



# Challenges in Flavor Physics



Dean Robinson

PPC

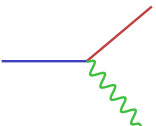
May 2021



# SM Flavor

**Nutshell:** How do we describe quark/lepton interactions?

SM EW Lagrangian:

$$\mathcal{L}_{EW} = \frac{g_2}{\sqrt{2}} (u \quad c \quad t) \not{W} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$


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CKM matrix		
3 × 3 unitary ~		
1	0.2	4 × 10 <sup>-3</sup>
0.2	1	4 × 10 <sup>-2</sup>
4 × 10 <sup>-3</sup>	4 × 10 <sup>-2</sup>	1

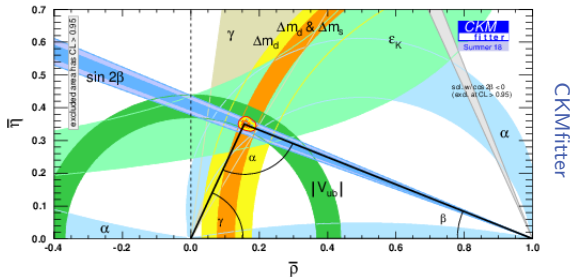
In the SM:

- Flavor changing processes through electroweak charged currents (CC)
- No tree-level flavor changing neutral currents (FCNC)
- Similar story for charged leptons with  $\nu$  masses

# Flavor Data

Can test SM flavor structure with CKM unitarity triangles, e.g.

$$V_{tb}^* V_{td} + V_{cb}^* V_{cd} + V_{ub}^* V_{ud} = 0$$



- **Huge multitude** of physical observables projected onto CKM parameter plane (from decays, (in)direct CP violation, mass splittings  $\Delta m$ ...)
- SM  $\implies$  all allowed regions should intersect. **Lesson: Good agreement with SM flavor structure**
- Leads to **powerful constraints** and **powerful discovery potential**

# New Physics (NP) Constraints

## History:

- $n \rightarrow p e \nu$ : Energy scale  $\sim$  MeV, **probes** EW current at  $\sim$  100 GeV!
- $\Delta m_K / m_K \simeq 7 \times 10^{-15}$  **predicted** charm,  $m_c \sim$  1–2 GeV

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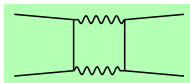
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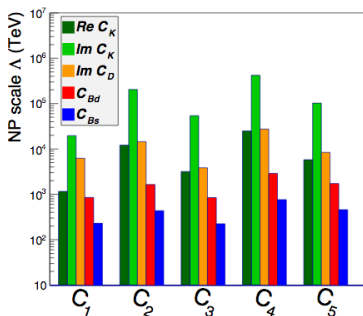
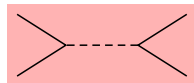
Constraints on 4-Fermi FCNC operators from e.g. **meson mixing**

$$\frac{(\bar{q}\Gamma q')(\bar{q}'\Gamma'q)}{\Lambda^2}$$

via:



vs



Indirect access to scales  
 $\sim 10^4$  TeV **far above**  
 LHC direct production!

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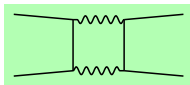
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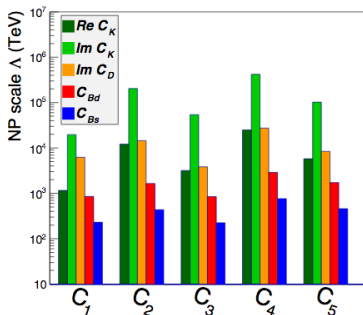
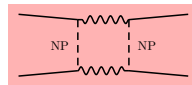
Constraints on 4-Fermi FCNC operators from e.g. **meson mixing**

$$\frac{V_{td} V_{ts}}{16\pi^2} \frac{(\bar{q}\Gamma q')(\bar{q}'\Gamma' q)}{\Lambda^2}$$

via:



vs

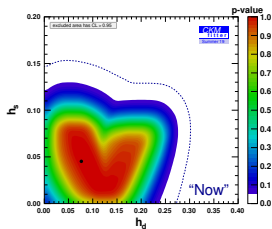


Indirect access to scales  
 $\sim 10^4$  TeV **far above**  
 LHC direct production!

But, with loop +  
 CKM suppression:  
 NP/SM  $\sim 20\%$  in  
 FCNC still compatible!

# Loop-level sensitivities

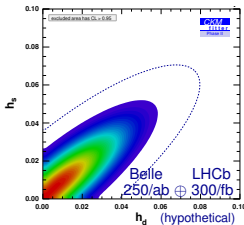
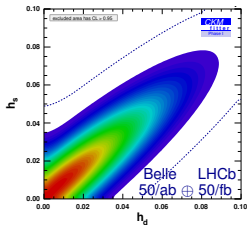
## Future sensitivity to NP in $B$ mixing



- What NP parameter space can be probed?

