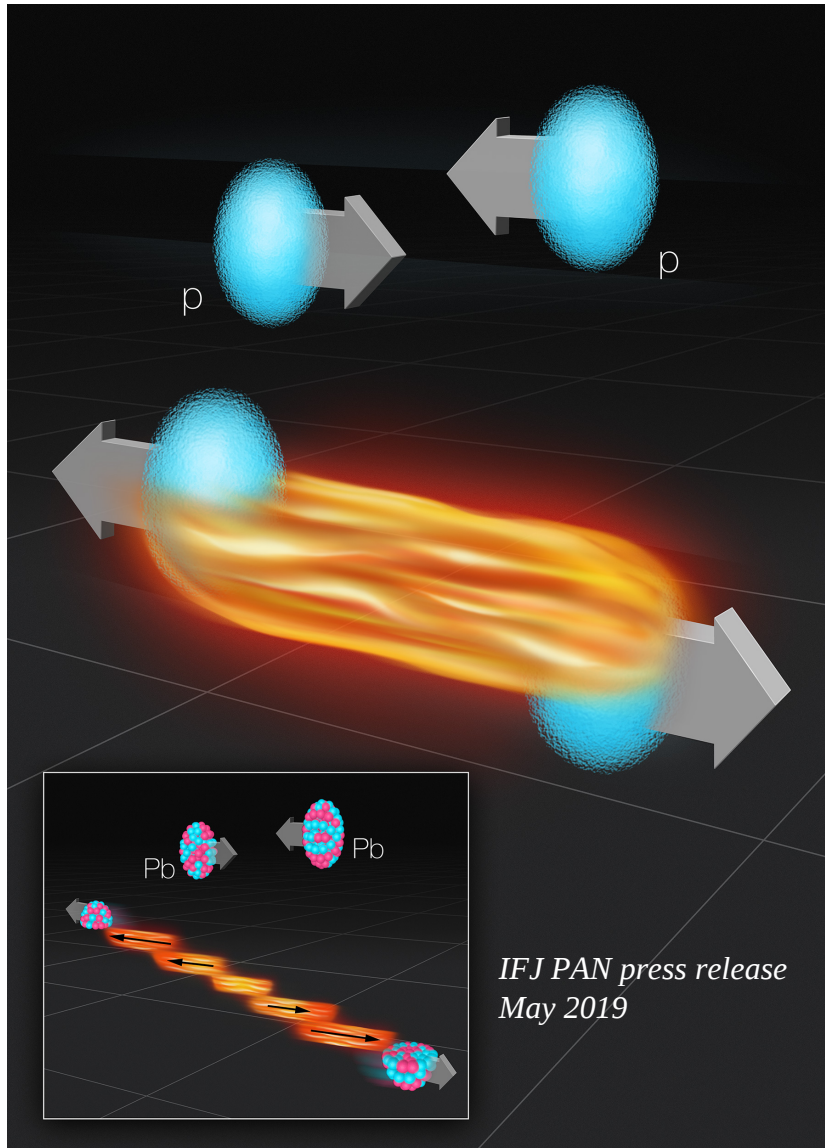


# Comments on the space-time evolution of the system created in the nucleus-nucleus collision at high energy



Andrzej Rybicki

H. Niewodniczański Institute of Nuclear Physics  
Polish Academy of Sciences

*Work done with*

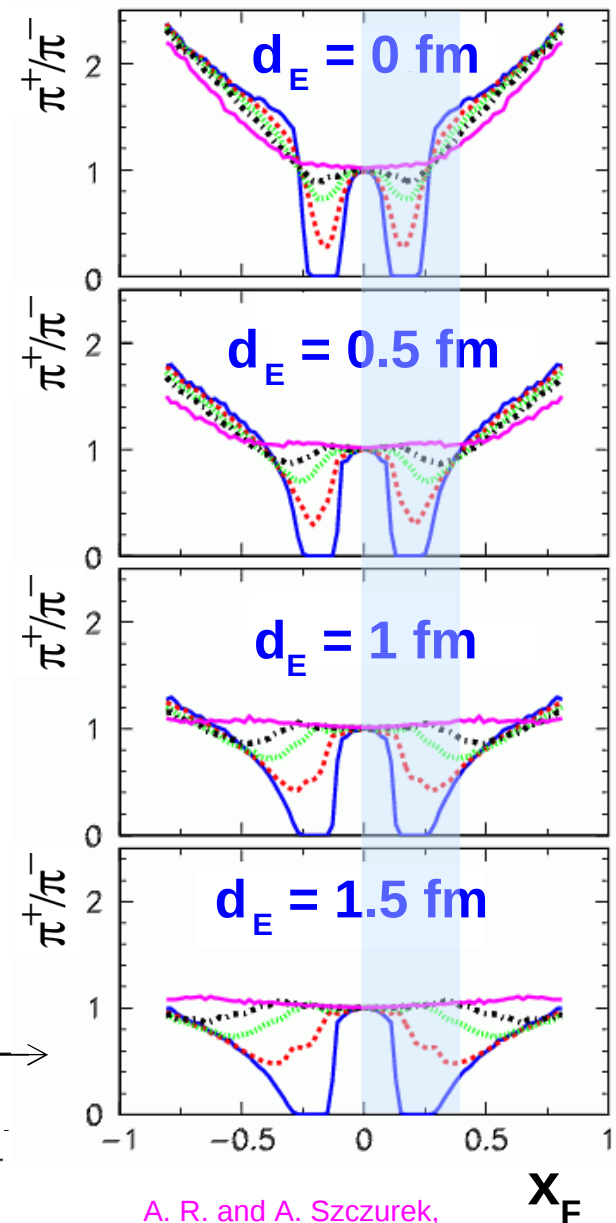
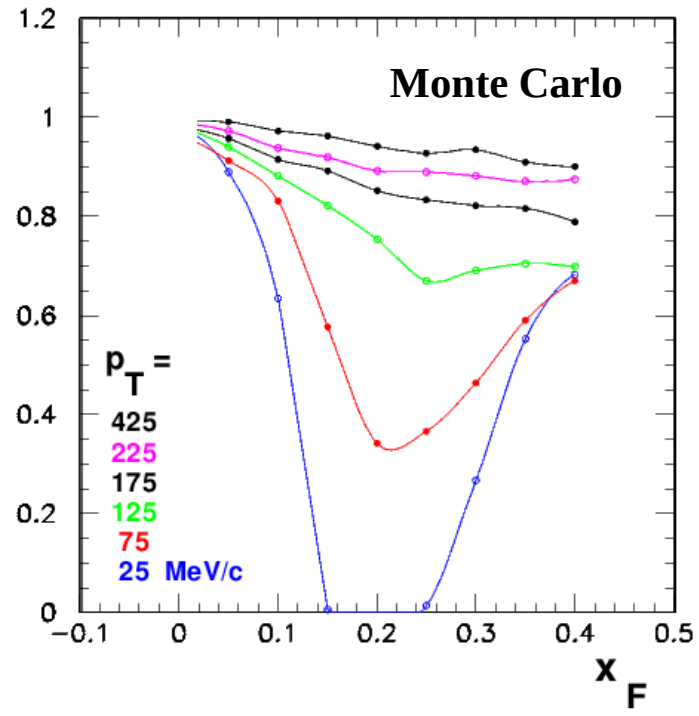
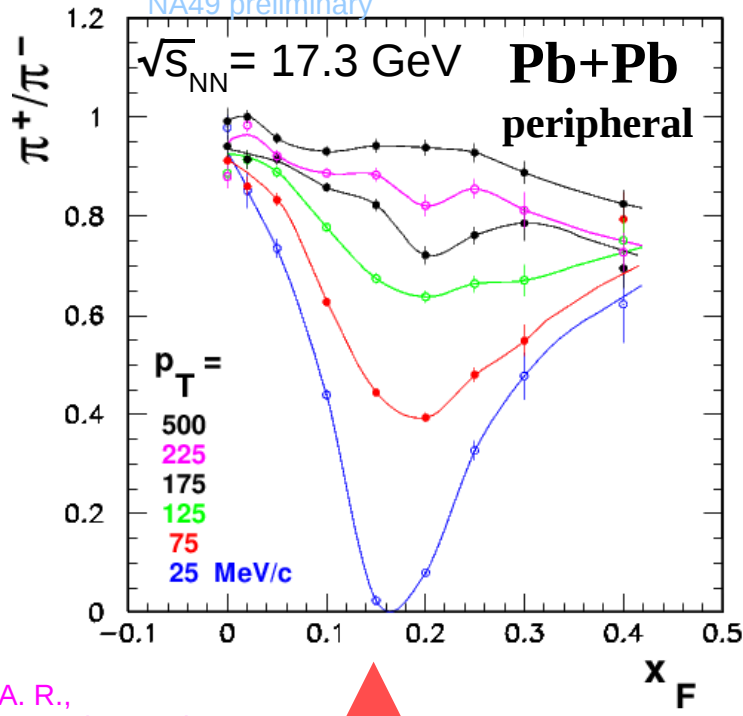
*A. Szczurek, V. Ozvenchuk, A. Marcinek, M. Kiełbowicz,  
Ł. Rozpłochowski, N. Davis, S. Bhosale, M. Kłusek-  
Gawenda*

See also:

1) PRC 99 (2019) 024908,  
2) arXiv: 1910.04544

1. The idea;
2. Getting information from EM effects ;
3. Space-time evolution of forward pion production ;
4. Summary.

# 1) The idea

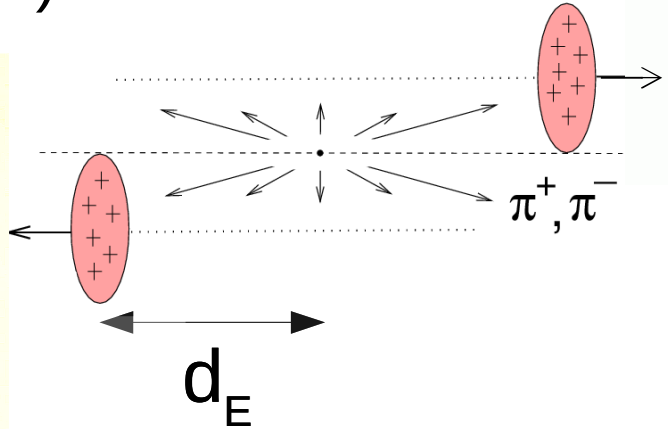
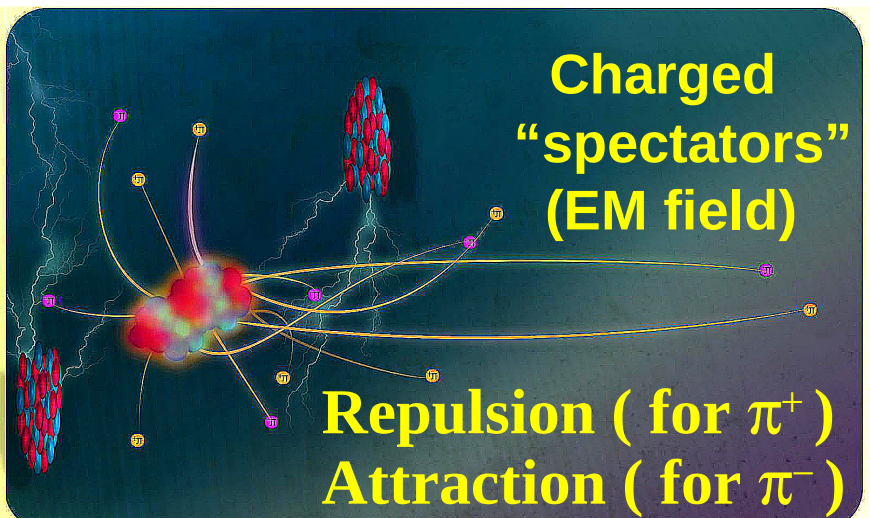


A. R.,  
Acta Phys. Polon.  
B42 (2011) 867

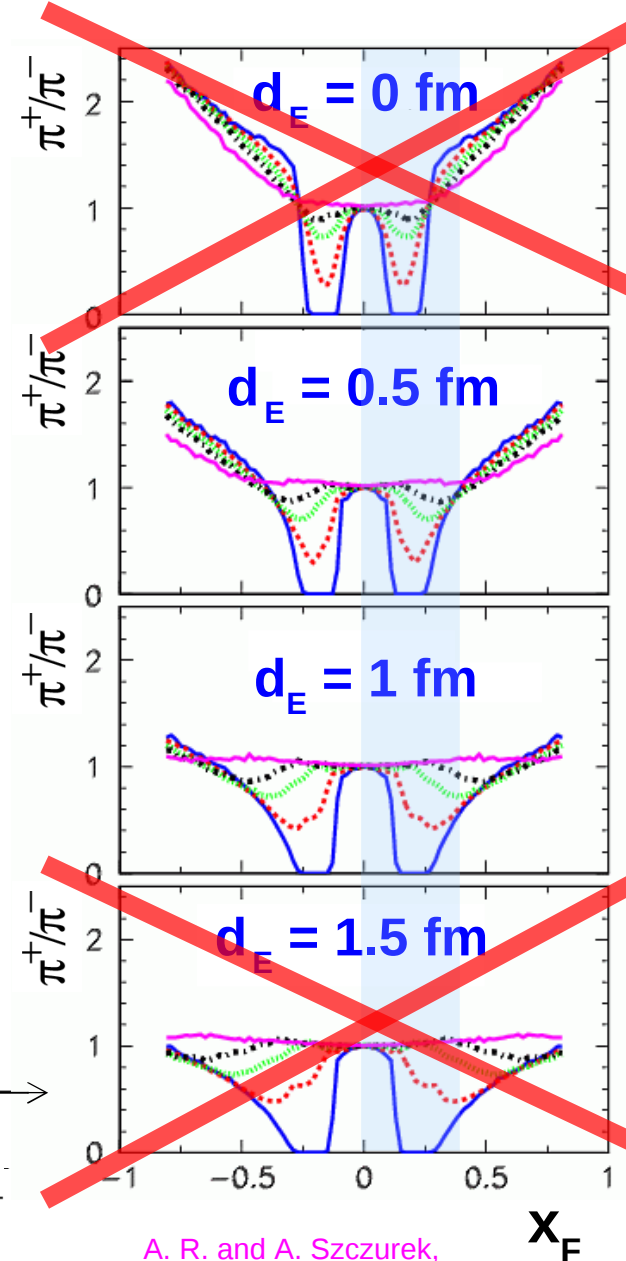
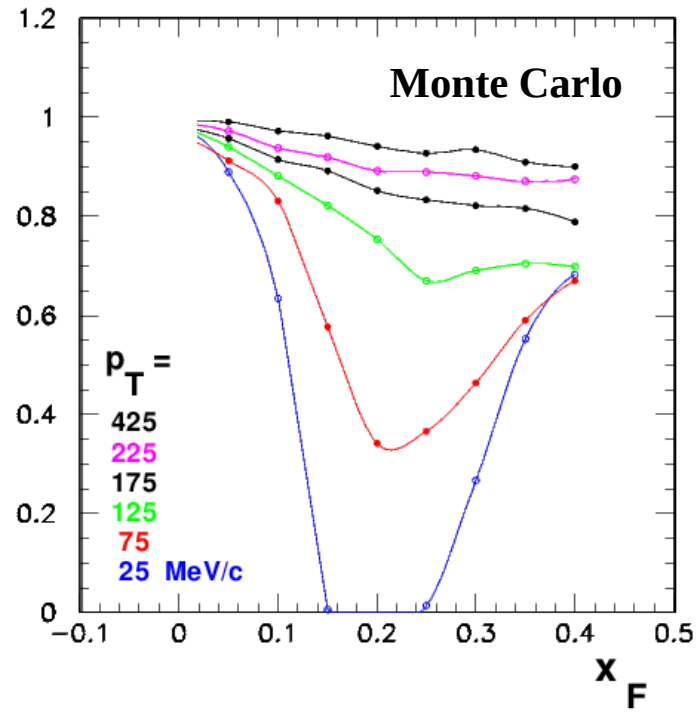
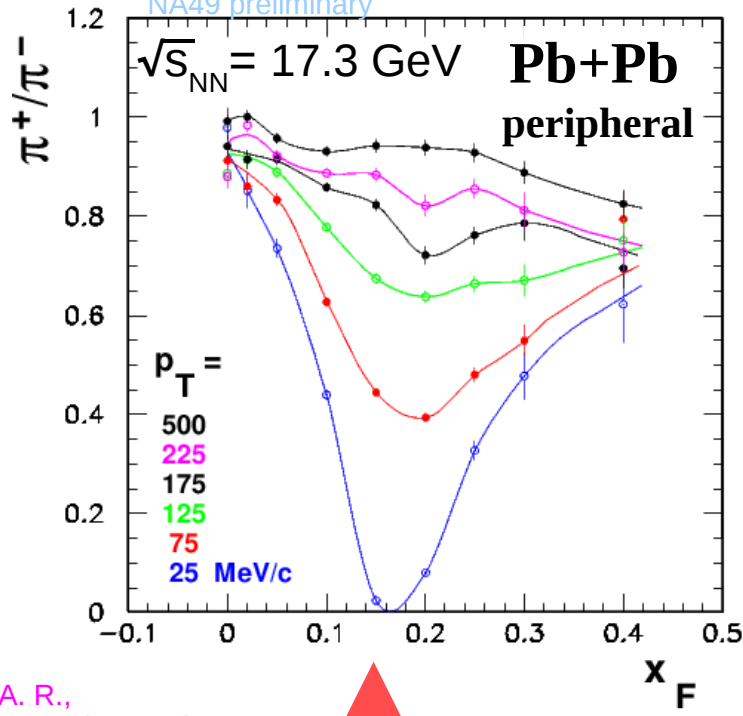
**spectator  
velocity**  
 $y = y_{beam}$

$$x_F = \frac{p_L}{p_L^{beam}}$$

(c.m.s.)



A. R. and A. Szczurek,  
Phys. Rev. C75 (2007)  
054903



A. R.,  
Acta Phys. Polon.  
B42 (2011) 867

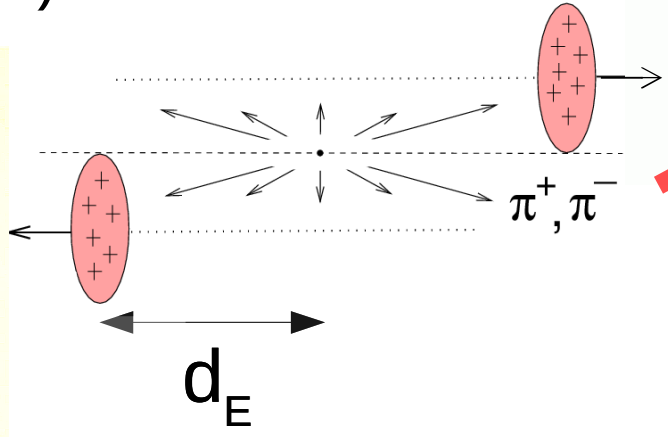
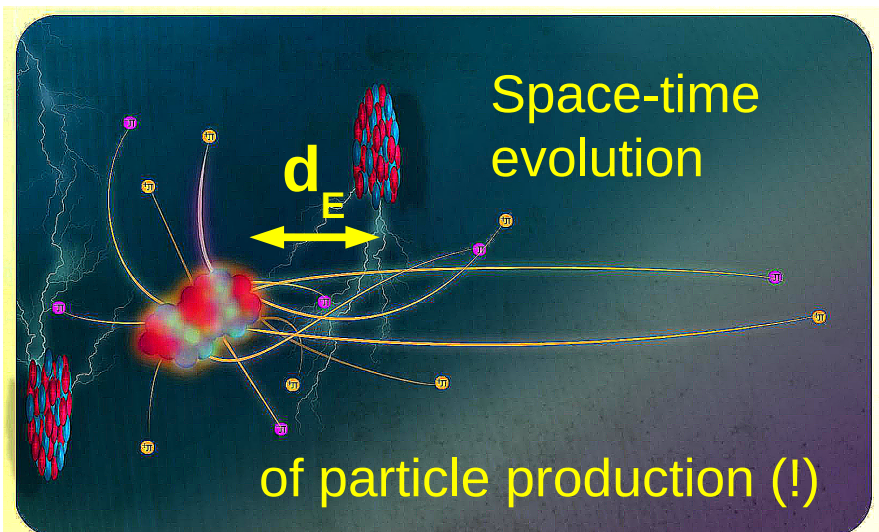
**spectator  
velocity  
 $y = y_{beam}$**

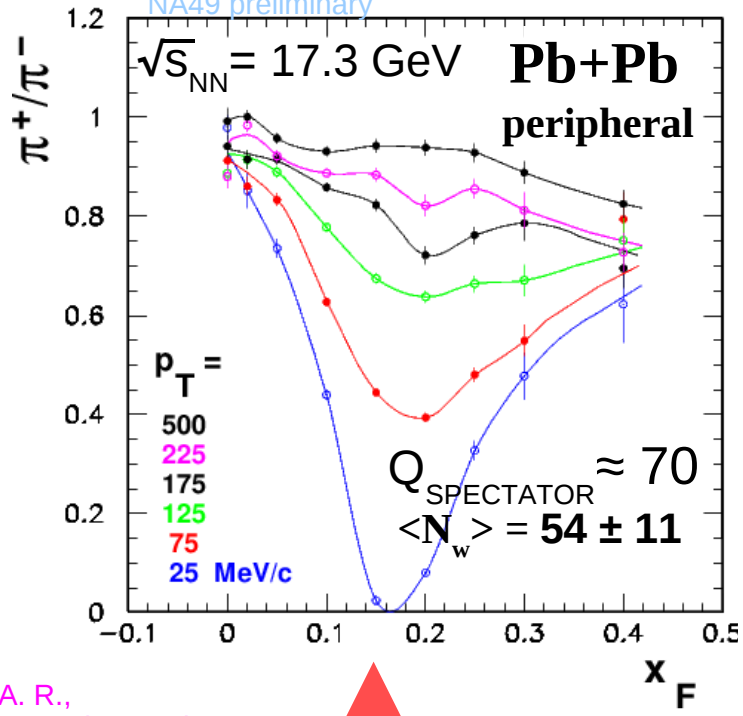
$$x_F = \frac{p_L}{p_L^{beam}}$$

(c.m.s.)

$$d_E \approx 0.75 \text{ fm}$$

A. R. and A. Szczurek,  
Phys. Rev. C75 (2007)  
054903



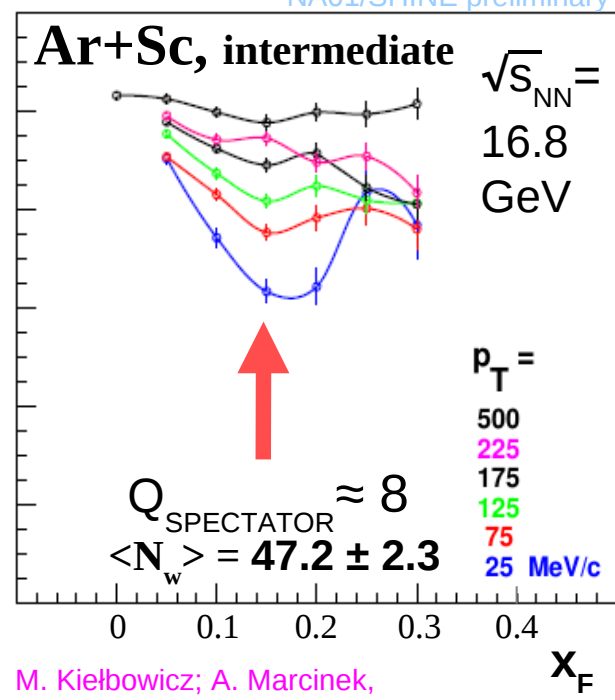


A. R.,  
Acta Phys. Polon.  
B42 (2011) 867

**spectator  
velocity**  
 $y = y_{\text{beam}}$

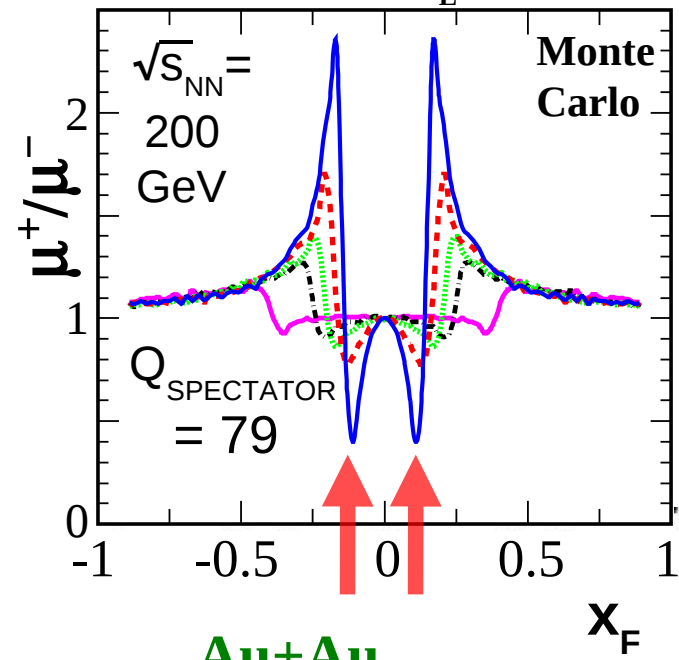
$$x_F = \frac{p_L}{p_L^{\text{beam}}}$$

(c.m.s.)

