

Experimental QCD at future pp & e⁺e⁻ colliders

**Strong interactions
ESPP Update**
Granada, May 2019

**David d'Enterria
(CERN)**

Future pp & e⁺e⁻ colliders with QCD programme

► Future proton-proton colliders:

1. HL-LHC: pp(14 TeV), 3 ab⁻¹

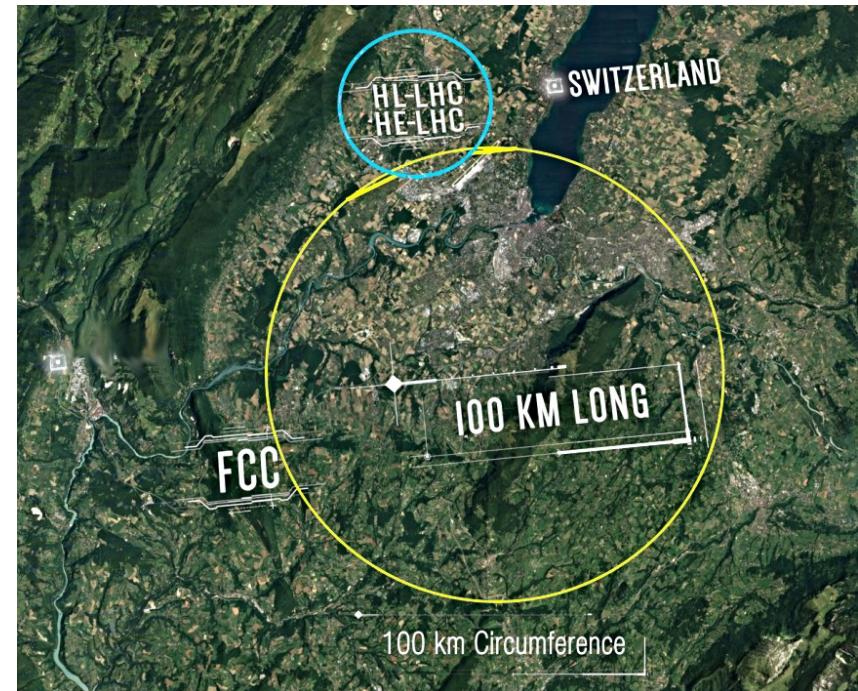
ESPPU input #110, #152

2. HE-LHC: pp(27 TeV), 10–15 ab⁻¹

ESPPU input #160

3. FCC-hh: pp(100 TeV), 20 ab⁻¹

ESPPU input #135



► Future electron-positron colliders:

4. FCC-ee: e⁺e⁻(90–350 GeV), 1–100 ab⁻¹

ESPPU input #160

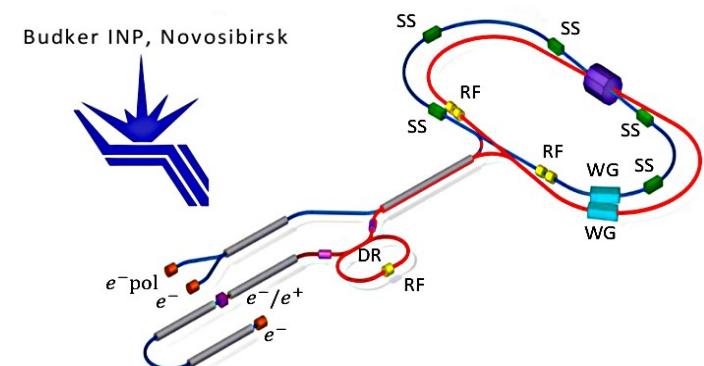
5. SCT (Super Charm-Tau) Factory:

e⁺e⁻(2–6 GeV), ~1 ab⁻¹

ESPPU input #132

[Note: Other QCD machines: DIS, heavy-ions and/or fixed-target, covered by other talks].

[Note: Also CEPC, ILC, CLIC, BELLE-II possibilities, but to be developed]



QCD = Key piece at future ee, pp colliders

► Though QCD is *not per se* the main driving force behind future colliders, QCD is crucial for many pp, ee measurements (signals & backgrounds):

- High-precision α_s : Affects all x-sections & decays (esp. Higgs, top, EWPOs).
- NⁿLO corrs., NⁿLL resummations: Affects all pQCD x-sections & decays.
- High-precision PDFs: Affects all precision W,Z,H (**mid-x**) measurements & all searches (**high-x**) in pp collisions.
- Heavy-Quark/Quark/Gluon separation (jet substructure, boosted topologies..): Needed for all **precision SM** measurements & **BSM** searches with final jets.
- Semihard QCD (low-x gluon saturation, multiple hard parton interactions,...): Leading x-sections at FCC-pp (Note: $Q_0 \sim 10$ GeV at 100 TeV).
- Non-perturbative QCD: Affects final-states with jets: Colour reconnection, $e^+e^- \rightarrow Z, WW$, $t\bar{t}$ → 4j, 6j... (m_W, m_{top} extractions). Parton hadronization,...

QCD physics at future pp & e⁺e⁻ machines

(1) QCD coupling

(FCC-ee, SCT, FCC-pp)

(2) Parton Distribution Functions

(HL-LHC, HE-LHC, FCC-hh)

(3) Jet substructure & flavour tagging

(FCC-ee, FCC-pp)

(4) Non-perturbative QCD

(FCC-ee, SCT, HL-LHC)

NOTE: Only UNIQUE QCD measurements, inaccessible at any current machine, are covered.

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Importance of the QCD coupling α_s

- Least-known of couplings: $\delta\alpha \sim 10^{-10} \ll \delta G_F \ll 10^{-7} \ll \delta G \sim 10^{-5} \ll \delta\alpha_s \sim 10^{-3}$
- Impacts all QCD x-sects.&decays. Leading param. uncert. H, t, EWPOs:

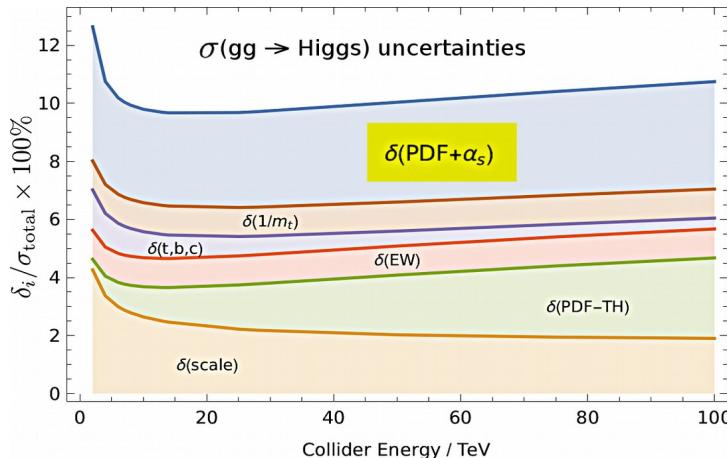
Decay	Partial width [keV]	current unc. $\Delta\Gamma/\Gamma$ [%]		
		Th _{Intr}	Th _{Par(m_q)}	Th _{Par(α_s)}
$H \rightarrow b\bar{b}$	2379	< 0.4	1.4	0.4
$H \rightarrow c\bar{c}$	118	< 0.4	4.0	0.4
$H \rightarrow gg$	335	3.2	< 0.2	3.7

Msbar mass error budget (from threshold scan)			
$(\delta M_t^{\text{SD-low}})^{\text{exp}}$	$(\delta M_t^{\text{SD-low}})^{\text{theo}}$	$(\delta \bar{m}_t(\bar{m}_t))^{\text{conversion}}$	$(\delta \bar{m}_t(\bar{m}_t))^{\alpha_s}$
40 MeV	50 MeV	7 – 23 MeV	70 MeV
⇒ improvement in α_s crucial			$\delta\alpha_s(M_z) = 0.001$
Quantity FCC-ee future param.unc. Main source			
Γ_Z [MeV]	0.1	0.1	$\delta\alpha_s$
R_b [10^{-5}]	6	< 1	$\delta\alpha_s$
R_ℓ [10^{-3}]	1	1.3	$\delta\alpha_s$

Sven Heinemeyer – 1st FCC physics workshop, CERN, 17.01.2017

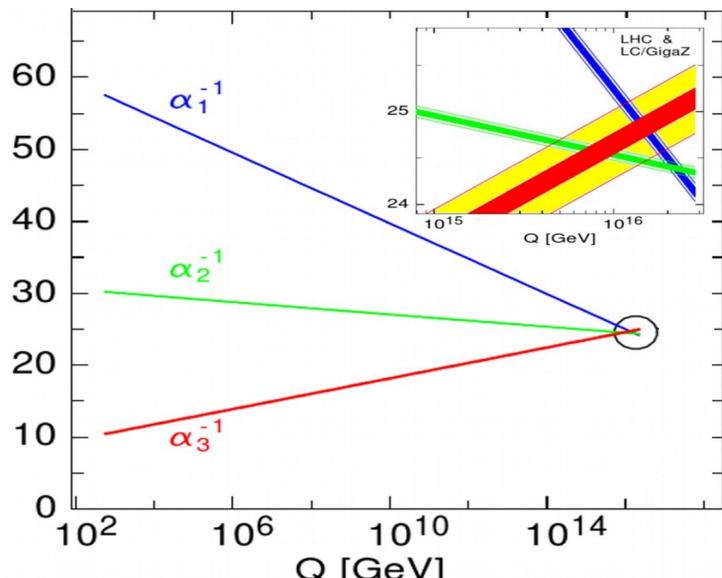
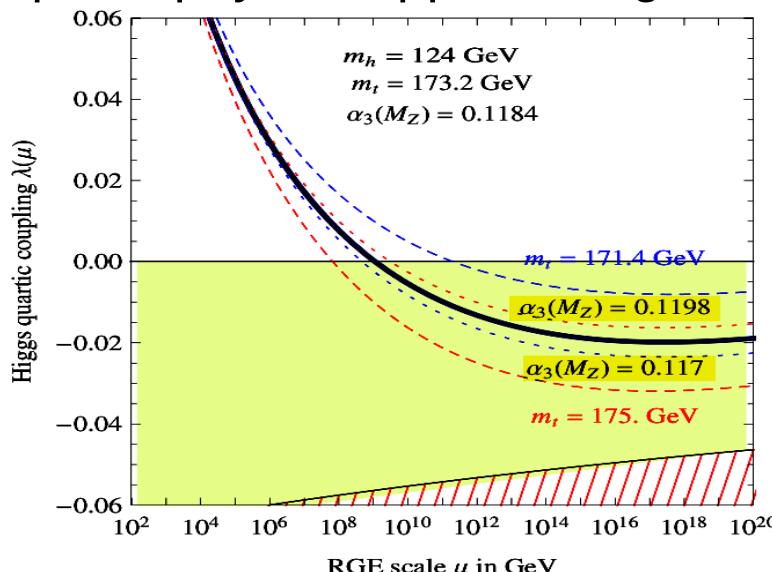
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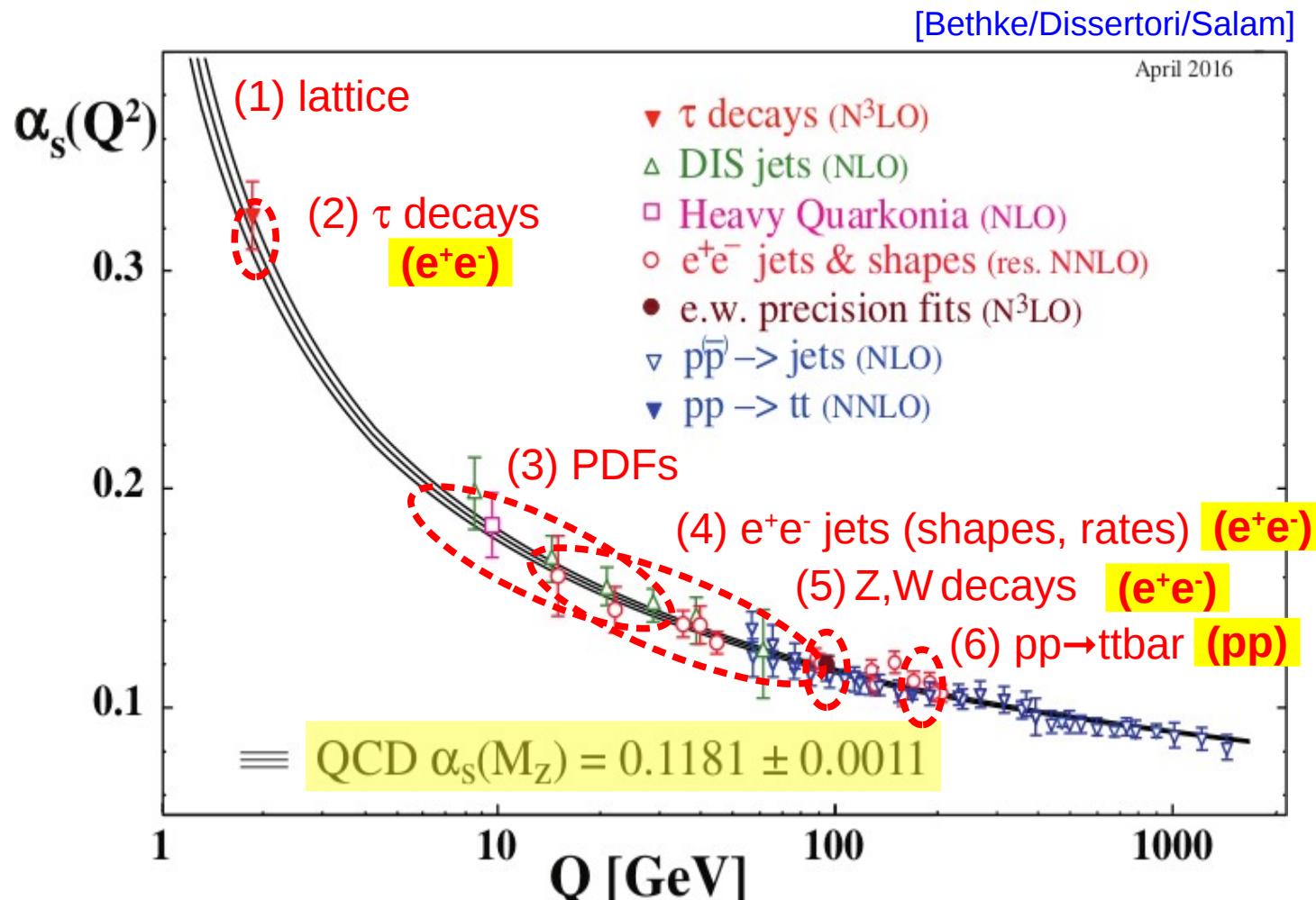
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- Impacts physics approaching Planck scale: EW vacuum stability, GUT



World α_s determination (PDG 2018)

