

Experimental QCD at future pp & e^+e^- colliders

“Strong interactions”

ESPP Update

Granada, May 2019

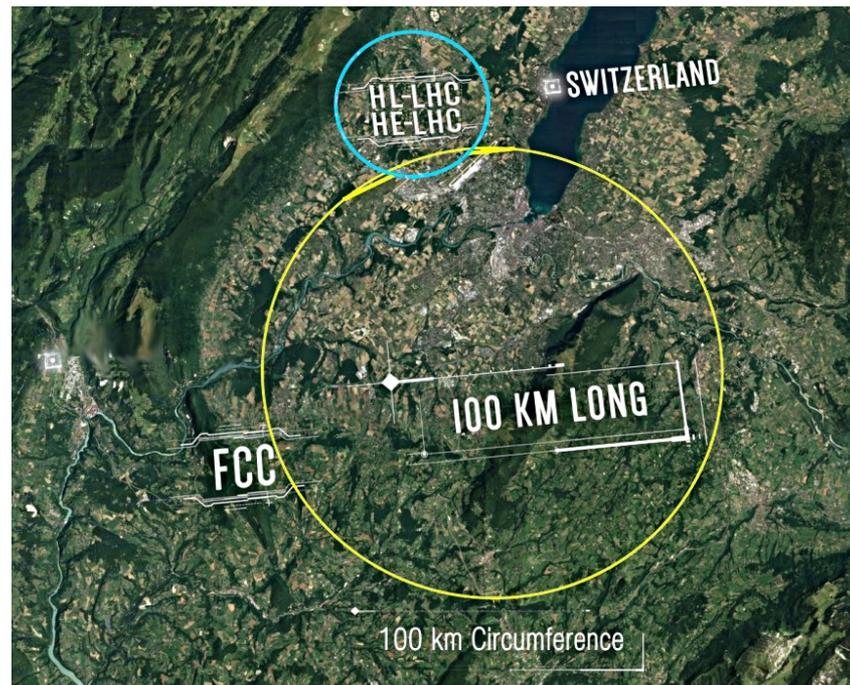
David d'Enterria

(CERN)

Future pp & e⁺e⁻ colliders with QCD programme

▶ Future proton-proton colliders:

1. HL-LHC: pp(14 TeV), 3 ab⁻¹
ESPPU input #110, #152
2. HE-LHC: pp(27 TeV), 10–15 ab⁻¹
ESPPU input #160
3. FCC-hh: pp(100 TeV), 20 ab⁻¹
ESPPU input #135



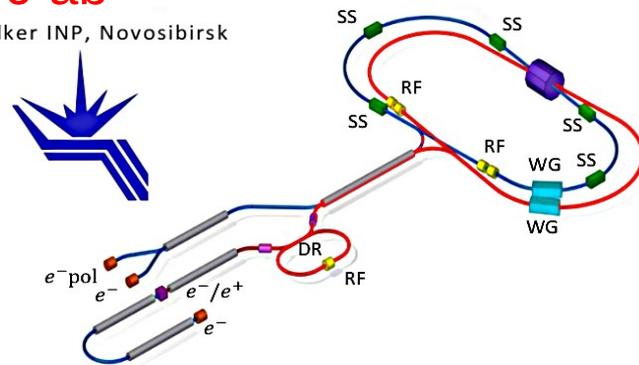
▶ Future electron-positron colliders:

4. FCC-ee(*): e⁺e⁻(90,160,250,350 GeV), 1–100 ab⁻¹
ESPPU input #160
5. SCT (Super Charm-Tau) Factory(**):
e⁺e⁻(2–6 GeV), ~1 ab⁻¹
ESPPU input #132

[Note: Other QCD machines: DIS, heavy-ions and/or fixed-target, covered by other talks].

[Note: Also in principle CEPC(*), BELLE-II(**) but to be developed]

Budker INP, Novosibirsk



QCD = Key piece at future ee, pp colliders

- ▶ Though QCD is *not per se* the main driving force behind future colliders, QCD is crucial for many pp, ee measurements (signals & backgrounds):
 - **High-precision α_s** : Affects all x-sections & decays (esp. Higgs, top, EWPOs).
 - **NⁿLO corr., NⁿLL resummations**: For all precise pQCD x-sections & decays.
 - **High-precision PDFs**: Affects all precision W,Z,H (mid-x) measurements & all searches (high-x) in pp collisions.
 - **Heavy-Quark/Quark/Gluon separation** (subjett structure, boosted topologies..): Needed for all precision SM measurements & BSM searches with final jets.
 - **Semihard QCD** (low-x gluon saturation, multiple hard parton interactions,...): Leading x-sections at FCC-pp (Note: $Q_0 \sim 10$ GeV at 100 TeV).
 - **Non-perturbative QCD**: Colour reconnection affects e⁺e⁻ jetty final-states: e⁺e⁻ → WW → 4j, Z → 4j, tt (m_{top} extraction). Parton hadronization, ...

QCD physics at future pp & e⁺e⁻ machines

(1) QCD coupling

(FCC-ee, FCC-pp, SCT)

(2) Parton Distribution Functions

(HL-LHC, HE-LHC, FCC-hh)

(3) Jet substructure & flavour tagging

(FCC-ee, FCC-pp)

(4) Non-perturbative QCD

(FCC-ee, SCT, HL-LHC)

NOTE: Only UNIQUE QCD measurements, inaccessible at any current machine, are covered.

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Importance of the QCD coupling α_s

- Least-known of couplings: $\delta\alpha \sim 10^{-10} \ll \delta G_F \ll 10^{-7} \ll \delta G \sim 10^{-5} \ll \delta\alpha_s \sim 10^{-3}$
- Impacts all QCD x-sects. & decays. Leading param. uncert. H, t, EWPOs:

Process	σ (pb)	$\delta\alpha_s$ (%)	PDF + α_s (%)	Scale (%)
ggH	49.87	± 3.7	-6.2 +7.4	-2.61 + 0.32
ttH	0.611	± 3.0	± 8.9	-9.3 + 5.9

Channel	M_H [GeV]	$\delta\alpha_s$ (%)	Δm_b	Δm_c
H $\rightarrow c\bar{c}$	126	± 7.1	$\pm 0.1\%$	$\pm 2.3\%$
H $\rightarrow gg$	126	± 4.1	$\pm 0.1\%$	$\pm 0\%$

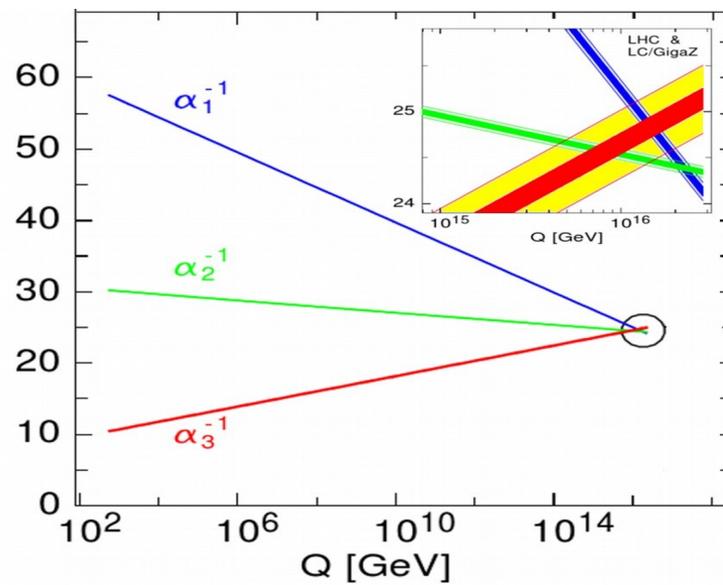
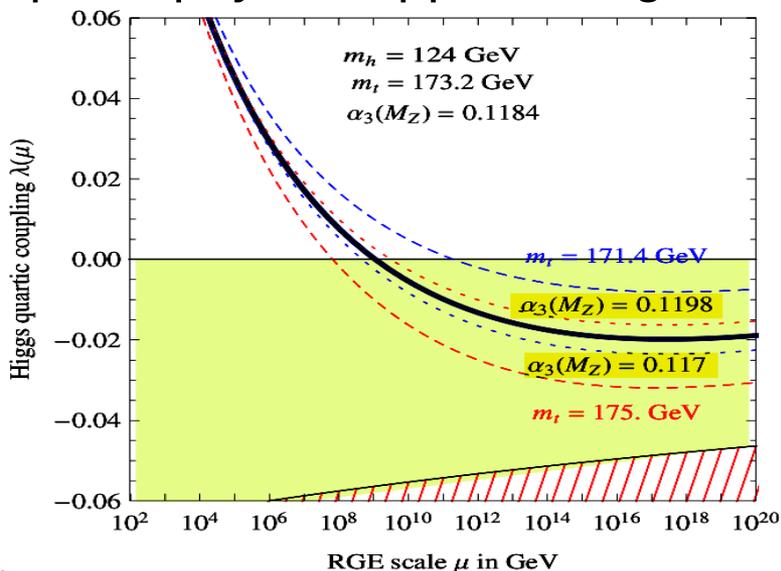
Msbar mass error budget (from threshold scan)

$(\delta M_t^{\text{SD-low}})_{\text{exp}}$	$(\delta M_t^{\text{SD-low}})_{\text{theo}}$	$(\delta \bar{m}_t(\bar{m}_t))_{\text{conversion}}$	$(\delta \bar{m}_t(\bar{m}_t))^{\alpha_s}$
40 MeV	50 MeV	7 - 23 MeV	70 MeV

\Rightarrow improvement in α_s crucial $\delta\alpha_s(M_Z) = 0.001$

Quantity	FCC-ee	future param.unc.	Main source
Γ_Z [MeV]	0.1	0.1	$\delta\alpha_s$
R_b [10^{-5}]	6	< 1	$\delta\alpha_s$
R_ℓ [10^{-3}]	1	1.3	$\delta\alpha_s$

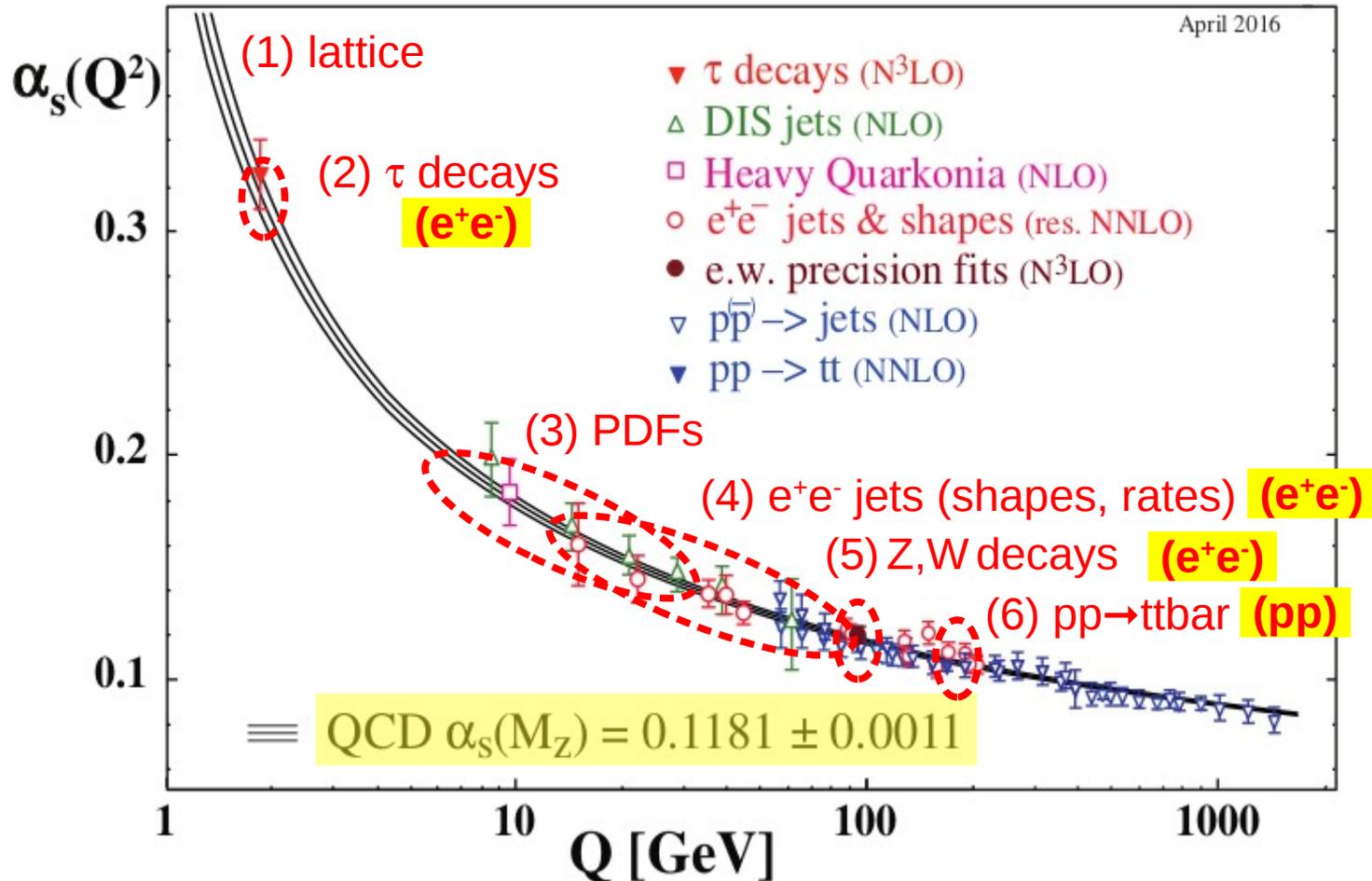
- Impacts physics approaching Planck scale: EW vacuum stability, GUT



World α_s determination (PDG 2018)

- Determined today by comparing 6 experimental observables to pQCD NNLO, N³LO predictions, plus global average at the Z pole scale:

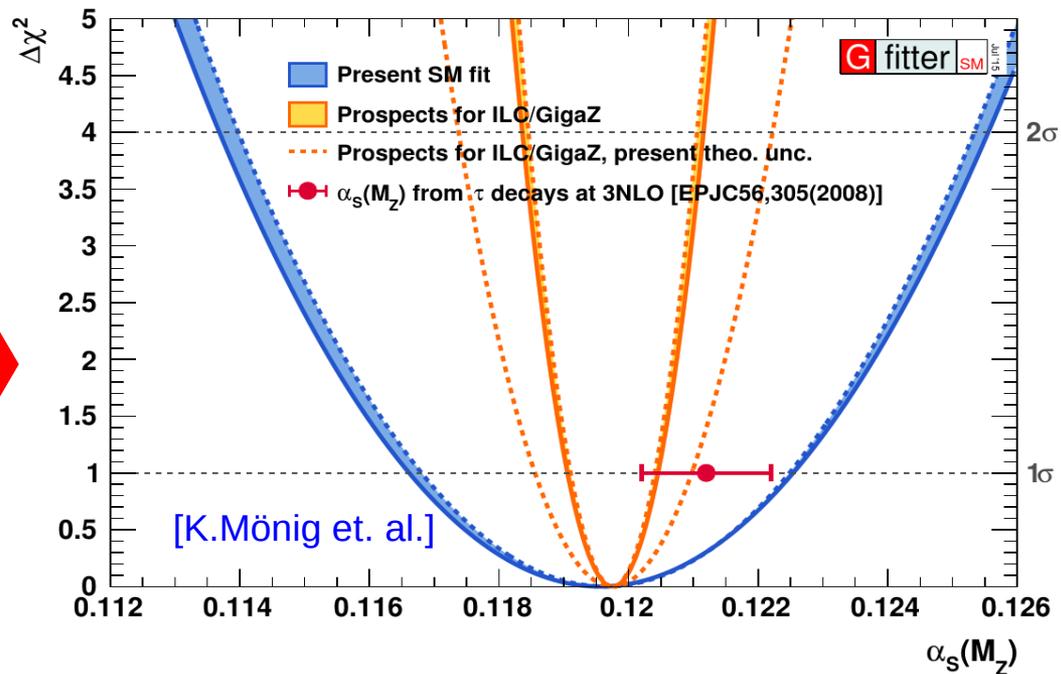
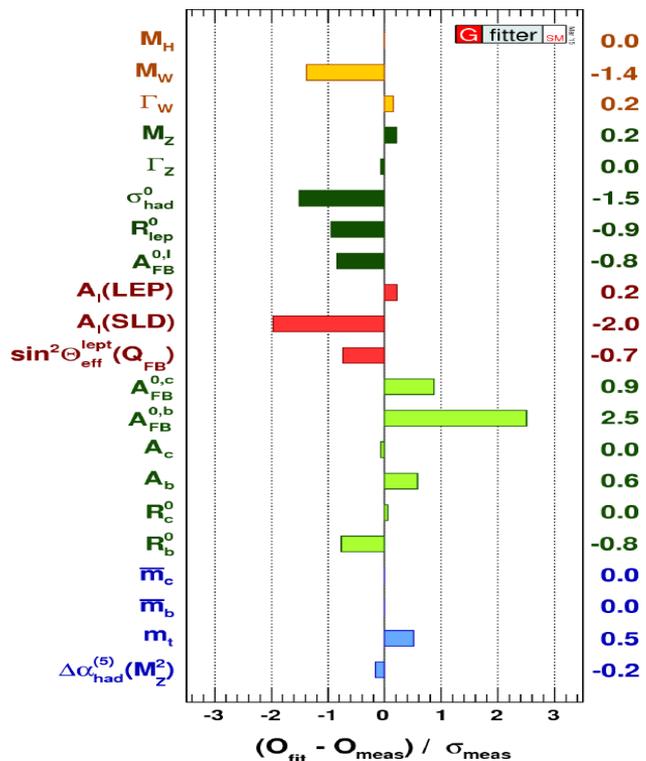
[Bethke/Dissertori/Salam]



α_s via hadronic Z decays (FCC-ee)

- Computed at **N³LO**: $R_Z \equiv \frac{\Gamma(Z \rightarrow h)}{\Gamma(Z \rightarrow l)} = R_Z^{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n \left(\frac{\alpha_s}{\pi}\right)^n + \mathcal{O}(\alpha_s^5) + \delta_m + \delta_{\text{np}})$
- LEP** Z pseudobservables: $R_\ell^0 = \frac{\Gamma_{\text{had}}}{\Gamma_\ell}$, $\sigma_{\text{had}}^0 = \frac{12\pi}{m_Z} \frac{\Gamma_e \Gamma_{\text{had}}}{\Gamma_Z^2}$, $\sigma_\ell^0 = \frac{12\pi}{m_Z} \frac{\Gamma_\ell^2}{\Gamma_Z^2}$ (exp. unc. <0.1%)

Also after Higgs discovery, α_s can be directly determined from **full fit of SM**:



Today: $\alpha_s(M_Z) = 0.1196 \pm 0.0030$ ($\pm 2.5\%$)

- FCC-ee**: – Z stats ($\times 10^5$ LEP) will lead to: **$\delta \alpha_s < 0.15\%$**

– TH (parametric) uncertainties: $\sin^2 \theta_{\text{eff}}, m_W, m_{\text{top}}$

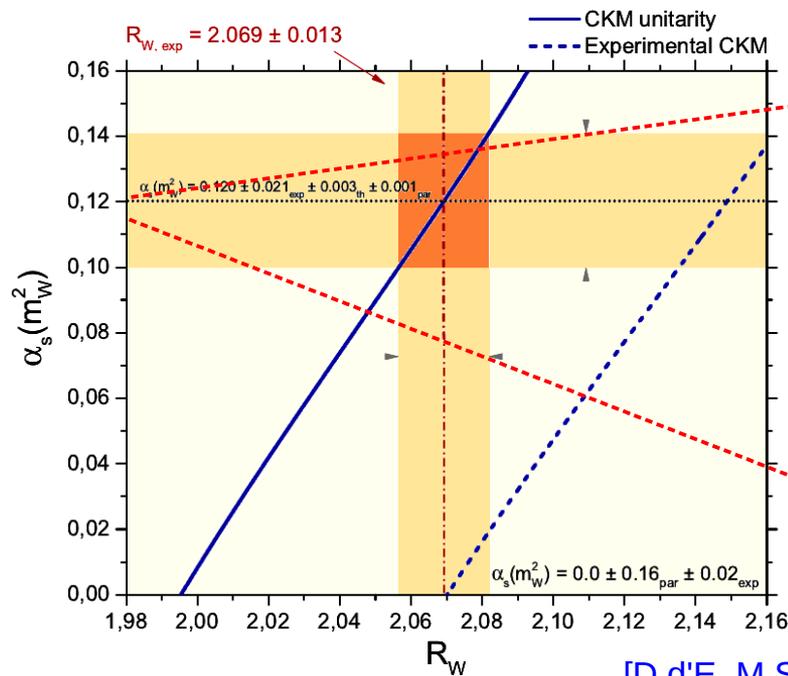
α_s via hadronic W decays (FCC-ee)

➔ Computed at **N^{2,3}LO**: $\Gamma_{W,\text{had}} = \frac{\sqrt{2}}{4\pi} G_F m_W^3 \sum_{\text{quarks } i,j} |V_{i,j}|^2 \left[1 + \sum_{k=1}^4 \left(\frac{\alpha_s}{\pi} \right)^k + \delta_{\text{electroweak}}(\alpha) + \delta_{\text{mixed}}(\alpha\alpha_s) \right]$

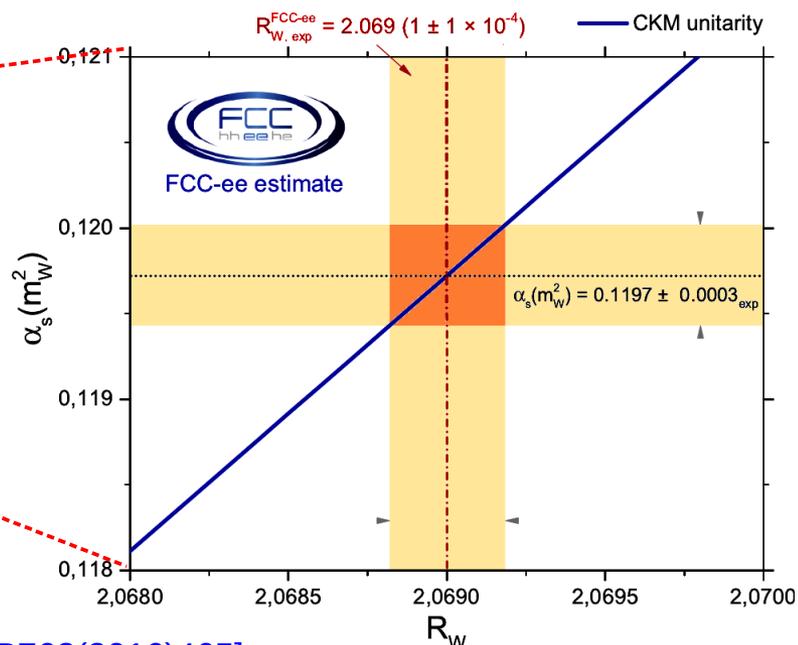
➔ **LEP**: $BR_W = 0.6741 \pm 0.0027$ ($\pm 0.4\%$)

Extraction with **large exp. & parametric**
(CKM V_{CS}) **uncertainties**:

Today: $\alpha_s(M_Z) = 0.117 \pm 0.040$ ($\pm 35\%$)



[D.d'E, M.Srebre, PLB763(2016)465]



➔ **FCC-ee**: – Huge W stats ($\times 10^4$ LEP) **will lead to: $\delta\alpha_s < 0.2\%$**

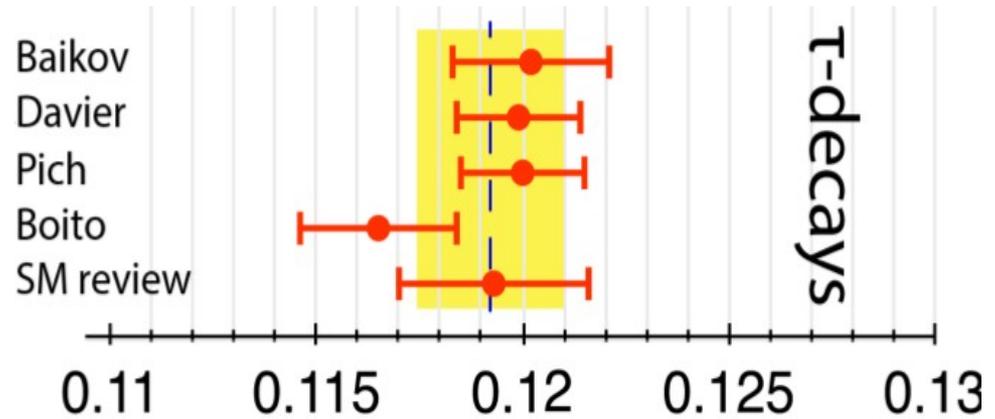
– TH (param.) uncertainty: $|\delta V_{CS}|$ to be significantly improved (10^{-4})

α_s from hadronic τ decays (SCT, FCC-ee)

➔ Computed at **N³LO**: $R_\tau \equiv \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} = S_{\text{EW}} N_C (1 + \sum_{n=1}^4 c_n \left(\frac{\alpha_s}{\pi}\right)^n + \mathcal{O}(\alpha_s^5)) + \delta_{\text{np}}$

➔ Experimentally: $R_{\tau, \text{exp}} = 3.4697 \pm 0.0080$ ($\pm 0.23\%$)

➔ Various pQCD approaches (FOPT vs CIPT) & treatment of non-pQCD corrections (note: $(\Lambda/m_\tau)^2 \sim 1\%$), yield different results.



Today: $\alpha_s(M_Z) = 0.1192 \pm 0.0018$ ($\pm 1.5\%$)

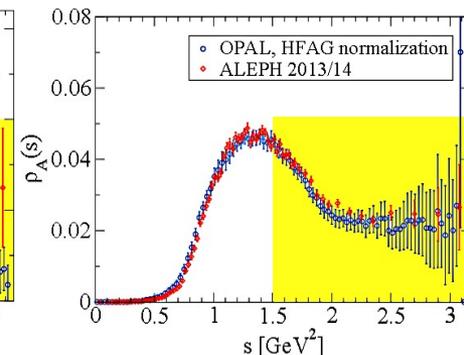
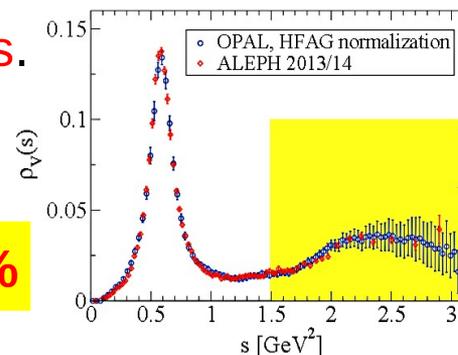
➔ Future prospects:

- Understand **FOPT vs CIPT differences**.
- **Better exp. spectral functions** needed (high stats & better precision):

SCT: $\mathcal{O}(10^{10})$ $e^+e^- \rightarrow \tau\tau$

FCC-ee: $\mathcal{O}(10^{11})$ from $Z(\tau\tau)$

$\delta\alpha_s < 1\%$



α_s running at the TeV scale (FCC-pp)

- Proton-proton collisions above LHC energies provide the only known means to **test asymptotic freedom & new coloured sectors above ~ 3 TeV**:

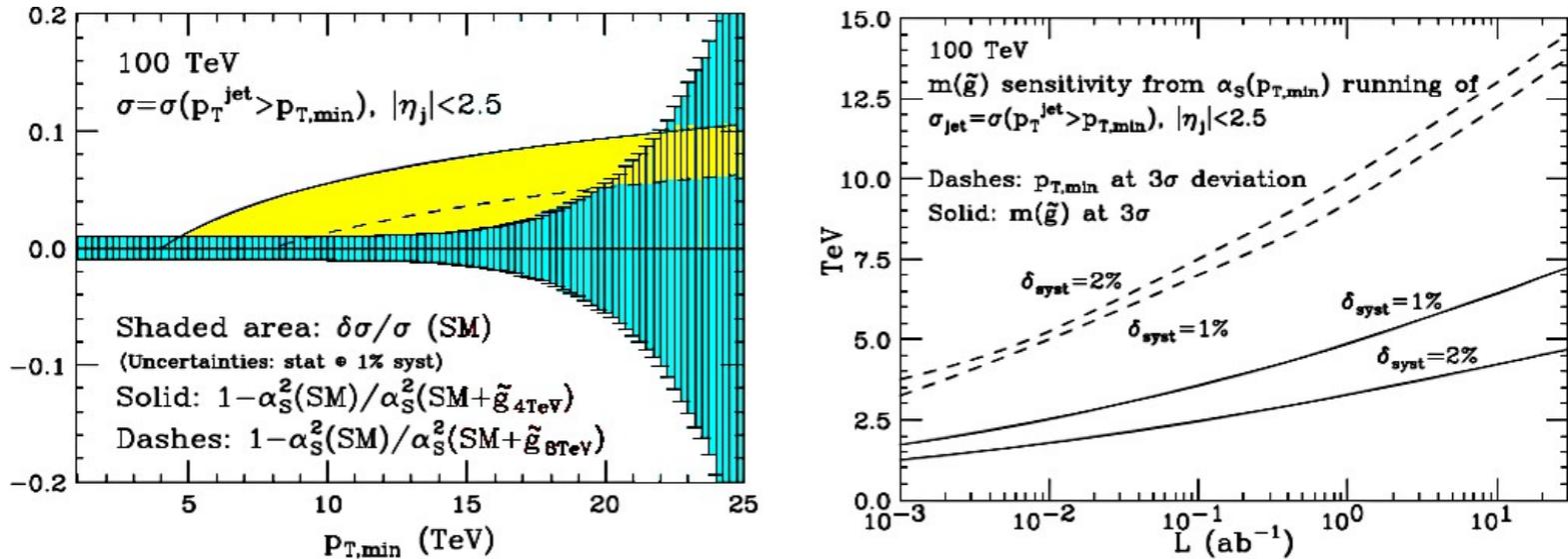


Figure 5.5: Left plot: combined statistical and 1% systematic uncertainties, at 30 ab^{-1} , vs p_T threshold; these are compared to the rate change induced by the presence of 4 or 8 TeV gluinos in the running of α_s . Right plot: the gluino mass that can be probed with a 3σ deviation from the SM jet rate (solid line), and the p_T scale at which the corresponding deviation is detected.

- FCC-pp**:
 - Jet cross sections with $<10\%$ stat. uncert. **up to $p_T \sim 25$ TeV**
 - **Sensitivity to $m_g = 4\text{--}8$ GeV gluinos** in α_s running.

