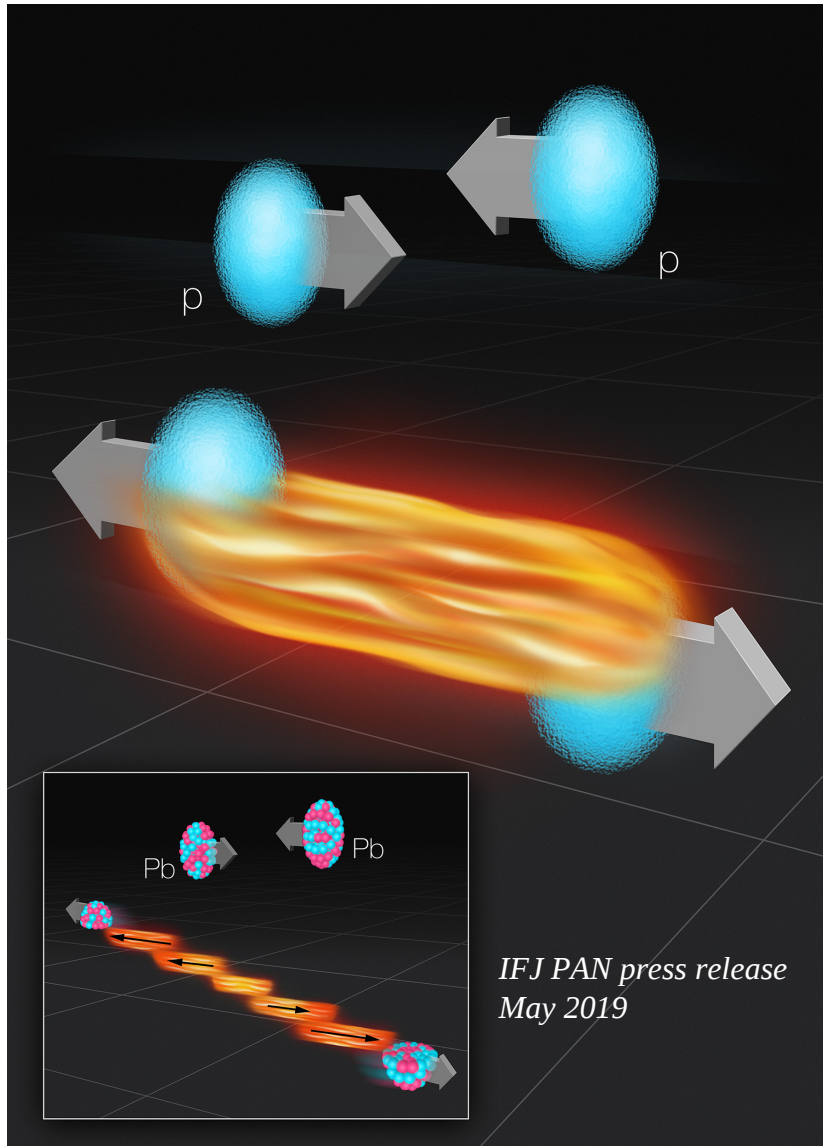


Comments on the space-time evolution of the system created in the nucleus-nucleus collision at high energy



Andrzej Rybicki

H. Niewodniczański Institute of Nuclear Physics
Polish Academy of Sciences

Work done with

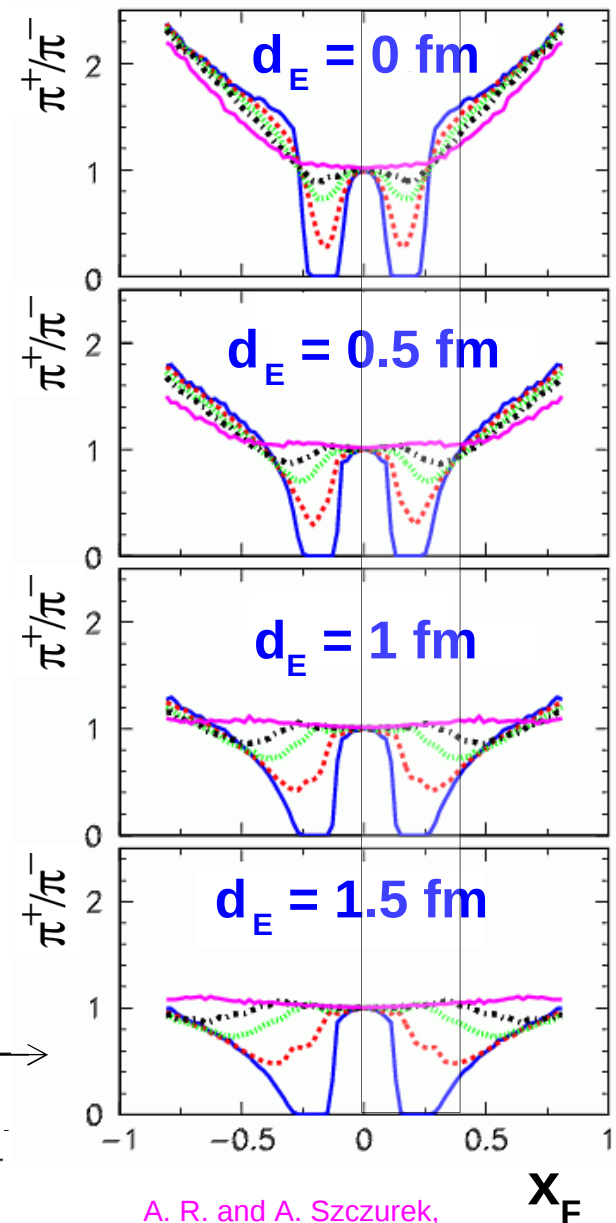
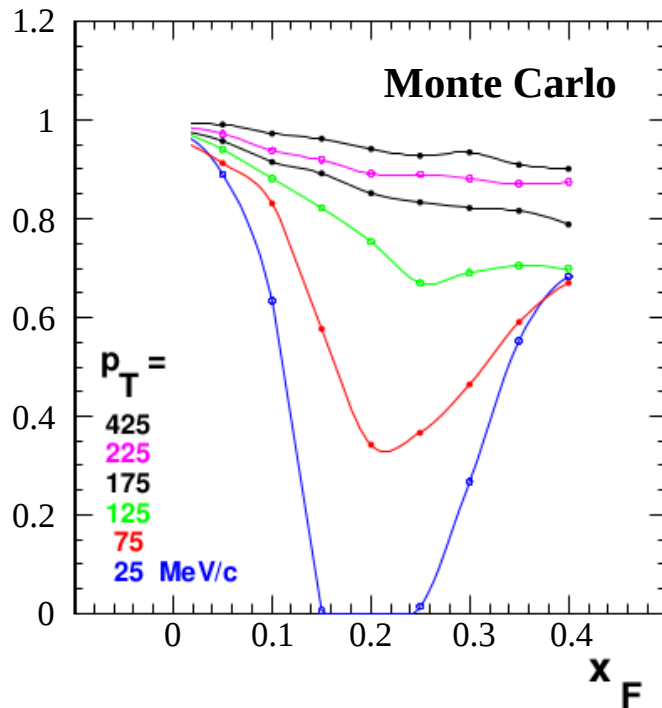
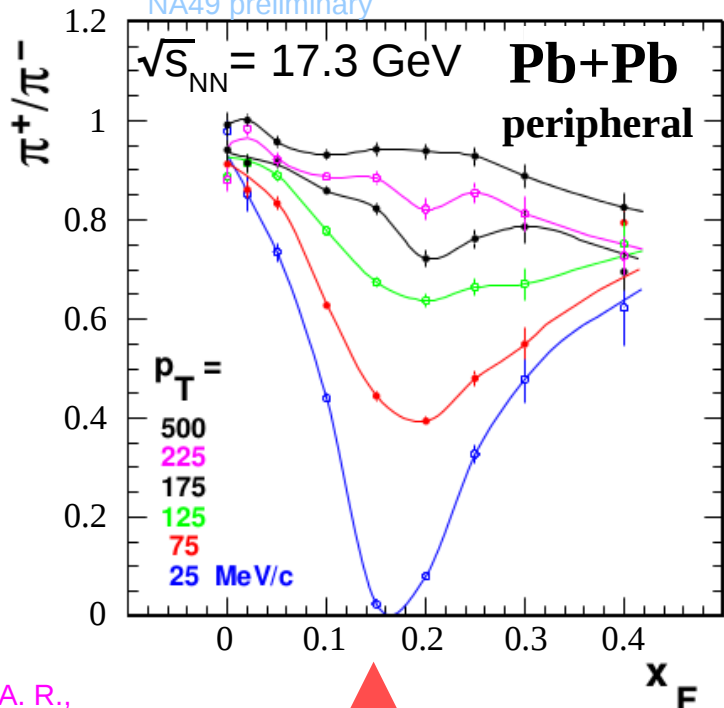
*A. Szczurek, V. Ozvenchuk, A. Marcinek, M. Kiełbowicz,
Ł. Rozpłochowski, N. Davis, S. Bhosale, M. Kłusek-
Gawenda*

See also:

1) PRC 99 (2019) 024908,
2) arXiv: 1910.04544

1. The idea;
2. Getting information from EM effects ;
3. Space-time evolution of forward pion production ;
4. Summary.

1) The idea

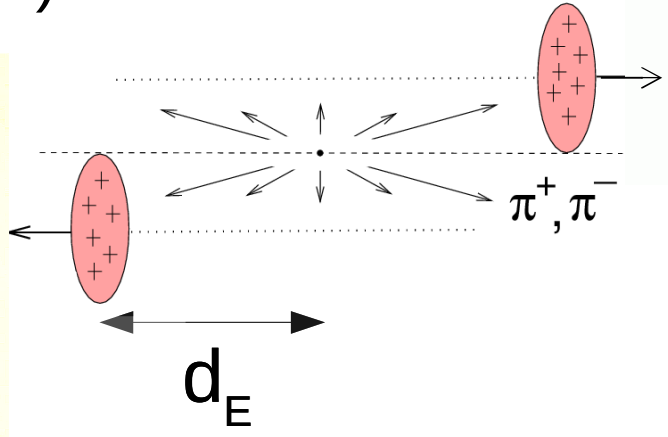
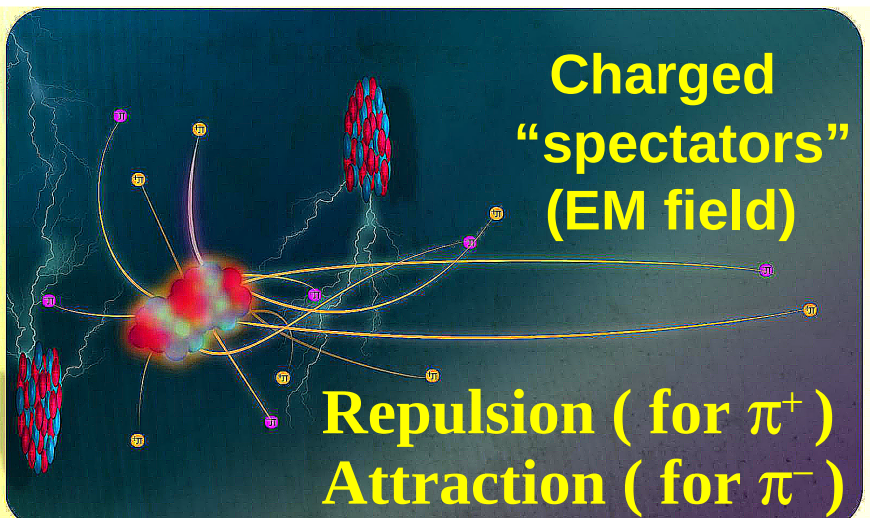


A. R.,
Acta Phys. Polon.
B42 (2011) 867

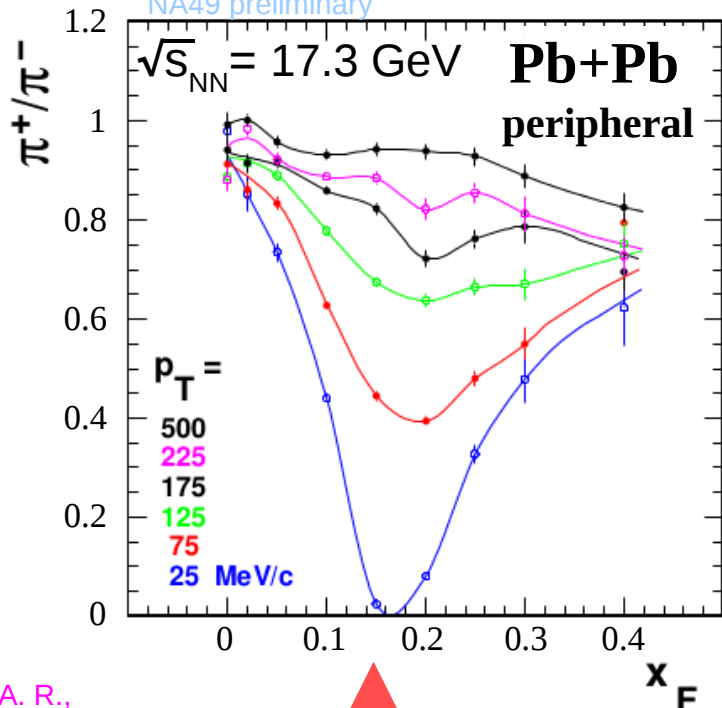
**spectator
velocity**
 $y = y_{beam}$

$$x_F = \frac{p_L}{p_L^{beam}}$$

(c.m.s.)



A. R. and A. Szczurek,
Phys. Rev. C75 (2007)
054903

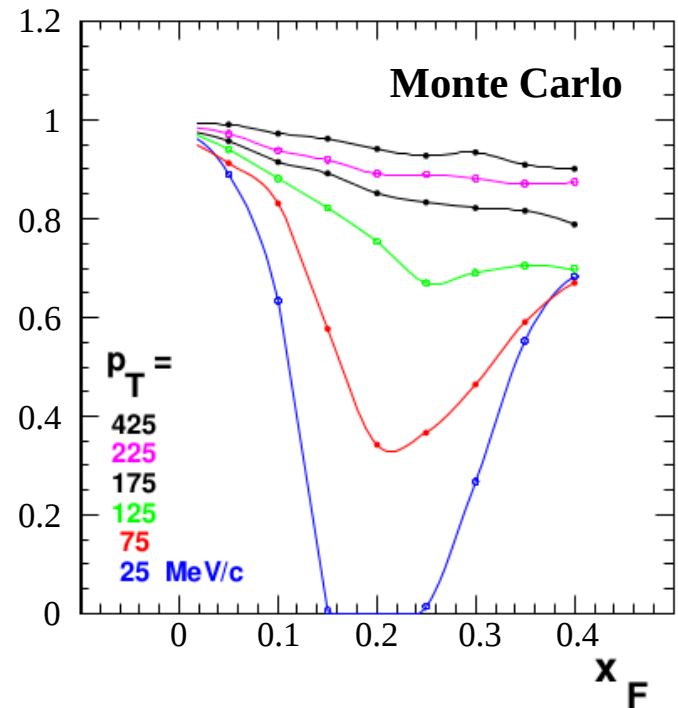


A. R.,
Acta Phys. Polon.
B42 (2011) 867

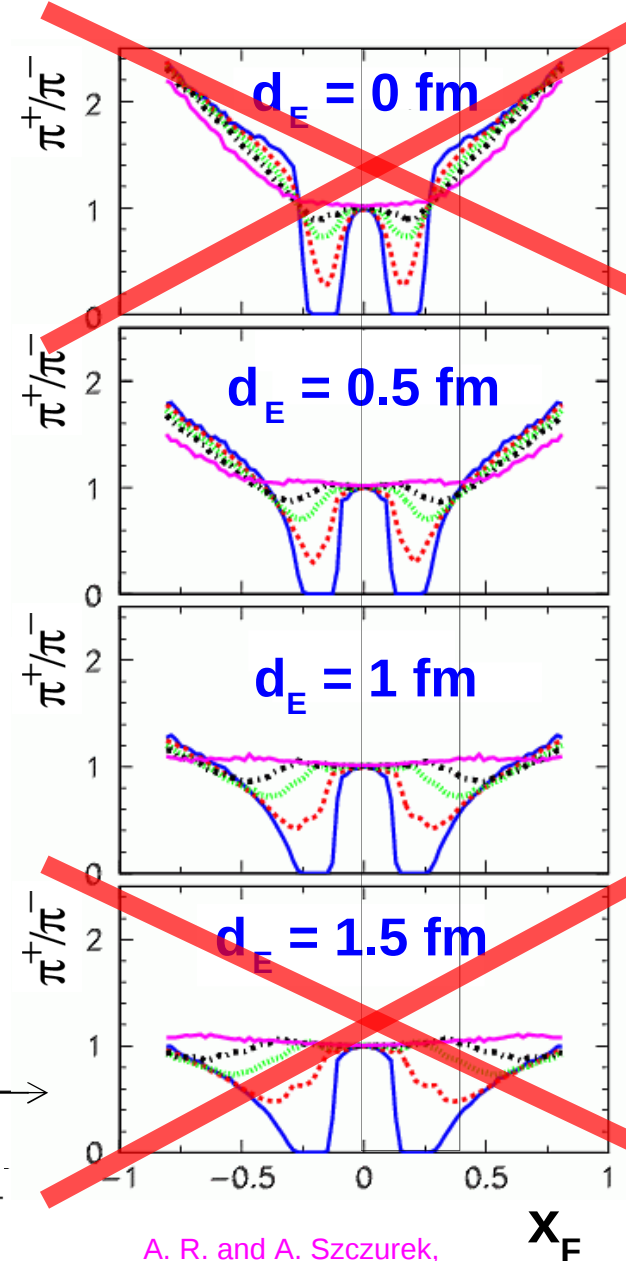
**spectator
velocity
 $y = y_{beam}$**

$$x_F = \frac{p_L}{p_L^{beam}}$$

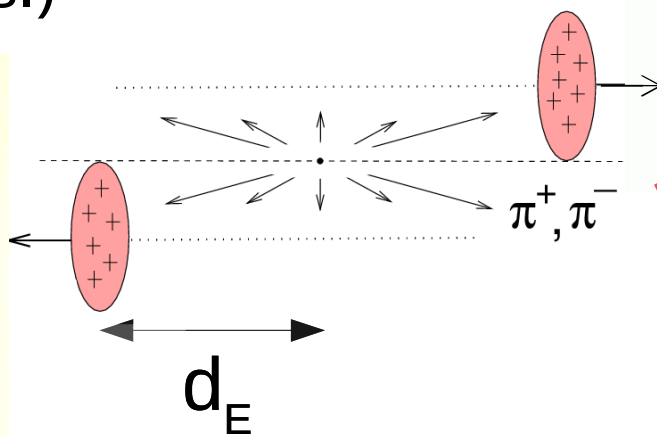
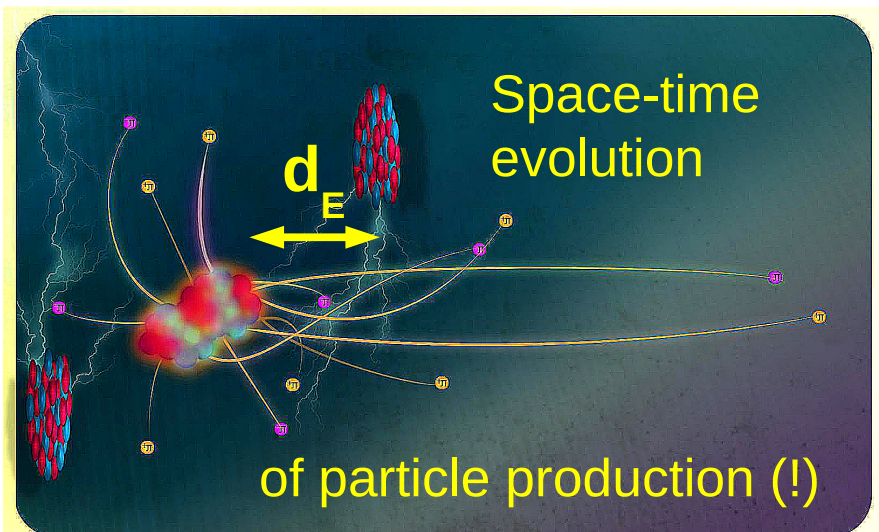
(c.m.s.)

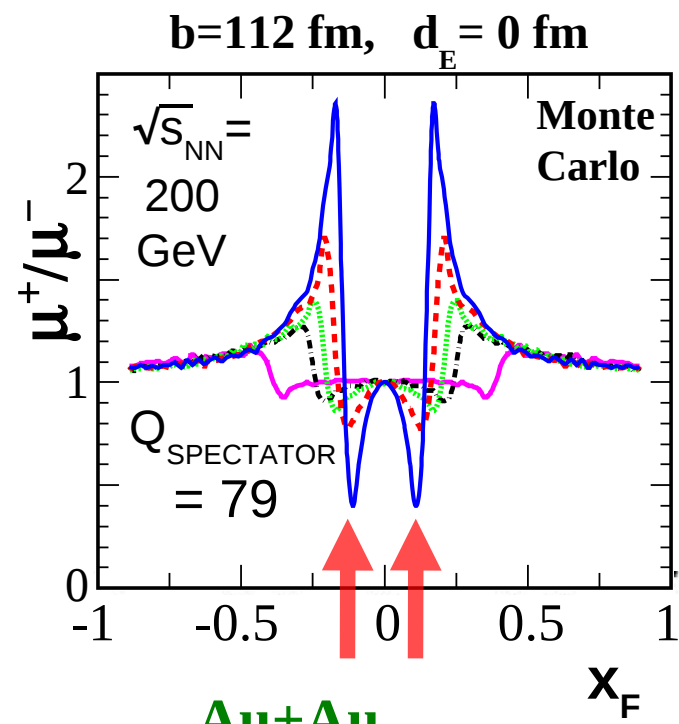
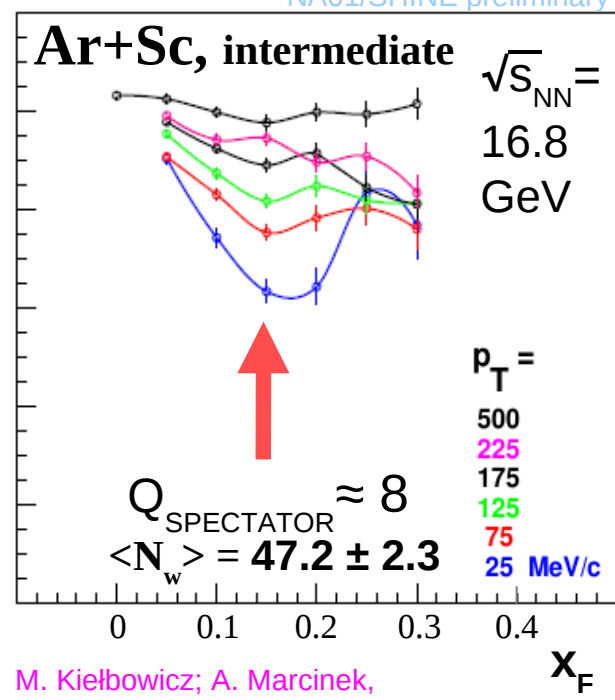
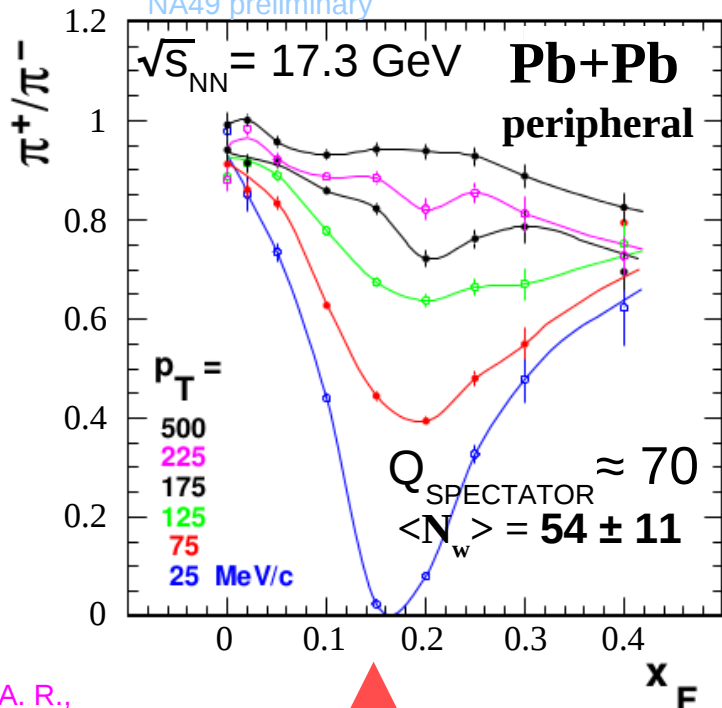


