

TOP PRECISION FOR THE ASSOCIATED TOP-PAIR PRODUCTION AT THE LHC

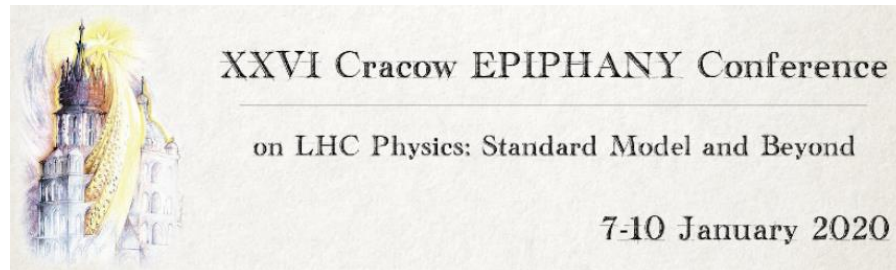
ANNA KULESZA
UNIVERSITY OF MÜNSTER

IN COLLABORATION WITH
L. MOTYKA, D. SCHWARTLÄNDER, T. STEBEL AND V. THEEUWES



WESTFÄLISCHE
WILHELMS-UNIVERSITÄT
MÜNSTER

DFG Deutsche
Forschungsgemeinschaft



TOP AT 25 !

VOLUME 74, NUMBER 14

PHYSICAL REVIEW LETTERS

3 APRIL 1995

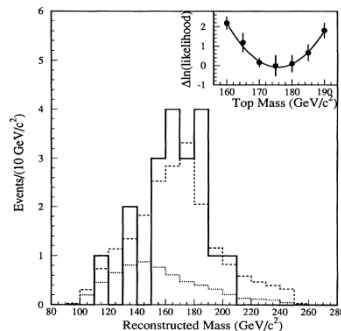
Observation of Top Quark Production in $p\bar{p}$ Collisions with the Collider Detector at Fermilab

F. Abe,¹⁴ H. Akimoto,³² A. Akopian,²⁷ M. G. Albrow,⁷ S. R. Amendolia,²⁴ D. Amidei,¹⁷ J. Antos,²⁹ C. Anway-Wiese,⁴

(Received 24 February 1995)

We establish the existence of the top quark using a 67 pb^{-1} data sample of $p\bar{p}$ collisions at $\sqrt{s} = 1.8 \text{ TeV}$ collected with the Collider Detector at Fermilab (CDF). Employing techniques similar to those we previously published, we observe a signal consistent with $t\bar{t}$ decay to $Wb\bar{b}$, but inconsistent with the background prediction by 4.8σ . Additional evidence for the top quark is provided by a peak in the reconstructed mass distribution. We measure the top quark mass to be $176 \pm 8(\text{stat}) \pm 10(\text{syst}) \text{ GeV}/c^2$, and the $t\bar{t}$ production cross section to be $6.8^{+3.6}_{-2.4} \text{ pb}$.

PACS numbers: 14.65.Ha, 13.85.Qk, 13.85.Ni



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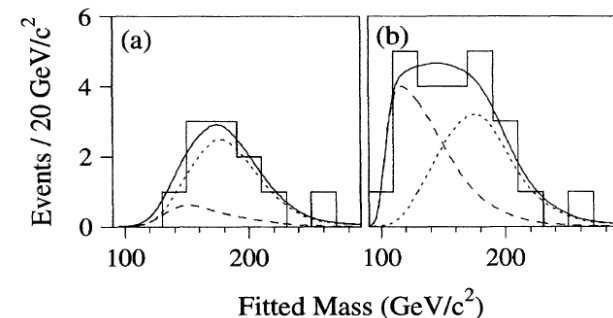
3 APRIL 1995

Observation of the Top Quark

S. Abachi,¹² B. Abbott,³³ M. Abolins,²³ B. S. Acharya,⁴⁰ I. Adam,¹⁰ D. L. Adams,³⁴ M. Adams,¹⁵ S. Ahn,¹² H. Aihara,²⁰ I. Aliri,³⁶ G. Alvarez,¹⁶ G. A. Alves,⁸ F. Amili,²⁷ N. Amos,²² F. W. Anderson,¹⁷ S. H. Aronson,³ R. Astur,³⁸ R. F.

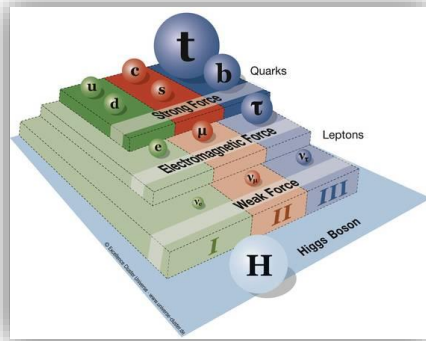
(Received 24 February 1995)

The D0 Collaboration reports on a search for the standard model top quark in $p\bar{p}$ collisions at $\sqrt{s} = 1.8 \text{ TeV}$ at the Fermilab Tevatron with an integrated luminosity of approximately 50 pb^{-1} . We have searched for $t\bar{t}$ production in the dilepton and single-lepton decay channels with and without tagging of b -quark jets. We observed 17 events with an expected background of 3.8 ± 0.6 events. The probability for an upward fluctuation of the background to produce the observed signal is 2×10^{-6} (equivalent to 4.6 standard deviations). The kinematic properties of the excess events are consistent with top quark decay. We conclude that we have observed the top quark and measured its mass to be $199^{+19}_{-21}(\text{stat}) \pm 22(\text{syst}) \text{ GeV}/c^2$ and its production cross section to be $6.4 \pm 2.2 \text{ pb}$.



Since then more than **4300** publications in the INSPIRE database and **275 million** top quarks produced @ the LHC in the Run 2 (139 fb^{-1}) alone !!

TOP IS...

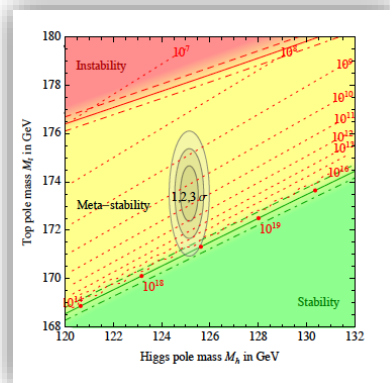


- ... **heavy**. The heaviest particle in the SM.
- ... **short-lived**, hence „bare“. It decays before it can hadronize.

- ... Higgs-friendly. **Large Yukawa coupling** $y_t \sim 1$ of central relevance in Higgs physics.
- ... working behind the scenes. **Top loops** provide important contributions to many observables (e.g. M_H).



- ... consequential. It's mass, together with M_H determines **the stability of the Universe**,
- ... probing the unknown. It offers a unique way to **test the SM and search for BSM**.

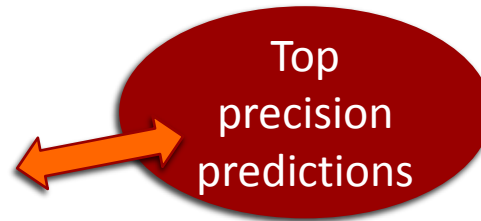


[Buttazzo et al.'13]

