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# **Neutrino Lecture 1**

Minerba Betancourt, Fermilab 22 July 2019

### Outline

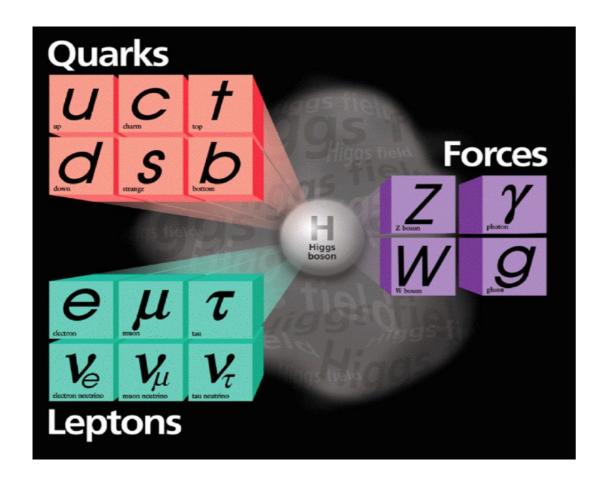
- Today:
  - A quick history of neutrinos
  - Basic of week interactions
  - Neutrino oscillations
- Tomorrow:
  - How we produce a neutrino beam
  - Neutrino interactions
  - Examples of nuclear effects in neutrino interactions
  - Cross section measurements



### Where do neutrinos come from?

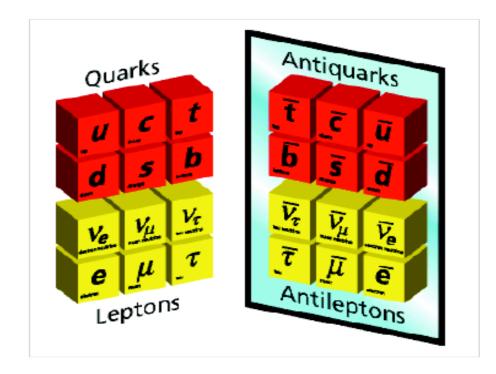
- Neutrinos are the most common matter particles in the universe **10**<sup>-1</sup>  $\overline{v}_{e} e^{-} in mb)$ **10**<sup>-4</sup> **SuperNova 10**<sup>-7</sup> Reactor 个 **10**<sup>-10</sup> Cross Section ( $\frac{v}{v_{e}}e^{-13}$ ) 10<sup>-13</sup> Accelerator Terrestrial Cosmic **Atmospheric** Solar **10**<sup>-25</sup> **Big Bang 10**<sup>-28</sup> **10**<sup>-31</sup> **10**<sup>10</sup> 10<sup>12</sup> 10<sup>8</sup> **10**<sup>16</sup> 10<sup>2</sup> **10**<sup>4</sup> **10<sup>6</sup> 10**<sup>14</sup> **10<sup>-2</sup> 10**<sup>18</sup> **10**<sup>-4</sup> 1 Neutrino Energy (eV)
- Concentrating on few neutrino interactions relevant to neutrino oscillation at the few GeV region
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#### **The Standard Model of Elementary Particles**



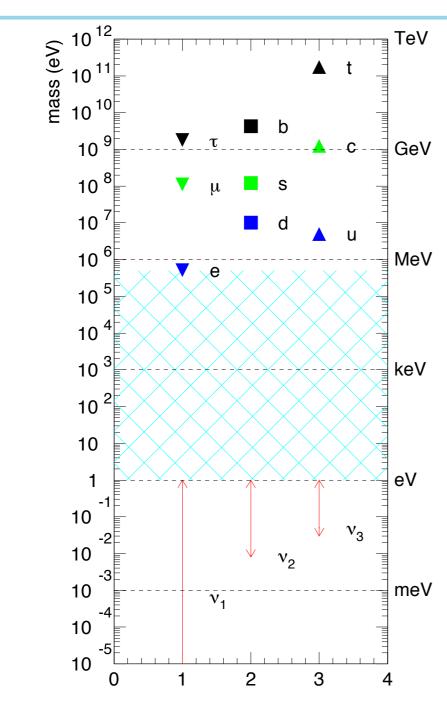
- Is the standard model complete?
  - Neutrino in the Standard Model has no mass
  - However neutrino mass has been observed, and it is much smaller than all other particles

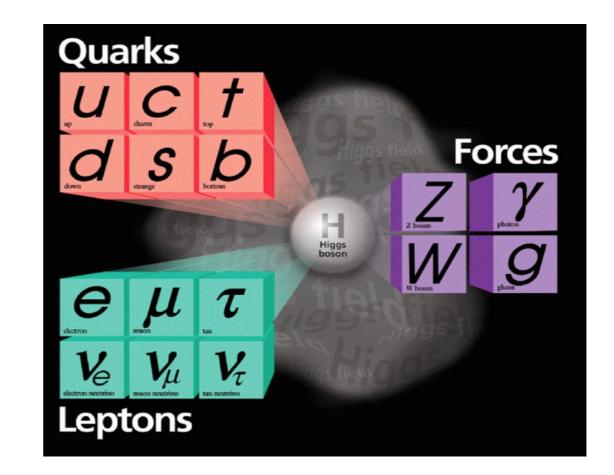
- Theory about fundamental ingredients of matter and how they interact with each other
- Everything known in this world is made of these (and the mirror images)





#### **Neutrinos have mass**



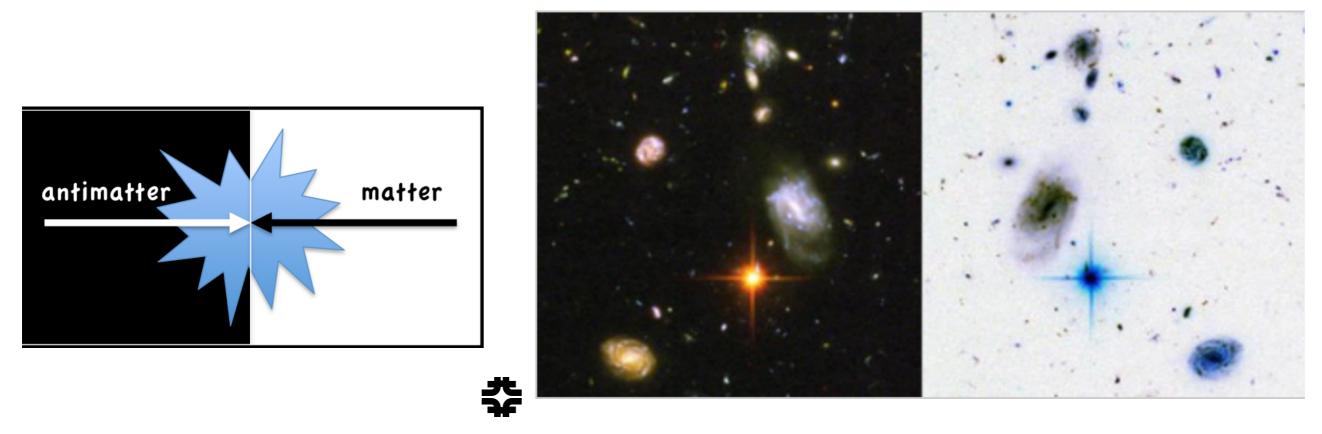


- Why is there such large gap between neutrino masses and quark masses?
- Why do quarks and leptons exhibit different behavior?
- What is the absolute mass of neutrino?



### What is the symmetry between matter and antimatter?

- Physics theorize that the big bang created equal amounts of matter and antimatter
- When corresponding particles of matter and antimatter meet, they annihilate one another



- But somehow we are still here and antimatter, for most part, has vanished
- Neutrinos could help to explain why the universe has more matter than antimatter!



#### How did we discover neutrinos?

- Radioactivity: Nucleus emits particle due to nuclear instability
- While studying the beta decay, the energy did not seem to be conserved in beta decay?
  - We know energy is always conserved
  - Energy can neither be created nor destroyed only can be transformed into a different form
- In 1930, Pauli postulated the neutrino

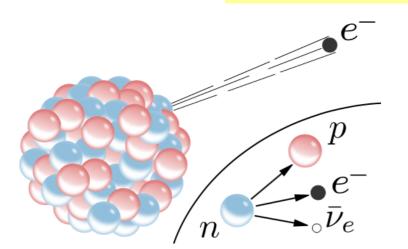
Dear Radioactive Ladies and Gentlemen,

I have done a terrible thing.

I have postulated a particle that cannot be detected



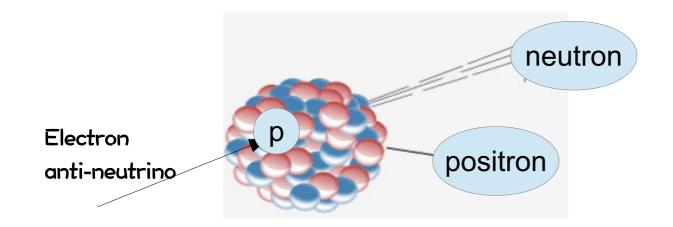




### **The Discovery of Anti-Neutrino (1956)**

- Artificially produced neutrinos from nuclear reactors
  - Emits around 10 trillion anti-neutrinos per cm<sup>2</sup>/s
- Inverse Beta decay

