

# Accelerator Physics\*

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(\*These slides are based on the lecture slides prepared by Prof. Litvinenko and you can find more materials from CASE website:  
[http://case.physics.stonybrook.edu/index.php/Main\\_Page](http://case.physics.stonybrook.edu/index.php/Main_Page))



*Billions of these tubes were made in 20<sup>th</sup> century – now most of them are in the landfills...*

# Outline

- How accelerators work
  - Overview of an accelerator facility
  - Charged particle sources
  - Way to accelerate charged particles
  - Circular accelerator
    - Phase stability/auto-phasing (how to keep particles together in the longitudinal direction)
    - Orbit stability (how to keep particle together in the transverse direction)

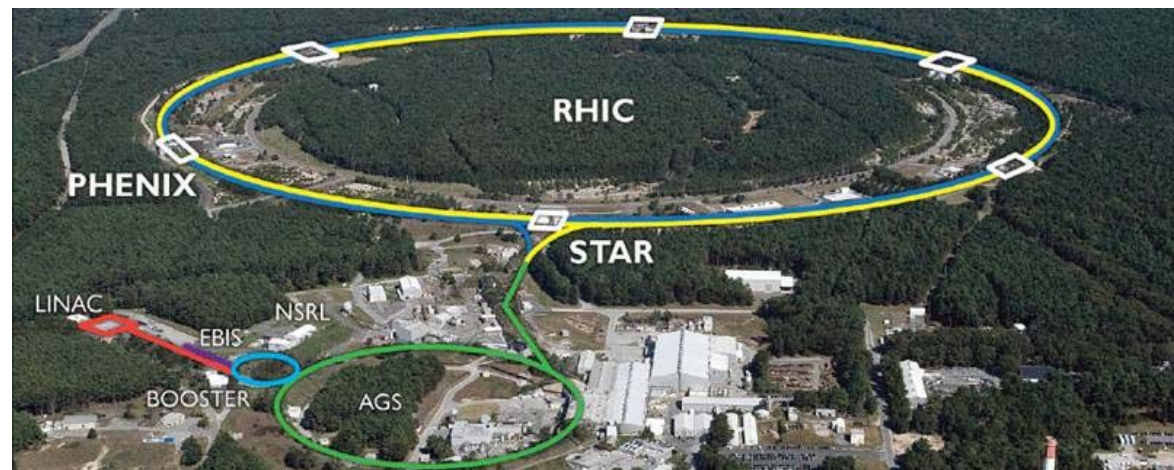
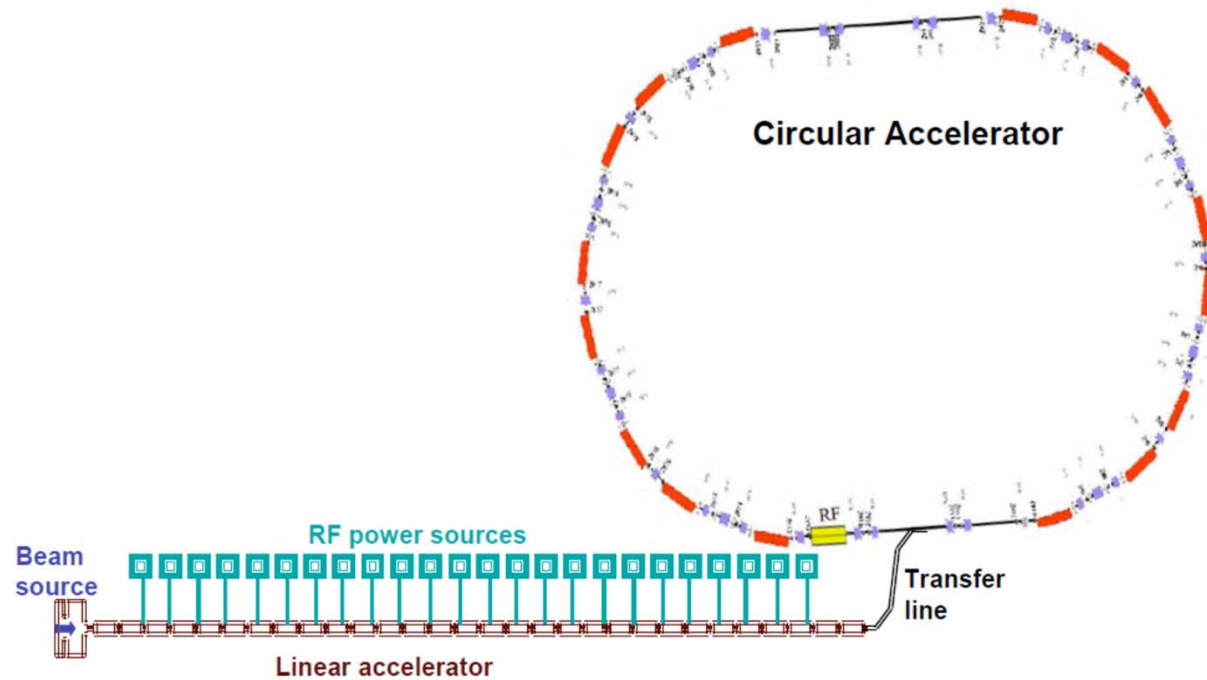
# Outline continued

- Application of accelerators
  - Scientific applications
    - Fundamental particle physics: colliders
    - Fundamental sciences using of synchrotron radiation, and FEL radiation
  - Medical
    - Medical diagnostics, cancer therapy, pharmaceutical research
  - Material science
    - Ion implant (essential for semiconductor industry), crosslinking of rubber, electron beam welding
  - Sterilization

# What Accelerators Are Good For

- High Energy Physics
  - Explore the electro-weak bosons Z, W (LEP)
  - Find and exploit “new“ and heavy quarks (Tevatron)
  - Find the HIGGS (LHC)
  - Well, this list will never be complete .....
- Nuclear Physics (RHIC, SPS)
  - First evidence of a new state of matter, quark gluon plasma? (SPS)
  - Create the QGP and determine its properties (RHIC)
  - Could it be something else? (EIC)
- Chemistry, Biology, Medicine, Material Sciences
  - Find the structure of molecules, proteins, cells...
  - Could people survive interstellar travel? (NASA Space Radiation Laboratory (NSRL))
  - Time-resolved structural changes in a natural (fsec) time scale
- Civil, Industrial and Military Applications
  - Treat cancers, produce isotopes for medical imaging, sterilize products...
  - Scan containers in ports for undesirable content (n's?)
  - High power free electron lasers as weapons for a ship defence

# Overview: Generic accelerator facility



# What do we accelerate?

- Usually we accelerate stable **charged** particles (particle has to be charged since we use electric field to accelerate them)

Particle	Charge	Charge, C	Rest mass, kg	Rest mass, $eV/c^2$
Electron, $e^-$	-e	$-1.60 \cdot 10^{-19}$	$9.11 \cdot 10^{-31}$	$0.511 \cdot 10^6$
Positron, $e^+$	+e	$+1.60 \cdot 10^{-19}$	$9.11 \cdot 10^{-31}$	$0.511 \cdot 10^6$
Proton, p	+e	$+1.60 \cdot 10^{-19}$	$1.6726 \cdot 10^{-27}$	$938.27 \cdot 10^6$
Antiproton	-e	$-1.60 \cdot 10^{-19}$	$1.6726 \cdot 10^{-27}$	$938.27 \cdot 10^6$
Ion, $Z_A$	$Ze$		$\sim A \cdot u$	$\sim A \cdot u$
Atomic mass unit, u			$1.6605 \cdot 10^{-27}$	$931.49 \cdot 10^6$

**Speed of the light, c**

**2.99792  $10^8$  m/sec**

$$1eV = 1.602 \cdot 10^{-19} J$$

1 eV – energy gained by an electron passing through a 1V potential differential

- Dedicated radioactive ion facility to accelerator unstable ion: FRIB at MSU
- There are discussions and developments towards a collider using unstable muon beam which has 2 microsecond lifetime in the rest frame.

# How to tell the performance of an accelerator? (Key parameters)

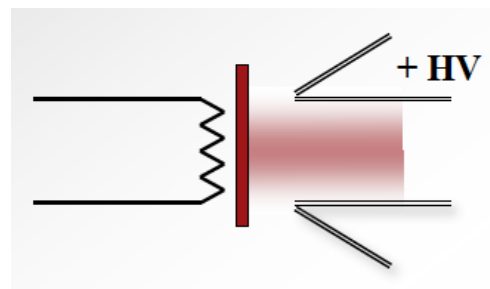
- **Energy** of the particle : keV, MeV, GeV, TeV...  
Au... 28 TeV at RHIC, 7 TeV protons at LHC, 10 keV electrons in X-ray tube, few MeV protons in Van-De-Graph (SBU basement),
- **Luminosity** or event rate, instantaneous and integrated luminosity
- **Beam intensity** - Number of particles per second, i.e. beam current ( $\Rightarrow$  instantaneous luminosity)
- **Beam quality** - transverse and longitudinal emittance, which is simply phase-space (remember Louisville theorem) occupied by the particles and its projections ( $\Rightarrow$  instantaneous luminosity)
- **Beam lifetime** – number of particles lost per second, i.e. Loss rate, lifetime limiting processes ( $\Rightarrow$  integrated luminosity)

1keV =  $10^3$  eV, 1 MeV =  $10^6$  eV, 1 GeV =  $10^9$  eV , 1TeV=  $10^{12}$ eV, ...1eV =  $1.6 \cdot 10^{-19}$  J

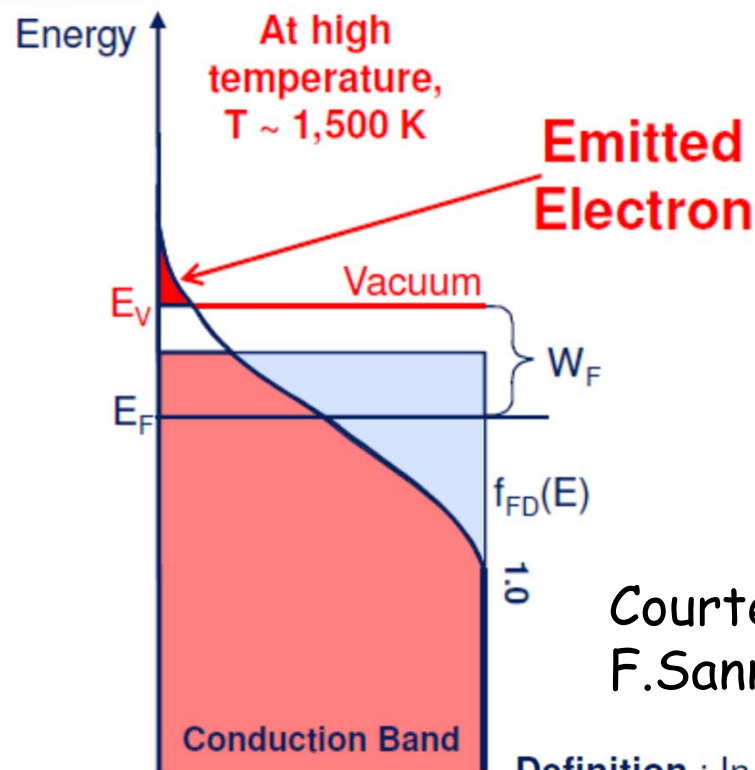
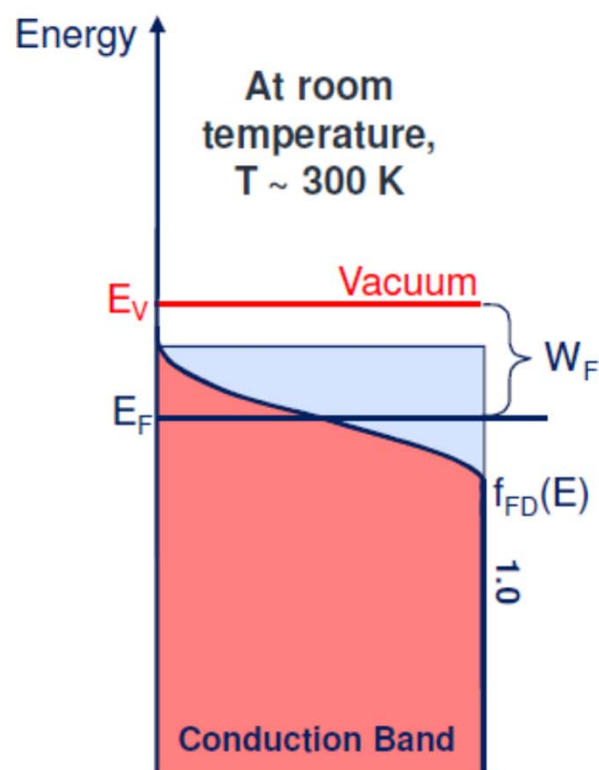
1 nsec =  $10^{-9}$  sec, 1 psec =  $10^{-12}$  sec, 1 fsec =  $10^{-15}$  sec, 1 asec =  $10^{-18}$  sec....

# Thermionic electron source

- Heated metals



**Definition:** the **work function**  $W_F$  is the energy needed to bring an electron from the Fermi level to the vacuum level



Courtesy to  
F.Sannibale

$$J = AT^2 e^{-w/kT}$$

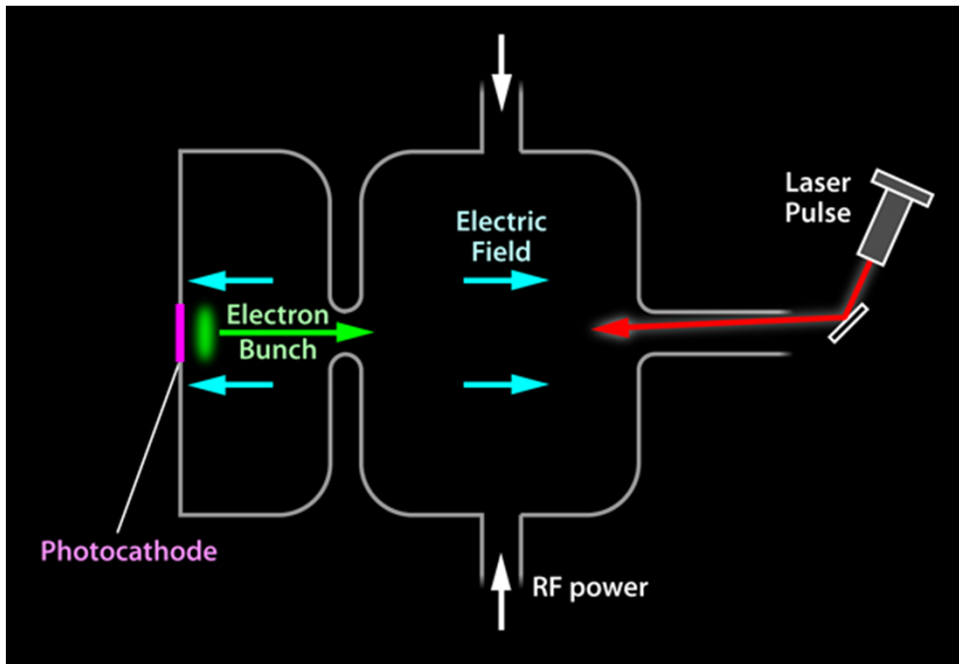
$$A = \frac{4\pi m k^2 e}{h^3} = 1.20173 \times 10^6 \text{ A m}^{-2} \text{ K}^{-2}$$

$w \equiv$  work function

**Definition :** In a system of fermions the **Fermi energy**  $E_F$  is the energy of the highest occupied state at zero temperature.



