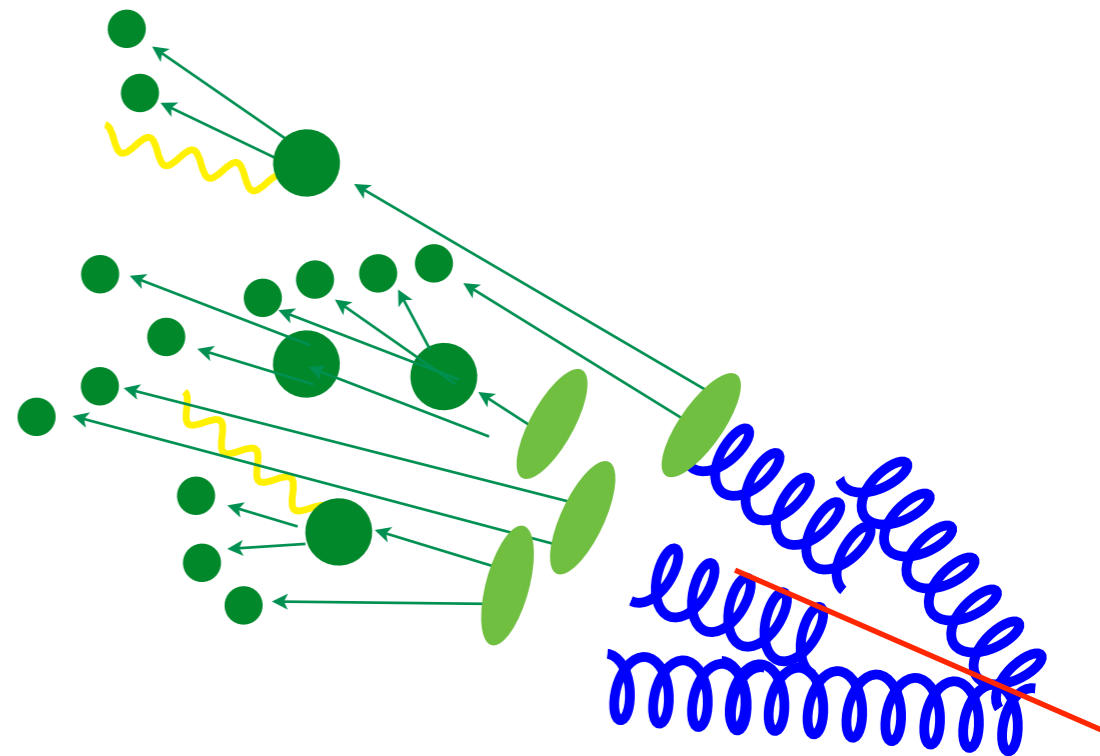


QCD physics at the LHC

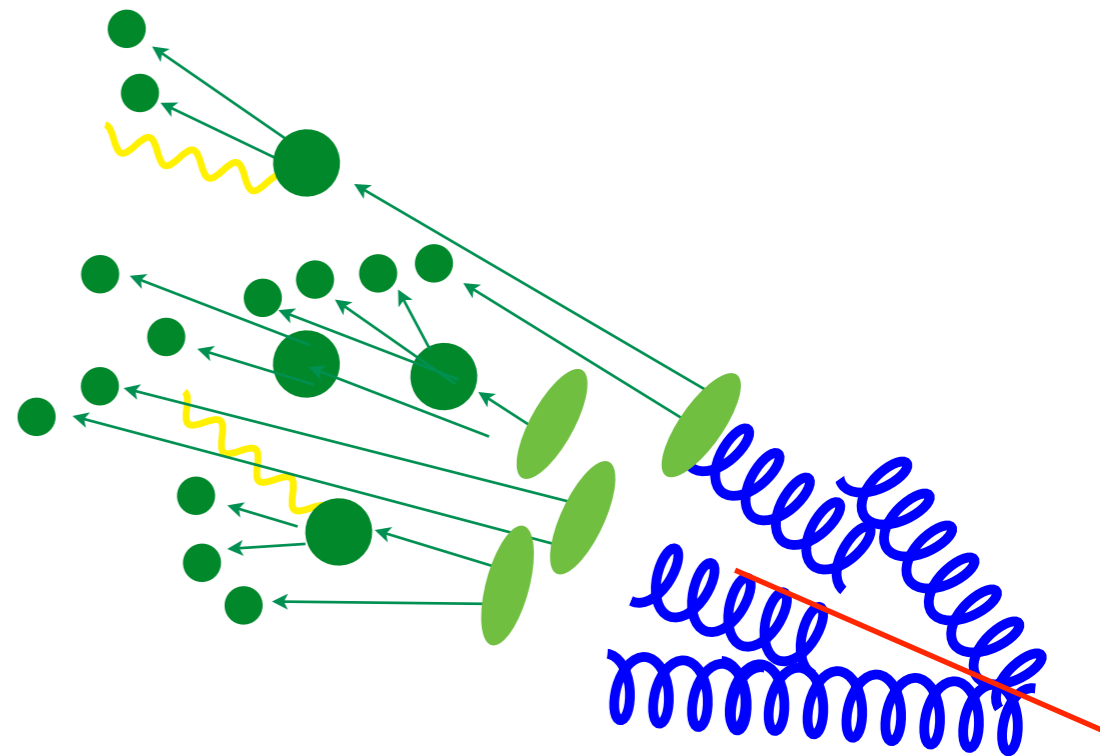
Benjamin Nachman

Lawrence Berkeley National Laboratory

CTEQ school 2019



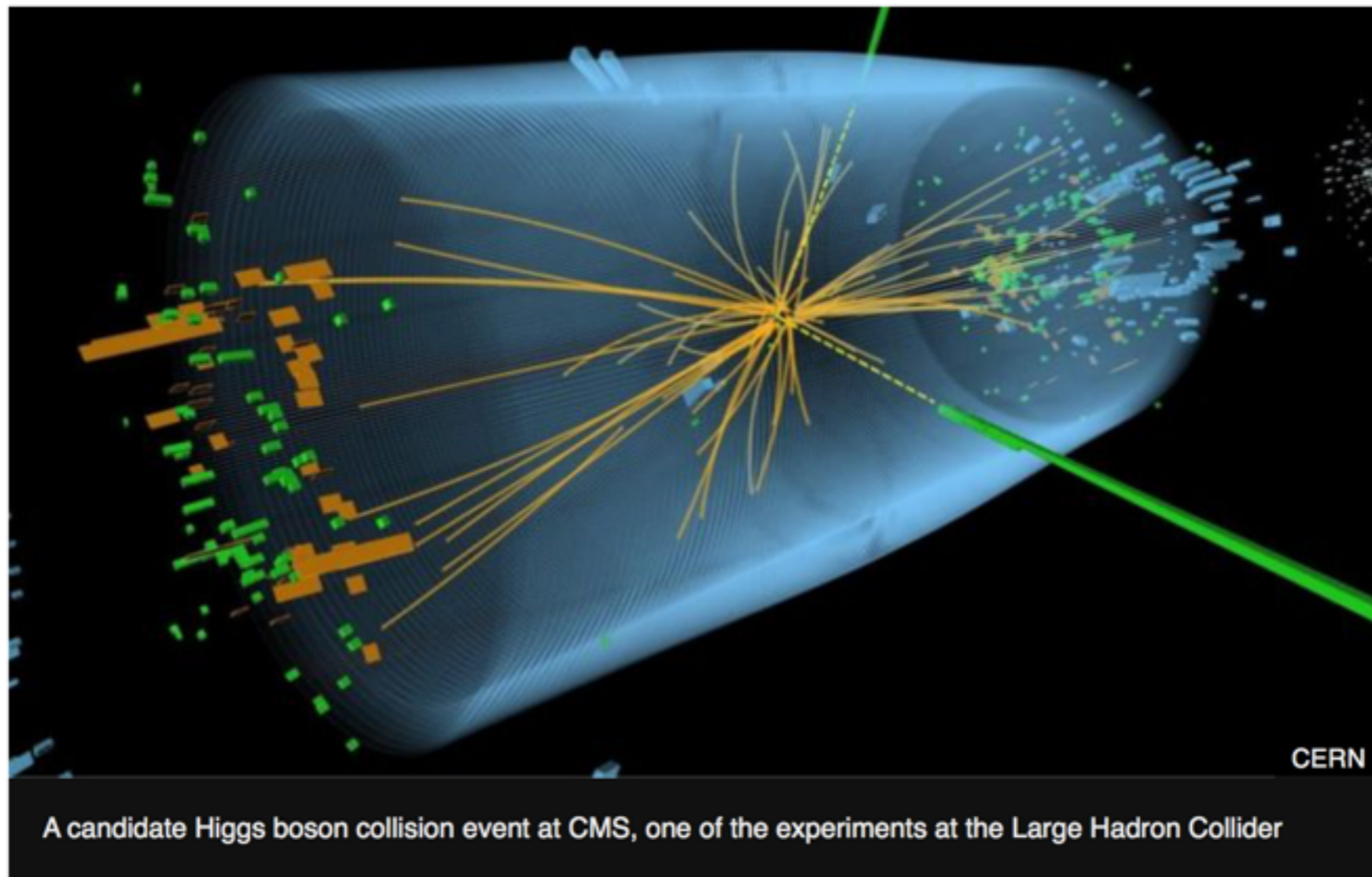
1. The Large Hadron Collider as a gluon factory
2. Overview of the QCD physics program at the LHC
3. Experimental considerations
 1. Calibration
 2. Unfolding
4. Physics topics
 1. PDFs
 2. α_s
 3. jet substructure
 4. other



What is the goal of the LHC?



BBC, March 2018



A candidate Higgs boson collision event at CMS, one of the experiments at the Large Hadron Collider

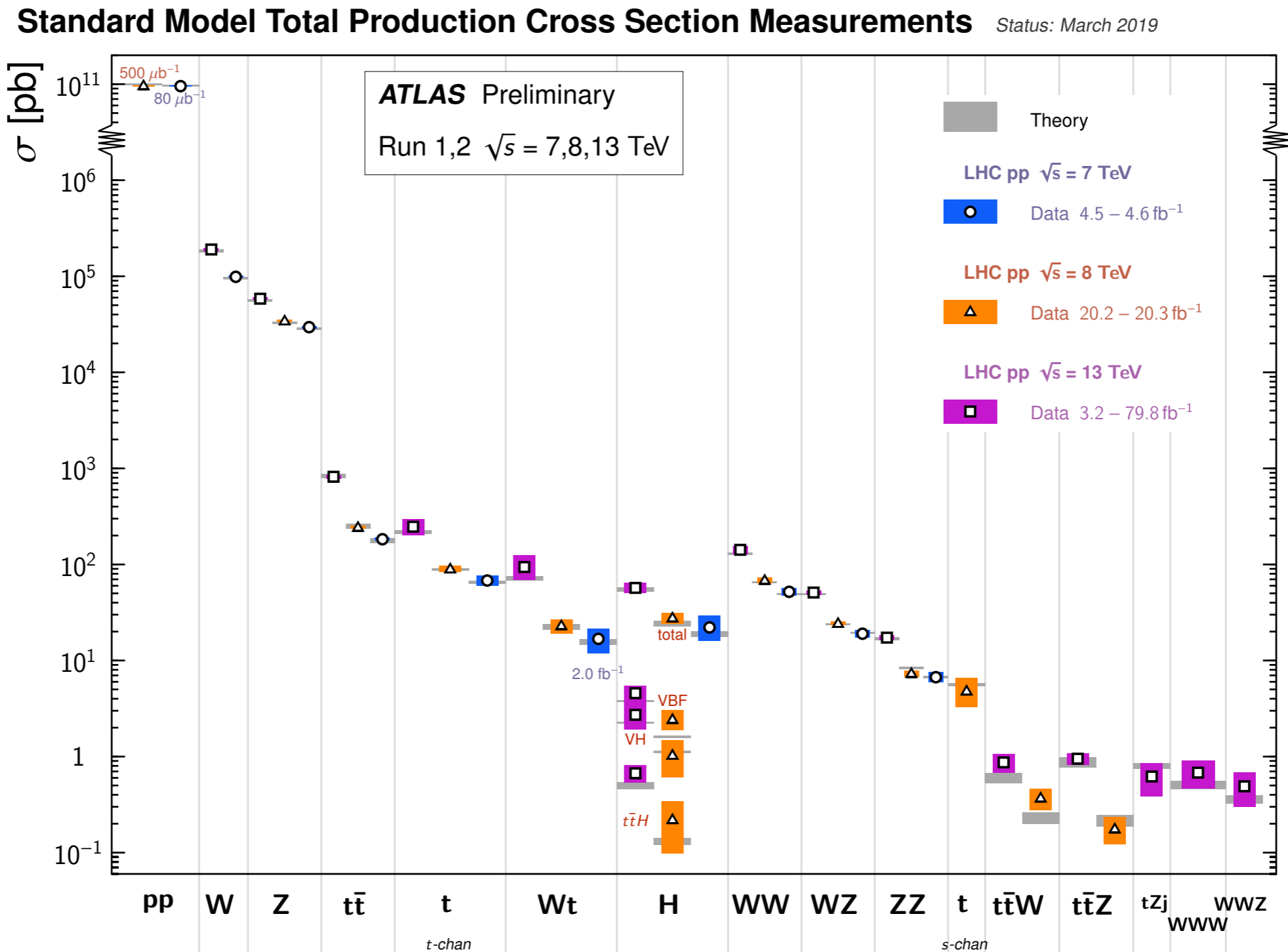
A top physicist says the construction of a "factory" to produce Higgs boson particles is a priority for the science community.

In an exclusive interview, Nigel Lockyer, head of America's premier particle physics lab, said studying the Higgs could hasten major discoveries.

Is the LHC a Higgs factory?



Rate at which
processes happen

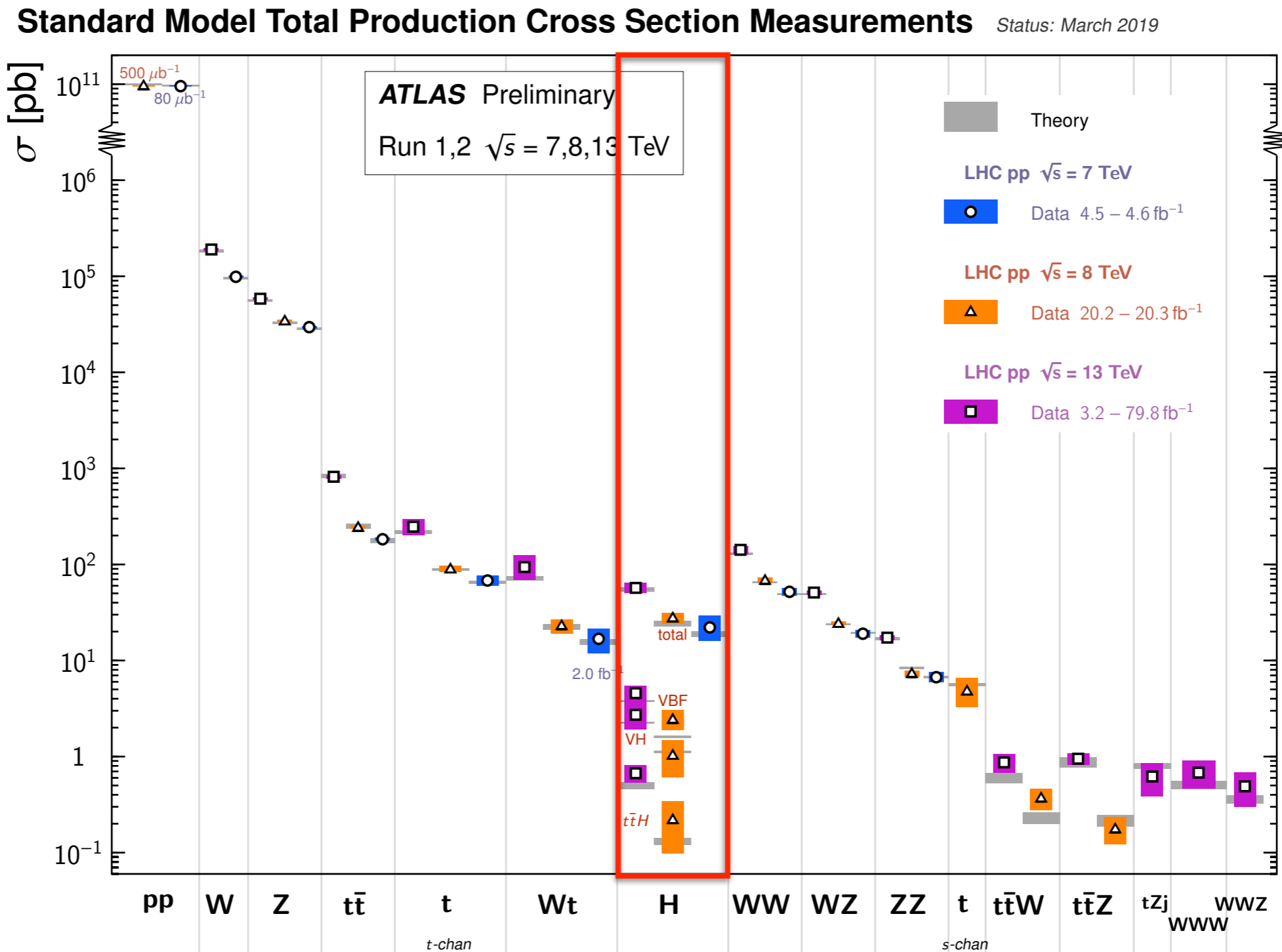


Process name: proton + proton goes to X

Is the LHC a Higgs factory?



Rate at which
processes happen

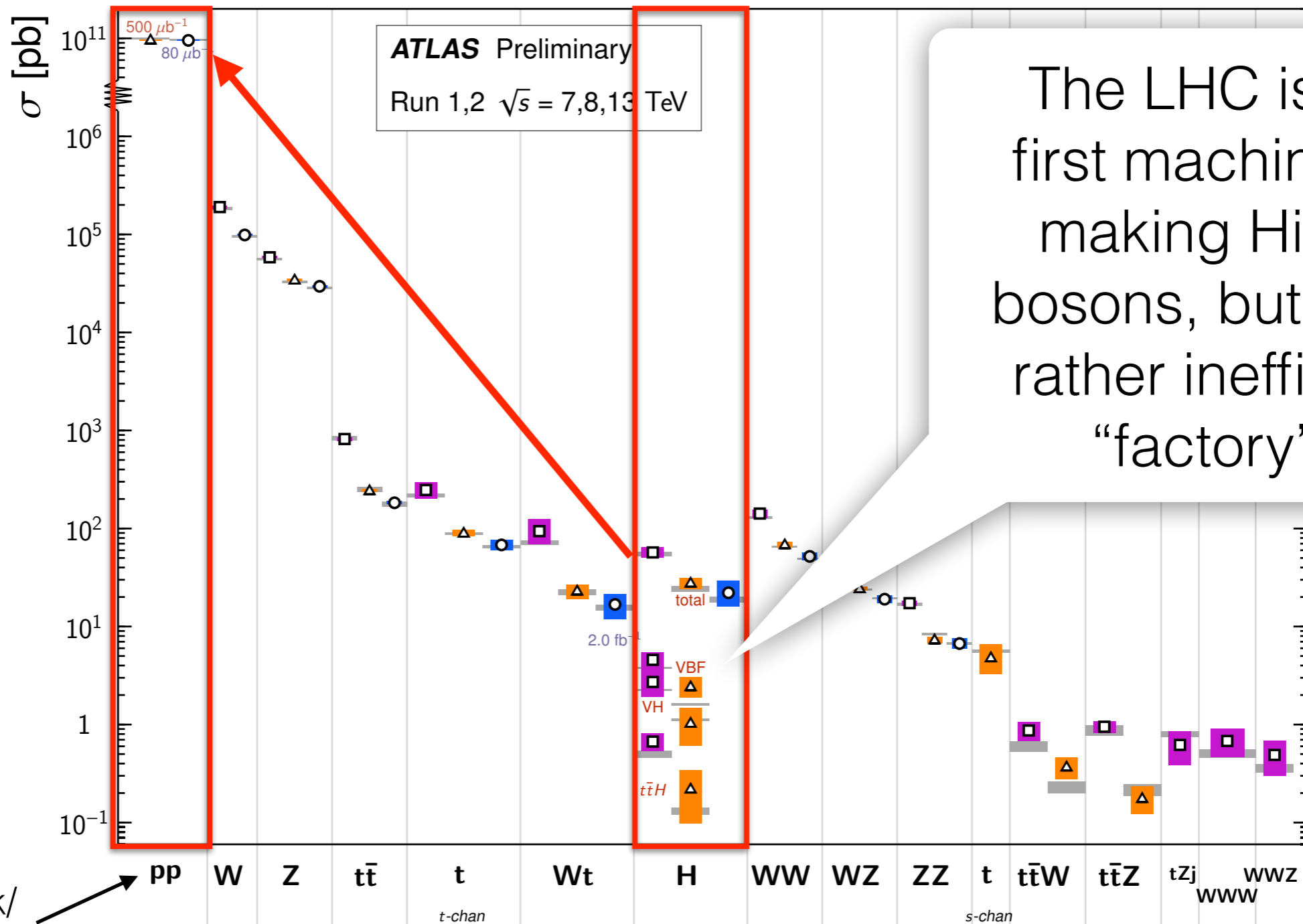


Process name: proton + proton goes to X

Is the LHC a Higgs factory?



Standard Model Total Production Cross Section Measurements *Status: March 2019*



Rate at which processes happen

The LHC is the first machine for making Higgs bosons, but it is a rather inefficient “factory” !

~Generic quark/gluon scattering

Process name: proton + proton goes to X

Higgs versus gluons



nature. One major ingredient in this model is a hypothetical, ubiquitous quantum field that is supposed to be responsible for giving particles their masses (this field would answer the basic question of why particles have the masses they do--or indeed, why they have any mass at all).

This field is called the **Higgs field**. As a consequence of wave-particle

- Scientific American

Higgs versus gluons

8

nature. One major ingredient in this model is a hypothetical, ubiquitous quantum field that is supposed to be responsible for giving particles their masses (this field would answer the basic question of why particles have the masses they do--or indeed, why they have any mass at all).

This field is called the **Higgs field**. As a consequence of wave-particle

- Scientific American



This is true, but it turns out that the gluon is responsible for most of our mass - without them, the proton mass would be many orders of magnitude lighter...

The Higgs-gluon connection



There is a **strong** connection between the Higgs boson and gluons.

Most Higgs bosons are produced when two gluons fuse

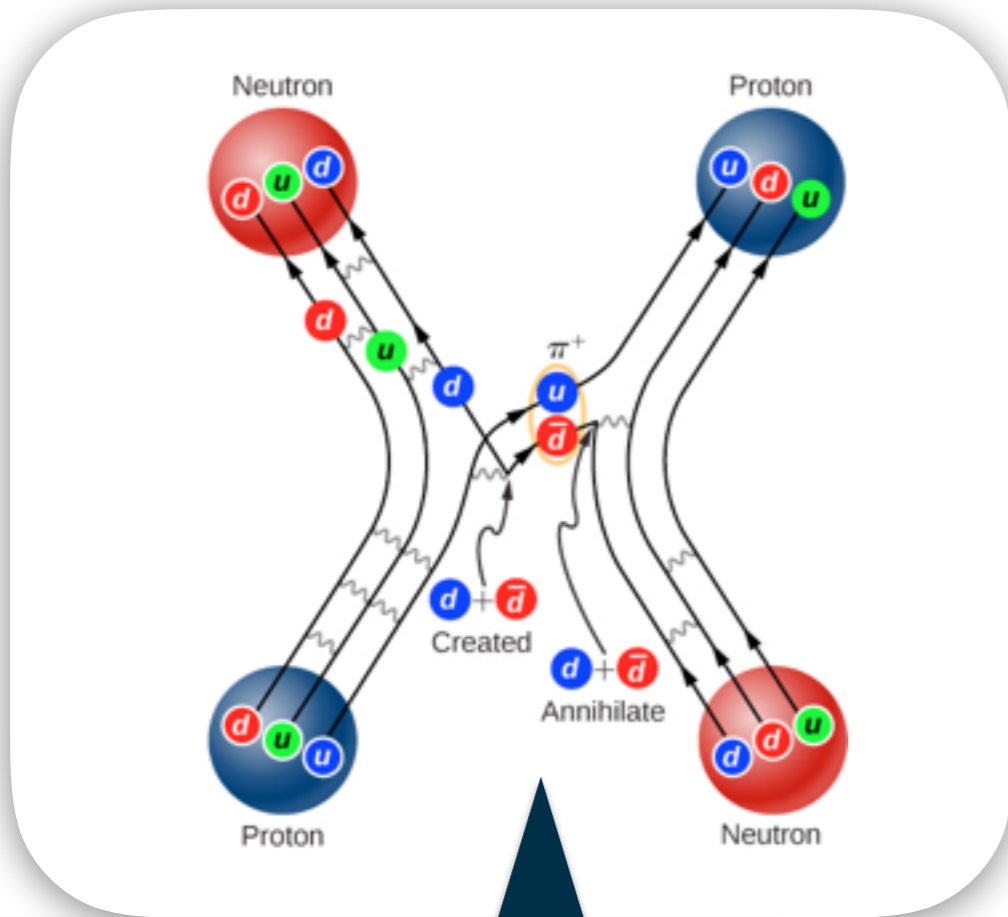
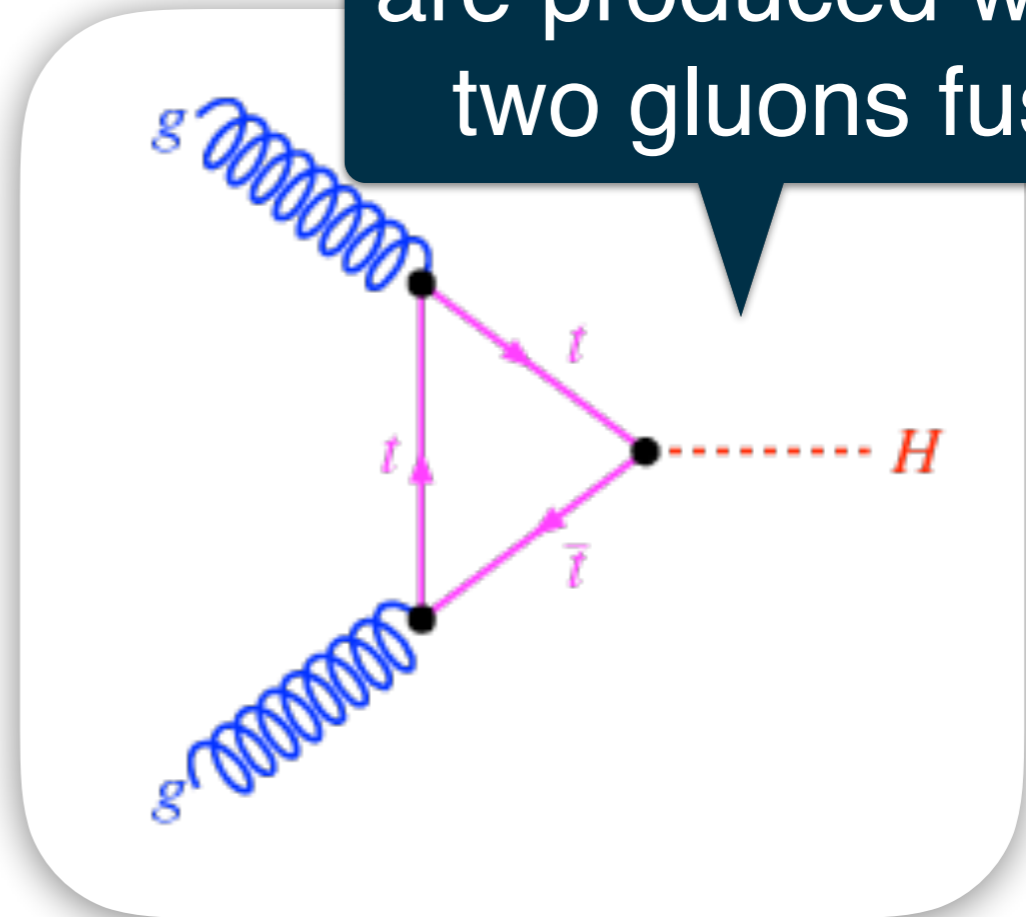


Image credit: University Physics



Due to the Higgs boson, the strong force is short-ranged

...okay, enough about the Higgs boson for now - more about the strong force!