$$\bar{\nu}_e + p \rightarrow e^+ + n$$



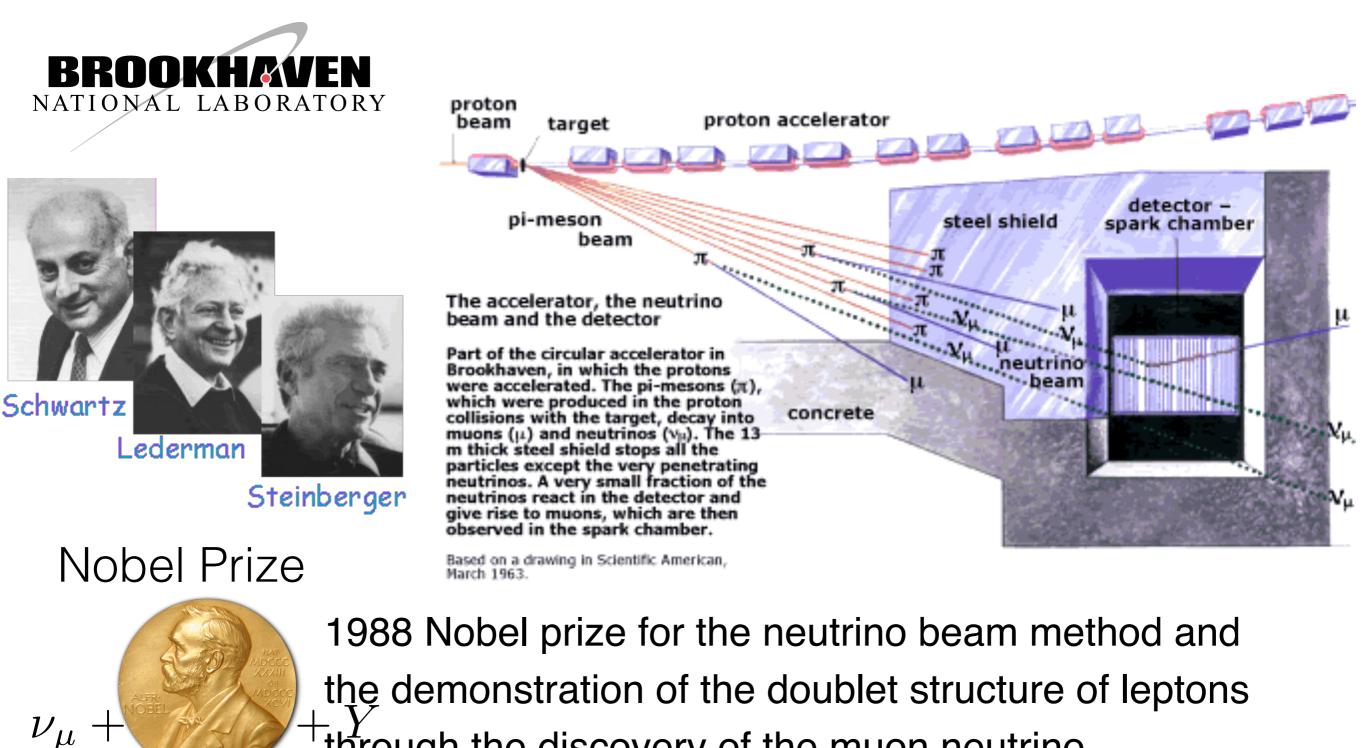
#### 1995 Nobel Prize







#### The Discovery of the Muon Neutrino



1962

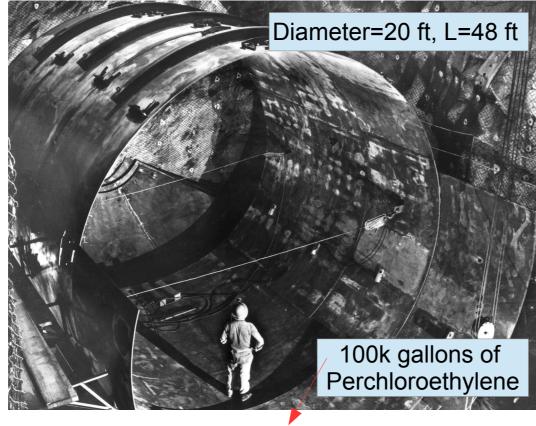
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through the discovery of the muon neutrino

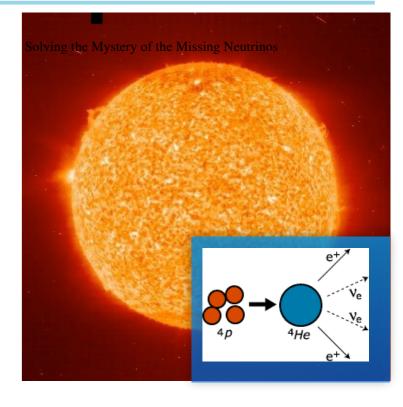


### **The Solar Neutrino Problem (1968)**

- Nuclear reactions in the core of the sun produce Ve
- In 1968, Ray Davis's HomeStake experiment measured the Ve that arrives at earth using a huge tank of cleaning fluid solar neutrino+chlorine atom->electron+argon atom



Cleaning fluid



#### 2002 Nobel Prize



• Davis published the first results indicating that only 1/3 of the neutrinos were observed, i.e. the solar neutrino problem



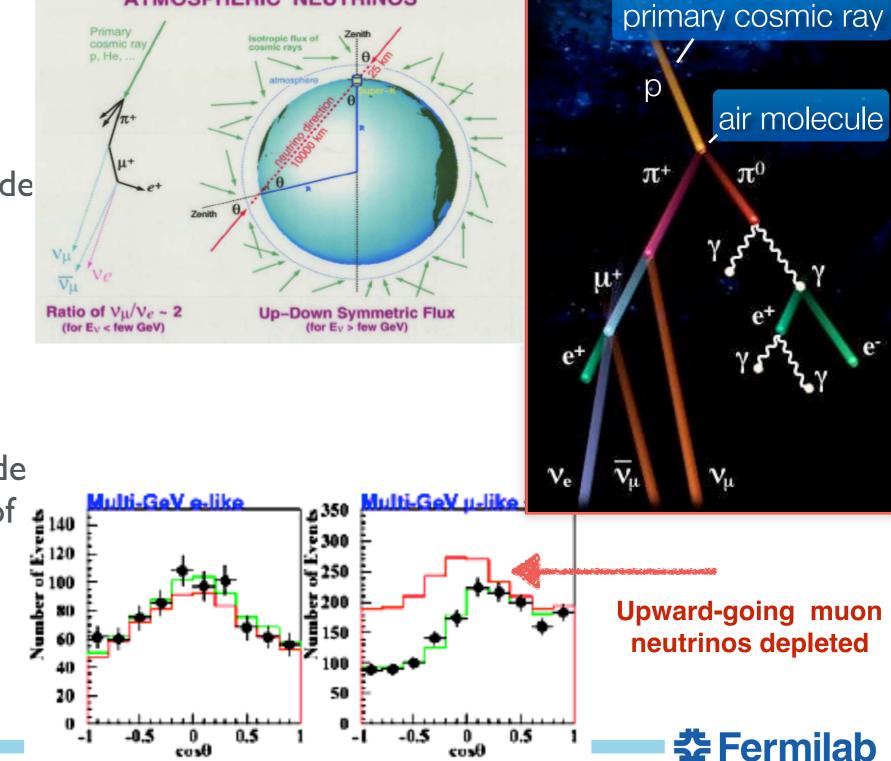
### **The Atmospheric Neutrino Anomaly**

- Cosmic rays hit the earth isotropically
- People expected:

 $\frac{\Phi_{\nu_{\mu}}(Up)}{\Phi_{\nu_{\mu}}(Down)} = 1$ 

 However, Super-Kamiokande found

 $\frac{\Phi_{\nu_{\mu}}(Up)}{\Phi_{\nu_{\mu}}(Down)} = 0.54 \pm 0.04$ 



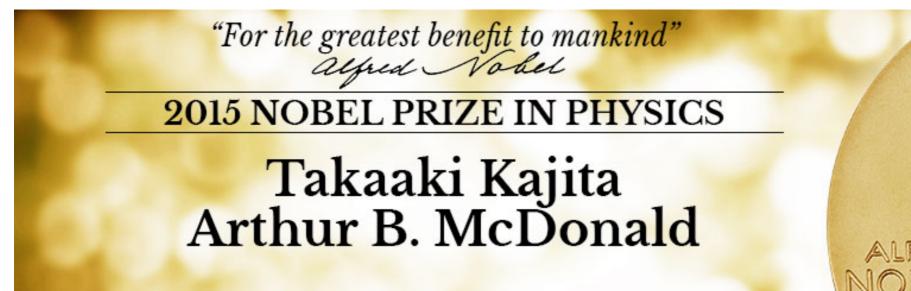
cost

ATMOSPHERIC NEUTRINOS

cost

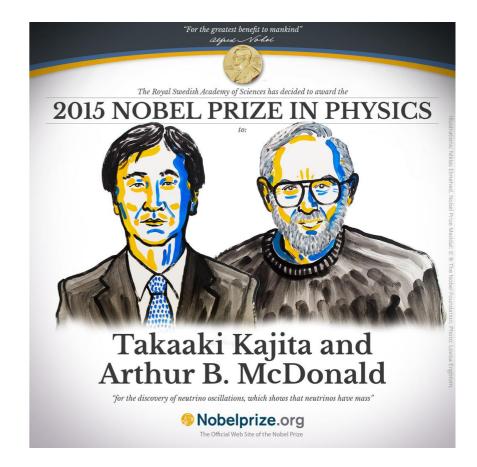
 In 1998 Super-Kamionkande announces the discovery of neutrino oscillation

#### **2015 NOBEL PRICE in PHYSICS**



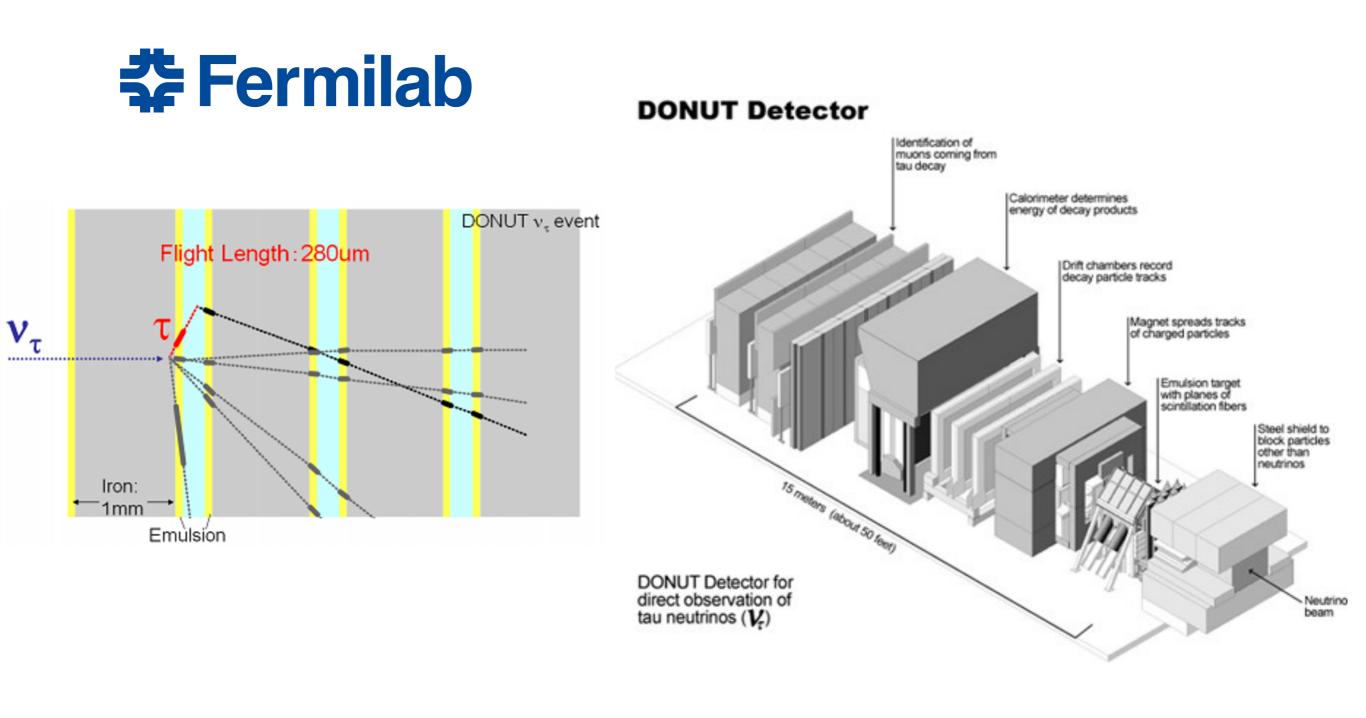
"for the discovery of neutrino oscillations, which shows that neutrinos have mass"







#### **Discovery of Tau Neutrino (2000)**



 $\nu_{\tau} + N \rightarrow \tau + X$ 

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#### Weak-Isospin Eigenstates, mass eigenstates and mixing

- In the SM, there is a weak Isospin Iw that is conserved until the Higgs develops a nonzero vacuum expectation value
- Particles are given the following lw assignments

$$\frac{I_{W3}}{\overset{+1}{}}_{0} \begin{pmatrix} W^{+} \\ W^{0} \\ -1 \end{pmatrix}, \quad \frac{I_{W3}}{\overset{+1/2}{}}_{-1/2} \begin{pmatrix} v_{Le}^{0} \\ e_{L}^{0} \end{pmatrix}, \quad \begin{pmatrix} v_{L\mu}^{0} \\ \mu_{L}^{0} \end{pmatrix}, \quad \begin{pmatrix} v_{L\tau}^{0} \\ \tau_{L}^{0} \end{pmatrix}, \quad \frac{I_{W3}}{\overset{0}{}}_{R} = \mu_{R}^{0} = \tau_{R}^{0}$$

The W – lepton coupling conserves  $I_W$ .