- $h_{d,s} \Leftrightarrow$  NP scale:  $h \simeq \frac{|C_{ij}|^2}{|V_{ti}^* V_{tj}|^2} \left( \frac{4.5 \text{ TeV}}{\Lambda} \right)^2$  [2006.04824]

Couplings	NP loop order	Sensitivity for Summer 2019 [TeV]		Phase I Sensitivity [TeV]		Phase II Sensitivity [TeV]	
		$B_d$ mixing	$B_s$ mixing	$B_d$ mixing	$B_s$ mixing	$B_d$ mixing	$B_s$ mixing
$ C_{ij}  =  V_{ti} V_{tj}^* $	tree level	9	13	17	18	20	21
(CKM-like)	one loop	0.7	1.0	1.3	1.4	1.6	1.7
$ C_{ij}  = 1$	tree level	$1 \times 10^3$	$3 \times 10^2$	$2 \times 10^3$	$4 \times 10^2$	$2 \times 10^3$	$5 \times 10^2$
(no hierarchy)	one loop	80	20	$2 \times 10^3$	30	$2 \times 10^3$	40



Big improvements in 2020s

Complementary to high- $p_T$  searches

Then theory improves or progress slows

Courtesy Z Ligeti





# Lepton Flavor Universality



## LFU tested to great precision



### LFU tests with 1<sup>st</sup>/2<sup>nd</sup> gen.

To **0.28%** in  
Z decays

$$\frac{\Gamma_{Z \rightarrow \mu\mu}}{\Gamma_{Z \rightarrow ee}} = 1.0009 \pm 0.0028$$

LEP, Phys. Rept. 427 (2006) 257

To **0.8%** in  
W decays

$$\frac{\mathcal{B}(W \rightarrow e\nu)}{\mathcal{B}(W \rightarrow \mu\nu)} = 1.004 \pm 0.008$$

CDF + LHC, JPG, NPP, 46, 2 (2019)

To **0.31%** in  
meson decays

$$\frac{\Gamma_{J/\psi \rightarrow \mu\mu}}{\Gamma_{J/\psi \rightarrow ee}} = 1.0016 \pm 0.0031$$

PDG (BESIII), RPP, Chin. Phys. C 40 (2016) 100001

$$\frac{\Gamma_{K \rightarrow e\nu}}{\Gamma_{K \rightarrow \mu\nu}} = (2.488 \pm 0.009) \times 10^{-5}$$

PDG (NA62), RPP, Chin. Phys. C 40 (2016) 100001

$$\frac{\Gamma_{\pi \rightarrow e\nu}}{\Gamma_{\pi \rightarrow \mu\nu}} = (1.230 \pm 0.004) \times 10^{-4}$$

PDG, Phys. Rev. Lett. 115, 071801 (2015)

To **0.14%** in  
 $\tau \rightarrow \ell\nu\nu$

$$g_\mu/g_e = 1.0018 \pm 0.0014$$

PDG, A. Pich, Prog. Part. Nucl. Phys. 75 (2014) 41

### LFU tests with 3<sup>rd</sup> gen.

To **0.32%** in  
Z decays

$$\frac{\Gamma_{Z \rightarrow \tau\tau}}{\Gamma_{Z \rightarrow ee}} = 1.0019 \pm 0.0032$$

LEP, Phys. Rept. 427 (2006) 257

**2.6 $\sigma$  tension** in  
W decays

$$\frac{\Gamma_{W \rightarrow \tau\nu}}{\Gamma_{W \rightarrow \mu\nu}} = 1.070 \pm 0.026$$

LEP, Phys. Rept. 532 (2013) 119

To **1.3%** in  
W decays

$$\frac{\Gamma_{W \rightarrow \tau\nu}}{\Gamma_{W \rightarrow \mu\nu}} = 0.992 \pm 0.013$$

ATLAS, arXiv:2007.14040

To **6.1%** in  
 $D_s$  decays

$$\frac{\Gamma_{D_s \rightarrow \tau\nu}}{\Gamma_{D_s \rightarrow \mu\nu}} = 9.95 \pm 0.61$$

HFLAV, Int. Phys. J. 377 (2017) 395

To **0.15%** in  
 $\tau \rightarrow \ell\nu\nu$  (with  $\tau_\tau$ )

$$g_\tau/g_\mu = 1.0030 \pm 0.0015$$

PDG, S. Pich, Prog. Part. Nucl. Phys. 75 (2014) 41

# (Rough) Perspectives on Flavor Probes

Precision Th.  
Control

NP

Smoking Guns

Tensions:

Measurements vs predictions

- $|V_{cb}|, |V_{ub}|$
- $(g-2)_\mu$
- $\Delta A_{CP}$  in charm
- $b \rightarrow s\mu\mu$
- ...

Precision Flavor

Flavor Models

Explain SM hierarchies:  
Quark/lepton mass and mixing  
Can imply NP signals

SM

Enhancement of  
rare/forbidden SM

Flavor symmetry violation

- $K \rightarrow \pi\nu\nu$
- $\mu \rightarrow e$
- $b \rightarrow c\ell\nu$ :  $\tau$  vs  $e, \mu$
- $b \rightarrow s\ell\ell$ :  $e$  vs  $\mu$
- CKM Unitarity
- ...

Constrain high NP scales  
(no obs  $\gg$  SM prediction)

- $B_s \rightarrow \mu\mu$
- $\Delta M_{s,d}$
- $b \rightarrow s\nu\nu$
- ...

Theoretically  
Clean

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Enhancement of rare/forbidden SM

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Precision Flavor

Constraints  
(no obs)

- $B_s \rightarrow \mu\mu$
- $\Delta M_{s,d}$
- $b \rightarrow s\nu\bar{\nu}$
- ...