$d_E \approx 0.75 \text{ fm}$



A. R. and A. Szczurek,
Phys. Rev. C75 (2007)
054903





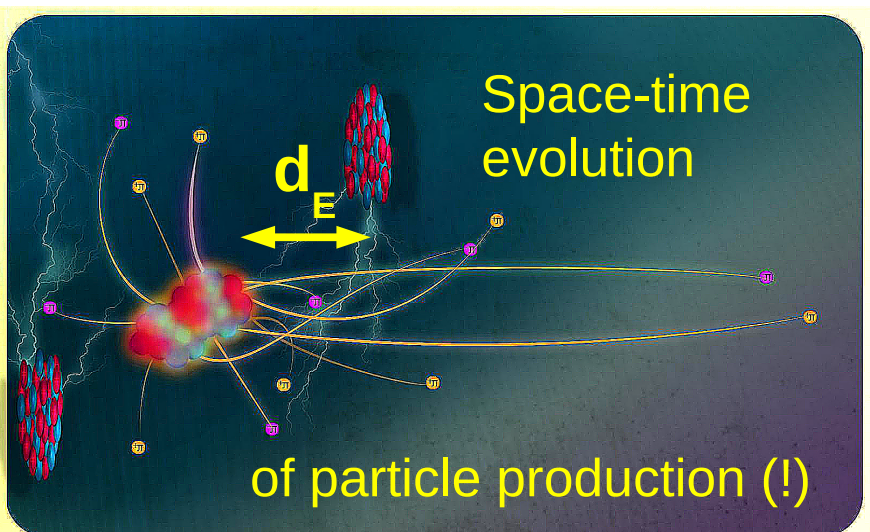
A. R.,
Acta Phys. Polon.
B42 (2011) 867

M. Kielbowicz; A. Marcinek,
Acta Phys. Polon. B50 (2019) 1127

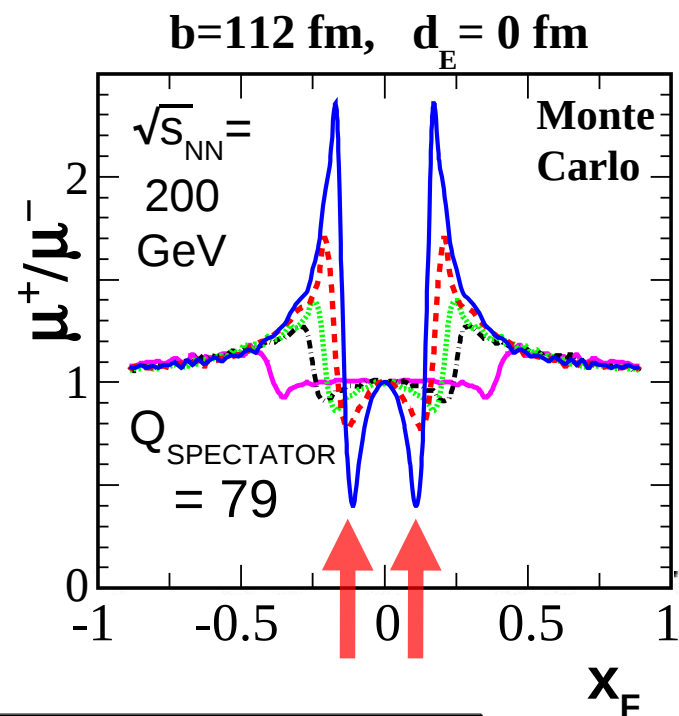
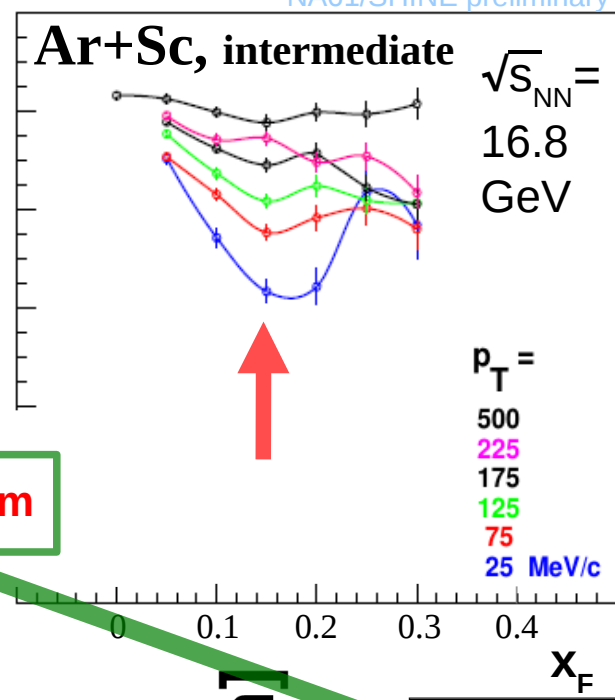
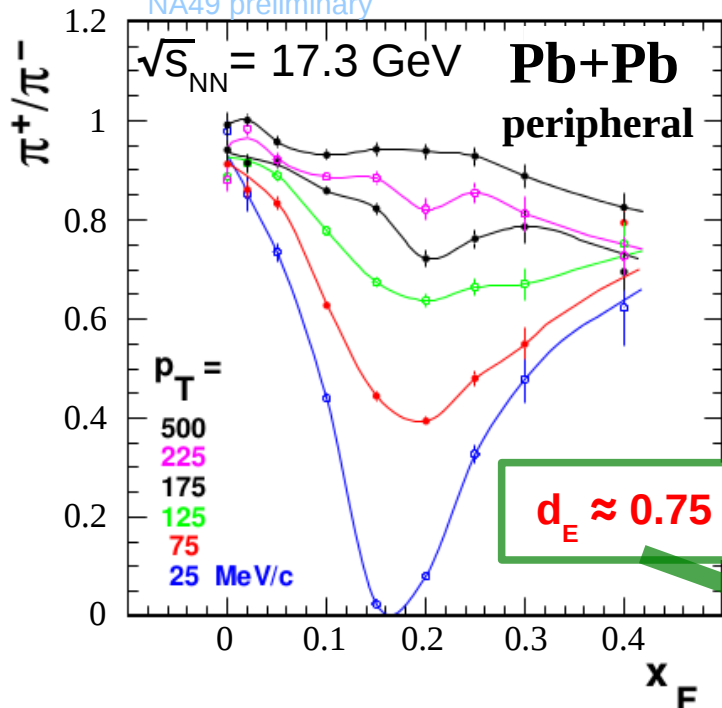
**spectator
velocity**
 $y = y_{beam}$

$$x_F = \frac{p_L}{p_L^{beam}} \quad (\text{c.m.s.})$$

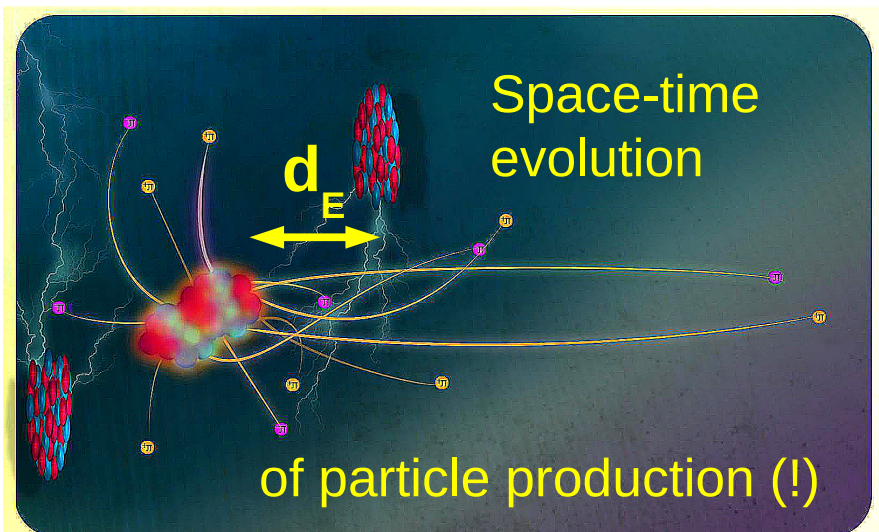
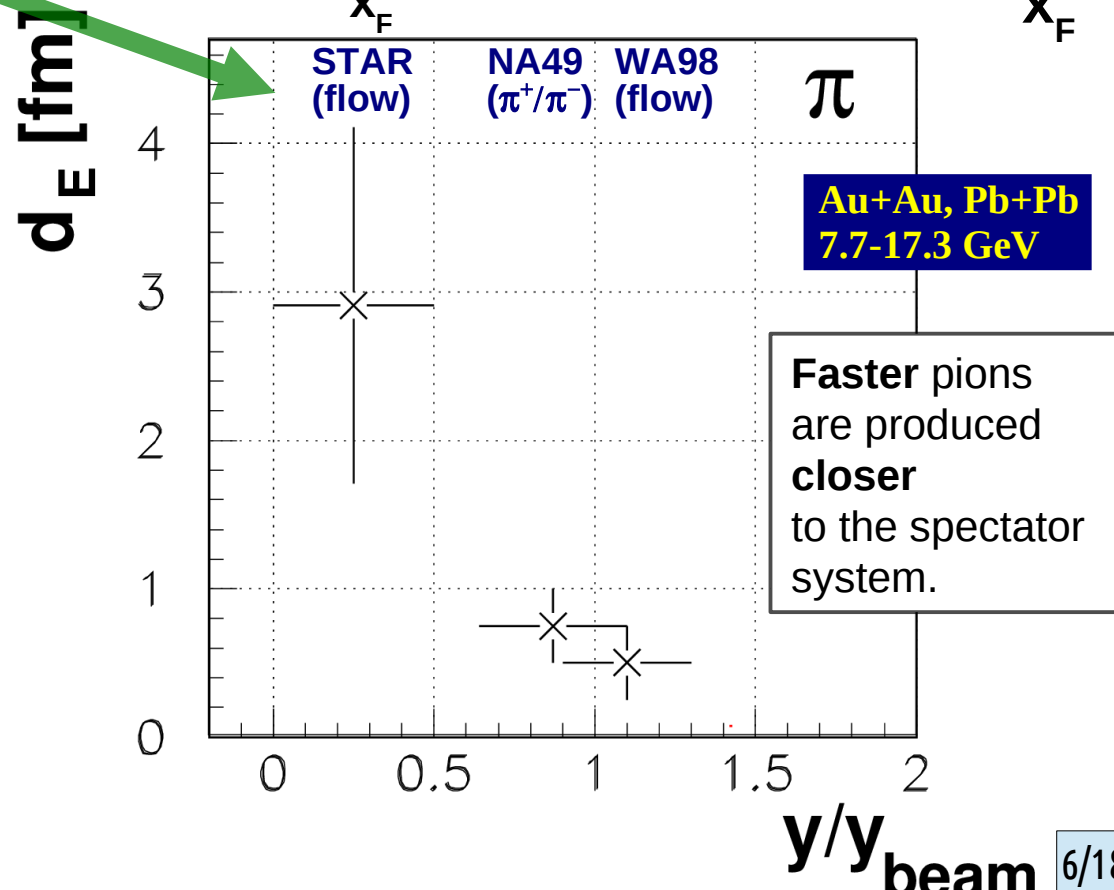
**Au+Au,
ultra-peripheral,
($\gamma\gamma \rightarrow \mu^+\mu^-$)**

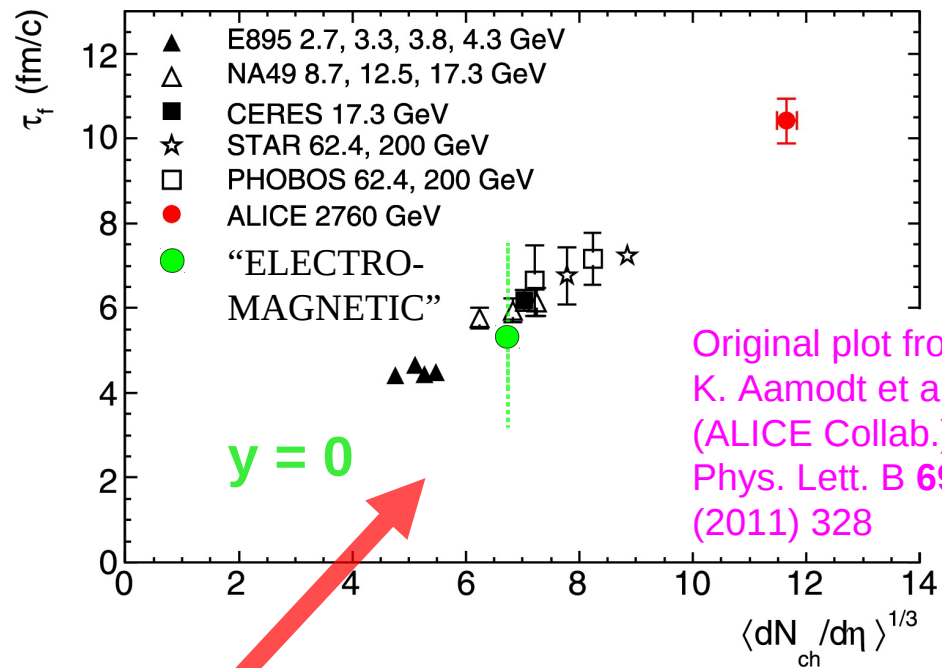
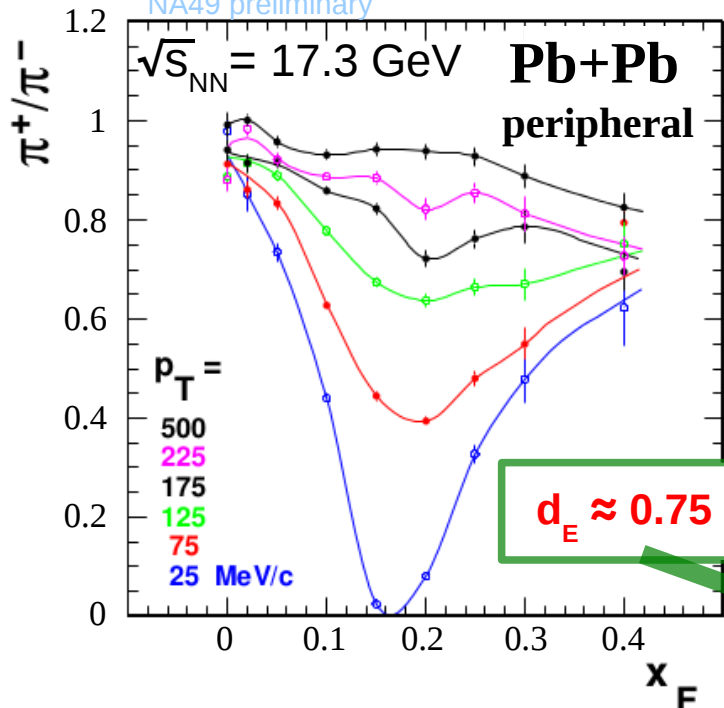


2) Getting information from EM effects



Note: the remaining points in the right plot are deduced from EM effects on azimuthal anisotropies (flow).
Data: L. Adamczyk et al., STAR, PRL 112, 2014, 725,
H. Schlagheck et al., WA98, NPA 663, 2000, 725.
See also: A. R. et al., APPB 46 (2015) 3, 737.

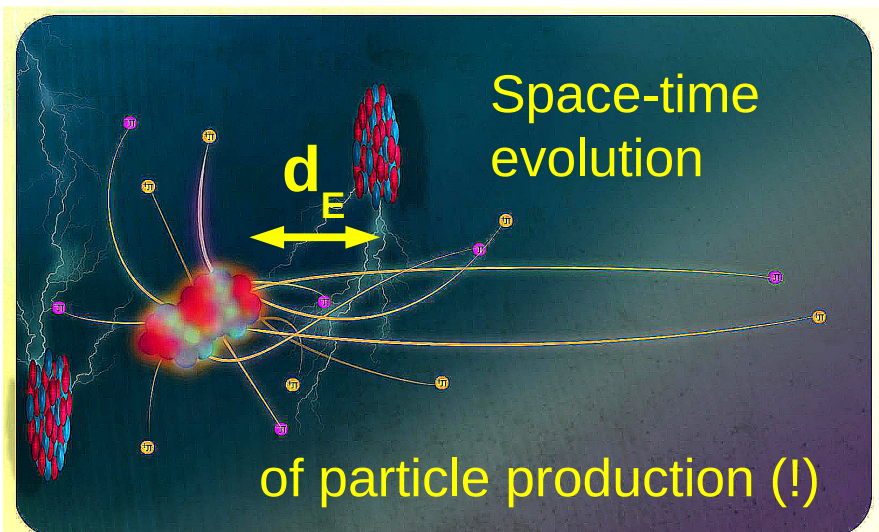
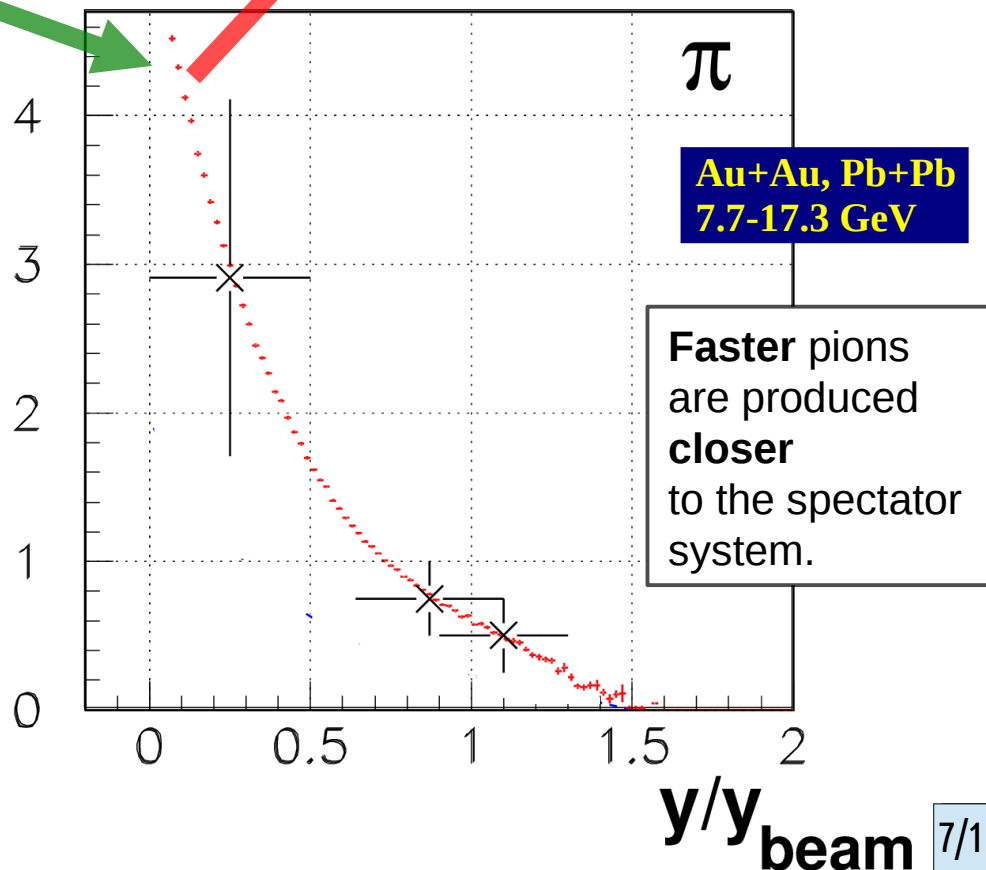




Original plot from:
K. Aamodt et al.
(ALICE Collab.),
Phys. Lett. B **696**
(2011) 328

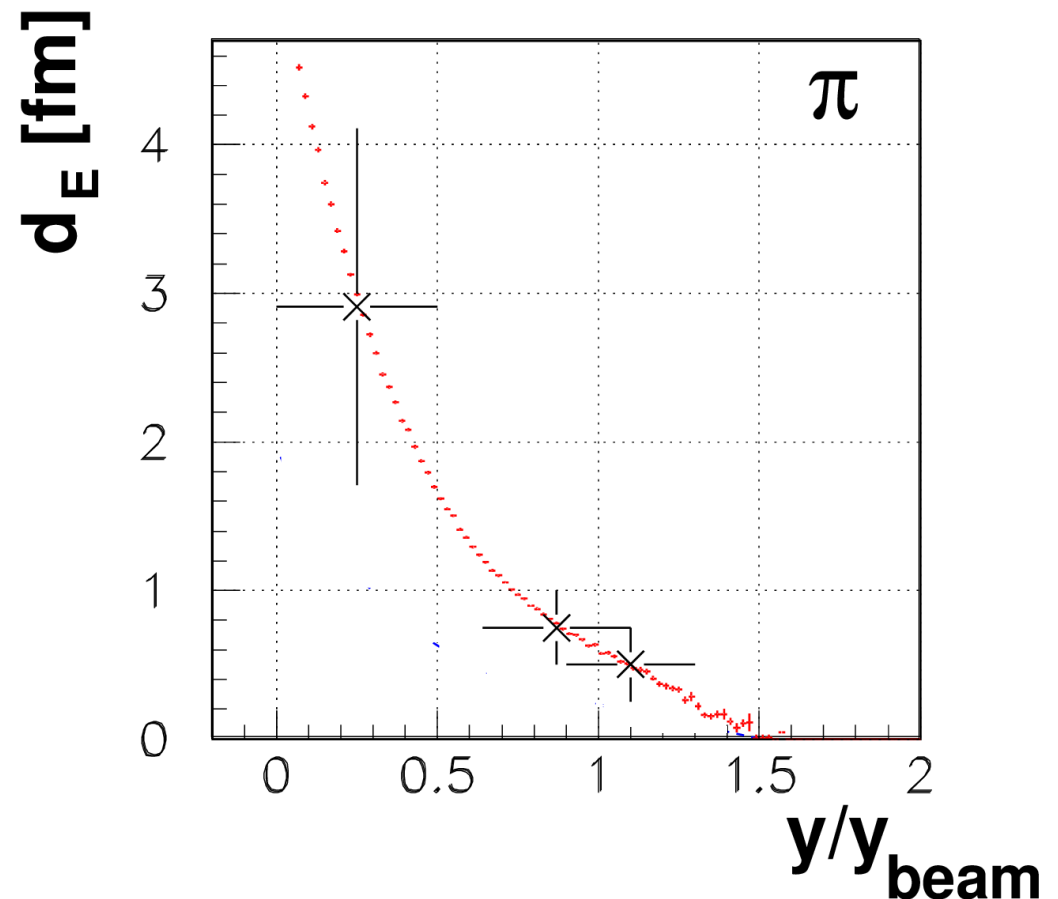
- EM effects give **their own estimate** for the time of pion creation, at $y=0$.

$d_E \text{ [fm]}$

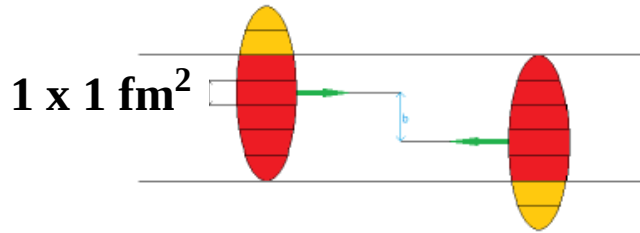


3)

Space-time evolution of forward pion production

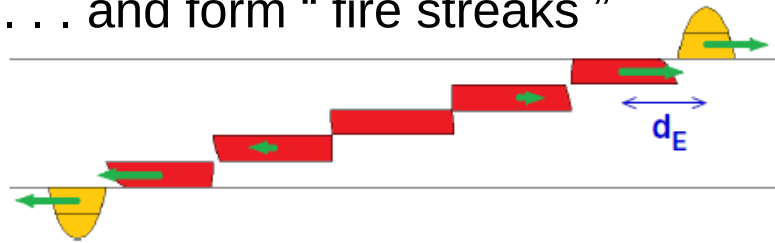


Bricks collide ...



