

# LHCb Status Report

Blake D. Leverington,  
on behalf of the LHCb Collaboration

138th LHCC Open Session, CERN  
June 5th, 2019



**UNIVERSITÄT  
HEIDELBERG**  
ZUKUNFT  
SEIT 1386

# Outline

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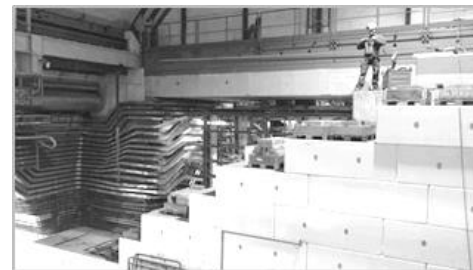


Upgrade and Operations

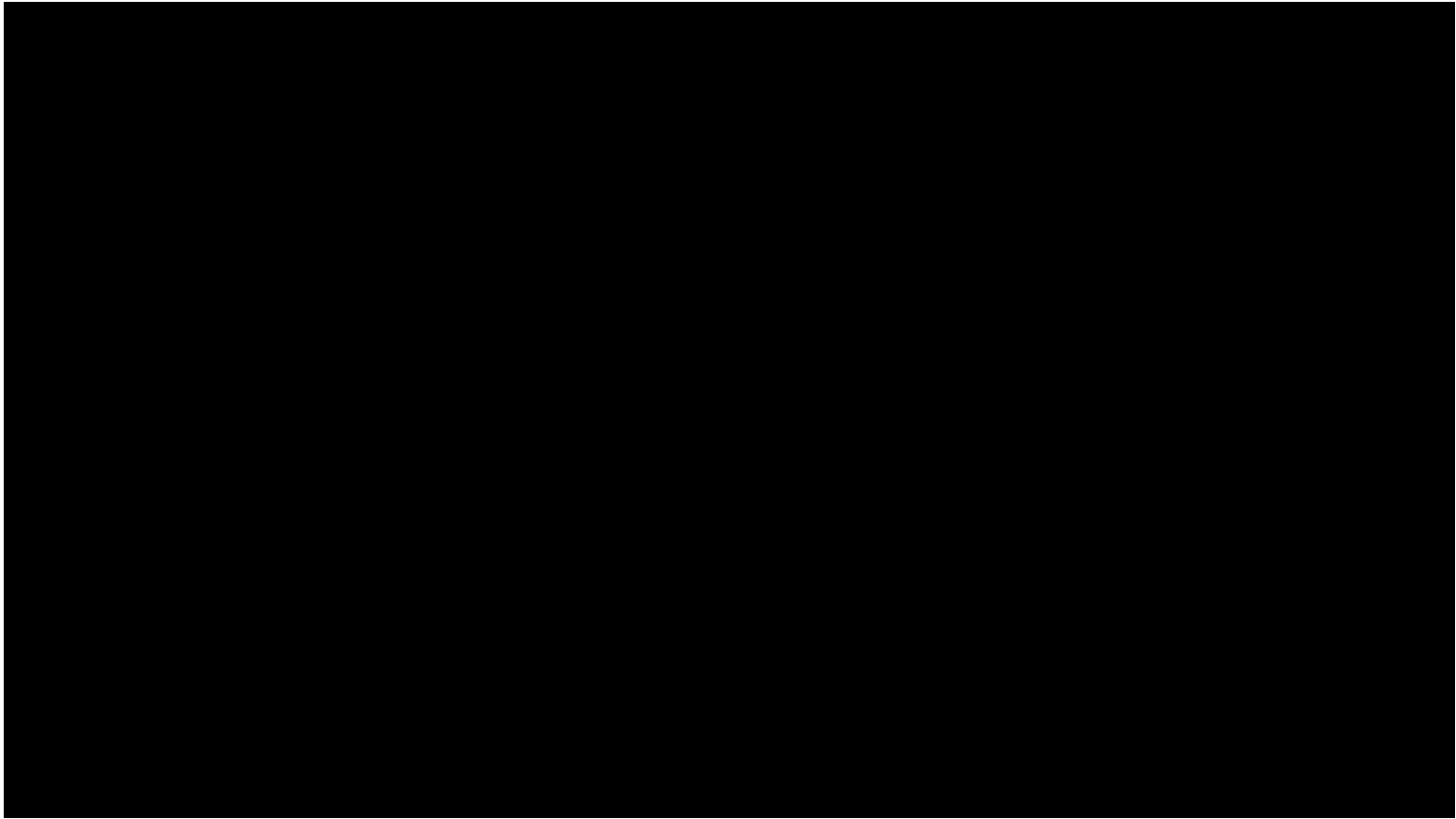
Physics Analysis and Publications

# Disassembly & Installation at LHCb

- Velo, RICH 1, TT, IT, OT, M1, Calorimeter Lead, PS/SPD are out
  - all obsolete services are removed
- dismantling is well on schedule, and done safely
- installation of upgrade services:
  - Modules 1-4 of 6 for Event Filter farm in place
  - Long distance fibres being installed with very good progress
  - Installation of new cooling plants advancing well
  - First new copper cables in place
  - Sub-systems will start to enter the experimental cavern in June

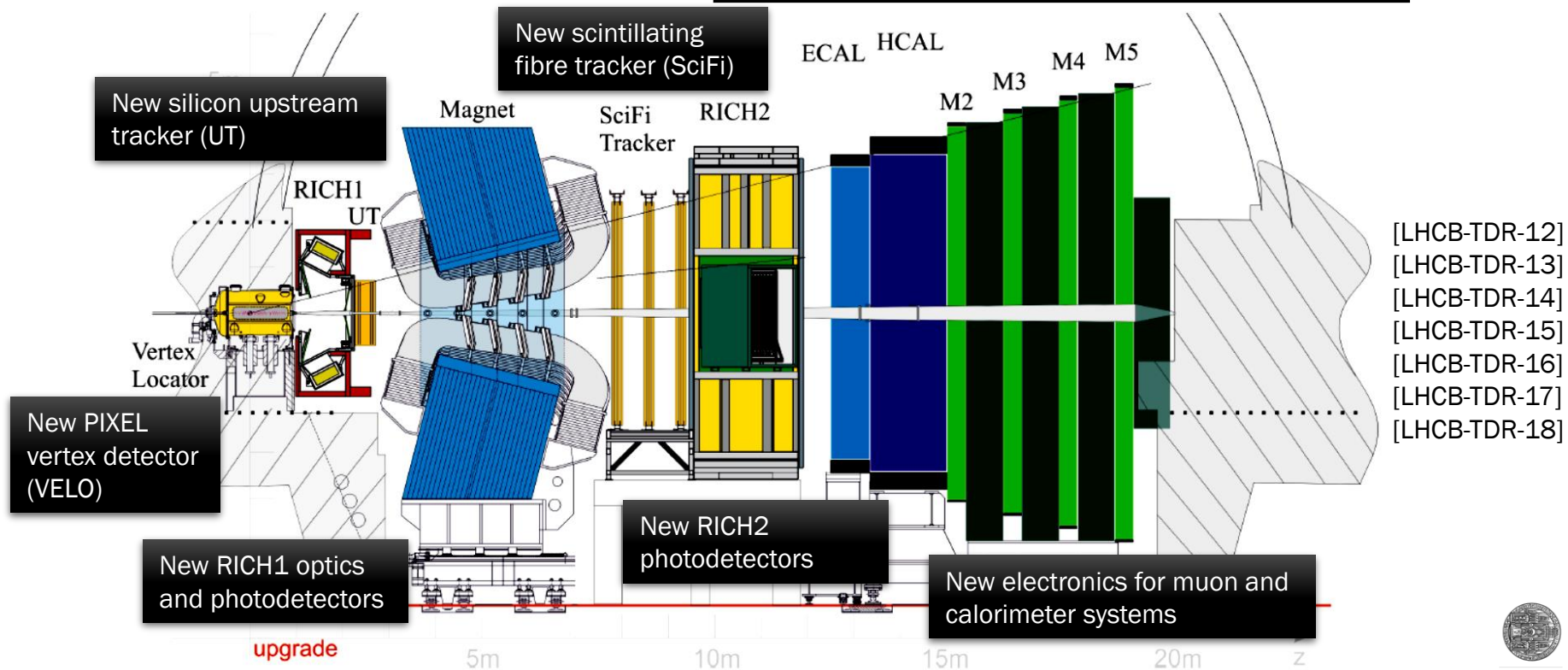


- Watch our weekly videos!  
<https://www.youtube.com/watch?v=CKLu1xewv7I>



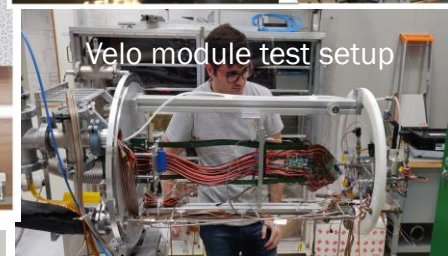
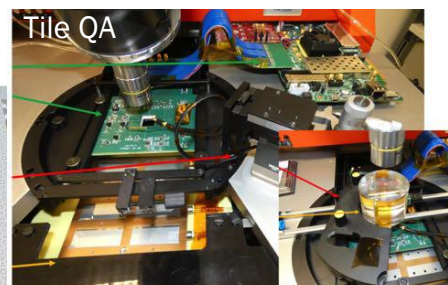
# LHCb Upgrade

