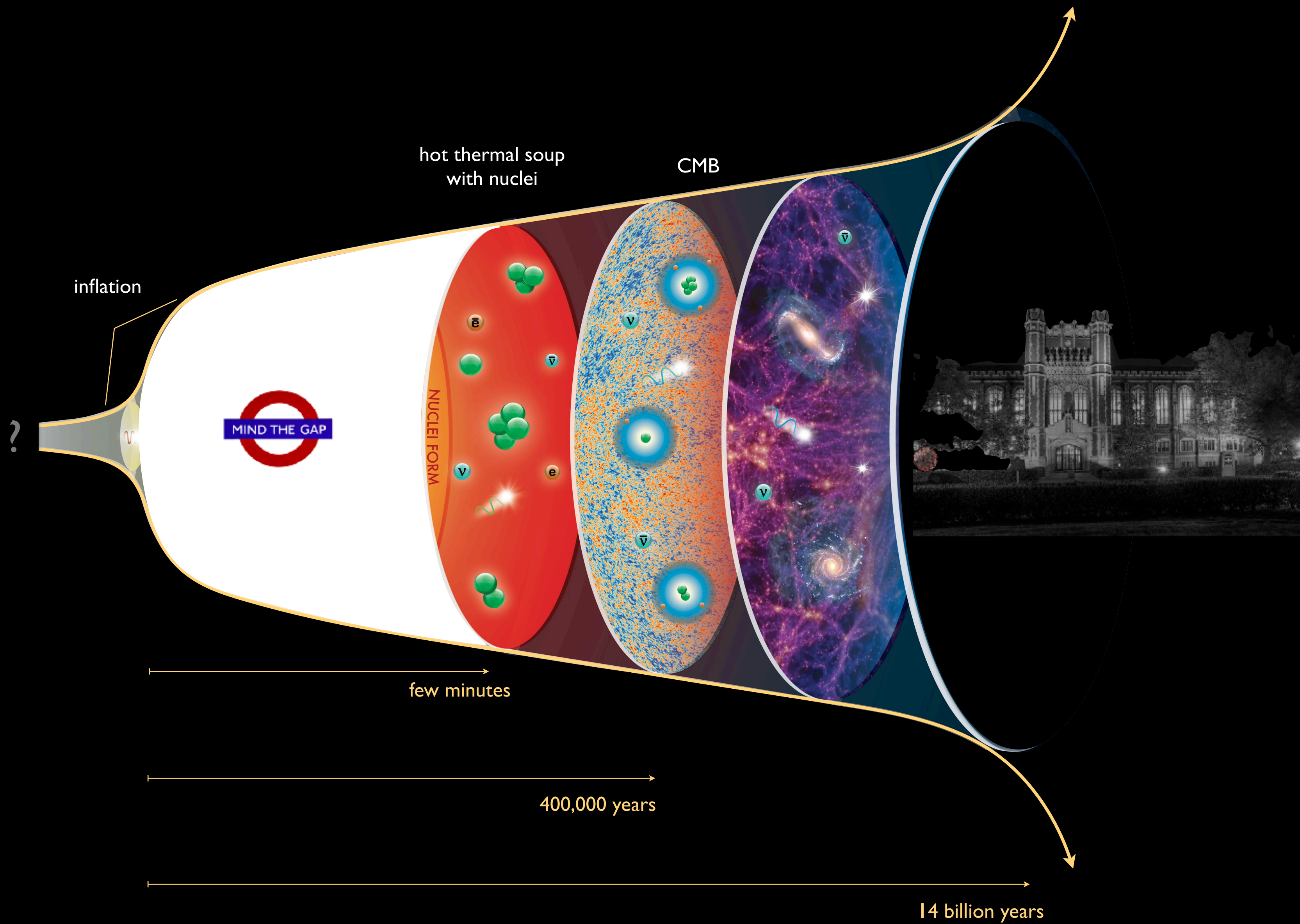




Inflation Ends, What's Next?

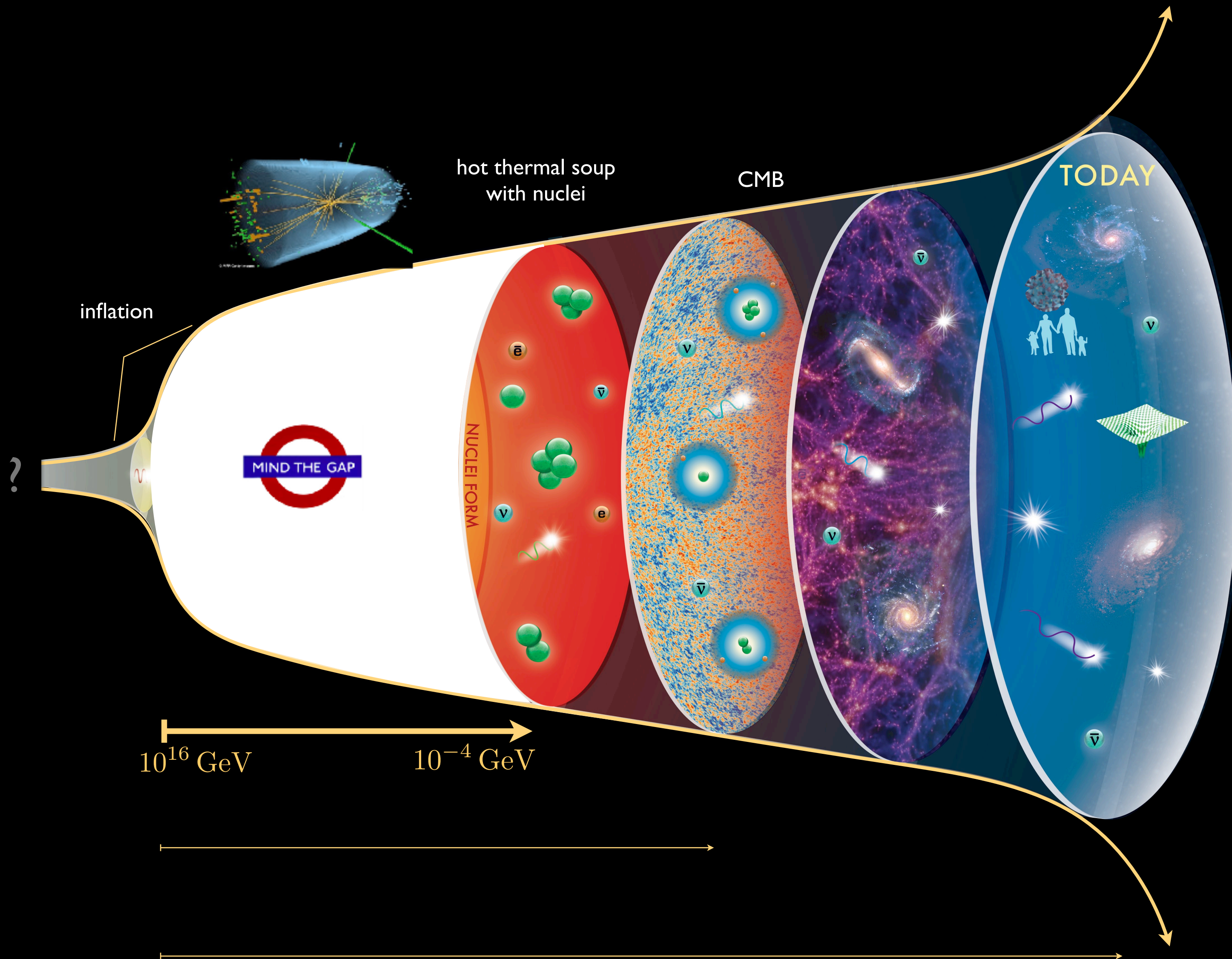
Mustafa A. Amin ( RICE University)

after inflation: a GAP in our cosmic history



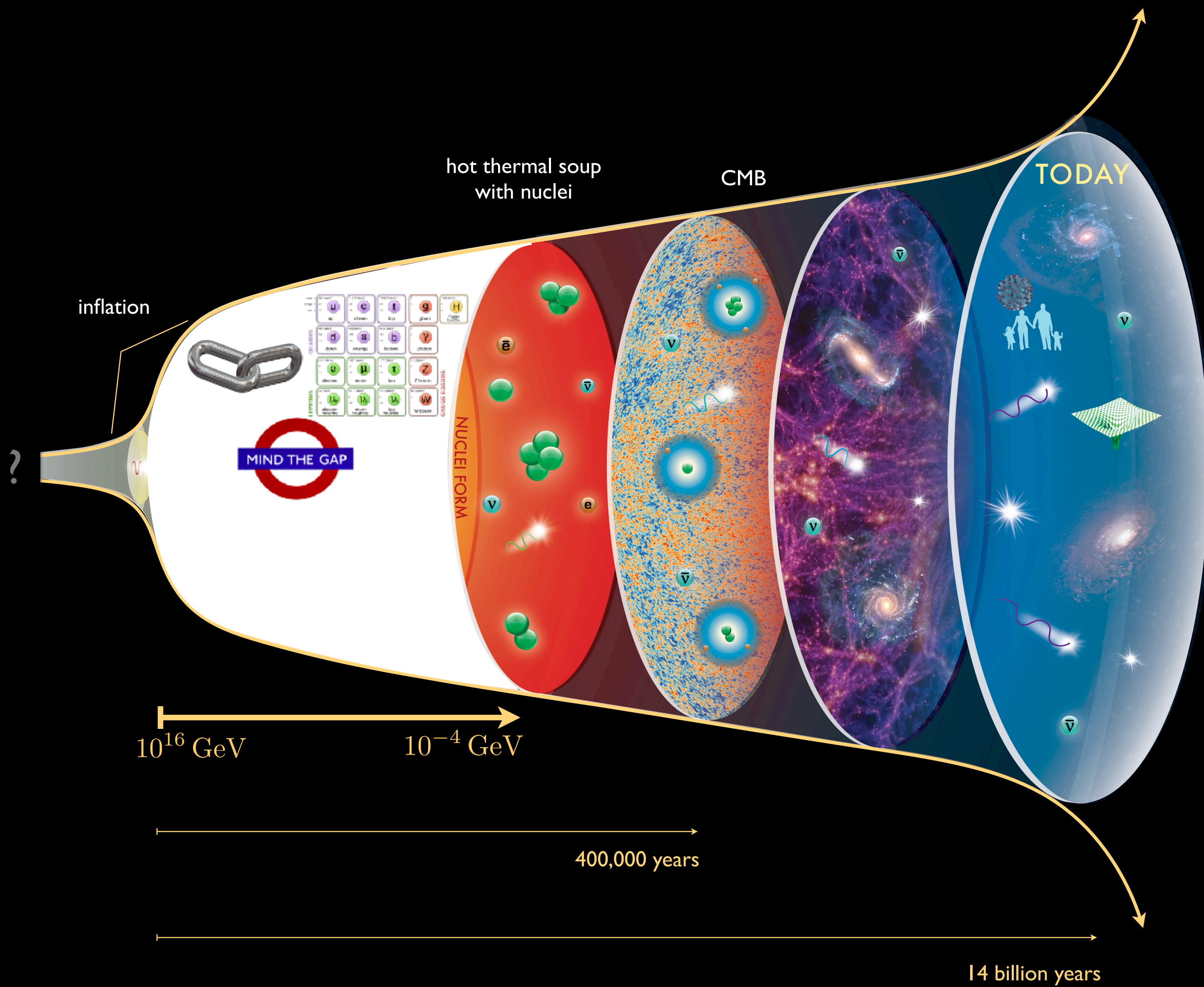
*image is my modification of the one produced by the PDG, 2014

after inflation: a huge energy GAP in our cosmic history

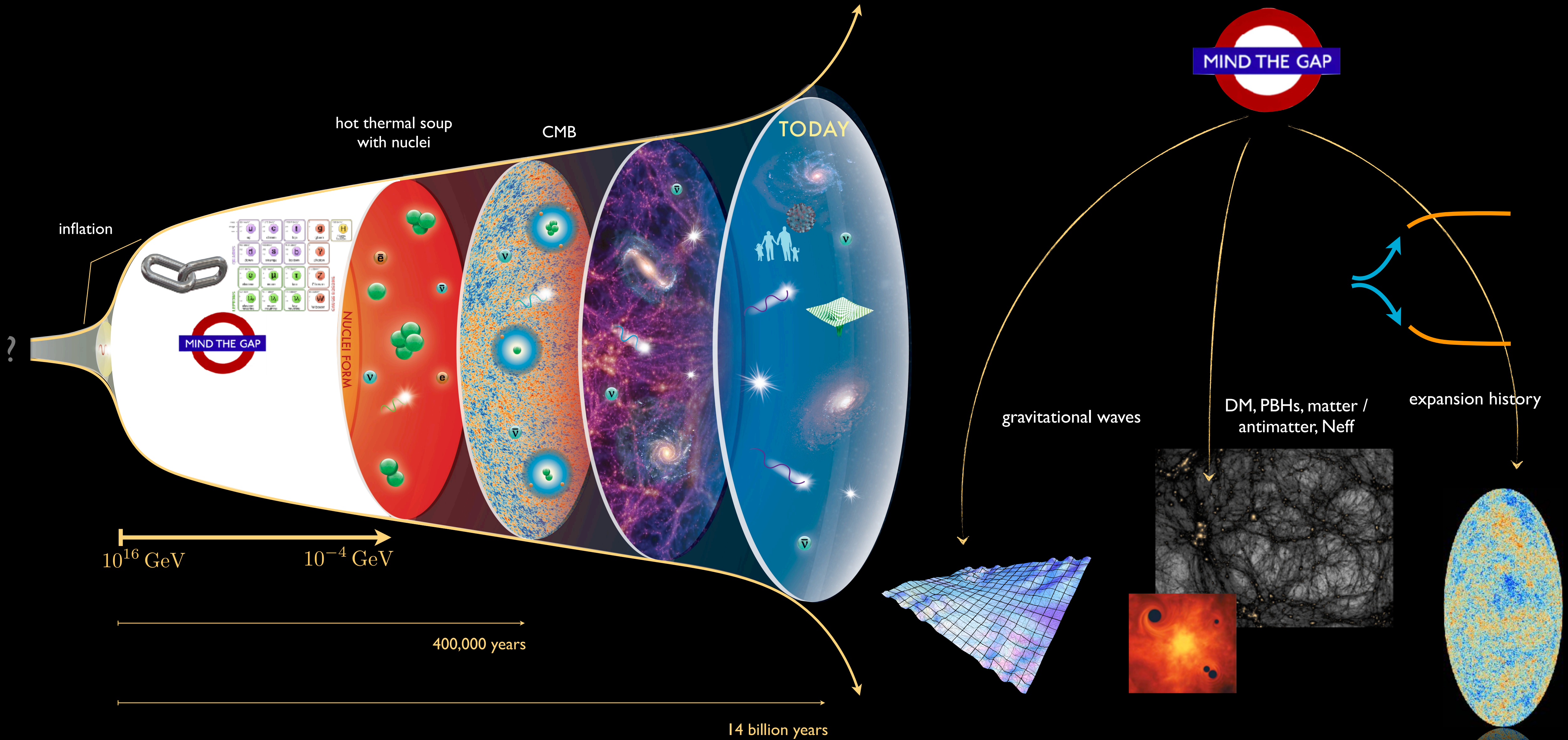


*image is my modification of the one produced by the PDG, 2014

after inflation: GAP — connects physics of inflation to the Standard Model

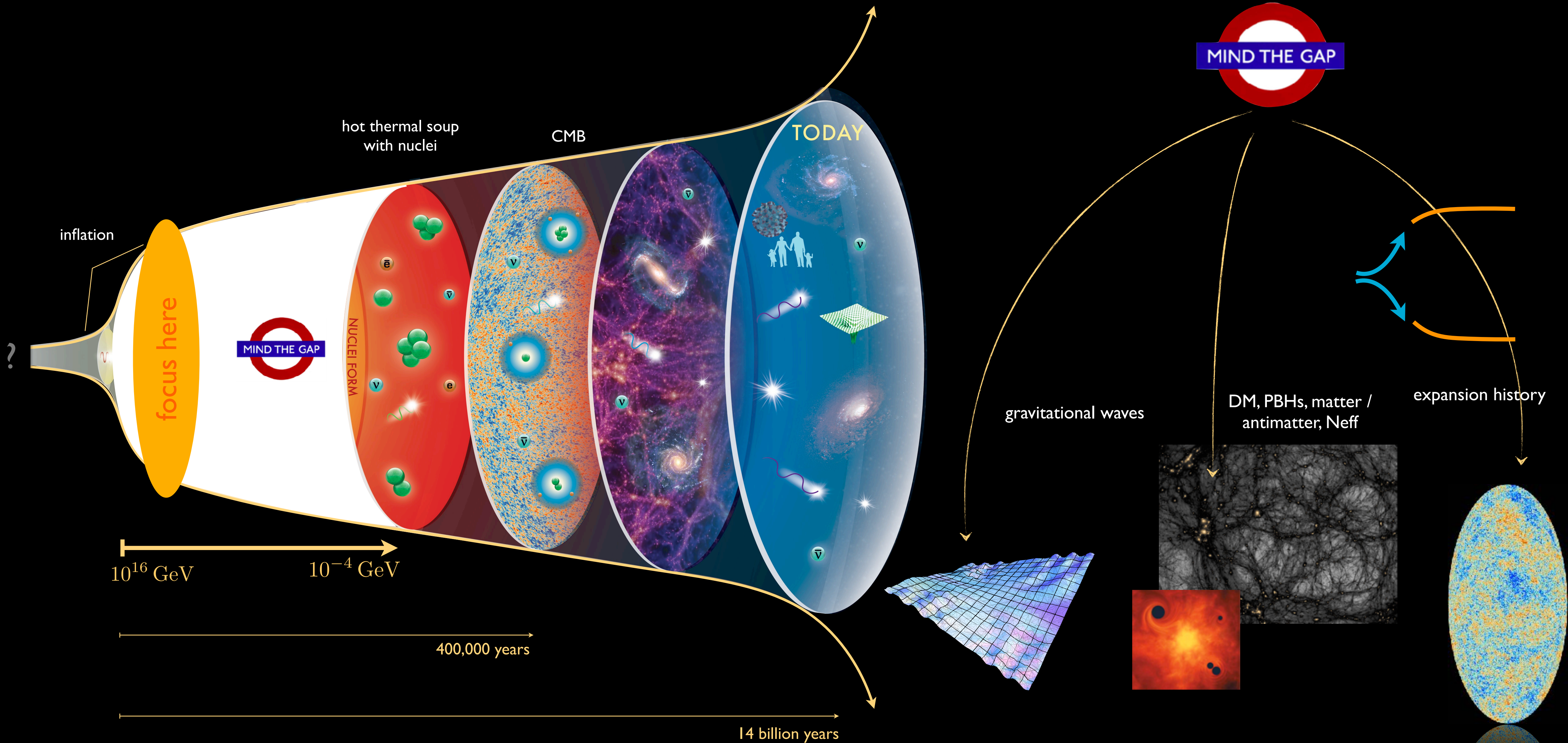


after inflation: GAP — consequences ?



Observationally challenging because: early times and small length scales (no inflationary “amplifier”), thermalization etc. But there is hope !

focus on: "soon" after the end of inflation, simple models with "universal" dynamics



For reviews: see MA et. al (2014), Lozanov (2019), Allahverdi et. al (2020)

2104.10128

1907.04402

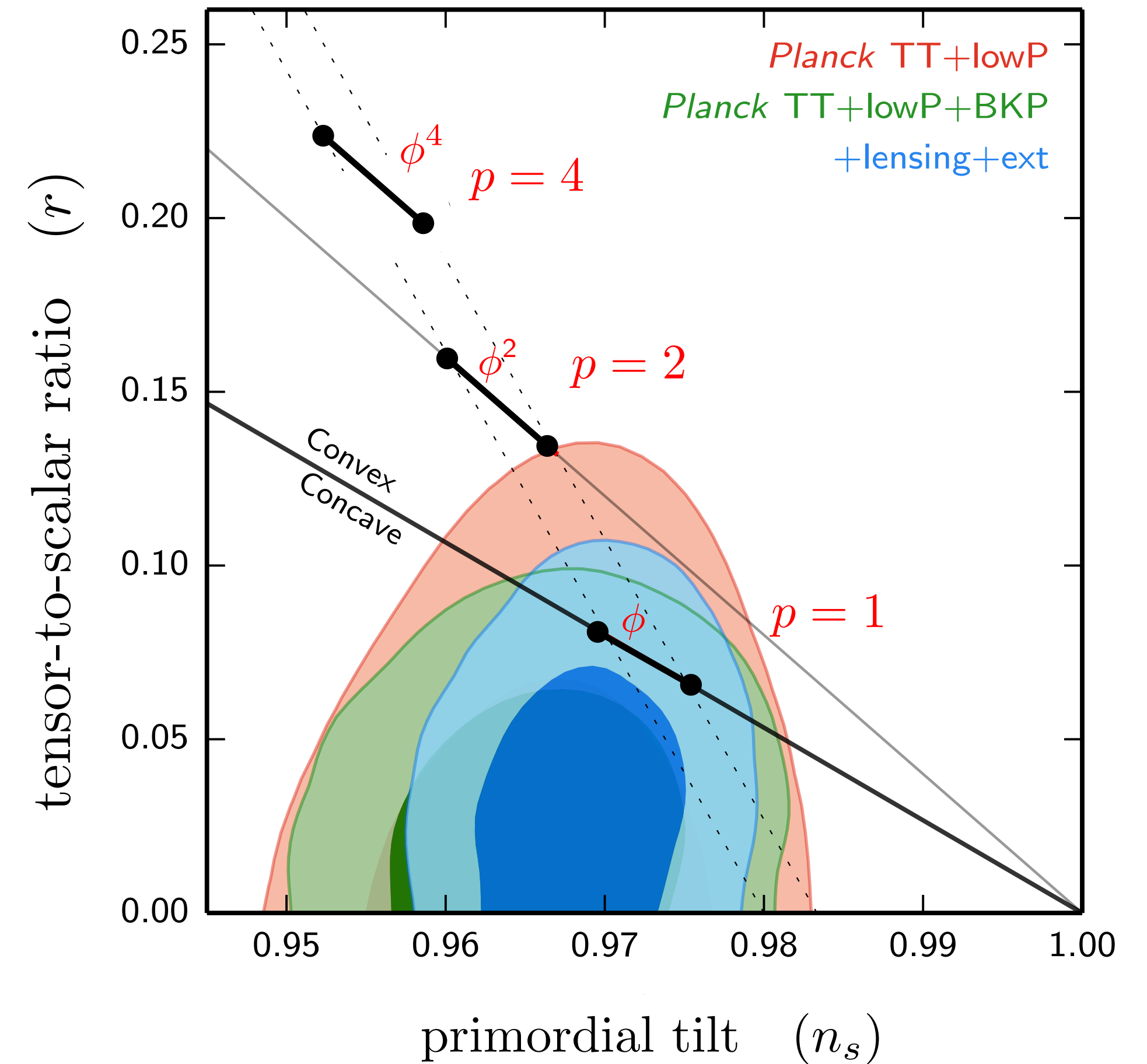
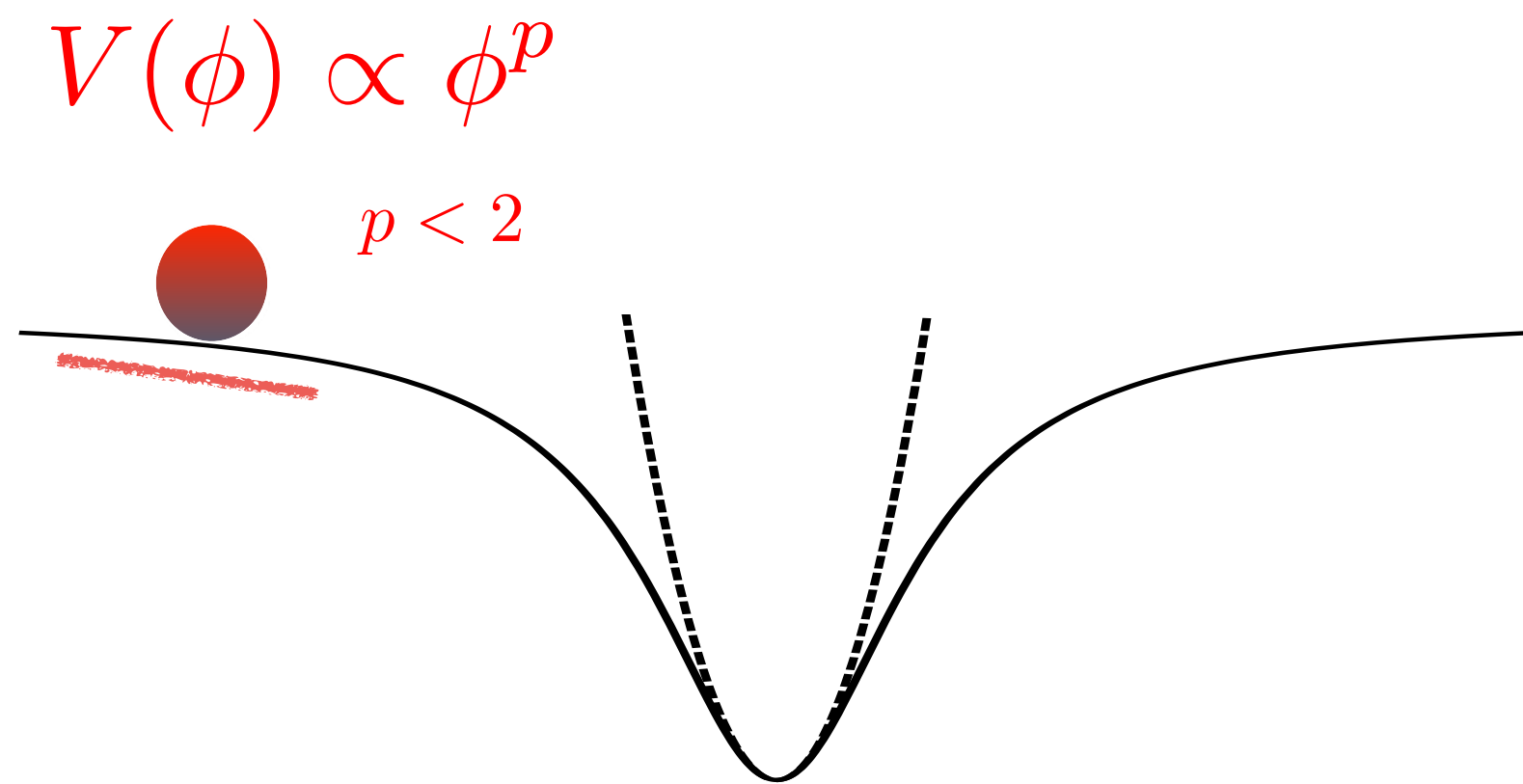
2006.16182

[with apologies for works which I will be unable to cite/highlight]

what we “know” about inflation (simplest case - scalar field driven inflation)

— flattened potentials

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) \right]$$

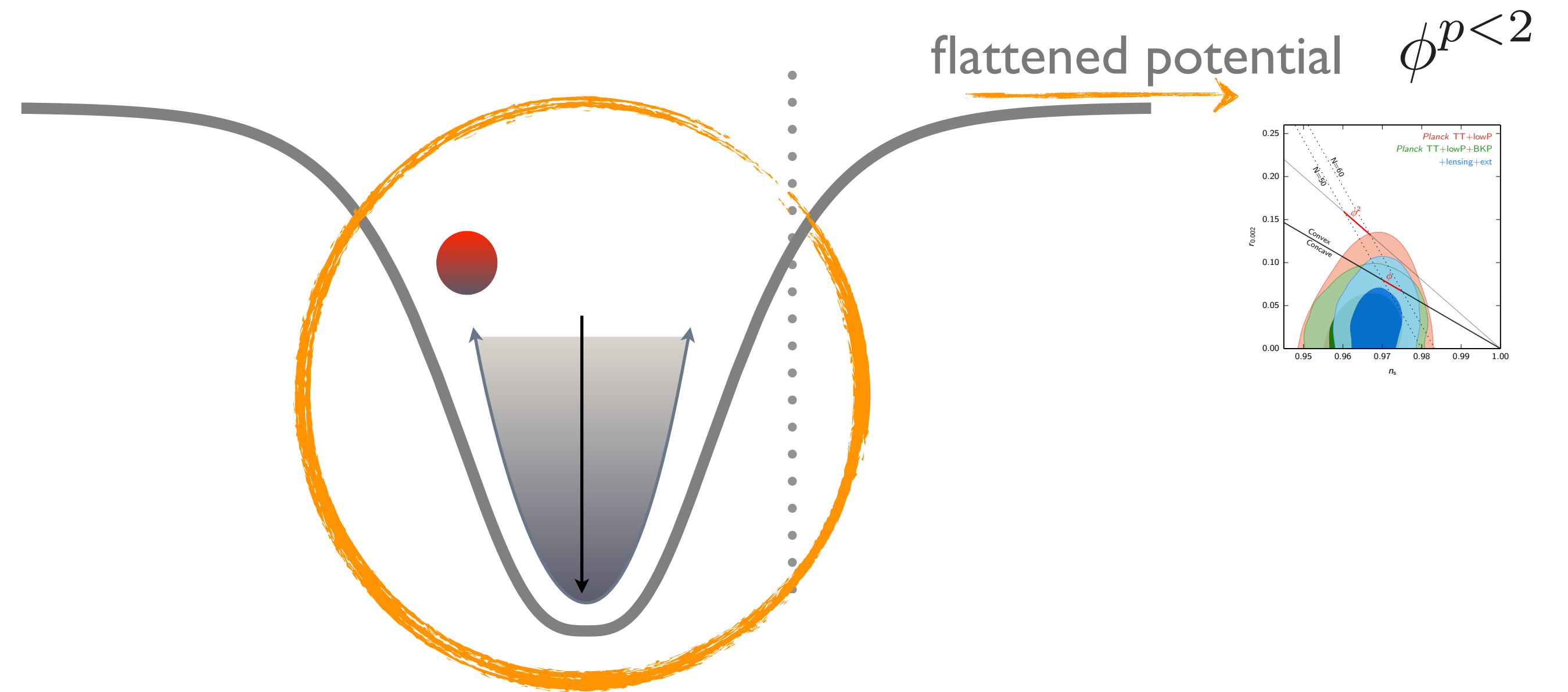


end of inflation ?

