

$$\Psi(x) = \frac{1}{\sqrt{k}} (A_- e^{ikx} + A_+ e^{-ikx}) \quad x < 0$$

$$k = \sqrt{2mE/\hbar^2}$$

$$R_{\gamma\gamma} - \frac{1}{2} R_{g\gamma} + \Lambda_{g\gamma} = \frac{8\pi G}{c^3} T_{\mu\nu}$$

Giorgio GALANTI

INAF - OA Brera

$$H = \frac{p \cdot p}{2m} + V(x)$$

$$p = -i\hbar \nabla$$



$$S = \frac{1}{2k} \int R \sqrt{-g} dx$$

$$\frac{d^2 k A}{4\hbar G}$$

$$L = \text{tr} \left\{ \frac{1}{g} F_{\mu\nu} F^{\mu\nu} - i\lambda \Gamma^A D_A \lambda \right\}$$

Revisiting $\gamma\gamma$ absorption for UHE photons

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\frac{1}{c^2} \frac{\partial^2 \psi}{\partial t^2} - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{c} = \frac{h}{\lambda}$$

G. Galanti, F. Tavecchio, F. Piccinini, M. Roncadelli

$$A_{ij} = \frac{8\pi h \nu^3}{c^3} B_{ij}$$

XSCRC2019



$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

CERN, Geneva, 13-15 November 2019

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=0}^{\infty} \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

Outline

- Ultra-high-energy photons
- Photon background
- Cross sections
- Results
- Conclusions

Ultra-high-energy photons

UHE photons

- Ultra-high-energy (UHE, $E > 10^{18}$ eV) photons \rightarrow by-product of the photo-meson reactions $p\gamma_{\text{CMB}} \rightarrow \Delta^+ \rightarrow p\pi^0 \rightarrow p\gamma\gamma$ (GZK radius)
- Resulting UHE photons interaction with background photons γ_b
- UHE photons absorbed via processes $\gamma_{\text{UHE}}\gamma_b \rightarrow \text{any}$
- Considered processes:
 - $\gamma\gamma \rightarrow e^+e^-$
 - $\gamma\gamma \rightarrow e^+e^-e^+e^-$