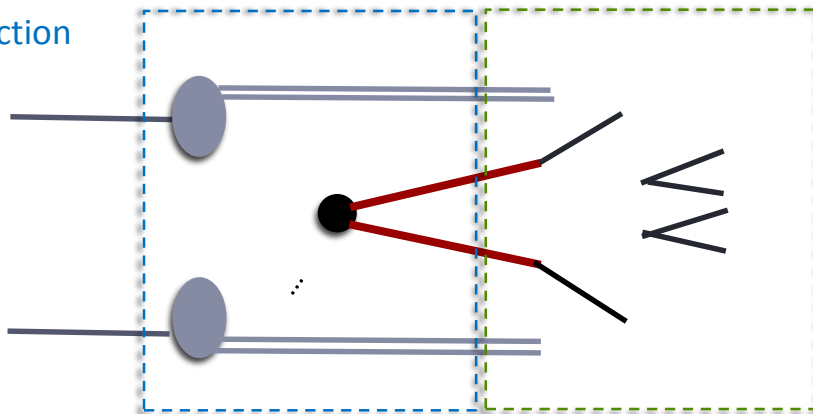
TOP PRECISION

Fixed order perturbation theory

- QCD (N(N)LO)
see R. Poncelet's talk on Friday
- Combined QCD-EW

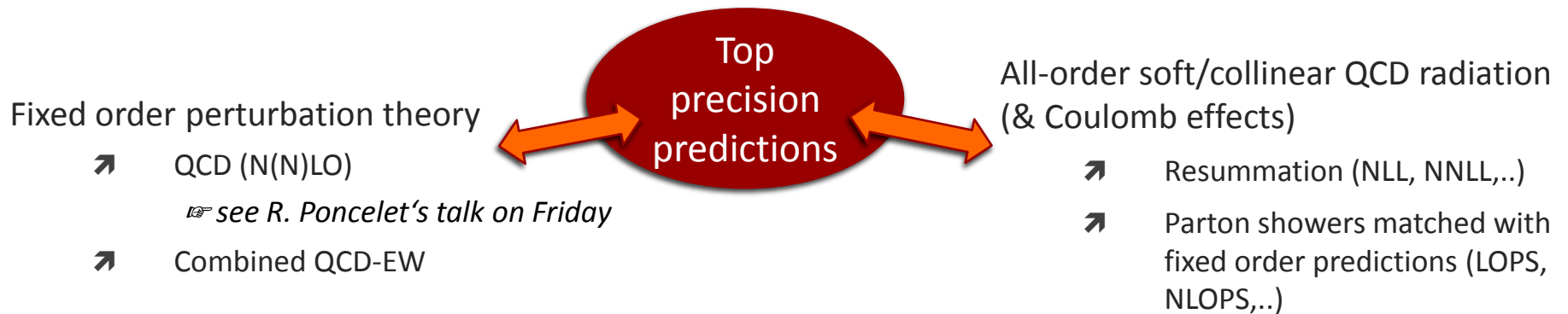


Production

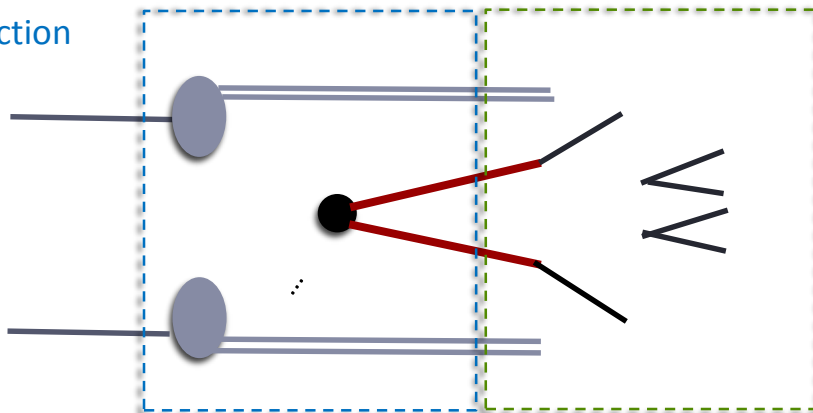


Decay

TOP PRECISION

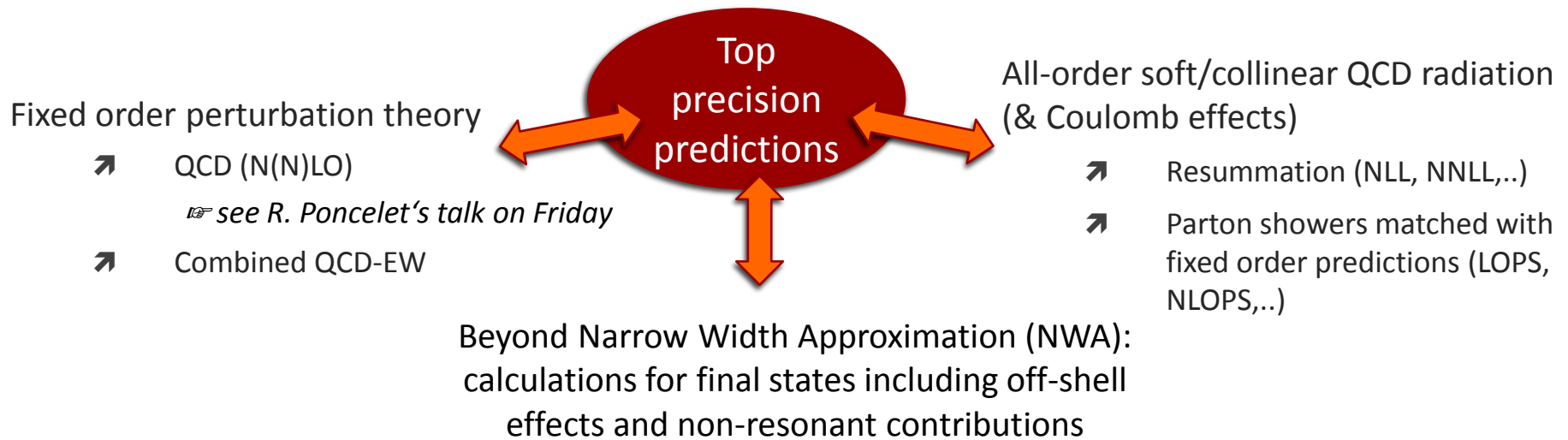


Production

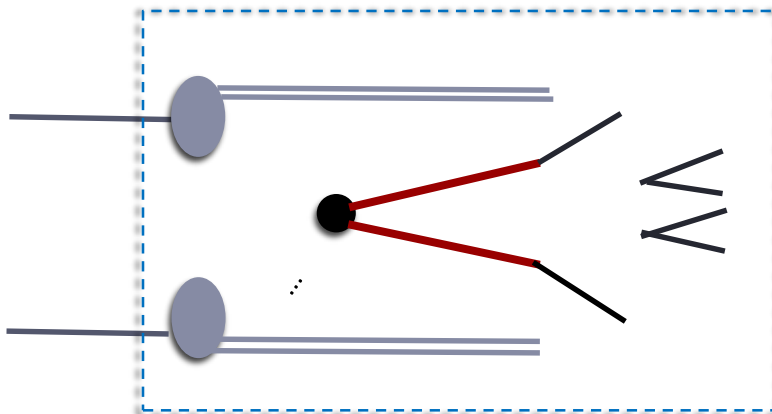


Decay

TOP PRECISION



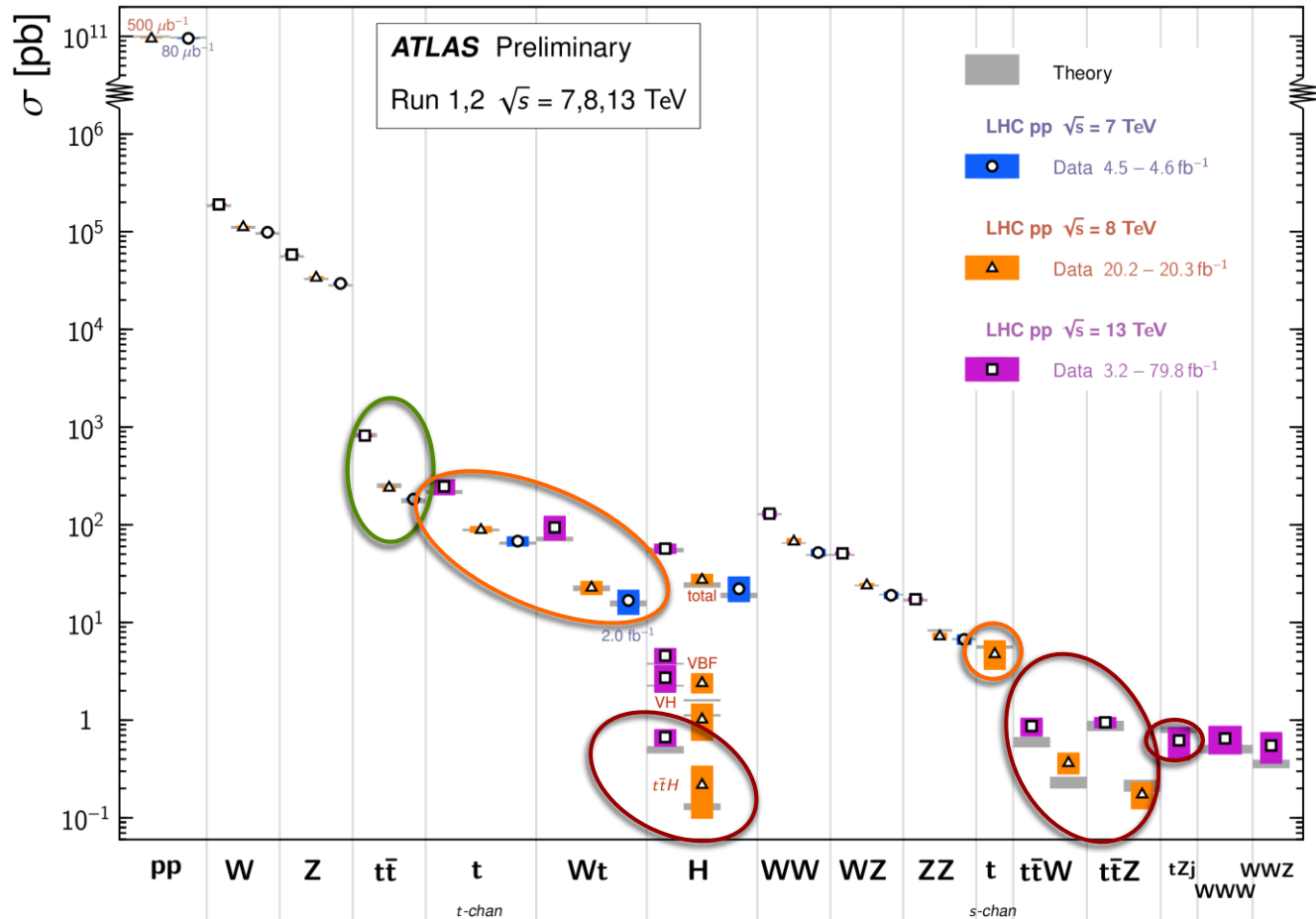
see G. Bevilacqua's talk on Friday



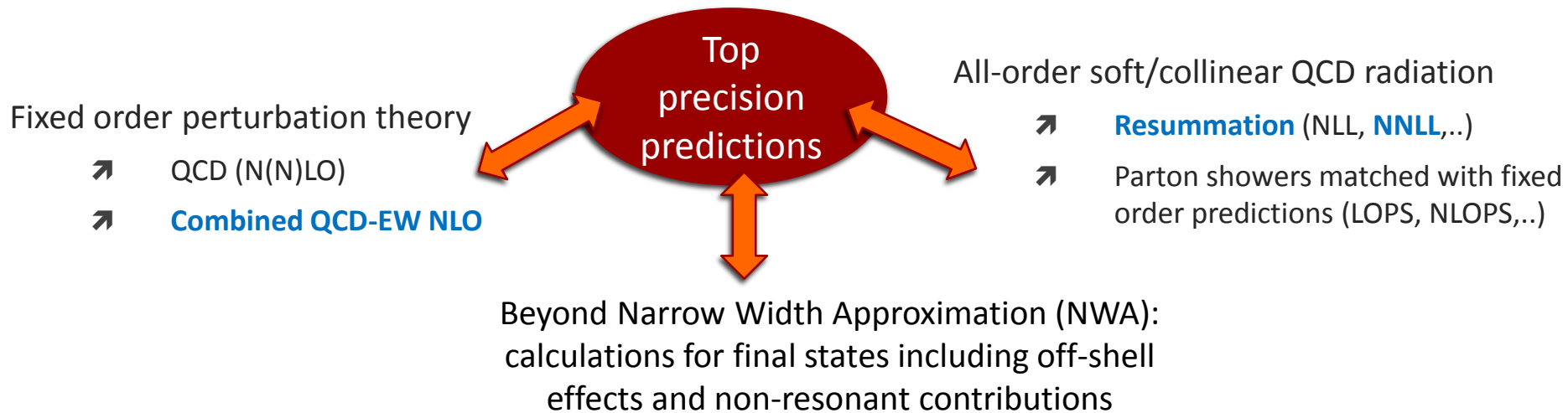
TOPS EN VOGUE

Standard Model Total Production Cross Section Measurements *Status: July 2019*

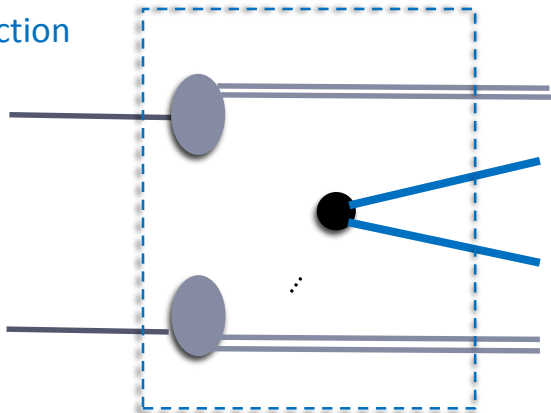
- Top-pairs
- Single top
- Associated production: ttH, ttZ, ttW