PRC 95 (2017) 024908
 Idea by A. Szczurek,
 See also:
 R. Hagedorn, CERN-71-12
 W.D. Myers, NPA 296, 1978, 177

... and form "fire streaks"



Each fire streak fragments independently into pions

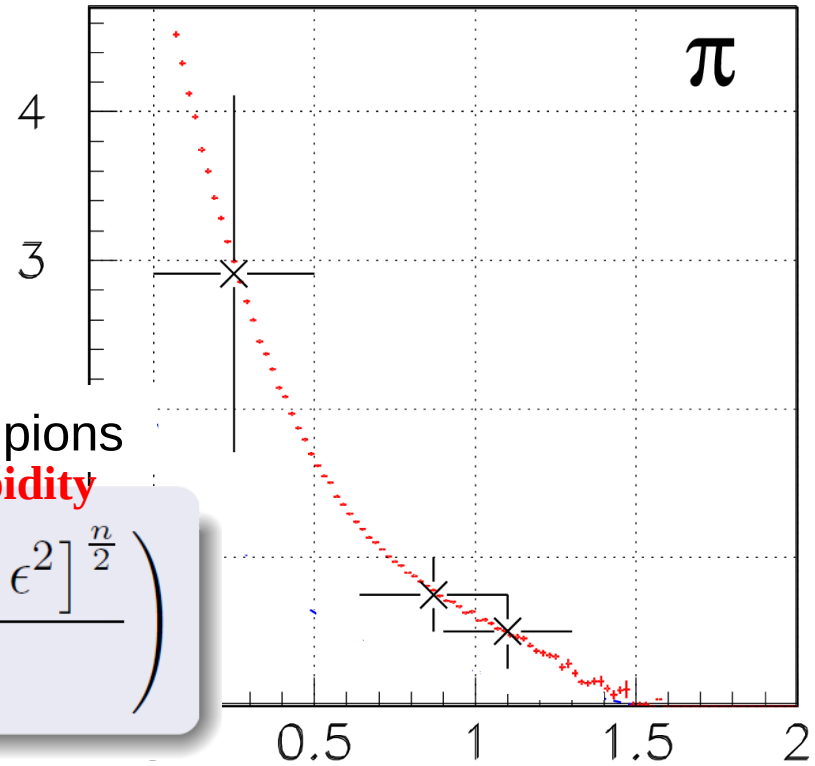
available energy **fire streak rapidity**

$$\frac{dn}{dy} = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

total fire streak energy

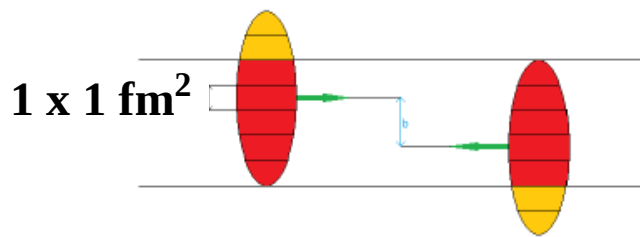
sum of brick masses

d_E [fm]



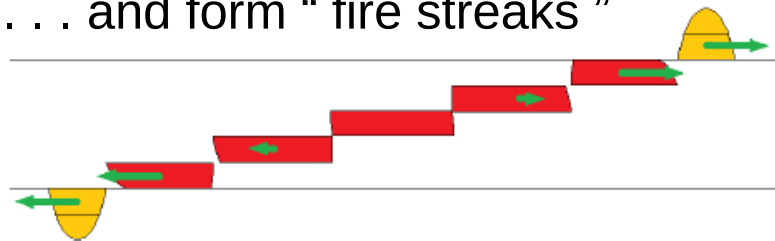
y/y_{beam}

Bricks collide ...



PRC 95 (2017) 024908
 Idea by A. Szczurek,
 See also:
 R. Hagedorn, CERN-71-12
 W.D. Myers, NPA 296, 1978, 177

... and form "fire streaks"

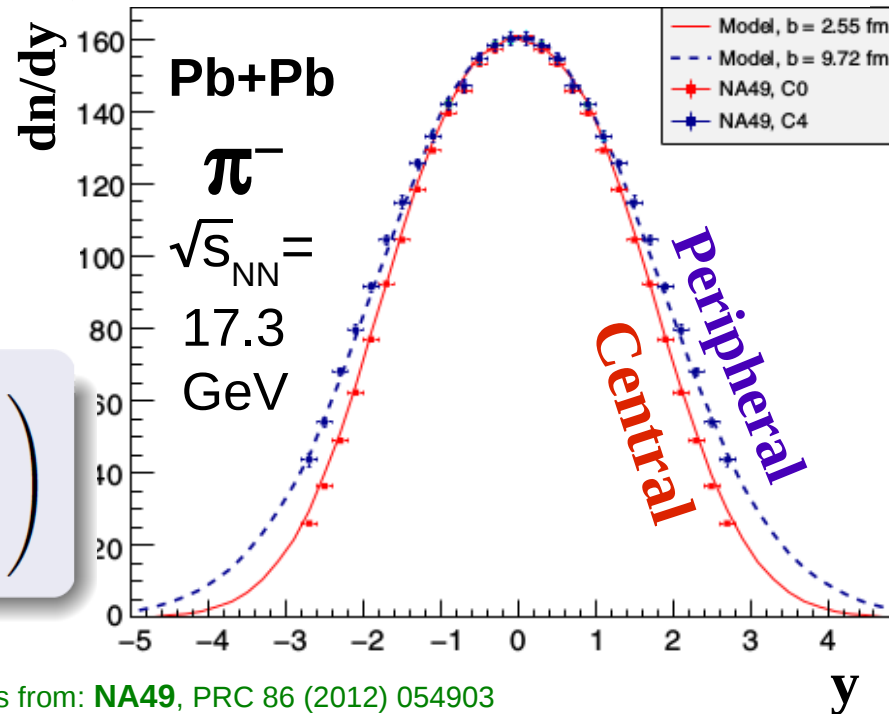
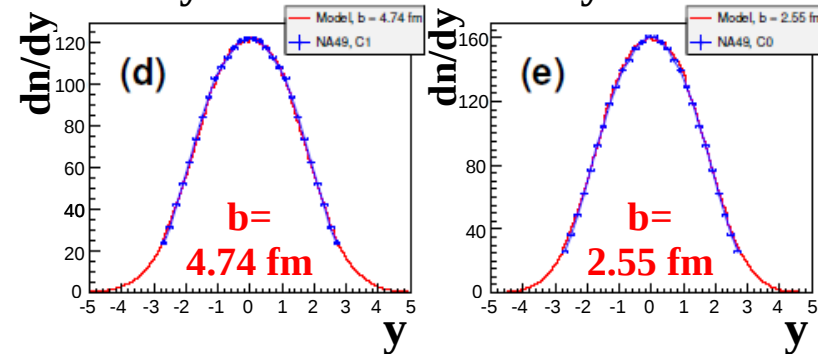
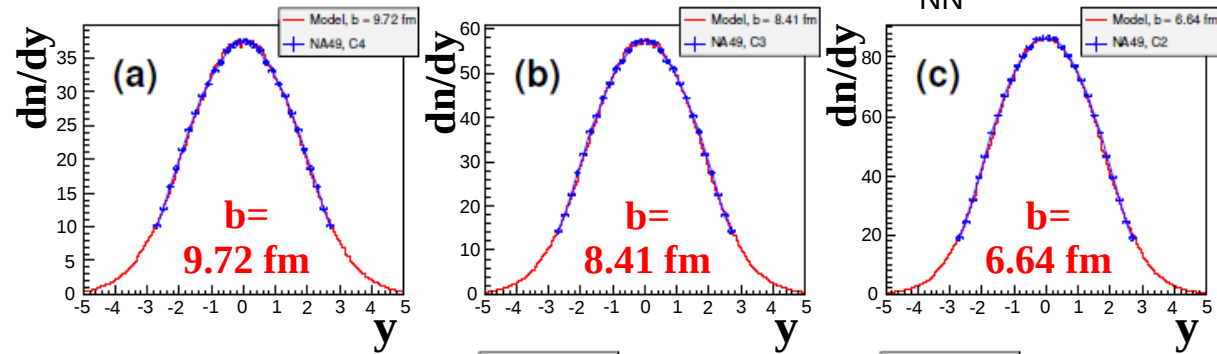


Each fire streak fragments independently into pions

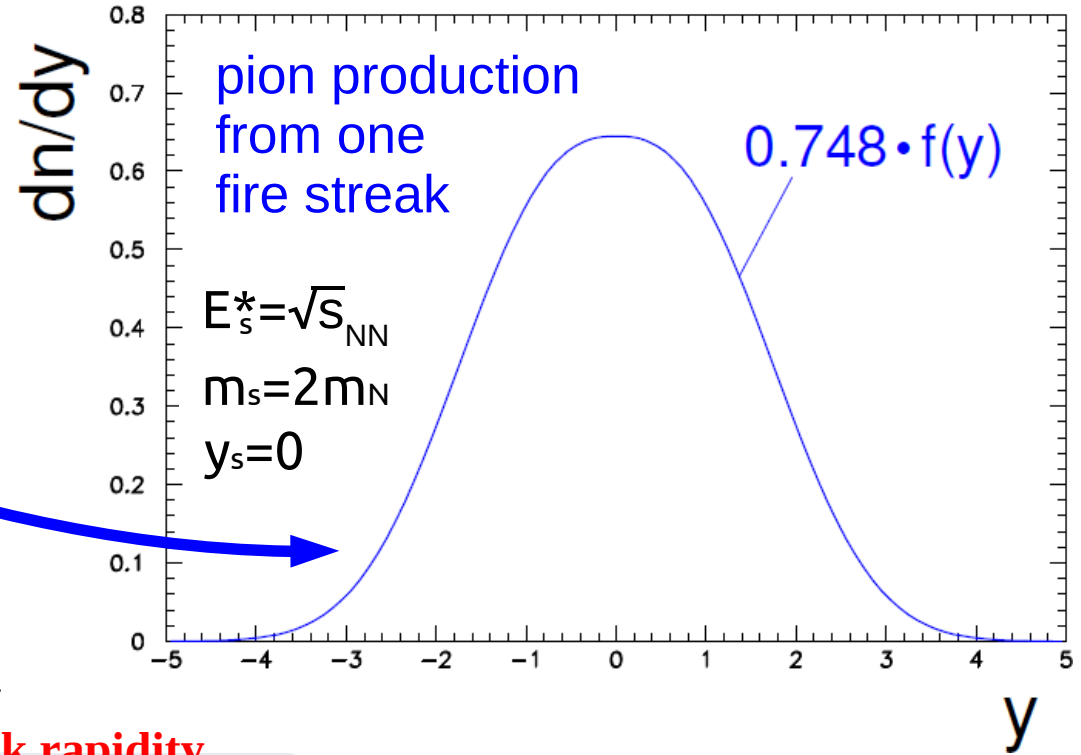
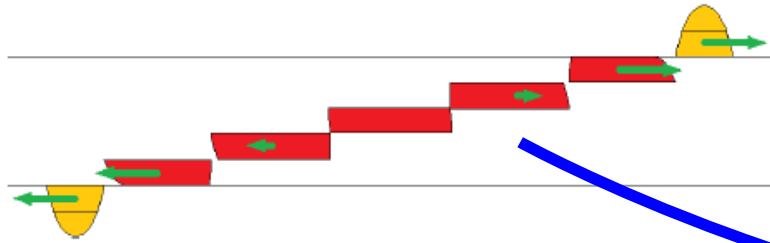
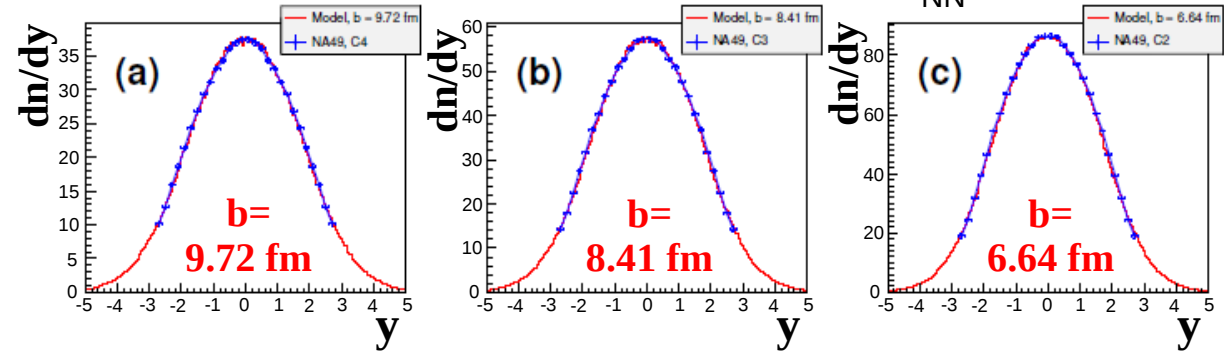
$$\frac{dn}{dy} = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

total fire streak energy
 sum of brick masses

NA49, π^- , Pb+Pb, $\sqrt{s}_{NN} = 17.3$ GeV



data points from: NA49, PRC 86 (2012) 054903



Each fire streak fragments independently

$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

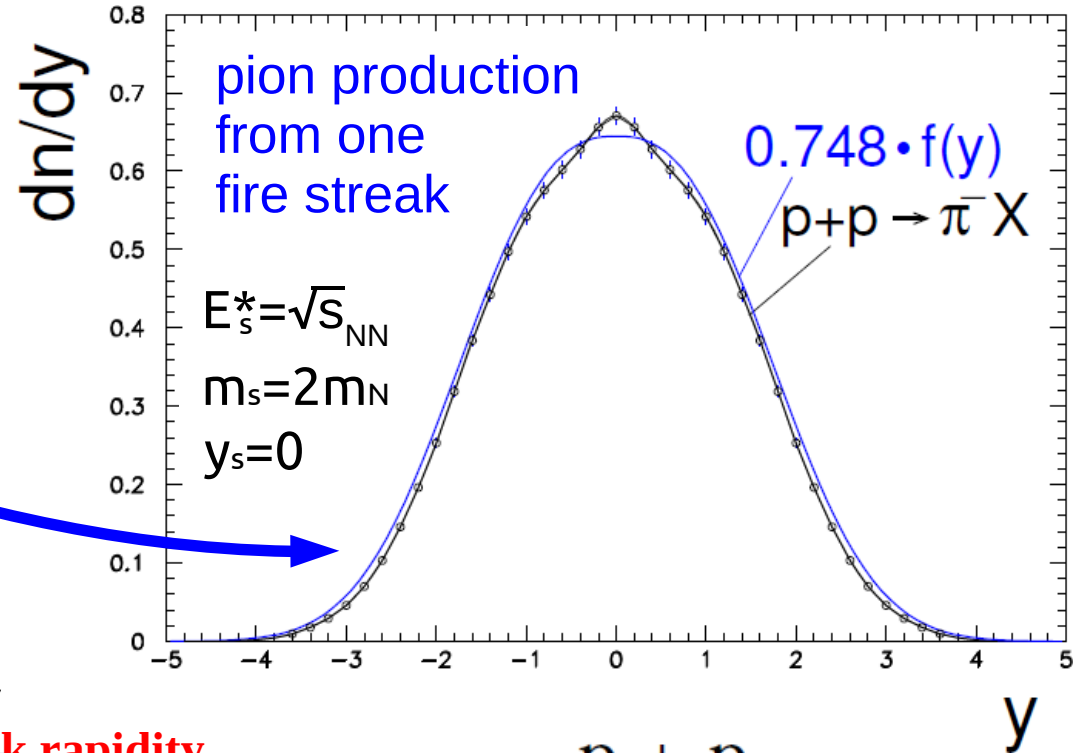
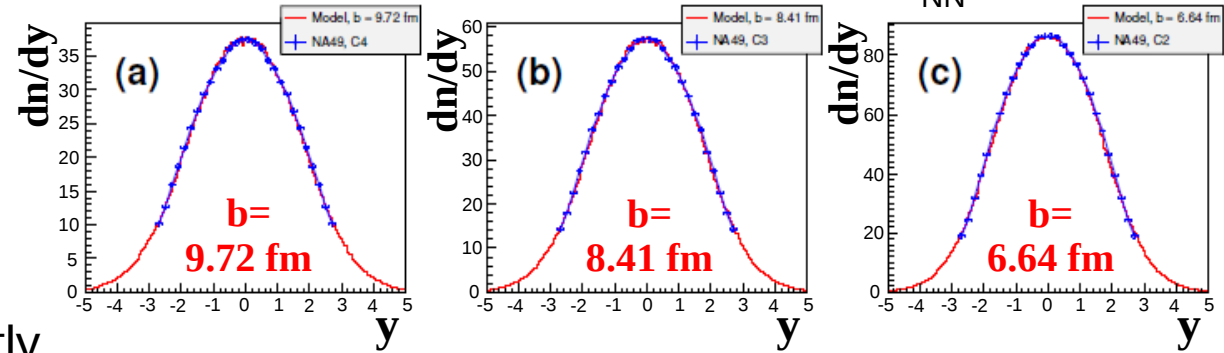
fire streak rapidity

total fire streak energy

sum of brick masses

- The pion rapidity distribution from **one fire streak** in Pb+Pb collisions is **similar** to the pion rapidity distribution in **p+p** reactions ;
- The difference in absolute normalization (**0.748**) can be directly obtained from the different energy repartition in **p+p** and **Pb+Pb** reactions (see PRC 99 (2019) 024908).

NA49, π^- , Pb+Pb, $\sqrt{s}_{NN} = 17.3$ GeV

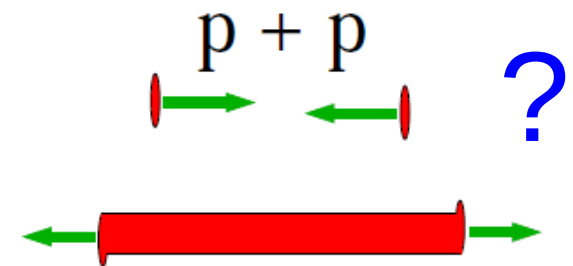


Each fire streak fragments independently

$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

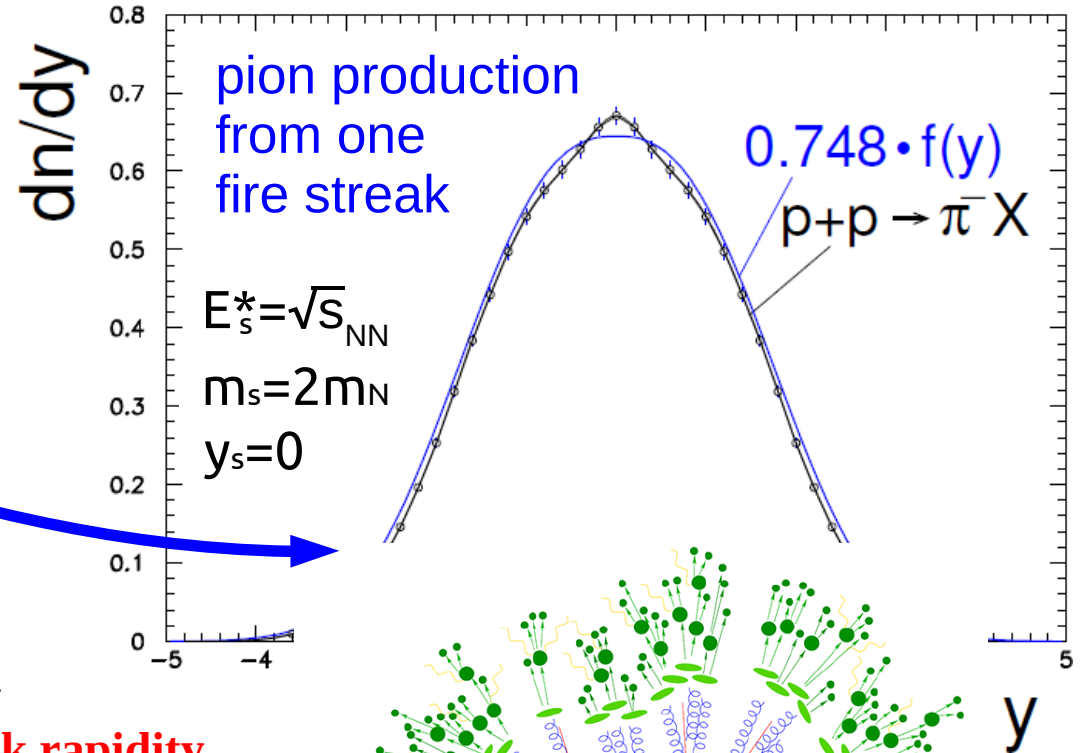
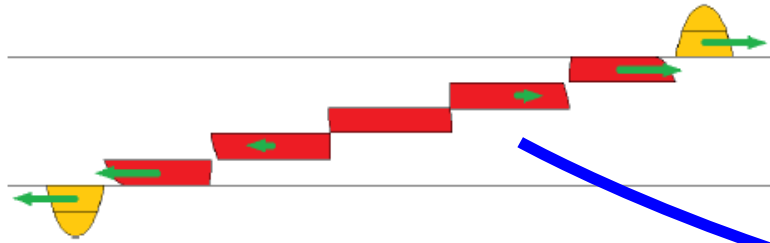
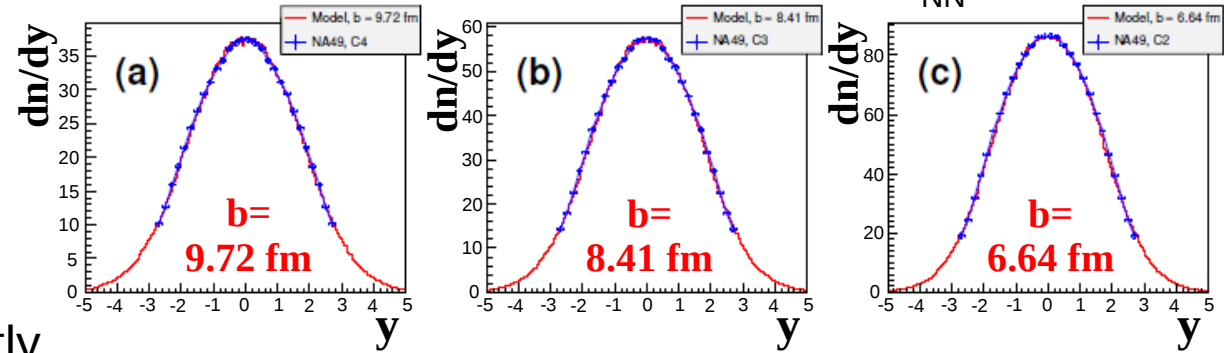
total fire streak energy

sum of brick masses



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- The difference in absolute normalization (**0.748**) can be directly obtained from the different energy repartition in **p+p** and **Pb+Pb** reactions (see PRC 99 (2019) 024908).

