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The Flavor of the ALPs

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based on ongoing work with Martin Bauer, Sophie Renner, Marvin Schnubel & Andrea Thamm

Motivation

 $\operatorname{Im}\phi$

- Axion-like particles (ALPs) appear in many BSM scenarios and are well motivated: strong CP problem, mediator to hidden sector, pNGB of spontaneously broken global symmetry, possible explanation of (g-2)_µ, ...
- * Assume the existence of a new pseudoscalar resonance *a*, which is a SM singlet and whose mass is protected by a (approximate) shift symmetry $a \rightarrow a+const$.
- Many studies of possible collider probes of ALPs exist
 [Kim, Lee 1989; Djouadi, Zerwas, Zunft 1991; Rupak, Simmons 1995; Kleban, Ramadan 2005; Mimasu, Sanz 2014; Jäckel, Spannowsky 2015; Knapen, Lin, Lou, Melia 2016; Brivio et al. 2017; Bauer, MN, Thamm 2017; ...]
- Here we focus on effects of ALPs on flavor observables
 [also: Izaguirre, Lin, Shuve 2016; Björkeroth, Chin, King 2018; Gavela, Houtz, Quilez, del Rey, Sumensari 2019; ...]

Effective Lagrangian

* The ALP couplings to the SM start at D=5 and are described by the effective Lagrangian (with $\Lambda = 32\pi^2 f_a |C_{GG}|$ a NP scale):

$$\mathcal{L}_{\text{eff}}^{D\leq5} = \frac{1}{2} (\partial_{\mu}a)(\partial^{\mu}a) - \frac{m_{a,0}^{2}}{2} a^{2} + \frac{\partial^{\mu}a}{\Lambda} \sum_{F} \bar{\psi}_{F} C_{F} \gamma_{\mu} \psi_{F}$$

$$+ g_{s}^{2} C_{GG} \frac{a}{\Lambda} G_{\mu\nu}^{A} \tilde{G}^{\mu\nu,A} + g^{2} C_{WW} \frac{a}{\Lambda} W_{\mu\nu}^{A} \tilde{W}^{\mu\nu,A} + g^{\prime 2} C_{BB} \frac{a}{\Lambda} B_{\mu\nu} \tilde{B}^{\mu\nu}$$

$$= WSB$$

$$e^{2} C_{\gamma\gamma} \frac{a}{\Lambda} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{2e^{2}}{s_{w}c_{w}} C_{\gamma Z} \frac{a}{\Lambda} F_{\mu\nu} \tilde{Z}^{\mu\nu} + \frac{e^{2}}{s_{w}^{2}c_{w}^{2}} C_{ZZ} \frac{a}{\Lambda} Z_{\mu\nu} \tilde{Z}^{\mu\nu} + \dots$$

$$(C_{\gamma\gamma} = C_{WW} + C_{BB} \text{ etc.})$$

$$\sum_{f} \frac{c_{ff}}{2} \frac{\partial^{\mu}a}{\Lambda} \bar{f} \gamma_{\mu}\gamma_{5} f + \text{flavor off-diagonal terms}$$
[Georgi, Kaplan, Randall 1986]

Loop-in
$$\underline{a}$$
 \underline{a} \underline{a}

 Of particular relevance are the ALP couplings to photons and charged leptons; at 1-loop order we find: only present for light ALPs

 $C_{\gamma\gamma}^{\text{eff}}(m_a \lesssim 1 \text{ GeV}) \approx C_{\gamma\gamma} - (1.92 \pm 0.04) C_{GG} - \frac{m_a^2}{m_\pi^2 - m_a^2} \left[C_{GG} \frac{m_d - m_u}{m_d + m_u} + \frac{c_{uu} - c_{dd}}{32\pi^2} \right] \\ + \sum_{q=c,b,t} \frac{N_c Q_q^2}{16\pi^2} c_{qq} B_1(\tau_q) + \sum_{\ell=e,\mu,\tau} \frac{c_{\ell\ell}}{16\pi^2} B_1(\tau_\ell) + \frac{2\alpha}{\pi} \frac{C_{WW}}{s_w^2} B_2(\tau_W) \\ \text{heavy particles decouple} \sim m_a^2 / m_{Wf}^2 \\ c_{\ell\ell}^{\text{eff}} = c_{\ell\ell}(\mu) \left[1 + \mathcal{O}(\alpha) \right] - 12Q_\ell^2 \alpha^2 C_{\gamma\gamma} \left[\ln \frac{\mu^2}{m_\ell^2} + \delta_1 + g(\tau_\ell) \right] \\ - \frac{3\alpha^2}{s_w^4} C_{WW} \left(\ln \frac{\mu^2}{m_W^2} + \delta_1 + \frac{1}{2} \right) - \frac{12\alpha^2}{s_w^2 c_w^2} C_{\gamma Z} Q_\ell \left(T_3^\ell - 2Q_\ell s_w^2 \right) \left(\ln \frac{\mu^2}{m_Z^2} + \delta_1 + \frac{3}{2} \right)$