TOP PRECISION

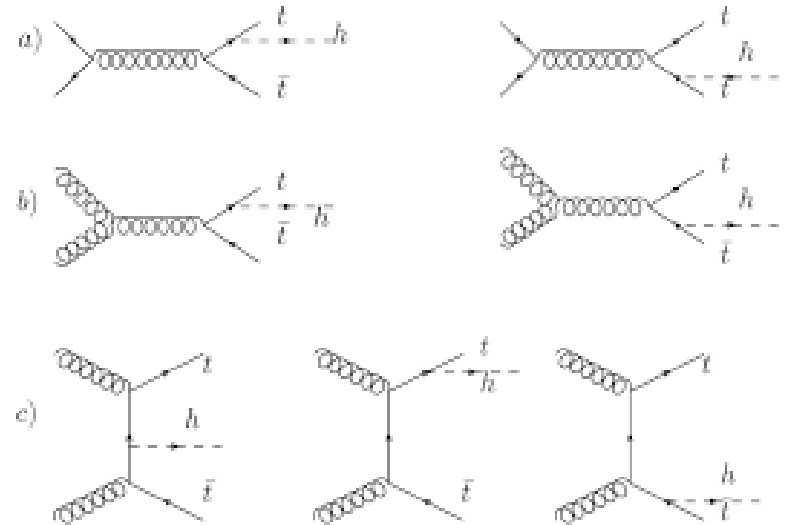


Production



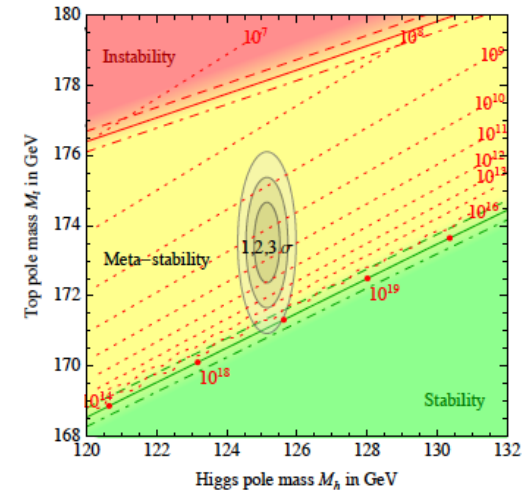
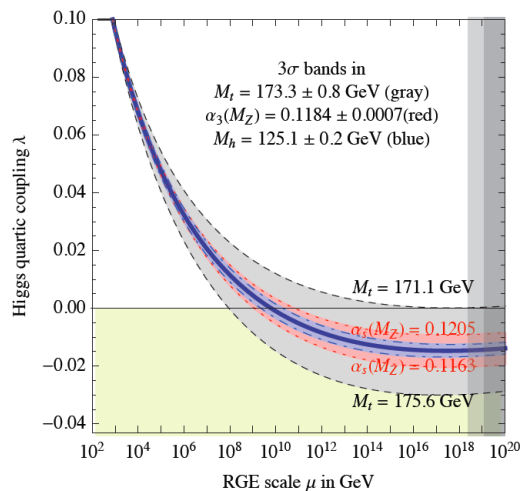
$T\bar{T} + H$

- Direct probe of the strength of the top-Yukawa coupling without making any assumptions regarding its nature



TTBAR+H

- Direct probe of the strength of the top-Yukawa coupling without making any assumptions regarding its nature
- Far-reaching consequences -> **stability of our Universe**



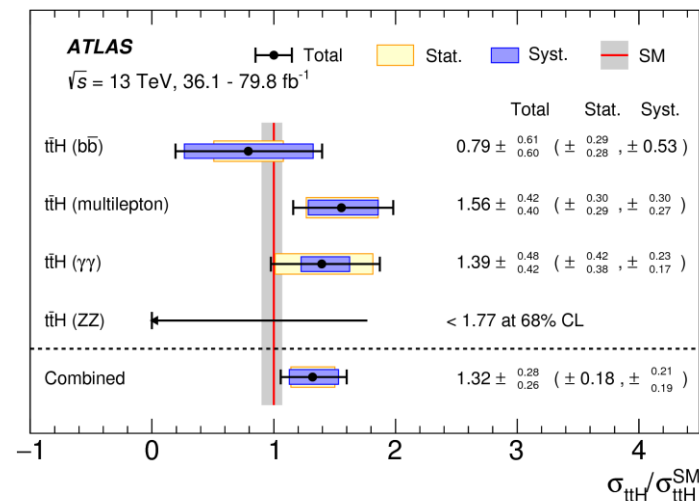
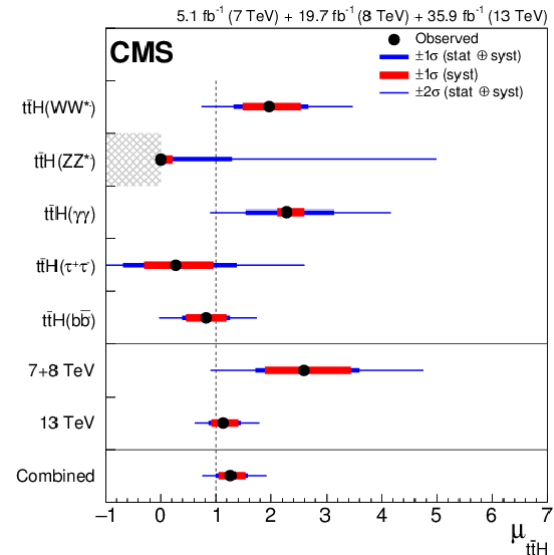
$$V = -\frac{m_H^2}{2}|H|^2 + \lambda|H|^4$$

$$4\rho^2 \frac{d\rho}{d \ln m^2} @ -3y_t^4 + 6/y_t^2 + 12/l^2 + \dots$$

[Buttazzo et al.'13]

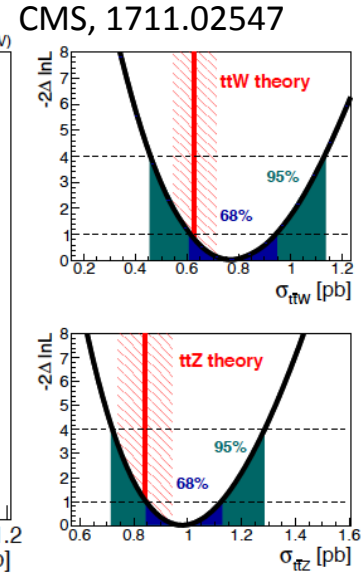
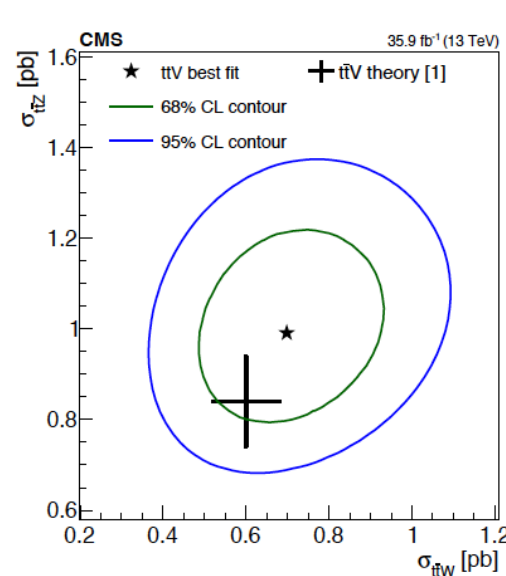
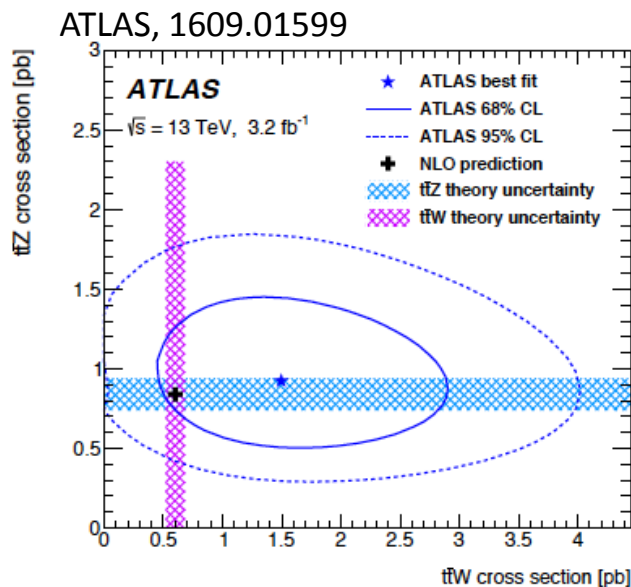
TTBAR+H

- Direct probe of the strength of the top-Yukawa coupling without making any assumptions regarding its nature
- Far-reaching consequences -> stability of our Universe
- **Fundamental Yukawa interactions probed** only very recently (2018)
- Small cross section $\sigma \approx 500 \text{ fb}$ @13 TeV
 - need advanced **experimental techniques**
 - **precise theory for signal and background**



TTBAR+W,Z

- Probes of top-quark couplings
- Sensitive to BSM contributions
- Dominant backgrounds to searches and SM precision measurements ($t\bar{t}H$ included)



- Signal strength (CMS, 1907.11270) $\sigma(pp \rightarrow t\bar{t}Z) = 0.95 \pm 0.05 \text{ (stat)} \pm 0.06 \text{ (syst)} \text{ pb}$
- Measurement of the transverse momentum distribution of the Z boson (CMS, 1907.11270)

THEORY STATUS: $tt\bar{b}RH$ AT FIXED ORDER

- **NLO QCD** available since (almost) 20 years [*Beenakker, Dittmaier, Krämer, Plumper, Spira, Zerwas '01-'02*][*Reina, Dawson'01*][*Reina, Dawson, Wackerath'02*][*Dawson, Orr, Reina, Wackerath'03*] [*Dawson, Jackson, Orr, Reina, Wackerath'03*]
- **NLO QCD matched with parton showers**
 - POWHEG-Box [*Garzelli, Kardos, Papadopoulos, Trocsanyi'11*] [*Hartanto, Jäger, Reina, Wackerath'15*]
 - aMC@NLO [*Frederix, Frixione, Hirschi, Maltoni, Pittau, Torrielli'11*]
 - SHERPA+RECOLA [*Biedermann et al.'17*]
- **QCD and EW@NLO** [*Frixione, Hirschi, Pagani, Shao, Zaro'14-'15*][*Zhang, Ma, Zhang, Chen, Guo'14*][*Biedermann, Bräuer, Denner, Pellen, Schumann, Thompson'17*]
- **NLO QCD** [*Denner, Feger'15*] **and EW** [*Denner, Lang, Pellen, Uccirati'16*] **with tops off-shell**
 - Top decays into b quarks and leptons: $pp \rightarrow ttH \rightarrow W^+W^-bbH \rightarrow e^+v_e \mu^-v_\mu bb H$
 - All resonant, non-resonant, interference and off-shell effects included