# Photo-emission electron source



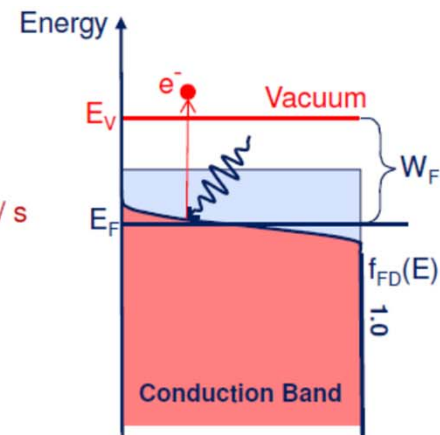
A **photocathode** is a surface engineered to convert light (photons) into electrons using the **photoelectric effect**. Photocathodes are important in accelerator physics where they are used inside of a photoinjector to generate high brightness electron beams.

$$\text{Photon Energy} = E_{ph} = h\nu$$

Planck Constant =  $6.626068 \times 10^{-34} \text{ m}^2 \text{ kg} / \text{s}$

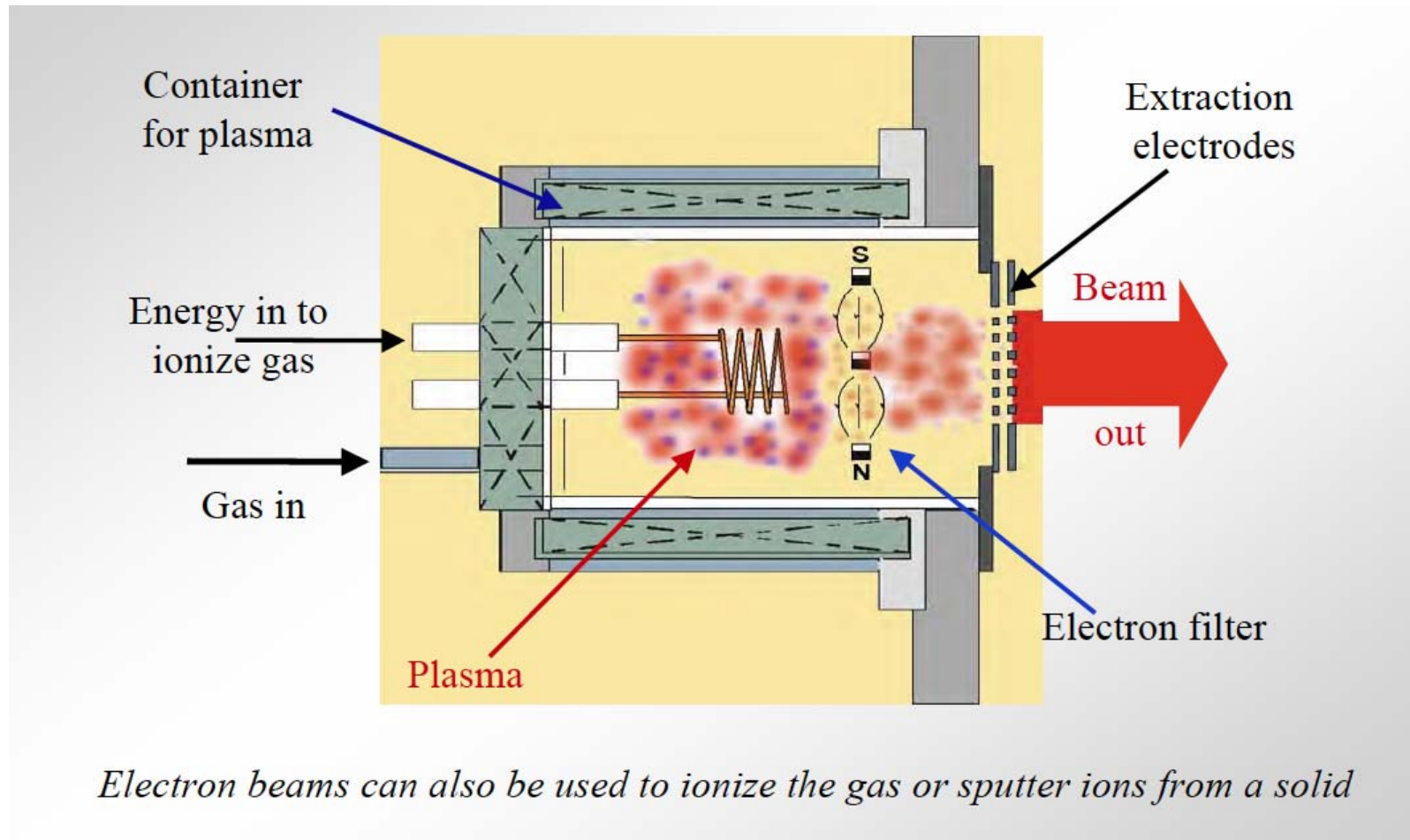
$$\text{If } E_{ph} \geq W_F$$

$$T_{e^-} = E_{ph} - W_F$$



Courtesy to F.Sannibale

# Typical ion source



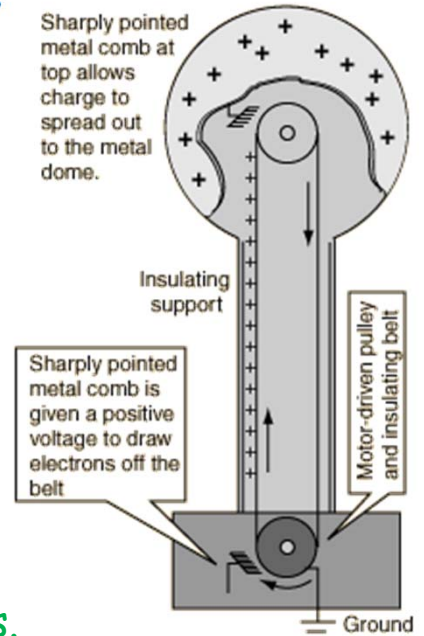
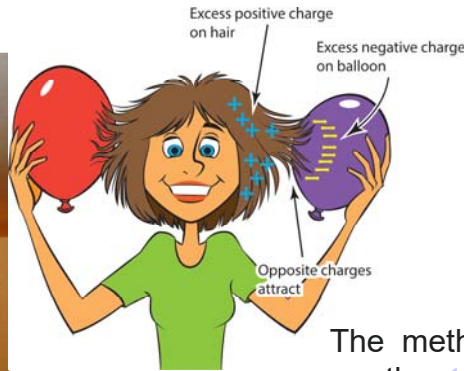
Courtesy of W. Barletta

# How to Accelerate charged particle?

- Methods of acceleration:
  - Electrostatic acceleration
  - Induction acceleration
  - Radio-Frequency (RF) fields
  - Advanced acceleration methods
    - Plasma wakefield accelerations
    - Dielectric wakefield accelerators
    - Photonic gap acceleration

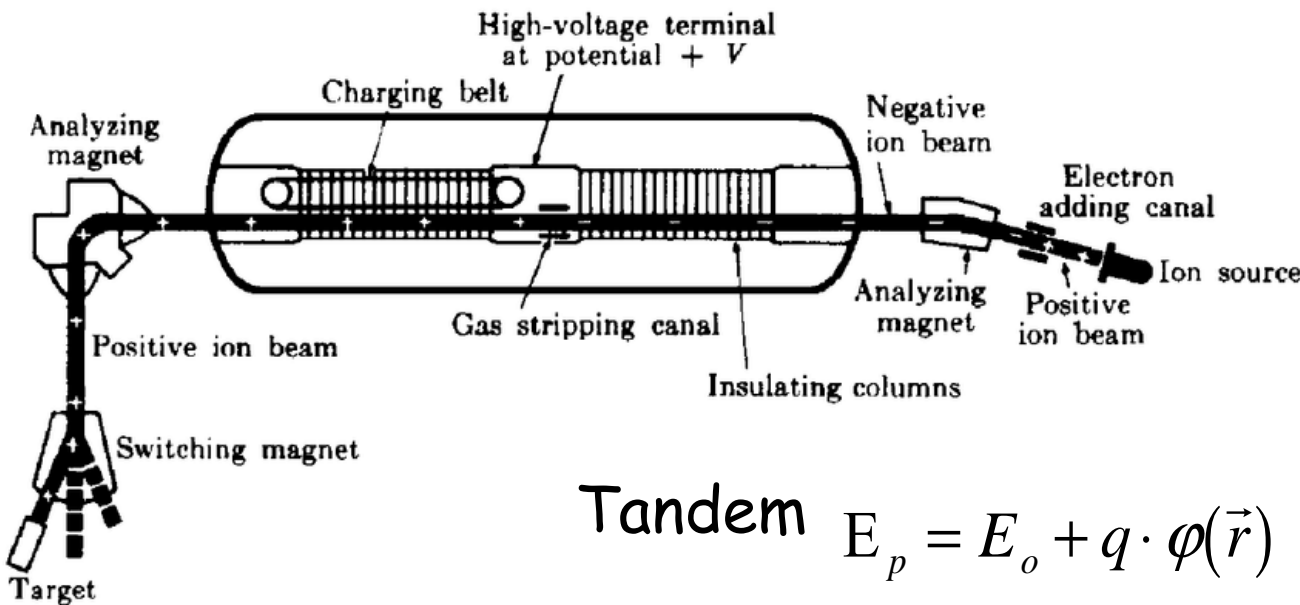
# How to Accelerate charged particle?

## Electrostatic: Van De Graff Generator

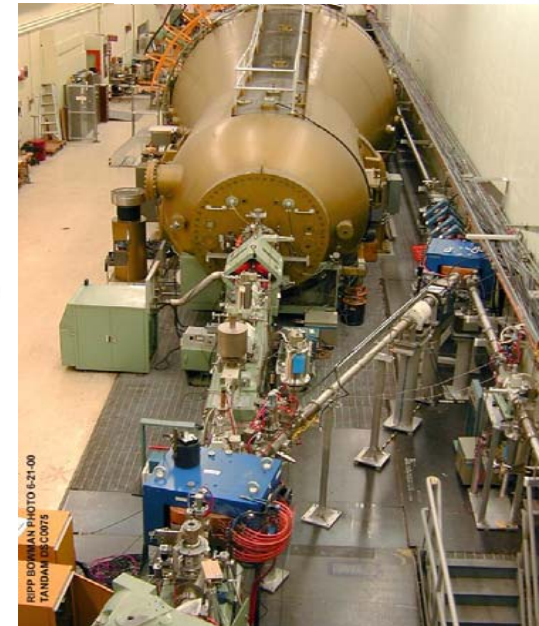


The method of charging is based on the [triboelectric effect](#), such that simple contact of dissimilar materials causes the transfer of some electrons from one material to the other.

Tandem accelerator is an updated configuration with two accelerations.



Tandem  $E_p = E_o + q \cdot \phi(\vec{r})$

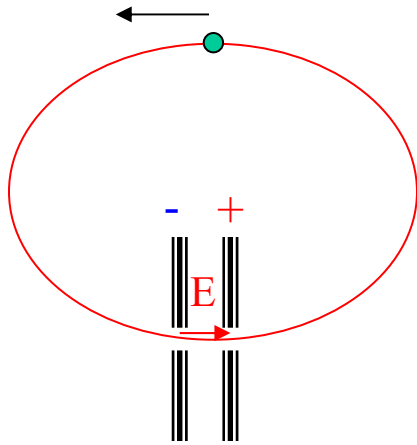


What LIMITS electrostatic acceleration?

Is it possible to accelerate particle many times  
in the same DC accelerator?

