

Monte Carlo generators and parton showers

– status and trends –

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GEFÖRDERT VOM



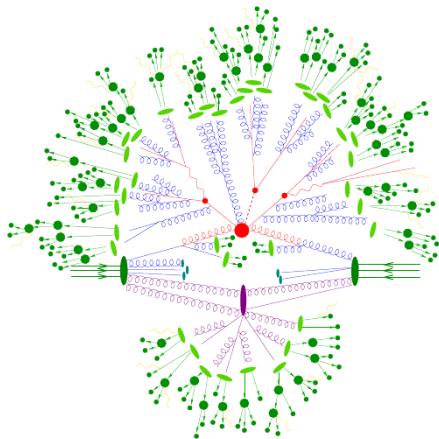
Bundesministerium
für Bildung
und Forschung

Stochastic simulation of fully exclusive collision events

[Buckley *et al.* Phys. Rept. 504 (2011) 145]

↪ factorize short- & long range physics

- perturbative phases
 - **Hard interaction**
exact matrix elements $|\mathcal{M}|^2$
LO, NLO, NNLO – QCD, NLO – EW
 - **Radiativ corrections**
parton showers in the initial and final state
resummation of soft-collinear logs: LL, NLL
- non-perturbative phases
 - **Hadronization**
parton-hadron transition
 - **Hadron Decays**
phase space or effective theories
 - **Underlying Event**
beyond factorization: modelling



- general purpose generators: PYTHIA, HERWIG, SHERPA
- dedicated to matching/merging: POWHEGBOX, MADGRAPH5-AMC@NLO

PYTHIA (latest release 8.240)

- p_T ordered (dipole inspired) parton shower
- automatic shower variations [Mrenna, Skands]
- string fragmentation model
- sophisticated underlying event, non-perturbative models
- VINCIA and DIRE supported as plugins

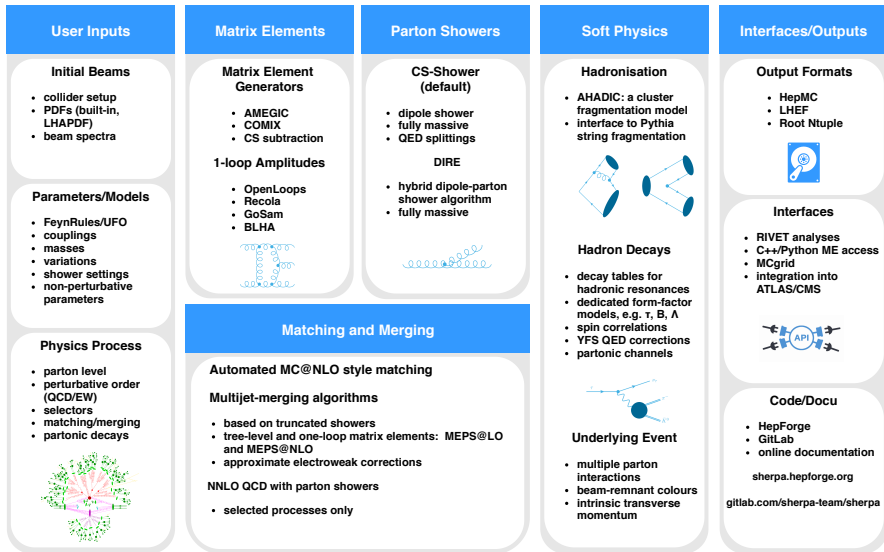


HERWIG (latest release 7.1.5)

- angular-ordered and CS dipole shower
- interfaces to ME generators
- on-the-fly uncertainty variations [Bellm et al.]
- cluster hadronization model
- generic matching/merging implementations
- underlying event & soft interactions



The SHERPA 2.2 event generator framework

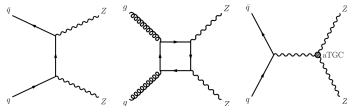


Precision Pheno: $ZZ \rightarrow ll\nu\nu$ production

Signals and backgrounds for SM measurements and BSM searches

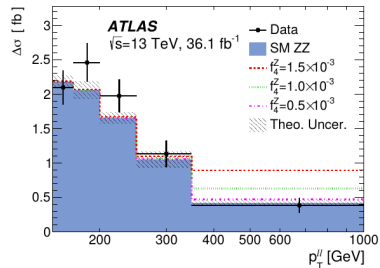
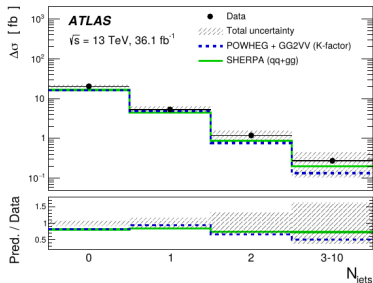
[Aaboud et al.: arXiv:1905.07163 [hep-ex]]