$$-\frac{12\alpha^2}{s_w^4 c_w^4} C_{ZZ} \left(Q_\ell^2 s_w^4 - T_3^\ell Q_\ell s_w^2 + \frac{1}{8} \right) \left(\ln \frac{\mu^2}{m_Z^2} + \delta_1 + \frac{1}{2} \right)$$

Fermion couplings after EWSB

* After transformation to the mass basis, we obtain:

with:

$$oldsymbol{K}_U = oldsymbol{U}_u^{\dagger} oldsymbol{C}_Q oldsymbol{U}_u \,, \qquad oldsymbol{K}_D = oldsymbol{U}_d^{\dagger} oldsymbol{C}_Q oldsymbol{U}_d \,, \qquad oldsymbol{K}_E = oldsymbol{U}_e^{\dagger} oldsymbol{C}_L oldsymbol{U}_e \,$$
 $oldsymbol{K}_f = oldsymbol{W}_f^{\dagger} oldsymbol{C}_f oldsymbol{W}_f \,; \quad f = u, d, e$

Flavor-diagonal couplings from before:

$$c_{u_i u_i} = (K_u)_{ii} - (K_U)_{ii}, \qquad c_{d_i d_i} = (K_d)_{ii} - (K_D)_{ii}, \qquad c_{e_i e_i} = (K_e)_{ii} - (K_E)_{ii}$$

Minimal flavor violation (MFV)

 Strong phenomenological bounds on off-diagonal couplings motivate MFV ansatz:

$$egin{aligned} m{C}_Q &= c_0^Q \, m{1} + \epsilon \left(c_1^Q \, m{Y}_u \, m{Y}_u^\dagger + c_2^Q \, m{Y}_d \, m{Y}_d^\dagger
ight) + \mathcal{O}(\epsilon^2 \ m{C}_u &= c_0^u \, m{1} + \epsilon \, c_1^u \, m{Y}_u^\dagger \, m{Y}_u + \mathcal{O}(\epsilon^2) \ m{C}_d &= c_0^d \, m{1} + \epsilon \, c_1^d \, m{Y}_d^\dagger \, m{Y}_d + \mathcal{O}(\epsilon^2) \end{aligned}$$

* This implies:

$$\begin{split} \boldsymbol{K}_{U} &= c_{0}^{Q} \, \mathbf{1} + \epsilon \left[c_{1}^{Q} \, \left(\boldsymbol{Y}_{u}^{\text{diag}} \right)^{2} + c_{2}^{Q} \, \boldsymbol{V} \left(\boldsymbol{Y}_{d}^{\text{diag}} \right)^{2} \boldsymbol{V}^{\dagger} \right] + \mathcal{O}(\epsilon^{2}) \checkmark \quad \text{related by CKM} \\ \boldsymbol{K}_{D} &= c_{0}^{Q} \, \mathbf{1} + \epsilon \left[c_{1}^{Q} \, \boldsymbol{V}^{\dagger} \, \left(\boldsymbol{Y}_{u}^{\text{diag}} \right)^{2} \, \boldsymbol{V} + c_{2}^{Q} \, \left(\boldsymbol{Y}_{d}^{\text{diag}} \right)^{2} \right] + \mathcal{O}(\epsilon^{2}) \checkmark \quad \text{matrix } \boldsymbol{V} \\ \boldsymbol{K}_{u} &= c_{0}^{u} \, \mathbf{1} + \epsilon \, c_{1}^{u} \, \left(\boldsymbol{Y}_{u}^{\text{diag}} \right)^{2} \, + \mathcal{O}(\epsilon^{2}) \\ \boldsymbol{K}_{d} &= c_{0}^{d} \, \mathbf{1} + \epsilon \, c_{1}^{d} \, \left(\boldsymbol{Y}_{d}^{\text{diag}} \right)^{2} \, + \mathcal{O}(\epsilon^{2}) \end{split}$$