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(FCC-ee, FCC-pp, SCT)

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(HL-LHC, HE-LHC, FCC-hh)

(3) Jet substructure & flavour tagging

(FCC-ee, FCC-pp)

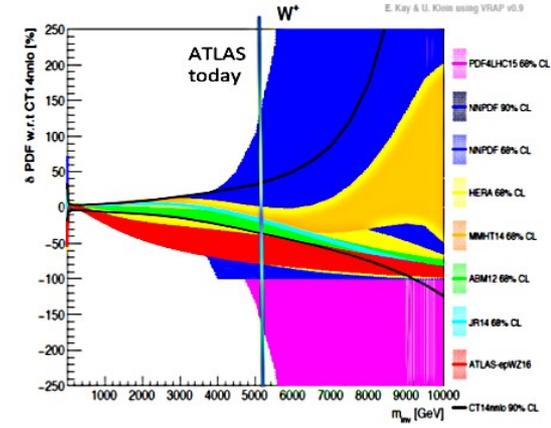
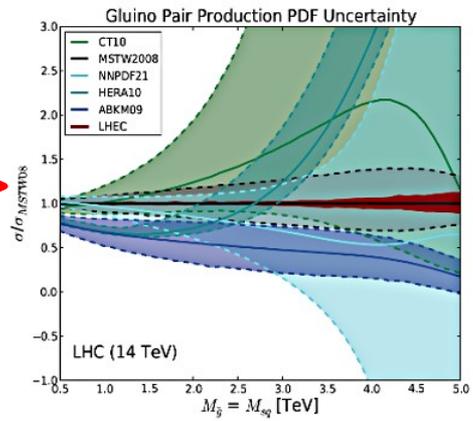
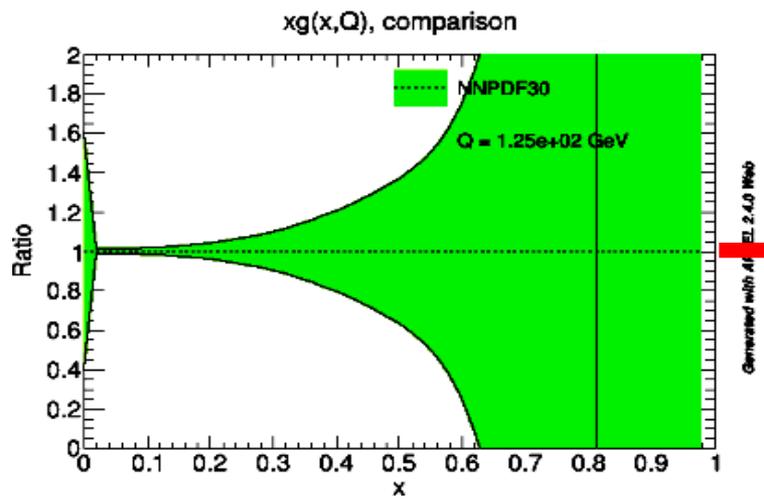
(4) Non-perturbative QCD

(FCC-ee, SCT, HL-LHC)

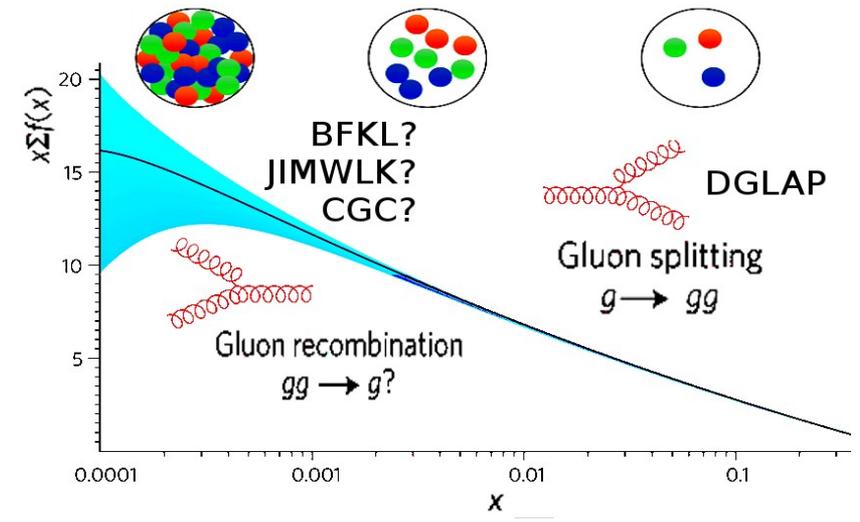
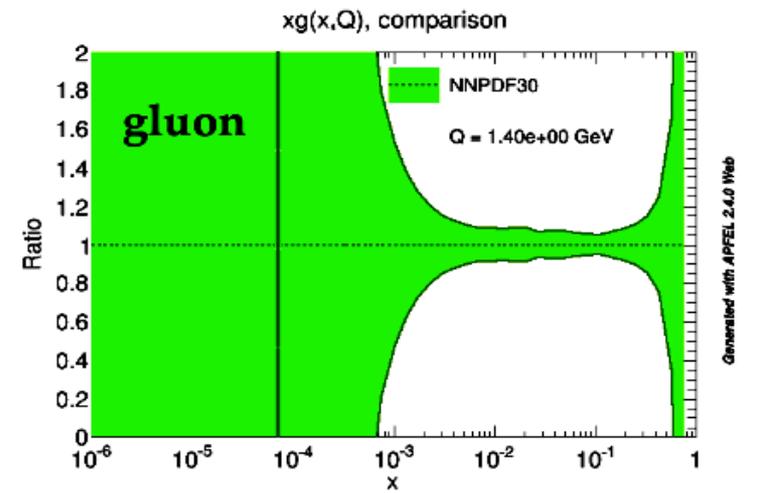
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PDFs impact on new BSM / QCD physics

New physics at high-x?

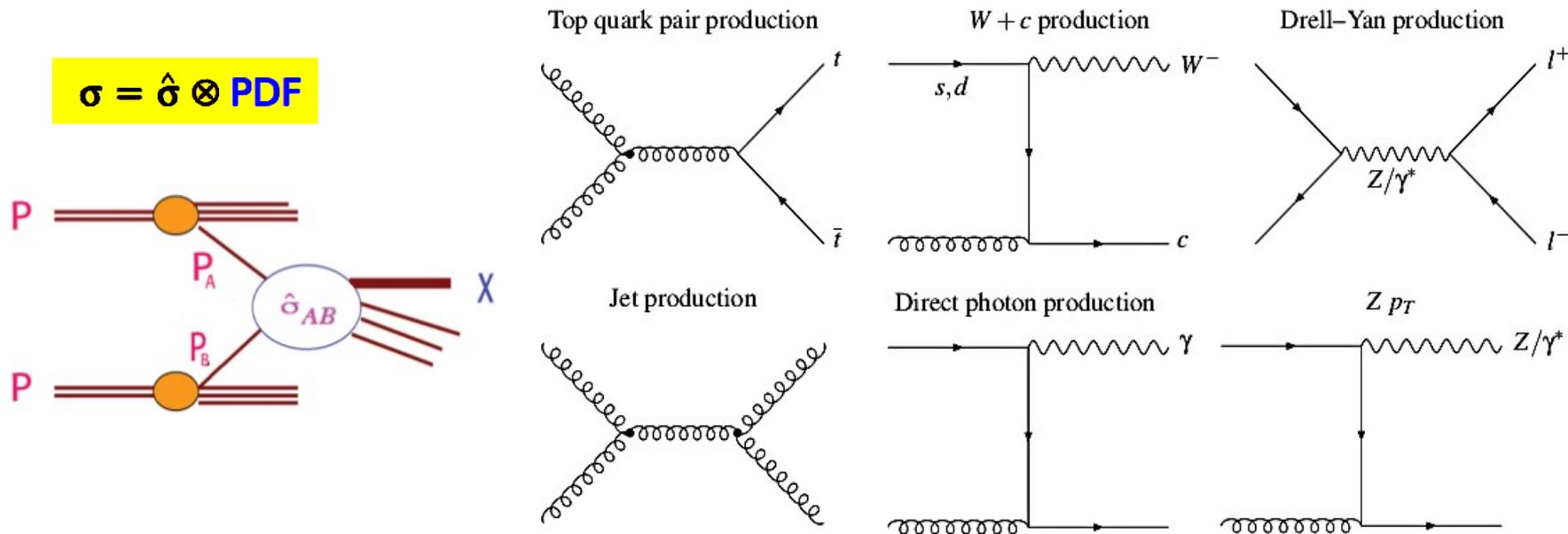


New QCD evolution at low-x?



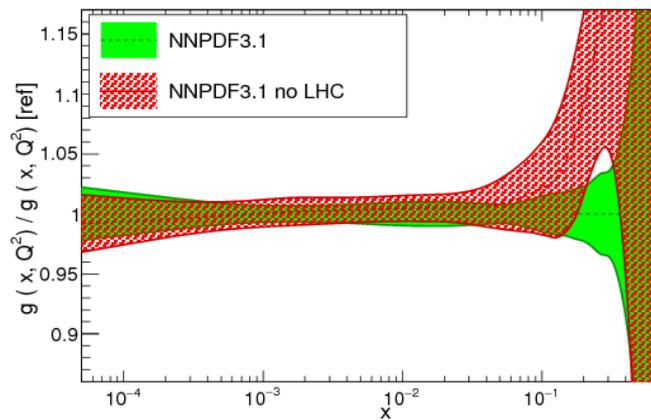
Improving PDFs with proton-proton data

- 6 partonic processes in pp at the LHC have provided key PDF constraints:

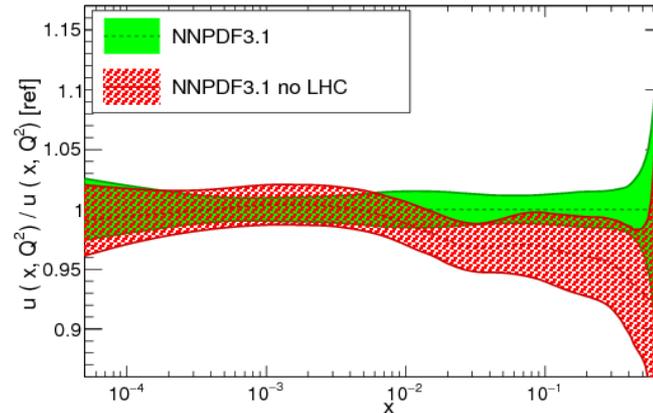


- Improved NNLO g, u, ... PDFs already today using LHC data:

NNPDF3.1 NNLO, Q = 100 GeV

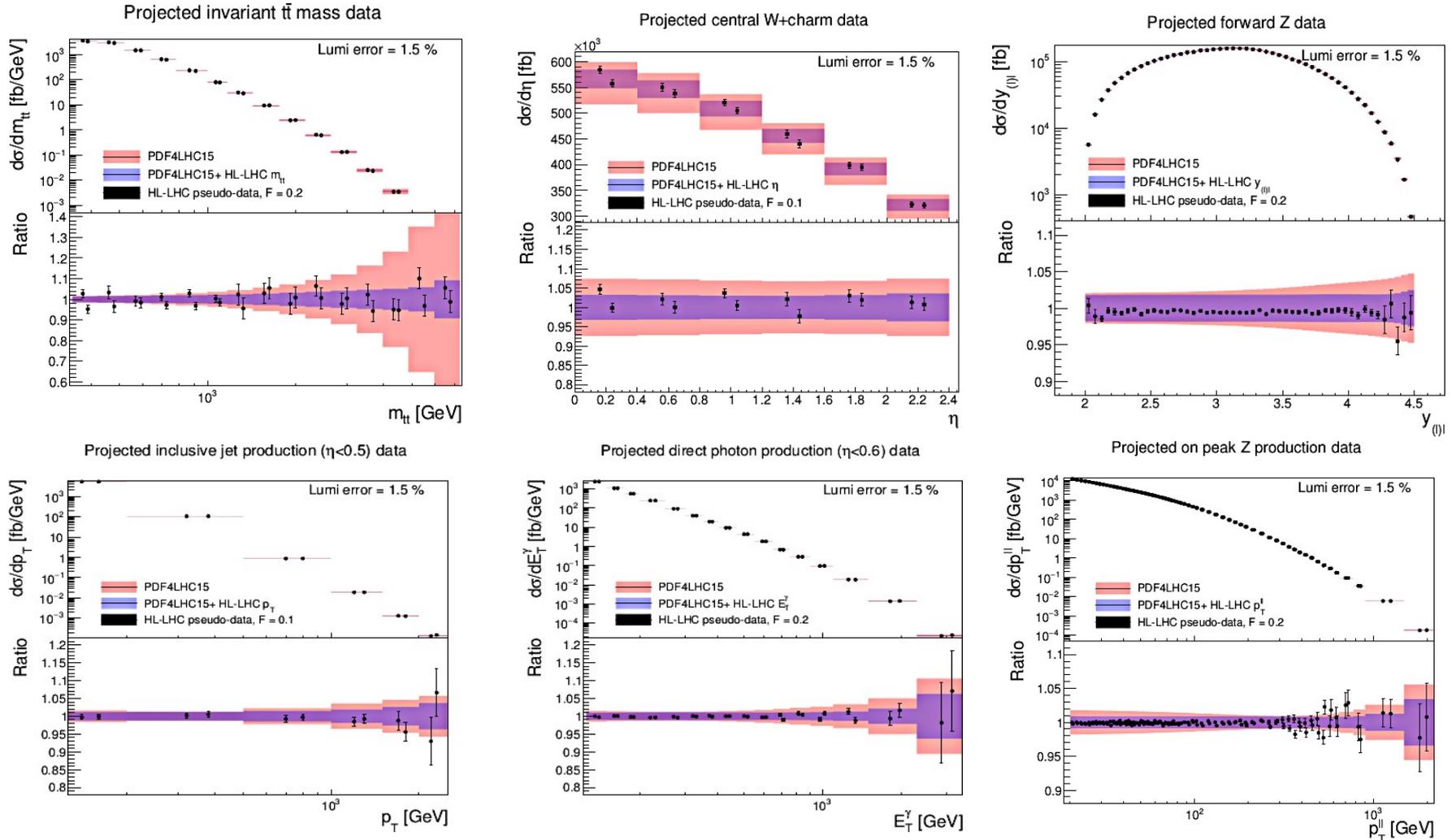


NNPDF3.1 NNLO, Q = 100 GeV



Improved PDFs with pp data (HL-LHC)

