

Collider-Cosmology Interface: EW Phase Transition

M.J. Ramsey-Musolf

U Mass Amherst / TDLI-SJTU



My pronouns: he/him/his



<http://www.physics.umass.edu/acfi/>



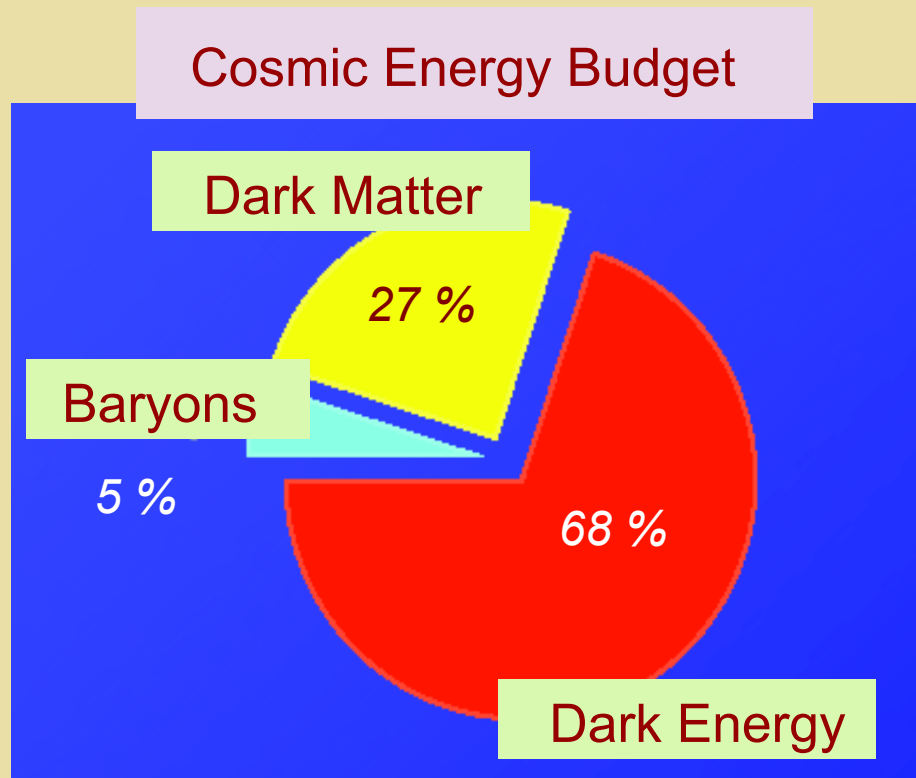
<http://tdli.sjtu.edu.cn/web/yjxy/5130001.htm>

US ATLAS Workshop
UMass Amherst, August 6, 2019

Ann E. Nelson

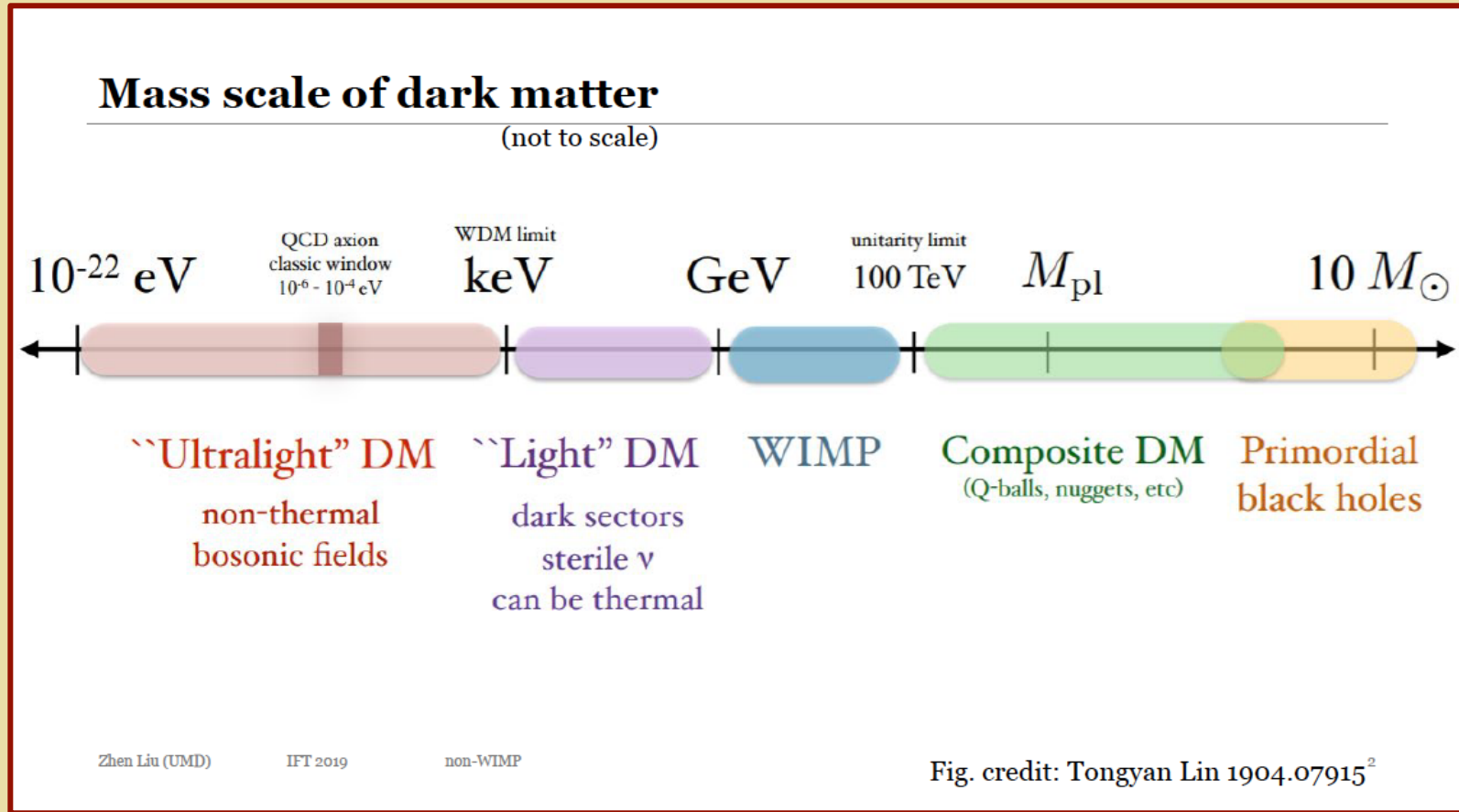


The Origin of Matter



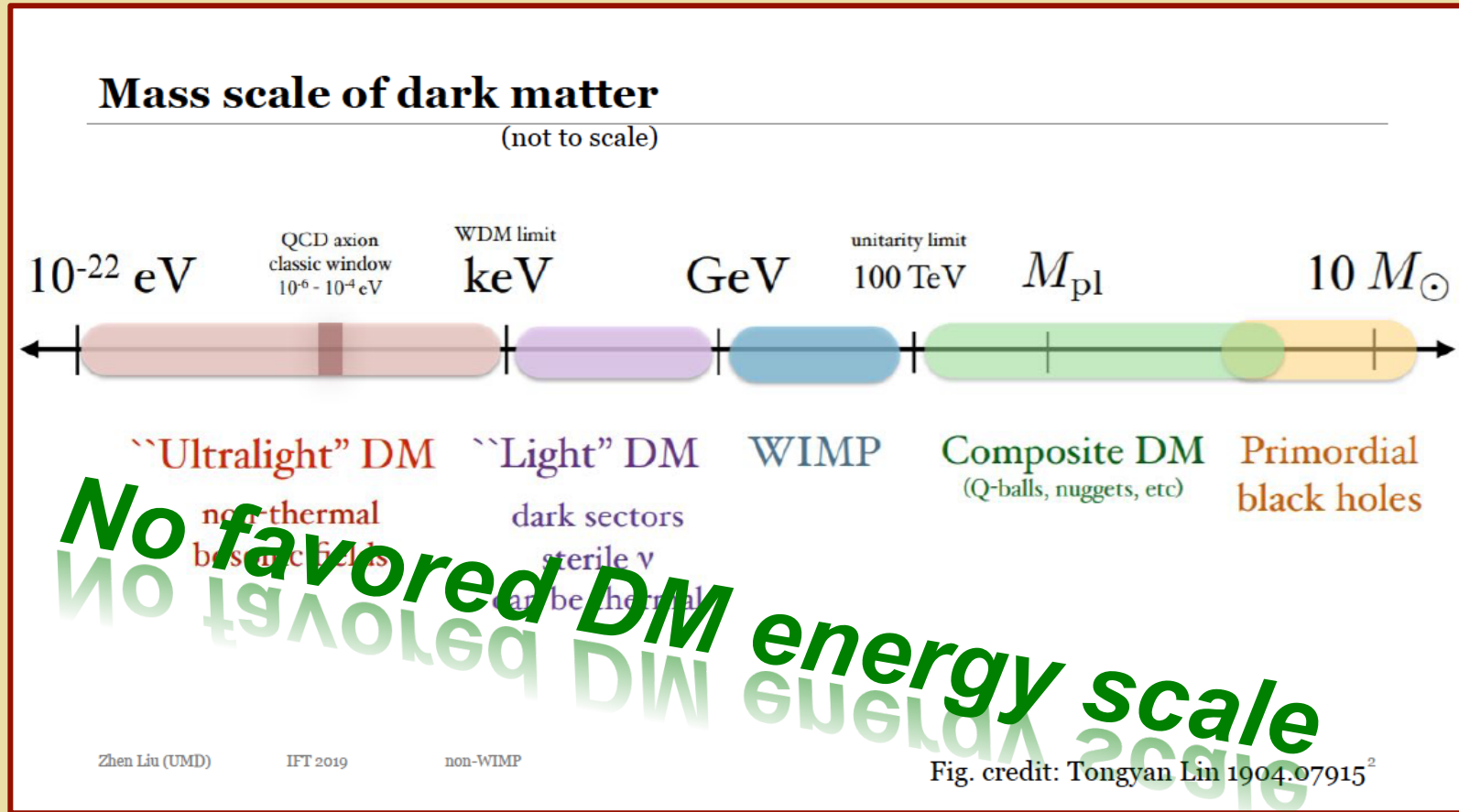
What can the LHC & future colliders teach us about open questions in cosmology ?

Dark Matter



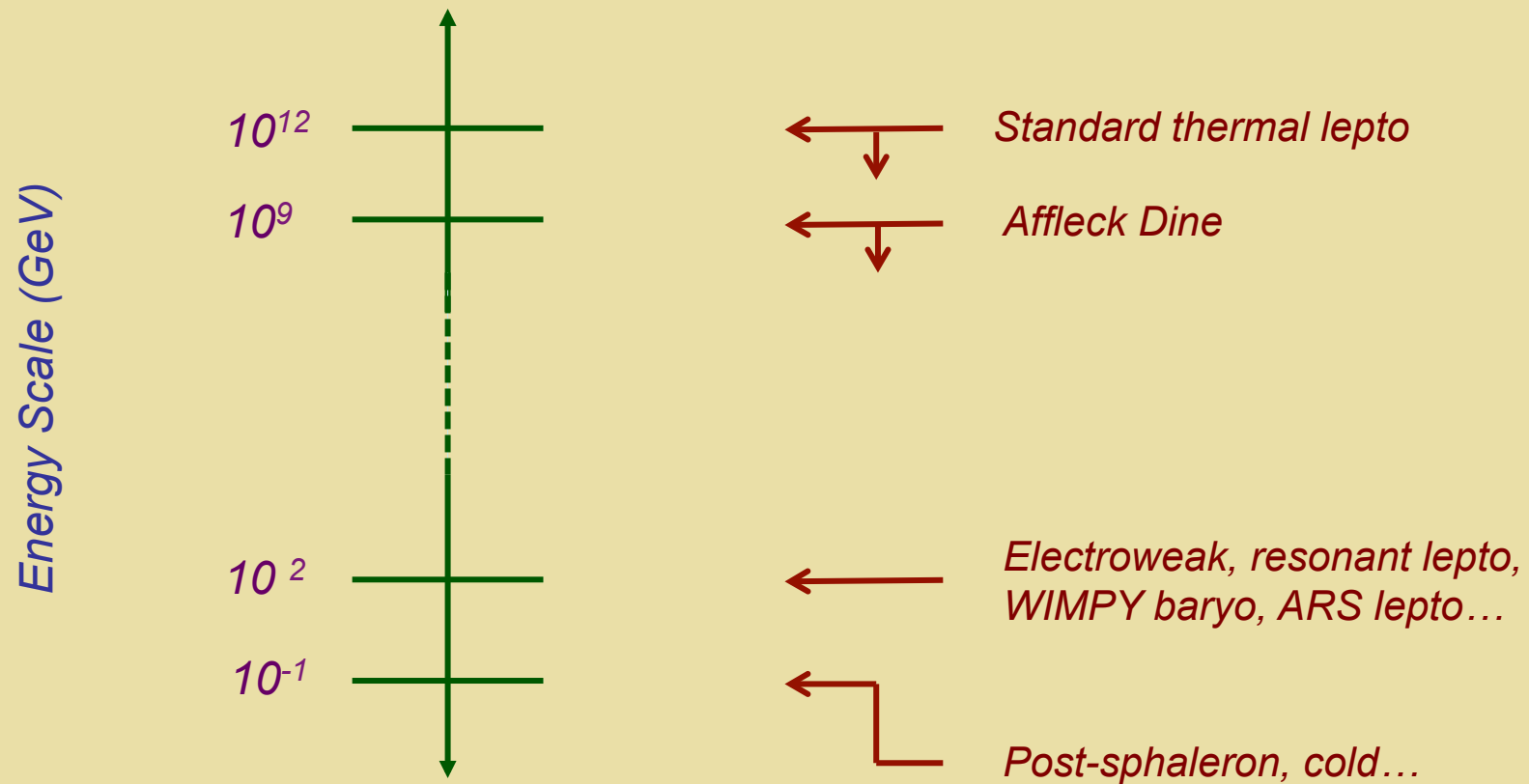
Thanks: Z. Liu

Dark Matter

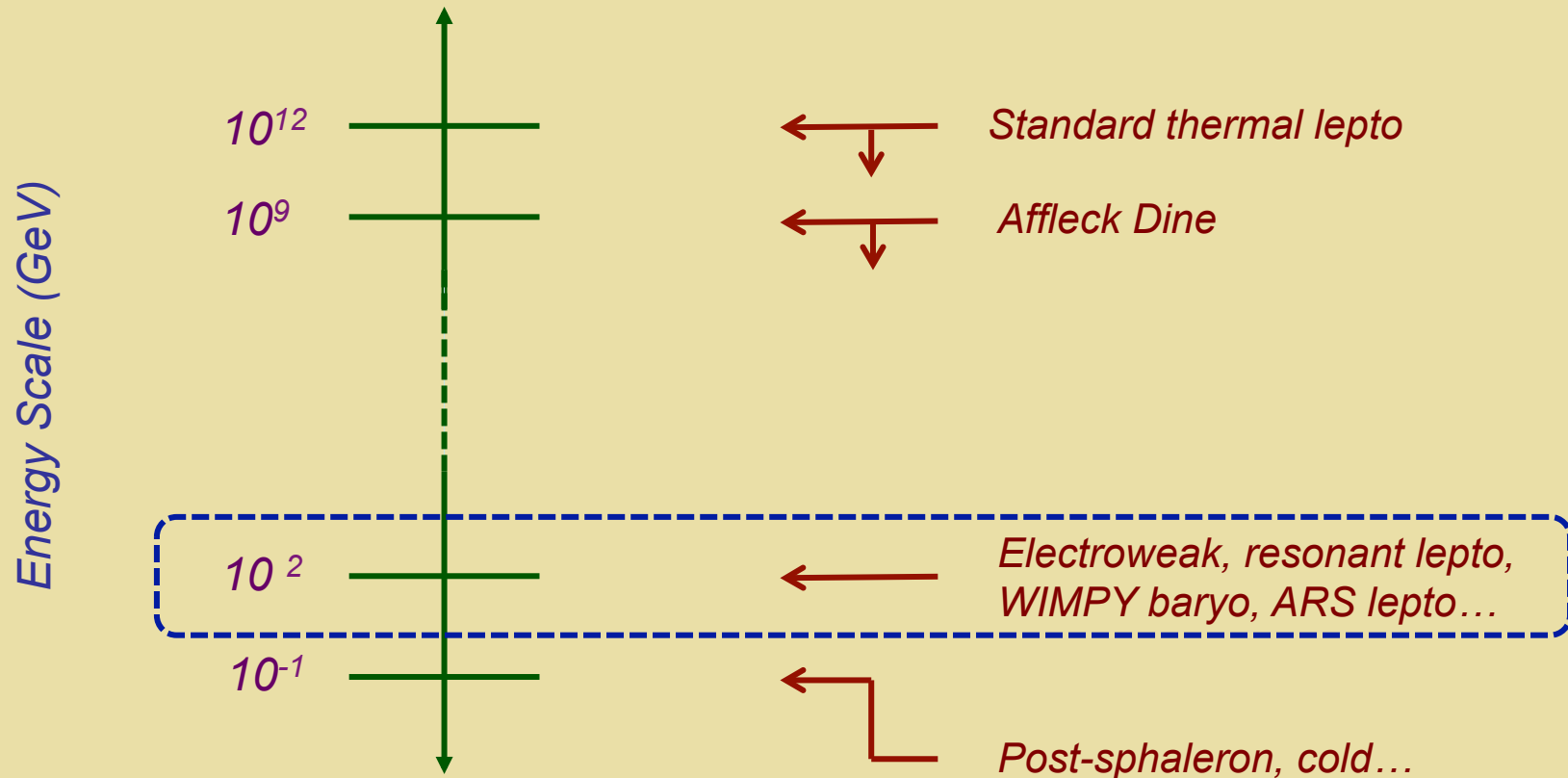


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Baryogenesis Scenarios

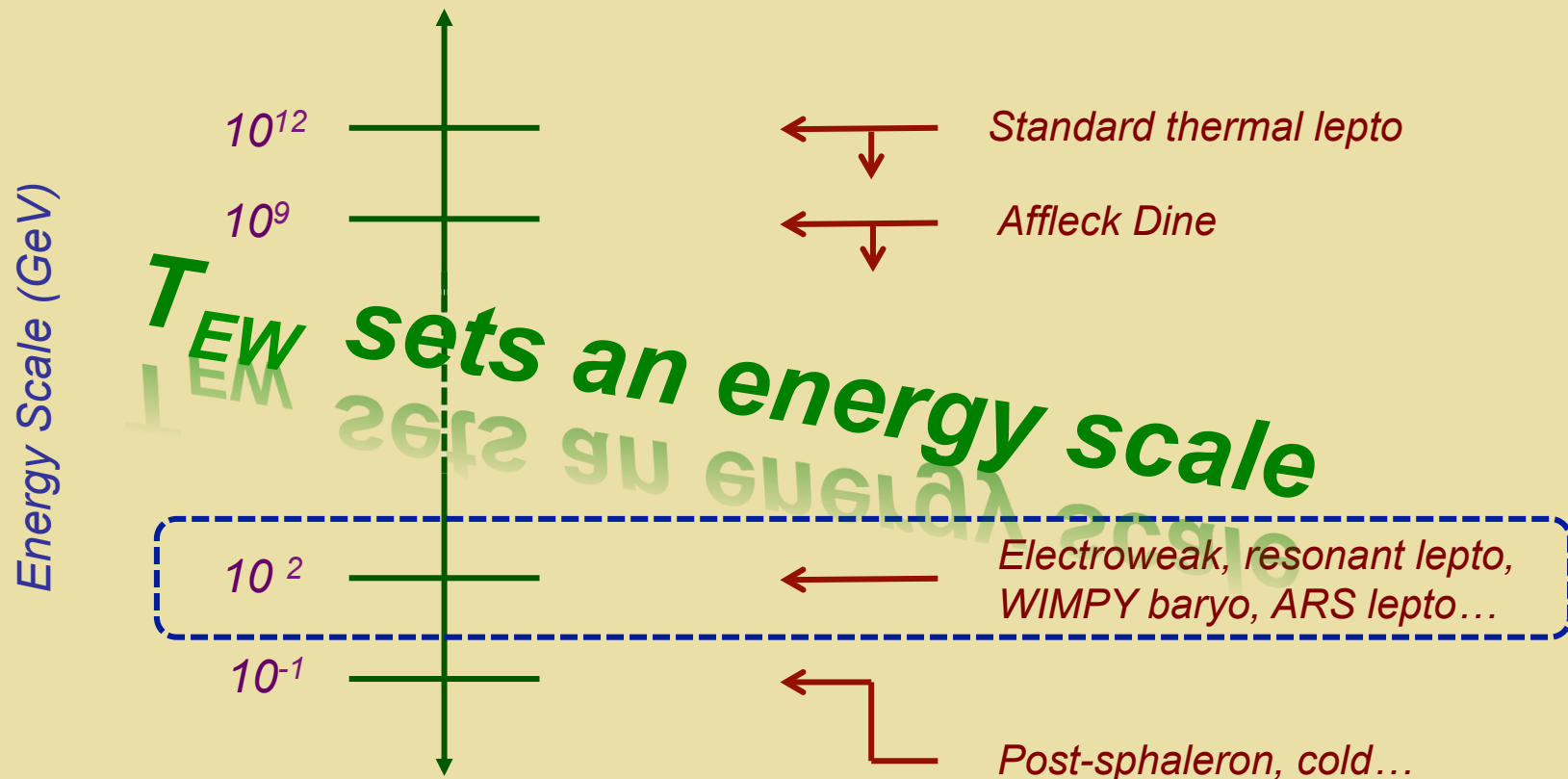


Baryogenesis Scenarios



Era of EWSB: $t_{univ} \sim 10$ ps

Baryogenesis Scenarios



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Main Theme for This Talk

$T_{EW} \rightarrow$ EW phase transition is a target for the LHC & beyond

Outline

- I. Context & Questions*
- II. EWPT: A Collider Target*
- III. Models & Phenomenology*
- IV. Outlook*