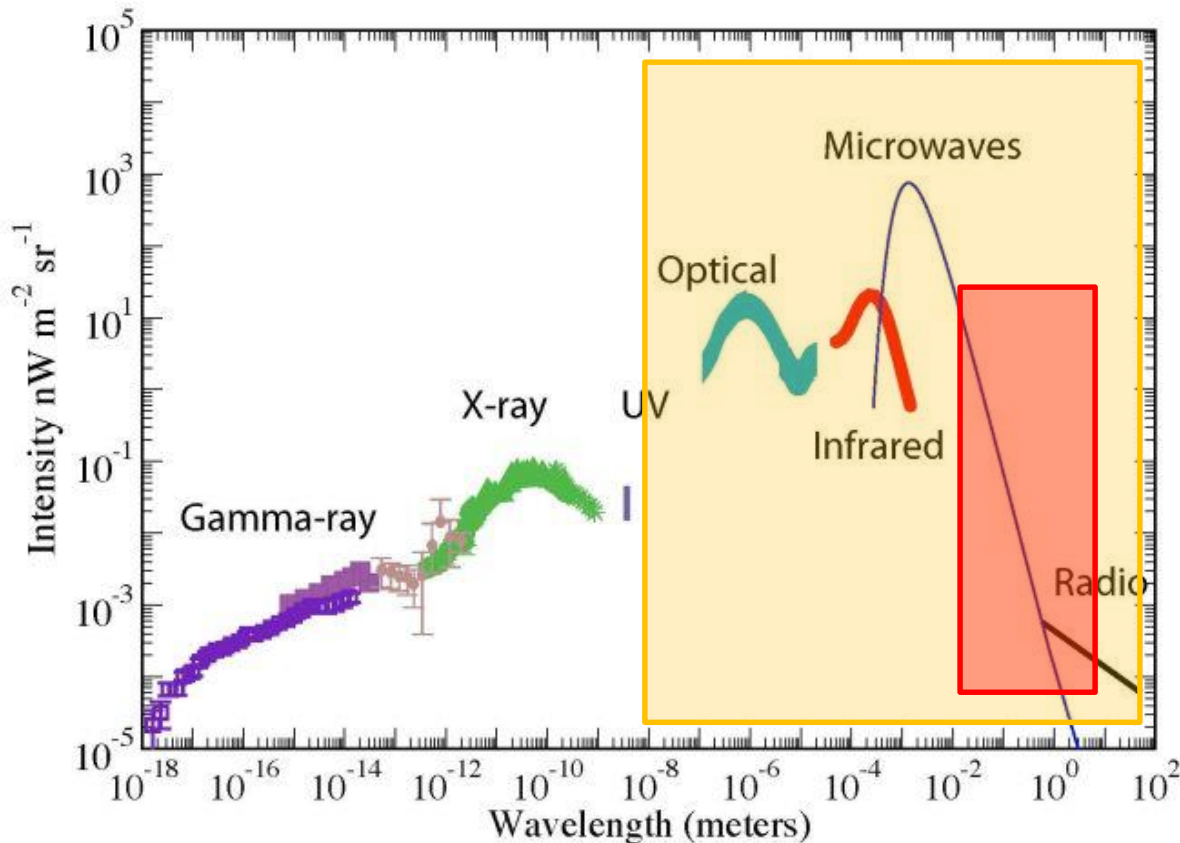
UHE photon propagation

Are other processes beyond the already considered ones $\gamma\gamma \rightarrow e^+e^-$ and $\gamma\gamma \rightarrow e^+e^-e^+e^-$ relevant for UHE photons?

YES: $\gamma\gamma \rightarrow \mu^+\mu^-$ and $\gamma\gamma \rightarrow$ hadrons give sizable effects for energies $E > 10^{19}$ eV

Photon background

Photon background



- Hard produced photons with energy $E > 100 \text{ GeV}$ interact mainly (near the threshold) with soft background photons with energy $\varepsilon < 10 \text{ eV}$ ($\gamma\gamma \rightarrow e^+e^-$)
- High background photon density from optical to radio wavelengths (**yellow area**)
- Sizable modification in the optical depth τ in low-microwave – radio range (**red area**)

Photon background (2)

EBL (Extragalactic Background Light)

- UV-optical-infrared background
- Direct product of the *stellar radiation* and *light absorbed and reradiated* by the *dust* during the whole cosmic evolution
- Photon number density from model of Gilmore et al., 2012

CMB (Cosmic Microwave Background)

- Photons (now redshifted) existing in the Universe at the time of photon decoupling for the formation of neutral atoms
- Black body photon number density at temperature $T = 2.7$ K

Radio Background

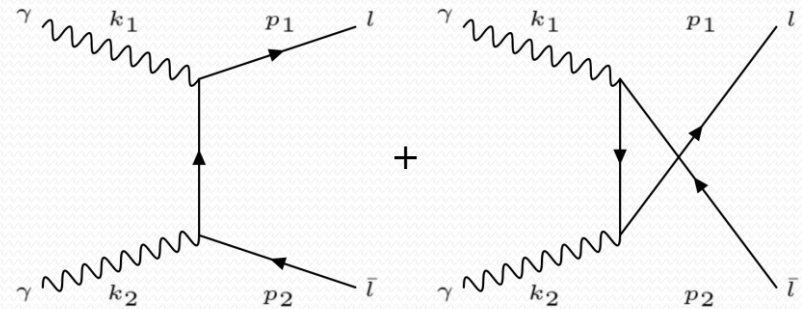
- Diffuse thermal and nonthermal, galactic and extragalactic radiation
- Photon number density from model of Gervasi et al., 2008