- $50 \text{ fb}^{-1}$ ,  $2 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- All front-end electronics read out at 40 MHz
- 30 MHz avg. input to a full software trigger



# VELO

- New hybrid pixel detector for LHCb! Evaporative CO<sub>2</sub> cooling in silicon microchannels.
- Project progressing very well, although the schedule is tight given the complexity.
- VeloPix ASIC bump bonding to silicon pixel sensors is complete.
- Module construction:
  - Several pre-production modules available;
  - Production site readiness review next week.
- RF boxes:
  - First installation pair complete; machined to 250 um thin, leak tight.
  - Second pair almost complete (in final weeks of machining).
- High speed copper links 50% manufactured.
- Other components (vacuum feedthrough boards, electronics...) on schedule.
- Large scale mechanics (base, hood, isolation vacuum volumes, piping and valve assembly) progressing well. First half currently being prepared

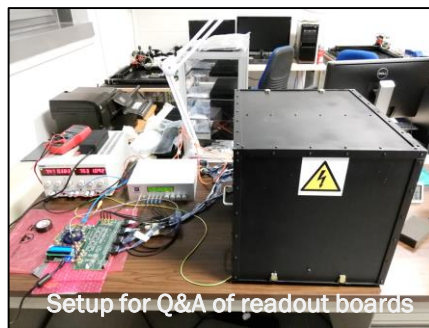


# RICH

- Dismantling of RICH 1 complete, HPD removal from RICH 2 to begin soon
- Upgrade RICH 1 installation about to begin, mechanics under way
- Spherical mirrors almost completed, flat mirror tender completed
- MA-PMT columns for RICH 1 & 2:  $22+24 = 46$  columns (+spares)
  - all 3500 MaPMTs tested, CLARO ASIC: all received (100k) 100% pass rate
  - Digital readout board (PDMDB): production of PCBs completed, first complete boards being received
  - received most BaseBoard, FEBs and BackBoard batches, all undergoing QA
- Commissioning Lab (ComLab@CERN) ready to integrate columns



PDMDB

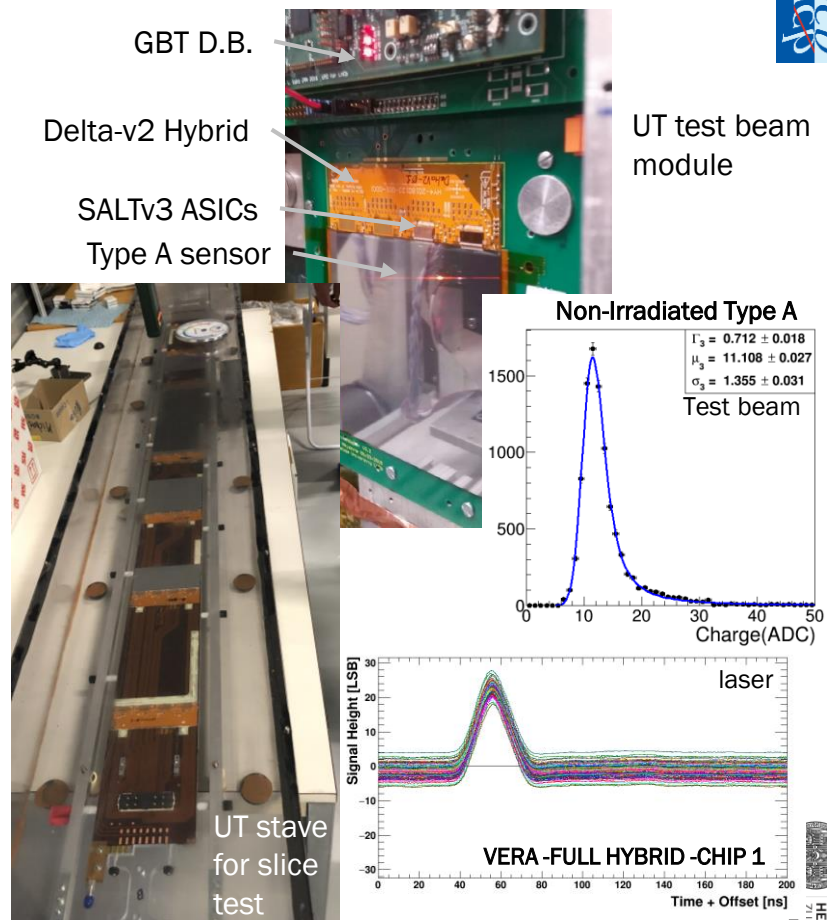


Setup for Q&A of readout boards



An assembled MaPMT column

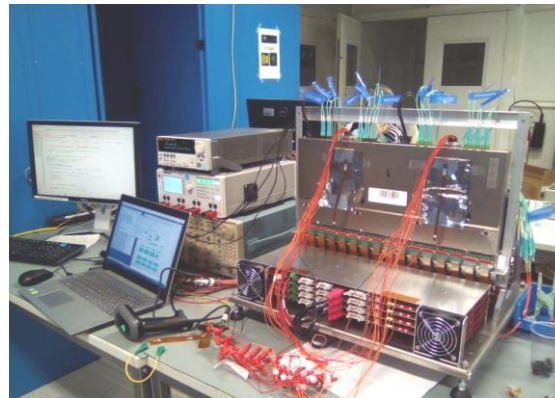
- SALT v3 asic received and tested, v3.5 sent for prod.
  - Issues seen in the previous version largely fixed
  - Test beam at Fermilab in March. Good results.
- Slice test setup in progress at Point 8
  - instrumented stave with realistic power, cooling and proto mechanics.
- Now to finalize the hybrid and start production
  - Hybrid production June 2019, QA and tools ready
- Sensors:
  - received all A-type, pre-series of B,C,D, prod. in Oct. 2019.
- Readout electronics: production started
  - Flex cables pre-series available, under test
- Bare staves: production finished
- Integration infrastructure at progressing full speed





# SciFi Tracker

- Excellent progress! First scintillating fibre detector for LHCb.
- C-Frame 1 (of 12) nearly complete
  - already equipped with modules. Electronics in Wk 25
- All 5500 SiPM arrays delivered and tested
- Electronics:
  - 40% of PACIFIC boards prod. and tested (100% of ASICS)
  - 60% of Cluster boards prod. and tested
  - Master Boards
    - 50 boards in pre-series delivered and tested
    - 500 boards to be delivered in batches soon
- SiPM Cold-box to Fibre Module assembly on schedule
  - All QA test results look good
- Readout and control of the prototype C-Frame (4 ROB) with PCIe40/WinCC (LHCb Upgrade read-out)
- Schedule is tight but experience will help us optimize the commissioning .