THEORY STATUS: $TT\bar{B}+W,Z$ AT FIXED ORDER

- **NLO QCD** [*Lazopoulos, Melnikov, Petriello'07*] [*Lazopoulos, McElmurry, Melnikov, Petriello'08*] [*Kardos, Trocsanyi, Papadopoulos'12*] with decays at NLO [*Campbell, Ellis'12*][*Roentsch, Schulze'14-'15*]
- **NLO interfaced to parton showers** in aMC@NLO [*Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattalaer, Shao Stelzer, Torrieli, Zaro,'14*] [*Maltoni, Mangano, Tsinikos, Zaro,'14*] [*Maltoni, Pagani, Tsinikos'15*] and POWHEG-Box [*Garzelli, Kardos, Papadopoulos, Trocsanyi'12*]
- **EW corrections** [*Frixione, Hirschi, Pagani, Shao, Zaro'14-15*][*Frederix, Pagani, Zaro'18*]

THEORY STATUS: $t\bar{t}W,Z$ AT FIXED ORDER

- **NLO QCD** [Lazopoulos, Melnikov, Petriello'07] [Lazopoulos, McElmurry, Melnikov, Petriello'08] [Kardos, Trocsanyi, Papadopoulos'12] with decays at NLO [Campbell, Ellis'12][Roentsch, Schulze'14-'15]
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From LHC HXSWG Report 4:

Process	\sqrt{s}	$\sigma_{\text{QCD}}^{\text{NLO}}$	$\sigma_{\text{QCD+EW}}^{\text{NLO}}$	K_{QCD}	$\delta_{\text{EW}}[\%]$	Scale[%]		PDF[%]		$\alpha_S[\%]$	
$t\bar{t}Z$	13	841.3(1.6)	839.3(1.6)	1.39	-0.2	+9.6%	-11.3%	+2.8%	-2.8%	+2.8%	-2.8%

THEORY STATUS: $t\bar{t}W, Z$ AT FIXED ORDER

- **NLO QCD** [Lazopoulos, Melnikov, Petriello'07] [Lazopoulos, McElmurry, Melnikov, Petriello'08] [Kardos, Trocsanyi, Papadopoulos'12] with decays at NLO [Campbell, Ellis'12][Roentsch, Schulze'14-'15]
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$t\bar{t}Z$	13	841.3(1.6)	839.3(1.6)	1.39	-0.2	+9.6%	-11.3%	+2.8%	-2.8%	+2.8%	-2.8%

From CMS, 1907.11270 (13 TeV, 77.5 fb^{-1}):

$$\sigma(\text{pp} \rightarrow t\bar{t}Z) = 0.95 \pm 0.05(\text{stat}) \pm 0.06(\text{syst}) \text{ pb}$$

$$\pm 5.3\%(\text{stat}) \pm 6.3\%(\text{syst})$$



BEYOND NLO QCD: THRESHOLD RESUMMATION

- **ttH : NLL+NLO resummation in the absolute threshold limit**, $\hat{s} \rightarrow M^2 = (m_t + m_{\bar{t}} + m_B)^2$ obtained using direct QCD approach [AK, Motyka, Stebel, Theeuwes'15]
- **ttH : NLL+NLO soft gluon and Coulomb resummation in the absolute threshold limit in SCET** [Ju and Yang'19]
- **ttH : "Approximated" NNLO** based on the SCET approach to resummation **in the invariant mass limit**, $\hat{s} \rightarrow Q^2 = (p_t + p_{\bar{t}} + p_B)^2$ [Broggio, Ferroglia, Pecjak, Signer, Yang'15]
- **ttH : NLL+NLO in the invariant mass limit for production with pseudoscalar Yukawa couplings** [Broggio, Ferroglia, Fiolhais, Onofre'17]
- **ttW : NNLL+NLO resummation in the invariant mass limit, SCET** [Li, Li, Li'14]
- **ttH, ttW, ttZ : NNLL+NLO resummation in the invariant mass limit, hybrid SCET/direct QCD method** [Broggio, Ferroglia, Ossola, Pecjak'16] [Broggio, Ferroglia, Pecjak, Yang'16] [Broggio, Ferroglia, Ossola, Pecjak, Samoshima'17] [Broggio et al. 19]
- **ttH, ttW, ttZ : NNLL+NLO QCD (+EW) resummation in the invariant mass limit, direct QCD method** [AK, Motyka, Stebel, Theeuwes'16], [AK, Motyka, Stebel, Theeuwes'17], [AK, Motyka, Schwartländer, Stebel, Theeuwes'18-'19]

RESUMMATION FOR $T\bar{T}B\bar{A}R+B$ ($B=H,Z,W$)

- Threshold limit in the invariant mass kinematics: $\hat{s} \rightarrow Q^2 = (p_t + p_{\bar{t}} + p_B)^2$
- Large logarithmic contributions of the form $\alpha_s^n \left(\frac{\log^m(1-\hat{\rho})}{1-\hat{\rho}} \right)_+$; $\hat{\rho} = Q^2/\hat{s}$; $m \leq 2n - 1$

- Direct QCD $\rightarrow N$ space:

$$\frac{d\tilde{\sigma}_{ij \rightarrow klB}}{dQ^2}(N, Q^2, \{m^2\}, \mu_F^2, \mu_R^2) = \int_0^1 d\hat{\rho} \hat{\rho}^{N-1} \frac{d\hat{\sigma}_{ij \rightarrow klB}}{dQ^2}(\hat{\rho}, Q^2, \{m^2\}, \mu_F^2, \mu_R^2)$$

- In Mellin space, logarithms of $1 - \hat{\rho}$ become logarithms of Mellin moments N
- Resummation

$$\hat{\sigma}^{(N)} \sim \mathcal{C}(\alpha_s) \exp [Lg_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \dots]$$

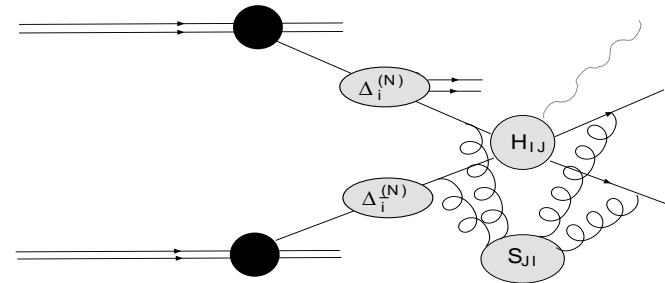
LL: $\alpha_s^n \log^{n+1}(N)$

NLL: $\alpha_s^n \log^n(N)$

NNLL: $\alpha_s^n \log^{n-1}(N)$

RESUMMATION FOR $\overline{TT} + B$ ($B=H,Z,W$)

- Resummation \leftrightarrow all-order factorization of soft and collinear emissions
- Exponentiation \leftrightarrow solutions of RGEs



$$\frac{d\tilde{\sigma}_{ij \rightarrow klB}^{(\text{res})}}{dQ^2}(N, Q^2, \{m^2\}, \mu_F^2, \mu_R^2) =$$

$$= \text{Tr} \left[\underbrace{\mathbf{H}_{ij \rightarrow klB}(Q^2, \{m^2\}, \mu_F^2, \mu_R^2)}_{\text{Hard off-shell}} \underbrace{\mathbf{S}_{ij \rightarrow klB}(N+1, Q^2, \{m^2\}, \mu_F^2, \mu_R^2)}_{\text{Soft wide-angle}} \right] \underbrace{\Delta^i(N+1, Q^2, \mu_F^2, \mu_R^2)}_{\text{Collinear}} \Delta^j(N+1, Q^2, \mu_F^2, \mu_R^2)$$

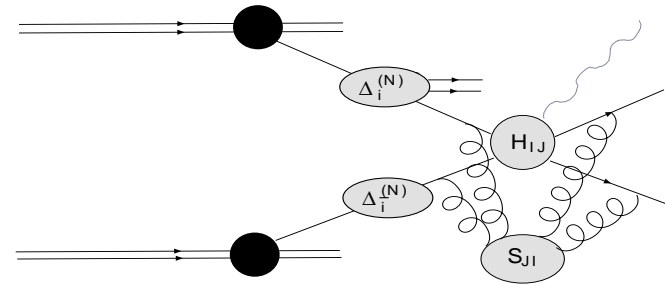
Process-dependent
Universal, known
✓

[Kodaira, Trentadue'82-'83][Catani, d'Emilio, Trentadue'88][Sterman'87][Moch, Vermaseren, Vogt'04]

Processes with four or more legs carrying colour: hard and soft functions are matrices in colour space

RESUMMATION FOR $TT\bar{B}+B$ ($B=H,Z,W$)

- Resummation \leftrightarrow all-order factorization of soft and collinear emissions
- Exponentiation \leftrightarrow solutions of RGEs



$$\frac{d\tilde{\sigma}_{ij\rightarrow klB}^{(\text{res})}}{dQ^2}(N, Q^2, \{m^2\}, \mu_F^2, \mu_R^2) =$$

$$= \text{Tr} \left[\underbrace{\mathbf{H}_{ij\rightarrow klB}(Q^2, \{m^2\}, \mu_F^2, \mu_R^2)}_{\text{Hard off-shell}} \underbrace{\mathbf{S}_{ij\rightarrow klB}(N+1, Q^2, \{m^2\}, \mu_F^2, \mu_R^2)}_{\text{Soft wide-angle}} \right] \underbrace{\Delta^i(N+1, Q^2, \mu_F^2, \mu_R^2) \Delta^j(N+1, Q^2, \mu_F^2, \mu_R^2)}_{\text{Collinear}}$$

Process-dependent
Universal, known
✓

[Kodaira, Trentadue'82-'83][Catani, d'Emilio, Trentadue'88][Sterman'87][Moch, Vermaseren, Vogt'04]

$\rightarrow \mathbf{H}^{(1)}$ extracted from aMC@NLO [Frederix, Frixione, Hirschi, Maltoni, Pittau, Torrielli'11] (ttH , ttW , ttZ) and PowHel (HELAC-NLO [Bevilacqua et al.'11] +POWHEG-Box) package [Garzelli, Kardos, Papadopoulos, Trocksanyi'11] (ttH)

RESUMMATION-IMPROVED NNLL+NLO TOTAL CROSS SECTION

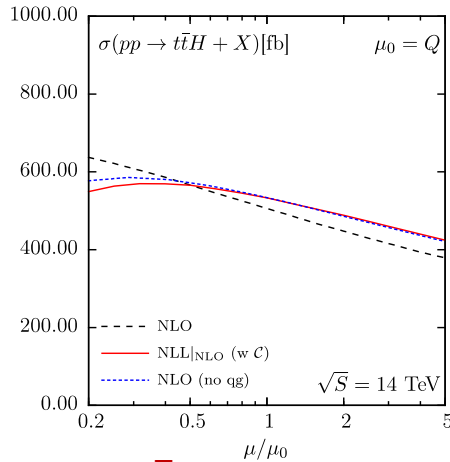
- NNLL resummed expression has to be matched with the full NLO (QCD+EW) result

$$\begin{aligned}
 \sigma_{h_1 h_2 \rightarrow kl}^{(\text{match})}(\rho, \{m^2\}, \mu^2) &= \sum_{i,j=q,\bar{q},g} \int_{C_{MP}-i\infty}^{C_{MP}+i\infty} \frac{dN}{2\pi i} \rho^{-N} f_{i/h_1}^{(N+1)}(\mu^2) f_{j/h_2}^{(N+1)}(\mu^2) \\
 &\times \left[\hat{\sigma}_{ij \rightarrow kl}^{(\text{res},N)}(\{m^2\}, \mu^2) - \hat{\sigma}_{ij \rightarrow kl}^{(\text{res},N)}(\{m^2\}, \mu^2) \Big|_{NLO\ QCD} \right] \\
 &+ \sigma_{h_1 h_2 \rightarrow kl}^{NLO\ QCD + EW}(\rho, \{m^2\}, \mu^2),
 \end{aligned}$$

