

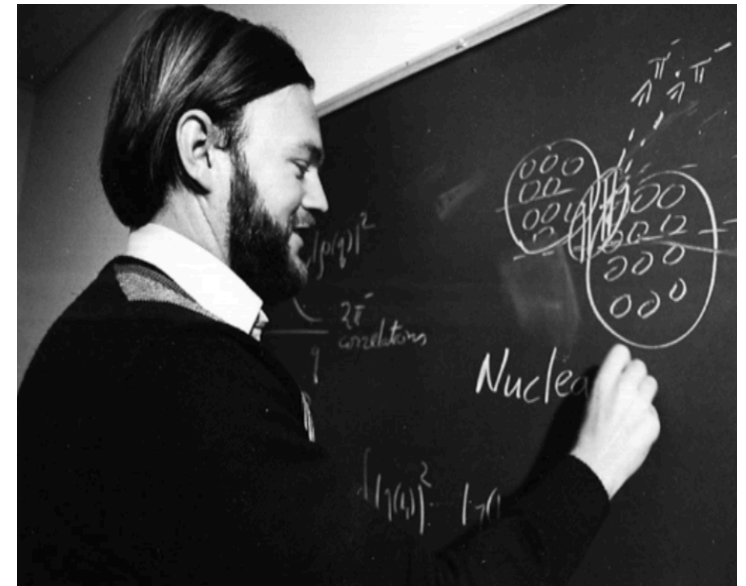
Universality in strong fields:  
the curious case of Color Glass Condensates and Black Holes

Raju Venugopalan  
Brookhaven National Laboratory

Wuhan, November 10, 2019

- ❑ Strong fields require strong personalities: some universal features
  
- ❑ The infrared structure of gauge theories:  
an adventure with Adam, Monica, Ana and Andy
  
- ❑ Exploring universal features of classicalization with Gia:  
A CGC-Black Hole Correspondence
  
- ❑ Putting it all together: Gravity as QCD's doppelgänger

Strong fields and strong personalities:  
extempore remarks on universality



# Generating strong fields by multi-particle production

Bremsstrahlung is ubiquitous in QCD because phase space logs compensate for the suppression in coupling:  $\alpha_S \ln(1/x) \sim 1$  and/or  $\alpha_S \ln(Q^2/\Lambda_{QCD}^2) \sim 1$

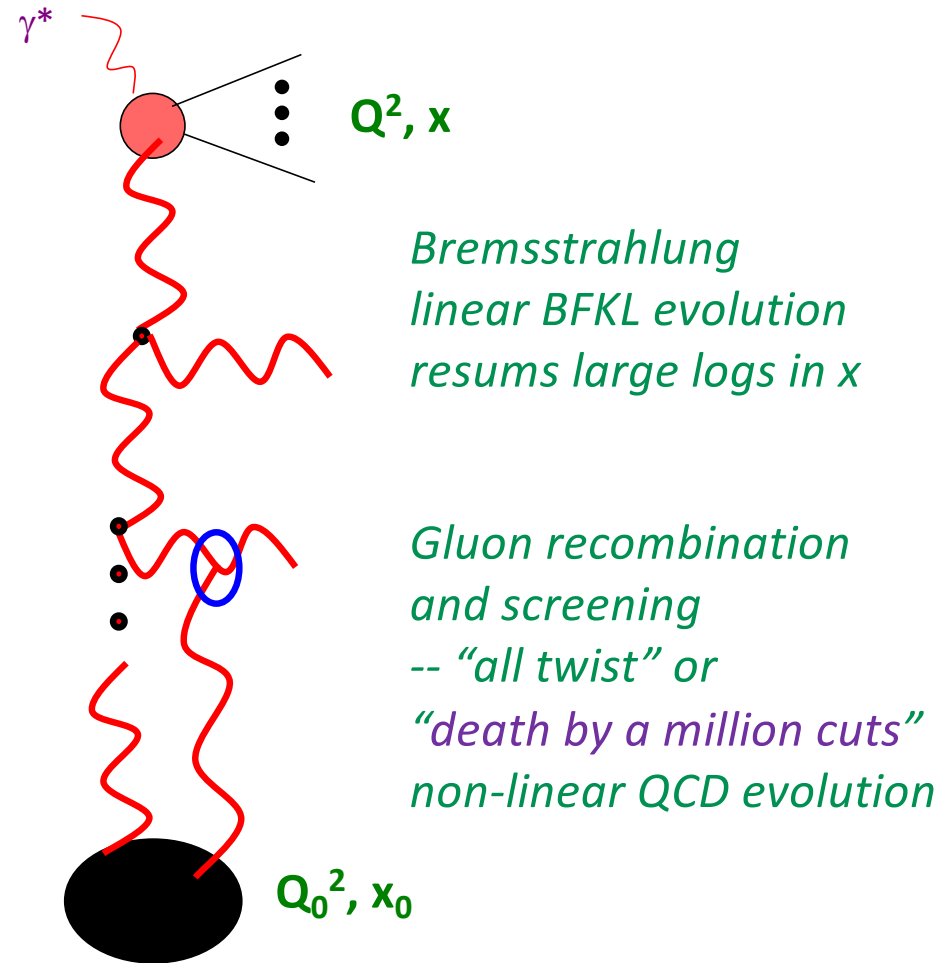
Appropriate limit for multi-particle production:

Regge limit of QCD

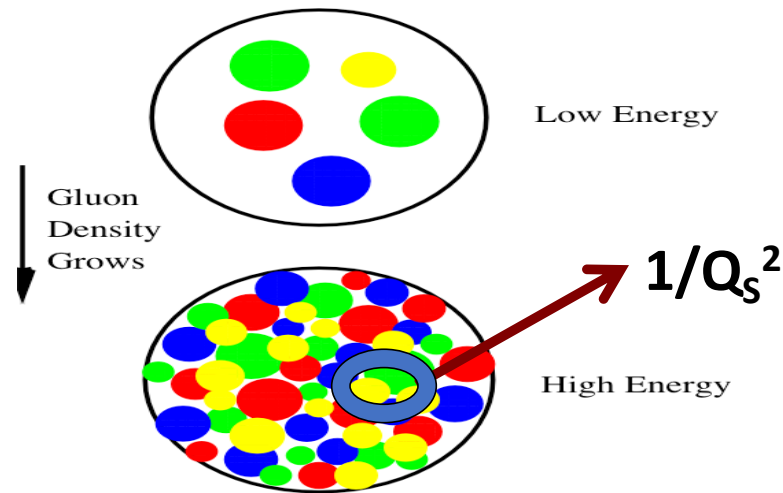
$s \rightarrow \infty, Q^2 = \text{fixed} \gg \Lambda_{QCD}^2, x \rightarrow 0$

*A fascinating equilibrium of splitting and recombination should eventually result. It is a considerable theoretical challenge to calculate this equilibrium in detail...*

*F. Wilczek, Nature (1999)*



# Gluon saturation



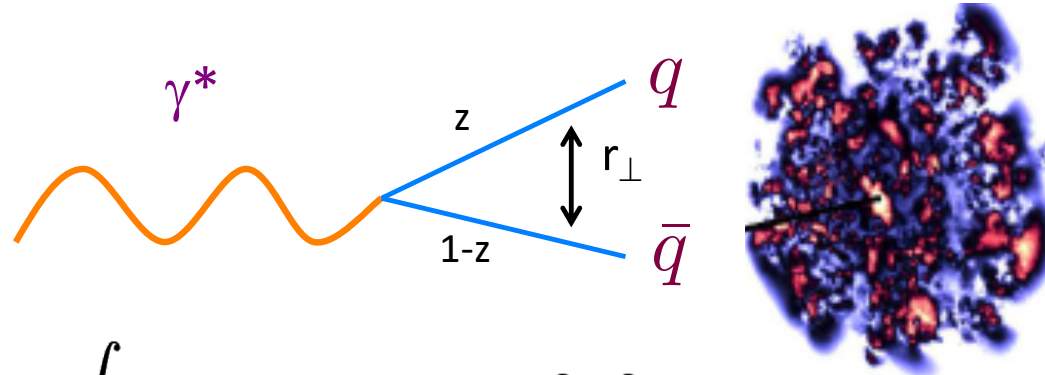
Gribov, Levin, Ryskin (1983)  
Mueller, Qiu (1986)

Gluons at maximal phase space occupancy  $n \sim 1/\alpha_s$ , resist close packing by recombining and screening their color charges -- gluon saturation

Emergent dynamical saturation scale  $Q_s(x) \gg \Lambda_{\text{QCD}}$

Asymptotic freedom!  $\alpha_s(Q_s) \ll 1$  provides weak coupling window into infrared

# Saturation as perturbative unitarization: the dipole model



$$\sigma_{T,L}^{\gamma^*,P} = \int d^2 r_{\perp} \int dz |\psi_{T,L}(r_{\perp}, z, Q^2)|^2 \sigma_{q,\bar{q},P}(r_{\perp}, x)$$

QED
QCD

Golec-Biernat Wusthoff model

$$\sigma_{q\bar{q}P}(r_{\perp}, x) = \sigma_0 \left[ 1 - \exp\left(-r_{\perp}^2 Q_s^2(x)\right) \right]$$

Color transparency for  $r_{\perp}^2 Q_s^2 \ll 1$  ( $\sigma \propto A$ )

Color opacity ("black disk") for  $r_{\perp}^2 Q_s^2 \gg 1$  ( $\sigma \propto A^{2/3}$ )