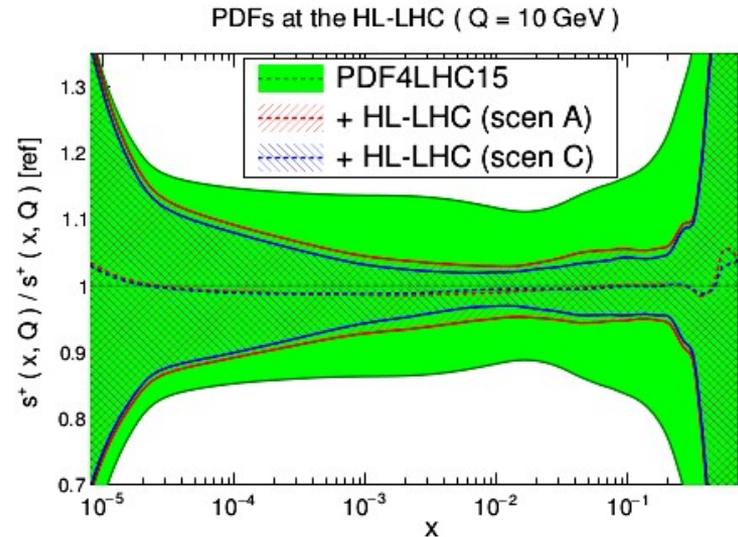
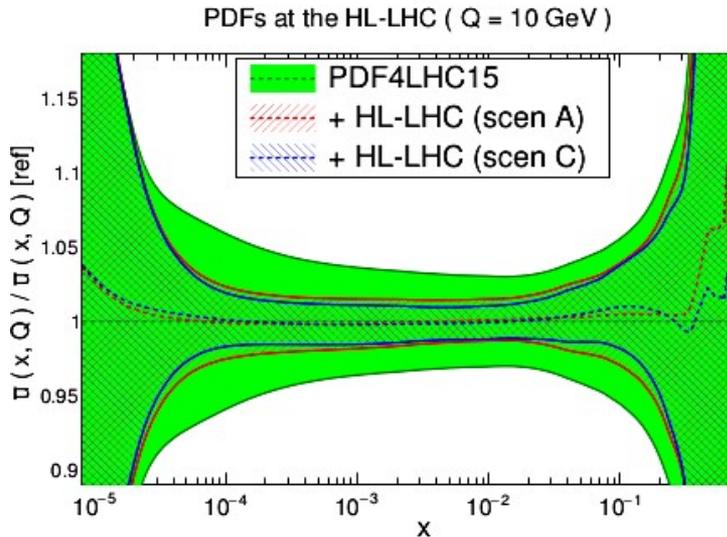
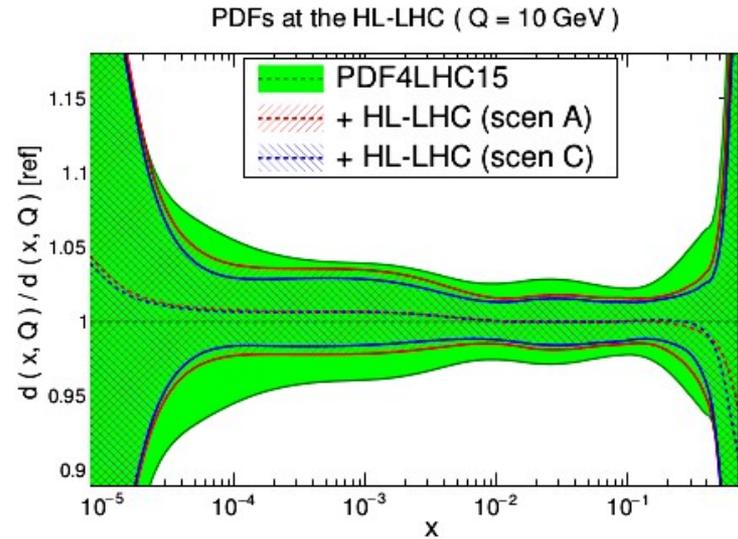
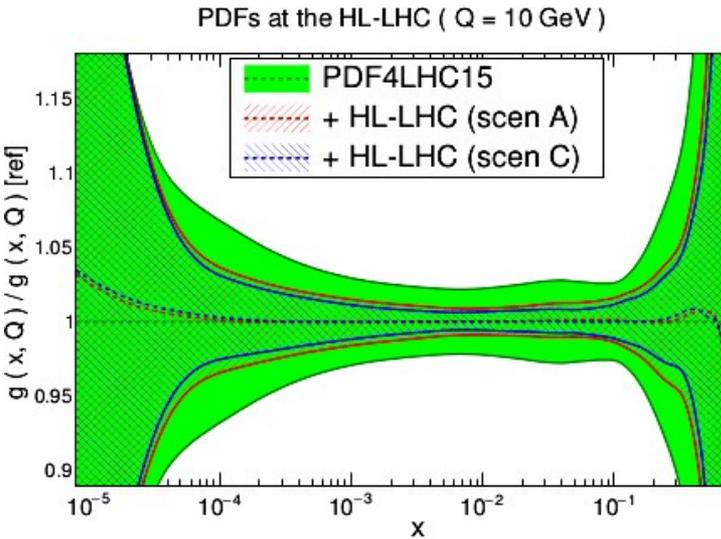
- Generation of HL-LHC pQCD pseudo-data (pp, 3 ab⁻¹):



- Significant constraining power in many phase space regions.

[R.A. Khalek et al. arXiv:1810.03639]

Improved PDFs with pp data (HL-LHC)

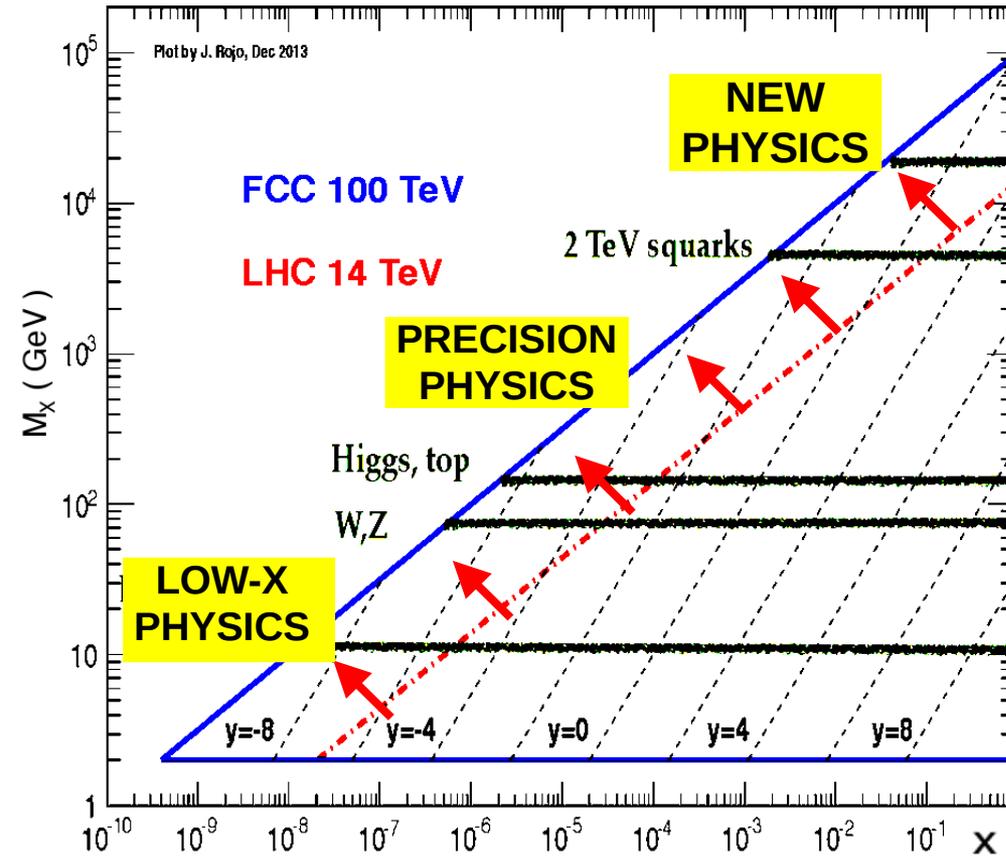


- Significant (factor ~ 2) PDF uncertainty reduction (with little dependence on projected systematics). But not at very low-, high- x ...

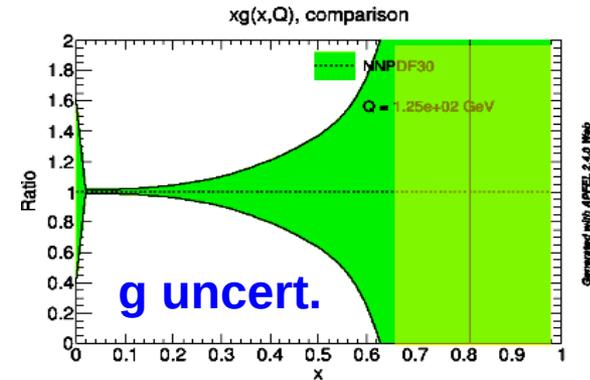
[R.A. Khalek et al. arXiv:1810.03639]

PDFs: Still work to do for FCC...

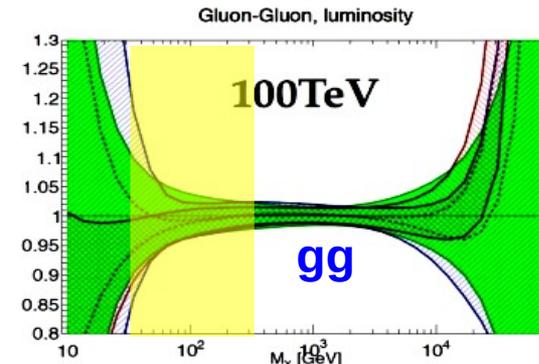
- Still large PDF uncertainties in pp at 100 TeV in key (x, Q^2) regions:



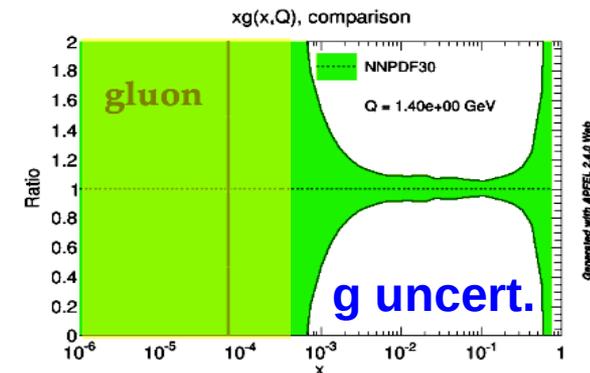
- FCC-ep required to reach $O(1\%)$ uncertainty for $\sigma(W, Z, H)$ at FCC-pp



High-x



Mid-x



Low-x

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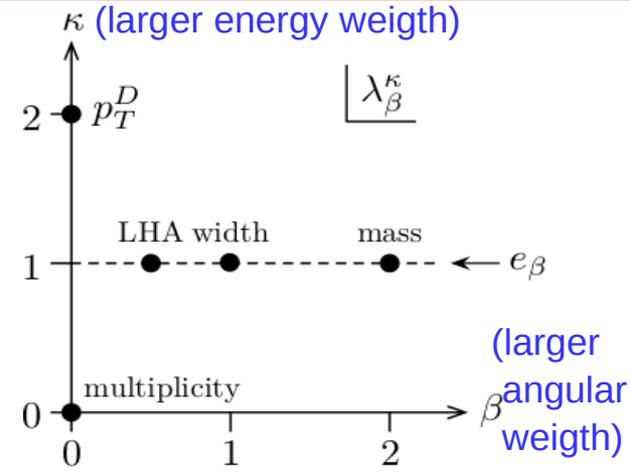
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Precise jet substruct. & flavour tagging (FCC-ee)

- State-of-the-art jet substructure studies based on **angularities** ("Sudakov"-safe) variables of **jet constituents**: multiplicity, LHA, width/broadening, mass/thrust, C-parameter,...

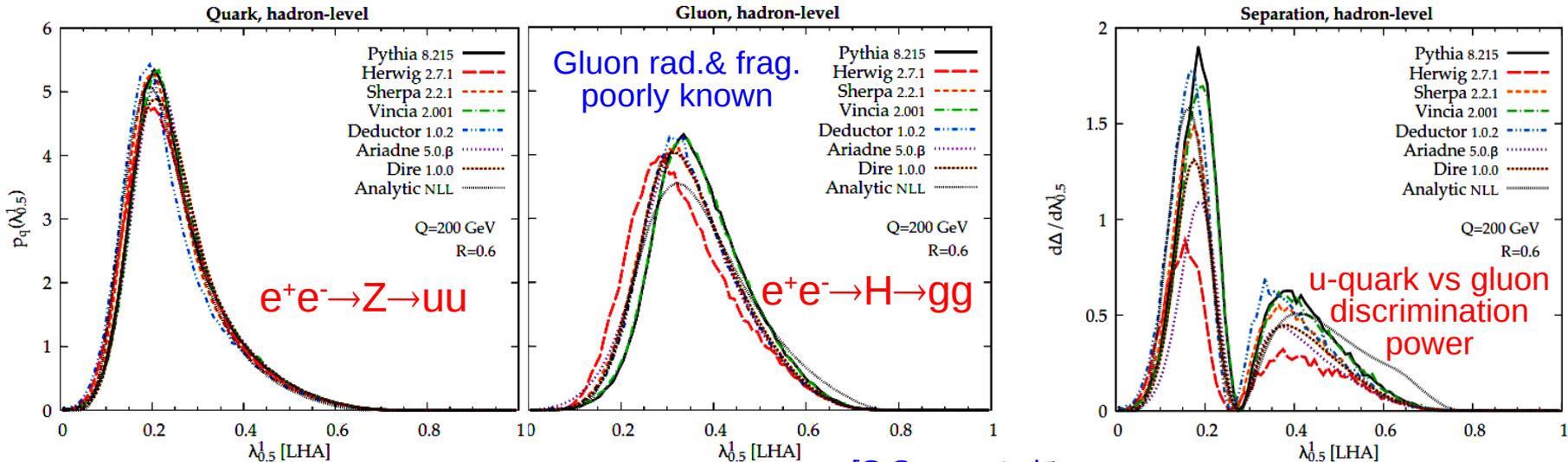
$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\beta},$$

(normalized $E^n \times \theta^n$ products)



[Larkoski, Salam, Thaler, 13]
[Larkoski, Thaler, Waalewijn, 14]

- k=1: IRC-safe** computable ($N^n\text{LO}+N^n\text{LL}$) via SCET (but uncertainties from non-pQCD effects)
- MC **parton showers differ on gluon** (less so quark) **radiation patterns**:

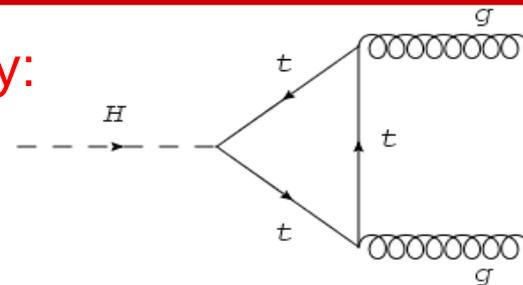


[G.Soyez et al.]

David d'Enterria (CERN)

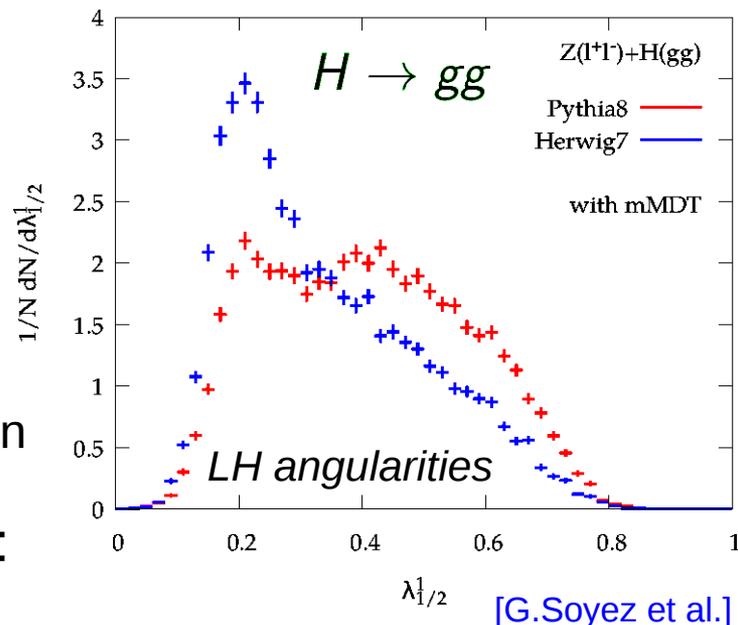
High-precision gluon & quark jet studies (FCC-ee)

- Exploit FCC-ee $H(gg)$ as a "pure gluon" factory:
 $H \rightarrow gg$ (BR~8% accurately known) provides
 $O(100.000)$ extra-clean digluon events.