**NO!**

EM II: 1<sup>st</sup> pair of Maxwell's Equations



$$\vec{E} = -\text{grad}\varphi - \frac{1}{c} \frac{\partial \vec{A}}{\partial t};$$

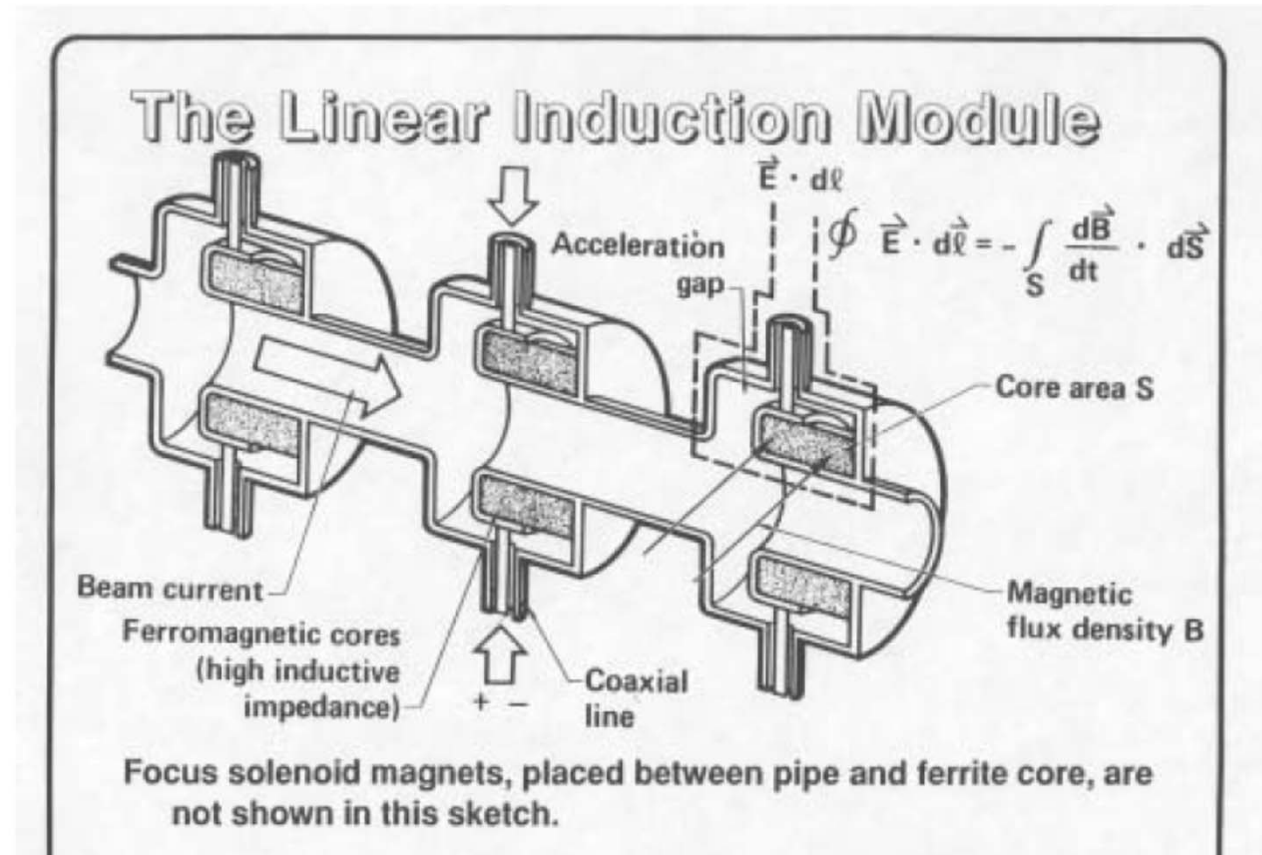
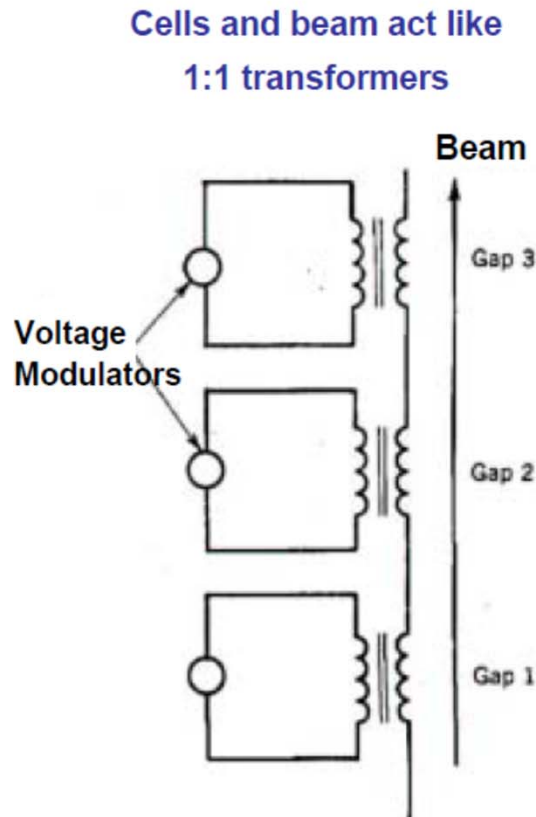
$$\vec{H} = \text{curl}\vec{A};$$

$$dE = q(\vec{E} \cdot d\vec{r}) \Rightarrow \Delta E_{\text{turn}} = q \oint \vec{E} \cdot d\vec{r} = -q \left( \varphi(\vec{r}_o, t + \tau) - \varphi(\vec{r}_o, t) + \frac{1}{c} \oint \frac{\partial \vec{A}}{\partial t} \cdot d\vec{r} \right);$$

Hence static field has limitation:

$$\frac{\partial \vec{A}}{\partial t} = 0, \quad \frac{\partial \varphi}{\partial t} = 0 \Rightarrow \Delta E_{\text{turn}} = 0;$$

# Induction Accelerator

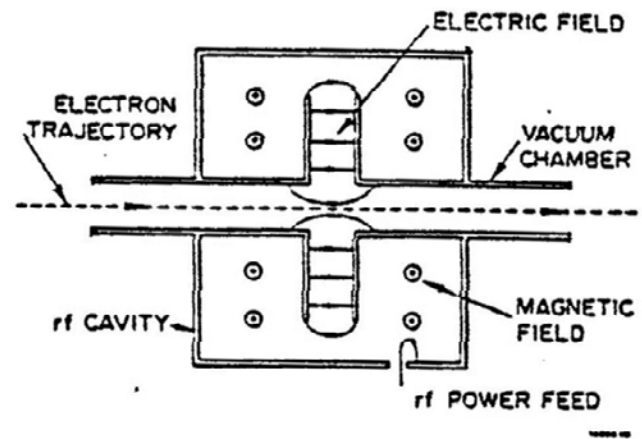


Changing magnetic fields generate accelerating electric field.

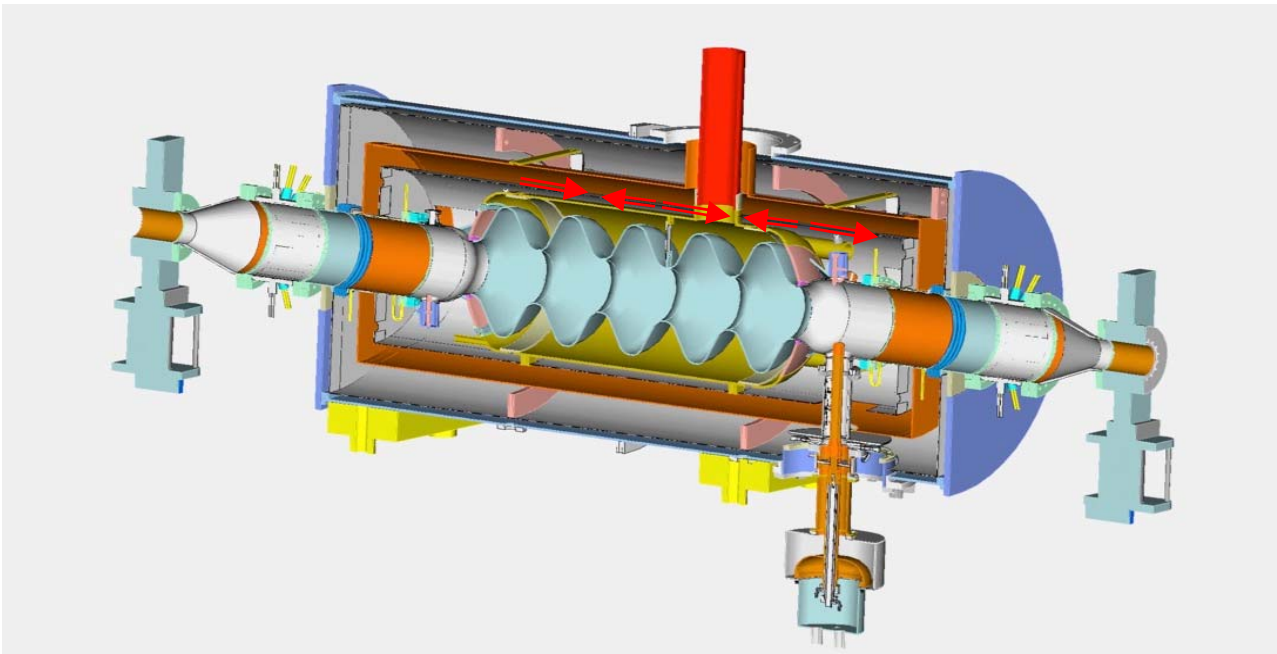
Pro/Cons: Low energy, high current applications:

- Induction accelerators can handle very **large currents** (up to 10KA)
- Generate much **lower voltage** than typical RF accelerators.

# RF accelerators

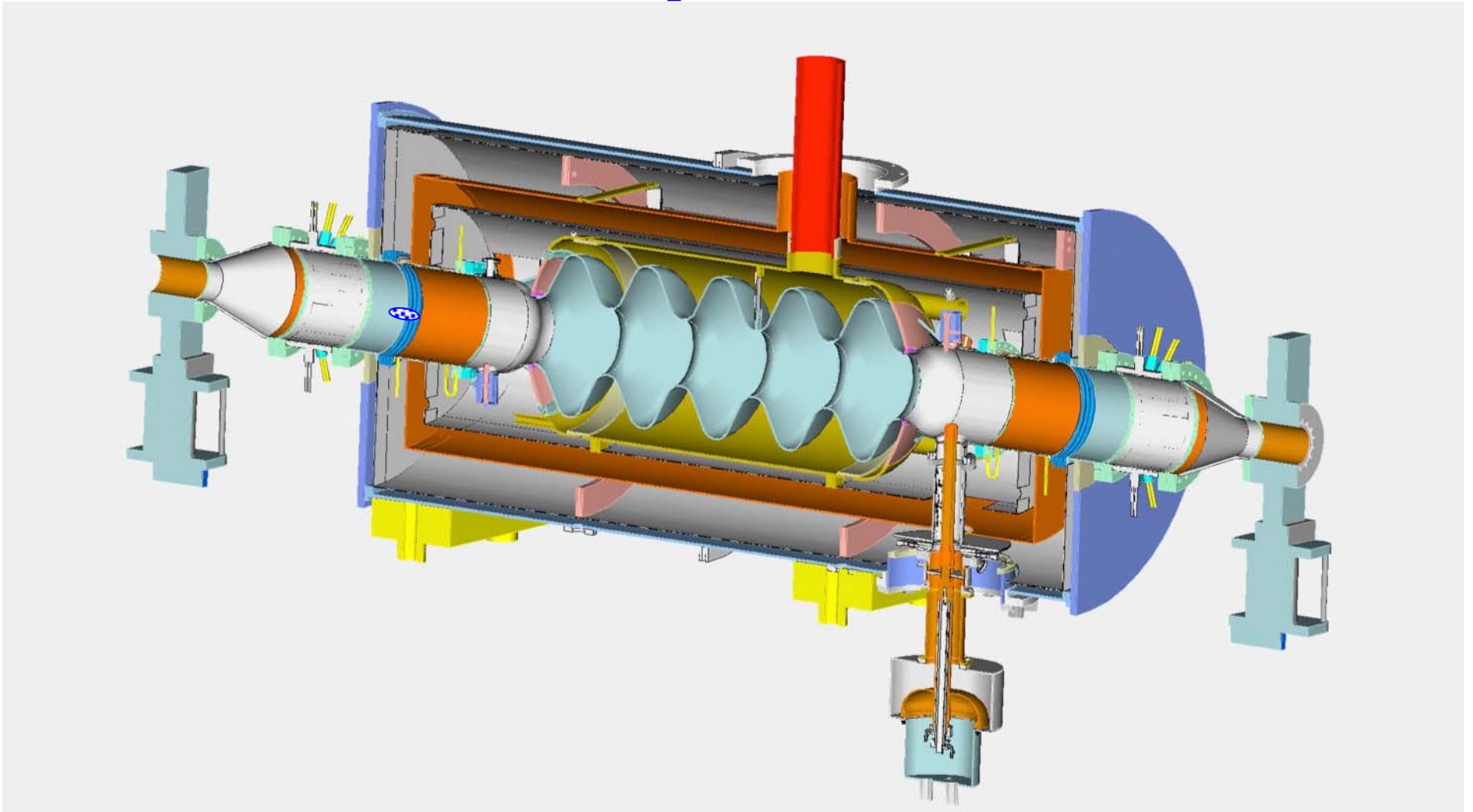


Schematic diagram of an rf accelerating cavity.



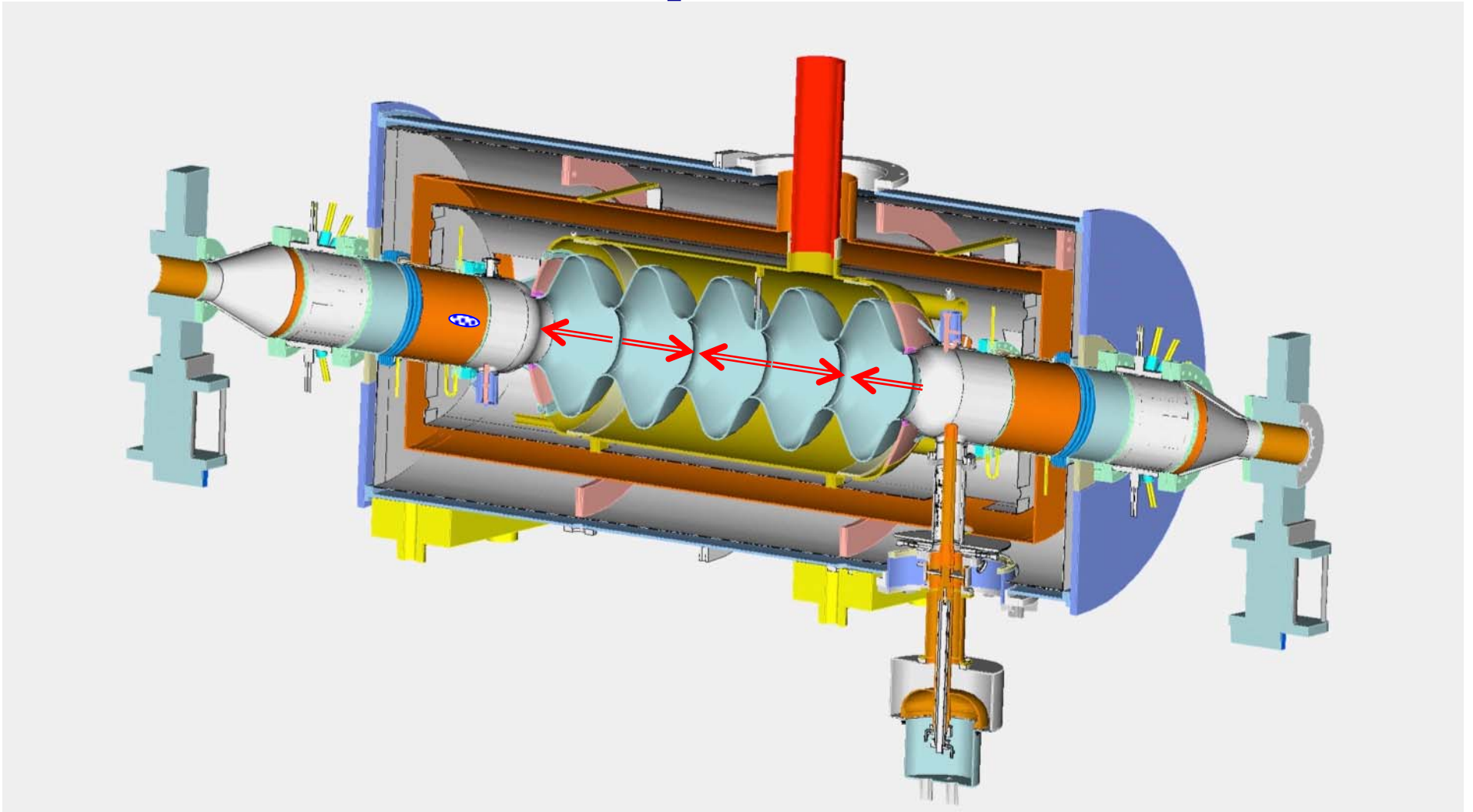
# How $\beta=1$ RF accelerator works?