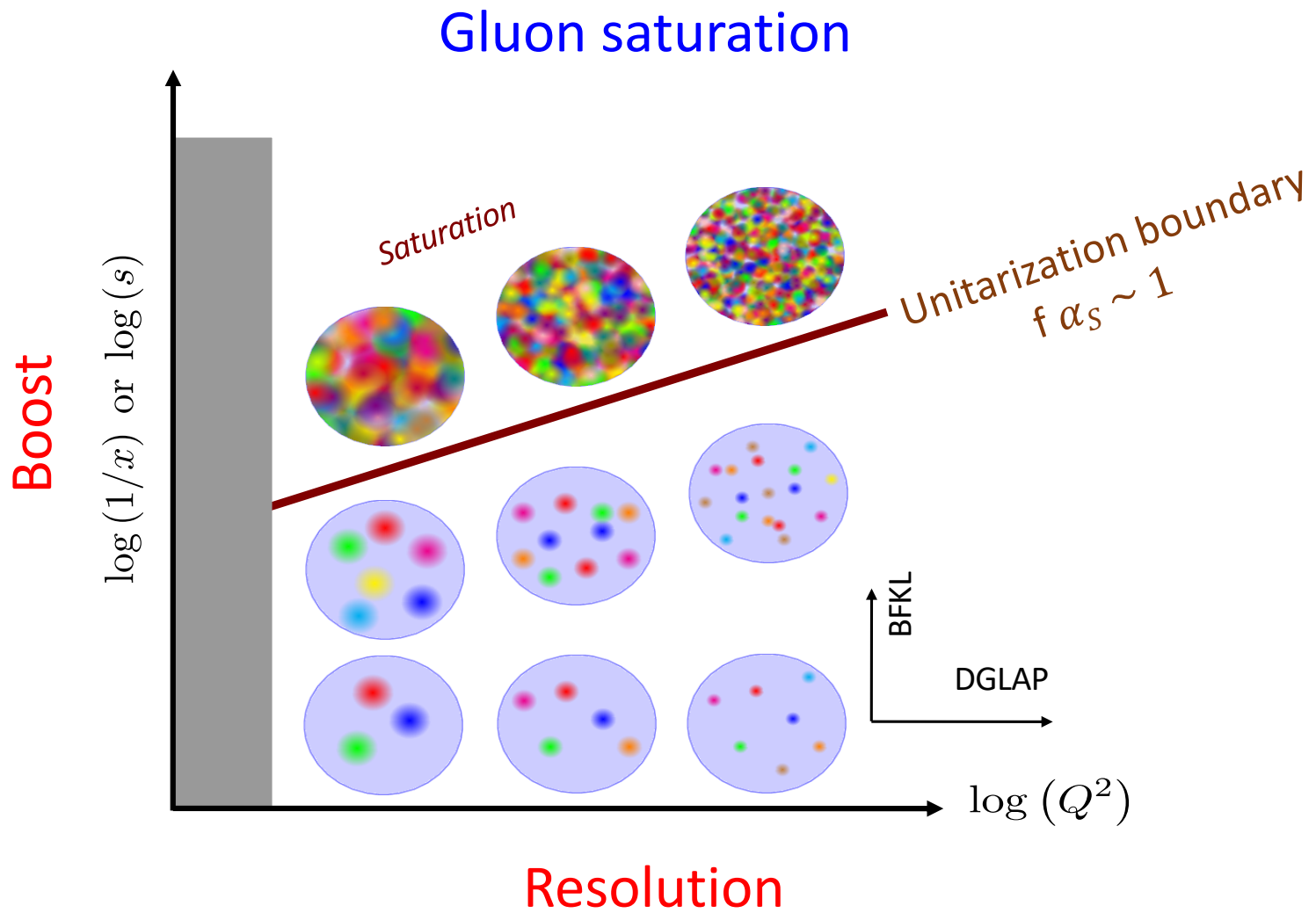
QCD picture of "shadowing"...

$$Q_s^2(x) = Q_0^2 \left( \frac{x_0}{x} \right)^{\lambda}$$

Parameters:

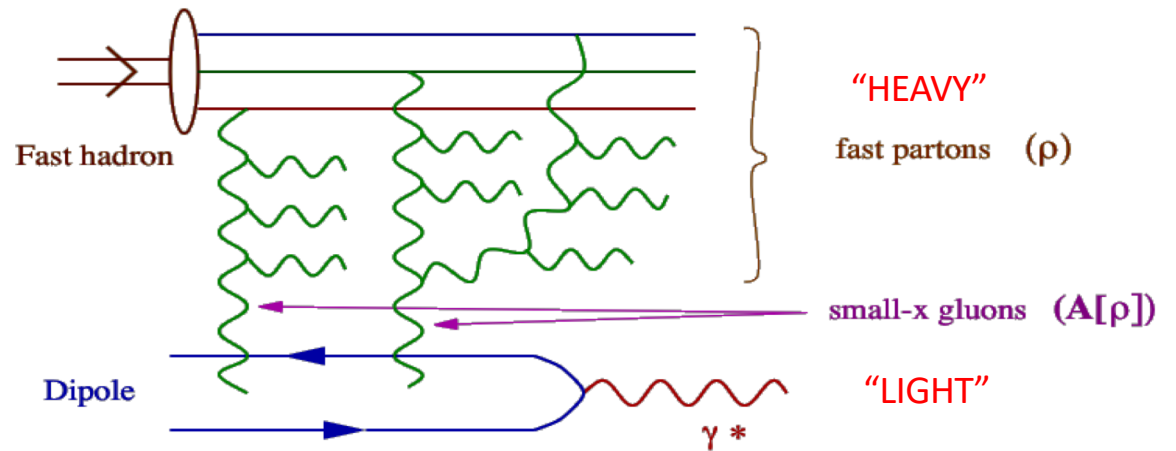
$Q_0 = 1 \text{ GeV}; \lambda = 0.3;$

$x_0 = 3 \cdot 10^{-4}; \sigma_0 = 23 \text{ mb}$



# Classicalization in the Regge limit: the Color Glass Condensate EFT

Born-Oppenheimer separation  
between fast and slow modes



CGC: Effective Field Theory  
of classical static quark/gluon sources  
and dynamical gluon fields

Remarkably, physics of extreme quantum fluctuations  
becomes classical because of high gluon occupancy...

McLerran, RV (1994)

