


A relation between **track length**
and **deposited energy** in
homogeneous calorimeter by
GEANT4 simulation at high energy

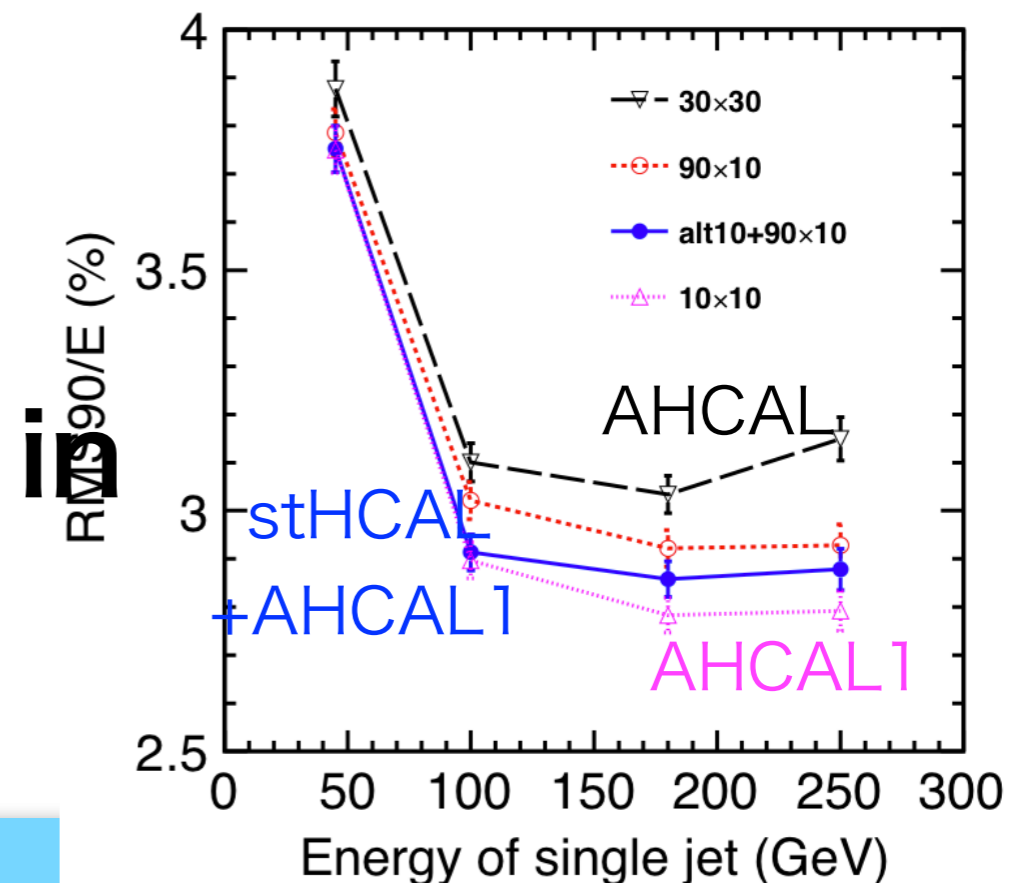
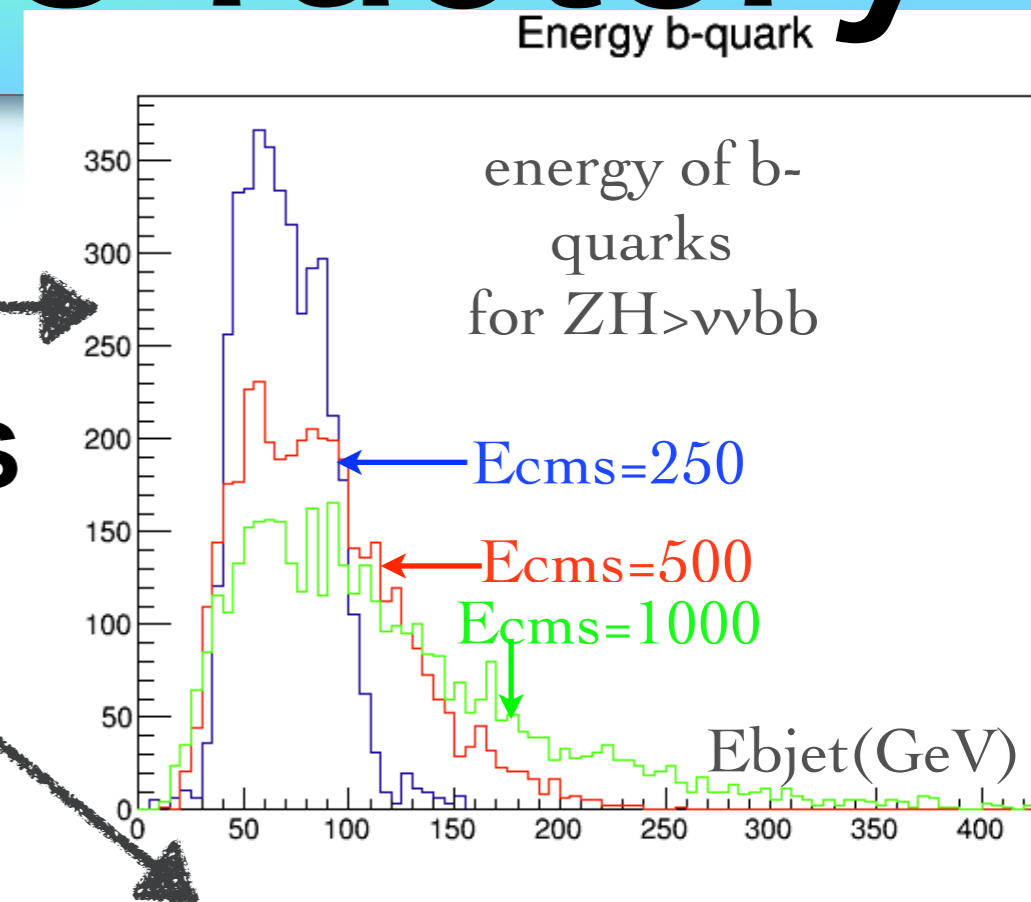


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bbjes from Higgs factory

- $E_{bjet} \sim 50-100 \text{ GeV}$ at HF
- Energy Resolution of Jets (JER) PFA is degraded
- due to HCAL E-resolution intrinsic
- PFA does work well at higher energies
- to improve Jet EReso. 50-100 GeV region

$E_{particle} < 10 \text{ GeV}$



bbjes from Higgs factory

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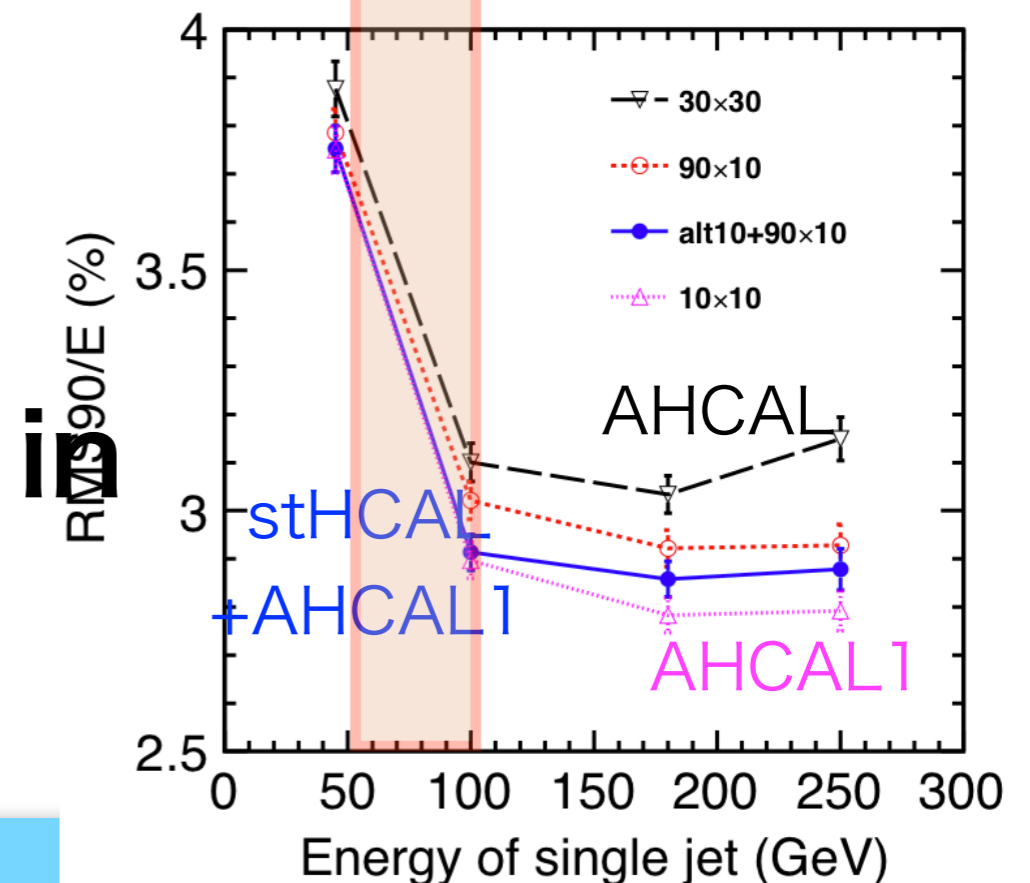
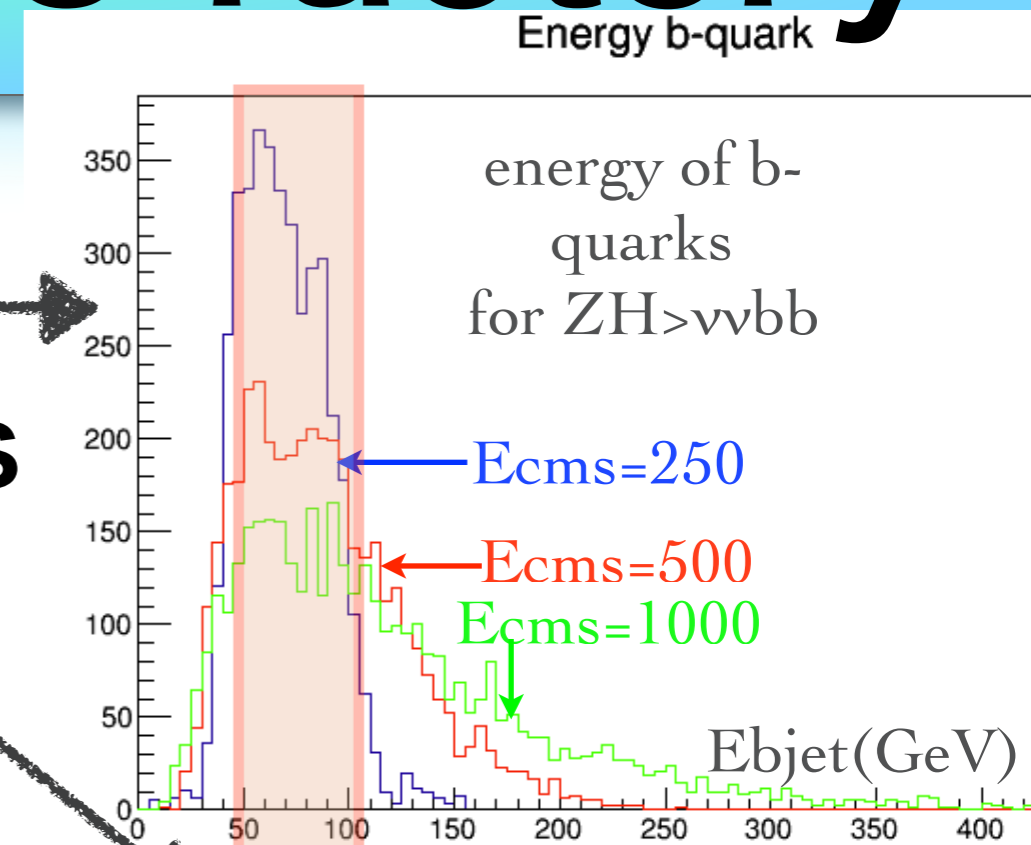
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Particle Flow Algorithm

- PFA requires 3D calorimeter

- with fine segmented cells

- to separate each particle

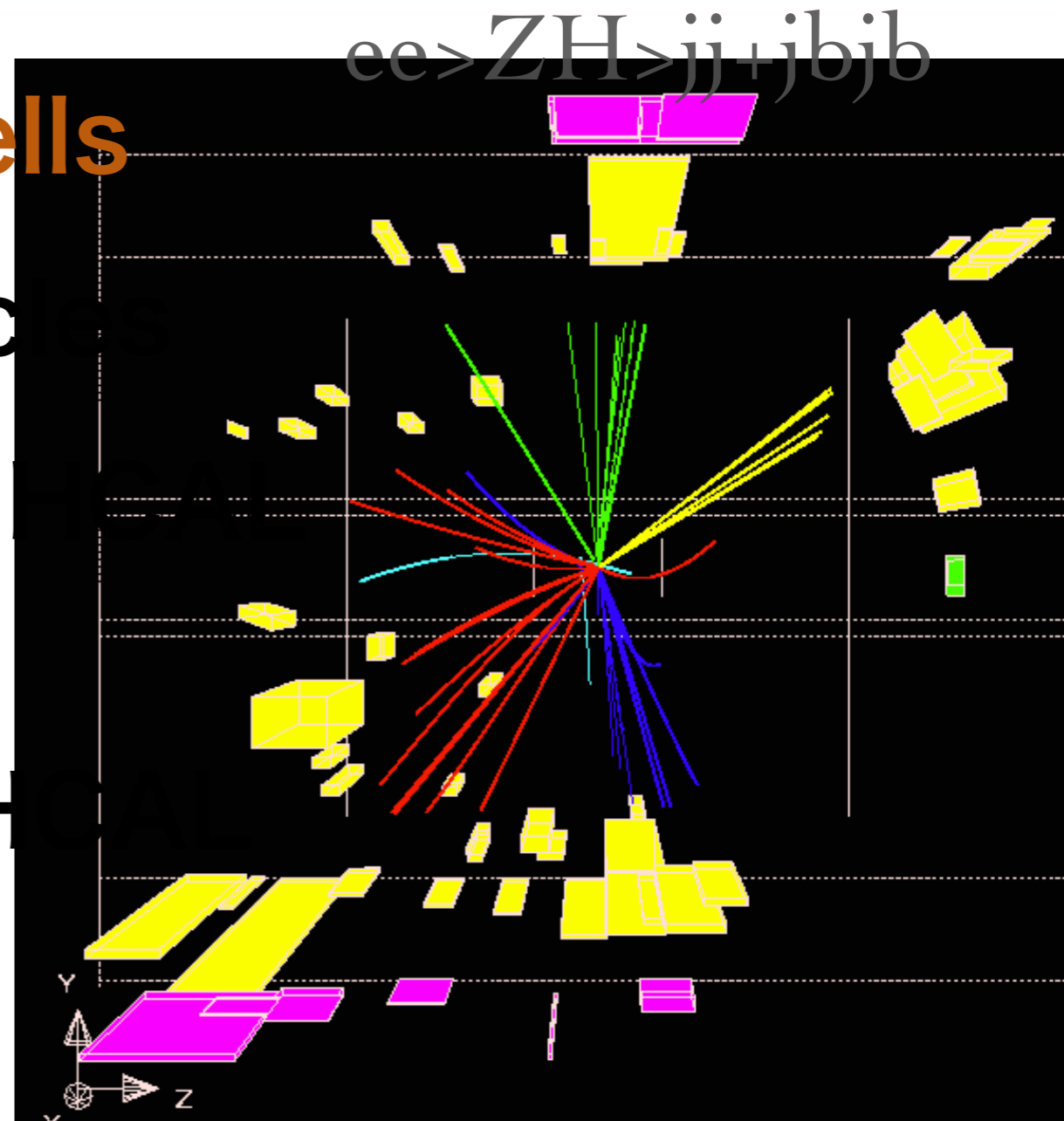
- JetER is dominated by R at lower energies

- intrinsic resolution of H

- measure total hadrons

best case

- hoping fine segmentation



ILD at 250GeV

Particle Flow Algorithm

- PFA requires 3D calorimeter

- **with fine segmented cells**

- to separate each particles

- JetER is dominated by HCAL
R at lower energies

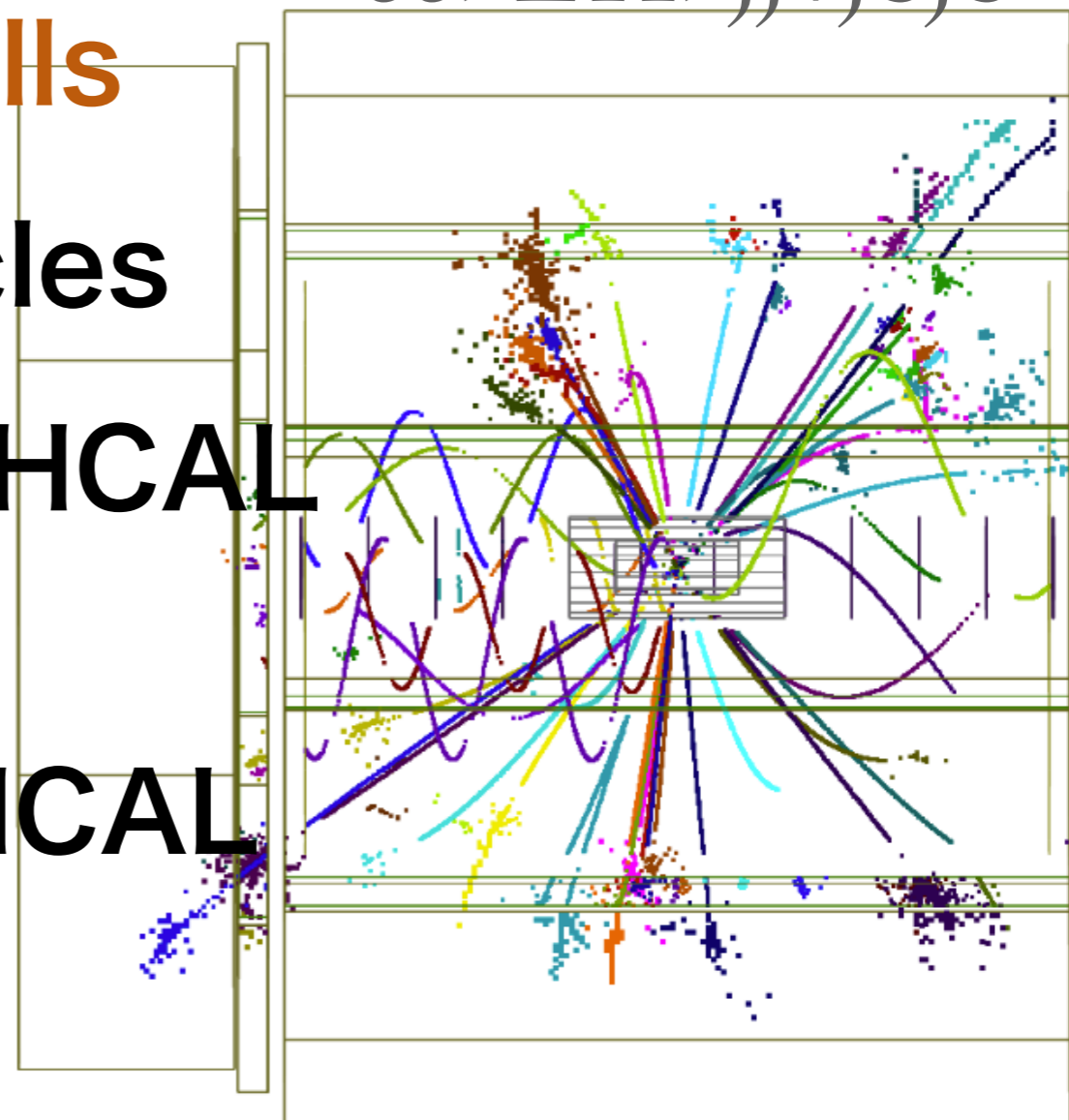
- intrinsic resolution of HCAL

- **measure total hadrons**

best case

- hoping fine segmentation

$ee \rightarrow ZH \rightarrow jj + jbjb$



ILD at 250GeV

total measurements

- GEANT4 simulation $2\text{m} \times 2\text{m} \times 2\text{m}$
 - Hadron model = FTFP-BERT
 - time cut < 100ns
- homogeneous CAL. for exam: absorber : PbWO_4
 $\lambda_1=16, X_0=225$
- two measures from the calorimeter