Cross Sections

Leptonic sector

SINGLE PAIR PRODUCTION

- $\gamma\gamma \rightarrow l^+l^-$ ($l = e, \mu, \tau$)
- $\sigma_{\gamma\gamma \rightarrow l\bar{l}}(\omega, p) = \frac{\pi\alpha^2}{\omega^2} \left\{ \left(1 + \frac{m^2}{\omega^2} - \frac{1}{2} \frac{m^4}{\omega^4} \right) \times \right.$
 $\left. \times \ln \left[\frac{(\omega + p)^2}{m^2} \right] - \frac{p}{\omega} \left(1 + \frac{m^2}{\omega^2} \right) \right\}$
- $\gamma\gamma \rightarrow e^+e^-$ already considered
- $\gamma\gamma \rightarrow \mu^+\mu^-$ gives sizable effects
- $\gamma\gamma \rightarrow \tau^+\tau^-$ negligible

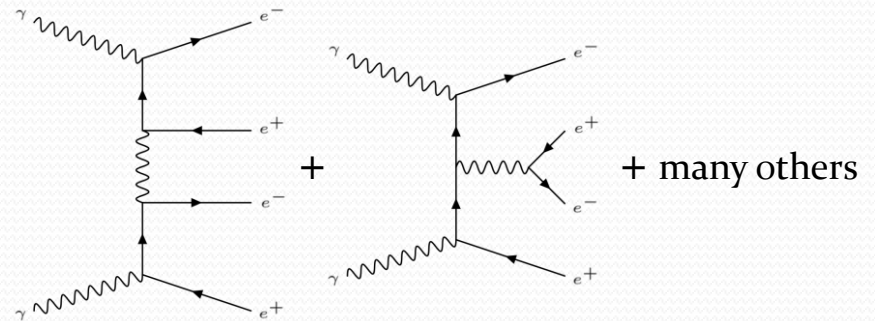


CM: $k_1 \equiv (\omega, \mathbf{\omega})$; $k_2 \equiv (\omega, -\mathbf{\omega})$; $p_1 \equiv (\omega, \mathbf{p})$; $p_2 \equiv (\omega, -\mathbf{p})$
 $\omega \rightarrow$ photon energy; $\mathbf{p} \rightarrow$ lepton 3-momentum
 $S_{\text{CM}} = 4\omega^2$

See also: Breit & Wheeler, 1934

DOUBLE PAIR PRODUCTION

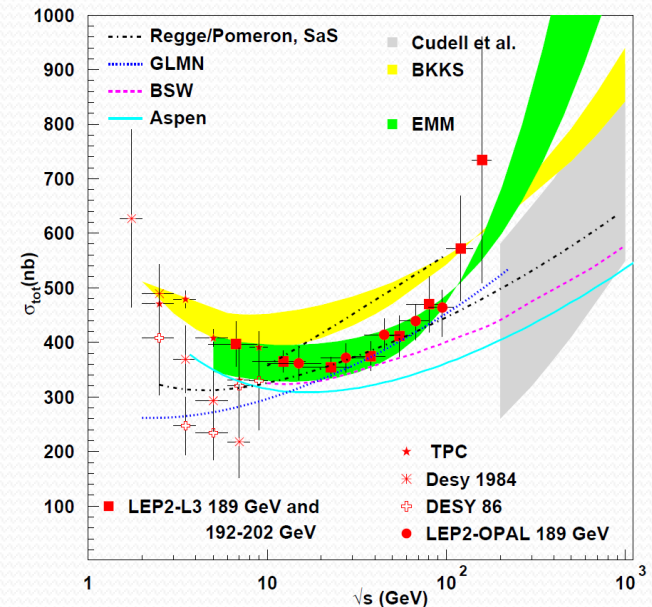
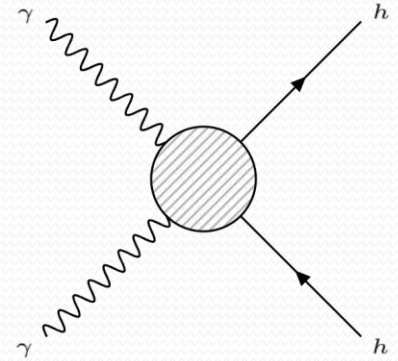
- $\gamma\gamma \rightarrow e^+e^-e^+e^-$ already considered
- $\sigma_{\text{DPP}}(s) = \frac{\alpha^4}{\pi m_e^2} \left(\frac{175}{36} \zeta(3) - \frac{19}{18} \right) \left(1 - \frac{16m_e^2}{s} \right)^6$
- Other four lepton production negligible