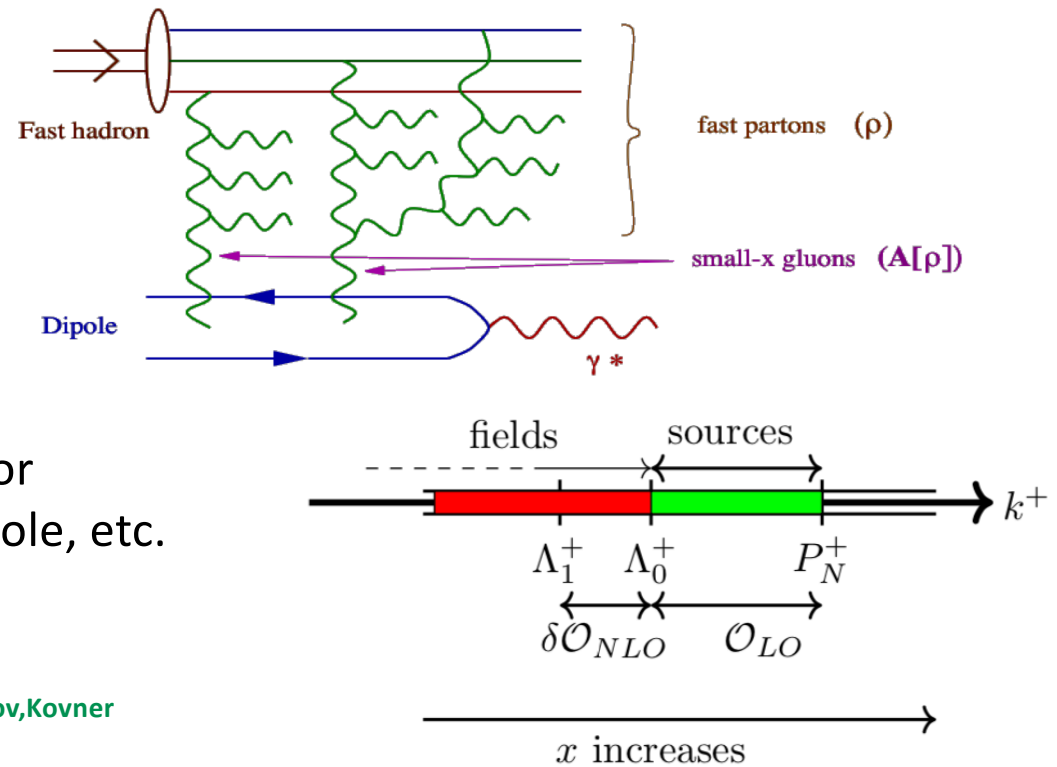


# Classicalization in the Regge limit: the Color Glass Condensate EFT

EFT allows one to compute many-body correlations just as in condensed matter physics

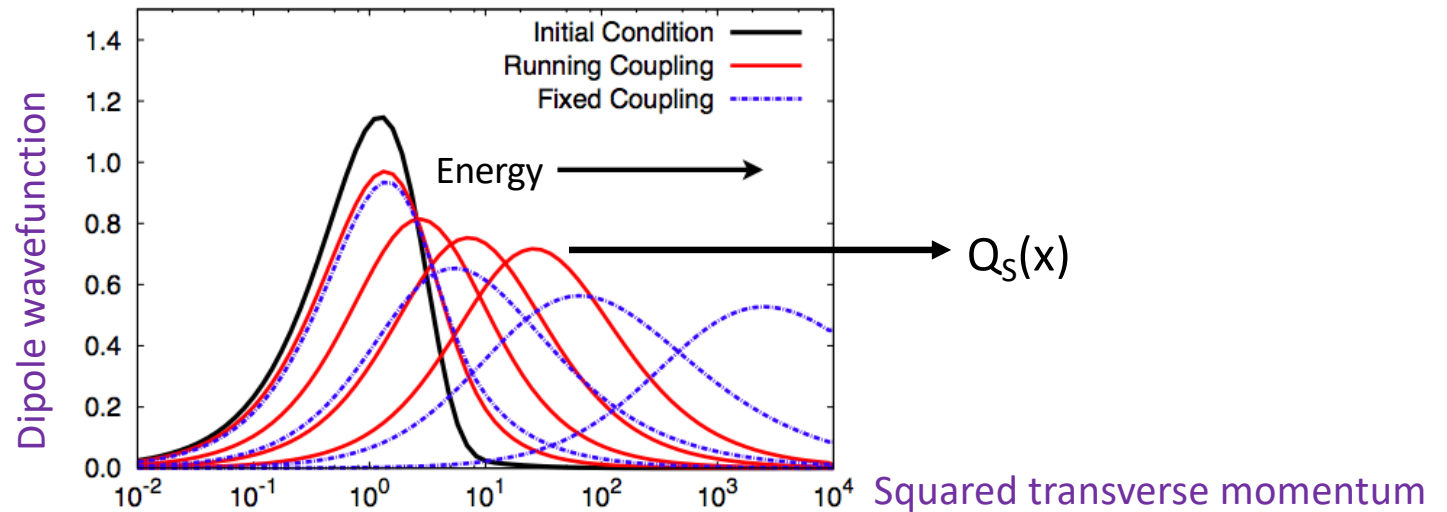
Wilsonian RG :  
2+1-D B-JIMWLK hierarchy of equations for multi-point "Wilson line" dipole, quadrupole, etc. correlators -- right degrees of freedom

Balitsky (1996)  
JIMWLK (1997-2001): Jalilian-Marian, Iancu, McLerran, Weigert, Leonidov, Kovner  
Kovchegov (1999)