- Multiple handles to study gluon radiation & g-jet properties:

- Gluon vs. quark via $H \rightarrow gg$ vs. $Z \rightarrow qq$
 (Profit from excellent g,b separation)
 - Gluon vs. quark via $Z \rightarrow bbg$ vs. $Z \rightarrow qq(g)$
 (g in one hemisphere recoiling against 2-b-jets in the other).
 - Vary E_{jet} range via ISR: $e^+e^- \rightarrow Z^*, \gamma^* \rightarrow jj(\gamma)$
 - Vary jet radius: small-R down to calo resolution

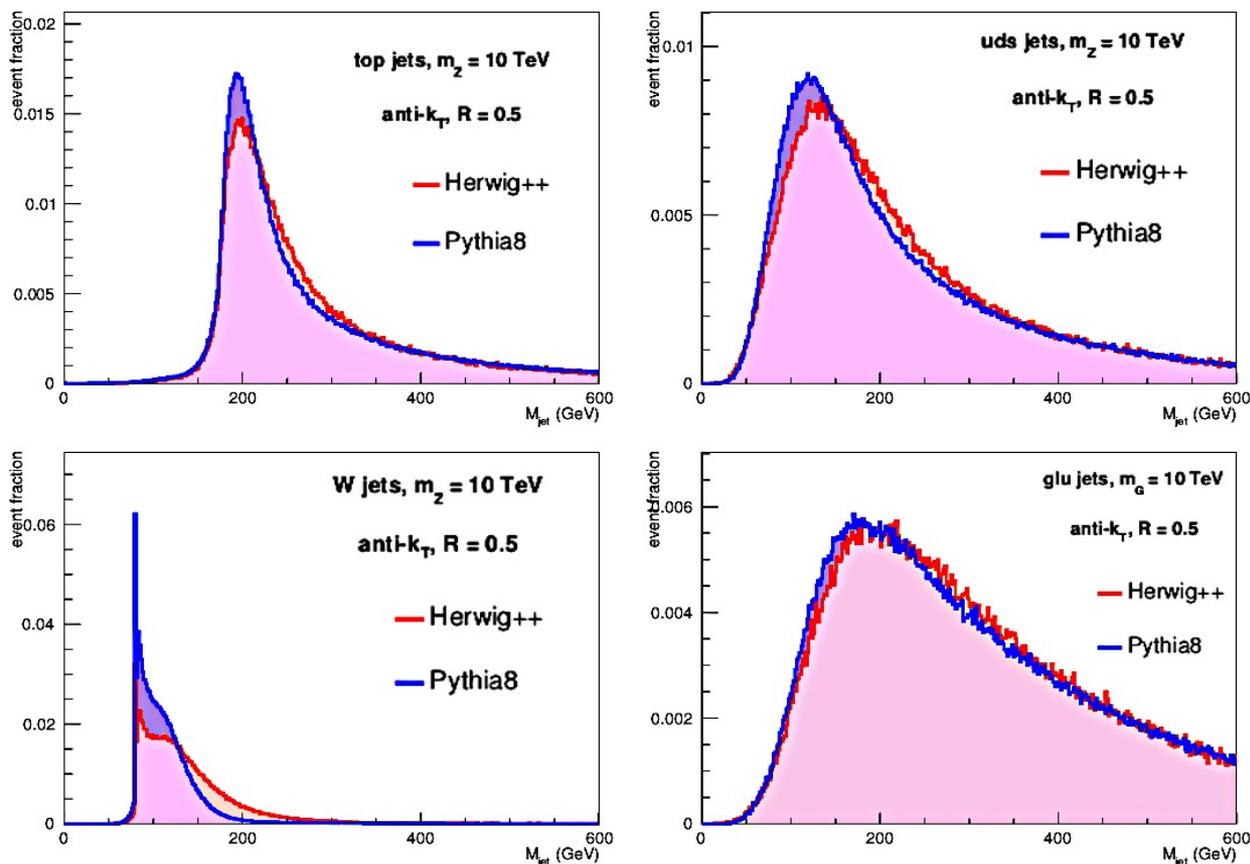


- Multiple high-precision analyses at hand:

- BSM: Improve $q/g/Q$ discrimination tools
- pQCD: Check N^{α} LO antenna functions. High-precision QCD coupling.
- non-pQCD: Gluon fragmentation: Octet neutralization? (zero-charge gluon jet with rap gaps). Colour reconnection? Glueballs? Leading η 's, baryons?

Highly-boosted partons (FCC-pp)

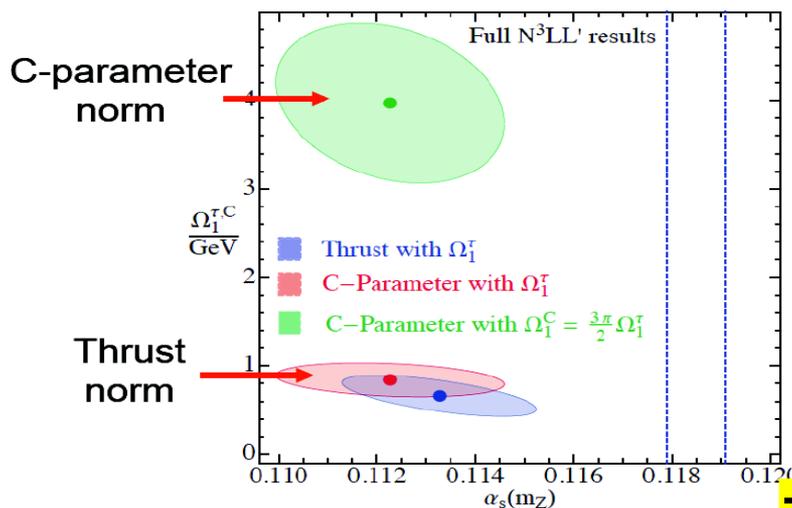
- Proton-proton collisions at 100 TeV provide **unique conditions** to produce & study **highly-boosted objects** ($\theta < E_j/m_{jj}$): boosted tops, $R_{\text{BSM}} \rightarrow jj$, high- p_T Higgs studies,...
- MC-dependent **quark vs. gluon jet (& jet radius) differences**:



α_s via e^+e^- event shapes & jet rates (FCC-ee)

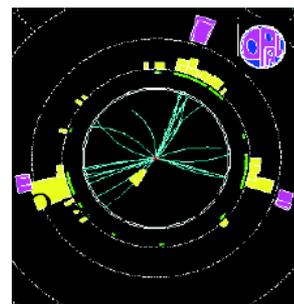
- ➔ Computed at $N^{2,3}LO+N^{(2)}LL$ accuracy.
- ➔ LEP data for thrust, C-parameter, jet shapes, 3-jet x-sections

Results sensitive to resummation & non-pQCD (hadronization) accounted for via MCs or analytically:



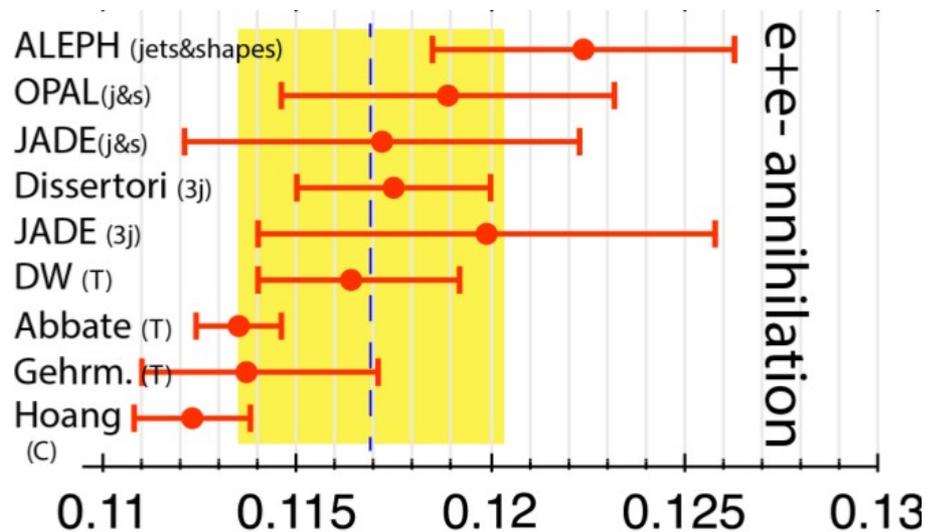
$$\tau = 1 - \max_{\hat{n}} \frac{\sum |\vec{p}_i \cdot \hat{n}|}{\sum |\vec{p}_i|}$$

$$C = \frac{3}{2} \frac{\sum_{i,j} |\vec{p}_i| |\vec{p}_j| \sin^2 \theta_{ij}}{(\sum_i |\vec{p}_i|)^2}$$



OPAL 3 jet event

[S.Kluth et al., A.Hoang et. al.]



Today: $\alpha_s(Mz) = 0.1169 \pm 0.0034$ ($\pm 2.9\%$)

➔ FCC-ee:

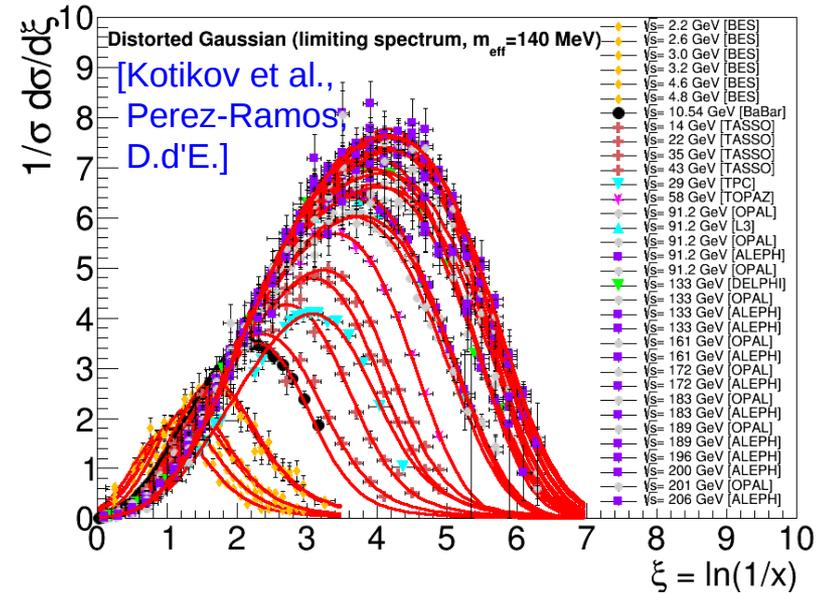
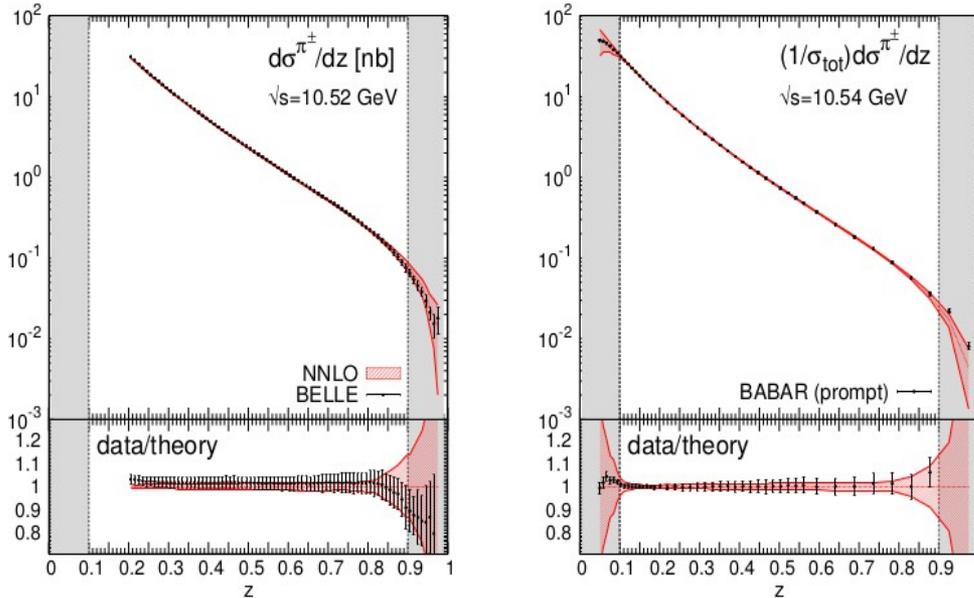
- Provides higher- \sqrt{s} data for rates & lower- \sqrt{s} for shapes: $\delta\alpha_s < 1\%$
- TH: Improved ($N^{2,3}LL$) resummation for rates & hadroniz. for shapes

High-precision parton FFs (FCC-ee)

- Parton-to-hadron **fragment. functions** evolution known at NNLO at high- z &

[D.Anderle et al., A.Vossen et al., B.Kniehl et al.,
V.Bertone et al., N.Sato et al., D.deFlorian et al.,...]

at **NNLO*+NNLL** at low- z :



Method	Current $\delta\alpha_s(m_Z^2)/\alpha_s(m_Z^2)$ uncertainty (theory & experiment state-of-the-art)	Future $\delta\alpha_s(m_Z^2)/\alpha_s(m_Z^2)$ uncertainty (theory & experiment progress)
soft FFs	$1.8\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 2\%$ (NNLO* only (+NNLL), npQCD small)	$0.7\%_{\text{th}} \oplus 0.7\%_{\text{exp}} \approx 1\%$ (~ 2 yrs), $<1\%$ (FCC-ee) (NNLO+NNLL. More precise e^+e^- data: 90–350 GeV)
hard FFs	$1\%_{\text{th}} \oplus 5\%_{\text{exp}} \approx 5\%$ (NLO only. LEP data only)	$0.7\%_{\text{th}} \oplus 2\%_{\text{exp}} \approx 2\%$ (+B-factories), $<1\%$ (FCC-ee) (NNLO. More precise e^+e^- data)

- FCC-ee (much broader z range) allows for α_s extraction with $\delta\alpha_s < 1\%$

QCD physics at future pp & e⁺e⁻ machines

(1) QCD coupling

(FCC-ee, FCC-pp, SCT)

(2) Parton Distribution Functions

(HL-LHC, HE-LHC, FCC-hh)

(3) Jet substructure & flavour tagging

(FCC-ee, FCC-pp)

(4) Non-perturbative QCD

(FCC-ee, SCT, HL-LHC)

NOTE: Only UNIQUE QCD measurements, inaccessible at any current machine, are covered.

Colour reconnection (FCC-ee)

- Colour reconnection among partons in e^+e^- = Source of **uncertainty in m_W , m_{top} , CP-violating Higgs in multijet final-states**: $e^+e^- \rightarrow WW(4j)$, $Z(4j)$, tt
- Use e^+e^- leptonic final-states to learn about CR:

At LEP 2: hot topic (by QCD standards): **'string drag' effect on W mass**

Non-zero effect convincingly demonstrated at LEP-2

No-CR excluded at 99.5% CL [Phys.Rept. 532 (2013) 119]

But not much detailed (differential) information

Thousand times more WW at FCC-ee

Sjöstrand: **turn the W mass problem around**; use huge sample of semi-leptonic events to measure m_W

→ **use as constraint to measure CR in hadronic WW**

Has become even hotter topic at LHC

It appears jet universality is under heavy attack.