## In pictures

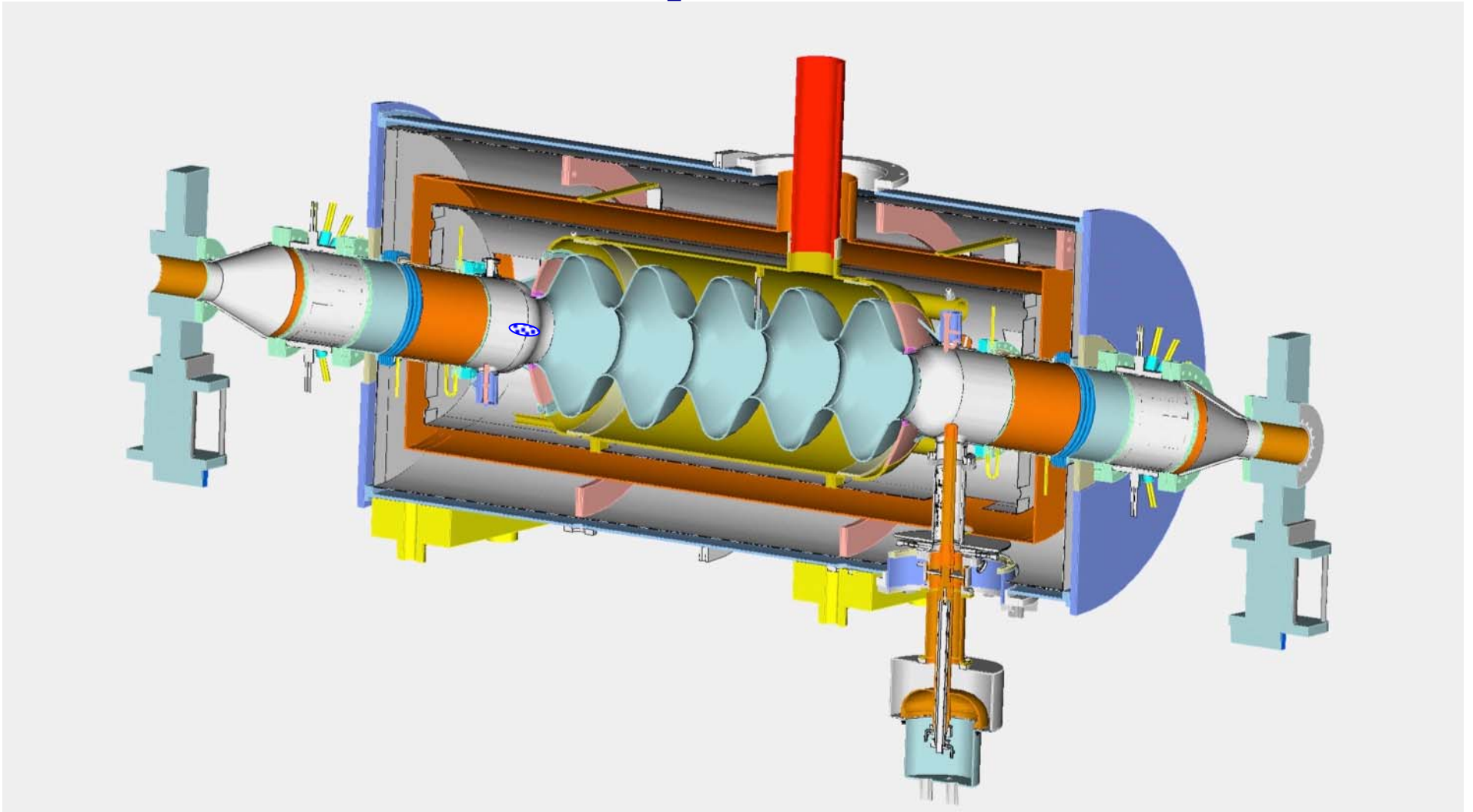




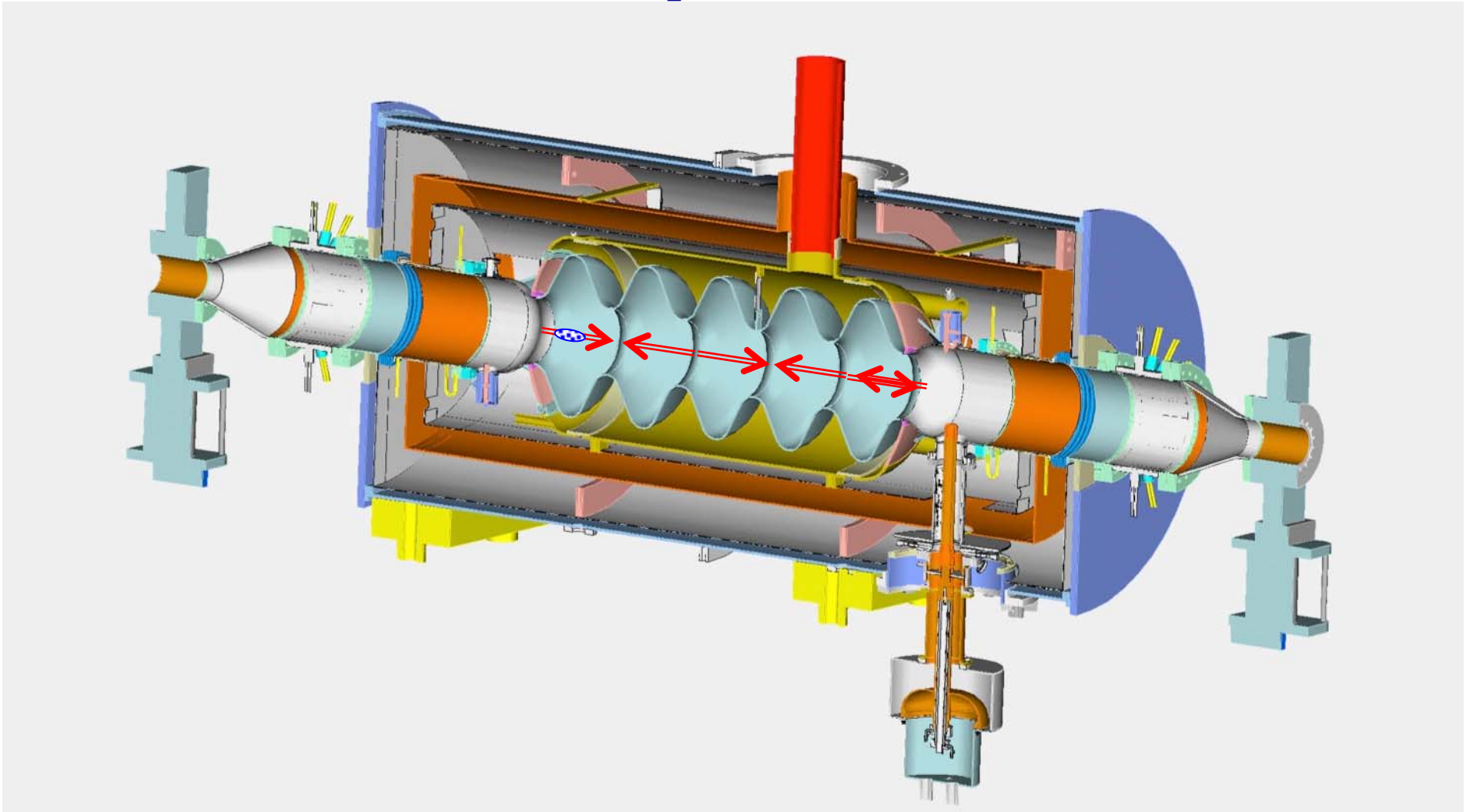
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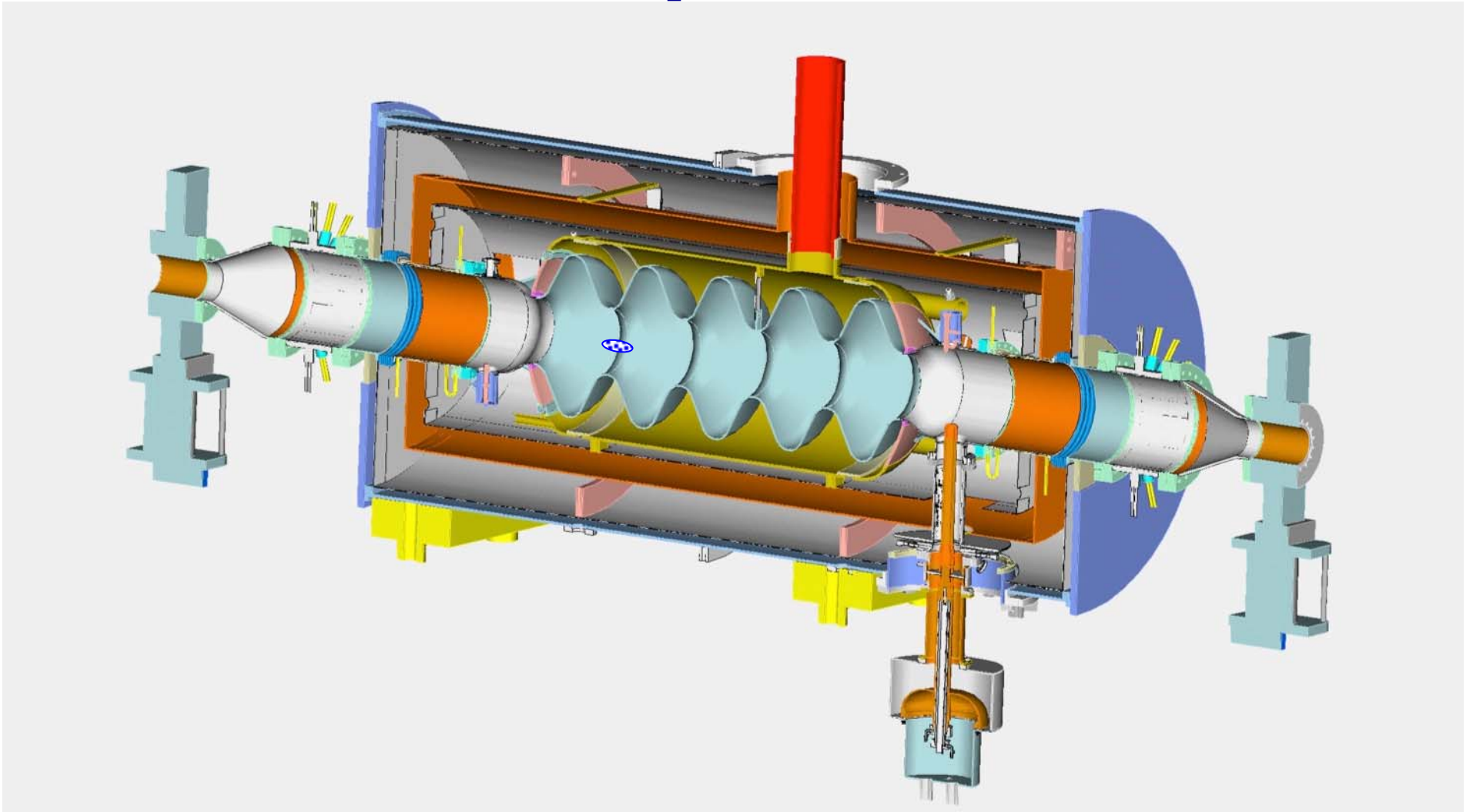
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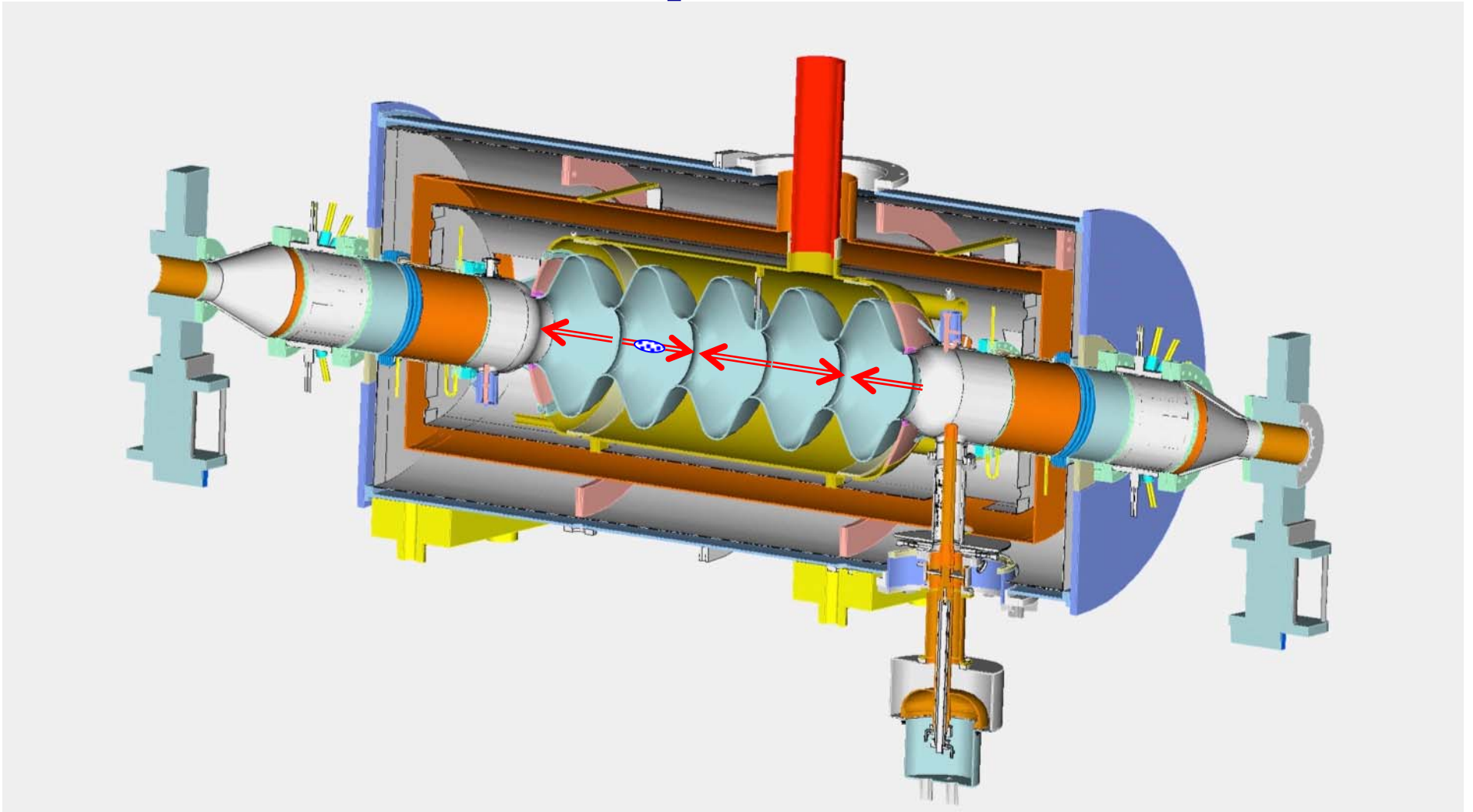