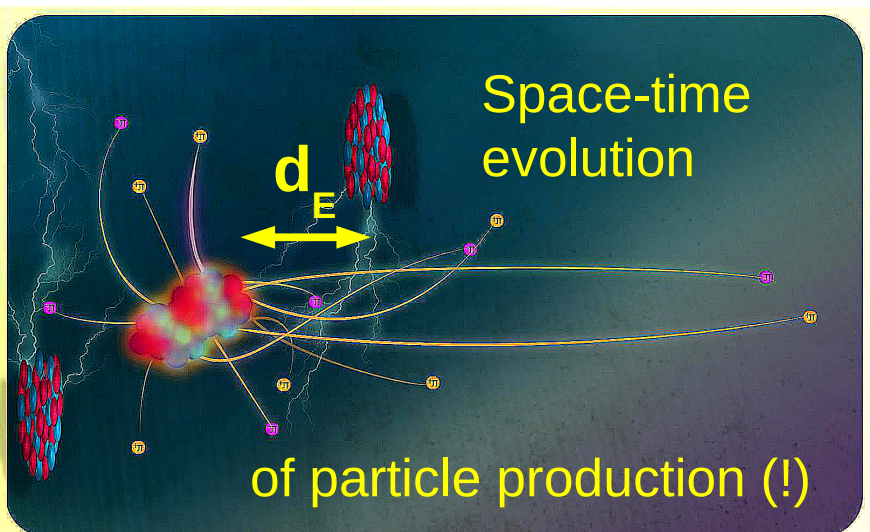


M. Kielbowicz; A. Marcinek,  
Acta Phys. Polon. B50 (2019) 1127

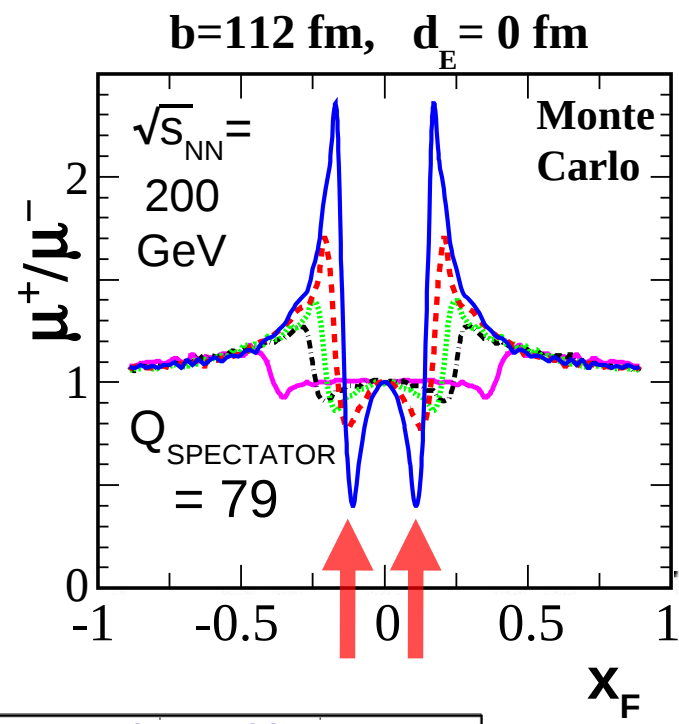
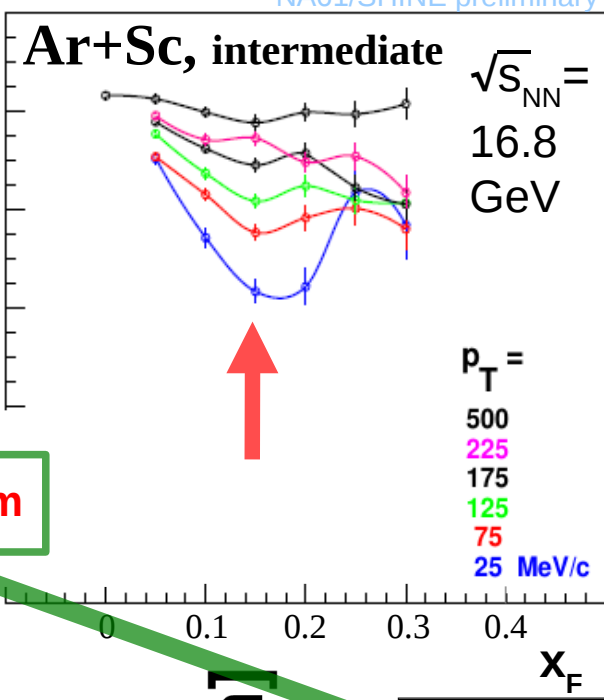
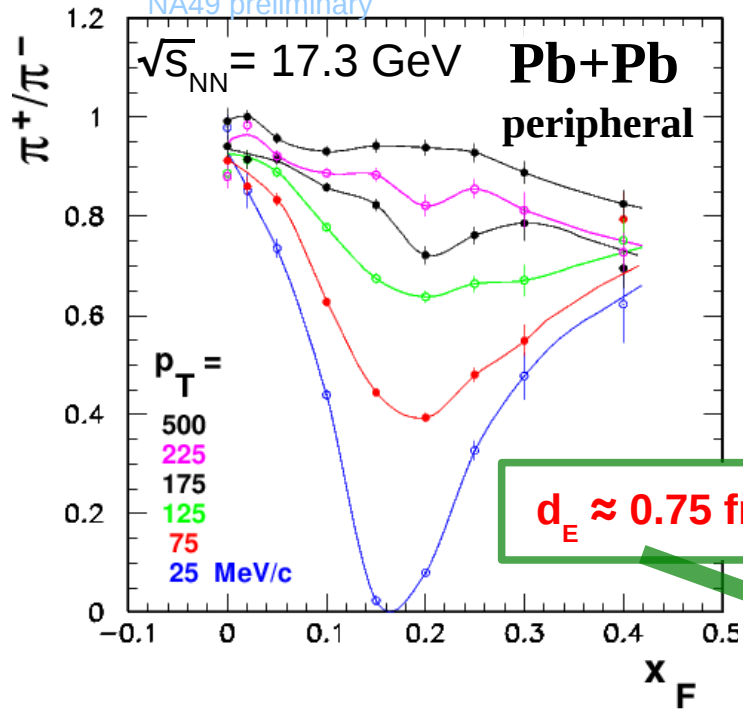
$b=112 \text{ fm}, d_E = 0 \text{ fm}$



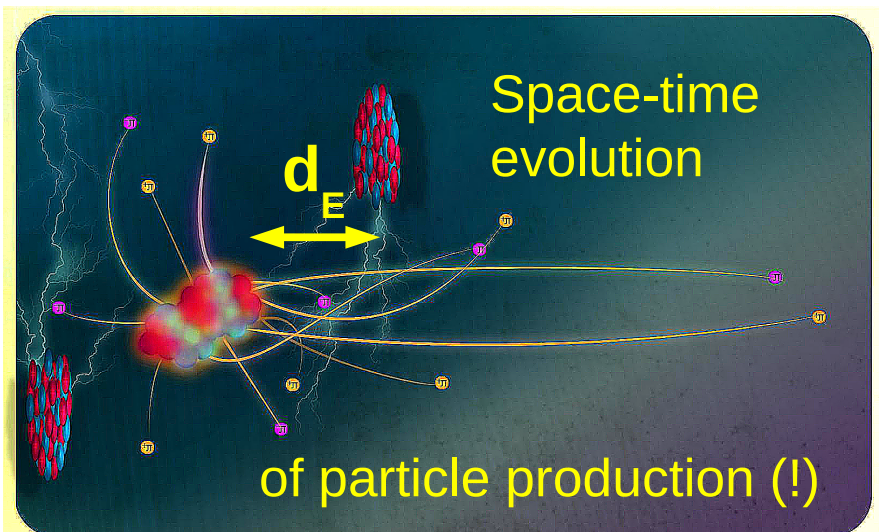
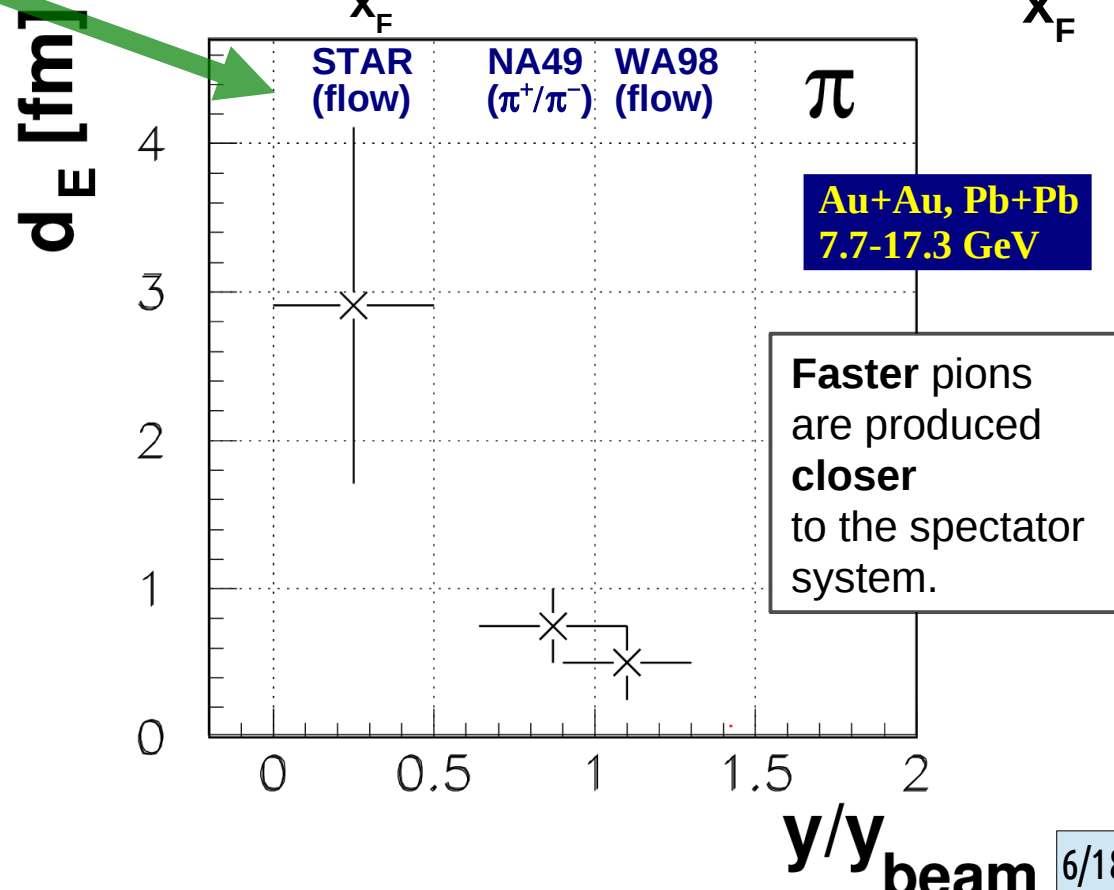
**Au+Au,  
ultra-peripheral,  
( $\gamma\gamma \rightarrow \mu^+\mu^-$ )**

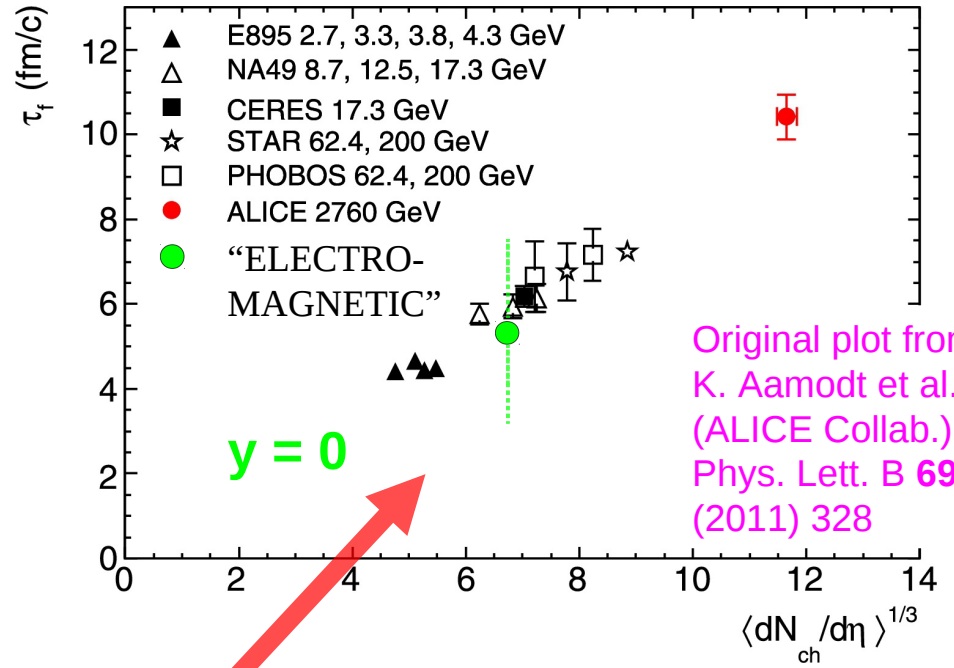
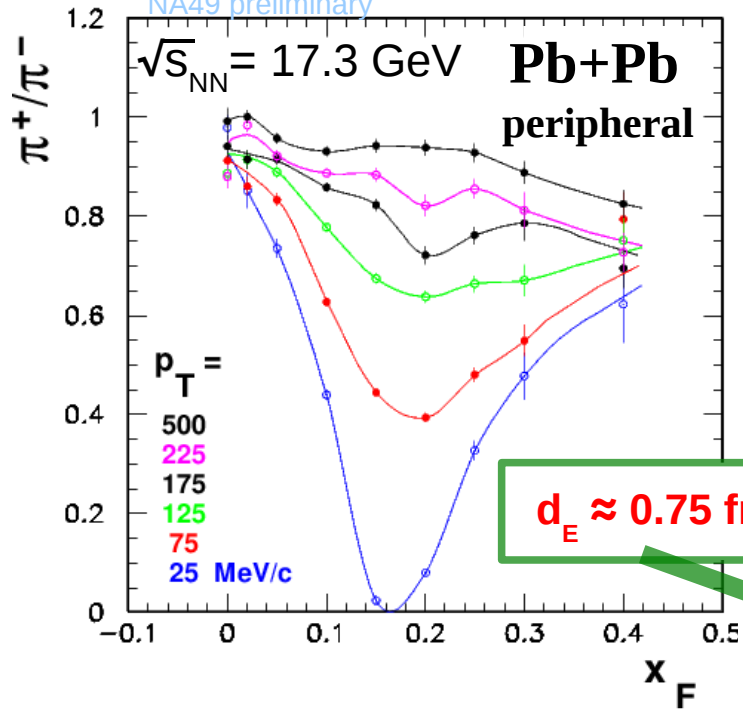


## 2) Getting information from EM effects



Note: the remaining points in the right plot are deduced from EM effects on azimuthal anisotropies (flow).  
Data: L. Adamczyk et al., STAR, PRL 112, 2014, 725,  
H. Schlagheck et al., WA98, NPA 663, 2000, 725.  
See also: A. R. et al., APPB 46 (2015) 3, 737.

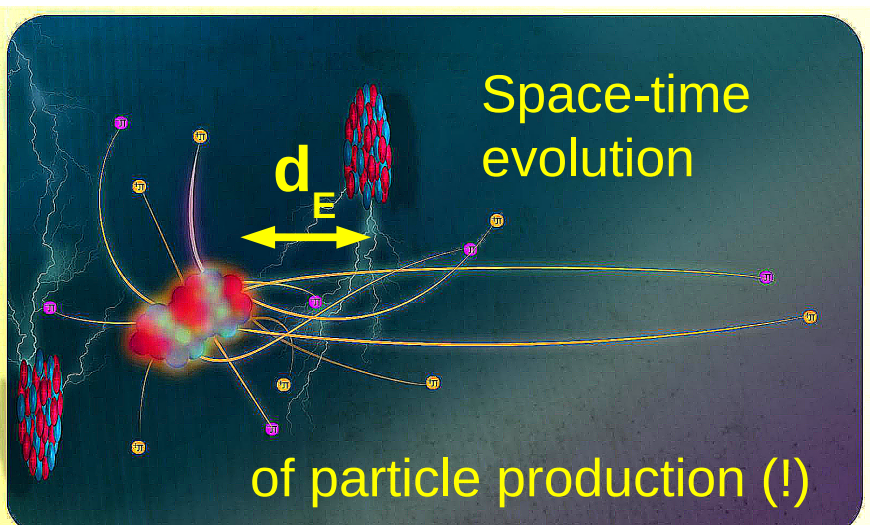
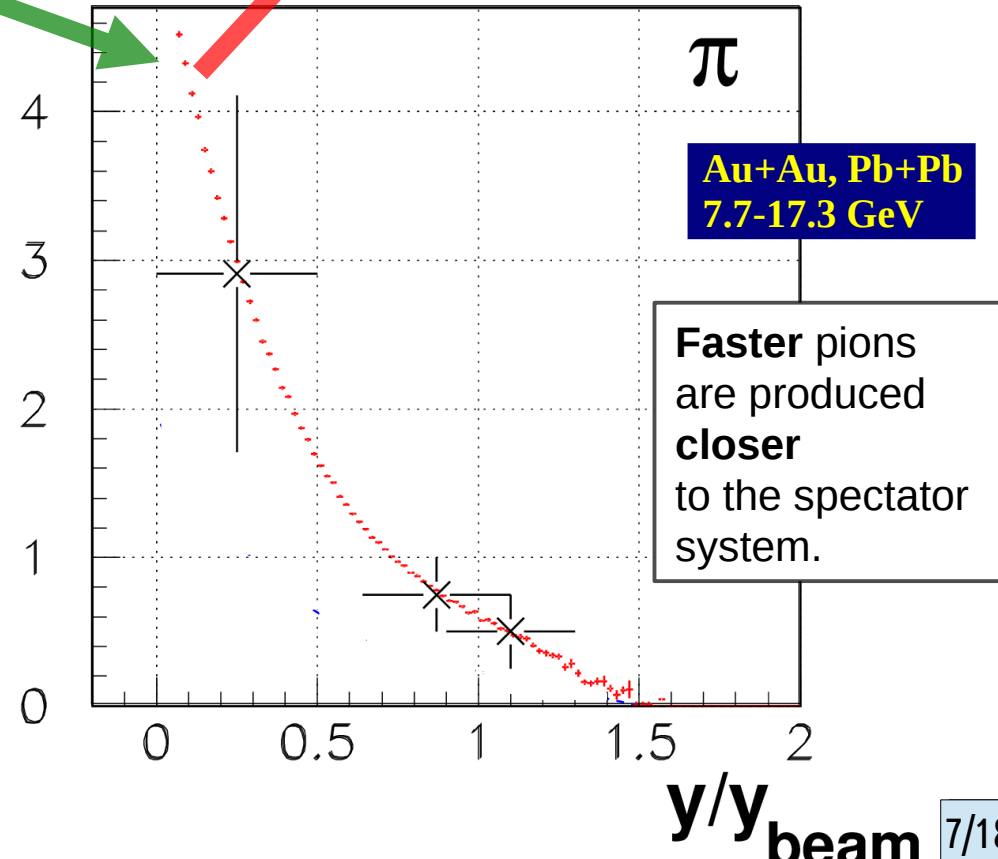




Original plot from:  
K. Aamodt et al.  
(ALICE Collab.),  
Phys. Lett. B **696**  
(2011) 328

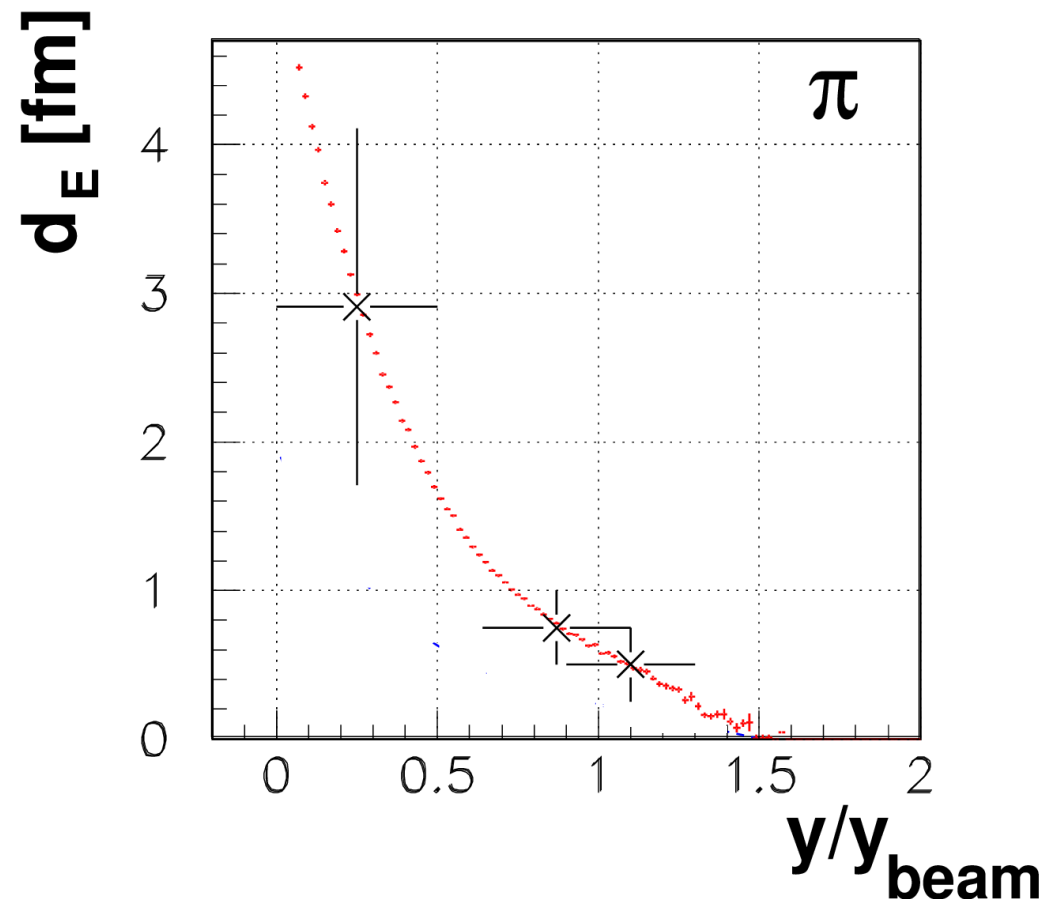
- EM effects **their own estimate** for the time of pion creation, at  $y=0$ .

$d_E \text{ [fm]}$



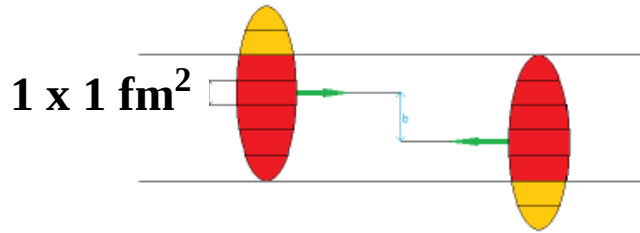
### 3)

# Space-time evolution of forward pion production



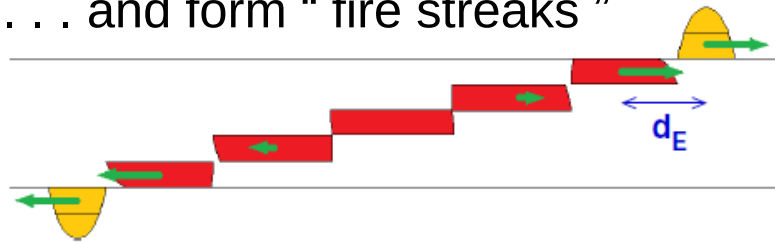


Bricks collide ...