Front-end tester at Point 8

C-Frame 1 with fibre modules

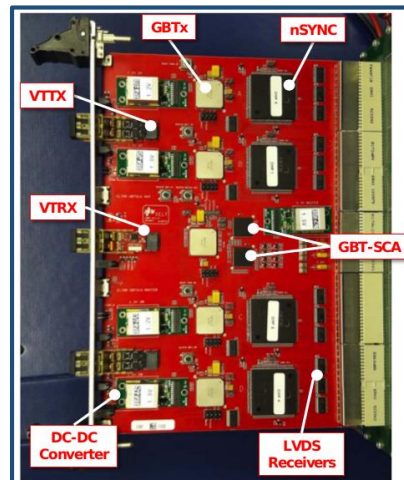


# Calorimeter and Muon

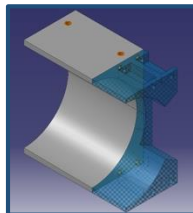
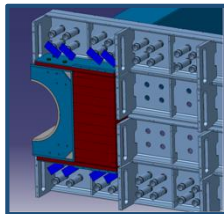
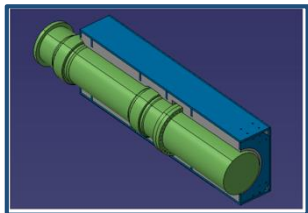
- To be produced: electronics boards + shielding plugs
  - All electronics in production and testing
    - **MUON: nSYNCs (prod. & tested), nODE (pre-prod.):** 40MHz readout, each nODE equipped with 4 nSYNCs, **nSB, nPDM (pre-prod.):** system configuration and pulsing, **nBP (pre-prod.):** custom Back Plane for nPDM/nSB crates
  - Full production finished in November
- New shielding plug, (3 parts, design finalized)
  - order placed last December, parts expected in the coming month
- Upgrade activities are proceeding well



278 CALO FEB needed  
+21 Control Boards  
+144 HV/Calib/Moni



Muon nODE  
~~1120 needed~~  
+8 nPDM



Details of the new Muon shielding plugs

# Online

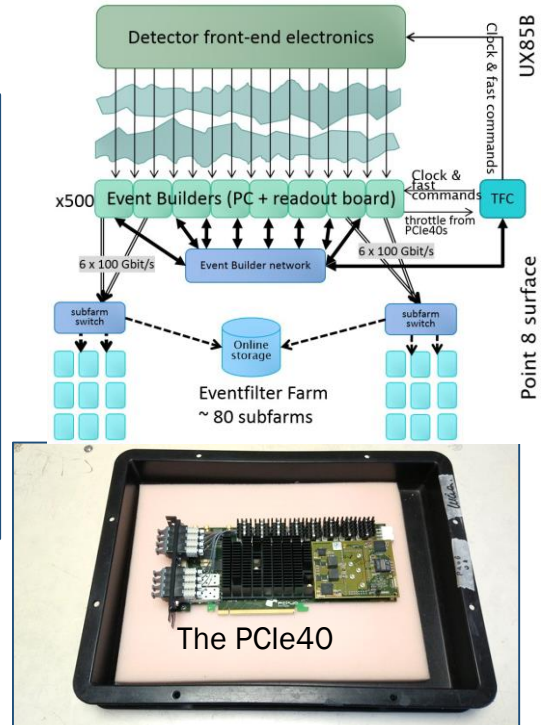
- Containers for Event Filter Farm and Event Builder:
  - First 4 modules installed, 2 more in Nov. 2019
  - 40% of the long-dist. optical fibres from detector to the EFF installed
- Event Builder:
  - simulation of traffic is now working for 500 nodes and gives confidence in scalability of system.
  - Review of Upgrade Event Builder on June 6
- Vertical Slice Test will allow checking simulation results at a scale of 20% of the final system.
- PCIe40 (LHCb readout) production in full swing.
  - First production batch of ~40 just delivered



Installation of one of the HLT farm modules



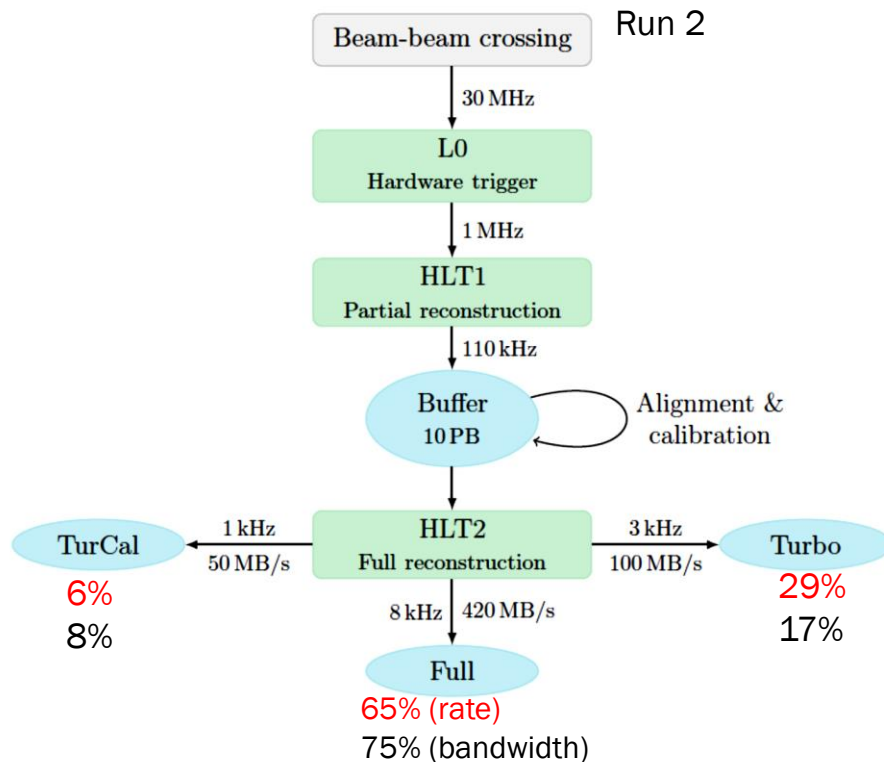
Event builder: Vertical slice setup already cabled with fibres and operational



# Real-time Analysis

- Quality reconstruction in the final trigger stage (HLT2), it is no longer necessary to run another reconstruction offline
  - LHCB-TDR-018
  - [JINST 14 \(2019\) P04006](#)
- Turbo model = exclusive selections, no additional objects
- Complete persistence = Turbo model for inclusive triggers,
- Selective persistence
  - explicit specification.
  - Event size reduction without sacrificing information needed offline
  - key for the migration to RTA model for Run3

[Run2: JINST 14 P04013](#)  
[Comput. Phys. Commun. 208 35-42](#)

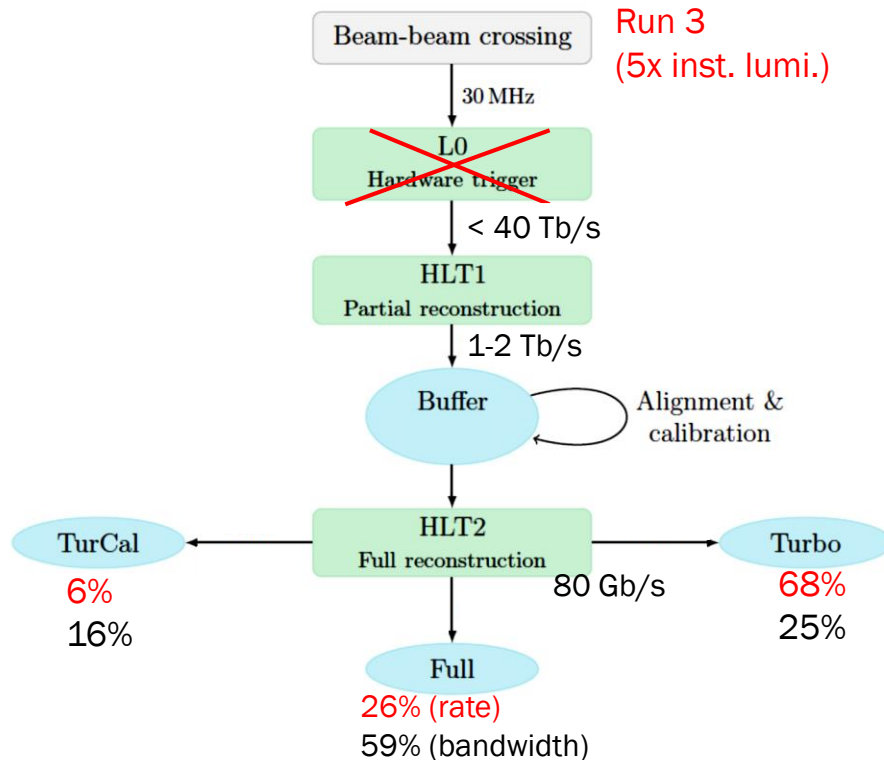


Persistence method	Average event size (kB)
Turbo	7
Selective persistence	16
Complete persistence	48
Raw event	69

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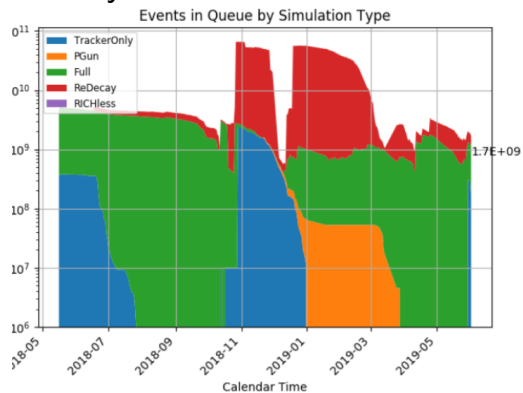