QCD physics program at the LHC

10

Parton Distribution
Functions (PDFs)

Perturbative QCD /
strong coupling

Fragmentation
Functions

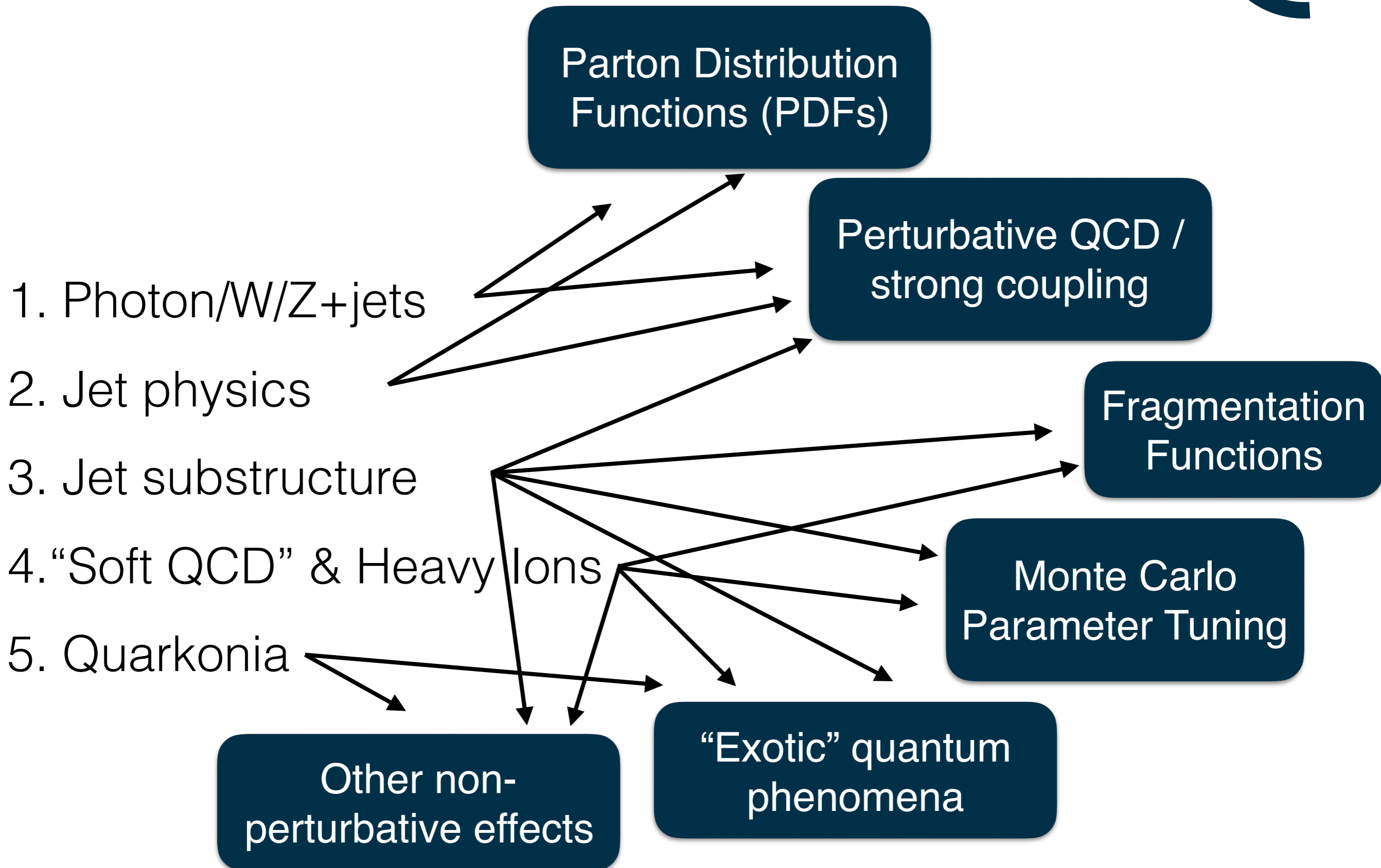
Monte Carlo
Parameter Tuning

“Exotic” quantum
phenomena

Other non-
perturbative effects

1. Photon/W/Z+jets
2. Jet physics
3. Jet substructure
4. “Soft QCD” & Heavy Ions
5. Quarkonia

QCD physics program at the LHC



Experimental considerations



12

We don't measure particles, we measure energy deposits and then infer particle properties.

Single-particle objects
(e.g. muons)

Composite objects
(e.g. jets)

Energy and angular biases

Energy and angular biases

Particles in inactive material

Particles bent out of cone

Secondary particles

Punchthrough

We don't measure particles, we measure energy deposits and then infer particle properties.

Single-particle objects (e.g. muons)	Composite objects (e.g. jets)
Energy and angular biases	Energy and angular biases
Usually one "bulk" correction	Particles in inactive material
	Particles bent out of cone
	Secondary particles
	Punchthrough

We don't measure particles, we measure energy deposits and then infer particle properties.

Single-particle objects
(e.g. muons)

Composite objects
(e.g. jets)

Energy and angular biases

Energy and angular biases

Usually one
"bulk" correction

Particles in inactive material

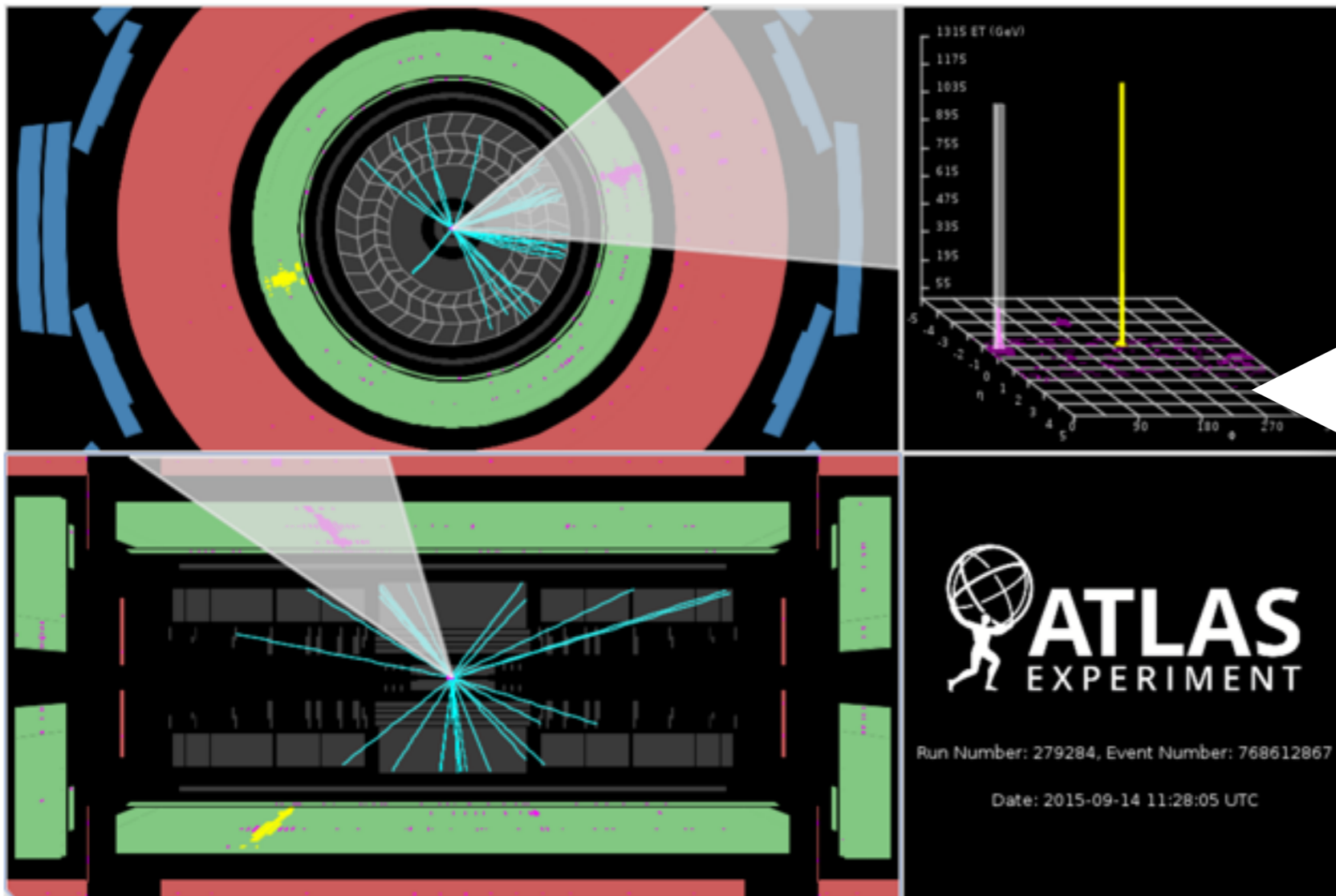
Particles bent out of cone

Food for thought: how would you do this without depending on the prior spectrum?

Secondary particles

Punchthrough

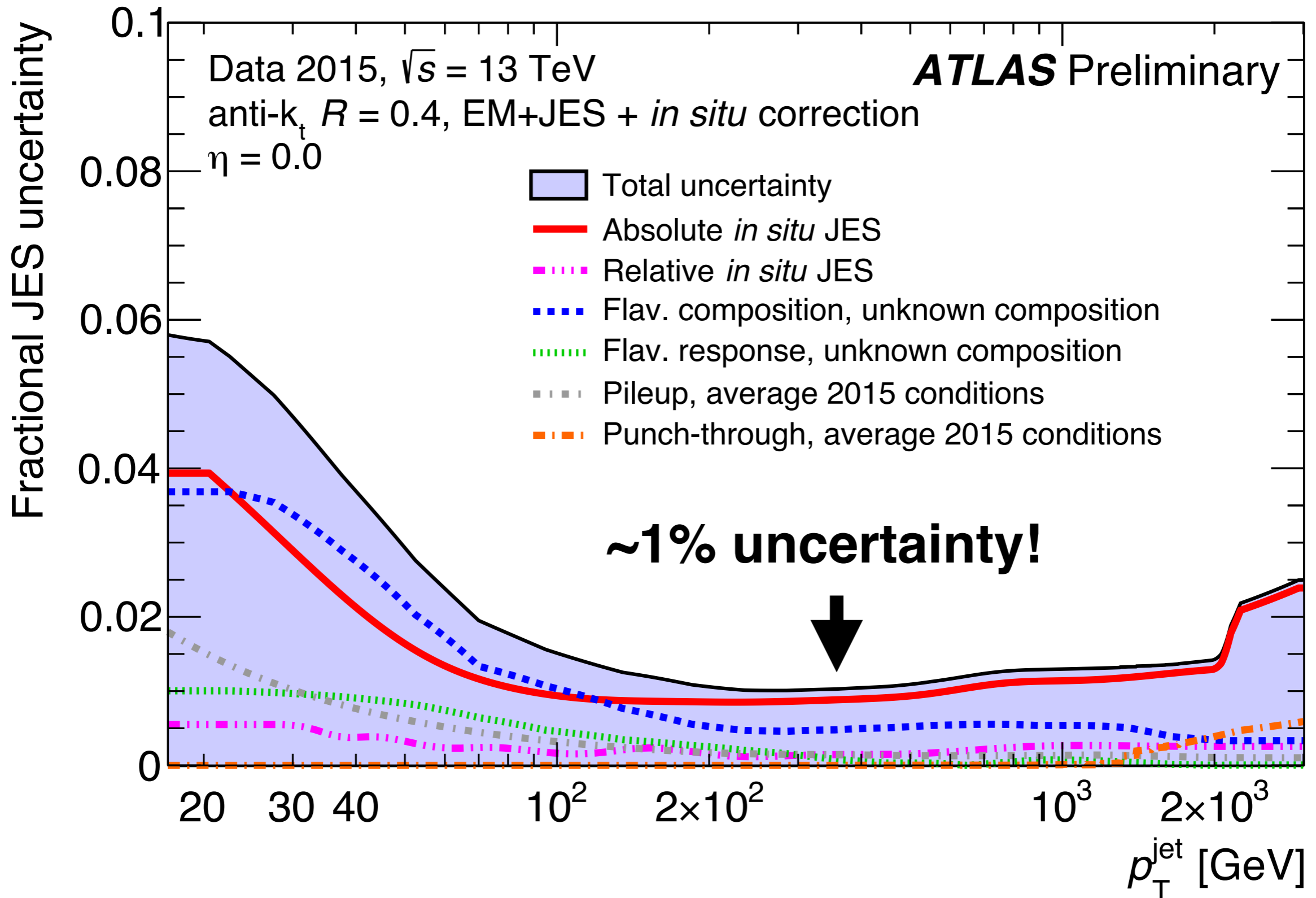
The nominal calibration is derived using simulation and then a residual calibration accounts for differences between data and simulation (derived using data).



Can use the balance of well-measured objects (e.g. photons) with jets to study the bias in data.

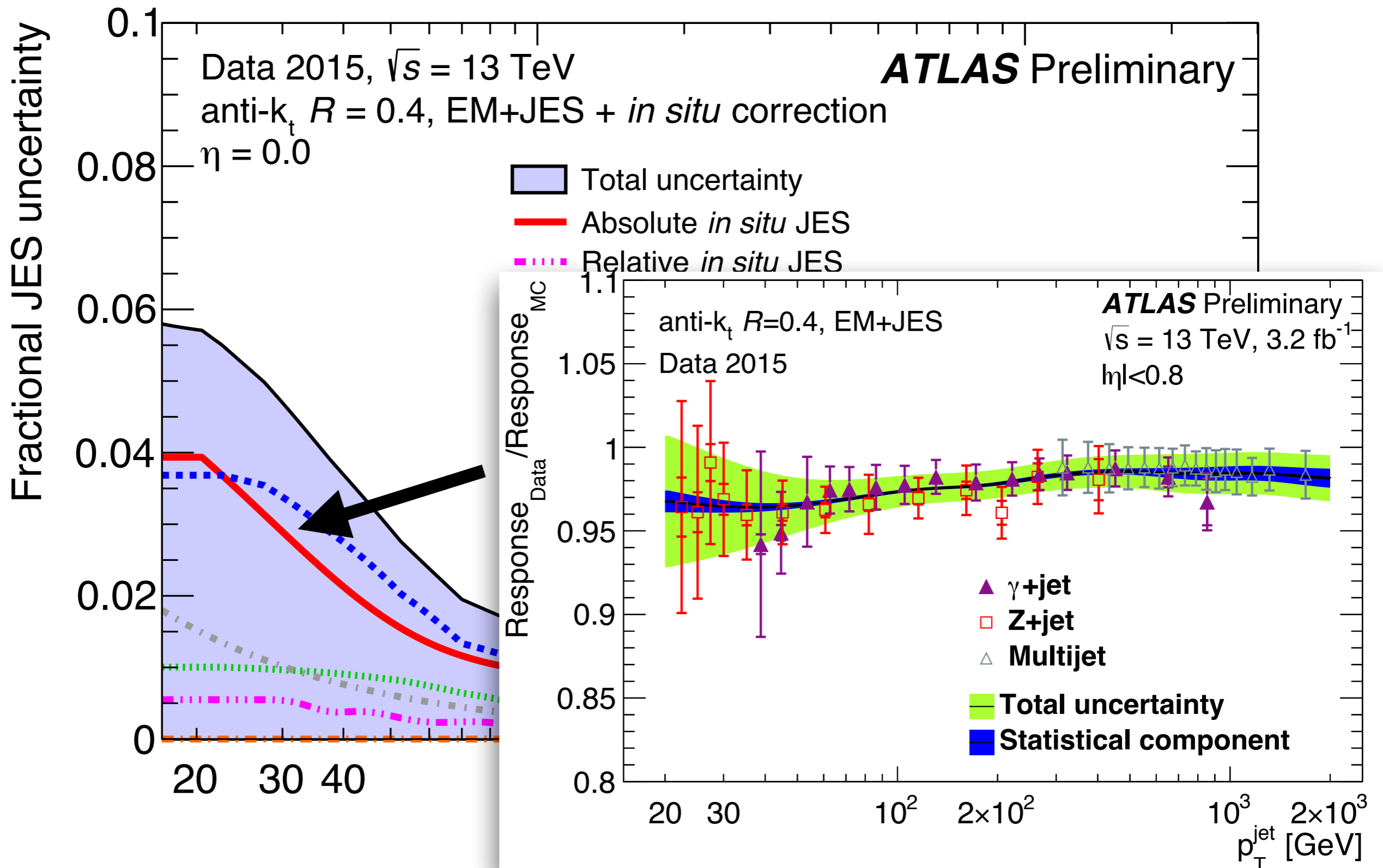
Jet energy bias uncertainty

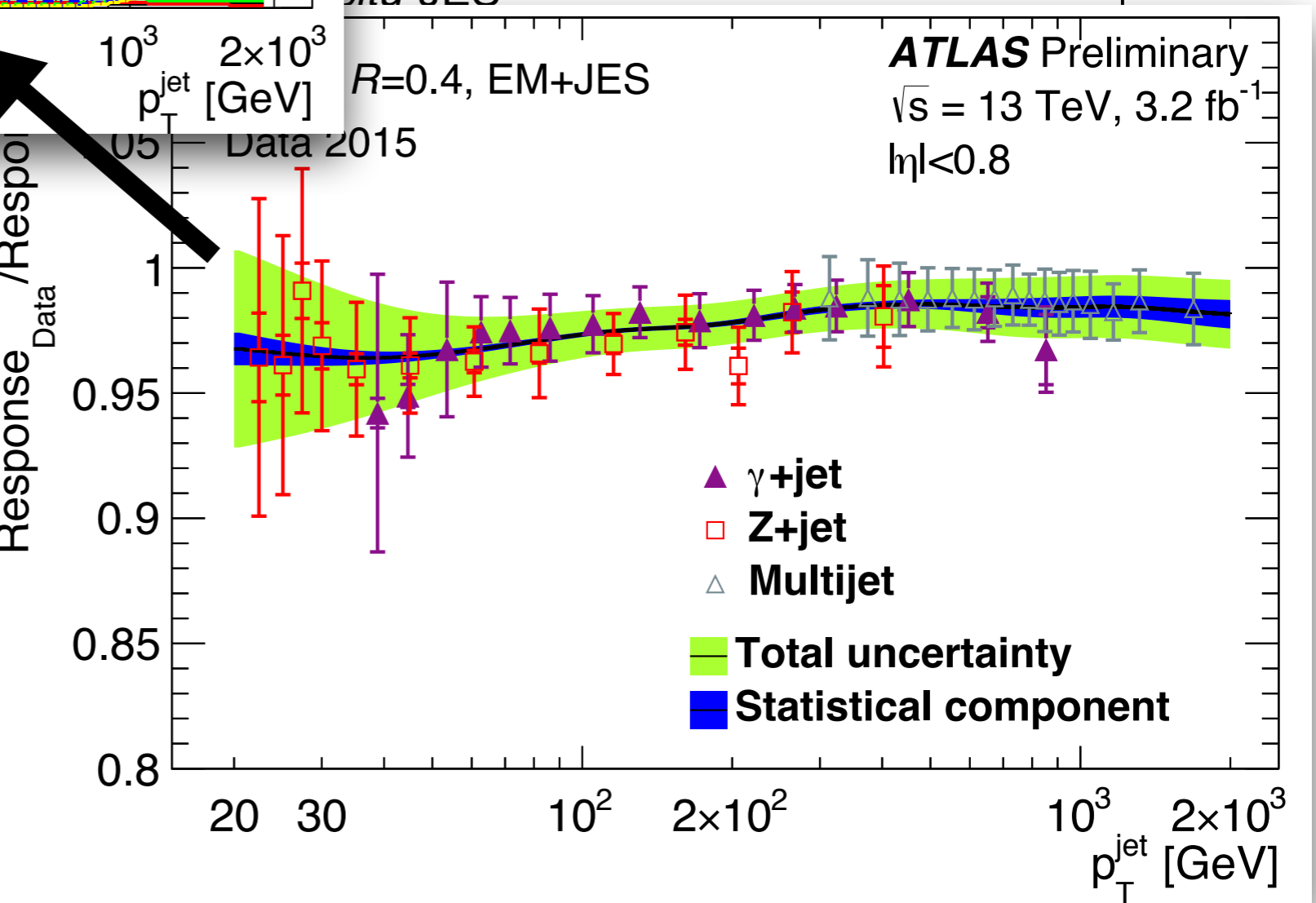
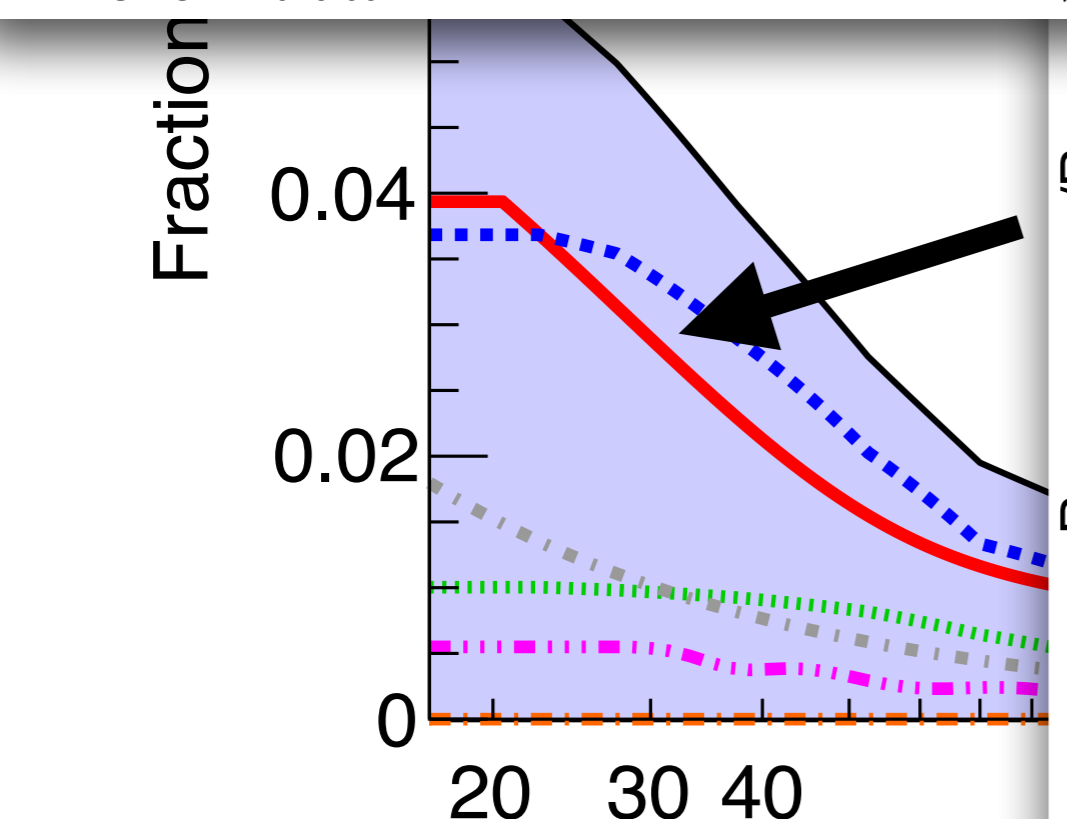
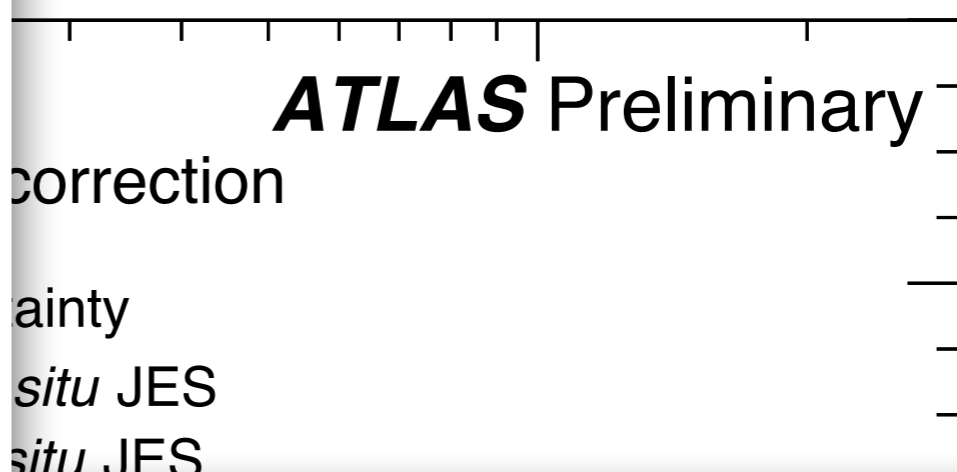
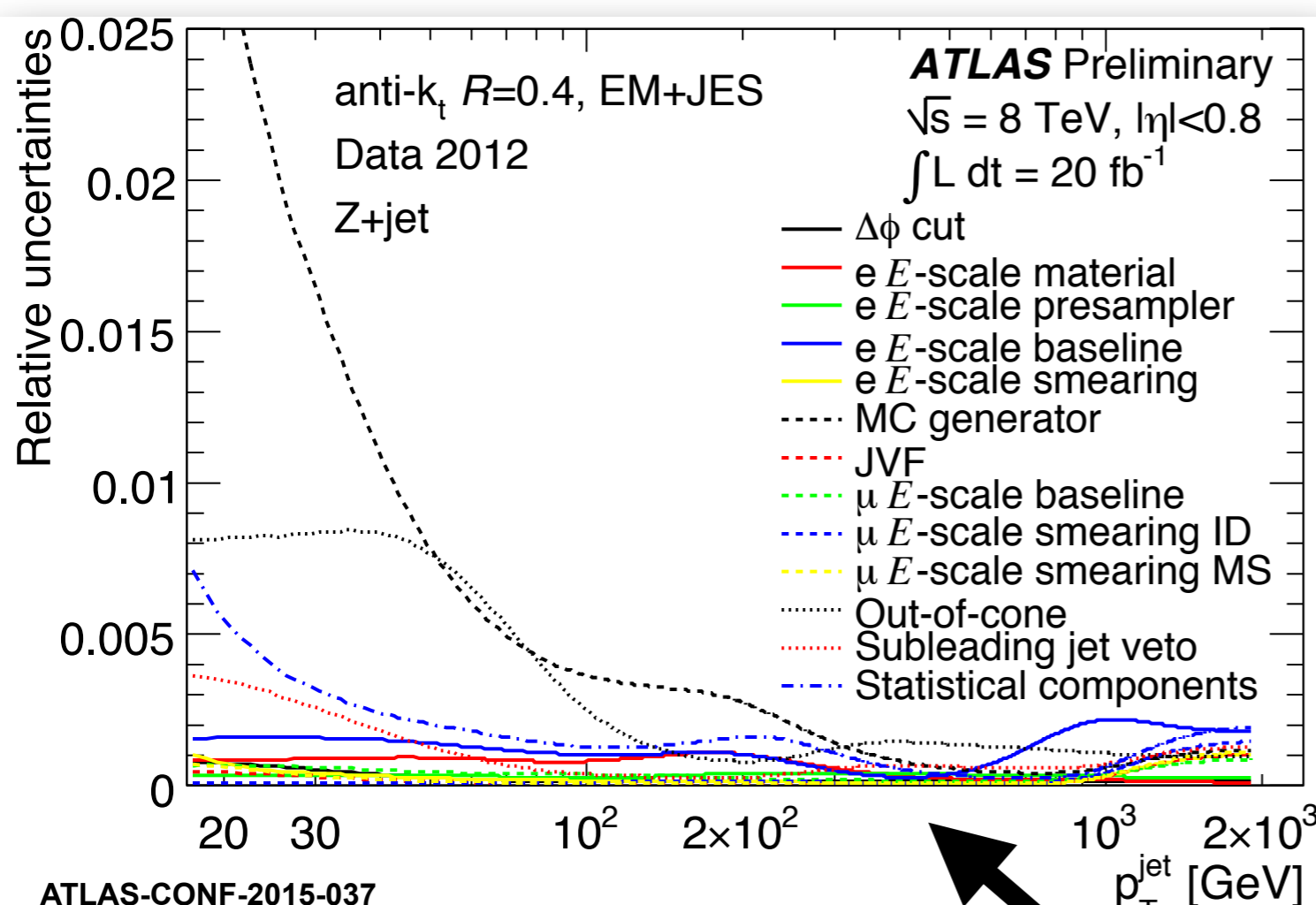
17

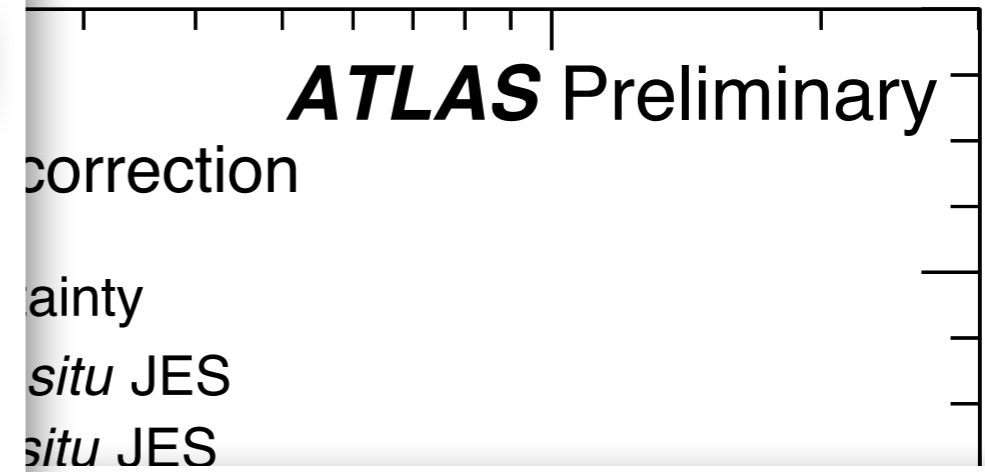
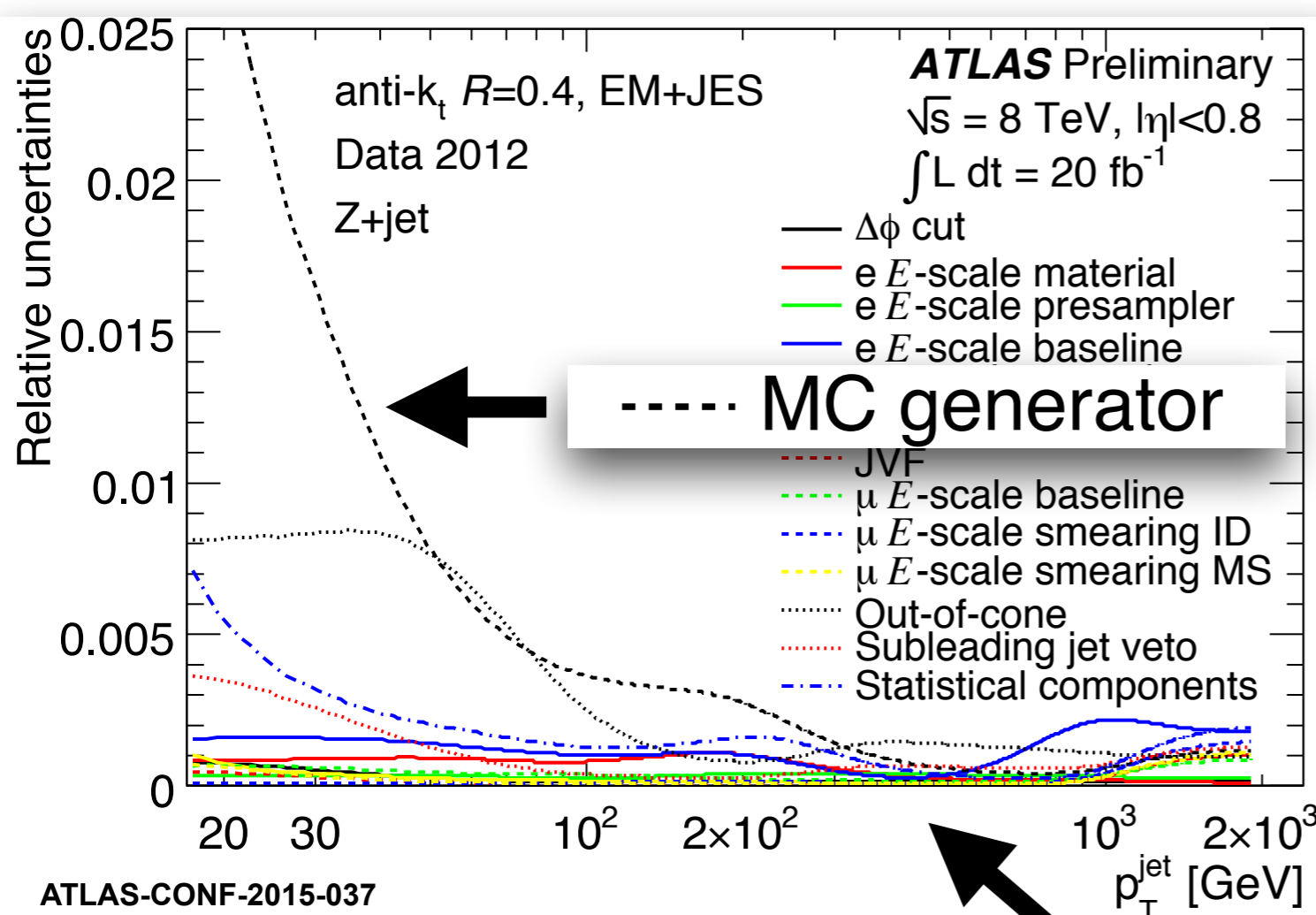