PRC 95 (2017) 024908  
 Idea by A. Szczurek,  
 See also:  
 R. Hagedorn, CERN-71-12  
 W.D. Myers, NPA 296, 1978, 177

... and form "fire streaks"

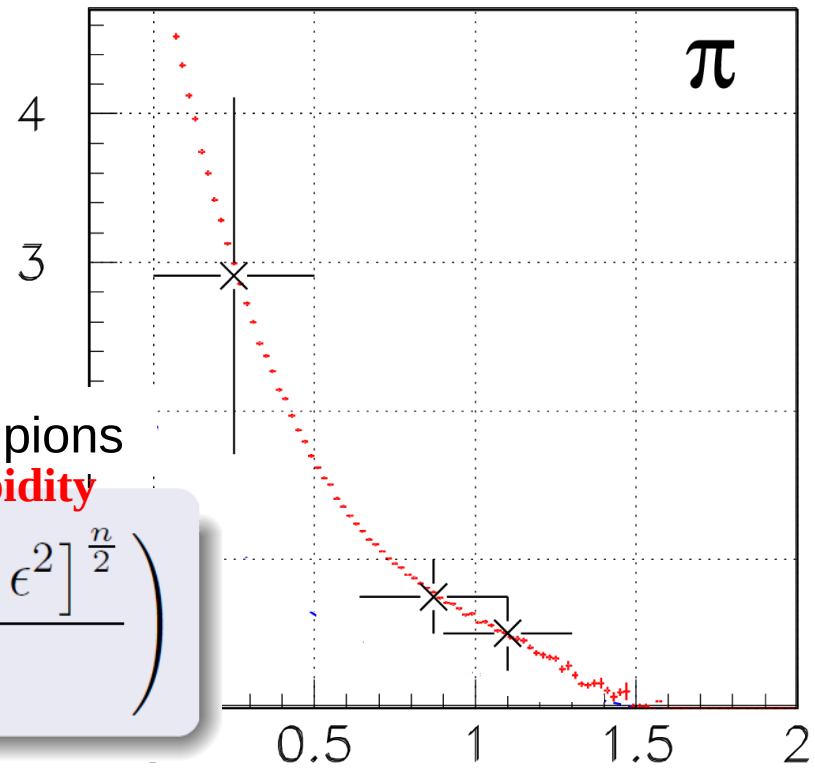


Each fire streak fragments independently into pions

$$\frac{dn}{dy} = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

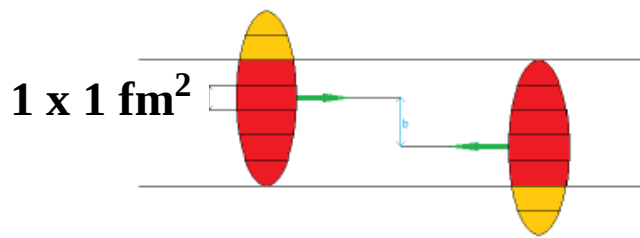
total fire streak energy  
 sum of brick masses

$d_E$  [fm]



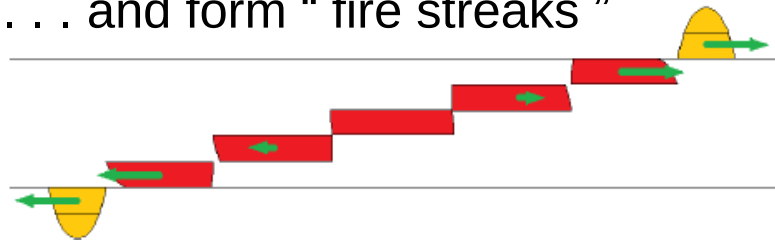
$y/y_{\text{beam}}$

Bricks collide ...



PRC 95 (2017) 024908  
 Idea by A. Szczurek,  
 See also:  
 R. Hagedorn, CERN-71-12  
 W.D. Myers, NPA 296, 1978, 177

... and form "fire streaks"

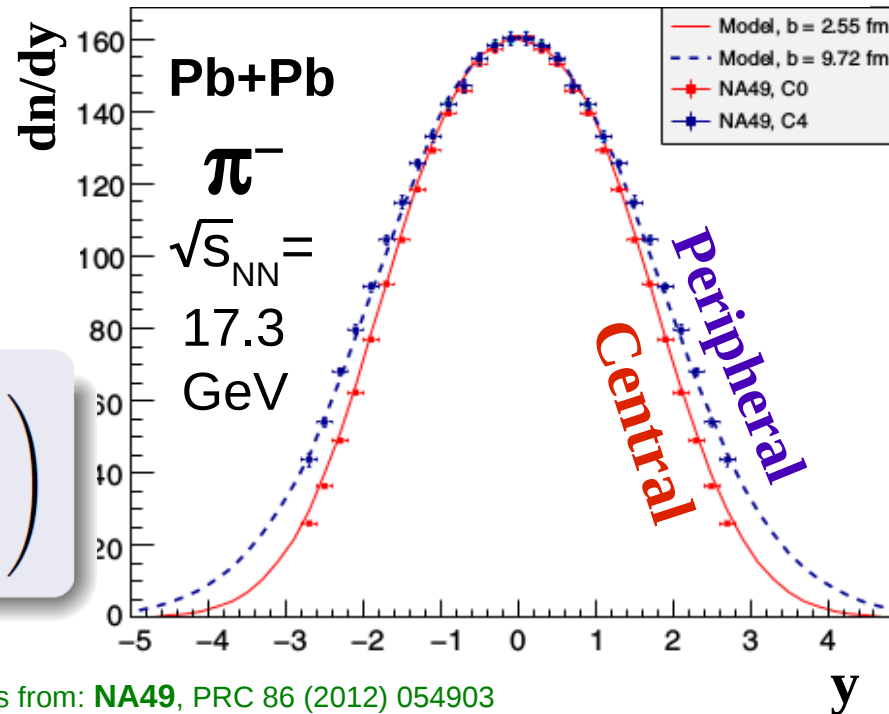
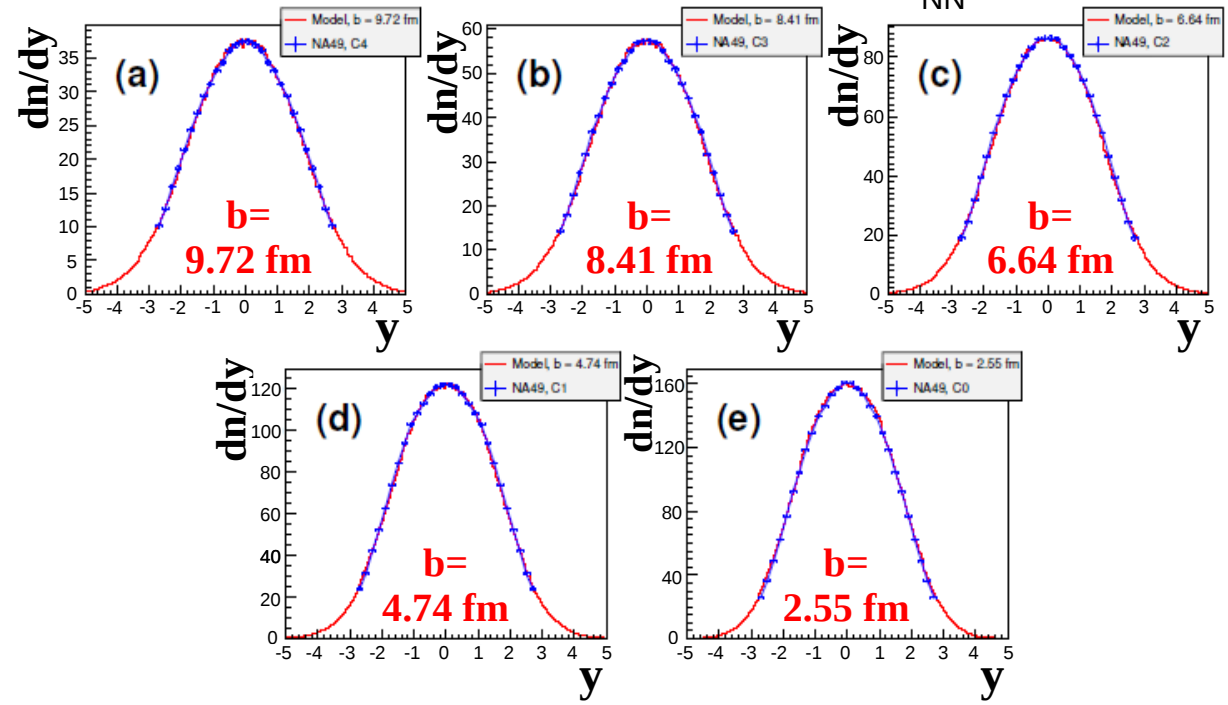


Each fire streak fragments independently into pions

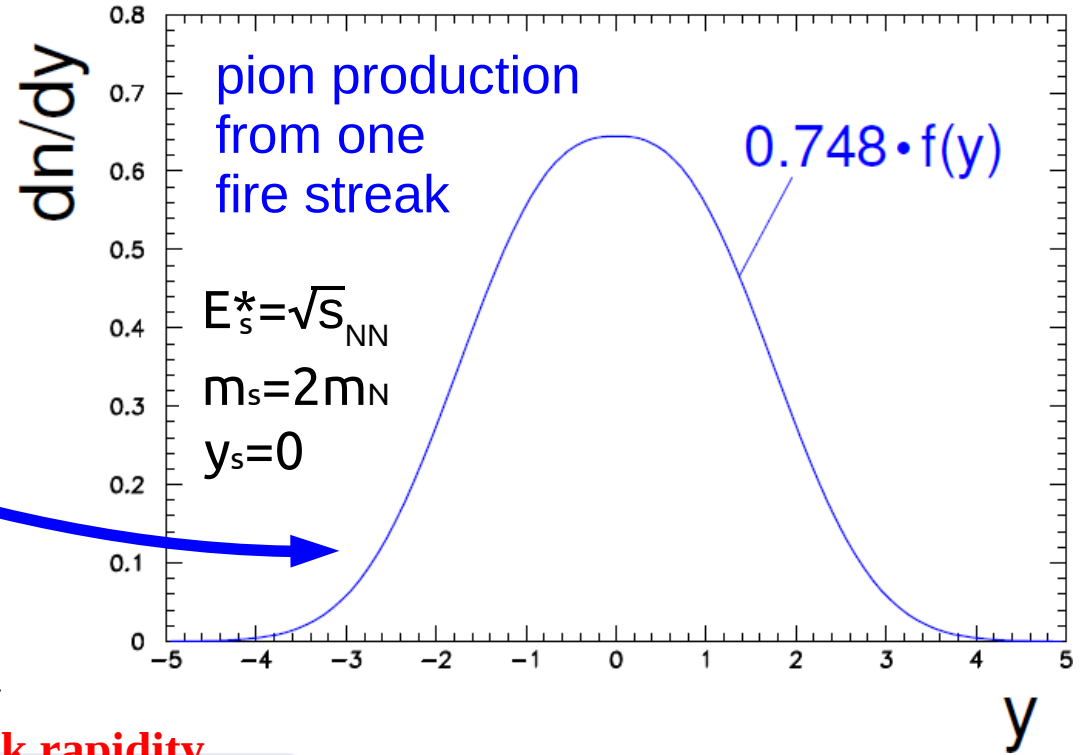
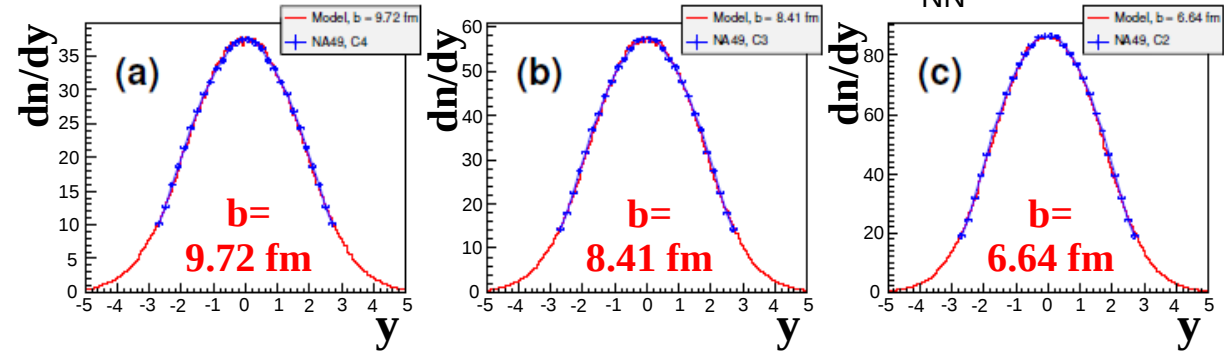
$$\frac{dn}{dy} = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

total fire streak energy  
 sum of brick masses

NA49,  $\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 17.3$  GeV



data points from: NA49, PRC 86 (2012) 054903



Each fire streak fragments independently

$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

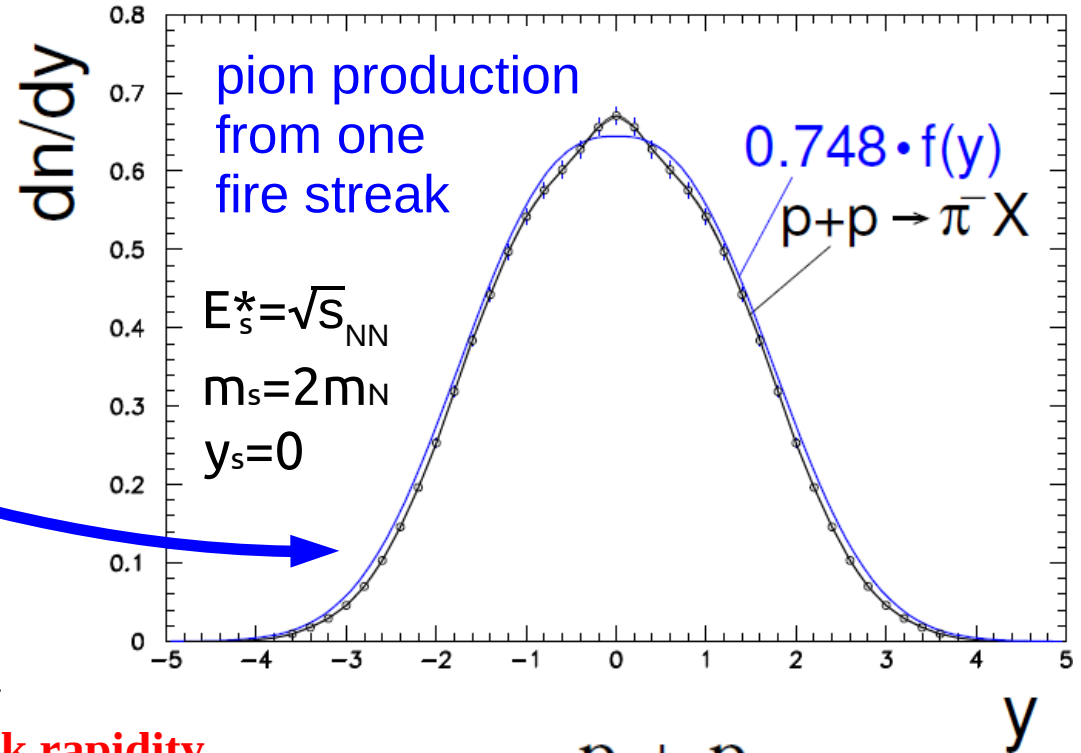
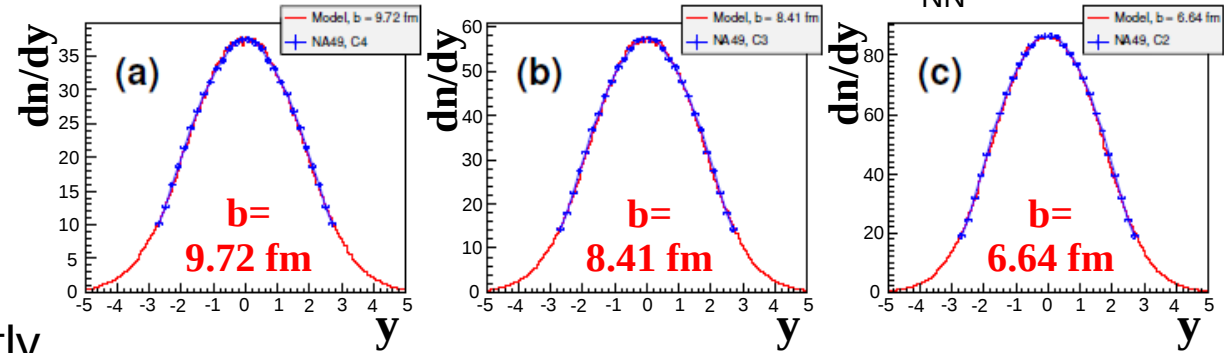
**fire streak rapidity**

total fire streak energy

sum of brick masses

- The pion rapidity distribution from **one fire streak** in Pb+Pb collisions is **similar** to the pion rapidity distribution in **p+p** reactions ;
- The difference in absolute normalization (**0.748**) can be directly obtained from the different energy repartition in **p+p** and **Pb+Pb** reactions (see PRC 99 (2019) 024908).

NA49,  $\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 17.3$  GeV

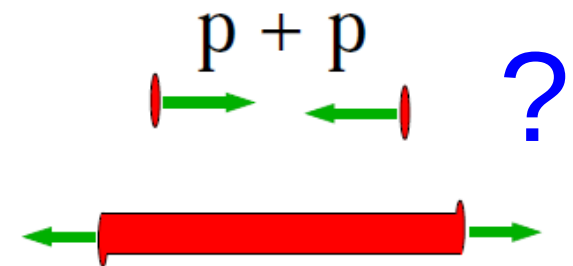


Each fire streak fragments independently

$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

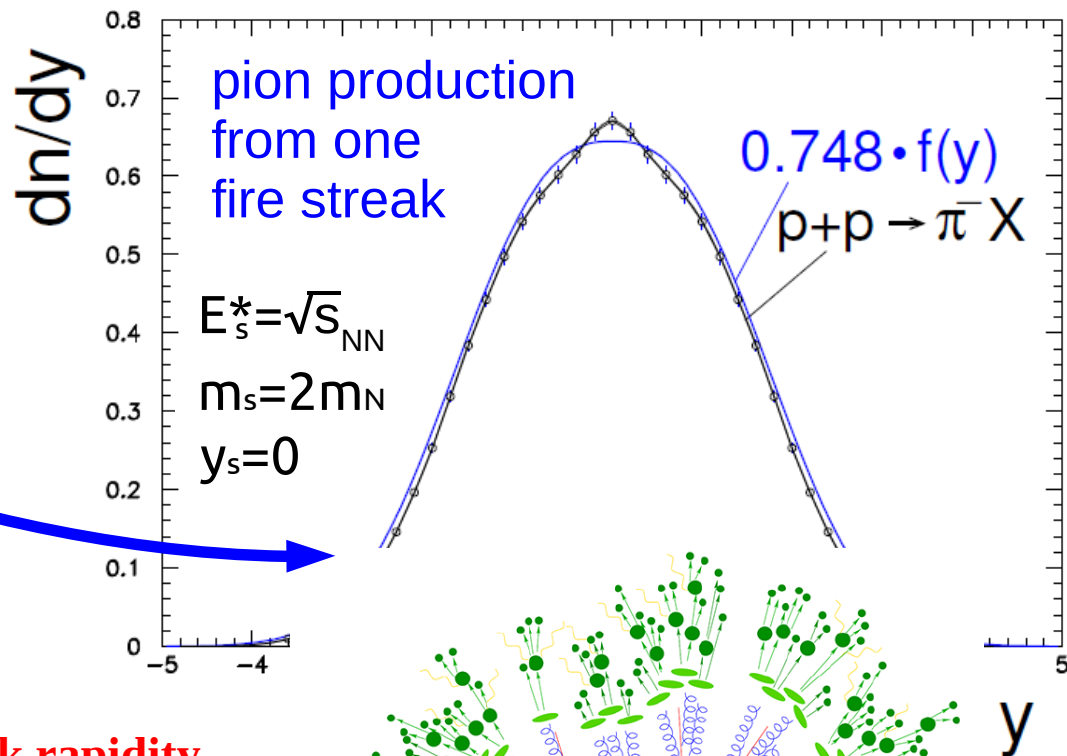
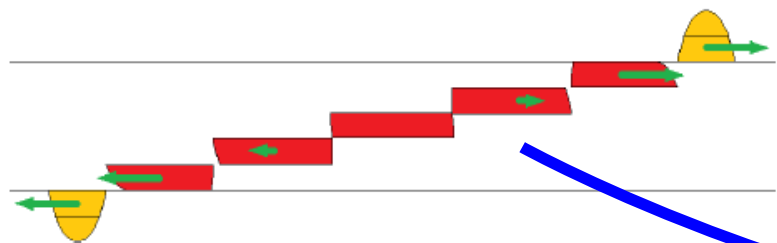
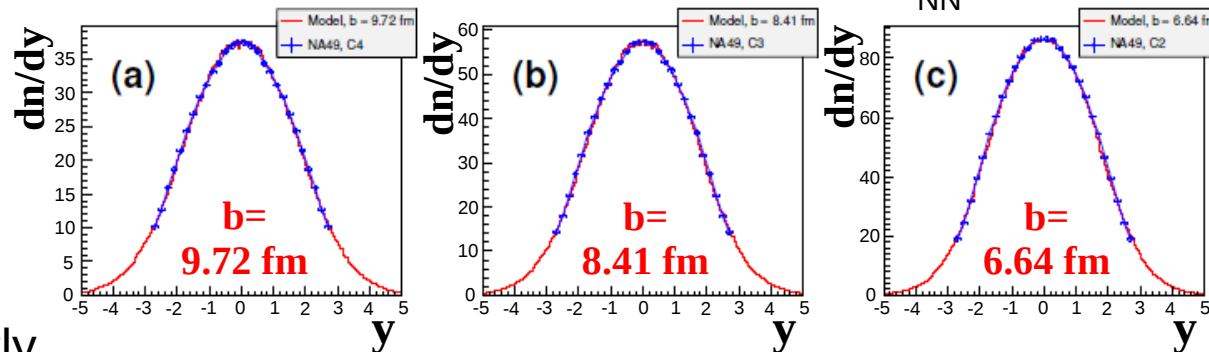
total fire streak energy

sum of brick masses



- The pion rapidity distribution from **one fire streak** in Pb+Pb collisions is **similar** to the pion rapidity distribution in **p+p** reactions ;
- The difference in absolute normalization (**0.748**) can be directly obtained from the different energy repartition in **p+p** and **Pb+Pb** reactions (see PRC 99 (2019) 024908).

