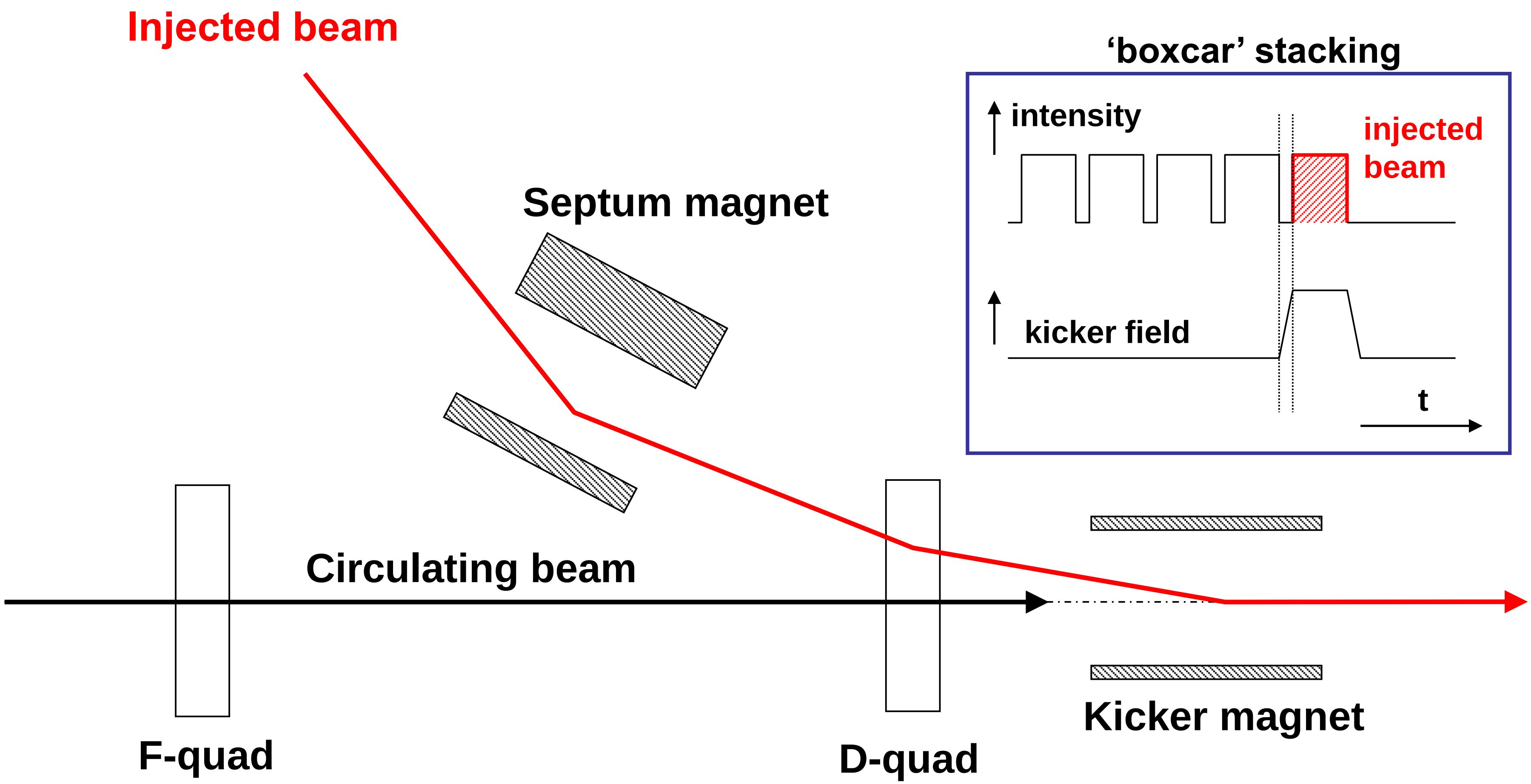
Kickers, septa and beam transfer lines

- Beam transfer devices
  - Kickers
  - Septa
  - Protection devices
- Beam transfer lines
  - Distinctions between transfer lines and circular machines
  - Linking machines/experiments together
  - Emittance blow-up from mismatch
  - Measure beam parameters (measurement lines)

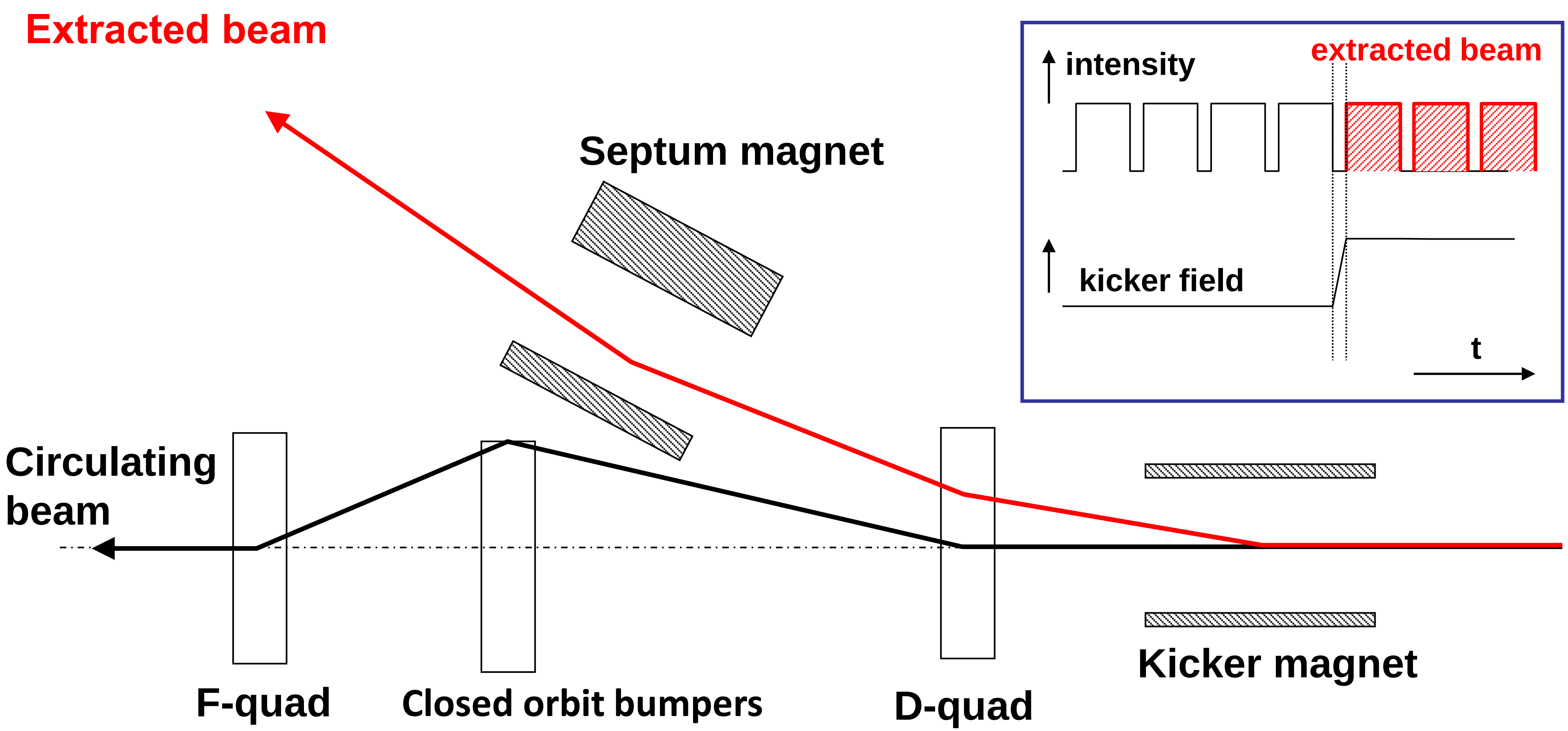
Francesco M. Velotti, CERN (TE-ABT-BTP) based on lectures by
M. Fraser, M.J. Barnes, W. Bartmann, J. Borburgh, B. Goddard, V. Kain and M. Meddahi

Reminder: injection, septum and kicker



- Kickers produce fast pulses, rising their field within the particle-free gap in the circulating beam (**temporal separation**)
- Septa compensate for the relatively low kicker strength, and approach closely the circulating beam (**spatial separation**)

Reminder: extraction, septum and kicker



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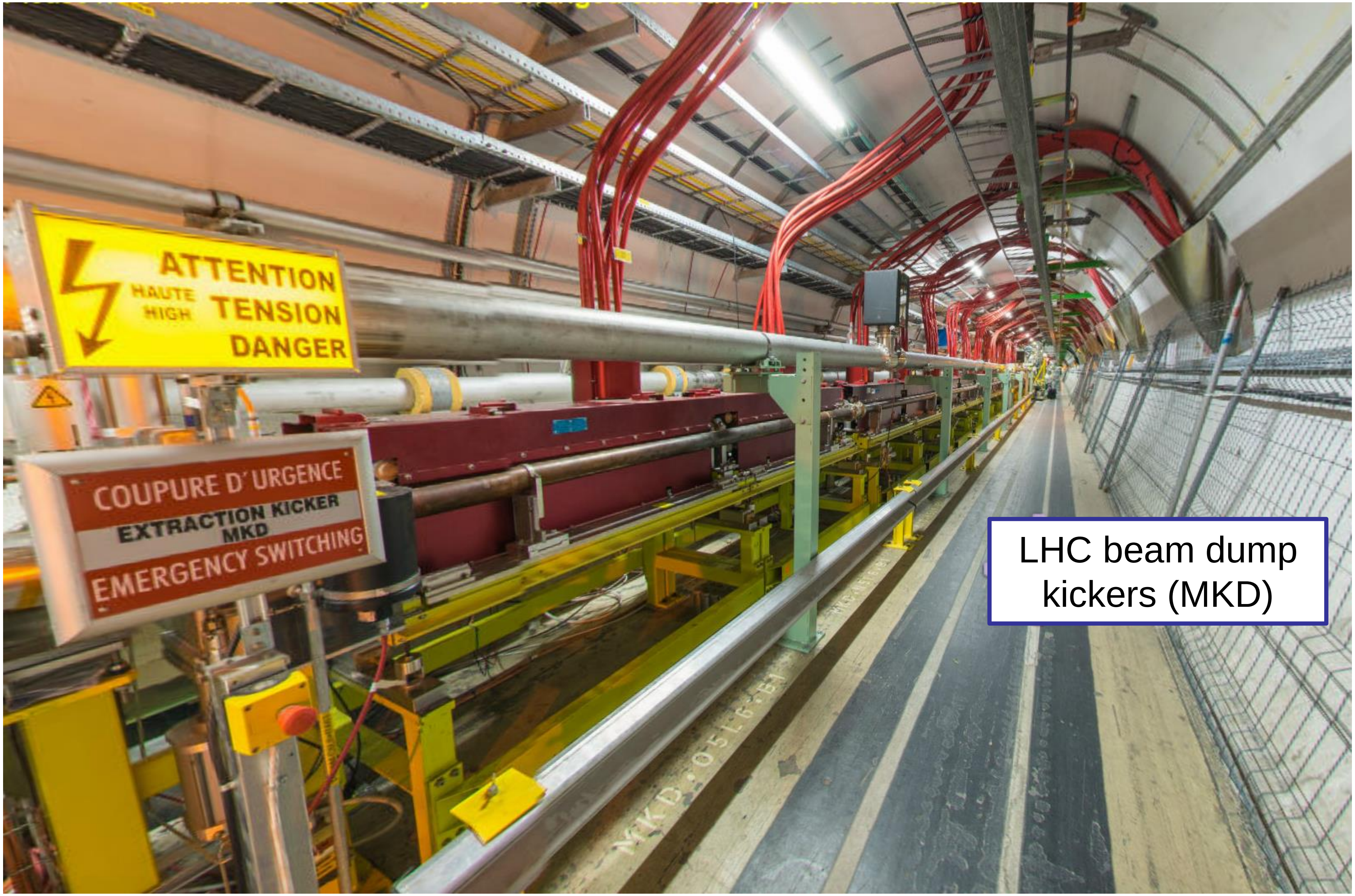
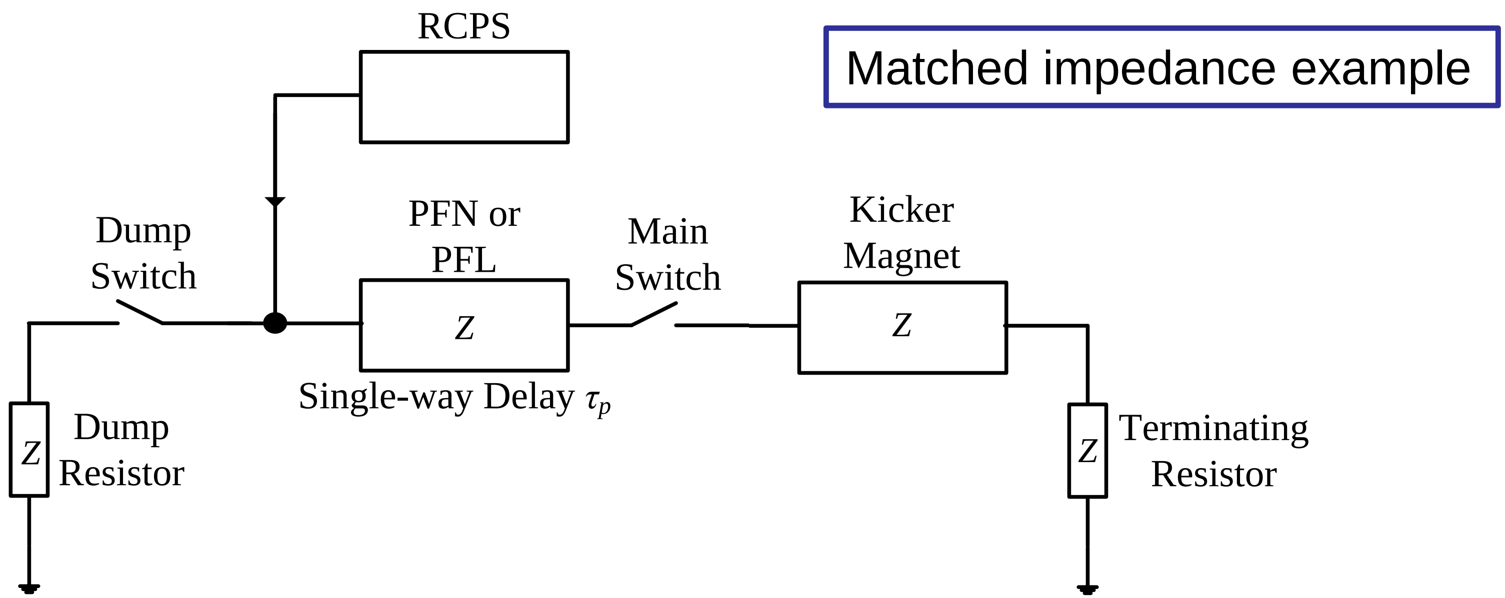
Kickers


ATTENTION
HAUTE
HIGH
TENSION
DANGER
COUPURE D'URGENCE
EXTRACTION KICKER
MKD
EMERGENCY SWITCHING
LHC beam dump kickers (MKD)

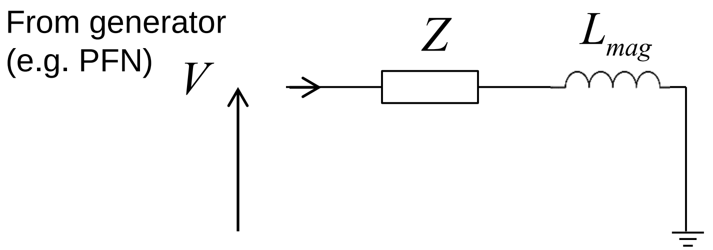
Simplified kicker system schematic



- Main sub-systems ("components") of kicker system;
  - **RCPS** = Resonant Charging Power Supply
  - **PFL** = Pulse Forming Line (coaxial cable) or **PFN** = Pulse Forming Network (lumped elements)
  - Fast high power **switch(es)**
  - **Transmission line(s)**: coaxial cable(s)
  - **Kicker Magnet**
  - **Terminators** (resistive)

Magnets – design options

- Type: “lumped inductance”



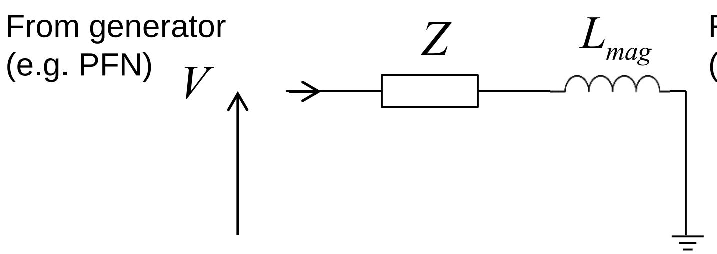
  - simple magnet design
  - magnet must be nearby the generator to minimise inductance
  - exponential field rise-time:

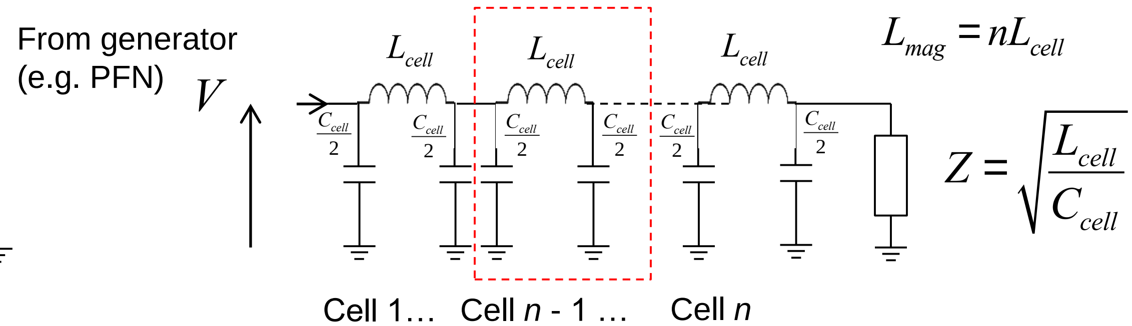
$$I = \frac{V}{Z}(1 - e^{-t/t}) \qquad t = \frac{L_{mag}}{Z}$$

  - slow: rise-times ~ 1 μs

Magnets – design options

- Type: “lumped inductance” or “distributed inductance” (**transmission line**)





- simple magnet design
- magnet must be nearby the generator to minimise inductance
- exponential field rise-time:

$$I = \frac{V}{Z}(1 - e^{-t/\tau}) \qquad \tau = \frac{L_{mag}}{Z}$$

- slow: rise-times ~ 1 μs

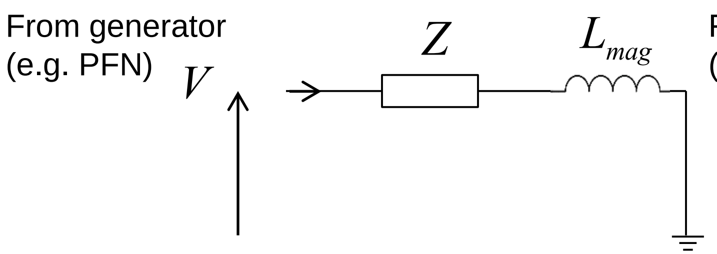
- complicated magnet design
- impedance matching important
- field rise-time depends on propagation time of pulse through magnet:

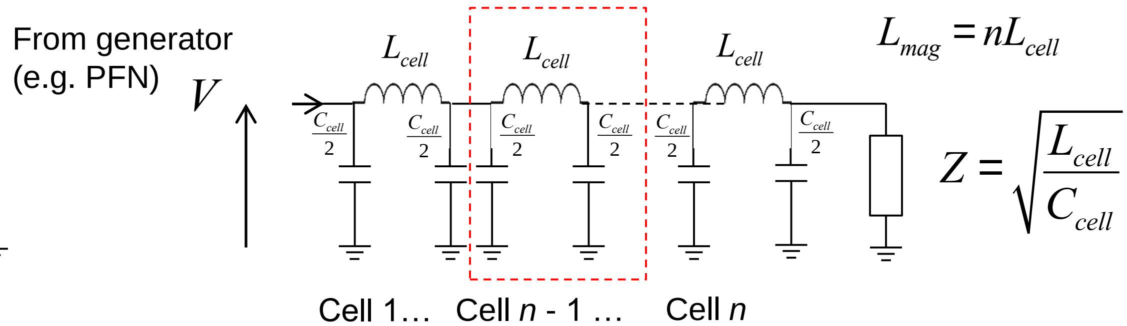
$$\tau = n\sqrt{L_{cell} \times C_{cell}} = n\frac{L_{cell}}{Z} = \frac{L_{mag}}{Z}$$

- **fast: rise-times << 1 μs**

Magnets – design options

- Type: “lumped inductance” or “distributed inductance” (**transmission line**)





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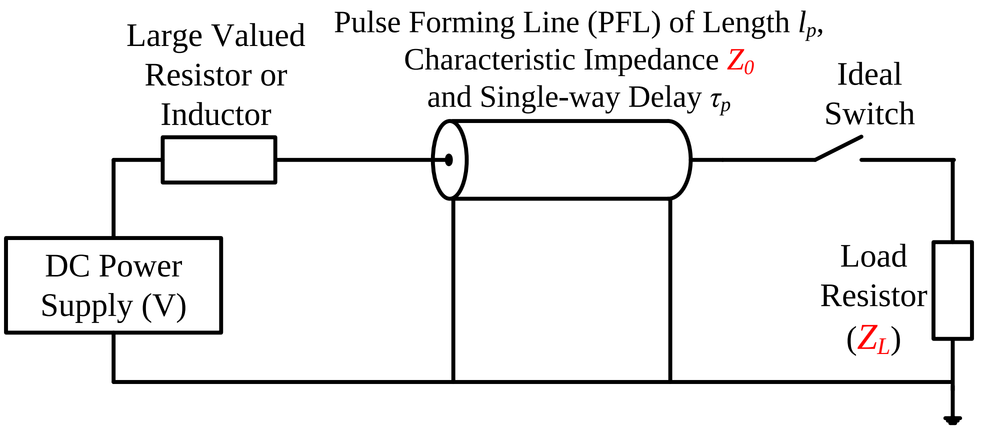
- **fast: rise-times << 1 μs**

- Other considerations:
  - **Machine vacuum**: kicker in-vacuum or external
  - **Aperture**: geometry of ferrite core
  - **Termination**: matched impedance or short-circuit

Reflections

- A simplified pulse forming circuit:



Match impedances to avoid reflections!

- When the switch is fired the voltage is divided as:

$$V_L = V \cdot \left(\frac{Z_L}{Z_0 + Z_L} \right) = \alpha V$$

Reflections

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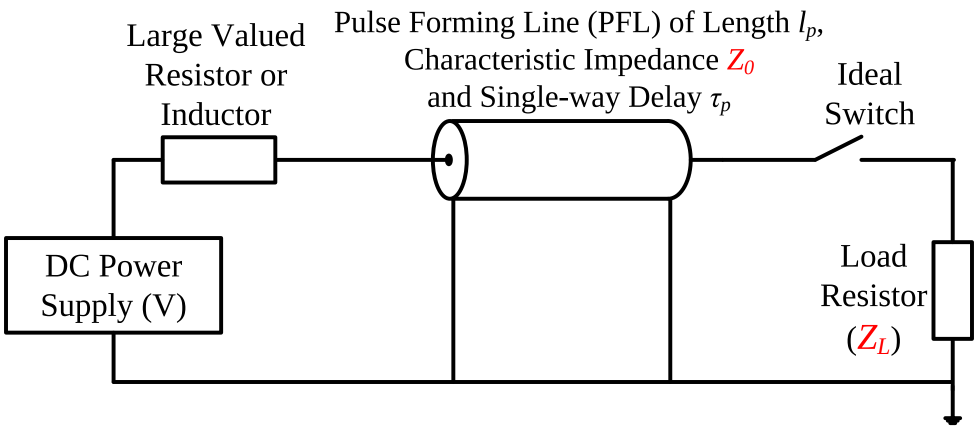

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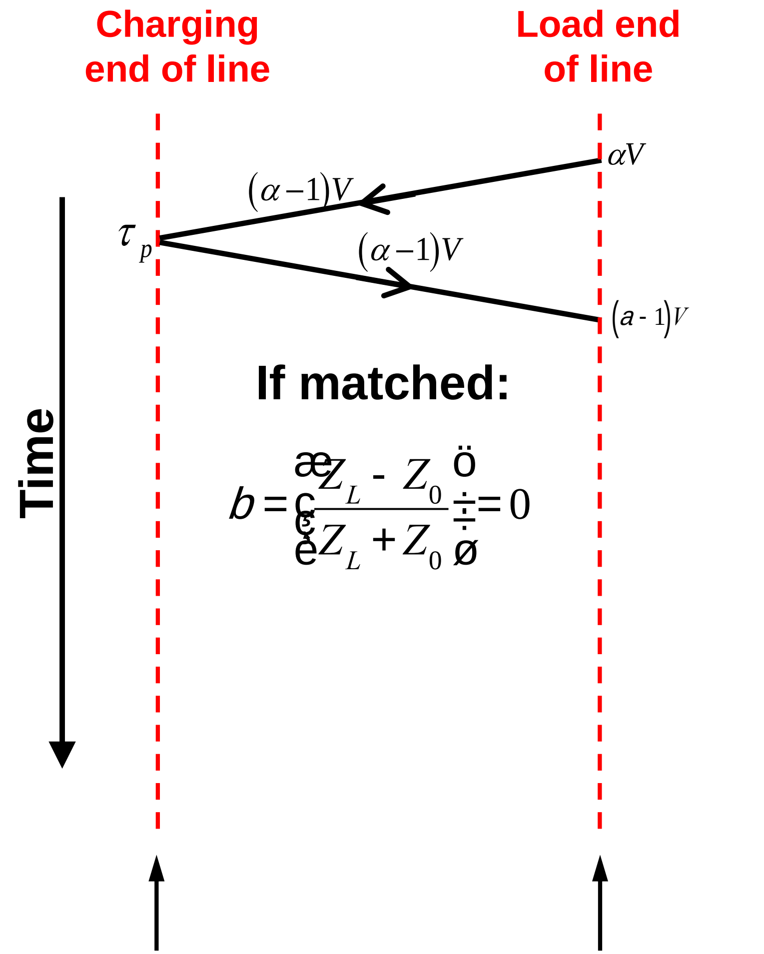
$$V_L = V \cdot \left(\frac{Z_L}{Z_0 + Z_L} \right) = \alpha V$$

- In the matched case:

$$Z_0 = Z_L \qquad a = \frac{1}{2},\ b = 0$$

- Mismatches will ring in the circuit causing ripples on the pulse, or post-pulse.



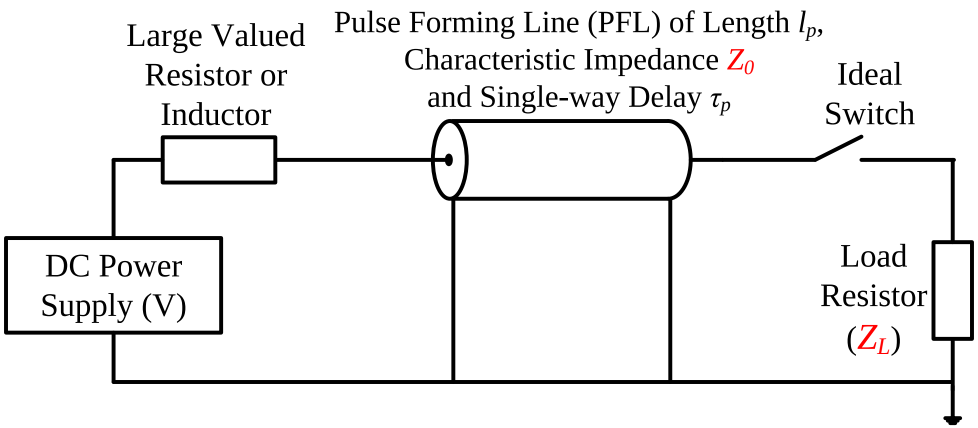
$$b = \left(\frac{Z_L - Z_0}{Z_L + Z_0} \right) = 0$$

G=1

$$\Gamma = \left(\frac{Z_L - Z_0}{Z_L + Z_0} \right) = \beta$$

Reflections

- A simplified pulse forming circuit:



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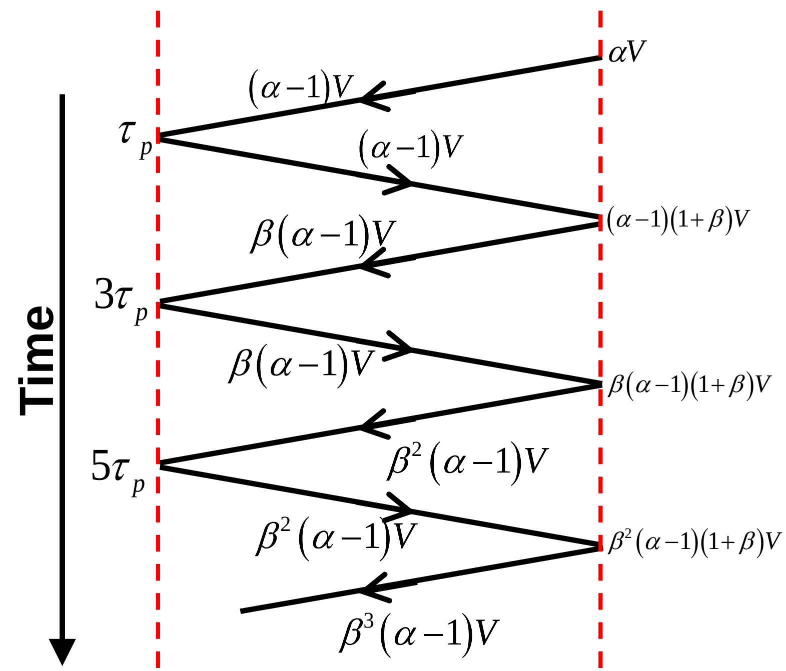


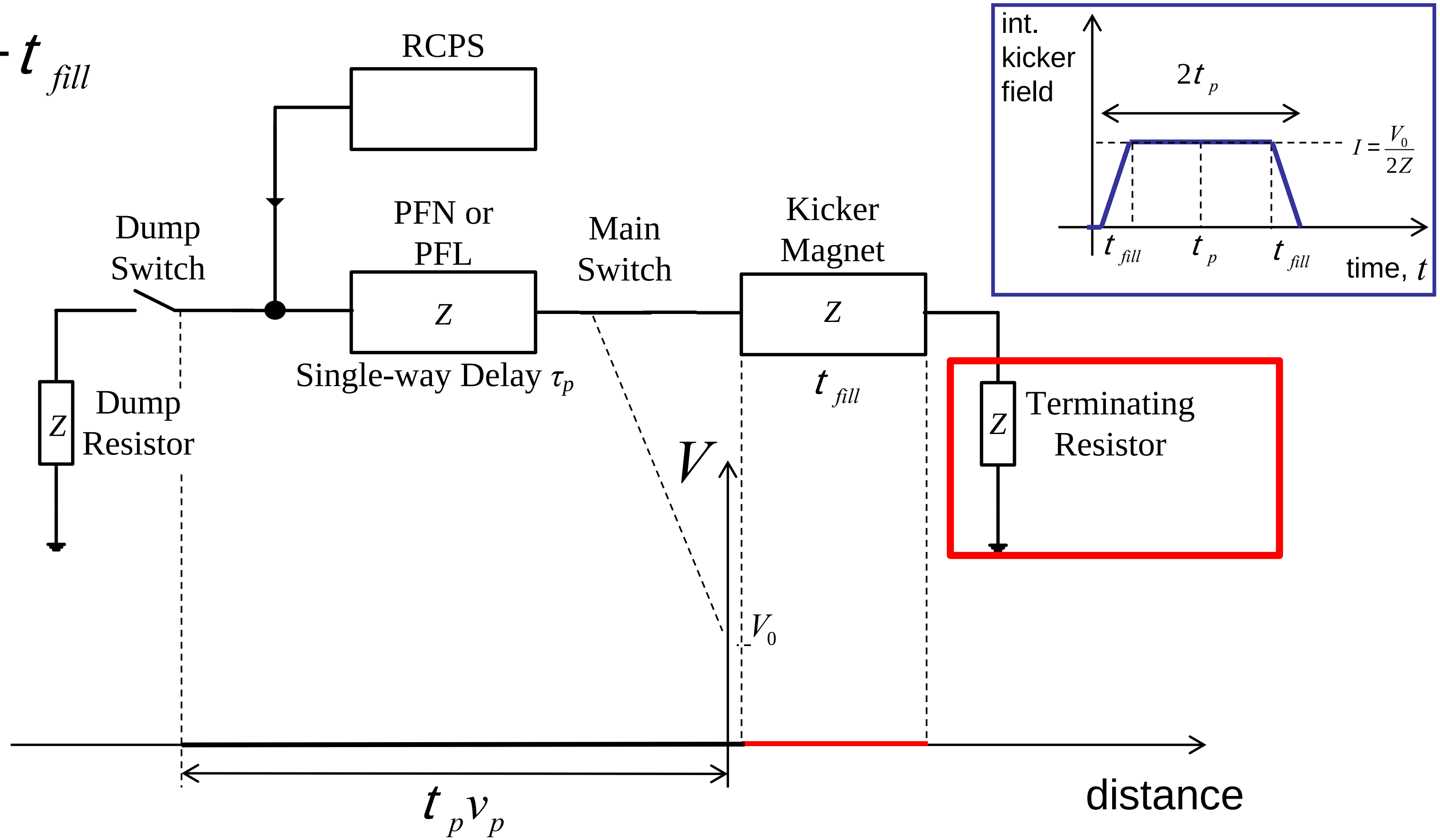
In general (mis-matched):

G=1

$$\Gamma = \left(\frac{Z_L - Z_0}{Z_L + Z_0} \right) = \beta$$

Terminated vs. short circuit

$$t = 2t_p + t_{fill}$$

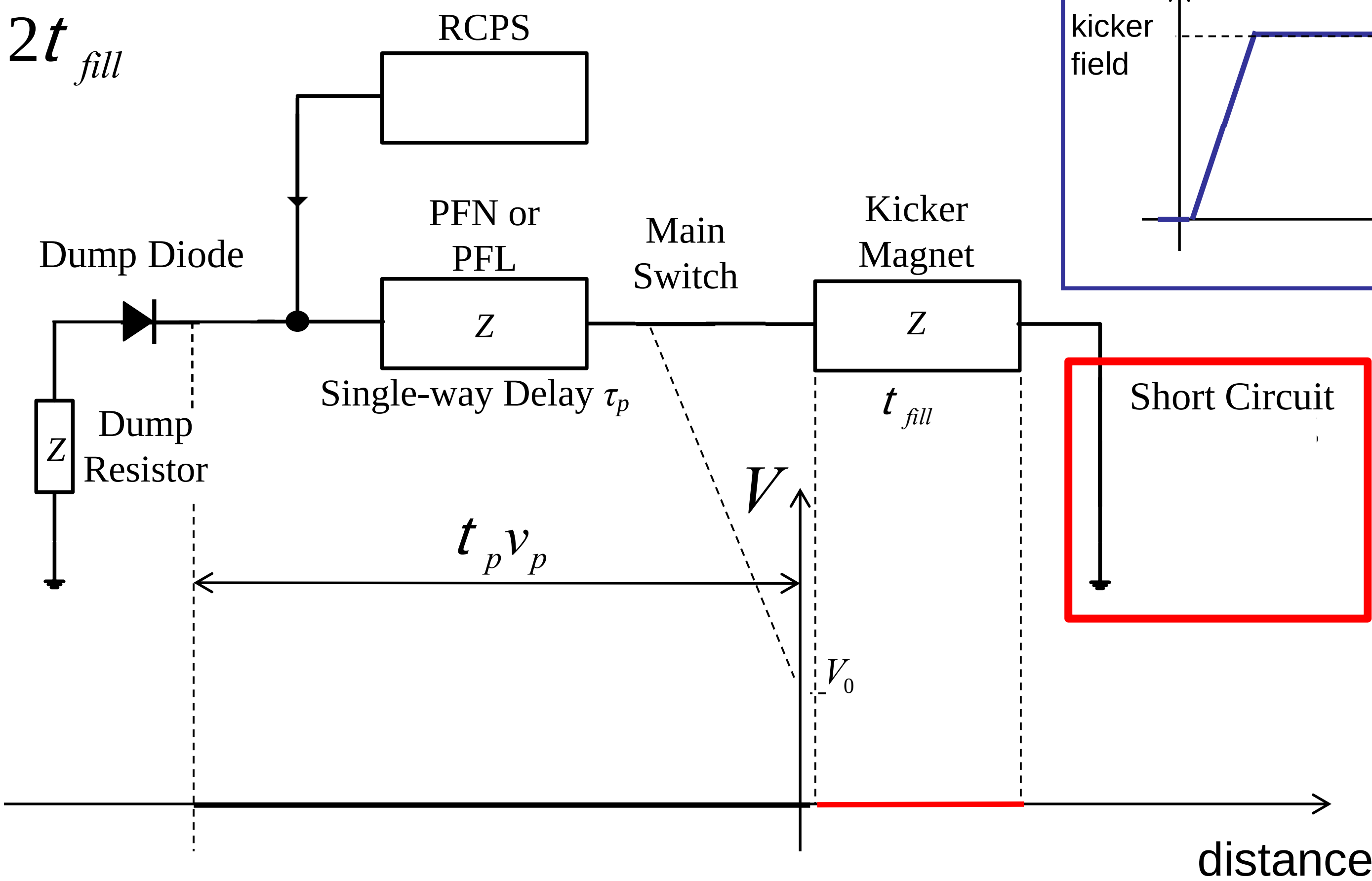


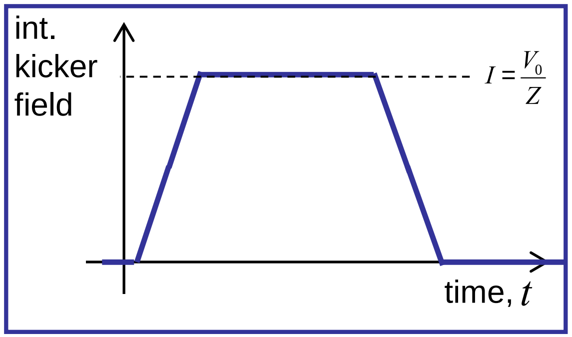
- A kicker pulse of approximately $2\tau_p$ is imparted on the beam and all energy has been emptied into the terminating resistor