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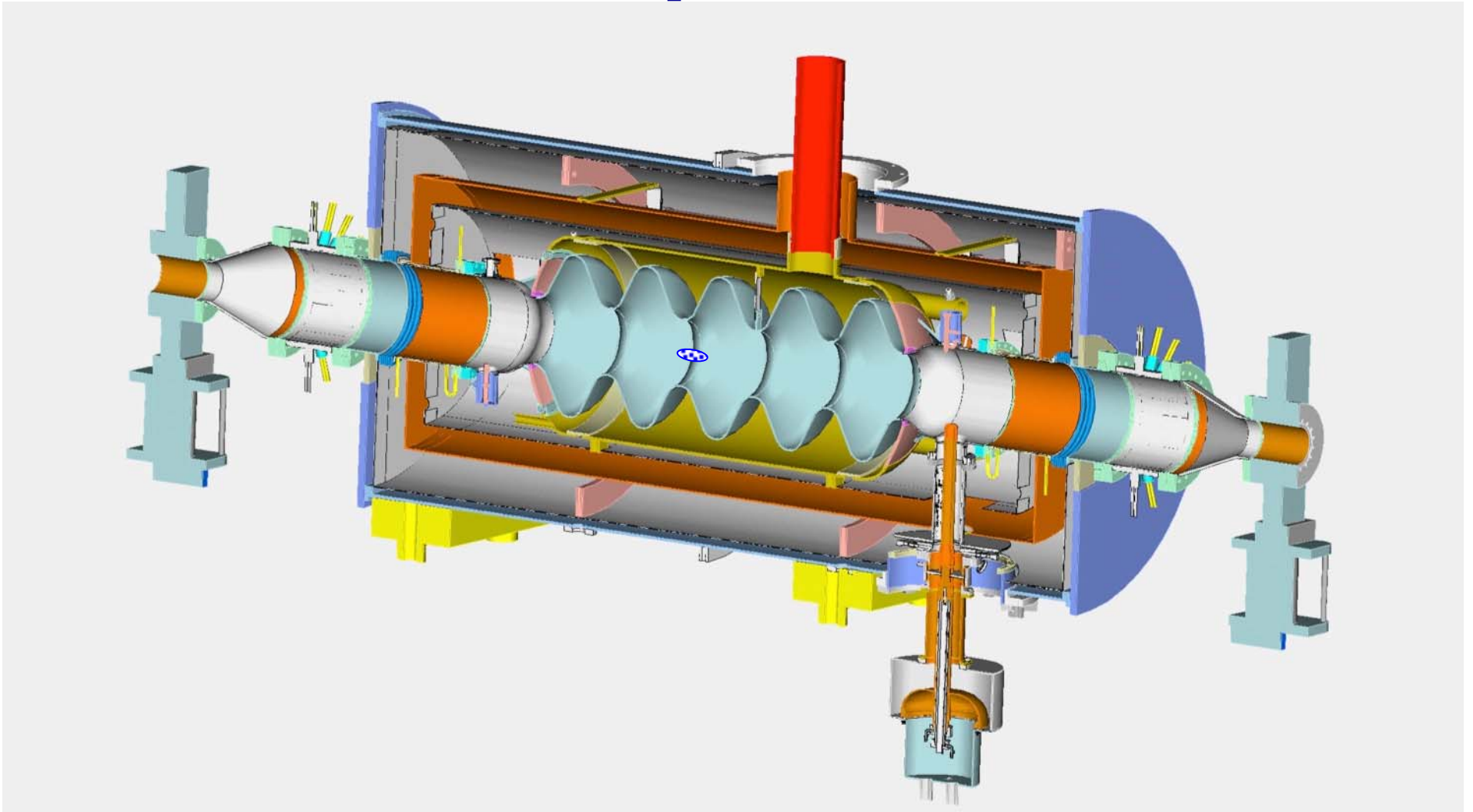


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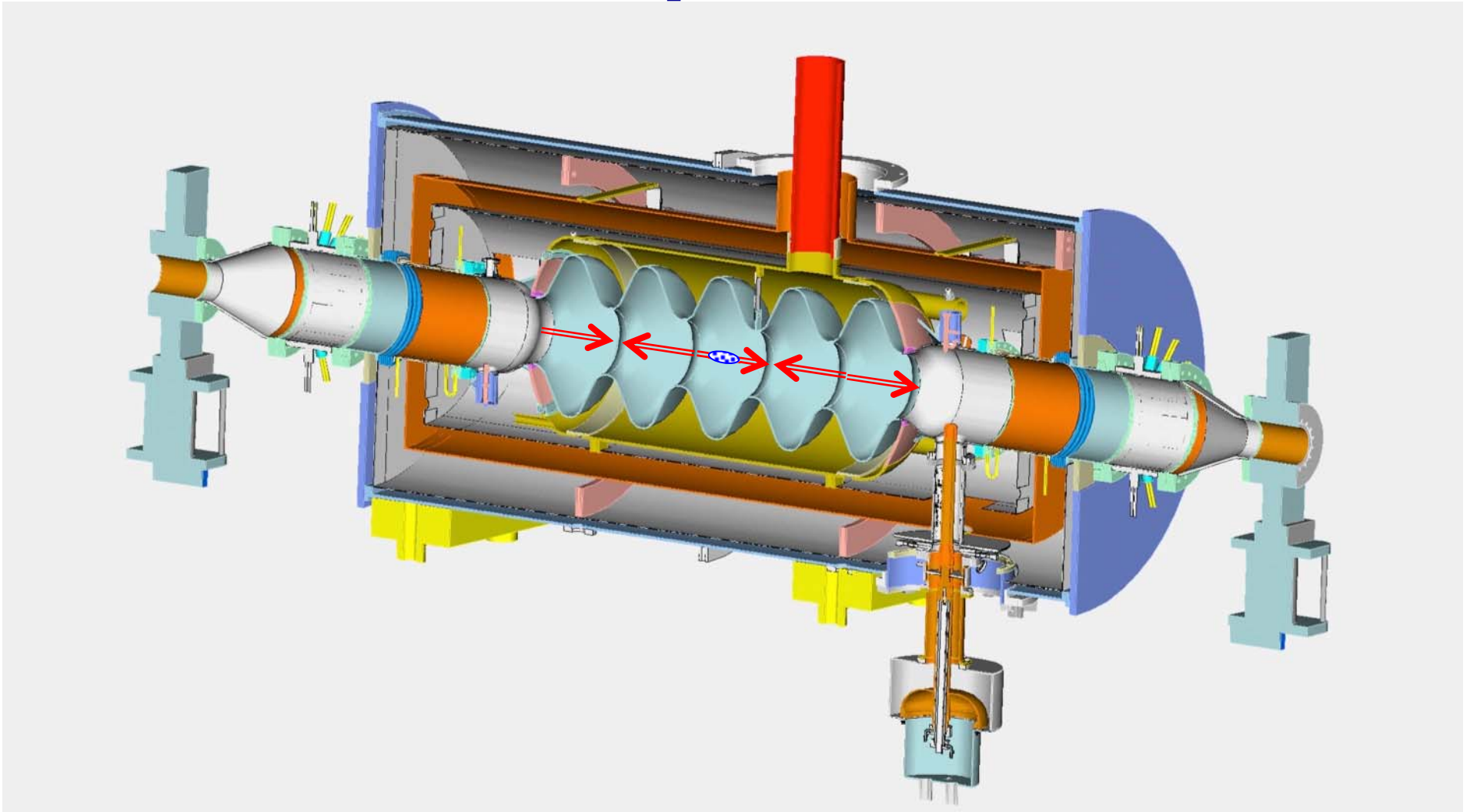
## In pictures