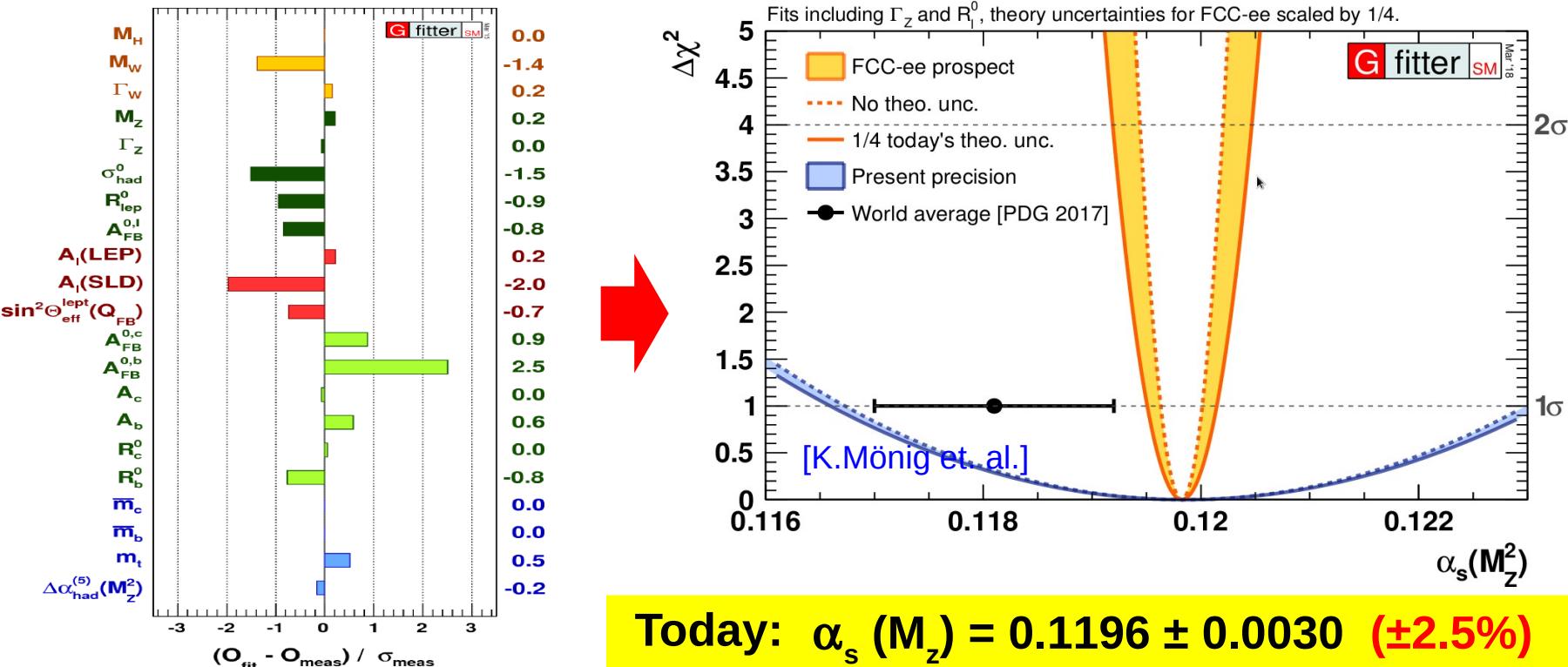
- Determined today by comparing 6 experimental observables to pQCD NNLO,N³LO predictions, plus global average at the Z pole scale:



α_s via hadronic Z decays (FCC-ee)

- Computed at **N³LO**: $R_Z \equiv \frac{\Gamma(Z \rightarrow h)}{\Gamma(Z \rightarrow l)} = R_Z^{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n \left(\frac{\alpha_s}{\pi}\right)^n + \mathcal{O}(\alpha_s^5)) + \delta_m + \delta_{\text{np}}$
- LEP Z pseudobservables: $R_\ell^0 = \frac{\Gamma_{\text{had}}}{\Gamma_\ell}$, $\sigma_{\text{had}}^0 = \frac{12\pi}{m_Z} \frac{\Gamma_e \Gamma_{\text{had}}}{\Gamma_Z^2}$, $\sigma_\ell^0 = \frac{12\pi}{m_Z} \frac{\Gamma_\ell^2}{\Gamma_Z^2}$ (exp. unc. <0.1%)

Also after Higgs discovery, α_s can be directly determined from **full fit of SM**:



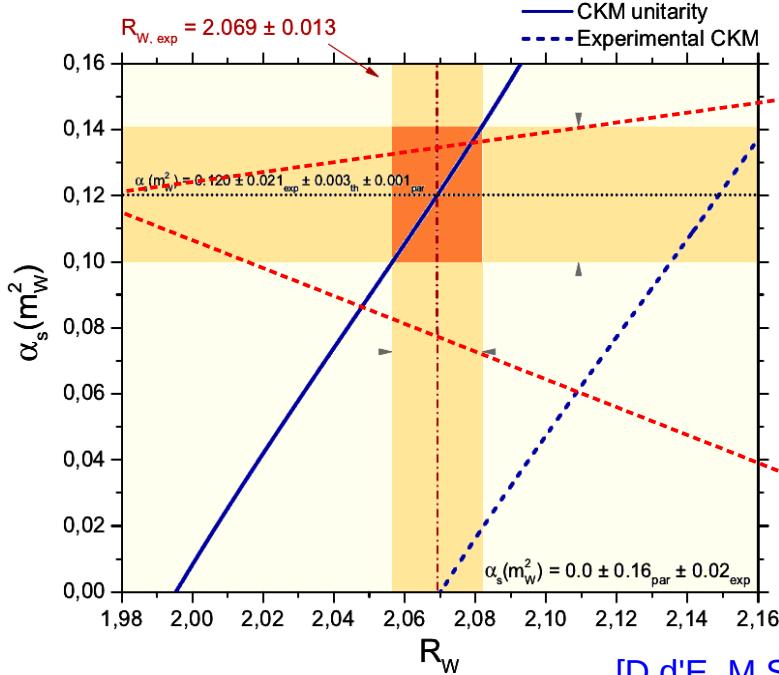
- FCC-ee: – Z stats ($\times 10^5$ LEP) will lead to: $\delta\alpha_s < 0.15\%$
 - TH (parametric) uncertainties: $\sin^2\theta_{\text{eff}}, m_W, m_{\text{top}}$

α_s via hadronic W decays (FCC-ee)

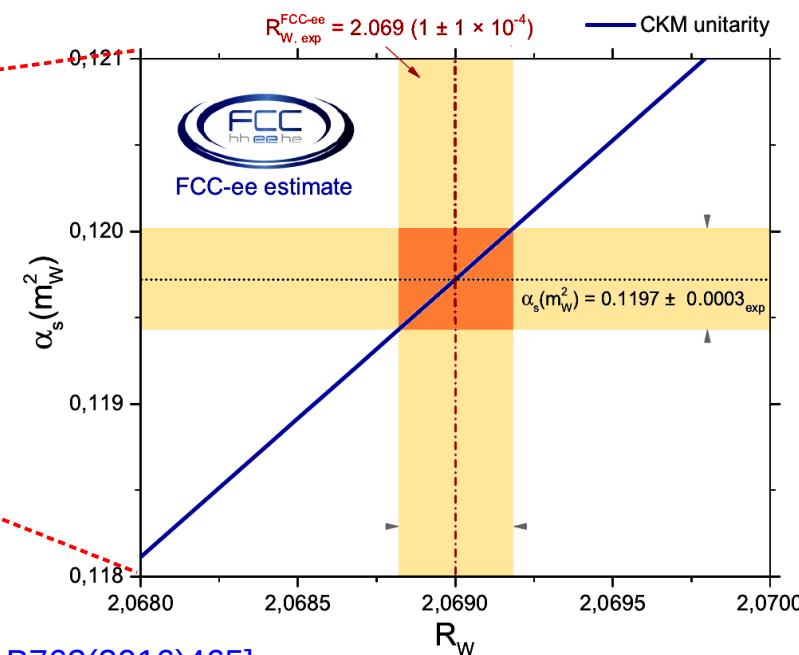
- Computed at N^{2,3}LO: $\Gamma_{W,\text{had}} = \frac{\sqrt{2}}{4\pi} G_F m_W^3 \sum_{\text{quarks } i,j} |V_{i,j}|^2 \left[1 + \sum_{k=1}^4 \left(\frac{\alpha_s}{\pi} \right)^k + \delta_{\text{electroweak}}(\alpha) + \delta_{\text{mixed}}(\alpha \alpha_s) \right]$
- LEP: $\text{BR}_W = 0.6741 \pm 0.0027 (\pm 0.4\%)$

Extraction with large exp. & parametric
(CKM V_{cs}) uncertainties:

Today: $\alpha_s(M_z) = 0.117 \pm 0.040 (\pm 35\%)$



[D.d'E, M.Srebre, PLB763(2016)465]

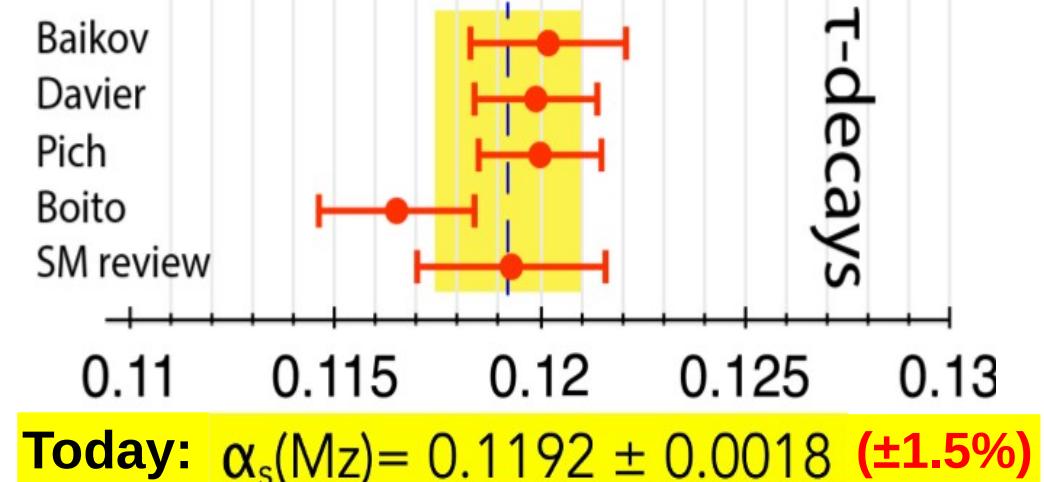


- FCC-ee: – Huge W stats ($\times 10^4$ LEP) will lead to: $\delta \alpha_s < 0.2\%$
– TH (param.) uncertainty: $|\delta V_{cs}|$ to be significantly improved (10^{-4})

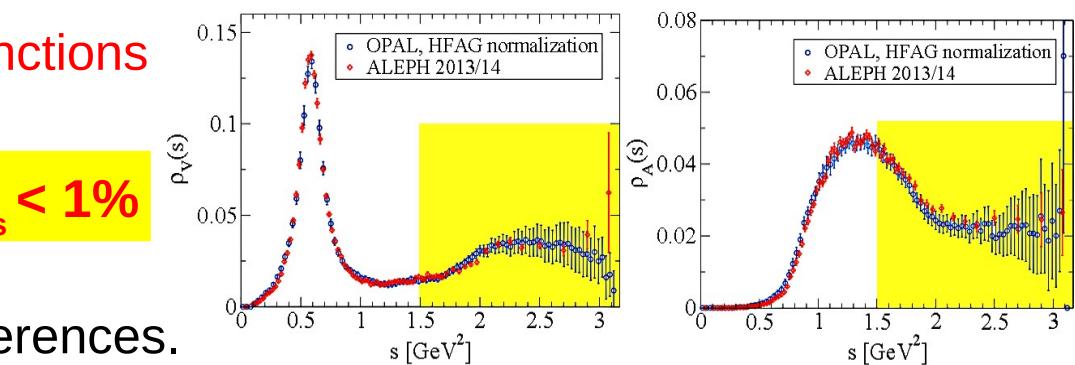
α_s from hadronic τ decays (SCT, FCC-ee)

- Computed at N³LO: $R_\tau \equiv \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} = S_{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n \left(\frac{\alpha_s}{\pi}\right)^n + \mathcal{O}(\alpha_s^5)) + \delta_{\text{np}}$
- Experimentally: $R_{\tau, \text{exp}} = 3.4697 \pm 0.0080 (\pm 0.23\%)$

- Various pQCD approaches (FOPT vs CIPT) & treatment of non-pQCD corrections (note: $(\Lambda/m_\tau)^2 \sim 1\%$), yield different results.



- Future prospects:
 - Better experimental spectral functions (high stats & better precision):
 - SCT: $\mathcal{O}(10^{10}) e^+ e^- \rightarrow \tau\tau$
 - FCC-ee: $\mathcal{O}(10^{11})$ from $Z(\tau\tau)$
 - Understand FOPT vs CIPT differences.



α_s running at the TeV scale (FCC-pp)

- Jets from pp collisions above LHC energies provide the only known means to **test asymptotic freedom & new coloured sectors above ~ 3 TeV**:

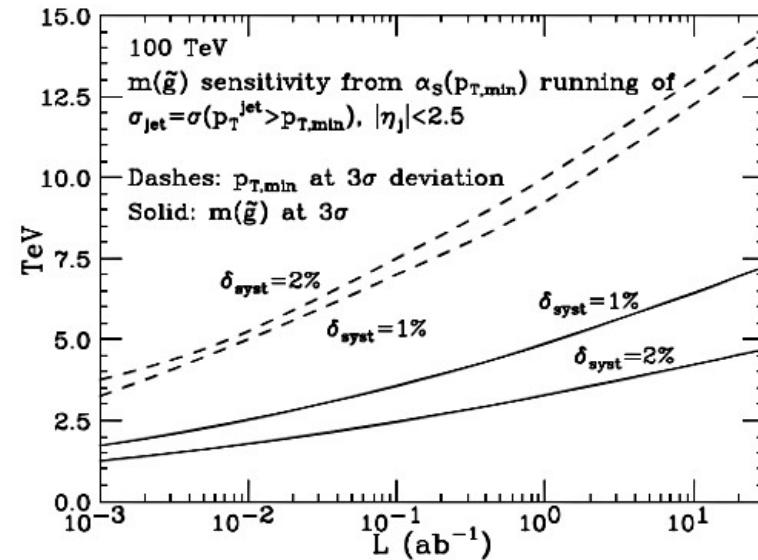
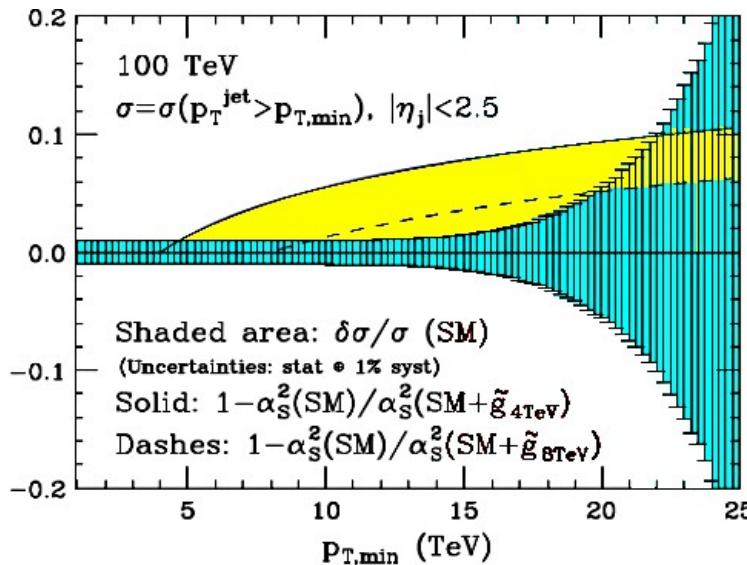


Figure 5.5: Left plot: combined statistical and 1% systematic uncertainties, at 30 ab^{-1} , vs p_T threshold; these are compared to the rate change induced by the presence of 4 or 8 TeV gluinos in the running of α_S . Right plot: the gluino mass that can be probed with a 3σ deviation from the SM jet rate (solid line), and the p_T scale at which the corresponding deviation is detected.