- shape of the potential (self couplings)
- couplings to other fields



χ, ψ, A_μ

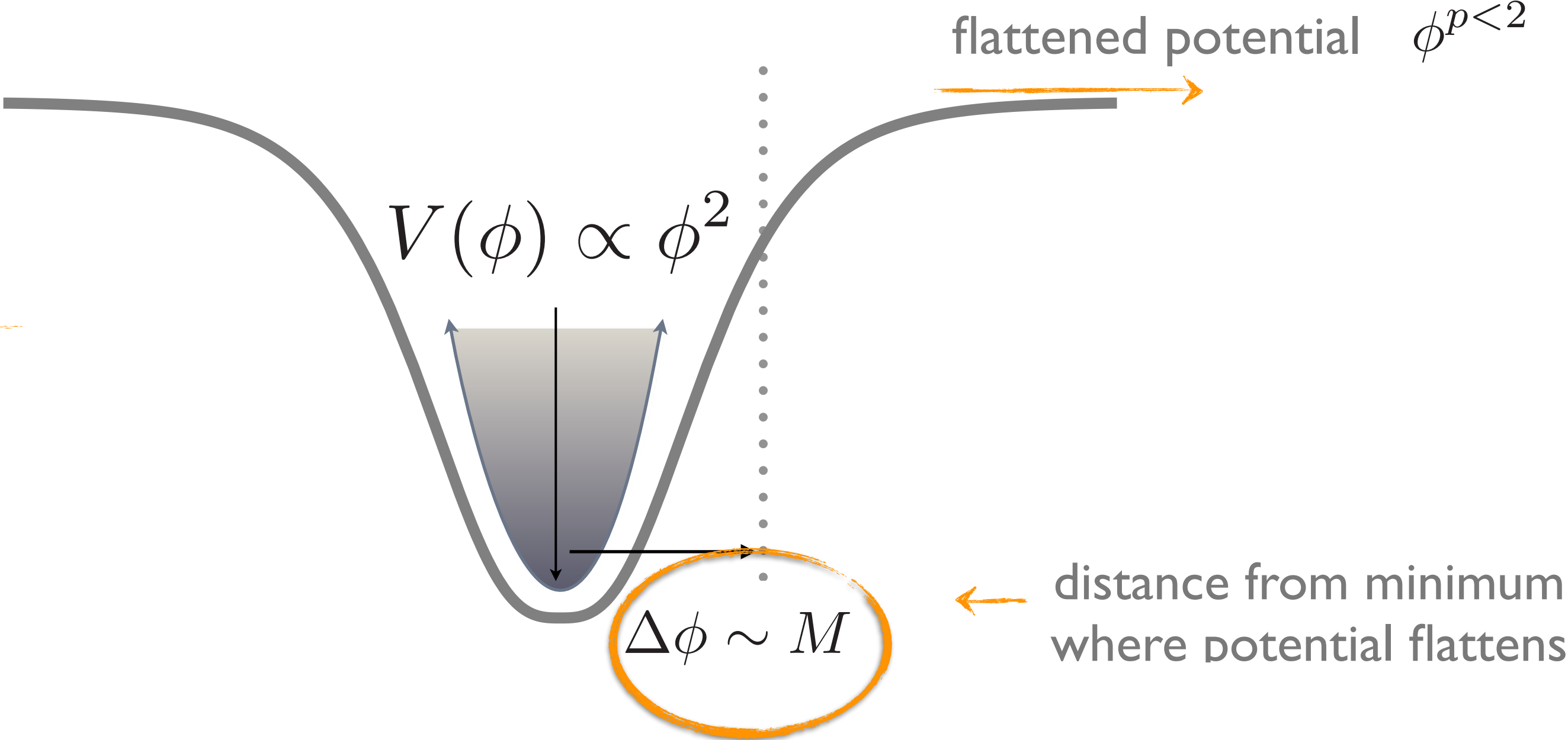


end of inflation (simplest)

- shape of the potential (self couplings)
- ~~couplings to other fields~~



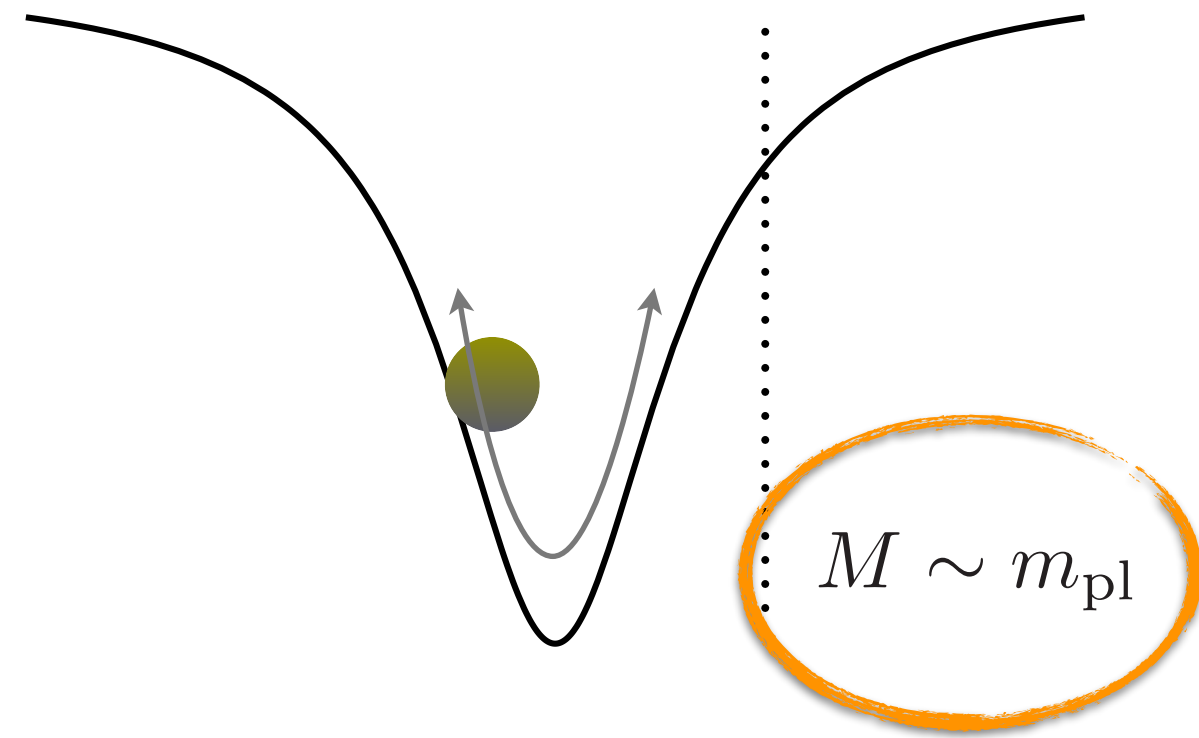
~~χ, ψ, A_μ~~



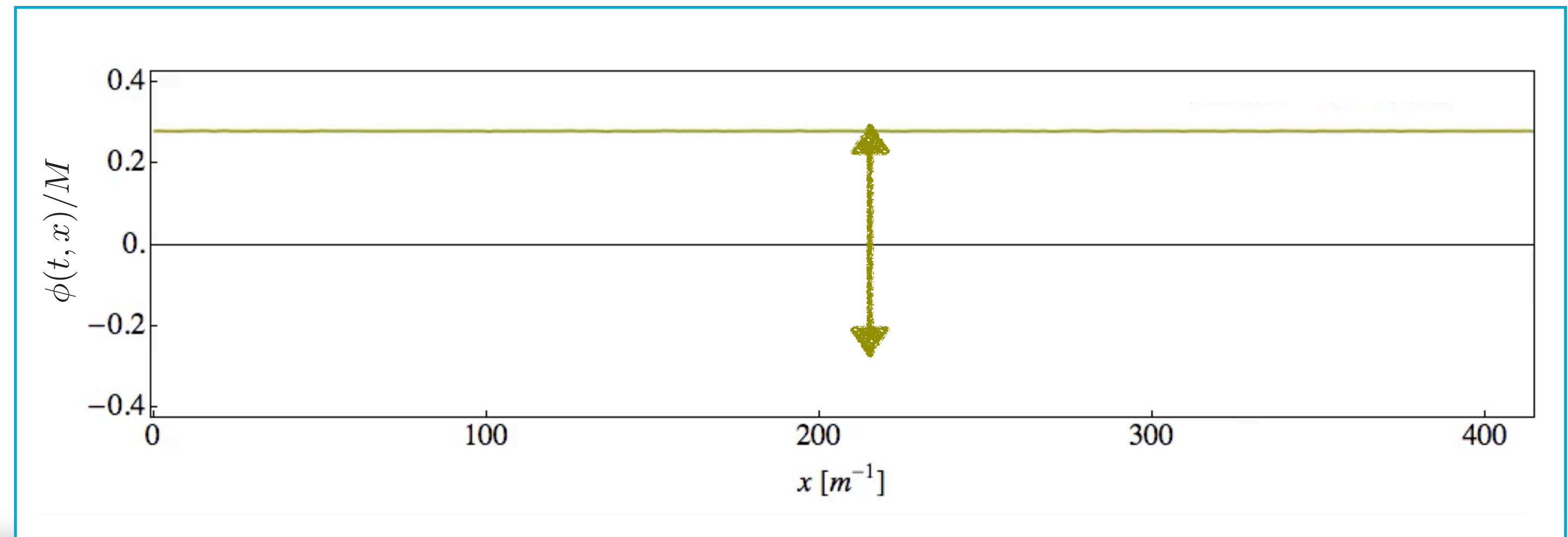
*there will still be gravitational particle production of other fields, see for example Kolb & Long (2021) and earlier papers

oscillating “free” scalar field: matter-dominated expansion + “slow” gravitational instability

- expansion ✓
- self-interactions ✗
- gravitational int. ✓



$$\square\phi \approx m^2\phi$$

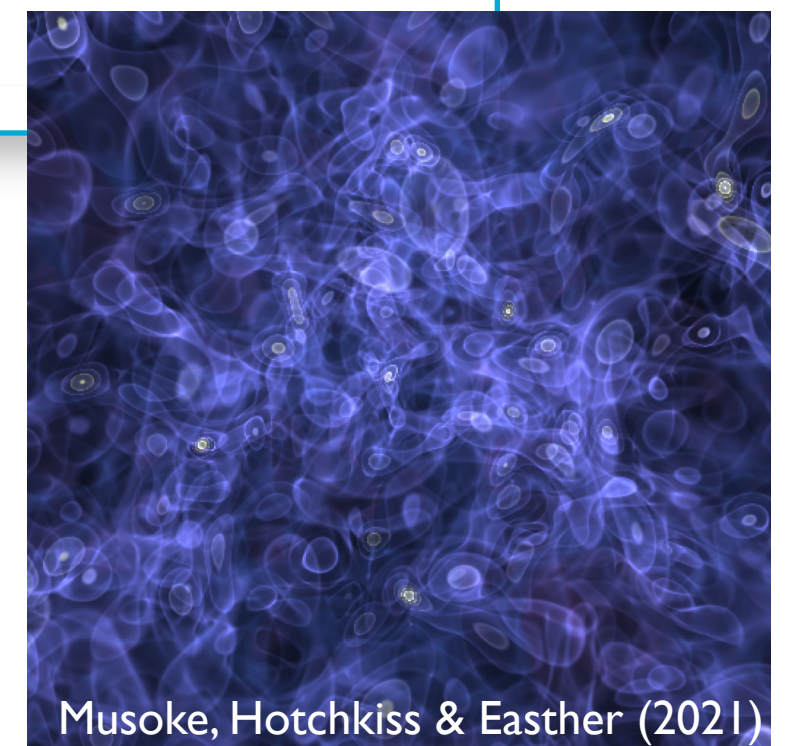
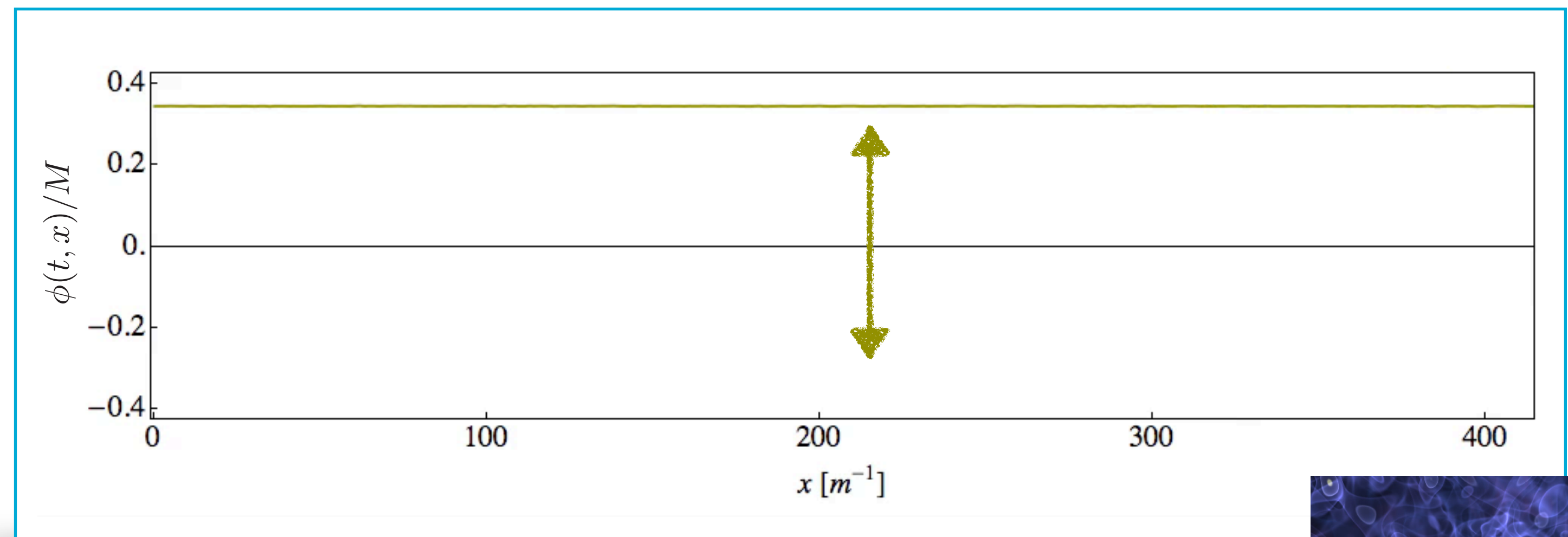
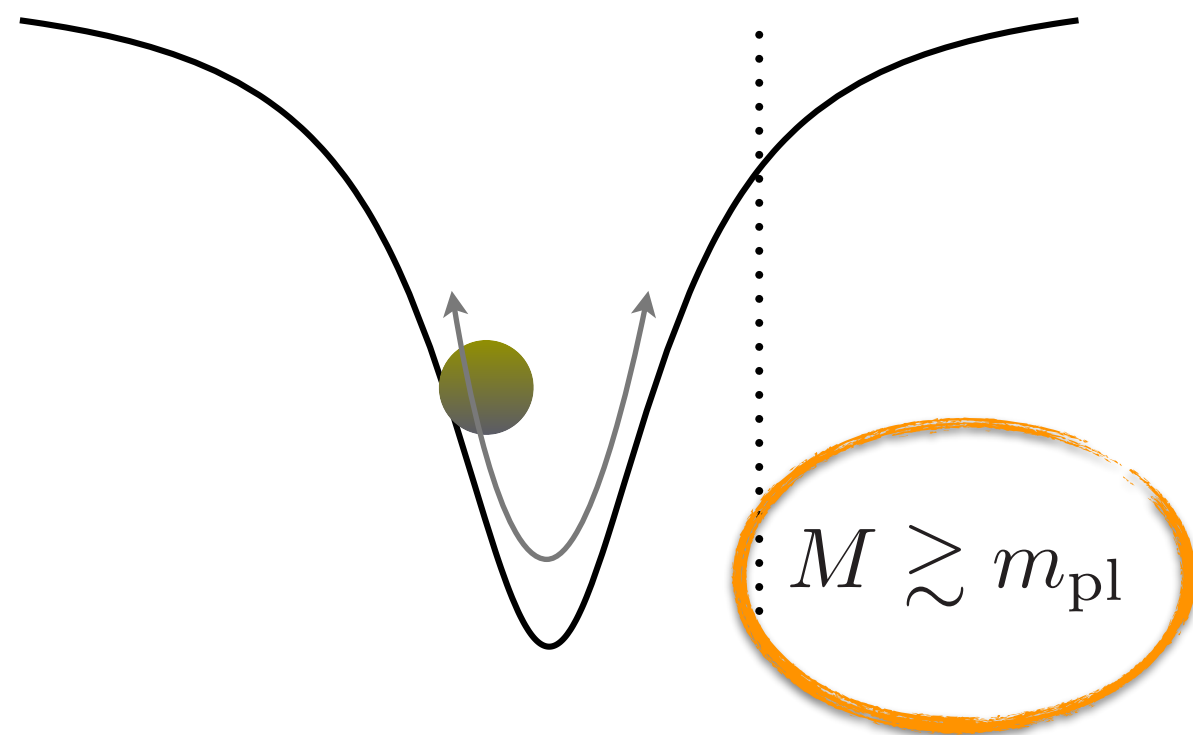


$$w \rightarrow 0$$

oscillating “free” scalar field: matter-dominated expansion + “slow” gravitational instability

- expansion ✓
- self-interactions ✗
- gravitational int. ✓

$$\square\phi \approx m^2\phi$$



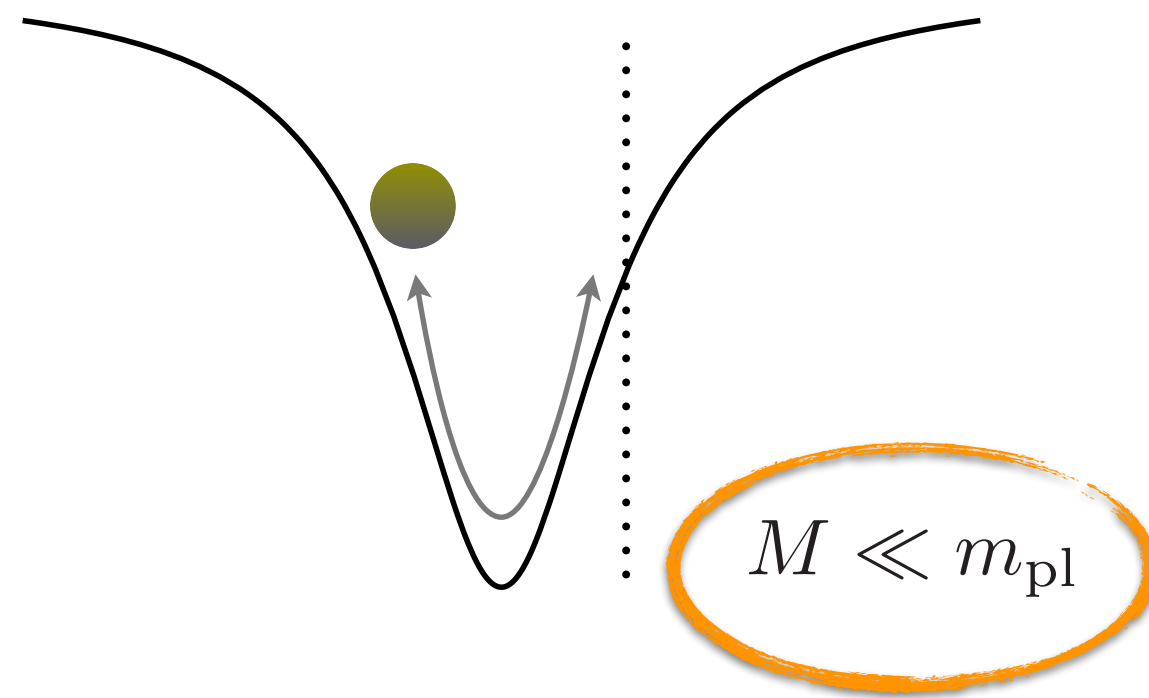
Musoke, Hotchkiss & Easter (2021)

*similar to a matter dominated universe, also see [Adrienne Erikcek's](#) talk

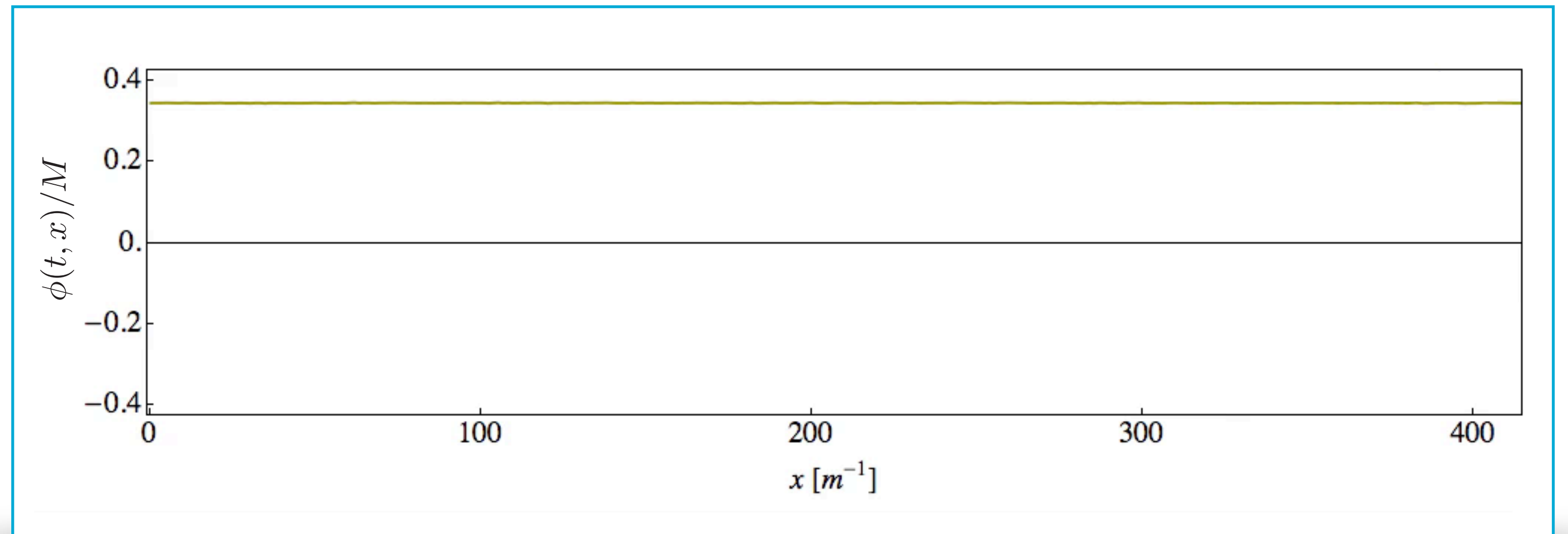
*also see [N. Musoke's](#) talk

oscillating scalar field: self-interaction driven fast instability & “oscillon” formation

- expansion ✓
- self-interactions ✓
- gravitational int. ✗



$$\square\phi = V'(\phi)$$

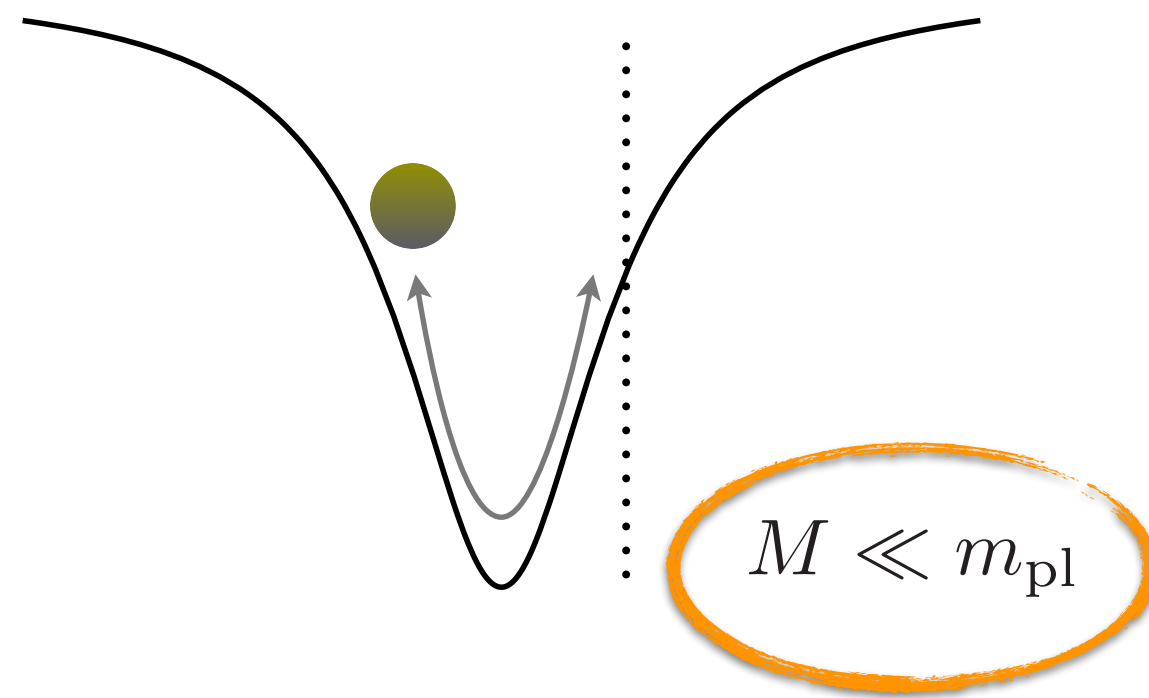


MA (2010) 1006.3075

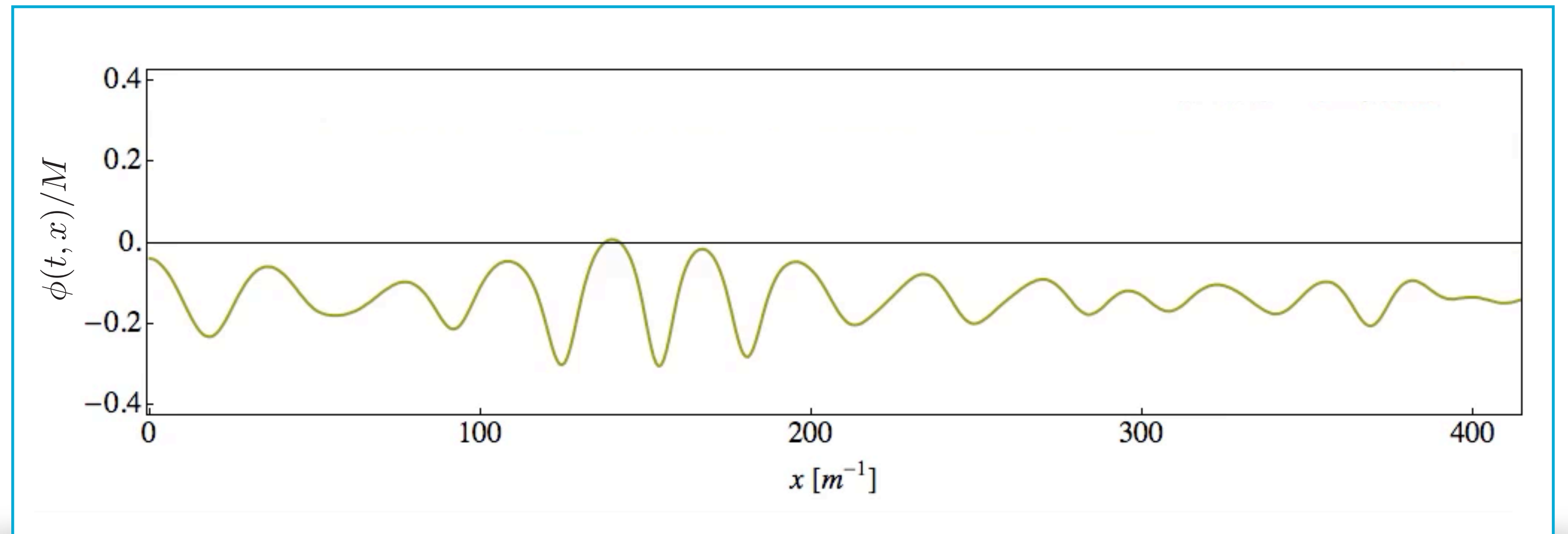
*without oscillons, but relevant for instabilities, see related (much) earlier work: Khlopov, Malomed & Zeldovich (1985)

oscillating scalar field: self-interaction driven fast instability & “oscillon” formation

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- self-interactions ✓
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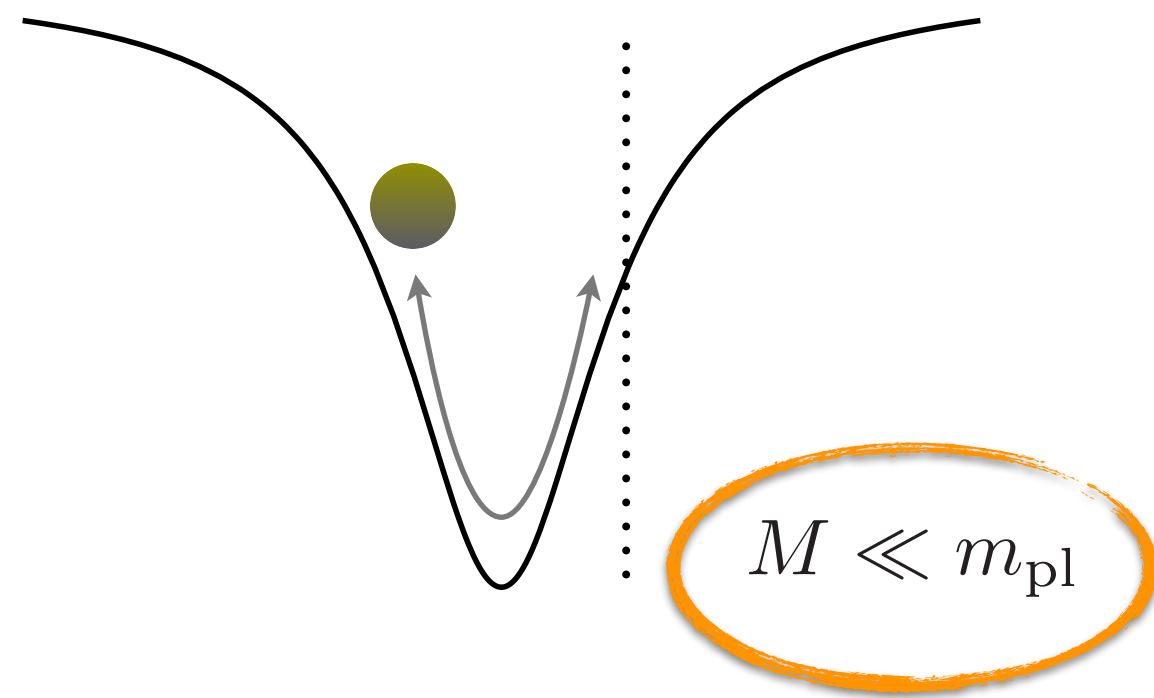