NA49,  $\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 17.3$  GeV

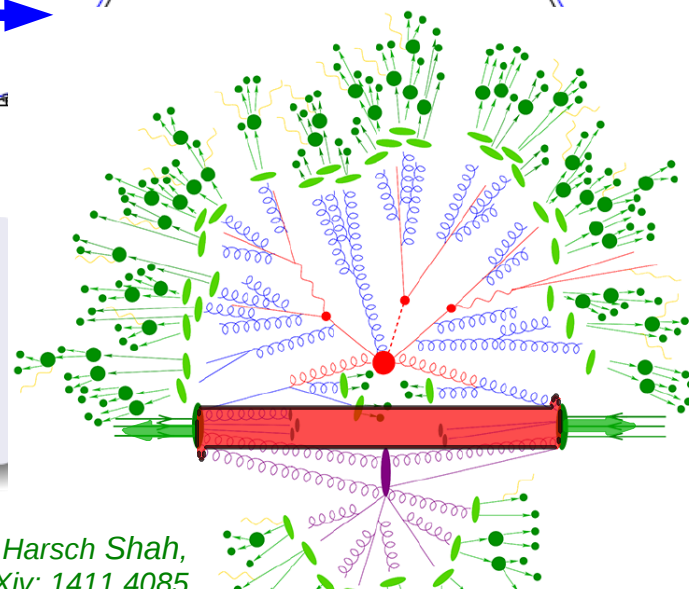


Each fire streak fragments independently

$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

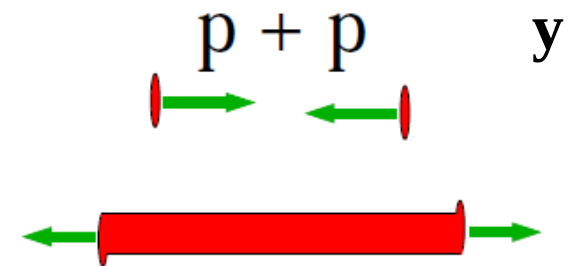
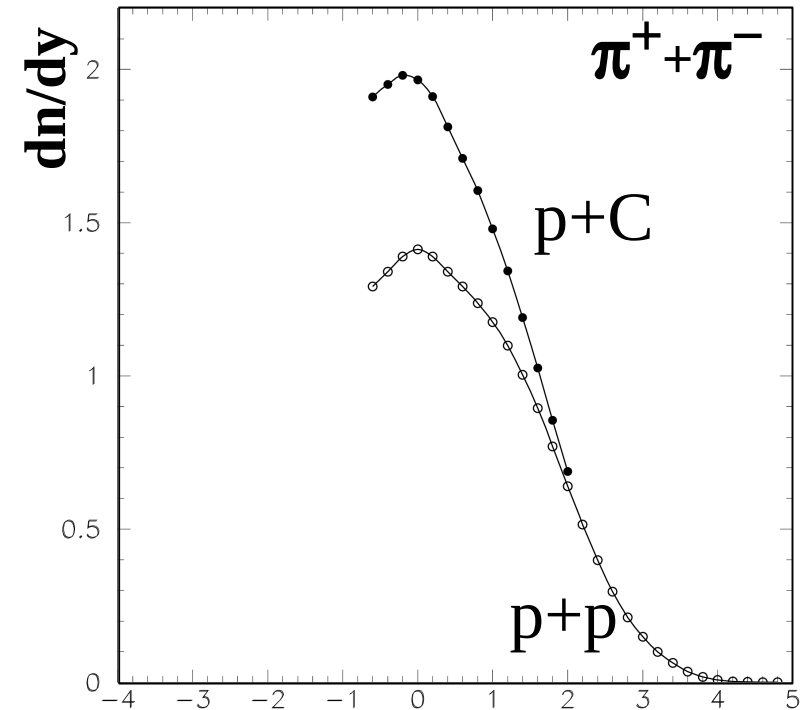
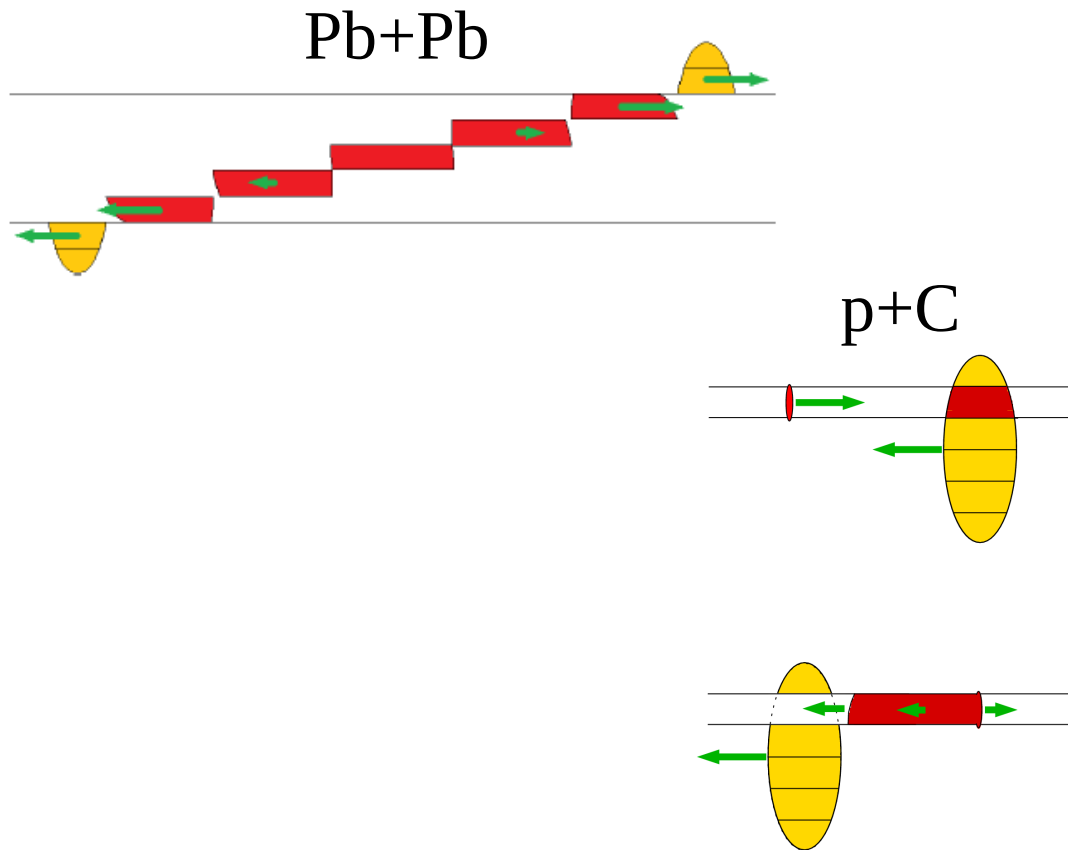
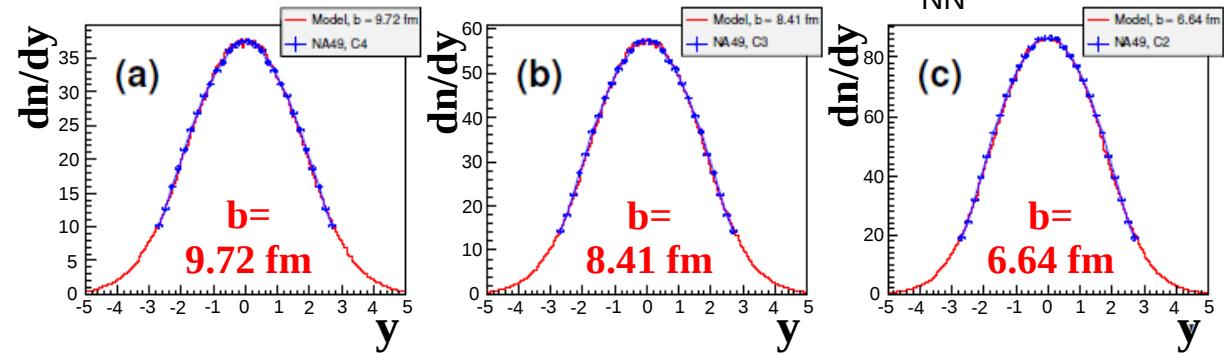
total fire streak energy

sum of brick masses

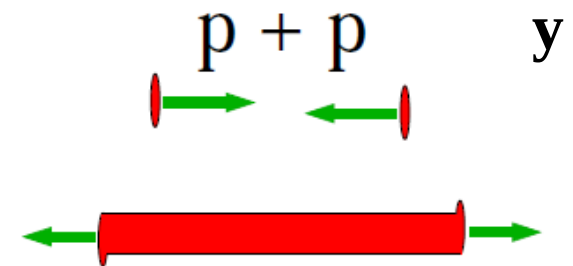
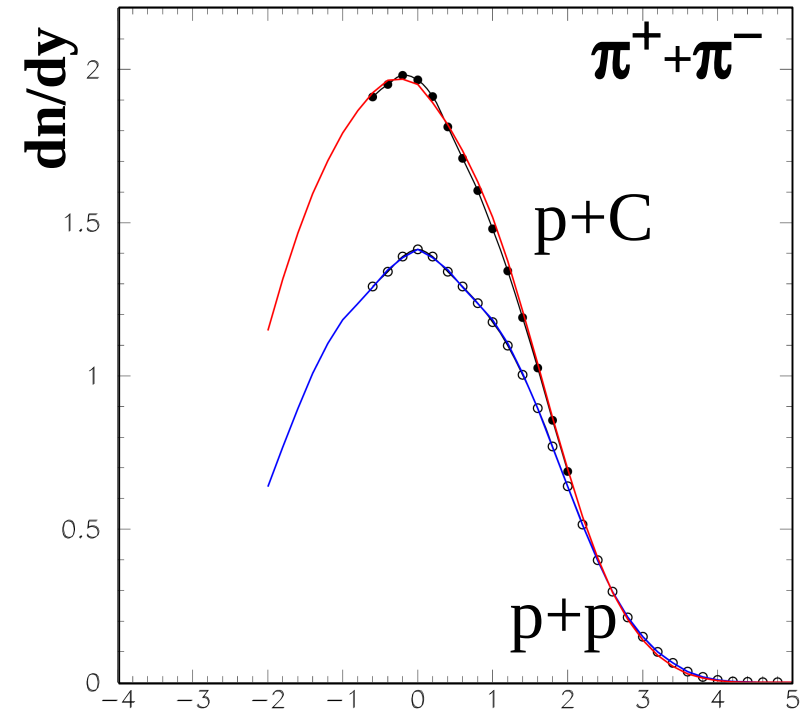
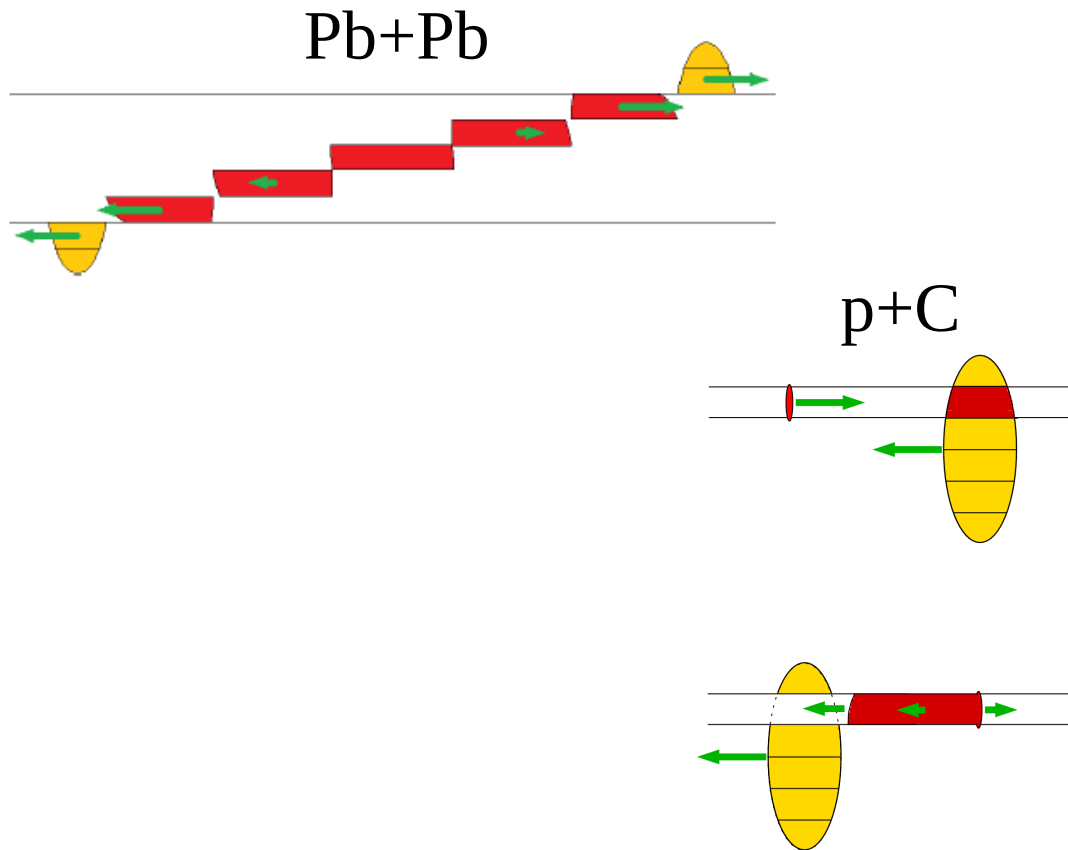
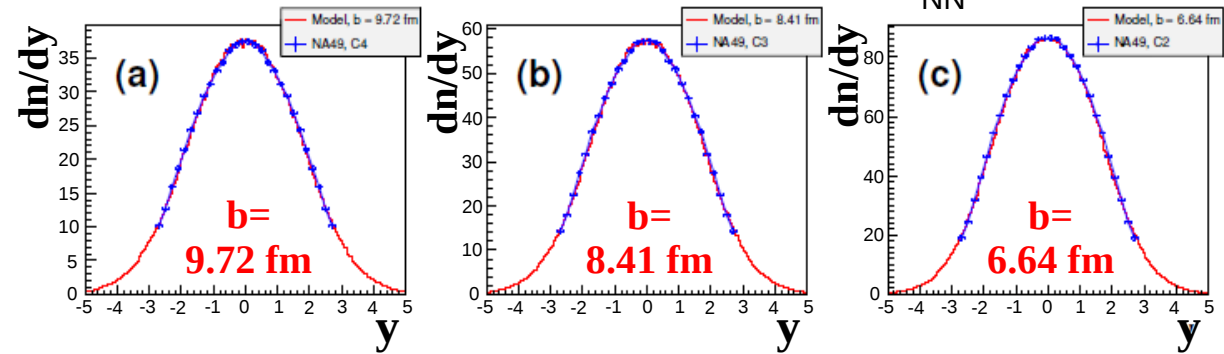


Courtesy by Harsch Shah, S.Hoche, arXiv: 1411.4085

- Link between p+p, p+A, and A+A collisions.

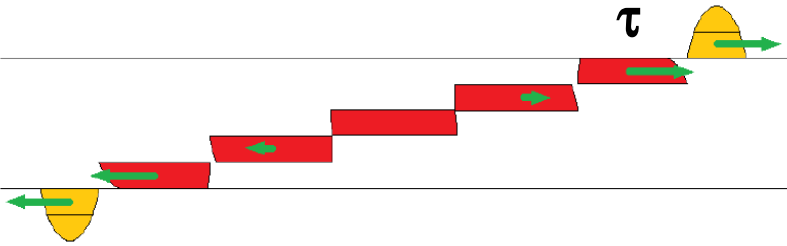


- Link between p+p, p+A, and A+A collisions.



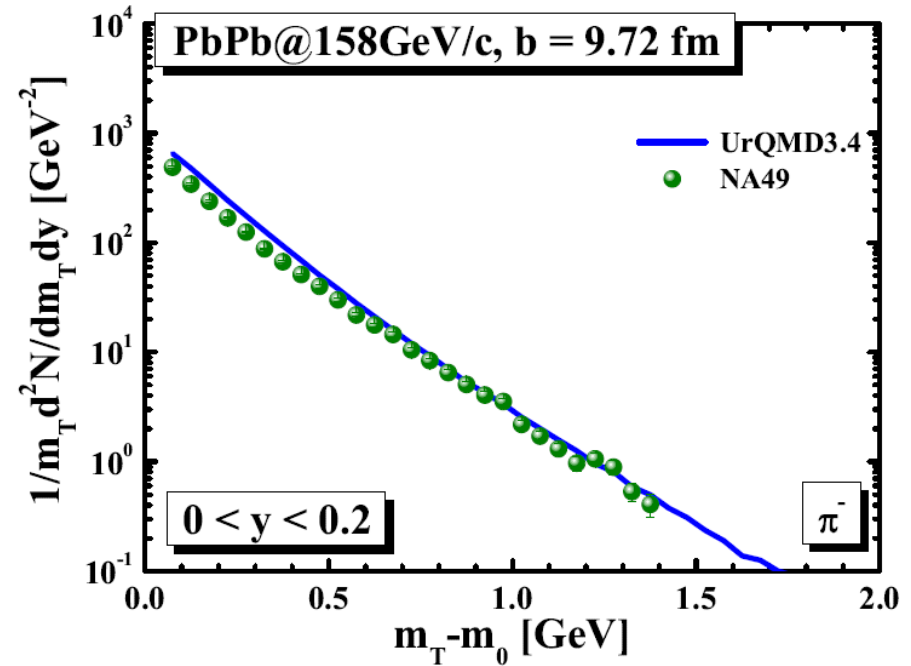
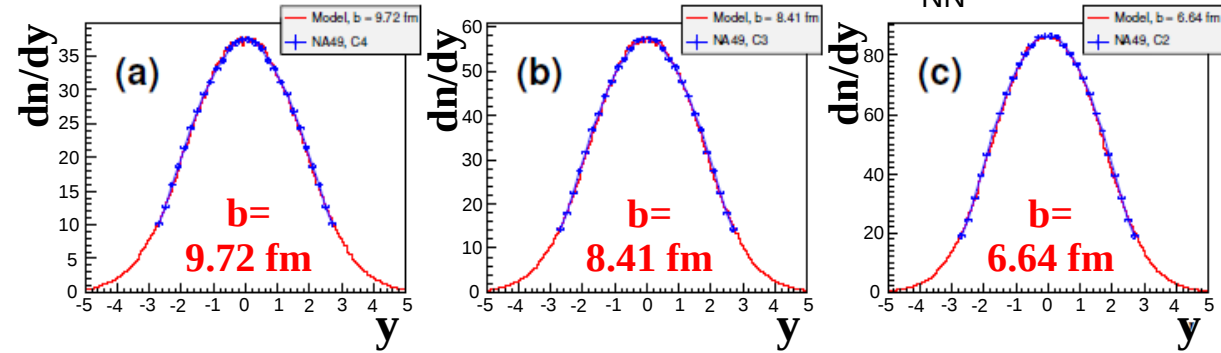
## Implementation of our model for studies of EM effects:

- Initial longitudinal evolution of the system → from our model ;
- Initial (before the action of the EM field) rapidity distribution of pions → from our model ;



- Initial  $p_T$  distribution of pions → from UrQMD v3.4 ;
- The pion creation time  $\tau$  (taken in the fire streak c.m.s.) → taken as free parameter ;
- Isospin effects between  $\pi^+$  and  $\pi^-$  → included → PRC 99 (2019) 024908 ;
- Fragmentation (expansion) of the spectator charge → included optionally;
- Azimuthal anisotropies (“flow”) → included optionally.

NA49,  $\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 17.3$  GeV





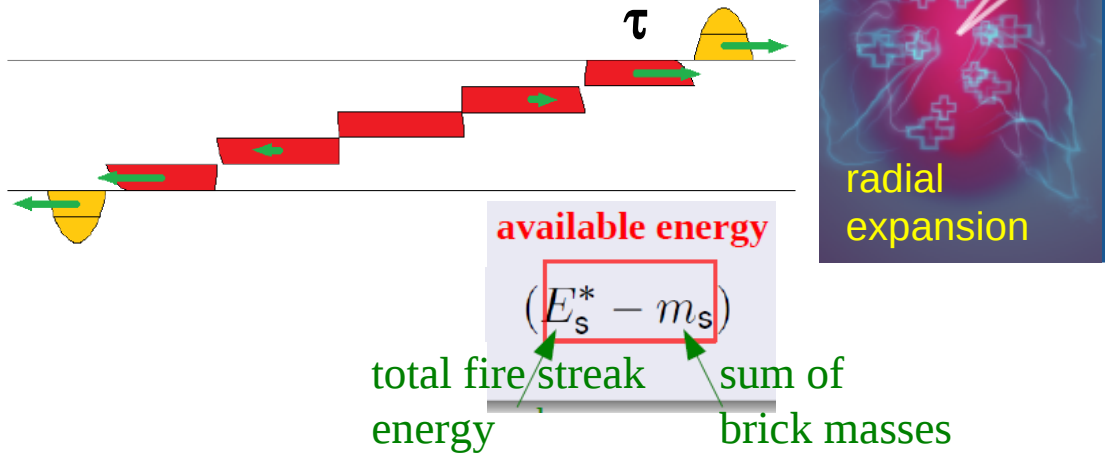
# Implementation of our model for studies of EM effects, state of the art:

- Simple parametrization of pion creation time :  $\tau = a(E_s^* - m_s) + \tau_0$

$$a \approx 0.08$$

$$\tau_0 = 0.5 \text{ fm}/c$$

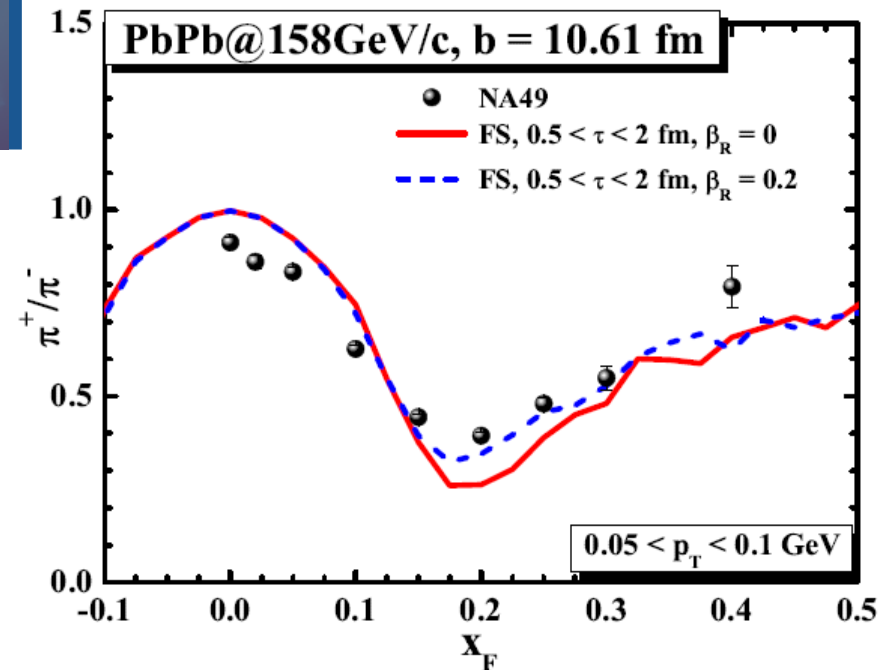
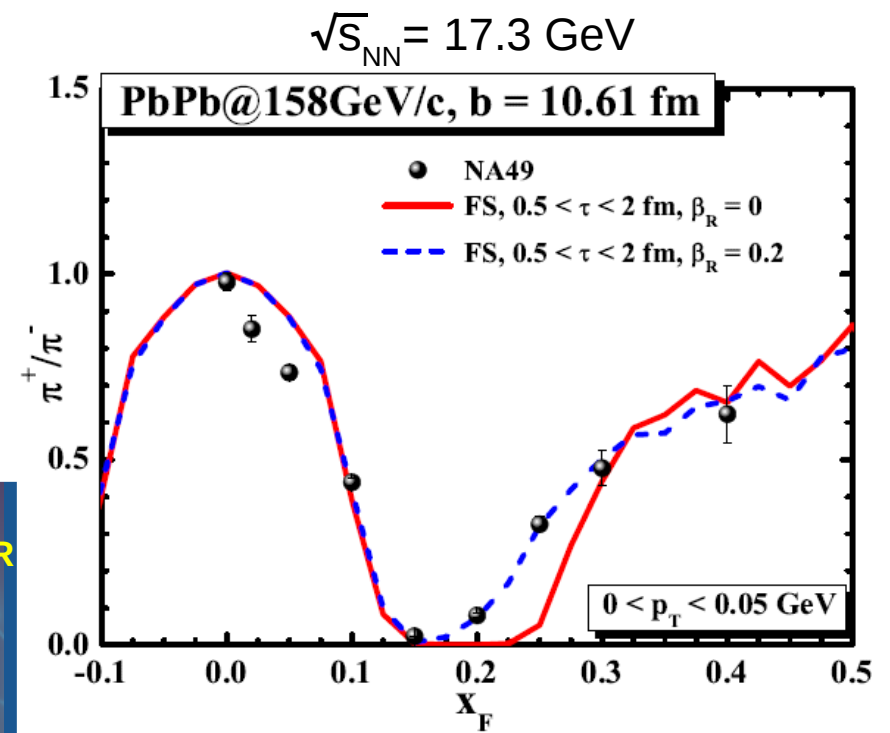
- Radial expansion assumed for spectator system.



→ Reasonable agreement with data for  $x_F \geq 0.1$ .

→ Inclusion of spectator expansion improves the description ;

→ **Short pion creation times** (  $0.5 < \tau < 2 \text{ fm}/c$ , to be compared with  $\sim 5.5 \text{ fm}/c$  at  $y=0$ ).