- FCC-pp:
 - Jet cross sections with <10% stat. uncert. up to $p_T \sim 25$ TeV
 - Sensitivity to $m_g = 4-8$ GeV gluinos in α_s running.

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(FCC-ee, FCC-pp, SCT)

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(4) Non-perturbative QCD

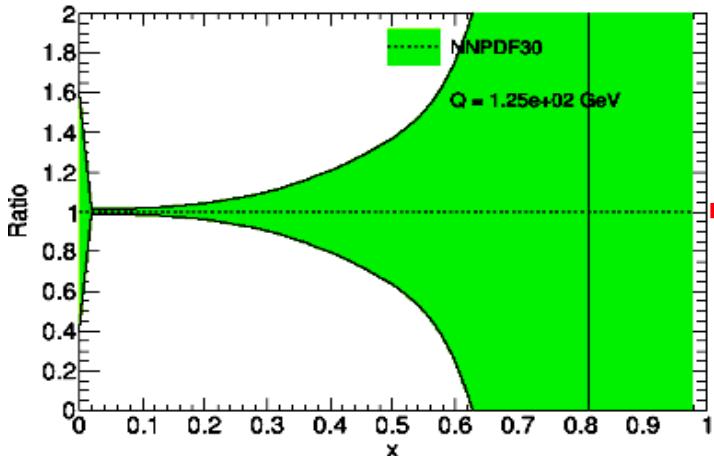
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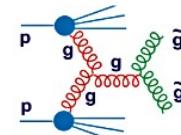
PDFs impact on new BSM / QCD physics

New physics at high- x ?

$xg(x,Q)$, comparison

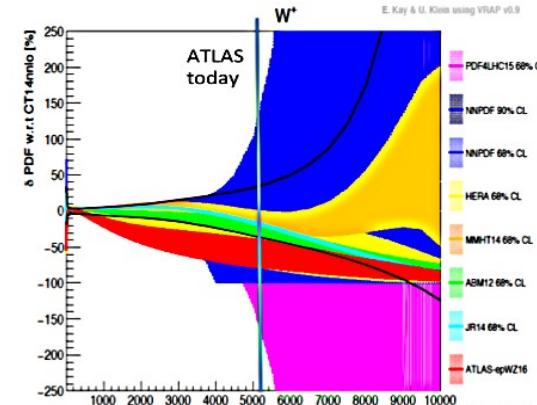
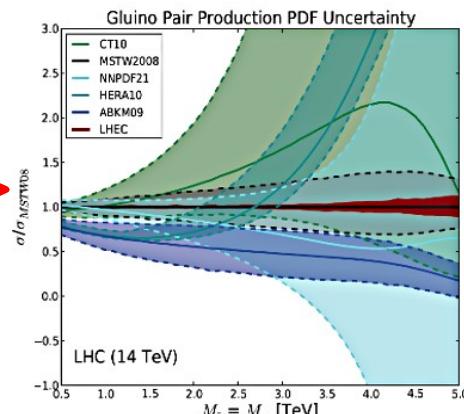


GLUON
SUSY, RPC, RPV, LQS..



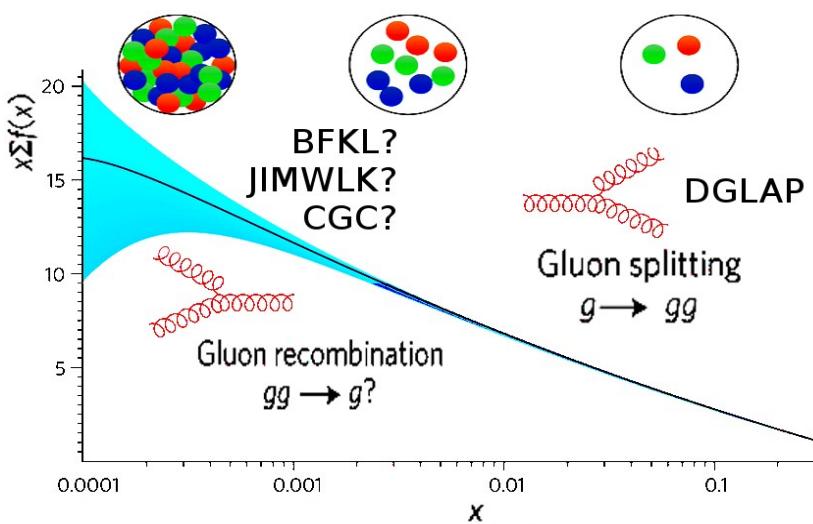
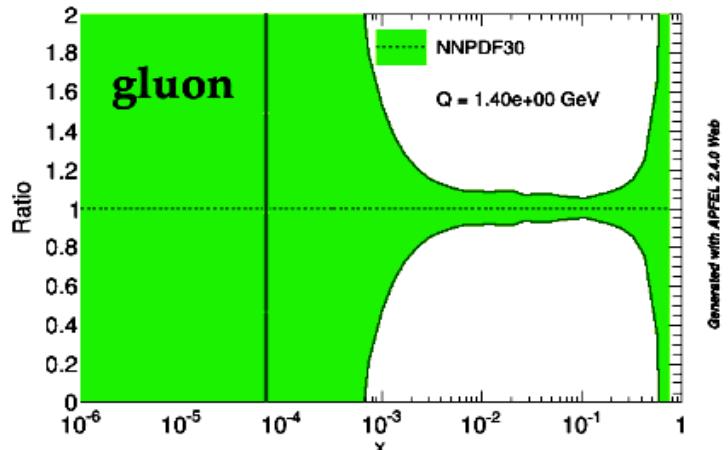
QUARKS

Exotic+ Extra boson searches at high mass



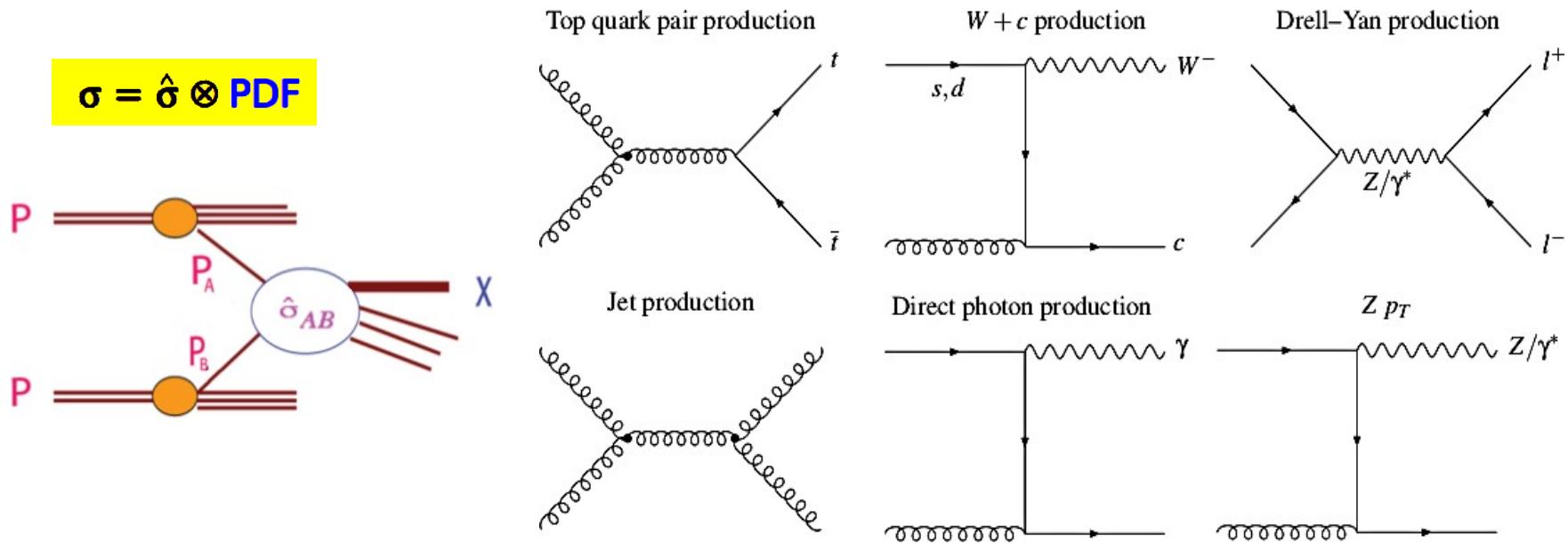
New QCD evolution at low- x ?

$xg(x,Q)$, comparison

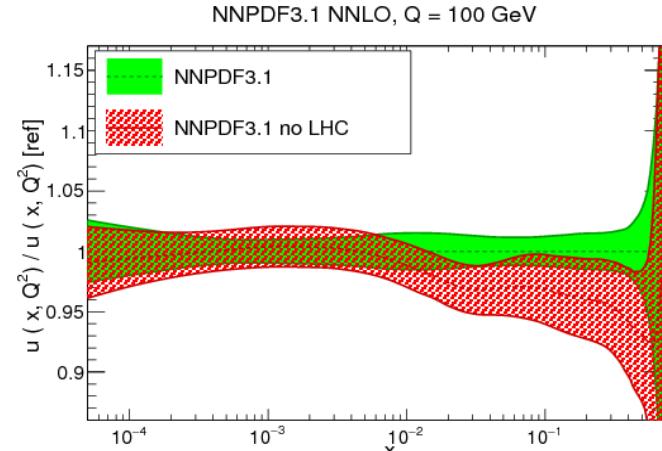
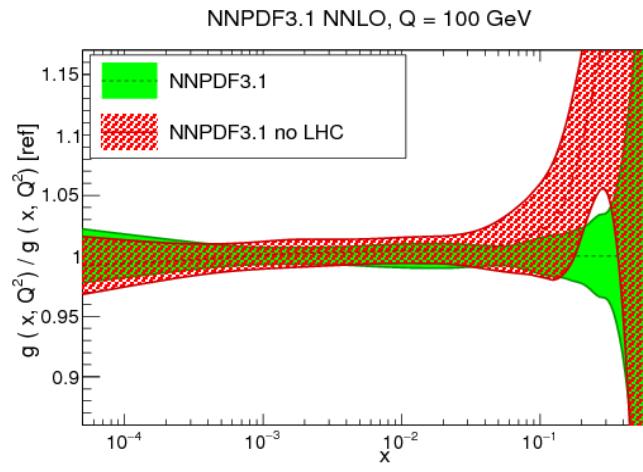


Improving PDFs with proton-proton data

- 6 partonic processes in pp at the LHC have provided key PDF constraints:

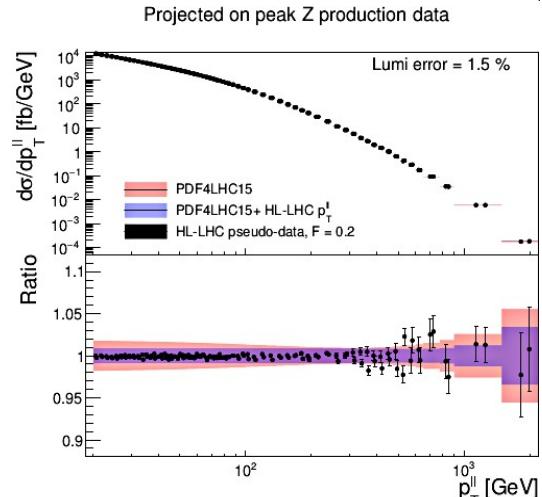
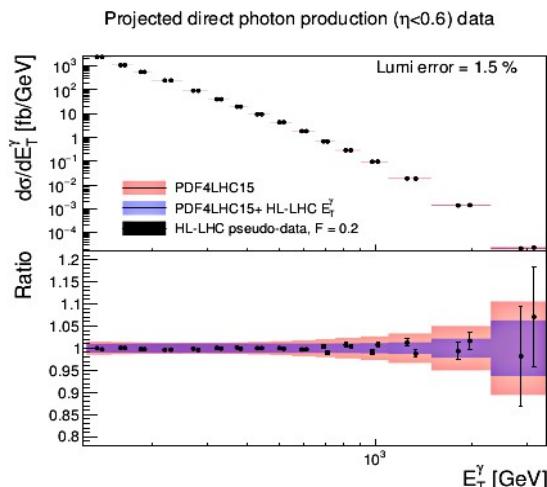
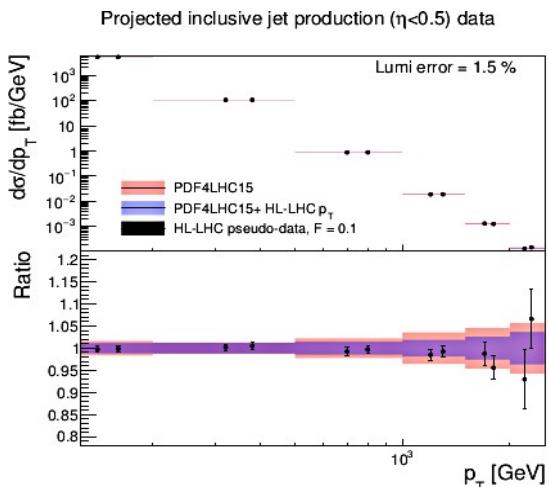
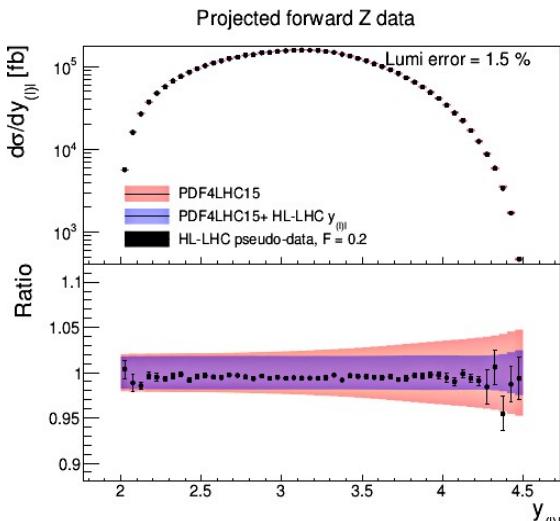
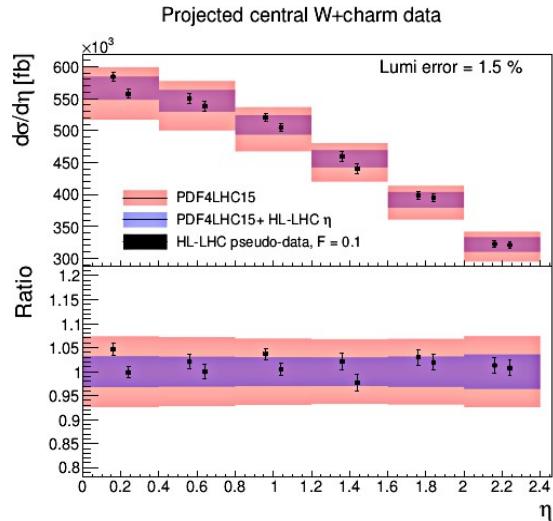
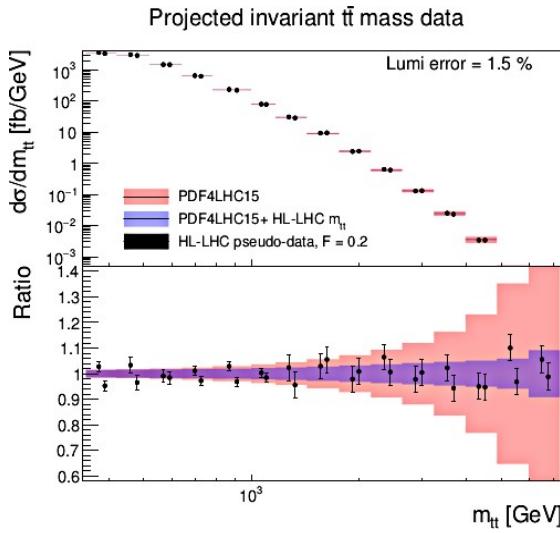