Persistence method	Average event size (kB)
Turbo	7 few
Selective persistence	16 tens
Complete persistence	48 ↓
Raw event	69 200-250

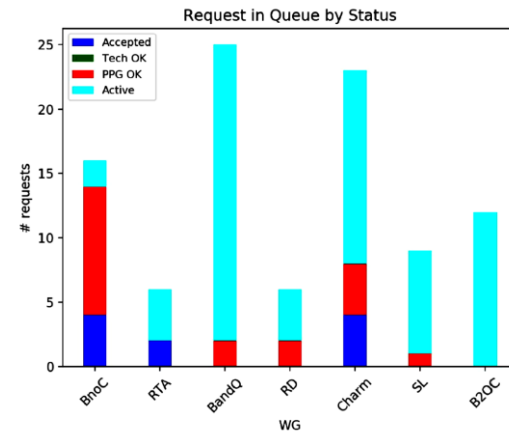
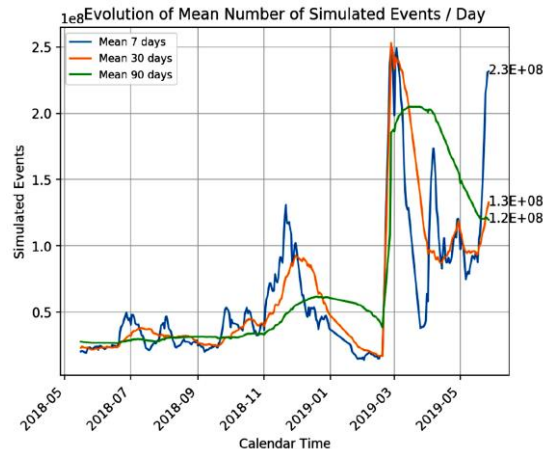
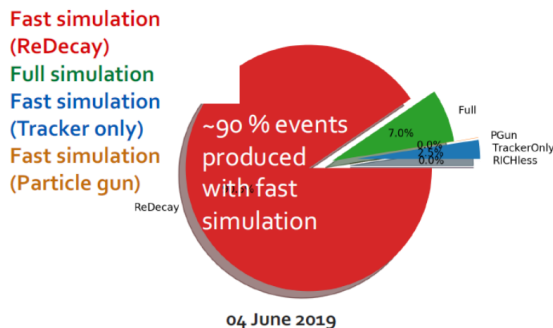


# Simulation

- Increasing use of fast MC techniques
- ReDecay: is one of most popular techniques [Eur. Phys. J. C (2018) 78: 1009]
- only the few participating particles in the signal decay under study are of interest
- Re-decay the signal N times but reuse the rest of the event from previously simulated events = an order of magnitude increase in speed
- Be careful: the resulting events are not statistically independent anymore



Events in last 365 days

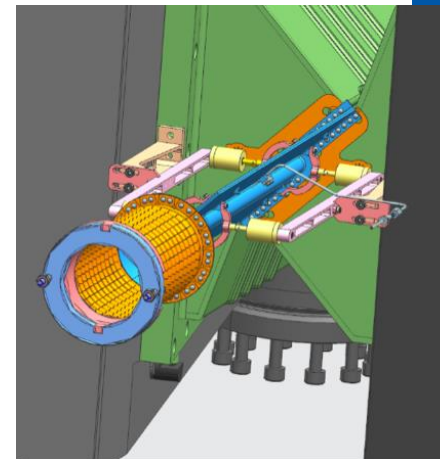


# SMOG 2

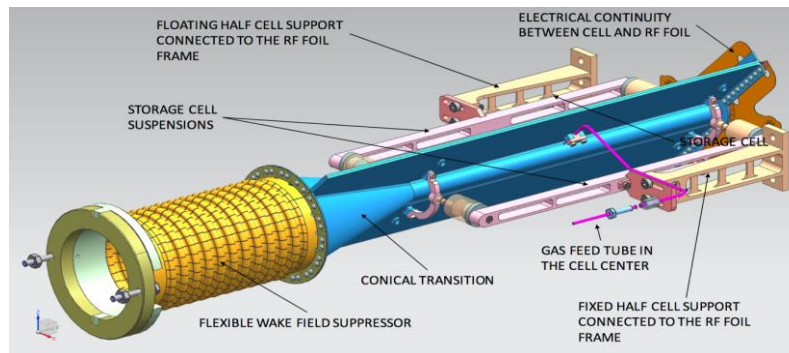
- LHCb has a unique fixed target physics programme at LHC [LHCb-PUB-2018-015]
  - Heavy ions
  - Cosmic ray physics
  - Useful for early measurements such as p/He cross-section
- New SMOG will increase by up to two orders of magnitude the effective target areal density [CERN-LHCC-2019-005 ; LHCb-TDR-020]
- significant increase of the luminosity for fixed-target collisions.
- Multiple gas capabilities being studied
  - Impact on accelerator



Dragon illustration in 13th century manuscript - Wikimedia Commons

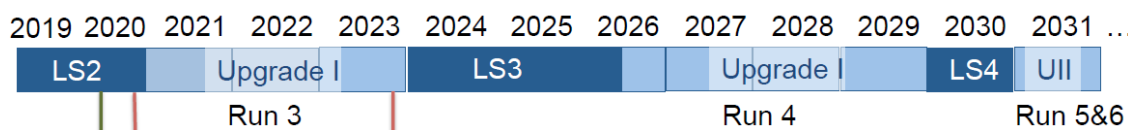


SMOG connected to the VELO RF boxes



Technical drawing of the gas storage cell to be installed inside the VELO

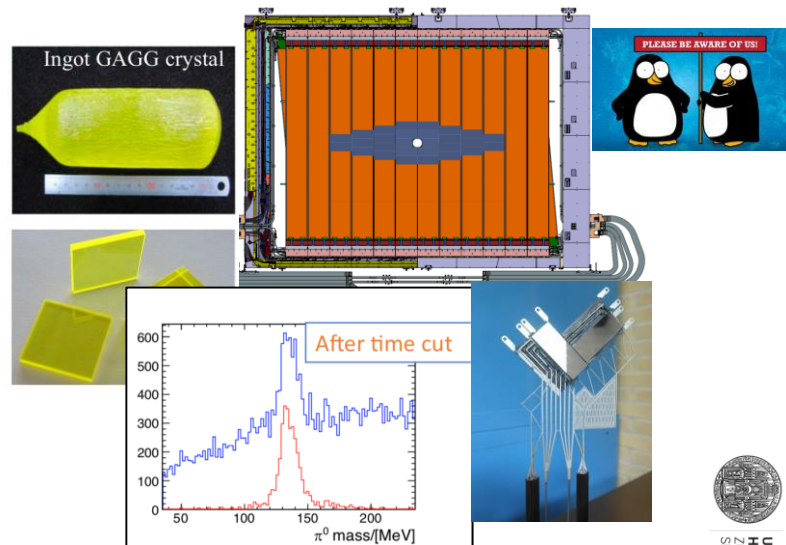
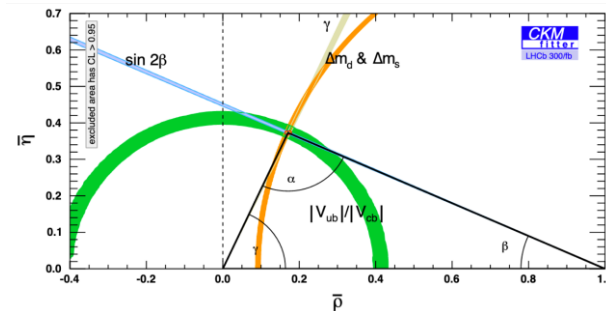
# Upgrade II



- The case for the upgrade was very well received at the ESPP meeting in Granada.
- Physics Case:
  - Collect  $250 \text{ fb}^{-1}$  more ( $2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ )
  - CERN-LHCC-2018-027 ([arXiv:1808.08865](https://arxiv.org/abs/1808.08865))
  - Order of magnitude increase in precision over current results
  - Rare Decays, CP violation, Heavy Ions

## Detector Ideas Summary:

- Timing needed in the VELO, and PID (TORCH)
- More granular rad-hard calorimeter with timing
- Chimera tracking detector from silicon/DMAPS (inner) and scifi (outer) aka the Mighty Tracker
- Non-cpu options for tracking