Today: mainly look at challenges in Heavy Flavor

Flavor mixing

Can imply NP signals

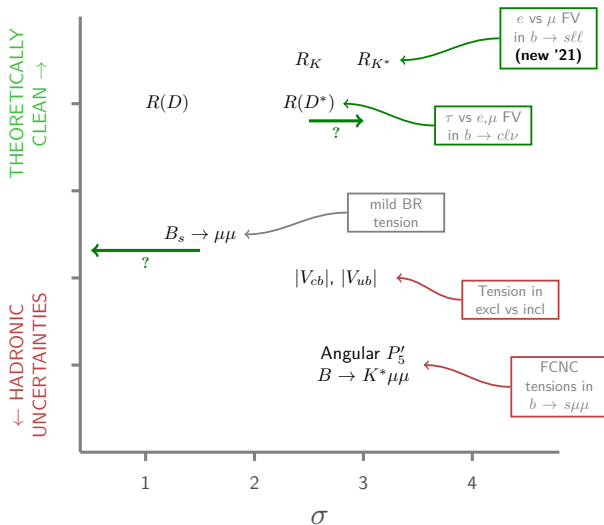
SM

Theoretically  
Clean

See also Bhupal Dev's talk on Monday; Sheldon Stone's talk today

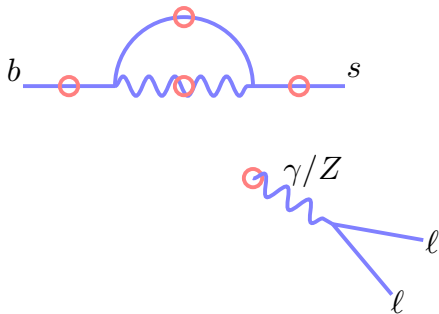
# Space of Heavy Flavor Anomalies

Involving  $B_q = (bq)$  mesons



Adapted from Z Ligeti and W Altmannshofer

# Rare decays: $b \rightarrow sll$

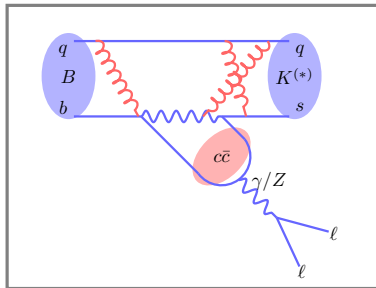
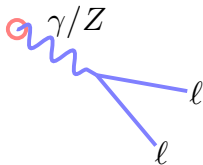
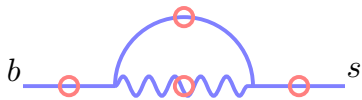


- Loop (penguin) process

$$\mathcal{M} \sim \frac{1}{16\pi^2} \frac{g^4}{m_W^2} V_{ts} V_{tb} \frac{m_t^2}{m_W^2}$$

- Experimentally clean signal:  $B \rightarrow K^{(*)} ll$

# Rare decays: $b \rightarrow s \ell \ell$



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- Experimentally clean signal:  $B \rightarrow K^{(*)} \ell \ell$
- But **hadronic uncertainties** less clear (long distance  $c\bar{c}$ )

# Lepton Universality Tests

Factor out hadronic uncertainties: Consider ratio

$$R_{K^{(*)}} = \frac{B \rightarrow K^{(*)} \mu \mu}{B \rightarrow K^{(*)} e e} \quad (\text{in various } q^2 \text{ binnings})$$

Should be  $1.00 \pm 0.01$  in SM!

Bordone, Isidori, Pattori [1605.07633]

New Run II result from LHCb;

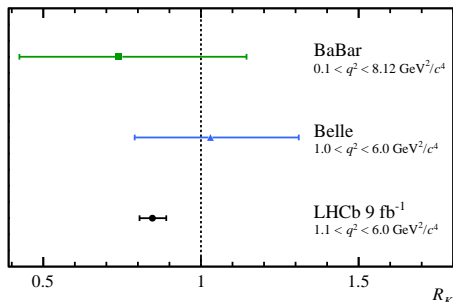
$$1.1 \leq q^2 \leq 6 \text{ GeV}^2$$

$$\text{Prior: } R_{K^+} = 0.846^{+0.060+0.016}_{-0.054-0.014}$$

$$\text{Updated: } R_{K^+} = 0.846^{+0.042+0.013}_{-0.039-0.012}$$

Tension now at  $2.5 \rightarrow 3.1\sigma$

[For eagle-eyed, central value remained the same despite shifts in the  $K_{ee}$  fit, likely because of slight changes in analysis technique]



LHCb-PAPER-2021-004

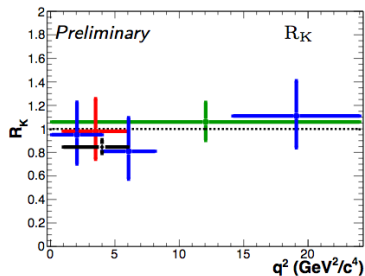
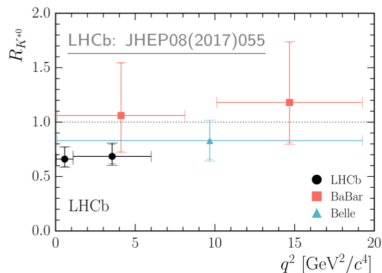
# Lepton Universality Tests