NA49, π^- , Pb+Pb, $\sqrt{s}_{NN} = 17.3$ GeV



Each fire streak fragments independently

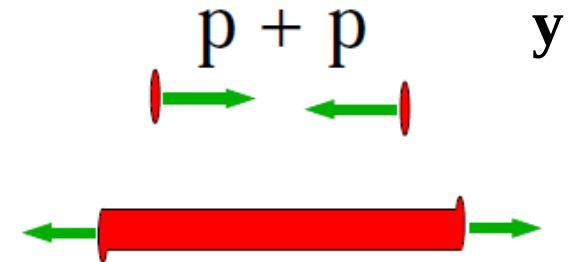
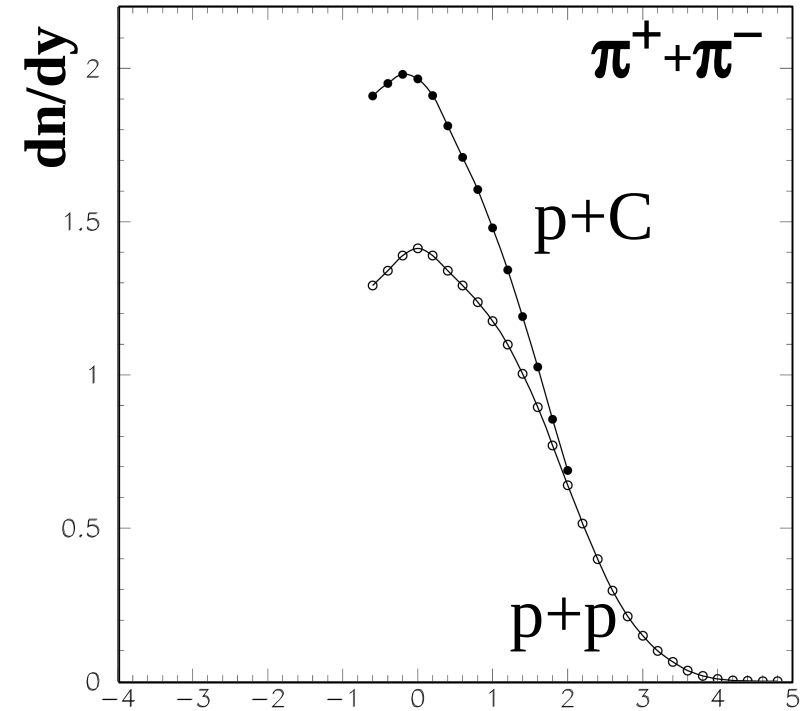
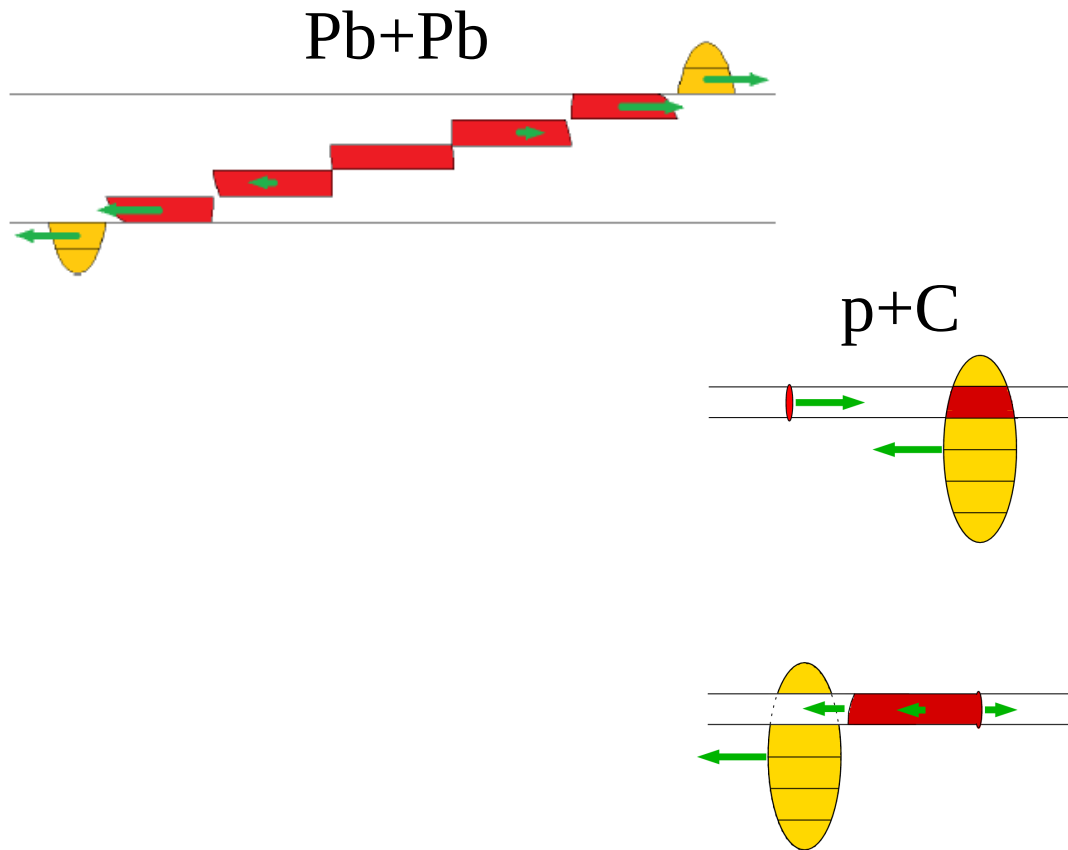
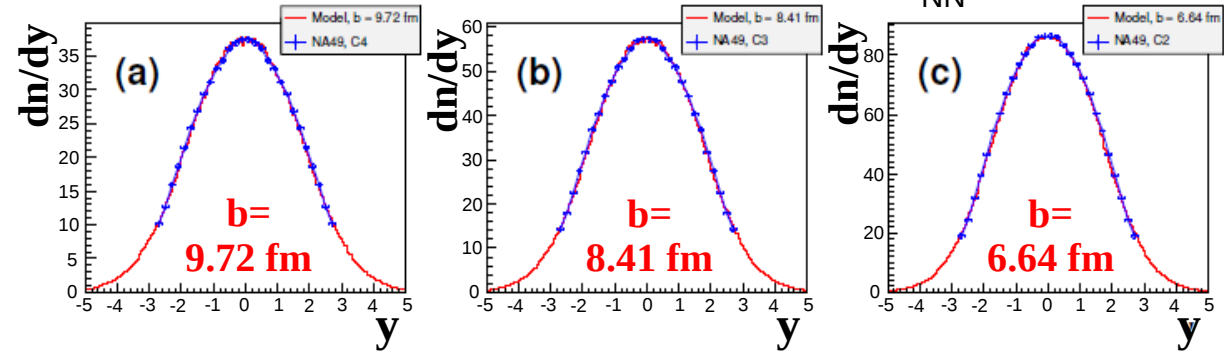
$$f(y) = A \cdot (E_s^* - m_s) \cdot \exp\left(-\frac{[(y - y_s)^2 + \epsilon^2]^{\frac{n}{2}}}{n\sigma_y^n}\right)$$

total fire streak energy

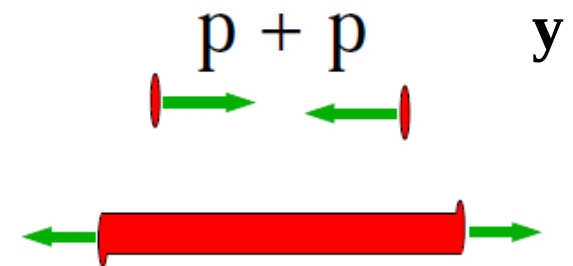
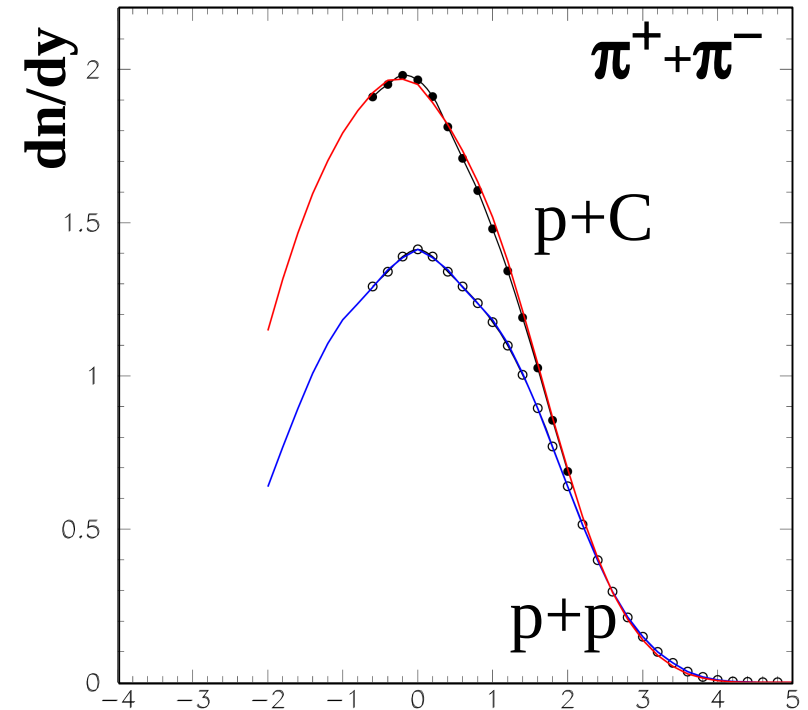
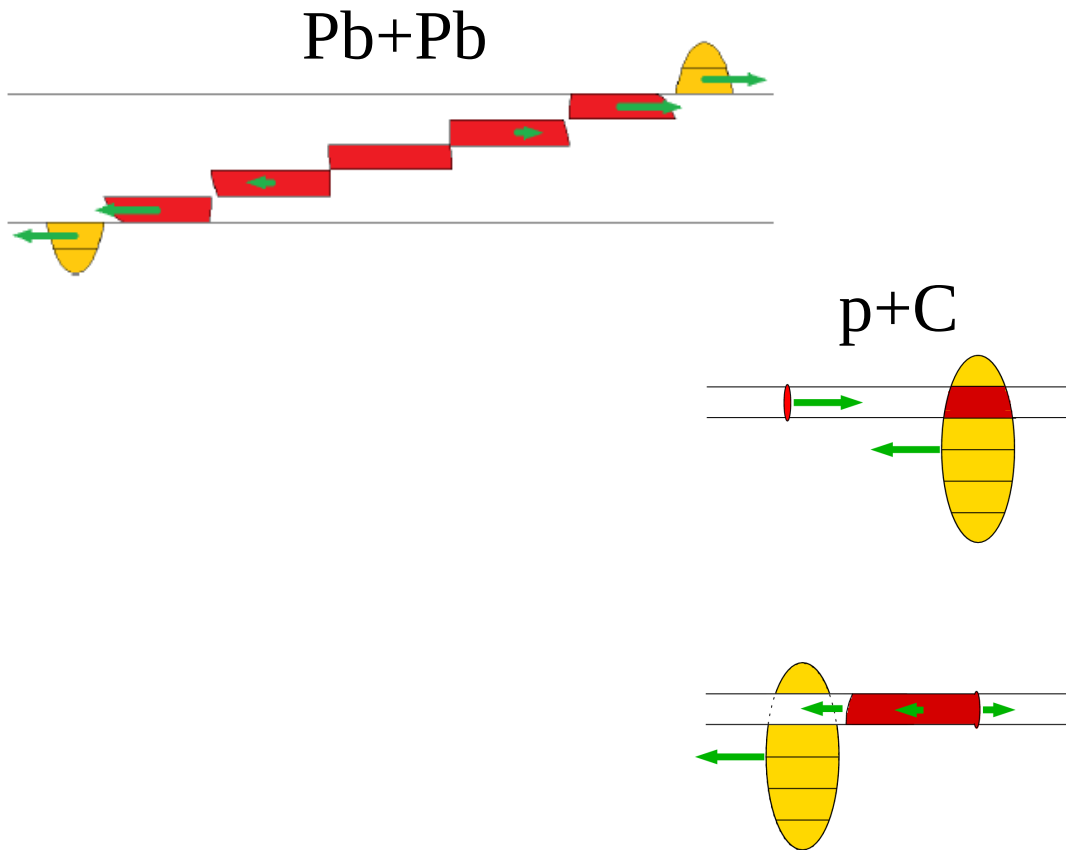
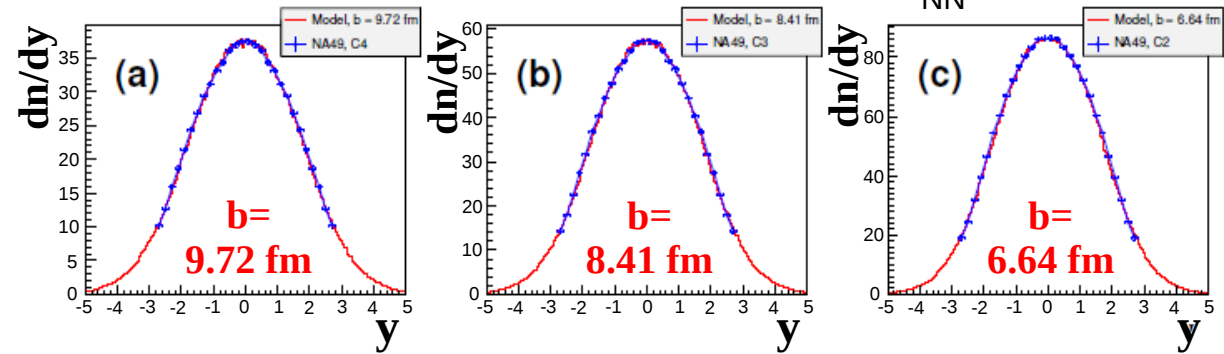
sum of brick masses

Courtesy by Harsch Shah, S.Hoche, arXiv: 1411.4085

- Link between p+p, p+A, and A+A collisions.

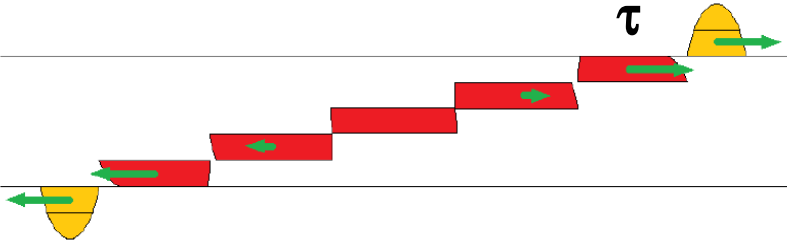


- Link between p+p, p+A, and A+A collisions.



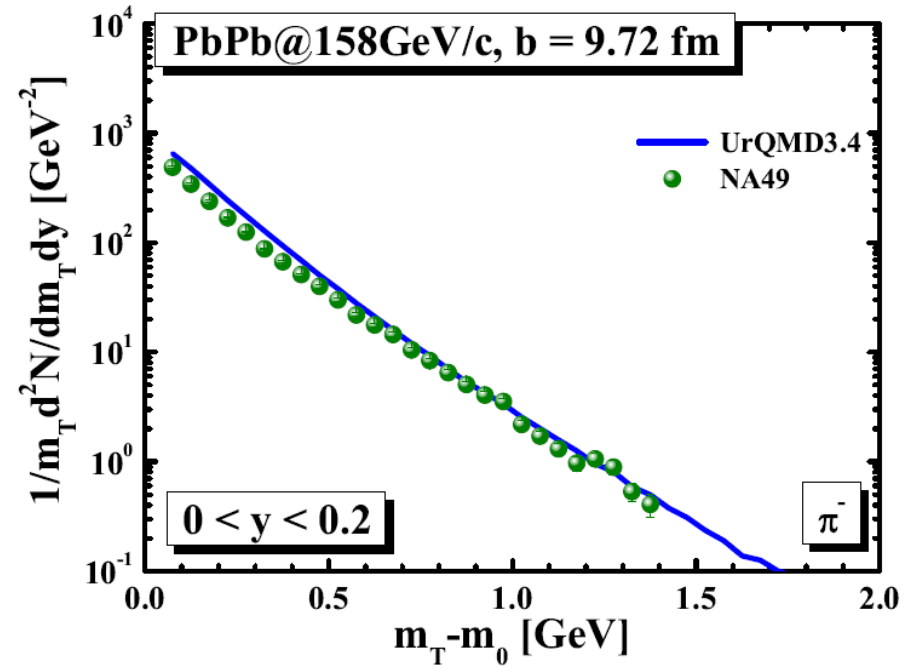
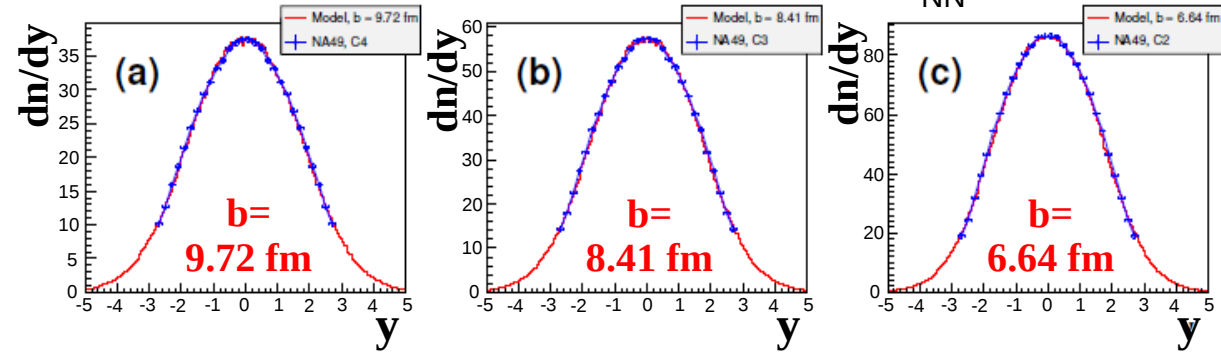
Implementation of our model for studies of EM effects:

- Initial longitudinal evolution of the system → from our model ;
- Initial (before the action of the EM field) rapidity distribution of pions → from our model ;



- Initial p_T distribution of pions → from UrQMD v3.4 ;
- The pion creation time τ (taken in the fire streak c.m.s.) → taken as free parameter ;
- Isospin effects between π^+ and π^- → included → PRC 99 (2019) 024908 ;
- Fragmentation (expansion) of the spectator charge → included optionally;
- Azimuthal anisotropies (“flow”) → included optionally.

NA49, π^- , Pb+Pb, $\sqrt{s}_{NN} = 17.3$ GeV



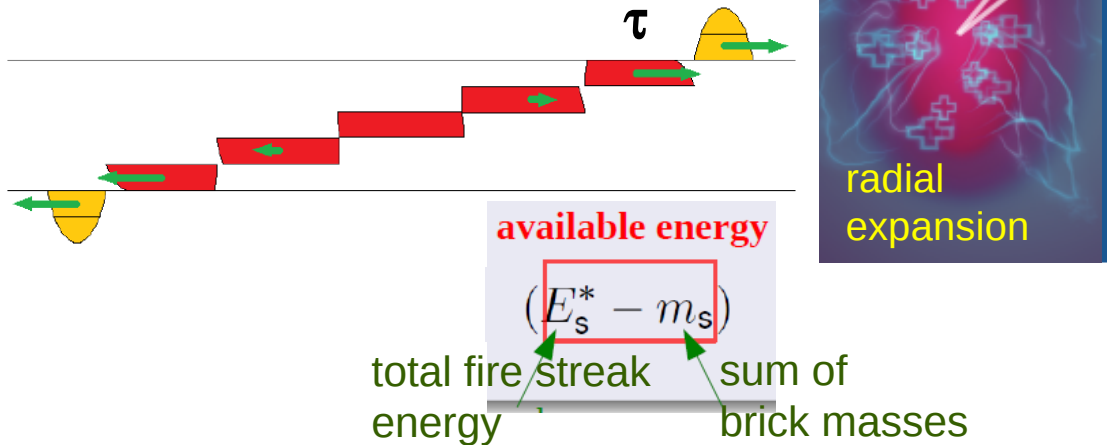
Implementation of our model for studies of EM effects, state of the art:

$$a \approx 0.08$$

$$\tau_0 = 0.5 \text{ fm}/c$$

- Simple parametrization of pion creation time : $\tau = a(E_s^* - m_s) + \tau_0$

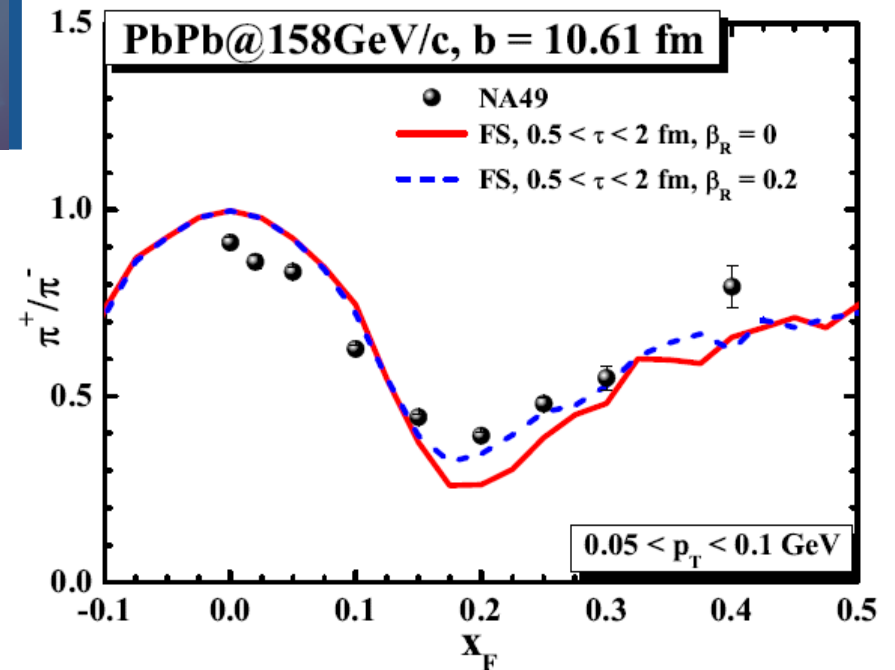
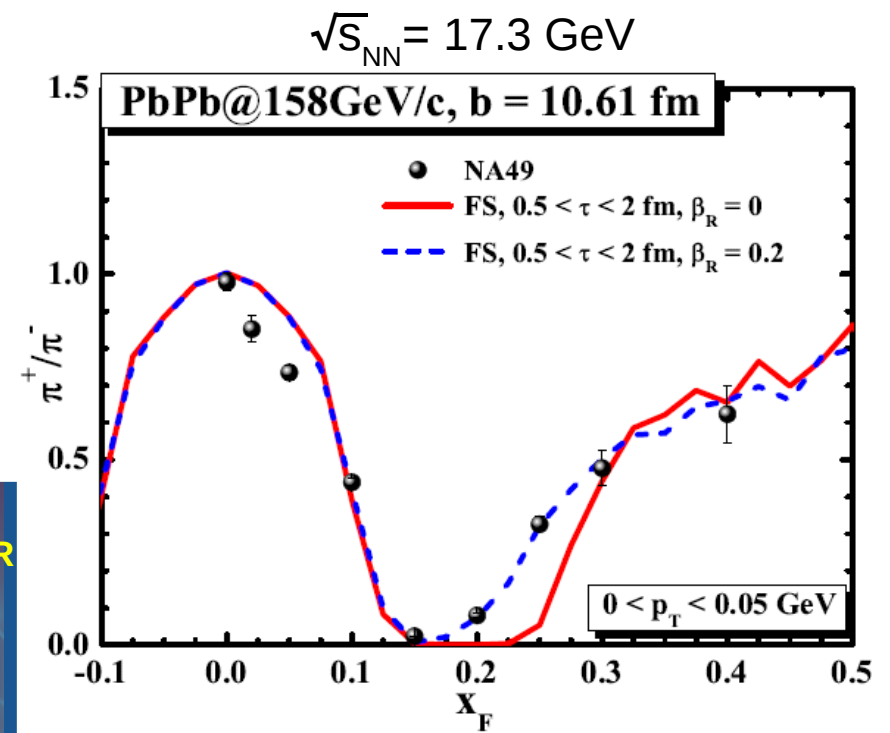
- Radial expansion assumed for spectator system.



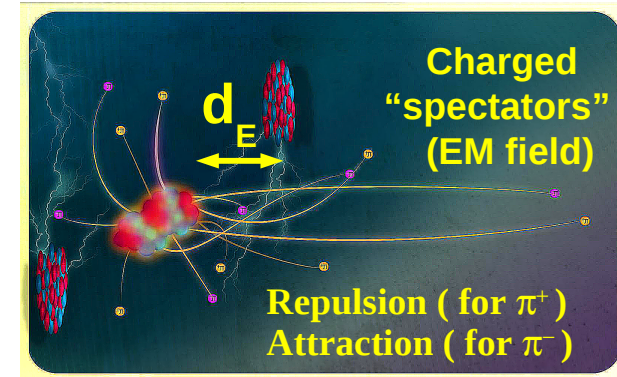
→ Reasonable agreement with data for $x_F \geq 0.1$.

→ Inclusion of spectator expansion improves the description ;

→ **Short pion creation times** ($0.5 < \tau < 2 \text{ fm}/c$, to be compared with $\sim 5.5 \text{ fm}/c$ at $y=0$).