- direct & loop-induced channels
- sensitivity to aTGC



↪ uncertainty estimates needed

Process	Generator	Simulation accuracy	Cross-section accuracy
$qqZZ$	POWHEG-Box v2 + Pythia8.186	NLO QCD	NNLO QCD + NLO EW
	SHERPA2.2.2	NLO QCD 0-1p, LO QCD 2-3p	
$ggZZ$	gg2vv3.1.6 + Pythia8.186	LO QCD	NLO QCD
	SHERPA2.1.1	LO QCD 0-1p	
$qqZZ$ (aTGCs)	SHERPA2.1.1	NLO QCD 0-1p, LO QCD 2-3p	
WZ	POWHEG-Box v2 + Pythia8.186	NLO QCD	
	POWHEG-Box v2 + Herwig++		
WW	POWHEG-Box v2 + Pythia8.186	NLO QCD	
$qqZZ \rightarrow 4l$	POWHEG-Box v2 + Pythia8.186	NLO QCD	NNLO QCD + NLO EW
$ggZZ \rightarrow 4l$	gg2vv3.1.6 + Pythia8.186	LO QCD	NLO QCD
$Z + \text{jets}$	SHERPA2.2.1	NLO QCD 0-2p, LO QCD 3-5p	NNLO QCD
$i\bar{i}$	POWHEG-Box v2 + Pythia6.428	NLO QCD	NNLO QCD
W_i	POWHEG-Box v2 + Pythia6.428	NLO QCD	NNLO QCD
VVV	SHERPA2.1.1	NLO QCD	
$i\nu$	MadGraph5_AMC@NLO + Pythia8.186	LO QCD	NLO QCD



Precision Pheno: α_s extractions from $e^+e^- \rightarrow \text{hadrons}$

α_s fits affected by non-perturbative corrections

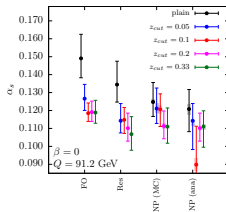
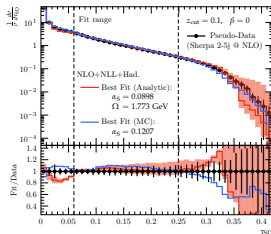
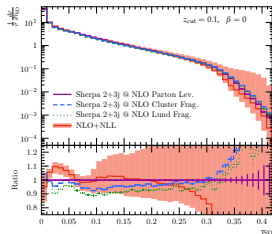
- resummed predictions with hadronization corrections from Monte Carlo
- uncertainty estimate via different generators/fragmentation models
↪ pitfall, PS lacks higher-order terms

- Jet-rates @ NNLO+NNLL [Verbytskyi et al.: arXiv:1902.08158 [hep-ph]]

$$\alpha_s(M_Z) = 0.11881 \pm 0.00063(\text{exp.}) \pm 0.00101(\text{hadr.}) \pm 0.00045(\text{ren.}) \pm 0.00034(\text{res.})$$

- Soft-drop thrust @ NLO+NLL [Marzani et al.: arXiv:1906.XXYY [hep-ph]]

- consider thrust shape with soft-drop grooming [Baron et al.]
- features reduced hadronization corrections
↪ uncertainty estimated from cluster model vs. Lund string



Electroweak Physics

- automation of NLO EW corrections [Frederix et al.; Schönherr et al.]
- approximate NLO EW in MEPS@NLO simulations [Kallweit et al.]