Also in the  $1.1 \leq q^2 \leq 6 \text{ GeV}^2$  bin

$$R_{K^*0} = 0.71^{+0.12}_{-0.09}$$

<https://hflav.web.cern.ch/>

- LHCb update of  $R_{K^*0}$  in the near term?
- Belle, BaBar in other  $q^2$  bins compatible with SM



Belle EPS-HEP [Choudhury]



# Rare Leptonic Decays

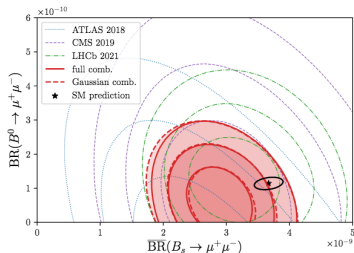
Associated meas. of  $B_{(s)} \rightarrow \mu\mu$

Combination ATLAS+CMS+LHCb:

$$BR_{\text{exp}}(B_s \rightarrow \mu\mu) = (2.93 \pm 0.35) \times 10^{-9}$$

$$BR_{\text{SM}}(B_s \rightarrow \mu\mu) = (3.67 \pm 0.15) \times 10^{-9}$$

Approx  $2\sigma$  tension



Altmannshofer, Stangl 2103.13370

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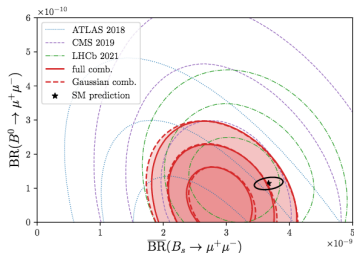
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**Caveat:** The SM prediction

$$BR_{\text{SM}}(B_s \rightarrow \mu\mu) \sim |C_{10}^{\text{SM}} V_{tb} V_{ts}^*|^2 f_{B_s}(\dots)$$

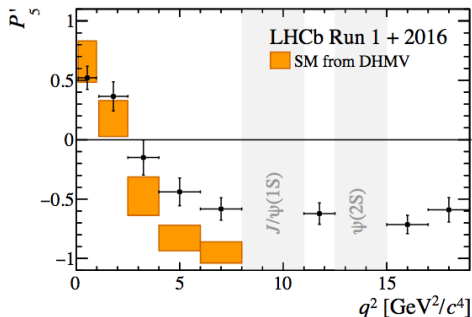
Wilson Coeff  
known to high  
precision

$b - s$  CKM unitarity: Sen-  
sitive to  $|V_{cb}|$  incl-excl. ten-  
sion (below)! [Using exclusive  
 $|V_{cb}|$  determination could relax  
BR tension entirely?!]

# Puzzle: Precision moments

Measure angular distributions in

$$B \rightarrow K^*(\rightarrow K\pi)\mu\mu$$

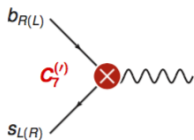


LHCb-PAPER-2020-002

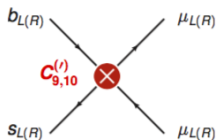
Deviations of about  $2.5\sigma$  in several  $q^2$  bins, but SM predictions are **hard**. [see also 'ASZB' SM predictions]

# NP Explanations?

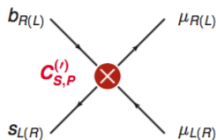
magnetic dipole operators



semileptonic operators



scalar operators



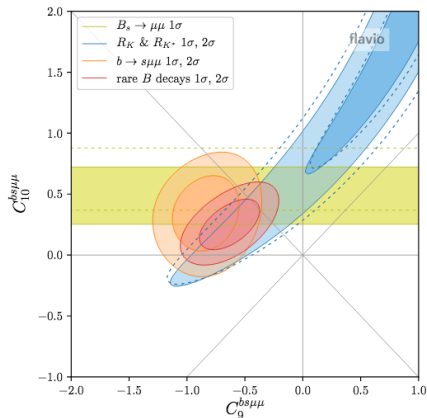
Courtesy W Altmannshofer

SM-like SL operators at dimension-6:

$$\frac{C_9^{(r)}}{\Lambda^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\mu \gamma^\mu \mu) + \frac{C_{10}^{(r)}}{\Lambda^2} (\bar{s} \gamma_\mu P_{L(R)} b) (\mu \gamma^\mu \gamma^5 \mu)$$

Normalized against loop SM:  $\Lambda \sim 4\pi v / \sqrt{V_{tb} V_{ts}} \sim 10 \text{ TeV}$ .  
 Expect 10 TeV scale NP

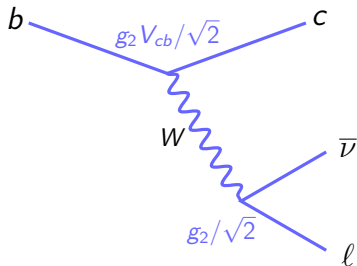
# Global NP Fit



Altmannshofer, Stangl 2103.13370

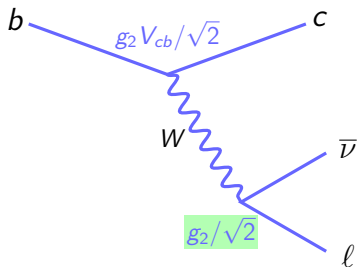
- **Large** amount of NP model building
- Typically leptoquarks or  $Z'$  models (e.g. gauged  $L_\mu - L_\tau$ )
- Some attempts to relate to  $R(D^{(*)})$  [Next!]