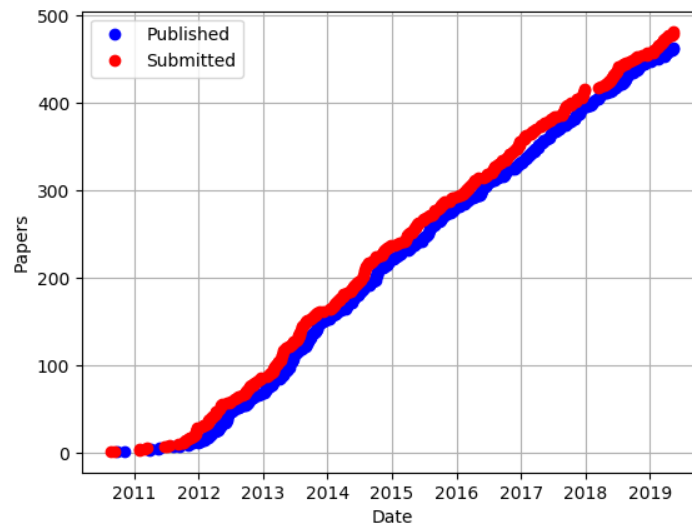
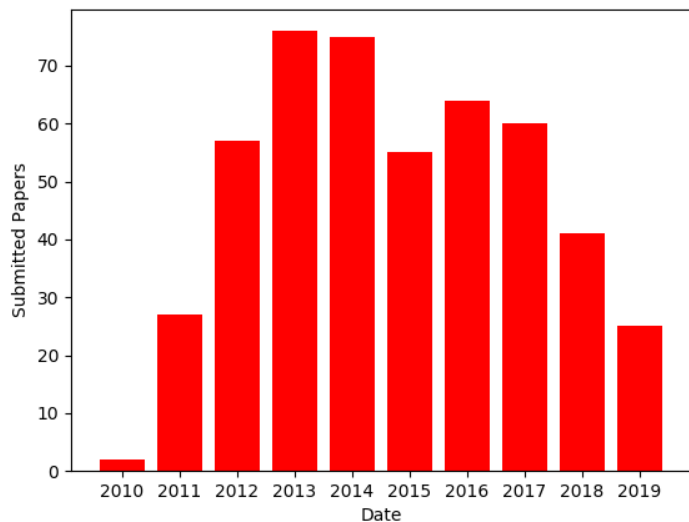


# Physics Analyses and Publications

(since the last LHCC)

# Publications

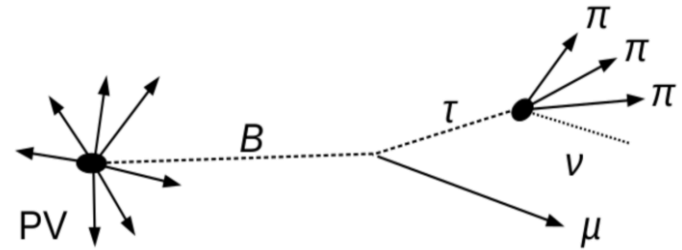
- 482 total publications
- 25 papers submitted to journals in 2019
  - 16 since last LHCC
- 9 being processed in the Editorial Board
- About 20 more in preparation



- Submitted
- PAPER-2019-004 Amplitude analysis of the  $B_{(s)}^0 \rightarrow K^{*0} \bar{K}^{*0}$  decay and measurement of its branching fraction relative to the  $B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$  decay
- PAPER-2019-016 Search for the lepton-flavour-violating decays  $B_s^0 \rightarrow \tau^\pm \mu^\mp$  and  $B^0 \rightarrow \tau^\pm \mu^\mp$**
- PAPER-2019-015 Measurement of the mixing-induced and  $CP$ -violating observables of  $B_s^0 \rightarrow \phi \gamma$  decays
- PAPER-2019-011 A search for  $\Xi_{cc}^{++} \rightarrow D^+ p K^- \pi^+$  decays
- PAPER-2019-012 Measurement of charged hadron production in  $Z$ -tagged jets in proton-proton collisions at  $\sqrt{s} = 8 \text{ TeV}$
- PAPER-2019-010 First observation of the radiative decay  $\Lambda_b^0 \rightarrow \Lambda \gamma$
- PAPER-2019-014 Observation of a narrow pentaquark state,  $P_c^+(4312)$ , and of two-peak structure of the  $P_c^+(4450)$**
- PAPER-2019-007 Observation of an excited  $B_c^+$  state
- PAPER-2019-009 Search for lepton-universality violation in  $B^+ \rightarrow K^+ \ell^+ \ell^-$  decays**
- PAPER-2019-006 Observation of  $CP$ -violation in charm decays**
- PAPER-2019-005 Near-threshold  $D\bar{D}$  spectroscopy and observation of a new charmonium state
- PAPER-2018-044 Measurements of  $CP$  asymmetries in charmless four-body  $\Lambda_b^0$  and  $\Xi_b^0$  decays
- PAPER-2019-003 Measurement of the  $CP$ -violating phase  $\phi_s$  from  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  decays in 13 TeV pp collisions**
- PAPER-2019-001 Measurement of the mass difference between neutral charm-meson eigenstates
- PAPER-2019-002 Search for  $CP$  violation in  $D_s^+ \rightarrow K_S^0 \pi^+$ ,  $D_s^+ \rightarrow K_S^0 K^+$  and  $D_s^+ \rightarrow \phi \pi^+$  decays
- PAPER-2018-051 Amplitude analysis of  $B^\pm \rightarrow \pi^\pm K^+ K^-$  decays
- Preliminary
- PAPER-2019-013 Updated measurement of time-dependent  $CP$ -violating observables in  $B_s^0 \rightarrow J/\psi K^+ K^-$  decays**
- PAPER-2019-020 Observation of the of the fragmentation-fraction ratio  $f_s/f_u$  variation with  $B$ -meson kinematics
- PAPER-2019-021 Measurement of  $CP$  observables in the process  $B^0 \rightarrow DK^{*0}$  with two- and four-body  $D$  decays
- PAPER-2019-019 Measurement of  $CP$ -violation in the  $B_s^0 \rightarrow \phi \phi$  decay and search for the  $B^0 \rightarrow \phi \phi$  decay**
- PAPER-2019-008 Precision measurement of the  $\Lambda_c^+$ ,  $\Xi_c^0$ , and  $\Xi_c^+$  baryon lifetimes**
- PAPER-2019-017 Amplitude analysis of the  $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  decay
- PAPER-2019-018 Observation of several sources of  $CP$ -violation in  $B^+ \rightarrow \pi^+ \pi^+ \pi^-$  decays
- PAPER-2019-022 Search for the lepton-flavour violating decays  $B^+ \rightarrow K^+ \mu^\pm e^\mp$
- PAPER-2019-021 Measurement of  $CP$  observables in the process  $B^0 \rightarrow DK^{*0}$  with two- and four-body  $D$  decays
- CONF-2019-001 Search for time-dependent  $CP$  violation in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$  decays

# Lepton flavour violating decay $B_{(s)}^0 \rightarrow \tau^\pm \mu^\mp$

- Search for lepton-flavour violating decays  $B_{(s)}^0 \rightarrow \tau^\pm \mu^\mp$
- BR in SM very small:  $\sim 10^{-54}$
- Can be strongly enhanced in NP models: up to  $O(10^{-9} - 10^{-5})$
- Look for three prong  $\tau$  decays



[LHCb-PAPER-2019-016, Run1 3 fb<sup>-1</sup>] [arXiv:1905.06614](https://arxiv.org/abs/1905.06614) Submitted to PRL

Mode	Limit	90% CL	95% CL
$B_s^0 \rightarrow \tau^\pm \mu^\mp$	Observed	$3.4 \times 10^{-5}$	$4.2 \times 10^{-5}$
	Expected	$3.9 \times 10^{-5}$	$4.7 \times 10^{-5}$
$B^0 \rightarrow \tau^\pm \mu^\mp$	Observed	$1.2 \times 10^{-5}$	$1.4 \times 10^{-5}$
	Expected	$1.6 \times 10^{-5}$	$1.9 \times 10^{-5}$

First limits

World Best limits (Factor of 2)

# Lepton universality

[LHCb-PAPER-2019-009 ]