• TL : Track length \propto Cherenkov

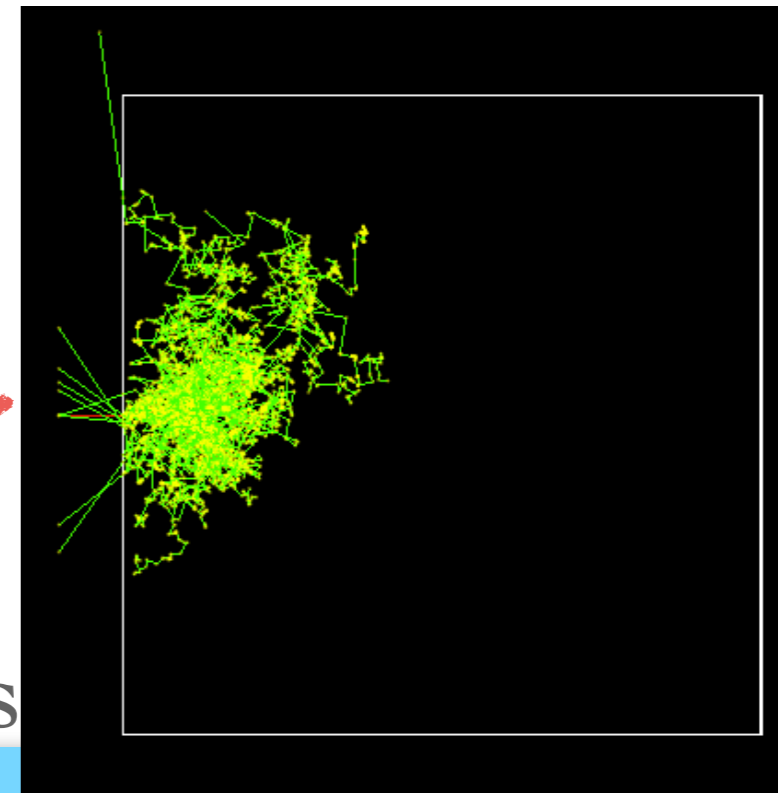
PbWO_4

• ED : $dE/dx \propto$ scintillation

• how much ER at best ?

no photon statistics

3 GeV π^-
green lines
are neutrons



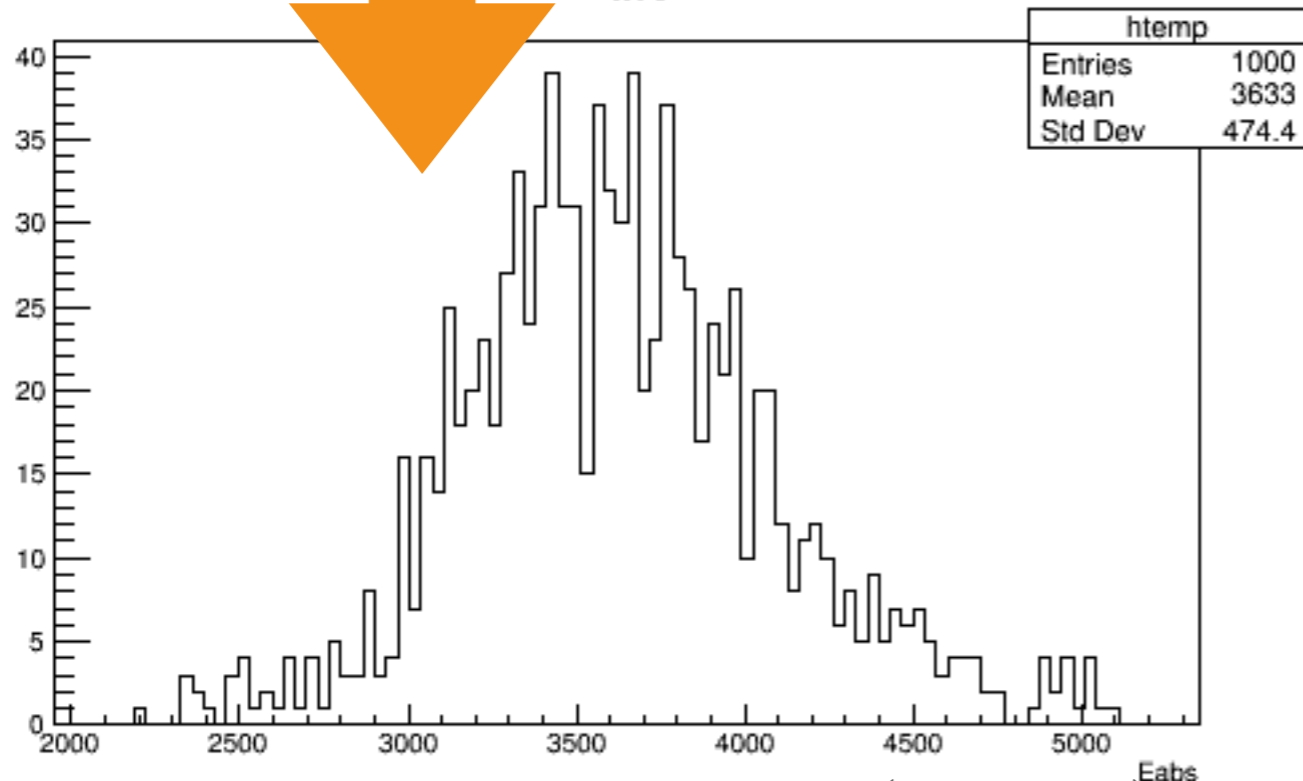
ED and TL

for 5 GeV pi-

energy sum



Eabs



ED (MeV)

resolution~13% @ 5GeV

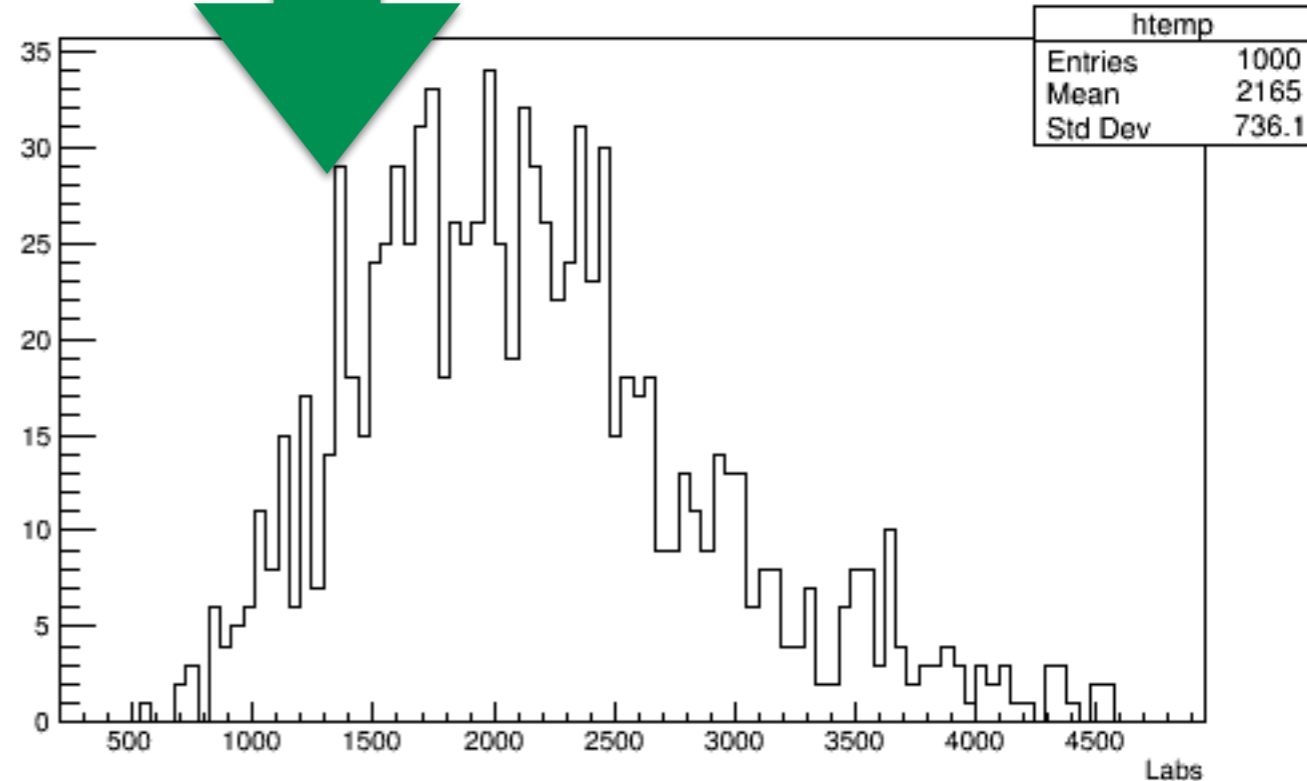
ED=sum of energy deposit

~ sum of scintillation lights in PbWO4

Cherenkov sum



Labs



TL (mm)

resolution~30% @ 5GeV

TL= sum of track length

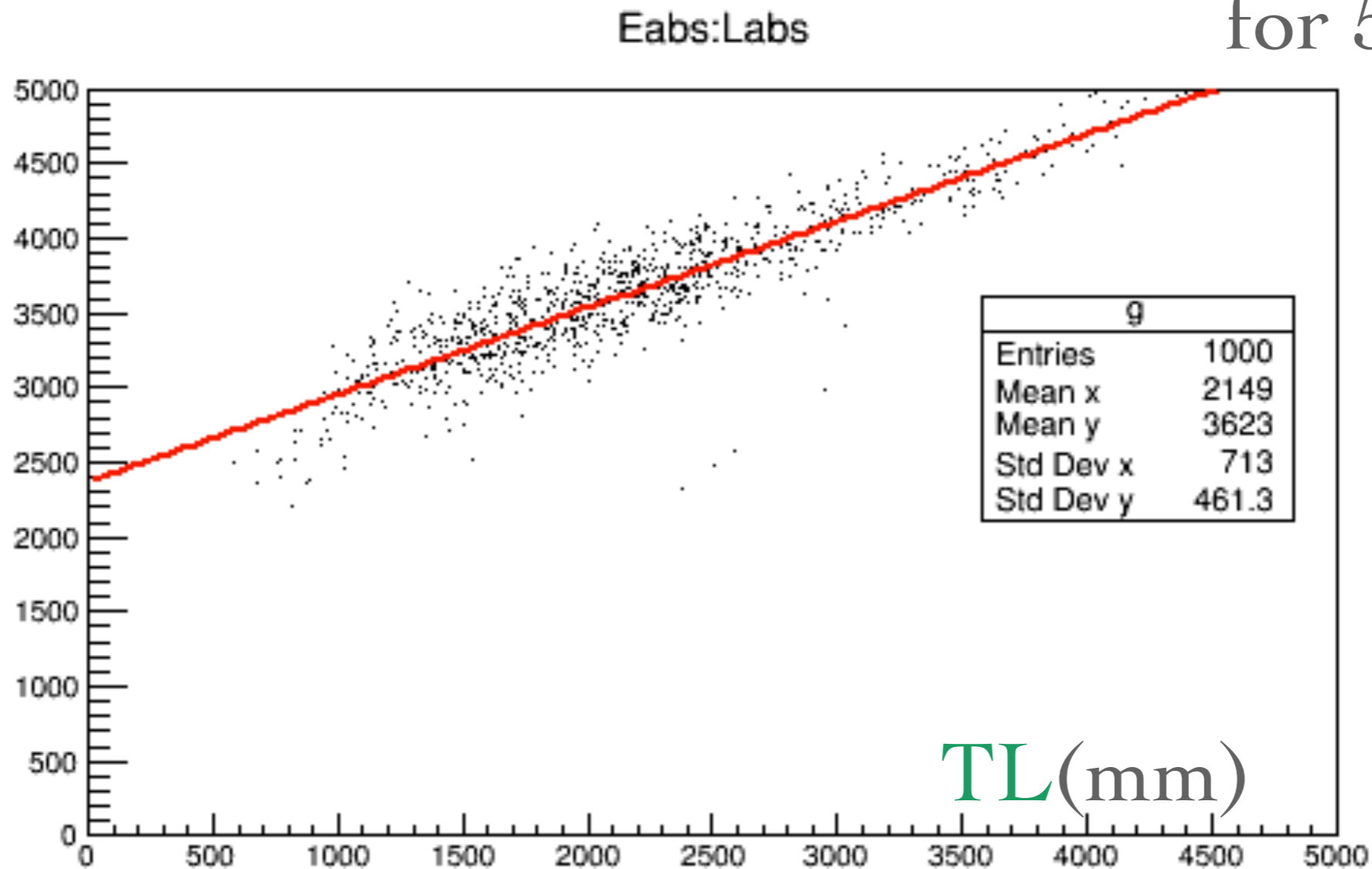
~ sum of Cherenkov lights in PbWO4

ED vs TL

- strong correlation between ED vs TL

for 5 GeV pi-

ED
(MeV)