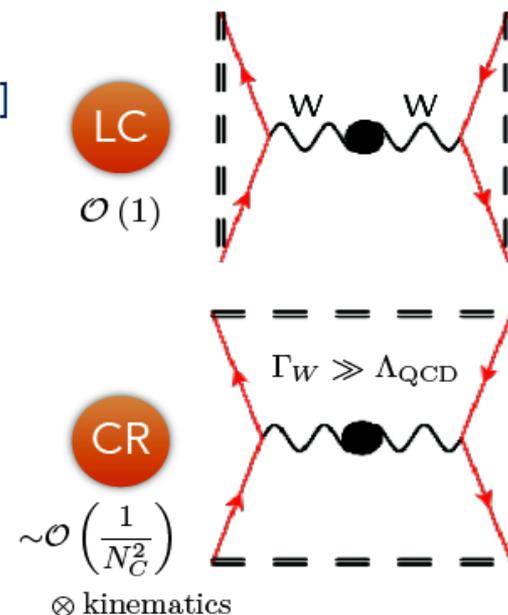
Fundamental to understanding & modeling hadronisation

Follow-up studies now underway at LHC.

T. Sjöstrand, W. Metzger, S. Kluth, C. Bierlich

High-stats ee → other side of story

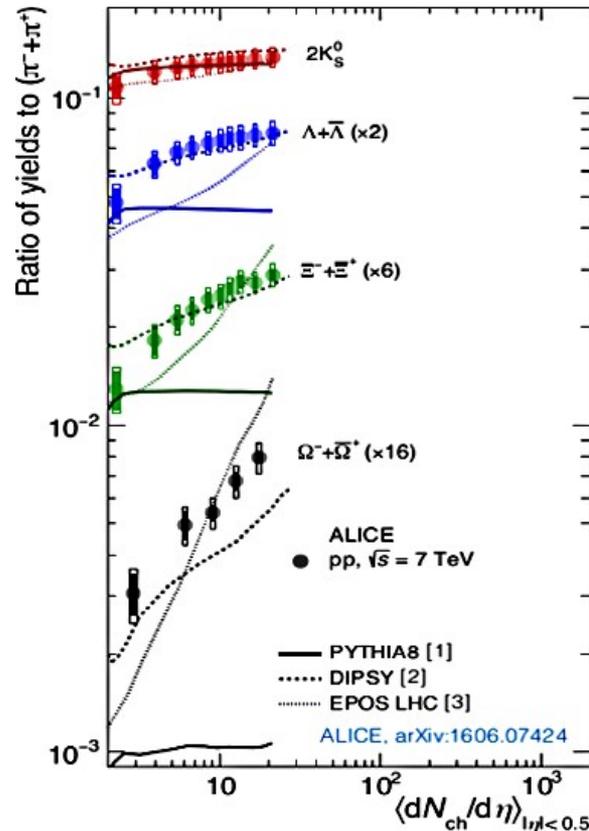
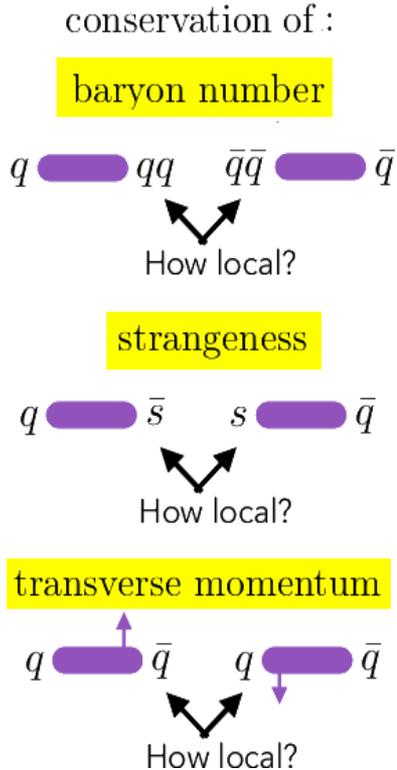
Also relevant in (hadronic) $ee \rightarrow tt$, and $Z \rightarrow 4$ jets



+ Overlaps → interactions?
increased tensions (strangeness)?
breakdown of string picture?

Other Non-pQCD (SCT, FCC-ee, HL-LHC)

- High-precision low- p_T PID hadrons in e^+e^- allow for detailed studies:
 - Baryon & strangeness production. Colour string dynamics.
 - Final-state correlations (spin: BE, FD; momenta; space)
 - Bound state formation: Onia, multiquark states, glueballs, ...



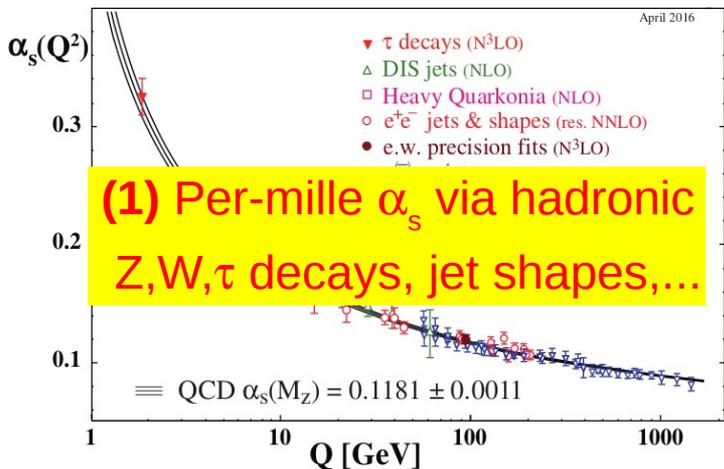
▶ Key test of universality of parton hadronization.

■ Baseline studies for high-density QCD in small and large systems.

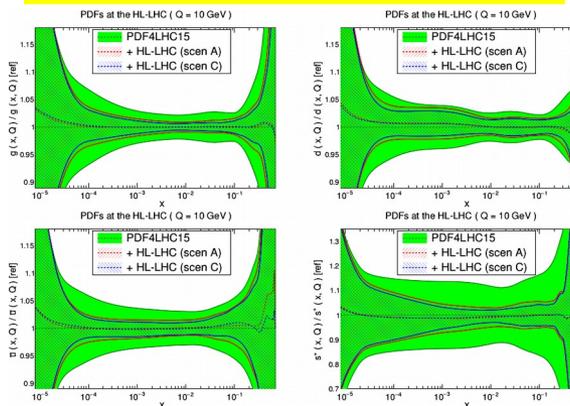
[Ultra-thin ALICE proposal beyond 2030].

Summary: QCD at future pp & e⁺e⁻ colliders

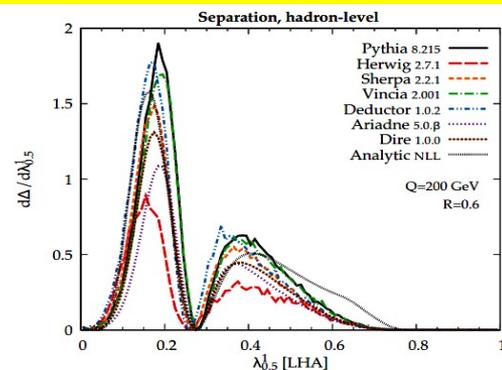
➤ The precision needed to fully exploit the future ee/pp/ep/eA/AA SM & BSM programs requires exquisite control of (n)pQCD, accessible in multiple, unique, high-stats, clean e⁺e⁻ & pp measurements:



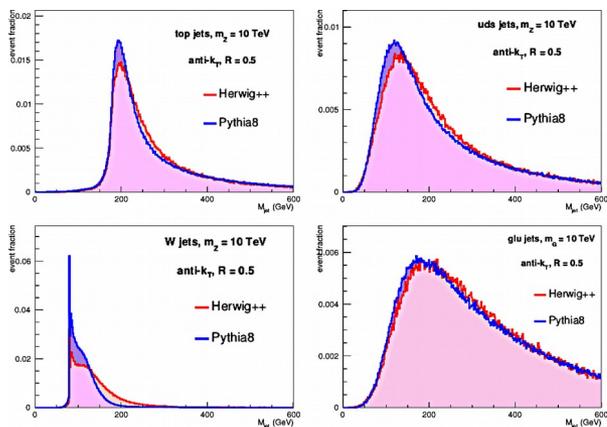
(2) High-precision PDFs



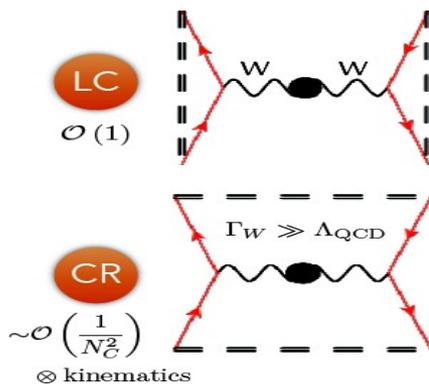
(3) NⁿLO+NⁿLL jet struct. High g/q/Q discrimination



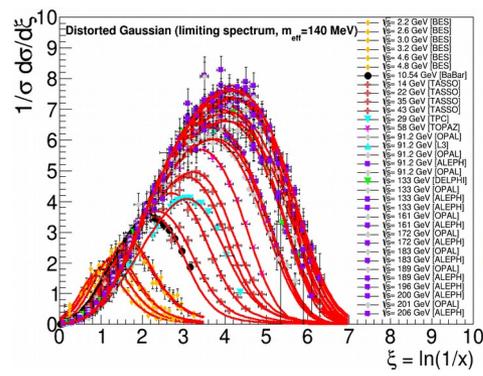
(4) Unique studies of highly-boosted dijet objects



(5) <1% control of colour reconnection



(6) High-precision hadronization:



conservation of:
baryon number



How local?

strangeness



How local?

transverse momentum

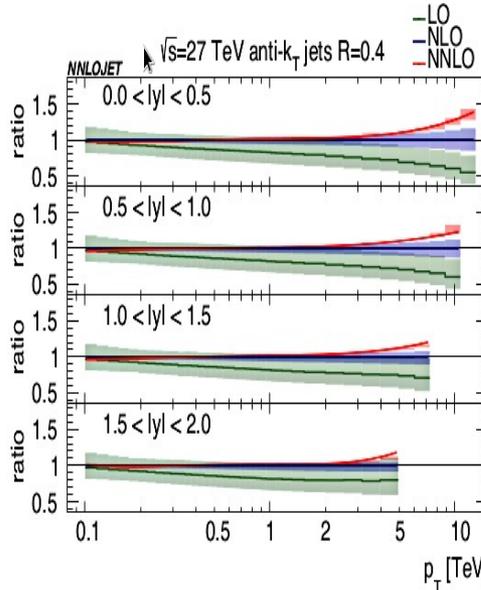
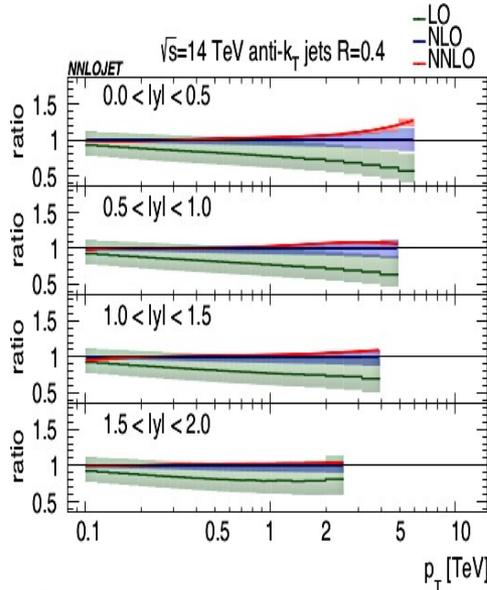
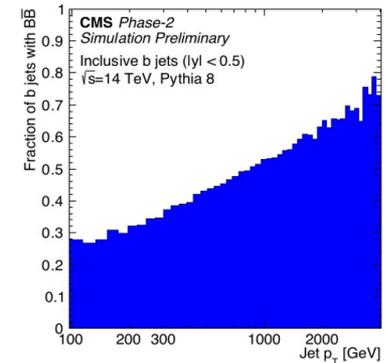
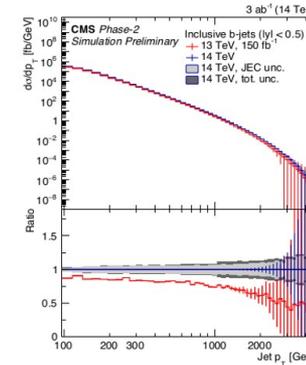
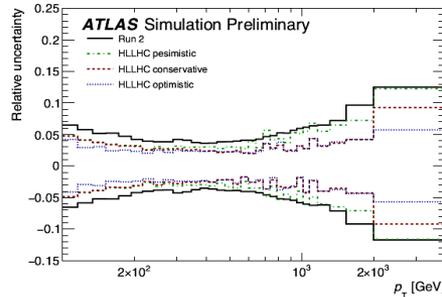
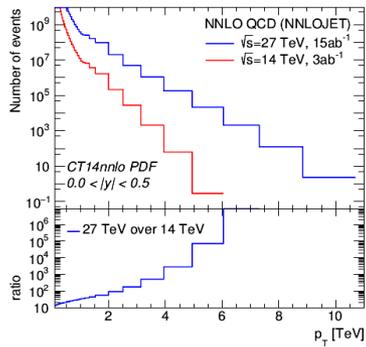


How local?

Backup slides

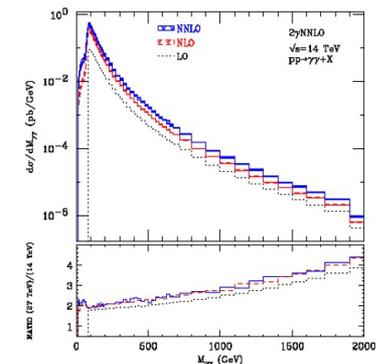
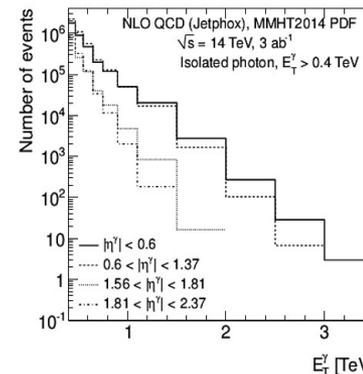
HL-LHC QCD performances: jets, γ

- ATLAS** projections for inclusive jet production at **HL** and **HE-LHC**, including detailed study of systematic uncertainties:
 - ★ Potentially significant improvement in uncertainties at both low and high jet p_{\perp} demonstrated, depending on scenario considered.
 - ★ Extensive jet p_{\perp} reach: ~ 5 (9) TeV at HL (HE) LHC.
- CMS** projections for b-jet production at **HL-LHC**:
 - ★ Increased b-jet reach: $p_{\perp} \sim 3$ TeV.
 - ★ New regime: b-quark \sim massless w.r.t. high p_{\perp} jet large fraction of jets with $B + \bar{B}$ due to PS ($g \rightarrow b\bar{b}$): important to disentangle from b-quarks produced in hard subprocess.



- Isolated photon**: **CMS** projections show extensive reach, $E_{\perp}^{\gamma} \sim 3(5)$ TeV for the HL(HE)-LHC. Increase by $\sim 2-3$ w.r.t. existing data.

- Diphoton** production: predictions with cutting-edge **NNLO** theory. Significant increase in reach with HE-LHC again shown.