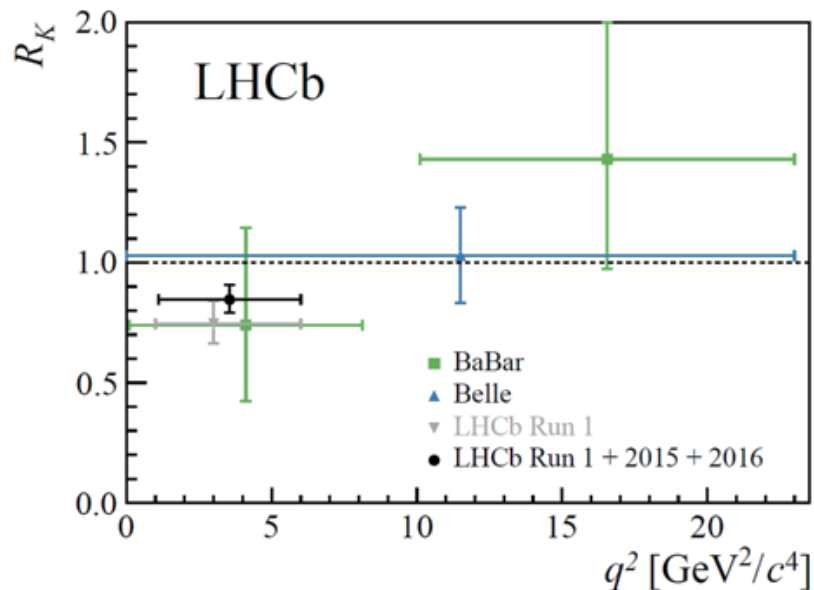
[Phys. Rev. Lett. 122 \(2019\) 191801](#)

[arXiv:1903.09252](#)



$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu\mu)}{\mathcal{B}(B^+ \rightarrow K^+ ee)} \bigg/ \underbrace{\frac{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\mu\mu))}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(ee))}}_{= 1 \text{ (cancels } e/\mu \text{ efficiency differences)}} \\ = 1.014 \pm 0.035 \text{ (stat. + syst.)}$$

- consistent with the SM expectation at the level of  $2.5 \sigma$
- the most precise measurement to date
  - Using integrated luminosity of  $5 \text{ fb}^{-1}$
  - Still  $4 \text{ fb}^{-1}$  in 2017+2018 to analyse
  - Will benefit from the Upgrade data
  - Other observables to investigate still (higher  $q^2$ , other  $B \rightarrow s\ell\ell$ , etc.)

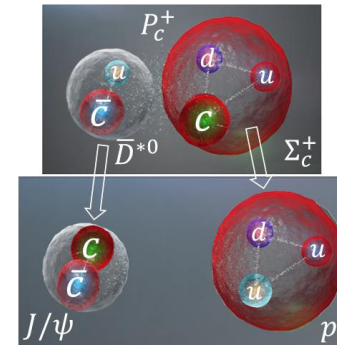
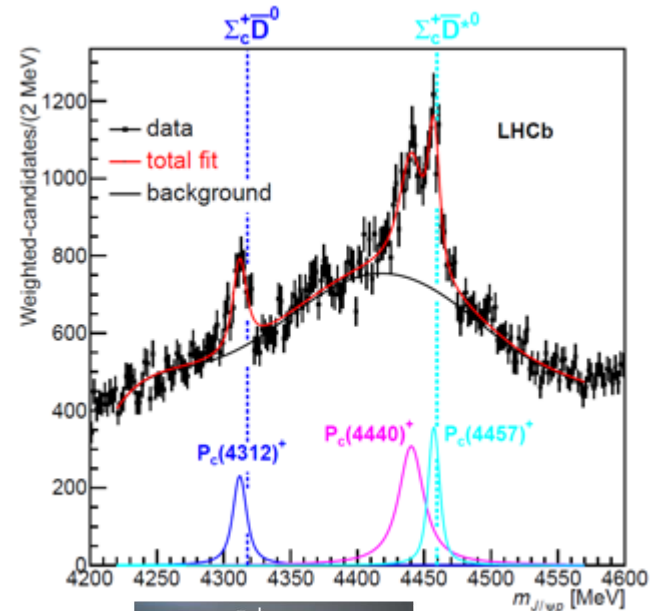


Global fit to 2011 - 2016 data

$$R_K = 0.846 \begin{matrix} +0.060 & +0.016 \\ -0.054 & -0.014 \end{matrix}$$

# Observation of new pentaquarks

- A narrow peak from  $\Lambda_b^0 \rightarrow J/\psi p K^-$  decays is observed near 4312 MeV with a width comparable to the mass resolution
  - Analysis uses full Run 1 and 2 data
  - statistical significance of  $7.3\sigma$
- The structure at 4450 MeV is now resolved into two narrow peaks, at 4440 and 4457 MeV
  - statistical significance of this two-peak interpretation is  $5.4\sigma$
- Indication of a bound state
- Full amplitude analysis required to better determine the nature of the states



[LHCb-PAPER-2019-014,  
Accepted by PRL]  
[arXiv: 1904.03947](https://arxiv.org/abs/1904.03947)

# CP violation in charm

[LHCb-PAPER-2019-006, Accepted by PRL]

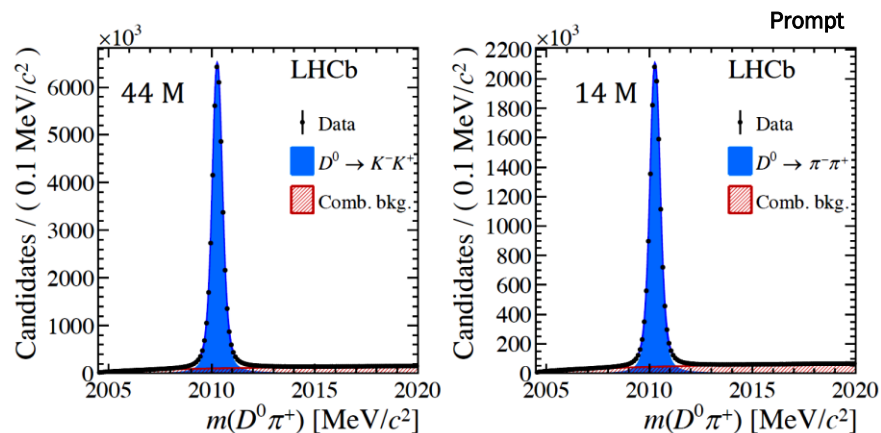
[arXiv:1903.08726](https://arxiv.org/abs/1903.08726)

$$\Delta A_{CP} \equiv A_{CP}(D^0 \rightarrow K^- K^+) - A_{CP}(D^0 \rightarrow \pi^- \pi^+)$$

$$\Delta A_{CP} \simeq \Delta a_{CP}^{dir} \left( 1 + \frac{\overline{\langle t \rangle}}{\tau(D^0)} y_{CP} \right) + \frac{\Delta \langle t \rangle}{\tau(D^0)} \Delta a_{\Gamma}$$

$\sim 0.01$                        $\sim 0.00003$

- $\Delta A_{CP}$  is primarily sensitive to direct CP-violation
  - largely insensitive to systematic uncertainties.
- differs from zero by  $5.3\sigma$ 
  - SM expectations  $10^{-4} - 10^{-3}$
- the first observation of CP violation in charm particle decays
- Reconstruction performed online (Turbo stream)
  - Comput. Phys. Commun. 208 (2016) 35



Run 1 and 2 combined result

$$\Delta A_{CP} = (-1.54 \pm 0.29) \cdot 10^{-3}$$

$$\Delta a_{CP}^{dir} = (-1.56 \pm 0.29) \cdot 10^{-3}$$

# Measurement of CP violation in $B_s^0 \rightarrow J/\psi h^+ h^-$

- New results using  $1.9 \text{ fb}^{-1}$  from 2015 and 2016

- [LHC Seminar by F. Dordei](#)

- 33,500  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  signal decays

- 5D fit: time, 3 angles,  $m_{\pi\pi}$
  - $\phi_s = -57 \pm 60 \pm 11 \text{ mrad}$

- 117,000  $B_s^0 \rightarrow J/\psi K^+ K^-$  signal decays

- Time-dependent angular analysis
  - Most precise single measurement to date
  - $\phi_s = -83 \pm 41 \pm 6 \text{ mrad}$