I. Context & Questions

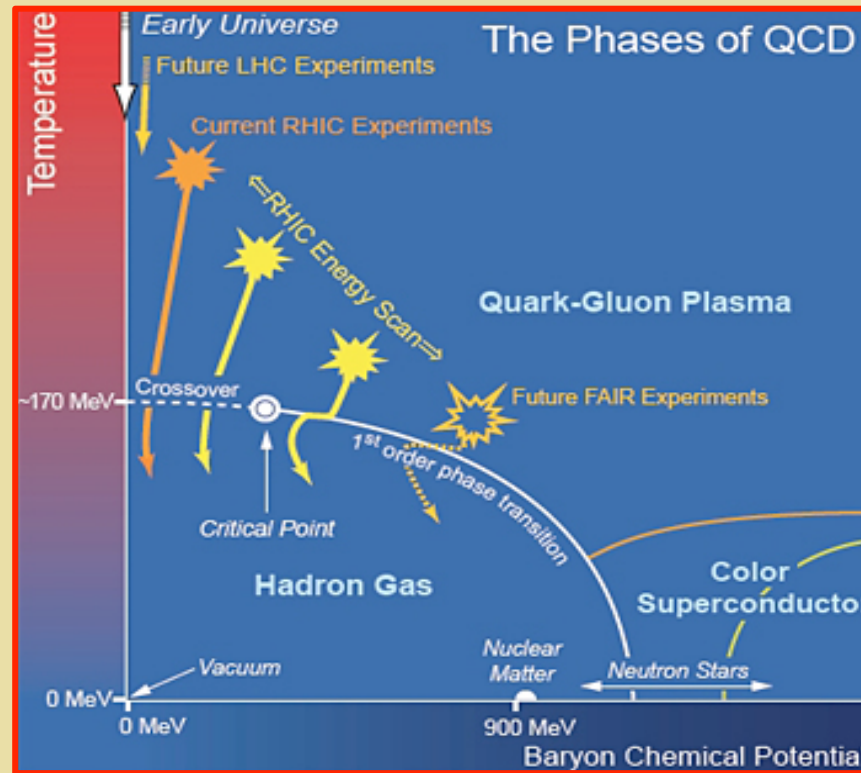
Electroweak Phase Transition

- *Higgs discovery → What was the thermal history of EWSB ?*
- *Baryogenesis → Was the matter-antimatter asymmetry generated in conjunction with EWSB (EW baryogenesis) ?*
- *Gravitational waves → If a signal observed in LISA, could a cosmological phase transition be responsible ?*

Electroweak Phase Transition

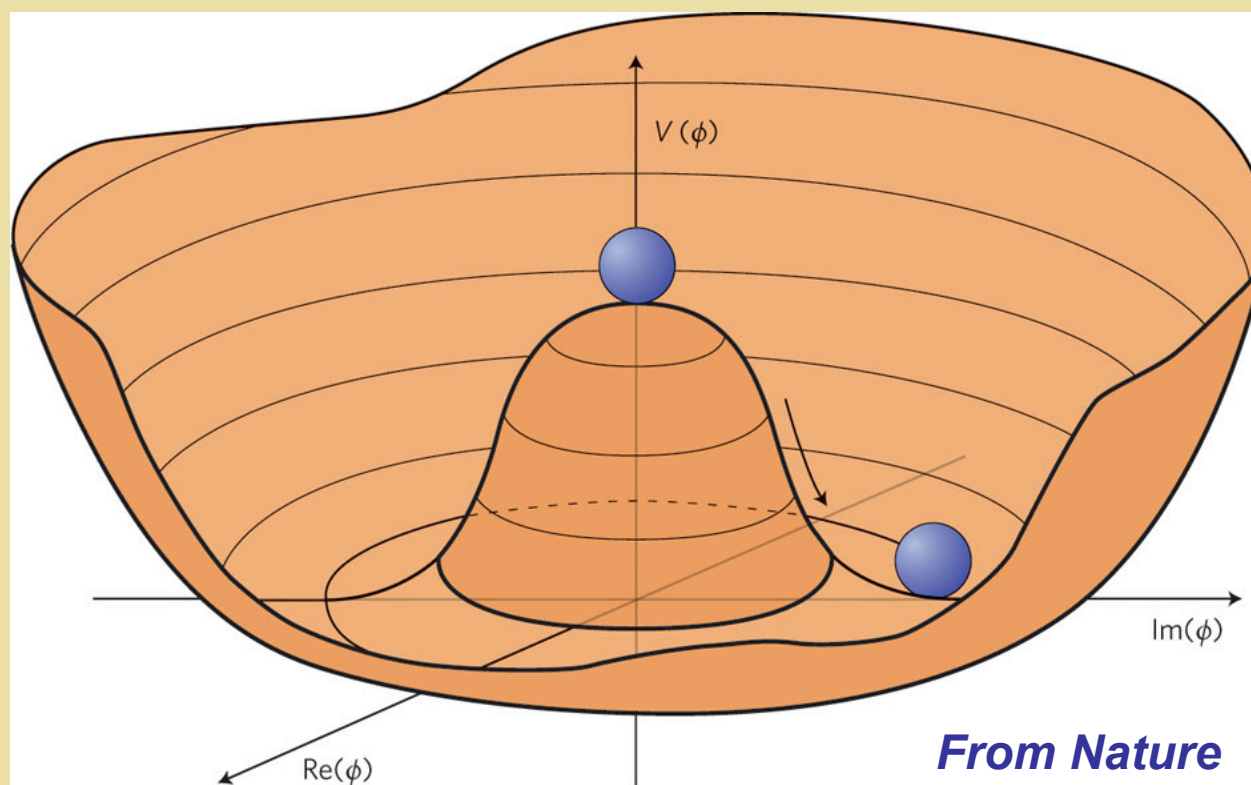
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Thermal History of Symmetry Breaking



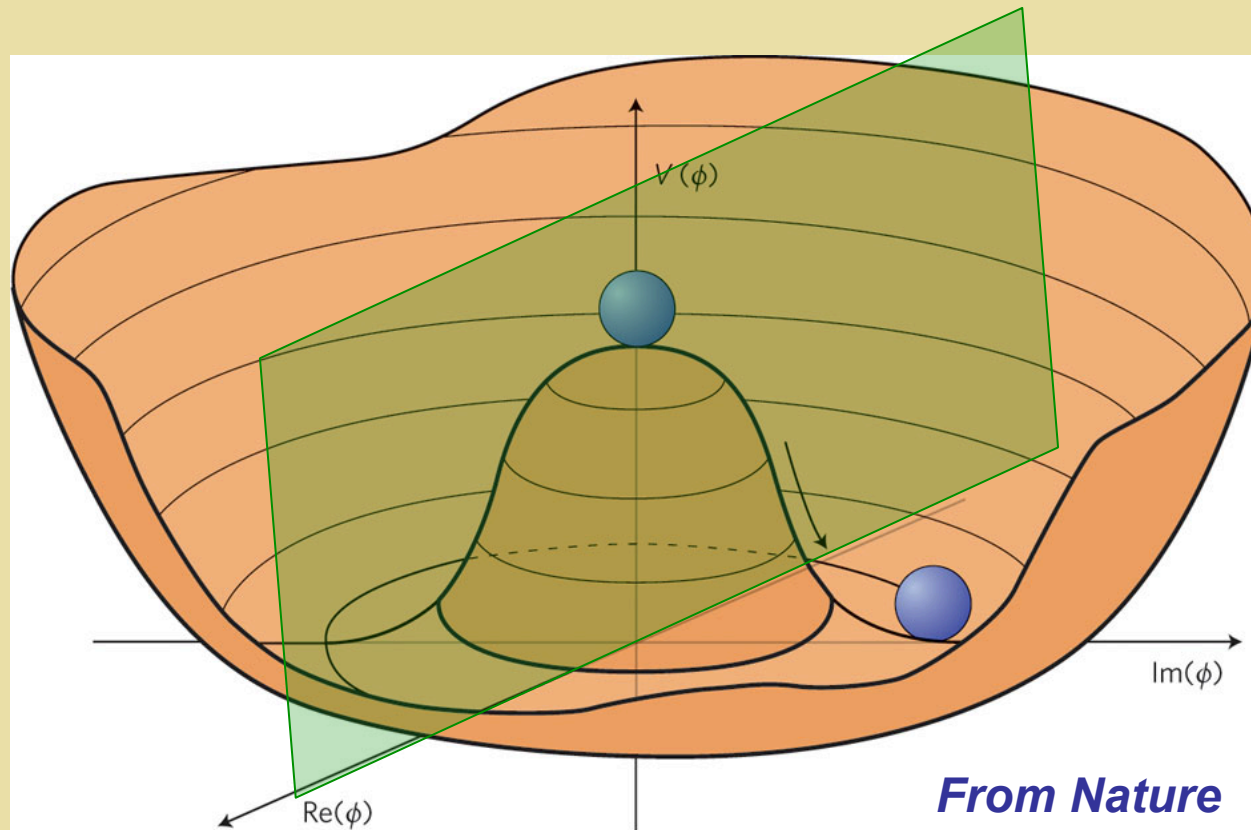
QCD Phase Diagram → EW Theory Analog?

EWSB: The Scalar Potential



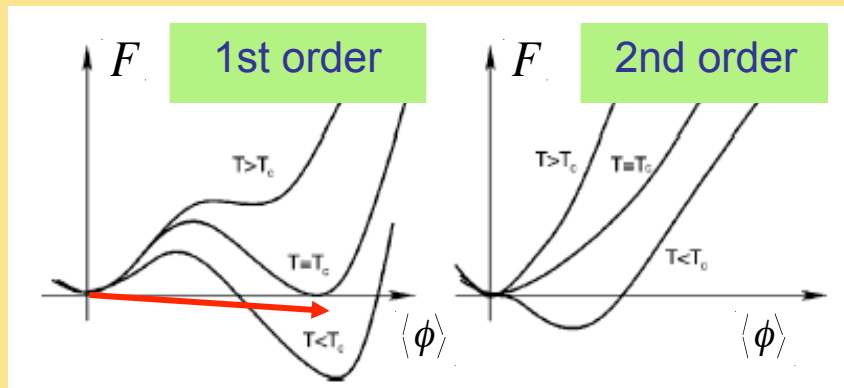
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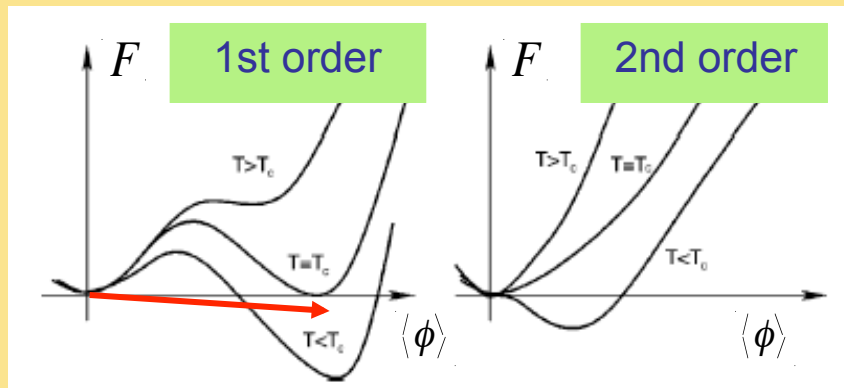
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EW Phase Transition: St'd Model



Increasing m_h \longrightarrow

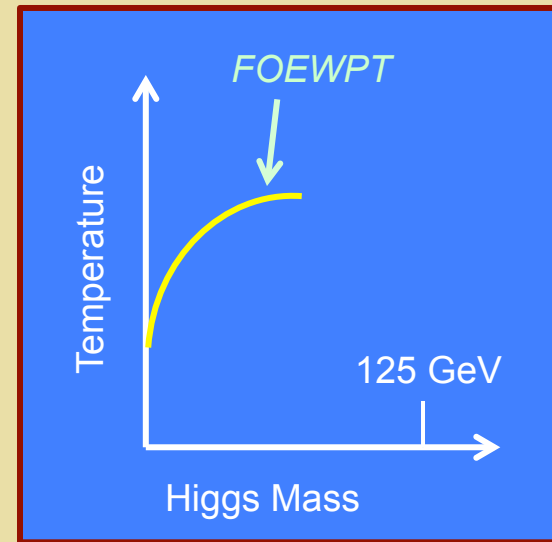
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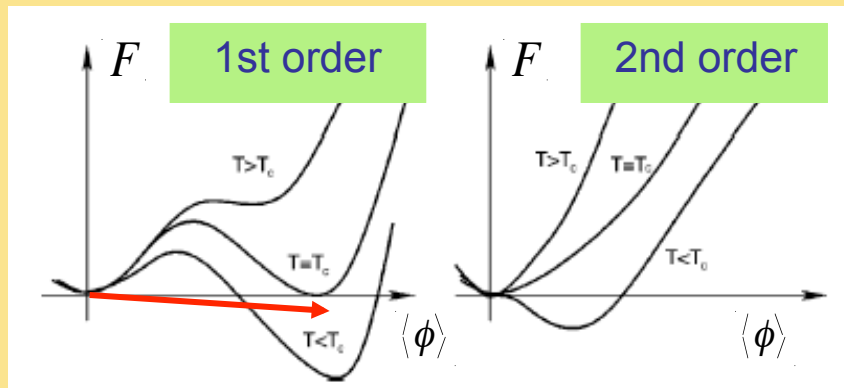
Lattice	Authors	M_h^C (GeV)
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SM EW: Cross over transition



EW Phase Diagram

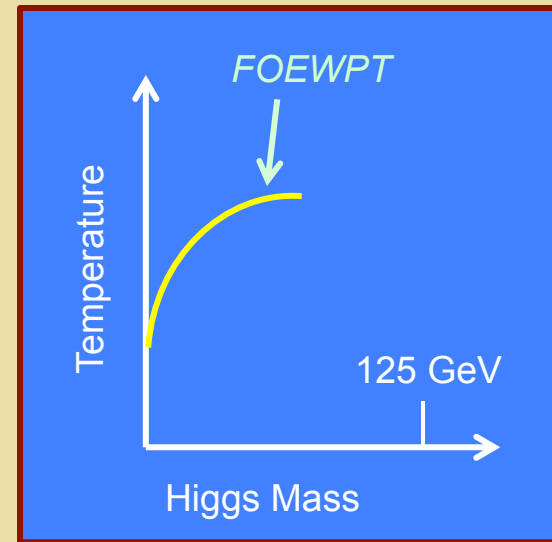
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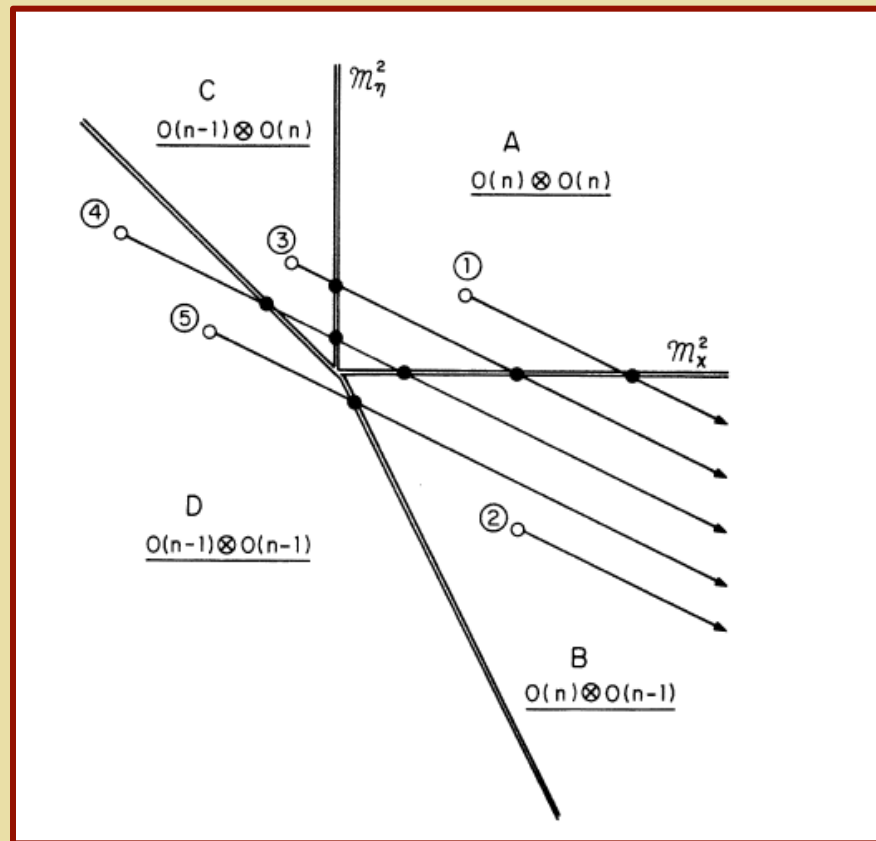
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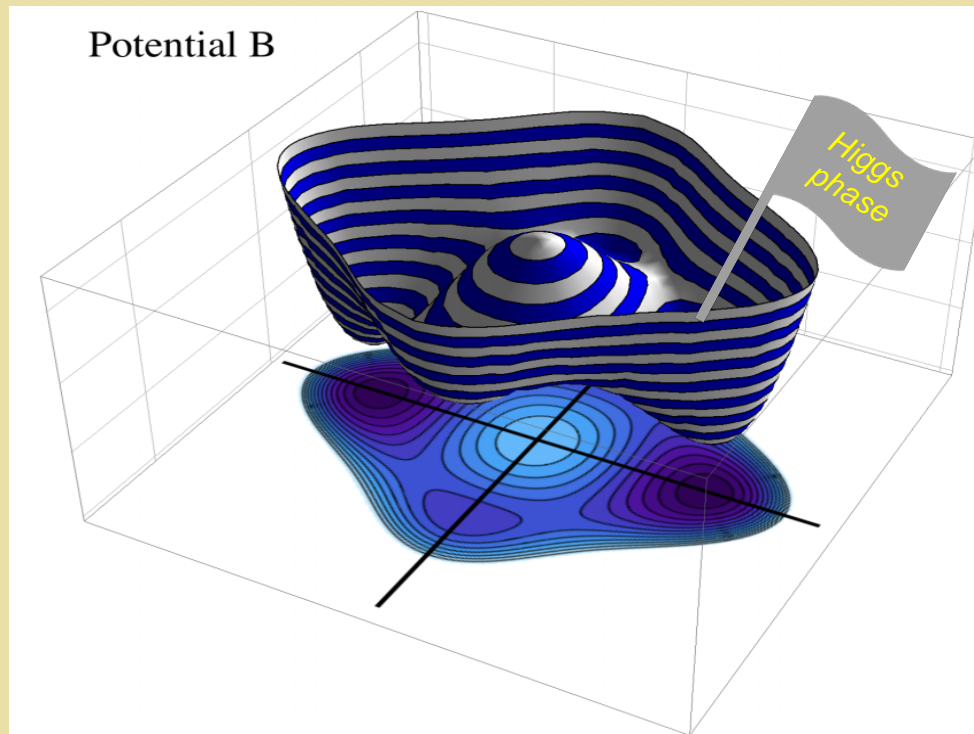
How does this picture change in presence of new TeV scale physics? What is the phase diagram? SFOEWPT?