• With

$$\ell_L^0 = \begin{bmatrix} e_L^0 \\ \mu_L^0 \\ \tau_L^0 \end{bmatrix} = \begin{bmatrix} \ell_{Le}^0 \\ \ell_{L\mu}^0 \\ \ell_{L\tau}^0 \end{bmatrix} \quad \text{and} \quad v_L^0 = \begin{bmatrix} v_{Le}^0 \\ v_{L\mu}^0 \\ v_{L\tau}^0 \end{bmatrix} ,$$

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$$\begin{bmatrix} \tau_L^0 \end{bmatrix} \begin{bmatrix} \ell_{L\tau}^0 \end{bmatrix} \begin{bmatrix} \nu_{L\tau}^0 \end{bmatrix}$$

#### **The Lagrangian**

- When the lepton masses are turned on, the charged lepton weak-isosping eigenstates are linear combinations of the charged lepton mass eigenstates

$$\ell_{L,R}^{0} = A_{L,R}\ell_{L,R}$$

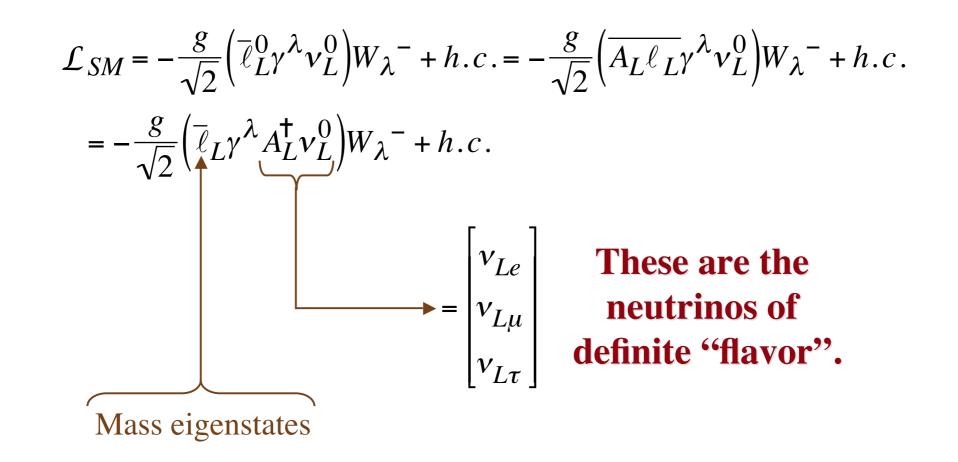
$$\int_{L,R} Column vectors including the 3 generations$$

$$\ell = \ell_{L} + \ell_{R} = \begin{bmatrix} e \\ \mu \\ \tau \end{bmatrix}$$
These are the familiar mass eigenstates.

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#### **The Lagrangian**



• The interaction is written in terms of the charged lepton mass eigenstates, but not the neutrino mass eigenstates



All mass eigenstates  

$$\mathcal{L}_{SM} = -\frac{g}{\sqrt{2}} \left( \overline{\ell}_L \gamma^{\lambda} A_L^{\dagger} v_L^0 \right) W_{\lambda}^{-} + h.c. = -\frac{g}{\sqrt{2}} \left( \overline{\ell}_L \gamma^{\lambda} A_L^{\dagger} B_L v_L \right) W_{\lambda}^{-} + h.c.$$
This is the leptonic mixing matrix  $U$ 

Explicitly –

$$\mathcal{L}_{SM} = -\frac{g}{\sqrt{2}} \sum_{\substack{\alpha=e,\mu,\tau\\i=1,2,3}} \left( \overline{\ell}_{L\alpha} \gamma^{\lambda} U_{\alpha i} v_{Li} W_{\lambda}^{-} + \overline{v}_{Li} \gamma^{\lambda} U_{\alpha i}^{*} \ell_{L\alpha} W_{\lambda}^{+} \right)$$

 $\bullet$  We can use this form of the SM IvW interaction to derivate the probability for neutrino oscillation

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### **Standard Model Neutrino Interactions**

• Lagrangian for electroweak interactions:

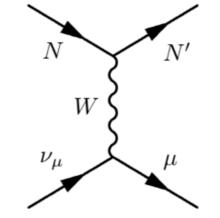
$$L_{\text{int}} = i \frac{g}{\sqrt{2}} \Big[ j_{\mu}^{(+)} W^{\mu} + j_{\mu}^{(-)} W^{\mu+} \Big] + i \Big[ g \cos \theta_W j_{\mu}^{(3)} - g' \sin \theta_W j_{\mu}^{(Y/2)} \Big] Z^{\mu} + i \Big[ g \sin \theta_W j_{\mu}^{(3)} + g' \cos \theta_W j_{\mu}^{(Y/2)} \Big] A^{\mu}$$

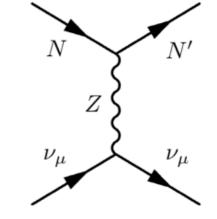
- First term: charged current interactions (W<sup>+</sup>,W<sup>-</sup> exchange)
- Second term: neutral current interactions (Z<sup>0</sup> exchange)
- Third term: electromagnetic interactions (photon exchange)
- Electron charge:  $e = g \sin \theta_W = g' \cos \theta_W$

Charged Current (CC) interactions via a W-boson

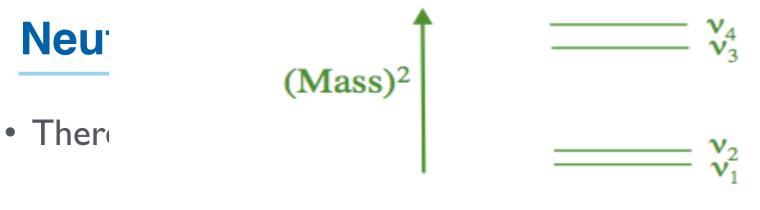
Neutral Current (NC) interactions via a Z-boson

Neutrinos only couple to W and  $Z^0$ 









Mass  $(v_i) = m_i$ 

When W<sup>+</sup> 
$$\rightarrow \ell_{\alpha}^{+} + \nu_{\alpha}^{+}$$
,  
 $\ell_{\alpha}^{+} + \nu_{\alpha}^{+}$ ,

the produced neutrino state  $|v_{\alpha}\rangle$  is

Neutrino of flavor 
$$\alpha$$
  $\stackrel{i}{\downarrow}$   $\stackrel{i}{\downarrow}$   $\stackrel{i}{\downarrow}$  Neutrino of definite mass  $m_i$   
Leptonic Mixing Matrix



- Interaction eigenstate (produced by weak interactions)
- Mass eigenstate (eigenstate of the Hamiltonian)

$$\mathcal{H}|\nu_i\rangle = E_i|\nu_i\rangle$$

$$\nu_{\alpha} = \sum_i U_{\alpha i}\nu_i \quad \text{Field } \psi \text{ annihilates state } |\psi\rangle$$

$$|\nu_{\alpha}\rangle = \sum_{i=1}^n U_{\alpha i}^*|\nu_i\rangle \quad |\nu_{\alpha}\rangle = \sum_i \nu_i^{\dagger}U_{\alpha i}^*|0\rangle = \sum_i U_{\alpha i}^*|\nu_i\rangle$$

• After producing a neutrino in a well defined flavor, it evolves like

$$|\nu_{\alpha}(t)\rangle = \sum_{i=1}^{n} U_{\alpha i}^{*} |\nu_{i}(t)\rangle$$

• We also detect it in a defined flavor, so the amplitude we measure is

$$A_{\alpha\beta}(t) = \langle \nu_{\beta} | \nu_{\alpha}(t) \rangle$$

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$$A_{\alpha\beta}(t) = \langle \nu_{\beta} | \nu_{\alpha}(t) \rangle$$
$$A_{\alpha\beta}(t) = \sum_{i=1}^{n} \sum_{j=1}^{n} U_{\alpha i}^{*} U_{\beta j} \langle \nu_{j} | \nu_{i}(t) \rangle$$

• The hamiltonian is related to the time evolution operator, so

$$|\nu_i(t)\rangle = e^{-iE_it}|\nu_i(0)\rangle$$

• Neutrinos are relativistic

$$E_i = \sqrt{p_i^2 + m_i^2} \simeq p + \frac{m_i^2}{2E}$$

$$A_{\alpha\beta}(t) = \langle \nu_{\beta} | \nu_{\alpha}(t) \rangle = U_{\alpha i}^* U_{\beta j} \langle \nu_{j} | e^{-iE_{i}t} | \nu_{i} \rangle$$

$$= e^{-ipt} U_{\alpha i}^* U_{\beta i} \exp\left(-i\frac{m_i^2 t}{2E}\right)$$

Isolated an overall phase Got lazy and stopped writing the sums Used orthogonality condition:  $\langle \nu_j | \nu_i \rangle = \delta_{ij}$ 



• Let's isolate another overall phase

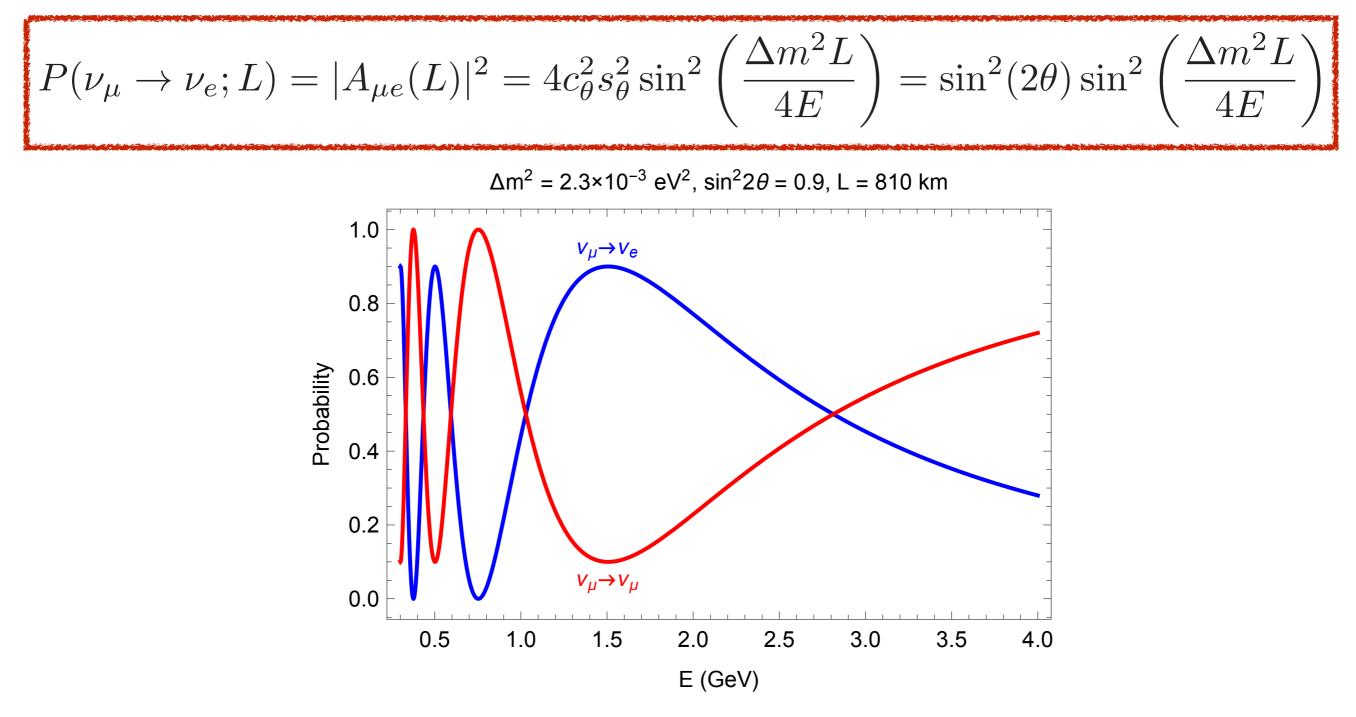
$$A_{\alpha\beta} = e^{-i(pt+m_1^2t/2E)}U_{\alpha i}^*U_{\beta i}\exp\left(-i\frac{\Delta m_{i1}^2t}{2E}\right)$$

• To make it simpler, consider two neutrinos (say  $\nu_e$  and  $\nu_{\mu)}$ 

$$U = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$$

$$P(\nu_{\mu} \to \nu_e; L) = |A_{\mu e}(L)|^2 = 4c_{\theta}^2 s_{\theta}^2 \sin^2\left(\frac{\Delta m^2 L}{4E}\right) = \sin^2(2\theta)\sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$





The probability of producing  $v_{\mu}$  and detect  $v_{e}$  really *oscillates*!