QCD Shower Improvements

- new shower-development platforms: DEDUCTOR [Nagy, Soper], DIRE [Höche, Prestel], HEJ [Andersen et al.], VINCIA [Skands et al.]
- shower logarithmic accuracy [Dreyer et al.; Richardson et al.; Reichelt et al.]
- spin correlations [Richardson et al.]
- resonance-aware subtraction/matching [Ježo, Nason; Liebschner et al.]
- beyond leading color
 - $N_C = 3$ corrections for real emissions [Plätzer et al.; Isaacson, Prestel]
 - evolution beyond LC+ with DEDUCTOR [Nagy, Soper]
 - amplitude-based evolution [Forshaw et al.]
 - perturbative color reconnection [Bellm; Gieseke et al.]
- higher-order corrections [Dulat et al.]

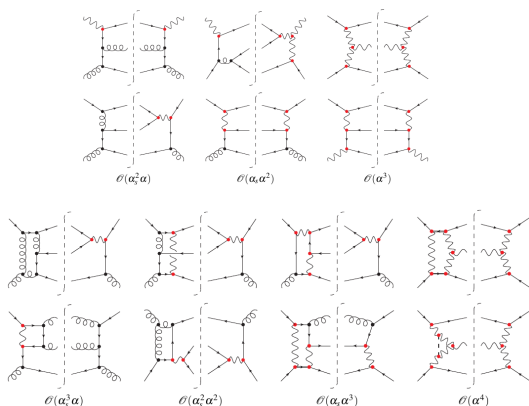
spin-offs

- frameworks for automated resummation [Becher et al.; Reichelt et al.]

Electroweak Corrections

parametrically $\alpha_s^n \alpha \approx \alpha_s^{n+2}$, Sudakov enhancements

↪ photonic initial states, EW Born & Loop corrections, QED reals



Full NLO corrections to hadronic 3-jet production

[Reyer, Schönherr, S.: Eur. Phys. J. C **79** (2019) no.4, 321]

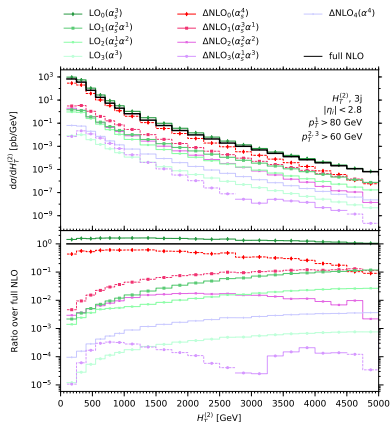
- QCD & QED dipole subtraction [Schönherr]
- virtuals from RECOLA [Actis et al.]

$$\sigma_{nj} = \sum_{i=0}^n \sigma_{nj}^{\text{LO}_i} + \sum_{i=0}^{n+1} \sigma_{nj}^{\Delta\text{NLO}_i}$$

$$\mathcal{O}(\sigma_{nj}^{\text{LO}_i}) = \alpha_s^{n-i} \alpha^i$$

$$\mathcal{O}(\sigma_{nj}^{\Delta\text{NLO}_i}) = \alpha_s^{n+1-i} \alpha^i$$

- ↪ subleading EW tree-level and one-loop contributions sizeable
- ↪ challenge for matching & merging



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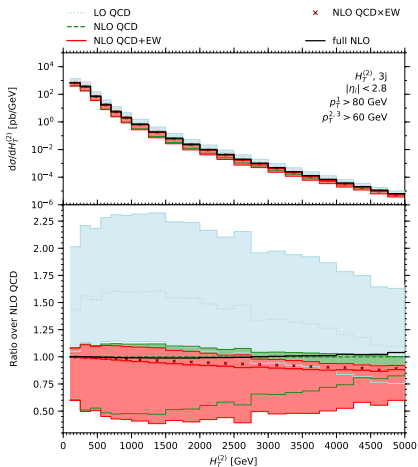
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Shower improvements

$$|\mathcal{M}_{n+1}|^2 \approx \sum_{i,j,k \neq i,j} \frac{1}{2p_i \cdot p_j} \langle \mathcal{M}_n | \frac{\mathbf{T}_{ij} \cdot \mathbf{T}_k}{\mathbf{T}_{ij}^2} \mathbf{V}_{ij,k} | \mathcal{M}_n \rangle$$

conventional shower: average spins, $N_C \rightarrow \infty$

↔ preserve spin correlations

↔ $N_C = 3$ corrections

↔ higher-order splitting functions

Spin-density formalism in HERWIG showers (angular and dipole)