Patterns of Symmetry Breaking



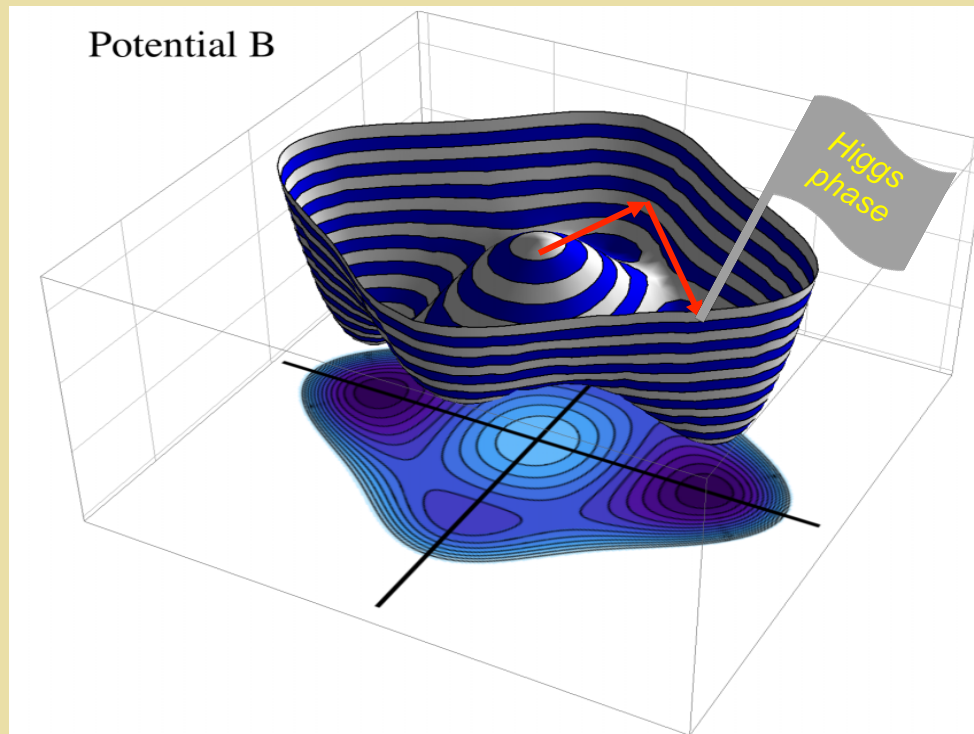
S. Weinberg, PRD 9 (1974) 3357

Patterns of Symmetry Breaking



*Extrema can evolve differently as T evolves →
rich possibilities for symmetry breaking*

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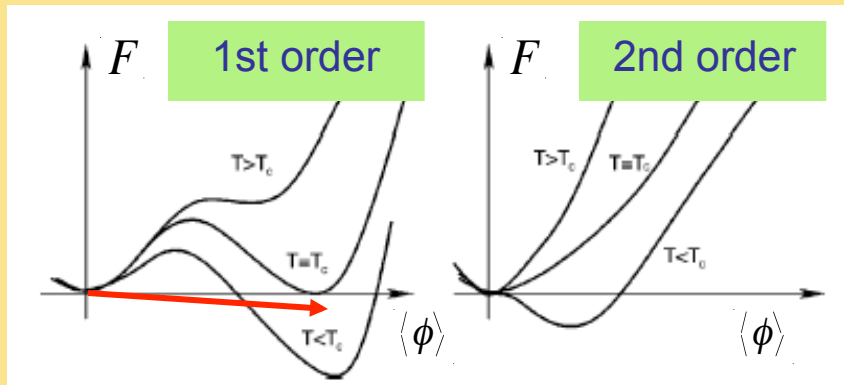


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EW Phase Transition: Baryogen & GW



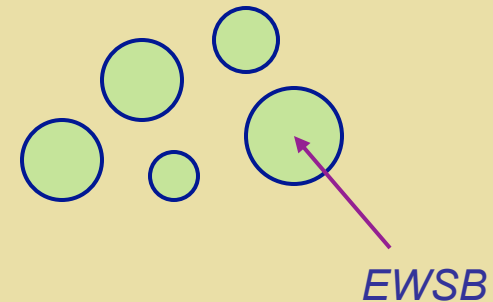
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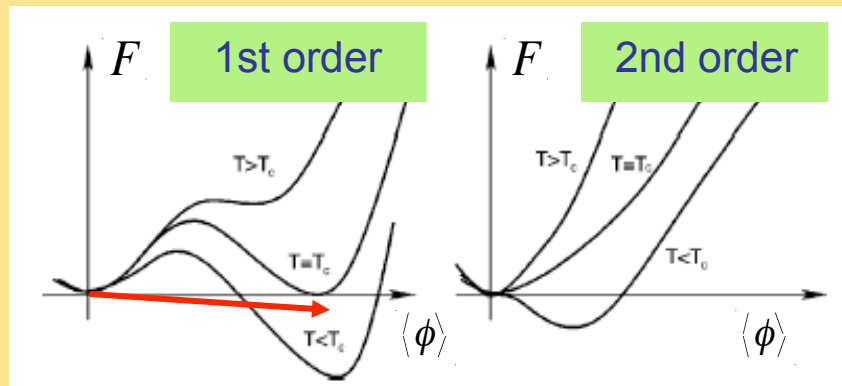
Baryogenesis
Gravity Waves
Scalar DM
LHC Searches

“Strong” 1st order EWPT

Bubble nucleation



EW Phase Transition: Baryogen & GW



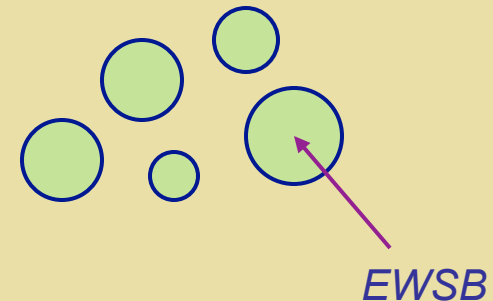
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Baryogenesis
Gravity Waves
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“Strong” 1st order EWPT

- Baryogen*
 - GW
- Bubble nucleation



* Need BSM CPV

II. EWPT: A Collider Target

MJRM 1908.NNNNN

T_{EW} Sets a Scale for Colliders

High- T SM Effective Potential

$$V(h, T)_{\text{SM}} = D(T^2 - T_0^2) h^2 + \lambda h^4 + \dots$$

$$T_0^2 = (8\lambda + \text{loops}) \left(\frac{3}{2} g^2 + g'^2 + 2y_t^2 + \dots \right)^{-1} v^2$$

$$T_0 \sim 140 \text{ GeV}$$

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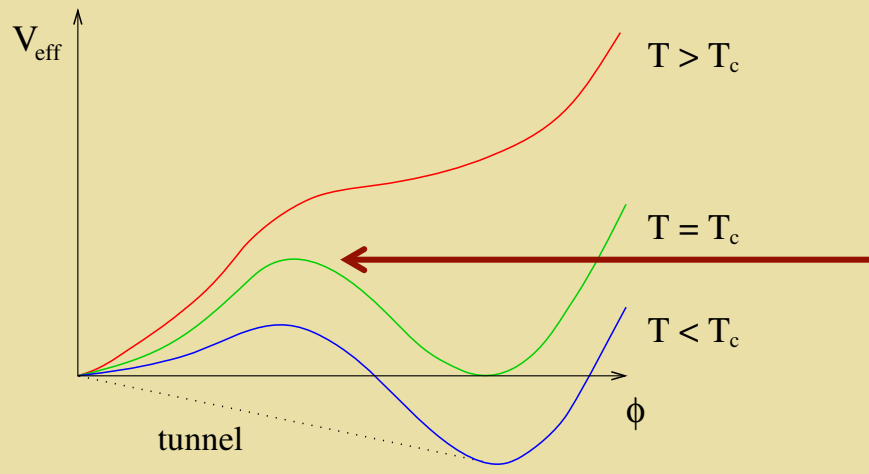
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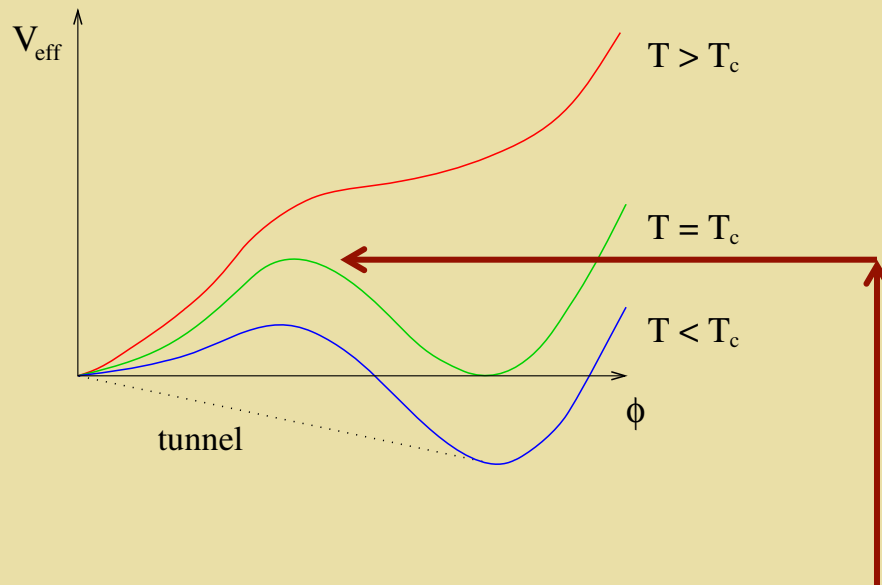
$$\equiv T_{EW}$$

First Order EWPT from BSM Physics



Generate finite-T barrier

First Order EWPT from BSM Physics



Generate finite-T barrier

$$V(H, \phi)_{T=0} = V(H) + \frac{a_2}{2} \phi^\dagger \phi H^\dagger H + V(\phi)$$

$$V(H) = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2$$

$$V(\phi) = \frac{b_2}{2} \phi^\dagger \phi + \frac{b_4}{4!} (\phi^\dagger \phi)^2$$

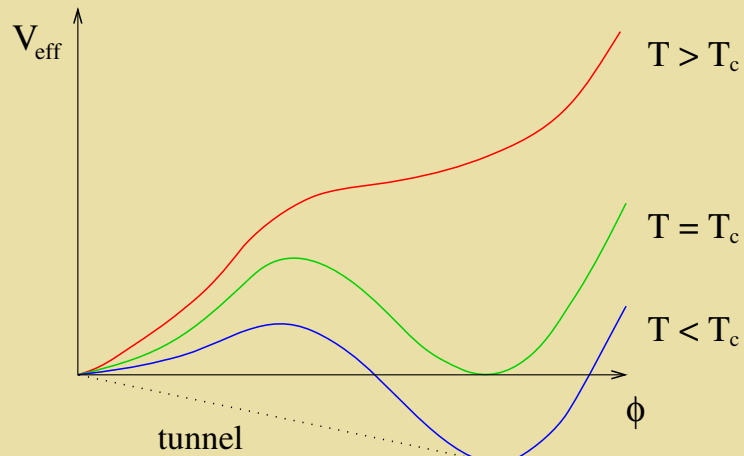
First Order EWPT from BSM Physics

- ***Thermal loops involving new bosons***
- ***T=0 loops (CW Potential)***
- ***Change tree-level vacuum structure***

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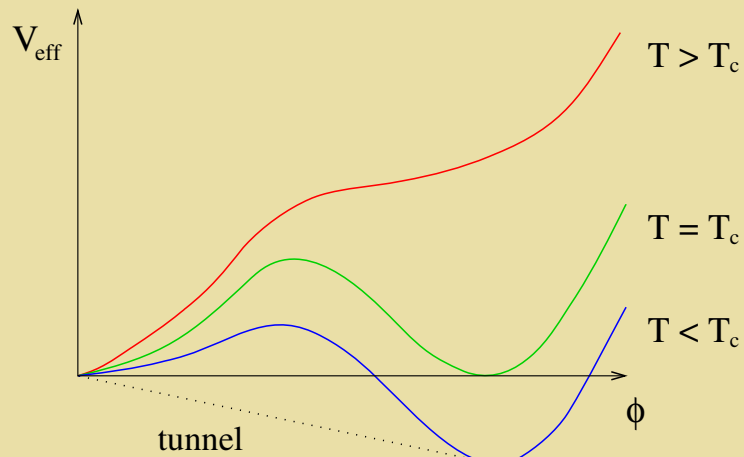
First Order EWPT from BSM Physics



$$\Delta V(h, T) \supset -\frac{T}{12\pi} M_\phi(h, T)^3$$

$$M_\phi(h, T)^3 = \left[\frac{a_2}{12} T^2 + b_2 + \frac{a_2}{4} h^2 \right]^{3/2}$$

First Order EWPT from BSM Physics

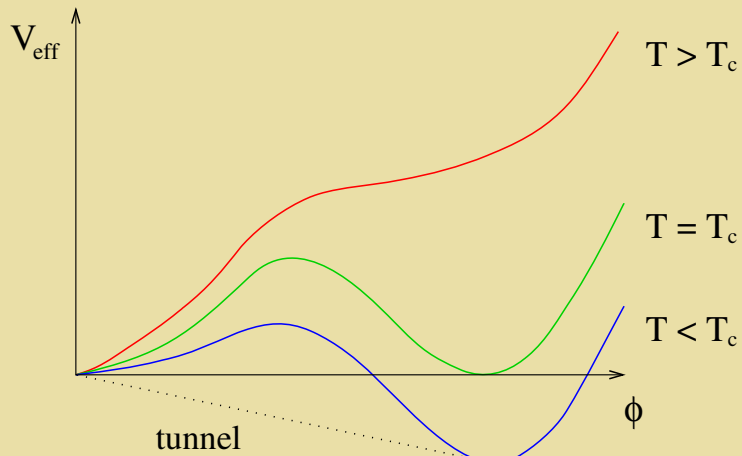


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Choose b_2, a_2 to cancel at $T \sim T_{EW}$

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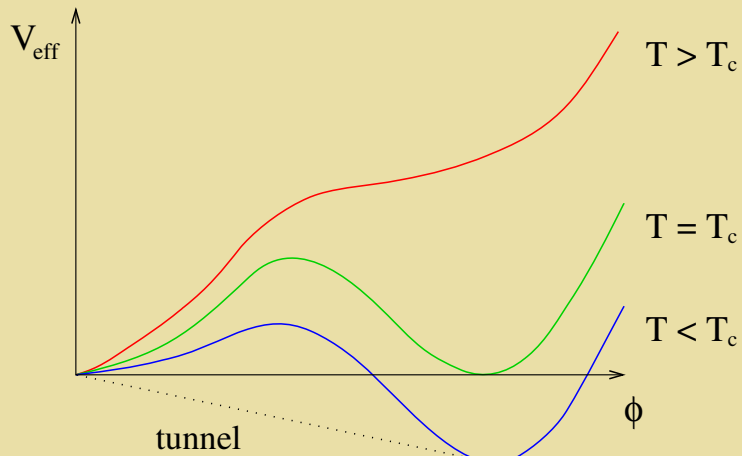
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$$\Delta V(h, T_{EW}) \supset -\frac{T_{EW}}{12\pi} \frac{a_2^{3/2}}{8} h^3$$

Choose b_2, a_2 to cancel at $T \sim T_{EW}$

$$M_\phi(T = 0) = \frac{a_2}{4} (v^2 - T_{EW}^2/3)$$

First Order EWPT from BSM Physics



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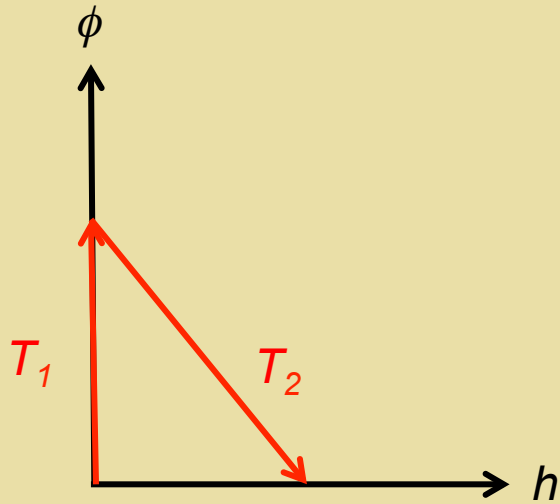
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**$M_\phi < 350$ GeV for
perturbative a_2**

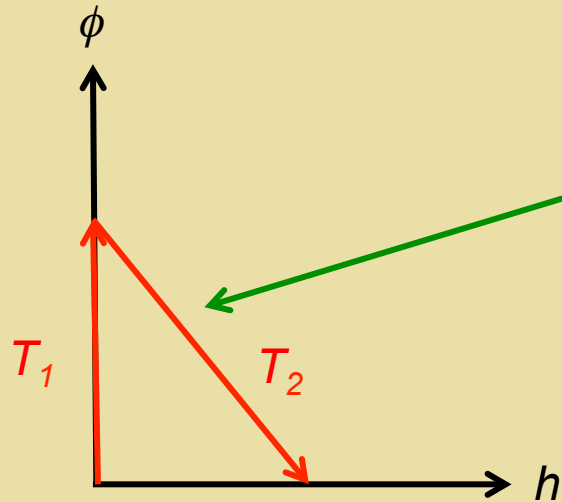
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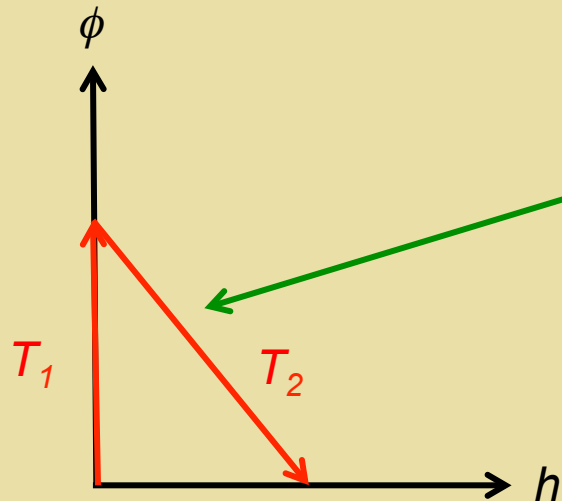


First Order EWPT from BSM Physics



- Tree-level barrier: $a_2 \phi^+ \phi H^+ H$
- Want $T_1 > T_2 \sim T_{EW}$

First Order EWPT from BSM Physics



- Tree-level barrier: $a_2 \phi^+ \phi H^+ H$
- Want $T_1 > T_2 \sim T_{EW}$

$$M_\phi(T=0) < \left[\frac{a_2}{4} v^2 - \frac{T_{EW}^2}{6} \left(a_2 + \frac{3}{2} b_4 \right) \right]^{1/2}$$

$M_\phi < 350 \text{ GeV}$ for
perturbative a_2, b_4

T_{EW} : A Scale for Collider Discovery

- *Foregoing arguments: good up to factor of $\sim 2 \rightarrow M_\phi < 800$ GeV (-ish)*
- *QCD production: LHC exclusion $\rightarrow \phi$ is colorless*
- *Electroweak or Higgs portal (h - ϕ mixing...) production $\rightarrow \sigma_{PROD} \sim (1-500)$ fb (LHC) and $(0.1-25)$ pb (100 TeV pp)*
- *Precision Higgs studies: see ahead*

III. Models & Phenomenology

Models & Phenomenology

What BSM Scenarios?

SM + Scalar Singlet

Espinosa, Quiros 93, Benson 93, Choi, Volkas 93, Vergara 96, Branco, Delepine, Emmanuel-Costa, Gonzalez 98, Ham, Jeong, Oh 04, Ahriche 07, Espinosa, Quiros 07, Profumo, Ramsey-Musolf, Shaughnessy 07, Noble, Perelstein 07, Espinosa, Konstandin, No, Quiros 08, Barger, Langacker, McCaskey, Ramsey-Musolf, Shaughnessy 09, Ashoorioon, Konstandin 09, Das, Fox, Kumar, Weiner 09, Espinosa, Konstandin, Riva 11, Chung, Long 11, Barger, Chung, Long, Wang 12, Huang, Shu, Zhang 12, Fairbairn, Hogan 13, Katz, Perelstein 14, Profumo, Ramsey-Musolf, Wainwright, Winslow 14, Jiang, Bian, Huang, Shu 15, Kozaczuk 15, Cline, Kainulainen, Tucker-Smith 17, Kurup, Perelstein 17, Chen, Kozaczuk, Lewis 17, Gould, Kozaczuk, Niemi, Ramsey-Musolf, Tenkanen, Weir 19...

SM + Scalar Doublet
(2HDM)

Turok, Zadrozny 92, Davies, Froggatt, Jenkins, Moorhouse 94, Cline, Lemieux 97, Huber 06, Froome, Huber, Seniuch 06, Cline, Kainulainen, Trott 11, Dorsch, Huber, No 13, Dorsch, Huber, Mimasu, No 14, Basler, Krause, Muhlleitner, Wittbrodt, Wlotzka 16, Dorsch, Huber, Mimasu, No 17, Bernon, Bian, Jiang 17, Andersen, Gorda, Helset, Niemi, Tenkanen, Tranberg, Vuorinen, Weir 18...

SM + Scalar Triplet

Patel, Ramsey-Musolf 12, Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir 18 ...

MSSM

Carena, Quiros, Wagner 96, Delepine, Gerard, Gonzalez Felipe, Weyers 96, Cline, Kainulainen 96, Laine, Rummukainen 98, Carena, Nardini, Quiros, Wagner 09, Cohen, Morrissey, Pierce 12, Curtin, Jaiswal, Meade 12, Carena, Nardini, Quiros, Wagner 13, Katz, Perelstein, Ramsey-Musolf, Winslow 14...

NMSSM...

Pietroni 93, Davies, Froggatt, Moorhouse 95, Huber, Schmidt 01, Ham, Oh, Kim, Yoo, Son 04, Menon, Morrissey, Wagner 04, Funakubo, Tao, Yokoda 05, Huber, Konstandin, Prokopec, Schmidt 07, Chung, Long 10, Kozaczuk, Profumo, Stephenson Haskins, Wainwright 15...