MA (2010) 1006.3075

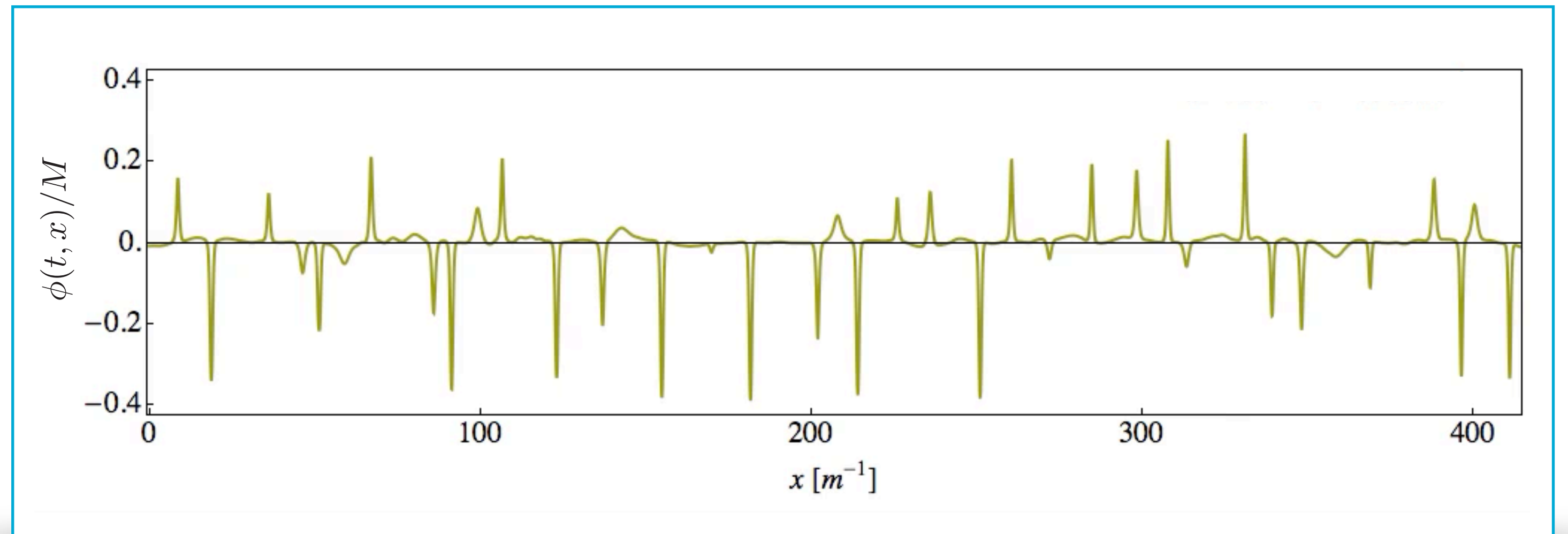
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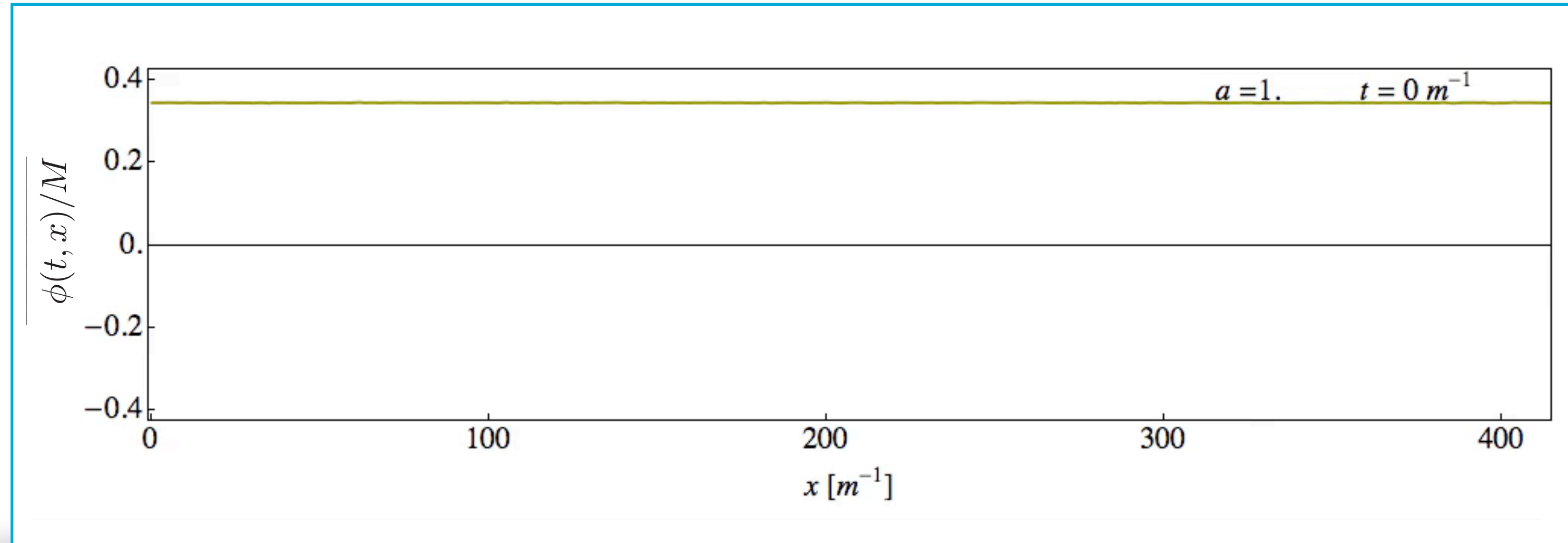
$$\square\phi = V'(\phi)$$



MA (2010) 1006.3075

*without oscillons, but relevant for instabilities, see related (much) earlier work: Khlopov, Malomed & Zeldovich (1985)

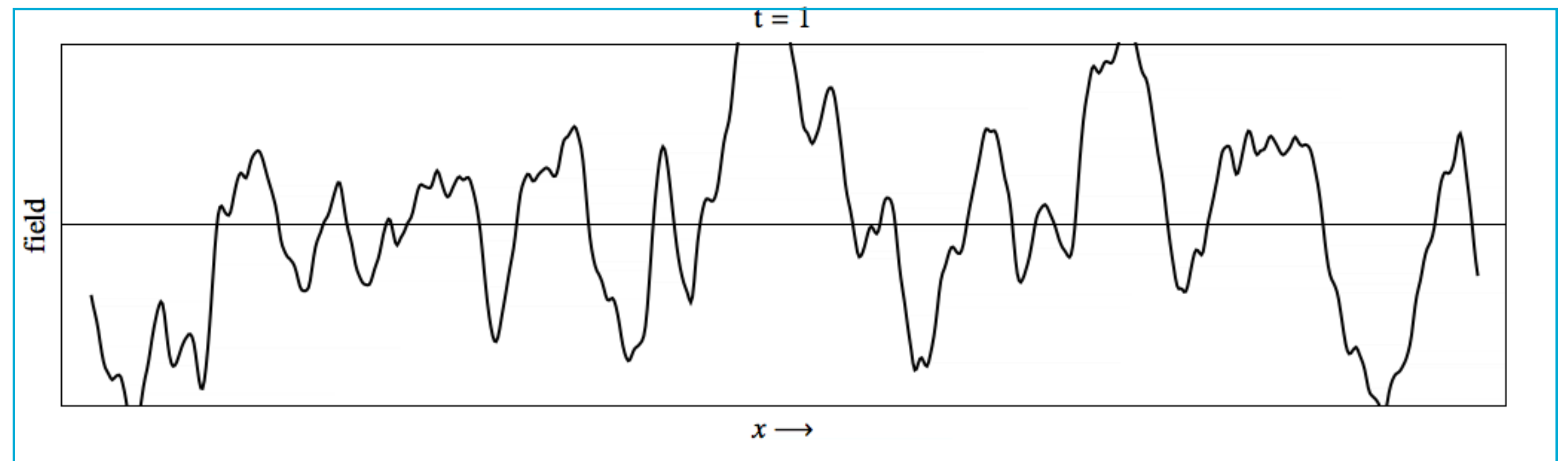
insensitivity to initial conditions



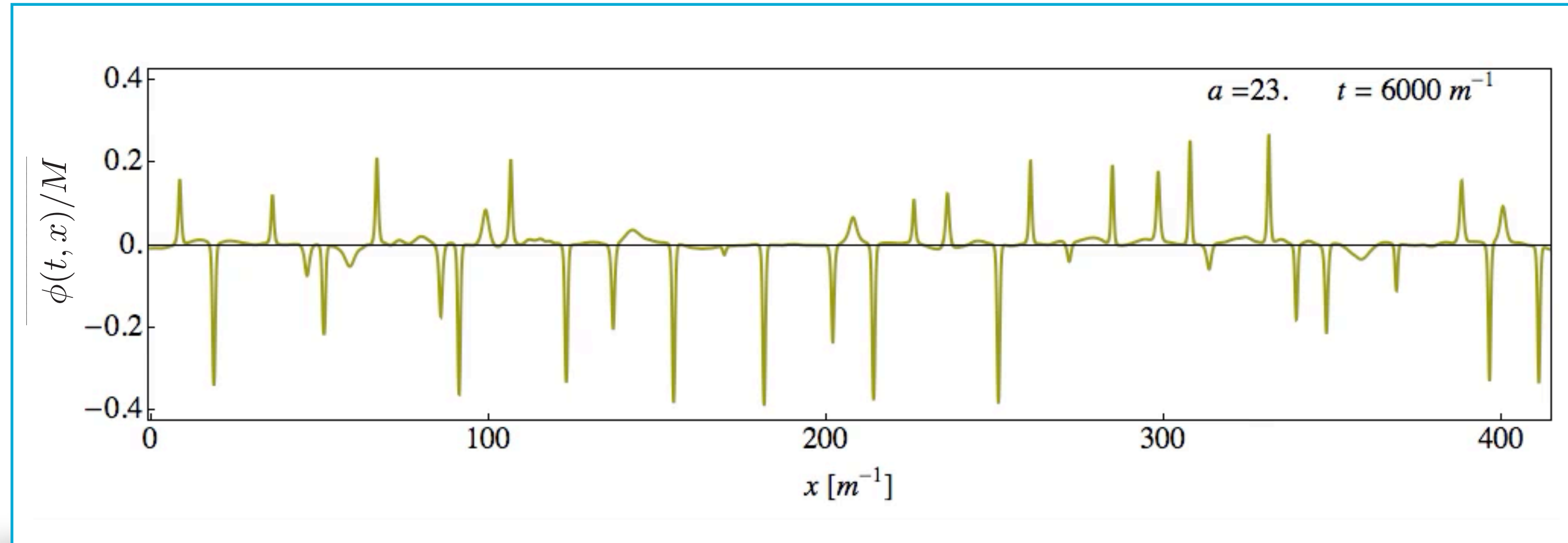
MA (2010)

instability growth rate/Hubble > 1

based on Farhi et. al (2008)



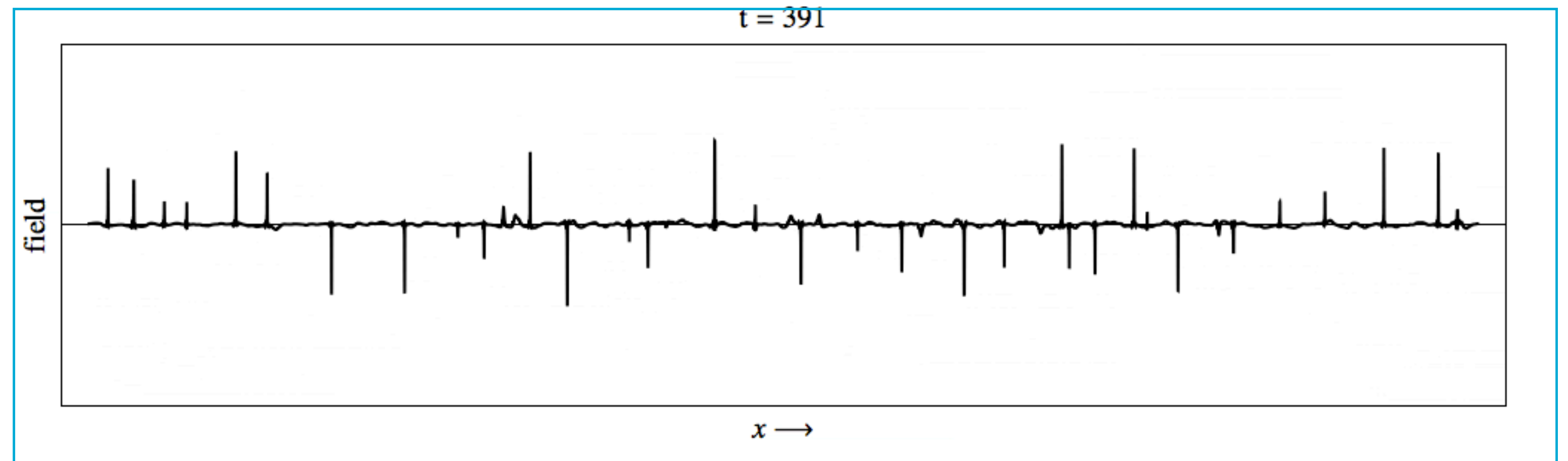
insensitivity to initial conditions



MA (2010)

instability growth rate/Hubble > 1

based on Farhi et. al (2008)

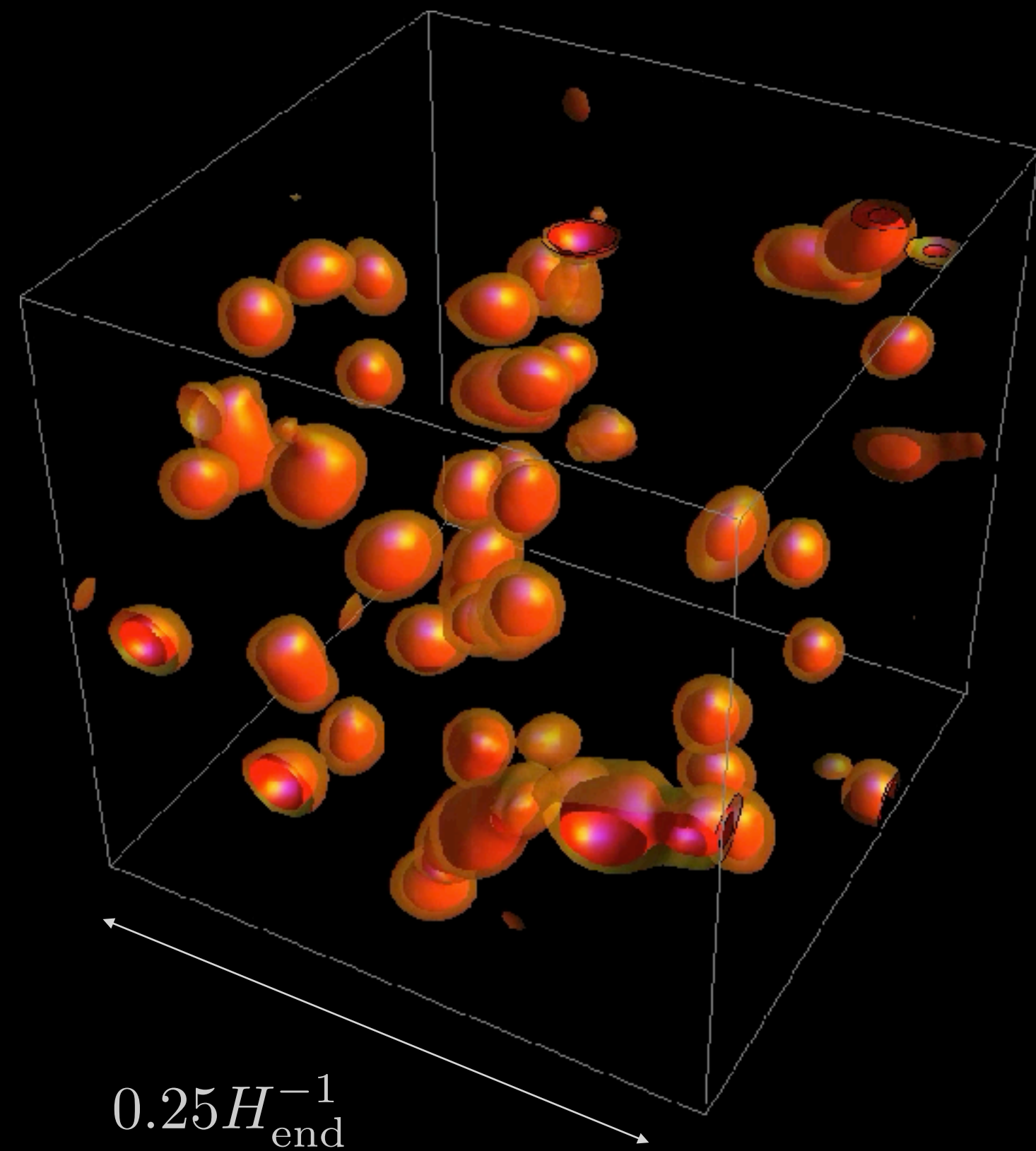


oscillating scalar field: self-interaction driven fast instability & “oscillon” formation

expansion

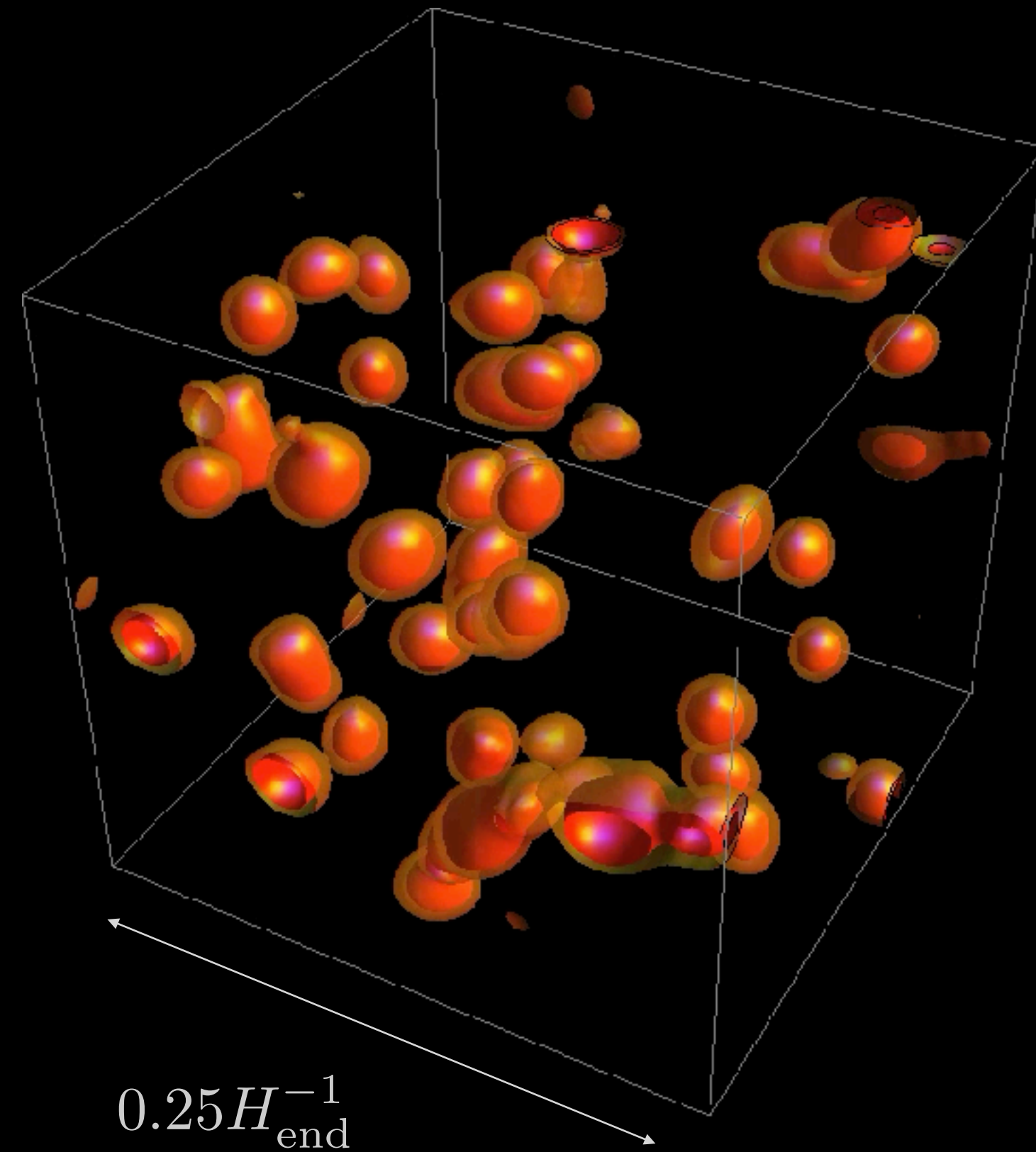
self-interactions ✓

gravitational int. ✗



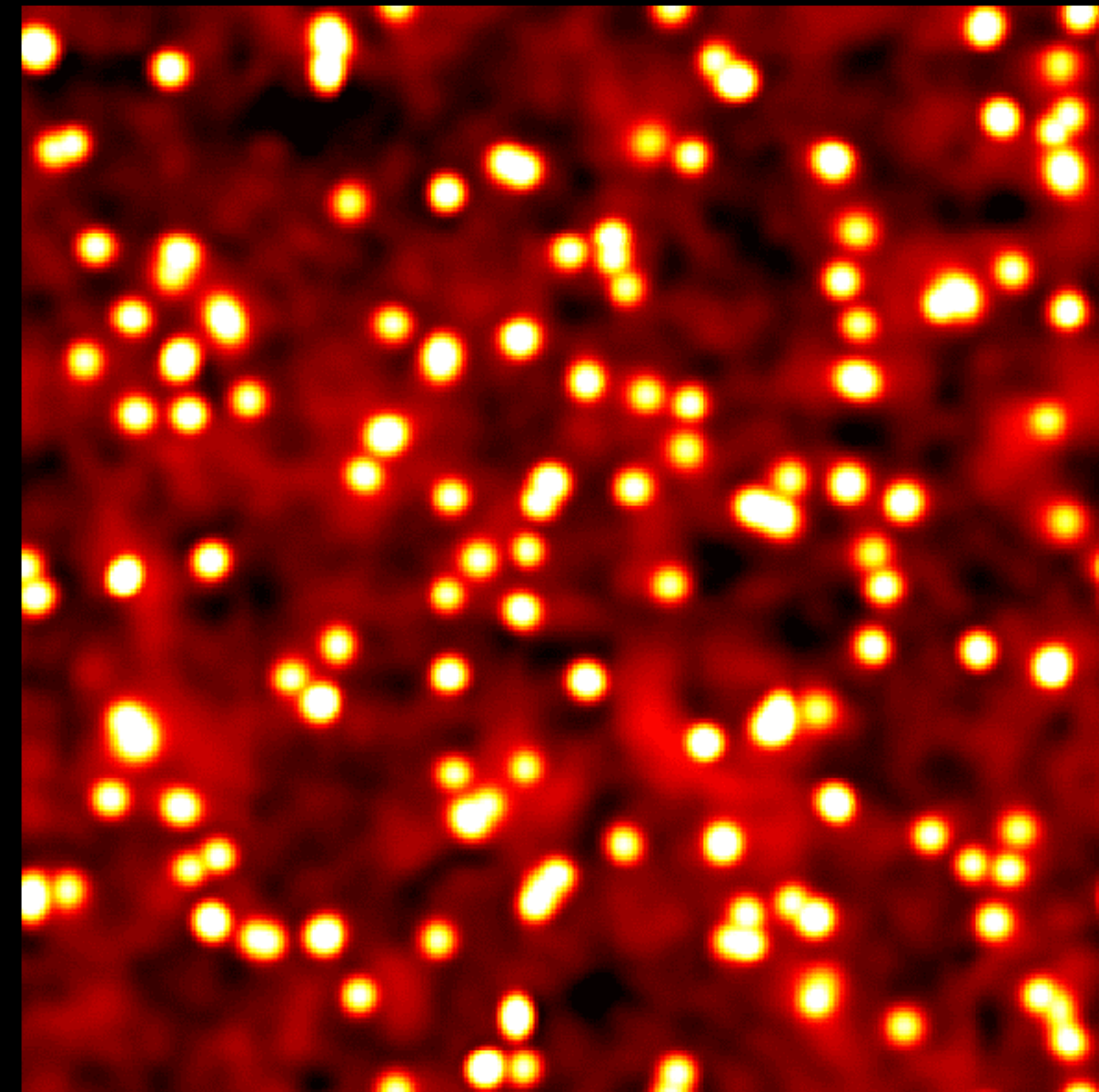
self-interaction driven fast instability & “oscillon” formation + gravitational clustering

- expansion ✓
- self-interactions ✓
- gravitational int. ✗



MA, Easter, Finkel, Flauger & Hertzberg (2011) 1106.3335

- expansion ✓
- self-interactions ✓
- gravitational int. ✓

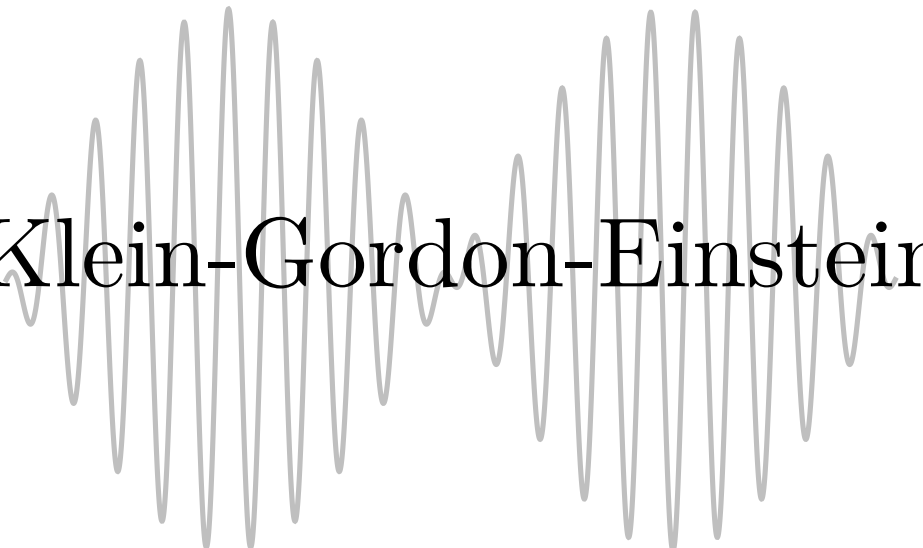


MA & Mocz (2019) 1902.07261

* non-relativistic, Schrodinger-Poisson

relativistic to non-relativistic effective theory

Klein-Gordon-Einstein



integrate out 'fast' modes



Nonrelativistic EFT for 'slow' modes
= Schrödinger-Poisson + corrections



solitons : oscillons

spatially localized

coherently oscillating

exceptionally long-lived

For example:

Bogolubsky & Makhankov (1976)

Gleiser (1994)

Copeland et al. (1995)

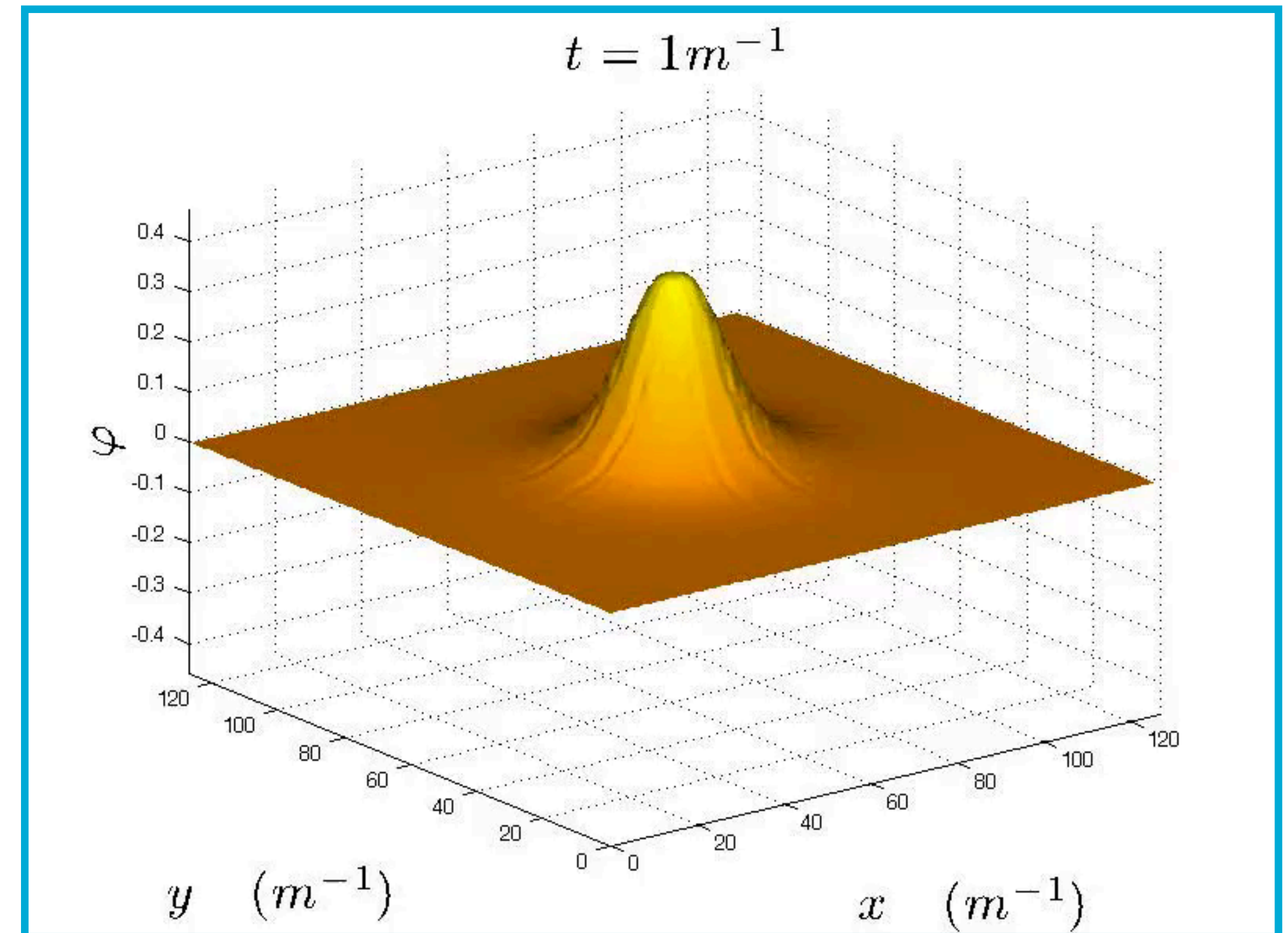
MA & Shirokoff (2010)

Hertzberg (2011)

MA (2013)

Mukaida et. al (2016)