[Richardson, Webster: arXiv:1807.01955 [hep-ph]]

helicity amplitudes for branchings

- (i) azimuthal correlations in parton splittings

$$\frac{1}{2\pi} (1 + AB \cos 2\Delta\phi)$$

- (ii) correlations between shower, hard process and decays

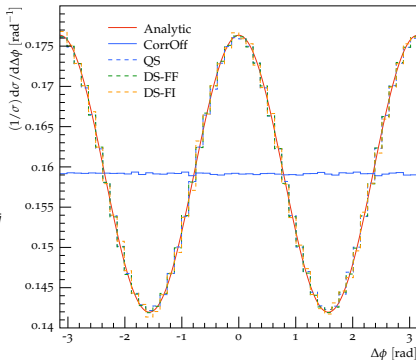
$$\rho_{g_1}^{\lambda_{g_1} \lambda'_{g_1}} \propto \mathcal{M}_{h^0 \rightarrow gg}^{\lambda_{g_1} \lambda_{g_2}} \mathcal{M}_{h^0 \rightarrow gg}^* \lambda'_{g_1} \lambda_{g_2}$$

$$f(\phi) \propto \rho_{g_1}^{\lambda_{g_1} \lambda'_{g_1}} \mathcal{M}_{g \rightarrow q\bar{q}}^{\lambda_{g_1} \lambda_q \lambda_{\bar{q}}} \mathcal{M}_{g \rightarrow q\bar{q}}^* \lambda'_{g_1} \lambda_q \lambda_{\bar{q}}$$

→ improved description of spin-correlated decays

→ available from HERWIG 7.2

FS $q \rightarrow qg_1$ with $g_1 \rightarrow gg$



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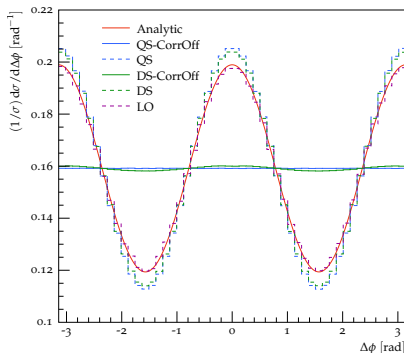
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$$h^0 \xrightarrow{\text{ME}} g_1 g_2 \xrightarrow{\text{PS}} q\bar{q} q' \bar{q}'$$



Pushing Frontiers: $N_C = 3$ corrections

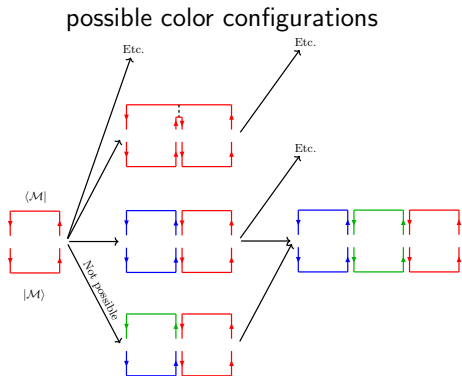
Stochastically sample $N_C = 3$ configurations

[Isaacson, Prestel: Phys. Rev. D **99** (2019) no.1, 014021]

full-color (FC) shower based on DIRE

- trace color assignments in *color flow basis*
- sample flows for emissions above $t_{\text{FC}}^{\text{cut}} > t_0$ according to
$$\langle \mathcal{M}' | t_k^\alpha t_{ij}^\beta | \mathcal{M} \rangle$$
- LC shower below $t_{\text{FC}}^{\text{cut}} > t_0$
- keep track of large- N_C flow for LC shower and hadronization

- ↪ possibly large weight fluctuations
- ↪ lack of kinematic corrections
- ↪ no virtual color rearrangements



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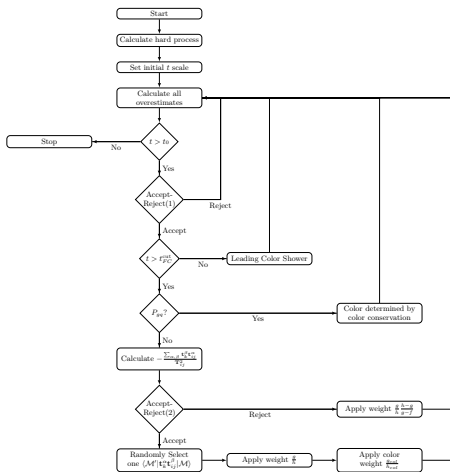
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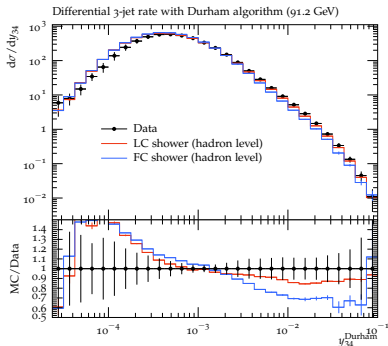
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Color matrix element corrections

