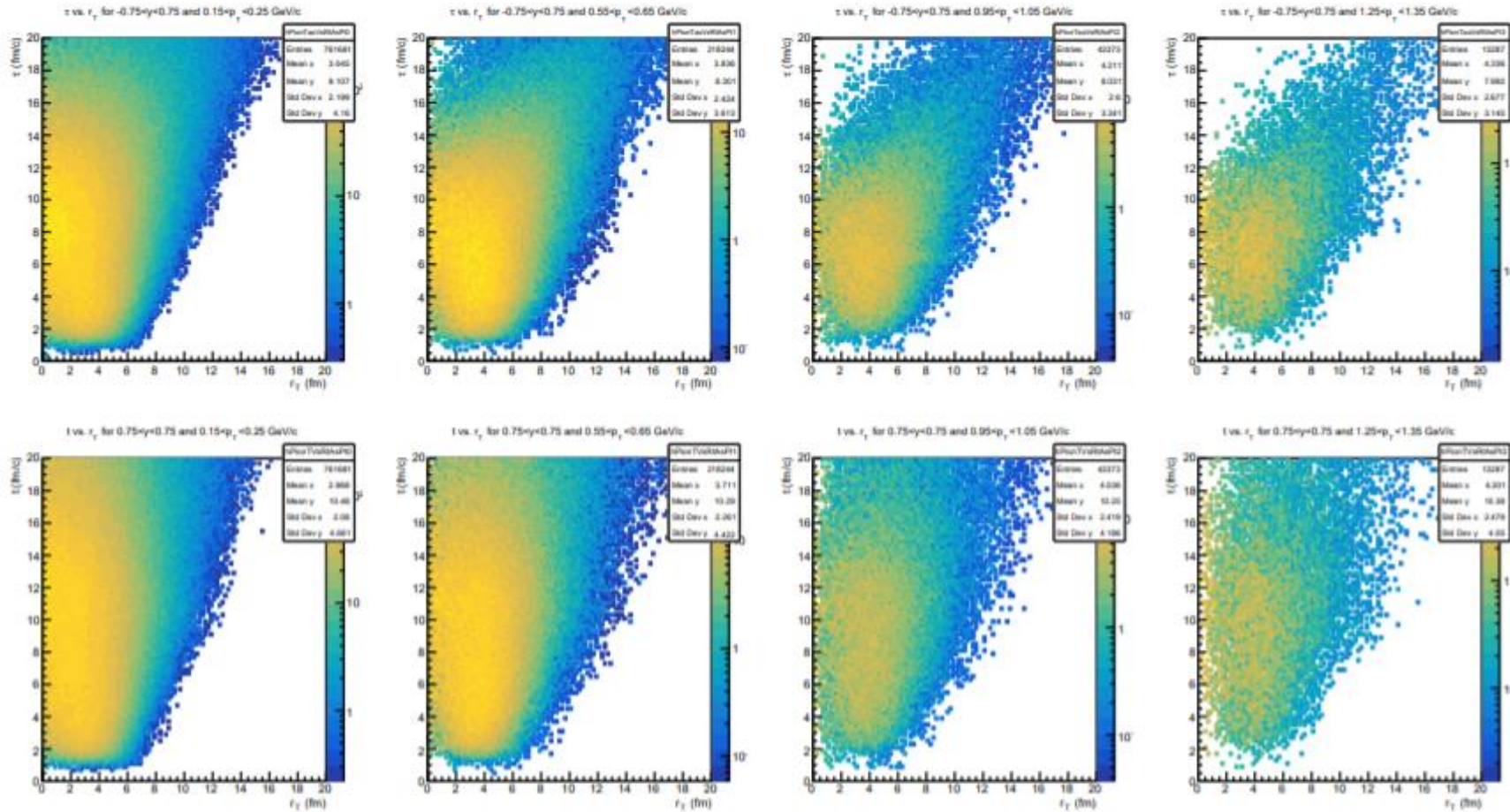
We studied the dependence of freeze-out time ( $t$  in Cartesian and

$\tau = \sqrt{t^2 - z^2}$  in hyperbolic coordinates) from transverse position of particle emission