Jet energy bias uncertainty

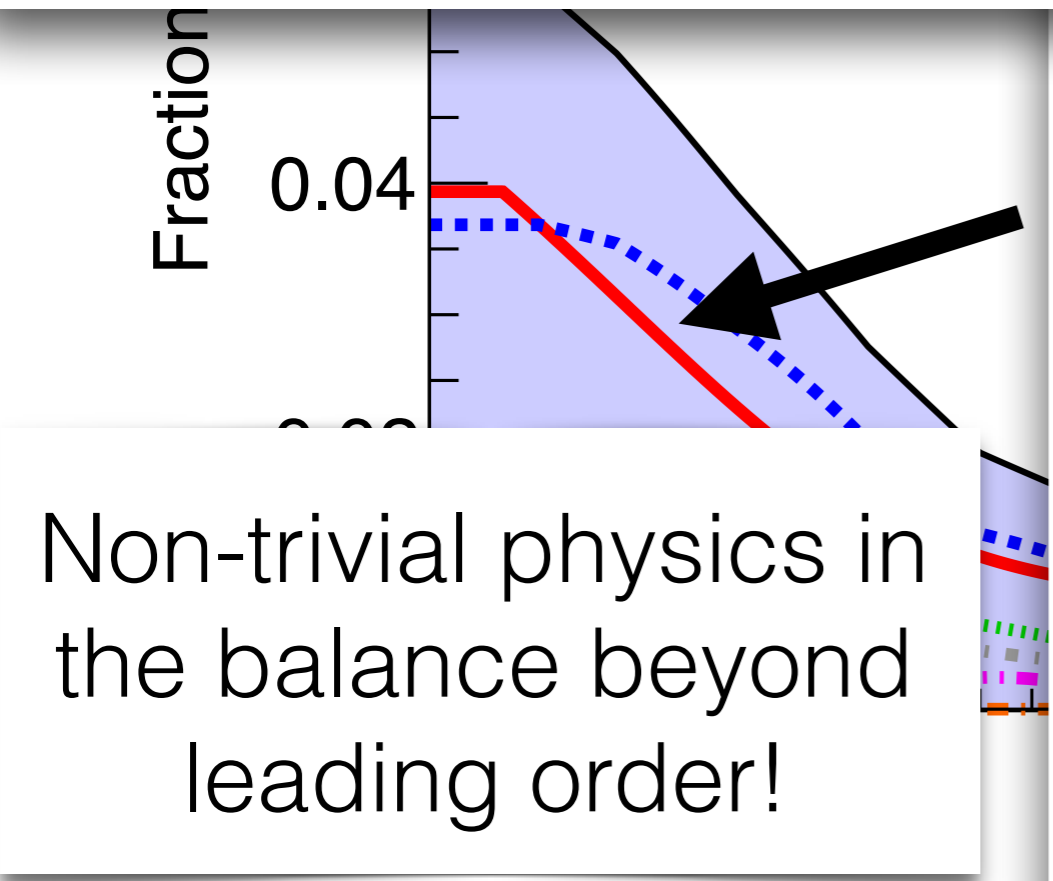
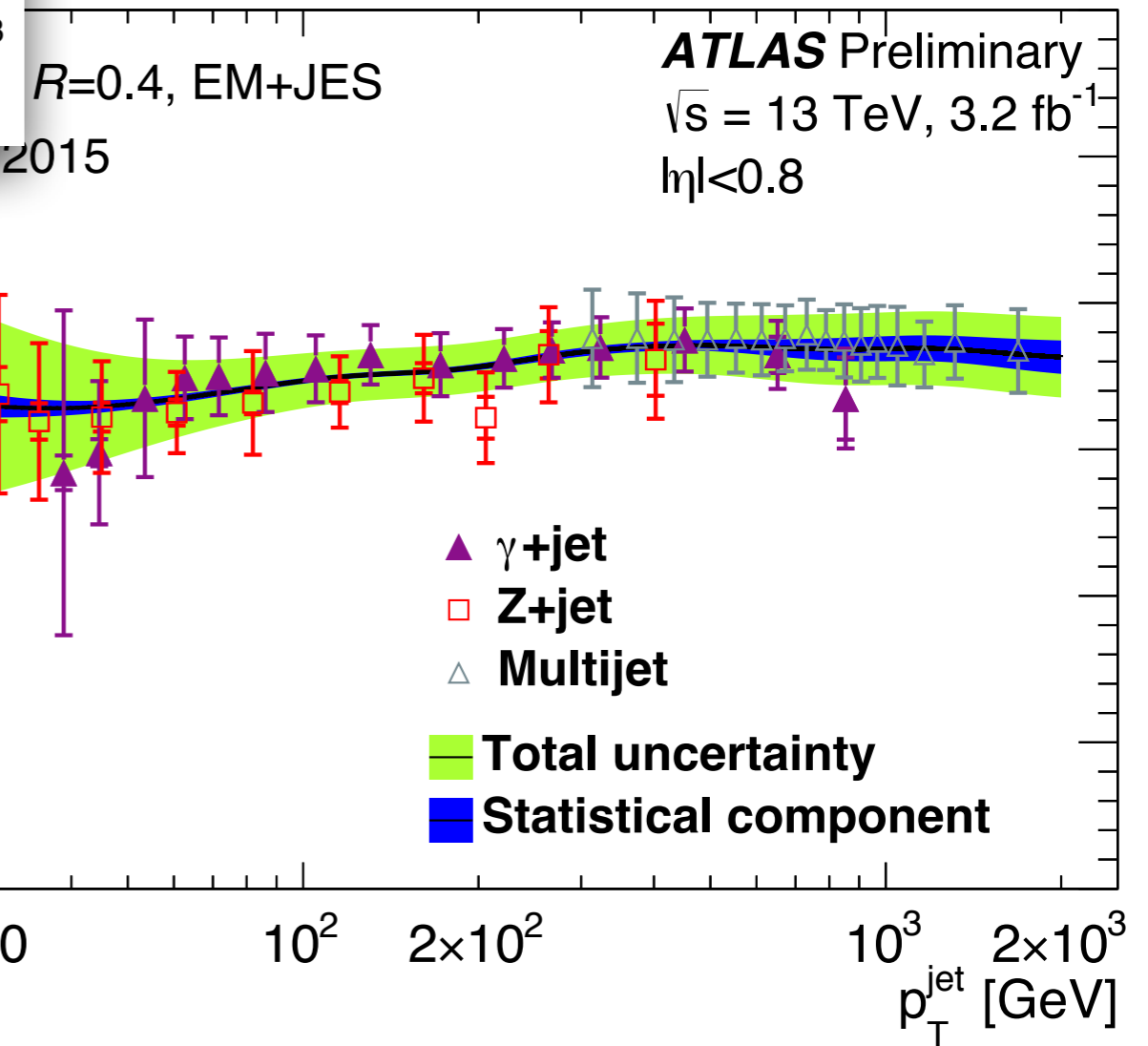
18







ATLAS-CONF-2015-037



Non-trivial physics in the balance beyond leading order!

When someone says they have measured a differential cross-section, they mean that it has been **unfolded**.

Unfolding corrects for detector effects so that our data can be directly compared with theory predictions.

It is not valid to directly compare theory predictions to detector-level data !!

Either the theory or the data must be corrected. Correcting the data is more general and can allow for multiple theory groups to reuse the same measurement.

What does unfolding do?

In general, unfolding needs to correct for interrelated effects:

- Acceptance and efficiency
 - ➔ Particles produced may not be measured
- Detector noise
 - ➔ Particles measured may not be from real particles
- Background processes
 - ➔ If you want to measure process X , need to remove Y
- Combinatorics
 - ➔ If N particles, chance that detector can change order
- Detector distortions
 - ➔ Bias and resolution effects

What does unfolding do?

23

In general, unfolding needs to correct for interrelated effects:

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I'll briefly
illustrate this



Illustrative toy example

24

$$m = Rt \quad m = \text{measured}; t = \text{true}$$

We usually call R the “response matrix” because m and t are binned (and thus vectors).

We (usually) get R from detailed detector simulations.

e.g. Geant4 (particle propagation and energy deposition) + custom code for analog and digital signal emulation.

Illustrative toy example

25

$$m = Rt \quad m = \text{measured}; t = \text{true}$$

I know what you want to do here is $t = R^{-1} m$.

Illustrative toy example

26

$$m = Rt \quad m = \text{measured}; t = \text{true}$$

I know what you want to do here is $t = R^{-1} m$.

In the next slides, I hope to convince you that this is not usually a good idea.

Illustrative toy example

27

$$m = Rt \quad m = \text{measured}; t = \text{true}$$

$$R = \begin{pmatrix} 1 - \epsilon & \epsilon \\ \epsilon & 1 - \epsilon \end{pmatrix}$$

Consider this case, where $0 \leq \epsilon \leq 0.5$

$$m = Rt \quad m = \text{measured}; t = \text{true}$$

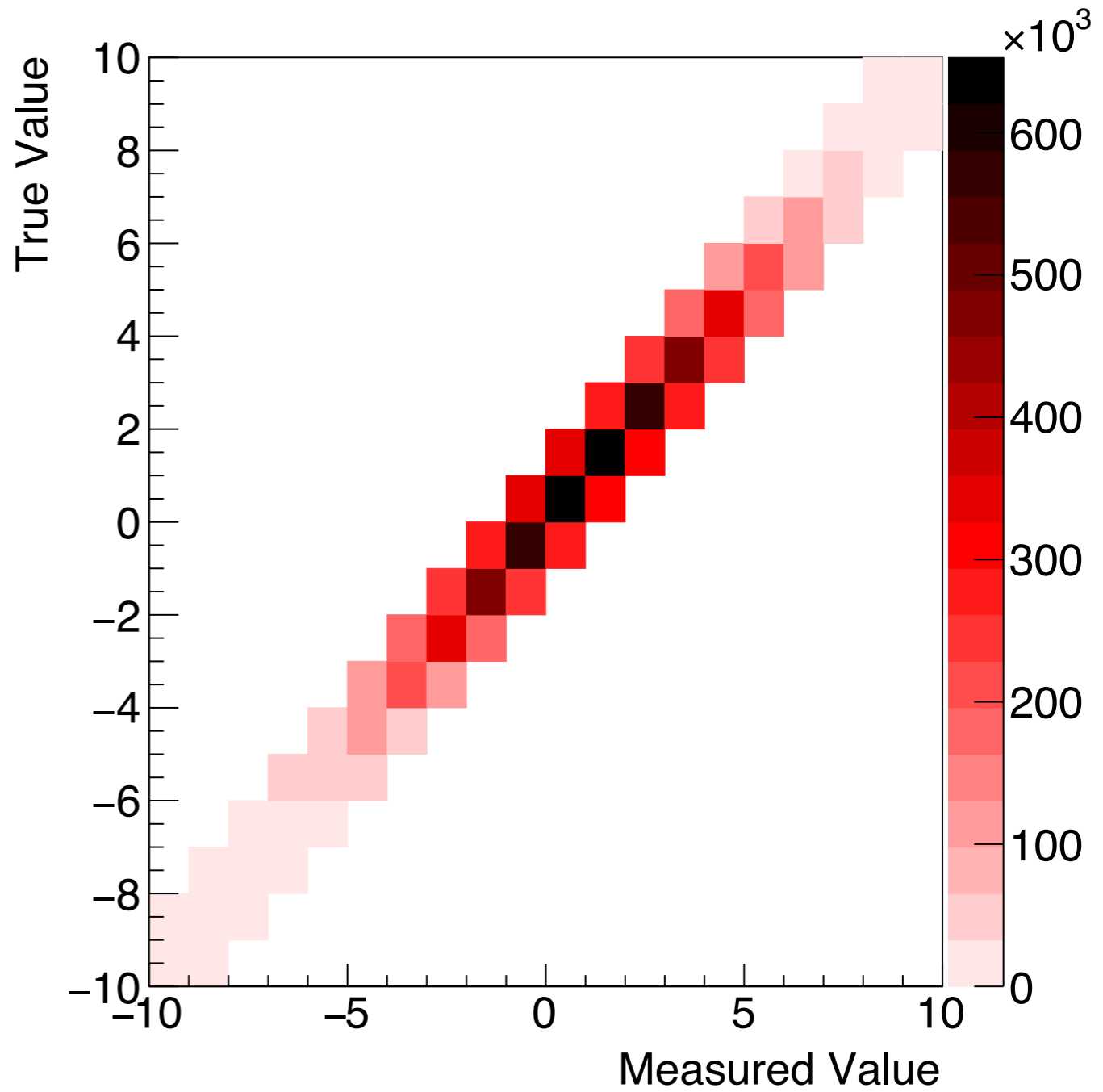
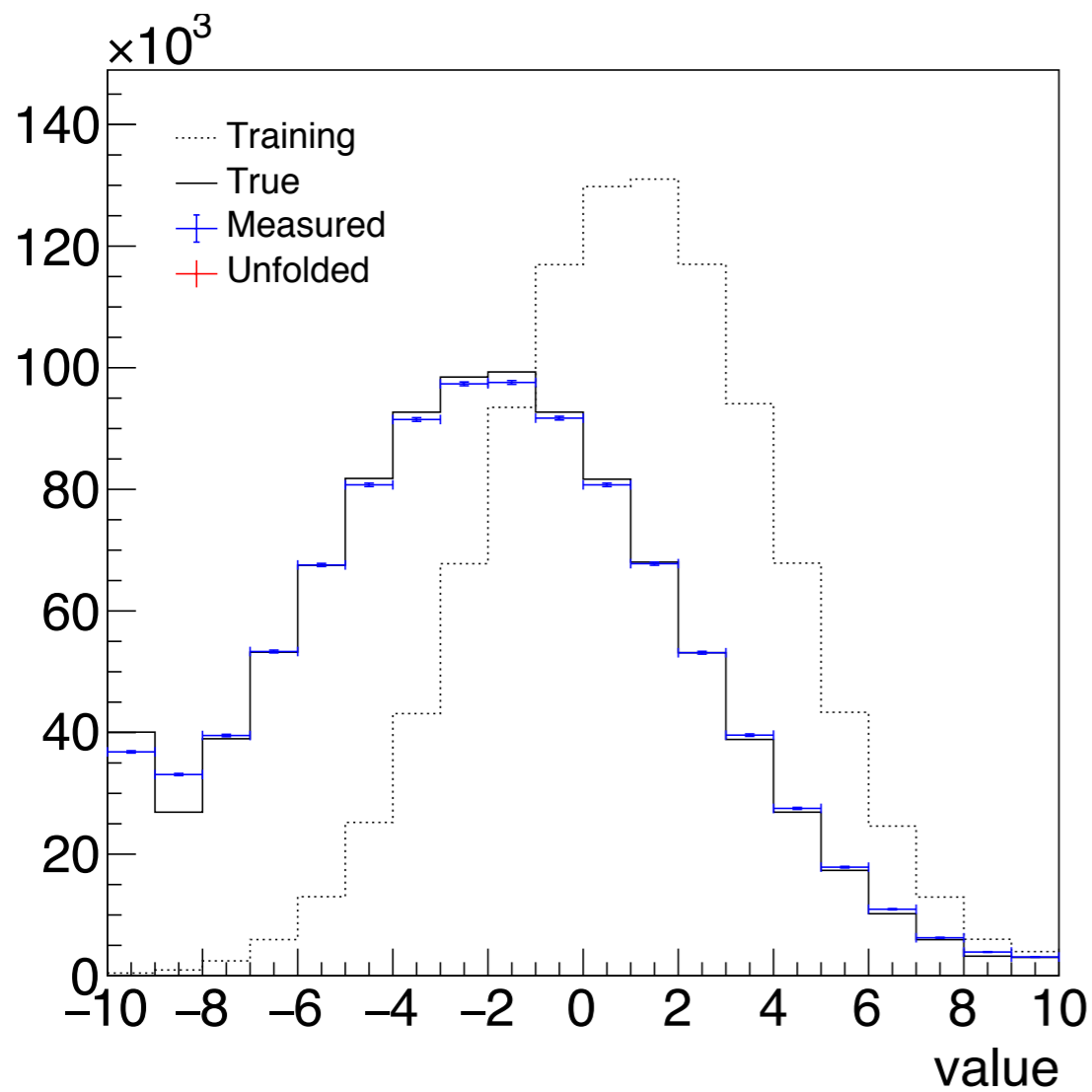
$$R = \begin{pmatrix} 1 - \epsilon & \epsilon \\ \epsilon & 1 - \epsilon \end{pmatrix}$$

$$\text{Var}(R^{-1}m) \propto 1/\text{Det}(R) = 1 - 2\epsilon$$

Statistical uncertainty blows up as $\epsilon \rightarrow 0.5$

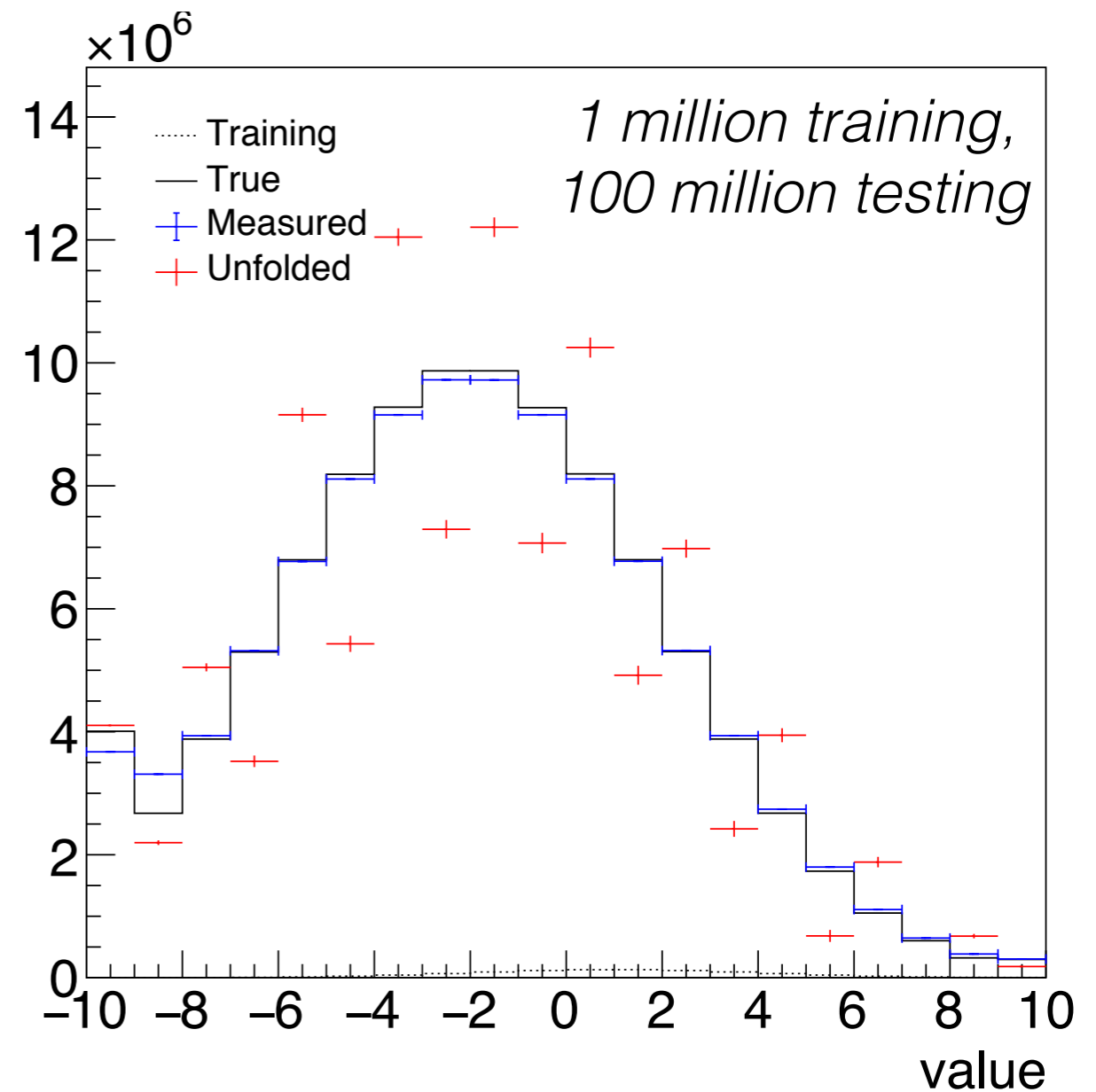
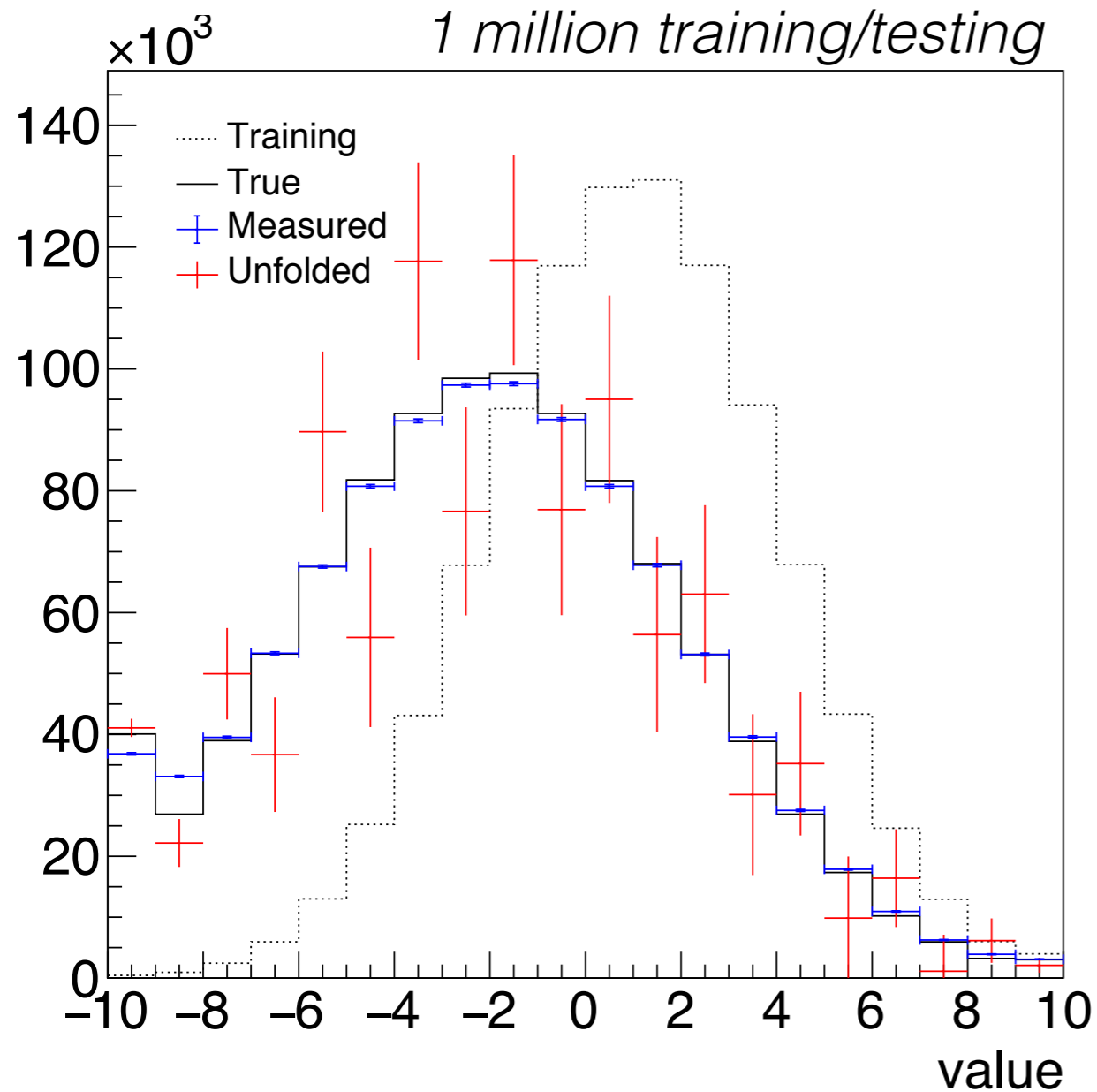
A more realistic example

$$R_{\text{norm}} = \begin{pmatrix} 0.75 & 0.25 & 0 & & & \\ 0.25 & 0.50 & 0.25 & 0 & & \\ 0 & 0.25 & 0.50 & 0.25 & 0 & \\ & 0 & 0.25 & 0.50 & 0.25 & \\ & & 0 & 0.25 & 0.50 & \\ & & & & & \ddots \end{pmatrix}$$



Unfolding by Matrix Inversion

30



Stat. uncertainty is large and there is a bias when training dataset is too small.

The HEP solution

31

Our solution is to do regularized matrix inversion.

There are two main techniques that we use:

“Iterative Bayesian Unfolding”

$$\theta_{ij} = \frac{\Pr(m_j|t_i) \cdot \Pr(t_i)}{\sum_i \Pr(m_j|t_i) \cdot \Pr(t_i)}$$

response
matrix

regularization
= number of iterations

$$\Pr_{k+1}(t_i) = \sum_j \theta_{ij} \Pr_k(t_j)$$

Nucl. Inst. Meth. A 362 (1995) 487

“Singular Value
Decomposition (SVD) Unfolding”

$$R = USV^T$$

U, V , orthogonal, S diagonal & non-negative

$$d = U^T m \quad z_i(\tau) = \frac{d_i}{s_i} \cdot \frac{s_i^2}{s_i^2 + \tau}$$

$$t = Vz$$

regularization
parameter

Nucl. Inst. Meth. A 372 (1995) 469

Main tool: RooUnfold (ROOT-based C++ code)

The HEP solution

32

Our solution is to do regularized matrix inversion.