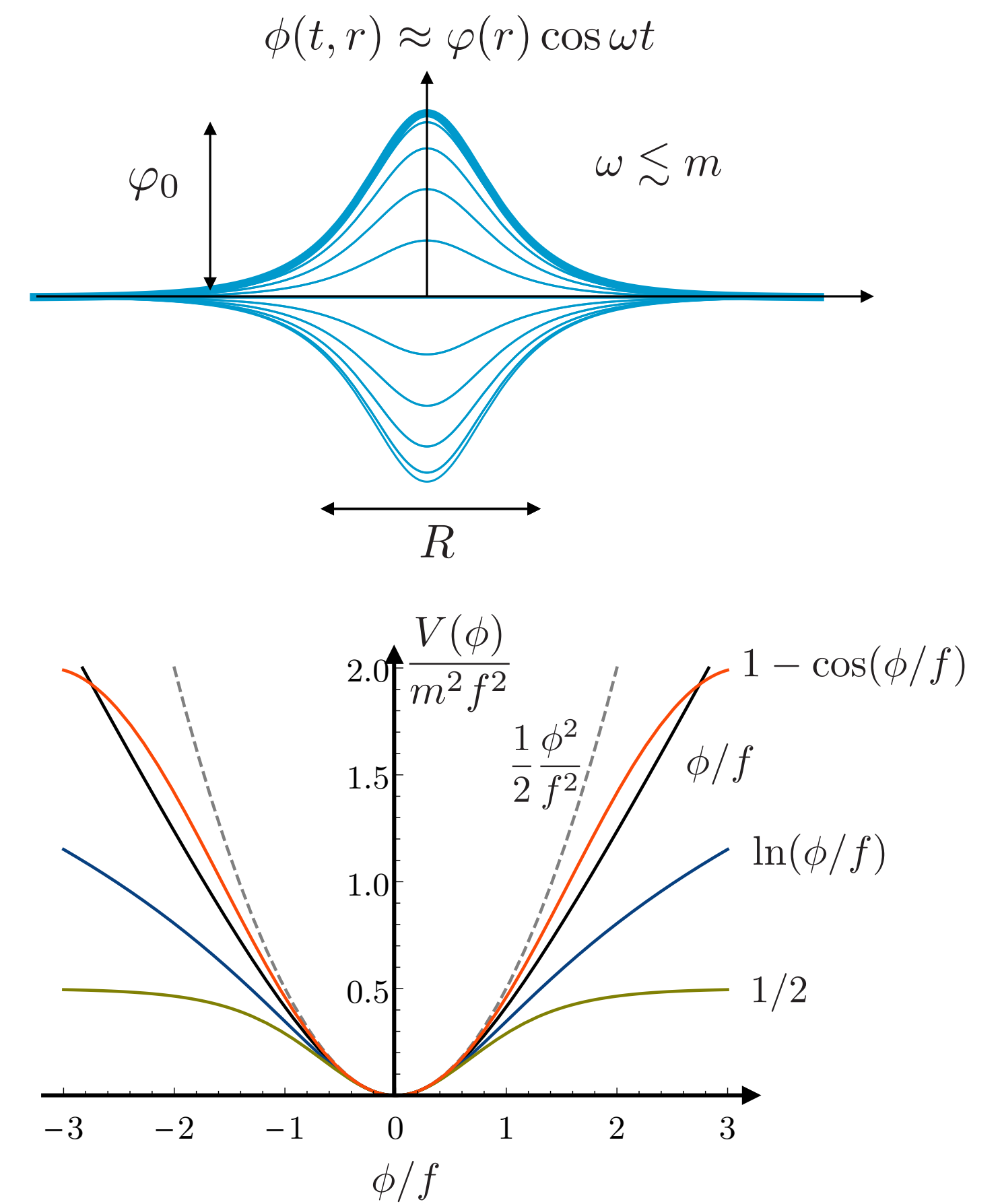
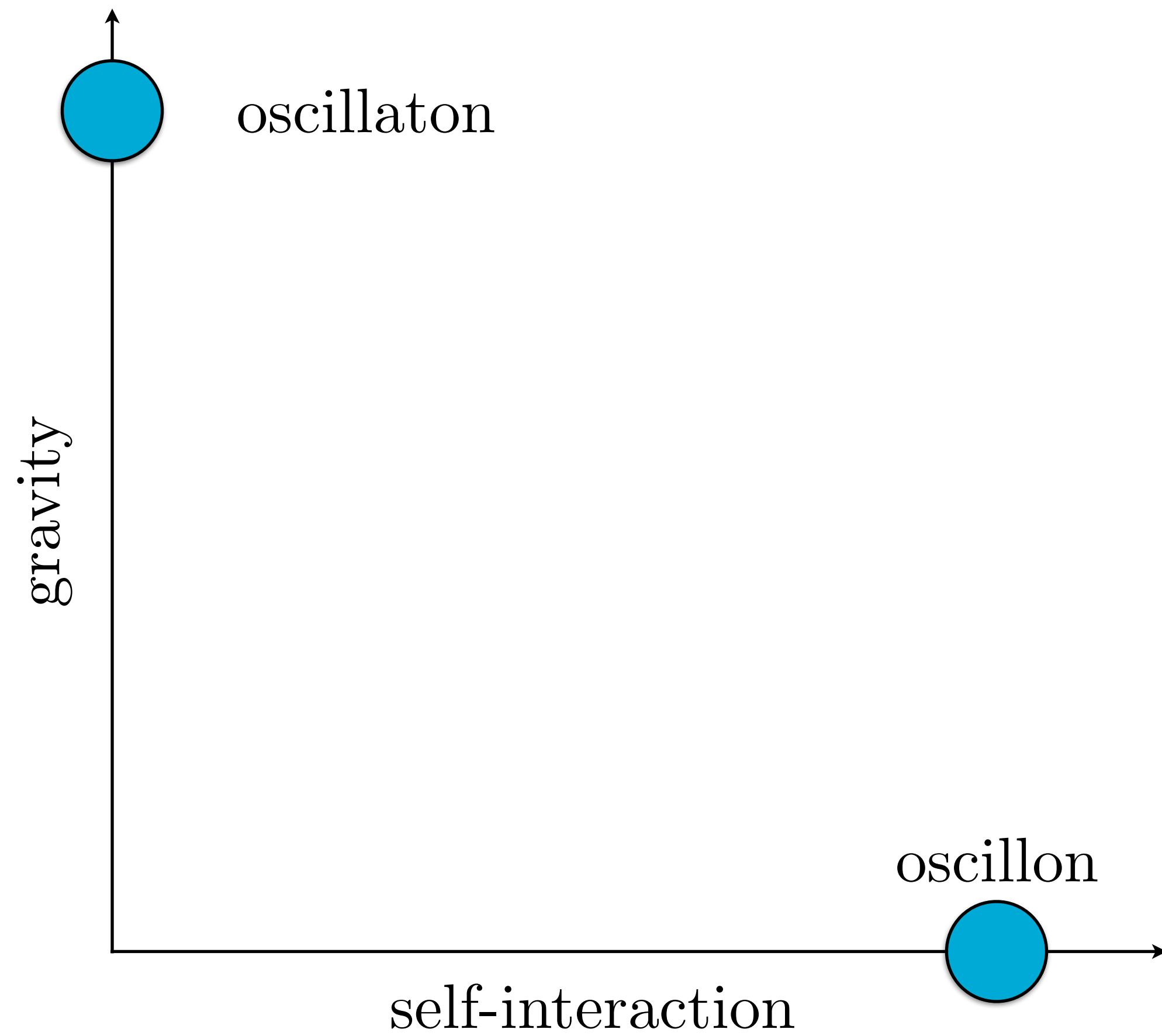
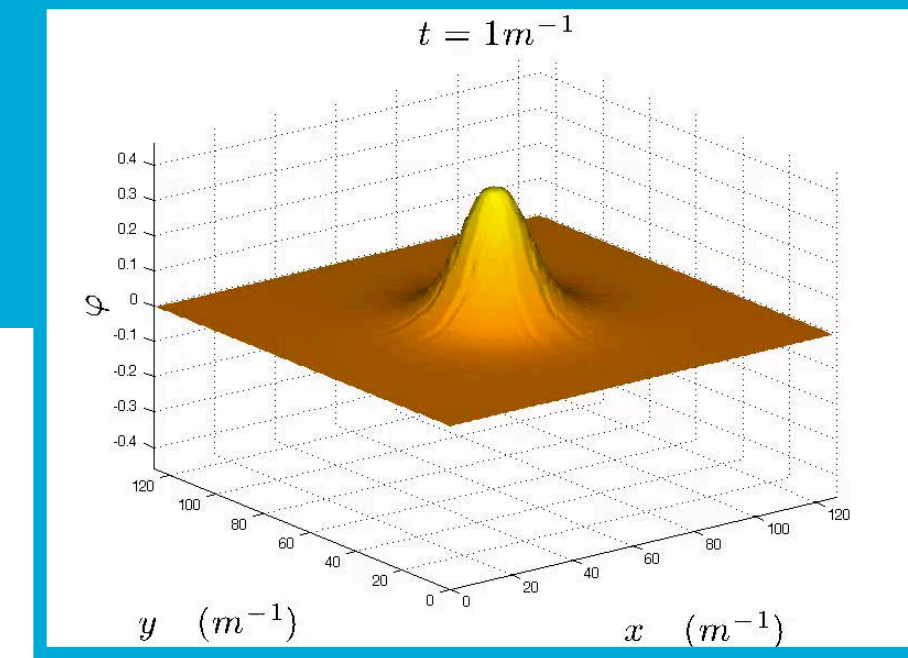
Zhang, MA, et. al (2020)



*see talk by [David Cyncynates](#) on lifetimes in the parallel session also

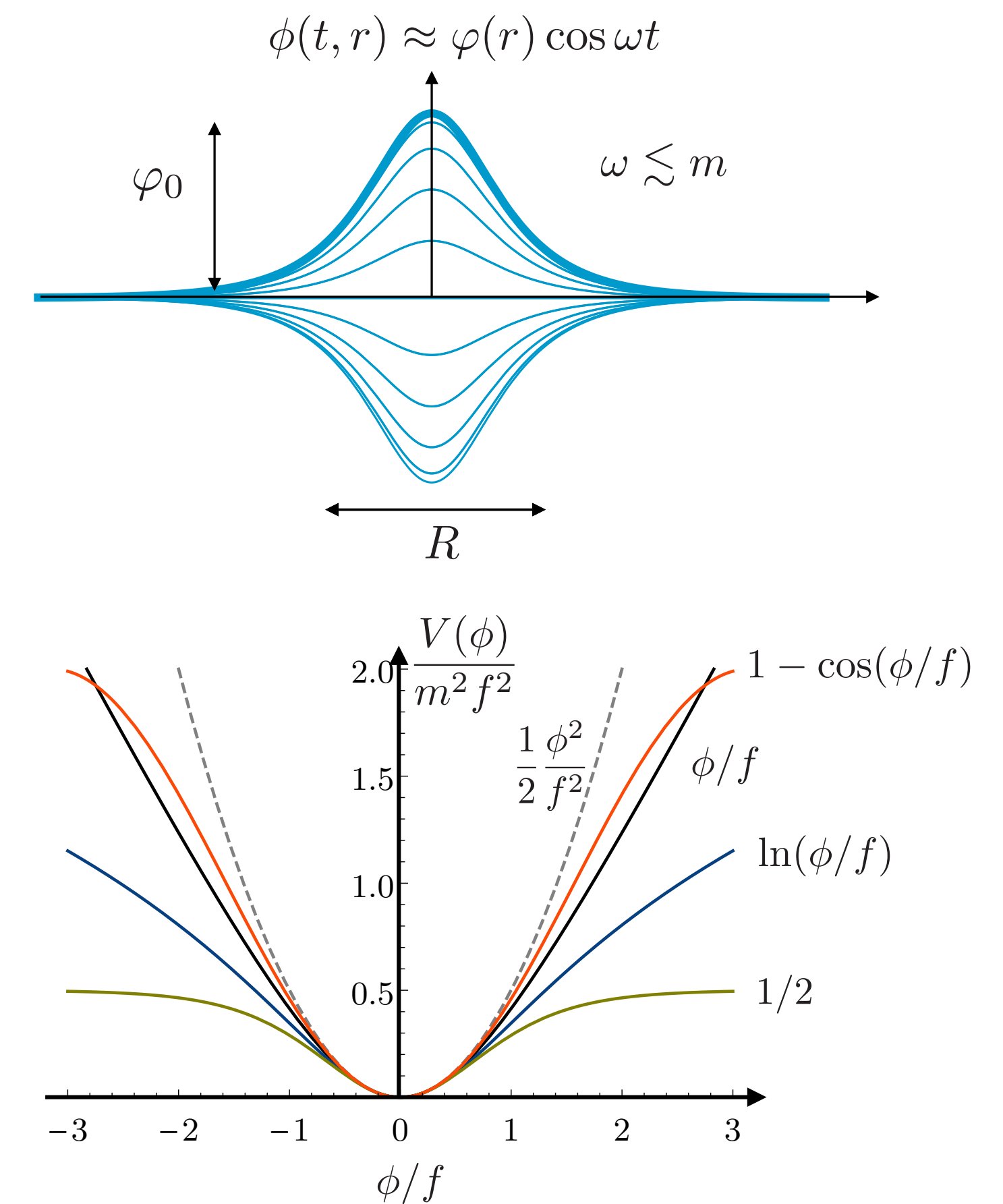
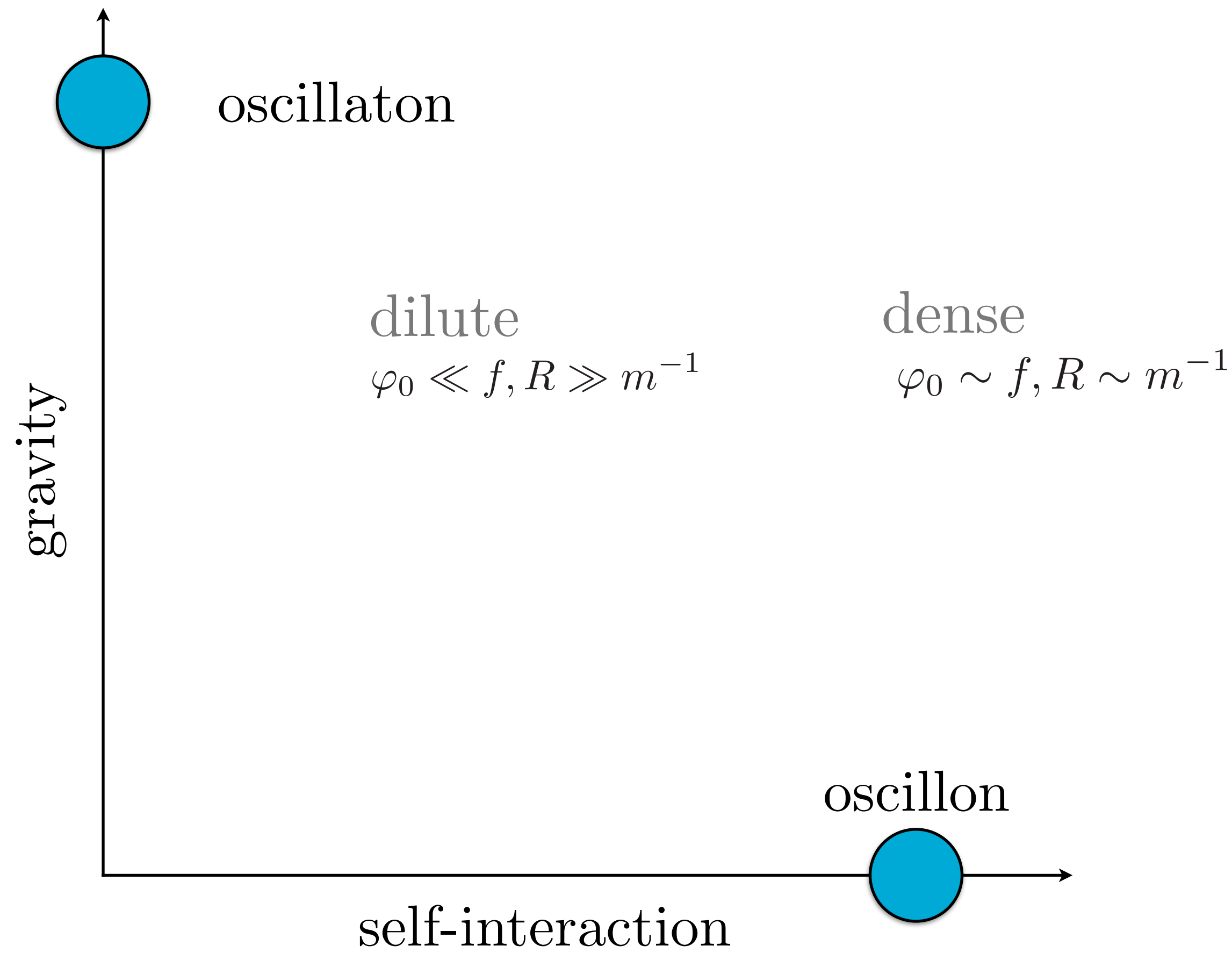
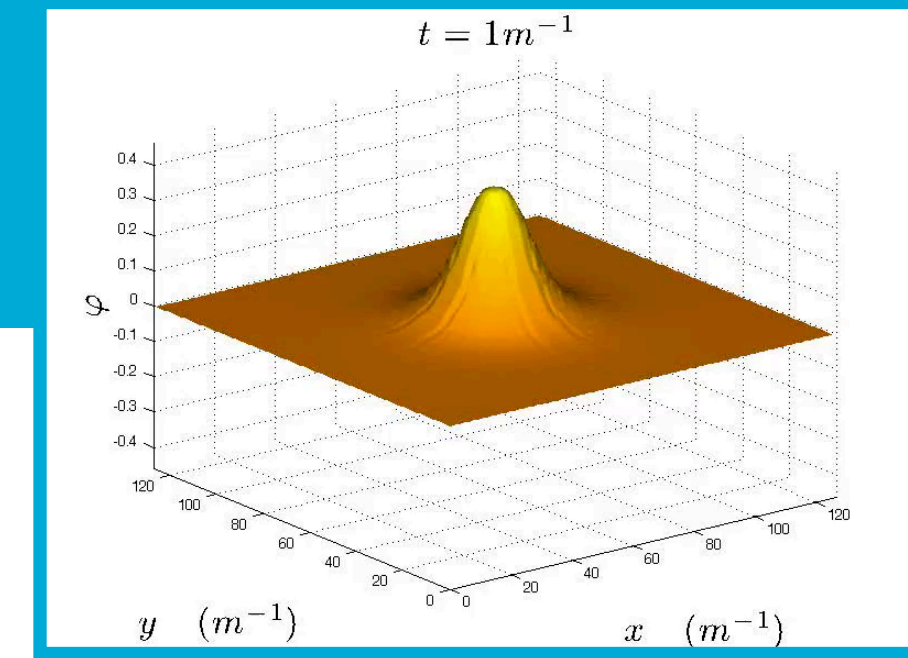
solitons : oscillons, scalar-stars ...

spatially localized, coherently oscillating, long-lived



solitons : oscillons, scalar stars ...

spatially localized, coherently oscillating, long-lived

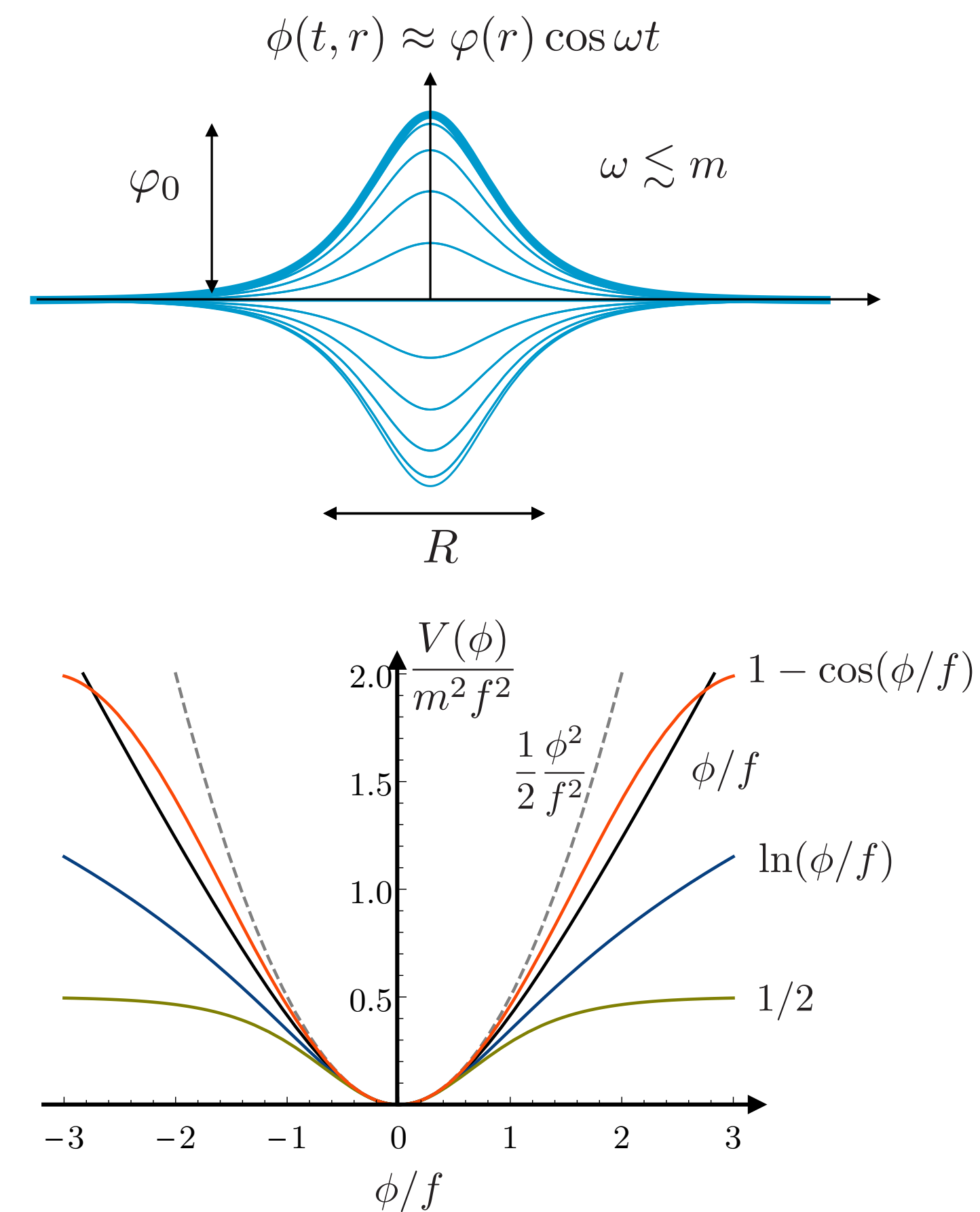
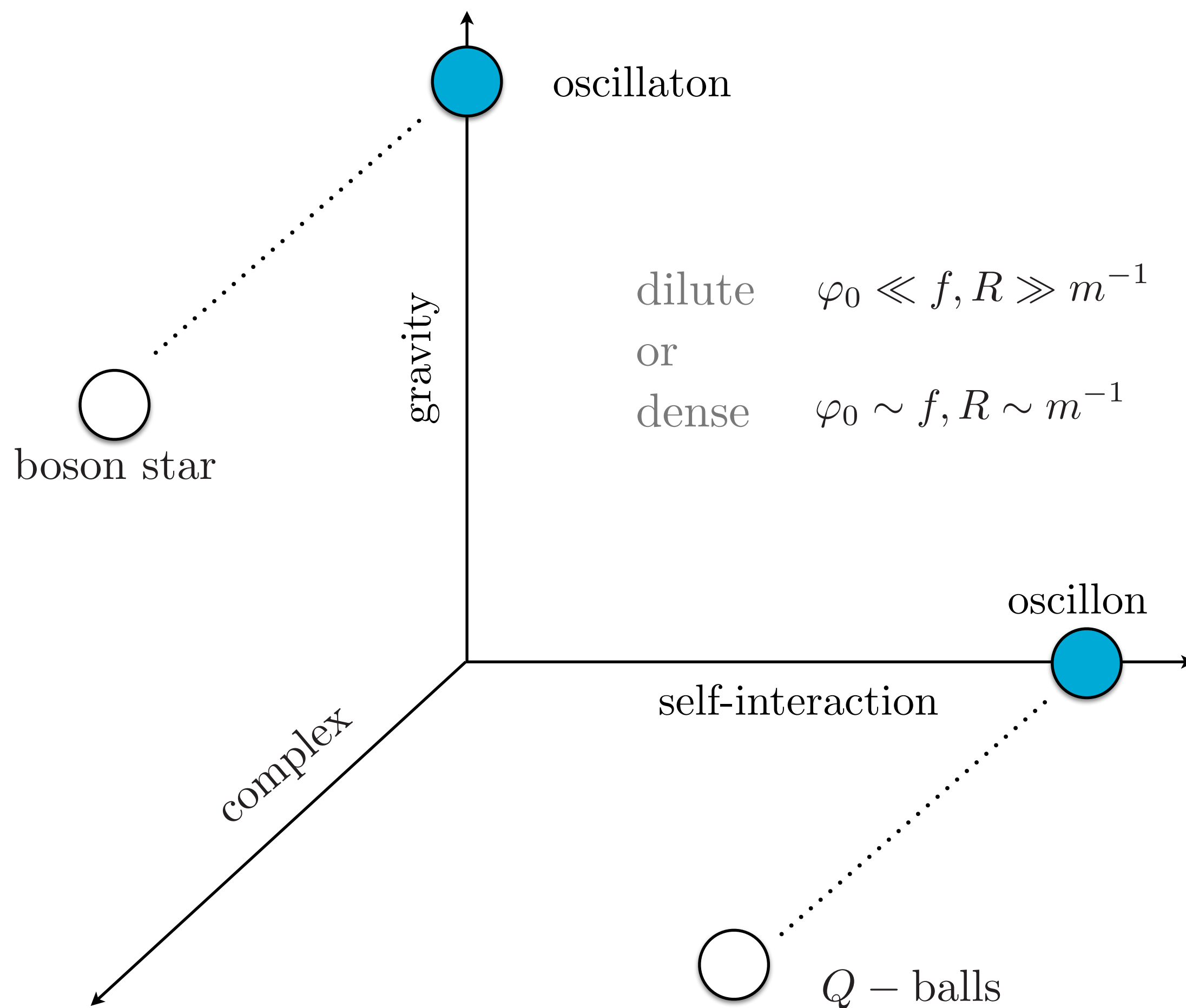
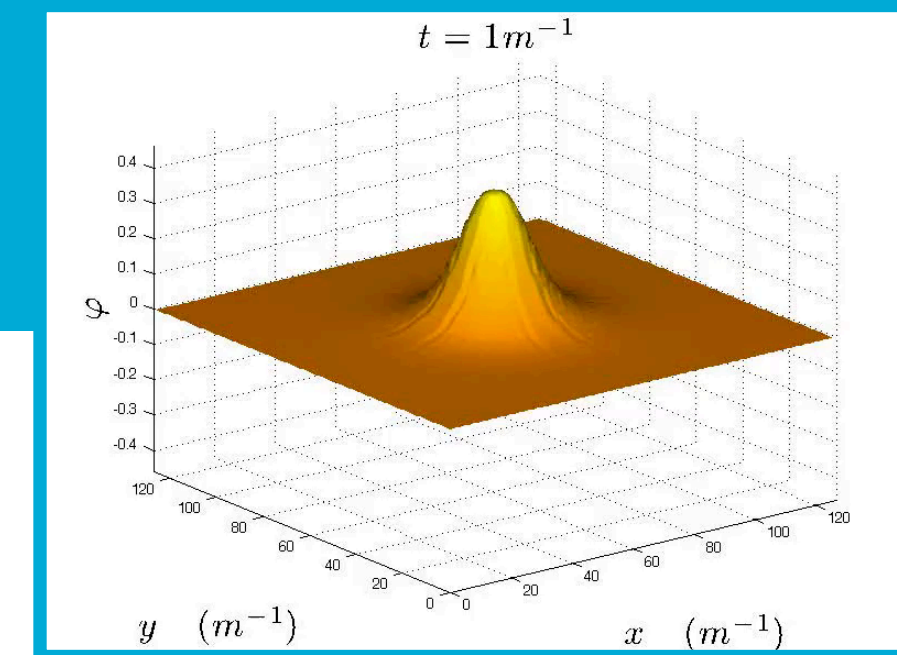


*lifetimes can be much, much larger than the Hubble time scale at the end of inflation

*for regime with strong field gravity regime, see also Muia et. al & Nazari et. al (2019,20)

solitons : oscillons, scalar/boson stars, Q-balls

spatially localized, coherently oscillating, long-lived

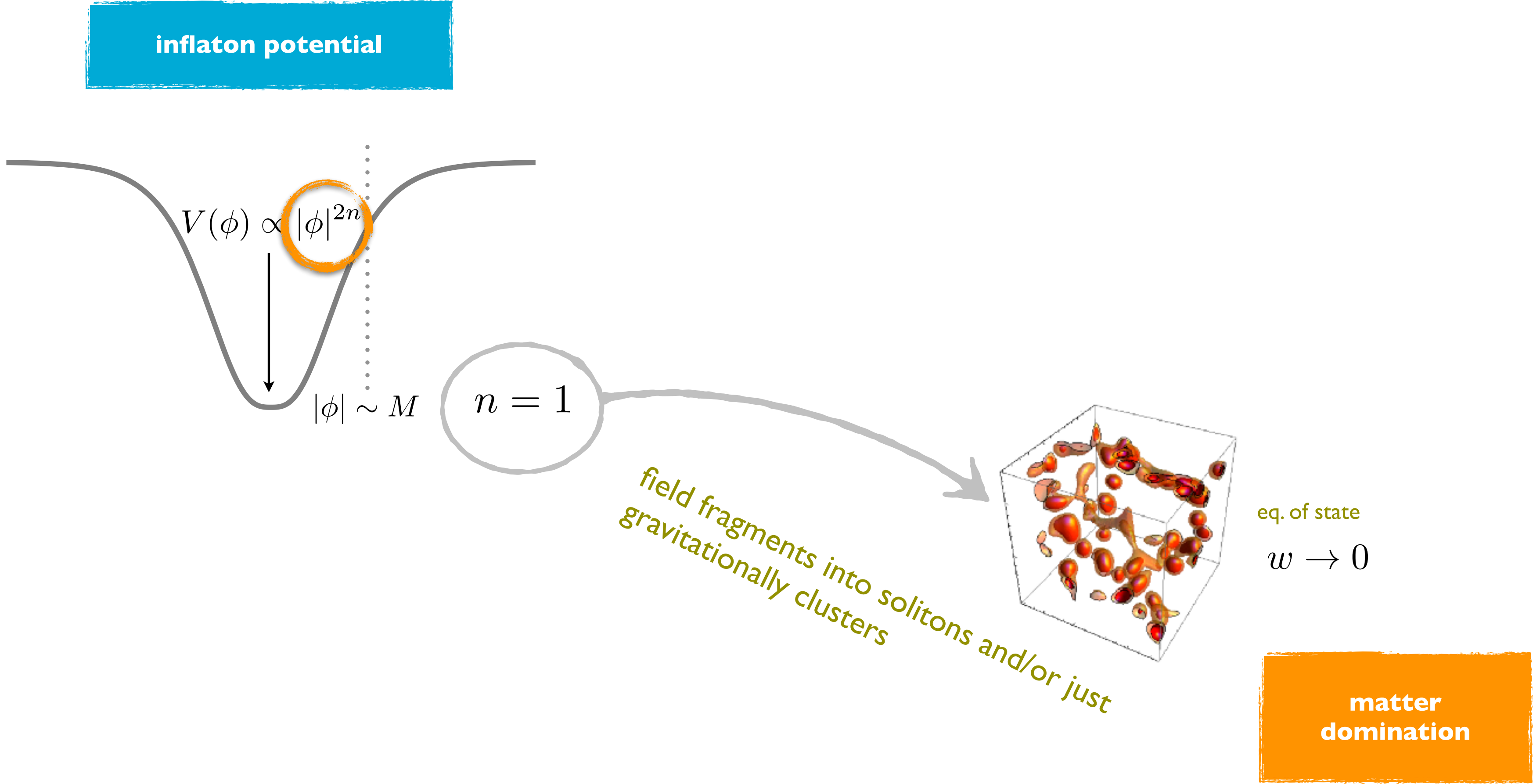


dynamics in quadratic power law minima + wings

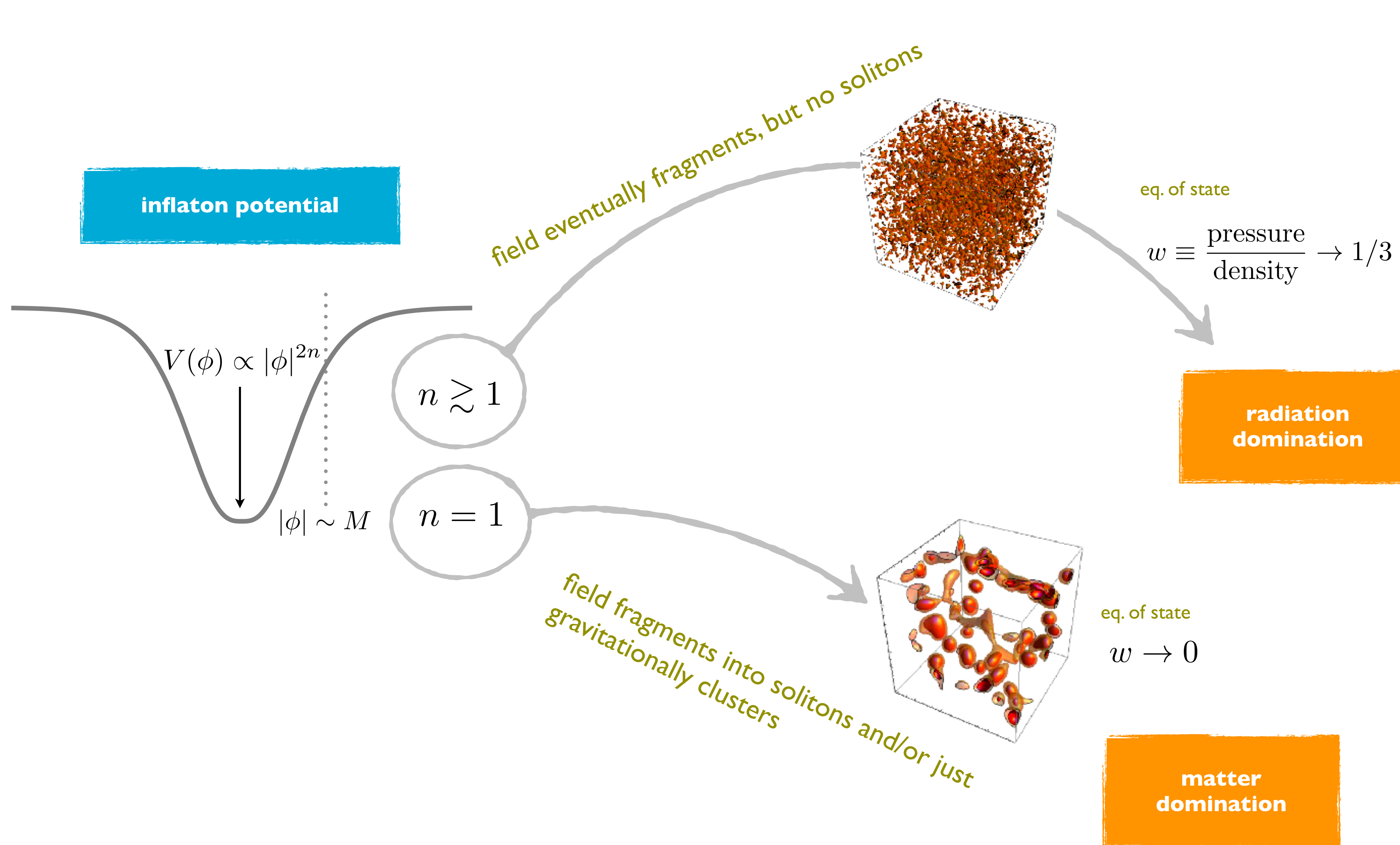
Homogeneous oscillations

$$w = \frac{n - 1}{n + 1}$$

Turner (1983)