4) Summary

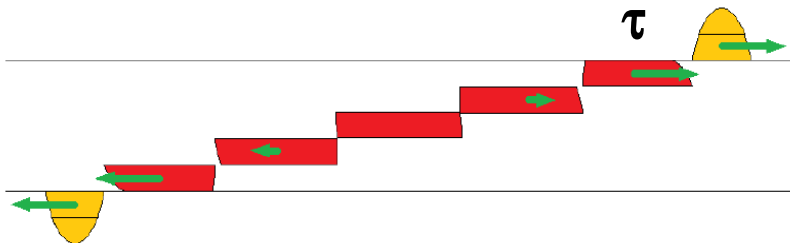


Spectator-induced electromagnetic (EM) effects can be used to study the **space-time evolution of particle production**.

Our studies have shown that in high energy nucleus-nucleus collisions, **faster** pions are produced **closer** to the spectator system, and provided an **independent estimate** for the time of pion creation, at $y=0$.

On that basis, we built a simple phenomenological model with realistic initial conditions (incidentally we found that it **works** for all the three reaction types). This we used to study the space-time evolution of the system w.r.t. forward production of **fast ($x_F > 0.1$) pions**.

This study gives an indication that relatively **short** pion production time scales (proper pion creation times τ) are needed to describe the experimental data.



Thank you !

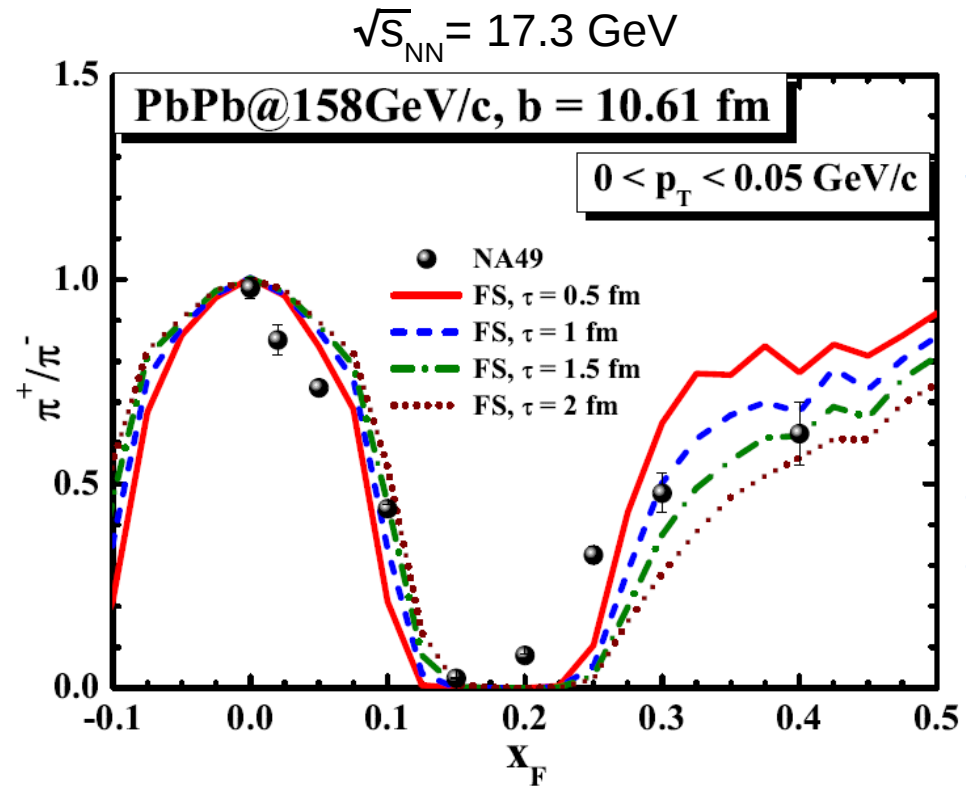
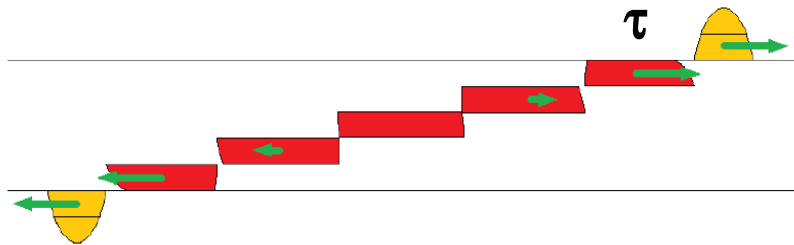
Acknowledgments.

This work was supported by the National Science Centre, Poland
(grant no. 2014/14/E/ST2/00018).

Extra slides

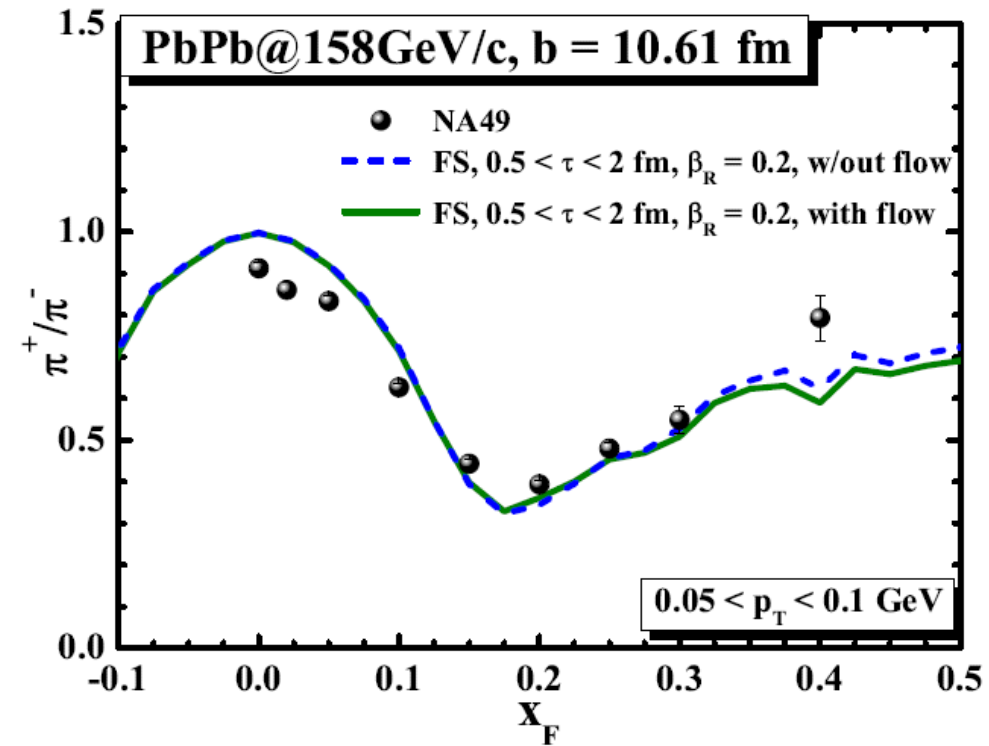
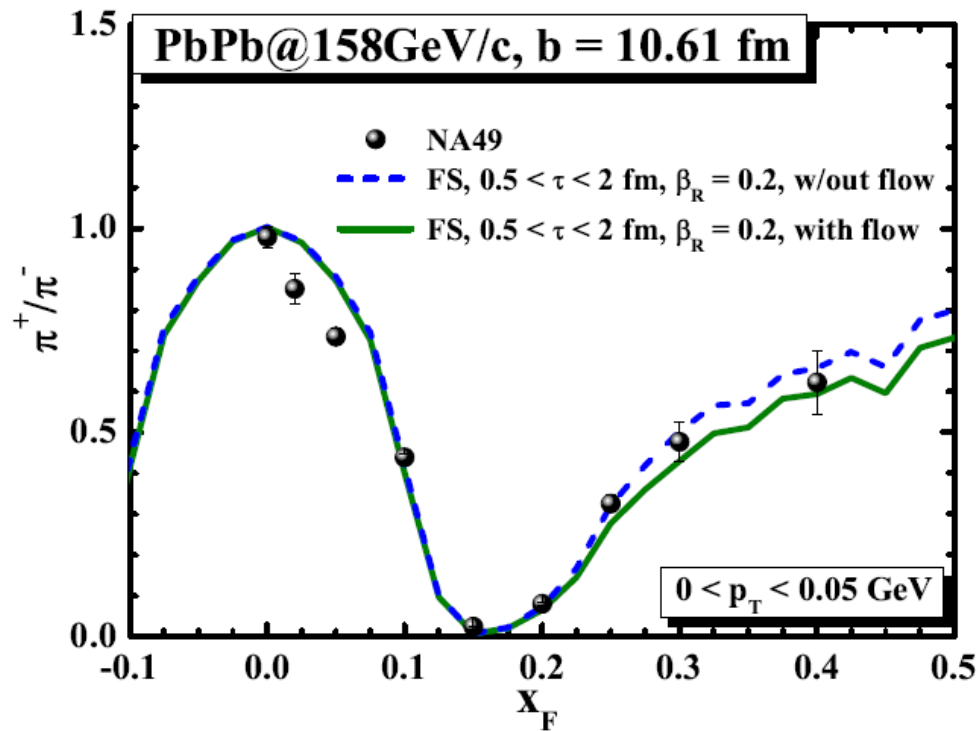
Implementation of our model for studies of EM effects, first results:

- Fixed pion creation time τ (in fire streak rest frame) ;
- No spectator fragmentation.

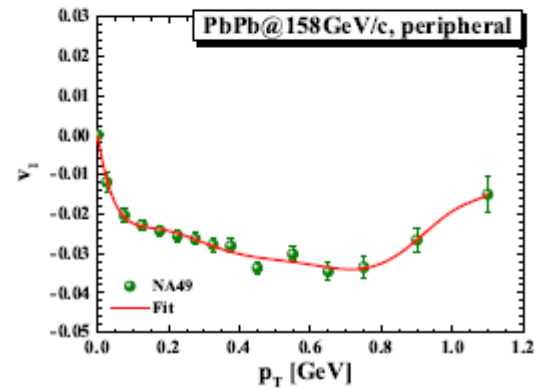
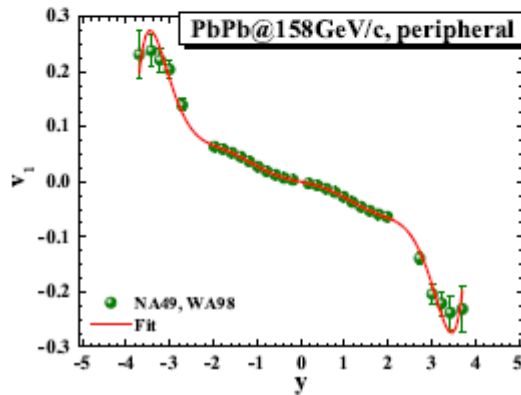
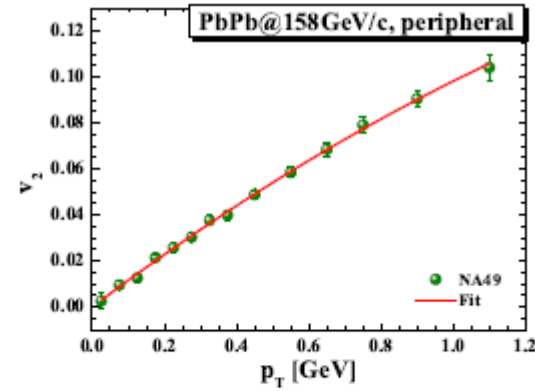
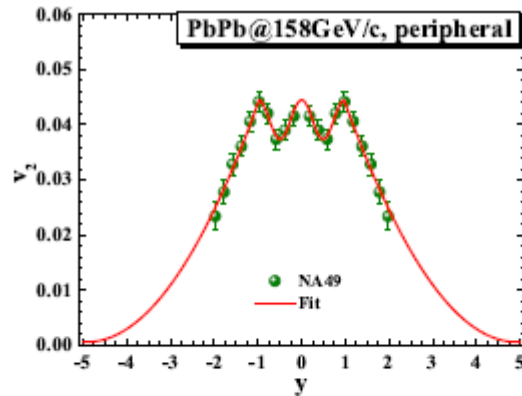


- ➔ Relatively **short pion creation times** are suggested by the exp. data ($\tau \sim 0.5 - 1.5 \text{ fm/c}$, to be compared with $\sim 5.5 \text{ fm/c}$ at $y=0$) ;
- ➔ Impossible to fit the data with **one single value** of τ ;
- ➔ Evident **problem** at $x_F = 0.2 - 0.25$.

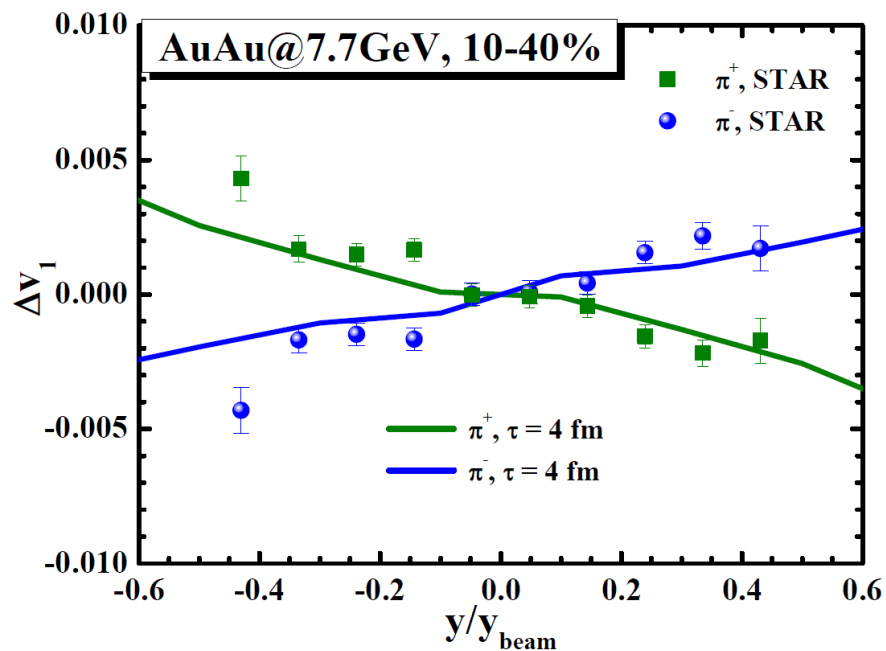
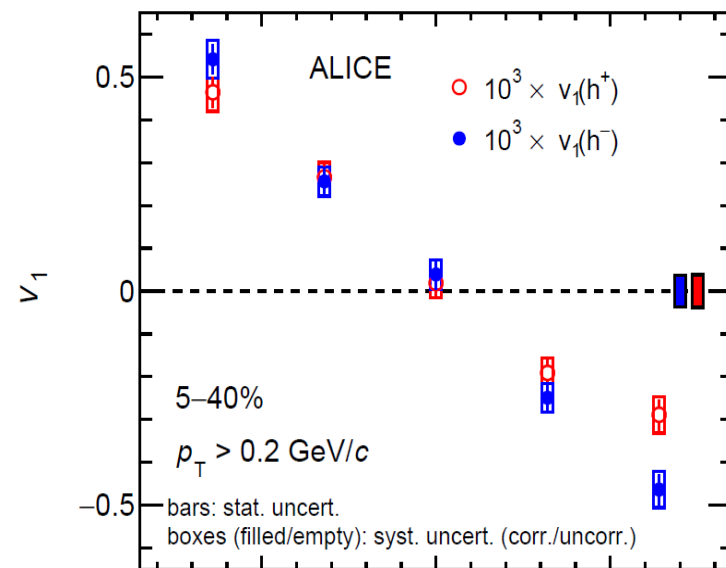
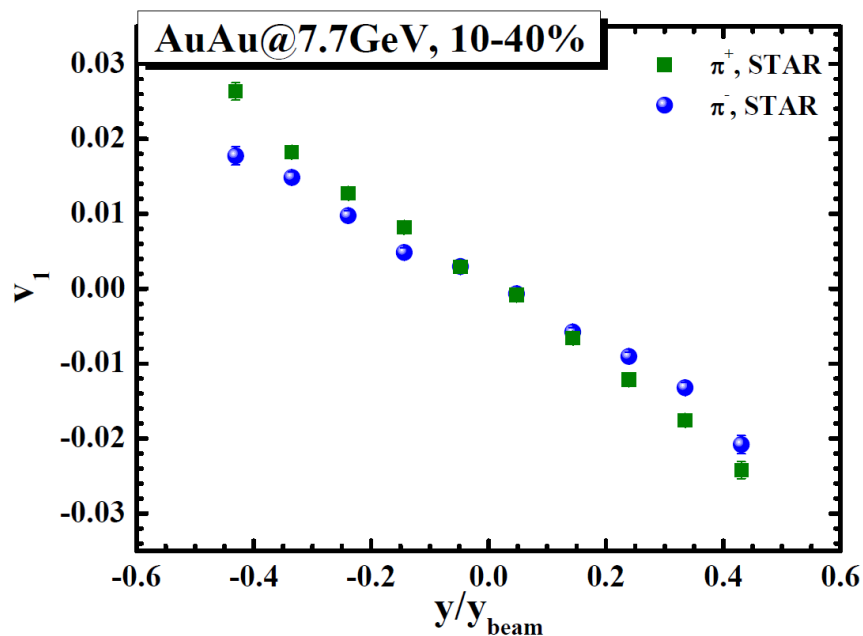
Influence of azimuthal anisotropies (flow) on π^+/π^- ratios



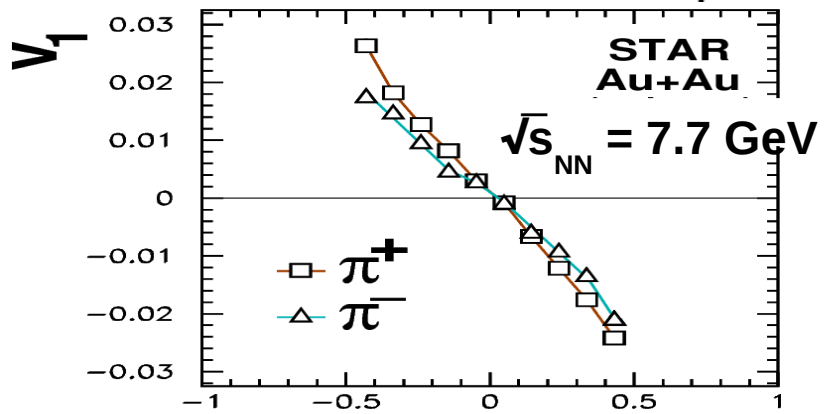
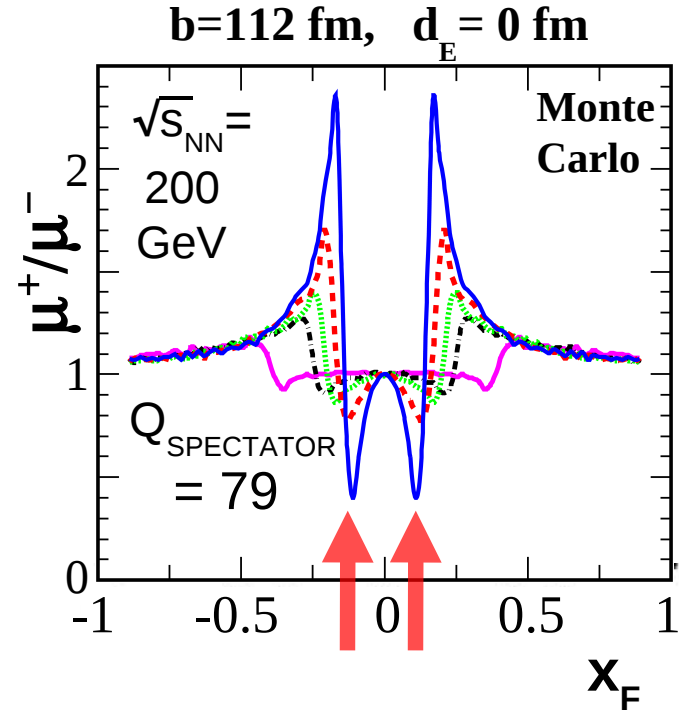
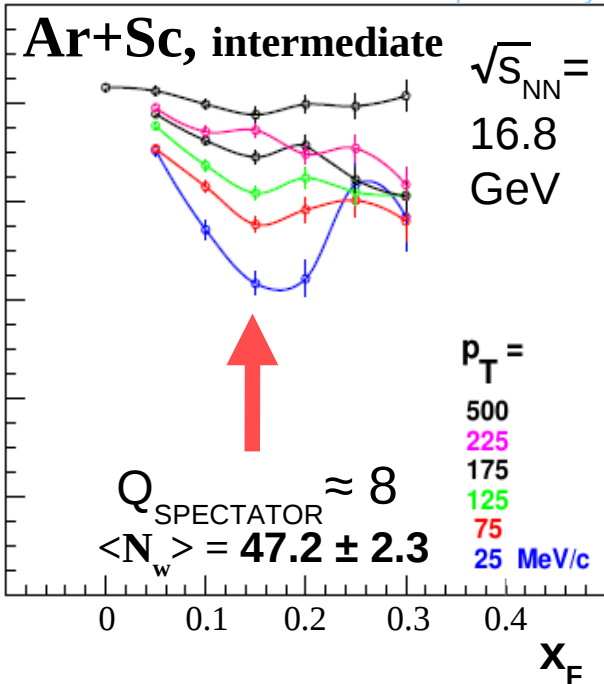
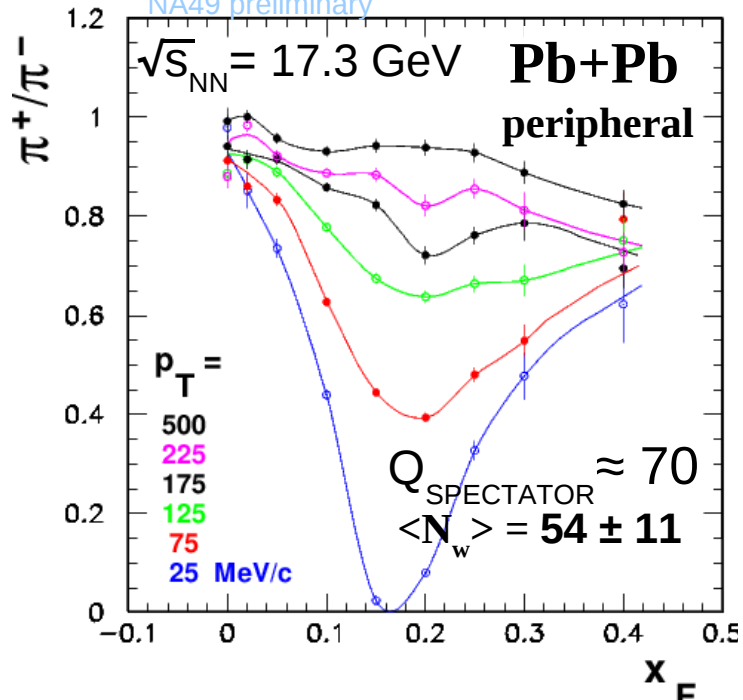
Inclusion of azimuthal anisotropies (flow) in the model



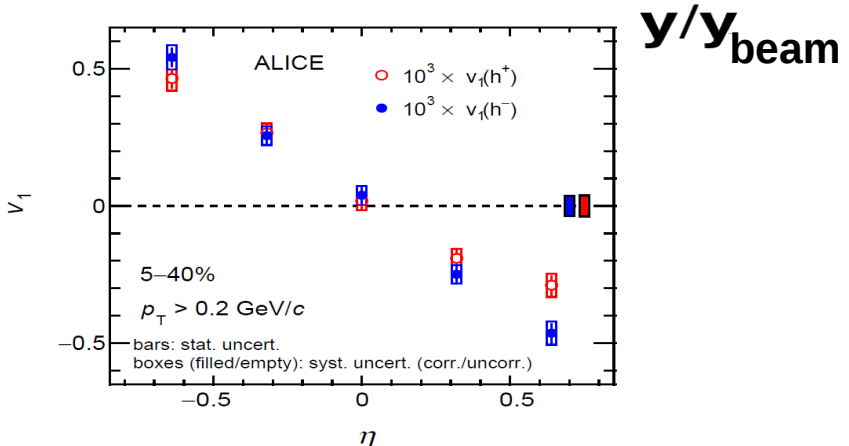
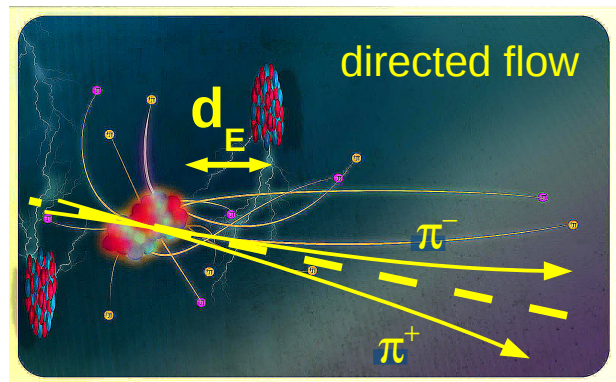
More on asimuthal anisotropies (flow)