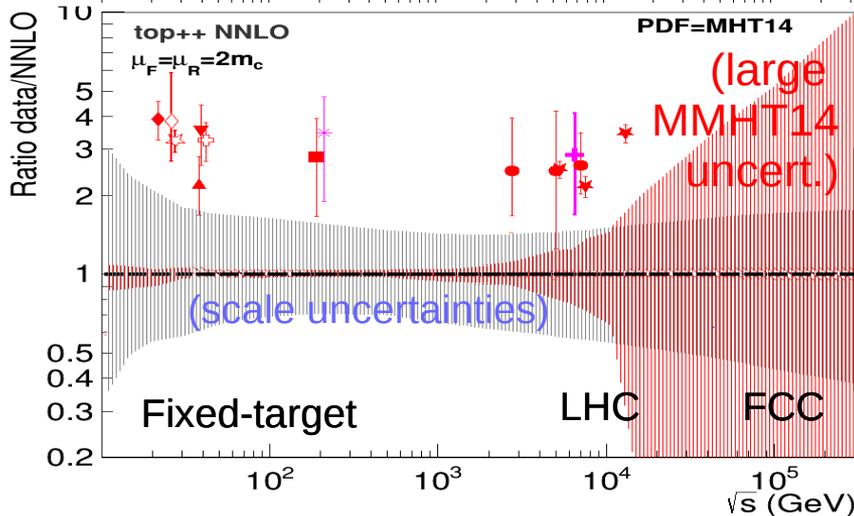
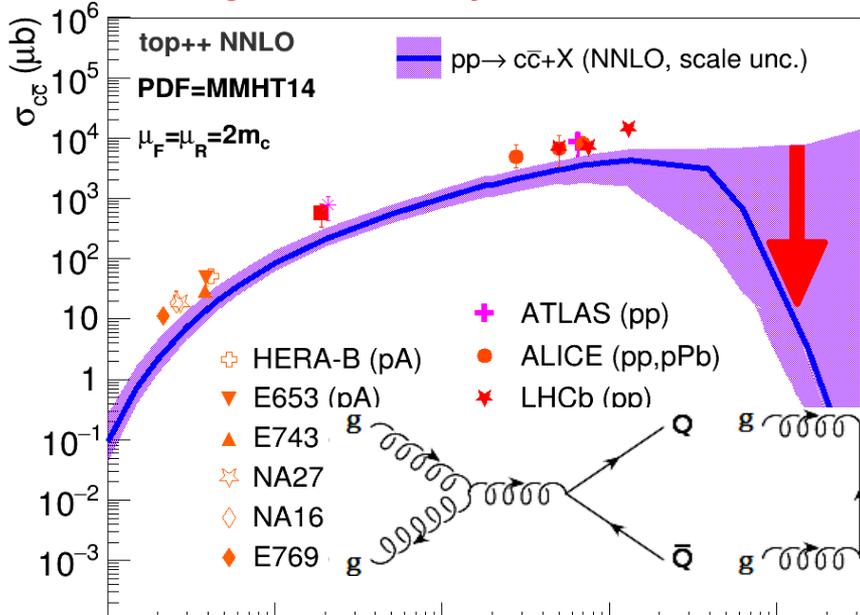


QCD physics at future pp & e⁺e⁻ machines

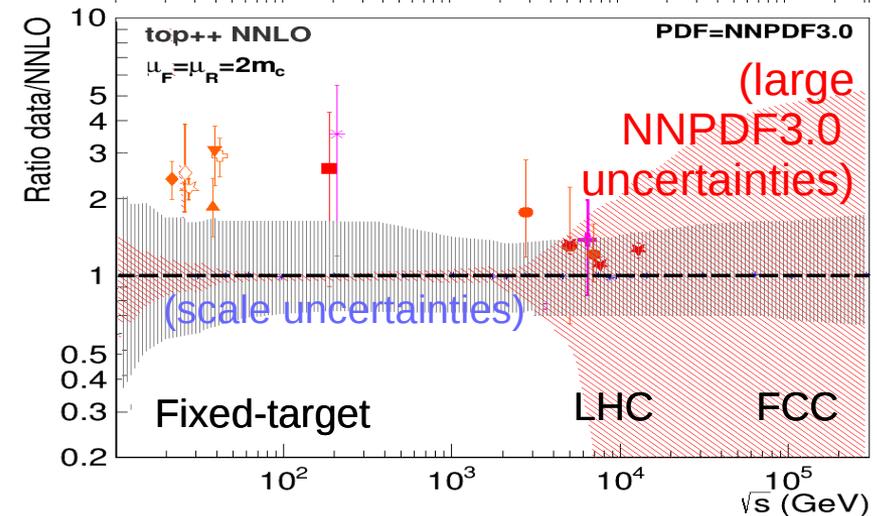
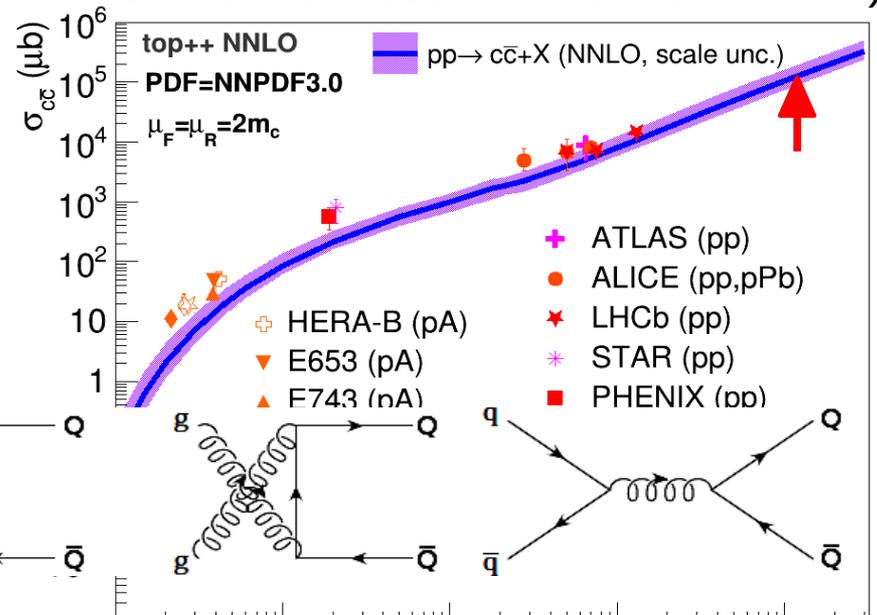
1. **High-precision α_s (parametric uncertainty on BSM via “SM stress tests”):**
 - Via $\sigma(\text{ttbar}), \sigma(W,Z)$ in p-p at HL-LHC, HE-LHC, FCC-hh
 - Via $\text{BR}_{\text{had}}(\tau, W, Z)$ and jets shapes/rates/FFs in e⁺e⁻ at FCC-ee (via tau at SCT)
2. **High-precision PDFs (impact on precision SM & high-x BSM searches):**
 - Via $d\sigma(W, Z, \text{jets}, \text{ttbar}, \gamma)$ in p-p at HL-LHC, HE-LHC, FCC-hh
3. **Heavy-Q/quark/gluon separation, jet substructure:**
 - Via jet observables in p-p at HL-LHC, HE-LHC, FCC-hh (**boosted** topologies)
 - Via jet observables in e⁺e⁻ at FCC-ee
4. **Soft gluon resummations (improvements of MC parton showers):**
 - Via $d\sigma/dp_T(\text{ttbar}, Z, W, H)$ in p-p at HL-LHC, HE-LHC, FCC-hh
 - Via various jet observables in e⁺e⁻ at FCC-ee
5. **Semi-hard QCD (low-x gluon saturation, multiple hard parton interactions, ...):**
 - Via various observables in p-p at HL-LHC, HE-LHC, FCC-hh
6. **Non-perturbative QCD (hadronization, onia bound states, colour reconnection):**
 - Via multiple observables in p-p at HL-LHC, HE-LHC, FCC-hh
 - Via jet FFs, CR via e⁺e⁻ → WW → 4j at FCC-ee

$\sigma(c\bar{c})$: Data vs. NNLO (MMHT14, NNPDF3.0)

■ Charm: Data $\times 2.5$ theory (negative gluon at very low x , $\sqrt{s} > 30$ TeV)



■ Charm: Data $\times 2$ theory (agreement within uncert. but "kink" at $\sqrt{s} > 10$ TeV)



CERN FCC-ee project

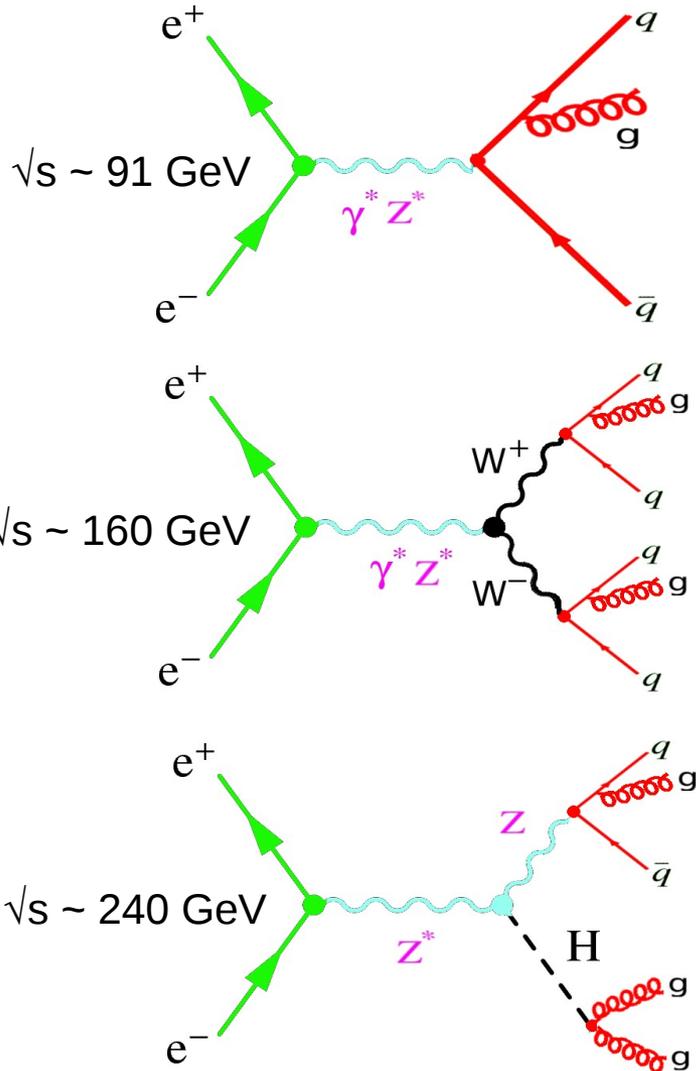
- e^+e^- option (before pp) at $\sqrt{s} = 90, (125), 160, 240, 350$ GeV



\sqrt{s} (GeV):	90 (Z)	125 (eeH)	160 (WW)	240 (HZ)	350 ($t\bar{t}$)	350 (WW \rightarrow H)
σ	43 nb	290 ab	4 pb	200 fb	0.5 pb	25 fb
\mathcal{L}/IP ($\text{cm}^{-2} \text{s}^{-1}$)	10^{36}	$5 \cdot 10^{35}$	10^{35}	$7 \cdot 10^{34}$	$1.5 \cdot 10^{34}$	$1.5 \cdot 10^{34}$
\mathcal{L}_{int} (ab^{-1}/yr , 2 IPs)	50	10	8	1.8	0.5	0.35
Events/year (2 IPs)	10^{12}	$3 \cdot 10^3$	$3 \cdot 10^7$	$3 \cdot 10^5$	$2.5 \cdot 10^5$	10^4
Years needed (2 IPs)	4	1.5	1	3	0.5	4
# of light- q jets/year:	$\mathcal{O}(10^{12})$	–	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	–	–
# of gluon-jets/year:	$\mathcal{O}(10^{11})$	$\mathcal{O}(10^2)$	$\mathcal{O}(10^6)$	$\mathcal{O}(10^4)$	–	$\mathcal{O}(10^3)$
# of heavy- Q jets/yr:	$\mathcal{O}(10^{12})$	$\mathcal{O}(10^3)$	$\mathcal{O}(10^7)$	$\mathcal{O}(10^5)$	$\mathcal{O}(10^5)$	$\mathcal{O}(10^4)$

QCD in e^+e^- collisions

- e^+e^- collisions provide an **extremely clean** environment with fully-controlled initial-state to very precisely probe q,g dynamics:

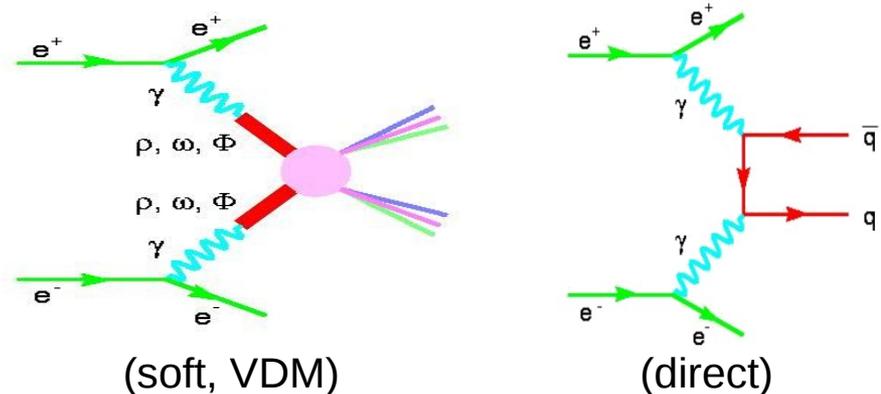


Advantages compared to p-p collisions:

- QED initial-state with **known kinematics**
- **Controlled QCD radiation** (only in final-state)
- Well-defined **heavy-Q, quark, gluon jets**
- **Smaller non-pQCD** uncertainties:
no PDFs, no QCD “underlying event”,...

Direct clean parton fragmentation & hadroniz.