dynamics in different power law minima + wings



Homogeneous oscillations

$$w = \frac{n - 1}{n + 1}$$

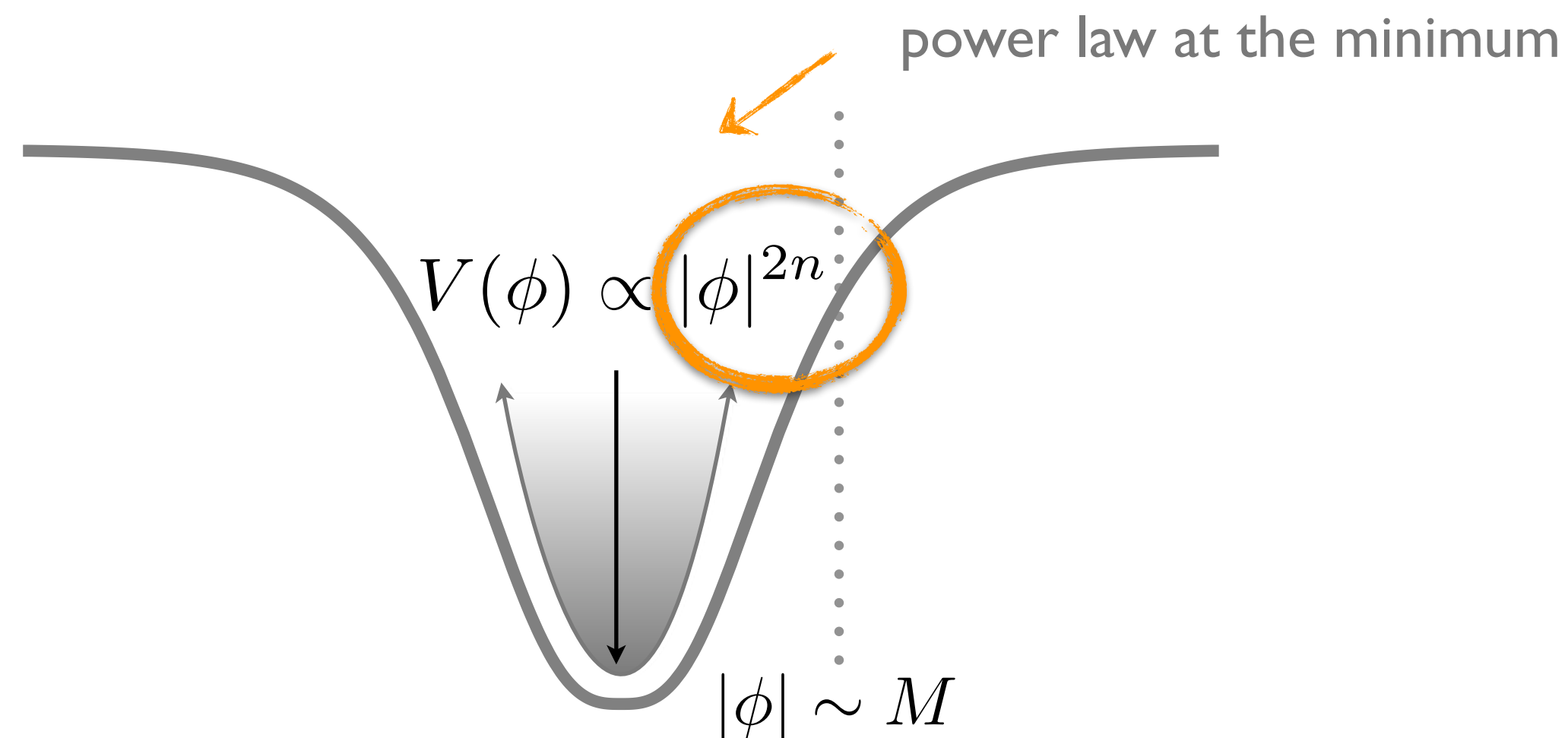
Turner (1983)

equation of state from oscillating fields

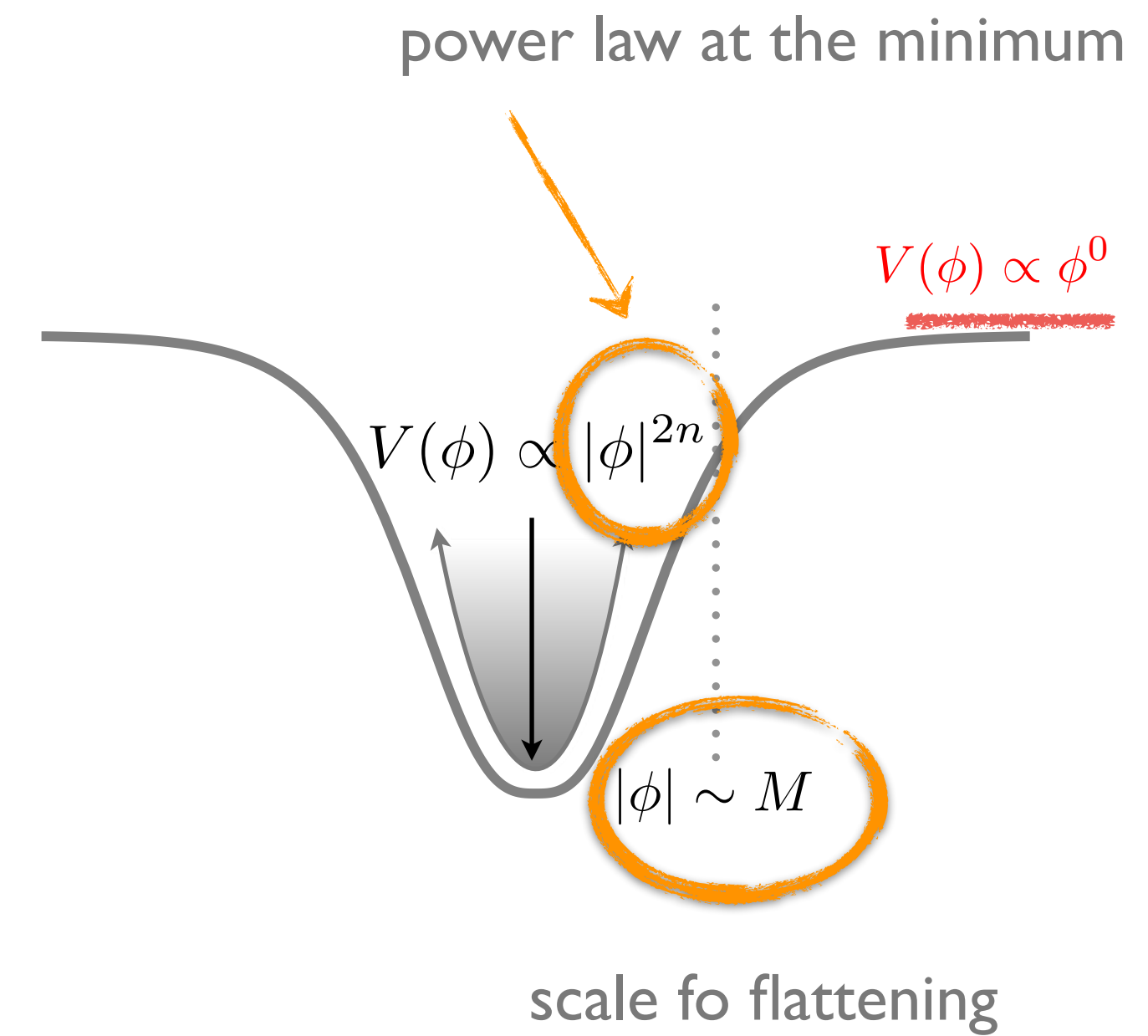
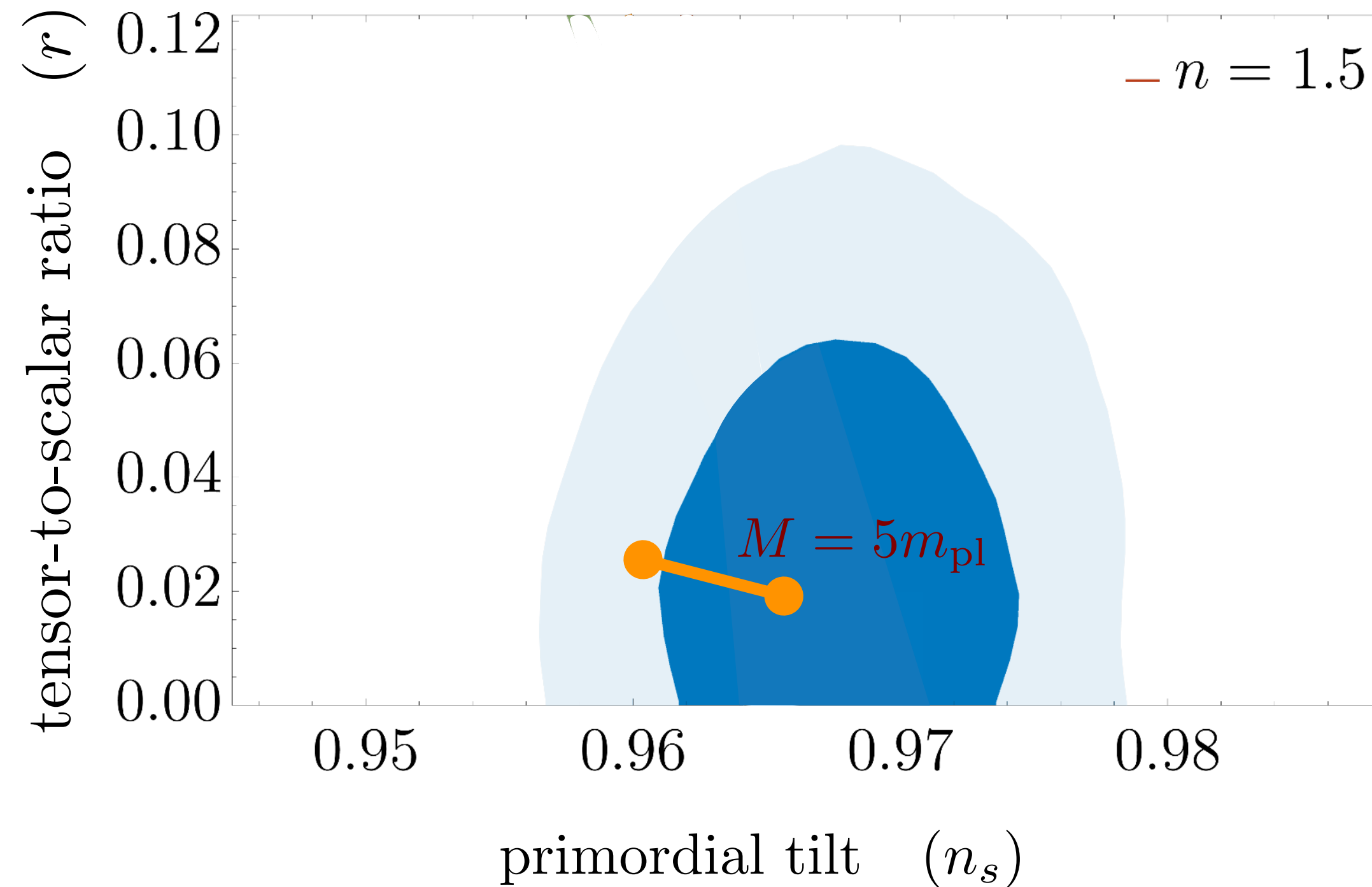
the *spatially averaged* equation-of-state of fields

- ($n = 1$) quadratic minima $w = 0$
- ($n > 1$) **non-quadratic minima** $w = 1/3$ (after sufficient time)

why? $\mu_k/H \propto \phi^{-1}$

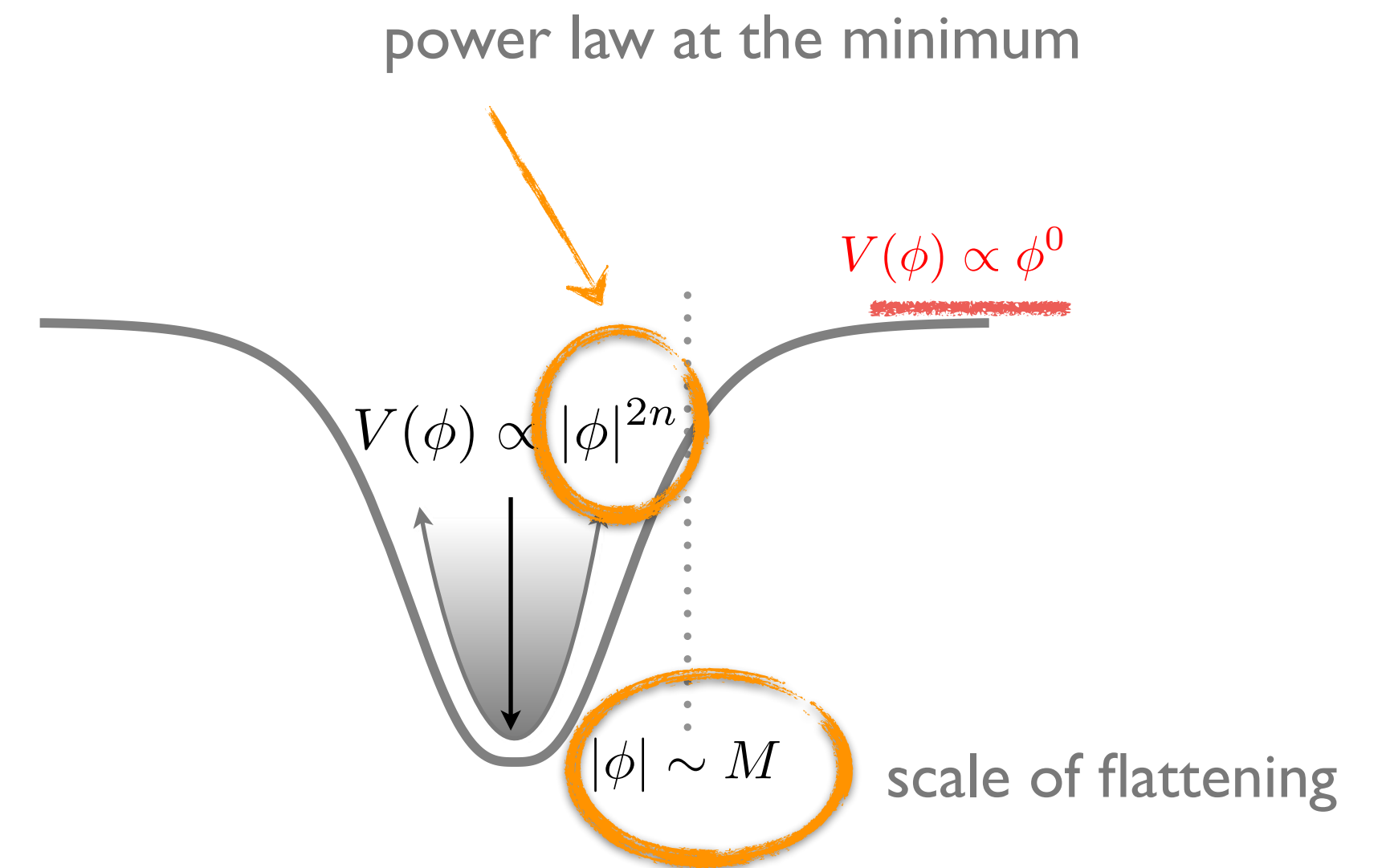
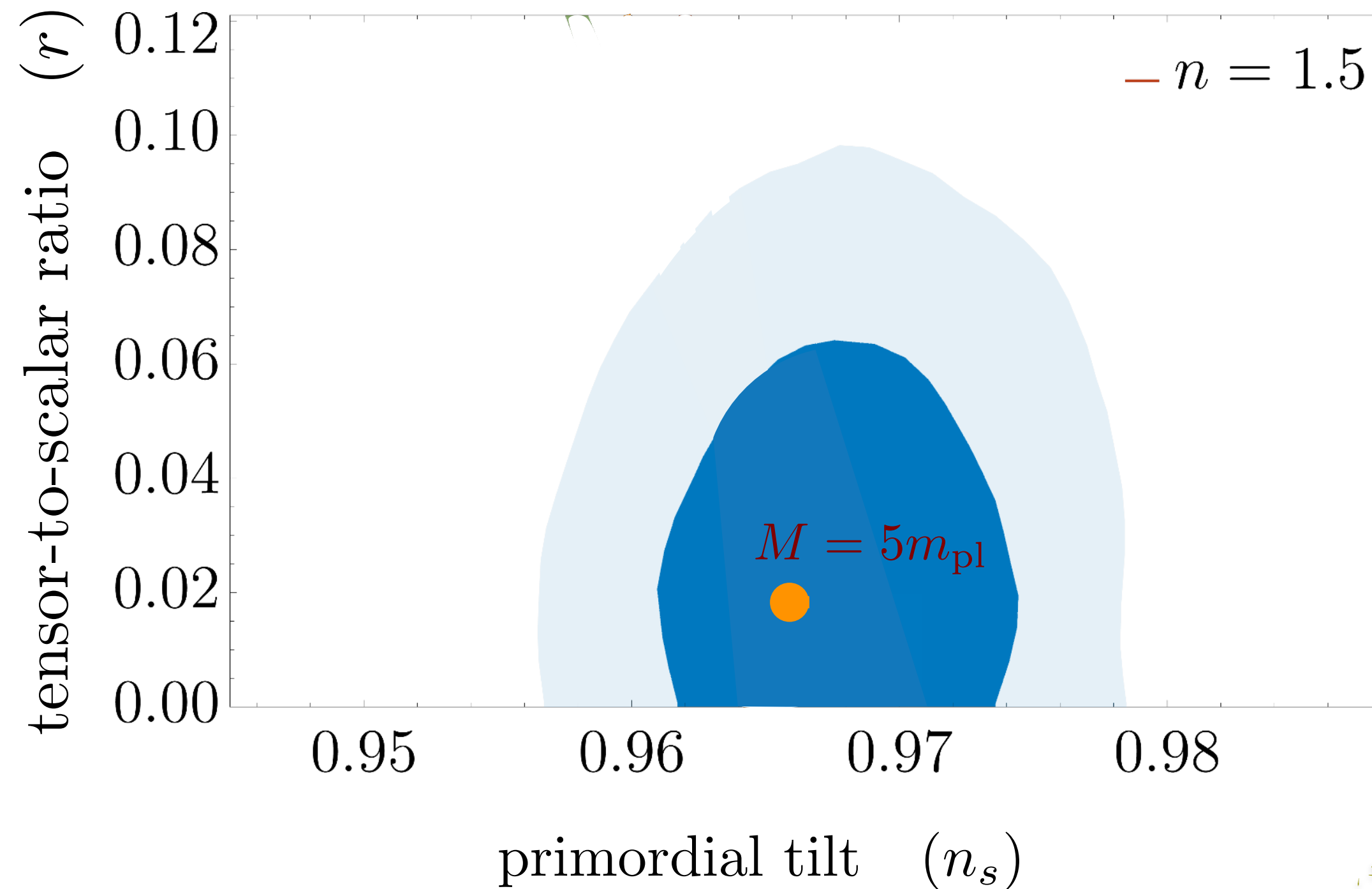


eq. of state & CMB observables



- * non-quadratic minimum
 $n \neq 1$
- * no oscillons here

upper bound on duration to radiation domination



Lozanov & MA (2017)

$$\Delta N_{\text{rad}} \sim \begin{cases} 1 & M \lesssim 10^{-2} m_{\text{Pl}}, \\ \frac{n+1}{3} \ln \left(\frac{\kappa}{\Delta\kappa} \frac{10M}{m_{\text{Pl}}} \right) & M \gtrsim 10^{-2} m_{\text{Pl}}. \end{cases}$$

$$n \neq 1$$

* non-quadratic minimum

* addition of other light fields, see Antusch, Figueroa, Marschall, Torrenti (2020)

couplings to other fields

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} \right. \\ \left. - \frac{1}{2} (\partial\chi)^2 - m_\chi^2 \chi^2 + g_{\phi\chi} \phi \chi^2 + \dots \right. \\ \left. - \bar{\psi} (i\gamma \cdot \partial - m) \psi - g_{\phi\psi} \phi \bar{\psi} \psi + \dots \right]$$

* lots of fun to be had with perturbative and non-perturbative dynamics

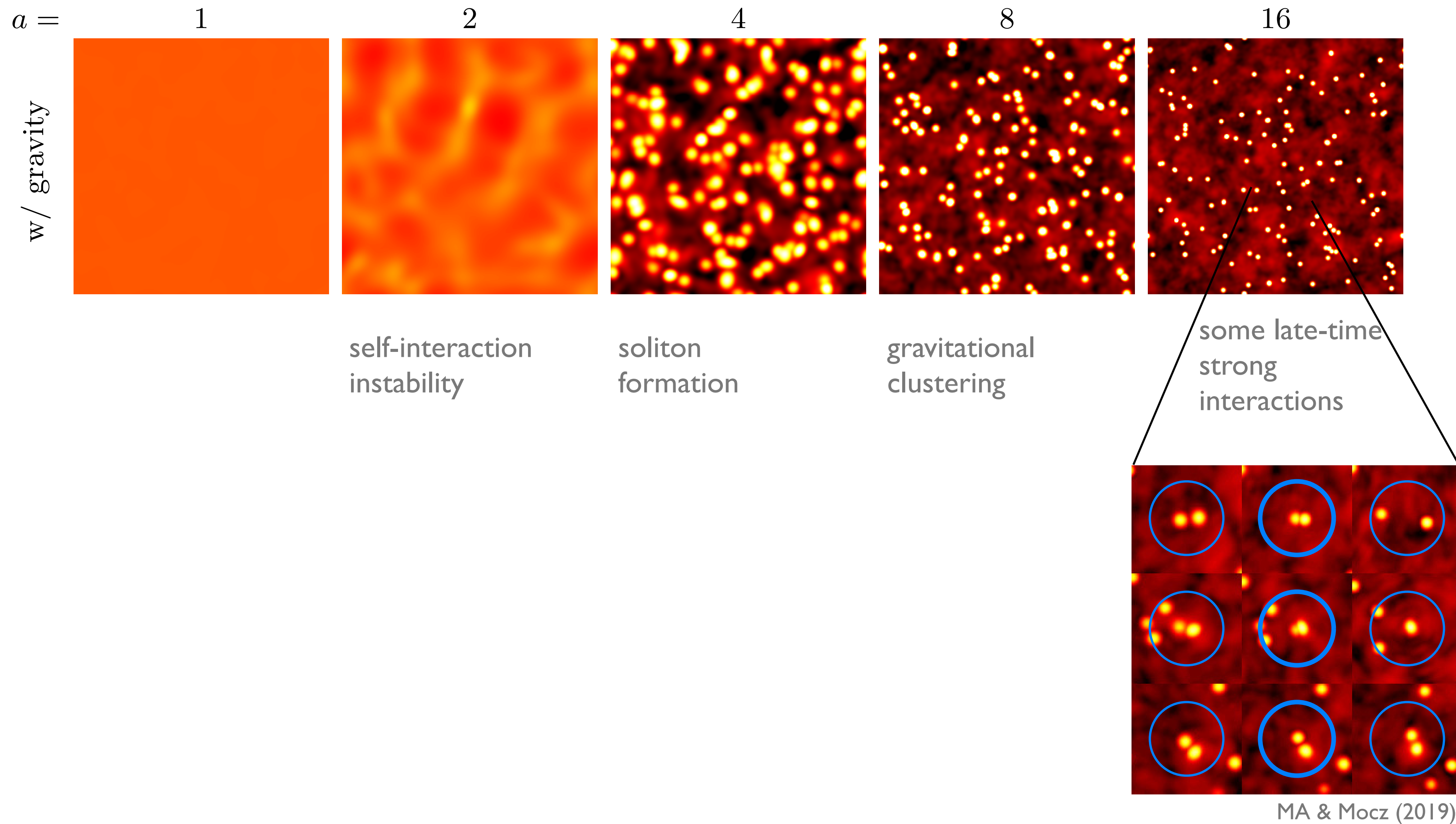
coupling to “photons”

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} \right.$$

$$- \frac{1}{2} (\partial\chi)^2 - m_\chi^2 \chi^2 + g_{\phi\chi} \phi \chi^2 + \dots$$

$$- \bar{\psi} (i\gamma \cdot \partial - m) \psi - g_{\phi\psi} \phi \bar{\psi} \psi + \dots \left. \right]$$

an application: “photons” from oscillons



*this scenario be modified because the coupling to photons is very strong Adshead et. al (2016) and later papers.