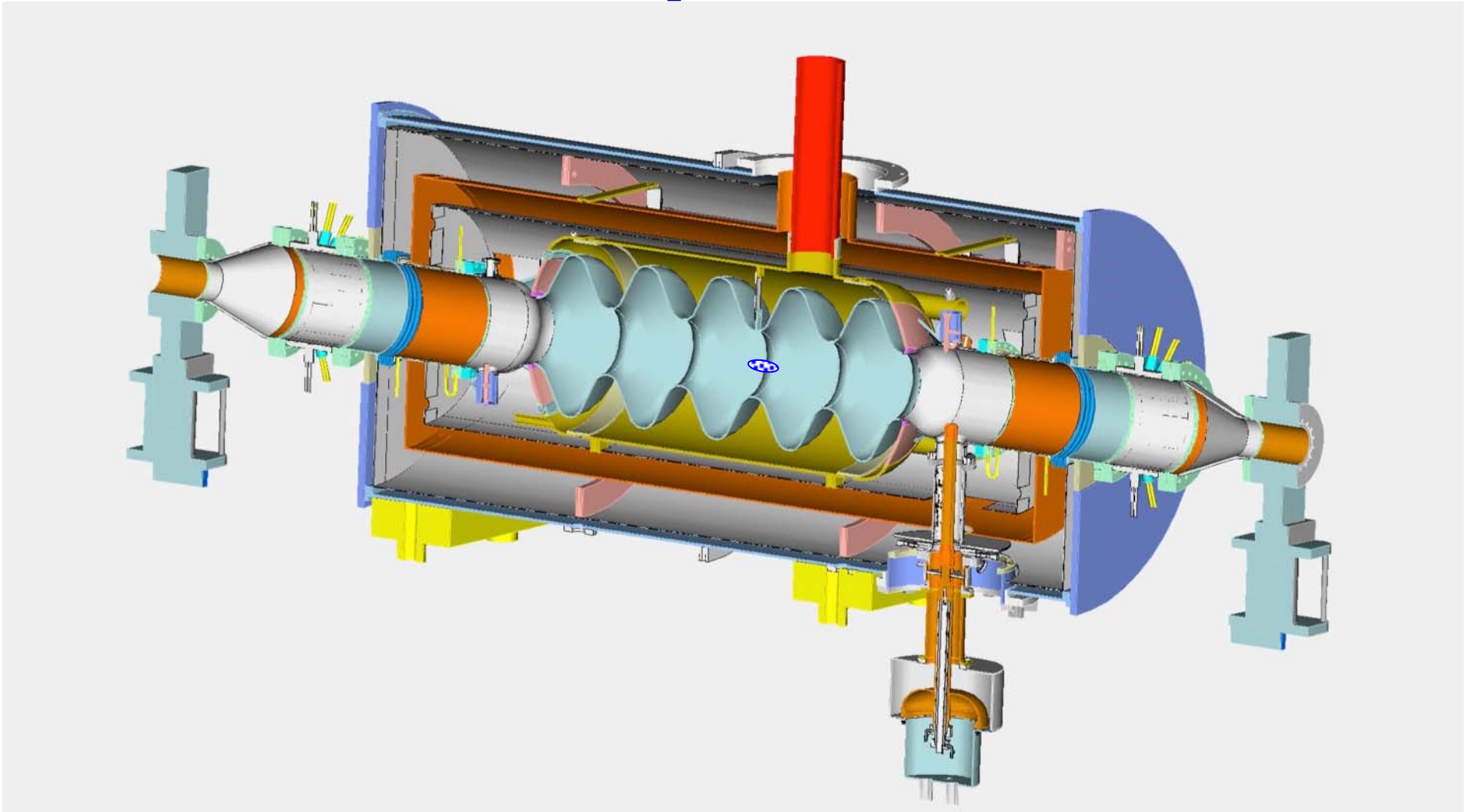
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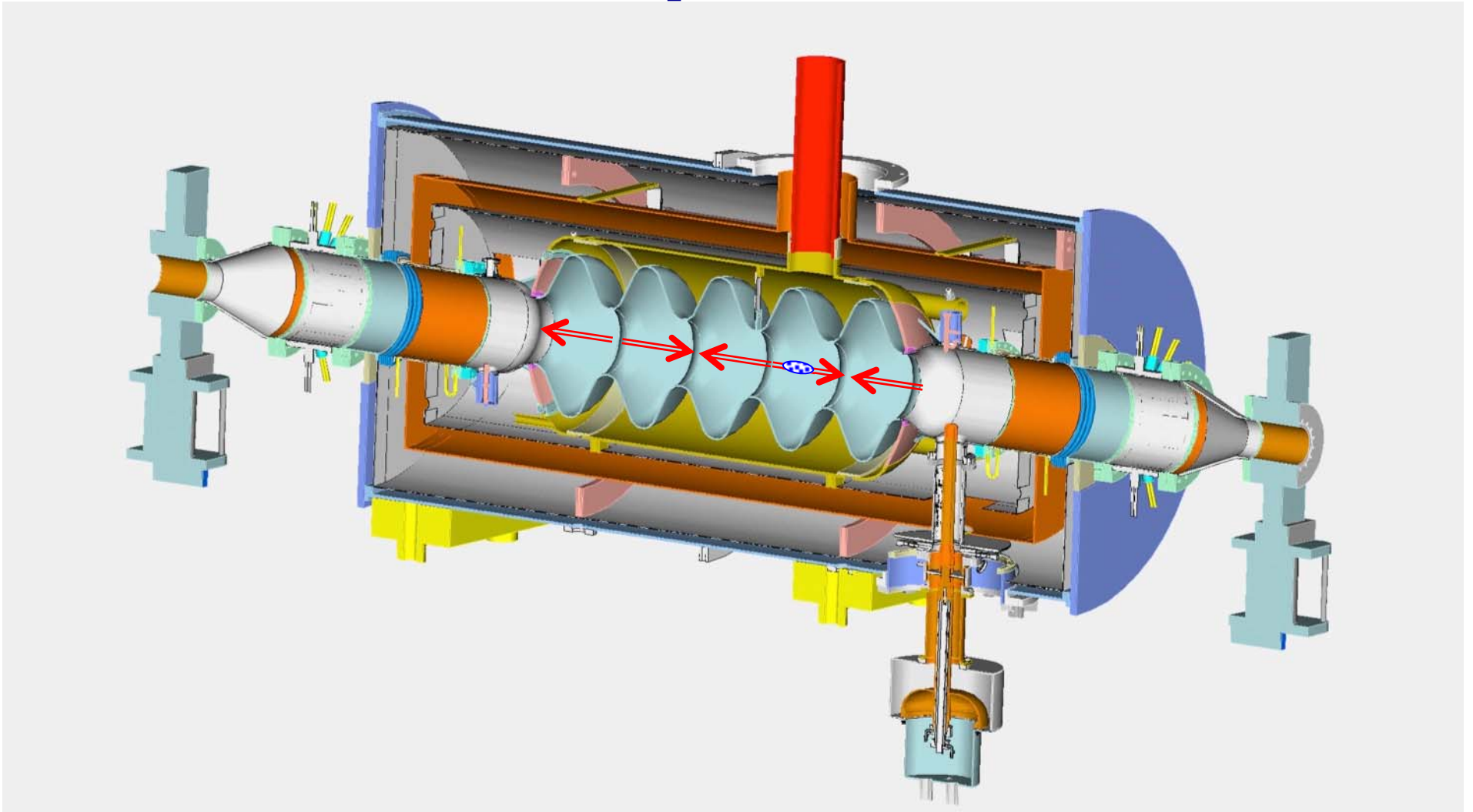
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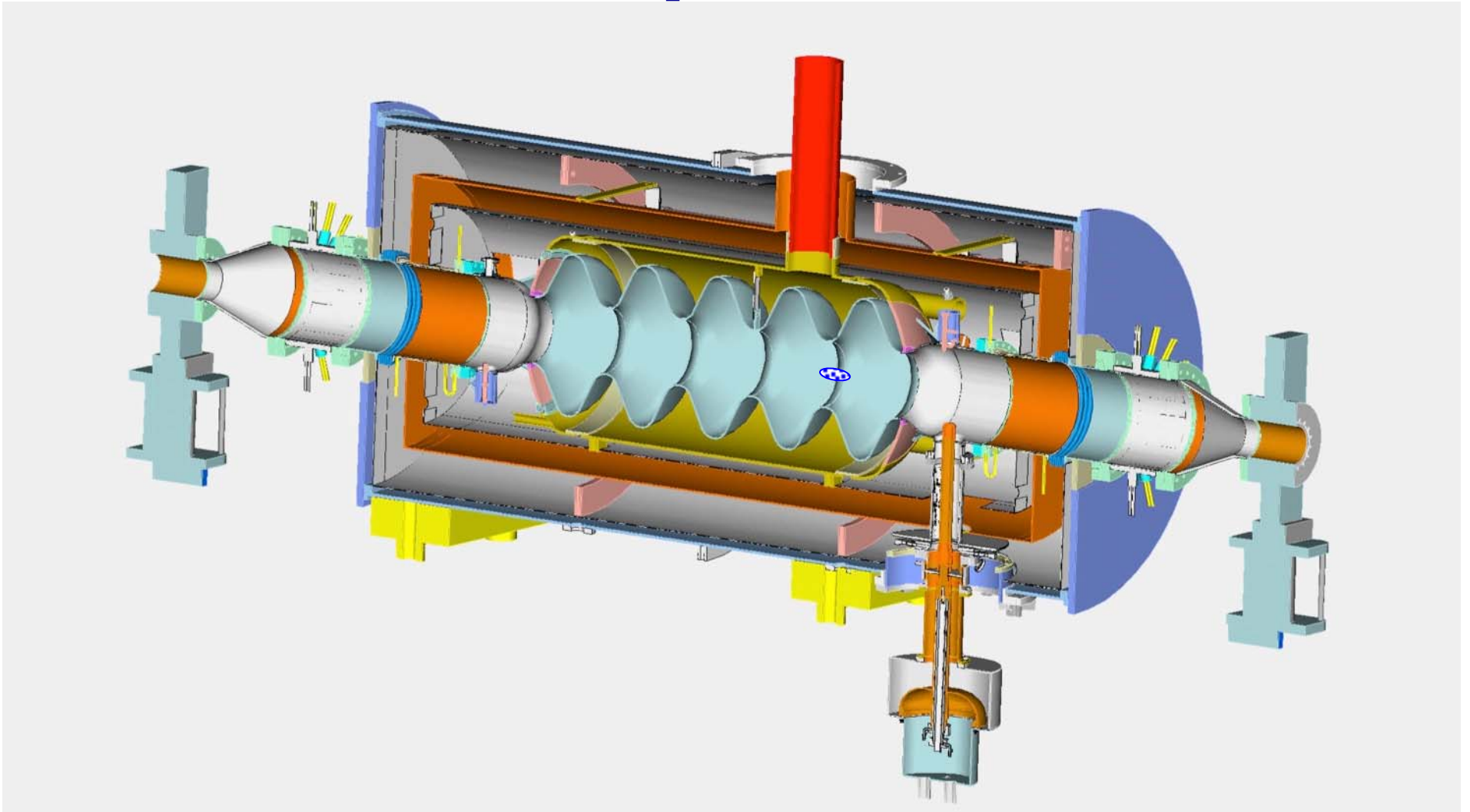


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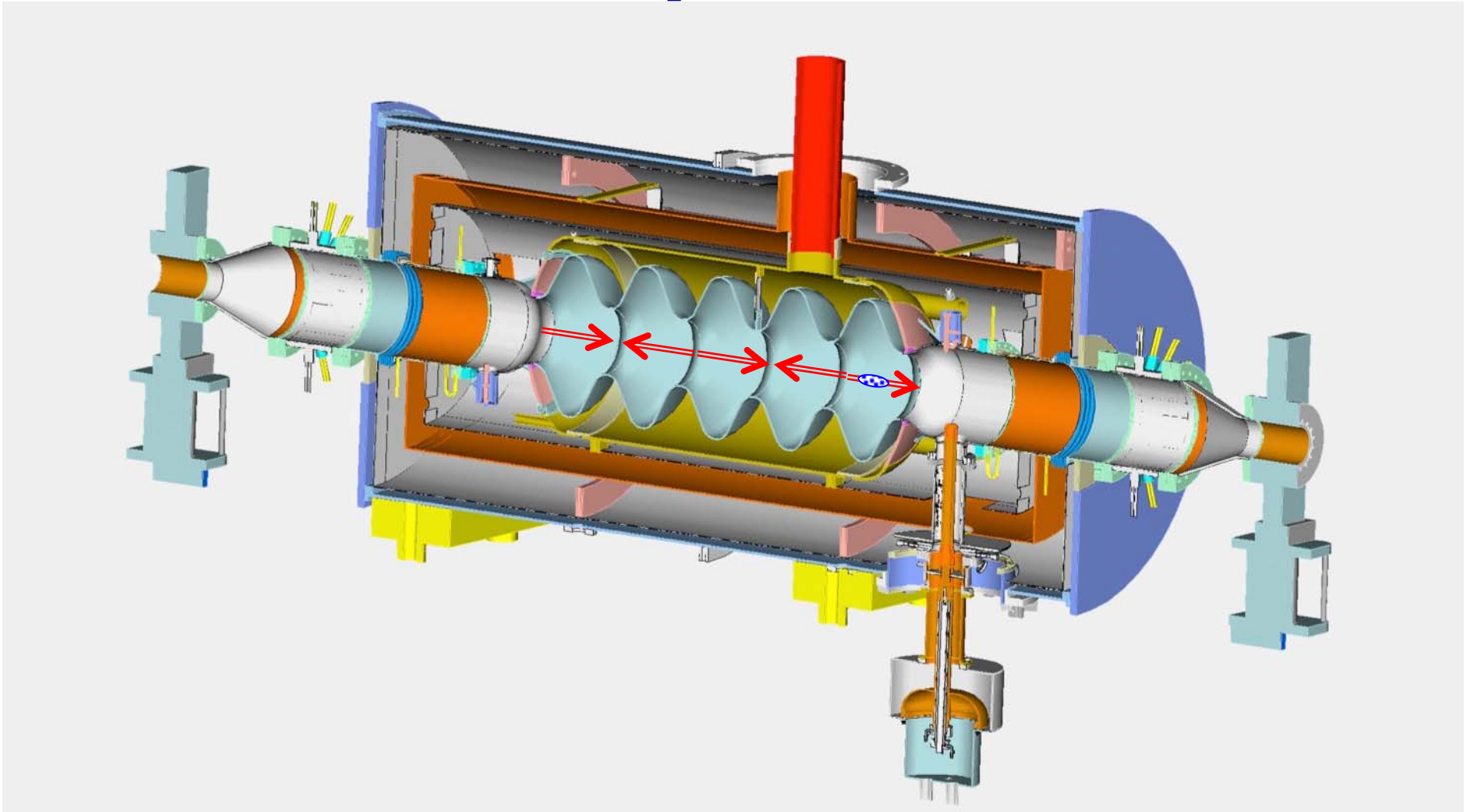
## In pictures



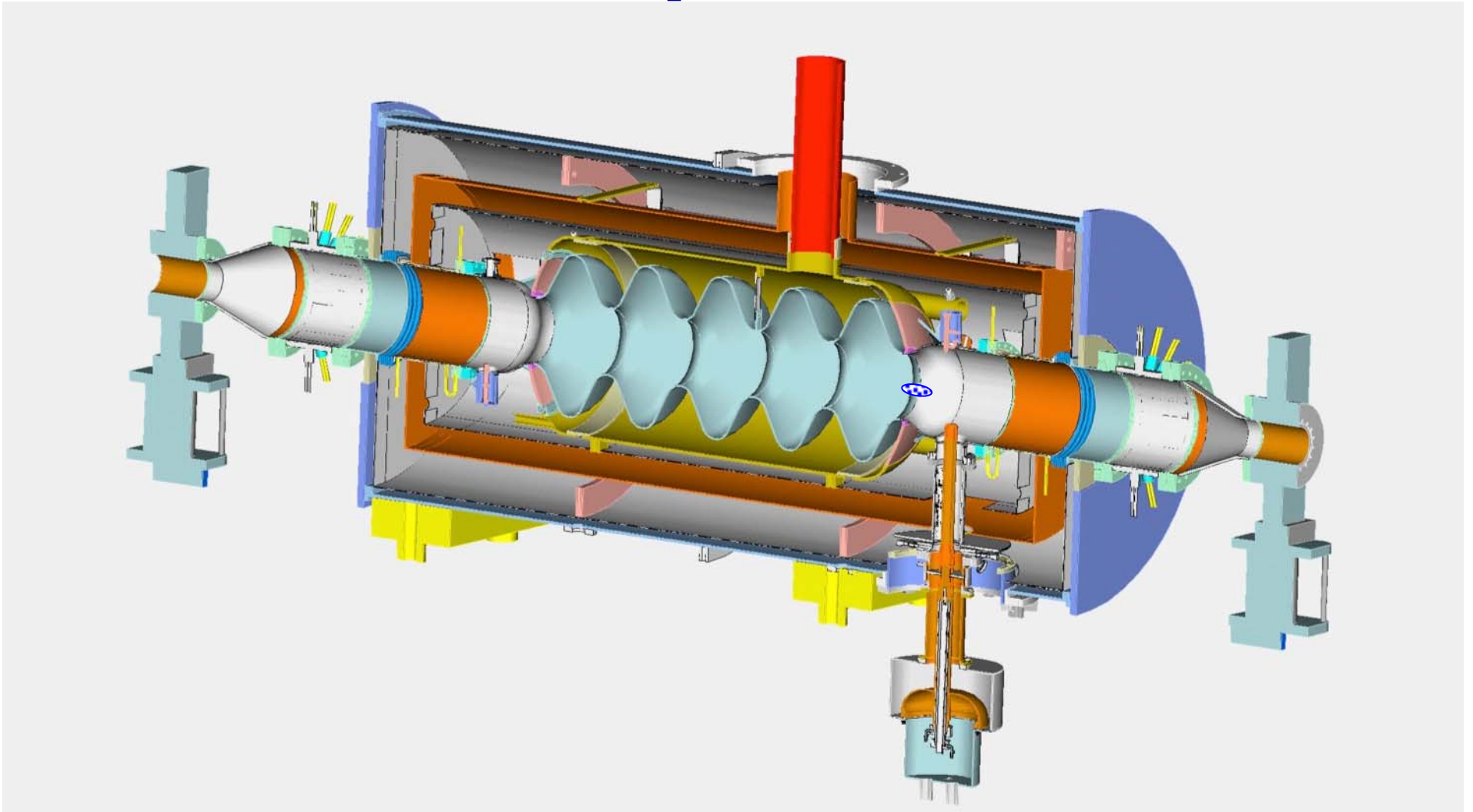
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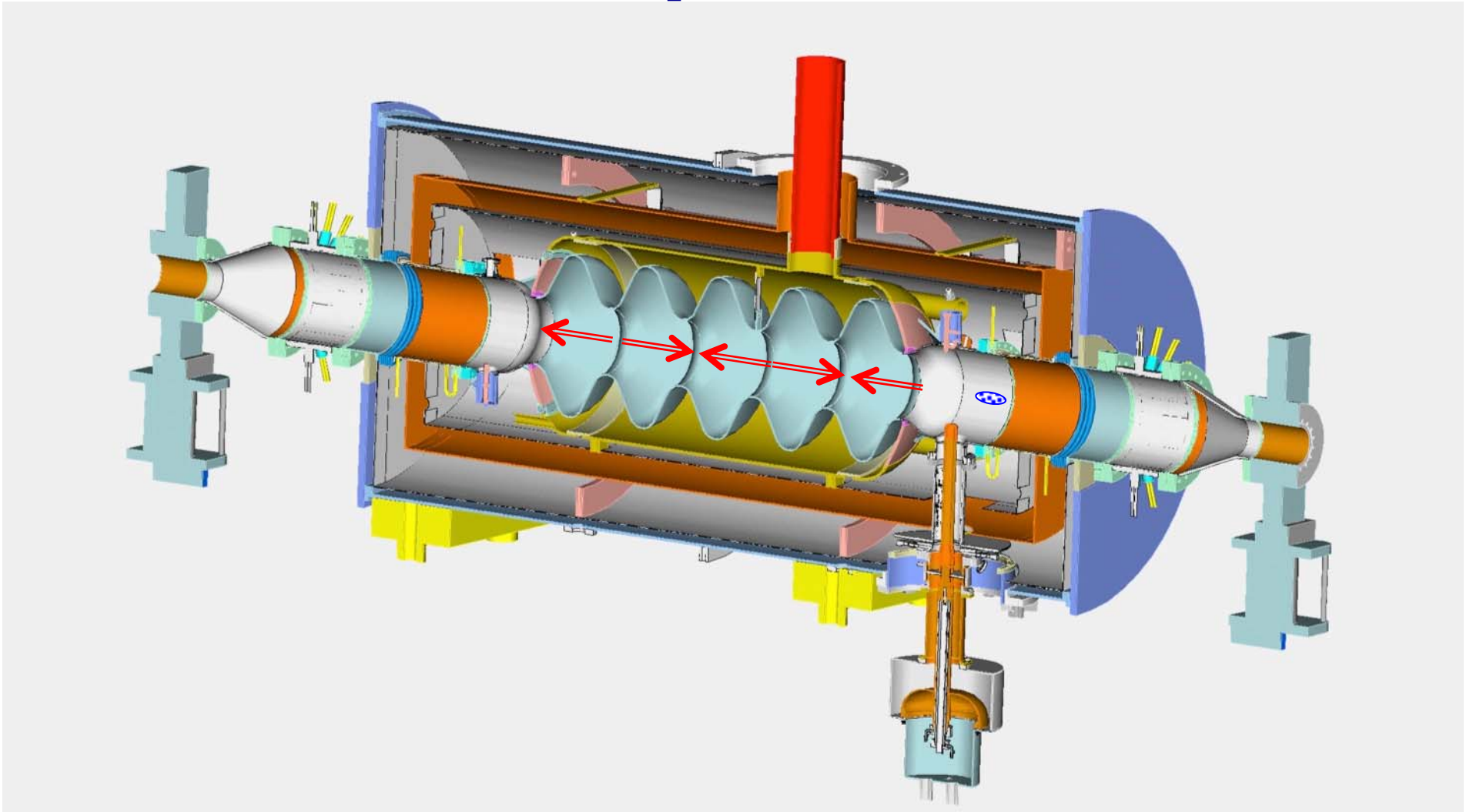