$r_T = \sqrt{x^2 + y^2}$  for different  $p_T$  and  $\cos(\theta)$

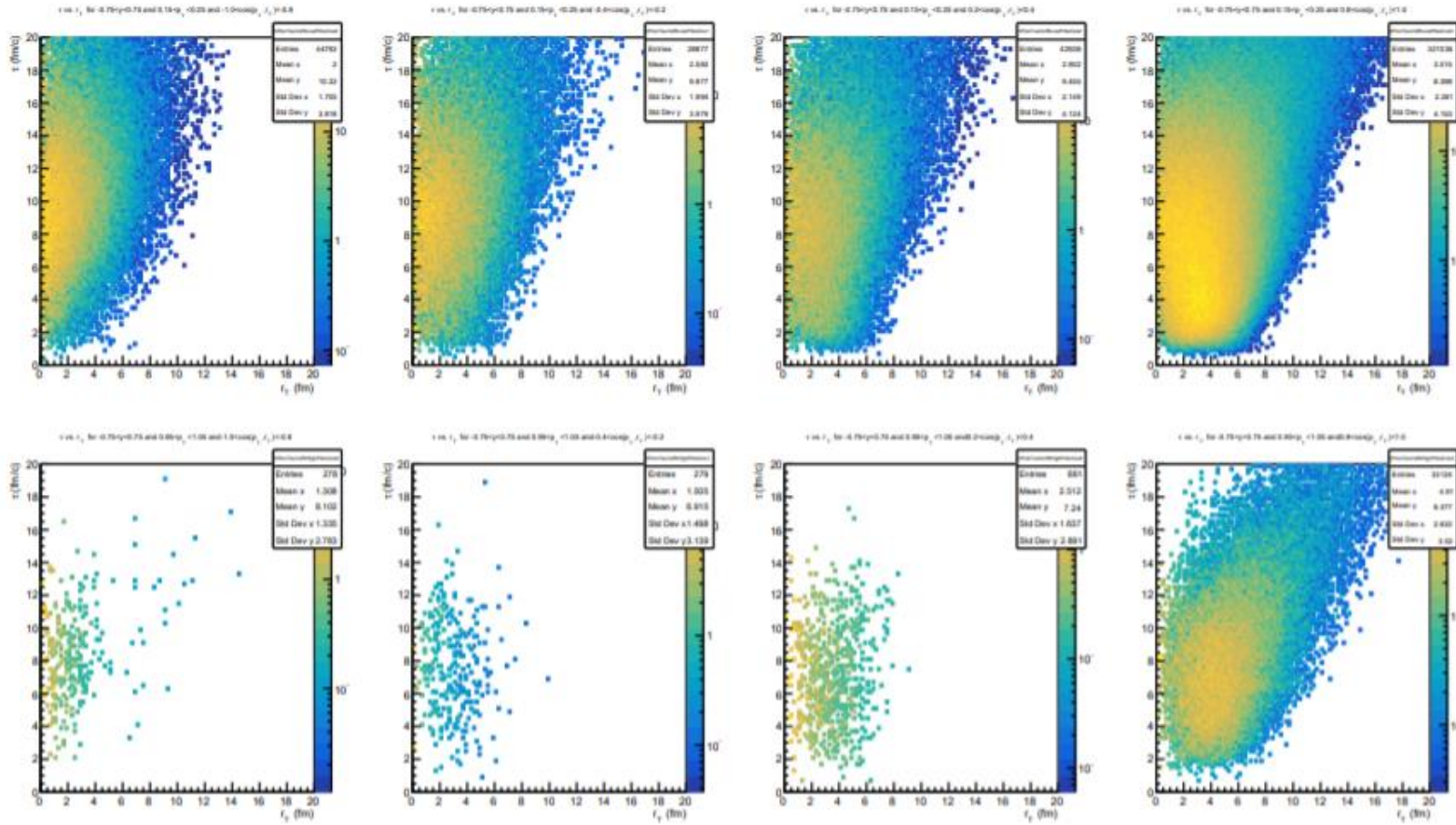






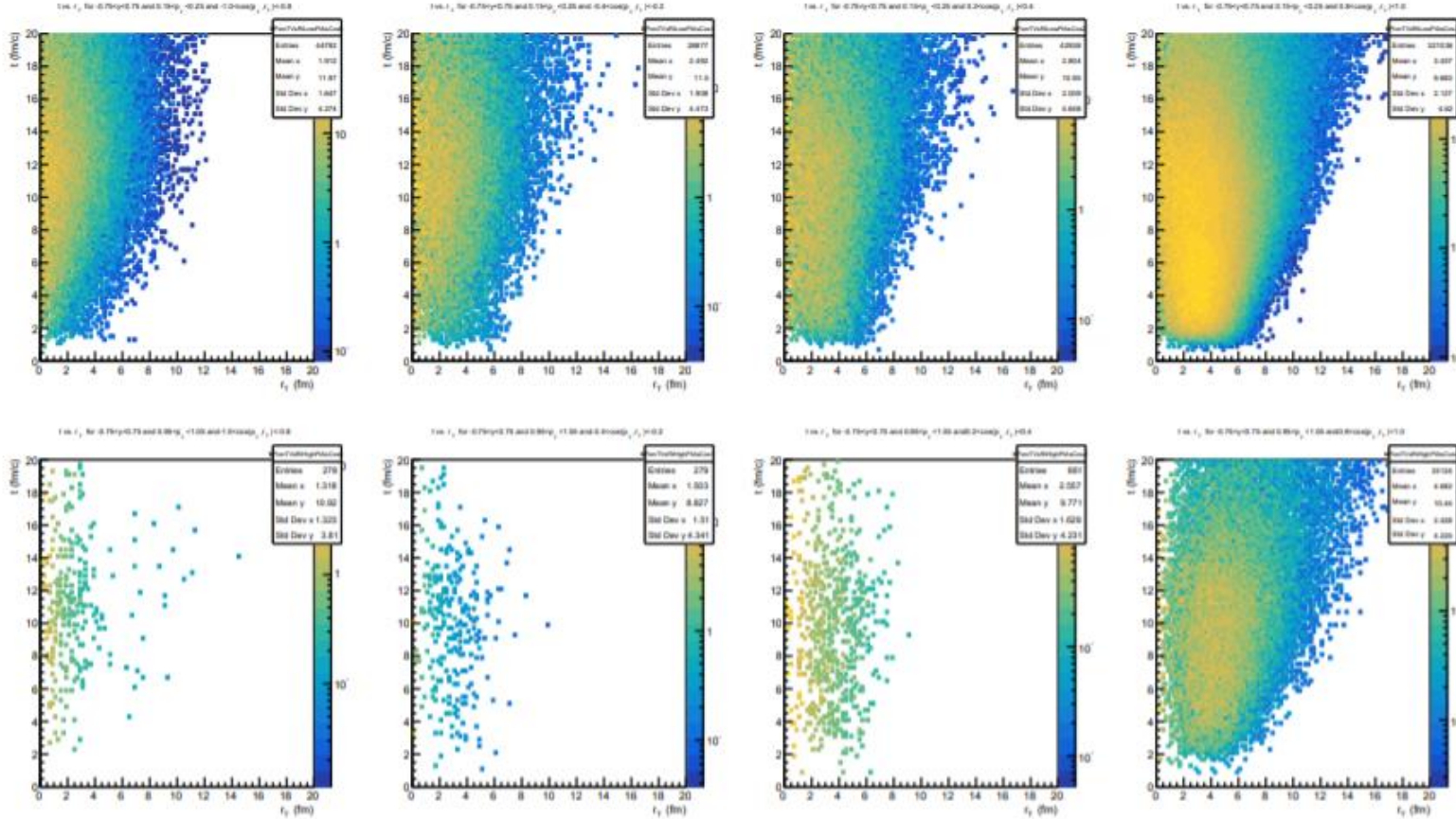
- The pion emission function for  $p_T \in (0.15 - 0.25)$ ,  $(0.55-0.65)$ ,  $(0.95-1.05)$ ,  $(1.25-1.35)$  GeV/c

•  $\tau$  VS  $r_T$



The pion emission function for  $\cos(p_T r_T) \in (-1; -0.8)$ ,  $(-0.4; -0.2)$ ,  $(0.2; 0.4)$ ,  $(0.8; 1.0)$  for low  $p_T \in (0.15; 0.25)$  and high  $p_T \in (0.95; 1.05)$

- t vs  $r_T$



The pion emission function for  $\cos(p_T r_T) \in (-1; -0.8)$ ,  $(-0.4; -0.2)$ ,  $(0.2; 0.4)$ ,  $(0.8; 1.0)$  for low  $p_T \in (0.15; 0.25)$  and high  $p_T \in (0.95; 1.05)$

## Summary

- 20-30% most central Au+Au collisions at 19.6 GeV have been simulated using UrQMD model
- Emission function have been studied as a function of  $p_T$  and  $\cos(p_T, r_T)$
- Lower  $p_T$  particles are emitted closer to the center
- Particles that are moving along emission direction are emitted earlier and from the surface
- Necessary parameters for fitting  $m_T$  dependence of longitudinal femtoscropy radius  $R_l$  have been extracted:  $T = 108.9\text{MeV}$ ,  $\alpha = 7.32$

## Outlook

- Simulate Au+Au@19.6 GeV, @11.5GeV, @7.7GeV (9 centrality ranges)
- Extract from fit of  $m_T$  dependence of longitudinal femtoscropy radius  $R_l$  time and compare this with time of maximum emission function.
- Study other hypersurfaces and particle species

# Thank you for your attention!