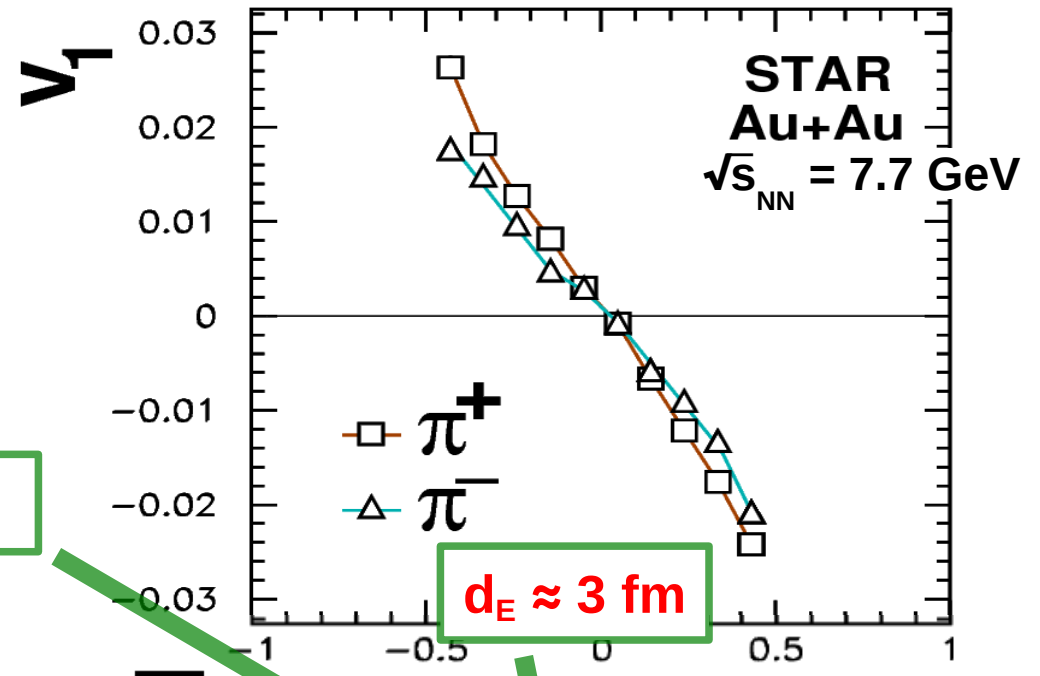
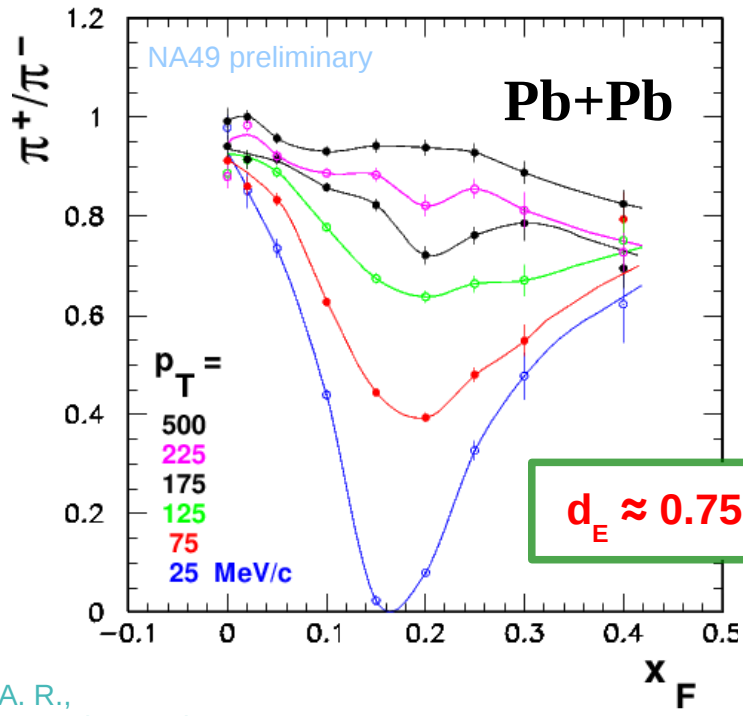
STAR:
L. Adamczyk et al., PRL 112 (2014) 162301
ALICE:
S. Acharya et al., arXiv:1910.14406 [nucl-ex]



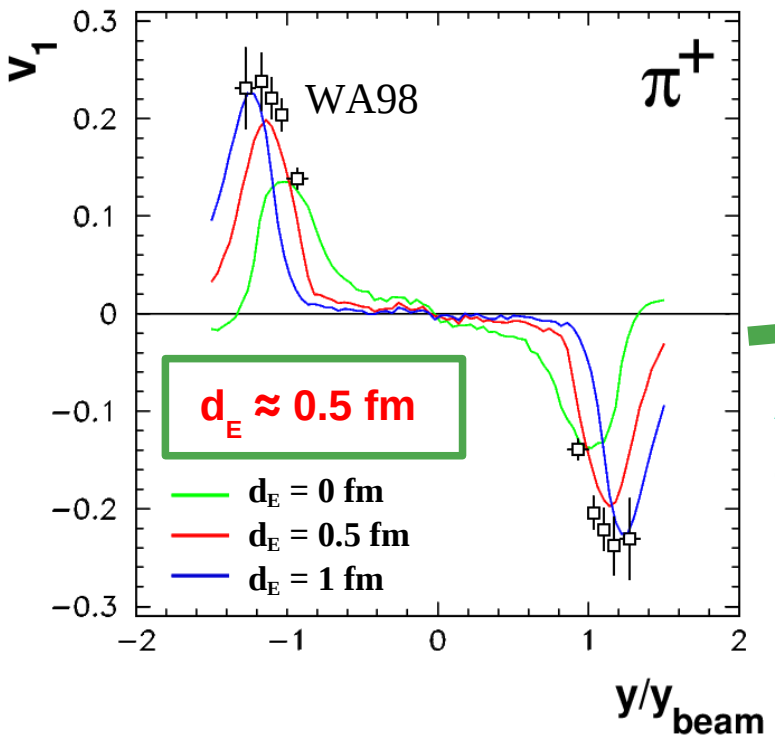
STAR:
L. Adamczyk et al., PRL 112 (2014) 162301
ALICE:
S. Acharya et al., arXiv:1910.14406 [nucl-ex]



- v_1 ("directed flow") is the sidewards deflection of pions in the reaction plane :
- $$v_1 \equiv \langle \cos(\varphi \text{ w.r.t. reaction plane}) \rangle$$
- the spectator charge induces *charge splitting* of v_1 .

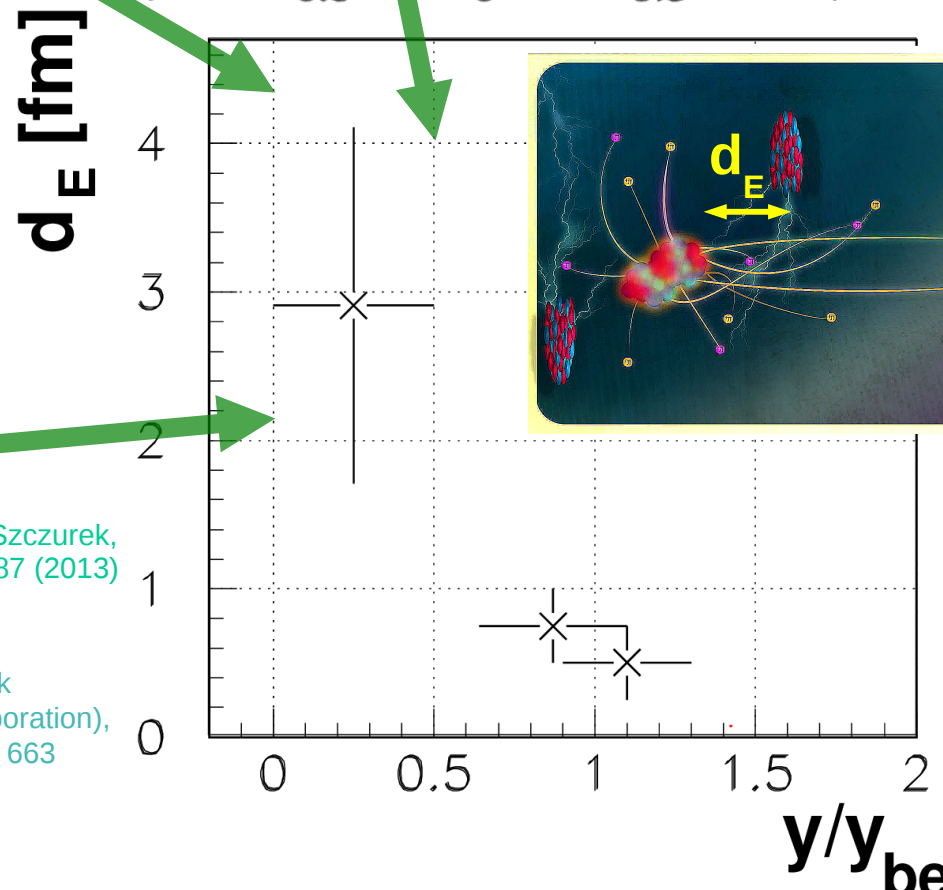


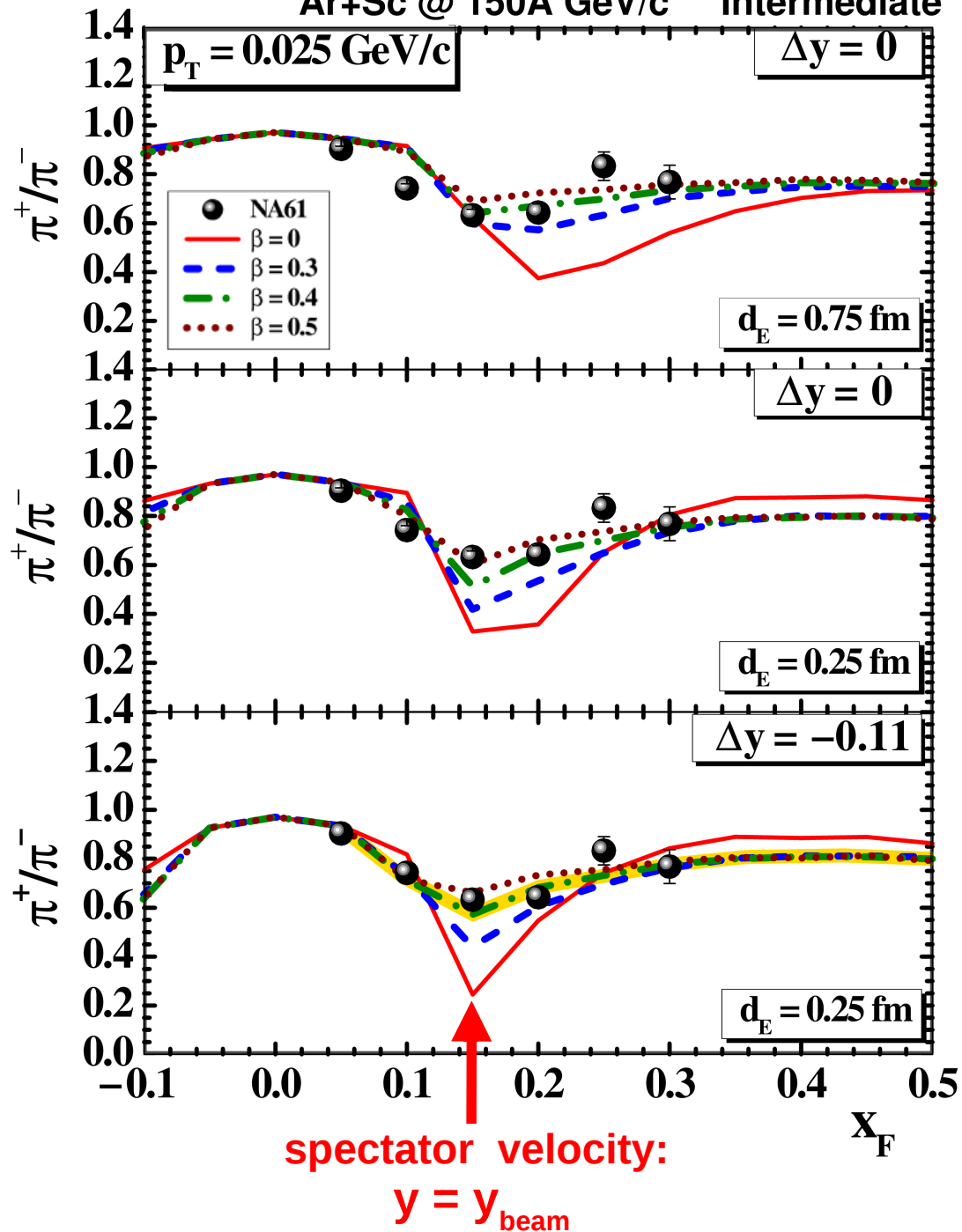
A. R.,
 Acta Phys. Polon.
 B42 (2011) 867



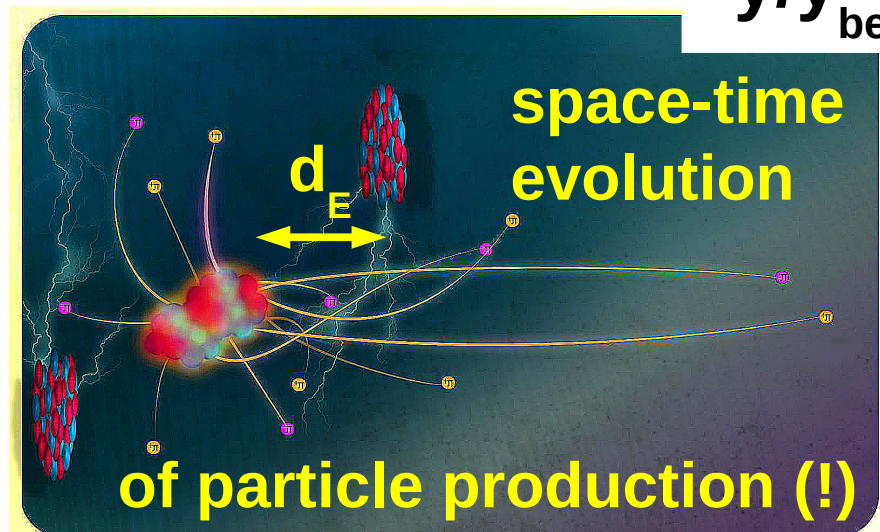
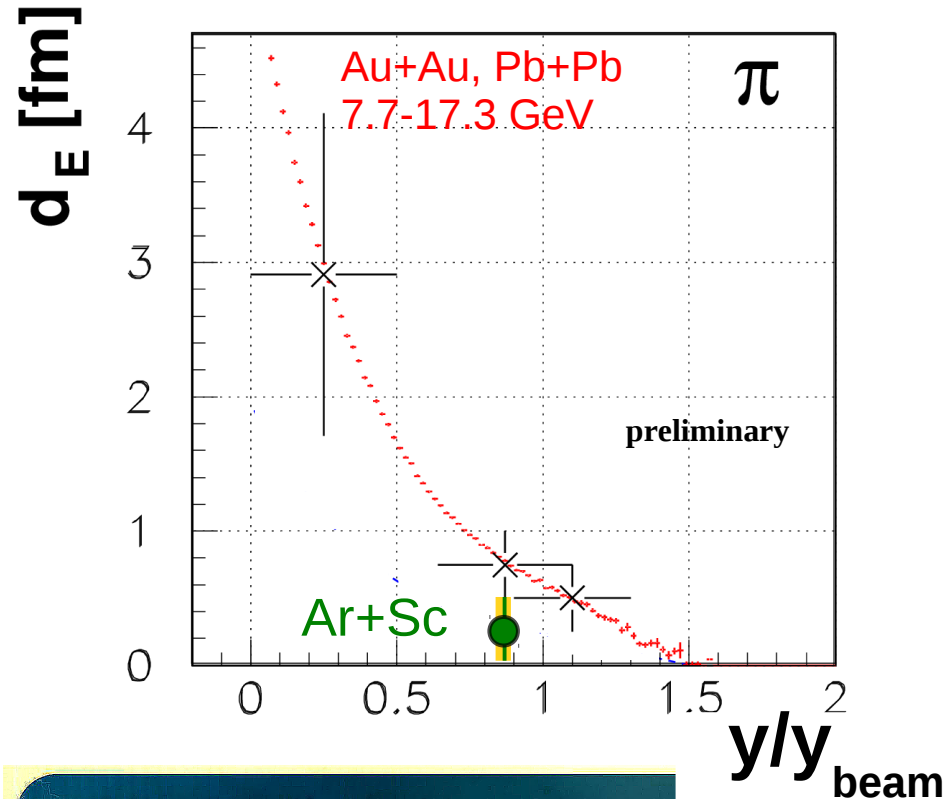
A. R. and A. Szczurek,
 Phys. Rev. C87 (2013)
 054909.

H. Schlagheck
 (WA98 Collaboration),
 Nucl. Phys. A 663
 (2000) 725.

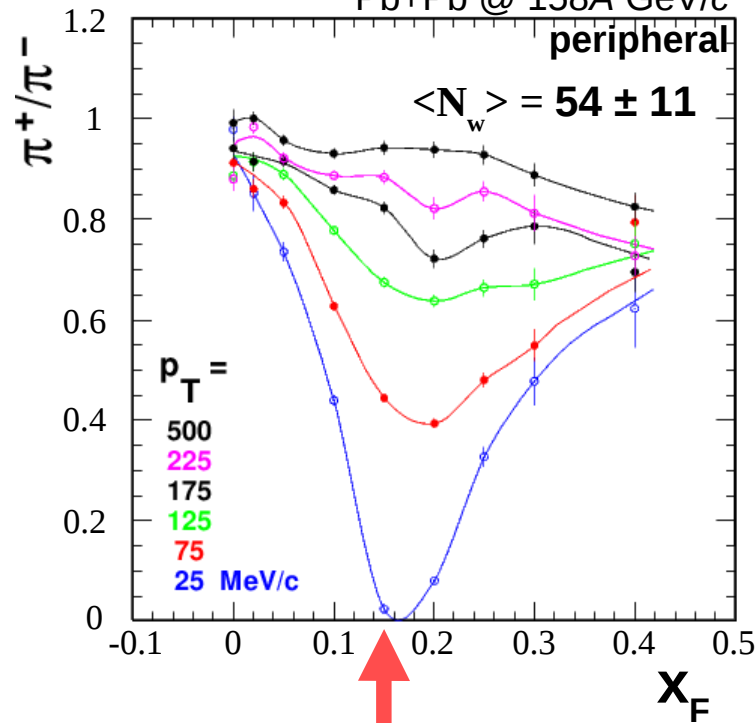




EM effects from NA61/SHINE

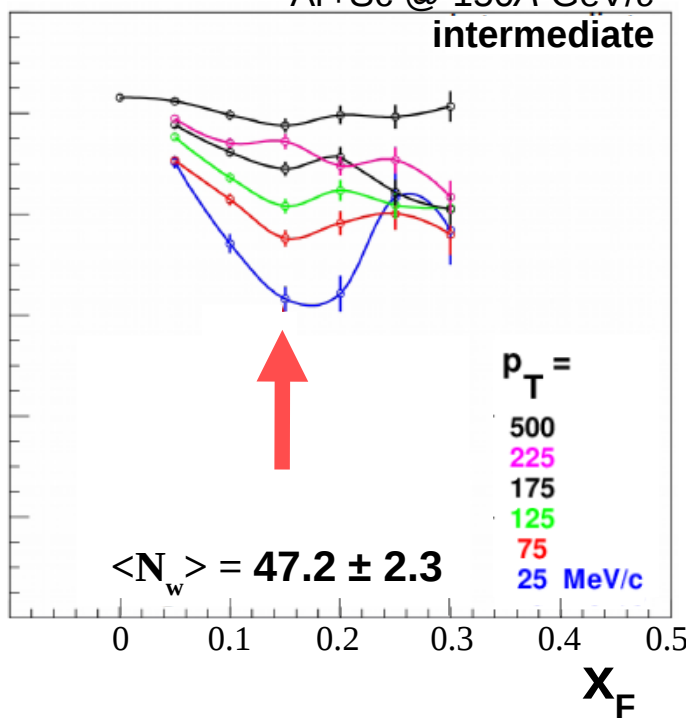


NA49 preliminary
Pb+Pb @ 158A GeV/c



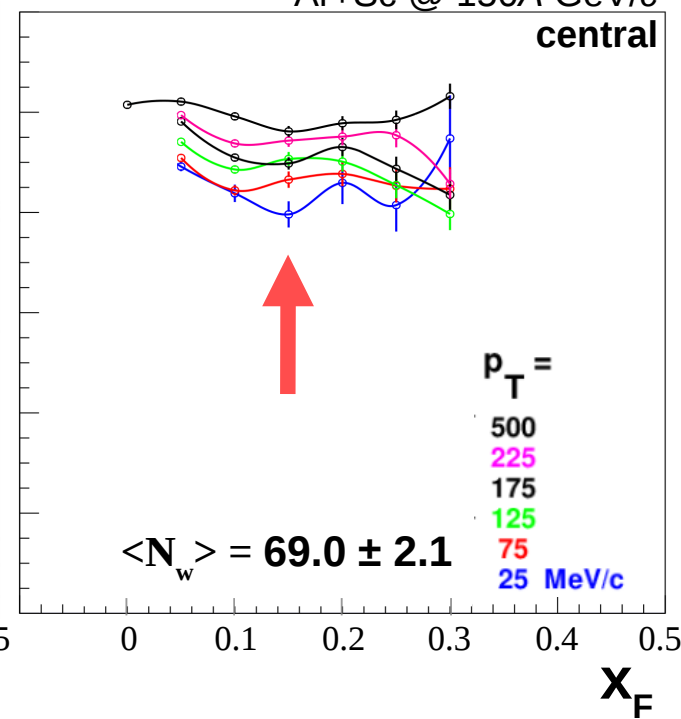
spectator velocity:
 $y = y_{\text{beam}}$

NA61/SHINE preliminary
Ar+Sc @ 150A GeV/c



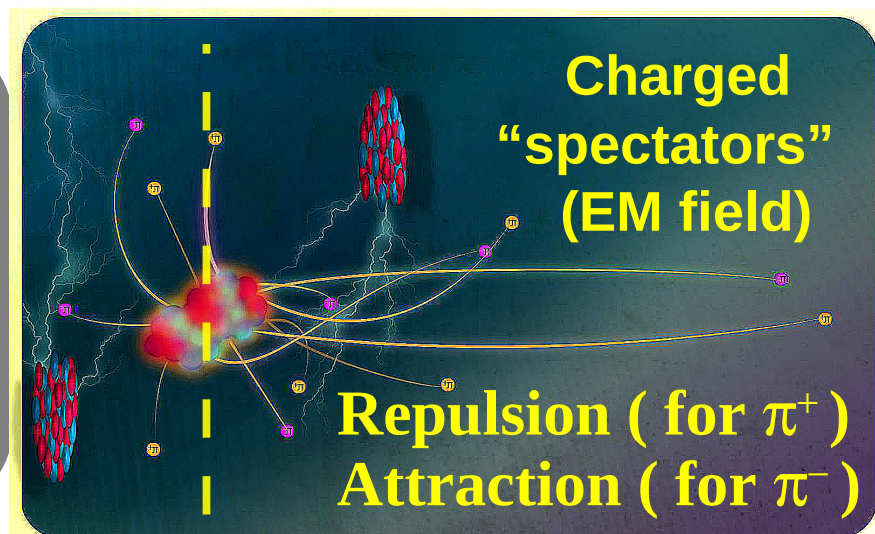
$$x_F = \frac{p_L}{p_L^{\text{beam}}} \quad (\text{c.m.s.})$$