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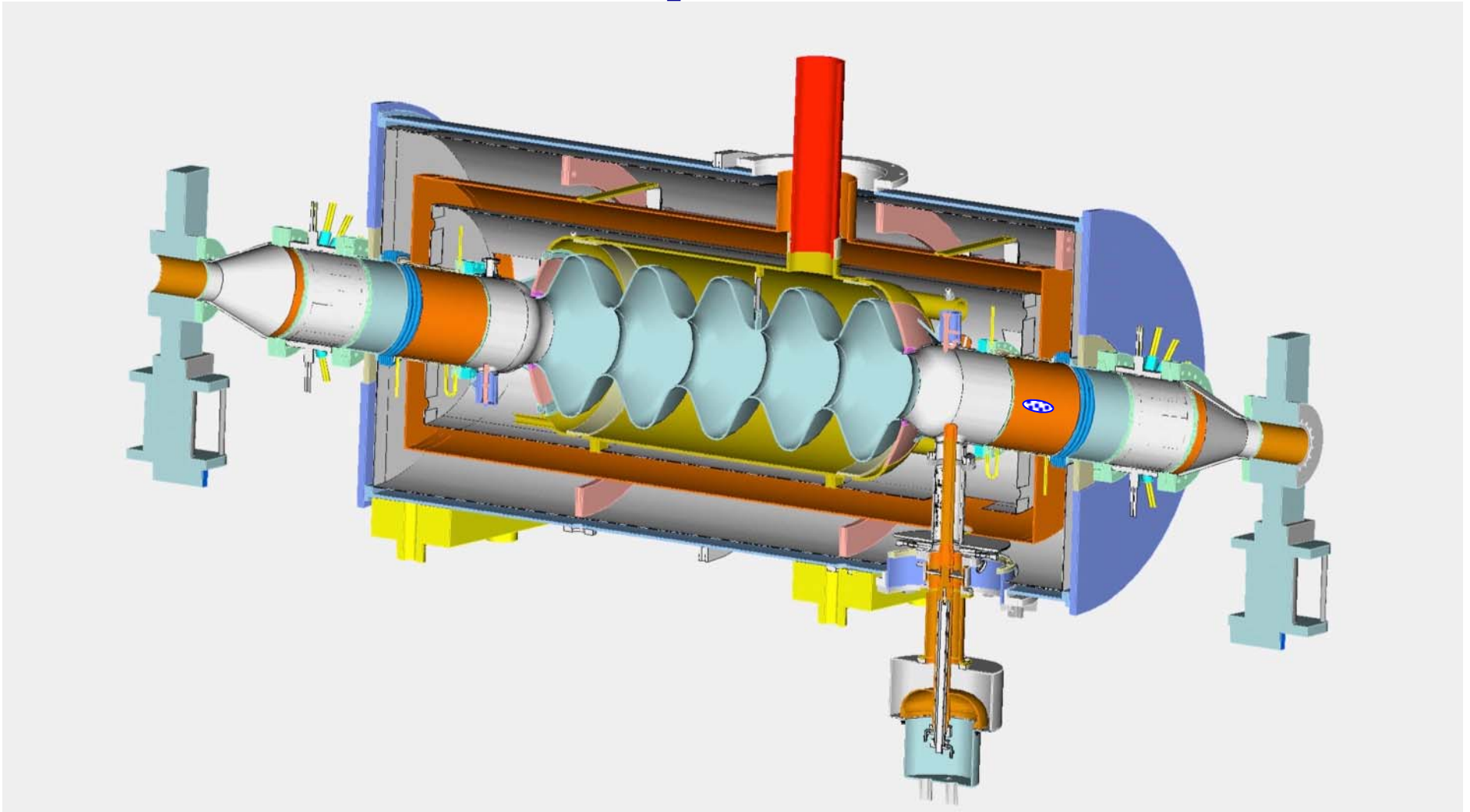


# How $\beta=1$ RF accelerator works?

## In pictures

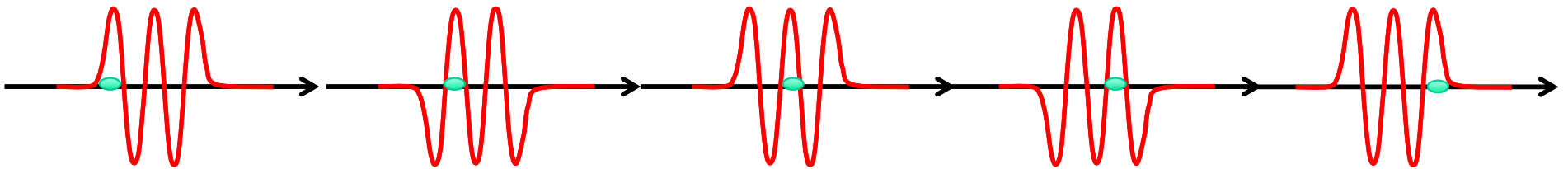
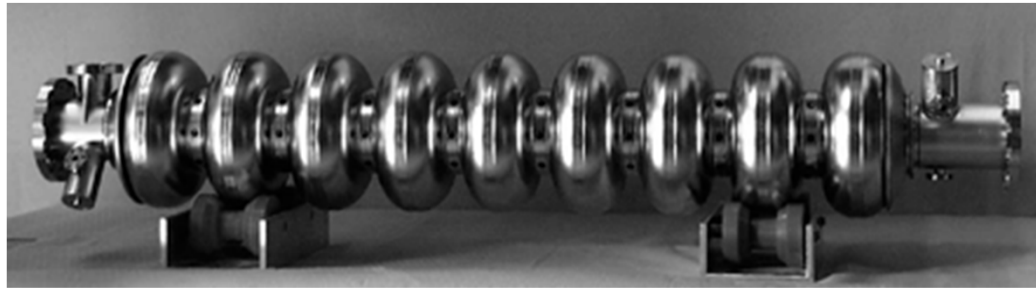
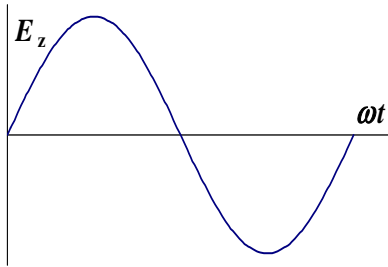


# How $\beta=1$ RF accelerator works? In pictures



# RF accelerator

$$\frac{dE}{dt} \equiv mc^2 \frac{d\gamma}{dt} = e\vec{\mathbf{E}}(\vec{r}, t) \cdot \vec{v};$$



$$\langle e\vec{\mathbf{E}}(\vec{r}, t) \cdot \vec{v} \rangle \neq 0$$

# The field limits of RF accelerator

Some limiting factor

- **Heating**  
RF field deposits power as heat, which, if not being removed efficiently, can lead to damage of the cavity.
- **RF breakdown**  
Breakdown occurs when a plasma discharge is generated in the cavity. When it occurs, all the incoming RF is reflected back up the coupler.
- **Field emission/dark current trapping**
- **Multipacting**
- **Quench**

RF accelerators limits:

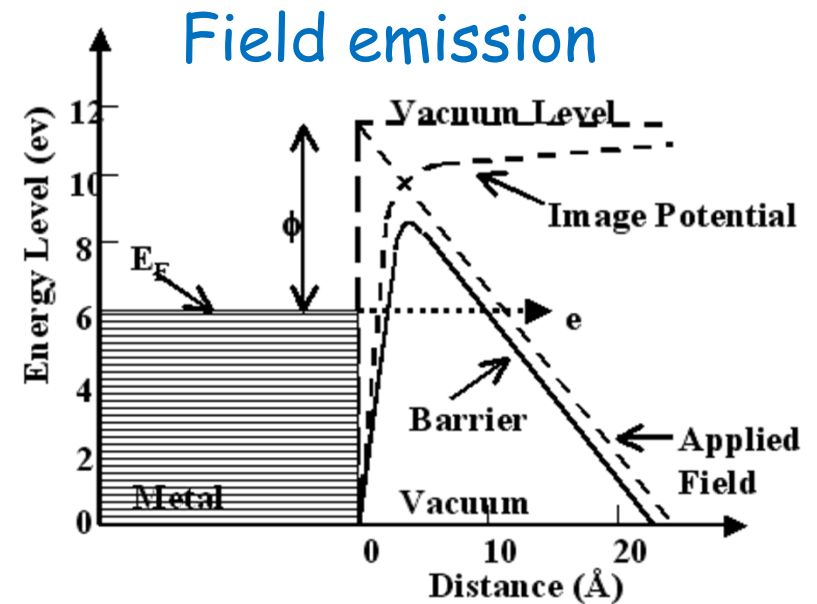
Room  $t^\circ$ : pulsed  $\sim 150$  MV/m

CW  $\sim 2$  MV/m

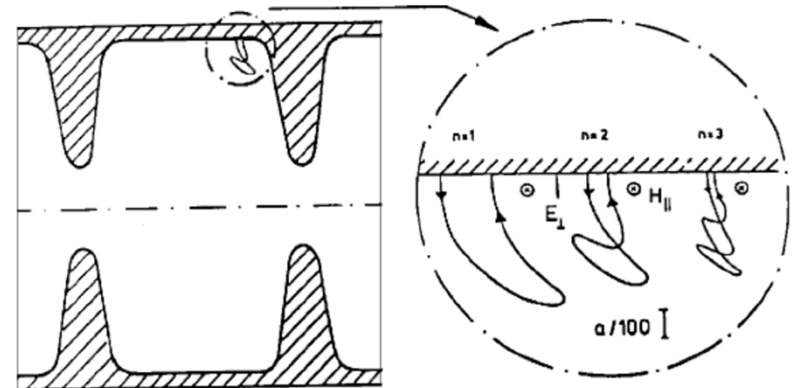
Superconducting ( $2K^\circ$ )

pulsed  $\sim 50$  MV/m

CW  $\sim 20$  MV/m



## Multipacting



Courtesy to Dr. G. Burt

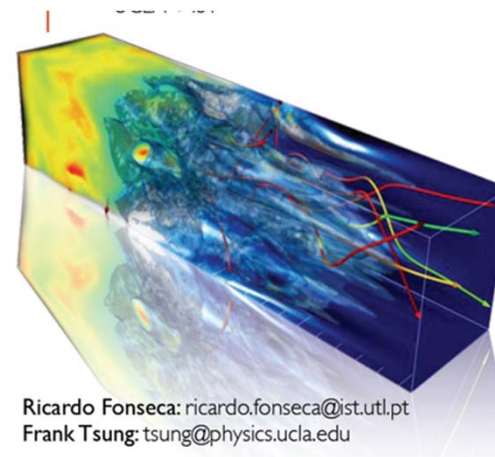
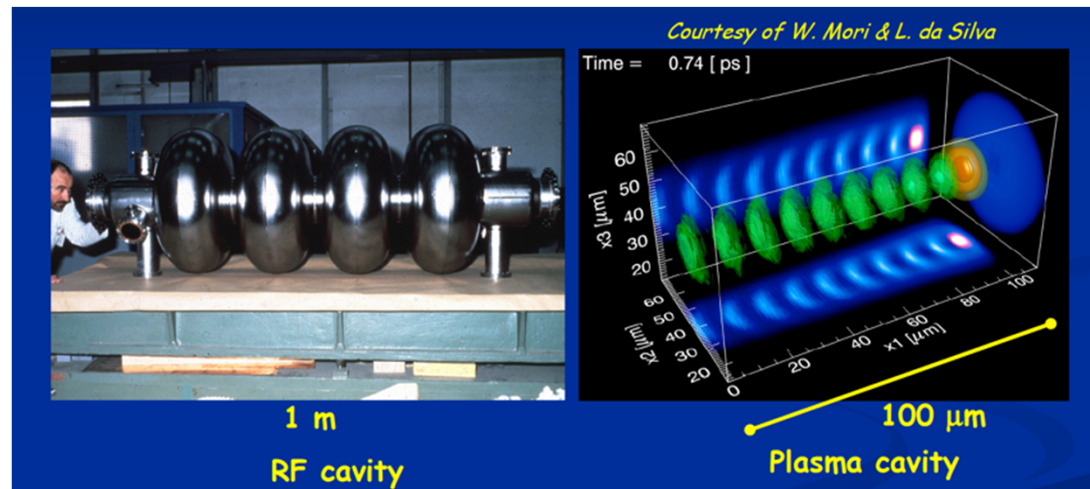