Note: regularized matrix inversion depends on unphysical regularization parameters

One chooses parameters to tradeoff bias and uncertainty.

$$\theta_{ij} = \frac{\Pr(m_j | t_i) \cdot \Pr(t_i)}{\sum_k \Pr(m_j | t_k) \cdot \Pr(t_k)}$$

IBU Unfolding

- depend on prior

- depends on # of iterations

Nucl. Inst. Meth. A 362 (1995) 487

SVD Unfolding

$$d = U^T \cdot \frac{d_i}{s_i} \cdot \frac{s_i^2}{s_i^2 + \tau}$$

$$t = Vz$$

regularization parameter

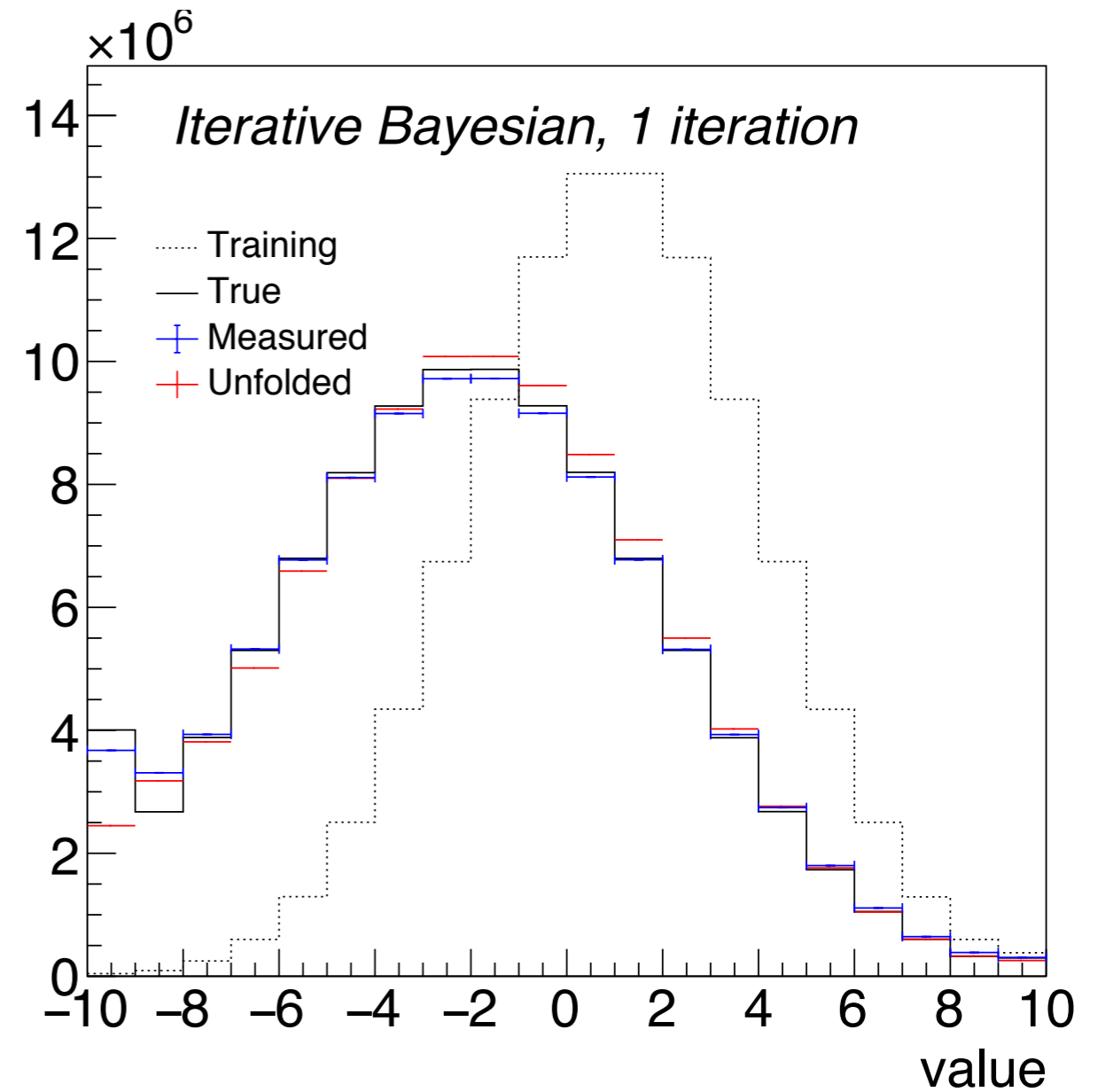
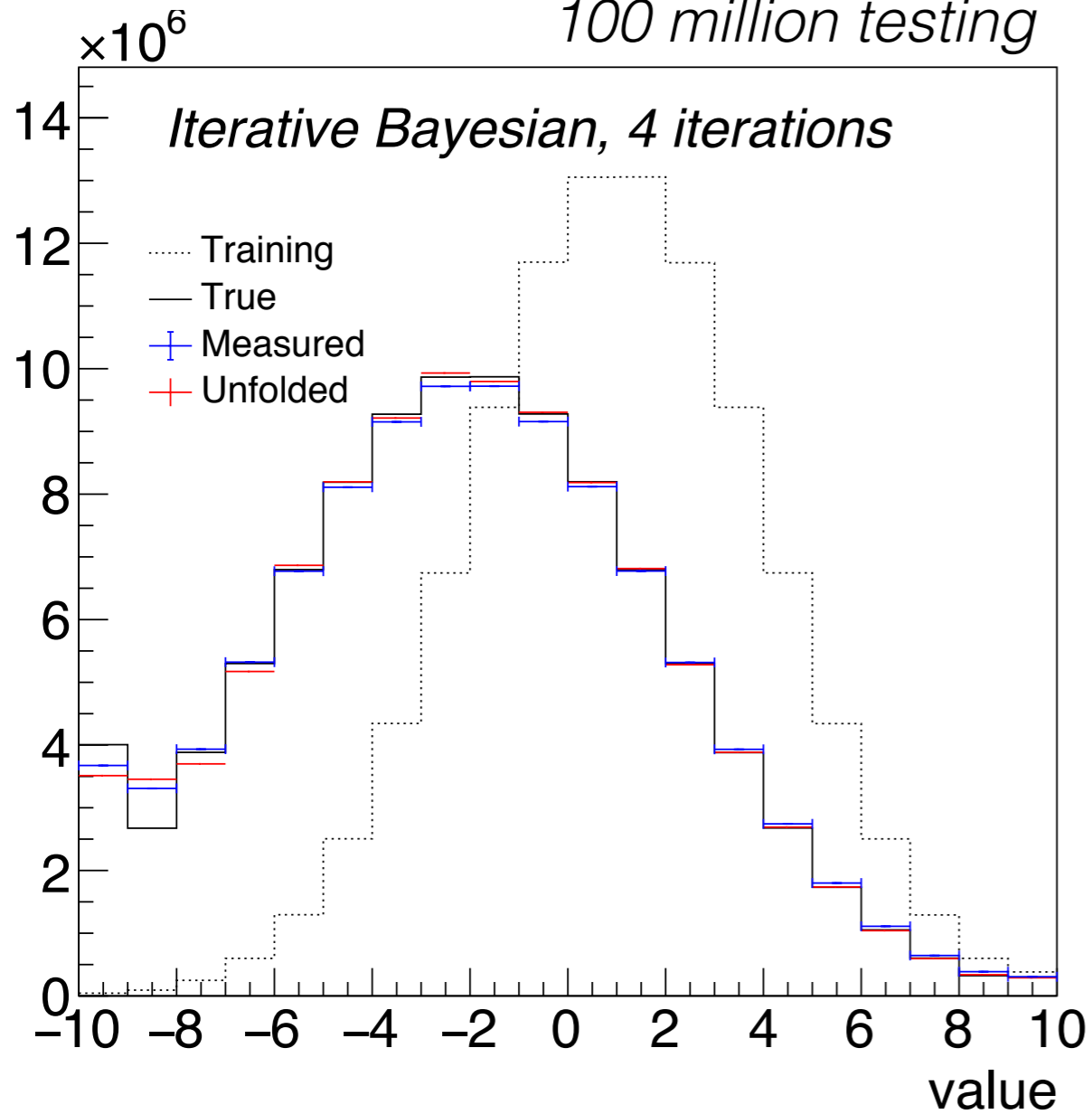
Nucl. Inst. Meth. A 372 (1995) 469

Main tool: RooUnfold (ROOT-based C++ code)

Example: Iterative Bayesian Unfolding

33

1 million training,
100 million testing



One last comment: phase space def.

34

Need to decide what to unfold to, called the “fiducial volume”

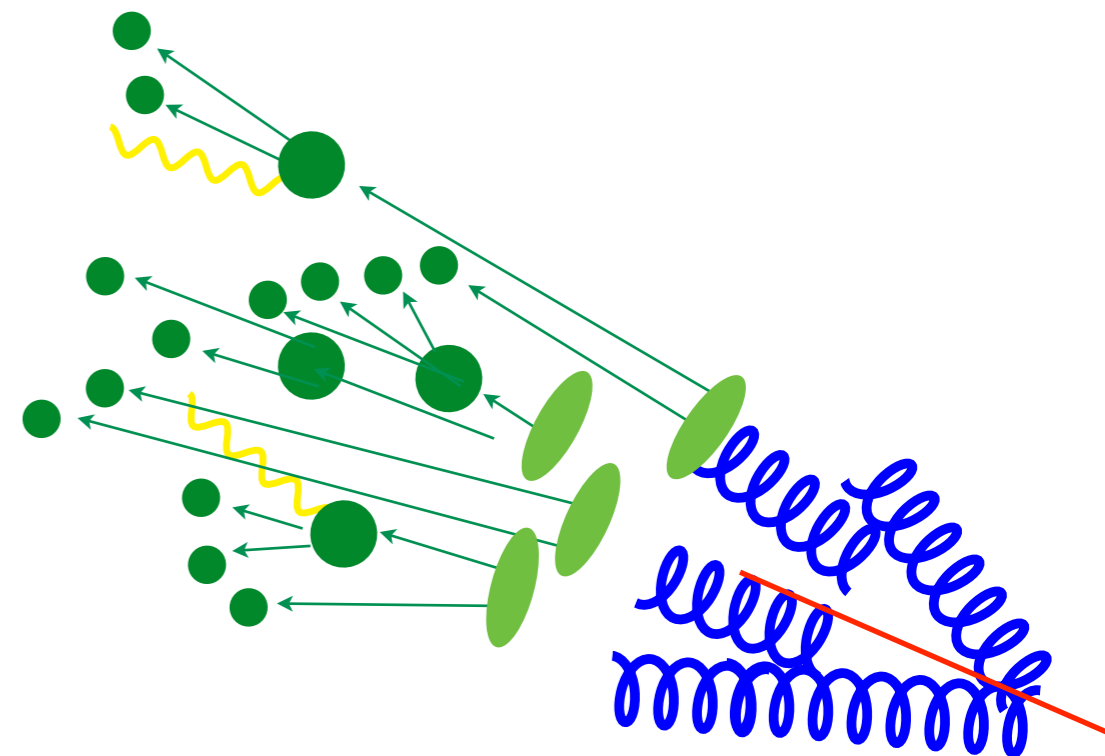
Calculations are often at the level of “born-level partons”

Measurements are at the level of hadrons.

+Non-perturbative corrections

+Resummation (“dressed”)

Born-level parton



One last comment: phase space def.

35

Need to decide what to unfold to, called the “fiducial volume”

Calculations are often at the level of “born-level partons”

Measurements are at the level of hadrons.

The closer the target is to the observable, the less the unfolding has to do and the smaller the modeling uncertainty.

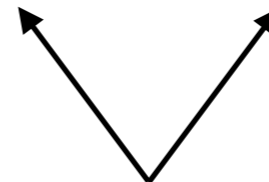
Please don't unfold to “born-level partons”. Better to “dress” the calculations with resummation and hadronization.

(fortunately, born measurements is becoming less fashionable these days)

Physics topics



$$\sigma = \sum_{ij \in \{q, \bar{q}, g\}} \int dx_1 dx_2 f_i(x_1, \mu) f_j(x_2, \mu) \hat{\sigma}_{ij}(x_1 E, x_2 E)$$



PDFs

Every* LHC measurement is sensitive to PDFs - the ones that are most useful for constraining them can be (1) measured precisely, (2) predicted precisely (see last term), and (3) mostly sensitive to ~one partonic channel

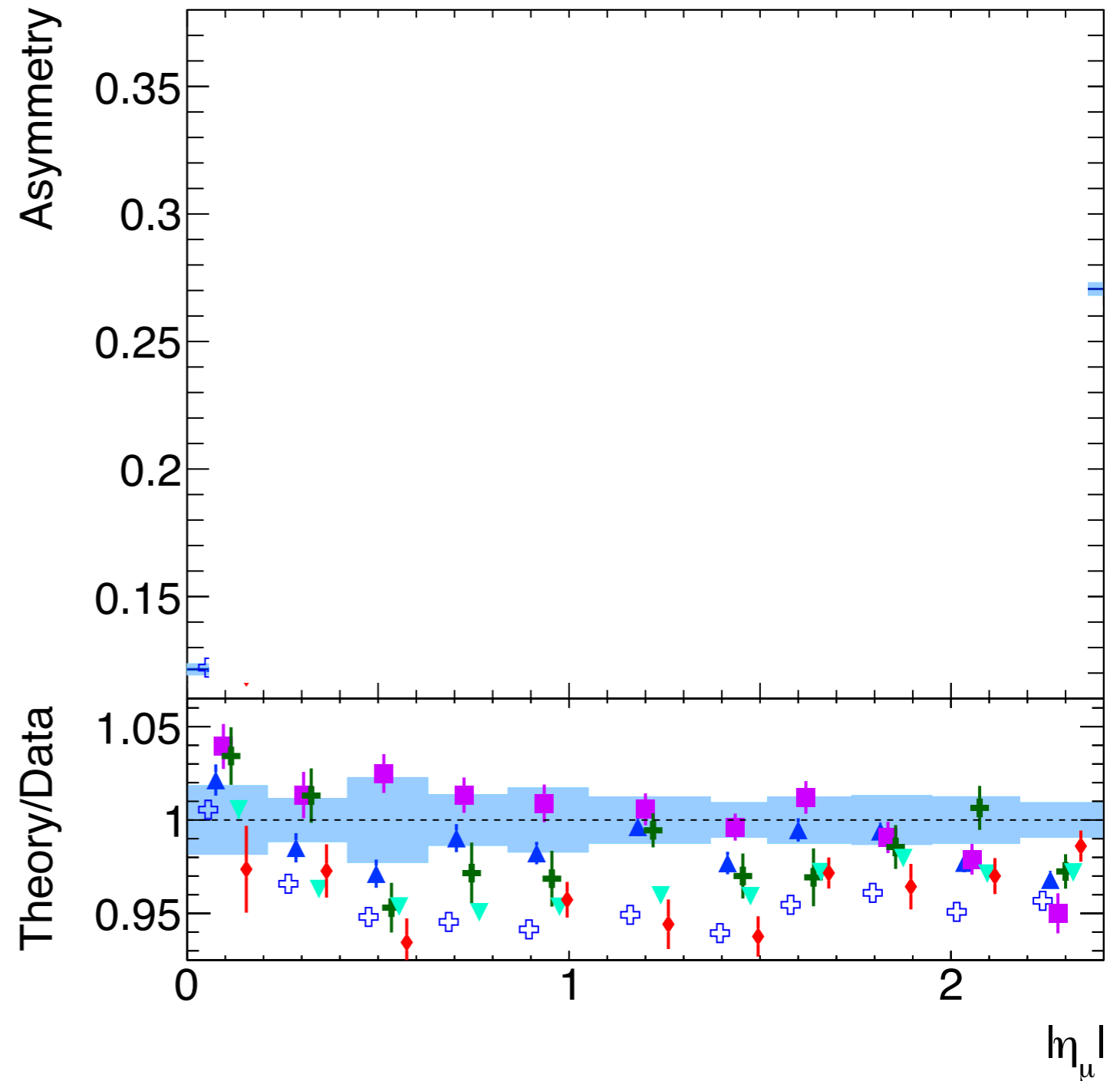
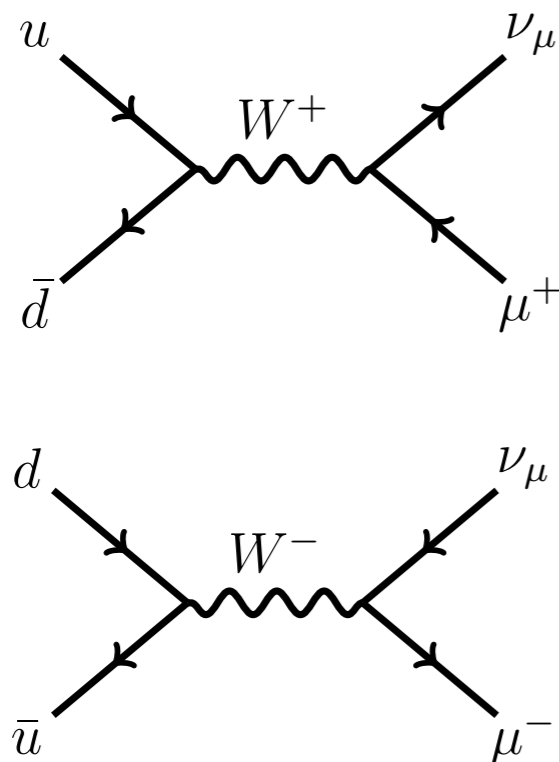
*Except when the protons interact coherently.

Valence quarks at moderate x

38

W +jets is a precise probe of the u/d content of the proton.

At a pp collide, more W^+ than W^-



Valence quarks at moderate x

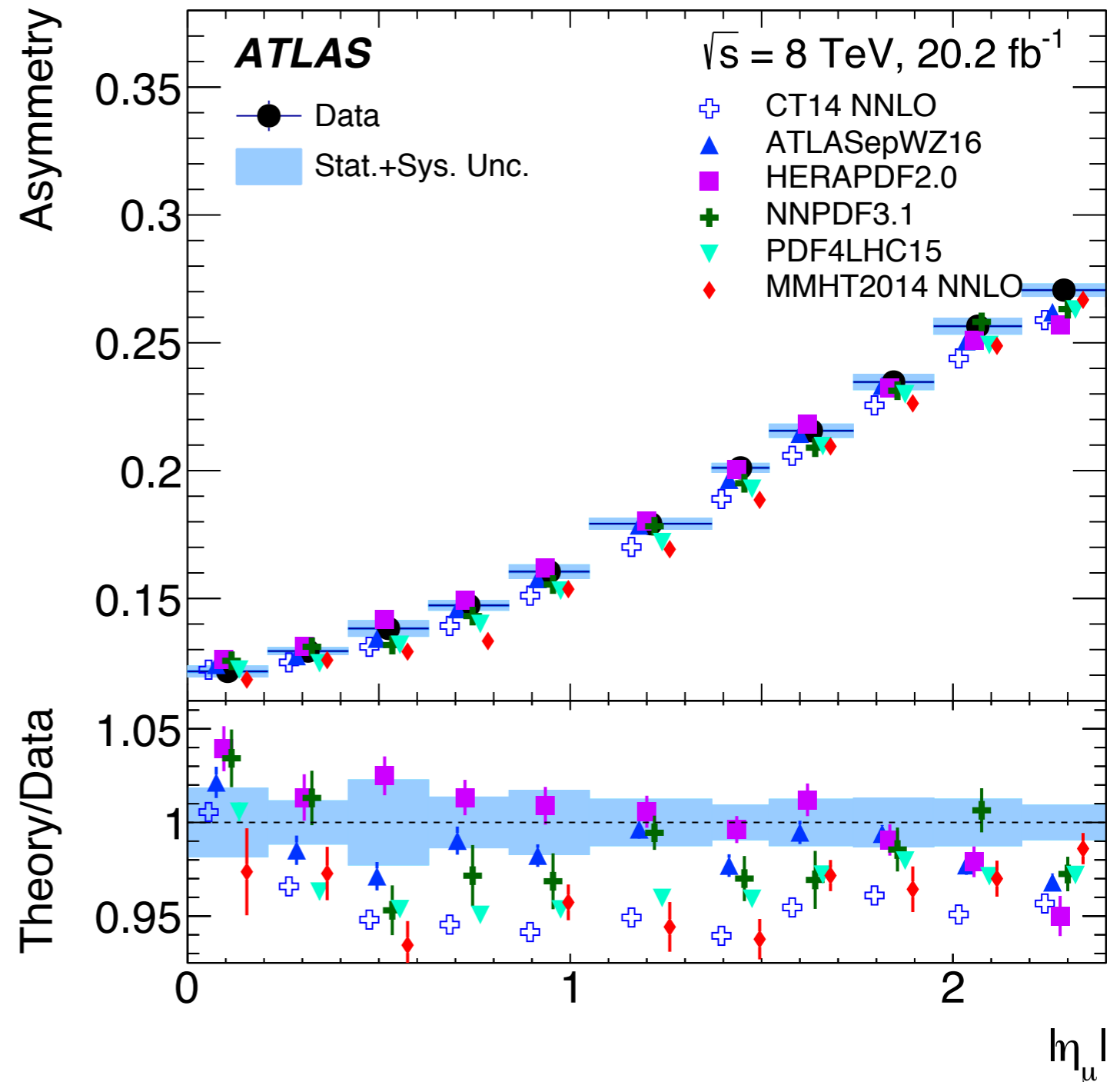
39

W +jets is a precise probe of the u/d content of the proton.

At a pp collide, more W^+ than W^-

$$A_\mu = \frac{d\sigma_{W_{\mu^+}}/d\eta_\mu - d\sigma_{W_{\mu^-}}/d\eta_\mu}{d\sigma_{W_{\mu^+}}/d\eta_\mu + d\sigma_{W_{\mu^-}}/d\eta_\mu}$$

Why not 1/3?



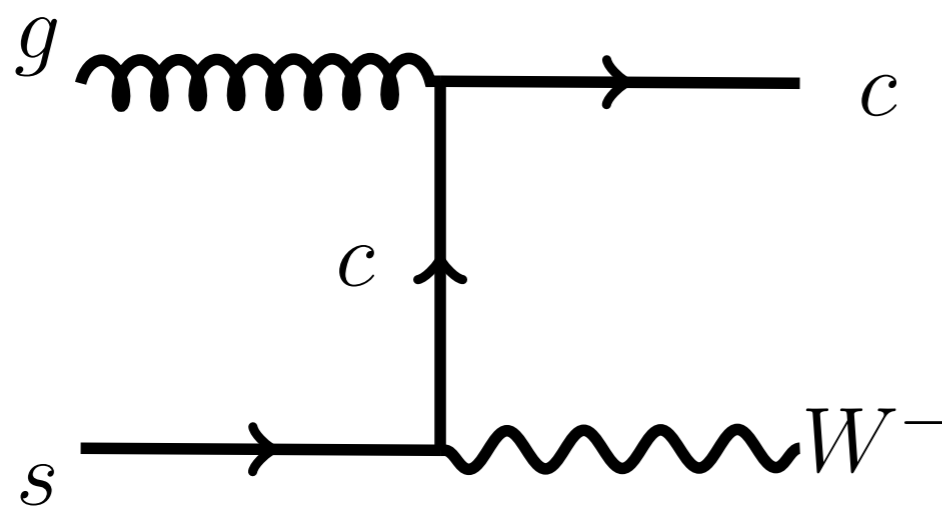
Heavier quarks

40

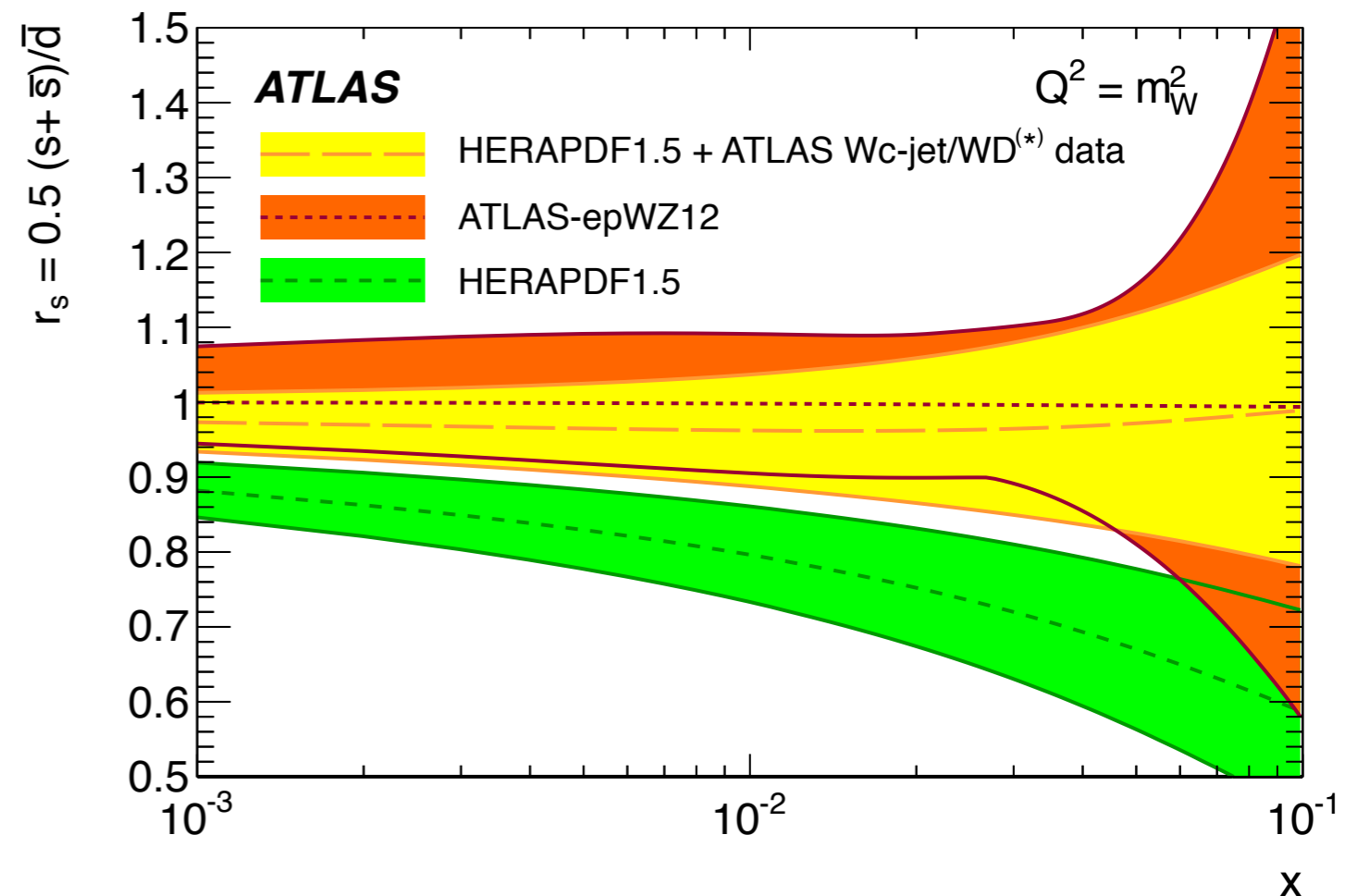
Various measurements are constructed to be sensitive to the s-, c-, and even b-component of the proton.

For example, W^+ -charm measurement can constrain the sea strangeness.

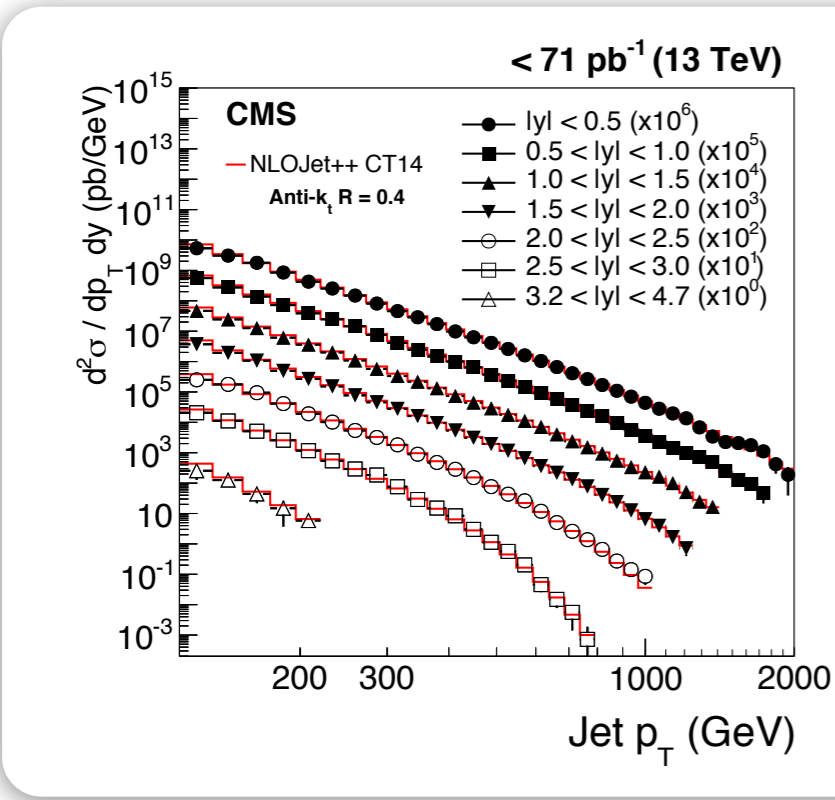
(ATLAS and to a lesser extent CMS find $s \sim$ other sea contributions)



Question: how would you identify the c -quark?