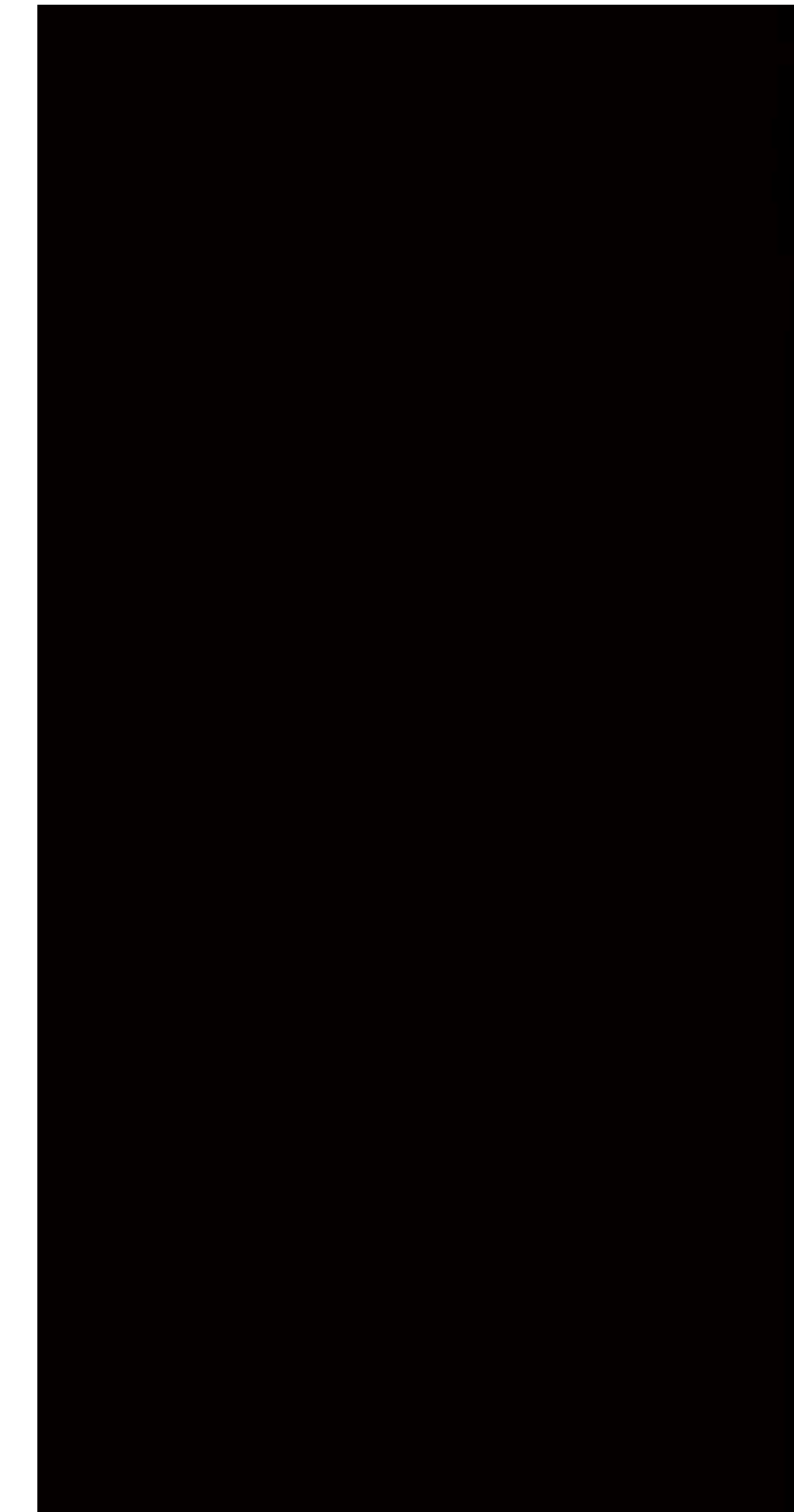
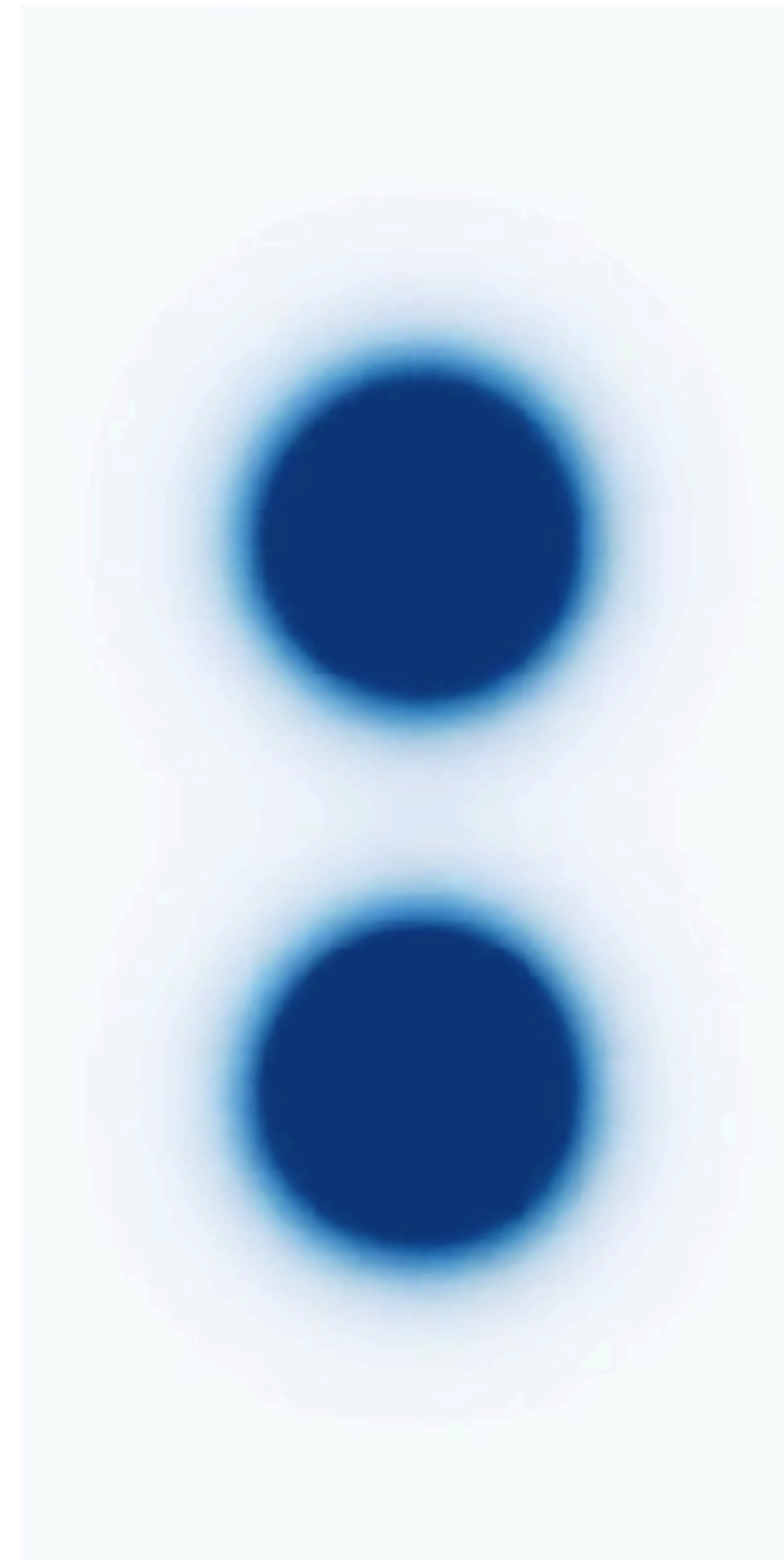
photons from oscillons



MA & Mou (2020)

2009.11337

- no emission before merger
- explosive after merger
- a threshold & resonant effect



*might not be easy to achieve because the amplitude is highest at the end of inflation, so most photons produced then before (if) soliton formation. Also, likely not enough for reheating

* but other mechanisms to produce the solitons might work, also applications in the late universe

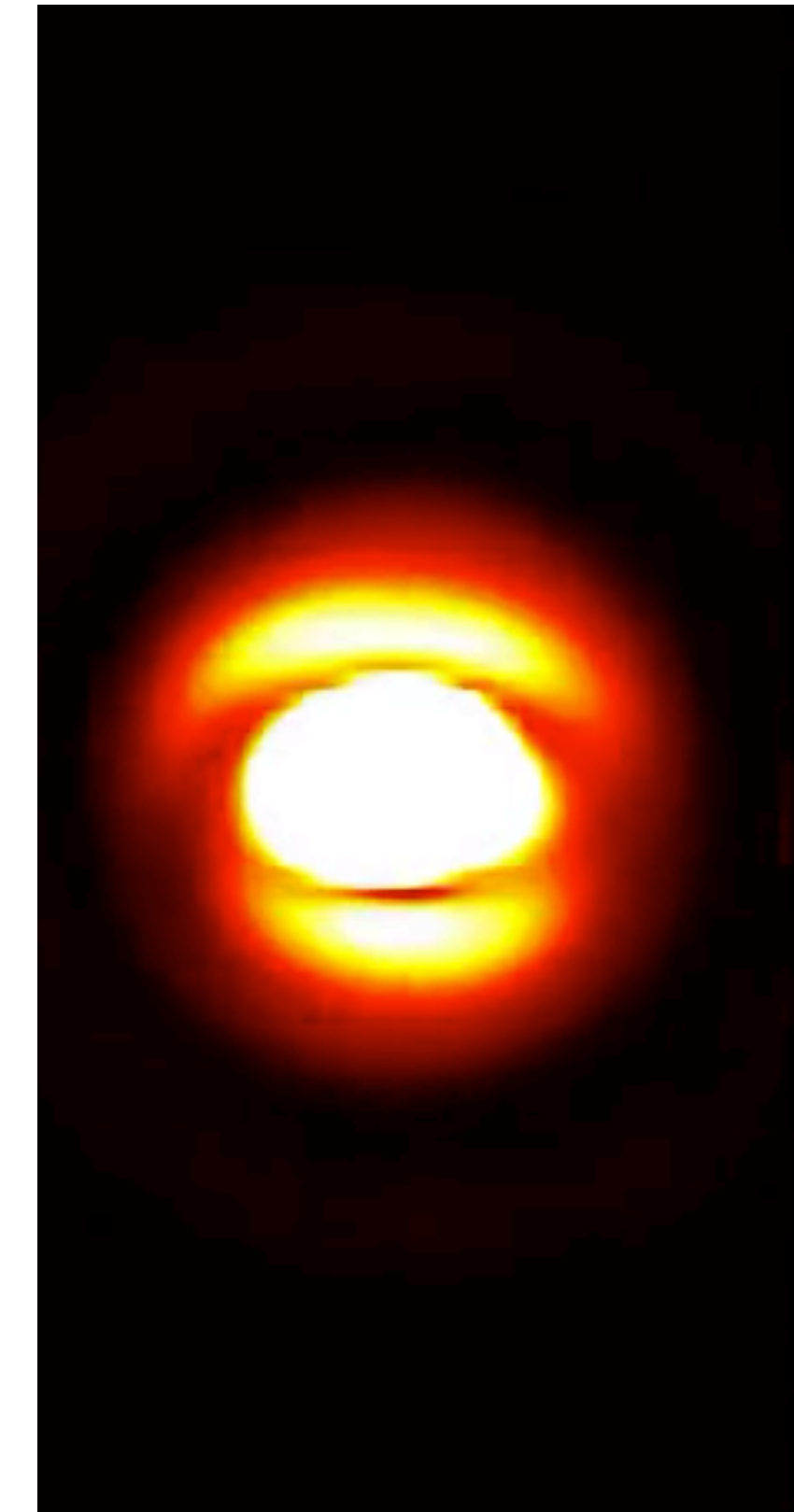
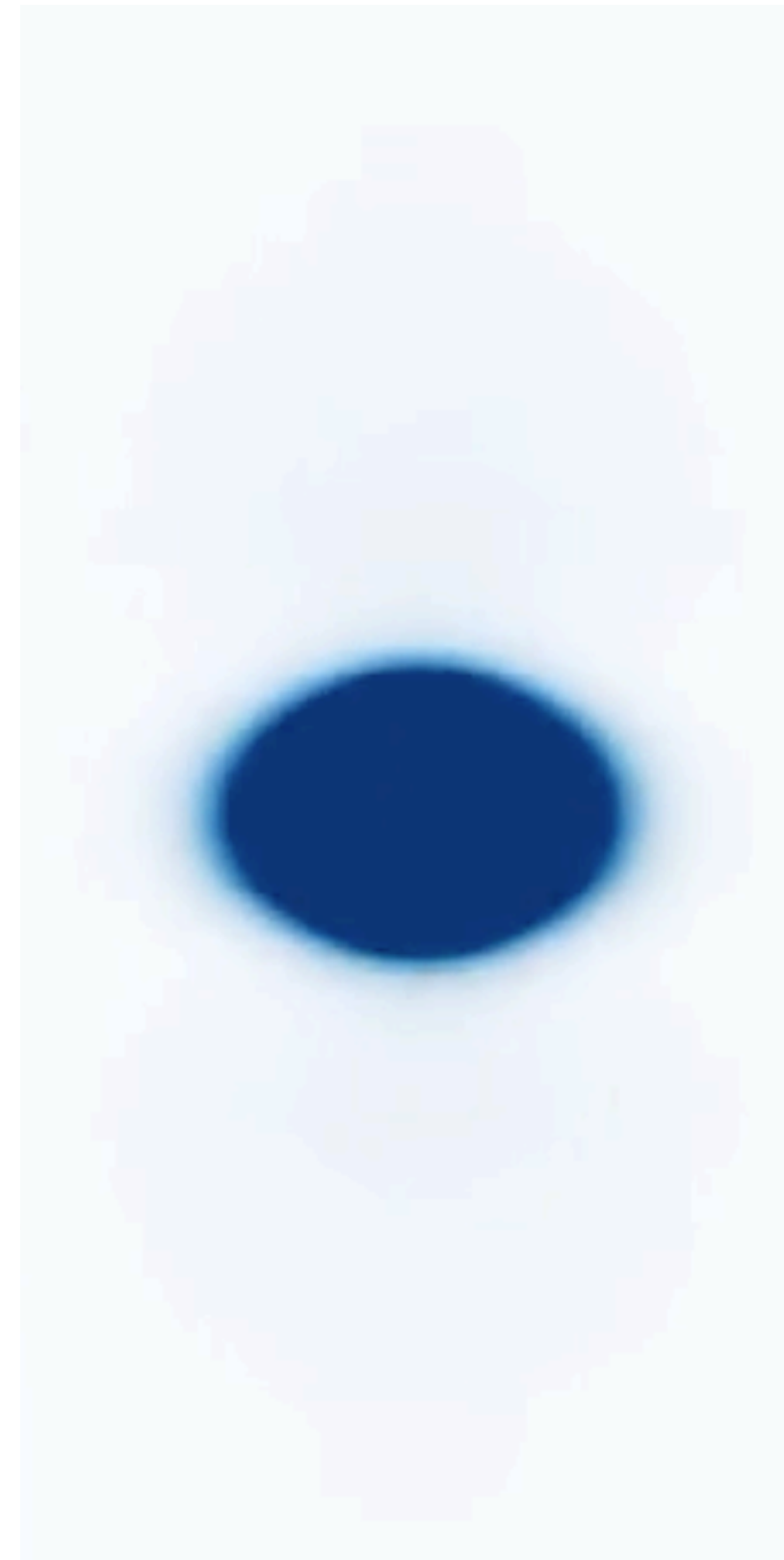
photons from oscillons



MA & Mou (2020)

2009.11337

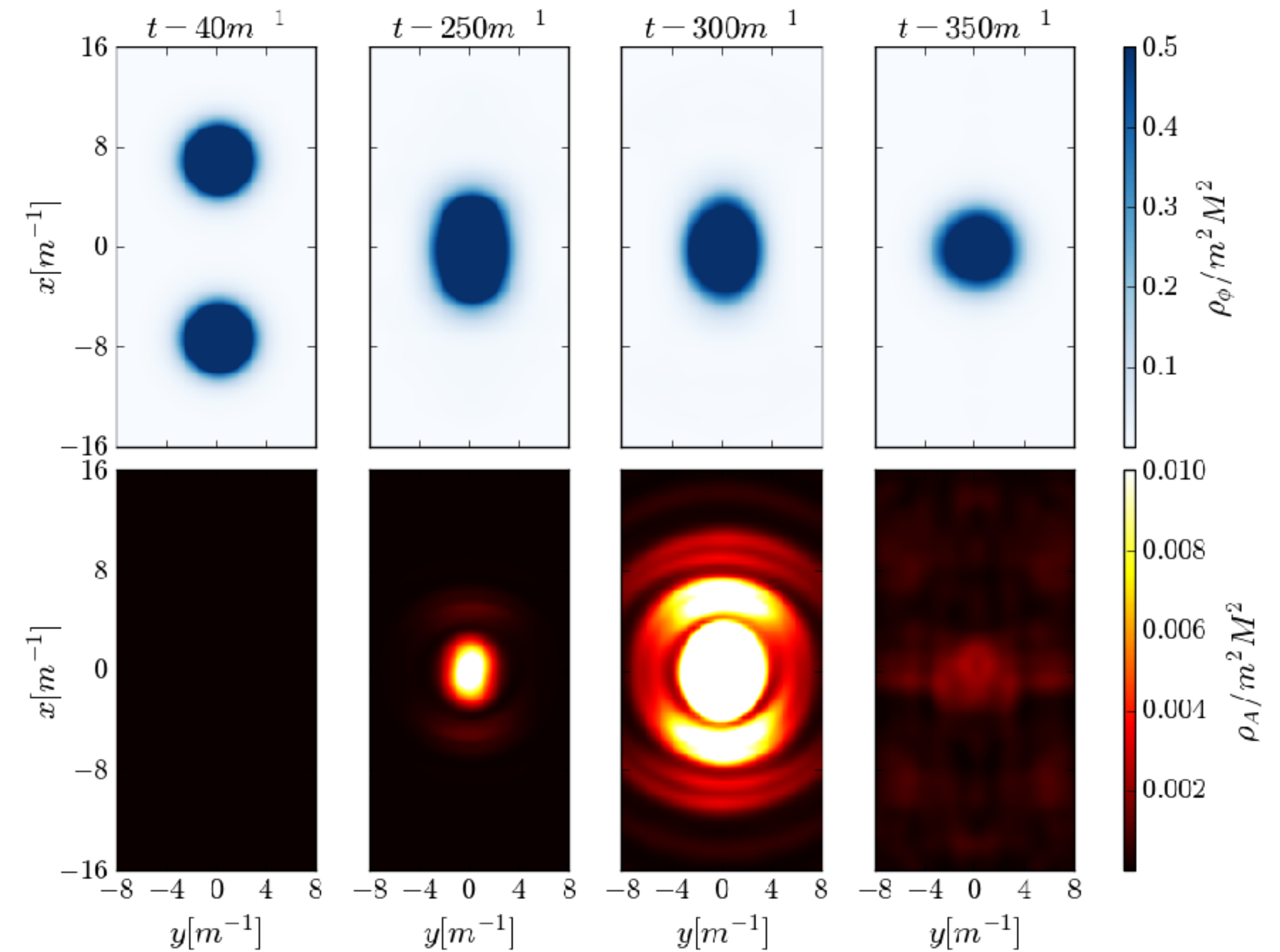
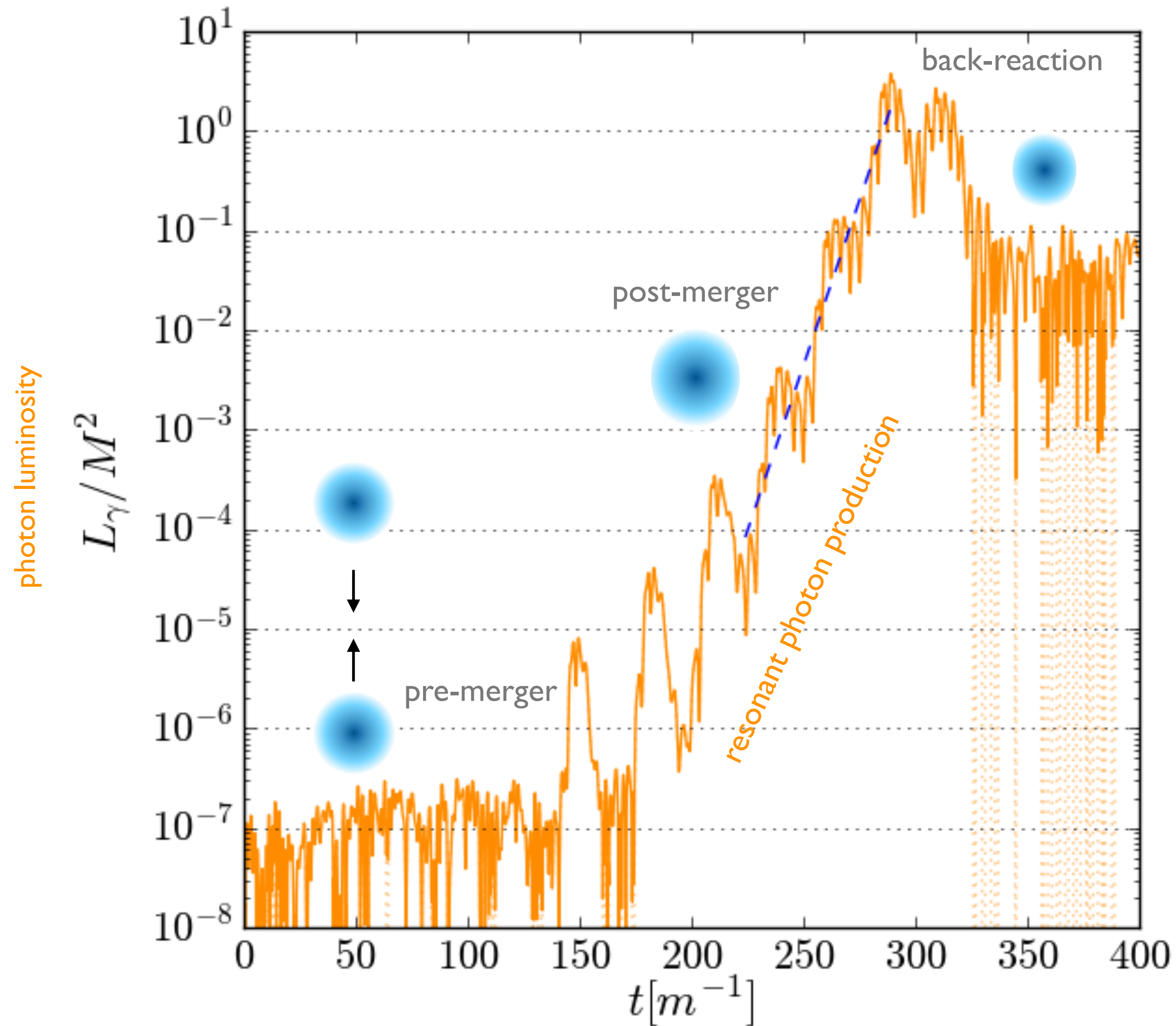
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* but other mechanisms to produce the solitons might work, also applications in the late universe

explosive, self-regulating photon production from mergers

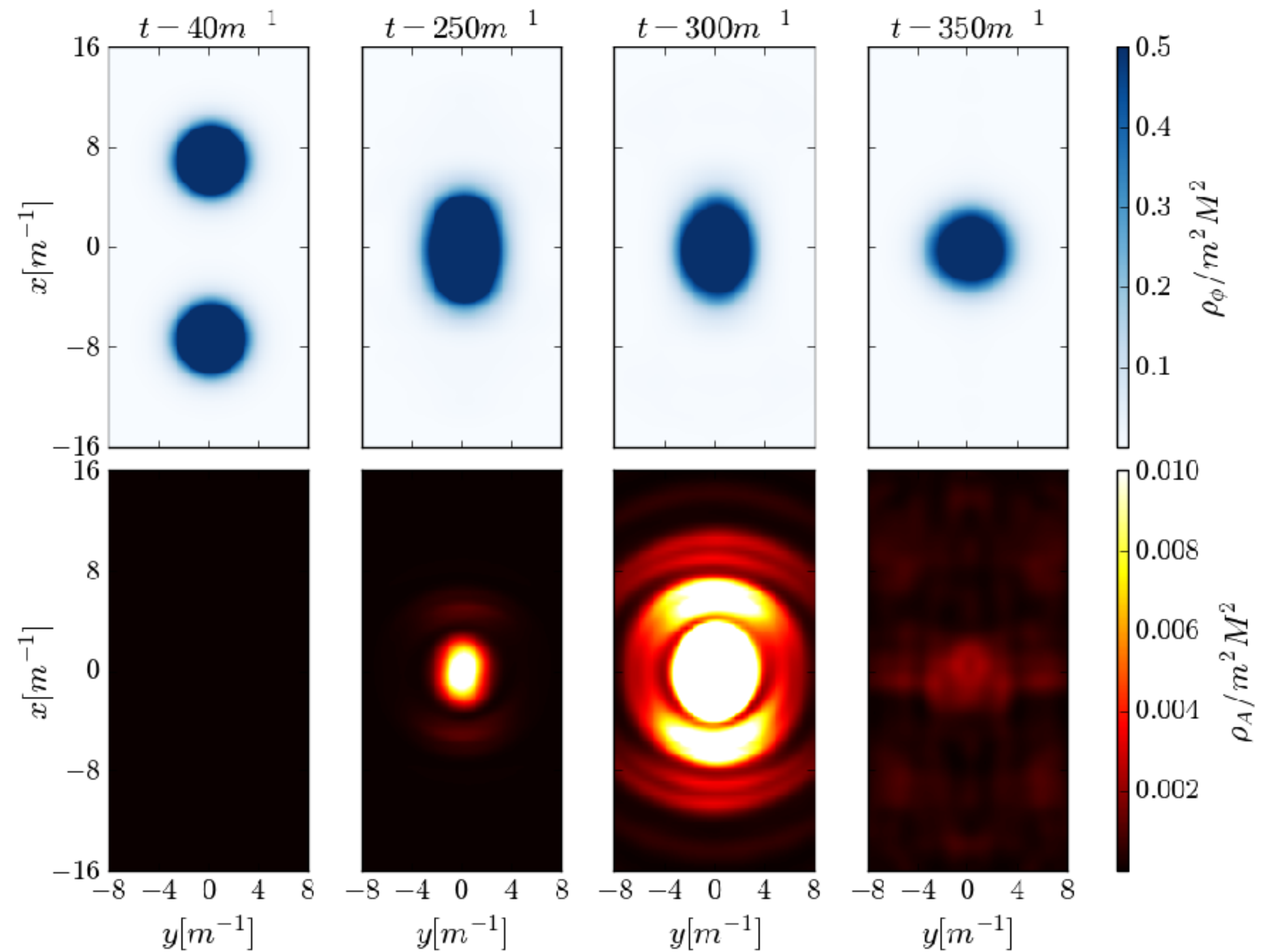


*after backreaction shuts off resonance, the luminosity falls to small values — at late times the apparent moderate value is due to a periodic box

explosive photon production from soliton mergers

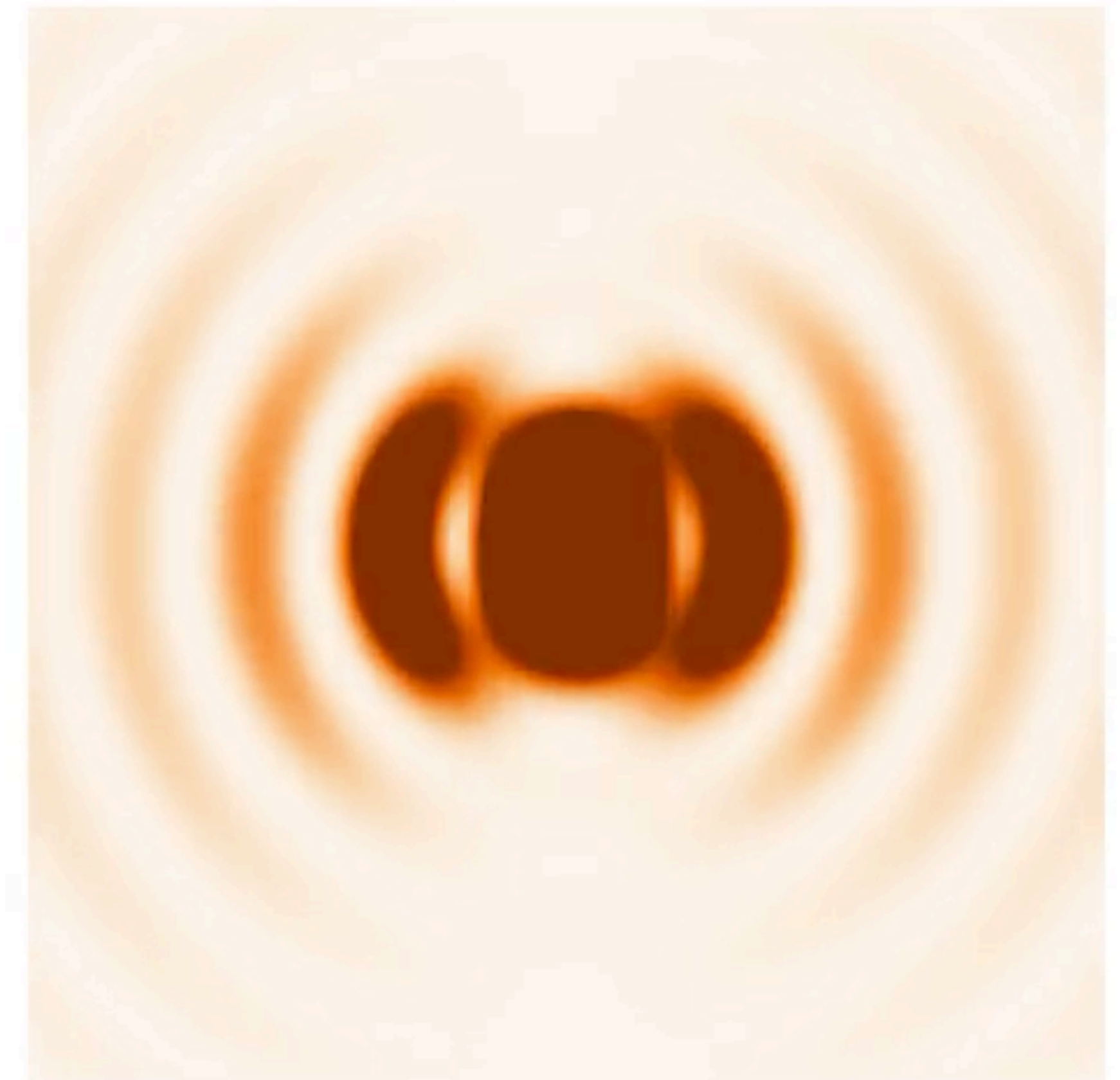
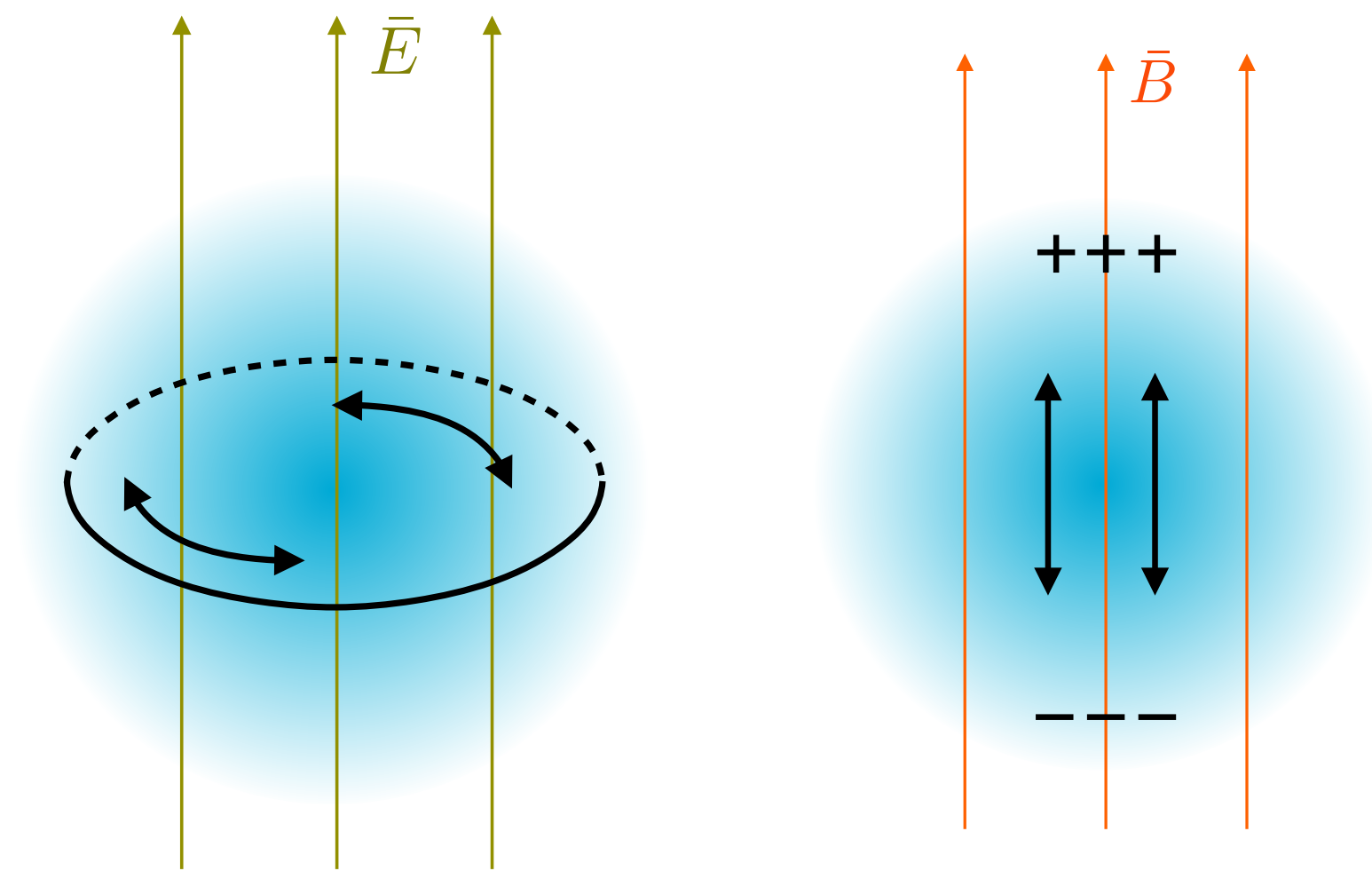
~30% of total energy goes into axion waves

~20% of remaining goes into EM radiation



* for an exploration of gravitational wave production from mergers, see [Helfer, Garcia et. al \(2018\)](#)