# Semileptonic Decays: $b \rightarrow cl\nu$



- Tree-level  $W$  exchange (in the SM)
- Approx. 25% of all  $B$  decays: huge statistics!

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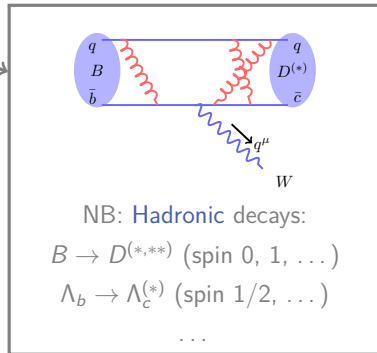
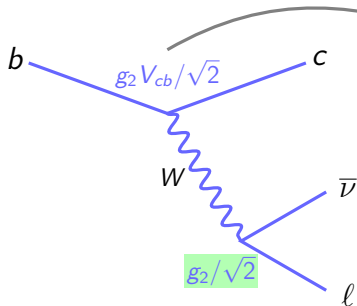
Probe of lepton flavor universality

$g_2$  ( $l = e, \mu, \tau$ ) up to masses:

$m_\tau \simeq 1777\text{MeV}$  vs  $m_\mu = 105\text{MeV}$ ;

PS and hadronic effects

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 PS and hadronic effects

Measurement of  $|V_{cb}|$  **inclusively** (OPE)  
**Hadronic matrix elements**  $\implies$  **measure**  
 $|V_{cb}|$  in exclusive  $l = e, \mu$  modes



# Two Anomalies/Puzzles

1. **Inclusive**  $B \rightarrow X_c l \nu$  versus **exclusive**  $B \rightarrow D^* l \nu$

Measurement is done with  $l = e, \mu$ : The  $\tau$  mode involves more  $\nu$ 's from  $\tau$  decays and less statistics

$$|V_{cb}|_{X_c} \simeq (42.2 \pm 0.8) \times 10^{-3}$$

$$|V_{cb}|_{D^*} \simeq (38.7 \pm 0.7) \times 10^{-3}$$

A  $3\sigma$  tension?!?

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$BR_{SM}(B_s \rightarrow \mu\mu) = 3.08(12) \times 10^{-9}$   
versus  $2.93(35) \times 10^{-9}$ .  
No more anomaly!?  
Cf  $|V_{ts}| \sim 38.8(1) \times 10^{-3}$   
in PDG

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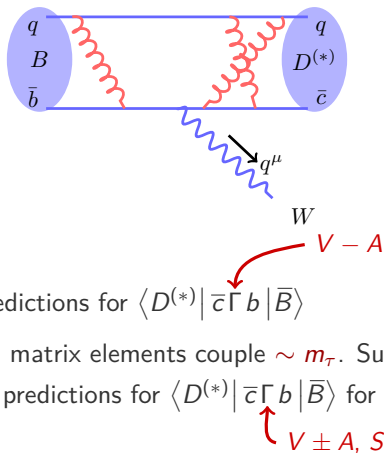
2. Factor out  $|V_{cb}|$ , measure lepton flavor universality violation (LFUV) ratios

$$R(H_c) \equiv \frac{\Gamma[H_b \rightarrow H_c \tau \nu]}{\Gamma[H_b \rightarrow H_c l \nu]}, \quad l = e, \mu.$$

$H_b :$	$B$	$B_s$	$\Lambda_b$	$B_c$
$H_c :$	$D, D^*, D^{**}$	$D_s^{(*,**)}$	$\Lambda_c, \Lambda_c^*$	$J/\psi$

# Puzzle: Hadronic Matrix Elements

For **exclusive processes**: Main **theory uncertainty** is mapping partons  $\rightarrow$  hadrons:



- $|V_{cb}|$ : Need SM predictions for  $\langle D^{(*)} | \bar{c} \Gamma b | \bar{B} \rangle$
- $R(D^{(*)})$ : Some SM matrix elements couple  $\sim m_\tau$ . Suppressed in  $e, \mu$ .
- $R(D^{(*)})$ : Need NP predictions for  $\langle D^{(*)} | \bar{c} \Gamma b | \bar{B} \rangle$  for any NP current
- Use **parametrizations** of form factors. **Ultimate(?)**: Lattice calculations

# $|V_{cb}|$ Determination

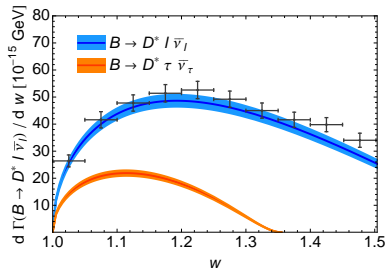
Represent  $B \rightarrow D^*$  matrix elements wrt form factors (FF):

$$\langle D^* | \bar{c} \Gamma^\mu b | \bar{B} \rangle \sim FF_\epsilon(q^2) \epsilon^\mu + FF_B(q^2) p_B^\mu + FF_{D^*}(q^2) p_{D^*}^\mu,$$

$$\frac{d\Gamma[B \rightarrow D^* l \nu]}{dw} \sim |V_{cb}|^2 \sqrt{w^2 - 1} \times \mathcal{F}(w)^2, \quad w = (m_B^2 + m_{D^*}^2 - q^2)/(2m_B m_{D^*})$$

Phase space  $\rightarrow 0$   
as  $w \rightarrow 1$

Comb. of FFs.  
 $\mathcal{F}(1)$  computed by  
lattice



- Obtain  $|V_{cb}| \mathcal{F}(1)$  by fitting  $d\Gamma/dw$  and extrapolating to  $w = 1$
- $\mathcal{F}(1)$  from lattice  $\Rightarrow |V_{cb}|$
- Extrapolation into low stats region highly sensitive to FF fit
- Care with choice of FF parametrization and theory inputs!