Terminated vs. short circuit

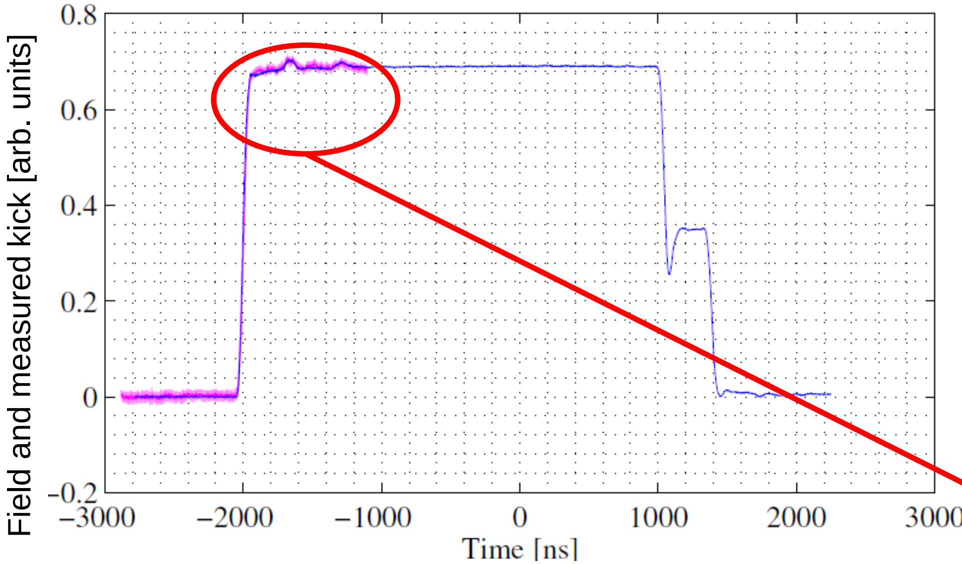
- Short-circuiting the termination offers twice the kick (for a given kicker magnet):
  - Fill time of kicker magnet is doubled
  - Diode as dump switch provides solution for fixed pulse length

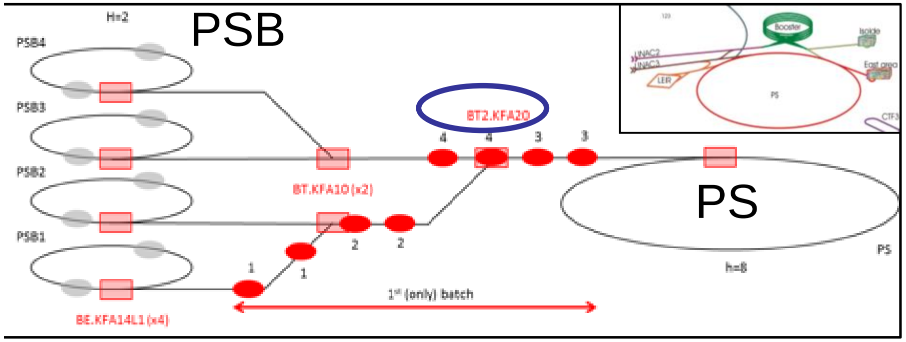
$$t = 3t_p + 2t_{fill}$$



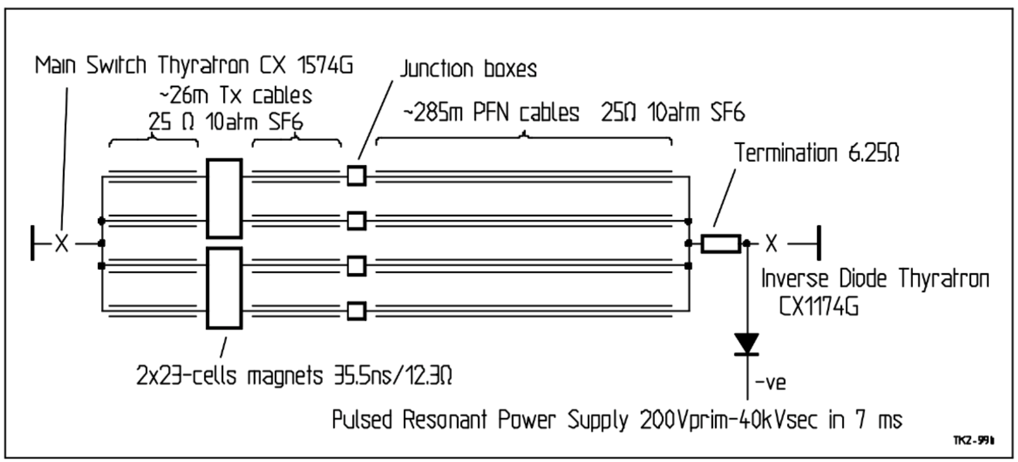


An example of reflections

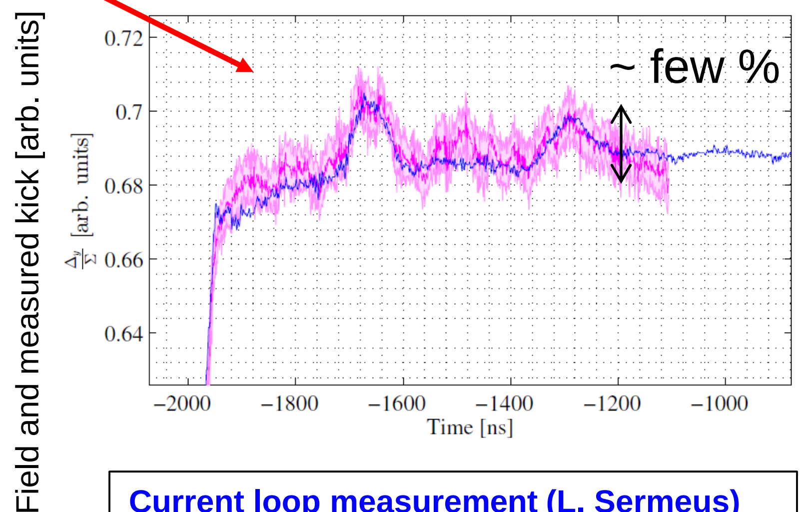




Recombination kicker KFA.20 deflects PS booster rings 1 and 2 vertically into plane of PS at CERN



BT.KFA20 circuit schematic: operates in "virtual" short-circuit

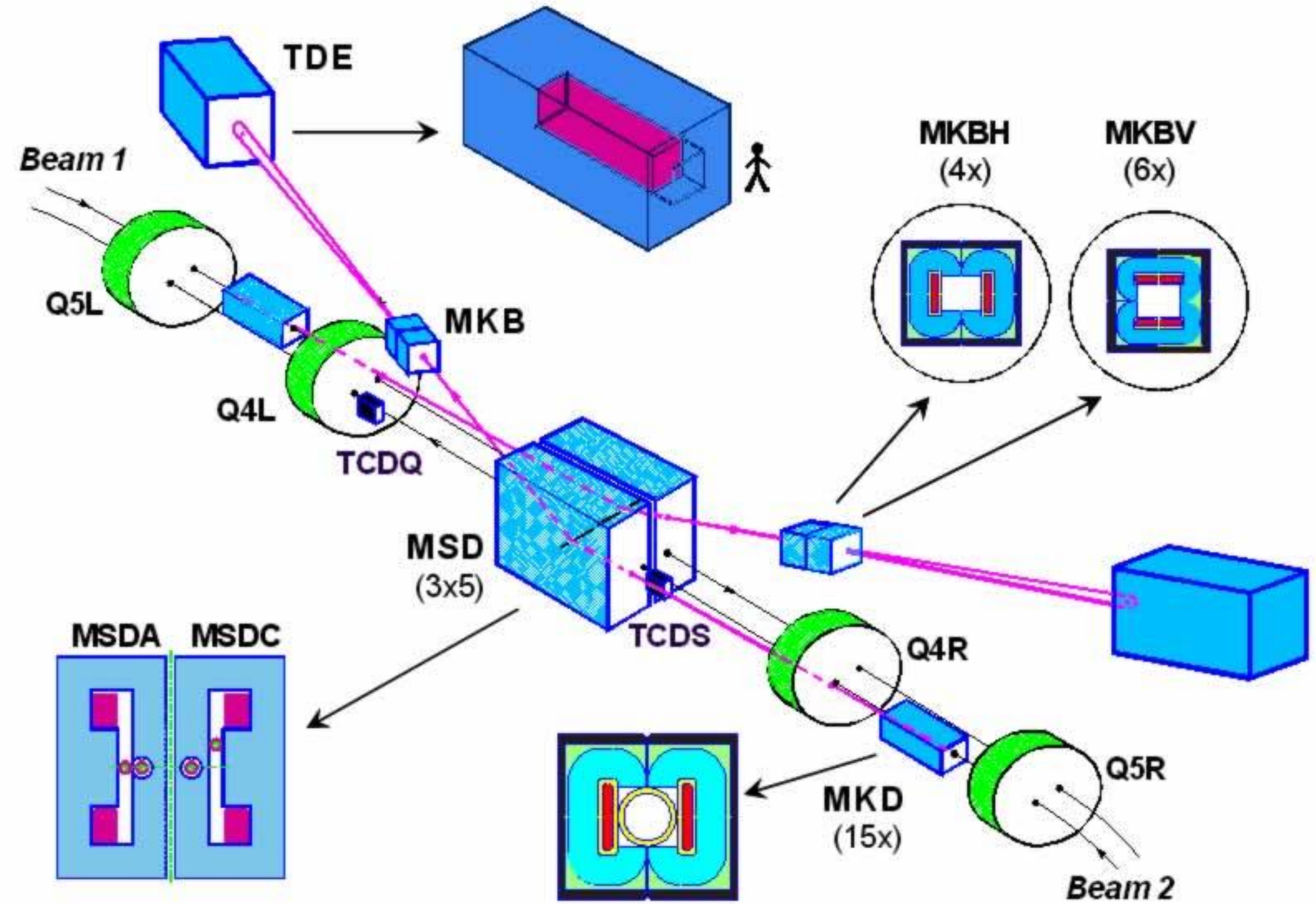


Current loop measurement (L. Sermeus)
Beam-based measurement (I=200e10 ppb)

Beam-based kicker measurements at higher intensities, V. Forte BT + PS injection kicker meeting, CERN (15th August 2016)

Magnets – lumped inductance

- Lumped inductance kicker magnets are robust and reliable, and suitable for applications where the rise-time is typically > 1 μs:
  - e.g. LHC beam dump extraction and dilution kicker magnets



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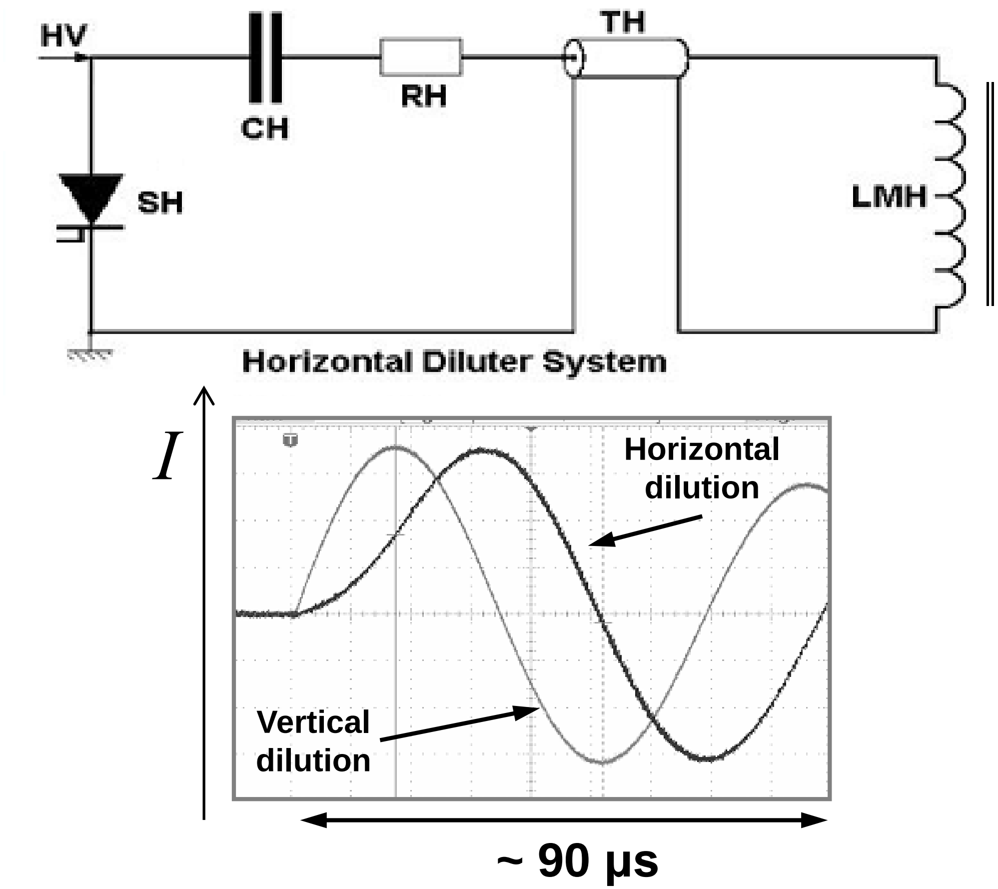
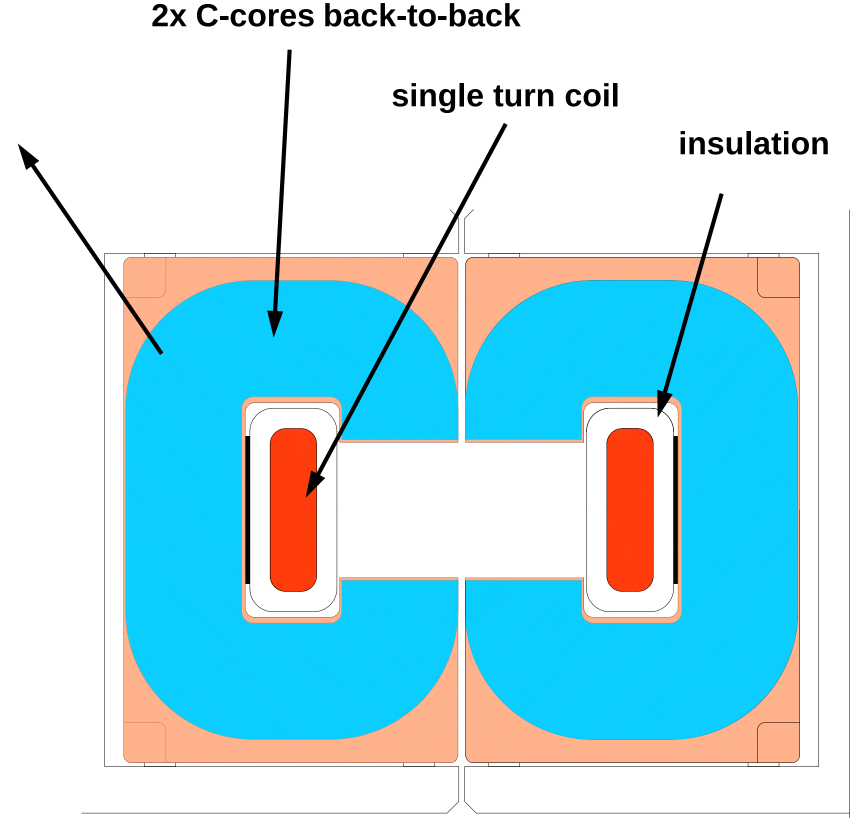


A damped series RLC circuit (switch closed after capacitor charged)



Cross-section of MKBH (horizontal dilution magnet)

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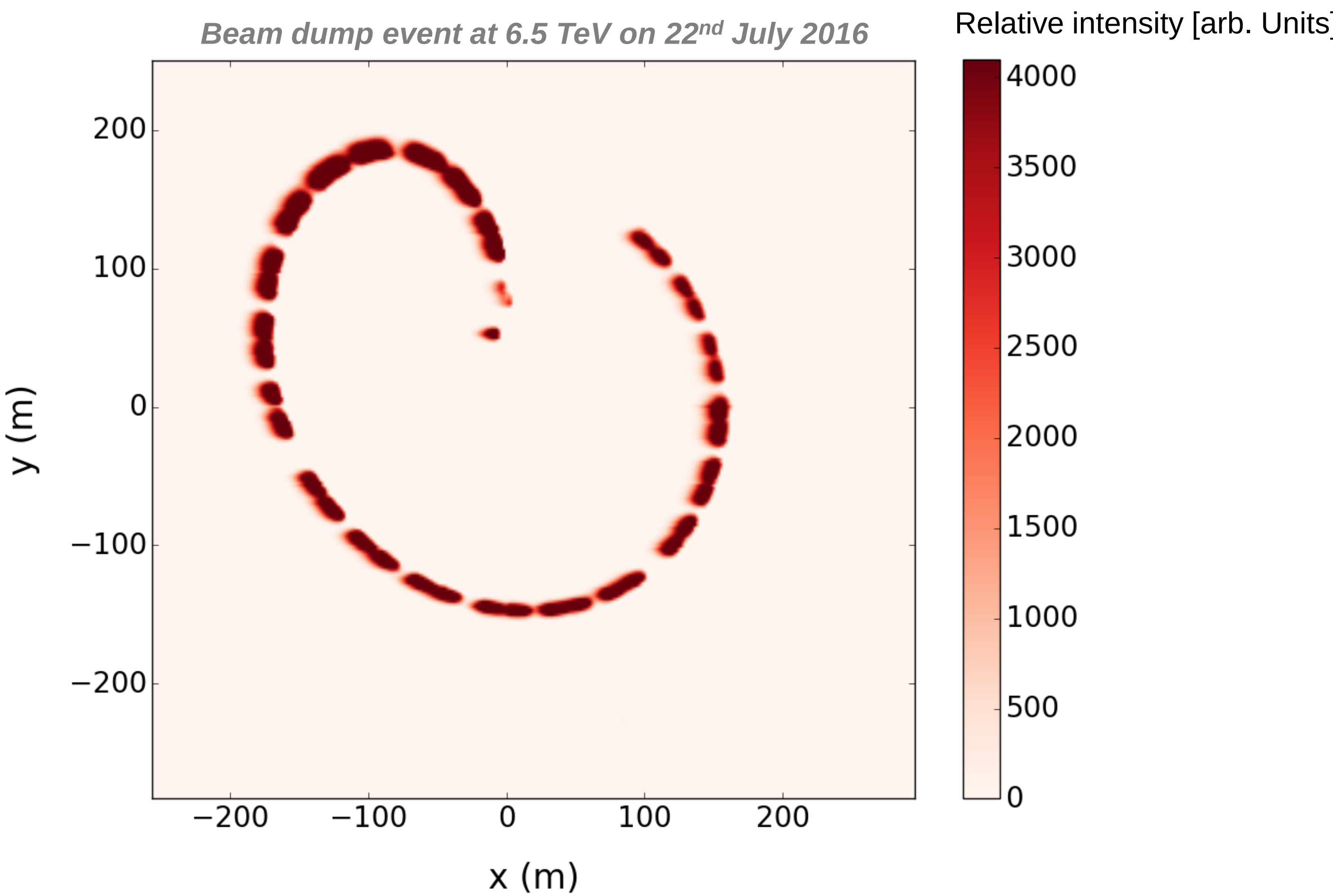

Magnets – lumped inductance

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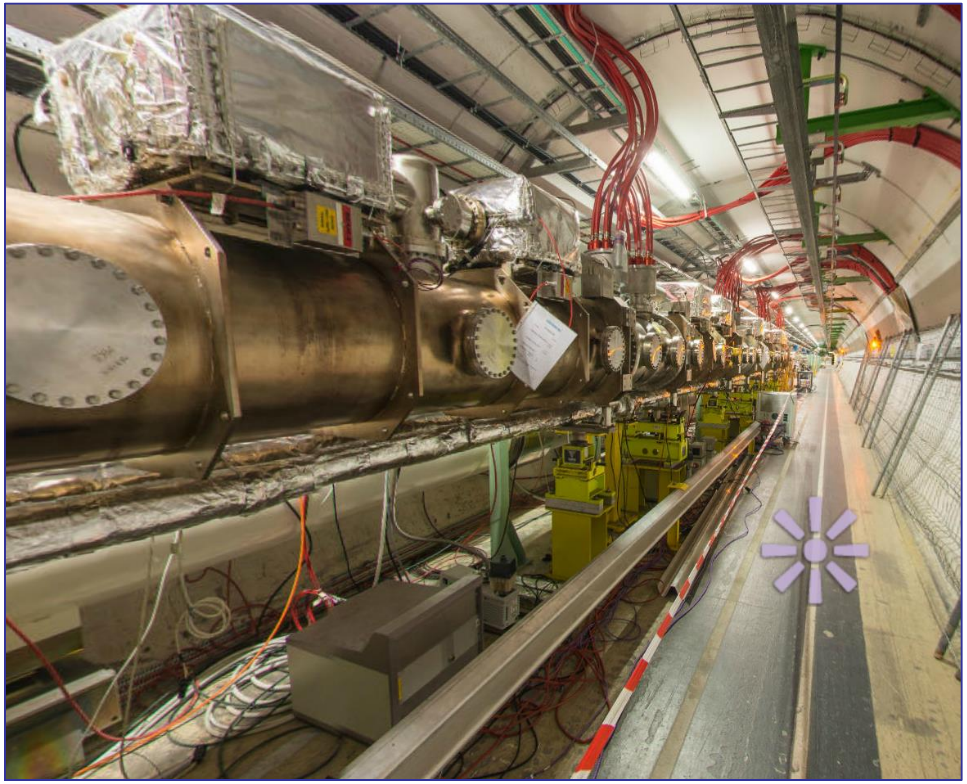
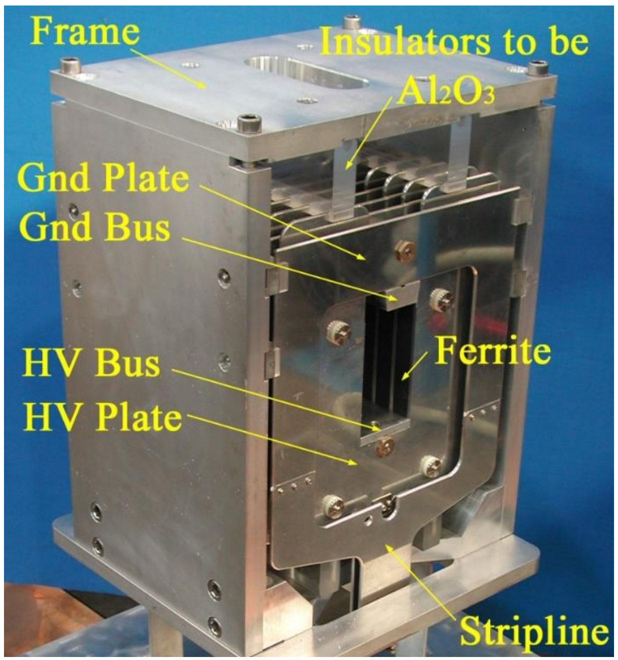
Generators nearby in gallery next to LHC tunnel



MKB dilution magnets in the LHC tunnel

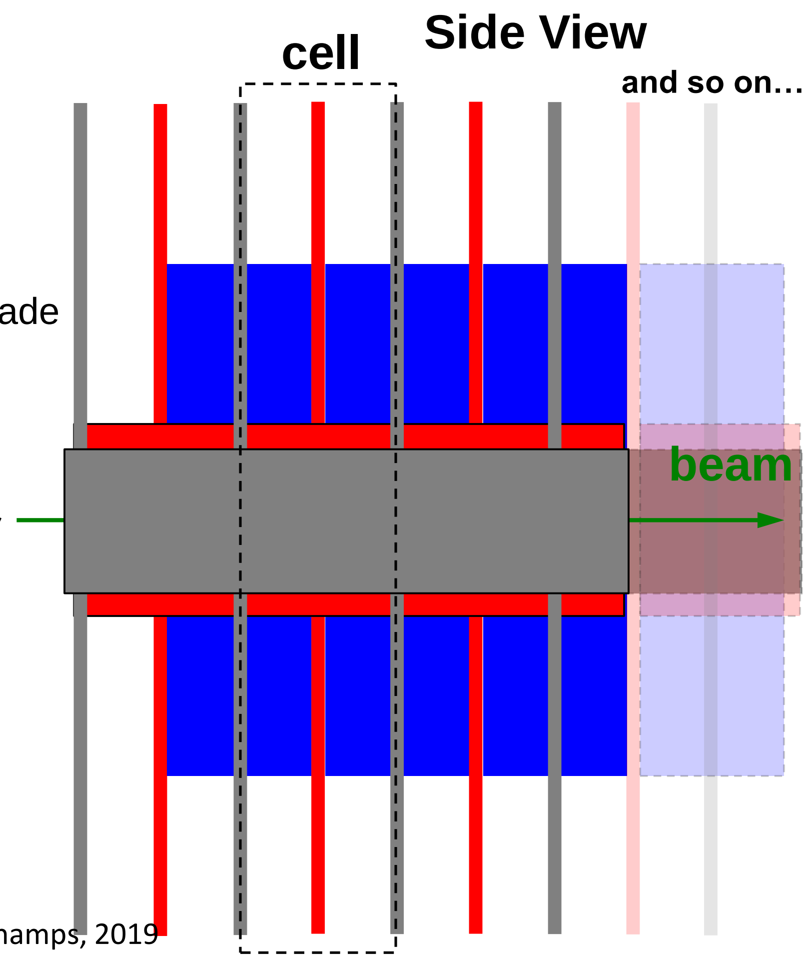
Magnets – transmission line

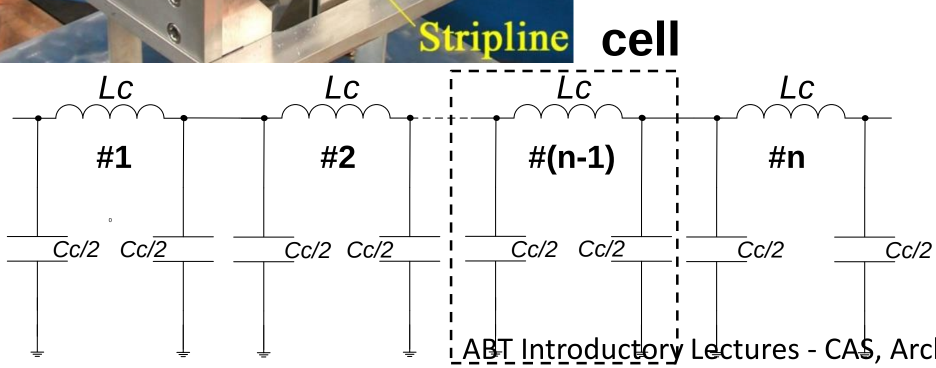
- Today's fast (rise-times of < few hundred ns) kicker magnets are generally **ferrite loaded** transmission lines:
  - Kicker magnets consists of many, relatively short, cells to approximate a broadband coaxial cable



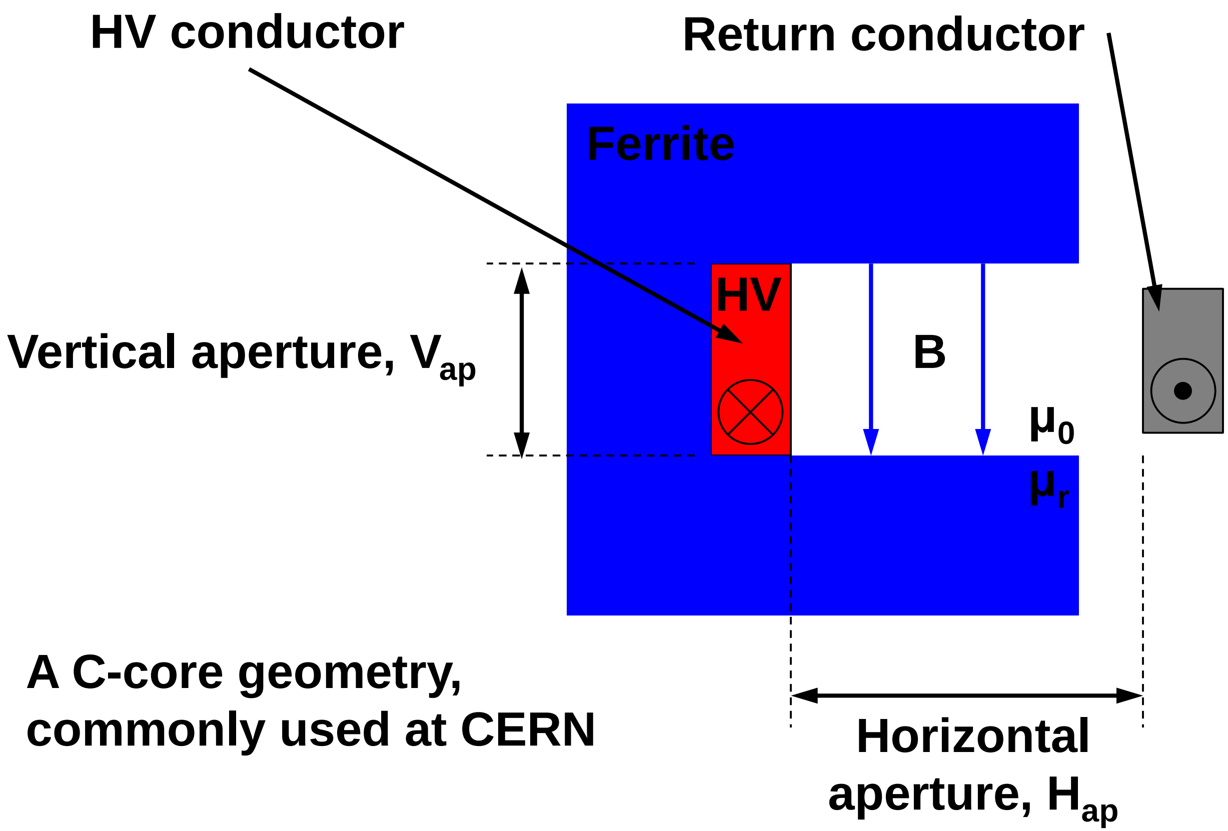
A real kicker…

Prototype for AGS injection kicker upgrade





Magnetic parameters



A C-core geometry, commonly used at CERN

Magnetic field

$$B_y \cong \mu_0 \left(\frac{N \cdot I}{V_{ap}} \right)$$

Derivation: remember Ampère's Law:

$$\oint_C \vec{B}.d\vec{l} = \mu_0 I_{enc}$$

Magnet inductance [per unit length]

$$L_{mag/\mathrm{m}} \cong \mu_0 \left(\frac{N^2 \cdot H_{ap}}{V_{ap}} \right)$$

Derivation: remember Faraday's Law:

$\Phi_B = \int V\,dt$ *and* $V = L\,dI/dt$

- Dimensions H_{ap} and V_{ap} specified by beam parameters at kicker location
- Ferrite ($\mu_r \approx 1000$) reinforces magnetic circuit and uniformity of the field in the gap
- For fast rise-times the inductance must be minimised: typically the number of turns, $N = 1$
- Kickers are often split into several magnet units, powered independently

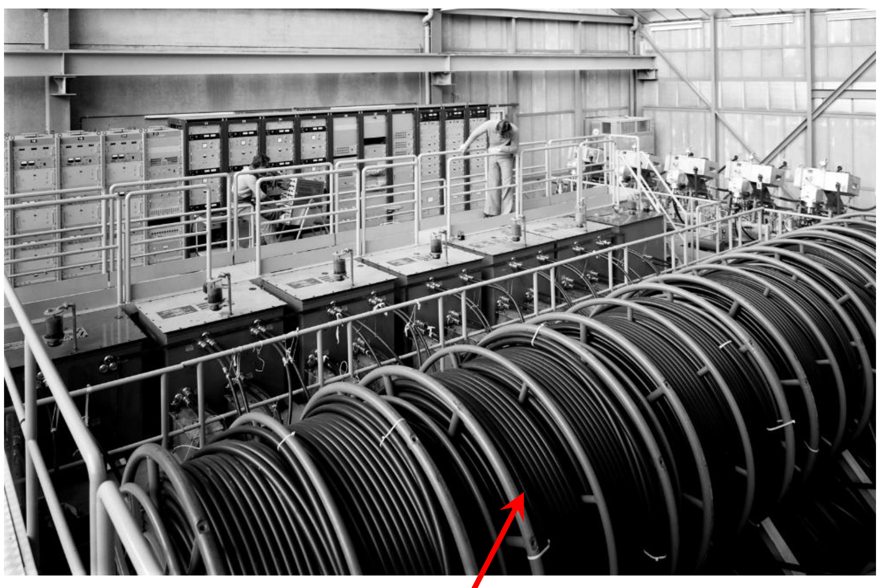
PFL/PFN

Pulse Forming Line (PFL)

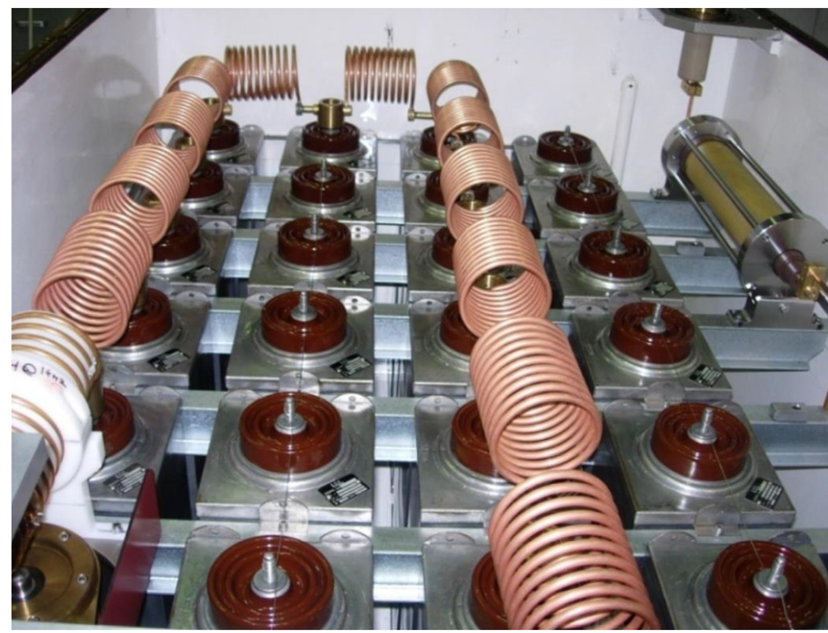
- Low-loss coaxial cable
- Fast and ripple-free pulses
- Attenuation (droop ~1%) becomes problematic for pulses > 3 μs
- Bulky: 3 μs pulse ~ 300 m of cable

Pulse Forming Network (PFN)

- Artificial coaxial cable made of lumped elements
- For low droop and long pulses > 3 μs
- Each cell individually adjustable: adjustment of pulse flat-top difficult and time consuming.



Reels of PFL used at the PS complex (as old as the photograph!)