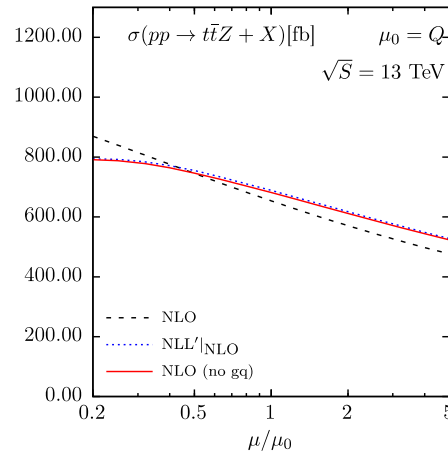
- Inverse Mellin transform evaluated using a contour in the complex N space according to 'Minimal Prescription' [Catani, Mangano, Nason Trentadue'96]
- NLO QCD+EW result obtained from MadGraph5_aMC@NLO [Frederix, Frixione, Hirschi, Pagani, Zaro'18] using LUXqed17_plus_PDF4LHC15_nnlo_100 pdfs, contains all mixed $\alpha^n \alpha_s^m$ terms

NLO vs. NLL_|NLO

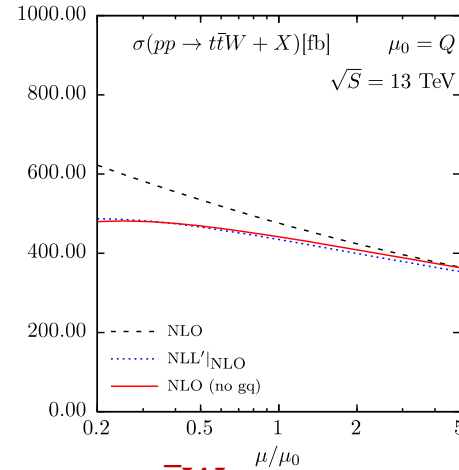
[AK, Motyka, Stebel, Theeuwes'17][AK, Motyka, Schwartländer, Stebel, Theeuwes'18]



$t\bar{t}H$



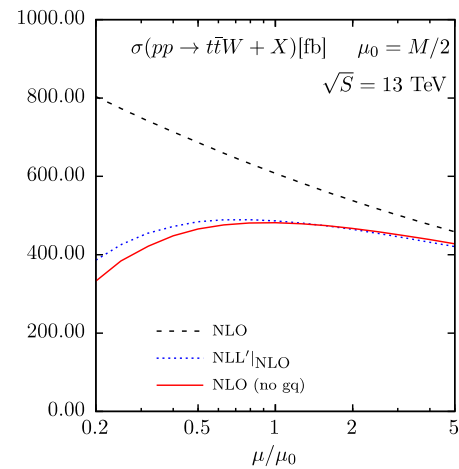
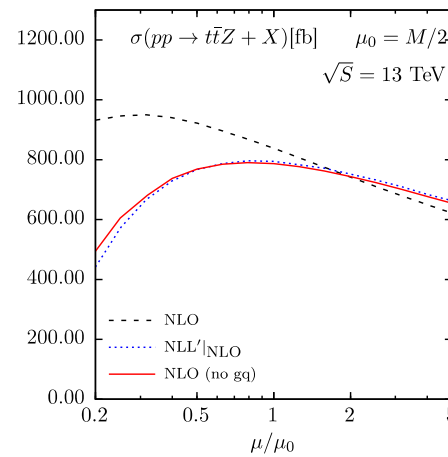
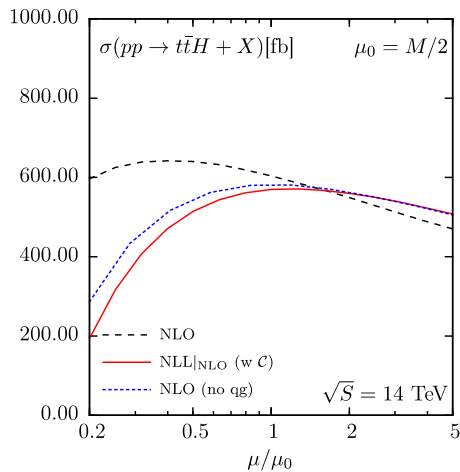
$t\bar{t}Z$



$t\bar{t}W$

$\mu_0 = Q$

$\mu_F = \mu_R = \mu$



$\mu_0 = \frac{M}{2} = m_t + \frac{M_B}{2}$

TOTAL CROSS SECTION FOR $TT\bar{B}ARH$

[AK, Motyka, Stebel, Theeuwes'17 and to appear]

μ_0	NLO[fb]	NLO+NLL[fb]	NLO+NLL _{wC} [fb]	NLO+NNLL[fb]	K_{NNLL}
Q	$425^{+12.1\%}_{-11.6\%}$	$445^{+10.0\%}_{-9.2\%}$	$489^{+8.4\%}_{-8.5\%}$	$505^{+7.5\%}_{-7.0\%}$	1.19
H_T	$434^{+11.6\%}_{-11.4\%}$	$451^{+9.5\%}_{-8.9\%}$	$491^{+7.9\%}_{-8.2\%}$	$502^{+7.3\%}_{-6.7\%}$	1.16
$Q/2$	$476^{+9.9\%}_{-10.8\%}$	$484^{+8.7\%}_{-8.2\%}$	$503^{+6.2\%}_{-7.3\%}$	$505^{+5.7\%}_{-6.4\%}$	1.06
$H_T/2$	$484^{+8.9\%}_{-10.4\%}$	$490^{+8.4\%}_{-8\%}$	$503^{+5.5\%}_{-6.8\%}$	$502^{+5.4\%}_{-6.1\%}$	1.04
$M/2$	$506^{+6\%}_{-9.3\%}$	$510^{+8.2\%}_{-7.8\%}$	$512^{+5.9\%}_{-6.2\%}$	$510^{+5.6\%}_{-6.1\%}$	1.01

$$K_{\text{NNLL}} = \sigma_{\text{NLO+NNLL}} / \sigma_{\text{NLO}}$$

error from scale variation
using the 7-point method

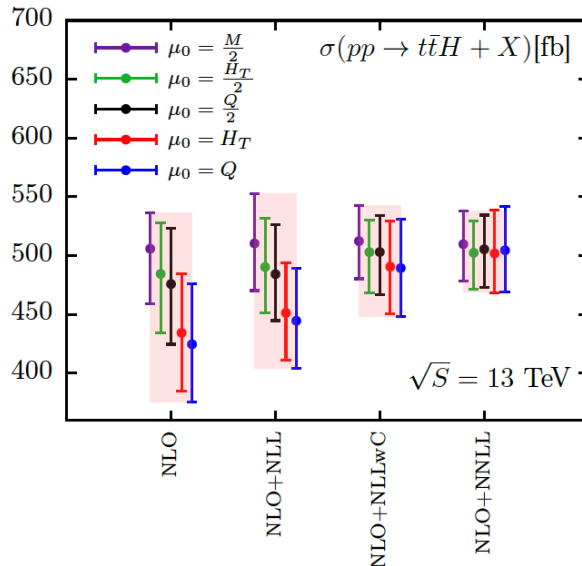
$$\mathbf{H}_R \tilde{\mathbf{S}}_R = \mathbf{H}_R^{(0)} \tilde{\mathbf{S}}_R^{(0)} + \frac{\alpha_s}{\pi} \left[\mathbf{H}_R^{(1)} \tilde{\mathbf{S}}_R^{(0)} + \mathbf{H}_R^{(0)} \tilde{\mathbf{S}}_R^{(1)} \right]$$

TOTAL CROSS SECTION FOR $T\bar{T}B\bar{A}R\bar{H}$

[AK, Motyka, Stebel, Theeuwes'17 and to appear]

μ_0	NLO[fb]	NLO+NLL[fb]	NLO+NLL _{wC} [fb]	NLO+NNLL[fb]	K_{NNLL}
Q	425 ^{+12.1%} _{-11.6%}	445 ^{+10.0%} _{-9.2%}	489 ^{+8.4%} _{-8.5%}	505 ^{+7.5%} _{-7.0%}	1.19
H_T	434 ^{+11.6%} _{-11.4%}	451 ^{+9.5%} _{-8.9%}	491 ^{+7.9%} _{-8.2%}	502 ^{+7.3%} _{-6.7%}	1.16
$Q/2$	476 ^{+9.9%} _{-10.8%}	484 ^{+8.7%} _{-8.2%}	503 ^{+6.2%} _{-7.3%}	505 ^{+5.7%} _{-6.4%}	1.06
$H_T/2$	484 ^{+8.9%} _{-10.4%}	490 ^{+8.4%} _{-8%}	503 ^{+5.5%} _{-6.8%}	502 ^{+5.4%} _{-6.1%}	1.04
$M/2$	506 ^{+6%} _{-9.3%}	510 ^{+8.2%} _{-7.8%}	512 ^{+5.9%} _{-6.2%}	510 ^{+5.6%} _{-6.1%}	1.01

$$K_{\text{NNLL}} = \sigma_{\text{NLO+NNLL}} / \sigma_{\text{NLO}}$$



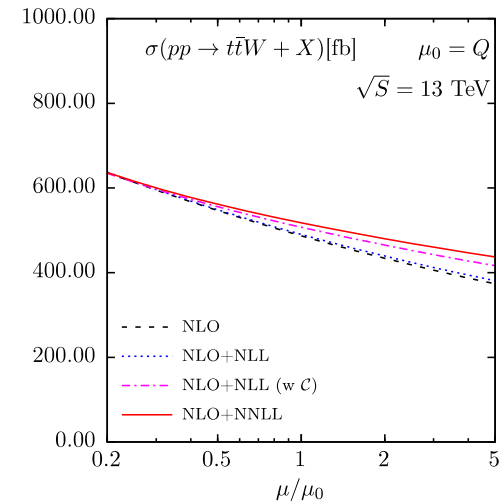
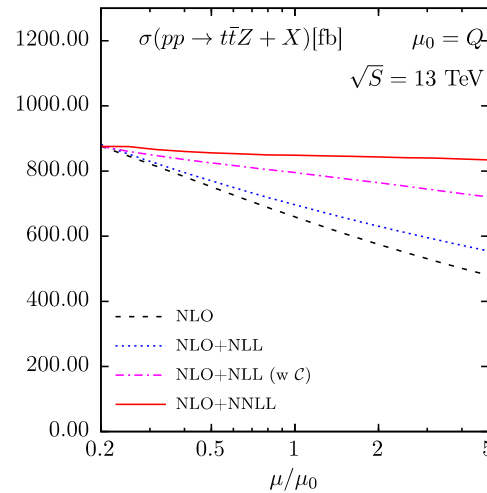
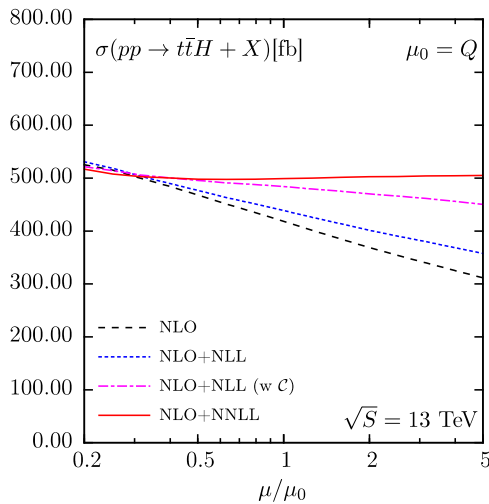
- Compared to NLO, remarkable stability of NLO+NNLL
- Stability improves with increasing accuracy of resummation
- Reduction of the theory scale error
- “Best” (envelope) NNLL+NLO prediction in agreement with NLO QCD+EW at $\mu_0 = M/2$

$$\sigma_{t\bar{t}H}^{\text{NLO+NNLL}} = 504^{+7.6\%+2.4\%}_{-7.1\%-2.4\%} \text{ fb}$$