[Plätzer, Sjödalh, Thorén: JHEP 1811 (2018) 009]

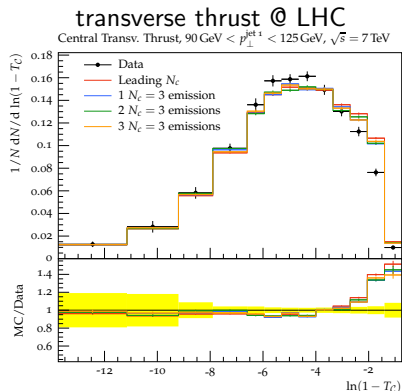
color corrections for first few emissions in HERWIG dipole shower

- use *trace basis* color representation
- color correction weight

$$\omega_{ij\bar{k}}^n = \frac{-1}{T_{ij}^2} \frac{\langle \mathcal{M}_n | T_{ij}^- \cdot T_{\bar{k}}^- | \mathcal{M}_n \rangle}{|\mathcal{M}_n|^2}$$

- evolve full color structure, LC shower beyond N_{\max} emissions
- available for final- and initial state

- ↪ limited to first few emissions
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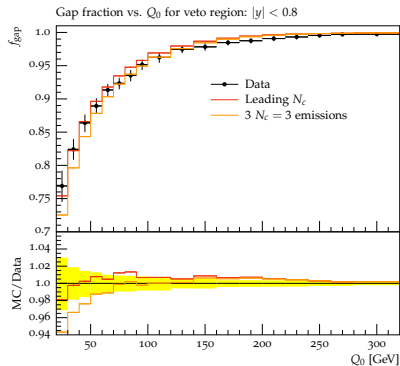
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gap fraction in $t\bar{t}$ events @ LHC



Pushing Frontiers: towards NLO precision

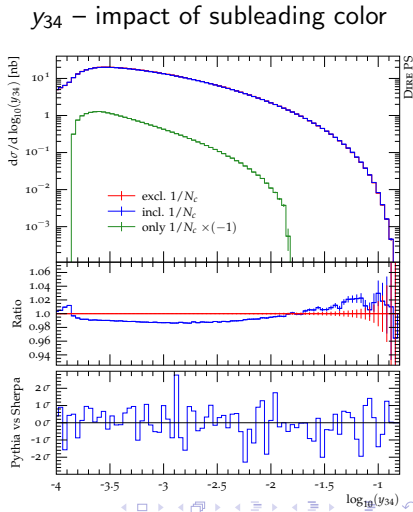
Fully differential two-loop soft corrections in dipole showers

[Dulat, Höche, Prestel: Phys. Rev. D **98** (2018) no.7, 074013]

correct DIRE emission pattern for NLO soft-gluon radiation

- differential in one-emission phase space
- correction weights for
 - phase-space coverage
 - spin correlations
 - subleading color
- final- and initial state emissions
- two independent implementations
PYTHIA and SHERPA

- ↪ good agreement with CMW
- ↪ meaningful uncertainty estimate



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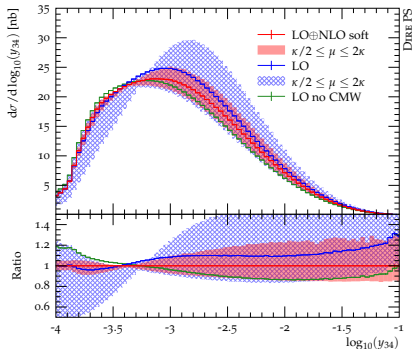
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y_{34} – full distribution



Conclusions

- NLO QCD matching/merging prescriptions routinely used for LHC pheno
- automation NLO EW achieved, more and more public tools emerging
- focus moving towards improvements of shower algorithms
 - ↪ sophisticated reweighting techniques for applying corrections (SVA)
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Looking forward to a productive workshop!