# $|V_{cb}|$ Developments

- “Traditional” experimental approach uses “CLN” param: HQET plus QCD sum rules (actually inconsistent with heavy quark expansion, but can be repaired [Bernlochner, Ligeti, Papucci, DR \[1703.05330\]](#))

$$|V_{cb}|_{\text{CLN}} = (38.2 \pm 1.5) \times 10^{-3}, \quad 1702.01521 \text{ [Belle]}$$

- **Unfolded**  $B \rightarrow D^* l \nu$  Belle dataset [1702.01521](#). Permitted fits to **different** FF param choices: “BGL” param using only **analyticity** and **unitarity**

$$|V_{cb}|_{\text{BGL}} = (41.7_{-2.1}^{+2.0}) \times 10^{-3}, \quad 1703.06124, 1707.09509 \text{ [Bigi, Gambino, Schacht]}$$
$$|V_{cb}|_{\text{BGL}} = (41.9_{-1.9}^{+2.0}) \times 10^{-3}, \quad 1703.08170 \text{ [Grinstein, Kobach]}$$

- $|V_{cb}|_{\text{incl}} = (42.2 \pm 0.8) \times 10^{-3}$ : Resolves  $|V_{cb}|$  incl vs excl tension? The fits lifting  $|V_{cb}|$  led to **HQET tensions** [BLPR \[1708.07134, 1902.09553\]](#).
- Subsequent **Belle untagged** analysis:

$$|V_{cb}|_{\text{BGL}} = (38.4 \pm 0.7) \times 10^{-3} \quad \text{Belle 1809.03290}$$

- But: Sensitive to truncation order of the BGL expansion [BLPR \[1902.09553\]](#)

# $|V_{cb}|$ Developments

- “Traditional” experimental approach uses “CLN” param: HQET plus QCD sum rules (actually inconsistent with heavy quark expansion, but can be repaired [Bernlochner, Ligeti, Papucci, DR \[1703.05330\]](#))

$$|V_{cb}|_{\text{CLN}} = (38.2 \pm 1.5) \times 10^{-3}$$

- **Unfolded**  $B \rightarrow D^* l \nu$  Belle dataset [1702.01524](#)  
FF param choices: “BGL” param using only

$$|V_{cb}|_{\text{BGL}} = (41.7_{-2.1}^{+2.0}) \times 10^{-3}, \quad \text{1703.06124,}$$

$$|V_{cb}|_{\text{BGL}} = (41.9_{-1.9}^{+2.0}) \times 10^{-3}, \quad \text{1703.08170}$$

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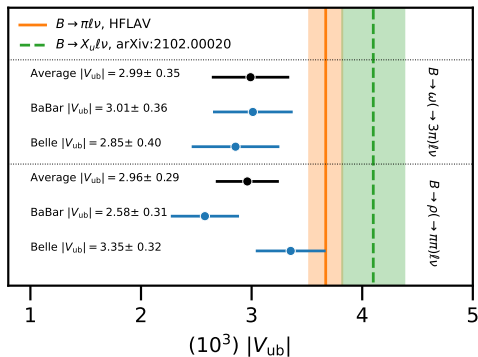
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- But: Sensitive to truncation order of the BGL expansion [BLPR \[1902.09553\]](#)

- Anticipated precision data will help resolve this (plus tools to allow different FF exp fits: [\[Hammer\]](#))
- **Debate**: How big are  $1/m_c^2$  terms in heavy quark expansion?
- Growing evidence of well controlled HQET expansion at  $1/m_c^2$  (cf.  $R(D^{(*)})$  predictions) [Bernlochner, Ligeti, DR \[1808.09464\]](#), [Bordone, Jung, van Dyk \[1908.09398\]](#), more soon!

# $|V_{ub}|$ Tensions

- There is a similar tension in  $V_{ub}$  from  $b \rightarrow ul\nu$  exclusive vs inclusive
- Eg  $B \rightarrow \rho/\omega l\nu$  or  $B \rightarrow \pi l\nu$



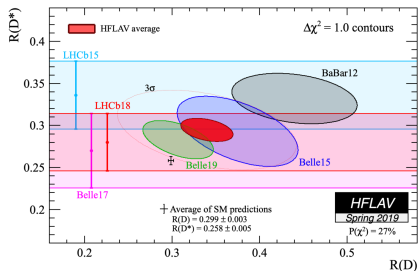
Bernlochner, Prim, DR [2104.05739]



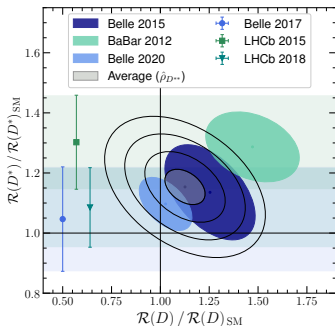
# $R(D^{(*)})$ anomaly

Persistent hints of **lepton flavor universality violation** for 8+ years  
Approx 10-20% upward deviations