*Universal classical dynamics of QCD in the infrared?*

## Classicalization in the Regge limit: the Color Glass Condensate EFT



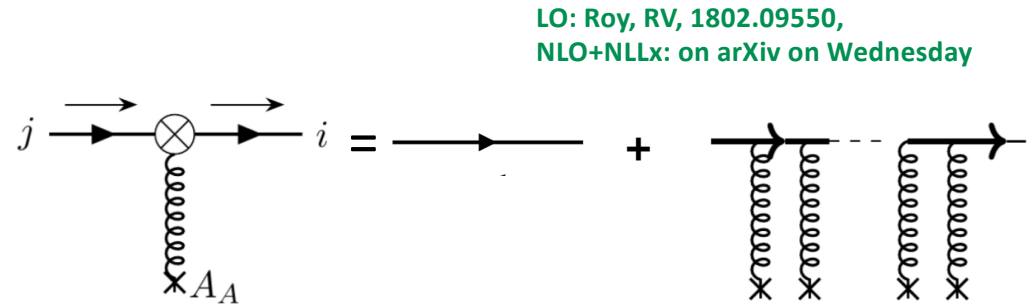
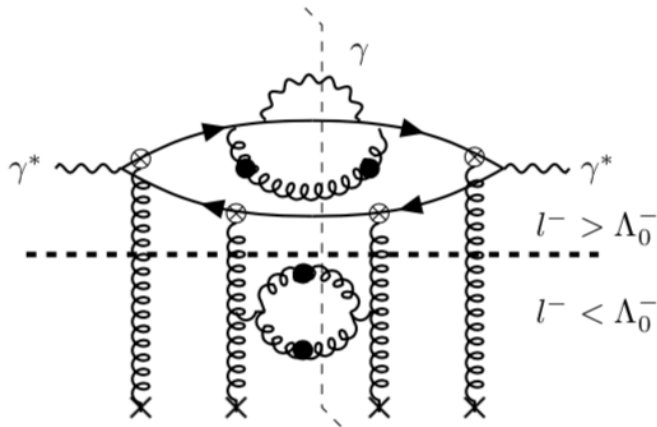
A closed form non-linear (Balitsky-Kovchegov) equation describes how  $q\bar{q}$  “dipole” probe evolves with energy – *providing a clean demonstration of unitarization in strong fields*

Its dynamics can be mapped\* to that of the **Fischer-Kolmogorov (FKPP) eqn.** describing the evolution of non-linear wave fronts. Rich synergy with stat. mech.

Munier, Peschanski (2003)

\* small caveat

# The power of Colored Glass: photons and di-jets to NLO+NLLx



LO: Roy, RV, 1802.09550,  
NLO+NLLx: on arXiv on Wednesday

Mom. dependent effective quark (and gluon) vertices include "all-twist" corrections  $(Q_s^2/Q^2)^n$

Compton amplitude for  $eA \rightarrow \gamma + \text{dijets} + X$

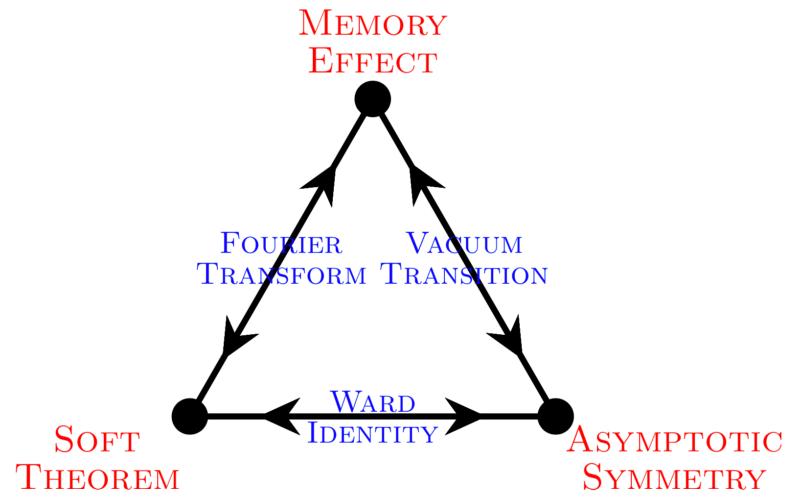
Differential DIS computations in the CGC EFT now available to  $O(\alpha_s^3 \text{Ln}(1/x))$  accuracy

Can be tested to  $\sim 10\%$  accuracy at an Electron-Ion Collider

Some remarkable features:

- Propagators are *identical* to those in Lipatov's Reggeon field theory
- Spacelike-timelike correspondence of soft gluons ("non-global" logs)
- Interesting pattern of violation of soft gluon "theorem"

# Infrared memory and asymptotic symmetries



Strominger, arXiv:1703.05448  
Motivation:  
Black hole information loss problem  
Hawking, Perry, Strominger, PRL (2016)

Conjectured to be very general property of the infrared in gauge theories & gravity  
In gravity, the symmetries are the **BMS symmetries** for asymptotically flat spacetime

BMS: Bondi, van der Burg, Metzner, Sachs (1962)

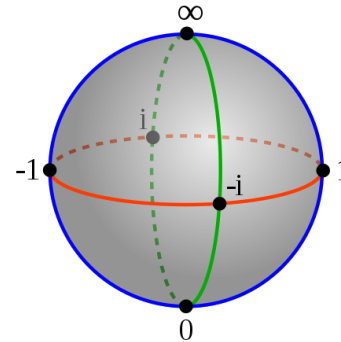
Corresponding *gravitational memory*: a physical displacement of inertial detectors

Zeldovich, Polnarev (1974)  
Christodoulou (1991)

Measurable by LIGO, LISA, Pulsar Time Arrays...