- Improved NNLO
 g , u , ... PDFs
already today
using LHC data:



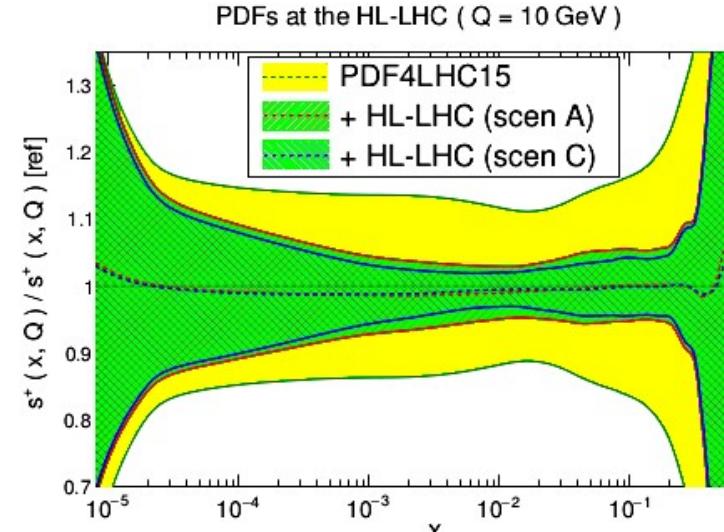
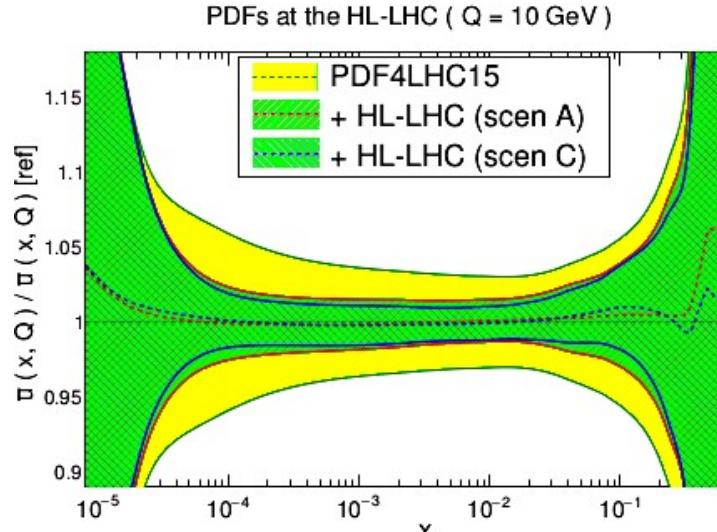
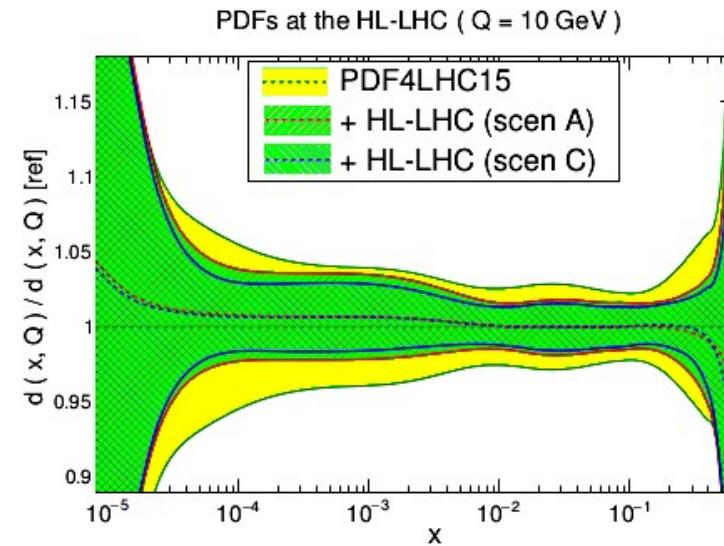
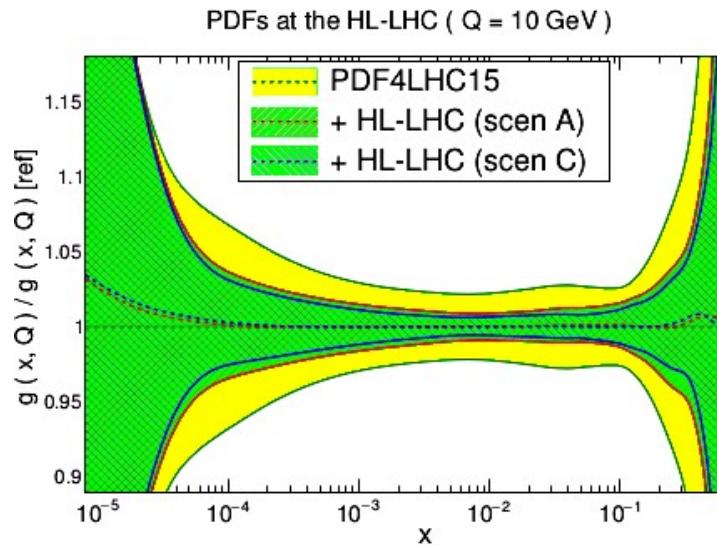
Improved PDFs with pp data (HL-LHC)

■ Generation of HL-LHC pQCD pseudo-data (pp, 3 ab⁻¹):



■ Significant constraining power in many phase space regions.

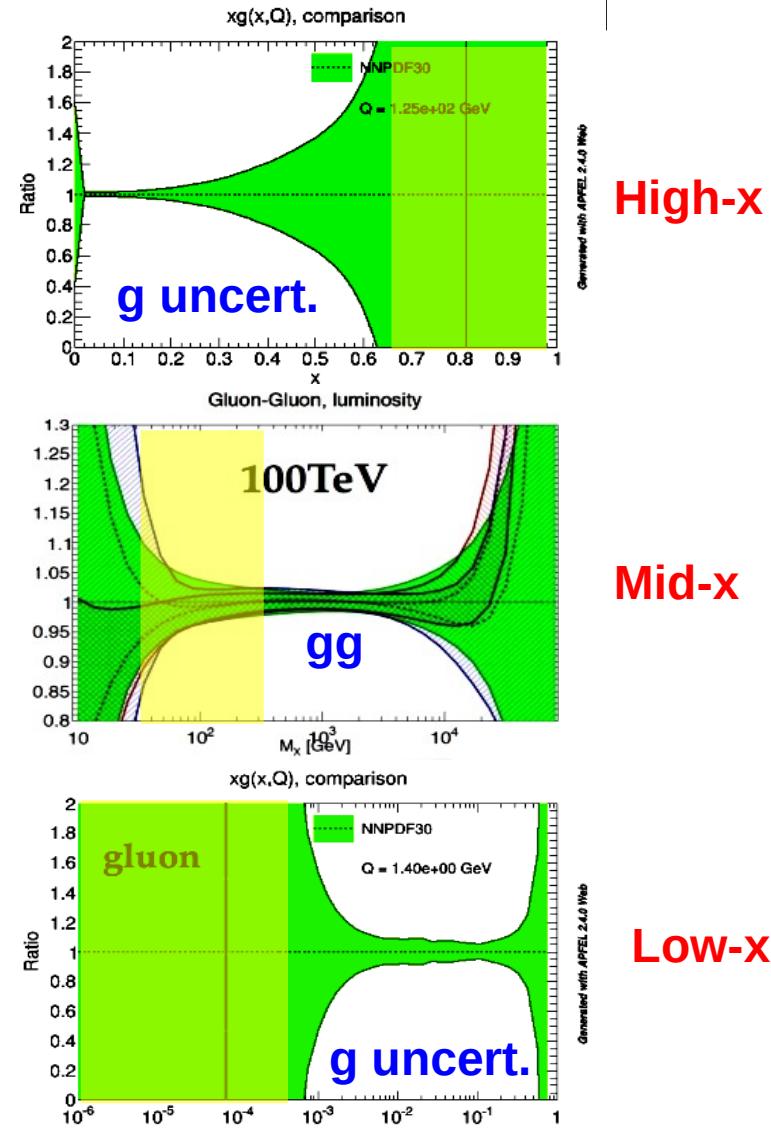
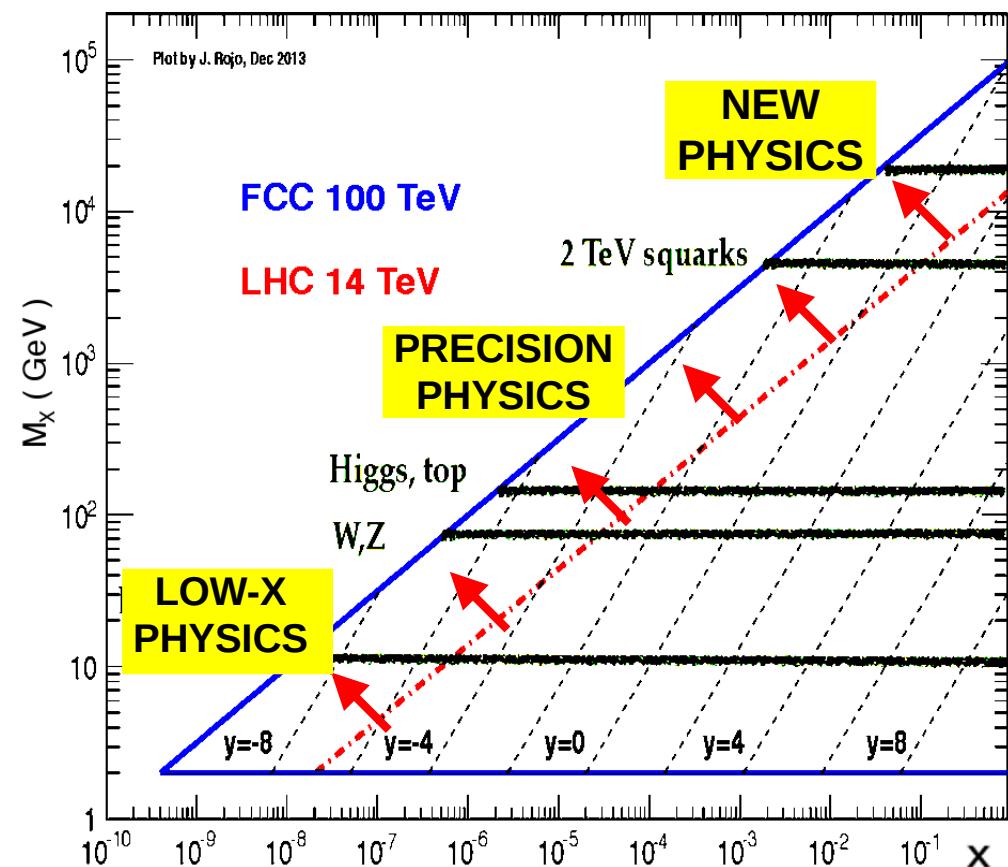
Improved PDFs with pp data (HL-LHC)



- Significant (factor ~ 2) PDF uncertainty reduction (with little dependence on projected systematics). But not at very low-,high- x ...

PDFs: Still work to do for FCC...

- Still large PDF uncertainties in pp at 100 TeV in key (x, Q^2) regions:



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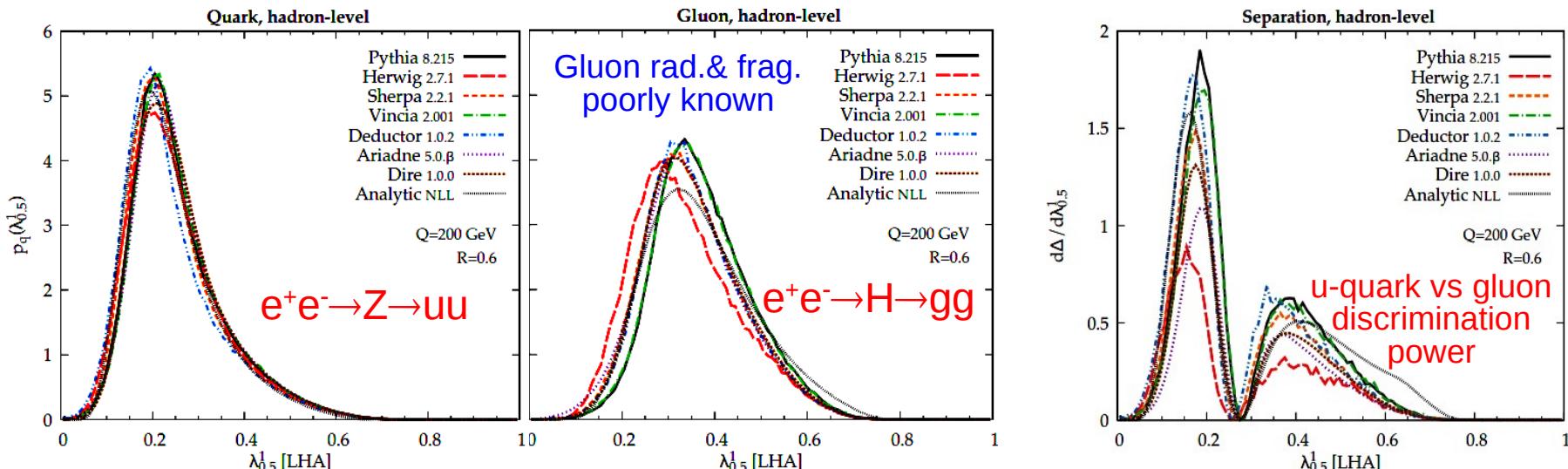
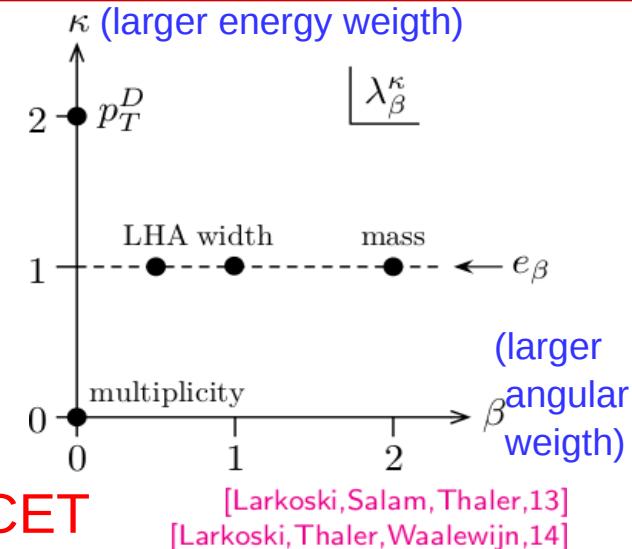
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Precise jet substruct. & flavour tagging (FCC-ee)

- State-of-the-art jet substructure studies based on **angularities** (normalized $E^n \times \theta^n$ products)
- "Sudakov"-safe variables of **jet constituents**: multiplicity, LHA, width/broadening, mass/thrust, C-parameter,...
- $k=1$: IRC-safe computable ($N^n\text{LO}+N^n\text{LL}$) via SCET (but uncertainties from non-pQCD effects)
- MC parton showers differ on gluon (less so quark) radiation patterns:

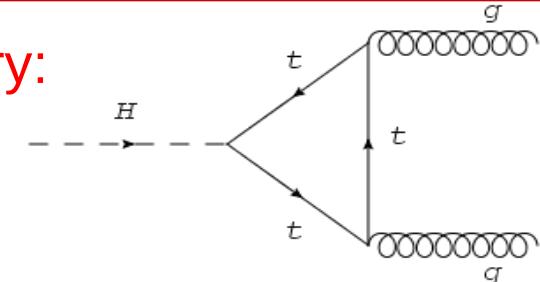
$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\beta},$$

(normalized $E^n \times \theta^n$ products)



High-precision gluon & quark jet studies (FCC-ee)

- Exploit FCC-ee $H(gg)$ as a "pure gluon" factory:
 $H \rightarrow gg$ (BR~8% accurately known) provides O(100.000) extra-clean digluon events.