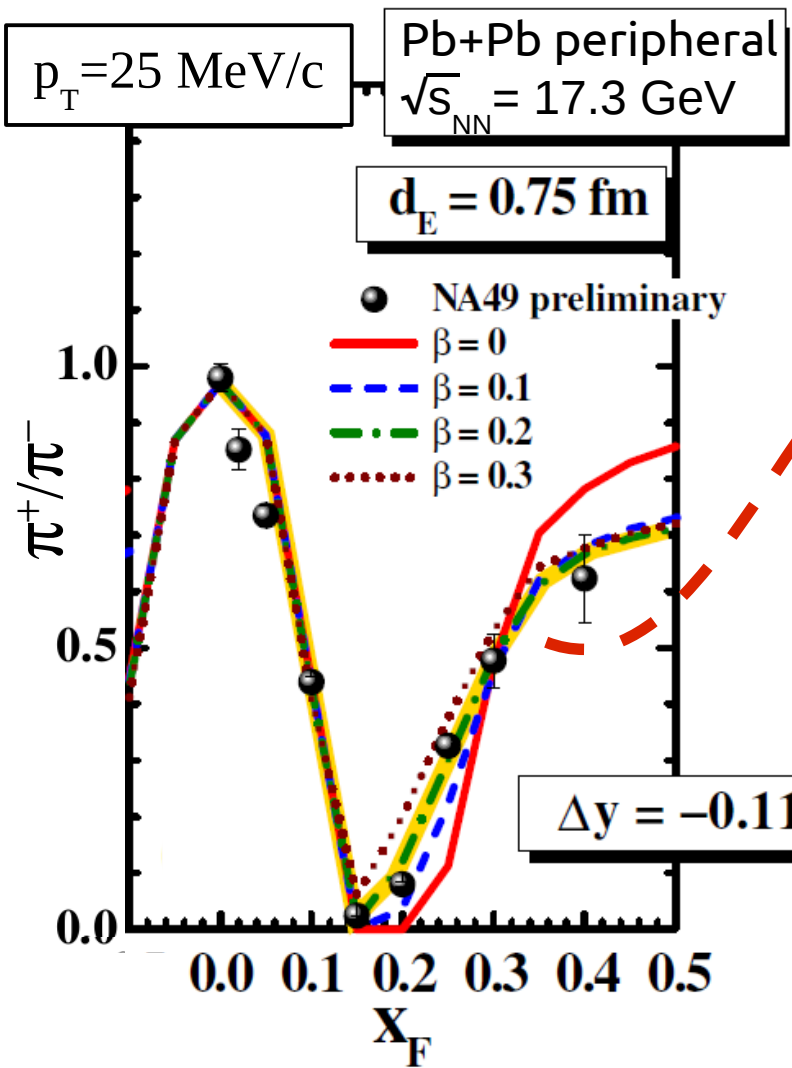
NA61/SHINE preliminary
Ar+Sc @ 150A GeV/c



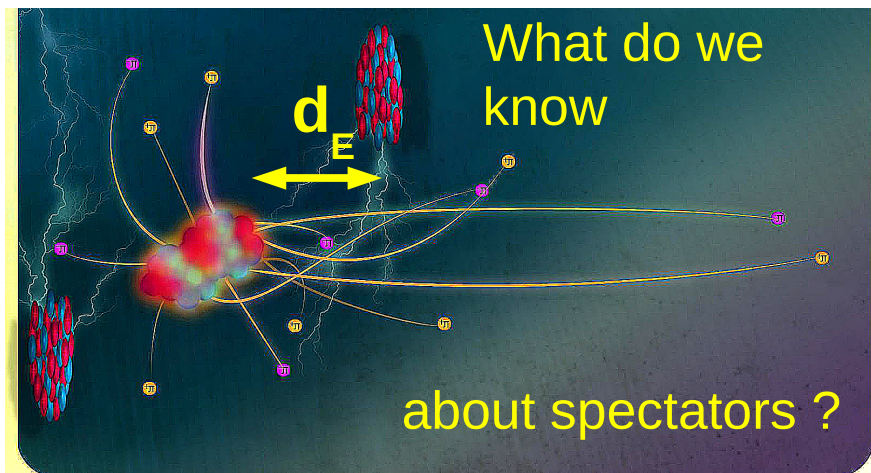
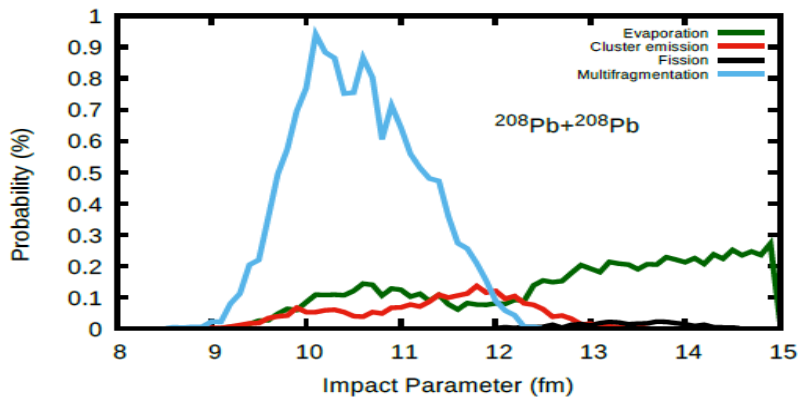
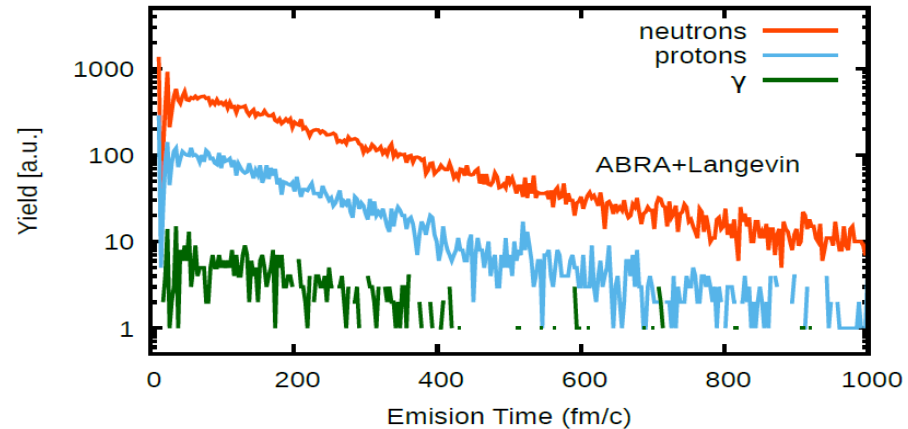
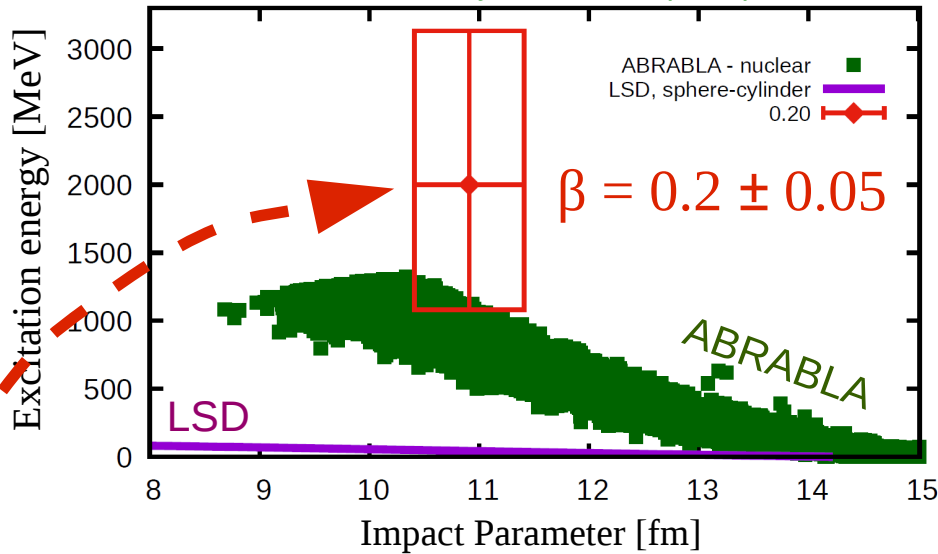
A. Marcinek,
Acta Phys. Polon. B50 (2019) 1127

- (a) Peripheral Pb+Pb ($Q_{\text{SPECTATOR}} \approx 70$)
→ large EM effect, $\pi^+/\pi^- \approx 0$.
- (b) Intermediate Ar+Sc ($Q_{\text{SPECTATOR}} \approx 8$)
→ visible EM effect, breaks isospin symmetry.
- (c) Central Ar+Sc ($Q_{\text{SPECTATOR}} \approx 3$)
→ still visible shadow of EM effect.





Spectators

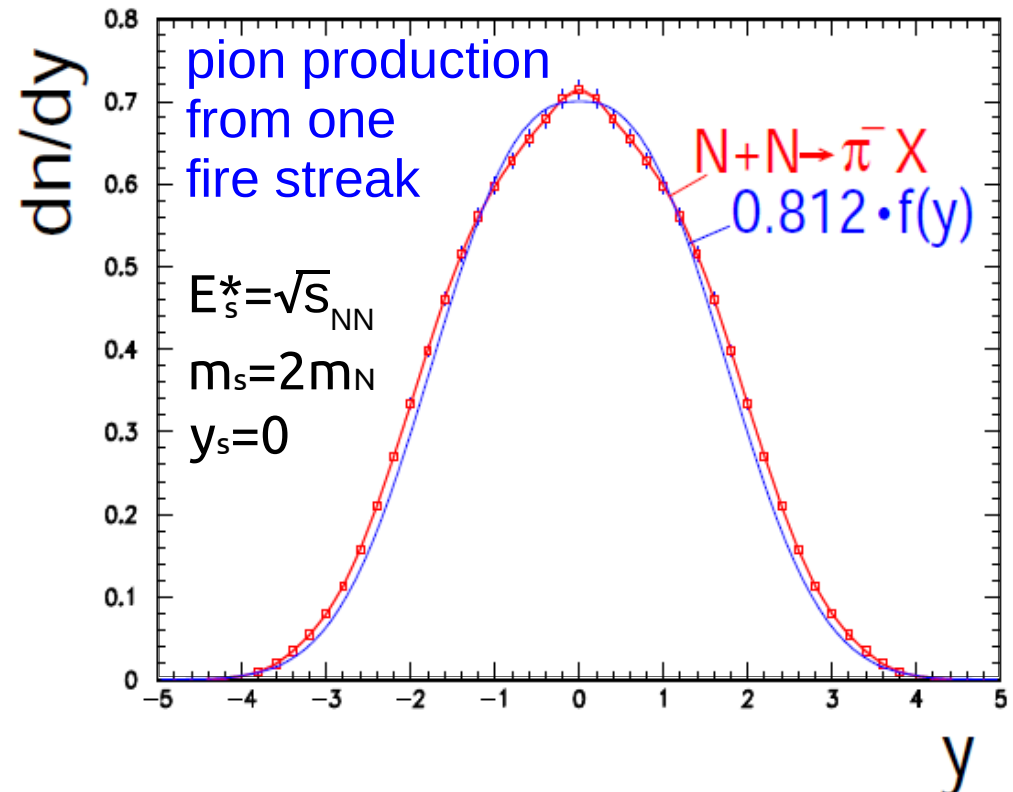
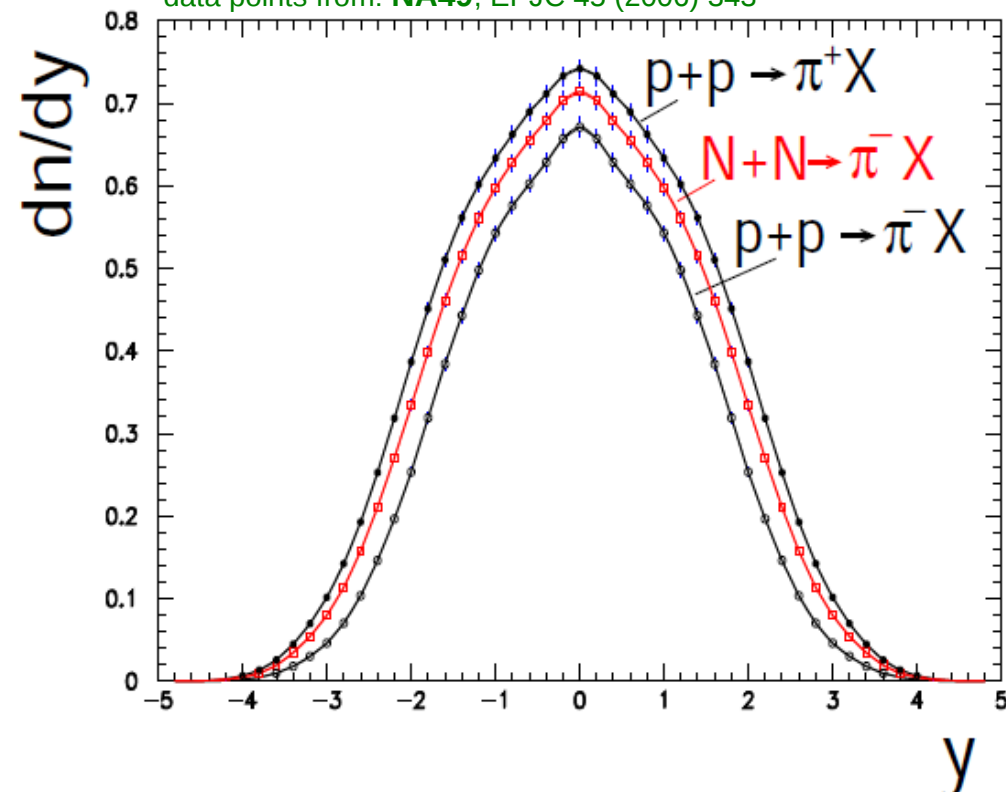


Isospin effects

- Pb+Pb collision: **40%** protons, **60%** neutrons ;
- **p+p** → **π⁻X** is not directly comparable to **Pb+Pb** → **π⁻X** !
- isospin symmetry: $\frac{dn}{dy}(n \rightarrow \pi^-) = \frac{dn}{dy}(p \rightarrow \pi^+)$
- isospin-averaged π^- distribution:

$$\frac{dn}{dy}(N + N \rightarrow \pi^- X) = \left(\frac{Z}{A}\right) \cdot \frac{dn}{dy}(p + p \rightarrow \pi^- X) + \left(1 - \frac{Z}{A}\right) \cdot \frac{dn}{dy}(p + p \rightarrow \pi^+ X)$$

data points from: **NA49**, EPJC 45 (2006) 343



Once isospin is taken into account, the difference in absolute scaling between p+p and Pb+Pb collisions changes from **0.748** to **0.812** .

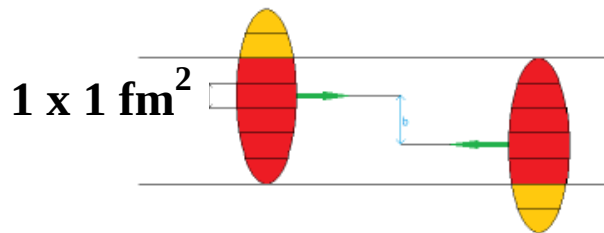
Includes:

- characteristics of “fire streaks”
- computation of energy balance
- energy dependence
- auxiliary information on proton-nucleus

More on our simple model

For a more extended description including formulae, numerical values, tables and plots, please see
PRC 99 (2019) 024908

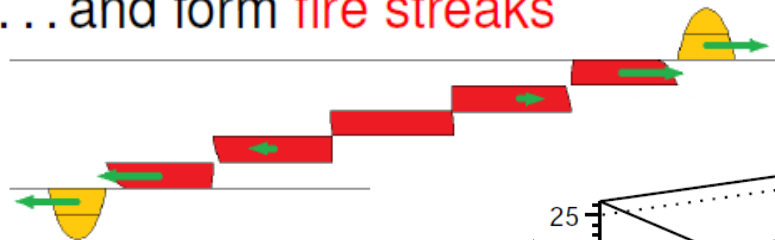
Bricks collide ...



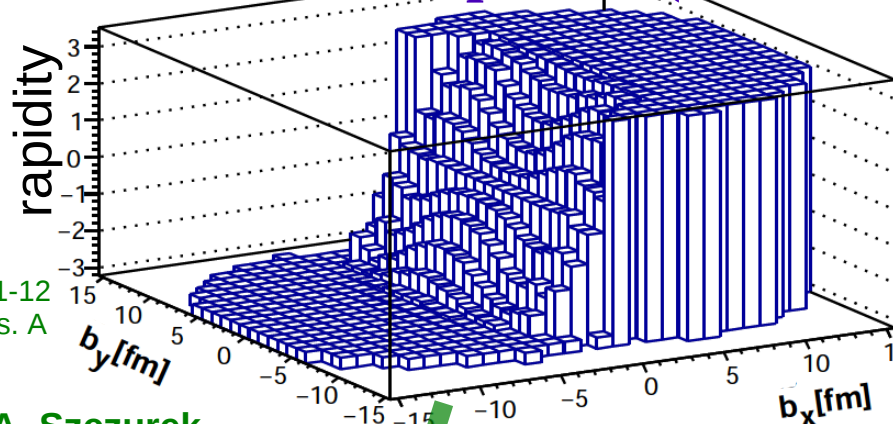
R. Hagedorn, CERN-71-12
W.D. Myers, Nucl. Phys. A

(Re)invented by A. Szczurek

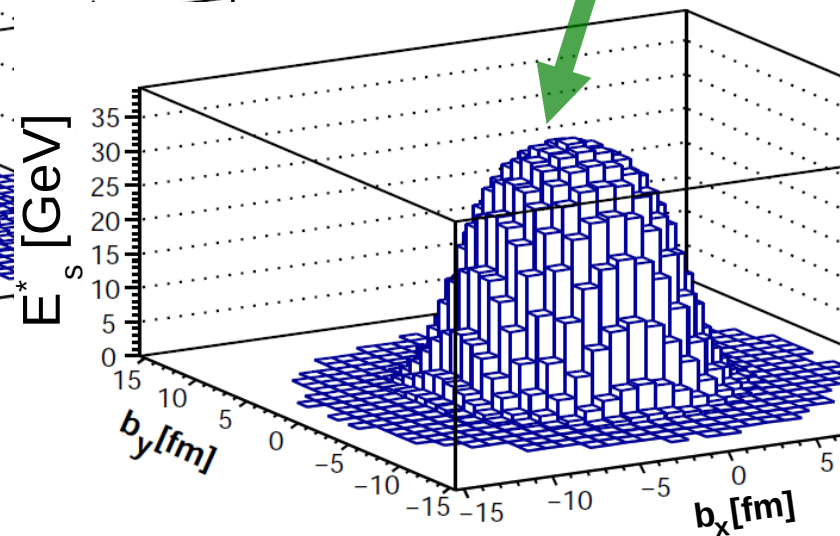
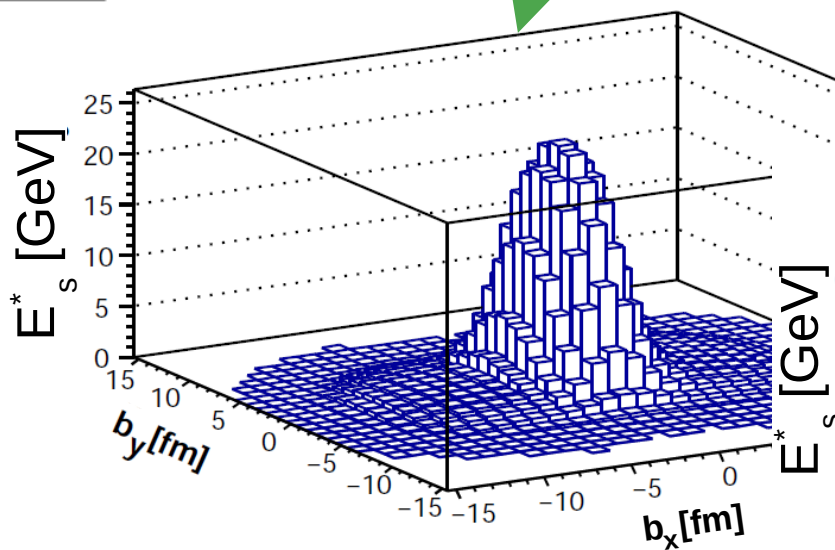
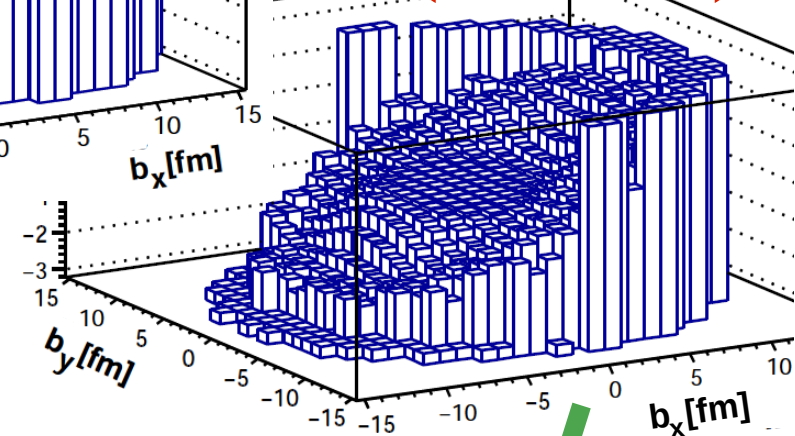
... and form **fire streaks**



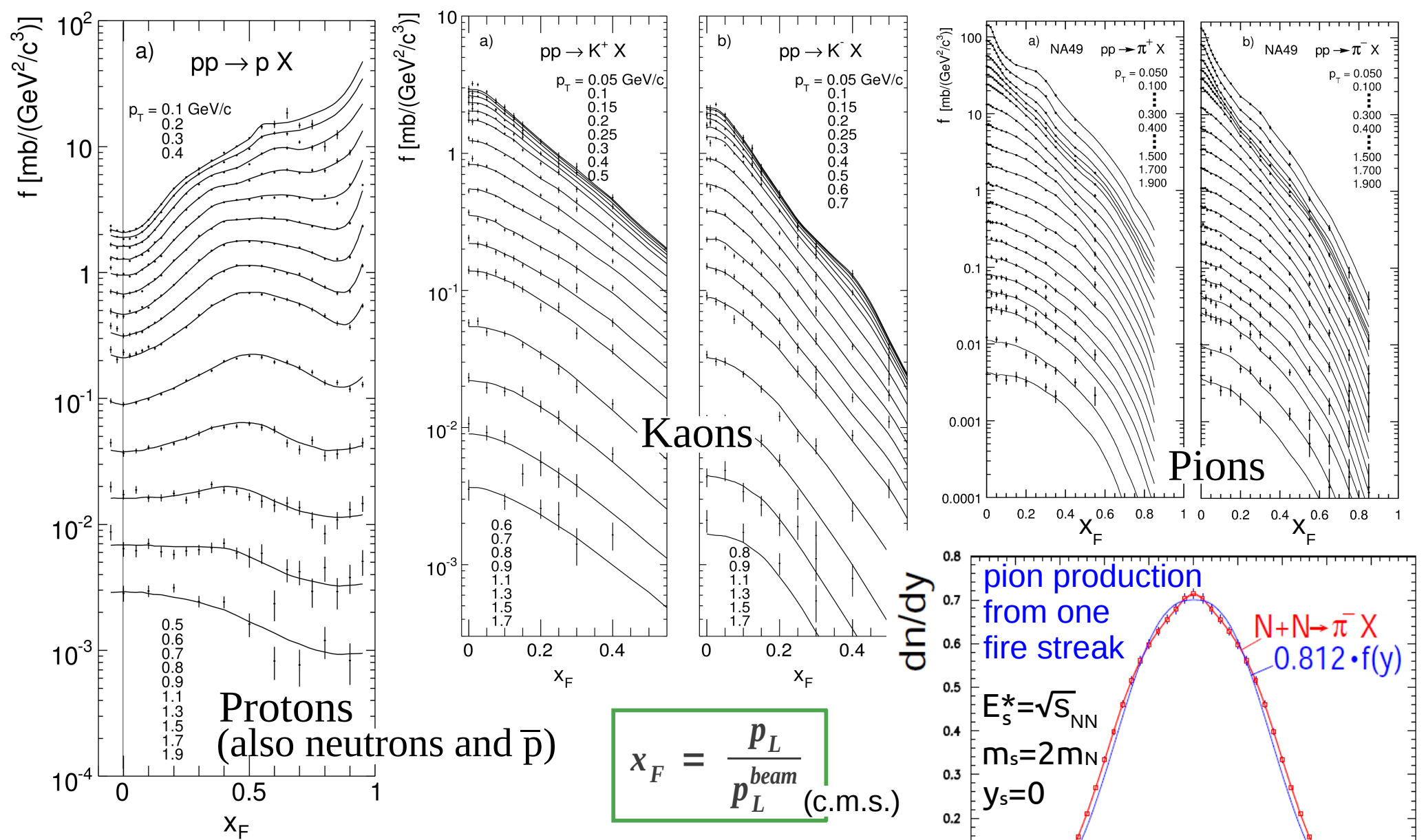
Peripheral (b=9.72 fm)



Central (b=2.55 fm)



Characteristics of “fire streaks”



In $p+p$ collisions, the average energies of pions, kaons and protons can be computed **directly from their spectra** :

$$\langle E_i \rangle = \frac{\int_0^1 \int_0^{p_T(\max)} E_i(x_F, p_T) \cdot \left(\frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}{\int_0^1 \int_0^{p_T(\max)} \left(\frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}$$

i – proton, π^+ , π^- , K^+ , K^- , ...