HFLAV combination:  $3.1\sigma$



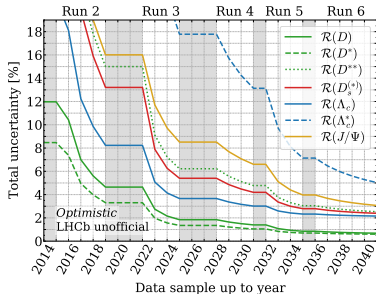
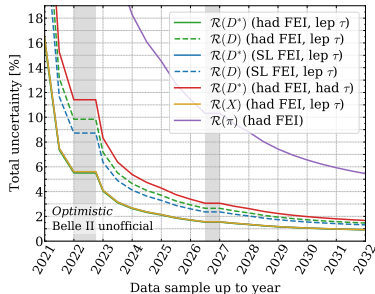
But: exp-exp correlations from  $B \rightarrow (D^{**} \rightarrow D^* \pi \dots) l \nu$  feed-down backgrounds



Combination:  $3.6\sigma$

# Forecasts

Huge amount of data from LHCb and Belle II:  $R(H_c)$  to percent level in some modes! Optimistic forecast:



$\mathcal{O}(\%)$   $R(D^{(*)})$  measurements  $\rightarrow$  excellent control of **systematics**

- Large MC datasets
- Control of  $B \rightarrow D^{**} l \nu$  excited state decays
- Consistent treatment of  $D^{**} \rightarrow D^{(*)} \pi(\pi)$  branching fractions

# Example Theory Systematic

- $R(D^{**})$  is a crucial input! [Two **broad** and two **narrow** modes:  $D_0^*$ ,  $D_1^*$ ,  $D_1'$  and  $D_2^*$ ]
  - Belle: average  $R(D^{**}) = 0.15$  [1910.05864]
  - Babar: average  $R(D^{**}) = 0.18$  [1303.0571]
  - LHCb:  $R(D^{**}) = 0.12$  [1506.08614]

- Data driven theory predictions [Bernlochner, Ligeti, DR \[1711.03110\]](#)

$$\begin{aligned} R(D_0^*) &= 0.08(3), & R(D_1') &= 0.05(2), \\ R(D_1) &= 0.10(2), & R(D_2^*) &= 0.07(1). \end{aligned}$$

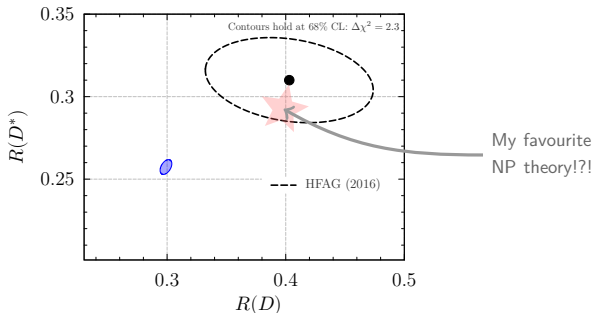
- About 50% smaller! **Would drive measured  $R(D^{(*)})$  higher by  $0.5\sigma$**  [2101.08326]

# Global NP fit strategy

General 4-Fermi basis: At dimension-6, there are 5 NP operators for left-handed  $\nu$ 's (and 5 NP operators for right-handed  $\nu$ 's)

$$\mathcal{O}_6 \sim \frac{C}{\Lambda^2} (\bar{c}\Gamma b) (\bar{\tau}\Gamma'\nu) \quad \Lambda \sim [2\sqrt{2}G_F/V_{cb}]^{-1/2} \sim 0.9 \text{ TeV}$$

- Calculate predictions for NP  $B \rightarrow D^{(*)}\tau\nu$  rates
- Fit to the measured  $R(D^{(*)})$  data (and other measurements)



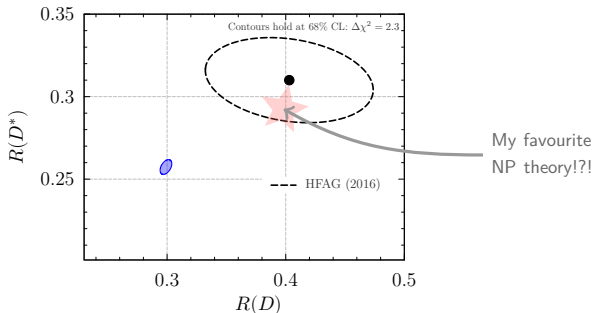
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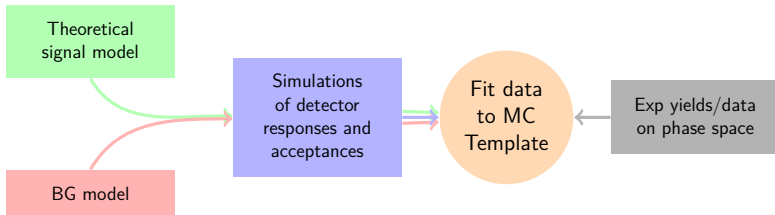
- Calculate predictions for NP  $B \rightarrow D^{(*)}\tau\nu$  rates
- Fit to the measured  $R(D^{(*)})$  data (and other measurements)