# Plasma accelerators



Laser Wake

Electron beam Wake

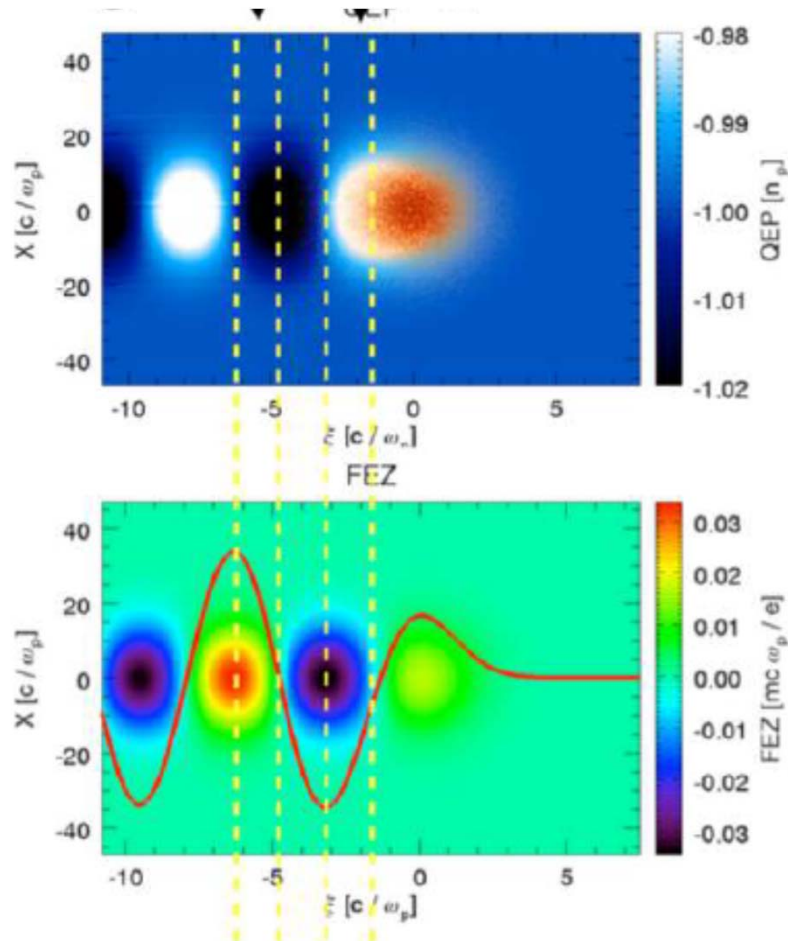


# Plasma accelerators

When the driver is weak, i.e.

$$a_0 = \frac{eE_0\lambda_0}{2\pi mc^2} \ll 1$$

the system works on linear regime.

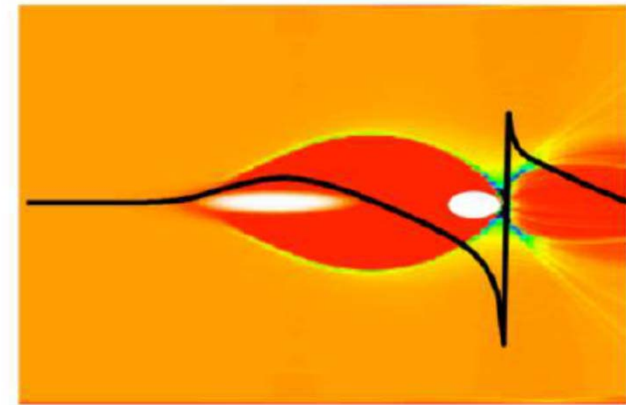


When the driver is strong, i.e.

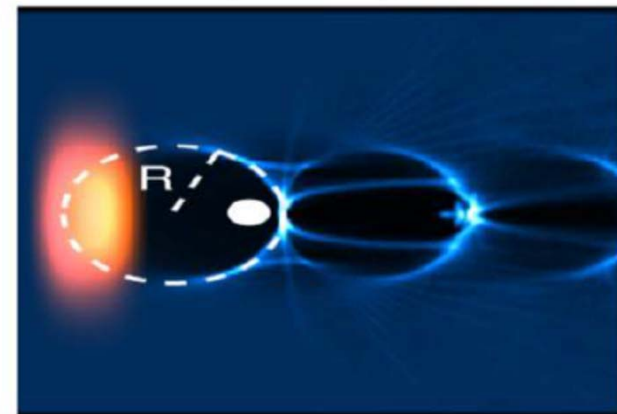
$$a_0 = \frac{eE_0\lambda_0}{2\pi mc^2} \gg 1$$

The system works on nonlinear regime and 'bubble' is created.

*Driven by an electron beam*



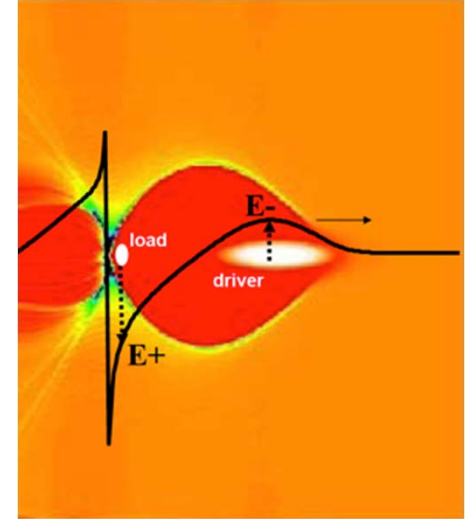
*Driven by a laser pulse*



# Plasma accelerators

Electrons motion is nonrelativistic, linear plasma

$$a_0 = \frac{eE_o \lambda_o}{2\pi mc^2} \gg 1$$



Relativistic motion of electrons, nonlinear plasma, blow-out regime (e.g.

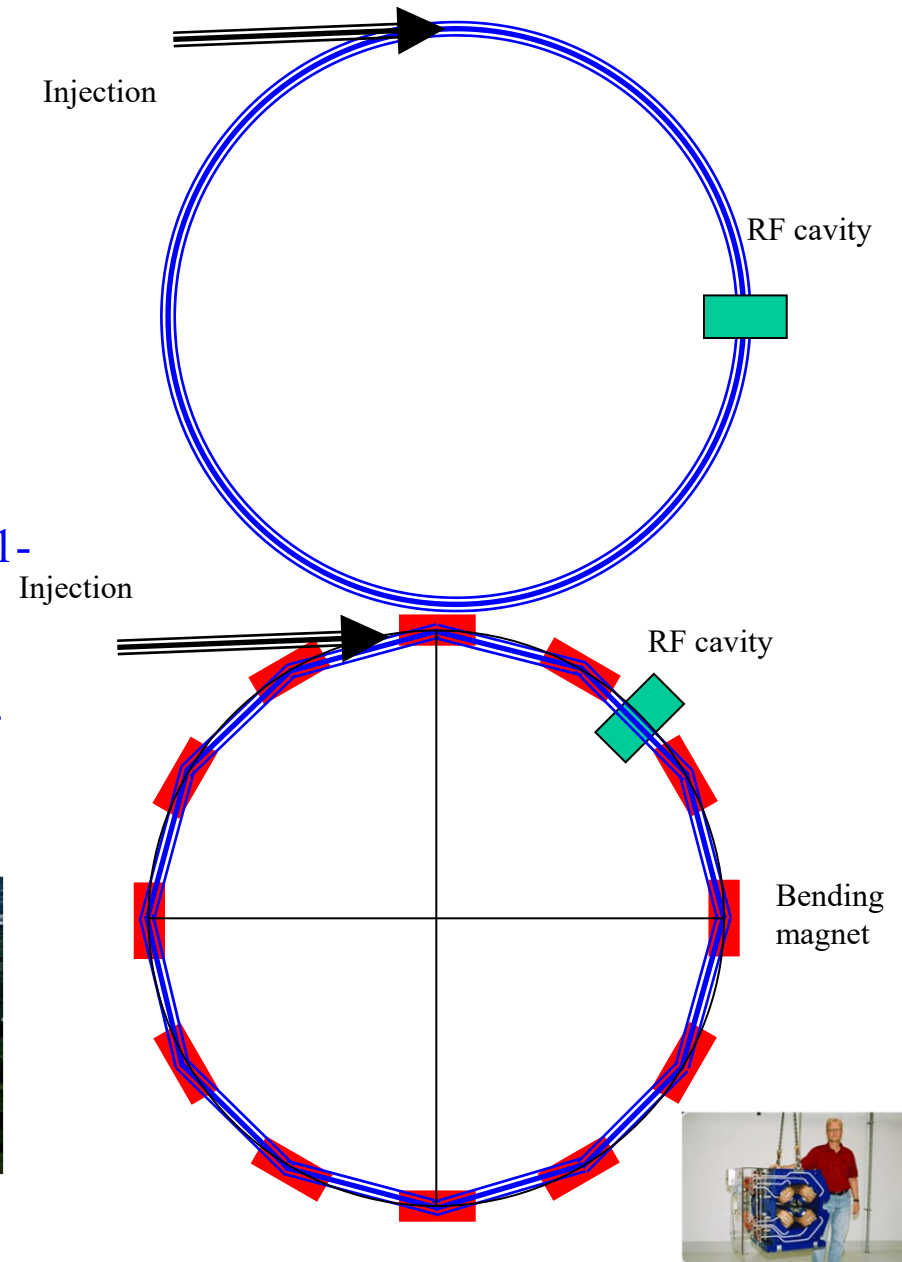
$$l_{buble} \sim \frac{c}{\omega_p}; \quad r_{buble} \sim l_{buble} / 2; \quad E \sim \frac{q}{\pi \epsilon_0 r_{buble}^2} \cong en_o \frac{l_{buble} \pi r_{buble}^2}{\epsilon_0 \pi r_{buble}^2} \cong \frac{ecn_o}{\epsilon_0 \omega_p} = c \sqrt{\frac{mn_o}{\epsilon_0}}$$

$$n_o = 10^{19} \text{ cm}^{-3}; E \approx 300 \text{ GV} / \text{ m}$$

Compare this 300 GeV/m with 150 MeV/m in RF linacs

# Circular accelerators

- Allow to accelerate or store particles to millions and billions of turns
- Largest energies of colliding beams today – **hadrons: 14 TeV p-p, in LHC**, 1 TeV for proton-antiproton ( $10^{12}$  eV) at Tevatron (closed), 24 TeV in Au-Au at RHIC, **1,150 TeV in Pb-Pb collisions in LHC**, **electron-positron: 208 GeV at LEP** (closed)
- Many medium energy electron accelerators (1-8 GeV) as synchrotron radiation sources
- Electrons and positrons radiate too much at high energy ( $\sim E^4$  - you should learn it soon) - hence this is the main limit to their energy



# Why to use magnetic field to guide particles? Why not electric field?

It is practical matter of what you can do easier or what you can do at all?

1 Gs = 29979 V/m -> warm magnet 20 kGs (2T) .eq. to 600 MV/m  
-> superconducting magnets 15T .eq. to 4.5 GV/m

Almost everything arcs at few MV/m

There is no chance to create DC electric field at Earth with the same intensity as DC magnetic field - it has something to do with absence of magnetic charges and, hence, no arcing.....

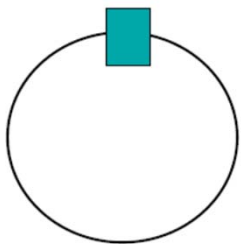
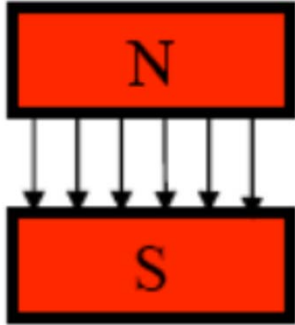
*1997 - BERKELEY, CA -- The world record for field strength in a dipole magnet has been shattered by researchers at the Ernest Orlando Lawrence Berkeley National Laboratory (Berkeley Lab). A one-meter long superconducting electromagnet, featuring coils wound out of 14 miles of niobium-tin wire, reached a field strength as high as 13.5 Tesla, far-surpassing the previous high of 11.03 Tesla set by a Dutch group in 1995.*

# Magnets for stable transverse motion in circular accelerators

Dipoles:  
Used for steering

$$B_x = 0$$

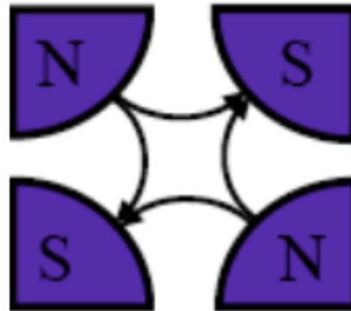
$$B_y = B_0$$



Quadrupoles:  
Used for focusing

$$B_x = Ky$$

$$B_y = Kx$$



Sextupoles:  
Used for chromatic correction

$$B_x = 2Sxy$$

$$B_y = S(x^2 - y^2)$$