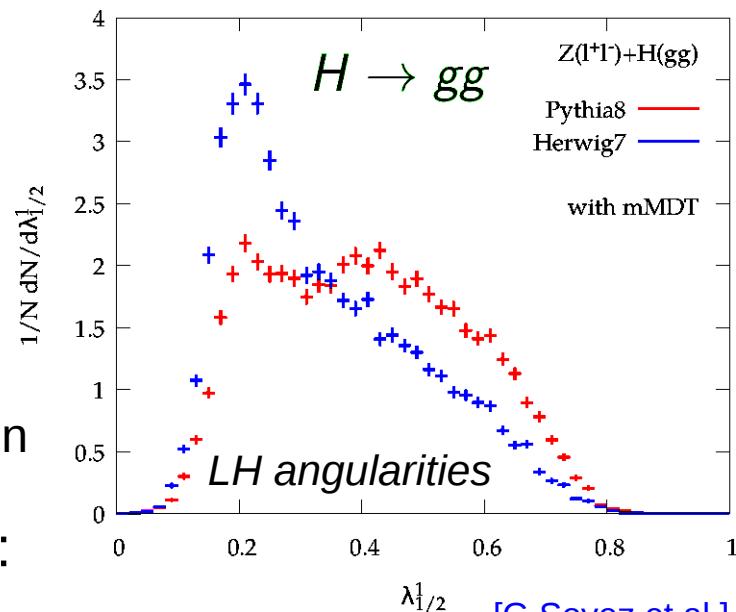


- Multiple handles to study gluon radiation & g-jet properties:

- Gluon vs. quark via $H \rightarrow gg$ vs. $Z \rightarrow qq$
(Profit from excellent g,b separation)
- Gluon vs. quark via $Z \rightarrow bbg$ vs. $Z \rightarrow qq(g)$
(g in one hemisphere recoiling against 2-b-jets in the other).
- Vary E_{jet} range via ISR: $e^+e^- \rightarrow Z^*, \gamma^* \rightarrow jj(\gamma)$
- Vary jet radius: small-R down to calo resolution

- Multiple high-precision analyses at hand:

- BSM: Improve q/g/Q discrimination tools
- pQCD: Check NⁿLO antenna functions. High-precision QCD coupling.
- non-pQCD: Gluon fragmentation: Octet neutralization? (zero-charge gluon jet with rap gaps). Colour reconnection? Glueballs ? Leading η 's,baryons?

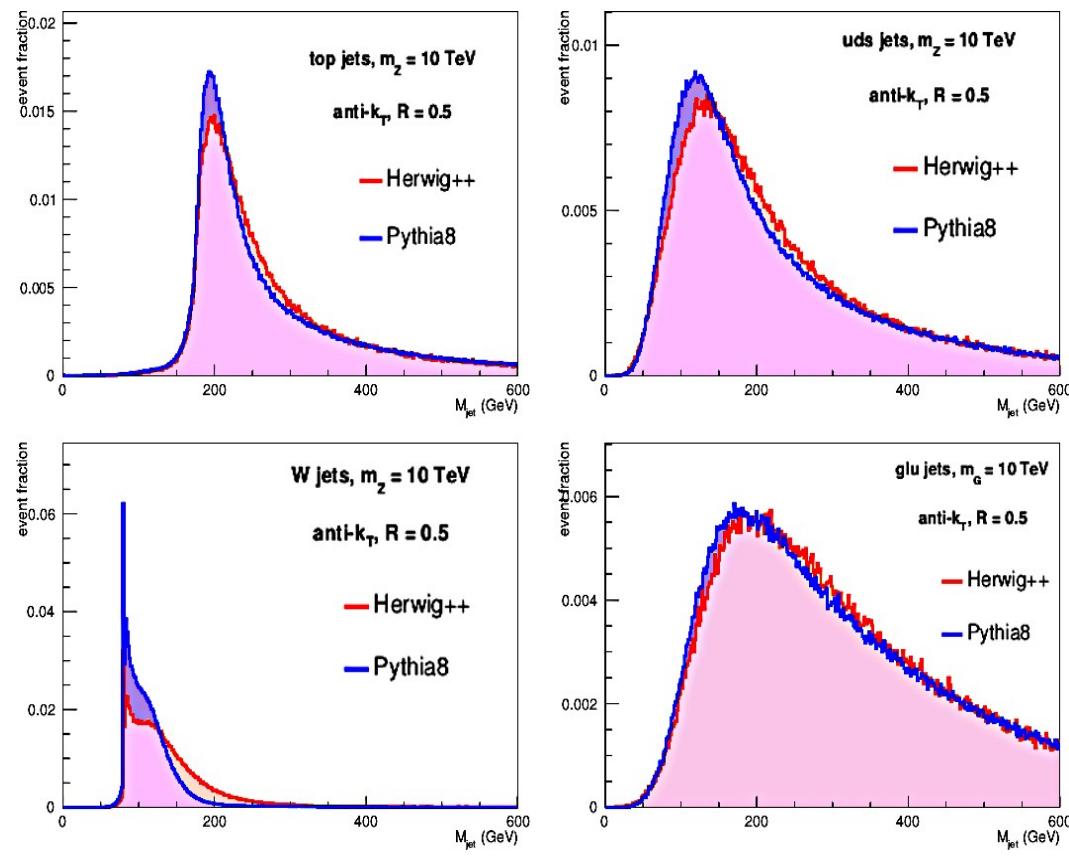
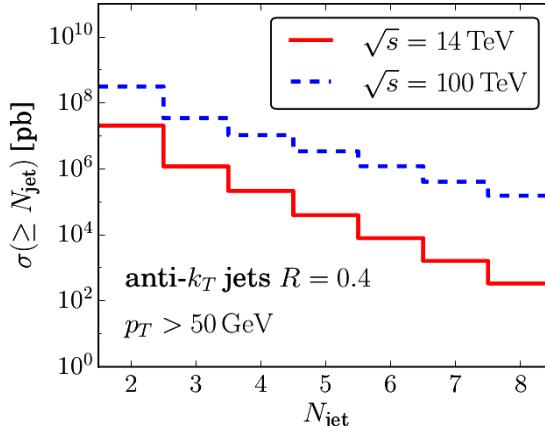


[G.Soyez et al.]

Highly-boosted jets, multijets (FCC-pp)

- Proton-proton collisions at 100 TeV provide **unique conditions** to produce & study **highly-boosted objects**: top, W, Z, H, $R_{\text{BSM}}(\text{jj})$,...
Resolving **small angular dijet sep.** $\Delta R \approx 2M(\text{jj})/p_T(\text{j})$.
- Jet substructure: key to separate **dijets from QCD & (un)coloured resonance decays**, e.g.
 $R_{10-\text{TeV}} \rightarrow tt, qq, gg, WW$
- Diffs. in MC generators for **quark vs. gluon jets**
(& jet radius).
- Also **unique multijet ($N >> 10$)**

BSM,
QCD
studies



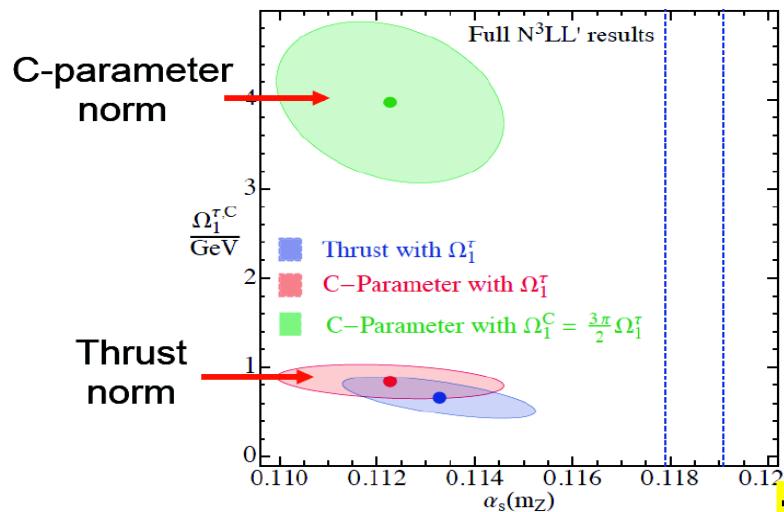
[FCC-pp, arXiv:1607.01831]

α_s via e^+e^- event shapes & jet rates (FCC-ee)

- Computed at $N^{2,3}\text{LO} + N^{(2)}\text{LL}$ accuracy.
- LEP data for thrust, C-parameter, jet shapes, 3-jet x-sections

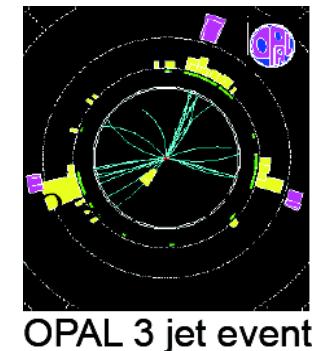
Results sensitive to resummation & non-pQCD (hadronization)

accounted for via MCs or analytically:

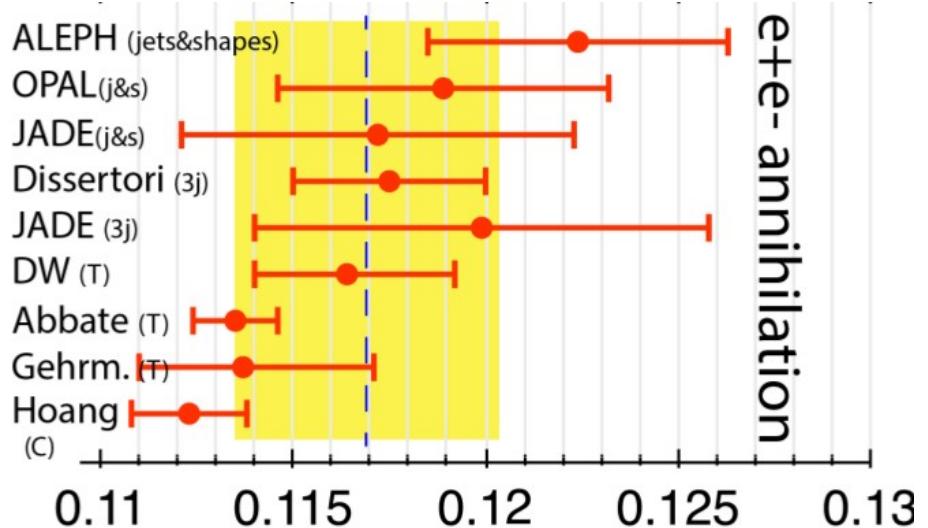


$$\tau = 1 - \max_{\hat{n}} \frac{\sum |\vec{p}_i \cdot \hat{n}|}{\sum |\vec{p}_i|}$$

$$C = \frac{3}{2} \frac{\sum_{i,j} |\vec{p}_i||\vec{p}_j| \sin^2 \theta_{ij}}{\left(\sum_i |\vec{p}_i|\right)^2}$$



[S.Kluth et al., A.Hoang et. al.]



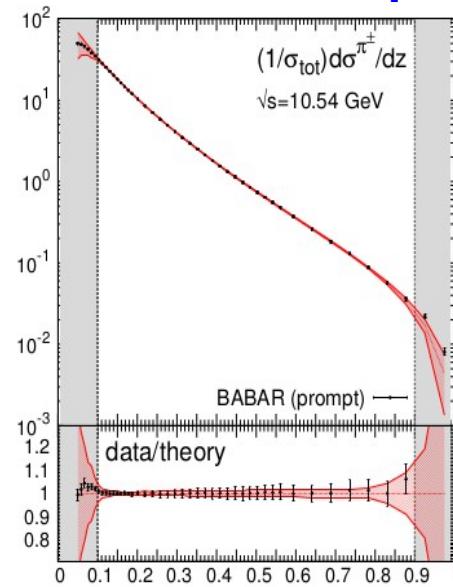
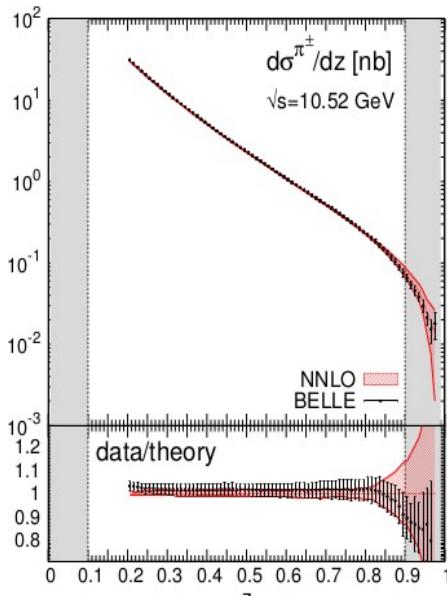
FCC-ee:

- Provides higher- \sqrt{s} data for rates & lower- \sqrt{s} for shapes: $\delta\alpha_s < 1\%$
- TH: Improved ($N^{2,3}\text{LL}$) resummation for rates & hadroniz. for shapes

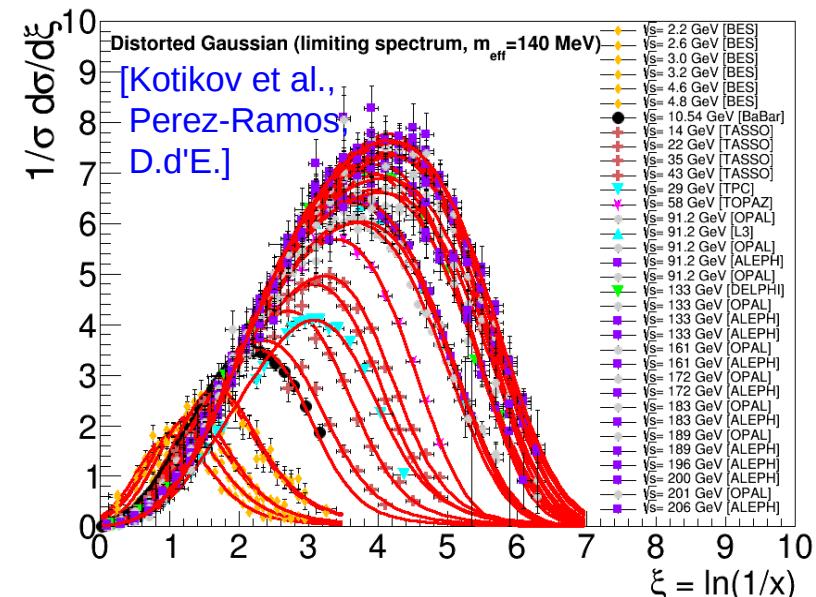
High-precision parton FFs (FCC-ee)