- This procedure is\* susceptible to **biases**. It is not the same as fitting NP Wilson coefficients to the experimental data!
- **Black ellipse tells us confidence to reject SM, not confidence to accept NP**

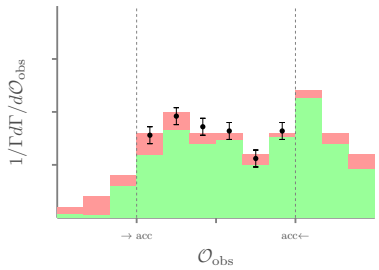


# MC Template Dependence

Have to translate **experimental yields** into **theoretically well-defined parameters**

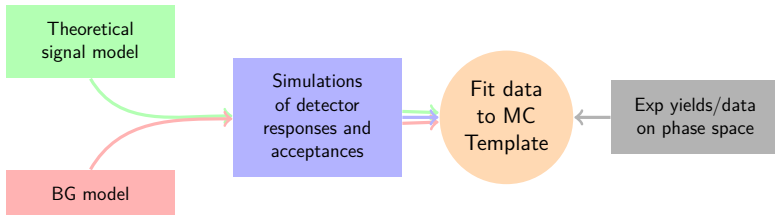


Parametrization of SM **signal** and **BG model** folded into **detector sim**  
Provides a **MC template** to be fit to data  
**Differential signal yields** → extract theory parameters

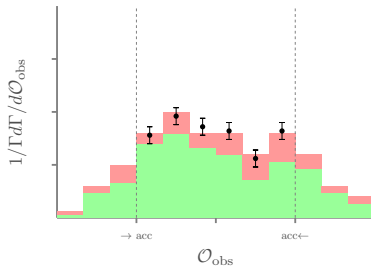


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Provides a **MC template** to be fit to data  
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NP modifies **signal** and **BG models**!

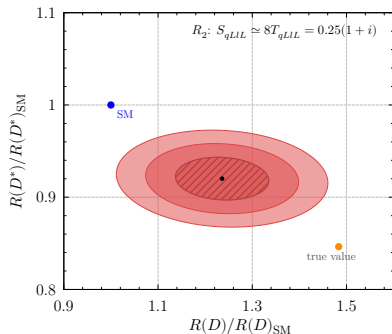
Generically alter **decay distributions** and **acceptances**

The extracted **signal yield** is different to the SM template!

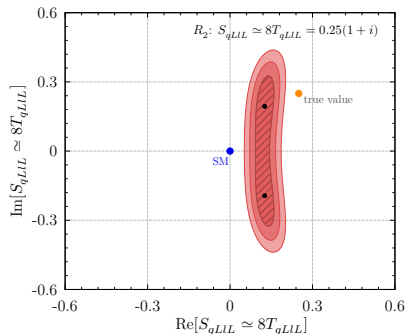
# SM Template $R(D^{(*)})$ biases

How big are these potential biases?

- Using Hammer library: [hammer.physics.lbl.gov](http://hammer.physics.lbl.gov)
- Inject truth  $R_2$  model:  $S_{qLIL} \simeq 8T_{qLIL} = 0.25(1 + i)$ . Fit **SM Template**.
- Allow  $B \rightarrow D^{(*)}l\nu$  rates to float independently in the fit



Extracted  $R(D^{(*)})$  sig.  
biased versus 'true' ratio!



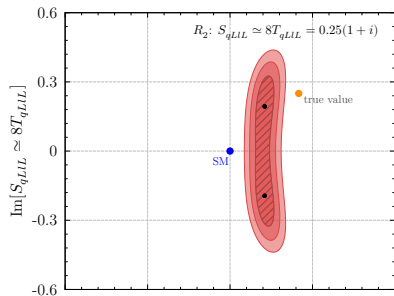
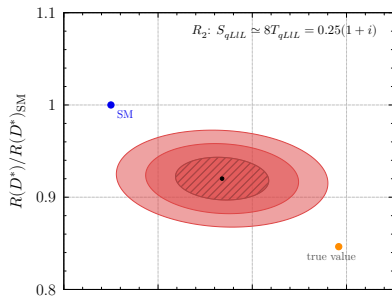
Fit of  $R_2$  WC to ex-  
tracted  $R(D^{(*)})$  sig.  
biased versus 'true' WC!



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- Allow  $B \rightarrow D^{(*)}l\nu$  rates to float independently in the fit



- Actual biases will depend on details of experimental acceptances and efficiencies
- To avoid NP-NP mismatches, LHCb and Belle II will eventually have to carry out an analysis with the full set of NP operators.
- **Caution** for interpretation of theory NP global fits of Wilson coefficients

# Summary

- Space of **smoking guns** and **precision** measurements: lots of heavy flavor mysteries to be understood (and how they could be related)!
- $R_{K^{(*)}}$  anomalies appear very clean: Are there crucial subtleties missing? **Care** is also needed with interpretation of  $B_s \rightarrow \mu\mu$  and angular  $b \rightarrow s\mu\mu$ .
- Precision tensions in  $|V_{cb}|$  will be **established** or **resolved** with more data (cf also  $|V_{ub}|$  inclusive vs exclusive)
- **Percent level measurement** of  $R(D^{(*)})$  will require precision control of various theory systematics. The anomalies suggest NP, but more careful, **self-consistent study** is needed by experiments

Thanks!