EWPT: Theory & Phenomenology

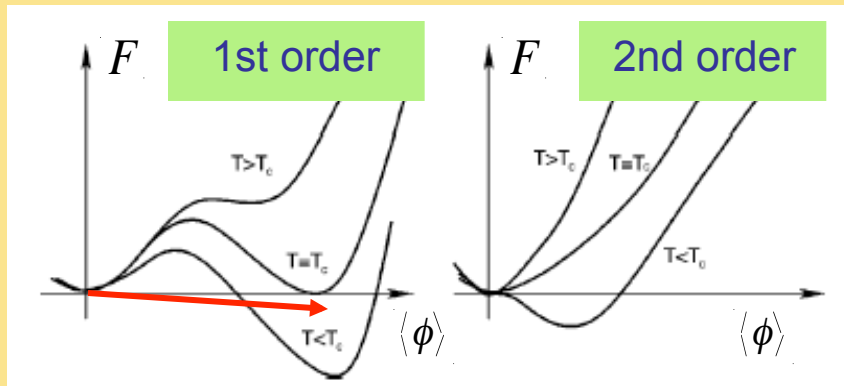
- *What models can lead to a (strong) first order electroweak phase transition (EW baryogenesis & gravitational waves) ?*
- *Can they also yield contributions to Ω_{DM} ?*
- *How can they be tested experimentally ?*
- *How reliably can we compute phase transition properties & make the connection with phenomenology ?*

EWPT “Poster Child”: MSSM Light Stop Scenario



Thermal loops

EW Phase Transition: SUSY



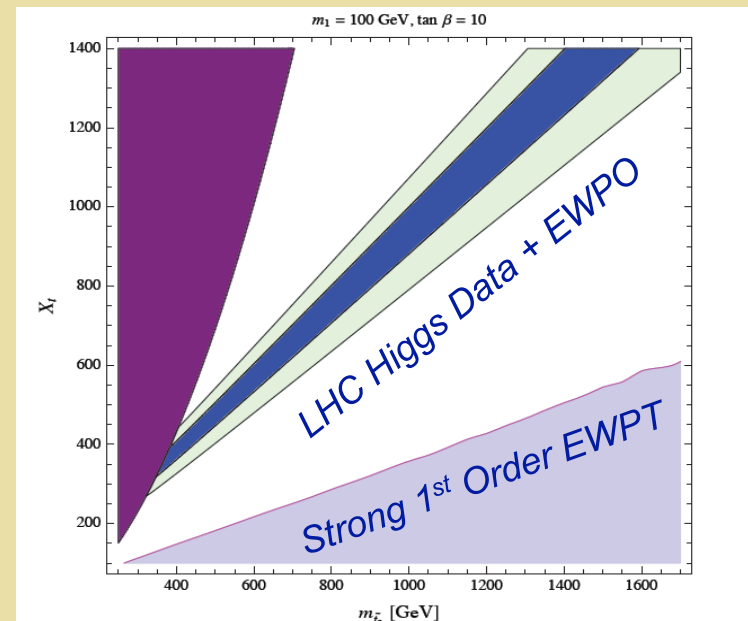
Increasing m_h \longrightarrow

\longleftarrow New scalars

Light RH stops also affect Higgs properties

Curtin, Jaiswal, Meade 1203.2932

$$MSSM + \delta\lambda_4 (H_u^\dagger H_u)^2$$



Katz, Perelstein, R-M,
Winslow 1509.02934

Strong 1st Order EWPT



**Definitive probe of the possibilities →
LHC + next generation colliders**

The Higgs Portal



Higgs Portal: Simple Scalar Extensions

<i>Extension</i>	<i>DOF</i>	<i>EWPT</i>	<i>DM</i>
<i>Real singlet: Z₂</i>	1	✓	✗
<i>Real singlet: Z₂</i>	1	✓	✓
<i>Complex Singlet</i>	2	✓	✓
<i>EW Multiplets</i>	3+	✓	✓

May be low-energy remnants of UV complete theory & illustrative of generic features

Higgs Portal: Simple Scalar Extensions



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Higgs Portal: Simple Scalar Extensions

	<i>Extension</i>	<i>DOF</i>	<i>EWPT</i>	<i>DM</i>
<i>This talk</i>	Real singlet: Z_2	1	✓	✗
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May be low-energy remnants of UV complete theory & illustrative of generic features

Simplest Extension

Standard Model + real singlet scalar

Singlet
Driven EW Phase Transition

(lots of) Motivation

- ⇒ Neutral Naturalness
- ⇒ Higgs Portal (Dark Sectors)
- ⇒ Non-minimal SUSY (e.g. NMSSM)
- ⇒ Warped Extra Dim (dilaton...)
- ...

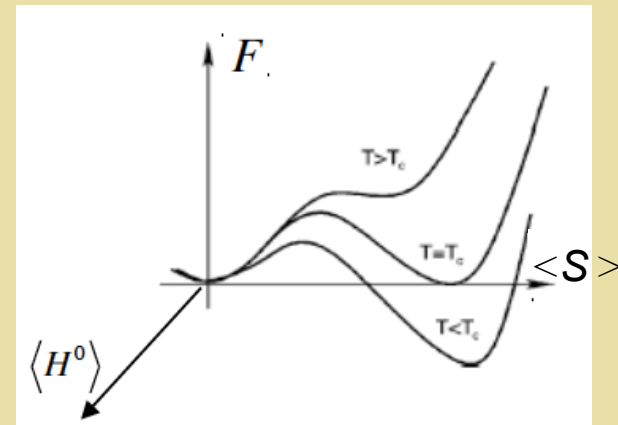
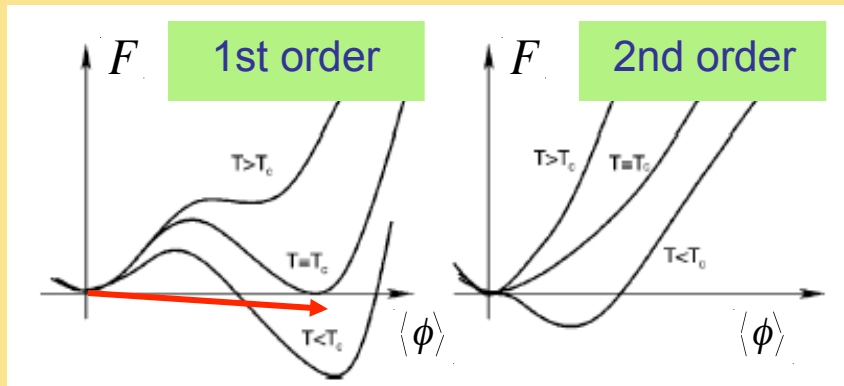
Simplest Extension

Standard Model + real singlet scalar

$$V_{\text{HS}} = \frac{a_1}{2} (H^\dagger H) S + \frac{a_2}{2} (H^\dagger H) S^2$$

- *Strong first order EWPT*
- *Two mixed singlet-doublet states*

EW Phase Transition: New Scalars

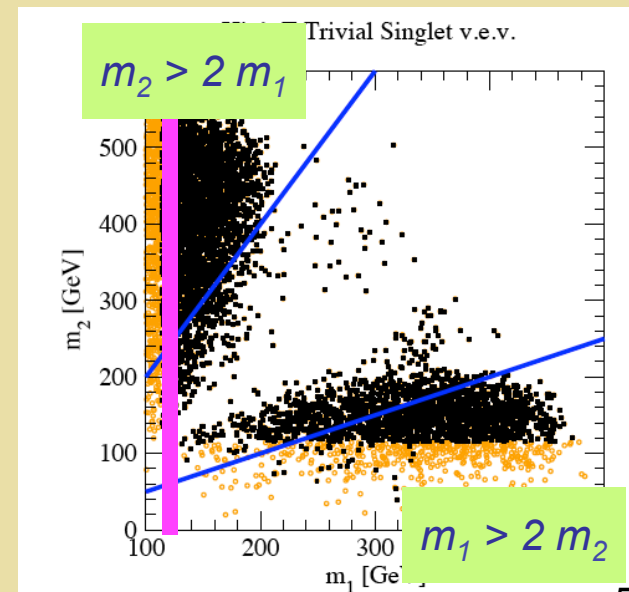


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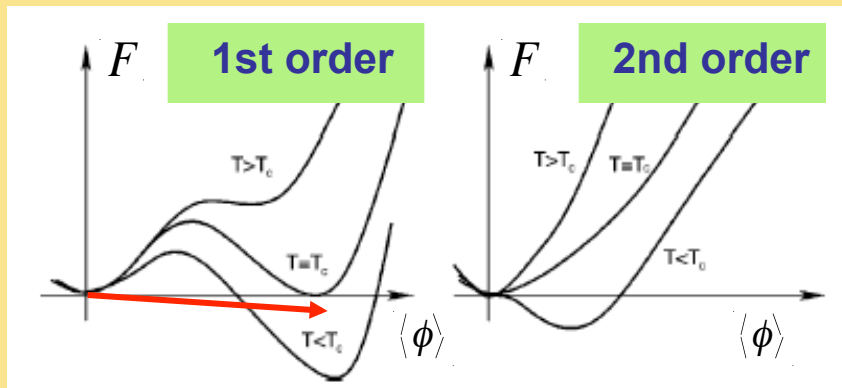
\longleftarrow New scalars

Real Singlet: $\phi \rightarrow S$

Simplest Extension:
two states h_1 & h_2



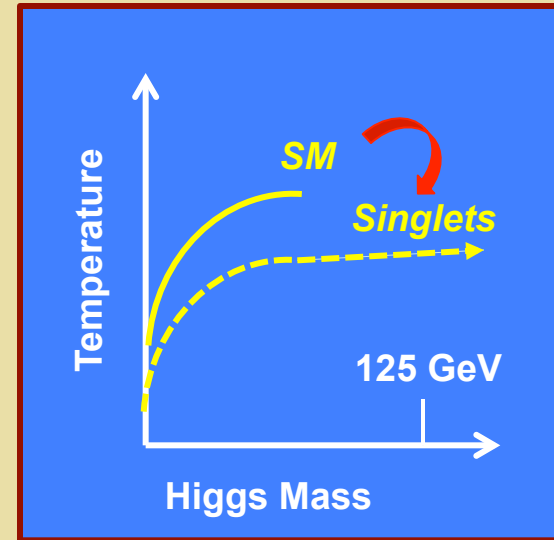
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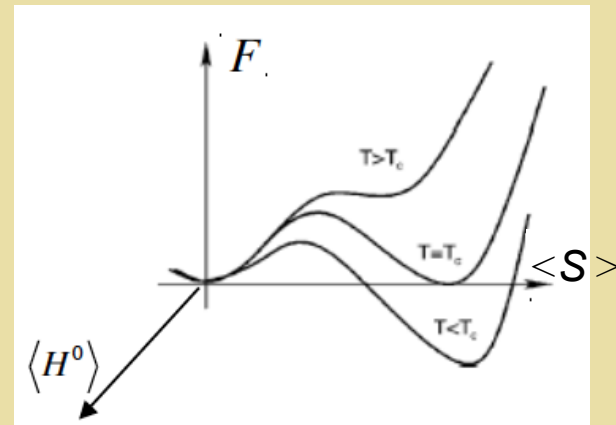
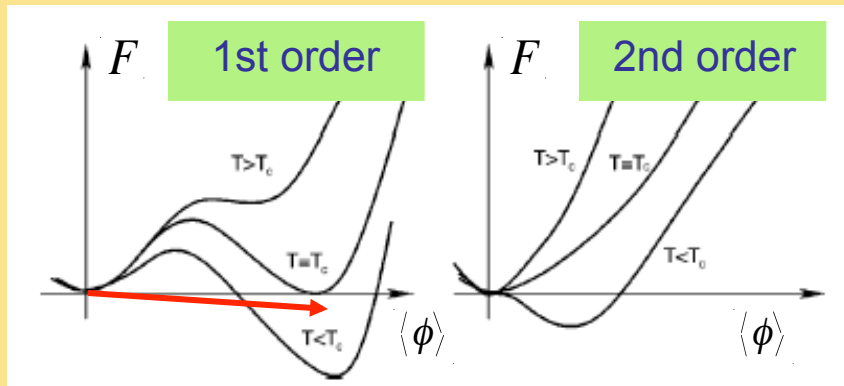
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EW Phase Diagram

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EW Phase Transition: Singlet Scalars

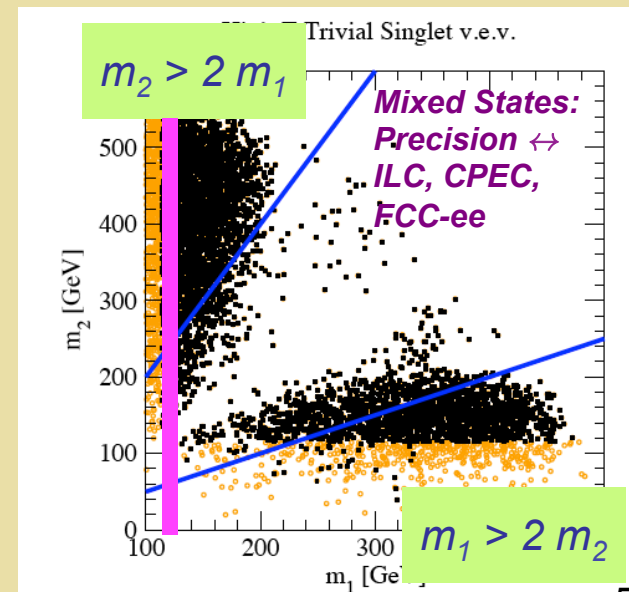


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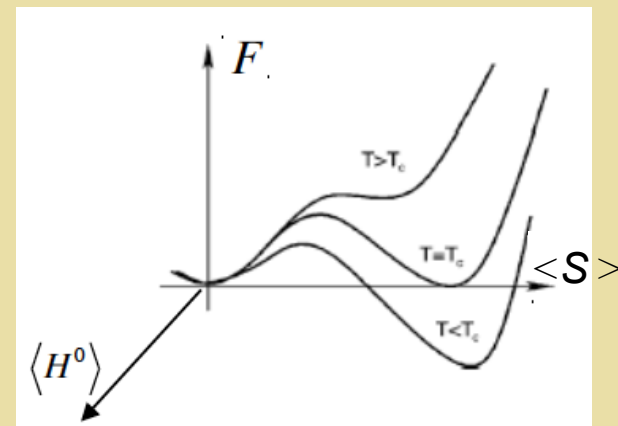
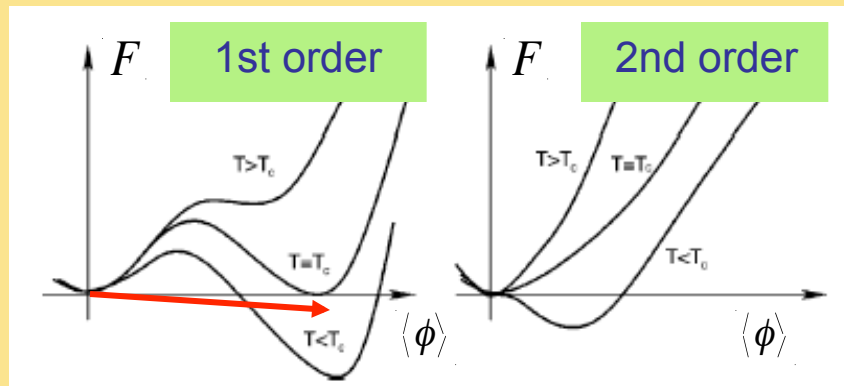
Real Singlet: $\phi \rightarrow S$

Simplest Extension: two states h_1 & h_2 – h, S mixtures



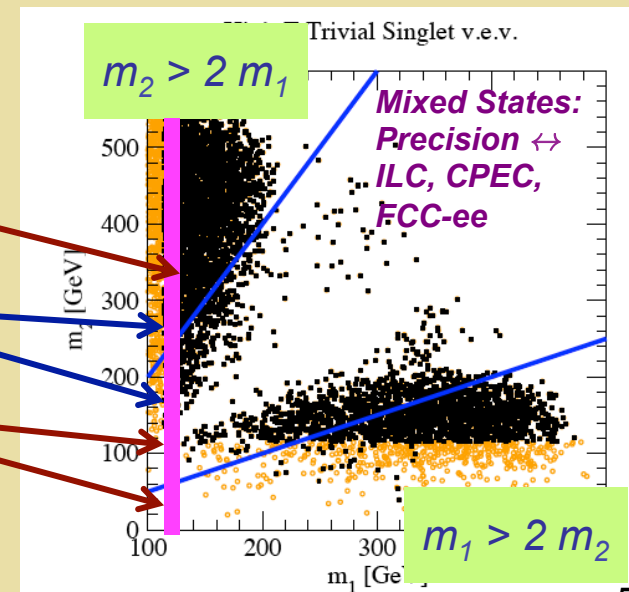
Profumo, MJRM, Shaughnessy '07

EW Phase Transition: Singlet Scalars



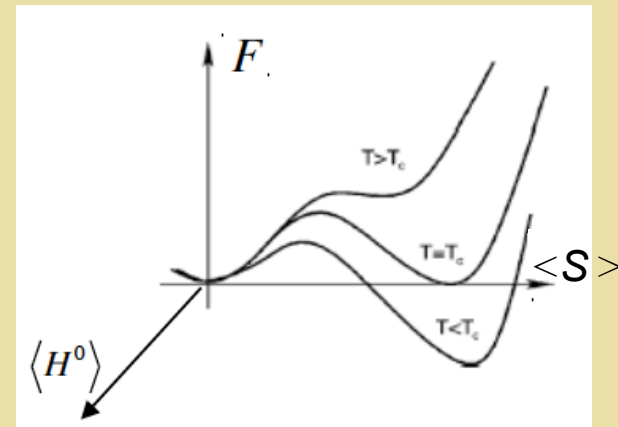
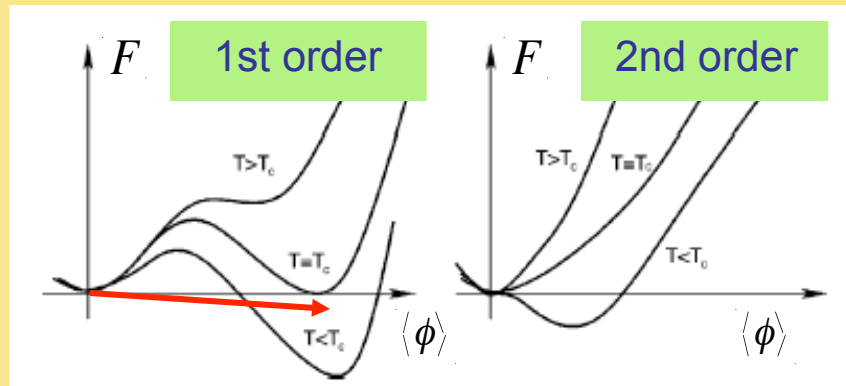
Collider probes

- Resonant di-Higgs production
- Precision Higgs measurements
- Non-resonant di-Higgs & exotic Higgs decays



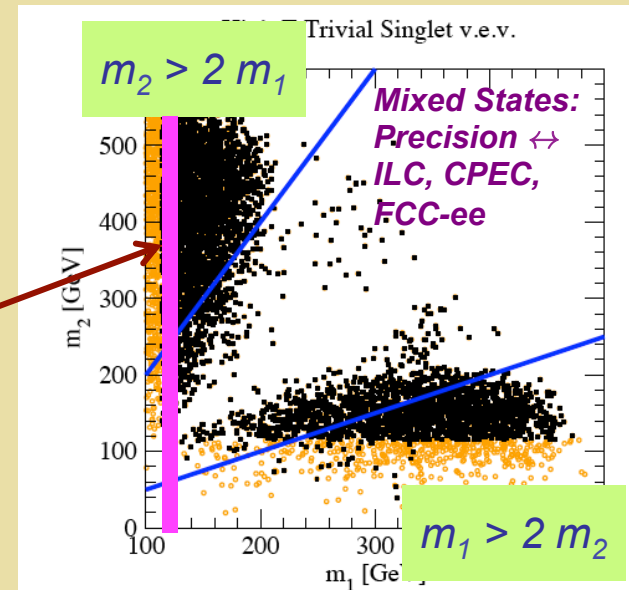
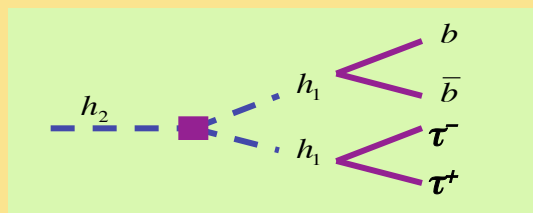
Profumo, MJRM, Shaughnessy '07