Brown, Hunt, Mikaelian & Muzinich, 1973
 da Silva & Kapusta, 2012

Hadronic sector

- $\gamma\gamma \rightarrow$ hadrons
- QCD non perturbative effects complicate a calculation from *first principles*
- Phenomenological approach
- Lowest massive hadrons $\rightarrow \pi^\pm, \pi^0$ mesons
- Threshold $\rightarrow E_{th} = 2 m_\pi$
- Near threshold $\sigma_{\gamma\gamma \rightarrow \text{hadrons}}$ similar (bigger) as respect to $\sigma_{\gamma\gamma \rightarrow \pi^+\pi^-}$ (sQED)
- At high energies \rightarrow data from colliders
- Smooth low-high energy junction with uncertainty



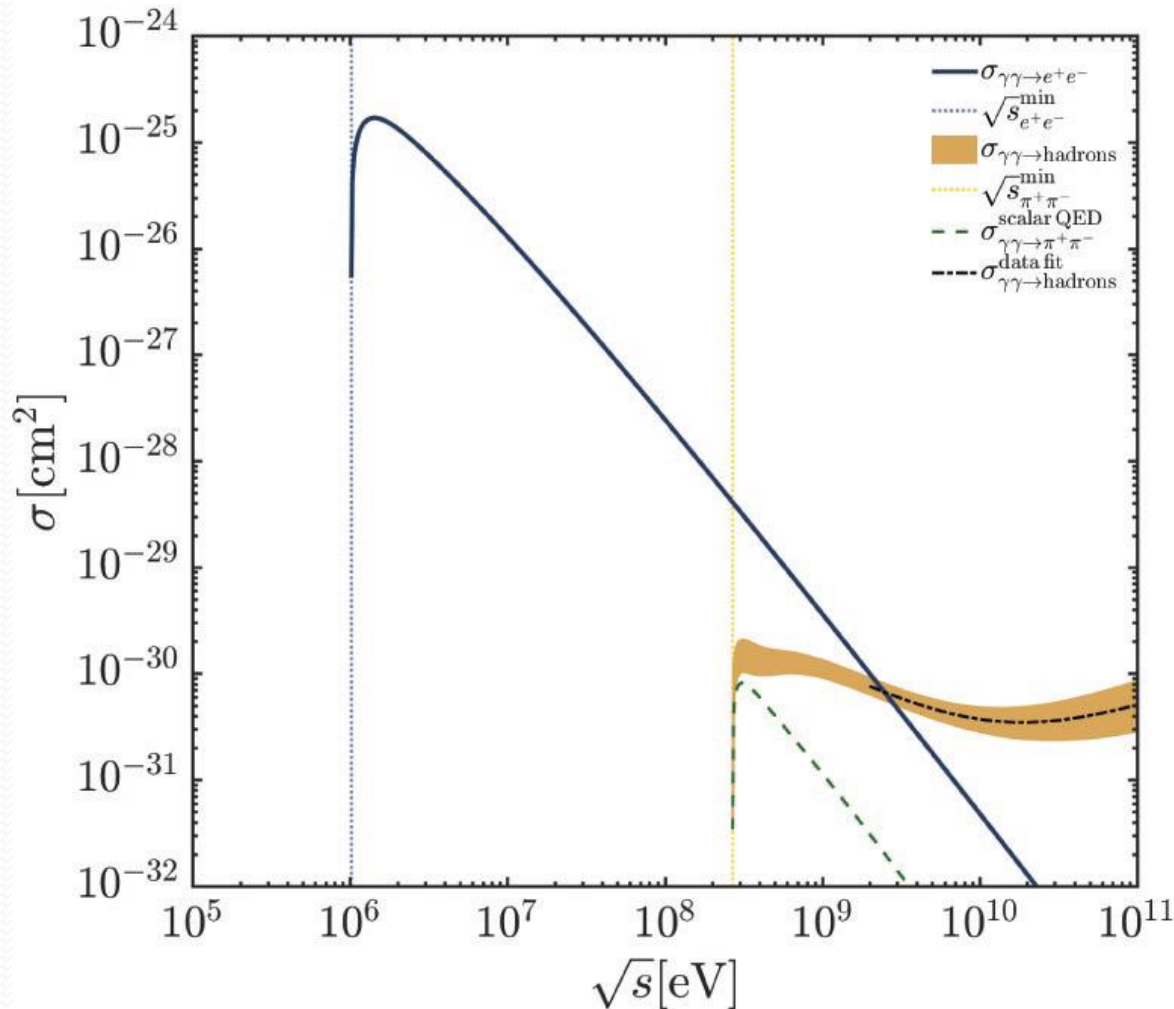
Resonances

- Prototype: single π^0 production $\gamma\gamma \rightarrow \pi^0$
- Inverse process of π^0 decay

$$\sigma_{\gamma\gamma \rightarrow \pi^0}(s) = \frac{8\pi^2}{m_{\pi^0}} \Gamma_{\pi^0 \rightarrow \gamma\gamma} \delta(s - m_{\pi^0}^2)$$

- $\Gamma_{\pi^0 \rightarrow \gamma\gamma} \rightarrow$ experimental π^0 decay rate
- We consider:
 - Single neutral meson production ($\pi^0, \eta, \eta', \eta_c$)
 - *para*-positronium *p*-Ps production
- Decay rates and masses from experimental data

Cross sections



Galanti, Tavecchio, Piccinini & Roncadelli, in preparation

- Hadronic data fitting function (high energies):

- $$\sigma_{\gamma\gamma \rightarrow \text{hadrons}}(s) = A \cdot s^\epsilon + B \cdot s^{-\eta}$$

with

- $A = 51 \cdot 10^{-33} \text{ cm}^2$
- $B = 1132 \cdot 10^{-33} \text{ cm}^2$
- $\epsilon = 0.240$
- $\eta = 0.358$

Godbole, Roeck, Grau & Pancheri 2003

- At low energies:
- $$\sigma_{\gamma\gamma \rightarrow \text{hadrons}} = \kappa \sigma_{\gamma\gamma \rightarrow \pi^+\pi^-}$$
 with $\kappa = 1.25 - 2.5$