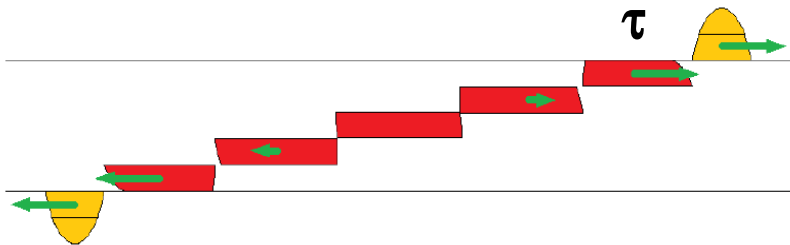
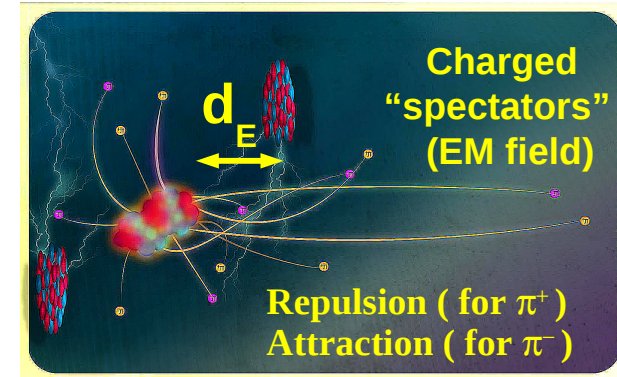
# 4) Summary

Spectator-induced electromagnetic (EM) effects can be used to study the **space-time evolution of particle production**.

Our studies have shown that in high energy nucleus-nucleus collisions, **faster** pions are produced **closer** to the spectator system, and provided an **independent estimate** for the time of pion creation, at  $y=0$ .

On that basis, we built a simple phenomenological model with realistic initial conditions (incidentally we found that it **works** for all the three reaction types). This we used to study the space-time evolution of the system w.r.t. forward production of **fast ( $x_F > 0.1$ ) pions**.

This study gives an indication that relatively **short** pion production time scales (proper pion creation times  $\tau$ ) are needed to describe the experimental data.



*Thank you !*

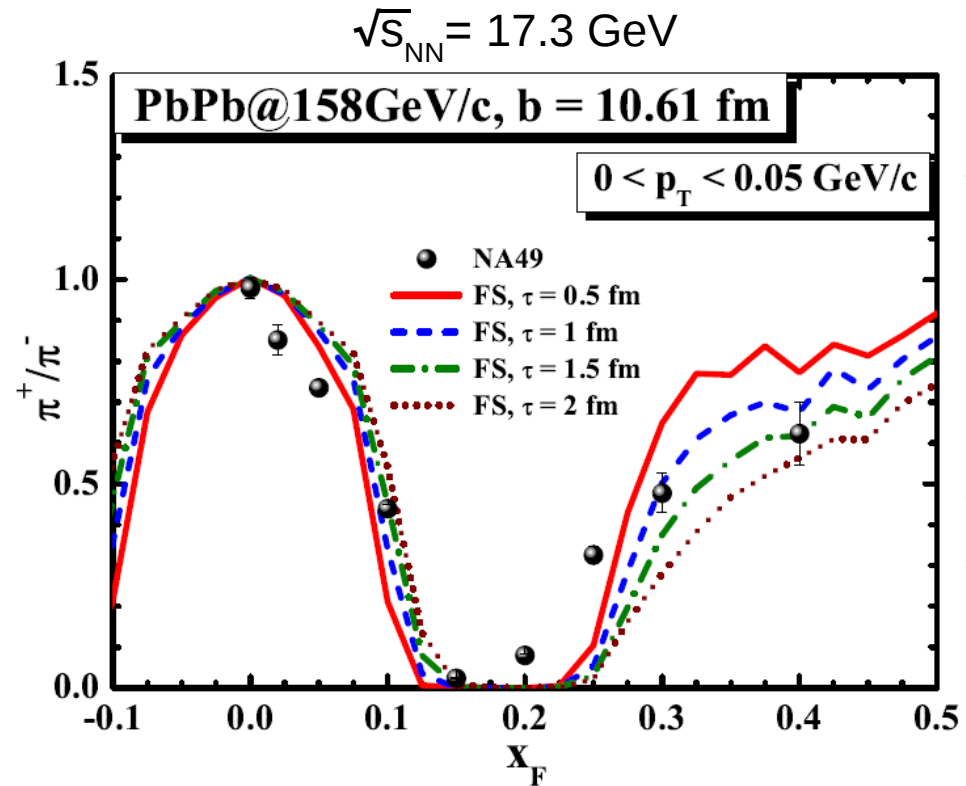
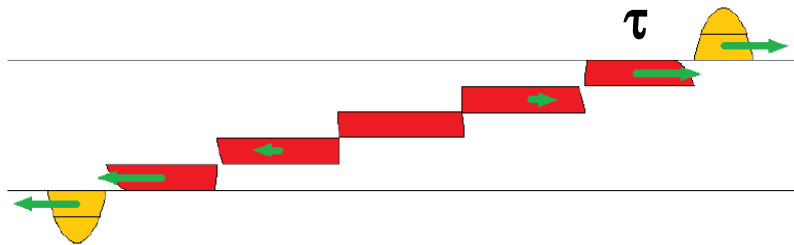
# Acknowledgments.

This work was supported by the National Science Centre, Poland  
(grant no. 2014/14/E/ST2/00018).

# *Extra slides*

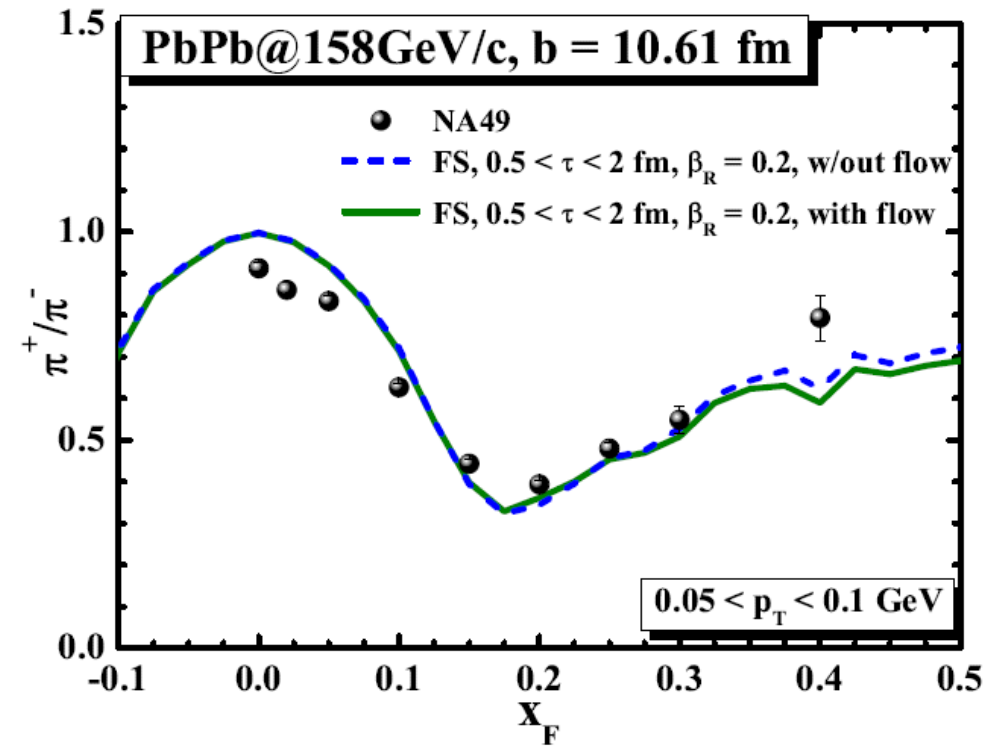
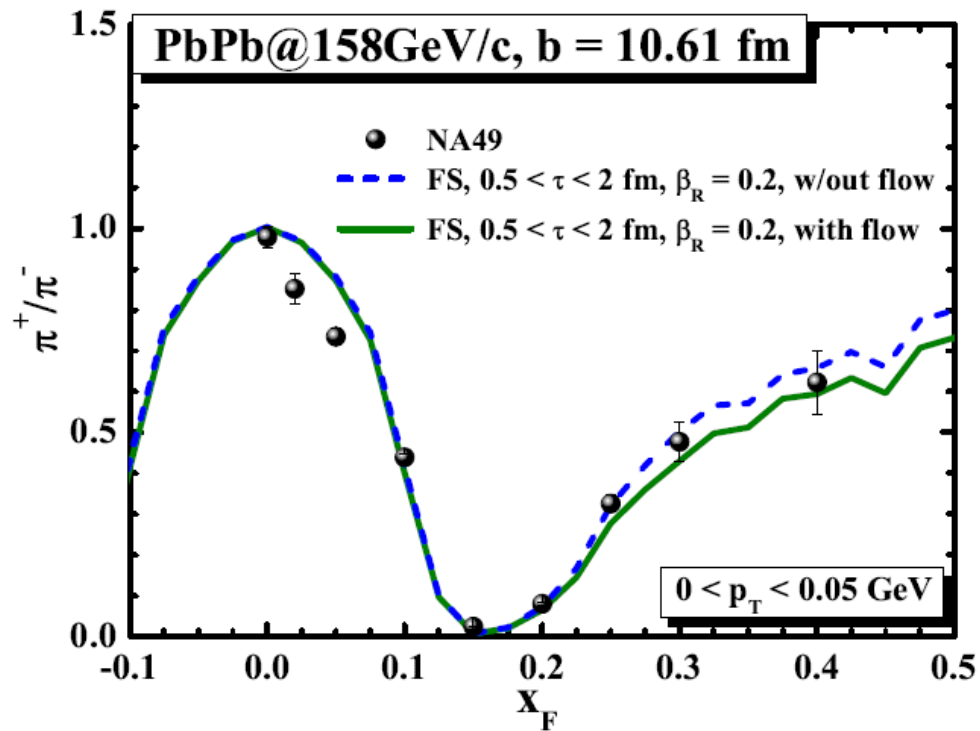
## Implementation of our model for studies of EM effects, first results:

- Fixed pion creation time  $\tau$  (in fire streak rest frame) ;
- No spectator fragmentation.

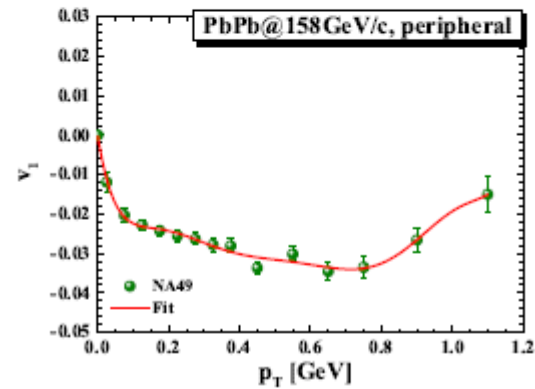
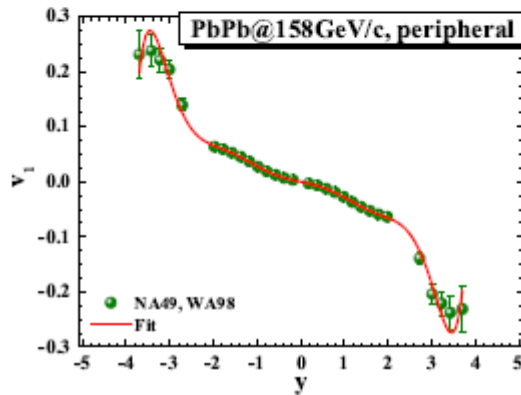
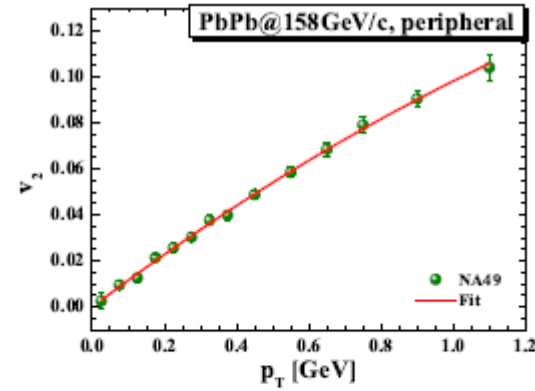
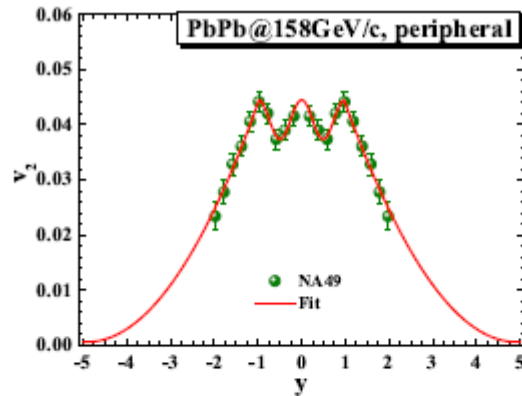


- ➔ Relatively **short pion creation times** are suggested by the exp. data ( $\tau \sim 0.5 - 1.5 \text{ fm/c}$ , to be compared with  $\sim 5.5 \text{ fm/c}$  at  $y=0$ ) ;
- ➔ Impossible to fit the data with **one single value** of  $\tau$  ;
- ➔ Evident **problem** at  $x_F = 0.2 - 0.25$ .

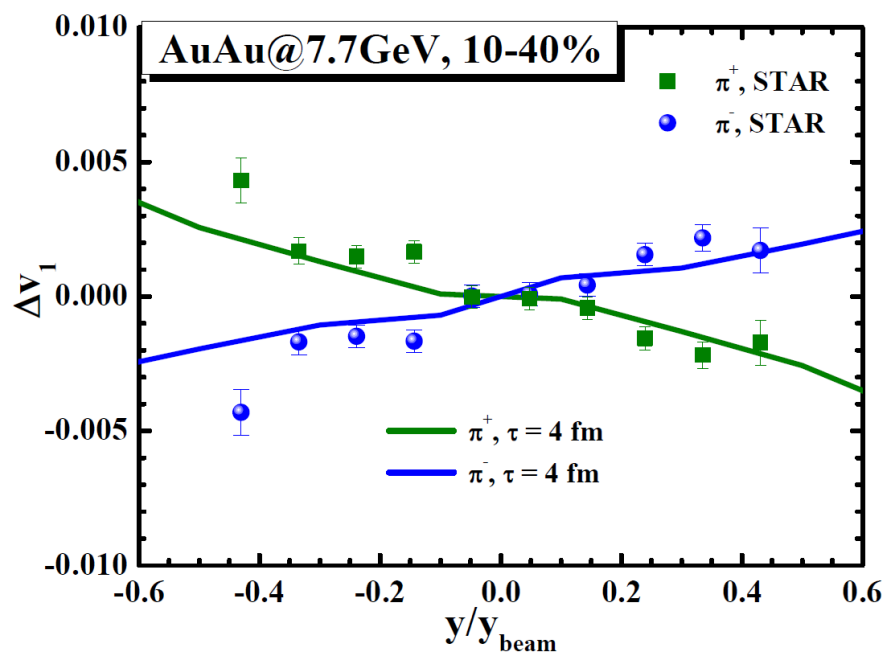
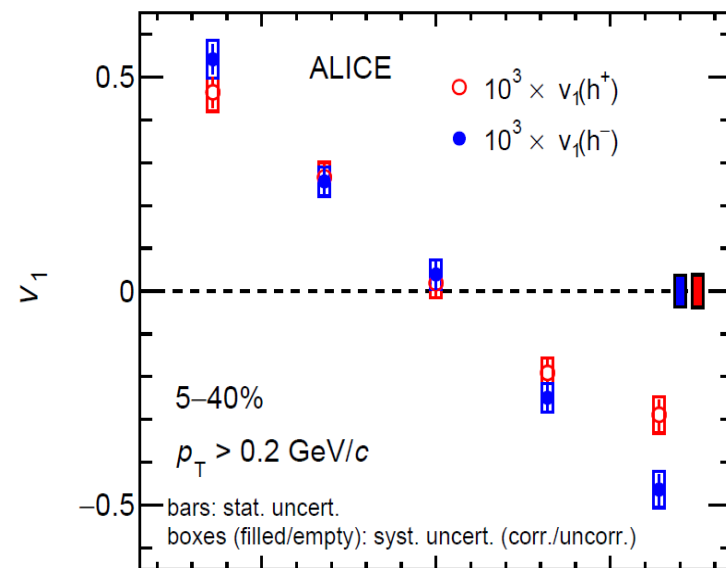
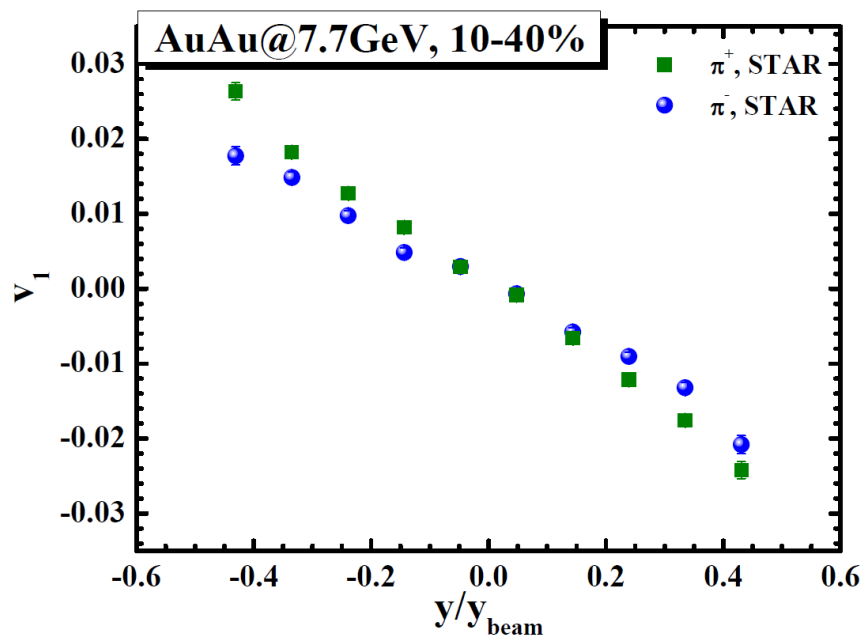
## Influence of azimuthal anisotropies (flow) on $\pi^+/\pi^-$ ratios



## Inclusion of azimuthal anisotropies (flow) in the model

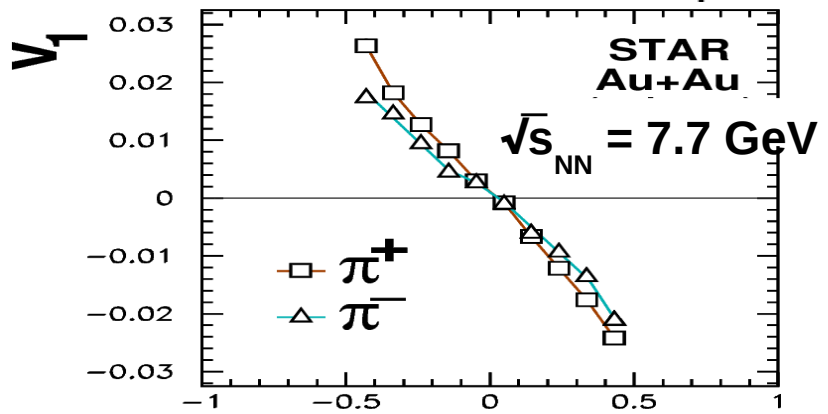
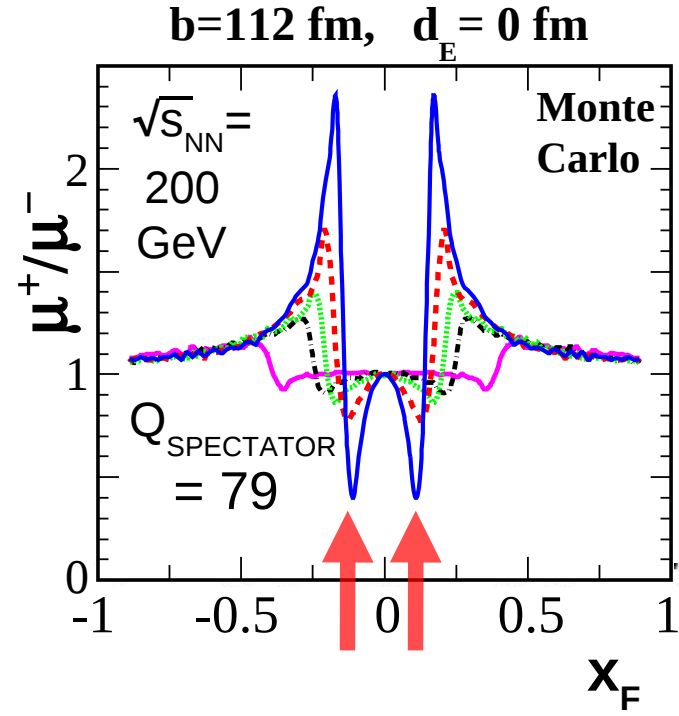
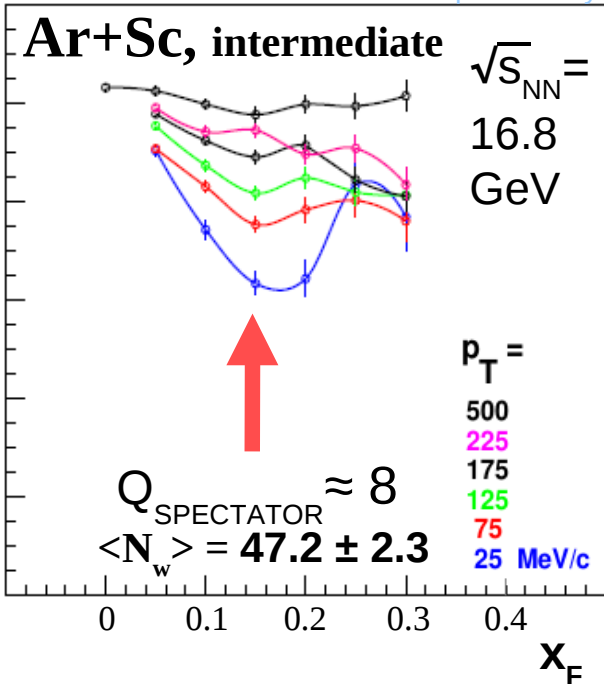
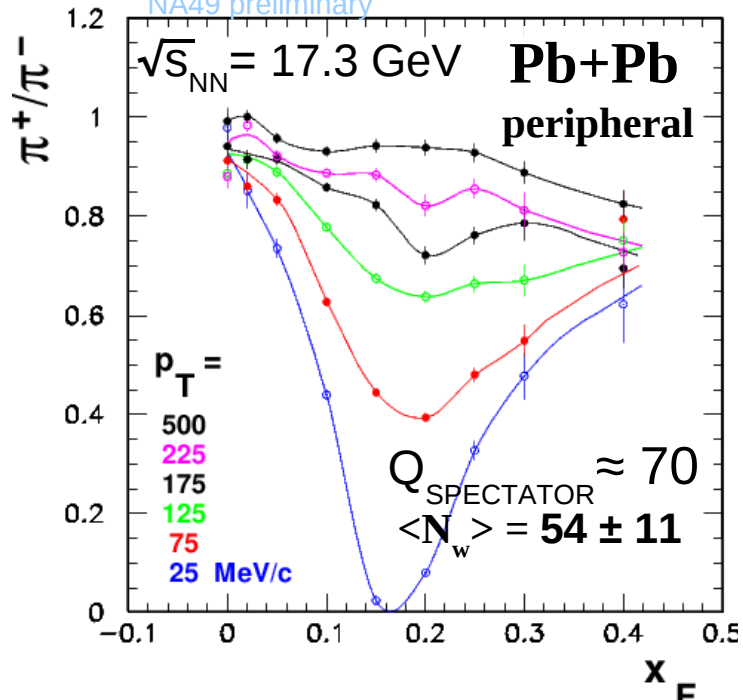