EW Phase Transition: New Scalars



Increasing m_h \longrightarrow

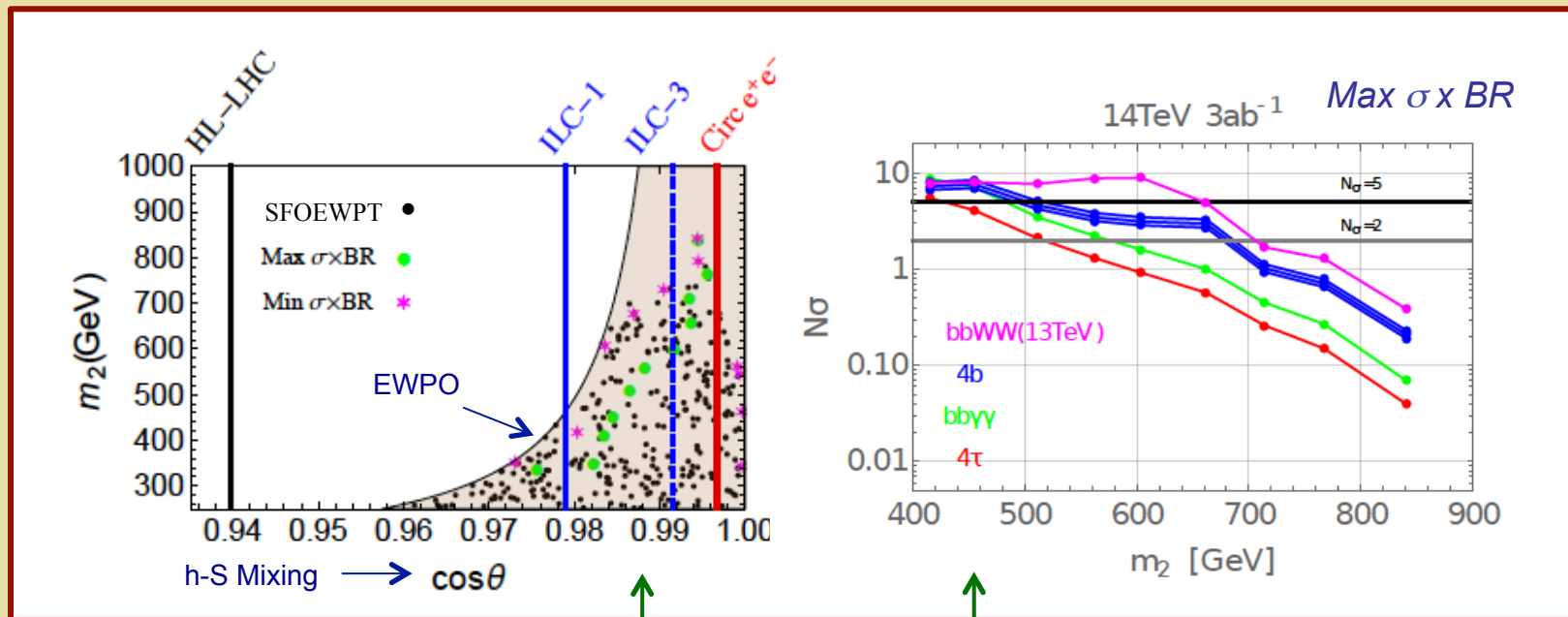
Resonant di-Higgs production



No & RM, arXiv:1310.6035 : LHC Discovery w/ 100 fb^{-1}

EWPT & Singlets: Res Di-Higgs Prod

SFOEWPT Benchmarks: Resonant di-Higgs & precision Higgs studies

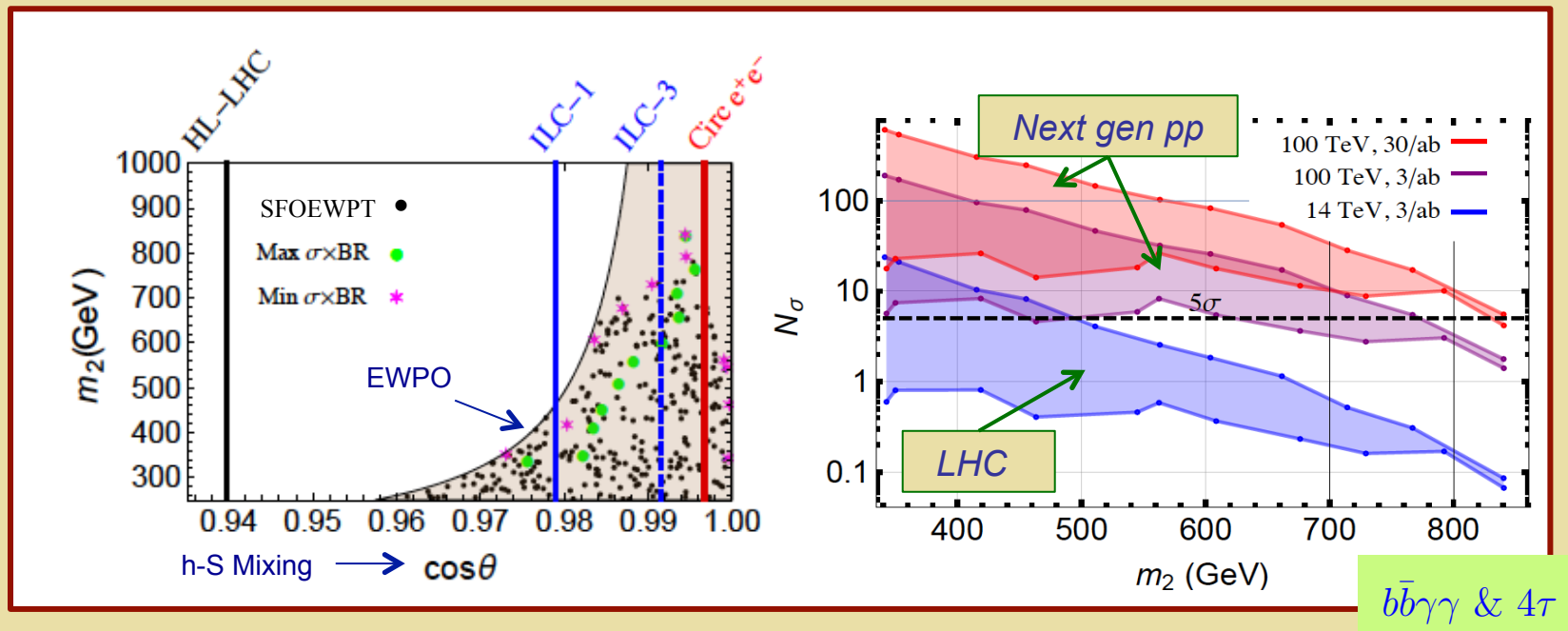


Kotwal, No, R-M, Winslow 1605.06123

Li, R-M, Willocq 1906.05289
See also: Huang et al, 1701.04442

EWPT & Singlets: Res Di-Higgs Prod

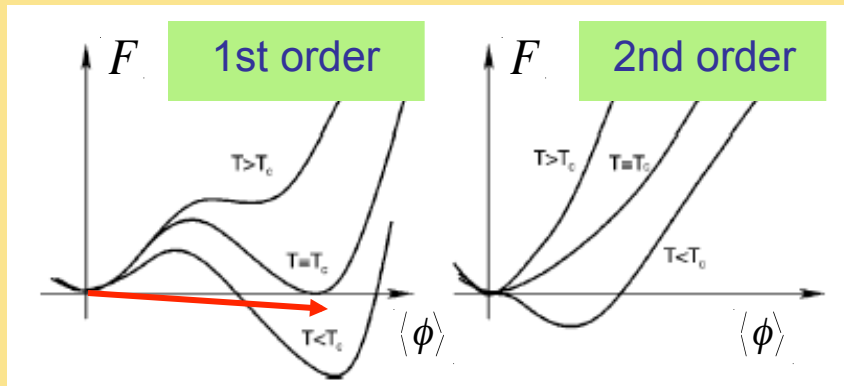
SFOEWPT Benchmarks: Resonant di-Higgs & precision Higgs studies



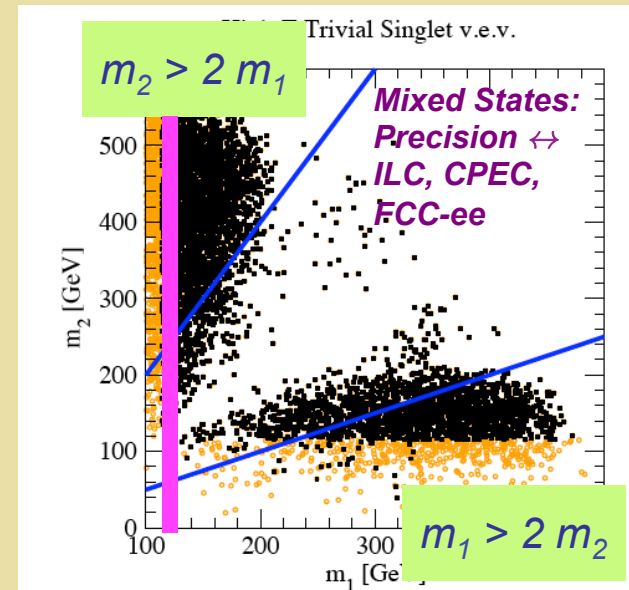
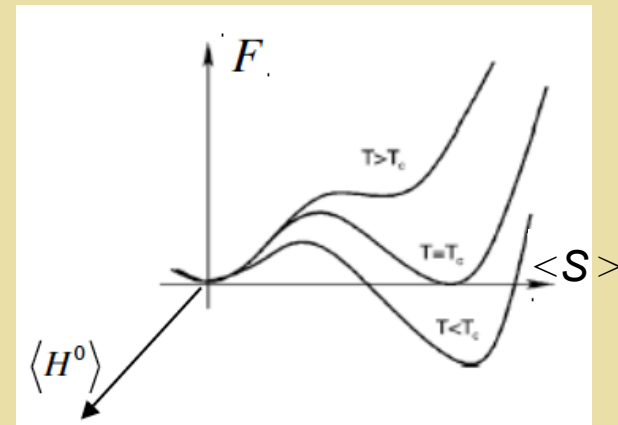
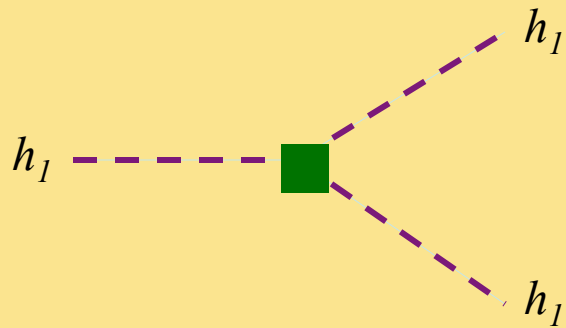
Kotwal, No, R-M, Winslow 1605.06123

See also: Huang et al, 1701.04442;
Li et al, 1906.05289

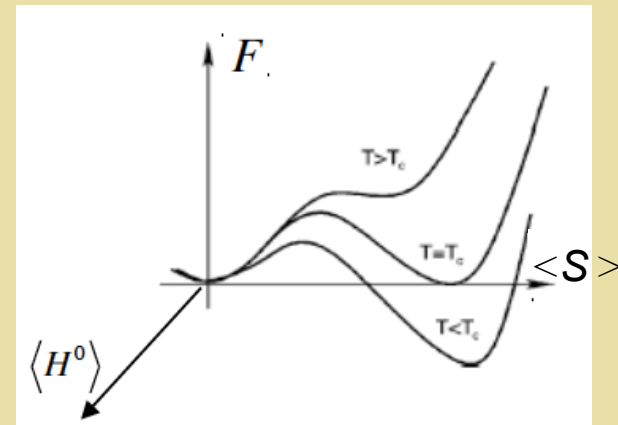
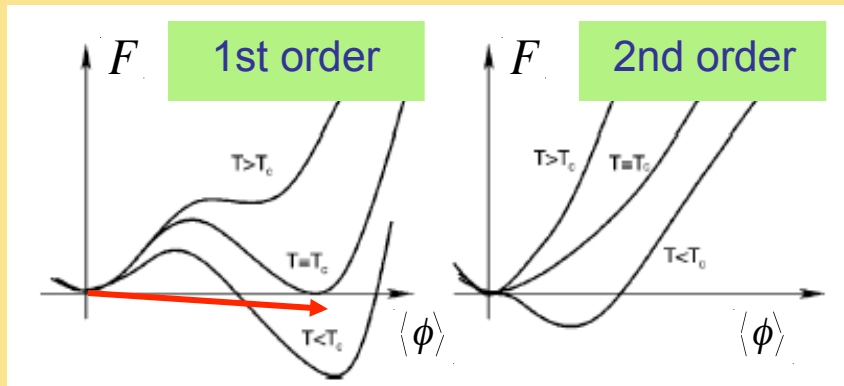
EW Phase Transition: New Scalars



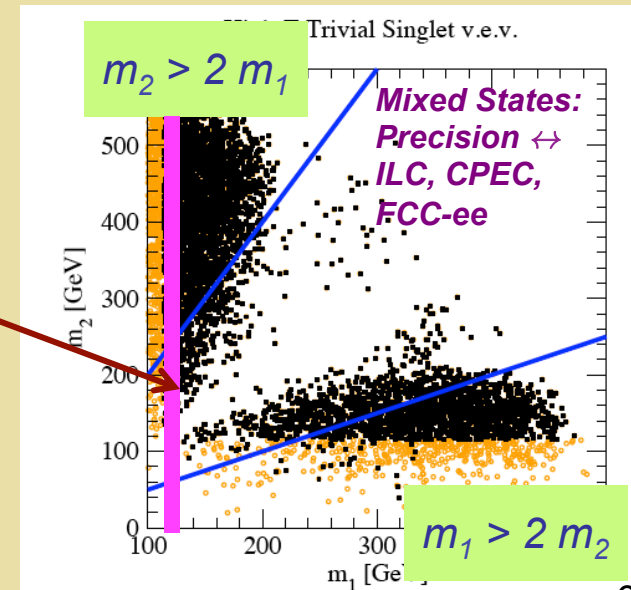
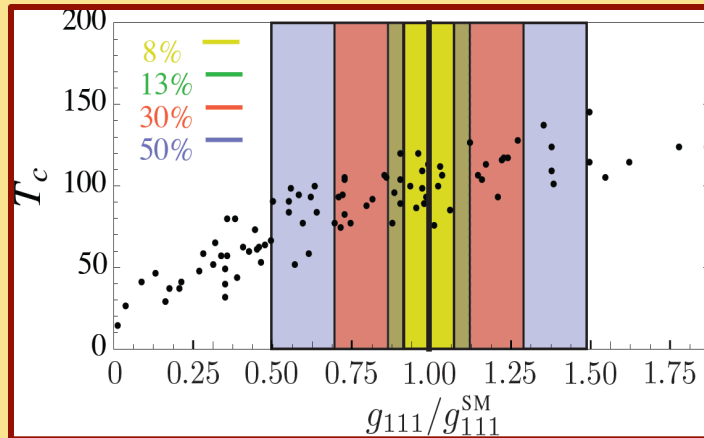
Modified Higgs Self-Coupling



EW Phase Transition: Singlet Scalars

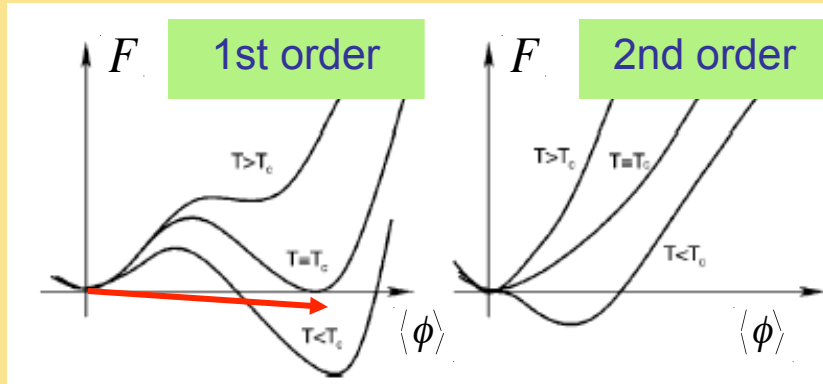


Modified Higgs Self-Coupling

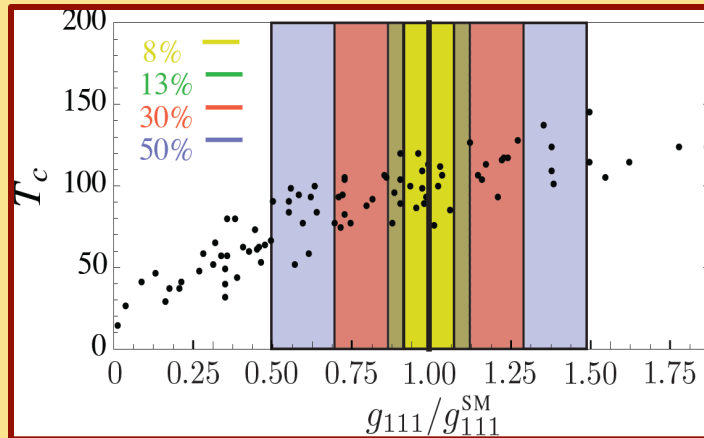


Profumo, R-M, Wainwright, Winslow: 1407.5342; see also Noble & Perelstein 0711.3018

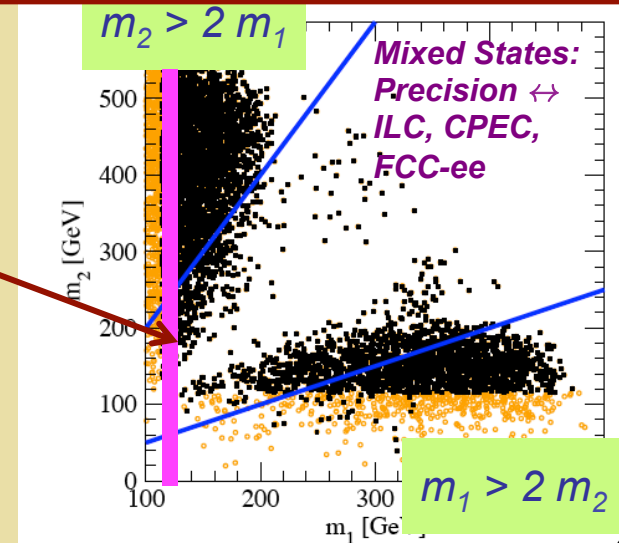
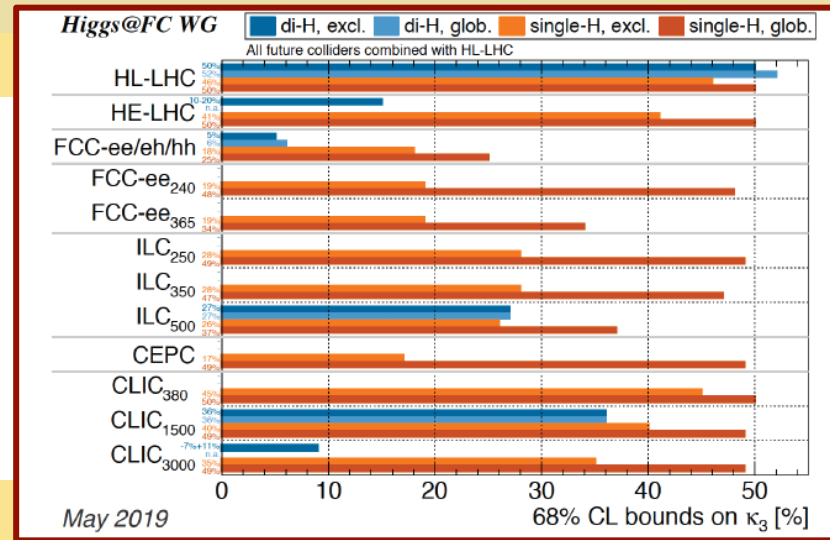
EW Phase Transition: Singlet Scalars



Modified Higgs Self-Coupling

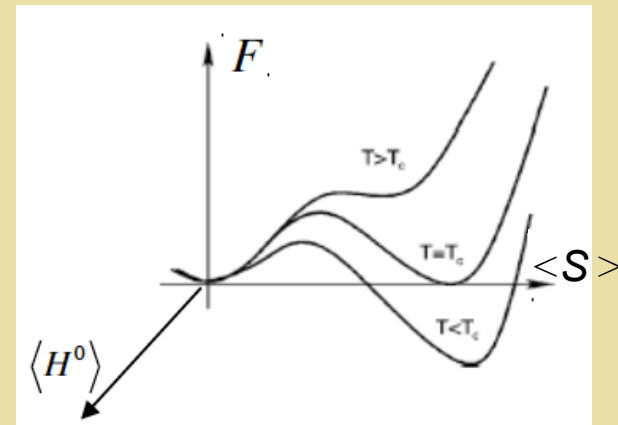
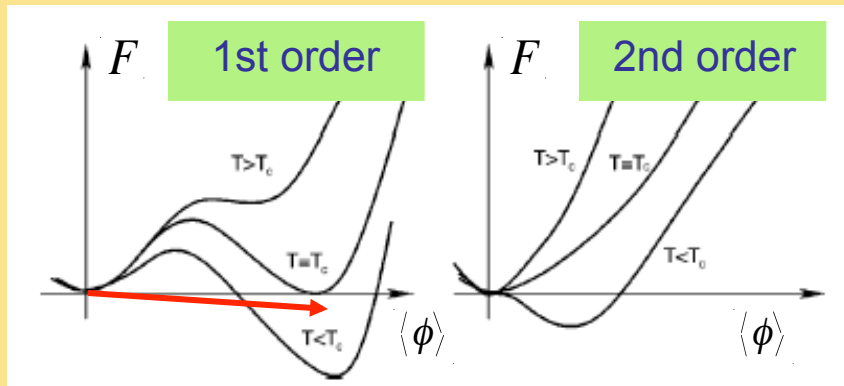


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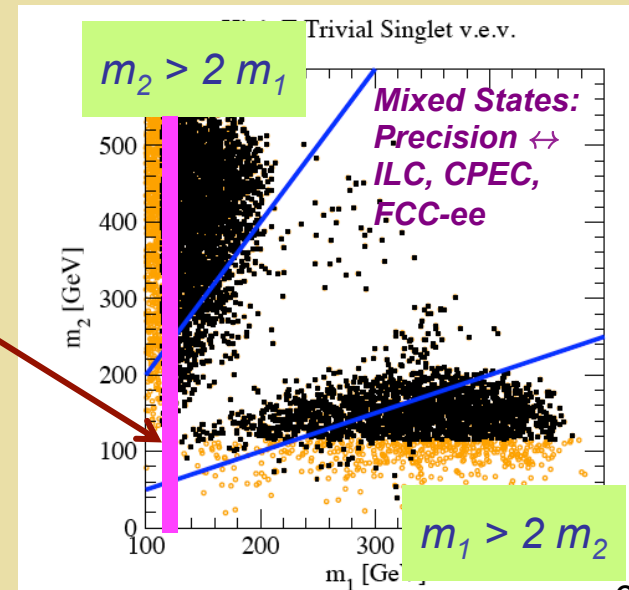
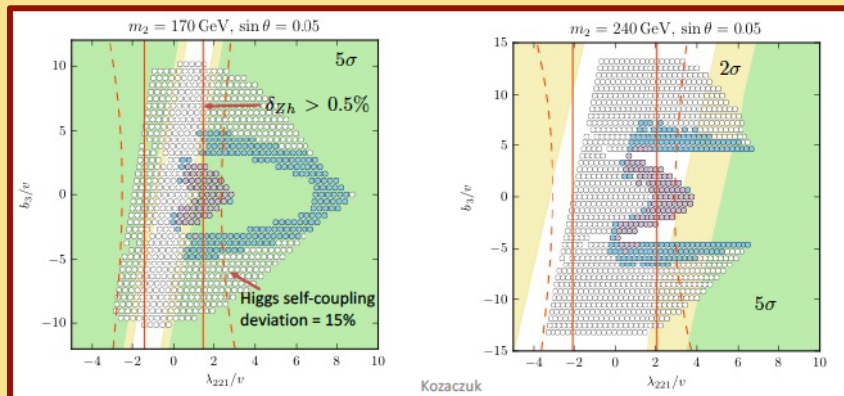