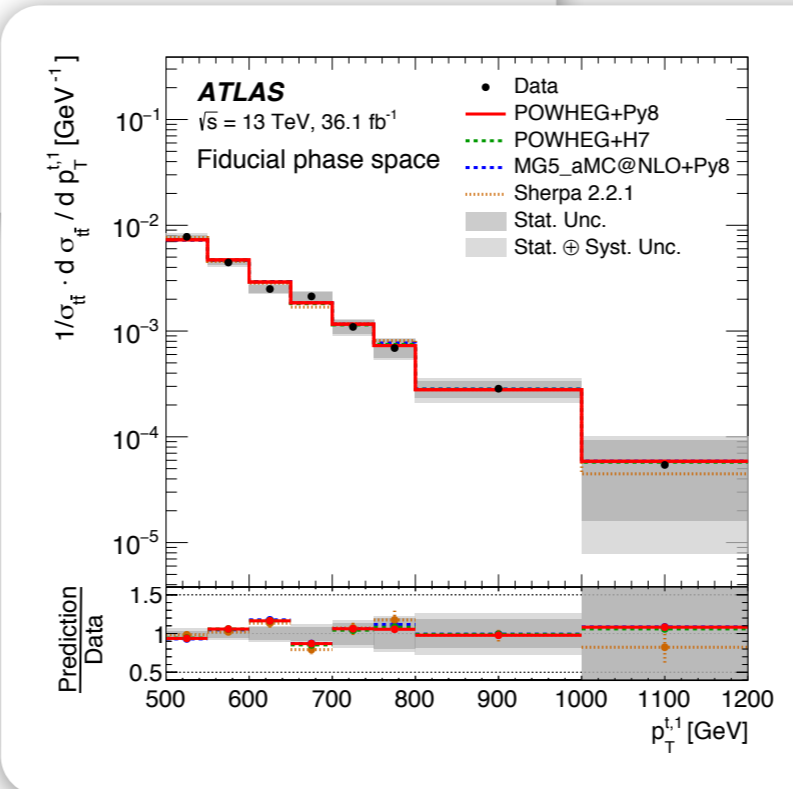
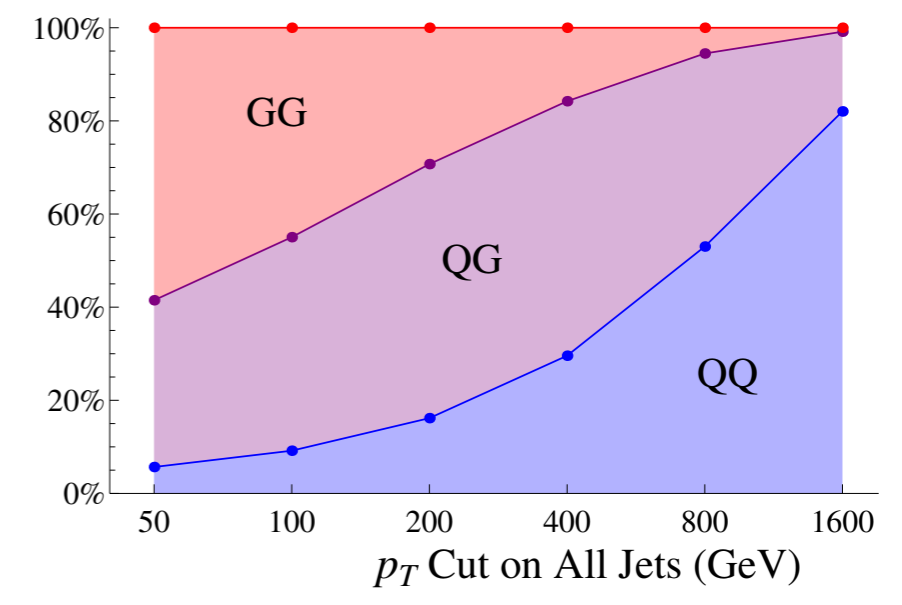
Gluon PDF at moderate - high x is constrained by two sources:



Dijets

High stats, ~10% precision across a wide kinematic range

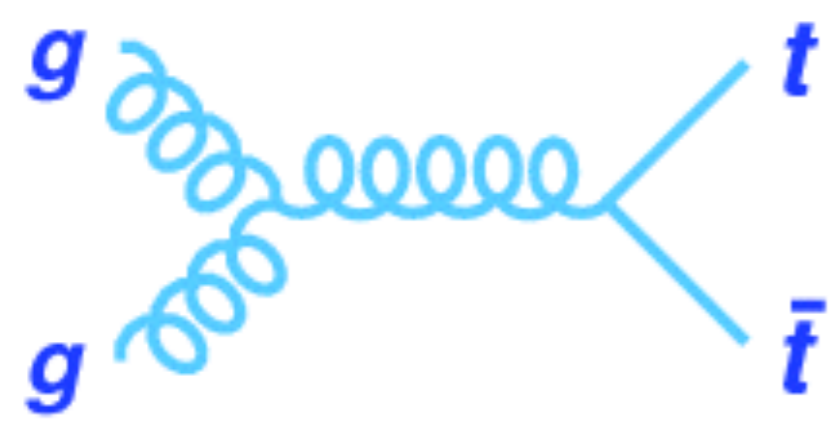
small gg/qg fraction at high jet p_T



Top quark pairs

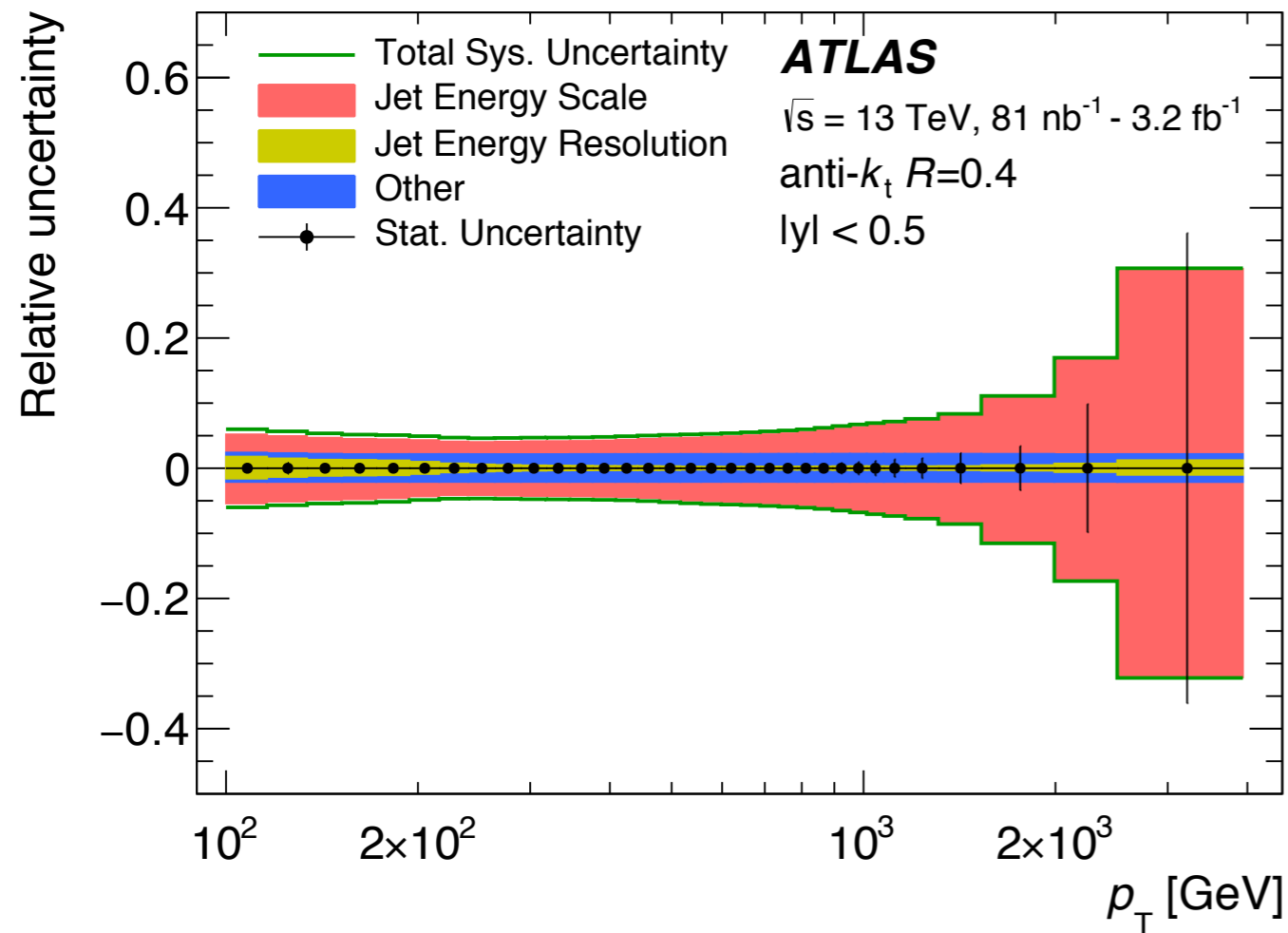
Dominated by gg initial state

run out of statistics much earlier than inclusive jets



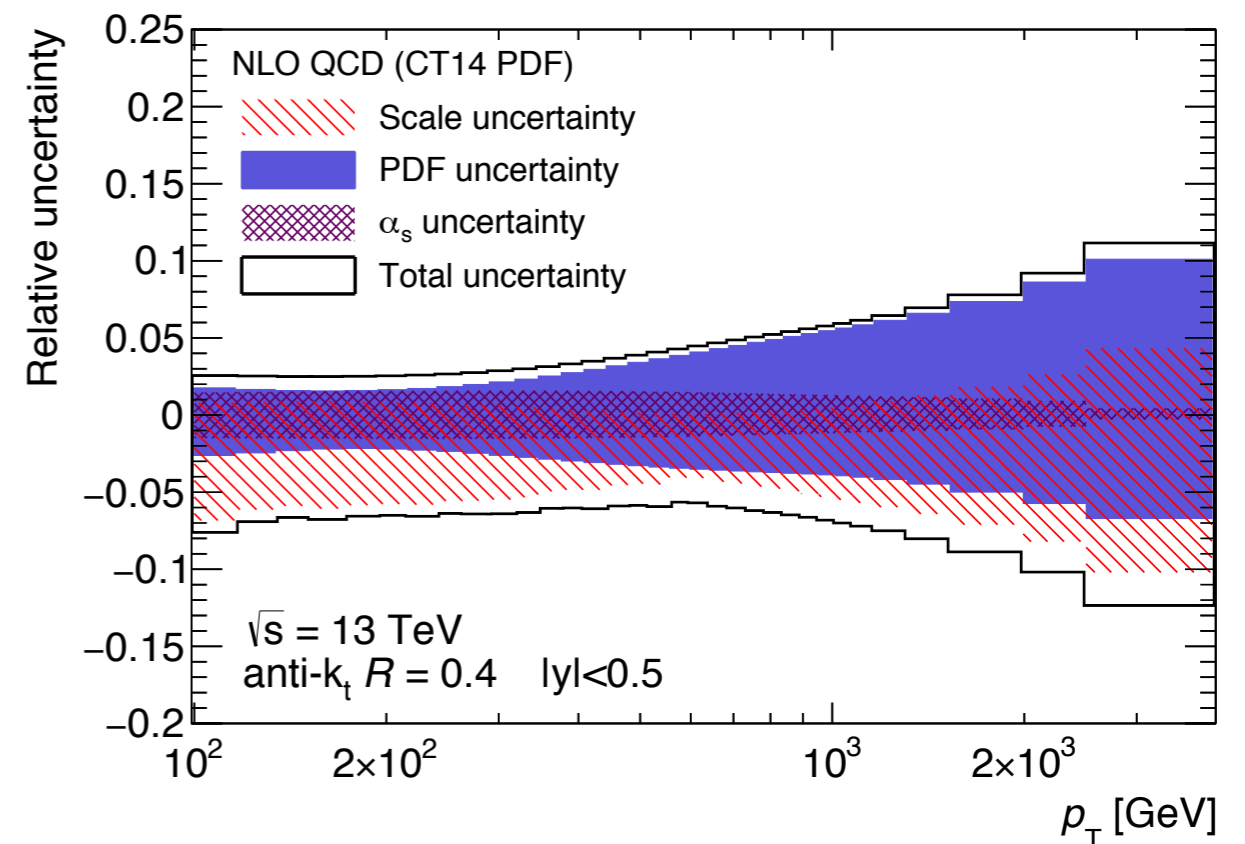
Dijets (gluons at low p_T , quarks at high p_T)

42

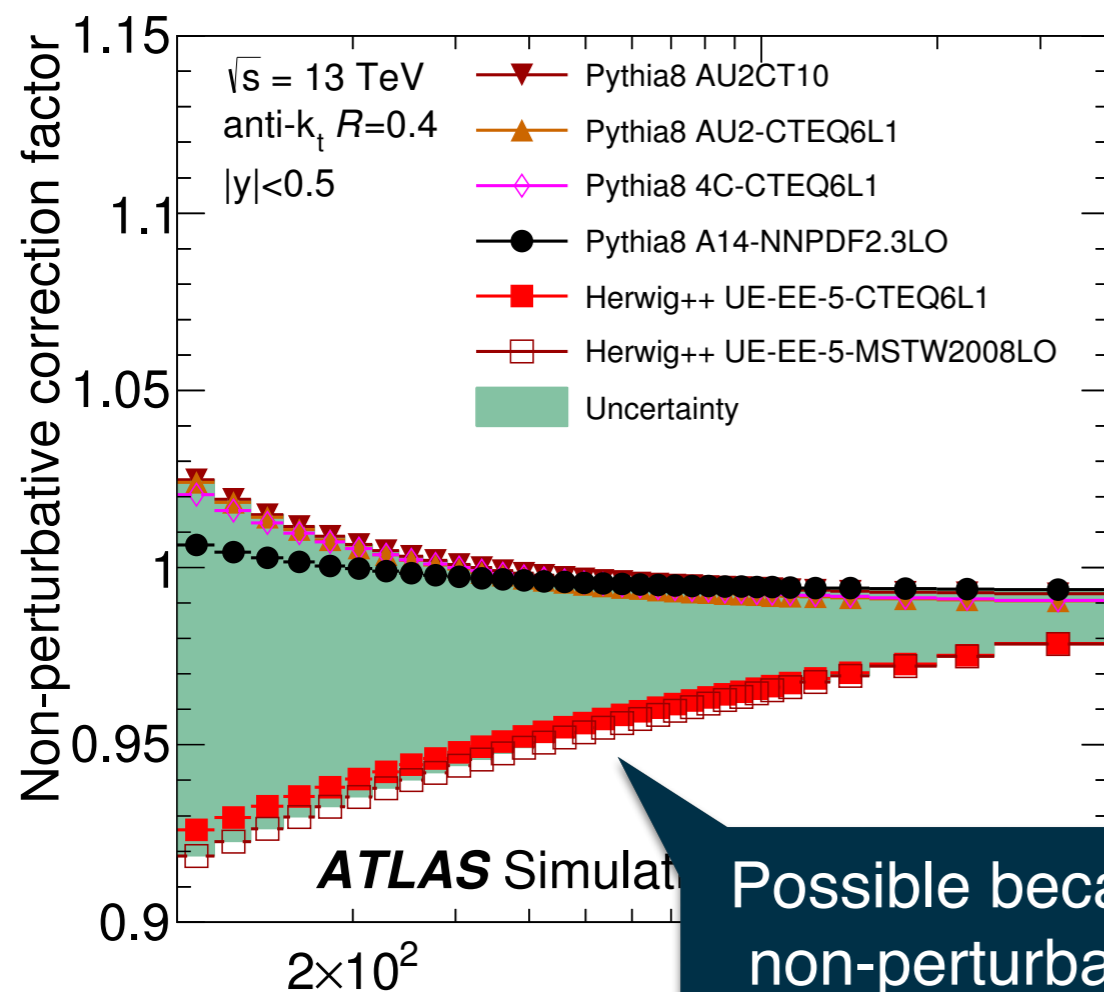


The PDF uncertainty is comparable to the measurement uncertainty at $\sim O(100)$ GeV
→ constraining power!

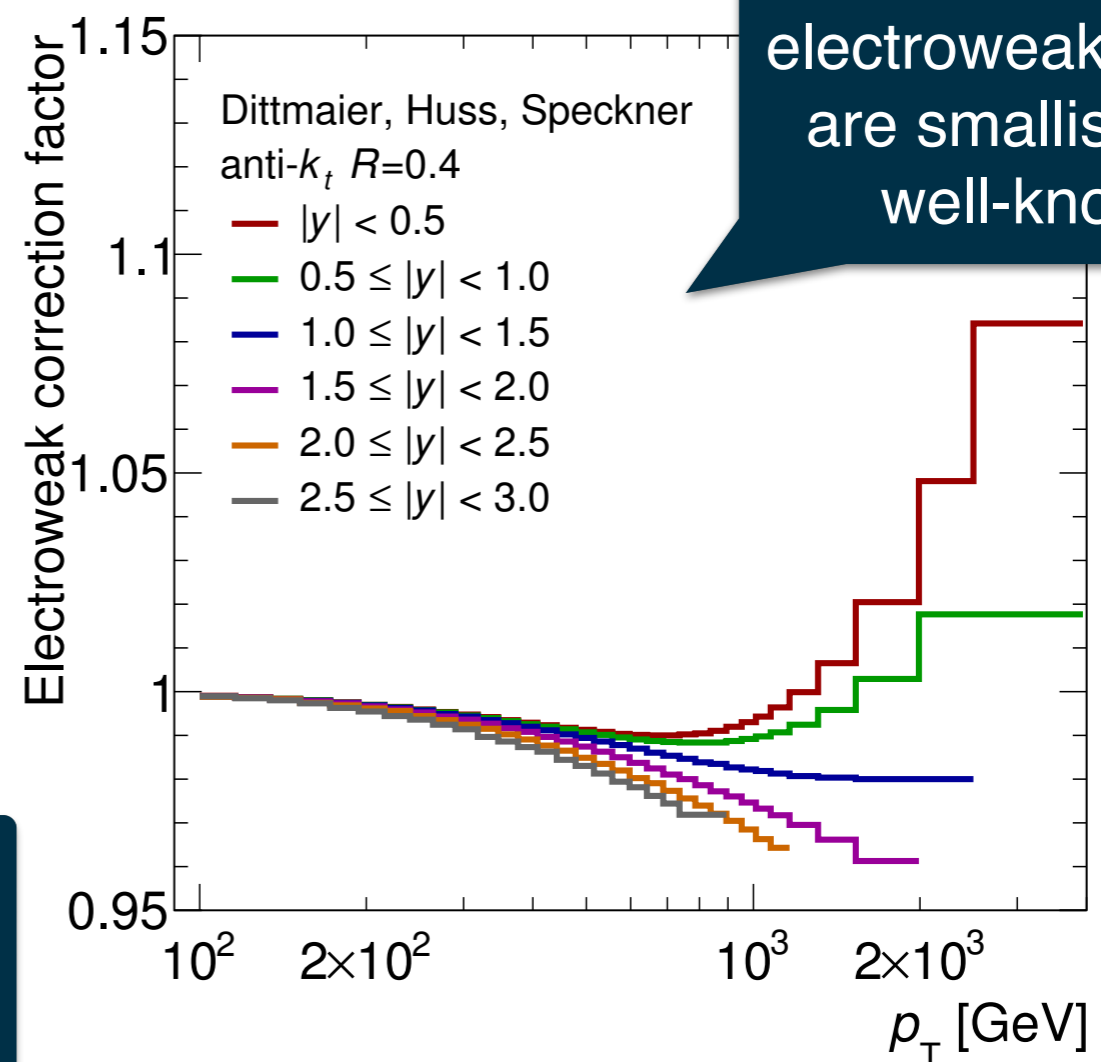
If the energy uncertainty is 1%, why is the cross-section uncertainty much larger?



Precise measurements and predictions can do more than provide input to PDFs - they also provide a powerful consistency test of QCD in new energy regimes.



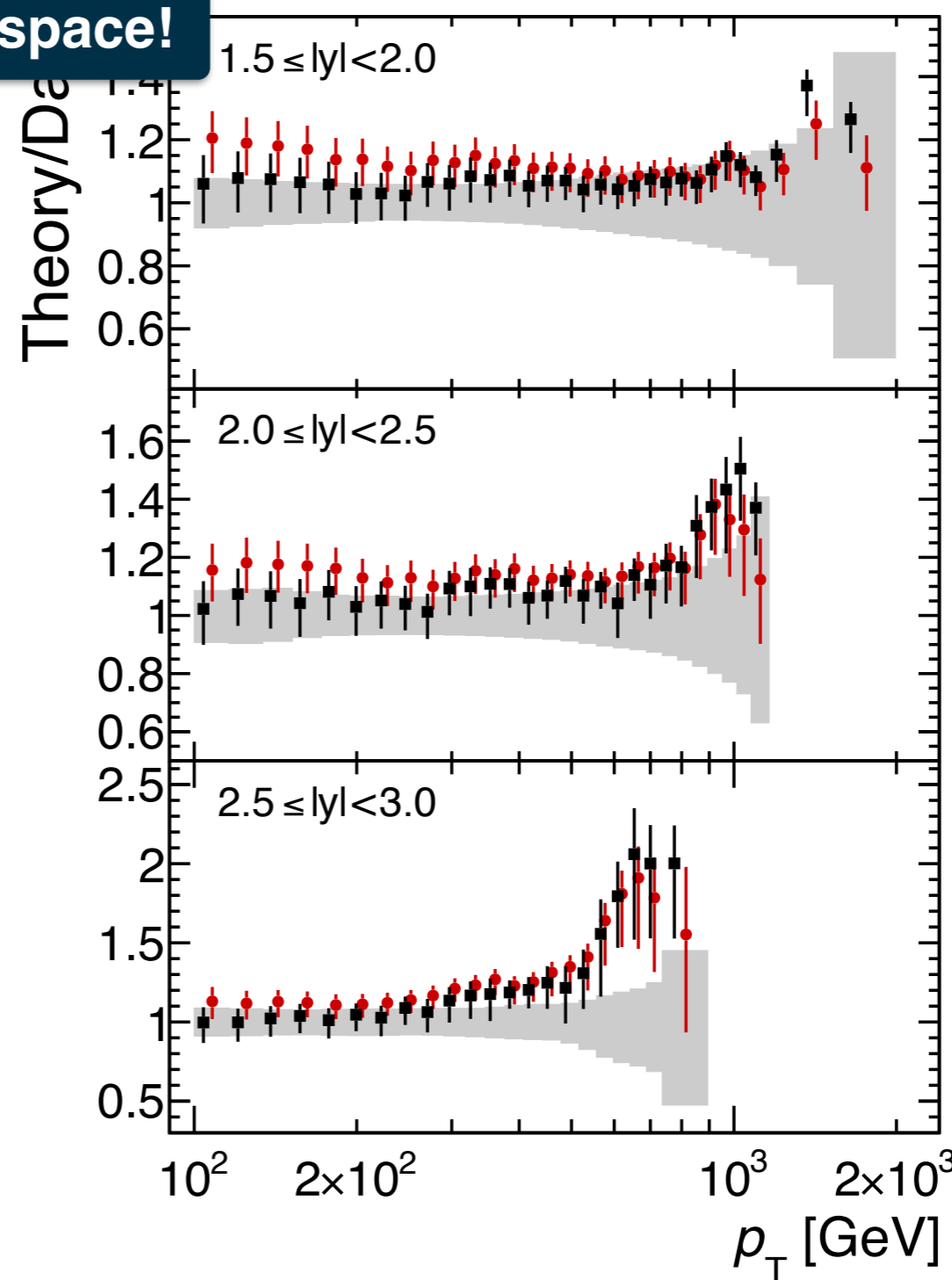
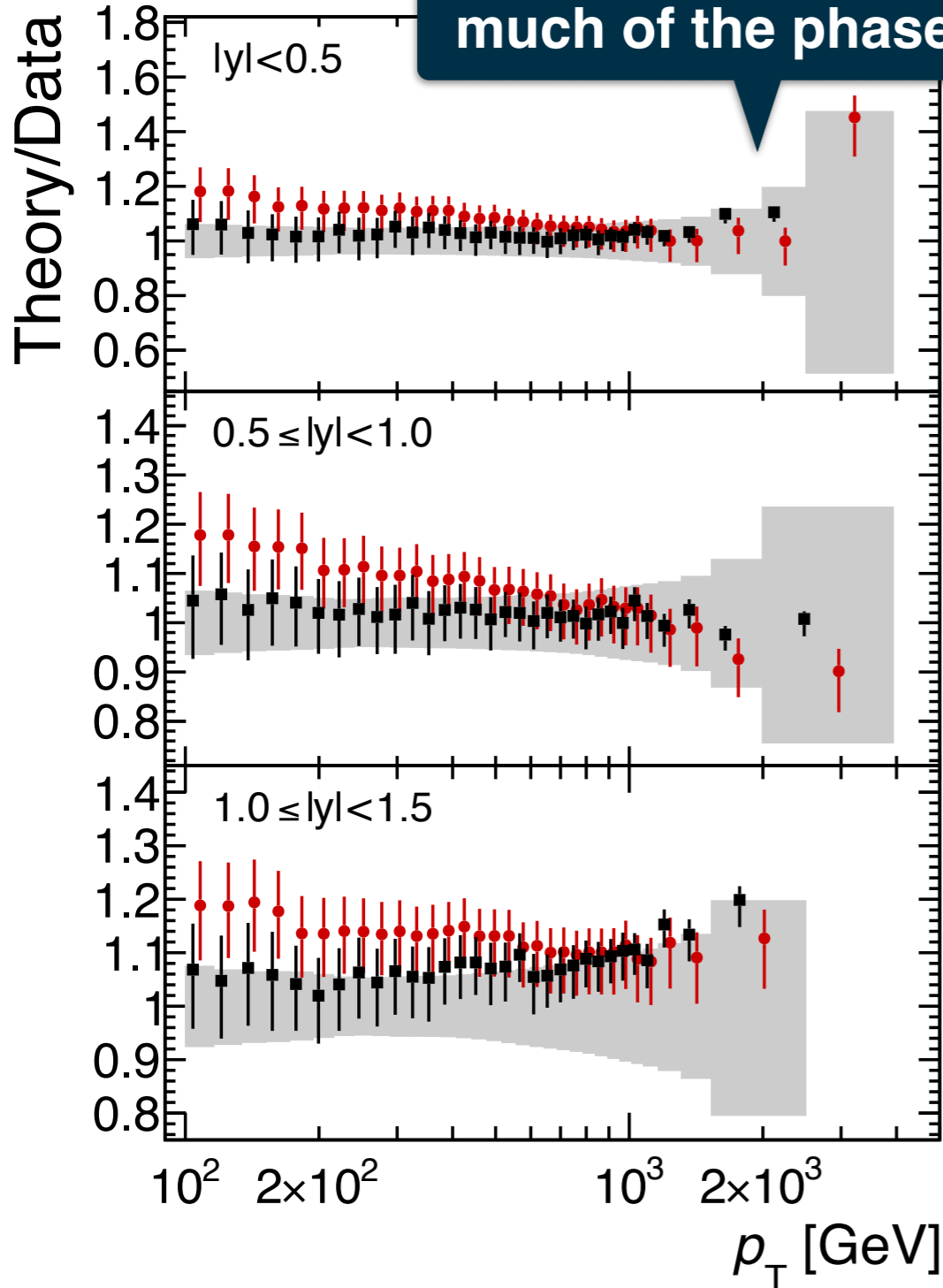
Possible because non-perturbative effects are small



Possible because electroweak effects are smallish and well-known

Fixed-order pQCD

Impressive agreement over much of the phase space!



ATLAS

$L = 81 \text{ nb}^{-1} - 3.2 \text{ fb}^{-1}$

$\sqrt{s} = 13 \text{ TeV}$

anti- k_t $R=0.4$

■ Data

NLO QCD

⊗ k_{EW} ⊗ k_{NP}

NNLO QCD

⊗ k_{EW} ⊗ k_{NP}

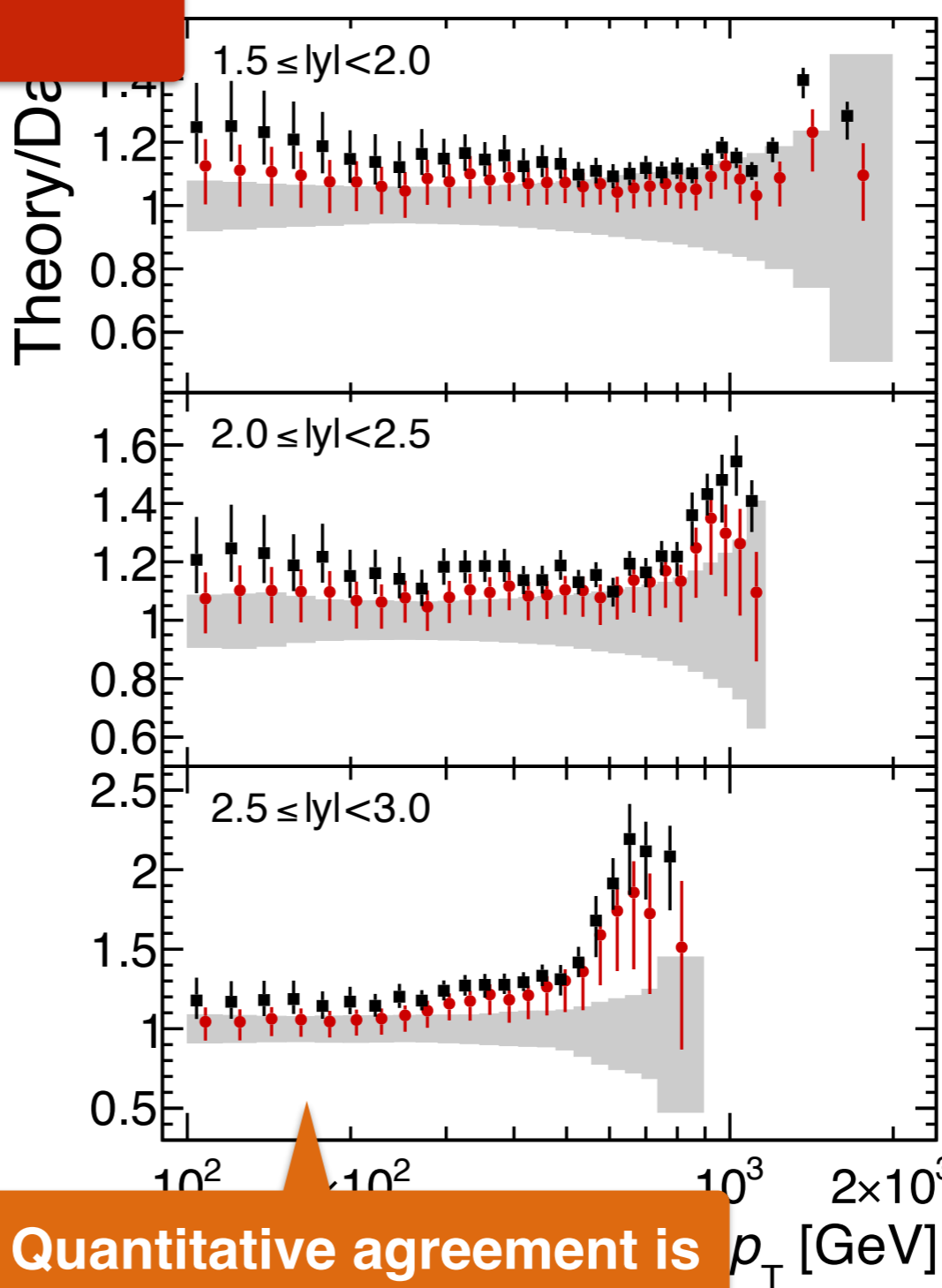
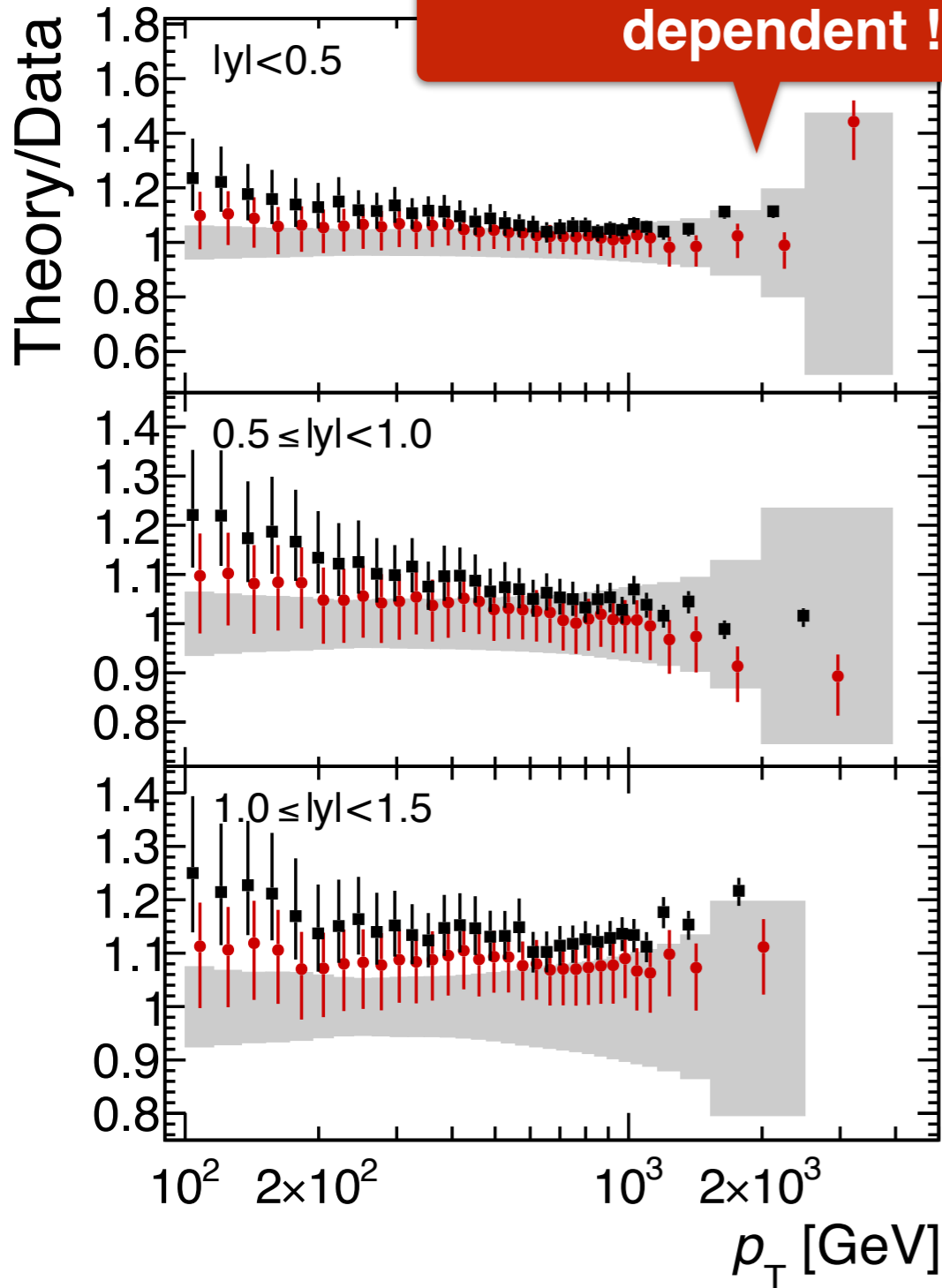
$\mu_R = \mu_F = p_T^{\text{jet}}$

● NLO
MMHT 2014 NLO

■ NNLO
MMHT 2014 NNLO

Fixed-order pQCD

Caution: story is scale-dependent !!