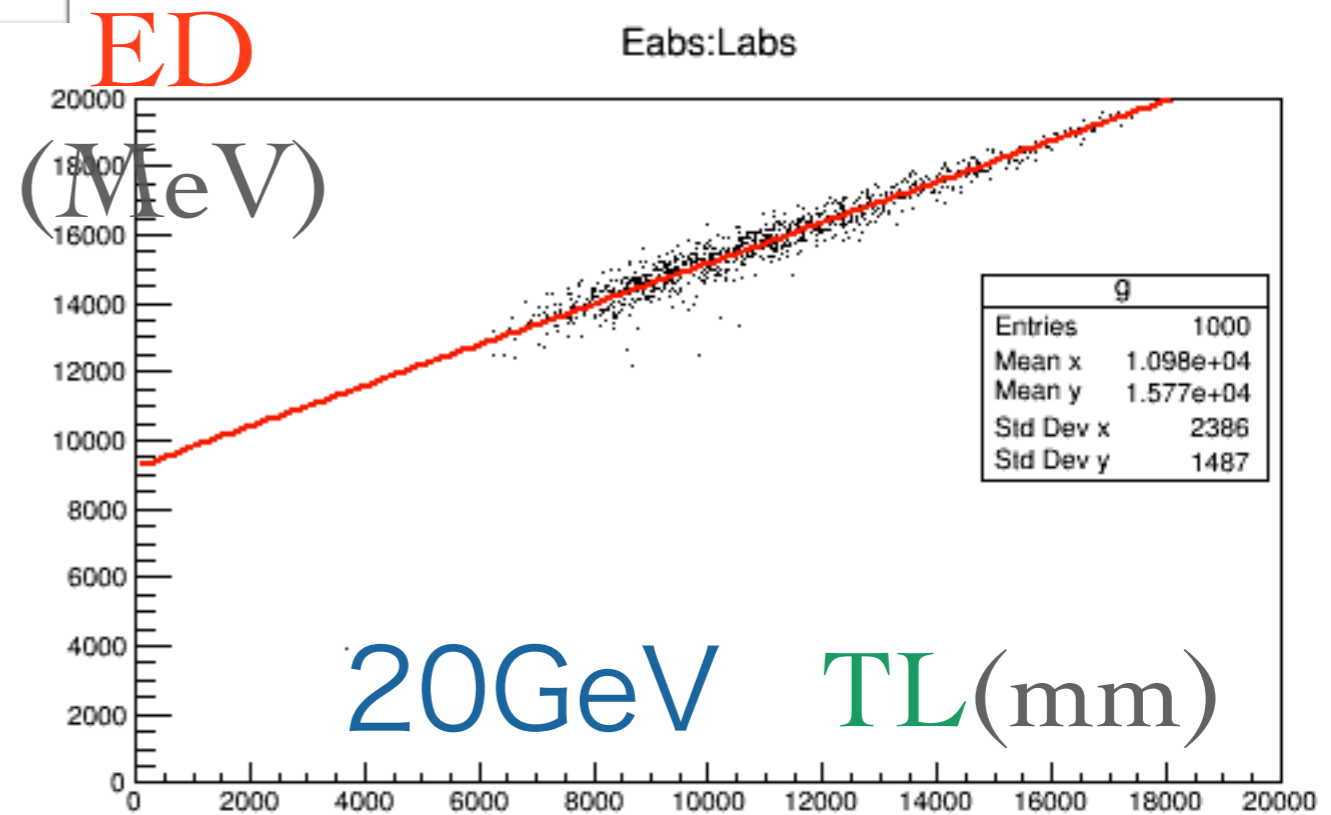
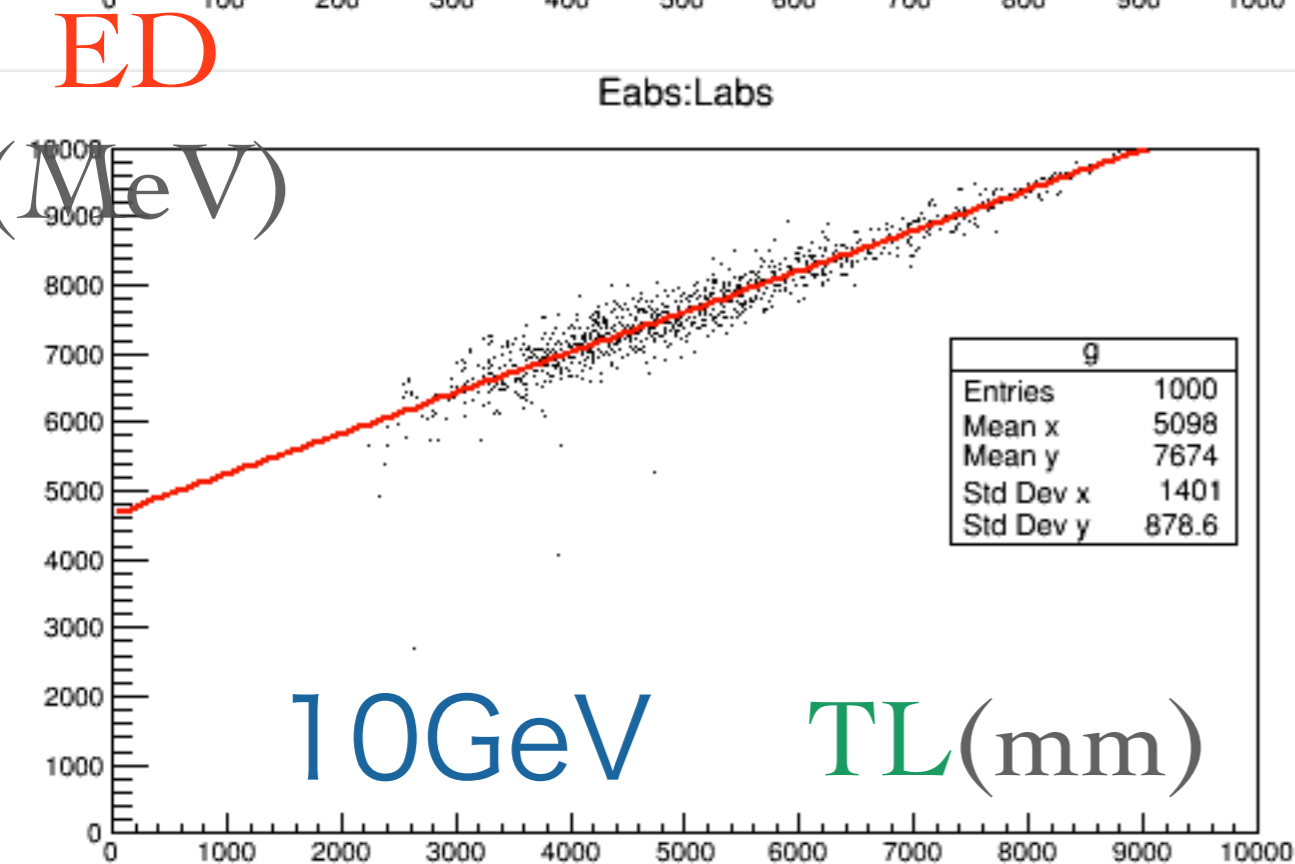
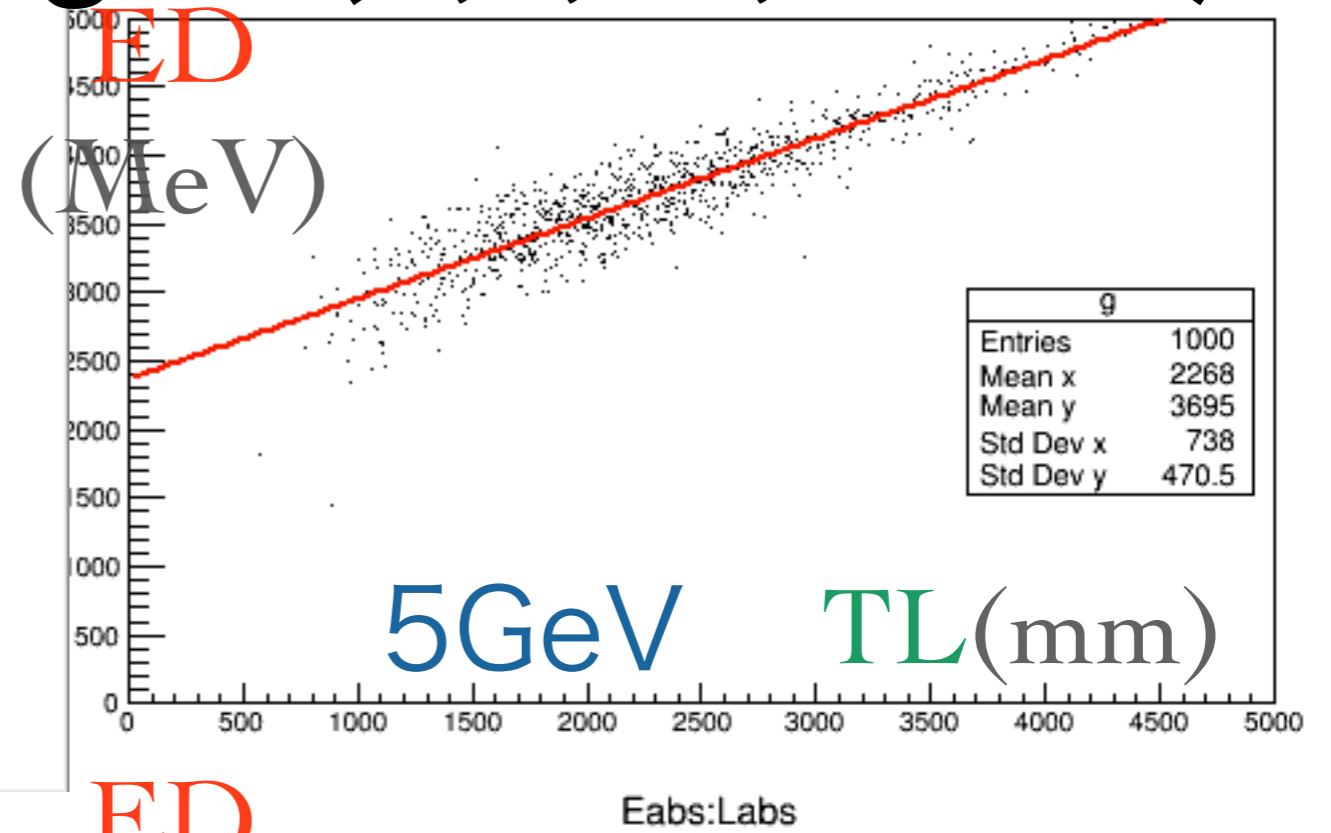
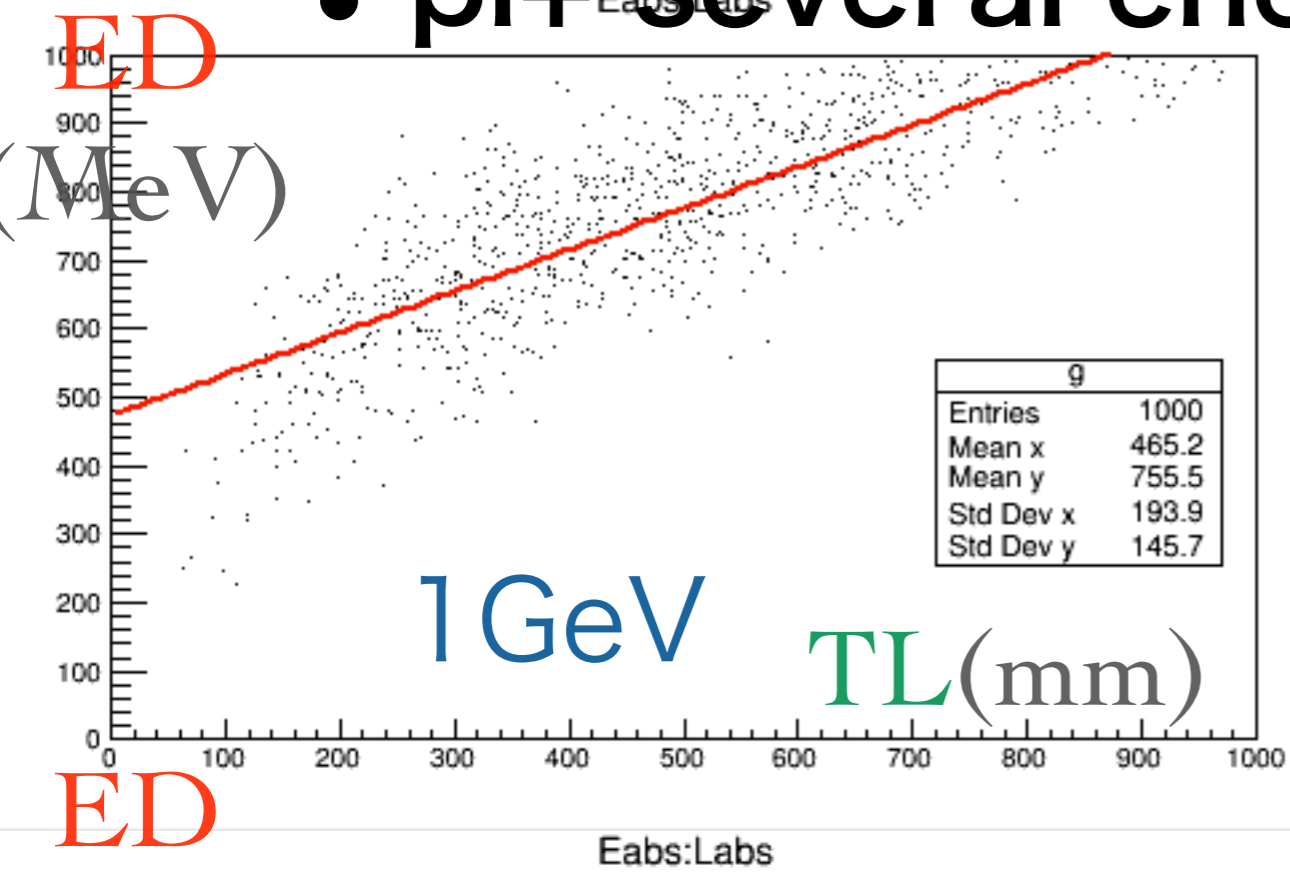


- approx. in linear with constant term in ED

ED vs TL

for π^+

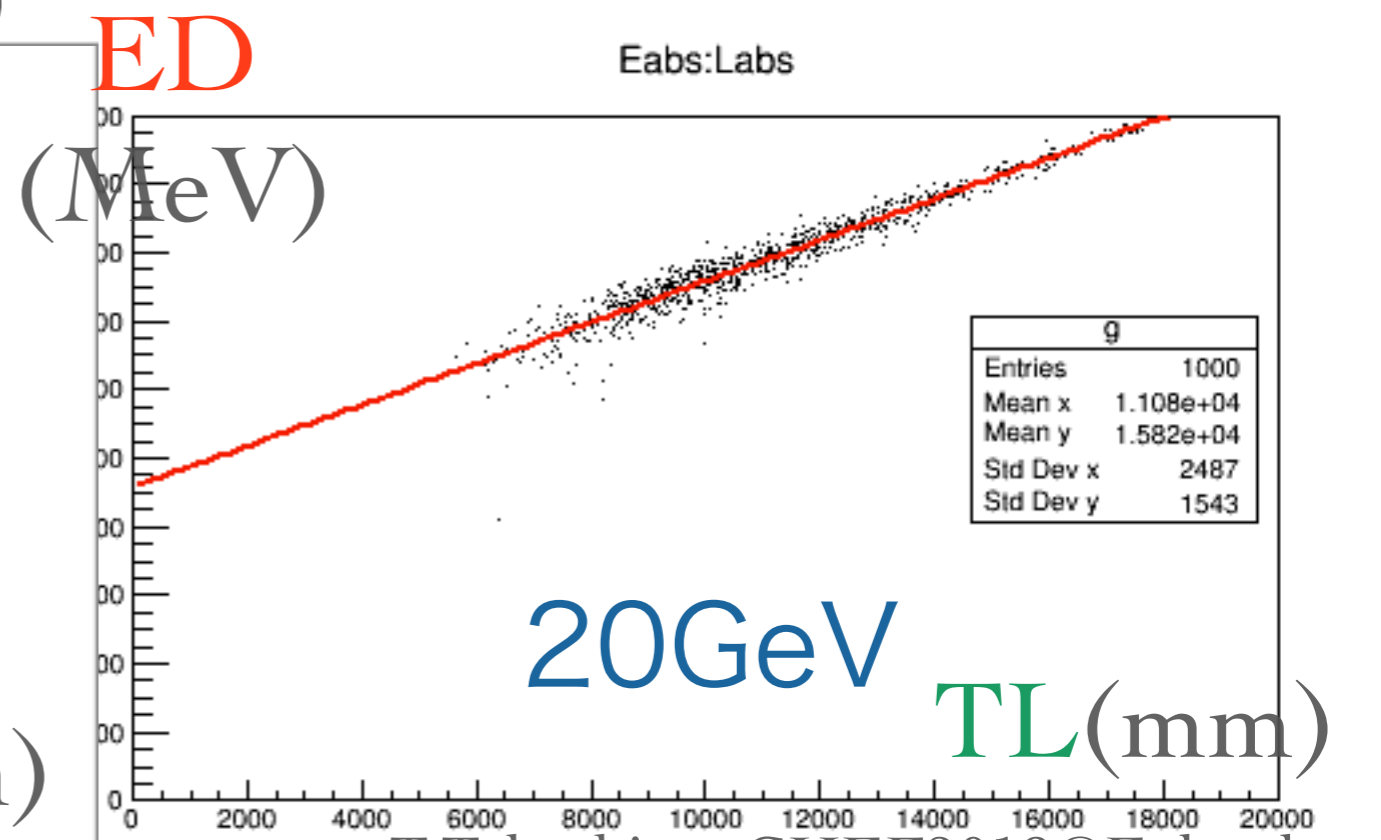
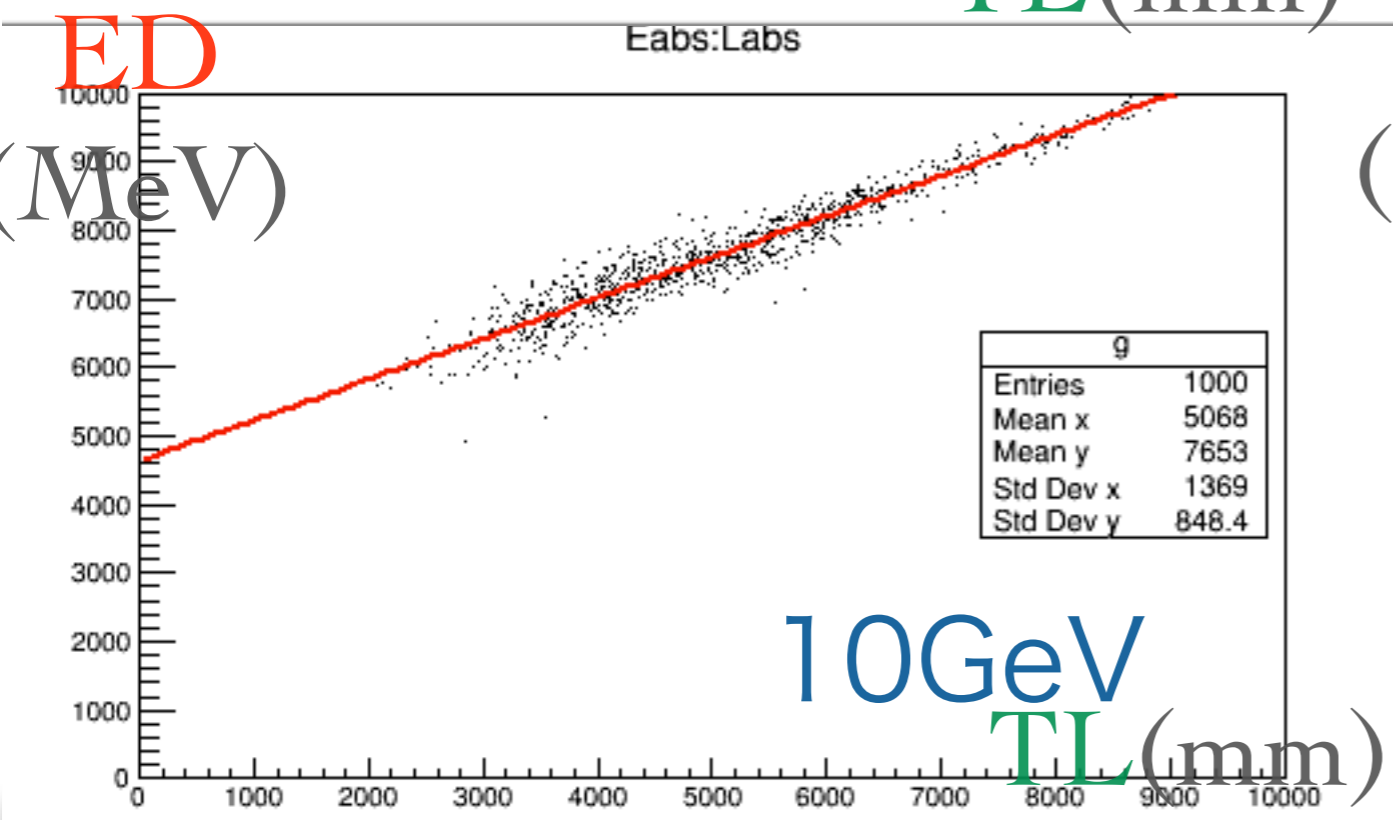
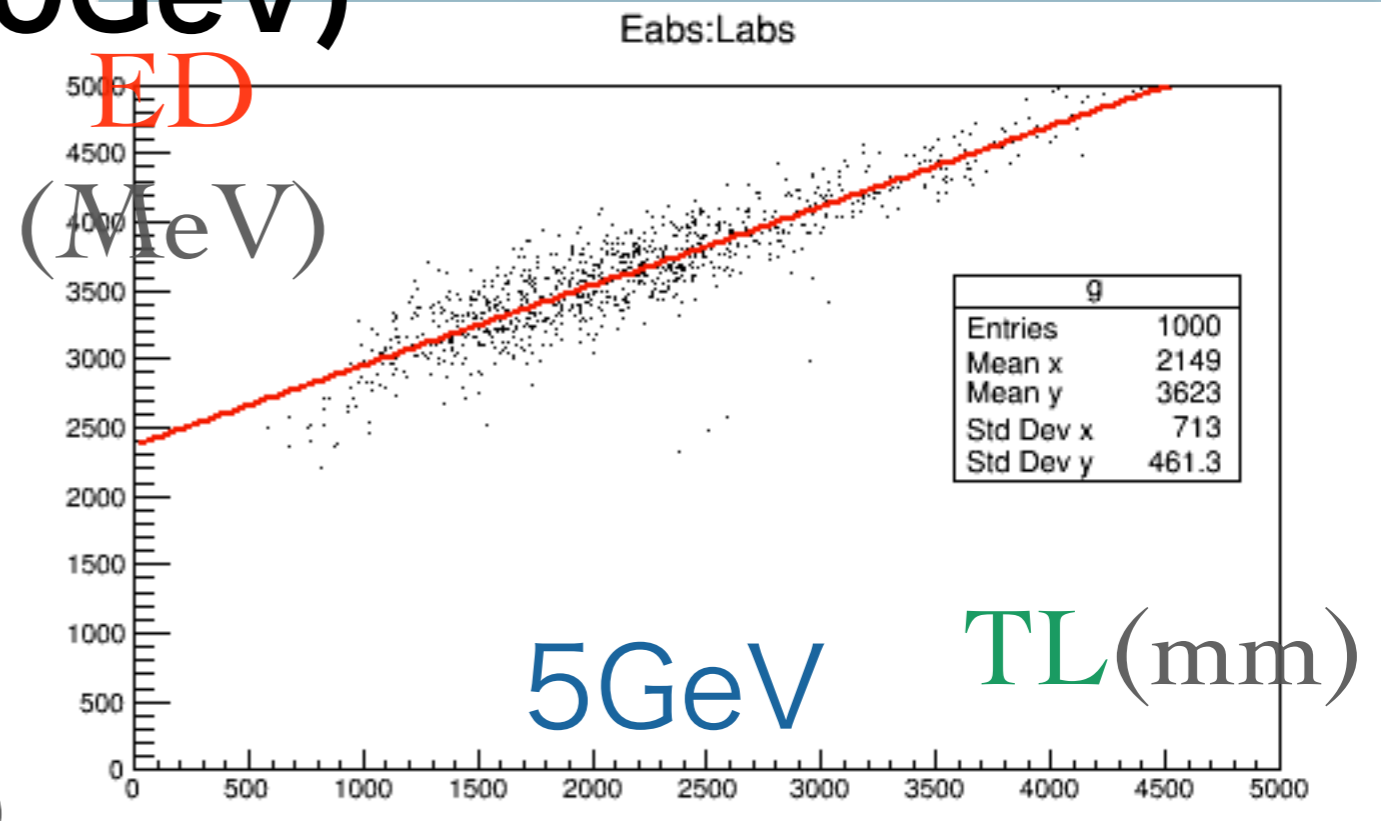
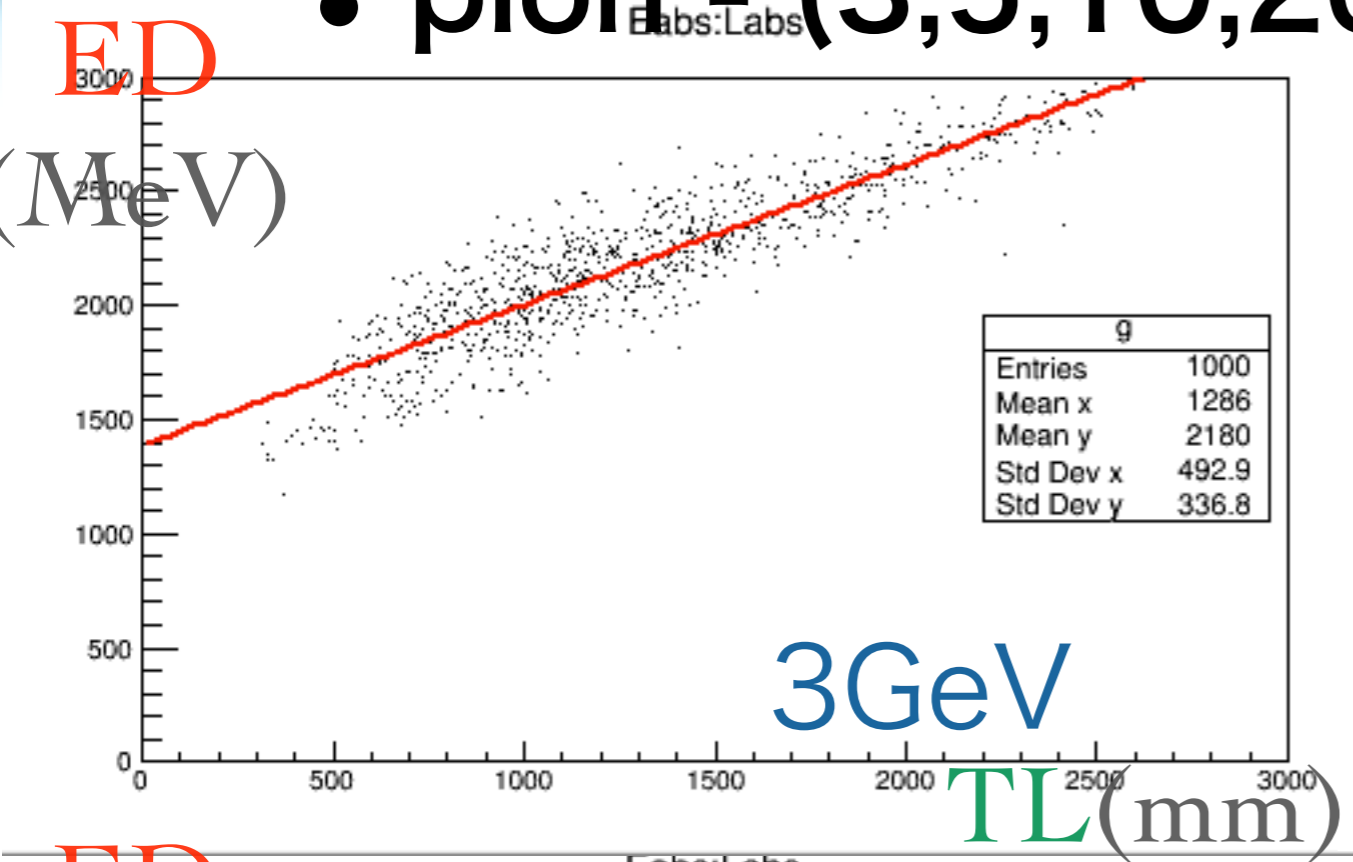
- π^+ several energies (1,5,10,20GeV)