Thanks: M. Cepeda

EW Phase Transition: Singlet Scalars



Singlet-like pair production (off shell)



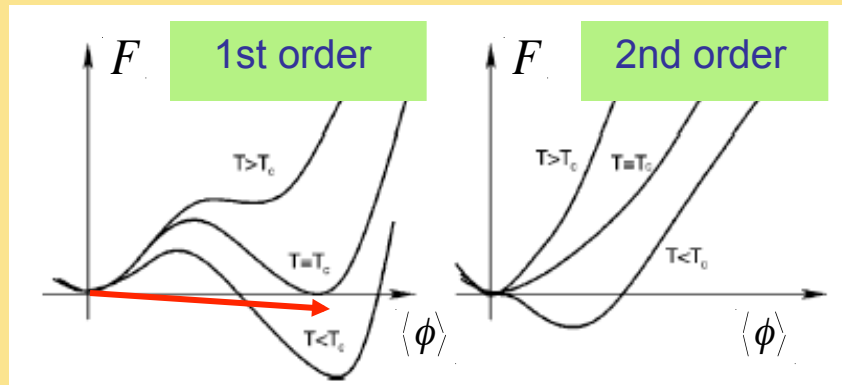
Chen, Kozacuk, Lewis 2017

Higgs Portal: Simple Scalar Extensions

<i>Extension</i>	<i>DOF</i>	<i>EWPT</i>	<i>DM</i>
<i>Real singlet: Z₂</i>	1	✓	✗
<i>Real singlet: Z₂</i>	1	✓	✓
<i>Complex Singlet</i>	2	✓	✓
<i>EW Multiplets</i>	3+	✓	✓

May be low-energy remnants of UV complete theory & illustrative of generic features

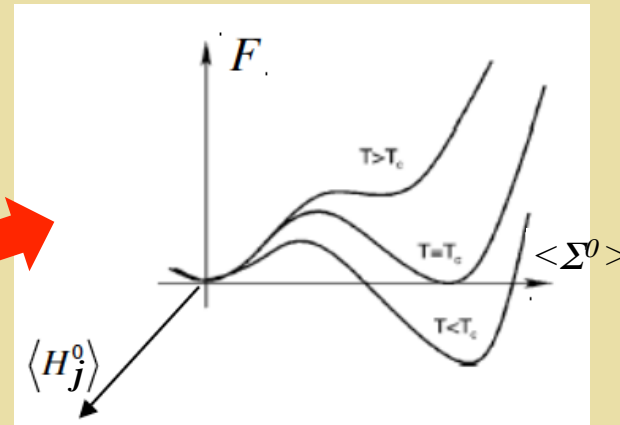
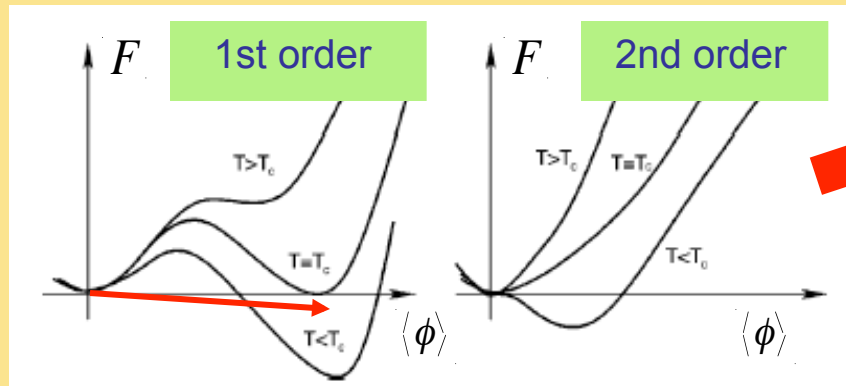
EW Multiplets: EWPT



Increasing m_h \longrightarrow

\longleftarrow New scalars

EW Multiplets: EWPT

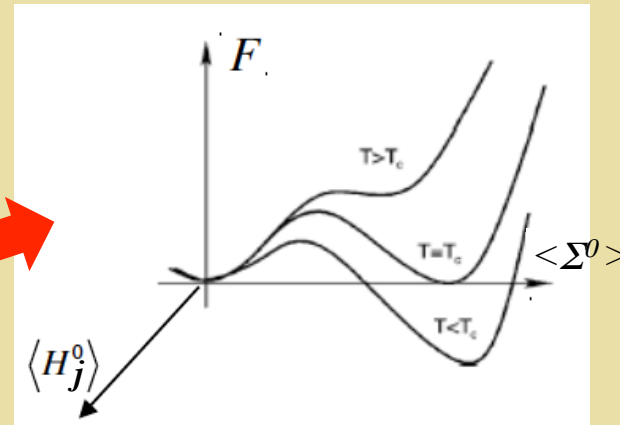
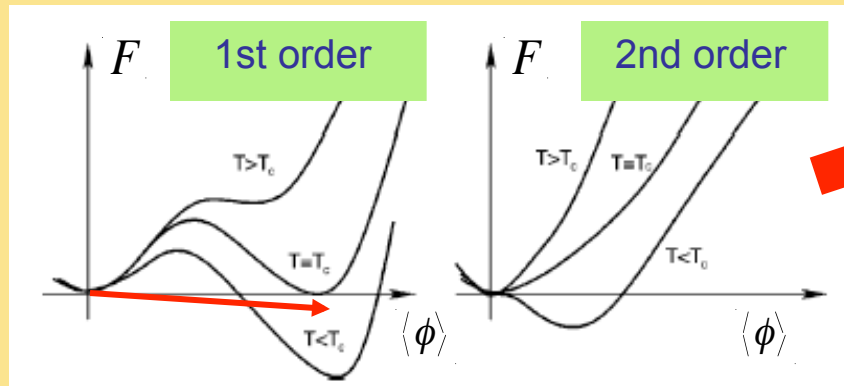


Increasing m_h \longrightarrow

\longleftarrow New scalars

- Thermal loops
- Tree-level barrier

EW Multiplets: EWPT



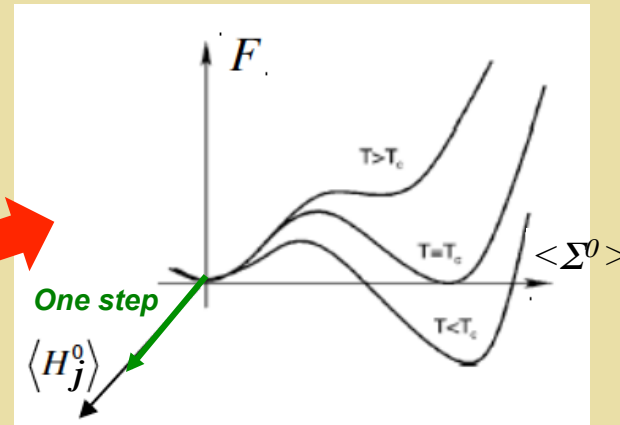
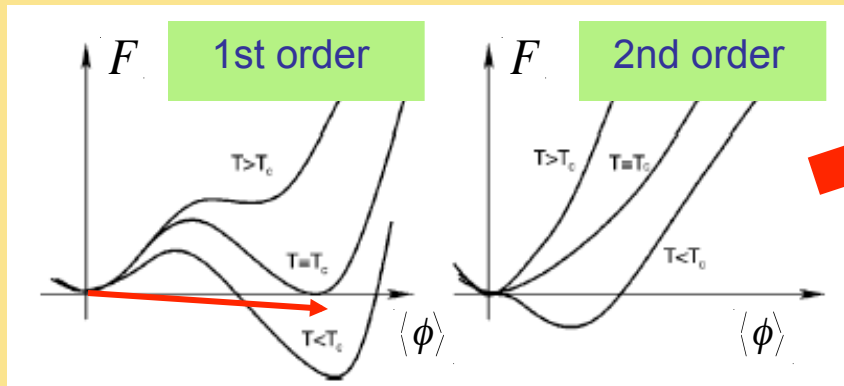
Increasing m_h \longrightarrow

\longleftarrow New scalars

- Thermal loops
- Tree-level barrier

Illustrate with real triplet: $\Sigma \sim (1, 3, 0)$

EW Multiplets: One-Step EWPT



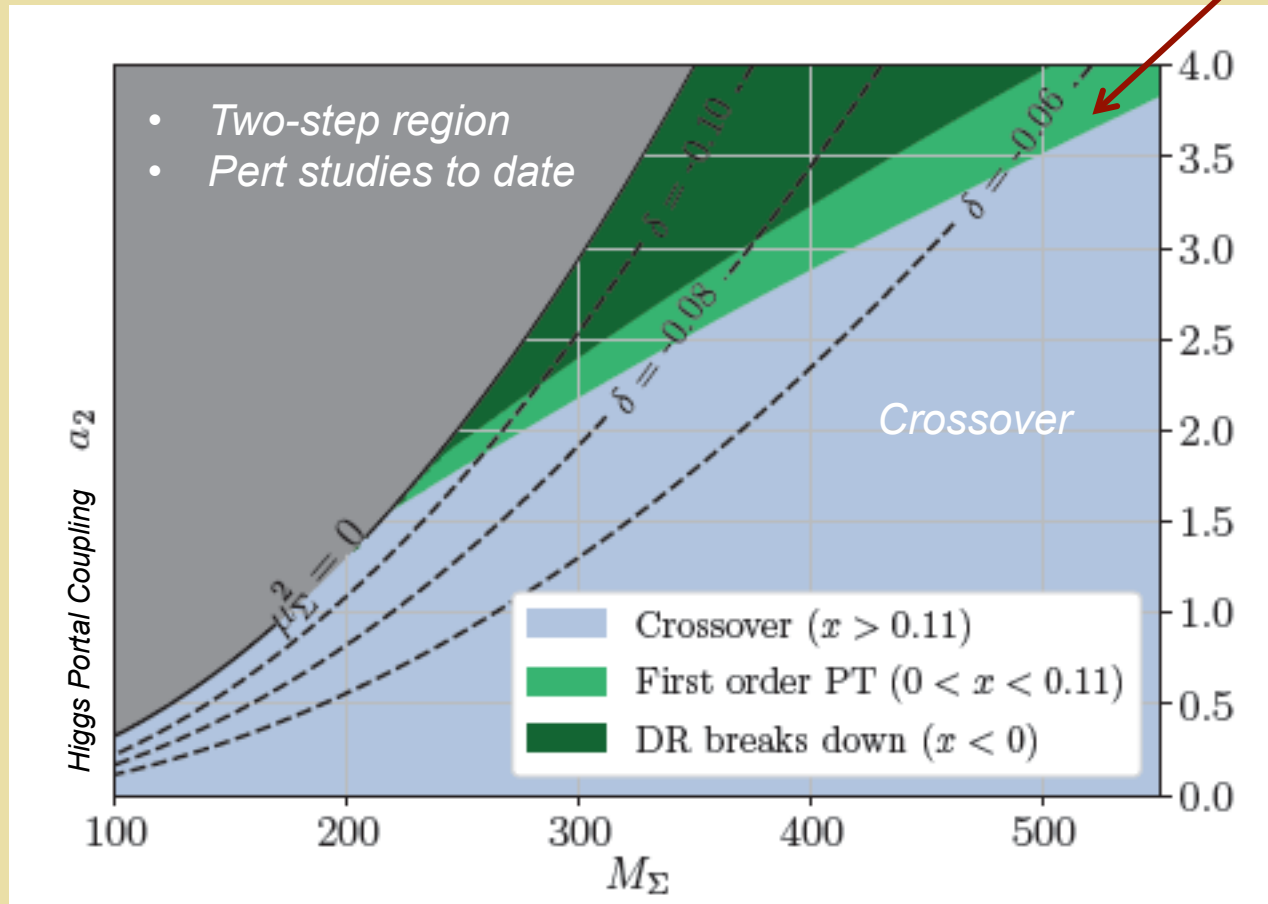
Increasing m_h \longrightarrow

\longleftarrow New scalars

- One-step: Sym phase \rightarrow Higgs phase

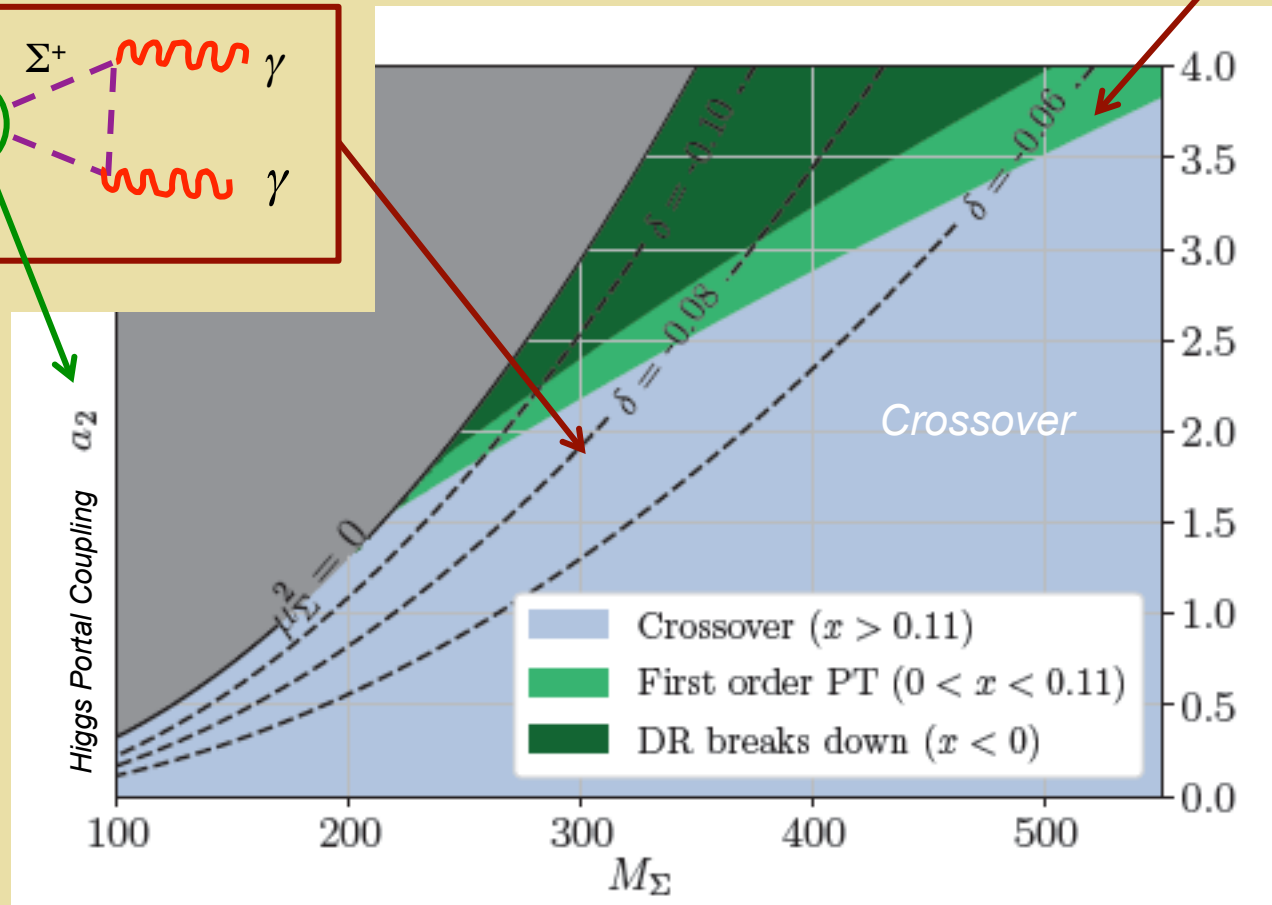
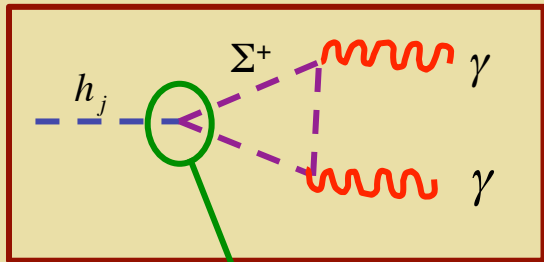
Real Triplet: One-Step EWPT

FOEWPT



- One-step
- Non-perturbative

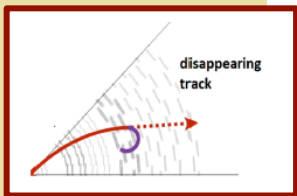
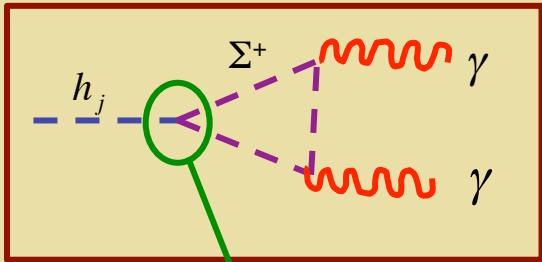
Real Triplet & EWPT



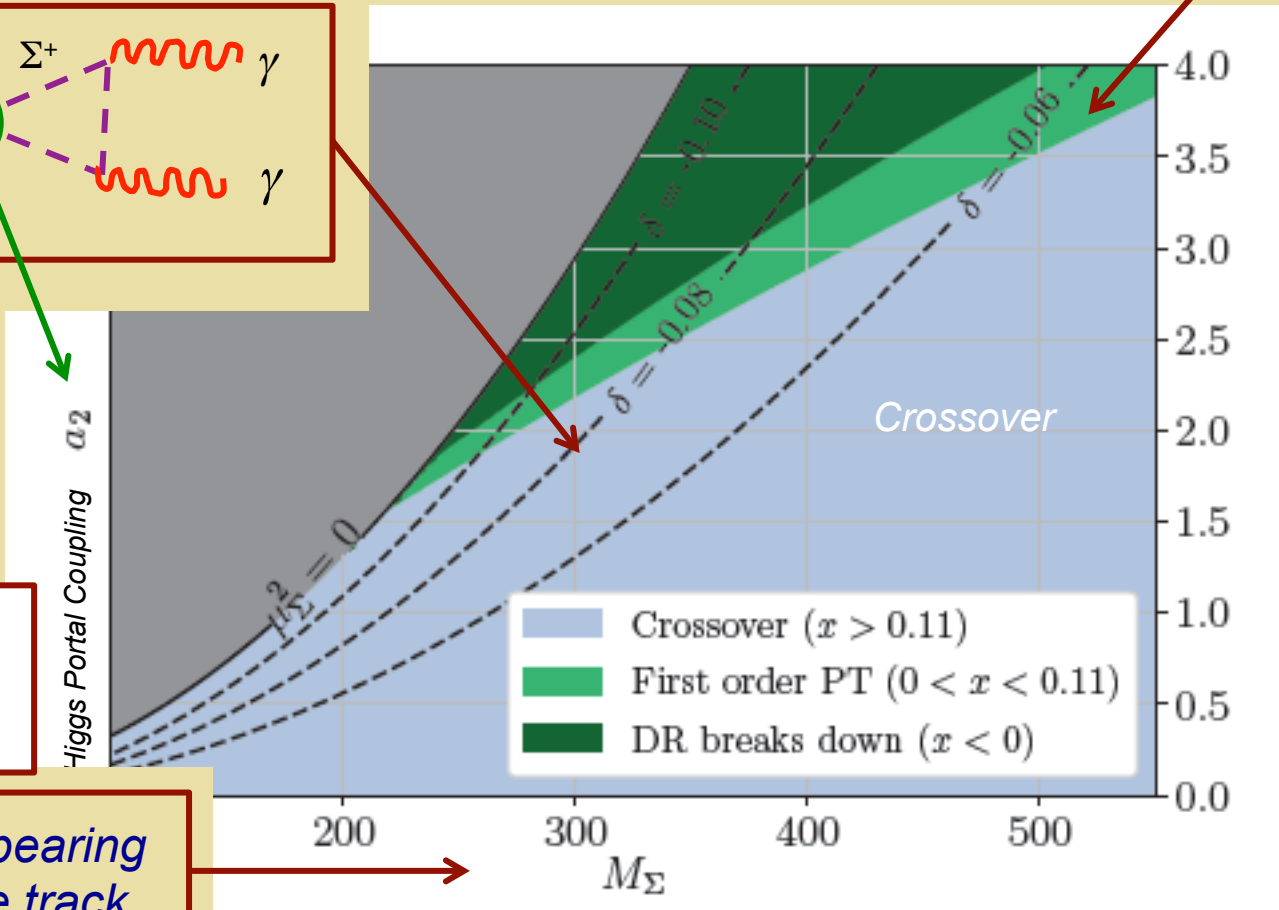
- One-step
- Non-perturbative

Real Triplet & EWPT

FOEWPT



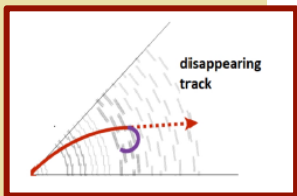
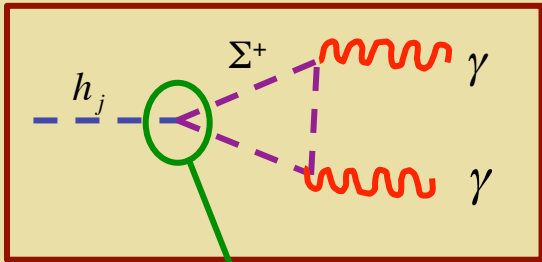
Disappearing charge track