Results

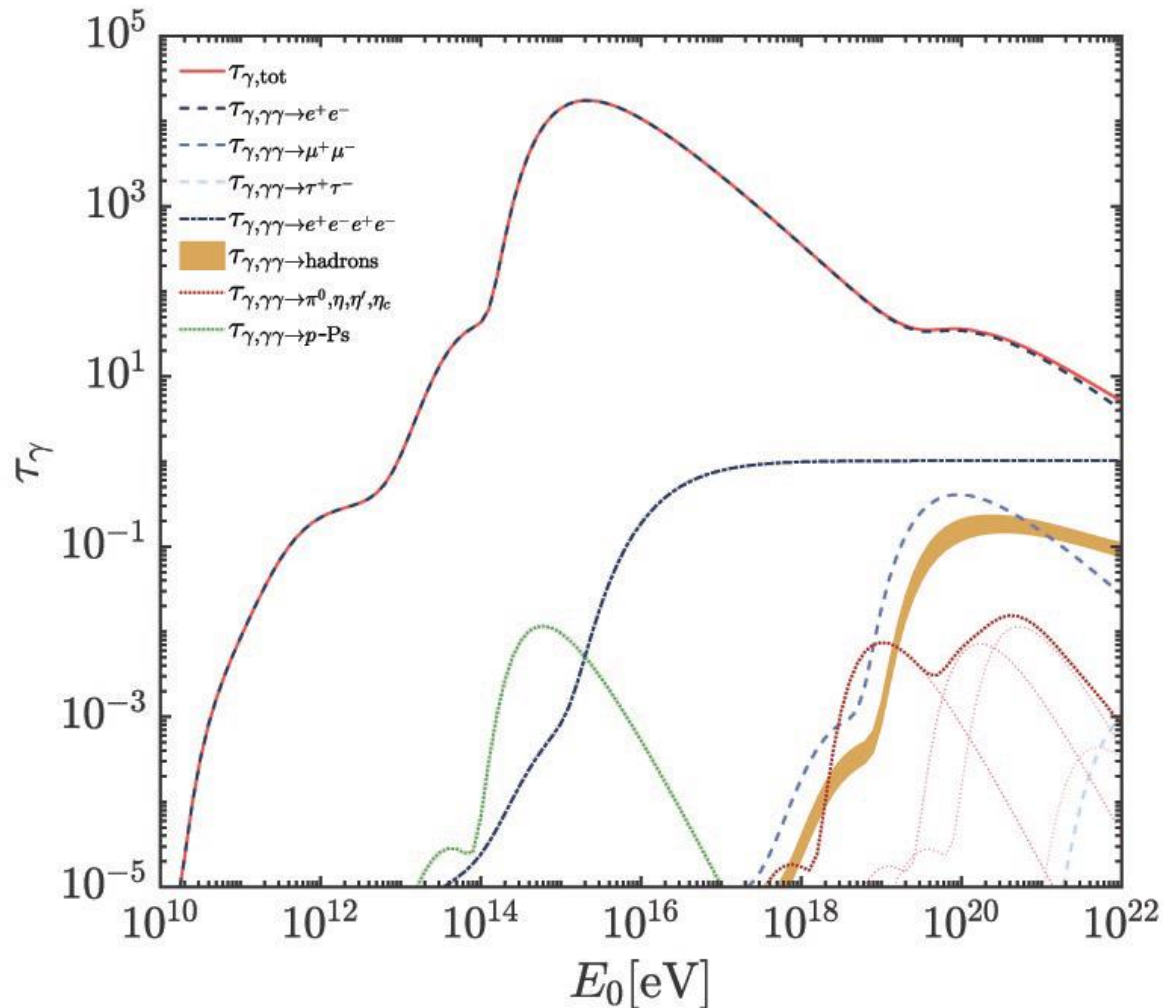
Calculation of the optical depth

- CM frame: $s_{\text{CM}} = 4\omega^2 \rightarrow$ generic frame: $s_{\text{gen}} = E \varepsilon (1 - \cos \varphi)$
 - $E \rightarrow$ incoming hard photon energy ($E_o \rightarrow$ observed energy)
 - $\varepsilon \rightarrow$ background photon energy
 - $\varphi \rightarrow$ angle between the two photon 3-momenta
- Optical depth τ_γ at a redshift z_s of a photon of energy $E = (1 + z_s)E_o$