Quantitative agreement is less good for all y-bins.

ATLAS

$L = 81 \text{ nb}^{-1} - 3.2 \text{ fb}^{-1}$

$\sqrt{s} = 13 \text{ TeV}$

anti- k_t $R=0.4$

■ Data

● NLO QCD

⊗ k_{EW} ⊗ k_{NP}

■ NNLO QCD

⊗ k_{EW} ⊗ k_{NP}

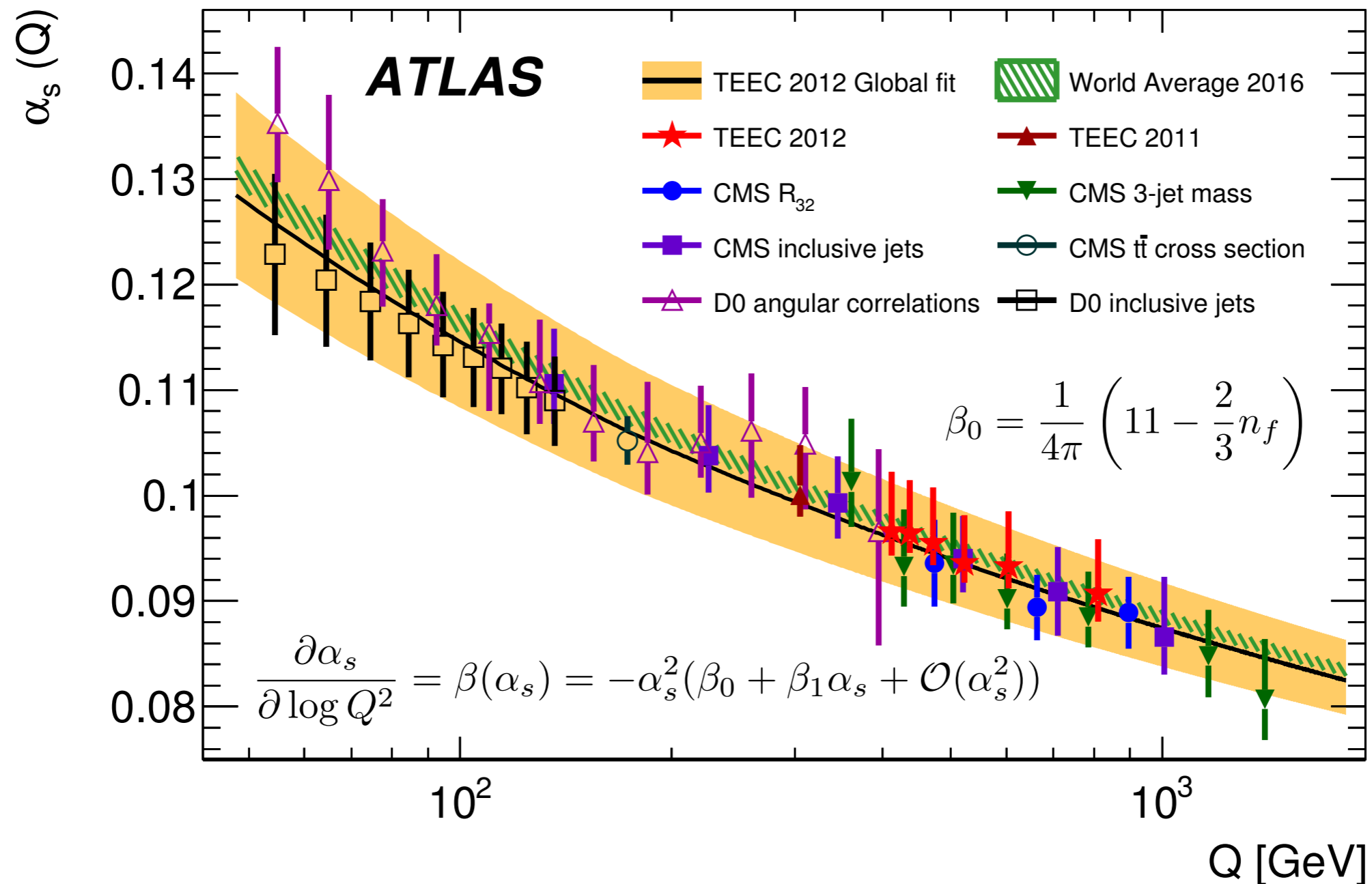
$\mu_R = \mu_F = p_T^{\max}$

● NLO
MMHT 2014 NLO

■ NNLO
MMHT 2014 NNLO

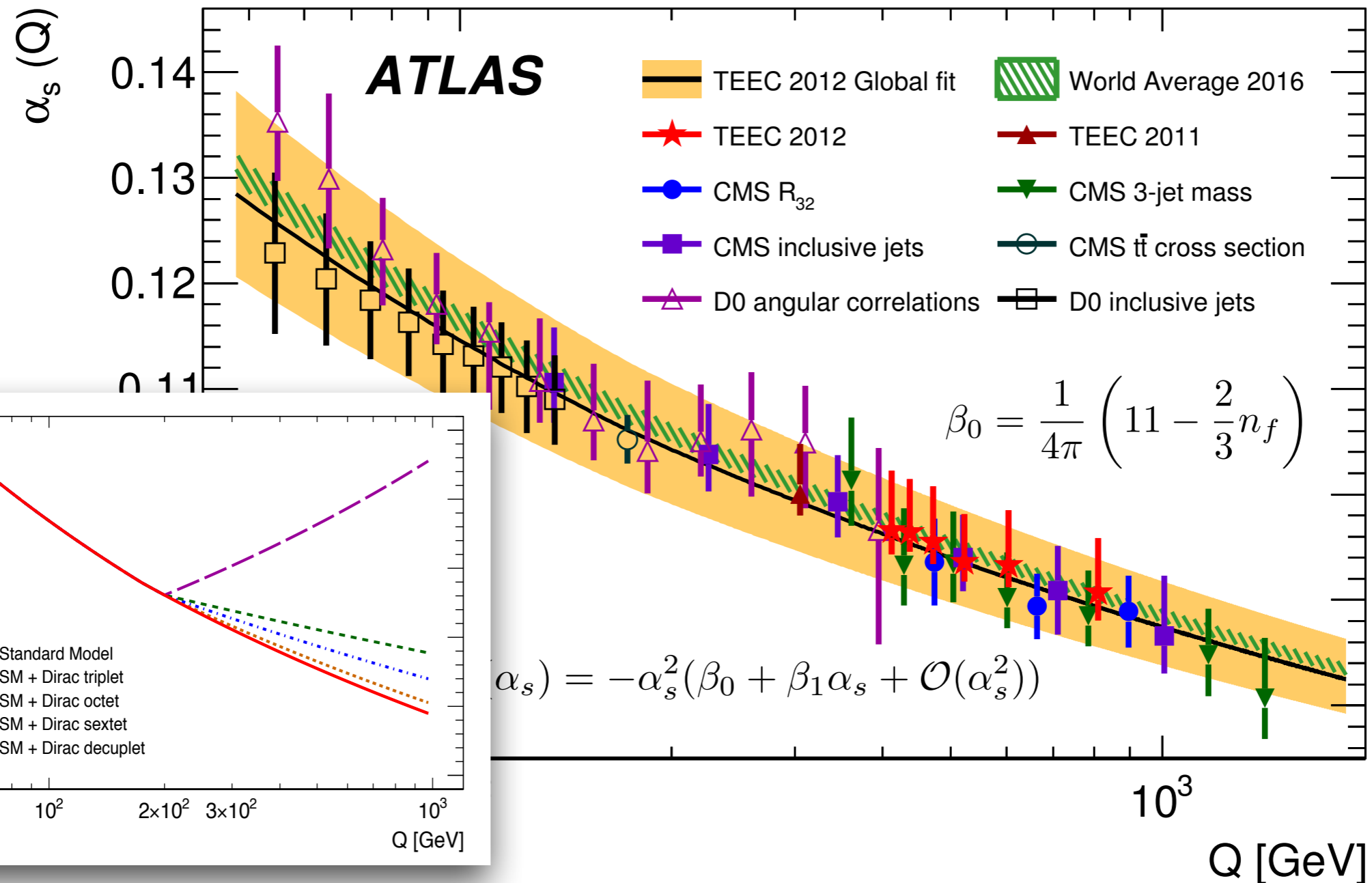
Strong coupling constant

Scale challenges aside, one can use these data to test the running of the strong coupling at the highest energies.



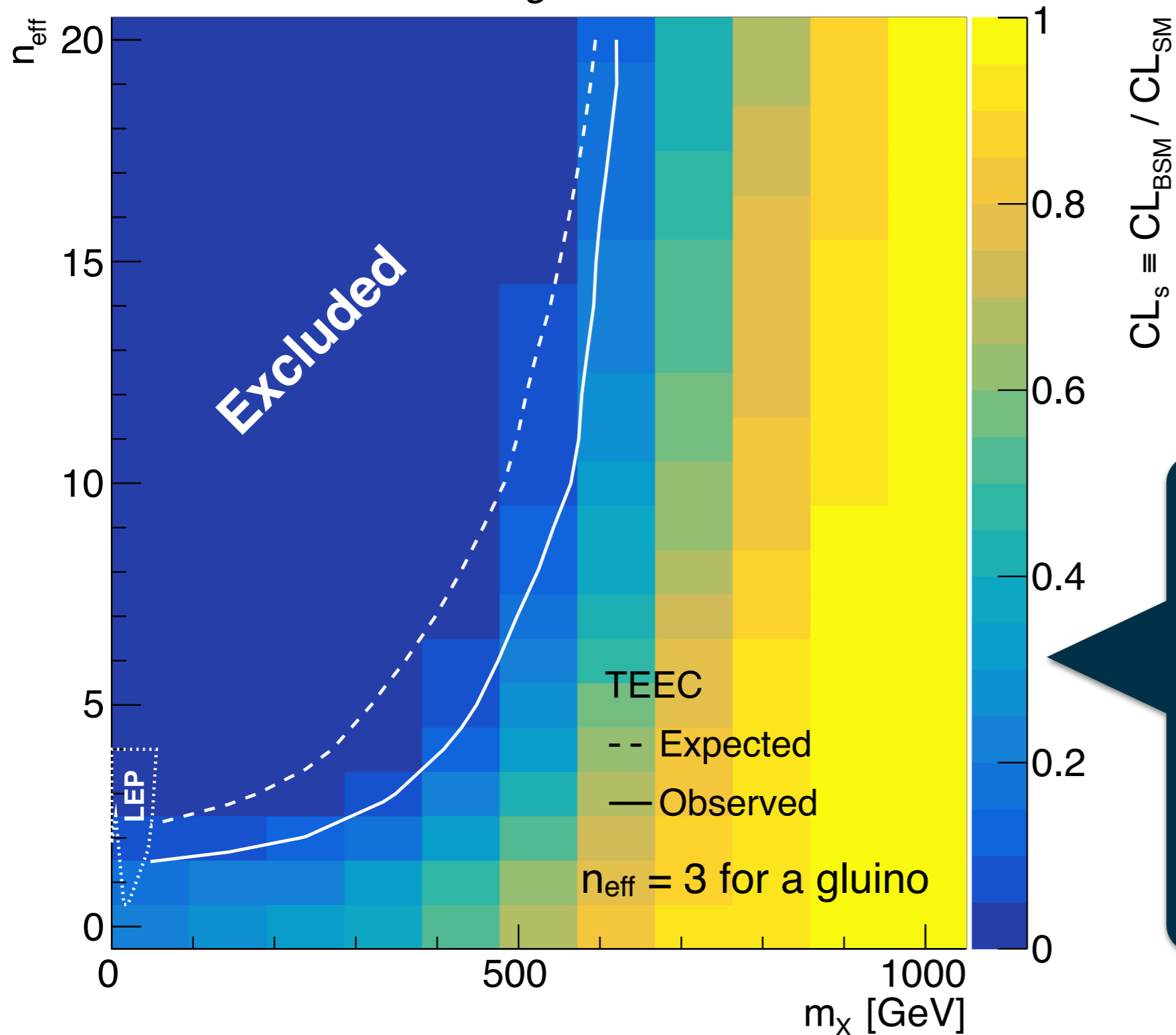
Strong coupling constant

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BSM from the running of α_s

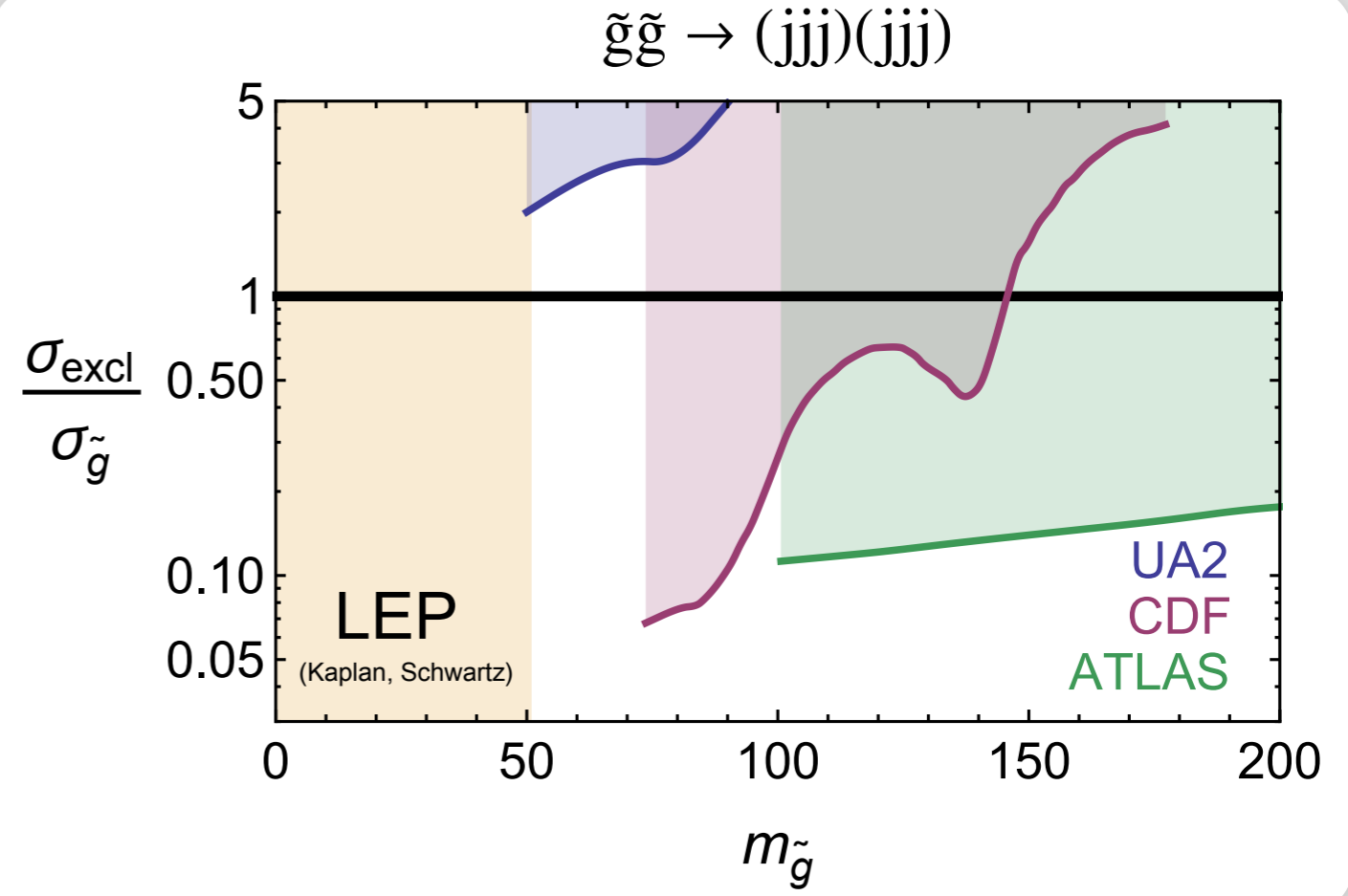
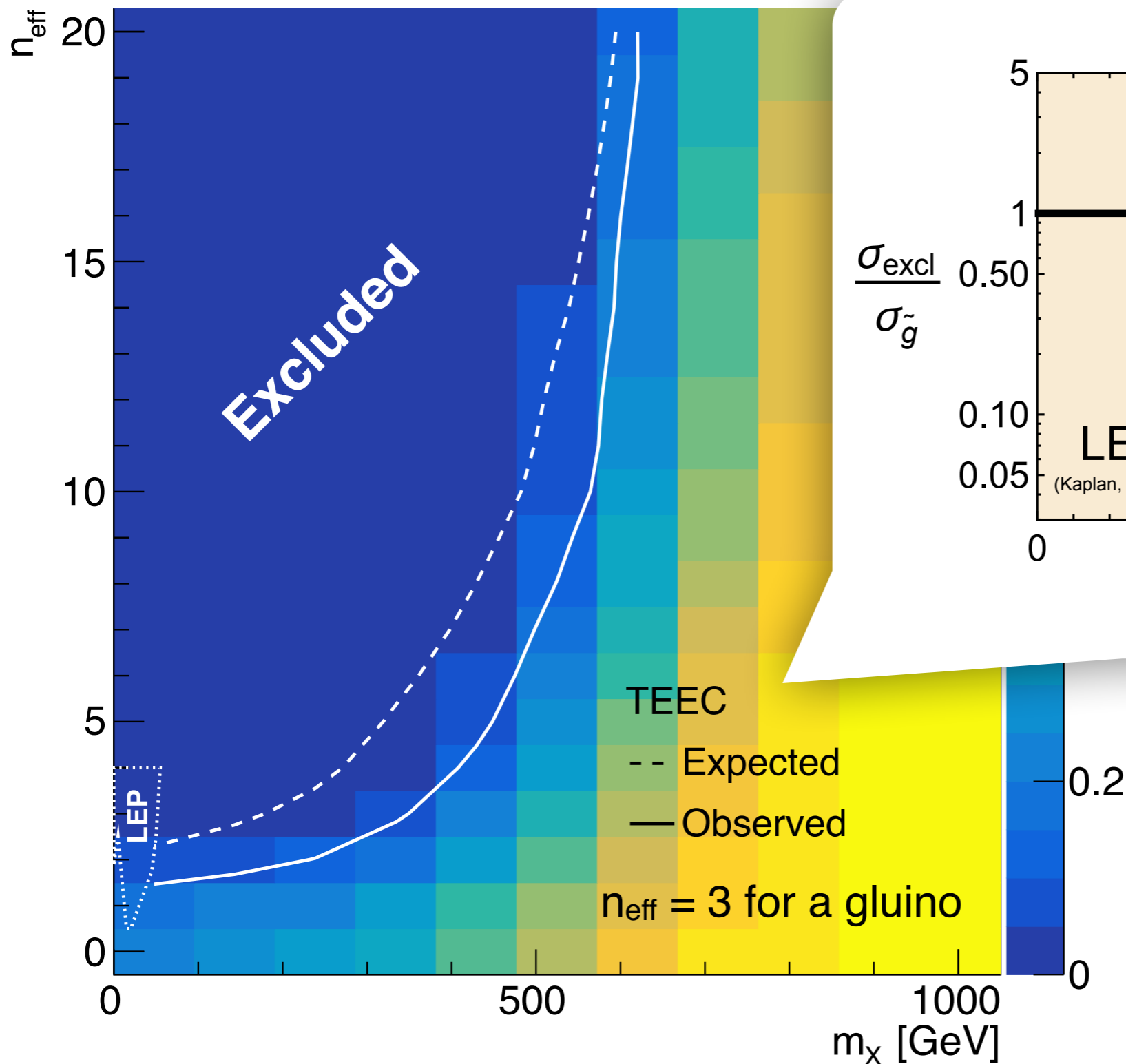
New fermion limits using NLOJet++ & ATLAS data



Complimentary to direct searches because \sim agnostic to the decay of the new particles.

BSM from the running of α_s

New fermion limits using NLOJet++ & ATLAS data

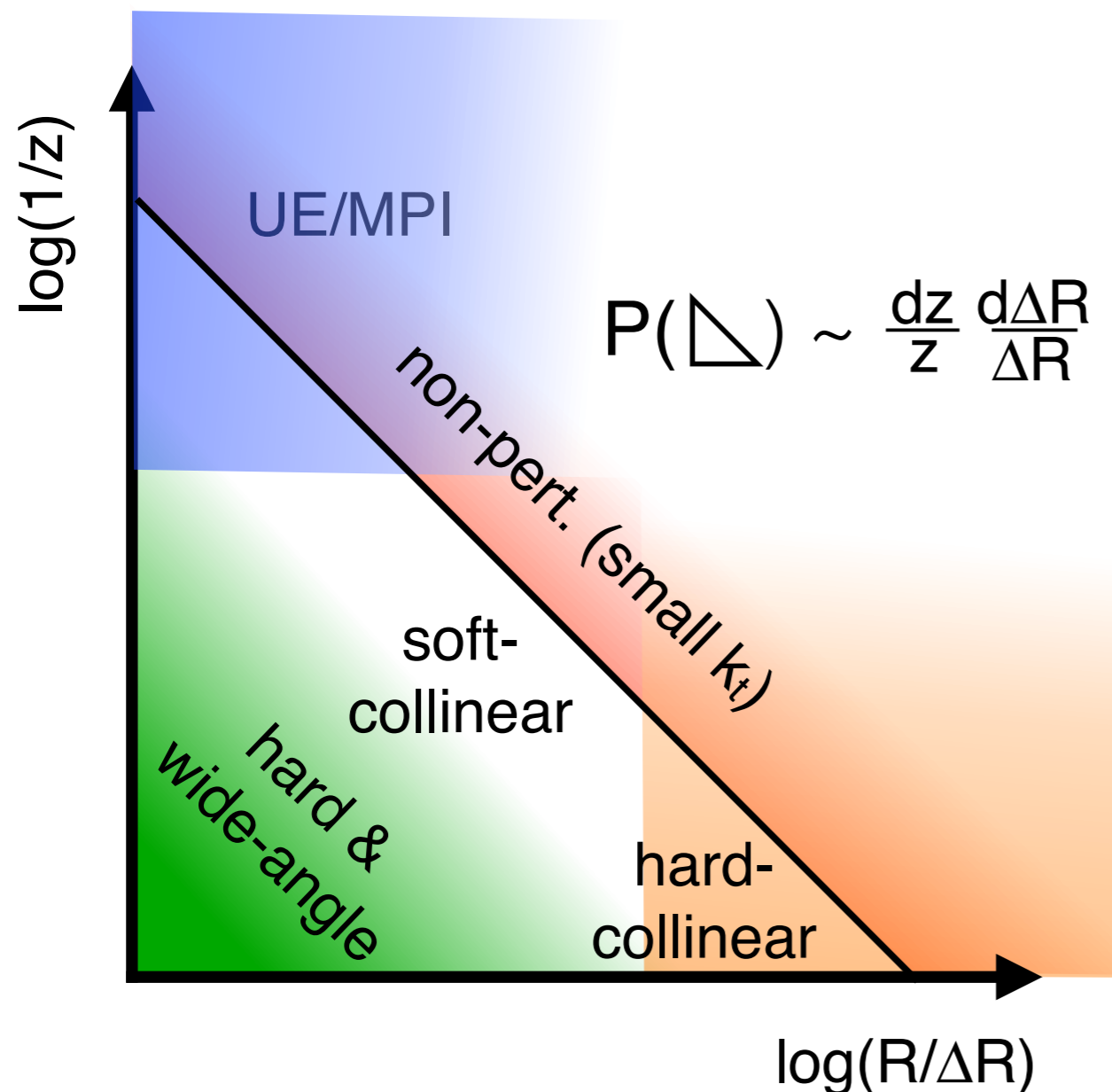


Even though direct limits are $O(\text{TeV})$, there may be some gaps at low mass that techniques like this can probe.

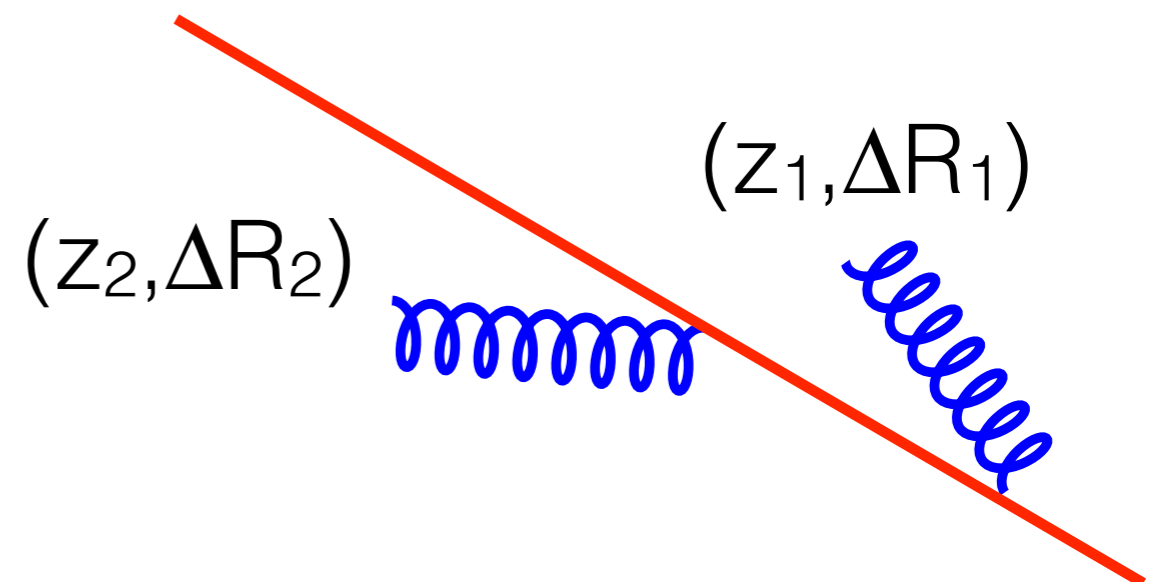
Resummed pQCD and jet substructure

50

Well-separated jets can be described by fixed-order pQCD but the radiation pattern **inside jets** requires resummation.



A useful way of thinking about radiation inside the jet is in the context of the *Lund plane*



Well-separated jets can be described by fixed-order pQCD but the radiation pattern inside jets requires resummation.