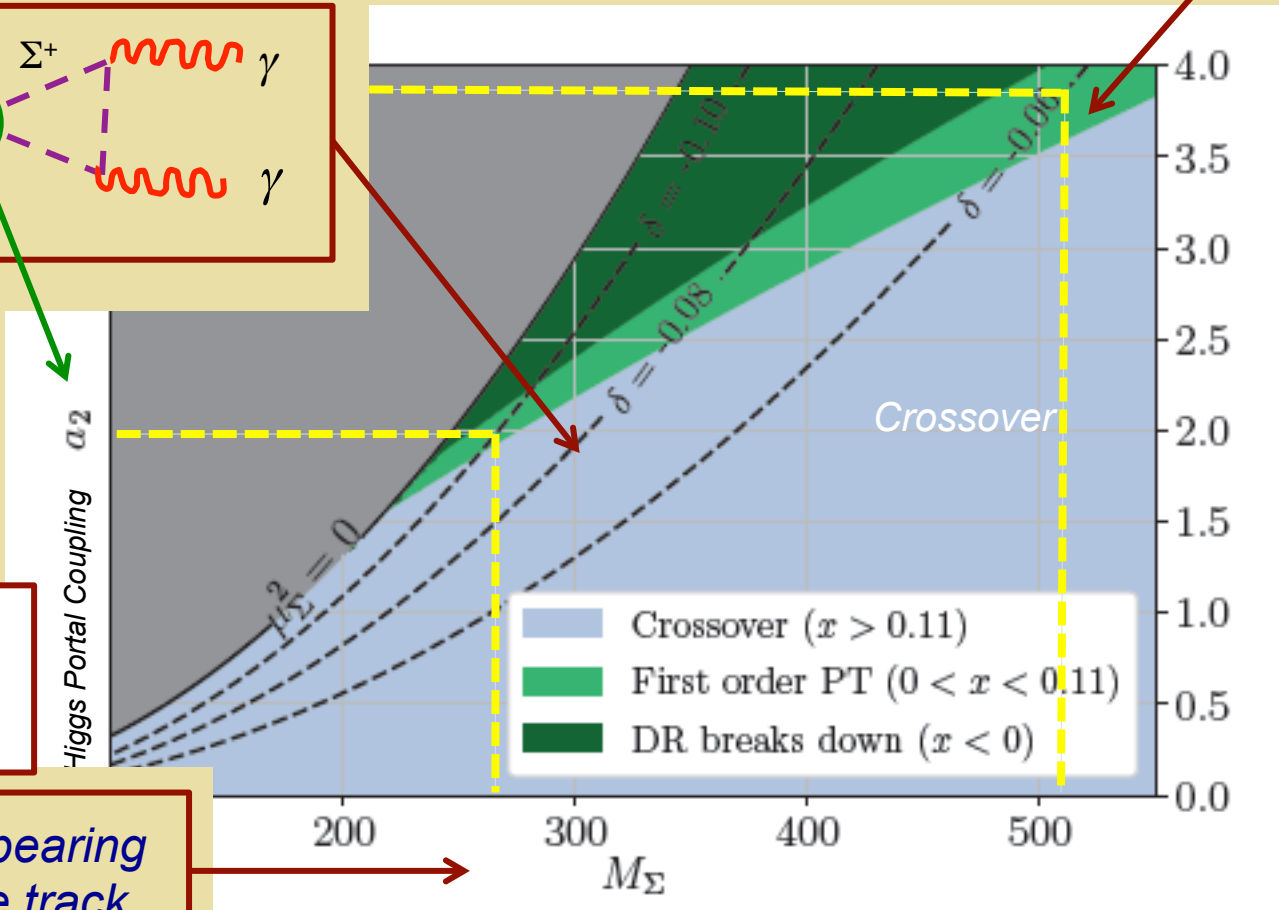
- One-step
- Non-perturbative

Real Triplet & EWPT

FOEWPT

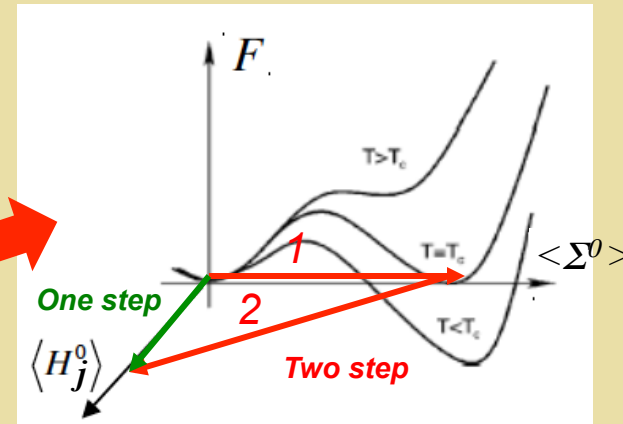
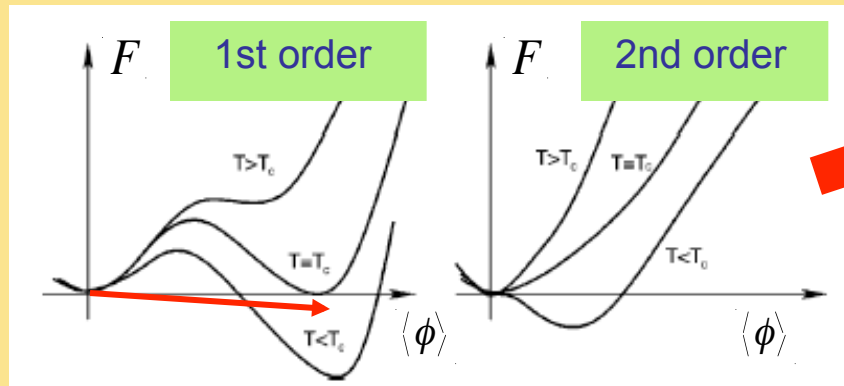


Disappearing charge track



- One-step
- Non-perturbative

EW Multiplets: Two-Step EWPT

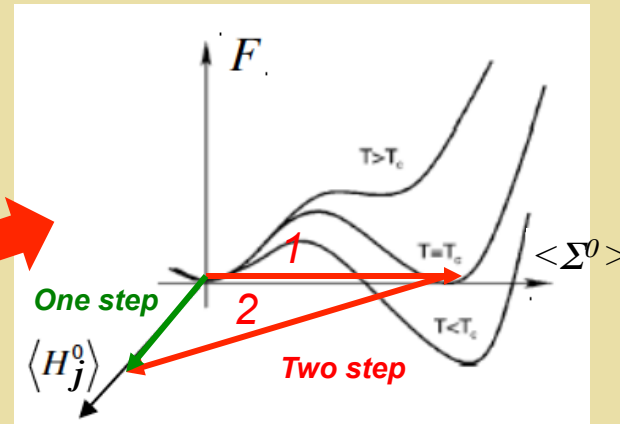
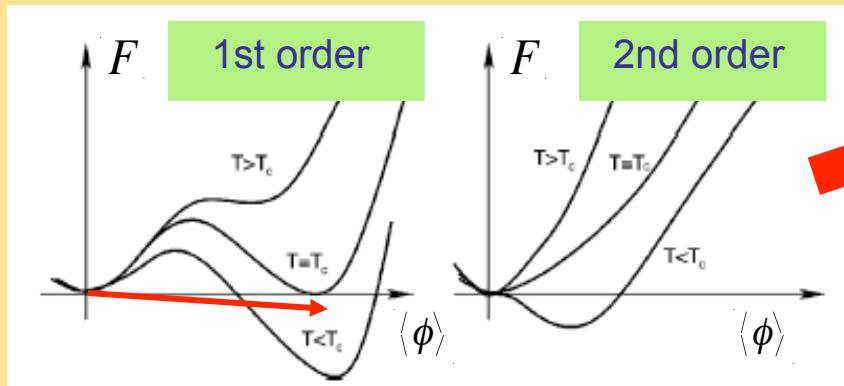


Increasing m_h \longrightarrow

\longleftarrow New scalars

- One-step: Sym phase \rightarrow Higgs phase
- Two-step: successive EW broken phases

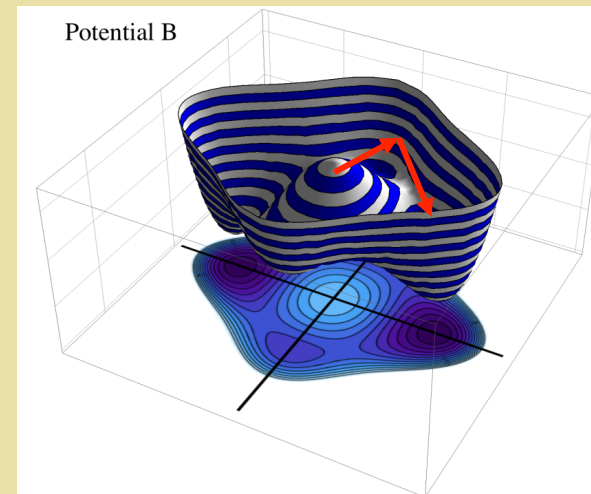
EW Multiplets: Two-Step EWPT



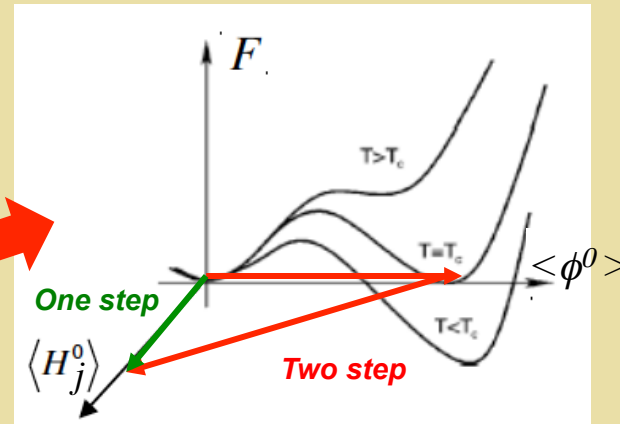
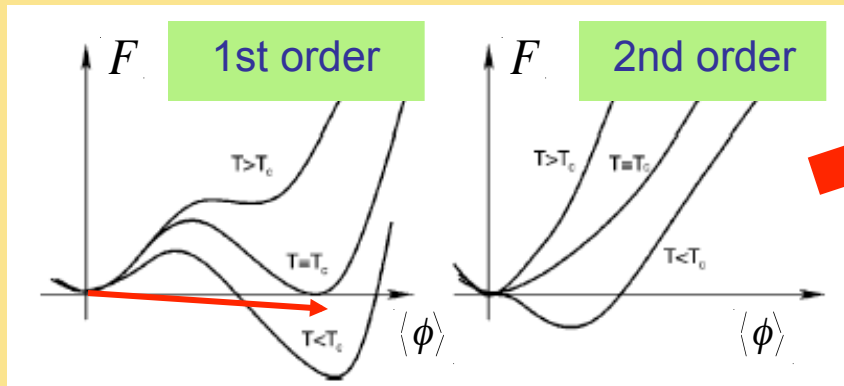
Increasing m_h \longrightarrow

\longleftarrow New scalars

- One-step: Sym phase \rightarrow Higgs phase
- Two-step: successive EW broken phases



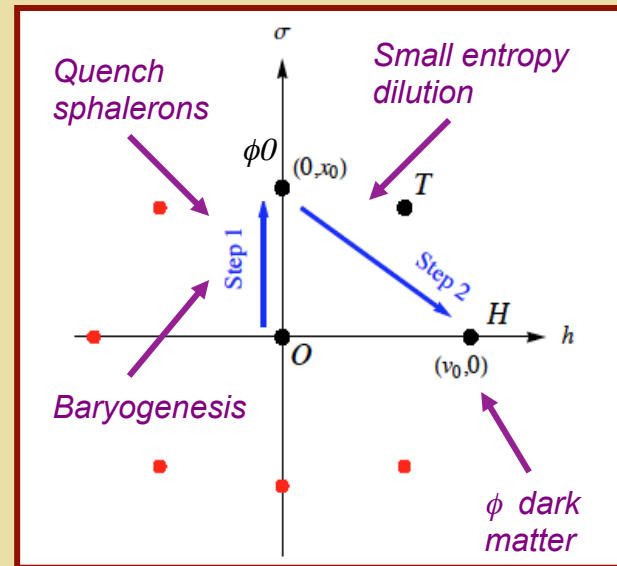
EW Multiplets: Two-Step EWPT



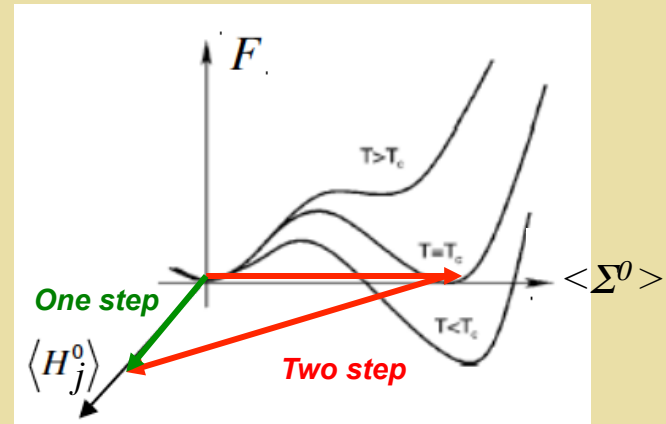
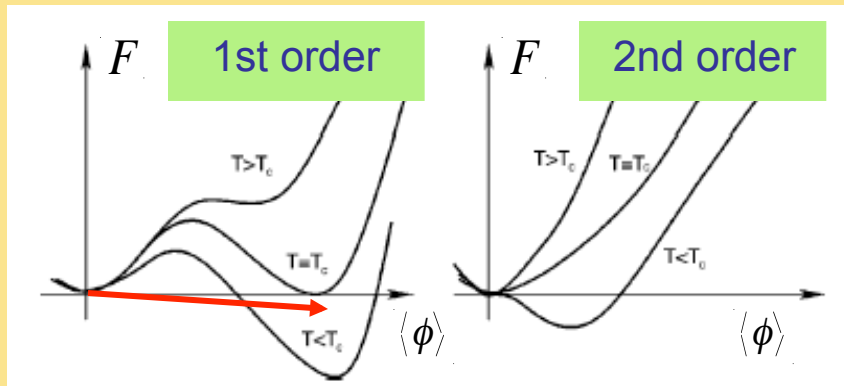
Increasing m_h \longrightarrow

\longleftarrow New scalars

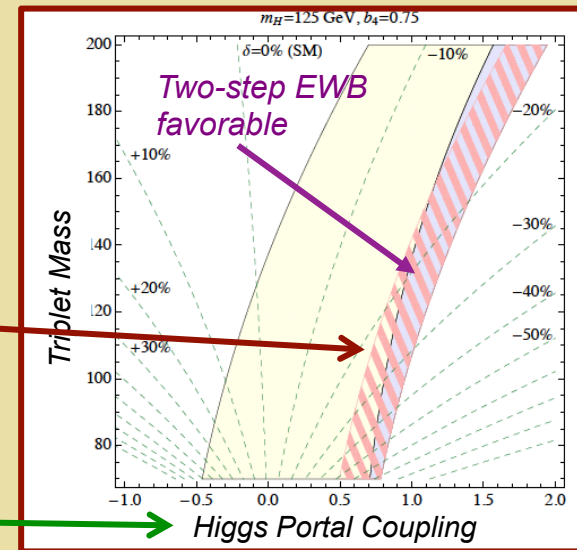
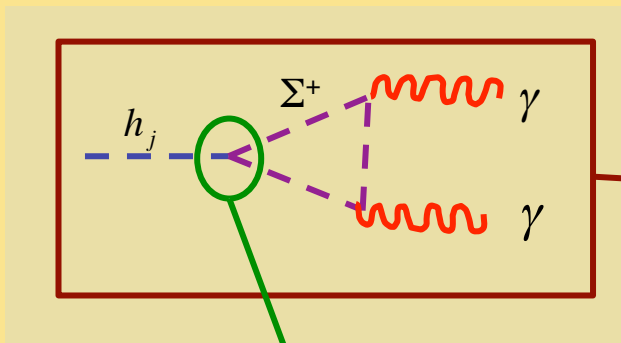
- Step 1: thermal loops
- Step 2: tree-level barrier



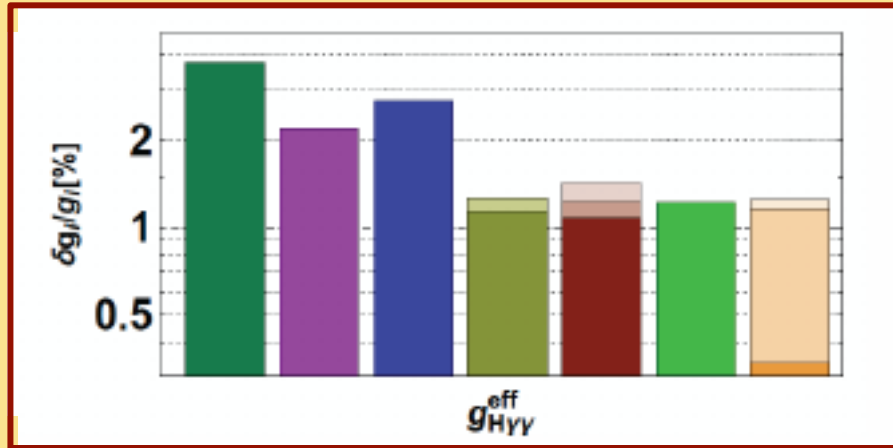
EW Multiplets: Two-Step EWPT



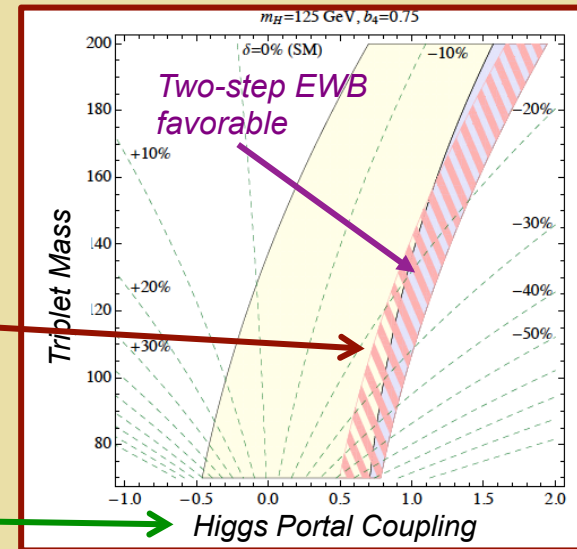
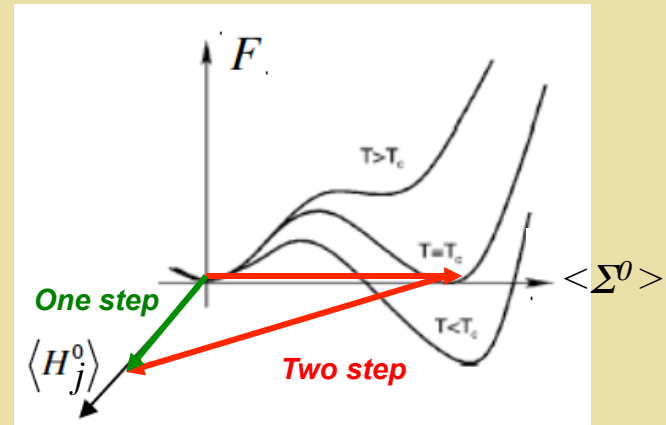
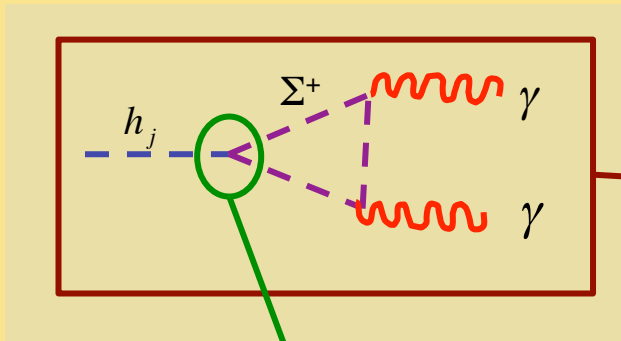
Increasing m_h \longrightarrow