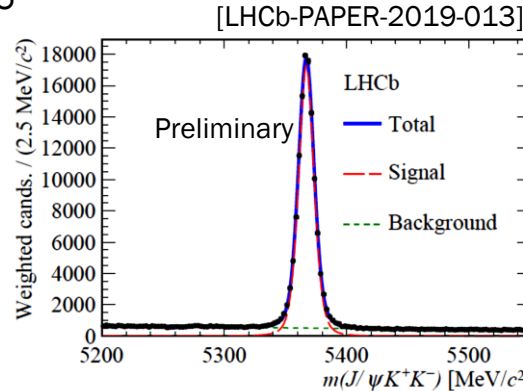
- LHCb average from combined 2011-2016 data analyses

- $\phi_s = -41 \pm 25 \pm 6 \text{ mrad}$
  - $\Delta\Gamma_s = 0.0816 \pm 0.0048 \text{ ps}^{-1}$

- HFLAV [preliminary] average including ATLAS-CONF-2019-009

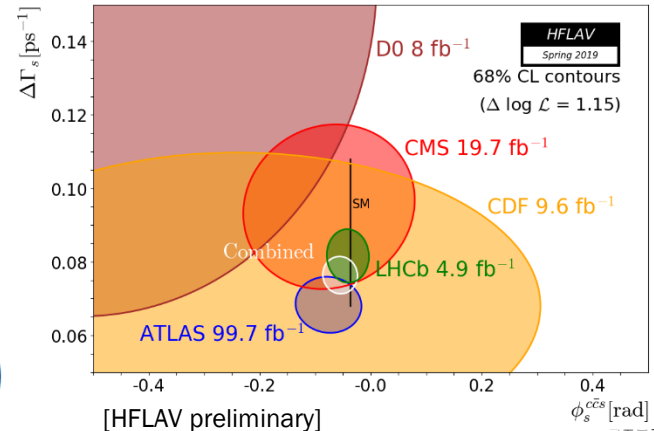
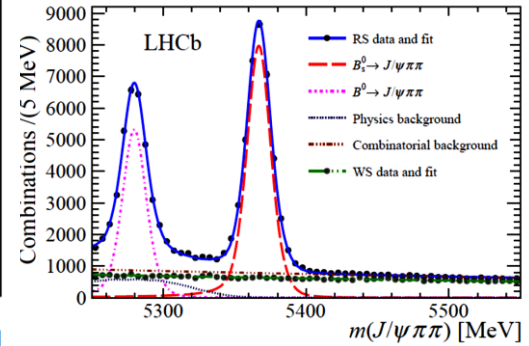
- $\phi_s = -55 \pm 21 \text{ mrad}$
  - $\Delta\Gamma_s = 0.0764^{+0.0034}_{-0.0033} \text{ ps}^{-1}$

$$\phi_s^{\text{SM}} \approx -2 \arg \left( \frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right)$$



[arXiv:1903.05530](https://arxiv.org/abs/1903.05530)

[LHCb-PAPER-2019-003, Submitted to PLB]





# Measurement of CP violation in $B_s \rightarrow \phi\phi$

- Decay dominated by a penguin loop: enhanced sensitivity to New Physics
- Measure the CP-violating phase  $\phi_s^{s\bar{s}s}$  analogous to  $\phi_s$ .
- Perform time dependent angular analysis

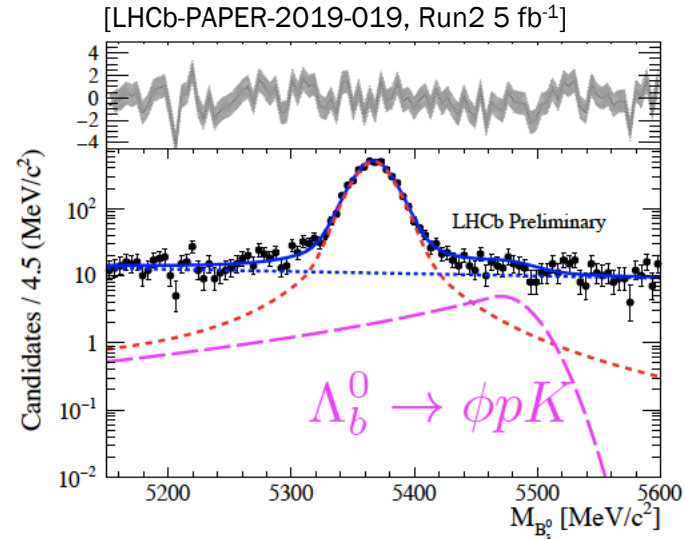
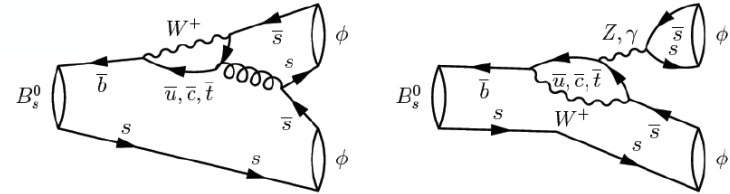
LHCb preliminary

$$\phi_s^{s\bar{s}s} = -0.073 \pm 0.115 \pm 0.027 \text{ [rad]}$$

$$|\lambda| = -0.99 \pm 0.05 \pm 0.01$$

- Consistent with SM predictions of CP-conservation in  $b \rightarrow s\bar{s}s$  transitions:  $\phi_s^{s\bar{s}s} < 20 \text{ mrad}$ 
  - [arXiv:0810.0249 Phys.Rev.D80:114026,2009]
- Most stringent limit on the branching fraction

$$\mathcal{B}(B^0 \rightarrow \phi\phi) < 2.7 \times 10^{-8} \text{ (90 \% CL)}$$



# new measurement of $\Lambda_c^+$ , $\Xi_c^+$ and $\Xi_c^0$ lifetimes

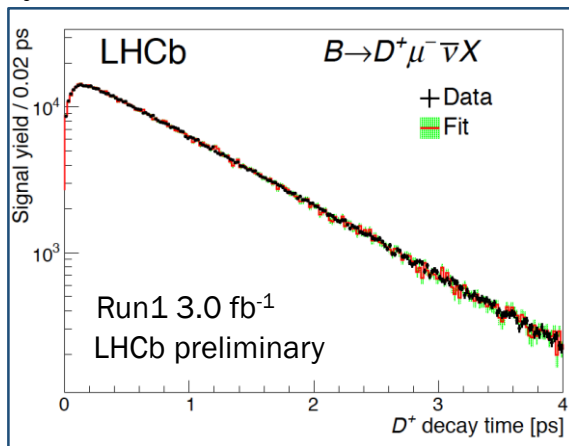


- Baryons selected from semileptonic b-baryon decays
- Measured relative to the  $D^+$  lifetime
- Very large data sets

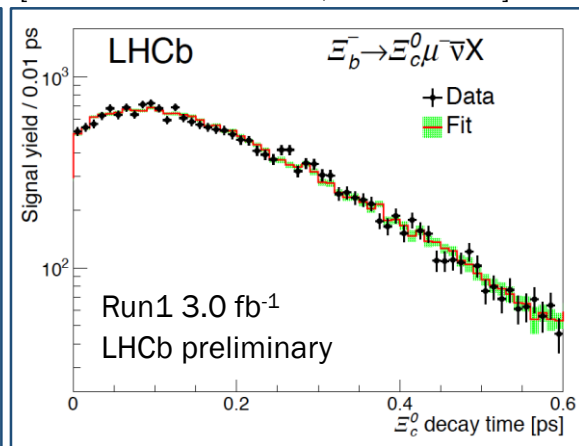
$H_c$	Yield ( $10^3$ )
$D^+$	$809.4 \pm 1.3$
$\Lambda_c^+$	$303.5 \pm 0.7$
$\Xi_c^+$	$55.8 \pm 0.5$
$\Xi_c^0$	$21.6 \pm 0.2$

LHCb preliminary

- Better precision by 3-4 times wrt world averages, but consistent.
- Lifetime of  $\Xi_c^0$  3.3 sigma larger than WA of  $112_{-10}^{+13}$  fs.