ED vs TL

for pi-

- pion - (3,5,10,20GeV)

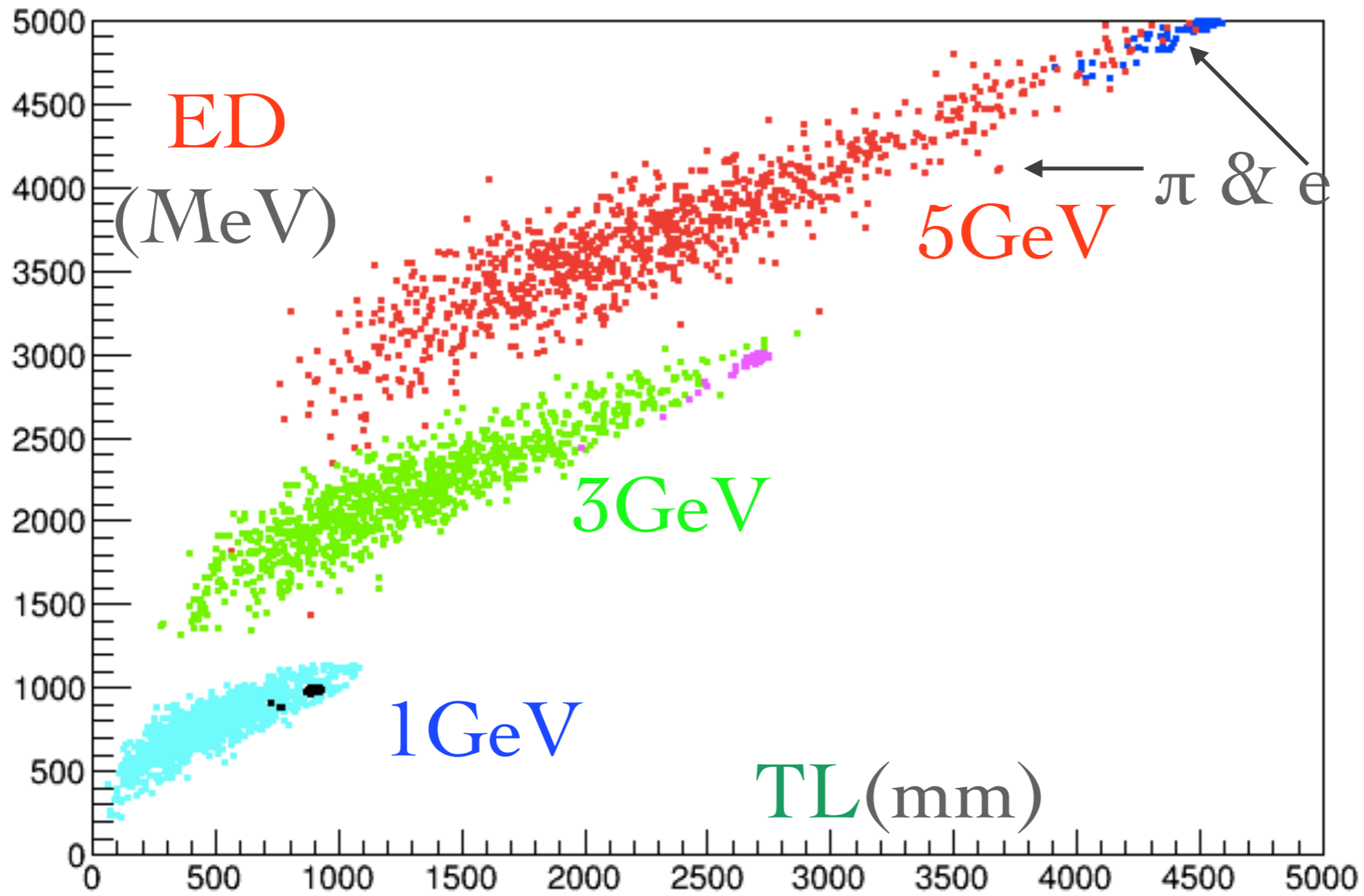


ED vs TL

constant slop for pi+ and e-
Eabs:Labs

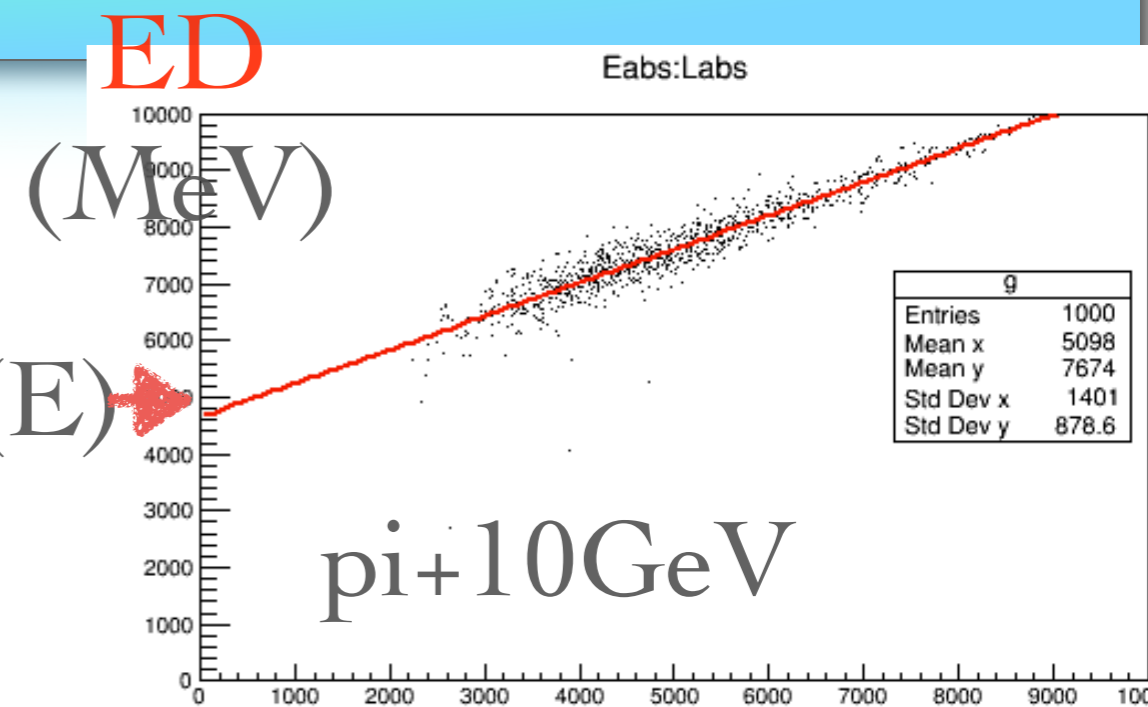
$$ED = A(E) + B * TL$$

MeV mm

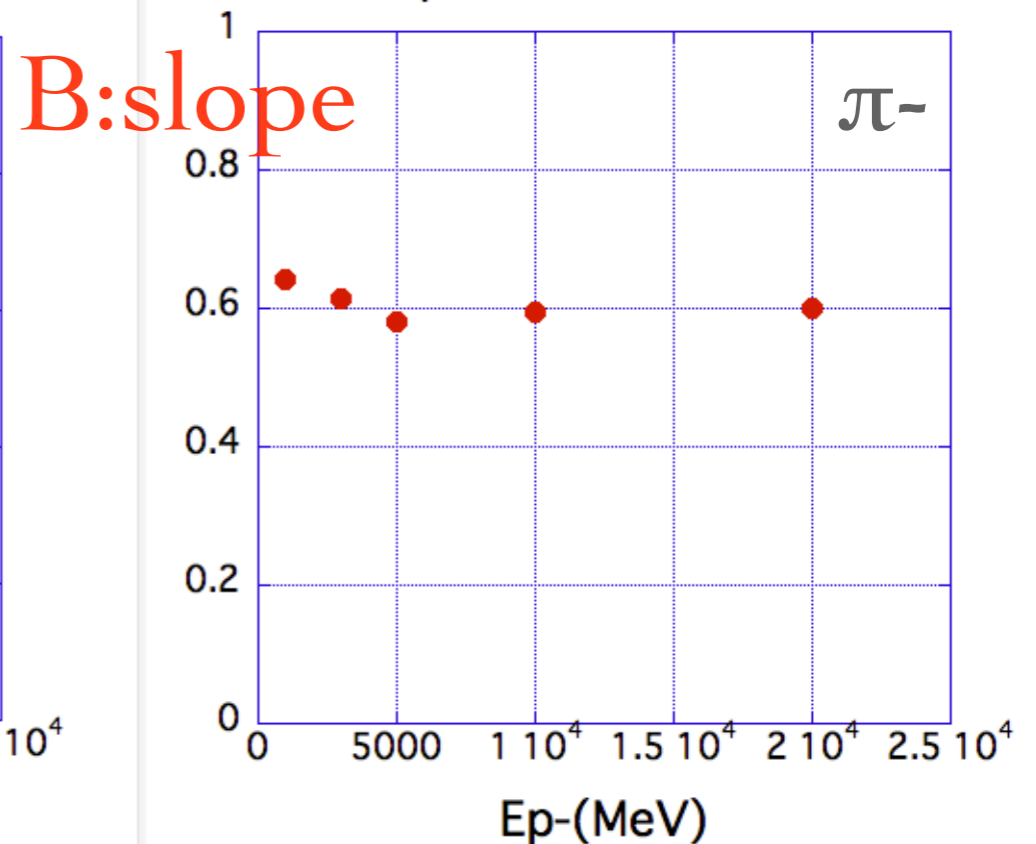
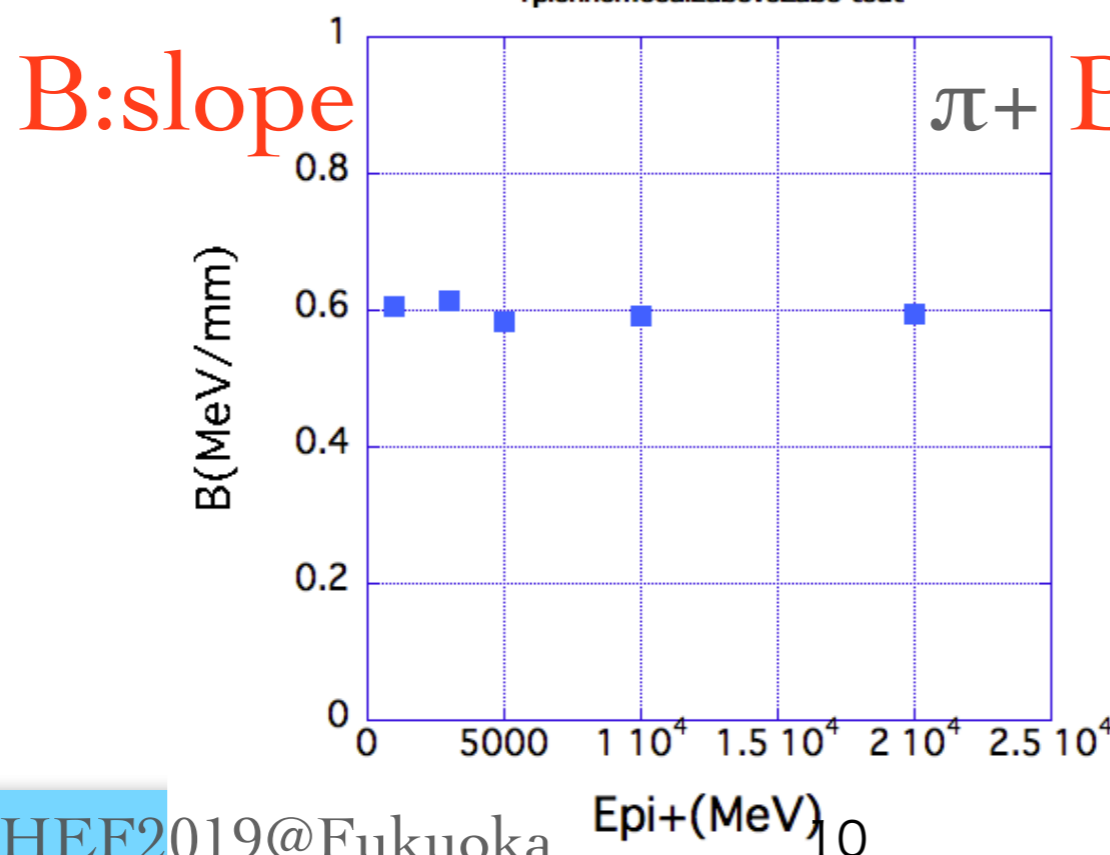


slop of ED and TL

- when fitted with linear $ED=A(E)+B*TL$
- slope=B is constant for all energies $E > 1\text{ GeV}$