# Infrared memory and asymptotic symmetries in QED

In QED, BMS-like symmetry:  
 group of conserved charges  
 on celestial sphere at "null infinity"  
 -satisfy conservation law with S-matrix

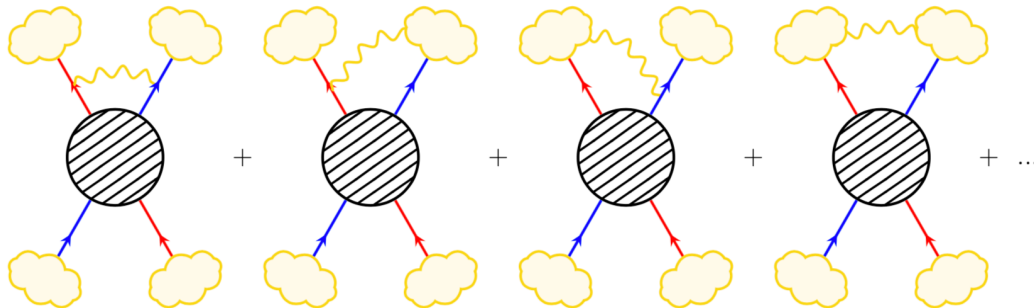


Riemann/Celestial sphere: stereographic projection of 2-D transverse plane

Equivalent to soft photon (Low) theorem

- S-matrices dressed by soft photon clouds are IR finite

$$\langle \text{out} | (Q_{\epsilon}^{+} \mathcal{S} - \mathcal{S} Q_{\epsilon}^{-}) | \text{in} \rangle = 0$$



“Faddeev-Kulish” (1970)

Coherent state basis for asymptotic states  
 avoids cumbersome cancelation  
 of collinear divergences in usual pert. theory

Kapec, Perry, Raclariu, Strominger, arXiv:1705.043011

# Yang-Mills memory and asymptotic symmetries

Pate, Raclariu, Strominger, PRL (2017)

Soft gluons satisfy a conformal 2-D (Kac-Moody) current algebra with an infinite # of conserved charges on  $S^2$

Nair (1988)

He, Mitra, Strominger (2015)

In Yang-Mills, exploiting these symmetries requires weak coupling scale in IR (CGC !)

How such symmetries constrain “boundary conditions at spatial infinity” may provide insight into Faddeev-Kulish coherent states in QCD (eigenstates of CGC “vacuum”)

# Color Memory in the CGC

Ball, Pate, Raclariu, Strominger, RV,  
Annals of Physics (407 2019) 15

$$A_i = 0 \quad \Big| \quad A_i = -\frac{1}{ig} U \partial_i U^\dagger$$

$x^- = 0$

In the CGC, solution of the YM-eqns: two **pure gauges** separated by shockwave discontinuity

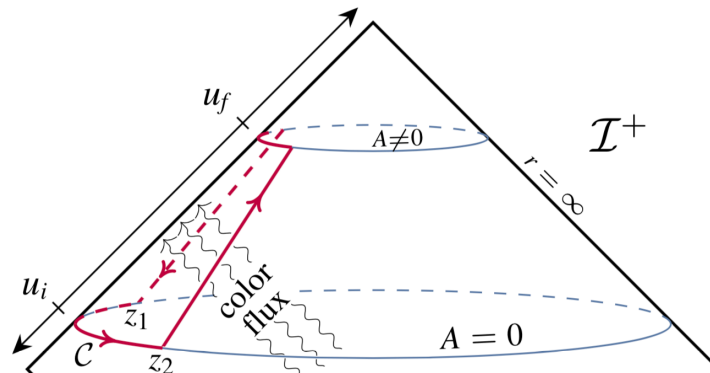
$y = \ln(x^-/x_0^-)$        $D_i \frac{dA^{i,a}}{dy} = g\rho^a(x_t, y)$  with the solution  $U = P \exp \left( i \int_y^\infty dy' \frac{\rho(x_t, y')}{\nabla_t^2} \right)$

Identical to expression for a YM vacuum transition on celestial sphere at null infinity

$$(r, u, z, \bar{z}) \rightarrow (\lambda r, \lambda^{-1} u, \lambda^{-1} z, \lambda^{-1} \bar{z})$$

$$\text{Map: } x^+ = \sqrt{2r}, \quad x^- = \frac{1}{\sqrt{2}}(u + rz\bar{z}), \quad x^1 + ix^2 = 2rz$$

$\lambda \rightarrow \infty$  Flatten  $S^2$  to transverse plane,  
 $r \rightarrow \infty$  corresponds to  $x^+ \rightarrow \infty$   
 $x^- \rightarrow 0$