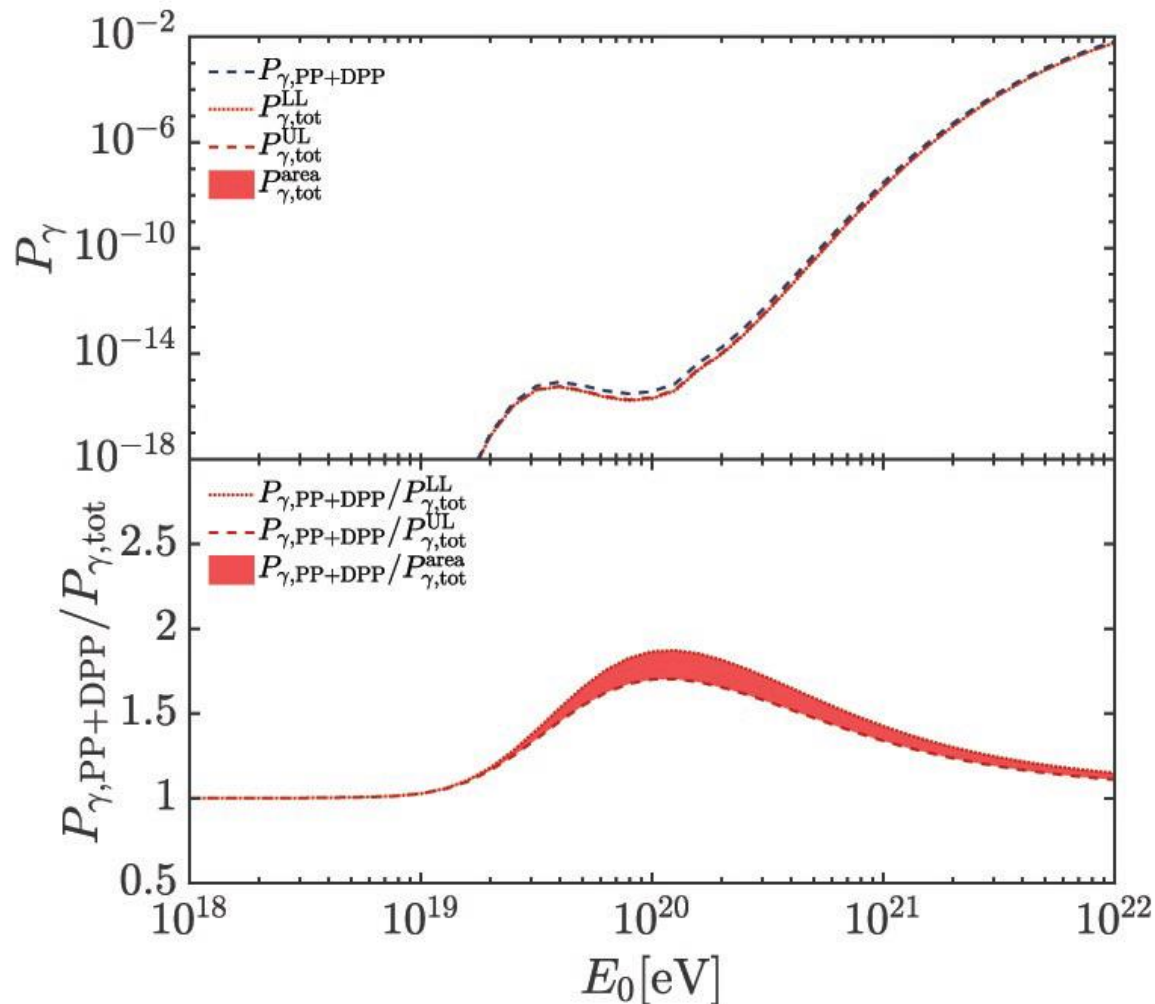
$$\tau_\gamma(E_o, z_s) = \int_0^{z_s} dz \frac{dl(z)}{dz} \int_{-1}^1 d(\cos \varphi) \frac{1 - \cos \varphi}{2} \int_{\varepsilon_{\text{thr}}(E(z), \varphi)}^{\infty} d\varepsilon(z) n_\gamma(\varepsilon(z), z) \sigma_{\gamma\gamma}(E(z), \varepsilon(z), \varphi)$$

- $dl(z) \rightarrow$ line element
- $n_\gamma \rightarrow$ background photon number density
- $\sigma_{\gamma\gamma} \rightarrow$ cross section of one of the considered processes $\gamma\gamma \rightarrow$ any
- $\varepsilon_{\text{thr}} = m_{\text{thr}}^2 / 2E(1 - \cos \varphi)$, $m_{\text{thr}} \rightarrow$ total mass of the produced particles
- Photon survival provability: $P_\gamma = e^{-\tau_\gamma}$

Optical depth $z_s = 0.03$ (≈ 130 Mpc)