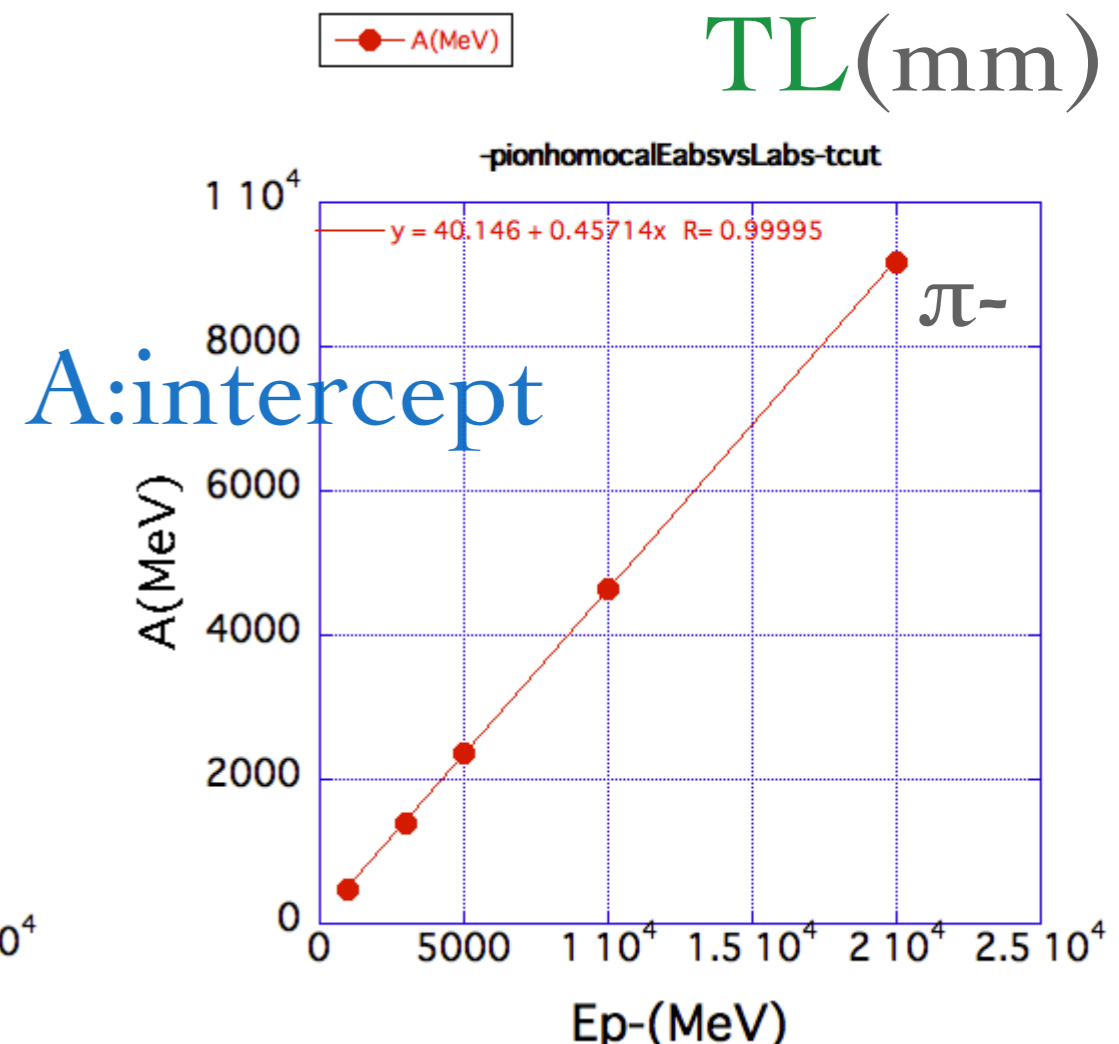
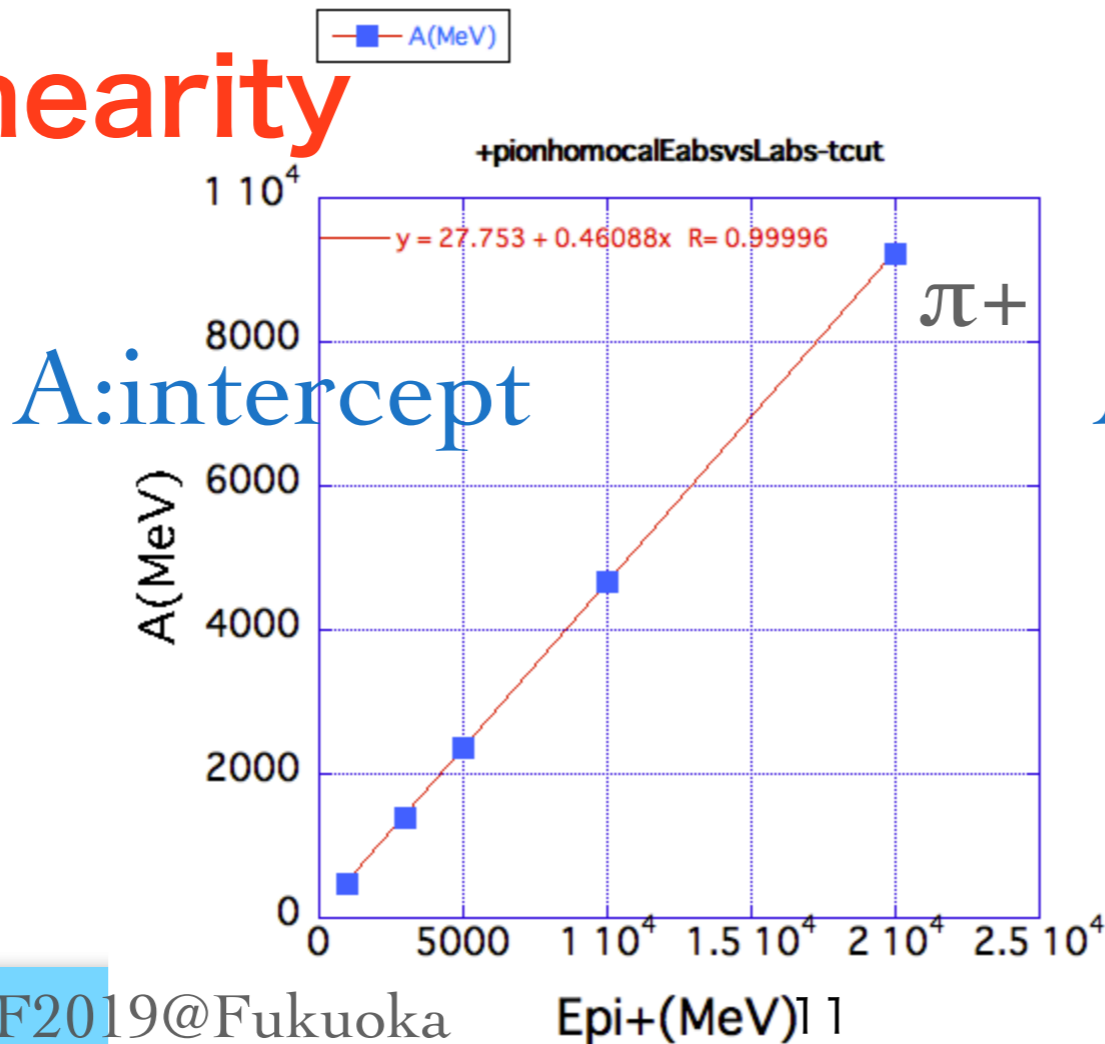
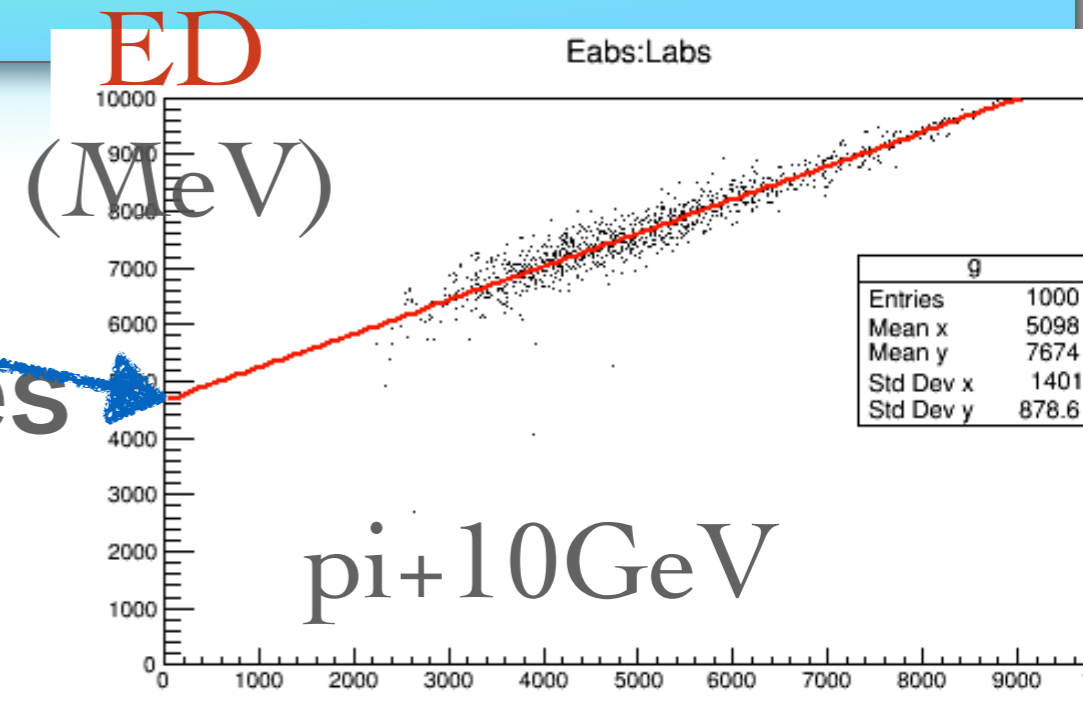
- no difference with π^- and π^+



intercept of fitted line

$$ED = A(E) + B * TL$$

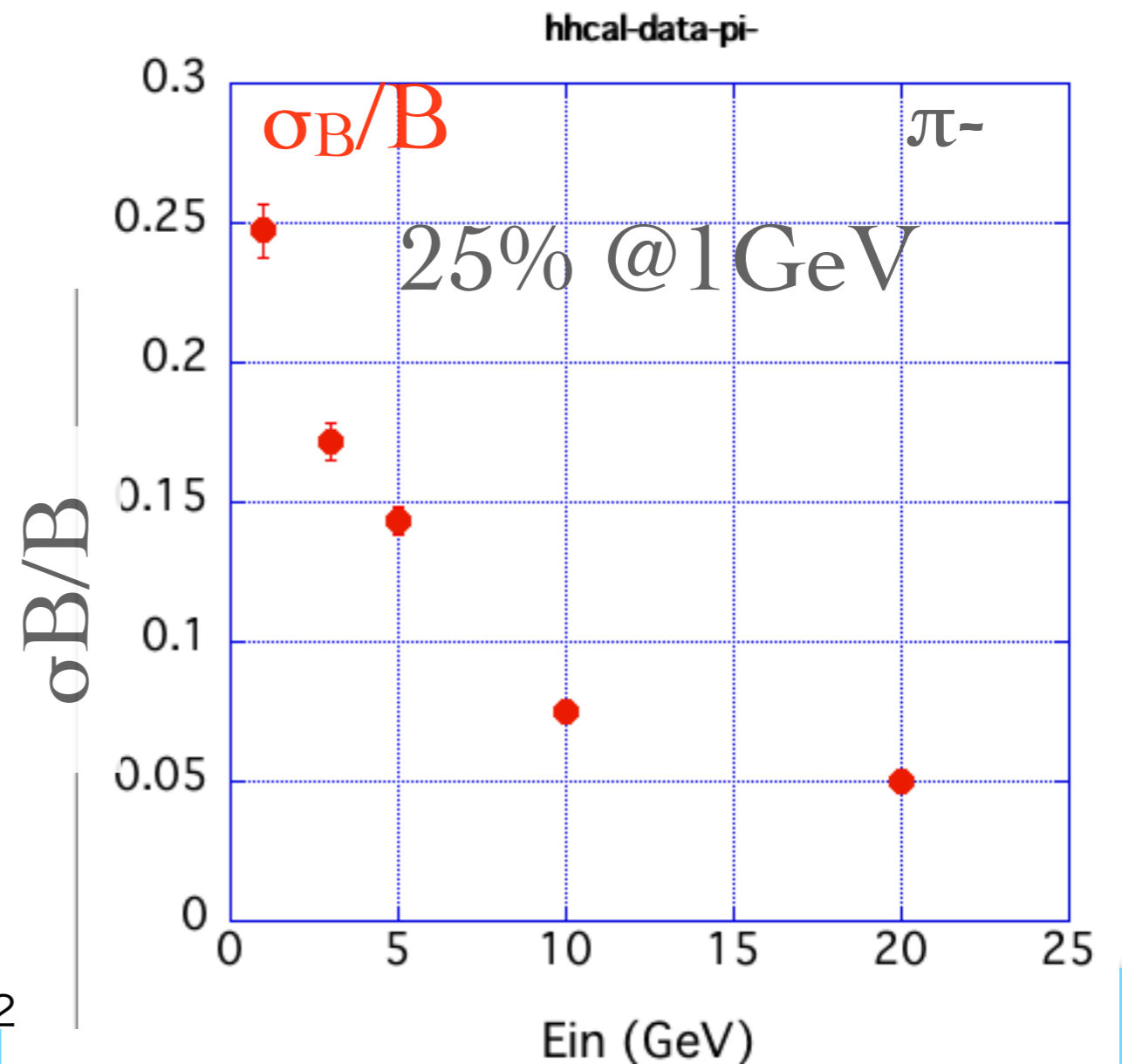
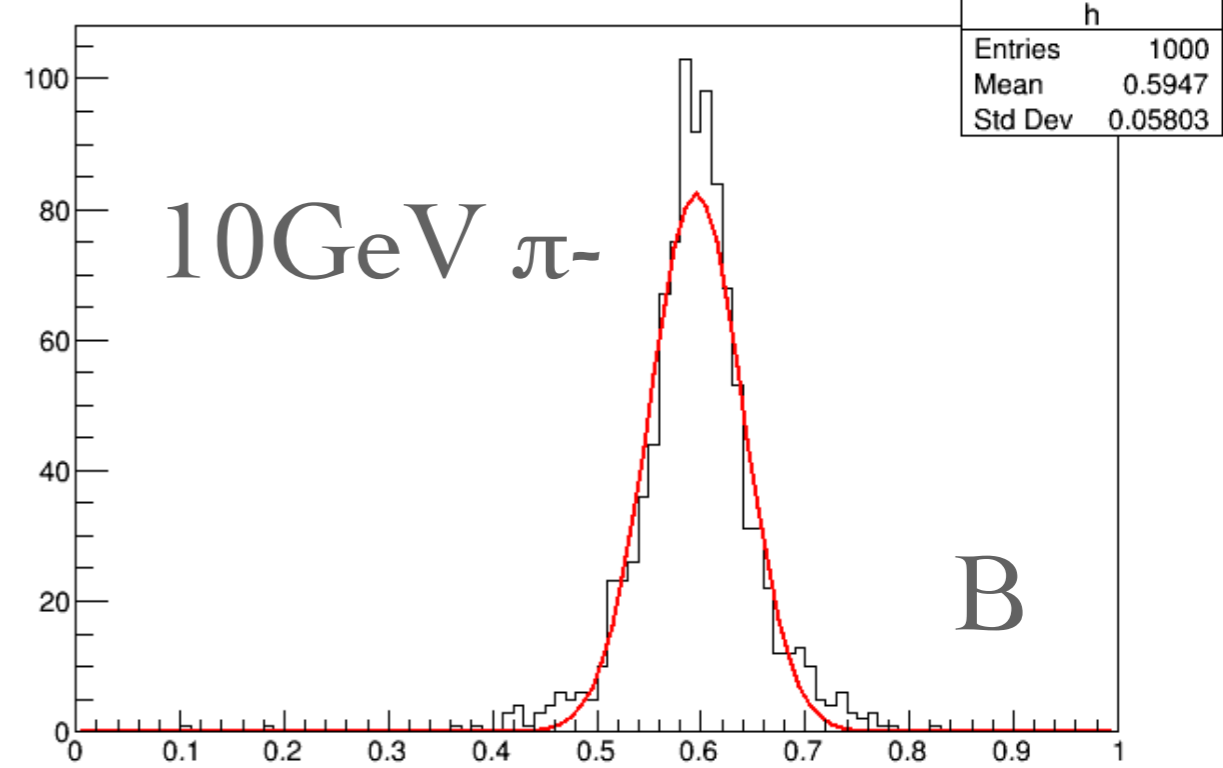
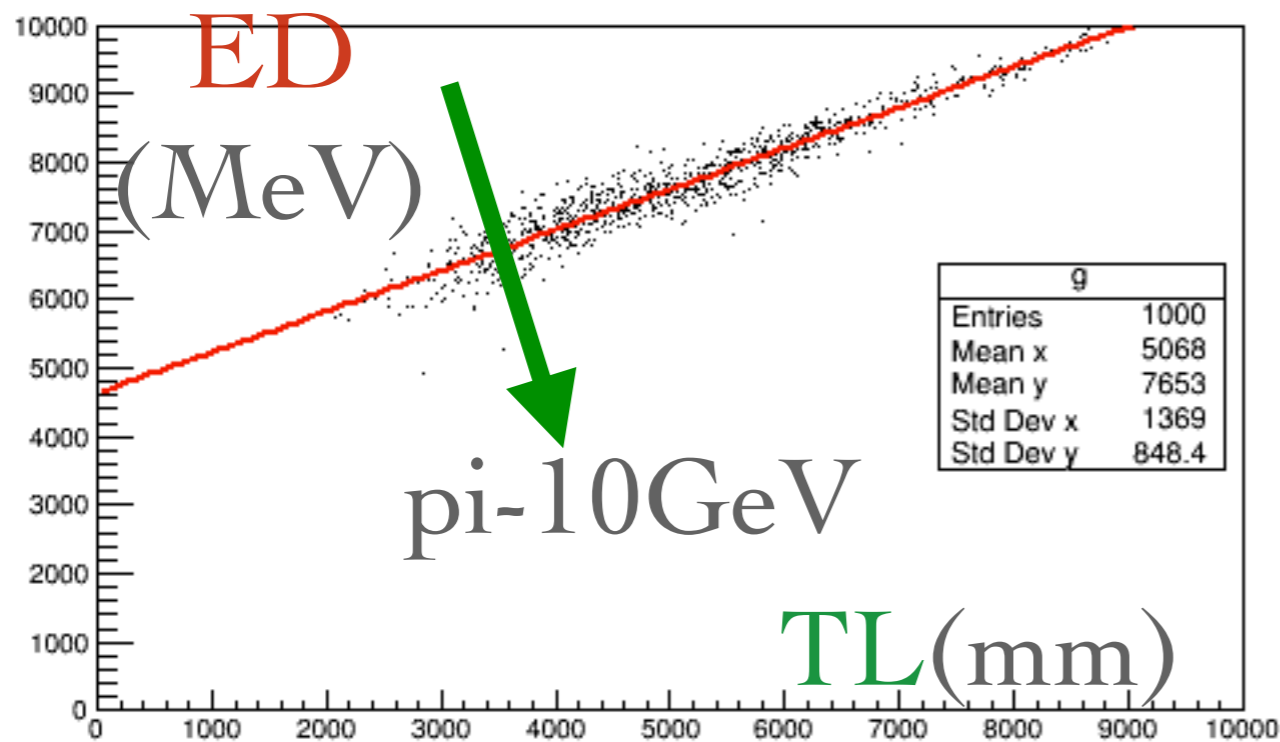
- intercept (cut) $A(E)$ is
- linear with injected energies
- same to π^- and π^+
- good **linearity**



Resolution

$$ED = A(E) + B * TL$$

- $B = (ED - A(E)) / TL$
- B is independent on E
- resolution of the calorimeter $\sim \sigma_B / B$



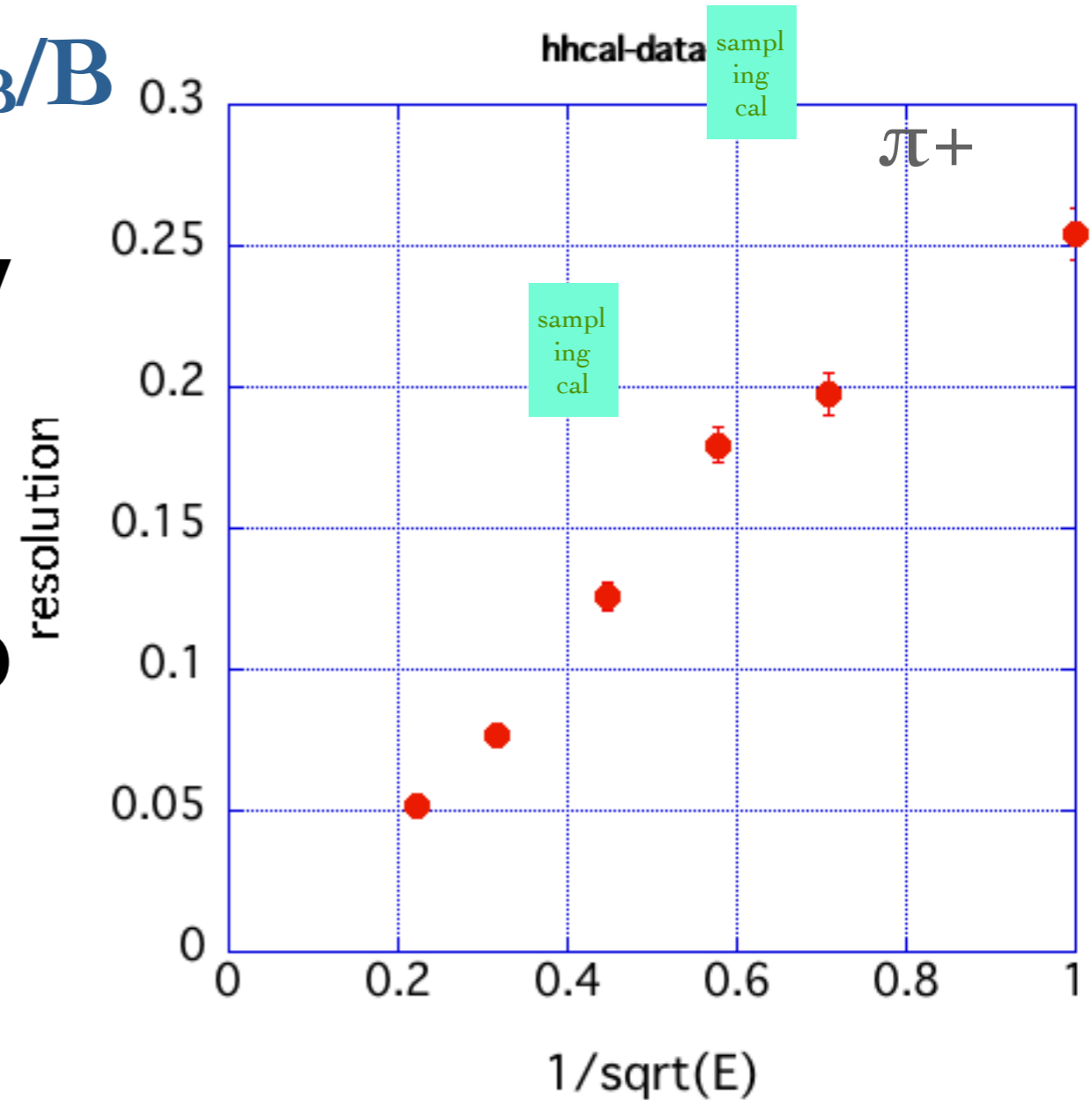
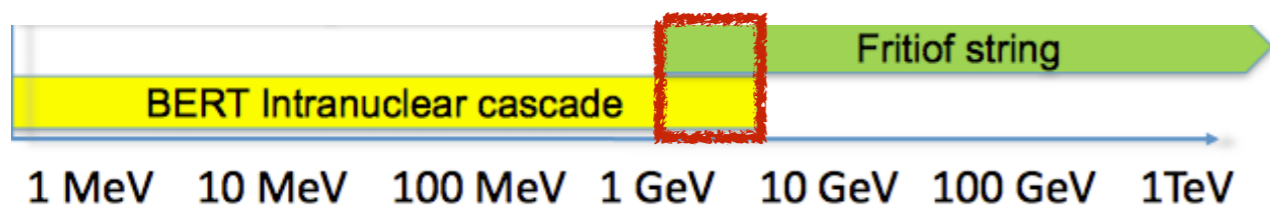
Energy resolution

sampling cal

$$ED = A(E) + B * TL$$

$$\sigma_B/B \sim 25\% / \sqrt{E}$$

- energy resolution = σ_B/B
- σ_B/B scales in $1/\sqrt{E(\text{GeV})}$
- kink at $\sim 5\text{GeV}$ due to
- Hadron model in G4