Calculation of energy balance (simplified):

$$\langle E_i \rangle = \frac{\int_0^1 \int_0^{p_T(\max)} E_i(x_F, p_T) \cdot \left(\frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}{\int_0^1 \int_0^{p_T(\max)} \left(\frac{d^2\sigma}{dx_F dp_T} \right)_i dp_T dx_F}$$

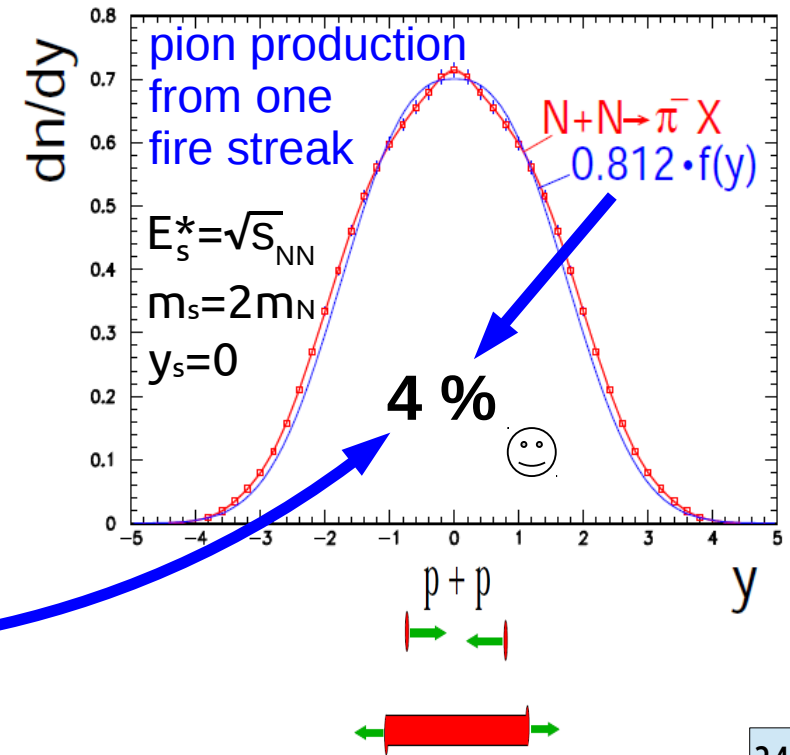
p+p: (pion energy) = **6862 MeV** ;
 (kaon energy) = **918 MeV** ;
 (baryon energy) → baryon inelasticity **K = 0.547**.

$$K = \frac{2 \cdot E_{inel}}{\sqrt{s} - 2m_p}$$

The relation between (baryon energy), (pion energy) and (kaon energy) in **Pb+Pb** collisions is calculated on the basis of:

- baryon inelasticity in Pb+Pb, **K ≈ 0.78** ; → C.Blume, **NA49**, J.Phys. G34 (2007) 951, and refs therein.
- the change in $\langle K \rangle / \langle \pi \rangle$ ratios between p+p and Pb+Pb (**~2**).

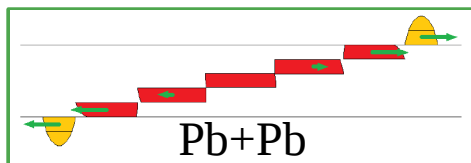
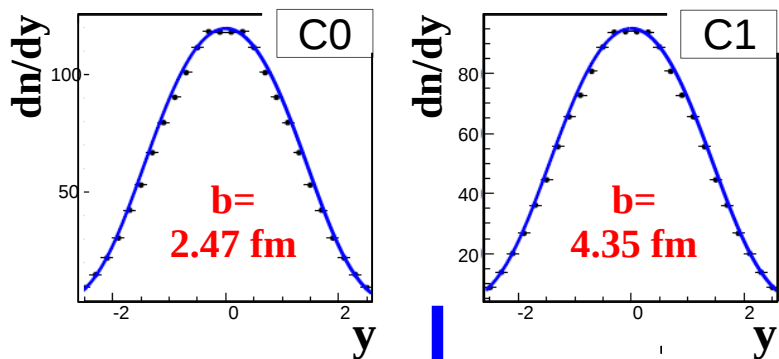
From:
NA49, EPJC 65 (2010) 9, EPJC 68 (2010) 1, EPJC 45 (2006) 343,
 PRC 86 (2012) 054903, and references therein.
NA49, compilation of numerical results, <http://na49info.web.cern.ch/na49info/na49>.



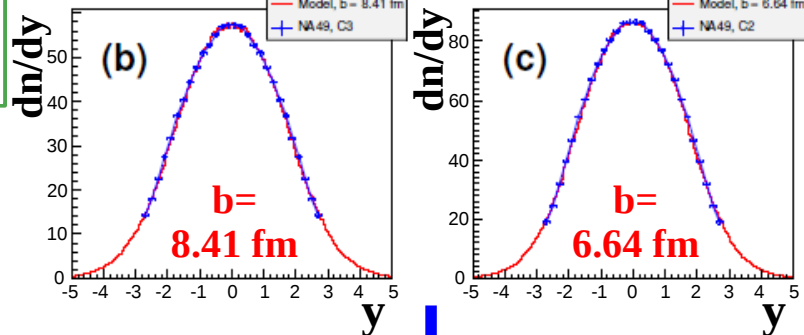
In this way we get (per unit of total collision energy):

$$\frac{\text{Energy spent on pions in p+p}}{\text{Energy spent on pions in Pb+Pb}} = 0.781$$

π^- , Pb+Pb, $\sqrt{s}_{NN} = 8.8$ GeV

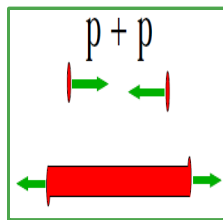
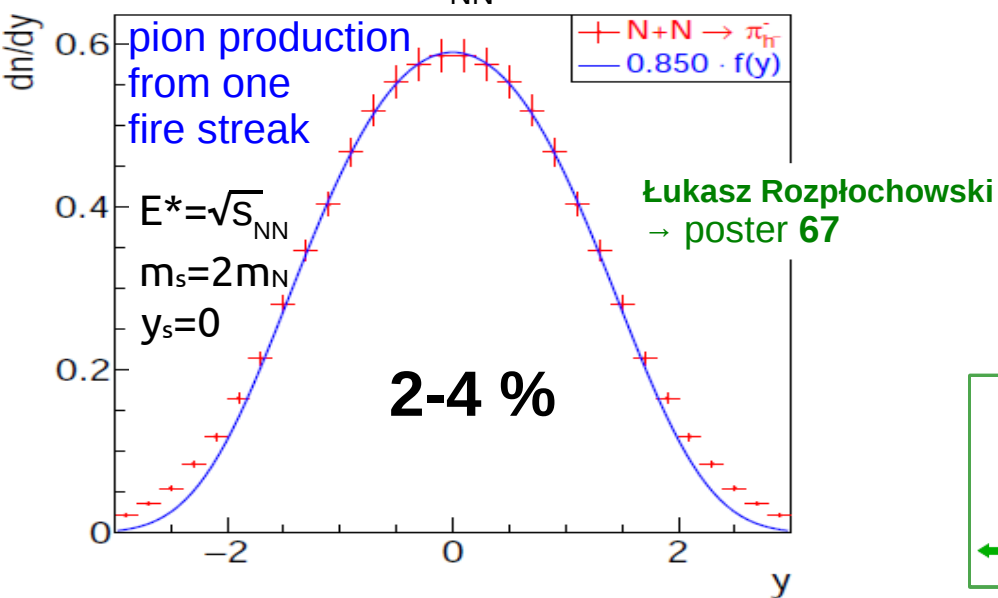


π^- , Pb+Pb, $\sqrt{s}_{NN} = 17.3$ GeV

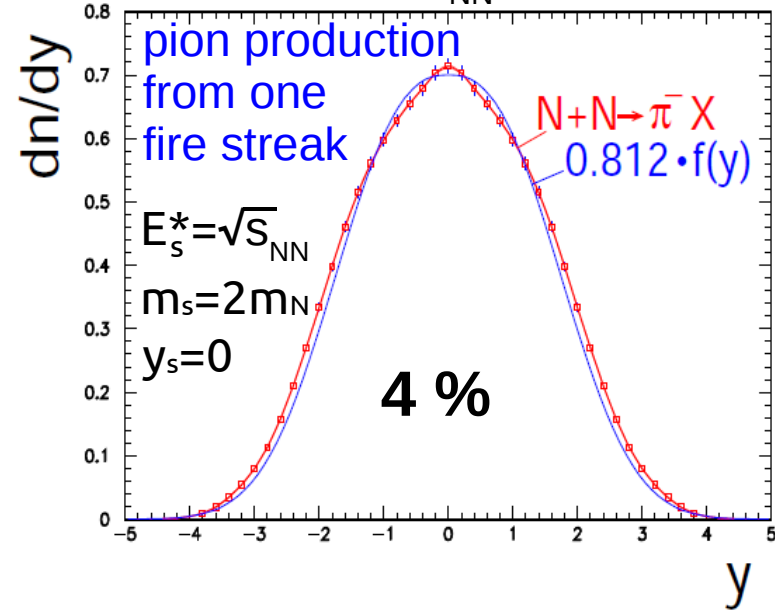


Valid for
 $8.8 \text{ GeV} \leq \sqrt{s}_{NN} \leq 17.3 \text{ GeV}$
 (or better)

π^- , N+N, $\sqrt{s}_{NN} = 8.8$ GeV



π^- , N+N, $\sqrt{s}_{NN} = 17.3$ GeV



The energy dependence of the fire streak fragmentation function (PRC 99 (2019) 024908, Appendix B)

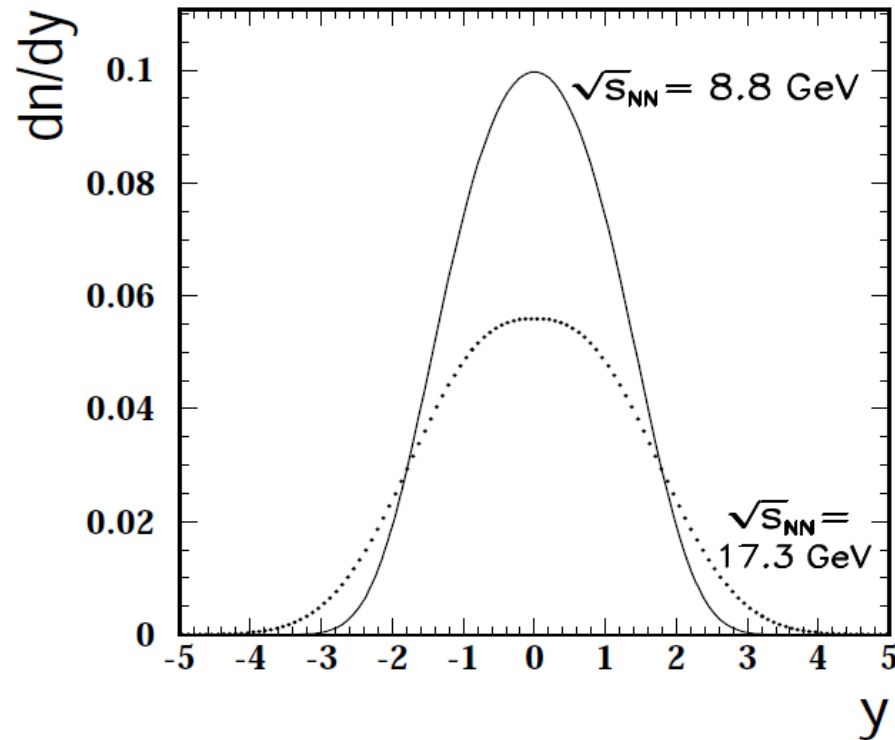
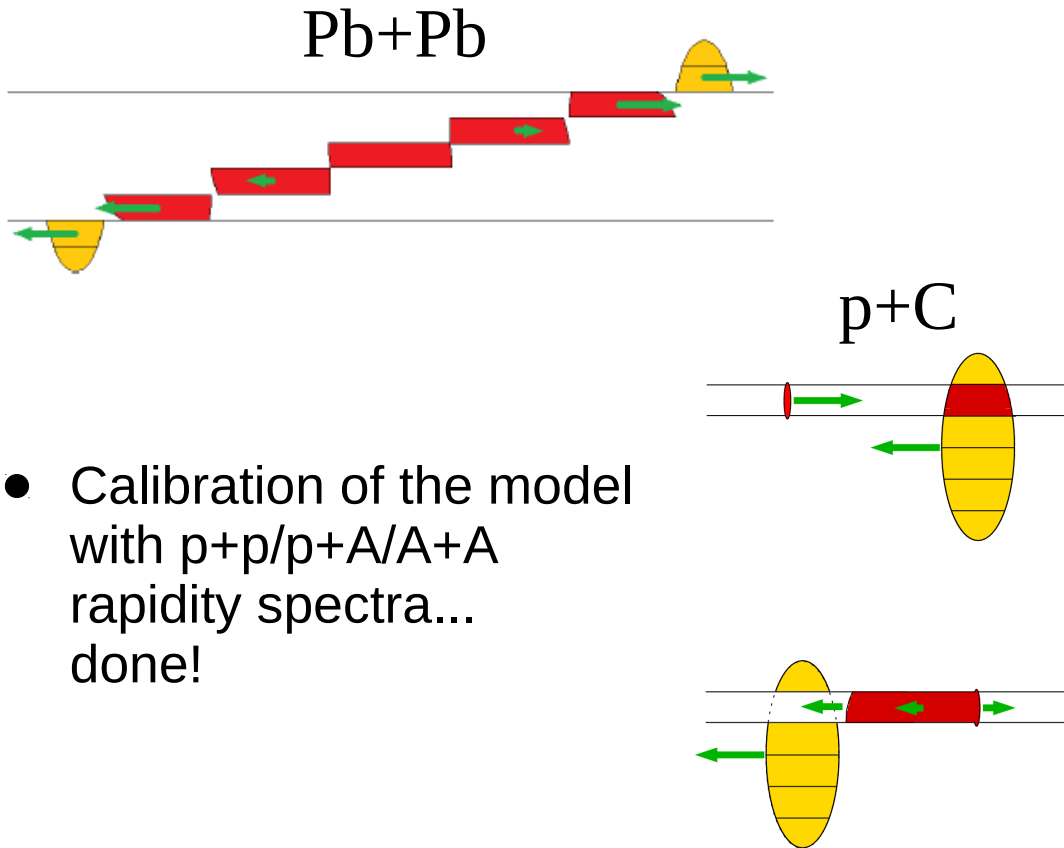
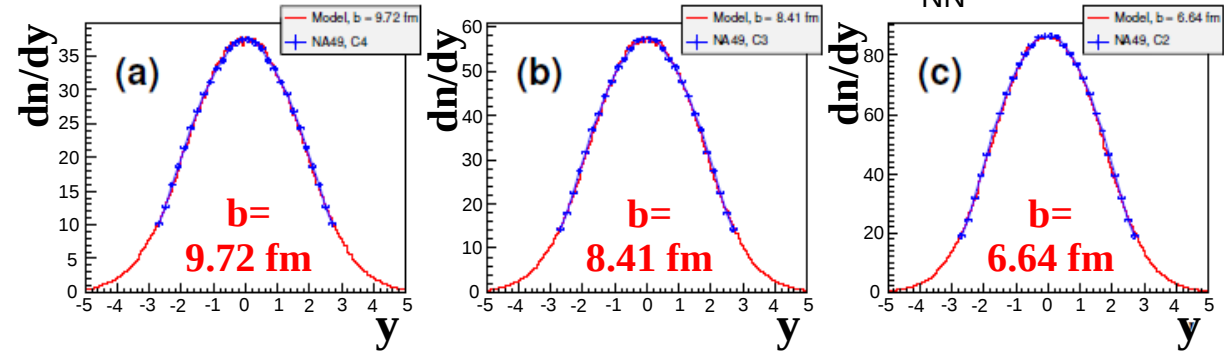


FIG. 7:

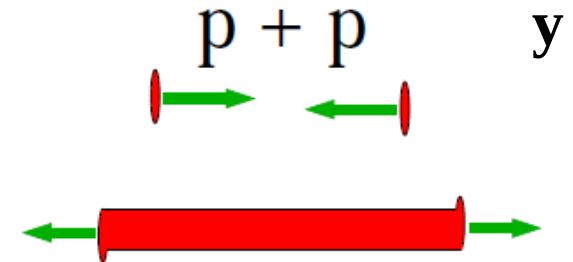
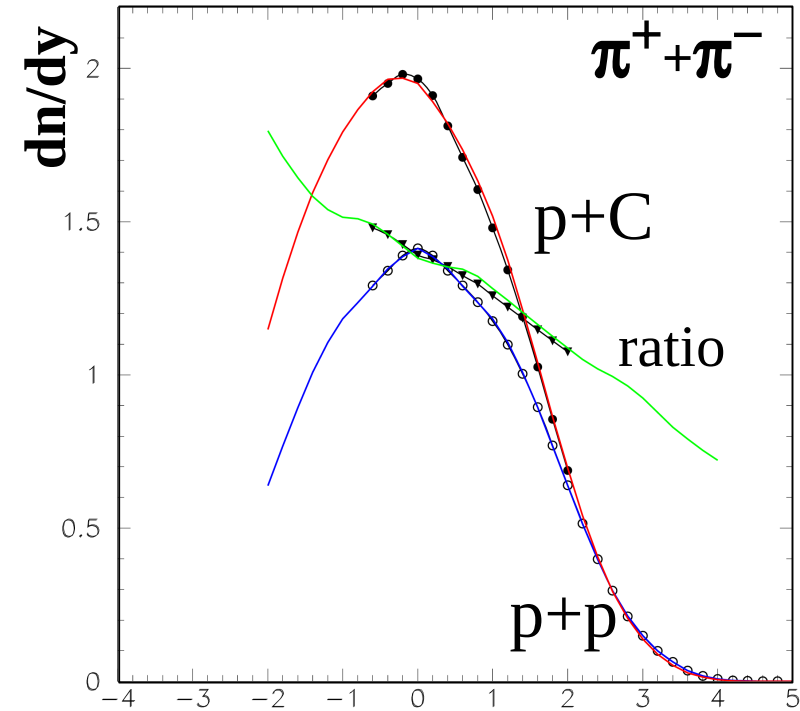
Comparison of single fire-streak fragmentation functions used for the description of π^- rapidity distributions in Pb+Pb collisions at $\sqrt{s_{NN}} = 8.8$ GeV (solid) and at $\sqrt{s_{NN}} = 17.3$ GeV (dotted).

The two presented functions are given by Eq. (2.1) with $(E_s^* - m_s) \equiv 1$ GeV. The numerical values of the function parameters are given in the text.

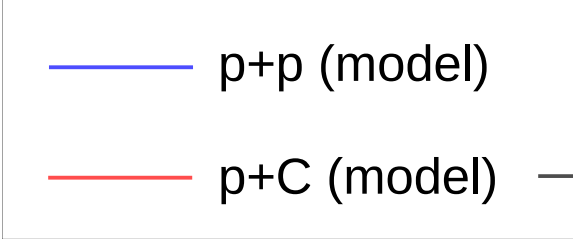
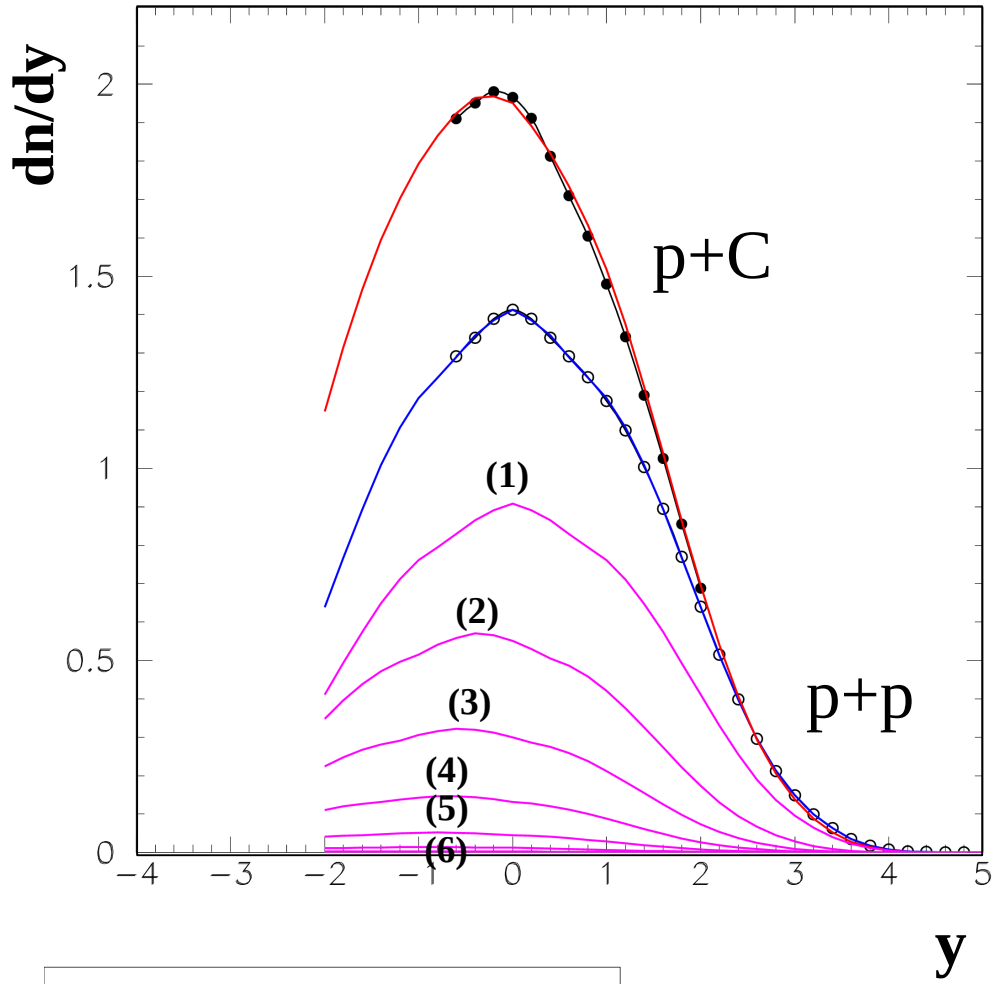
- Link between p+p, p+A, and A+A collisions.



- Calibration of the model with p+p/p+A/A+A rapidity spectra... done!



$\pi^+ + \pi^-$, $\sqrt{s_{NN}} = 17.3$ GeV



Energy balance:
change in energy spent on pions by **+13 %** w.r.t. p+p, can be explained by baryon stopping.