• For the three families there are 3 mixing angles, 2 mass splitting and one complex phase

$$U = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix}$$

- The components of U involve  $\theta_{13,}\theta_{23,}$   $\theta_{12,}\Delta^2 m_{13,}\Delta^2 m_{23,}\Delta^2 m_{12,}\delta$ 



#### **Probability of v\_{\mu}—>v\_e Oscillation in Vacuum**

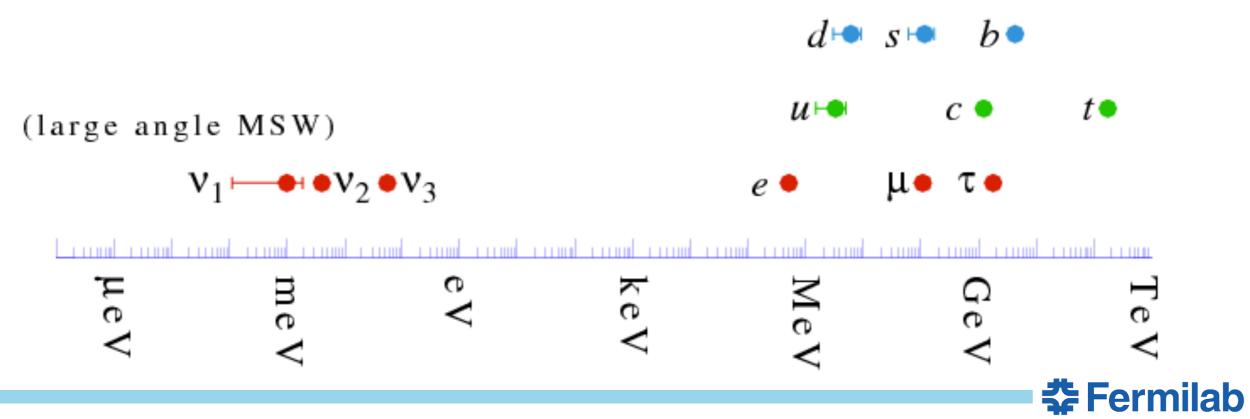
$$P(\nu_{\mu} \to \nu_{e}) = s_{23}^{2} sin^{2} 2\theta_{13} sin^{2} \frac{\Delta m_{31}^{2} L}{4E} + c_{13}^{2} c_{23}^{2} sin^{2} 2\theta_{12} sin^{2} \frac{\Delta m_{21}^{2} L}{4E} + 8c_{13}^{2} s_{13} c_{12} s_{12} s_{23} c_{23} sin \frac{\Delta m_{21}^{2} L}{4E} sin \frac{\Delta m_{31}^{2} L}{4E} cos(\frac{\Delta m_{32}^{2} L}{4E} + \delta) - 2s_{12}^{2} s_{23}^{2} sin^{2} 2\theta_{13} sin \frac{\Delta m_{21}^{2} L}{4E} sin \frac{\Delta m_{31}^{2} cos \frac{\Delta m_{32}^{2} L}{4E} + 4c_{13}^{2} s_{12}^{2} s_{13} s_{23} (s_{23} s_{13} s_{12} - 2c_{12} c_{23} cos \delta) sin^{2} \frac{\Delta m_{21}^{2} L}{4E}$$
(2.8)



#### Is there a reason behind the masses and mixing?

$$V_{MNS} \sim \begin{pmatrix} 0.8 & 0.5 & \textbf{0.2} \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix} \qquad V_{CKM} \sim \begin{pmatrix} 1 & 0.2 & ... & ... \\ 0.2 & 1 & 0.01 \\ ... & 1 \end{pmatrix}$$

• Lepton mixing is very different from quark mixing

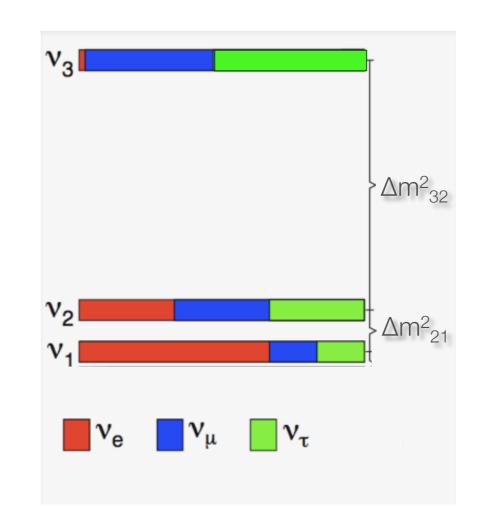


#### What do we know?

• The probability of a neutrino 
$$V_{\mu}$$
 transforming into  $V_{e}$   
Considering three generations of neutrinos, in the neutrino is with mass eigenstates through the PANS matrix. Writing is  $\begin{bmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \end{bmatrix} = U^{*} \begin{bmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \end{bmatrix}$   
• where the mixing matrix bias  $\begin{bmatrix} u_{e1} & u_{e2} & u_{e3} \\ U_{\mu} & U_{\mu} & U_{\mu2} & U_{\mu3} \end{bmatrix} = \begin{bmatrix} u_{p2} & u_{p3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\mu2} & U_{\mu2} & U_{\mu3} \\ U_{\mu2} & U_{\mu2} & U_{\mu3} \\ U_{\mu2} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} & U_{\mu3} \\ U$ 

### **Remaining Questions**

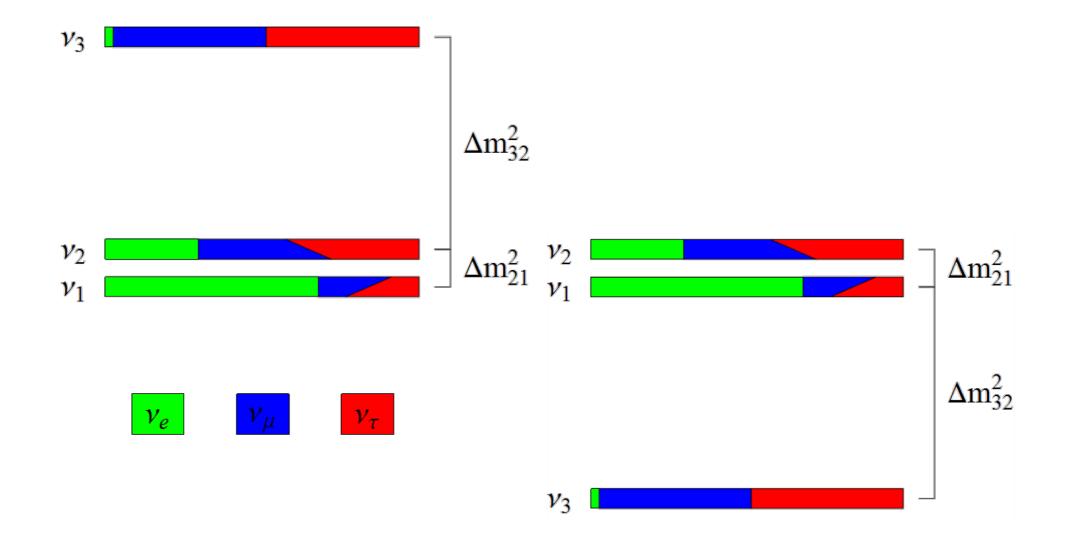
- Is there CP violation in the lepton sector?
  - May explain matter-antimatter asymmetry
- What is the mass hierarchy? (sign of  $\Delta m_{32}^2$ )
  - Important to be able to understand the reach of experiments that study whether neutrinos are their own antiparticle or not
- Is  $\theta_{23}$  maximal?
- Is there a fourth "sterile neutrino"?





### **Remaining Questions**

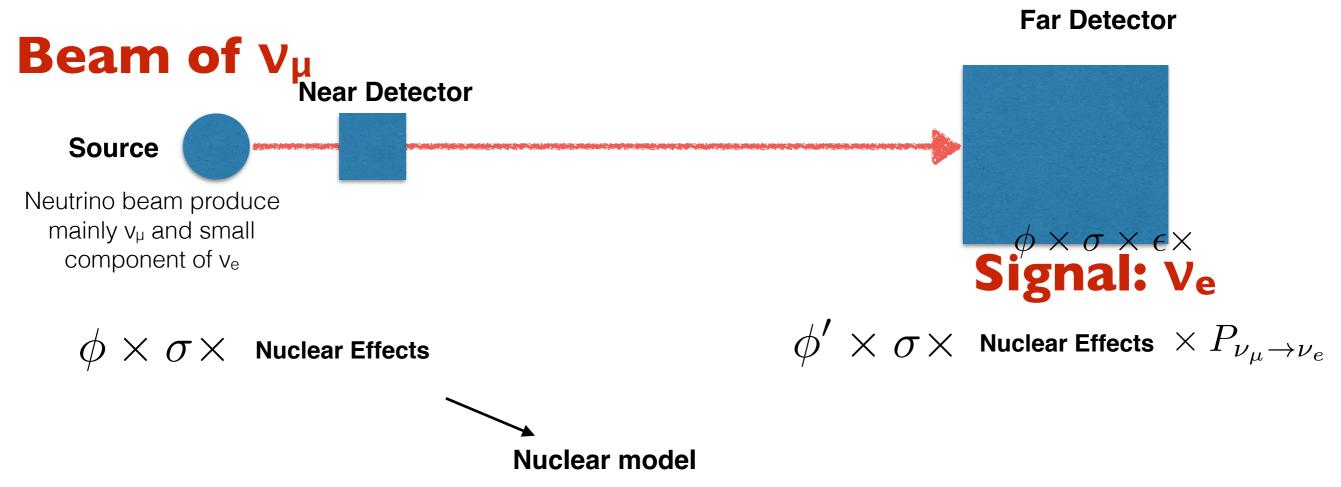
• Is the mass hierarchy "normal" or "inverted"?