## More on asimuthal anisotropies (flow)

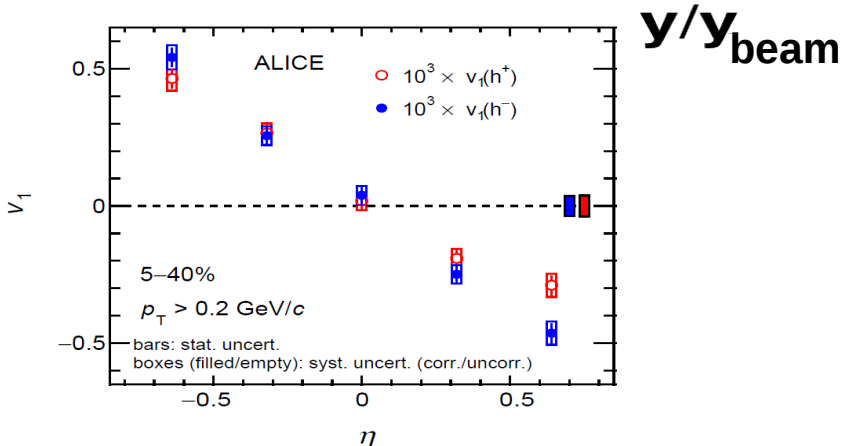
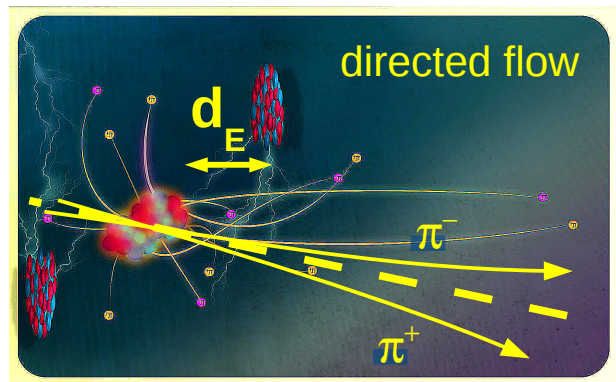


STAR:  
L. Adamczyk et al., PRL 112 (2014) 162301  
ALICE:  
S. Acharya et al., arXiv:1910.14406 [nucl-ex]



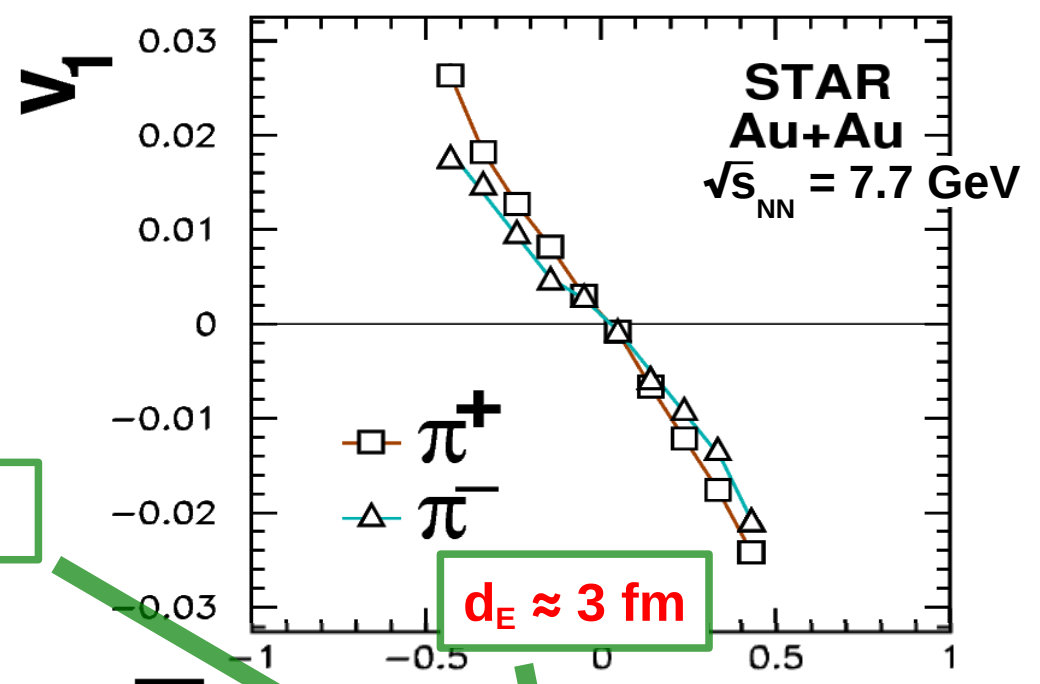
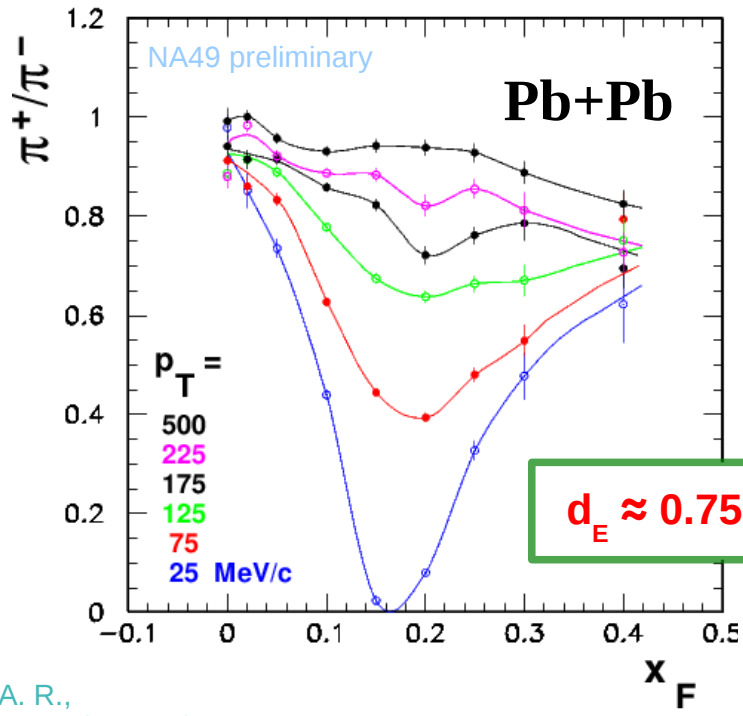


STAR:  
L. Adamczyk et al., PRL 112 (2014) 162301  
ALICE:  
S. Acharya et al., arXiv:1910.14406 [nucl-ex]

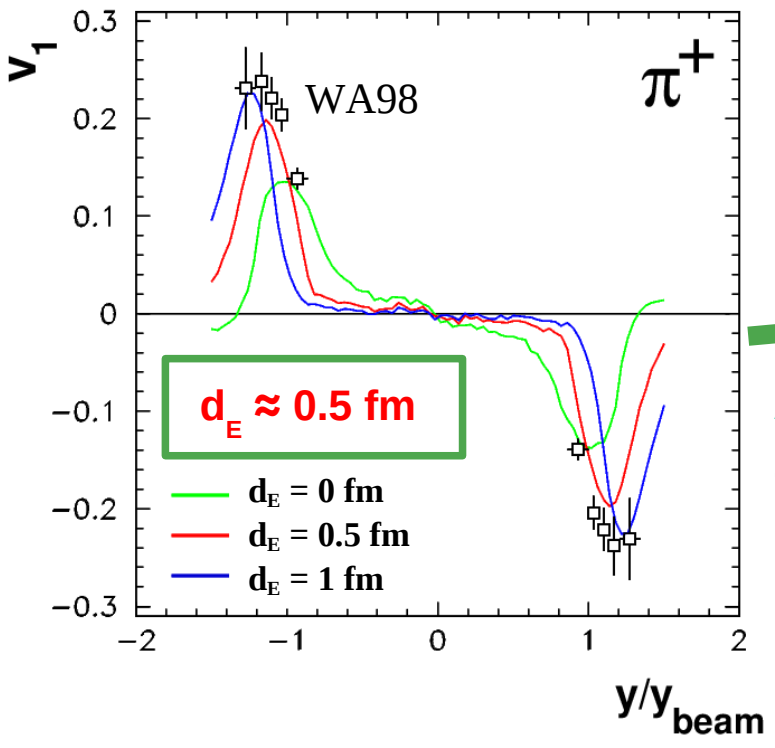


- $v_1$  (“directed flow”) is the sidewards deflection of pions in the reaction plane :  

$$v_1 \equiv \langle \cos(\varphi \text{ w.r.t. reaction plane}) \rangle$$
- the spectator charge induces *charge splitting* of  $v_1$ .

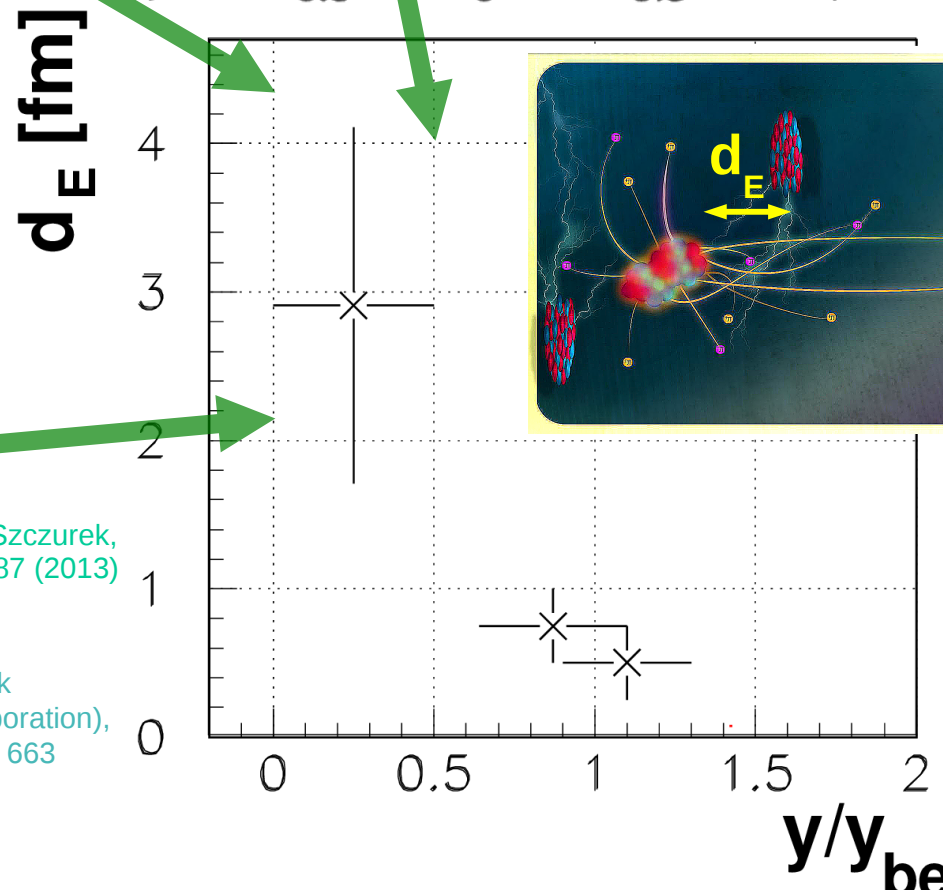


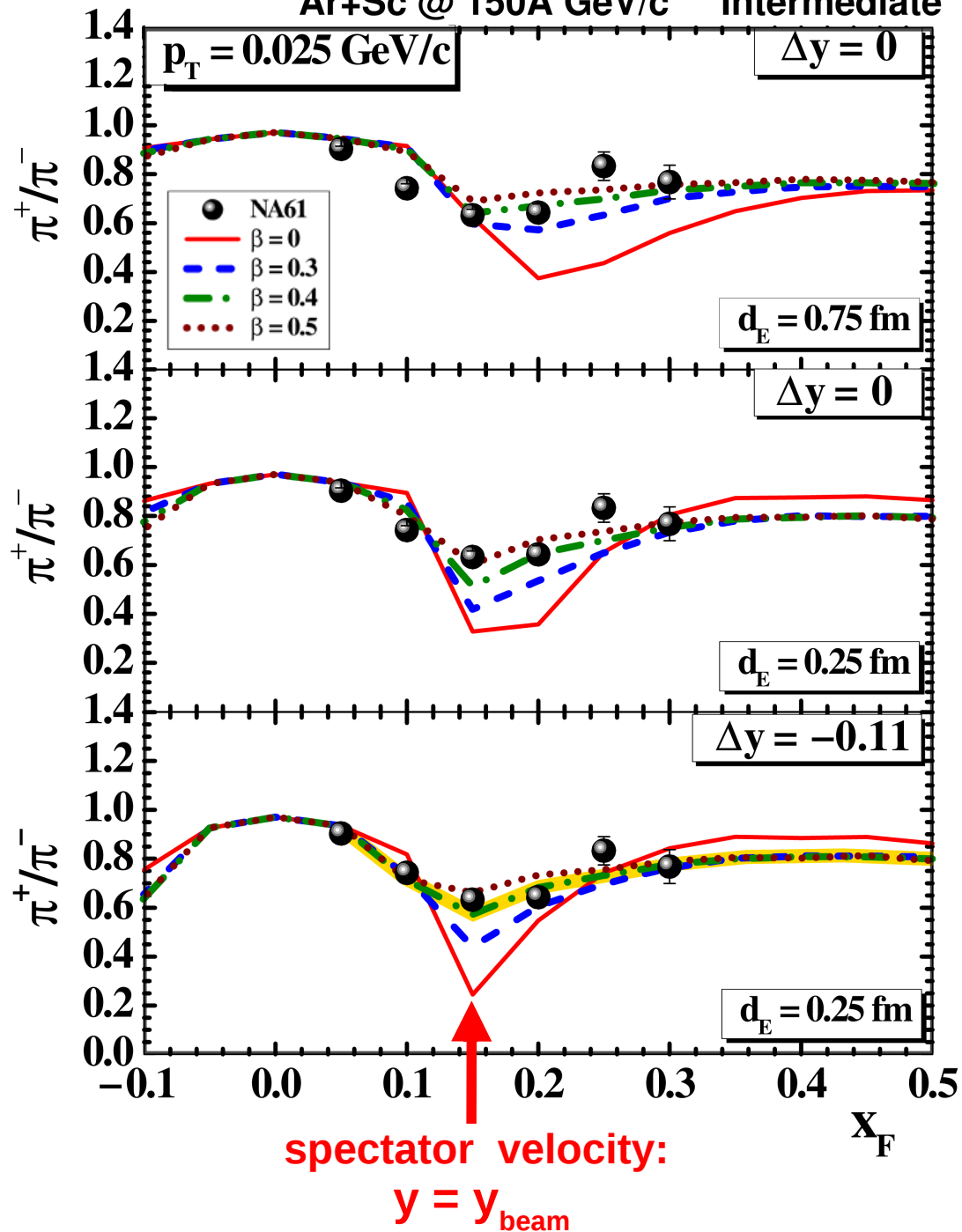
A. R.,  
Acta Phys. Polon.  
B42 (2011) 867



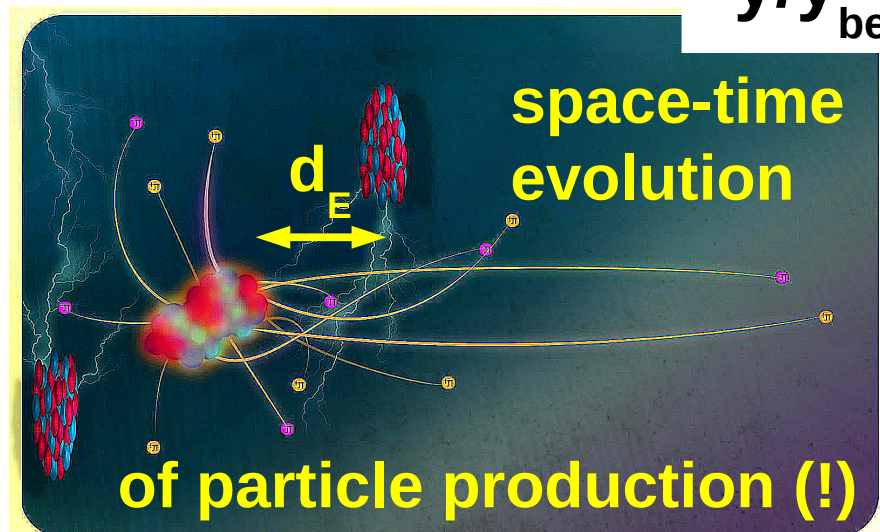
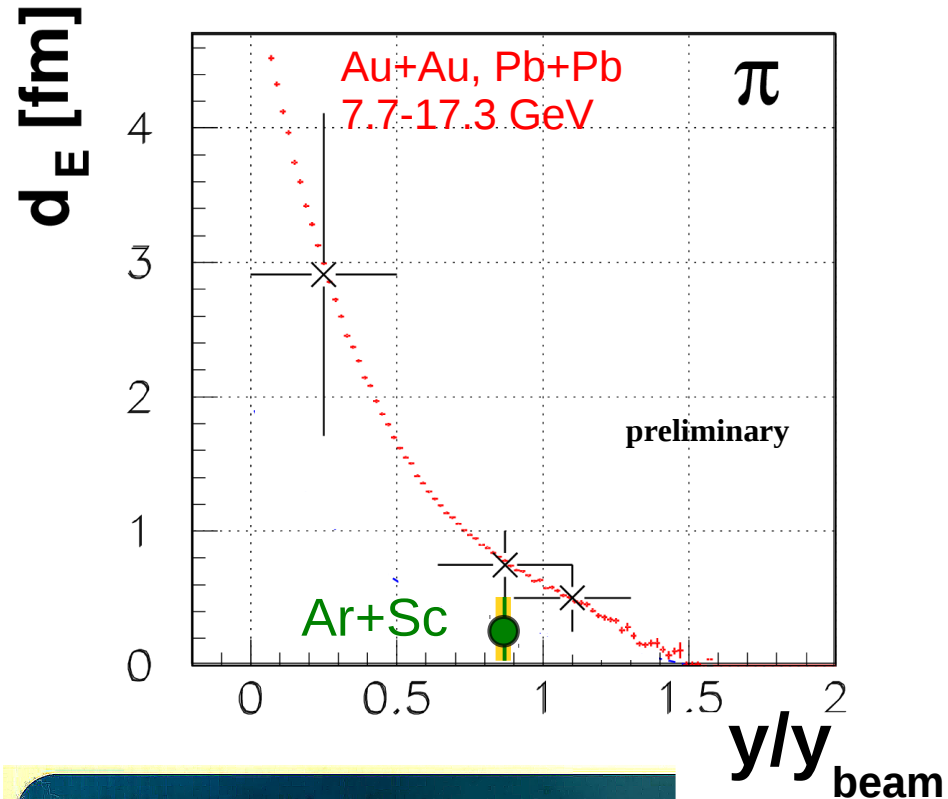
A. R. and A. Szczurek,  
Phys. Rev. C87 (2013)  
054909.

H. Schlagheck  
(WA98 Collaboration),  
Nucl. Phys. A 663  
(2000) 725.

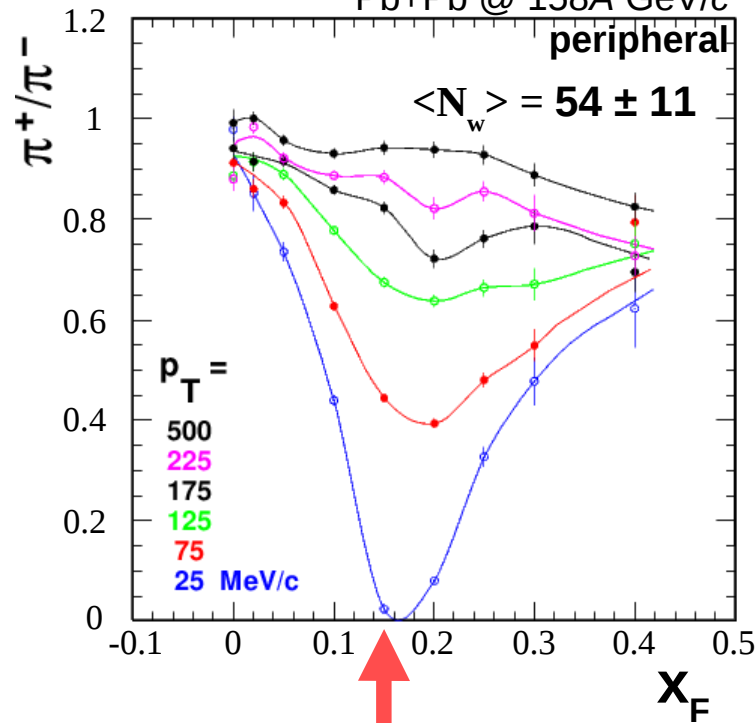




EM effects from NA61/SHINE

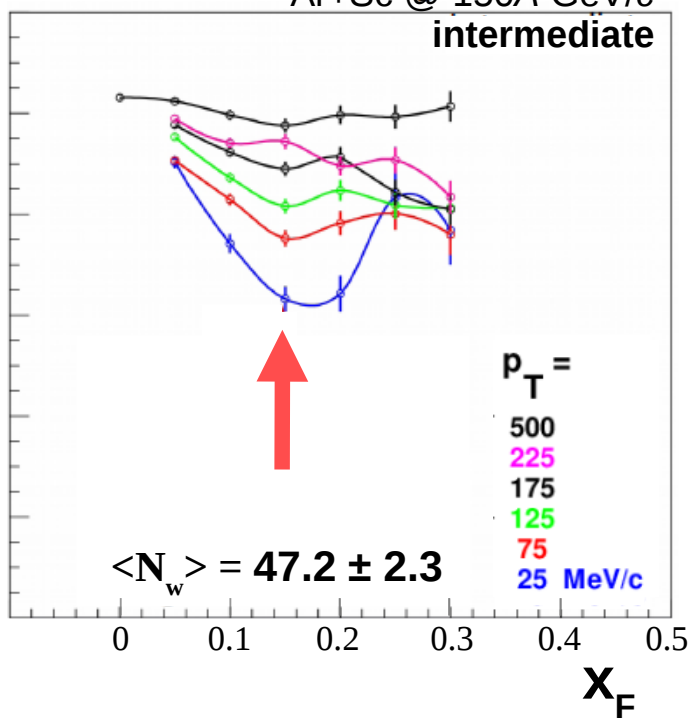


NA49 preliminary  
Pb+Pb @ 158A GeV/c



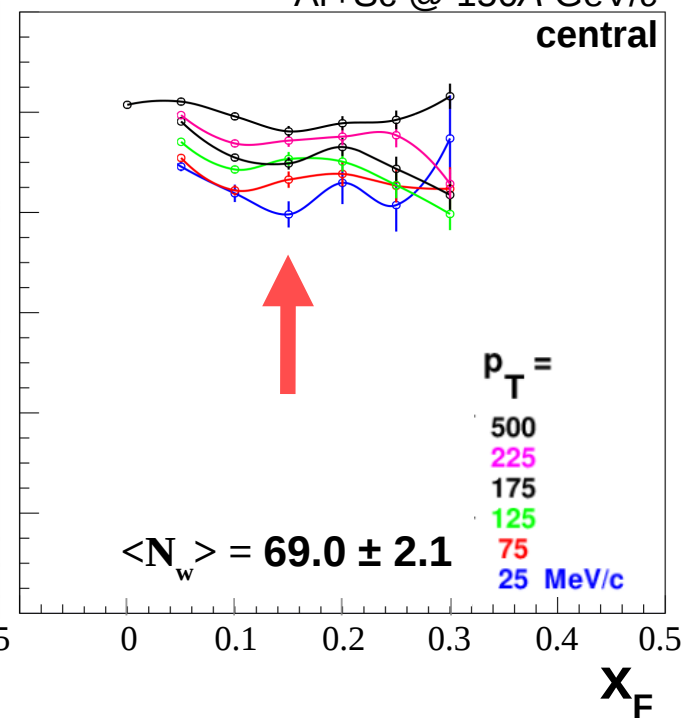
**spectator velocity:**  
 $y = y_{\text{beam}}$

NA61/SHINE preliminary  
Ar+Sc @ 150A GeV/c



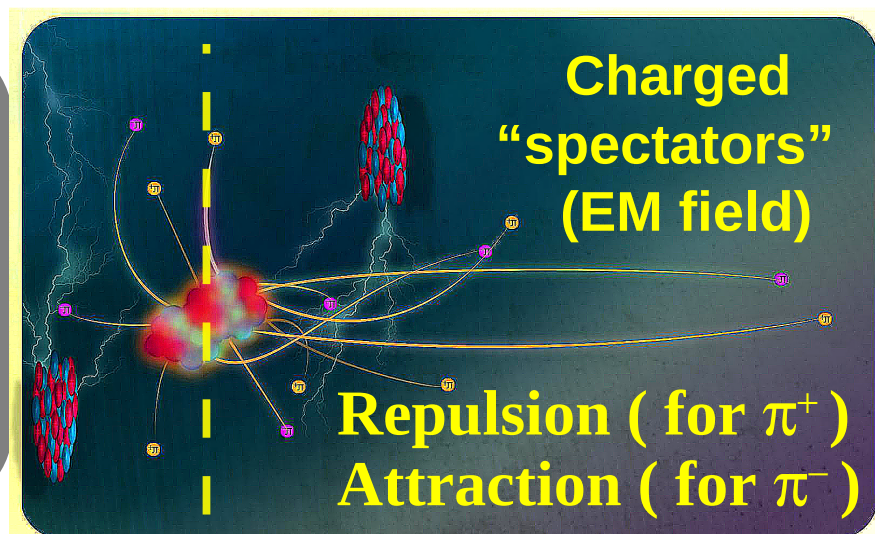
$$x_F = \frac{p_L}{p_L^{\text{beam}}} \quad (\text{c.m.s.})$$