[LHCb-PAPER-2019-008, Run1 3.0 fb<sup>-1</sup>]



$$\tau_{\Lambda_c^+} = 203.5 \pm 1.0 \pm 1.3 \pm 1.4 \text{ fs}$$

$$\tau_{\Xi_c^+} = 456.8 \pm 3.5 \pm 2.9 \pm 3.1 \text{ fs}$$

$$\tau_{\Xi_c^0} = 154.5 \pm 1.7 \pm 1.6 \pm 1.0 \text{ fs}$$

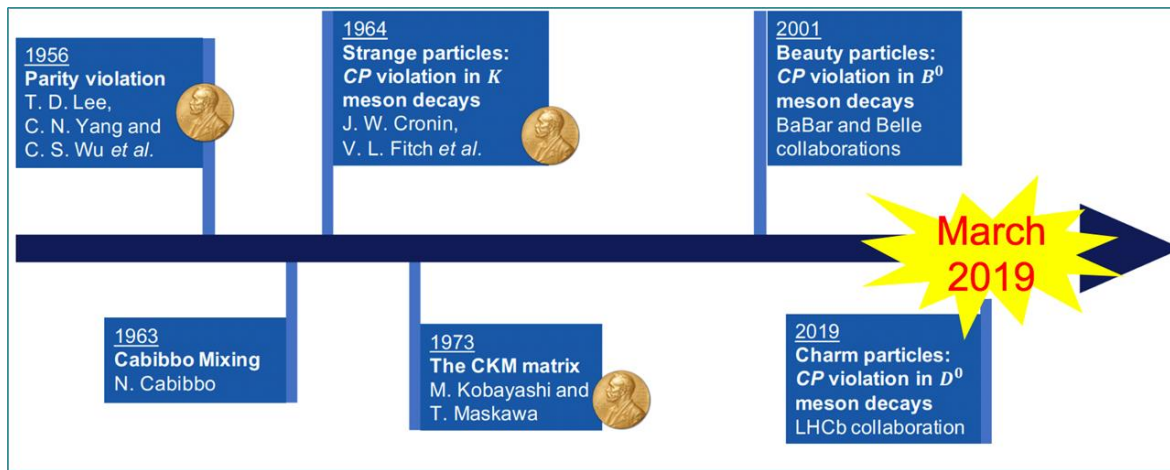
Stat. Syst. D+ lifetime uncertainty

LHCb  
preliminary

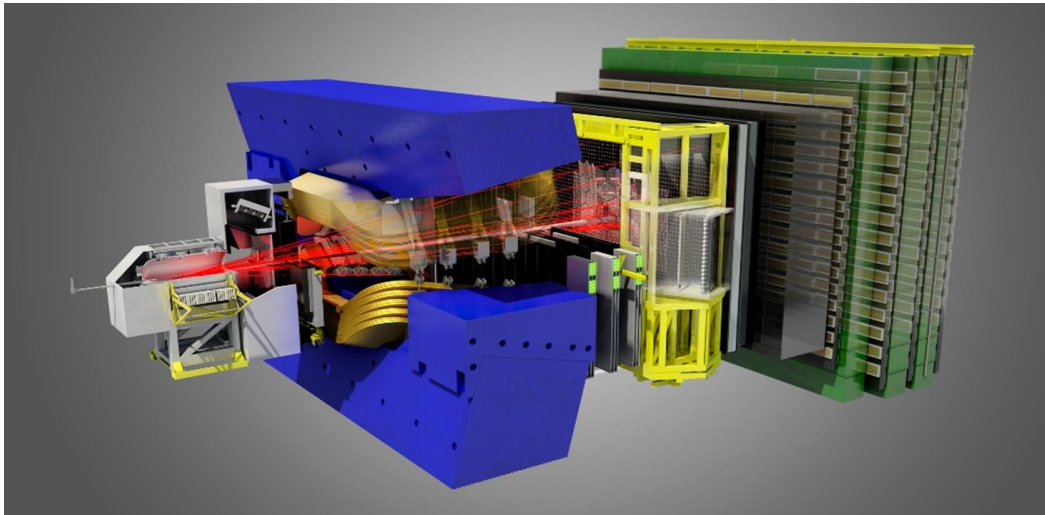


# Conclusion

The milestones of  
Flavour Physics



- Run 1 & 2 data analyses progressing well with many World's Best measurements being published
  - Many more publications in the pipeline
- Upgrade 1 well under way
  - Old detector disassembly complete, with new installations started already
  - Detector production, construction and assembly under way for all detectors
  - Schedule is tight but still manageable
- Upgrade 2 on the horizon



# Backups

# Strategy – Prompt tag



$$A_{\text{raw}}(f) = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow f)}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow f)}$$



Valid up to  $\mathcal{O}(10^{-6})$

$$A_{\text{raw}}(f) \simeq A_{CP}(f) + A_D(f) + A_D(\pi_s) + A_P(D^{*+})$$

Physical CP asymmetry

$D^0$  detection asymmetry  
 $\rightarrow$  equal to 0, since  $K^- K^+$  and  $\pi^- \pi^+$  are symmetric final states

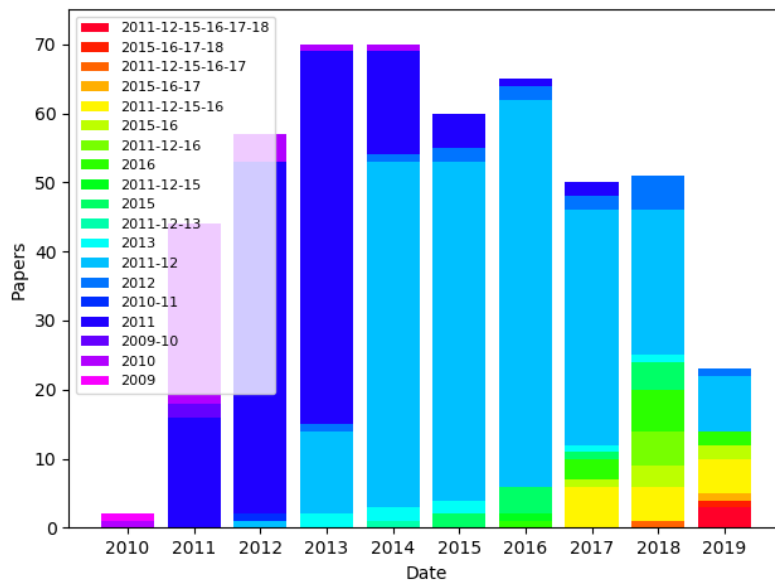
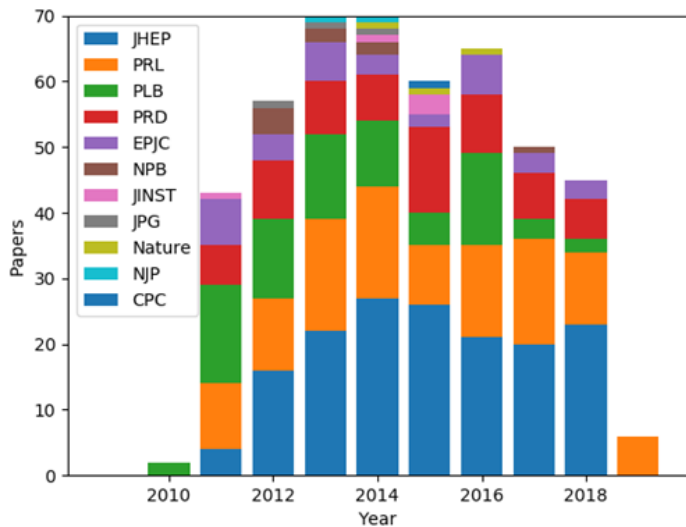
$\pi_s$  detection asymmetry

$D^*$  production asymmetry

Independent on the final state

If the **kinematics** of the  $D^{*+}$  and  $\pi_s$  for the two decay modes are equal

$$\Rightarrow A_{CP}(K^- K^+) - A_{CP}(\pi^- \pi^+) = A_{\text{raw}}(K^- K^+) - A_{\text{raw}}(\pi^- \pi^+)$$



# Measuring $\varphi_s$

Definition of time-dependent CP asymmetry:  $A_{CP}(t) = \frac{\Gamma(\bar{B}_s^0 \rightarrow f) - \Gamma(B_s^0 \rightarrow f)}{\Gamma(\bar{B}_s^0 \rightarrow f) + \Gamma(B_s^0 \rightarrow f)} = \eta_f \sin \varphi_s \sin(\Delta m_s t)$

Experimentally it becomes:  $A_{CP}(t) = \eta_f \cdot e^{-\frac{1}{2}\Delta m_s^2 \sigma_t^2} \cdot (1 - 2\omega) \cdot \sin \varphi_s \cdot \sin(\Delta m_s t)$

Critical requirements:

- CP eigenvalue of the final state  $\eta_f \rightarrow$  angular analysis
- Excellent decay-time resolution  $\sigma_t \sim 45$  fs
- Tagging of meson flavour @ production: probability of getting the wrong tag  $\omega$
- + in the fit need to model decay-time efficiency  $\varepsilon(t)$  (due to selection and reconstruction) and angular efficiency  $\varepsilon(\Omega)$