SPS extraction kicker (MKE) PFN (17 cells)

Switches

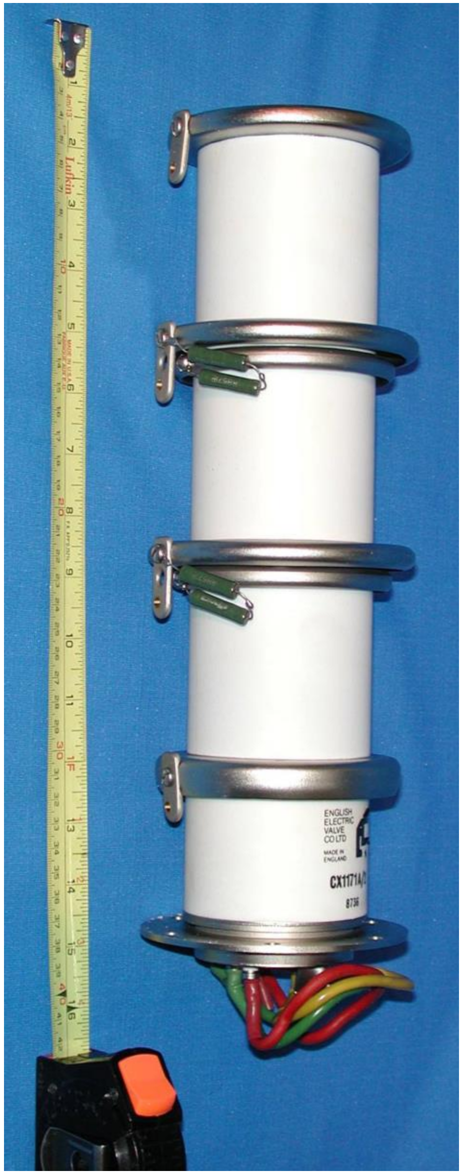
Thyratrons

- Deuterium gas thyratrons are commonly used
- Hold off 80 kV and switch up to 6 kA
- **Fast switching** ~ 30 ns (~150 kA/μs)
- Erratic turn-on: use with RCPS to reduce hold-off time

Power semiconductor switches

- Suitable for scenarios where erratic turn-on is not allowed
- For example, LHC beam dump kickers held at nominal voltage throughout operation (>10h) ready to fire and safely abort at any moment.
- Hold off up to 30 kV and switch up to 18 kA
- **Slower switching** > 1 μs (~18kA/μs)
- Low maintenance

Stack of high-power semiconductor switches (GTOs)

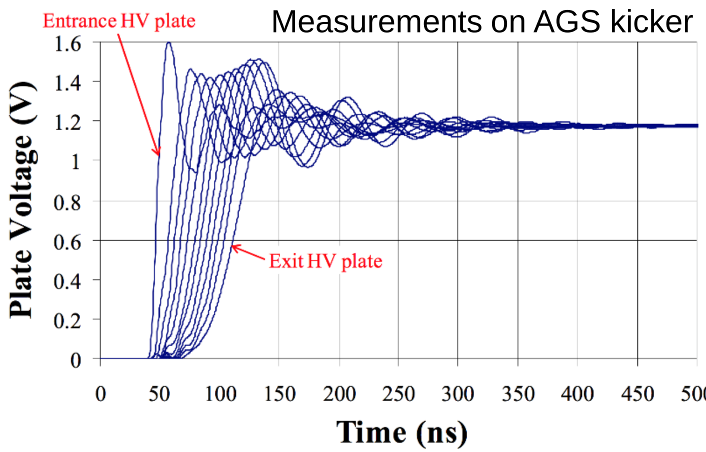


Thyratron

Other topics and considerations

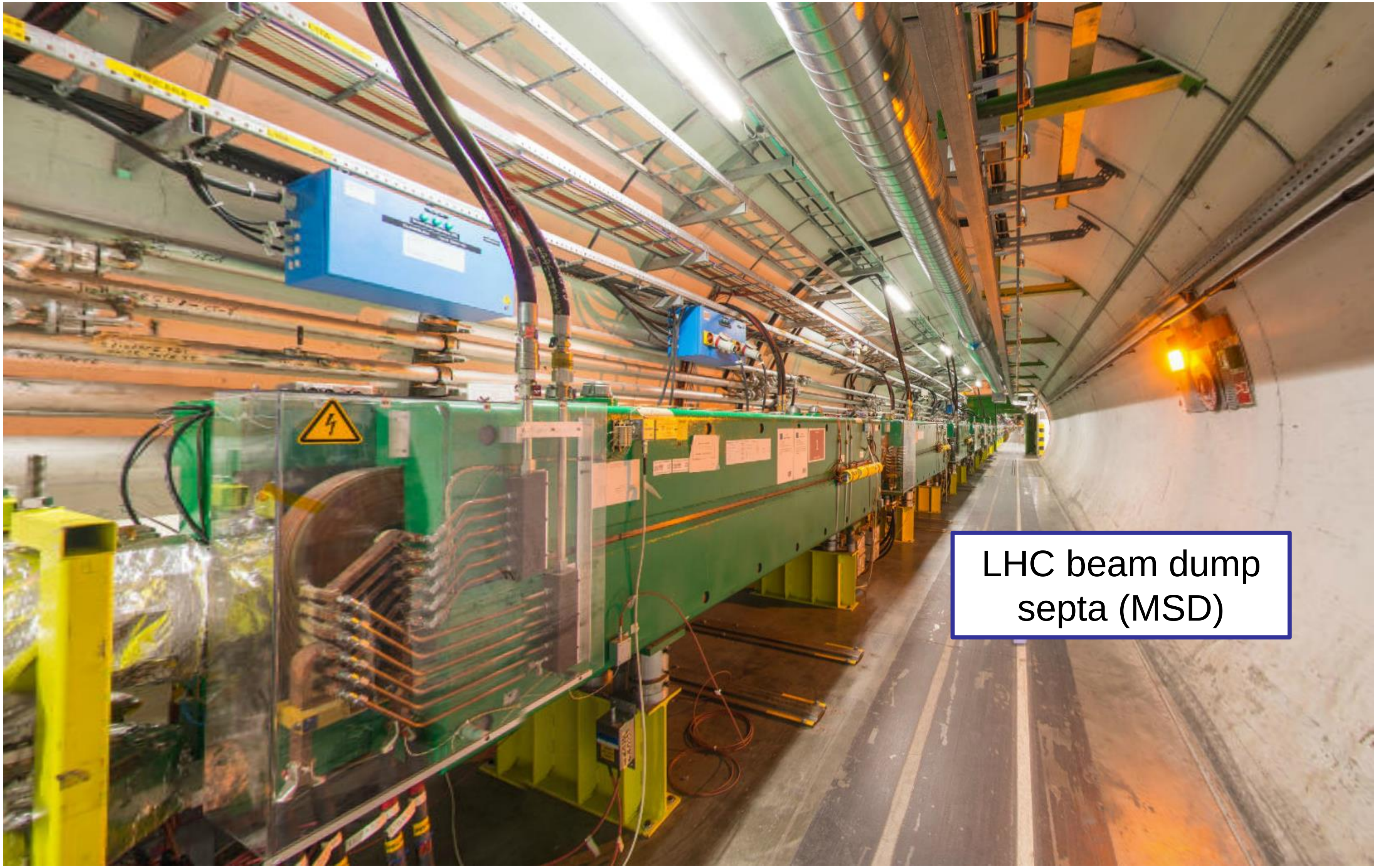
- **Ripple:** cells of a transmission line kicker have a cut-off frequency that introduces dispersion in pulse:
  - Cut-off frequency:

$$\omega_c = \frac{2}{\sqrt{L_{cell}C_{cell}}} = \frac{Z}{L_{cell}}$$



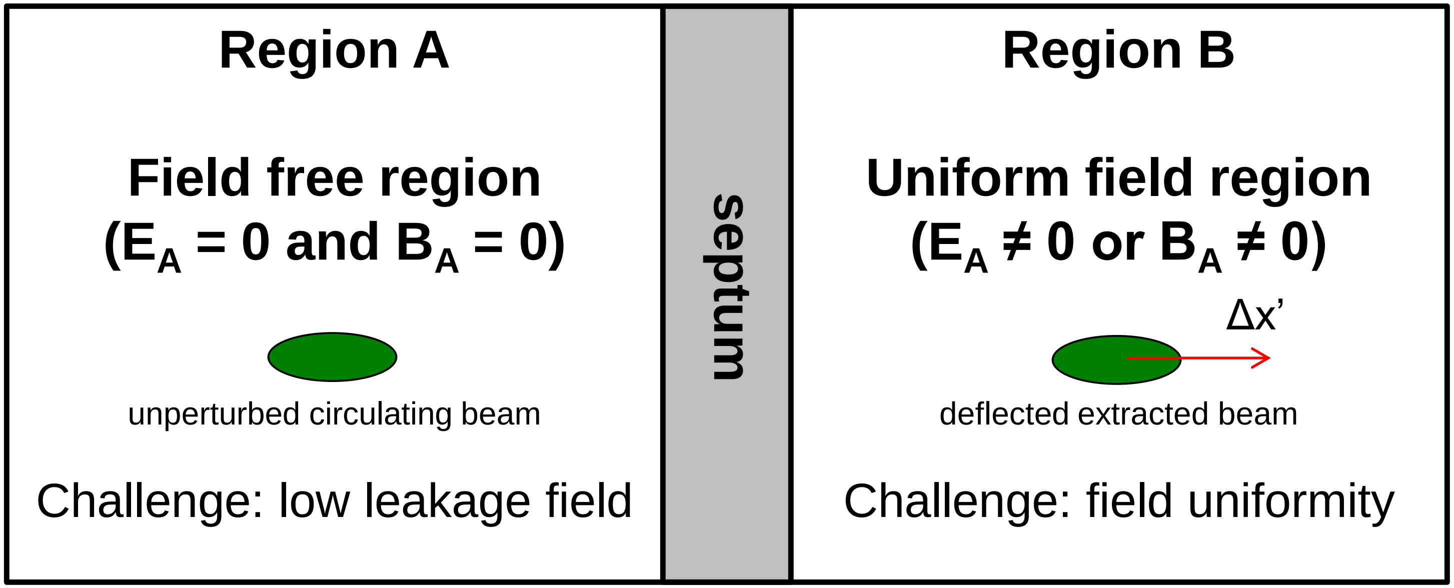
- **In vacuum:** aperture dimensions (H_{ap} and V_{ap}) minimised if in vacuum:
  - For given B, lower I and L can be achieved with smaller H_{ap} and V_{ap}
  - Machine vacuum is a reliable dielectric, recovers after flashover
  - Costly and time consuming to construct/maintain (cleanliness, bake-out)
- **Beam coupling impedance:** kickers are a source of beam impedance in accelerators (wakefields and beam instabilities)
  - Ferrite is shielded from beam with beam screens or serigraphy by permitting a smooth conducting path for beam induced image charges
  - Beam induced heating of ferrite yoke can heat it above the Curie temp.

Septa

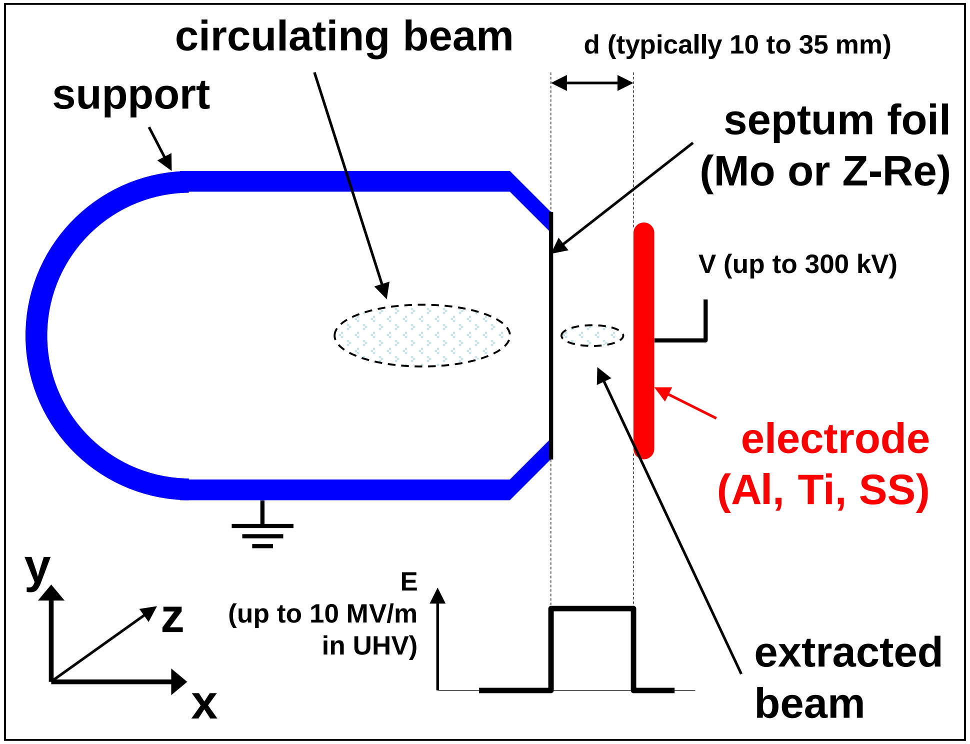


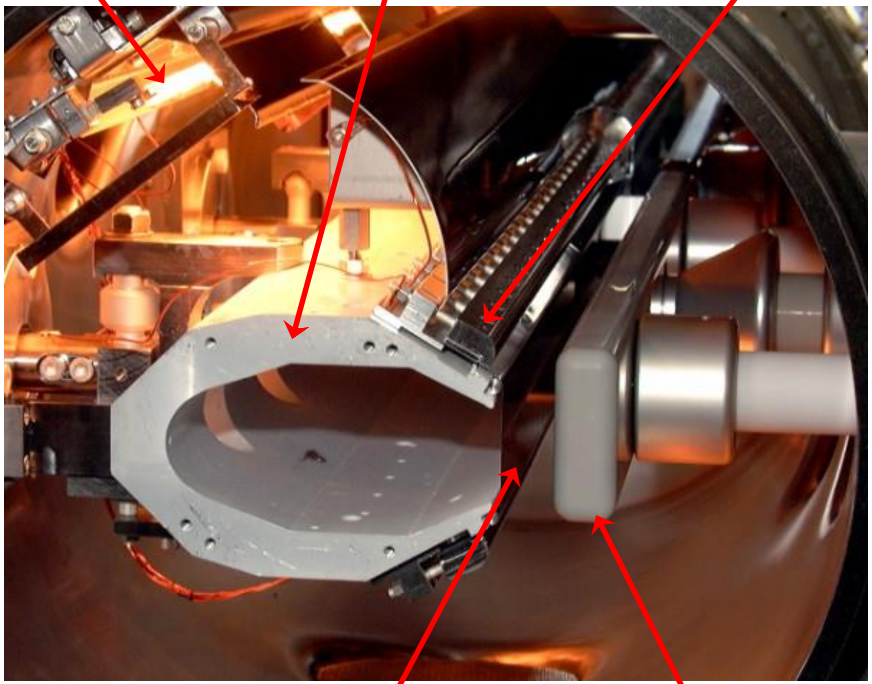
Septa

- Two main types:
  - Electrostatic septa (DC)
  - Magnetic septa (DC and pulsed):
    - Direct drive septum
    - Eddy current septum (pulsed only)
    - Lambertson septum (deflection parallel to septum)



Electrostatic septum



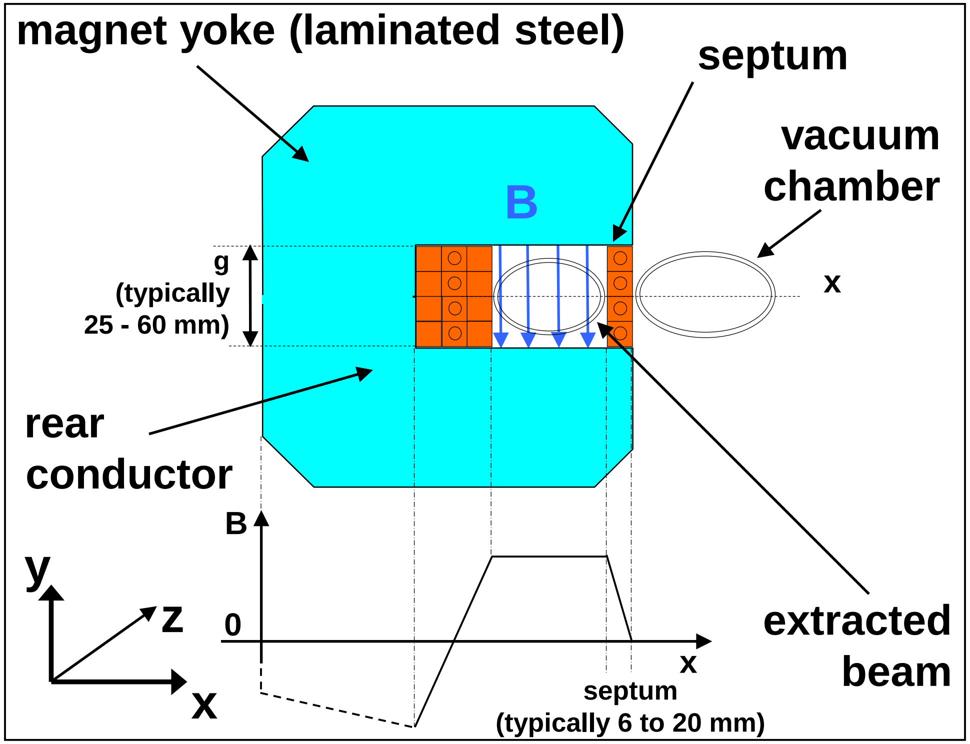


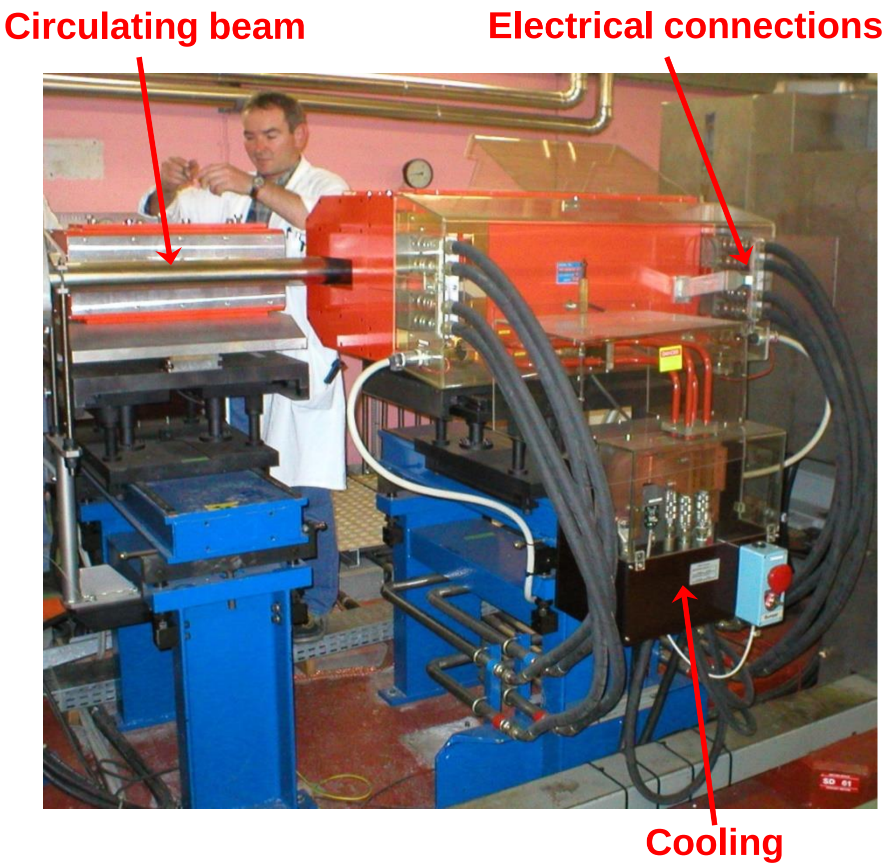
- Thin septum ~ 0.1 mm needed for high extraction efficiency:
  - Foils typically used
  - Stretched wire arrays provide thinner septa and lower effective density
- Challenges include conditioning and preparation of HV surfaces, vacuum in range of 10^{-9} – 10^{-12} mbar and in-vacuum precision position alignment

Electrostatic septum

- At SPS we slow-extract 400 GeV protons using approximately 15 m of septum split into 5 separate vacuum tanks each over 3 m long:
  - Alignment of the 60 - 100 μm wire array over 15 m is challenging!

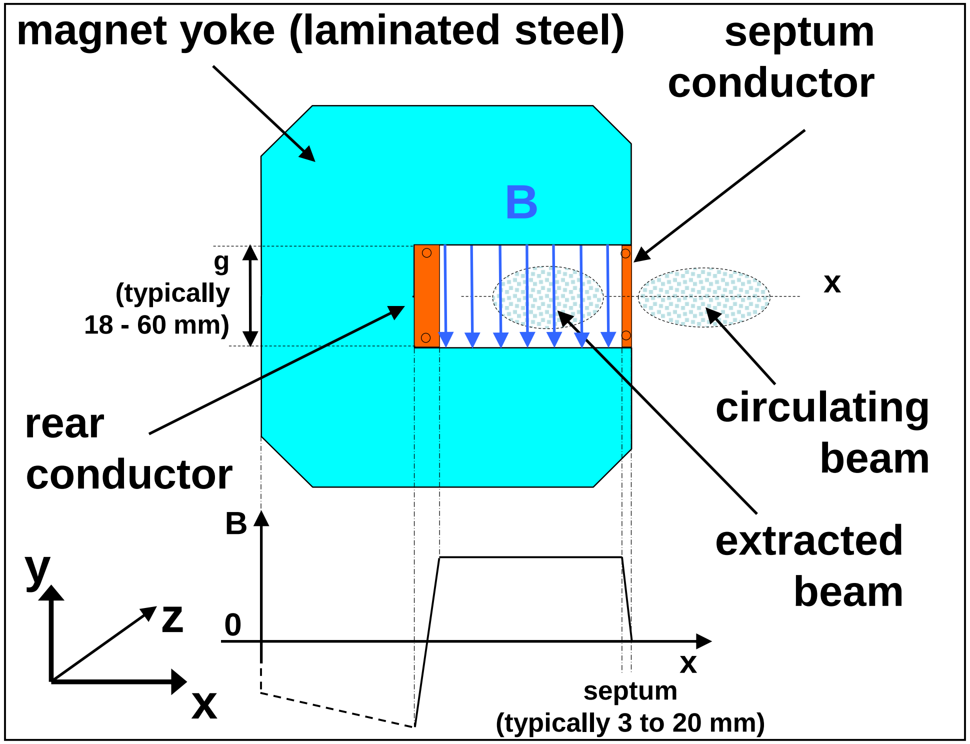
DC direct drive magnetic septum

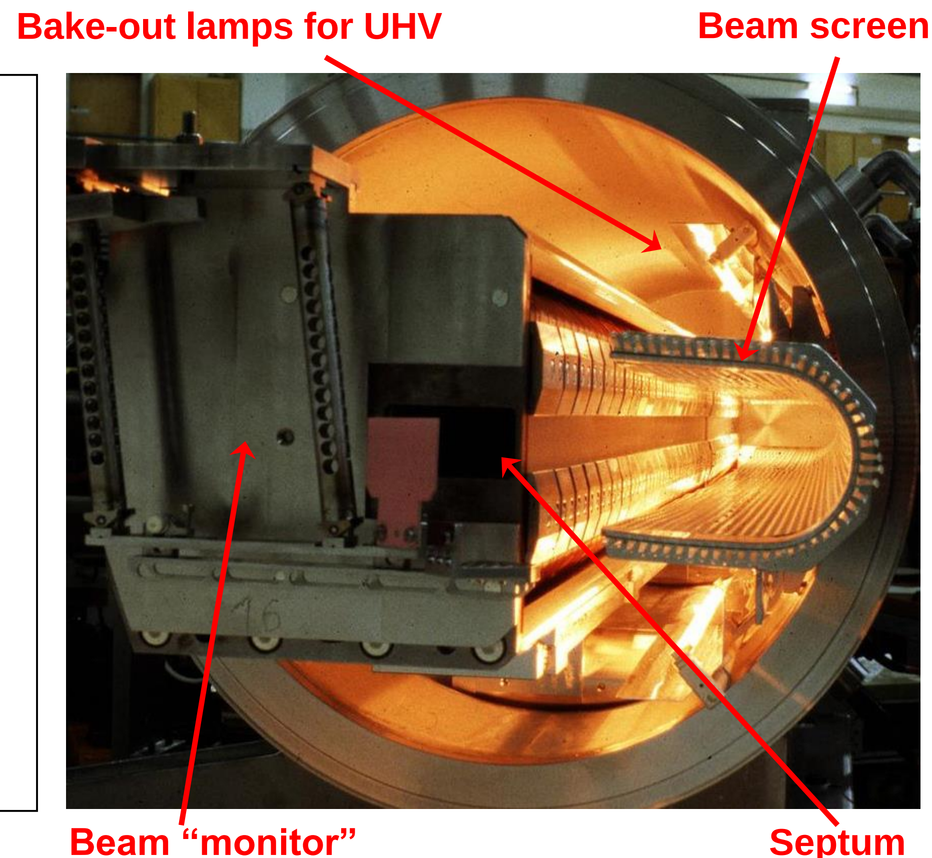




- Continuously powered, rarely under vacuum
- Multi-turn coil to reduce current needed but cooling still an issue:
  - Cooling water circuits flow rate typically at 12 – 60 l/min
  - Current can range from 0.5 to 4 kA and power consumption up to 100 kW!

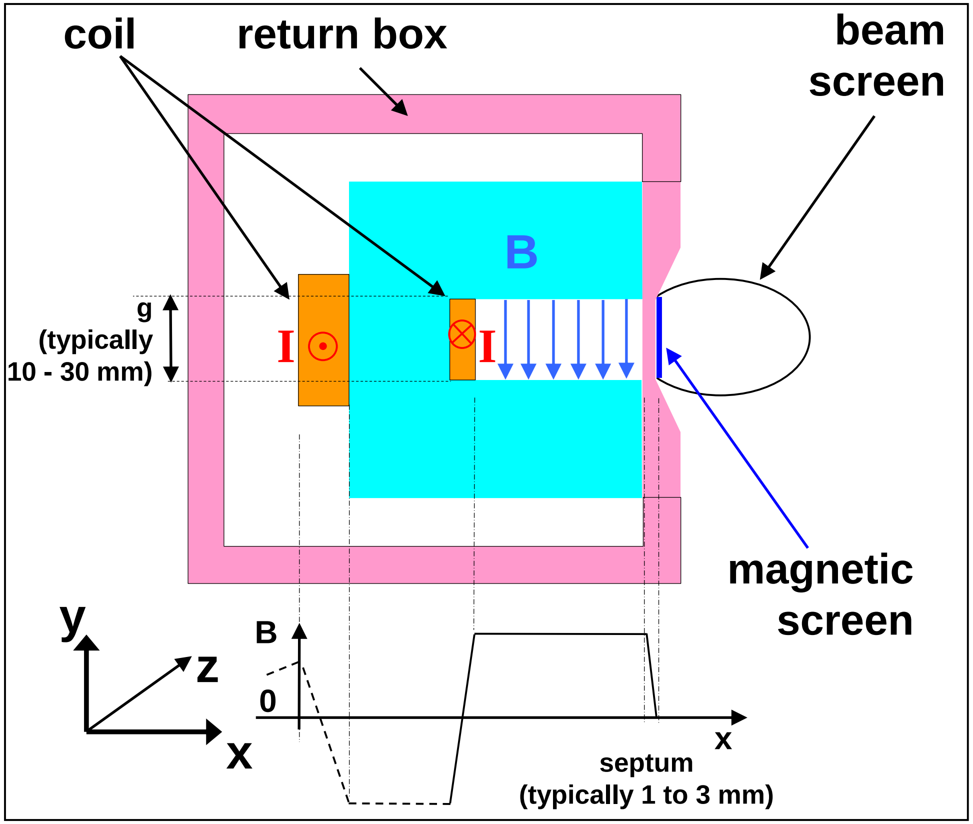
Direct drive **pulsed** magnetic septum





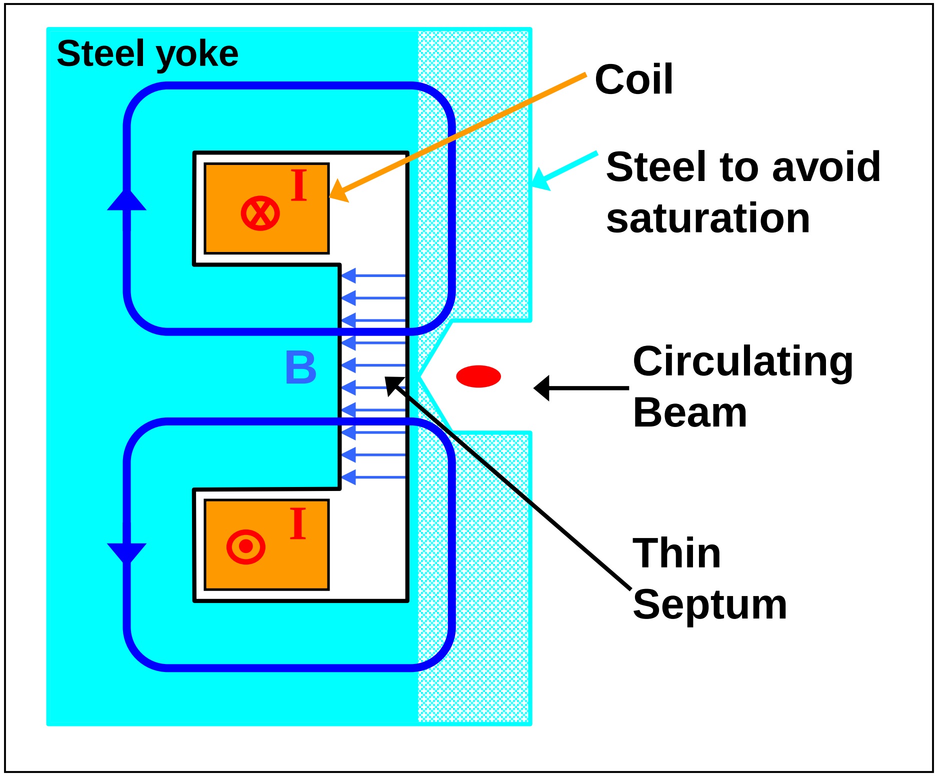
- In vacuum, to minimise distance between circulating and extracted beam
- Single-turn coil to minimise inductance, bake-out up to 200 ° C (~10^{-9} mbar)
- Pulsed by capacitor discharge (third harmonic flattens the pulse):
  - Current in range 7 – 40 kA with a few ms oscillation period
  - Cooling water circuits flow rate from 1 – 80 l/min

Eddy current septum



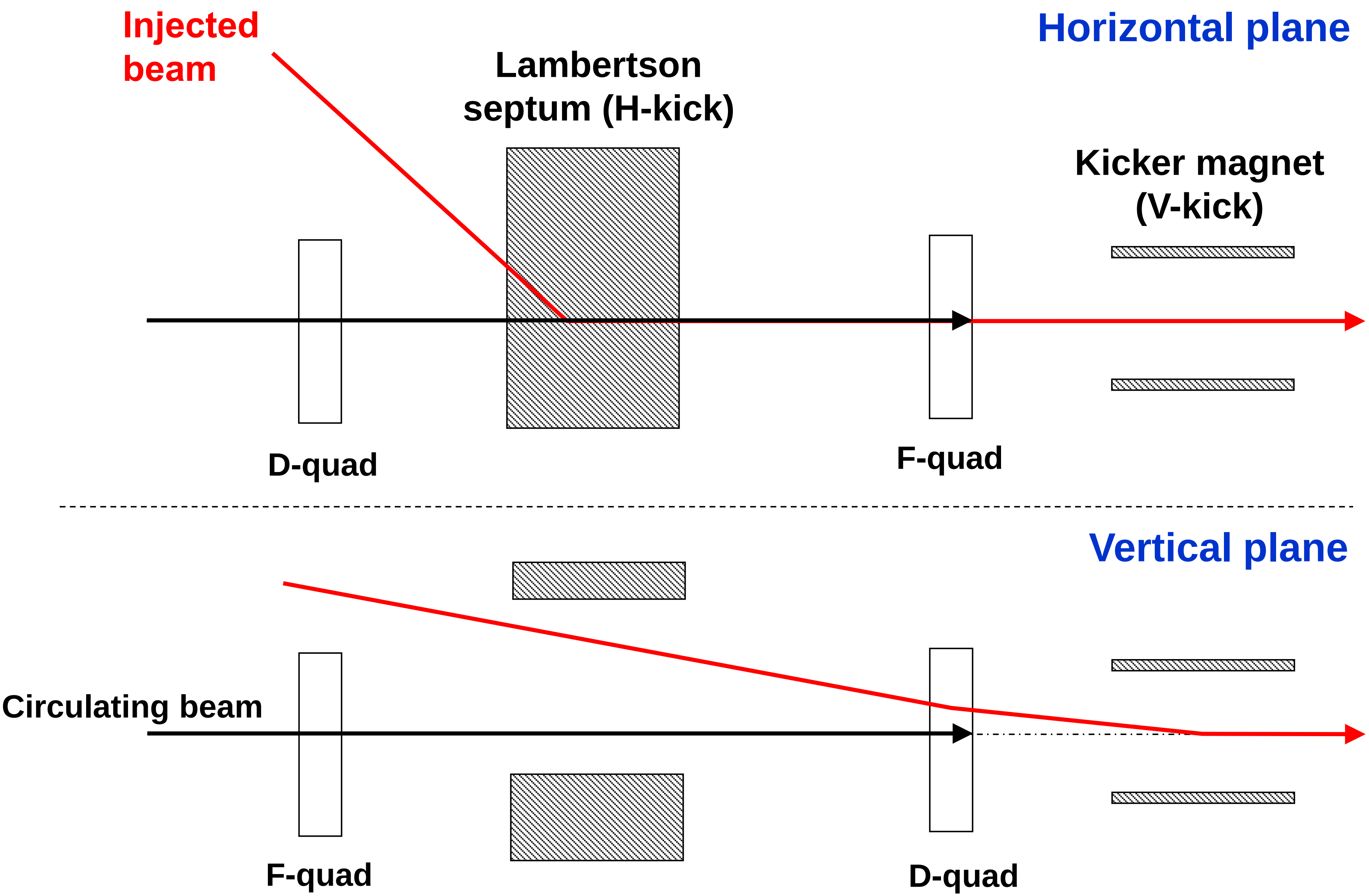
- Coil removed from septum and placed behind C-core yoke:
  - Coil dimension not critical
  - Very thin septum blade
- Magnetic field pulse induces eddy currents in septum blade
- Eddy currents shield the circulating beam from magnetic field
- Return box and magnetic screen reduce fringe field seen by circulating beam
- In or out of vacuum, single-turn coil
- Pulsed by capacitor discharge (third harmonic flattens the pulse):
  - Current ~10 kA fast pulsed with ~ 50 μs oscillation period
  - Cooling water circuits flow rate from 1 – 10 l/min

Lambertson septum



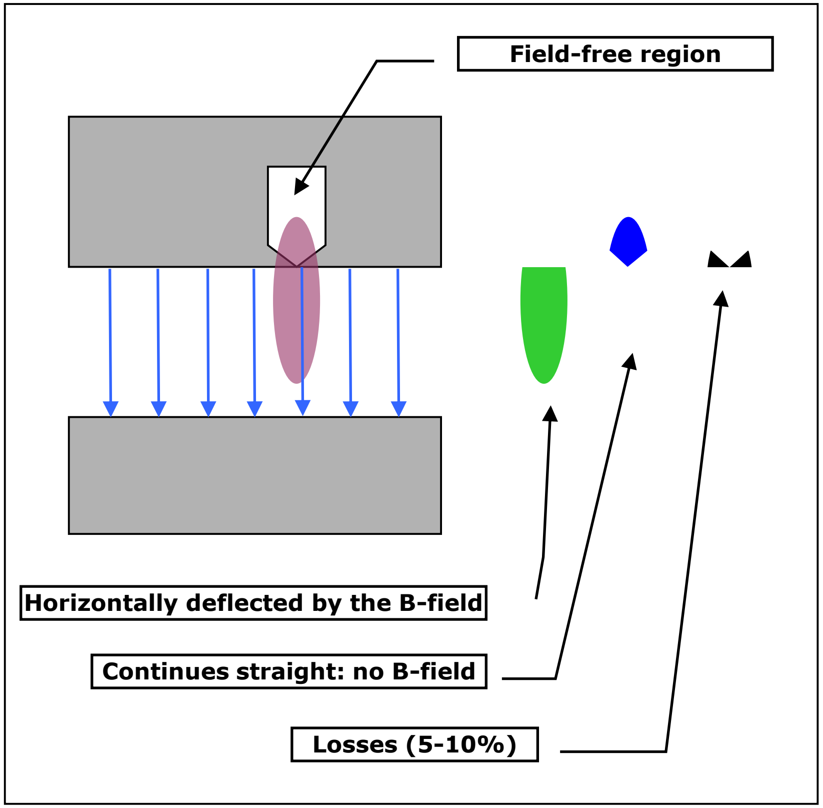
- Magnetic field in gap orthogonal to previous examples of septa:
  - Lambertson deflects beam orthogonal to kicker: dual plane injection/extraction
- Rugged design: conductors safely hidden away from the beam
- Thin steel yoke between aperture and circulating beam – however extra steel required to avoid saturation, magnetic shielding often added

Two plane injection with Lambertson



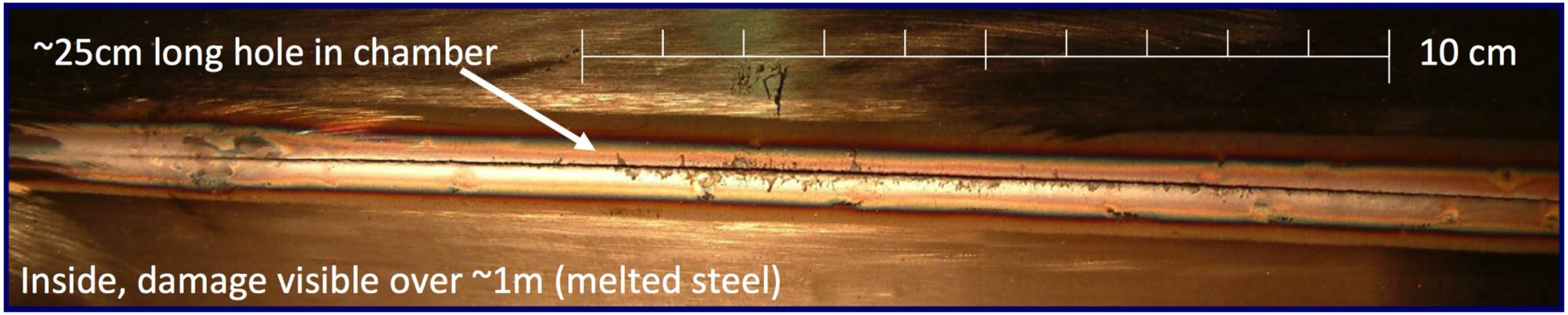
Lambertson septum

- At SPS we use Lambertson septa to split the 400 GeV slow-extracted proton spill (~ seconds) to different target stations simultaneously:
  - These devices are radioactive: critical that coils are located away from the septum



Protection devices

- When things go wrong…!
  - SPS extraction septum power supply tripped during setting-up of LHC beam, 25th October 2004:



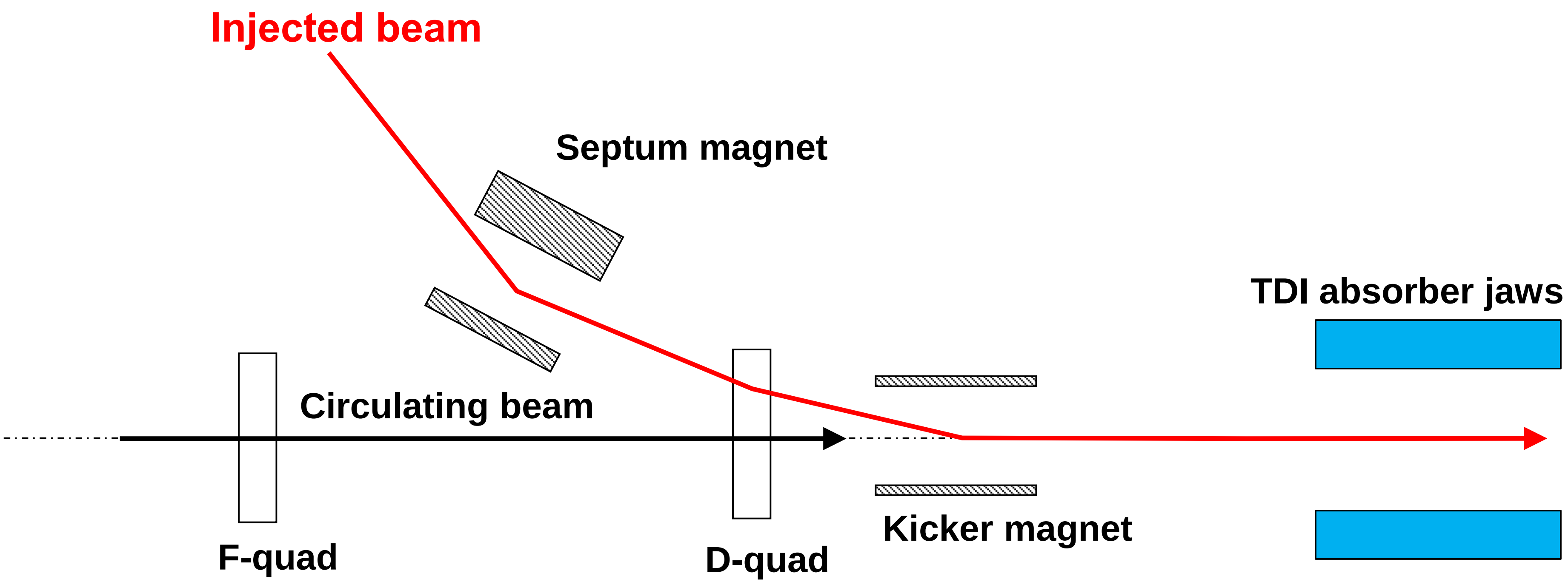
  - Septum field dropped by 5% in 11 ms
  - 3.4×10^{13} protons at 450 GeV, i.e. 2.5 MJ of beam energy dissipated on the aperture of the transfer line
  - Vacuum chamber and quadrupole magnet damaged requiring replacement
  - Upgraded fast interlock system was implemented to protect against such fast failures

Protection devices

- When beam energy exceeds damage limit for machine equipment one has to design for certain failure scenarios
- Critical beam transfer systems have redundancy and multiple layers of protection:
  - Passive protection devices form the last layer of this security
- Protection devices are designed to dilute and absorb beam energy safely
- Failures associated with beam transfer equipment are typically very fast and difficult to catch, for example:
  - No turn-on of kicker: injection protection
  - Erratic turn-on of kicker: sweep circulating beam in the machine
  - Flash-over (short-circuit) in kicker: impart the wrong kicker angle
  - Transfer line magnet failure: steering beam onto aperture of downstream machine

Injection protection: e.g. LHC injection

- LHC has a dedicated injection dump (TDI) to protect against fast failures on the injection kicker



In reality the LHC injection is dual plane: Lambertson septum kick orthogonal to kicker