### **Addressing the Remaining Questions**

- Is there CP violation in the lepton sector
- What is the mass hierarchy? (sign of  $\Delta m_{32}^2$ )

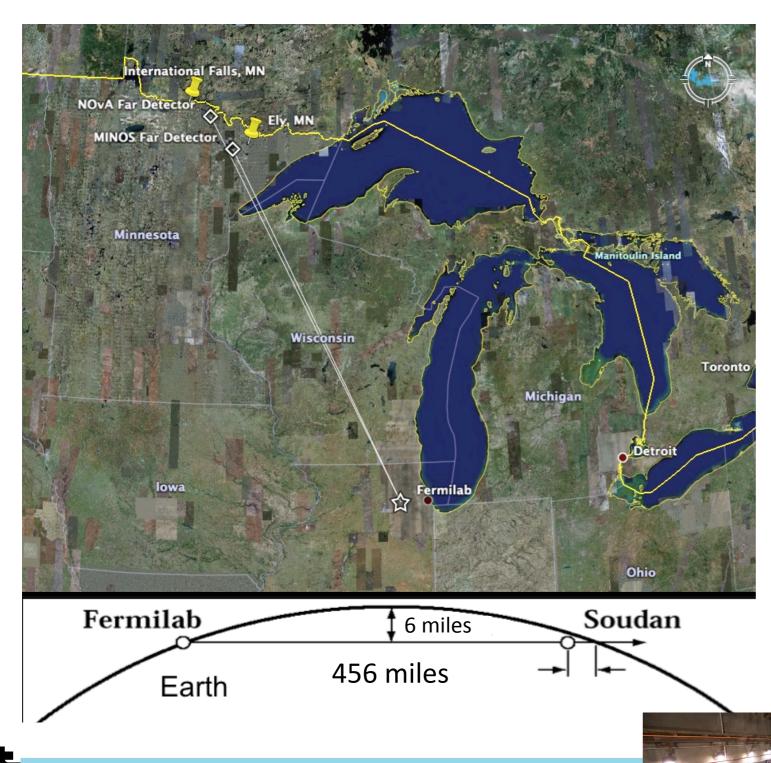


 $P[\nu_{\mu} \rightarrow \nu_{e}] \neq P[\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e}]$ ?

- Use simulations to extrapolate from near detector to far detector  $\sigma_{\nu\mu}$  >  $\sigma_{\nu e}$
- We definitely need a nuclear model to convert from produced to detected energy spectra and topologies in the near and the far detectors

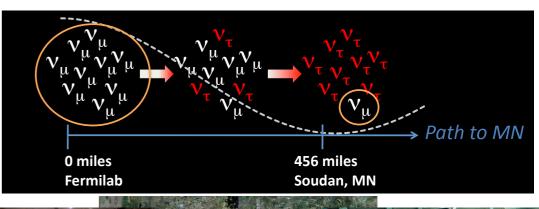


#### Where is the Far and Near Detector?



Neutrinos make the journey from Fermilab to northern Minnesota

#### Illinois Wisconsin Minnesota



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#### Long-baseline Experiments: What can we learn?

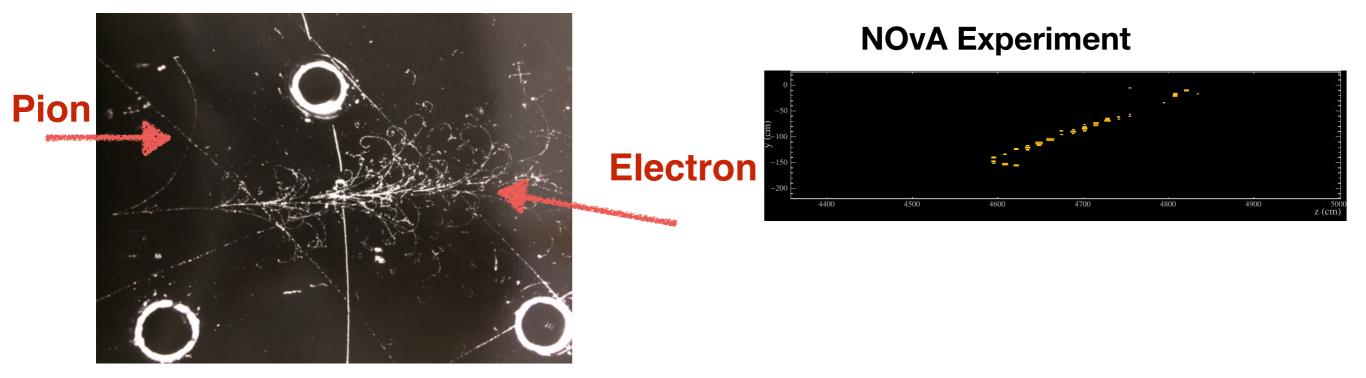
- Use a high intensity beam of neutrinos from Fermilab
- Construct detectors at far locations: MINOS+ at 735 Km (ended data-taking), NOvA at 810 km (taking data) and DUNE at 1300 km (in design)

$$P[\nu_{\mu} \rightarrow \nu_{e}] \neq P[\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e}] ?$$

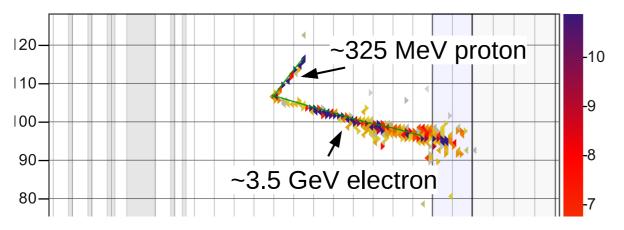


### **Electron Neutrinos Topologies at Different Detectors**

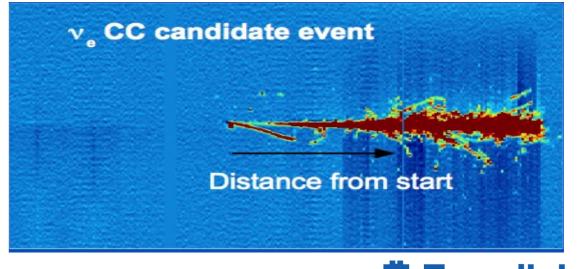
#### Electron Neutrino from Gargamelle (1978)



#### **MINERvA** Experiment



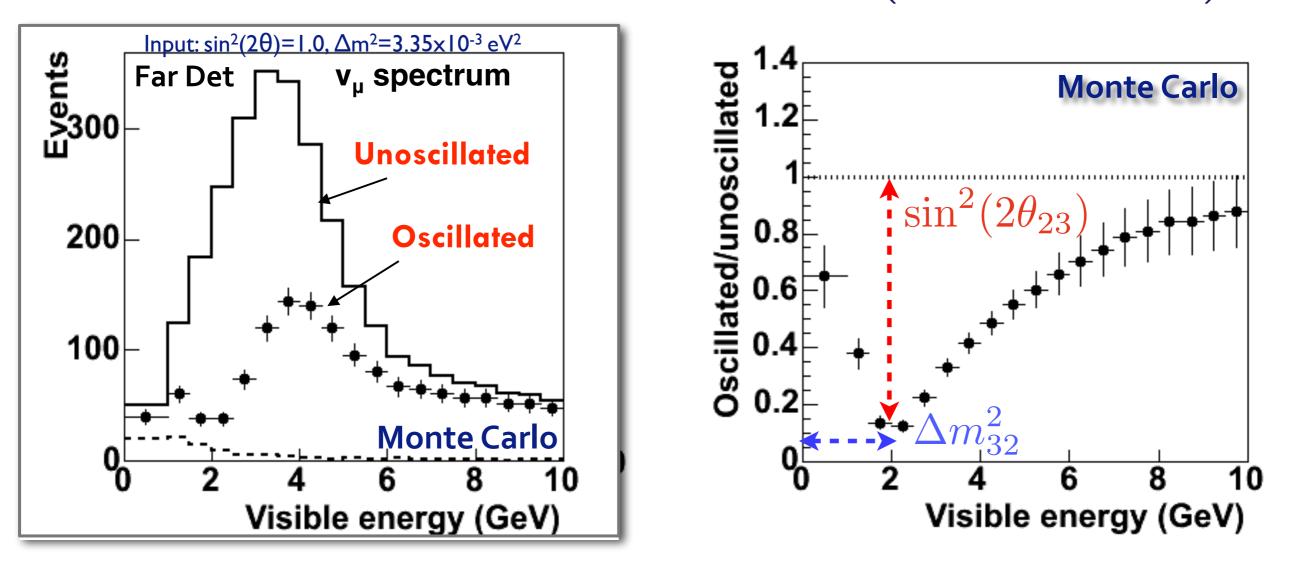
#### Electron Neutrino from Liquid Argon





### Searching for $v_{\boldsymbol{\mu}}$ Disappearance

• In long baseline experiment, we compare a prediction obtained from Near Detector data with a Far Detector measurement  $P(\nu_{\mu} \rightarrow \nu_{\mu}) \simeq 1 - \frac{1}{\sin^2(2\theta_{23})} \sin^2\left(1.267\Delta m_{32}^2 \frac{L}{E}\right)$ 

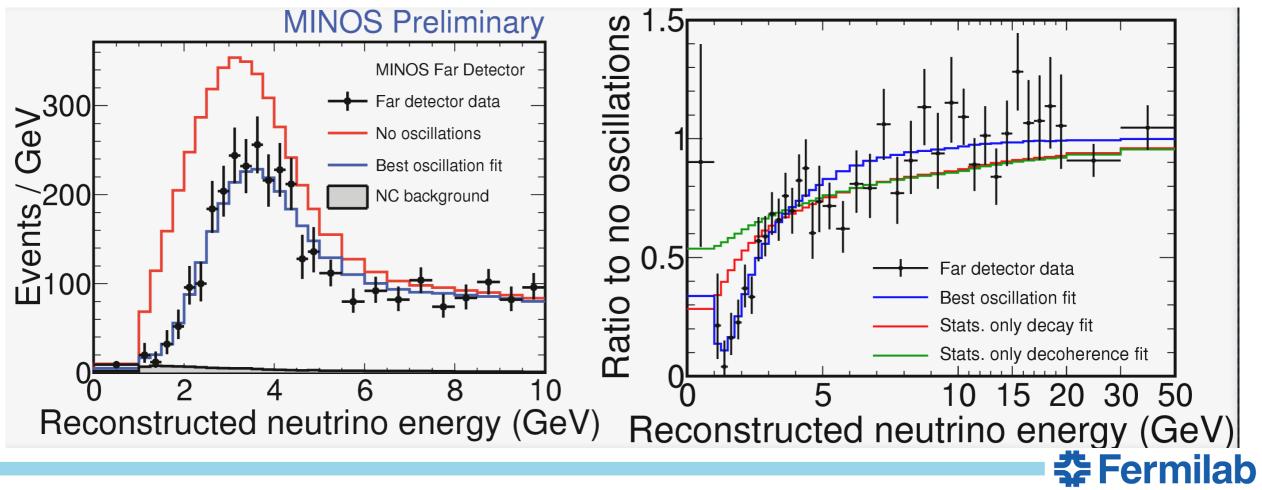




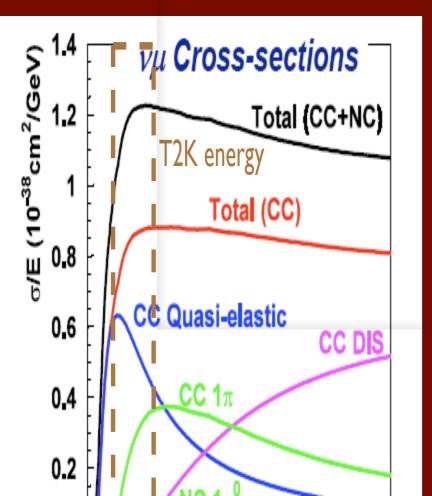
## **MINOS Experiment**

- Near and Far detectors
- Steel planes (2.54 cm), magnetized detector
- Alternating with planes of scintillator strips
  - Near detector: I ton
  - Far detector: 5.4 kton