For example, the jet mass is approximately

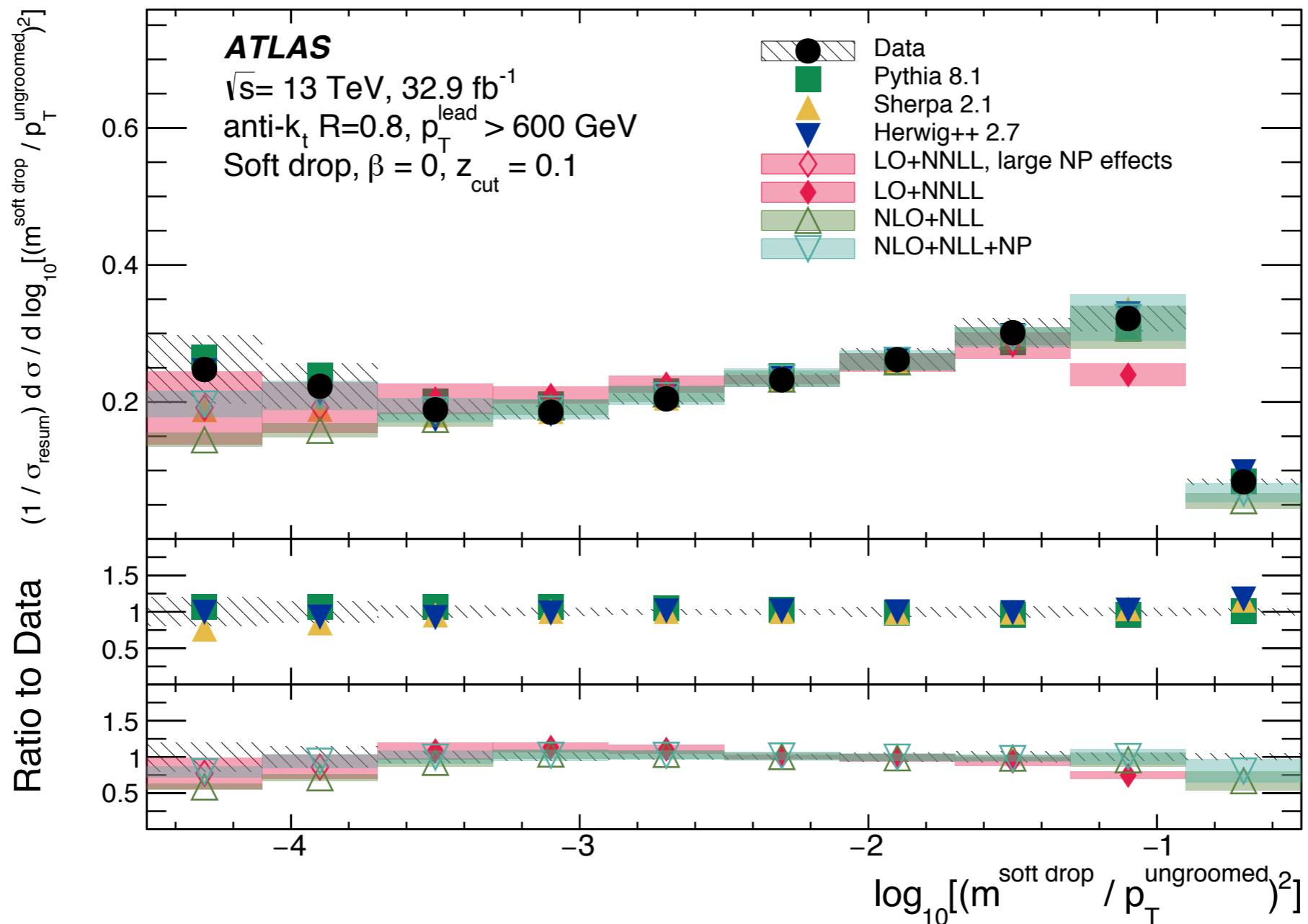
$m^2/p_T^2 \sim z\Delta R^2$ which is a line in the Lund plane:

(where did this come from?)

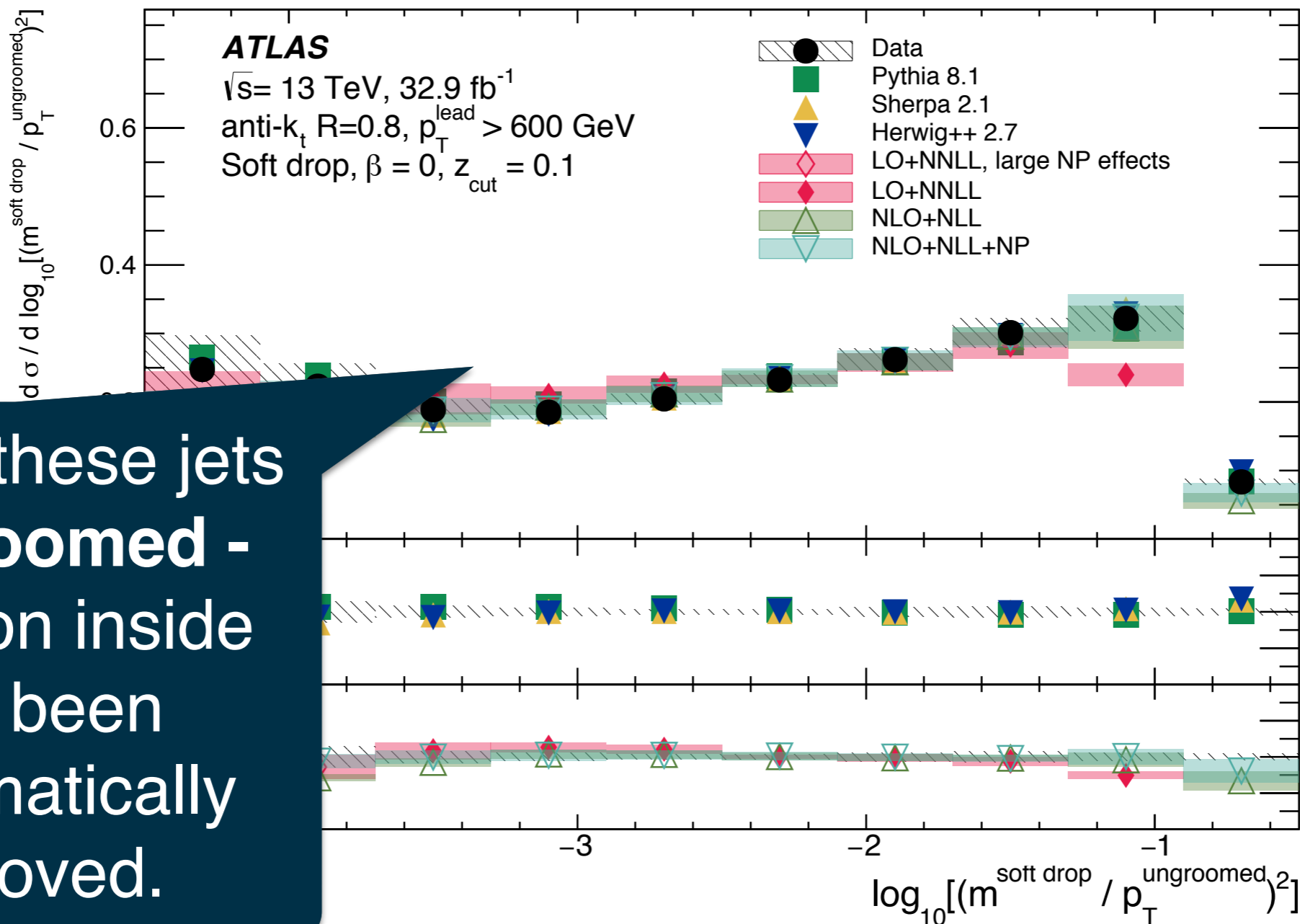
$$\log(1/z) = \text{constant} - 2 \log(R/\Delta R)$$

One can use this to derive the probability distribution at leading logarithm accuracy.

In fact, the jet mass has been calculated to higher accuracy and precisely measured!

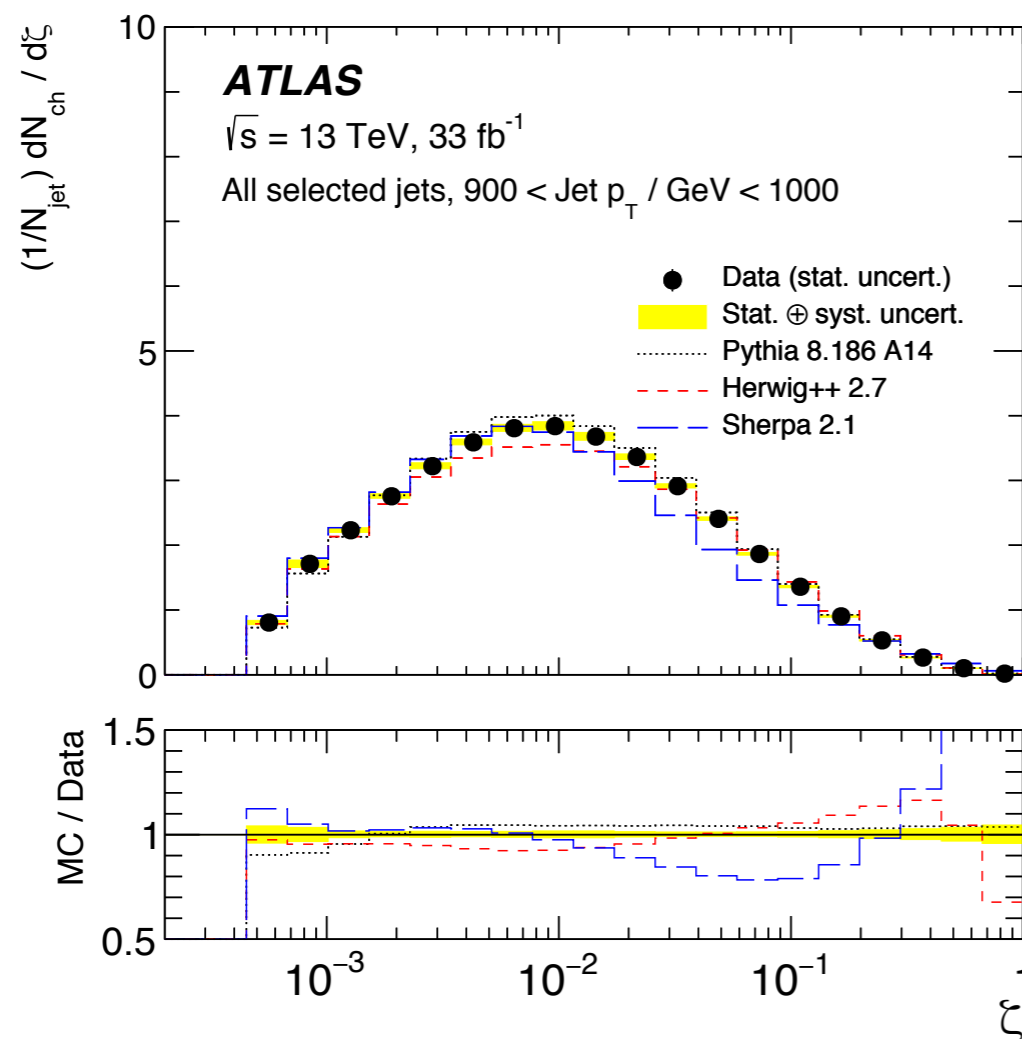


In fact, the jet mass has been calculated to higher accuracy and precisely measured!



Subtly: these jets are groomed - radiation inside has been systematically removed.

While jet substructure nowadays typically refers to observables like the jet mass and Lund plane coordinates, there is a long history of more traditional “fragmentation function” measurements which probe similar physical regimes.

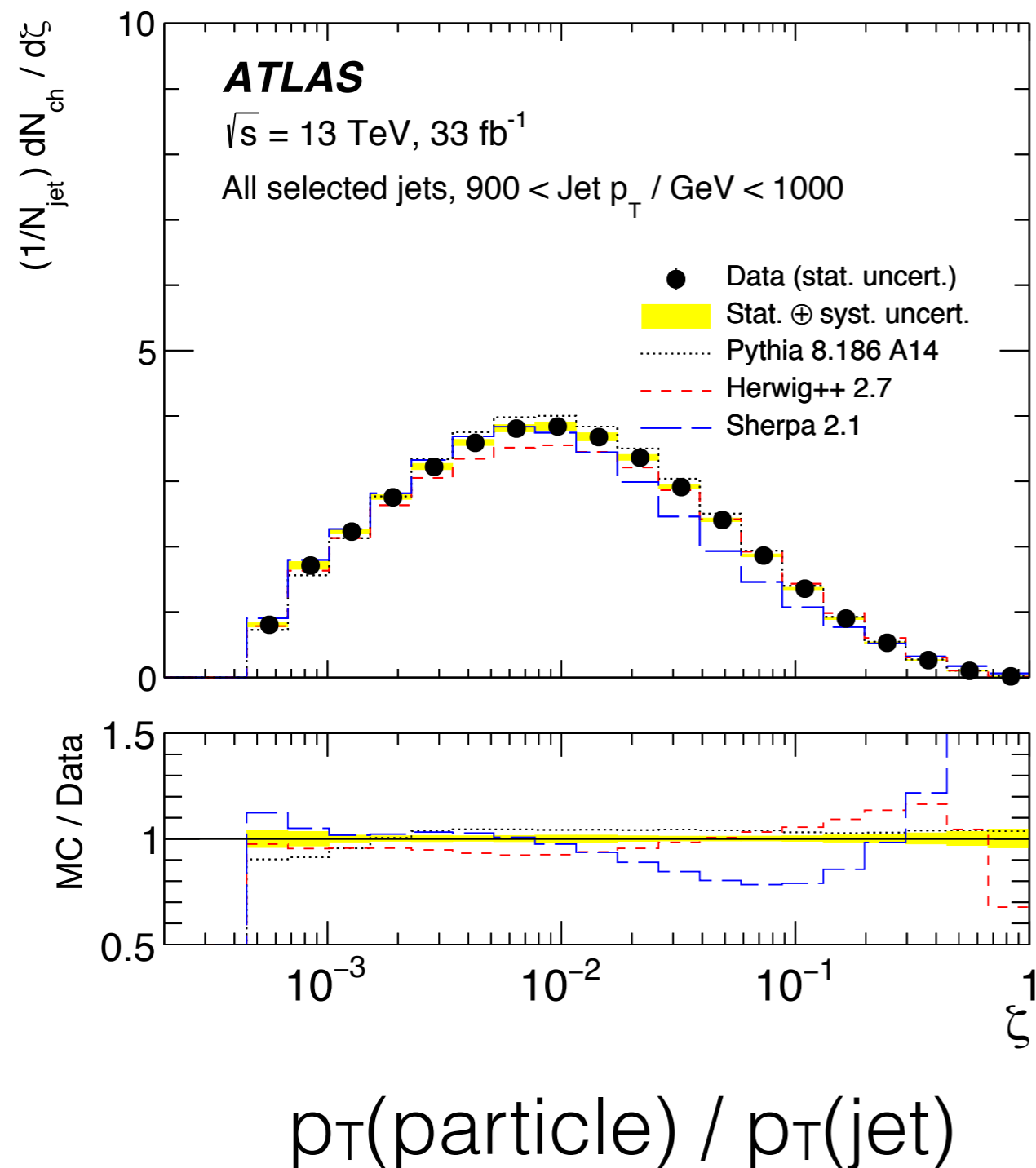


These studies are crucial inputs to tuning Parton Shower Monte Carlo algorithms, but can also be used to study pQCD.

← $p_T(\text{particle}) / p_T(\text{jet})$

Fragmentation: generic q/g jets

55



We can't generally measure individual particles, but we can for charged particles.

With charged-only, we can't predict this distribution from first principles. But for a given jet type (q/g) we can predict how it depend on jet p_T .

How can we extract just the gluon (or quark) contribution?

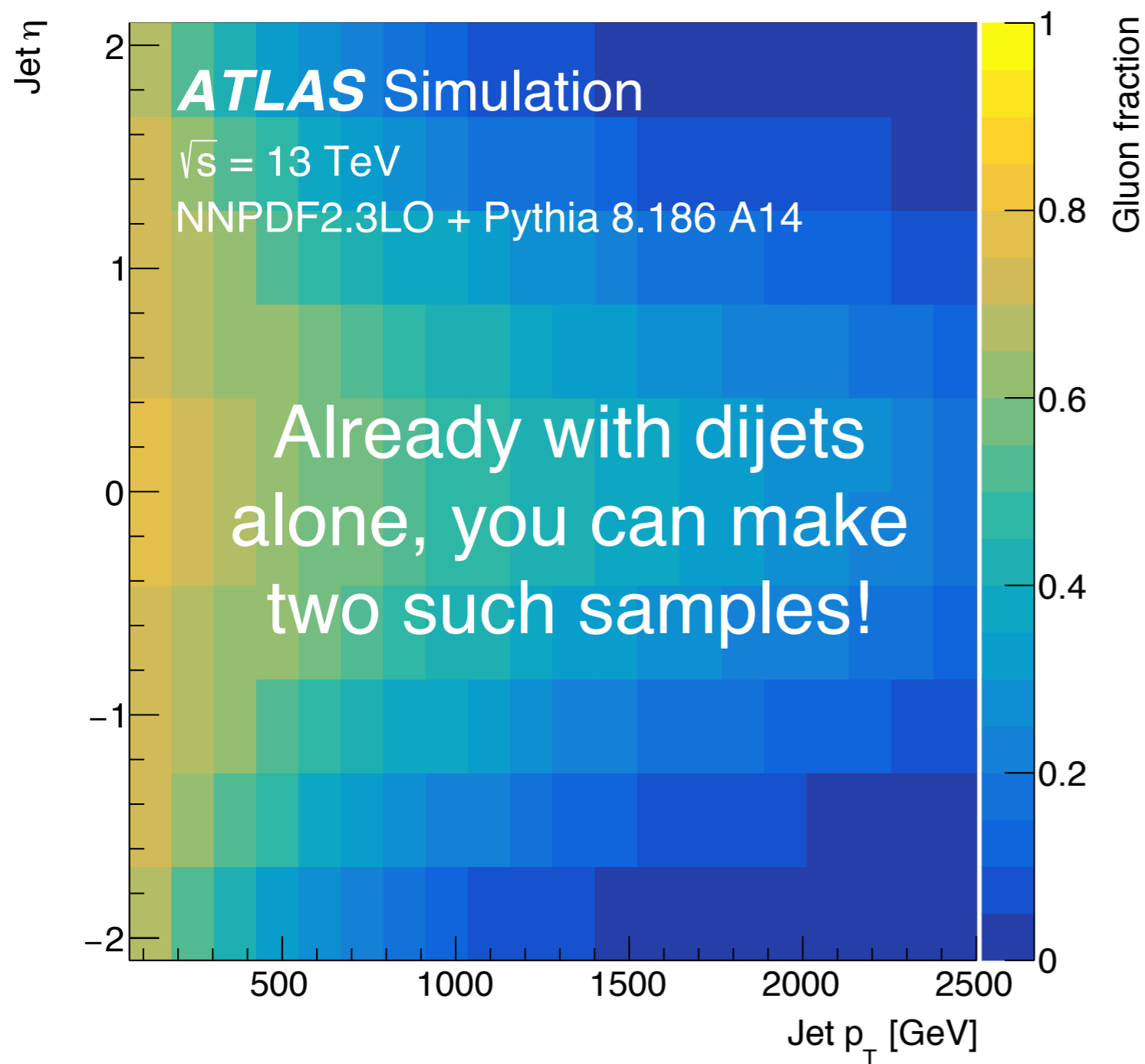
One way is to find two event samples (f and c) with different q/g compositions.

Given the fractions f_q , you can extract the q/g bin contents h :

$$h_i^f = f_q^f h_i^q + (1 - f_q^f) h_i^g$$
$$h_i^c = f_q^c h_i^q + (1 - f_q^c) h_i^g$$

The rapidity trick

57



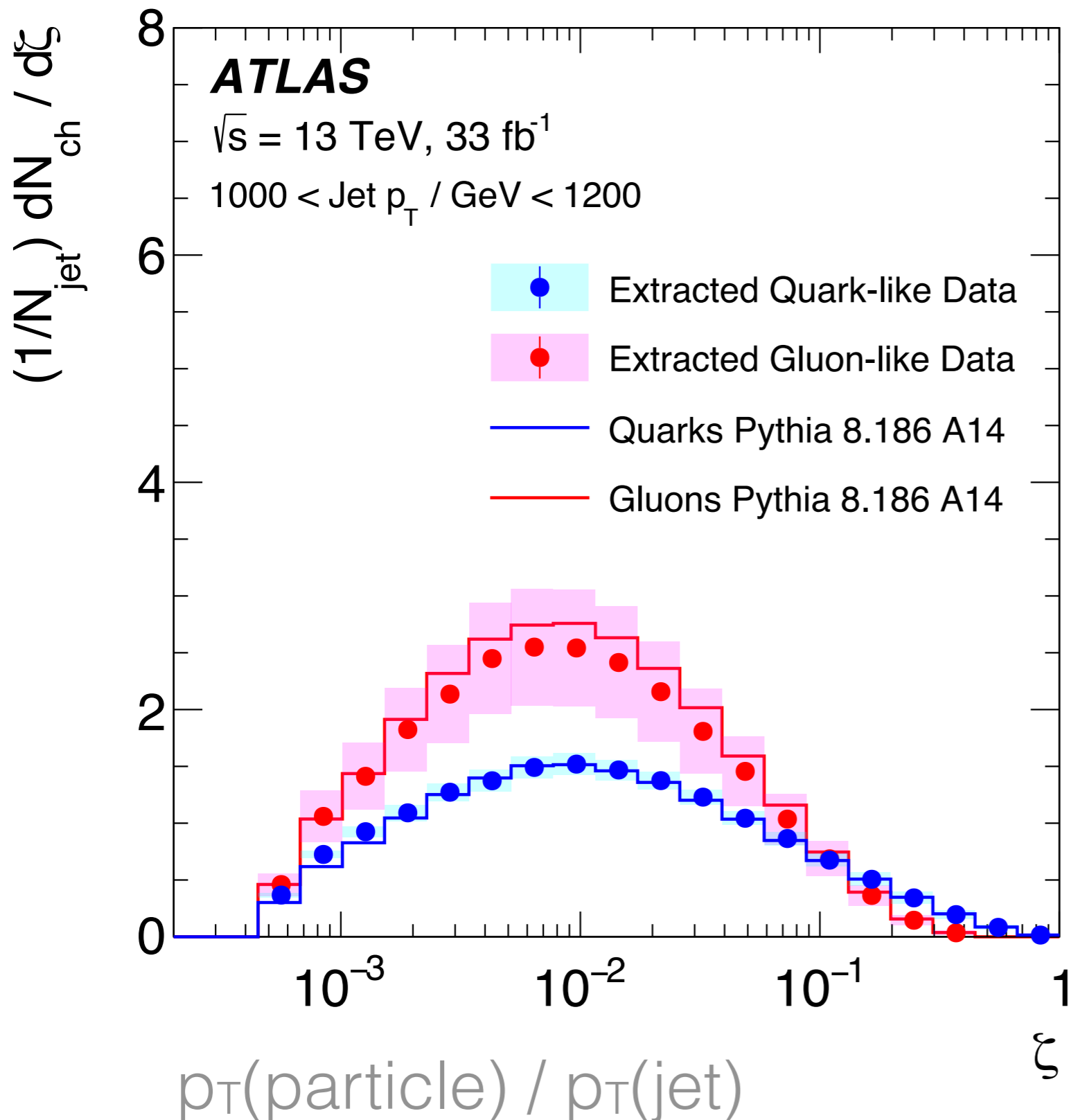
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The rapidity trick

58



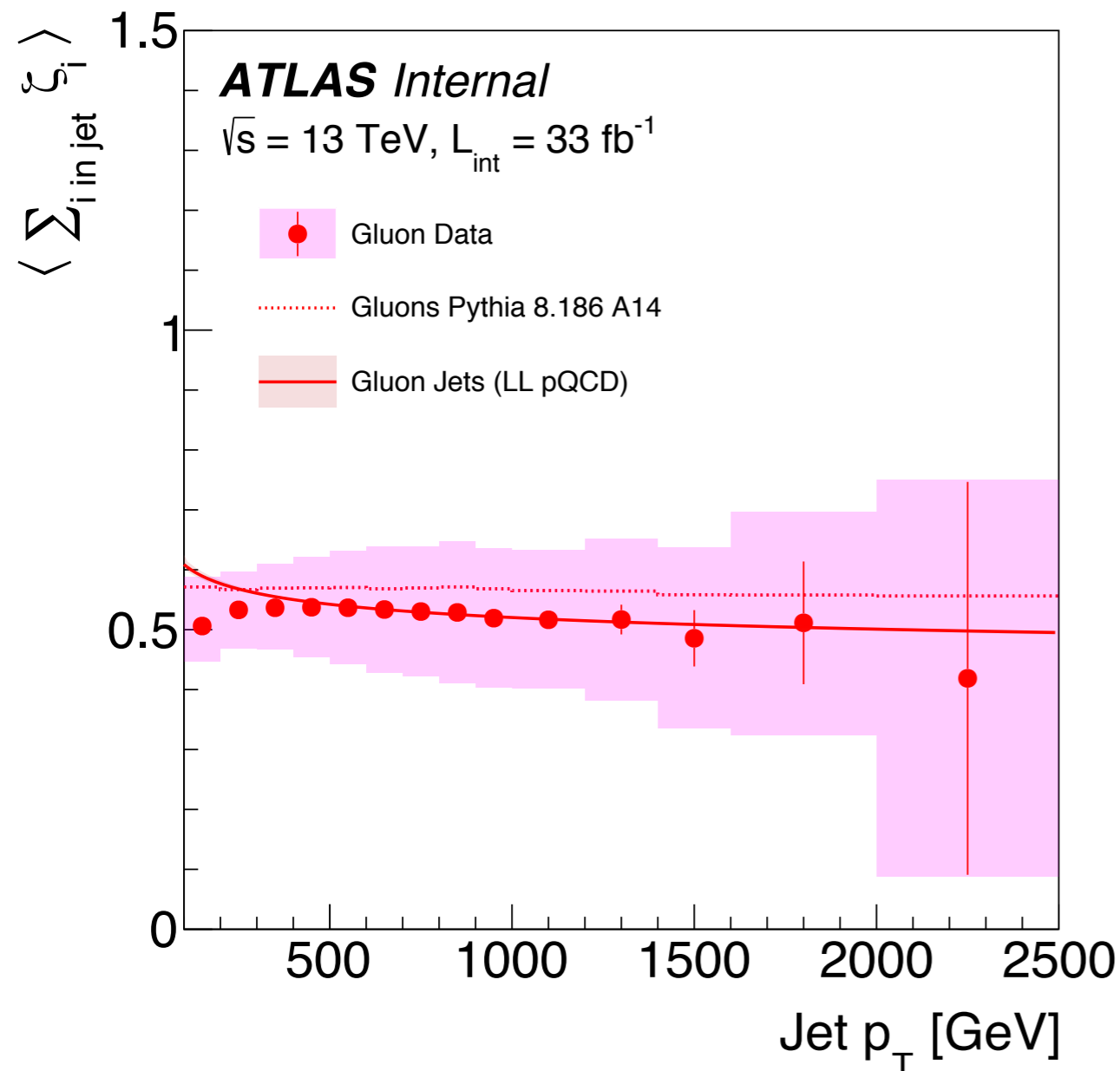
Gluons have more, softer particles than quarks.

roughly gluons have 2x the particles as quarks since they have ~twice as much color charge

The p_T dependence

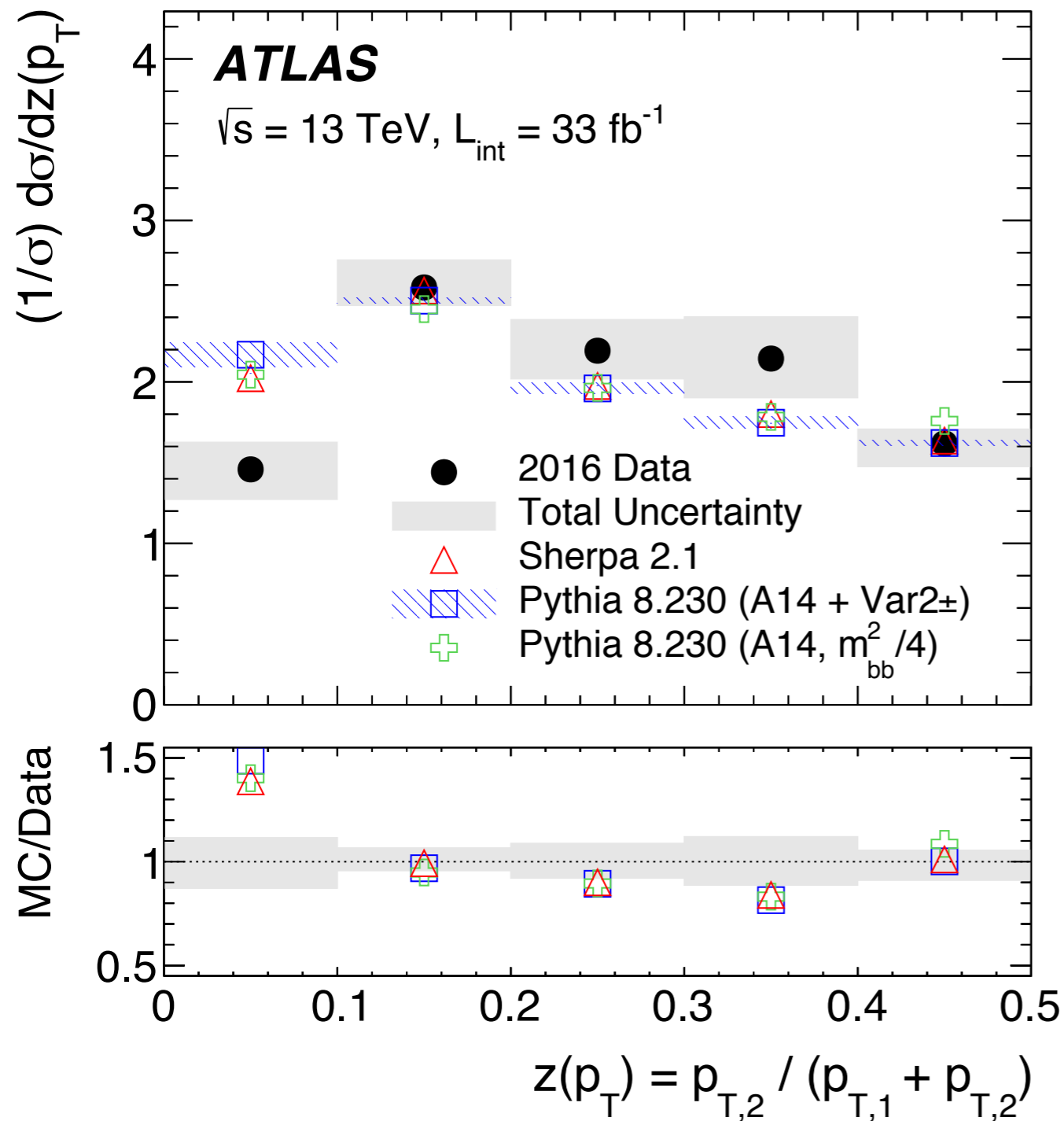
59

One can predict the p_T dependence of these observables, but let's just do a quick sanity check:

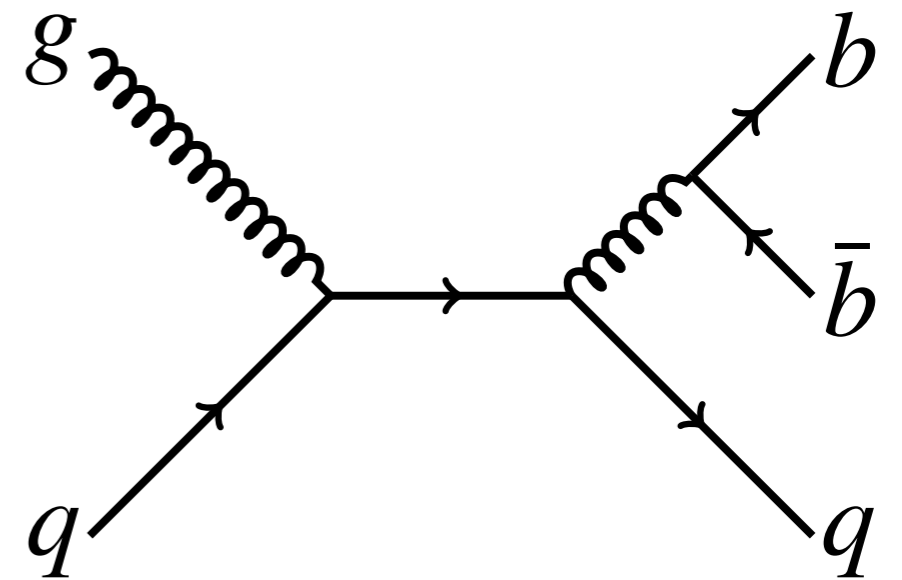


Why is the value \sim constant and a bit above 1/2?