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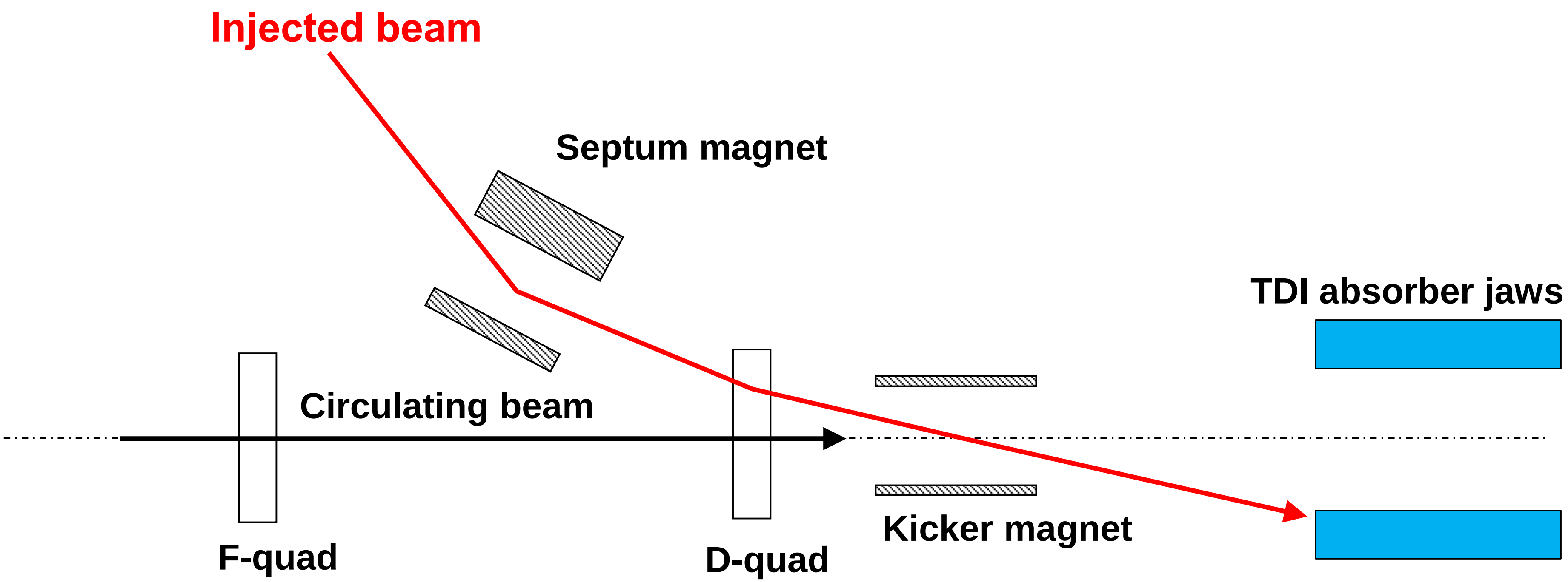

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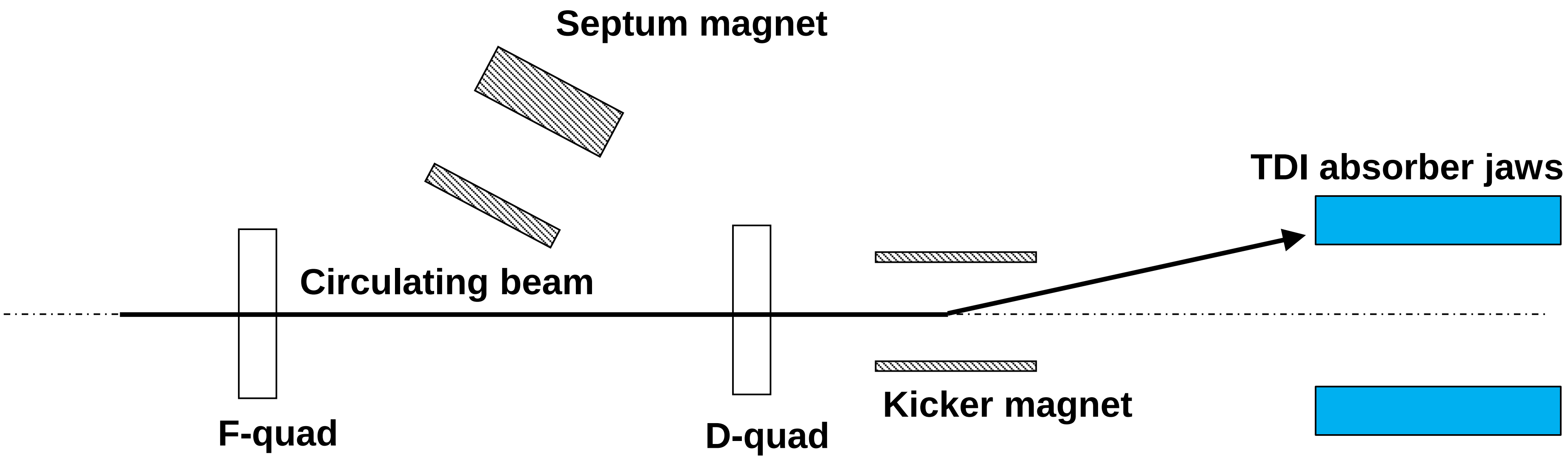

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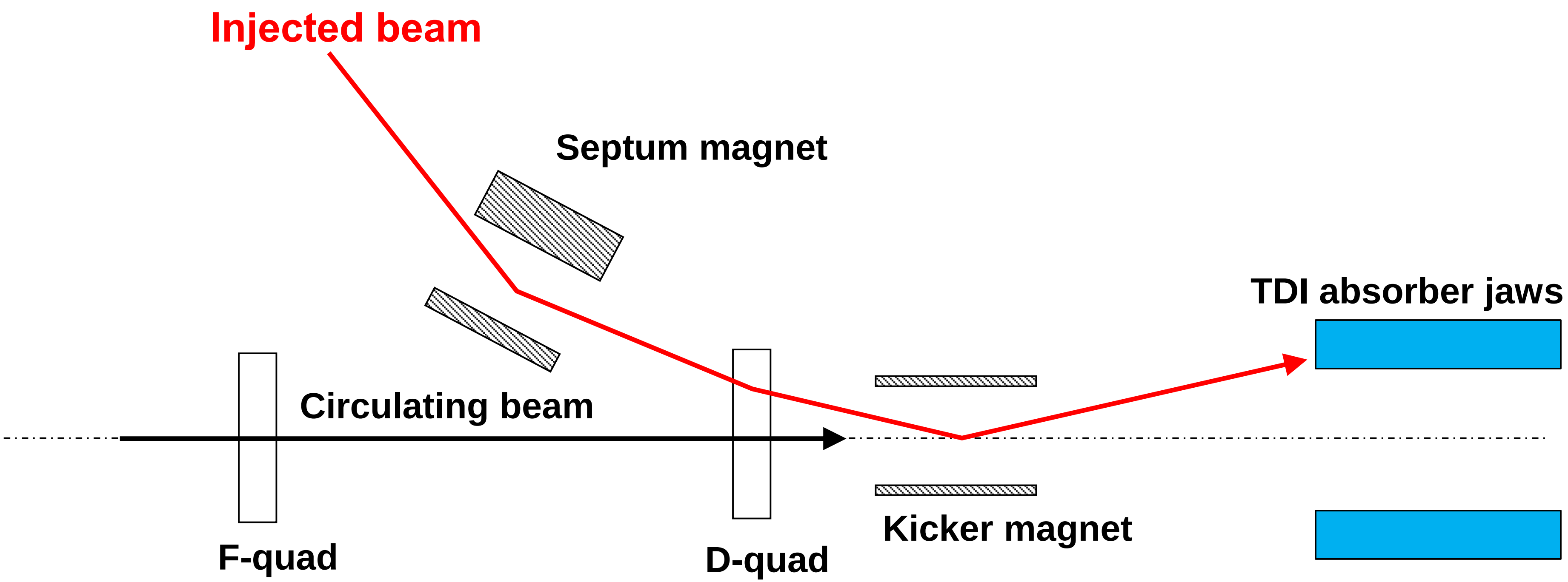
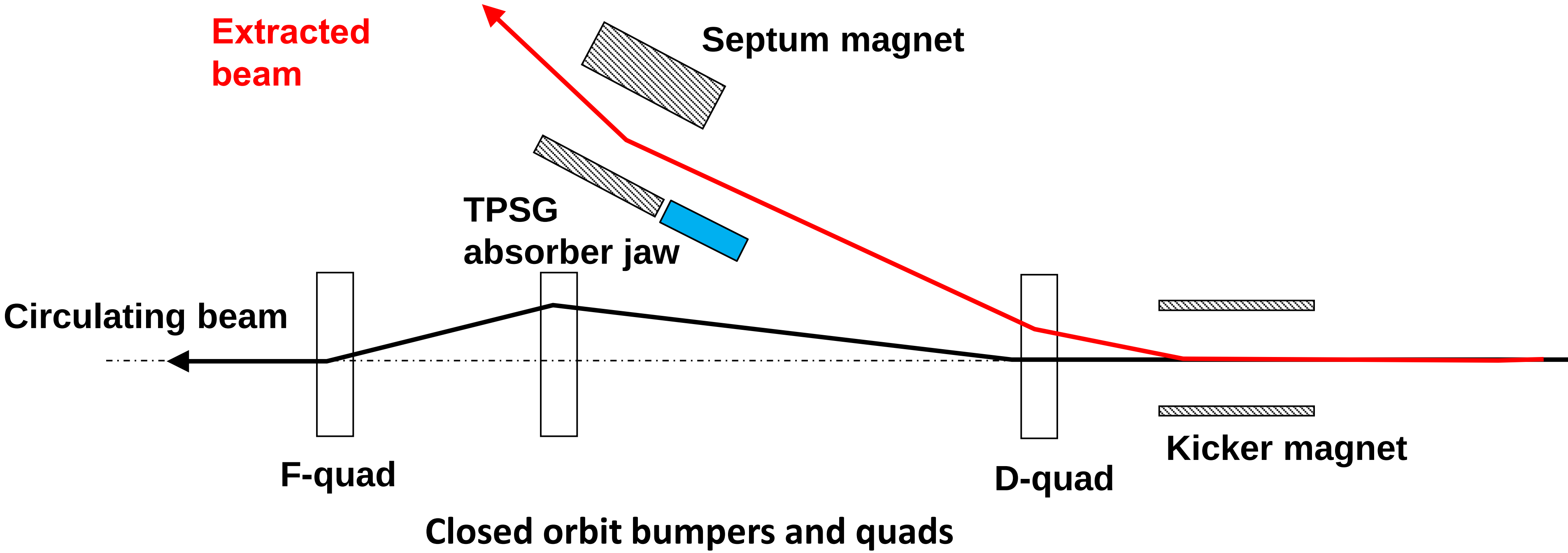
  - No turn-on of kicker: beam steered safely onto absorber
  - Erratic turn-on of kicker: circulating beam steered safely onto absorber
  - Flash-over (short-circuit) in kicker: “worst-case” gives twice deflection:



In reality the LHC injection is dual plane: Lambertson septum kick orthogonal to kicker

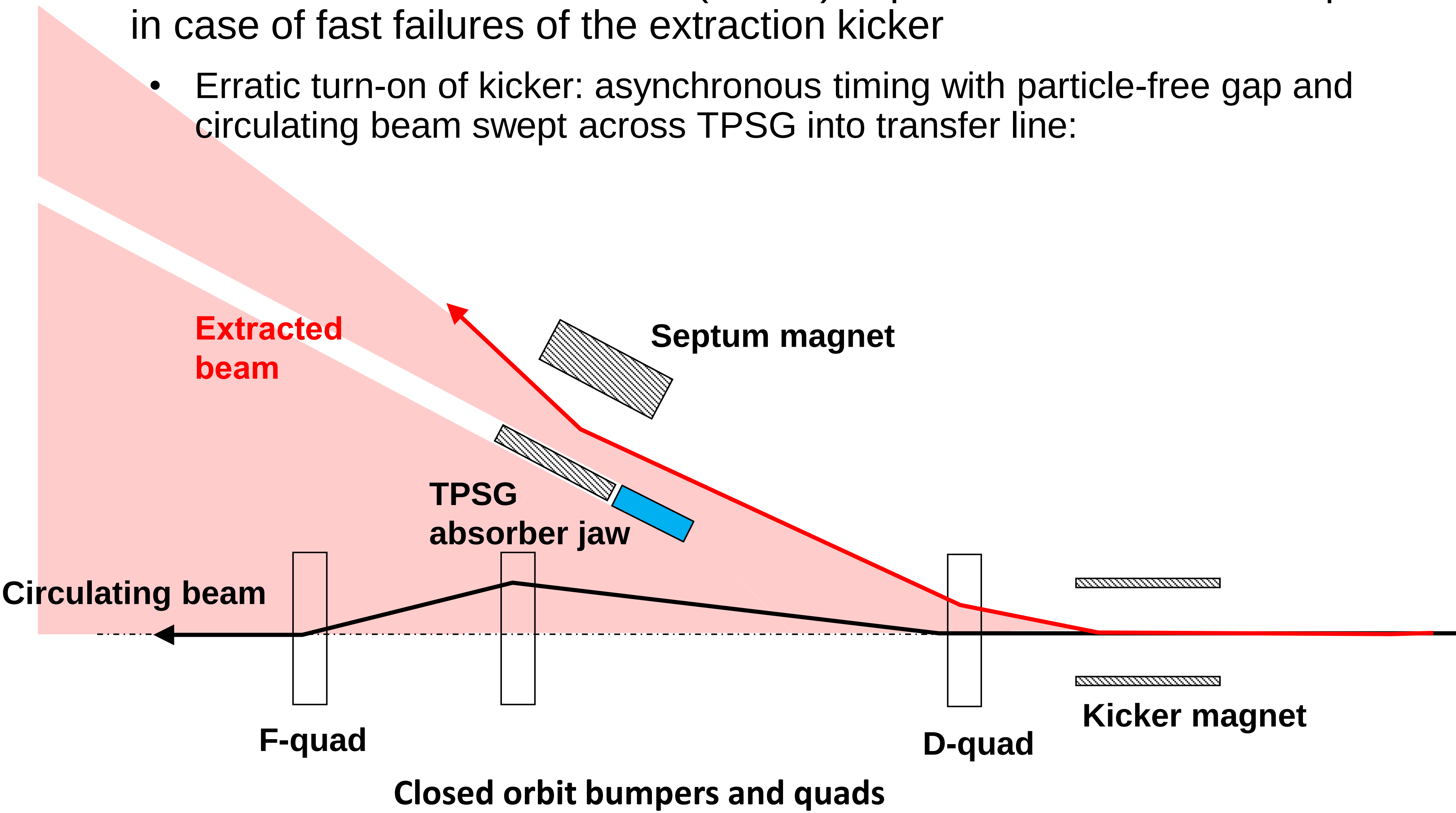
Extraction protection: e.g. SPS extraction

- SPS has a dedicated absorber (TPSG) to protect the extraction septum in case of fast failures of the extraction kicker



Extraction protection: e.g. SPS extraction

- SPS has a dedicated absorber (TPSG) to protect the extraction septum in case of fast failures of the extraction kicker
  - Erratic turn-on of kicker: asynchronous timing with particle-free gap and circulating beam swept across TPSG into transfer line:



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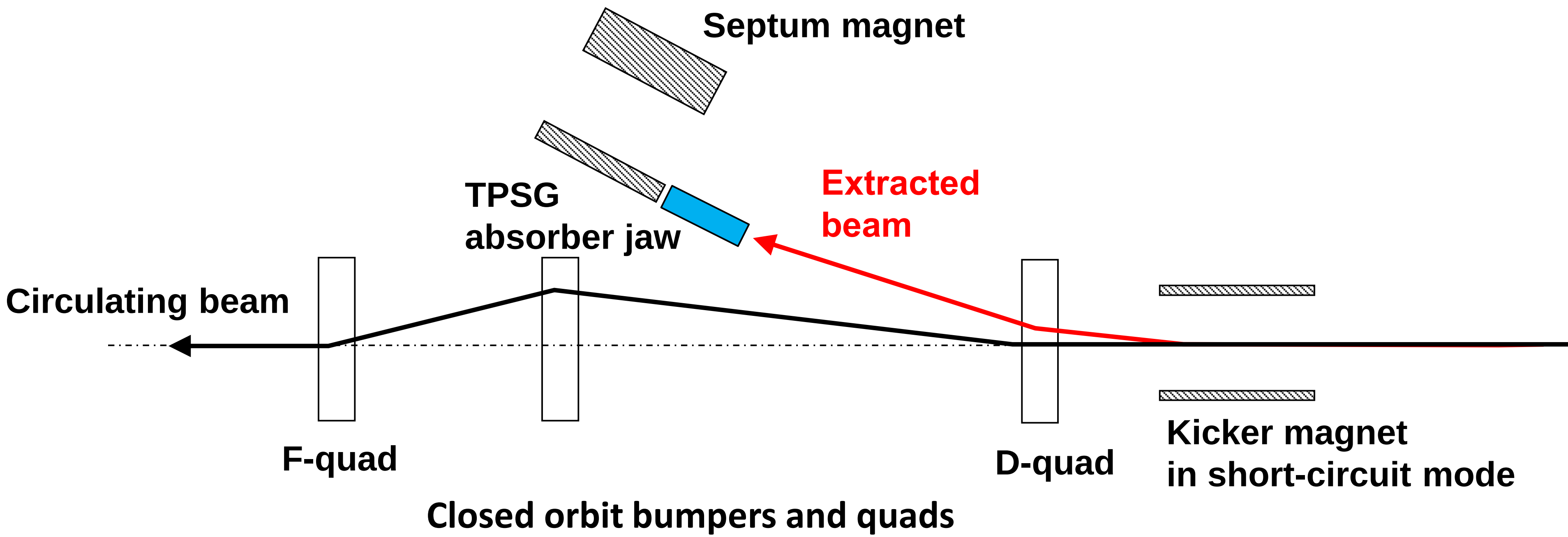
  - Erratic turn-on of kicker: asynchronous timing with particle-free gap and circulating beam swept across TPSG into transfer line
  - Flash-over (short-circuit) in kicker: worst-case amplitude places the extracted beam onto the absorber jaw:



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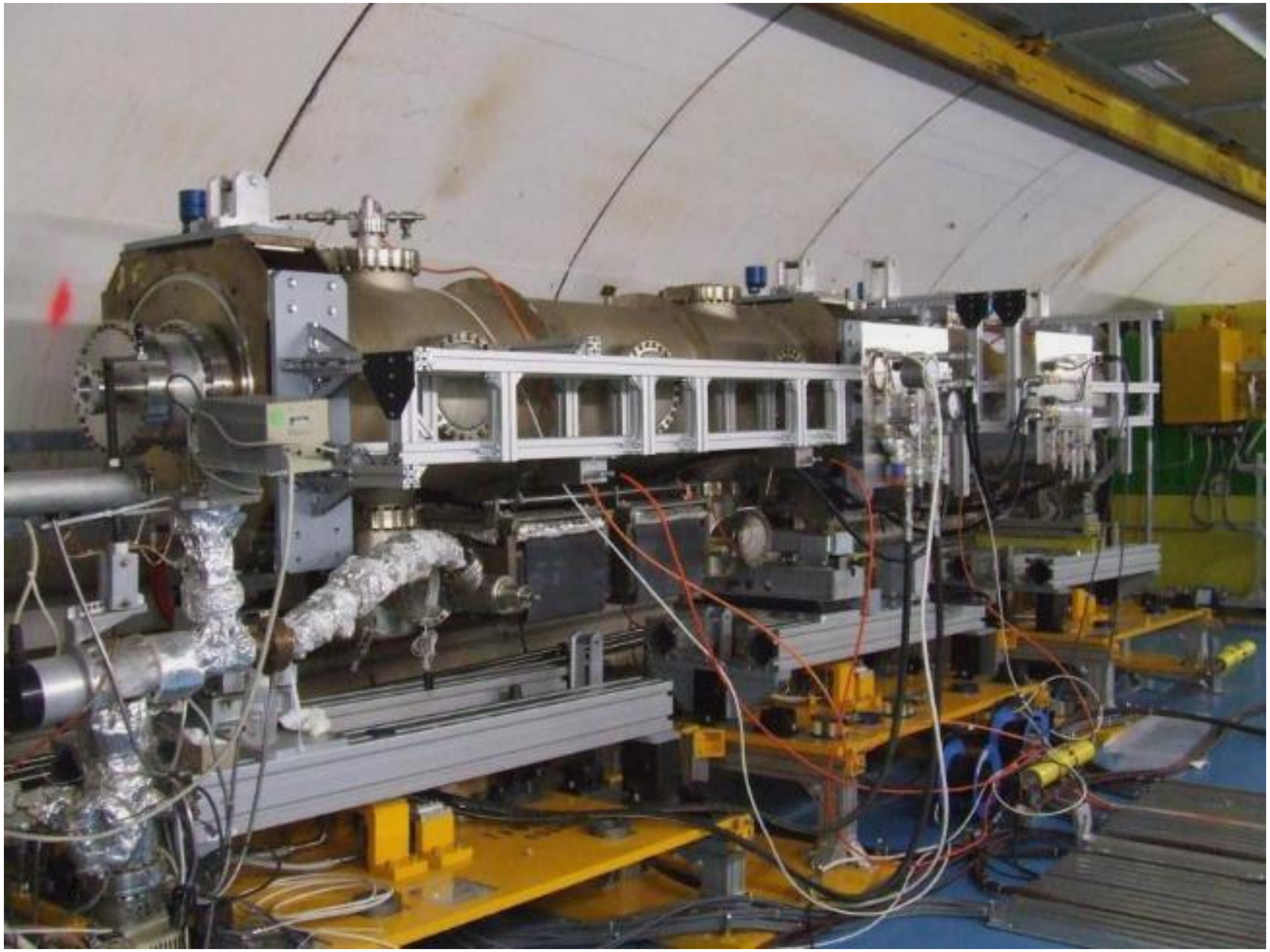
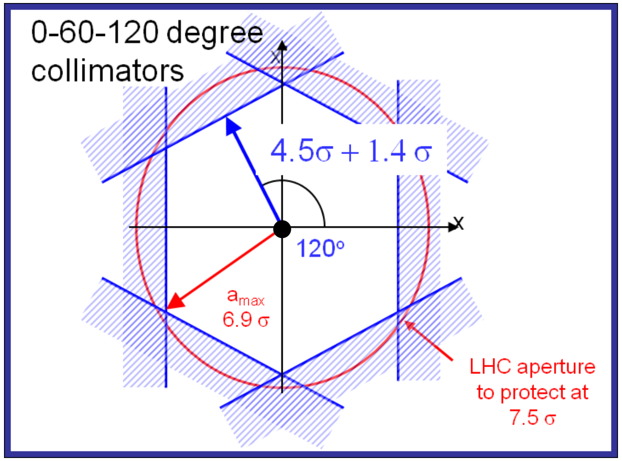
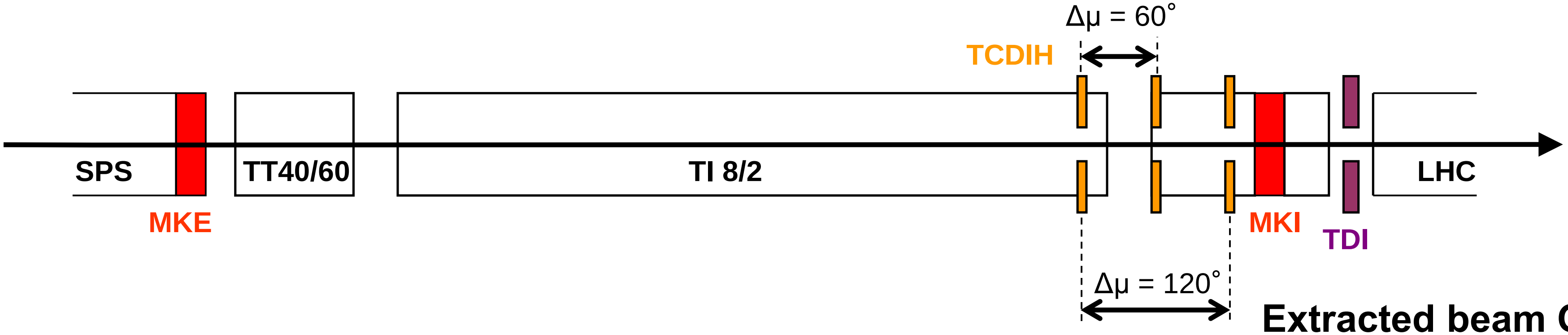


TPSG and MSE (magnetic septum) installed at HIRADMAT irradiation test facility in 2012: impacted with LHC nominal intensity (288b and 1.1 ×10^{11} p/b): both devices survived!

Transfer protection: e.g. SPS-to-LHC

- SPS to LHC transfer lines have dedicated transfer line collimators (TCDIH and V) in case of fast failures to protect LHC aperture:





Extracted beam ON nominal trajectory

Transfer protection: e.g. SPS-to-LHC

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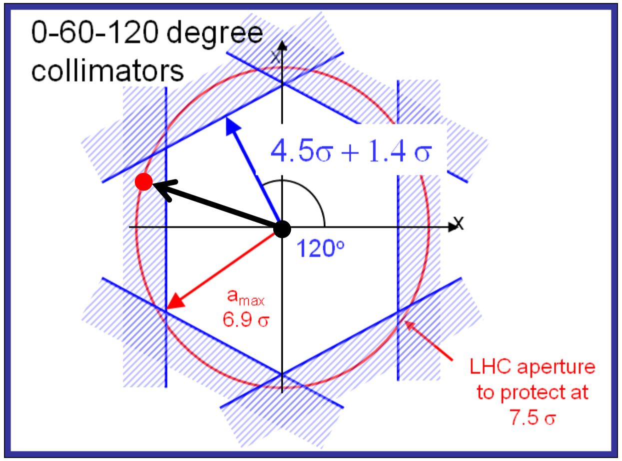
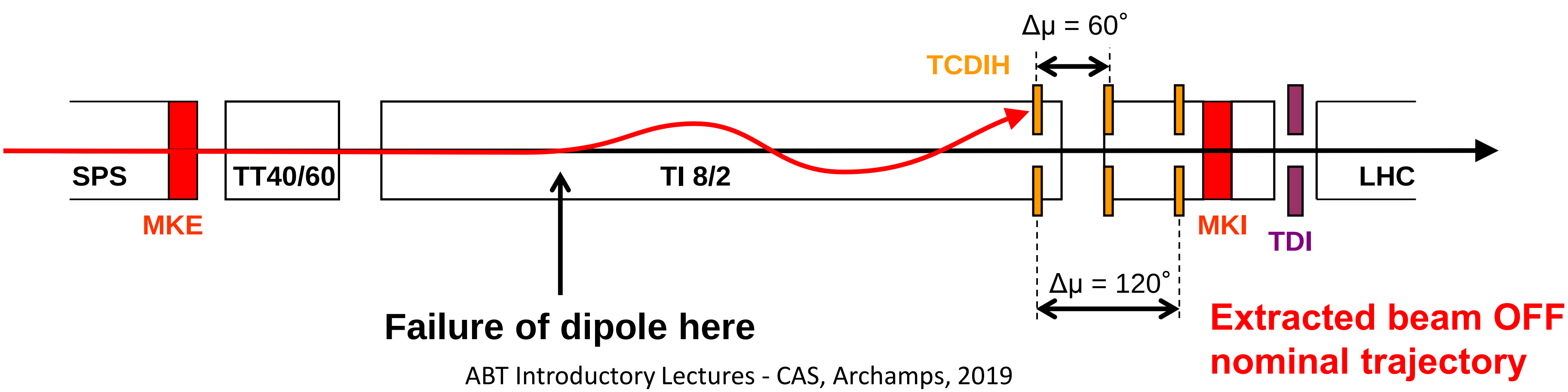
  - Magnet power supply trips at time *t* after the last extraction interlock check: beam steered onto collimator
  - Current (field) error depends on circuit:

$$\Delta I_{error}(t) = I_{nom}(1 - e^{-t/\tau}) \qquad \tau = \frac{L_{mag}}{R}$$





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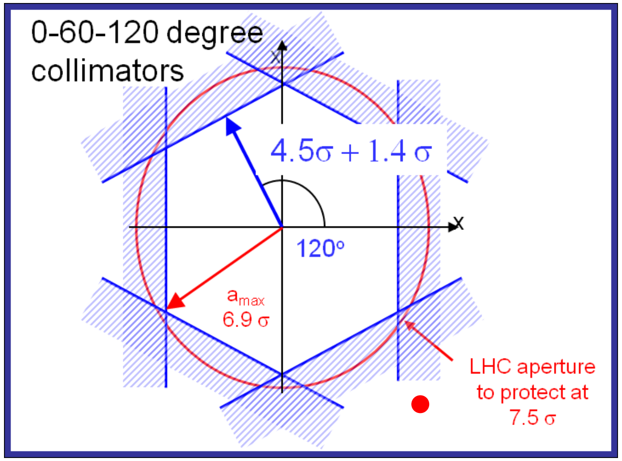

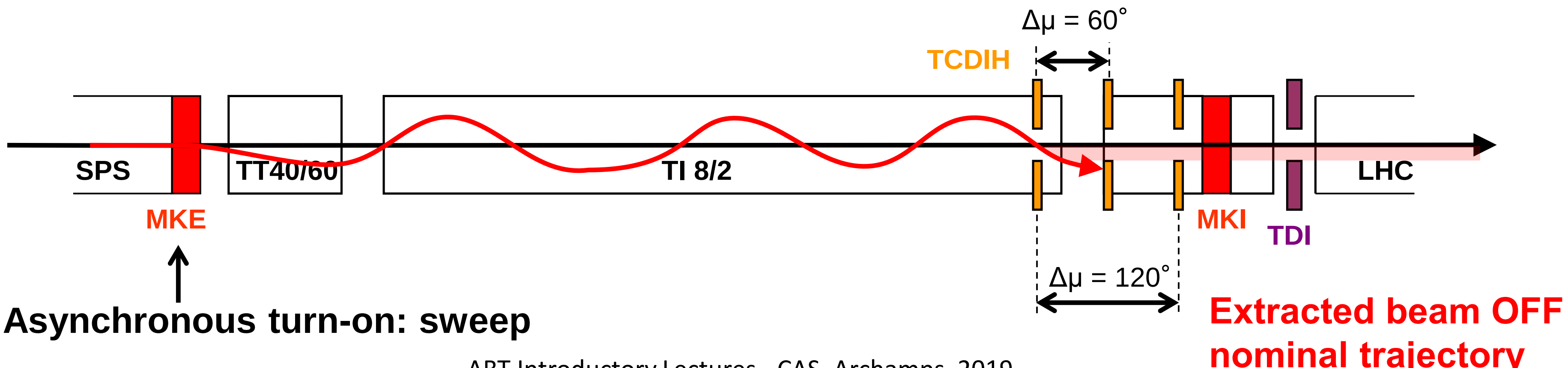

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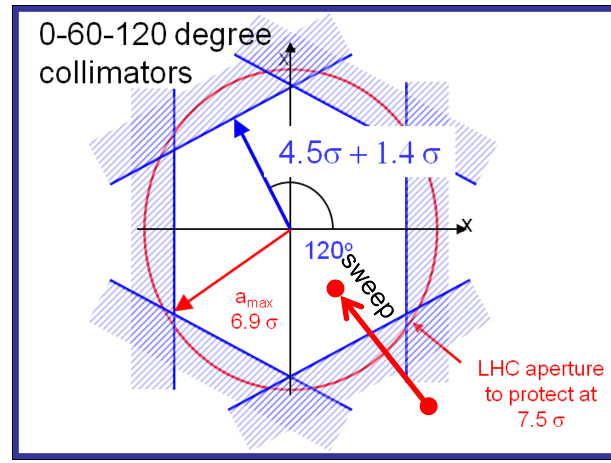

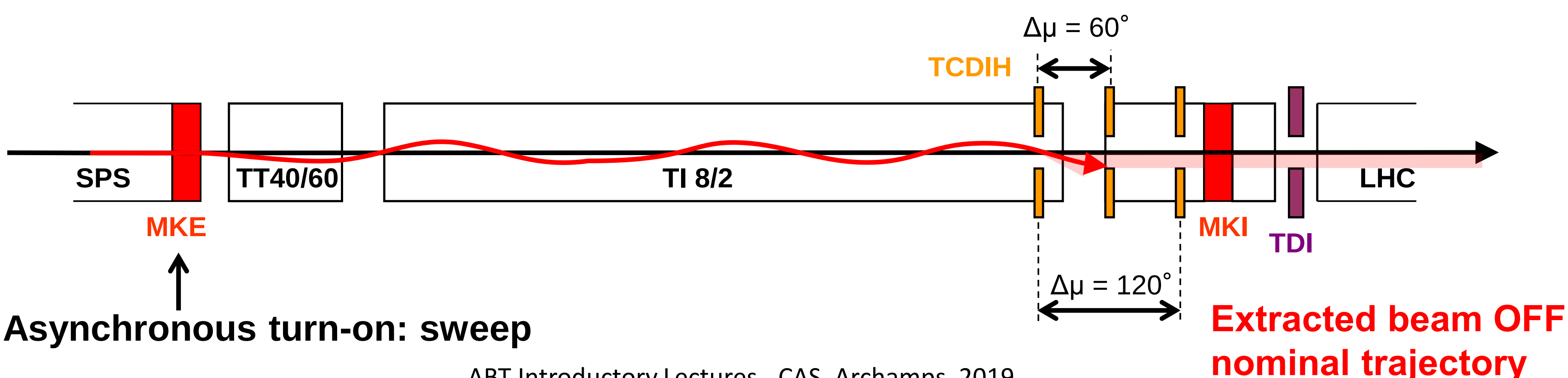

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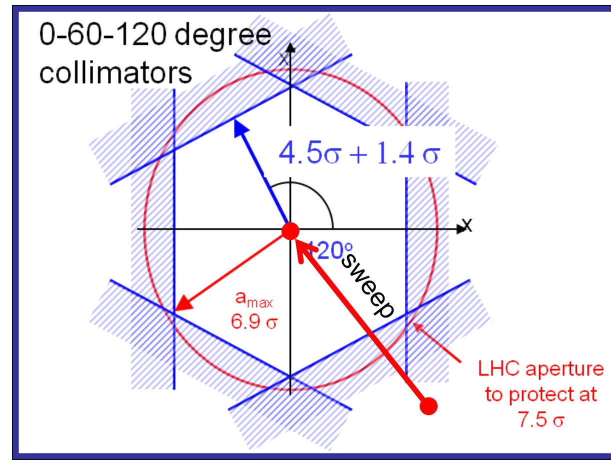

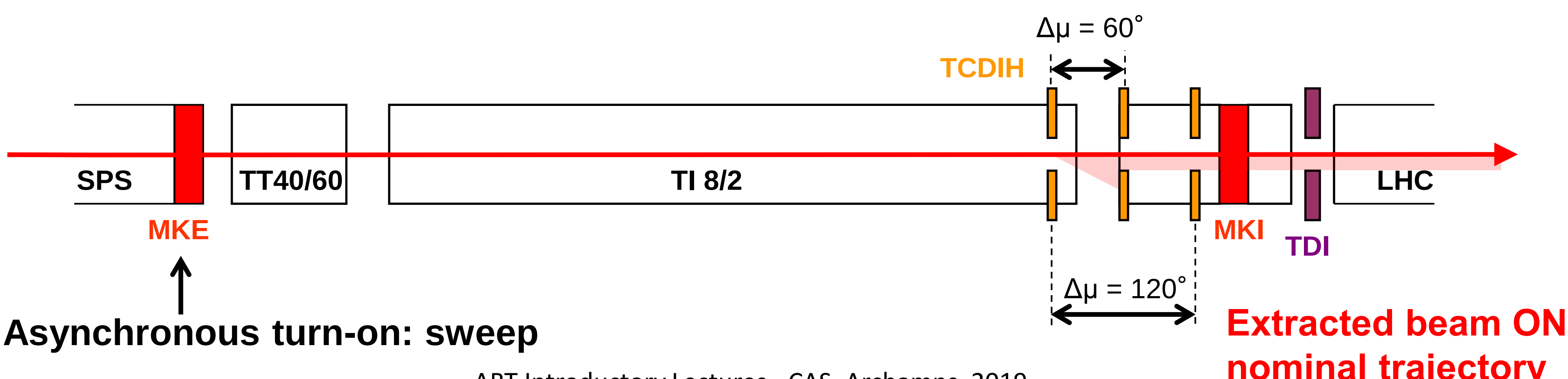

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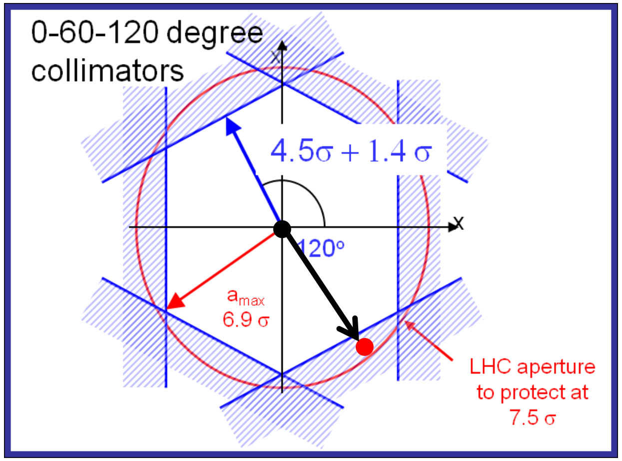

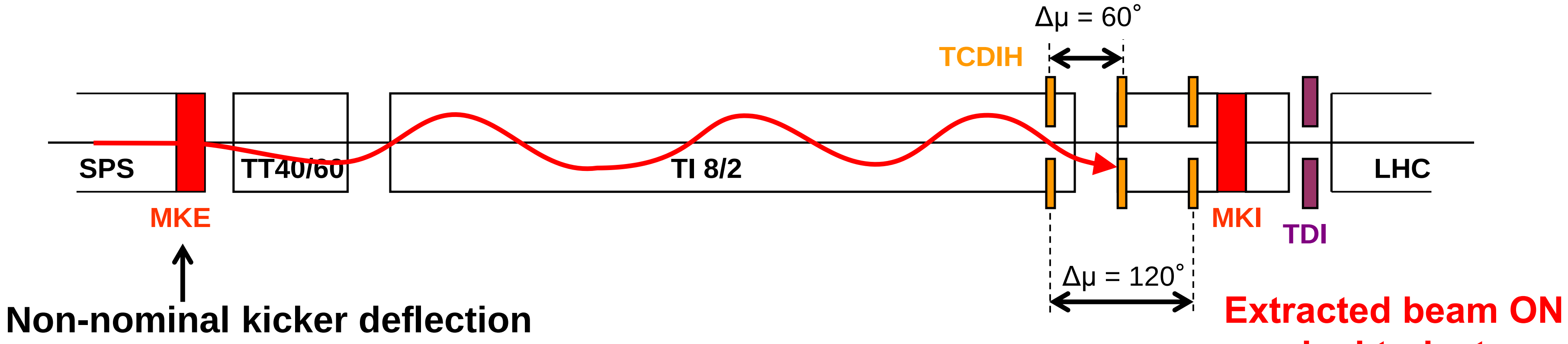

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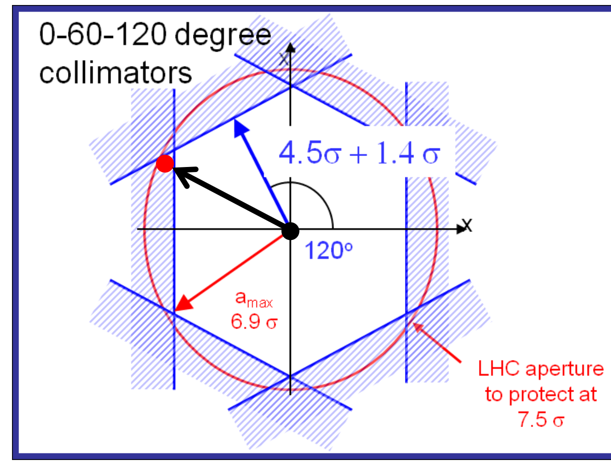
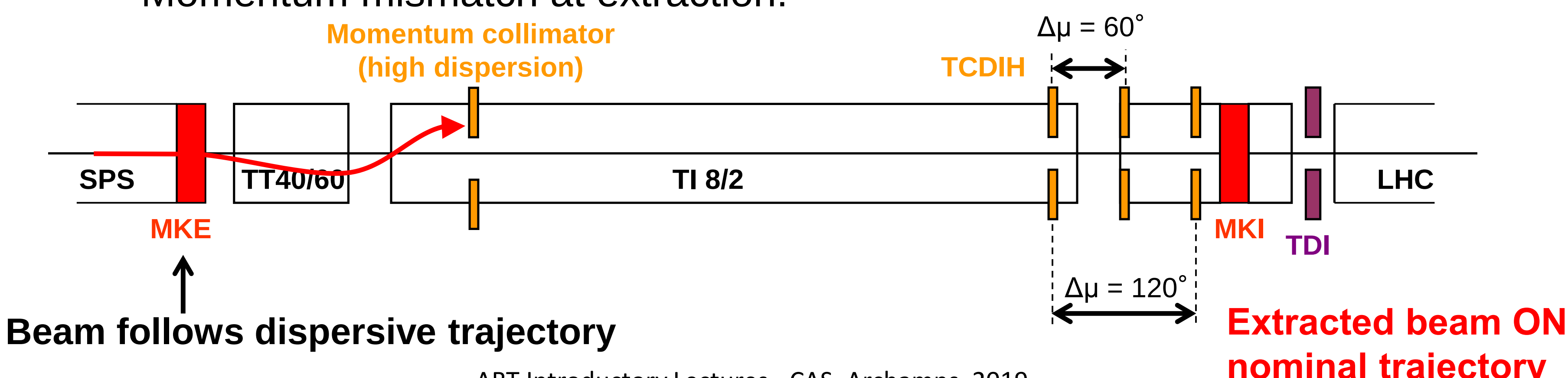
  - Erratic turn-on of extraction kicker: sweep (asynchronous with particle-free abort gap)
  - Flash-over (short-circuit) in kicker
  - Momentum mismatch at extraction:

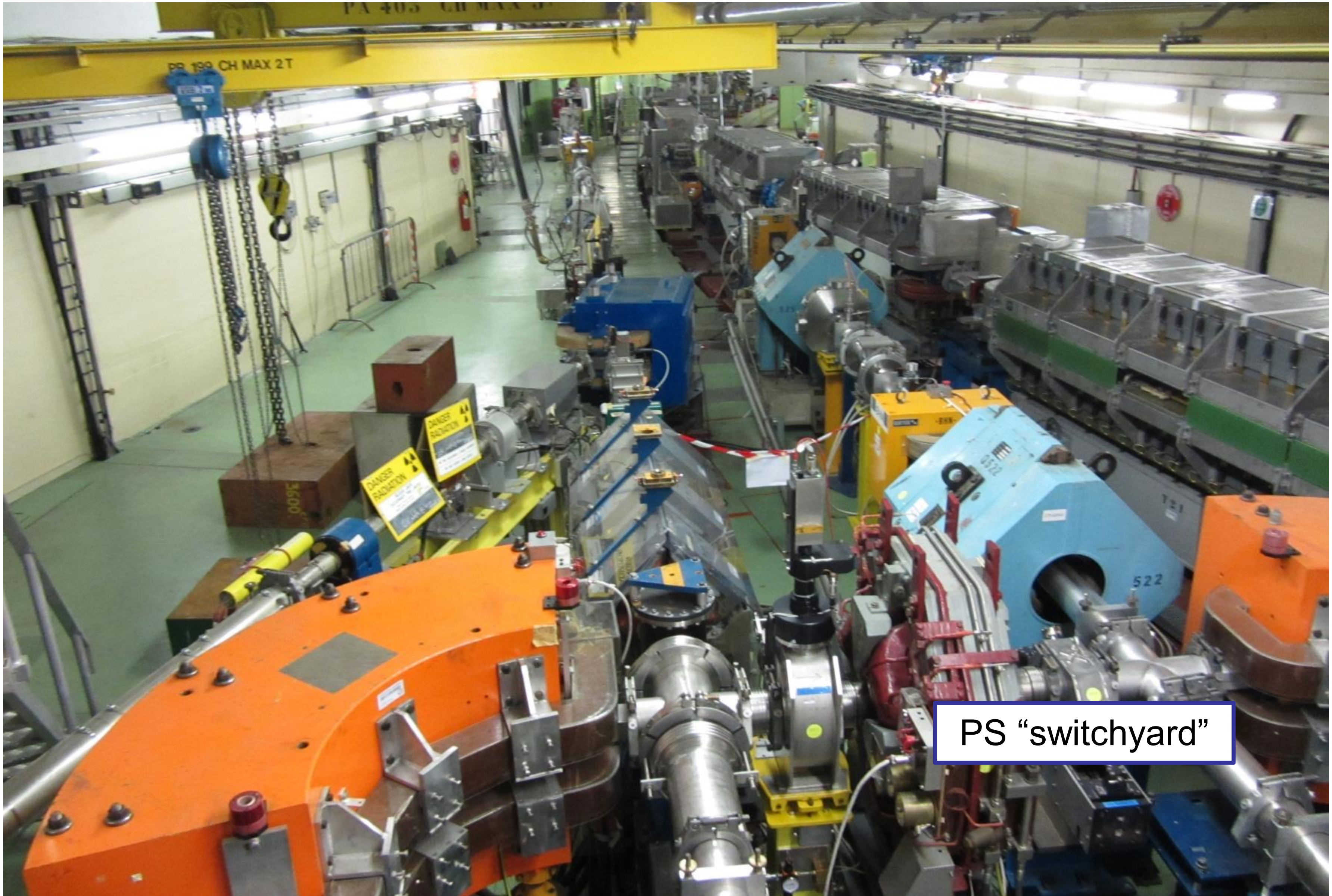




Beam transfer lines

LHC beam dump
extraction line
(TD62/68)

Beam transfer lines



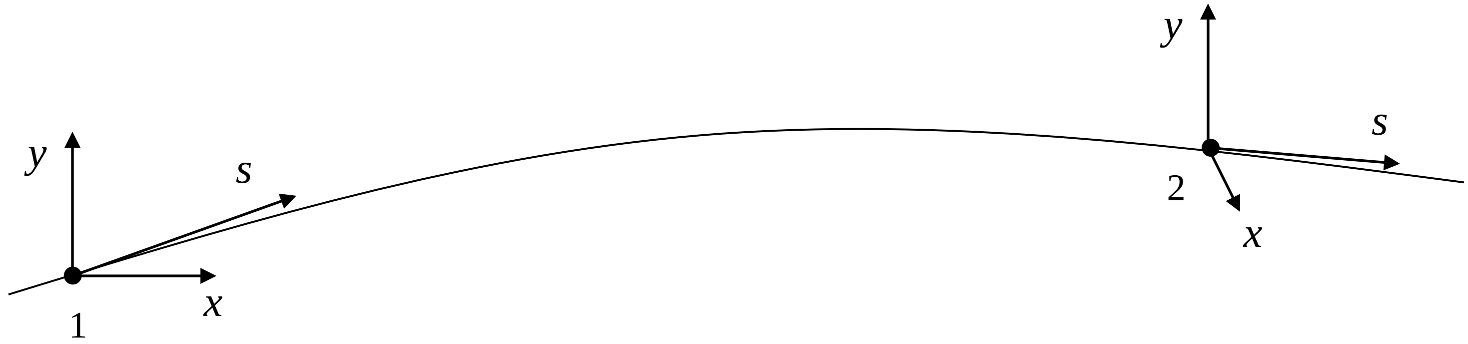
Beam transfer lines

Transfer lines transport beams between accelerators (extraction of one to injection of the next) and on to experimental targets and beam dumps

- Requirements:
  - Geometric link between machines/experiment
  - Match optics between machines/experiment
  - Preserve emittance
  - Change particles' charge state (stripping foils)
  - Measure beam parameters (measurement lines)
  - Protect downstream machine/experiment

General transport

Beam transport: moving from s_1 to s_2 through *n* elements, each with transfer matrix M_i



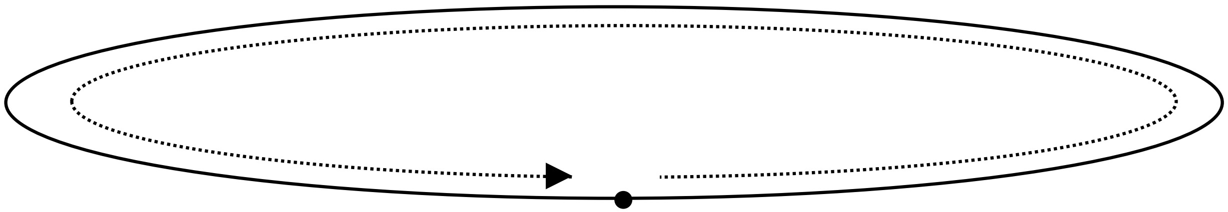
$$\begin{bmatrix} x_2 \\ x_2' \end{bmatrix} = \mathbf{M}_{1\to 2} \cdot \begin{bmatrix} x \\ x' \end{bmatrix} = \begin{bmatrix} C & S \\ C' & S' \end{bmatrix} \cdot \begin{bmatrix} x \\ x' \end{bmatrix} \qquad \mathbf{M}_{1\to 2} = \prod_{i=1}^{n} \mathbf{M}_n$$

The transfer matrix (M_i) can be expressed using the Twiss formalism:

$$\mathbf{M}_{1\to 2} = \begin{bmatrix} \sqrt{\beta_2/\beta_1}\left(\cos\Delta\mu + \alpha_1 \sin\Delta\mu\right) & \sqrt{\beta_1\beta_2}\sin\Delta\mu \\ \sqrt{1/\beta_1\beta_2}\left[\left(\alpha_1 - \alpha_2\right)\cos\Delta\mu - \left(1+\alpha_1\alpha_2\right)\sin\Delta\mu\right] & \sqrt{\beta_1/\beta_2}\left(\cos\Delta\mu - \alpha_2\sin\Delta\mu\right) \end{bmatrix}$$

Circular Machine

Circumference = L



One turn:

$$\Delta\mu = 2\pi Q$$

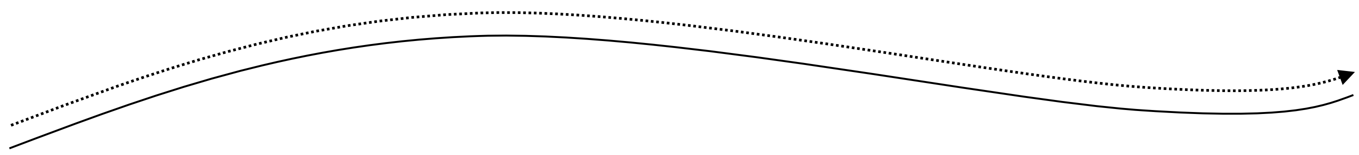
$$\mathbf{M}_{1\to 2} = \mathbf{M}_{0\to L} = \begin{bmatrix} \cos 2\pi Q + \alpha \sin 2\pi Q & \beta \sin 2\pi Q \\ -\frac{1}{\beta}\left(1+\alpha^2\right)\sin 2\pi Q & \cos 2\pi Q - \alpha \sin 2\pi Q \end{bmatrix}$$

- The solution is *periodic*
- Periodicity condition for one turn (closed ring) imposes $\alpha_1 = \alpha_2$, $\beta_1 = \beta_2$, $D_1 = D_2$
- This condition *uniquely* determines α(*s*), β(*s*), μ(*s*), D(s) around the whole ring
  - i.e. a single matched ellipse exists for each given location, *s*

Transfer line

One pass: $$\begin{bmatrix} x_2 \\ x_2' \end{bmatrix} = \mathbf{M}_{1\to2} \cdot \begin{bmatrix} x_1 \\ x_1' \end{bmatrix}$$

$$\begin{bmatrix} x_1 \\ x_1' \end{bmatrix}$$



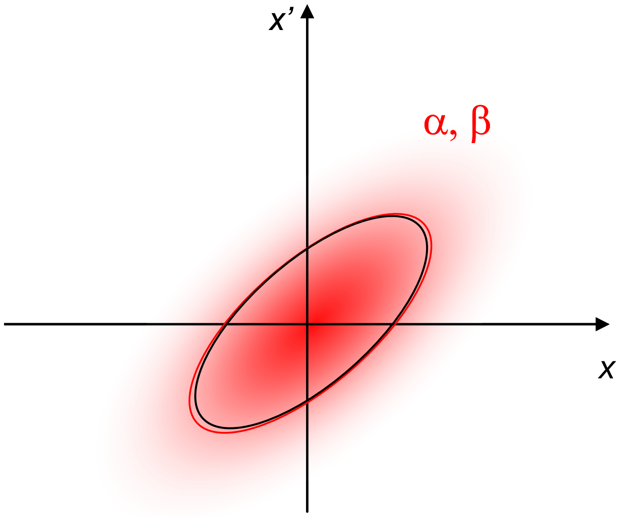
$$\begin{bmatrix} x_2 \\ x_2' \end{bmatrix}$$

$$\mathbf{M}_{1\to2} = \begin{bmatrix} \sqrt{\beta_2/\beta_1}\left(\cos\Delta\mu + \alpha_1 \sin\Delta\mu\right) & \sqrt{\beta_1\beta_2}\sin\Delta\mu \\ \sqrt{1/\beta_1\beta_2}\left[\left(\alpha_1-\alpha_2\right)\cos\Delta\mu - \left(1+\alpha_1\alpha_2\right)\sin\Delta\mu\right] & \sqrt{\beta_1/\beta_2}\left(\cos\Delta\mu - \alpha_2\sin\Delta\mu\right) \end{bmatrix}$$

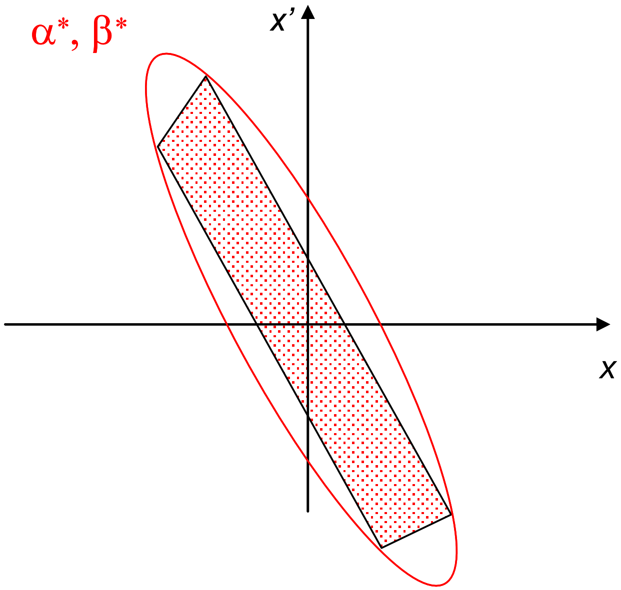
- No periodic condition exists
- The Twiss parameters are simply propagated from beginning to end of line
- At any point in line, α(s) β(s) are functions of α_1 and β_1

Transfer line

- Initial α, β are defined for a transfer line by the beam shape at the entrance



Gaussian beam

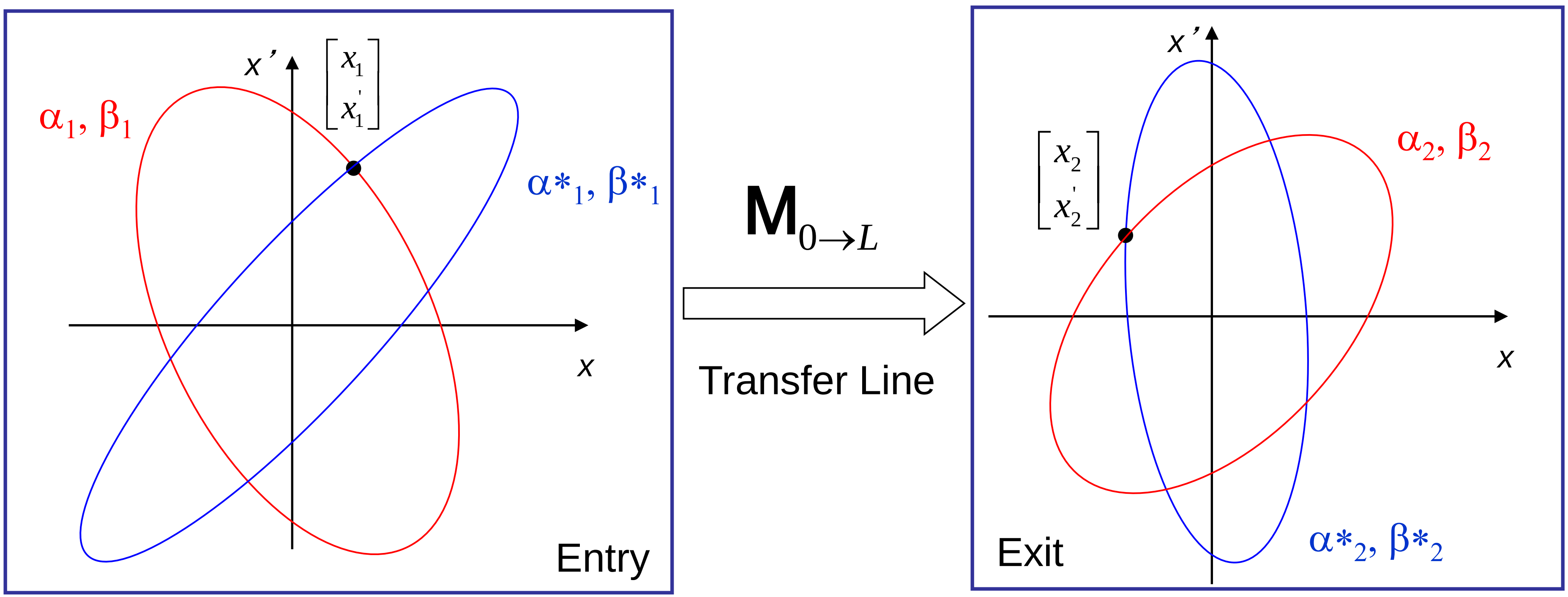


Non-Gaussian beam
(e.g. slow extracted)

- Propagation of this beam ellipse depends on the line
- A transfer line optics is different for different input beams:
  - Synchrotrons are often multi-purpose, accelerating different beams but extracting through a common line transfer line: optics must switch to match the input and output conditions for each beam type

Transfer line

- On a single pass of a finite transfer line there is no regular motion from entrance to exit
  - Periodicity is not enforced: it's actually a design choice
  - Infinite number of possible starting ellipses are transported to an infinite number of final ellipses



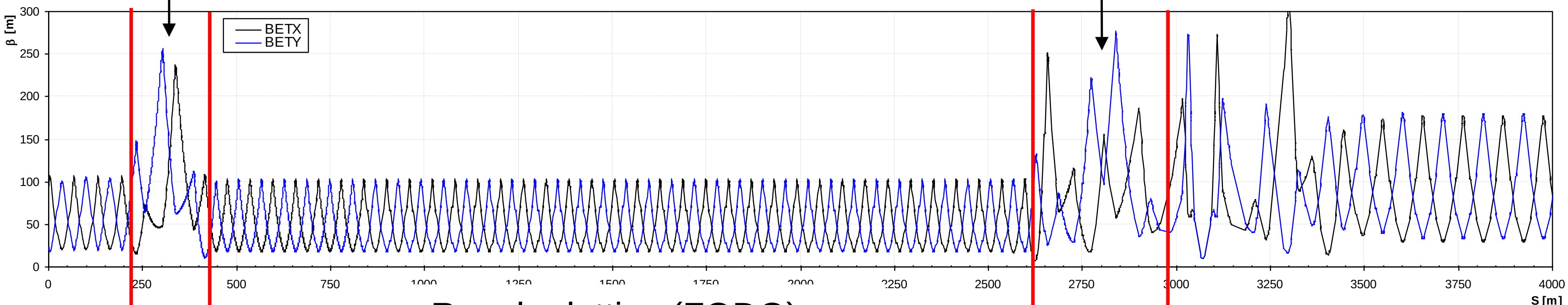
Optics Matching

Initial matching section

Independently powered (tuneable) quadrupoles

Final matching section

Independently powered (tuneable) quadrupoles and (in this case) passive protection devices



SPS

Regular lattice (FODO)
(elements all powered in series
with same strengths)

LHC

SPS to LHC Transfer Line (3 km)

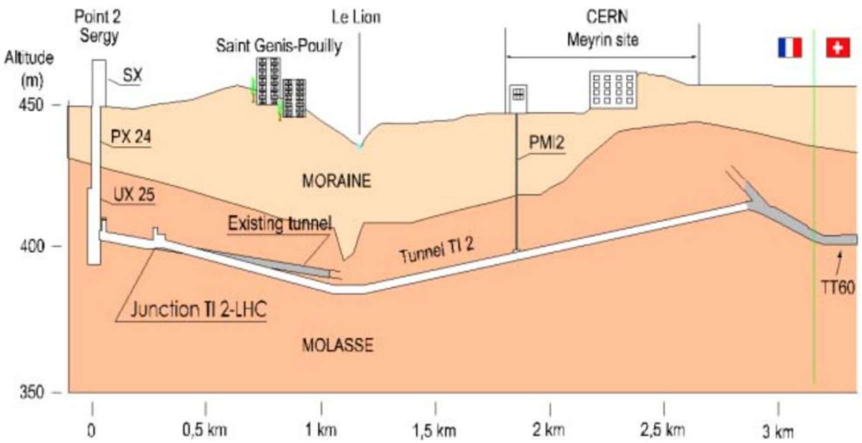
Extraction point

Injection point

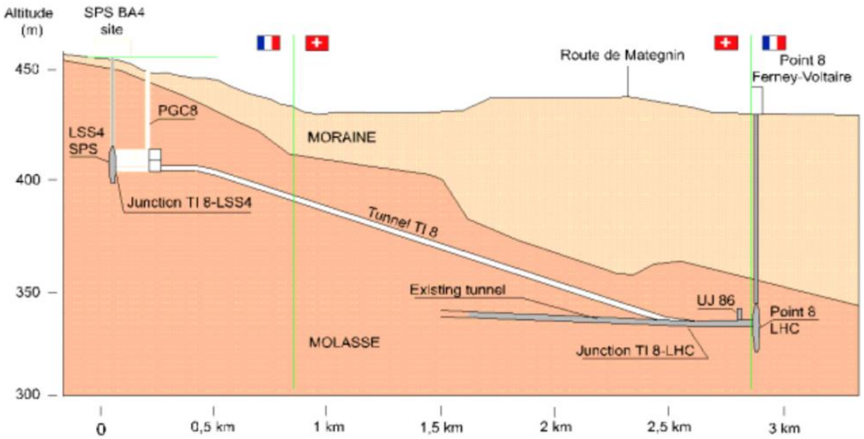
Linking Machines

- Beams have to be transported from extraction of one machine to injection of the next machine:
  - Trajectory must be matched in all 6 geometric degrees of freedom (x,y,z,θ,Φ,ψ)

- Other important constraints can include:
  - Minimum bend radius, maximum quadrupole gradient, magnet aperture, cost, geology or other obstacles, etc.



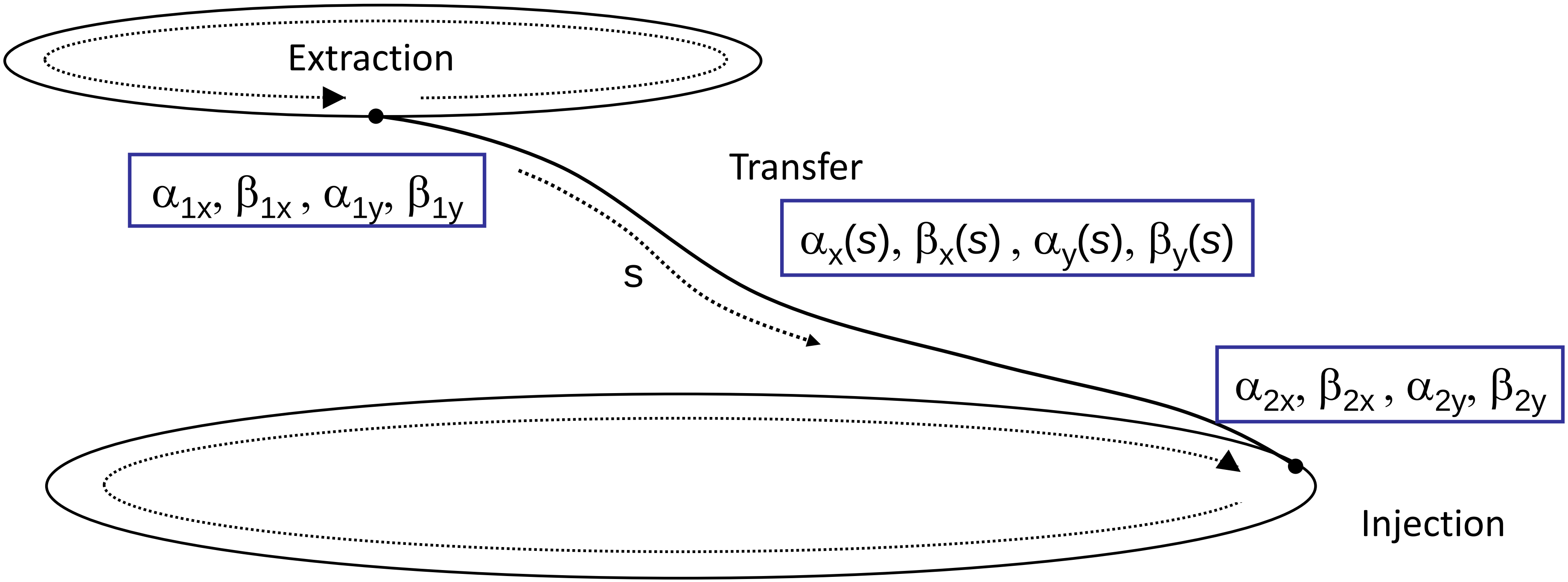
SPS to LHC transfer tunnel TI2 (Beam 1)



SPS to LHC transfer tunnel TI8 (Beam 2)

An example of how geology can influence transfer line design

Linking Machines



The Twiss parameters can be propagated when the transfer matrix **M** is known

$$\begin{bmatrix} x_2 \\ x_2' \end{bmatrix} = \mathbf{M}_{1\to2} \cdot \begin{bmatrix} x_1 \\ x_1' \end{bmatrix} = \begin{bmatrix} C & S \\ C' & S' \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_1' \end{bmatrix}$$

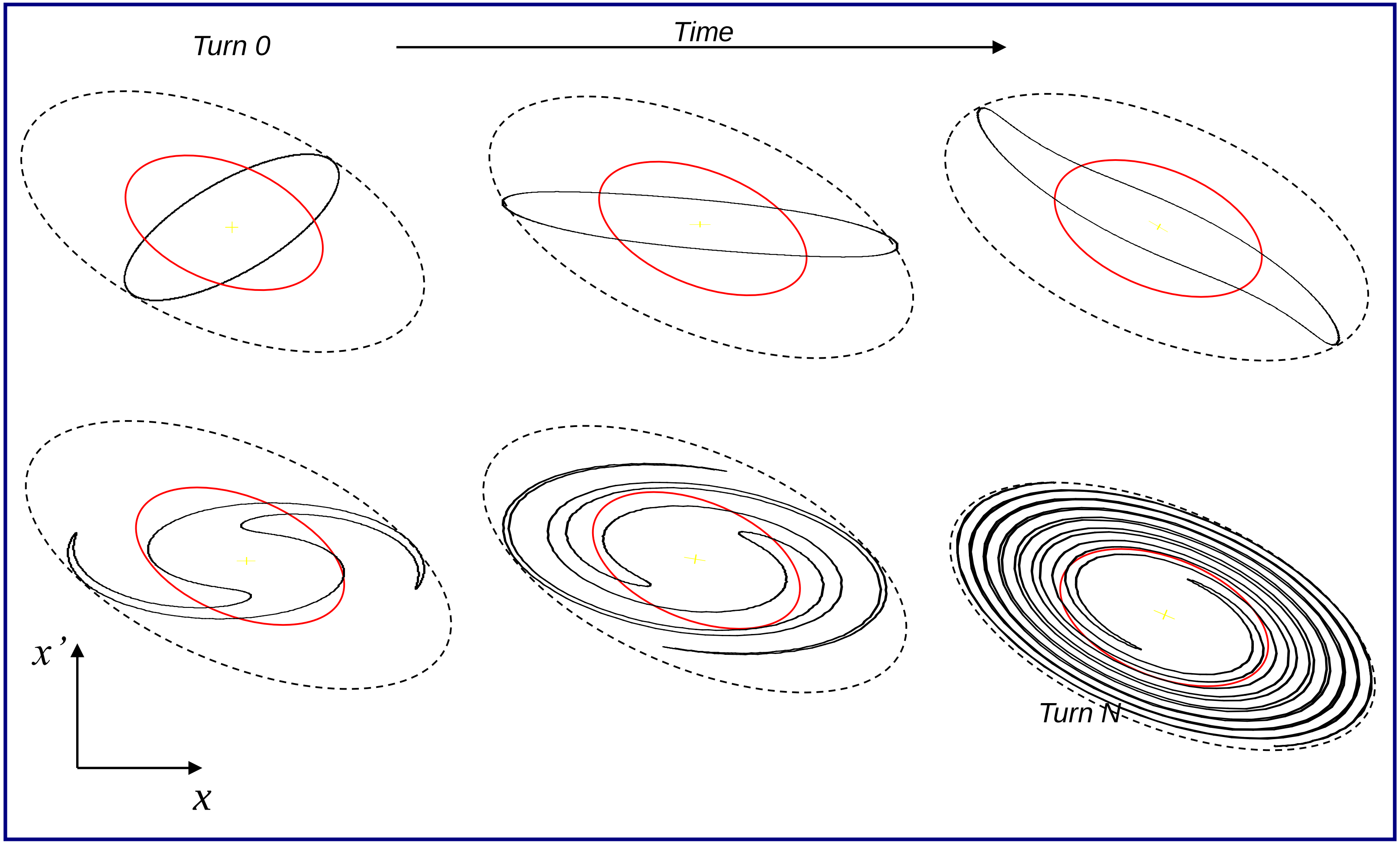
$$\begin{bmatrix} \beta_2 \\ \alpha_2 \\ \gamma_2 \end{bmatrix} = \begin{bmatrix} C^2 & -2CS & S^2 \\ -CC' & CS'+SC' & -SS' \\ C'^2 & -2C'S' & S'^2 \end{bmatrix} \cdot \begin{bmatrix} \beta_1 \\ \alpha_1 \\ \gamma_1 \end{bmatrix}$$

Linking Machines

- Linking the optics is a complicated process:
  - Parameters at start of line have to be propagated to matched parameters at the end of the line (injection to another machine, fixed target etc.)
  - Need to "match" 8 variables (α_x, β_x, D_x, D'_x and α_y, β_y, D_y, D'_y)
  - Matching done with number of independently power ("matching") quadrupoles
  - Maximum β and D values are imposed by magnetic apertures
  - Other constraints exist:
    - Phase conditions for collimators
    - Insertions for special equipment like stripping foils
- Matching with computer codes and relying on mixture of theory, experience, intuition, trial and error.

Optical Mismatch at Injection

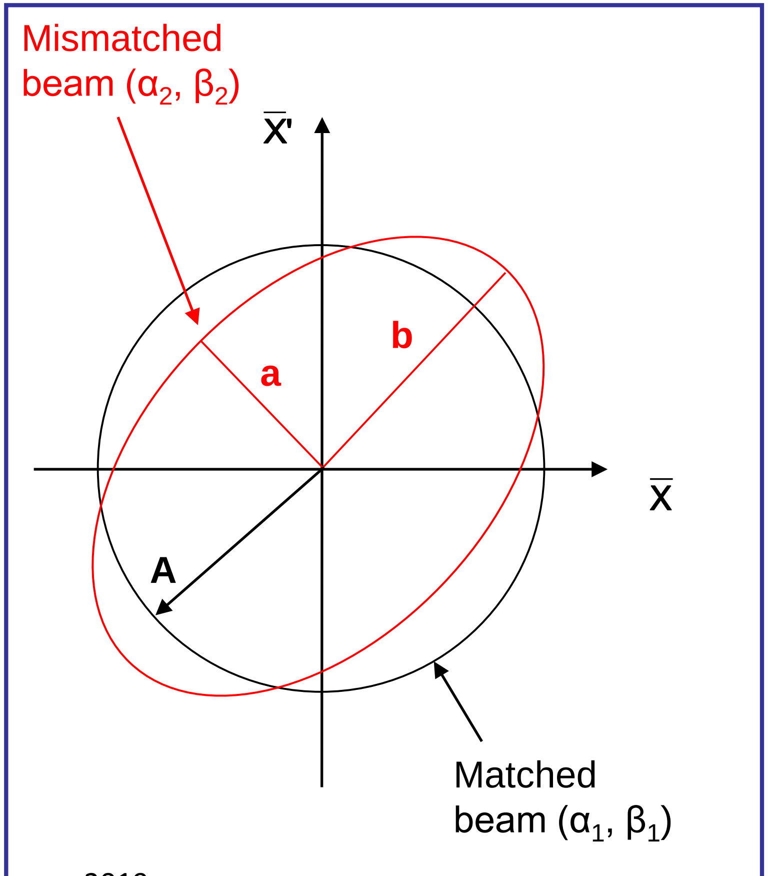
- Filamentation fills larger ellipse with same shape as matched ellipse



- Dispersion mismatch at injection will also cause emittance blow-up

Blow-up from betatron mismatch

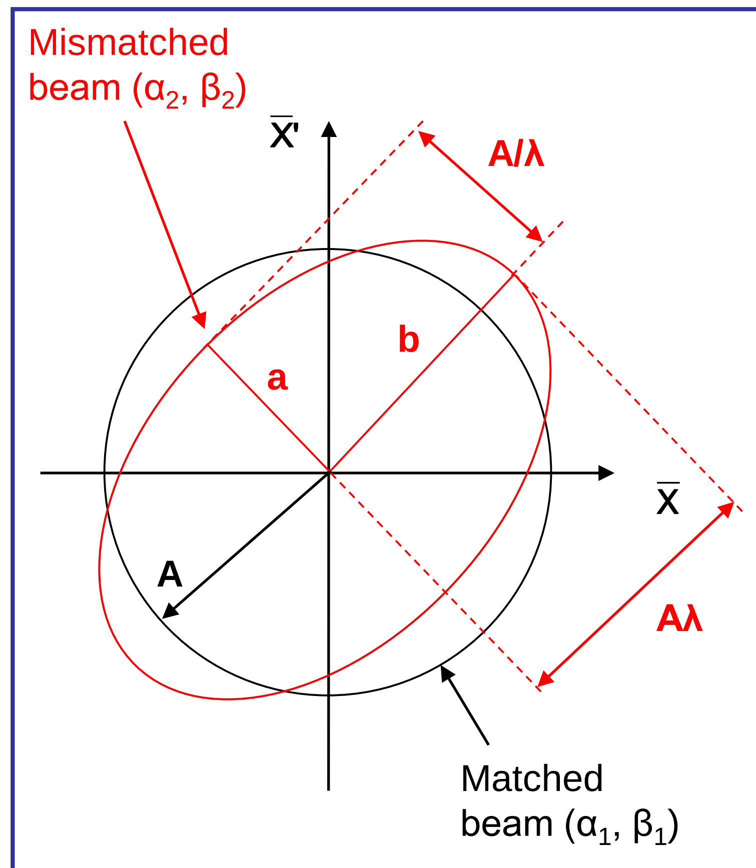
- Optical errors occur in transfer line and ring, such that the beam can be injected with a mismatch
- Filamentation will produce an emittance increase
- In normalised phase space, consider the matched beam as a circle, and the mismatched beam as an ellipse



Blow-up from betatron mismatch

- Optical errors occur in transfer line and ring, such that the beam can be injected with a mismatch
- Filamentation will produce an emittance increase
- In normalised phase space, consider the matched beam as a circle, and the mismatched beam as an ellipse
- The emittance after filamentation:

$$\epsilon_{diluted} = \frac{\epsilon_{matched}}{2}\left(\lambda^2 + \frac{1}{\lambda^2}\right) \quad \text{where} \quad \lambda = \sqrt{\beta / \alpha}$$



Blow-up from betatron mismatch

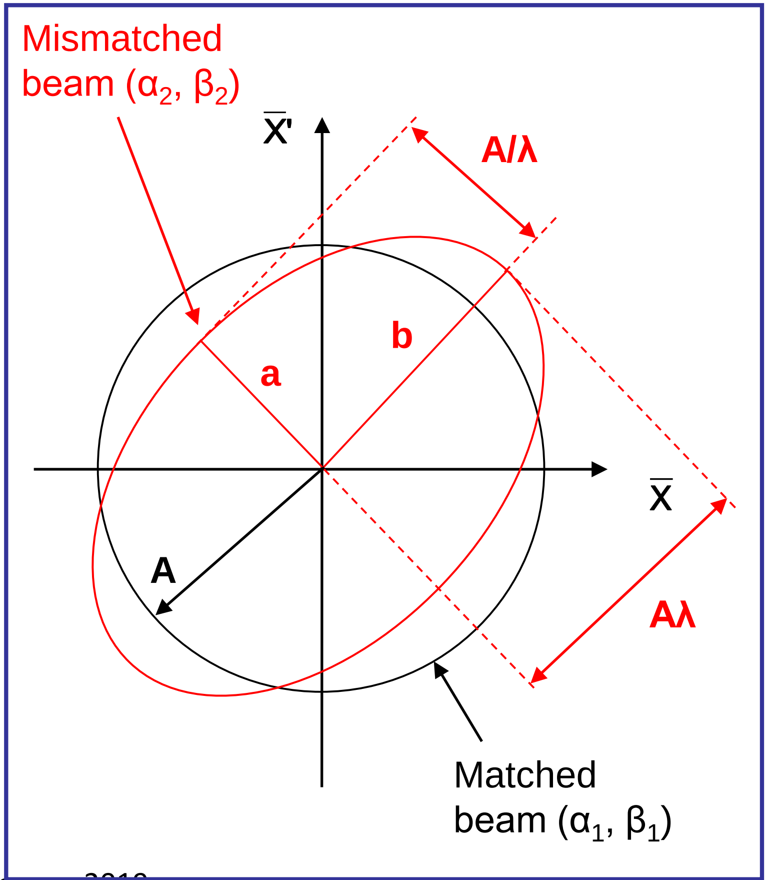
- Optical errors occur in transfer line and ring, such that the beam can be injected with a mismatch
- Filamentation will produce an emittance increase
- In normalised phase space, consider the matched beam as a circle, and the mismatched beam as an ellipse
- The emittance after filamentation:

$$\epsilon_{diluted} = \frac{\epsilon_{matched}}{2}\left(\lambda^2 + \frac{1}{\lambda^2}\right) \quad \text{where} \quad \lambda = \sqrt{b/a}$$

- Writing λ as a function of the matched and mismatched Twiss parameters is an exercise in geometry:

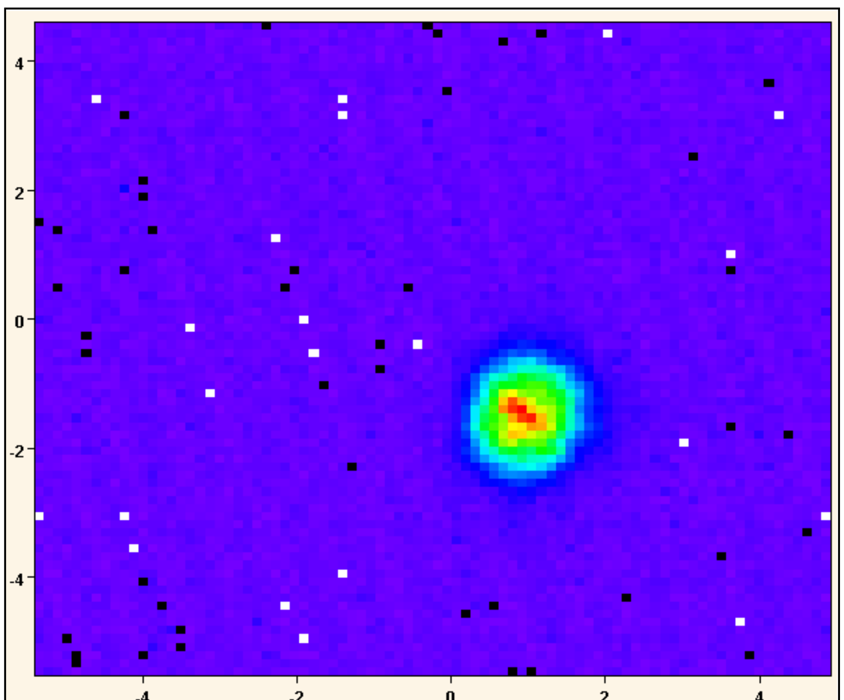
$$\epsilon_{diluted} = \frac{1}{2}\left(\frac{\beta_1}{\beta_2} + \frac{\beta_2}{\beta_1}\left(\alpha_1 - \alpha_2\frac{\beta_1}{\beta_2}\right)^2 + \frac{\beta_2}{\beta_1}\right)\epsilon_{matched}$$

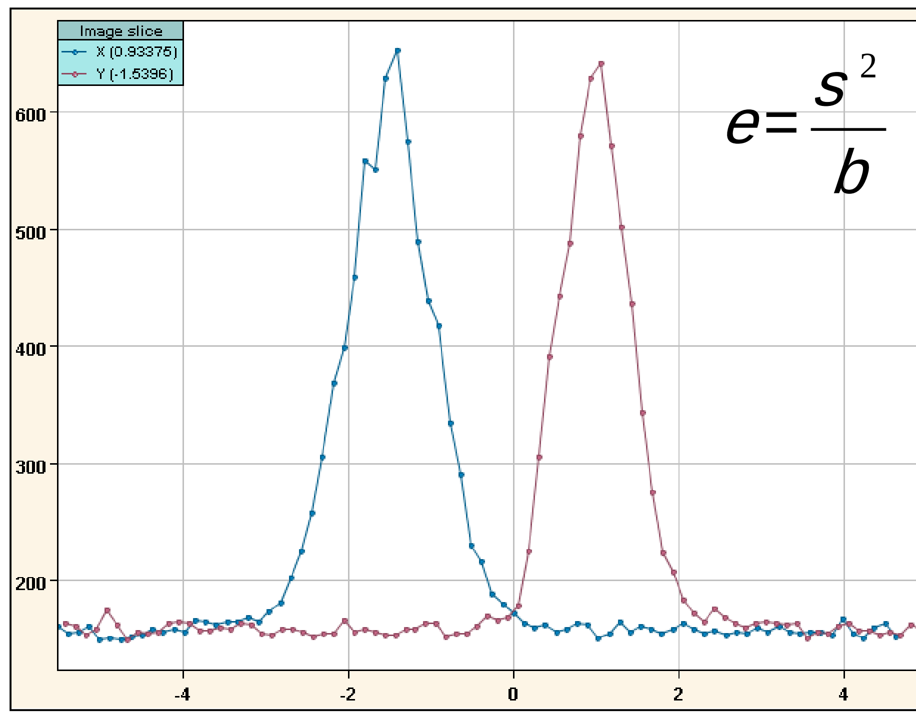
See appendix for derivation



Optics measurement with screens

- A profile monitor is needed to measure the beam size
  - e.g. beam screen (luminescent) provides 2D density profile of the beam
- Profile fit gives transverse beam size: σ
- If optics (Twiss parameters) are known, ε can be calculated from a single screen:





$$e = \frac{s^2}{b}$$

Optics measurement with 3 screens

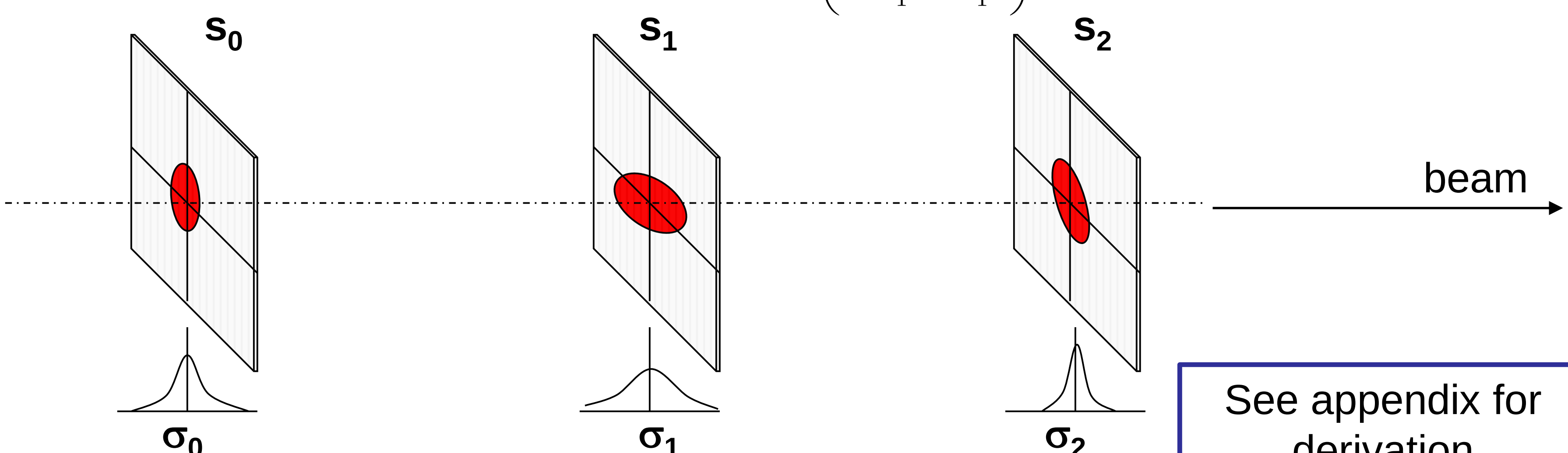
- Assume 3 screens in a dispersion free region and that the emittance is constant along the line:

$$\varepsilon = \frac{\sigma_0^2}{\beta_0} = \frac{\sigma_1^2}{\beta_1} = \frac{\sigma_2^2}{\beta_2}$$

- Measurements of σ at s_1, s_2, s_3 plus knowledge of the two transfer matrices M_{12} and M_{13} allows determination of ε, α and β

$$\mathbf{M}_{0\rightarrow 2} = \begin{pmatrix} C_2 & S_2 \\ C'_2 & S'_2 \end{pmatrix}$$

$$\mathbf{M}_{1\rightarrow 2} = \begin{pmatrix} C_1 & S_1 \\ C'_1 & S'_1 \end{pmatrix}$$



See appendix for derivation

Summary

- Depending on the injection/extraction concept we chose a dedicated combination of septa (spatial separation of fields) and kickers (temporal separation of fields)

- Transfer lines present interesting challenges and differences from circular machines:
  - No periodic condition mean optics is defined by transfer line element strengths and by initial beam ellipse
  - Matching is subject to many constraints
  - Emittance blow-up is an important consideration, and arises from several sources: mis-steering, mismatch (betatron and dispersion)
  - Measurement of beam parameters is important for ensuring beams are well matched between machines and/or experiments

Summary

- Depending on the injection/extraction concept we chose a dedicated combination of septa (spatial separation of fields) and kickers (temporal separation of fields)

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  - No periodic condition mean optics is defined by transfer line element strengths and by initial beam ellipse
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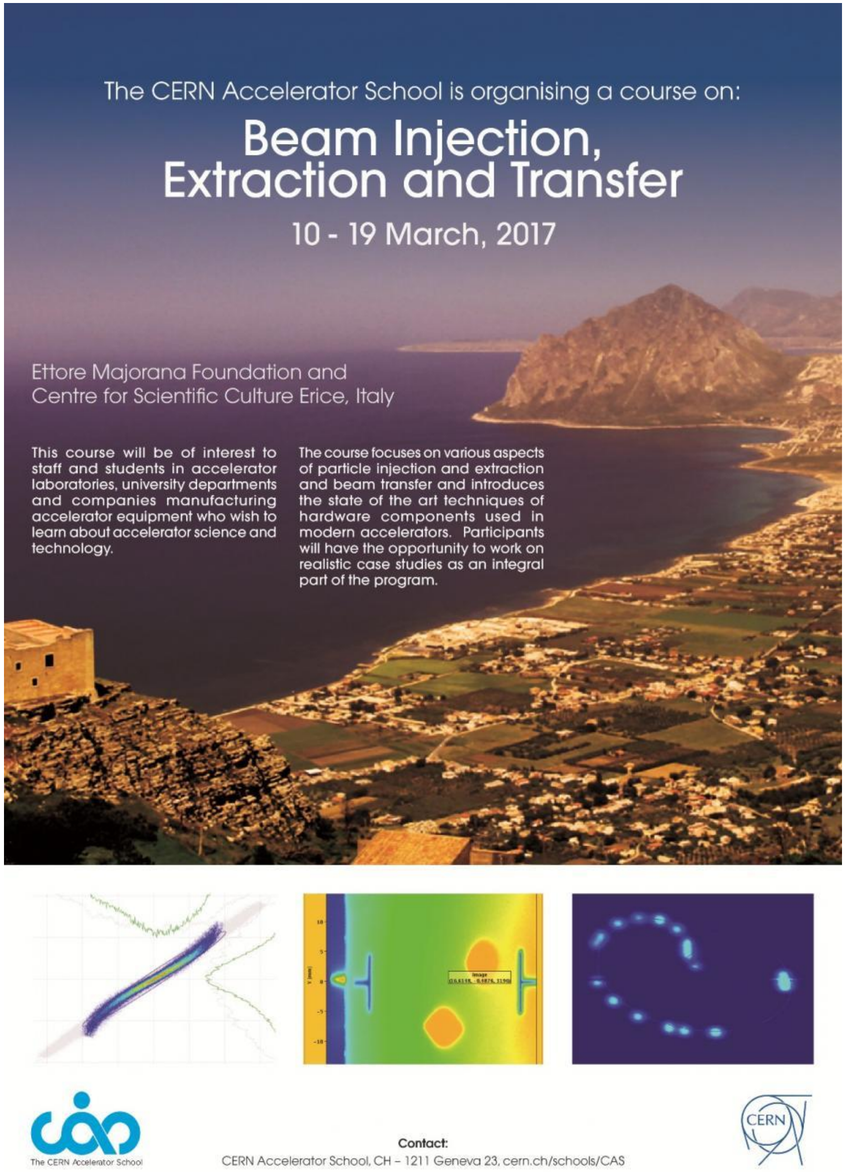
Thank you for your attention

Further reading and references

- Lot's of resources presented at the recent CAS Specialised School:
- Beam Injection, Extraction and Transfer, 10-19 March 2017, Erice, Italy
- https://cas.web.cern.ch/schools/erice-2017



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Example parameters for kickers at CERN

Kicker Location	Beam momentum (GeV/c)	# Magnets	Gap Height [V_{ap}] (mm)	Current (kA)	Impedance (Ω)	Rise Time (ns)	Total Deflection (mrad)
CTF3	0.2	4	40	0.056	50	~4	1.2
PS Inj.	2.14	4	53	1.52	26.3	42	4.2
SPS Inj.	13/26	16	54 to 61	1.47/1.96	16.67/12.5	115/200	3.92
SPS Ext. (MKE4)	450	5	32 to 35	2.56	10	1100	0.48
LHC Inj.	450	4	54	5.12	5	900	0.82
LHC Abort	450 to 7000	15	73	1.3 to 18.5	1.5 (not T-line)	2700	0.275

Example parameters for septa at CERN

Septum Location	Beam momentum (GeV/c)	Gap Height (mm)	Max. Current (kA)	B (T)	Deflection (mrad)	Septum thickness (mm)
LEIR/AD/CTF (13 systems)	Various	25 to 55	1 DC to 40 pulsed	0.5 to 1.6	up to 130	1.7 - 19.2
PS Booster (6 systems)	1.4	25 to 60	28 pulsed	0.1 to 0.6	up to 80	1 – 15
PS complex (8 systems)	26	20 to 60	2.5 DC to 33 pulsed	0.2 to 1.2	up to 55	3 - 11.2
SPS Ext.	450	20	24	1.5	2.25	4.2 - 17.2

Blow-up from betatron mismatch

- General betatron motion:

$$x_2 = \sqrt{a_2 b_2}\,\sin(j + j_o), \qquad x'_2 = \sqrt{a_2 / b_2}\left[\cos(j + j_o) - a_2 \sin(j + j_o)\right]$$

- Applying the normalisation transformation for the matched beam…

$$\begin{bmatrix} \overline{X}_2 \\ \overline{X}'_2 \end{bmatrix} = \sqrt{\frac{1}{\beta_1}} \cdot \begin{bmatrix} 1 & 0 \\ \alpha_1 & \beta_1 \end{bmatrix} \cdot \begin{bmatrix} x_2 \\ x'_2 \end{bmatrix}$$

…an ellipse is obtained in normalised phase space:

$$A^2 = \underbrace{\overline{X}_2^2 \left[\frac{\beta_1}{\beta_2} + \frac{\beta_2}{\beta_1}\left(\alpha_1 - \alpha_2 \frac{\beta_1}{\beta_2}\right)^2 \right]}_{g_{new}} + \underbrace{\overline{X}'^2_2 \frac{\beta_2}{\beta_1}}_{b_{new}} - 2\overline{X}_2 \overline{X}'_2 \underbrace{\left[\frac{\beta_2}{\beta_1}\left(\alpha_1 - \alpha_2 \frac{\beta_1}{\beta_2}\right) \right]}_{a_{new}}$$

Blow-up from betatron mismatch

- From general ellipse properties one can write:

$$a = \frac{A}{\sqrt{2}}\left(\sqrt{H+1}+\sqrt{H-1}\right), \qquad b = \frac{A}{\sqrt{2}}\left(\sqrt{H+1}-\sqrt{H-1}\right) \qquad \text{where} \qquad H = \frac{1}{2}\left(g_{new} + b_{new}\right)$$

Giving:

$$\lambda = \frac{1}{\sqrt{2}}\left(\sqrt{H+1}+\sqrt{H-1}\right),$$

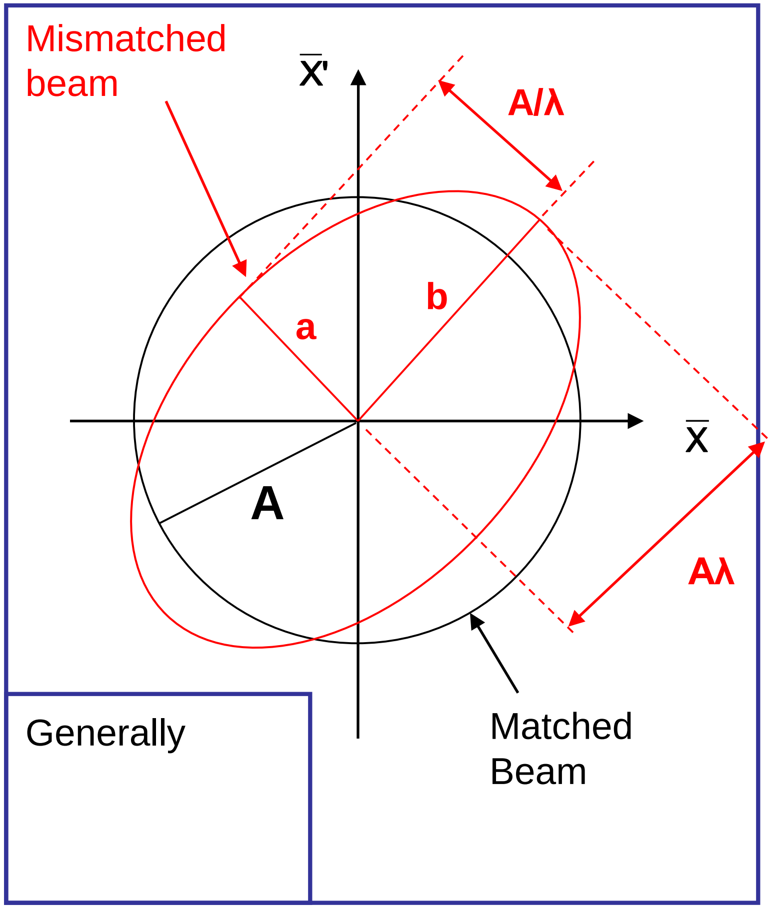
$$a = \mathrm{A}/\lambda$$

$$b = \mathrm{A}\cdot\lambda$$

$$\frac{1}{\lambda} = \frac{1}{\sqrt{2}}\left(\sqrt{H+1}-\sqrt{H-1}\right)$$

- The co-ordinates of the mismatched beam can be expressed:

$$\overline{\mathbf{X}}_{new} = \lambda\cdot\mathbf{A}\sin(\phi+\phi_1), \qquad \overline{\mathbf{X}}'_{new} = \frac{1}{\lambda}\mathbf{A}\cos(\phi+\phi_1)$$



Blow-up from betatron mismatch

- We can evaluate the square of the distance of a particle from the origin as:

$$\mathbf{A}_{new}^2 = \overline{\mathbf{X}}_{new}^2 + \overline{\mathbf{X}}'^2_{new} = \lambda^2 \cdot \mathbf{A}_0^2 \sin^2(\phi + \phi_1) + \frac{1}{\lambda^2} \mathbf{A}_0^2 \cos^2(\phi + \phi_1)$$

- The new emittance is the average for all particles with positions Ai over all phases:

$$\varepsilon_{diluted} = \frac{1}{2}\left\langle A_{new}^2 \right\rangle = \frac{1}{2}\left(\lambda^2 \left\langle A_0^2 \sin^2(\varphi + \varphi_1) \right\rangle + \frac{1}{\lambda^2} \left\langle A_0^2 \cos^2(\varphi + \varphi_1) \right\rangle \right)$$

1/2 1/2

$$= \frac{1}{2}\left\langle A_0^2 \right\rangle \left(\lambda^2 \left\langle \sin^2(\varphi + \varphi_1) \right\rangle + \frac{1}{\lambda^2} \left\langle \cos^2(\varphi + \varphi_1) \right\rangle \right) = \frac{1}{2}\varepsilon_0 \left(\lambda^2 + \frac{1}{\lambda^2} \right)$$

- If we're feeling diligent, we can substitute back for λ:

$$\varepsilon_{diluted} = \frac{1}{2}\varepsilon_{matched}\left(\lambda^2 + \frac{1}{\lambda^2} \right) = H\varepsilon_{matched} = \frac{1}{2}\varepsilon_{matched}\left(\frac{\beta_1}{\beta_2} + \frac{\beta_2}{\beta_1}\left(\alpha_1 - \alpha_2 \frac{\beta_1}{\beta_2} \right)^2 + \frac{\beta_2}{\beta_1} \right)$$

where subscript 1 refers to the matched and 2 refers to mismatched cases

Blow-up from dispersion mismatch

- Dispersion mismatch will also introduce emittance blow-up through filamentation much like optical mismatch
- Introducing normalised dispersion: $D_n = \frac{D}{\sqrt{\beta}}$ $\quad D'_n = \frac{\alpha}{\sqrt{\beta}} D + \sqrt{\beta} D'$
- With a momentum error of the mismatch is: $\delta = \frac{\Delta p}{p}$

$$\bar{X} = \bar{X} + \Delta D_n \delta \qquad \bar{X}' = \bar{X}' + \Delta D'_n \delta$$

- Rotating the reference frame to a convenient reference (see plot):

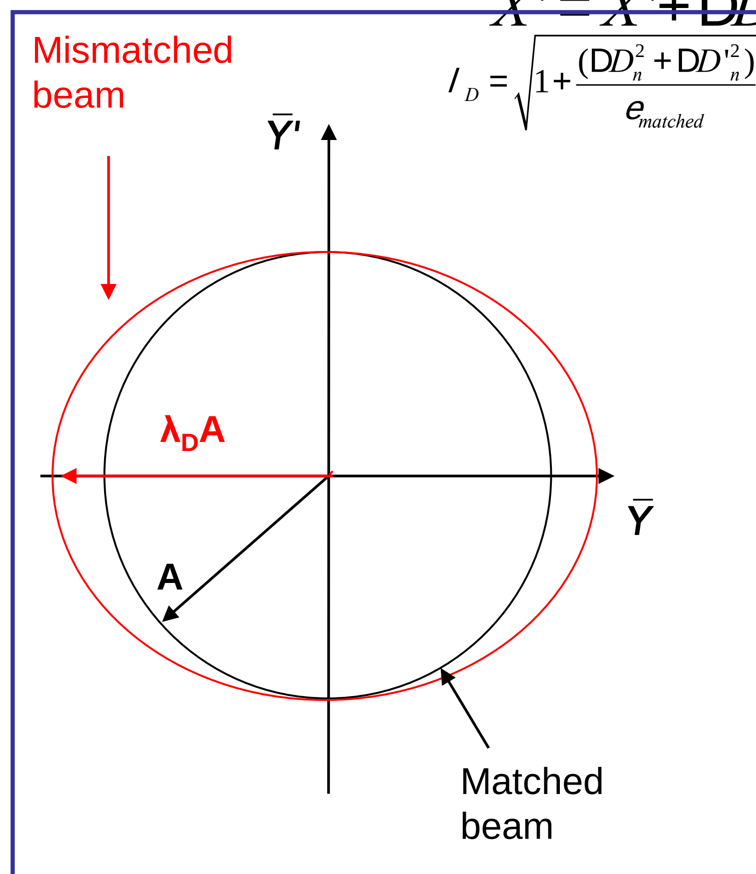
$$\bar{Y} = \bar{Y} + \sqrt{\Delta D_n^2 + \Delta D'^2_n}\,\delta \qquad \bar{Y}' = \bar{Y}'$$

- And averaging over a distribution of particles, one can write the emittance blow-up as:

$$\varepsilon_{diluted} = \varepsilon_{matched} + \frac{\Delta D_n^2 + \Delta D'^2_n}{2} \delta^2_{rms}$$

$$\bar{X}' = \bar{X}' + \Delta D'_n \delta$$

$$\lambda_D = \sqrt{1 + \frac{(\Delta D_n^2 + \Delta D'^2_n)}{\varepsilon_{matched}}} \delta_{rms}$$



Blow-up from betatron mismatch

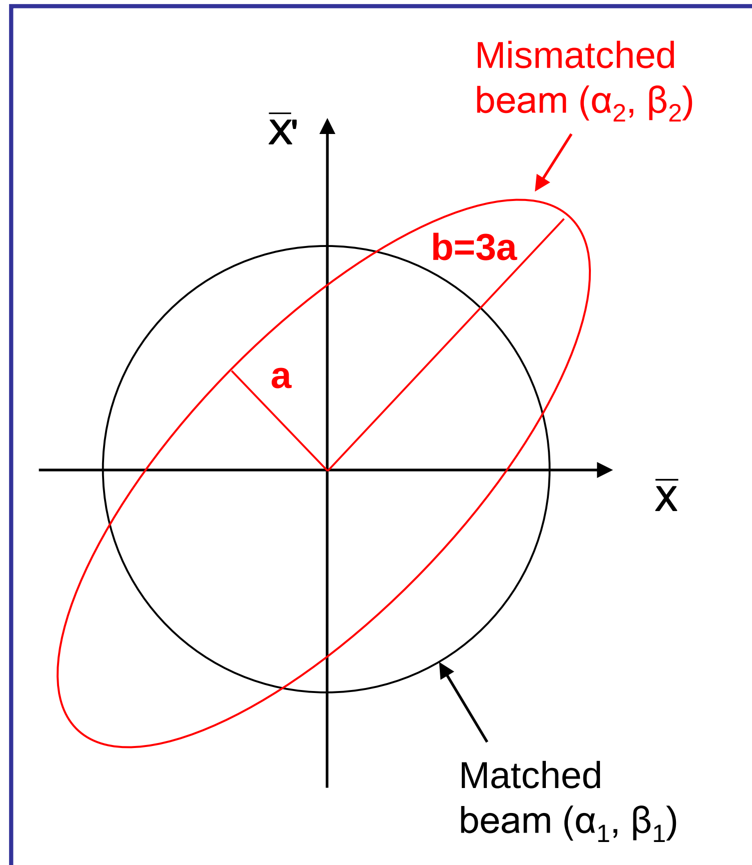
- A numerical example…

- Consider b = 3a for the mismatched ellipse:

$$\lambda = \sqrt{b/a} = \sqrt{3}$$

$$\varepsilon_{diluted} = \frac{\varepsilon_{matched}}{2}\left(\lambda^2 + \frac{1}{\lambda^2}\right)$$

$$= 1.67\,\varepsilon_{matched}$$



See appendix for blow-up from dispersion mismatch

Optics measurement with 3 screens

- Remember how we propagate Twiss parameters from s_0 to s_1:

$$\begin{bmatrix} \beta_1 \\ \alpha_1 \\ \gamma_1 \end{bmatrix} = \begin{bmatrix} C_1^2 & -2C_1S_1 & S_1^2 \\ -C_1C_1' & C_0S_0' + S_0C_0' & -S_1S_1' \\ C_1'^2 & -2C_1'S_1' & S_1'^2 \end{bmatrix} \cdot \begin{bmatrix} \beta_0 \\ \alpha_0 \\ \gamma_0 \end{bmatrix}$$

- Giving us three simultaneous equations and three unknowns ε_0, α_0 and β_0:

$$\beta_0 = C_0^2 \cdot \beta_0 - 2C_0S_0 \cdot \alpha_0 + S_0^2 \cdot \gamma_0$$

$$\beta_1 = C_1^2 \cdot \beta_0 - 2C_1S_1 \cdot \alpha_0 + S_1^2 \cdot \gamma_0$$

$$\beta_2 = C_2^2 \cdot \beta_0 - 2C_2S_2 \cdot \alpha_0 + S_2^2 \cdot \gamma_0$$

$\times\ \varepsilon$

$$\sigma_0^2 = \beta_0 \varepsilon$$

$$\sigma_1^2 = C_1^2 \cdot \beta_0 \varepsilon - 2C_1S_1 \cdot \alpha_0 \varepsilon + S_1^2 \cdot \frac{(1+\alpha_0^2)}{\beta_0} \varepsilon$$

$$\sigma_2^2 = C_2^2 \cdot \beta_0 \varepsilon - 2C_2S_2 \cdot \alpha_0 \varepsilon + S_2^2 \cdot \frac{(1+\alpha_0^2)}{\beta_0} \varepsilon$$

- After a bit of algebra… we find:

$$\alpha_0 = -\frac{\beta_0}{2} W \qquad W = \frac{\left(\sigma_2/\sigma_0\right)^2 / S_2^2 - \left(\sigma_1/\sigma_0\right)^2 / S_1^2 - \left(C_2/S_2\right)^2 + \left(C_1/S_1\right)^2}{\left(C_1/S_1\right) - \left(C_2/S_2\right)}$$

Optics measurement with 3 screens

- Some (more) algebra with the above equations and we can finally express the beta function at the first screen:

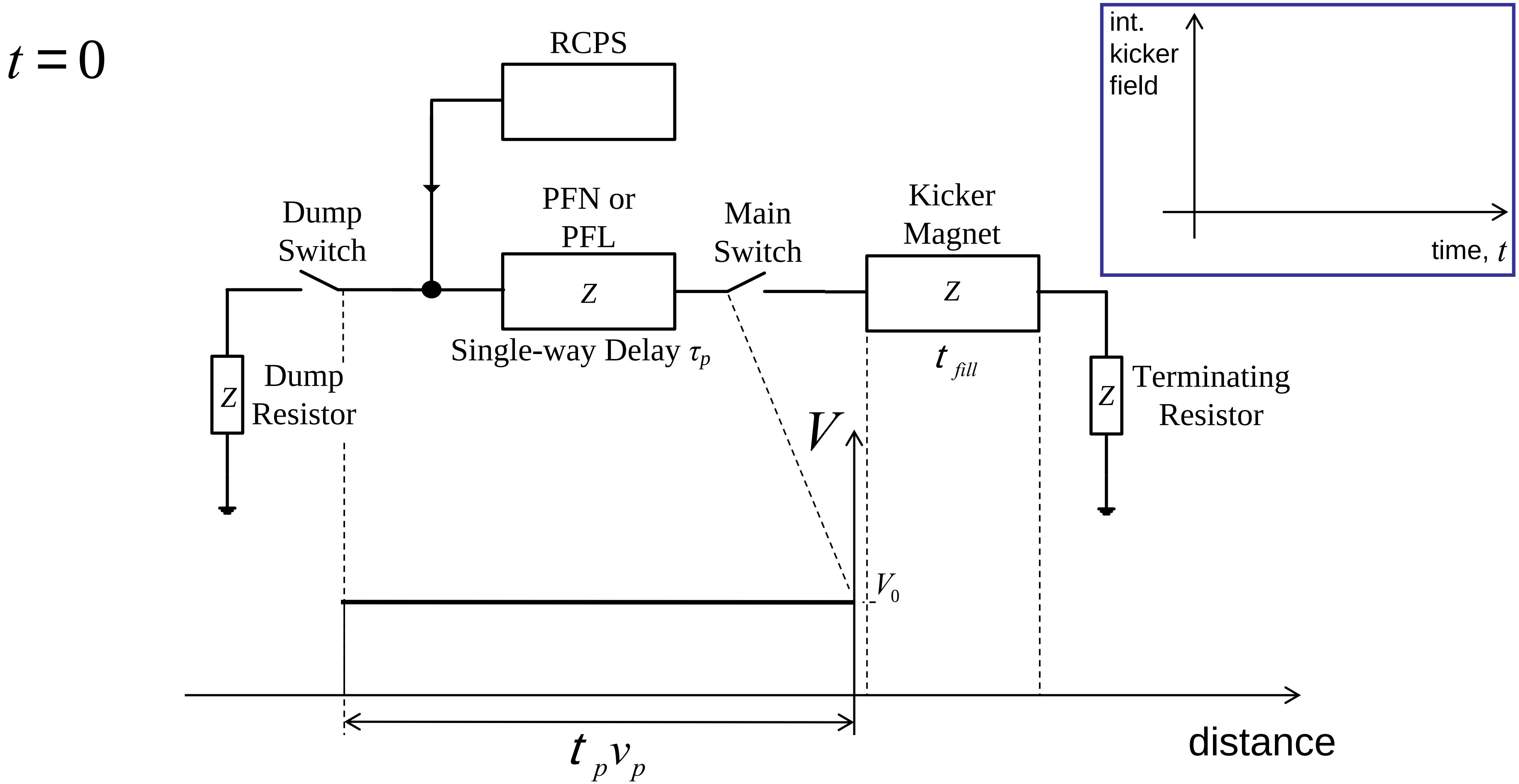
$$b_0 = 1 \Big/ \left| \sqrt{\left(s_2/s_0\right)^2 \Big/ S_2^2 - \left(C_2/S_2\right)^2 + W\left(C_2/S_2\right)^2 - W^2/4} \right|$$

- And therefore also the emittance and the divergence of the beta function:

$$e = \frac{s_0^2}{b_0} \qquad a_0 = \frac{b_0}{2} W$$

- Other methods of emittance measurement:
  - Extension of the above method to multiple screens: tomography
  - Quad scan: same as above but use one screen and change $M_{\text{quad} \rightarrow \text{screen}}$
  - Direct measurements (lower intensity/energy beams):
    - slit-grid or pepper-pot, laser “wire” for H- beams

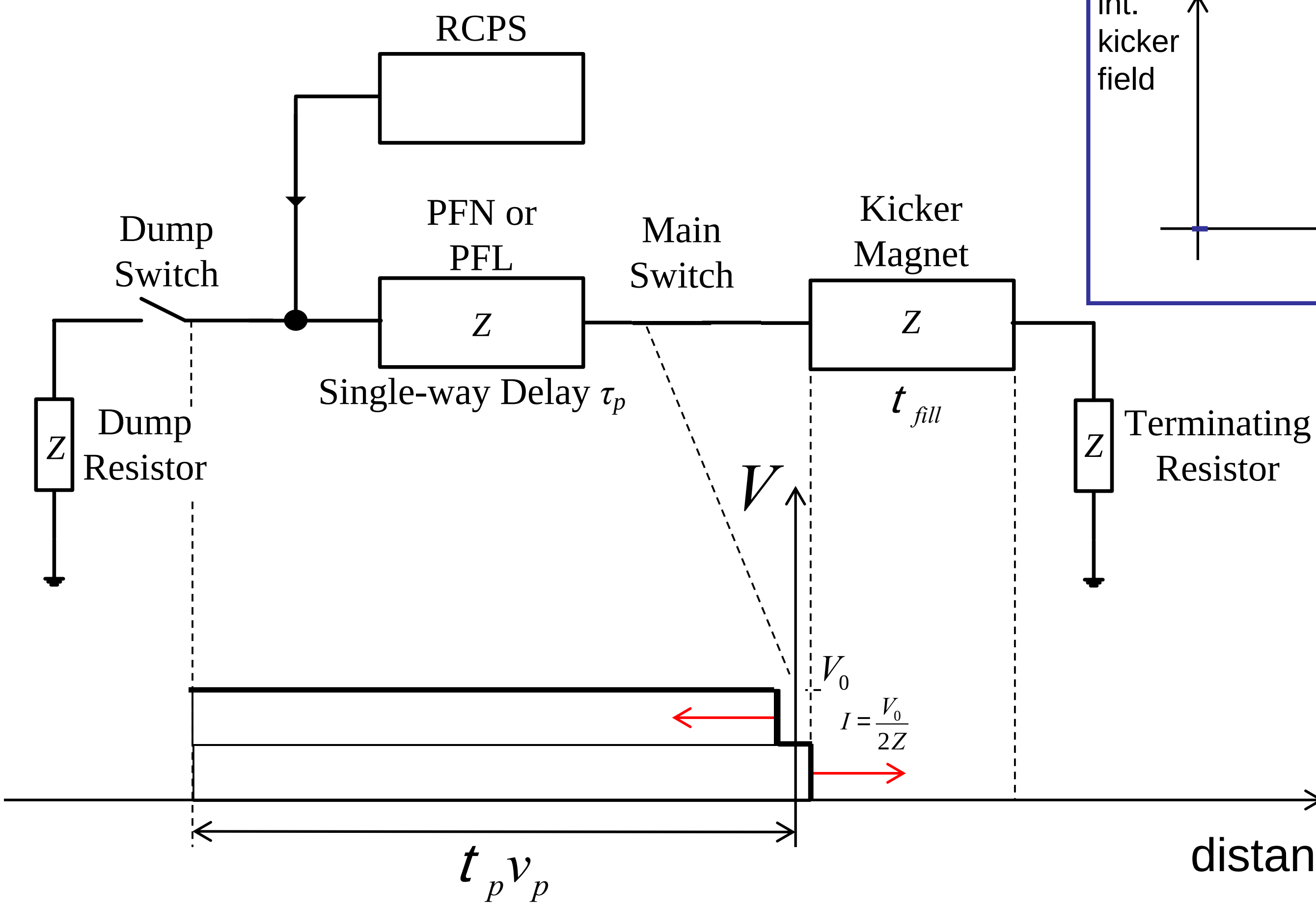
Simplified kicker system schematic

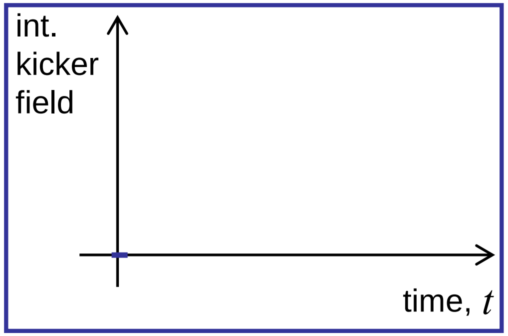


- Pulse forming network or line (PFL/PFN) charged to voltage V_0 by the resonant charging power supply (RCPS)
  - RCPS is de-coupled from the system through a diode stack