■ Parton-to-hadron fragment. functions evolution known at NNLO at high-z &

[D.Anderle et al., A.Vossen et al., B.Kniehl et al.,
V.Bertone et al., N.Sato et al., D.deFlorian et al.,...]



at NNLO*+NNLL at low-z:



provide additional QCD coupling extractions:

Method	Current $\delta\alpha_s(m_z^2)/\alpha_s(m_z^2)$ uncertainty (theory & experiment state-of-the-art)	Future $\delta\alpha_s(m_z^2)/\alpha_s(m_z^2)$ uncertainty (theory & experiment progress)
soft FFs	$1.8\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 2\%$ (NNLO* only (+NNLL), npQCD small)	$0.7\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 1\%$ (~ 2 yrs), $< 1\%$ (FCC-ee) (NNLO+NNLL. More precise e^+e^- data: 90–350 GeV)
hard FFs	$1\%_{\text{th}} \oplus 5\%_{\text{exp}} \approx 5\%$ (NLO only. LEP data only)	$0.7\%_{\text{th}} \oplus 2\%_{\text{exp}} \approx 2\%$ (+B-factories), $< 1\%$ (FCC-ee) (NNLO. More precise e^+e^- data)

■ FCC-ee (much broader z range) allows for α_s extraction with $\delta\alpha_s < 1\%$

QCD physics at future pp & e⁺e⁻ machines

(1) QCD coupling

(FCC-ee, FCC-pp, SCT)

(2) Parton Distribution Functions

(HL-LHC, HE-LHC, FCC-hh)

(3) Jet substructure & flavour tagging

(FCC-ee, FCC-pp)

(4) Non-perturbative QCD

(FCC-ee, SCT, HL-LHC)

NOTE: Only UNIQUE QCD measurements, inaccessible at any current machine, are covered.

Colour reconnection (FCC-ee)

- Colour reconnection among partons in e^+e^- = Source of uncertainty in m_W , m_{top} , CP-violating Higgs in multijet final-states: $e^+e^- \rightarrow WW(4j)$, $Z(4j)$, $t\bar{t}$
- Use e^+e^- leptonic final-states to learn about CR:

At LEP 2: hot topic (by QCD standards): 'string drag' effect on W mass

Non-zero effect convincingly demonstrated at LEP-2

- No-CR excluded at 99.5% CL [Phys.Rept. 532 (2013) 119]
- But not much detailed (differential) information

Thousand times more WW at FCC-ee

Sjöstrand: turn the W mass problem around; use huge sample of semi-leptonic events to measure m_W

→ use as constraint to measure CR in hadronic WW

Has become even hotter topic at LHC

It appears jet universality is under heavy attack.

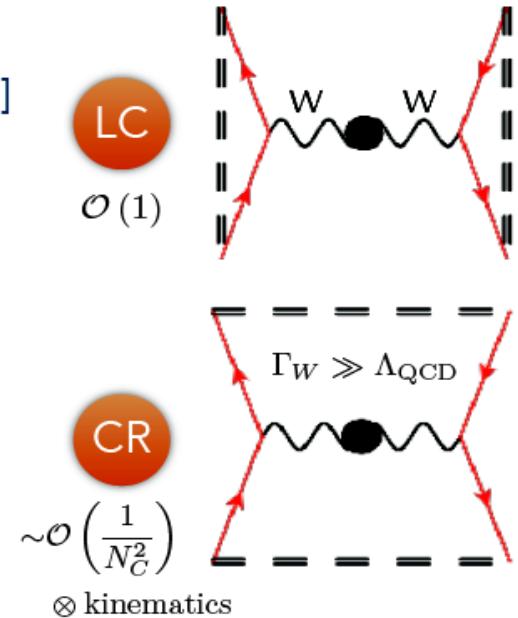
Fundamental to understanding & modeling hadronisation

Follow-up studies now underway at LHC.

T. Sjöstrand, W. Metzger, S. Kluth, C. Bierlich

High-stats ee → other side of story

Also relevant in (hadronic) $ee \rightarrow tt$, and $Z \rightarrow 4$ jets



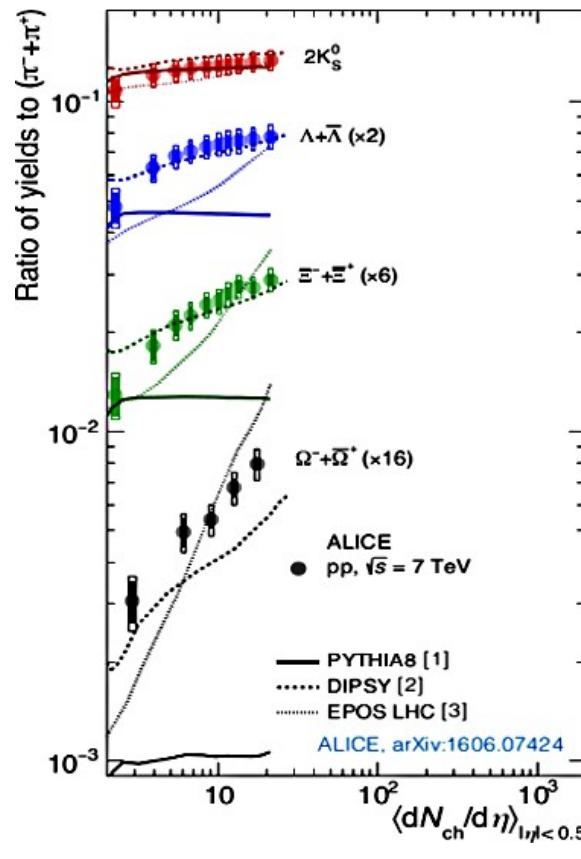
+ Overlaps → interactions?
increased tensions (strangeness)?
breakdown of string picture?

Other Non-pQCD (FCC-ee, SCT, HL-LHC)

- High-precision low- p_T PID hadrons in e^+e^- , pp for detailed studies:
 - Baryon & strangeness production. Colour string dynamics.
 - Final-state correlations (spin: BE, FD; momenta; space)
 - Bound state formation: Onia, multi-quark states, glueballs, ...

conservation of :

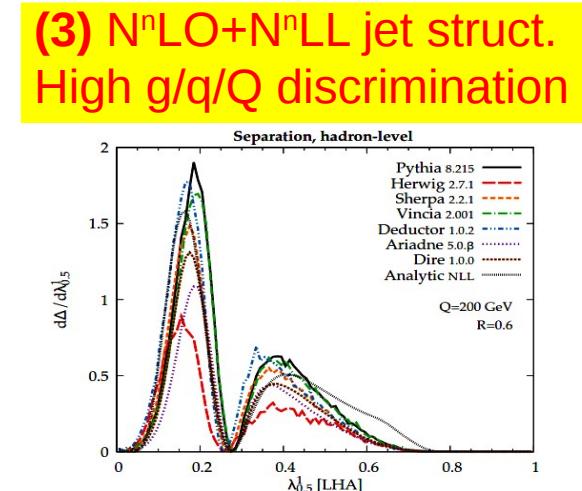
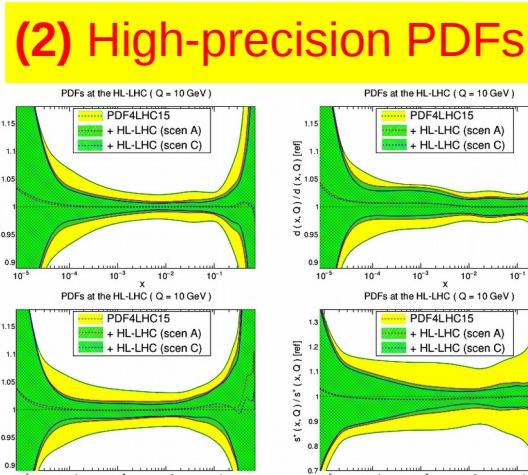
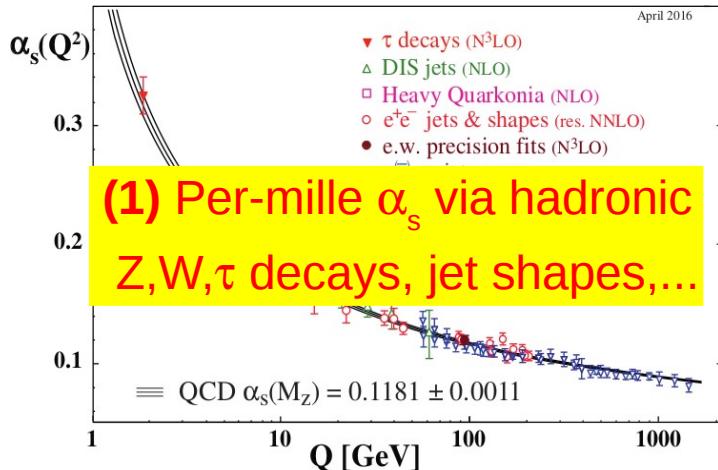
- baryon number
- $q \quad q\bar{q} \quad \bar{q}\bar{q}$
How local?
- strangeness
- $q \quad \bar{s} \quad s \quad \bar{q}$
How local?
- transverse momentum
- $q \quad \bar{q} \quad q \quad \bar{q}$
How local?



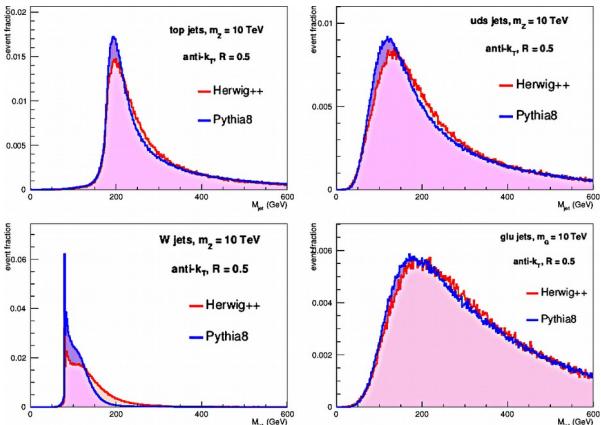
- ▶ Understand breakdown of universality of parton hadronization observed at LHC.
- Baseline vacuum e^+e^- studies for high-density QCD in small & large systems.
 - [Ultra-thin ALICE proposal beyond 2030].

Summary: QCD at future pp & e⁺e⁻ colliders

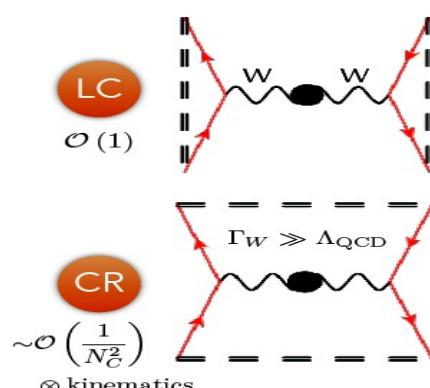
- The precision needed to fully exploit all future ee/pp/ep/eA/AA SM & BSM programs requires exquisite control of pQCD & non-pQCD physics.
- Unique QCD precision studies accessible at FCC-ee, SCT, FCC-pp:



(4) Unique studies of highly-boosted dijet & multijets

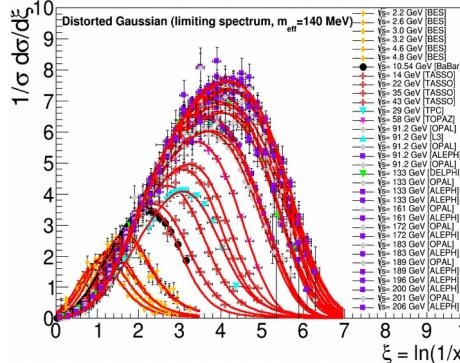
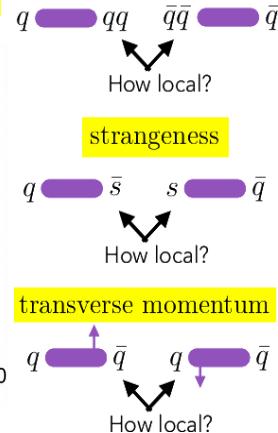


(5) <1% control of colour reconnection



(6) High-precision hadronization:

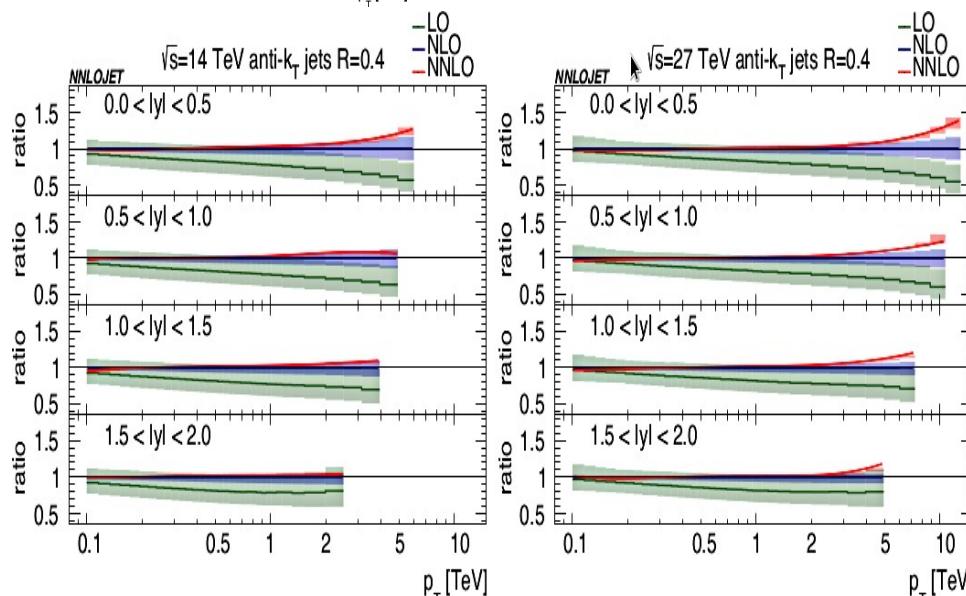
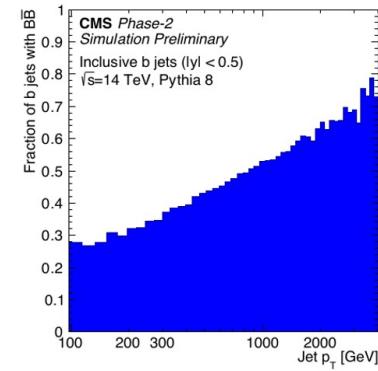
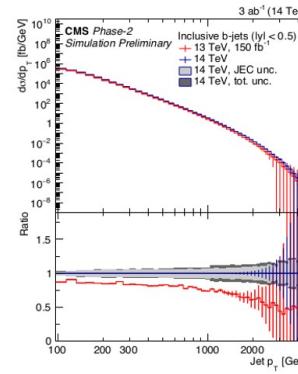
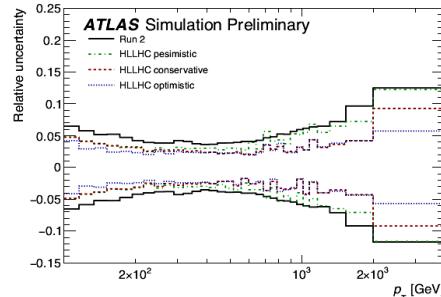
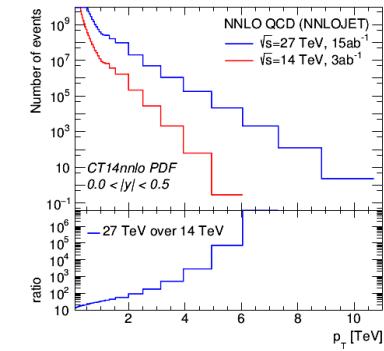
conservation of:
baryon number