EW Multiplets: Two-Step EWPT



Increasing m_h \longrightarrow



IV. Outlook

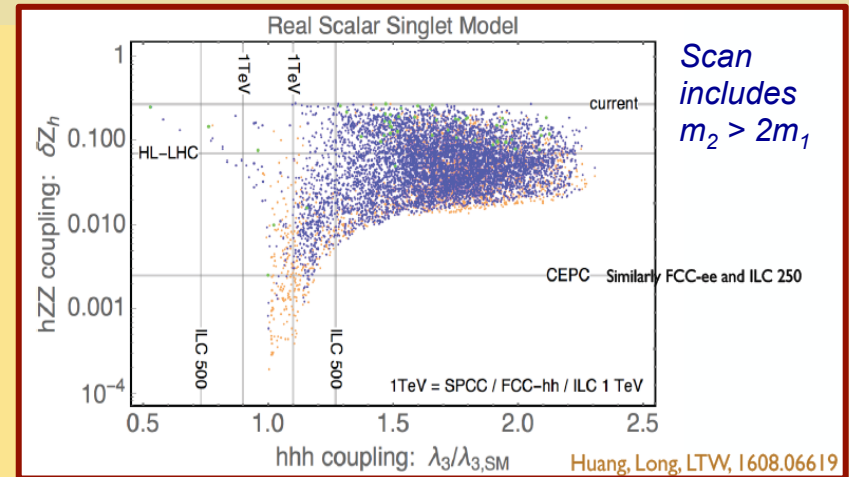
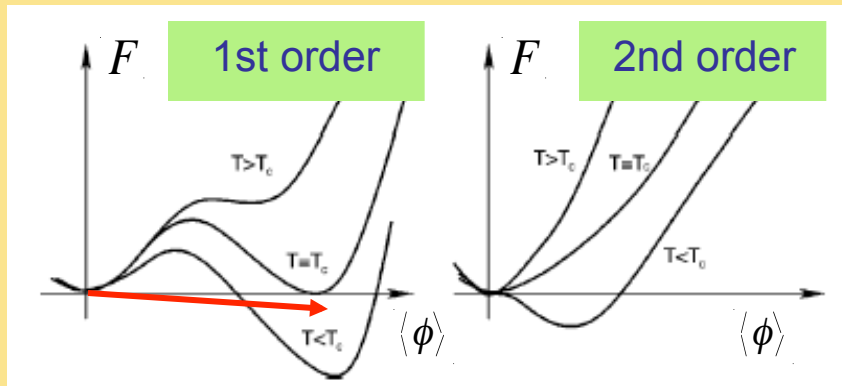
- *Determining the thermal history of EWSB is field theoretically interesting in its own right and of practical importance for baryogenesis and GW*
- *The scale $T_{EW} \rightarrow$ any new physics that modifies the SM crossover transition to a first order transition must live at $M < 1 \text{ TeV}$*
- *Searches for new scalars and precision Higgs measurements at the LHC and prospective next gen colliders could conclusively determine the nature of the EWSB transition*

Main Theme for This Talk

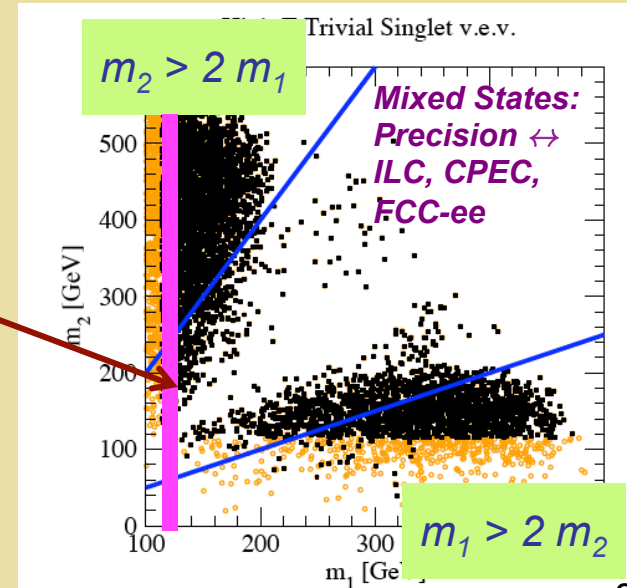
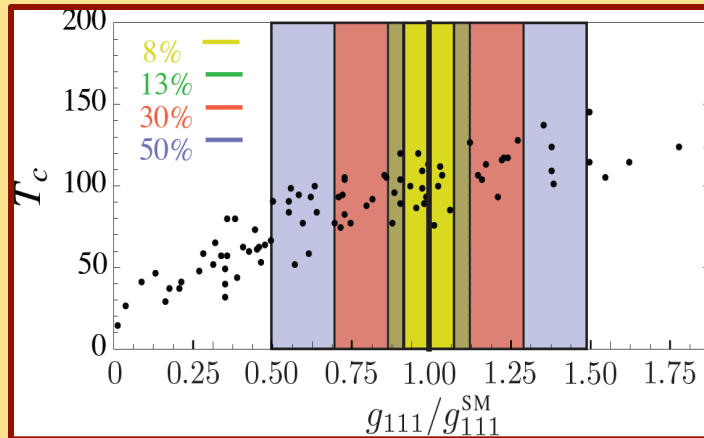
$T_{EW} \rightarrow$ EW phase transition is a target for the LHC & beyond

Back Up Slides

EW Phase Transition: Singlet Scalars



Modified Higgs Self-Coupling

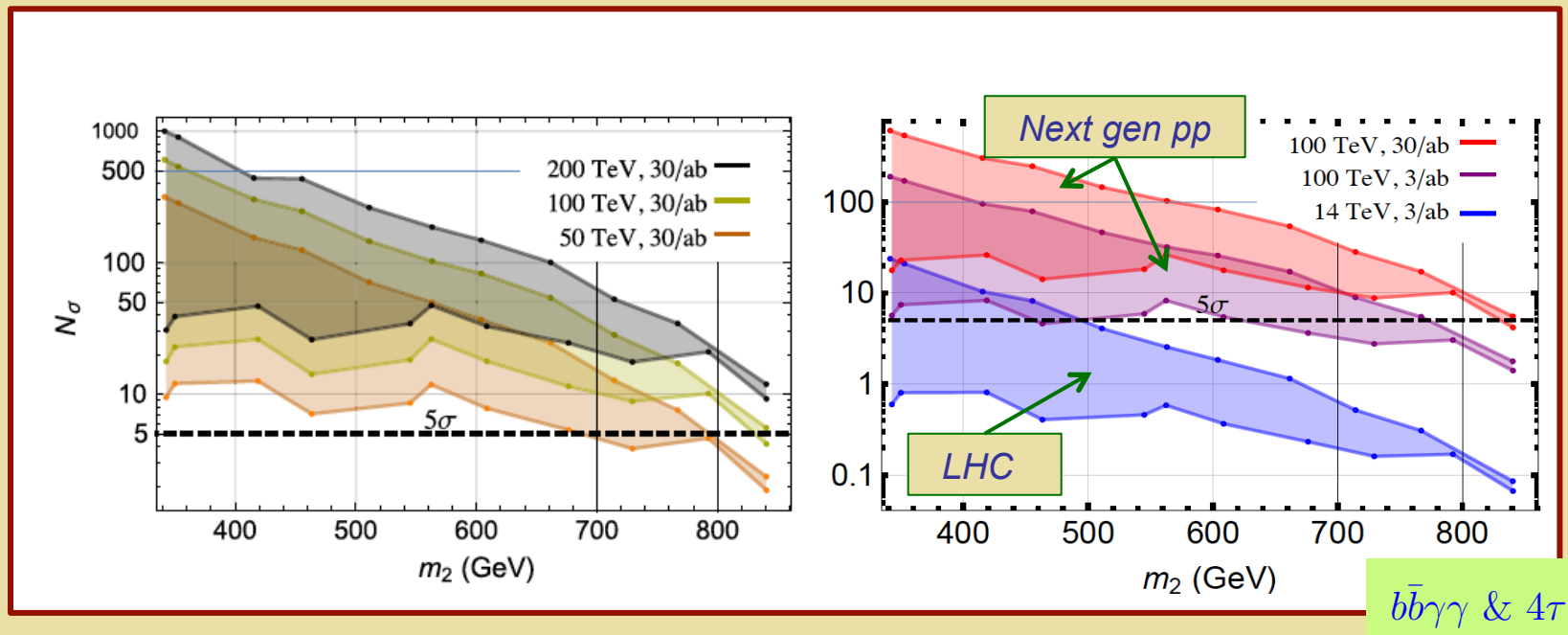


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Thanks: M. Cepeda

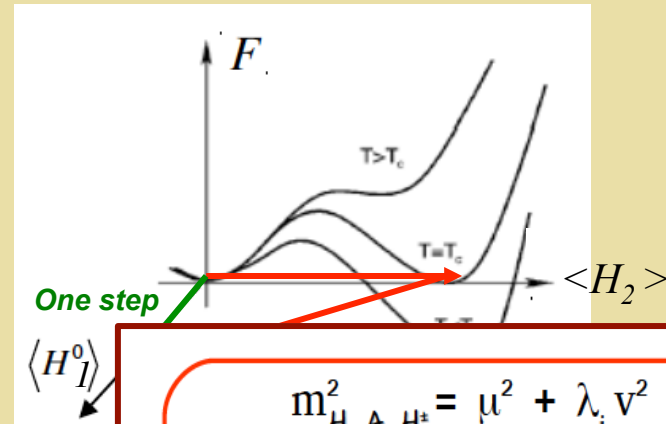
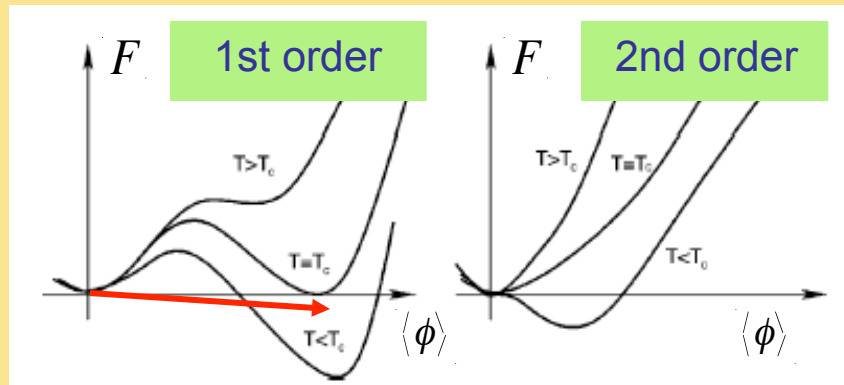
EW Phase Transition: Singlet Scalars

SFOEWPT Benchmarks: Resonant di-Higgs



Kotwal, No, R-M, Winslow 1605.06123

EW Multiplets: 2HDM



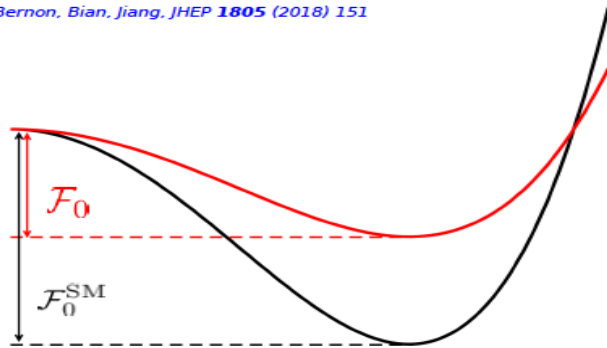
$$m_{H_0, A_0, H^\pm}^2 = \mu^2 + \lambda_i v^2$$

Difference between Symmetric - Broken phase in CW piece guaranteed for large BSM mass splitting!

$$m_{A_0} - m_{H_0}$$

Increasing m_h \longrightarrow

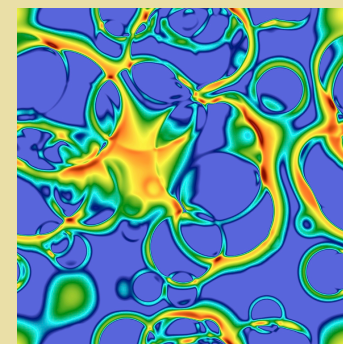
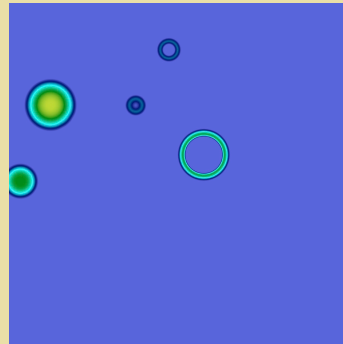
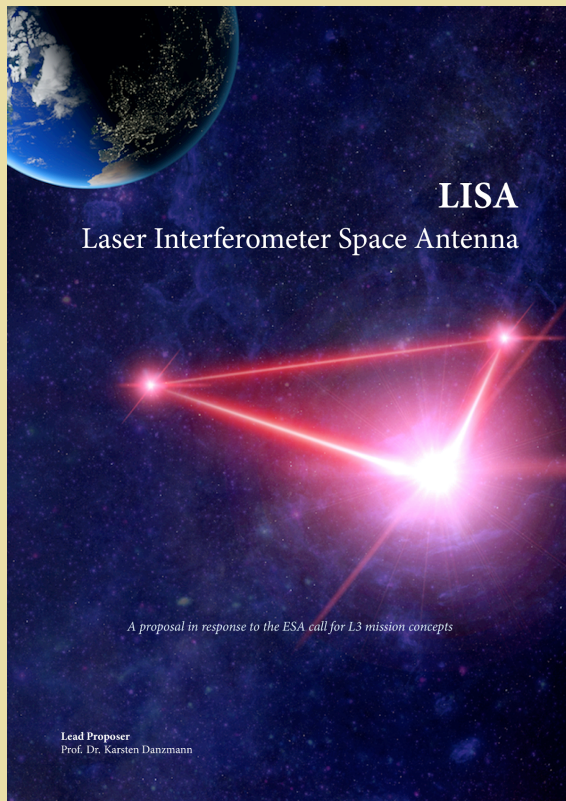
Nature of EWPT dominantly controlled by $T=0$ Vacuum energy difference
 Dorsch, Huber, Mimasu, JMN, JHEP 1712 (2017) 086
 Bernon, Bian, Jiang, JHEP 1805 (2018) 151



$$\Delta\mathcal{F} \equiv \mathcal{F}_0 - \mathcal{F}_0^{SM} = -\frac{v^2}{8} \cos(\beta - \alpha)^2 (m_{H_0}^2 - m_h^2) + \left[\sum_s \frac{m_s^4}{64\pi^2} \left(\log \frac{|m_s^2|}{Q^2} - \frac{1}{2} \right) \right]_{\text{broken}} - \left[\sum_s \frac{m_s^4}{64\pi^2} \left(\log \frac{|m_s^2|}{Q^2} - \frac{1}{2} \right) \right]_{\text{symmetric}}$$

Broken \longleftarrow \longrightarrow Symmetric
 1-loop (Coleman-Weinberg)

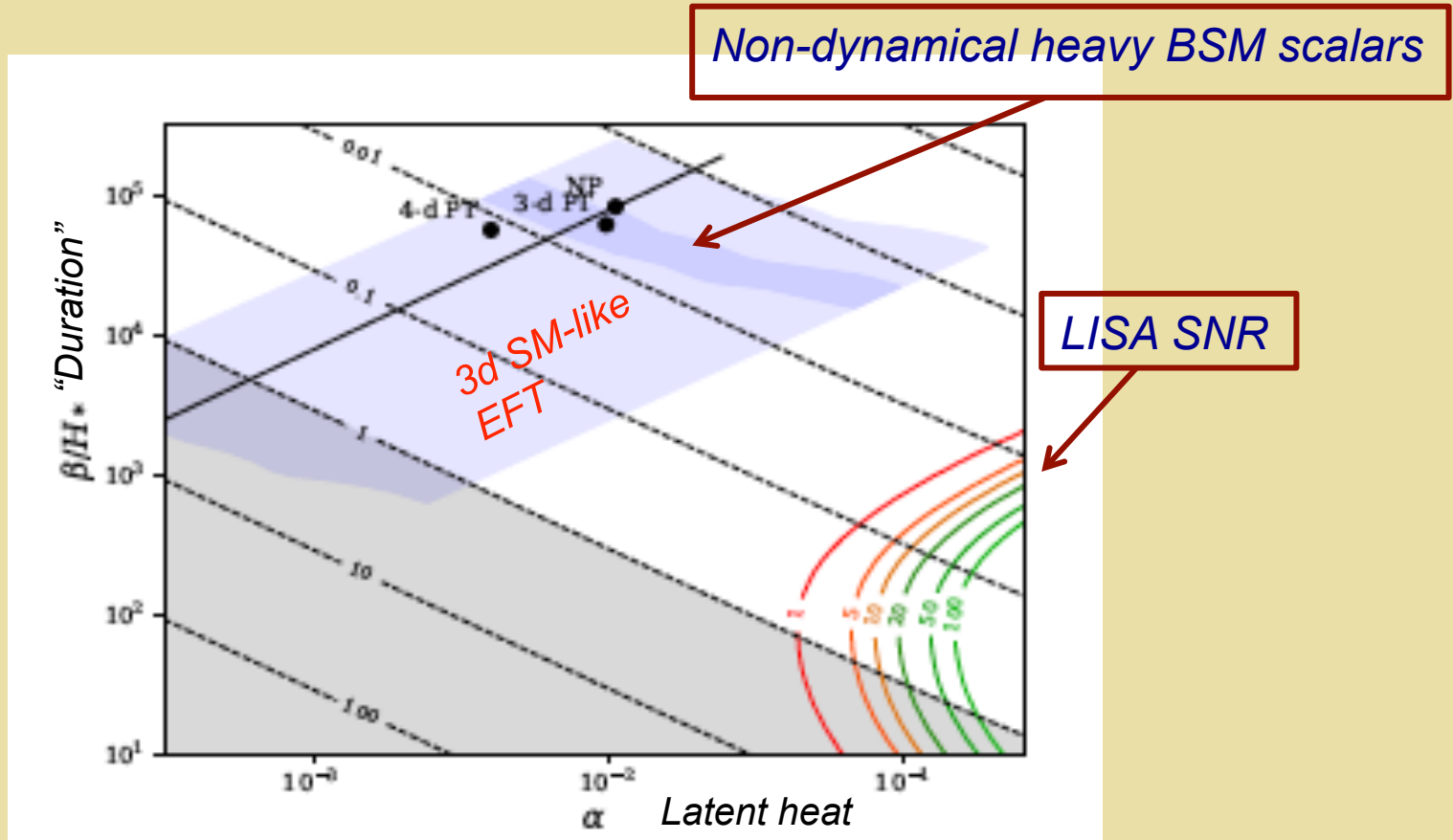
Gravitational Radiation



1. Bubbles nucleate and grow
2. Expand in a plasma - create reaction fronts
3. Bubbles + fronts collide - violent process
4. Sound waves left behind in plasma
5. Turbulence; damping

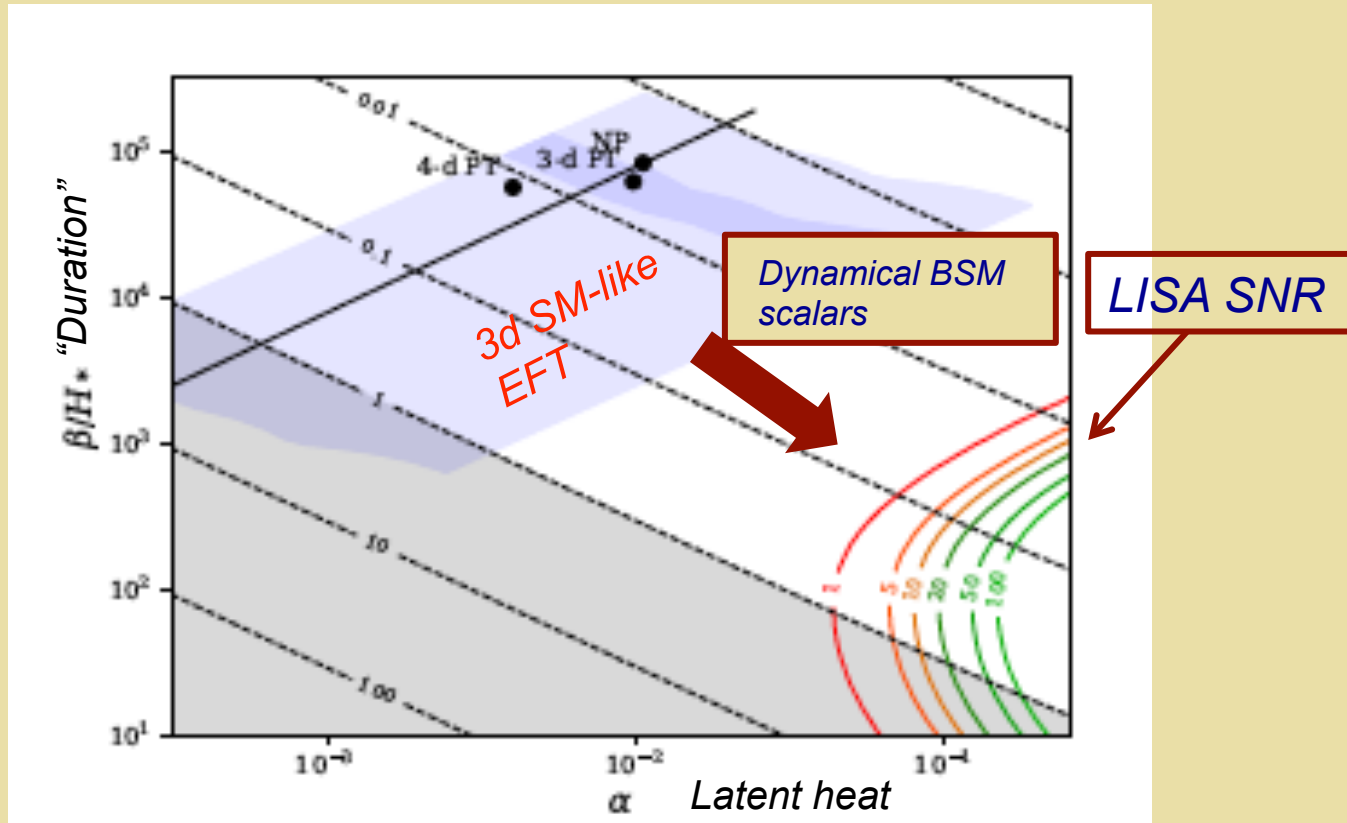
Thanks: D. Weir

Heavy Real Singlet: EWPT & GW



- One-step
- Non-perturbative

Heavy Real Singlet: EWPT & GW



- One-step
- Non-perturbative