## Color Memory in the CGC

$$A_i = 0 \quad \Big| \quad A_i = -\frac{1}{ig} U \partial_i U^\dagger$$

$x^- = 0$

Ball, Pate, Raclariu, Strominger, RV,  
Annals of Physics (407 2019) 15

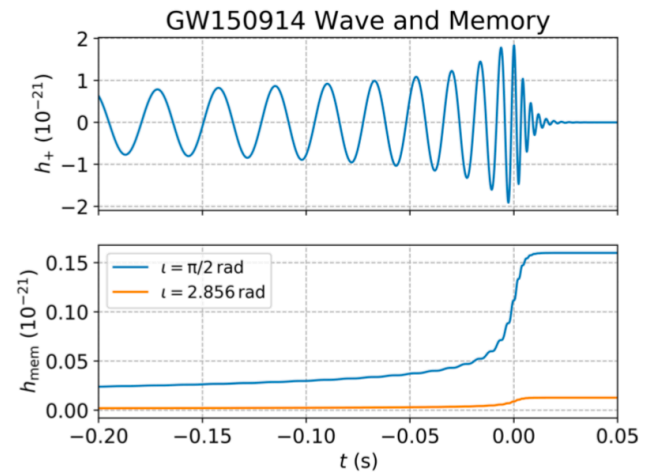
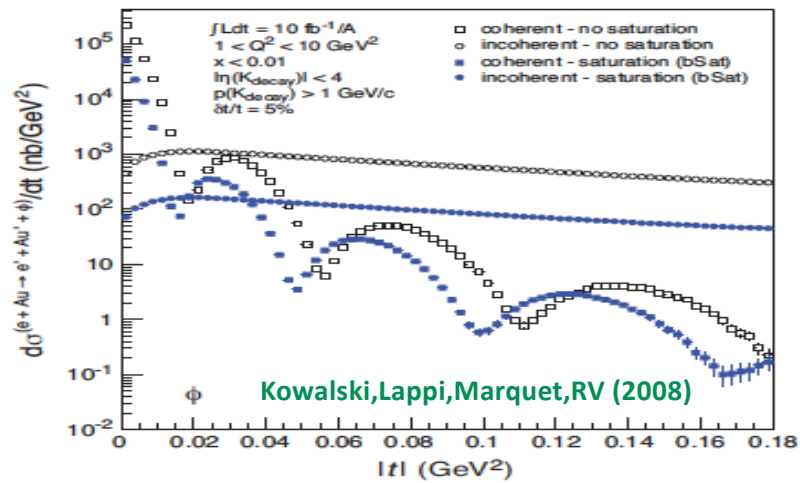
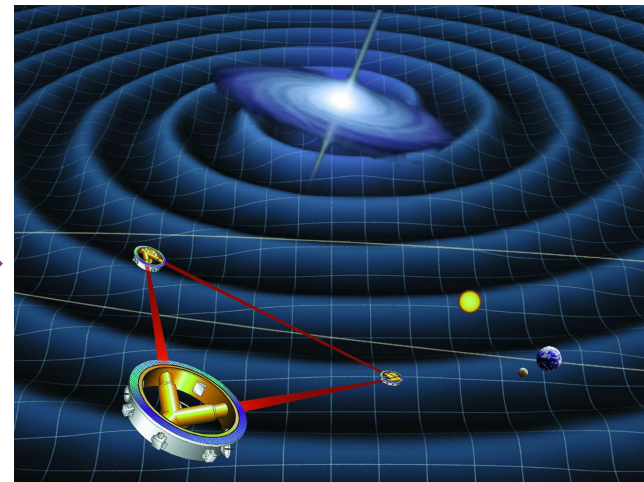
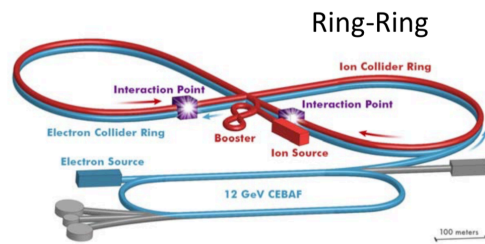
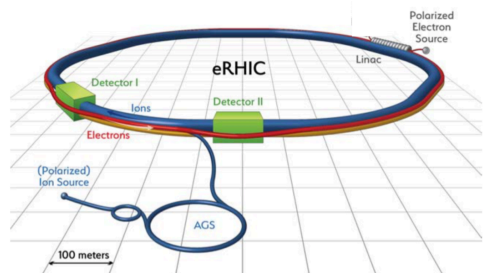
$U$  is precisely the *color memory* effect corresponding to a color rotation and  $p_T \sim Q_S$  kick experienced by quark-antiquark pair traversing the shock wave

Pate, Raclariu, Strominger, PRL (2017)

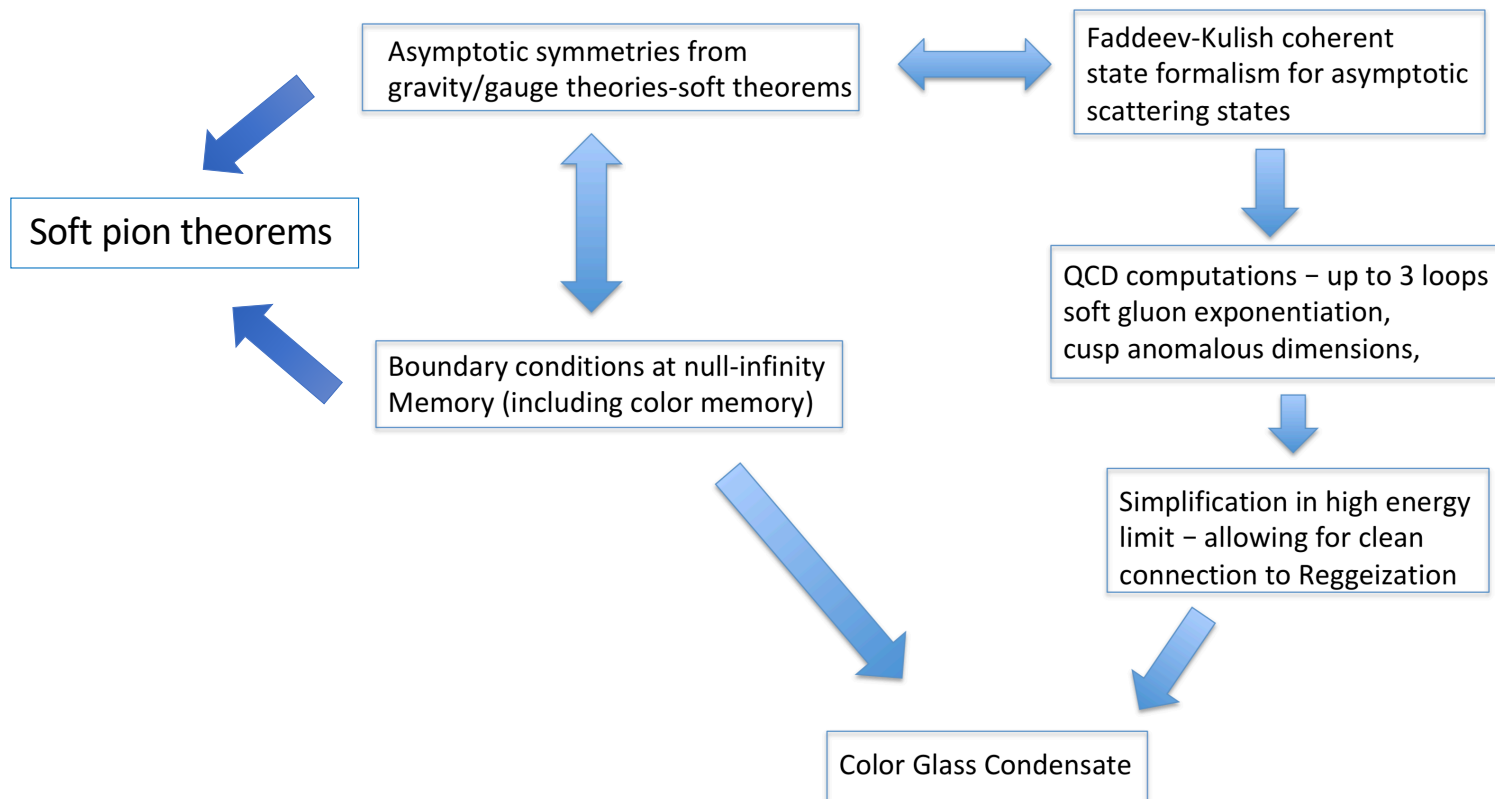
*Its presence is ubiquitous in DIS final states*