- Plus **QCD physics** in $\gamma\gamma$ (EPA) collisions:



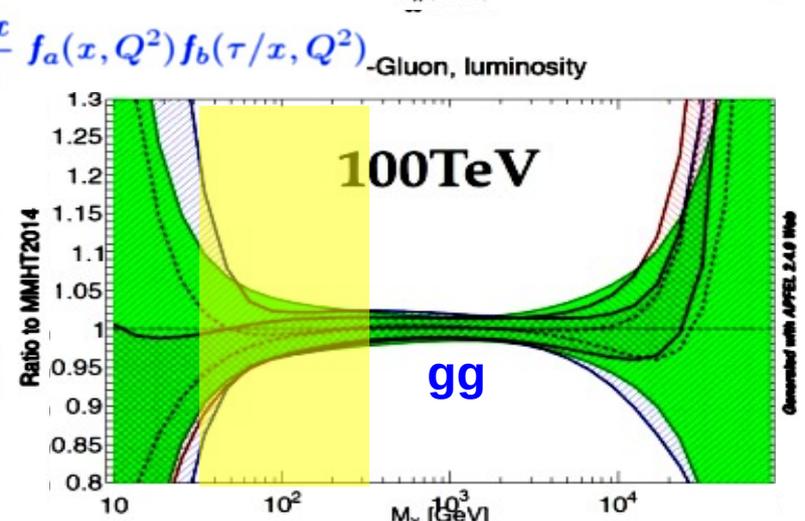
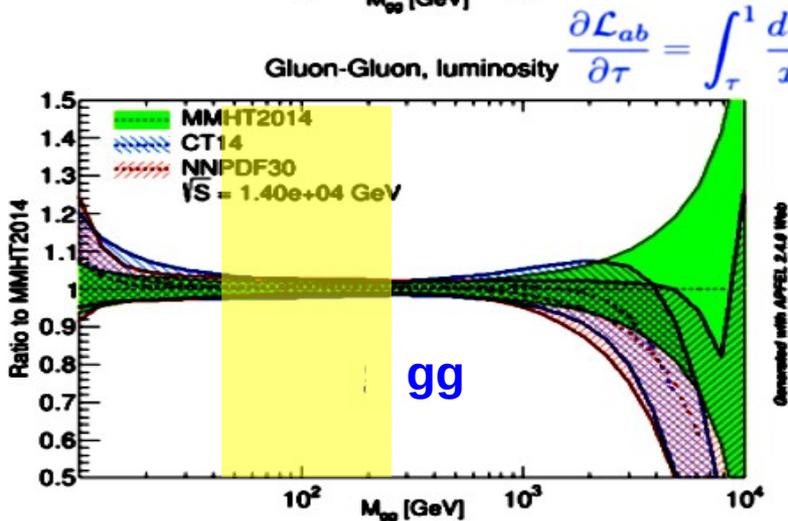
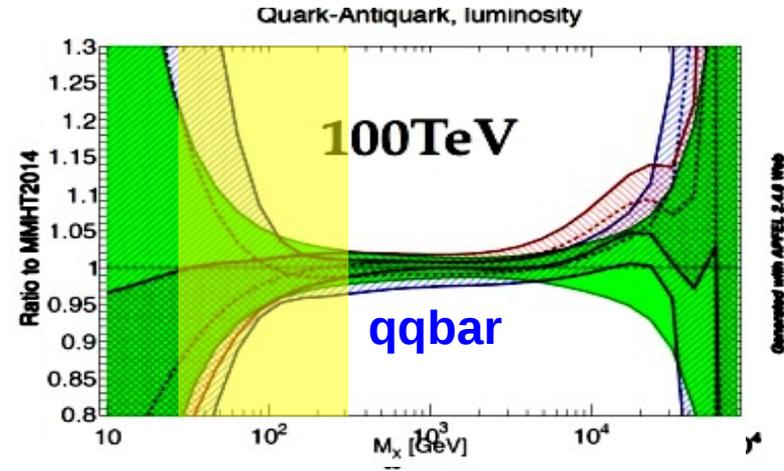
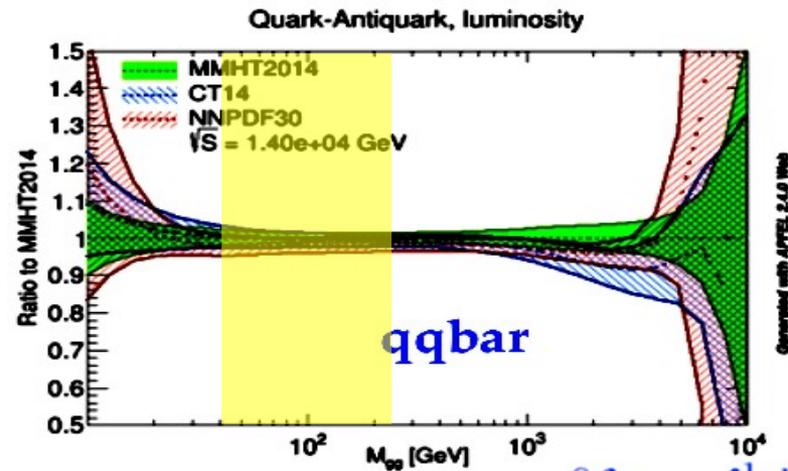
Parton luminosities at FCC “precision” region

- “Precision” region at FCC-pp: 5–7% PDF uncertainty for $\sigma(W,Z,H)$

14 TeV



100 TeV



$$\frac{\partial \mathcal{L}_{ab}}{\partial \tau} = \int_{\tau}^1 \frac{dx}{x} f_a(x, Q^2) f_b(\tau/x, Q^2)$$

QCD physics at future pp & e⁺e⁻ machines

- (1) QCD coupling** (FCC-ee, FCC-pp, SCT)
- (2) PDFs** (HL-LHC, HE-LHC, FCC-hh)
- (3) Jet substructure & flavour tagging**
(FCC-ee, FCC-pp)
- (4) Beyond DGLAP** (FCC-pp, FCC-hh)
- (5) Non-perturbative QCD** (FCC-ee, FCC-hh)

NOTE: Only UNIQUE QCD measurements, not accessible at any current machine, are covered.

α_s from γ QCD structure function

➔ Computed at NNLO: $\int_0^1 dx F_2^\gamma(x, Q^2, P^2) = \frac{\alpha}{4\pi} \frac{1}{2\beta_0} \left\{ \frac{4\pi}{\alpha_s(Q^2)} c_{LO} + c_{NLO} + \frac{\alpha_s(Q^2)}{4\pi} c_{NNLO} + \mathcal{O}(\alpha_s^2) \right\}$

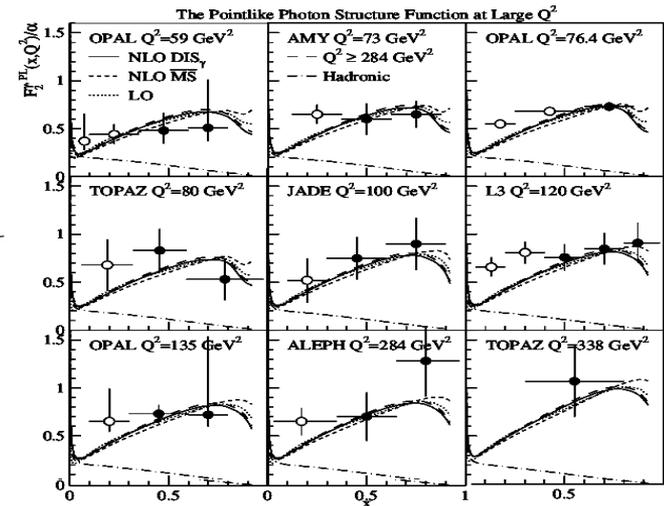
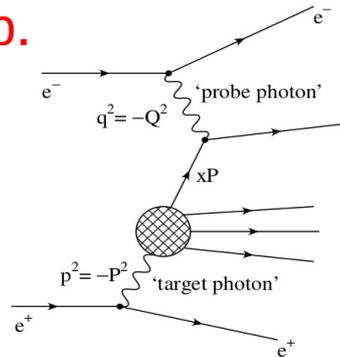
➔ Poor $F_2^\gamma(x, Q^2)$ experimental measurements:

➔ Extraction (NLO) with large exp. uncertainties today:

$$\alpha_s(M_Z) = 0.1198 \pm 0.0054$$

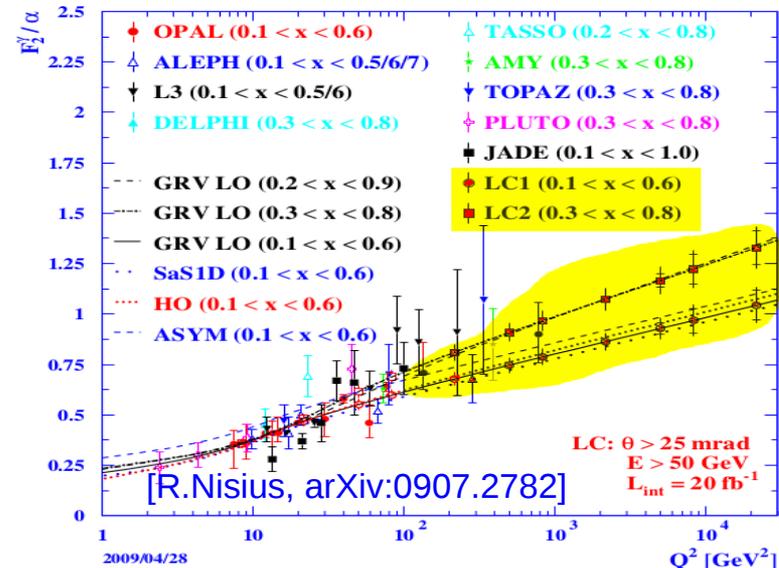
(±4.5%)

[M.Klasen et al. PRL89 (2002)122004]



➔ Future prospects:

- Better data badly needed.
- Belle-II ?
- Dedicated studies at ILC exist:
- Huge $\gamma\gamma$ (EPA) stats at FCC-ee will lead to: $\delta\alpha_s < 1\%$



Reduced QCD uncertainties on EWK observables

- With $\times 10^5$ more Z's than LEP, EWK uncertainties at FCC-ee will be dominated by syst. (QCD).

Example: $e^+e^- \rightarrow b\bar{b}$ forward-backward asymmetry

- 8 measurements at LEP:
 - 4 lepton-based, 4 jet-charge-based
- Exp. observable with **largest discrepancy today wrt. the SM: 2.8σ**

- Exp. Uncertainties: $\sim 1.6\%$

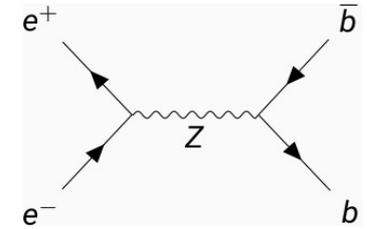
- **Statistical: $\pm 1.5\%$ ($\sim 0.05\%$ at FCC-ee)**
- **Systematics: $\pm 0.6\%$ (QCD-related: $\pm 0.4\%$)**

- QCD effects on $A_{FB}^{0,b}$ (depending strongly on exp. selection procedure):

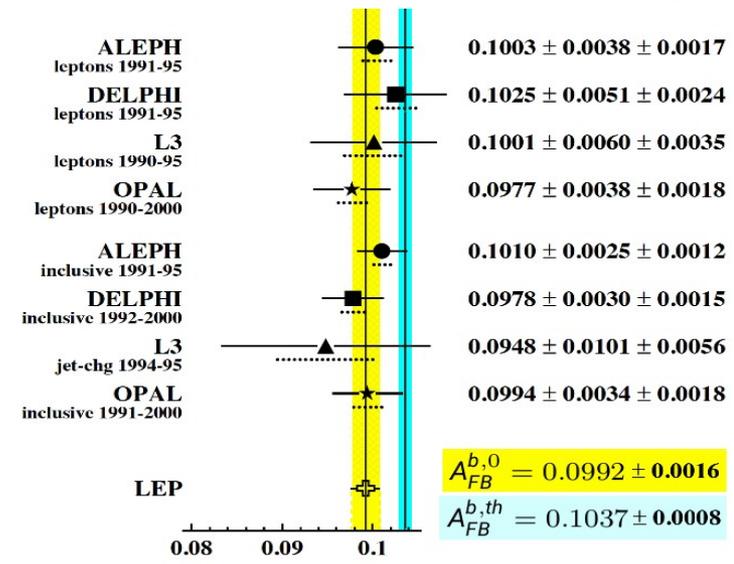
- **Gluon splitting** (TH control: α_s^2 corrections)
- Smearing of **b-jet/thrust axis**
- **b and c radiation & fragmentation**. B and D decay models.

[Uncertainties estimated by Abbaneo et al., EPJC 4 (1998)]

- We have **revisited** the impact of QCD effects on $A_{FB}^{0,b}$ implementing original analyses in up-to-date retuned parton-shower+hadronization MCs

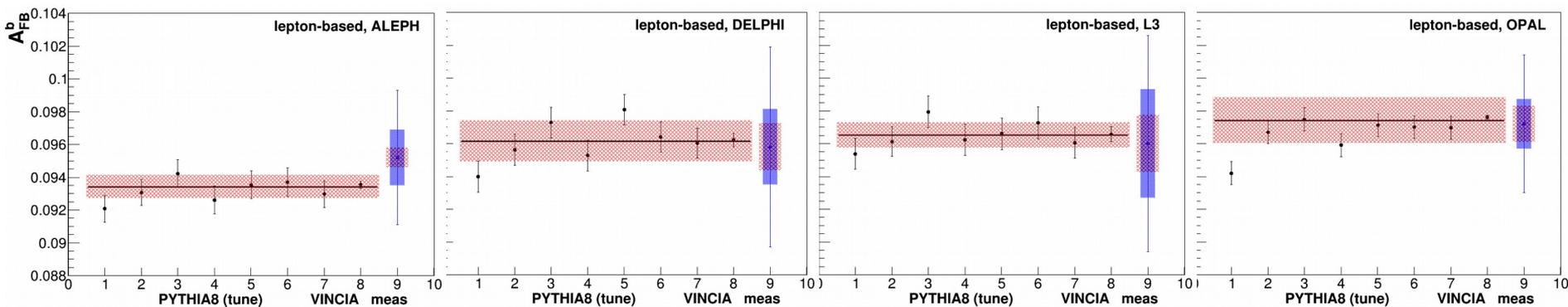


$$A_{FB}^{b} = \frac{N_F - N_B}{N_F + N_B} \quad A_{FB} = \frac{\sigma_A}{\sigma_S} \propto \frac{-g_{\mu\nu} T^{\mu\nu}}{i\epsilon_{\mu\nu\lambda\rho} \frac{n^\lambda Q^\rho}{n \cdot Q} T^{\mu\nu}}$$

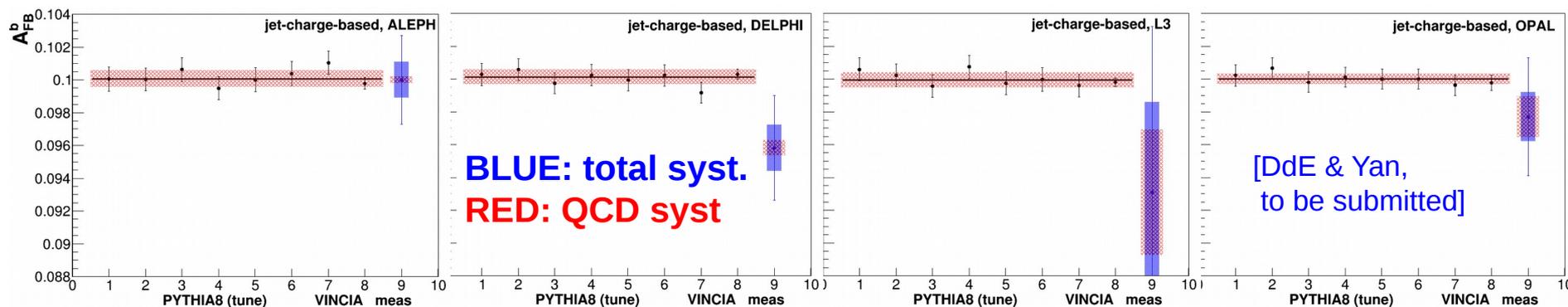


Reduced QCD uncertainties on A_{FB}^b at Z pole

- QCD uncertainties recomputed from **PYTHIA8.226 (7 tunes) & VINCIA2.2**
- $e^+e^- \rightarrow bb$ forward–backward asymmetry for **lepton-based analyses**:



- $e^+e^- \rightarrow bb$ forward–backward asymmetry for **jet-charge-based analyses**:



- 2018 vs. 1998 **PS+hadronization uncertainties**:

- Lepton-based: Consistent for ALEPH/DELPHI, **smaller for L3, larger for OPAL.**
- Jet-charge-based: Consistent for DELPHI, **smaller for ALEPH/L3/OPAL.**

- LEP average to be recomputed (likely no change as stat.unc. dominates)