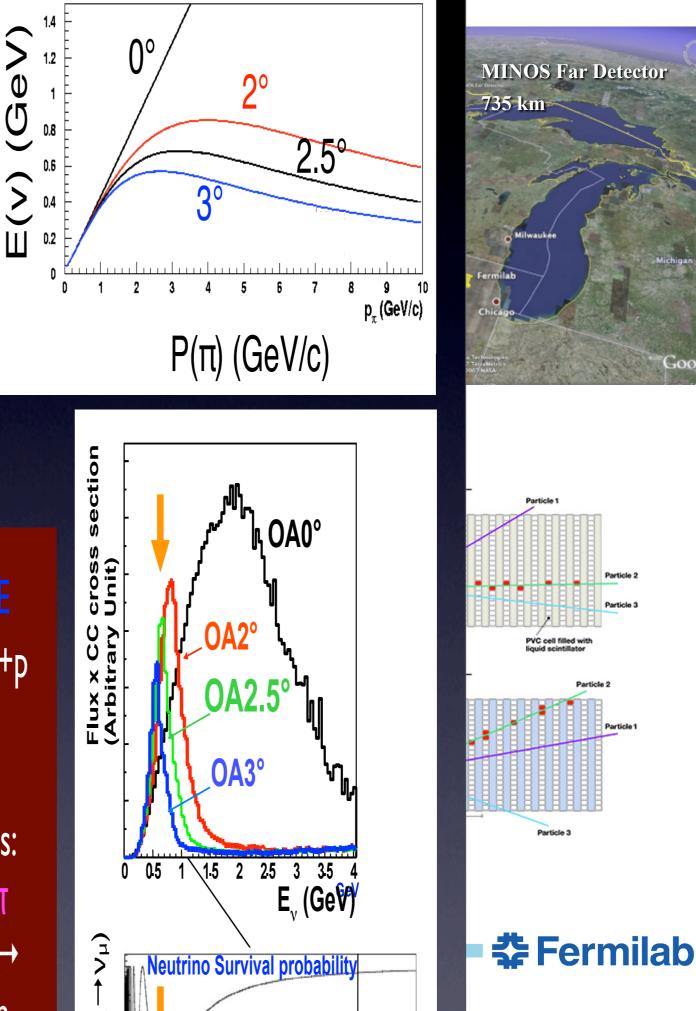


- I 2K is the first long baseline experiment using off-axis technique
- Reduced dependence of  $E_{\nu}$  from  $E_{\pi}$ 
  - Intense beam where the oscillation effect is maximum (~0.6 GeV)
  - Enhance the CCQE sample, reducing the high energy tails of the beam  $\rightarrow$  reduce the backgrounds to oscillation signal



Signal: CCQE  $V_{e(\mu)}+n \rightarrow e(\mu)+p$ 

Main backgrounds: **CCI**π, **NCI**π, π produced in DIS  $\rightarrow$ coming from high



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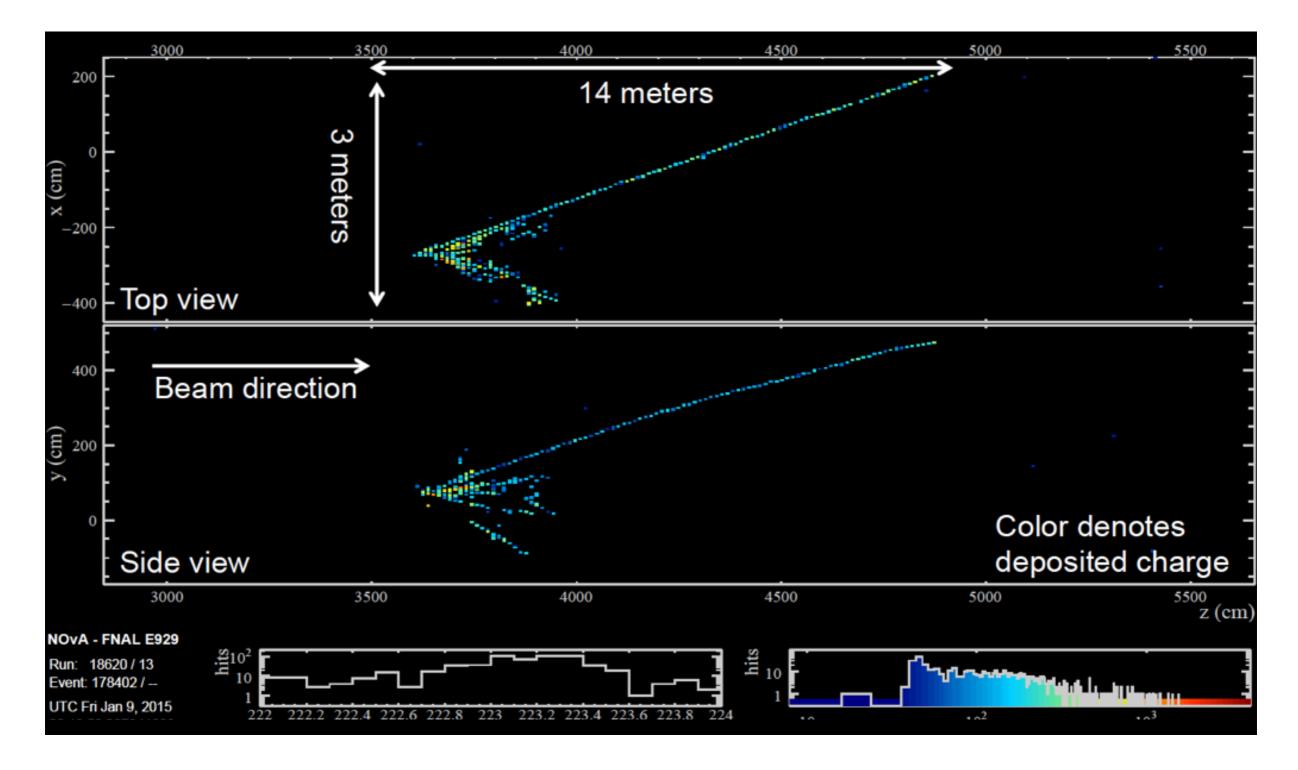
# **NOvA Experiment**





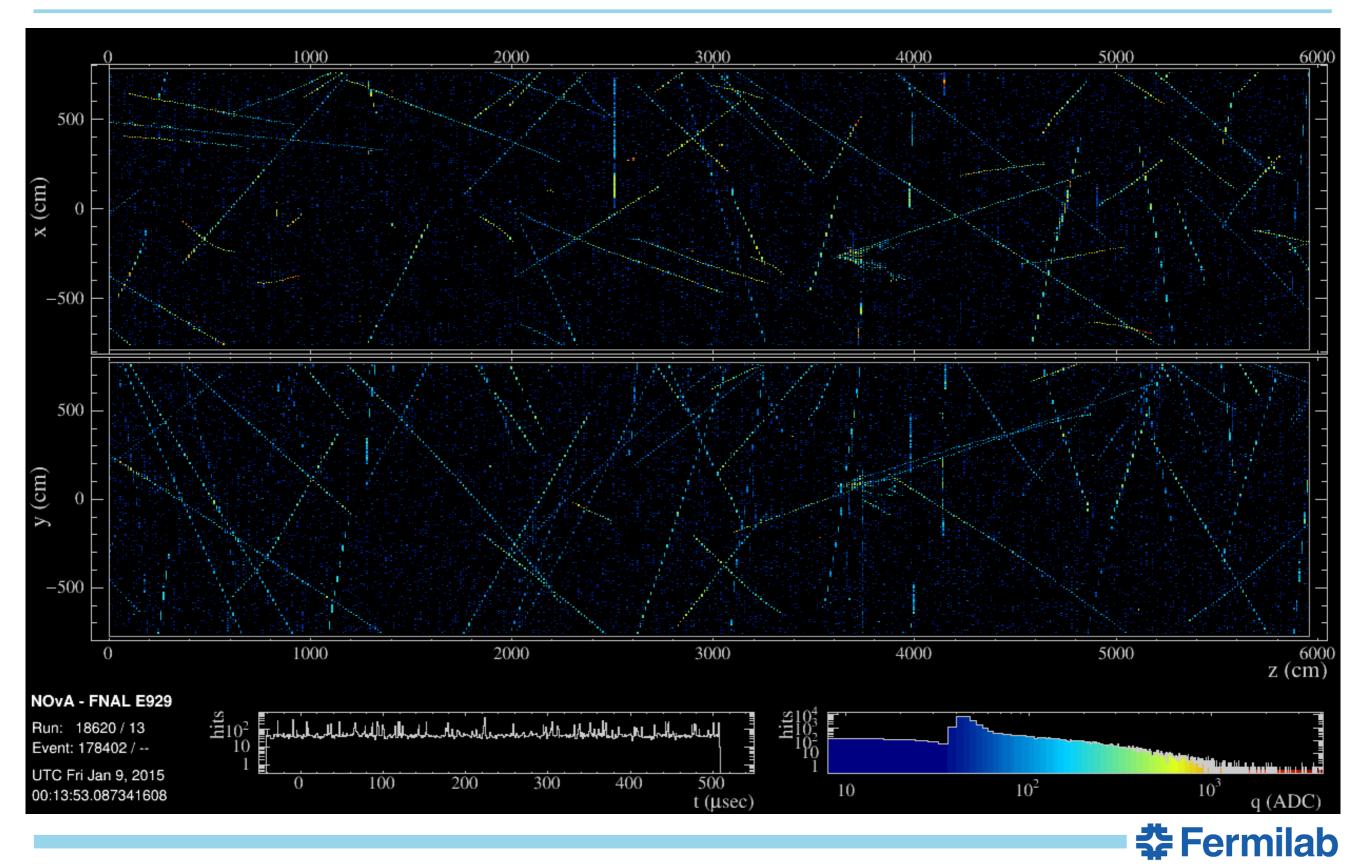


### **A Neutrino Interaction from the NOvA Experiment**





### What do we see at the NOvA Experiment?



## **NOvA Experiment**

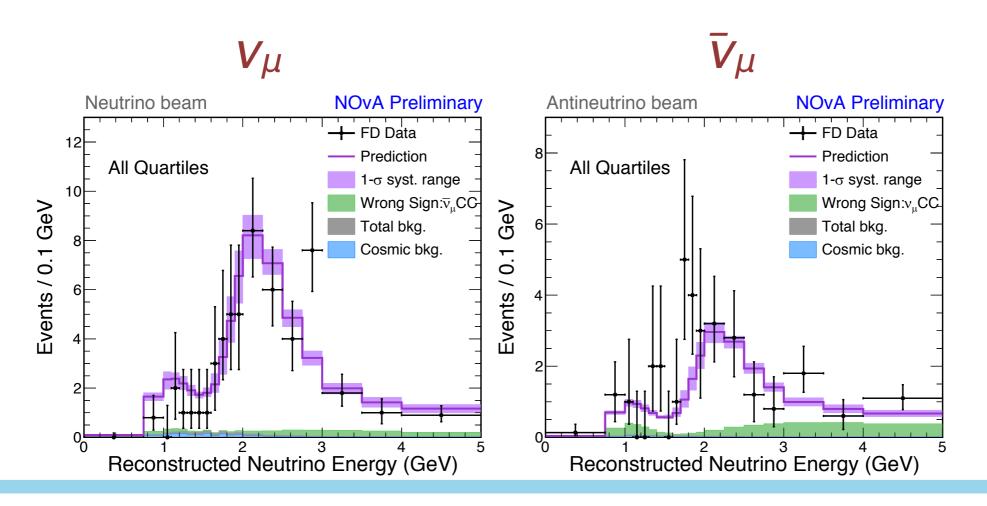
#### $V_{\mu}$

Total Observed	113
Best fit prediction	121
Cosmic Bkgd.	2.1
Beam Bkgd.	1.2
Unoscillated	730