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ight) + \mathcal{O}(\epsilon^2) \ m{C}_u &= c_0^u \, m{1} + \epsilon \, c_1^u \, m{Y}_u^\dagger \, m{Y}_u + \mathcal{O}(\epsilon^2) \ m{C}_d &= c_0^d \, m{1} + \epsilon \, c_1^d \, m{Y}_d^\dagger \, m{Y}_d + \mathcal{O}(\epsilon^2) \end{aligned}$$

Neglecting the down-type quark masses:

$$\begin{split} \boldsymbol{K}_{U} &\approx c_{0}^{Q} \, \mathbf{1} + \epsilon \, c_{1}^{Q} \, \left(\boldsymbol{Y}_{t} \right)^{2} + \mathcal{O}(\epsilon^{2}) & \text{only source of flavor} \\ \boldsymbol{K}_{D} &\approx c_{0}^{Q} \, \mathbf{1} + \epsilon \, c_{1}^{Q} \, \boldsymbol{V}^{\dagger} \, \left(\boldsymbol{Y}_{t} \right)^{2} \, \boldsymbol{V} + \mathcal{O}(\epsilon^{2}) \\ \boldsymbol{K}_{u} &\approx c_{0}^{u} \, \mathbf{1} + \epsilon \, c_{1}^{u} \, \left(\boldsymbol{Y}_{t} \right)^{2} + \mathcal{O}(\epsilon^{2}) \\ \boldsymbol{K}_{d} &\approx c_{0}^{d} \, \mathbf{1} \end{split}$$

Low-energy effective Lagrangian

* Integrating out heavy SM fields, we find at 1-loop order $(i \neq j)$:

$$(K_{D})_{ij}^{\text{eff}} = (K_{D})_{ij} (\mu) + \frac{y_{t}^{2}}{16\pi^{2}} V_{ti}^{*} V_{tj} \left\{ c_{tt} \left[\frac{1}{2} \ln \frac{\mu^{2}}{m_{t}^{2}} - \frac{7 - 8x_{t} + x_{t}^{2} + 6 \ln x_{t}}{4(1 - x_{t})^{2}} \right] - 6g^{2} C_{WW} \frac{1 - x_{t} + x_{t} \ln x_{t}}{(1 - x_{t})^{2}} \right\} \leftarrow \text{[Izaguirre, Lin, Shuve 2016]}$$

$$(K_{d})_{ij}^{\text{eff}} = (K_{d})_{ij}$$
For $\Lambda = \mu = 1$ TeV:

 $(K_D)_{ij}^{\text{eff}} = (K_D)_{ij} (\Lambda) + V_{ti}^* V_{tj} [0.01 c_{tt} - 0.004 C_{WW}]$

 No corresponding contributions to up-type quark and lepton couplings

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Rare decays of kaons and B mesons

- * On-shell decays $K \to \pi a$ and $B \to K^{(*)}a$ provide very strong bounds if kinematically allowed
- ALP can be long-lived or decay into photons or charged leptons
- * Due to ALP- π^0 mixing, the $K \to \pi a$ amplitude receives a contribution from the strong decay $K \to \pi \pi^0$, since:

$$\pi^{0} = \pi_{\rm phys}^{0} - \frac{\epsilon m_{a}^{2}}{m_{\pi}^{2} - m_{a}^{2}} a_{\rm phys} + O(\epsilon^{2}); \text{ for } |m_{\pi}^{2} - m_{a}^{2}| \gg 2\epsilon m_{a}m_{\pi}$$
$$\epsilon = \frac{f_{\pi}}{2\sqrt{2}\Lambda} \left[(c_{uu} - c_{dd}) + 32\pi^{2}C_{GG}\frac{m_{d} - m_{u}}{m_{d} + m_{u}} \right]$$

Resulting bounds (95% CL)

Model-independent upper limits:

Observable	Mass Range [MeV]	ALP decay mode	Constrained coupling c	Limit (95% CL) on $ c \cdot \left(\frac{\text{TeV}}{\Lambda}\right) \cdot \sqrt{\mathcal{B}}$
$\mathcal{B}(K^+ \to \pi^+ \bar{\nu} \nu)$	$0 < m_a < 265 \; (*)$	Long-lived	$(K_D + K_d)_{ds}$	4.9×10^{-9}
$\mathcal{B}(B^+ \to K^+ \bar{\nu} \nu)$	$0 < m_a < 4785$	Long-lived	$(K_D + K_d)_{sb}$	$6.9 imes 10^{-6}$
$\mathcal{B}(B \to K^* \bar{\nu} \nu)$	$0 < m_a < 4387$	Long-lived	$(K_D - K_d)_{sb}$	$5.1 imes 10^{-6}$
$\mathcal{B}(\Upsilon \to \gamma a(\text{invisible}))$	$m_a < 9200$	Long-lived	$(K_D - K_d)_{bb}$	0.76
$\mathcal{B}(K^+ \to \pi^+ \gamma \gamma)$	$m_a < 108$	$\gamma\gamma$	$(K_D + K_d)_{ds}$	2.1×10^{-8}
$\mathcal{B}(K^+ \to \pi^+ \gamma \gamma)$	$220 < m_a < 354$	$\gamma\gamma$	$(K_D + K_d)_{ds}$	2.4×10^{-7}
$\mathcal{B}(K_L^0 o \pi^0 \gamma \gamma)$	$m_a < 110$	$\gamma\gamma$	$\operatorname{Im}(K_D + K_d)_{ds}$	$1.4 imes 10^{-8}$
$\mathcal{B}(K_L^0 \to \pi^0 \gamma \gamma)$	$m_a < 363$	$\gamma\gamma$	$\operatorname{Im}(K_D + K_d)_{ds}$	1.2×10^{-7}
$\mathcal{B}(K_L \to \pi^0 e^+ e^-)$	$140 < m_a < 362$	e^+e^-	$\operatorname{Im}(K_D + K_d)_{ds}$	$2.9 imes 10^{-9}$
$d\mathcal{B}/dq^2(B^0 \to K^{*0}e^+e^-)_{[0.0,0.05]}$	$0 < m_a < 224$	e^+e^-	$(K_D - K_d)_{sb}$	$8.3 imes10^{-7}$
$d\mathcal{B}/dq^2(B^0 \to K^{*0}e^+e^-)_{[0.05, 0.15]}$	$224 < m_a < 387$	e^+e^-	$(K_D - K_d)_{sb}$	$6.5 imes 10^{-7}$
$\mathcal{B}(K_L \to \pi^0 \mu^+ \mu^-)$	$210 < m_a < 350$	$\mu^+\mu^-$	$\operatorname{Im}(K_D + K_d)_{ds}$	$4.0 imes 10^{-9}$
$\mathcal{B}(B^+ \to K^+ a(\mu^+ \mu^-))$	$250 < m_a < 4700 \ (\dagger)$	$\mu^+\mu^-$	$(K_D + K_d)_{sb}$	$4.4 imes 10^{-8}$
$\mathcal{B}(B^0 \to K^{*0} a(\mu^+ \mu^-))$	$214 < m_a < 4350 \ (\dagger)$	$\mu^+\mu^-$	$(K_D - K_d)_{sb}$	$5.1 imes 10^{-8}$
$\mathcal{B}(J/\psi \to \gamma a(\mu^+\mu^-))$	$212 < m_a < 3000$	$\mu^+\mu^-$	$(K_U - K_u)_{cc}$	0.16
$\mathcal{B}(\Upsilon \to \gamma a(\mu^+ \mu^-))$	$212 < m_a < 9200$	$\mu^+\mu^-$	$(K_D - K_d)_{bb}$	0.24
$\mathcal{B}(B^+ \to K^+ \tau^+ \tau^-)$	$3552 < m_a < 4785$	$\tau^+\tau^-$	$(K_D + K_d)_{sb}$	8.2×10^{-5}
$\mathcal{B}(\Upsilon \to \gamma a(\tau^+ \tau^-))$	$3500 < m_a < 9200$	$\tau^+\tau^-$	$(K_D - K_d)_{bb}$	1.5
$\mathcal{B}(\Upsilon \to \gamma a(\text{hadrons}))$	$300 < m_a < 7000$	hadrons	$(K_D - K_d)_{bb}$	0.56

- * Consider some concrete scenarios in which only one ALP coupling is present at tree level (very conservative)
- * All other ALP couplings are induced via loops in the EFT
- Calculate the relevant ALP branching ratios and the ALP decay length, which is relevant for determining which fraction of ALP decays can be reconstructed in the detector