Simplified kicker system schematic

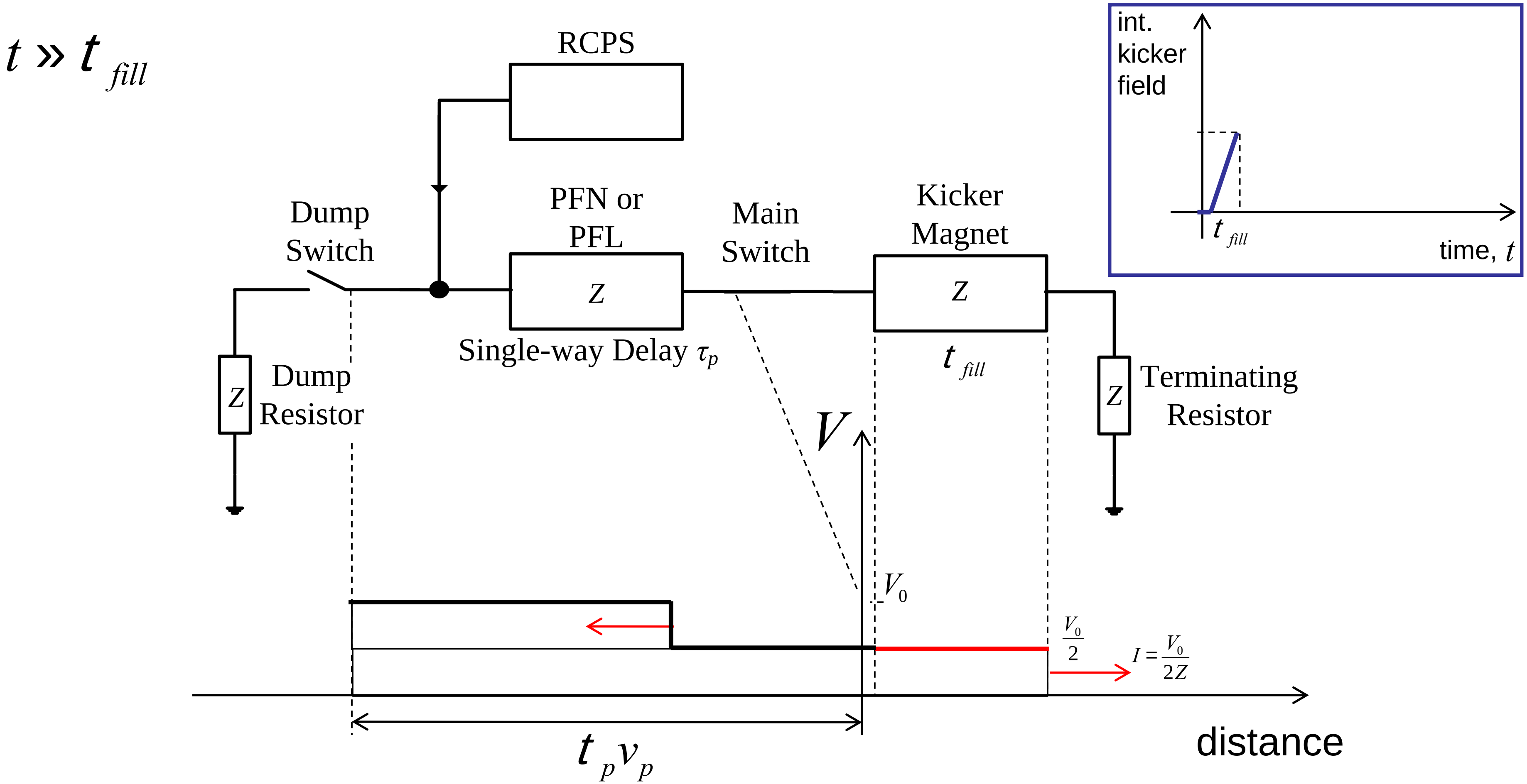
$t \gg 0$





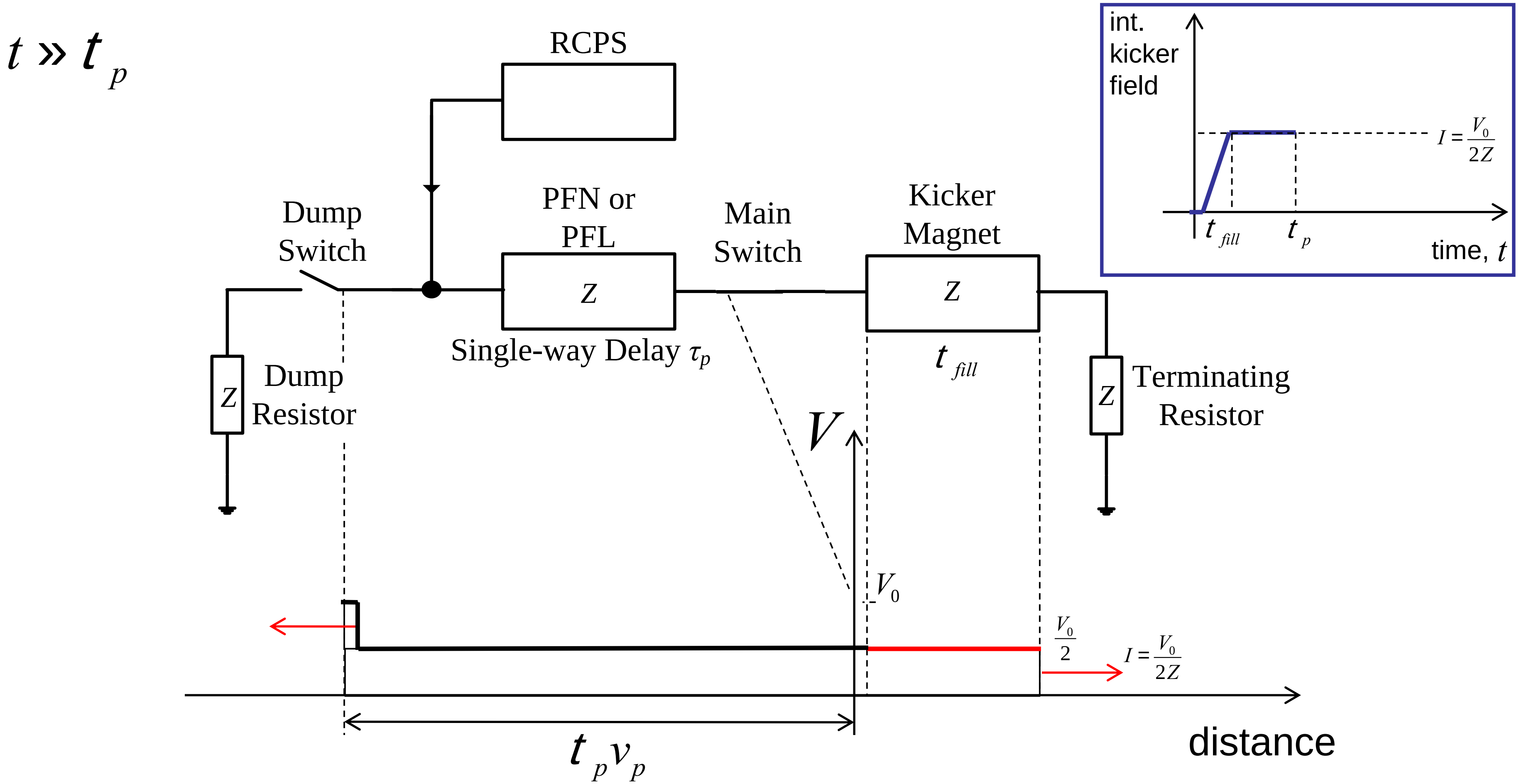
- Pulse forming network or line (PFL/PFN) charged to voltage V_0 by the resonant charging power supply (RCPS)
  - RCPS is de-coupled from the system through a diode stack
- At t = 0, main switch is closed and current starts to flow into the kicker

Simplified kicker system schematic



- At t = τ_{fill}, the voltage pulse of magnitude $V_0/2$ has propagated through the kicker and nominal field achieved with a current $V_0/2Z$
  - typically $\tau_p >> \tau_{fill}$ (schematic for illustration purposes)

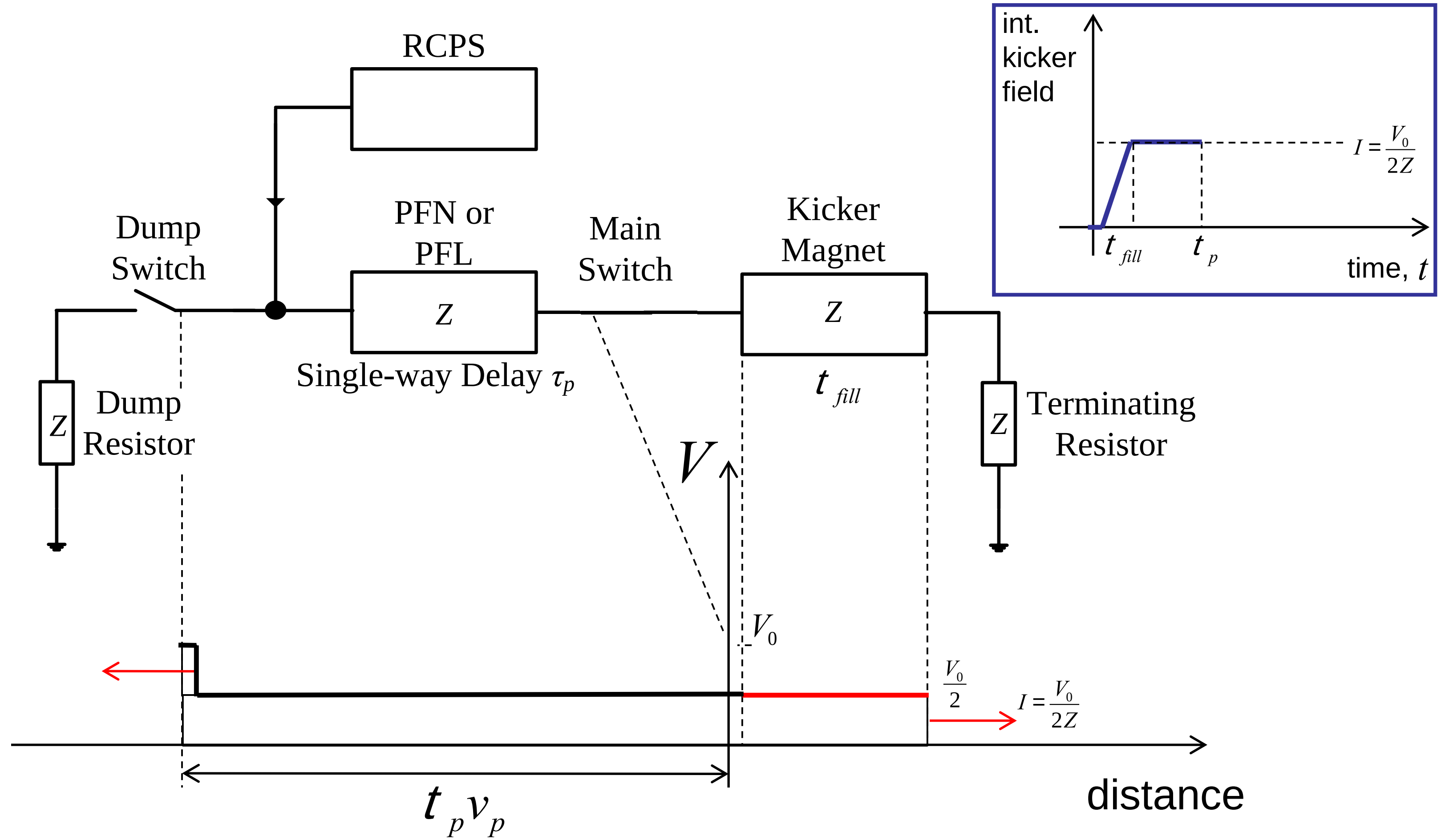
Simplified kicker system schematic



- PFN continues to discharge energy into kicker magnet and matched terminating resistor

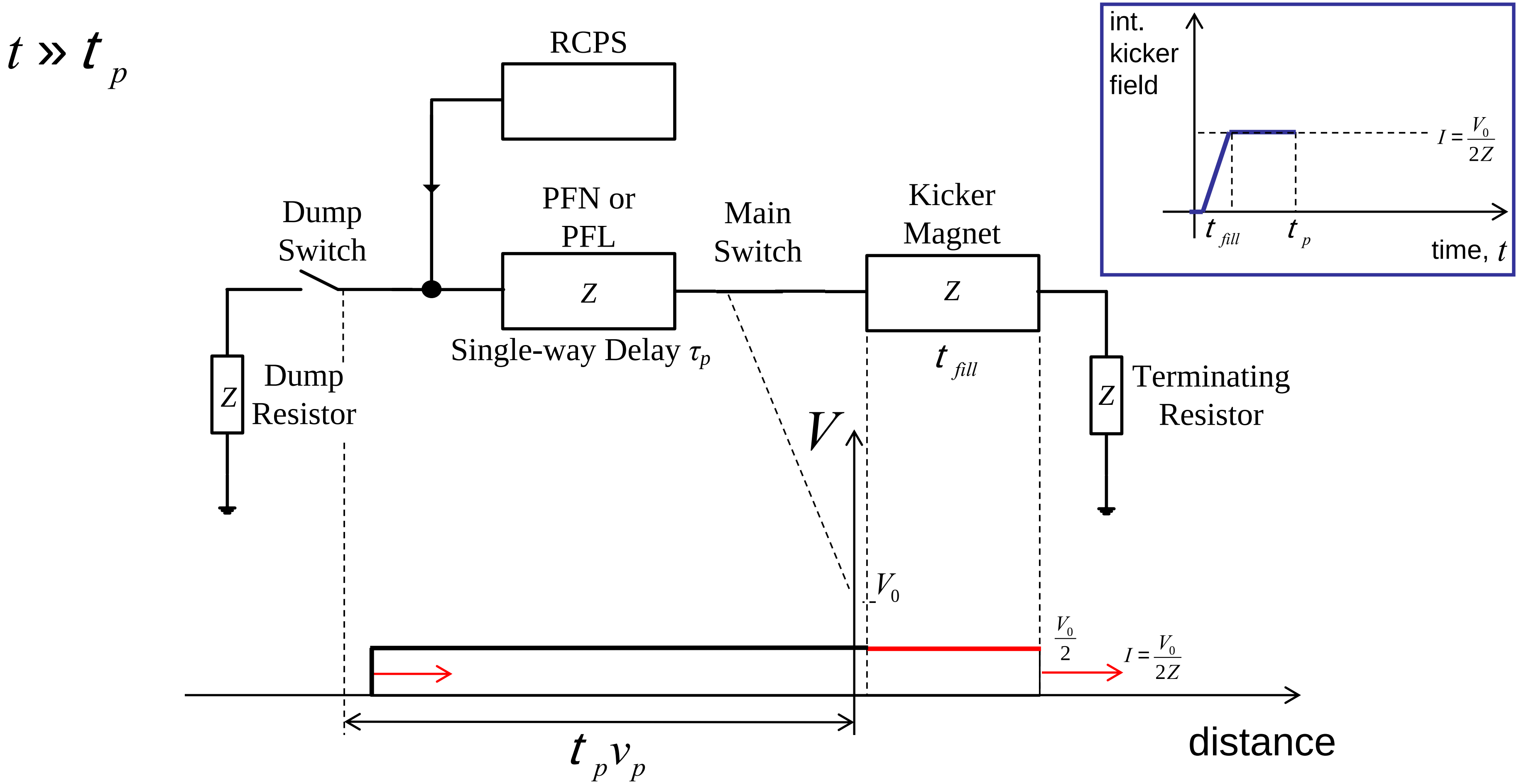
Simplified kicker system schematic

$t \gg t_p$



- PFN continues to discharge energy into kicker magnet and matched terminating resistor
- At t ≈ τ_p the negative pulse reflects off the open end of the circuit (dump switch) and back towards the kicker

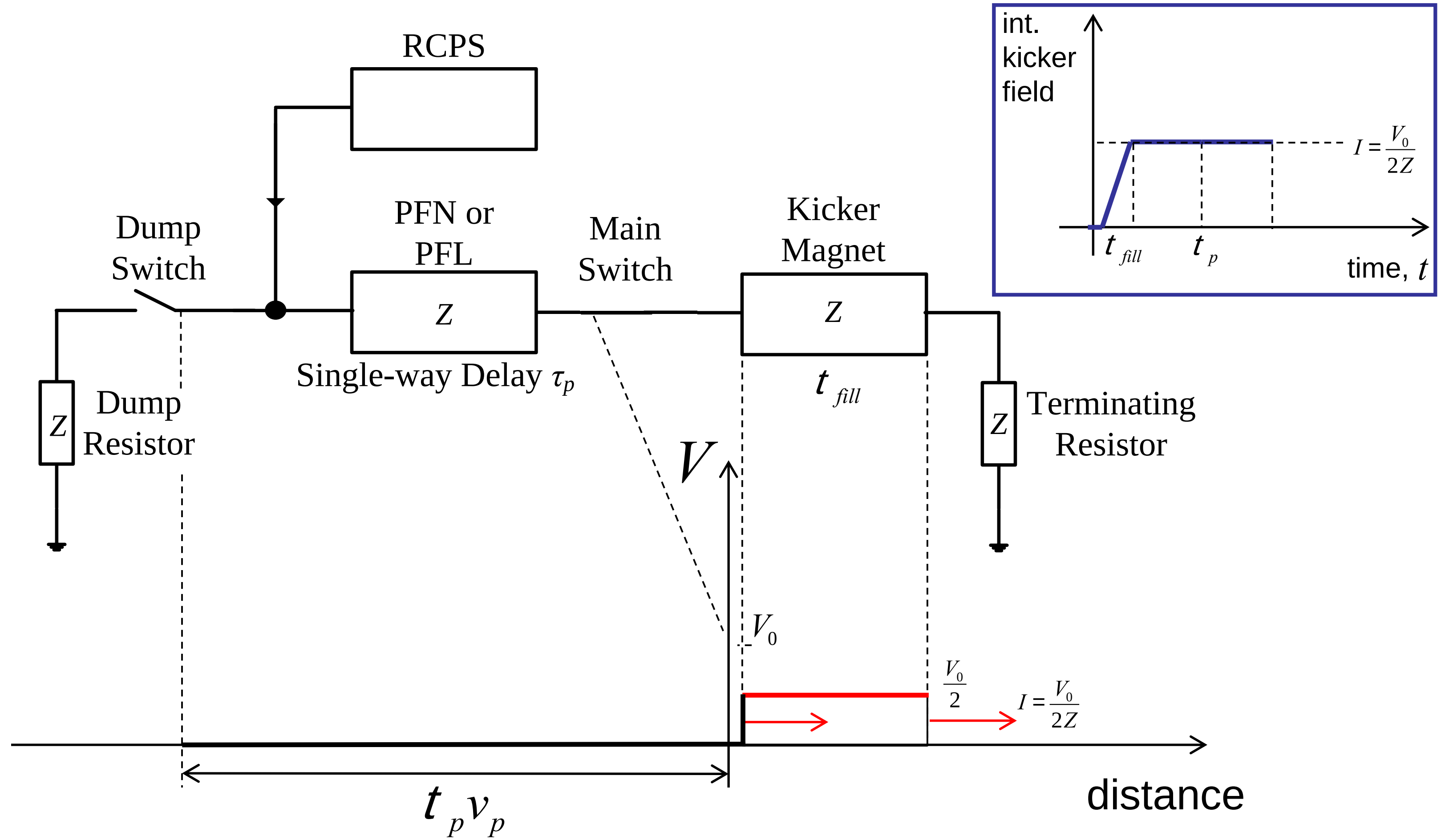
Simplified kicker system schematic



- PFN continues to discharge energy into matched terminating resistor
- At t ≈ τ_p the negative pulse reflects off the open end of the circuit and back towards the kicker

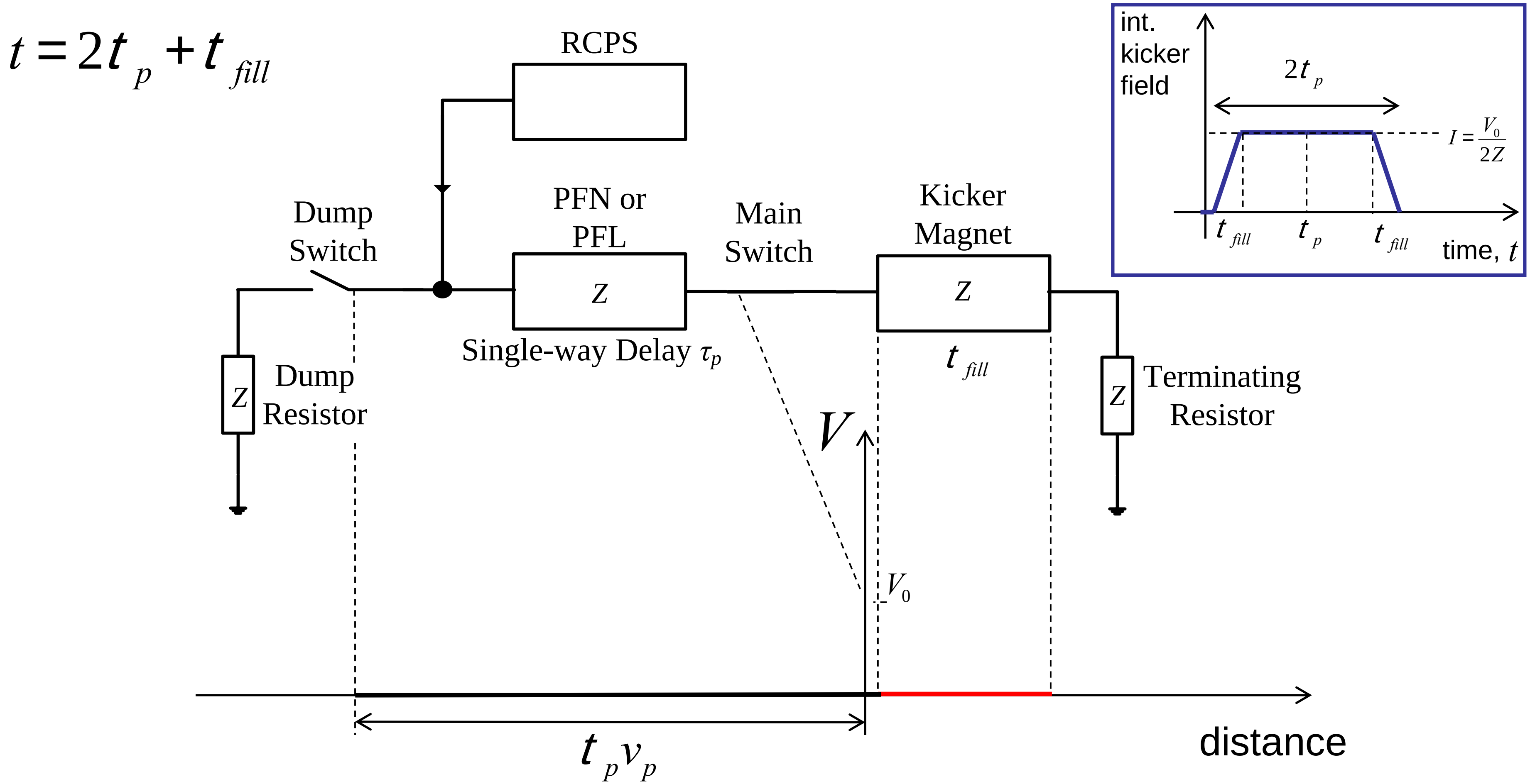
Simplified kicker system schematic

$t \gg 2t_p$



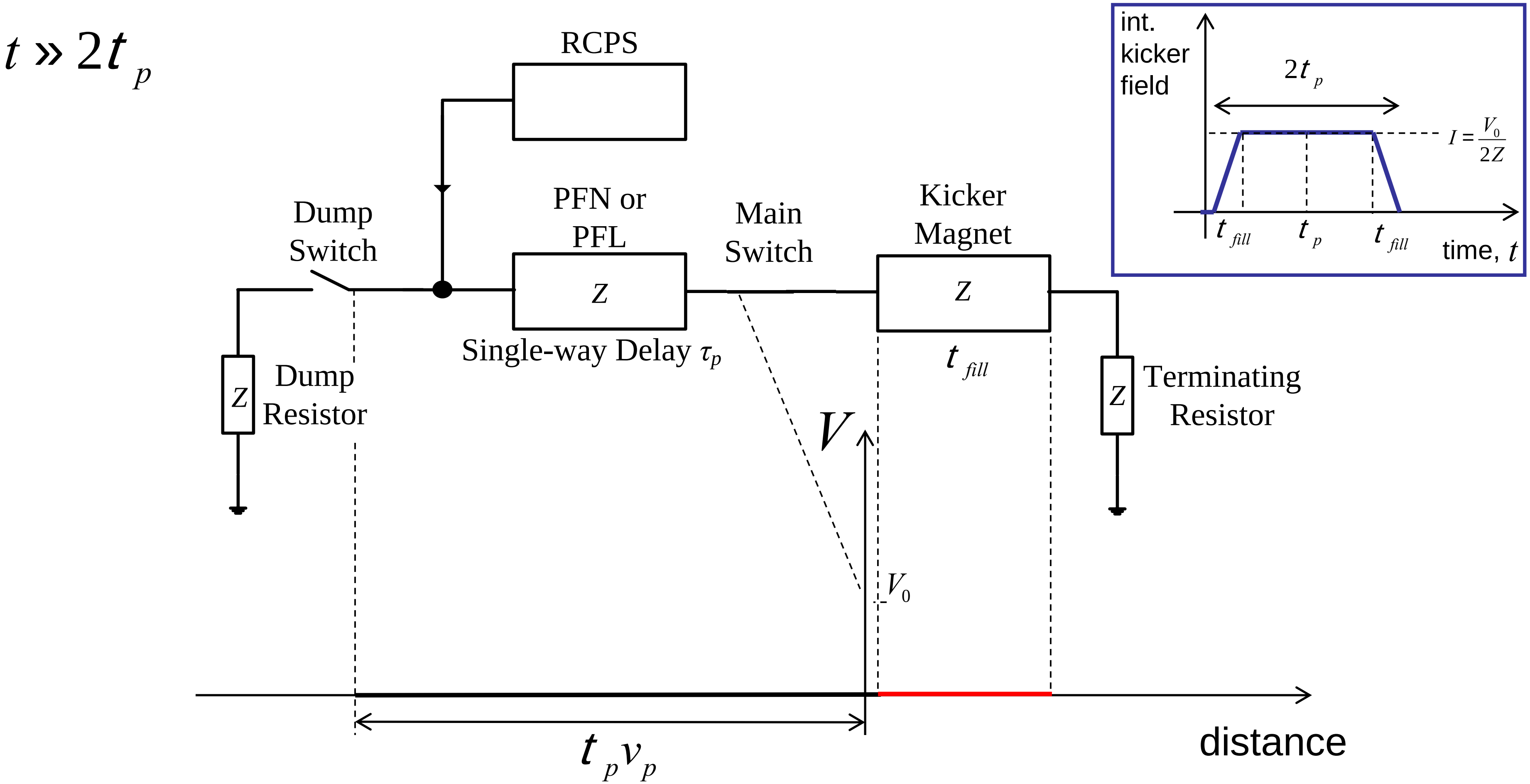
- At t ≈ 2τ_p the pulse arrives at the kicker and field starts to decay

Simplified kicker system schematic



- A kicker pulse of approximately $2\tau_p$ is imparted on the beam and all energy has been emptied into the terminating resistor

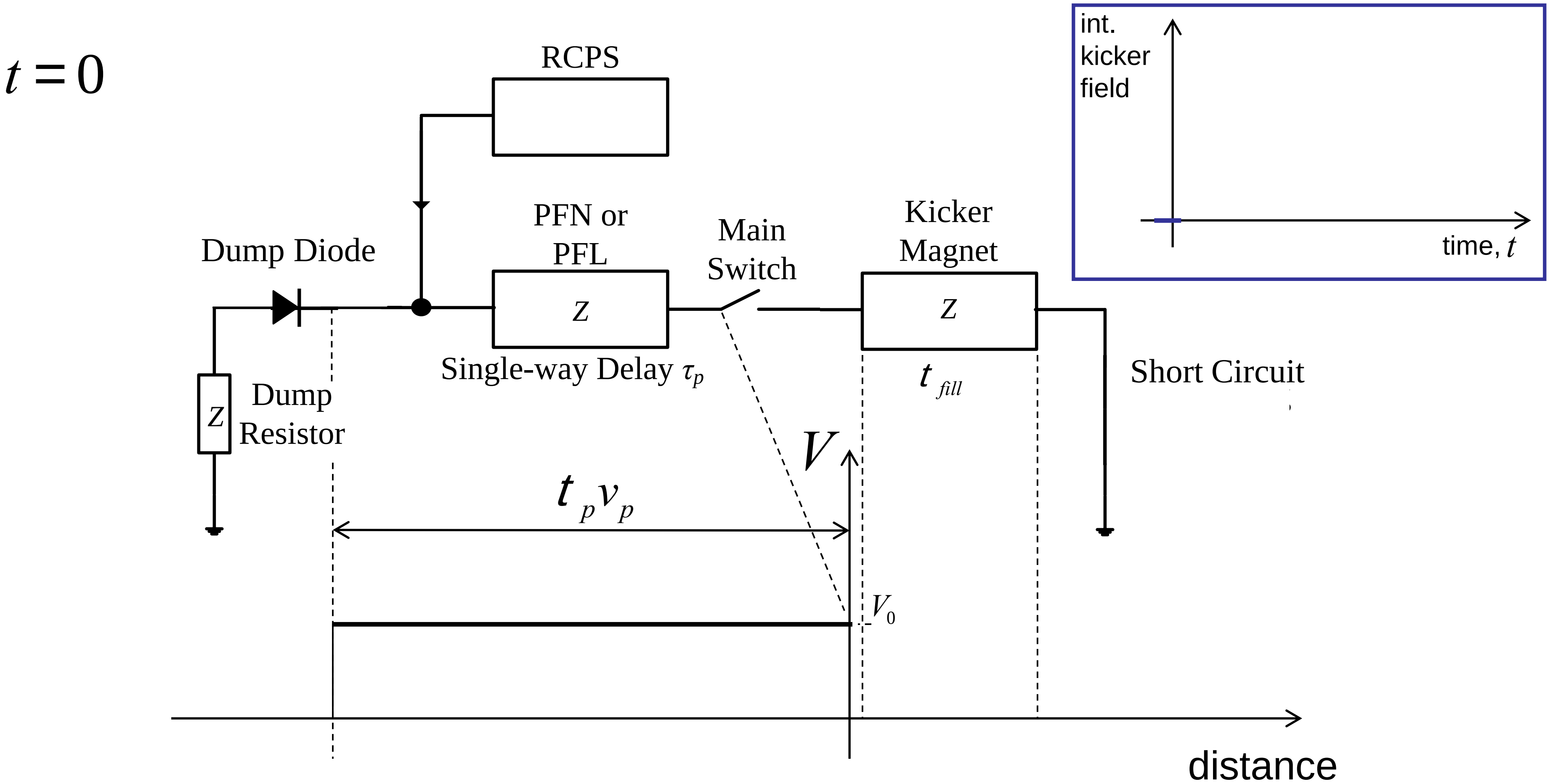
Simplified kicker system schematic



- Kicker pulse length can be changed by adjusting the relative timing of dump and main switches:
  - e.g. if the dump and main switches are fired simultaneously the pulse length will be halved and energy shared on dump and terminating resistors

Terminated vs. short circuit

- Short-circuiting the termination offers twice the kick (for a given kicker magnet):
  - Fill time of kicker magnet is doubled
  - Diode as dump switch provides solution for fixed pulse length



Terminated vs. short circuit

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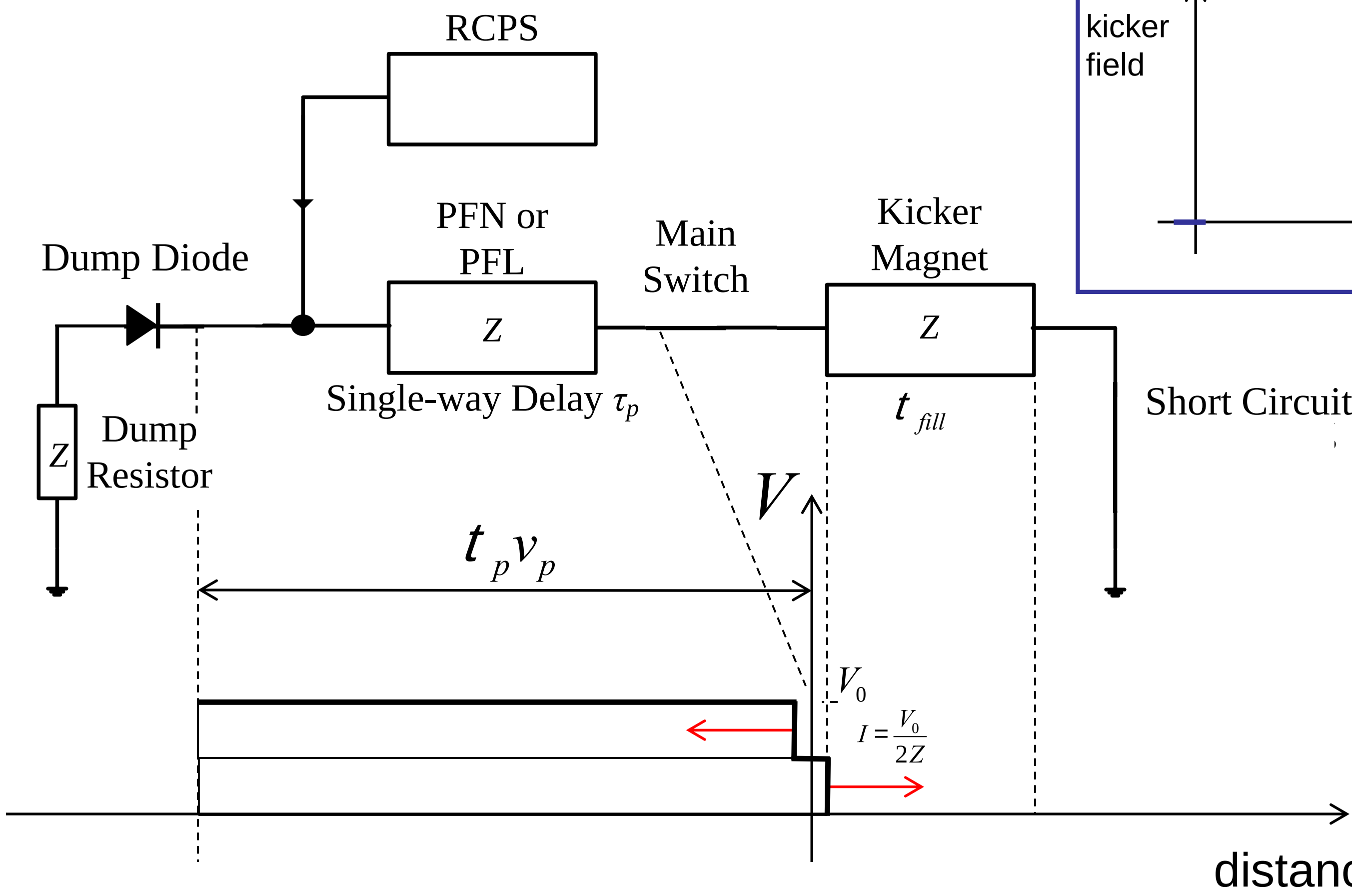
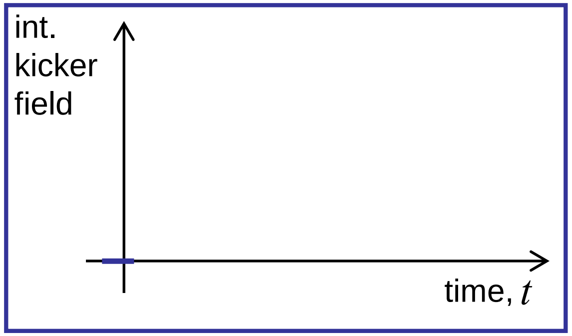
$t \gg 0$





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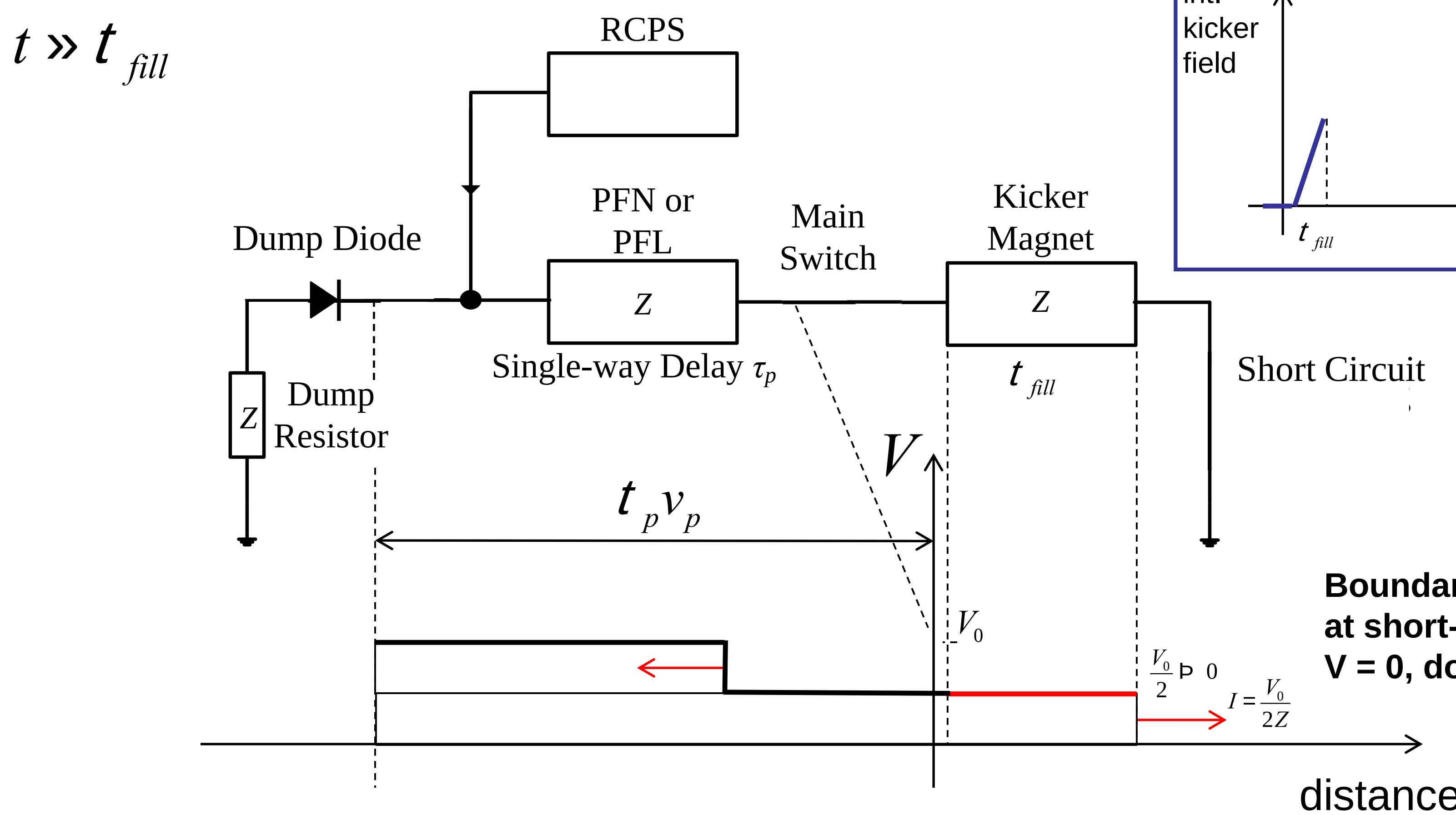
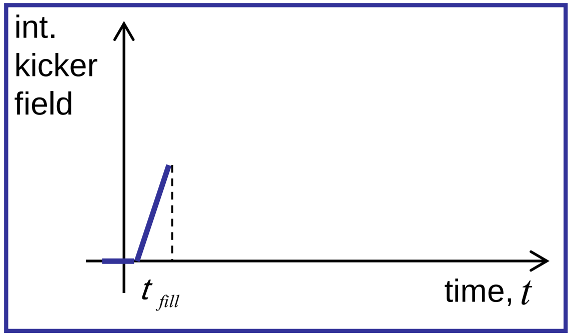