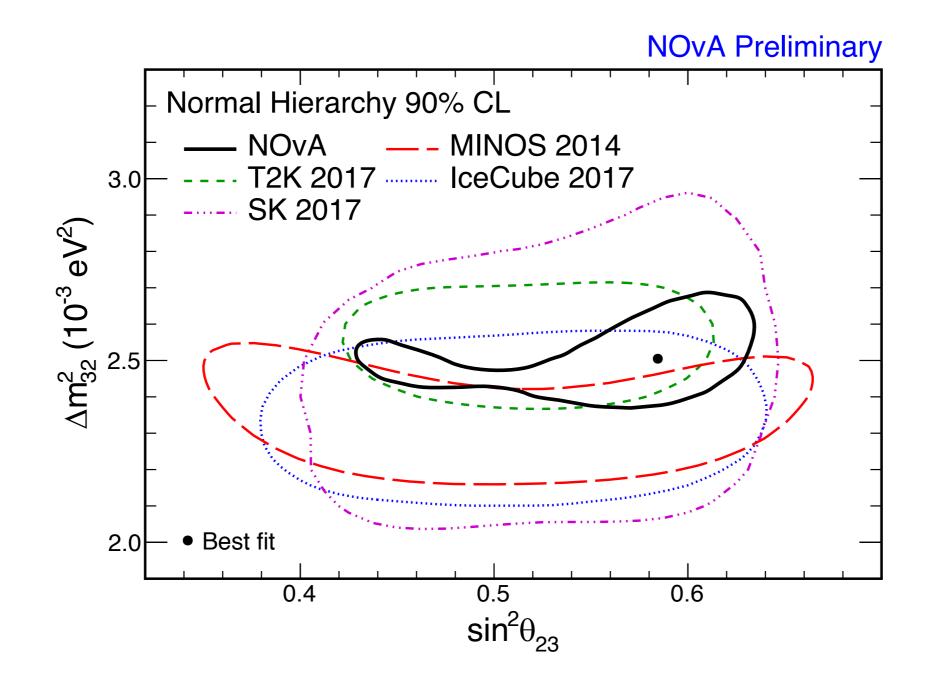
# $ar{m{V}}_{\mu}$

Total Observed	65
Best fit prediction	50
Cosmic Bkgd.	0.5
Beam Bkgd.	0.6
Unoscillated	266

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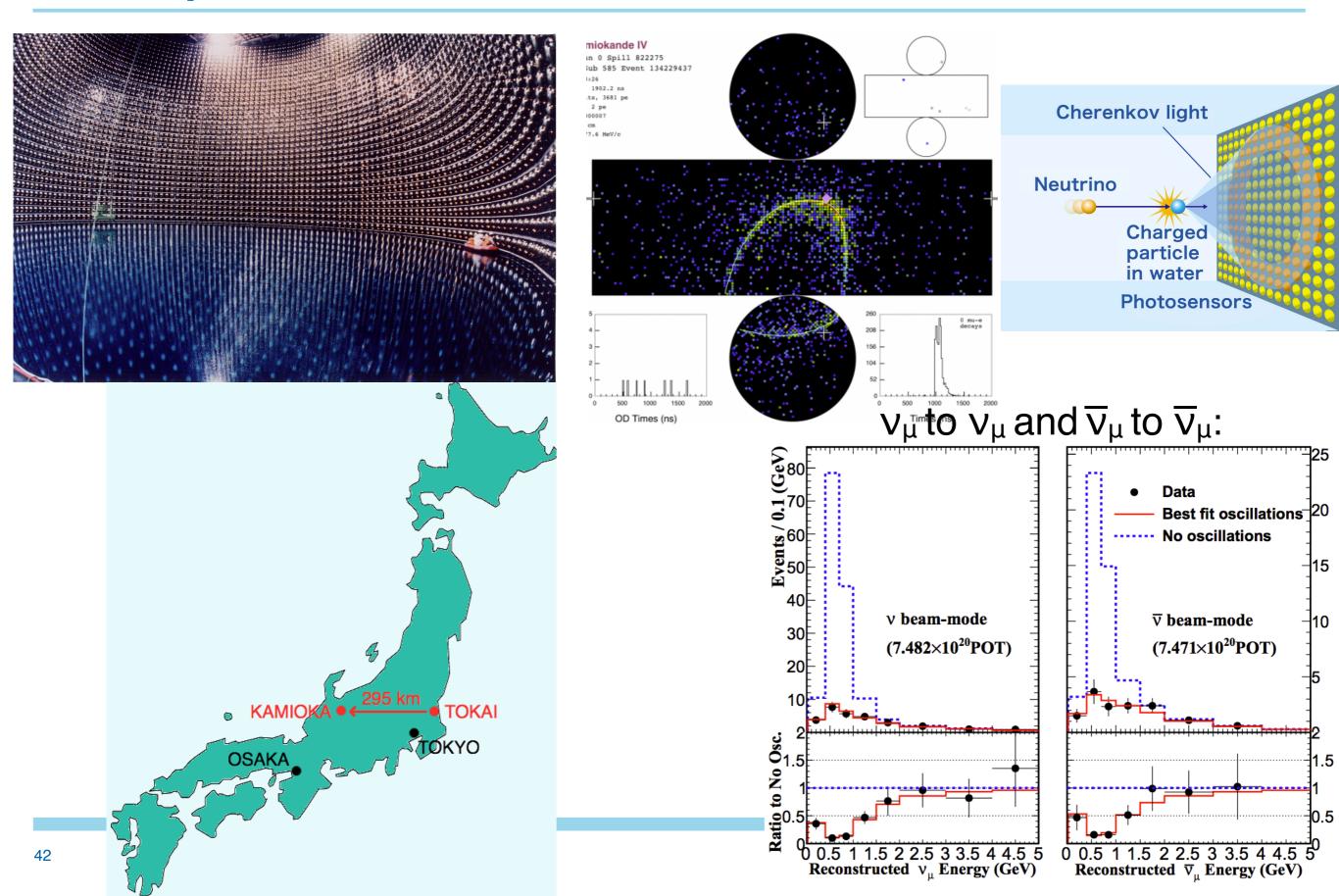