* Scenario 1: Bounds on C_{WW} , assuming all other couplings vanish at tree level $\checkmark \Upsilon \rightarrow \gamma a(\mu^+ \mu^-)$



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* Scenario 2: Bounds on $c_{uu} = c_{cc} = c_{tt}$, assuming all other couplings vanish at tree level



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* Scenario 3: Bounds on $c_{dd} = c_{ss} = c_{bb}$, assuming all other couplings vanish at tree level



Lepton flavor violation

- * Interesting (and complementary) bounds on lepton flavorviolating couplings can be derived from decays such as $\ell_i = \ell_i - \ell_i$ $\mu \rightarrow e \dot{\gamma}, \mu \rightarrow 3e$ and $\mu \rightarrow e + invisible$ (and corresp. τ decays) $\ell_k = \ell_k$
- Relevant diagrams:



 For simplicity, we will assume that one combination of couplings dominates

Resulting bounds (95% CL)

* Model-independent upper bounds (assuming on-shell ALP):

Observable	Mass Range [MeV]	ALP decay mode	Constrained coupling c	Limit (95% CL) on $ c \cdot \left(\frac{\text{TeV}}{\Lambda}\right) \cdot \sqrt{\mathcal{B}}$
$\mathcal{B}(\mu \to ea(\text{invisible}))$	$13 < m_a < 80$	Long-lived	$\sqrt{ K_e^{e\mu} ^2 + K_L^{e\mu} ^2}$	3.8×10^{-7}
$\mathcal{B}(\mu \to ea(\text{invisible}))$	$0 < m_a < 13$	Long-lived	$\sqrt{ K_e^{e\mu} ^2 + K_L^{e\mu} ^2}$	$1.5 imes 10^{-6}$
$\mathcal{B}(\tau \to ea(\text{invisible}))$	$0 < m_a < 1600$	Long-lived	$\sqrt{ K_e^{e\tau} ^2 + K_L^{e\tau} ^2}$	$2.3 imes 10^{-4}$
$\mathcal{B}(\tau \to \mu a(\text{invisible}))$	$0 < m_a < 1600$	Long-lived	$\sqrt{ K_e^{\mu\tau} ^2 + K_L^{\mu\tau} ^2}$	3.2×10^{-4}
$\mathcal{B}(\mu o e \gamma \gamma)$	$0 < m_a < 105$	$\gamma\gamma$	$\sqrt{ K_e^{e\mu} ^2 + K_L^{e\mu} ^2}$	2.6×10^{-6}
$\mathcal{B}(\mu \to 3e)$	$0 < m_a < 105$	e^+e^-	$\sqrt{ K_e^{e\mu} ^2 + K_L^{e\mu} ^2}$	3.1×10^{-7}
$\mathcal{B}(\tau^- \to \mu^- e^+ e^-)$	$200 < m_a < 1671$	e^+e^-	$\sqrt{ K_e^{\mu\tau} ^2 + K_L^{\mu\tau} ^2}$	6.1×10^{-7}
$\mathcal{B}(\tau \to 3e)$	$200 < m_a < 1776$	e^+e^-	$\sqrt{ K_e^{e au} ^2 + K_L^{e au} ^2}$	$7.5 imes 10^{-7}$
$\mathcal{B}(\tau \to 3\mu)$	$211 < m_a < 1671$	$\mu^+\mu^-$	$\sqrt{ K_e^{\mu\tau} ^2 + K_L^{\mu\tau} ^2}$	6.6×10^{-7}
$\mathcal{B}(\tau^- \to \mu^- \pi^- K^+)$	$633 < m_a < 1671$	$\pi^- K^+$	$\sqrt{ K_e^{\mu\tau} ^2 + K_L^{\mu\tau} ^2}$	1.1×10^{-6}

* Weaker bounds apply, if the ALP is too heavy to be on shell











Note the that $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ give rise to **complementary constraints**, and in many cases Mu3e will provide **stronger bounds** than MEG II !









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tree level

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Conclusions

- ALPs with masses below 10 GeV (and higher) would potentially lead to interesting new-physics effects in a variety of flavor observables
- * Allows one to probe flavor-changing ALP couplings to quarks and leptons down to few $10^{-9} \Lambda/\text{TeV}$ (quarks) and few $10^{-7} \Lambda/\text{TeV}$ (leptons)
- In lepton case, ALP represent a class of models where future bounds from Mu3e experiment will outperform those of MEG II