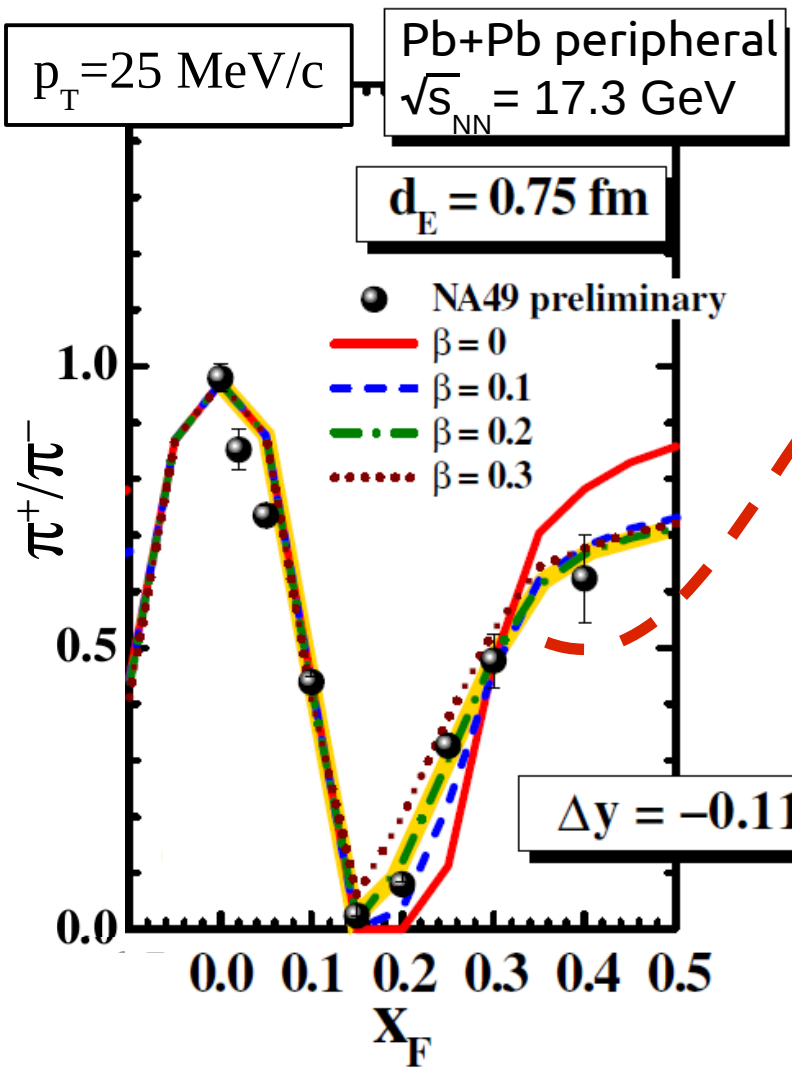
NA61/SHINE preliminary  
Ar+Sc @ 150A GeV/c



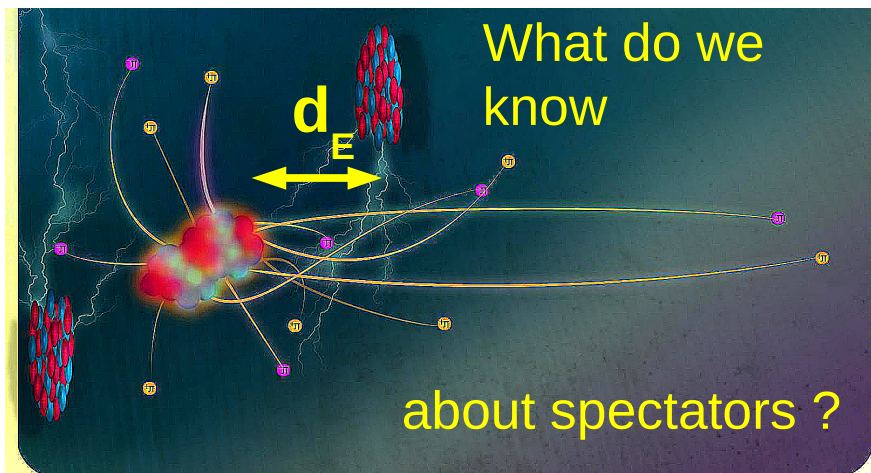
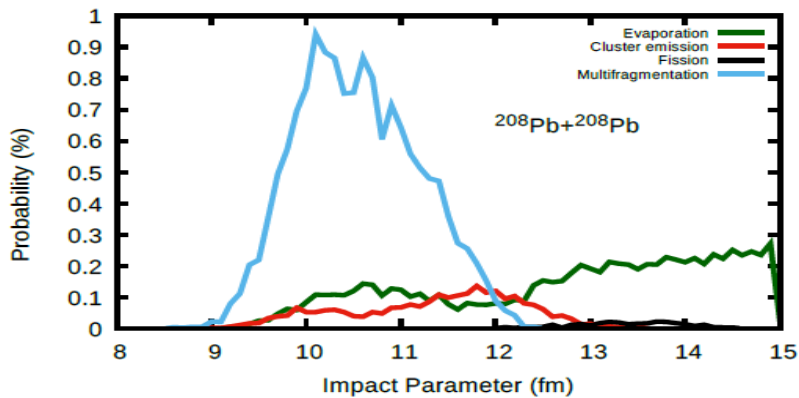
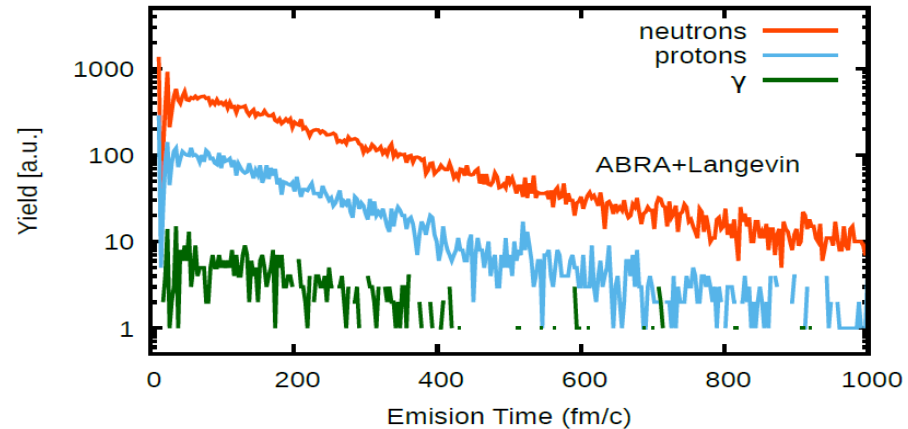
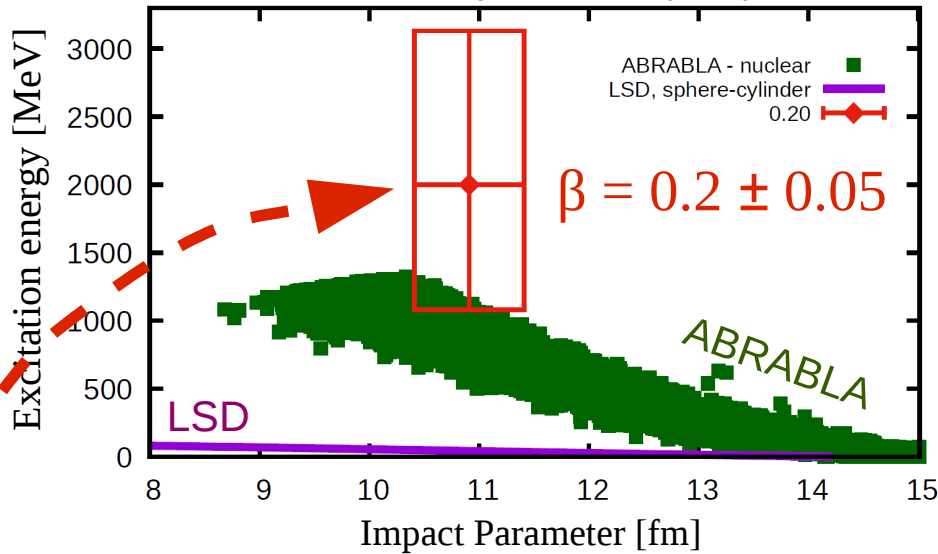
A. Marcinek,  
Acta Phys. Polon. B50 (2019) 1127

- (a) Peripheral Pb+Pb ( $Q_{\text{SPECTATOR}} \approx 70$ )  
→ large EM effect,  $\pi^+/\pi^- \approx 0$ .
- (b) Intermediate Ar+Sc ( $Q_{\text{SPECTATOR}} \approx 8$ )  
→ visible EM effect, breaks isospin symmetry.
- (c) Central Ar+Sc ( $Q_{\text{SPECTATOR}} \approx 3$ )  
→ still visible shadow of EM effect.





**Spectators**

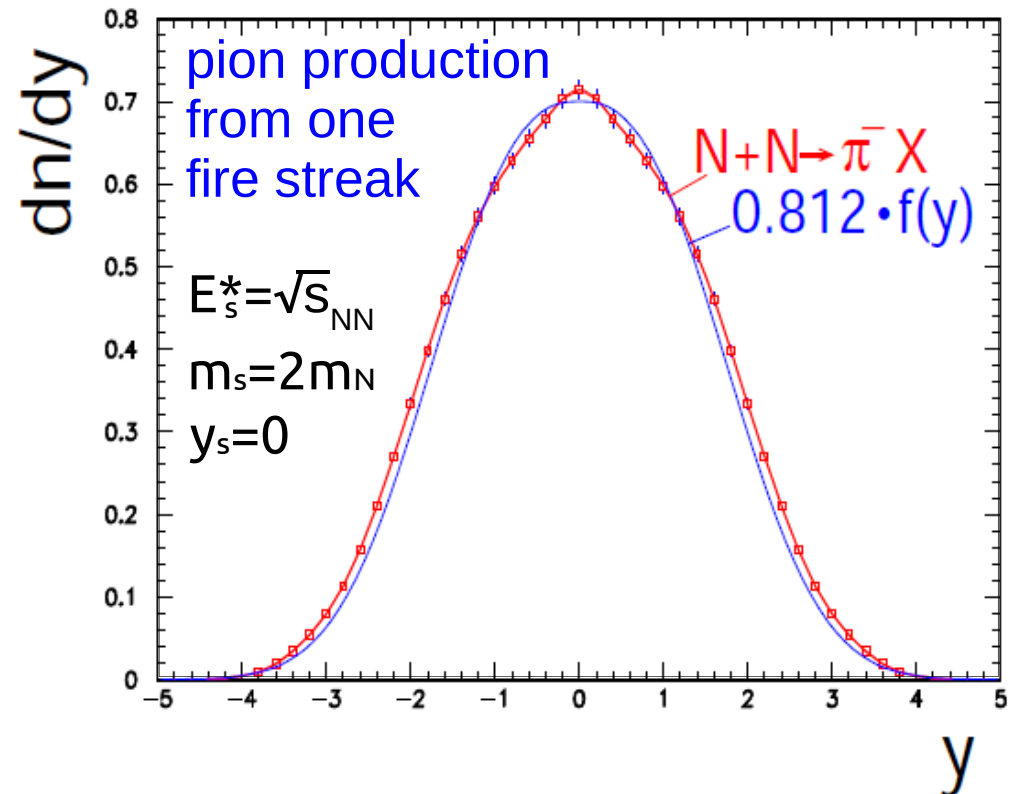
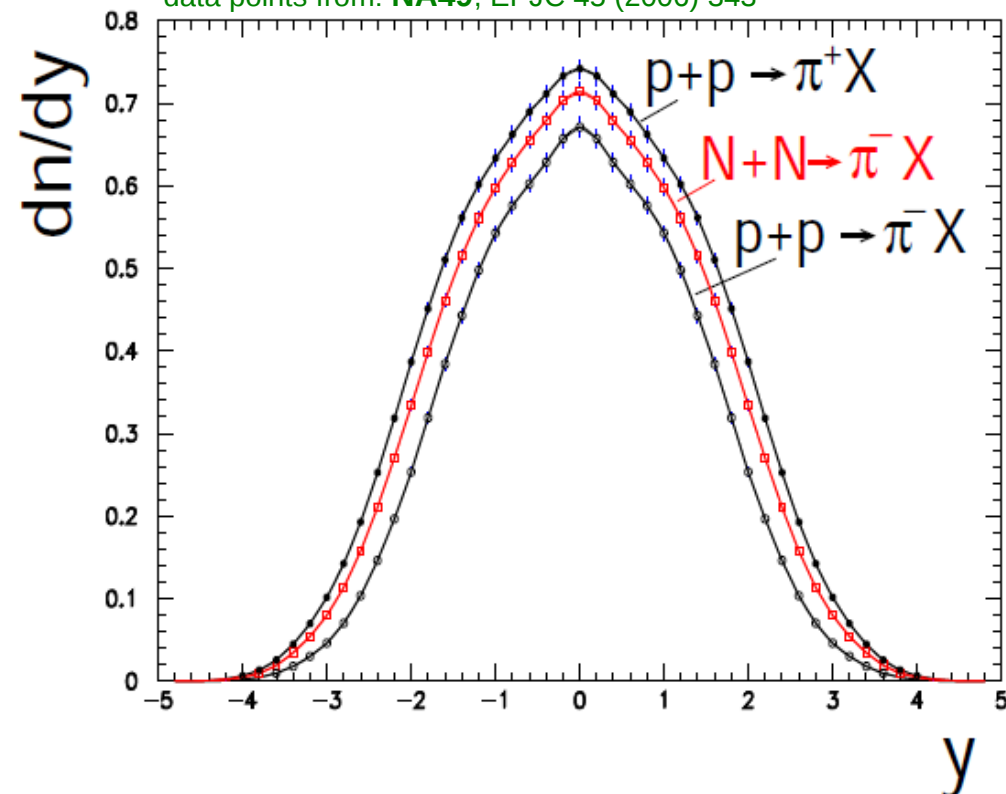


## Isospin effects

- Pb+Pb collision: **40%** protons, **60%** neutrons ;
- **p+p** → **π<sup>-</sup>X** is not directly comparable to **Pb+Pb** → **π<sup>-</sup>X** !
- isospin symmetry:  $\frac{dn}{dy}(n \rightarrow \pi^-) = \frac{dn}{dy}(p \rightarrow \pi^+)$
- isospin-averaged  $\pi^-$  distribution:

$$\frac{dn}{dy}(N + N \rightarrow \pi^- X) = \left(\frac{Z}{A}\right) \cdot \frac{dn}{dy}(p + p \rightarrow \pi^- X) + \left(1 - \frac{Z}{A}\right) \cdot \frac{dn}{dy}(p + p \rightarrow \pi^+ X)$$

data points from: **NA49**, EPJC 45 (2006) 343



Once isospin is taken into account, the difference in absolute scaling between p+p and Pb+Pb collisions changes from **0.748** to **0.812** .

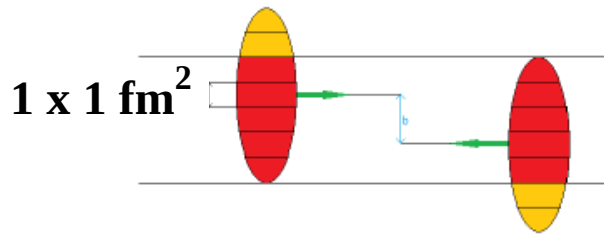
Includes:

- characteristics of “fire streaks”
- computation of energy balance
- energy dependence
- auxiliary information on proton-nucleus

## ***More on our simple model***

For a more extended description including formulae, numerical values, tables and plots, please see  
PRC 99 (2019) 024908

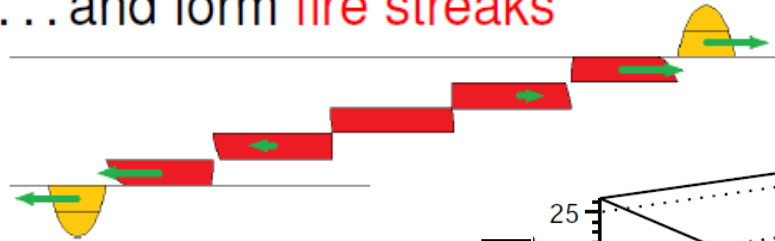
Bricks collide ...



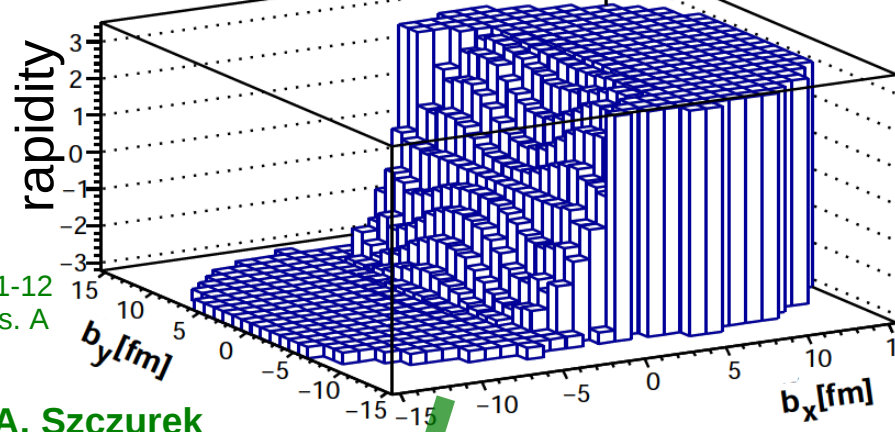
R. Hagedorn, CERN-71-12  
W.D. Myers, Nucl. Phys. A

(Re)invented by A. Szczurek

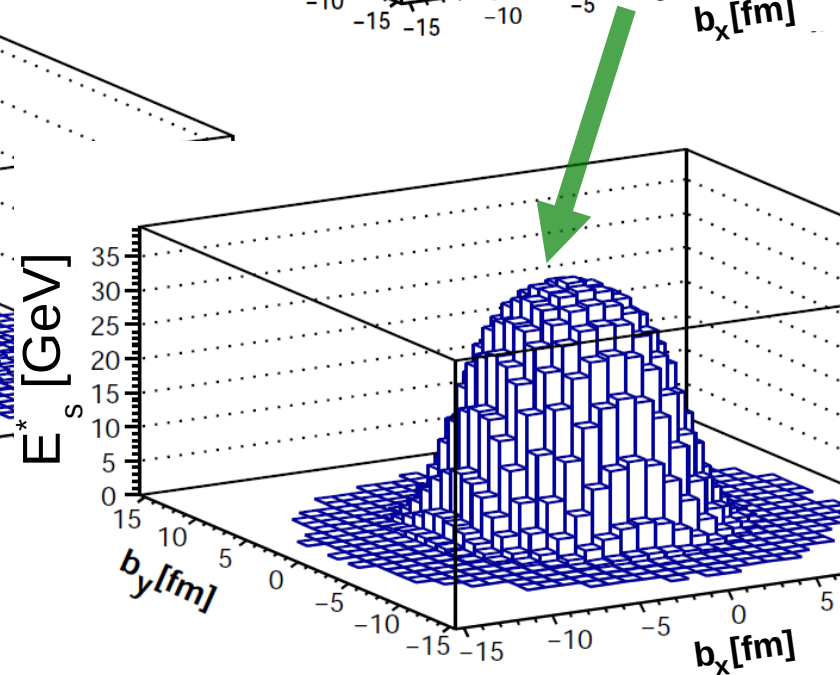
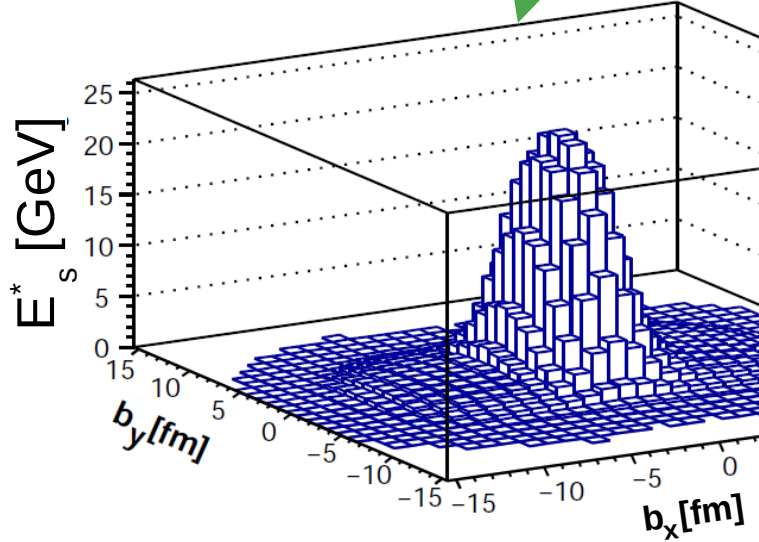
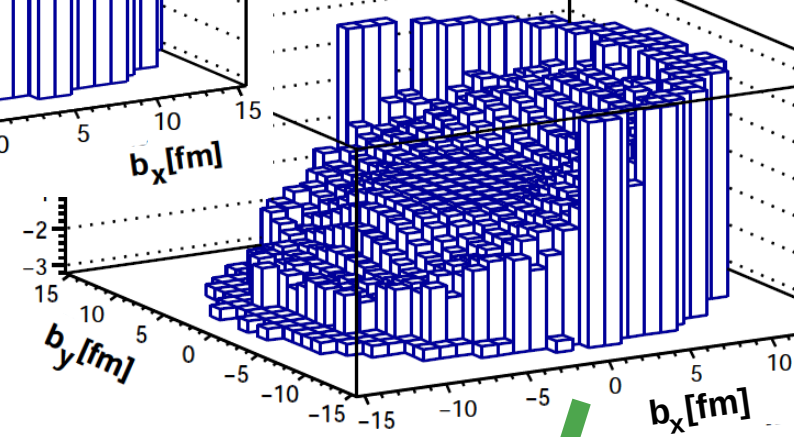
... and form **fire streaks**



**Peripheral (b=9.72 fm)**

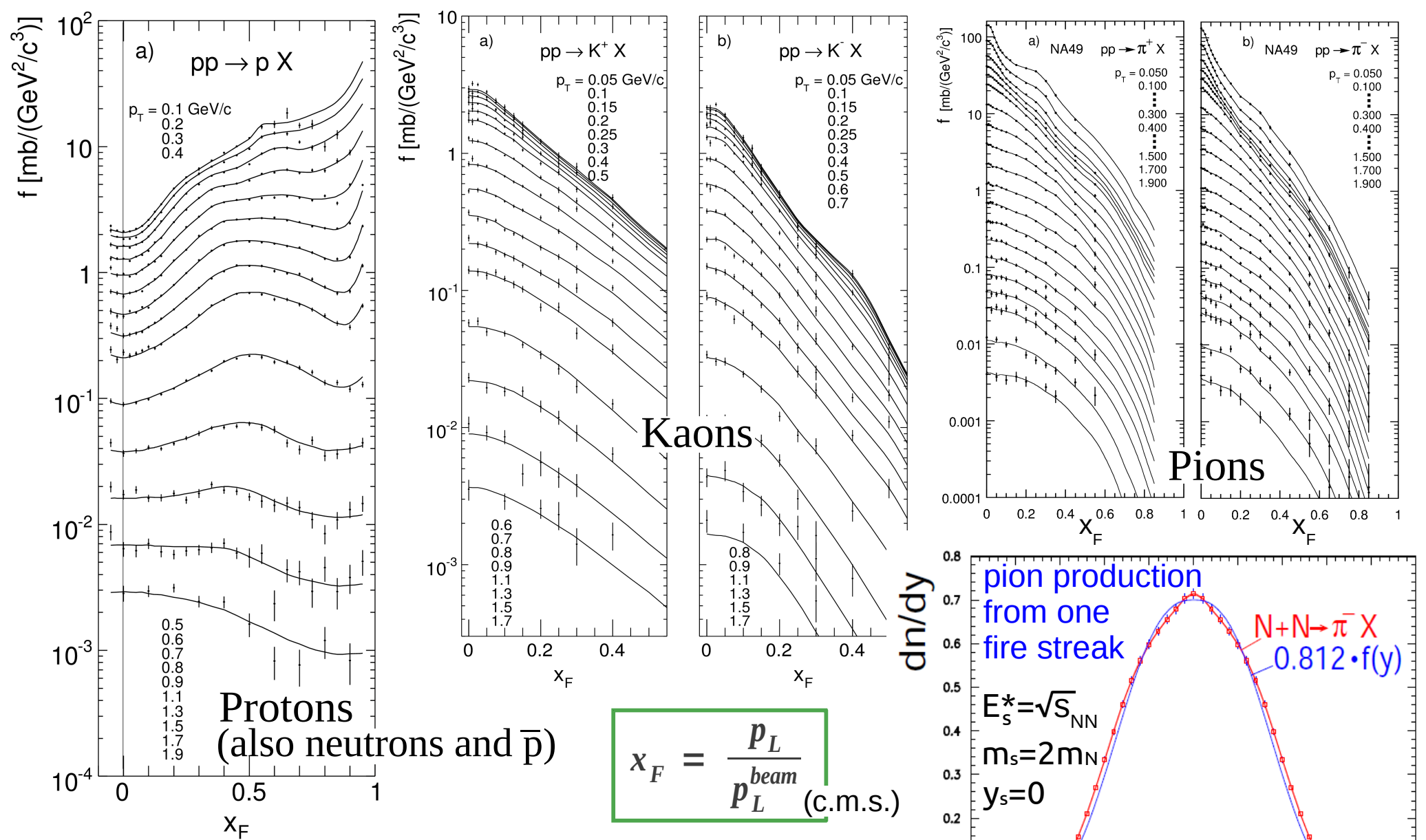


**Central (b=2.55 fm)**



**Characteristics of “fire streaks”**





In  $p+p$  collisions, the average energies of pions, kaons and protons can be computed **directly from their spectra** :

$$\langle E_i \rangle = \frac{\int_0^1 \int_0^{p_T(\max)} E_i(x_F, p_T) \cdot \left( \frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}{\int_0^1 \int_0^{p_T(\max)} \left( \frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}$$

$i$  – proton,  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , ...