(± scale) (± pdf)

SCALE DEPENDENCE OF THE TOTAL CROSS SECTION

$$\mu_F = \mu_R = \mu$$



- For $\mu_0 = Q$, decrease in scale dependence with increasing accuracy. NLO+NNLL scale dependence in the $\mu_0/2 - 2\mu_0$ range of order 1%.
- For $\mu_0 = M/2$, mostly similar behaviour

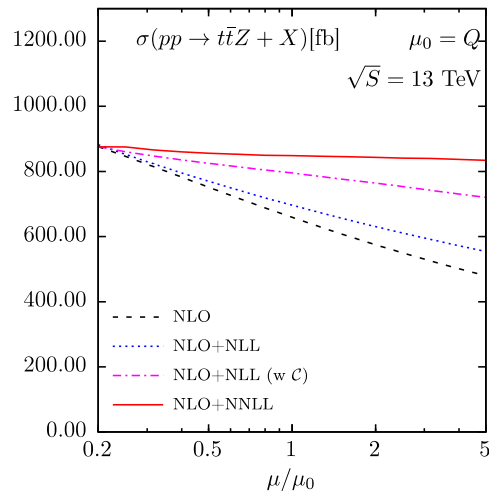
[AK, Motyka, Stebel, Theeuwes'17]

[AK, Motyka, Schwartländer, Stebel, Theeuwes'18]

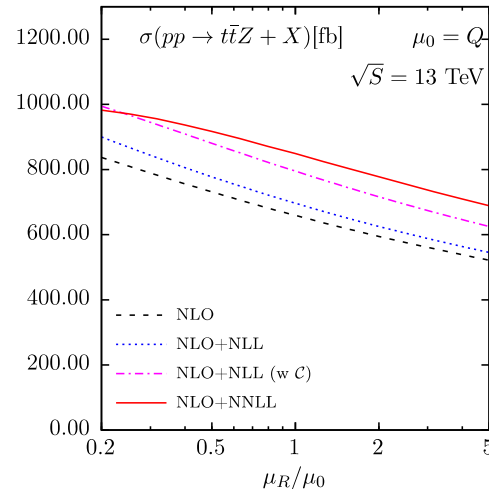
SCALE DEPENDENCE OF THE TOTAL CROSS SECTION

[AK, Motyka, Schwartländer, Stebel, Theeuwes'18]

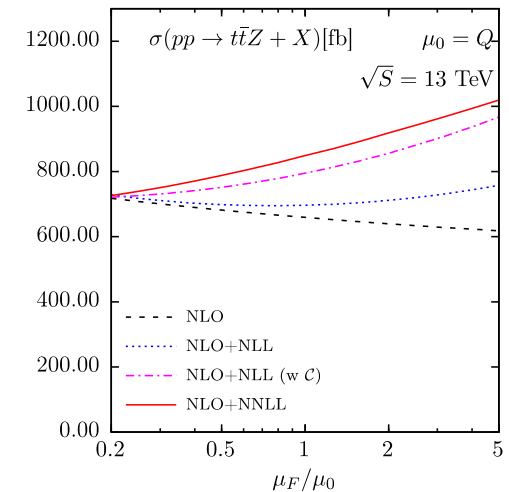
$\mu_F = \mu_R = \mu$ varied



μ_F fixed, μ_R varied



μ_R fixed, μ_F varied



➤ Apparent cancellations between μ_F and μ_R scale dependence → 7-point used for estimation of scale variation error: **conservative scale error estimate**

TOTAL CROSS SECTION FOR $T\bar{T}B\bar{A}R+W,Z$

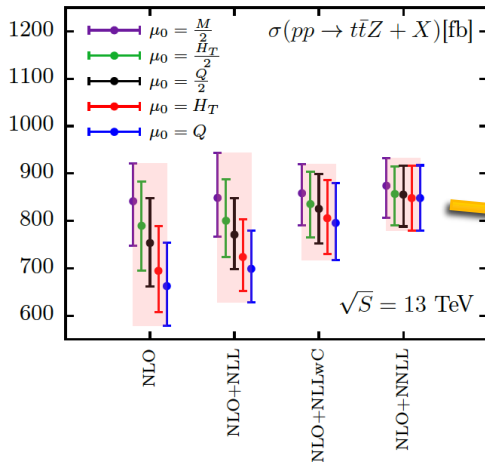
[AK, Motyka, Schwartländer, Stebel, Theeuwes'18 and to appear]

process	μ_0	NLO[fb]	NLO+NLL[fb]	NLO+NLLwC[fb]	NLO+NNLL[fb]	K_{NNLL}
$t\bar{t}Z$	Q	661 ^{+13.8%} _{-12.5%}	698 ^{+11.5%} _{-10.1%}	795 ^{+10.6%} _{-9.7%}	847 ^{+8.1%} _{-8.2%}	1.28
	H_T	694 ^{+13.6%} _{-12.6%}	723 ^{+11.0%} _{-9.8%}	805 ^{+10.0%} _{-9.5%}	848 ^{+7.9%} _{-8.0%}	1.22
	$Q/2$	752 ^{+12.5%} _{-12.1%}	770 ^{+10.6%} _{-9.4%}	824 ^{+8.8%} _{-8.8%}	854 ^{+7.1%} _{-7.8%}	1.14
	$H_T/2$	788 ^{+11.7%} _{-11.9%}	798 ^{+10.7%} _{-9.5%}	834 ^{+8.1%} _{-8.4%}	855 ^{+6.6%} _{-7.7%}	1.09
	$M/2$	841 ^{+9.4%} _{-11.1%}	848 ^{+11.2%} _{-9.7%}	858 ^{+7.1%} _{-7.9%}	874 ^{+6.7%} _{-7.8%}	1.04
$t\bar{t}W$	Q	512 ^{+12.5%} _{-11.1%}	516 ^{+12.1%} _{-10.6%}	533 ^{+9.9%} _{-8.9%}	541 ^{+8.9%} _{-8.4%}	1.06
	H_T	539 ^{+13.0%} _{-11.3%}	542 ^{+12.6%} _{-10.9%}	556 ^{+10.5%} _{-9.0%}	562 ^{+9.6%} _{-8.5%}	1.04
	$Q/2$	577 ^{+12.5%} _{-11.1%}	579 ^{+12.3%} _{-10.8%}	586 ^{+10.7%} _{-9.0%}	590 ^{+10.0%} _{-8.5%}	1.02
	$H_T/2$	609 ^{+13.0%} _{-11.5%}	610 ^{+13%} _{-11.2%}	614 ^{+11.8%} _{-9.5%}	616 ^{+11.2%} _{-8.8%}	1.01
	$M/2$	656 ^{+13.2%} _{-11.7%}	658 ^{+13.6%} _{-11.6%}	657 ^{+13.4%} _{-10.3%}	659 ^{+13.3%} _{-9.8%}	1.00

- Significant reduction in the scale dependence of the $t\bar{t}Z$ total cross section
- Depending on the central scale, correction up to $\sim 30\%$ for the $t\bar{t}Z$ cross section
- Smaller impact on the $t\bar{t}W$ predictions: only $q\bar{q}$ initial channel at LO

TTBAR+W,Z AT NLO+NNLL

[AK, Motyka, Schwartländer, Stebel, Theeuwes'18 and to appear]

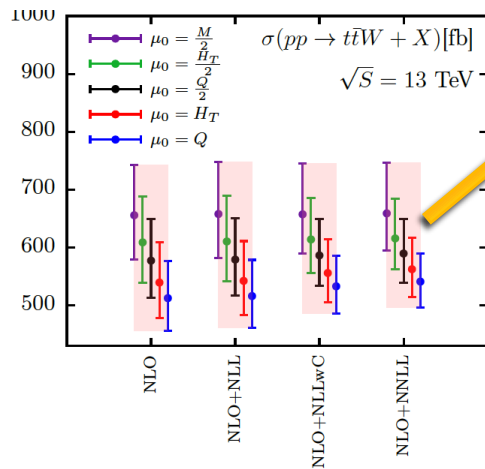


Envelope over results for different central scales

NLO(QCD+EW) +NNLL (\pm scale) (\pm pdf)

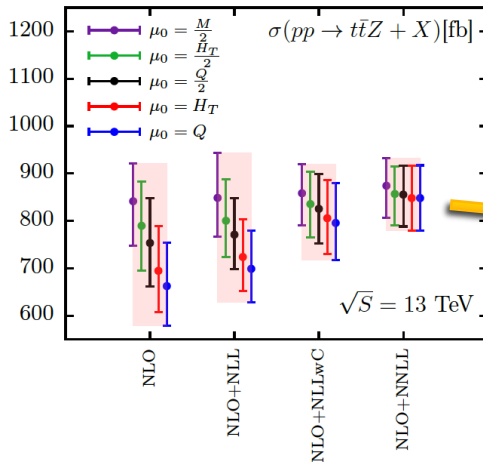
$$\sigma_{t\bar{t}Z}^{\text{NLO+NNLL}} = 859^{+8.6\%+2.3\%}_{-9.5\%-2.3\%} \text{ fb},$$

$$\sigma_{t\bar{t}W}^{\text{NLO+NNLL}} = 592^{+26.1\%+2.1\%}_{-16.2\%-2.1\%} \text{ fb}$$



TTBAR+W,Z AT NLO+NNLL

[AK, Motyka, Schwartländer, Stebel, Theeuwes'18 and to appear]