Photon survival probability



Conclusions

Conclusions

- Already considered processes: $\gamma\gamma \rightarrow e^+e^-$ and $\gamma\gamma \rightarrow e^+e^-e^+e^-$
- $\gamma\gamma \rightarrow \mu^+\mu^-$ and $\gamma\gamma \rightarrow$ hadrons are not negligible in the UHE band and especially around 10^{20} eV
- Other processes are subdominant
- Some uncertainty in the hadronic sector
- Total optical depth $\tau_{\gamma,\text{tot}}$ changes by about 2%
- The photon survival probability $P_{\gamma,\text{tot}}$ modified by a factor of 2 at redshift $z_s = 0.03$ (≈ 130 Mpc)
- Upper limits of UHE photon flux should be accordingly modified

$$G_{rr} = R_{rr} - \frac{1}{2} R g_{rr} = \frac{8\pi G}{c^4} T_{rr}$$



$$S_B = \frac{k_B 4\pi G}{\hbar c} M^2$$

$$\Psi(x) = \frac{1}{\sqrt{2\pi}} (A_+ e^{ikx} + A_- e^{-ikx}) \quad x < 0$$

$$k = \sqrt{2mE/\hbar^2}$$

$$R_{rr} - \frac{1}{2} R g_{rr} + \Lambda g_{rr} = \frac{8\pi G}{c^4} T_{rr}$$

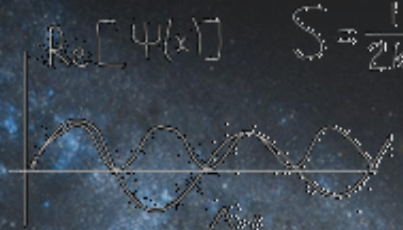
$$\partial = \frac{2\pi i \hbar^2}{\hbar^2 (1-\beta)}$$



$$S = \frac{e^2 k A}{4\hbar c}$$

$$H = \frac{P P}{2m} + V(x)$$

$$P = -i\hbar \nabla$$



$$S = \frac{1}{2k} \int R \sqrt{-g} dx$$

$$L = \text{tr} \left[\frac{1}{g} F_{\mu\nu} F^{\mu\nu} - i\lambda \Gamma^{\mu} D_{\mu} \lambda \right]$$

Thank you

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$E = \frac{p^2}{2m} + (mc^2)$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{\lambda} = \frac{h}{\lambda}$$

$$S = \frac{1}{2} \int d^4x \left(P - \frac{P^2}{8\pi^2} \right)$$



$$A_{ij} = \frac{8\pi h \nu^3}{c^3} B_{ij}$$

$$S_{fi} = \langle f | S | i \rangle$$

$$dY = e^{-\frac{m^2 c^2}{\hbar^2} V(X_{cc})} dr_o(X_s) \frac{\partial u}{\partial X} dW$$

$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=0}^{\infty} \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

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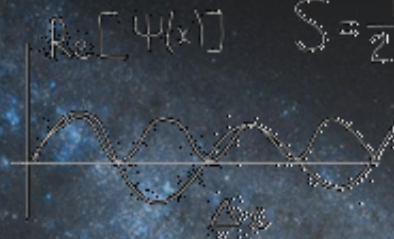
$$\sigma = \frac{2\pi \hbar^2 k^2}{m^2 (1-\sigma)}$$



$$S = \frac{e^2 k A}{4\hbar c}$$

$$H = \frac{P P}{2m} + V(x)$$

$$P = -i\hbar \nabla$$



$$S = \frac{1}{2\hbar} \int R \sqrt{-g} dx$$

$$L = \text{tr} \left[\frac{1}{g} F_{\mu\nu} F^{\mu\nu} - i\lambda \Gamma^{\mu} D_{\mu} \lambda \right]$$

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$\frac{\delta(\hbar \cdot \hbar^2)}{\hbar^2}$$

$$E = mc^2$$

$$E^2 = (pc)^2 + (mc^2)^2$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

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