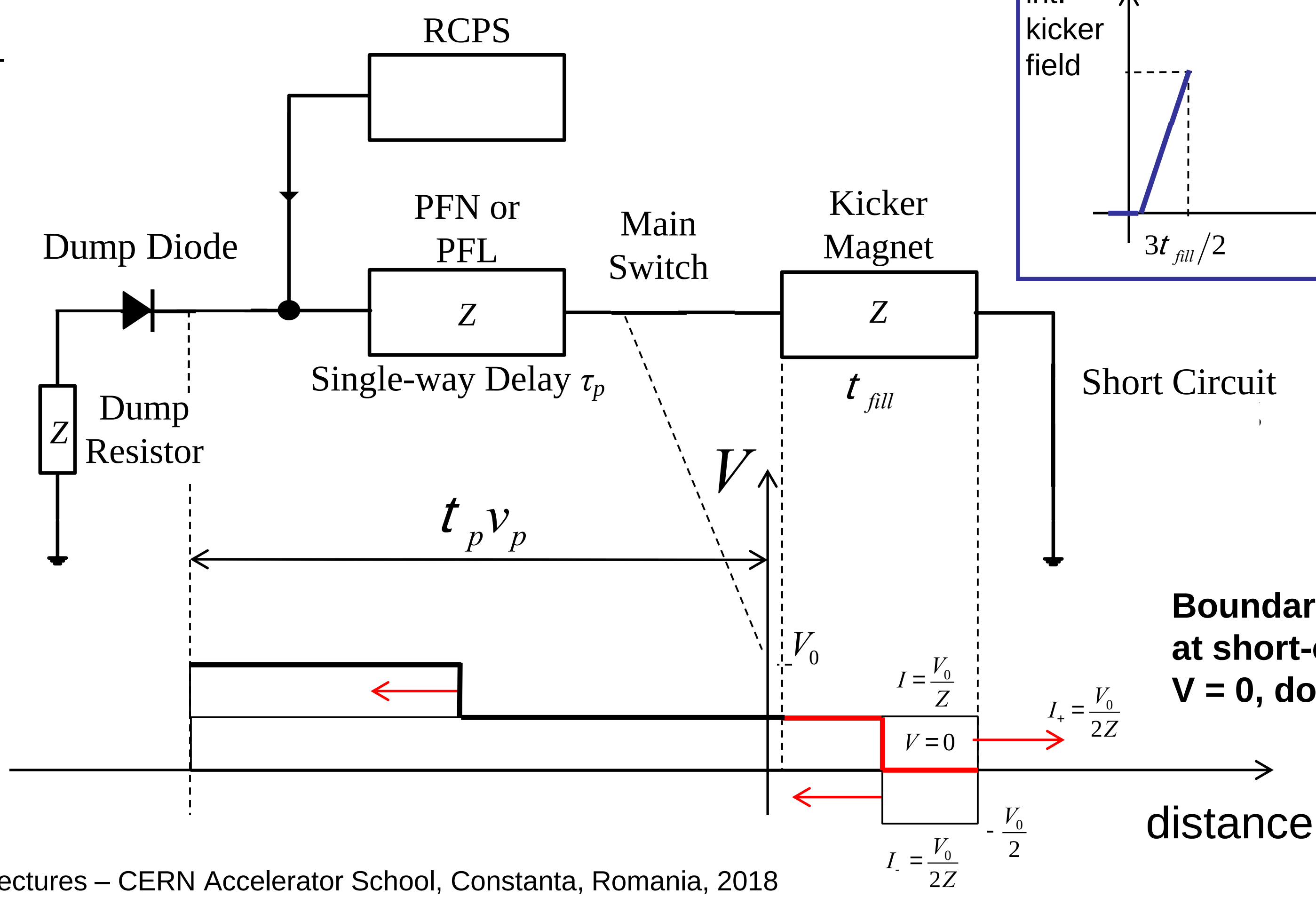


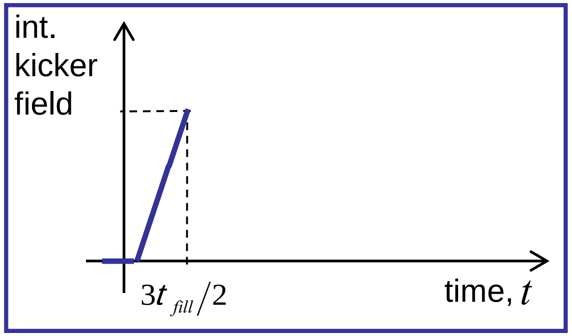
Boundary condition at short-circuit: V = 0, doubling I

Terminated vs. short circuit

- Short-circuiting the termination offers twice the kick (for a given kicker magnet):
  - Fill time of kicker magnet is doubled
  - Diode as dump switch provides solution for fixed pulse length

$$t \gg \frac{3t_{fill}}{2}$$





Boundary condition at short-circuit: V = 0, doubling I

Terminated vs. short circuit

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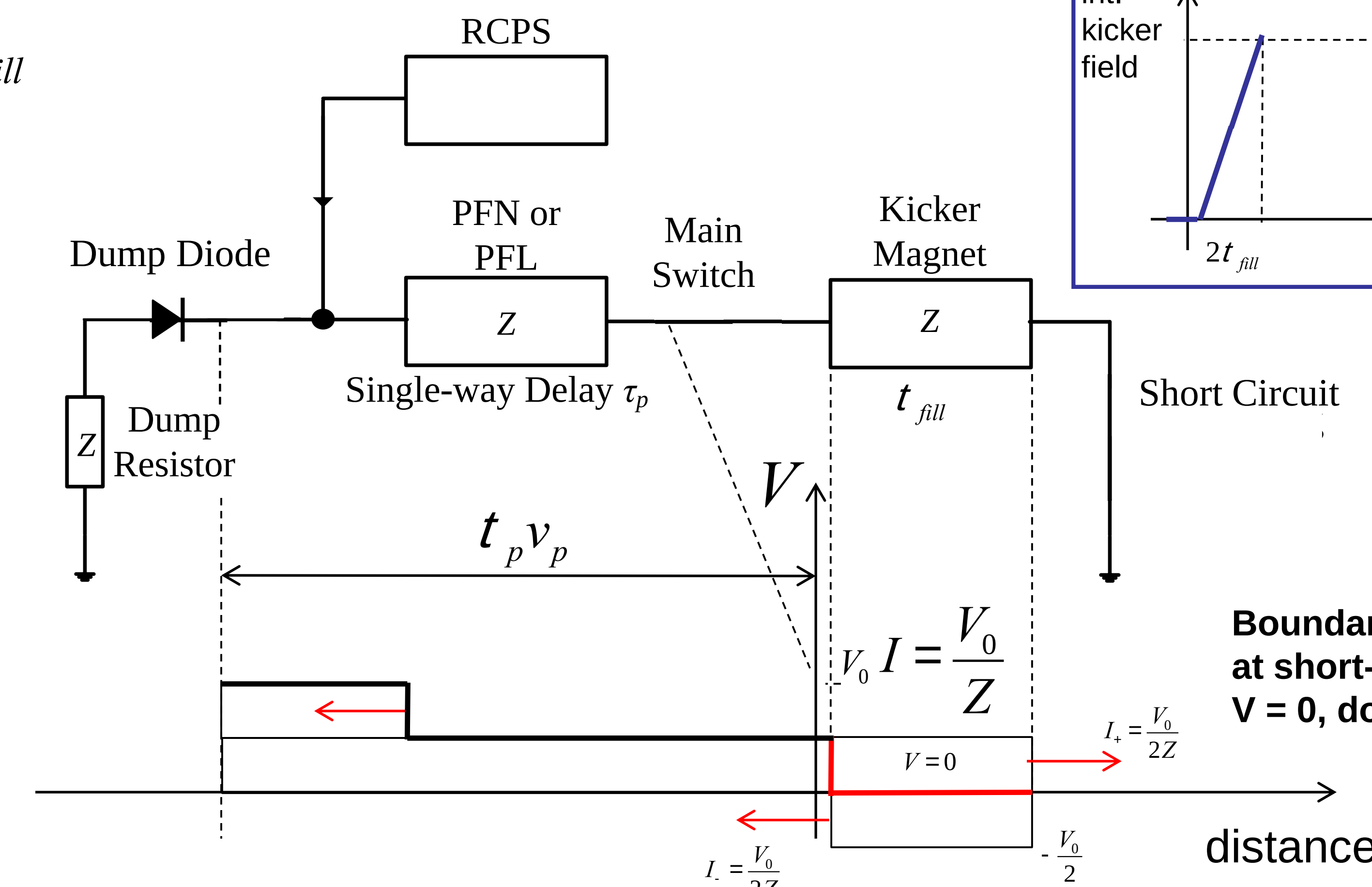
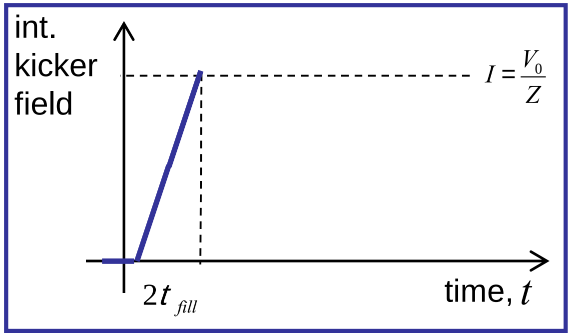
$t \gg 2t_{fill}$





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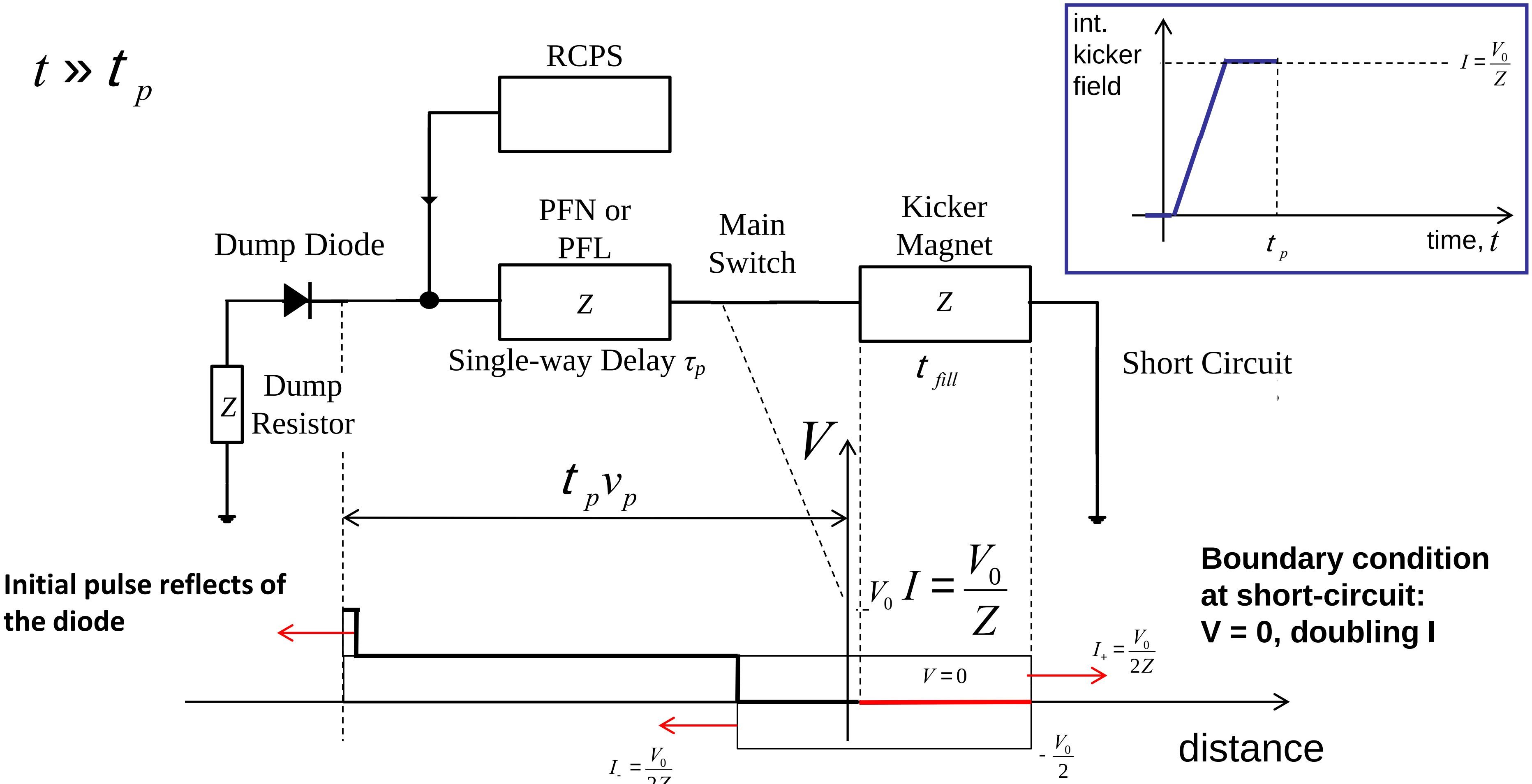

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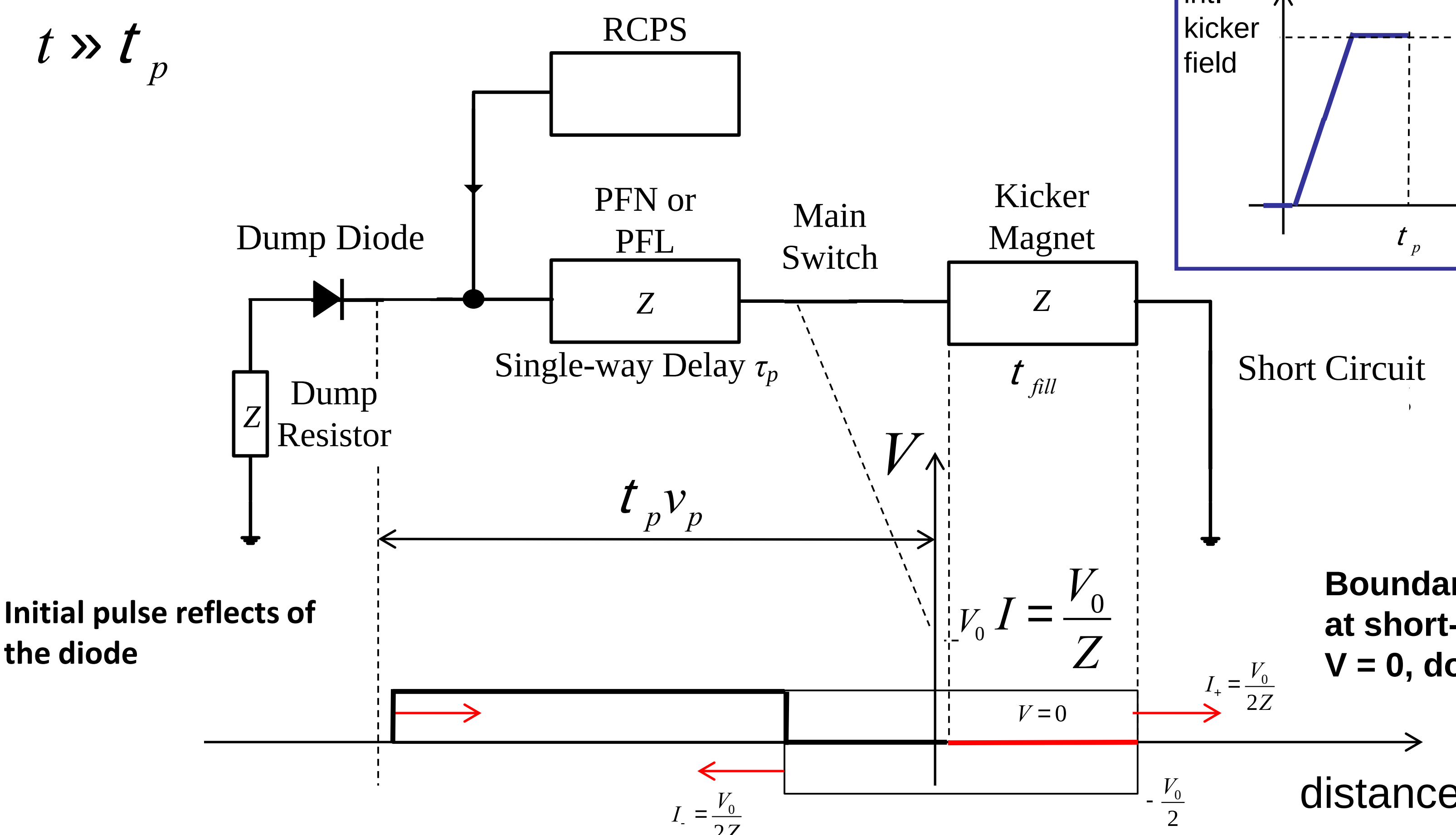

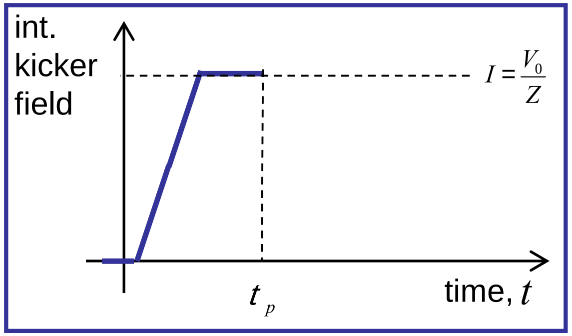

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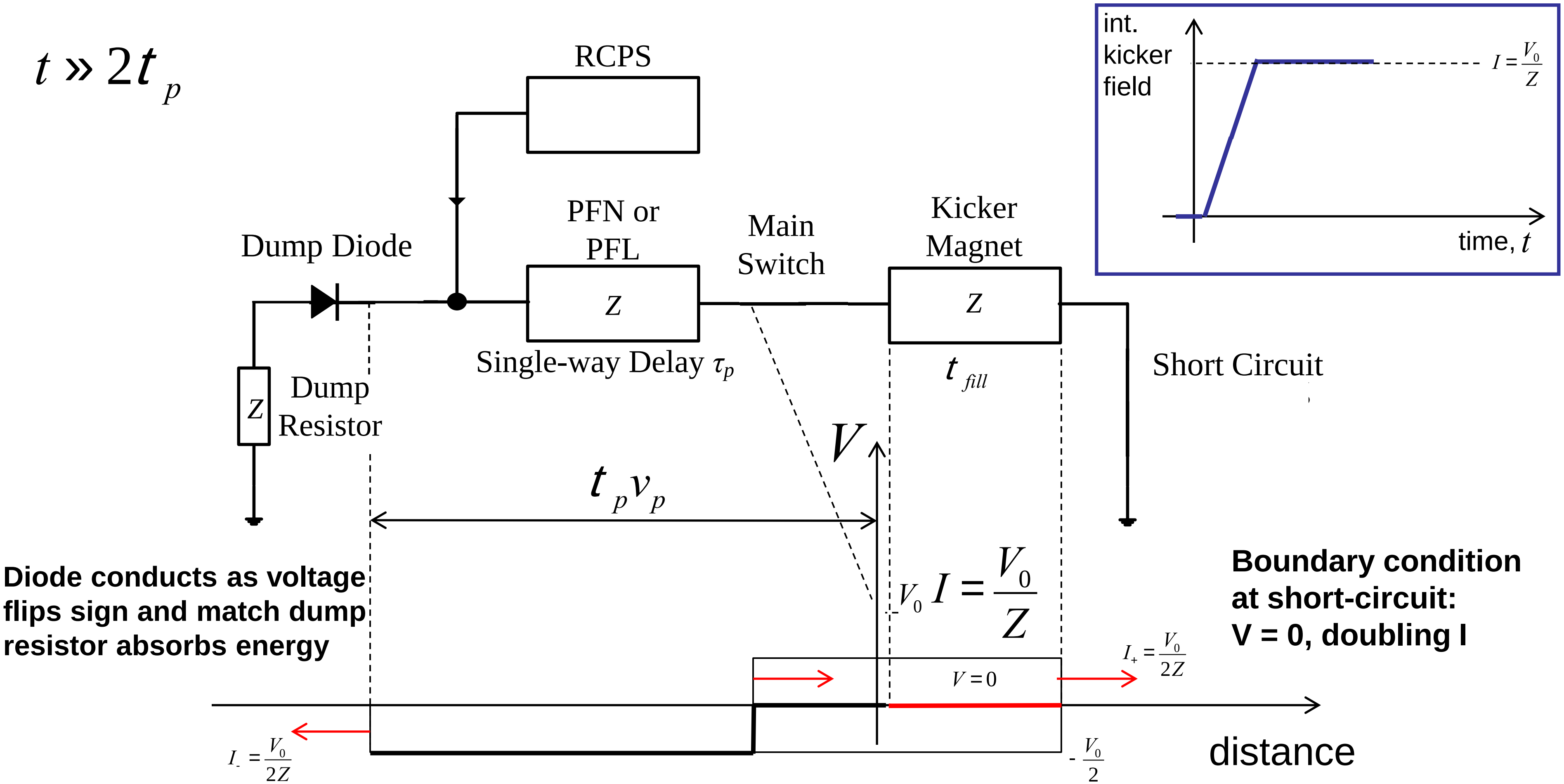

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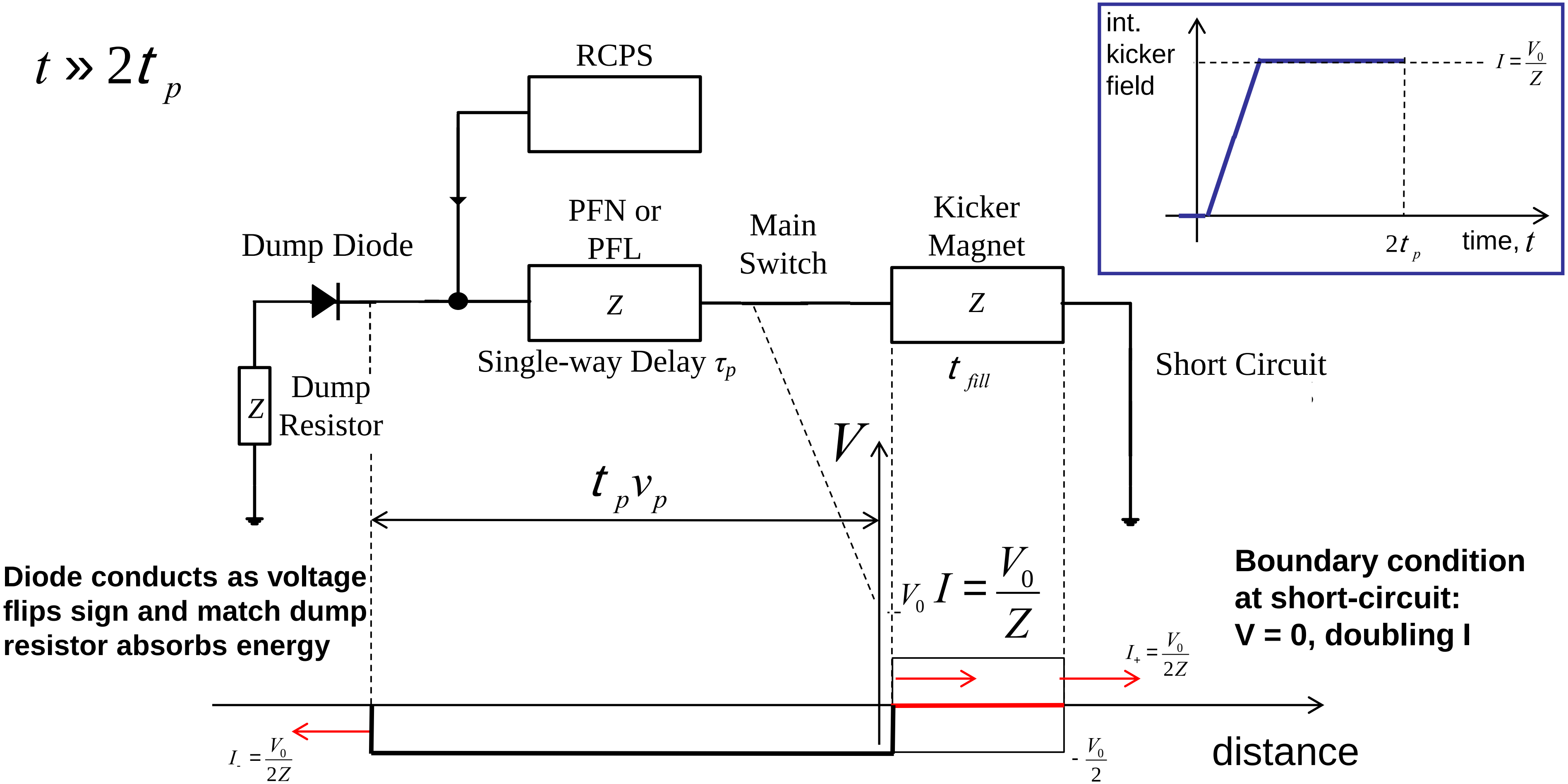

Diode conducts as voltage flips sign and match dump resistor absorbs energy

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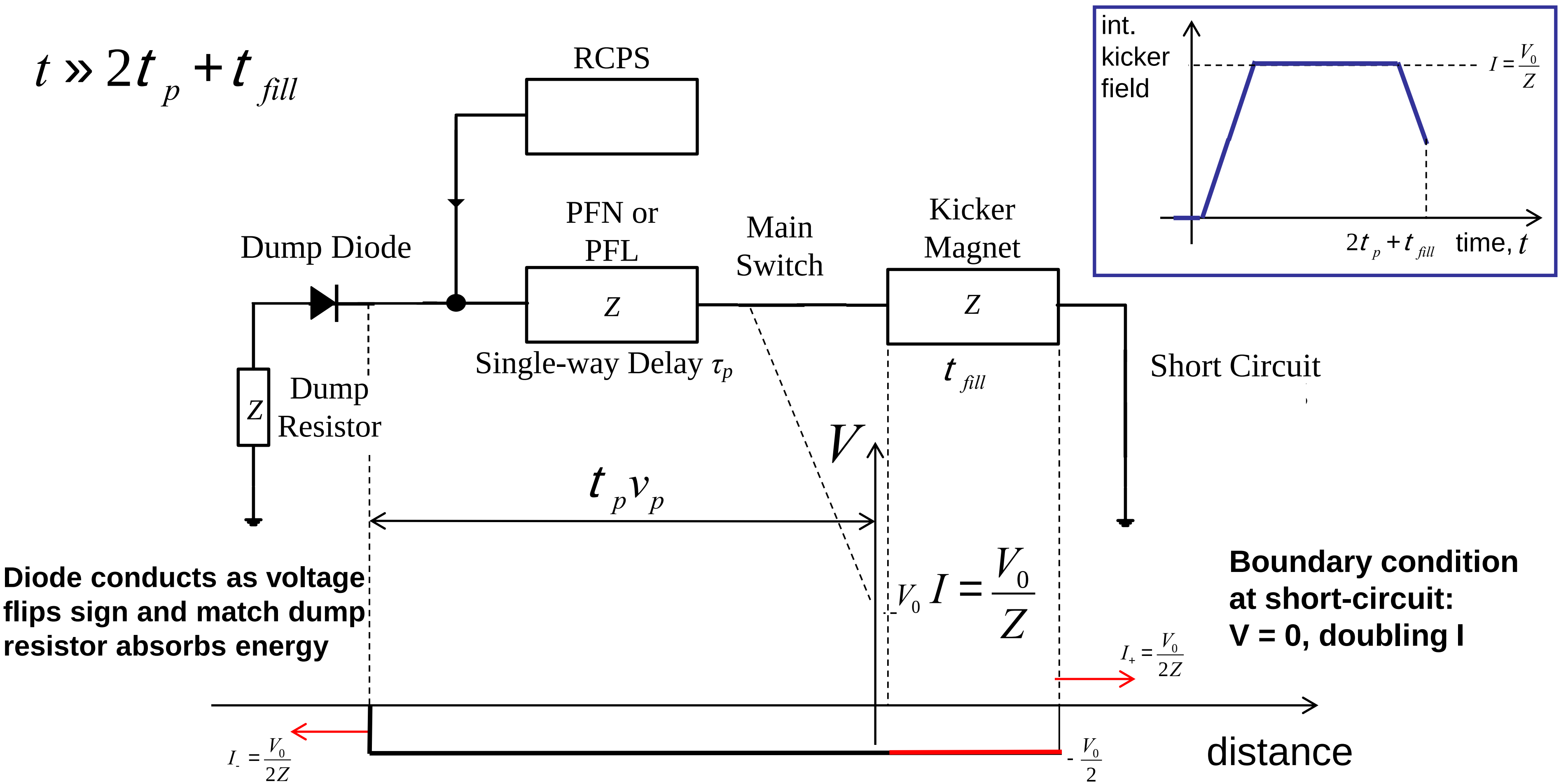

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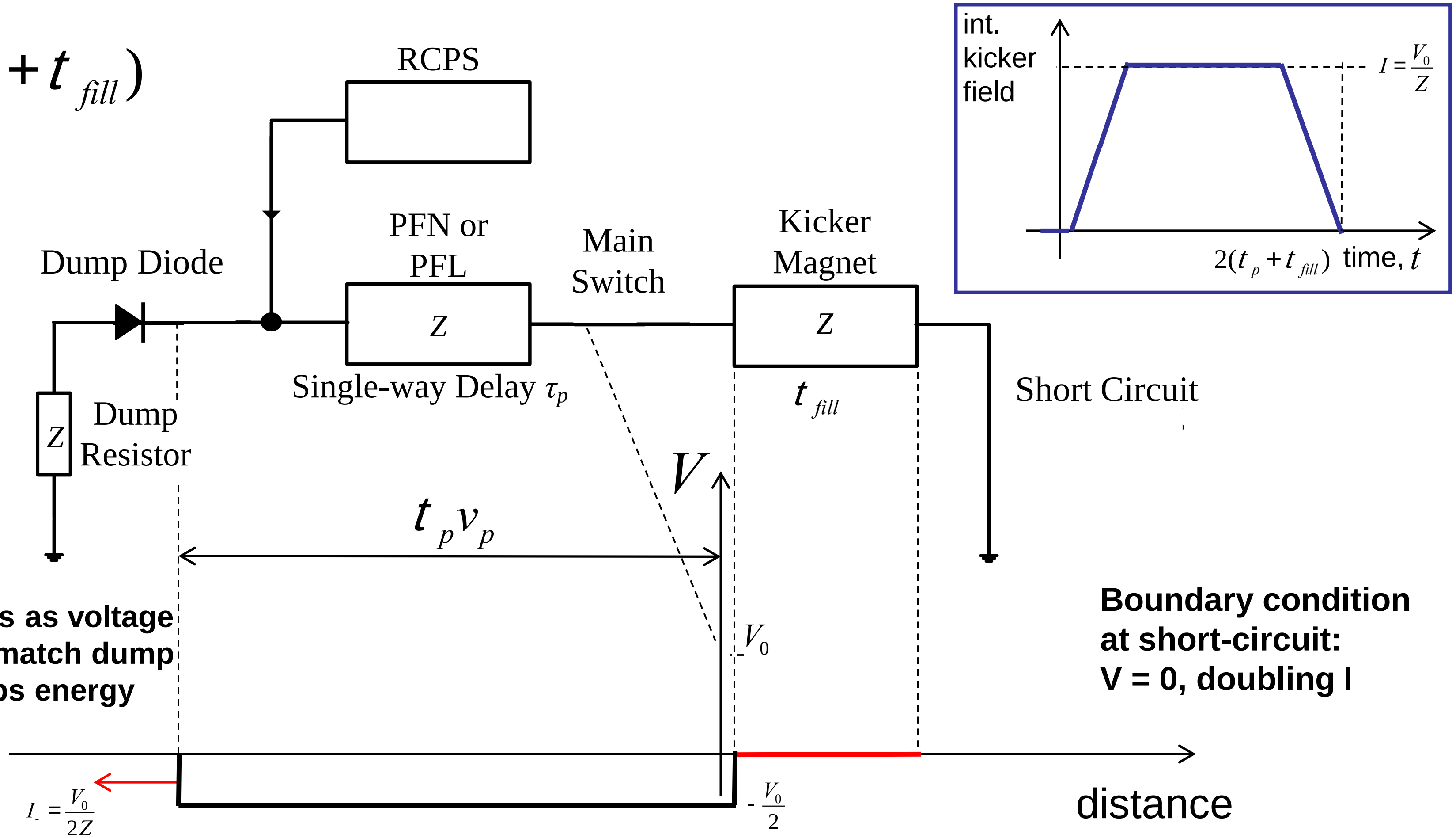
$$t \gg 2(t_p + t_{fill})$$



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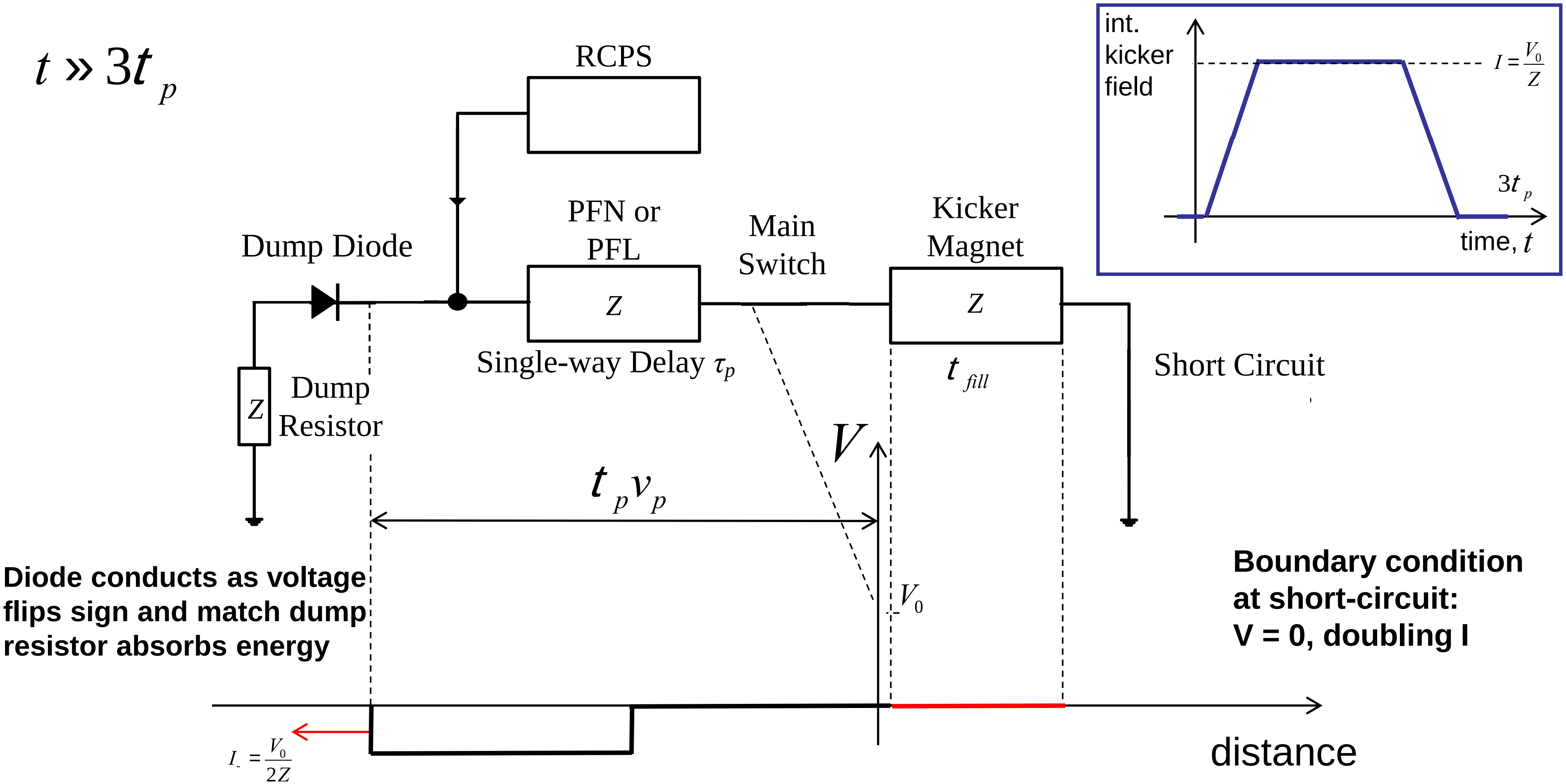

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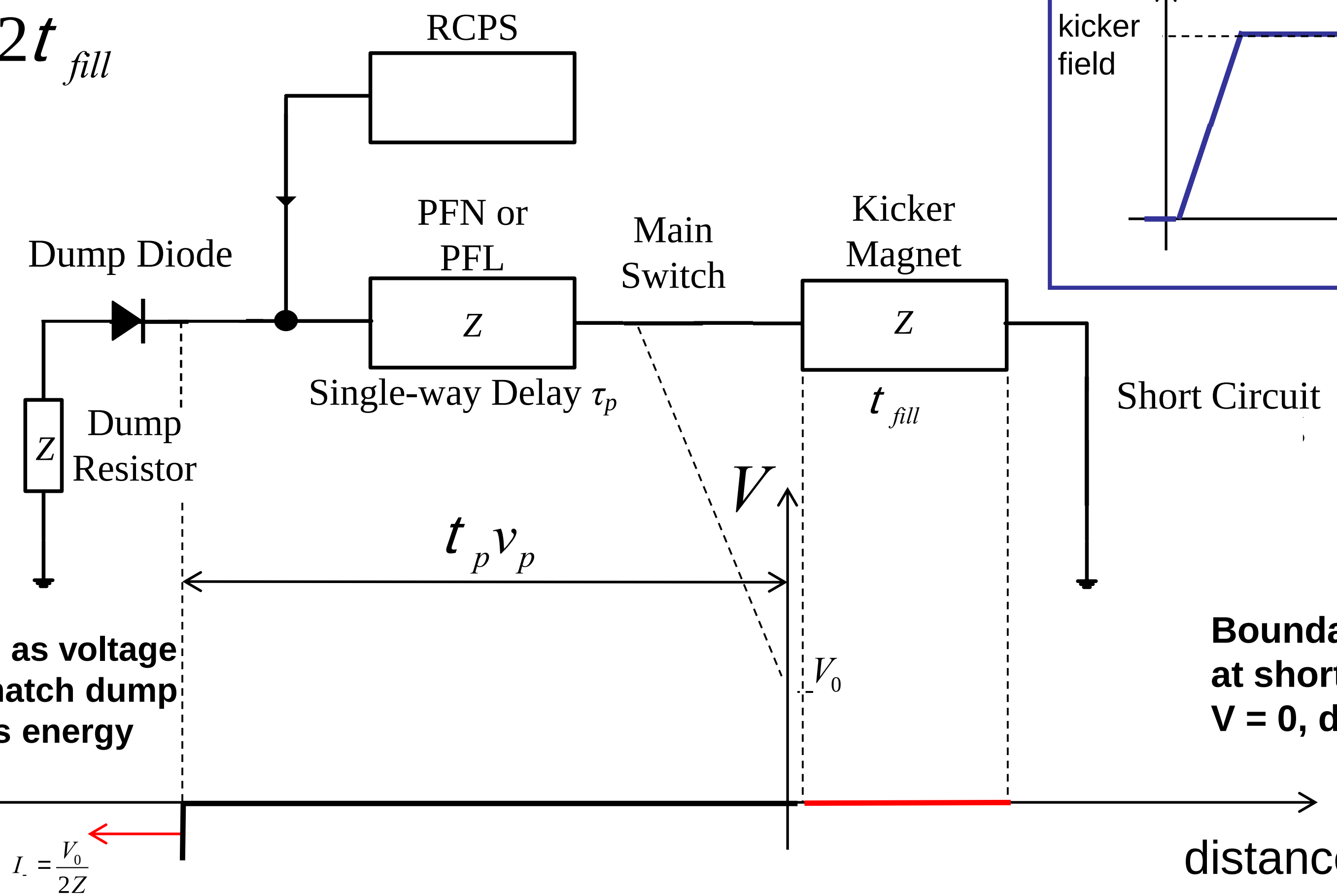
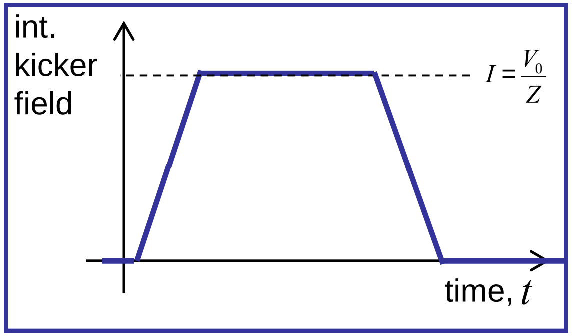
$$t = 3t_p + 2t_{fill}$$





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