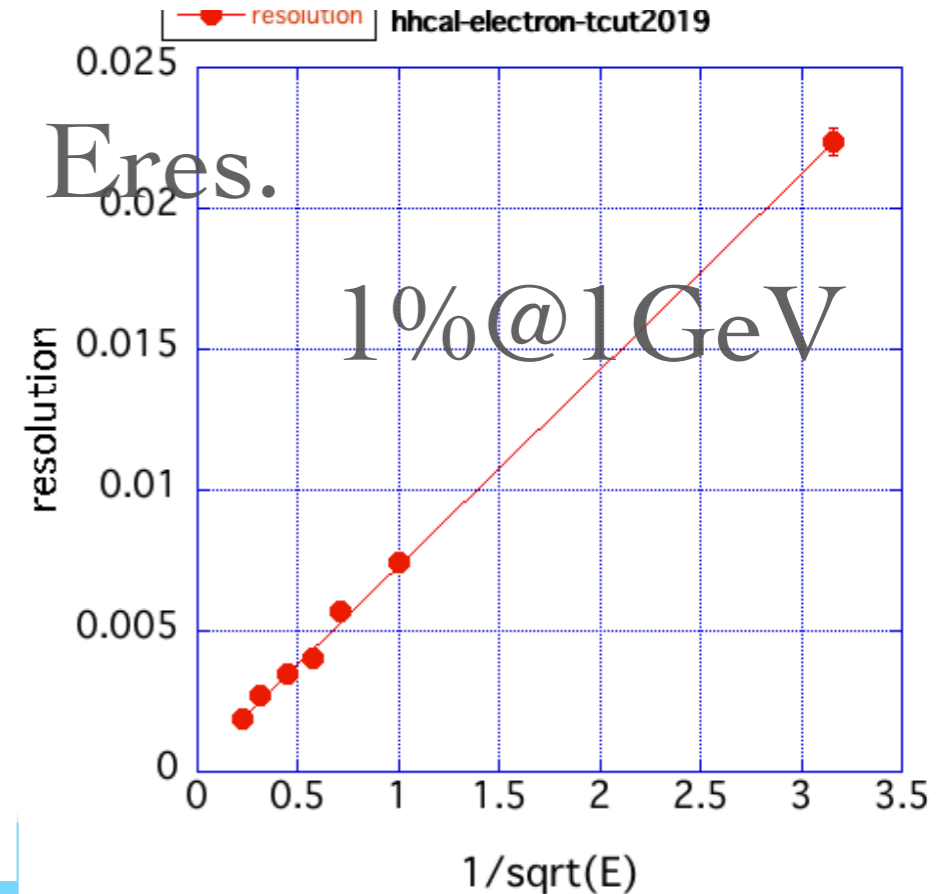
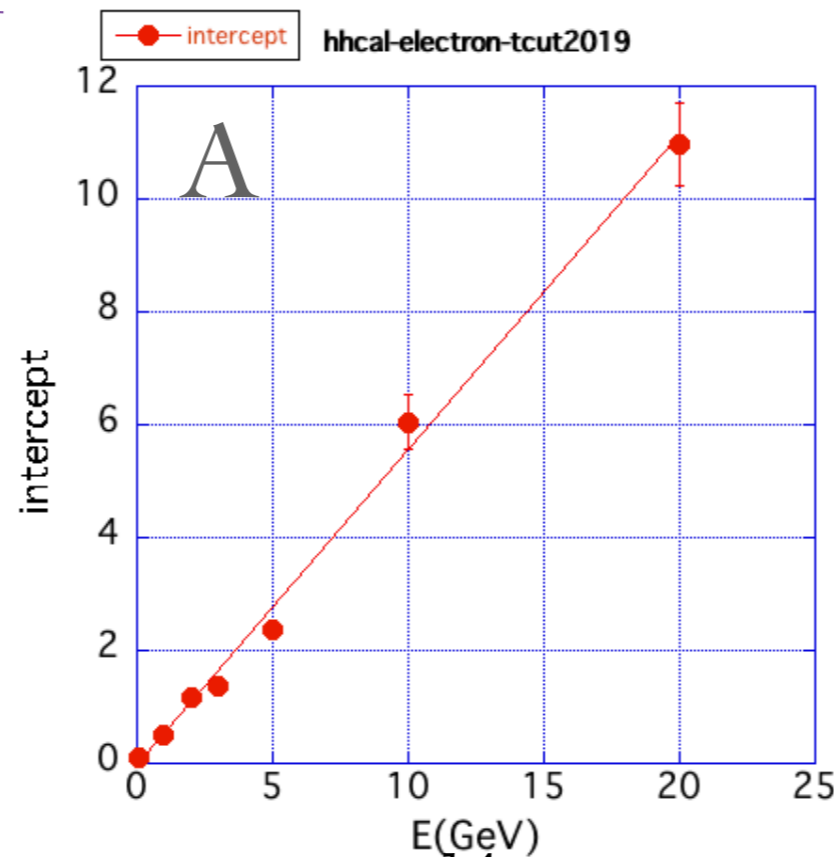
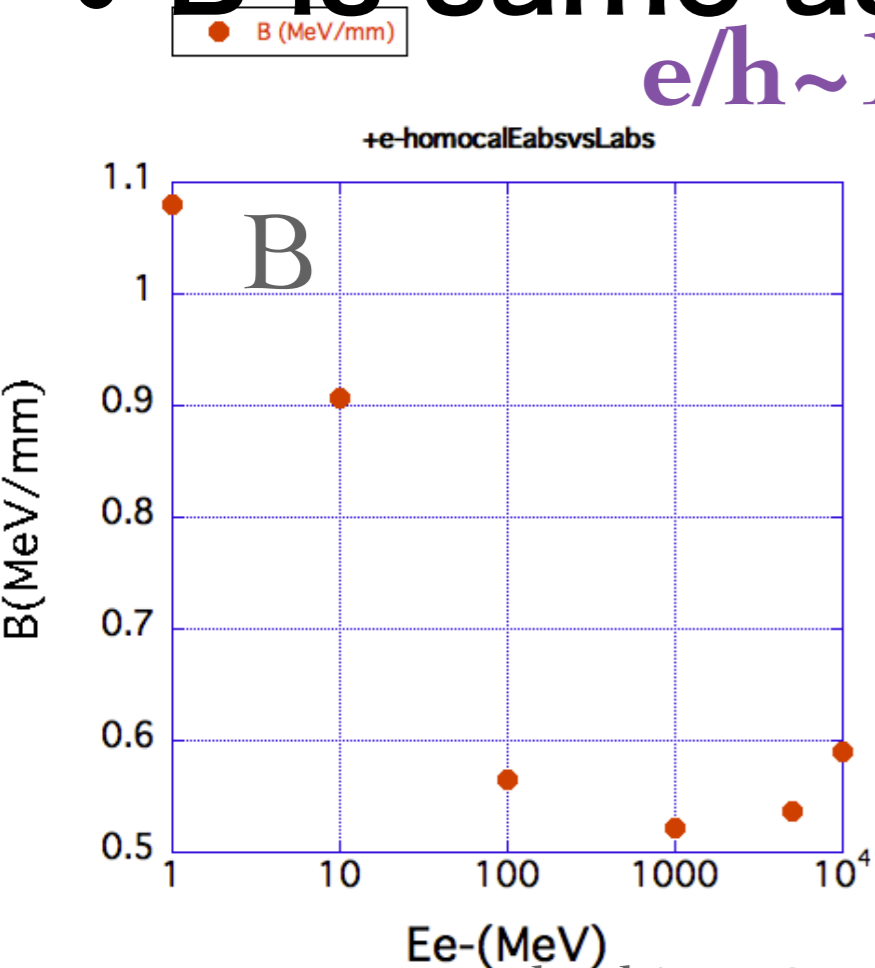
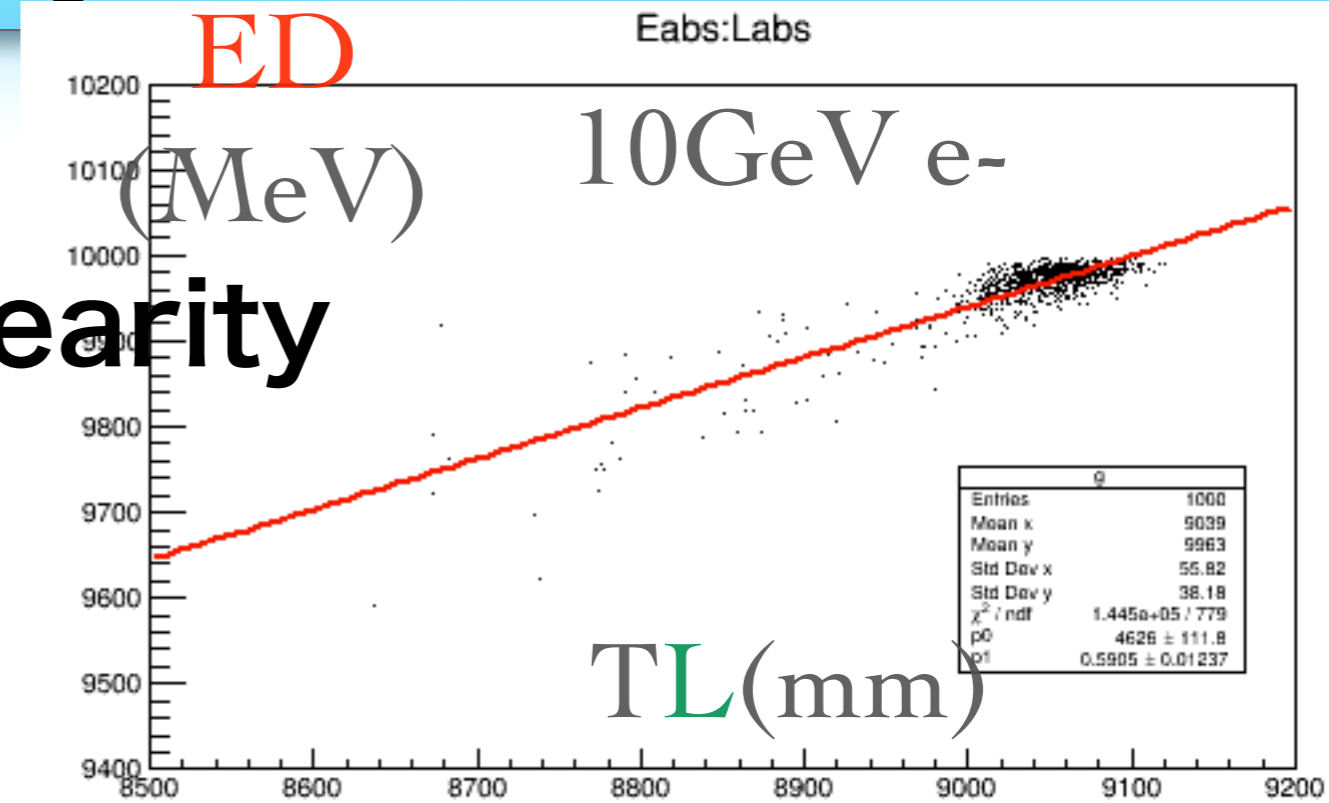


50, 20, 10, 5, 3, 1 GeV

EM response

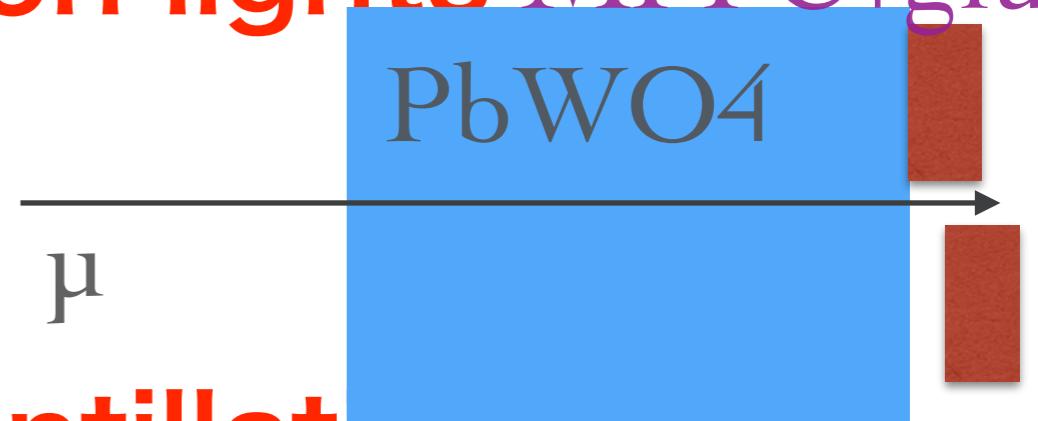
$$ED = A(E) + B * TL$$

- **ED vs TL:**
- **A(E) shows good linearity**
- **B is const. at $E > 100 \text{ MeV}$**
- **B is same as $\sim \pi \pm e/h \sim 1$**



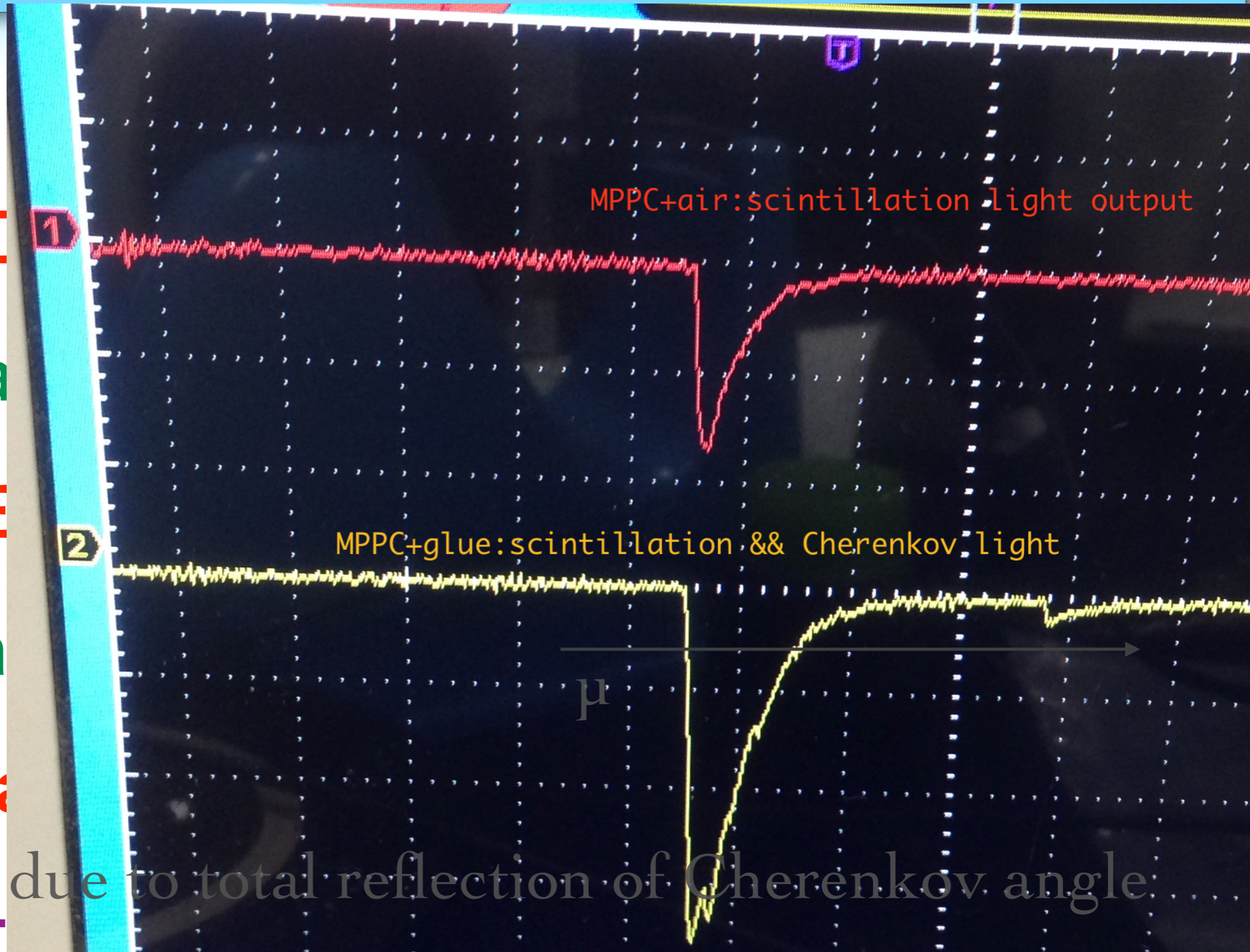
how to measure

- energy resolution $\sim 25\% / \sqrt{E}$
- from **ED** and **TL**
- use **heavy crystal** such as PbWO_4
- **ED** $\sim dE/dx \sim$ **scintillation lights** **MPPC+glue**
- **TL** \sim **Cherenkov lights**
- **MPPC+air coupling: scintillation** **MPPC+air**
- **MPPC+glue : Cherenkov + scintillation**
due to total reflection of Cherenkov angle