One last note on gluon fragmentation



Gluon splitting to b -quarks offers a unique opportunity to directly probe gluon fragmentation.



Question: why did I pick this diagram?

QCD has much more to offer

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I've offered a (biased) collection of results,
but there are many more!

More on PDFs, fixed-order effects, ...

...Resummation, non-global effects (“entanglement”), ...

...Quark and gluon properties, W/Z/H hadronic decays, ...

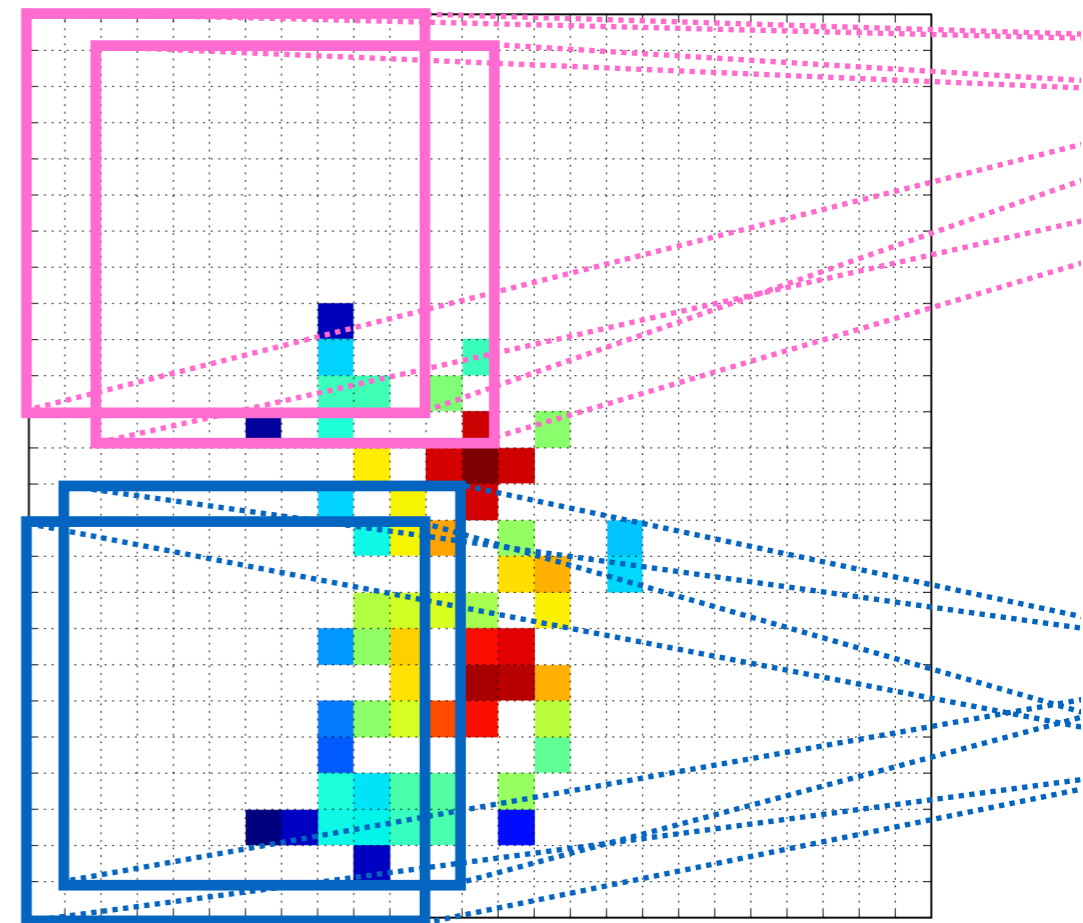
...Collective effects, connections with heavy ions, ...

...However, I stand between you and lunch, so let's wrap up!

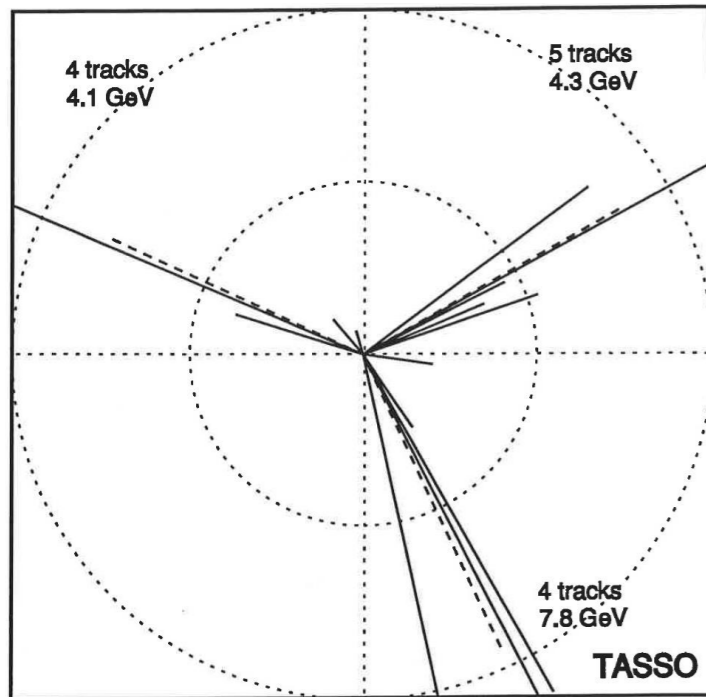
Even though QCD has only ~ 1 free parameter, it is a **rich theory with various regimes** that we can probe at the LHC.

Studying QCD is **inherently interesting** as a quantum theory of nature. Understanding it is also critical for direct and indirect **new particles searches**.

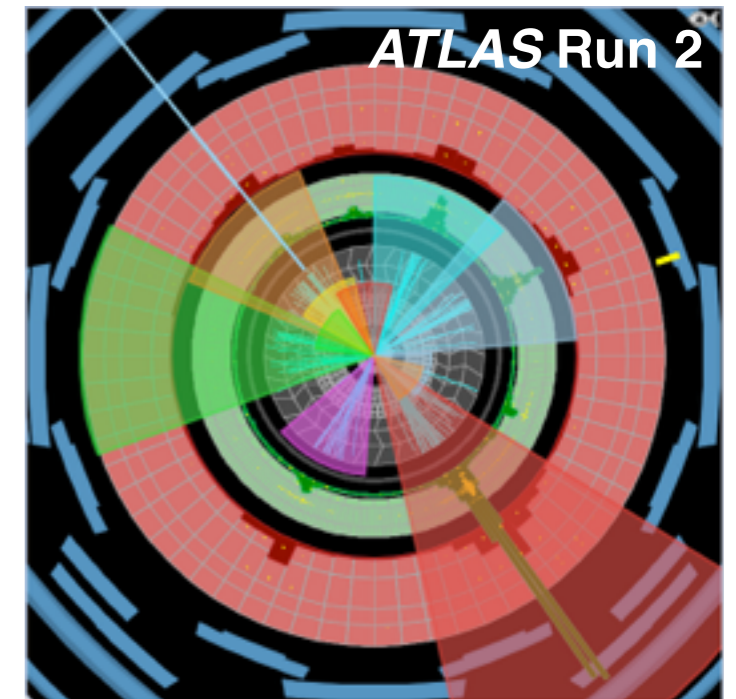
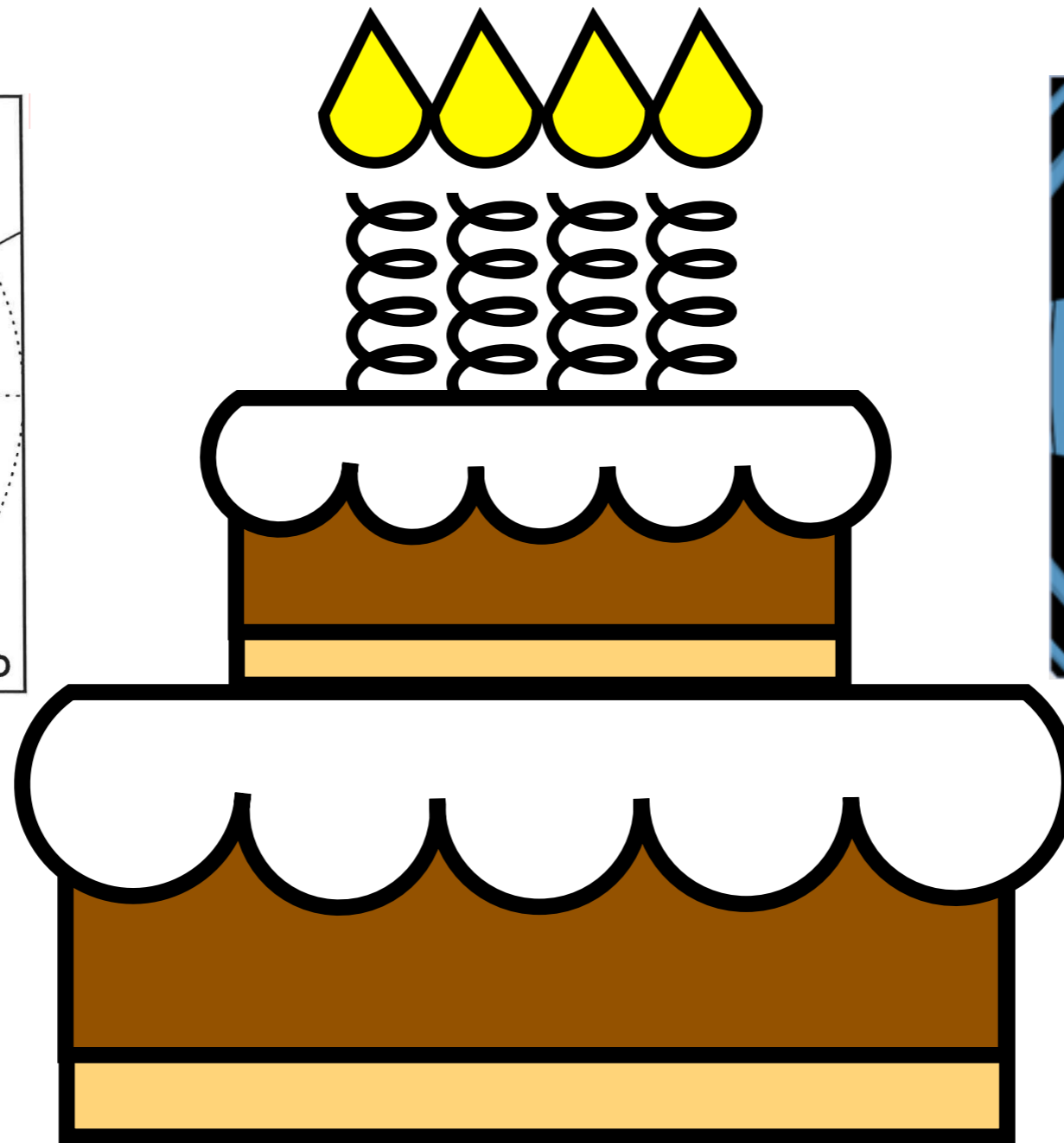
...there are also many exciting connections to modern machine learning that I did not have time to discuss - consider attending [ML4Jets2020!](#)



Happy Birthday to the Gluon!



Summer 1979



Summer 2019

Questions?

Soft drop procedure

65

Take a jet clustered with e.g. anti- k_t



Re-cluster it with C/A



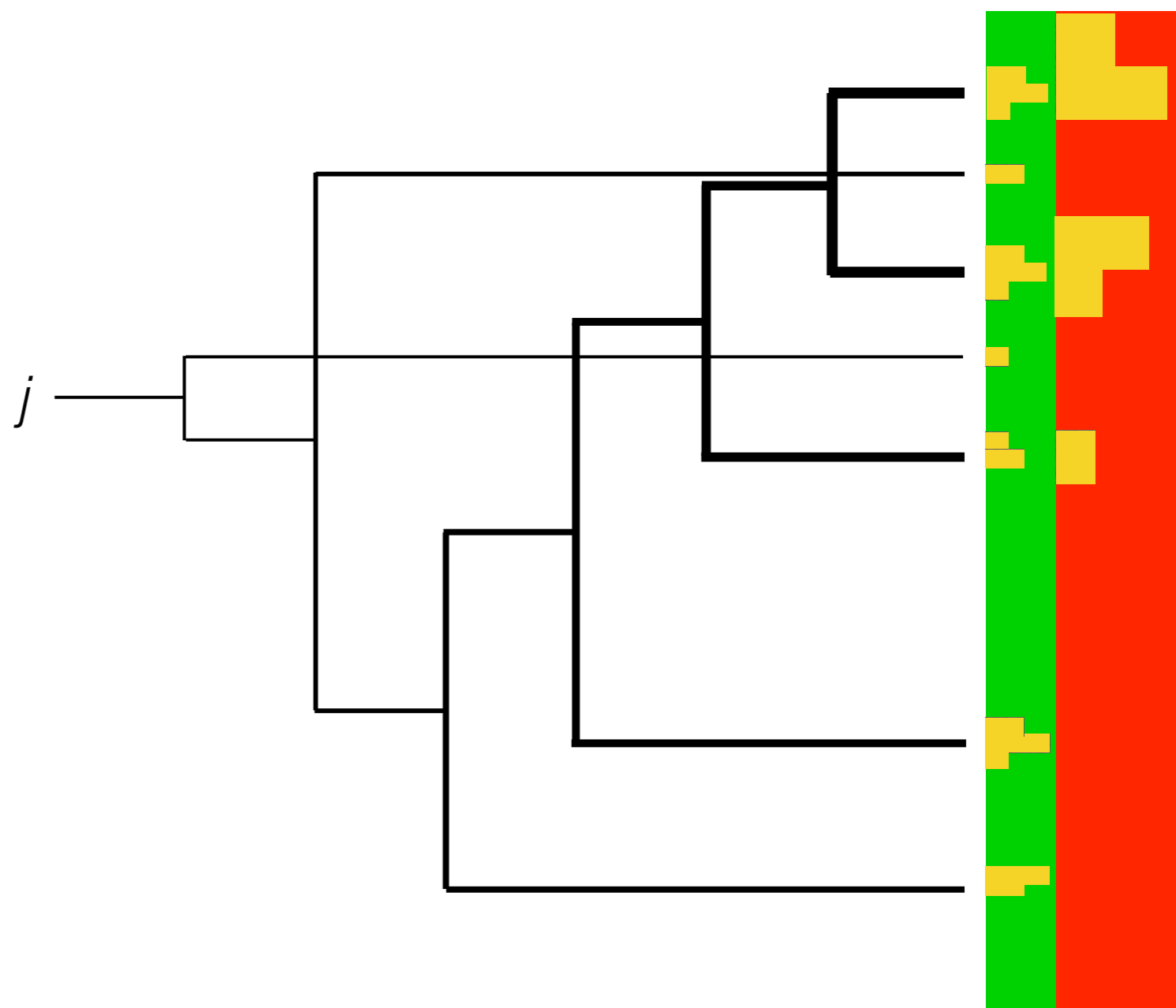
Traverse the clustering tree backwards



If a branch point satisfies the soft drop condition, stop.



Otherwise remove the softer branch and continue down the harder branch.



**clusters hardest
radiation first**

Soft drop procedure

Take a jet clustered with e.g. anti- k_t



Re-cluster it with C/A



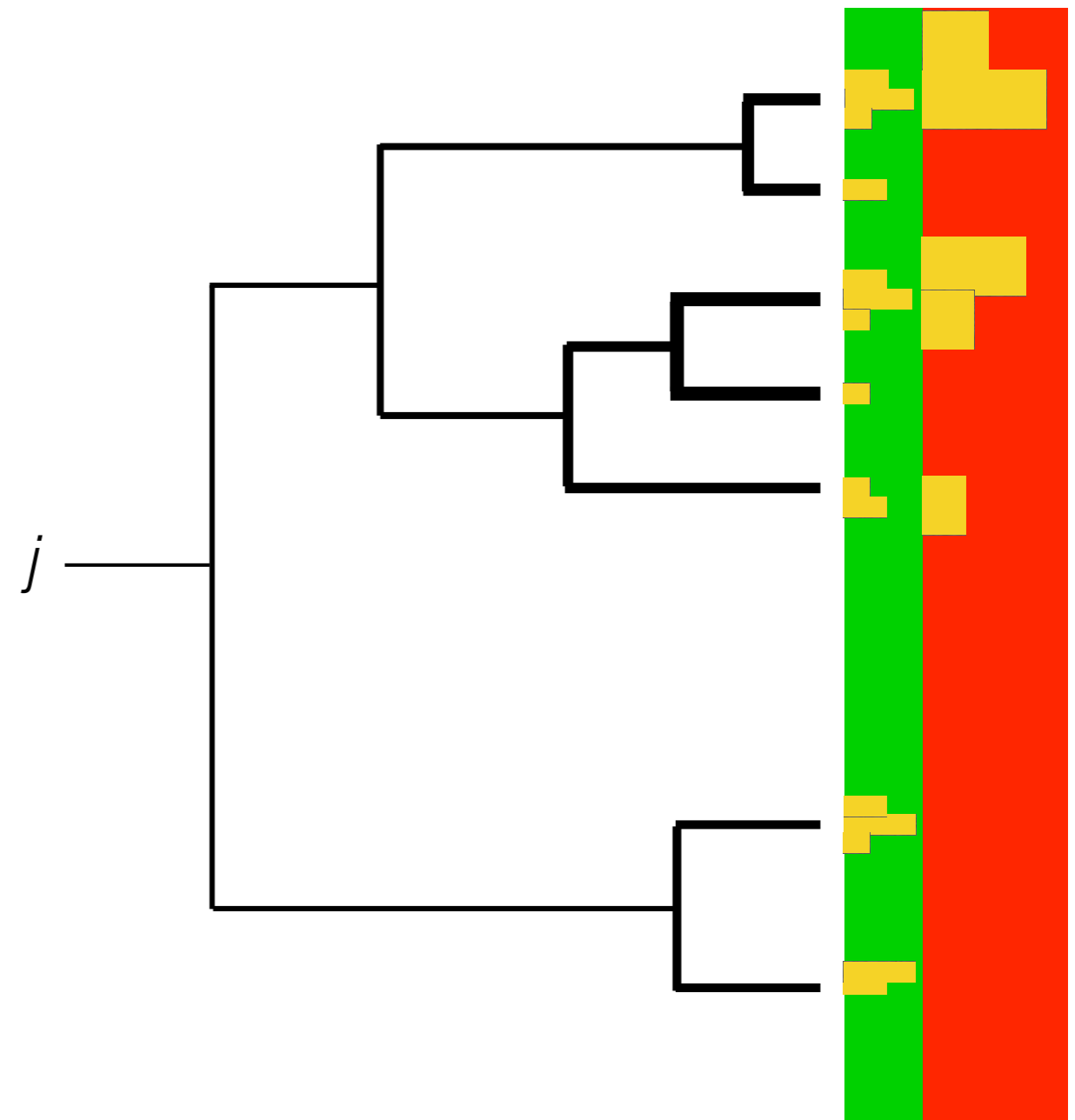
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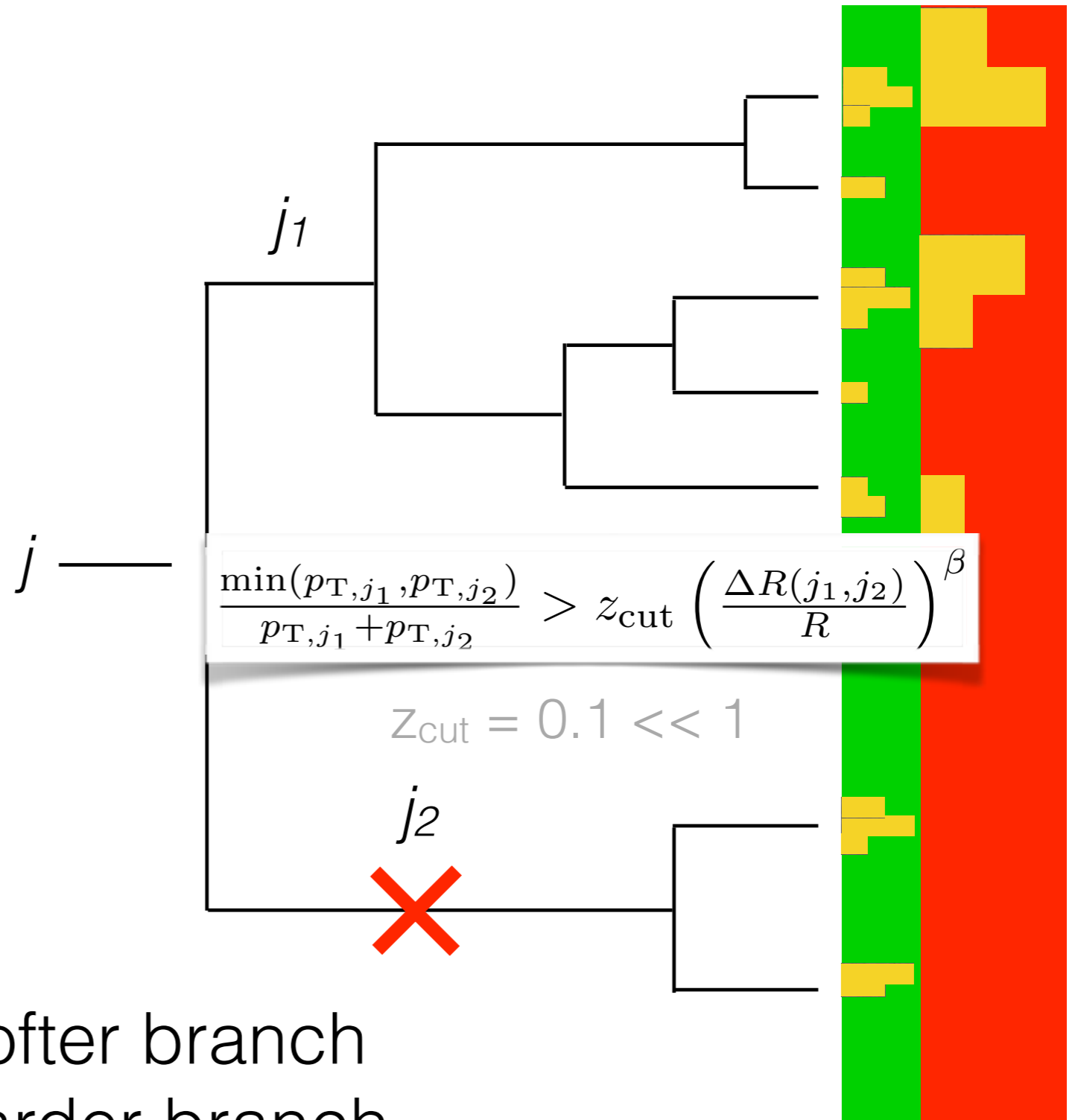
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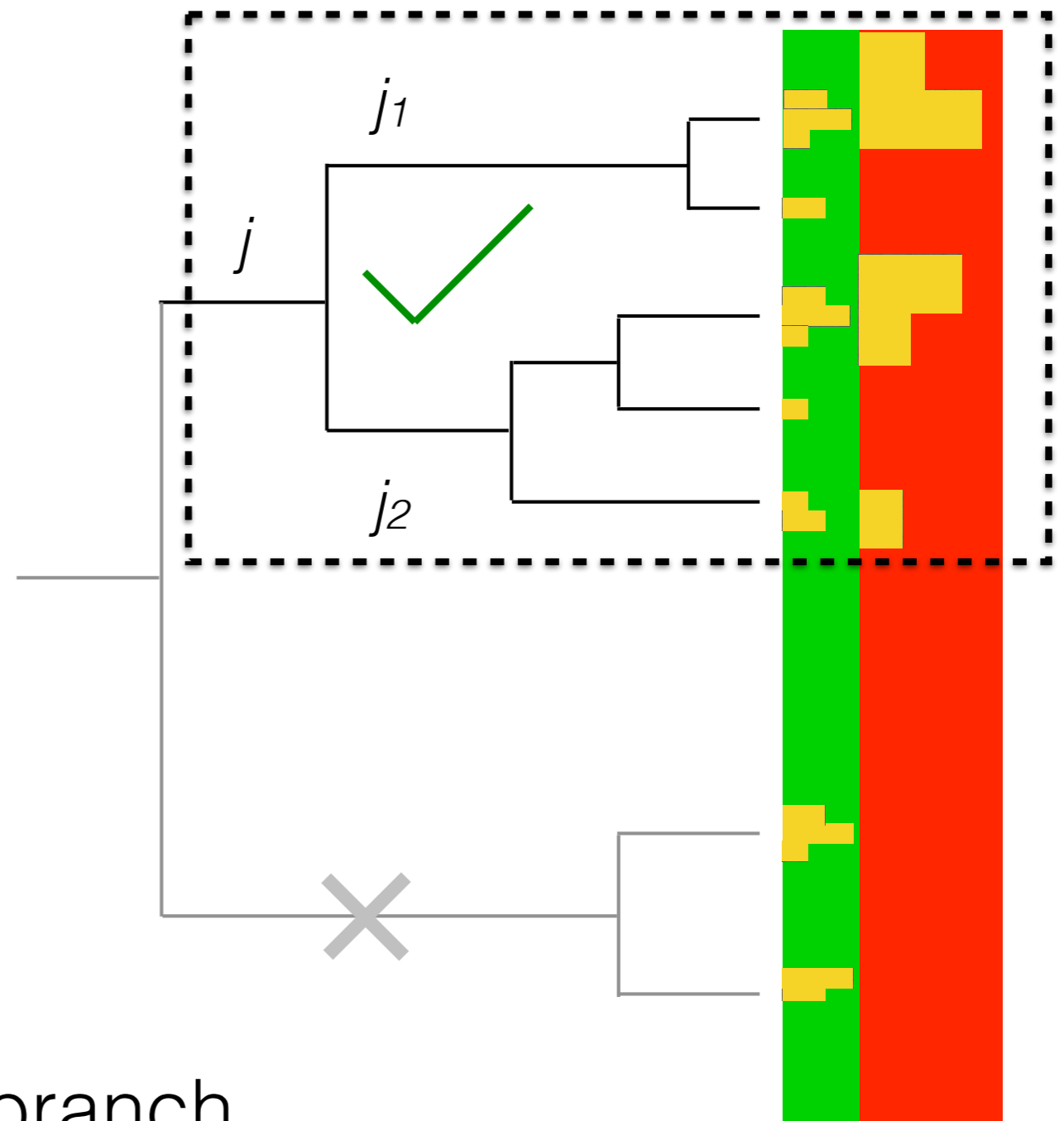
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Jet constituents