# Infrared Memory: from EIC to LISA, etc...



# Conjecture: Completing the circle on QCD in the infrared



# UV/IR correspondence of quantum portraits of Black Holes and CGCs

Dvali, RV, in preparation

Conjecture: Classicalization of gluons (gravitons) occurs at unitarization boundary ( $\alpha n = 1$ )

Gluons are weakly coupled in the UV and strongly coupled in the IR ( $\Lambda_{QCD}$ )

Gravitons are weakly coupled in the IR and strongly coupled in the UV ( $L_{Planck} = \sqrt{\hbar G_N}$ )

However, we argued that in QCD, unitarization can occur at the scale  $Q_S \gg \Lambda_{QCD}$

Likewise, in gravity, unitarization occurs at the Schwarzschild radius  $R_S = \sqrt{2 M G_N} \gg L_{Planck}$

Self-bound gravitons form a quantum portrait of a Black Hole at the unitarization boundary

Dvali, Gomez (2011)

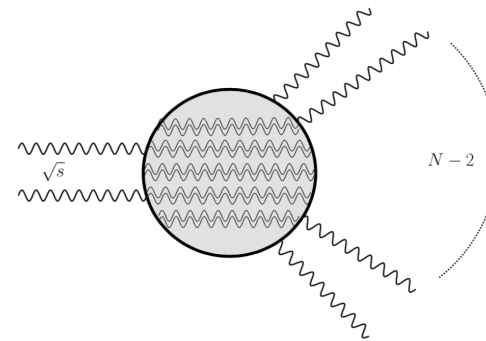
*Is the physics universal for  $\alpha n = 1$  ?*

# UV/IR correspondence of quantum portraits of Black Holes and CGCs

A quantitative correspondence emerges in the Trans-Planckian limit of  $2 \rightarrow N$  graviton scattering

Lipatov (1991)

Explicit computations by Veneziano et al. of **unitarized gravity amplitudes** reproduces semi-classical Black Hole portrait of Dvali et al.



Amati, Ciafaloni, Veneziano, arXiv:0712.1209

Adazzi, Bianchi, Veneziano, arXiv:1611.03643

Dvali, Gomez, Isermann, Lust, Stieberger, arXiv:1409.7405

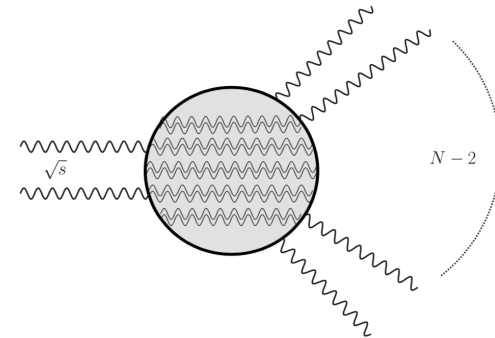
This is exactly analogous to how the semi-classical CGC description of  $2 \rightarrow N$  scattering of gluons reproduces the explicit (BFKL) computations in pQCD

A common feature in QCD and Gravity is “**Reggeization**” of propagators by dressed propagators: this is captured efficiently in the semi-classical EFT picture...

# UV/IR correspondence of quantum portraits of Black Holes and CGCs

Black Hole entropy versus CGC entropy:

$$S_{\text{BH}} = \frac{\text{Area}}{G} = \frac{R_{\perp}^2}{G} = \frac{c_{\text{gr}}}{\alpha_{\text{gr}}} \frac{R_{\perp}^2}{R_S^2} \quad S_{\text{CGC}} = \frac{c_{\text{QCD}}}{\alpha_S} Q_S^2 R_{\perp}^2$$



Other interesting apparently universal features of this UV/IR correspondence:  
scrambling, radiation, thermalization

Making it quantitative: a classical "double copy" between QCD and gravity

KLT: Kawai, Lewellen, Tye (1986)  
BCJ: Bern, Carrasco, Johansson (2008)  
Goldberger, Ridgeway (2017)

Stay tuned...

Warmest wishes to Jean-Paul, Miklos and Larry  
– and to many productive years ahead !