#### **Results**

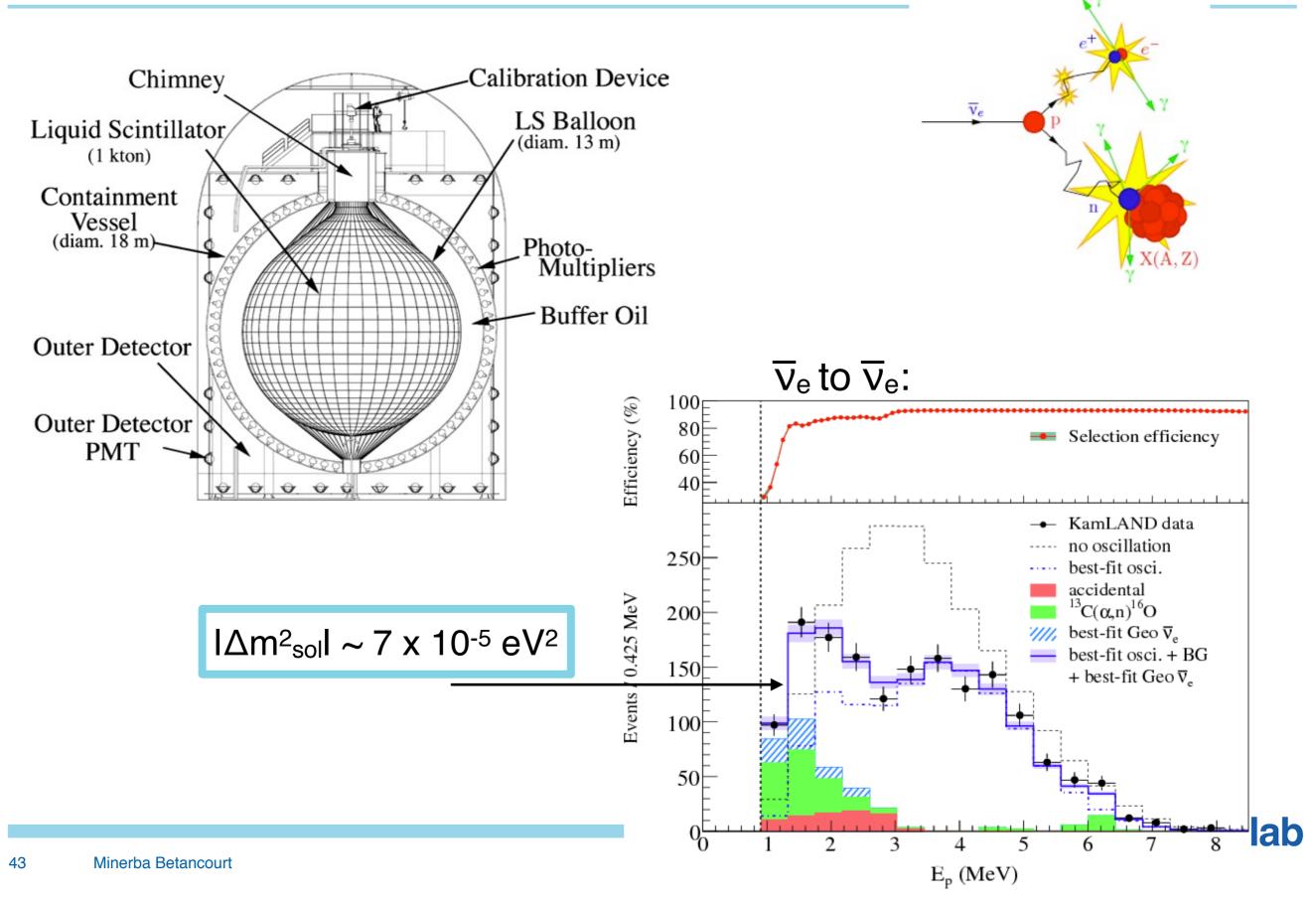


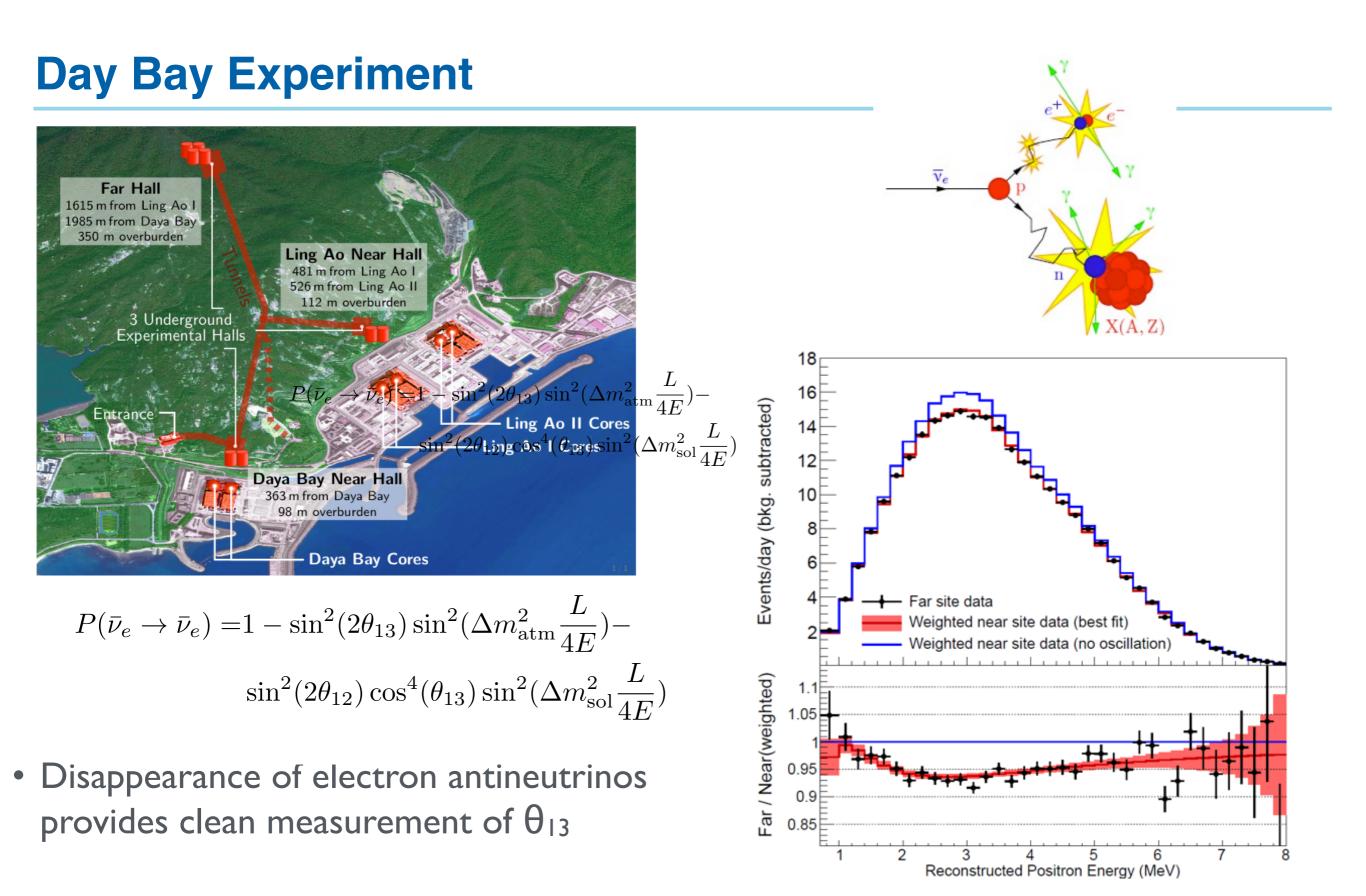


#### **T2K Experiment**



## **KamLAND Experiment**





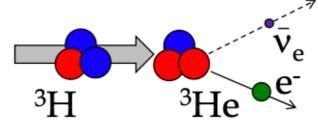
**Fermilab** 

## **Many Experiments!**



#### What about direct measurements of absolute mass of neutrinos ?

- When a neutrino is produced, some of the energy exchanged in the process should be spent by the non-zero neutrino mass
- The most sensitive observable is the electron energy spectrum from tritium decay



- This decay is sensitive to an effective "electron neutrino mass"
- Experiment measure the shape of the end-point of the spectrum, not the value of the end point 1.2

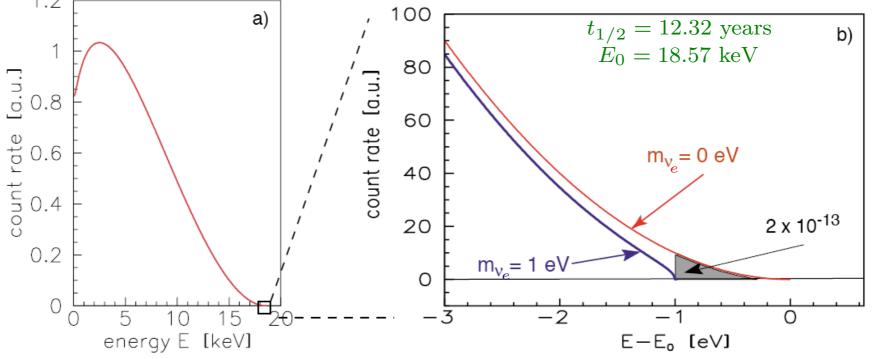


Figure 2: The electron energy spectrum of tritium  $\beta$  decay: (a) complete and (b) narrow region around endpoint  $E_0$ . The  $\beta$  spectrum is shown for neutrino masses of 0 and 1 eV.

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# **KATRIN Experiment**

- First tritium injection May 18 2018
- Commissioned the detector 2018

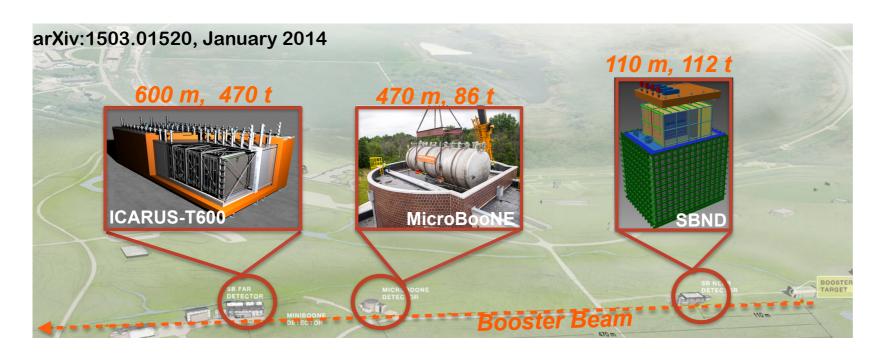


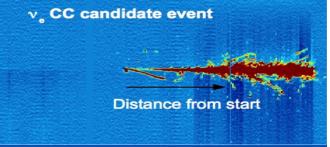
• Taking data!



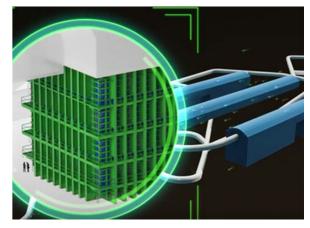
# **Short-Baseline Neutrino Program**

- Short-baseline neutrino program at Fermilab:
  - Search for a fourth type of neutrino (sterile neutrino)
  - Measure cross sections on liquid argon
  - First time multiple liquid argon detectors are putting together: understand how systematics cancel in preparation for DUNE





**DUNE (40Kton)** 

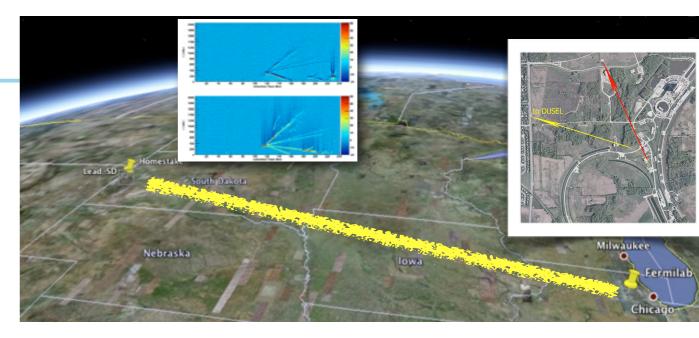


 MicroBooNE is running, SBND: commissioning is scheduled to start in 2020 and ICARUS: commissioning is scheduled to start in 2019

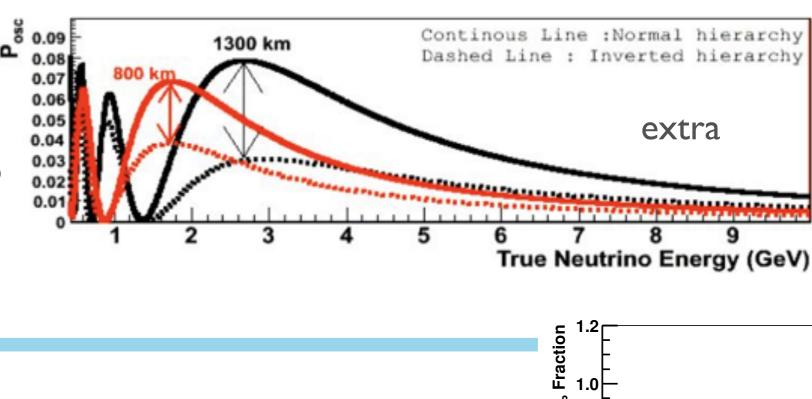


# **DUNE Experiment**

- Build new detectors farther away (1300 km) on axis
- A longer baseline provides more matter effects enhancing the asymmetry between neutrino and antineutrino appearance probabilities



- DUNE will measure the mass hierarchy and search for the  $\delta$
- DUNE will constrain  $sin^2(\theta_{13})$ ,  $sin^2(\theta_{23})$ ,  $\Delta^2 m_{13}$ ,  $\Delta 2 m_{23}$
- Has the potential to determine the  $\theta_{23}$  octant
- Physics goals include
  - Constrain the PMNS metric
  - Search for exotic physics like NSI, CPT/Lorentz violation, dimensions and sterile neutrino



#### **Back Slides**



#### **From Quarks**

• The interaction basis

$$\sum_{i=1}^{3} \bar{Q}_{Li} \not D Q_{Li} = \sum_{i=1}^{3} \frac{g}{\sqrt{2}} \left( \bar{u}_{Li} \gamma^{\mu} d_{Li} W_{\mu}^{+} + \text{h.c.} \right) + \dots$$

• The masses do not need to be diagonal

$$\sum_{i,j=1}^{3} y_{ij} \bar{Q}_{Li} \tilde{H} u_{Rj} \to \bar{\mathcal{U}}_L \cdot \mathbf{M}_u \cdot \mathcal{U}_R = \bar{\mathbf{u}}_L \cdot (V_L^u)^{\dagger} \cdot \mathbf{M}_u \cdot V_R^u \cdot \mathbf{u}_R$$
quarks in mass basis
(masses are diagonal)
$$M_u^{\text{diag}}$$

$$\sum_{i,j=1}^{3} y_{ij} \bar{Q}_{Li} H d_{Rj} \to \bar{\mathcal{D}}_L \cdot \mathbf{M}_d \cdot \mathcal{D}_R = \bar{\mathbf{d}}_L \cdot (V_L^d)^{\dagger} \cdot \mathbf{M}_d \cdot V_R^d \cdot \mathbf{d}_R$$
Fermilab

#### **From Quarks**

• The interaction basis

$$\sum_{i=1}^{3} \bar{Q}_{Li} \not D Q_{Li} = \sum_{i=1}^{3} \frac{g}{\sqrt{2}} \left( \bar{u}_{Li} \gamma^{\mu} d_{Li} W_{\mu}^{+} + \text{h.c.} \right) + \dots$$

• The mass basis

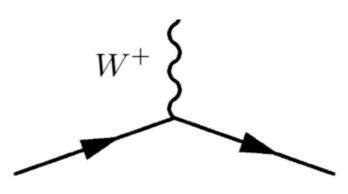
$$\sum_{i=1}^{3} \bar{Q}_{Li} \not D Q_{Li} = \frac{g}{\sqrt{2}} \left[ \bar{\mathbf{u}}_L \gamma^{\mu} (V_L^u)^{\dagger} V_L^d \mathbf{d}_L W_{\mu}^+ + \text{h.c.} \right] + \dots$$

CKM mixing matrix



### **From Quarks**

• Fermion states that have a well defined mass can have mixing under weak interactions



• Same thing happens to neutrino, but we do not know the mechanism that generates neutrino masses!