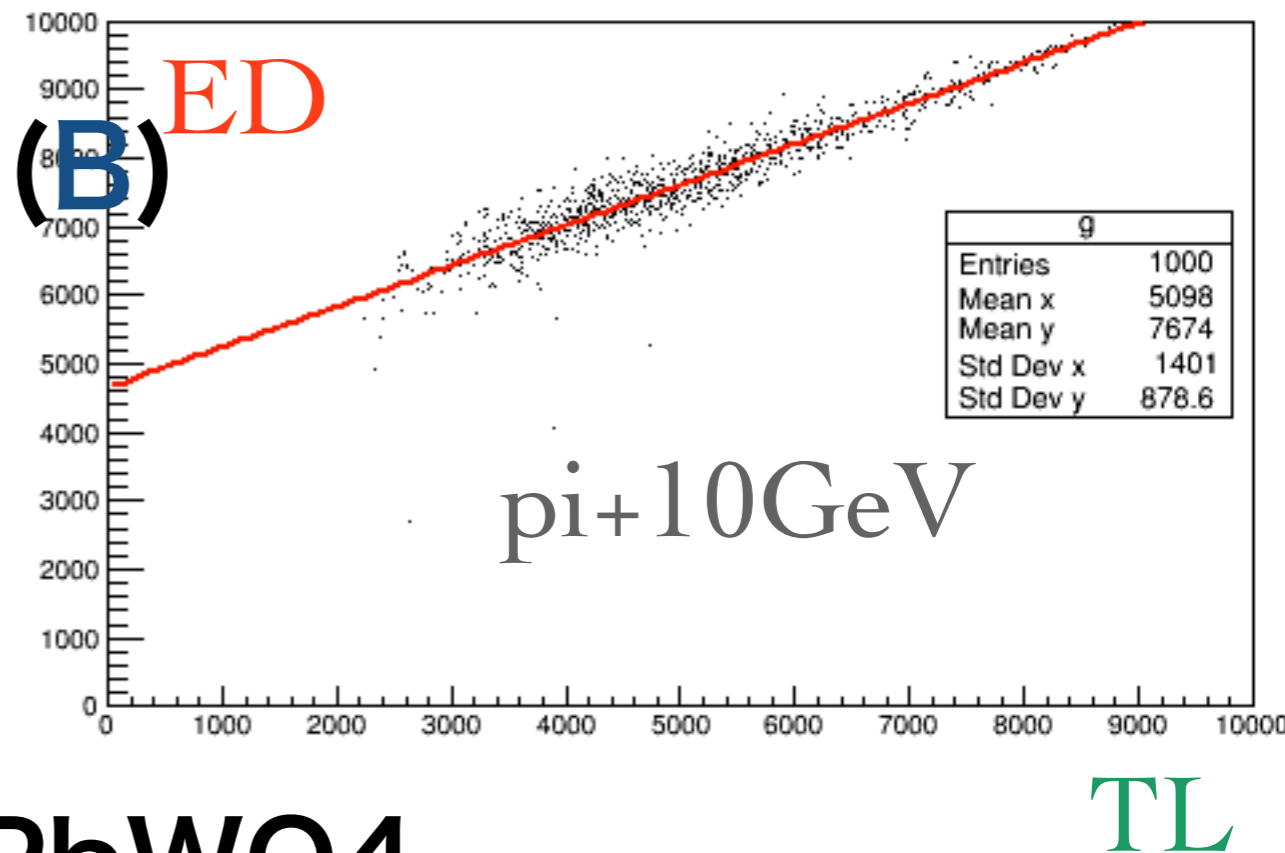
how to measure

- energy
- from ED
- use heat
- $ED \sim dE$
- $TL \sim Ch$
- MPPC+air
- MPPC+



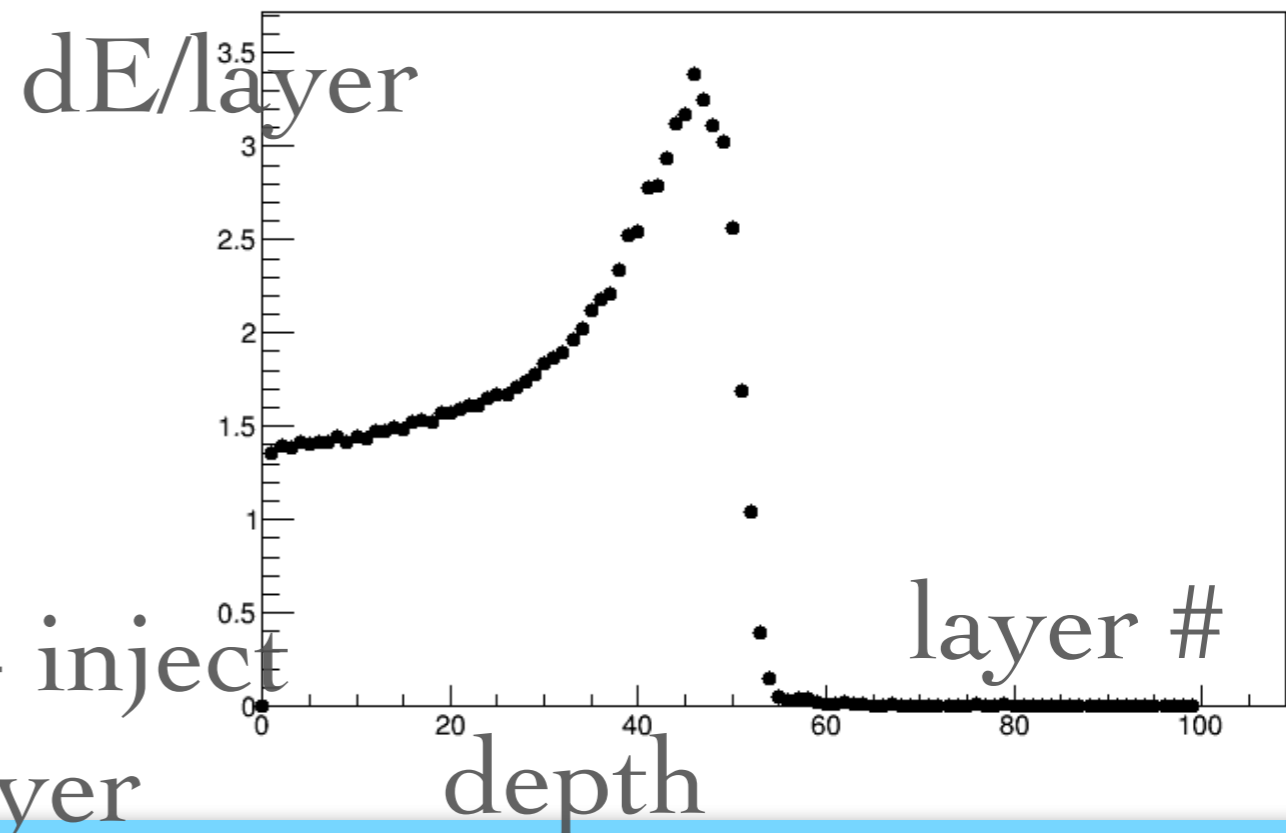
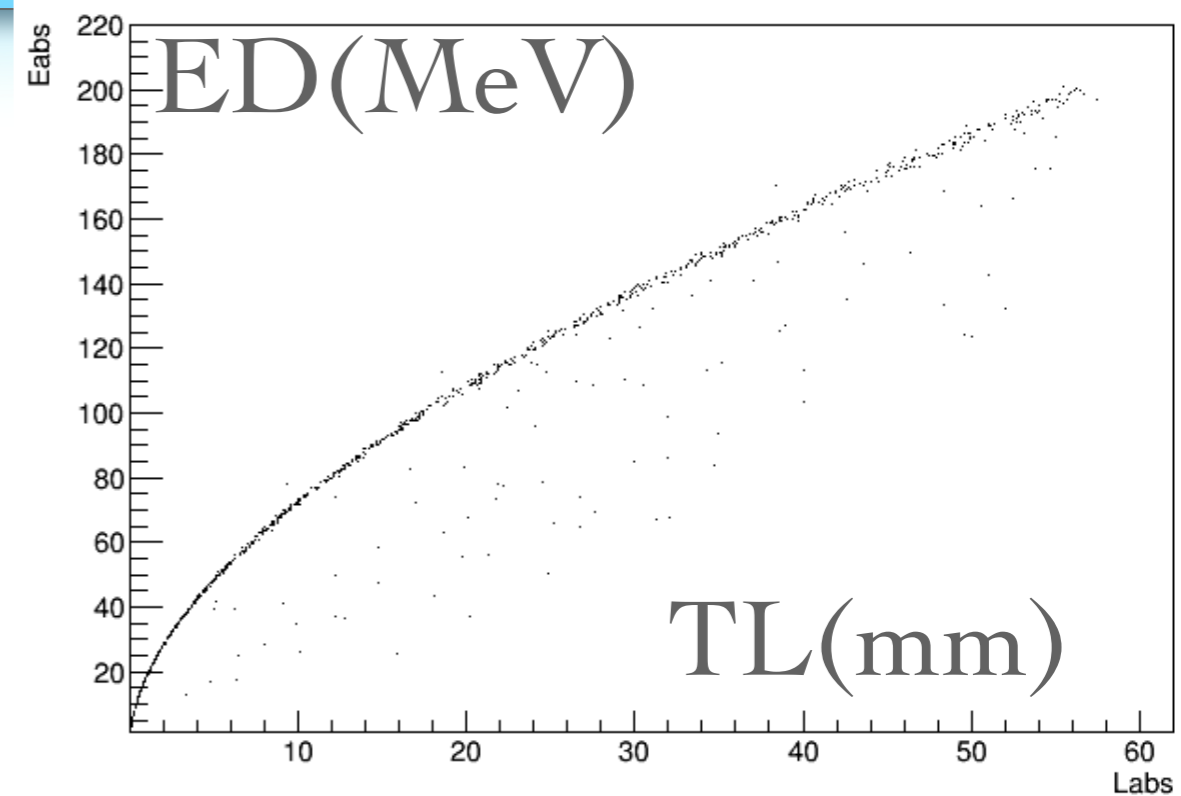
summary and outlook

- homogeneous calorimeter is simulated
- found a linear relation between ED and TL
$$ED = A(E) + B * TL$$
- good linearity by intercept $A(E)$
- fine energy resolution B
for pions no photon stat.
- ED ~ scintillation light
- TL ~ Cherenkov light
- test calorimeter with PbWO4



discussion

- reason of intercept
- muon+ : $< 200\text{MeV}$
uniform injection
- non-linear
response close to
 $0 = ED$
- due to Bragg curve

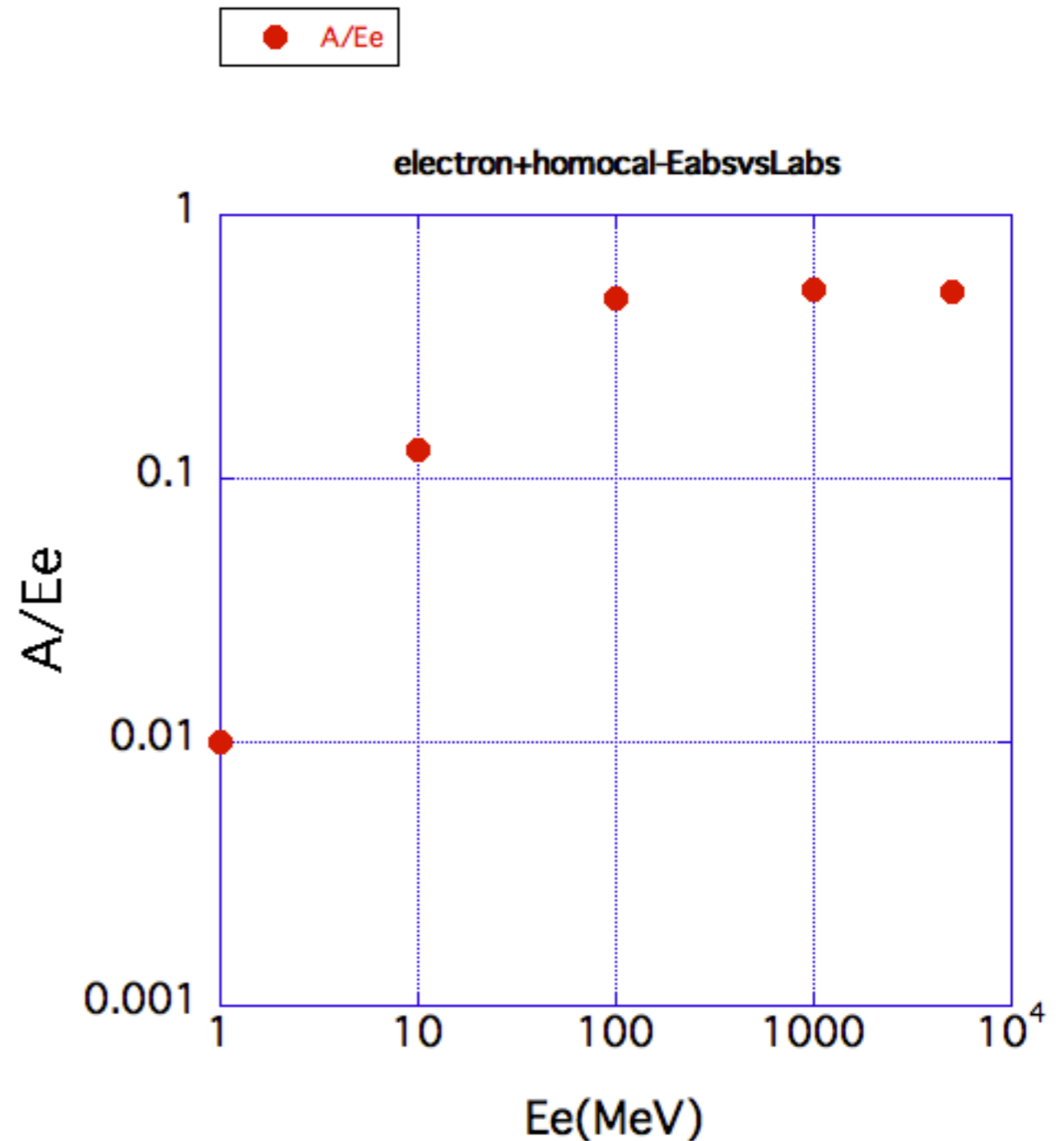


100MeV mu+ inject

1mmPb/layer

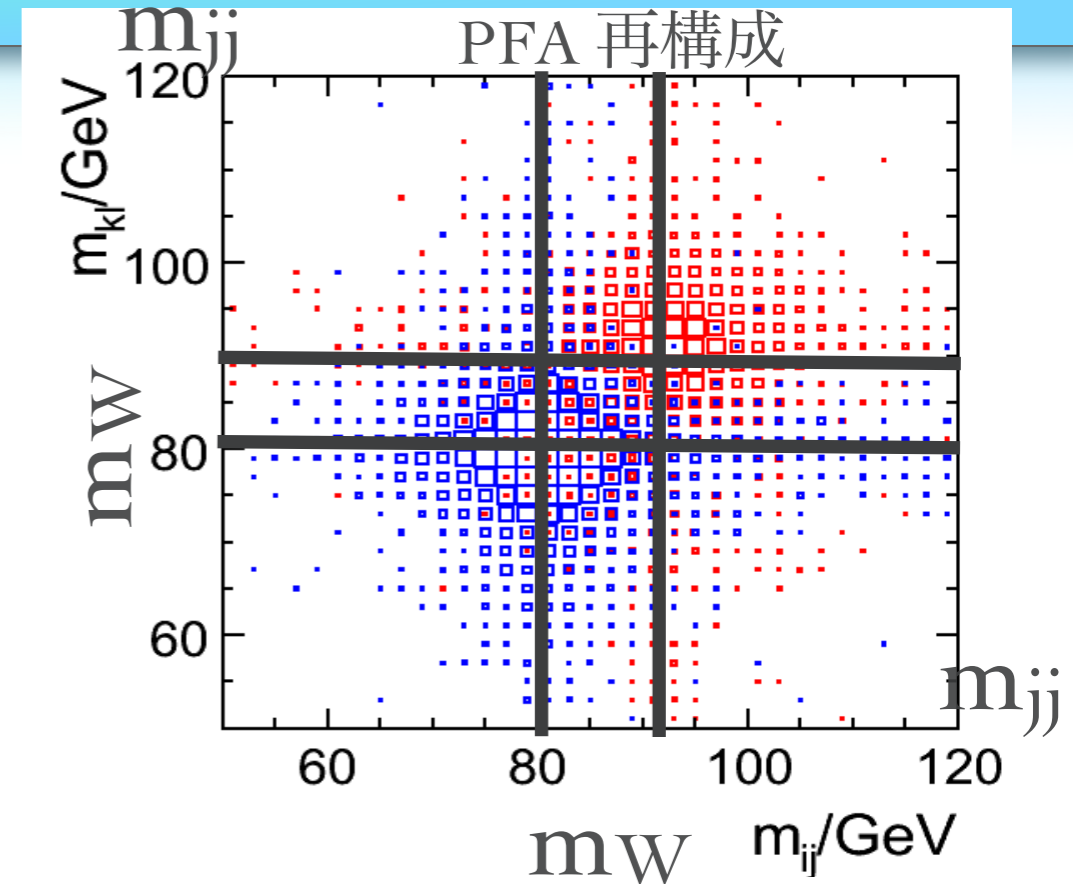
discussion

- electron cases are tested
- $A/E_e \sim \text{const.}$ at $E_e > 100 \text{ MeV}$ where EM shower dominates
- at lower E_e , close to zero



PFA performance

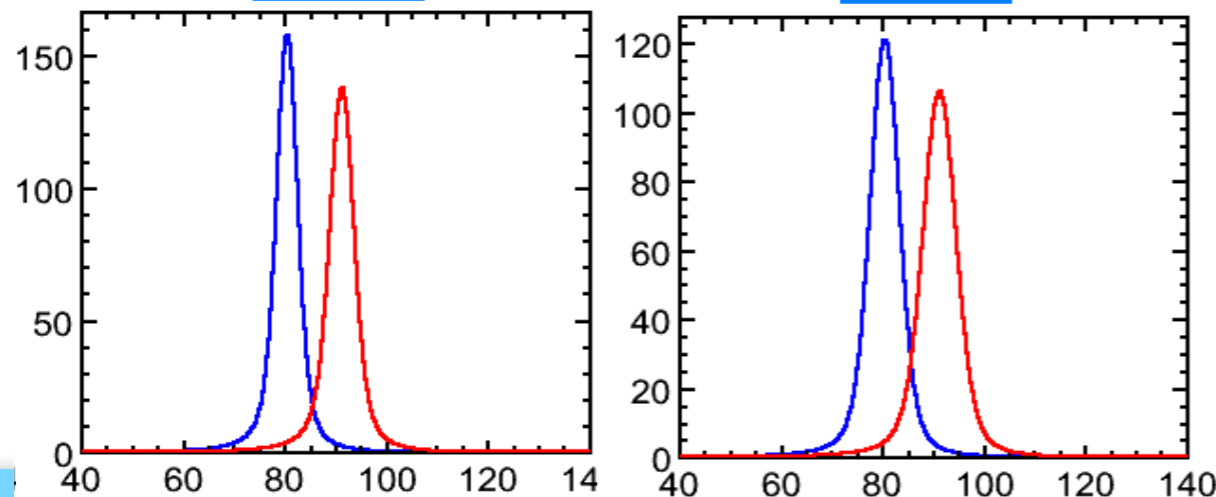
- PFA utilises
- tracker for charged
- ECAL for photons
- HCAL for KoL
- can separate W and Z