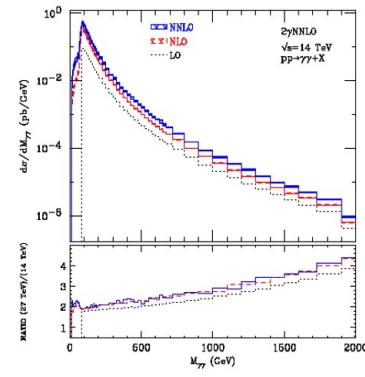
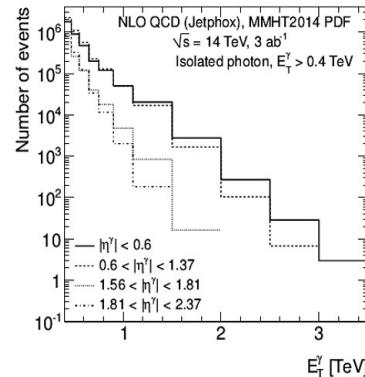
Backup slides

HL-LHC QCD performances: jets, γ

- **ATLAS** projections for inclusive jet production at **HL** and **HE-LHC**, including detailed study of systematic uncertainties:
 - ★ Potentially significant improvement in uncertainties at both low and high jet p_T demonstrated, depending on scenario considered.
 - ★ Extensive jet p_T reach: ~ 5 (9) TeV at HL (HE) LHC.
- **CMS** projections for b-jet production at **HL-LHC**:
 - ★ Increased b -jet reach: $p_T \sim 3$ TeV.
 - ★ New regime: b -quark \sim massless w.r.t. high p_T jet large fraction of jets with $B + \bar{B}$ due to PS ($g \rightarrow b\bar{b}$): important to disentangle from b -quarks produced in hard subprocess.

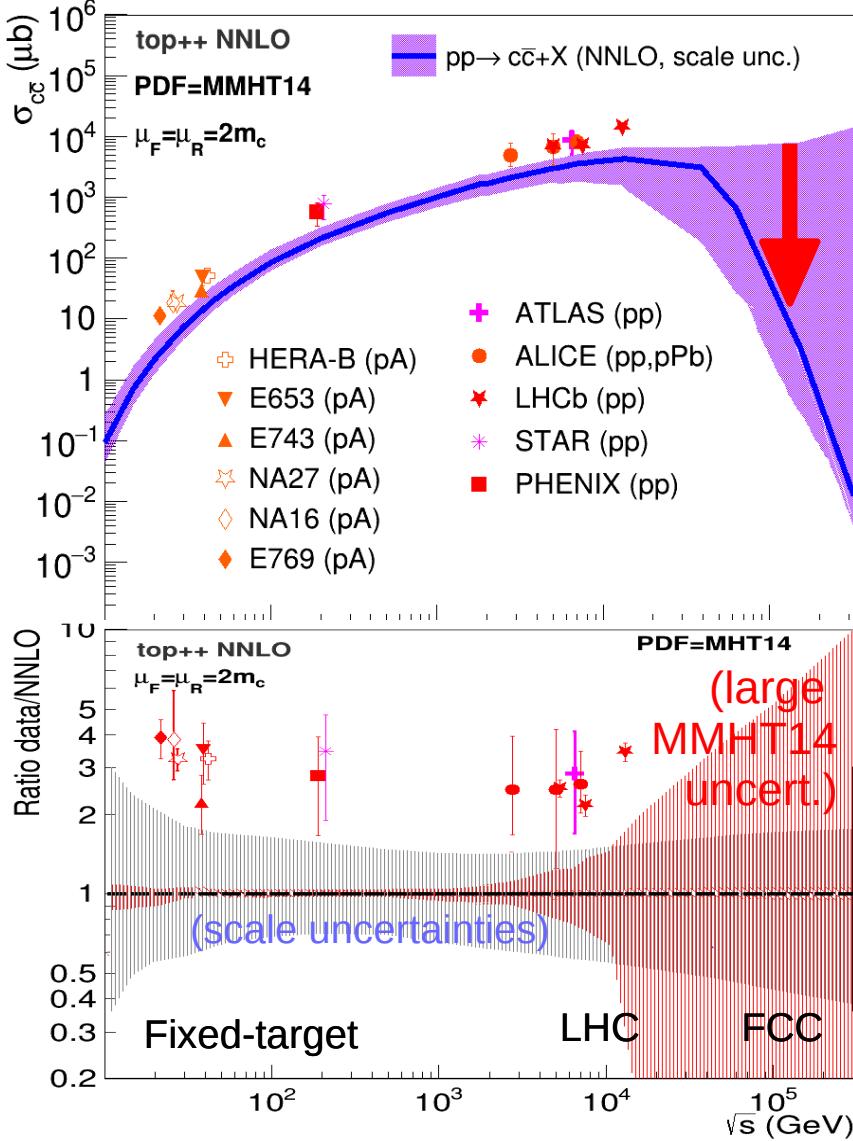


- ★ **Isolated photon:** CMS projections show extensive reach, $E_T^\gamma \sim 3(5)$ TeV for the HL(HE)-LHC. Increase by ~ 2 -3 w.r.t. existing data.
- ★ **Diphoton** production: predictions with cutting-edge **NNLO** theory. Significant increase in reach with HE-LHC again shown.

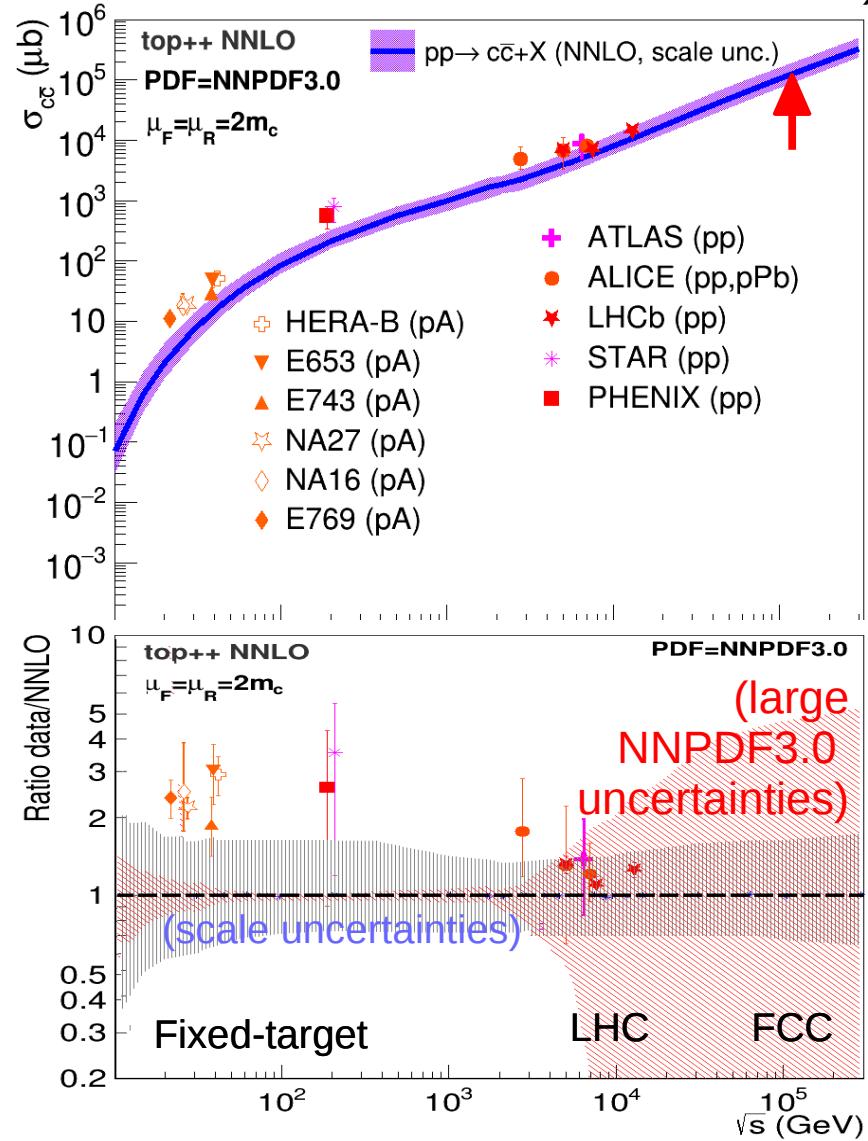


Heavy-quark production (FCC-pp)

■ Charm: Data $\times 2.5$ theory (negative gluon at very low x , $\sqrt{s} > 30$ TeV)



■ Charm: Data $\times 2$ theory (agreement within uncert. but “kink” at $\sqrt{s} > 10$ TeV)



CERN FCC-ee project

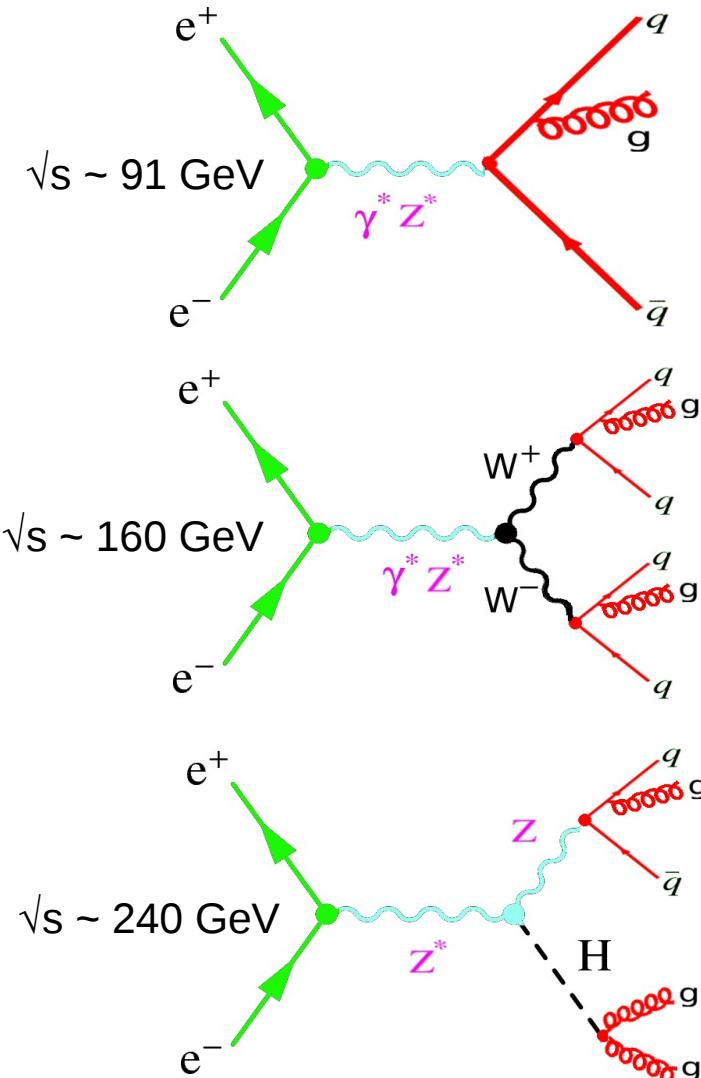
- e^+e^- option (before pp) at $\sqrt{s} = 90, (125), 160, 240, 350$ GeV



\sqrt{s} (GeV):	90 (Z)	125 (eeH)	160 (WW)	240 (HZ)	350 ($t\bar{t}$)	350 (WW \rightarrow H)
σ	43 nb	290 ab	4 pb	200 fb	0.5 pb	25 fb
$\mathcal{L}/\text{IP (cm}^{-2}\text{s}^{-1}\text{)}$	10^{36}	$5 \cdot 10^{35}$	10^{35}	$7 \cdot 10^{34}$	$1.5 \cdot 10^{34}$	$1.5 \cdot 10^{34}$
\mathcal{L}_{int} (ab $^{-1}$ /yr, 2 IPs)	50	10	8	1.8	0.5	0.35
Events/year (2 IPs)	10^{12}	$3 \cdot 10^3$	$3 \cdot 10^7$	$3 \cdot 10^5$	$2.5 \cdot 10^5$	10^4
Years needed (2 IPs)	4	1.5	1	3	0.5	4
# of light-q jets/year:	$\mathcal{O}(10^{12})$	–	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	–	–
# of gluon-jets/year:	$\mathcal{O}(10^{11})$	$\mathcal{O}(10^2)$	$\mathcal{O}(10^6)$	$\mathcal{O}(10^4)$	–	$\mathcal{O}(10^3)$
# of heavy-Q jets/yr:	$\mathcal{O}(10^{12})$	$\mathcal{O}(10^3)$	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	$\mathcal{O}(10^5)$	$\mathcal{O}(10^4)$

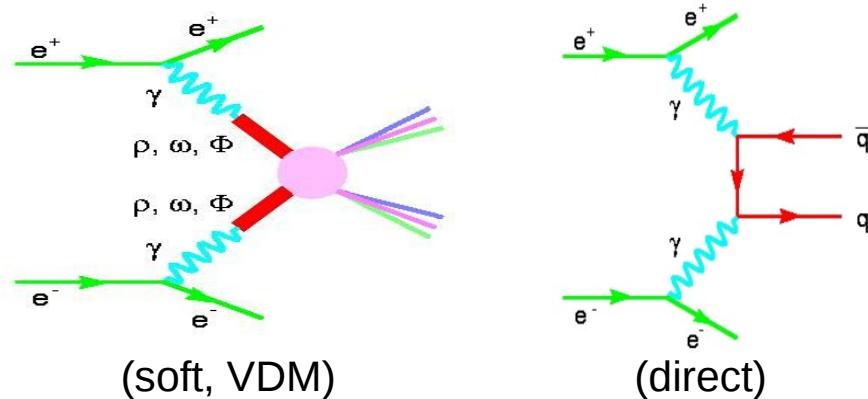
QCD in e^+e^- collisions

- e^+e^- collisions provide an **extremely clean** environment with fully-controlled initial-state to very precisely probe q,g dynamics:



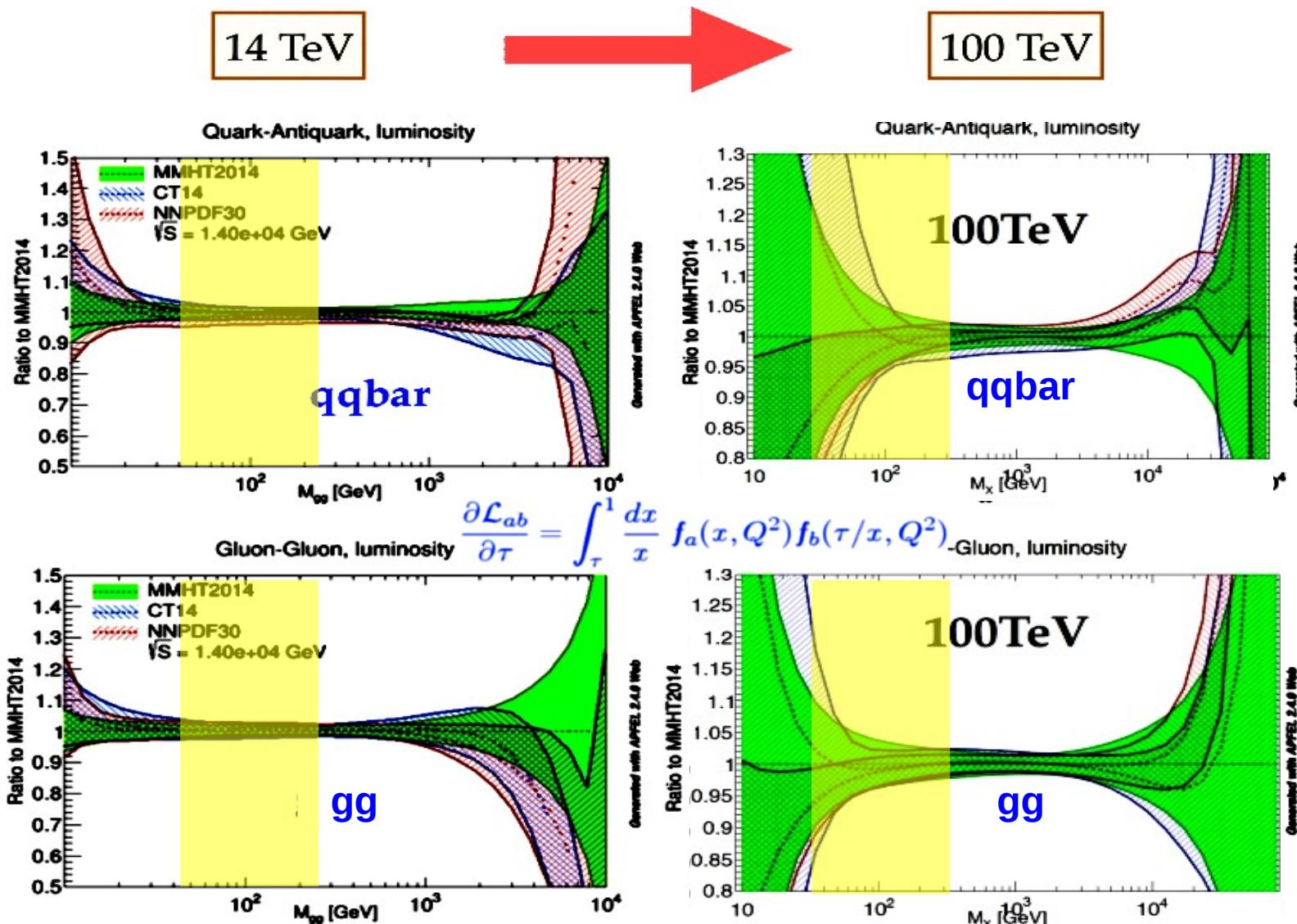
Advantages compared to p-p collisions:

- QED initial-state with **known kinematics**
 - **Controlled QCD radiation** (only in final-state)
 - Well-defined **heavy-Q, quark, gluon jets**
 - **Smaller non-pQCD uncertainties:**
no PDFs, no QCD “underlying event”,...
- Direct clean parton fragmentation & hadroniz.
- Plus **QCD physics** in $\gamma\gamma$ (EPA) collisions:



Parton lumis at FCC “precision” region

- “Precision” region at FCC-pp: 5–7% PDF uncertainty for $\sigma(W, Z, H)$



$$\frac{\partial \mathcal{L}_{ab}}{\partial \tau} = \int_{\tau}^1 \frac{dx}{x} f_a(x, Q^2) f_b(\tau/x, Q^2)$$

α_s from γ QCD structure function

→ Computed at NNLO: $\int_0^1 dx F_2^\gamma(x, Q^2, P^2) = \frac{\alpha}{4\pi} \frac{1}{2\beta_0} \left\{ \frac{4\pi}{\alpha_s(Q^2)} c_{LO} + c_{NLO} + \frac{\alpha_s(Q^2)}{4\pi} c_{NNLO} + \mathcal{O}(\alpha_s^2) \right\}$

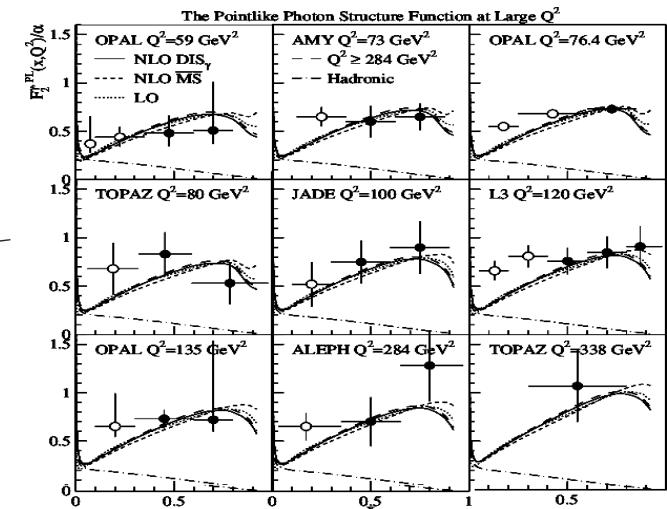
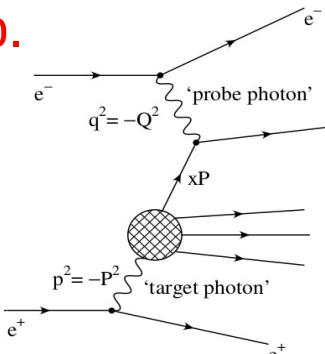
→ Poor $F_2^\gamma(x, Q^2)$ experimental measurements:

→ Extraction (NLO) with large exp. uncertainties today:

$$\alpha_s(M_Z) = 0.1198 \pm 0.0054$$

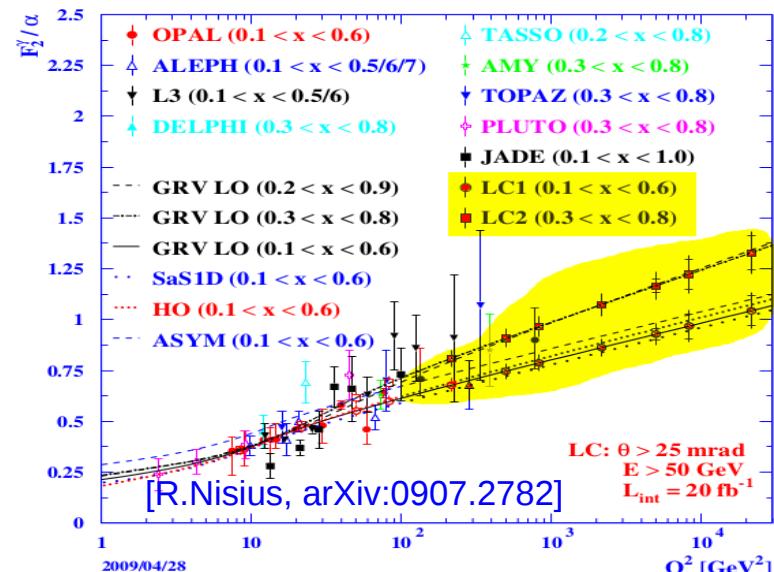
(±4.5%)

[M.Klasen et al. PRL89 (2002)122004]



→ Future prospects:

- Better data badly needed.
- Belle-II ?
- Dedicated studies at ILC exist:
- Huge γ (EPA) stats at FCC-ee will lead to: $\delta\alpha_s < 1\%$

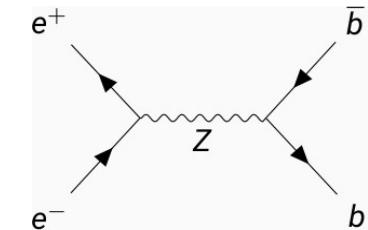


Reduced QCD uncertainties on EWK observables

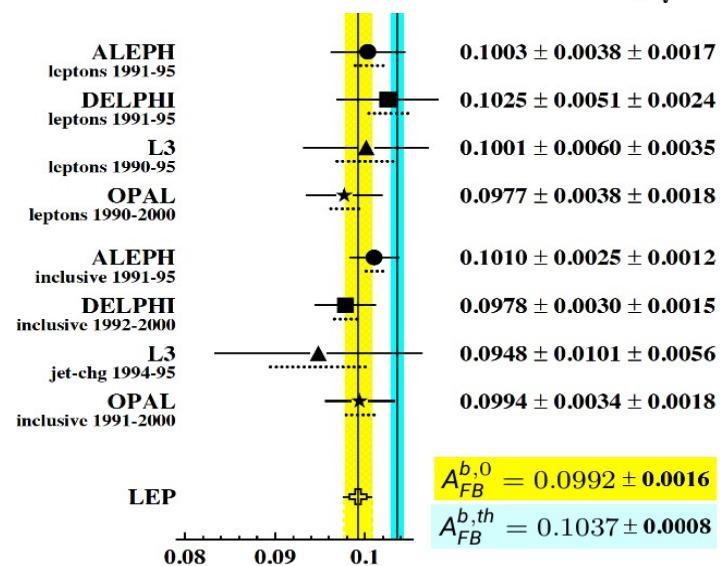
- With $\times 10^5$ more Z's than LEP, EWK uncertainties at FCC-ee will be dominated by syst. (QCD).
Example: $e^+e^- \rightarrow bb$ forward–backward asymmetry

- 8 measurements at LEP:
 - 4 lepton-based, 4 jet-charge-based
- Exp. observable with **largest discrepancy** today wrt. the SM: 2.8σ

- Exp. Uncertainties: $\sim 1.6\%$
 - Statistical: $\pm 1.5\%$ ($\sim 0.05\%$ at FCC-ee)
 - Systematics: $\pm 0.6\%$ (QCD-related: $\pm 0.4\%$)
- QCD effects on $A_{FB}^{0,b}$ (depending strongly on exp. selection procedure):
 - Gluon splitting (TH control: α_s^2 corrections)
 - Smearing of b-jet/thrust axis
 - b and c radiation & fragmentation. B and D decay models.
[Uncertainties estimated by Abbaneo et al., EPJC 4 (1998)]
- We have **revisited** the impact of QCD effects on $A_{FB}^{0,b}$ implementing original analyses in up-to-date retuned parton-shower+hadronization MCs

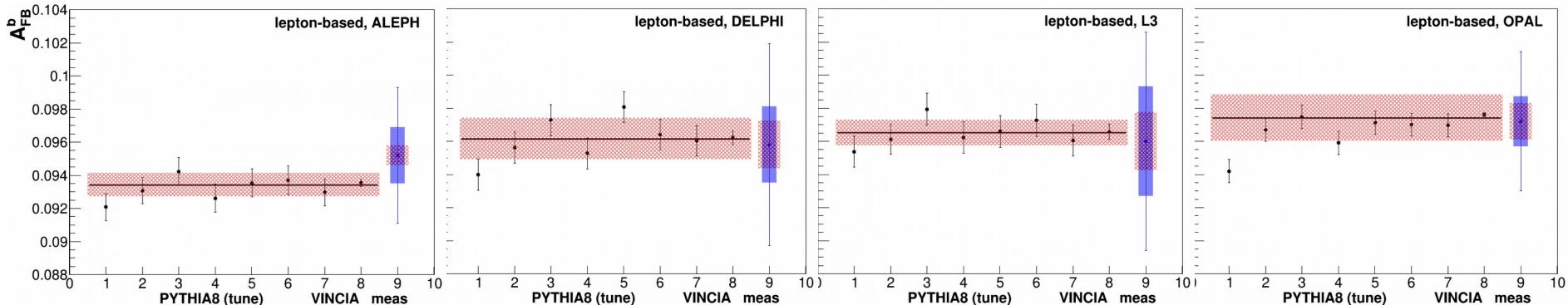


$$A_{FB}^b = \frac{N_F - N_B}{N_F + N_B} \quad A_{FB} = \frac{\sigma_A}{\sigma_S} \propto \frac{-g_{\mu\nu} T^{\mu\nu}}{ie_{\mu\nu\lambda\rho} \frac{n^\lambda Q^\rho}{n \cdot Q} T^{\mu\nu}}$$

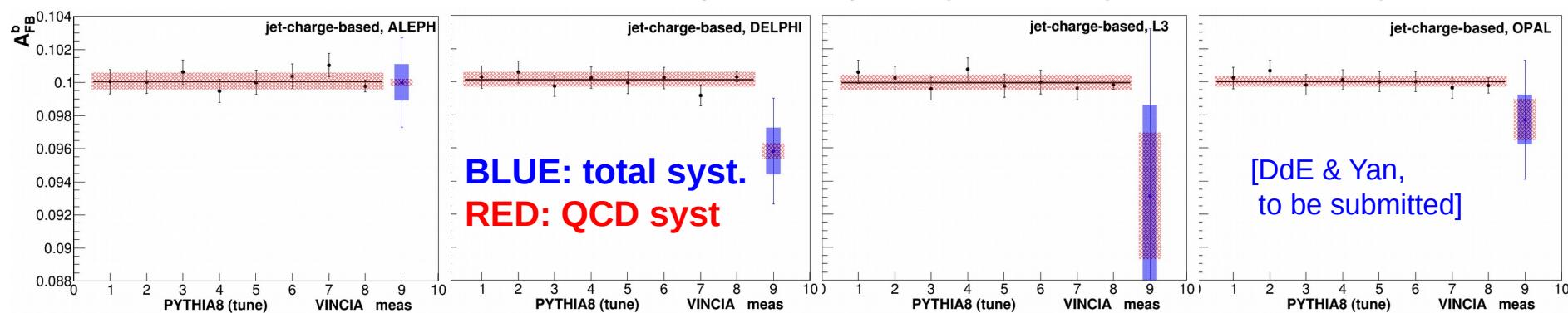


Reduced QCD uncertainties on A_{FB} at Z pole

- QCD uncertainties recomputed from PYTHIA8.226 (7 tunes) & VINCIA2.2
- $e^+e^- \rightarrow bb$ forward–backward asymmetry for lepton-based analyses:



- $e^+e^- \rightarrow bb$ forward–backward asymmetry for jet-charge-based analyses:



- 2018 vs. 1998 PS+hadronization uncertainties:
 - Lepton-based: Consistent for ALEPH/DELPHI, smaller for L3, larger for OPAL.
 - Jet-charge-based: Consistent for DELPHI, smaller for ALEPH/L3/OPAL.
- LEP average to be recomputed (likely no change as stat.unc. dominates)