“photons” from oscillons: in external fields



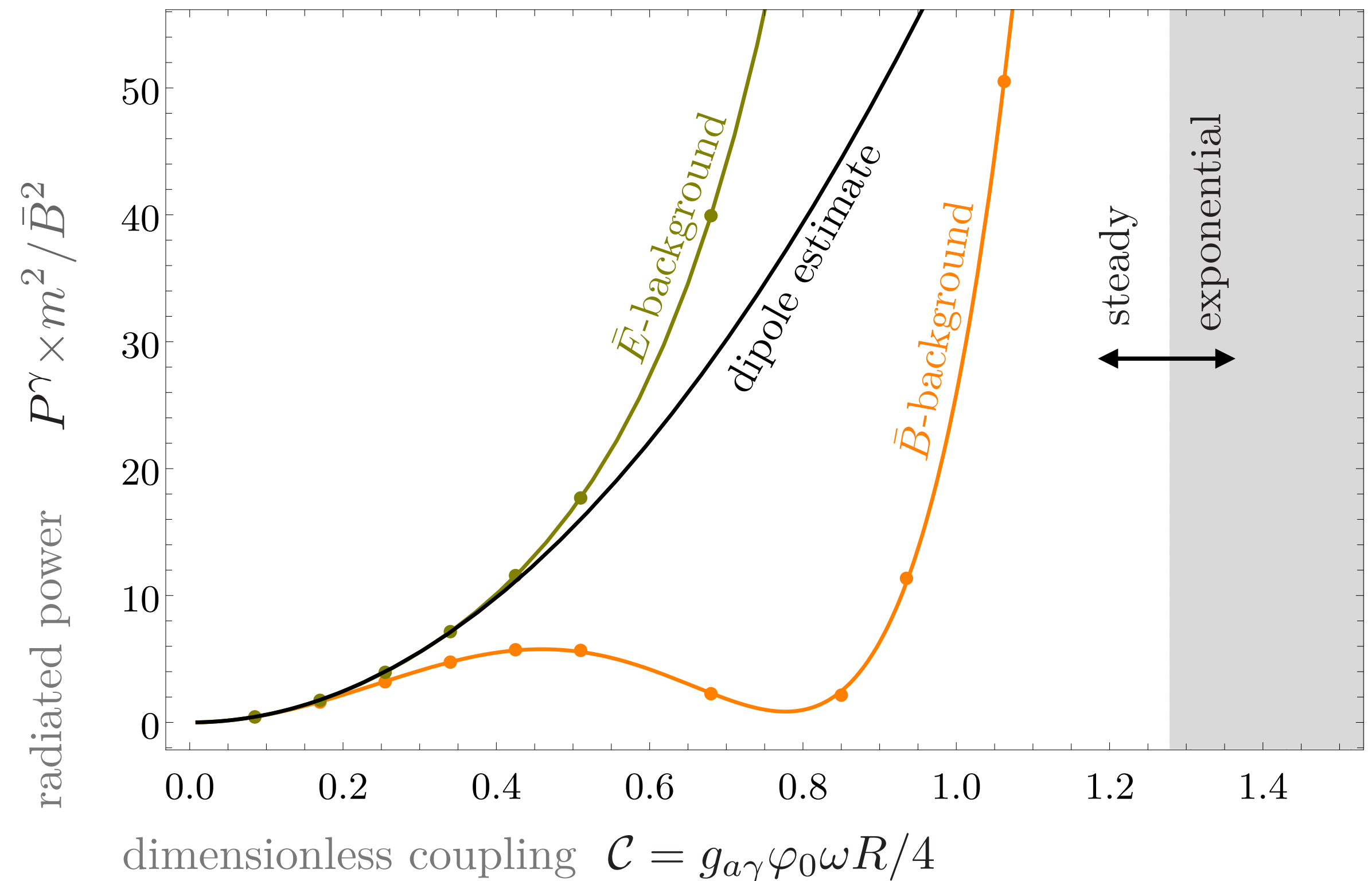
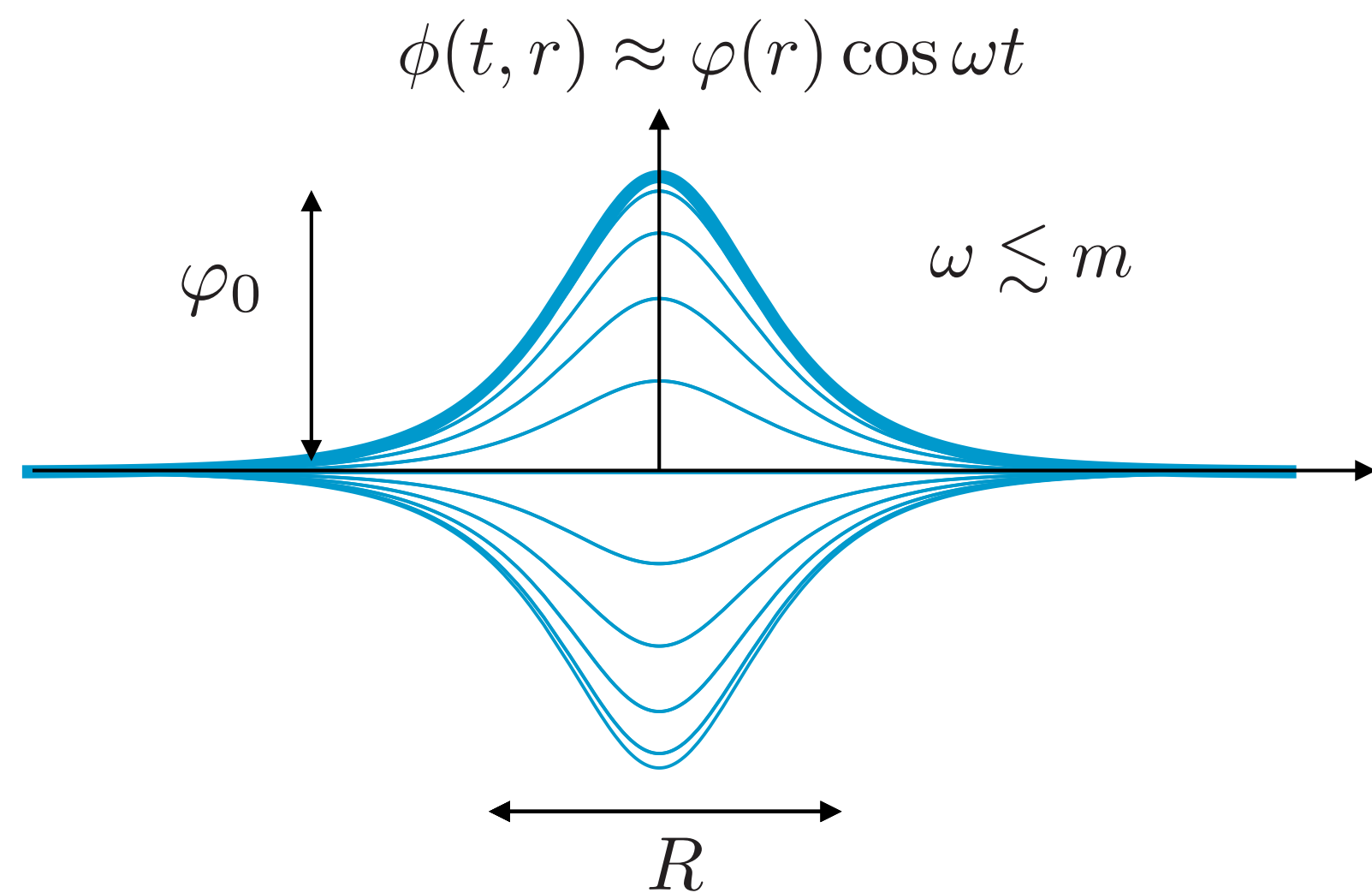
MA, Long, Mou & Saffin (2021)

2103.12082

explosive vs. steady radiation

scalar stars/oscillons/solitons can radiate energy in electromagnetic fields $g_{a\gamma}\phi\mathbf{E}\cdot\mathbf{B}$

radiated power depends on **axion-photon coupling** and characteristics of **soliton configuration**



coupling to massive “photons”

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right. \\ \left. - \frac{1}{2} (\partial\chi)^2 + m_\chi^2 \chi^2 + g_{\phi\chi} \phi \chi^2 + \dots \right. \\ \left. - \bar{\psi} (i\gamma \cdot \partial - m) \psi - g_{\phi\psi} \phi \bar{\psi} \psi + \dots \right]$$

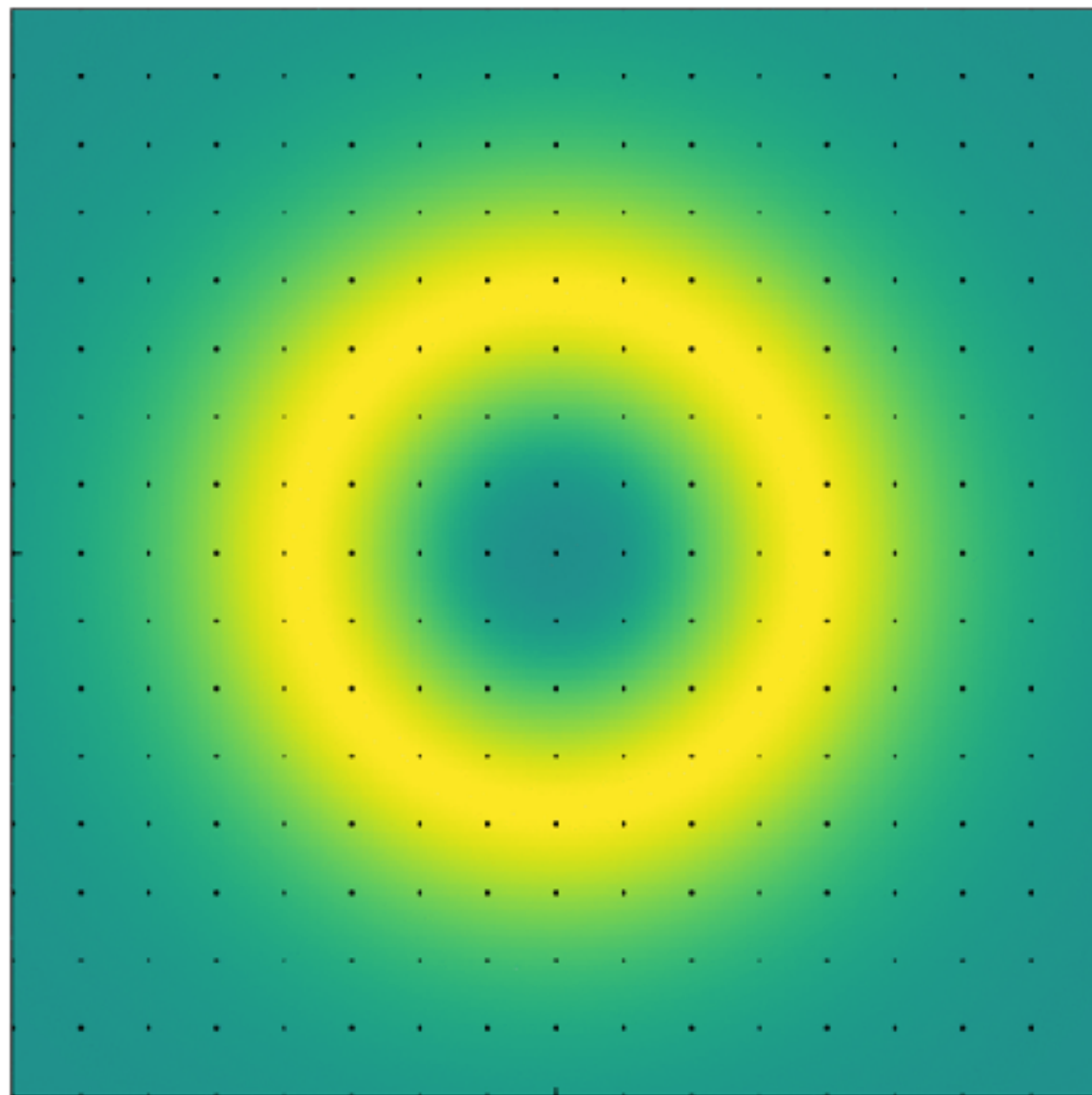
* production could be via “misalignment” of inflaton, for example: Co et. al (2018), Agrawal et. al (2018) in context of dark matter

Vector oscillons

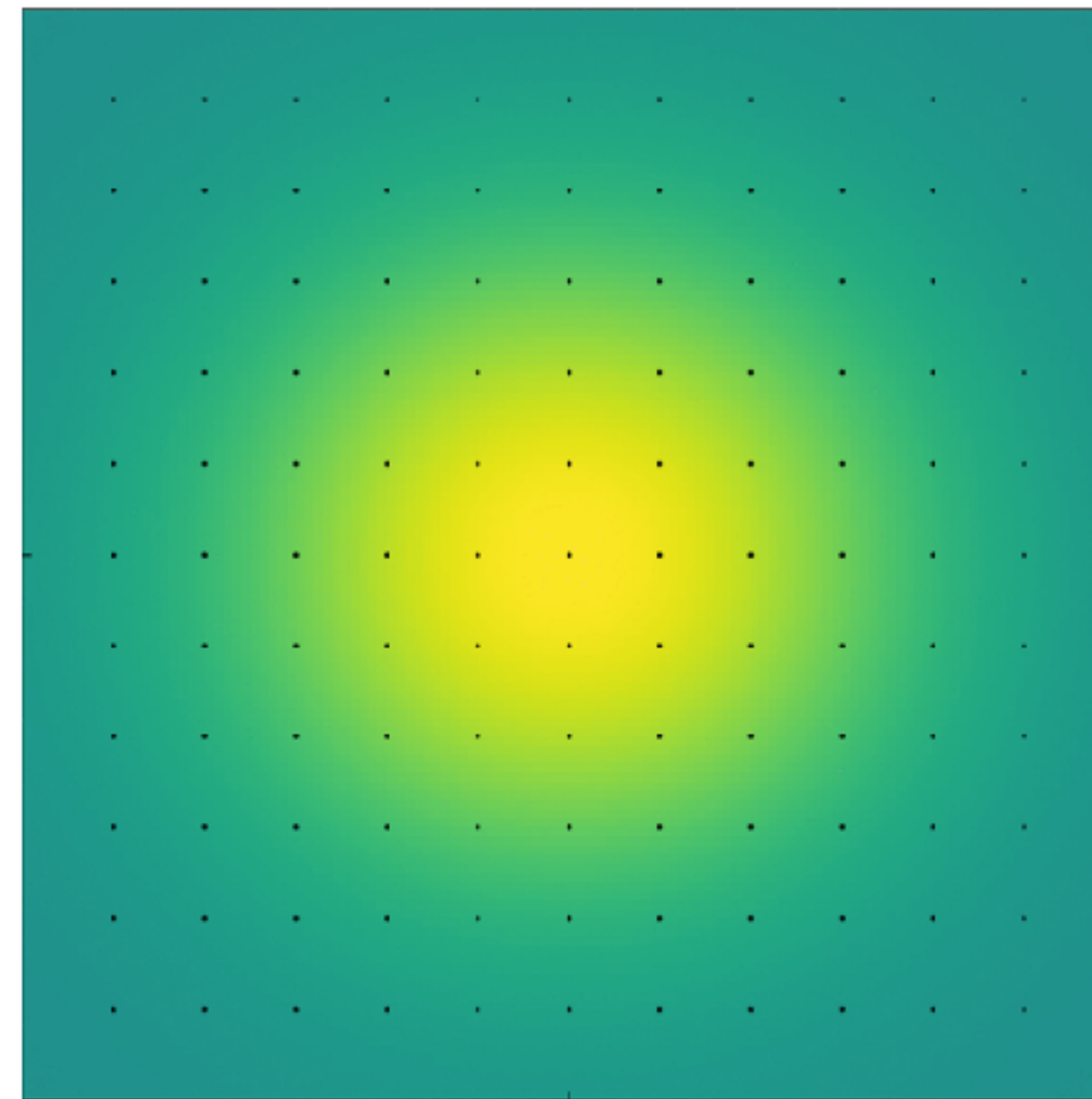
WORK IN
PROGRESS

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right]$$

hedgehog oscillon 



directional oscillon (easier to form) 



Zhang & MA (coming out < month)

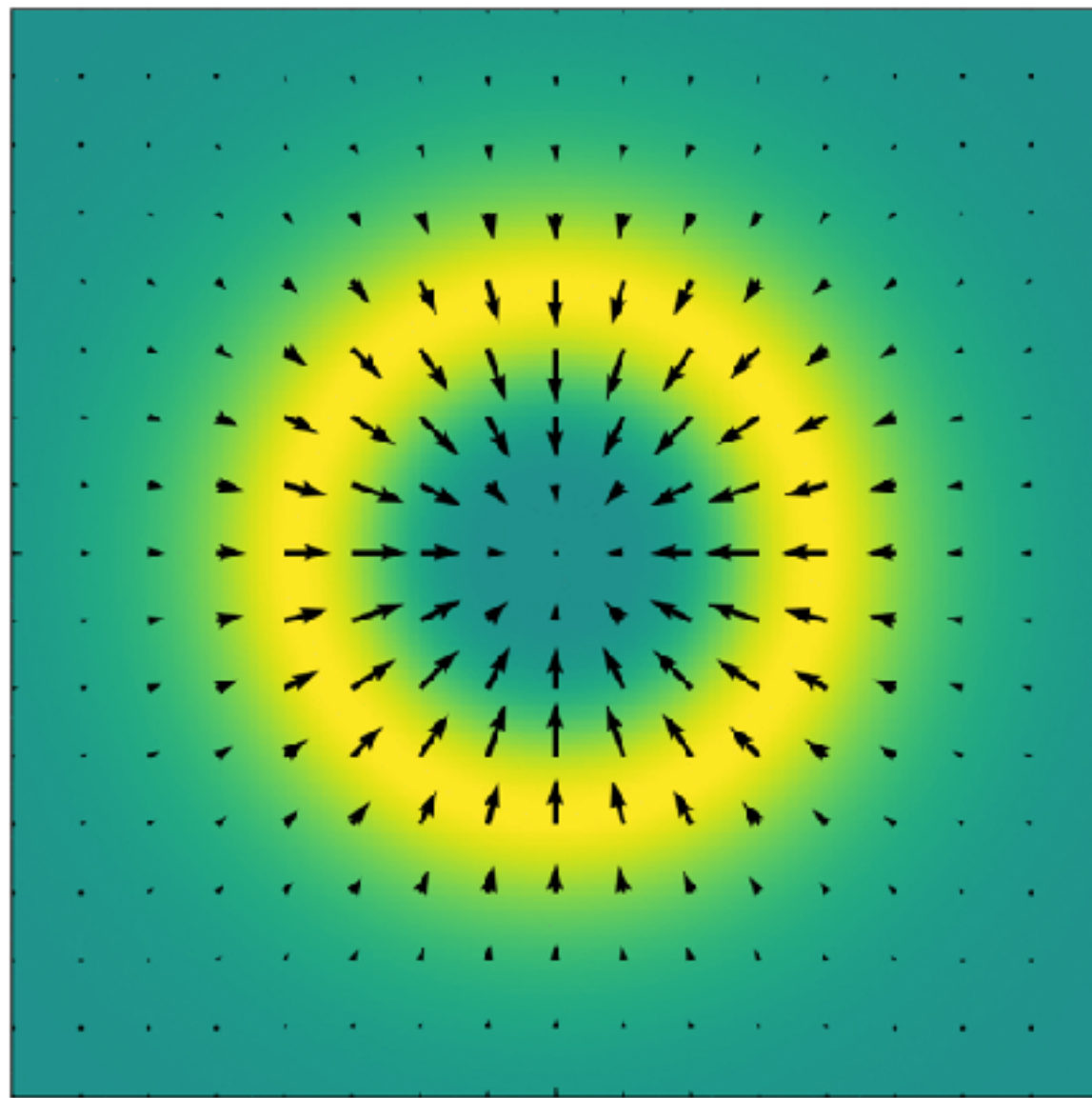
* for dilute ones supported by gravity, see Adshead and Lozanov (2021), for analogs in complex vector fields for the hedgehog case, see Loginov (2015)

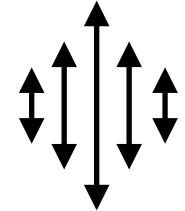
Vector oscillons

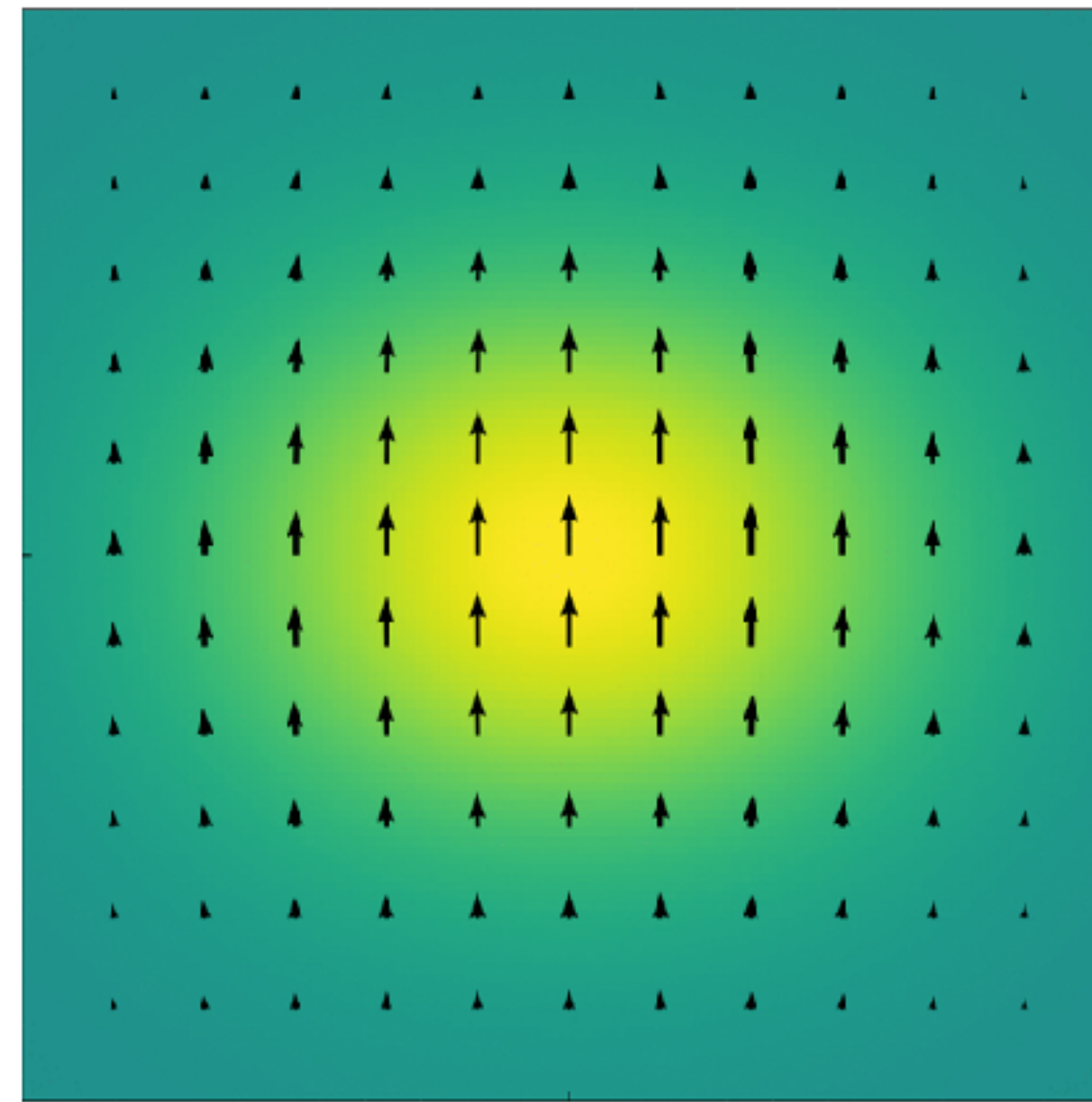
WORK IN
PROGRESS

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right]$$

hedgehog oscillon 



directional oscillon (easier to form) 



Zhang & MA (coming out < month)

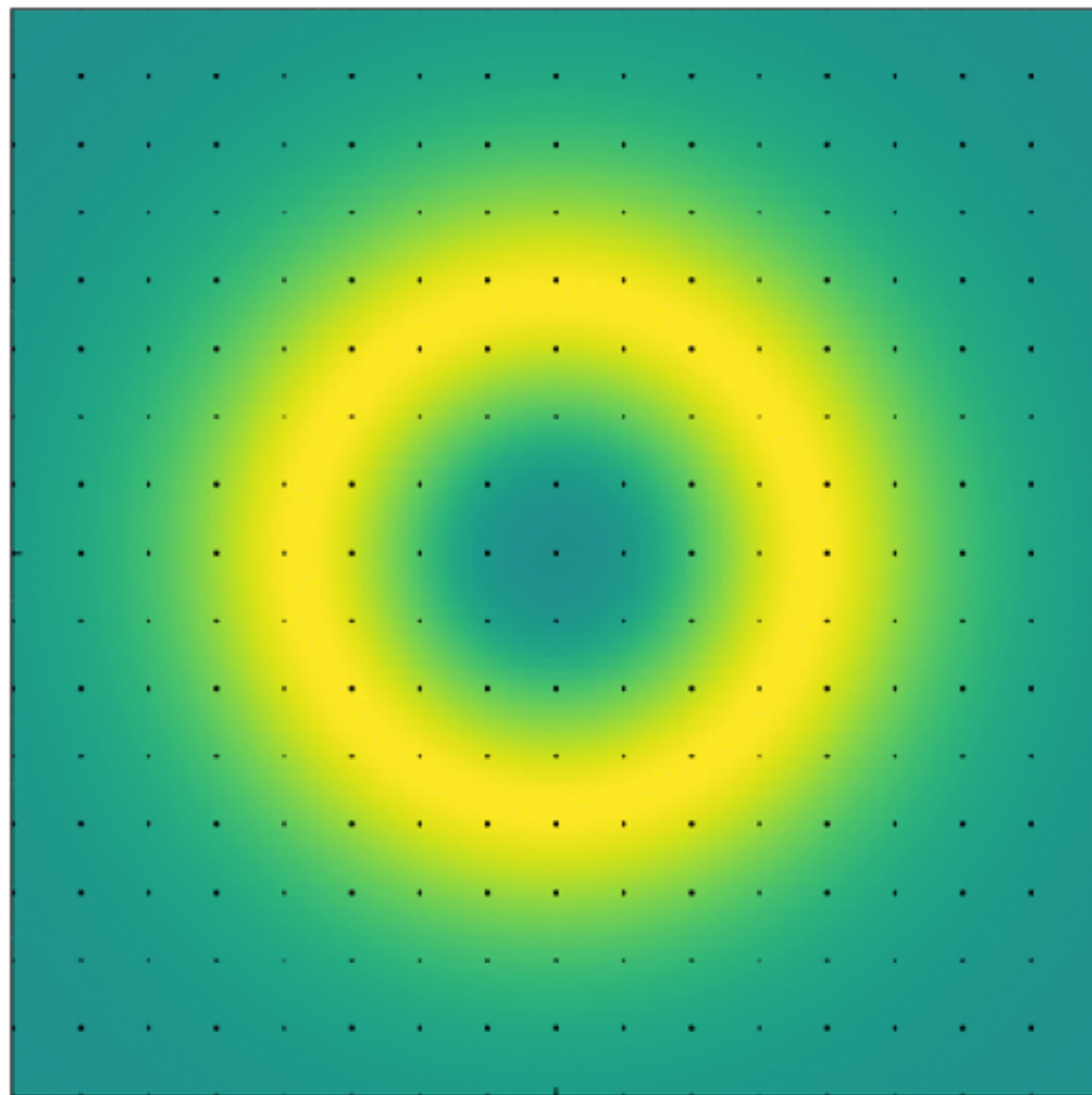
* for dilute ones supported by gravity, see Adshead and Lozanov (2021), for analogs in complex vector fields for the hedgehog case, see Loginov (2015)

Vector oscillons

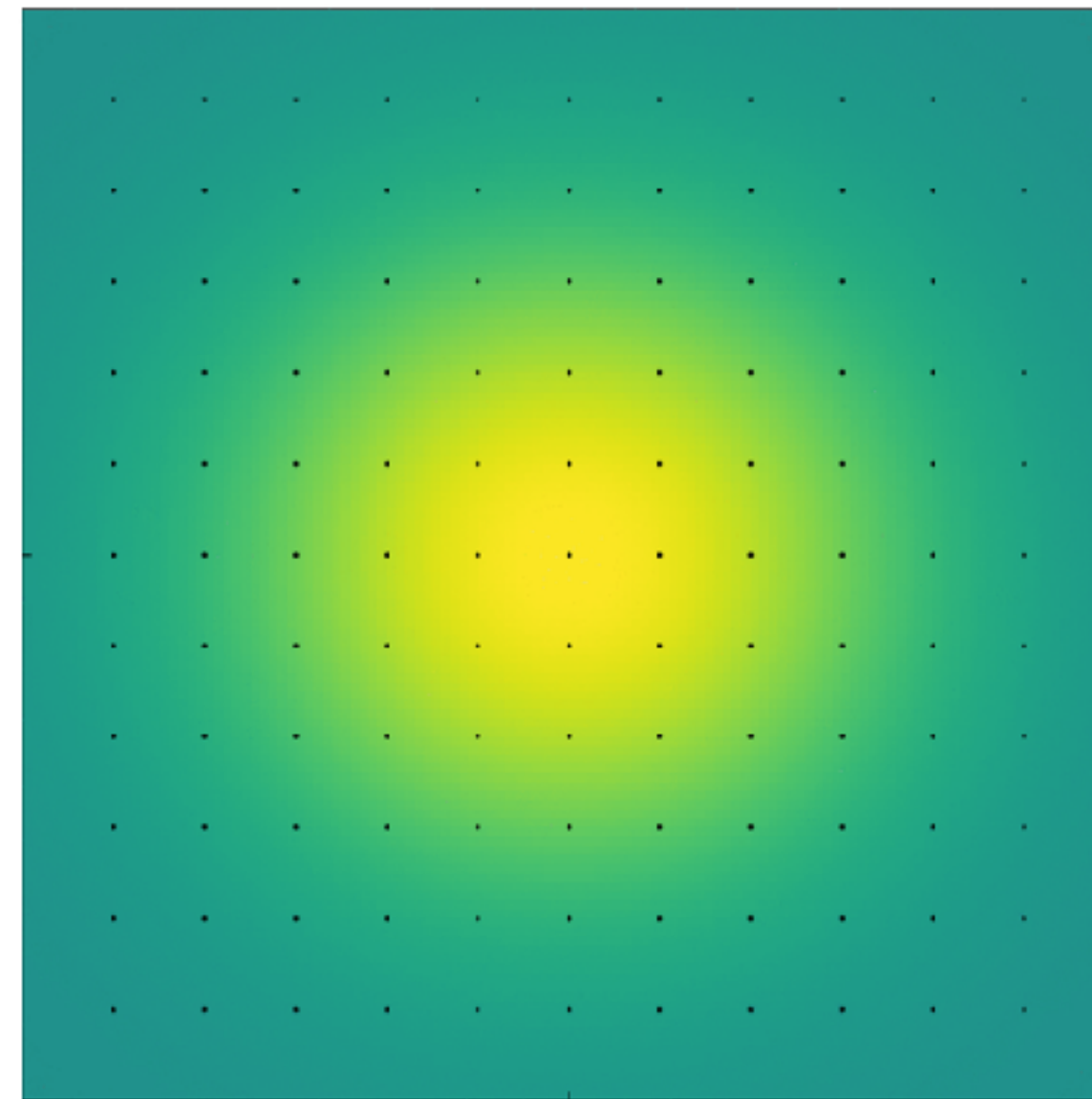
WORK IN
PROGRESS

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right]$$

hedgehog oscillon 



directional oscillon (easier to form) 



Zhang & MA (coming out < month)