m_{jj}

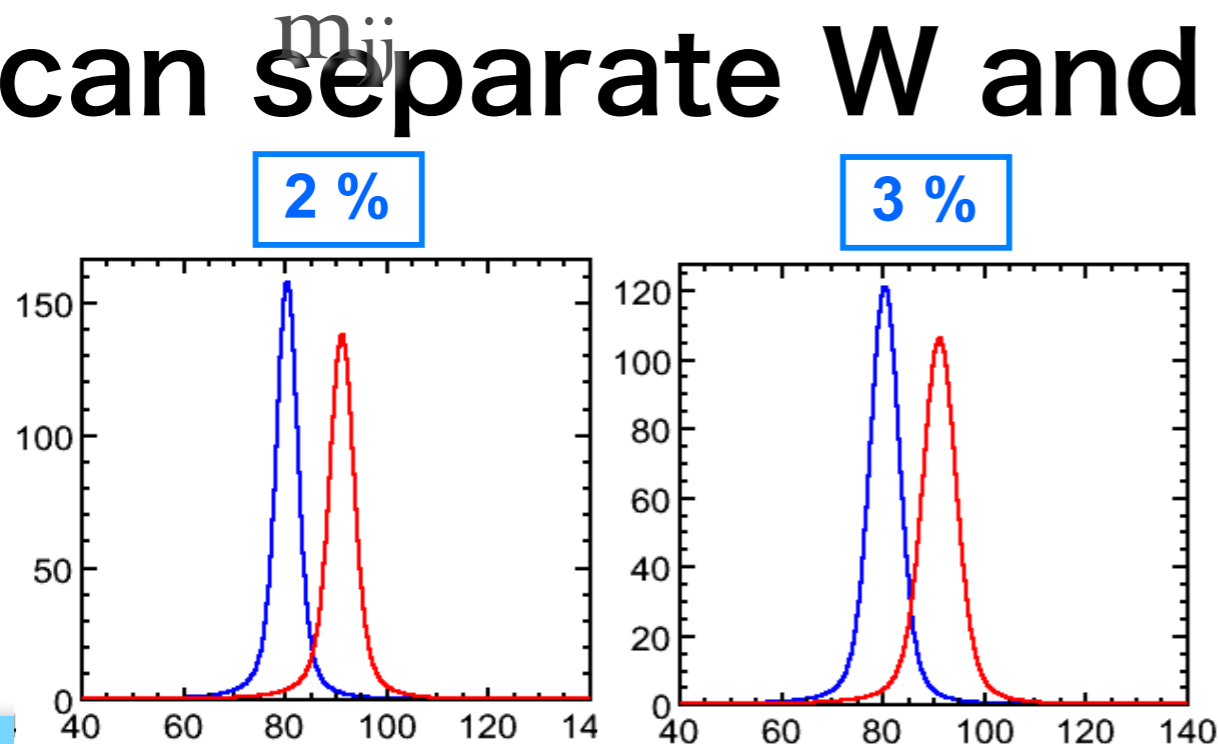
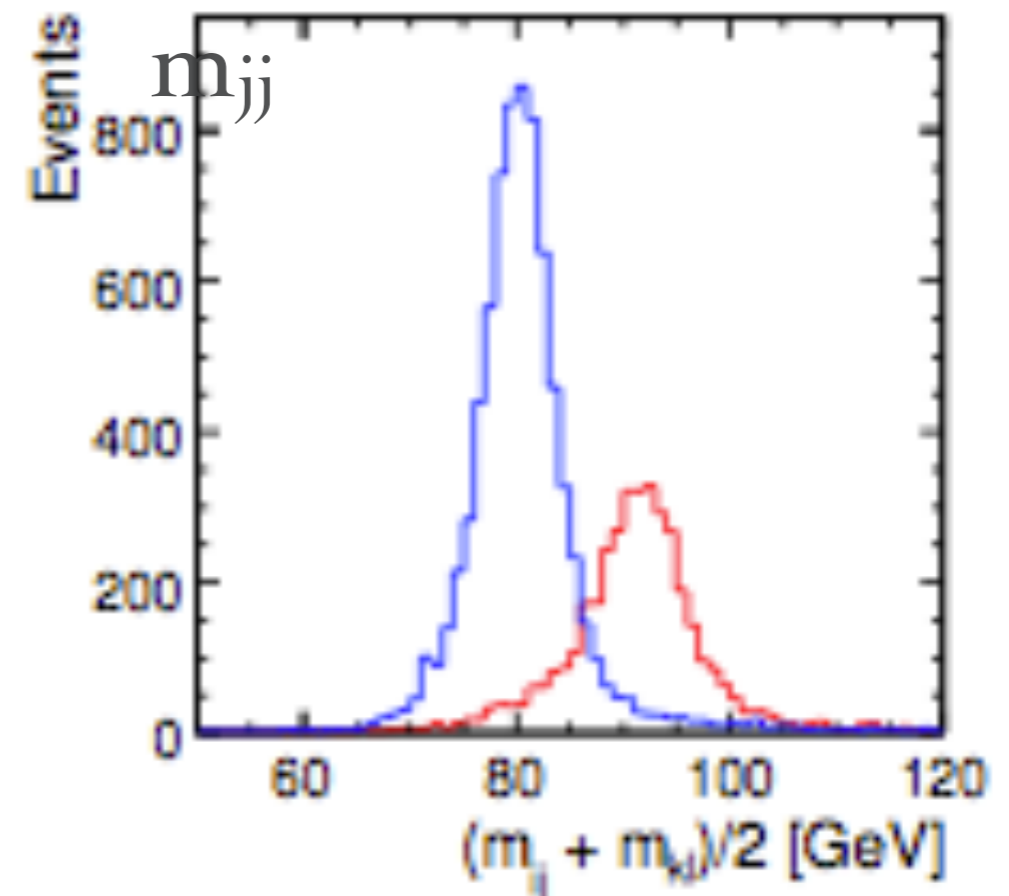
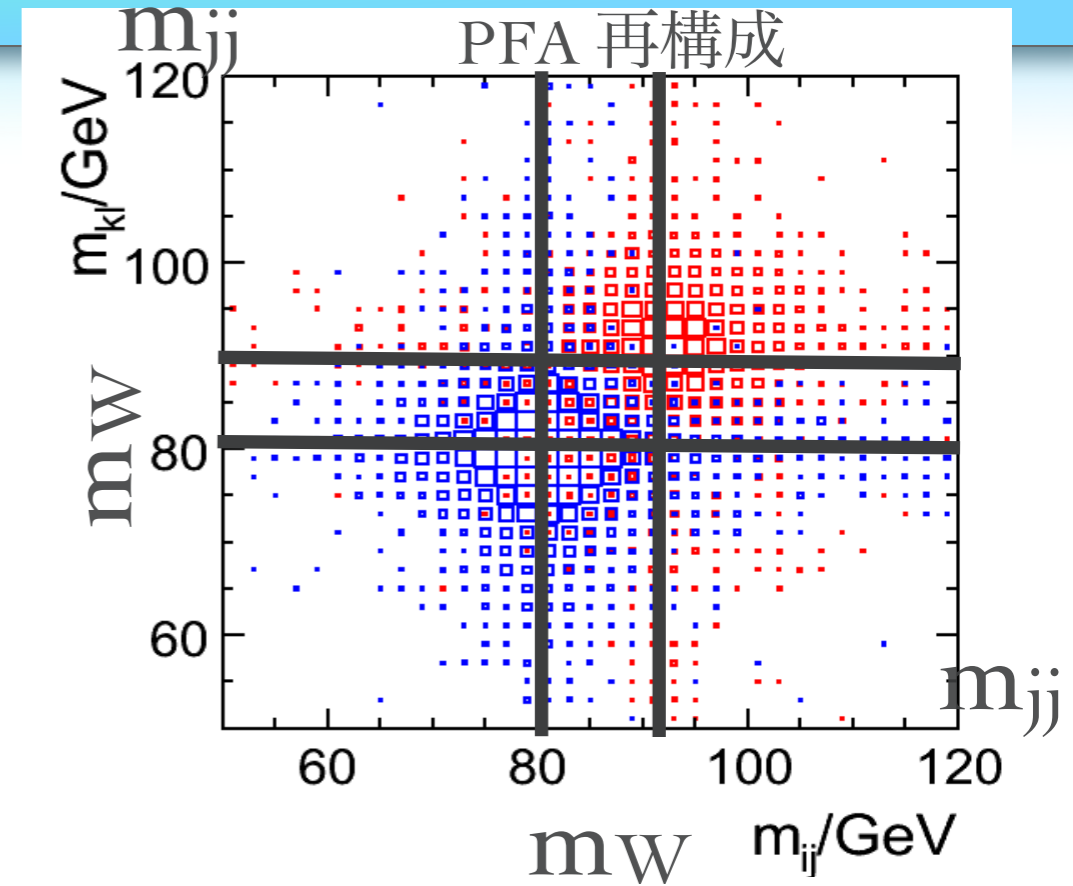
2%

3%



PFA performance

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- HCAL for KoL
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track length vs

for electrons

Ncherenkov light

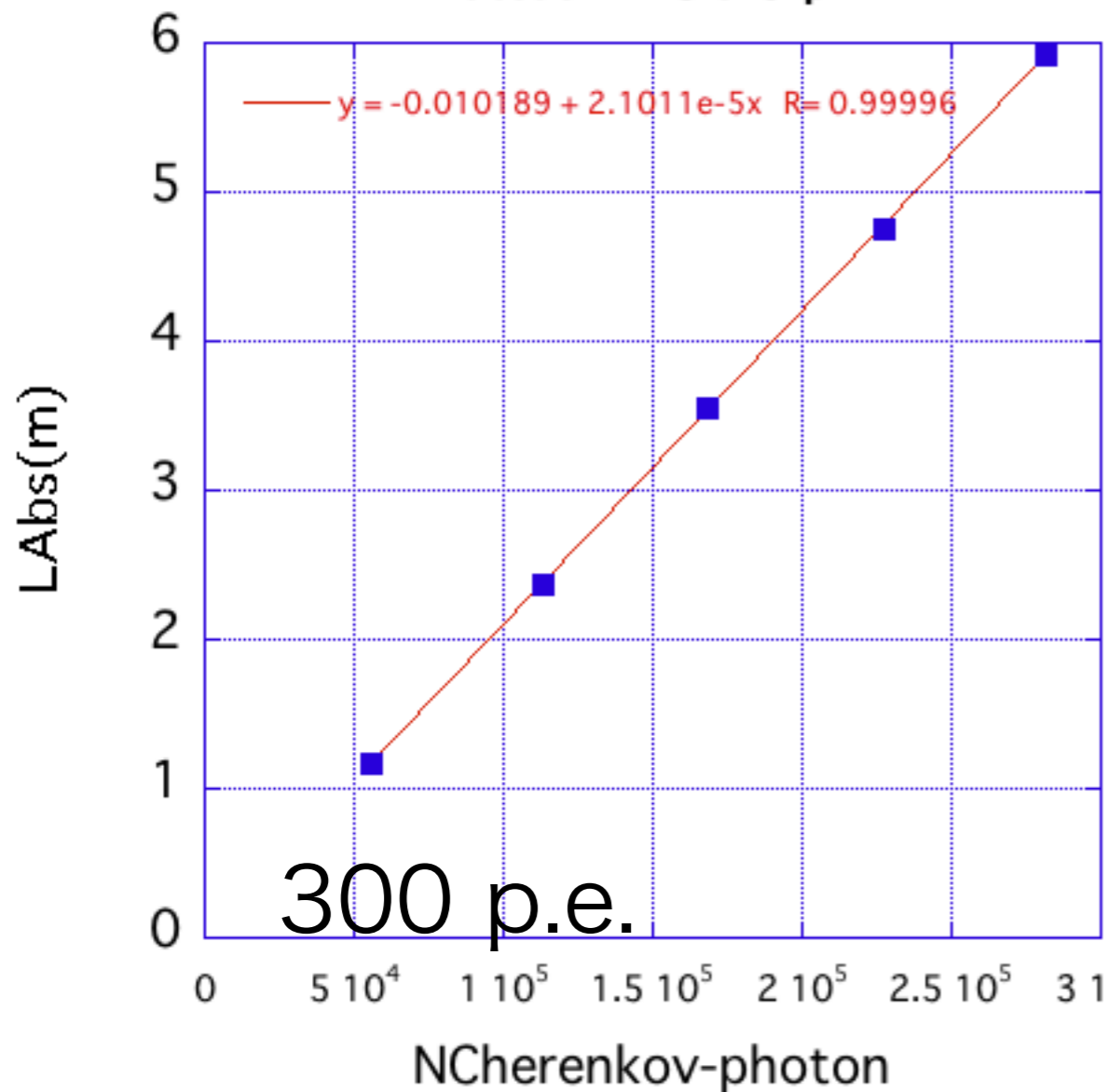
- nice correlation : we can use track length instead of number of cherenkov light which consume CPU power for simulation

—■— LAbs

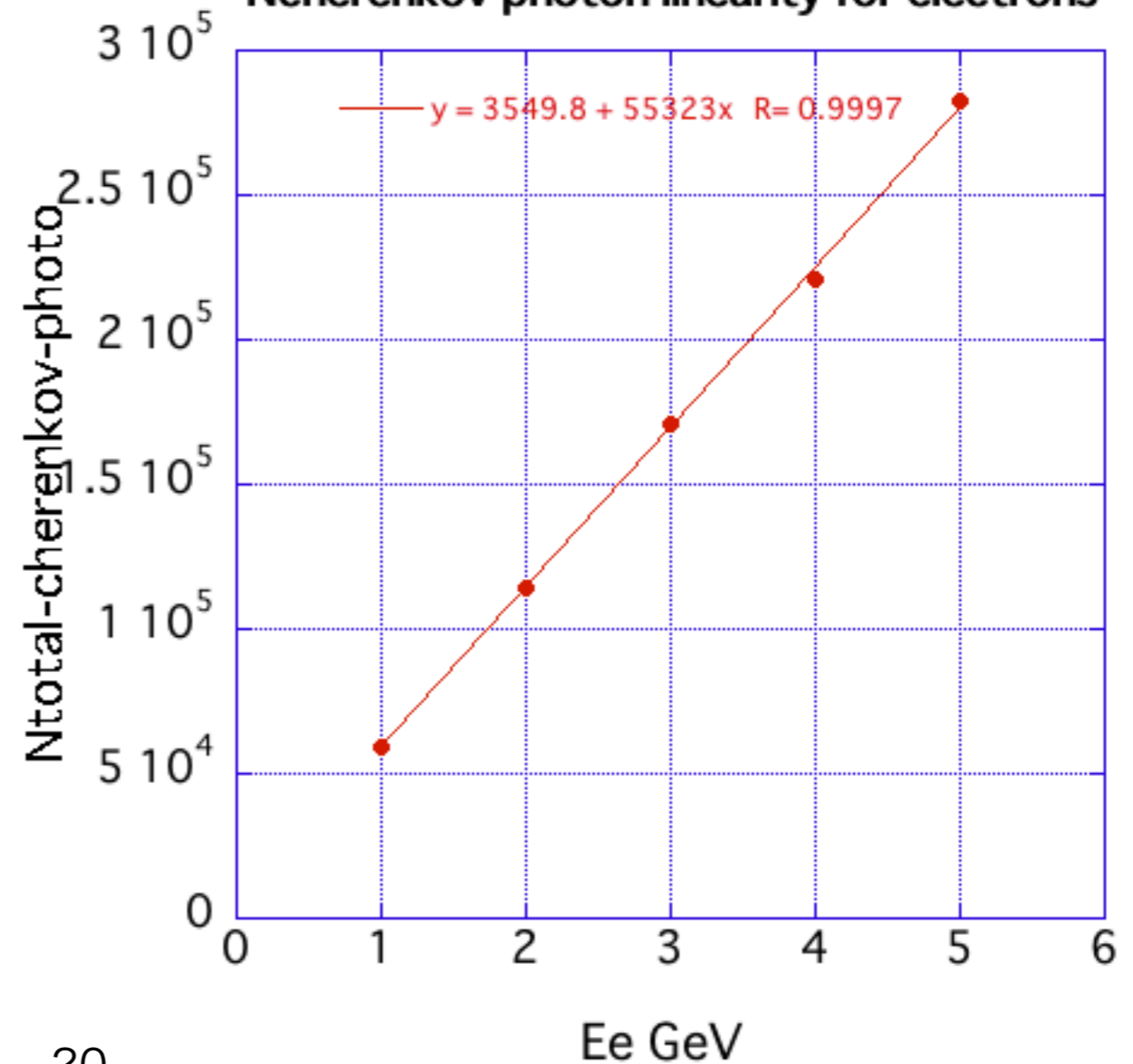
—●— Ntotal-cherenkov-photo

track length

electron-LABSvsNCHph

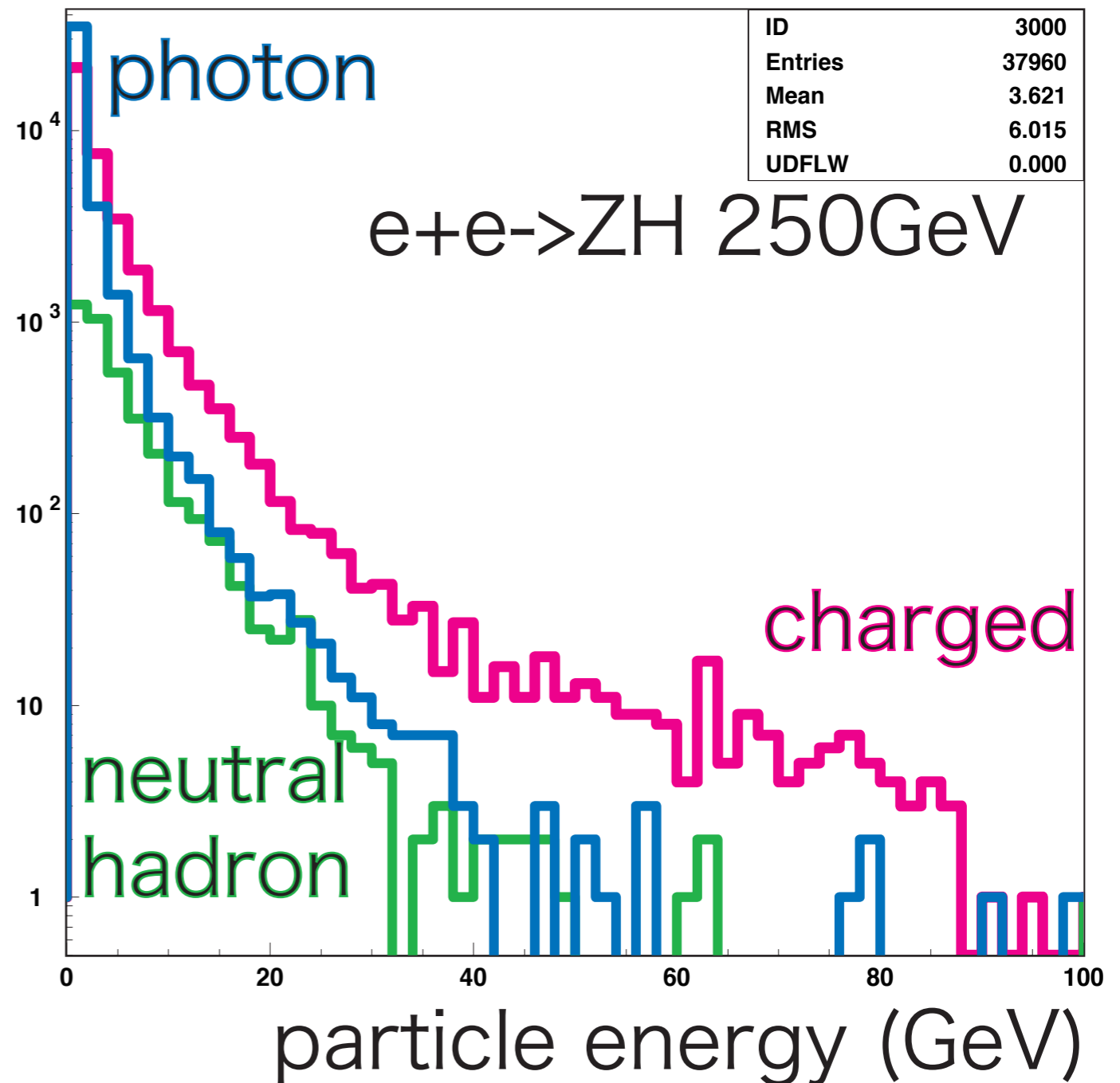


Ncherenkov photon linearity for electrons



particle energy in jet

- particle energy distribution
- $E < 10$ GeV dominating



PbWO₄



Scintillation properties of lead tungstate (PbWO₄) crystals:

Density (g.cm ⁻³)	8.28
Radiation length (cm)	0.92
Decay constant (ns)	6/30
Emission peak (nm)	440/530
Light yield (% that of NaI:TI)	0.5
Melting point (°C)	1123
Hardness (Mho)	/
refractive Index	2.16
Hygroscopicity	none
Cleavage	101