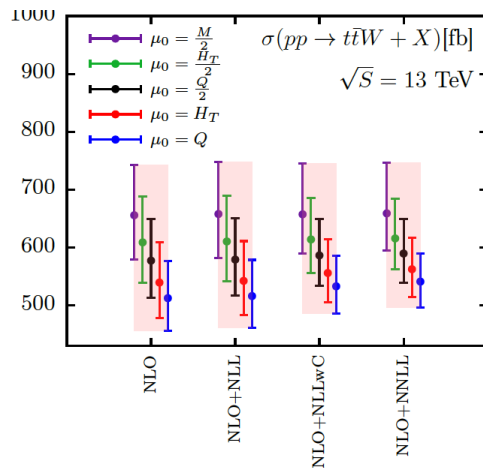
Envelope over results for different central scales

NLO(QCD+EW) +NNLL (\pm scale) (\pm pdf)

$$\sigma_{t\bar{t}Z}^{\text{NLO+NNLL}} = 859^{+8.6\%+2.3\%}_{-9.5\%-2.3\%} = 0.859^{+0.073+0.028}_{-0.085-0.028} \text{ pb}$$

CMS, 1907.11270:

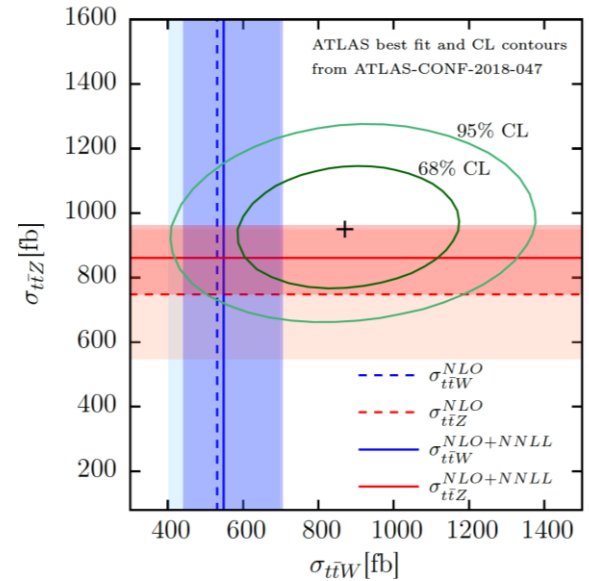
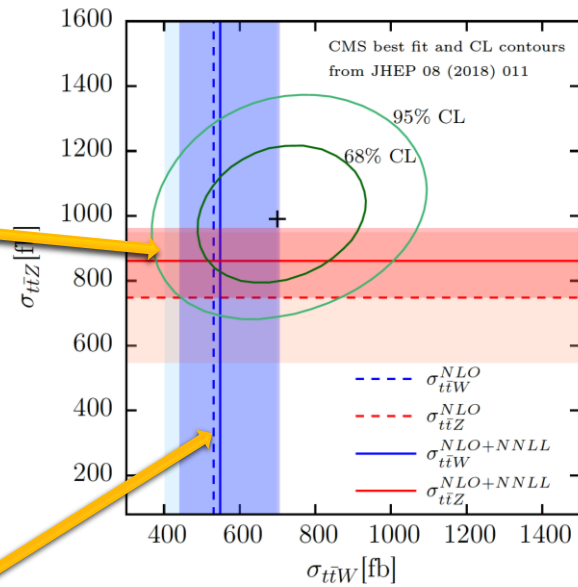
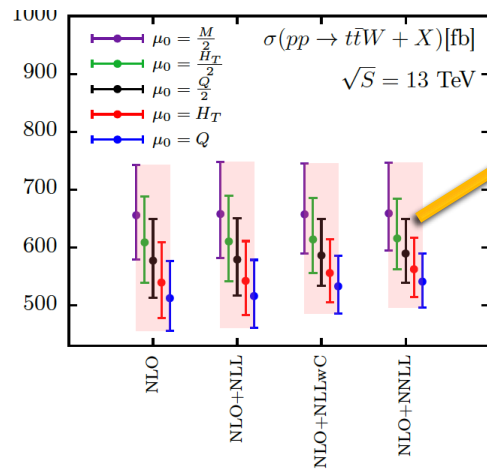
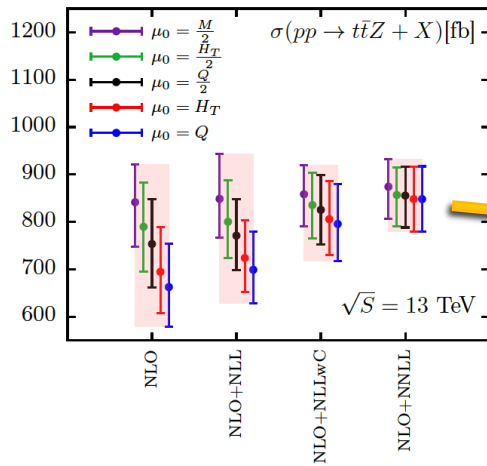
$$\sigma(pp \rightarrow t\bar{t}Z) = 0.95 \pm 0.05 (\text{stat}) \pm 0.06 (\text{syst}) \text{ pb}$$



Accuracy of the NLO+NNLL result
comparable with experimental
precision!

TTBAR+W,Z AT NLO+NNLL

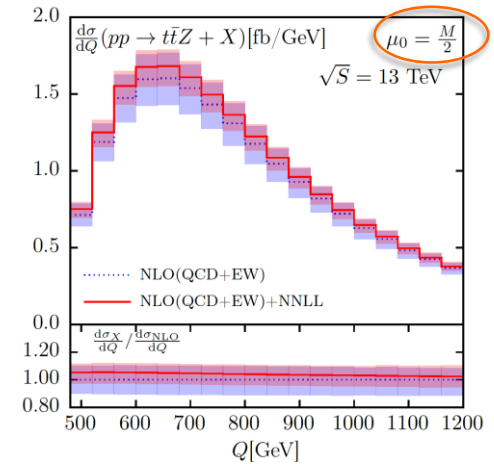
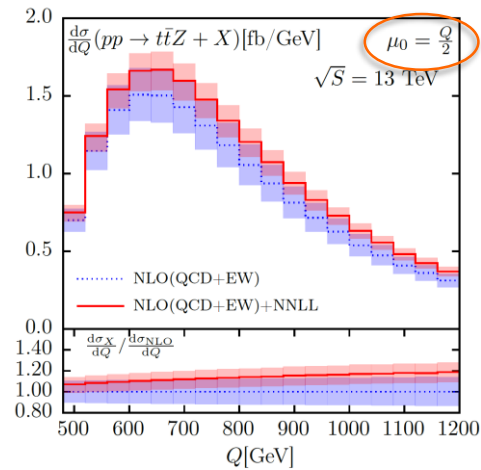
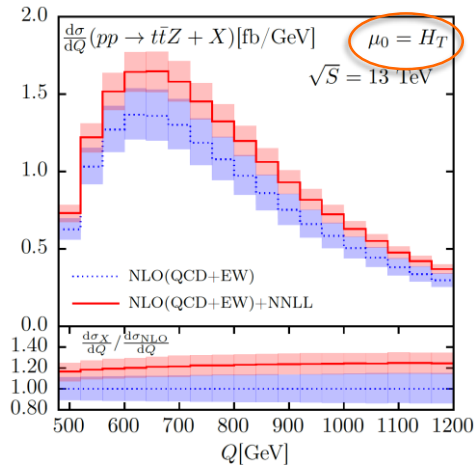
[AK, Motyka, Schwartländer, Stebel, Theeuwes'18 and to appear]



Central values of the theoretical predictions brought closer to the measured cross section; theory errors reduced (by half for ttZ)

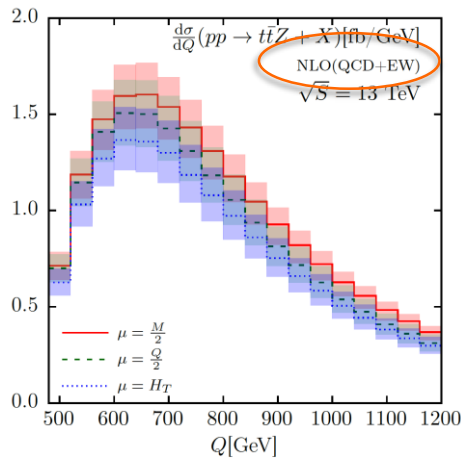
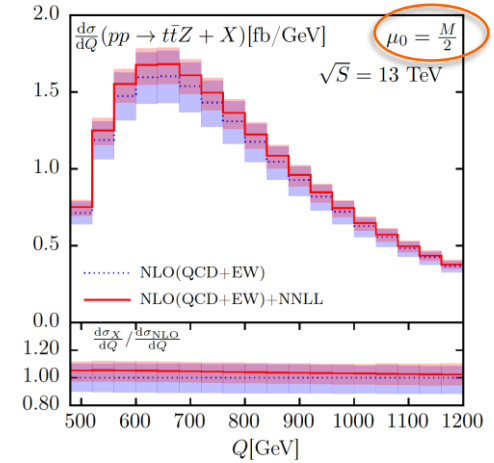
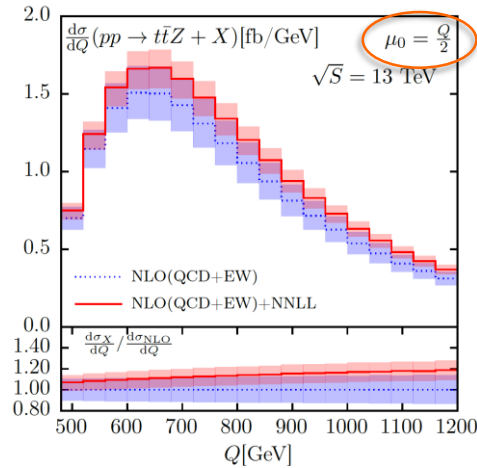
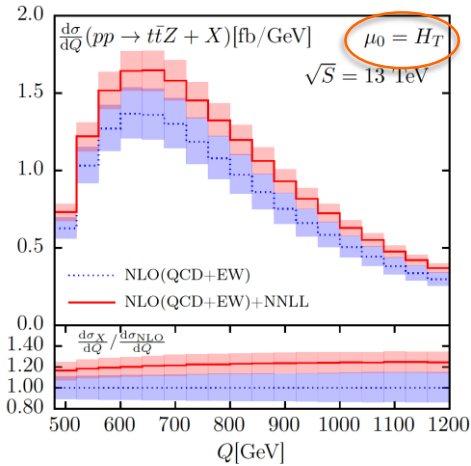
TTBARZ: INVARIANT MASS DISTRIBUTION

[AK, Motyka, Schwartländer, Stebel, Theeuwes'19 and to appear]