## Calculation of energy balance (simplified):

$$\langle E_i \rangle = \frac{\int_0^1 \int_0^{p_T(\max)} E_i(x_F, p_T) \cdot \left( \frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}{\int_0^1 \int_0^{p_T(\max)} \left( \frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}$$

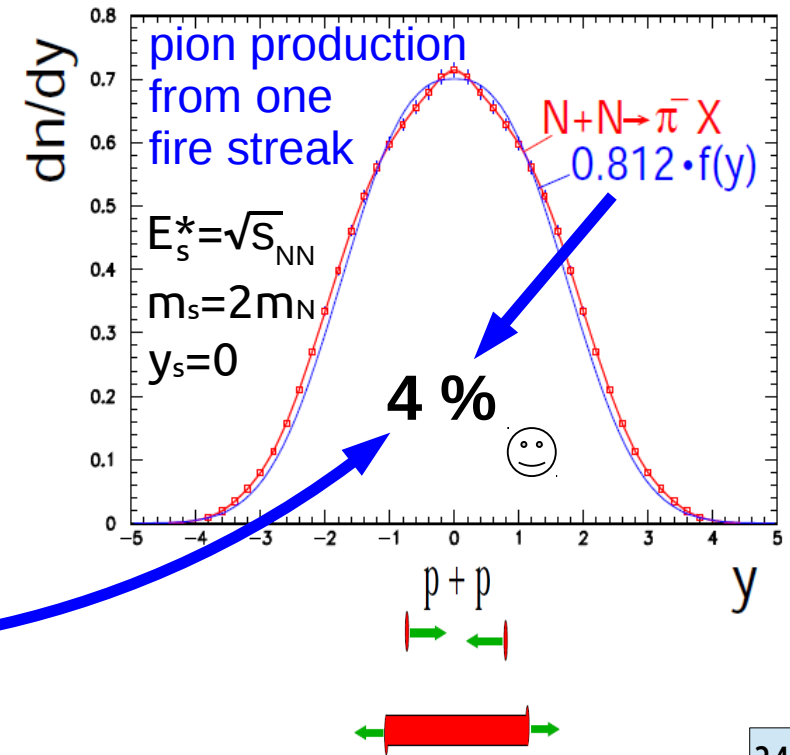
**p+p:** (pion energy) = **6862 MeV** ;  
 (kaon energy) = **918 MeV** ;  
 (baryon energy) → baryon inelasticity **K = 0.547**.

$$K = \frac{2 \cdot E_{inel}}{\sqrt{s} - 2m_p}$$

The relation between (baryon energy), (pion energy) and (kaon energy) in **Pb+Pb** collisions is calculated on the basis of:

- baryon inelasticity in Pb+Pb, **K ≈ 0.78** ; → C.Blume, **NA49**, J.Phys. G34 (2007) 951, and refs therein.
- the change in  $\langle K \rangle / \langle \pi \rangle$  ratios between p+p and Pb+Pb (**~2**).

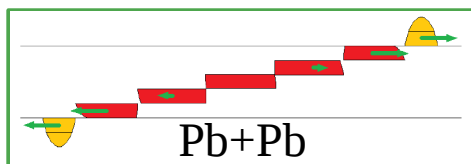
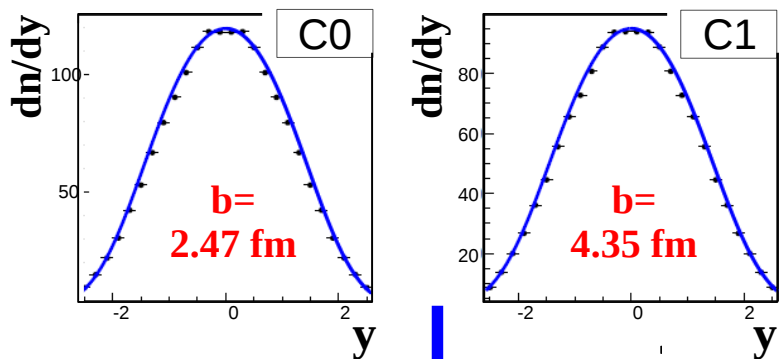
From:  
**NA49**, EPJC 65 (2010) 9, EPJC 68 (2010) 1, EPJC 45 (2006) 343,  
 PRC 86 (2012) 054903, and references therein.  
**NA49**, compilation of numerical results, <http://na49info.web.cern.ch/na49info/na49>.



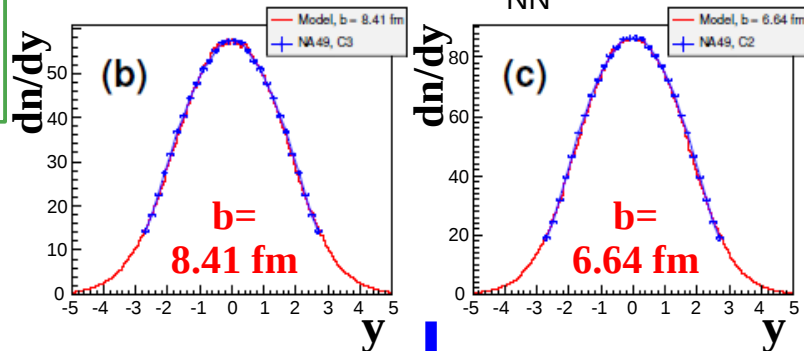
In this way we get (per unit of total collision energy):

$$\frac{\text{Energy spent on pions in p+p}}{\text{Energy spent on pions in Pb+Pb}} = 0.781$$

$\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 8.8$  GeV

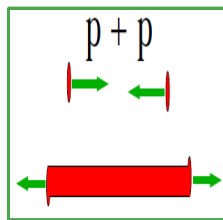
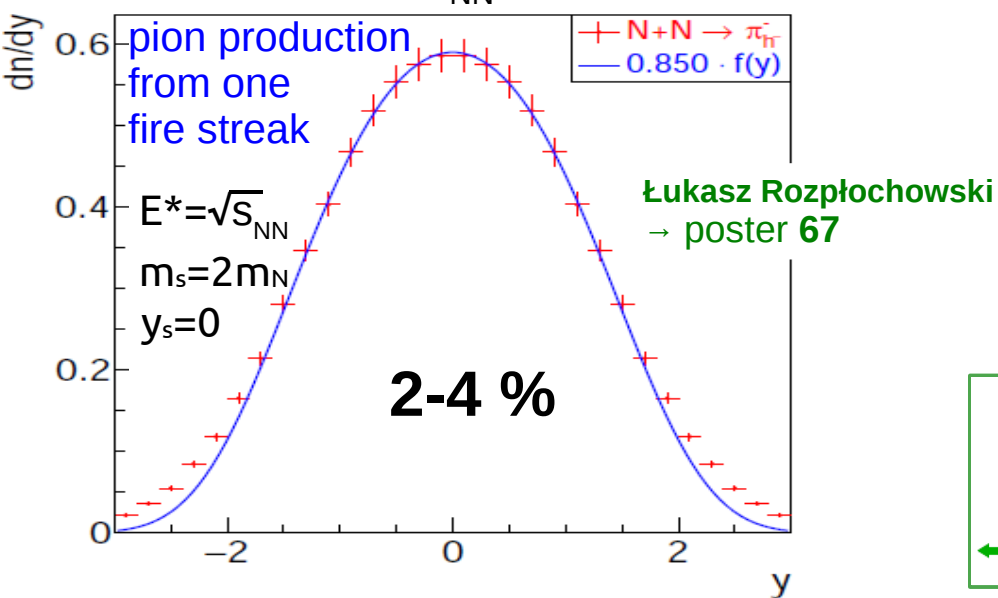


$\pi^-$ , Pb+Pb,  $\sqrt{s}_{NN} = 17.3$  GeV

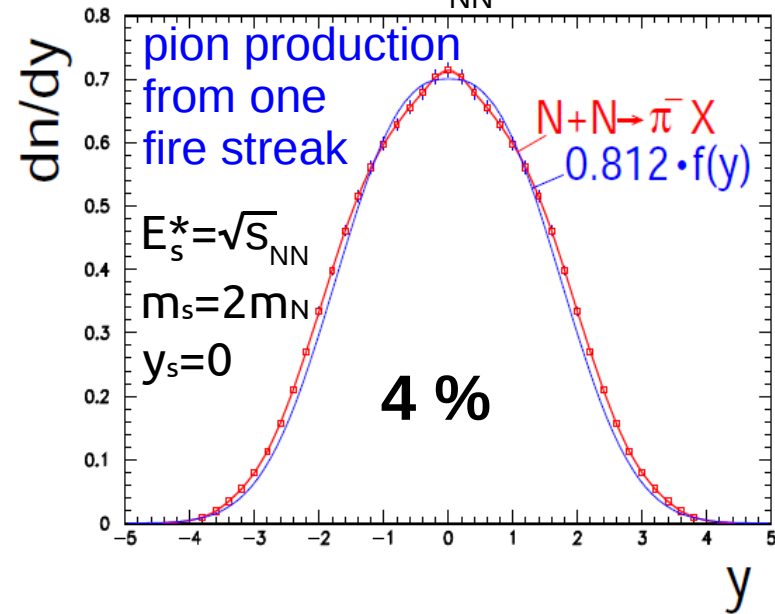


Valid for  
 $8.8 \text{ GeV} \leq \sqrt{s}_{NN} \leq 17.3 \text{ GeV}$   
 (or better)

$\pi^-$ , N+N,  $\sqrt{s}_{NN} = 8.8$  GeV



$\pi^-$ , N+N,  $\sqrt{s}_{NN} = 17.3$  GeV



# The energy dependence of the fire streak fragmentation function (PRC 99 (2019) 024908, Appendix B)

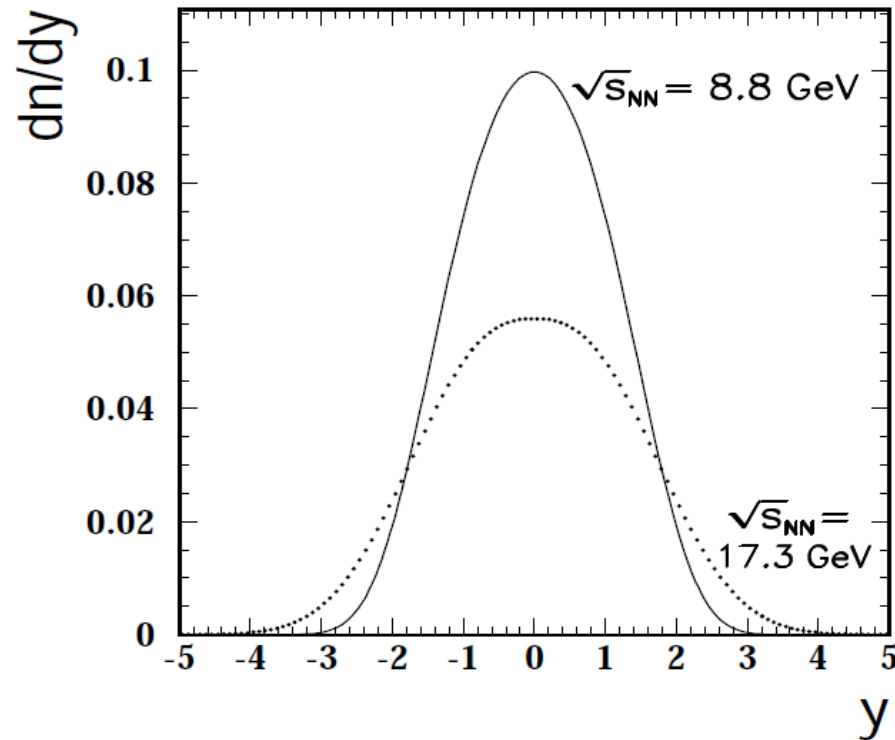
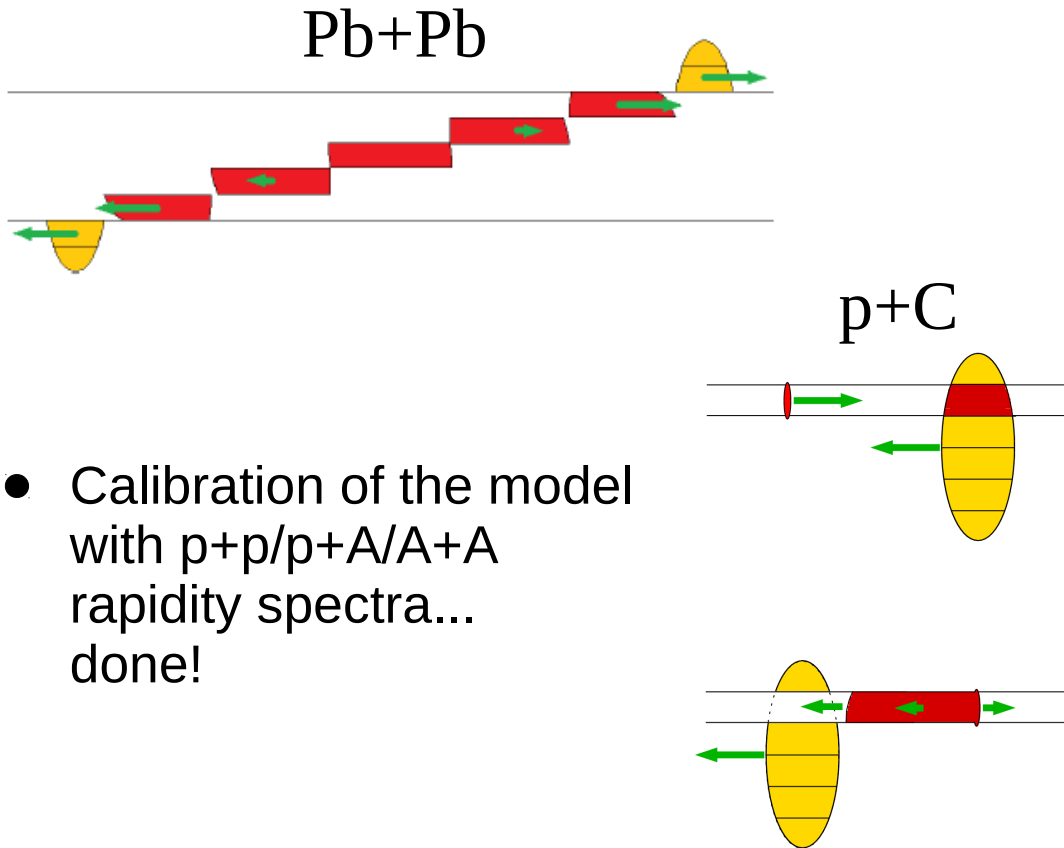
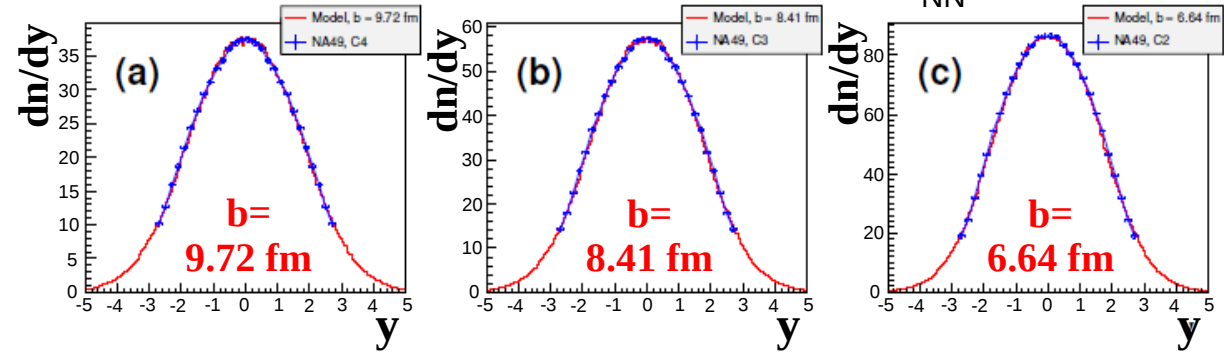


FIG. 7:

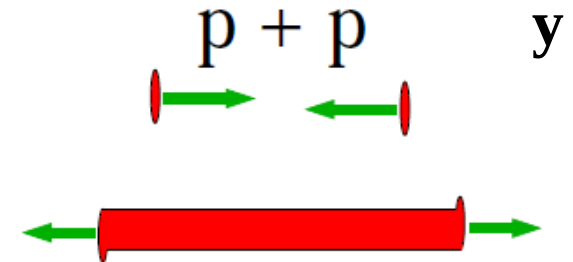
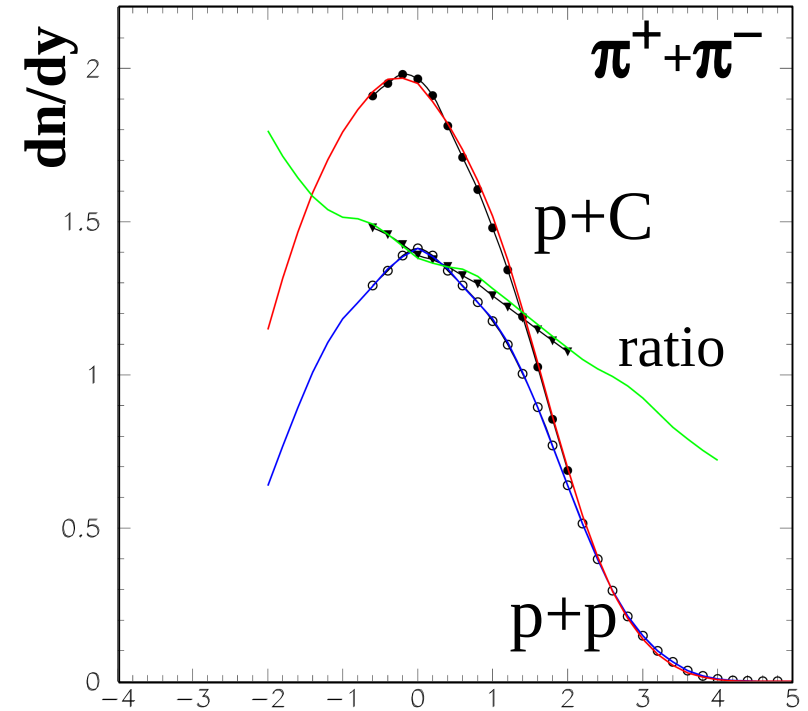
Comparison of single fire-streak fragmentation functions used for the description of  $\pi^-$  rapidity distributions in Pb+Pb collisions at  $\sqrt{s_{NN}} = 8.8$  GeV (solid) and at  $\sqrt{s_{NN}} = 17.3$  GeV (dotted).

The two presented functions are given by Eq. (2.1) with  $(E_s^* - m_s) \equiv 1$  GeV. The numerical values of the function parameters are given in the text.

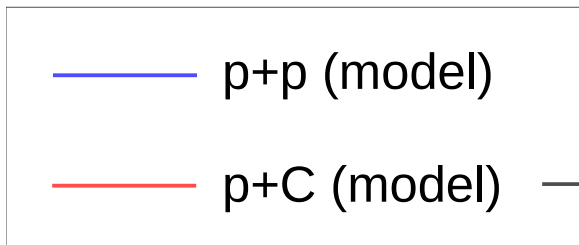
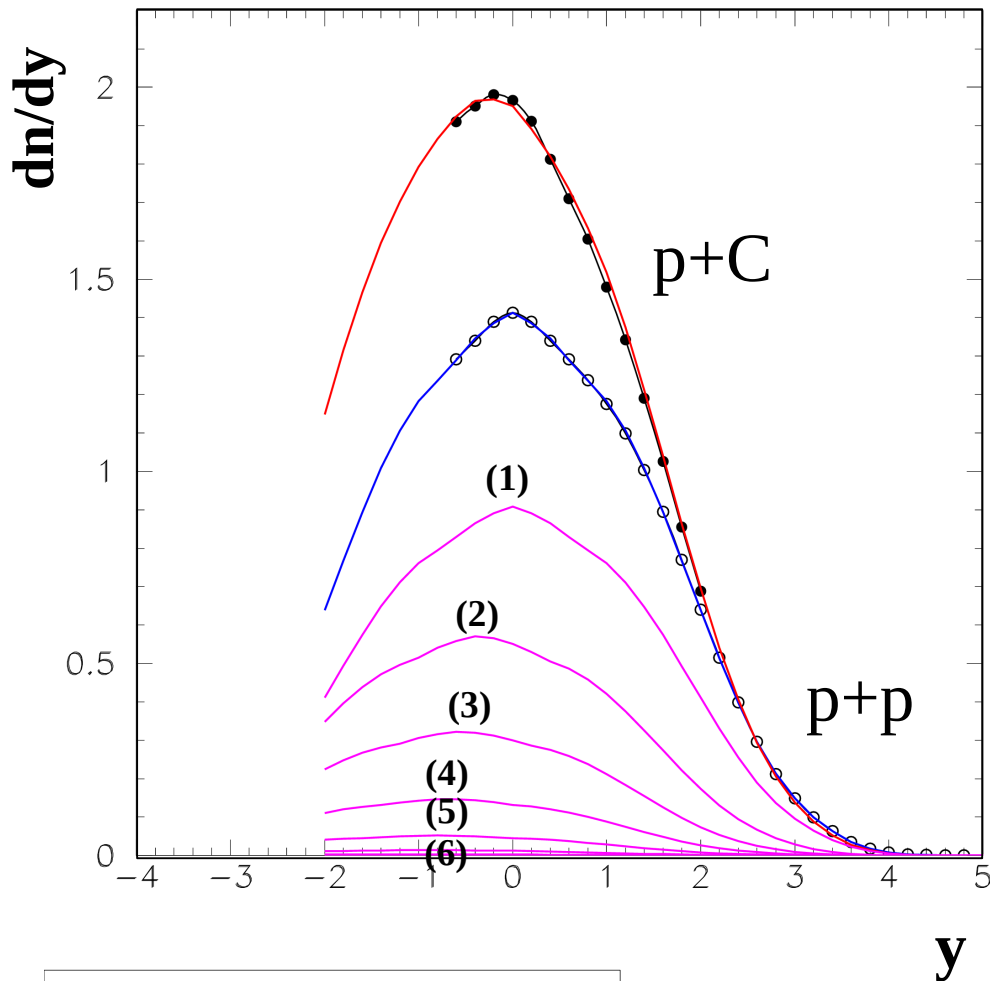
- Link between p+p, p+A, and A+A collisions.



- Calibration of the model with p+p/p+A/A+A rapidity spectra... done!



$\pi^+ + \pi^-$ ,  $\sqrt{s_{NN}} = 17.3$  GeV



Energy balance:  
change in energy spent on pions by **+13 %** w.r.t. p+p, can be explained by baryon stopping.