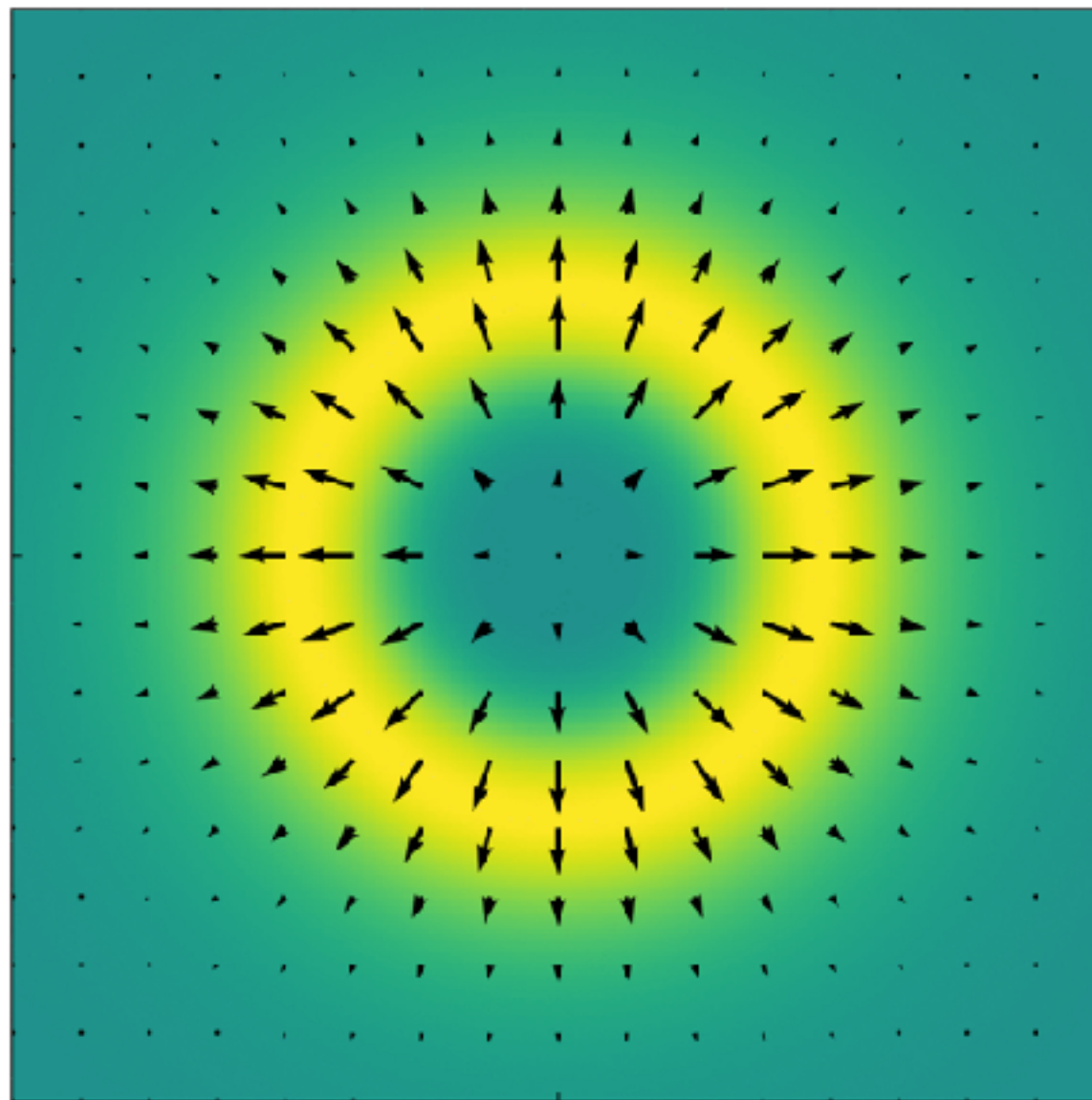
* for dilute ones supported by gravity, see Adshead and Lozanov (2021), for analogs in complex vector fields for the hedgehog case, see Loginov (2015)

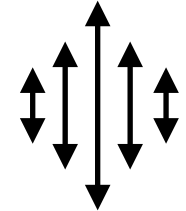
Vector oscillons

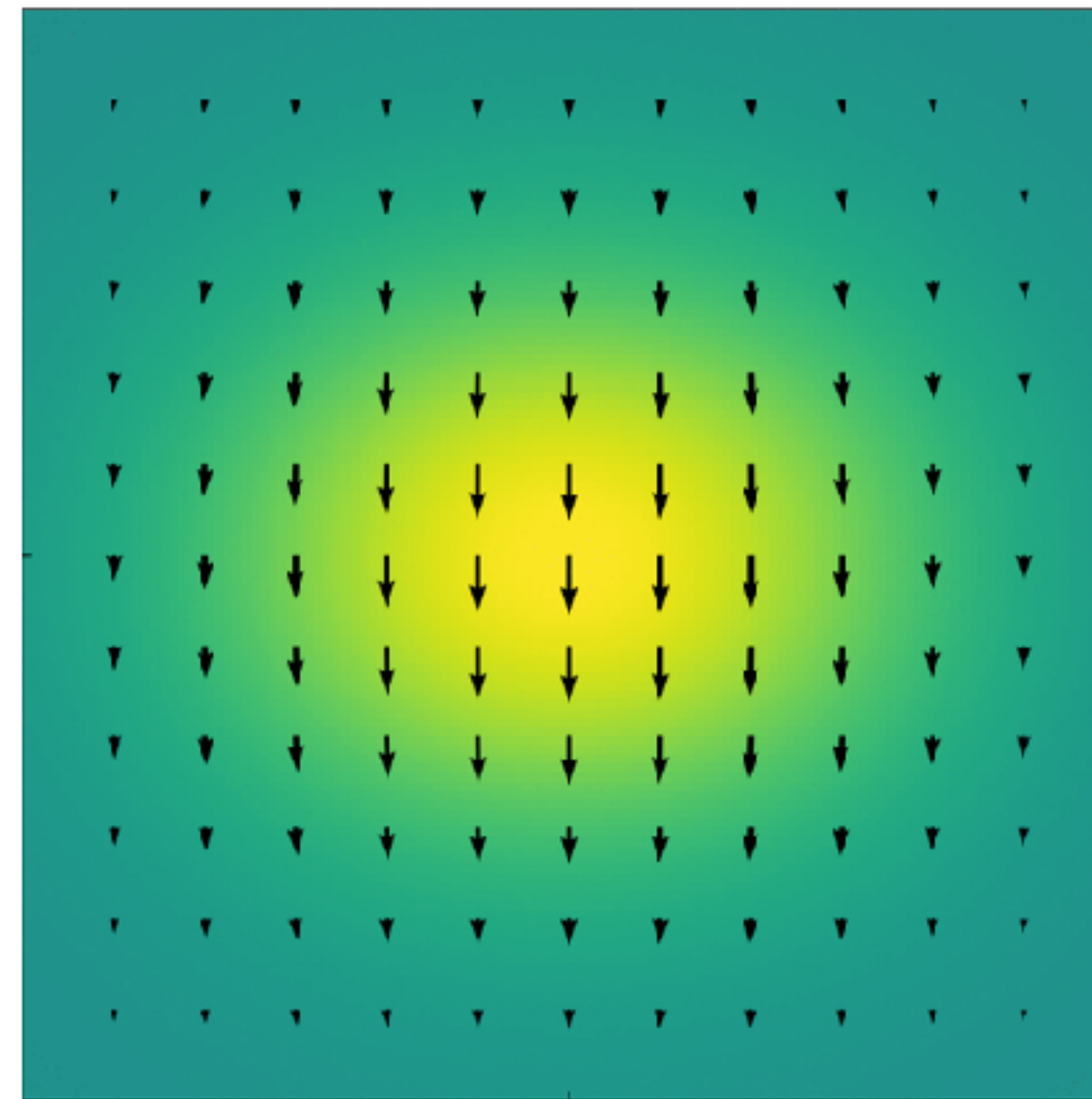
WORK IN
PROGRESS

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right]$$

hedgehog oscillon 



directional oscillon (easier to form) 



Zhang & MA (coming out < month)

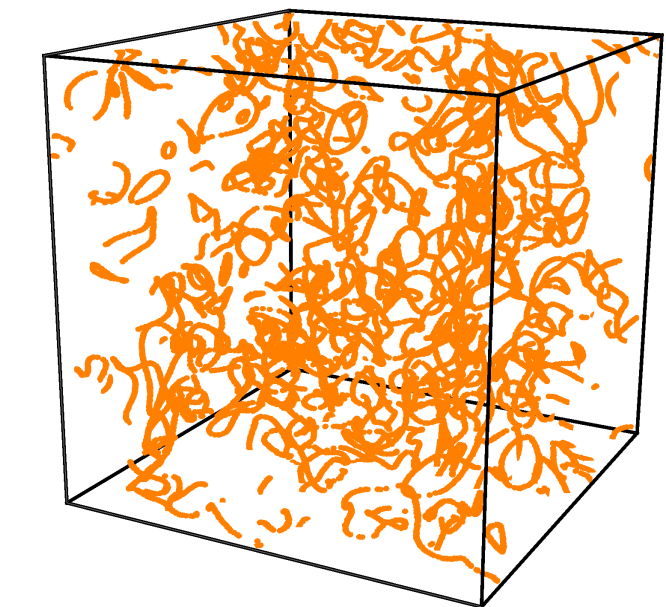
* for dilute ones supported by gravity, see Adshead and Lozanov (2021), for analogs in complex vector fields for the hedgehog case, see Loginov (2015)

lots more to explore!

$$S = \int d^4x \sqrt{-g} \left[\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\phi)^2 - V(\phi) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{g_{\phi\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{2} m_\gamma^2 A^2 + V_{\text{nl}}(A^2) \right. \\ \left. - \frac{1}{2} (\partial\chi)^2 - m_\chi^2 \chi^2 + g_{\phi\chi} \phi \chi^2 + \dots \right. \\ \left. - \bar{\psi} (i\gamma \cdot \partial - m) \psi - g_{\phi\psi} \phi \bar{\psi} \psi + \dots \right]$$

* Abelian Higgs / GFIRE (Lozanov & MA 2019)

1603.05663, 1911.06827

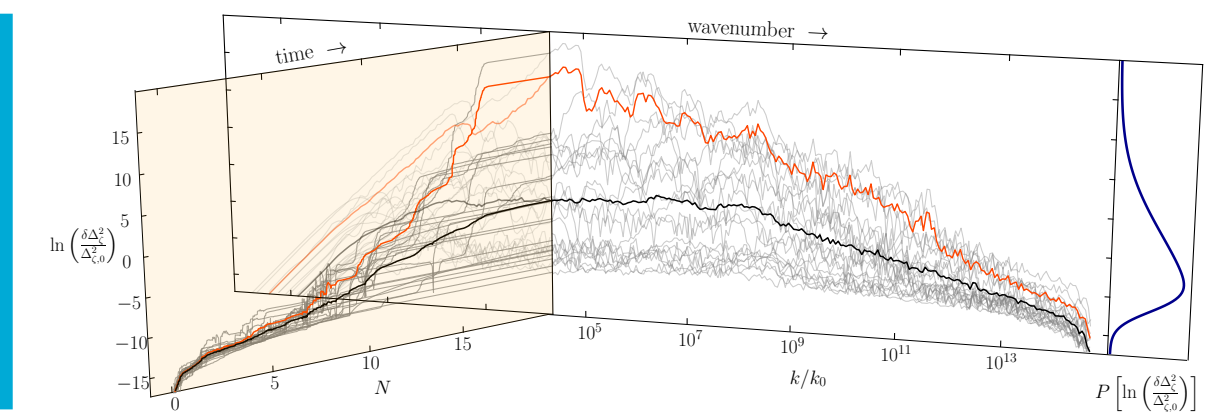


* thermal vs. non-thermal effects, see for example Garcia & MA 2018

1806.01865

* towards model independent characterization: *Wires to Cosmology* (MA, Baumann, Carlsten, Garcia, Green, Wen +)

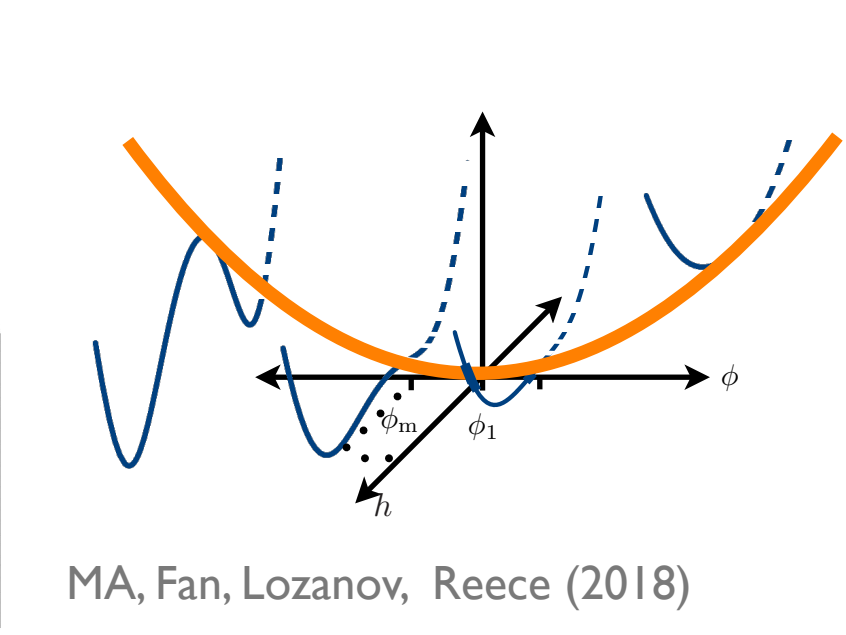
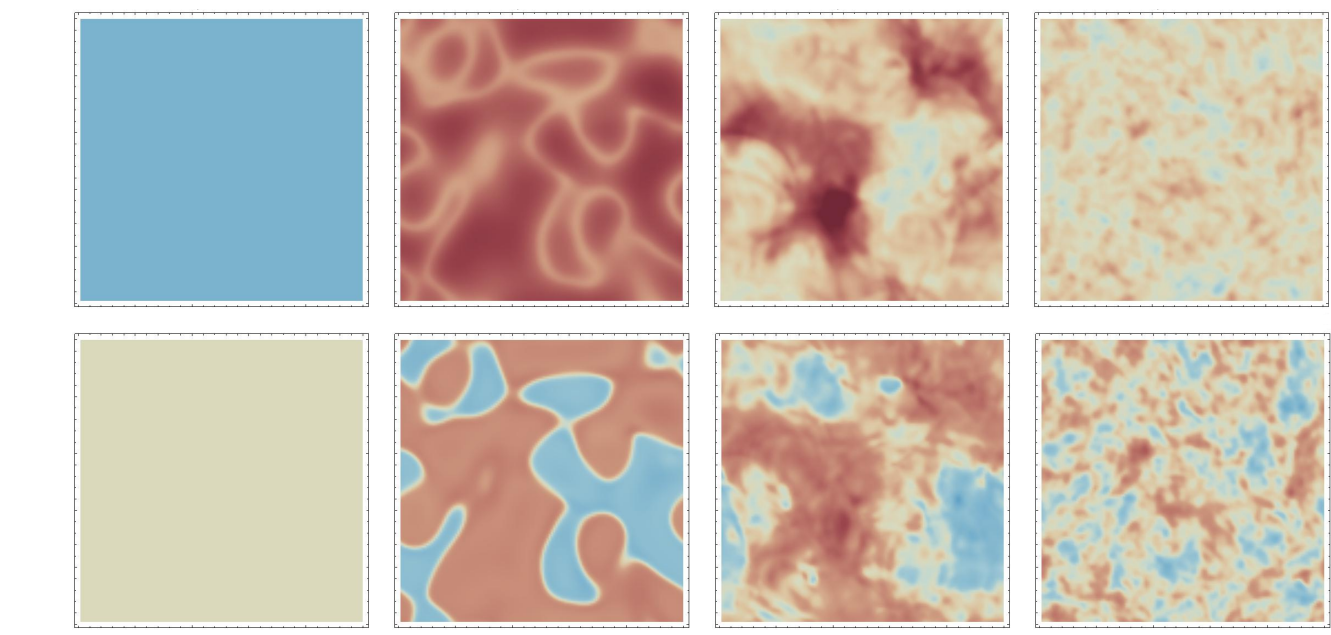
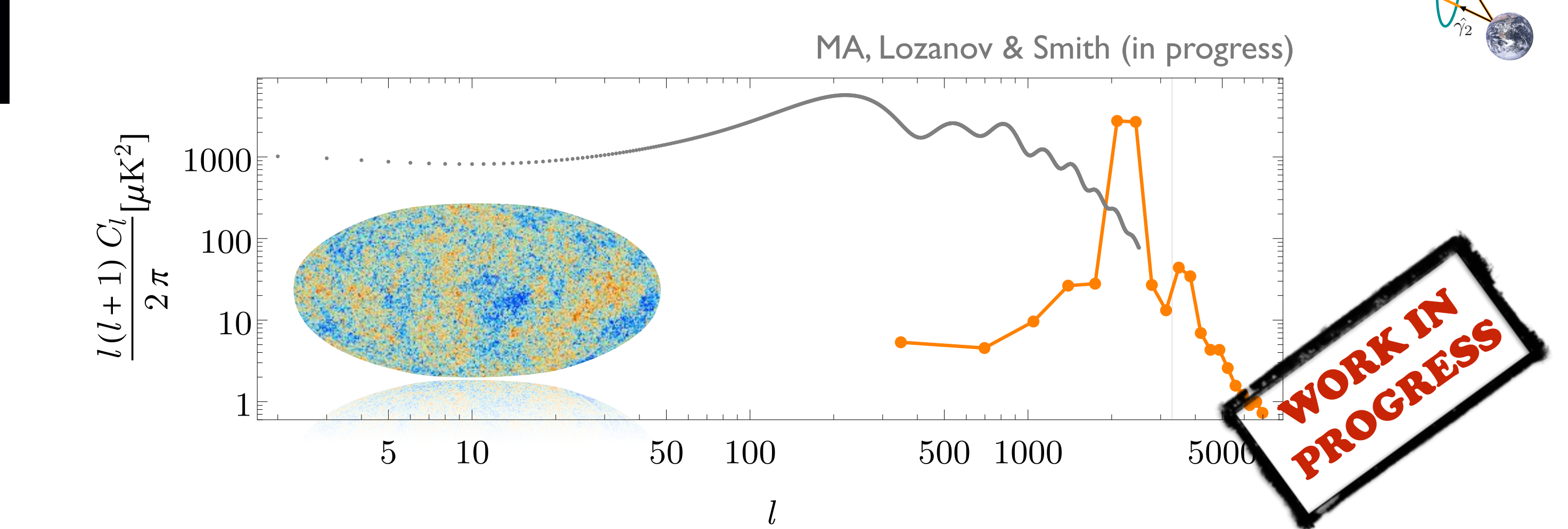
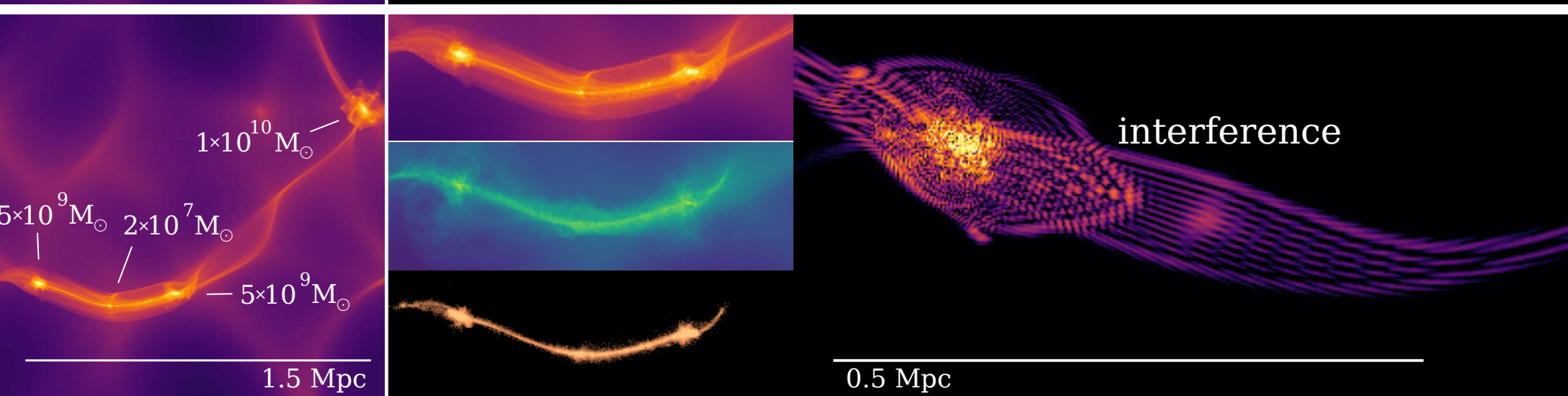
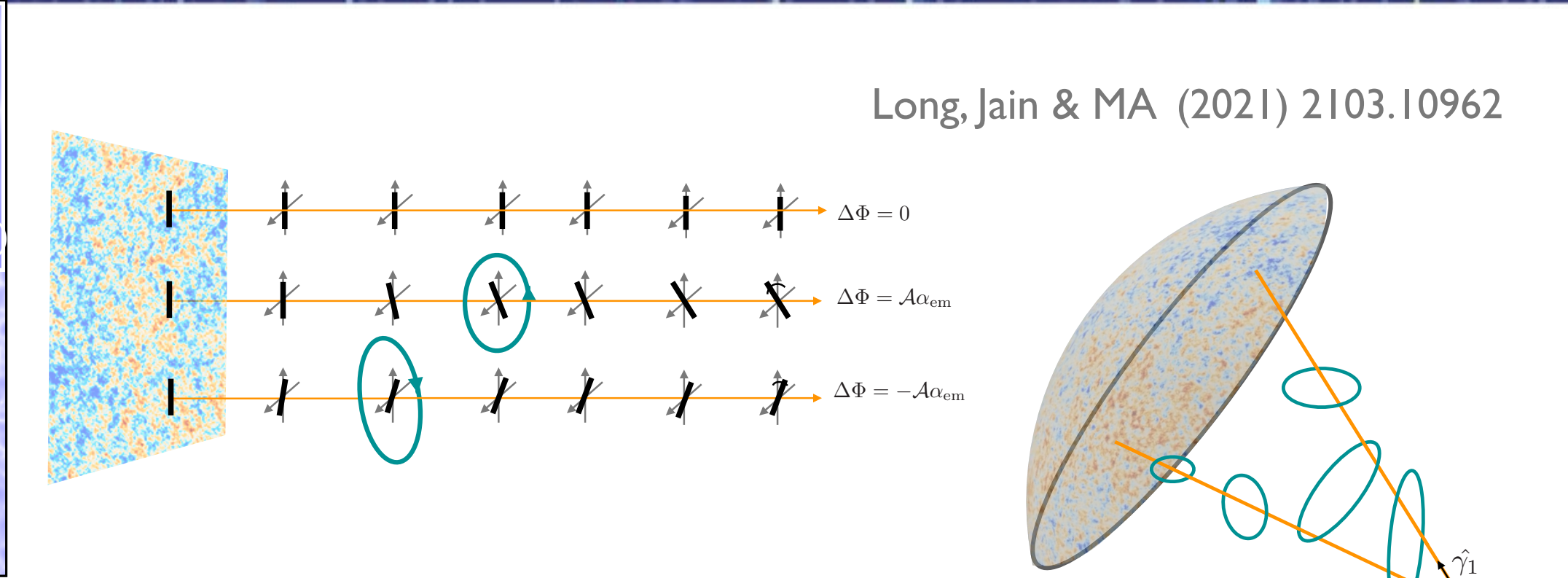
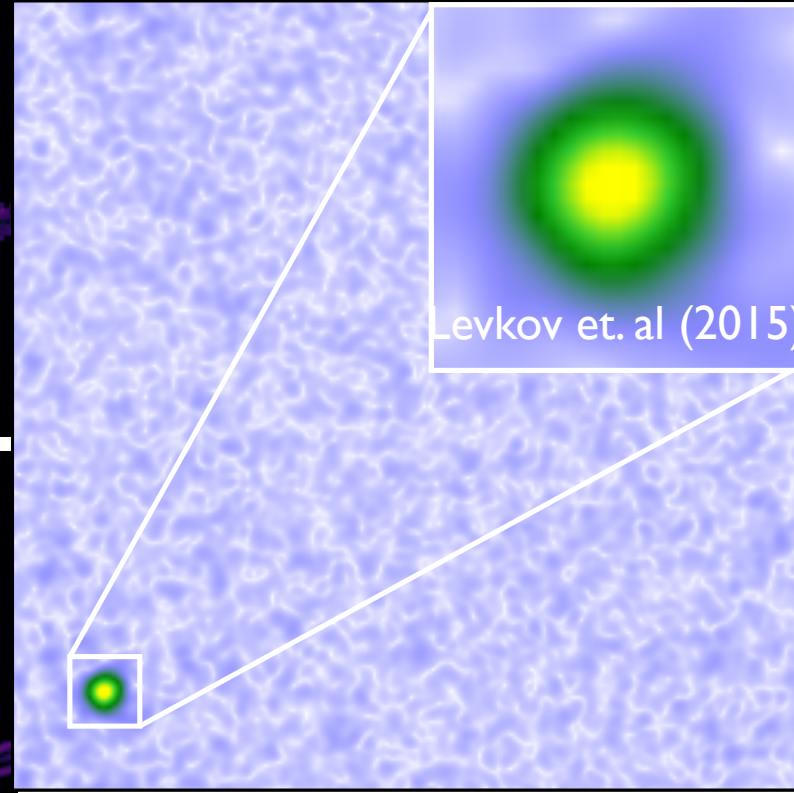
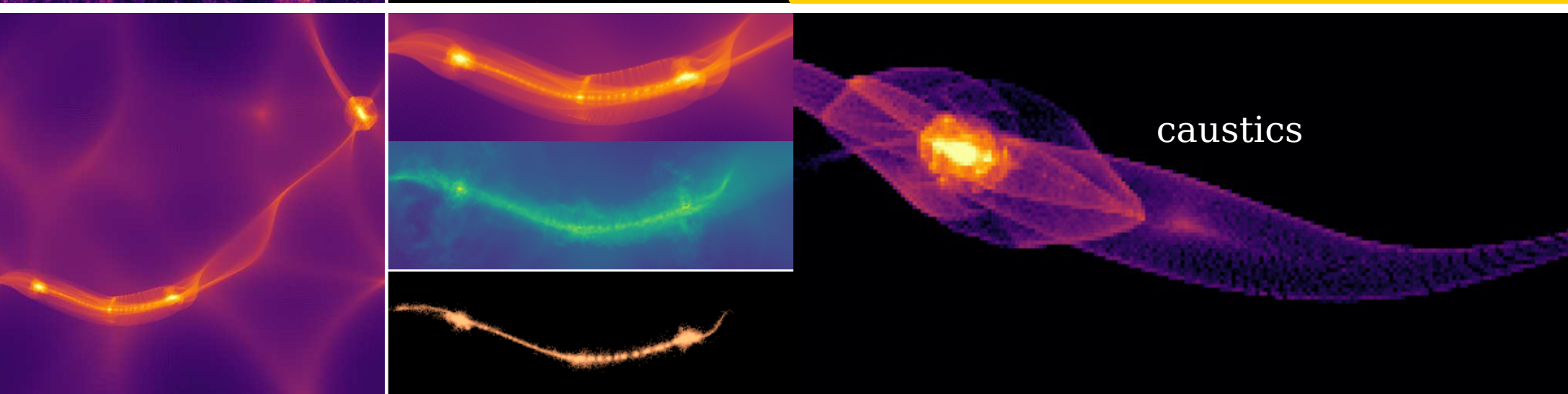
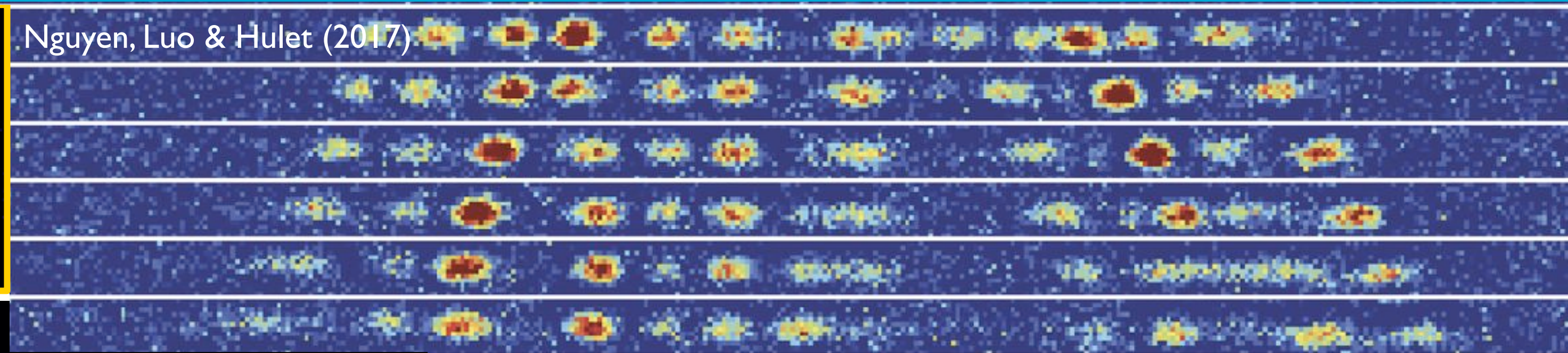
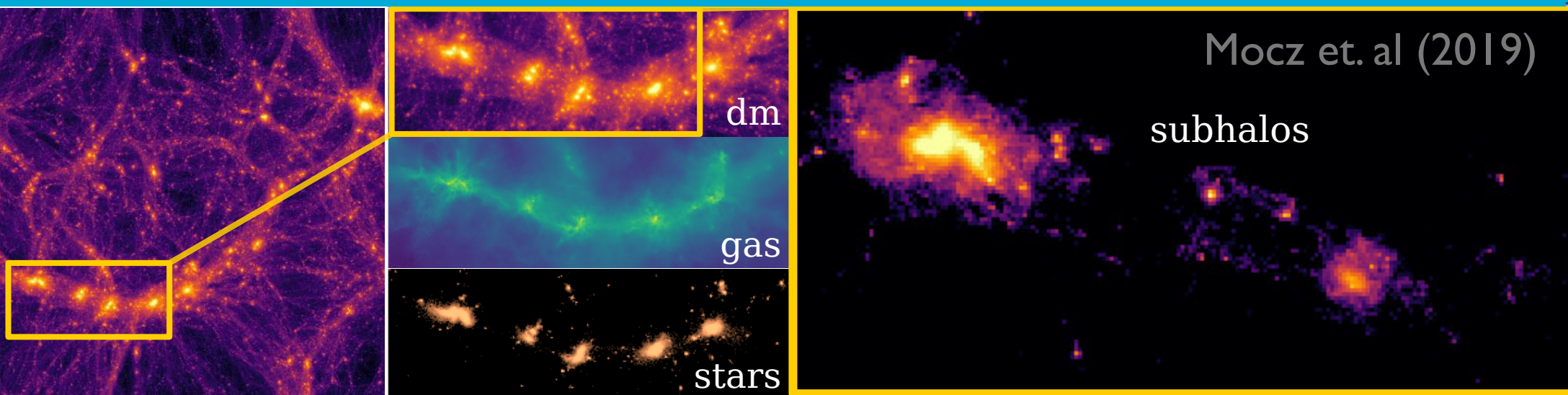
2001.09158, 1512.02637



(also earlier paper on random potentials, for example McAllister et. al 2012, and recent multifield reheating, Martin & Pinol 2021)

* lots more to explore: see talk by Qianshu Lu on “Spillway Preheating” (Fan, Lozanov and Lu 2021 2101.11008)

related phenomenology for moduli, axions, early dark energy etc. and BECs



For a general moduli review, see Kane Watson and Sinha (2015)

after inflation: a GAP in our cosmic history