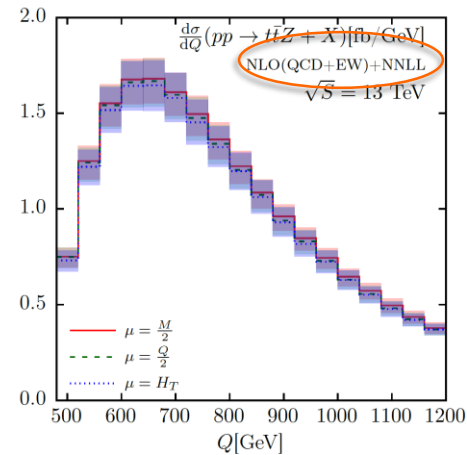


TTBARZ: INVARIANT MASS DISTRIBUTION

[AK, Motyka, Schwartländer, Stebel, Theeuwes'19 and to appear]

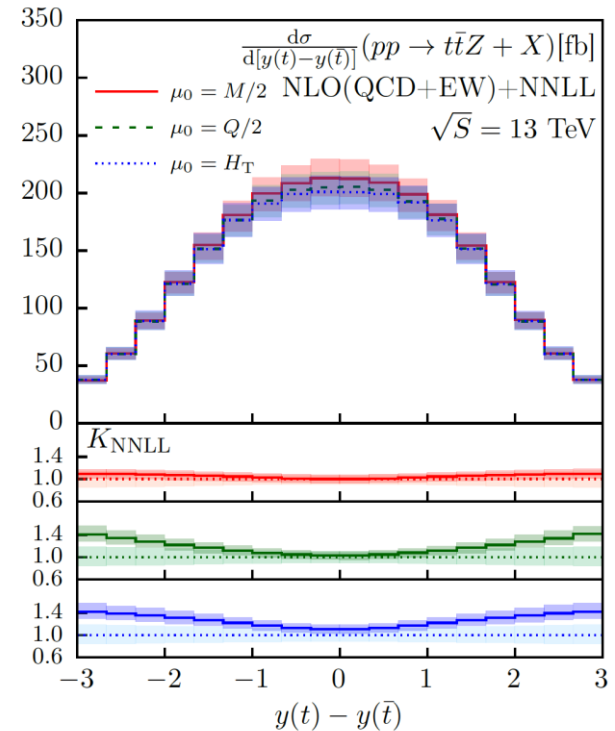
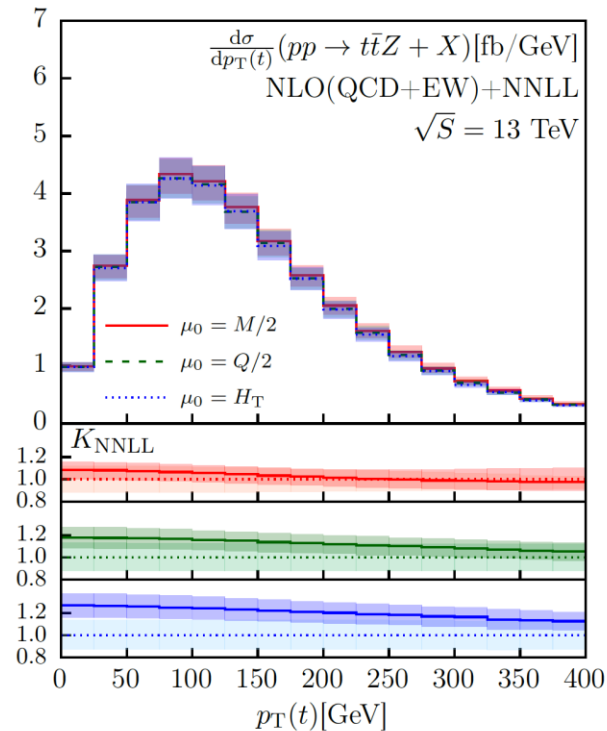
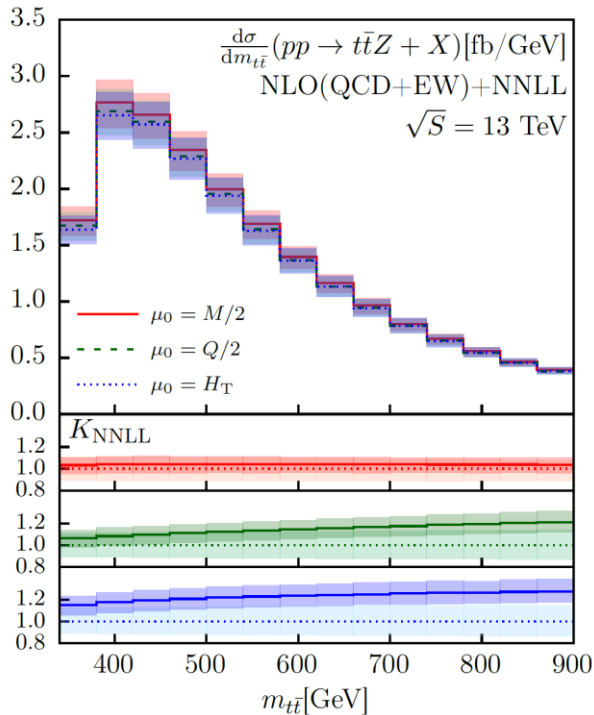


vs.



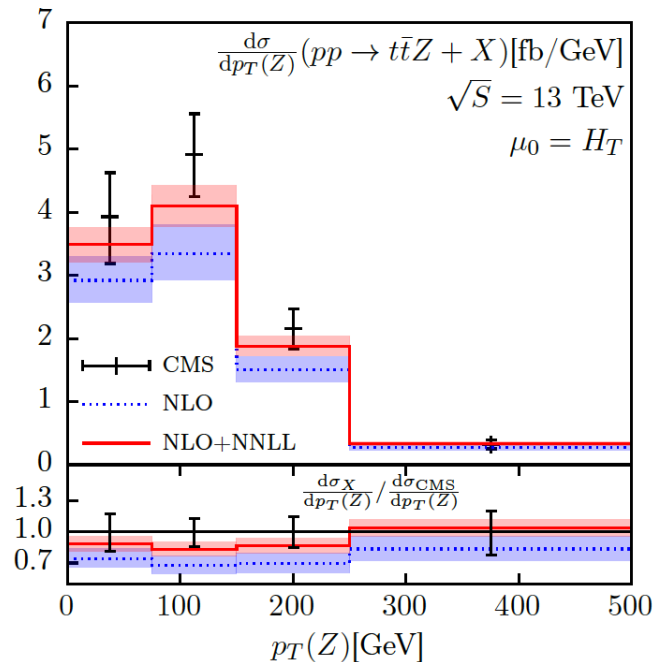
TTBARZ: DIFFERENTIAL DISTRIBUTIONS AT NLO(QCD+EW)+NNLL

[AK, Motyka, Stebel, Schwartländer, Theeuwes, to appear]



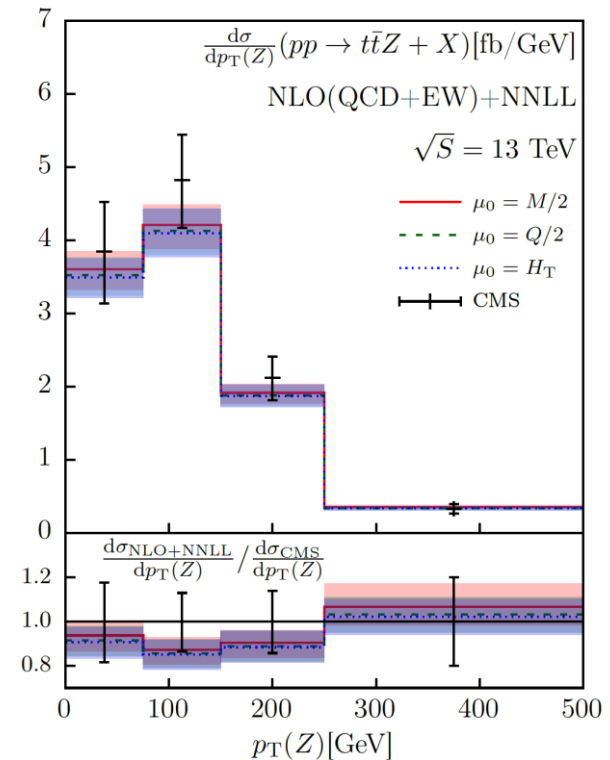
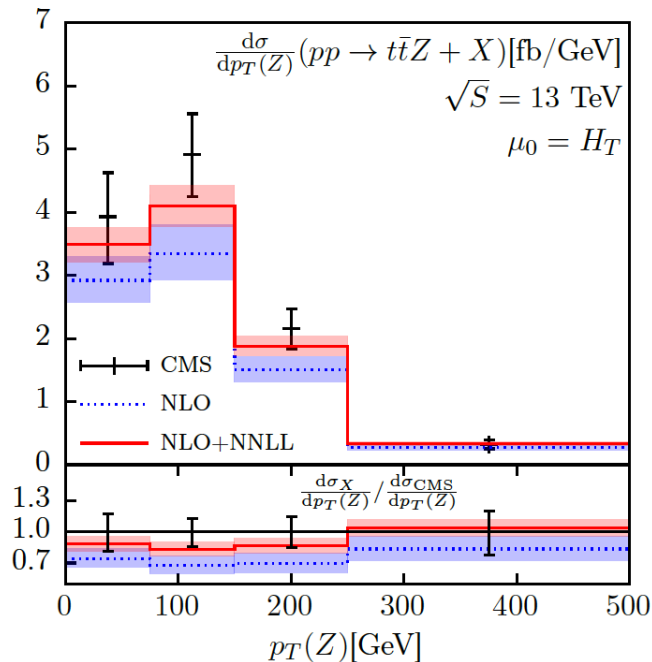
TTBARZ: Z'S TRANSVERSE MOMENTUM DISTRIBUTION AT NLO(QCD+EW)+NNLL

[AK, Motyka, Schwartländer, Stebel, Theeuwes'19 and to appear]



TTBARZ: Z'S TRANSVERSE MOMENTUM DISTRIBUTION AT NLO(QCD+EW)+NNLL

[AK, Motyka, Schwartländer, Stebel, Theeuwes'19 and to appear]



SUMMARY

- Associated top quark pair-production @ the LHC is one of the most promising windows onto new physics → precise theoretical prediction are essential → a lot of recent progress!
- **Most precise predictions** for the production processes $pp \rightarrow t\bar{t} H$, $pp \rightarrow t\bar{t} W^\pm$, $pp \rightarrow t\bar{t} Z$ involve **resummation** and reach **NNLL+NLO (QCD+EW) accuracy** -- first application of threshold resummation to a class of 2 → 3 processes
 - **Remarkable stability** of the NNLL+NLO differential and total cross sections w.r.t. scale variation
 - **Stability improves with growing accuracy** of the calculations
 - **Reduction of the theory error** due to scale variation → for ttZ the **NLO+NNLL theory error comparable with experimental uncertainty** of the latest CMS measurement